

Computer algebra independent integration tests

1-Algebraic-functions/1.1-Binomial-products/1.1.1-Linear/1.1.1.2-a+b-x-
^m-c+d-x-^n

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3.59	$\int \frac{(a+bx)^2}{x^4} dx$	726
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3.61	$\int \frac{(a+bx)^2}{x^6} dx$	732

3.62	$\int \frac{(a+bx)^2}{x^7} dx$	735
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3.85	$\int \frac{(a+bx)^5}{x^2} dx$	804
3.86	$\int \frac{(a+bx)^5}{x^3} dx$	807
3.87	$\int \frac{(a+bx)^5}{x^4} dx$	810
3.88	$\int \frac{(a+bx)^5}{x^5} dx$	813
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3.91	$\int \frac{(a+bx)^5}{x^8} dx$	822
3.92	$\int \frac{(a+bx)^5}{x^9} dx$	825
3.93	$\int \frac{(a+bx)^5}{x^{10}} dx$	828

3.94	$\int \frac{(a+bx)^5}{x^{11}} dx$	831
3.95	$\int \frac{(a+bx)^5}{x^{12}} dx$	834
3.96	$\int \frac{(a+bx)^5}{x^{13}} dx$	837
3.97	$\int \frac{(a+bx)^5}{x^{14}} dx$	840
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3.99	$\int x^7(a+bx)^7 dx$	846
3.100	$\int x^6(a+bx)^7 dx$	849
3.101	$\int x^5(a+bx)^7 dx$	852
3.102	$\int x^4(a+bx)^7 dx$	855
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3.122	$\int \frac{(a+bx)^7}{x^{16}} dx$	916
3.123	$\int x^{11}(a+bx)^{10} dx$	919
3.124	$\int x^{10}(a+bx)^{10} dx$	922
3.125	$\int x^9(a+bx)^{10} dx$	925

3.126	$\int x^8(a + bx)^{10} dx$	928
3.127	$\int x^7(a + bx)^{10} dx$	931
3.128	$\int x^6(a + bx)^{10} dx$	934
3.129	$\int x^5(a + bx)^{10} dx$	937
3.130	$\int x^4(a + bx)^{10} dx$	940
3.131	$\int x^3(a + bx)^{10} dx$	943
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3.133	$\int x(a + bx)^{10} dx$	949
3.134	$\int (a + bx)^{10} dx$	952
3.135	$\int \frac{(a+bx)^{10}}{x} dx$	955
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3.137	$\int \frac{(a+bx)^{10}}{x^3} dx$	961
3.138	$\int \frac{(a+bx)^{10}}{x^4} dx$	964
3.139	$\int \frac{(a+bx)^{10}}{x^5} dx$	967
3.140	$\int \frac{(a+bx)^{10}}{x^6} dx$	970
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3.142	$\int \frac{(a+bx)^{10}}{x^8} dx$	976
3.143	$\int \frac{(a+bx)^{10}}{x^9} dx$	979
3.144	$\int \frac{(a+bx)^{10}}{x^{10}} dx$	982
3.145	$\int \frac{(a+bx)^{10}}{x^{11}} dx$	985
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3.147	$\int \frac{(a+bx)^{10}}{x^{13}} dx$	991
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3.149	$\int \frac{(a+bx)^{10}}{x^{15}} dx$	998
3.150	$\int \frac{(a+bx)^{10}}{x^{16}} dx$	1002
3.151	$\int \frac{(a+bx)^{10}}{x^{17}} dx$	1006
3.152	$\int \frac{(a+bx)^{10}}{x^{18}} dx$	1010
3.153	$\int \frac{(a+bx)^{10}}{x^{19}} dx$	1014
3.154	$\int \frac{(a+bx)^{10}}{x^{20}} dx$	1017
3.155	$\int c(a + bx) dx$	1020
3.156	$\int \frac{(c+d)(a+bx)}{e} dx$	1023

3.157	$\int \frac{x^5}{a+bx} dx$.1026
3.158	$\int \frac{x^4}{a+bx} dx$.1029
3.159	$\int \frac{x^3}{a+bx} dx$.1032
3.160	$\int \frac{x^2}{a+bx} dx$.1035
3.161	$\int \frac{x}{a+bx} dx$.1038
3.162	$\int \frac{1}{a+bx} dx$.1041
3.163	$\int \frac{1}{x(a+bx)} dx$.1044
3.164	$\int \frac{1}{x^2(a+bx)} dx$.1047
3.165	$\int \frac{1}{x^3(a+bx)} dx$.1050
3.166	$\int \frac{1}{x^4(a+bx)} dx$.1053
3.167	$\int \frac{1}{x^5(a+bx)} dx$.1056
3.168	$\int \frac{x^6}{(a+bx)^2} dx$.1059
3.169	$\int \frac{x^5}{(a+bx)^2} dx$.1062
3.170	$\int \frac{x^4}{(a+bx)^2} dx$.1065
3.171	$\int \frac{x^3}{(a+bx)^2} dx$.1068
3.172	$\int \frac{x^2}{(a+bx)^2} dx$.1071
3.173	$\int \frac{x}{(a+bx)^2} dx$.1074
3.174	$\int \frac{1}{(a+bx)^2} dx$.1077
3.175	$\int \frac{1}{x(a+bx)^2} dx$.1080
3.176	$\int \frac{1}{x^2(a+bx)^2} dx$.1083
3.177	$\int \frac{1}{x^3(a+bx)^2} dx$.1086
3.178	$\int \frac{1}{x^4(a+bx)^2} dx$.1089
3.179	$\int \frac{1}{x^5(a+bx)^2} dx$.1092
3.180	$\int \frac{x^7}{(a+bx)^3} dx$.1095
3.181	$\int \frac{x^6}{(a+bx)^3} dx$.1098
3.182	$\int \frac{x^5}{(a+bx)^3} dx$.1101
3.183	$\int \frac{x^4}{(a+bx)^3} dx$.1104
3.184	$\int \frac{x^3}{(a+bx)^3} dx$.1107

3.185	$\int \frac{x^2}{(a+bx)^3} dx$.1110
3.186	$\int \frac{x}{(a+bx)^3} dx$.1113
3.187	$\int \frac{1}{(a+bx)^3} dx$.1116
3.188	$\int \frac{1}{x(a+bx)^3} dx$.1119
3.189	$\int \frac{1}{x^2(a+bx)^3} dx$.1122
3.190	$\int \frac{1}{x^3(a+bx)^3} dx$.1125
3.191	$\int \frac{1}{x^4(a+bx)^3} dx$.1128
3.192	$\int \frac{1}{x^5(a+bx)^3} dx$.1131
3.193	$\int \frac{x^8}{(a+bx)^4} dx$.1134
3.194	$\int \frac{x^7}{(a+bx)^4} dx$.1137
3.195	$\int \frac{x^6}{(a+bx)^4} dx$.1140
3.196	$\int \frac{x^5}{(a+bx)^4} dx$.1143
3.197	$\int \frac{x^4}{(a+bx)^4} dx$.1146
3.198	$\int \frac{x^3}{(a+bx)^4} dx$.1149
3.199	$\int \frac{x^2}{(a+bx)^4} dx$.1152
3.200	$\int \frac{x}{(a+bx)^4} dx$.1155
3.201	$\int \frac{1}{(a+bx)^4} dx$.1158
3.202	$\int \frac{1}{x(a+bx)^4} dx$.1161
3.203	$\int \frac{1}{x^2(a+bx)^4} dx$.1164
3.204	$\int \frac{1}{x^3(a+bx)^4} dx$.1167
3.205	$\int \frac{1}{x^4(a+bx)^4} dx$.1170
3.206	$\int \frac{1}{x^5(a+bx)^4} dx$.1173
3.207	$\int \frac{x^{10}}{(a+bx)^7} dx$.1176
3.208	$\int \frac{x^9}{(a+bx)^7} dx$.1180
3.209	$\int \frac{x^8}{(a+bx)^7} dx$.1183
3.210	$\int \frac{x^7}{(a+bx)^7} dx$.1186
3.211	$\int \frac{x^6}{(a+bx)^7} dx$.1189
3.212	$\int \frac{x^5}{(a+bx)^7} dx$.1192

3.213	$\int \frac{x^4}{(a+bx)^7} dx$.1195
3.214	$\int \frac{x^3}{(a+bx)^7} dx$.1198
3.215	$\int \frac{x^2}{(a+bx)^7} dx$.1201
3.216	$\int \frac{x}{(a+bx)^7} dx$.1204
3.217	$\int \frac{1}{(a+bx)^7} dx$.1207
3.218	$\int \frac{1}{x(a+bx)^7} dx$.1210
3.219	$\int \frac{1}{x^2(a+bx)^7} dx$.1213
3.220	$\int \frac{1}{x^3(a+bx)^7} dx$.1216
3.221	$\int \frac{1}{x^4(a+bx)^7} dx$.1220
3.222	$\int \frac{x^{12}}{(a+bx)^{10}} dx$.1224
3.223	$\int \frac{x^{11}}{(a+bx)^{10}} dx$.1228
3.224	$\int \frac{x^{10}}{(a+bx)^{10}} dx$.1232
3.225	$\int \frac{x^9}{(a+bx)^{10}} dx$.1236
3.226	$\int \frac{x^8}{(a+bx)^{10}} dx$.1240
3.227	$\int \frac{x^7}{(a+bx)^{10}} dx$.1243
3.228	$\int \frac{x^6}{(a+bx)^{10}} dx$.1247
3.229	$\int \frac{x^5}{(a+bx)^{10}} dx$.1251
3.230	$\int \frac{x^4}{(a+bx)^{10}} dx$.1255
3.231	$\int \frac{x^3}{(a+bx)^{10}} dx$.1258
3.232	$\int \frac{x^2}{(a+bx)^{10}} dx$.1261
3.233	$\int \frac{x}{(a+bx)^{10}} dx$.1264
3.234	$\int \frac{1}{(a+bx)^{10}} dx$.1267
3.235	$\int \frac{1}{x(a+bx)^{10}} dx$.1270
3.236	$\int \frac{1}{x^2(a+bx)^{10}} dx$.1274
3.237	$\int \frac{1}{x^3(a+bx)^{10}} dx$.1278
3.238	$\int \frac{1}{x^4(a+bx)^{10}} dx$.1282
3.239	$\int \frac{(a+bx)^{12}}{x^{10}} dx$.1286
3.240	$\int \frac{(a+bx)^{11}}{x^{10}} dx$.1289

3.241	$\int \frac{(a+bx)^{10}}{x^{10}} dx$1292
3.242	$\int \frac{(a+bx)^9}{x^{10}} dx$1295
3.243	$\int \frac{(a+bx)^8}{x^{10}} dx$1298
3.244	$\int \frac{(a+bx)^7}{x^{10}} dx$1301
3.245	$\int \frac{(a+bx)^6}{x^{10}} dx$1304
3.246	$\int \frac{(a+bx)^5}{x^{10}} dx$1307
3.247	$\int \frac{(a+bx)^4}{x^{10}} dx$1310
3.248	$\int \frac{(a+bx)^3}{x^{10}} dx$1313
3.249	$\int \frac{(a+bx)^2}{x^{10}} dx$1316
3.250	$\int \frac{a+bx}{x^{10}} dx$1319
3.251	$\int \frac{1}{x^{10}} dx$1322
3.252	$\int \frac{1}{x^{10}(a+bx)} dx$1325
3.253	$\int \frac{1}{x^{10}(a+bx)^2} dx$1328
3.254	$\int \frac{1}{x^{10}(a+bx)^3} dx$1332
3.255	$\int \frac{1}{x(2+3x)} dx$1336
3.256	$\int \frac{1}{x(4+6x)} dx$1339
3.257	$\int \frac{1}{x^2(4+6x)} dx$1342
3.258	$\int \frac{1}{x^3(4+6x)} dx$1345
3.259	$\int \frac{1}{x^4(4+6x)} dx$1348
3.260	$\int \frac{1}{x^5(4+6x)} dx$1351
3.261	$\int \frac{1}{x(4+6x)^2} dx$1354
3.262	$\int \frac{1}{x^2(4+6x)^2} dx$1357
3.263	$\int \frac{1}{x^3(4+6x)^2} dx$1360
3.264	$\int \frac{1}{x^4(4+6x)^2} dx$1363
3.265	$\int \frac{1}{x^5(4+6x)^2} dx$1366
3.266	$\int \frac{1}{x(4+6x)^3} dx$1369
3.267	$\int \frac{1}{x^2(4+6x)^3} dx$1372
3.268	$\int \frac{1}{x^3(4+6x)^3} dx$1375
3.269	$\int \frac{1}{x^4(4+6x)^3} dx$1378

3.270	$\int \frac{1}{x^5(4+6x)^3} dx$.1381
3.271	$\int \frac{1}{2+2x} dx$.1384
3.272	$\int \frac{1}{4-6x} dx$.1387
3.273	$\int \frac{1}{a+\sqrt{a}x} dx$.1390
3.274	$\int \frac{1}{a+\sqrt{-a}x} dx$.1393
3.275	$\int \frac{1}{a^2+\sqrt{-a}x} dx$.1396
3.276	$\int \frac{1}{a^3+\sqrt{-a}x} dx$.1399
3.277	$\int \frac{1}{\frac{1}{a}+\sqrt{-a}x} dx$.1402
3.278	$\int \frac{1}{\frac{1}{a^2}+\sqrt{-a}x} dx$.1405
3.279	$\int \frac{1}{x(1+bx)} dx$.1408
3.280	$\int \frac{1}{x(-1+bx)} dx$.1411
3.281	$\int \frac{1}{x^2(1+bx)} dx$.1414
3.282	$\int \frac{1}{x^2(-1+bx)} dx$.1417
3.283	$\int \left(\frac{b}{x} + \frac{1}{x^2(1+bx)} \right) dx$.1420
3.284	$\int x^3 \sqrt{a+bx} dx$.1423
3.285	$\int x^2 \sqrt{a+bx} dx$.1427
3.286	$\int x \sqrt{a+bx} dx$.1430
3.287	$\int \sqrt{a+bx} dx$.1433
3.288	$\int \frac{\sqrt{a+bx}}{x} dx$.1436
3.289	$\int \frac{\sqrt{a+bx}}{x^2} dx$.1439
3.290	$\int \frac{\sqrt{a+bx}}{x^3} dx$.1443
3.291	$\int \frac{\sqrt{a+bx}}{x^4} dx$.1447
3.292	$\int x^3(a+bx)^{3/2} dx$.1451
3.293	$\int x^2(a+bx)^{3/2} dx$.1455
3.294	$\int x(a+bx)^{3/2} dx$.1458
3.295	$\int (a+bx)^{3/2} dx$.1461
3.296	$\int \frac{(a+bx)^{3/2}}{x} dx$.1464
3.297	$\int \frac{(a+bx)^{3/2}}{x^2} dx$.1468
3.298	$\int \frac{(a+bx)^{3/2}}{x^3} dx$.1472
3.299	$\int \frac{(a+bx)^{3/2}}{x^4} dx$.1476

3.300	$\int x^3(a + bx)^{5/2} dx$.1480
3.301	$\int x^2(a + bx)^{5/2} dx$.1483
3.302	$\int x(a + bx)^{5/2} dx$.1486
3.303	$\int (a + bx)^{5/2} dx$.1489
3.304	$\int \frac{(a+bx)^{5/2}}{x} dx$.1492
3.305	$\int \frac{(a+bx)^{5/2}}{x^2} dx$.1496
3.306	$\int \frac{(a+bx)^{5/2}}{x^3} dx$.1500
3.307	$\int \frac{(a+bx)^{5/2}}{x^4} dx$.1504
3.308	$\int \frac{(a+bx)^{5/2}}{x^5} dx$.1508
3.309	$\int x^7(a + bx)^{9/2} dx$.1512
3.310	$\int x^6(a + bx)^{9/2} dx$.1516
3.311	$\int x^5(a + bx)^{9/2} dx$.1520
3.312	$\int x^4(a + bx)^{9/2} dx$.1524
3.313	$\int x^3(a + bx)^{9/2} dx$.1528
3.314	$\int x^2(a + bx)^{9/2} dx$.1532
3.315	$\int x(a + bx)^{9/2} dx$.1535
3.316	$\int (a + bx)^{9/2} dx$.1538
3.317	$\int \frac{(a+bx)^{9/2}}{x} dx$.1541
3.318	$\int \frac{(a+bx)^{9/2}}{x^2} dx$.1545
3.319	$\int \frac{(a+bx)^{9/2}}{x^3} dx$.1549
3.320	$\int \frac{(a+bx)^{9/2}}{x^4} dx$.1553
3.321	$\int \frac{(a+bx)^{9/2}}{x^5} dx$.1557
3.322	$\int \frac{(a+bx)^{9/2}}{x^6} dx$.1561
3.323	$\int \frac{(a+bx)^{9/2}}{x^7} dx$.1565
3.324	$\int \frac{(a+bx)^{9/2}}{x^8} dx$.1570
3.325	$\int \frac{\sqrt{-a+bx}}{x} dx$.1575
3.326	$\int \frac{\sqrt{-a+bx}}{x^2} dx$.1579
3.327	$\int \frac{\sqrt{-a+bx}}{x^3} dx$.1583
3.328	$\int \frac{(-a+bx)^{3/2}}{x} dx$.1587
3.329	$\int \frac{(-a+bx)^{3/2}}{x^2} dx$.1591
3.330	$\int \frac{(-a+bx)^{3/2}}{x^3} dx$.1595

3.331	$\int \frac{(-a+bx)^{5/2}}{x} dx$.1599
3.332	$\int \frac{(-a+bx)^{5/2}}{x^2} dx$.1603
3.333	$\int \frac{(-a+bx)^{5/2}}{x^3} dx$.1607
3.334	$\int \frac{x^4}{\sqrt{a+bx}} dx$.1611
3.335	$\int \frac{x^3}{\sqrt{a+bx}} dx$.1616
3.336	$\int \frac{x^2}{\sqrt{a+bx}} dx$.1620
3.337	$\int \frac{x}{\sqrt{a+bx}} dx$.1623
3.338	$\int \frac{1}{\sqrt{a+bx}} dx$.1626
3.339	$\int \frac{1}{x\sqrt{a+bx}} dx$.1629
3.340	$\int \frac{1}{x^2\sqrt{a+bx}} dx$.1632
3.341	$\int \frac{1}{x^3\sqrt{a+bx}} dx$.1636
3.342	$\int \frac{1}{x^4\sqrt{a+bx}} dx$.1640
3.343	$\int \frac{x^4}{(a+bx)^{3/2}} dx$.1644
3.344	$\int \frac{x^3}{(a+bx)^{3/2}} dx$.1649
3.345	$\int \frac{x^2}{(a+bx)^{3/2}} dx$.1653
3.346	$\int \frac{x}{(a+bx)^{3/2}} dx$.1656
3.347	$\int \frac{1}{(a+bx)^{3/2}} dx$.1659
3.348	$\int \frac{1}{x(a+bx)^{3/2}} dx$.1662
3.349	$\int \frac{1}{x^2(a+bx)^{3/2}} dx$.1666
3.350	$\int \frac{1}{x^3(a+bx)^{3/2}} dx$.1670
3.351	$\int \frac{x^4}{(a+bx)^{5/2}} dx$.1674
3.352	$\int \frac{x^3}{(a+bx)^{5/2}} dx$.1679
3.353	$\int \frac{x^2}{(a+bx)^{5/2}} dx$.1682
3.354	$\int \frac{x}{(a+bx)^{5/2}} dx$.1685
3.355	$\int \frac{1}{(a+bx)^{5/2}} dx$.1688
3.356	$\int \frac{1}{x(a+bx)^{5/2}} dx$.1691
3.357	$\int \frac{1}{x^2(a+bx)^{5/2}} dx$.1695
3.358	$\int \frac{1}{x^3(a+bx)^{5/2}} dx$.1699

3.359	$\int \frac{1}{x\sqrt{-a+bx}} dx$.1703
3.360	$\int \frac{1}{x^2\sqrt{-a+bx}} dx$.1707
3.361	$\int \frac{1}{x^3\sqrt{-a+bx}} dx$.1711
3.362	$\int \frac{1}{x(-a+bx)^{3/2}} dx$.1715
3.363	$\int \frac{1}{x^2(-a+bx)^{3/2}} dx$.1719
3.364	$\int \frac{1}{x^3(-a+bx)^{3/2}} dx$.1723
3.365	$\int \frac{1}{x(-a+bx)^{5/2}} dx$.1727
3.366	$\int \frac{1}{x^2(-a+bx)^{5/2}} dx$.1731
3.367	$\int \frac{1}{x^3(-a+bx)^{5/2}} dx$.1735
3.368	$\int \frac{x^{-1+m}(2am+b(-1+2m)x)}{2(a+bx)^{3/2}} dx$.1740
3.369	$\int \left(-\frac{bx^m}{2(a+bx)^{3/2}} + \frac{mx^{-1+m}}{\sqrt{a+bx}} \right) dx$.1743
3.370	$\int x^{\frac{1-n}{2} + \frac{1}{2}(-3+n)} \frac{1}{\sqrt{a+bx}} dx$.1747
3.371	$\int x^3 \sqrt[3]{a+bx} dx$.1750
3.372	$\int x^2 \sqrt[3]{a+bx} dx$.1754
3.373	$\int x \sqrt[3]{a+bx} dx$.1757
3.374	$\int \sqrt[3]{a+bx} dx$.1760
3.375	$\int \frac{\sqrt[3]{a+bx}}{x} dx$.1763
3.376	$\int \frac{\sqrt[3]{a+bx}}{x^2} dx$.1767
3.377	$\int \frac{\sqrt[3]{a+bx}}{x^3} dx$.1772
3.378	$\int x^3(a+bx)^{2/3} dx$.1779
3.379	$\int x^2(a+bx)^{2/3} dx$.1783
3.380	$\int x(a+bx)^{2/3} dx$.1786
3.381	$\int (a+bx)^{2/3} dx$.1789
3.382	$\int \frac{(a+bx)^{2/3}}{x} dx$.1792
3.383	$\int \frac{(a+bx)^{2/3}}{x^2} dx$.1797
3.384	$\int \frac{(a+bx)^{2/3}}{x^3} dx$.1802
3.385	$\int x^3(a+bx)^{4/3} dx$.1809
3.386	$\int x^2(a+bx)^{4/3} dx$.1813
3.387	$\int x(a+bx)^{4/3} dx$.1816
3.388	$\int (a+bx)^{4/3} dx$.1819

3.389	$\int \frac{(a+bx)^{4/3}}{x} dx$.1822
3.390	$\int \frac{(a+bx)^{4/3}}{x^2} dx$.1827
3.391	$\int \frac{(a+bx)^{4/3}}{x^3} dx$.1833
3.392	$\int \frac{x^3}{\sqrt[3]{a+bx}} dx$.1839
3.393	$\int \frac{x^2}{\sqrt[3]{a+bx}} dx$.1843
3.394	$\int \frac{x}{\sqrt[3]{a+bx}} dx$.1846
3.395	$\int \frac{1}{\sqrt[3]{a+bx}} dx$.1849
3.396	$\int \frac{1}{x \sqrt[3]{a+bx}} dx$.1852
3.397	$\int \frac{1}{x^2 \sqrt[3]{a+bx}} dx$.1857
3.398	$\int \frac{1}{x^3 \sqrt[3]{a+bx}} dx$.1862
3.399	$\int \frac{x^3}{\sqrt[3]{-a+bx}} dx$.1869
3.400	$\int \frac{x^2}{\sqrt[3]{-a+bx}} dx$.1875
3.401	$\int \frac{x}{\sqrt[3]{-a+bx}} dx$.1879
3.402	$\int \frac{1}{\sqrt[3]{-a+bx}} dx$.1882
3.403	$\int \frac{1}{x \sqrt[3]{-a+bx}} dx$.1885
3.404	$\int \frac{1}{x^2 \sqrt[3]{-a+bx}} dx$.1889
3.405	$\int \frac{1}{x^3 \sqrt[3]{-a+bx}} dx$.1894
3.406	$\int \frac{x^3}{(a+bx)^{2/3}} dx$.1901
3.407	$\int \frac{x^2}{(a+bx)^{2/3}} dx$.1905
3.408	$\int \frac{x}{(a+bx)^{2/3}} dx$.1908
3.409	$\int \frac{1}{(a+bx)^{2/3}} dx$.1911
3.410	$\int \frac{1}{x(a+bx)^{2/3}} dx$.1914
3.411	$\int \frac{1}{x^2(a+bx)^{2/3}} dx$.1918
3.412	$\int \frac{1}{x^3(a+bx)^{2/3}} dx$.1923
3.413	$\int \frac{x^3}{(a+bx)^{4/3}} dx$.1929
3.414	$\int \frac{x^2}{(a+bx)^{4/3}} dx$.1933
3.415	$\int \frac{x}{(a+bx)^{4/3}} dx$.1936

3.416	$\int \frac{1}{(a+bx)^{4/3}} dx$1939
3.417	$\int \frac{1}{x(a+bx)^{4/3}} dx$1942
3.418	$\int \frac{1}{x^2(a+bx)^{4/3}} dx$1947
3.419	$\int \frac{1}{x^3(a+bx)^{4/3}} dx$1952
3.420	$\int \frac{1}{x\sqrt[3]{a^3+b^3x}} dx$1959
3.421	$\int \frac{1}{x\sqrt[3]{a^3-b^3x}} dx$1963
3.422	$\int \frac{1}{x\sqrt[3]{-a^3+b^3x}} dx$1967
3.423	$\int \frac{1}{x\sqrt[3]{-a^3-b^3x}} dx$1971
3.424	$\int \frac{1}{x(a^3+b^3x)^{2/3}} dx$1975
3.425	$\int \frac{1}{x(a^3-b^3x)^{2/3}} dx$1979
3.426	$\int \frac{1}{x(-a^3+b^3x)^{2/3}} dx$1983
3.427	$\int \frac{1}{x(-a^3-b^3x)^{2/3}} dx$1987
3.428	$\int x^m(a+bx) dx$1991
3.429	$\int x^{5/2}(a+bx) dx$1994
3.430	$\int x^{3/2}(a+bx) dx$1997
3.431	$\int \sqrt{x}(a+bx) dx$2000
3.432	$\int \frac{a+bx}{\sqrt{x}} dx$2003
3.433	$\int \frac{a+bx}{x^{3/2}} dx$2006
3.434	$\int \frac{a+bx}{x^{5/2}} dx$2009
3.435	$\int x^m(a+bx)^2 dx$2012
3.436	$\int x^{5/2}(a+bx)^2 dx$2015
3.437	$\int x^{3/2}(a+bx)^2 dx$2018
3.438	$\int \sqrt{x}(a+bx)^2 dx$2021
3.439	$\int \frac{(a+bx)^2}{\sqrt{x}} dx$2024
3.440	$\int \frac{(a+bx)^2}{x^{3/2}} dx$2027
3.441	$\int \frac{(a+bx)^2}{x^{5/2}} dx$2030
3.442	$\int x^m(a+bx)^3 dx$2033
3.443	$\int x^{5/2}(a+bx)^3 dx$2037
3.444	$\int x^{3/2}(a+bx)^3 dx$2040
3.445	$\int \sqrt{x}(a+bx)^3 dx$2043

3.446	$\int \frac{(a+bx)^3}{\sqrt{x}} dx$.2046
3.447	$\int \frac{(a+bx)^3}{x^{3/2}} dx$.2049
3.448	$\int \frac{(a+bx)^3}{x^{5/2}} dx$.2052
3.449	$\int \frac{x^{5/2}}{a+bx} dx$.2055
3.450	$\int \frac{x^{3/2}}{a+bx} dx$.2059
3.451	$\int \frac{\sqrt{x}}{a+bx} dx$.2063
3.452	$\int \frac{1}{\sqrt{x}(a+bx)} dx$.2067
3.453	$\int \frac{1}{x^{3/2}(a+bx)} dx$.2070
3.454	$\int \frac{1}{x^{5/2}(a+bx)} dx$.2074
3.455	$\int \frac{1}{x^{7/2}(a+bx)} dx$.2078
3.456	$\int \frac{x^{5/2}}{(a+bx)^2} dx$.2082
3.457	$\int \frac{x^{3/2}}{(a+bx)^2} dx$.2087
3.458	$\int \frac{\sqrt{x}}{(a+bx)^2} dx$.2091
3.459	$\int \frac{1}{\sqrt{x}(a+bx)^2} dx$.2095
3.460	$\int \frac{1}{x^{3/2}(a+bx)^2} dx$.2099
3.461	$\int \frac{1}{x^{5/2}(a+bx)^2} dx$.2103
3.462	$\int \frac{x^{7/2}}{(a+bx)^3} dx$.2107
3.463	$\int \frac{x^{5/2}}{(a+bx)^3} dx$.2112
3.464	$\int \frac{x^{3/2}}{(a+bx)^3} dx$.2117
3.465	$\int \frac{\sqrt{x}}{(a+bx)^3} dx$.2121
3.466	$\int \frac{1}{\sqrt{x}(a+bx)^3} dx$.2126
3.467	$\int \frac{1}{x^{3/2}(a+bx)^3} dx$.2130
3.468	$\int \frac{1}{x^{5/2}(a+bx)^3} dx$.2135
3.469	$\int \frac{x^{5/2}}{-a+bx} dx$.2140
3.470	$\int \frac{x^{3/2}}{-a+bx} dx$.2144
3.471	$\int \frac{\sqrt{x}}{-a+bx} dx$.2148
3.472	$\int \frac{1}{\sqrt{x}(-a+bx)} dx$.2152
3.473	$\int \frac{1}{x^{3/2}(-a+bx)} dx$.2155

3.474	$\int \frac{1}{x^{5/2}(-a+bx)} dx$.2159
3.475	$\int \frac{1}{x^{7/2}(-a+bx)} dx$.2163
3.476	$\int \frac{x^{5/2}}{(-a+bx)^2} dx$.2167
3.477	$\int \frac{x^{3/2}}{(-a+bx)^2} dx$.2171
3.478	$\int \frac{\sqrt{x}}{(-a+bx)^2} dx$.2175
3.479	$\int \frac{1}{\sqrt{x}(-a+bx)^2} dx$.2179
3.480	$\int \frac{1}{x^{3/2}(-a+bx)^2} dx$.2183
3.481	$\int \frac{1}{x^{5/2}(-a+bx)^2} dx$.2187
3.482	$\int \frac{x^{7/2}}{(-a+bx)^3} dx$.2191
3.483	$\int \frac{x^{5/2}}{(-a+bx)^3} dx$.2196
3.484	$\int \frac{x^{3/2}}{(-a+bx)^3} dx$.2201
3.485	$\int \frac{\sqrt{x}}{(-a+bx)^3} dx$.2205
3.486	$\int \frac{1}{\sqrt{x}(-a+bx)^3} dx$.2209
3.487	$\int \frac{1}{x^{3/2}(-a+bx)^3} dx$.2213
3.488	$\int \frac{1}{x^{5/2}(-a+bx)^3} dx$.2218
3.489	$\int x^{5/2}\sqrt{a+bx} dx$.2223
3.490	$\int x^{3/2}\sqrt{a+bx} dx$.2227
3.491	$\int \sqrt{x}\sqrt{a+bx} dx$.2231
3.492	$\int \frac{\sqrt{a+bx}}{\sqrt{x}} dx$.2235
3.493	$\int \frac{\sqrt{a+bx}}{x^{3/2}} dx$.2239
3.494	$\int \frac{\sqrt{a+bx}}{x^{5/2}} dx$.2243
3.495	$\int \frac{\sqrt{a+bx}}{x^{7/2}} dx$.2246
3.496	$\int \frac{\sqrt{a+bx}}{x^{9/2}} dx$.2249
3.497	$\int x^{5/2}\sqrt{a-bx} dx$.2253
3.498	$\int x^{3/2}\sqrt{a-bx} dx$.2258
3.499	$\int \sqrt{x}\sqrt{a-bx} dx$.2262
3.500	$\int \frac{\sqrt{a-bx}}{\sqrt{x}} dx$.2266
3.501	$\int \frac{\sqrt{a-bx}}{x^{3/2}} dx$.2270

3.502	$\int \frac{\sqrt{a-bx}}{x^{5/2}} dx$2274
3.503	$\int \frac{\sqrt{a-bx}}{x^{7/2}} dx$2277
3.504	$\int \frac{\sqrt{a-bx}}{x^{9/2}} dx$2280
3.505	$\int x^{5/2} \sqrt{2+bx} dx$2284
3.506	$\int x^{3/2} \sqrt{2+bx} dx$2289
3.507	$\int \sqrt{x} \sqrt{2+bx} dx$2294
3.508	$\int \frac{\sqrt{2+bx}}{\sqrt{x}} dx$2299
3.509	$\int \frac{\sqrt{2+bx}}{x^{3/2}} dx$2303
3.510	$\int \frac{\sqrt{2+bx}}{x^{5/2}} dx$2307
3.511	$\int \frac{\sqrt{2+bx}}{x^{7/2}} dx$2310
3.512	$\int \frac{\sqrt{2+bx}}{x^{9/2}} dx$2313
3.513	$\int x^{5/2} \sqrt{2-bx} dx$2317
3.514	$\int x^{3/2} \sqrt{2-bx} dx$2322
3.515	$\int \sqrt{x} \sqrt{2-bx} dx$2327
3.516	$\int \frac{\sqrt{2-bx}}{\sqrt{x}} dx$2332
3.517	$\int \frac{\sqrt{2-bx}}{x^{3/2}} dx$2336
3.518	$\int \frac{\sqrt{2-bx}}{x^{5/2}} dx$2340
3.519	$\int \frac{\sqrt{2-bx}}{x^{7/2}} dx$2343
3.520	$\int \frac{\sqrt{2-bx}}{x^{9/2}} dx$2346
3.521	$\int x^{5/2} (a+bx)^{3/2} dx$2350
3.522	$\int x^{3/2} (a+bx)^{3/2} dx$2354
3.523	$\int \sqrt{x} (a+bx)^{3/2} dx$2358
3.524	$\int \frac{(a+bx)^{3/2}}{\sqrt{x}} dx$2362
3.525	$\int \frac{(a+bx)^{3/2}}{x^{3/2}} dx$2366
3.526	$\int \frac{(a+bx)^{3/2}}{x^{5/2}} dx$2370
3.527	$\int x^{5/2} (a-bx)^{3/2} dx$2374
3.528	$\int x^{3/2} (a-bx)^{3/2} dx$2379
3.529	$\int \sqrt{x} (a-bx)^{3/2} dx$2384
3.530	$\int \frac{(a-bx)^{3/2}}{\sqrt{x}} dx$2388
3.531	$\int \frac{(a-bx)^{3/2}}{x^{3/2}} dx$2392

3.532	$\int \frac{(a-bx)^{3/2}}{x^{5/2}} dx$.2396
3.533	$\int x^{5/2}(2+bx)^{3/2} dx$.2400
3.534	$\int x^{3/2}(2+bx)^{3/2} dx$.2406
3.535	$\int \sqrt{x}(2+bx)^{3/2} dx$.2412
3.536	$\int \frac{(2+bx)^{3/2}}{\sqrt{x}} dx$.2418
3.537	$\int \frac{(2+bx)^{3/2}}{x^{3/2}} dx$.2422
3.538	$\int \frac{(2+bx)^{3/2}}{x^{5/2}} dx$.2426
3.539	$\int x^{5/2}(2-bx)^{3/2} dx$.2430
3.540	$\int x^{3/2}(2-bx)^{3/2} dx$.2436
3.541	$\int \sqrt{x}(2-bx)^{3/2} dx$.2442
3.542	$\int \frac{(2-bx)^{3/2}}{\sqrt{x}} dx$.2448
3.543	$\int \frac{(2-bx)^{3/2}}{x^{3/2}} dx$.2452
3.544	$\int \frac{(2-bx)^{3/2}}{x^{5/2}} dx$.2457
3.545	$\int x^{5/2}(a+bx)^{5/2} dx$.2461
3.546	$\int x^{3/2}(a+bx)^{5/2} dx$.2466
3.547	$\int \sqrt{x}(a+bx)^{5/2} dx$.2470
3.548	$\int \frac{(a+bx)^{5/2}}{\sqrt{x}} dx$.2474
3.549	$\int \frac{(a+bx)^{5/2}}{x^{3/2}} dx$.2478
3.550	$\int \frac{(a+bx)^{5/2}}{x^{5/2}} dx$.2482
3.551	$\int x^{5/2}(a-bx)^{5/2} dx$.2486
3.552	$\int x^{3/2}(a-bx)^{5/2} dx$.2491
3.553	$\int \sqrt{x}(a-bx)^{5/2} dx$.2496
3.554	$\int \frac{(a-bx)^{5/2}}{\sqrt{x}} dx$.2501
3.555	$\int \frac{(a-bx)^{5/2}}{x^{3/2}} dx$.2505
3.556	$\int \frac{(a-bx)^{5/2}}{x^{5/2}} dx$.2509
3.557	$\int x^{5/2}(2+bx)^{5/2} dx$.2513
3.558	$\int x^{3/2}(2+bx)^{5/2} dx$.2520
3.559	$\int \sqrt{x}(2+bx)^{5/2} dx$.2527
3.560	$\int \frac{(2+bx)^{5/2}}{\sqrt{x}} dx$.2533
3.561	$\int \frac{(2+bx)^{5/2}}{x^{3/2}} dx$.2537
3.562	$\int \frac{(2+bx)^{5/2}}{x^{5/2}} dx$.2542
3.563	$\int x^{5/2}(2-bx)^{5/2} dx$.2547

3.564	$\int x^{3/2}(2-bx)^{5/2} dx$.2551
3.565	$\int \sqrt{x}(2-bx)^{5/2} dx$.2558
3.566	$\int \frac{(2-bx)^{5/2}}{\sqrt{x}} dx$.2565
3.567	$\int \frac{(2-bx)^{5/2}}{x^{3/2}} dx$.2570
3.568	$\int \frac{(2-bx)^{5/2}}{x^{5/2}} dx$.2575
3.569	$\int \frac{x^{5/2}}{\sqrt{a+bx}} dx$.2580
3.570	$\int \frac{x^{3/2}}{\sqrt{a+bx}} dx$.2584
3.571	$\int \frac{\sqrt{x}}{\sqrt{a+bx}} dx$.2588
3.572	$\int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx$.2592
3.573	$\int \frac{1}{x^{3/2}\sqrt{a+bx}} dx$.2596
3.574	$\int \frac{1}{x^{5/2}\sqrt{a+bx}} dx$.2599
3.575	$\int \frac{1}{x^{7/2}\sqrt{a+bx}} dx$.2602
3.576	$\int \frac{1}{x^{9/2}\sqrt{a+bx}} dx$.2606
3.577	$\int \frac{x^{5/2}}{(a+bx)^{3/2}} dx$.2610
3.578	$\int \frac{x^{3/2}}{(a+bx)^{3/2}} dx$.2615
3.579	$\int \frac{\sqrt{x}}{(a+bx)^{3/2}} dx$.2619
3.580	$\int \frac{1}{\sqrt{x}(a+bx)^{3/2}} dx$.2623
3.581	$\int \frac{1}{x^{3/2}(a+bx)^{3/2}} dx$.2626
3.582	$\int \frac{1}{x^{5/2}(a+bx)^{3/2}} dx$.2629
3.583	$\int \frac{1}{x^{7/2}(a+bx)^{3/2}} dx$.2633
3.584	$\int \frac{x^{5/2}}{(a+bx)^{5/2}} dx$.2637
3.585	$\int \frac{x^{3/2}}{(a+bx)^{5/2}} dx$.2642
3.586	$\int \frac{\sqrt{x}}{(a+bx)^{5/2}} dx$.2646
3.587	$\int \frac{1}{\sqrt{x}(a+bx)^{5/2}} dx$.2649
3.588	$\int \frac{1}{x^{3/2}(a+bx)^{5/2}} dx$.2652
3.589	$\int \frac{1}{x^{5/2}(a+bx)^{5/2}} dx$.2656
3.590	$\int \frac{x^{5/2}}{\sqrt{a-bx}} dx$.2660
3.591	$\int \frac{x^{3/2}}{\sqrt{a-bx}} dx$.2664

3.592	$\int \frac{\sqrt{x}}{\sqrt{a-bx}} dx$.2668
3.593	$\int \frac{1}{\sqrt{x} \sqrt{a-bx}} dx$.2672
3.594	$\int \frac{1}{x^{3/2} \sqrt{a-bx}} dx$.2676
3.595	$\int \frac{1}{x^{5/2} \sqrt{a-bx}} dx$.2679
3.596	$\int \frac{x^{5/2}}{(a-bx)^{3/2}} dx$.2682
3.597	$\int \frac{x^{3/2}}{(a-bx)^{3/2}} dx$.2687
3.598	$\int \frac{\sqrt{x}}{(a-bx)^{3/2}} dx$.2691
3.599	$\int \frac{1}{\sqrt{x} (a-bx)^{3/2}} dx$.2695
3.600	$\int \frac{1}{x^{3/2} (a-bx)^{3/2}} dx$.2698
3.601	$\int \frac{1}{x^{5/2} (a-bx)^{3/2}} dx$.2701
3.602	$\int \frac{x^{5/2}}{(a-bx)^{5/2}} dx$.2705
3.603	$\int \frac{x^{3/2}}{(a-bx)^{5/2}} dx$.2710
3.604	$\int \frac{\sqrt{x}}{(a-bx)^{5/2}} dx$.2715
3.605	$\int \frac{1}{\sqrt{x} (a-bx)^{5/2}} dx$.2718
3.606	$\int \frac{1}{x^{3/2} (a-bx)^{5/2}} dx$.2722
3.607	$\int \frac{1}{x^{5/2} (a-bx)^{5/2}} dx$.2726
3.608	$\int \frac{x^{5/2}}{\sqrt{2+bx}} dx$.2730
3.609	$\int \frac{x^{3/2}}{\sqrt{2+bx}} dx$.2735
3.610	$\int \frac{\sqrt{x}}{\sqrt{2+bx}} dx$.2739
3.611	$\int \frac{1}{\sqrt{x} \sqrt{2+bx}} dx$.2743
3.612	$\int \frac{1}{x^{3/2} \sqrt{2+bx}} dx$.2747
3.613	$\int \frac{1}{x^{5/2} \sqrt{2+bx}} dx$.2750
3.614	$\int \frac{1}{x^{7/2} \sqrt{2+bx}} dx$.2753
3.615	$\int \frac{1}{x^{9/2} \sqrt{2+bx}} dx$.2757
3.616	$\int \frac{x^{5/2}}{(2+bx)^{3/2}} dx$.2761
3.617	$\int \frac{x^{3/2}}{(2+bx)^{3/2}} dx$.2765
3.618	$\int \frac{\sqrt{x}}{(2+bx)^{3/2}} dx$.2769

3.619	$\int \frac{1}{\sqrt{x}(2+bx)^{3/2}} dx$.2773
3.620	$\int \frac{1}{x^{3/2}(2+bx)^{3/2}} dx$.2776
3.621	$\int \frac{1}{x^{5/2}(2+bx)^{3/2}} dx$.2779
3.622	$\int \frac{1}{x^{7/2}(2+bx)^{3/2}} dx$.2783
3.623	$\int \frac{x^{5/2}}{(2+bx)^{5/2}} dx$.2787
3.624	$\int \frac{x^{3/2}}{(2+bx)^{5/2}} dx$.2792
3.625	$\int \frac{\sqrt{x}}{(2+bx)^{5/2}} dx$.2796
3.626	$\int \frac{1}{\sqrt{x}(2+bx)^{5/2}} dx$.2799
3.627	$\int \frac{1}{x^{3/2}(2+bx)^{5/2}} dx$.2802
3.628	$\int \frac{1}{x^{5/2}(2+bx)^{5/2}} dx$.2806
3.629	$\int \frac{x^{5/2}}{\sqrt{2-bx}} dx$.2810
3.630	$\int \frac{x^{3/2}}{\sqrt{2-bx}} dx$.2815
3.631	$\int \frac{\sqrt{x}}{\sqrt{2-bx}} dx$.2819
3.632	$\int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx$.2823
3.633	$\int \frac{1}{x^{3/2}\sqrt{2-bx}} dx$.2827
3.634	$\int \frac{1}{x^{5/2}\sqrt{2-bx}} dx$.2830
3.635	$\int \frac{x^{5/2}}{(2-bx)^{3/2}} dx$.2833
3.636	$\int \frac{x^{3/2}}{(2-bx)^{3/2}} dx$.2837
3.637	$\int \frac{\sqrt{x}}{(2-bx)^{3/2}} dx$.2841
3.638	$\int \frac{1}{\sqrt{x}(2-bx)^{3/2}} dx$.2845
3.639	$\int \frac{1}{x^{3/2}(2-bx)^{3/2}} dx$.2848
3.640	$\int \frac{1}{x^{5/2}(2-bx)^{3/2}} dx$.2851
3.641	$\int \frac{x^{5/2}}{(2-bx)^{5/2}} dx$.2855
3.642	$\int \frac{x^{3/2}}{(2-bx)^{5/2}} dx$.2860
3.643	$\int \frac{\sqrt{x}}{(2-bx)^{5/2}} dx$.2864
3.644	$\int \frac{1}{\sqrt{x}(2-bx)^{5/2}} dx$.2867
3.645	$\int \frac{1}{x^{3/2}(2-bx)^{5/2}} dx$.2871

3.646	$\int \frac{1}{x^{5/2}(2-bx)^{5/2}} dx$.2875
3.647	$\int \frac{\sqrt{x}}{\sqrt{1-x}} dx$.2879
3.648	$\int \frac{1}{\sqrt{1-x}\sqrt{x}} dx$.2882
3.649	$\int \frac{1}{\sqrt{x}\sqrt{1-bx}} dx$.2885
3.650	$\int x^{5/3}(a+bx) dx$.2889
3.651	$\int x^{4/3}(a+bx) dx$.2892
3.652	$\int x^{2/3}(a+bx) dx$.2895
3.653	$\int \sqrt[3]{x}(a+bx) dx$.2898
3.654	$\int \frac{a+bx}{\sqrt[3]{x}} dx$.2901
3.655	$\int \frac{a+bx}{x^{2/3}} dx$.2904
3.656	$\int \frac{a+bx}{x^{4/3}} dx$.2907
3.657	$\int \frac{a+bx}{x^{5/3}} dx$.2910
3.658	$\int x^{5/3}(a+bx)^2 dx$.2913
3.659	$\int x^{4/3}(a+bx)^2 dx$.2916
3.660	$\int x^{2/3}(a+bx)^2 dx$.2919
3.661	$\int \sqrt[3]{x}(a+bx)^2 dx$.2922
3.662	$\int \frac{(a+bx)^2}{\sqrt[3]{x}} dx$.2926
3.663	$\int \frac{(a+bx)^2}{x^{2/3}} dx$.2930
3.664	$\int \frac{(a+bx)^2}{x^{4/3}} dx$.2934
3.665	$\int \frac{(a+bx)^2}{x^{5/3}} dx$.2938
3.666	$\int x^{5/3}(a+bx)^3 dx$.2942
3.667	$\int x^{4/3}(a+bx)^3 dx$.2945
3.668	$\int x^{2/3}(a+bx)^3 dx$.2948
3.669	$\int \sqrt[3]{x}(a+bx)^3 dx$.2951
3.670	$\int \frac{(a+bx)^3}{\sqrt[3]{x}} dx$.2957
3.671	$\int \frac{(a+bx)^3}{x^{2/3}} dx$.2964
3.672	$\int \frac{(a+bx)^3}{x^{4/3}} dx$.2971
3.673	$\int \frac{(a+bx)^3}{x^{5/3}} dx$.2976
3.674	$\int \frac{x^{5/3}}{a+bx} dx$.2981
3.675	$\int \frac{a+bx}{x^{4/3}} dx$.2986
3.676	$\int \frac{a+bx}{x^{2/3}} dx$.2991

3.677	$\int \frac{\sqrt[3]{x}}{a+bx} dx$2996
3.678	$\int \frac{1}{\sqrt[3]{x}(a+bx)} dx$3001
3.679	$\int \frac{1}{x^{2/3}(a+bx)} dx$3006
3.680	$\int \frac{1}{x^{4/3}(a+bx)} dx$3011
3.681	$\int \frac{1}{x^{5/3}(a+bx)} dx$3016
3.682	$\int \frac{x^{5/3}}{(a+bx)^2} dx$3021
3.683	$\int \frac{x^{4/3}}{(a+bx)^2} dx$3026
3.684	$\int \frac{x^{2/3}}{(a+bx)^2} dx$3031
3.685	$\int \frac{\sqrt[3]{x}}{(a+bx)^2} dx$3037
3.686	$\int \frac{1}{\sqrt[3]{x}(a+bx)^2} dx$3042
3.687	$\int \frac{1}{x^{2/3}(a+bx)^2} dx$3048
3.688	$\int \frac{1}{x^{4/3}(a+bx)^2} dx$3053
3.689	$\int \frac{1}{x^{5/3}(a+bx)^2} dx$3058
3.690	$\int \frac{x^{5/3}}{(a+bx)^3} dx$3063
3.691	$\int \frac{x^{4/3}}{(a+bx)^3} dx$3068
3.692	$\int \frac{x^{2/3}}{(a+bx)^3} dx$3073
3.693	$\int \frac{\sqrt[3]{x}}{(a+bx)^3} dx$3078
3.694	$\int \frac{1}{\sqrt[3]{x}(a+bx)^3} dx$3083
3.695	$\int \frac{1}{x^{2/3}(a+bx)^3} dx$3088
3.696	$\int \frac{1}{x^{4/3}(a+bx)^3} dx$3093
3.697	$\int \frac{1}{x^{5/3}(a+bx)^3} dx$3098
3.698	$\int \frac{\sqrt[4]{1-x}}{1+x} dx$3103
3.699	$\int x^m(a+bx)^{10} dx$3107
3.700	$\int x^m(a+bx)^7 dx$3122
3.701	$\int x^m(a+bx)^3 dx$3129
3.702	$\int x^m(a+bx)^2 dx$3133
3.703	$\int x^m(a+bx) dx$3136
3.704	$\int \frac{x^m}{a+bx} dx$3139
3.705	$\int \frac{x^m}{(a+bx)^2} dx$3142

3.706	$\int \frac{x^m}{(a+bx)^3} dx$3145
3.707	$\int x^m(a+bx)^{5/2} dx$3148
3.708	$\int x^m(a+bx)^{3/2} dx$3151
3.709	$\int x^m \sqrt{a+bx} dx$3154
3.710	$\int \frac{x^m}{\sqrt{a+bx}} dx$3157
3.711	$\int \frac{x^m}{(a+bx)^{3/2}} dx$3160
3.712	$\int \frac{x^m}{(a+bx)^{5/2}} dx$3163
3.713	$\int \frac{x^{2+m}}{\sqrt{a+bx}} dx$3166
3.714	$\int \frac{x^{1+m}}{\sqrt{a+bx}} dx$3169
3.715	$\int \frac{x^m}{\sqrt{a+bx}} dx$3172
3.716	$\int \frac{x^{-1+m}}{\sqrt{a+bx}} dx$3175
3.717	$\int \frac{x^{-2+m}}{\sqrt{a+bx}} dx$3178
3.718	$\int \frac{x^{-3+m}}{\sqrt{a+bx}} dx$3181
3.719	$\int \frac{x^m}{\sqrt{2+3x}} dx$3184
3.720	$\int \frac{x^m}{\sqrt{2-3x}} dx$3187
3.721	$\int \frac{x^m}{\sqrt{-2+3x}} dx$3190
3.722	$\int \frac{x^m}{\sqrt{-2-3x}} dx$3193
3.723	$\int \frac{(-x)^m}{\sqrt{a+bx}} dx$3196
3.724	$\int \frac{(-x)^m}{\sqrt{2+3x}} dx$3199
3.725	$\int \frac{(-x)^m}{\sqrt{2-3x}} dx$3202
3.726	$\int \frac{(-x)^m}{\sqrt{-2+3x}} dx$3205
3.727	$\int \frac{(-x)^m}{\sqrt{-2-3x}} dx$3208
3.728	$\int \frac{x^n}{\sqrt{1-x}} dx$3211
3.729	$\int \frac{x^n}{\sqrt{a-ax}} dx$3214
3.730	$\int x^m(a+bx)^n dx$3217
3.731	$\int (cx)^m(a+bx)^n dx$3220
3.732	$\int x^3(a+bx)^n dx$3223
3.733	$\int x^2(a+bx)^n dx$3227
3.734	$\int x(a+bx)^n dx$3231

3.735	$\int (a + bx)^n dx$3234
3.736	$\int \frac{(a+bx)^n}{x} dx$3237
3.737	$\int \frac{(a+bx)^n}{x^2} dx$3240
3.738	$\int \frac{(a+bx)^n}{x^3} dx$3243
3.739	$\int x^{-4+n}(a + bx)^{-n} dx$3246
3.740	$\int x^{-3+n}(a + bx)^{-n} dx$3249
3.741	$\int x^{-2+n}(a + bx)^{-n} dx$3252
3.742	$\int x^{-1+n}(a + bx)^{-n} dx$3255
3.743	$\int x^n(a + bx)^{-n} dx$3258
3.744	$\int x^{1+n}(a + bx)^{-n} dx$3261
3.745	$\int x^{3/2}(a + bx)^n dx$3264
3.746	$\int \sqrt{x}(a + bx)^n dx$3267
3.747	$\int \frac{(a+bx)^n}{\sqrt{x}} dx$3270
3.748	$\int \frac{(a+bx)^n}{x^{3/2}} dx$3273
3.749	$\int \frac{(a+bx)^n}{x^{5/2}} dx$3276
3.750	$\int (bx)^m(2 + dx)^n dx$3279
3.751	$\int (bx)^m(c - bcx)^n dx$3282
3.752	$\int (bx)^m(c + dx)^n dx$3285
3.753	$\int x^{-1+n}(a + bx)^{-1-n} dx$3288
3.754	$\int x^{-3-n}(a + bx)^n dx$3291
3.755	$\int x^{2n-3(1+n)}(a + bx)^n dx$3295
3.756	$\int x^3\sqrt{cx^2}(a + bx) dx$3299
3.757	$\int x^2\sqrt{cx^2}(a + bx) dx$3302
3.758	$\int x\sqrt{cx^2}(a + bx) dx$3305
3.759	$\int \sqrt{cx^2}(a + bx) dx$3308
3.760	$\int \frac{\sqrt{cx^2}(a+bx)}{x} dx$3311
3.761	$\int \frac{\sqrt{cx^2}(a+bx)}{x^2} dx$3314
3.762	$\int \frac{\sqrt{cx^2}(a+bx)}{x^3} dx$3317
3.763	$\int \frac{\sqrt{cx^2}(a+bx)}{x^4} dx$3320
3.764	$\int x^3 (cx^2)^{3/2} (a + bx) dx$3323
3.765	$\int x^2 (cx^2)^{3/2} (a + bx) dx$3326
3.766	$\int x (cx^2)^{3/2} (a + bx) dx$3329
3.767	$\int (cx^2)^{3/2} (a + bx) dx$3332

3.768	$\int \frac{(cx^2)^{3/2}(a+bx)}{x} dx$.3335
3.769	$\int \frac{(cx^2)^{3/2}(a+bx)}{x^2} dx$.3338
3.770	$\int \frac{(cx^2)^{3/2}(a+bx)}{x^3} dx$.3341
3.771	$\int \frac{(cx^2)^{3/2}(a+bx)}{x^4} dx$.3344
3.772	$\int x^3 (cx^2)^{5/2} (a+bx) dx$.3347
3.773	$\int x^2 (cx^2)^{5/2} (a+bx) dx$.3350
3.774	$\int x (cx^2)^{5/2} (a+bx) dx$.3353
3.775	$\int (cx^2)^{5/2} (a+bx) dx$.3356
3.776	$\int \frac{(cx^2)^{5/2}(a+bx)}{x} dx$.3359
3.777	$\int \frac{(cx^2)^{5/2}(a+bx)}{x^2} dx$.3362
3.778	$\int \frac{(cx^2)^{5/2}(a+bx)}{x^3} dx$.3365
3.779	$\int \frac{(cx^2)^{5/2}(a+bx)}{x^4} dx$.3368
3.780	$\int \frac{x^3(a+bx)}{\sqrt{cx^2}} dx$.3371
3.781	$\int \frac{x^2(a+bx)}{\sqrt{cx^2}} dx$.3374
3.782	$\int \frac{x(a+bx)}{\sqrt{cx^2}} dx$.3377
3.783	$\int \frac{a+bx}{\sqrt{cx^2}} dx$.3380
3.784	$\int \frac{a+bx}{x\sqrt{cx^2}} dx$.3383
3.785	$\int \frac{a+bx}{x^2\sqrt{cx^2}} dx$.3386
3.786	$\int \frac{a+bx}{x^3\sqrt{cx^2}} dx$.3389
3.787	$\int \frac{a+bx}{x^4\sqrt{cx^2}} dx$.3392
3.788	$\int \frac{x^3(a+bx)}{(cx^2)^{3/2}} dx$.3395
3.789	$\int \frac{x^2(a+bx)}{(cx^2)^{3/2}} dx$.3398
3.790	$\int \frac{x(a+bx)}{(cx^2)^{3/2}} dx$.3401
3.791	$\int \frac{a+bx}{(cx^2)^{3/2}} dx$.3404
3.792	$\int \frac{a+bx}{x(cx^2)^{3/2}} dx$.3407

3.793	$\int \frac{a+bx}{x^2(cx^2)^{3/2}} dx$3410
3.794	$\int \frac{a+bx}{x^3(cx^2)^{3/2}} dx$3413
3.795	$\int \frac{a+bx}{x^4(cx^2)^{3/2}} dx$3416
3.796	$\int \frac{x^3(a+bx)}{(cx^2)^{5/2}} dx$3419
3.797	$\int \frac{x^2(a+bx)}{(cx^2)^{5/2}} dx$3422
3.798	$\int \frac{x(a+bx)}{(cx^2)^{5/2}} dx$3425
3.799	$\int \frac{a+bx}{(cx^2)^{5/2}} dx$3428
3.800	$\int \frac{a+bx}{x(cx^2)^{5/2}} dx$3431
3.801	$\int \frac{a+bx}{x^2(cx^2)^{5/2}} dx$3434
3.802	$\int \frac{a+bx}{x^3(cx^2)^{5/2}} dx$3437
3.803	$\int \frac{a+bx}{x^4(cx^2)^{5/2}} dx$3440
3.804	$\int x^3 \sqrt{cx^2} (a+bx)^2 dx$3443
3.805	$\int x^2 \sqrt{cx^2} (a+bx)^2 dx$3446
3.806	$\int x \sqrt{cx^2} (a+bx)^2 dx$3449
3.807	$\int \sqrt{cx^2} (a+bx)^2 dx$3452
3.808	$\int \frac{\sqrt{cx^2} (a+bx)^2}{x} dx$3455
3.809	$\int \frac{\sqrt{cx^2} (a+bx)^2}{x^2} dx$3458
3.810	$\int \frac{\sqrt{cx^2} (a+bx)^2}{x^3} dx$3461
3.811	$\int \frac{\sqrt{cx^2} (a+bx)^2}{x^4} dx$3464
3.812	$\int x^3 (cx^2)^{3/2} (a+bx)^2 dx$3467
3.813	$\int x^2 (cx^2)^{3/2} (a+bx)^2 dx$3470
3.814	$\int x (cx^2)^{3/2} (a+bx)^2 dx$3473
3.815	$\int (cx^2)^{3/2} (a+bx)^2 dx$3476
3.816	$\int \frac{(cx^2)^{3/2} (a+bx)^2}{x} dx$3479
3.817	$\int \frac{(cx^2)^{3/2} (a+bx)^2}{x^2} dx$3482

3.818	$\int \frac{(cx^2)^{3/2}(a+bx)^2}{x^3} dx$.3485
3.819	$\int \frac{(cx^2)^{3/2}(a+bx)^2}{x^4} dx$.3488
3.820	$\int x(cx^2)^{5/2}(a+bx)^2 dx$.3491
3.821	$\int (cx^2)^{5/2}(a+bx)^2 dx$.3494
3.822	$\int \frac{(cx^2)^{5/2}(a+bx)^2}{x} dx$.3497
3.823	$\int \frac{(cx^2)^{5/2}(a+bx)^2}{x^2} dx$.3500
3.824	$\int \frac{(cx^2)^{5/2}(a+bx)^2}{x^3} dx$.3503
3.825	$\int \frac{(cx^2)^{5/2}(a+bx)^2}{x^4} dx$.3506
3.826	$\int \frac{(cx^2)^{5/2}(a+bx)^2}{x^5} dx$.3509
3.827	$\int \frac{(cx^2)^{5/2}(a+bx)^2}{x^6} dx$.3512
3.828	$\int \frac{x^3(a+bx)^2}{\sqrt{cx^2}} dx$.3515
3.829	$\int \frac{x^2(a+bx)^2}{\sqrt{cx^2}} dx$.3518
3.830	$\int \frac{x(a+bx)^2}{\sqrt{cx^2}} dx$.3521
3.831	$\int \frac{(a+bx)^2}{\sqrt{cx^2}} dx$.3524
3.832	$\int \frac{(a+bx)^2}{x\sqrt{cx^2}} dx$.3527
3.833	$\int \frac{(a+bx)^2}{x^2\sqrt{cx^2}} dx$.3530
3.834	$\int \frac{(a+bx)^2}{x^3\sqrt{cx^2}} dx$.3533
3.835	$\int \frac{(a+bx)^2}{x^4\sqrt{cx^2}} dx$.3536
3.836	$\int \frac{x^3(a+bx)^2}{(cx^2)^{3/2}} dx$.3539
3.837	$\int \frac{x^2(a+bx)^2}{(cx^2)^{3/2}} dx$.3542
3.838	$\int \frac{x(a+bx)^2}{(cx^2)^{3/2}} dx$.3545
3.839	$\int \frac{(a+bx)^2}{(cx^2)^{3/2}} dx$.3548
3.840	$\int \frac{(a+bx)^2}{x(cx^2)^{3/2}} dx$.3551
3.841	$\int \frac{(a+bx)^2}{x^2(cx^2)^{3/2}} dx$.3554

3.842	$\int \frac{(a+bx)^2}{x^3(cx^2)^{3/2}} dx$.3557
3.843	$\int \frac{(a+bx)^2}{x^4(cx^2)^{3/2}} dx$.3560
3.844	$\int \frac{x^3(a+bx)^2}{(cx^2)^{5/2}} dx$.3563
3.845	$\int \frac{x^2(a+bx)^2}{(cx^2)^{5/2}} dx$.3566
3.846	$\int \frac{x(a+bx)^2}{(cx^2)^{5/2}} dx$.3569
3.847	$\int \frac{(a+bx)^2}{(cx^2)^{5/2}} dx$.3572
3.848	$\int \frac{(a+bx)^2}{x(cx^2)^{5/2}} dx$.3575
3.849	$\int \frac{(a+bx)^2}{x^2(cx^2)^{5/2}} dx$.3578
3.850	$\int \frac{(a+bx)^2}{x^3(cx^2)^{5/2}} dx$.3581
3.851	$\int \frac{(a+bx)^2}{x^4(cx^2)^{5/2}} dx$.3584
3.852	$\int \frac{x^3\sqrt{cx^2}}{a+bx} dx$.3587
3.853	$\int \frac{x^2\sqrt{cx^2}}{a+bx} dx$.3590
3.854	$\int \frac{x\sqrt{cx^2}}{a+bx} dx$.3593
3.855	$\int \frac{\sqrt{cx^2}}{a+bx} dx$.3596
3.856	$\int \frac{\sqrt{cx^2}}{x(a+bx)} dx$.3599
3.857	$\int \frac{\sqrt{cx^2}}{x^2(a+bx)} dx$.3602
3.858	$\int \frac{\sqrt{cx^2}}{x^3(a+bx)} dx$.3605
3.859	$\int \frac{\sqrt{cx^2}}{x^4(a+bx)} dx$.3608
3.860	$\int \frac{x(cx^2)^{3/2}}{a+bx} dx$.3611
3.861	$\int \frac{(cx^2)^{3/2}}{a+bx} dx$.3615
3.862	$\int \frac{(cx^2)^{3/2}}{x(a+bx)} dx$.3618
3.863	$\int \frac{(cx^2)^{3/2}}{x^2(a+bx)} dx$.3621
3.864	$\int \frac{(cx^2)^{3/2}}{x^3(a+bx)} dx$.3624

3.865	$\int \frac{(cx^2)^{3/2}}{x^4(a+bx)} dx$3627
3.866	$\int \frac{(cx^2)^{3/2}}{x^5(a+bx)} dx$3630
3.867	$\int \frac{(cx^2)^{3/2}}{x^6(a+bx)} dx$3633
3.868	$\int \frac{(cx^2)^{3/2}}{x^7(a+bx)} dx$3636
3.869	$\int \frac{(cx^2)^{5/2}}{a+bx} dx$3639
3.870	$\int \frac{(cx^2)^{5/2}}{x(a+bx)} dx$3643
3.871	$\int \frac{(cx^2)^{5/2}}{x^2(a+bx)} dx$3647
3.872	$\int \frac{(cx^2)^{5/2}}{x^3(a+bx)} dx$3651
3.873	$\int \frac{(cx^2)^{5/2}}{x^4(a+bx)} dx$3654
3.874	$\int \frac{(cx^2)^{5/2}}{x^5(a+bx)} dx$3657
3.875	$\int \frac{(cx^2)^{5/2}}{x^6(a+bx)} dx$3660
3.876	$\int \frac{(cx^2)^{5/2}}{x^7(a+bx)} dx$3663
3.877	$\int \frac{x^4}{\sqrt{cx^2}(a+bx)} dx$3666
3.878	$\int \frac{x^3}{\sqrt{cx^2}(a+bx)} dx$3669
3.879	$\int \frac{x^2}{\sqrt{cx^2}(a+bx)} dx$3672
3.880	$\int \frac{x}{\sqrt{cx^2}(a+bx)} dx$3675
3.881	$\int \frac{1}{\sqrt{cx^2}(a+bx)} dx$3678
3.882	$\int \frac{1}{x\sqrt{cx^2}(a+bx)} dx$3681
3.883	$\int \frac{1}{x^2\sqrt{cx^2}(a+bx)} dx$3684
3.884	$\int \frac{1}{x^3\sqrt{cx^2}(a+bx)} dx$3687
3.885	$\int \frac{x^6}{(cx^2)^{3/2}(a+bx)} dx$3690
3.886	$\int \frac{x^5}{(cx^2)^{3/2}(a+bx)} dx$3694
3.887	$\int \frac{x^4}{(cx^2)^{3/2}(a+bx)} dx$3698

3.888	$\int \frac{x^3}{(cx^2)^{3/2}(a+bx)} dx$3701
3.889	$\int \frac{x^2}{(cx^2)^{3/2}(a+bx)} dx$3704
3.890	$\int \frac{x}{(cx^2)^{3/2}(a+bx)} dx$3707
3.891	$\int \frac{1}{(cx^2)^{3/2}(a+bx)} dx$3710
3.892	$\int \frac{1}{x(cx^2)^{3/2}(a+bx)} dx$3713
3.893	$\int \frac{x^3\sqrt{cx^2}}{(a+bx)^2} dx$3716
3.894	$\int \frac{x^2\sqrt{cx^2}}{(a+bx)^2} dx$3720
3.895	$\int \frac{x\sqrt{cx^2}}{(a+bx)^2} dx$3724
3.896	$\int \frac{\sqrt{cx^2}}{(a+bx)^2} dx$3727
3.897	$\int \frac{\sqrt{cx^2}}{x(a+bx)^2} dx$3730
3.898	$\int \frac{\sqrt{cx^2}}{x^2(a+bx)^2} dx$3733
3.899	$\int \frac{\sqrt{cx^2}}{x^3(a+bx)^2} dx$3736
3.900	$\int \frac{\sqrt{cx^2}}{x^4(a+bx)^2} dx$3739
3.901	$\int \frac{x(cx^2)^{3/2}}{(a+bx)^2} dx$3742
3.902	$\int \frac{(cx^2)^{3/2}}{(a+bx)^2} dx$3746
3.903	$\int \frac{(cx^2)^{3/2}}{x(a+bx)^2} dx$3750
3.904	$\int \frac{(cx^2)^{3/2}}{x^2(a+bx)^2} dx$3754
3.905	$\int \frac{(cx^2)^{3/2}}{x^3(a+bx)^2} dx$3757
3.906	$\int \frac{(cx^2)^{3/2}}{x^4(a+bx)^2} dx$3760
3.907	$\int \frac{(cx^2)^{3/2}}{x^5(a+bx)^2} dx$3763
3.908	$\int \frac{(cx^2)^{3/2}}{x^6(a+bx)^2} dx$3766
3.909	$\int \frac{x^5}{\sqrt{cx^2}(a+bx)^2} dx$3769
3.910	$\int \frac{x^4}{\sqrt{cx^2}(a+bx)^2} dx$3773

3.911	$\int \frac{x^3}{\sqrt{cx^2(a+bx)^2}} dx$.3777
3.912	$\int \frac{x^2}{\sqrt{cx^2(a+bx)^2}} dx$.3781
3.913	$\int \frac{x}{\sqrt{cx^2(a+bx)^2}} dx$.3784
3.914	$\int \frac{1}{\sqrt{cx^2(a+bx)^2}} dx$.3787
3.915	$\int \frac{1}{x\sqrt{cx^2(a+bx)^2}} dx$.3790
3.916	$\int \frac{1}{x^2\sqrt{cx^2(a+bx)^2}} dx$.3793
3.917	$\int \frac{x^5}{(cx^2)^{3/2}(a+bx)^2} dx$.3797
3.918	$\int \frac{x^4}{(cx^2)^{3/2}(a+bx)^2} dx$.3801
3.919	$\int \frac{x^3}{(cx^2)^{3/2}(a+bx)^2} dx$.3805
3.920	$\int \frac{x^2}{(cx^2)^{3/2}(a+bx)^2} dx$.3808
3.921	$\int \frac{x}{(cx^2)^{3/2}(a+bx)^2} dx$.3812
3.922	$\int \frac{1}{(cx^2)^{3/2}(a+bx)^2} dx$.3816
3.923	$\int x^2\sqrt{cx^2(a+bx)^n} dx$.3820
3.924	$\int x\sqrt{cx^2(a+bx)^n} dx$.3825
3.925	$\int \sqrt{cx^2(a+bx)^n} dx$.3829
3.926	$\int \frac{\sqrt{cx^2(a+bx)^n}}{x} dx$.3833
3.927	$\int \frac{\sqrt{cx^2(a+bx)^n}}{x^2} dx$.3836
3.928	$\int \frac{\sqrt{cx^2(a+bx)^n}}{x^3} dx$.3839
3.929	$\int \frac{\sqrt{cx^2(a+bx)^n}}{x^4} dx$.3842
3.930	$\int x(cx^2)^{3/2}(a+bx)^n dx$.3845
3.931	$\int (cx^2)^{3/2}(a+bx)^n dx$.3849
3.932	$\int \frac{(cx^2)^{3/2}(a+bx)^n}{x} dx$.3853
3.933	$\int \frac{(cx^2)^{3/2}(a+bx)^n}{x^2} dx$.3857
3.934	$\int \frac{(cx^2)^{3/2}(a+bx)^n}{x^3} dx$.3861
3.935	$\int \frac{(cx^2)^{3/2}(a+bx)^n}{x^4} dx$.3864

3.936	$\int \frac{(cx^2)^{3/2} (a+bx)^n}{x^5} dx$.3867
3.937	$\int \frac{(cx^2)^{3/2} (a+bx)^n}{x^{5/2}} dx$.3870
3.938	$\int (cx^2)^{5/2} (a+bx)^n dx$.3873
3.939	$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x} dx$.3877
3.940	$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x^2} dx$.3881
3.941	$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x^3} dx$.3885
3.942	$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x^4} dx$.3889
3.943	$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x^5} dx$.3893
3.944	$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x^6} dx$.3896
3.945	$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x^7} dx$.3899
3.946	$\int \frac{x^4(a+bx)^n}{\sqrt{cx^2}} dx$.3902
3.947	$\int \frac{x^3(a+bx)^n}{\sqrt{cx^2}} dx$.3906
3.948	$\int \frac{x^2(a+bx)^n}{\sqrt{cx^2}} dx$.3910
3.949	$\int \frac{x(a+bx)^n}{\sqrt{cx^2}} dx$.3914
3.950	$\int \frac{(a+bx)^n}{\sqrt{cx^2}} dx$.3917
3.951	$\int \frac{(a+bx)^n}{x\sqrt{cx^2}} dx$.3920
3.952	$\int \frac{(a+bx)^n}{x^2\sqrt{cx^2}} dx$.3923
3.953	$\int \frac{x^6(a+bx)^n}{(cx^2)^{3/2}} dx$.3926
3.954	$\int \frac{x^5(a+bx)^n}{(cx^2)^{3/2}} dx$.3931
3.955	$\int \frac{x^4(a+bx)^n}{(cx^2)^{3/2}} dx$.3935
3.956	$\int \frac{x^3(a+bx)^n}{(cx^2)^{3/2}} dx$.3939
3.957	$\int \frac{x^2(a+bx)^n}{(cx^2)^{3/2}} dx$.3942
3.958	$\int \frac{x(a+bx)^n}{(cx^2)^{3/2}} dx$.3945

3.959	$\int \frac{(a+bx)^n}{(cx^2)^{3/2}} dx$3948
3.960	$\int \frac{(a+bx)^n}{x(cx^2)^{3/2}} dx$3951
3.961	$\int \frac{x^8(a+bx)^n}{(cx^2)^{5/2}} dx$3954
3.962	$\int \frac{x^7(a+bx)^n}{(cx^2)^{5/2}} dx$3959
3.963	$\int \frac{x^6(a+bx)^n}{(cx^2)^{5/2}} dx$3963
3.964	$\int \frac{x^5(a+bx)^n}{(cx^2)^{5/2}} dx$3967
3.965	$\int \frac{x^4(a+bx)^n}{(cx^2)^{5/2}} dx$3970
3.966	$\int \frac{x^3(a+bx)^n}{(cx^2)^{5/2}} dx$3973
3.967	$\int \frac{x^2(a+bx)^n}{(cx^2)^{5/2}} dx$3976
3.968	$\int \frac{x(a+bx)^n}{(cx^2)^{5/2}} dx$3979
3.969	$\int (dx)^m (cx^2)^{5/2} (a+bx) dx$3982
3.970	$\int (dx)^m (cx^2)^{3/2} (a+bx) dx$3986
3.971	$\int (dx)^m \sqrt{cx^2} (a+bx) dx$3990
3.972	$\int \frac{(dx)^m (a+bx)}{\sqrt{cx^2}} dx$3994
3.973	$\int \frac{(dx)^m (a+bx)}{(cx^2)^{3/2}} dx$3998
3.974	$\int \frac{(dx)^m (a+bx)}{(cx^2)^{5/2}} dx$4002
3.975	$\int (dx)^m (cx^2)^{5/2} (a+bx)^2 dx$4006
3.976	$\int (dx)^m (cx^2)^{3/2} (a+bx)^2 dx$4010
3.977	$\int (dx)^m \sqrt{cx^2} (a+bx)^2 dx$4014
3.978	$\int \frac{(dx)^m (a+bx)^2}{\sqrt{cx^2}} dx$4018
3.979	$\int \frac{(dx)^m (a+bx)^2}{(cx^2)^{3/2}} dx$4022
3.980	$\int \frac{(dx)^m (a+bx)^2}{(cx^2)^{5/2}} dx$4026
3.981	$\int (dx)^m (cx^2)^{5/2} (a+bx)^n dx$4030
3.982	$\int (dx)^m (cx^2)^{3/2} (a+bx)^n dx$4033

3.983	$\int (dx)^m \sqrt{cx^2} (a + bx)^n dx$.4036
3.984	$\int \frac{(dx)^m (a+bx)^n}{\sqrt{cx^2}} dx$.4039
3.985	$\int \frac{(dx)^m (a+bx)^n}{(cx^2)^{3/2}} dx$.4043
3.986	$\int \frac{(dx)^m (a+bx)^n}{(cx^2)^{5/2}} dx$.4047
3.987	$\int x^3 (cx^2)^p (a + bx)^{-5-2p} dx$.4051
3.988	$\int x^2 (cx^2)^p (a + bx)^{-4-2p} dx$.4054
3.989	$\int x (cx^2)^p (a + bx)^{-3-2p} dx$.4057
3.990	$\int (cx^2)^p (a + bx)^{-2-2p} dx$.4060
3.991	$\int \frac{(cx^2)^p (a+bx)^{-1-2p}}{x} dx$.4064
3.992	$\int \frac{(cx^2)^p (a+bx)^{-2p}}{x^2} dx$.4067
3.993	$\int \frac{(cx^2)^p (a+bx)^{1-2p}}{x^3} dx$.4070
3.994	$\int \frac{(cx^2)^p (a+bx)^{2-2p}}{x^4} dx$.4073
3.995	$\int x^m (cx^2)^p (a + bx)^{-2-m-2p} dx$.4076
3.996	$\int (dx)^m (cx^2)^p (a + bx)^{-2-m-2p} dx$.4079
3.997	$\int x^m (cx^2)^p (a + bx)^n dx$.4082
3.998	$\int (dx)^m (cx^2)^p (a + bx)^n dx$.4085
3.999	$\int \frac{(a+bx)^5}{\left(\frac{ad}{b} + dx\right)^3} dx$.4088
3.1000	$\int \frac{(a+bx)^4}{\left(\frac{ad}{b} + dx\right)^3} dx$.4091
3.1001	$\int \frac{(a+bx)^3}{\left(\frac{ad}{b} + dx\right)^3} dx$.4094
3.1002	$\int \frac{(a+bx)^2}{\left(\frac{ad}{b} + dx\right)^3} dx$.4097
3.1003	$\int \frac{a+bx}{\left(\frac{ad}{b} + dx\right)^3} dx$.4100
3.1004	$\int \frac{1}{(a+bx)\left(\frac{ad}{b} + dx\right)^3} dx$.4103
3.1005	$\int \frac{1}{(a+bx)^2\left(\frac{ad}{b} + dx\right)^3} dx$.4106
3.1006	$\int \frac{1}{(a+bx)^3\left(\frac{ad}{b} + dx\right)^3} dx$.4109

3.1007	$\int \frac{\left(\frac{bc}{d}+bx\right)^5}{(c+dx)^3} dx$4112
3.1008	$\int \frac{\left(\frac{bc}{d}+bx\right)^4}{(c+dx)^3} dx$4115
3.1009	$\int \frac{\left(\frac{bc}{d}+bx\right)^3}{(c+dx)^3} dx$4118
3.1010	$\int \frac{\left(\frac{bc}{d}+bx\right)^2}{(c+dx)^3} dx$4121
3.1011	$\int \frac{\frac{bc}{d}+bx}{(c+dx)^3} dx$4124
3.1012	$\int \frac{1}{\left(\frac{bc}{d}+bx\right)(c+dx)^3} dx$4127
3.1013	$\int \frac{1}{\left(\frac{bc}{d}+bx\right)^2(c+dx)^3} dx$4130
3.1014	$\int \frac{1}{\left(\frac{bc}{d}+bx\right)^3(c+dx)^3} dx$4133
3.1015	$\int (a+bx)^5(ac+bcx)^n dx$4136
3.1016	$\int (a+bx)^5(ac+bcx)^3 dx$4140
3.1017	$\int (a+bx)^5(ac+bcx)^2 dx$4143
3.1018	$\int (a+bx)^5(ac+bcx) dx$4146
3.1019	$\int \frac{(a+bx)^5}{ac+bcx} dx$4149
3.1020	$\int \frac{(a+bx)^5}{(ac+bcx)^2} dx$4152
3.1021	$\int \frac{(a+bx)^5}{(ac+bcx)^3} dx$4155
3.1022	$\int \frac{(a+bx)^5}{(ac+bcx)^4} dx$4158
3.1023	$\int \frac{(a+bx)^5}{(ac+bcx)^5} dx$4161
3.1024	$\int \frac{(a+bx)^5}{(ac+bcx)^6} dx$4164
3.1025	$\int \frac{(a+bx)^5}{(ac+bcx)^7} dx$4167
3.1026	$\int \frac{(a+bx)^5}{(ac+bcx)^8} dx$4170
3.1027	$\int \frac{1}{\sqrt{-2-3x}\sqrt{2+3x}} dx$4173
3.1028	$\int (a+bx)(ac-bcx)^3 dx$4176
3.1029	$\int (a+bx)(ac-bcx)^2 dx$4179
3.1030	$\int (a+bx)(ac-bcx) dx$4182
3.1031	$\int (a+bx) dx$4185
3.1032	$\int \frac{a+bx}{ac-bcx} dx$4188

3.1033	$\int \frac{a+bx}{(ac-bcx)^2} dx$4191
3.1034	$\int \frac{a+bx}{(ac-bcx)^3} dx$4194
3.1035	$\int \frac{a+bx}{(ac-bcx)^4} dx$4197
3.1036	$\int \frac{a+bx}{(ac-bcx)^5} dx$4200
3.1037	$\int \frac{a+bx}{(ac-bcx)^6} dx$4203
3.1038	$\int (a+bx)^2(ac-bcx)^3 dx$4206
3.1039	$\int (a+bx)^2(ac-bcx)^2 dx$4209
3.1040	$\int (a+bx)^2(ac-bcx) dx$4212
3.1041	$\int (a+bx)^2 dx$4215
3.1042	$\int \frac{(a+bx)^2}{ac-bcx} dx$4218
3.1043	$\int \frac{(a+bx)^2}{(ac-bcx)^2} dx$4221
3.1044	$\int \frac{(a+bx)^2}{(ac-bcx)^3} dx$4224
3.1045	$\int \frac{(a+bx)^2}{(ac-bcx)^4} dx$4227
3.1046	$\int \frac{(a+bx)^2}{(ac-bcx)^5} dx$4230
3.1047	$\int \frac{(a+bx)^2}{(ac-bcx)^6} dx$4233
3.1048	$\int \frac{(a+bx)^2}{(ac-bcx)^7} dx$4236
3.1049	$\int \frac{(ac-bcx)^3}{a+bx} dx$4239
3.1050	$\int \frac{(ac-bcx)^2}{a+bx} dx$4242
3.1051	$\int \frac{ac-bcx}{a+bx} dx$4245
3.1052	$\int \frac{1}{a+bx} dx$4248
3.1053	$\int \frac{1}{(a+bx)(ac-bcx)} dx$4251
3.1054	$\int \frac{1}{(a+bx)(ac-bcx)^2} dx$4254
3.1055	$\int \frac{1}{(a+bx)(ac-bcx)^3} dx$4257
3.1056	$\int \frac{(ac-bcx)^3}{(a+bx)^2} dx$4261
3.1057	$\int \frac{(ac-bcx)^2}{(a+bx)^2} dx$4264
3.1058	$\int \frac{ac-bcx}{(a+bx)^2} dx$4267
3.1059	$\int \frac{1}{(a+bx)^2} dx$4270
3.1060	$\int \frac{1}{(a+bx)^2(ac-bcx)} dx$4273
3.1061	$\int \frac{1}{(a+bx)^2(ac-bcx)^2} dx$4276

3.1062	$\int \frac{1}{(a+bx)^2(ac-bcx)^3} dx$.4280
3.1063	$\int (1-x)^{9/2} \sqrt{1+x} dx$.4284
3.1064	$\int (1-x)^{7/2} \sqrt{1+x} dx$.4288
3.1065	$\int (1-x)^{5/2} \sqrt{1+x} dx$.4292
3.1066	$\int (1-x)^{3/2} \sqrt{1+x} dx$.4296
3.1067	$\int \sqrt{1-x} \sqrt{1+x} dx$.4300
3.1068	$\int \frac{\sqrt{1+x}}{\sqrt{1-x}} dx$.4303
3.1069	$\int \frac{\sqrt{1+x}}{(1-x)^{3/2}} dx$.4306
3.1070	$\int \frac{\sqrt{1+x}}{(1-x)^{5/2}} dx$.4309
3.1071	$\int \frac{\sqrt{1+x}}{(1-x)^{7/2}} dx$.4312
3.1072	$\int \frac{\sqrt{1+x}}{(1-x)^{9/2}} dx$.4315
3.1073	$\int \frac{\sqrt{1+x}}{(1-x)^{11/2}} dx$.4319
3.1074	$\int \frac{\sqrt{1+x}}{(1-x)^{13/2}} dx$.4324
3.1075	$\int (1-x)^{9/2} (1+x)^{3/2} dx$.4330
3.1076	$\int (1-x)^{7/2} (1+x)^{3/2} dx$.4334
3.1077	$\int (1-x)^{5/2} (1+x)^{3/2} dx$.4338
3.1078	$\int (1-x)^{3/2} (1+x)^{3/2} dx$.4342
3.1079	$\int \sqrt{1-x} (1+x)^{3/2} dx$.4346
3.1080	$\int \frac{(1+x)^{3/2}}{\sqrt{1-x}} dx$.4350
3.1081	$\int \frac{(1+x)^{3/2}}{(1-x)^{3/2}} dx$.4354
3.1082	$\int \frac{(1+x)^{3/2}}{(1-x)^{5/2}} dx$.4358
3.1083	$\int \frac{(1+x)^{3/2}}{(1-x)^{7/2}} dx$.4362
3.1084	$\int \frac{(1+x)^{3/2}}{(1-x)^{9/2}} dx$.4365
3.1085	$\int \frac{(1+x)^{3/2}}{(1-x)^{11/2}} dx$.4369
3.1086	$\int \frac{(1+x)^{3/2}}{(1-x)^{13/2}} dx$.4373
3.1087	$\int \frac{(1+x)^{3/2}}{(1-x)^{15/2}} dx$.4378
3.1088	$\int (1-x)^{11/2} (1+x)^{5/2} dx$.4382
3.1089	$\int (1-x)^{9/2} (1+x)^{5/2} dx$.4386
3.1090	$\int (1-x)^{7/2} (1+x)^{5/2} dx$.4390
3.1091	$\int (1-x)^{5/2} (1+x)^{5/2} dx$.4394

3.1092	$\int (1-x)^{3/2}(1+x)^{5/2} dx$.4398
3.1093	$\int \sqrt{1-x}(1+x)^{5/2} dx$.4402
3.1094	$\int \frac{(1+x)^{5/2}}{\sqrt{1-x}} dx$.4406
3.1095	$\int \frac{(1+x)^{5/2}}{(1-x)^{3/2}} dx$.4410
3.1096	$\int \frac{(1+x)^{5/2}}{(1-x)^{5/2}} dx$.4414
3.1097	$\int \frac{(1+x)^{5/2}}{(1-x)^{7/2}} dx$.4418
3.1098	$\int \frac{(1+x)^{5/2}}{(1-x)^{9/2}} dx$.4423
3.1099	$\int \frac{(1+x)^{5/2}}{(1-x)^{11/2}} dx$.4426
3.1100	$\int \frac{(1+x)^{5/2}}{(1-x)^{13/2}} dx$.4430
3.1101	$\int \frac{(1+x)^{5/2}}{(1-x)^{15/2}} dx$.4434
3.1102	$\int \frac{(1+x)^{5/2}}{(1-x)^{17/2}} dx$.4438
3.1103	$\int \frac{(1+x)^{5/2}}{(1-x)^{19/2}} dx$.4442
3.1104	$\int \frac{(1+ax)^{3/2}}{\sqrt{1-ax}} dx$.4446
3.1105	$\int \frac{(1+ax)\sqrt{1-a^2x^2}}{1-ax} dx$.4450
3.1106	$\int \frac{(1-x)^{7/2}}{\sqrt{1+x}} dx$.4454
3.1107	$\int \frac{(1-x)^{5/2}}{\sqrt{1+x}} dx$.4458
3.1108	$\int \frac{(1-x)^{3/2}}{\sqrt{1+x}} dx$.4462
3.1109	$\int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx$.4466
3.1110	$\int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx$.4469
3.1111	$\int \frac{1}{(1-x)^{3/2}\sqrt{1+x}} dx$.4472
3.1112	$\int \frac{1}{(1-x)^{5/2}\sqrt{1+x}} dx$.4475
3.1113	$\int \frac{1}{(1-x)^{7/2}\sqrt{1+x}} dx$.4478
3.1114	$\int \frac{1}{(1-x)^{9/2}\sqrt{1+x}} dx$.4482
3.1115	$\int \frac{1}{(1-x)^{11/2}\sqrt{1+x}} dx$.4486
3.1116	$\int \frac{(1-x)^{7/2}}{(1+x)^{3/2}} dx$.4490
3.1117	$\int \frac{(1-x)^{5/2}}{(1+x)^{3/2}} dx$.4494
3.1118	$\int \frac{(1-x)^{3/2}}{(1+x)^{3/2}} dx$.4498

3.1119	$\int \frac{\sqrt{1-x}}{(1+x)^{3/2}} dx$.4502
3.1120	$\int \frac{1}{\sqrt{1-x}(1+x)^{3/2}} dx$.4505
3.1121	$\int \frac{1}{(1-x)^{3/2}(1+x)^{3/2}} dx$.4508
3.1122	$\int \frac{1}{(1-x)^{5/2}(1+x)^{3/2}} dx$.4511
3.1123	$\int \frac{1}{(1-x)^{7/2}(1+x)^{3/2}} dx$.4514
3.1124	$\int \frac{1}{(1-x)^{9/2}(1+x)^{3/2}} dx$.4518
3.1125	$\int \frac{1}{(1-x)^{11/2}(1+x)^{3/2}} dx$.4522
3.1126	$\int \frac{(1-x)^{9/2}}{(1+x)^{5/2}} dx$.4526
3.1127	$\int \frac{(1-x)^{7/2}}{(1+x)^{5/2}} dx$.4530
3.1128	$\int \frac{(1-x)^{5/2}}{(1+x)^{5/2}} dx$.4534
3.1129	$\int \frac{(1-x)^{3/2}}{(1+x)^{5/2}} dx$.4538
3.1130	$\int \frac{\sqrt{1-x}}{(1+x)^{5/2}} dx$.4542
3.1131	$\int \frac{1}{\sqrt{1-x}(1+x)^{5/2}} dx$.4545
3.1132	$\int \frac{1}{(1-x)^{3/2}(1+x)^{5/2}} dx$.4548
3.1133	$\int \frac{1}{(1-x)^{5/2}(1+x)^{5/2}} dx$.4552
3.1134	$\int \frac{1}{(1-x)^{7/2}(1+x)^{5/2}} dx$.4555
3.1135	$\int \frac{1}{(1-x)^{9/2}(1+x)^{5/2}} dx$.4559
3.1136	$\int \frac{1}{(1-x)^{11/2}(1+x)^{5/2}} dx$.4563
3.1137	$\int (a+ax)^{5/2}(c-cx)^{5/2} dx$.4567
3.1138	$\int (a+ax)^{3/2}(c-cx)^{3/2} dx$.4571
3.1139	$\int \sqrt{a+ax} \sqrt{c-cx} dx$.4575
3.1140	$\int \frac{1}{\sqrt{a+ax} \sqrt{c-cx}} dx$.4579
3.1141	$\int \frac{1}{(a+ax)^{3/2}(c-cx)^{3/2}} dx$.4583
3.1142	$\int \frac{1}{(a+ax)^{5/2}(c-cx)^{5/2}} dx$.4586
3.1143	$\int \frac{1}{(a+ax)^{7/2}(c-cx)^{7/2}} dx$.4589
3.1144	$\int \frac{1}{(a+ax)^{9/2}(c-cx)^{9/2}} dx$.4593
3.1145	$\int (a+bx)^{5/2}(ac-bcx)^{5/2} dx$.4597
3.1146	$\int (a+bx)^{3/2}(ac-bcx)^{3/2} dx$.4601
3.1147	$\int \sqrt{a+bx} \sqrt{ac-bcx} dx$.4605

3.1148	$\int \frac{1}{\sqrt{a+bx} \sqrt{ac-bcx}} dx$.4609
3.1149	$\int \frac{1}{(a+bx)^{3/2}(ac-bcx)^{3/2}} dx$.4613
3.1150	$\int \frac{1}{(a+bx)^{5/2}(ac-bcx)^{5/2}} dx$.4616
3.1151	$\int \frac{1}{(a+bx)^{7/2}(ac-bcx)^{7/2}} dx$.4619
3.1152	$\int \frac{1}{(a+bx)^{9/2}(ac-bcx)^{9/2}} dx$.4623
3.1153	$\int (3-6x)^{5/2}(2+4x)^{5/2} dx$.4627
3.1154	$\int (3-6x)^{3/2}(2+4x)^{3/2} dx$.4631
3.1155	$\int \sqrt{3-6x} \sqrt{2+4x} dx$.4634
3.1156	$\int \frac{1}{\sqrt{3-6x} \sqrt{2+4x}} dx$.4638
3.1157	$\int \frac{1}{(3-6x)^{3/2}(2+4x)^{3/2}} dx$.4641
3.1158	$\int \frac{1}{(3-6x)^{5/2}(2+4x)^{5/2}} dx$.4644
3.1159	$\int \frac{1}{(3-6x)^{7/2}(2+4x)^{7/2}} dx$.4647
3.1160	$\int (3-x)^{3/2}(-2+x)^{3/2} dx$.4651
3.1161	$\int \sqrt{3-x} \sqrt{-2+x} dx$.4655
3.1162	$\int \frac{1}{\sqrt{3-x} \sqrt{-2+x}} dx$.4659
3.1163	$\int \frac{1}{(3-x)^{3/2}(-2+x)^{3/2}} dx$.4662
3.1164	$\int \frac{1}{(3-x)^{5/2}(-2+x)^{5/2}} dx$.4665
3.1165	$\int \frac{1}{(3-x)^{3/2}(3+x)^{3/2}} dx$.4669
3.1166	$\int \frac{1}{(3-bx)^{3/2}(3+bx)^{3/2}} dx$.4672
3.1167	$\int \frac{1}{(6-2x)^{3/2}(3+x)^{3/2}} dx$.4675
3.1168	$\int \frac{1}{(6-2bx)^{3/2}(3+bx)^{3/2}} dx$.4678
3.1169	$\int \frac{1}{\sqrt{a+bx} \sqrt{-ad+bdx}} dx$.4681
3.1170	$\int \frac{1}{\sqrt[4]{6-3ex} (2+ex)^{3/4}} dx$.4685
3.1171	$\int \frac{(a-iax)^{7/4}}{\sqrt[4]{a+iax}} dx$.4690
3.1172	$\int \frac{(a-iax)^{3/4}}{\sqrt[4]{a+iax}} dx$.4694
3.1173	$\int \frac{1}{\sqrt[4]{a-iax} \sqrt[4]{a+iax}} dx$.4698
3.1174	$\int \frac{1}{(a-iax)^{5/4} \sqrt[4]{a+iax}} dx$.4702
3.1175	$\int \frac{1}{(a-iax)^{9/4} \sqrt[4]{a+iax}} dx$.4706
3.1176	$\int \frac{1}{(a-iax)^{13/4} \sqrt[4]{a+iax}} dx$.4710

3.1177	$\int \frac{1}{(a-iax)^{17/4} \sqrt[4]{a+iax}} dx$.4714
3.1178	$\int \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} dx$.4718
3.1179	$\int \frac{1}{(a-iax)^{3/4} \sqrt[4]{a+iax}} dx$.4723
3.1180	$\int \frac{1}{(a-iax)^{7/4} \sqrt[4]{a+iax}} dx$.4728
3.1181	$\int \frac{1}{(a-iax)^{11/4} \sqrt[4]{a+iax}} dx$.4731
3.1182	$\int \frac{1}{(a-iax)^{15/4} \sqrt[4]{a+iax}} dx$.4734
3.1183	$\int \frac{1}{(a-iax)^{19/4} \sqrt[4]{a+iax}} dx$.4737
3.1184	$\int \frac{(a-iax)^{3/4}}{(a+iax)^{3/4}} dx$.4740
3.1185	$\int \frac{1}{\sqrt[4]{a-iax} (a+iax)^{3/4}} dx$.4745
3.1186	$\int \frac{1}{(a-iax)^{5/4} (a+iax)^{3/4}} dx$.4750
3.1187	$\int \frac{1}{(a-iax)^{9/4} (a+iax)^{3/4}} dx$.4753
3.1188	$\int \frac{1}{(a-iax)^{13/4} (a+iax)^{3/4}} dx$.4756
3.1189	$\int \frac{(a-iax)^{5/4}}{(a+iax)^{3/4}} dx$.4759
3.1190	$\int \frac{\sqrt[4]{a-iax}}{(a+iax)^{3/4}} dx$.4763
3.1191	$\int \frac{1}{(a-iax)^{3/4} (a+iax)^{3/4}} dx$.4767
3.1192	$\int \frac{1}{(a-iax)^{7/4} (a+iax)^{3/4}} dx$.4771
3.1193	$\int \frac{1}{(a-iax)^{11/4} (a+iax)^{3/4}} dx$.4775
3.1194	$\int \frac{(a-iax)^{7/4}}{(a+iax)^{7/4}} dx$.4779
3.1195	$\int \frac{(a-iax)^{3/4}}{(a+iax)^{7/4}} dx$.4785
3.1196	$\int \frac{1}{\sqrt[4]{a-iax} (a+iax)^{7/4}} dx$.4790
3.1197	$\int \frac{1}{(a-iax)^{5/4} (a+iax)^{7/4}} dx$.4793
3.1198	$\int \frac{1}{(a-iax)^{9/4} (a+iax)^{7/4}} dx$.4796
3.1199	$\int \frac{(a-iax)^{9/4}}{(a+iax)^{7/4}} dx$.4799
3.1200	$\int \frac{(a-iax)^{5/4}}{(a+iax)^{7/4}} dx$.4803
3.1201	$\int \frac{\sqrt[4]{a-iax}}{(a+iax)^{7/4}} dx$.4807
3.1202	$\int \frac{1}{(a-iax)^{3/4} (a+iax)^{7/4}} dx$.4811
3.1203	$\int \frac{1}{(a-iax)^{7/4} (a+iax)^{7/4}} dx$.4815

3.1204	$\int \frac{1}{(a-iax)^{11/4}(a+iax)^{7/4}} dx$.4819
3.1205	$\int \frac{1}{(a-iax)^{15/4}(a+iax)^{7/4}} dx$.4823
3.1206	$\int \frac{(a-iax)^{7/4}}{(a+iax)^{5/4}} dx$.4827
3.1207	$\int \frac{(a-iax)^{3/4}}{(a+iax)^{5/4}} dx$.4832
3.1208	$\int \frac{1}{\sqrt[4]{a-iax}(a+iax)^{5/4}} dx$.4836
3.1209	$\int \frac{1}{(a-iax)^{5/4}(a+iax)^{5/4}} dx$.4840
3.1210	$\int \frac{1}{(a-iax)^{9/4}(a+iax)^{5/4}} dx$.4844
3.1211	$\int \frac{1}{(a-iax)^{13/4}(a+iax)^{5/4}} dx$.4848
3.1212	$\int \frac{(a-iax)^{5/4}}{(a+iax)^{5/4}} dx$.4852
3.1213	$\int \frac{\sqrt[4]{a-iax}}{(a+iax)^{5/4}} dx$.4858
3.1214	$\int \frac{1}{(a-iax)^{3/4}(a+iax)^{5/4}} dx$.4863
3.1215	$\int \frac{1}{(a-iax)^{7/4}(a+iax)^{5/4}} dx$.4866
3.1216	$\int \frac{1}{(a-iax)^{11/4}(a+iax)^{5/4}} dx$.4869
3.1217	$\int \frac{(a-iax)^{7/4}}{(a+iax)^{9/4}} dx$.4872
3.1218	$\int \frac{(a-iax)^{3/4}}{(a+iax)^{9/4}} dx$.4876
3.1219	$\int \frac{1}{\sqrt[4]{a-iax}(a+iax)^{9/4}} dx$.4880
3.1220	$\int \frac{1}{(a-iax)^{5/4}(a+iax)^{9/4}} dx$.4884
3.1221	$\int \frac{1}{(a-iax)^{9/4}(a+iax)^{9/4}} dx$.4888
3.1222	$\int \frac{1}{(a-iax)^{13/4}(a+iax)^{9/4}} dx$.4892
3.1223	$\int \frac{1}{(a-iax)^{17/4}(a+iax)^{9/4}} dx$.4896
3.1224	$\int \frac{(a-iax)^{5/4}}{(a+iax)^{9/4}} dx$.4901
3.1225	$\int \frac{\sqrt[4]{a-iax}}{(a+iax)^{9/4}} dx$.4907
3.1226	$\int \frac{1}{(a-iax)^{3/4}(a+iax)^{9/4}} dx$.4910
3.1227	$\int \frac{1}{(a-iax)^{7/4}(a+iax)^{9/4}} dx$.4913
3.1228	$\int \frac{1}{(a-iax)^{11/4}(a+iax)^{9/4}} dx$.4916
3.1229	$\int (a+bx)^2(ac-bcx)^n dx$.4919
3.1230	$\int (a+bx)(ac-bcx)^n dx$.4923
3.1231	$\int \frac{(ac-bcx)^n}{a+bx} dx$.4926

3.1232	$\int \frac{(ac-bcx)^n}{(a+bx)^2} dx$4929
3.1233	$\int (a+ax)^m(c-cx)^m dx$4932
3.1234	$\int (a+bx)^m(ac-bcx)^m dx$4935
3.1235	$\int (3-6x)^m(2+4x)^m dx$4938
3.1236	$\int (a+bx)^4(c+dx) dx$4941
3.1237	$\int (a+bx)^3(c+dx) dx$4944
3.1238	$\int (a+bx)^2(c+dx) dx$4947
3.1239	$\int (a+bx)(c+dx) dx$4950
3.1240	$\int (c+dx) dx$4953
3.1241	$\int \frac{c+dx}{a+bx} dx$4956
3.1242	$\int \frac{c+dx}{(a+bx)^2} dx$4959
3.1243	$\int \frac{c+dx}{(a+bx)^3} dx$4962
3.1244	$\int \frac{c+dx}{(a+bx)^4} dx$4965
3.1245	$\int \frac{c+dx}{(a+bx)^5} dx$4968
3.1246	$\int (a+bx)^4(c+dx)^2 dx$4971
3.1247	$\int (a+bx)^3(c+dx)^2 dx$4974
3.1248	$\int (a+bx)^2(c+dx)^2 dx$4977
3.1249	$\int (a+bx)(c+dx)^2 dx$4980
3.1250	$\int (c+dx)^2 dx$4983
3.1251	$\int \frac{(c+dx)^2}{a+bx} dx$4986
3.1252	$\int \frac{(c+dx)^2}{(a+bx)^2} dx$4989
3.1253	$\int \frac{(c+dx)^2}{(a+bx)^3} dx$4992
3.1254	$\int \frac{(c+dx)^2}{(a+bx)^4} dx$4995
3.1255	$\int \frac{(c+dx)^2}{(a+bx)^5} dx$4998
3.1256	$\int \frac{(c+dx)^2}{(a+bx)^6} dx$5001
3.1257	$\int \frac{(c+dx)^2}{(a+bx)^7} dx$5004
3.1258	$\int (a+bx)^5(c+dx)^3 dx$5007
3.1259	$\int (a+bx)^4(c+dx)^3 dx$5011
3.1260	$\int (a+bx)^3(c+dx)^3 dx$5015
3.1261	$\int (a+bx)^2(c+dx)^3 dx$5018
3.1262	$\int (a+bx)(c+dx)^3 dx$5021
3.1263	$\int (c+dx)^3 dx$5024
3.1264	$\int \frac{(c+dx)^3}{a+bx} dx$5027

3.1265	$\int \frac{(c+dx)^3}{(a+bx)^2} dx$.5030
3.1266	$\int \frac{(c+dx)^3}{(a+bx)^3} dx$.5033
3.1267	$\int \frac{(c+dx)^3}{(a+bx)^4} dx$.5036
3.1268	$\int \frac{(c+dx)^3}{(a+bx)^5} dx$.5039
3.1269	$\int \frac{(c+dx)^3}{(a+bx)^6} dx$.5042
3.1270	$\int \frac{(c+dx)^3}{(a+bx)^7} dx$.5046
3.1271	$\int \frac{(c+dx)^3}{(a+bx)^8} dx$.5049
3.1272	$\int \frac{(c+dx)^3}{(a+bx)^9} dx$.5052
3.1273	$\int (a+bx)^9(c+dx)^7 dx$.5055
3.1274	$\int (a+bx)^8(c+dx)^7 dx$.5062
3.1275	$\int (a+bx)^7(c+dx)^7 dx$.5068
3.1276	$\int (a+bx)^6(c+dx)^7 dx$.5074
3.1277	$\int (a+bx)^5(c+dx)^7 dx$.5079
3.1278	$\int (a+bx)^4(c+dx)^7 dx$.5084
3.1279	$\int (a+bx)^3(c+dx)^7 dx$.5088
3.1280	$\int (a+bx)^2(c+dx)^7 dx$.5092
3.1281	$\int (a+bx)(c+dx)^7 dx$.5096
3.1282	$\int (c+dx)^7 dx$.5099
3.1283	$\int \frac{(c+dx)^7}{a+bx} dx$.5102
3.1284	$\int \frac{(c+dx)^7}{(a+bx)^2} dx$.5107
3.1285	$\int \frac{(c+dx)^7}{(a+bx)^3} dx$.5112
3.1286	$\int \frac{(c+dx)^7}{(a+bx)^4} dx$.5117
3.1287	$\int \frac{(c+dx)^7}{(a+bx)^5} dx$.5122
3.1288	$\int \frac{(c+dx)^7}{(a+bx)^6} dx$.5127
3.1289	$\int \frac{(c+dx)^7}{(a+bx)^7} dx$.5132
3.1290	$\int \frac{(c+dx)^7}{(a+bx)^8} dx$.5136
3.1291	$\int \frac{(c+dx)^7}{(a+bx)^9} dx$.5140
3.1292	$\int \frac{(c+dx)^7}{(a+bx)^{10}} dx$.5144
3.1293	$\int \frac{(c+dx)^7}{(a+bx)^{11}} dx$.5148
3.1294	$\int \frac{(c+dx)^7}{(a+bx)^{12}} dx$.5153

3.1295	$\int \frac{(c+dx)^7}{(a+bx)^{13}} dx$.5158
3.1296	$\int \frac{(c+dx)^7}{(a+bx)^{14}} dx$.5163
3.1297	$\int \frac{(c+dx)^7}{(a+bx)^{15}} dx$.5167
3.1298	$\int \frac{(c+dx)^7}{(a+bx)^{16}} dx$.5171
3.1299	$\int (a+bx)^{12}(c+dx)^{10} dx$.5175
3.1300	$\int (a+bx)^{11}(c+dx)^{10} dx$.5185
3.1301	$\int (a+bx)^{10}(c+dx)^{10} dx$.5195
3.1302	$\int (a+bx)^9(c+dx)^{10} dx$.5204
3.1303	$\int (a+bx)^8(c+dx)^{10} dx$.5212
3.1304	$\int (a+bx)^7(c+dx)^{10} dx$.5219
3.1305	$\int (a+bx)^6(c+dx)^{10} dx$.5226
3.1306	$\int (a+bx)^5(c+dx)^{10} dx$.5232
3.1307	$\int (a+bx)^4(c+dx)^{10} dx$.5238
3.1308	$\int (a+bx)^3(c+dx)^{10} dx$.5243
3.1309	$\int (a+bx)^2(c+dx)^{10} dx$.5248
3.1310	$\int (a+bx)(c+dx)^{10} dx$.5252
3.1311	$\int (c+dx)^{10} dx$.5256
3.1312	$\int \frac{(c+dx)^{10}}{a+bx} dx$.5259
3.1313	$\int \frac{(c+dx)^{10}}{(a+bx)^2} dx$.5267
3.1314	$\int \frac{(c+dx)^{10}}{(a+bx)^3} dx$.5275
3.1315	$\int \frac{(c+dx)^{10}}{(a+bx)^4} dx$.5283
3.1316	$\int \frac{(c+dx)^{10}}{(a+bx)^5} dx$.5290
3.1317	$\int \frac{(c+dx)^{10}}{(a+bx)^6} dx$.5296
3.1318	$\int \frac{(c+dx)^{10}}{(a+bx)^7} dx$.5302
3.1319	$\int \frac{(c+dx)^{10}}{(a+bx)^8} dx$.5308
3.1320	$\int \frac{(c+dx)^{10}}{(a+bx)^9} dx$.5314
3.1321	$\int \frac{(c+dx)^{10}}{(a+bx)^{10}} dx$.5320
3.1322	$\int \frac{(c+dx)^{10}}{(a+bx)^{11}} dx$.5326
3.1323	$\int \frac{(c+dx)^{10}}{(a+bx)^{12}} dx$.5332
3.1324	$\int \frac{(c+dx)^{10}}{(a+bx)^{13}} dx$.5337
3.1325	$\int \frac{(c+dx)^{10}}{(a+bx)^{14}} dx$.5342

3.1326	$\int \frac{(c+dx)^{10}}{(a+bx)^{15}} dx$.5348
3.1327	$\int \frac{(c+dx)^{10}}{(a+bx)^{16}} dx$.5354
3.1328	$\int \frac{(c+dx)^{10}}{(a+bx)^{17}} dx$.5360
3.1329	$\int \frac{(c+dx)^{10}}{(a+bx)^{18}} dx$.5366
3.1330	$\int \frac{(c+dx)^{10}}{(a+bx)^{19}} dx$.5373
3.1331	$\int \frac{(c+dx)^{10}}{(a+bx)^{20}} dx$.5380
3.1332	$\int \frac{(c+dx)^{10}}{(a+bx)^{21}} dx$.5386
3.1333	$\int \frac{(c+dx)^{10}}{(a+bx)^{22}} dx$.5392
3.1334	$\int \frac{(a+bx)^5}{c+dx} dx$.5398
3.1335	$\int \frac{(a+bx)^4}{c+dx} dx$.5402
3.1336	$\int \frac{(a+bx)^3}{c+dx} dx$.5405
3.1337	$\int \frac{(a+bx)^2}{c+dx} dx$.5408
3.1338	$\int \frac{a+bx}{c+dx} dx$.5411
3.1339	$\int \frac{1}{c+dx} dx$.5414
3.1340	$\int \frac{1}{(a+bx)(c+dx)} dx$.5417
3.1341	$\int \frac{1}{(a+bx)^2(c+dx)} dx$.5420
3.1342	$\int \frac{1}{(a+bx)^3(c+dx)} dx$.5423
3.1343	$\int \frac{(a+bx)^5}{(c+dx)^2} dx$.5427
3.1344	$\int \frac{(a+bx)^4}{(c+dx)^2} dx$.5431
3.1345	$\int \frac{(a+bx)^3}{(c+dx)^2} dx$.5435
3.1346	$\int \frac{(a+bx)^2}{(c+dx)^2} dx$.5438
3.1347	$\int \frac{a+bx}{(c+dx)^2} dx$.5441
3.1348	$\int \frac{1}{(c+dx)^2} dx$.5444
3.1349	$\int \frac{1}{(a+bx)(c+dx)^2} dx$.5447
3.1350	$\int \frac{1}{(a+bx)^2(c+dx)^2} dx$.5450
3.1351	$\int \frac{1}{(a+bx)^3(c+dx)^2} dx$.5453
3.1352	$\int \frac{(a+bx)^6}{(c+dx)^3} dx$.5457
3.1353	$\int \frac{(a+bx)^5}{(c+dx)^3} dx$.5461

3.1354	$\int \frac{(a+bx)^4}{(c+dx)^3} dx$.5465
3.1355	$\int \frac{(a+bx)^3}{(c+dx)^3} dx$.5469
3.1356	$\int \frac{(a+bx)^2}{(c+dx)^3} dx$.5472
3.1357	$\int \frac{a+bx}{(c+dx)^3} dx$.5475
3.1358	$\int \frac{1}{(c+dx)^3} dx$.5478
3.1359	$\int \frac{1}{(a+bx)(c+dx)^3} dx$.5481
3.1360	$\int \frac{1}{(a+bx)^2(c+dx)^3} dx$.5485
3.1361	$\int \frac{1}{(a+bx)^3(c+dx)^3} dx$.5489
3.1362	$\int \frac{(a+bx)^9}{(c+dx)^8} dx$.5494
3.1363	$\int \frac{(a+bx)^8}{(c+dx)^8} dx$.5499
3.1364	$\int \frac{(a+bx)^7}{(c+dx)^8} dx$.5504
3.1365	$\int \frac{(a+bx)^6}{(c+dx)^8} dx$.5508
3.1366	$\int \frac{(a+bx)^5}{(c+dx)^8} dx$.5512
3.1367	$\int \frac{(a+bx)^4}{(c+dx)^8} dx$.5516
3.1368	$\int \frac{(a+bx)^3}{(c+dx)^8} dx$.5520
3.1369	$\int \frac{(a+bx)^2}{(c+dx)^8} dx$.5523
3.1370	$\int \frac{a+bx}{(c+dx)^8} dx$.5526
3.1371	$\int \frac{1}{(c+dx)^8} dx$.5529
3.1372	$\int \frac{1}{(a+bx)(c+dx)^8} dx$.5532
3.1373	$\int \frac{1}{(a+bx)^2(c+dx)^8} dx$.5538
3.1374	$\int \frac{1}{(a+bx)^3(c+dx)^8} dx$.5545
3.1375	$\int (a+bx)^5 \sqrt{c+dx} dx$.5554
3.1376	$\int (a+bx)^4 \sqrt{c+dx} dx$.5558
3.1377	$\int (a+bx)^3 \sqrt{c+dx} dx$.5562
3.1378	$\int (a+bx)^2 \sqrt{c+dx} dx$.5565
3.1379	$\int (a+bx) \sqrt{c+dx} dx$.5568
3.1380	$\int \sqrt{c+dx} dx$.5571
3.1381	$\int \frac{\sqrt{c+dx}}{a+bx} dx$.5574
3.1382	$\int \frac{\sqrt{c+dx}}{(a+bx)^2} dx$.5578

3.1383	$\int \frac{\sqrt{c+dx}}{(a+bx)^3} dx$.5582
3.1384	$\int \frac{\sqrt{c+dx}}{(a+bx)^4} dx$.5586
3.1385	$\int \frac{\sqrt{c+dx}}{(a+bx)^5} dx$.5591
3.1386	$\int \frac{\sqrt{c+dx}}{(a+bx)^6} dx$.5596
3.1387	$\int (a+bx)^5 (c+dx)^{3/2} dx$.5601
3.1388	$\int (a+bx)^4 (c+dx)^{3/2} dx$.5606
3.1389	$\int (a+bx)^3 (c+dx)^{3/2} dx$.5610
3.1390	$\int (a+bx)^2 (c+dx)^{3/2} dx$.5614
3.1391	$\int (a+bx)(c+dx)^{3/2} dx$.5618
3.1392	$\int (c+dx)^{3/2} dx$.5621
3.1393	$\int \frac{(c+dx)^{3/2}}{a+bx} dx$.5624
3.1394	$\int \frac{(c+dx)^{3/2}}{(a+bx)^2} dx$.5628
3.1395	$\int \frac{(c+dx)^{3/2}}{(a+bx)^3} dx$.5632
3.1396	$\int \frac{(c+dx)^{3/2}}{(a+bx)^4} dx$.5636
3.1397	$\int \frac{(c+dx)^{3/2}}{(a+bx)^5} dx$.5640
3.1398	$\int \frac{(c+dx)^{3/2}}{(a+bx)^6} dx$.5645
3.1399	$\int (a+bx)^5 (c+dx)^{5/2} dx$.5650
3.1400	$\int (a+bx)^4 (c+dx)^{5/2} dx$.5655
3.1401	$\int (a+bx)^3 (c+dx)^{5/2} dx$.5660
3.1402	$\int (a+bx)^2 (c+dx)^{5/2} dx$.5664
3.1403	$\int (a+bx)(c+dx)^{5/2} dx$.5668
3.1404	$\int (c+dx)^{5/2} dx$.5671
3.1405	$\int \frac{(c+dx)^{5/2}}{a+bx} dx$.5674
3.1406	$\int \frac{(c+dx)^{5/2}}{(a+bx)^2} dx$.5678
3.1407	$\int \frac{(c+dx)^{5/2}}{(a+bx)^3} dx$.5682
3.1408	$\int \frac{(c+dx)^{5/2}}{(a+bx)^4} dx$.5686
3.1409	$\int \frac{(c+dx)^{5/2}}{(a+bx)^5} dx$.5690
3.1410	$\int \frac{(c+dx)^{5/2}}{(a+bx)^6} dx$.5695
3.1411	$\int \frac{\sqrt{-1+x}}{(1+x)^2} dx$.5700
3.1412	$\int \frac{\sqrt{-1+x}}{(1+x)^3} dx$.5704

3.1413	$\int \frac{(a+bx)^5}{\sqrt{c+dx}} dx$.5708
3.1414	$\int \frac{(a+bx)^4}{\sqrt{c+dx}} dx$.5712
3.1415	$\int \frac{(a+bx)^3}{\sqrt{c+dx}} dx$.5716
3.1416	$\int \frac{(a+bx)^2}{\sqrt{c+dx}} dx$.5720
3.1417	$\int \frac{a+bx}{\sqrt{c+dx}} dx$.5724
3.1418	$\int \frac{1}{\sqrt{c+dx}} dx$.5727
3.1419	$\int \frac{1}{(a+bx)\sqrt{c+dx}} dx$.5730
3.1420	$\int \frac{1}{(a+bx)^2\sqrt{c+dx}} dx$.5734
3.1421	$\int \frac{1}{(a+bx)^3\sqrt{c+dx}} dx$.5738
3.1422	$\int \frac{1}{(a+bx)^4\sqrt{c+dx}} dx$.5742
3.1423	$\int \frac{1}{(a+bx)^5\sqrt{c+dx}} dx$.5746
3.1424	$\int \frac{(a+bx)^5}{(c+dx)^{3/2}} dx$.5751
3.1425	$\int \frac{(a+bx)^4}{(c+dx)^{3/2}} dx$.5755
3.1426	$\int \frac{(a+bx)^3}{(c+dx)^{3/2}} dx$.5759
3.1427	$\int \frac{(a+bx)^2}{(c+dx)^{3/2}} dx$.5762
3.1428	$\int \frac{a+bx}{(c+dx)^{3/2}} dx$.5765
3.1429	$\int \frac{1}{(c+dx)^{3/2}} dx$.5768
3.1430	$\int \frac{1}{(a+bx)(c+dx)^{3/2}} dx$.5771
3.1431	$\int \frac{1}{(a+bx)^2(c+dx)^{3/2}} dx$.5775
3.1432	$\int \frac{1}{(a+bx)^3(c+dx)^{3/2}} dx$.5779
3.1433	$\int \frac{1}{(a+bx)^4(c+dx)^{3/2}} dx$.5783
3.1434	$\int \frac{(a+bx)^5}{(c+dx)^{5/2}} dx$.5788
3.1435	$\int \frac{(a+bx)^4}{(c+dx)^{5/2}} dx$.5792
3.1436	$\int \frac{(a+bx)^3}{(c+dx)^{5/2}} dx$.5796
3.1437	$\int \frac{(a+bx)^2}{(c+dx)^{5/2}} dx$.5800
3.1438	$\int \frac{a+bx}{(c+dx)^{5/2}} dx$.5803
3.1439	$\int \frac{1}{(c+dx)^{5/2}} dx$.5806

3.1440	$\int \frac{1}{(a+bx)(c+dx)^{5/2}} dx$5809
3.1441	$\int \frac{1}{(a+bx)^2(c+dx)^{5/2}} dx$5813
3.1442	$\int \frac{1}{(a+bx)^3(c+dx)^{5/2}} dx$5817
3.1443	$\int \frac{1}{(a+bx)^4(c+dx)^{5/2}} dx$5822
3.1444	$\int (a+bx)^5(ac+bcx)^{3/2} dx$5827
3.1445	$\int (a+bx)^5 \sqrt{ac+bcx} dx$5831
3.1446	$\int \frac{(a+bx)^5}{\sqrt{ac+bcx}} dx$5834
3.1447	$\int \frac{(a+bx)^5}{(ac+bcx)^{3/2}} dx$5838
3.1448	$\int \frac{(a+bx)^5}{(ac+bcx)^{5/2}} dx$5841
3.1449	$\int \frac{(a+bx)^5}{(ac+bcx)^{7/2}} dx$5844
3.1450	$\int \frac{(a+bx)^5}{(ac+bcx)^{9/2}} dx$5847
3.1451	$\int \frac{(a+bx)^5}{(ac+bcx)^{11/2}} dx$5850
3.1452	$\int \frac{(a+bx)^5}{(ac+bcx)^{13/2}} dx$5853
3.1453	$\int \frac{1}{(-2+x)\sqrt{2+x}} dx$5856
3.1454	$\int \frac{1}{(2+3x)\sqrt{1+5x}} dx$5859
3.1455	$\int \frac{\sqrt[3]{1-x}}{1+x} dx$5862
3.1456	$\int \sqrt[3]{3-2x} (7+x) dx$5866
3.1457	$\int \sqrt[3]{1-x} (1+x)^2 dx$5869
3.1458	$\int \frac{1}{(a+bx)\sqrt[3]{c+dx}} dx$5872
3.1459	$\int \frac{1}{(a+bx)(c+dx)^{2/3}} dx$5877
3.1460	$\int (a+bx)^{7/2} \sqrt{c+dx} dx$5882
3.1461	$\int (a+bx)^{5/2} \sqrt{c+dx} dx$5887
3.1462	$\int (a+bx)^{3/2} \sqrt{c+dx} dx$5892
3.1463	$\int \sqrt{a+bx} \sqrt{c+dx} dx$5897
3.1464	$\int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx$5901
3.1465	$\int \frac{\sqrt{c+dx}}{(a+bx)^{3/2}} dx$5905
3.1466	$\int \frac{\sqrt{c+dx}}{(a+bx)^{5/2}} dx$5909
3.1467	$\int \frac{\sqrt{c+dx}}{(a+bx)^{7/2}} dx$5912
3.1468	$\int \frac{\sqrt{c+dx}}{(a+bx)^{9/2}} dx$5916

3.1469	$\int \frac{\sqrt{c+dx}}{(a+bx)^{11/2}} dx$.5920
3.1470	$\int \frac{\sqrt{c+dx}}{(a+bx)^{13/2}} dx$.5924
3.1471	$\int (a+bx)^{5/2}(c+dx)^{3/2} dx$.5929
3.1472	$\int (a+bx)^{3/2}(c+dx)^{3/2} dx$.5935
3.1473	$\int \sqrt{a+bx}(c+dx)^{3/2} dx$.5940
3.1474	$\int \frac{(c+dx)^{3/2}}{\sqrt{a+bx}} dx$.5945
3.1475	$\int \frac{(c+dx)^{3/2}}{(a+bx)^{3/2}} dx$.5949
3.1476	$\int \frac{(c+dx)^{3/2}}{(a+bx)^{5/2}} dx$.5953
3.1477	$\int \frac{(c+dx)^{3/2}}{(a+bx)^{7/2}} dx$.5957
3.1478	$\int \frac{(c+dx)^{3/2}}{(a+bx)^{9/2}} dx$.5960
3.1479	$\int \frac{(c+dx)^{3/2}}{(a+bx)^{11/2}} dx$.5964
3.1480	$\int \frac{(c+dx)^{3/2}}{(a+bx)^{13/2}} dx$.5968
3.1481	$\int (a+bx)^{5/2}(c+dx)^{5/2} dx$.5973
3.1482	$\int (a+bx)^{3/2}(c+dx)^{5/2} dx$.5980
3.1483	$\int \sqrt{a+bx}(c+dx)^{5/2} dx$.5986
3.1484	$\int \frac{(c+dx)^{5/2}}{\sqrt{a+bx}} dx$.5991
3.1485	$\int \frac{(c+dx)^{5/2}}{(a+bx)^{3/2}} dx$.5996
3.1486	$\int \frac{(c+dx)^{5/2}}{(a+bx)^{5/2}} dx$.6001
3.1487	$\int \frac{(c+dx)^{5/2}}{(a+bx)^{7/2}} dx$.6006
3.1488	$\int \frac{(c+dx)^{5/2}}{(a+bx)^{9/2}} dx$.6011
3.1489	$\int \frac{(c+dx)^{5/2}}{(a+bx)^{11/2}} dx$.6014
3.1490	$\int \frac{(c+dx)^{5/2}}{(a+bx)^{13/2}} dx$.6019
3.1491	$\int \frac{(c+dx)^{5/2}}{(a+bx)^{15/2}} dx$.6024
3.1492	$\int \frac{(a+bx)^{7/2}}{\sqrt{c+dx}} dx$.6030
3.1493	$\int \frac{(a+bx)^{5/2}}{\sqrt{c+dx}} dx$.6035
3.1494	$\int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx$.6040
3.1495	$\int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx$.6044
3.1496	$\int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx$.6048

3.1497	$\int \frac{1}{(a+bx)^{3/2} \sqrt{c+dx}} dx$6052
3.1498	$\int \frac{1}{(a+bx)^{5/2} \sqrt{c+dx}} dx$6055
3.1499	$\int \frac{1}{(a+bx)^{7/2} \sqrt{c+dx}} dx$6059
3.1500	$\int \frac{1}{(a+bx)^{9/2} \sqrt{c+dx}} dx$6063
3.1501	$\int \frac{1}{(a+bx)^{11/2} \sqrt{c+dx}} dx$6067
3.1502	$\int \frac{(a+bx)^{7/2}}{(c+dx)^{3/2}} dx$6072
3.1503	$\int \frac{(a+bx)^{5/2}}{(c+dx)^{3/2}} dx$6077
3.1504	$\int \frac{(a+bx)^{3/2}}{(c+dx)^{3/2}} dx$6082
3.1505	$\int \frac{\sqrt{a+bx}}{(c+dx)^{3/2}} dx$6086
3.1506	$\int \frac{1}{\sqrt{a+bx} (c+dx)^{3/2}} dx$6090
3.1507	$\int \frac{1}{(a+bx)^{3/2} (c+dx)^{3/2}} dx$6093
3.1508	$\int \frac{1}{(a+bx)^{5/2} (c+dx)^{3/2}} dx$6097
3.1509	$\int \frac{1}{(a+bx)^{7/2} (c+dx)^{3/2}} dx$6101
3.1510	$\int \frac{1}{(a+bx)^{9/2} (c+dx)^{3/2}} dx$6105
3.1511	$\int \frac{1}{(a+bx)^{11/2} (c+dx)^{3/2}} dx$6110
3.1512	$\int \frac{(a+bx)^{9/2}}{(c+dx)^{5/2}} dx$6116
3.1513	$\int \frac{(a+bx)^{7/2}}{(c+dx)^{5/2}} dx$6122
3.1514	$\int \frac{(a+bx)^{5/2}}{(c+dx)^{5/2}} dx$6127
3.1515	$\int \frac{(a+bx)^{3/2}}{(c+dx)^{5/2}} dx$6132
3.1516	$\int \frac{\sqrt{a+bx}}{(c+dx)^{5/2}} dx$6136
3.1517	$\int \frac{1}{\sqrt{a+bx} (c+dx)^{5/2}} dx$6139
3.1518	$\int \frac{1}{(a+bx)^{3/2} (c+dx)^{5/2}} dx$6143
3.1519	$\int \frac{1}{(a+bx)^{5/2} (c+dx)^{5/2}} dx$6147
3.1520	$\int \frac{1}{(a+bx)^{7/2} (c+dx)^{5/2}} dx$6151
3.1521	$\int \frac{1}{(a+bx)^{9/2} (c+dx)^{5/2}} dx$6156
3.1522	$\int \frac{1}{\sqrt{a+bx} \sqrt{4+a+bx}} dx$6162
3.1523	$\int \frac{1}{\sqrt{2+bx} \sqrt{6+bx}} dx$6165

3.1524	$\int \frac{1}{\sqrt{1+bx} \sqrt{5+bx}} dx$.6168
3.1525	$\int \frac{1}{\sqrt{bx} \sqrt{4+bx}} dx$.6171
3.1526	$\int \frac{1}{\sqrt{-1+bx} \sqrt{3+bx}} dx$.6174
3.1527	$\int \frac{1}{\sqrt{-2+bx} \sqrt{2+bx}} dx$.6177
3.1528	$\int \frac{1}{\sqrt{-3+bx} \sqrt{1+bx}} dx$.6180
3.1529	$\int \frac{1}{\sqrt{2+bx} \sqrt{3+bx}} dx$.6183
3.1530	$\int \frac{1}{2+bx} dx$.6186
3.1531	$\int \frac{1}{\sqrt{1+bx} \sqrt{2+bx}} dx$.6189
3.1532	$\int \frac{1}{\sqrt{bx} \sqrt{2+bx}} dx$.6192
3.1533	$\int \frac{1}{\sqrt{-1+bx} \sqrt{2+bx}} dx$.6195
3.1534	$\int \frac{1}{\sqrt{-2+bx} \sqrt{2+bx}} dx$.6198
3.1535	$\int \frac{1}{\sqrt{-3+bx} \sqrt{2+bx}} dx$.6201
3.1536	$\int \frac{1}{\sqrt{3-bx} \sqrt{2+bx}} dx$.6204
3.1537	$\int \frac{1}{\sqrt{2-bx} \sqrt{2+bx}} dx$.6207
3.1538	$\int \frac{1}{\sqrt{1-bx} \sqrt{2+bx}} dx$.6210
3.1539	$\int \frac{1}{\sqrt{-bx} \sqrt{2+bx}} dx$.6213
3.1540	$\int \frac{1}{\sqrt{-1-bx} \sqrt{2+bx}} dx$.6216
3.1541	$\int \frac{1}{\sqrt{-2-bx} \sqrt{2+bx}} dx$.6219
3.1542	$\int \frac{1}{\sqrt{-3-bx} \sqrt{2+bx}} dx$.6222
3.1543	$\int \frac{1}{\sqrt{2-bx} \sqrt{3-bx}} dx$.6225
3.1544	$\int \frac{1}{2-bx} dx$.6228
3.1545	$\int \frac{1}{\sqrt{1-bx} \sqrt{2-bx}} dx$.6231
3.1546	$\int \frac{1}{\sqrt{-bx} \sqrt{2-bx}} dx$.6234
3.1547	$\int \frac{1}{\sqrt{-1-bx} \sqrt{2-bx}} dx$.6237
3.1548	$\int \frac{1}{\sqrt{-2-bx} \sqrt{2-bx}} dx$.6240
3.1549	$\int \frac{1}{\sqrt{-3-bx} \sqrt{2-bx}} dx$.6243
3.1550	$\int \frac{1}{\sqrt{-4+bx} \sqrt{4+bx}} dx$.6246
3.1551	$\int \frac{1}{\sqrt{\frac{-b+bc}{d}+bx} \sqrt{c+dx}} dx$.6249

3.1552	$\int \frac{1}{\sqrt{x} \sqrt{-3+2x}} dx$.6253
3.1553	$\int \frac{1}{\sqrt{-3+2x} \sqrt{2+3x}} dx$.6256
3.1554	$\int \frac{1}{\sqrt{\frac{b-bc}{d}+bx} \sqrt{c-dx}} dx$.6259
3.1555	$\int \frac{1}{\sqrt{4-x} \sqrt{x}} dx$.6263
3.1556	$\int \frac{1}{\sqrt{3-2x} \sqrt{x}} dx$.6266
3.1557	$\int \frac{1}{\sqrt{3-2x} \sqrt{3+5x}} dx$.6269
3.1558	$\int \frac{1}{\sqrt{a-bx} \sqrt{c+dx}} dx$.6272
3.1559	$\int (a+bx)^{3/2} \sqrt[3]{c+dx} dx$.6276
3.1560	$\int \sqrt{a+bx} \sqrt[3]{c+dx} dx$.6280
3.1561	$\int \frac{\sqrt[3]{c+dx}}{\sqrt{a+bx}} dx$.6284
3.1562	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{3/2}} dx$.6288
3.1563	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{5/2}} dx$.6292
3.1564	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{7/2}} dx$.6297
3.1565	$\int \frac{(a+bx)^{3/2}}{\sqrt[3]{c+dx}} dx$.6302
3.1566	$\int \frac{\sqrt{a+bx}}{\sqrt[3]{c+dx}} dx$.6307
3.1567	$\int \frac{1}{\sqrt{a+bx} \sqrt[3]{c+dx}} dx$.6312
3.1568	$\int \frac{1}{(a+bx)^{3/2} \sqrt[3]{c+dx}} dx$.6317
3.1569	$\int \frac{1}{(a+bx)^{5/2} \sqrt[3]{c+dx}} dx$.6322
3.1570	$\int \frac{(a+bx)^{3/2}}{(c+dx)^{2/3}} dx$.6327
3.1571	$\int \frac{\sqrt{a+bx}}{(c+dx)^{2/3}} dx$.6332
3.1572	$\int \frac{1}{\sqrt{a+bx} (c+dx)^{2/3}} dx$.6336
3.1573	$\int \frac{1}{(a+bx)^{3/2} (c+dx)^{2/3}} dx$.6340
3.1574	$\int \frac{1}{(a+bx)^{5/2} (c+dx)^{2/3}} dx$.6344
3.1575	$\int (a+bx)^{2/3} \sqrt[3]{c+dx} dx$.6349
3.1576	$\int \frac{\sqrt[3]{c+dx}}{\sqrt[3]{a+bx}} dx$.6353
3.1577	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{4/3}} dx$.6357

3.1578	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{7/3}} dx$.6361
3.1579	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{10/3}} dx$.6364
3.1580	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{13/3}} dx$.6368
3.1581	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{16/3}} dx$.6372
3.1582	$\int (a+bx)^{4/3} \sqrt[3]{c+dx} dx$.6376
3.1583	$\int \sqrt[3]{a+bx} \sqrt[3]{c+dx} dx$.6381
3.1584	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{2/3}} dx$.6385
3.1585	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{5/3}} dx$.6390
3.1586	$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{8/3}} dx$.6395
3.1587	$\int \frac{(a+bx)^{4/3}}{\sqrt[3]{c+dx}} dx$.6400
3.1588	$\int \frac{\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} dx$.6404
3.1589	$\int \frac{1}{(a+bx)^{2/3} \sqrt[3]{c+dx}} dx$.6408
3.1590	$\int \frac{1}{(a+bx)^{5/3} \sqrt[3]{c+dx}} dx$.6412
3.1591	$\int \frac{1}{(a+bx)^{8/3} \sqrt[3]{c+dx}} dx$.6415
3.1592	$\int \frac{1}{(a+bx)^{11/3} \sqrt[3]{c+dx}} dx$.6418
3.1593	$\int \frac{1}{(a+bx)^{14/3} \sqrt[3]{c+dx}} dx$.6422
3.1594	$\int \frac{(a+bx)^{8/3}}{\sqrt[3]{c+dx}} dx$.6426
3.1595	$\int \frac{(a+bx)^{5/3}}{\sqrt[3]{c+dx}} dx$.6432
3.1596	$\int \frac{(a+bx)^{2/3}}{\sqrt[3]{c+dx}} dx$.6438
3.1597	$\int \frac{1}{\sqrt[3]{a+bx} \sqrt[3]{c+dx}} dx$.6444
3.1598	$\int \frac{1}{(a+bx)^{4/3} \sqrt[3]{c+dx}} dx$.6450
3.1599	$\int \frac{1}{(a+bx)^{7/3} \sqrt[3]{c+dx}} dx$.6456
3.1600	$\int \frac{1}{(a+bx)^{10/3} \sqrt[3]{c+dx}} dx$.6462
3.1601	$\int \frac{(a+bx)^{5/3}}{(c+dx)^{2/3}} dx$.6468
3.1602	$\int \frac{(a+bx)^{2/3}}{(c+dx)^{2/3}} dx$.6472
3.1603	$\int \frac{1}{\sqrt[3]{a+bx} (c+dx)^{2/3}} dx$.6476

3.1604	$\int \frac{1}{(a+bx)^{4/3}(c+dx)^{2/3}} dx$.6480
3.1605	$\int \frac{1}{(a+bx)^{7/3}(c+dx)^{2/3}} dx$.6483
3.1606	$\int \frac{1}{(a+bx)^{10/3}(c+dx)^{2/3}} dx$.6486
3.1607	$\int \frac{1}{(a+bx)^{13/3}(c+dx)^{2/3}} dx$.6490
3.1608	$\int \frac{(a+bx)^{7/3}}{(c+dx)^{2/3}} dx$.6494
3.1609	$\int \frac{(a+bx)^{4/3}}{(c+dx)^{2/3}} dx$.6499
3.1610	$\int \frac{\sqrt[3]{a+bx}}{(c+dx)^{2/3}} dx$.6504
3.1611	$\int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx$.6508
3.1612	$\int \frac{1}{(a+bx)^{5/3}(c+dx)^{2/3}} dx$.6512
3.1613	$\int \frac{1}{(a+bx)^{8/3}(c+dx)^{2/3}} dx$.6517
3.1614	$\int \frac{1}{(a+bx)^{11/3}(c+dx)^{2/3}} dx$.6522
3.1615	$\int \frac{(a+bx)^{7/3}}{(c+dx)^{4/3}} dx$.6527
3.1616	$\int \frac{(a+bx)^{4/3}}{(c+dx)^{4/3}} dx$.6531
3.1617	$\int \frac{\sqrt[3]{a+bx}}{(c+dx)^{4/3}} dx$.6535
3.1618	$\int \frac{1}{(a+bx)^{2/3}(c+dx)^{4/3}} dx$.6539
3.1619	$\int \frac{1}{(a+bx)^{5/3}(c+dx)^{4/3}} dx$.6542
3.1620	$\int \frac{1}{(a+bx)^{8/3}(c+dx)^{4/3}} dx$.6545
3.1621	$\int \frac{1}{(a+bx)^{11/3}(c+dx)^{4/3}} dx$.6548
3.1622	$\int \frac{(a+bx)^{8/3}}{(c+dx)^{4/3}} dx$.6552
3.1623	$\int \frac{(a+bx)^{5/3}}{(c+dx)^{4/3}} dx$.6558
3.1624	$\int \frac{(a+bx)^{2/3}}{(c+dx)^{4/3}} dx$.6564
3.1625	$\int \frac{1}{\sqrt[3]{a+bx}(c+dx)^{4/3}} dx$.6570
3.1626	$\int \frac{1}{(a+bx)^{4/3}(c+dx)^{4/3}} dx$.6576
3.1627	$\int \frac{1}{(a+bx)^{7/3}(c+dx)^{4/3}} dx$.6582
3.1628	$\int \frac{\sqrt[3]{-1+x}}{\sqrt[3]{1+x}} dx$.6588
3.1629	$\int (a+bx)^{3/2} \sqrt[4]{c+dx} dx$.6592
3.1630	$\int \sqrt{a+bx} \sqrt[4]{c+dx} dx$.6596
3.1631	$\int \frac{\sqrt[4]{c+dx}}{\sqrt{a+bx}} dx$.6600

3.1632	$\int \frac{\sqrt[4]{c+dx}}{(a+bx)^{3/2}} dx$6604
3.1633	$\int \frac{\sqrt[4]{c+dx}}{(a+bx)^{5/2}} dx$6608
3.1634	$\int \frac{\sqrt[4]{c+dx}}{(a+bx)^{7/2}} dx$6613
3.1635	$\int (a+bx)^{3/2}(c+dx)^{3/4} dx$6618
3.1636	$\int \sqrt{a+bx}(c+dx)^{3/4} dx$6623
3.1637	$\int \frac{(c+dx)^{3/4}}{\sqrt{a+bx}} dx$6628
3.1638	$\int \frac{(c+dx)^{3/4}}{(a+bx)^{3/2}} dx$6633
3.1639	$\int \frac{(c+dx)^{3/4}}{(a+bx)^{5/2}} dx$6638
3.1640	$\int \frac{(c+dx)^{3/4}}{(a+bx)^{7/2}} dx$6643
3.1641	$\int (a+bx)^{3/2}(c+dx)^{5/4} dx$6649
3.1642	$\int \sqrt{a+bx}(c+dx)^{5/4} dx$6653
3.1643	$\int \frac{(c+dx)^{5/4}}{\sqrt{a+bx}} dx$6657
3.1644	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{3/2}} dx$6661
3.1645	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{5/2}} dx$6666
3.1646	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{7/2}} dx$6670
3.1647	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{9/2}} dx$6675
3.1648	$\int \frac{(a+bx)^{5/2}}{\sqrt[4]{c+dx}} dx$6680
3.1649	$\int \frac{(a+bx)^{3/2}}{\sqrt[4]{c+dx}} dx$6685
3.1650	$\int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx$6690
3.1651	$\int \frac{1}{\sqrt{a+bx}\sqrt[4]{c+dx}} dx$6695
3.1652	$\int \frac{1}{(a+bx)^{3/2}\sqrt[4]{c+dx}} dx$6700
3.1653	$\int \frac{1}{(a+bx)^{5/2}\sqrt[4]{c+dx}} dx$6705
3.1654	$\int \frac{(a+bx)^{3/2}}{(c+dx)^{3/4}} dx$6710
3.1655	$\int \frac{\sqrt{a+bx}}{(c+dx)^{3/4}} dx$6714
3.1656	$\int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx$6718
3.1657	$\int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/4}} dx$6722
3.1658	$\int \frac{1}{(a+bx)^{5/2}(c+dx)^{3/4}} dx$6726

3.1659	$\int \frac{(a+bx)^{5/2}}{(c+dx)^{5/4}} dx$.6730
3.1660	$\int \frac{(a+bx)^{3/2}}{(c+dx)^{5/4}} dx$.6736
3.1661	$\int \frac{\sqrt{a+bx}}{(c+dx)^{5/4}} dx$.6741
3.1662	$\int \frac{1}{\sqrt{a+bx}(c+dx)^{5/4}} dx$.6746
3.1663	$\int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/4}} dx$.6751
3.1664	$\int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/4}} dx$.6756
3.1665	$\int \frac{(a+bx)^{7/2}}{(c+dx)^{7/4}} dx$.6761
3.1666	$\int \frac{(a+bx)^{3/2}}{(c+dx)^{7/4}} dx$.6766
3.1667	$\int \frac{\sqrt{a+bx}}{(c+dx)^{7/4}} dx$.6771
3.1668	$\int \frac{1}{\sqrt{a+bx}(c+dx)^{7/4}} dx$.6775
3.1669	$\int \frac{1}{(a+bx)^{3/2}(c+dx)^{7/4}} dx$.6779
3.1670	$\int \frac{1}{(a+bx)^{5/2}(c+dx)^{7/4}} dx$.6783
3.1671	$\int \frac{(a+bx)^{7/2}}{(c+dx)^{9/4}} dx$.6787
3.1672	$\int \frac{(a+bx)^{5/2}}{(c+dx)^{9/4}} dx$.6793
3.1673	$\int \frac{(a+bx)^{3/2}}{(c+dx)^{9/4}} dx$.6798
3.1674	$\int \frac{\sqrt{a+bx}}{(c+dx)^{9/4}} dx$.6803
3.1675	$\int \frac{1}{\sqrt{a+bx}(c+dx)^{9/4}} dx$.6808
3.1676	$\int \frac{1}{(a+bx)^{3/2}(c+dx)^{9/4}} dx$.6813
3.1677	$\int \frac{1}{(a+bx)^{5/2}(c+dx)^{9/4}} dx$.6818
3.1678	$\int (a+bx)^{3/4}(c+dx)^{5/4} dx$.6823
3.1679	$\int \frac{(c+dx)^{5/4}}{\sqrt[4]{a+bx}} dx$.6829
3.1680	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{5/4}} dx$.6834
3.1681	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{9/4}} dx$.6839
3.1682	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{13/4}} dx$.6844
3.1683	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{17/4}} dx$.6847
3.1684	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{21/4}} dx$.6851
3.1685	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{25/4}} dx$.6855

3.1686	$\int (a + bx)^{5/4}(c + dx)^{5/4} dx$.6859
3.1687	$\int \sqrt[4]{a + bx} (c + dx)^{5/4} dx$.6864
3.1688	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{3/4}} dx$.6868
3.1689	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{7/4}} dx$.6873
3.1690	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{11/4}} dx$.6878
3.1691	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{15/4}} dx$.6883
3.1692	$\int \frac{(c+dx)^{5/4}}{(a+bx)^{19/4}} dx$.6888
3.1693	$\int \frac{(a+bx)^{5/4}}{\sqrt[4]{c+dx}} dx$.6893
3.1694	$\int \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} dx$.6898
3.1695	$\int \frac{1}{(a+bx)^{3/4} \sqrt[4]{c+dx}} dx$.6903
3.1696	$\int \frac{1}{(a+bx)^{7/4} \sqrt[4]{c+dx}} dx$.6907
3.1697	$\int \frac{1}{(a+bx)^{11/4} \sqrt[4]{c+dx}} dx$.6910
3.1698	$\int \frac{1}{(a+bx)^{15/4} \sqrt[4]{c+dx}} dx$.6913
3.1699	$\int \frac{1}{(a+bx)^{19/4} \sqrt[4]{c+dx}} dx$.6916
3.1700	$\int \frac{(a+bx)^{7/4}}{\sqrt[4]{c+dx}} dx$.6920
3.1701	$\int \frac{(a+bx)^{3/4}}{\sqrt[4]{c+dx}} dx$.6925
3.1702	$\int \frac{1}{\sqrt[4]{a+bx} \sqrt[4]{c+dx}} dx$.6930
3.1703	$\int \frac{1}{(a+bx)^{5/4} \sqrt[4]{c+dx}} dx$.6935
3.1704	$\int \frac{1}{(a+bx)^{9/4} \sqrt[4]{c+dx}} dx$.6940
3.1705	$\int \frac{(a+bx)^{7/4}}{(c+dx)^{3/4}} dx$.6945
3.1706	$\int \frac{(a+bx)^{3/4}}{(c+dx)^{3/4}} dx$.6950
3.1707	$\int \frac{1}{\sqrt[4]{a+bx} (c+dx)^{3/4}} dx$.6955
3.1708	$\int \frac{1}{(a+bx)^{5/4} (c+dx)^{3/4}} dx$.6959
3.1709	$\int \frac{1}{(a+bx)^{9/4} (c+dx)^{3/4}} dx$.6962
3.1710	$\int \frac{1}{(a+bx)^{13/4} (c+dx)^{3/4}} dx$.6965
3.1711	$\int \frac{1}{(a+bx)^{17/4} (c+dx)^{3/4}} dx$.6969
3.1712	$\int \frac{(a+bx)^{5/4}}{(c+dx)^{3/4}} dx$.6973

3.1713	$\int \frac{\sqrt[4]{a+bx}}{(c+dx)^{3/4}} dx$.6978
3.1714	$\int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx$.6982
3.1715	$\int \frac{1}{(a+bx)^{7/4}(c+dx)^{3/4}} dx$.6986
3.1716	$\int \frac{1}{(a+bx)^{11/4}(c+dx)^{3/4}} dx$.6990
3.1717	$\int \frac{(a+bx)^{5/4}}{(c+dx)^{5/4}} dx$.6995
3.1718	$\int \frac{\sqrt[4]{a+bx}}{(c+dx)^{5/4}} dx$.7000
3.1719	$\int \frac{1}{(a+bx)^{3/4}(c+dx)^{5/4}} dx$.7005
3.1720	$\int \frac{1}{(a+bx)^{7/4}(c+dx)^{5/4}} dx$.7008
3.1721	$\int \frac{1}{(a+bx)^{11/4}(c+dx)^{5/4}} dx$.7011
3.1722	$\int \frac{1}{(a+bx)^{15/4}(c+dx)^{5/4}} dx$.7015
3.1723	$\int \frac{(a+bx)^{11/4}}{(c+dx)^{5/4}} dx$.7019
3.1724	$\int \frac{(a+bx)^{7/4}}{(c+dx)^{5/4}} dx$.7025
3.1725	$\int \frac{(a+bx)^{3/4}}{(c+dx)^{5/4}} dx$.7031
3.1726	$\int \frac{1}{\sqrt[4]{a+bx}(c+dx)^{5/4}} dx$.7036
3.1727	$\int \frac{1}{(a+bx)^{5/4}(c+dx)^{5/4}} dx$.7041
3.1728	$\int \frac{1}{(a+bx)^{9/4}(c+dx)^{5/4}} dx$.7046
3.1729	$\int \frac{1}{\sqrt[4]{1-ax}(1+bx)^{3/4}} dx$.7052
3.1730	$\int \frac{1}{\sqrt[4]{1-ax}(1+ax)^{3/4}} dx$.7057
3.1731	$\int \frac{(a+bx)^{3/2}}{\sqrt[5]{c+dx}} dx$.7062
3.1732	$\int \frac{\sqrt{a+bx}}{\sqrt[5]{c+dx}} dx$.7065
3.1733	$\int \frac{1}{\sqrt{a+bx}\sqrt[5]{c+dx}} dx$.7068
3.1734	$\int \frac{1}{(a+bx)^{3/2}\sqrt[5]{c+dx}} dx$.7071
3.1735	$\int \frac{1}{(a+bx)^{5/2}\sqrt[5]{c+dx}} dx$.7074
3.1736	$\int (a+bx)^{5/2}\sqrt[6]{c+dx} dx$.7077
3.1737	$\int (a+bx)^{3/2}\sqrt[6]{c+dx} dx$.7082
3.1738	$\int \sqrt{a+bx}\sqrt[6]{c+dx} dx$.7086
3.1739	$\int \frac{\sqrt[6]{c+dx}}{\sqrt{a+bx}} dx$.7090

3.1740	$\int \frac{\sqrt[6]{c+dx}}{(a+bx)^{3/2}} dx$7094
3.1741	$\int \frac{\sqrt[6]{c+dx}}{(a+bx)^{5/2}} dx$7098
3.1742	$\int (a+bx)^{3/2} (c+dx)^{5/6} dx$7103
3.1743	$\int \sqrt{a+bx} (c+dx)^{5/6} dx$7109
3.1744	$\int \frac{(c+dx)^{5/6}}{\sqrt{a+bx}} dx$7115
3.1745	$\int \frac{(c+dx)^{5/6}}{(a+bx)^{3/2}} dx$7121
3.1746	$\int \frac{(c+dx)^{5/6}}{(a+bx)^{5/2}} dx$7127
3.1747	$\int \frac{(c+dx)^{5/6}}{(a+bx)^{7/2}} dx$7133
3.1748	$\int \frac{(a+bx)^{5/2}}{\sqrt[6]{c+dx}} dx$7139
3.1749	$\int \frac{(a+bx)^{3/2}}{\sqrt[6]{c+dx}} dx$7145
3.1750	$\int \frac{\sqrt{a+bx}}{\sqrt[6]{c+dx}} dx$7151
3.1751	$\int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx$7157
3.1752	$\int \frac{1}{(a+bx)^{3/2} \sqrt[6]{c+dx}} dx$7162
3.1753	$\int \frac{1}{(a+bx)^{5/2} \sqrt[6]{c+dx}} dx$7168
3.1754	$\int \frac{(a+bx)^{5/2}}{(c+dx)^{5/6}} dx$7174
3.1755	$\int \frac{(a+bx)^{3/2}}{(c+dx)^{5/6}} dx$7179
3.1756	$\int \frac{\sqrt{a+bx}}{(c+dx)^{5/6}} dx$7184
3.1757	$\int \frac{1}{\sqrt{a+bx} (c+dx)^{5/6}} dx$7188
3.1758	$\int \frac{1}{(a+bx)^{3/2} (c+dx)^{5/6}} dx$7192
3.1759	$\int \frac{1}{(a+bx)^{5/2} (c+dx)^{5/6}} dx$7196
3.1760	$\int \frac{(a+bx)^{5/2}}{(c+dx)^{7/6}} dx$7201
3.1761	$\int \frac{(a+bx)^{3/2}}{(c+dx)^{7/6}} dx$7207
3.1762	$\int \frac{\sqrt{a+bx}}{(c+dx)^{7/6}} dx$7213
3.1763	$\int \frac{1}{\sqrt{a+bx} (c+dx)^{7/6}} dx$7219
3.1764	$\int \frac{1}{(a+bx)^{3/2} (c+dx)^{7/6}} dx$7224
3.1765	$\int \frac{1}{(a+bx)^{5/2} (c+dx)^{7/6}} dx$7230
3.1766	$\int \sqrt[6]{a+bx} (c+dx)^{13/6} dx$7236

3.1767	$\int \sqrt[6]{a+bx} (c+dx)^{7/6} dx$.7239
3.1768	$\int \sqrt[6]{a+bx} \sqrt[6]{c+dx} dx$.7242
3.1769	$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{5/6}} dx$.7245
3.1770	$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{11/6}} dx$.7248
3.1771	$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{17/6}} dx$.7251
3.1772	$\int \sqrt[6]{a+bx} (c+dx)^{5/6} dx$.7254
3.1773	$\int \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} dx$.7262
3.1774	$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{7/6}} dx$.7269
3.1775	$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{13/6}} dx$.7275
3.1776	$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{19/6}} dx$.7278
3.1777	$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{25/6}} dx$.7281
3.1778	$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{31/6}} dx$.7285
3.1779	$\int (a+bx)^{5/6} \sqrt[6]{c+dx} dx$.7289
3.1780	$\int \frac{(a+bx)^{5/6}}{(c+dx)^{5/6}} dx$.7297
3.1781	$\int \frac{(a+bx)^{5/6}}{(c+dx)^{11/6}} dx$.7304
3.1782	$\int \frac{(a+bx)^{5/6}}{(c+dx)^{17/6}} dx$.7310
3.1783	$\int \frac{(a+bx)^{5/6}}{(c+dx)^{23/6}} dx$.7313
3.1784	$\int \frac{(a+bx)^{5/6}}{(c+dx)^{29/6}} dx$.7316
3.1785	$\int \frac{(a+bx)^{5/6}}{(c+dx)^{35/6}} dx$.7320
3.1786	$\int (a+bx)^{5/6} (c+dx)^{11/6} dx$.7324
3.1787	$\int (a+bx)^{5/6} (c+dx)^{5/6} dx$.7327
3.1788	$\int \frac{(a+bx)^{5/6}}{\sqrt[6]{c+dx}} dx$.7330
3.1789	$\int \frac{(a+bx)^{5/6}}{(c+dx)^{7/6}} dx$.7333
3.1790	$\int \frac{(a+bx)^{5/6}}{(c+dx)^{13/6}} dx$.7336
3.1791	$\int \frac{(a+bx)^{5/6}}{(c+dx)^{19/6}} dx$.7339
3.1792	$\int (a+bx)^{7/6} (c+dx)^{13/6} dx$.7342
3.1793	$\int (a+bx)^{7/6} (c+dx)^{7/6} dx$.7345
3.1794	$\int (a+bx)^{7/6} \sqrt[6]{c+dx} dx$.7348

3.1795	$\int \frac{(a+bx)^{7/6}}{(c+dx)^{5/6}} dx$.7351
3.1796	$\int \frac{(a+bx)^{7/6}}{(c+dx)^{11/6}} dx$.7354
3.1797	$\int \frac{(a+bx)^{7/6}}{(c+dx)^{17/6}} dx$.7357
3.1798	$\int \frac{(a+bx)^{7/6}}{\sqrt[6]{c+dx}} dx$.7360
3.1799	$\int \frac{(a+bx)^{7/6}}{(c+dx)^{7/6}} dx$.7369
3.1800	$\int \frac{(a+bx)^{7/6}}{(c+dx)^{13/6}} dx$.7376
3.1801	$\int \frac{(a+bx)^{7/6}}{(c+dx)^{19/6}} dx$.7382
3.1802	$\int \frac{(a+bx)^{7/6}}{(c+dx)^{25/6}} dx$.7385
3.1803	$\int \frac{(a+bx)^{7/6}}{(c+dx)^{31/6}} dx$.7389
3.1804	$\int \frac{(a+bx)^{7/6}}{(c+dx)^{37/6}} dx$.7393
3.1805	$\int \frac{(c+dx)^{7/6}}{\sqrt[6]{a+bx}} dx$.7397
3.1806	$\int \frac{\sqrt[6]{c+dx}}{\sqrt[6]{a+bx}} dx$.7406
3.1807	$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{5/6}} dx$.7413
3.1808	$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{11/6}} dx$.7418
3.1809	$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{17/6}} dx$.7421
3.1810	$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{23/6}} dx$.7424
3.1811	$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{29/6}} dx$.7428
3.1812	$\int \frac{(c+dx)^{11/6}}{\sqrt[6]{a+bx}} dx$.7432
3.1813	$\int \frac{(c+dx)^{5/6}}{\sqrt[6]{a+bx}} dx$.7435
3.1814	$\int \frac{1}{\sqrt[6]{a+bx} \sqrt[6]{c+dx}} dx$.7438
3.1815	$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{7/6}} dx$.7441
3.1816	$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{13/6}} dx$.7444
3.1817	$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{19/6}} dx$.7447
3.1818	$\int \frac{(c+dx)^{13/6}}{(a+bx)^{5/6}} dx$.7450
3.1819	$\int \frac{(c+dx)^{7/6}}{(a+bx)^{5/6}} dx$.7453
3.1820	$\int \frac{\sqrt[6]{c+dx}}{(a+bx)^{5/6}} dx$.7456

3.1821	$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{5/6}} dx$.7459
3.1822	$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{11/6}} dx$.7462
3.1823	$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{17/6}} dx$.7465
3.1824	$\int \frac{(c+dx)^{11/6}}{(a+bx)^{5/6}} dx$.7468
3.1825	$\int \frac{(c+dx)^{5/6}}{(a+bx)^{5/6}} dx$.7477
3.1826	$\int \frac{1}{(a+bx)^{5/6} \sqrt[6]{c+dx}} dx$.7484
3.1827	$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{7/6}} dx$.7489
3.1828	$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{13/6}} dx$.7492
3.1829	$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{19/6}} dx$.7495
3.1830	$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{25/6}} dx$.7498
3.1831	$\int \frac{(c+dx)^{13/6}}{(a+bx)^{7/6}} dx$.7502
3.1832	$\int \frac{(c+dx)^{7/6}}{(a+bx)^{7/6}} dx$.7511
3.1833	$\int \frac{\sqrt[6]{c+dx}}{(a+bx)^{7/6}} dx$.7518
3.1834	$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{5/6}} dx$.7524
3.1835	$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{11/6}} dx$.7527
3.1836	$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{17/6}} dx$.7530
3.1837	$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{23/6}} dx$.7534
3.1838	$\int \frac{(c+dx)^{11/6}}{(a+bx)^{7/6}} dx$.7538
3.1839	$\int \frac{(c+dx)^{5/6}}{(a+bx)^{7/6}} dx$.7541
3.1840	$\int \frac{1}{(a+bx)^{7/6} \sqrt[6]{c+dx}} dx$.7544
3.1841	$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{7/6}} dx$.7547
3.1842	$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{13/6}} dx$.7550
3.1843	$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{19/6}} dx$.7553
3.1844	$\int (a+bx)^m (a+b(2+m)x) dx$.7556
3.1845	$\int (a+bx)^m (c+dx)^n dx$.7559
3.1846	$\int (a+bx)^m (c+dx)^3 dx$.7562
3.1847	$\int (a+bx)^m (c+dx)^2 dx$.7568
3.1848	$\int (a+bx)^m (c+dx) dx$.7572
3.1849	$\int \frac{(a+bx)^m}{c+dx} dx$.7575

3.1850	$\int \frac{(a+bx)^m}{(c+dx)^2} dx$.7578
3.1851	$\int \frac{(a+bx)^m}{(c+dx)^3} dx$.7581
3.1852	$\int (a+bx)^3(c+dx)^n dx$.7584
3.1853	$\int (a+bx)^2(c+dx)^n dx$.7590
3.1854	$\int (a+bx)(c+dx)^n dx$.7594
3.1855	$\int (c+dx)^n dx$.7597
3.1856	$\int \frac{(c+dx)^n}{a+bx} dx$.7600
3.1857	$\int \frac{(c+dx)^n}{(a+bx)^2} dx$.7603
3.1858	$\int \frac{(c+dx)^n}{(a+bx)^3} dx$.7606
3.1859	$\int (a+bx)^{-4+n}(c+dx)^{-n} dx$.7609
3.1860	$\int (a+bx)^{-3+n}(c+dx)^{-n} dx$.7613
3.1861	$\int (a+bx)^{-2+n}(c+dx)^{-n} dx$.7616
3.1862	$\int (a+bx)^{-1+n}(c+dx)^{-n} dx$.7619
3.1863	$\int (a+bx)^n(c+dx)^{-n} dx$.7622
3.1864	$\int (a+bx)^{1+n}(c+dx)^{-n} dx$.7625
3.1865	$\int (a+bx)^{2+n}(c+dx)^{-n} dx$.7628
3.1866	$\int (a+bx)^{-n}(c+dx)^n dx$.7631
3.1867	$\int (a+bx)^{-1-n}(c+dx)^n dx$.7634
3.1868	$\int (a+bx)^{-2-n}(c+dx)^n dx$.7637
3.1869	$\int (a+bx)^{-3-n}(c+dx)^n dx$.7640
3.1870	$\int (a+bx)^{-4-n}(c+dx)^n dx$.7643
3.1871	$\int (a+bx)^{-5-n}(c+dx)^n dx$.7647
3.1872	$\int (a+bx)^n(c+dx)^{-n} dx$.7652
3.1873	$\int (a+bx)^n(c+dx)^{-1-n} dx$.7655
3.1874	$\int (a+bx)^n(c+dx)^{-2-n} dx$.7658
3.1875	$\int (a+bx)^n(c+dx)^{-3-n} dx$.7661
3.1876	$\int (a+bx)^n(c+dx)^{-4-n} dx$.7664
3.1877	$\int (a+bx)^n(c+dx)^{-5-n} dx$.7668
3.1878	$\int (a+bx)^{-2+n}(c+dx)^{1-n} dx$.7673
3.1879	$\int (a+bx)^{1+n}(c+dx)^{-1-n} dx$.7676
3.1880	$\int (a+bx)^m(c+dx)^{1+2n-2(1+n)} dx$.7679
3.1881	$\int \frac{(c+dx)^{1+2n-2(1+n)}}{(a+bx)^2} dx$.7682
3.1882	$\int (a+bx)^m(ac(1+m)+bc(2+m)x)^{-3-m} dx$.7685
3.1883	$\int (a+bx)^{-1-\frac{bc}{bc-ad}}(c+dx)^{-1+\frac{ad}{bc-ad}} dx$.7688
3.1884	$\int (a+bx)^{\frac{-2bc+ad}{bc-ad}}(c+dx)^{\frac{bc-2ad}{-bc+ad}} dx$.7691

3.1885	$\int \frac{(1-x)^n}{\sqrt{1+x}} dx$.7694
3.1886	$\int \frac{(1+x)^n}{\sqrt{1-x}} dx$.7697
3.1887	$\int (1-x)^n (1+x)^{7/3} dx$.7700
3.1888	$\int (1-x)^{7/3} (1+x)^n dx$.7703
3.1889	$\int (1+2x)^{-m} (2+3x)^m dx$.7706
3.1890	$\int \left(\frac{d(a+bx)}{-bc+ad} \right)^m (c+dx)^n dx$.7709
3.1891	$\int (a+bx+cx^2+dx^3) dx$.7712
3.1892	$\int (-x^3+x^4) dx$.7715
3.1893	$\int (-1+x^5) dx$.7718
3.1894	$\int (7+4x) dx$.7721
3.1895	$\int (4x+\pi x^3) dx$.7723
3.1896	$\int (2x+5x^2) dx$.7726
3.1897	$\int \left(\frac{x^2}{2} + \frac{x^3}{3} \right) dx$.7729
3.1898	$\int (3-5x+2x^2) dx$.7732
3.1899	$\int (-2x+x^2+x^3) dx$.7735
3.1900	$\int (1-x^2-3x^5) dx$.7738
3.1901	$\int (5+2x+3x^2+4x^3) dx$.7741
3.1902	$\int \left(a + \frac{d}{x^3} + \frac{c}{x^2} + \frac{b}{x} \right) dx$.7743
3.1903	$\int \left(\frac{1}{x^5} + x + x^5 \right) dx$.7746
3.1904	$\int \left(\frac{1}{x^3} + \frac{1}{x^2} + \frac{1}{x} \right) dx$.7749
3.1905	$\int \left(-\frac{2}{x^2} + \frac{3}{x} \right) dx$.7752
3.1906	$\int \left(-\frac{1}{7x^6} + x^6 \right) dx$.7755
3.1907	$\int \left(1 + \frac{1}{x} + x \right) dx$.7758
3.1908	$\int \left(-\frac{3}{x^3} + \frac{4}{x^2} \right) dx$.7761
3.1909	$\int \left(\frac{1}{x} + 2x + x^2 \right) dx$.7764
3.1910	$\int (x^{5/6} - x^3) dx$.7767
3.1911	$\int (33 + \sqrt[3]{x}) dx$.7770
3.1912	$\int \left(\frac{1}{2\sqrt{x}} + 2\sqrt{x} \right) dx$.7773
3.1913	$\int \left(-\frac{1}{x^2} + \frac{10}{x} + 6\sqrt{x} \right) dx$.7776
3.1914	$\int \left(\frac{1}{x^{3/2}} + x^{3/2} \right) dx$.7779

3.1915	$\int (-5x^{3/2} + 7x^{5/2}) dx$.7782
3.1916	$\int \left(\frac{2}{\sqrt{x}} + \sqrt{x} - \frac{x}{2} \right) dx$.7784
3.1917	$\int \left(-\frac{2}{x} + \frac{\sqrt{x}}{5} + x^{3/2} \right) dx$.7787
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Chapter 1

Introduction

This report gives the result of running the computer algebra independent integration problems. The listing of the problems are maintained by and can be downloaded from <https://rulebasedintegration.org>

The number of integrals in this report is [1917]. This is test number [13].

1.1 Listing of CAS systems tested

The following systems were tested at this time.

1. Mathematica 12.3 (64 bit) on windows 10.
2. Rubi 4.16.1 in Mathematica 12.1 on windows 10.
3. Maple 2021.1 (64 bit) on windows 10.
4. Maxima 5.44 on Linux. (via sagemath 9.3)
5. Fricas 1.3.7 on Linux (via sagemath 9.3)
6. Giac/Xcas 1.7 on Linux. (via sagemath 9.3)
7. Sympy 1.8 under Python 3.8.8 using Anaconda distribution on Ubuntu.
8. Mupad using Matlab 2021a with Symbolic Math Toolbox Version 8.7 under windows 10 (64 bit)

Maxima, Fricas and Giac/Xcas were called from inside SageMath. This was done using SageMath integrate command by changing the name of the algorithm to use the different CAS systems.

Sympy was called directly using Python.

1.2 Results

Important note: A number of problems in this test suite have no antiderivative in closed form. This means the antiderivative of these integrals can not be expressed in terms of elementary, special functions or Hypergeometric₂F₁ functions. RootSum and RootOf are not allowed.

If a CAS returns the above integral unevaluated within the time limit, then the result is counted as passed and assigned an A grade.

However, if CAS times out, then it is assigned an F grade even if the integral is not integrable, as this implies CAS could not determine that the integral is not integrable in the time limit.

If a CAS returns an antiderivative to such an integral, it is assigned an A grade automatically and this special result is listed in the introduction section of each individual test report to make it easy to identify as this can be important result to investigate.

The results given in in the table below reflects the above.

System	solved	Failed
Rubi	% 100.00 (1917)	% 0.00 (0)
Mathematica	% 100.00 (1917)	% 0.00 (0)
Maple	% 81.38 (1560)	% 18.62 (357)
Maxima	% 69.27 (1328)	% 30.73 (589)
Fricas	% 83.62 (1603)	% 16.38 (314)
Sympy	% 62.65 (1201)	% 37.35 (716)
Giac	% 66.56 (1276)	% 33.44 (641)
Mupad	% 64.74 (1241)	% 35.26 (676)

Table 1.1: Percentage solved for each CAS

The table below gives additional break down of the grading of quality of the antiderivatives generated by each CAS. The grading is given using the letters A,B,C and F with A being the best quality. The grading is accomplished by comparing the antiderivative generated with the optimal antiderivatives included in the test suite. The following table describes the meaning of these grades.

grade	description
A	Integral was solved and antiderivative is optimal in quality and leaf size.
B	Integral was solved and antiderivative is optimal in quality but leaf size is larger than twice the optimal antiderivatives leaf size.
C	Integral was solved and antiderivative is non-optimal in quality. This can be due to one or more of the following reasons <ol style="list-style-type: none"> 1. antiderivative contains a hypergeometric function and the optimal antiderivative does not. 2. antiderivative contains a special function and the optimal antiderivative does not. 3. antiderivative contains the imaginary unit and the optimal antiderivative does not.
F	Integral was not solved. Either the integral was returned unevaluated within the time limit, or it timed out, or CAS hanged or crashed or an exception was raised.

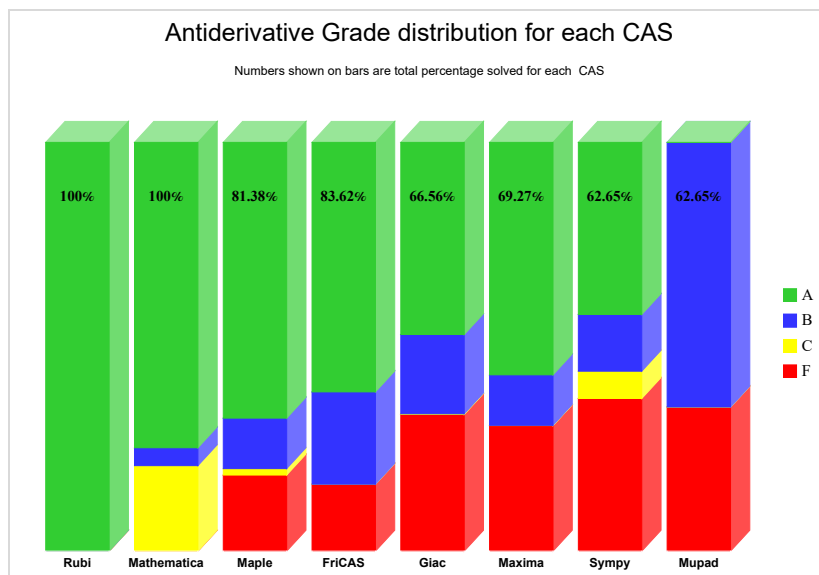
Table 1.2: Description of grading applied to integration result

Grading is implemented for all CAS systems. Based on the above, the following table summarizes the grading for this test suite.

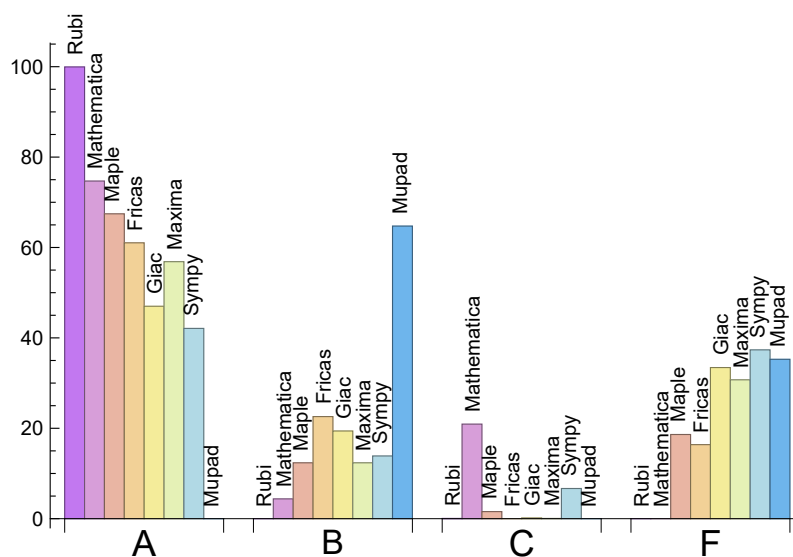
System	% A grade	% B grade	% C grade	% F grade
Rubi	99.95	0.00	0.05	0.00
Mathematica	74.70	4.38	20.92	0.00
Maple	67.45	12.36	1.56	18.62
Maxima	56.86	12.36	0.05	30.73
Fricas	61.03	22.59	0.00	16.38
Sympy	42.10	13.88	6.68	37.35
Giac	47.00	19.41	0.16	33.44
Mupad	0.00	64.74	0.00	35.26

Table 1.3: Antiderivative Grade distribution of each CAS

The following is a Bar chart illustration of the data in the above table.



The figure below compares the CAS systems for each grade level.



The following table shows the distribution of the different types of failure for each CAS. There are 3 types of reasons why it can fail. The first is when CAS returns back the input within the time limit, which means it could not solve it. This is the typical normal failure **F**.

The second is due to time out. CAS could not solve the integral within the 3 minutes time limit which is assigned **F(-1)**.

The third is due to an exception generated. Assigned **F(-2)**. This most likely indicates an interface problem between sagemath and the CAS (applicable only to FriCAS, Maxima and Giac) or it could be an indication of an internal error in CAS. This type of error requires more investigations to determine the cause.

System	Number failed	Percentage normal failure	Percentage time-out failure	Percentage exception failure
Rubi	0	0.00 %	0.00 %	0.00 %
Mathematica	0	0.00 %	0.00 %	0.00 %
Maple	357	100.00 %	0.00 %	0.00 %
Maxima	589	78.10 %	0.00 %	21.90 %
Fricas	314	100.00 %	0.00 %	0.00 %
Sympy	716	69.97 %	28.49 %	1.54 %
Giac	641	78.00 %	9.20 %	12.79 %
Mupad	676	100.00 %	0.00 %	0.00 %

Table 1.4: Time and leaf size performance for each CAS

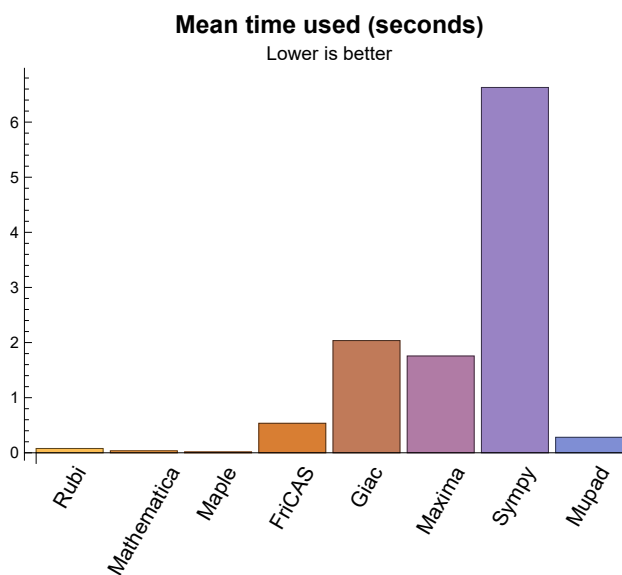
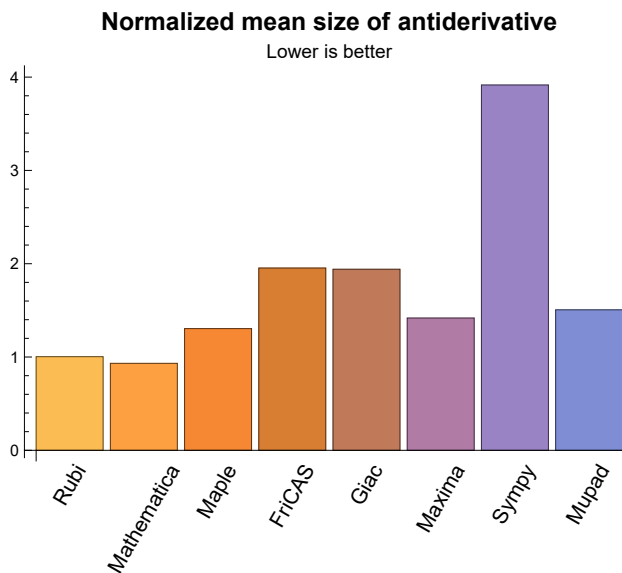
1.3 Performance

The table below summarizes the performance of each CAS system in terms of CPU time and leaf size of results.

System	Mean time (sec)	Mean size	Normalized mean	Median size	Normalized median
Rubi	0.08	108.10	1.00	66.00	1.00
Mathematica	0.04	72.01	0.93	48.00	0.85
Maple	0.02	105.94	1.30	54.00	0.93
Maxima	1.76	107.90	1.42	56.00	0.99
Fricas	0.54	202.55	1.95	77.00	1.35
Sympy	6.63	263.67	3.92	88.00	1.53
Giac	2.04	159.13	1.94	65.00	1.07
Mupad	0.28	123.92	1.51	52.00	0.97

Table 1.5: Time and leaf size performance for each CAS

The following are bar charts for the normalized leafsize and time used columns from the above table.



1.4 list of integrals that has no closed form antiderivative

{

1.5 list of integrals solved by CAS but has no known antiderivative

Rubi {}

Mathematica {}

Maple {}

Maxima {}

Fricas {}

Sympy {}

Giac {}

Mupad {}

1.6 list of integrals solved by CAS but failed verification

The following are integrals solved by CAS but the verification phase failed to verify the anti-derivative produced is correct. This does not mean necessarily that the anti-derivative is wrong, as additional methods of verification might be needed, or more time is needed (3 minutes time limit was used). These integrals are listed here to make it easier to do further investigation to determine why it was not possible to verify the result produced.

Rubi {}

Mathematica {}

Maple Verification phase not implemented yet.

Maxima Verification phase not implemented yet.

Fricas Verification phase not implemented yet.

Sympy Verification phase not implemented yet.

Giac Verification phase not implemented yet.

Mupad Verification phase not implemented yet.

1.7 Timing

The command `AbsoluteTiming[]` was used in Mathematica to obtain the elapsed time for each integrate call. In Maple, the command `Usage` was used as in the following example

```
cpu_time := Usage(assign ('result_of _int',int(expr,x)),output='realtime')
```

For all other CAS systems, the elapsed time to complete each integral was found by taking the difference between the time after the call has completed from the time before the call was made. This was done using Python's `time.time()` call.

All elapsed times shown are in seconds. A time limit of 3 minutes was used for each integral. If the integrate command did not complete within this time limit, the integral was aborted and considered to have failed and assigned an F grade. The time used by failed integrals due to time out is not counted in the final statistics.

1.8 Verification

A verification phase was applied on the result of integration for Rubi and Mathematica. Future version of this report will implement verification for the other CAS systems. For the integrals whose result was not run through a verification phase, it is assumed that the antiderivative produced was correct.

Verification phase has 3 minutes time out. An integral whose result was not verified could still be correct. Further investigation is needed on those integrals which failed verifications. Such integrals are marked in the summary table below and also in each integral separate section so they are easy to identify and locate.

1.9 Important notes about some of the results

1.9.1 Important note about Maxima results

Since these integrals are run in a batch mode, using an automated script, and by using `sagemath` (SageMath uses Maxima), then any integral where Maxima needs an interactive response from the user to answer a question during evaluation of the integral in order to complete the integration, will fail and is counted as failed.

The exception raised is `ValueError`. Therefore Maxima result below is lower than what could result if Maxima was run directly and each question Maxima asks was answered correctly.

The percentage of such failures were not counted for each test file, but for an example, for the Timofeev test file, there were about 14 such integrals out of total 705, or about 2 percent. This percentage can be higher or lower depending on the specific input test file.

Such integrals can be indentified by looking at the output of the integration in each section for Maxima. The exception message will indicate of the error is due to the interactive question being asked or not.

Maxima integrate was run using SageMath with the following settings set by default

```
'besselexpand : true'
'display2d : false'
'domain : complex'
'keepfloat : true'
'load(to_poly_solve)'
'load(simplify_sum)'
'load(abs_integrate)' 'load(diag)'
```

SageMath loading of Maxima `abs_integrate` was found to cause some problem. So the following code was added to disable this effect.

```
from sage.interfaces.maxima_lib import maxima_lib
maxima_lib.set('extra_definite_integration_methods', '[]')
maxima_lib.set('extra_integration_methods', '[]')
```

See <https://ask.sagemath.org/question/43088/integrate-results-that-are-different-from-using-maxima/> for reference.

1.9.2 Important note about FriCAS and Giac/X-CAS results

There are Few integrals which failed due to SageMath not able to translate the result back to SageMath syntax and not because these CAS system were not able to do the integrations.

These will fail With error `Exception raised: NotImplementedError`

The number of such cases seems to be very small. About 1 or 2 percent of all integrals.

Hopefully the next version of SageMath will have complete translation of FriCAS and XCAS syntax and I will re-run all the tests again when this happens.

1.9.3 Important note about finding leaf size of antiderivative

For Mathematica, Rubi and Maple, the builtin system function `LeafSize` is used to find the leaf size of each antiderivative.

The other CAS systems (SageMath and Sympy) do not have special builtin function for this purpose at this time. Therefore the leaf size for Fricas and Sympy and Giac antiderivatives is determined using the following function, thanks to user `slelievre` at <https://>

ask.sagemath.org/question/57123/could-we-have-a-leaf_count-function-in-base-sagemath/

```
def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)
```

For Sympy, which is called directly from Python, the following code is used to obtain the leafsize of its result

```
try:
    # 1.7 is a fudge factor since it is low side from actual leaf count
    leafCount = round(1.7*count_ops(anti))

except Exception as ee:
    leafCount = 1
```

1.9.4 Important note about Mupad results

Matlab's symbolic toolbox does not have a leaf count function to measure the size of the antiderivative, Maple was used to determine the leaf size of Mupad output by post processing.

Currently no grading of the antiderivative for Mupad is implemented. If it can integrate the problem, it was assigned a B grade automatically as a placeholder. In the future, when grading function is implemented for Mupad, the tests will be rerun again.

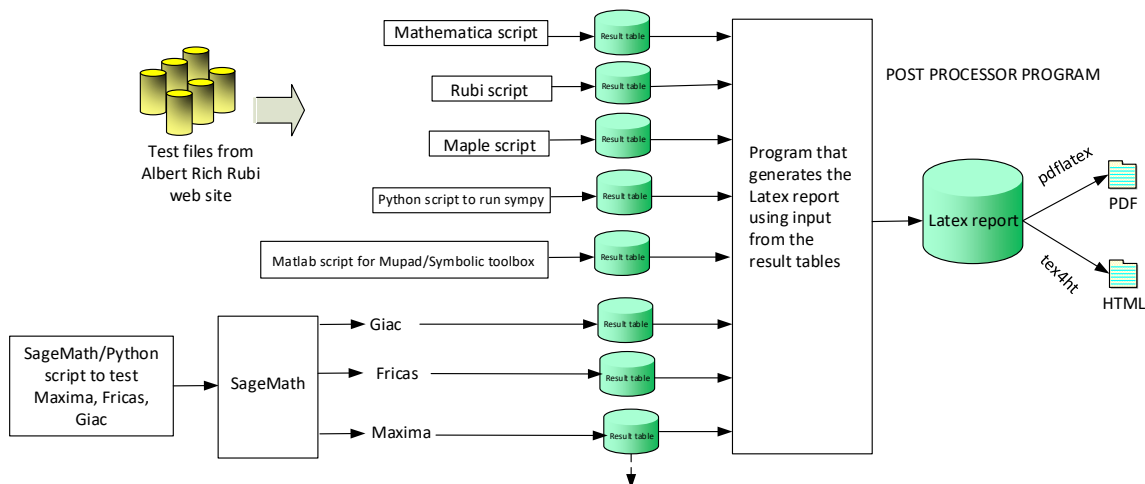
The following is an example of using Matlab's symbolic toolbox (Mupad) to solve an integral

```
integrand = evalin(symengine, 'cos(x)*sin(x)')
the_variable = evalin(symengine, 'x')
anti = int(integrand, the_variable)
```

Which gives $\sin(x)^2/2$

1.10 Design of the test system

The following diagram gives a high level view of the current test build system.



One record (line) per one integral result. The line is CSV comma separated. This is description of each record

1. integer, the problem number.
 2. integer. 0 for failed, 1 for passed, -1 for timeout, -2 for CAS specific exception. (this is not the grade field)
 3. integer. Leaf size of result.
 4. integer. Leaf size of the optimal antiderivative.
 5. number. CPU time used to solve this integral. 0 if failed.
 6. string. The integral in Latex format
 7. string. The input used in CAS own syntax.
 8. string. The result (antiderivative) produced by CAS in Latex format
 9. string. The optimal antiderivative in Latex format.
 10. integer. 0 or 1. Indicates if problem has known antiderivative or not
 11. String. The result (antiderivative) in CAS own syntax.
 12. String. The grade of the antiderivative. Can be "A", "B", "C", or "F"
- The following field present only in Rubi and Mathematica Tables*
13. integer. 1 if result was verified or 0 if not verified.
- The following fields present only in Rubi Tables*
14. integer. Number of rules used.
 15. integer. Integrand leaf size.
 16. real number. Ratio of field 14 over field 15
 17. integer. 1 if result was verified or 0 if not verified.
 18. String of form "{n,n,...}" which is list of the rules used by Rubi

High level overview of the CAS independent integration test build system

Chapter 2

detailed summary tables of results

2.1 List of integrals sorted by grade for each CAS

2.1.1 Rubi

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 331, 332, 333, 334, 335, 336, 337, 338, 339, 340, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 365, 366, 367, 368, 370, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 383, 384, 385, 386, 387, 388, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400, 401, 402, 403, 404, 405, 406, 407, 408, 409, 410, 411, 412, 413, 414, 415, 416, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 428, 429, 430, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 442, 443, 444, 445, 446, 447, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463, 464, 465, 466, 467, 468, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 487, 488, 489, 490, 491, 492, 493, 494, 495, 496, 497, 498, 499, 500, 501, 502, 503, 504, 505, 506, 507, 508, 509, 510, 511, 512, 513, 514, 515, 516, 517, 518, 519, 520, 521, 522, 523, 524, 525, 526, 527, 528, 529, 530, 531, 532, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 543, 544, 545, 546, 547, 548, 549, 550,

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B grade: { }

C grade: { 369 }

F grade: { }

2.1.2 Mathematica

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 74, 75, 76, 77, 78, 79, 80, 81, 83, 84, 85, 86, 87, 88, 89, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 106, 107, 108, 109, 110, 111, 112, 113, 114, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 134, 135, 136,

137, 138, 139, 140, 141, 142, 143, 144, 145, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 292, 293, 294, 295, 296, 298, 300, 301, 302, 303, 304, 307, 309, 310, 311, 312, 313, 314, 315, 316, 317, 322, 325, 326, 328, 330, 331, 334, 335, 336, 337, 338, 339, 340, 343, 344, 345, 346, 347, 351, 352, 353, 354, 355, 359, 360, 368, 369, 370, 371, 372, 373, 374, 375, 378, 379, 380, 381, 382, 385, 386, 387, 388, 389, 392, 393, 394, 395, 396, 399, 400, 401, 402, 406, 407, 408, 409, 410, 413, 414, 415, 416, 420, 421, 424, 425, 426, 427, 428, 429, 430, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 442, 443, 444, 445, 446, 447, 448, 449, 450, 451, 452, 458, 459, 464, 469, 470, 471, 472, 478, 479, 484, 489, 490, 491, 492, 493, 494, 495, 496, 497, 498, 499, 500, 501, 502, 503, 504, 505, 506, 507, 508, 509, 510, 511, 512, 513, 514, 515, 516, 517, 518, 519, 520, 521, 522, 523, 524, 527, 528, 529, 530, 533, 534, 535, 536, 539, 540, 541, 542, 545, 546, 547, 548, 551, 552, 553, 554, 557, 558, 559, 560, 563, 564, 565, 566, 569, 570, 571, 572, 573, 574, 575, 576, 579, 580, 581, 582, 583, 585, 586, 587, 588, 589, 590, 591, 592, 593, 594, 595, 598, 599, 600, 601, 603, 604, 605, 606, 607, 608, 609, 610, 611, 612, 613, 614, 615, 618, 619, 620, 621, 622, 624, 625, 626, 627, 628, 629, 630, 631, 632, 633, 634, 637, 638, 639, 640, 642, 643, 644, 645, 646, 647, 648, 649, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 672, 673, 675, 677, 679, 698, 699, 700, 701, 702, 703, 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 730, 731, 732, 733, 734, 735, 736, 737, 738, 739, 740, 741, 742, 743, 744, 745, 746, 747, 748, 749, 750, 751, 752, 753, 754, 755, 756, 757, 758, 759, 760, 761, 762, 763, 764, 765, 766, 767, 768, 769, 770, 771, 772, 773, 774, 775, 776, 777, 778, 779, 780, 781, 782, 783, 784, 785, 786, 787, 788, 789, 790, 791, 792, 793, 794, 795, 796, 797, 798, 799, 800, 801, 802, 803, 804, 805, 806, 807, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823, 824, 825, 826, 827, 828, 829, 830, 831, 832, 833, 834, 835, 836, 837, 838, 839, 840, 841, 842, 843, 844, 845, 846, 847, 848, 849, 850, 851, 852, 853, 854, 855, 856, 857, 858, 859, 860, 861, 862, 863, 864, 865, 866, 867, 868, 869, 870, 871, 872, 873, 874, 875, 876, 877, 878, 879, 880, 881, 882, 883, 884, 885, 886, 887, 888, 889, 890, 891, 892, 893, 894, 895, 896, 897, 898, 899, 900, 901, 902, 903, 904, 905, 906, 907, 908, 909, 910, 911, 912, 913, 914, 915, 916, 917, 918, 919, 920, 921, 922, 923, 924, 925, 926, 927, 928, 929, 930, 931, 932, 933, 934, 935, 936, 937, 938, 939, 940, 941, 942, 943, 944, 945, 946, 947, 948, 949, 950, 951, 952, 953, 954, 955, 956, 957, 958, 959, 960, 961, 962, 963, 964, 965, 966, 967, 968, 969, 970, 971, 972, 973, 974, 975, 976, 977, 978, 979, 980, 981, 982, 983, 984, 985, 986, 987, 988, 989, 990, 991, 992, 993, 994, 995, 996, 997, 998, 999, 1000, 1001, 1002, 1003, 1004, 1005, 1006, 1007, 1008, 1009, 1010, 1011, 1012, 1013, 1014, 1015, 1016, 1017, 1018, 1019, 1020, 1021, 1022, 1023, 1024, 1025, 1026, 1027, 1028, 1029, 1030, 1031, 1032, 1033, 1034, 1035, 1036, 1037, 1038, 1039, 1040, 1041, 1042, 1043, 1044, 1045, 1046, 1047, 1048, 1049, 1050, 1051, 1052, 1053, 1054, 1055, 1056, 1057, 1058, 1059, 1060, 1061, 1062, 1063, 1064, 1065, 1066, 1067, 1068, 1069, 1070, 1071, 1072, 1073, 1074, 1075, 1076, 1077, 1078, 1079, 1080, 1083, 1084, 1085, 1086, 1087, 1088, 1089, 1090, 1091, 1092, 1093, 1094, 1098, 1099, 1100, 1101, 1102, 1103, 1104, 1105, 1106, 1107, 1108, 1109, 1110, 1111, 1112, 1113, 1114, 1115, 1119, 1120, 1121, 1122, 1123, 1124, 1125, 1129, 1130, 1131, 1132, 1133, 1134, 1135, 1136, 1137, 1138, 1139, 1140, 1141, 1142, 1143, 1144, 1145, 1146, 1147, 1148, 1149, 1150, 1151, 1152, 1153, 1154, 1155, 1156, 1157, 1158, 1159, 1160, 1161, 1162, 1163, 1164, 1165, 1166, 1167, 1168, 1169, 1180, 1181, 1182, 1183, 1186, 1187, 1188, 1196, 1197, 1198, 1214, 1215, 1216, 1225, 1226,

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B grade: { 73, 82, 90, 105, 115, 116, 132, 133, 146, 147, 148, 212, 226, 227, 243, 244, 1236, 1246, 1258, 1259, 1268, 1273, 1274, 1275, 1276, 1277, 1278, 1279, 1280, 1281, 1284, 1285, 1288, 1289, 1291, 1292, 1293, 1294, 1295, 1299, 1300, 1301, 1302, 1303, 1304, 1305, 1306, 1307, 1308, 1309, 1310, 1312, 1313, 1314, 1320, 1321, 1322, 1323, 1324, 1325, 1326, 1327, 1328, 1329, 1330, 1331, 1332, 1333, 1362, 1363, 1365, 1366, 1523, 1524, 1526, 1527, 1528, 1534, 1539, 1540, 1542, 1548, 1550, 1558 }

C grade: { 290, 291, 297, 299, 305, 306, 308, 318, 319, 320, 321, 323, 324, 327, 329, 332, 333, 341, 342, 348, 349, 350, 356, 357, 358, 361, 362, 363, 364, 365, 366, 367, 376, 377, 383, 384, 390, 391, 397, 398, 403, 404, 405, 411, 412, 417, 418, 419, 422, 423, 453, 454, 455, 456, 457, 460, 461, 462, 463, 465, 466, 467, 468, 473, 474, 475, 476, 477, 480, 481, 482, 483, 485, 486, 487, 488, 525, 526, 531, 532, 537, 538, 543, 544, 549, 550, 555, 556, 561, 562, 567, 568, 577, 578, 584, 596, 597, 602, 616, 617, 623, 635, 636, 641, 674, 676, 678, 680, 681, 682, 683, 684, 685, 686, 687, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 1081, 1082, 1095, 1096, 1097, 1116, 1117, 1118, 1126, 1127, 1128, 1170, 1171, 1172, 1173, 1174, 1175, 1176, 1177, 1178, 1179, 1184, 1185, 1189, 1190, 1191, 1192, 1193, 1194, 1195, 1199, 1200, 1201, 1202, 1203, 1204, 1205, 1206, 1207, 1208, 1209, 1210, 1211, 1212, 1213, 1217, 1218, 1219, 1220, 1221, 1222, 1223, 1224, 1383, 1384, 1385, 1386, 1394, 1396, 1397, 1398, 1406, 1407, 1409, 1410, 1412, 1421, 1422, 1423, 1430, 1431, 1432, 1433, 1440, 1441, 1442, 1443, 1475, 1476, 1485, 1486, 1487, 1502, 1503, 1504, 1512, 1513, 1514, 1559, 1560, 1561, 1562, 1563, 1564, 1565, 1566, 1567, 1568, 1569, 1570, 1571, 1572, 1573, 1574, 1575, 1576, 1577, 1582, 1583, 1584, 1585, 1586, 1587, 1588, 1589, 1594, 1595, 1596, 1597, 1598, 1599, 1600, 1601, 1602, 1603, 1608, 1609, 1610, 1611, 1612, 1613, 1614, 1615, 1616, 1617, 1622, 1623, 1624, 1625, 1626, 1627, 1628, 1629, 1630, 1631, 1632, 1633, 1634, 1635, 1636, 1637,

1638, 1639, 1640, 1641, 1642, 1643, 1644, 1645, 1646, 1647, 1648, 1649, 1650, 1651, 1652, 1653, 1654, 1655, 1656, 1657, 1658, 1659, 1660, 1661, 1662, 1663, 1664, 1665, 1666, 1667, 1668, 1669, 1670, 1671, 1672, 1673, 1674, 1675, 1676, 1677, 1678, 1679, 1680, 1681, 1686, 1687, 1688, 1689, 1690, 1691, 1692, 1693, 1694, 1695, 1700, 1701, 1702, 1703, 1704, 1705, 1706, 1707, 1712, 1713, 1714, 1715, 1716, 1717, 1718, 1723, 1724, 1725, 1726, 1727, 1728, 1729, 1730, 1736, 1737, 1738, 1739, 1740, 1741, 1742, 1743, 1744, 1745, 1746, 1747, 1748, 1749, 1750, 1751, 1752, 1753, 1754, 1755, 1756, 1757, 1758, 1759, 1760, 1761, 1762, 1763, 1764, 1765, 1772, 1773, 1774, 1779, 1780, 1781, 1798, 1799, 1800, 1805, 1806, 1807, 1824, 1825, 1826, 1831, 1832, 1833 }

F grade: { }

2.1.3 Maple

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 74, 75, 76, 77, 78, 79, 80, 81, 83, 84, 85, 86, 87, 88, 89, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 106, 107, 108, 109, 110, 111, 112, 113, 114, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 331, 332, 333, 334, 335, 336, 337, 338, 339, 340, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 365, 366, 367, 368, 370, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 383, 384, 385, 386, 387, 388, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400, 401, 402, 403, 404, 405, 406, 407, 408, 409, 410, 411, 412, 413, 414, 415, 416, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 428, 429, 430, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 443, 444, 445, 446, 447, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463, 464, 465, 466, 467, 468, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 487, 488, 489, 490, 491, 492, 493, 494, 495, 496, 497, 498, 499, 500, 502, 503, 504, 505, 506, 507, 508, 509, 510, 511, 512, 513, 514, 515, 518, 519, 520, 521, 522, 523, 524, 525, 526, 527, 528, 529, 530, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 545, 546, 547, 548, 549, 550, 551, 552, 553, 554, 557, 558, 559, 560, 561, 562, 563, 564, 565, 566, 567, 568, 569, 570, 571, 573, 574, 575, 576, 577, 580, 581, 582, 583, 586, 587, 588, 589, 590, 591, 592, 594, 595, 596, 599, 600, 601, 604, 605, 606, 607, 608, 609, 610, 612, 613, 614, 615, 616, 618, 619, 620, 621, 622, 624, 625, 626, 627, 628, 629, 630, 631, 633, 634, 637, 638, 639, 640, 642, 643, 644, 645, 646, 647, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 672, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 684, 685, 686, 687, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 698, 702, 703, 719, 720, 724, 725, 728, 732, 733, 734, 735, 739, 740, 741, 750, 753, 754, 755, 756, 757, 758, 759, 760, 761, 762,

763, 764, 765, 766, 767, 768, 769, 770, 771, 772, 773, 774, 775, 776, 777, 778, 779, 780, 781, 782, 783, 784, 785, 786, 787, 788, 789, 790, 791, 792, 793, 794, 795, 796, 797, 798, 799, 800, 801, 802, 803, 804, 805, 806, 807, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823, 824, 825, 826, 827, 828, 829, 830, 831, 832, 833, 834, 835, 836, 837, 838, 839, 840, 841, 842, 843, 844, 845, 846, 847, 848, 849, 850, 851, 852, 853, 854, 855, 856, 857, 858, 859, 860, 861, 862, 863, 864, 865, 866, 867, 868, 869, 870, 871, 872, 873, 874, 875, 876, 877, 878, 879, 880, 881, 882, 883, 884, 885, 886, 887, 888, 889, 890, 891, 892, 893, 894, 895, 896, 897, 898, 899, 900, 901, 902, 903, 904, 905, 906, 907, 908, 909, 910, 911, 912, 913, 914, 915, 916, 917, 918, 919, 920, 921, 922, 923, 924, 925, 926, 930, 931, 932, 933, 934, 938, 939, 940, 941, 942, 943, 946, 947, 948, 949, 953, 954, 955, 956, 961, 962, 963, 964, 969, 970, 971, 972, 973, 974, 975, 976, 977, 978, 979, 980, 987, 988, 989, 990, 991, 992, 993, 994, 995, 996, 999, 1000, 1001, 1002, 1003, 1004, 1005, 1006, 1007, 1008, 1009, 1010, 1011, 1012, 1013, 1014, 1015, 1019, 1020, 1021, 1022, 1023, 1024, 1025, 1026, 1027, 1028, 1029, 1030, 1031, 1032, 1033, 1035, 1036, 1037, 1038, 1039, 1040, 1041, 1042, 1043, 1044, 1045, 1046, 1047, 1048, 1049, 1050, 1051, 1052, 1054, 1055, 1056, 1057, 1058, 1059, 1060, 1061, 1062, 1063, 1064, 1065, 1070, 1071, 1072, 1073, 1074, 1075, 1076, 1077, 1080, 1083, 1084, 1085, 1086, 1087, 1088, 1089, 1090, 1092, 1093, 1094, 1095, 1096, 1097, 1098, 1099, 1100, 1101, 1102, 1103, 1104, 1106, 1107, 1108, 1111, 1112, 1113, 1114, 1115, 1116, 1117, 1120, 1121, 1122, 1123, 1124, 1125, 1126, 1127, 1128, 1130, 1131, 1132, 1133, 1134, 1135, 1136, 1139, 1140, 1141, 1142, 1143, 1144, 1149, 1150, 1151, 1152, 1153, 1157, 1158, 1159, 1160, 1161, 1163, 1164, 1165, 1166, 1167, 1168, 1180, 1181, 1182, 1183, 1186, 1187, 1188, 1196, 1197, 1198, 1214, 1215, 1216, 1226, 1227, 1228, 1229, 1230, 1238, 1239, 1240, 1241, 1242, 1243, 1244, 1245, 1248, 1249, 1250, 1251, 1252, 1253, 1255, 1256, 1257, 1263, 1264, 1270, 1271, 1272, 1282, 1311, 1336, 1337, 1338, 1339, 1340, 1341, 1342, 1346, 1347, 1348, 1349, 1350, 1351, 1356, 1357, 1358, 1359, 1360, 1361, 1368, 1369, 1370, 1371, 1372, 1373, 1374, 1376, 1377, 1378, 1379, 1380, 1381, 1382, 1383, 1384, 1385, 1386, 1388, 1389, 1390, 1391, 1392, 1395, 1396, 1397, 1398, 1400, 1401, 1402, 1403, 1404, 1408, 1409, 1410, 1411, 1412, 1414, 1415, 1416, 1417, 1418, 1419, 1420, 1421, 1422, 1423, 1425, 1426, 1427, 1428, 1429, 1430, 1431, 1432, 1435, 1436, 1437, 1438, 1439, 1440, 1441, 1442, 1443, 1444, 1445, 1446, 1447, 1448, 1449, 1450, 1451, 1452, 1454, 1455, 1456, 1457, 1458, 1459, 1464, 1466, 1467, 1468, 1469, 1470, 1477, 1478, 1479, 1480, 1488, 1489, 1490, 1491, 1495, 1497, 1498, 1499, 1500, 1501, 1506, 1507, 1508, 1509, 1510, 1516, 1517, 1518, 1519, 1520, 1530, 1541, 1544, 1578, 1579, 1580, 1581, 1590, 1591, 1592, 1593, 1604, 1605, 1606, 1607, 1618, 1619, 1620, 1621, 1682, 1683, 1684, 1685, 1696, 1697, 1698, 1699, 1708, 1709, 1710, 1711, 1719, 1720, 1721, 1722, 1775, 1776, 1777, 1778, 1782, 1783, 1784, 1785, 1801, 1802, 1803, 1804, 1808, 1809, 1810, 1811, 1827, 1828, 1829, 1830, 1834, 1835, 1836, 1837, 1844, 1848, 1854, 1855, 1860, 1861, 1868, 1869, 1874, 1875, 1881, 1882, 1883, 1884, 1891, 1892, 1893, 1894, 1895, 1896, 1897, 1898, 1899, 1900, 1901, 1902, 1903, 1904, 1905, 1906, 1907, 1908, 1909, 1910, 1911, 1912, 1913, 1914, 1915, 1916, 1917 }

B grade: { 73, 82, 90, 105, 115, 116, 132, 133, 146, 147, 148, 199, 212, 213, 226, 227, 228, 243, 244, 442, 516, 517, 543, 544, 572, 578, 584, 593, 597, 602, 611, 617, 623, 632, 635, 636, 641, 648, 649, 699, 700, 701, 1016, 1017, 1018, 1034, 1053, 1066, 1067, 1068, 1069, 1078, 1079, 1081, 1082, 1091, 1105, 1109, 1110, 1118, 1119, 1129, 1137, 1138, 1145, 1146, 1147, 1148, 1154, 1155, 1156, 1162, 1169, 1225, 1236, 1237, 1246, 1247, 1254, 1258, 1259, 1260, 1261, 1262, 1265, 1266, 1267, 1268, 1269, 1273, 1274, 1275, 1276, 1277, 1278, 1279, 1280, 1281, 1283, 1284, 1285, 1286, 1287, 1288, 1289, 1290, 1291, 1292, 1293, 1294, 1295, 1296, 1297, 1298, 1299, 1300, 1301, 1302, 1303, 1304, 1305, 1306, 1307, 1308, 1309, 1310, 1312, 1313, 1314, 1315, 1316, 1317, 1318, 1319, 1320, 1321, 1322, 1323, 1324, 1325, 1326, 1327, 1328, 1329, 1330, 1331, 1332, 1333, 1334, 1335, 1343, 1344, 1345, 1352, 1353, 1354, 1355, 1362, 1363, }

1364, 1365, 1366, 1367, 1375, 1387, 1393, 1394, 1399, 1405, 1406, 1407, 1413, 1424, 1433, 1434, 1453, 1460, 1461, 1462, 1463, 1471, 1472, 1473, 1474, 1481, 1482, 1483, 1484, 1492, 1493, 1494, 1496, 1511, 1521, 1522, 1523, 1524, 1525, 1526, 1527, 1528, 1529, 1531, 1532, 1533, 1534, 1535, 1536, 1537, 1538, 1539, 1540, 1542, 1543, 1545, 1546, 1547, 1548, 1549, 1550, 1551, 1552, 1553, 1554, 1555, 1556, 1557, 1558, 1846, 1847, 1852, 1853, 1859, 1870, 1871, 1876, 1877 }

C grade: { 721, 722, 726, 727, 1171, 1172, 1174, 1175, 1176, 1177, 1178, 1184, 1194, 1195, 1206, 1207, 1208, 1209, 1210, 1211, 1212, 1213, 1217, 1218, 1219, 1220, 1222, 1223, 1224, 1628 }

F grade: { 369, 501, 531, 532, 555, 556, 579, 585, 598, 603, 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 723, 729, 730, 731, 736, 737, 738, 742, 743, 744, 745, 746, 747, 748, 749, 751, 752, 927, 928, 929, 935, 936, 937, 944, 945, 950, 951, 952, 957, 958, 959, 960, 965, 966, 967, 968, 981, 982, 983, 984, 985, 986, 997, 998, 1170, 1173, 1179, 1185, 1189, 1190, 1191, 1192, 1193, 1199, 1200, 1201, 1202, 1203, 1204, 1205, 1221, 1231, 1232, 1233, 1234, 1235, 1465, 1475, 1476, 1485, 1486, 1487, 1502, 1503, 1504, 1505, 1512, 1513, 1514, 1515, 1559, 1560, 1561, 1562, 1563, 1564, 1565, 1566, 1567, 1568, 1569, 1570, 1571, 1572, 1573, 1574, 1575, 1576, 1577, 1582, 1583, 1584, 1585, 1586, 1587, 1588, 1589, 1594, 1595, 1596, 1597, 1598, 1599, 1600, 1601, 1602, 1603, 1608, 1609, 1610, 1611, 1612, 1613, 1614, 1615, 1616, 1617, 1622, 1623, 1624, 1625, 1626, 1627, 1629, 1630, 1631, 1632, 1633, 1634, 1635, 1636, 1637, 1638, 1639, 1640, 1641, 1642, 1643, 1644, 1645, 1646, 1647, 1648, 1649, 1650, 1651, 1652, 1653, 1654, 1655, 1656, 1657, 1658, 1659, 1660, 1661, 1662, 1663, 1664, 1665, 1666, 1667, 1668, 1669, 1670, 1671, 1672, 1673, 1674, 1675, 1676, 1677, 1678, 1679, 1680, 1681, 1686, 1687, 1688, 1689, 1690, 1691, 1692, 1693, 1694, 1695, 1700, 1701, 1702, 1703, 1704, 1705, 1706, 1707, 1712, 1713, 1714, 1715, 1716, 1717, 1718, 1723, 1724, 1725, 1726, 1727, 1728, 1729, 1730, 1731, 1732, 1733, 1734, 1735, 1736, 1737, 1738, 1739, 1740, 1741, 1742, 1743, 1744, 1745, 1746, 1747, 1748, 1749, 1750, 1751, 1752, 1753, 1754, 1755, 1756, 1757, 1758, 1759, 1760, 1761, 1762, 1763, 1764, 1765, 1766, 1767, 1768, 1769, 1770, 1771, 1772, 1773, 1774, 1779, 1780, 1781, 1786, 1787, 1788, 1789, 1790, 1791, 1792, 1793, 1794, 1795, 1796, 1797, 1798, 1799, 1800, 1805, 1806, 1807, 1812, 1813, 1814, 1815, 1816, 1817, 1818, 1819, 1820, 1821, 1822, 1823, 1824, 1825, 1826, 1831, 1832, 1833, 1838, 1839, 1840, 1841, 1842, 1843, 1845, 1849, 1850, 1851, 1856, 1857, 1858, 1862, 1863, 1864, 1865, 1866, 1867, 1872, 1873, 1878, 1879, 1880, 1885, 1886, 1887, 1888, 1889, 1890 }

2.1.4 Maxima

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 69, 70, 71, 72, 74, 75, 76, 77, 78, 79, 80, 81, 84, 85, 86, 87, 88, 89, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 106, 107, 108, 109, 110, 111, 112, 113, 114, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 217, 218, 219, 220, 221, 222, 223, 224, 225, 230, 234, 235, 236, 237, 238, 239, 240, 241, 242, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304,

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B grade: { 68, 73, 82, 83, 90, 105, 115, 116, 132, 133, 146, 147, 148, 186, 199, 212, 213, 214, 215, 216, 226, 227, 228, 229, 231, 232, 233, 243, 244, 489, 490, 491, 492, 505, 506, 507, 508, 521, 522, 523,

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C grade: { 1027 }

F grade: { 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 730, 731, 736, 737, 738, 739, 740, 741, 742, 743, 744, 745, 746, 747, 748, 749, 750, 751, 752, 754, 755, 760, 761, 762, 763, 769, 770, 771, 778, 779, 808, 809, 810, 811, 817, 818, 819, 824, 825, 826, 827, 856, 927, 928, 929, 935, 936, 937, 944, 945, 950, 951, 952, 957, 958, 959, 960, 965, 966, 967, 968, 981, 982, 983, 984, 985, 986, 987, 988, 989, 990, 992, 993, 994, 995, 996, 997, 998, 1170, 1171, 1172, 1173, 1174, 1175, 1176, 1177, 1178, 1179, 1180, 1181, 1182, 1183, 1184, 1185, 1186, 1187, 1188, 1189, 1190, 1191, 1192, 1193, 1194, 1195, 1196, 1197, 1198, 1199, 1200, 1201, 1202, 1203, 1204, 1205, 1206, 1207, 1208, 1209, 1210, 1211, 1212, 1213, 1214, 1215, 1216, 1217, 1218, 1219, 1220, 1221, 1222, 1223, 1224, 1225, 1226, 1227, 1228, 1231, 1232, 1233, 1234, 1235, 1381, 1382, 1383, 1384, 1385, 1386, 1393, 1394, 1395, 1396, 1397, 1398, 1405, 1406, 1407, 1408, 1409, 1410, 1419, 1420, 1421, 1422, 1423, 1430, 1431, 1432, 1433, 1440, 1441, 1442, 1443, 1458, 1459, 1460, 1461, 1462, 1463, 1464, 1465, 1466, 1467, 1468, 1469, 1470, 1471, 1472, 1473, 1474, 1475, 1476, 1477, 1478, 1479, 1480, 1481, 1482, 1483, 1484, 1485, 1486, 1487, 1488, 1489, 1490, 1491, 1492, 1493, 1494, 1495, 1496, 1497, 1498, 1499, 1500, 1501, 1502, 1503, 1504, 1505, 1506, 1507, 1508, 1509, 1510, 1511, 1512, 1513, 1514, 1515, 1516, 1517, 1518, 1519, 1520, 1521, 1551, 1554, 1558, 1559, 1560, 1561, 1562, 1563, 1564, 1565, 1566, 1567, 1568, 1569, 1570, 1571, 1572, 1573, 1574, 1575, 1576, 1577, 1578, 1579, 1580, 1581, 1582, 1583, 1584, 1585, 1586, 1587, 1588, 1589, 1590, 1591, 1592, 1593, 1594, 1595, 1596, 1597, 1598, 1599, 1600, 1601, 1602, 1603, 1604, 1605, 1606, 1607, 1608, 1609, 1610, 1611, 1612, 1613, 1614, 1615, 1616, 1617, 1618, 1619, 1620, 1621, 1622, 1623, 1624, 1625, 1626, 1627, 1628, 1629, 1630, 1631, 1632, 1633, 1634, 1635, 1636, 1637, 1638, 1639, 1640, 1641, 1642, 1643, 1644, 1645, 1646, 1647, 1648, 1649, 1650, 1651, 1652, 1653, 1654, 1655, 1656, 1657, 1658, 1659, 1660, 1661, 1662, 1663, 1664, 1665, 1666, 1667, 1668, 1669, 1670, 1671, 1672, 1673, 1674, 1675, 1676, 1677, 1678, 1679, 1680, 1681, 1682, 1683, 1684, 1685, 1686, 1687, 1688, 1689, 1690, 1691, 1692, 1693, 1694, 1695, 1696, 1697, 1698, 1699, 1700, 1701, 1702, 1703, 1704, 1705, 1706, 1707, 1708, 1709, 1710, 1711, 1712, 1713, 1714, 1715, 1716, 1717, 1718, 1719, 1720, 1721, 1722, 1723, 1724, 1725, 1726, 1727, 1728, 1729, 1730, 1731, 1732, 1733, 1734, 1735, 1736, 1737, 1738, 1739, 1740, 1741, 1742, 1743, 1744, 1745, 1746, 1747, 1748, 1749, 1750, 1751, 1752, 1753, 1754, 1755, 1756, 1757, 1758, 1759, 1760, 1761, 1762, 1763, 1764, 1765, 1766, 1767, 1768, 1769, 1770, 1771, 1772, 1773, 1774, 1775, 1776, 1777, 1778, 1779, 1780, 1781, 1782, 1783, 1784, 1785, 1786, 1787, 1788, 1789, 1790, 1791, 1792, 1793, 1794, 1795, 1796, 1797, 1798, 1799, 1800, 1801, 1802, 1803, 1804, 1805, 1806, 1807, 1808, 1809, 1810, 1811, 1812, 1813, 1814, 1815, 1816, 1817, 1818, 1819, 1820, 1821, 1822, 1823, 1824, 1825, 1826, 1827, 1828, 1829, 1830, 1831, 1832, 1833, 1834, 1835, 1836,

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2.1.5 FriCAS

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 39, 40, 41, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 69, 70, 71, 72, 74, 75, 76, 77, 78, 79, 80, 81, 84, 85, 86, 87, 88, 89, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 107, 108, 109, 110, 111, 112, 113, 114, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 200, 204, 205, 206, 207, 208, 209, 210, 211, 222, 223, 230, 239, 240, 241, 242, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 296, 297, 298, 299, 300, 301, 302, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 331, 332, 333, 334, 335, 336, 337, 338, 339, 340, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 357, 358, 359, 360, 361, 362, 363, 364, 365, 366, 367, 368, 369, 370, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 383, 384, 385, 386, 387, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400, 401, 402, 403, 404, 405, 406, 407, 408, 409, 412, 413, 414, 415, 416, 417, 419, 420, 421, 422, 423, 424, 425, 426, 427, 428, 429, 430, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 443, 444, 445, 446, 447, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463, 464, 465, 466, 467, 468, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 487, 488, 489, 490, 491, 492, 493, 494, 495, 496, 497, 498, 499, 500, 501, 502, 503, 504, 505, 506, 507, 508, 509, 510, 511, 512, 513, 514, 515, 516, 517, 518, 519, 520, 521, 522, 523, 524, 525, 526, 527, 528, 529, 530, 531, 532, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 543, 544, 545, 546, 547, 548, 549, 550, 551, 552, 553, 554, 555, 556, 557, 558, 559, 560, 561, 562, 563, 564, 565, 566, 567, 568, 569, 570, 571, 572, 573, 574, 575, 576, 577, 578, 579, 580, 581, 582, 583, 584, 585, 587, 588, 589, 590, 591, 592, 593, 594, 595, 596, 597, 598, 599, 600, 601, 602, 603, 605, 606, 607, 608, 609, 610, 611, 612, 613, 614, 615, 616, 617, 618, 619, 620, 621, 622, 623, 624, 626, 627, 628, 629, 630, 631, 632, 633, 634, 635, 636, 637, 638, 639, 640, 641, 642, 644, 645, 646, 647, 649, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 672, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 688, 696, 698, 702, 703, 732, 733, 734, 735, 739, 740, 741, 753, 754, 755, 756, 757, 758, 759, 760, 761, 762, 763, 764, 765, 766, 767, 768, 769, 770, 771, 772, 773, 774, 775, 776, 777, 778, 779, 780, 781, 782, 783, 784, 785, 786, 787, 788, 789, 790, 791, 792, 793, 794, 795, 796, 797, 798, 799, 800, 801, 802, 803, 804, 805, 806, 807, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823, 824, 825, 826, 827, 828, 829, 830, 831, 832, 833, 834, 835, 836, 837, 838, 839, 840, 841, 842, 843, 844, 845, 846, 847, 848, 849, 850, 851, 852, 853, 854, 855, 856, 857, 858, 859, 860, 861, 862, 863, 864, 865, 866, 867, 868, 869, 870, 871, 872, 873, 874, 875, 876, 877, 878, 879, 880, 881, 882, 883, 884, 885, 886, 887, 888, 889, 890, 891, 892, 893, 894, 895, 896, 897, 898, 899, 900, 901, 902, 903, 904, 905, 906, 907, 908, 909, 910, 911, 912, 913, 914, 915, 916, 917, 918, 919, 920, 921, 922, 923, 924, 925, 926, 930, 931, 932, 933, 934, 938, 939, 940, 941, 942, 943, 946, 947, 948, 949, 953, 954,

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B grade: { 37, 38, 42, 68, 73, 82, 83, 90, 105, 106, 115, 116, 132, 133, 134, 146, 147, 148, 186, 199, 201, 202, 203, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 224, 225, 226, 227, 228, 229, 231, 232, 233, 234, 235, 236, 237, 238, 243, 244, 295, 303, 314, 315, 316, 355, 356, 388, 410, 411, 418, 442, 586, 604, 625, 643, 648, 684, 685, 686, 687, 689, 690, 691, 692, 693, 694, 695, 697, 699, 700, 701, 999, 1004, 1005, 1006, 1007, 1012, 1013, 1014, 1015, 1016, 1017, 1018, 1019, 1020, 1026, 1034, 1037, 1045, 1068, 1069, 1070, 1082, 1083, 1084, 1098, 1099, 1100, 1101, 1109, 1110, 1119, 1129, 1130, 1156, 1162, 1170, 1225, 1236, 1237, 1246, 1247, 1254, 1257, 1258, 1259, 1260, 1261, 1262, 1263, 1265, 1266, 1267, 1268, 1269, 1270, 1271, 1272, 1273, 1274, 1275, 1276, 1277, 1278, 1279, 1280, 1281, 1282, 1283, 1284, 1285, 1286, 1287, 1288, 1289, 1290, 1291, 1292, 1293, 1294, 1295, 1296, 1297, 1298, 1299, 1300, 1301, 1302, 1303, 1304, 1305, 1306, 1307, 1308, 1309, 1310, 1311, 1312, 1313, 1314, 1315, 1316, 1317, 1318, 1319, 1320, 1321, 1322, 1323, 1324, 1325, 1326, 1327, 1328, 1329, 1330, 1331, 1332, 1333, 1334, 1342, 1343, 1344, 1345, 1350, 1351, 1352, 1353, 1354, 1355, 1359, 1360, 1361, 1362, 1363, 1364, 1365, 1366, 1367, 1368, 1369, 1370, 1371, 1372, 1373, 1374, 1375, 1376, 1383, 1384, 1385, 1386, 1387, 1388, 1389, 1390, 1391, 1392, 1395, 1396, 1397, 1398, 1399, 1400, 1401, 1402, 1403, 1404, 1408, 1409, 1410, 1420, 1421, 1422, 1423, 1424, 1431, 1432, 1433, 1434, 1439, 1440, 1441, 1442, 1443, 1444, 1445, 1446, 1447, 1448, 1453, 1458, 1459, 1465, 1466, 1467, 1468, 1469, 1470, 1476, 1477, 1478, 1479, 1480, 1481, 1486, 1487, 1488, 1489, 1490, 1491, 1496, 1498, 1499, 1500, 1501, 1502, 1505, 1507, 1508, 1509, 1510, 1511, 1512, 1513, 1514, 1515, 1516, 1517, 1518, 1519, 1520, 1521, 1522, 1527, 1529, 1531, 1534, 1536, 1537, 1538, 1539, 1540, 1543, 1545, 1548, 1550, 1551, 1553, 1554, 1555, 1557, 1558, 1576, 1577, 1578, 1579, 1580, 1581, 1587, 1588, 1589, 1591, 1592, 1593, 1601, 1602, 1603, 1605, 1606, 1607, 1615, 1617, 1619, 1620, 1621, 1678, 1679, 1680, 1681, 1682, 1683, 1684, 1685, 1693, 1694, 1695, 1697, 1698, 1699, 1705, 1706, 1707, 1709, 1710, 1711, 1717, 1718, 1720, 1721, 1722, 1730, 1772, 1773, 1774, 1775, 1776, 1777, 1778, 1779, 1780, 1781, 1782, 1783, 1784, 1785, 1798, 1799, 1800, 1801, 1802, 1803, 1804, 1805, 1806, 1807,

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C grade: { }

F grade: { 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 730, 731, 736, 737, 738, 742, 743, 744, 745, 746, 747, 748, 749, 750, 751, 752, 927, 928, 929, 935, 936, 937, 944, 945, 950, 951, 952, 957, 958, 959, 960, 965, 966, 967, 968, 981, 982, 983, 984, 985, 986, 997, 998, 1171, 1172, 1173, 1174, 1175, 1176, 1177, 1189, 1190, 1191, 1192, 1193, 1199, 1200, 1201, 1202, 1203, 1204, 1205, 1206, 1207, 1208, 1209, 1210, 1211, 1217, 1218, 1219, 1220, 1221, 1222, 1223, 1231, 1232, 1233, 1234, 1235, 1559, 1560, 1561, 1562, 1563, 1564, 1565, 1566, 1567, 1568, 1569, 1570, 1571, 1572, 1573, 1574, 1582, 1583, 1584, 1585, 1586, 1594, 1595, 1596, 1597, 1598, 1599, 1600, 1608, 1609, 1610, 1611, 1612, 1613, 1614, 1622, 1623, 1624, 1625, 1626, 1627, 1629, 1630, 1631, 1632, 1633, 1634, 1635, 1636, 1637, 1638, 1639, 1640, 1641, 1642, 1643, 1644, 1645, 1646, 1647, 1648, 1649, 1650, 1651, 1652, 1653, 1654, 1655, 1656, 1657, 1658, 1659, 1660, 1661, 1662, 1663, 1664, 1665, 1666, 1667, 1668, 1669, 1670, 1671, 1672, 1673, 1674, 1675, 1676, 1677, 1686, 1687, 1688, 1689, 1690, 1691, 1692, 1700, 1701, 1702, 1703, 1704, 1712, 1713, 1714, 1715, 1716, 1723, 1724, 1725, 1726, 1727, 1728, 1731, 1732, 1733, 1734, 1735, 1736, 1737, 1738, 1739, 1740, 1741, 1742, 1743, 1744, 1745, 1746, 1747, 1748, 1749, 1750, 1751, 1752, 1753, 1754, 1755, 1756, 1757, 1758, 1759, 1760, 1761, 1762, 1763, 1764, 1765, 1766, 1767, 1768, 1769, 1770, 1771, 1786, 1787, 1788, 1789, 1790, 1791, 1792, 1793, 1794, 1795, 1796, 1797, 1812, 1813, 1814, 1815, 1816, 1817, 1818, 1819, 1820, 1821, 1822, 1823, 1838, 1839, 1840, 1841, 1842, 1843, 1845, 1849, 1850, 1851, 1856, 1857, 1858, 1862, 1863, 1864, 1865, 1866, 1867, 1872, 1873, 1878, 1879, 1880, 1885, 1886, 1887, 1888, 1889, 1890 }

2.1.6 Sympy

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 69, 70, 71, 72, 74, 75, 76, 77, 78, 79, 80, 81, 84, 85, 86, 87, 88, 89, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 107, 108, 109, 110, 111, 112, 113, 114, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 200, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 218, 219, 220, 221, 222, 223, 224, 225, 235, 236, 237, 238, 239, 240, 241, 242, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 287, 289, 290, 291, 294, 295, 296, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 326, 327, 330, 333, 338, 339, 340, 341, 342, 346, 347, 349, 350, 352, 353, 354, 355, 359, 361, 363, 364, 370, 374, 381, 387, 388, 395, 402, 409, 415, 416, 428, 429, 430, 431, 432, 433, 434, 435, 436, 437, 439, 440, 441, 442, 443, 444, 446, 447, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463, 464, 465, 466, 467, 468, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 487, 488, 489, 490, 491, 492, 493, 495, 497, 498, 499, 500, 501, 503, 505, 506, 507, 508, 509, 511, 513, 514, 515, 516, 519, 521, 522, 523, 524, 525, 526, 527, 528, 529, 530, 531, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 543, 545, 546, 547, 548, 549, 550, 551, 552, 553,

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B grade: { 55, 68, 73, 82, 83, 90, 91, 104, 105, 106, 115, 116, 131, 132, 133, 134, 146, 147, 148, 186, 187, 199, 201, 212, 213, 214, 215, 216, 217, 226, 227, 228, 229, 230, 231, 232, 233, 234, 243, 244, 284, 285, 286, 288, 292, 293, 297, 325, 329, 334, 335, 336, 337, 343, 344, 345, 348, 351, 356, 357, 358, 360, 367, 371, 372, 373, 378, 379, 380, 385, 386, 392, 393, 394, 406, 407, 408, 413, 414, 494, 496, 502, 504, 510, 512, 518, 520, 575, 576, 582, 583, 584, 585, 586, 587, 588, 589, 601, 602, 603, 604, 606, 607, 614, 615, 621, 622, 623, 624, 626, 627, 628, 640, 641, 642, 643, 645, 646, 736, 737, 738, 808, 818, 826, 830, 834, 836, 840, 846, 999, 1004, 1005, 1006, 1007, 1012, 1013, 1014, 1016, 1017, 1018, 1019, 1020, 1021, 1026, 1034, 1036, 1037, 1041, 1045, 1047, 1048, 1053, 1066, 1067, 1068, 1071, 1072, 1073, 1074, 1077, 1078, 1079, 1082, 1083, 1084, 1085, 1086, 1091, 1092, 1096, 1097, 1098, 1099, 1100, 1109, 1110, 1119, 1122, 1123, 1124, 1125, 1133, 1134, 1135, 1155, 1157, 1164, 1236, 1237, 1245, 1246, 1247, 1250, 1254, 1256, 1257, 1258, 1259, 1260, 1261, 1262, 1263, 1268, 1269, 1270, 1271, 1272, 1273, 1274, 1275, 1276, 1277, 1278, 1279, 1280, 1281, 1282, 1283, 1284, 1285, 1286, 1287, 1288, 1299, 1300, 1301, 1302, 1303, 1304, 1305, 1306, 1307, 1308, 1309, 1310, 1311, 1312, 1313, 1314, 1315, 1334, 1340, 1341, 1342, 1349, 1350, 1351, 1352, 1353, 1358, 1359, 1360, 1361, 1366, 1367, 1368, 1369, 1370, 1371, 1372, 1373, 1374, 1375, 1382, 1844, 1881 }

C grade: { 328, 331, 332, 362, 368, 369, 375, 376, 377, 382, 383, 384, 389, 390, 391, 396, 397, 398, 399, 400, 401, 403, 404, 405, 410, 411, 412, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 517, 532, 544, 556, 568, 605, 644, 661, 662, 663, 664, 665, 669, 670, 671, 672, 673, 698, 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 730, 731, 743, 745, 746, 747, 748, 750, 751, 752, 1027, 1112, 1113, 1114, 1115, 1127, 1128, 1129, 1140, 1141, 1142, 1143, 1148, 1149, 1150, 1151, 1166, 1168, 1169, 1233, 1234, 1235, 1455, 1527, 1534, 1537, 1539, 1541, 1548, 1550, 1628, 1885, 1886, 1887, 1888, 1889 }

F grade: { 365, 366, 438, 445, 682, 683, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 739, 740, 741, 742, 744, 749, 753, 761, 762, 771, 783, 784, 789, 790, 796, 809, 810, 811, 819, 827, 831, 832, 833, 837, 838, 839, 844, 845, 852, 853, 854, 855, 856, 857, 858, 859, 860, 861, 862, 863, 864, 865, 866, 867, 868, 869, 870, 871, 872, 873, 874, 875, 876, 877, 878, 879, 880, 881, 882, 883, 884, 885, 886, 887, 888, 889, 890, 891, 892, 893, 894, 895, 896, 898, 899, 900, 901, 902, 903, 904, 906, 907, 908, 909, 910, 911, 912, 914, 915, 916, 917, 918, 920, 921, 922, 923, 924, 925, 926, 927, 928, 929, 930, 931, 932, 933, 934, 935, 936, 937, 938, 939, 940, 941, 942, 943, 944, 945, 946, 947, 948, 949, 950, 951, 952, 953, 954, 955, 956, 957, 958, 959, 960, 961, 962, 963, 964, 965, 966, 967, 968, 969, 970, 971, 972, 973, 974, 975, 976, 977, 978, 979, 980, 981, 982, 983, 984, 985, 986, 987, 988, 989, 990, 992, 993, 994, 995, 996, 997, 998, 1087, 1088, 1101, 1102, 1103, 1136, 1137, 1138, 1139, 1144, 1145, 1146, 1147, 1152, 1153, 1154, 1158, 1159, 1170, 1171, 1172, 1174, 1175, 1176, 1177, 1178, 1179, 1180, 1181, 1182, 1183, 1184, 1185, 1186, 1187, 1188, 1189, 1190, 1192, 1193, 1194, 1195, 1196, 1197, 1198, 1199, 1200, 1201, 1202, 1204, 1205, 1206, 1207, 1208, 1210, 1211, 1212, 1213, 1214, 1215, 1216, 1217, 1218, 1219, 1220, 1222, 1223, 1224, 1225, 1226, 1227, 1228, 1231, 1232, 1289, 1290, 1291, 1292, 1293, 1294, 1295, 1296, 1297, 1298, 1316, 1317, 1318, 1319, 1320, 1321, 1322, 1323, 1324, 1325, 1326, 1327, 1328, 1329, 1330, 1331, 1332, 1333, 1362, 1363, 1364, 1365, 1383, 1384, 1385, 1386, 1394, 1395, 1396, 1397, 1398, 1406, 1407, 1408, 1409, 1410, 1420, 1421, 1422, 1423, 1431, 1432, 1433, 1441, 1442, 1443, 1458, 1459, 1460, 1461, 1462, 1463, 1464, 1465, 1466, 1467, 1468, 1469, 1470, 1471, 1472, 1473, 1474, 1475, 1476, 1477, 1478, 1479, 1480, 1481, 1482, 1483, 1484, 1485, 1486, 1487, 1488, 1489, 1490, 1491, 1492, 1493, 1494, 1495, 1496, 1497, 1498, 1499, 1500, 1501, 1502, 1503, 1504, 1505, 1506, 1507, 1508, 1509, 1510, 1511, 1512, 1513, 1514, 1515, 1516, 1517, 1518, 1519, 1520, 1521, 1522, 1523, 1524, 1526, 1528, 1529, 1531, 1533, 1535, 1536, 1538, 1540, 1542, 1543, 1545, 1547, 1549, 1551, 1554, 1558, 1559, 1560, 1561, 1562, 1563, 1564, 1565, 1566, 1567, 1568, 1569, 1570, 1571, 1572, 1573, 1574, 1575, 1576, 1577, 1578, 1579, 1580, 1581, 1582, 1583, 1584, 1585, 1586, 1587, 1588, 1589, 1590, 1591, 1592, 1593, 1594, 1595, 1596, 1597, 1598, 1599, 1600, 1601, 1602, 1603, 1604, 1605, 1606, 1607, 1608, 1609, 1610, 1611, 1612, 1613, 1614, 1615, 1616, 1617, 1618, 1619, 1620, 1621, 1622, 1623, 1624, 1625, 1626, 1627, 1629, 1630, 1631, 1632, 1633, 1634, 1635, 1636, 1637, 1638, 1639, 1640, 1641, 1643, 1644, 1645, 1646, 1647, 1648, 1649, 1650, 1651, 1652, 1653, 1654, 1655, 1656, 1657, 1658, 1659, 1660, 1661, 1662, 1663, 1664, 1665, 1666, 1667, 1668, 1669, 1670, 1671, 1672, 1673, 1674, 1675, 1676, 1677, 1678, 1679, 1680, 1681, 1682, 1683, 1684, 1685, 1686, 1687, 1688, 1689, 1690, 1691, 1692, 1693, 1694, 1695, 1696, 1697, 1698, 1699, 1700, 1701, 1702, 1703, 1704, 1705, 1706, 1707, 1708, 1709, 1710, 1711, 1712, 1713, 1714, 1715, 1716, 1717, 1718, 1719, 1720, 1721, 1722, 1723, 1724, 1725, 1726, 1727, 1728, 1729, 1730, 1731, 1732, 1733, 1734, 1735, 1736, 1737, 1738, 1739, 1740, 1741, 1742, 1743, 1744, 1745, 1746, 1747, 1748, 1749, 1750, 1751, 1752, 1753, 1754, 1755, 1756, 1757, 1758, 1759, 1760, 1761, 1762, 1763, 1764, 1765, 1766, 1767, 1768, 1769, 1770, 1771, 1772, 1773, 1774, 1775, 1776, 1777, 1778, 1779, 1780, 1781, 1782, 1783, 1784, 1785, 1786, 1787, 1788, 1789, 1790, 1791, 1792, 1793, 1794, 1795, 1796, 1797, 1798, 1799, 1800, 1801, 1802, 1803, 1804, 1805, 1806, 1807, 1808, 1809, 1810, 1811, 1812, 1813, 1814, 1815, 1816, 1817, 1818, 1819, 1820, 1821, 1822, 1823, 1824, 1825, 1826, 1827, 1828, 1829, 1830, 1831, 1832, 1833, 1834, 1835, 1836, 1837, 1838, 1839, 1840, 1841, 1842, 1843, 1845, 1849, 1850, 1851, 1856, 1857, 1858, 1859, 1860, 1861, 1862, 1863, 1864, 1865, 1866, 1867, 1868, 1869, 1870, 1871, 1872, 1873, 1874, 1875, 1876, 1877, 1878, 1879, 1880, 1882, 1883, 1884, 1890 }

2.1.7 Giac

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 74, 75, 76, 77, 78, 79, 80, 81, 83, 84, 85, 86, 87, 88, 89, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 106, 107, 108, 109, 110, 111, 112, 113, 114, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 287, 288, 289, 290, 291, 296, 297, 298, 299, 304, 305, 306, 307, 308, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 331, 332, 333, 334, 335, 336, 337, 338, 339, 340, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 365, 366, 367, 370, 374, 375, 376, 377, 381, 382, 383, 384, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400, 401, 402, 403, 404, 405, 406, 407, 408, 409, 410, 411, 412, 413, 414, 415, 416, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 428, 429, 430, 431, 432, 433, 434, 436, 437, 438, 439, 440, 441, 443, 444, 445, 446, 447, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463, 464, 465, 466, 467, 468, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 487, 488, 495, 496, 503, 504, 511, 512, 519, 520, 574, 575, 576, 577, 583, 595, 613, 614, 615, 616, 634, 647, 648, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 672, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 684, 685, 686, 687, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 698, 703, 734, 735, 756, 757, 758, 759, 760, 761, 762, 763, 764, 765, 766, 767, 768, 769, 770, 771, 772, 773, 774, 775, 776, 777, 778, 779, 780, 781, 782, 783, 788, 789, 790, 796, 804, 805, 806, 807, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823, 824, 825, 826, 827, 828, 829, 830, 831, 832, 836, 837, 838, 844, 852, 853, 854, 855, 856, 860, 861, 862, 863, 864, 869, 870, 871, 872, 873, 874, 877, 878, 879, 880, 881, 882, 885, 886, 887, 888, 889, 890, 893, 894, 895, 896, 897, 901, 902, 903, 904, 905, 909, 910, 913, 914, 915, 916, 917, 918, 919, 920, 921, 922, 926, 933, 934, 1000, 1001, 1002, 1003, 1004, 1005, 1006, 1008, 1009, 1010, 1011, 1012, 1013, 1014, 1020, 1021, 1022, 1024, 1025, 1026, 1028, 1029, 1030, 1031, 1032, 1034, 1035, 1036, 1037, 1038, 1039, 1040, 1041, 1042, 1043, 1044, 1045, 1046, 1047, 1048, 1049, 1050, 1051, 1052, 1054, 1055, 1056, 1057, 1058, 1059, 1060, 1061, 1062, 1064, 1066, 1068, 1069, 1070, 1071, 1072, 1073, 1074, 1077, 1079, 1080, 1081, 1082, 1083, 1084, 1085, 1086, 1087, 1094, 1095, 1096, 1097, 1098, 1099, 1100, 1101, 1102, 1103, 1104, 1105, 1106, 1107, 1108, 1109, 1111, 1112, 1113, 1114, 1115, 1116, 1117, 1123, 1124, 1125, 1126, 1127, 1136, 1140, 1155, 1156, 1160, 1161, 1162, 1163, 1164, 1230, 1238, 1239, 1240, 1241, 1242, 1243, 1244, 1245, 1248, 1249, 1250, 1251, 1252, 1253, 1255, 1256, 1257, 1263, 1264, 1266, 1267, 1270, 1271, 1272, 1282, 1311, 1335, 1336, 1337, 1338, 1339, 1340, 1341, 1346, 1347, 1348, 1349, 1350, 1354, 1355, 1356, 1357, 1358, 1368, 1369, 1370, 1371, 1380, 1381, 1382, 1383, 1384, 1393, 1394, 1395, 1396, 1397, 1405, 1406, 1407, 1408, 1409, 1411, 1412, 1414, 1415, 1416, 1417, 1418, 1419, 1420, 1421, 1422, 1426, 1427, 1428, 1429, 1430, 1431, 1436, 1437, 1438, 1439, 1440, 1451, 1452, 1454, 1455, 1456, 1457, 1458, 1459, 1464, 1492, 1493, 1494, 1495, 1496, 1503, 1504, 1505, 1506, 1516, 1522, 1523, 1524, 1525, 1526, 1528, 1529, 1530, 1531, 1532, 1533,

1535, 1536, 1537, 1538, 1539, 1540, 1543, 1544, 1545, 1546, 1547, 1549, 1551, 1552, 1553, 1554, 1555, 1556, 1557, 1558, 1855, 1881, 1891, 1892, 1893, 1894, 1895, 1896, 1897, 1898, 1899, 1900, 1901, 1902, 1903, 1904, 1905, 1906, 1907, 1908, 1909, 1910, 1911, 1912, 1913, 1914, 1915, 1916, 1917 }

B grade: { 37, 38, 73, 82, 90, 105, 115, 116, 132, 133, 146, 147, 148, 212, 226, 227, 243, 244, 284, 285, 286, 292, 293, 294, 295, 300, 301, 302, 303, 309, 310, 311, 312, 313, 314, 315, 316, 371, 372, 373, 378, 379, 380, 385, 386, 387, 388, 435, 442, 494, 502, 510, 518, 573, 578, 579, 580, 581, 582, 584, 585, 586, 587, 588, 589, 594, 596, 597, 598, 599, 600, 601, 602, 603, 604, 605, 606, 607, 612, 617, 618, 619, 620, 621, 622, 623, 624, 625, 626, 627, 628, 633, 635, 636, 637, 638, 639, 640, 641, 642, 643, 644, 645, 646, 699, 700, 701, 702, 732, 733, 784, 911, 912, 923, 924, 925, 930, 931, 938, 987, 989, 999, 1007, 1015, 1016, 1017, 1018, 1019, 1023, 1033, 1053, 1063, 1065, 1067, 1075, 1076, 1078, 1088, 1089, 1090, 1091, 1092, 1093, 1110, 1118, 1119, 1120, 1121, 1122, 1128, 1129, 1130, 1131, 1132, 1133, 1134, 1135, 1137, 1138, 1139, 1141, 1142, 1143, 1144, 1149, 1150, 1151, 1152, 1153, 1154, 1157, 1158, 1159, 1165, 1166, 1167, 1168, 1229, 1236, 1237, 1246, 1247, 1254, 1258, 1259, 1260, 1261, 1262, 1265, 1268, 1269, 1273, 1274, 1275, 1276, 1277, 1278, 1279, 1280, 1281, 1283, 1284, 1285, 1286, 1287, 1288, 1289, 1290, 1291, 1292, 1293, 1294, 1295, 1296, 1297, 1298, 1299, 1300, 1301, 1302, 1303, 1304, 1305, 1306, 1307, 1308, 1309, 1310, 1312, 1313, 1314, 1315, 1316, 1317, 1318, 1319, 1320, 1321, 1322, 1323, 1324, 1325, 1326, 1327, 1328, 1329, 1330, 1331, 1332, 1333, 1334, 1342, 1343, 1344, 1345, 1351, 1352, 1353, 1359, 1360, 1361, 1362, 1363, 1364, 1365, 1366, 1367, 1372, 1373, 1374, 1375, 1376, 1377, 1378, 1379, 1385, 1386, 1387, 1388, 1389, 1390, 1391, 1392, 1398, 1399, 1400, 1401, 1402, 1403, 1404, 1410, 1413, 1423, 1424, 1425, 1432, 1433, 1434, 1435, 1441, 1442, 1443, 1444, 1445, 1446, 1447, 1448, 1449, 1450, 1453, 1460, 1461, 1462, 1463, 1465, 1466, 1467, 1468, 1469, 1470, 1471, 1472, 1473, 1474, 1475, 1476, 1477, 1478, 1479, 1480, 1481, 1482, 1483, 1484, 1485, 1486, 1487, 1488, 1489, 1490, 1491, 1497, 1498, 1499, 1500, 1501, 1502, 1507, 1508, 1509, 1510, 1511, 1512, 1513, 1514, 1515, 1517, 1518, 1519, 1520, 1521, 1527, 1534, 1548, 1550, 1844, 1846, 1847, 1848, 1852, 1853, 1854 }

C grade: { 1027, 1541, 1542 }

F grade: { 368, 369, 489, 490, 491, 492, 493, 497, 498, 499, 500, 501, 505, 506, 507, 508, 509, 513, 514, 515, 516, 517, 521, 522, 523, 524, 525, 526, 527, 528, 529, 530, 531, 532, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 543, 544, 545, 546, 547, 548, 549, 550, 551, 552, 553, 554, 555, 556, 557, 558, 559, 560, 561, 562, 563, 564, 565, 566, 567, 568, 569, 570, 571, 572, 590, 591, 592, 593, 608, 609, 610, 611, 629, 630, 631, 632, 649, 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 730, 731, 736, 737, 738, 739, 740, 741, 742, 743, 744, 745, 746, 747, 748, 749, 750, 751, 752, 753, 754, 755, 785, 786, 787, 791, 792, 793, 794, 795, 797, 798, 799, 800, 801, 802, 803, 833, 834, 835, 839, 840, 841, 842, 843, 845, 846, 847, 848, 849, 850, 851, 857, 858, 859, 865, 866, 867, 868, 875, 876, 883, 884, 891, 892, 898, 899, 900, 906, 907, 908, 927, 928, 929, 932, 935, 936, 937, 939, 940, 941, 942, 943, 944, 945, 946, 947, 948, 949, 950, 951, 952, 953, 954, 955, 956, 957, 958, 959, 960, 961, 962, 963, 964, 965, 966, 967, 968, 969, 970, 971, 972, 973, 974, 975, 976, 977, 978, 979, 980, 981, 982, 983, 984, 985, 986, 988, 990, 991, 992, 993, 994, 995, 996, 997, 998, 1145, 1146, 1147, 1148, 1169, 1170, 1171, 1172, 1173, 1174, 1175, 1176, 1177, 1178, 1179, 1180, 1181, 1182, 1183, 1184, 1185, 1186, 1187, 1188, 1189, 1190, 1191, 1192, 1193, 1194, 1195, 1196, 1197, 1198, 1199, 1200, 1201, 1202, 1203, 1204, 1205, 1206, 1207, 1208, 1209, 1210, 1211, 1212, 1213, 1214, 1215, 1216, 1217, 1218, 1219, 1220, 1221, 1222, 1223, 1224, 1225, 1226, 1227, 1228, 1231, 1232, 1233, 1234, 1235, 1559, 1560, 1561, 1562, 1563, 1564, 1565, 1566, 1567, 1568, 1569, 1570, 1571, 1572, 1573, 1574, 1575, 1576, 1577, 1578, 1579, 1580, 1581, 1582, 1583, 1584, 1585, 1586, 1587, 1588, 1589, 1590, 1591,

1592, 1593, 1594, 1595, 1596, 1597, 1598, 1599, 1600, 1601, 1602, 1603, 1604, 1605, 1606, 1607, 1608, 1609, 1610, 1611, 1612, 1613, 1614, 1615, 1616, 1617, 1618, 1619, 1620, 1621, 1622, 1623, 1624, 1625, 1626, 1627, 1628, 1629, 1630, 1631, 1632, 1633, 1634, 1635, 1636, 1637, 1638, 1639, 1640, 1641, 1642, 1643, 1644, 1645, 1646, 1647, 1648, 1649, 1650, 1651, 1652, 1653, 1654, 1655, 1656, 1657, 1658, 1659, 1660, 1661, 1662, 1663, 1664, 1665, 1666, 1667, 1668, 1669, 1670, 1671, 1672, 1673, 1674, 1675, 1676, 1677, 1678, 1679, 1680, 1681, 1682, 1683, 1684, 1685, 1686, 1687, 1688, 1689, 1690, 1691, 1692, 1693, 1694, 1695, 1696, 1697, 1698, 1699, 1700, 1701, 1702, 1703, 1704, 1705, 1706, 1707, 1708, 1709, 1710, 1711, 1712, 1713, 1714, 1715, 1716, 1717, 1718, 1719, 1720, 1721, 1722, 1723, 1724, 1725, 1726, 1727, 1728, 1729, 1730, 1731, 1732, 1733, 1734, 1735, 1736, 1737, 1738, 1739, 1740, 1741, 1742, 1743, 1744, 1745, 1746, 1747, 1748, 1749, 1750, 1751, 1752, 1753, 1754, 1755, 1756, 1757, 1758, 1759, 1760, 1761, 1762, 1763, 1764, 1765, 1766, 1767, 1768, 1769, 1770, 1771, 1772, 1773, 1774, 1775, 1776, 1777, 1778, 1779, 1780, 1781, 1782, 1783, 1784, 1785, 1786, 1787, 1788, 1789, 1790, 1791, 1792, 1793, 1794, 1795, 1796, 1797, 1798, 1799, 1800, 1801, 1802, 1803, 1804, 1805, 1806, 1807, 1808, 1809, 1810, 1811, 1812, 1813, 1814, 1815, 1816, 1817, 1818, 1819, 1820, 1821, 1822, 1823, 1824, 1825, 1826, 1827, 1828, 1829, 1830, 1831, 1832, 1833, 1834, 1835, 1836, 1837, 1838, 1839, 1840, 1841, 1842, 1843, 1844, 1845, 1849, 1850, 1851, 1856, 1857, 1858, 1859, 1860, 1861, 1862, 1863, 1864, 1865, 1866, 1867, 1868, 1869, 1870, 1871, 1872, 1873, 1874, 1875, 1876, 1877, 1878, 1879, 1880, 1882, 1883, 1884, 1885, 1886, 1887, 1888, 1889, 1890 }

2.1.8 Mupad

A grade: { }

B grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 331, 332, 333, 334, 335, 336, 337, 338, 339, 340, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 365, 366, 367, 368, 370, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 383, 384, 385, 386, 387, 388, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400, 401, 402, 403, 404, 405, 406, 407, 408, 409, 410, 411, 412, 413, 414, 415, 416, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 428, 429, 430, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 442, 443, 444, 445, 446, 447, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463, 464, 465, 466,

467, 468, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 487, 488, 491, 492, 494, 495, 496, 499, 500, 502, 503, 504, 507, 508, 510, 511, 512, 515, 516, 518, 519, 520, 571, 572, 573, 574, 575, 576, 580, 581, 582, 583, 586, 587, 588, 589, 592, 593, 594, 595, 599, 600, 601, 604, 605, 606, 607, 610, 611, 612, 613, 614, 615, 619, 620, 621, 622, 625, 626, 627, 628, 631, 632, 633, 634, 638, 639, 640, 643, 644, 645, 646, 647, 648, 649, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 672, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 684, 685, 686, 687, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 698, 699, 700, 701, 702, 703, 732, 733, 734, 735, 739, 740, 741, 753, 754, 755, 759, 760, 763, 769, 770, 777, 778, 779, 781, 782, 783, 784, 785, 786, 787, 789, 790, 791, 792, 793, 794, 795, 797, 798, 799, 800, 801, 802, 803, 834, 835, 840, 841, 842, 843, 846, 847, 848, 849, 850, 851, 897, 905, 913, 919, 923, 924, 925, 926, 930, 931, 932, 933, 934, 938, 939, 940, 941, 942, 943, 946, 947, 948, 949, 953, 954, 955, 956, 961, 962, 963, 964, 969, 970, 971, 972, 973, 974, 975, 976, 977, 978, 979, 980, 987, 988, 989, 990, 991, 992, 993, 994, 995, 996, 999, 1000, 1001, 1002, 1003, 1004, 1005, 1006, 1007, 1008, 1009, 1010, 1011, 1012, 1013, 1014, 1015, 1016, 1017, 1018, 1019, 1020, 1021, 1022, 1023, 1024, 1025, 1026, 1027, 1028, 1029, 1030, 1031, 1032, 1033, 1034, 1035, 1036, 1037, 1038, 1039, 1040, 1041, 1042, 1043, 1044, 1045, 1046, 1047, 1048, 1049, 1050, 1051, 1052, 1053, 1054, 1055, 1056, 1057, 1058, 1059, 1060, 1061, 1062, 1067, 1068, 1070, 1071, 1072, 1073, 1074, 1083, 1084, 1085, 1086, 1087, 1098, 1099, 1100, 1101, 1102, 1103, 1105, 1109, 1110, 1111, 1112, 1113, 1114, 1115, 1120, 1121, 1122, 1123, 1124, 1125, 1130, 1131, 1132, 1133, 1134, 1135, 1136, 1139, 1140, 1141, 1142, 1143, 1144, 1147, 1148, 1149, 1150, 1151, 1152, 1155, 1156, 1157, 1158, 1159, 1161, 1162, 1163, 1164, 1165, 1166, 1167, 1168, 1169, 1180, 1181, 1182, 1183, 1214, 1215, 1216, 1225, 1226, 1227, 1228, 1229, 1230, 1236, 1237, 1238, 1239, 1240, 1241, 1242, 1243, 1244, 1245, 1246, 1247, 1248, 1249, 1250, 1251, 1252, 1253, 1254, 1255, 1256, 1257, 1258, 1259, 1260, 1261, 1262, 1263, 1264, 1265, 1266, 1267, 1268, 1269, 1270, 1271, 1272, 1273, 1274, 1275, 1276, 1277, 1278, 1279, 1280, 1281, 1282, 1283, 1284, 1285, 1286, 1287, 1288, 1289, 1290, 1291, 1292, 1293, 1294, 1295, 1296, 1297, 1298, 1299, 1300, 1301, 1302, 1303, 1304, 1305, 1306, 1307, 1308, 1309, 1310, 1311, 1312, 1313, 1314, 1315, 1316, 1317, 1318, 1319, 1320, 1321, 1322, 1323, 1324, 1325, 1326, 1327, 1328, 1329, 1330, 1331, 1332, 1333, 1334, 1335, 1336, 1337, 1338, 1339, 1340, 1341, 1342, 1343, 1344, 1345, 1346, 1347, 1348, 1349, 1350, 1351, 1352, 1353, 1354, 1355, 1356, 1357, 1358, 1359, 1360, 1361, 1362, 1363, 1364, 1365, 1366, 1367, 1368, 1369, 1370, 1371, 1372, 1373, 1374, 1375, 1376, 1377, 1378, 1379, 1380, 1381, 1382, 1383, 1384, 1385, 1386, 1387, 1388, 1389, 1390, 1391, 1392, 1393, 1394, 1395, 1396, 1397, 1398, 1399, 1400, 1401, 1402, 1403, 1404, 1405, 1406, 1407, 1408, 1409, 1410, 1411, 1412, 1413, 1414, 1415, 1416, 1417, 1418, 1419, 1420, 1421, 1422, 1423, 1424, 1425, 1426, 1427, 1428, 1429, 1430, 1431, 1432, 1433, 1434, 1435, 1436, 1437, 1438, 1439, 1440, 1441, 1442, 1443, 1444, 1445, 1446, 1447, 1448, 1449, 1450, 1451, 1452, 1453, 1454, 1455, 1456, 1457, 1458, 1459, 1463, 1464, 1466, 1467, 1468, 1469, 1470, 1477, 1478, 1479, 1480, 1488, 1489, 1490, 1491, 1495, 1496, 1497, 1498, 1499, 1500, 1501, 1506, 1507, 1508, 1509, 1510, 1511, 1516, 1517, 1518, 1519, 1520, 1521, 1522, 1523, 1524, 1525, 1526, 1527, 1528, 1529, 1530, 1531, 1532, 1533, 1534, 1535, 1536, 1537, 1538, 1539, 1540, 1541, 1542, 1543, 1544, 1545, 1546, 1547, 1548, 1549, 1550, 1551, 1552, 1553, 1554, 1555, 1556, 1557, 1558, 1578, 1579, 1580, 1581, 1604, 1605, 1606, 1607, 1682, 1683, 1684, 1685, 1708, 1709, 1710, 1711, 1775, 1776, 1777, 1778, 1782, 1783, 1784, 1785, 1801, 1802, 1803, 1804, 1808, 1809, 1810, 1811, 1834, 1835, 1836, 1837, 1844, 1846, 1847, 1848, 1852, 1853, 1854, 1855, 1859, 1860, 1861, 1868, 1869, 1870, 1871, 1874, 1875, 1876, 1877, 1881, 1882, 1883, 1884, 1891, 1892, 1893, 1894, 1895, 1896, 1897, 1898, 1899, 1900, 1901, 1902, 1903, 1904, 1905, 1906, 1907, 1908, 1909, 1910, 1911, 1912, 1913, 1914, 1915, 1916, 1917 }

C grade: { }

F grade: { 369, 489, 490, 493, 497, 498, 501, 505, 506, 509, 513, 514, 517, 521, 522, 523, 524, 525, 526, 527, 528, 529, 530, 531, 532, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 543, 544, 545, 546, 547, 548, 549, 550, 551, 552, 553, 554, 555, 556, 557, 558, 559, 560, 561, 562, 563, 564, 565, 566, 567, 568, 569, 570, 577, 578, 579, 584, 585, 590, 591, 596, 597, 598, 602, 603, 608, 609, 616, 617, 618, 623, 624, 629, 630, 635, 636, 637, 641, 642, 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 730, 731, 736, 737, 738, 742, 743, 744, 745, 746, 747, 748, 749, 750, 751, 752, 756, 757, 758, 761, 762, 764, 765, 766, 767, 768, 771, 772, 773, 774, 775, 776, 780, 788, 796, 804, 805, 806, 807, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823, 824, 825, 826, 827, 828, 829, 830, 831, 832, 833, 836, 837, 838, 839, 844, 845, 852, 853, 854, 855, 856, 857, 858, 859, 860, 861, 862, 863, 864, 865, 866, 867, 868, 869, 870, 871, 872, 873, 874, 875, 876, 877, 878, 879, 880, 881, 882, 883, 884, 885, 886, 887, 888, 889, 890, 891, 892, 893, 894, 895, 896, 898, 899, 900, 901, 902, 903, 904, 906, 907, 908, 909, 910, 911, 912, 914, 915, 916, 917, 918, 920, 921, 922, 927, 928, 929, 935, 936, 937, 944, 945, 950, 951, 952, 957, 958, 959, 960, 965, 966, 967, 968, 981, 982, 983, 984, 985, 986, 997, 998, 1063, 1064, 1065, 1066, 1069, 1075, 1076, 1077, 1078, 1079, 1080, 1081, 1082, 1088, 1089, 1090, 1091, 1092, 1093, 1094, 1095, 1096, 1097, 1104, 1106, 1107, 1108, 1116, 1117, 1118, 1119, 1126, 1127, 1128, 1129, 1137, 1138, 1145, 1146, 1153, 1154, 1160, 1170, 1171, 1172, 1173, 1174, 1175, 1176, 1177, 1178, 1179, 1184, 1185, 1186, 1187, 1188, 1189, 1190, 1191, 1192, 1193, 1194, 1195, 1196, 1197, 1198, 1199, 1200, 1201, 1202, 1203, 1204, 1205, 1206, 1207, 1208, 1209, 1210, 1211, 1212, 1213, 1217, 1218, 1219, 1220, 1221, 1222, 1223, 1224, 1231, 1232, 1233, 1234, 1235, 1460, 1461, 1462, 1465, 1471, 1472, 1473, 1474, 1475, 1476, 1481, 1482, 1483, 1484, 1485, 1486, 1487, 1492, 1493, 1494, 1502, 1503, 1504, 1505, 1512, 1513, 1514, 1515, 1559, 1560, 1561, 1562, 1563, 1564, 1565, 1566, 1567, 1568, 1569, 1570, 1571, 1572, 1573, 1574, 1575, 1576, 1577, 1582, 1583, 1584, 1585, 1586, 1587, 1588, 1589, 1590, 1591, 1592, 1593, 1594, 1595, 1596, 1597, 1598, 1599, 1600, 1601, 1602, 1603, 1608, 1609, 1610, 1611, 1612, 1613, 1614, 1615, 1616, 1617, 1618, 1619, 1620, 1621, 1622, 1623, 1624, 1625, 1626, 1627, 1628, 1629, 1630, 1631, 1632, 1633, 1634, 1635, 1636, 1637, 1638, 1639, 1640, 1641, 1642, 1643, 1644, 1645, 1646, 1647, 1648, 1649, 1650, 1651, 1652, 1653, 1654, 1655, 1656, 1657, 1658, 1659, 1660, 1661, 1662, 1663, 1664, 1665, 1666, 1667, 1668, 1669, 1670, 1671, 1672, 1673, 1674, 1675, 1676, 1677, 1678, 1679, 1680, 1681, 1686, 1687, 1688, 1689, 1690, 1691, 1692, 1693, 1694, 1695, 1696, 1697, 1698, 1699, 1700, 1701, 1702, 1703, 1704, 1705, 1706, 1707, 1712, 1713, 1714, 1715, 1716, 1717, 1718, 1719, 1720, 1721, 1722, 1723, 1724, 1725, 1726, 1727, 1728, 1729, 1730, 1731, 1732, 1733, 1734, 1735, 1736, 1737, 1738, 1739, 1740, 1741, 1742, 1743, 1744, 1745, 1746, 1747, 1748, 1749, 1750, 1751, 1752, 1753, 1754, 1755, 1756, 1757, 1758, 1759, 1760, 1761, 1762, 1763, 1764, 1765, 1766, 1767, 1768, 1769, 1770, 1771, 1772, 1773, 1774, 1779, 1780, 1781, 1786, 1787, 1788, 1789, 1790, 1791, 1792, 1793, 1794, 1795, 1796, 1797, 1798, 1799, 1800, 1805, 1806, 1807, 1812, 1813, 1814, 1815, 1816, 1817, 1818, 1819, 1820, 1821, 1822, 1823, 1824, 1825, 1826, 1827, 1828, 1829, 1830, 1831, 1832, 1833, 1838, 1839, 1840, 1841, 1842, 1843, 1845, 1849, 1850, 1851, 1856, 1857, 1858, 1862, 1863, 1864, 1865, 1866, 1867, 1872, 1873, 1878, 1879, 1880, 1885, 1886, 1887, 1888, 1889, 1890 }

2.2 Detailed conclusion table per each integral for all CAS systems

Detailed conclusion table per each integral is given by table below. The elapsed time is in seconds. For failed result it is given as F(-1) if the failure was due to timeout. It is given as F(-2) if the failure was due to an exception being raised, which could indicate a bug in the system. If the failure was due to integral not being evaluated within the time limit, then it is given just an F.

In this table, the column **normalized size** is defined as $\frac{\text{antiderivative leaf size}}{\text{optimal antiderivative leaf size}}$

Problem 1	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1	1	1	2	1	1	0	1	1
normalized size	1	1.00	1.00	2.00	1.00	1.00	0.00	1.00	1.00
time (sec)	N/A	0.000	0.000	0.005	0.420	0.342	0.008	1.087	0.041
Problem 2	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1	1	1	2	1	1	0	1	1
normalized size	1	1.00	1.00	2.00	1.00	1.00	0.00	1.00	1.00
time (sec)	N/A	0.000	0.000	0.002	0.415	0.358	0.023	1.067	0.005
Problem 3	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	3	3	3	4	3	3	2	3	3
normalized size	1	1.00	1.00	1.33	1.00	1.00	0.67	1.00	1.00
time (sec)	N/A	0.000	0.000	0.000	0.413	0.360	0.016	1.037	0.006

Problem 4	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	3	3	3	4	3	3	3	3	3
normalized size	1	1.00	1.00	1.33	1.00	1.00	1.00	1.00	1.00
time (sec)	N/A	0.000	0.000	0.000	0.419	0.346	0.015	1.114	0.004

Problem 5	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	5	5	5	4	3	3	5	3	3
normalized size	1	1.00	1.00	0.80	0.60	0.60	1.00	0.60	0.60
time (sec)	N/A	0.000	0.000	0.000	0.422	0.380	0.015	1.158	0.008

Problem 6	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	3	3	3	4	3	3	2	3	3
normalized size	1	1.00	1.00	1.33	1.00	1.00	0.67	1.00	1.00
time (sec)	N/A	0.001	0.000	0.000	0.434	0.384	0.015	0.836	0.002

Problem 7	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	3	3	3	4	3	3	2	3	3
normalized size	1	1.00	1.00	1.33	1.00	1.00	0.67	1.00	1.00
time (sec)	N/A	0.000	0.000	0.000	0.436	0.363	0.016	0.747	0.002

Problem 8	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	4	4	4	5	4	4	3	4	4
normalized size	1	1.00	1.00	1.25	1.00	1.00	0.75	1.00	1.00
time (sec)	N/A	0.000	0.000	0.000	0.426	0.360	0.016	1.248	0.002

Problem 9	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	12	11	18	10	11	11
normalized size	1	1.00	1.00	0.86	0.79	1.29	0.71	0.79	0.79
time (sec)	N/A	0.008	0.000	0.000	0.445	0.403	0.055	1.075	0.003

Problem 10	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	3	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	0.43	0.71	0.71
time (sec)	N/A	0.000	0.000	0.001	0.421	0.337	0.055	1.182	0.118

Problem 11	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	3	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	0.43	0.71	0.71
time (sec)	N/A	0.000	0.000	0.002	0.416	0.338	0.054	1.183	0.022

Problem 12	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	3	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	0.43	0.71	0.71
time (sec)	N/A	0.000	0.000	0.000	0.420	0.346	0.055	1.095	0.010

Problem 13	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	3	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	0.43	0.71	0.71
time (sec)	N/A	0.000	0.000	0.001	0.415	0.353	0.017	0.953	0.012

Problem 14	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1	1	1	2	1	1	0	1	1
normalized size	1	1.00	1.00	2.00	1.00	1.00	0.00	1.00	1.00
time (sec)	N/A	0.000	0.000	0.000	0.442	0.340	0.015	1.002	0.002

Problem 15	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	2	2	2	3	2	2	2	3	2
normalized size	1	1.00	1.00	1.50	1.00	1.00	1.00	1.50	1.00
time (sec)	N/A	0.000	0.000	0.002	0.435	0.385	0.060	0.803	0.036

Problem 16	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	5	5	5	6	5	5	3	5	5
normalized size	1	1.00	1.00	1.20	1.00	1.00	0.60	1.00	1.00
time (sec)	N/A	0.001	0.000	0.000	0.432	0.383	0.058	0.849	0.035

Problem 17	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	1.00	0.71	0.71
time (sec)	N/A	0.000	0.000	0.001	0.489	0.374	0.058	0.841	0.014

Problem 18	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	1.00	0.71	0.71
time (sec)	N/A	0.000	0.000	0.000	0.426	0.387	0.059	1.132	0.012

Problem 19	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	1.00	0.71	0.71
time (sec)	N/A	0.000	0.000	0.000	0.416	0.405	0.060	1.290	0.070

Problem 20	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.67	0.56	0.56	0.78	0.56	0.56
time (sec)	N/A	0.001	0.001	0.017	0.428	0.406	0.068	0.900	0.077

Problem 21	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.67	0.56	0.56	0.78	0.56	0.56
time (sec)	N/A	0.000	0.001	0.002	0.415	0.389	0.059	0.982	0.031

Problem 22	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.67	0.56	0.56	0.78	0.56	0.56
time (sec)	N/A	0.000	0.001	0.002	0.425	0.388	0.062	1.042	0.029

Problem 23	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	5	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	0.71	0.71	0.71
time (sec)	N/A	0.000	0.001	0.003	0.419	0.388	0.059	1.127	0.031

Problem 24	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	1.00	0.71	0.71
time (sec)	N/A	0.000	0.001	0.002	0.698	0.418	0.061	1.010	0.031

Problem 25	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	6	5	5	8	5	5
normalized size	1	1.00	1.00	0.67	0.56	0.56	0.89	0.56	0.56
time (sec)	N/A	0.000	0.001	0.001	0.616	0.404	0.061	0.924	0.034

Problem 26	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.67	0.56	0.56	0.78	0.56	0.56
time (sec)	N/A	0.001	0.001	0.003	0.559	0.398	0.060	1.051	0.073

Problem 27	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.67	0.56	0.56	0.78	0.56	0.56
time (sec)	N/A	0.000	0.001	0.003	0.555	0.399	0.061	1.047	0.066

Problem 28	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.67	0.56	0.56	0.78	0.56	0.56
time (sec)	N/A	0.000	0.001	0.001	0.505	0.413	0.062	0.913	0.065

Problem 29	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.67	0.56	0.56	0.78	0.56	0.56
time (sec)	N/A	0.000	0.001	0.002	0.480	0.392	0.061	0.848	0.065

Problem 30	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.67	0.56	0.56	0.78	0.56	0.56
time (sec)	N/A	0.000	0.001	0.001	0.456	0.380	0.061	1.136	0.040

Problem 31	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	5	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	0.71	0.71	0.71
time (sec)	N/A	0.000	0.001	0.002	0.521	0.376	0.060	0.949	0.067

Problem 32	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	1.00	0.71	0.71
time (sec)	N/A	0.000	0.001	0.003	0.513	0.384	0.060	1.119	0.073

Problem 33	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	6	5	5	8	5	5
normalized size	1	1.00	1.00	0.67	0.56	0.56	0.89	0.56	0.56
time (sec)	N/A	0.000	0.001	0.001	0.491	0.390	0.060	0.923	0.051

Problem 34	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	11	12	11	10	12	11	20
normalized size	1	1.00	1.00	1.09	1.00	0.91	1.09	1.00	1.82
time (sec)	N/A	0.002	0.001	0.003	0.638	0.423	0.063	0.948	0.345

Problem 35	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	12	13	16	12	17	16	12
normalized size	1	1.00	0.75	0.81	1.00	0.75	1.06	1.00	0.75
time (sec)	N/A	0.003	0.002	0.003	0.537	0.411	0.064	1.037	0.183

Problem 36	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	23	22	21	21	19	22	21
normalized size	1	1.00	1.00	0.96	0.91	0.91	0.83	0.96	0.91
time (sec)	N/A	0.014	0.004	0.002	0.665	0.419	0.087	1.071	0.143

Problem 37	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	23	20	19	104	270	444	93
normalized size	1	1.00	1.00	0.87	0.83	4.52	11.74	19.30	4.04
time (sec)	N/A	0.012	0.020	0.003	0.558	0.402	71.801	1.635	0.183

Problem 38	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	23	20	19	59	156	195	45
normalized size	1	1.00	1.00	0.87	0.83	2.57	6.78	8.48	1.96
time (sec)	N/A	0.011	0.014	0.002	0.885	0.394	5.270	1.043	0.170

Problem 39	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	23	20	19	19	82	19	19
normalized size	1	1.00	1.00	0.87	0.83	0.83	3.57	0.83	0.83
time (sec)	N/A	0.011	0.010	0.003	0.738	0.404	0.444	1.070	0.075

Problem 40	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	20	19	19	31	19	19
normalized size	1	1.00	1.00	0.95	0.90	0.90	1.48	0.90	0.90
time (sec)	N/A	0.010	0.008	0.004	0.920	0.399	1.782	1.165	0.106

Problem 41	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	20	19	34	58	19	19
normalized size	1	1.00	1.00	0.95	0.90	1.62	2.76	0.90	0.90
time (sec)	N/A	0.011	0.008	0.002	1.003	0.400	1.795	1.645	0.135

Problem 42	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	23	20	19	68	102	19	19
normalized size	1	1.00	1.00	0.87	0.83	2.96	4.43	0.83	0.83
time (sec)	N/A	0.011	0.011	0.003	0.848	0.398	6.786	1.317	0.179

Problem 43	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	14	13	13	12	13	13
normalized size	1	1.00	1.00	0.82	0.76	0.76	0.71	0.76	0.76
time (sec)	N/A	0.008	0.001	0.000	0.895	0.333	0.063	1.216	0.020

Problem 44	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	14	13	13	12	13	13
normalized size	1	1.00	1.00	0.82	0.76	0.76	0.71	0.76	0.76
time (sec)	N/A	0.007	0.001	0.000	0.861	0.353	0.063	1.738	0.019

Problem 45	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	14	13	13	12	13	13
normalized size	1	1.00	1.00	0.82	0.76	0.76	0.71	0.76	0.76
time (sec)	N/A	0.006	0.001	0.001	0.831	0.330	0.064	1.172	0.019

Problem 46	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	12	12	12	11	10	10	8	10	10
normalized size	1	1.00	1.00	0.92	0.83	0.83	0.67	0.83	0.83
time (sec)	N/A	0.002	0.000	0.002	0.887	0.358	0.060	1.248	0.017

Problem 47	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	8	8	8	9	8	8	7	9	8
normalized size	1	1.00	1.00	1.12	1.00	1.00	0.88	1.12	1.00
time (sec)	N/A	0.003	0.001	0.008	0.843	0.389	0.090	1.057	0.017

Problem 48	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	11	12	11	13	7	12	11
normalized size	1	1.00	1.00	1.09	1.00	1.18	0.64	1.09	1.00
time (sec)	N/A	0.004	0.002	0.018	0.871	0.378	0.111	1.048	0.033

Problem 49	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	15	14	11	11	12	11	11
normalized size	1	1.00	0.88	0.82	0.65	0.65	0.71	0.65	0.65
time (sec)	N/A	0.002	0.001	0.005	1.125	0.372	0.110	1.223	0.023

Problem 50	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	14	13	13	14	13	13
normalized size	1	1.00	1.00	0.82	0.76	0.76	0.82	0.76	0.76
time (sec)	N/A	0.005	0.002	0.004	1.097	0.382	0.131	1.383	0.026

Problem 51	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	14	13	13	14	13	13
normalized size	1	1.00	1.00	0.82	0.76	0.76	0.82	0.76	0.76
time (sec)	N/A	0.005	0.002	0.006	1.051	0.380	0.163	1.679	0.027

Problem 52	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	25	24	24	26	24	24
normalized size	1	1.00	1.00	0.83	0.80	0.80	0.87	0.80	0.80
time (sec)	N/A	0.012	0.002	0.002	1.195	0.353	0.072	1.611	0.077

Problem 53	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	25	24	24	24	24	24
normalized size	1	1.00	1.00	0.83	0.80	0.80	0.80	0.80	0.80
time (sec)	N/A	0.010	0.002	0.000	1.051	0.351	0.073	1.023	0.031

Problem 54	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	25	24	24	26	24	24
normalized size	1	1.00	1.00	0.83	0.80	0.80	0.87	0.80	0.80
time (sec)	N/A	0.009	0.001	0.002	0.989	0.345	0.067	1.414	0.030

Problem 55	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	20	20	19	12	20
normalized size	1	1.00	1.00	0.93	1.43	1.43	1.36	0.86	1.43
time (sec)	N/A	0.001	0.001	0.001	1.078	0.410	0.071	1.163	0.029

Problem 56	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	22	21	20	20	20	21	20
normalized size	1	1.00	1.00	0.95	0.91	0.91	0.91	0.95	0.91
time (sec)	N/A	0.006	0.001	0.001	1.115	0.423	0.108	1.350	0.029

Problem 57	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	21	20	24	17	21	20
normalized size	1	1.00	1.00	1.05	1.00	1.20	0.85	1.05	1.00
time (sec)	N/A	0.008	0.001	0.006	1.103	0.413	0.126	1.092	0.066

Problem 58	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	24	24	24	23	21	26	22	22	23
normalized size	1	1.00	1.00	0.96	0.88	1.08	0.92	0.92	0.96
time (sec)	N/A	0.008	0.003	0.007	1.179	0.432	0.167	1.179	0.044

Problem 59	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	26	25	22	22	24	22	22
normalized size	1	1.00	1.53	1.47	1.29	1.29	1.41	1.29	1.29
time (sec)	N/A	0.002	0.006	0.006	1.354	0.439	0.178	1.479	0.035

Problem 60	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	25	24	24	26	24	24
normalized size	1	1.00	1.00	0.83	0.80	0.80	0.87	0.80	0.80
time (sec)	N/A	0.008	0.003	0.005	1.344	0.453	0.187	1.116	0.035

Problem 61	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	25	24	24	26	24	24
normalized size	1	1.00	1.00	0.83	0.80	0.80	0.87	0.80	0.80
time (sec)	N/A	0.008	0.007	0.005	1.329	0.448	0.190	1.191	0.035

Problem 62	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	25	24	24	26	24	24
normalized size	1	1.00	1.00	0.83	0.80	0.80	0.87	0.80	0.80
time (sec)	N/A	0.008	0.003	0.005	1.347	0.504	0.198	1.069	0.034

Problem 63	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	25	24	24	26	24	24
normalized size	1	1.00	1.00	0.83	0.80	0.80	0.87	0.80	0.80
time (sec)	N/A	0.008	0.006	0.006	1.351	0.433	0.214	1.199	0.036

Problem 64	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	43	36	35	35	37	35	35
normalized size	1	1.00	1.00	0.84	0.81	0.81	0.86	0.81	0.81
time (sec)	N/A	0.018	0.002	0.002	1.320	0.419	0.077	1.218	0.042

Problem 65	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	43	36	35	35	37	35	35
normalized size	1	1.00	1.00	0.84	0.81	0.81	0.86	0.81	0.81
time (sec)	N/A	0.016	0.002	0.001	1.354	0.394	0.074	1.272	0.041

Problem 66	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	43	36	35	35	39	35	35
normalized size	1	1.00	1.00	0.84	0.81	0.81	0.91	0.81	0.81
time (sec)	N/A	0.015	0.002	0.000	1.337	0.368	0.072	1.221	0.039

Problem 67	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	40	35	34	34	36	34	34
normalized size	1	1.00	1.33	1.17	1.13	1.13	1.20	1.13	1.13
time (sec)	N/A	0.009	0.002	0.001	1.378	0.410	0.074	1.206	0.040

Problem 68	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	31	31	32	12	31
normalized size	1	1.00	1.00	0.93	2.21	2.21	2.29	0.86	2.21
time (sec)	N/A	0.002	0.002	0.001	1.386	0.376	0.074	1.364	0.041

Problem 69	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	35	32	31	31	34	32	31
normalized size	1	1.00	1.00	0.91	0.89	0.89	0.97	0.91	0.89
time (sec)	N/A	0.011	0.003	0.003	1.343	0.506	0.122	0.949	0.035

Problem 70	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	34	33	32	36	31	33	32
normalized size	1	1.00	1.00	0.97	0.94	1.06	0.91	0.97	0.94
time (sec)	N/A	0.013	0.004	0.006	1.293	0.428	0.130	1.357	0.035

Problem 71	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	33	32	30	37	32	31	32
normalized size	1	1.00	1.00	0.97	0.91	1.12	0.97	0.94	0.97
time (sec)	N/A	0.013	0.005	0.004	1.344	0.523	0.187	1.177	0.030

Problem 72	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	37	34	34	37	36	35	34
normalized size	1	1.00	1.00	0.92	0.92	1.00	0.97	0.95	0.92
time (sec)	N/A	0.012	0.004	0.006	1.305	0.489	0.235	1.141	0.071

Problem 73	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	39	36	33	33	36	33	33
normalized size	1	1.00	2.29	2.12	1.94	1.94	2.12	1.94	1.94
time (sec)	N/A	0.002	0.003	0.006	1.334	0.436	0.256	1.286	0.026

Problem 74	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	41	36	35	35	37	35	34
normalized size	1	1.00	1.14	1.00	0.97	0.97	1.03	0.97	0.94
time (sec)	N/A	0.005	0.006	0.005	1.351	0.439	0.247	1.133	0.027

Problem 75	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	43	36	35	35	37	35	35
normalized size	1	1.00	1.00	0.84	0.81	0.81	0.86	0.81	0.81
time (sec)	N/A	0.013	0.004	0.006	1.355	0.414	0.336	1.152	0.025

Problem 76	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	43	36	35	35	37	35	35
normalized size	1	1.00	1.00	0.84	0.81	0.81	0.86	0.81	0.81
time (sec)	N/A	0.013	0.003	0.004	1.355	0.434	0.290	1.123	0.026

Problem 77	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	66	57	56	56	63	56	56
normalized size	1	1.00	1.00	0.86	0.85	0.85	0.95	0.85	0.85
time (sec)	N/A	0.032	0.003	0.006	1.383	0.500	0.089	0.940	0.025

Problem 78	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	69	58	57	57	65	57	57
normalized size	1	1.00	1.00	0.84	0.83	0.83	0.94	0.83	0.83
time (sec)	N/A	0.028	0.002	0.001	1.362	0.486	0.082	1.205	0.023

Problem 79	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	69	58	57	57	66	57	57
normalized size	1	1.00	1.00	0.84	0.83	0.83	0.96	0.83	0.83
time (sec)	N/A	0.025	0.002	0.000	1.469	0.408	0.079	1.095	0.024

Problem 80	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	66	57	56	56	63	56	56
normalized size	1	1.00	1.03	0.89	0.88	0.88	0.98	0.88	0.88
time (sec)	N/A	0.026	0.002	0.001	1.397	0.404	0.100	1.047	0.024

Problem 81	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	67	58	57	57	65	57	57
normalized size	1	1.00	1.43	1.23	1.21	1.21	1.38	1.21	1.21
time (sec)	N/A	0.021	0.002	0.002	1.322	0.406	0.077	1.715	0.024

Problem 82	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	67	58	57	57	65	57	57
normalized size	1	1.00	2.23	1.93	1.90	1.90	2.17	1.90	1.90
time (sec)	N/A	0.008	0.002	0.000	1.311	0.398	0.084	0.930	0.023

Problem 83	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	53	53	60	12	53
normalized size	1	1.00	1.00	0.93	3.79	3.79	4.29	0.86	3.79
time (sec)	N/A	0.002	0.002	0.002	1.367	0.405	0.081	1.202	0.024

Problem 84	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	59	54	53	53	60	54	53
normalized size	1	1.00	1.00	0.92	0.90	0.90	1.02	0.92	0.90
time (sec)	N/A	0.018	0.003	0.003	1.372	0.444	0.155	1.116	0.029

Problem 85	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	58	55	54	59	56	55	54
normalized size	1	1.00	1.00	0.95	0.93	1.02	0.97	0.95	0.93
time (sec)	N/A	0.021	0.005	0.007	1.396	0.467	0.175	1.275	0.029

Problem 86	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	60	55	53	59	60	54	55
normalized size	1	1.00	1.00	0.92	0.88	0.98	1.00	0.90	0.92
time (sec)	N/A	0.022	0.005	0.005	1.362	0.453	0.204	1.187	0.029

Problem 87	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	60	55	55	59	60	56	55
normalized size	1	1.00	1.00	0.92	0.92	0.98	1.00	0.93	0.92
time (sec)	N/A	0.022	0.004	0.006	1.407	0.478	0.258	0.995	0.039

Problem 88	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	57	54	54	59	58	55	54
normalized size	1	1.00	1.00	0.95	0.95	1.04	1.02	0.96	0.95
time (sec)	N/A	0.020	0.005	0.007	1.365	0.435	0.289	1.380	0.077

Problem 89	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	61	56	56	59	60	57	56
normalized size	1	1.00	1.00	0.92	0.92	0.97	0.98	0.93	0.92
time (sec)	N/A	0.021	0.004	0.007	1.348	0.433	0.357	1.368	0.041

Problem 90	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	65	58	55	55	60	55	55
normalized size	1	1.00	3.82	3.41	3.24	3.24	3.53	3.24	3.24
time (sec)	N/A	0.002	0.004	0.004	1.299	0.431	0.371	0.941	0.039

Problem 91	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	67	58	57	57	61	57	57
normalized size	1	1.00	1.86	1.61	1.58	1.58	1.69	1.58	1.58
time (sec)	N/A	0.005	0.004	0.006	1.356	0.449	0.414	1.116	0.073

Problem 92	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	67	58	57	57	61	57	57
normalized size	1	1.00	1.20	1.04	1.02	1.02	1.09	1.02	1.02
time (sec)	N/A	0.010	0.004	0.006	1.395	0.427	0.431	1.100	0.039

Problem 93	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	67	58	57	57	61	57	56
normalized size	1	1.00	1.00	0.87	0.85	0.85	0.91	0.85	0.84
time (sec)	N/A	0.022	0.006	0.003	1.333	0.460	0.450	1.207	0.084

Problem 94	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	69	58	57	57	61	57	57
normalized size	1	1.00	1.00	0.84	0.83	0.83	0.88	0.83	0.83
time (sec)	N/A	0.021	0.004	0.007	1.374	0.420	0.490	1.003	0.082

Problem 95	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	69	58	57	57	61	57	57
normalized size	1	1.00	1.00	0.84	0.83	0.83	0.88	0.83	0.83
time (sec)	N/A	0.021	0.004	0.006	1.314	0.439	0.582	1.381	0.042

Problem 96	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	67	58	57	57	61	57	56
normalized size	1	1.00	1.00	0.87	0.85	0.85	0.91	0.85	0.84
time (sec)	N/A	0.021	0.004	0.006	1.364	0.436	0.616	1.233	0.040

Problem 97	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	67	58	57	57	61	57	56
normalized size	1	1.00	1.00	0.87	0.85	0.85	0.91	0.85	0.84
time (sec)	N/A	0.022	0.004	0.004	1.378	0.427	0.625	1.116	0.038

Problem 98	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	95	80	79	79	94	79	79
normalized size	1	1.00	1.00	0.84	0.83	0.83	0.99	0.83	0.83
time (sec)	N/A	0.048	0.003	0.001	1.400	0.411	0.098	0.952	0.153

Problem 99	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	95	80	79	79	92	79	79
normalized size	1	1.00	1.00	0.84	0.83	0.83	0.97	0.83	0.83
time (sec)	N/A	0.040	0.002	0.001	1.299	0.423	0.093	0.992	0.074

Problem 100	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	95	80	79	79	94	79	79
normalized size	1	1.00	1.00	0.84	0.83	0.83	0.99	0.83	0.83
time (sec)	N/A	0.039	0.002	0.001	1.292	0.396	0.107	1.009	0.068

Problem 101	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	92	79	78	78	90	78	78
normalized size	1	1.00	0.96	0.82	0.81	0.81	0.94	0.81	0.81
time (sec)	N/A	0.040	0.002	0.000	1.389	0.376	0.106	1.083	0.060

Problem 102	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	93	80	79	79	92	79	79
normalized size	1	1.00	1.15	0.99	0.98	0.98	1.14	0.98	0.98
time (sec)	N/A	0.036	0.002	0.001	1.351	0.359	0.099	1.127	0.062

Problem 103	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	93	80	79	79	92	79	79
normalized size	1	1.00	1.45	1.25	1.23	1.23	1.44	1.23	1.23
time (sec)	N/A	0.030	0.002	0.001	1.341	0.389	0.089	1.221	0.104

Problem 104	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	93	80	79	79	92	79	31
normalized size	1	1.00	1.98	1.70	1.68	1.68	1.96	1.68	0.66
time (sec)	N/A	0.024	0.002	0.001	1.327	0.475	0.093	0.911	0.121

Problem 105	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	91	80	79	79	90	79	25
normalized size	1	1.00	3.03	2.67	2.63	2.63	3.00	2.63	0.83
time (sec)	N/A	0.008	0.002	0.001	1.349	0.430	0.090	0.918	0.115

Problem 106	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	75	83	12	75
normalized size	1	1.00	1.00	0.93	0.86	5.36	5.93	0.86	5.36
time (sec)	N/A	0.002	0.001	0.000	1.389	0.413	0.082	1.062	0.060

Problem 107	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	87	87	87	76	75	75	88	76	75
normalized size	1	1.00	1.00	0.87	0.86	0.86	1.01	0.87	0.86
time (sec)	N/A	0.027	0.003	0.003	1.338	0.450	0.187	1.301	0.072

Problem 108	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	86	77	76	81	85	77	76
normalized size	1	1.00	1.00	0.90	0.88	0.94	0.99	0.90	0.88
time (sec)	N/A	0.032	0.004	0.007	1.357	0.441	0.201	1.123	0.055

Problem 109	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	84	77	75	81	85	76	77
normalized size	1	1.00	1.00	0.92	0.89	0.96	1.01	0.90	0.92
time (sec)	N/A	0.033	0.004	0.007	1.377	0.475	0.252	1.060	0.051

Problem 110	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	86	77	77	81	87	78	77
normalized size	1	1.00	1.00	0.90	0.90	0.94	1.01	0.91	0.90
time (sec)	N/A	0.032	0.004	0.007	1.329	0.497	0.308	1.091	0.051

Problem 111	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	86	77	77	81	85	78	77
normalized size	1	1.00	1.00	0.90	0.90	0.94	0.99	0.91	0.90
time (sec)	N/A	0.032	0.004	0.008	1.397	0.441	0.328	1.042	0.090

Problem 112	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	84	77	77	81	83	78	77
normalized size	1	1.00	1.00	0.92	0.92	0.96	0.99	0.93	0.92
time (sec)	N/A	0.032	0.004	0.006	1.382	0.438	0.449	1.014	0.106

Problem 113	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	85	85	85	76	76	81	82	77	81
normalized size	1	1.00	1.00	0.89	0.89	0.95	0.96	0.91	0.95
time (sec)	N/A	0.031	0.005	0.008	1.384	0.399	0.595	0.995	0.110

Problem 114	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	89	78	78	81	83	79	78
normalized size	1	1.00	1.00	0.88	0.88	0.91	0.93	0.89	0.88
time (sec)	N/A	0.033	0.004	0.007	1.363	0.455	0.627	1.274	0.068

Problem 115	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	87	80	77	77	83	77	77
normalized size	1	1.00	5.12	4.71	4.53	4.53	4.88	4.53	4.53
time (sec)	N/A	0.002	0.004	0.005	1.295	0.428	0.604	0.923	0.067

Problem 116	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	91	80	79	79	85	79	23
normalized size	1	1.00	2.53	2.22	2.19	2.19	2.36	2.19	0.64
time (sec)	N/A	0.005	0.004	0.006	1.314	0.463	0.729	1.007	0.093

Problem 117	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	93	80	79	79	85	79	79
normalized size	1	1.00	1.66	1.43	1.41	1.41	1.52	1.41	1.41
time (sec)	N/A	0.010	0.004	0.005	1.382	0.429	0.762	1.064	0.109

Problem 118	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	76	76	93	80	79	79	85	79	79
normalized size	1	1.00	1.22	1.05	1.04	1.04	1.12	1.04	1.04
time (sec)	N/A	0.016	0.004	0.006	1.364	0.457	0.747	1.149	0.106

Problem 119	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	93	80	79	79	85	79	79
normalized size	1	1.00	0.97	0.83	0.82	0.82	0.89	0.82	0.82
time (sec)	N/A	0.026	0.004	0.006	1.445	0.474	0.795	1.147	0.066

Problem 120	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	93	80	79	79	85	79	78
normalized size	1	1.00	1.00	0.86	0.85	0.85	0.91	0.85	0.84
time (sec)	N/A	0.033	0.006	0.005	1.368	0.424	0.782	1.039	0.066

Problem 121	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	95	80	79	79	85	79	79
normalized size	1	1.00	1.00	0.84	0.83	0.83	0.89	0.83	0.83
time (sec)	N/A	0.030	0.004	0.006	1.343	0.453	0.878	0.890	0.070

Problem 122	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	95	80	79	79	85	79	79
normalized size	1	1.00	1.00	0.84	0.83	0.83	0.89	0.83	0.83
time (sec)	N/A	0.030	0.004	0.005	1.390	0.432	0.878	1.002	0.110

Problem 123	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	132	132	132	113	112	112	133	112	112
normalized size	1	1.00	1.00	0.86	0.85	0.85	1.01	0.85	0.85
time (sec)	N/A	0.076	0.003	0.001	1.326	0.409	0.108	0.978	0.150

Problem 124	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	132	132	132	113	112	112	131	112	112
normalized size	1	1.00	1.00	0.86	0.85	0.85	0.99	0.85	0.85
time (sec)	N/A	0.059	0.004	0.001	1.340	0.606	0.111	0.987	0.084

Problem 125	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	132	132	132	113	112	112	133	112	112
normalized size	1	1.00	1.00	0.86	0.85	0.85	1.01	0.85	0.85
time (sec)	N/A	0.060	0.003	0.000	1.369	0.436	0.104	1.119	0.125

Problem 126	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	147	147	125	112	111	111	126	111	111
normalized size	1	1.00	0.85	0.76	0.76	0.76	0.86	0.76	0.76
time (sec)	N/A	0.064	0.003	0.001	1.365	0.603	0.113	1.013	0.087

Problem 127	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	132	132	130	113	112	112	131	112	112
normalized size	1	1.00	0.98	0.86	0.85	0.85	0.99	0.85	0.85
time (sec)	N/A	0.057	0.003	0.001	1.337	0.654	0.106	0.836	0.082

Problem 128	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	112	112	126	113	112	112	128	112	112
normalized size	1	1.00	1.12	1.01	1.00	1.00	1.14	1.00	1.00
time (sec)	N/A	0.052	0.003	0.000	1.384	0.424	0.102	1.102	0.121

Problem 129	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	132	113	112	112	133	112	112
normalized size	1	1.00	1.35	1.15	1.14	1.14	1.36	1.14	1.14
time (sec)	N/A	0.045	0.003	0.000	1.365	0.416	0.102	1.143	0.123

Problem 130	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	130	113	112	112	131	112	112
normalized size	1	1.00	1.60	1.40	1.38	1.38	1.62	1.38	1.38
time (sec)	N/A	0.039	0.003	0.001	1.292	0.428	0.109	1.055	0.120

Problem 131	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	128	113	112	112	129	112	112
normalized size	1	1.00	2.00	1.77	1.75	1.75	2.02	1.75	1.75
time (sec)	N/A	0.036	0.003	0.002	1.358	0.401	0.118	1.087	0.118

Problem 132	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	126	113	112	112	128	112	31
normalized size	1	1.00	2.68	2.40	2.38	2.38	2.72	2.38	0.66
time (sec)	N/A	0.030	0.003	0.002	1.374	0.406	0.107	1.178	0.070

Problem 133	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	128	113	112	112	129	112	25
normalized size	1	1.00	4.27	3.77	3.73	3.73	4.30	3.73	0.83
time (sec)	N/A	0.008	0.003	0.001	1.345	0.381	0.110	1.444	0.095

Problem 134	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	108	114	12	108
normalized size	1	1.00	1.00	0.93	0.86	7.71	8.14	0.86	7.71
time (sec)	N/A	0.002	0.001	0.000	1.335	0.383	0.115	1.164	0.112

Problem 135	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	122	122	122	109	108	108	126	109	108
normalized size	1	1.00	1.00	0.89	0.89	0.89	1.03	0.89	0.89
time (sec)	N/A	0.043	0.004	0.004	1.388	0.438	0.257	1.076	0.079

Problem 136	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	115	110	109	114	117	110	109
normalized size	1	1.00	1.00	0.96	0.95	0.99	1.02	0.96	0.95
time (sec)	N/A	0.047	0.010	0.007	1.352	0.465	0.266	0.960	0.115

Problem 137	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	119	110	108	114	122	109	110
normalized size	1	1.00	1.00	0.92	0.91	0.96	1.03	0.92	0.92
time (sec)	N/A	0.049	0.005	0.006	1.438	0.451	0.310	0.928	0.071

Problem 138	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	115	110	108	114	119	109	110
normalized size	1	1.00	1.00	0.96	0.94	0.99	1.03	0.95	0.96
time (sec)	N/A	0.047	0.010	0.007	1.368	0.432	0.338	1.139	0.062

Problem 139	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	119	110	110	114	121	111	110
normalized size	1	1.00	1.00	0.92	0.92	0.96	1.02	0.93	0.92
time (sec)	N/A	0.049	0.008	0.008	1.269	0.466	0.437	1.118	0.098

Problem 140	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	117	117	117	110	110	114	121	111	110
normalized size	1	1.00	1.00	0.94	0.94	0.97	1.03	0.95	0.94
time (sec)	N/A	0.052	0.010	0.006	1.399	0.468	0.573	1.145	0.099

Problem 141	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	119	110	110	114	122	111	110
normalized size	1	1.00	1.00	0.92	0.92	0.96	1.03	0.93	0.92
time (sec)	N/A	0.049	0.005	0.008	1.367	0.490	0.566	1.240	0.055

Problem 142	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	115	110	110	114	119	111	110
normalized size	1	1.00	1.00	0.96	0.96	0.99	1.03	0.97	0.96
time (sec)	N/A	0.050	0.010	0.009	1.298	0.464	0.695	1.100	0.095

Problem 143	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	119	110	110	114	119	111	110
normalized size	1	1.00	1.00	0.92	0.92	0.96	1.00	0.93	0.92
time (sec)	N/A	0.049	0.005	0.009	1.422	0.451	0.765	1.156	0.068

Problem 144	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	114	114	114	109	109	114	117	110	114
normalized size	1	1.00	1.00	0.96	0.96	1.00	1.03	0.96	1.00
time (sec)	N/A	0.053	0.006	0.008	1.398	0.478	0.825	1.211	0.076

Problem 145	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	124	124	124	111	111	114	119	112	111
normalized size	1	1.00	1.00	0.90	0.90	0.92	0.96	0.90	0.90
time (sec)	N/A	0.048	0.005	0.009	1.400	0.452	1.013	1.128	0.074

Problem 146	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	114	113	110	110	119	110	110
normalized size	1	1.00	6.71	6.65	6.47	6.47	7.00	6.47	6.47
time (sec)	N/A	0.002	0.010	0.006	1.335	0.432	1.026	1.064	0.134

Problem 147	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	128	113	112	112	121	112	23
normalized size	1	1.00	3.56	3.14	3.11	3.11	3.36	3.11	0.64
time (sec)	N/A	0.005	0.004	0.004	1.393	0.446	0.992	0.963	0.096

Problem 148	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	126	113	112	112	121	112	112
normalized size	1	1.00	2.25	2.02	2.00	2.00	2.16	2.00	2.00
time (sec)	N/A	0.010	0.009	0.005	1.373	0.457	1.223	1.031	0.132

Problem 149	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	76	76	128	113	112	112	121	112	112
normalized size	1	1.00	1.68	1.49	1.47	1.47	1.59	1.47	1.47
time (sec)	N/A	0.017	0.008	0.007	1.285	0.455	1.099	0.891	0.094

Problem 150	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	130	113	112	112	121	112	112
normalized size	1	1.00	1.35	1.18	1.17	1.17	1.26	1.17	1.17
time (sec)	N/A	0.025	0.010	0.006	1.361	0.443	1.253	1.517	0.130

Problem 151	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	116	116	132	113	112	112	121	112	112
normalized size	1	1.00	1.14	0.97	0.97	0.97	1.04	0.97	0.97
time (sec)	N/A	0.035	0.005	0.006	1.388	0.543	1.268	1.101	0.135

Problem 152	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	126	113	112	112	121	112	112
normalized size	1	1.00	0.93	0.83	0.82	0.82	0.89	0.82	0.82
time (sec)	N/A	0.049	0.010	0.007	1.402	0.539	1.327	1.153	0.134

Problem 153	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	130	130	130	113	112	112	121	112	112
normalized size	1	1.00	1.00	0.87	0.86	0.86	0.93	0.86	0.86
time (sec)	N/A	0.047	0.004	0.007	1.362	0.425	1.350	0.975	0.099

Problem 154	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	126	113	112	112	121	112	111
normalized size	1	1.00	1.00	0.90	0.89	0.89	0.96	0.89	0.88
time (sec)	N/A	0.049	0.007	0.007	1.396	0.448	1.424	1.110	0.137

Problem 155	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	14	13	13	12	12	13	11
normalized size	1	1.00	0.93	0.87	0.87	0.80	0.80	0.87	0.73
time (sec)	N/A	0.002	0.001	0.002	1.360	0.406	0.068	1.092	0.021

Problem 156	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	19	18	18	27	22	17	16
normalized size	1	1.00	0.95	0.90	0.90	1.35	1.10	0.85	0.80
time (sec)	N/A	0.004	0.001	0.000	1.374	0.451	0.077	1.204	0.075

Problem 157	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	70	63	64	63	61	65	62
normalized size	1	1.00	1.00	0.90	0.91	0.90	0.87	0.93	0.89
time (sec)	N/A	0.034	0.004	0.003	1.394	0.444	0.163	1.003	0.080

Problem 158	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	57	52	52	52	49	53	51
normalized size	1	1.00	1.00	0.91	0.91	0.91	0.86	0.93	0.89
time (sec)	N/A	0.023	0.004	0.003	1.325	0.434	0.152	1.353	0.100

Problem 159	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	44	44	44	41	42	41	37	43	40
normalized size	1	1.00	1.00	0.93	0.95	0.93	0.84	0.98	0.91
time (sec)	N/A	0.020	0.004	0.003	1.237	0.454	0.144	1.050	0.038

Problem 160	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	31	30	29	29	26	30	29
normalized size	1	1.00	1.00	0.97	0.94	0.94	0.84	0.97	0.94
time (sec)	N/A	0.014	0.003	0.003	1.374	0.438	0.130	0.938	0.039

Problem 161	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	19	18	17	14	19	18
normalized size	1	1.00	1.00	1.06	1.00	0.94	0.78	1.06	1.00
time (sec)	N/A	0.009	0.003	0.001	1.309	0.442	0.122	1.019	0.076

Problem 162	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	10	10	10	11	10	10	7	11	10
normalized size	1	1.00	1.00	1.10	1.00	1.00	0.70	1.10	1.00
time (sec)	N/A	0.002	0.001	0.000	1.297	0.445	0.070	0.922	0.021

Problem 163	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	19	18	16	10	20	15
normalized size	1	1.00	1.00	1.06	1.00	0.89	0.56	1.11	0.83
time (sec)	N/A	0.004	0.004	0.005	1.395	0.470	0.153	1.104	0.085

Problem 164	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	28	29	28	26	19	30	25
normalized size	1	1.00	1.00	1.04	1.00	0.93	0.68	1.07	0.89
time (sec)	N/A	0.013	0.005	0.008	1.300	0.491	0.195	0.968	0.051

Problem 165	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	42	41	40	41	31	45	38
normalized size	1	1.00	1.00	0.98	0.95	0.98	0.74	1.07	0.90
time (sec)	N/A	0.018	0.005	0.007	1.337	0.447	0.217	1.021	0.058

Problem 166	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	56	53	51	54	44	56	48
normalized size	1	1.00	1.00	0.95	0.91	0.96	0.79	1.00	0.86
time (sec)	N/A	0.021	0.005	0.007	1.353	0.499	0.242	1.070	0.105

Problem 167	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	68	63	62	65	56	67	60
normalized size	1	1.00	1.00	0.93	0.91	0.96	0.82	0.99	0.88
time (sec)	N/A	0.035	0.005	0.007	1.365	0.462	0.275	1.060	0.065

Problem 168	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	77	78	82	96	78	103	83
normalized size	1	1.00	0.95	0.96	1.01	1.19	0.96	1.27	1.02
time (sec)	N/A	0.059	0.024	0.009	1.332	0.460	0.275	1.140	0.140

Problem 169	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	66	67	70	85	71	90	72
normalized size	1	1.00	0.92	0.93	0.97	1.18	0.99	1.25	1.00
time (sec)	N/A	0.042	0.017	0.007	1.327	0.439	0.252	1.222	0.070

Problem 170	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	54	57	59	73	54	79	62
normalized size	1	1.00	0.93	0.98	1.02	1.26	0.93	1.36	1.07
time (sec)	N/A	0.033	0.019	0.009	1.367	0.463	0.215	1.071	0.067

Problem 171	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	43	45	47	62	44	66	50
normalized size	1	1.00	0.93	0.98	1.02	1.35	0.96	1.43	1.09
time (sec)	N/A	0.027	0.013	0.006	1.357	0.447	0.204	1.139	0.079

Problem 172	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	29	34	36	47	31	50	36
normalized size	1	1.00	0.88	1.03	1.09	1.42	0.94	1.52	1.09
time (sec)	N/A	0.018	0.013	0.006	1.341	0.446	0.173	1.147	0.081

Problem 173	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	20	24	26	28	20	42	23
normalized size	1	1.00	0.87	1.04	1.13	1.22	0.87	1.83	1.00
time (sec)	N/A	0.012	0.007	0.007	1.320	0.452	0.169	1.049	0.036

Problem 174	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	12	12	12	13	12	13	10	12	12
normalized size	1	1.00	1.00	1.08	1.00	1.08	0.83	1.00	1.00
time (sec)	N/A	0.002	0.002	0.000	1.376	0.436	0.149	1.175	0.029

Problem 175	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	24	30	28	39	22	38	26
normalized size	1	1.00	0.83	1.03	0.97	1.34	0.76	1.31	0.90
time (sec)	N/A	0.014	0.012	0.008	1.302	0.464	0.222	1.000	0.122

Problem 176	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	35	43	45	63	37	52	45
normalized size	1	1.00	0.83	1.02	1.07	1.50	0.88	1.24	1.07
time (sec)	N/A	0.021	0.039	0.008	1.393	0.468	0.303	1.217	0.120

Problem 177	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	53	57	64	86	54	74	57
normalized size	1	1.00	0.91	0.98	1.10	1.48	0.93	1.28	0.98
time (sec)	N/A	0.028	0.050	0.010	1.405	0.449	0.312	1.130	0.110

Problem 178	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	66	68	73	95	66	90	69
normalized size	1	1.00	0.96	0.99	1.06	1.38	0.96	1.30	1.00
time (sec)	N/A	0.035	0.056	0.009	1.410	0.503	0.336	1.015	0.080

Problem 179	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	79	79	86	108	80	104	79
normalized size	1	1.00	0.94	0.94	1.02	1.29	0.95	1.24	0.94
time (sec)	N/A	0.043	0.043	0.012	1.340	0.598	0.394	0.988	0.116

Problem 180	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	99	99	89	94	103	129	109	95	91
normalized size	1	1.00	0.90	0.95	1.04	1.30	1.10	0.96	0.92
time (sec)	N/A	0.070	0.027	0.008	1.386	0.581	0.532	0.891	0.234

Problem 181	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	77	83	91	117	92	83	78
normalized size	1	1.00	0.90	0.97	1.06	1.36	1.07	0.97	0.91
time (sec)	N/A	0.053	0.025	0.007	1.395	0.447	0.405	1.153	0.158

Problem 182	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	77	77	67	72	81	107	85	73	67
normalized size	1	1.00	0.87	0.94	1.05	1.39	1.10	0.95	0.87
time (sec)	N/A	0.046	0.023	0.007	1.357	0.447	0.359	1.120	0.124

Problem 183	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	55	61	69	95	70	61	54
normalized size	1	1.00	0.86	0.95	1.08	1.48	1.09	0.95	0.84
time (sec)	N/A	0.036	0.018	0.007	1.332	0.484	0.339	0.947	0.078

Problem 184	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	40	49	57	83	58	44	43
normalized size	1	1.00	0.80	0.98	1.14	1.66	1.16	0.88	0.86
time (sec)	N/A	0.026	0.040	0.007	1.315	0.464	0.310	0.964	0.146

Problem 185	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	33	40	48	61	46	37	46
normalized size	1	1.00	0.80	0.98	1.17	1.49	1.12	0.90	1.12
time (sec)	N/A	0.020	0.013	0.006	1.341	0.465	0.250	1.080	0.093

Problem 186	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	20	27	32	32	32	18	32
normalized size	1	1.00	1.18	1.59	1.88	1.88	1.88	1.06	1.88
time (sec)	N/A	0.002	0.005	0.003	1.392	0.481	0.200	1.142	0.072

Problem 187	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	24	26	12	26
normalized size	1	1.00	1.00	0.93	0.86	1.71	1.86	0.86	1.86
time (sec)	N/A	0.001	0.002	0.000	1.287	0.483	0.209	0.948	0.068

Problem 188	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	37	42	51	80	46	43	43
normalized size	1	1.00	0.86	0.98	1.19	1.86	1.07	1.00	1.00
time (sec)	N/A	0.019	0.029	0.008	1.349	0.448	0.349	1.031	0.100

Problem 189	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	53	56	69	109	66	60	63
normalized size	1	1.00	0.93	0.98	1.21	1.91	1.16	1.05	1.11
time (sec)	N/A	0.029	0.049	0.009	1.318	0.497	0.404	1.074	0.114

Problem 190	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	76	76	68	73	86	130	78	73	79
normalized size	1	1.00	0.89	0.96	1.13	1.71	1.03	0.96	1.04
time (sec)	N/A	0.036	0.052	0.010	1.371	0.545	0.406	1.386	0.119

Problem 191	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	79	84	97	141	92	86	91
normalized size	1	1.00	0.89	0.94	1.09	1.58	1.03	0.97	1.02
time (sec)	N/A	0.048	0.068	0.012	1.456	0.513	0.480	0.938	0.128

Problem 192	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	97	97	90	94	108	152	102	97	101
normalized size	1	1.00	0.93	0.97	1.11	1.57	1.05	1.00	1.04
time (sec)	N/A	0.052	0.057	0.012	1.348	0.498	0.476	1.008	0.092

Problem 193	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	114	114	101	109	125	162	131	106	103
normalized size	1	1.00	0.89	0.96	1.10	1.42	1.15	0.93	0.90
time (sec)	N/A	0.085	0.036	0.008	1.435	0.583	0.524	1.110	0.370

Problem 194	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	105	105	90	98	114	151	119	95	90
normalized size	1	1.00	0.86	0.93	1.09	1.44	1.13	0.90	0.86
time (sec)	N/A	0.070	0.028	0.008	1.395	0.470	0.483	1.013	0.221

Problem 195	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	90	90	90	87	102	139	107	83	79
normalized size	1	1.00	1.00	0.97	1.13	1.54	1.19	0.92	0.88
time (sec)	N/A	0.057	0.022	0.009	1.422	0.429	0.484	1.110	0.153

Problem 196	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	68	76	91	129	94	72	66
normalized size	1	1.00	0.84	0.94	1.12	1.59	1.16	0.89	0.81
time (sec)	N/A	0.048	0.024	0.008	1.458	0.437	0.461	0.873	0.125

Problem 197	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	51	64	79	116	82	55	55
normalized size	1	1.00	0.78	0.98	1.22	1.78	1.26	0.85	0.85
time (sec)	N/A	0.036	0.045	0.008	1.405	0.429	0.398	0.864	0.173

Problem 198	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	44	55	70	94	70	46	45
normalized size	1	1.00	0.76	0.95	1.21	1.62	1.21	0.79	0.78
time (sec)	N/A	0.030	0.016	0.006	1.391	0.449	0.306	1.032	0.070

Problem 199	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	31	41	54	54	56	29	56
normalized size	1	1.00	1.82	2.41	3.18	3.18	3.29	1.71	3.29
time (sec)	N/A	0.002	0.011	0.005	1.405	0.445	0.297	1.269	0.085

Problem 200	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	20	27	43	43	44	18	44
normalized size	1	1.00	0.67	0.90	1.43	1.43	1.47	0.60	1.47
time (sec)	N/A	0.013	0.005	0.005	1.374	0.456	0.317	1.008	0.072

Problem 201	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	35	37	12	37
normalized size	1	1.00	1.00	0.93	0.86	2.50	2.64	0.86	2.64
time (sec)	N/A	0.002	0.003	0.002	1.379	0.414	0.265	1.021	0.077

Problem 202	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	48	54	73	124	70	54	60
normalized size	1	1.00	0.84	0.95	1.28	2.18	1.23	0.95	1.05
time (sec)	N/A	0.028	0.034	0.007	1.466	0.462	0.444	1.024	0.128

Problem 203	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	64	69	91	153	90	71	85
normalized size	1	1.00	0.91	0.99	1.30	2.19	1.29	1.01	1.21
time (sec)	N/A	0.039	0.059	0.009	1.401	0.464	0.460	1.160	0.084

Problem 204	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	79	88	108	174	104	86	101
normalized size	1	1.00	0.85	0.95	1.16	1.87	1.12	0.92	1.09
time (sec)	N/A	0.048	0.057	0.012	1.413	0.479	0.557	0.953	0.136

Problem 205	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	88	99	117	183	114	93	113
normalized size	1	1.00	0.86	0.97	1.15	1.79	1.12	0.91	1.11
time (sec)	N/A	0.053	0.055	0.011	1.405	0.489	0.529	0.987	0.104

Problem 206	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	117	117	101	110	130	196	128	108	123
normalized size	1	1.00	0.86	0.94	1.11	1.68	1.09	0.92	1.05
time (sec)	N/A	0.070	0.068	0.011	1.390	0.445	0.582	1.000	0.173

Problem 207	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	150	150	139	143	180	250	190	128	126
normalized size	1	1.00	0.93	0.95	1.20	1.67	1.27	0.85	0.84
time (sec)	N/A	0.135	0.027	0.011	1.472	0.487	0.931	1.207	1.086

Problem 208	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	139	139	128	132	169	239	180	117	115
normalized size	1	1.00	0.92	0.95	1.22	1.72	1.29	0.84	0.83
time (sec)	N/A	0.114	0.032	0.010	1.587	0.474	0.914	1.475	0.553

Problem 209	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	128	128	104	121	157	228	165	105	102
normalized size	1	1.00	0.81	0.95	1.23	1.78	1.29	0.82	0.80
time (sec)	N/A	0.089	0.048	0.009	1.564	0.475	0.843	1.069	0.179

Problem 210	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	118	118	104	109	145	215	153	88	91
normalized size	1	1.00	0.88	0.92	1.23	1.82	1.30	0.75	0.77
time (sec)	N/A	0.071	0.029	0.009	1.490	0.436	0.820	0.916	0.336

Problem 211	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	109	109	77	100	136	193	141	79	81
normalized size	1	1.00	0.71	0.92	1.25	1.77	1.29	0.72	0.74
time (sec)	N/A	0.064	0.024	0.007	1.448	0.467	0.642	1.164	0.106

Problem 212	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	64	87	120	120	128	62	72
normalized size	1	1.00	3.76	5.12	7.06	7.06	7.53	3.65	4.24
time (sec)	N/A	0.002	0.011	0.005	1.434	0.448	0.583	1.083	0.122

Problem 213	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	53	72	109	109	116	51	22
normalized size	1	1.00	1.51	2.06	3.11	3.11	3.31	1.46	0.63
time (sec)	N/A	0.005	0.010	0.006	1.452	0.480	0.573	1.143	0.072

Problem 214	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	64	42	57	98	98	104	40	48
normalized size	1	1.23	0.81	1.10	1.88	1.88	2.00	0.77	0.92
time (sec)	N/A	0.029	0.010	0.005	1.401	0.442	0.559	1.001	0.068

Problem 215	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	31	42	87	87	92	29	31
normalized size	1	1.00	0.66	0.89	1.85	1.85	1.96	0.62	0.66
time (sec)	N/A	0.021	0.008	0.004	1.451	0.452	0.547	0.997	0.080

Problem 216	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	20	27	76	76	80	18	18
normalized size	1	1.00	0.67	0.90	2.53	2.53	2.67	0.60	0.60
time (sec)	N/A	0.013	0.006	0.007	1.373	0.440	0.503	1.392	0.100

Problem 217	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	68	73	12	70
normalized size	1	1.00	1.00	0.93	0.86	4.86	5.21	0.86	5.00
time (sec)	N/A	0.002	0.003	0.001	1.411	0.479	0.464	1.091	0.064

Problem 218	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	99	99	81	90	139	256	141	87	102
normalized size	1	1.00	0.82	0.91	1.40	2.59	1.42	0.88	1.03
time (sec)	N/A	0.049	0.063	0.010	1.512	0.461	0.681	1.014	0.455

Problem 219	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	117	117	97	108	157	285	162	104	151
normalized size	1	1.00	0.83	0.92	1.34	2.44	1.38	0.89	1.29
time (sec)	N/A	0.073	0.094	0.010	1.590	0.450	0.797	1.048	0.186

Problem 220	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	144	144	112	133	174	306	175	119	167
normalized size	1	1.00	0.78	0.92	1.21	2.12	1.22	0.83	1.16
time (sec)	N/A	0.089	0.073	0.012	1.548	0.509	0.843	1.273	0.209

Problem 221	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	157	157	123	144	185	317	187	130	179
normalized size	1	1.00	0.78	0.92	1.18	2.02	1.19	0.83	1.14
time (sec)	N/A	0.103	0.092	0.013	1.592	0.436	0.992	1.254	0.311

Problem 222	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	186	186	161	177	234	338	250	149	151
normalized size	1	1.00	0.87	0.95	1.26	1.82	1.34	0.80	0.81
time (sec)	N/A	0.177	0.047	0.012	1.730	0.466	1.545	1.069	0.979

Problem 223	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	177	177	150	166	223	327	236	138	138
normalized size	1	1.00	0.85	0.94	1.26	1.85	1.33	0.78	0.78
time (sec)	N/A	0.142	0.029	0.010	1.651	0.433	1.477	1.696	0.227

Problem 224	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	159	159	137	154	211	314	224	121	127
normalized size	1	1.00	0.86	0.97	1.33	1.97	1.41	0.76	0.80
time (sec)	N/A	0.121	0.033	0.011	1.660	0.467	1.326	1.287	0.943

Problem 225	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	154	154	111	145	202	292	212	112	117
normalized size	1	1.00	0.72	0.94	1.31	1.90	1.38	0.73	0.76
time (sec)	N/A	0.108	0.034	0.007	1.601	0.462	1.105	1.216	0.187

Problem 226	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	97	131	186	186	199	95	107
normalized size	1	1.00	5.71	7.71	10.94	10.94	11.71	5.59	6.29
time (sec)	N/A	0.002	0.018	0.006	1.509	0.451	0.980	1.231	0.141

Problem 227	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	86	117	175	175	187	84	22
normalized size	1	1.00	2.46	3.34	5.00	5.00	5.34	2.40	0.63
time (sec)	N/A	0.005	0.014	0.006	1.592	0.472	0.999	0.962	0.126

Problem 228	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	52	75	102	164	164	175	73	85
normalized size	1	1.00	1.44	1.96	3.15	3.15	3.37	1.40	1.63
time (sec)	N/A	0.010	0.016	0.007	1.493	0.460	0.913	1.013	0.140

Problem 229	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	64	86	153	153	163	62	71
normalized size	1	1.00	0.93	1.25	2.22	2.22	2.36	0.90	1.03
time (sec)	N/A	0.016	0.015	0.004	1.538	0.438	0.840	0.899	0.078

Problem 230	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	53	72	142	142	151	51	61
normalized size	1	1.00	0.65	0.89	1.75	1.75	1.86	0.63	0.75
time (sec)	N/A	0.040	0.015	0.006	1.455	0.444	0.794	1.219	0.077

Problem 231	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	42	57	131	131	139	40	48
normalized size	1	1.00	0.66	0.89	2.05	2.05	2.17	0.62	0.75
time (sec)	N/A	0.030	0.010	0.005	1.475	0.456	0.698	1.125	0.127

Problem 232	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	31	42	120	120	128	29	31
normalized size	1	1.00	0.66	0.89	2.55	2.55	2.72	0.62	0.66
time (sec)	N/A	0.021	0.011	0.005	1.416	0.442	0.679	1.043	0.150

Problem 233	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	20	27	109	109	116	18	18
normalized size	1	1.00	0.67	0.90	3.63	3.63	3.87	0.60	0.60
time (sec)	N/A	0.014	0.006	0.004	1.421	0.449	0.723	1.045	0.067

Problem 234	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	101	109	12	103
normalized size	1	1.00	1.00	0.93	0.86	7.21	7.79	0.86	7.36
time (sec)	N/A	0.002	0.003	0.001	1.336	0.444	0.671	1.034	0.141

Problem 235	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	141	141	127	126	205	388	212	120	145
normalized size	1	1.00	0.90	0.89	1.45	2.75	1.50	0.85	1.03
time (sec)	N/A	0.075	0.102	0.012	1.755	0.506	1.023	1.048	0.762

Problem 236	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	158	158	130	147	223	417	233	137	217
normalized size	1	1.00	0.82	0.93	1.41	2.64	1.47	0.87	1.37
time (sec)	N/A	0.125	0.127	0.014	1.705	0.500	1.148	1.014	0.395

Problem 237	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	191	191	145	178	240	438	246	152	233
normalized size	1	1.00	0.76	0.93	1.26	2.29	1.29	0.80	1.22
time (sec)	N/A	0.141	0.111	0.015	1.712	0.487	1.176	1.102	0.438

Problem 238	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	198	198	156	189	251	449	258	163	245
normalized size	1	1.00	0.79	0.95	1.27	2.27	1.30	0.82	1.24
time (sec)	N/A	0.165	0.124	0.013	1.720	0.477	1.241	1.349	0.586

Problem 239	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	141	141	141	132	132	136	143	133	132
normalized size	1	1.00	1.00	0.94	0.94	0.96	1.01	0.94	0.94
time (sec)	N/A	0.079	0.011	0.010	1.372	0.482	0.914	1.139	0.081

Problem 240	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	132	132	132	121	121	125	131	122	121
normalized size	1	1.00	1.00	0.92	0.92	0.95	0.99	0.92	0.92
time (sec)	N/A	0.070	0.005	0.010	1.373	0.541	0.848	1.277	0.092

Problem 241	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	114	114	114	109	109	114	117	110	114
normalized size	1	1.00	1.00	0.96	0.96	1.00	1.03	0.96	1.00
time (sec)	N/A	0.058	0.006	0.000	1.432	0.430	0.865	1.056	0.002

Problem 242	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	109	109	109	100	100	103	107	101	100
normalized size	1	1.00	1.00	0.92	0.92	0.94	0.98	0.93	0.92
time (sec)	N/A	0.052	0.005	0.008	1.335	0.465	0.786	1.040	0.082

Problem 243	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	96	91	88	88	95	88	88
normalized size	1	1.00	5.65	5.35	5.18	5.18	5.59	5.18	5.18
time (sec)	N/A	0.002	0.009	0.008	1.337	0.529	0.727	1.168	0.090

Problem 244	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	91	80	79	79	85	79	23
normalized size	1	1.00	2.53	2.22	2.19	2.19	2.36	2.19	0.64
time (sec)	N/A	0.006	0.004	0.000	1.357	0.450	0.705	1.037	0.002

Problem 245	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	80	69	68	68	73	68	68
normalized size	1	1.00	1.43	1.23	1.21	1.21	1.30	1.21	1.21
time (sec)	N/A	0.010	0.009	0.007	1.368	0.432	0.563	1.018	0.098

Problem 246	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	67	58	57	57	61	57	56
normalized size	1	1.00	1.00	0.87	0.85	0.85	0.91	0.85	0.84
time (sec)	N/A	0.025	0.007	0.000	1.362	0.441	0.493	1.011	0.002

Problem 247	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	56	47	46	46	49	46	46
normalized size	1	1.00	1.00	0.84	0.82	0.82	0.88	0.82	0.82
time (sec)	N/A	0.019	0.008	0.006	1.335	0.455	0.497	1.246	0.035

Problem 248	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	43	36	35	35	37	35	35
normalized size	1	1.00	1.00	0.84	0.81	0.81	0.86	0.81	0.81
time (sec)	N/A	0.014	0.004	0.004	1.346	0.473	0.379	1.086	0.032

Problem 249	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	25	24	24	26	24	24
normalized size	1	1.00	1.00	0.83	0.80	0.80	0.87	0.80	0.80
time (sec)	N/A	0.009	0.007	0.005	1.341	0.430	0.270	0.873	0.036

Problem 250	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	14	13	13	14	13	13
normalized size	1	1.00	1.00	0.82	0.76	0.76	0.82	0.76	0.76
time (sec)	N/A	0.005	0.002	0.005	1.303	0.460	0.210	0.995	0.029

Problem 251	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	6	5	5	7	5	5
normalized size	1	1.00	1.00	0.86	0.71	0.71	1.00	0.71	0.71
time (sec)	N/A	0.000	0.000	0.002	1.318	0.448	0.074	1.044	0.020

Problem 252	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	134	134	134	119	117	120	116	122	114
normalized size	1	1.00	1.00	0.89	0.87	0.90	0.87	0.91	0.85
time (sec)	N/A	0.061	0.006	0.010	1.349	0.501	0.410	1.161	0.127

Problem 253	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	146	146	134	135	141	163	139	180	135
normalized size	1	1.00	0.92	0.92	0.97	1.12	0.95	1.23	0.92
time (sec)	N/A	0.090	0.094	0.011	1.398	0.472	0.613	1.284	0.083

Problem 254	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	163	163	145	150	163	207	163	152	157
normalized size	1	1.00	0.89	0.92	1.00	1.27	1.00	0.93	0.96
time (sec)	N/A	0.108	0.108	0.014	1.432	0.478	0.678	1.128	0.228

Problem 255	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	14	13	13	12	15	10
normalized size	1	1.00	1.00	0.82	0.76	0.76	0.71	0.88	0.59
time (sec)	N/A	0.002	0.003	0.006	1.342	0.462	0.117	1.147	0.170

Problem 256	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	14	13	13	12	15	10
normalized size	1	1.00	1.00	0.82	0.76	0.76	0.71	0.88	0.59
time (sec)	N/A	0.002	0.003	0.001	1.295	0.530	0.120	1.006	0.143

Problem 257	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	24	24	24	19	18	21	20	20	18
normalized size	1	1.00	1.00	0.79	0.75	0.88	0.83	0.83	0.75
time (sec)	N/A	0.008	0.003	0.007	1.381	0.531	0.139	1.013	0.054

Problem 258	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	31	24	23	28	26	25	18
normalized size	1	1.00	1.00	0.77	0.74	0.90	0.84	0.81	0.58
time (sec)	N/A	0.010	0.003	0.008	1.294	0.518	0.147	1.072	0.037

Problem 259	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	38	29	28	33	31	30	24
normalized size	1	1.00	1.00	0.76	0.74	0.87	0.82	0.79	0.63
time (sec)	N/A	0.012	0.003	0.006	1.353	0.472	0.162	1.028	0.088

Problem 260	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	45	34	33	38	36	35	28
normalized size	1	1.00	1.00	0.76	0.73	0.84	0.80	0.78	0.62
time (sec)	N/A	0.012	0.003	0.006	1.325	0.480	0.166	1.140	0.040

Problem 261	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	26	23	22	32	19	25	20
normalized size	1	1.00	0.93	0.82	0.79	1.14	0.68	0.89	0.71
time (sec)	N/A	0.009	0.013	0.007	1.367	0.451	0.136	1.114	0.055

Problem 262	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	31	28	31	48	31	40	34
normalized size	1	1.00	0.89	0.80	0.89	1.37	0.89	1.14	0.97
time (sec)	N/A	0.010	0.013	0.008	1.387	0.505	0.148	0.951	0.089

Problem 263	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	36	33	38	59	36	51	31
normalized size	1	1.00	0.86	0.79	0.90	1.40	0.86	1.21	0.74
time (sec)	N/A	0.014	0.013	0.009	1.315	0.467	0.157	0.937	0.042

Problem 264	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	44	38	43	64	41	60	37
normalized size	1	1.00	0.90	0.78	0.88	1.31	0.84	1.22	0.76
time (sec)	N/A	0.016	0.030	0.006	1.308	0.445	0.169	1.232	0.093

Problem 265	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	56	43	48	69	46	69	41
normalized size	1	1.00	1.00	0.77	0.86	1.23	0.82	1.23	0.73
time (sec)	N/A	0.020	0.010	0.009	1.357	0.491	0.175	1.154	0.095

Problem 266	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	29	32	30	50	27	27	29
normalized size	1	1.00	0.74	0.82	0.77	1.28	0.69	0.69	0.74
time (sec)	N/A	0.012	0.020	0.007	1.389	0.487	0.170	1.034	0.125

Problem 267	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	39	37	41	68	41	37	35
normalized size	1	1.00	0.85	0.80	0.89	1.48	0.89	0.80	0.76
time (sec)	N/A	0.015	0.021	0.009	1.391	0.482	0.180	0.894	0.092

Problem 268	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	44	42	48	79	46	43	41
normalized size	1	1.00	0.83	0.79	0.91	1.49	0.87	0.81	0.77
time (sec)	N/A	0.016	0.025	0.009	1.384	0.500	0.181	1.068	0.094

Problem 269	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	49	47	53	84	51	47	47
normalized size	1	1.00	0.82	0.78	0.88	1.40	0.85	0.78	0.78
time (sec)	N/A	0.021	0.019	0.008	1.380	0.453	0.207	1.291	0.046

Problem 270	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	54	52	58	89	56	52	51
normalized size	1	1.00	0.81	0.78	0.87	1.33	0.84	0.78	0.76
time (sec)	N/A	0.022	0.022	0.010	1.385	0.474	0.216	1.133	0.047

Problem 271	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	8	8	10	9	6	6	7	7	6
normalized size	1	1.00	1.25	1.12	0.75	0.75	0.88	0.88	0.75
time (sec)	N/A	0.001	0.001	0.001	1.337	0.515	0.074	0.902	0.151

Problem 272	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	10	10	10	9	8	8	8	9	6
normalized size	1	1.00	1.00	0.90	0.80	0.80	0.80	0.90	0.60
time (sec)	N/A	0.001	0.001	0.002	1.339	0.494	0.071	1.146	0.077

Problem 273	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	16	13	12	10	14	13	10
normalized size	1	1.00	1.14	0.93	0.86	0.71	1.00	0.93	0.71
time (sec)	N/A	0.002	0.004	0.002	1.251	0.482	0.079	1.285	0.105

Problem 274	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	17	16	20	17	17	16
normalized size	1	1.00	1.00	0.85	0.80	1.00	0.85	0.85	0.80
time (sec)	N/A	0.007	0.005	0.000	1.372	0.490	0.081	1.102	0.108

Problem 275	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	22	19	18	21	19	19	14
normalized size	1	1.00	1.00	0.86	0.82	0.95	0.86	0.86	0.64
time (sec)	N/A	0.002	0.004	0.001	1.322	0.505	0.079	0.931	0.052

Problem 276	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	22	19	18	23	19	19	16
normalized size	1	1.00	1.00	0.86	0.82	1.05	0.86	0.86	0.73
time (sec)	N/A	0.002	0.004	0.001	1.308	0.481	0.080	1.091	0.057

Problem 277	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	19	18	24	19	19	16
normalized size	1	1.00	1.00	0.90	0.86	1.14	0.90	0.90	0.76
time (sec)	N/A	0.004	0.007	0.000	1.327	0.489	0.092	1.040	0.152

Problem 278	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	22	19	18	24	20	19	14
normalized size	1	1.00	1.10	0.95	0.90	1.20	1.00	0.95	0.70
time (sec)	N/A	0.004	0.009	0.001	1.310	0.488	0.088	1.079	0.175

Problem 279	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	11	12	11	11	8	13	9
normalized size	1	1.00	1.00	1.09	1.00	1.00	0.73	1.18	0.82
time (sec)	N/A	0.002	0.003	0.004	1.305	0.458	0.135	0.992	0.097

Problem 280	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	12	12	12	12	11	11	8	13	9
normalized size	1	1.00	1.00	1.00	0.92	0.92	0.67	1.08	0.75
time (sec)	N/A	0.002	0.003	0.006	1.361	0.481	0.125	1.021	0.036

Problem 281	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	19	20	19	21	14	21	16
normalized size	1	1.00	1.00	1.05	1.00	1.11	0.74	1.11	0.84
time (sec)	N/A	0.008	0.004	0.007	1.318	0.462	0.177	0.916	0.043

Problem 282	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	18	17	21	14	19	14
normalized size	1	1.00	1.00	1.00	0.94	1.17	0.78	1.06	0.78
time (sec)	N/A	0.010	0.003	0.006	1.333	0.505	0.191	1.144	0.029

Problem 283	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	15	14	15	10	15	20
normalized size	1	1.00	1.00	1.07	1.00	1.07	0.71	1.07	1.43
time (sec)	N/A	0.009	0.005	0.001	1.325	0.483	0.148	1.251	0.036

Problem 284	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	46	43	56	53	1742	116	56
normalized size	1	1.00	0.64	0.60	0.78	0.74	24.19	1.61	0.78
time (sec)	N/A	0.018	0.023	0.015	1.250	0.507	2.910	0.948	0.050

Problem 285	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	35	32	41	42	666	93	37
normalized size	1	1.00	0.66	0.60	0.77	0.79	12.57	1.75	0.70
time (sec)	N/A	0.013	0.016	0.004	1.407	0.561	2.039	1.032	0.046

Problem 286	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	24	21	26	30	202	66	25
normalized size	1	1.00	0.71	0.62	0.76	0.88	5.94	1.94	0.74
time (sec)	N/A	0.008	0.011	0.003	1.315	0.519	1.393	1.284	0.028

Problem 287	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	12	12	12	12
normalized size	1	1.00	1.00	0.81	0.75	0.75	0.75	0.75	0.75
time (sec)	N/A	0.001	0.004	0.003	1.336	0.517	0.074	1.058	0.021

Problem 288	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	35	28	42	73	68	32	27
normalized size	1	1.00	1.00	0.80	1.20	2.09	1.94	0.91	0.77
time (sec)	N/A	0.010	0.009	0.013	2.919	0.569	1.602	1.131	0.094

Problem 289	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	47	37	47	93	44	41	31
normalized size	1	1.00	1.21	0.95	1.21	2.38	1.13	1.05	0.79
time (sec)	N/A	0.011	0.027	0.012	2.869	0.544	2.221	0.964	0.053

Problem 290	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	35	53	88	119	97	66	48
normalized size	1	1.00	0.54	0.82	1.35	1.83	1.49	1.02	0.74
time (sec)	N/A	0.018	0.007	0.012	3.027	0.559	4.015	1.136	0.068

Problem 291	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	87	87	35	65	121	145	122	84	66
normalized size	1	1.00	0.40	0.75	1.39	1.67	1.40	0.97	0.76
time (sec)	N/A	0.027	0.007	0.013	3.020	0.592	6.678	1.229	0.107

Problem 292	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	46	43	56	64	1742	193	56
normalized size	1	1.00	0.64	0.60	0.78	0.89	24.19	2.68	0.78
time (sec)	N/A	0.019	0.024	0.005	1.348	0.468	3.199	1.108	0.048

Problem 293	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	35	32	41	53	733	156	37
normalized size	1	1.00	0.66	0.60	0.77	1.00	13.83	2.94	0.70
time (sec)	N/A	0.013	0.017	0.006	1.347	0.478	2.175	0.936	0.041

Problem 294	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	24	21	26	41	80	119	25
normalized size	1	1.00	0.71	0.62	0.76	1.21	2.35	3.50	0.74
time (sec)	N/A	0.008	0.013	0.002	1.347	0.498	0.740	1.240	0.026

Problem 295	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	28	12	58	12
normalized size	1	1.00	1.00	0.81	0.75	1.75	0.75	3.62	0.75
time (sec)	N/A	0.001	0.005	0.001	1.287	0.442	0.072	1.126	0.016

Problem 296	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	44	38	52	88	71	44	37
normalized size	1	1.00	0.90	0.78	1.06	1.80	1.45	0.90	0.76
time (sec)	N/A	0.014	0.021	0.007	2.937	0.514	2.295	1.077	0.042

Problem 297	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	33	47	58	102	92	56	42
normalized size	1	1.00	0.65	0.92	1.14	2.00	1.80	1.10	0.82
time (sec)	N/A	0.015	0.007	0.011	2.875	0.473	2.664	1.043	0.100

Problem 298	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	62	62	68	51	86	124	76	64	46
normalized size	1	1.00	1.10	0.82	1.39	2.00	1.23	1.03	0.74
time (sec)	N/A	0.016	0.034	0.012	2.984	0.523	3.283	1.287	0.057

Problem 299	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	35	63	119	145	124	84	64
normalized size	1	1.00	0.42	0.75	1.42	1.73	1.48	1.00	0.76
time (sec)	N/A	0.022	0.009	0.012	3.047	0.543	5.837	1.161	0.102

Problem 300	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	46	43	56	75	146	281	56
normalized size	1	1.00	0.64	0.60	0.78	1.04	2.03	3.90	0.78
time (sec)	N/A	0.017	0.027	0.006	1.347	0.478	4.469	1.158	0.050

Problem 301	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	35	32	41	64	124	233	37
normalized size	1	1.00	0.66	0.60	0.77	1.21	2.34	4.40	0.70
time (sec)	N/A	0.012	0.020	0.005	1.366	0.436	3.770	1.090	0.044

Problem 302	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	24	21	26	52	102	182	25
normalized size	1	1.00	0.71	0.62	0.76	1.53	3.00	5.35	0.74
time (sec)	N/A	0.009	0.016	0.003	1.371	0.485	2.599	1.152	0.028

Problem 303	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	39	12	95	12
normalized size	1	1.00	1.00	0.81	0.75	2.44	0.75	5.94	0.75
time (sec)	N/A	0.001	0.006	0.002	1.341	0.435	0.077	0.983	0.018

Problem 304	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	58	50	64	114	97	56	52
normalized size	1	1.00	0.89	0.77	0.98	1.75	1.49	0.86	0.80
time (sec)	N/A	0.021	0.048	0.007	3.017	0.480	4.117	1.027	0.053

Problem 305	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	33	61	71	126	99	74	58
normalized size	1	1.00	0.50	0.92	1.08	1.91	1.50	1.12	0.88
time (sec)	N/A	0.020	0.009	0.010	2.945	0.478	3.747	1.088	0.115

Problem 306	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	35	61	101	133	126	80	64
normalized size	1	1.00	0.45	0.78	1.29	1.71	1.62	1.03	0.82
time (sec)	N/A	0.021	0.009	0.010	2.940	0.488	4.300	1.120	0.053

Problem 307	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	79	63	115	146	104	79	64
normalized size	1	1.00	0.98	0.78	1.42	1.80	1.28	0.98	0.79
time (sec)	N/A	0.023	0.038	0.010	2.985	0.493	5.157	1.130	0.046

Problem 308	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	103	103	35	75	144	167	155	99	79
normalized size	1	1.00	0.34	0.73	1.40	1.62	1.50	0.96	0.77
time (sec)	N/A	0.031	0.009	0.012	2.934	0.502	8.359	1.094	0.111

Problem 309	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	146	146	90	87	116	141	279	781	116
normalized size	1	1.00	0.62	0.60	0.79	0.97	1.91	5.35	0.79
time (sec)	N/A	0.042	0.055	0.006	1.334	0.462	40.296	1.140	0.036

Problem 310	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	127	127	79	76	101	130	257	709	101
normalized size	1	1.00	0.62	0.60	0.80	1.02	2.02	5.58	0.80
time (sec)	N/A	0.035	0.042	0.007	1.343	0.468	36.609	1.324	0.031

Problem 311	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	110	110	68	65	86	119	235	637	86
normalized size	1	1.00	0.62	0.59	0.78	1.08	2.14	5.79	0.78
time (sec)	N/A	0.032	0.038	0.006	1.347	0.559	28.760	1.054	0.027

Problem 312	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	91	91	57	54	71	108	212	565	71
normalized size	1	1.00	0.63	0.59	0.78	1.19	2.33	6.21	0.78
time (sec)	N/A	0.023	0.032	0.006	1.359	0.516	25.700	1.122	0.025

Problem 313	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	46	43	56	97	190	493	56
normalized size	1	1.00	0.64	0.60	0.78	1.35	2.64	6.85	0.78
time (sec)	N/A	0.018	0.030	0.006	1.293	0.461	20.346	1.102	0.045

Problem 314	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	35	32	41	86	168	421	36
normalized size	1	1.00	0.66	0.60	0.77	1.62	3.17	7.94	0.68
time (sec)	N/A	0.013	0.022	0.004	1.341	0.460	16.856	1.058	0.040

Problem 315	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	24	21	26	74	146	347	25
normalized size	1	1.00	0.71	0.62	0.76	2.18	4.29	10.21	0.74
time (sec)	N/A	0.008	0.017	0.003	1.356	0.468	14.851	1.269	0.030

Problem 316	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	61	12	229	12
normalized size	1	1.00	1.00	0.81	0.75	3.81	0.75	14.31	0.75
time (sec)	N/A	0.002	0.007	0.003	1.336	0.468	0.083	0.991	0.018

Problem 317	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	97	97	78	74	88	158	148	80	76
normalized size	1	1.00	0.80	0.76	0.91	1.63	1.53	0.82	0.78
time (sec)	N/A	0.034	0.085	0.007	2.942	0.499	11.102	1.227	0.037

Problem 318	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	33	84	97	172	150	104	84
normalized size	1	1.00	0.34	0.86	0.99	1.76	1.53	1.06	0.86
time (sec)	N/A	0.034	0.011	0.010	2.968	0.467	9.922	1.427	0.043

Problem 319	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	114	114	35	86	131	180	184	112	117
normalized size	1	1.00	0.31	0.75	1.15	1.58	1.61	0.98	1.03
time (sec)	N/A	0.035	0.011	0.011	2.952	0.484	8.989	1.104	0.047

Problem 320	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	114	114	35	87	145	178	184	112	131
normalized size	1	1.00	0.31	0.76	1.27	1.56	1.61	0.98	1.15
time (sec)	N/A	0.036	0.011	0.013	2.939	0.480	7.912	1.101	0.121

Problem 321	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	116	116	35	85	155	177	182	110	94
normalized size	1	1.00	0.30	0.73	1.34	1.53	1.57	0.95	0.81
time (sec)	N/A	0.037	0.011	0.013	2.965	0.545	8.547	1.215	0.062

Problem 322	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	101	87	169	190	158	109	94
normalized size	1	1.00	0.85	0.73	1.42	1.60	1.33	0.92	0.79
time (sec)	N/A	0.039	0.044	0.013	2.965	0.550	10.250	1.190	0.119

Problem 323	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	141	141	35	99	198	211	209	129	109
normalized size	1	1.00	0.25	0.70	1.40	1.50	1.48	0.91	0.77
time (sec)	N/A	0.051	0.011	0.014	3.034	0.467	15.689	1.042	0.133

Problem 324	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	163	163	35	111	229	233	236	144	124
normalized size	1	1.00	0.21	0.68	1.40	1.43	1.45	0.88	0.76
time (sec)	N/A	0.068	0.011	0.014	3.083	0.503	22.200	0.951	0.126

Problem 325	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	39	32	31	78	148	31	31
normalized size	1	1.00	1.00	0.82	0.79	2.00	3.79	0.79	0.79
time (sec)	N/A	0.011	0.011	0.007	2.939	0.540	1.737	1.136	0.094

Problem 326	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	52	35	34	98	121	41	34
normalized size	1	1.00	1.24	0.83	0.81	2.33	2.88	0.98	0.81
time (sec)	N/A	0.010	0.024	0.012	2.942	0.486	2.140	1.081	0.097

Problem 327	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	38	55	83	124	207	66	54
normalized size	1	1.00	0.54	0.77	1.17	1.75	2.92	0.93	0.76
time (sec)	N/A	0.016	0.009	0.010	2.964	0.486	4.161	1.081	0.103

Problem 328	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	55	55	48	44	43	93	187	43	43
normalized size	1	1.00	0.87	0.80	0.78	1.69	3.40	0.78	0.78
time (sec)	N/A	0.015	0.024	0.007	3.018	0.519	2.463	1.058	0.041

Problem 329	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	36	48	47	105	197	58	47
normalized size	1	1.00	0.63	0.84	0.82	1.84	3.46	1.02	0.82
time (sec)	N/A	0.014	0.009	0.011	3.001	0.483	2.837	0.959	0.045

Problem 330	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	72	53	80	129	190	66	52
normalized size	1	1.00	1.06	0.78	1.18	1.90	2.79	0.97	0.76
time (sec)	N/A	0.015	0.035	0.012	3.021	0.521	3.302	0.952	0.097

Problem 331	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	73	73	60	58	57	119	240	57	57
normalized size	1	1.00	0.82	0.79	0.78	1.63	3.29	0.78	0.78
time (sec)	N/A	0.019	0.033	0.006	2.918	0.527	4.241	1.218	0.043

Problem 332	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	36	64	63	131	245	75	63
normalized size	1	1.00	0.49	0.86	0.85	1.77	3.31	1.01	0.85
time (sec)	N/A	0.020	0.011	0.012	3.049	0.502	3.686	1.020	0.103

Problem 333	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	38	70	97	139	267	83	69
normalized size	1	1.00	0.44	0.81	1.13	1.62	3.10	0.97	0.80
time (sec)	N/A	0.022	0.010	0.013	2.924	0.506	3.927	1.037	0.095

Problem 334	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	57	54	71	53	3755	61	71
normalized size	1	1.00	0.64	0.61	0.80	0.60	42.19	0.69	0.80
time (sec)	N/A	0.022	0.028	0.006	1.345	0.785	4.839	1.040	0.024

Problem 335	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	46	43	56	42	1640	49	56
normalized size	1	1.00	0.68	0.63	0.82	0.62	24.12	0.72	0.82
time (sec)	N/A	0.018	0.026	0.003	1.254	0.442	2.703	1.207	0.046

Problem 336	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	35	32	41	31	600	37	37
normalized size	1	1.00	0.69	0.63	0.80	0.61	11.76	0.73	0.73
time (sec)	N/A	0.012	0.016	0.005	1.323	0.447	1.767	1.342	0.038

Problem 337	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	23	21	26	19	162	23	25
normalized size	1	1.00	0.72	0.66	0.81	0.59	5.06	0.72	0.78
time (sec)	N/A	0.008	0.011	0.003	1.320	0.432	1.160	1.006	0.027

Problem 338	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	12	10	12	12
normalized size	1	1.00	1.00	0.93	0.86	0.86	0.71	0.86	0.86
time (sec)	N/A	0.001	0.003	0.002	1.298	0.443	0.066	0.985	0.018

Problem 339	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	23	18	32	56	24	21	17
normalized size	1	1.00	1.00	0.78	1.39	2.43	1.04	0.91	0.74
time (sec)	N/A	0.007	0.004	0.006	2.936	0.430	1.108	1.244	0.055

Problem 340	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	47	40	60	93	44	47	33
normalized size	1	1.00	1.15	0.98	1.46	2.27	1.07	1.15	0.80
time (sec)	N/A	0.011	0.065	0.006	2.999	0.441	2.302	1.069	0.111

Problem 341	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	33	66	92	123	102	69	51
normalized size	1	1.00	0.49	0.97	1.35	1.81	1.50	1.01	0.75
time (sec)	N/A	0.017	0.006	0.006	2.917	0.495	4.366	1.195	0.061

Problem 342	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	90	90	33	90	121	145	129	84	69
normalized size	1	1.00	0.37	1.00	1.34	1.61	1.43	0.93	0.77
time (sec)	N/A	0.025	0.006	0.008	2.916	0.478	7.022	0.908	0.052

Problem 343	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	85	85	57	54	71	63	3606	77	71
normalized size	1	1.00	0.67	0.64	0.84	0.74	42.42	0.91	0.84
time (sec)	N/A	0.024	0.028	0.006	1.329	0.418	4.806	1.252	0.028

Problem 344	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	45	42	56	51	1538	61	56
normalized size	1	1.00	0.68	0.64	0.85	0.77	23.30	0.92	0.85
time (sec)	N/A	0.017	0.020	0.006	1.375	0.451	2.935	1.102	0.048

Problem 345	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	34	32	41	40	534	46	35
normalized size	1	1.00	0.69	0.65	0.84	0.82	10.90	0.94	0.71
time (sec)	N/A	0.013	0.016	0.006	1.290	0.449	1.827	1.145	0.040

Problem 346	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	21	20	26	29	37	29	19
normalized size	1	1.00	0.70	0.67	0.87	0.97	1.23	0.97	0.63
time (sec)	N/A	0.008	0.010	0.003	1.324	0.479	0.669	0.995	0.087

Problem 347	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	20	12	12	12
normalized size	1	1.00	1.00	0.93	0.86	1.43	0.86	0.86	0.86
time (sec)	N/A	0.001	0.004	0.002	1.341	0.460	0.070	1.238	0.019

Problem 348	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	30	31	45	110	146	37	30
normalized size	1	1.00	0.79	0.82	1.18	2.89	3.84	0.97	0.79
time (sec)	N/A	0.011	0.005	0.009	2.926	0.463	1.866	1.070	0.043

Problem 349	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	59	31	55	76	151	73	64	60
normalized size	1	1.04	0.54	0.96	1.33	2.65	1.28	1.12	1.05
time (sec)	N/A	0.017	0.007	0.011	3.012	0.503	3.411	0.905	0.122

Problem 350	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	87	85	33	67	108	189	107	80	90
normalized size	1	0.98	0.38	0.77	1.24	2.17	1.23	0.92	1.03
time (sec)	N/A	0.023	0.006	0.013	3.063	0.472	5.983	1.047	0.059

Problem 351	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	87	87	57	54	71	74	3456	75	68
normalized size	1	1.00	0.66	0.62	0.82	0.85	39.72	0.86	0.78
time (sec)	N/A	0.022	0.028	0.005	1.349	0.440	4.575	1.081	0.049

Problem 352	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	45	43	56	62	163	59	47
normalized size	1	1.00	0.66	0.63	0.82	0.91	2.40	0.87	0.69
time (sec)	N/A	0.017	0.024	0.006	1.253	0.475	1.200	1.032	0.043

Problem 353	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	35	32	41	52	121	39	35
normalized size	1	1.00	0.71	0.65	0.84	1.06	2.47	0.80	0.71
time (sec)	N/A	0.013	0.017	0.004	1.328	0.443	1.275	0.940	0.084

Problem 354	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	24	21	26	41	80	20	20
normalized size	1	1.00	0.75	0.66	0.81	1.28	2.50	0.62	0.62
time (sec)	N/A	0.008	0.012	0.003	1.338	0.442	1.128	1.055	0.033

Problem 355	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	31	14	12	12
normalized size	1	1.00	1.00	0.81	0.75	1.94	0.88	0.75	0.75
time (sec)	N/A	0.001	0.005	0.002	1.307	0.478	0.075	1.038	0.018

Problem 356	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	32	43	53	177	697	45	42
normalized size	1	1.00	0.59	0.80	0.98	3.28	12.91	0.83	0.78
time (sec)	N/A	0.015	0.006	0.010	2.912	0.492	2.993	1.003	0.050

Problem 357	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	80	33	67	89	221	818	65	73
normalized size	1	1.08	0.45	0.91	1.20	2.99	11.05	0.88	0.99
time (sec)	N/A	0.024	0.006	0.012	3.032	0.495	5.596	1.027	0.109

Problem 358	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	106	106	35	80	123	255	464	93	105
normalized size	1	1.00	0.33	0.75	1.16	2.41	4.38	0.88	0.99
time (sec)	N/A	0.034	0.007	0.015	3.001	0.479	8.571	0.994	0.120

Problem 359	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	25	25	25	20	19	58	54	19	19
normalized size	1	1.00	1.00	0.80	0.76	2.32	2.16	0.76	0.76
time (sec)	N/A	0.006	0.005	0.004	2.991	0.452	1.226	0.986	0.048

Problem 360	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	44	44	53	37	46	97	121	43	36
normalized size	1	1.00	1.20	0.84	1.05	2.20	2.75	0.98	0.82
time (sec)	N/A	0.011	0.065	0.007	2.976	0.448	2.458	0.886	0.041

Problem 361	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	36	59	86	128	216	68	57
normalized size	1	1.00	0.49	0.80	1.16	1.73	2.92	0.92	0.77
time (sec)	N/A	0.017	0.006	0.007	2.957	0.463	4.199	0.965	0.045

Problem 362	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	33	35	34	124	478	34	34
normalized size	1	1.00	0.79	0.83	0.81	2.95	11.38	0.81	0.81
time (sec)	N/A	0.010	0.007	0.008	2.972	0.484	2.199	1.016	0.095

Problem 363	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	62	65	34	54	67	164	156	64	52
normalized size	1	1.05	0.55	0.87	1.08	2.65	2.52	1.03	0.84
time (sec)	N/A	0.016	0.007	0.014	3.022	0.539	3.499	1.013	0.063

Problem 364	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	93	36	75	104	198	226	81	101
normalized size	1	0.98	0.38	0.79	1.09	2.08	2.38	0.85	1.06
time (sec)	N/A	0.023	0.007	0.014	2.926	0.497	5.567	1.006	0.132

Problem 365	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	35	49	42	182	0	42	48
normalized size	1	1.00	0.58	0.82	0.70	3.03	0.00	0.70	0.80
time (sec)	N/A	0.015	0.008	0.010	2.938	0.480	0.000	1.057	0.092

Problem 366	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	88	36	68	82	226	0	66	70
normalized size	1	1.09	0.44	0.84	1.01	2.79	0.00	0.81	0.86
time (sec)	N/A	0.023	0.009	0.013	2.928	0.479	0.000	1.004	0.118

Problem 367	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	116	116	38	92	121	260	1108	97	117
normalized size	1	1.00	0.33	0.79	1.04	2.24	9.55	0.84	1.01
time (sec)	N/A	0.033	0.007	0.015	2.875	0.467	11.219	0.902	0.071

Problem 368	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	12	11	14	78	0	11
normalized size	1	1.00	1.00	0.92	0.85	1.08	6.00	0.00	0.85
time (sec)	N/A	0.006	0.041	0.006	1.875	0.478	84.074	0.000	0.413

Problem 369	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	C	A	F	A	A	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	92	13	0	11	11	73	0	-1
normalized size	1	7.08	1.00	0.00	0.85	0.85	5.62	0.00	-0.08
time (sec)	N/A	0.045	0.015	0.085	1.862	0.515	5.344	0.000	0.000

Problem 370	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	23	18	32	56	24	21	17
normalized size	1	1.00	1.00	0.78	1.39	2.43	1.04	0.91	0.74
time (sec)	N/A	0.008	0.004	0.000	2.991	0.461	1.091	0.847	0.002

Problem 371	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	46	43	56	53	1742	117	56
normalized size	1	1.00	0.64	0.60	0.78	0.74	24.19	1.62	0.78
time (sec)	N/A	0.019	0.024	0.005	1.385	0.448	2.833	0.867	0.052

Problem 372	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	35	32	41	42	666	92	37
normalized size	1	1.00	0.66	0.60	0.77	0.79	12.57	1.74	0.70
time (sec)	N/A	0.012	0.017	0.006	1.304	0.479	1.856	0.834	0.038

Problem 373	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	24	21	26	30	202	67	25
normalized size	1	1.00	0.71	0.62	0.76	0.88	5.94	1.97	0.74
time (sec)	N/A	0.008	0.012	0.003	1.293	0.491	1.201	1.038	0.028

Problem 374	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	12	12	12	12
normalized size	1	1.00	1.00	0.81	0.75	0.75	0.75	0.75	0.75
time (sec)	N/A	0.001	0.004	0.003	1.257	0.494	0.065	0.892	0.017

Problem 375	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	91	91	113	85	86	91	180	87	107
normalized size	1	1.00	1.24	0.93	0.95	1.00	1.98	0.96	1.18
time (sec)	N/A	0.047	0.047	0.007	3.078	0.494	2.018	2.374	0.121

Problem 376	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	97	97	33	92	93	139	643	105	117
normalized size	1	1.00	0.34	0.95	0.96	1.43	6.63	1.08	1.21
time (sec)	N/A	0.033	0.006	0.008	2.959	0.460	2.185	2.555	0.067

Problem 377	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	127	127	35	113	139	187	2266	128	196
normalized size	1	1.00	0.28	0.89	1.09	1.47	17.84	1.01	1.54
time (sec)	N/A	0.049	0.007	0.011	2.986	0.494	2.577	2.426	0.230

Problem 378	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	46	43	56	53	1742	117	56
normalized size	1	1.00	0.64	0.60	0.78	0.74	24.19	1.62	0.78
time (sec)	N/A	0.018	0.025	0.004	1.364	0.486	3.073	1.125	0.045

Problem 379	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	35	32	41	42	666	92	37
normalized size	1	1.00	0.66	0.60	0.77	0.79	12.57	1.74	0.70
time (sec)	N/A	0.013	0.017	0.006	1.349	0.475	1.938	0.825	0.041

Problem 380	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	24	21	26	31	202	68	25
normalized size	1	1.00	0.71	0.62	0.76	0.91	5.94	2.00	0.74
time (sec)	N/A	0.008	0.012	0.003	1.350	0.480	1.276	0.892	0.028

Problem 381	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	12	12	12	12
normalized size	1	1.00	1.00	0.81	0.75	0.75	0.75	0.75	0.75
time (sec)	N/A	0.002	0.004	0.003	1.286	0.480	0.065	1.144	0.018

Problem 382	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	86	84	85	110	182	86	117
normalized size	1	1.00	0.93	0.91	0.92	1.20	1.98	0.93	1.27
time (sec)	N/A	0.032	0.039	0.003	2.971	0.482	2.056	2.200	0.113

Problem 383	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	94	94	33	92	93	252	643	106	127
normalized size	1	1.00	0.35	0.98	0.99	2.68	6.84	1.13	1.35
time (sec)	N/A	0.033	0.007	0.011	2.982	0.534	2.238	2.292	0.114

Problem 384	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	127	127	35	113	139	350	2266	129	194
normalized size	1	1.00	0.28	0.89	1.09	2.76	17.84	1.02	1.53
time (sec)	N/A	0.047	0.008	0.011	2.983	0.507	2.655	2.470	0.329

Problem 385	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	46	43	56	64	1844	193	56
normalized size	1	1.00	0.64	0.60	0.78	0.89	25.61	2.68	0.78
time (sec)	N/A	0.018	0.025	0.006	1.357	0.496	3.178	1.223	0.047

Problem 386	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	35	32	41	53	733	157	37
normalized size	1	1.00	0.66	0.60	0.77	1.00	13.83	2.96	0.70
time (sec)	N/A	0.013	0.018	0.004	1.303	0.521	2.160	0.984	0.042

Problem 387	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	24	21	26	41	80	118	25
normalized size	1	1.00	0.71	0.62	0.76	1.21	2.35	3.47	0.74
time (sec)	N/A	0.009	0.013	0.003	1.286	0.453	1.493	1.018	0.027

Problem 388	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	28	12	58	12
normalized size	1	1.00	1.00	0.81	0.75	1.75	0.75	3.62	0.75
time (sec)	N/A	0.002	0.005	0.002	1.330	0.511	0.066	1.249	0.018

Problem 389	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	105	105	130	95	96	98	209	97	123
normalized size	1	1.00	1.24	0.90	0.91	0.93	1.99	0.92	1.17
time (sec)	N/A	0.041	0.032	0.006	3.026	0.512	2.388	2.025	0.060

Problem 390	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	107	107	33	103	104	111	719	119	131
normalized size	1	1.00	0.31	0.96	0.97	1.04	6.72	1.11	1.22
time (sec)	N/A	0.042	0.007	0.011	3.028	0.515	2.580	2.348	0.073

Problem 391	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	124	124	35	111	136	162	2266	127	174
normalized size	1	1.00	0.28	0.90	1.10	1.31	18.27	1.02	1.40
time (sec)	N/A	0.044	0.008	0.012	3.055	0.498	2.738	1.940	0.122

Problem 392	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	46	43	56	42	1640	49	56
normalized size	1	1.00	0.64	0.60	0.78	0.58	22.78	0.68	0.78
time (sec)	N/A	0.018	0.028	0.005	1.315	0.604	2.777	0.903	0.043

Problem 393	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	35	32	41	31	600	37	37
normalized size	1	1.00	0.66	0.60	0.77	0.58	11.32	0.70	0.70
time (sec)	N/A	0.012	0.020	0.005	1.376	0.511	1.770	0.908	0.038

Problem 394	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	24	21	26	20	162	25	25
normalized size	1	1.00	0.71	0.62	0.76	0.59	4.76	0.74	0.74
time (sec)	N/A	0.008	0.012	0.003	1.297	0.478	1.157	0.900	0.029

Problem 395	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	12	12	12	12
normalized size	1	1.00	1.00	0.81	0.75	0.75	0.75	0.75	0.75
time (sec)	N/A	0.002	0.003	0.002	1.317	0.518	0.064	0.973	0.016

Problem 396	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	66	75	76	213	155	77	99
normalized size	1	1.00	0.84	0.95	0.96	2.70	1.96	0.97	1.25
time (sec)	N/A	0.025	0.013	0.004	2.932	0.553	1.881	2.371	0.086

Problem 397	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	33	95	106	306	831	109	130
normalized size	1	1.00	0.33	0.95	1.06	3.06	8.31	1.09	1.30
time (sec)	N/A	0.033	0.006	0.006	2.995	0.510	2.204	2.445	0.137

Problem 398	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	130	130	35	117	142	296	2730	130	182
normalized size	1	1.00	0.27	0.90	1.09	2.28	21.00	1.00	1.40
time (sec)	N/A	0.048	0.007	0.006	3.028	0.530	2.586	2.236	0.226

Problem 399	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	48	45	64	44	4974	57	64
normalized size	1	1.00	0.60	0.56	0.80	0.55	62.18	0.71	0.80
time (sec)	N/A	0.019	0.027	0.004	1.339	0.496	2.977	1.069	0.048

Problem 400	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	37	34	47	33	1326	43	43
normalized size	1	1.00	0.63	0.58	0.80	0.56	22.47	0.73	0.73
time (sec)	N/A	0.013	0.021	0.005	1.330	0.490	1.897	1.071	0.040

Problem 401	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	26	23	30	22	486	29	29
normalized size	1	1.00	0.68	0.61	0.79	0.58	12.79	0.76	0.76
time (sec)	N/A	0.009	0.012	0.003	1.340	0.605	1.261	0.979	0.029

Problem 402	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	15	14	14	12	14	14
normalized size	1	1.00	1.00	0.83	0.78	0.78	0.67	0.78	0.78
time (sec)	N/A	0.001	0.004	0.002	1.317	0.554	0.066	1.017	0.020

Problem 403	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	35	83	86	285	160	112	117
normalized size	1	1.00	0.43	1.01	1.05	3.48	1.95	1.37	1.43
time (sec)	N/A	0.033	0.011	0.007	3.007	0.540	1.878	2.509	0.095

Problem 404	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	103	103	36	103	116	328	838	144	133
normalized size	1	1.00	0.35	1.00	1.13	3.18	8.14	1.40	1.29
time (sec)	N/A	0.034	0.006	0.007	2.989	0.646	2.236	2.429	0.175

Problem 405	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	38	128	159	374	2744	167	216
normalized size	1	1.00	0.28	0.94	1.17	2.75	20.18	1.23	1.59
time (sec)	N/A	0.044	0.006	0.008	3.093	0.565	2.615	2.242	0.220

Problem 406	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	46	43	56	42	1640	49	56
normalized size	1	1.00	0.66	0.61	0.80	0.60	23.43	0.70	0.80
time (sec)	N/A	0.018	0.024	0.006	1.345	0.476	2.787	1.026	0.045

Problem 407	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	35	32	41	31	600	37	37
normalized size	1	1.00	0.69	0.63	0.80	0.61	11.76	0.73	0.73
time (sec)	N/A	0.012	0.017	0.004	1.314	0.406	1.817	0.897	0.041

Problem 408	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	23	21	26	19	162	23	25
normalized size	1	1.00	0.72	0.66	0.81	0.59	5.06	0.72	0.78
time (sec)	N/A	0.007	0.011	0.003	1.335	0.456	1.190	0.891	0.029

Problem 409	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	12	10	12	12
normalized size	1	1.00	1.00	0.93	0.86	0.86	0.71	0.86	0.86
time (sec)	N/A	0.001	0.003	0.003	1.295	0.414	0.063	0.976	0.017

Problem 410	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	93	76	77	115	150	78	95
normalized size	1	1.00	1.16	0.95	0.96	1.44	1.88	0.98	1.19
time (sec)	N/A	0.024	0.026	0.005	2.874	0.477	1.930	2.317	0.166

Problem 411	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	31	95	106	166	830	108	122
normalized size	1	1.00	0.32	0.97	1.08	1.69	8.47	1.10	1.24
time (sec)	N/A	0.033	0.005	0.007	2.951	0.450	2.266	2.373	0.130

Problem 412	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	130	130	33	117	142	162	2728	130	175
normalized size	1	1.00	0.25	0.90	1.09	1.25	20.98	1.00	1.35
time (sec)	N/A	0.048	0.006	0.009	3.043	0.430	2.727	2.049	0.131

Problem 413	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	46	43	56	52	1538	62	56
normalized size	1	1.00	0.66	0.61	0.80	0.74	21.97	0.89	0.80
time (sec)	N/A	0.018	0.022	0.004	1.358	0.416	2.891	1.103	0.053

Problem 414	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	34	32	41	40	534	46	35
normalized size	1	1.00	0.69	0.65	0.84	0.82	10.90	0.94	0.71
time (sec)	N/A	0.013	0.016	0.006	1.327	0.417	1.882	0.996	0.042

Problem 415	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	23	20	26	29	41	30	20
normalized size	1	1.00	0.72	0.62	0.81	0.91	1.28	0.94	0.62
time (sec)	N/A	0.009	0.011	0.003	1.303	0.527	0.724	0.934	0.030

Problem 416	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	20	12	12	12
normalized size	1	1.00	1.00	0.93	0.86	1.43	0.86	0.86	0.86
time (sec)	N/A	0.001	0.004	0.002	1.353	0.428	0.067	0.764	0.021

Problem 417	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	30	87	88	285	184	89	114
normalized size	1	1.00	0.32	0.94	0.95	3.06	1.98	0.96	1.23
time (sec)	N/A	0.033	0.005	0.009	3.032	0.449	2.215	2.377	0.056

Problem 418	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	113	115	31	108	122	407	857	120	173
normalized size	1	1.02	0.27	0.96	1.08	3.60	7.58	1.06	1.53
time (sec)	N/A	0.044	0.006	0.013	2.993	0.592	2.525	2.399	0.068

Problem 419	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	149	147	33	131	158	407	2793	140	221
normalized size	1	0.99	0.22	0.88	1.06	2.73	18.74	0.94	1.48
time (sec)	N/A	0.058	0.006	0.014	2.960	0.619	3.185	2.590	0.131

Problem 420	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	66	87	86	88	138	87	105
normalized size	1	1.00	0.93	1.23	1.21	1.24	1.94	1.23	1.48
time (sec)	N/A	0.031	0.021	0.011	3.089	0.499	2.134	1.032	0.101

Problem 421	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	73	73	68	91	90	92	136	91	108
normalized size	1	1.00	0.93	1.25	1.23	1.26	1.86	1.25	1.48
time (sec)	N/A	0.031	0.022	0.004	2.995	0.589	1.889	0.767	0.128

Problem 422	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	41	97	94	93	134	95	112
normalized size	1	1.00	0.55	1.31	1.27	1.26	1.81	1.28	1.51
time (sec)	N/A	0.032	0.013	0.009	2.903	0.710	1.824	1.068	0.108

Problem 423	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	76	76	41	101	98	97	139	99	115
normalized size	1	1.00	0.54	1.33	1.29	1.28	1.83	1.30	1.51
time (sec)	N/A	0.028	0.012	0.004	2.922	0.444	1.827	1.003	0.072

Problem 424	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	95	88	87	86	134	88	101
normalized size	1	1.00	1.32	1.22	1.21	1.19	1.86	1.22	1.40
time (sec)	N/A	0.024	0.025	0.009	2.877	0.445	1.857	1.003	0.141

Problem 425	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	99	92	91	90	136	92	104
normalized size	1	1.00	1.34	1.24	1.23	1.22	1.84	1.24	1.41
time (sec)	N/A	0.025	0.025	0.003	2.978	0.451	1.921	1.086	0.107

Problem 426	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	108	96	93	95	134	94	107
normalized size	1	1.00	1.46	1.30	1.26	1.28	1.81	1.27	1.45
time (sec)	N/A	0.023	0.032	0.008	2.951	0.430	1.983	0.988	0.156

Problem 427	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	76	76	112	100	97	99	133	98	110
normalized size	1	1.00	1.47	1.32	1.28	1.30	1.75	1.29	1.45
time (sec)	N/A	0.023	0.031	0.003	2.889	0.438	1.895	1.074	0.160

Problem 428	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	25	25	22	31	25	33	87	43	30
normalized size	1	1.00	0.88	1.24	1.00	1.32	3.48	1.72	1.20
time (sec)	N/A	0.008	0.015	0.003	1.339	0.436	0.299	1.006	0.313

Problem 429	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	17	14	13	18	19	13	13
normalized size	1	1.00	0.81	0.67	0.62	0.86	0.90	0.62	0.62
time (sec)	N/A	0.004	0.005	0.003	1.334	0.465	1.589	0.828	0.091

Problem 430	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	17	14	13	18	19	13	13
normalized size	1	1.00	0.81	0.67	0.62	0.86	0.90	0.62	0.62
time (sec)	N/A	0.004	0.005	0.003	1.293	0.418	0.547	0.880	0.027

Problem 431	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	17	14	13	16	19	13	13
normalized size	1	1.00	0.81	0.67	0.62	0.76	0.90	0.62	0.62
time (sec)	N/A	0.004	0.005	0.003	1.338	0.440	1.621	0.859	0.025

Problem 432	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	16	13	13	12	17	13	12
normalized size	1	1.00	0.84	0.68	0.68	0.63	0.89	0.68	0.63
time (sec)	N/A	0.004	0.005	0.004	1.316	0.430	0.156	1.081	0.025

Problem 433	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	14	12	13	12	15	13	11
normalized size	1	1.00	0.82	0.71	0.76	0.71	0.88	0.76	0.65
time (sec)	N/A	0.004	0.005	0.003	1.328	0.448	0.350	0.920	0.028

Problem 434	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	15	12	11	11	19	11	13
normalized size	1	1.00	0.79	0.63	0.58	0.58	1.00	0.58	0.68
time (sec)	N/A	0.004	0.005	0.002	1.362	0.417	0.562	0.966	0.027

Problem 435	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	38	87	43	85	299	117	93
normalized size	1	1.00	0.88	2.02	1.00	1.98	6.95	2.72	2.16
time (sec)	N/A	0.014	0.033	0.005	1.357	0.441	0.535	1.102	0.416

Problem 436	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	28	25	24	29	34	24	24
normalized size	1	1.00	0.78	0.69	0.67	0.81	0.94	0.67	0.67
time (sec)	N/A	0.007	0.008	0.003	1.272	0.413	2.597	1.156	0.103

Problem 437	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	28	25	24	29	34	24	24
normalized size	1	1.00	0.78	0.69	0.67	0.81	0.94	0.67	0.67
time (sec)	N/A	0.007	0.007	0.004	1.318	0.423	1.031	1.118	0.035

Problem 438	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	28	25	24	27	0	24	24
normalized size	1	1.00	0.78	0.69	0.67	0.75	0.00	0.67	0.67
time (sec)	N/A	0.007	0.007	0.004	1.294	0.425	0.000	0.899	0.042

Problem 439	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	28	25	24	24	32	24	24
normalized size	1	1.00	0.82	0.74	0.71	0.71	0.94	0.71	0.71
time (sec)	N/A	0.007	0.007	0.004	1.381	0.414	0.262	0.917	0.037

Problem 440	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	27	25	24	23	31	24	24
normalized size	1	1.00	0.84	0.78	0.75	0.72	0.97	0.75	0.75
time (sec)	N/A	0.007	0.008	0.004	1.318	0.429	0.430	1.016	0.035

Problem 441	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	26	23	23	24	31	23	24
normalized size	1	1.00	0.81	0.72	0.72	0.75	0.97	0.72	0.75
time (sec)	N/A	0.007	0.009	0.004	1.289	0.436	0.593	1.002	0.030

Problem 442	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	54	170	61	157	663	224	167
normalized size	1	1.00	0.89	2.79	1.00	2.57	10.87	3.67	2.74
time (sec)	N/A	0.020	0.032	0.004	1.358	0.444	0.884	1.027	0.389

Problem 443	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	39	36	35	40	49	35	35
normalized size	1	1.00	0.76	0.71	0.69	0.78	0.96	0.69	0.69
time (sec)	N/A	0.011	0.010	0.004	1.343	0.450	3.881	0.990	0.045

Problem 444	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	39	36	35	40	49	35	35
normalized size	1	1.00	0.76	0.71	0.69	0.78	0.96	0.69	0.69
time (sec)	N/A	0.012	0.010	0.004	1.339	0.441	1.703	0.991	0.046

Problem 445	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	39	36	35	38	0	35	35
normalized size	1	1.00	0.76	0.71	0.69	0.75	0.00	0.69	0.69
time (sec)	N/A	0.011	0.010	0.005	1.256	0.428	0.000	1.082	0.042

Problem 446	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	39	36	35	35	46	35	35
normalized size	1	1.00	0.83	0.77	0.74	0.74	0.98	0.74	0.74
time (sec)	N/A	0.011	0.010	0.004	1.352	0.415	0.445	0.939	0.043

Problem 447	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	38	36	35	34	44	35	35
normalized size	1	1.00	0.84	0.80	0.78	0.76	0.98	0.78	0.78
time (sec)	N/A	0.011	0.011	0.005	1.356	0.413	0.639	1.032	0.047

Problem 448	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	38	34	34	34	46	34	35
normalized size	1	1.00	0.81	0.72	0.72	0.72	0.98	0.72	0.74
time (sec)	N/A	0.011	0.012	0.005	1.368	0.436	0.777	1.065	0.039

Problem 449	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	61	54	54	132	121	59	48
normalized size	1	1.00	0.90	0.79	0.79	1.94	1.78	0.87	0.71
time (sec)	N/A	0.032	0.026	0.009	3.010	0.442	7.295	0.875	0.057

Problem 450	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	49	43	42	103	105	45	37
normalized size	1	1.00	0.92	0.81	0.79	1.94	1.98	0.85	0.70
time (sec)	N/A	0.017	0.019	0.007	2.941	0.460	1.926	1.238	0.052

Problem 451	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	40	32	31	85	92	31	28
normalized size	1	1.00	1.00	0.80	0.78	2.12	2.30	0.78	0.70
time (sec)	N/A	0.012	0.010	0.006	2.971	0.491	0.724	0.989	0.041

Problem 452	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	29	19	18	68	94	18	19
normalized size	1	1.00	1.00	0.66	0.62	2.34	3.24	0.62	0.66
time (sec)	N/A	0.008	0.005	0.006	2.926	0.474	1.291	0.947	0.044

Problem 453	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	25	32	31	93	102	31	28
normalized size	1	1.00	0.62	0.80	0.78	2.32	2.55	0.78	0.70
time (sec)	N/A	0.013	0.005	0.008	2.883	0.471	2.773	0.997	0.044

Problem 454	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	27	43	41	118	121	41	38
normalized size	1	1.00	0.51	0.81	0.77	2.23	2.28	0.77	0.72
time (sec)	N/A	0.018	0.005	0.011	3.017	0.464	7.834	1.157	0.102

Problem 455	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	27	54	52	144	139	52	49
normalized size	1	1.00	0.40	0.79	0.76	2.12	2.04	0.76	0.72
time (sec)	N/A	0.023	0.006	0.010	2.915	0.455	24.823	0.994	0.110

Problem 456	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	27	61	63	161	479	65	58
normalized size	1	1.00	0.39	0.87	0.90	2.30	6.84	0.93	0.83
time (sec)	N/A	0.022	0.005	0.011	2.964	0.469	24.566	0.928	0.114

Problem 457	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	27	47	49	134	411	46	46
normalized size	1	1.00	0.47	0.82	0.86	2.35	7.21	0.81	0.81
time (sec)	N/A	0.017	0.004	0.011	2.907	0.440	9.176	0.956	0.124

Problem 458	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	46	37	37	115	337	36	34
normalized size	1	1.00	1.00	0.80	0.80	2.50	7.33	0.78	0.74
time (sec)	N/A	0.013	0.020	0.010	2.936	0.461	4.445	0.901	0.040

Problem 459	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	45	36	35	116	328	35	33
normalized size	1	1.00	1.00	0.80	0.78	2.58	7.29	0.78	0.73
time (sec)	N/A	0.013	0.017	0.009	2.925	0.451	7.527	0.894	0.095

Problem 460	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	25	48	51	147	434	49	48
normalized size	1	1.00	0.45	0.86	0.91	2.62	7.75	0.88	0.86
time (sec)	N/A	0.017	0.005	0.013	2.943	0.443	17.734	1.006	0.124

Problem 461	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	27	60	64	184	507	58	58
normalized size	1	1.00	0.39	0.87	0.93	2.67	7.35	0.84	0.84
time (sec)	N/A	0.022	0.005	0.015	2.882	0.457	50.524	0.957	0.150

Problem 462	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	27	79	86	227	906	77	81
normalized size	1	1.00	0.28	0.83	0.91	2.39	9.54	0.81	0.85
time (sec)	N/A	0.033	0.005	0.015	3.067	0.476	135.242	1.027	0.122

Problem 463	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	27	66	73	200	816	59	69
normalized size	1	1.00	0.33	0.80	0.89	2.44	9.95	0.72	0.84
time (sec)	N/A	0.023	0.005	0.015	2.941	0.458	53.287	0.953	0.143

Problem 464	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	59	50	61	185	726	47	58
normalized size	1	1.00	0.84	0.71	0.87	2.64	10.37	0.67	0.83
time (sec)	N/A	0.019	0.035	0.013	2.960	0.450	29.374	0.908	0.131

Problem 465	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	73	73	27	52	64	186	721	52	56
normalized size	1	1.00	0.37	0.71	0.88	2.55	9.88	0.71	0.77
time (sec)	N/A	0.019	0.005	0.009	3.012	0.442	15.275	1.066	0.125

Problem 466	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	25	53	60	186	712	47	57
normalized size	1	1.00	0.36	0.76	0.86	2.66	10.17	0.67	0.81
time (sec)	N/A	0.019	0.005	0.009	2.956	0.459	25.687	0.862	0.126

Problem 467	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	25	66	73	214	865	59	70
normalized size	1	1.00	0.30	0.80	0.89	2.61	10.55	0.72	0.85
time (sec)	N/A	0.025	0.005	0.015	2.992	0.484	54.354	1.142	0.149

Problem 468	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	27	79	86	250	962	71	80
normalized size	1	1.00	0.28	0.83	0.91	2.63	10.13	0.75	0.84
time (sec)	N/A	0.029	0.005	0.016	2.981	0.455	138.083	1.101	0.155

Problem 469	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	61	54	70	131	116	61	51
normalized size	1	1.00	0.90	0.79	1.03	1.93	1.71	0.90	0.75
time (sec)	N/A	0.024	0.026	0.006	2.942	0.433	7.100	1.034	0.147

Problem 470	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	49	43	58	103	100	47	37
normalized size	1	1.00	0.92	0.81	1.09	1.94	1.89	0.89	0.70
time (sec)	N/A	0.018	0.019	0.008	2.920	0.460	1.870	0.940	0.114

Problem 471	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	40	32	47	83	87	33	28
normalized size	1	1.00	1.00	0.80	1.18	2.08	2.18	0.82	0.70
time (sec)	N/A	0.014	0.010	0.004	3.075	0.464	0.708	1.045	0.112

Problem 472	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	29	19	34	67	88	20	19
normalized size	1	1.00	1.00	0.66	1.17	2.31	3.03	0.69	0.66
time (sec)	N/A	0.011	0.006	0.005	3.026	0.454	1.253	1.005	0.125

Problem 473	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	24	32	47	91	94	33	28
normalized size	1	1.00	0.60	0.80	1.18	2.28	2.35	0.82	0.70
time (sec)	N/A	0.014	0.004	0.007	2.867	0.439	2.757	1.019	0.056

Problem 474	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	26	43	55	113	112	41	37
normalized size	1	1.00	0.49	0.81	1.04	2.13	2.11	0.77	0.70
time (sec)	N/A	0.018	0.005	0.010	2.960	0.447	7.665	0.981	0.122

Problem 475	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	26	54	68	143	131	54	48
normalized size	1	1.00	0.38	0.79	1.00	2.10	1.93	0.79	0.71
time (sec)	N/A	0.022	0.005	0.010	2.975	0.456	24.442	0.968	0.129

Problem 476	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	26	61	81	167	444	69	61
normalized size	1	1.00	0.37	0.87	1.16	2.39	6.34	0.99	0.87
time (sec)	N/A	0.025	0.005	0.012	3.057	0.483	24.751	0.984	0.071

Problem 477	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	26	49	68	138	381	51	47
normalized size	1	1.00	0.46	0.86	1.19	2.42	6.68	0.89	0.82
time (sec)	N/A	0.018	0.005	0.011	2.919	0.456	9.127	0.978	0.115

Problem 478	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	61	40	56	123	311	40	35
normalized size	1	1.00	1.30	0.85	1.19	2.62	6.62	0.85	0.74
time (sec)	N/A	0.015	0.016	0.009	2.988	0.447	4.428	1.064	0.112

Problem 479	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	46	39	56	122	303	41	34
normalized size	1	1.00	1.00	0.85	1.22	2.65	6.59	0.89	0.74
time (sec)	N/A	0.014	0.020	0.008	2.970	0.483	7.413	0.883	0.055

Problem 480	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	24	49	69	151	403	52	49
normalized size	1	1.00	0.42	0.86	1.21	2.65	7.07	0.91	0.86
time (sec)	N/A	0.018	0.006	0.013	3.005	0.456	17.544	1.006	0.073

Problem 481	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	26	60	82	187	471	61	60
normalized size	1	1.00	0.37	0.86	1.17	2.67	6.73	0.87	0.86
time (sec)	N/A	0.022	0.006	0.016	2.998	0.454	50.249	0.930	0.138

Problem 482	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	97	97	26	70	103	227	840	81	83
normalized size	1	1.00	0.27	0.72	1.06	2.34	8.66	0.84	0.86
time (sec)	N/A	0.030	0.006	0.015	2.992	0.455	136.150	1.033	0.141

Problem 483	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	26	58	90	199	756	63	69
normalized size	1	1.00	0.31	0.69	1.07	2.37	9.00	0.75	0.82
time (sec)	N/A	0.026	0.005	0.012	2.996	0.475	53.453	0.951	0.065

Problem 484	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	60	52	78	186	673	51	58
normalized size	1	1.00	0.83	0.72	1.08	2.58	9.35	0.71	0.81
time (sec)	N/A	0.021	0.036	0.013	2.989	0.446	29.248	0.916	0.143

Problem 485	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	75	75	26	54	80	183	668	55	57
normalized size	1	1.00	0.35	0.72	1.07	2.44	8.91	0.73	0.76
time (sec)	N/A	0.020	0.005	0.010	2.848	0.446	15.189	0.933	0.137

Problem 486	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	24	63	77	185	660	51	58
normalized size	1	1.00	0.33	0.88	1.07	2.57	9.17	0.71	0.81
time (sec)	N/A	0.020	0.005	0.009	2.884	0.446	25.674	1.155	0.135

Problem 487	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	24	58	90	213	802	63	69
normalized size	1	1.00	0.29	0.69	1.07	2.54	9.55	0.75	0.82
time (sec)	N/A	0.024	0.005	0.015	2.930	0.452	54.560	1.046	0.155

Problem 488	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	97	97	26	69	103	249	892	73	80
normalized size	1	1.00	0.27	0.71	1.06	2.57	9.20	0.75	0.82
time (sec)	N/A	0.030	0.004	0.017	2.950	0.495	138.884	1.042	0.165

Problem 489	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	122	122	96	120	178	162	153	0	-1
normalized size	1	1.00	0.79	0.98	1.46	1.33	1.25	0.00	-0.01
time (sec)	N/A	0.042	0.185	0.009	2.950	0.452	11.697	0.000	0.000

Problem 490	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	85	102	146	141	122	0	-1
normalized size	1	1.00	0.87	1.04	1.49	1.44	1.24	0.00	-0.01
time (sec)	N/A	0.031	0.107	0.005	3.044	0.439	6.383	0.000	0.000

Problem 491	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	72	81	108	114	97	0	52
normalized size	1	1.00	0.97	1.09	1.46	1.54	1.31	0.00	0.70
time (sec)	N/A	0.023	0.110	0.006	2.962	0.447	3.570	0.000	0.150

Problem 492	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	44	44	62	62	70	93	42	0	41
normalized size	1	1.00	1.41	1.41	1.59	2.11	0.95	0.00	0.93
time (sec)	N/A	0.017	0.086	0.004	2.992	0.455	1.916	0.000	0.683

Problem 493	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	64	61	54	89	68	0	-1
normalized size	1	1.00	1.42	1.36	1.20	1.98	1.51	0.00	-0.02
time (sec)	N/A	0.017	0.095	0.037	3.004	0.436	1.561	0.000	0.000

Problem 494	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	16	15	15	41	33	21
normalized size	1	1.00	1.00	0.76	0.71	0.71	1.95	1.57	1.00
time (sec)	N/A	0.002	0.007	0.004	1.357	0.414	1.461	1.327	0.237

Problem 495	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	44	44	29	24	31	34	65	50	32
normalized size	1	1.00	0.66	0.55	0.70	0.77	1.48	1.14	0.73
time (sec)	N/A	0.005	0.009	0.004	1.287	0.429	4.875	1.102	0.255

Problem 496	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	40	35	46	45	347	66	43
normalized size	1	1.00	0.59	0.51	0.68	0.66	5.10	0.97	0.63
time (sec)	N/A	0.010	0.011	0.005	1.354	0.417	13.772	0.974	0.264

Problem 497	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	127	127	98	127	170	164	323	0	-1
normalized size	1	1.00	0.77	1.00	1.34	1.29	2.54	0.00	-0.01
time (sec)	N/A	0.042	0.141	0.010	3.010	0.449	11.648	0.000	0.000

Problem 498	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	87	108	135	142	260	0	-1
normalized size	1	1.00	0.85	1.06	1.32	1.39	2.55	0.00	-0.01
time (sec)	N/A	0.030	0.117	0.006	2.990	0.438	6.325	0.000	0.000

Problem 499	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	77	77	75	86	95	118	207	0	58
normalized size	1	1.00	0.97	1.12	1.23	1.53	2.69	0.00	0.75
time (sec)	N/A	0.024	0.097	0.006	2.974	0.463	3.595	0.000	0.083

Problem 500	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	65	66	52	94	119	0	43
normalized size	1	1.00	1.41	1.43	1.13	2.04	2.59	0.00	0.93
time (sec)	N/A	0.017	0.090	0.004	2.899	0.501	1.959	0.000	0.593

Problem 501	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	69	0	35	91	148	0	-1
normalized size	1	1.00	1.47	0.00	0.74	1.94	3.15	0.00	-0.02
time (sec)	N/A	0.016	0.060	0.032	2.928	0.435	1.701	0.000	0.000

Problem 502	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	22	17	16	23	88	42	21
normalized size	1	1.00	1.00	0.77	0.73	1.05	4.00	1.91	0.95
time (sec)	N/A	0.002	0.007	0.004	1.315	0.439	1.549	1.396	0.243

Problem 503	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	30	25	33	34	241	61	32
normalized size	1	1.00	0.65	0.54	0.72	0.74	5.24	1.33	0.70
time (sec)	N/A	0.005	0.009	0.005	1.336	0.453	5.006	1.384	0.253

Problem 504	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	41	36	49	46	707	79	43
normalized size	1	1.00	0.58	0.51	0.69	0.65	9.96	1.11	0.61
time (sec)	N/A	0.010	0.011	0.005	1.351	0.458	26.813	1.336	0.269

Problem 505	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	108	108	70	108	163	140	117	0	-1
normalized size	1	1.00	0.65	1.00	1.51	1.30	1.08	0.00	-0.01
time (sec)	N/A	0.032	0.047	0.008	3.030	0.463	10.124	0.000	0.000

Problem 506	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	58	93	134	121	90	0	-1
normalized size	1	1.00	0.69	1.11	1.60	1.44	1.07	0.00	-0.01
time (sec)	N/A	0.020	0.034	0.005	3.016	0.459	5.223	0.000	0.000

Problem 507	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	51	75	98	101	71	0	46
normalized size	1	1.00	0.80	1.17	1.53	1.58	1.11	0.00	0.72
time (sec)	N/A	0.015	0.027	0.004	2.906	0.450	2.912	0.000	0.098

Problem 508	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	40	58	68	86	37	0	40
normalized size	1	1.00	1.00	1.45	1.70	2.15	0.92	0.00	1.00
time (sec)	N/A	0.008	0.013	0.004	2.959	0.494	1.648	0.000	0.617

Problem 509	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	41	59	54	87	48	0	-1
normalized size	1	1.00	1.00	1.44	1.32	2.12	1.17	0.00	-0.02
time (sec)	N/A	0.009	0.012	0.024	2.951	0.483	1.429	0.000	0.000

Problem 510	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	13	12	12	37	29	18
normalized size	1	1.00	1.00	0.72	0.67	0.67	2.06	1.61	1.00
time (sec)	N/A	0.001	0.005	0.003	1.314	0.419	1.451	1.152	0.208

Problem 511	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	23	18	26	25	56	42	26
normalized size	1	1.00	0.61	0.47	0.68	0.66	1.47	1.11	0.68
time (sec)	N/A	0.004	0.007	0.004	1.317	0.423	4.717	1.092	0.215

Problem 512	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	32	27	41	34	270	55	34
normalized size	1	1.00	0.54	0.46	0.69	0.58	4.58	0.93	0.58
time (sec)	N/A	0.008	0.010	0.003	1.274	0.425	13.796	1.111	0.224

Problem 513	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	112	112	71	116	147	141	252	0	-1
normalized size	1	1.00	0.63	1.04	1.31	1.26	2.25	0.00	-0.01
time (sec)	N/A	0.029	0.044	0.009	2.932	0.439	9.916	0.000	0.000

Problem 514	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	87	87	60	100	117	125	196	0	-1
normalized size	1	1.00	0.69	1.15	1.34	1.44	2.25	0.00	-0.01
time (sec)	N/A	0.023	0.035	0.005	2.976	0.445	5.294	0.000	0.000

Problem 515	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	51	81	81	107	156	0	53
normalized size	1	1.00	0.78	1.25	1.25	1.65	2.40	0.00	0.82
time (sec)	N/A	0.015	0.029	0.005	2.953	0.463	2.942	0.000	0.104

Problem 516	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	41	63	49	89	121	0	42
normalized size	1	1.00	1.00	1.54	1.20	2.17	2.95	0.00	1.02
time (sec)	N/A	0.008	0.014	0.003	2.912	0.459	1.711	0.000	0.562

Problem 517	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	C	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	42	90	35	90	136	0	-1
normalized size	1	1.00	1.00	2.14	0.83	2.14	3.24	0.00	-0.02
time (sec)	N/A	0.009	0.014	0.036	3.013	0.476	1.580	0.000	0.000

Problem 518	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	19	14	13	18	82	35	18
normalized size	1	1.00	1.00	0.74	0.68	0.95	4.32	1.84	0.95
time (sec)	N/A	0.001	0.005	0.003	1.285	0.435	1.506	1.116	0.224

Problem 519	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	24	19	28	25	194	48	26
normalized size	1	1.00	0.60	0.48	0.70	0.62	4.85	1.20	0.65
time (sec)	N/A	0.004	0.008	0.004	1.334	0.410	4.909	0.853	0.219

Problem 520	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	62	62	33	28	44	35	554	61	34
normalized size	1	1.00	0.53	0.45	0.71	0.56	8.94	0.98	0.55
time (sec)	N/A	0.008	0.010	0.003	1.312	0.422	24.598	0.975	0.224

Problem 521	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	143	143	107	138	212	184	178	0	-1
normalized size	1	1.00	0.75	0.97	1.48	1.29	1.24	0.00	-0.01
time (sec)	N/A	0.051	0.208	0.007	2.964	0.442	17.714	0.000	0.000

Problem 522	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	96	120	178	163	153	0	-1
normalized size	1	1.00	0.81	1.01	1.50	1.37	1.29	0.00	-0.01
time (sec)	N/A	0.038	0.125	0.006	2.961	0.452	9.279	0.000	0.000

Problem 523	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	85	96	144	140	124	0	-1
normalized size	1	1.00	0.89	1.01	1.52	1.47	1.31	0.00	-0.01
time (sec)	N/A	0.029	0.115	0.006	3.022	0.448	5.590	0.000	0.000

Problem 524	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	69	78	107	119	75	0	-1
normalized size	1	1.00	0.97	1.10	1.51	1.68	1.06	0.00	-0.01
time (sec)	N/A	0.022	0.098	0.006	2.985	0.474	3.173	0.000	0.000

Problem 525	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	46	71	84	109	92	0	-1
normalized size	1	1.00	0.73	1.13	1.33	1.73	1.46	0.00	-0.02
time (sec)	N/A	0.021	0.011	0.018	2.987	0.532	2.722	0.000	0.000

Problem 526	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	48	67	67	109	71	0	-1
normalized size	1	1.00	0.75	1.05	1.05	1.70	1.11	0.00	-0.02
time (sec)	N/A	0.021	0.010	0.019	2.926	0.470	3.036	0.000	0.000

Problem 527	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	149	149	110	146	207	185	376	0	-1
normalized size	1	1.00	0.74	0.98	1.39	1.24	2.52	0.00	-0.01
time (sec)	N/A	0.053	0.171	0.007	3.115	0.481	17.693	0.000	0.000

Problem 528	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	124	124	99	127	170	163	323	0	-1
normalized size	1	1.00	0.80	1.02	1.37	1.31	2.60	0.00	-0.01
time (sec)	N/A	0.041	0.145	0.006	2.968	0.444	9.060	0.000	0.000

Problem 529	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	99	99	87	102	133	141	264	0	-1
normalized size	1	1.00	0.88	1.03	1.34	1.42	2.67	0.00	-0.01
time (sec)	N/A	0.031	0.121	0.007	2.990	0.462	5.537	0.000	0.000

Problem 530	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	71	83	93	119	190	0	-1
normalized size	1	1.00	0.96	1.12	1.26	1.61	2.57	0.00	-0.01
time (sec)	N/A	0.021	0.116	0.005	2.896	0.445	3.212	0.000	0.000

Problem 531	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	47	0	68	109	197	0	-1
normalized size	1	1.00	0.71	0.00	1.03	1.65	2.98	0.00	-0.02
time (sec)	N/A	0.020	0.011	0.025	2.846	0.448	2.881	0.000	0.000

Problem 532	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	A	A	C	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	49	0	49	115	187	0	-1
normalized size	1	1.00	0.73	0.00	0.73	1.72	2.79	0.00	-0.01
time (sec)	N/A	0.022	0.011	0.029	2.859	0.455	3.241	0.000	0.000

Problem 533	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	78	123	194	156	136	0	-1
normalized size	1	1.00	0.62	0.98	1.54	1.24	1.08	0.00	-0.01
time (sec)	N/A	0.034	0.050	0.006	2.986	0.438	15.671	0.000	0.000

Problem 534	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	105	105	70	108	163	137	117	0	-1
normalized size	1	1.00	0.67	1.03	1.55	1.30	1.11	0.00	-0.01
time (sec)	N/A	0.026	0.032	0.004	3.043	0.450	7.858	0.000	0.000

Problem 535	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	60	87	132	124	92	0	-1
normalized size	1	1.00	0.73	1.06	1.61	1.51	1.12	0.00	-0.01
time (sec)	N/A	0.016	0.033	0.004	2.993	0.448	4.809	0.000	0.000

Problem 536	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	48	72	98	105	76	0	-1
normalized size	1	1.00	0.79	1.18	1.61	1.72	1.25	0.00	-0.02
time (sec)	N/A	0.011	0.026	0.005	2.895	0.516	2.816	0.000	0.000

Problem 537	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	28	72	81	99	73	0	-1
normalized size	1	1.00	0.48	1.24	1.40	1.71	1.26	0.00	-0.02
time (sec)	N/A	0.012	0.005	0.018	2.914	0.482	2.442	0.000	0.000

Problem 538	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	30	73	67	108	70	0	-1
normalized size	1	1.00	0.50	1.22	1.12	1.80	1.17	0.00	-0.02
time (sec)	N/A	0.014	0.006	0.017	2.972	0.454	2.812	0.000	0.000

Problem 539	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	131	131	79	132	179	157	291	0	-1
normalized size	1	1.00	0.60	1.01	1.37	1.20	2.22	0.00	-0.01
time (sec)	N/A	0.040	0.052	0.006	2.943	0.472	15.279	0.000	0.000

Problem 540	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	109	109	70	116	147	139	252	0	-1
normalized size	1	1.00	0.64	1.06	1.35	1.28	2.31	0.00	-0.01
time (sec)	N/A	0.028	0.045	0.006	2.925	0.472	7.726	0.000	0.000

Problem 541	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	60	94	115	125	199	0	-1
normalized size	1	1.00	0.71	1.12	1.37	1.49	2.37	0.00	-0.01
time (sec)	N/A	0.016	0.042	0.004	3.042	0.464	4.780	0.000	0.000

Problem 542	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	49	78	79	107	167	0	-1
normalized size	1	1.00	0.78	1.24	1.25	1.70	2.65	0.00	-0.02
time (sec)	N/A	0.012	0.029	0.004	2.984	0.464	2.863	0.000	0.000

Problem 543	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	28	97	63	101	160	0	-1
normalized size	1	1.00	0.47	1.62	1.05	1.68	2.67	0.00	-0.02
time (sec)	N/A	0.012	0.005	0.020	2.989	0.460	2.493	0.000	0.000

Problem 544	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	C	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	62	62	30	98	49	111	182	0	-1
normalized size	1	1.00	0.48	1.58	0.79	1.79	2.94	0.00	-0.02
time (sec)	N/A	0.013	0.006	0.022	3.004	0.483	2.923	0.000	0.000

Problem 545	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	164	164	118	156	244	206	207	0	-1
normalized size	1	1.00	0.72	0.95	1.49	1.26	1.26	0.00	-0.01
time (sec)	N/A	0.063	0.244	0.005	2.989	0.488	25.936	0.000	0.000

Problem 546	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	140	140	107	138	212	185	180	0	-1
normalized size	1	1.00	0.76	0.99	1.51	1.32	1.29	0.00	-0.01
time (sec)	N/A	0.048	0.138	0.006	2.979	0.438	16.411	0.000	0.000

Problem 547	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	116	116	96	111	176	162	155	0	-1
normalized size	1	1.00	0.83	0.96	1.52	1.40	1.34	0.00	-0.01
time (sec)	N/A	0.038	0.199	0.006	2.981	0.471	9.860	0.000	0.000

Problem 548	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	80	93	141	141	102	0	-1
normalized size	1	1.00	0.87	1.01	1.53	1.53	1.11	0.00	-0.01
time (sec)	N/A	0.028	0.111	0.006	2.991	0.451	6.229	0.000	0.000

Problem 549	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	48	84	125	137	126	0	-1
normalized size	1	1.00	0.54	0.94	1.40	1.54	1.42	0.00	-0.01
time (sec)	N/A	0.028	0.012	0.018	2.977	0.455	6.148	0.000	0.000

Problem 550	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	50	82	100	138	99	0	-1
normalized size	1	1.00	0.58	0.95	1.16	1.60	1.15	0.00	-0.01
time (sec)	N/A	0.026	0.011	0.020	2.949	0.442	5.622	0.000	0.000

Problem 551	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	171	171	120	165	242	208	435	0	-1
normalized size	1	1.00	0.70	0.96	1.42	1.22	2.54	0.00	-0.01
time (sec)	N/A	0.061	0.191	0.007	2.864	0.444	25.960	0.000	0.000

Problem 552	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	146	146	109	146	207	186	379	0	-1
normalized size	1	1.00	0.75	1.00	1.42	1.27	2.60	0.00	-0.01
time (sec)	N/A	0.051	0.149	0.006	3.008	0.459	16.398	0.000	0.000

Problem 553	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	121	121	98	118	168	164	326	0	-1
normalized size	1	1.00	0.81	0.98	1.39	1.36	2.69	0.00	-0.01
time (sec)	N/A	0.038	0.132	0.007	3.046	0.455	9.807	0.000	0.000

Problem 554	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	82	99	130	142	246	0	-1
normalized size	1	1.00	0.85	1.03	1.35	1.48	2.56	0.00	-0.01
time (sec)	N/A	0.030	0.123	0.005	2.930	0.450	6.228	0.000	0.000

Problem 555	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	49	0	112	137	267	0	-1
normalized size	1	1.00	0.53	0.00	1.20	1.47	2.87	0.00	-0.01
time (sec)	N/A	0.028	0.012	0.030	2.992	0.476	6.222	0.000	0.000

Problem 556	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	A	A	C	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	90	90	51	0	84	139	245	0	-1
normalized size	1	1.00	0.57	0.00	0.93	1.54	2.72	0.00	-0.01
time (sec)	N/A	0.030	0.012	0.028	3.000	0.451	5.845	0.000	0.000

Problem 557	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	144	144	86	138	223	172	158	0	-1
normalized size	1	1.00	0.60	0.96	1.55	1.19	1.10	0.00	-0.01
time (sec)	N/A	0.045	0.059	0.005	2.977	0.450	22.960	0.000	0.000

Problem 558	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	123	123	78	123	194	155	138	0	-1
normalized size	1	1.00	0.63	1.00	1.58	1.26	1.12	0.00	-0.01
time (sec)	N/A	0.028	0.048	0.004	2.943	0.450	14.423	0.000	0.000

Problem 559	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	70	99	161	140	119	0	-1
normalized size	1	1.00	0.69	0.97	1.58	1.37	1.17	0.00	-0.01
time (sec)	N/A	0.022	0.041	0.006	2.986	0.445	8.611	0.000	0.000

Problem 560	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	57	84	129	123	97	0	-1
normalized size	1	1.00	0.72	1.06	1.63	1.56	1.23	0.00	-0.01
time (sec)	N/A	0.016	0.032	0.004	3.028	0.454	5.458	0.000	0.000

Problem 561	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	28	81	113	116	94	0	-1
normalized size	1	1.00	0.35	1.03	1.43	1.47	1.19	0.00	-0.01
time (sec)	N/A	0.016	0.007	0.019	2.943	0.467	5.602	0.000	0.000

Problem 562	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	30	82	96	123	88	0	-1
normalized size	1	1.00	0.37	1.01	1.19	1.52	1.09	0.00	-0.01
time (sec)	N/A	0.017	0.006	0.019	2.945	0.448	5.152	0.000	0.000

Problem 563	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	150	150	87	148	209	173	337	0	-1
normalized size	1	1.00	0.58	0.99	1.39	1.15	2.25	0.00	-0.01
time (sec)	N/A	0.045	0.059	0.004	2.960	0.446	22.838	0.000	0.000

Problem 564	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	128	128	79	132	179	157	294	0	-1
normalized size	1	1.00	0.62	1.03	1.40	1.23	2.30	0.00	-0.01
time (sec)	N/A	0.029	0.046	0.006	3.013	0.445	14.298	0.000	0.000

Problem 565	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	106	106	71	107	145	141	255	0	-1
normalized size	1	1.00	0.67	1.01	1.37	1.33	2.41	0.00	-0.01
time (sec)	N/A	0.023	0.041	0.005	2.887	0.466	8.592	0.000	0.000

Problem 566	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	58	91	112	125	209	0	-1
normalized size	1	1.00	0.71	1.11	1.37	1.52	2.55	0.00	-0.01
time (sec)	N/A	0.017	0.034	0.005	2.976	0.454	5.522	0.000	0.000

Problem 567	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	28	106	96	117	202	0	-1
normalized size	1	1.00	0.34	1.29	1.17	1.43	2.46	0.00	-0.01
time (sec)	N/A	0.017	0.006	0.019	2.923	0.480	5.619	0.000	0.000

Problem 568	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	30	107	79	126	221	0	-1
normalized size	1	1.00	0.36	1.27	0.94	1.50	2.63	0.00	-0.01
time (sec)	N/A	0.017	0.007	0.020	2.888	0.436	5.346	0.000	0.000

Problem 569	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	85	102	146	140	128	0	-1
normalized size	1	1.00	0.84	1.01	1.45	1.39	1.27	0.00	-0.01
time (sec)	N/A	0.030	0.161	0.006	3.014	0.448	8.521	0.000	0.000

Problem 570	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	77	77	85	84	112	119	100	0	-1
normalized size	1	1.00	1.10	1.09	1.45	1.55	1.30	0.00	-0.01
time (sec)	N/A	0.022	0.050	0.006	2.867	0.455	4.301	0.000	0.000

Problem 571	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	68	65	73	91	44	0	44
normalized size	1	1.00	1.42	1.35	1.52	1.90	0.92	0.00	0.92
time (sec)	N/A	0.016	0.039	0.004	2.913	0.463	2.187	0.000	0.548

Problem 572	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	A	A	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	50	48	41	57	22	0	30
normalized size	1	1.00	1.79	1.71	1.46	2.04	0.79	0.00	1.07
time (sec)	N/A	0.013	0.013	0.004	2.953	0.462	1.097	0.000	0.030

Problem 573	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	19	16	15	15	19	33	15
normalized size	1	1.00	1.00	0.84	0.79	0.79	1.00	1.74	0.79
time (sec)	N/A	0.002	0.004	0.004	1.342	0.456	0.913	2.050	0.349

Problem 574	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	44	44	27	22	31	23	42	50	25
normalized size	1	1.00	0.61	0.50	0.70	0.52	0.95	1.14	0.57
time (sec)	N/A	0.005	0.007	0.004	1.299	0.456	1.920	1.902	0.342

Problem 575	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	40	35	46	34	287	66	36
normalized size	1	1.00	0.59	0.51	0.68	0.50	4.22	0.97	0.53
time (sec)	N/A	0.010	0.009	0.005	1.337	0.482	6.249	1.669	0.353

Problem 576	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	51	46	61	45	488	82	47
normalized size	1	1.00	0.55	0.50	0.66	0.49	5.30	0.89	0.51
time (sec)	N/A	0.016	0.012	0.004	1.304	0.442	16.137	1.412	0.382

Problem 577	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	50	119	131	175	105	131	-1
normalized size	1	1.00	0.52	1.24	1.36	1.82	1.09	1.36	-0.01
time (sec)	N/A	0.029	0.010	0.035	2.924	0.499	8.139	92.143	0.000

Problem 578	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	50	106	92	145	71	115	-1
normalized size	1	1.00	0.74	1.56	1.35	2.13	1.04	1.69	-0.01
time (sec)	N/A	0.022	0.010	0.030	3.019	0.437	3.678	93.123	0.000

Problem 579	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	64	0	57	119	46	85	-1
normalized size	1	1.00	1.33	0.00	1.19	2.48	0.96	1.77	-0.02
time (sec)	N/A	0.016	0.069	0.035	2.981	0.452	1.780	94.858	0.000

Problem 580	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	19	16	15	22	17	45	22
normalized size	1	1.00	1.00	0.84	0.79	1.16	0.89	2.37	1.16
time (sec)	N/A	0.002	0.005	0.005	1.321	0.426	0.879	1.109	0.326

Problem 581	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	25	22	32	34	41	82	39
normalized size	1	1.00	0.64	0.56	0.82	0.87	1.05	2.10	1.00
time (sec)	N/A	0.005	0.008	0.006	1.320	0.433	1.598	1.052	0.386

Problem 582	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	38	33	50	49	219	98	46
normalized size	1	1.00	0.60	0.52	0.79	0.78	3.48	1.56	0.73
time (sec)	N/A	0.010	0.009	0.005	1.310	0.426	3.983	1.201	0.413

Problem 583	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	87	87	49	44	64	58	348	121	58
normalized size	1	1.00	0.56	0.51	0.74	0.67	4.00	1.39	0.67
time (sec)	N/A	0.017	0.010	0.005	1.309	0.422	11.154	1.213	0.426

Problem 584	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	91	91	50	147	109	214	396	197	-1
normalized size	1	1.00	0.55	1.62	1.20	2.35	4.35	2.16	-0.01
time (sec)	N/A	0.028	0.010	0.049	2.939	0.445	7.610	92.464	0.000

Problem 585	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	80	0	69	186	328	165	-1
normalized size	1	1.00	1.16	0.00	1.00	2.70	4.75	2.39	-0.01
time (sec)	N/A	0.022	0.121	0.032	2.826	0.481	4.027	105.595	0.000

Problem 586	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	16	15	33	42	86	36
normalized size	1	1.00	1.00	0.76	0.71	1.57	2.00	4.10	1.71
time (sec)	N/A	0.002	0.005	0.003	1.328	0.431	1.427	1.631	0.242

Problem 587	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	29	24	27	43	92	81	54
normalized size	1	1.00	0.67	0.56	0.63	1.00	2.14	1.88	1.26
time (sec)	N/A	0.005	0.009	0.005	1.344	0.435	1.896	1.500	0.400

Problem 588	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	40	35	46	58	153	159	71
normalized size	1	1.00	0.62	0.55	0.72	0.91	2.39	2.48	1.11
time (sec)	N/A	0.009	0.011	0.007	1.340	0.430	3.972	1.632	0.420

Problem 589	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	49	44	64	71	337	175	88
normalized size	1	1.00	0.58	0.52	0.76	0.85	4.01	2.08	1.05
time (sec)	N/A	0.015	0.014	0.005	1.268	0.441	7.061	2.238	0.471

Problem 590	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	105	105	88	108	135	141	270	0	-1
normalized size	1	1.00	0.84	1.03	1.29	1.34	2.57	0.00	-0.01
time (sec)	N/A	0.030	0.146	0.007	2.964	0.460	8.432	0.000	0.000

Problem 591	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	86	89	98	119	214	0	-1
normalized size	1	1.00	1.08	1.11	1.22	1.49	2.68	0.00	-0.01
time (sec)	N/A	0.023	0.048	0.006	2.960	0.457	4.296	0.000	0.000

Problem 592	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	71	70	56	93	121	0	47
normalized size	1	1.00	1.42	1.40	1.12	1.86	2.42	0.00	0.94
time (sec)	N/A	0.017	0.042	0.006	3.004	0.447	2.278	0.000	0.517

Problem 593	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	52	51	21	57	54	0	27
normalized size	1	1.00	1.79	1.76	0.72	1.97	1.86	0.00	0.93
time (sec)	N/A	0.013	0.014	0.006	2.883	0.435	1.153	0.000	0.031

Problem 594	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	17	16	16	46	35	16
normalized size	1	1.00	1.00	0.85	0.80	0.80	2.30	1.75	0.80
time (sec)	N/A	0.002	0.004	0.005	1.341	0.430	0.969	1.277	0.401

Problem 595	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	28	23	32	22	177	54	26
normalized size	1	1.00	0.61	0.50	0.70	0.48	3.85	1.17	0.57
time (sec)	N/A	0.005	0.007	0.004	1.302	0.444	2.055	1.453	0.350

Problem 596	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	51	127	118	181	224	154	-1
normalized size	1	1.00	0.51	1.27	1.18	1.81	2.24	1.54	-0.01
time (sec)	N/A	0.030	0.010	0.040	2.922	0.454	8.030	98.066	0.000

Problem 597	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	51	114	75	152	155	130	-1
normalized size	1	1.00	0.72	1.61	1.06	2.14	2.18	1.83	-0.01
time (sec)	N/A	0.022	0.010	0.030	2.952	0.450	3.704	111.127	0.000

Problem 598	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	66	0	38	128	102	98	-1
normalized size	1	1.00	1.32	0.00	0.76	2.56	2.04	1.96	-0.02
time (sec)	N/A	0.016	0.075	0.030	3.012	0.458	1.891	113.038	0.000

Problem 599	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	17	16	25	44	53	24
normalized size	1	1.00	1.00	0.85	0.80	1.25	2.20	2.65	1.20
time (sec)	N/A	0.002	0.005	0.003	1.297	0.434	0.943	1.374	0.339

Problem 600	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	26	23	34	38	112	94	42
normalized size	1	1.00	0.63	0.56	0.83	0.93	2.73	2.29	1.02
time (sec)	N/A	0.005	0.008	0.003	1.305	0.443	1.678	1.441	0.400

Problem 601	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	39	34	52	51	452	112	48
normalized size	1	1.00	0.59	0.52	0.79	0.77	6.85	1.70	0.73
time (sec)	N/A	0.010	0.009	0.005	1.347	0.451	4.640	1.478	0.432

Problem 602	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	51	160	94	215	971	221	-1
normalized size	1	1.00	0.54	1.68	0.99	2.26	10.22	2.33	-0.01
time (sec)	N/A	0.029	0.012	0.043	3.018	0.459	8.483	112.518	0.000

Problem 603	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	82	0	52	188	833	194	-1
normalized size	1	1.00	1.14	0.00	0.72	2.61	11.57	2.69	-0.01
time (sec)	N/A	0.022	0.171	0.031	2.940	0.447	4.496	110.078	0.000

Problem 604	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	22	17	16	34	95	102	37
normalized size	1	1.00	1.00	0.77	0.73	1.55	4.32	4.64	1.68
time (sec)	N/A	0.002	0.005	0.005	1.364	0.416	1.507	1.633	0.252

Problem 605	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	30	25	30	44	211	96	56
normalized size	1	1.00	0.67	0.56	0.67	0.98	4.69	2.13	1.24
time (sec)	N/A	0.005	0.009	0.003	1.344	0.418	1.996	1.426	0.406

Problem 606	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	41	36	50	59	314	189	73
normalized size	1	1.00	0.61	0.54	0.75	0.88	4.69	2.82	1.09
time (sec)	N/A	0.010	0.012	0.005	1.290	0.435	4.265	1.613	0.441

Problem 607	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	88	88	50	45	68	70	688	207	92
normalized size	1	1.00	0.57	0.51	0.77	0.80	7.82	2.35	1.05
time (sec)	N/A	0.016	0.014	0.005	1.329	0.444	13.450	1.697	0.475

Problem 608	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	88	88	60	93	134	124	95	0	-1
normalized size	1	1.00	0.68	1.06	1.52	1.41	1.08	0.00	-0.01
time (sec)	N/A	0.022	0.040	0.005	2.975	0.439	7.397	0.000	0.000

Problem 609	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	51	78	102	105	75	0	-1
normalized size	1	1.00	0.76	1.16	1.52	1.57	1.12	0.00	-0.01
time (sec)	N/A	0.014	0.028	0.005	2.858	0.443	3.671	0.000	0.000

Problem 610	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	43	62	70	87	54	0	43
normalized size	1	1.00	1.00	1.44	1.63	2.02	1.26	0.00	1.00
time (sec)	N/A	0.009	0.016	0.004	2.919	0.428	1.934	0.000	0.585

Problem 611	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	A	A	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	24	24	24	46	41	55	24	0	30
normalized size	1	1.00	1.00	1.92	1.71	2.29	1.00	0.00	1.25
time (sec)	N/A	0.006	0.004	0.004	2.959	0.462	1.022	0.000	0.035

Problem 612	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	12	15	29	12
normalized size	1	1.00	1.00	0.81	0.75	0.75	0.94	1.81	0.75
time (sec)	N/A	0.001	0.004	0.003	1.355	0.420	0.879	1.108	0.330

Problem 613	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	23	18	26	17	34	42	17
normalized size	1	1.00	0.61	0.47	0.68	0.45	0.89	1.11	0.45
time (sec)	N/A	0.004	0.006	0.005	1.315	0.423	1.873	1.087	0.316

Problem 614	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	32	27	41	26	224	55	26
normalized size	1	1.00	0.54	0.46	0.69	0.44	3.80	0.93	0.44
time (sec)	N/A	0.007	0.008	0.006	1.311	0.417	6.104	1.065	0.323

Problem 615	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	40	35	56	34	374	68	33
normalized size	1	1.00	0.50	0.44	0.70	0.42	4.68	0.85	0.41
time (sec)	N/A	0.012	0.009	0.006	1.295	0.411	15.993	1.025	0.333

Problem 616	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	30	106	119	152	80	119	-1
normalized size	1	1.00	0.35	1.23	1.38	1.77	0.93	1.38	-0.01
time (sec)	N/A	0.020	0.006	0.028	3.055	0.458	7.099	11.125	0.000

Problem 617	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	30	100	90	134	58	106	-1
normalized size	1	1.00	0.48	1.59	1.43	2.13	0.92	1.68	-0.02
time (sec)	N/A	0.014	0.006	0.024	2.988	0.457	3.065	10.155	0.000

Problem 618	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	44	44	44	48	57	117	41	82	-1
normalized size	1	1.00	1.00	1.09	1.30	2.66	0.93	1.86	-0.02
time (sec)	N/A	0.009	0.029	0.112	2.896	0.487	1.565	10.610	0.000

Problem 619	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	12	11	11	15	44	11
normalized size	1	1.00	1.00	0.80	0.73	0.73	1.00	2.93	0.73
time (sec)	N/A	0.001	0.003	0.004	1.340	0.426	0.862	1.216	0.307

Problem 620	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	21	18	26	28	34	74	17
normalized size	1	1.00	0.66	0.56	0.81	0.88	1.06	2.31	0.53
time (sec)	N/A	0.003	0.007	0.005	1.335	0.442	1.543	1.123	0.348

Problem 621	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	32	27	41	39	170	86	37
normalized size	1	1.00	0.60	0.51	0.77	0.74	3.21	1.62	0.70
time (sec)	N/A	0.007	0.008	0.004	1.372	0.429	3.857	1.232	0.380

Problem 622	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	39	35	56	47	269	107	46
normalized size	1	1.00	0.53	0.47	0.76	0.64	3.64	1.45	0.62
time (sec)	N/A	0.014	0.008	0.004	1.303	0.449	10.971	1.110	0.426

Problem 623	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	30	136	105	186	308	182	-1
normalized size	1	1.00	0.35	1.58	1.22	2.16	3.58	2.12	-0.01
time (sec)	N/A	0.020	0.007	0.036	3.003	0.453	6.617	10.823	0.000

Problem 624	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	52	55	69	171	257	154	-1
normalized size	1	1.00	0.80	0.85	1.06	2.63	3.95	2.37	-0.02
time (sec)	N/A	0.014	0.069	0.040	2.971	0.433	3.578	10.772	0.000

Problem 625	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	13	12	27	27	82	12
normalized size	1	1.00	1.00	0.72	0.67	1.50	1.50	4.56	0.67
time (sec)	N/A	0.001	0.004	0.005	1.328	0.413	1.404	1.224	0.252

Problem 626	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	23	18	24	32	75	79	42
normalized size	1	1.00	0.62	0.49	0.65	0.86	2.03	2.14	1.14
time (sec)	N/A	0.003	0.006	0.005	1.318	0.433	1.842	1.215	0.357

Problem 627	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	55	55	32	27	40	45	117	145	57
normalized size	1	1.00	0.58	0.49	0.73	0.82	2.13	2.64	1.04
time (sec)	N/A	0.006	0.008	0.004	1.401	0.425	3.889	1.362	0.378

Problem 628	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	40	35	55	55	257	158	71
normalized size	1	1.00	0.56	0.49	0.77	0.77	3.62	2.23	1.00
time (sec)	N/A	0.009	0.010	0.005	1.276	0.426	6.853	1.272	0.418

Problem 629	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	91	91	61	100	117	125	206	0	-1
normalized size	1	1.00	0.67	1.10	1.29	1.37	2.26	0.00	-0.01
time (sec)	N/A	0.021	0.041	0.005	3.033	0.441	7.511	0.000	0.000

Problem 630	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	52	84	85	107	163	0	-1
normalized size	1	1.00	0.75	1.22	1.23	1.55	2.36	0.00	-0.01
time (sec)	N/A	0.015	0.029	0.004	2.927	0.470	3.591	0.000	0.000

Problem 631	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	45	67	52	90	121	0	46
normalized size	1	1.00	1.00	1.49	1.16	2.00	2.69	0.00	1.02
time (sec)	N/A	0.010	0.016	0.006	2.928	0.462	1.966	0.000	0.520

Problem 632	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	24	24	24	50	21	56	58	0	27
normalized size	1	1.00	1.00	2.08	0.88	2.33	2.42	0.00	1.12
time (sec)	N/A	0.007	0.004	0.004	2.962	0.445	1.081	0.000	0.032

Problem 633	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	14	13	13	39	30	13
normalized size	1	1.00	1.00	0.82	0.76	0.76	2.29	1.76	0.76
time (sec)	N/A	0.001	0.004	0.004	1.351	0.421	0.934	1.283	0.310

Problem 634	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	24	19	28	18	139	43	19
normalized size	1	1.00	0.60	0.48	0.70	0.45	3.48	1.08	0.48
time (sec)	N/A	0.004	0.006	0.003	1.346	0.451	1.957	1.117	0.292

Problem 635	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	30	138	101	155	173	136	-1
normalized size	1	1.00	0.34	1.55	1.13	1.74	1.94	1.53	-0.01
time (sec)	N/A	0.021	0.006	0.028	2.991	0.476	7.026	10.853	0.000

Problem 636	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	30	133	71	138	128	119	-1
normalized size	1	1.00	0.46	2.05	1.09	2.12	1.97	1.83	-0.02
time (sec)	N/A	0.014	0.006	0.028	2.995	0.459	3.199	10.407	0.000

Problem 637	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	45	67	38	122	92	92	-1
normalized size	1	1.00	1.00	1.49	0.84	2.71	2.04	2.04	-0.02
time (sec)	N/A	0.009	0.038	0.046	2.982	0.457	1.693	10.063	0.000

Problem 638	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	20	39	50	12
normalized size	1	1.00	1.00	0.81	0.75	1.25	2.44	3.12	0.75
time (sec)	N/A	0.001	0.004	0.005	1.273	0.420	0.931	1.026	0.299

Problem 639	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	21	18	28	29	90	83	27
normalized size	1	1.00	0.62	0.53	0.82	0.85	2.65	2.44	0.79
time (sec)	N/A	0.003	0.007	0.004	1.259	0.411	1.606	1.086	0.321

Problem 640	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	33	28	44	40	354	96	38
normalized size	1	1.00	0.59	0.50	0.79	0.71	6.32	1.71	0.68
time (sec)	N/A	0.008	0.008	0.006	1.281	0.413	4.293	1.168	0.362

Problem 641	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	30	168	86	187	753	200	-1
normalized size	1	1.00	0.34	1.89	0.97	2.10	8.46	2.25	-0.01
time (sec)	N/A	0.022	0.007	0.038	2.990	0.465	6.803	10.724	0.000

Problem 642	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	53	73	50	173	649	178	-1
normalized size	1	1.00	0.79	1.09	0.75	2.58	9.69	2.66	-0.01
time (sec)	N/A	0.015	0.056	0.041	2.919	0.458	3.700	10.628	0.000

Problem 643	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	19	14	13	28	65	95	13
normalized size	1	1.00	1.00	0.74	0.68	1.47	3.42	5.00	0.68
time (sec)	N/A	0.001	0.005	0.003	1.382	0.437	1.458	1.252	0.232

Problem 644	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	24	19	25	33	177	90	45
normalized size	1	1.00	0.62	0.49	0.64	0.85	4.54	2.31	1.15
time (sec)	N/A	0.004	0.008	0.005	1.302	0.451	1.908	1.100	0.357

Problem 645	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	33	28	42	46	243	170	59
normalized size	1	1.00	0.57	0.48	0.72	0.79	4.19	2.93	1.02
time (sec)	N/A	0.006	0.010	0.004	1.352	0.440	3.995	1.122	0.367

Problem 646	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	75	75	41	36	58	56	529	183	73
normalized size	1	1.00	0.55	0.48	0.77	0.75	7.05	2.44	0.97
time (sec)	N/A	0.010	0.013	0.004	1.351	0.439	12.398	1.250	0.438

Problem 647	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	25	41	37	27	54	17	31
normalized size	1	1.00	0.93	1.52	1.37	1.00	2.00	0.63	1.15
time (sec)	N/A	0.005	0.009	0.006	3.004	0.419	1.646	1.174	0.570

Problem 648	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	8	8	12	27	14	14	20	6	16
normalized size	1	1.00	1.50	3.38	1.75	1.75	2.50	0.75	2.00
time (sec)	N/A	0.003	0.008	0.004	2.951	0.458	0.971	1.095	0.051

Problem 649	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	19	48	21	57	42	0	23
normalized size	1	1.00	1.00	2.53	1.11	3.00	2.21	0.00	1.21
time (sec)	N/A	0.005	0.005	0.007	2.889	0.433	1.060	0.000	0.125

Problem 650	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	17	14	13	18	19	13	13
normalized size	1	1.00	0.81	0.67	0.62	0.86	0.90	0.62	0.62
time (sec)	N/A	0.004	0.005	0.001	1.296	0.402	2.009	0.977	0.028

Problem 651	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	17	14	13	18	19	13	13
normalized size	1	1.00	0.81	0.67	0.62	0.86	0.90	0.62	0.62
time (sec)	N/A	0.004	0.005	0.002	1.351	0.413	1.304	1.045	0.025

Problem 652	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	17	14	13	16	19	13	13
normalized size	1	1.00	0.81	0.67	0.62	0.76	0.90	0.62	0.62
time (sec)	N/A	0.004	0.005	0.003	1.348	0.398	0.446	0.988	0.024

Problem 653	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	17	14	13	16	19	13	13
normalized size	1	1.00	0.81	0.67	0.62	0.76	0.90	0.62	0.62
time (sec)	N/A	0.004	0.005	0.003	1.368	0.456	1.520	1.027	0.025

Problem 654	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	17	14	13	13	19	13	13
normalized size	1	1.00	0.81	0.67	0.62	0.62	0.90	0.62	0.62
time (sec)	N/A	0.004	0.005	0.003	1.307	0.437	1.659	1.121	0.024

Problem 655	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	16	13	13	12	17	13	12
normalized size	1	1.00	0.84	0.68	0.68	0.63	0.89	0.68	0.63
time (sec)	N/A	0.003	0.005	0.002	1.283	0.424	1.494	1.116	0.023

Problem 656	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	16	14	13	12	17	13	13
normalized size	1	1.00	0.84	0.74	0.68	0.63	0.89	0.68	0.68
time (sec)	N/A	0.004	0.005	0.001	1.336	0.425	0.387	1.126	0.027

Problem 657	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	19	12	13	13	17	13	13
normalized size	1	1.00	1.00	0.63	0.68	0.68	0.89	0.68	0.68
time (sec)	N/A	0.004	0.005	0.003	1.299	0.457	0.451	1.101	0.026

Problem 658	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	28	25	24	29	34	24	24
normalized size	1	1.00	0.78	0.69	0.67	0.81	0.94	0.67	0.67
time (sec)	N/A	0.007	0.008	0.004	1.312	0.450	3.748	1.044	0.045

Problem 659	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	28	25	24	29	34	24	24
normalized size	1	1.00	0.78	0.69	0.67	0.81	0.94	0.67	0.67
time (sec)	N/A	0.007	0.008	0.005	1.324	0.428	2.646	1.059	0.038

Problem 660	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	28	25	24	27	34	24	24
normalized size	1	1.00	0.78	0.69	0.67	0.75	0.94	0.67	0.67
time (sec)	N/A	0.007	0.007	0.003	1.320	0.489	1.062	1.050	0.038

Problem 661	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	28	25	24	27	2633	24	24
normalized size	1	1.00	0.78	0.69	0.67	0.75	73.14	0.67	0.67
time (sec)	N/A	0.007	0.007	0.006	1.277	0.441	2.218	1.036	0.035

Problem 662	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	28	25	24	24	1765	24	24
normalized size	1	1.00	0.78	0.69	0.67	0.67	49.03	0.67	0.67
time (sec)	N/A	0.008	0.008	0.005	1.318	0.458	2.045	1.106	0.038

Problem 663	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	28	25	24	24	1741	24	24
normalized size	1	1.00	0.82	0.74	0.71	0.71	51.21	0.71	0.71
time (sec)	N/A	0.007	0.008	0.006	1.380	0.442	2.075	0.921	0.034

Problem 664	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	27	25	24	23	1826	24	24
normalized size	1	1.00	0.84	0.78	0.75	0.72	57.06	0.75	0.75
time (sec)	N/A	0.007	0.008	0.003	1.355	0.455	2.090	1.175	0.037

Problem 665	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	27	25	24	23	1957	24	24
normalized size	1	1.00	0.79	0.74	0.71	0.68	57.56	0.71	0.71
time (sec)	N/A	0.007	0.008	0.004	1.351	0.455	2.063	1.221	0.036

Problem 666	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	39	36	35	40	49	35	35
normalized size	1	1.00	0.76	0.71	0.69	0.78	0.96	0.69	0.69
time (sec)	N/A	0.010	0.011	0.005	1.346	0.423	6.393	1.060	0.043

Problem 667	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	39	36	35	40	49	35	35
normalized size	1	1.00	0.76	0.71	0.69	0.78	0.96	0.69	0.69
time (sec)	N/A	0.011	0.010	0.005	1.289	0.424	4.551	1.061	0.044

Problem 668	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	39	36	35	38	49	35	35
normalized size	1	1.00	0.76	0.71	0.69	0.75	0.96	0.69	0.69
time (sec)	N/A	0.011	0.010	0.006	1.337	0.462	2.187	1.066	0.044

Problem 669	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	39	36	35	38	5012	35	35
normalized size	1	1.00	0.76	0.71	0.69	0.75	98.27	0.69	0.69
time (sec)	N/A	0.011	0.010	0.005	1.349	0.443	3.223	1.161	0.048

Problem 670	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	39	36	35	35	6246	35	35
normalized size	1	1.00	0.76	0.71	0.69	0.69	122.47	0.69	0.69
time (sec)	N/A	0.010	0.010	0.005	1.327	0.425	3.191	0.859	0.044

Problem 671	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	39	36	35	35	6667	35	35
normalized size	1	1.00	0.80	0.73	0.71	0.71	136.06	0.71	0.71
time (sec)	N/A	0.011	0.010	0.006	1.293	0.453	3.171	0.941	0.044

Problem 672	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	39	36	35	35	4004	35	35
normalized size	1	1.00	0.80	0.73	0.71	0.71	81.71	0.71	0.71
time (sec)	N/A	0.011	0.011	0.004	1.323	0.452	3.261	1.072	0.044

Problem 673	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	39	36	35	35	3964	35	35
normalized size	1	1.00	0.80	0.73	0.71	0.71	80.90	0.71	0.71
time (sec)	N/A	0.011	0.011	0.005	1.361	0.423	3.238	1.167	0.043

Problem 674	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	125	125	38	122	130	147	241	138	151
normalized size	1	1.00	0.30	0.98	1.04	1.18	1.93	1.10	1.21
time (sec)	N/A	0.070	0.010	0.008	3.003	0.463	47.121	1.037	0.243

Problem 675	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	123	123	140	121	128	116	240	136	126
normalized size	1	1.00	1.14	0.98	1.04	0.94	1.95	1.11	1.02
time (sec)	N/A	0.056	0.058	0.006	3.051	0.464	25.855	1.208	0.068

Problem 676	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	111	111	29	107	114	128	228	118	130
normalized size	1	1.00	0.26	0.96	1.03	1.15	2.05	1.06	1.17
time (sec)	N/A	0.040	0.009	0.007	2.905	0.451	9.084	1.043	0.150

Problem 677	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	109	109	126	108	115	114	219	119	126
normalized size	1	1.00	1.16	0.99	1.06	1.05	2.01	1.09	1.16
time (sec)	N/A	0.039	0.026	0.007	2.926	0.493	6.098	1.147	0.074

Problem 678	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	27	96	103	313	212	118	120
normalized size	1	1.00	0.27	0.96	1.03	3.13	2.12	1.18	1.20
time (sec)	N/A	0.028	0.007	0.005	2.833	0.478	7.412	1.171	0.113

Problem 679	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	103	95	102	307	212	117	110
normalized size	1	1.00	1.03	0.95	1.02	3.07	2.12	1.17	1.10
time (sec)	N/A	0.028	0.024	0.006	2.963	0.508	11.348	1.175	0.206

Problem 680	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	109	109	25	104	111	113	218	125	124
normalized size	1	1.00	0.23	0.95	1.02	1.04	2.00	1.15	1.14
time (sec)	N/A	0.038	0.005	0.009	2.963	0.473	25.292	1.211	0.147

Problem 681	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	111	111	27	105	112	147	221	120	138
normalized size	1	1.00	0.24	0.95	1.01	1.32	1.99	1.08	1.24
time (sec)	N/A	0.039	0.005	0.008	2.994	0.472	34.964	1.139	0.072

Problem 682	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	129	129	27	123	133	162	0	135	150
normalized size	1	1.00	0.21	0.95	1.03	1.26	0.00	1.05	1.16
time (sec)	N/A	0.047	0.005	0.011	2.959	0.471	0.000	1.052	0.265

Problem 683	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	125	125	27	123	133	147	0	135	142
normalized size	1	1.00	0.22	0.98	1.06	1.18	0.00	1.08	1.14
time (sec)	N/A	0.047	0.005	0.013	2.932	0.486	0.000	1.069	0.152

Problem 684	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	27	112	120	394	787	136	142
normalized size	1	1.00	0.23	0.97	1.04	3.43	6.84	1.18	1.23
time (sec)	N/A	0.038	0.004	0.010	2.994	0.481	106.983	1.199	0.236

Problem 685	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	117	117	27	112	120	389	607	136	120
normalized size	1	1.00	0.23	0.96	1.03	3.32	5.19	1.16	1.03
time (sec)	N/A	0.038	0.005	0.011	3.026	0.496	71.720	1.129	0.063

Problem 686	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	116	116	27	120	127	396	774	132	144
normalized size	1	1.00	0.23	1.03	1.09	3.41	6.67	1.14	1.24
time (sec)	N/A	0.041	0.005	0.009	2.964	0.513	79.660	1.111	0.358

Problem 687	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	113	113	25	120	127	387	590	132	134
normalized size	1	1.00	0.22	1.06	1.12	3.42	5.22	1.17	1.19
time (sec)	N/A	0.040	0.005	0.008	3.009	0.513	115.985	1.035	0.223

Problem 688	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	124	124	25	121	132	156	0	145	151
normalized size	1	1.00	0.20	0.98	1.06	1.26	0.00	1.17	1.22
time (sec)	N/A	0.049	0.005	0.012	3.036	0.490	0.000	0.975	0.152

Problem 689	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	128	128	27	121	132	189	0	137	166
normalized size	1	1.00	0.21	0.95	1.03	1.48	0.00	1.07	1.30
time (sec)	N/A	0.050	0.005	0.014	2.943	0.497	0.000	1.006	0.165

Problem 690	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	140	140	27	124	143	506	0	146	165
normalized size	1	1.00	0.19	0.89	1.02	3.61	0.00	1.04	1.18
time (sec)	N/A	0.049	0.005	0.013	2.952	0.497	0.000	1.058	0.172

Problem 691	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	140	140	27	124	143	503	0	146	139
normalized size	1	1.00	0.19	0.89	1.02	3.59	0.00	1.04	0.99
time (sec)	N/A	0.054	0.004	0.012	2.879	0.484	0.000	1.125	0.066

Problem 692	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	143	143	27	132	153	508	0	149	172
normalized size	1	1.00	0.19	0.92	1.07	3.55	0.00	1.04	1.20
time (sec)	N/A	0.050	0.005	0.013	2.922	0.484	0.000	1.064	0.265

Problem 693	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	143	143	27	132	152	501	0	148	146
normalized size	1	1.00	0.19	0.92	1.06	3.50	0.00	1.03	1.02
time (sec)	N/A	0.052	0.005	0.013	2.959	0.484	0.000	1.110	0.235

Problem 694	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	140	140	27	136	151	510	0	143	167
normalized size	1	1.00	0.19	0.97	1.08	3.64	0.00	1.02	1.19
time (sec)	N/A	0.053	0.005	0.007	2.963	0.475	0.000	1.064	0.192

Problem 695	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	140	140	25	136	151	499	0	143	157
normalized size	1	1.00	0.18	0.97	1.08	3.56	0.00	1.02	1.12
time (sec)	N/A	0.050	0.004	0.007	2.997	0.811	0.000	0.999	0.241

Problem 696	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	152	152	25	139	154	211	0	155	174
normalized size	1	1.00	0.16	0.91	1.01	1.39	0.00	1.02	1.14
time (sec)	N/A	0.060	0.005	0.017	2.989	0.506	0.000	1.163	0.087

Problem 697	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	152	152	27	139	154	244	0	150	182
normalized size	1	1.00	0.18	0.91	1.01	1.61	0.00	0.99	1.20
time (sec)	N/A	0.061	0.005	0.017	2.991	0.489	0.000	1.080	0.173

Problem 698	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	58	62	61	82	243	64	46
normalized size	1	1.00	1.00	1.07	1.05	1.41	4.19	1.10	0.79
time (sec)	N/A	0.021	0.017	0.010	2.909	0.520	2.352	1.169	0.068

Problem 699	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	187	187	166	1535	187	1277	9996	1925	1274
normalized size	1	1.00	0.89	8.21	1.00	6.83	53.45	10.29	6.81
time (sec)	N/A	0.085	0.111	0.007	1.387	0.506	6.929	1.204	1.370

Problem 700	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	133	133	118	782	133	665	4257	992	683
normalized size	1	1.00	0.89	5.88	1.00	5.00	32.01	7.46	5.14
time (sec)	N/A	0.050	0.068	0.006	1.366	0.497	3.337	1.396	0.777

Problem 701	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	54	170	61	157	663	224	167
normalized size	1	1.00	0.89	2.79	1.00	2.57	10.87	3.67	2.74
time (sec)	N/A	0.018	0.031	0.000	1.299	0.518	0.917	1.067	0.443

Problem 702	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	38	87	43	85	299	117	93
normalized size	1	1.00	0.88	2.02	1.00	1.98	6.95	2.72	2.16
time (sec)	N/A	0.013	0.031	0.000	1.323	0.462	0.546	1.044	0.370

Problem 703	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	25	25	22	31	25	33	87	43	30
normalized size	1	1.00	0.88	1.24	1.00	1.32	3.48	1.72	1.20
time (sec)	N/A	0.006	0.014	0.000	1.354	0.460	0.308	1.021	0.304

Problem 704	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	29	0	0	0	61	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	2.10	0.00	-0.03
time (sec)	N/A	0.006	0.007	0.035	0.000	0.467	0.785	0.000	0.000

Problem 705	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	29	0	0	0	262	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	9.03	0.00	-0.03
time (sec)	N/A	0.005	0.006	0.036	0.000	0.457	1.039	0.000	0.000

Problem 706	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	29	0	0	0	717	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	24.72	0.00	-0.03
time (sec)	N/A	0.005	0.006	0.044	0.000	0.481	1.449	0.000	0.000

Problem 707	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	48	0	0	0	37	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.77	0.00	-0.02
time (sec)	N/A	0.011	0.064	0.042	0.000	0.468	10.168	0.000	0.000

Problem 708	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	48	0	0	0	37	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.77	0.00	-0.02
time (sec)	N/A	0.012	0.040	0.039	0.000	0.455	3.455	0.000	0.000

Problem 709	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	48	0	0	0	37	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.77	0.00	-0.02
time (sec)	N/A	0.011	0.031	0.043	0.000	0.466	1.684	0.000	0.000

Problem 710	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	46	0	0	0	36	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.78	0.00	-0.02
time (sec)	N/A	0.011	0.024	0.040	0.000	0.468	1.562	0.000	0.000

Problem 711	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	46	0	0	0	36	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.78	0.00	-0.02
time (sec)	N/A	0.011	0.036	0.037	0.000	0.488	1.903	0.000	0.000

Problem 712	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	48	0	0	0	36	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.75	0.00	-0.02
time (sec)	N/A	0.011	0.039	0.035	0.000	0.536	3.540	0.000	0.000

Problem 713	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	51	0	0	0	37	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.73	0.00	-0.02
time (sec)	N/A	0.012	0.036	0.036	0.000	0.482	3.378	0.000	0.000

Problem 714	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	49	0	0	0	37	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.76	0.00	-0.02
time (sec)	N/A	0.012	0.035	0.036	0.000	0.479	2.465	0.000	0.000

Problem 715	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	46	0	0	0	36	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.78	0.00	-0.02
time (sec)	N/A	0.011	0.015	0.000	0.000	0.466	1.508	0.000	0.000

Problem 716	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	48	0	0	0	31	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.65	0.00	-0.02
time (sec)	N/A	0.012	0.029	0.033	0.000	0.509	3.748	0.000	0.000

Problem 717	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	49	0	0	0	32	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.65	0.00	-0.02
time (sec)	N/A	0.012	0.031	0.033	0.000	0.542	9.261	0.000	0.000

Problem 718	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	51	0	0	0	37	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.73	0.00	-0.02
time (sec)	N/A	0.013	0.032	0.036	0.000	0.584	24.006	0.000	0.000

Problem 719	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	31	29	0	0	37	0	-1
normalized size	1	1.00	1.00	0.94	0.00	0.00	1.19	0.00	-0.03
time (sec)	N/A	0.006	0.006	0.054	0.000	0.484	1.199	0.000	0.000

Problem 720	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	31	29	0	0	46	0	-1
normalized size	1	1.00	1.00	0.94	0.00	0.00	1.48	0.00	-0.03
time (sec)	N/A	0.004	0.006	0.052	0.000	0.562	1.216	0.000	0.000

Problem 721	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	36	43	0	0	36	0	-1
normalized size	1	1.00	1.00	1.19	0.00	0.00	1.00	0.00	-0.03
time (sec)	N/A	0.008	0.007	0.059	0.000	0.544	1.216	0.000	0.000

Problem 722	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	48	30	0	0	41	0	-1
normalized size	1	1.00	0.96	0.60	0.00	0.00	0.82	0.00	-0.02
time (sec)	N/A	0.011	0.027	0.038	0.000	0.592	1.191	0.000	0.000

Problem 723	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	48	0	0	0	42	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.88	0.00	-0.02
time (sec)	N/A	0.011	0.017	0.036	0.000	0.455	1.537	0.000	0.000

Problem 724	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	32	30	0	0	44	0	-1
normalized size	1	1.00	0.94	0.88	0.00	0.00	1.29	0.00	-0.03
time (sec)	N/A	0.006	0.006	0.062	0.000	0.444	1.201	0.000	0.000

Problem 725	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	34	34	32	30	0	0	53	0	-1
normalized size	1	1.00	0.94	0.88	0.00	0.00	1.56	0.00	-0.03
time (sec)	N/A	0.005	0.006	0.046	0.000	0.484	1.258	0.000	0.000

Problem 726	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	49	44	0	0	42	0	-1
normalized size	1	1.00	1.00	0.90	0.00	0.00	0.86	0.00	-0.02
time (sec)	N/A	0.011	0.009	0.064	0.000	0.556	1.278	0.000	0.000

Problem 727	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	57	31	0	0	48	0	-1
normalized size	1	1.00	1.54	0.84	0.00	0.00	1.30	0.00	-0.03
time (sec)	N/A	0.005	0.016	0.042	0.000	0.483	1.193	0.000	0.000

Problem 728	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	26	23	0	0	26	0	-1
normalized size	1	1.00	1.00	0.88	0.00	0.00	1.00	0.00	-0.04
time (sec)	N/A	0.004	0.004	0.051	0.000	0.504	1.112	0.000	0.000

Problem 729	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	0	0	0	31	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	1.03	0.00	-0.03
time (sec)	N/A	0.004	0.008	0.043	0.000	0.488	1.160	0.000	0.000

Problem 730	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	47	0	0	0	34	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.72	0.00	-0.02
time (sec)	N/A	0.011	0.010	0.072	0.000	0.519	3.570	0.000	0.000

Problem 731	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	52	48	0	0	0	37	0	-1
normalized size	1	1.00	0.92	0.00	0.00	0.00	0.71	0.00	-0.02
time (sec)	N/A	0.014	0.008	0.089	0.000	0.514	3.139	0.000	0.000

Problem 732	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	83	83	67	126	101	143	1318	226	176
normalized size	1	1.00	0.81	1.52	1.22	1.72	15.88	2.72	2.12
time (sec)	N/A	0.031	0.054	0.007	1.364	0.482	2.326	1.212	0.534

Problem 733	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	57	73	68	96	597	140	192
normalized size	1	1.00	0.95	1.22	1.13	1.60	9.95	2.33	3.20
time (sec)	N/A	0.019	0.028	0.006	1.374	0.476	1.315	1.074	0.557

Problem 734	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	33	36	42	53	201	76	94
normalized size	1	1.00	0.85	0.92	1.08	1.36	5.15	1.95	2.41
time (sec)	N/A	0.012	0.017	0.002	1.311	0.471	0.702	1.051	0.378

Problem 735	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	17	19	18	20	20	18	18
normalized size	1	1.00	0.94	1.06	1.00	1.11	1.11	1.00	1.00
time (sec)	N/A	0.003	0.009	0.003	1.296	0.492	0.066	1.137	0.198

Problem 736	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	B	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	35	0	0	0	83	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	2.37	0.00	-0.03
time (sec)	N/A	0.006	0.009	0.039	0.000	0.467	1.600	0.000	0.000

Problem 737	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	B	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	35	0	0	0	354	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	10.11	0.00	-0.03
time (sec)	N/A	0.007	0.006	0.040	0.000	0.504	2.092	0.000	0.000

Problem 738	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	B	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	38	0	0	0	918	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	24.16	0.00	-0.03
time (sec)	N/A	0.008	0.006	0.038	0.000	0.488	2.839	0.000	0.000

Problem 739	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	110	110	64	77	0	104	0	0	136
normalized size	1	1.00	0.58	0.70	0.00	0.95	0.00	0.00	1.24
time (sec)	N/A	0.036	0.026	0.006	0.000	0.517	0.000	0.000	0.523

Problem 740	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	39	44	0	64	0	0	80
normalized size	1	1.00	0.61	0.69	0.00	1.00	0.00	0.00	1.25
time (sec)	N/A	0.009	0.016	0.005	0.000	0.477	0.000	0.000	0.447

Problem 741	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	25	29	0	33	0	0	29
normalized size	1	1.00	0.89	1.04	0.00	1.18	0.00	0.00	1.04
time (sec)	N/A	0.003	0.006	0.003	0.000	0.481	0.000	0.000	0.349

Problem 742	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	39	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.03
time (sec)	N/A	0.010	0.007	0.061	0.000	0.497	0.000	0.000	0.000

Problem 743	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	45	0	0	0	32	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.71	0.00	-0.02
time (sec)	N/A	0.010	0.007	0.059	0.000	0.497	28.691	0.000	0.000

Problem 744	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	45	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.011	0.008	0.063	0.000	0.447	0.000	0.000	0.000

Problem 745	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	45	0	0	0	27	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.60	0.00	-0.02
time (sec)	N/A	0.009	0.008	0.042	0.000	0.493	87.985	0.000	0.000

Problem 746	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	45	0	0	0	27	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.60	0.00	-0.02
time (sec)	N/A	0.009	0.007	0.040	0.000	0.480	8.378	0.000	0.000

Problem 747	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	43	0	0	0	26	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.60	0.00	-0.02
time (sec)	N/A	0.009	0.006	0.036	0.000	0.483	5.692	0.000	0.000

Problem 748	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	43	0	0	0	29	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.67	0.00	-0.02
time (sec)	N/A	0.009	0.008	0.038	0.000	0.484	31.961	0.000	0.000

Problem 749	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	45	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.009	0.007	0.036	0.000	0.497	0.000	0.000	0.000

Problem 750	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	31	32	0	0	37	0	-1
normalized size	1	1.00	0.89	0.91	0.00	0.00	1.06	0.00	-0.03
time (sec)	N/A	0.011	0.007	0.091	0.000	0.462	2.530	0.000	0.000

Problem 751	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	44	0	0	0	37	0	-1
normalized size	1	1.00	1.10	0.00	0.00	0.00	0.92	0.00	-0.02
time (sec)	N/A	0.009	0.010	0.125	0.000	0.466	2.502	0.000	0.000

Problem 752	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	52	48	0	0	0	37	0	-1
normalized size	1	1.00	0.92	0.00	0.00	0.00	0.71	0.00	-0.02
time (sec)	N/A	0.013	0.012	0.070	0.000	0.700	3.171	0.000	0.000

Problem 753	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	19	20	22	32	0	0	19
normalized size	1	1.00	1.00	1.05	1.16	1.68	0.00	0.00	1.00
time (sec)	N/A	0.003	0.005	0.003	1.302	0.511	0.000	0.000	0.504

Problem 754	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	40	41	0	64	323	0	86
normalized size	1	1.00	0.69	0.71	0.00	1.10	5.57	0.00	1.48
time (sec)	N/A	0.013	0.014	0.005	0.000	0.486	94.815	0.000	0.498

Problem 755	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	40	41	0	64	323	0	86
normalized size	1	1.00	0.69	0.71	0.00	1.10	5.57	0.00	1.48
time (sec)	N/A	0.011	0.002	0.000	0.000	0.466	94.488	0.000	0.002

Problem 756	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	24	21	33	22	36	22	-1
normalized size	1	1.00	0.69	0.60	0.94	0.63	1.03	0.63	-0.03
time (sec)	N/A	0.011	0.005	0.006	1.334	0.419	0.435	0.886	0.000

Problem 757	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	24	21	31	22	36	22	-1
normalized size	1	1.00	0.69	0.60	0.89	0.63	1.03	0.63	-0.03
time (sec)	N/A	0.010	0.004	0.002	1.370	0.428	0.339	1.031	0.000

Problem 758	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	24	21	28	22	36	22	-1
normalized size	1	1.00	0.69	0.60	0.80	0.63	1.03	0.63	-0.03
time (sec)	N/A	0.009	0.004	0.004	1.348	0.455	0.268	0.854	0.000

Problem 759	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	22	19	25	20	34	22	20
normalized size	1	1.00	0.67	0.58	0.76	0.61	1.03	0.67	0.61
time (sec)	N/A	0.008	0.003	0.010	1.316	0.426	0.224	1.047	0.542

Problem 760	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	24	17	0	16	29	17	14
normalized size	1	1.00	0.89	0.63	0.00	0.59	1.07	0.63	0.52
time (sec)	N/A	0.004	0.005	0.003	0.000	0.470	0.228	1.090	0.192

Problem 761	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	20	20	0	19	0	17	-1
normalized size	1	1.00	0.71	0.71	0.00	0.68	0.00	0.61	-0.04
time (sec)	N/A	0.005	0.005	0.022	0.000	0.470	0.000	0.925	0.000

Problem 762	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	20	21	0	20	0	20	-1
normalized size	1	1.00	0.62	0.66	0.00	0.62	0.00	0.62	-0.03
time (sec)	N/A	0.007	0.006	0.008	0.000	0.436	0.000	1.099	0.000

Problem 763	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	22	19	0	18	36	19	28
normalized size	1	1.00	0.85	0.73	0.00	0.69	1.38	0.73	1.08
time (sec)	N/A	0.004	0.004	0.005	0.000	0.430	0.507	0.971	0.144

Problem 764	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	24	21	33	24	36	22	-1
normalized size	1	1.00	0.65	0.57	0.89	0.65	0.97	0.59	-0.03
time (sec)	N/A	0.013	0.006	0.003	1.335	0.447	1.161	1.173	0.000

Problem 765	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	24	21	31	24	36	22	-1
normalized size	1	1.00	0.65	0.57	0.84	0.65	0.97	0.59	-0.03
time (sec)	N/A	0.012	0.006	0.005	1.339	0.430	0.909	0.929	0.000

Problem 766	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	24	21	28	24	36	22	-1
normalized size	1	1.00	0.65	0.57	0.76	0.65	0.97	0.59	-0.03
time (sec)	N/A	0.011	0.005	0.003	1.353	0.422	0.728	0.993	0.000

Problem 767	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	22	19	25	24	34	22	-1
normalized size	1	1.00	0.59	0.51	0.68	0.65	0.92	0.59	-0.03
time (sec)	N/A	0.010	0.005	0.003	1.297	0.431	0.558	0.878	0.000

Problem 768	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	25	18	22	24	31	22	-1
normalized size	1	1.00	0.68	0.49	0.59	0.65	0.84	0.59	-0.03
time (sec)	N/A	0.009	0.002	0.005	1.336	0.439	0.577	1.090	0.000

Problem 769	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	23	21	0	22	31	22	20
normalized size	1	1.00	0.66	0.60	0.00	0.63	0.89	0.63	0.57
time (sec)	N/A	0.008	0.002	0.003	0.000	0.451	0.572	1.082	0.267

Problem 770	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	21	20	0	18	32	17	14
normalized size	1	1.00	0.72	0.69	0.00	0.62	1.10	0.59	0.48
time (sec)	N/A	0.004	0.003	0.003	0.000	0.428	0.741	0.989	0.222

Problem 771	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	21	20	0	21	0	17	-1
normalized size	1	1.00	0.70	0.67	0.00	0.70	0.00	0.57	-0.03
time (sec)	N/A	0.005	0.005	0.003	0.000	0.461	0.000	0.958	0.000

Problem 772	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	24	21	33	28	36	28	-1
normalized size	1	1.00	0.59	0.51	0.80	0.68	0.88	0.68	-0.02
time (sec)	N/A	0.016	0.007	0.003	1.244	0.432	2.543	0.966	0.000

Problem 773	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	24	21	31	28	36	28	-1
normalized size	1	1.00	0.59	0.51	0.76	0.68	0.88	0.68	-0.02
time (sec)	N/A	0.015	0.007	0.003	1.305	0.453	2.097	0.801	0.000

Problem 774	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	24	21	28	28	36	28	-1
normalized size	1	1.00	0.59	0.51	0.68	0.68	0.88	0.68	-0.02
time (sec)	N/A	0.013	0.007	0.003	1.351	0.418	1.742	1.027	0.000

Problem 775	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	22	19	25	28	34	28	-1
normalized size	1	1.00	0.54	0.46	0.61	0.68	0.83	0.68	-0.02
time (sec)	N/A	0.013	0.006	0.005	1.341	0.429	1.410	0.948	0.000

Problem 776	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	25	18	22	28	31	28	-1
normalized size	1	1.00	0.61	0.44	0.54	0.68	0.76	0.68	-0.02
time (sec)	N/A	0.012	0.003	0.002	1.402	0.470	1.429	1.074	0.000

Problem 777	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	23	21	24	28	31	28	25
normalized size	1	1.00	0.56	0.51	0.59	0.68	0.76	0.68	0.61
time (sec)	N/A	0.011	0.003	0.003	1.283	0.403	1.529	1.103	0.284

Problem 778	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	27	21	0	28	34	28	25
normalized size	1	1.00	0.66	0.51	0.00	0.68	0.83	0.68	0.61
time (sec)	N/A	0.010	0.003	0.003	0.000	0.452	1.578	0.994	0.265

Problem 779	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	25	21	0	26	36	28	20
normalized size	1	1.00	0.64	0.54	0.00	0.67	0.92	0.72	0.51
time (sec)	N/A	0.008	0.002	0.004	0.000	0.465	1.623	1.139	0.260

Problem 780	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	24	21	33	25	36	26	-1
normalized size	1	1.00	0.69	0.60	0.94	0.71	1.03	0.74	-0.03
time (sec)	N/A	0.009	0.005	0.003	1.403	0.430	0.606	1.305	0.000

Problem 781	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	24	21	26	23	36	24	23
normalized size	1	1.00	0.69	0.60	0.74	0.66	1.03	0.69	0.66
time (sec)	N/A	0.008	0.004	0.003	1.301	0.484	0.522	1.158	0.251

Problem 782	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	23	20	22	19	34	22	19
normalized size	1	1.00	0.72	0.62	0.69	0.59	1.06	0.69	0.59
time (sec)	N/A	0.004	0.002	0.003	1.301	0.458	0.462	1.105	0.221

Problem 783	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	19	18	20	22	0	35	17
normalized size	1	1.00	0.66	0.62	0.69	0.76	0.00	1.21	0.59
time (sec)	N/A	0.005	0.002	0.004	1.325	0.429	0.000	1.321	0.513

Problem 784	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	23	18	17	23	0	47	22
normalized size	1	1.00	0.85	0.67	0.63	0.85	0.00	1.74	0.81
time (sec)	N/A	0.006	0.006	0.004	1.326	0.456	0.000	0.984	1.222

Problem 785	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	23	19	19	21	31	0	25
normalized size	1	1.00	0.88	0.73	0.73	0.81	1.19	0.00	0.96
time (sec)	N/A	0.004	0.006	0.003	1.251	0.474	0.544	0.000	0.157

Problem 786	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	22	21	19	23	36	0	26
normalized size	1	1.00	0.63	0.60	0.54	0.66	1.03	0.00	0.74
time (sec)	N/A	0.007	0.006	0.005	1.279	0.419	0.636	0.000	0.149

Problem 787	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	24	21	19	23	37	0	26
normalized size	1	1.00	0.69	0.60	0.54	0.66	1.06	0.00	0.74
time (sec)	N/A	0.007	0.005	0.003	1.296	0.438	0.810	0.000	0.149

Problem 788	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	23	20	32	19	34	25	-1
normalized size	1	1.00	0.61	0.53	0.84	0.50	0.89	0.66	-0.03
time (sec)	N/A	0.006	0.004	0.003	1.307	0.436	0.635	1.014	0.000

Problem 789	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	21	20	23	22	0	40	30
normalized size	1	1.00	0.60	0.57	0.66	0.63	0.00	1.14	0.86
time (sec)	N/A	0.005	0.004	0.004	1.346	0.499	0.000	0.986	0.320

Problem 790	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	22	21	21	23	0	47	28
normalized size	1	1.00	0.67	0.64	0.64	0.70	0.00	1.42	0.85
time (sec)	N/A	0.007	0.003	0.003	1.312	0.430	0.000	1.224	0.250

Problem 791	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	22	17	23	21	34	0	25
normalized size	1	1.00	0.76	0.59	0.79	0.72	1.17	0.00	0.86
time (sec)	N/A	0.004	0.003	0.003	1.346	0.463	0.538	0.000	0.149

Problem 792	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	25	18	19	23	32	0	26
normalized size	1	1.00	0.61	0.44	0.46	0.56	0.78	0.00	0.63
time (sec)	N/A	0.008	0.008	0.003	1.318	0.449	0.632	0.000	0.158

Problem 793	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	27	21	19	23	32	0	26
normalized size	1	1.00	0.66	0.51	0.46	0.56	0.78	0.00	0.63
time (sec)	N/A	0.007	0.008	0.004	1.338	0.450	0.769	0.000	0.151

Problem 794	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	22	21	19	23	36	0	26
normalized size	1	1.00	0.54	0.51	0.46	0.56	0.88	0.00	0.63
time (sec)	N/A	0.008	0.007	0.004	1.278	0.459	0.934	0.000	0.149

Problem 795	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	24	21	19	23	37	0	26
normalized size	1	1.00	0.59	0.51	0.46	0.56	0.90	0.00	0.63
time (sec)	N/A	0.007	0.006	0.004	1.348	0.507	1.164	0.000	0.151

Problem 796	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	22	21	24	23	0	47	-1
normalized size	1	1.00	0.67	0.64	0.73	0.70	0.00	1.42	-0.03
time (sec)	N/A	0.008	0.005	0.004	1.429	0.484	0.000	1.015	0.000

Problem 797	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	24	19	26	21	36	0	25
normalized size	1	1.00	0.83	0.66	0.90	0.72	1.24	0.00	0.86
time (sec)	N/A	0.005	0.006	0.003	1.342	0.442	0.931	0.000	0.153

Problem 798	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	24	21	23	23	37	0	26
normalized size	1	1.00	0.59	0.51	0.56	0.56	0.90	0.00	0.63
time (sec)	N/A	0.008	0.004	0.003	1.387	0.435	0.918	0.000	0.151

Problem 799	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	27	19	23	23	36	0	26
normalized size	1	1.00	0.66	0.46	0.56	0.56	0.88	0.00	0.63
time (sec)	N/A	0.007	0.003	0.003	1.374	0.433	0.916	0.000	0.160

Problem 800	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	27	18	19	23	32	0	26
normalized size	1	1.00	0.66	0.44	0.46	0.56	0.78	0.00	0.63
time (sec)	N/A	0.008	0.008	0.003	1.334	0.445	1.121	0.000	0.158

Problem 801	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	27	21	19	23	32	0	26
normalized size	1	1.00	0.66	0.51	0.46	0.56	0.78	0.00	0.63
time (sec)	N/A	0.008	0.007	0.004	1.316	0.436	1.341	0.000	0.162

Problem 802	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	22	21	19	23	36	0	26
normalized size	1	1.00	0.54	0.51	0.46	0.56	0.88	0.00	0.63
time (sec)	N/A	0.009	0.008	0.005	1.370	0.419	1.644	0.000	0.159

Problem 803	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	24	21	19	23	37	0	26
normalized size	1	1.00	0.59	0.51	0.46	0.56	0.90	0.00	0.63
time (sec)	N/A	0.008	0.007	0.002	1.342	0.496	1.968	0.000	0.162

Problem 804	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	35	32	54	33	60	35	-1
normalized size	1	1.00	0.61	0.56	0.95	0.58	1.05	0.61	-0.02
time (sec)	N/A	0.015	0.006	0.004	1.395	0.411	0.587	1.078	0.000

Problem 805	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	35	32	52	33	61	35	-1
normalized size	1	1.00	0.61	0.56	0.91	0.58	1.07	0.61	-0.02
time (sec)	N/A	0.015	0.006	0.005	1.348	0.449	0.463	1.042	0.000

Problem 806	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	35	32	49	33	60	35	-1
normalized size	1	1.00	0.61	0.56	0.86	0.58	1.05	0.61	-0.02
time (sec)	N/A	0.013	0.006	0.004	1.311	0.416	0.368	1.110	0.000

Problem 807	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	55	55	33	30	44	31	60	35	-1
normalized size	1	1.00	0.60	0.55	0.80	0.56	1.09	0.64	-0.02
time (sec)	N/A	0.014	0.007	0.004	1.352	0.443	0.297	0.948	0.000

Problem 808	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	25	28	0	27	51	29	-1
normalized size	1	1.00	0.96	1.08	0.00	1.04	1.96	1.12	-0.04
time (sec)	N/A	0.004	0.005	0.003	0.000	0.438	0.297	0.972	0.000

Problem 809	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	33	33	0	32	0	32	-1
normalized size	1	1.00	0.67	0.67	0.00	0.65	0.00	0.65	-0.02
time (sec)	N/A	0.009	0.009	0.007	0.000	0.451	0.000	1.081	0.000

Problem 810	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	31	32	0	31	0	31	-1
normalized size	1	1.00	0.63	0.65	0.00	0.63	0.00	0.63	-0.02
time (sec)	N/A	0.011	0.011	0.010	0.000	0.440	0.000	1.015	0.000

Problem 811	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	36	34	0	33	0	35	-1
normalized size	1	1.00	0.67	0.63	0.00	0.61	0.00	0.65	-0.02
time (sec)	N/A	0.012	0.010	0.010	0.000	0.449	0.000	0.987	0.000

Problem 812	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	35	32	54	36	60	35	-1
normalized size	1	1.00	0.58	0.53	0.90	0.60	1.00	0.58	-0.02
time (sec)	N/A	0.019	0.008	0.006	1.345	0.411	1.498	1.086	0.000

Problem 813	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	35	32	52	36	61	35	-1
normalized size	1	1.00	0.58	0.53	0.87	0.60	1.02	0.58	-0.02
time (sec)	N/A	0.017	0.008	0.005	1.329	0.466	1.225	1.085	0.000

Problem 814	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	35	32	49	36	60	35	-1
normalized size	1	1.00	0.58	0.53	0.82	0.60	1.00	0.58	-0.02
time (sec)	N/A	0.016	0.007	0.005	1.312	0.414	0.971	1.185	0.000

Problem 815	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	33	30	44	36	60	35	-1
normalized size	1	1.00	0.55	0.50	0.73	0.60	1.00	0.58	-0.02
time (sec)	N/A	0.015	0.007	0.006	1.359	0.411	0.770	1.129	0.000

Problem 816	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	36	29	40	36	54	35	-1
normalized size	1	1.00	0.60	0.48	0.67	0.60	0.90	0.58	-0.02
time (sec)	N/A	0.015	0.004	0.003	1.296	0.405	0.793	0.951	0.000

Problem 817	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	34	32	0	34	54	35	-1
normalized size	1	1.00	0.59	0.55	0.00	0.59	0.93	0.60	-0.02
time (sec)	N/A	0.013	0.004	0.004	0.000	0.417	0.805	1.026	0.000

Problem 818	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	26	31	0	30	51	29	-1
normalized size	1	1.00	0.96	1.15	0.00	1.11	1.89	1.07	-0.04
time (sec)	N/A	0.004	0.005	0.003	0.000	0.396	0.939	1.224	0.000

Problem 819	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	52	34	33	0	35	0	32	-1
normalized size	1	1.00	0.65	0.63	0.00	0.67	0.00	0.62	-0.02
time (sec)	N/A	0.010	0.009	0.005	0.000	0.412	0.000	1.198	0.000

Problem 820	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	35	32	49	42	60	44	-1
normalized size	1	1.00	0.53	0.48	0.74	0.64	0.91	0.67	-0.02
time (sec)	N/A	0.019	0.008	0.004	1.344	0.446	2.186	1.221	0.000

Problem 821	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	33	30	44	42	60	44	-1
normalized size	1	1.00	0.50	0.45	0.67	0.64	0.91	0.67	-0.02
time (sec)	N/A	0.017	0.008	0.005	1.317	0.436	1.802	1.048	0.000

Problem 822	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	36	29	40	42	54	44	-1
normalized size	1	1.00	0.55	0.44	0.61	0.64	0.82	0.67	-0.02
time (sec)	N/A	0.016	0.004	0.004	1.281	0.409	1.823	0.956	0.000

Problem 823	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	34	32	40	42	54	44	-1
normalized size	1	1.00	0.52	0.48	0.61	0.64	0.82	0.67	-0.02
time (sec)	N/A	0.015	0.005	0.005	1.375	0.403	1.841	0.991	0.000

Problem 824	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	38	32	0	42	54	44	-1
normalized size	1	1.00	0.58	0.48	0.00	0.64	0.82	0.67	-0.02
time (sec)	N/A	0.014	0.004	0.004	0.000	0.463	1.948	0.942	0.000

Problem 825	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	36	32	0	40	60	44	-1
normalized size	1	1.00	0.56	0.50	0.00	0.62	0.94	0.69	-0.02
time (sec)	N/A	0.015	0.003	0.005	0.000	0.423	2.007	1.053	0.000

Problem 826	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	26	31	0	36	56	41	-1
normalized size	1	1.00	0.90	1.07	0.00	1.24	1.93	1.41	-0.03
time (sec)	N/A	0.004	0.006	0.002	0.000	0.421	2.034	1.116	0.000

Problem 827	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	35	33	0	41	0	41	-1
normalized size	1	1.00	0.60	0.57	0.00	0.71	0.00	0.71	-0.02
time (sec)	N/A	0.011	0.010	0.006	0.000	0.427	0.000	1.082	0.000

Problem 828	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	35	32	54	36	60	41	-1
normalized size	1	1.00	0.61	0.56	0.95	0.63	1.05	0.72	-0.02
time (sec)	N/A	0.013	0.006	0.004	1.345	0.408	0.788	0.943	0.000

Problem 829	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	35	32	47	34	61	38	-1
normalized size	1	1.00	0.61	0.56	0.82	0.60	1.07	0.67	-0.02
time (sec)	N/A	0.012	0.005	0.002	1.322	0.408	0.647	1.252	0.000

Problem 830	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	24	24	24	31	42	30	56	36	-1
normalized size	1	1.00	1.00	1.29	1.75	1.25	2.33	1.50	-0.04
time (sec)	N/A	0.003	0.002	0.003	1.370	0.426	0.540	1.147	0.000

Problem 831	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	52	32	31	35	35	0	50	-1
normalized size	1	1.00	0.62	0.60	0.67	0.67	0.00	0.96	-0.02
time (sec)	N/A	0.010	0.003	0.005	1.348	0.406	0.000	1.118	0.000

Problem 832	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	34	29	35	34	0	65	-1
normalized size	1	1.00	0.72	0.62	0.74	0.72	0.00	1.38	-0.02
time (sec)	N/A	0.011	0.009	0.003	1.357	0.424	0.000	0.943	0.000

Problem 833	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	35	34	31	36	0	0	-1
normalized size	1	1.00	0.71	0.69	0.63	0.73	0.00	0.00	-0.02
time (sec)	N/A	0.011	0.008	0.007	1.289	0.428	0.000	0.000	0.000

Problem 834	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	33	30	33	32	53	0	33
normalized size	1	1.00	1.27	1.15	1.27	1.23	2.04	0.00	1.27
time (sec)	N/A	0.004	0.010	0.005	1.330	0.450	0.662	0.000	0.183

Problem 835	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	35	32	33	34	61	0	42
normalized size	1	1.00	0.61	0.56	0.58	0.60	1.07	0.00	0.74
time (sec)	N/A	0.013	0.007	0.006	1.326	0.422	0.819	0.000	0.187

Problem 836	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	26	31	52	30	56	39	-1
normalized size	1	1.00	0.96	1.15	1.93	1.11	2.07	1.44	-0.04
time (sec)	N/A	0.004	0.004	0.003	1.356	0.410	0.804	1.054	0.000

Problem 837	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	34	33	45	35	0	55	-1
normalized size	1	1.00	0.56	0.54	0.74	0.57	0.00	0.90	-0.02
time (sec)	N/A	0.011	0.007	0.005	1.331	0.433	0.000	1.096	0.000

Problem 838	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	33	32	42	34	0	69	-1
normalized size	1	1.00	0.59	0.57	0.75	0.61	0.00	1.23	-0.02
time (sec)	N/A	0.012	0.005	0.004	1.379	0.427	0.000	1.083	0.000

Problem 839	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	34	32	35	36	0	0	-1
normalized size	1	1.00	0.59	0.55	0.60	0.62	0.00	0.00	-0.02
time (sec)	N/A	0.012	0.004	0.004	1.327	0.439	0.000	0.000	0.000

Problem 840	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	36	27	37	32	53	0	33
normalized size	1	1.00	1.24	0.93	1.28	1.10	1.83	0.00	1.14
time (sec)	N/A	0.004	0.012	0.005	1.361	0.424	0.667	0.000	0.191

Problem 841	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	38	32	33	34	56	0	42
normalized size	1	1.00	0.58	0.48	0.50	0.52	0.85	0.00	0.64
time (sec)	N/A	0.013	0.009	0.006	1.310	0.424	0.812	0.000	0.193

Problem 842	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	33	32	33	34	56	0	42
normalized size	1	1.00	0.50	0.48	0.50	0.52	0.85	0.00	0.64
time (sec)	N/A	0.013	0.012	0.005	1.358	0.464	0.982	0.000	0.197

Problem 843	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	35	32	33	34	61	0	42
normalized size	1	1.00	0.53	0.48	0.50	0.52	0.92	0.00	0.64
time (sec)	N/A	0.014	0.009	0.005	1.293	0.433	1.183	0.000	0.175

Problem 844	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	33	32	45	34	0	65	-1
normalized size	1	1.00	0.59	0.57	0.80	0.61	0.00	1.16	-0.02
time (sec)	N/A	0.013	0.008	0.005	1.451	0.516	0.000	1.066	0.000

Problem 845	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	36	34	38	36	0	0	-1
normalized size	1	1.00	0.62	0.59	0.66	0.62	0.00	0.00	-0.02
time (sec)	N/A	0.012	0.009	0.006	1.398	0.475	0.000	0.000	0.000

Problem 846	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	35	30	44	32	58	0	33
normalized size	1	1.00	1.21	1.03	1.52	1.10	2.00	0.00	1.14
time (sec)	N/A	0.004	0.007	0.004	1.377	0.420	0.957	0.000	0.180

Problem 847	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	38	30	37	34	61	0	42
normalized size	1	1.00	0.58	0.45	0.56	0.52	0.92	0.00	0.64
time (sec)	N/A	0.013	0.004	0.005	1.357	0.413	0.963	0.000	0.175

Problem 848	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	38	29	37	34	56	0	42
normalized size	1	1.00	0.58	0.44	0.56	0.52	0.85	0.00	0.64
time (sec)	N/A	0.012	0.012	0.006	1.309	0.439	1.154	0.000	0.176

Problem 849	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	38	32	33	34	56	0	42
normalized size	1	1.00	0.58	0.48	0.50	0.52	0.85	0.00	0.64
time (sec)	N/A	0.013	0.009	0.004	1.345	0.430	1.399	0.000	0.180

Problem 850	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	33	32	33	34	56	0	42
normalized size	1	1.00	0.50	0.48	0.50	0.52	0.85	0.00	0.64
time (sec)	N/A	0.013	0.014	0.005	1.369	0.428	1.704	0.000	0.182

Problem 851	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	35	32	33	34	61	0	42
normalized size	1	1.00	0.53	0.48	0.50	0.52	0.92	0.00	0.64
time (sec)	N/A	0.013	0.009	0.006	1.352	0.430	2.029	0.000	0.180

Problem 852	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	63	63	128	62	0	81	-1
normalized size	1	1.00	0.62	0.62	1.25	0.61	0.00	0.79	-0.01
time (sec)	N/A	0.036	0.018	0.006	1.570	0.432	0.000	1.106	0.000

Problem 853	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	52	52	110	51	0	69	-1
normalized size	1	1.00	0.65	0.65	1.38	0.64	0.00	0.86	-0.01
time (sec)	N/A	0.025	0.015	0.008	1.561	0.424	0.000	0.944	0.000

Problem 854	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	40	40	91	39	0	54	-1
normalized size	1	1.00	0.69	0.69	1.57	0.67	0.00	0.93	-0.02
time (sec)	N/A	0.018	0.011	0.007	1.494	0.418	0.000	1.015	0.000

Problem 855	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	28	29	74	27	0	37	-1
normalized size	1	1.00	0.74	0.76	1.95	0.71	0.00	0.97	-0.03
time (sec)	N/A	0.012	0.007	0.005	1.451	0.408	0.000	0.962	0.000

Problem 856	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	21	21	0	20	0	28	-1
normalized size	1	1.00	0.95	0.95	0.00	0.91	0.00	1.27	-0.05
time (sec)	N/A	0.003	0.004	0.004	0.000	0.413	0.000	0.949	0.000

Problem 857	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	26	26	24	64	0	0	-1
normalized size	1	1.00	0.62	0.62	0.57	1.52	0.00	0.00	-0.02
time (sec)	N/A	0.007	0.007	0.008	1.376	0.452	0.000	0.000	0.000

Problem 858	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	32	33	37	31	0	0	-1
normalized size	1	1.00	0.52	0.54	0.61	0.51	0.00	0.00	-0.02
time (sec)	N/A	0.017	0.011	0.011	1.384	0.439	0.000	0.000	0.000

Problem 859	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	53	51	52	44	0	0	-1
normalized size	1	1.00	0.63	0.61	0.62	0.52	0.00	0.00	-0.01
time (sec)	N/A	0.023	0.015	0.010	1.361	0.417	0.000	0.000	0.000

Problem 860	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	107	107	64	63	124	67	0	81	-1
normalized size	1	1.00	0.60	0.59	1.16	0.63	0.00	0.76	-0.01
time (sec)	N/A	0.032	0.013	0.006	1.619	0.433	0.000	0.998	0.000

Problem 861	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	53	52	109	55	0	69	-1
normalized size	1	1.00	0.63	0.62	1.30	0.65	0.00	0.82	-0.01
time (sec)	N/A	0.025	0.011	0.005	1.541	0.413	0.000	1.155	0.000

Problem 862	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	42	40	93	42	0	54	-1
normalized size	1	1.00	0.69	0.66	1.52	0.69	0.00	0.89	-0.02
time (sec)	N/A	0.019	0.005	0.005	1.482	0.414	0.000	1.119	0.000

Problem 863	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	30	29	75	29	0	37	-1
normalized size	1	1.00	0.75	0.72	1.88	0.72	0.00	0.92	-0.02
time (sec)	N/A	0.012	0.004	0.003	1.479	0.439	0.000	0.998	0.000

Problem 864	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	22	21	13	21	0	28	-1
normalized size	1	1.00	0.96	0.91	0.57	0.91	0.00	1.22	-0.04
time (sec)	N/A	0.004	0.003	0.004	1.357	0.456	0.000	1.137	0.000

Problem 865	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	44	44	27	26	24	66	0	0	-1
normalized size	1	1.00	0.61	0.59	0.55	1.50	0.00	0.00	-0.02
time (sec)	N/A	0.007	0.008	0.005	1.380	0.444	0.000	0.000	0.000

Problem 866	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	34	33	37	33	0	0	-1
normalized size	1	1.00	0.53	0.52	0.58	0.52	0.00	0.00	-0.02
time (sec)	N/A	0.016	0.011	0.006	1.356	0.430	0.000	0.000	0.000

Problem 867	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	88	88	53	51	52	47	0	0	-1
normalized size	1	1.00	0.60	0.58	0.59	0.53	0.00	0.00	-0.01
time (sec)	N/A	0.024	0.015	0.005	1.446	0.442	0.000	0.000	0.000

Problem 868	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	112	112	65	62	66	59	0	0	-1
normalized size	1	1.00	0.58	0.55	0.59	0.53	0.00	0.00	-0.01
time (sec)	N/A	0.031	0.026	0.012	1.449	0.420	0.000	0.000	0.000

Problem 869	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	142	142	76	74	146	91	0	116	-1
normalized size	1	1.00	0.54	0.52	1.03	0.64	0.00	0.82	-0.01
time (sec)	N/A	0.045	0.022	0.006	1.584	0.408	0.000	1.184	0.000

Problem 870	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	117	117	65	63	130	77	0	99	-1
normalized size	1	1.00	0.56	0.54	1.11	0.66	0.00	0.85	-0.01
time (sec)	N/A	0.051	0.006	0.006	1.602	0.418	0.000	1.011	0.000

Problem 871	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	54	52	114	63	0	84	-1
normalized size	1	1.00	0.59	0.57	1.24	0.68	0.00	0.91	-0.01
time (sec)	N/A	0.030	0.005	0.004	1.562	0.433	0.000	0.960	0.000

Problem 872	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	42	40	97	48	0	66	-1
normalized size	1	1.00	0.63	0.60	1.45	0.72	0.00	0.99	-0.01
time (sec)	N/A	0.020	0.005	0.006	1.496	0.434	0.000	1.134	0.000

Problem 873	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	44	44	30	29	77	33	0	46	-1
normalized size	1	1.00	0.68	0.66	1.75	0.75	0.00	1.05	-0.02
time (sec)	N/A	0.012	0.004	0.004	1.512	0.408	0.000	1.043	0.000

Problem 874	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	25	25	22	21	13	23	0	34	-1
normalized size	1	1.00	0.88	0.84	0.52	0.92	0.00	1.36	-0.04
time (sec)	N/A	0.004	0.004	0.003	1.359	0.418	0.000	1.102	0.000

Problem 875	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	28	27	24	70	0	0	-1
normalized size	1	1.00	0.58	0.56	0.50	1.46	0.00	0.00	-0.02
time (sec)	N/A	0.008	0.009	0.006	1.352	0.449	0.000	0.000	0.000

Problem 876	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	34	33	37	37	0	0	-1
normalized size	1	1.00	0.49	0.47	0.53	0.53	0.00	0.00	-0.01
time (sec)	N/A	0.017	0.012	0.006	1.394	0.431	0.000	0.000	0.000

Problem 877	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	83	83	51	50	142	54	0	81	-1
normalized size	1	1.00	0.61	0.60	1.71	0.65	0.00	0.98	-0.01
time (sec)	N/A	0.024	0.011	0.006	1.519	0.423	0.000	1.153	0.000

Problem 878	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	39	38	100	42	0	67	-1
normalized size	1	1.00	0.64	0.62	1.64	0.69	0.00	1.10	-0.02
time (sec)	N/A	0.017	0.012	0.004	1.494	0.416	0.000	1.087	0.000

Problem 879	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	27	27	64	30	0	51	-1
normalized size	1	1.00	0.69	0.69	1.64	0.77	0.00	1.31	-0.03
time (sec)	N/A	0.012	0.007	0.003	1.472	0.475	0.000	1.187	0.000

Problem 880	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	19	46	23	0	36	-1
normalized size	1	1.00	1.00	0.95	2.30	1.15	0.00	1.80	-0.05
time (sec)	N/A	0.004	0.002	0.005	1.459	0.434	0.000	0.901	0.000

Problem 881	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	25	24	35	70	0	59	-1
normalized size	1	1.00	0.66	0.63	0.92	1.84	0.00	1.55	-0.03
time (sec)	N/A	0.007	0.004	0.005	1.461	0.440	0.000	0.966	0.000

Problem 882	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	36	30	37	34	0	91	-1
normalized size	1	1.00	0.67	0.56	0.69	0.63	0.00	1.69	-0.02
time (sec)	N/A	0.016	0.011	0.006	1.370	0.430	0.000	1.194	0.000

Problem 883	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	77	77	52	51	55	47	0	0	-1
normalized size	1	1.00	0.68	0.66	0.71	0.61	0.00	0.00	-0.01
time (sec)	N/A	0.029	0.012	0.005	1.375	0.448	0.000	0.000	0.000

Problem 884	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	63	62	69	58	0	0	-1
normalized size	1	1.00	0.63	0.62	0.69	0.58	0.00	0.00	-0.01
time (sec)	N/A	0.026	0.012	0.005	1.396	0.432	0.000	0.000	0.000

Problem 885	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	53	52	162	54	0	86	-1
normalized size	1	1.00	0.56	0.55	1.71	0.57	0.00	0.91	-0.01
time (sec)	N/A	0.027	0.011	0.006	1.790	0.422	0.000	1.181	0.000

Problem 886	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	41	40	140	42	0	71	-1
normalized size	1	1.00	0.59	0.57	2.00	0.60	0.00	1.01	-0.01
time (sec)	N/A	0.020	0.008	0.005	1.660	0.423	0.000	0.958	0.000

Problem 887	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	29	29	116	30	0	55	-1
normalized size	1	1.00	0.64	0.64	2.58	0.67	0.00	1.22	-0.02
time (sec)	N/A	0.013	0.007	0.004	1.602	0.412	0.000	1.094	0.000

Problem 888	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	22	21	74	23	0	36	-1
normalized size	1	1.00	0.96	0.91	3.22	1.00	0.00	1.57	-0.04
time (sec)	N/A	0.004	0.004	0.002	1.604	0.425	0.000	0.970	0.000

Problem 889	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	44	44	27	26	35	70	0	63	-1
normalized size	1	1.00	0.61	0.59	0.80	1.59	0.00	1.43	-0.02
time (sec)	N/A	0.008	0.007	0.005	1.430	0.428	0.000	1.047	0.000

Problem 890	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	35	33	51	34	0	91	-1
normalized size	1	1.00	0.56	0.52	0.81	0.54	0.00	1.44	-0.02
time (sec)	N/A	0.017	0.006	0.006	1.481	0.434	0.000	1.080	0.000

Problem 891	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	51	49	65	47	0	0	-1
normalized size	1	1.00	0.57	0.55	0.73	0.53	0.00	0.00	-0.01
time (sec)	N/A	0.022	0.007	0.006	1.538	0.439	0.000	0.000	0.000

Problem 892	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	66	59	69	58	0	0	-1
normalized size	1	1.00	0.57	0.51	0.60	0.50	0.00	0.00	-0.01
time (sec)	N/A	0.028	0.015	0.006	1.359	0.422	0.000	0.000	0.000

Problem 893	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	106	106	81	88	135	83	0	96	-1
normalized size	1	1.00	0.76	0.83	1.27	0.78	0.00	0.91	-0.01
time (sec)	N/A	0.039	0.028	0.012	1.516	0.425	0.000	0.997	0.000

Problem 894	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	85	85	70	76	118	72	0	80	-1
normalized size	1	1.00	0.82	0.89	1.39	0.85	0.00	0.94	-0.01
time (sec)	N/A	0.032	0.021	0.012	1.545	0.423	0.000	1.057	0.000

Problem 895	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	53	62	96	57	0	58	-1
normalized size	1	1.00	0.82	0.95	1.48	0.88	0.00	0.89	-0.02
time (sec)	N/A	0.022	0.020	0.010	1.515	0.441	0.000	0.920	0.000

Problem 896	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	36	41	79	38	0	46	-1
normalized size	1	1.00	0.77	0.87	1.68	0.81	0.00	0.98	-0.02
time (sec)	N/A	0.016	0.012	0.008	1.467	0.458	0.000	1.061	0.000

Problem 897	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	24	24	23	23	16	23	39	29	22
normalized size	1	1.00	0.96	0.96	0.67	0.96	1.62	1.21	0.92
time (sec)	N/A	0.004	0.007	0.004	1.361	0.492	0.816	1.016	0.165

Problem 898	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	45	52	38	42	0	0	-1
normalized size	1	1.00	0.69	0.80	0.58	0.65	0.00	0.00	-0.02
time (sec)	N/A	0.018	0.017	0.011	1.318	0.429	0.000	0.000	0.000

Problem 899	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	87	87	57	74	58	60	0	0	-1
normalized size	1	1.00	0.66	0.85	0.67	0.69	0.00	0.00	-0.01
time (sec)	N/A	0.027	0.030	0.013	1.397	0.437	0.000	0.000	0.000

Problem 900	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	112	112	82	95	79	77	0	0	-1
normalized size	1	1.00	0.73	0.85	0.71	0.69	0.00	0.00	-0.01
time (sec)	N/A	0.036	0.024	0.016	1.420	0.503	0.000	0.000	0.000

Problem 901	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	111	111	82	88	132	91	0	96	-1
normalized size	1	1.00	0.74	0.79	1.19	0.82	0.00	0.86	-0.01
time (sec)	N/A	0.037	0.020	0.007	1.625	0.419	0.000	1.174	0.000

Problem 902	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	71	76	115	79	0	80	-1
normalized size	1	1.00	0.80	0.85	1.29	0.89	0.00	0.90	-0.01
time (sec)	N/A	0.029	0.017	0.005	1.553	0.452	0.000	0.947	0.000

Problem 903	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	55	62	98	63	0	58	-1
normalized size	1	1.00	0.81	0.91	1.44	0.93	0.00	0.85	-0.01
time (sec)	N/A	0.020	0.007	0.006	1.424	0.440	0.000	0.956	0.000

Problem 904	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	38	41	80	43	0	46	-1
normalized size	1	1.00	0.78	0.84	1.63	0.88	0.00	0.94	-0.02
time (sec)	N/A	0.015	0.009	0.004	1.480	0.420	0.000	0.961	0.000

Problem 905	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	25	25	24	23	16	24	44	29	24
normalized size	1	1.00	0.96	0.92	0.64	0.96	1.76	1.16	0.96
time (sec)	N/A	0.004	0.006	0.003	1.335	0.446	2.226	1.143	0.148

Problem 906	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	46	52	38	47	0	0	-1
normalized size	1	1.00	0.68	0.76	0.56	0.69	0.00	0.00	-0.01
time (sec)	N/A	0.018	0.017	0.006	1.397	0.426	0.000	0.000	0.000

Problem 907	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	91	91	59	74	58	65	0	0	-1
normalized size	1	1.00	0.65	0.81	0.64	0.71	0.00	0.00	-0.01
time (sec)	N/A	0.024	0.022	0.007	1.435	0.449	0.000	0.000	0.000

Problem 908	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	117	117	82	95	79	82	0	0	-1
normalized size	1	1.00	0.70	0.81	0.68	0.70	0.00	0.00	-0.01
time (sec)	N/A	0.032	0.022	0.006	1.332	0.444	0.000	0.000	0.000

Problem 909	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	107	107	80	86	168	85	0	155	-1
normalized size	1	1.00	0.75	0.80	1.57	0.79	0.00	1.45	-0.01
time (sec)	N/A	0.033	0.015	0.006	1.558	0.421	0.000	1.131	0.000

Problem 910	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	69	74	129	74	0	143	-1
normalized size	1	1.00	0.80	0.86	1.50	0.86	0.00	1.66	-0.01
time (sec)	N/A	0.026	0.012	0.005	1.555	0.433	0.000	1.041	0.000

Problem 911	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	52	60	88	59	0	127	-1
normalized size	1	1.00	0.81	0.94	1.38	0.92	0.00	1.98	-0.02
time (sec)	N/A	0.020	0.012	0.006	1.450	0.413	0.000	1.133	0.000

Problem 912	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	35	39	68	40	0	89	-1
normalized size	1	1.00	0.81	0.91	1.58	0.93	0.00	2.07	-0.02
time (sec)	N/A	0.013	0.009	0.004	1.411	0.412	0.000	1.149	0.000

Problem 913	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	22	21	21	25	85	38	25
normalized size	1	1.00	1.00	0.95	0.95	1.14	3.86	1.73	1.14
time (sec)	N/A	0.003	0.003	0.003	1.453	0.443	1.169	1.159	0.156

Problem 914	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	44	50	61	44	0	86	-1
normalized size	1	1.00	0.75	0.85	1.03	0.75	0.00	1.46	-0.02
time (sec)	N/A	0.016	0.005	0.006	1.460	0.438	0.000	1.084	0.000

Problem 915	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	60	71	57	62	0	126	-1
normalized size	1	1.00	0.77	0.91	0.73	0.79	0.00	1.62	-0.01
time (sec)	N/A	0.022	0.026	0.006	1.432	0.434	0.000	1.142	0.000

Problem 916	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	103	103	81	95	76	79	0	152	-1
normalized size	1	1.00	0.79	0.92	0.74	0.77	0.00	1.48	-0.01
time (sec)	N/A	0.032	0.018	0.006	1.407	0.418	0.000	1.222	0.000

Problem 917	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	73	73	54	62	149	63	0	127	-1
normalized size	1	1.00	0.74	0.85	2.04	0.86	0.00	1.74	-0.01
time (sec)	N/A	0.021	0.015	0.005	1.611	0.431	0.000	1.264	0.000

Problem 918	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	37	41	108	44	0	89	-1
normalized size	1	1.00	0.76	0.84	2.20	0.90	0.00	1.82	-0.02
time (sec)	N/A	0.014	0.011	0.003	1.557	0.421	0.000	1.025	0.000

Problem 919	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	25	25	24	23	47	29	90	38	25
normalized size	1	1.00	0.96	0.92	1.88	1.16	3.60	1.52	1.00
time (sec)	N/A	0.004	0.006	0.003	1.483	0.424	1.940	1.164	0.167

Problem 920	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	46	52	82	48	0	83	-1
normalized size	1	1.00	0.68	0.76	1.21	0.71	0.00	1.22	-0.01
time (sec)	N/A	0.017	0.014	0.006	1.520	0.435	0.000	1.057	0.000

Problem 921	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	90	90	59	74	79	66	0	137	-1
normalized size	1	1.00	0.66	0.82	0.88	0.73	0.00	1.52	-0.01
time (sec)	N/A	0.024	0.011	0.005	1.412	0.442	0.000	1.109	0.000

Problem 922	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	118	118	80	93	98	83	0	152	-1
normalized size	1	1.00	0.68	0.79	0.83	0.70	0.00	1.29	-0.01
time (sec)	N/A	0.032	0.009	0.007	1.463	0.436	0.000	1.027	0.000

Problem 923	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	131	131	97	136	116	153	0	300	214
normalized size	1	1.00	0.74	1.04	0.89	1.17	0.00	2.29	1.63
time (sec)	N/A	0.037	0.068	0.007	1.464	0.461	0.000	1.111	0.348

Problem 924	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	68	83	80	106	0	200	142
normalized size	1	1.00	0.71	0.86	0.83	1.10	0.00	2.08	1.48
time (sec)	N/A	0.029	0.047	0.006	1.413	0.461	0.000	0.961	0.252

Problem 925	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	44	46	51	63	0	119	85
normalized size	1	1.00	0.70	0.73	0.81	1.00	0.00	1.89	1.35
time (sec)	N/A	0.017	0.030	0.003	1.450	0.450	0.000	1.144	0.222

Problem 926	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	29	29	28	30	0	42	31
normalized size	1	1.00	0.97	0.97	0.93	1.00	0.00	1.40	1.03
time (sec)	N/A	0.006	0.014	0.002	1.395	0.454	0.000	1.011	0.228

Problem 927	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	46	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.011	0.011	0.046	0.000	0.444	0.000	0.000	0.000

Problem 928	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	47	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.011	0.015	0.043	0.000	0.446	0.000	0.000	0.000

Problem 929	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	50	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.012	0.016	0.043	0.000	0.451	0.000	0.000	0.000

Problem 930	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	169	169	132	199	157	233	0	426	307
normalized size	1	1.00	0.78	1.18	0.93	1.38	0.00	2.52	1.82
time (sec)	N/A	0.055	0.077	0.009	1.437	0.552	0.000	1.196	0.414

Problem 931	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	135	135	98	136	116	164	0	300	219
normalized size	1	1.00	0.73	1.01	0.86	1.21	0.00	2.22	1.62
time (sec)	N/A	0.039	0.055	0.007	1.441	0.444	0.000	1.141	0.320

Problem 932	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	99	99	70	83	80	113	0	0	146
normalized size	1	1.00	0.71	0.84	0.81	1.14	0.00	0.00	1.47
time (sec)	N/A	0.028	0.031	0.006	1.426	0.465	0.000	0.000	0.261

Problem 933	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	46	46	51	68	0	119	88
normalized size	1	1.00	0.71	0.71	0.78	1.05	0.00	1.83	1.35
time (sec)	N/A	0.018	0.008	0.004	1.426	0.440	0.000	0.910	0.231

Problem 934	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	30	29	28	33	0	42	45
normalized size	1	1.00	0.97	0.94	0.90	1.06	0.00	1.35	1.45
time (sec)	N/A	0.006	0.015	0.001	1.423	0.445	0.000	1.087	0.229

Problem 935	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	47	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.011	0.010	0.044	0.000	0.447	0.000	0.000	0.000

Problem 936	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	47	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.011	0.011	0.044	0.000	0.477	0.000	0.000	0.000

Problem 937	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	50	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.013	0.013	0.045	0.000	0.451	0.000	0.000	0.000

Problem 938	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	217	217	172	280	203	352	0	640	424
normalized size	1	1.00	0.79	1.29	0.94	1.62	0.00	2.95	1.95
time (sec)	N/A	0.074	0.108	0.009	1.529	0.465	0.000	1.063	0.496

Problem 939	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	179	179	133	199	157	265	0	0	319
normalized size	1	1.00	0.74	1.11	0.88	1.48	0.00	0.00	1.78
time (sec)	N/A	0.051	0.022	0.007	1.452	0.471	0.000	0.000	0.379

Problem 940	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	143	143	99	136	116	186	0	0	229
normalized size	1	1.00	0.69	0.95	0.81	1.30	0.00	0.00	1.60
time (sec)	N/A	0.042	0.018	0.007	1.454	0.451	0.000	0.000	0.317

Problem 941	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	105	105	70	83	80	127	0	0	154
normalized size	1	1.00	0.67	0.79	0.76	1.21	0.00	0.00	1.47
time (sec)	N/A	0.029	0.045	0.006	1.361	0.461	0.000	0.000	0.265

Problem 942	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	46	46	51	76	0	0	94
normalized size	1	1.00	0.67	0.67	0.74	1.10	0.00	0.00	1.36
time (sec)	N/A	0.019	0.009	0.002	1.453	0.470	0.000	0.000	0.239

Problem 943	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	31	29	28	37	0	0	49
normalized size	1	1.00	0.94	0.88	0.85	1.12	0.00	0.00	1.48
time (sec)	N/A	0.006	0.017	0.002	1.388	0.477	0.000	0.000	0.231

Problem 944	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	47	0	0	0	0	0	-1
normalized size	1	1.00	0.94	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.012	0.011	0.047	0.000	0.440	0.000	0.000	0.000

Problem 945	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	47	0	0	0	0	0	-1
normalized size	1	1.00	0.94	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.012	0.012	0.046	0.000	0.438	0.000	0.000	0.000

Problem 946	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	123	123	96	134	104	158	0	0	186
normalized size	1	1.00	0.78	1.09	0.85	1.28	0.00	0.00	1.51
time (sec)	N/A	0.037	0.040	0.006	1.449	0.467	0.000	0.000	0.369

Problem 947	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	90	90	67	81	83	110	0	0	121
normalized size	1	1.00	0.74	0.90	0.92	1.22	0.00	0.00	1.34
time (sec)	N/A	0.026	0.029	0.004	1.464	0.430	0.000	0.000	0.295

Problem 948	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	43	44	45	66	0	0	71
normalized size	1	1.00	0.73	0.75	0.76	1.12	0.00	0.00	1.20
time (sec)	N/A	0.016	0.021	0.003	1.487	0.434	0.000	0.000	0.277

Problem 949	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	28	27	31	33	0	0	36
normalized size	1	1.00	1.00	0.96	1.11	1.18	0.00	0.00	1.29
time (sec)	N/A	0.005	0.011	0.002	1.437	0.437	0.000	0.000	0.220

Problem 950	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	45	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.010	0.009	0.044	0.000	0.479	0.000	0.000	0.000

Problem 951	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	48	0	0	0	0	0	-1
normalized size	1	1.00	1.07	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.010	0.012	0.045	0.000	0.447	0.000	0.000	0.000

Problem 952	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	51	0	0	0	0	0	-1
normalized size	1	1.00	1.06	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.012	0.013	0.042	0.000	0.441	0.000	0.000	0.000

Problem 953	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	135	135	98	136	104	168	0	0	201
normalized size	1	1.00	0.73	1.01	0.77	1.24	0.00	0.00	1.49
time (sec)	N/A	0.044	0.041	0.007	1.464	0.425	0.000	0.000	0.404

Problem 954	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	99	99	69	83	83	118	0	0	133
normalized size	1	1.00	0.70	0.84	0.84	1.19	0.00	0.00	1.34
time (sec)	N/A	0.031	0.034	0.005	1.455	0.435	0.000	0.000	0.313

Problem 955	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	45	46	45	72	0	0	80
normalized size	1	1.00	0.69	0.71	0.69	1.11	0.00	0.00	1.23
time (sec)	N/A	0.019	0.023	0.003	1.467	0.428	0.000	0.000	0.289

Problem 956	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	30	29	31	37	0	0	42
normalized size	1	1.00	0.97	0.94	1.00	1.19	0.00	0.00	1.35
time (sec)	N/A	0.007	0.014	0.002	1.441	0.463	0.000	0.000	0.229

Problem 957	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	47	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.012	0.010	0.046	0.000	0.448	0.000	0.000	0.000

Problem 958	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	47	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.012	0.010	0.043	0.000	0.443	0.000	0.000	0.000

Problem 959	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	50	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.014	0.011	0.048	0.000	0.435	0.000	0.000	0.000

Problem 960	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	50	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.014	0.014	0.045	0.000	0.469	0.000	0.000	0.000

Problem 961	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	135	135	99	136	104	168	0	0	201
normalized size	1	1.00	0.73	1.01	0.77	1.24	0.00	0.00	1.49
time (sec)	N/A	0.046	0.037	0.006	1.472	0.442	0.000	0.000	0.410

Problem 962	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	99	99	70	83	83	118	0	0	133
normalized size	1	1.00	0.71	0.84	0.84	1.19	0.00	0.00	1.34
time (sec)	N/A	0.031	0.030	0.006	1.451	0.454	0.000	0.000	0.355

Problem 963	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	46	46	45	72	0	0	80
normalized size	1	1.00	0.71	0.71	0.69	1.11	0.00	0.00	1.23
time (sec)	N/A	0.020	0.020	0.003	1.407	0.454	0.000	0.000	0.285

Problem 964	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	31	29	31	37	0	0	42
normalized size	1	1.00	1.00	0.94	1.00	1.19	0.00	0.00	1.35
time (sec)	N/A	0.007	0.012	0.003	1.453	0.436	0.000	0.000	0.230

Problem 965	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	47	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.013	0.010	0.045	0.000	0.453	0.000	0.000	0.000

Problem 966	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	47	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.013	0.012	0.046	0.000	0.466	0.000	0.000	0.000

Problem 967	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	50	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.015	0.013	0.045	0.000	0.461	0.000	0.000	0.000

Problem 968	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	49	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.013	0.011	0.043	0.000	0.466	0.000	0.000	0.000

Problem 969	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	38	40	39	58	0	0	44
normalized size	1	1.00	0.58	0.62	0.60	0.89	0.00	0.00	0.68
time (sec)	N/A	0.030	0.027	0.003	1.518	0.492	0.000	0.000	0.266

Problem 970	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	38	40	39	50	0	0	42
normalized size	1	1.00	0.62	0.66	0.64	0.82	0.00	0.00	0.69
time (sec)	N/A	0.029	0.024	0.002	1.554	0.431	0.000	0.000	0.237

Problem 971	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	38	40	39	44	0	0	39
normalized size	1	1.00	0.64	0.68	0.66	0.75	0.00	0.00	0.66
time (sec)	N/A	0.027	0.020	0.003	1.520	0.443	0.000	0.000	0.212

Problem 972	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	33	32	32	36	0	0	30
normalized size	1	1.00	0.69	0.67	0.67	0.75	0.00	0.00	0.62
time (sec)	N/A	0.019	0.015	0.001	1.482	0.441	0.000	0.000	0.211

Problem 973	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	38	40	39	53	0	0	48
normalized size	1	1.00	0.58	0.62	0.60	0.82	0.00	0.00	0.74
time (sec)	N/A	0.036	0.025	0.003	1.506	0.458	0.000	0.000	0.259

Problem 974	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	38	40	39	53	0	0	47
normalized size	1	1.00	0.57	0.60	0.58	0.79	0.00	0.00	0.70
time (sec)	N/A	0.037	0.027	0.002	1.517	0.637	0.000	0.000	0.275

Problem 975	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	103	103	48	95	64	123	0	0	127
normalized size	1	1.00	0.47	0.92	0.62	1.19	0.00	0.00	1.23
time (sec)	N/A	0.049	0.051	0.004	1.600	0.746	0.000	0.000	0.312

Problem 976	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	97	97	48	95	64	105	0	0	121
normalized size	1	1.00	0.49	0.98	0.66	1.08	0.00	0.00	1.25
time (sec)	N/A	0.045	0.045	0.005	1.551	0.433	0.000	0.000	0.279

Problem 977	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	94	94	72	95	64	94	0	0	116
normalized size	1	1.00	0.77	1.01	0.68	1.00	0.00	0.00	1.23
time (sec)	N/A	0.041	0.043	0.004	1.525	0.466	0.000	0.000	0.264

Problem 978	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	62	79	57	85	0	0	62
normalized size	1	1.00	0.77	0.98	0.70	1.05	0.00	0.00	0.77
time (sec)	N/A	0.036	0.034	0.005	1.635	0.450	0.000	0.000	0.258

Problem 979	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	62	83	59	92	0	0	66
normalized size	1	1.00	0.67	0.89	0.63	0.99	0.00	0.00	0.71
time (sec)	N/A	0.045	0.039	0.006	1.583	0.512	0.000	0.000	0.319

Problem 980	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	105	105	72	95	64	106	0	0	82
normalized size	1	1.00	0.69	0.90	0.61	1.01	0.00	0.00	0.78
time (sec)	N/A	0.054	0.046	0.006	1.569	0.475	0.000	0.000	0.339

Problem 981	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	57	0	0	0	0	0	-1
normalized size	1	1.00	0.85	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.029	0.017	0.045	0.000	0.513	0.000	0.000	0.000

Problem 982	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	57	0	0	0	0	0	-1
normalized size	1	1.00	0.88	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.029	0.014	0.047	0.000	0.472	0.000	0.000	0.000

Problem 983	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	57	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.028	0.011	0.046	0.000	0.497	0.000	0.000	0.000

Problem 984	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	53	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.021	0.010	0.046	0.000	0.473	0.000	0.000	0.000

Problem 985	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	57	0	0	0	0	0	-1
normalized size	1	1.00	0.84	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.032	0.014	0.046	0.000	0.470	0.000	0.000	0.000

Problem 986	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	57	0	0	0	0	0	-1
normalized size	1	1.00	0.84	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.031	0.016	0.046	0.000	0.472	0.000	0.000	0.000

Problem 987	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	32	32	0	40	0	74	33
normalized size	1	1.00	0.97	0.97	0.00	1.21	0.00	2.24	1.00
time (sec)	N/A	0.010	0.017	0.004	0.000	0.451	0.000	1.261	0.266

Problem 988	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	34	33	0	40	0	0	34
normalized size	1	1.00	1.06	1.03	0.00	1.25	0.00	0.00	1.06
time (sec)	N/A	0.009	0.019	0.003	0.000	0.467	0.000	0.000	0.235

Problem 989	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	32	32	0	38	0	72	33
normalized size	1	1.00	0.97	0.97	0.00	1.15	0.00	2.18	1.00
time (sec)	N/A	0.010	0.015	0.004	0.000	0.465	0.000	1.070	0.217

Problem 990	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	28	31	0	36	0	0	32
normalized size	1	1.00	0.93	1.03	0.00	1.20	0.00	0.00	1.07
time (sec)	N/A	0.008	0.015	0.004	0.000	0.459	0.000	0.000	0.200

Problem 991	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	26	25	27	31	264	0	26
normalized size	1	1.00	1.00	0.96	1.04	1.19	10.15	0.00	1.00
time (sec)	N/A	0.006	0.007	0.003	1.446	0.466	59.694	0.000	0.262

Problem 992	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	32	38	0	37	0	0	32
normalized size	1	1.00	0.97	1.15	0.00	1.12	0.00	0.00	0.97
time (sec)	N/A	0.011	0.010	0.003	0.000	0.457	0.000	0.000	0.240

Problem 993	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	32	32	0	37	0	0	50
normalized size	1	1.00	0.91	0.91	0.00	1.06	0.00	0.00	1.43
time (sec)	N/A	0.011	0.010	0.003	0.000	0.453	0.000	0.000	0.248

Problem 994	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	32	33	0	37	0	0	51
normalized size	1	1.00	0.97	1.00	0.00	1.12	0.00	0.00	1.55
time (sec)	N/A	0.010	0.010	0.002	0.000	0.463	0.000	0.000	0.251

Problem 995	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	38	39	0	49	0	0	50
normalized size	1	1.00	1.00	1.03	0.00	1.29	0.00	0.00	1.32
time (sec)	N/A	0.010	0.029	0.003	0.000	0.493	0.000	0.000	0.338

Problem 996	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	39	40	0	57	0	0	39
normalized size	1	1.00	1.00	1.03	0.00	1.46	0.00	0.00	1.00
time (sec)	N/A	0.010	0.015	0.003	0.000	0.468	0.000	0.000	0.265

Problem 997	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	63	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.019	0.011	0.117	0.000	0.481	0.000	0.000	0.000

Problem 998	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	64	64	0	0	0	0	0	-1
normalized size	1	0.94	0.94	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.022	0.009	0.185	0.000	0.469	0.000	0.000	0.000

Problem 999	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	16	31	31	34	31	27
normalized size	1	1.00	1.00	0.94	1.82	1.82	2.00	1.82	1.59
time (sec)	N/A	0.004	0.002	0.002	1.367	0.404	0.121	1.086	0.050

Problem 1000	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	19	18	20	20	20	20	16
normalized size	1	1.00	0.83	0.78	0.87	0.87	0.87	0.87	0.70
time (sec)	N/A	0.006	0.001	0.001	1.239	0.469	0.119	1.194	0.034

Problem 1001	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	8	8	8	9	8	8	7	8	8
normalized size	1	1.00	1.00	1.12	1.00	1.00	0.88	1.00	1.00
time (sec)	N/A	0.002	0.000	0.001	1.270	0.446	0.107	1.004	0.010

Problem 1002	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	14	13	13	19	14	13
normalized size	1	1.00	1.00	1.08	1.00	1.00	1.46	1.08	1.00
time (sec)	N/A	0.003	0.002	0.001	1.310	0.420	0.112	1.073	0.048

Problem 1003	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	16	19	19	19	15	15
normalized size	1	1.00	1.00	1.07	1.27	1.27	1.27	1.00	1.00
time (sec)	N/A	0.003	0.004	0.000	1.338	0.440	0.177	0.988	0.037

Problem 1004	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	16	47	47	53	15	49
normalized size	1	1.00	1.00	0.94	2.76	2.76	3.12	0.88	2.88
time (sec)	N/A	0.003	0.005	0.001	1.307	0.413	0.288	1.187	0.153

Problem 1005	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	16	61	61	68	15	63
normalized size	1	1.00	1.00	0.94	3.59	3.59	4.00	0.88	3.71
time (sec)	N/A	0.003	0.006	0.002	1.354	0.432	0.363	0.905	0.064

Problem 1006	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	16	75	75	83	15	77
normalized size	1	1.00	1.00	0.94	4.41	4.41	4.88	0.88	4.53
time (sec)	N/A	0.003	0.006	0.002	1.332	0.426	0.422	0.962	0.054

Problem 1007	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	16	35	35	34	35	27
normalized size	1	1.00	1.00	0.94	2.06	2.06	2.00	2.06	1.59
time (sec)	N/A	0.004	0.003	0.002	1.372	0.426	0.130	1.007	0.156

Problem 1008	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	19	18	21	21	20	21	16
normalized size	1	1.00	0.83	0.78	0.91	0.91	0.87	0.91	0.70
time (sec)	N/A	0.005	0.001	0.001	1.315	0.409	0.118	1.037	0.030

Problem 1009	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	8	8	8	9	8	8	7	8	8
normalized size	1	1.00	1.00	1.12	1.00	1.00	0.88	1.00	1.00
time (sec)	N/A	0.001	0.000	0.000	1.327	0.402	0.104	1.050	0.009

Problem 1010	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	14	13	13	17	14	13
normalized size	1	1.00	1.00	1.08	1.00	1.00	1.31	1.08	1.00
time (sec)	N/A	0.003	0.002	0.001	1.367	0.409	0.104	0.890	0.142

Problem 1011	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	14	16	16	12	13	13
normalized size	1	1.00	1.00	1.08	1.23	1.23	0.92	1.00	1.00
time (sec)	N/A	0.003	0.004	0.002	1.381	0.420	0.154	1.001	0.040

Problem 1012	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	36	36	44	12	38
normalized size	1	1.00	1.00	0.93	2.57	2.57	3.14	0.86	2.71
time (sec)	N/A	0.003	0.005	0.001	1.344	0.411	0.280	1.136	0.047

Problem 1013	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	14	59	59	68	20	61
normalized size	1	1.00	1.00	0.93	3.93	3.93	4.53	1.33	4.07
time (sec)	N/A	0.003	0.006	0.001	1.346	0.409	0.362	0.978	0.050

Problem 1014	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	16	75	75	83	15	77
normalized size	1	1.00	1.00	0.94	4.41	4.41	4.88	0.88	4.53
time (sec)	N/A	0.003	0.006	0.000	1.360	0.448	0.419	0.922	0.173

Problem 1015	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	24	24	25	27	649	80	212	141	107
normalized size	1	1.00	1.04	1.12	27.04	3.33	8.83	5.88	4.46
time (sec)	N/A	0.009	0.020	0.002	1.809	0.453	2.293	1.132	0.326

Problem 1016	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	114	113	113	124	113	113
normalized size	1	1.00	1.00	6.71	6.65	6.65	7.29	6.65	6.65
time (sec)	N/A	0.004	0.002	0.001	1.313	0.373	0.099	0.957	0.051

Problem 1017	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	100	99	99	110	99	99
normalized size	1	1.00	1.00	5.88	5.82	5.82	6.47	5.82	5.82
time (sec)	N/A	0.004	0.002	0.003	1.359	0.369	0.095	0.986	0.041

Problem 1018	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	72	71	71	78	71	71
normalized size	1	1.00	1.00	4.80	4.73	4.73	5.20	4.73	4.73
time (sec)	N/A	0.003	0.002	0.002	1.353	0.402	0.084	1.093	0.030

Problem 1019	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	16	48	48	51	48	57
normalized size	1	1.00	1.00	0.94	2.82	2.82	3.00	2.82	3.35
time (sec)	N/A	0.004	0.002	0.000	1.351	0.406	0.102	0.893	0.025

Problem 1020	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	16	37	37	46	18	43
normalized size	1	1.00	1.00	0.94	2.18	2.18	2.71	1.06	2.53
time (sec)	N/A	0.004	0.001	0.002	1.309	0.406	0.107	0.978	0.048

Problem 1021	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	16	26	26	29	26	24
normalized size	1	1.00	1.00	0.94	1.53	1.53	1.71	1.53	1.41
time (sec)	N/A	0.004	0.001	0.000	1.305	0.409	0.109	1.002	0.036

Problem 1022	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	16	15	15	15	15	15	13
normalized size	1	1.00	0.89	0.83	0.83	0.83	0.83	0.83	0.72
time (sec)	N/A	0.005	0.001	0.001	1.380	0.406	0.109	1.211	0.024

Problem 1023	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	5	5	5	6	5	5	3	15	5
normalized size	1	1.00	1.00	1.20	1.00	1.00	0.60	3.00	1.00
time (sec)	N/A	0.001	0.000	0.002	1.399	0.412	0.107	1.111	0.008

Problem 1024	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	14	13	13	17	14	13
normalized size	1	1.00	1.00	1.08	1.00	1.00	1.31	1.08	1.00
time (sec)	N/A	0.004	0.002	0.002	1.311	0.421	0.123	0.955	0.040

Problem 1025	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	16	19	19	17	15	19
normalized size	1	1.00	1.00	1.07	1.27	1.27	1.13	1.00	1.27
time (sec)	N/A	0.004	0.002	0.000	1.328	0.441	0.200	1.090	0.046

Problem 1026	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	16	33	33	36	15	35
normalized size	1	1.00	1.00	0.94	1.94	1.94	2.12	0.88	2.06
time (sec)	N/A	0.004	0.004	0.001	1.332	0.424	0.260	1.047	0.146

Problem 1027	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	C	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	28	23	6	1	53	11	35
normalized size	1	1.00	1.00	0.82	0.21	0.04	1.89	0.39	1.25
time (sec)	N/A	0.003	0.006	0.003	2.992	0.454	1.461	1.008	0.222

Problem 1028	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	40	45	44	44	44	44	44
normalized size	1	1.00	1.05	1.18	1.16	1.16	1.16	1.16	1.16
time (sec)	N/A	0.012	0.003	0.002	1.228	0.402	0.080	0.998	0.160

Problem 1029	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	42	45	44	44	46	44	44
normalized size	1	1.00	1.11	1.18	1.16	1.16	1.21	1.16	1.16
time (sec)	N/A	0.017	0.002	0.002	1.313	0.382	0.074	1.037	0.048

Problem 1030	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	17	16	16	15	16	18
normalized size	1	1.00	1.00	0.94	0.89	0.89	0.83	0.89	1.00
time (sec)	N/A	0.004	0.001	0.001	1.351	0.384	0.063	1.010	0.023

Problem 1031	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	12	12	12	11	10	10	8	10	10
normalized size	1	1.00	1.00	0.92	0.83	0.83	0.67	0.83	0.83
time (sec)	N/A	0.002	0.000	0.000	1.336	0.377	0.058	0.859	0.017

Problem 1032	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	23	25	24	23	17	25	23
normalized size	1	1.00	1.00	1.09	1.04	1.00	0.74	1.09	1.00
time (sec)	N/A	0.012	0.005	0.003	1.308	0.410	0.140	0.924	0.046

Problem 1033	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	28	35	37	39	29	81	37
normalized size	1	1.00	0.88	1.09	1.16	1.22	0.91	2.53	1.16
time (sec)	N/A	0.017	0.017	0.006	1.308	0.413	0.187	1.114	0.052

Problem 1034	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	33	30	30	27	14	13
normalized size	1	1.00	1.00	2.54	2.31	2.31	2.08	1.08	1.00
time (sec)	N/A	0.002	0.008	0.005	1.310	0.412	0.241	0.892	0.148

Problem 1035	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	25	35	54	54	56	23	54
normalized size	1	1.00	0.66	0.92	1.42	1.42	1.47	0.61	1.42
time (sec)	N/A	0.019	0.011	0.007	1.337	0.472	0.307	0.979	0.049

Problem 1036	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	24	35	67	67	73	40	67
normalized size	1	1.00	0.63	0.92	1.76	1.76	1.92	1.05	1.76
time (sec)	N/A	0.019	0.010	0.004	1.349	0.415	0.392	0.953	0.167

Problem 1037	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	27	35	84	84	88	25	82
normalized size	1	1.00	0.71	0.92	2.21	2.21	2.32	0.66	2.16
time (sec)	N/A	0.019	0.013	0.004	1.312	0.450	0.463	1.035	0.075

Problem 1038	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	68	73	72	72	78	72	72
normalized size	1	1.00	1.19	1.28	1.26	1.26	1.37	1.26	1.26
time (sec)	N/A	0.030	0.003	0.001	1.293	0.381	0.086	1.041	0.032

Problem 1039	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	38	35	34	34	36	34	31
normalized size	1	1.00	1.00	0.92	0.89	0.89	0.95	0.89	0.82
time (sec)	N/A	0.017	0.002	0.001	1.338	0.382	0.078	1.105	0.040

Problem 1040	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	40	37	36	36	39	36	36
normalized size	1	1.00	1.25	1.16	1.12	1.12	1.22	1.12	1.12
time (sec)	N/A	0.015	0.002	0.002	1.318	0.387	0.074	1.020	0.049

Problem 1041	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	20	20	19	12	20
normalized size	1	1.00	1.00	0.93	1.43	1.43	1.36	0.86	1.43
time (sec)	N/A	0.001	0.001	0.002	1.270	0.374	0.064	0.967	0.027

Problem 1042	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	37	37	35	34	31	46	34
normalized size	1	1.00	0.86	0.86	0.81	0.79	0.72	1.07	0.79
time (sec)	N/A	0.014	0.007	0.003	1.289	0.440	0.165	0.875	0.047

Problem 1043	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	35	44	46	57	39	79	46
normalized size	1	1.00	0.85	1.07	1.12	1.39	0.95	1.93	1.12
time (sec)	N/A	0.022	0.029	0.007	1.378	0.411	0.199	1.083	0.149

Problem 1044	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	52	33	56	61	69	54	46	59
normalized size	1	1.00	0.63	1.08	1.17	1.33	1.04	0.88	1.13
time (sec)	N/A	0.028	0.024	0.007	1.333	0.406	0.306	1.072	0.172

Problem 1045	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	31	52	60	60	61	29	58
normalized size	1	1.00	1.11	1.86	2.14	2.14	2.18	1.04	2.07
time (sec)	N/A	0.005	0.018	0.004	1.333	0.403	0.351	0.984	0.046

Problem 1046	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	35	51	78	78	85	64	76
normalized size	1	1.00	0.62	0.91	1.39	1.39	1.52	1.14	1.36
time (sec)	N/A	0.024	0.012	0.005	1.380	0.409	0.439	1.070	0.052

Problem 1047	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	38	52	95	95	100	36	91
normalized size	1	1.00	0.67	0.91	1.67	1.67	1.75	0.63	1.60
time (sec)	N/A	0.025	0.018	0.004	1.386	0.442	0.505	0.846	0.187

Problem 1048	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	37	52	108	108	117	36	104
normalized size	1	1.00	0.63	0.88	1.83	1.83	1.98	0.61	1.76
time (sec)	N/A	0.029	0.015	0.006	1.420	0.439	0.600	0.934	0.108

Problem 1049	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	42	49	48	52	49	59	48
normalized size	1	1.00	0.69	0.80	0.79	0.85	0.80	0.97	0.79
time (sec)	N/A	0.021	0.006	0.003	1.342	0.449	0.181	1.148	0.049

Problem 1050	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	31	35	34	38	34	45	32
normalized size	1	1.00	0.72	0.81	0.79	0.88	0.79	1.05	0.74
time (sec)	N/A	0.014	0.005	0.003	1.342	0.422	0.153	0.871	0.148

Problem 1051	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	19	18	20	15	19	18
normalized size	1	1.00	1.00	1.06	1.00	1.11	0.83	1.06	1.00
time (sec)	N/A	0.010	0.003	0.003	1.339	0.423	0.122	1.013	0.039

Problem 1052	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	10	10	10	11	10	10	7	11	10
normalized size	1	1.00	1.00	1.10	1.00	1.00	0.70	1.10	1.00
time (sec)	N/A	0.002	0.001	0.000	1.326	0.436	0.066	1.055	0.019

Problem 1053	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	38	37	28	22	39	17
normalized size	1	1.00	1.00	2.24	2.18	1.65	1.29	2.29	1.00
time (sec)	N/A	0.009	0.006	0.006	1.401	0.433	0.171	1.195	0.170

Problem 1054	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	53	58	60	60	48	53	42
normalized size	1	1.00	1.26	1.38	1.43	1.43	1.14	1.26	1.00
time (sec)	N/A	0.029	0.015	0.007	1.256	0.414	0.283	1.030	0.071

Problem 1055	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	65	78	82	98	71	69	64
normalized size	1	1.00	1.03	1.24	1.30	1.56	1.13	1.10	1.02
time (sec)	N/A	0.039	0.022	0.007	1.348	0.433	0.381	0.866	0.078

Problem 1056	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	46	53	53	79	51	80	52
normalized size	1	1.00	0.85	0.98	0.98	1.46	0.94	1.48	0.96
time (sec)	N/A	0.031	0.020	0.007	1.294	0.433	0.246	1.119	0.055

Problem 1057	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	33	40	40	61	36	59	39
normalized size	1	1.00	0.85	1.03	1.03	1.56	0.92	1.51	1.00
time (sec)	N/A	0.021	0.017	0.007	1.362	0.464	0.194	1.183	0.168

Problem 1058	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	23	28	28	33	24	54	27
normalized size	1	1.00	0.85	1.04	1.04	1.22	0.89	2.00	1.00
time (sec)	N/A	0.013	0.009	0.005	1.338	0.408	0.172	1.022	0.043

Problem 1059	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	12	12	12	13	12	13	10	12	12
normalized size	1	1.00	1.00	1.08	1.00	1.08	0.83	1.00	1.00
time (sec)	N/A	0.001	0.002	0.000	1.372	0.409	0.137	1.106	0.024

Problem 1060	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	50	56	55	51	44	44	37
normalized size	1	1.00	1.22	1.37	1.34	1.24	1.07	1.07	0.90
time (sec)	N/A	0.028	0.016	0.007	1.376	0.443	0.284	0.953	0.177

Problem 1061	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	74	76	64	76	49	83	46
normalized size	1	1.00	1.61	1.65	1.39	1.65	1.07	1.80	1.00
time (sec)	N/A	0.017	0.024	0.010	1.315	0.441	0.273	1.066	0.181

Problem 1062	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	83	83	68	96	108	146	104	81	86
normalized size	1	1.00	0.82	1.16	1.30	1.76	1.25	0.98	1.04
time (sec)	N/A	0.050	0.043	0.011	1.355	0.448	0.512	0.961	0.098

Problem 1063	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	108	108	60	113	68	62	289	185	-1
normalized size	1	1.00	0.56	1.05	0.63	0.57	2.68	1.71	-0.01
time (sec)	N/A	0.021	0.052	0.008	3.005	0.436	48.589	1.273	0.000

Problem 1064	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	88	88	56	99	54	57	253	115	-1
normalized size	1	1.00	0.64	1.12	0.61	0.65	2.88	1.31	-0.01
time (sec)	N/A	0.015	0.051	0.005	2.965	0.444	21.067	1.061	0.000

Problem 1065	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	50	85	40	52	218	101	-1
normalized size	1	1.00	0.74	1.25	0.59	0.76	3.21	1.49	-0.01
time (sec)	N/A	0.011	0.041	0.006	2.953	0.447	9.031	1.293	0.000

Problem 1066	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	44	71	28	47	168	50	-1
normalized size	1	1.00	0.92	1.48	0.58	0.98	3.50	1.04	-0.02
time (sec)	N/A	0.006	0.038	0.005	2.902	0.434	4.494	1.023	0.000

Problem 1067	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	20	57	17	38	133	42	37
normalized size	1	1.00	0.71	2.04	0.61	1.36	4.75	1.50	1.32
time (sec)	N/A	0.004	0.006	0.005	2.978	0.447	2.728	1.036	0.205

Problem 1068	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	32	42	14	37	100	28	14
normalized size	1	1.00	1.52	2.00	0.67	1.76	4.76	1.33	0.67
time (sec)	N/A	0.004	0.007	0.006	2.901	0.442	1.843	1.014	0.145

Problem 1069	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	36	64	21	48	71	33	-1
normalized size	1	1.00	1.57	2.78	0.91	2.09	3.09	1.43	-0.04
time (sec)	N/A	0.004	0.013	0.030	2.954	0.471	1.619	1.064	0.000

Problem 1070	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	15	38	33	61	19	34
normalized size	1	1.00	1.00	0.75	1.90	1.65	3.05	0.95	1.70
time (sec)	N/A	0.002	0.005	0.003	1.261	0.433	1.674	0.937	0.270

Problem 1071	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	23	18	64	53	173	22	50
normalized size	1	1.00	0.56	0.44	1.56	1.29	4.22	0.54	1.22
time (sec)	N/A	0.004	0.009	0.003	1.397	0.419	6.547	1.046	0.244

Problem 1072	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	30	25	95	70	568	29	64
normalized size	1	1.00	0.49	0.41	1.56	1.15	9.31	0.48	1.05
time (sec)	N/A	0.008	0.012	0.003	1.272	0.447	19.923	1.224	0.269

Problem 1073	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	35	30	131	85	1562	35	80
normalized size	1	1.00	0.43	0.37	1.62	1.05	19.28	0.43	0.99
time (sec)	N/A	0.013	0.014	0.003	1.348	0.438	53.780	1.118	0.282

Problem 1074	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	40	35	172	100	3650	42	94
normalized size	1	1.00	0.40	0.35	1.70	0.99	36.14	0.42	0.93
time (sec)	N/A	0.019	0.017	0.004	1.322	0.453	135.085	1.359	0.292
Problem 1075	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	109	109	66	127	66	67	325	237	-1
normalized size	1	1.00	0.61	1.17	0.61	0.61	2.98	2.17	-0.01
time (sec)	N/A	0.020	0.058	0.005	3.027	0.430	75.198	1.256	0.000
Problem 1076	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	61	113	52	62	289	185	-1
normalized size	1	1.00	0.69	1.27	0.58	0.70	3.25	2.08	-0.01
time (sec)	N/A	0.013	0.055	0.005	2.904	0.462	32.987	1.330	0.000
Problem 1077	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	55	99	40	57	250	91	-1
normalized size	1	1.00	0.80	1.43	0.58	0.83	3.62	1.32	-0.01
time (sec)	N/A	0.008	0.043	0.005	2.977	0.443	15.248	1.164	0.000
Problem 1078	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	29	85	29	46	214	101	-1
normalized size	1	1.00	0.59	1.73	0.59	0.94	4.37	2.06	-0.02
time (sec)	N/A	0.007	0.011	0.005	2.911	0.435	7.461	1.116	0.000

Problem 1079	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	44	71	28	47	165	66	-1
normalized size	1	1.00	0.92	1.48	0.58	0.98	3.44	1.38	-0.02
time (sec)	N/A	0.006	0.033	0.006	2.967	0.453	4.820	0.920	0.000

Problem 1080	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	37	57	28	40	136	31	-1
normalized size	1	1.00	0.79	1.21	0.60	0.85	2.89	0.66	-0.02
time (sec)	N/A	0.007	0.012	0.004	3.088	0.473	3.275	1.172	0.000

Problem 1081	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	35	72	42	52	100	35	-1
normalized size	1	1.00	0.85	1.76	1.02	1.27	2.44	0.85	-0.02
time (sec)	N/A	0.007	0.006	0.016	2.993	0.439	2.920	1.190	0.000

Problem 1082	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	B	B	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	37	76	66	71	500	38	-1
normalized size	1	1.00	0.90	1.85	1.61	1.73	12.20	0.93	-0.02
time (sec)	N/A	0.005	0.006	0.020	2.973	0.445	3.698	1.019	0.000

Problem 1083	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	15	94	52	88	19	50
normalized size	1	1.00	1.00	0.75	4.70	2.60	4.40	0.95	2.50
time (sec)	N/A	0.002	0.006	0.003	1.284	0.439	6.256	1.057	0.252

Problem 1084	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	23	18	131	69	228	22	64
normalized size	1	1.00	0.56	0.44	3.20	1.68	5.56	0.54	1.56
time (sec)	N/A	0.004	0.010	0.003	1.384	0.448	19.081	1.127	0.268

Problem 1085	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	30	25	172	86	677	29	80
normalized size	1	1.00	0.49	0.41	2.82	1.41	11.10	0.48	1.31
time (sec)	N/A	0.008	0.012	0.003	1.365	0.434	51.652	1.106	0.319

Problem 1086	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	35	30	218	101	1753	35	94
normalized size	1	1.00	0.43	0.37	2.69	1.25	21.64	0.43	1.16
time (sec)	N/A	0.013	0.015	0.002	1.392	0.423	132.965	1.167	0.310

Problem 1087	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	40	35	269	116	0	42	110
normalized size	1	1.00	0.40	0.35	2.66	1.15	0.00	0.42	1.09
time (sec)	N/A	0.019	0.017	0.003	1.380	0.433	0.000	1.231	0.328

Problem 1088	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	130	130	75	155	78	77	0	323	-1
normalized size	1	1.00	0.58	1.19	0.60	0.59	0.00	2.48	-0.01
time (sec)	N/A	0.025	0.069	0.006	3.012	0.449	0.000	1.400	0.000

Problem 1089	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	110	110	70	141	64	72	360	296	-1
normalized size	1	1.00	0.64	1.28	0.58	0.65	3.27	2.69	-0.01
time (sec)	N/A	0.019	0.061	0.005	2.970	0.440	117.569	1.493	0.000

Problem 1090	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	90	90	66	127	52	67	321	143	-1
normalized size	1	1.00	0.73	1.41	0.58	0.74	3.57	1.59	-0.01
time (sec)	N/A	0.012	0.063	0.005	3.006	0.437	53.580	1.143	0.000

Problem 1091	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	34	113	41	51	286	185	-1
normalized size	1	1.00	0.49	1.61	0.59	0.73	4.09	2.64	-0.01
time (sec)	N/A	0.011	0.014	0.004	3.103	0.436	25.761	1.308	0.000

Problem 1092	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	55	99	40	57	246	114	-1
normalized size	1	1.00	0.80	1.43	0.58	0.83	3.57	1.65	-0.01
time (sec)	N/A	0.008	0.045	0.005	3.049	0.443	16.531	1.181	0.000

Problem 1093	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	50	85	40	52	214	101	-1
normalized size	1	1.00	0.74	1.25	0.59	0.76	3.15	1.49	-0.01
time (sec)	N/A	0.009	0.037	0.005	3.060	0.424	9.886	1.045	0.000

Problem 1094	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	44	71	42	47	172	39	-1
normalized size	1	1.00	0.66	1.06	0.63	0.70	2.57	0.58	-0.01
time (sec)	N/A	0.010	0.023	0.005	2.934	0.417	7.503	1.053	0.000

Problem 1095	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	35	77	56	58	139	42	-1
normalized size	1	1.00	0.54	1.18	0.86	0.89	2.14	0.65	-0.02
time (sec)	N/A	0.010	0.007	0.018	2.971	0.445	7.762	1.007	0.000

Problem 1096	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	B	A	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	37	84	99	75	576	44	-1
normalized size	1	1.00	0.59	1.33	1.57	1.19	9.14	0.70	-0.02
time (sec)	N/A	0.010	0.008	0.020	2.971	0.434	7.473	0.977	0.000

Problem 1097	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	B	A	B	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	37	84	160	91	1608	44	-1
normalized size	1	1.00	0.59	1.33	2.54	1.44	25.52	0.70	-0.02
time (sec)	N/A	0.007	0.009	0.022	3.075	0.461	11.213	0.982	0.000

Problem 1098	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	15	171	66	116	19	64
normalized size	1	1.00	1.00	0.75	8.55	3.30	5.80	0.95	3.20
time (sec)	N/A	0.002	0.008	0.003	1.355	0.437	19.494	1.108	0.279

Problem 1099	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	23	18	218	83	282	22	80
normalized size	1	1.00	0.56	0.44	5.32	2.02	6.88	0.54	1.95
time (sec)	N/A	0.004	0.011	0.005	1.403	0.422	53.145	1.227	0.303

Problem 1100	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	30	25	269	100	785	29	94
normalized size	1	1.00	0.49	0.41	4.41	1.64	12.87	0.48	1.54
time (sec)	N/A	0.008	0.016	0.003	1.415	0.461	133.938	1.268	0.310

Problem 1101	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	35	30	325	115	0	35	110
normalized size	1	1.00	0.43	0.37	4.01	1.42	0.00	0.43	1.36
time (sec)	N/A	0.013	0.017	0.002	1.456	0.430	0.000	0.990	0.315

Problem 1102	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	40	35	386	130	0	42	124
normalized size	1	1.00	0.40	0.35	3.82	1.29	0.00	0.42	1.23
time (sec)	N/A	0.019	0.021	0.003	1.393	0.456	0.000	0.877	0.352

Problem 1103	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	121	121	45	40	452	145	0	48	140
normalized size	1	1.00	0.37	0.33	3.74	1.20	0.00	0.40	1.16
time (sec)	N/A	0.025	0.022	0.003	1.384	0.432	0.000	0.858	0.370

Problem 1104	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	47	98	42	55	75	42	-1
normalized size	1	1.00	0.73	1.53	0.66	0.86	1.17	0.66	-0.02
time (sec)	N/A	0.012	0.039	0.013	2.989	0.448	33.751	0.699	0.000

Problem 1105	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	62	62	91	118	42	48	76	34	55
normalized size	1	1.00	1.47	1.90	0.68	0.77	1.23	0.55	0.89
time (sec)	N/A	0.028	0.102	0.013	3.030	0.453	7.083	0.702	0.151

Problem 1106	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	87	87	61	85	56	52	201	101	-1
normalized size	1	1.00	0.70	0.98	0.64	0.60	2.31	1.16	-0.01
time (sec)	N/A	0.018	0.025	0.006	2.993	0.449	14.676	0.758	0.000

Problem 1107	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	54	71	42	47	175	69	-1
normalized size	1	1.00	0.81	1.06	0.63	0.70	2.61	1.03	-0.01
time (sec)	N/A	0.011	0.026	0.005	2.901	0.439	5.643	0.703	0.000

Problem 1108	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	47	57	28	40	139	44	-1
normalized size	1	1.00	1.00	1.21	0.60	0.85	2.96	0.94	-0.02
time (sec)	N/A	0.007	0.020	0.003	3.023	0.455	2.586	0.697	0.000

Problem 1109	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	30	41	12	36	100	27	12
normalized size	1	1.00	1.50	2.05	0.60	1.80	5.00	1.35	0.60
time (sec)	N/A	0.003	0.013	0.004	3.101	0.433	1.547	0.650	0.119

Problem 1110	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	2	2	2	27	2	22	41	13	22
normalized size	1	1.00	1.00	13.50	1.00	11.00	20.50	6.50	11.00
time (sec)	N/A	0.001	0.005	0.004	2.946	0.451	1.035	0.654	0.078

Problem 1111	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	14	16	23	29	19	13
normalized size	1	1.00	1.00	0.82	0.94	1.35	1.71	1.12	0.76
time (sec)	N/A	0.003	0.003	0.002	2.983	0.443	0.937	0.677	0.283

Problem 1112	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	23	18	38	39	139	22	43
normalized size	1	1.00	0.56	0.44	0.93	0.95	3.39	0.54	1.05
time (sec)	N/A	0.004	0.007	0.003	3.120	0.463	2.246	0.643	0.309

Problem 1113	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	30	25	64	56	332	29	55
normalized size	1	1.00	0.49	0.41	1.05	0.92	5.44	0.48	0.90
time (sec)	N/A	0.008	0.009	0.004	3.026	0.441	7.892	0.690	0.324

Problem 1114	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	35	30	95	71	595	35	67
normalized size	1	1.00	0.43	0.37	1.17	0.88	7.35	0.43	0.83
time (sec)	N/A	0.014	0.011	0.004	3.029	0.471	22.133	0.664	0.345

Problem 1115	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	40	35	131	86	933	42	80
normalized size	1	1.00	0.40	0.35	1.30	0.85	9.24	0.42	0.79
time (sec)	N/A	0.018	0.012	0.004	3.085	0.462	58.395	0.672	0.363

Problem 1116	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	85	85	37	84	70	65	207	81	-1
normalized size	1	1.00	0.44	0.99	0.82	0.76	2.44	0.95	-0.01
time (sec)	N/A	0.016	0.013	0.017	2.839	0.448	17.475	0.748	0.000

Problem 1117	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	37	77	56	58	168	73	-1
normalized size	1	1.00	0.57	1.18	0.86	0.89	2.58	1.12	-0.02
time (sec)	N/A	0.011	0.011	0.017	2.987	0.438	6.987	0.795	0.000

Problem 1118	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	A	A	A	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	37	71	41	53	133	70	-1
normalized size	1	1.00	0.90	1.73	1.00	1.29	3.24	1.71	-0.02
time (sec)	N/A	0.007	0.010	0.016	2.862	0.435	2.485	0.726	0.000

Problem 1119	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	B	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	34	67	21	50	104	55	-1
normalized size	1	1.00	1.48	2.91	0.91	2.17	4.52	2.39	-0.04
time (sec)	N/A	0.003	0.036	0.015	2.863	0.467	1.538	0.691	0.000

Problem 1120	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	15	16	23	29	43	14
normalized size	1	1.00	1.00	0.83	0.89	1.28	1.61	2.39	0.78
time (sec)	N/A	0.002	0.004	0.004	2.940	0.452	1.199	0.651	0.360

Problem 1121	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	13	15	11	22	65	62	14
normalized size	1	1.00	0.72	0.83	0.61	1.22	3.61	3.44	0.78
time (sec)	N/A	0.002	0.003	0.002	1.338	0.430	1.857	0.719	0.305

Problem 1122	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	30	25	40	54	158	67	42
normalized size	1	1.00	0.71	0.60	0.95	1.29	3.76	1.60	1.00
time (sec)	N/A	0.005	0.007	0.003	1.416	0.440	5.279	0.701	0.322

Problem 1123	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	62	62	33	28	79	59	282	73	55
normalized size	1	1.00	0.53	0.45	1.27	0.95	4.55	1.18	0.89
time (sec)	N/A	0.008	0.009	0.003	1.346	0.431	16.833	0.664	0.337

Problem 1124	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	40	35	134	86	423	79	68
normalized size	1	1.00	0.49	0.43	1.63	1.05	5.16	0.96	0.83
time (sec)	N/A	0.013	0.010	0.004	1.375	0.430	44.937	0.695	0.355

Problem 1125	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	45	40	201	91	592	85	80
normalized size	1	1.00	0.44	0.39	1.97	0.89	5.80	0.83	0.78
time (sec)	N/A	0.020	0.012	0.005	1.367	0.482	113.605	0.676	0.363

Problem 1126	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	103	103	37	89	125	85	250	127	-1
normalized size	1	1.00	0.36	0.86	1.21	0.83	2.43	1.23	-0.01
time (sec)	N/A	0.021	0.015	0.022	3.009	0.444	45.202	0.889	0.000

Problem 1127	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	C	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	87	87	37	84	111	81	207	119	-1
normalized size	1	1.00	0.43	0.97	1.28	0.93	2.38	1.37	-0.01
time (sec)	N/A	0.015	0.012	0.020	3.000	0.426	17.501	0.800	0.000

Problem 1128	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	B	A	C	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	37	79	98	75	160	115	-1
normalized size	1	1.00	0.59	1.25	1.56	1.19	2.54	1.83	-0.02
time (sec)	N/A	0.011	0.011	0.021	2.965	0.446	6.461	0.752	0.000

Problem 1129	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	C	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	49	73	66	71	126	102	-1
normalized size	1	1.00	1.20	1.78	1.61	1.73	3.07	2.49	-0.02
time (sec)	N/A	0.006	0.057	0.018	3.011	0.449	3.284	0.703	0.000

Problem 1130	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	15	38	37	65	89	32
normalized size	1	1.00	1.00	0.75	1.90	1.85	3.25	4.45	1.60
time (sec)	N/A	0.002	0.004	0.002	1.324	0.452	1.694	0.708	0.263

Problem 1131	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	23	18	38	38	65	89	33
normalized size	1	1.00	0.56	0.44	0.93	0.93	1.59	2.17	0.80
time (sec)	N/A	0.004	0.005	0.003	2.934	0.436	2.346	0.672	0.310

Problem 1132	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	30	25	38	49	165	108	48
normalized size	1	1.00	0.52	0.43	0.66	0.84	2.84	1.86	0.83
time (sec)	N/A	0.008	0.006	0.003	1.351	0.440	5.397	0.678	0.338

Problem 1133	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	23	23	25	35	279	113	41
normalized size	1	1.00	0.53	0.53	0.58	0.81	6.49	2.63	0.95
time (sec)	N/A	0.005	0.007	0.002	1.391	0.475	9.607	0.683	0.365

Problem 1134	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	40	35	52	84	423	119	75
normalized size	1	1.00	0.63	0.56	0.83	1.33	6.71	1.89	1.19
time (sec)	N/A	0.008	0.011	0.001	1.394	0.437	27.605	0.710	0.377

Problem 1135	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	83	83	45	40	91	101	592	125	86
normalized size	1	1.00	0.54	0.48	1.10	1.22	7.13	1.51	1.04
time (sec)	N/A	0.014	0.013	0.002	1.344	0.444	71.007	0.693	0.413

Problem 1136	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	103	103	50	45	146	114	0	131	99
normalized size	1	1.00	0.49	0.44	1.42	1.11	0.00	1.27	0.96
time (sec)	N/A	0.019	0.014	0.003	1.421	0.429	0.000	0.737	0.423

Problem 1137	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	114	193	72	201	0	679	-1
normalized size	1	1.00	0.90	1.53	0.57	1.60	0.00	5.39	-0.01
time (sec)	N/A	0.055	0.100	0.011	3.025	0.474	0.000	1.574	0.000

Problem 1138	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	104	143	50	155	0	403	-1
normalized size	1	1.00	1.08	1.49	0.52	1.61	0.00	4.20	-0.01
time (sec)	N/A	0.037	0.082	0.005	3.092	0.466	0.000	1.253	0.000

Problem 1139	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	69	98	28	127	0	173	59
normalized size	1	1.00	1.03	1.46	0.42	1.90	0.00	2.58	0.88
time (sec)	N/A	0.029	0.061	0.006	3.083	0.469	0.000	0.902	0.300

Problem 1140	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	47	57	8	101	85	49	44
normalized size	1	1.00	1.09	1.33	0.19	2.35	1.98	1.14	1.02
time (sec)	N/A	0.024	0.017	0.005	2.991	0.447	3.953	0.764	0.175

Problem 1141	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	27	25	21	39	82	116	23
normalized size	1	1.00	1.00	0.93	0.78	1.44	3.04	4.30	0.85
time (sec)	N/A	0.003	0.017	0.003	1.315	0.418	4.444	0.701	0.391

Problem 1142	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	61	42	32	45	57	82	237	62
normalized size	1	1.00	0.69	0.52	0.74	0.93	1.34	3.89	1.02
time (sec)	N/A	0.010	0.028	0.002	1.347	0.451	13.690	0.807	0.415

Problem 1143	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	91	91	49	37	67	74	85	333	50
normalized size	1	1.00	0.54	0.41	0.74	0.81	0.93	3.66	0.55
time (sec)	N/A	0.018	0.036	0.003	1.358	0.444	55.151	1.065	0.442

Problem 1144	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	121	121	54	42	89	89	0	437	66
normalized size	1	1.00	0.45	0.35	0.74	0.74	0.00	3.61	0.55
time (sec)	N/A	0.028	0.040	0.003	1.401	0.432	0.000	1.563	0.478

Problem 1145	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	135	135	120	243	89	232	0	0	-1
normalized size	1	1.00	0.89	1.80	0.66	1.72	0.00	0.00	-0.01
time (sec)	N/A	0.052	0.150	0.012	3.121	0.471	0.000	0.000	0.000

Problem 1146	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	109	185	63	193	0	0	-1
normalized size	1	1.00	1.07	1.81	0.62	1.89	0.00	0.00	-0.01
time (sec)	N/A	0.036	0.127	0.006	3.024	0.493	0.000	0.000	0.000

Problem 1147	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	F	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	95	127	39	159	0	0	72
normalized size	1	1.00	1.40	1.87	0.57	2.34	0.00	0.00	1.06
time (sec)	N/A	0.027	0.123	0.006	3.086	0.472	0.000	0.000	0.203

Problem 1148	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	C	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	48	71	14	108	90	0	53
normalized size	1	1.00	1.26	1.87	0.37	2.84	2.37	0.00	1.39
time (sec)	N/A	0.020	0.014	0.005	2.933	0.487	4.688	0.000	0.177

Problem 1149	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	29	30	25	45	94	115	26
normalized size	1	1.00	0.97	1.00	0.83	1.50	3.13	3.83	0.87
time (sec)	N/A	0.004	0.014	0.003	1.400	0.427	5.179	1.861	0.497

Problem 1150	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	46	45	53	72	94	251	80
normalized size	1	1.00	0.69	0.67	0.79	1.07	1.40	3.75	1.19
time (sec)	N/A	0.011	0.025	0.003	1.426	0.448	15.849	2.380	0.584

Problem 1151	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	57	56	79	98	97	366	111
normalized size	1	1.00	0.57	0.56	0.79	0.98	0.97	3.66	1.11
time (sec)	N/A	0.020	0.031	0.004	1.322	0.461	59.496	2.573	0.650

Problem 1152	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	133	133	76	67	105	122	0	487	170
normalized size	1	1.00	0.57	0.50	0.79	0.92	0.00	3.66	1.28
time (sec)	N/A	0.034	0.041	0.003	1.293	0.518	0.000	3.296	0.714

Problem 1153	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	44	134	46	65	0	227	-1
normalized size	1	1.00	0.44	1.34	0.46	0.65	0.00	2.27	-0.01
time (sec)	N/A	0.017	0.034	0.009	2.864	0.445	0.000	1.243	0.000

Problem 1154	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	39	102	34	60	0	125	-1
normalized size	1	1.00	0.53	1.38	0.46	0.81	0.00	1.69	-0.01
time (sec)	N/A	0.010	0.035	0.005	2.859	0.427	0.000	0.984	0.000

Problem 1155	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	30	70	22	52	187	55	44
normalized size	1	1.00	0.70	1.63	0.51	1.21	4.35	1.28	1.02
time (sec)	N/A	0.006	0.010	0.004	3.068	0.440	4.742	1.069	0.256

Problem 1156	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	37	9	28	41	15	40
normalized size	1	1.00	1.00	2.85	0.69	2.15	3.15	1.15	3.08
time (sec)	N/A	0.003	0.016	0.003	2.943	0.438	3.347	0.885	0.051

Problem 1157	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	16	28	12	26	156	71	24
normalized size	1	1.00	0.57	1.00	0.43	0.93	5.57	2.54	0.86
time (sec)	N/A	0.002	0.018	0.004	1.358	0.418	85.283	1.062	0.461

Problem 1158	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	37	35	25	39	0	128	49
normalized size	1	1.00	0.65	0.61	0.44	0.68	0.00	2.25	0.86
time (sec)	N/A	0.006	0.025	0.003	1.277	0.414	0.000	1.017	0.311

Problem 1159	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	85	85	42	40	37	49	0	181	66
normalized size	1	1.00	0.49	0.47	0.44	0.58	0.00	2.13	0.78
time (sec)	N/A	0.011	0.032	0.003	1.315	0.424	0.000	1.021	0.452

Problem 1160	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	91	91	80	89	67	62	199	101	-1
normalized size	1	1.00	0.88	0.98	0.74	0.68	2.19	1.11	-0.01
time (sec)	N/A	0.022	0.047	0.009	2.968	0.440	7.482	0.879	0.000

Problem 1161	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	69	61	38	52	124	42	41
normalized size	1	1.00	1.35	1.20	0.75	1.02	2.43	0.82	0.80
time (sec)	N/A	0.010	0.023	0.006	2.964	0.438	3.010	1.019	0.207

Problem 1162	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	8	8	12	31	6	32	26	8	31
normalized size	1	1.00	1.50	3.88	0.75	4.00	3.25	1.00	3.88
time (sec)	N/A	0.004	0.010	0.004	3.001	0.436	1.607	1.019	0.178

Problem 1163	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	21	20	30	29	100	53	32
normalized size	1	1.00	0.57	0.54	0.81	0.78	2.70	1.43	0.86
time (sec)	N/A	0.004	0.006	0.004	1.318	0.490	2.302	0.848	0.255

Problem 1164	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	33	30	59	49	282	97	69
normalized size	1	1.00	0.42	0.38	0.75	0.62	3.57	1.23	0.87
time (sec)	N/A	0.013	0.013	0.004	1.337	0.469	9.849	1.096	0.370

Problem 1165	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	16	16	12	22	73	62	22
normalized size	1	1.00	0.76	0.76	0.57	1.05	3.48	2.95	1.05
time (sec)	N/A	0.002	0.005	0.003	1.367	0.427	1.800	0.896	0.364

Problem 1166	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	24	24	19	19	15	29	73	82	26
normalized size	1	1.00	0.79	0.79	0.62	1.21	3.04	3.42	1.08
time (sec)	N/A	0.003	0.007	0.003	1.371	0.457	5.162	1.098	0.463

Problem 1167	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	21	19	12	22	90	71	22
normalized size	1	1.00	0.81	0.73	0.46	0.85	3.46	2.73	0.85
time (sec)	N/A	0.002	0.013	0.002	1.332	0.465	20.446	1.044	0.374

Problem 1168	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	19	24	15	29	83	91	26
normalized size	1	1.00	0.66	0.83	0.52	1.00	2.86	3.14	0.90
time (sec)	N/A	0.003	0.018	0.003	1.254	0.433	31.496	1.144	0.321

Problem 1169	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	C	F(-1)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	39	76	39	108	88	0	56
normalized size	1	1.00	1.00	1.95	1.00	2.77	2.26	0.00	1.44
time (sec)	N/A	0.024	0.020	0.010	1.429	0.465	4.766	0.000	0.218

Problem 1170	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	241	241	42	0	0	505	0	0	-1
normalized size	1	1.00	0.17	0.00	0.00	2.10	0.00	0.00	-0.00
time (sec)	N/A	0.254	0.021	0.072	0.000	0.497	0.000	0.000	0.000

Problem 1171	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	144	144	70	104	0	0	0	0	-1
normalized size	1	1.00	0.49	0.72	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.034	0.036	0.099	0.000	0.481	0.000	0.000	0.000

Problem 1172	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	106	106	70	94	0	0	0	0	-1
normalized size	1	1.00	0.66	0.89	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.022	0.023	0.066	0.000	0.465	0.000	0.000	0.000

Problem 1173	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	70	0	0	0	102	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	1.44	0.00	-0.01
time (sec)	N/A	0.012	0.023	0.080	0.000	0.482	3.793	0.000	0.000

Problem 1174	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	68	94	0	0	0	0	-1
normalized size	1	1.00	0.87	1.21	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.016	0.023	0.068	0.000	0.485	0.000	0.000	0.000

Problem 1175	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	70	105	0	0	0	0	-1
normalized size	1	1.00	0.85	1.28	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.017	0.026	0.081	0.000	0.492	0.000	0.000	0.000

Problem 1176	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	70	113	0	0	0	0	-1
normalized size	1	1.00	0.61	0.98	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.026	0.028	0.079	0.000	0.488	0.000	0.000	0.000

Problem 1177	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	148	148	70	114	0	0	0	0	-1
normalized size	1	1.00	0.47	0.77	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.038	0.030	0.078	0.000	0.484	0.000	0.000	0.000

Problem 1178	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	256	256	70	477	0	194	0	0	-1
normalized size	1	1.00	0.27	1.86	0.00	0.76	0.00	0.00	-0.00
time (sec)	N/A	0.173	0.021	2.284	0.000	0.468	0.000	0.000	0.000

Problem 1179	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	233	233	68	0	0	227	0	0	-1
normalized size	1	1.00	0.29	0.00	0.00	0.97	0.00	0.00	-0.00
time (sec)	N/A	0.131	0.023	0.076	0.000	0.477	0.000	0.000	0.000

Problem 1180	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	33	31	0	31	0	0	38
normalized size	1	1.00	1.00	0.94	0.00	0.94	0.00	0.00	1.15
time (sec)	N/A	0.003	0.014	0.046	0.000	0.451	0.000	0.000	0.549

Problem 1181	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	45	44	0	44	0	0	46
normalized size	1	1.00	0.67	0.66	0.00	0.66	0.00	0.00	0.69
time (sec)	N/A	0.009	0.021	0.048	0.000	0.447	0.000	0.000	0.666

Problem 1182	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	52	50	0	58	0	0	51
normalized size	1	1.00	0.52	0.50	0.00	0.58	0.00	0.00	0.51
time (sec)	N/A	0.018	0.025	0.054	0.000	0.458	0.000	0.000	0.752

Problem 1183	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	133	133	57	55	0	70	0	0	57
normalized size	1	1.00	0.43	0.41	0.00	0.53	0.00	0.00	0.43
time (sec)	N/A	0.028	0.029	0.062	0.000	0.468	0.000	0.000	0.794

Problem 1184	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	256	256	70	464	0	204	0	0	-1
normalized size	1	1.00	0.27	1.81	0.00	0.80	0.00	0.00	-0.00
time (sec)	N/A	0.158	0.025	2.142	0.000	0.476	0.000	0.000	0.000

Problem 1185	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	233	233	70	0	0	227	0	0	-1
normalized size	1	1.00	0.30	0.00	0.00	0.97	0.00	0.00	-0.00
time (sec)	N/A	0.135	0.023	0.060	0.000	0.470	0.000	0.000	0.000

Problem 1186	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	31	31	0	31	0	0	-1
normalized size	1	1.00	1.00	1.00	0.00	1.00	0.00	0.00	-0.03
time (sec)	N/A	0.003	0.014	0.042	0.000	0.443	0.000	0.000	0.000

Problem 1187	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	45	44	0	44	0	0	-1
normalized size	1	1.00	0.67	0.66	0.00	0.66	0.00	0.00	-0.01
time (sec)	N/A	0.010	0.020	0.053	0.000	0.436	0.000	0.000	0.000

Problem 1188	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	52	50	0	58	0	0	-1
normalized size	1	1.00	0.52	0.50	0.00	0.58	0.00	0.00	-0.01
time (sec)	N/A	0.018	0.024	0.056	0.000	0.446	0.000	0.000	0.000

Problem 1189	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	112	112	70	0	0	0	0	0	-1
normalized size	1	1.00	0.62	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.024	0.027	0.104	0.000	0.473	0.000	0.000	0.000

Problem 1190	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	76	76	70	0	0	0	0	0	-1
normalized size	1	1.00	0.92	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.015	0.022	0.065	0.000	0.462	0.000	0.000	0.000

Problem 1191	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	A	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	68	0	0	0	100	0	-1
normalized size	1	1.00	1.58	0.00	0.00	0.00	2.33	0.00	-0.02
time (sec)	N/A	0.008	0.021	0.062	0.000	0.461	5.338	0.000	0.000

Problem 1192	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	70	0	0	0	0	0	-1
normalized size	1	1.00	0.85	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.015	0.022	0.074	0.000	0.465	0.000	0.000	0.000

Problem 1193	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	70	0	0	0	0	0	-1
normalized size	1	1.00	0.61	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.025	0.025	0.085	0.000	0.463	0.000	0.000	0.000

Problem 1194	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	291	291	70	469	0	241	0	0	-1
normalized size	1	1.00	0.24	1.61	0.00	0.83	0.00	0.00	-0.00
time (sec)	N/A	0.181	0.028	2.013	0.000	0.491	0.000	0.000	0.000

Problem 1195	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	266	266	70	459	0	304	0	0	-1
normalized size	1	1.00	0.26	1.73	0.00	1.14	0.00	0.00	-0.00
time (sec)	N/A	0.140	0.022	1.882	0.000	0.513	0.000	0.000	0.000

Problem 1196	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	33	31	0	31	0	0	-1
normalized size	1	1.00	1.00	0.94	0.00	0.94	0.00	0.00	-0.03
time (sec)	N/A	0.003	0.012	0.044	0.000	0.444	0.000	0.000	0.000

Problem 1197	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	38	33	0	36	0	0	-1
normalized size	1	1.00	0.58	0.51	0.00	0.55	0.00	0.00	-0.02
time (sec)	N/A	0.009	0.017	0.049	0.000	0.462	0.000	0.000	0.000

Problem 1198	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	50	44	0	58	0	0	-1
normalized size	1	1.00	0.50	0.44	0.00	0.58	0.00	0.00	-0.01
time (sec)	N/A	0.017	0.023	0.058	0.000	0.441	0.000	0.000	0.000

Problem 1199	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	139	139	70	0	0	0	0	0	-1
normalized size	1	1.00	0.50	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.034	0.031	0.077	0.000	0.473	0.000	0.000	0.000

Problem 1200	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	113	113	70	0	0	0	0	0	-1
normalized size	1	1.00	0.62	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.024	0.026	0.067	0.000	0.478	0.000	0.000	0.000

Problem 1201	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	70	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.014	0.023	0.071	0.000	0.491	0.000	0.000	0.000

Problem 1202	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	68	0	0	0	0	0	-1
normalized size	1	1.00	0.83	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.015	0.021	0.048	0.000	0.486	0.000	0.000	0.000

Problem 1203	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	70	0	0	0	95	0	-1
normalized size	1	1.00	0.86	0.00	0.00	0.00	1.17	0.00	-0.01
time (sec)	N/A	0.015	0.025	0.051	0.000	0.456	36.699	0.000	0.000

Problem 1204	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	114	114	70	0	0	0	0	0	-1
normalized size	1	1.00	0.61	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.025	0.024	0.088	0.000	0.490	0.000	0.000	0.000

Problem 1205	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	147	147	70	0	0	0	0	0	-1
normalized size	1	1.00	0.48	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.035	0.028	0.106	0.000	0.474	0.000	0.000	0.000

Problem 1206	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	137	137	70	96	0	0	0	0	-1
normalized size	1	1.00	0.51	0.70	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.032	0.030	0.073	0.000	0.496	0.000	0.000	0.000

Problem 1207	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	70	88	0	0	0	0	-1
normalized size	1	1.00	0.69	0.86	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.023	0.060	0.000	0.470	0.000	0.000	0.000

Problem 1208	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	70	94	0	0	0	0	-1
normalized size	1	1.00	0.90	1.21	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.016	0.022	0.045	0.000	0.454	0.000	0.000	0.000

Problem 1209	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	68	91	0	0	97	0	-1
normalized size	1	1.00	1.48	1.98	0.00	0.00	2.11	0.00	-0.02
time (sec)	N/A	0.009	0.024	0.045	0.000	0.466	11.910	0.000	0.000

Problem 1210	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F(-2)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	70	107	0	0	0	0	-1
normalized size	1	1.00	0.85	1.30	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.016	0.025	0.072	0.000	0.465	0.000	0.000	0.000

Problem 1211	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F(-2)	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	70	113	0	0	0	0	-1
normalized size	1	1.00	0.61	0.98	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.026	0.029	0.083	0.000	0.476	0.000	0.000	0.000

Problem 1212	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	287	287	70	481	0	239	0	0	-1
normalized size	1	1.00	0.24	1.68	0.00	0.83	0.00	0.00	-0.00
time (sec)	N/A	0.178	0.029	2.037	0.000	0.473	0.000	0.000	0.000

Problem 1213	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	264	264	70	476	0	302	0	0	-1
normalized size	1	1.00	0.27	1.80	0.00	1.14	0.00	0.00	-0.00
time (sec)	N/A	0.139	0.024	2.008	0.000	0.493	0.000	0.000	0.000

Problem 1214	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	31	31	0	31	0	0	27
normalized size	1	1.00	1.00	1.00	0.00	1.00	0.00	0.00	0.87
time (sec)	N/A	0.003	0.012	0.041	0.000	0.444	0.000	0.000	1.161

Problem 1215	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	38	33	0	36	0	0	40
normalized size	1	1.00	0.57	0.49	0.00	0.54	0.00	0.00	0.60
time (sec)	N/A	0.009	0.018	0.049	0.000	0.443	0.000	0.000	0.597

Problem 1216	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	50	44	0	58	0	0	46
normalized size	1	1.00	0.50	0.44	0.00	0.58	0.00	0.00	0.46
time (sec)	N/A	0.018	0.022	0.057	0.000	0.443	0.000	0.000	0.764

Problem 1217	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	141	141	70	101	0	0	0	0	-1
normalized size	1	1.00	0.50	0.72	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.030	0.031	0.064	0.000	0.472	0.000	0.000	0.000

Problem 1218	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	70	107	0	0	0	0	-1
normalized size	1	1.00	0.61	0.93	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.025	0.024	0.044	0.000	0.466	0.000	0.000	0.000

Problem 1219	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	70	105	0	0	0	0	-1
normalized size	1	1.00	0.85	1.28	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.016	0.025	0.044	0.000	0.479	0.000	0.000	0.000

Problem 1220	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F(-2)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	68	107	0	0	0	0	-1
normalized size	1	1.00	0.83	1.30	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.025	0.027	0.065	0.000	0.473	0.000	0.000	0.000

Problem 1221	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	88	88	70	0	0	0	95	0	-1
normalized size	1	1.00	0.80	0.00	0.00	0.00	1.08	0.00	-0.01
time (sec)	N/A	0.016	0.030	0.061	0.000	0.487	132.493	0.000	0.000

Problem 1222	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F(-2)	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	121	121	70	124	0	0	0	0	-1
normalized size	1	1.00	0.58	1.02	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.026	0.029	0.096	0.000	0.484	0.000	0.000	0.000

Problem 1223	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F(-2)	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	154	154	70	130	0	0	0	0	-1
normalized size	1	1.00	0.45	0.84	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.040	0.036	0.100	0.000	0.480	0.000	0.000	0.000

Problem 1224	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	A	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	297	297	70	490	0	351	0	0	-1
normalized size	1	1.00	0.24	1.65	0.00	1.18	0.00	0.00	-0.00
time (sec)	N/A	0.140	0.025	0.059	0.000	0.486	0.000	0.000	0.000

Problem 1225	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	B	F	F(-2)	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	33	50	0	45	0	0	38
normalized size	1	1.00	1.00	1.52	0.00	1.36	0.00	0.00	1.15
time (sec)	N/A	0.003	0.012	0.044	0.000	0.442	0.000	0.000	0.546

Problem 1226	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	45	44	0	44	0	0	38
normalized size	1	1.00	0.67	0.66	0.00	0.66	0.00	0.00	0.57
time (sec)	N/A	0.010	0.020	0.045	0.000	0.463	0.000	0.000	0.633

Problem 1227	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	50	44	0	58	0	0	45
normalized size	1	1.00	0.50	0.44	0.00	0.58	0.00	0.00	0.45
time (sec)	N/A	0.018	0.023	0.055	0.000	0.457	0.000	0.000	0.535

Problem 1228	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	133	133	57	56	0	54	0	0	56
normalized size	1	1.00	0.43	0.42	0.00	0.41	0.00	0.00	0.42
time (sec)	N/A	0.029	0.030	0.065	0.000	0.435	0.000	0.000	0.687

Problem 1229	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	83	83	77	103	167	128	819	256	133
normalized size	1	1.00	0.93	1.24	2.01	1.54	9.87	3.08	1.60
time (sec)	N/A	0.029	0.043	0.007	1.530	0.460	1.295	1.145	0.493

Problem 1230	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	43	47	81	58	245	103	66
normalized size	1	1.00	0.81	0.89	1.53	1.09	4.62	1.94	1.25
time (sec)	N/A	0.017	0.021	0.003	1.396	0.472	0.699	1.050	0.319

Problem 1231	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	52	52	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.015	0.012	0.072	0.000	0.478	0.000	0.000	0.000

Problem 1232	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	52	52	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.011	0.011	0.075	0.000	0.451	0.000	0.000	0.000

Problem 1233	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	53	0	0	0	124	0	-1
normalized size	1	1.00	1.29	0.00	0.00	0.00	3.02	0.00	-0.02
time (sec)	N/A	0.012	0.022	0.119	0.000	0.479	4.378	0.000	0.000

Problem 1234	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	72	0	0	0	146	0	-1
normalized size	1	1.00	1.26	0.00	0.00	0.00	2.56	0.00	-0.02
time (sec)	N/A	0.018	0.026	0.094	0.000	0.469	5.865	0.000	0.000

Problem 1235	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	0	0	0	42	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	2.10	0.00	-0.05
time (sec)	N/A	0.006	0.006	0.093	0.000	0.505	4.342	0.000	0.000

Problem 1236	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	84	97	96	97	100	97	88
normalized size	1	1.00	2.21	2.55	2.53	2.55	2.63	2.55	2.32
time (sec)	N/A	0.015	0.019	0.002	1.383	0.374	0.083	1.032	0.190

Problem 1237	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	67	73	69	72	73	72	65
normalized size	1	1.00	1.76	1.92	1.82	1.89	1.92	1.89	1.71
time (sec)	N/A	0.012	0.011	0.000	1.406	0.376	0.078	1.139	0.159

Problem 1238	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	46	49	48	49	49	49	47
normalized size	1	1.00	1.21	1.29	1.26	1.29	1.29	1.29	1.24
time (sec)	N/A	0.027	0.008	0.000	1.300	0.393	0.071	0.993	0.047

Problem 1239	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	28	25	24	26	26	26	25
normalized size	1	1.00	1.00	0.89	0.86	0.93	0.93	0.93	0.89
time (sec)	N/A	0.015	0.005	0.001	1.350	0.392	0.060	0.994	0.035

Problem 1240	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	12	12	12	11	10	10	8	10	10
normalized size	1	1.00	1.00	0.92	0.83	0.83	0.67	0.83	0.83
time (sec)	N/A	0.002	0.000	0.000	1.350	0.391	0.055	0.903	0.019

Problem 1241	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	25	25	25	32	25	24	20	26	26
normalized size	1	1.00	1.00	1.28	1.00	0.96	0.80	1.04	1.04
time (sec)	N/A	0.017	0.008	0.004	1.251	0.438	0.150	0.955	0.049

Problem 1242	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	31	39	35	39	27	57	31
normalized size	1	1.00	0.97	1.22	1.09	1.22	0.84	1.78	0.97
time (sec)	N/A	0.019	0.012	0.005	1.339	0.443	0.187	1.020	0.171

Problem 1243	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	26	35	38	38	39	24	39
normalized size	1	1.00	0.93	1.25	1.36	1.36	1.39	0.86	1.39
time (sec)	N/A	0.004	0.009	0.006	1.362	0.434	0.260	1.062	0.159

Problem 1244	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	27	35	50	50	53	25	52
normalized size	1	1.00	0.71	0.92	1.32	1.32	1.39	0.66	1.37
time (sec)	N/A	0.020	0.009	0.006	1.315	0.420	0.338	0.749	0.165

Problem 1245	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	27	35	61	61	65	41	63
normalized size	1	1.00	0.71	0.92	1.61	1.61	1.71	1.08	1.66
time (sec)	N/A	0.020	0.010	0.004	1.385	0.416	0.428	0.924	0.041

Problem 1246	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	148	163	156	170	168	170	144
normalized size	1	1.00	2.28	2.51	2.40	2.62	2.58	2.62	2.22
time (sec)	N/A	0.088	0.027	0.002	1.362	0.380	0.097	1.132	0.066

Problem 1247	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	122	125	124	130	133	130	115
normalized size	1	1.00	1.88	1.92	1.91	2.00	2.05	2.00	1.77
time (sec)	N/A	0.064	0.015	0.001	1.344	0.379	0.091	1.132	0.050

Problem 1248	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	79	87	81	89	87	89	74
normalized size	1	1.00	1.22	1.34	1.25	1.37	1.34	1.37	1.14
time (sec)	N/A	0.045	0.011	0.001	1.339	0.379	0.080	0.795	0.166

Problem 1249	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	47	49	48	49	49	49	47
normalized size	1	1.00	1.24	1.29	1.26	1.29	1.29	1.29	1.24
time (sec)	N/A	0.027	0.010	0.001	1.306	0.386	0.071	1.027	0.044

Problem 1250	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	20	20	19	12	20
normalized size	1	1.00	1.00	0.93	1.43	1.43	1.36	0.86	1.43
time (sec)	N/A	0.002	0.002	0.000	1.314	0.414	0.061	0.963	0.028

Problem 1251	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	49	49	43	74	61	63	44	60	62
normalized size	1	1.00	0.88	1.51	1.24	1.29	0.90	1.22	1.27
time (sec)	N/A	0.019	0.018	0.003	1.356	0.440	0.224	1.196	0.190

Problem 1252	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	47	86	67	92	60	98	71
normalized size	1	1.00	0.92	1.69	1.31	1.80	1.18	1.92	1.39
time (sec)	N/A	0.035	0.037	0.009	1.372	0.429	0.337	0.937	0.200

Problem 1253	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	49	92	79	99	80	68	77
normalized size	1	1.00	0.83	1.56	1.34	1.68	1.36	1.15	1.31
time (sec)	N/A	0.035	0.025	0.006	1.300	0.418	0.454	1.031	0.197

Problem 1254	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	53	70	84	84	88	59	80
normalized size	1	1.00	1.89	2.50	3.00	3.00	3.14	2.11	2.86
time (sec)	N/A	0.004	0.022	0.006	1.374	0.412	0.597	0.960	0.037

Problem 1255	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	56	71	98	98	104	96	39
normalized size	1	1.00	0.86	1.09	1.51	1.51	1.60	1.48	0.60
time (sec)	N/A	0.033	0.019	0.006	1.329	0.446	0.764	1.126	0.193

Problem 1256	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	57	71	109	109	116	61	107
normalized size	1	1.00	0.88	1.09	1.68	1.68	1.78	0.94	1.65
time (sec)	N/A	0.033	0.024	0.007	1.350	0.413	0.956	0.870	0.202

Problem 1257	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	58	71	120	120	128	61	118
normalized size	1	1.00	0.89	1.09	1.85	1.85	1.97	0.94	1.82
time (sec)	N/A	0.033	0.020	0.005	1.391	0.416	1.159	1.036	0.089

Problem 1258	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	235	281	277	303	308	303	261
normalized size	1	1.00	2.55	3.05	3.01	3.29	3.35	3.29	2.84
time (sec)	N/A	0.157	0.075	0.000	1.380	0.388	0.116	1.011	0.240

Problem 1259	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	217	229	225	245	243	245	208
normalized size	1	1.00	2.36	2.49	2.45	2.66	2.64	2.66	2.26
time (sec)	N/A	0.114	0.029	0.001	1.318	0.374	0.106	1.116	0.214

Problem 1260	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	161	177	167	188	190	188	152
normalized size	1	1.00	1.75	1.92	1.82	2.04	2.07	2.04	1.65
time (sec)	N/A	0.083	0.019	0.002	1.340	0.375	0.097	0.973	0.056

Problem 1261	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	122	125	124	130	133	130	115
normalized size	1	1.00	1.88	1.92	1.91	2.00	2.05	2.00	1.77
time (sec)	N/A	0.064	0.014	0.001	1.340	0.371	0.087	1.039	0.046

Problem 1262	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	67	73	69	72	73	72	65
normalized size	1	1.00	1.76	1.92	1.82	1.89	1.92	1.89	1.71
time (sec)	N/A	0.015	0.008	0.000	1.390	0.405	0.077	0.877	0.032

Problem 1263	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	31	31	32	12	31
normalized size	1	1.00	1.00	0.93	2.21	2.21	2.29	0.86	2.21
time (sec)	N/A	0.002	0.001	0.000	1.346	0.530	0.065	0.997	0.037

Problem 1264	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	73	73	74	133	114	116	83	115	118
normalized size	1	1.00	1.01	1.82	1.56	1.59	1.14	1.58	1.62
time (sec)	N/A	0.028	0.031	0.004	1.327	0.524	0.303	1.031	0.201

Problem 1265	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	75	75	72	149	118	173	102	167	123
normalized size	1	1.00	0.96	1.99	1.57	2.31	1.36	2.23	1.64
time (sec)	N/A	0.055	0.051	0.008	1.317	0.585	0.503	0.991	0.215

Problem 1266	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	114	160	125	188	128	112	130
normalized size	1	1.00	1.46	2.05	1.60	2.41	1.64	1.44	1.67
time (sec)	N/A	0.052	0.042	0.009	1.373	0.781	0.821	0.952	0.821

Problem 1267	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	80	166	142	176	148	118	138
normalized size	1	1.00	0.93	1.93	1.65	2.05	1.72	1.37	1.60
time (sec)	N/A	0.050	0.041	0.006	1.353	0.444	1.126	0.944	0.254

Problem 1268	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	91	122	143	143	155	159	135
normalized size	1	1.00	3.25	4.36	5.11	5.11	5.54	5.68	4.82
time (sec)	N/A	0.003	0.031	0.007	1.392	0.449	1.497	0.965	0.072

Problem 1269	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	97	121	160	160	172	114	39
normalized size	1	1.00	1.67	2.09	2.76	2.76	2.97	1.97	0.67
time (sec)	N/A	0.010	0.035	0.006	1.467	0.437	1.961	1.001	0.082

Problem 1270	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	97	122	171	171	184	114	165
normalized size	1	1.00	1.05	1.33	1.86	1.86	2.00	1.24	1.79
time (sec)	N/A	0.050	0.031	0.006	1.439	0.444	2.536	0.985	0.222

Problem 1271	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	97	122	182	182	196	114	176
normalized size	1	1.00	1.05	1.33	1.98	1.98	2.13	1.24	1.91
time (sec)	N/A	0.049	0.032	0.006	1.445	0.429	3.123	0.947	0.114

Problem 1272	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	97	122	193	193	207	114	187
normalized size	1	1.00	1.05	1.33	2.10	2.10	2.25	1.24	2.03
time (sec)	N/A	0.046	0.036	0.006	1.522	0.428	3.954	0.864	0.232

Problem 1273	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	200	200	993	1033	1023	1175	1163	1175	997
normalized size	1	1.00	4.96	5.16	5.12	5.88	5.82	5.88	4.98
time (sec)	N/A	0.676	0.147	0.002	1.431	0.378	0.232	1.046	0.554

Problem 1274	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	200	200	897	925	921	1050	1046	1050	892
normalized size	1	1.00	4.48	4.62	4.60	5.25	5.23	5.25	4.46
time (sec)	N/A	0.574	0.111	0.002	1.396	0.390	0.214	1.006	0.357

Problem 1275	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	200	200	785	817	807	924	935	924	781
normalized size	1	1.00	3.92	4.08	4.04	4.62	4.68	4.62	3.90
time (sec)	N/A	0.454	0.086	0.003	1.335	0.375	0.194	1.009	0.402

Problem 1276	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	173	173	684	709	706	798	796	798	683
normalized size	1	1.00	3.95	4.10	4.08	4.61	4.60	4.61	3.95
time (sec)	N/A	0.435	0.081	0.001	1.317	0.399	0.178	0.953	0.256

Problem 1277	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	144	144	574	601	594	670	673	670	570
normalized size	1	1.00	3.99	4.17	4.12	4.65	4.67	4.65	3.96
time (sec)	N/A	0.360	0.076	0.002	1.384	0.389	0.164	1.279	0.214

Problem 1278	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	473	493	489	546	549	546	470
normalized size	1	1.00	3.97	4.14	4.11	4.59	4.61	4.59	3.95
time (sec)	N/A	0.279	0.054	0.001	1.479	0.370	0.146	1.215	0.313

Problem 1279	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	360	385	376	420	427	420	356
normalized size	1	1.00	3.91	4.18	4.09	4.57	4.64	4.57	3.87
time (sec)	N/A	0.218	0.042	0.002	1.373	0.387	0.131	1.259	0.273

Problem 1280	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	261	277	273	294	303	294	249
normalized size	1	1.00	4.02	4.26	4.20	4.52	4.66	4.52	3.83
time (sec)	N/A	0.159	0.030	0.001	1.363	0.387	0.116	1.240	0.107

Problem 1281	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	151	169	163	169	178	169	143
normalized size	1	1.00	3.97	4.45	4.29	4.45	4.68	4.45	3.76
time (sec)	N/A	0.016	0.015	0.000	1.376	0.398	0.100	1.297	0.079

Problem 1282	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	75	83	12	75
normalized size	1	1.00	1.00	0.93	0.86	5.36	5.93	0.86	5.36
time (sec)	N/A	0.002	0.001	0.000	1.315	0.380	0.076	1.298	0.057

Problem 1283	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	169	169	304	539	460	462	408	497	509
normalized size	1	1.00	1.80	3.19	2.72	2.73	2.41	2.94	3.01
time (sec)	N/A	0.073	0.148	0.007	1.395	0.426	0.802	1.298	0.217

Problem 1284	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	187	187	388	571	467	632	428	567	841
normalized size	1	1.00	2.07	3.05	2.50	3.38	2.29	3.03	4.50
time (sec)	N/A	0.235	0.123	0.011	1.403	0.423	1.445	1.281	0.241

Problem 1285	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	185	185	389	599	473	703	447	477	690
normalized size	1	1.00	2.10	3.24	2.56	3.80	2.42	2.58	3.73
time (sec)	N/A	0.217	0.132	0.014	1.538	0.434	2.949	1.265	0.266

Problem 1286	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	187	187	199	622	484	739	474	470	559
normalized size	1	1.00	1.06	3.33	2.59	3.95	2.53	2.51	2.99
time (sec)	N/A	0.213	0.109	0.014	1.628	0.436	6.124	1.318	0.289

Problem 1287	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	187	187	173	641	494	754	500	660	512
normalized size	1	1.00	0.93	3.43	2.64	4.03	2.67	3.53	2.74
time (sec)	N/A	0.198	0.112	0.015	1.734	0.446	22.438	1.287	0.772

Problem 1288	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	181	181	389	656	504	732	524	463	508
normalized size	1	1.00	2.15	3.62	2.78	4.04	2.90	2.56	2.81
time (sec)	N/A	0.191	0.153	0.014	1.817	0.428	97.193	1.381	0.339

Problem 1289	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	186	186	390	666	516	692	0	459	517
normalized size	1	1.00	2.10	3.58	2.77	3.72	0.00	2.47	2.78
time (sec)	N/A	0.172	0.204	0.013	1.799	0.437	0.000	1.298	0.369

Problem 1290	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	194	194	308	672	534	624	0	466	461
normalized size	1	1.00	1.59	3.46	2.75	3.22	0.00	2.40	2.38
time (sec)	N/A	0.156	0.163	0.010	1.648	0.430	0.000	1.281	0.353

Problem 1291	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	353	464	509	509	0	489	571
normalized size	1	1.00	12.61	16.57	18.18	18.18	0.00	17.46	20.39
time (sec)	N/A	0.003	0.125	0.008	1.650	0.429	0.000	1.290	0.169

Problem 1292	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	367	464	548	548	0	496	39
normalized size	1	1.00	6.33	8.00	9.45	9.45	0.00	8.55	0.67
time (sec)	N/A	0.009	0.126	0.009	1.709	0.413	0.000	1.272	0.146

Problem 1293	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	371	464	559	559	0	496	600
normalized size	1	1.00	4.17	5.21	6.28	6.28	0.00	5.57	6.74
time (sec)	N/A	0.022	0.123	0.008	1.731	0.432	0.000	1.311	0.446

Problem 1294	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	120	120	369	464	570	570	0	496	548
normalized size	1	1.00	3.08	3.87	4.75	4.75	0.00	4.13	4.57
time (sec)	N/A	0.033	0.122	0.005	1.812	0.460	0.000	1.303	0.518

Problem 1295	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	151	151	371	464	581	581	0	496	559
normalized size	1	1.00	2.46	3.07	3.85	3.85	0.00	3.28	3.70
time (sec)	N/A	0.047	0.129	0.008	1.757	0.442	0.000	1.264	0.229

Problem 1296	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	198	198	369	463	592	592	0	496	570
normalized size	1	1.00	1.86	2.34	2.99	2.99	0.00	2.51	2.88
time (sec)	N/A	0.153	0.127	0.009	1.745	0.435	0.000	1.237	0.399

Problem 1297	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	200	200	371	464	603	603	0	496	581
normalized size	1	1.00	1.86	2.32	3.02	3.02	0.00	2.48	2.90
time (sec)	N/A	0.143	0.127	0.008	1.835	0.427	0.000	1.285	1.238

Problem 1298	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	200	200	371	464	614	614	0	496	592
normalized size	1	1.00	1.86	2.32	3.07	3.07	0.00	2.48	2.96
time (sec)	N/A	0.140	0.128	0.006	1.911	0.443	0.000	1.288	2.196

Problem 1299	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	275	275	1817	1891	1877	2186	2088	2186	1847
normalized size	1	1.00	6.61	6.88	6.83	7.95	7.59	7.95	6.72
time (sec)	N/A	1.465	0.290	0.003	1.546	0.395	0.372	1.314	0.984

Problem 1300	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	279	279	1702	1741	1740	2010	1965	2010	1702
normalized size	1	1.00	6.10	6.24	6.24	7.20	7.04	7.20	6.10
time (sec)	N/A	1.275	0.226	0.004	1.575	0.396	0.344	1.352	1.026

Problem 1301	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	279	279	1539	1591	1581	1833	1775	1833	1549
normalized size	1	1.00	5.52	5.70	5.67	6.57	6.36	6.57	5.55
time (sec)	N/A	1.112	0.173	0.002	1.555	0.385	0.313	1.343	0.689

Problem 1302	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	250	250	1397	1441	1437	1656	1598	1656	1404
normalized size	1	1.00	5.59	5.76	5.75	6.62	6.39	6.62	5.62
time (sec)	N/A	1.042	0.185	0.003	1.508	0.388	0.296	1.298	0.788

Problem 1303	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	225	225	1241	1291	1283	1478	1428	1478	1253
normalized size	1	1.00	5.52	5.74	5.70	6.57	6.35	6.57	5.57
time (sec)	N/A	0.899	0.161	0.002	1.512	0.417	0.273	1.290	0.707

Problem 1304	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	200	200	1105	1141	1135	1302	1280	1302	1106
normalized size	1	1.00	5.52	5.70	5.68	6.51	6.40	6.51	5.53
time (sec)	N/A	0.766	0.136	0.001	1.520	0.389	0.246	1.260	0.613

Problem 1305	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	170	170	939	991	977	1124	1088	1124	953
normalized size	1	1.00	5.52	5.83	5.75	6.61	6.40	6.61	5.61
time (sec)	N/A	0.673	0.124	0.001	1.439	0.393	0.227	1.296	0.532

Problem 1306	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	146	146	811	841	835	948	940	948	806
normalized size	1	1.00	5.55	5.76	5.72	6.49	6.44	6.49	5.52
time (sec)	N/A	0.529	0.088	0.003	1.465	0.373	0.209	1.316	0.341

Problem 1307	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	660	691	686	771	748	771	664
normalized size	1	1.00	5.55	5.81	5.76	6.48	6.29	6.48	5.58
time (sec)	N/A	0.437	0.079	0.002	1.423	0.386	0.183	1.270	0.426

Problem 1308	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	511	541	535	594	586	594	495
normalized size	1	1.00	5.55	5.88	5.82	6.46	6.37	6.46	5.38
time (sec)	N/A	0.349	0.065	0.002	1.324	0.386	0.162	1.275	0.231

Problem 1309	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	358	391	384	417	415	417	348
normalized size	1	1.00	5.51	6.02	5.91	6.42	6.38	6.42	5.35
time (sec)	N/A	0.251	0.046	0.001	1.332	0.393	0.145	1.263	0.320

Problem 1310	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	220	241	240	241	248	241	208
normalized size	1	1.00	5.79	6.34	6.32	6.34	6.53	6.34	5.47
time (sec)	N/A	0.016	0.029	0.001	1.434	0.385	0.119	1.265	0.129

Problem 1311	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	108	114	12	108
normalized size	1	1.00	1.00	0.93	0.86	7.71	8.14	0.86	7.71
time (sec)	N/A	0.002	0.001	0.001	1.371	0.363	0.088	1.278	0.080

Problem 1312	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	241	241	591	1022	866	868	799	961	979
normalized size	1	1.00	2.45	4.24	3.59	3.60	3.32	3.99	4.06
time (sec)	N/A	0.098	0.339	0.009	1.523	0.446	1.415	1.345	0.130

Problem 1313	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	258	258	708	1066	874	1124	816	1012	3475
normalized size	1	1.00	2.74	4.13	3.39	4.36	3.16	3.92	13.47
time (sec)	N/A	0.473	0.240	0.016	1.395	0.443	2.653	1.265	0.352

Problem 1314	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	262	262	708	1105	881	1233	843	924	3299
normalized size	1	1.00	2.70	4.22	3.36	4.71	3.22	3.53	12.59
time (sec)	N/A	0.444	0.241	0.018	1.621	0.460	5.671	1.252	0.378

Problem 1315	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	258	258	427	1141	891	1316	867	907	2219
normalized size	1	1.00	1.66	4.42	3.45	5.10	3.36	3.52	8.60
time (sec)	N/A	0.441	0.179	0.022	1.730	0.457	32.528	1.261	0.385

Problem 1316	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	262	262	359	1172	903	1365	0	1168	1494
normalized size	1	1.00	1.37	4.47	3.45	5.21	0.00	4.46	5.70
time (sec)	N/A	0.422	0.196	0.020	1.932	0.472	0.000	1.379	0.381

Problem 1317	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	260	260	305	1199	912	1395	0	883	1141
normalized size	1	1.00	1.17	4.61	3.51	5.37	0.00	3.40	4.39
time (sec)	N/A	0.421	0.214	0.023	2.253	0.449	0.000	1.339	0.396

Problem 1318	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	262	262	265	1222	925	1386	0	878	997
normalized size	1	1.00	1.01	4.66	3.53	5.29	0.00	3.35	3.81
time (sec)	N/A	0.387	0.219	0.021	2.451	0.445	0.000	1.290	0.422

Problem 1319	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	258	258	239	1241	934	1362	0	872	950
normalized size	1	1.00	0.93	4.81	3.62	5.28	0.00	3.38	3.68
time (sec)	N/A	0.365	0.249	0.022	2.444	0.463	0.000	1.258	0.428

Problem 1320	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	258	258	712	1256	945	1296	0	871	946
normalized size	1	1.00	2.76	4.87	3.66	5.02	0.00	3.38	3.67
time (sec)	N/A	0.341	0.317	0.019	2.584	0.451	0.000	1.292	0.263

Problem 1321	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	257	257	708	1266	957	1216	0	867	955
normalized size	1	1.00	2.75	4.93	3.72	4.73	0.00	3.37	3.72
time (sec)	N/A	0.311	0.424	0.018	2.362	0.470	0.000	1.248	0.502

Problem 1322	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	271	271	591	1271	975	1107	0	874	866
normalized size	1	1.00	2.18	4.69	3.60	4.08	0.00	3.23	3.20
time (sec)	N/A	0.287	0.361	0.013	2.014	0.441	0.000	1.357	0.555

Problem 1323	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	665	866	920	920	0	951	1066
normalized size	1	1.00	23.75	30.93	32.86	32.86	0.00	33.96	38.07
time (sec)	N/A	0.003	0.285	0.007	2.128	0.453	0.000	1.355	0.458

Problem 1324	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	684	867	986	986	0	961	39
normalized size	1	1.00	11.79	14.95	17.00	17.00	0.00	16.57	0.67
time (sec)	N/A	0.010	0.281	0.009	2.167	0.461	0.000	1.322	0.394

Problem 1325	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	690	867	997	997	0	961	1098
normalized size	1	1.00	7.75	9.74	11.20	11.20	0.00	10.80	12.34
time (sec)	N/A	0.020	0.294	0.009	2.208	0.445	0.000	1.283	0.475

Problem 1326	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	120	120	692	867	1008	1008	0	961	1109
normalized size	1	1.00	5.77	7.22	8.40	8.40	0.00	8.01	9.24
time (sec)	N/A	0.030	0.287	0.009	2.160	0.462	0.000	1.393	1.295

Problem 1327	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	151	151	690	867	1019	1019	0	961	1120
normalized size	1	1.00	4.57	5.74	6.75	6.75	0.00	6.36	7.42
time (sec)	N/A	0.044	0.288	0.009	2.257	0.499	0.000	1.319	2.279

Problem 1328	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	182	182	694	867	1030	1030	0	961	1131
normalized size	1	1.00	3.81	4.76	5.66	5.66	0.00	5.28	6.21
time (sec)	N/A	0.063	0.280	0.009	2.266	0.477	0.000	1.311	0.584

Problem 1329	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	213	213	690	867	1041	1041	0	961	1142
normalized size	1	1.00	3.24	4.07	4.89	4.89	0.00	4.51	5.36
time (sec)	N/A	0.079	0.323	0.010	2.293	0.483	0.000	1.322	0.658

Problem 1330	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	244	244	694	867	1052	1052	0	961	1153
normalized size	1	1.00	2.84	3.55	4.31	4.31	0.00	3.94	4.73
time (sec)	N/A	0.105	0.279	0.009	2.545	0.435	0.000	1.403	12.020

Problem 1331	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	273	273	692	866	1063	1063	0	961	1164
normalized size	1	1.00	2.53	3.17	3.89	3.89	0.00	3.52	4.26
time (sec)	N/A	0.284	0.282	0.009	2.454	0.465	0.000	1.310	25.721

Problem 1332	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	279	279	692	867	1074	1074	0	961	1175
normalized size	1	1.00	2.48	3.11	3.85	3.85	0.00	3.44	4.21
time (sec)	N/A	0.272	0.288	0.009	2.509	0.483	0.000	1.308	0.799

Problem 1333	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	279	279	692	867	1085	1085	0	961	1186
normalized size	1	1.00	2.48	3.11	3.89	3.89	0.00	3.44	4.25
time (sec)	N/A	0.271	0.301	0.008	2.457	0.465	0.000	1.301	1.036

Problem 1334	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	122	122	167	302	258	259	209	273	280
normalized size	1	1.00	1.37	2.48	2.11	2.12	1.71	2.24	2.30
time (sec)	N/A	0.053	0.072	0.005	1.350	0.440	0.500	1.260	0.074

Problem 1335	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	115	209	177	179	136	184	189
normalized size	1	1.00	1.17	2.13	1.81	1.83	1.39	1.88	1.93
time (sec)	N/A	0.038	0.044	0.005	1.405	0.449	0.392	1.228	0.218

Problem 1336	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	74	133	114	115	83	116	118
normalized size	1	1.00	1.00	1.80	1.54	1.55	1.12	1.57	1.59
time (sec)	N/A	0.030	0.028	0.004	1.301	0.433	0.299	1.200	0.065

Problem 1337	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	43	74	60	62	44	60	62
normalized size	1	1.00	0.86	1.48	1.20	1.24	0.88	1.20	1.24
time (sec)	N/A	0.021	0.017	0.003	1.354	0.428	0.219	1.210	0.225

Problem 1338	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	25	32	26	25	20	27	25
normalized size	1	1.00	0.96	1.23	1.00	0.96	0.77	1.04	0.96
time (sec)	N/A	0.018	0.008	0.003	1.319	0.480	0.148	1.200	0.201

Problem 1339	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	10	10	10	11	10	10	7	11	10
normalized size	1	1.00	1.00	1.10	1.00	1.00	0.70	1.10	1.00
time (sec)	N/A	0.001	0.001	0.001	1.304	0.418	0.062	1.261	0.022

Problem 1340	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	26	37	36	26	128	46	25
normalized size	1	1.00	0.72	1.03	1.00	0.72	3.56	1.28	0.69
time (sec)	N/A	0.008	0.013	0.006	1.360	0.448	0.328	1.243	0.258

Problem 1341	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	53	57	92	93	233	78	46
normalized size	1	1.00	0.93	1.00	1.61	1.63	4.09	1.37	0.81
time (sec)	N/A	0.032	0.025	0.008	1.363	0.460	0.682	1.316	0.142

Problem 1342	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	67	81	202	242	381	165	182
normalized size	1	1.00	0.82	0.99	2.46	2.95	4.65	2.01	2.22
time (sec)	N/A	0.045	0.066	0.009	1.411	0.463	1.064	1.294	0.161

Problem 1343	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	130	130	228	326	264	373	231	339	327
normalized size	1	1.00	1.75	2.51	2.03	2.87	1.78	2.61	2.52
time (sec)	N/A	0.139	0.075	0.010	1.398	0.440	0.886	1.267	0.245

Problem 1344	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	104	104	165	230	183	267	155	245	203
normalized size	1	1.00	1.59	2.21	1.76	2.57	1.49	2.36	1.95
time (sec)	N/A	0.100	0.057	0.009	1.357	0.458	0.680	1.265	0.073

Problem 1345	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	75	75	114	149	117	172	102	166	123
normalized size	1	1.00	1.52	1.99	1.56	2.29	1.36	2.21	1.64
time (sec)	N/A	0.062	0.036	0.009	1.357	0.444	0.506	1.264	0.077

Problem 1346	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	47	86	67	92	60	98	71
normalized size	1	1.00	0.92	1.69	1.31	1.80	1.18	1.92	1.39
time (sec)	N/A	0.039	0.037	0.007	1.351	0.447	0.338	1.246	0.236

Problem 1347	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	31	39	34	37	27	57	32
normalized size	1	1.00	1.00	1.26	1.10	1.19	0.87	1.84	1.03
time (sec)	N/A	0.021	0.011	0.006	1.337	0.434	0.185	1.262	0.041

Problem 1348	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	12	12	12	13	12	13	10	12	12
normalized size	1	1.00	1.00	1.08	1.00	1.08	0.83	1.00	1.00
time (sec)	N/A	0.002	0.003	0.001	1.285	0.423	0.128	1.229	0.187

Problem 1349	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	53	58	90	92	233	77	47
normalized size	1	1.00	0.95	1.04	1.61	1.64	4.16	1.38	0.84
time (sec)	N/A	0.032	0.029	0.008	1.321	0.457	0.684	1.342	0.292

Problem 1350	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	66	82	208	241	406	153	74
normalized size	1	1.00	0.81	1.01	2.57	2.98	5.01	1.89	0.91
time (sec)	N/A	0.050	0.071	0.008	1.429	0.454	1.113	1.207	0.334

Problem 1351	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	109	109	98	109	386	494	634	216	330
normalized size	1	1.00	0.90	1.00	3.54	4.53	5.82	1.98	3.03
time (sec)	N/A	0.076	0.074	0.013	1.555	0.460	1.717	1.347	0.396

Problem 1352	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	158	158	303	464	364	548	340	362	441
normalized size	1	1.00	1.92	2.94	2.30	3.47	2.15	2.29	2.79
time (sec)	N/A	0.202	0.113	0.011	1.474	0.439	2.154	1.276	0.274

Problem 1353	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	133	133	230	346	271	416	258	264	291
normalized size	1	1.00	1.73	2.60	2.04	3.13	1.94	1.98	2.19
time (sec)	N/A	0.121	0.073	0.009	1.476	0.476	1.650	1.288	0.099

Problem 1354	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	103	103	167	245	191	291	185	183	196
normalized size	1	1.00	1.62	2.38	1.85	2.83	1.80	1.78	1.90
time (sec)	N/A	0.087	0.056	0.008	1.386	0.450	1.246	1.354	0.099

Problem 1355	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	114	160	125	188	128	112	130
normalized size	1	1.00	1.46	2.05	1.60	2.41	1.64	1.44	1.67
time (sec)	N/A	0.055	0.039	0.009	1.340	0.429	0.827	1.276	0.109

Problem 1356	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	48	92	80	100	80	69	77
normalized size	1	1.00	0.81	1.56	1.36	1.69	1.36	1.17	1.31
time (sec)	N/A	0.038	0.025	0.006	1.327	0.443	0.450	1.299	0.228

Problem 1357	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	26	35	38	38	39	24	39
normalized size	1	1.00	0.93	1.25	1.36	1.36	1.39	0.86	1.39
time (sec)	N/A	0.003	0.009	0.004	1.359	0.446	0.263	1.251	0.029

Problem 1358	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	24	26	12	26
normalized size	1	1.00	1.00	0.93	0.86	1.71	1.86	0.86	1.86
time (sec)	N/A	0.002	0.003	0.000	1.335	0.427	0.182	1.203	0.024

Problem 1359	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	67	81	202	242	381	165	183
normalized size	1	1.00	0.82	0.99	2.46	2.95	4.65	2.01	2.23
time (sec)	N/A	0.046	0.053	0.010	1.452	0.441	1.074	1.360	0.299

Problem 1360	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	110	110	97	108	386	495	632	217	329
normalized size	1	1.00	0.88	0.98	3.51	4.50	5.75	1.97	2.99
time (sec)	N/A	0.074	0.105	0.013	1.594	0.466	1.720	1.265	0.395

Problem 1361	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	143	143	128	140	594	760	881	345	542
normalized size	1	1.00	0.90	0.98	4.15	5.31	6.16	2.41	3.79
time (sec)	N/A	0.102	0.116	0.012	1.551	0.470	2.419	1.277	0.526

Problem 1362	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	232	232	584	1035	786	1093	0	723	784
normalized size	1	1.00	2.52	4.46	3.39	4.71	0.00	3.12	3.38
time (sec)	N/A	0.357	0.271	0.017	2.198	0.563	0.000	1.321	0.257

Problem 1363	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	209	209	474	845	649	852	0	581	649
normalized size	1	1.00	2.27	4.04	3.11	4.08	0.00	2.78	3.11
time (sec)	N/A	0.278	0.204	0.013	1.959	0.480	0.000	1.268	0.430

Problem 1364	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	194	194	308	672	535	625	0	467	460
normalized size	1	1.00	1.59	3.46	2.76	3.22	0.00	2.41	2.37
time (sec)	N/A	0.209	0.162	0.009	1.662	0.549	0.000	1.298	0.383

Problem 1365	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	271	357	398	398	0	369	378
normalized size	1	1.00	9.68	12.75	14.21	14.21	0.00	13.18	13.50
time (sec)	N/A	0.003	0.090	0.007	1.606	0.473	0.000	1.282	0.146

Problem 1366	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	58	58	205	265	326	326	354	271	39
normalized size	1	1.00	3.53	4.57	5.62	5.62	6.10	4.67	0.67
time (sec)	N/A	0.011	0.060	0.008	1.579	0.430	54.908	1.317	0.277

Problem 1367	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	89	89	144	186	247	247	267	184	237
normalized size	1	1.00	1.62	2.09	2.78	2.78	3.00	2.07	2.66
time (sec)	N/A	0.019	0.048	0.006	1.517	0.442	9.645	1.294	0.110

Problem 1368	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	94	122	182	182	196	114	176
normalized size	1	1.00	1.02	1.33	1.98	1.98	2.13	1.24	1.91
time (sec)	N/A	0.057	0.029	0.007	1.469	0.417	3.101	1.240	0.099

Problem 1369	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	55	71	131	131	139	61	129
normalized size	1	1.00	0.85	1.09	2.02	2.02	2.14	0.94	1.98
time (sec)	N/A	0.040	0.024	0.005	1.456	0.433	1.391	1.222	0.086

Problem 1370	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	27	35	94	94	100	25	96
normalized size	1	1.00	0.71	0.92	2.47	2.47	2.63	0.66	2.53
time (sec)	N/A	0.022	0.010	0.006	1.380	0.431	0.731	1.309	0.226

Problem 1371	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	79	85	12	81
normalized size	1	1.00	1.00	0.93	0.86	5.64	6.07	0.86	5.79
time (sec)	N/A	0.002	0.003	0.000	1.365	0.433	0.456	1.257	0.223

Problem 1372	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	202	202	196	192	1418	1589	1776	703	1299
normalized size	1	1.00	0.97	0.95	7.02	7.87	8.79	3.48	6.43
time (sec)	N/A	0.169	0.097	0.016	2.975	0.516	4.488	1.333	0.873

Problem 1373	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	231	231	213	223	1881	2264	2336	714	1738
normalized size	1	1.00	0.92	0.97	8.14	9.80	10.11	3.09	7.52
time (sec)	N/A	0.270	0.243	0.020	3.883	0.544	7.745	1.370	1.386

Problem 1374	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	276	276	254	265	2399	3016	2917	1029	2224
normalized size	1	1.00	0.92	0.96	8.69	10.93	10.57	3.73	8.06
time (sec)	N/A	0.356	0.205	0.020	5.223	0.555	20.658	1.493	1.911

Problem 1375	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	156	156	123	273	259	338	314	641	137
normalized size	1	1.00	0.79	1.75	1.66	2.17	2.01	4.11	0.88
time (sec)	N/A	0.063	0.145	0.008	1.425	0.451	5.117	1.378	0.081

Problem 1376	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	129	129	101	186	181	245	223	470	112
normalized size	1	1.00	0.78	1.44	1.40	1.90	1.73	3.64	0.87
time (sec)	N/A	0.052	0.095	0.007	1.365	0.433	4.195	1.249	0.225

Problem 1377	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	79	116	118	164	146	322	87
normalized size	1	1.00	0.79	1.16	1.18	1.64	1.46	3.22	0.87
time (sec)	N/A	0.036	0.063	0.005	1.374	0.431	3.336	1.275	0.065

Problem 1378	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	61	63	68	99	85	200	68
normalized size	1	1.00	0.86	0.89	0.96	1.39	1.20	2.82	0.96
time (sec)	N/A	0.025	0.038	0.007	1.350	0.451	2.695	1.291	0.240

Problem 1379	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	30	27	33	46	36	100	29
normalized size	1	1.00	0.71	0.64	0.79	1.10	0.86	2.38	0.69
time (sec)	N/A	0.014	0.019	0.004	1.294	0.424	2.123	1.372	0.043

Problem 1380	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	12	12	12	12
normalized size	1	1.00	1.00	0.81	0.75	0.75	0.75	0.75	0.75
time (sec)	N/A	0.002	0.004	0.002	1.350	0.439	0.060	1.342	0.021

Problem 1381	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	62	62	62	92	0	143	61	62	50
normalized size	1	1.00	1.00	1.48	0.00	2.31	0.98	1.00	0.81
time (sec)	N/A	0.053	0.038	0.011	0.000	0.467	4.389	1.265	0.066

Problem 1382	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	69	64	0	232	573	72	61
normalized size	1	1.00	0.99	0.91	0.00	3.31	8.19	1.03	0.87
time (sec)	N/A	0.030	0.081	0.013	0.000	0.453	58.580	1.380	0.242

Problem 1383	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	110	110	52	111	0	456	0	126	135
normalized size	1	1.00	0.47	1.01	0.00	4.15	0.00	1.15	1.23
time (sec)	N/A	0.078	0.016	0.013	0.000	0.461	0.000	1.331	0.302

Problem 1384	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	146	146	52	170	0	785	0	207	207
normalized size	1	1.00	0.36	1.16	0.00	5.38	0.00	1.42	1.42
time (sec)	N/A	0.098	0.014	0.015	0.000	0.455	0.000	1.350	0.374

Problem 1385	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	182	182	52	248	0	1176	0	311	297
normalized size	1	1.00	0.29	1.36	0.00	6.46	0.00	1.71	1.63
time (sec)	N/A	0.123	0.015	0.016	0.000	0.475	0.000	1.386	0.217

Problem 1386	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	218	218	52	337	0	1673	0	432	401
normalized size	1	1.00	0.24	1.55	0.00	7.67	0.00	1.98	1.84
time (sec)	N/A	0.151	0.016	0.018	0.000	0.498	0.000	1.473	0.490

Problem 1387	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	158	158	123	273	259	418	763	1084	137
normalized size	1	1.00	0.78	1.73	1.64	2.65	4.83	6.86	0.87
time (sec)	N/A	0.053	0.146	0.007	1.346	0.437	26.419	1.532	0.244

Problem 1388	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	129	129	101	186	181	311	559	807	112
normalized size	1	1.00	0.78	1.44	1.40	2.41	4.33	6.26	0.87
time (sec)	N/A	0.042	0.097	0.007	1.355	0.444	20.089	1.403	0.242

Problem 1389	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	79	116	118	216	386	566	87
normalized size	1	1.00	0.79	1.16	1.18	2.16	3.86	5.66	0.87
time (sec)	N/A	0.034	0.069	0.006	1.359	0.427	14.380	1.311	0.249

Problem 1390	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	61	63	68	137	240	360	68
normalized size	1	1.00	0.86	0.89	0.96	1.93	3.38	5.07	0.96
time (sec)	N/A	0.024	0.043	0.006	1.378	0.429	9.606	1.413	0.059

Problem 1391	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	30	27	33	69	146	192	29
normalized size	1	1.00	0.71	0.64	0.79	1.64	3.48	4.57	0.69
time (sec)	N/A	0.014	0.021	0.003	1.374	0.442	0.666	1.227	0.215

Problem 1392	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	28	12	58	12
normalized size	1	1.00	1.00	0.81	0.75	1.75	0.75	3.62	0.75
time (sec)	N/A	0.001	0.005	0.002	1.359	0.422	0.061	1.244	0.017

Problem 1393	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	77	167	0	188	82	105	93
normalized size	1	1.00	0.90	1.94	0.00	2.19	0.95	1.22	1.08
time (sec)	N/A	0.046	0.073	0.009	0.000	0.468	14.700	1.287	0.075

Problem 1394	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	F(-2)	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	85	85	50	148	0	210	0	113	109
normalized size	1	1.00	0.59	1.74	0.00	2.47	0.00	1.33	1.28
time (sec)	N/A	0.038	0.014	0.013	0.000	0.475	0.000	1.299	0.105

Problem 1395	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	90	121	0	383	0	108	135
normalized size	1	1.00	0.90	1.21	0.00	3.83	0.00	1.08	1.35
time (sec)	N/A	0.048	0.100	0.013	0.000	0.463	0.000	1.357	0.284

Problem 1396	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	52	163	0	666	0	185	209
normalized size	1	1.00	0.38	1.20	0.00	4.90	0.00	1.36	1.54
time (sec)	N/A	0.057	0.017	0.015	0.000	0.499	0.000	1.400	0.338

Problem 1397	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	172	172	52	222	0	1043	0	285	296
normalized size	1	1.00	0.30	1.29	0.00	6.06	0.00	1.66	1.72
time (sec)	N/A	0.074	0.016	0.017	0.000	0.493	0.000	1.467	0.371

Problem 1398	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	208	208	52	300	0	1492	0	410	398
normalized size	1	1.00	0.25	1.44	0.00	7.17	0.00	1.97	1.91
time (sec)	N/A	0.093	0.017	0.017	0.000	0.478	0.000	1.392	0.473

Problem 1399	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	158	158	123	273	259	497	1292	1599	137
normalized size	1	1.00	0.78	1.73	1.64	3.15	8.18	10.12	0.87
time (sec)	N/A	0.051	0.114	0.005	1.362	0.444	43.079	1.522	0.267

Problem 1400	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	129	129	101	186	181	377	960	1204	112
normalized size	1	1.00	0.78	1.44	1.40	2.92	7.44	9.33	0.87
time (sec)	N/A	0.043	0.110	0.007	1.332	0.451	33.636	1.447	0.234

Problem 1401	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	79	116	118	268	549	857	87
normalized size	1	1.00	0.79	1.16	1.18	2.68	5.49	8.57	0.87
time (sec)	N/A	0.031	0.072	0.007	1.402	0.419	4.609	1.579	0.076

Problem 1402	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	61	63	68	174	355	558	68
normalized size	1	1.00	0.86	0.89	0.96	2.45	5.00	7.86	0.96
time (sec)	N/A	0.023	0.046	0.007	1.381	0.430	3.579	1.764	0.067

Problem 1403	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	30	27	33	93	194	306	29
normalized size	1	1.00	0.71	0.64	0.79	2.21	4.62	7.29	0.69
time (sec)	N/A	0.015	0.024	0.003	1.395	0.443	2.363	1.615	0.045

Problem 1404	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	39	12	95	12
normalized size	1	1.00	1.00	0.81	0.75	2.44	0.75	5.94	0.75
time (sec)	N/A	0.001	0.006	0.002	1.296	0.424	0.065	1.781	0.021

Problem 1405	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	112	112	105	263	0	290	121	171	130
normalized size	1	1.00	0.94	2.35	0.00	2.59	1.08	1.53	1.16
time (sec)	N/A	0.058	0.155	0.008	0.000	0.497	27.012	1.598	0.083

Problem 1406	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	F(-2)	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	110	110	50	258	0	330	0	181	161
normalized size	1	1.00	0.45	2.35	0.00	3.00	0.00	1.65	1.46
time (sec)	N/A	0.055	0.015	0.014	0.000	0.478	0.000	1.277	0.124

Problem 1407	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	F(-2)	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	52	238	0	344	0	171	199
normalized size	1	1.00	0.44	2.00	0.00	2.89	0.00	1.44	1.67
time (sec)	N/A	0.049	0.018	0.016	0.000	0.471	0.000	1.242	0.160

Problem 1408	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	119	204	0	563	0	161	222
normalized size	1	1.00	0.94	1.62	0.00	4.47	0.00	1.28	1.76
time (sec)	N/A	0.050	0.152	0.015	0.000	0.494	0.000	0.985	0.365

Problem 1409	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	162	162	52	246	0	894	0	259	309
normalized size	1	1.00	0.32	1.52	0.00	5.52	0.00	1.60	1.91
time (sec)	N/A	0.070	0.018	0.015	0.000	0.479	0.000	1.091	0.412

Problem 1410	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	198	198	52	305	0	1337	0	380	411
normalized size	1	1.00	0.26	1.54	0.00	6.75	0.00	1.92	2.08
time (sec)	N/A	0.092	0.018	0.018	0.000	0.473	0.000	1.251	0.503

Problem 1411	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	51	30	29	33	104	29	29
normalized size	1	1.00	1.46	0.86	0.83	0.94	2.97	0.83	0.83
time (sec)	N/A	0.008	0.030	0.010	2.970	0.442	1.498	0.962	0.062

Problem 1412	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	28	40	43	46	167	37	45
normalized size	1	1.00	0.50	0.71	0.77	0.82	2.98	0.66	0.80
time (sec)	N/A	0.013	0.005	0.010	3.033	0.473	2.609	1.036	0.041

Problem 1413	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	154	154	123	273	283	261	728	283	137
normalized size	1	1.00	0.80	1.77	1.84	1.69	4.73	1.84	0.89
time (sec)	N/A	0.051	0.088	0.007	1.383	0.450	79.908	1.066	0.069

Problem 1414	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	127	127	101	186	204	182	532	204	112
normalized size	1	1.00	0.80	1.46	1.61	1.43	4.19	1.61	0.88
time (sec)	N/A	0.041	0.088	0.006	1.381	0.434	56.898	0.959	0.241

Problem 1415	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	79	116	137	115	366	137	87
normalized size	1	1.00	0.82	1.21	1.43	1.20	3.81	1.43	0.91
time (sec)	N/A	0.031	0.056	0.006	1.378	0.426	37.064	1.010	0.264

Problem 1416	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	60	63	82	64	231	82	68
normalized size	1	1.00	0.87	0.91	1.19	0.93	3.35	1.19	0.99
time (sec)	N/A	0.021	0.035	0.005	1.369	0.457	20.940	1.099	0.067

Problem 1417	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	29	26	39	25	121	39	28
normalized size	1	1.00	0.72	0.65	0.98	0.62	3.02	0.98	0.70
time (sec)	N/A	0.013	0.017	0.003	1.345	0.421	4.778	0.884	0.048

Problem 1418	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	12	10	12	12
normalized size	1	1.00	1.00	0.93	0.86	0.86	0.71	0.86	0.86
time (sec)	N/A	0.001	0.003	0.001	1.298	0.431	0.063	0.909	0.021

Problem 1419	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	47	37	0	119	44	38	38
normalized size	1	1.00	1.00	0.79	0.00	2.53	0.94	0.81	0.81
time (sec)	N/A	0.020	0.015	0.006	0.000	0.439	5.409	0.879	0.273

Problem 1420	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	76	76	76	77	0	280	0	87	74
normalized size	1	1.00	1.00	1.01	0.00	3.68	0.00	1.14	0.97
time (sec)	N/A	0.027	0.071	0.010	0.000	0.449	0.000	1.030	0.094

Problem 1421	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	114	114	50	115	0	549	0	148	142
normalized size	1	1.00	0.44	1.01	0.00	4.82	0.00	1.30	1.25
time (sec)	N/A	0.037	0.011	0.009	0.000	0.470	0.000	0.933	0.332

Problem 1422	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	147	147	50	147	0	884	0	231	218
normalized size	1	1.00	0.34	1.00	0.00	6.01	0.00	1.57	1.48
time (sec)	N/A	0.050	0.011	0.008	0.000	0.468	0.000	1.020	0.395

Problem 1423	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	180	180	50	179	0	1325	0	331	307
normalized size	1	1.00	0.28	0.99	0.00	7.36	0.00	1.84	1.71
time (sec)	N/A	0.065	0.012	0.010	0.000	0.485	0.000	1.134	0.455

Problem 1424	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	152	152	123	273	267	271	243	350	192
normalized size	1	1.00	0.81	1.80	1.76	1.78	1.60	2.30	1.26
time (sec)	N/A	0.049	0.120	0.006	1.556	0.421	47.937	1.008	0.077

Problem 1425	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	123	123	101	186	189	192	168	240	153
normalized size	1	1.00	0.82	1.51	1.54	1.56	1.37	1.95	1.24
time (sec)	N/A	0.037	0.080	0.007	1.353	0.415	32.865	1.082	0.056

Problem 1426	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	94	94	78	116	125	124	109	152	114
normalized size	1	1.00	0.83	1.23	1.33	1.32	1.16	1.62	1.21
time (sec)	N/A	0.030	0.056	0.006	1.381	0.427	21.510	1.049	0.082

Problem 1427	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	59	63	75	73	65	84	67
normalized size	1	1.00	0.88	0.94	1.12	1.09	0.97	1.25	1.00
time (sec)	N/A	0.021	0.031	0.005	1.300	0.459	13.292	1.041	0.264

Problem 1428	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	27	26	37	35	60	34	25
normalized size	1	1.00	0.71	0.68	0.97	0.92	1.58	0.89	0.66
time (sec)	N/A	0.014	0.019	0.003	1.332	0.430	0.614	1.027	0.054

Problem 1429	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	20	12	12	12
normalized size	1	1.00	1.00	0.93	0.86	1.43	0.86	0.86	0.86
time (sec)	N/A	0.002	0.004	0.003	1.331	0.447	0.064	1.020	0.024

Problem 1430	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	46	68	0	214	60	69	57
normalized size	1	1.00	0.67	0.99	0.00	3.10	0.87	1.00	0.83
time (sec)	N/A	0.027	0.010	0.010	0.000	0.488	11.487	0.935	0.270

Problem 1431	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	99	99	48	101	0	423	0	143	123
normalized size	1	1.00	0.48	1.02	0.00	4.27	0.00	1.44	1.24
time (sec)	N/A	0.038	0.013	0.014	0.000	0.472	0.000	1.025	0.186

Problem 1432	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	140	140	50	179	0	782	0	234	205
normalized size	1	1.00	0.36	1.28	0.00	5.59	0.00	1.67	1.46
time (sec)	N/A	0.052	0.013	0.018	0.000	0.477	0.000	1.030	0.444

Problem 1433	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	B	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	173	173	50	292	0	1204	0	326	294
normalized size	1	1.00	0.29	1.69	0.00	6.96	0.00	1.88	1.70
time (sec)	N/A	0.066	0.015	0.022	0.000	0.491	0.000	1.312	0.541

Problem 1434	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	152	152	123	273	265	283	196	335	229
normalized size	1	1.00	0.81	1.80	1.74	1.86	1.29	2.20	1.51
time (sec)	N/A	0.048	0.119	0.007	1.380	0.451	59.926	0.913	0.083

Problem 1435	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	125	125	101	186	187	203	136	229	175
normalized size	1	1.00	0.81	1.49	1.50	1.62	1.09	1.83	1.40
time (sec)	N/A	0.039	0.084	0.007	1.462	0.448	43.586	1.016	0.302

Problem 1436	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	76	115	122	136	461	141	128
normalized size	1	1.00	0.79	1.20	1.27	1.42	4.80	1.47	1.33
time (sec)	N/A	0.031	0.058	0.007	1.374	0.442	1.436	0.995	0.088

Problem 1437	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	62	62	72	85	265	72	68
normalized size	1	1.00	0.93	0.93	1.07	1.27	3.96	1.07	1.01
time (sec)	N/A	0.021	0.035	0.007	1.394	0.424	1.265	1.105	0.072

Problem 1438	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	29	26	28	46	124	28	29
normalized size	1	1.00	0.72	0.65	0.70	1.15	3.10	0.70	0.72
time (sec)	N/A	0.014	0.020	0.003	1.279	0.486	1.122	1.021	0.246

Problem 1439	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	31	14	12	12
normalized size	1	1.00	1.00	0.81	0.75	1.94	0.88	0.75	0.75
time (sec)	N/A	0.001	0.004	0.004	1.363	0.431	0.066	0.958	0.026

Problem 1440	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	48	90	0	398	83	113	100
normalized size	1	1.00	0.52	0.97	0.00	4.28	0.89	1.22	1.08
time (sec)	N/A	0.039	0.010	0.013	0.000	0.481	13.575	1.156	0.333

Problem 1441	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	124	124	50	125	0	782	0	216	161
normalized size	1	1.00	0.40	1.01	0.00	6.31	0.00	1.74	1.30
time (sec)	N/A	0.050	0.015	0.017	0.000	0.484	0.000	1.111	0.377

Problem 1442	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	167	167	52	206	0	1226	0	298	243
normalized size	1	1.00	0.31	1.23	0.00	7.34	0.00	1.78	1.46
time (sec)	N/A	0.062	0.016	0.019	0.000	0.518	0.000	1.198	0.285

Problem 1443	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	200	200	52	319	0	1840	0	432	334
normalized size	1	1.00	0.26	1.60	0.00	9.20	0.00	2.16	1.67
time (sec)	N/A	0.134	0.019	0.023	0.000	0.523	0.000	1.199	0.641

Problem 1444	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	25	23	18	95	66	637	17
normalized size	1	1.00	1.14	1.05	0.82	4.32	3.00	28.95	0.77
time (sec)	N/A	0.005	0.020	0.004	1.373	0.420	1.215	1.262	0.050

Problem 1445	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	25	23	18	75	66	495	17
normalized size	1	1.00	1.14	1.05	0.82	3.41	3.00	22.50	0.77
time (sec)	N/A	0.005	0.012	0.003	1.364	0.426	1.063	1.274	0.034

Problem 1446	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	25	23	374	67	73	374	17
normalized size	1	1.00	1.14	1.05	17.00	3.05	3.32	17.00	0.77
time (sec)	N/A	0.004	0.014	0.003	1.460	0.411	1.542	0.973	0.028

Problem 1447	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	25	23	18	56	73	266	17
normalized size	1	1.00	1.14	1.05	0.82	2.55	3.32	12.09	0.77
time (sec)	N/A	0.004	0.015	0.003	1.431	0.454	1.646	1.176	0.028

Problem 1448	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	25	23	18	45	73	178	17
normalized size	1	1.00	1.14	1.05	0.82	2.05	3.32	8.09	0.77
time (sec)	N/A	0.004	0.014	0.002	1.381	0.411	1.615	0.956	0.028

Problem 1449	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	25	23	18	34	80	106	17
normalized size	1	1.00	1.14	1.05	0.82	1.55	3.64	4.82	0.77
time (sec)	N/A	0.004	0.014	0.004	1.411	0.428	4.108	0.987	0.028

Problem 1450	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	26	23	18	23	53	54	17
normalized size	1	1.00	1.18	1.05	0.82	1.05	2.41	2.45	0.77
time (sec)	N/A	0.004	0.014	0.003	1.393	0.437	8.308	1.070	0.029

Problem 1451	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	24	23	18	18	29	18	17
normalized size	1	1.00	1.20	1.15	0.90	0.90	1.45	0.90	0.85
time (sec)	N/A	0.004	0.008	0.003	1.383	0.416	15.476	1.028	0.030

Problem 1452	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	24	23	18	29	48	18	17
normalized size	1	1.00	1.20	1.15	0.90	1.45	2.40	0.90	0.85
time (sec)	N/A	0.005	0.010	0.002	1.340	0.411	39.429	0.811	0.030

Problem 1453	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	22	21	21	27	22	10
normalized size	1	1.00	1.00	1.57	1.50	1.50	1.93	1.57	0.71
time (sec)	N/A	0.004	0.003	0.008	1.350	0.431	0.659	0.870	0.054

Problem 1454	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	25	25	25	19	18	18	61	18	15
normalized size	1	1.00	1.00	0.76	0.72	0.72	2.44	0.72	0.60
time (sec)	N/A	0.009	0.009	0.006	3.003	0.418	1.124	0.980	0.060

Problem 1455	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	104	84	86	86	170	87	104
normalized size	1	1.00	1.24	1.00	1.02	1.02	2.02	1.04	1.24
time (sec)	N/A	0.038	0.048	0.006	3.003	0.423	2.257	1.045	0.068

Problem 1456	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	18	15	19	19	114	26	14
normalized size	1	1.00	0.67	0.56	0.70	0.70	4.22	0.96	0.52
time (sec)	N/A	0.005	0.009	0.003	1.349	0.417	1.093	0.945	0.255

Problem 1457	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	38	38	23	20	28	24	146	38	21
normalized size	1	1.00	0.61	0.53	0.74	0.63	3.84	1.00	0.55
time (sec)	N/A	0.007	0.010	0.003	1.360	0.448	1.518	0.860	0.046

Problem 1458	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	139	139	106	161	0	570	0	196	204
normalized size	1	1.00	0.76	1.16	0.00	4.10	0.00	1.41	1.47
time (sec)	N/A	0.108	0.076	0.008	0.000	0.495	0.000	1.100	0.211

Problem 1459	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	140	140	154	160	0	900	0	207	206
normalized size	1	1.00	1.10	1.14	0.00	6.43	0.00	1.48	1.47
time (sec)	N/A	0.074	0.075	0.007	0.000	0.496	0.000	0.959	0.369

Problem 1460	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	230	230	194	858	0	702	0	1107	-1
normalized size	1	1.00	0.84	3.73	0.00	3.05	0.00	4.81	-0.00
time (sec)	N/A	0.160	1.465	0.012	0.000	0.510	0.000	1.838	0.000

Problem 1461	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	192	192	190	645	0	540	0	726	-1
normalized size	1	1.00	0.99	3.36	0.00	2.81	0.00	3.78	-0.01
time (sec)	N/A	0.095	0.598	0.008	0.000	0.488	0.000	1.639	0.000

Problem 1462	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	154	154	151	460	0	410	0	438	-1
normalized size	1	1.00	0.98	2.99	0.00	2.66	0.00	2.84	-0.01
time (sec)	N/A	0.072	0.435	0.008	0.000	0.508	0.000	1.377	0.000

Problem 1463	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	116	116	118	305	0	300	0	232	88
normalized size	1	1.00	1.02	2.63	0.00	2.59	0.00	2.00	0.76
time (sec)	N/A	0.055	0.277	0.007	0.000	0.473	0.000	1.254	0.136

Problem 1464	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	117	107	0	236	0	93	260
normalized size	1	1.00	1.62	1.49	0.00	3.28	0.00	1.29	3.61
time (sec)	N/A	0.038	0.104	0.006	0.000	0.450	0.000	1.095	4.005

Problem 1465	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-2)	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	99	0	0	241	0	131	-1
normalized size	1	1.00	1.50	0.00	0.00	3.65	0.00	1.98	-0.02
time (sec)	N/A	0.033	0.227	0.082	0.000	0.496	0.000	1.192	0.000

Problem 1466	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	65	0	152	27
normalized size	1	1.00	1.00	0.84	0.00	2.03	0.00	4.75	0.84
time (sec)	N/A	0.003	0.012	0.005	0.000	0.517	0.000	1.433	0.717

Problem 1467	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	175	0	447	127
normalized size	1	1.00	0.70	0.82	0.00	2.65	0.00	6.77	1.92
time (sec)	N/A	0.009	0.020	0.006	0.000	0.727	0.000	1.444	0.822

Problem 1468	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	337	0	689	203
normalized size	1	1.00	0.76	1.04	0.00	3.34	0.00	6.82	2.01
time (sec)	N/A	0.016	0.039	0.009	0.000	1.262	0.000	1.582	0.966

Problem 1469	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	532	0	989	292
normalized size	1	1.00	0.87	1.26	0.00	3.91	0.00	7.27	2.15
time (sec)	N/A	0.029	0.054	0.011	0.000	4.383	0.000	2.041	1.184

Problem 1470	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	171	171	170	256	0	781	0	1345	397
normalized size	1	1.00	0.99	1.50	0.00	4.57	0.00	7.87	2.32
time (sec)	N/A	0.041	0.077	0.013	0.000	9.214	0.000	2.383	1.432

Problem 1471	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	227	227	187	853	0	702	0	1740	-1
normalized size	1	1.00	0.82	3.76	0.00	3.09	0.00	7.67	-0.00
time (sec)	N/A	0.130	1.780	0.006	0.000	0.495	0.000	2.297	0.000

Problem 1472	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	189	189	193	640	0	534	0	1071	-1
normalized size	1	1.00	1.02	3.39	0.00	2.83	0.00	5.67	-0.01
time (sec)	N/A	0.090	0.567	0.007	0.000	0.486	0.000	1.892	0.000

Problem 1473	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	151	151	152	459	0	410	0	576	-1
normalized size	1	1.00	1.01	3.04	0.00	2.72	0.00	3.81	-0.01
time (sec)	N/A	0.068	0.445	0.006	0.000	0.478	0.000	1.606	0.000

Problem 1474	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	113	113	109	308	0	306	0	233	-1
normalized size	1	1.00	0.96	2.73	0.00	2.71	0.00	2.06	-0.01
time (sec)	N/A	0.051	0.291	0.007	0.000	0.473	0.000	1.246	0.000

Problem 1475	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	71	0	0	311	0	204	-1
normalized size	1	1.00	0.72	0.00	0.00	3.17	0.00	2.08	-0.01
time (sec)	N/A	0.047	0.053	0.079	0.000	0.511	0.000	1.499	0.000

Problem 1476	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	73	0	0	325	0	455	-1
normalized size	1	1.00	0.79	0.00	0.00	3.53	0.00	4.95	-0.01
time (sec)	N/A	0.040	0.050	0.079	0.000	0.605	0.000	1.744	0.000

Problem 1477	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	104	0	374	27
normalized size	1	1.00	1.00	0.84	0.00	3.25	0.00	11.69	0.84
time (sec)	N/A	0.003	0.015	0.005	0.000	0.719	0.000	1.695	0.796

Problem 1478	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	235	0	1024	178
normalized size	1	1.00	0.70	0.82	0.00	3.56	0.00	15.52	2.70
time (sec)	N/A	0.008	0.025	0.005	0.000	1.349	0.000	2.122	0.926

Problem 1479	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	426	0	1394	268
normalized size	1	1.00	0.76	1.04	0.00	4.22	0.00	13.80	2.65
time (sec)	N/A	0.016	0.045	0.007	0.000	4.399	0.000	2.937	1.113

Problem 1480	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	649	0	1823	376
normalized size	1	1.00	0.87	1.26	0.00	4.77	0.00	13.40	2.76
time (sec)	N/A	0.028	0.064	0.011	0.000	9.760	0.000	3.282	1.333

Problem 1481	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	262	262	209	1089	0	882	0	3120	-1
normalized size	1	1.00	0.80	4.16	0.00	3.37	0.00	11.91	-0.00
time (sec)	N/A	0.149	2.529	0.008	0.000	0.558	0.000	3.533	0.000

Problem 1482	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	224	224	187	848	0	702	0	1962	-1
normalized size	1	1.00	0.83	3.79	0.00	3.13	0.00	8.76	-0.00
time (sec)	N/A	0.119	1.468	0.008	0.000	0.503	0.000	2.326	0.000

Problem 1483	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	186	186	191	641	0	540	0	1083	-1
normalized size	1	1.00	1.03	3.45	0.00	2.90	0.00	5.82	-0.01
time (sec)	N/A	0.086	0.580	0.008	0.000	0.500	0.000	1.926	0.000

Problem 1484	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	148	148	139	465	0	412	0	446	-1
normalized size	1	1.00	0.94	3.14	0.00	2.78	0.00	3.01	-0.01
time (sec)	N/A	0.066	0.407	0.008	0.000	0.483	0.000	1.431	0.000

Problem 1485	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	138	138	71	0	0	439	0	287	-1
normalized size	1	1.00	0.51	0.00	0.00	3.18	0.00	2.08	-0.01
time (sec)	N/A	0.063	0.068	0.083	0.000	0.559	0.000	2.018	0.000

Problem 1486	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	B	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	128	128	73	0	0	475	0	650	-1
normalized size	1	1.00	0.57	0.00	0.00	3.71	0.00	5.08	-0.01
time (sec)	N/A	0.062	0.062	0.080	0.000	0.748	0.000	2.186	0.000

Problem 1487	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	B	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	120	120	73	0	0	463	0	1025	-1
normalized size	1	1.00	0.61	0.00	0.00	3.86	0.00	8.54	-0.01
time (sec)	N/A	0.052	0.070	0.082	0.000	0.952	0.000	2.477	0.000

Problem 1488	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	138	0	706	27
normalized size	1	1.00	1.00	0.84	0.00	4.31	0.00	22.06	0.84
time (sec)	N/A	0.003	0.018	0.003	0.000	1.436	0.000	2.541	0.971

Problem 1489	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	295	0	1826	229
normalized size	1	1.00	0.70	0.82	0.00	4.47	0.00	27.67	3.47
time (sec)	N/A	0.009	0.031	0.005	0.000	4.705	0.000	3.803	1.140

Problem 1490	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	513	0	2316	333
normalized size	1	1.00	0.76	1.04	0.00	5.08	0.00	22.93	3.30
time (sec)	N/A	0.016	0.052	0.007	0.000	10.681	0.000	4.592	1.355

Problem 1491	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	765	0	2868	459
normalized size	1	1.00	0.87	1.26	0.00	5.62	0.00	21.09	3.38
time (sec)	N/A	0.028	0.074	0.010	0.000	23.042	0.000	6.088	1.615

Problem 1492	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F(-1)	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	183	183	189	650	0	542	0	268	-1
normalized size	1	1.00	1.03	3.55	0.00	2.96	0.00	1.46	-0.01
time (sec)	N/A	0.097	0.656	0.007	0.000	0.544	0.000	1.229	0.000

Problem 1493	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F(-1)	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	148	148	150	465	0	412	0	198	-1
normalized size	1	1.00	1.01	3.14	0.00	2.78	0.00	1.34	-0.01
time (sec)	N/A	0.072	0.524	0.009	0.000	0.514	0.000	1.270	0.000

Problem 1494	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	113	113	119	308	0	306	0	139	-1
normalized size	1	1.00	1.05	2.73	0.00	2.71	0.00	1.23	-0.01
time (sec)	N/A	0.050	0.365	0.007	0.000	0.469	0.000	0.945	0.000

Problem 1495	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	73	73	103	107	0	235	0	97	261
normalized size	1	1.00	1.41	1.47	0.00	3.22	0.00	1.33	3.58
time (sec)	N/A	0.035	0.268	0.006	0.000	0.494	0.000	1.115	3.803

Problem 1496	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	77	76	0	178	0	50	45
normalized size	1	1.00	1.83	1.81	0.00	4.24	0.00	1.19	1.07
time (sec)	N/A	0.026	0.065	0.007	0.000	0.475	0.000	1.097	0.288

Problem 1497	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	27	0	42	0	66	26
normalized size	1	1.00	1.00	0.90	0.00	1.40	0.00	2.20	0.87
time (sec)	N/A	0.003	0.009	0.006	0.000	0.439	0.000	1.043	0.732

Problem 1498	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	118	0	121	71
normalized size	1	1.00	0.70	0.82	0.00	1.79	0.00	1.83	1.08
time (sec)	N/A	0.008	0.017	0.004	0.000	0.510	0.000	1.080	0.894

Problem 1499	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	75	105	0	251	0	227	133
normalized size	1	1.00	0.74	1.04	0.00	2.49	0.00	2.25	1.32
time (sec)	N/A	0.016	0.031	0.007	0.000	0.712	0.000	1.270	1.005

Problem 1500	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	116	171	0	419	0	386	209
normalized size	1	1.00	0.85	1.26	0.00	3.08	0.00	2.84	1.54
time (sec)	N/A	0.028	0.047	0.008	0.000	1.219	0.000	1.468	1.192

Problem 1501	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	171	171	168	256	0	638	0	596	303
normalized size	1	1.00	0.98	1.50	0.00	3.73	0.00	3.49	1.77
time (sec)	N/A	0.041	0.066	0.012	0.000	4.004	0.000	1.568	1.370

Problem 1502	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	174	174	73	0	0	603	0	279	-1
normalized size	1	1.00	0.42	0.00	0.00	3.47	0.00	1.60	-0.01
time (sec)	N/A	0.089	0.067	0.079	0.000	0.751	0.000	1.385	0.000

Problem 1503	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	138	138	73	0	0	441	0	201	-1
normalized size	1	1.00	0.53	0.00	0.00	3.20	0.00	1.46	-0.01
time (sec)	N/A	0.067	0.055	0.082	0.000	0.584	0.000	1.260	0.000

Problem 1504	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	73	0	0	311	0	137	-1
normalized size	1	1.00	0.74	0.00	0.00	3.17	0.00	1.40	-0.01
time (sec)	N/A	0.047	0.048	0.087	0.000	0.534	0.000	1.273	0.000

Problem 1505	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-2)	B	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	95	0	0	241	0	96	-1
normalized size	1	1.00	1.44	0.00	0.00	3.65	0.00	1.45	-0.02
time (sec)	N/A	0.032	0.349	0.088	0.000	0.502	0.000	1.223	0.000

Problem 1506	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	27	0	42	0	47	26
normalized size	1	1.00	1.00	0.90	0.00	1.40	0.00	1.57	0.87
time (sec)	N/A	0.003	0.008	0.005	0.000	0.469	0.000	1.038	0.741

Problem 1507	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	62	62	42	52	0	125	0	142	71
normalized size	1	1.00	0.68	0.84	0.00	2.02	0.00	2.29	1.15
time (sec)	N/A	0.009	0.017	0.004	0.000	0.500	0.000	1.222	0.858

Problem 1508	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	75	105	0	273	0	368	141
normalized size	1	1.00	0.74	1.04	0.00	2.70	0.00	3.64	1.40
time (sec)	N/A	0.018	0.030	0.009	0.000	0.648	0.000	1.544	1.064

Problem 1509	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	114	170	0	455	0	830	227
normalized size	1	1.00	0.84	1.25	0.00	3.35	0.00	6.10	1.67
time (sec)	N/A	0.027	0.042	0.010	0.000	0.983	0.000	2.459	1.312

Problem 1510	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	171	171	166	256	0	689	0	1518	337
normalized size	1	1.00	0.97	1.50	0.00	4.03	0.00	8.88	1.97
time (sec)	N/A	0.043	0.061	0.012	0.000	2.583	0.000	4.771	1.500

Problem 1511	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	206	206	226	356	0	955	0	2438	454
normalized size	1	1.00	1.10	1.73	0.00	4.64	0.00	11.83	2.20
time (sec)	N/A	0.057	0.080	0.013	0.000	6.350	0.000	8.708	1.959

Problem 1512	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	B	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	204	204	73	0	0	879	0	500	-1
normalized size	1	1.00	0.36	0.00	0.00	4.31	0.00	2.45	-0.00
time (sec)	N/A	0.109	0.097	0.083	0.000	1.346	0.000	2.418	0.000

Problem 1513	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	B	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	170	170	73	0	0	657	0	380	-1
normalized size	1	1.00	0.43	0.00	0.00	3.86	0.00	2.24	-0.01
time (sec)	N/A	0.079	0.082	0.088	0.000	0.926	0.000	2.141	0.000

Problem 1514	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F(-2)	B	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	128	128	73	0	0	475	0	276	-1
normalized size	1	1.00	0.57	0.00	0.00	3.71	0.00	2.16	-0.01
time (sec)	N/A	0.058	0.078	0.082	0.000	0.732	0.000	1.972	0.000

Problem 1515	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-2)	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	111	0	0	325	0	181	-1
normalized size	1	1.00	1.21	0.00	0.00	3.53	0.00	1.97	-0.01
time (sec)	N/A	0.040	0.550	0.086	0.000	0.629	0.000	1.434	0.000

Problem 1516	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	65	0	51	130
normalized size	1	1.00	1.00	0.84	0.00	2.03	0.00	1.59	4.06
time (sec)	N/A	0.003	0.010	0.005	0.000	0.538	0.000	1.147	0.561

Problem 1517	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	53	0	118	0	126	127
normalized size	1	1.00	0.70	0.80	0.00	1.79	0.00	1.91	1.92
time (sec)	N/A	0.008	0.015	0.004	0.000	0.602	0.000	1.019	0.897

Problem 1518	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	78	104	0	273	0	373	132
normalized size	1	1.00	0.80	1.06	0.00	2.79	0.00	3.81	1.35
time (sec)	N/A	0.017	0.031	0.007	0.000	0.817	0.000	1.480	1.030

Problem 1519	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	135	135	118	169	0	447	0	670	224
normalized size	1	1.00	0.87	1.25	0.00	3.31	0.00	4.96	1.66
time (sec)	N/A	0.028	0.052	0.010	0.000	1.079	0.000	2.063	1.289

Problem 1520	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F(-2)	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	172	172	170	256	0	715	0	1203	346
normalized size	1	1.00	0.99	1.49	0.00	4.16	0.00	6.99	2.01
time (sec)	N/A	0.044	0.067	0.010	0.000	3.428	0.000	3.918	1.531

Problem 1521	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	207	207	233	356	0	999	0	1964	478
normalized size	1	1.00	1.13	1.72	0.00	4.83	0.00	9.49	2.31
time (sec)	N/A	0.061	0.082	0.015	0.000	7.600	0.000	7.760	1.908

Problem 1522	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	19	86	48	31	0	24	50
normalized size	1	1.00	1.00	4.53	2.53	1.63	0.00	1.26	2.63
time (sec)	N/A	0.006	0.010	0.009	1.361	0.428	0.000	1.018	0.308

Problem 1523	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	39	66	33	27	0	23	47
normalized size	1	1.00	2.05	3.47	1.74	1.42	0.00	1.21	2.47
time (sec)	N/A	0.005	0.012	0.009	1.366	0.423	0.000	1.055	0.339

Problem 1524	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	39	66	33	27	0	23	43
normalized size	1	1.00	2.05	3.47	1.74	1.42	0.00	1.21	2.26
time (sec)	N/A	0.005	0.011	0.008	1.389	0.447	0.000	0.965	0.326

Problem 1525	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	34	60	32	25	15	21	33
normalized size	1	1.00	2.00	3.53	1.88	1.47	0.88	1.24	1.94
time (sec)	N/A	0.004	0.010	0.007	1.330	0.458	1.265	0.936	0.309

Problem 1526	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	39	64	33	27	0	23	44
normalized size	1	1.00	2.05	3.37	1.74	1.42	0.00	1.21	2.32
time (sec)	N/A	0.005	0.011	0.008	1.316	0.426	0.000	1.032	0.318

Problem 1527	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	25	57	26	26	75	23	50
normalized size	1	1.00	2.27	5.18	2.36	2.36	6.82	2.09	4.55
time (sec)	N/A	0.003	0.005	0.007	1.329	0.436	4.199	1.075	0.304

Problem 1528	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	39	66	33	27	0	23	46
normalized size	1	1.00	2.05	3.47	1.74	1.42	0.00	1.21	2.42
time (sec)	N/A	0.005	0.011	0.009	1.375	0.438	0.000	0.995	0.292

Problem 1529	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	66	33	28	0	23	47
normalized size	1	1.00	1.00	4.40	2.20	1.87	0.00	1.53	3.13
time (sec)	N/A	0.004	0.004	0.007	1.380	0.432	0.000	1.012	0.293

Problem 1530	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	10	10	10	11	10	10	7	11	10
normalized size	1	1.00	1.00	1.10	1.00	1.00	0.70	1.10	1.00
time (sec)	N/A	0.001	0.001	0.001	1.319	0.412	0.062	0.952	0.257

Problem 1531	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	66	33	28	0	23	43
normalized size	1	1.00	1.00	4.40	2.20	1.87	0.00	1.53	2.87
time (sec)	N/A	0.004	0.004	0.006	1.386	0.424	0.000	0.925	0.286

Problem 1532	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	19	19	36	58	32	25	20	21	37
normalized size	1	1.00	1.89	3.05	1.68	1.32	1.05	1.11	1.95
time (sec)	N/A	0.005	0.009	0.006	1.382	0.437	1.349	1.067	0.280

Problem 1533	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	41	65	30	28	0	23	44
normalized size	1	1.00	1.95	3.10	1.43	1.33	0.00	1.10	2.10
time (sec)	N/A	0.006	0.009	0.007	1.682	0.441	0.000	1.023	0.286

Problem 1534	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	25	57	26	26	75	23	50
normalized size	1	1.00	2.27	5.18	2.36	2.36	6.82	2.09	4.55
time (sec)	N/A	0.002	0.003	0.000	1.361	0.425	4.282	0.959	0.002

Problem 1535	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	41	66	33	28	0	23	50
normalized size	1	1.00	1.95	3.14	1.57	1.33	0.00	1.10	2.38
time (sec)	N/A	0.006	0.011	0.007	1.242	0.432	0.000	0.958	0.283

Problem 1536	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	22	65	21	44	0	18	44
normalized size	1	1.00	1.38	4.06	1.31	2.75	0.00	1.12	2.75
time (sec)	N/A	0.014	0.013	0.012	2.990	0.445	0.000	1.049	0.084

Problem 1537	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	11	56	9	31	76	15	44
normalized size	1	1.00	1.00	5.09	0.82	2.82	6.91	1.36	4.00
time (sec)	N/A	0.003	0.009	0.007	3.033	0.436	4.440	0.907	0.078

Problem 1538	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	22	66	19	43	0	18	40
normalized size	1	1.00	1.38	4.12	1.19	2.69	0.00	1.12	2.50
time (sec)	N/A	0.013	0.013	0.010	3.008	0.462	0.000	1.050	0.320

Problem 1539	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	A	B	C	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	10	10	51	58	18	26	24	18	34
normalized size	1	1.00	5.10	5.80	1.80	2.60	2.40	1.80	3.40
time (sec)	N/A	0.010	0.014	0.004	3.140	0.425	1.277	0.934	0.293

Problem 1540	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	A	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	49	66	21	44	0	13	41
normalized size	1	1.00	4.45	6.00	1.91	4.00	0.00	1.18	3.73
time (sec)	N/A	0.010	0.015	0.009	3.014	0.454	0.000	1.172	0.303

Problem 1541	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	28	26	16	1	53	12	47
normalized size	1	1.00	0.97	0.90	0.55	0.03	1.83	0.41	1.62
time (sec)	N/A	0.004	0.009	0.004	1.355	0.442	1.980	0.968	0.069

Problem 1542	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	A	A	F	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	53	66	21	44	0	23	47
normalized size	1	1.00	2.04	2.54	0.81	1.69	0.00	0.88	1.81
time (sec)	N/A	0.014	0.016	0.010	3.012	0.454	0.000	1.071	0.297

Problem 1543	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	70	33	30	0	25	49
normalized size	1	1.00	1.00	4.38	2.06	1.88	0.00	1.56	3.06
time (sec)	N/A	0.005	0.007	0.009	1.357	0.448	0.000	1.037	0.312

Problem 1544	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	12	12	12	13	11	11	8	12	11
normalized size	1	1.00	1.00	1.08	0.92	0.92	0.67	1.00	0.92
time (sec)	N/A	0.001	0.001	0.001	1.423	0.445	0.066	1.102	0.034

Problem 1545	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	70	33	30	0	25	45
normalized size	1	1.00	1.00	4.38	2.06	1.88	0.00	1.56	2.81
time (sec)	N/A	0.005	0.007	0.008	1.327	0.419	0.000	0.853	0.311

Problem 1546	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	37	64	32	27	53	23	39
normalized size	1	1.00	1.85	3.20	1.60	1.35	2.65	1.15	1.95
time (sec)	N/A	0.005	0.008	0.007	1.356	0.435	1.337	1.025	0.282

Problem 1547	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	40	70	33	30	0	25	46
normalized size	1	1.00	1.82	3.18	1.50	1.36	0.00	1.14	2.09
time (sec)	N/A	0.007	0.011	0.007	1.383	0.429	0.000	1.095	0.285

Problem 1548	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	12	12	27	61	26	28	78	25	52
normalized size	1	1.00	2.25	5.08	2.17	2.33	6.50	2.08	4.33
time (sec)	N/A	0.003	0.005	0.006	1.274	0.432	4.625	1.104	0.294

Problem 1549	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	40	69	30	30	0	25	52
normalized size	1	1.00	1.82	3.14	1.36	1.36	0.00	1.14	2.36
time (sec)	N/A	0.007	0.011	0.007	1.369	0.431	0.000	1.277	0.292

Problem 1550	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	C	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	25	57	26	26	75	23	40
normalized size	1	1.00	2.27	5.18	2.36	2.36	6.82	2.09	3.64
time (sec)	N/A	0.002	0.005	0.006	1.377	0.426	4.209	1.040	0.324

Problem 1551	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	41	100	0	175	0	57	66
normalized size	1	1.00	0.95	2.33	0.00	4.07	0.00	1.33	1.53
time (sec)	N/A	0.015	0.025	0.018	0.000	0.464	0.000	0.972	0.495

Problem 1552	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	31	48	41	26	44	23	30
normalized size	1	1.00	1.41	2.18	1.86	1.18	2.00	1.05	1.36
time (sec)	N/A	0.004	0.009	0.007	2.869	0.442	1.029	0.923	0.439

Problem 1553	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	26	57	28	46	58	30	43
normalized size	1	1.00	1.00	2.19	1.08	1.77	2.23	1.15	1.65
time (sec)	N/A	0.008	0.009	0.007	3.041	0.447	1.092	1.260	0.122

Problem 1554	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	67	118	0	176	0	58	63
normalized size	1	1.00	1.60	2.81	0.00	4.19	0.00	1.38	1.50
time (sec)	N/A	0.016	0.050	0.043	0.000	0.463	0.000	1.079	0.515

Problem 1555	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	10	10	14	27	14	14	26	8	16
normalized size	1	1.00	1.40	2.70	1.40	1.40	2.60	0.80	1.60
time (sec)	N/A	0.007	0.010	0.005	2.993	0.430	0.992	1.099	0.290

Problem 1556	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	31	21	21	44	13	27
normalized size	1	1.00	1.00	1.55	1.05	1.05	2.20	0.65	1.35
time (sec)	N/A	0.007	0.004	0.006	3.119	0.430	1.003	1.085	0.295

Problem 1557	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	45	39	11	44	58	21	40
normalized size	1	1.00	1.73	1.50	0.42	1.69	2.23	0.81	1.54
time (sec)	N/A	0.009	0.012	0.006	3.000	0.430	1.069	0.934	0.080

Problem 1558	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	F(-2)	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	103	84	0	185	0	54	44
normalized size	1	1.00	2.40	1.95	0.00	4.30	0.00	1.26	1.02
time (sec)	N/A	0.028	0.081	0.009	0.000	0.462	0.000	1.162	0.343

Problem 1559	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	457	457	73	0	0	0	0	0	-1
normalized size	1	1.00	0.16	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.627	0.042	0.152	0.000	0.482	0.000	0.000	0.000

Problem 1560	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	419	419	73	0	0	0	0	0	-1
normalized size	1	1.00	0.17	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.374	0.028	0.076	0.000	0.492	0.000	0.000	0.000

Problem 1561	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	381	381	71	0	0	0	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.272	0.023	0.074	0.000	0.496	0.000	0.000	0.000

Problem 1562	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	366	366	71	0	0	0	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.262	0.026	0.085	0.000	0.492	0.000	0.000	0.000

Problem 1563	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	417	417	73	0	0	0	0	0	-1
normalized size	1	1.00	0.18	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.366	0.025	0.084	0.000	0.486	0.000	0.000	0.000

Problem 1564	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	457	457	73	0	0	0	0	0	-1
normalized size	1	1.00	0.16	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.447	0.026	0.085	0.000	0.488	0.000	0.000	0.000

Problem 1565	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	839	839	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.938	0.030	0.120	0.000	0.585	0.000	0.000	0.000

Problem 1566	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	804	804	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.668	0.026	0.062	0.000	0.572	0.000	0.000	0.000

Problem 1567	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	762	762	71	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.578	0.022	0.085	0.000	0.557	0.000	0.000	0.000

Problem 1568	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	796	796	71	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.690	0.023	0.083	0.000	0.545	0.000	0.000	0.000

Problem 1569	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	842	842	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.834	0.022	0.084	0.000	0.551	0.000	0.000	0.000

Problem 1570	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	416	416	73	0	0	0	0	0	-1
normalized size	1	1.00	0.18	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.385	0.035	0.076	0.000	0.481	0.000	0.000	0.000

Problem 1571	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	381	381	73	0	0	0	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.296	0.027	0.071	0.000	0.476	0.000	0.000	0.000

Problem 1572	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	345	345	71	0	0	0	0	0	-1
normalized size	1	1.00	0.21	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.223	0.023	0.084	0.000	0.487	0.000	0.000	0.000

Problem 1573	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	383	383	71	0	0	0	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.294	0.023	0.081	0.000	0.537	0.000	0.000	0.000

Problem 1574	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	421	421	73	0	0	0	0	0	-1
normalized size	1	1.00	0.17	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.368	0.023	0.083	0.000	0.503	0.000	0.000	0.000

Problem 1575	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	219	219	73	0	0	717	0	0	-1
normalized size	1	1.00	0.33	0.00	0.00	3.27	0.00	0.00	-0.00
time (sec)	N/A	0.088	0.034	0.060	0.000	0.469	0.000	0.000	0.000

Problem 1576	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	172	172	73	0	0	596	0	0	-1
normalized size	1	1.00	0.42	0.00	0.00	3.47	0.00	0.00	-0.01
time (sec)	N/A	0.046	0.025	0.033	0.000	0.510	0.000	0.000	0.000

Problem 1577	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	149	149	71	0	0	233	0	0	-1
normalized size	1	1.00	0.48	0.00	0.00	1.56	0.00	0.00	-0.01
time (sec)	N/A	0.033	0.028	0.084	0.000	0.444	0.000	0.000	0.000

Problem 1578	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	65	0	0	92
normalized size	1	1.00	1.00	0.84	0.00	2.03	0.00	0.00	2.88
time (sec)	N/A	0.003	0.013	0.005	0.000	0.422	0.000	0.000	0.713

Problem 1579	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	175	0	0	127
normalized size	1	1.00	0.70	0.82	0.00	2.65	0.00	0.00	1.92
time (sec)	N/A	0.009	0.023	0.006	0.000	0.421	0.000	0.000	1.032

Problem 1580	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	337	0	0	203
normalized size	1	1.00	0.76	1.04	0.00	3.34	0.00	0.00	2.01
time (sec)	N/A	0.017	0.040	0.008	0.000	0.439	0.000	0.000	1.017

Problem 1581	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	533	0	0	293
normalized size	1	1.00	0.87	1.26	0.00	3.92	0.00	0.00	2.15
time (sec)	N/A	0.028	0.058	0.009	0.000	0.438	0.000	0.000	1.152

Problem 1582	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	655	655	73	0	0	0	0	0	-1
normalized size	1	1.00	0.11	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.416	0.033	0.079	0.000	0.447	0.000	0.000	0.000

Problem 1583	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	617	617	73	0	0	0	0	0	-1
normalized size	1	1.00	0.12	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.849	0.033	0.043	0.000	0.443	0.000	0.000	0.000

Problem 1584	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	576	576	71	0	0	0	0	0	-1
normalized size	1	1.00	0.12	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.563	0.028	0.042	0.000	0.441	0.000	0.000	0.000

Problem 1585	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	568	568	73	0	0	0	0	0	-1
normalized size	1	1.00	0.13	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.594	0.023	0.084	0.000	0.463	0.000	0.000	0.000

Problem 1586	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	617	617	73	0	0	0	0	0	-1
normalized size	1	1.00	0.12	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.843	0.027	0.082	0.000	0.466	0.000	0.000	0.000

Problem 1587	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	216	216	73	0	0	740	0	0	-1
normalized size	1	1.00	0.34	0.00	0.00	3.43	0.00	0.00	-0.00
time (sec)	N/A	0.090	0.030	0.063	0.000	0.480	0.000	0.000	0.000

Problem 1588	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	171	171	73	0	0	618	0	0	-1
normalized size	1	1.00	0.43	0.00	0.00	3.61	0.00	0.00	-0.01
time (sec)	N/A	0.041	0.029	0.035	0.000	0.467	0.000	0.000	0.000

Problem 1589	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	71	0	0	519	0	0	-1
normalized size	1	1.00	0.56	0.00	0.00	4.12	0.00	0.00	-0.01
time (sec)	N/A	0.014	0.029	0.086	0.000	0.468	0.000	0.000	0.000

Problem 1590	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	42	0	0	-1
normalized size	1	1.00	1.00	0.84	0.00	1.31	0.00	0.00	-0.03
time (sec)	N/A	0.003	0.012	0.006	0.000	0.458	0.000	0.000	0.000

Problem 1591	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	118	0	0	-1
normalized size	1	1.00	0.70	0.82	0.00	1.79	0.00	0.00	-0.02
time (sec)	N/A	0.009	0.017	0.004	0.000	0.442	0.000	0.000	0.000

Problem 1592	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	251	0	0	-1
normalized size	1	1.00	0.76	1.04	0.00	2.49	0.00	0.00	-0.01
time (sec)	N/A	0.018	0.034	0.007	0.000	0.508	0.000	0.000	0.000

Problem 1593	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	420	0	0	-1
normalized size	1	1.00	0.87	1.26	0.00	3.09	0.00	0.00	-0.01
time (sec)	N/A	0.028	0.048	0.009	0.000	0.555	0.000	0.000	0.000

Problem 1594	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1365	1365	73	0	0	0	0	0	-1
normalized size	1	1.00	0.05	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	2.803	0.034	0.085	0.000	0.495	0.000	0.000	0.000

Problem 1595	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1330	1330	73	0	0	0	0	0	-1
normalized size	1	1.00	0.05	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	2.010	0.035	0.080	0.000	0.490	0.000	0.000	0.000

Problem 1596	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1293	1293	73	0	0	0	0	0	-1
normalized size	1	1.00	0.06	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.563	0.029	0.083	0.000	0.467	0.000	0.000	0.000

Problem 1597	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1257	1257	73	0	0	0	0	0	-1
normalized size	1	1.00	0.06	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.179	0.023	0.091	0.000	0.447	0.000	0.000	0.000

Problem 1598	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1297	1297	71	0	0	0	0	0	-1
normalized size	1	1.00	0.05	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.586	0.024	0.086	0.000	0.454	0.000	0.000	0.000

Problem 1599	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1335	1335	73	0	0	0	0	0	-1
normalized size	1	1.00	0.05	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	2.012	0.025	0.085	0.000	0.456	0.000	0.000	0.000

Problem 1600	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1372	1372	73	0	0	0	0	0	-1
normalized size	1	1.00	0.05	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	2.442	0.025	0.086	0.000	0.492	0.000	0.000	0.000

Problem 1601	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	216	216	73	0	0	741	0	0	-1
normalized size	1	1.00	0.34	0.00	0.00	3.43	0.00	0.00	-0.00
time (sec)	N/A	0.080	0.035	0.038	0.000	0.472	0.000	0.000	0.000

Problem 1602	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	169	169	73	0	0	619	0	0	-1
normalized size	1	1.00	0.43	0.00	0.00	3.66	0.00	0.00	-0.01
time (sec)	N/A	0.041	0.027	0.033	0.000	0.474	0.000	0.000	0.000

Problem 1603	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	73	0	0	521	0	0	-1
normalized size	1	1.00	0.58	0.00	0.00	4.13	0.00	0.00	-0.01
time (sec)	N/A	0.015	0.030	0.089	0.000	0.484	0.000	0.000	0.000

Problem 1604	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	27	0	42	0	0	26
normalized size	1	1.00	1.00	0.90	0.00	1.40	0.00	0.00	0.87
time (sec)	N/A	0.003	0.009	0.005	0.000	0.424	0.000	0.000	0.828

Problem 1605	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	118	0	0	71
normalized size	1	1.00	0.70	0.82	0.00	1.79	0.00	0.00	1.08
time (sec)	N/A	0.010	0.017	0.004	0.000	0.426	0.000	0.000	0.977

Problem 1606	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	75	105	0	251	0	0	133
normalized size	1	1.00	0.74	1.04	0.00	2.49	0.00	0.00	1.32
time (sec)	N/A	0.017	0.033	0.007	0.000	0.415	0.000	0.000	1.508

Problem 1607	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	116	171	0	419	0	0	209
normalized size	1	1.00	0.85	1.26	0.00	3.08	0.00	0.00	1.54
time (sec)	N/A	0.030	0.049	0.010	0.000	0.449	0.000	0.000	1.273

Problem 1608	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	649	649	73	0	0	0	0	0	-1
normalized size	1	1.00	0.11	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.118	0.034	0.049	0.000	0.441	0.000	0.000	0.000

Problem 1609	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	614	614	73	0	0	0	0	0	-1
normalized size	1	1.00	0.12	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.817	0.030	0.046	0.000	0.446	0.000	0.000	0.000

Problem 1610	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	577	577	73	0	0	0	0	0	-1
normalized size	1	1.00	0.13	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.547	0.027	0.038	0.000	0.456	0.000	0.000	0.000

Problem 1611	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	542	542	71	0	0	0	0	0	-1
normalized size	1	1.00	0.13	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.430	0.023	0.086	0.000	0.432	0.000	0.000	0.000

Problem 1612	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	586	586	73	0	0	0	0	0	-1
normalized size	1	1.00	0.12	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.550	0.024	0.088	0.000	0.449	0.000	0.000	0.000

Problem 1613	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	621	621	73	0	0	0	0	0	-1
normalized size	1	1.00	0.12	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.812	0.024	0.084	0.000	0.489	0.000	0.000	0.000

Problem 1614	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	656	656	73	0	0	0	0	0	-1
normalized size	1	1.00	0.11	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.090	0.026	0.092	0.000	0.486	0.000	0.000	0.000

Problem 1615	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	241	241	73	0	0	423	0	0	-1
normalized size	1	1.00	0.30	0.00	0.00	1.76	0.00	0.00	-0.00
time (sec)	N/A	0.107	0.062	0.098	0.000	0.454	0.000	0.000	0.000

Problem 1616	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	195	195	73	0	0	306	0	0	-1
normalized size	1	1.00	0.37	0.00	0.00	1.57	0.00	0.00	-0.01
time (sec)	N/A	0.071	0.048	0.099	0.000	0.475	0.000	0.000	0.000

Problem 1617	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	149	149	73	0	0	233	0	0	-1
normalized size	1	1.00	0.49	0.00	0.00	1.56	0.00	0.00	-0.01
time (sec)	N/A	0.031	0.044	0.082	0.000	0.449	0.000	0.000	0.000

Problem 1618	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	27	0	42	0	0	-1
normalized size	1	1.00	1.00	0.90	0.00	1.40	0.00	0.00	-0.03
time (sec)	N/A	0.003	0.007	0.004	0.000	0.455	0.000	0.000	0.000

Problem 1619	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	45	53	0	126	0	0	-1
normalized size	1	1.00	0.68	0.80	0.00	1.91	0.00	0.00	-0.02
time (sec)	N/A	0.009	0.020	0.005	0.000	0.420	0.000	0.000	0.000

Problem 1620	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	75	105	0	273	0	0	-1
normalized size	1	1.00	0.74	1.04	0.00	2.70	0.00	0.00	-0.01
time (sec)	N/A	0.018	0.031	0.007	0.000	0.445	0.000	0.000	0.000

Problem 1621	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	116	171	0	456	0	0	-1
normalized size	1	1.00	0.85	1.26	0.00	3.35	0.00	0.00	-0.01
time (sec)	N/A	0.030	0.047	0.009	0.000	0.533	0.000	0.000	0.000

Problem 1622	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1355	1355	73	0	0	0	0	0	-1
normalized size	1	1.00	0.05	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	2.511	0.060	0.084	0.000	0.470	0.000	0.000	0.000

Problem 1623	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1317	1317	73	0	0	0	0	0	-1
normalized size	1	1.00	0.06	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.998	0.051	0.086	0.000	0.462	0.000	0.000	0.000

Problem 1624	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1279	1279	73	0	0	0	0	0	-1
normalized size	1	1.00	0.06	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.541	0.043	0.082	0.000	0.454	0.000	0.000	0.000

Problem 1625	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1298	1298	73	0	0	0	0	0	-1
normalized size	1	1.00	0.06	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.524	0.037	0.083	0.000	0.452	0.000	0.000	0.000

Problem 1626	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1327	1327	71	0	0	0	0	0	-1
normalized size	1	1.00	0.05	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.958	0.038	0.087	0.000	0.460	0.000	0.000	0.000

Problem 1627	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	1370	1370	73	0	0	0	0	0	-1
normalized size	1	1.00	0.05	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	2.418	0.042	0.087	0.000	0.473	0.000	0.000	0.000

Problem 1628	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	C	F	A	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	77	77	48	573	0	107	39	0	-1
normalized size	1	1.00	0.62	7.44	0.00	1.39	0.51	0.00	-0.01
time (sec)	N/A	0.014	0.019	0.377	0.000	0.447	2.548	0.000	0.000

Problem 1629	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	185	185	73	0	0	0	0	0	-1
normalized size	1	1.00	0.39	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.212	0.038	0.097	0.000	0.456	0.000	0.000	0.000

Problem 1630	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	147	147	73	0	0	0	0	0	-1
normalized size	1	1.00	0.50	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.089	0.030	0.053	0.000	0.479	0.000	0.000	0.000

Problem 1631	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	111	111	71	0	0	0	0	0	-1
normalized size	1	1.00	0.64	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.067	0.024	0.054	0.000	0.458	0.000	0.000	0.000

Problem 1632	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	104	104	71	0	0	0	0	0	-1
normalized size	1	1.00	0.68	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.064	0.023	0.084	0.000	0.473	0.000	0.000	0.000

Problem 1633	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	145	145	73	0	0	0	0	0	-1
normalized size	1	1.00	0.50	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.094	0.025	0.084	0.000	0.451	0.000	0.000	0.000

Problem 1634	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	185	185	73	0	0	0	0	0	-1
normalized size	1	1.00	0.39	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.128	0.026	0.085	0.000	0.463	0.000	0.000	0.000

Problem 1635	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	270	270	73	0	0	0	0	0	-1
normalized size	1	1.00	0.27	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.365	0.039	0.082	0.000	0.507	0.000	0.000	0.000

Problem 1636	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	232	232	73	0	0	0	0	0	-1
normalized size	1	1.00	0.31	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.246	0.030	0.050	0.000	0.480	0.000	0.000	0.000

Problem 1637	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	196	196	71	0	0	0	0	0	-1
normalized size	1	1.00	0.36	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.222	0.023	0.050	0.000	0.486	0.000	0.000	0.000

Problem 1638	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	184	184	71	0	0	0	0	0	-1
normalized size	1	1.00	0.39	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.215	0.023	0.085	0.000	0.466	0.000	0.000	0.000

Problem 1639	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	221	221	73	0	0	0	0	0	-1
normalized size	1	1.00	0.33	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.236	0.026	0.082	0.000	0.479	0.000	0.000	0.000

Problem 1640	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	270	270	73	0	0	0	0	0	-1
normalized size	1	1.00	0.27	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.285	0.031	0.086	0.000	0.478	0.000	0.000	0.000

Problem 1641	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	220	220	73	0	0	0	0	0	-1
normalized size	1	1.00	0.33	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.168	0.070	0.059	0.000	0.464	0.000	0.000	0.000

Problem 1642	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	182	182	73	0	0	0	218	0	-1
normalized size	1	1.00	0.40	0.00	0.00	0.00	1.20	0.00	-0.01
time (sec)	N/A	0.104	0.049	0.056	0.000	0.454	14.769	0.000	0.000

Problem 1643	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	144	144	71	0	0	0	0	0	-1
normalized size	1	1.00	0.49	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.084	0.039	0.057	0.000	0.452	0.000	0.000	0.000

Problem 1644	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	132	132	71	0	0	0	0	0	-1
normalized size	1	1.00	0.54	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.078	0.039	0.118	0.000	0.480	0.000	0.000	0.000

Problem 1645	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	135	135	73	0	0	0	0	0	-1
normalized size	1	1.00	0.54	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.076	0.045	0.086	0.000	0.482	0.000	0.000	0.000

Problem 1646	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	175	175	73	0	0	0	0	0	-1
normalized size	1	1.00	0.42	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.104	0.048	0.089	0.000	0.519	0.000	0.000	0.000

Problem 1647	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	213	213	73	0	0	0	0	0	-1
normalized size	1	1.00	0.34	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.120	0.052	0.082	0.000	0.558	0.000	0.000	0.000

Problem 1648	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	264	264	73	0	0	0	0	0	-1
normalized size	1	1.00	0.28	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.298	0.035	0.053	0.000	0.490	0.000	0.000	0.000

Problem 1649	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	229	229	73	0	0	0	0	0	-1
normalized size	1	1.00	0.32	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.245	0.031	0.049	0.000	0.477	0.000	0.000	0.000

Problem 1650	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	196	196	73	0	0	0	0	0	-1
normalized size	1	1.00	0.37	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.216	0.026	0.046	0.000	0.474	0.000	0.000	0.000

Problem 1651	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	167	167	71	0	0	0	0	0	-1
normalized size	1	1.00	0.43	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.194	0.022	0.085	0.000	0.481	0.000	0.000	0.000

Problem 1652	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	191	191	71	0	0	0	0	0	-1
normalized size	1	1.00	0.37	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.224	0.023	0.085	0.000	0.475	0.000	0.000	0.000

Problem 1653	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	224	224	73	0	0	0	0	0	-1
normalized size	1	1.00	0.33	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.262	0.024	0.087	0.000	0.475	0.000	0.000	0.000

Problem 1654	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	144	144	73	0	0	0	0	0	-1
normalized size	1	1.00	0.51	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.083	0.037	0.056	0.000	0.472	0.000	0.000	0.000

Problem 1655	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	111	111	73	0	0	0	0	0	-1
normalized size	1	1.00	0.66	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.067	0.029	0.049	0.000	0.444	0.000	0.000	0.000

Problem 1656	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	83	83	71	0	0	0	0	0	-1
normalized size	1	1.00	0.86	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.051	0.023	0.087	0.000	0.449	0.000	0.000	0.000

Problem 1657	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	111	111	71	0	0	0	0	0	-1
normalized size	1	1.00	0.64	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.060	0.023	0.086	0.000	0.457	0.000	0.000	0.000

Problem 1658	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	149	149	73	0	0	0	0	0	-1
normalized size	1	1.00	0.49	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.075	0.026	0.083	0.000	0.461	0.000	0.000	0.000

Problem 1659	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	254	254	73	0	0	0	0	0	-1
normalized size	1	1.00	0.29	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.262	0.062	0.112	0.000	0.481	0.000	0.000	0.000

Problem 1660	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	220	220	73	0	0	0	0	0	-1
normalized size	1	1.00	0.33	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.235	0.049	0.114	0.000	0.475	0.000	0.000	0.000

Problem 1661	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	190	190	73	0	0	0	0	0	-1
normalized size	1	1.00	0.38	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.207	0.042	0.086	0.000	0.485	0.000	0.000	0.000

Problem 1662	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	197	197	71	0	0	0	0	0	-1
normalized size	1	1.00	0.36	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.211	0.037	0.088	0.000	0.473	0.000	0.000	0.000

Problem 1663	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	222	222	71	0	0	0	0	0	-1
normalized size	1	1.00	0.32	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.231	0.036	0.093	0.000	0.473	0.000	0.000	0.000

Problem 1664	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	261	261	73	0	0	0	0	0	-1
normalized size	1	1.00	0.28	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.260	0.039	0.085	0.000	0.485	0.000	0.000	0.000

Problem 1665	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	207	207	73	0	0	0	0	0	-1
normalized size	1	1.00	0.35	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.136	0.076	0.115	0.000	0.489	0.000	0.000	0.000

Problem 1666	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	137	137	73	0	0	0	0	0	-1
normalized size	1	1.00	0.53	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.080	0.051	0.118	0.000	0.476	0.000	0.000	0.000

Problem 1667	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	111	111	73	0	0	0	0	0	-1
normalized size	1	1.00	0.66	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.064	0.046	0.084	0.000	0.459	0.000	0.000	0.000

Problem 1668	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	118	118	71	0	0	0	0	0	-1
normalized size	1	1.00	0.60	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.070	0.038	0.086	0.000	0.449	0.000	0.000	0.000

Problem 1669	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	146	146	71	0	0	0	0	0	-1
normalized size	1	1.00	0.49	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.078	0.036	0.082	0.000	0.481	0.000	0.000	0.000

Problem 1670	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	178	178	73	0	0	0	0	0	-1
normalized size	1	1.00	0.41	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.103	0.040	0.085	0.000	0.460	0.000	0.000	0.000

Problem 1671	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	286	286	73	0	0	0	0	0	-1
normalized size	1	1.00	0.26	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.297	0.088	0.153	0.000	0.530	0.000	0.000	0.000

Problem 1672	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	248	248	73	0	0	0	0	0	-1
normalized size	1	1.00	0.29	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.257	0.073	0.136	0.000	0.526	0.000	0.000	0.000

Problem 1673	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	222	222	73	0	0	0	0	0	-1
normalized size	1	1.00	0.33	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.235	0.063	0.085	0.000	0.487	0.000	0.000	0.000

Problem 1674	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	232	232	73	0	0	0	0	0	-1
normalized size	1	1.00	0.31	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.233	0.055	0.089	0.000	0.482	0.000	0.000	0.000

Problem 1675	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	236	236	71	0	0	0	0	0	-1
normalized size	1	1.00	0.30	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.236	0.044	0.096	0.000	0.479	0.000	0.000	0.000

Problem 1676	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	262	262	71	0	0	0	0	0	-1
normalized size	1	1.00	0.27	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.257	0.045	0.083	0.000	0.499	0.000	0.000	0.000

Problem 1677	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	303	303	73	0	0	0	0	0	-1
normalized size	1	1.00	0.24	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.290	0.050	0.088	0.000	0.501	0.000	0.000	0.000

Problem 1678	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	205	205	73	0	0	2151	0	0	-1
normalized size	1	1.00	0.36	0.00	0.00	10.49	0.00	0.00	-0.00
time (sec)	N/A	0.139	0.059	0.080	0.000	0.633	0.000	0.000	0.000

Problem 1679	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	167	167	73	0	0	1468	0	0	-1
normalized size	1	1.00	0.44	0.00	0.00	8.79	0.00	0.00	-0.01
time (sec)	N/A	0.102	0.043	0.045	0.000	0.594	0.000	0.000	0.000

Problem 1680	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	152	152	71	0	0	857	0	0	-1
normalized size	1	1.00	0.47	0.00	0.00	5.64	0.00	0.00	-0.01
time (sec)	N/A	0.098	0.047	0.105	0.000	0.533	0.000	0.000	0.000

Problem 1681	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	134	134	73	0	0	368	0	0	-1
normalized size	1	1.00	0.54	0.00	0.00	2.75	0.00	0.00	-0.01
time (sec)	N/A	0.088	0.053	0.092	0.000	0.485	0.000	0.000	0.000

Problem 1682	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	104	0	0	99
normalized size	1	1.00	1.00	0.84	0.00	3.25	0.00	0.00	3.09
time (sec)	N/A	0.003	0.015	0.004	0.000	0.473	0.000	0.000	0.810

Problem 1683	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	235	0	0	178
normalized size	1	1.00	0.70	0.82	0.00	3.56	0.00	0.00	2.70
time (sec)	N/A	0.009	0.027	0.006	0.000	0.514	0.000	0.000	0.955

Problem 1684	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	426	0	0	268
normalized size	1	1.00	0.76	1.04	0.00	4.22	0.00	0.00	2.65
time (sec)	N/A	0.017	0.049	0.006	0.000	0.575	0.000	0.000	1.126

Problem 1685	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	649	0	0	376
normalized size	1	1.00	0.87	1.26	0.00	4.77	0.00	0.00	2.76
time (sec)	N/A	0.029	0.067	0.013	0.000	0.683	0.000	0.000	1.360

Problem 1686	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	408	408	73	0	0	0	0	0	-1
normalized size	1	1.00	0.18	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.590	0.057	0.106	0.000	0.492	0.000	0.000	0.000

Problem 1687	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	370	370	73	0	0	0	0	0	-1
normalized size	1	1.00	0.20	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.378	0.051	0.058	0.000	0.479	0.000	0.000	0.000

Problem 1688	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	332	332	71	0	0	0	0	0	-1
normalized size	1	1.00	0.21	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.287	0.046	0.058	0.000	0.439	0.000	0.000	0.000

Problem 1689	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	325	325	73	0	0	0	0	0	-1
normalized size	1	1.00	0.22	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.278	0.041	0.121	0.000	0.443	0.000	0.000	0.000

Problem 1690	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	325	325	73	0	0	0	0	0	-1
normalized size	1	1.00	0.22	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.299	0.047	0.087	0.000	0.475	0.000	0.000	0.000

Problem 1691	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	363	363	73	0	0	0	0	0	-1
normalized size	1	1.00	0.20	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.352	0.051	0.088	0.000	0.502	0.000	0.000	0.000

Problem 1692	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	401	401	73	0	0	0	0	0	-1
normalized size	1	1.00	0.18	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.425	0.053	0.085	0.000	0.576	0.000	0.000	0.000

Problem 1693	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	167	167	73	0	0	1468	0	0	-1
normalized size	1	1.00	0.44	0.00	0.00	8.79	0.00	0.00	-0.01
time (sec)	N/A	0.102	0.031	0.077	0.000	0.585	0.000	0.000	0.000

Problem 1694	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	127	127	73	0	0	814	0	0	-1
normalized size	1	1.00	0.57	0.00	0.00	6.41	0.00	0.00	-0.01
time (sec)	N/A	0.074	0.026	0.042	0.000	0.487	0.000	0.000	0.000

Problem 1695	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	85	85	71	0	0	234	0	0	-1
normalized size	1	1.00	0.84	0.00	0.00	2.75	0.00	0.00	-0.01
time (sec)	N/A	0.058	0.029	0.092	0.000	0.449	0.000	0.000	0.000

Problem 1696	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	42	0	0	-1
normalized size	1	1.00	1.00	0.84	0.00	1.31	0.00	0.00	-0.03
time (sec)	N/A	0.003	0.012	0.005	0.000	0.435	0.000	0.000	0.000

Problem 1697	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	118	0	0	-1
normalized size	1	1.00	0.70	0.82	0.00	1.79	0.00	0.00	-0.02
time (sec)	N/A	0.009	0.017	0.005	0.000	0.585	0.000	0.000	0.000

Problem 1698	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	252	0	0	-1
normalized size	1	1.00	0.76	1.04	0.00	2.50	0.00	0.00	-0.01
time (sec)	N/A	0.017	0.033	0.009	0.000	1.030	0.000	0.000	0.000

Problem 1699	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	419	0	0	-1
normalized size	1	1.00	0.87	1.26	0.00	3.08	0.00	0.00	-0.01
time (sec)	N/A	0.031	0.049	0.010	0.000	2.122	0.000	0.000	0.000

Problem 1700	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	751	751	73	0	0	0	0	0	-1
normalized size	1	1.00	0.10	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.789	0.032	0.088	0.000	0.512	0.000	0.000	0.000

Problem 1701	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	705	705	73	0	0	0	0	0	-1
normalized size	1	1.00	0.10	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.617	0.027	0.090	0.000	0.549	0.000	0.000	0.000

Problem 1702	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	688	688	73	0	0	0	0	0	-1
normalized size	1	1.00	0.11	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.495	0.023	0.088	0.000	0.512	0.000	0.000	0.000

Problem 1703	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	718	718	71	0	0	0	0	0	-1
normalized size	1	1.00	0.10	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.609	0.024	0.084	0.000	0.515	0.000	0.000	0.000

Problem 1704	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	760	760	73	0	0	0	0	0	-1
normalized size	1	1.00	0.10	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.726	0.024	0.098	0.000	0.552	0.000	0.000	0.000

Problem 1705	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	167	167	73	0	0	1457	0	0	-1
normalized size	1	1.00	0.44	0.00	0.00	8.72	0.00	0.00	-0.01
time (sec)	N/A	0.105	0.035	0.046	0.000	0.583	0.000	0.000	0.000

Problem 1706	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	127	127	73	0	0	808	0	0	-1
normalized size	1	1.00	0.57	0.00	0.00	6.36	0.00	0.00	-0.01
time (sec)	N/A	0.081	0.028	0.042	0.000	0.532	0.000	0.000	0.000

Problem 1707	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	85	85	73	0	0	234	0	0	-1
normalized size	1	1.00	0.86	0.00	0.00	2.75	0.00	0.00	-0.01
time (sec)	N/A	0.067	0.031	0.092	0.000	0.460	0.000	0.000	0.000

Problem 1708	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	27	0	42	0	0	26
normalized size	1	1.00	1.00	0.90	0.00	1.40	0.00	0.00	0.87
time (sec)	N/A	0.003	0.007	0.005	0.000	0.504	0.000	0.000	0.706

Problem 1709	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	118	0	0	71
normalized size	1	1.00	0.70	0.82	0.00	1.79	0.00	0.00	1.08
time (sec)	N/A	0.009	0.015	0.005	0.000	0.864	0.000	0.000	0.868

Problem 1710	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	75	105	0	251	0	0	133
normalized size	1	1.00	0.74	1.04	0.00	2.49	0.00	0.00	1.32
time (sec)	N/A	0.017	0.033	0.007	0.000	0.690	0.000	0.000	1.020

Problem 1711	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	116	171	0	419	0	0	209
normalized size	1	1.00	0.85	1.26	0.00	3.08	0.00	0.00	1.54
time (sec)	N/A	0.028	0.048	0.010	0.000	0.769	0.000	0.000	1.260

Problem 1712	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	332	332	73	0	0	0	0	0	-1
normalized size	1	1.00	0.22	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.286	0.031	0.059	0.000	0.678	0.000	0.000	0.000

Problem 1713	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	295	295	73	0	0	0	0	0	-1
normalized size	1	1.00	0.25	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.224	0.027	0.056	0.000	0.615	0.000	0.000	0.000

Problem 1714	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	270	270	71	0	0	0	0	0	-1
normalized size	1	1.00	0.26	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.175	0.025	0.091	0.000	0.633	0.000	0.000	0.000

Problem 1715	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	306	306	73	0	0	0	0	0	-1
normalized size	1	1.00	0.24	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.215	0.025	0.095	0.000	0.629	0.000	0.000	0.000

Problem 1716	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	339	339	73	0	0	0	0	0	-1
normalized size	1	1.00	0.22	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.280	0.025	0.091	0.000	0.859	0.000	0.000	0.000

Problem 1717	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	152	152	73	0	0	857	0	0	-1
normalized size	1	1.00	0.48	0.00	0.00	5.64	0.00	0.00	-0.01
time (sec)	N/A	0.087	0.050	0.106	0.000	0.839	0.000	0.000	0.000

Problem 1718	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	108	108	73	0	0	273	0	0	-1
normalized size	1	1.00	0.68	0.00	0.00	2.53	0.00	0.00	-0.01
time (sec)	N/A	0.065	0.044	0.089	0.000	0.590	0.000	0.000	0.000

Problem 1719	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	27	0	42	0	0	-1
normalized size	1	1.00	1.00	0.90	0.00	1.40	0.00	0.00	-0.03
time (sec)	N/A	0.003	0.008	0.005	0.000	0.651	0.000	0.000	0.000

Problem 1720	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	45	53	0	126	0	0	-1
normalized size	1	1.00	0.68	0.80	0.00	1.91	0.00	0.00	-0.02
time (sec)	N/A	0.008	0.017	0.006	0.000	0.593	0.000	0.000	0.000

Problem 1721	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	76	105	0	273	0	0	-1
normalized size	1	1.00	0.75	1.04	0.00	2.70	0.00	0.00	-0.01
time (sec)	N/A	0.017	0.033	0.007	0.000	0.845	0.000	0.000	0.000

Problem 1722	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	116	171	0	457	0	0	-1
normalized size	1	1.00	0.85	1.26	0.00	3.36	0.00	0.00	-0.01
time (sec)	N/A	0.027	0.043	0.010	0.000	1.536	0.000	0.000	0.000

Problem 1723	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	776	776	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.880	0.060	0.095	0.000	1.118	0.000	0.000	0.000

Problem 1724	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	730	730	73	0	0	0	0	0	-1
normalized size	1	1.00	0.10	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.725	0.066	0.097	0.000	0.726	0.000	0.000	0.000

Problem 1725	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	712	712	73	0	0	0	0	0	-1
normalized size	1	1.00	0.10	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.609	0.060	0.092	0.000	0.633	0.000	0.000	0.000

Problem 1726	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	719	719	73	0	0	0	0	0	-1
normalized size	1	1.00	0.10	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.612	0.051	0.091	0.000	0.930	0.000	0.000	0.000

Problem 1727	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	750	750	71	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.740	0.054	0.090	0.000	1.227	0.000	0.000	0.000

Problem 1728	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	795	795	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.865	0.053	0.092	0.000	0.858	0.000	0.000	0.000

Problem 1729	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	279	279	65	0	0	247	0	0	-1
normalized size	1	1.00	0.23	0.00	0.00	0.89	0.00	0.00	-0.00
time (sec)	N/A	0.304	0.037	0.088	0.000	0.795	0.000	0.000	0.000

Problem 1730	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	193	193	42	0	0	448	0	0	-1
normalized size	1	1.00	0.22	0.00	0.00	2.32	0.00	0.00	-0.01
time (sec)	N/A	0.138	0.010	0.082	0.000	0.651	0.000	0.000	0.000

Problem 1731	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.029	0.034	0.194	0.000	4.078	0.000	0.000	0.000

Problem 1732	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.026	0.092	0.000	4.409	0.000	0.000	0.000

Problem 1733	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	71	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.022	0.092	0.000	5.558	0.000	0.000	0.000

Problem 1734	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	71	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.023	0.096	0.000	4.858	0.000	0.000	0.000

Problem 1735	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.023	0.089	0.000	5.751	0.000	0.000	0.000

Problem 1736	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	487	487	73	0	0	0	0	0	-1
normalized size	1	1.00	0.15	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.522	0.043	0.153	0.000	1.224	0.000	0.000	0.000

Problem 1737	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	449	449	73	0	0	0	0	0	-1
normalized size	1	1.00	0.16	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.336	0.032	0.079	0.000	0.748	0.000	0.000	0.000

Problem 1738	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	411	411	73	0	0	0	0	0	-1
normalized size	1	1.00	0.18	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.284	0.028	0.077	0.000	0.638	0.000	0.000	0.000

Problem 1739	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	375	375	71	0	0	0	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.233	0.024	0.085	0.000	0.815	0.000	0.000	0.000

Problem 1740	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	367	367	71	0	0	0	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.229	0.026	0.097	0.000	0.647	0.000	0.000	0.000

Problem 1741	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	409	409	73	0	0	0	0	0	-1
normalized size	1	1.00	0.18	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.280	0.024	0.089	0.000	0.849	0.000	0.000	0.000

Problem 1742	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	896	896	73	0	0	0	0	0	-1
normalized size	1	1.00	0.08	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.078	0.039	0.099	0.000	1.035	0.000	0.000	0.000

Problem 1743	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	858	858	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.823	0.032	0.058	0.000	0.924	0.000	0.000	0.000

Problem 1744	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	817	817	71	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.710	0.023	0.060	0.000	1.175	0.000	0.000	0.000

Problem 1745	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	798	798	71	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.684	0.023	0.091	0.000	1.422	0.000	0.000	0.000

Problem 1746	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	854	854	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.798	0.025	0.093	0.000	0.978	0.000	0.000	0.000

Problem 1747	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	896	896	73	0	0	0	0	0	-1
normalized size	1	1.00	0.08	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.901	0.026	0.092	0.000	1.159	0.000	0.000	0.000

Problem 1748	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	890	890	73	0	0	0	0	0	-1
normalized size	1	1.00	0.08	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.952	0.034	0.063	0.000	1.517	0.000	0.000	0.000

Problem 1749	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	855	855	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.790	0.033	0.059	0.000	1.077	0.000	0.000	0.000

Problem 1750	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	820	820	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.690	0.026	0.059	0.000	1.262	0.000	0.000	0.000

Problem 1751	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	780	780	71	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.582	0.022	0.090	0.000	0.903	0.000	0.000	0.000

Problem 1752	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	813	813	71	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.677	0.023	0.086	0.000	1.157	0.000	0.000	0.000

Problem 1753	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	858	858	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.752	0.024	0.095	0.000	1.201	0.000	0.000	0.000

Problem 1754	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	440	440	73	0	0	0	0	0	-1
normalized size	1	1.00	0.17	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.327	0.051	0.087	0.000	0.899	0.000	0.000	0.000

Problem 1755	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	405	405	73	0	0	0	0	0	-1
normalized size	1	1.00	0.18	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.279	0.044	0.081	0.000	0.634	0.000	0.000	0.000

Problem 1756	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	372	372	73	0	0	0	0	0	-1
normalized size	1	1.00	0.20	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.236	0.033	0.078	0.000	0.900	0.000	0.000	0.000

Problem 1757	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	343	343	71	0	0	0	0	0	-1
normalized size	1	1.00	0.21	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.194	0.039	0.098	0.000	0.737	0.000	0.000	0.000

Problem 1758	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	372	372	71	0	0	0	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.231	0.025	0.097	0.000	0.681	0.000	0.000	0.000

Problem 1759	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	410	410	73	0	0	0	0	0	-1
normalized size	1	1.00	0.18	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.268	0.032	0.092	0.000	0.756	0.000	0.000	0.000

Problem 1760	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	880	880	73	0	0	0	0	0	-1
normalized size	1	1.00	0.08	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.901	0.077	0.133	0.000	0.957	0.000	0.000	0.000

Problem 1761	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	844	844	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.773	0.068	0.129	0.000	1.017	0.000	0.000	0.000

Problem 1762	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	806	806	73	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.668	0.049	0.091	0.000	0.971	0.000	0.000	0.000

Problem 1763	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	817	817	71	0	0	0	0	0	-1
normalized size	1	1.00	0.09	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.672	0.042	0.090	0.000	1.155	0.000	0.000	0.000

Problem 1764	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	844	844	71	0	0	0	0	0	-1
normalized size	1	1.00	0.08	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.759	0.042	0.099	0.000	1.198	0.000	0.000	0.000

Problem 1765	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	893	893	73	0	0	0	0	0	-1
normalized size	1	1.00	0.08	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.868	0.055	0.093	0.000	0.874	0.000	0.000	0.000

Problem 1766	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	73	0	0	0	0	0	-1
normalized size	1	1.00	0.87	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.110	0.190	0.000	0.739	0.000	0.000	0.000

Problem 1767	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	73	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.024	0.064	0.095	0.000	0.640	0.000	0.000	0.000

Problem 1768	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.038	0.098	0.000	0.668	0.000	0.000	0.000

Problem 1769	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.040	0.095	0.000	0.908	0.000	0.000	0.000

Problem 1770	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	73	0	0	0	0	0	-1
normalized size	1	1.00	0.90	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.072	0.098	0.000	0.666	0.000	0.000	0.000

Problem 1771	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	81	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.051	0.092	0.000	0.710	0.000	0.000	0.000

Problem 1772	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	427	427	73	0	0	5633	0	0	-1
normalized size	1	1.00	0.17	0.00	0.00	13.19	0.00	0.00	-0.00
time (sec)	N/A	0.643	0.053	0.105	0.000	1.180	0.000	0.000	0.000

Problem 1773	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	378	378	73	0	0	3025	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	8.00	0.00	0.00	-0.00
time (sec)	N/A	0.497	0.041	0.052	0.000	0.927	0.000	0.000	0.000

Problem 1774	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	332	332	73	0	0	663	0	0	-1
normalized size	1	1.00	0.22	0.00	0.00	2.00	0.00	0.00	-0.00
time (sec)	N/A	0.487	0.056	0.097	0.000	0.916	0.000	0.000	0.000

Problem 1775	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	65	0	0	130
normalized size	1	1.00	1.00	0.84	0.00	2.03	0.00	0.00	4.06
time (sec)	N/A	0.003	0.015	0.006	0.000	0.840	0.000	0.000	0.565

Problem 1776	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	175	0	0	137
normalized size	1	1.00	0.70	0.82	0.00	2.65	0.00	0.00	2.08
time (sec)	N/A	0.009	0.034	0.006	0.000	0.792	0.000	0.000	0.750

Problem 1777	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	338	0	0	213
normalized size	1	1.00	0.76	1.04	0.00	3.35	0.00	0.00	2.11
time (sec)	N/A	0.021	0.057	0.009	0.000	0.881	0.000	0.000	0.949

Problem 1778	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	533	0	0	302
normalized size	1	1.00	0.87	1.26	0.00	3.92	0.00	0.00	2.22
time (sec)	N/A	0.034	0.082	0.011	0.000	0.808	0.000	0.000	1.147

Problem 1779	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	427	427	73	0	0	5633	0	0	-1
normalized size	1	1.00	0.17	0.00	0.00	13.19	0.00	0.00	-0.00
time (sec)	N/A	0.642	0.047	0.098	0.000	1.260	0.000	0.000	0.000

Problem 1780	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	378	378	73	0	0	2997	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	7.93	0.00	0.00	-0.00
time (sec)	N/A	0.557	0.037	0.050	0.000	1.277	0.000	0.000	0.000

Problem 1781	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	334	334	73	0	0	755	0	0	-1
normalized size	1	1.00	0.22	0.00	0.00	2.26	0.00	0.00	-0.00
time (sec)	N/A	0.561	0.072	0.092	0.000	1.012	0.000	0.000	0.000

Problem 1782	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	65	0	0	130
normalized size	1	1.00	1.00	0.84	0.00	2.03	0.00	0.00	4.06
time (sec)	N/A	0.003	0.011	0.004	0.000	0.787	0.000	0.000	0.587

Problem 1783	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	175	0	0	137
normalized size	1	1.00	0.70	0.82	0.00	2.65	0.00	0.00	2.08
time (sec)	N/A	0.009	0.032	0.005	0.000	0.900	0.000	0.000	0.744

Problem 1784	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	338	0	0	214
normalized size	1	1.00	0.76	1.04	0.00	3.35	0.00	0.00	2.12
time (sec)	N/A	0.020	0.055	0.008	0.000	1.116	0.000	0.000	0.944

Problem 1785	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	533	0	0	303
normalized size	1	1.00	0.87	1.26	0.00	3.92	0.00	0.00	2.23
time (sec)	N/A	0.033	0.089	0.010	0.000	0.814	0.000	0.000	1.158

Problem 1786	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	73	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.026	0.083	0.095	0.000	1.777	0.000	0.000	0.000

Problem 1787	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.036	0.095	0.000	2.092	0.000	0.000	0.000

Problem 1788	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.043	0.095	0.000	1.716	0.000	0.000	0.000

Problem 1789	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	73	0	0	0	0	0	-1
normalized size	1	1.00	0.90	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.059	0.092	0.000	2.133	0.000	0.000	0.000

Problem 1790	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	73	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.022	0.078	0.102	0.000	1.788	0.000	0.000	0.000

Problem 1791	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	81	0	0	0	0	0	-1
normalized size	1	1.00	0.96	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.022	0.048	0.091	0.000	1.808	0.000	0.000	0.000

Problem 1792	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	73	0	0	0	0	0	-1
normalized size	1	1.00	0.87	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.114	0.102	0.000	1.084	0.000	0.000	0.000

Problem 1793	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	73	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.022	0.074	0.094	0.000	1.035	0.000	0.000	0.000

Problem 1794	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.040	0.095	0.000	0.768	0.000	0.000	0.000

Problem 1795	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.018	0.040	0.097	0.000	0.913	0.000	0.000	0.000

Problem 1796	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	73	0	0	0	0	0	-1
normalized size	1	1.00	0.90	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.019	0.069	0.165	0.000	1.006	0.000	0.000	0.000

Problem 1797	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	81	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.048	0.096	0.000	0.825	0.000	0.000	0.000

Problem 1798	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	424	424	73	0	0	5633	0	0	-1
normalized size	1	1.00	0.17	0.00	0.00	13.29	0.00	0.00	-0.00
time (sec)	N/A	0.552	0.039	0.058	0.000	1.140	0.000	0.000	0.000

Problem 1799	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	403	403	73	0	0	3084	0	0	-1
normalized size	1	1.00	0.18	0.00	0.00	7.65	0.00	0.00	-0.00
time (sec)	N/A	0.526	0.066	0.136	0.000	1.214	0.000	0.000	0.000

Problem 1800	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	358	358	73	0	0	855	0	0	-1
normalized size	1	1.00	0.20	0.00	0.00	2.39	0.00	0.00	-0.00
time (sec)	N/A	0.501	0.085	0.096	0.000	1.143	0.000	0.000	0.000

Problem 1801	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	104	0	0	199
normalized size	1	1.00	1.00	0.84	0.00	3.25	0.00	0.00	6.22
time (sec)	N/A	0.003	0.023	0.006	0.000	0.905	0.000	0.000	0.756

Problem 1802	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	235	0	0	189
normalized size	1	1.00	0.70	0.82	0.00	3.56	0.00	0.00	2.86
time (sec)	N/A	0.009	0.036	0.004	0.000	0.999	0.000	0.000	0.907

Problem 1803	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	427	0	0	278
normalized size	1	1.00	0.76	1.04	0.00	4.23	0.00	0.00	2.75
time (sec)	N/A	0.018	0.060	0.008	0.000	1.002	0.000	0.000	1.144

Problem 1804	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	649	0	0	385
normalized size	1	1.00	0.87	1.26	0.00	4.77	0.00	0.00	2.83
time (sec)	N/A	0.030	0.094	0.010	0.000	1.042	0.000	0.000	1.429

Problem 1805	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	424	424	73	0	0	5633	0	0	-1
normalized size	1	1.00	0.17	0.00	0.00	13.29	0.00	0.00	-0.00
time (sec)	N/A	0.610	0.054	0.056	0.000	1.305	0.000	0.000	0.000

Problem 1806	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	378	378	73	0	0	3025	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	8.00	0.00	0.00	-0.00
time (sec)	N/A	0.560	0.036	0.051	0.000	1.220	0.000	0.000	0.000

Problem 1807	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	309	309	73	0	0	620	0	0	-1
normalized size	1	1.00	0.24	0.00	0.00	2.01	0.00	0.00	-0.00
time (sec)	N/A	0.509	0.047	0.098	0.000	1.084	0.000	0.000	0.000

Problem 1808	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	27	0	42	0	0	27
normalized size	1	1.00	1.00	0.84	0.00	1.31	0.00	0.00	0.84
time (sec)	N/A	0.003	0.013	0.004	0.000	0.976	0.000	0.000	0.763

Problem 1809	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	54	0	118	0	0	127
normalized size	1	1.00	0.70	0.82	0.00	1.79	0.00	0.00	1.92
time (sec)	N/A	0.010	0.027	0.005	0.000	0.915	0.000	0.000	0.860

Problem 1810	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	252	0	0	203
normalized size	1	1.00	0.76	1.04	0.00	2.50	0.00	0.00	2.01
time (sec)	N/A	0.020	0.045	0.008	0.000	0.827	0.000	0.000	1.033

Problem 1811	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	420	0	0	292
normalized size	1	1.00	0.87	1.26	0.00	3.09	0.00	0.00	2.15
time (sec)	N/A	0.030	0.068	0.010	0.000	0.986	0.000	0.000	1.200

Problem 1812	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	73	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.024	0.068	0.091	0.000	1.899	0.000	0.000	0.000

Problem 1813	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.036	0.095	0.000	2.063	0.000	0.000	0.000

Problem 1814	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	74	74	73	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.031	0.101	0.000	1.820	0.000	0.000	0.000

Problem 1815	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	73	0	0	0	0	0	-1
normalized size	1	1.00	0.90	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.046	0.096	0.000	1.878	0.000	0.000	0.000

Problem 1816	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	73	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.059	0.092	0.000	1.594	0.000	0.000	0.000

Problem 1817	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	81	0	0	0	0	0	-1
normalized size	1	1.00	0.96	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.044	0.099	0.000	1.644	0.000	0.000	0.000

Problem 1818	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	71	0	0	0	0	0	-1
normalized size	1	1.00	0.87	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.088	0.100	0.000	1.007	0.000	0.000	0.000

Problem 1819	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	71	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.022	0.046	0.092	0.000	0.997	0.000	0.000	0.000

Problem 1820	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	71	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.019	0.031	0.088	0.000	0.979	0.000	0.000	0.000

Problem 1821	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	71	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.038	0.094	0.000	0.614	0.000	0.000	0.000

Problem 1822	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	71	0	0	0	0	0	-1
normalized size	1	1.00	0.90	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.019	0.058	0.092	0.000	1.017	0.000	0.000	0.000

Problem 1823	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	79	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.020	0.040	0.102	0.000	0.827	0.000	0.000	0.000

Problem 1824	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F(-1)	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	424	424	71	0	0	5591	0	0	-1
normalized size	1	1.00	0.17	0.00	0.00	13.19	0.00	0.00	-0.00
time (sec)	N/A	0.549	0.056	0.059	0.000	1.320	0.000	0.000	0.000

Problem 1825	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	378	378	71	0	0	2997	0	0	-1
normalized size	1	1.00	0.19	0.00	0.00	7.93	0.00	0.00	-0.00
time (sec)	N/A	0.479	0.034	0.055	0.000	0.849	0.000	0.000	0.000

Problem 1826	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	309	309	71	0	0	620	0	0	-1
normalized size	1	1.00	0.23	0.00	0.00	2.01	0.00	0.00	-0.00
time (sec)	N/A	0.444	0.042	0.099	0.000	1.047	0.000	0.000	0.000

Problem 1827	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	27	0	42	0	0	-1
normalized size	1	1.00	1.00	0.90	0.00	1.40	0.00	0.00	-0.03
time (sec)	N/A	0.003	0.010	0.004	0.000	0.938	0.000	0.000	0.000

Problem 1828	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	46	53	0	118	0	0	-1
normalized size	1	1.00	0.70	0.80	0.00	1.79	0.00	0.00	-0.02
time (sec)	N/A	0.009	0.016	0.006	0.000	0.860	0.000	0.000	0.000

Problem 1829	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	101	101	77	105	0	252	0	0	-1
normalized size	1	1.00	0.76	1.04	0.00	2.50	0.00	0.00	-0.01
time (sec)	N/A	0.018	0.036	0.008	0.000	0.624	0.000	0.000	0.000

Problem 1830	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	118	171	0	420	0	0	-1
normalized size	1	1.00	0.87	1.26	0.00	3.09	0.00	0.00	-0.01
time (sec)	N/A	0.031	0.060	0.010	0.000	0.915	0.000	0.000	0.000

Problem 1831	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	449	449	71	0	0	5690	0	0	-1
normalized size	1	1.00	0.16	0.00	0.00	12.67	0.00	0.00	-0.00
time (sec)	N/A	0.660	0.079	0.124	0.000	1.396	0.000	0.000	0.000

Problem 1832	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	403	403	71	0	0	3084	0	0	-1
normalized size	1	1.00	0.18	0.00	0.00	7.65	0.00	0.00	-0.00
time (sec)	N/A	0.596	0.055	0.126	0.000	1.261	0.000	0.000	0.000

Problem 1833	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	332	332	71	0	0	663	0	0	-1
normalized size	1	1.00	0.21	0.00	0.00	2.00	0.00	0.00	-0.00
time (sec)	N/A	0.541	0.031	0.095	0.000	0.929	0.000	0.000	0.000

Problem 1834	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	27	0	42	0	0	26
normalized size	1	1.00	1.00	0.90	0.00	1.40	0.00	0.00	0.87
time (sec)	N/A	0.003	0.010	0.006	0.000	0.949	0.000	0.000	0.680

Problem 1835	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	45	53	0	126	0	0	72
normalized size	1	1.00	0.70	0.83	0.00	1.97	0.00	0.00	1.12
time (sec)	N/A	0.011	0.027	0.007	0.000	0.978	0.000	0.000	0.834

Problem 1836	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	77	105	0	273	0	0	132
normalized size	1	1.00	0.79	1.07	0.00	2.79	0.00	0.00	1.35
time (sec)	N/A	0.020	0.040	0.007	0.000	0.707	0.000	0.000	0.960

Problem 1837	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	134	134	118	171	0	457	0	0	209
normalized size	1	1.00	0.88	1.28	0.00	3.41	0.00	0.00	1.56
time (sec)	N/A	0.033	0.063	0.012	0.000	1.092	0.000	0.000	1.146

Problem 1838	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	71	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.024	0.065	0.094	0.000	1.788	0.000	0.000	0.000

Problem 1839	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	71	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.029	0.098	0.000	1.681	0.000	0.000	0.000

Problem 1840	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	71	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.028	0.096	0.000	1.854	0.000	0.000	0.000

Problem 1841	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	71	0	0	0	0	0	-1
normalized size	1	1.00	0.90	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.046	0.100	0.000	1.638	0.000	0.000	0.000

Problem 1842	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	71	0	0	0	0	0	-1
normalized size	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.021	0.059	0.102	0.000	1.522	0.000	0.000	0.000

Problem 1843	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	79	0	0	0	0	0	-1
normalized size	1	1.00	0.96	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.022	0.052	0.102	0.000	1.690	0.000	0.000	0.000

Problem 1844	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	11	12	106	17	20	23	11
normalized size	1	1.00	1.00	1.09	9.64	1.55	1.82	2.09	1.00
time (sec)	N/A	0.002	0.013	0.003	1.123	0.993	0.269	0.996	0.462

Problem 1845	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	61	74	73	0	0	0	0	0	-1
normalized size	1	1.21	1.20	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.026	0.037	0.101	0.000	0.683	0.000	0.000	0.000

Problem 1846	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	110	110	94	389	246	497	4058	833	478
normalized size	1	1.00	0.85	3.54	2.24	4.52	36.89	7.57	4.35
time (sec)	N/A	0.055	0.107	0.009	1.166	0.944	4.666	1.036	0.942

Problem 1847	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	67	159	138	235	1506	385	226
normalized size	1	1.00	0.86	2.04	1.77	3.01	19.31	4.94	2.90
time (sec)	N/A	0.032	0.096	0.008	1.147	0.942	2.137	0.970	0.655

Problem 1848	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	41	49	63	83	377	132	88
normalized size	1	1.00	0.89	1.07	1.37	1.80	8.20	2.87	1.91
time (sec)	N/A	0.018	0.033	0.003	1.063	0.997	0.856	0.859	0.484

Problem 1849	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	51	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.011	0.012	0.094	0.000	0.802	0.000	0.000	0.000

Problem 1850	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	52	52	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.011	0.022	0.099	0.000	0.843	0.000	0.000	0.000

Problem 1851	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	54	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.013	0.020	0.093	0.000	0.964	0.000	0.000	0.000

Problem 1852	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	111	111	95	386	246	496	4058	833	478
normalized size	1	1.00	0.86	3.48	2.22	4.47	36.56	7.50	4.31
time (sec)	N/A	0.057	0.110	0.009	1.295	0.926	4.439	0.979	0.913

Problem 1853	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	67	159	138	237	1506	385	226
normalized size	1	1.00	0.86	2.04	1.77	3.04	19.31	4.94	2.90
time (sec)	N/A	0.032	0.096	0.008	1.168	1.196	2.089	0.925	0.618

Problem 1854	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	41	46	63	83	377	132	88
normalized size	1	1.00	0.87	0.98	1.34	1.77	8.02	2.81	1.87
time (sec)	N/A	0.018	0.037	0.003	1.169	0.944	0.822	0.999	0.494

Problem 1855	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	17	19	18	20	20	18	18
normalized size	1	1.00	0.94	1.06	1.00	1.11	1.11	1.00	1.00
time (sec)	N/A	0.003	0.011	0.003	1.116	0.697	0.063	1.018	0.379

Problem 1856	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	51	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.012	0.010	0.092	0.000	0.643	0.000	0.000	0.000

Problem 1857	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	52	0	0	0	0	0	-1
normalized size	1	1.00	1.02	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.011	0.022	0.099	0.000	0.688	0.000	0.000	0.000

Problem 1858	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	54	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.015	0.020	0.096	0.000	0.654	0.000	0.000	0.000

Problem 1859	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	143	143	112	322	0	512	0	0	528
normalized size	1	1.00	0.78	2.25	0.00	3.58	0.00	0.00	3.69
time (sec)	N/A	0.063	0.097	0.007	0.000	0.927	0.000	0.000	1.096

Problem 1860	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	59	127	0	206	0	0	220
normalized size	1	1.00	0.69	1.48	0.00	2.40	0.00	0.00	2.56
time (sec)	N/A	0.012	0.039	0.006	0.000	0.885	0.000	0.000	0.767

Problem 1861	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-2)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	39	39	36	45	0	60	0	0	102
normalized size	1	1.00	0.92	1.15	0.00	1.54	0.00	0.00	2.62
time (sec)	N/A	0.004	0.017	0.003	0.000	1.050	0.000	0.000	0.559

Problem 1862	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	65	0	0	0	0	0	-1
normalized size	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.024	0.031	0.099	0.000	0.855	0.000	0.000	0.000

Problem 1863	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	71	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.023	0.028	0.098	0.000	0.787	0.000	0.000	0.000

Problem 1864	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	89	0	0	0	0	0	-1
normalized size	1	1.00	1.24	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.023	0.058	0.097	0.000	0.739	0.000	0.000	0.000

Problem 1865	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	92	0	0	0	0	0	-1
normalized size	1	1.00	1.28	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.023	0.049	0.094	0.000	0.805	0.000	0.000	0.000

Problem 1866	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	71	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.031	0.030	0.100	0.000	1.083	0.000	0.000	0.000

Problem 1867	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	75	75	74	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.024	0.030	0.093	0.000	0.675	0.000	0.000	0.000

Problem 1868	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-2)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	38	41	0	59	0	0	97
normalized size	1	1.00	1.03	1.11	0.00	1.59	0.00	0.00	2.62
time (sec)	N/A	0.006	0.021	0.004	0.000	0.729	0.000	0.000	0.532

Problem 1869	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	60	123	0	207	0	0	214
normalized size	1	1.00	0.75	1.54	0.00	2.59	0.00	0.00	2.68
time (sec)	N/A	0.020	0.033	0.004	0.000	0.977	0.000	0.000	0.736

Problem 1870	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	131	131	113	318	0	509	0	0	525
normalized size	1	1.00	0.86	2.43	0.00	3.89	0.00	0.00	4.01
time (sec)	N/A	0.046	0.084	0.008	0.000	0.987	0.000	0.000	0.992

Problem 1871	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	186	186	195	661	0	959	0	0	944
normalized size	1	1.00	1.05	3.55	0.00	5.16	0.00	0.00	5.08
time (sec)	N/A	0.086	0.124	0.010	0.000	0.982	0.000	0.000	1.642

Problem 1872	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	71	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.023	0.024	0.000	0.000	0.979	0.000	0.000	0.000

Problem 1873	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	75	75	74	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.026	0.030	0.101	0.000	0.581	0.000	0.000	0.000

Problem 1874	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	36	42	0	58	0	0	98
normalized size	1	1.00	1.00	1.17	0.00	1.61	0.00	0.00	2.72
time (sec)	N/A	0.005	0.013	0.005	0.000	0.836	0.000	0.000	0.556

Problem 1875	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	59	124	0	205	0	0	214
normalized size	1	1.00	0.75	1.57	0.00	2.59	0.00	0.00	2.71
time (sec)	N/A	0.017	0.037	0.005	0.000	0.564	0.000	0.000	0.745

Problem 1876	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	130	130	112	319	0	507	0	0	528
normalized size	1	1.00	0.86	2.45	0.00	3.90	0.00	0.00	4.06
time (sec)	N/A	0.037	0.092	0.007	0.000	0.790	0.000	0.000	1.023

Problem 1877	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	B	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	185	185	195	662	0	954	0	0	945
normalized size	1	1.00	1.05	3.58	0.00	5.16	0.00	0.00	5.11
time (sec)	N/A	0.062	0.129	0.009	0.000	0.731	0.000	0.000	1.609

Problem 1878	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	83	83	75	0	0	0	0	0	-1
normalized size	1	1.00	0.90	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.029	0.059	0.099	0.000	0.571	0.000	0.000	0.000

Problem 1879	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	83	0	0	0	0	0	-1
normalized size	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.030	0.050	0.100	0.000	0.741	0.000	0.000	0.000

Problem 1880	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	51	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.009	0.019	0.000	0.000	0.760	0.000	0.000	0.000

Problem 1881	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	53	57	92	93	233	78	46
normalized size	1	1.00	0.93	1.00	1.61	1.63	4.09	1.37	0.81
time (sec)	N/A	0.030	0.030	0.008	1.162	0.686	0.694	0.923	0.439

Problem 1882	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	54	57	0	85	0	0	81
normalized size	1	1.00	0.57	0.60	0.00	0.89	0.00	0.00	0.85
time (sec)	N/A	0.036	0.074	0.006	0.000	0.721	0.000	0.000	1.037

Problem 1883	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	97	97	46	66	0	84	0	0	119
normalized size	1	1.00	0.47	0.68	0.00	0.87	0.00	0.00	1.23
time (sec)	N/A	0.022	0.040	0.004	0.000	0.791	0.000	0.000	2.138

Problem 1884	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	97	97	46	66	0	84	0	0	142
normalized size	1	1.00	0.47	0.68	0.00	0.87	0.00	0.00	1.46
time (sec)	N/A	0.018	0.066	0.005	0.000	1.075	0.000	0.000	0.850

Problem 1885	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	0	0	0	29	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.97	0.00	-0.03
time (sec)	N/A	0.007	0.007	0.098	0.000	0.947	2.108	0.000	0.000

Problem 1886	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	35	0	0	0	31	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.89	0.00	-0.03
time (sec)	N/A	0.006	0.013	0.094	0.000	0.482	2.124	0.000	0.000

Problem 1887	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	33	0	0	0	37	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	1.12	0.00	-0.03
time (sec)	N/A	0.007	0.017	0.097	0.000	0.479	89.943	0.000	0.000

Problem 1888	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	37	0	0	0	42	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	1.14	0.00	-0.03
time (sec)	N/A	0.005	0.024	0.104	0.000	0.474	90.089	0.000	0.000

Problem 1889	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	47	0	0	0	42	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.89	0.00	-0.02
time (sec)	N/A	0.014	0.020	0.090	0.000	0.483	25.034	0.000	0.000

Problem 1890	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	88	0	0	0	0	0	-1
normalized size	1	1.00	1.96	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.019	0.042	0.147	0.000	0.474	0.000	0.000	0.000

Problem 1891	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	28	23	22	22	22	22	22
normalized size	1	1.00	1.00	0.82	0.79	0.79	0.79	0.79	0.79
time (sec)	N/A	0.005	0.000	0.000	1.073	0.390	0.060	1.009	0.037

Problem 1892	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	12	11	11	8	11	10
normalized size	1	1.00	1.00	0.80	0.73	0.73	0.53	0.73	0.67
time (sec)	N/A	0.002	0.000	0.000	1.082	0.382	0.054	1.084	0.021

Problem 1893	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	11	10	9	9	5	9	8
normalized size	1	1.00	1.00	0.91	0.82	0.82	0.45	0.82	0.73
time (sec)	N/A	0.002	0.000	0.000	0.962	0.377	0.054	0.941	0.017

Problem 1894	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	9	9	9	10	9	9	7	9	7
normalized size	1	1.00	1.00	1.11	1.00	1.00	0.78	1.00	0.78
time (sec)	N/A	0.001	0.000	0.000	1.015	0.421	0.053	0.961	0.029

Problem 1895	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	12	12	10	12	12
normalized size	1	1.00	1.00	0.93	0.86	0.86	0.71	0.86	0.86
time (sec)	N/A	0.002	0.000	0.000	1.000	0.431	0.055	1.059	0.020

Problem 1896	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	11	10	9	9	8	9	10
normalized size	1	1.00	1.00	0.91	0.82	0.82	0.73	0.82	0.91
time (sec)	N/A	0.001	0.000	0.001	1.097	0.399	0.054	1.104	0.019

Problem 1897	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	12	11	11	8	11	8
normalized size	1	1.00	1.00	0.80	0.73	0.73	0.53	0.73	0.53
time (sec)	N/A	0.002	0.000	0.001	1.054	0.396	0.055	0.886	0.021

Problem 1898	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	15	14	14	15	14	13
normalized size	1	1.00	1.00	0.83	0.78	0.78	0.83	0.78	0.72
time (sec)	N/A	0.003	0.000	0.000	0.971	0.370	0.057	0.848	0.024

Problem 1899	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	17	16	16	12	16	15
normalized size	1	1.00	1.00	0.85	0.80	0.80	0.60	0.80	0.75
time (sec)	N/A	0.003	0.000	0.000	0.973	0.384	0.054	1.098	0.026

Problem 1900	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	13	12	12	10	12	12
normalized size	1	1.00	1.00	0.81	0.75	0.75	0.62	0.75	0.75
time (sec)	N/A	0.002	0.000	0.000	0.984	0.391	0.056	0.959	0.023

Problem 1901	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	14	13	13	12	13	13
normalized size	1	1.00	1.00	1.08	1.00	1.00	0.92	1.00	1.00
time (sec)	N/A	0.002	0.000	0.000	1.145	0.385	0.057	1.005	0.028

Problem 1902	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	22	21	20	27	20	21	20
normalized size	1	1.00	1.00	0.95	0.91	1.23	0.91	0.95	0.91
time (sec)	N/A	0.004	0.007	0.002	1.034	0.441	0.160	0.848	0.037

Problem 1903	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	22	17	16	17	15	16	17
normalized size	1	1.00	1.00	0.77	0.73	0.77	0.68	0.73	0.77
time (sec)	N/A	0.003	0.001	0.001	1.084	0.429	0.081	0.809	0.029

Problem 1904	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	14	13	17	14	14	11
normalized size	1	1.00	1.00	0.93	0.87	1.13	0.93	0.93	0.73
time (sec)	N/A	0.002	0.002	0.001	1.041	0.467	0.085	1.082	0.029

Problem 1905	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	10	10	10	11	10	11	7	11	10
normalized size	1	1.00	1.00	1.10	1.00	1.10	0.70	1.10	1.00
time (sec)	N/A	0.002	0.002	0.002	1.026	0.473	0.078	1.119	0.033

Problem 1906	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	12	11	12	10	11	12
normalized size	1	1.00	1.00	0.80	0.73	0.80	0.67	0.73	0.80
time (sec)	N/A	0.002	0.001	0.000	0.965	0.425	0.083	1.075	0.025

Problem 1907	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	11	11	11	10	9	9	8	10	9
normalized size	1	1.00	1.00	0.91	0.82	0.82	0.73	0.91	0.82
time (sec)	N/A	0.001	0.001	0.001	0.919	0.435	0.076	0.888	0.027

Problem 1908	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	12	11	10	8	11	10
normalized size	1	1.00	1.00	0.92	0.85	0.77	0.62	0.85	0.77
time (sec)	N/A	0.002	0.002	0.001	0.966	0.408	0.076	0.902	0.031

Problem 1909	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	12	11	11	10	12	11
normalized size	1	1.00	1.00	0.92	0.85	0.85	0.77	0.92	0.85
time (sec)	N/A	0.002	0.001	0.000	1.077	0.471	0.076	1.014	0.026

Problem 1910	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	17	12	11	11	12	11	11
normalized size	1	1.00	1.00	0.71	0.65	0.65	0.71	0.65	0.65
time (sec)	N/A	0.002	0.002	0.001	1.066	0.441	0.059	1.063	0.030

Problem 1911	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	10	9	9	10	9	8
normalized size	1	1.00	1.00	0.77	0.69	0.69	0.77	0.69	0.62
time (sec)	N/A	0.002	0.002	0.000	1.001	0.435	0.057	0.855	0.024

Problem 1912	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	14	11	9	10	12	9	10
normalized size	1	1.00	0.93	0.73	0.60	0.67	0.80	0.60	0.67
time (sec)	N/A	0.001	0.007	0.003	1.113	0.439	0.061	1.077	0.021

Problem 1913	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	15	14	13	18	14	14	15
normalized size	1	1.00	1.00	0.93	0.87	1.20	0.93	0.93	1.00
time (sec)	N/A	0.002	0.014	0.002	1.015	0.441	0.061	0.955	0.291

Problem 1914	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	17	14	11	11	10	14	11	12
normalized size	1	1.00	0.82	0.65	0.65	0.59	0.82	0.65	0.71
time (sec)	N/A	0.002	0.005	0.003	1.003	0.428	0.059	1.138	0.027

Problem 1915	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	15	15	10	9	11	14	12	11	8
normalized size	1	1.00	0.67	0.60	0.73	0.93	0.80	0.73	0.53
time (sec)	N/A	0.002	0.004	0.003	1.007	0.438	0.061	0.892	0.027

Problem 1916	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	24	24	24	17	16	14	19	16	15
normalized size	1	1.00	1.00	0.71	0.67	0.58	0.79	0.67	0.62
time (sec)	N/A	0.002	0.005	0.001	1.046	0.602	0.062	1.089	0.029

Problem 1917	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	23	23	16	15	19	20	16	17
normalized size	1	1.00	1.00	0.70	0.65	0.83	0.87	0.70	0.74
time (sec)	N/A	0.003	0.015	0.001	1.034	0.773	0.062	0.824	0.281

2.3 Detailed conclusion table specific for Rubi results

The following table is specific to Rubi. It gives additional statistics for each integral. the column **steps** is the number of steps used by Rubi to obtain the antiderivative. The **rules**

column is the number of unique rules used. The **integrand size** column is the leaf size of the integrand. Finally the ratio $\frac{\text{number of rules}}{\text{integrand size}}$ is given. The larger this ratio is, the harder the integral was to solve. In this test, problem number [1] had the largest ratio of [1.000]

Table 2.1: Rubi specific breakdown of results for each integral

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1	A	1	1	1.00	1	1.000
2	A	1	1	1.00	1	1.000
3	A	1	1	1.00	1	1.000
4	A	1	1	1.00	1	1.000
5	A	1	1	1.00	3	0.333
6	A	1	1	1.00	1	1.000
7	A	1	1	1.00	1	1.000
8	A	1	1	1.00	3	0.333
9	A	1	1	1.00	13	0.077
10	A	1	1	1.00	3	0.333
11	A	1	1	1.00	3	0.333
12	A	1	1	1.00	3	0.333
13	A	1	1	1.00	1	1.000
14	A	1	1	1.00	1	1.000
15	A	1	1	1.00	3	0.333
16	A	1	1	1.00	3	0.333
17	A	1	1	1.00	3	0.333
18	A	1	1	1.00	3	0.333
19	A	1	1	1.00	3	0.333
20	A	1	1	1.00	5	0.200
21	A	1	1	1.00	5	0.200
22	A	1	1	1.00	5	0.200

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
23	A	1	1	1.00	5	0.200
24	A	1	1	1.00	5	0.200
25	A	1	1	1.00	5	0.200
26	A	1	1	1.00	5	0.200
27	A	1	1	1.00	5	0.200
28	A	1	1	1.00	5	0.200
29	A	1	1	1.00	5	0.200
30	A	1	1	1.00	5	0.200
31	A	1	1	1.00	5	0.200
32	A	1	1	1.00	5	0.200
33	A	1	1	1.00	5	0.200
34	A	1	1	1.00	3	0.333
35	A	1	1	1.00	5	0.200
36	A	2	2	1.00	17	0.118
37	A	2	2	1.00	13	0.154
38	A	2	2	1.00	13	0.154
39	A	2	2	1.00	13	0.154
40	A	2	2	1.00	13	0.154
41	A	2	2	1.00	13	0.154
42	A	2	2	1.00	13	0.154
43	A	2	1	1.00	9	0.111
44	A	2	1	1.00	9	0.111
45	A	2	1	1.00	7	0.143
46	A	1	0	1.00	5	0.000
47	A	2	1	1.00	9	0.111
48	A	2	1	1.00	9	0.111

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
49	A	1	1	1.00	9	0.111
50	A	2	1	1.00	9	0.111
51	A	2	1	1.00	9	0.111
52	A	2	1	1.00	11	0.091
53	A	2	1	1.00	11	0.091
54	A	2	1	1.00	9	0.111
55	A	1	1	1.00	7	0.143
56	A	2	1	1.00	11	0.091
57	A	2	1	1.00	11	0.091
58	A	2	1	1.00	11	0.091
59	A	1	1	1.00	11	0.091
60	A	2	1	1.00	11	0.091
61	A	2	1	1.00	11	0.091
62	A	2	1	1.00	11	0.091
63	A	2	1	1.00	11	0.091
64	A	2	1	1.00	11	0.091
65	A	2	1	1.00	11	0.091
66	A	2	1	1.00	11	0.091
67	A	2	1	1.00	9	0.111
68	A	1	1	1.00	7	0.143
69	A	2	1	1.00	11	0.091
70	A	2	1	1.00	11	0.091
71	A	2	1	1.00	11	0.091
72	A	2	1	1.00	11	0.091
73	A	1	1	1.00	11	0.091
74	A	2	2	1.00	11	0.182

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
75	A	2	1	1.00	11	0.091
76	A	2	1	1.00	11	0.091
77	A	2	1	1.00	11	0.091
78	A	2	1	1.00	11	0.091
79	A	2	1	1.00	11	0.091
80	A	2	1	1.00	11	0.091
81	A	2	1	1.00	11	0.091
82	A	2	1	1.00	9	0.111
83	A	1	1	1.00	7	0.143
84	A	2	1	1.00	11	0.091
85	A	2	1	1.00	11	0.091
86	A	2	1	1.00	11	0.091
87	A	2	1	1.00	11	0.091
88	A	2	1	1.00	11	0.091
89	A	2	1	1.00	11	0.091
90	A	1	1	1.00	11	0.091
91	A	2	2	1.00	11	0.182
92	A	3	2	1.00	11	0.182
93	A	2	1	1.00	11	0.091
94	A	2	1	1.00	11	0.091
95	A	2	1	1.00	11	0.091
96	A	2	1	1.00	11	0.091
97	A	2	1	1.00	11	0.091
98	A	2	1	1.00	11	0.091
99	A	2	1	1.00	11	0.091
100	A	2	1	1.00	11	0.091

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
101	A	2	1	1.00	11	0.091
102	A	2	1	1.00	11	0.091
103	A	2	1	1.00	11	0.091
104	A	2	1	1.00	11	0.091
105	A	2	1	1.00	9	0.111
106	A	1	1	1.00	7	0.143
107	A	2	1	1.00	11	0.091
108	A	2	1	1.00	11	0.091
109	A	2	1	1.00	11	0.091
110	A	2	1	1.00	11	0.091
111	A	2	1	1.00	11	0.091
112	A	2	1	1.00	11	0.091
113	A	2	1	1.00	11	0.091
114	A	2	1	1.00	11	0.091
115	A	1	1	1.00	11	0.091
116	A	2	2	1.00	11	0.182
117	A	3	2	1.00	11	0.182
118	A	4	2	1.00	11	0.182
119	A	5	2	1.00	11	0.182
120	A	2	1	1.00	11	0.091
121	A	2	1	1.00	11	0.091
122	A	2	1	1.00	11	0.091
123	A	2	1	1.00	11	0.091
124	A	2	1	1.00	11	0.091
125	A	2	1	1.00	11	0.091
126	A	2	1	1.00	11	0.091

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
127	A	2	1	1.00	11	0.091
128	A	2	1	1.00	11	0.091
129	A	2	1	1.00	11	0.091
130	A	2	1	1.00	11	0.091
131	A	2	1	1.00	11	0.091
132	A	2	1	1.00	11	0.091
133	A	2	1	1.00	9	0.111
134	A	1	1	1.00	7	0.143
135	A	2	1	1.00	11	0.091
136	A	2	1	1.00	11	0.091
137	A	2	1	1.00	11	0.091
138	A	2	1	1.00	11	0.091
139	A	2	1	1.00	11	0.091
140	A	2	1	1.00	11	0.091
141	A	2	1	1.00	11	0.091
142	A	2	1	1.00	11	0.091
143	A	2	1	1.00	11	0.091
144	A	2	1	1.00	11	0.091
145	A	2	1	1.00	11	0.091
146	A	1	1	1.00	11	0.091
147	A	2	2	1.00	11	0.182
148	A	3	2	1.00	11	0.182
149	A	4	2	1.00	11	0.182
150	A	5	2	1.00	11	0.182
151	A	6	2	1.00	11	0.182
152	A	7	2	1.00	11	0.182

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
153	A	2	1	1.00	11	0.091
154	A	2	1	1.00	11	0.091
155	A	1	1	1.00	7	0.143
156	A	1	1	1.00	12	0.083
157	A	2	1	1.00	11	0.091
158	A	2	1	1.00	11	0.091
159	A	2	1	1.00	11	0.091
160	A	2	1	1.00	11	0.091
161	A	2	1	1.00	9	0.111
162	A	1	1	1.00	7	0.143
163	A	3	3	1.00	11	0.273
164	A	2	1	1.00	11	0.091
165	A	2	1	1.00	11	0.091
166	A	2	1	1.00	11	0.091
167	A	2	1	1.00	11	0.091
168	A	2	1	1.00	11	0.091
169	A	2	1	1.00	11	0.091
170	A	2	1	1.00	11	0.091
171	A	2	1	1.00	11	0.091
172	A	2	1	1.00	11	0.091
173	A	2	1	1.00	9	0.111
174	A	1	1	1.00	7	0.143
175	A	2	1	1.00	11	0.091
176	A	2	1	1.00	11	0.091
177	A	2	1	1.00	11	0.091
178	A	2	1	1.00	11	0.091

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
179	A	2	1	1.00	11	0.091
180	A	2	1	1.00	11	0.091
181	A	2	1	1.00	11	0.091
182	A	2	1	1.00	11	0.091
183	A	2	1	1.00	11	0.091
184	A	2	1	1.00	11	0.091
185	A	2	1	1.00	11	0.091
186	A	1	1	1.00	9	0.111
187	A	1	1	1.00	7	0.143
188	A	2	1	1.00	11	0.091
189	A	2	1	1.00	11	0.091
190	A	2	1	1.00	11	0.091
191	A	2	1	1.00	11	0.091
192	A	2	1	1.00	11	0.091
193	A	2	1	1.00	11	0.091
194	A	2	1	1.00	11	0.091
195	A	2	1	1.00	11	0.091
196	A	2	1	1.00	11	0.091
197	A	2	1	1.00	11	0.091
198	A	2	1	1.00	11	0.091
199	A	1	1	1.00	11	0.091
200	A	2	1	1.00	9	0.111
201	A	1	1	1.00	7	0.143
202	A	2	1	1.00	11	0.091
203	A	2	1	1.00	11	0.091
204	A	2	1	1.00	11	0.091

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
205	A	2	1	1.00	11	0.091
206	A	2	1	1.00	11	0.091
207	A	2	1	1.00	11	0.091
208	A	2	1	1.00	11	0.091
209	A	2	1	1.00	11	0.091
210	A	2	1	1.00	11	0.091
211	A	2	1	1.00	11	0.091
212	A	1	1	1.00	11	0.091
213	A	2	2	1.00	11	0.182
214	A	2	1	1.23	11	0.091
215	A	2	1	1.00	11	0.091
216	A	2	1	1.00	9	0.111
217	A	1	1	1.00	7	0.143
218	A	2	1	1.00	11	0.091
219	A	2	1	1.00	11	0.091
220	A	2	1	1.00	11	0.091
221	A	2	1	1.00	11	0.091
222	A	2	1	1.00	11	0.091
223	A	2	1	1.00	11	0.091
224	A	2	1	1.00	11	0.091
225	A	2	1	1.00	11	0.091
226	A	1	1	1.00	11	0.091
227	A	2	2	1.00	11	0.182
228	A	3	2	1.00	11	0.182
229	A	4	2	1.00	11	0.182
230	A	2	1	1.00	11	0.091

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
231	A	2	1	1.00	11	0.091
232	A	2	1	1.00	11	0.091
233	A	2	1	1.00	9	0.111
234	A	1	1	1.00	7	0.143
235	A	2	1	1.00	11	0.091
236	A	2	1	1.00	11	0.091
237	A	2	1	1.00	11	0.091
238	A	2	1	1.00	11	0.091
239	A	2	1	1.00	11	0.091
240	A	2	1	1.00	11	0.091
241	A	2	1	1.00	11	0.091
242	A	2	1	1.00	11	0.091
243	A	1	1	1.00	11	0.091
244	A	2	2	1.00	11	0.182
245	A	3	2	1.00	11	0.182
246	A	2	1	1.00	11	0.091
247	A	2	1	1.00	11	0.091
248	A	2	1	1.00	11	0.091
249	A	2	1	1.00	11	0.091
250	A	2	1	1.00	9	0.111
251	A	1	1	1.00	3	0.333
252	A	2	1	1.00	11	0.091
253	A	2	1	1.00	11	0.091
254	A	2	1	1.00	11	0.091
255	A	3	3	1.00	11	0.273
256	A	3	3	1.00	11	0.273

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
257	A	2	1	1.00	11	0.091
258	A	2	1	1.00	11	0.091
259	A	2	1	1.00	11	0.091
260	A	2	1	1.00	11	0.091
261	A	2	1	1.00	11	0.091
262	A	2	1	1.00	11	0.091
263	A	2	1	1.00	11	0.091
264	A	2	1	1.00	11	0.091
265	A	2	1	1.00	11	0.091
266	A	2	1	1.00	11	0.091
267	A	2	1	1.00	11	0.091
268	A	2	1	1.00	11	0.091
269	A	2	1	1.00	11	0.091
270	A	2	1	1.00	11	0.091
271	A	1	1	1.00	7	0.143
272	A	1	1	1.00	7	0.143
273	A	1	1	1.00	11	0.091
274	A	1	1	1.00	13	0.077
275	A	1	1	1.00	15	0.067
276	A	1	1	1.00	15	0.067
277	A	1	1	1.00	15	0.067
278	A	1	1	1.00	15	0.067
279	A	3	3	1.00	11	0.273
280	A	3	3	1.00	11	0.273
281	A	2	1	1.00	11	0.091
282	A	2	1	1.00	11	0.091

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
283	A	3	1	1.00	17	0.059
284	A	2	1	1.00	13	0.077
285	A	2	1	1.00	13	0.077
286	A	2	1	1.00	11	0.091
287	A	1	1	1.00	9	0.111
288	A	3	3	1.00	13	0.231
289	A	3	3	1.00	13	0.231
290	A	4	4	1.00	13	0.308
291	A	5	4	1.00	13	0.308
292	A	2	1	1.00	13	0.077
293	A	2	1	1.00	13	0.077
294	A	2	1	1.00	11	0.091
295	A	1	1	1.00	9	0.111
296	A	4	3	1.00	13	0.231
297	A	4	4	1.00	13	0.308
298	A	4	3	1.00	13	0.231
299	A	5	4	1.00	13	0.308
300	A	2	1	1.00	13	0.077
301	A	2	1	1.00	13	0.077
302	A	2	1	1.00	11	0.091
303	A	1	1	1.00	9	0.111
304	A	5	3	1.00	13	0.231
305	A	5	4	1.00	13	0.308
306	A	5	4	1.00	13	0.308
307	A	5	3	1.00	13	0.231
308	A	6	4	1.00	13	0.308

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
309	A	2	1	1.00	13	0.077
310	A	2	1	1.00	13	0.077
311	A	2	1	1.00	13	0.077
312	A	2	1	1.00	13	0.077
313	A	2	1	1.00	13	0.077
314	A	2	1	1.00	13	0.077
315	A	2	1	1.00	11	0.091
316	A	1	1	1.00	9	0.111
317	A	7	3	1.00	13	0.231
318	A	7	4	1.00	13	0.308
319	A	7	4	1.00	13	0.308
320	A	7	4	1.00	13	0.308
321	A	7	4	1.00	13	0.308
322	A	7	3	1.00	13	0.231
323	A	8	4	1.00	13	0.308
324	A	9	4	1.00	13	0.308
325	A	3	3	1.00	15	0.200
326	A	3	3	1.00	15	0.200
327	A	4	4	1.00	15	0.267
328	A	4	3	1.00	15	0.200
329	A	4	4	1.00	15	0.267
330	A	4	3	1.00	15	0.200
331	A	5	3	1.00	15	0.200
332	A	5	4	1.00	15	0.267
333	A	5	4	1.00	15	0.267
334	A	2	1	1.00	13	0.077

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
335	A	2	1	1.00	13	0.077
336	A	2	1	1.00	13	0.077
337	A	2	1	1.00	11	0.091
338	A	1	1	1.00	9	0.111
339	A	2	2	1.00	13	0.154
340	A	3	3	1.00	13	0.231
341	A	4	3	1.00	13	0.231
342	A	5	3	1.00	13	0.231
343	A	2	1	1.00	13	0.077
344	A	2	1	1.00	13	0.077
345	A	2	1	1.00	13	0.077
346	A	2	1	1.00	11	0.091
347	A	1	1	1.00	9	0.111
348	A	3	3	1.00	13	0.231
349	A	4	3	1.04	13	0.231
350	A	5	3	0.98	13	0.231
351	A	2	1	1.00	13	0.077
352	A	2	1	1.00	13	0.077
353	A	2	1	1.00	13	0.077
354	A	2	1	1.00	11	0.091
355	A	1	1	1.00	9	0.111
356	A	4	3	1.00	13	0.231
357	A	5	3	1.08	13	0.231
358	A	6	3	1.00	13	0.231
359	A	2	2	1.00	15	0.133
360	A	3	3	1.00	15	0.200

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
361	A	4	3	1.00	15	0.200
362	A	3	3	1.00	15	0.200
363	A	4	3	1.05	15	0.200
364	A	5	3	0.98	15	0.200
365	A	4	3	1.00	15	0.200
366	A	5	3	1.09	15	0.200
367	A	6	3	1.00	15	0.200
368	A	2	2	1.00	31	0.065
369	C	5	2	7.08	34	0.059
370	A	3	3	1.00	29	0.103
371	A	2	1	1.00	13	0.077
372	A	2	1	1.00	13	0.077
373	A	2	1	1.00	11	0.091
374	A	1	1	1.00	9	0.111
375	A	5	5	1.00	13	0.385
376	A	5	5	1.00	13	0.385
377	A	6	6	1.00	13	0.462
378	A	2	1	1.00	13	0.077
379	A	2	1	1.00	13	0.077
380	A	2	1	1.00	11	0.091
381	A	1	1	1.00	9	0.111
382	A	5	5	1.00	13	0.385
383	A	5	5	1.00	13	0.385
384	A	6	6	1.00	13	0.462
385	A	2	1	1.00	13	0.077
386	A	2	1	1.00	13	0.077

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
387	A	2	1	1.00	11	0.091
388	A	1	1	1.00	9	0.111
389	A	6	5	1.00	13	0.385
390	A	6	6	1.00	13	0.462
391	A	6	5	1.00	13	0.385
392	A	2	1	1.00	13	0.077
393	A	2	1	1.00	13	0.077
394	A	2	1	1.00	11	0.091
395	A	1	1	1.00	9	0.111
396	A	4	4	1.00	13	0.308
397	A	5	5	1.00	13	0.385
398	A	6	5	1.00	13	0.385
399	A	2	1	1.00	15	0.067
400	A	2	1	1.00	15	0.067
401	A	2	1	1.00	13	0.077
402	A	1	1	1.00	11	0.091
403	A	4	4	1.00	15	0.267
404	A	5	5	1.00	15	0.333
405	A	6	5	1.00	15	0.333
406	A	2	1	1.00	13	0.077
407	A	2	1	1.00	13	0.077
408	A	2	1	1.00	11	0.091
409	A	1	1	1.00	9	0.111
410	A	4	4	1.00	13	0.308
411	A	5	5	1.00	13	0.385
412	A	6	5	1.00	13	0.385

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
413	A	2	1	1.00	13	0.077
414	A	2	1	1.00	13	0.077
415	A	2	1	1.00	11	0.091
416	A	1	1	1.00	9	0.111
417	A	5	5	1.00	13	0.385
418	A	6	5	1.02	13	0.385
419	A	7	5	0.99	13	0.385
420	A	4	4	1.00	17	0.235
421	A	4	4	1.00	18	0.222
422	A	4	4	1.00	19	0.210
423	A	4	4	1.00	20	0.200
424	A	4	4	1.00	17	0.235
425	A	4	4	1.00	18	0.222
426	A	4	4	1.00	19	0.210
427	A	4	4	1.00	20	0.200
428	A	2	1	1.00	9	0.111
429	A	2	1	1.00	11	0.091
430	A	2	1	1.00	11	0.091
431	A	2	1	1.00	11	0.091
432	A	2	1	1.00	11	0.091
433	A	2	1	1.00	11	0.091
434	A	2	1	1.00	11	0.091
435	A	2	1	1.00	11	0.091
436	A	2	1	1.00	13	0.077
437	A	2	1	1.00	13	0.077
438	A	2	1	1.00	13	0.077

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
439	A	2	1	1.00	13	0.077
440	A	2	1	1.00	13	0.077
441	A	2	1	1.00	13	0.077
442	A	2	1	1.00	11	0.091
443	A	2	1	1.00	13	0.077
444	A	2	1	1.00	13	0.077
445	A	2	1	1.00	13	0.077
446	A	2	1	1.00	13	0.077
447	A	2	1	1.00	13	0.077
448	A	2	1	1.00	13	0.077
449	A	5	3	1.00	13	0.231
450	A	4	3	1.00	13	0.231
451	A	3	3	1.00	13	0.231
452	A	2	2	1.00	13	0.154
453	A	3	3	1.00	13	0.231
454	A	4	3	1.00	13	0.231
455	A	5	3	1.00	13	0.231
456	A	5	4	1.00	13	0.308
457	A	4	4	1.00	13	0.308
458	A	3	3	1.00	13	0.231
459	A	3	3	1.00	13	0.231
460	A	4	3	1.00	13	0.231
461	A	5	3	1.00	13	0.231
462	A	6	4	1.00	13	0.308
463	A	5	4	1.00	13	0.308
464	A	4	3	1.00	13	0.231

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
465	A	4	4	1.00	13	0.308
466	A	4	3	1.00	13	0.231
467	A	5	3	1.00	13	0.231
468	A	6	3	1.00	13	0.231
469	A	5	3	1.00	15	0.200
470	A	4	3	1.00	15	0.200
471	A	3	3	1.00	15	0.200
472	A	2	2	1.00	15	0.133
473	A	3	3	1.00	15	0.200
474	A	4	3	1.00	15	0.200
475	A	5	3	1.00	15	0.200
476	A	5	4	1.00	15	0.267
477	A	4	4	1.00	15	0.267
478	A	3	3	1.00	15	0.200
479	A	3	3	1.00	15	0.200
480	A	4	3	1.00	15	0.200
481	A	5	3	1.00	15	0.200
482	A	6	4	1.00	15	0.267
483	A	5	4	1.00	15	0.267
484	A	4	3	1.00	15	0.200
485	A	4	4	1.00	15	0.267
486	A	4	3	1.00	15	0.200
487	A	5	3	1.00	15	0.200
488	A	6	3	1.00	15	0.200
489	A	7	4	1.00	15	0.267
490	A	6	4	1.00	15	0.267
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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
491	A	5	4	1.00	15	0.267
492	A	4	4	1.00	15	0.267
493	A	4	4	1.00	15	0.267
494	A	1	1	1.00	15	0.067
495	A	2	2	1.00	15	0.133
496	A	3	2	1.00	15	0.133
497	A	7	4	1.00	16	0.250
498	A	6	4	1.00	16	0.250
499	A	5	4	1.00	16	0.250
500	A	4	4	1.00	16	0.250
501	A	4	4	1.00	16	0.250
502	A	1	1	1.00	16	0.062
503	A	2	2	1.00	16	0.125
504	A	3	2	1.00	16	0.125
505	A	6	3	1.00	15	0.200
506	A	5	3	1.00	15	0.200
507	A	4	3	1.00	15	0.200
508	A	3	3	1.00	15	0.200
509	A	3	3	1.00	15	0.200
510	A	1	1	1.00	15	0.067
511	A	2	2	1.00	15	0.133
512	A	3	2	1.00	15	0.133
513	A	6	3	1.00	16	0.188
514	A	5	3	1.00	16	0.188
515	A	4	3	1.00	16	0.188
516	A	3	3	1.00	16	0.188

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
517	A	3	3	1.00	16	0.188
518	A	1	1	1.00	16	0.062
519	A	2	2	1.00	16	0.125
520	A	3	2	1.00	16	0.125
521	A	8	4	1.00	15	0.267
522	A	7	4	1.00	15	0.267
523	A	6	4	1.00	15	0.267
524	A	5	4	1.00	15	0.267
525	A	5	5	1.00	15	0.333
526	A	5	4	1.00	15	0.267
527	A	8	4	1.00	16	0.250
528	A	7	4	1.00	16	0.250
529	A	6	4	1.00	16	0.250
530	A	5	4	1.00	16	0.250
531	A	5	5	1.00	16	0.312
532	A	5	4	1.00	16	0.250
533	A	7	3	1.00	15	0.200
534	A	6	3	1.00	15	0.200
535	A	5	3	1.00	15	0.200
536	A	4	3	1.00	15	0.200
537	A	4	4	1.00	15	0.267
538	A	4	3	1.00	15	0.200
539	A	7	3	1.00	16	0.188
540	A	6	3	1.00	16	0.188
541	A	5	3	1.00	16	0.188
542	A	4	3	1.00	16	0.188

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
543	A	4	4	1.00	16	0.250
544	A	4	3	1.00	16	0.188
545	A	9	4	1.00	15	0.267
546	A	8	4	1.00	15	0.267
547	A	7	4	1.00	15	0.267
548	A	6	4	1.00	15	0.267
549	A	6	5	1.00	15	0.333
550	A	6	5	1.00	15	0.333
551	A	9	4	1.00	16	0.250
552	A	8	4	1.00	16	0.250
553	A	7	4	1.00	16	0.250
554	A	6	4	1.00	16	0.250
555	A	6	5	1.00	16	0.312
556	A	6	5	1.00	16	0.312
557	A	8	3	1.00	15	0.200
558	A	7	3	1.00	15	0.200
559	A	6	3	1.00	15	0.200
560	A	5	3	1.00	15	0.200
561	A	5	4	1.00	15	0.267
562	A	5	4	1.00	15	0.267
563	A	8	3	1.00	16	0.188
564	A	7	3	1.00	16	0.188
565	A	6	3	1.00	16	0.188
566	A	5	3	1.00	16	0.188
567	A	5	4	1.00	16	0.250
568	A	5	4	1.00	16	0.250

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
569	A	6	4	1.00	15	0.267
570	A	5	4	1.00	15	0.267
571	A	4	4	1.00	15	0.267
572	A	3	3	1.00	15	0.200
573	A	1	1	1.00	15	0.067
574	A	2	2	1.00	15	0.133
575	A	3	2	1.00	15	0.133
576	A	4	2	1.00	15	0.133
577	A	6	5	1.00	15	0.333
578	A	5	5	1.00	15	0.333
579	A	4	4	1.00	15	0.267
580	A	1	1	1.00	15	0.067
581	A	2	2	1.00	15	0.133
582	A	3	2	1.00	15	0.133
583	A	4	2	1.00	15	0.133
584	A	6	5	1.00	15	0.333
585	A	5	4	1.00	15	0.267
586	A	1	1	1.00	15	0.067
587	A	2	2	1.00	15	0.133
588	A	3	2	1.00	15	0.133
589	A	4	2	1.00	15	0.133
590	A	6	4	1.00	16	0.250
591	A	5	4	1.00	16	0.250
592	A	4	4	1.00	16	0.250
593	A	3	3	1.00	16	0.188
594	A	1	1	1.00	16	0.062

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
595	A	2	2	1.00	16	0.125
596	A	6	5	1.00	16	0.312
597	A	5	5	1.00	16	0.312
598	A	4	4	1.00	16	0.250
599	A	1	1	1.00	16	0.062
600	A	2	2	1.00	16	0.125
601	A	3	2	1.00	16	0.125
602	A	6	5	1.00	16	0.312
603	A	5	4	1.00	16	0.250
604	A	1	1	1.00	16	0.062
605	A	2	2	1.00	16	0.125
606	A	3	2	1.00	16	0.125
607	A	4	2	1.00	16	0.125
608	A	5	3	1.00	15	0.200
609	A	4	3	1.00	15	0.200
610	A	3	3	1.00	15	0.200
611	A	2	2	1.00	15	0.133
612	A	1	1	1.00	15	0.067
613	A	2	2	1.00	15	0.133
614	A	3	2	1.00	15	0.133
615	A	4	2	1.00	15	0.133
616	A	5	4	1.00	15	0.267
617	A	4	4	1.00	15	0.267
618	A	3	3	1.00	15	0.200
619	A	1	1	1.00	15	0.067
620	A	2	2	1.00	15	0.133

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
621	A	3	2	1.00	15	0.133
622	A	4	2	1.00	15	0.133
623	A	5	4	1.00	15	0.267
624	A	4	3	1.00	15	0.200
625	A	1	1	1.00	15	0.067
626	A	2	2	1.00	15	0.133
627	A	3	2	1.00	15	0.133
628	A	4	2	1.00	15	0.133
629	A	5	3	1.00	16	0.188
630	A	4	3	1.00	16	0.188
631	A	3	3	1.00	16	0.188
632	A	2	2	1.00	16	0.125
633	A	1	1	1.00	16	0.062
634	A	2	2	1.00	16	0.125
635	A	5	4	1.00	16	0.250
636	A	4	4	1.00	16	0.250
637	A	3	3	1.00	16	0.188
638	A	1	1	1.00	16	0.062
639	A	2	2	1.00	16	0.125
640	A	3	2	1.00	16	0.125
641	A	5	4	1.00	16	0.250
642	A	4	3	1.00	16	0.188
643	A	1	1	1.00	16	0.062
644	A	2	2	1.00	16	0.125
645	A	3	2	1.00	16	0.125
646	A	4	2	1.00	16	0.125

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
647	A	4	4	1.00	15	0.267
648	A	3	3	1.00	15	0.200
649	A	2	2	1.00	16	0.125
650	A	2	1	1.00	11	0.091
651	A	2	1	1.00	11	0.091
652	A	2	1	1.00	11	0.091
653	A	2	1	1.00	11	0.091
654	A	2	1	1.00	11	0.091
655	A	2	1	1.00	11	0.091
656	A	2	1	1.00	11	0.091
657	A	2	1	1.00	11	0.091
658	A	2	1	1.00	13	0.077
659	A	2	1	1.00	13	0.077
660	A	2	1	1.00	13	0.077
661	A	2	1	1.00	13	0.077
662	A	2	1	1.00	13	0.077
663	A	2	1	1.00	13	0.077
664	A	2	1	1.00	13	0.077
665	A	2	1	1.00	13	0.077
666	A	2	1	1.00	13	0.077
667	A	2	1	1.00	13	0.077
668	A	2	1	1.00	13	0.077
669	A	2	1	1.00	13	0.077
670	A	2	1	1.00	13	0.077
671	A	2	1	1.00	13	0.077
672	A	2	1	1.00	13	0.077

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
673	A	2	1	1.00	13	0.077
674	A	6	5	1.00	13	0.385
675	A	6	5	1.00	13	0.385
676	A	5	5	1.00	13	0.385
677	A	5	5	1.00	13	0.385
678	A	4	4	1.00	13	0.308
679	A	4	4	1.00	13	0.308
680	A	5	5	1.00	13	0.385
681	A	5	5	1.00	13	0.385
682	A	6	6	1.00	13	0.462
683	A	6	6	1.00	13	0.462
684	A	5	5	1.00	13	0.385
685	A	5	5	1.00	13	0.385
686	A	5	5	1.00	13	0.385
687	A	5	5	1.00	13	0.385
688	A	6	5	1.00	13	0.385
689	A	6	5	1.00	13	0.385
690	A	6	5	1.00	13	0.385
691	A	6	5	1.00	13	0.385
692	A	6	6	1.00	13	0.462
693	A	6	6	1.00	13	0.462
694	A	6	5	1.00	13	0.385
695	A	6	5	1.00	13	0.385
696	A	7	5	1.00	13	0.385
697	A	7	5	1.00	13	0.385
698	A	5	5	1.00	15	0.333

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
699	A	2	1	1.00	11	0.091
700	A	2	1	1.00	11	0.091
701	A	2	1	1.00	11	0.091
702	A	2	1	1.00	11	0.091
703	A	2	1	1.00	9	0.111
704	A	1	1	1.00	11	0.091
705	A	1	1	1.00	11	0.091
706	A	1	1	1.00	11	0.091
707	A	2	2	1.00	13	0.154
708	A	2	2	1.00	13	0.154
709	A	2	2	1.00	13	0.154
710	A	2	2	1.00	13	0.154
711	A	2	2	1.00	13	0.154
712	A	2	2	1.00	13	0.154
713	A	2	2	1.00	15	0.133
714	A	2	2	1.00	15	0.133
715	A	2	2	1.00	13	0.154
716	A	2	2	1.00	15	0.133
717	A	2	2	1.00	15	0.133
718	A	2	2	1.00	15	0.133
719	A	1	1	1.00	13	0.077
720	A	1	1	1.00	13	0.077
721	A	1	1	1.00	13	0.077
722	A	3	3	1.00	13	0.231
723	A	2	2	1.00	15	0.133
724	A	1	1	1.00	15	0.067

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
725	A	1	1	1.00	15	0.067
726	A	3	3	1.00	15	0.200
727	A	1	1	1.00	15	0.067
728	A	1	1	1.00	13	0.077
729	A	1	1	1.00	14	0.071
730	A	2	2	1.00	11	0.182
731	A	2	2	1.00	13	0.154
732	A	2	1	1.00	11	0.091
733	A	2	1	1.00	11	0.091
734	A	2	1	1.00	9	0.111
735	A	1	1	1.00	7	0.143
736	A	1	1	1.00	11	0.091
737	A	1	1	1.00	11	0.091
738	A	1	1	1.00	11	0.091
739	A	3	2	1.00	15	0.133
740	A	2	2	1.00	15	0.133
741	A	1	1	1.00	15	0.067
742	A	2	2	1.00	15	0.133
743	A	2	2	1.00	13	0.154
744	A	2	2	1.00	15	0.133
745	A	2	2	1.00	13	0.154
746	A	2	2	1.00	13	0.154
747	A	2	2	1.00	13	0.154
748	A	2	2	1.00	13	0.154
749	A	2	2	1.00	13	0.154
750	A	1	1	1.00	13	0.077

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
751	A	1	1	1.00	15	0.067
752	A	2	2	1.00	13	0.154
753	A	1	1	1.00	17	0.059
754	A	2	2	1.00	15	0.133
755	A	2	2	1.00	19	0.105
756	A	3	2	1.00	18	0.111
757	A	3	2	1.00	18	0.111
758	A	3	2	1.00	16	0.125
759	A	3	2	1.00	15	0.133
760	A	2	1	1.00	18	0.056
761	A	3	2	1.00	18	0.111
762	A	3	2	1.00	18	0.111
763	A	2	2	1.00	18	0.111
764	A	3	2	1.00	18	0.111
765	A	3	2	1.00	18	0.111
766	A	3	2	1.00	16	0.125
767	A	3	2	1.00	15	0.133
768	A	3	2	1.00	18	0.111
769	A	3	2	1.00	18	0.111
770	A	2	1	1.00	18	0.056
771	A	3	2	1.00	18	0.111
772	A	3	2	1.00	18	0.111
773	A	3	2	1.00	18	0.111
774	A	3	2	1.00	16	0.125
775	A	3	2	1.00	15	0.133
776	A	3	2	1.00	18	0.111

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
777	A	3	2	1.00	18	0.111
778	A	3	2	1.00	18	0.111
779	A	3	2	1.00	18	0.111
780	A	3	2	1.00	18	0.111
781	A	3	2	1.00	18	0.111
782	A	2	1	1.00	16	0.062
783	A	3	2	1.00	15	0.133
784	A	3	2	1.00	18	0.111
785	A	2	2	1.00	18	0.111
786	A	3	2	1.00	18	0.111
787	A	3	2	1.00	18	0.111
788	A	2	1	1.00	18	0.056
789	A	3	2	1.00	18	0.111
790	A	3	2	1.00	16	0.125
791	A	2	2	1.00	15	0.133
792	A	3	2	1.00	18	0.111
793	A	3	2	1.00	18	0.111
794	A	3	2	1.00	18	0.111
795	A	3	2	1.00	18	0.111
796	A	3	2	1.00	18	0.111
797	A	2	2	1.00	18	0.111
798	A	3	2	1.00	16	0.125
799	A	3	2	1.00	15	0.133
800	A	3	2	1.00	18	0.111
801	A	3	2	1.00	18	0.111
802	A	3	2	1.00	18	0.111

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
803	A	3	2	1.00	18	0.111
804	A	3	2	1.00	20	0.100
805	A	3	2	1.00	20	0.100
806	A	3	2	1.00	18	0.111
807	A	3	2	1.00	17	0.118
808	A	2	2	1.00	20	0.100
809	A	3	2	1.00	20	0.100
810	A	3	2	1.00	20	0.100
811	A	3	2	1.00	20	0.100
812	A	3	2	1.00	20	0.100
813	A	3	2	1.00	20	0.100
814	A	3	2	1.00	18	0.111
815	A	3	2	1.00	17	0.118
816	A	3	2	1.00	20	0.100
817	A	3	2	1.00	20	0.100
818	A	2	2	1.00	20	0.100
819	A	3	2	1.00	20	0.100
820	A	3	2	1.00	18	0.111
821	A	3	2	1.00	17	0.118
822	A	3	2	1.00	20	0.100
823	A	3	2	1.00	20	0.100
824	A	3	2	1.00	20	0.100
825	A	3	2	1.00	20	0.100
826	A	2	2	1.00	20	0.100
827	A	3	2	1.00	20	0.100
828	A	3	2	1.00	20	0.100

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
829	A	3	2	1.00	20	0.100
830	A	2	2	1.00	18	0.111
831	A	3	2	1.00	17	0.118
832	A	3	2	1.00	20	0.100
833	A	3	2	1.00	20	0.100
834	A	2	2	1.00	20	0.100
835	A	3	2	1.00	20	0.100
836	A	2	2	1.00	20	0.100
837	A	3	2	1.00	20	0.100
838	A	3	2	1.00	18	0.111
839	A	3	2	1.00	17	0.118
840	A	2	2	1.00	20	0.100
841	A	3	2	1.00	20	0.100
842	A	3	2	1.00	20	0.100
843	A	3	2	1.00	20	0.100
844	A	3	2	1.00	20	0.100
845	A	3	2	1.00	20	0.100
846	A	2	2	1.00	18	0.111
847	A	3	2	1.00	17	0.118
848	A	3	2	1.00	20	0.100
849	A	3	2	1.00	20	0.100
850	A	3	2	1.00	20	0.100
851	A	3	2	1.00	20	0.100
852	A	3	2	1.00	20	0.100
853	A	3	2	1.00	20	0.100
854	A	3	2	1.00	18	0.111

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
855	A	3	2	1.00	17	0.118
856	A	2	2	1.00	20	0.100
857	A	4	4	1.00	20	0.200
858	A	3	2	1.00	20	0.100
859	A	3	2	1.00	20	0.100
860	A	3	2	1.00	18	0.111
861	A	3	2	1.00	17	0.118
862	A	3	2	1.00	20	0.100
863	A	3	2	1.00	20	0.100
864	A	2	2	1.00	20	0.100
865	A	4	4	1.00	20	0.200
866	A	3	2	1.00	20	0.100
867	A	3	2	1.00	20	0.100
868	A	3	2	1.00	20	0.100
869	A	3	2	1.00	17	0.118
870	A	3	2	1.00	20	0.100
871	A	3	2	1.00	20	0.100
872	A	3	2	1.00	20	0.100
873	A	3	2	1.00	20	0.100
874	A	2	2	1.00	20	0.100
875	A	4	4	1.00	20	0.200
876	A	3	2	1.00	20	0.100
877	A	3	2	1.00	20	0.100
878	A	3	2	1.00	20	0.100
879	A	3	2	1.00	20	0.100
880	A	2	2	1.00	18	0.111

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
881	A	4	4	1.00	17	0.235
882	A	3	2	1.00	20	0.100
883	A	3	2	1.00	20	0.100
884	A	3	2	1.00	20	0.100
885	A	3	2	1.00	20	0.100
886	A	3	2	1.00	20	0.100
887	A	3	2	1.00	20	0.100
888	A	2	2	1.00	20	0.100
889	A	4	4	1.00	20	0.200
890	A	3	2	1.00	18	0.111
891	A	3	2	1.00	17	0.118
892	A	3	2	1.00	20	0.100
893	A	3	2	1.00	20	0.100
894	A	3	2	1.00	20	0.100
895	A	3	2	1.00	18	0.111
896	A	3	2	1.00	17	0.118
897	A	2	2	1.00	20	0.100
898	A	3	2	1.00	20	0.100
899	A	3	2	1.00	20	0.100
900	A	3	2	1.00	20	0.100
901	A	3	2	1.00	18	0.111
902	A	3	2	1.00	17	0.118
903	A	3	2	1.00	20	0.100
904	A	3	2	1.00	20	0.100
905	A	2	2	1.00	20	0.100
906	A	3	2	1.00	20	0.100

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
907	A	3	2	1.00	20	0.100
908	A	3	2	1.00	20	0.100
909	A	3	2	1.00	20	0.100
910	A	3	2	1.00	20	0.100
911	A	3	2	1.00	20	0.100
912	A	3	2	1.00	20	0.100
913	A	2	2	1.00	18	0.111
914	A	3	2	1.00	17	0.118
915	A	3	2	1.00	20	0.100
916	A	3	2	1.00	20	0.100
917	A	3	2	1.00	20	0.100
918	A	3	2	1.00	20	0.100
919	A	2	2	1.00	20	0.100
920	A	3	2	1.00	20	0.100
921	A	3	2	1.00	18	0.111
922	A	3	2	1.00	17	0.118
923	A	3	2	1.00	20	0.100
924	A	3	2	1.00	18	0.111
925	A	3	2	1.00	17	0.118
926	A	2	2	1.00	20	0.100
927	A	2	2	1.00	20	0.100
928	A	2	2	1.00	20	0.100
929	A	2	2	1.00	20	0.100
930	A	3	2	1.00	18	0.111
931	A	3	2	1.00	17	0.118
932	A	3	2	1.00	20	0.100

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
933	A	3	2	1.00	20	0.100
934	A	2	2	1.00	20	0.100
935	A	2	2	1.00	20	0.100
936	A	2	2	1.00	20	0.100
937	A	2	2	1.00	20	0.100
938	A	3	2	1.00	17	0.118
939	A	3	2	1.00	20	0.100
940	A	3	2	1.00	20	0.100
941	A	3	2	1.00	20	0.100
942	A	3	2	1.00	20	0.100
943	A	2	2	1.00	20	0.100
944	A	2	2	1.00	20	0.100
945	A	2	2	1.00	20	0.100
946	A	3	2	1.00	20	0.100
947	A	3	2	1.00	20	0.100
948	A	3	2	1.00	20	0.100
949	A	2	2	1.00	18	0.111
950	A	2	2	1.00	17	0.118
951	A	2	2	1.00	20	0.100
952	A	2	2	1.00	20	0.100
953	A	3	2	1.00	20	0.100
954	A	3	2	1.00	20	0.100
955	A	3	2	1.00	20	0.100
956	A	2	2	1.00	20	0.100
957	A	2	2	1.00	20	0.100
958	A	2	2	1.00	18	0.111

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
959	A	2	2	1.00	17	0.118
960	A	2	2	1.00	20	0.100
961	A	3	2	1.00	20	0.100
962	A	3	2	1.00	20	0.100
963	A	3	2	1.00	20	0.100
964	A	2	2	1.00	20	0.100
965	A	2	2	1.00	20	0.100
966	A	2	2	1.00	20	0.100
967	A	2	2	1.00	20	0.100
968	A	2	2	1.00	18	0.111
969	A	4	3	1.00	20	0.150
970	A	4	3	1.00	20	0.150
971	A	4	3	1.00	20	0.150
972	A	4	3	1.00	20	0.150
973	A	4	3	1.00	20	0.150
974	A	4	3	1.00	20	0.150
975	A	4	3	1.00	22	0.136
976	A	4	3	1.00	22	0.136
977	A	4	3	1.00	22	0.136
978	A	4	3	1.00	22	0.136
979	A	4	3	1.00	22	0.136
980	A	4	3	1.00	22	0.136
981	A	4	4	1.00	22	0.182
982	A	4	4	1.00	22	0.182
983	A	4	4	1.00	22	0.182
984	A	4	4	1.00	22	0.182

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
985	A	4	4	1.00	22	0.182
986	A	4	4	1.00	22	0.182
987	A	2	2	1.00	22	0.091
988	A	2	2	1.00	22	0.091
989	A	2	2	1.00	20	0.100
990	A	2	2	1.00	19	0.105
991	A	2	2	1.00	22	0.091
992	A	2	2	1.00	20	0.100
993	A	2	2	1.00	22	0.091
994	A	2	2	1.00	22	0.091
995	A	2	2	1.00	25	0.080
996	A	3	3	1.00	27	0.111
997	A	3	3	1.00	18	0.167
998	A	4	4	0.94	20	0.200
999	A	2	2	1.00	20	0.100
1000	A	2	1	1.00	20	0.050
1001	A	2	2	1.00	20	0.100
1002	A	2	2	1.00	20	0.100
1003	A	2	2	1.00	18	0.111
1004	A	2	2	1.00	20	0.100
1005	A	2	2	1.00	20	0.100
1006	A	2	2	1.00	20	0.100
1007	A	2	2	1.00	20	0.100
1008	A	2	1	1.00	20	0.050
1009	A	2	2	1.00	20	0.100
1010	A	2	2	1.00	20	0.100

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1011	A	2	2	1.00	18	0.111
1012	A	2	2	1.00	20	0.100
1013	A	2	2	1.00	20	0.100
1014	A	2	2	1.00	20	0.100
1015	A	2	2	1.00	18	0.111
1016	A	2	2	1.00	18	0.111
1017	A	2	2	1.00	18	0.111
1018	A	2	2	1.00	16	0.125
1019	A	2	2	1.00	18	0.111
1020	A	2	2	1.00	18	0.111
1021	A	2	2	1.00	18	0.111
1022	A	2	1	1.00	18	0.056
1023	A	2	2	1.00	18	0.111
1024	A	2	2	1.00	18	0.111
1025	A	2	2	1.00	18	0.111
1026	A	2	2	1.00	18	0.111
1027	A	2	2	1.00	19	0.105
1028	A	2	1	1.00	17	0.059
1029	A	2	1	1.00	17	0.059
1030	A	2	1	1.00	15	0.067
1031	A	1	0	1.00	5	0.000
1032	A	2	1	1.00	17	0.059
1033	A	2	1	1.00	17	0.059
1034	A	1	1	1.00	17	0.059
1035	A	2	1	1.00	17	0.059
1036	A	2	1	1.00	17	0.059

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1037	A	2	1	1.00	17	0.059
1038	A	2	1	1.00	19	0.053
1039	A	3	2	1.00	19	0.105
1040	A	2	1	1.00	17	0.059
1041	A	1	1	1.00	7	0.143
1042	A	2	1	1.00	19	0.053
1043	A	2	1	1.00	19	0.053
1044	A	2	1	1.00	19	0.053
1045	A	1	1	1.00	19	0.053
1046	A	2	1	1.00	19	0.053
1047	A	2	1	1.00	19	0.053
1048	A	2	1	1.00	19	0.053
1049	A	2	1	1.00	19	0.053
1050	A	2	1	1.00	19	0.053
1051	A	2	1	1.00	17	0.059
1052	A	1	1	1.00	7	0.143
1053	A	2	2	1.00	19	0.105
1054	A	3	2	1.00	19	0.105
1055	A	3	2	1.00	19	0.105
1056	A	2	1	1.00	19	0.053
1057	A	2	1	1.00	19	0.053
1058	A	2	1	1.00	17	0.059
1059	A	1	1	1.00	7	0.143
1060	A	3	2	1.00	19	0.105
1061	A	3	3	1.00	19	0.158
1062	A	3	2	1.00	19	0.105

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1063	A	7	4	1.00	17	0.235
1064	A	6	4	1.00	17	0.235
1065	A	5	4	1.00	17	0.235
1066	A	4	4	1.00	17	0.235
1067	A	3	3	1.00	17	0.176
1068	A	3	3	1.00	17	0.176
1069	A	3	3	1.00	17	0.176
1070	A	1	1	1.00	17	0.059
1071	A	2	2	1.00	17	0.118
1072	A	3	2	1.00	17	0.118
1073	A	4	2	1.00	17	0.118
1074	A	5	2	1.00	17	0.118
1075	A	7	4	1.00	17	0.235
1076	A	6	4	1.00	17	0.235
1077	A	5	4	1.00	17	0.235
1078	A	4	3	1.00	17	0.176
1079	A	4	4	1.00	17	0.235
1080	A	4	3	1.00	17	0.176
1081	A	4	4	1.00	17	0.235
1082	A	4	3	1.00	17	0.176
1083	A	1	1	1.00	17	0.059
1084	A	2	2	1.00	17	0.118
1085	A	3	2	1.00	17	0.118
1086	A	4	2	1.00	17	0.118
1087	A	5	2	1.00	17	0.118
1088	A	8	4	1.00	17	0.235

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1089	A	7	4	1.00	17	0.235
1090	A	6	4	1.00	17	0.235
1091	A	5	3	1.00	17	0.176
1092	A	5	4	1.00	17	0.235
1093	A	5	4	1.00	17	0.235
1094	A	5	3	1.00	17	0.176
1095	A	5	4	1.00	17	0.235
1096	A	5	4	1.00	17	0.235
1097	A	5	3	1.00	17	0.176
1098	A	1	1	1.00	17	0.059
1099	A	2	2	1.00	17	0.118
1100	A	3	2	1.00	17	0.118
1101	A	4	2	1.00	17	0.118
1102	A	5	2	1.00	17	0.118
1103	A	6	2	1.00	17	0.118
1104	A	4	3	1.00	20	0.150
1105	A	3	3	1.00	28	0.107
1106	A	6	3	1.00	17	0.176
1107	A	5	3	1.00	17	0.176
1108	A	4	3	1.00	17	0.176
1109	A	3	3	1.00	17	0.176
1110	A	2	2	1.00	17	0.118
1111	A	1	1	1.00	17	0.059
1112	A	2	2	1.00	17	0.118
1113	A	3	2	1.00	17	0.118
1114	A	4	2	1.00	17	0.118

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1115	A	5	2	1.00	17	0.118
1116	A	6	4	1.00	17	0.235
1117	A	5	4	1.00	17	0.235
1118	A	4	4	1.00	17	0.235
1119	A	3	3	1.00	17	0.176
1120	A	1	1	1.00	17	0.059
1121	A	1	1	1.00	17	0.059
1122	A	2	2	1.00	17	0.118
1123	A	3	2	1.00	17	0.118
1124	A	4	2	1.00	17	0.118
1125	A	5	2	1.00	17	0.118
1126	A	7	4	1.00	17	0.235
1127	A	6	4	1.00	17	0.235
1128	A	5	4	1.00	17	0.235
1129	A	4	3	1.00	17	0.176
1130	A	1	1	1.00	17	0.059
1131	A	2	2	1.00	17	0.118
1132	A	3	2	1.00	17	0.118
1133	A	2	2	1.00	17	0.118
1134	A	3	3	1.00	17	0.176
1135	A	4	3	1.00	17	0.176
1136	A	5	3	1.00	17	0.176
1137	A	6	4	1.00	20	0.200
1138	A	5	4	1.00	20	0.200
1139	A	4	4	1.00	20	0.200
1140	A	3	3	1.00	20	0.150

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1141	A	1	1	1.00	20	0.050
1142	A	2	2	1.00	20	0.100
1143	A	3	2	1.00	20	0.100
1144	A	4	2	1.00	20	0.100
1145	A	6	4	1.00	23	0.174
1146	A	5	4	1.00	23	0.174
1147	A	4	4	1.00	23	0.174
1148	A	3	3	1.00	23	0.130
1149	A	1	1	1.00	23	0.043
1150	A	2	2	1.00	23	0.087
1151	A	3	2	1.00	23	0.087
1152	A	4	2	1.00	23	0.087
1153	A	5	3	1.00	19	0.158
1154	A	4	3	1.00	19	0.158
1155	A	3	3	1.00	19	0.158
1156	A	2	2	1.00	19	0.105
1157	A	1	1	1.00	19	0.053
1158	A	2	2	1.00	19	0.105
1159	A	3	2	1.00	19	0.105
1160	A	7	4	1.00	17	0.235
1161	A	5	4	1.00	17	0.235
1162	A	3	3	1.00	17	0.176
1163	A	2	2	1.00	17	0.118
1164	A	4	2	1.00	17	0.118
1165	A	1	1	1.00	17	0.059
1166	A	1	1	1.00	20	0.050

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1167	A	1	1	1.00	17	0.059
1168	A	1	1	1.00	20	0.050
1169	A	3	3	1.00	23	0.130
1170	A	11	8	1.00	20	0.400
1171	A	6	5	1.00	25	0.200
1172	A	5	5	1.00	25	0.200
1173	A	4	4	1.00	25	0.160
1174	A	4	4	1.00	25	0.160
1175	A	4	4	1.00	25	0.160
1176	A	5	5	1.00	25	0.200
1177	A	6	5	1.00	25	0.200
1178	A	12	9	1.00	25	0.360
1179	A	11	8	1.00	25	0.320
1180	A	1	1	1.00	25	0.040
1181	A	2	2	1.00	25	0.080
1182	A	3	2	1.00	25	0.080
1183	A	4	2	1.00	25	0.080
1184	A	12	9	1.00	25	0.360
1185	A	11	8	1.00	25	0.320
1186	A	1	1	1.00	25	0.040
1187	A	2	2	1.00	25	0.080
1188	A	3	2	1.00	25	0.080
1189	A	5	4	1.00	25	0.160
1190	A	4	4	1.00	25	0.160
1191	A	3	3	1.00	25	0.120
1192	A	4	4	1.00	25	0.160

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1193	A	5	4	1.00	25	0.160
1194	A	13	10	1.00	25	0.400
1195	A	12	9	1.00	25	0.360
1196	A	1	1	1.00	25	0.040
1197	A	2	2	1.00	25	0.080
1198	A	3	2	1.00	25	0.080
1199	A	6	5	1.00	25	0.200
1200	A	5	5	1.00	25	0.200
1201	A	4	4	1.00	25	0.160
1202	A	4	4	1.00	25	0.160
1203	A	4	4	1.00	25	0.160
1204	A	5	5	1.00	25	0.200
1205	A	6	5	1.00	25	0.200
1206	A	6	6	1.00	25	0.240
1207	A	5	5	1.00	25	0.200
1208	A	4	4	1.00	25	0.160
1209	A	3	3	1.00	25	0.120
1210	A	4	4	1.00	25	0.160
1211	A	5	4	1.00	25	0.160
1212	A	13	10	1.00	25	0.400
1213	A	12	9	1.00	25	0.360
1214	A	1	1	1.00	25	0.040
1215	A	2	2	1.00	25	0.080
1216	A	3	2	1.00	25	0.080
1217	A	6	5	1.00	25	0.200
1218	A	5	5	1.00	25	0.200

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1219	A	4	4	1.00	25	0.160
1220	A	5	5	1.00	25	0.200
1221	A	4	4	1.00	25	0.160
1222	A	5	5	1.00	25	0.200
1223	A	6	5	1.00	25	0.200
1224	A	13	9	1.00	25	0.360
1225	A	1	1	1.00	25	0.040
1226	A	2	2	1.00	25	0.080
1227	A	3	2	1.00	25	0.080
1228	A	4	2	1.00	25	0.080
1229	A	2	1	1.00	19	0.053
1230	A	2	1	1.00	17	0.059
1231	A	1	1	1.00	19	0.053
1232	A	1	1	1.00	19	0.053
1233	A	3	3	1.00	16	0.188
1234	A	3	3	1.00	19	0.158
1235	A	2	2	1.00	15	0.133
1236	A	2	1	1.00	13	0.077
1237	A	2	1	1.00	13	0.077
1238	A	2	1	1.00	13	0.077
1239	A	2	1	1.00	11	0.091
1240	A	1	0	1.00	5	0.000
1241	A	2	1	1.00	13	0.077
1242	A	2	1	1.00	13	0.077
1243	A	1	1	1.00	13	0.077
1244	A	2	1	1.00	13	0.077

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1245	A	2	1	1.00	13	0.077
1246	A	2	1	1.00	15	0.067
1247	A	2	1	1.00	15	0.067
1248	A	2	1	1.00	15	0.067
1249	A	2	1	1.00	13	0.077
1250	A	1	1	1.00	7	0.143
1251	A	2	1	1.00	15	0.067
1252	A	2	1	1.00	15	0.067
1253	A	2	1	1.00	15	0.067
1254	A	1	1	1.00	15	0.067
1255	A	2	1	1.00	15	0.067
1256	A	2	1	1.00	15	0.067
1257	A	2	1	1.00	15	0.067
1258	A	2	1	1.00	15	0.067
1259	A	2	1	1.00	15	0.067
1260	A	2	1	1.00	15	0.067
1261	A	2	1	1.00	15	0.067
1262	A	2	1	1.00	13	0.077
1263	A	1	1	1.00	7	0.143
1264	A	2	1	1.00	15	0.067
1265	A	2	1	1.00	15	0.067
1266	A	2	1	1.00	15	0.067
1267	A	2	1	1.00	15	0.067
1268	A	1	1	1.00	15	0.067
1269	A	2	2	1.00	15	0.133
1270	A	2	1	1.00	15	0.067

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1271	A	2	1	1.00	15	0.067
1272	A	2	1	1.00	15	0.067
1273	A	2	1	1.00	15	0.067
1274	A	2	1	1.00	15	0.067
1275	A	2	1	1.00	15	0.067
1276	A	2	1	1.00	15	0.067
1277	A	2	1	1.00	15	0.067
1278	A	2	1	1.00	15	0.067
1279	A	2	1	1.00	15	0.067
1280	A	2	1	1.00	15	0.067
1281	A	2	1	1.00	13	0.077
1282	A	1	1	1.00	7	0.143
1283	A	2	1	1.00	15	0.067
1284	A	2	1	1.00	15	0.067
1285	A	2	1	1.00	15	0.067
1286	A	2	1	1.00	15	0.067
1287	A	2	1	1.00	15	0.067
1288	A	2	1	1.00	15	0.067
1289	A	2	1	1.00	15	0.067
1290	A	2	1	1.00	15	0.067
1291	A	1	1	1.00	15	0.067
1292	A	2	2	1.00	15	0.133
1293	A	3	2	1.00	15	0.133
1294	A	4	2	1.00	15	0.133
1295	A	5	2	1.00	15	0.133
1296	A	2	1	1.00	15	0.067

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1297	A	2	1	1.00	15	0.067
1298	A	2	1	1.00	15	0.067
1299	A	2	1	1.00	15	0.067
1300	A	2	1	1.00	15	0.067
1301	A	2	1	1.00	15	0.067
1302	A	2	1	1.00	15	0.067
1303	A	2	1	1.00	15	0.067
1304	A	2	1	1.00	15	0.067
1305	A	2	1	1.00	15	0.067
1306	A	2	1	1.00	15	0.067
1307	A	2	1	1.00	15	0.067
1308	A	2	1	1.00	15	0.067
1309	A	2	1	1.00	15	0.067
1310	A	2	1	1.00	13	0.077
1311	A	1	1	1.00	7	0.143
1312	A	2	1	1.00	15	0.067
1313	A	2	1	1.00	15	0.067
1314	A	2	1	1.00	15	0.067
1315	A	2	1	1.00	15	0.067
1316	A	2	1	1.00	15	0.067
1317	A	2	1	1.00	15	0.067
1318	A	2	1	1.00	15	0.067
1319	A	2	1	1.00	15	0.067
1320	A	2	1	1.00	15	0.067
1321	A	2	1	1.00	15	0.067
1322	A	2	1	1.00	15	0.067

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1323	A	1	1	1.00	15	0.067
1324	A	2	2	1.00	15	0.133
1325	A	3	2	1.00	15	0.133
1326	A	4	2	1.00	15	0.133
1327	A	5	2	1.00	15	0.133
1328	A	6	2	1.00	15	0.133
1329	A	7	2	1.00	15	0.133
1330	A	8	2	1.00	15	0.133
1331	A	2	1	1.00	15	0.067
1332	A	2	1	1.00	15	0.067
1333	A	2	1	1.00	15	0.067
1334	A	2	1	1.00	15	0.067
1335	A	2	1	1.00	15	0.067
1336	A	2	1	1.00	15	0.067
1337	A	2	1	1.00	15	0.067
1338	A	2	1	1.00	13	0.077
1339	A	1	1	1.00	7	0.143
1340	A	3	2	1.00	15	0.133
1341	A	2	1	1.00	15	0.067
1342	A	2	1	1.00	15	0.067
1343	A	2	1	1.00	15	0.067
1344	A	2	1	1.00	15	0.067
1345	A	2	1	1.00	15	0.067
1346	A	2	1	1.00	15	0.067
1347	A	2	1	1.00	13	0.077
1348	A	1	1	1.00	7	0.143

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1349	A	2	1	1.00	15	0.067
1350	A	2	1	1.00	15	0.067
1351	A	2	1	1.00	15	0.067
1352	A	2	1	1.00	15	0.067
1353	A	2	1	1.00	15	0.067
1354	A	2	1	1.00	15	0.067
1355	A	2	1	1.00	15	0.067
1356	A	2	1	1.00	15	0.067
1357	A	1	1	1.00	13	0.077
1358	A	1	1	1.00	7	0.143
1359	A	2	1	1.00	15	0.067
1360	A	2	1	1.00	15	0.067
1361	A	2	1	1.00	15	0.067
1362	A	2	1	1.00	15	0.067
1363	A	2	1	1.00	15	0.067
1364	A	2	1	1.00	15	0.067
1365	A	1	1	1.00	15	0.067
1366	A	2	2	1.00	15	0.133
1367	A	3	2	1.00	15	0.133
1368	A	2	1	1.00	15	0.067
1369	A	2	1	1.00	15	0.067
1370	A	2	1	1.00	13	0.077
1371	A	1	1	1.00	7	0.143
1372	A	2	1	1.00	15	0.067
1373	A	2	1	1.00	15	0.067
1374	A	2	1	1.00	15	0.067

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1375	A	2	1	1.00	17	0.059
1376	A	2	1	1.00	17	0.059
1377	A	2	1	1.00	17	0.059
1378	A	2	1	1.00	17	0.059
1379	A	2	1	1.00	15	0.067
1380	A	1	1	1.00	9	0.111
1381	A	3	3	1.00	17	0.176
1382	A	3	3	1.00	17	0.176
1383	A	4	4	1.00	17	0.235
1384	A	5	4	1.00	17	0.235
1385	A	6	4	1.00	17	0.235
1386	A	7	4	1.00	17	0.235
1387	A	2	1	1.00	17	0.059
1388	A	2	1	1.00	17	0.059
1389	A	2	1	1.00	17	0.059
1390	A	2	1	1.00	17	0.059
1391	A	2	1	1.00	15	0.067
1392	A	1	1	1.00	9	0.111
1393	A	4	3	1.00	17	0.176
1394	A	4	4	1.00	17	0.235
1395	A	4	3	1.00	17	0.176
1396	A	5	4	1.00	17	0.235
1397	A	6	4	1.00	17	0.235
1398	A	7	4	1.00	17	0.235
1399	A	2	1	1.00	17	0.059
1400	A	2	1	1.00	17	0.059

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1401	A	2	1	1.00	17	0.059
1402	A	2	1	1.00	17	0.059
1403	A	2	1	1.00	15	0.067
1404	A	1	1	1.00	9	0.111
1405	A	5	3	1.00	17	0.176
1406	A	5	4	1.00	17	0.235
1407	A	5	4	1.00	17	0.235
1408	A	5	3	1.00	17	0.176
1409	A	6	4	1.00	17	0.235
1410	A	7	4	1.00	17	0.235
1411	A	3	3	1.00	13	0.231
1412	A	4	4	1.00	13	0.308
1413	A	2	1	1.00	17	0.059
1414	A	2	1	1.00	17	0.059
1415	A	2	1	1.00	17	0.059
1416	A	2	1	1.00	17	0.059
1417	A	2	1	1.00	15	0.067
1418	A	1	1	1.00	9	0.111
1419	A	2	2	1.00	17	0.118
1420	A	3	3	1.00	17	0.176
1421	A	4	3	1.00	17	0.176
1422	A	5	3	1.00	17	0.176
1423	A	6	3	1.00	17	0.176
1424	A	2	1	1.00	17	0.059
1425	A	2	1	1.00	17	0.059
1426	A	2	1	1.00	17	0.059

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1427	A	2	1	1.00	17	0.059
1428	A	2	1	1.00	15	0.067
1429	A	1	1	1.00	9	0.111
1430	A	3	3	1.00	17	0.176
1431	A	4	3	1.00	17	0.176
1432	A	5	3	1.00	17	0.176
1433	A	6	3	1.00	17	0.176
1434	A	2	1	1.00	17	0.059
1435	A	2	1	1.00	17	0.059
1436	A	2	1	1.00	17	0.059
1437	A	2	1	1.00	17	0.059
1438	A	2	1	1.00	15	0.067
1439	A	1	1	1.00	9	0.111
1440	A	4	3	1.00	17	0.176
1441	A	5	3	1.00	17	0.176
1442	A	6	3	1.00	17	0.176
1443	A	7	3	1.00	17	0.176
1444	A	2	2	1.00	20	0.100
1445	A	2	2	1.00	20	0.100
1446	A	2	2	1.00	20	0.100
1447	A	2	2	1.00	20	0.100
1448	A	2	2	1.00	20	0.100
1449	A	2	2	1.00	20	0.100
1450	A	2	2	1.00	20	0.100
1451	A	2	2	1.00	20	0.100
1452	A	2	2	1.00	20	0.100

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1453	A	2	2	1.00	13	0.154
1454	A	2	2	1.00	17	0.118
1455	A	5	5	1.00	15	0.333
1456	A	2	1	1.00	13	0.077
1457	A	2	1	1.00	15	0.067
1458	A	4	4	1.00	17	0.235
1459	A	4	4	1.00	17	0.235
1460	A	8	4	1.00	19	0.210
1461	A	7	4	1.00	19	0.210
1462	A	6	4	1.00	19	0.210
1463	A	5	4	1.00	19	0.210
1464	A	4	4	1.00	19	0.210
1465	A	4	4	1.00	19	0.210
1466	A	1	1	1.00	19	0.053
1467	A	2	2	1.00	19	0.105
1468	A	3	2	1.00	19	0.105
1469	A	4	2	1.00	19	0.105
1470	A	5	2	1.00	19	0.105
1471	A	8	4	1.00	19	0.210
1472	A	7	4	1.00	19	0.210
1473	A	6	4	1.00	19	0.210
1474	A	5	4	1.00	19	0.210
1475	A	5	5	1.00	19	0.263
1476	A	5	4	1.00	19	0.210
1477	A	1	1	1.00	19	0.053
1478	A	2	2	1.00	19	0.105

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1479	A	3	2	1.00	19	0.105
1480	A	4	2	1.00	19	0.105
1481	A	9	4	1.00	19	0.210
1482	A	8	4	1.00	19	0.210
1483	A	7	4	1.00	19	0.210
1484	A	6	4	1.00	19	0.210
1485	A	6	5	1.00	19	0.263
1486	A	6	5	1.00	19	0.263
1487	A	6	4	1.00	19	0.210
1488	A	1	1	1.00	19	0.053
1489	A	2	2	1.00	19	0.105
1490	A	3	2	1.00	19	0.105
1491	A	4	2	1.00	19	0.105
1492	A	7	4	1.00	19	0.210
1493	A	6	4	1.00	19	0.210
1494	A	5	4	1.00	19	0.210
1495	A	4	4	1.00	19	0.210
1496	A	3	3	1.00	19	0.158
1497	A	1	1	1.00	19	0.053
1498	A	2	2	1.00	19	0.105
1499	A	3	2	1.00	19	0.105
1500	A	4	2	1.00	19	0.105
1501	A	5	2	1.00	19	0.105
1502	A	7	5	1.00	19	0.263
1503	A	6	5	1.00	19	0.263
1504	A	5	5	1.00	19	0.263

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1505	A	4	4	1.00	19	0.210
1506	A	1	1	1.00	19	0.053
1507	A	2	2	1.00	19	0.105
1508	A	3	2	1.00	19	0.105
1509	A	4	2	1.00	19	0.105
1510	A	5	2	1.00	19	0.105
1511	A	6	2	1.00	19	0.105
1512	A	8	5	1.00	19	0.263
1513	A	7	5	1.00	19	0.263
1514	A	6	5	1.00	19	0.263
1515	A	5	4	1.00	19	0.210
1516	A	1	1	1.00	19	0.053
1517	A	2	2	1.00	19	0.105
1518	A	3	2	1.00	19	0.105
1519	A	4	2	1.00	19	0.105
1520	A	5	2	1.00	19	0.105
1521	A	6	2	1.00	19	0.105
1522	A	2	2	1.00	20	0.100
1523	A	2	2	1.00	19	0.105
1524	A	2	2	1.00	19	0.105
1525	A	2	2	1.00	17	0.118
1526	A	2	2	1.00	19	0.105
1527	A	1	1	1.00	19	0.053
1528	A	2	2	1.00	19	0.105
1529	A	2	2	1.00	19	0.105
1530	A	1	1	1.00	7	0.143

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1531	A	2	2	1.00	19	0.105
1532	A	2	2	1.00	17	0.118
1533	A	2	2	1.00	19	0.105
1534	A	1	1	1.00	19	0.053
1535	A	2	2	1.00	19	0.105
1536	A	3	3	1.00	20	0.150
1537	A	2	2	1.00	20	0.100
1538	A	3	3	1.00	20	0.150
1539	A	3	3	1.00	18	0.167
1540	A	3	3	1.00	20	0.150
1541	A	2	2	1.00	20	0.100
1542	A	3	3	1.00	20	0.150
1543	A	2	2	1.00	21	0.095
1544	A	1	1	1.00	8	0.125
1545	A	2	2	1.00	21	0.095
1546	A	2	2	1.00	19	0.105
1547	A	2	2	1.00	21	0.095
1548	A	1	1	1.00	21	0.048
1549	A	2	2	1.00	21	0.095
1550	A	1	1	1.00	19	0.053
1551	A	2	2	1.00	29	0.069
1552	A	2	2	1.00	15	0.133
1553	A	2	2	1.00	19	0.105
1554	A	2	2	1.00	29	0.069
1555	A	3	3	1.00	15	0.200
1556	A	2	2	1.00	15	0.133

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1557	A	2	2	1.00	19	0.105
1558	A	3	3	1.00	20	0.150
1559	A	5	3	1.00	19	0.158
1560	A	4	3	1.00	19	0.158
1561	A	3	3	1.00	19	0.158
1562	A	3	3	1.00	19	0.158
1563	A	4	4	1.00	19	0.210
1564	A	5	4	1.00	19	0.210
1565	A	6	5	1.00	19	0.263
1566	A	5	5	1.00	19	0.263
1567	A	4	4	1.00	19	0.210
1568	A	5	5	1.00	19	0.263
1569	A	6	5	1.00	19	0.263
1570	A	4	3	1.00	19	0.158
1571	A	3	3	1.00	19	0.158
1572	A	2	2	1.00	19	0.105
1573	A	3	3	1.00	19	0.158
1574	A	4	3	1.00	19	0.158
1575	A	3	2	1.00	19	0.105
1576	A	2	2	1.00	19	0.105
1577	A	2	2	1.00	19	0.105
1578	A	1	1	1.00	19	0.053
1579	A	2	2	1.00	19	0.105
1580	A	3	2	1.00	19	0.105
1581	A	4	2	1.00	19	0.105
1582	A	6	4	1.00	19	0.210

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1583	A	5	4	1.00	19	0.210
1584	A	4	4	1.00	19	0.210
1585	A	4	4	1.00	19	0.210
1586	A	5	5	1.00	19	0.263
1587	A	3	2	1.00	19	0.105
1588	A	2	2	1.00	19	0.105
1589	A	1	1	1.00	19	0.053
1590	A	1	1	1.00	19	0.053
1591	A	2	2	1.00	19	0.105
1592	A	3	2	1.00	19	0.105
1593	A	4	2	1.00	19	0.105
1594	A	8	6	1.00	19	0.316
1595	A	7	6	1.00	19	0.316
1596	A	6	6	1.00	19	0.316
1597	A	5	5	1.00	19	0.263
1598	A	6	6	1.00	19	0.316
1599	A	7	6	1.00	19	0.316
1600	A	8	6	1.00	19	0.316
1601	A	3	2	1.00	19	0.105
1602	A	2	2	1.00	19	0.105
1603	A	1	1	1.00	19	0.053
1604	A	1	1	1.00	19	0.053
1605	A	2	2	1.00	19	0.105
1606	A	3	2	1.00	19	0.105
1607	A	4	2	1.00	19	0.105
1608	A	6	4	1.00	19	0.210

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1609	A	5	4	1.00	19	0.210
1610	A	4	4	1.00	19	0.210
1611	A	3	3	1.00	19	0.158
1612	A	4	4	1.00	19	0.210
1613	A	5	4	1.00	19	0.210
1614	A	6	4	1.00	19	0.210
1615	A	4	3	1.00	19	0.158
1616	A	3	3	1.00	19	0.158
1617	A	2	2	1.00	19	0.105
1618	A	1	1	1.00	19	0.053
1619	A	2	2	1.00	19	0.105
1620	A	3	2	1.00	19	0.105
1621	A	4	2	1.00	19	0.105
1622	A	8	7	1.00	19	0.368
1623	A	7	7	1.00	19	0.368
1624	A	6	6	1.00	19	0.316
1625	A	6	6	1.00	19	0.316
1626	A	7	6	1.00	19	0.316
1627	A	8	6	1.00	19	0.316
1628	A	2	2	1.00	15	0.133
1629	A	6	4	1.00	19	0.210
1630	A	5	4	1.00	19	0.210
1631	A	4	4	1.00	19	0.210
1632	A	4	4	1.00	19	0.210
1633	A	5	5	1.00	19	0.263
1634	A	6	5	1.00	19	0.263

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1635	A	10	8	1.00	19	0.421
1636	A	9	8	1.00	19	0.421
1637	A	8	8	1.00	19	0.421
1638	A	8	8	1.00	19	0.421
1639	A	9	9	1.00	19	0.474
1640	A	10	9	1.00	19	0.474
1641	A	7	4	1.00	19	0.210
1642	A	6	4	1.00	19	0.210
1643	A	5	4	1.00	19	0.210
1644	A	5	5	1.00	19	0.263
1645	A	5	4	1.00	19	0.210
1646	A	6	5	1.00	19	0.263
1647	A	7	5	1.00	19	0.263
1648	A	10	8	1.00	19	0.421
1649	A	9	8	1.00	19	0.421
1650	A	8	8	1.00	19	0.421
1651	A	7	7	1.00	19	0.368
1652	A	8	8	1.00	19	0.421
1653	A	9	8	1.00	19	0.421
1654	A	5	4	1.00	19	0.210
1655	A	4	4	1.00	19	0.210
1656	A	3	3	1.00	19	0.158
1657	A	4	4	1.00	19	0.210
1658	A	5	4	1.00	19	0.210
1659	A	10	9	1.00	19	0.474
1660	A	9	9	1.00	19	0.474

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1661	A	8	8	1.00	19	0.421
1662	A	8	8	1.00	19	0.421
1663	A	9	8	1.00	19	0.421
1664	A	10	8	1.00	19	0.421
1665	A	7	5	1.00	19	0.263
1666	A	5	5	1.00	19	0.263
1667	A	4	4	1.00	19	0.210
1668	A	4	4	1.00	19	0.210
1669	A	5	4	1.00	19	0.210
1670	A	6	4	1.00	19	0.210
1671	A	11	9	1.00	19	0.474
1672	A	10	9	1.00	19	0.474
1673	A	9	8	1.00	19	0.421
1674	A	9	9	1.00	19	0.474
1675	A	9	8	1.00	19	0.421
1676	A	10	8	1.00	19	0.421
1677	A	11	8	1.00	19	0.421
1678	A	8	6	1.00	19	0.316
1679	A	7	6	1.00	19	0.316
1680	A	7	7	1.00	19	0.368
1681	A	7	6	1.00	19	0.316
1682	A	1	1	1.00	19	0.053
1683	A	2	2	1.00	19	0.105
1684	A	3	2	1.00	19	0.105
1685	A	4	2	1.00	19	0.105
1686	A	7	4	1.00	19	0.210

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1687	A	6	4	1.00	19	0.210
1688	A	5	4	1.00	19	0.210
1689	A	5	5	1.00	19	0.263
1690	A	5	4	1.00	19	0.210
1691	A	6	5	1.00	19	0.263
1692	A	7	5	1.00	19	0.263
1693	A	7	6	1.00	19	0.316
1694	A	6	6	1.00	19	0.316
1695	A	5	5	1.00	19	0.263
1696	A	1	1	1.00	19	0.053
1697	A	2	2	1.00	19	0.105
1698	A	3	2	1.00	19	0.105
1699	A	4	2	1.00	19	0.105
1700	A	7	6	1.00	19	0.316
1701	A	6	6	1.00	19	0.316
1702	A	5	5	1.00	19	0.263
1703	A	6	6	1.00	19	0.316
1704	A	7	6	1.00	19	0.316
1705	A	7	6	1.00	19	0.316
1706	A	6	6	1.00	19	0.316
1707	A	5	5	1.00	19	0.263
1708	A	1	1	1.00	19	0.053
1709	A	2	2	1.00	19	0.105
1710	A	3	2	1.00	19	0.105
1711	A	4	2	1.00	19	0.105
1712	A	5	4	1.00	19	0.210

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1713	A	4	4	1.00	19	0.210
1714	A	3	3	1.00	19	0.158
1715	A	4	4	1.00	19	0.210
1716	A	5	4	1.00	19	0.210
1717	A	7	7	1.00	19	0.368
1718	A	6	6	1.00	19	0.316
1719	A	1	1	1.00	19	0.053
1720	A	2	2	1.00	19	0.105
1721	A	3	2	1.00	19	0.105
1722	A	4	2	1.00	19	0.105
1723	A	8	7	1.00	19	0.368
1724	A	7	7	1.00	19	0.368
1725	A	6	6	1.00	19	0.316
1726	A	6	6	1.00	19	0.316
1727	A	7	6	1.00	19	0.316
1728	A	8	6	1.00	19	0.316
1729	A	11	8	1.00	20	0.400
1730	A	11	8	1.00	20	0.400
1731	A	2	2	1.00	19	0.105
1732	A	2	2	1.00	19	0.105
1733	A	2	2	1.00	19	0.105
1734	A	2	2	1.00	19	0.105
1735	A	2	2	1.00	19	0.105
1736	A	6	3	1.00	19	0.158
1737	A	5	3	1.00	19	0.158
1738	A	4	3	1.00	19	0.158

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1739	A	3	3	1.00	19	0.158
1740	A	3	3	1.00	19	0.158
1741	A	4	4	1.00	19	0.210
1742	A	7	5	1.00	19	0.263
1743	A	6	5	1.00	19	0.263
1744	A	5	5	1.00	19	0.263
1745	A	5	5	1.00	19	0.263
1746	A	6	6	1.00	19	0.316
1747	A	7	6	1.00	19	0.316
1748	A	7	5	1.00	19	0.263
1749	A	6	5	1.00	19	0.263
1750	A	5	5	1.00	19	0.263
1751	A	4	4	1.00	19	0.210
1752	A	5	5	1.00	19	0.263
1753	A	6	5	1.00	19	0.263
1754	A	5	3	1.00	19	0.158
1755	A	4	3	1.00	19	0.158
1756	A	3	3	1.00	19	0.158
1757	A	2	2	1.00	19	0.105
1758	A	3	3	1.00	19	0.158
1759	A	4	3	1.00	19	0.158
1760	A	7	6	1.00	19	0.316
1761	A	6	6	1.00	19	0.316
1762	A	5	5	1.00	19	0.263
1763	A	5	5	1.00	19	0.263
1764	A	6	5	1.00	19	0.263

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1765	A	7	5	1.00	19	0.263
1766	A	2	2	1.00	19	0.105
1767	A	2	2	1.00	19	0.105
1768	A	2	2	1.00	19	0.105
1769	A	2	2	1.00	19	0.105
1770	A	2	2	1.00	19	0.105
1771	A	2	2	1.00	19	0.105
1772	A	14	9	1.00	19	0.474
1773	A	13	9	1.00	19	0.474
1774	A	13	9	1.00	19	0.474
1775	A	1	1	1.00	19	0.053
1776	A	2	2	1.00	19	0.105
1777	A	3	2	1.00	19	0.105
1778	A	4	2	1.00	19	0.105
1779	A	14	9	1.00	19	0.474
1780	A	13	9	1.00	19	0.474
1781	A	13	9	1.00	19	0.474
1782	A	1	1	1.00	19	0.053
1783	A	2	2	1.00	19	0.105
1784	A	3	2	1.00	19	0.105
1785	A	4	2	1.00	19	0.105
1786	A	2	2	1.00	19	0.105
1787	A	2	2	1.00	19	0.105
1788	A	2	2	1.00	19	0.105
1789	A	2	2	1.00	19	0.105
1790	A	2	2	1.00	19	0.105

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1791	A	2	2	1.00	19	0.105
1792	A	2	2	1.00	19	0.105
1793	A	2	2	1.00	19	0.105
1794	A	2	2	1.00	19	0.105
1795	A	2	2	1.00	19	0.105
1796	A	2	2	1.00	19	0.105
1797	A	2	2	1.00	19	0.105
1798	A	14	9	1.00	19	0.474
1799	A	14	10	1.00	19	0.526
1800	A	14	9	1.00	19	0.474
1801	A	1	1	1.00	19	0.053
1802	A	2	2	1.00	19	0.105
1803	A	3	2	1.00	19	0.105
1804	A	4	2	1.00	19	0.105
1805	A	14	9	1.00	19	0.474
1806	A	13	9	1.00	19	0.474
1807	A	12	8	1.00	19	0.421
1808	A	1	1	1.00	19	0.053
1809	A	2	2	1.00	19	0.105
1810	A	3	2	1.00	19	0.105
1811	A	4	2	1.00	19	0.105
1812	A	2	2	1.00	19	0.105
1813	A	2	2	1.00	19	0.105
1814	A	2	2	1.00	19	0.105
1815	A	2	2	1.00	19	0.105
1816	A	2	2	1.00	19	0.105

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1817	A	2	2	1.00	19	0.105
1818	A	2	2	1.00	19	0.105
1819	A	2	2	1.00	19	0.105
1820	A	2	2	1.00	19	0.105
1821	A	2	2	1.00	19	0.105
1822	A	2	2	1.00	19	0.105
1823	A	2	2	1.00	19	0.105
1824	A	14	9	1.00	19	0.474
1825	A	13	9	1.00	19	0.474
1826	A	12	8	1.00	19	0.421
1827	A	1	1	1.00	19	0.053
1828	A	2	2	1.00	19	0.105
1829	A	3	2	1.00	19	0.105
1830	A	4	2	1.00	19	0.105
1831	A	15	10	1.00	19	0.526
1832	A	14	10	1.00	19	0.526
1833	A	13	9	1.00	19	0.474
1834	A	1	1	1.00	19	0.053
1835	A	2	2	1.00	19	0.105
1836	A	3	2	1.00	19	0.105
1837	A	4	2	1.00	19	0.105
1838	A	2	2	1.00	19	0.105
1839	A	2	2	1.00	19	0.105
1840	A	2	2	1.00	19	0.105
1841	A	2	2	1.00	19	0.105
1842	A	2	2	1.00	19	0.105

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1843	A	2	2	1.00	19	0.105
1844	A	1	1	1.00	16	0.062
1845	A	2	2	1.21	15	0.133
1846	A	2	1	1.00	15	0.067
1847	A	2	1	1.00	15	0.067
1848	A	2	1	1.00	13	0.077
1849	A	1	1	1.00	15	0.067
1850	A	1	1	1.00	15	0.067
1851	A	1	1	1.00	15	0.067
1852	A	2	1	1.00	15	0.067
1853	A	2	1	1.00	15	0.067
1854	A	2	1	1.00	13	0.077
1855	A	1	1	1.00	7	0.143
1856	A	1	1	1.00	15	0.067
1857	A	1	1	1.00	15	0.067
1858	A	1	1	1.00	15	0.067
1859	A	3	2	1.00	19	0.105
1860	A	2	2	1.00	19	0.105
1861	A	1	1	1.00	19	0.053
1862	A	2	2	1.00	19	0.105
1863	A	2	2	1.00	17	0.118
1864	A	2	2	1.00	19	0.105
1865	A	2	2	1.00	19	0.105
1866	A	2	2	1.00	17	0.118
1867	A	2	2	1.00	19	0.105
1868	A	1	1	1.00	19	0.053

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1869	A	2	2	1.00	19	0.105
1870	A	3	2	1.00	19	0.105
1871	A	4	2	1.00	19	0.105
1872	A	2	2	1.00	17	0.118
1873	A	2	2	1.00	19	0.105
1874	A	1	1	1.00	19	0.053
1875	A	2	2	1.00	19	0.105
1876	A	3	2	1.00	19	0.105
1877	A	4	2	1.00	19	0.105
1878	A	2	2	1.00	21	0.095
1879	A	2	2	1.00	21	0.095
1880	A	2	2	1.00	24	0.083
1881	A	3	2	1.00	24	0.083
1882	A	2	2	1.00	28	0.071
1883	A	2	2	1.00	44	0.045
1884	A	2	2	1.00	51	0.039
1885	A	1	1	1.00	15	0.067
1886	A	1	1	1.00	15	0.067
1887	A	1	1	1.00	15	0.067
1888	A	1	1	1.00	15	0.067
1889	A	1	1	1.00	17	0.059
1890	A	2	2	1.00	27	0.074
1891	A	1	0	1.00	15	0.000
1892	A	1	0	1.00	9	0.000
1893	A	1	0	1.00	5	0.000
1894	A	1	0	1.00	5	0.000

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1895	A	1	0	1.00	9	0.000
1896	A	1	0	1.00	9	0.000
1897	A	1	0	1.00	15	0.000
1898	A	1	0	1.00	10	0.000
1899	A	1	0	1.00	10	0.000
1900	A	1	0	1.00	12	0.000
1901	A	1	0	1.00	15	0.000
1902	A	1	0	1.00	17	0.000
1903	A	1	0	1.00	8	0.000
1904	A	1	0	1.00	10	0.000
1905	A	1	0	1.00	11	0.000
1906	A	1	0	1.00	11	0.000
1907	A	1	0	1.00	6	0.000
1908	A	1	0	1.00	11	0.000
1909	A	1	0	1.00	10	0.000
1910	A	1	0	1.00	11	0.000
1911	A	1	0	1.00	7	0.000
1912	A	1	0	1.00	17	0.000
1913	A	1	0	1.00	18	0.000
1914	A	1	0	1.00	11	0.000
1915	A	1	0	1.00	15	0.000
1916	A	1	0	1.00	18	0.000
1917	A	1	0	1.00	20	0.000

Chapter 3

Listing of integrals

3.1 $\int 0 dx$

Optimal. Leaf size=1

0

[Out] 0

Rubi [A] time = 0.00, antiderivative size = 1, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 1, $\frac{\text{number of rules}}{\text{integrand size}} = 1.000$, Rules used = {8}

0

Antiderivative was successfully verified.

[In] Int[0,x]

[Out] 0

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\int 0 dx = 0$$

Mathematica [A] time = 0.00, size = 1, normalized size = 1.00

0

Antiderivative was successfully verified.

```
[In] Integrate[0,x]
```

```
[Out] 0
```

```
fricas [A]   time = 0.34, size = 1, normalized size = 1.00
```

0

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(0,x, algorithm="fricas")
```

```
[Out] 0
```

```
giac [A]   time = 1.09, size = 1, normalized size = 1.00
```

0

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(0,x, algorithm="giac")
```

```
[Out] 0
```

```
maple [A]   time = 0.00, size = 2, normalized size = 2.00
```

0

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(0,x)
```

```
[Out] 0
```

```
maxima [A]   time = 0.42, size = 1, normalized size = 1.00
```

0

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(0,x, algorithm="maxima")
```

```
[Out] 0
```

```
mupad [B]   time = 0.04, size = 1, normalized size = 1.00
```

0

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(0,x)
```

```
[Out] 0
```

```
sympy [A] time = 0.01, size = 0, normalized size = 0.00
```

0

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(0,x)
```

```
[Out] 0
```

3.2 $\int 1 dx$

Optimal. Leaf size=1

x

[Out] x

Rubi [A] time = 0.00, antiderivative size = 1, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 1, $\frac{\text{number of rules}}{\text{integrand size}} = 1.000$, Rules used = {8}

x

Antiderivative was successfully verified.

[In] Int[1,x]

[Out] x

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\int 1 dx = x$$

Mathematica [A] time = 0.00, size = 1, normalized size = 1.00

x

Antiderivative was successfully verified.

[In] Integrate[1,x]

[Out] x

fricas [A] time = 0.36, size = 1, normalized size = 1.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1,x, algorithm="fricas")

[Out] x

giac [A] time = 1.07, size = 1, normalized size = 1.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1,x, algorithm="giac")`

[Out] x

maple [A] time = 0.00, size = 2, normalized size = 2.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1,x)`

[Out] x

maxima [A] time = 0.41, size = 1, normalized size = 1.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1,x, algorithm="maxima")`

[Out] x

mupad [B] time = 0.01, size = 1, normalized size = 1.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1,x)`

[Out] x

sympy [A] time = 0.02, size = 0, normalized size = 0.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1,x)`

[Out] x

3.3 $\int 5 dx$

Optimal. Leaf size=3

$$5x$$

[Out] 5*x

Rubi [A] time = 0.00, antiderivative size = 3, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 1, $\frac{\text{number of rules}}{\text{integrand size}} = 1.000$, Rules used = {8}

$$5x$$

Antiderivative was successfully verified.

[In] Int[5,x]

[Out] 5*x

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\int 5 dx = 5x$$

Mathematica [A] time = 0.00, size = 3, normalized size = 1.00

$$5x$$

Antiderivative was successfully verified.

[In] Integrate[5,x]

[Out] 5*x

fricas [A] time = 0.36, size = 3, normalized size = 1.00

$$5x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(5,x, algorithm="fricas")

[Out] $5x$

giac [A] time = 1.04, size = 3, normalized size = 1.00

$5x$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(5,x, algorithm="giac")`

[Out] $5x$

maple [A] time = 0.00, size = 4, normalized size = 1.33

$5x$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(5,x)`

[Out] $5x$

maxima [A] time = 0.41, size = 3, normalized size = 1.00

$5x$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(5,x, algorithm="maxima")`

[Out] $5x$

mupad [B] time = 0.01, size = 3, normalized size = 1.00

$5x$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(5,x)`

[Out] $5x$

sympy [A] time = 0.02, size = 2, normalized size = 0.67

$5x$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(5,x)`

[Out] $5x$

3.4 $\int -2 dx$

Optimal. Leaf size=3

$$-2x$$

[Out] -2*x

Rubi [A] time = 0.00, antiderivative size = 3, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 1, $\frac{\text{number of rules}}{\text{integrand size}} = 1.000$, Rules used = {8}

$$-2x$$

Antiderivative was successfully verified.

[In] Int[-2,x]

[Out] -2*x

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\int -2 dx = -2x$$

Mathematica [A] time = 0.00, size = 3, normalized size = 1.00

$$-2x$$

Antiderivative was successfully verified.

[In] Integrate[-2,x]

[Out] -2*x

fricas [A] time = 0.35, size = 3, normalized size = 1.00

$$-2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-2,x, algorithm="fricas")

[Out] $-2*x$

giac [A] time = 1.11, size = 3, normalized size = 1.00

$-2x$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-2,x, algorithm="giac")`

[Out] $-2*x$

maple [A] time = 0.00, size = 4, normalized size = 1.33

$-2x$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-2,x)`

[Out] $-2*x$

maxima [A] time = 0.42, size = 3, normalized size = 1.00

$-2x$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-2,x, algorithm="maxima")`

[Out] $-2*x$

mupad [B] time = 0.00, size = 3, normalized size = 1.00

$-2x$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-2,x)`

[Out] $-2*x$

sympy [A] time = 0.02, size = 3, normalized size = 1.00

$-2x$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-2,x)`

[Out] $-2*x$

$$3.5 \quad \int -\frac{3}{2} dx$$

Optimal. Leaf size=5

$$-\frac{3x}{2}$$

[Out] -3/2*x

Rubi [A] time = 0.00, antiderivative size = 5, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {8}

$$-\frac{3x}{2}$$

Antiderivative was successfully verified.

[In] Int[-3/2,x]

[Out] (-3*x)/2

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\int -\frac{3}{2} dx = -\frac{3x}{2}$$

Mathematica [A] time = 0.00, size = 5, normalized size = 1.00

$$-\frac{3x}{2}$$

Antiderivative was successfully verified.

[In] Integrate[-3/2,x]

[Out] (-3*x)/2

fricas [A] time = 0.38, size = 3, normalized size = 0.60

$$-\frac{3}{2}x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-3/2,x, algorithm="fricas")

[Out] -3/2*x

giac [A] time = 1.16, size = 3, normalized size = 0.60

$$-\frac{3}{2}x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-3/2,x, algorithm="giac")

[Out] -3/2*x

maple [A] time = 0.00, size = 4, normalized size = 0.80

$$-\frac{3x}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-3/2,x)

[Out] -3/2*x

maxima [A] time = 0.42, size = 3, normalized size = 0.60

$$-\frac{3}{2}x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-3/2,x, algorithm="maxima")

[Out] -3/2*x

mupad [B] time = 0.01, size = 3, normalized size = 0.60

$$-\frac{3x}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-3/2,x)

[Out] -(3*x)/2

sympy [A] time = 0.01, size = 5, normalized size = 1.00

$$-\frac{3x}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-3/2,x)

[Out] -3*x/2

3.6 $\int \pi dx$

Optimal. Leaf size=3

$$\pi x$$

[Out] Pi*x

Rubi [A] time = 0.00, antiderivative size = 3, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 1, $\frac{\text{number of rules}}{\text{integrand size}} = 1.000$, Rules used = {8}

$$\pi x$$

Antiderivative was successfully verified.

[In] Int[Pi,x]

[Out] Pi*x

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\int \pi dx = \pi x$$

Mathematica [A] time = 0.00, size = 3, normalized size = 1.00

$$\pi x$$

Antiderivative was successfully verified.

[In] Integrate[Pi,x]

[Out] Pi*x

fricas [A] time = 0.38, size = 3, normalized size = 1.00

$$\pi x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(pi,x, algorithm="fricas")

[Out] pi*x

giac [A] time = 0.84, size = 3, normalized size = 1.00

$$\pi x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(pi,x, algorithm="giac")

[Out] pi*x

maple [A] time = 0.00, size = 4, normalized size = 1.33

$$\pi x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Pi,x)

[Out] Pi*x

maxima [A] time = 0.43, size = 3, normalized size = 1.00

$$\pi x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(pi,x, algorithm="maxima")

[Out] pi*x

mupad [B] time = 0.00, size = 3, normalized size = 1.00

$$\Pi x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Pi,x)

[Out] Pi*x

sympy [A] time = 0.01, size = 2, normalized size = 0.67

$$\pi x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(pi,x)

[Out] pi*x

3.7 $\int a dx$

Optimal. Leaf size=3

$$ax$$

[Out] a*x

Rubi [A] time = 0.00, antiderivative size = 3, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 1, $\frac{\text{number of rules}}{\text{integrand size}} = 1.000$, Rules used = {8}

$$ax$$

Antiderivative was successfully verified.

[In] Int[a,x]

[Out] a*x

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\int a dx = ax$$

Mathematica [A] time = 0.00, size = 3, normalized size = 1.00

$$ax$$

Antiderivative was successfully verified.

[In] Integrate[a,x]

[Out] a*x

fricas [A] time = 0.36, size = 3, normalized size = 1.00

$$xa$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(a,x, algorithm="fricas")

[Out] $x*a$

giac [A] time = 0.75, size = 3, normalized size = 1.00

ax

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(a,x, algorithm="giac")`

[Out] $a*x$

maple [A] time = 0.00, size = 4, normalized size = 1.33

ax

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(a,x)`

[Out] $a*x$

maxima [A] time = 0.44, size = 3, normalized size = 1.00

ax

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(a,x, algorithm="maxima")`

[Out] $a*x$

mupad [B] time = 0.00, size = 3, normalized size = 1.00

ax

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(a,x)`

[Out] $a*x$

sympy [A] time = 0.02, size = 2, normalized size = 0.67

ax

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(a,x)`

[Out] $a*x$

3.8 $\int 3a dx$

Optimal. Leaf size=4

$$3ax$$

[Out] 3*a*x

Rubi [A] time = 0.00, antiderivative size = 4, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {8}

$$3ax$$

Antiderivative was successfully verified.

[In] Int[3*a,x]

[Out] 3*a*x

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\int 3a dx = 3ax$$

Mathematica [A] time = 0.00, size = 4, normalized size = 1.00

$$3ax$$

Antiderivative was successfully verified.

[In] Integrate[3*a,x]

[Out] 3*a*x

fricas [A] time = 0.36, size = 4, normalized size = 1.00

$$3xa$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(3*a,x, algorithm="fricas")

[Out] $3*x*a$

giac [A] time = 1.25, size = 4, normalized size = 1.00

$$3ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(3*a,x, algorithm="giac")`

[Out] $3*a*x$

maple [A] time = 0.00, size = 5, normalized size = 1.25

$$3ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(3*a,x)`

[Out] $3*a*x$

maxima [A] time = 0.43, size = 4, normalized size = 1.00

$$3ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(3*a,x, algorithm="maxima")`

[Out] $3*a*x$

mupad [B] time = 0.00, size = 4, normalized size = 1.00

$$3ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(3*a,x)`

[Out] $3*a*x$

sympy [A] time = 0.02, size = 3, normalized size = 0.75

$$3ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(3*a,x)`

[Out] $3*a*x$

$$3.9 \quad \int \frac{\pi}{\sqrt{16-e^2}} dx$$

Optimal. Leaf size=14

$$\frac{\pi x}{\sqrt{16-e^2}}$$

[Out] Pi*x/(16-exp(2))^(1/2)

Rubi [A] time = 0.01, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {8}

$$\frac{\pi x}{\sqrt{16-e^2}}$$

Antiderivative was successfully verified.

[In] Int [Pi/Sqrt [16 - E^2], x]

[Out] (Pi*x)/Sqrt [16 - E^2]

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\int \frac{\pi}{\sqrt{16-e^2}} dx = \frac{\pi x}{\sqrt{16-e^2}}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{\pi x}{\sqrt{16-e^2}}$$

Antiderivative was successfully verified.

[In] Integrate [Pi/Sqrt [16 - E^2], x]

[Out] (Pi*x)/Sqrt [16 - E^2]

fricas [A] time = 0.40, size = 18, normalized size = 1.29

$$-\frac{\pi x \sqrt{-e^2 + 16}}{e^2 - 16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(pi/(16-exp(2))^(1/2),x, algorithm="fricas")

[Out] -pi*x*sqrt(-e^2 + 16)/(e^2 - 16)

giac [A] time = 1.08, size = 11, normalized size = 0.79

$$\frac{\pi x}{\sqrt{-e^2 + 16}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(pi/(16-exp(2))^(1/2),x, algorithm="giac")

[Out] pi*x/sqrt(-e^2 + 16)

maple [A] time = 0.00, size = 12, normalized size = 0.86

$$\frac{\pi x}{\sqrt{16 - e^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Pi/(16-exp(2))^(1/2),x)

[Out] Pi*x/(16-exp(2))^(1/2)

maxima [A] time = 0.45, size = 11, normalized size = 0.79

$$\frac{\pi x}{\sqrt{-e^2 + 16}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(pi/(16-exp(2))^(1/2),x, algorithm="maxima")

[Out] pi*x/sqrt(-e^2 + 16)

mupad [B] time = 0.00, size = 11, normalized size = 0.79

$$\frac{\Pi x}{\sqrt{16 - e^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Pi/(16 - exp(2))^(1/2),x)

[Out] (Pi*x)/(16 - exp(2))^(1/2)

sympy [A] time = 0.06, size = 10, normalized size = 0.71

$$\frac{\pi x}{\sqrt{16 - e^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(pi/(16-exp(2))**(1/2),x)
```

```
[Out] pi*x/sqrt(16 - exp(2))
```

3.10 $\int x^{100} dx$

Optimal. Leaf size=7

$$\frac{x^{101}}{101}$$

[Out] 1/101*x^101

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {30}

$$\frac{x^{101}}{101}$$

Antiderivative was successfully verified.

[In] Int[x^100,x]

[Out] x^101/101

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int x^{100} dx = \frac{x^{101}}{101}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$\frac{x^{101}}{101}$$

Antiderivative was successfully verified.

[In] Integrate[x^100,x]

[Out] x^101/101

fricas [A] time = 0.34, size = 5, normalized size = 0.71

$$\frac{1}{101}x^{101}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^100,x, algorithm="fricas")

[Out] 1/101*x^101

giac [A] time = 1.18, size = 5, normalized size = 0.71

$$\frac{1}{101} x^{101}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^100,x, algorithm="giac")

[Out] 1/101*x^101

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$\frac{x^{101}}{101}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^100,x)

[Out] 1/101*x^101

maxima [A] time = 0.42, size = 5, normalized size = 0.71

$$\frac{1}{101} x^{101}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^100,x, algorithm="maxima")

[Out] 1/101*x^101

mupad [B] time = 0.12, size = 5, normalized size = 0.71

$$\frac{x^{101}}{101}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^100,x)

[Out] x^101/101

sympy [A] time = 0.06, size = 3, normalized size = 0.43

$$\frac{x^{101}}{101}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**100,x)

[Out] x**101/101

3.11 $\int x^3 dx$

Optimal. Leaf size=7

$$\frac{x^4}{4}$$

[Out] 1/4*x^4

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {30}

$$\frac{x^4}{4}$$

Antiderivative was successfully verified.

[In] Int[x^3,x]

[Out] x^4/4

Rule 30

Int[(x_)^(m_), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int x^3 dx = \frac{x^4}{4}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$\frac{x^4}{4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3,x]

[Out] x^4/4

fricas [A] time = 0.34, size = 5, normalized size = 0.71

$$\frac{1}{4}x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3,x, algorithm="fricas")

[Out] 1/4*x^4

giac [A] time = 1.18, size = 5, normalized size = 0.71

$$\frac{1}{4}x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3,x, algorithm="giac")

[Out] 1/4*x^4

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$\frac{x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3,x)

[Out] 1/4*x^4

maxima [A] time = 0.42, size = 5, normalized size = 0.71

$$\frac{1}{4}x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3,x, algorithm="maxima")

[Out] 1/4*x^4

mupad [B] time = 0.02, size = 5, normalized size = 0.71

$$\frac{x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3,x)

[Out] x^4/4

sympy [A] time = 0.05, size = 3, normalized size = 0.43

$$\frac{x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3,x)

[Out] x**4/4

3.12 $\int x^2 dx$

Optimal. Leaf size=7

$$\frac{x^3}{3}$$

[Out] 1/3*x^3

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {30}

$$\frac{x^3}{3}$$

Antiderivative was successfully verified.

[In] Int[x^2,x]

[Out] x^3/3

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int x^2 dx = \frac{x^3}{3}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$\frac{x^3}{3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2,x]

[Out] x^3/3

fricas [A] time = 0.35, size = 5, normalized size = 0.71

$$\frac{1}{3}x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2,x, algorithm="fricas")

[Out] 1/3*x^3

giac [A] time = 1.10, size = 5, normalized size = 0.71

$$\frac{1}{3}x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2,x, algorithm="giac")

[Out] 1/3*x^3

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$\frac{x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2,x)

[Out] 1/3*x^3

maxima [A] time = 0.42, size = 5, normalized size = 0.71

$$\frac{1}{3}x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2,x, algorithm="maxima")

[Out] 1/3*x^3

mupad [B] time = 0.01, size = 5, normalized size = 0.71

$$\frac{x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2,x)

[Out] x^3/3

sympy [A] time = 0.05, size = 3, normalized size = 0.43

$$\frac{x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2,x)

[Out] x**3/3

3.13 $\int x dx$

Optimal. Leaf size=7

$$\frac{x^2}{2}$$

[Out] 1/2*x^2

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 1, $\frac{\text{number of rules}}{\text{integrand size}} = 1.000$, Rules used = {30}

$$\frac{x^2}{2}$$

Antiderivative was successfully verified.

[In] Int[x,x]

[Out] x^2/2

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int x dx = \frac{x^2}{2}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$\frac{x^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[x,x]

[Out] x^2/2

fricas [A] time = 0.35, size = 5, normalized size = 0.71

$$\frac{1}{2}x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x,x, algorithm="fricas")

[Out] 1/2*x^2

giac [A] time = 0.95, size = 5, normalized size = 0.71

$$\frac{1}{2}x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x,x, algorithm="giac")

[Out] 1/2*x^2

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$\frac{x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x,x)

[Out] 1/2*x^2

maxima [A] time = 0.42, size = 5, normalized size = 0.71

$$\frac{1}{2}x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x,x, algorithm="maxima")

[Out] 1/2*x^2

mupad [B] time = 0.01, size = 5, normalized size = 0.71

$$\frac{x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x,x)

[Out] x^2/2

sympy [A] time = 0.02, size = 3, normalized size = 0.43

$$\frac{x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x,x)

[Out] x**2/2

3.14 $\int 1 dx$

Optimal. Leaf size=1

x

[Out] x

Rubi [A] time = 0.00, antiderivative size = 1, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 1, $\frac{\text{number of rules}}{\text{integrand size}} = 1.000$, Rules used = {8}

x

Antiderivative was successfully verified.

[In] Int[1,x]

[Out] x

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\int 1 dx = x$$

Mathematica [A] time = 0.00, size = 1, normalized size = 1.00

x

Antiderivative was successfully verified.

[In] Integrate[1,x]

[Out] x

fricas [A] time = 0.34, size = 1, normalized size = 1.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1,x, algorithm="fricas")

[Out] x

giac [A] time = 1.00, size = 1, normalized size = 1.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1,x, algorithm="giac")`

[Out] x

maple [A] time = 0.00, size = 2, normalized size = 2.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1,x)`

[Out] x

maxima [A] time = 0.44, size = 1, normalized size = 1.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1,x, algorithm="maxima")`

[Out] x

mupad [B] time = 0.00, size = 1, normalized size = 1.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1,x)`

[Out] x

sympy [A] time = 0.01, size = 0, normalized size = 0.00

x

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1,x)`

[Out] x

3.15 $\int \frac{1}{x} dx$

Optimal. Leaf size=2

$$\log(x)$$

[Out] ln(x)

Rubi [A] time = 0.00, antiderivative size = 2, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {29}

$$\log(x)$$

Antiderivative was successfully verified.

[In] Int[x⁽⁻¹⁾, x]

[Out] Log[x]

Rule 29

Int[(x_)⁽⁻¹⁾, x_Symbol] :> Simp[Log[x], x]

Rubi steps

$$\int \frac{1}{x} dx = \log(x)$$

Mathematica [A] time = 0.00, size = 2, normalized size = 1.00

$$\log(x)$$

Antiderivative was successfully verified.

[In] Integrate[x⁽⁻¹⁾, x]

[Out] Log[x]

fricas [A] time = 0.38, size = 2, normalized size = 1.00

$$\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x,x, algorithm="fricas")

[Out] $\log(x)$

giac [A] time = 0.80, size = 3, normalized size = 1.50

$\log(|x|)$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x,x, algorithm="giac")`

[Out] $\log(\text{abs}(x))$

maple [A] time = 0.00, size = 3, normalized size = 1.50

$\ln(x)$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x,x)`

[Out] $\ln(x)$

maxima [A] time = 0.44, size = 2, normalized size = 1.00

$\log(x)$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x,x, algorithm="maxima")`

[Out] $\log(x)$

mupad [B] time = 0.04, size = 2, normalized size = 1.00

$\ln(x)$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x,x)`

[Out] $\log(x)$

sympy [A] time = 0.06, size = 2, normalized size = 1.00

$\log(x)$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x,x)`

[Out] $\log(x)$

3.16 $\int \frac{1}{x^2} dx$

Optimal. Leaf size=5

$$-\frac{1}{x}$$

[Out] -1/x

Rubi [A] time = 0.00, antiderivative size = 5, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {30}

$$-\frac{1}{x}$$

Antiderivative was successfully verified.

[In] Int[x^(-2), x]

[Out] -x^(-1)

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^2} dx = -\frac{1}{x}$$

Mathematica [A] time = 0.00, size = 5, normalized size = 1.00

$$-\frac{1}{x}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-2), x]

[Out] -x^(-1)

fricas [A] time = 0.38, size = 5, normalized size = 1.00

$$-\frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2,x, algorithm="fricas")

[Out] -1/x

giac [A] time = 0.85, size = 5, normalized size = 1.00

$$-\frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2,x, algorithm="giac")

[Out] -1/x

maple [A] time = 0.00, size = 6, normalized size = 1.20

$$-\frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2,x)

[Out] -1/x

maxima [A] time = 0.43, size = 5, normalized size = 1.00

$$-\frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2,x, algorithm="maxima")

[Out] -1/x

mupad [B] time = 0.03, size = 5, normalized size = 1.00

$$-\frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2,x)

[Out] -1/x

sympy [A] time = 0.06, size = 3, normalized size = 0.60

$$-\frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2,x)

[Out] -1/x

$$3.17 \quad \int \frac{1}{x^3} dx$$

Optimal. Leaf size=7

$$-\frac{1}{2x^2}$$

[Out] -1/2/x^2

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {30}

$$-\frac{1}{2x^2}$$

Antiderivative was successfully verified.

[In] Int[x^(-3), x]

[Out] -1/(2*x^2)

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^3} dx = -\frac{1}{2x^2}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$-\frac{1}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-3), x]

[Out] -1/2*1/x^2

fricas [A] time = 0.37, size = 5, normalized size = 0.71

$$-\frac{1}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3,x, algorithm="fricas")

[Out] -1/2/x^2

giac [A] time = 0.84, size = 5, normalized size = 0.71

$$-\frac{1}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3,x, algorithm="giac")

[Out] -1/2/x^2

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$-\frac{1}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3,x)

[Out] -1/2/x^2

maxima [A] time = 0.49, size = 5, normalized size = 0.71

$$-\frac{1}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3,x, algorithm="maxima")

[Out] -1/2/x^2

mupad [B] time = 0.01, size = 5, normalized size = 0.71

$$-\frac{1}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3,x)

[Out] -1/(2*x^2)

sympy [A] time = 0.06, size = 7, normalized size = 1.00

$$-\frac{1}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3,x)

[Out] -1/(2*x**2)

3.18 $\int \frac{1}{x^4} dx$

Optimal. Leaf size=7

$$-\frac{1}{3x^3}$$

[Out] -1/3/x^3

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {30}

$$-\frac{1}{3x^3}$$

Antiderivative was successfully verified.

[In] Int[x^(-4), x]

[Out] -1/(3*x^3)

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^4} dx = -\frac{1}{3x^3}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$-\frac{1}{3x^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-4), x]

[Out] -1/3*1/x^3

fricas [A] time = 0.39, size = 5, normalized size = 0.71

$$-\frac{1}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4,x, algorithm="fricas")

[Out] -1/3/x^3

giac [A] time = 1.13, size = 5, normalized size = 0.71

$$-\frac{1}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4,x, algorithm="giac")

[Out] -1/3/x^3

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$-\frac{1}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^4,x)

[Out] -1/3/x^3

maxima [A] time = 0.43, size = 5, normalized size = 0.71

$$-\frac{1}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4,x, algorithm="maxima")

[Out] -1/3/x^3

mupad [B] time = 0.01, size = 5, normalized size = 0.71

$$-\frac{1}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^4,x)

[Out] -1/(3*x^3)

sympy [A] time = 0.06, size = 7, normalized size = 1.00

$$-\frac{1}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**4,x)

[Out] -1/(3*x**3)

$$3.19 \quad \int \frac{1}{x^{100}} dx$$

Optimal. Leaf size=7

$$-\frac{1}{99x^{99}}$$

[Out] -1/99/x^99

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {30}

$$-\frac{1}{99x^{99}}$$

Antiderivative was successfully verified.

[In] Int[x^(-100), x]

[Out] -1/(99*x^99)

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{100}} dx = -\frac{1}{99x^{99}}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$-\frac{1}{99x^{99}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-100), x]

[Out] -1/99*1/x^99

fricas [A] time = 0.40, size = 5, normalized size = 0.71

$$-\frac{1}{99x^{99}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^100,x, algorithm="fricas")

[Out] -1/99/x^99

giac [A] time = 1.29, size = 5, normalized size = 0.71

$$-\frac{1}{99x^{99}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^100,x, algorithm="giac")

[Out] -1/99/x^99

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$-\frac{1}{99x^{99}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^100,x)

[Out] -1/99/x^99

maxima [A] time = 0.42, size = 5, normalized size = 0.71

$$-\frac{1}{99x^{99}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^100,x, algorithm="maxima")

[Out] -1/99/x^99

mupad [B] time = 0.07, size = 5, normalized size = 0.71

$$-\frac{1}{99x^{99}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^100,x)

[Out] -1/(99*x^99)

sympy [A] time = 0.06, size = 7, normalized size = 1.00

$$-\frac{1}{99x^{99}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**100,x)

[Out] -1/(99*x**99)

3.20 $\int x^{5/2} dx$

Optimal. Leaf size=9

$$\frac{2x^{7/2}}{7}$$

[Out] 2/7*x^(7/2)

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$\frac{2x^{7/2}}{7}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2), x]

[Out] (2*x^(7/2))/7

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int x^{5/2} dx = \frac{2x^{7/2}}{7}$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$\frac{2x^{7/2}}{7}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2), x]

[Out] (2*x^(7/2))/7

fricas [A] time = 0.41, size = 5, normalized size = 0.56

$$\frac{2}{7} x^{\frac{7}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2),x, algorithm="fricas")

[Out] 2/7*x^(7/2)

giac [A] time = 0.90, size = 5, normalized size = 0.56

$$\frac{2}{7}x^{\frac{7}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2),x, algorithm="giac")

[Out] 2/7*x^(7/2)

maple [A] time = 0.02, size = 6, normalized size = 0.67

$$\frac{2x^{\frac{7}{2}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2),x)

[Out] 2/7*x^(7/2)

maxima [A] time = 0.43, size = 5, normalized size = 0.56

$$\frac{2}{7}x^{\frac{7}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2),x, algorithm="maxima")

[Out] 2/7*x^(7/2)

mupad [B] time = 0.08, size = 5, normalized size = 0.56

$$\frac{2x^{7/2}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2),x)

[Out] (2*x^(7/2))/7

sympy [A] time = 0.07, size = 7, normalized size = 0.78

$$\frac{2x^{\frac{7}{2}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/2),x)`

[Out] `2*x**(7/2)/7`

3.21 $\int x^{3/2} dx$

Optimal. Leaf size=9

$$\frac{2x^{5/2}}{5}$$

[Out] 2/5*x^(5/2)

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$\frac{2x^{5/2}}{5}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2), x]

[Out] (2*x^(5/2))/5

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int x^{3/2} dx = \frac{2x^{5/2}}{5}$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$\frac{2x^{5/2}}{5}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2), x]

[Out] (2*x^(5/2))/5

fricas [A] time = 0.39, size = 5, normalized size = 0.56

$$\frac{2}{5} x^{5/2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2),x, algorithm="fricas")

[Out] 2/5*x^(5/2)

giac [A] time = 0.98, size = 5, normalized size = 0.56

$$\frac{2}{5}x^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2),x, algorithm="giac")

[Out] 2/5*x^(5/2)

maple [A] time = 0.00, size = 6, normalized size = 0.67

$$\frac{2x^{\frac{5}{2}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2),x)

[Out] 2/5*x^(5/2)

maxima [A] time = 0.42, size = 5, normalized size = 0.56

$$\frac{2}{5}x^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2),x, algorithm="maxima")

[Out] 2/5*x^(5/2)

mupad [B] time = 0.03, size = 5, normalized size = 0.56

$$\frac{2x^{5/2}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2),x)

[Out] (2*x^(5/2))/5

sympy [A] time = 0.06, size = 7, normalized size = 0.78

$$\frac{2x^{\frac{5}{2}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2),x)

[Out] 2*x**(5/2)/5

3.22 $\int \sqrt{x} dx$

Optimal. Leaf size=9

$$\frac{2x^{3/2}}{3}$$

[Out] 2/3*x^(3/2)

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$\frac{2x^{3/2}}{3}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x], x]

[Out] (2*x^(3/2))/3

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \sqrt{x} dx = \frac{2x^{3/2}}{3}$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$\frac{2x^{3/2}}{3}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x], x]

[Out] (2*x^(3/2))/3

fricas [A] time = 0.39, size = 5, normalized size = 0.56

$$\frac{2}{3} x^{3/2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2),x, algorithm="fricas")

[Out] 2/3*x^(3/2)

giac [A] time = 1.04, size = 5, normalized size = 0.56

$$\frac{2}{3}x^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2),x, algorithm="giac")

[Out] 2/3*x^(3/2)

maple [A] time = 0.00, size = 6, normalized size = 0.67

$$\frac{2x^{\frac{3}{2}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2),x)

[Out] 2/3*x^(3/2)

maxima [A] time = 0.42, size = 5, normalized size = 0.56

$$\frac{2}{3}x^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2),x, algorithm="maxima")

[Out] 2/3*x^(3/2)

mupad [B] time = 0.03, size = 5, normalized size = 0.56

$$\frac{2x^{3/2}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2),x)

[Out] (2*x^(3/2))/3

sympy [A] time = 0.06, size = 7, normalized size = 0.78

$$\frac{2x^{\frac{3}{2}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2),x)`

[Out] `2*x**(3/2)/3`

3.23 $\int \frac{1}{\sqrt{x}} dx$

Optimal. Leaf size=7

$$2\sqrt{x}$$

[Out] $2*x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$2\sqrt{x}$$

Antiderivative was successfully verified.

[In] Int[1/Sqrt[x],x]

[Out] 2*Sqrt[x]

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt{x}} dx = 2\sqrt{x}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$2\sqrt{x}$$

Antiderivative was successfully verified.

[In] Integrate[1/Sqrt[x],x]

[Out] 2*Sqrt[x]

fricas [A] time = 0.39, size = 5, normalized size = 0.71

$$2\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2),x, algorithm="fricas")

[Out] 2*sqrt(x)

giac [A] time = 1.13, size = 5, normalized size = 0.71

$$2\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2),x, algorithm="giac")

[Out] 2*sqrt(x)

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$2\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/2),x)

[Out] 2*x^(1/2)

maxima [A] time = 0.42, size = 5, normalized size = 0.71

$$2\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2),x, algorithm="maxima")

[Out] 2*sqrt(x)

mupad [B] time = 0.03, size = 5, normalized size = 0.71

$$2\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/2),x)

[Out] 2*x^(1/2)

sympy [A] time = 0.06, size = 5, normalized size = 0.71

$$2\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(1/2),x)

[Out] 2*sqrt(x)

$$3.24 \quad \int \frac{1}{x^{3/2}} dx$$

Optimal. Leaf size=7

$$-\frac{2}{\sqrt{x}}$$

[Out] $-2/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$-\frac{2}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[x^(-3/2), x]

[Out] -2/Sqrt[x]

Rule 30

Int[(x_)^(m_), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{3/2}} dx = -\frac{2}{\sqrt{x}}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$-\frac{2}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-3/2), x]

[Out] -2/Sqrt[x]

fricas [A] time = 0.42, size = 5, normalized size = 0.71

$$-\frac{2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2),x, algorithm="fricas")

[Out] -2/sqrt(x)

giac [A] time = 1.01, size = 5, normalized size = 0.71

$$-\frac{2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2),x, algorithm="giac")

[Out] -2/sqrt(x)

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$-\frac{2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2),x)

[Out] -2/x^(1/2)

maxima [A] time = 0.70, size = 5, normalized size = 0.71

$$-\frac{2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2),x, algorithm="maxima")

[Out] -2/sqrt(x)

mupad [B] time = 0.03, size = 5, normalized size = 0.71

$$-\frac{2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2),x)

[Out] $-2/x^{(1/2)}$

sympy [A] time = 0.06, size = 7, normalized size = 1.00

$$-\frac{2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2),x)`

[Out] $-2/\text{sqrt}(x)$

$$3.25 \quad \int \frac{1}{x^{5/2}} dx$$

Optimal. Leaf size=9

$$-\frac{2}{3x^{3/2}}$$

[Out] -2/3/x^(3/2)

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$-\frac{2}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[x^(-5/2), x]

[Out] -2/(3*x^(3/2))

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{5/2}} dx = -\frac{2}{3x^{3/2}}$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$-\frac{2}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-5/2), x]

[Out] -2/(3*x^(3/2))

fricas [A] time = 0.40, size = 5, normalized size = 0.56

$$-\frac{2}{3x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2),x, algorithm="fricas")`

[Out] $-2/3/x^{(3/2)}$

giac [A] time = 0.92, size = 5, normalized size = 0.56

$$-\frac{2}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2),x, algorithm="giac")`

[Out] $-2/3/x^{(3/2)}$

maple [A] time = 0.00, size = 6, normalized size = 0.67

$$-\frac{2}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/2),x)`

[Out] $-2/3/x^{(3/2)}$

maxima [A] time = 0.62, size = 5, normalized size = 0.56

$$-\frac{2}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2),x, algorithm="maxima")`

[Out] $-2/3/x^{(3/2)}$

mupad [B] time = 0.03, size = 5, normalized size = 0.56

$$-\frac{2}{3x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/2),x)`

[Out] $-2/(3*x^{(3/2)})$

sympy [A] time = 0.06, size = 8, normalized size = 0.89

$$-\frac{2}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2),x)`

[Out] $-2/(3*x^{(3/2)})$

3.26 $\int x^{5/3} dx$

Optimal. Leaf size=9

$$\frac{3x^{8/3}}{8}$$

[Out] 3/8*x^(8/3)

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$\frac{3x^{8/3}}{8}$$

Antiderivative was successfully verified.

[In] Int[x^(5/3), x]

[Out] (3*x^(8/3))/8

Rule 30

Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int x^{5/3} dx = \frac{3x^{8/3}}{8}$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$\frac{3x^{8/3}}{8}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/3), x]

[Out] (3*x^(8/3))/8

fricas [A] time = 0.40, size = 5, normalized size = 0.56

$$\frac{3}{8} x^{8/3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3),x, algorithm="fricas")

[Out] 3/8*x^(8/3)

giac [A] time = 1.05, size = 5, normalized size = 0.56

$$\frac{3}{8}x^{\frac{8}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3),x, algorithm="giac")

[Out] 3/8*x^(8/3)

maple [A] time = 0.00, size = 6, normalized size = 0.67

$$\frac{3x^{\frac{8}{3}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/3),x)

[Out] 3/8*x^(8/3)

maxima [A] time = 0.56, size = 5, normalized size = 0.56

$$\frac{3}{8}x^{\frac{8}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3),x, algorithm="maxima")

[Out] 3/8*x^(8/3)

mupad [B] time = 0.07, size = 5, normalized size = 0.56

$$\frac{3x^{8/3}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/3),x)

[Out] (3*x^(8/3))/8

sympy [A] time = 0.06, size = 7, normalized size = 0.78

$$\frac{3x^{\frac{8}{3}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/3),x)

[Out] 3*x**(8/3)/8

3.27 $\int x^{4/3} dx$

Optimal. Leaf size=9

$$\frac{3x^{7/3}}{7}$$

[Out] 3/7*x^(7/3)

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$\frac{3x^{7/3}}{7}$$

Antiderivative was successfully verified.

[In] Int[x^(4/3), x]

[Out] (3*x^(7/3))/7

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int x^{4/3} dx = \frac{3x^{7/3}}{7}$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$\frac{3x^{7/3}}{7}$$

Antiderivative was successfully verified.

[In] Integrate[x^(4/3), x]

[Out] (3*x^(7/3))/7

fricas [A] time = 0.40, size = 5, normalized size = 0.56

$$\frac{3}{7} x^{7/3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(4/3),x, algorithm="fricas")`

[Out] $3/7*x^{(7/3)}$

giac [A] time = 1.05, size = 5, normalized size = 0.56

$$\frac{3}{7}x^{\frac{7}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(4/3),x, algorithm="giac")`

[Out] $3/7*x^{(7/3)}$

maple [A] time = 0.00, size = 6, normalized size = 0.67

$$\frac{3x^{\frac{7}{3}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(4/3),x)`

[Out] $3/7*x^{(7/3)}$

maxima [A] time = 0.56, size = 5, normalized size = 0.56

$$\frac{3}{7}x^{\frac{7}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(4/3),x, algorithm="maxima")`

[Out] $3/7*x^{(7/3)}$

mupad [B] time = 0.07, size = 5, normalized size = 0.56

$$\frac{3x^{7/3}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(4/3),x)`

[Out] $(3*x^{(7/3)})/7$

sympy [A] time = 0.06, size = 7, normalized size = 0.78

$$\frac{3x^{\frac{7}{3}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(4/3),x)`

[Out] `3*x**(7/3)/7`

3.28 $\int x^{2/3} dx$

Optimal. Leaf size=9

$$\frac{3x^{5/3}}{5}$$

[Out] 3/5*x^(5/3)

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$\frac{3x^{5/3}}{5}$$

Antiderivative was successfully verified.

[In] Int[x^(2/3),x]

[Out] (3*x^(5/3))/5

Rule 30

Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int x^{2/3} dx = \frac{3x^{5/3}}{5}$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$\frac{3x^{5/3}}{5}$$

Antiderivative was successfully verified.

[In] Integrate[x^(2/3),x]

[Out] (3*x^(5/3))/5

fricas [A] time = 0.41, size = 5, normalized size = 0.56

$$\frac{3}{5} x^{5/3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3),x, algorithm="fricas")

[Out] 3/5*x^(5/3)

giac [A] time = 0.91, size = 5, normalized size = 0.56

$$\frac{3}{5}x^{\frac{5}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3),x, algorithm="giac")

[Out] 3/5*x^(5/3)

maple [A] time = 0.00, size = 6, normalized size = 0.67

$$\frac{3x^{\frac{5}{3}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(2/3),x)

[Out] 3/5*x^(5/3)

maxima [A] time = 0.51, size = 5, normalized size = 0.56

$$\frac{3}{5}x^{\frac{5}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3),x, algorithm="maxima")

[Out] 3/5*x^(5/3)

mupad [B] time = 0.07, size = 5, normalized size = 0.56

$$\frac{3x^{5/3}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(2/3),x)

[Out] (3*x^(5/3))/5

sympy [A] time = 0.06, size = 7, normalized size = 0.78

$$\frac{3x^{\frac{5}{3}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(2/3),x)

[Out] 3*x**(5/3)/5

3.29 $\int \sqrt[3]{x} dx$

Optimal. Leaf size=9

$$\frac{3x^{4/3}}{4}$$

[Out] 3/4*x^(4/3)

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$\frac{3x^{4/3}}{4}$$

Antiderivative was successfully verified.

[In] Int[x^(1/3), x]

[Out] (3*x^(4/3))/4

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \sqrt[3]{x} dx = \frac{3x^{4/3}}{4}$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$\frac{3x^{4/3}}{4}$$

Antiderivative was successfully verified.

[In] Integrate[x^(1/3), x]

[Out] (3*x^(4/3))/4

fricas [A] time = 0.39, size = 5, normalized size = 0.56

$$\frac{3}{4} x^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(1/3),x, algorithm="fricas")`

[Out] $3/4*x^{4/3}$

giac [A] time = 0.85, size = 5, normalized size = 0.56

$$\frac{3}{4}x^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(1/3),x, algorithm="giac")`

[Out] $3/4*x^{4/3}$

maple [A] time = 0.00, size = 6, normalized size = 0.67

$$\frac{3x^{\frac{4}{3}}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/3),x)`

[Out] $3/4*x^{4/3}$

maxima [A] time = 0.48, size = 5, normalized size = 0.56

$$\frac{3}{4}x^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(1/3),x, algorithm="maxima")`

[Out] $3/4*x^{4/3}$

mupad [B] time = 0.06, size = 5, normalized size = 0.56

$$\frac{3x^{4/3}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/3),x)`

[Out] $(3*x^{4/3})/4$

sympy [A] time = 0.06, size = 7, normalized size = 0.78

$$\frac{3x^{\frac{4}{3}}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(1/3),x)

[Out] 3*x**(4/3)/4

$$3.30 \quad \int \frac{1}{\sqrt[3]{x}} dx$$

Optimal. Leaf size=9

$$\frac{3x^{2/3}}{2}$$

[Out] 3/2*x^(2/3)

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$\frac{3x^{2/3}}{2}$$

Antiderivative was successfully verified.

[In] Int[x^(-1/3), x]

[Out] (3*x^(2/3))/2

Rule 30

Int[(x_)^(m_), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt[3]{x}} dx = \frac{3x^{2/3}}{2}$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$\frac{3x^{2/3}}{2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-1/3), x]

[Out] (3*x^(2/3))/2

fricas [A] time = 0.38, size = 5, normalized size = 0.56

$$\frac{3}{2} x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3),x, algorithm="fricas")

[Out] 3/2*x^(2/3)

giac [A] time = 1.14, size = 5, normalized size = 0.56

$$\frac{3}{2}x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3),x, algorithm="giac")

[Out] 3/2*x^(2/3)

maple [A] time = 0.00, size = 6, normalized size = 0.67

$$\frac{3x^{\frac{2}{3}}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/3),x)

[Out] 3/2*x^(2/3)

maxima [A] time = 0.46, size = 5, normalized size = 0.56

$$\frac{3}{2}x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3),x, algorithm="maxima")

[Out] 3/2*x^(2/3)

mupad [B] time = 0.04, size = 5, normalized size = 0.56

$$\frac{3x^{2/3}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/3),x)

[Out] (3*x^(2/3))/2

sympy [A] time = 0.06, size = 7, normalized size = 0.78

$$\frac{3x^{\frac{2}{3}}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(1/3),x)`

[Out] `3*x**(2/3)/2`

$$3.31 \quad \int \frac{1}{x^{2/3}} dx$$

Optimal. Leaf size=7

$$3\sqrt[3]{x}$$

[Out] 3*x^(1/3)

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$3\sqrt[3]{x}$$

Antiderivative was successfully verified.

[In] Int[x^(-2/3), x]

[Out] 3*x^(1/3)

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{2/3}} dx = 3\sqrt[3]{x}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$3\sqrt[3]{x}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-2/3), x]

[Out] 3*x^(1/3)

fricas [A] time = 0.38, size = 5, normalized size = 0.71

$$3x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3),x, algorithm="fricas")

[Out] 3*x^(1/3)

giac [A] time = 0.95, size = 5, normalized size = 0.71

$$3x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3),x, algorithm="giac")

[Out] 3*x^(1/3)

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$3x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(2/3),x)

[Out] 3*x^(1/3)

maxima [A] time = 0.52, size = 5, normalized size = 0.71

$$3x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3),x, algorithm="maxima")

[Out] 3*x^(1/3)

mupad [B] time = 0.07, size = 5, normalized size = 0.71

$$3x^{1/3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(2/3),x)

[Out] 3*x^(1/3)

sympy [A] time = 0.06, size = 5, normalized size = 0.71

$$3\sqrt[3]{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**(2/3),x)
```

```
[Out] 3*x**(1/3)
```


$$3.32 \quad \int \frac{1}{x^{4/3}} dx$$

Optimal. Leaf size=7

$$-\frac{3}{\sqrt[3]{x}}$$

[Out] $-3/x^{(1/3)}$

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$-\frac{3}{\sqrt[3]{x}}$$

Antiderivative was successfully verified.

[In] Int[x^(-4/3), x]

[Out] $-3/x^{(1/3)}$

Rule 30

Int[(x_)^(m_), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{4/3}} dx = -\frac{3}{\sqrt[3]{x}}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$-\frac{3}{\sqrt[3]{x}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-4/3), x]

[Out] $-3/x^{(1/3)}$

fricas [A] time = 0.38, size = 5, normalized size = 0.71

$$-\frac{3}{x^{3/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3),x, algorithm="fricas")

[Out] -3/x^(1/3)

giac [A] time = 1.12, size = 5, normalized size = 0.71

$$-\frac{3}{x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3),x, algorithm="giac")

[Out] -3/x^(1/3)

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$-\frac{3}{x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(4/3),x)

[Out] -3/x^(1/3)

maxima [A] time = 0.51, size = 5, normalized size = 0.71

$$-\frac{3}{x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3),x, algorithm="maxima")

[Out] -3/x^(1/3)

mupad [B] time = 0.07, size = 5, normalized size = 0.71

$$-\frac{3}{x^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(4/3),x)

[Out] $-3/x^{(1/3)}$

sympy [A] time = 0.06, size = 7, normalized size = 1.00

$$-\frac{3}{\sqrt[3]{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(4/3),x)`

[Out] $-3/x^{(1/3)}$

$$3.33 \quad \int \frac{1}{x^{5/3}} dx$$

Optimal. Leaf size=9

$$-\frac{3}{2x^{2/3}}$$

[Out] $-3/2/x^{(2/3)}$

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {30}

$$-\frac{3}{2x^{2/3}}$$

Antiderivative was successfully verified.

[In] Int[x^(-5/3), x]

[Out] $-3/(2*x^{(2/3)})$

Rule 30

Int[(x_)^(m_), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{5/3}} dx = -\frac{3}{2x^{2/3}}$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$-\frac{3}{2x^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-5/3), x]

[Out] $-3/(2*x^{(2/3)})$

fricas [A] time = 0.39, size = 5, normalized size = 0.56

$$-\frac{3}{2x^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/3),x, algorithm="fricas")`

[Out] $-3/2/x^{(2/3)}$

giac [A] time = 0.92, size = 5, normalized size = 0.56

$$-\frac{3}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/3),x, algorithm="giac")`

[Out] $-3/2/x^{(2/3)}$

maple [A] time = 0.00, size = 6, normalized size = 0.67

$$-\frac{3}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/3),x)`

[Out] $-3/2/x^{(2/3)}$

maxima [A] time = 0.49, size = 5, normalized size = 0.56

$$-\frac{3}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/3),x, algorithm="maxima")`

[Out] $-3/2/x^{(2/3)}$

mupad [B] time = 0.05, size = 5, normalized size = 0.56

$$-\frac{3}{2x^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/3),x)`

[Out] $-3/(2*x^{(2/3)})$

sympy [A] time = 0.06, size = 8, normalized size = 0.89

$$-\frac{3}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/3),x)`

[Out] $-3/(2*x^{(2/3)})$

3.34 $\int x^n dx$

Optimal. Leaf size=11

$$\frac{x^{n+1}}{n+1}$$

[Out] $x^{(1+n)/(1+n)}$

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {30}

$$\frac{x^{n+1}}{n+1}$$

Antiderivative was successfully verified.

[In] Int[x^n,x]

[Out] $x^{(1+n)/(1+n)}$

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int x^n dx = \frac{x^{1+n}}{1+n}$$

Mathematica [A] time = 0.00, size = 11, normalized size = 1.00

$$\frac{x^{n+1}}{n+1}$$

Antiderivative was successfully verified.

[In] Integrate[x^n,x]

[Out] $x^{(1+n)/(1+n)}$

fricas [A] time = 0.42, size = 10, normalized size = 0.91

$$\frac{xx^n}{n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^n,x, algorithm="fricas")

[Out] x*x^n/(n + 1)

giac [A] time = 0.95, size = 11, normalized size = 1.00

$$\frac{x^{n+1}}{n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^n,x, algorithm="giac")

[Out] x^(n + 1)/(n + 1)

maple [A] time = 0.00, size = 12, normalized size = 1.09

$$\frac{x^{n+1}}{n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^n,x)

[Out] x^(1+n)/(1+n)

maxima [A] time = 0.64, size = 11, normalized size = 1.00

$$\frac{x^{n+1}}{n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^n,x, algorithm="maxima")

[Out] x^(n + 1)/(n + 1)

mupad [B] time = 0.35, size = 20, normalized size = 1.82

$$\begin{cases} \ln(x) & \text{if } n = -1 \\ \frac{x^{n+1}}{n+1} & \text{if } n \neq -1 \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^n,x)


```
[Out] piecewise(n == -1, log(x), n != -1, x^(n + 1)/(n + 1))
```

```
sympy [A] time = 0.06, size = 12, normalized size = 1.09
```

$$\begin{cases} \frac{x^{n+1}}{n+1} & \text{for } n \neq -1 \\ \log(x) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**n,x)
```

```
[Out] Piecewise((x**(n + 1)/(n + 1), Ne(n, -1)), (log(x), True))
```

3.35 $\int (bx)^n dx$

Optimal. Leaf size=16

$$\frac{(bx)^{n+1}}{b(n+1)}$$

[Out] $(b*x)^{(1+n)}/b/(1+n)$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {32}

$$\frac{(bx)^{n+1}}{b(n+1)}$$

Antiderivative was successfully verified.

[In] Int[(b*x)^n, x]

[Out] $(b*x)^{(1+n)}/(b*(1+n))$

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (bx)^n dx = \frac{(bx)^{1+n}}{b(1+n)}$$

Mathematica [A] time = 0.00, size = 12, normalized size = 0.75

$$\frac{x(bx)^n}{n+1}$$

Antiderivative was successfully verified.

[In] Integrate[(b*x)^n, x]

[Out] $(x*(b*x)^n)/(1+n)$

fricas [A] time = 0.41, size = 12, normalized size = 0.75

$$\frac{(bx)^n x}{n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^n,x, algorithm="fricas")

[Out] (b*x)^n*x/(n + 1)

giac [A] time = 1.04, size = 16, normalized size = 1.00

$$\frac{(bx)^{n+1}}{b(n+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^n,x, algorithm="giac")

[Out] (b*x)^(n + 1)/(b*(n + 1))

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{x(bx)^n}{n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^n,x)

[Out] x/(n+1)*(b*x)^n

maxima [A] time = 0.54, size = 16, normalized size = 1.00

$$\frac{(bx)^{n+1}}{b(n+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^n,x, algorithm="maxima")

[Out] (b*x)^(n + 1)/(b*(n + 1))

mupad [B] time = 0.18, size = 12, normalized size = 0.75

$$\frac{x(bx)^n}{n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^n,x)

[Out] $(x*(b*x)^n)/(n + 1)$

sympy [A] time = 0.06, size = 17, normalized size = 1.06

$$\frac{\begin{cases} \frac{(bx)^{n+1}}{n+1} & \text{for } n \neq -1 \\ \log(bx) & \text{otherwise} \end{cases}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x)**n,x)`

[Out] `Piecewise(((b*x)**(n + 1)/(n + 1), Ne(n, -1)), (log(b*x), True))/b`

$$3.36 \quad \int \frac{1}{\sqrt{-a} + e(c+dx)} dx$$

Optimal. Leaf size=23

$$\frac{\log(\sqrt{-a} + ce + dex)}{de}$$

[Out] $\ln(c*e+d*e*x+(-a)^{(1/2)})/d/e$

Rubi [A] time = 0.01, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {33, 31}

$$\frac{\log(\sqrt{-a} + ce + dex)}{de}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(\text{Sqrt}[-a] + e*(c + d*x))^{-1}, x]$

[Out] $\text{Log}[\text{Sqrt}[-a] + c*e + d*e*x]/(d*e)$

Rule 31

$\text{Int}[(a_. + (b_.)*(x_.))^{-1}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] \text{ /; FreeQ}[\{a, b\}, x]$

Rule 33

$\text{Int}[(a_. + (b_.)*(u_.))^{m_.}, x_Symbol] \rightarrow \text{Dist}[1/\text{Coefficient}[u, x, 1], \text{Subst}[\text{Int}[(a + b*x)^m, x], x, u], x] \text{ /; FreeQ}[\{a, b, m\}, x] \ \&\& \ \text{LinearQ}[u, x] \ \&\& \ \text{NeQ}[u, x]$

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-a} + e(c+dx)} dx &= \frac{\text{Subst}\left(\int \frac{1}{\sqrt{-a}+ex} dx, x, c+dx\right)}{d} \\ &= \frac{\log(\sqrt{-a} + ce + dex)}{de} \end{aligned}$$

Mathematica [A] time = 0.00, size = 23, normalized size = 1.00

$$\frac{\log(\sqrt{-a} + ce + dex)}{de}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[-a] + e*(c + d*x))⁽⁻¹⁾,x]

[Out] Log[Sqrt[-a] + c*e + d*e*x]/(d*e)

fricas [A] time = 0.42, size = 21, normalized size = 0.91

$$\frac{\log(dex + ce + \sqrt{-a})}{de}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(e*(d*x+c)+(-a)^(1/2)),x, algorithm="fricas")

[Out] log(d*e*x + c*e + sqrt(-a))/(d*e)

giac [A] time = 1.07, size = 22, normalized size = 0.96

$$\frac{e^{(-1)} \log(|(dx + c)e + \sqrt{-a}|)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(e*(d*x+c)+(-a)^(1/2)),x, algorithm="giac")

[Out] e⁽⁻¹⁾*log(abs((d*x + c)*e + sqrt(-a)))/d

maple [A] time = 0.00, size = 22, normalized size = 0.96

$$\frac{\ln(dex + ce + \sqrt{-a})}{de}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(e*(d*x+c)+(-a)^(1/2)),x)

[Out] ln(c*e+d*e*x+(-a)^(1/2))/d/e

maxima [A] time = 0.67, size = 21, normalized size = 0.91

$$\frac{\log((dx + c)e + \sqrt{-a})}{de}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(e*(d*x+c)+(-a)^(1/2)),x, algorithm="maxima")

[Out] $\log((d*x + c)*e + \sqrt{-a})/(d*e)$

mupad [B] time = 0.14, size = 21, normalized size = 0.91

$$\frac{\ln(\sqrt{-a} + ce + dex)}{de}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/((-a)^{(1/2)} + e*(c + d*x)), x)$

[Out] $\log((-a)^{(1/2)} + c*e + d*e*x)/(d*e)$

sympy [A] time = 0.09, size = 19, normalized size = 0.83

$$\frac{\log(ce + dex + \sqrt{-a})}{de}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(e*(d*x+c)+(-a)**(1/2)), x)$

[Out] $\log(c*e + d*e*x + \sqrt{-a})/(d*e)$

3.37 $\int (c + d(a + bx))^{5/2} dx$

Optimal. Leaf size=23

$$\frac{2(d(a + bx) + c)^{7/2}}{7bd}$$

[Out] $2/7*(c+d*(b*x+a))^(7/2)/b/d$

Rubi [A] time = 0.01, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {33, 32}

$$\frac{2(d(a + bx) + c)^{7/2}}{7bd}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*(a + b*x))^(5/2), x]$

[Out] $(2*(c + d*(a + b*x))^(7/2))/(7*b*d)$

Rule 32

$\text{Int}[(a_.) + (b_.)*(x_.))^(m_.), x_Symbol] \text{ :> Simp}[(a + b*x)^(m + 1)/(b*(m + 1)), x] \text{ /; FreeQ}\{a, b, m\}, x] \ \&\& \ \text{NeQ}\{m, -1\}$

Rule 33

$\text{Int}[(a_.) + (b_.)*(u_.))^(m_.), x_Symbol] \text{ :> Dist}[1/\text{Coefficient}[u, x, 1], \text{Subst}[\text{Int}[(a + b*x)^m, x], x, u], x] \text{ /; FreeQ}\{a, b, m\}, x] \ \&\& \ \text{LinearQ}[u, x] \ \&\& \ \text{NeQ}[u, x]$

Rubi steps

$$\begin{aligned} \int (c + d(a + bx))^{5/2} dx &= \frac{\text{Subst}\left(\int (c + dx)^{5/2} dx, x, a + bx\right)}{b} \\ &= \frac{2(c + d(a + bx))^{7/2}}{7bd} \end{aligned}$$

Mathematica [A] time = 0.02, size = 23, normalized size = 1.00

$$\frac{2(d(a + bx) + c)^{7/2}}{7bd}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*(a + b*x))^(5/2),x]

[Out] (2*(c + d*(a + b*x))^(7/2))/(7*b*d)

fricas [B] time = 0.40, size = 104, normalized size = 4.52

$$\frac{2(b^3d^3x^3 + a^3d^3 + 3a^2cd^2 + 3ac^2d + c^3 + 3(ab^2d^3 + b^2cd^2)x^2 + 3(a^2bd^3 + 2abcd^2 + bc^2d)x)\sqrt{bdx + ad + c}}{7bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d*(b*x+a))^(5/2),x, algorithm="fricas")

[Out] 2/7*(b^3*d^3*x^3 + a^3*d^3 + 3*a^2*c*d^2 + 3*a*c^2*d + c^3 + 3*(a*b^2*d^3 + b^2*c*d^2)*x^2 + 3*(a^2*b*d^3 + 2*a*b*c*d^2 + b*c^2*d)*x)*sqrt(b*d*x + a*d + c)/(b*d)

giac [B] time = 1.64, size = 444, normalized size = 19.30

$$\frac{2\left(35(bdx + ad + c)^{\frac{3}{2}}a^2d^2 - 35\left(3\sqrt{bdx + ad + c}ad - (bdx + ad + c)^{\frac{3}{2}} + 3\sqrt{bdx + ad + c}c\right)a^2d^2 - 21(bdx + ad + c)\sqrt{bdx + ad + c}\right)}{7bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d*(b*x+a))^(5/2),x, algorithm="giac")

[Out] 2/35*(35*(b*d*x + a*d + c)^(3/2)*a^2*d^2 - 35*(3*sqrt(b*d*x + a*d + c)*a*d - (b*d*x + a*d + c)^(3/2) + 3*sqrt(b*d*x + a*d + c)*c)*a^2*d^2 - 21*(b*d*x + a*d + c)^(5/2)*a*d + 70*(b*d*x + a*d + c)^(3/2)*a*c*d - 70*(3*sqrt(b*d*x + a*d + c)*a*d - (b*d*x + a*d + c)^(3/2) + 3*sqrt(b*d*x + a*d + c)*c)*a*c*d + 5*(b*d*x + a*d + c)^(7/2) - 21*(b*d*x + a*d + c)^(5/2)*c + 35*(b*d*x + a*d + c)^(3/2)*c^2 - 35*(3*sqrt(b*d*x + a*d + c)*a*d - (b*d*x + a*d + c)^(3/2) + 3*sqrt(b*d*x + a*d + c)*c)*c^2 + 7*(15*sqrt(b*d*x + a*d + c)*a^2*d^2 - 10*(b*d*x + a*d + c)^(3/2)*a*d + 30*sqrt(b*d*x + a*d + c)*a*c*d + 3*(b*d*x + a*d + c)^(5/2) - 10*(b*d*x + a*d + c)^(3/2)*c + 15*sqrt(b*d*x + a*d + c)*c^2)*a*d + 7*(15*sqrt(b*d*x + a*d + c)*a^2*d^2 - 10*(b*d*x + a*d + c)^(3/2)*a*d + 30*sqrt(b*d*x + a*d + c)*a*c*d + 3*(b*d*x + a*d + c)^(5/2) - 10*(b*d*x + a*d + c)^(3/2)*c + 15*sqrt(b*d*x + a*d + c)*c^2)*c)/(b*d)

maple [A] time = 0.00, size = 20, normalized size = 0.87

$$\frac{2(bdx + ad + c)^{\frac{7}{2}}}{7bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c+d*(b*x+a))^(5/2),x)`

[Out] $2/7*(b*d*x+a*d+c)^(7/2)/d/b$

maxima [A] time = 0.56, size = 19, normalized size = 0.83

$$\frac{2((bx+a)d+c)^{\frac{7}{2}}}{7bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c+d*(b*x+a))^(5/2),x, algorithm="maxima")`

[Out] $2/7*((b*x+a)*d+c)^(7/2)/(b*d)$

mupad [B] time = 0.18, size = 93, normalized size = 4.04

$$\frac{6x\sqrt{c+d(a+bx)}(c+ad)^2}{7} + \frac{2\sqrt{c+d(a+bx)}(c+ad)^3}{7bd} + \frac{2b^2d^2x^3\sqrt{c+d(a+bx)}}{7} + \frac{6bdx^2\sqrt{c+d(a+bx)}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c+d*(a+b*x))^(5/2),x)`

[Out] $(6*x*(c+d*(a+b*x))^(1/2)*(c+a*d)^2)/7 + (2*(c+d*(a+b*x))^(1/2)*(c+a*d)^3)/(7*b*d) + (2*b^2*d^2*x^3*(c+d*(a+b*x))^(1/2))/7 + (6*b*d*x^2*(c+d*(a+b*x))^(1/2)*(c+a*d))/7$

sympy [A] time = 71.80, size = 270, normalized size = 11.74

$$\left\{ \begin{array}{l} c^{\frac{5}{2}}x \\ x(ad+c)^{\frac{5}{2}} \\ c^{\frac{5}{2}}x \\ \frac{2a^3d^2\sqrt{ad+bdx+c}}{7b} + \frac{6a^2d^2x\sqrt{ad+bdx+c}}{7} + \frac{6a^2cd\sqrt{ad+bdx+c}}{7b} + \frac{6abd^2x^2\sqrt{ad+bdx+c}}{7} + \frac{12acdx\sqrt{ad+bdx+c}}{7} + \frac{6ac^2\sqrt{ad+bdx+c}}{7b} + \frac{2b^2d^2x^3}{7} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c+d*(b*x+a))**(5/2),x)`

[Out] `Piecewise((c**(5/2)*x, Eq(b, 0) & Eq(d, 0)), (x*(a*d + c)**(5/2), Eq(b, 0)), (c**(5/2)*x, Eq(d, 0)), (2*a**3*d**2*sqrt(a*d + b*d*x + c)/(7*b) + 6*a**2*d**2*x*sqrt(a*d + b*d*x + c)/7 + 6*a**2*c*d*sqrt(a*d + b*d*x + c)/(7*b) + 6*a*b*d**2*x**2*sqrt(a*d + b*d*x + c)/7 + 12*a*c*d*x*sqrt(a*d + b*d*x + c)/7 + 6*a*c**2*sqrt(a*d + b*d*x + c)/(7*b) + 2*b**2*d**2*x**3*sqrt(a*d + b*d*x + c)/7 + 6*b*c*d*x**2*sqrt(a*d + b*d*x + c)/7 + 6*c**2*x*sqrt(a*d + b*d*x + c)/7 + 2*c**3*sqrt(a*d + b*d*x + c)/(7*b*d), True))`

3.38 $\int (c + d(a + bx))^{3/2} dx$

Optimal. Leaf size=23

$$\frac{2(d(a + bx) + c)^{5/2}}{5bd}$$

[Out] $2/5*(c+d*(b*x+a))^(5/2)/b/d$

Rubi [A] time = 0.01, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {33, 32}

$$\frac{2(d(a + bx) + c)^{5/2}}{5bd}$$

Antiderivative was successfully verified.

[In] Int[(c + d*(a + b*x))^(3/2), x]

[Out] (2*(c + d*(a + b*x))^(5/2))/(5*b*d)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rule 33

Int[((a_.) + (b_.)*(u_))^(m_), x_Symbol] :> Dist[1/Coefficient[u, x, 1], Subst[Int[(a + b*x)^m, x], x, u], x] /; FreeQ[{a, b, m}, x] && LinearQ[u, x] && NeQ[u, x]

Rubi steps

$$\begin{aligned} \int (c + d(a + bx))^{3/2} dx &= \frac{\text{Subst}\left(\int (c + dx)^{3/2} dx, x, a + bx\right)}{b} \\ &= \frac{2(c + d(a + bx))^{5/2}}{5bd} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 1.00

$$\frac{2(d(a + bx) + c)^{5/2}}{5bd}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*(a + b*x))^(3/2), x]

[Out] (2*(c + d*(a + b*x))^(5/2))/(5*b*d)

fricas [B] time = 0.39, size = 59, normalized size = 2.57

$$\frac{2(b^2d^2x^2 + a^2d^2 + 2acd + c^2 + 2(abd^2 + bcd)x)\sqrt{bdx + ad + c}}{5bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d*(b*x+a))^(3/2), x, algorithm="fricas")

[Out] 2/5*(b^2*d^2*x^2 + a^2*d^2 + 2*a*c*d + c^2 + 2*(a*b*d^2 + b*c*d)*x)*sqrt(b*d*x + a*d + c)/(b*d)

giac [B] time = 1.04, size = 195, normalized size = 8.48

$$\frac{2\left(30\sqrt{bdx + ad + c}a^2d^2 - 10(bdx + ad + c)^{\frac{3}{2}}ad + 60\sqrt{bdx + ad + c}acd - 10\left(3\sqrt{bdx + ad + c}ad - (bdx + ad + c)\right)\right)}{5bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d*(b*x+a))^(3/2), x, algorithm="giac")

[Out] 2/15*(30*sqrt(b*d*x + a*d + c)*a^2*d^2 - 10*(b*d*x + a*d + c)^(3/2)*a*d + 60*sqrt(b*d*x + a*d + c)*a*c*d - 10*(3*sqrt(b*d*x + a*d + c)*a*d - (b*d*x + a*d + c)^(3/2) + 3*sqrt(b*d*x + a*d + c)*c)*a*d + 3*(b*d*x + a*d + c)^(5/2) - 10*(b*d*x + a*d + c)^(3/2)*c + 30*sqrt(b*d*x + a*d + c)*c^2 - 10*(3*sqrt(b*d*x + a*d + c)*a*d - (b*d*x + a*d + c)^(3/2) + 3*sqrt(b*d*x + a*d + c)*c)*c)/(b*d)

maple [A] time = 0.00, size = 20, normalized size = 0.87

$$\frac{2(bdx + ad + c)^{\frac{5}{2}}}{5bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c+d*(b*x+a))^(3/2), x)

[Out] 2/5*(b*d*x+a*d+c)^(5/2)/d/b

maxima [A] time = 0.88, size = 19, normalized size = 0.83

$$\frac{2((bx + a)d + c)^{\frac{5}{2}}}{5bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d*(b*x+a))^(3/2),x, algorithm="maxima")

[Out] $2/5*((b*x + a)*d + c)^{(5/2)}/(b*d)$

mupad [B] time = 0.17, size = 45, normalized size = 1.96

$$\sqrt{c+d(a+bx)} \left(x \left(\frac{4c}{5} + \frac{4ad}{5} \right) + \frac{2(c+ad)^2}{5bd} + \frac{2bdx^2}{5} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*(a + b*x))^(3/2),x)

[Out] $(c + d*(a + b*x))^{(1/2)}*(x*((4*c)/5 + (4*a*d)/5) + (2*(c + a*d)^2)/(5*b*d) + (2*b*d*x^2)/5)$

sympy [A] time = 5.27, size = 156, normalized size = 6.78

$$\begin{cases} c^{\frac{3}{2}}x & \text{for } b = 0 \wedge d = 0 \\ x(ad + c)^{\frac{3}{2}} & \text{for } b = 0 \\ c^{\frac{3}{2}}x & \text{for } d = 0 \\ \frac{2a^2d\sqrt{ad+bdx+c}}{5b} + \frac{4adx\sqrt{ad+bdx+c}}{5} + \frac{4ac\sqrt{ad+bdx+c}}{5b} + \frac{2bdx^2\sqrt{ad+bdx+c}}{5} + \frac{4cx\sqrt{ad+bdx+c}}{5} + \frac{2c^2\sqrt{ad+bdx+c}}{5bd} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d*(b*x+a))**(3/2),x)

[Out] Piecewise((c**(3/2)*x, Eq(b, 0) & Eq(d, 0)), (x*(a*d + c)**(3/2), Eq(b, 0)), (c**(3/2)*x, Eq(d, 0)), (2*a**2*d*sqrt(a*d + b*d*x + c)/(5*b) + 4*a*d*x*sqrt(a*d + b*d*x + c)/5 + 4*a*c*sqrt(a*d + b*d*x + c)/(5*b) + 2*b*d*x**2*sqrt(a*d + b*d*x + c)/5 + 4*c*x*sqrt(a*d + b*d*x + c)/5 + 2*c**2*sqrt(a*d + b*d*x + c)/(5*b*d), True))

3.39 $\int \sqrt{c + d(a + bx)} dx$

Optimal. Leaf size=23

$$\frac{2(d(a + bx) + c)^{3/2}}{3bd}$$

[Out] $2/3*(c+d*(b*x+a))^(3/2)/b/d$

Rubi [A] time = 0.01, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {33, 32}

$$\frac{2(d(a + bx) + c)^{3/2}}{3bd}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[c + d*(a + b*x)],x]`

[Out] $(2*(c + d*(a + b*x))^(3/2))/(3*b*d)$

Rule 32

`Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]`

Rule 33

`Int[((a_.) + (b_.)*(u_))^(m_), x_Symbol] := Dist[1/Coefficient[u, x, 1], Subst[Int[(a + b*x)^m, x], x, u], x] /; FreeQ[{a, b, m}, x] && LinearQ[u, x] && NeQ[u, x]`

Rubi steps

$$\begin{aligned} \int \sqrt{c + d(a + bx)} dx &= \frac{\text{Subst}\left(\int \sqrt{c + dx} dx, x, a + bx\right)}{b} \\ &= \frac{2(c + d(a + bx))^{3/2}}{3bd} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 1.00

$$\frac{2(d(a + bx) + c)^{3/2}}{3bd}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*(a + b*x)],x]

[Out] $(2*(c + d*(a + b*x))^{3/2})/(3*b*d)$

fricas [A] time = 0.40, size = 19, normalized size = 0.83

$$\frac{2(bdx + ad + c)^{\frac{3}{2}}}{3bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d*(b*x+a))^(1/2),x, algorithm="fricas")

[Out] $2/3*(b*d*x + a*d + c)^{3/2}/(b*d)$

giac [A] time = 1.07, size = 19, normalized size = 0.83

$$\frac{2(bdx + ad + c)^{\frac{3}{2}}}{3bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d*(b*x+a))^(1/2),x, algorithm="giac")

[Out] $2/3*(b*d*x + a*d + c)^{3/2}/(b*d)$

maple [A] time = 0.00, size = 20, normalized size = 0.87

$$\frac{2(bdx + ad + c)^{\frac{3}{2}}}{3bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c+d*(b*x+a))^(1/2),x)

[Out] $2/3*(b*d*x+a*d+c)^{3/2}/d/b$

maxima [A] time = 0.74, size = 19, normalized size = 0.83

$$\frac{2((bx + a)d + c)^{\frac{3}{2}}}{3bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d*(b*x+a))^(1/2),x, algorithm="maxima")

[Out] $2/3*((b*x + a)*d + c)^{(3/2)}/(b*d)$

mupad [B] time = 0.08, size = 19, normalized size = 0.83

$$\frac{2(c + d(a + bx))^{3/2}}{3bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*(a + b*x))^(1/2), x)`

[Out] $(2*(c + d*(a + b*x))^{(3/2)})/(3*b*d)$

sympy [A] time = 0.44, size = 82, normalized size = 3.57

$$\left\{ \begin{array}{ll} \sqrt{c} x & \text{for } b = 0 \wedge d = 0 \\ x\sqrt{ad + c} & \text{for } b = 0 \\ \sqrt{c} x & \text{for } d = 0 \\ \frac{2a\sqrt{ad+bdx+c}}{3b} + \frac{2x\sqrt{ad+bdx+c}}{3} + \frac{2c\sqrt{ad+bdx+c}}{3bd} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c+d*(b*x+a))**(1/2), x)`

[Out] `Piecewise((sqrt(c)*x, Eq(b, 0) & Eq(d, 0)), (x*sqrt(a*d + c), Eq(b, 0)), (sqrt(c)*x, Eq(d, 0)), (2*a*sqrt(a*d + b*d*x + c)/(3*b) + 2*x*sqrt(a*d + b*d*x + c)/3 + 2*c*sqrt(a*d + b*d*x + c)/(3*b*d), True))`

$$3.40 \quad \int \frac{1}{\sqrt{c+d(a+bx)}} dx$$

Optimal. Leaf size=21

$$\frac{2\sqrt{d(a+bx)+c}}{bd}$$

[Out] 2*(c+d*(b*x+a))^(1/2)/b/d

Rubi [A] time = 0.01, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {33, 32}

$$\frac{2\sqrt{d(a+bx)+c}}{bd}$$

Antiderivative was successfully verified.

[In] Int[1/Sqrt[c + d*(a + b*x)],x]

[Out] (2*Sqrt[c + d*(a + b*x)])/(b*d)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rule 33

Int[((a_.) + (b_.)*(u_))^(m_), x_Symbol] :> Dist[1/Coefficient[u, x, 1], Subst[Int[(a + b*x)^m, x], x, u], x] /; FreeQ[{a, b, m}, x] && LinearQ[u, x] && NeQ[u, x]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{c+d(a+bx)}} dx &= \frac{\text{Subst}\left(\int \frac{1}{\sqrt{c+dx}} dx, x, a+bx\right)}{b} \\ &= \frac{2\sqrt{c+d(a+bx)}}{bd} \end{aligned}$$

Mathematica [A] time = 0.01, size = 21, normalized size = 1.00

$$\frac{2\sqrt{d(a+bx)+c}}{bd}$$

Antiderivative was successfully verified.

[In] Integrate[1/Sqrt[c + d*(a + b*x)],x]

[Out] (2*Sqrt[c + d*(a + b*x)])/(b*d)

fricas [A] time = 0.40, size = 19, normalized size = 0.90

$$\frac{2\sqrt{bdx + ad + c}}{bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c+d*(b*x+a))^(1/2),x, algorithm="fricas")

[Out] 2*sqrt(b*d*x + a*d + c)/(b*d)

giac [A] time = 1.17, size = 19, normalized size = 0.90

$$\frac{2\sqrt{bdx + ad + c}}{bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c+d*(b*x+a))^(1/2),x, algorithm="giac")

[Out] 2*sqrt(b*d*x + a*d + c)/(b*d)

maple [A] time = 0.00, size = 20, normalized size = 0.95

$$\frac{2\sqrt{bdx + ad + c}}{bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c+d*(b*x+a))^(1/2),x)

[Out] 2*(b*d*x+a*d+c)^(1/2)/d/b

maxima [A] time = 0.92, size = 19, normalized size = 0.90

$$\frac{2\sqrt{(bx + a)d + c}}{bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c+d*(b*x+a))^(1/2),x, algorithm="maxima")

[Out] 2*sqrt((b*x + a)*d + c)/(b*d)

mupad [B] time = 0.11, size = 19, normalized size = 0.90

$$\frac{2\sqrt{c+d(a+bx)}}{bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(c + d*(a + b*x))^(1/2), x)`

[Out] `(2*(c + d*(a + b*x))^(1/2))/(b*d)`

sympy [A] time = 1.78, size = 31, normalized size = 1.48

$$\begin{cases} \frac{x}{\sqrt{ad+c}} & \text{for } b = 0 \\ \frac{x}{\sqrt{c}} & \text{for } d = 0 \\ \frac{2\sqrt{c+d(a+bx)}}{bd} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(c+d*(b*x+a))**(1/2), x)`

[Out] `Piecewise((x/sqrt(a*d + c), Eq(b, 0)), (x/sqrt(c), Eq(d, 0)), (2*sqrt(c + d*(a + b*x))/(b*d), True))`

$$3.41 \quad \int \frac{1}{(c+d(a+bx))^{3/2}} dx$$

Optimal. Leaf size=21

$$-\frac{2}{bd\sqrt{d(a+bx)+c}}$$

[Out] -2/b/d/(c+d*(b*x+a))^(1/2)

Rubi [A] time = 0.01, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {33, 32}

$$-\frac{2}{bd\sqrt{d(a+bx)+c}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*(a + b*x))^(-3/2), x]

[Out] -2/(b*d*Sqrt[c + d*(a + b*x)])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rule 33

Int[((a_.) + (b_.)*(u_))^(m_), x_Symbol] := Dist[1/Coefficient[u, x, 1], Subst[Int[(a + b*x)^m, x], x, u], x] /; FreeQ[{a, b, m}, x] && LinearQ[u, x] && NeQ[u, x]

Rubi steps

$$\begin{aligned} \int \frac{1}{(c+d(a+bx))^{3/2}} dx &= \frac{\text{Subst}\left(\int \frac{1}{(c+dx)^{3/2}} dx, x, a+bx\right)}{b} \\ &= -\frac{2}{bd\sqrt{c+d(a+bx)}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 21, normalized size = 1.00

$$-\frac{2}{bd\sqrt{d(a+bx)+c}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*(a + b*x))^(-3/2),x]

[Out] -2/(b*d*Sqrt[c + d*(a + b*x)])

fricas [A] time = 0.40, size = 34, normalized size = 1.62

$$-\frac{2\sqrt{bdx + ad + c}}{b^2d^2x + abd^2 + bcd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c+d*(b*x+a))^(3/2),x, algorithm="fricas")

[Out] -2*sqrt(b*d*x + a*d + c)/(b²*d²*x + a*b*d² + b*c*d)

giac [A] time = 1.65, size = 19, normalized size = 0.90

$$-\frac{2}{\sqrt{bdx + ad + c}bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c+d*(b*x+a))^(3/2),x, algorithm="giac")

[Out] -2/(sqrt(b*d*x + a*d + c)*b*d)

maple [A] time = 0.00, size = 20, normalized size = 0.95

$$-\frac{2}{\sqrt{bdx + ad + c}bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c+d*(b*x+a))^(3/2),x)

[Out] -2/(b*d*x+a*d+c)^(1/2)/d/b

maxima [A] time = 1.00, size = 19, normalized size = 0.90

$$-\frac{2}{\sqrt{(bx + a)d + c}bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c+d*(b*x+a))^(3/2),x, algorithm="maxima")

[Out] -2/(sqrt((b*x + a)*d + c)*b*d)

mupad [B] time = 0.13, size = 19, normalized size = 0.90

$$-\frac{2}{bd\sqrt{c+dx}(a+bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(c + d*(a + b*x))^(3/2), x)`

[Out] `-2/(b*d*(c + d*(a + b*x))^(1/2))`

sympy [A] time = 1.79, size = 58, normalized size = 2.76

$$\left\{ \begin{array}{ll} \frac{x}{c^2} & \text{for } b = 0 \wedge d = 0 \\ \frac{x}{(ad+c)^2} & \text{for } b = 0 \\ \frac{x}{c^2} & \text{for } d = 0 \\ -\frac{2\sqrt{ad+bdx+c}}{abd^2+b^2d^2x+bcd} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(c+d*(b*x+a))**(3/2), x)`

[Out] `Piecewise((x/c**(3/2), Eq(b, 0) & Eq(d, 0)), (x/(a*d + c)**(3/2), Eq(b, 0)), (x/c**(3/2), Eq(d, 0)), (-2*sqrt(a*d + b*d*x + c)/(a*b*d**2 + b**2*d**2*x + b*c*d), True))`

$$3.42 \quad \int \frac{1}{(c+d(a+bx))^{5/2}} dx$$

Optimal. Leaf size=23

$$-\frac{2}{3bd(d(a+bx)+c)^{3/2}}$$

[Out] -2/3/b/d/(c+d*(b*x+a))^(3/2)

Rubi [A] time = 0.01, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {33, 32}

$$-\frac{2}{3bd(d(a+bx)+c)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*(a + b*x))^(5/2), x]

[Out] -2/(3*b*d*(c + d*(a + b*x))^(3/2))

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rule 33

Int[((a_.) + (b_.)*(u_))^(m_), x_Symbol] :> Dist[1/Coefficient[u, x, 1], Subst[Int[(a + b*x)^m, x], x, u], x] /; FreeQ[{a, b, m}, x] && LinearQ[u, x] && NeQ[u, x]

Rubi steps

$$\begin{aligned} \int \frac{1}{(c+d(a+bx))^{5/2}} dx &= \frac{\text{Subst}\left(\int \frac{1}{(c+dx)^{5/2}} dx, x, a+bx\right)}{b} \\ &= -\frac{2}{3bd(c+d(a+bx))^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 1.00

$$-\frac{2}{3bd(d(a+bx)+c)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*(a + b*x))^(-5/2), x]

[Out] -2/(3*b*d*(c + d*(a + b*x))^(3/2))

fricas [B] time = 0.40, size = 68, normalized size = 2.96

$$-\frac{2\sqrt{bdx + ad + c}}{3(b^3d^3x^2 + a^2bd^3 + 2abcd^2 + bc^2d + 2(ab^2d^3 + b^2cd^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c+d*(b*x+a))^(5/2), x, algorithm="fricas")

[Out] -2/3*sqrt(b*d*x + a*d + c)/(b³*d³*x² + a²*b*d³ + 2*a*b*c*d² + b*c²*d + 2*(a*b²*d³ + b²*c*d²)*x)

giac [A] time = 1.32, size = 19, normalized size = 0.83

$$-\frac{2}{3(bdx + ad + c)^{\frac{3}{2}}bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c+d*(b*x+a))^(5/2), x, algorithm="giac")

[Out] -2/3/((b*d*x + a*d + c)^(3/2)*b*d)

maple [A] time = 0.00, size = 20, normalized size = 0.87

$$-\frac{2}{3(bdx + ad + c)^{\frac{3}{2}}bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c+d*(b*x+a))^(5/2), x)

[Out] -2/3/(b*d*x+a*d+c)^(3/2)/d/b

maxima [A] time = 0.85, size = 19, normalized size = 0.83

$$-\frac{2}{3((bx + a)d + c)^{\frac{3}{2}}bd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c+d*(b*x+a))^(5/2),x, algorithm="maxima")

[Out] -2/3/(((b*x + a)*d + c)^(3/2)*b*d)

mupad [B] time = 0.18, size = 19, normalized size = 0.83

$$-\frac{2}{3bd(c+d(ax+b))^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c + d*(a + b*x))^(5/2),x)

[Out] -2/(3*b*d*(c + d*(a + b*x))^(3/2))

sympy [A] time = 6.79, size = 102, normalized size = 4.43

$$\left\{ \begin{array}{ll} \frac{x}{c^{\frac{5}{2}}} & \text{for } b = 0 \wedge d = 0 \\ \frac{x}{(ad+c)^{\frac{5}{2}}} & \text{for } b = 0 \\ \frac{x}{c^{\frac{5}{2}}} & \text{for } d = 0 \\ -\frac{2\sqrt{ad+bdx+c}}{3a^2bd^3+6ab^2d^3x+6abcd^2+3b^3d^3x^2+6b^2cd^2x+3bc^2d} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c+d*(b*x+a))**(5/2),x)

[Out] Piecewise((x/c**(5/2), Eq(b, 0) & Eq(d, 0)), (x/(a*d + c)**(5/2), Eq(b, 0)), (x/c**(5/2), Eq(d, 0)), (-2*sqrt(a*d + b*d*x + c)/(3*a**2*b*d**3 + 6*a*b**2*d**3*x + 6*a*b*c*d**2 + 3*b**3*d**3*x**2 + 6*b**2*c*d**2*x + 3*b*c**2*d), True))

3.43 $\int x^3(a + bx) dx$

Optimal. Leaf size=17

$$\frac{ax^4}{4} + \frac{bx^5}{5}$$

[Out] 1/4*a*x^4+1/5*b*x^5

Rubi [A] time = 0.01, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{ax^4}{4} + \frac{bx^5}{5}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x), x]

[Out] (a*x^4)/4 + (b*x^5)/5

Rule 43

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int
[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n},
x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && Le
Q[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])
```

Rubi steps

$$\begin{aligned} \int x^3(a + bx) dx &= \int (ax^3 + bx^4) dx \\ &= \frac{ax^4}{4} + \frac{bx^5}{5} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{ax^4}{4} + \frac{bx^5}{5}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x), x]

[Out] (a*x^4)/4 + (b*x^5)/5

fricas [A] time = 0.33, size = 13, normalized size = 0.76

$$\frac{1}{5}x^5b + \frac{1}{4}x^4a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a),x, algorithm="fricas")

[Out] 1/5*x^5*b + 1/4*x^4*a

giac [A] time = 1.22, size = 13, normalized size = 0.76

$$\frac{1}{5}bx^5 + \frac{1}{4}ax^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a),x, algorithm="giac")

[Out] 1/5*b*x^5 + 1/4*a*x^4

maple [A] time = 0.00, size = 14, normalized size = 0.82

$$\frac{1}{5}bx^5 + \frac{1}{4}ax^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a),x)

[Out] 1/4*a*x^4+1/5*b*x^5

maxima [A] time = 0.89, size = 13, normalized size = 0.76

$$\frac{1}{5}bx^5 + \frac{1}{4}ax^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a),x, algorithm="maxima")

[Out] 1/5*b*x^5 + 1/4*a*x^4

mupad [B] time = 0.02, size = 13, normalized size = 0.76

$$\frac{x^4 (5a + 4bx)}{20}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*(a + b*x),x)
```

```
[Out] (x^4*(5*a + 4*b*x))/20
```

sympy [A] time = 0.06, size = 12, normalized size = 0.71

$$\frac{ax^4}{4} + \frac{bx^5}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*(b*x+a),x)
```

```
[Out] a*x**4/4 + b*x**5/5
```

3.44 $\int x^2(a + bx) dx$

Optimal. Leaf size=17

$$\frac{ax^3}{3} + \frac{bx^4}{4}$$

[Out] 1/3*x^3*a+1/4*b*x^4

Rubi [A] time = 0.01, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{ax^3}{3} + \frac{bx^4}{4}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*x), x]

[Out] (a*x^3)/3 + (b*x^4)/4

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2(a + bx) dx &= \int (ax^2 + bx^3) dx \\ &= \frac{ax^3}{3} + \frac{bx^4}{4} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{ax^3}{3} + \frac{bx^4}{4}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x), x]

[Out] (a*x^3)/3 + (b*x^4)/4

fricas [A] time = 0.35, size = 13, normalized size = 0.76

$$\frac{1}{4}x^4b + \frac{1}{3}x^3a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a),x, algorithm="fricas")

[Out] 1/4*x^4*b + 1/3*x^3*a

giac [A] time = 1.74, size = 13, normalized size = 0.76

$$\frac{1}{4}bx^4 + \frac{1}{3}ax^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a),x, algorithm="giac")

[Out] 1/4*b*x^4 + 1/3*a*x^3

maple [A] time = 0.00, size = 14, normalized size = 0.82

$$\frac{1}{4}bx^4 + \frac{1}{3}ax^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a),x)

[Out] 1/3*a*x^3+1/4*b*x^4

maxima [A] time = 0.86, size = 13, normalized size = 0.76

$$\frac{1}{4}bx^4 + \frac{1}{3}ax^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a),x, algorithm="maxima")

[Out] 1/4*b*x^4 + 1/3*a*x^3

mupad [B] time = 0.02, size = 13, normalized size = 0.76

$$\frac{x^3 (4a + 3bx)}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*(a + b*x),x)
```

```
[Out] (x^3*(4*a + 3*b*x))/12
```

```
sympy [A] time = 0.06, size = 12, normalized size = 0.71
```

$$\frac{ax^3}{3} + \frac{bx^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*(b*x+a),x)
```

```
[Out] a*x**3/3 + b*x**4/4
```

3.45 $\int x(a + bx) dx$

Optimal. Leaf size=17

$$\frac{ax^2}{2} + \frac{bx^3}{3}$$

[Out] 1/2*a*x^2+1/3*b*x^3

Rubi [A] time = 0.01, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {43}

$$\frac{ax^2}{2} + \frac{bx^3}{3}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x), x]

[Out] (a*x^2)/2 + (b*x^3)/3

Rule 43

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int
[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n},
x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && ( !IntegerQ[n] || (EqQ[c, 0] && Le
Q[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])
```

Rubi steps

$$\begin{aligned} \int x(a + bx) dx &= \int (ax + bx^2) dx \\ &= \frac{ax^2}{2} + \frac{bx^3}{3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{ax^2}{2} + \frac{bx^3}{3}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x), x]

[Out] (a*x^2)/2 + (b*x^3)/3

fricas [A] time = 0.33, size = 13, normalized size = 0.76

$$\frac{1}{3}x^3b + \frac{1}{2}x^2a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a),x, algorithm="fricas")

[Out] 1/3*x^3*b + 1/2*x^2*a

giac [A] time = 1.17, size = 13, normalized size = 0.76

$$\frac{1}{3}bx^3 + \frac{1}{2}ax^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a),x, algorithm="giac")

[Out] 1/3*b*x^3 + 1/2*a*x^2

maple [A] time = 0.00, size = 14, normalized size = 0.82

$$\frac{1}{3}bx^3 + \frac{1}{2}ax^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a),x)

[Out] 1/2*a*x^2+1/3*b*x^3

maxima [A] time = 0.83, size = 13, normalized size = 0.76

$$\frac{1}{3}bx^3 + \frac{1}{2}ax^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a),x, algorithm="maxima")

[Out] 1/3*b*x^3 + 1/2*a*x^2

mupad [B] time = 0.02, size = 13, normalized size = 0.76

$$\frac{x^2 (3a + 2bx)}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*(a + b*x),x)
```

```
[Out] (x^2*(3*a + 2*b*x))/6
```

sympy [A] time = 0.06, size = 12, normalized size = 0.71

$$\frac{ax^2}{2} + \frac{bx^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*(b*x+a),x)
```

```
[Out] a*x**2/2 + b*x**3/3
```

3.46 $\int(a + bx) dx$

Optimal. Leaf size=12

$$ax + \frac{bx^2}{2}$$

[Out] a*x+1/2*b*x^2

Rubi [A] time = 0.00, antiderivative size = 12, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$ax + \frac{bx^2}{2}$$

Antiderivative was successfully verified.

[In] Int[a + b*x,x]

[Out] a*x + (b*x^2)/2

Rubi steps

$$\int(a + bx) dx = ax + \frac{bx^2}{2}$$

Mathematica [A] time = 0.00, size = 12, normalized size = 1.00

$$ax + \frac{bx^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[a + b*x,x]

[Out] a*x + (b*x^2)/2

fricas [A] time = 0.36, size = 10, normalized size = 0.83

$$\frac{1}{2}x^2b + xa$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(b*x+a,x, algorithm="fricas")

[Out] $\frac{1}{2}x^2b + xa$

giac [A] time = 1.25, size = 10, normalized size = 0.83

$$\frac{1}{2}bx^2 + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(b*x+a,x, algorithm="giac")`

[Out] $\frac{1}{2}b*x^2 + a*x$

maple [A] time = 0.00, size = 11, normalized size = 0.92

$$\frac{1}{2}bx^2 + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(b*x+a,x)`

[Out] $a*x + \frac{1}{2}b*x^2$

maxima [A] time = 0.89, size = 10, normalized size = 0.83

$$\frac{1}{2}bx^2 + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(b*x+a,x, algorithm="maxima")`

[Out] $\frac{1}{2}b*x^2 + a*x$

mupad [B] time = 0.02, size = 10, normalized size = 0.83

$$\frac{bx^2}{2} + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(a + b*x,x)`

[Out] $a*x + (b*x^2)/2$

sympy [A] time = 0.06, size = 8, normalized size = 0.67

$$ax + \frac{bx^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(b*x+a,x)
```

```
[Out] a*x + b*x**2/2
```

$$3.47 \quad \int \frac{a+bx}{x} dx$$

Optimal. Leaf size=8

$$a \log(x) + bx$$

[Out] b*x+a*ln(x)

Rubi [A] time = 0.00, antiderivative size = 8, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$a \log(x) + bx$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x,x]

[Out] b*x + a*Log[x]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x} dx &= \int \left(b + \frac{a}{x} \right) dx \\ &= bx + a \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 8, normalized size = 1.00

$$a \log(x) + bx$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x,x]

[Out] b*x + a*Log[x]

fricas [A] time = 0.39, size = 8, normalized size = 1.00

$$bx + a \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x,x, algorithm="fricas")

[Out] b*x + a*log(x)

giac [A] time = 1.06, size = 9, normalized size = 1.12

$$bx + a \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x,x, algorithm="giac")

[Out] b*x + a*log(abs(x))

maple [A] time = 0.01, size = 9, normalized size = 1.12

$$a \ln(x) + bx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x,x)

[Out] b*x+a*ln(x)

maxima [A] time = 0.84, size = 8, normalized size = 1.00

$$bx + a \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x,x, algorithm="maxima")

[Out] b*x + a*log(x)

mupad [B] time = 0.02, size = 8, normalized size = 1.00

$$bx + a \ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/x,x)

[Out] b*x + a*log(x)

sympy [A] time = 0.09, size = 7, normalized size = 0.88

$$a \log(x) + bx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x,x)
```

```
[Out] a*log(x) + b*x
```


$$3.48 \quad \int \frac{a+bx}{x^2} dx$$

Optimal. Leaf size=11

$$b \log(x) - \frac{a}{x}$$

[Out] -a/x+b*ln(x)

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$b \log(x) - \frac{a}{x}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x^2, x]

[Out] -(a/x) + b*Log[x]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^2} dx &= \int \left(\frac{a}{x^2} + \frac{b}{x} \right) dx \\ &= -\frac{a}{x} + b \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 11, normalized size = 1.00

$$b \log(x) - \frac{a}{x}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x^2, x]

[Out] -(a/x) + b*Log[x]

fricas [A] time = 0.38, size = 13, normalized size = 1.18

$$\frac{bx \log(x) - a}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^2,x, algorithm="fricas")

[Out] (b*x*log(x) - a)/x

giac [A] time = 1.05, size = 12, normalized size = 1.09

$$b \log(|x|) - \frac{a}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^2,x, algorithm="giac")

[Out] b*log(abs(x)) - a/x

maple [A] time = 0.02, size = 12, normalized size = 1.09

$$b \ln(x) - \frac{a}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^2,x)

[Out] -a/x+b*ln(x)

maxima [A] time = 0.87, size = 11, normalized size = 1.00

$$b \log(x) - \frac{a}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^2,x, algorithm="maxima")

[Out] b*log(x) - a/x

mupad [B] time = 0.03, size = 11, normalized size = 1.00

$$b \ln(x) - \frac{a}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^2,x)
```

```
[Out] b*log(x) - a/x
```

```
sympy [A] time = 0.11, size = 7, normalized size = 0.64
```

$$-\frac{a}{x} + b \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**2,x)
```

```
[Out] -a/x + b*log(x)
```

$$3.49 \quad \int \frac{a+bx}{x^3} dx$$

Optimal. Leaf size=17

$$-\frac{(a+bx)^2}{2ax^2}$$

[Out] $-1/2*(b*x+a)^2/a/x^2$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {37}

$$-\frac{(a+bx)^2}{2ax^2}$$

Antiderivative was successfully verified.

[In] `Int[(a + b*x)/x^3,x]`

[Out] $-(a + b*x)^2/(2*a*x^2)$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp
[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
1]
```

Rubi steps

$$\int \frac{a+bx}{x^3} dx = -\frac{(a+bx)^2}{2ax^2}$$

Mathematica [A] time = 0.00, size = 15, normalized size = 0.88

$$-\frac{a}{2x^2} - \frac{b}{x}$$

Antiderivative was successfully verified.

[In] `Integrate[(a + b*x)/x^3,x]`

[Out] $-1/2*a/x^2 - b/x$

fricas [A] time = 0.37, size = 11, normalized size = 0.65

$$-\frac{2bx+a}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3,x, algorithm="fricas")

[Out] -1/2*(2*b*x + a)/x^2

giac [A] time = 1.22, size = 11, normalized size = 0.65

$$-\frac{2bx+a}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3,x, algorithm="giac")

[Out] -1/2*(2*b*x + a)/x^2

maple [A] time = 0.00, size = 14, normalized size = 0.82

$$-\frac{b}{x} - \frac{a}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^3,x)

[Out] -b/x-1/2*a/x^2

maxima [A] time = 1.12, size = 11, normalized size = 0.65

$$-\frac{2bx+a}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3,x, algorithm="maxima")

[Out] -1/2*(2*b*x + a)/x^2

mupad [B] time = 0.02, size = 11, normalized size = 0.65

$$-\frac{a+2bx}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^3,x)
```

```
[Out] -(a + 2*b*x)/(2*x^2)
```

sympy [A] time = 0.11, size = 12, normalized size = 0.71

$$\frac{-a - 2bx}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**3,x)
```

```
[Out] (-a - 2*b*x)/(2*x**2)
```

$$3.50 \quad \int \frac{a+bx}{x^4} dx$$

Optimal. Leaf size=17

$$-\frac{a}{3x^3} - \frac{b}{2x^2}$$

[Out] $-1/3*a/x^3-1/2*b/x^2$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$-\frac{a}{3x^3} - \frac{b}{2x^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x^4,x]

[Out] $-a/(3*x^3) - b/(2*x^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^4} dx &= \int \left(\frac{a}{x^4} + \frac{b}{x^3} \right) dx \\ &= -\frac{a}{3x^3} - \frac{b}{2x^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$-\frac{a}{3x^3} - \frac{b}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x^4,x]

[Out] $-1/3*a/x^3 - b/(2*x^2)$

fricas [A] time = 0.38, size = 13, normalized size = 0.76

$$-\frac{3bx + 2a}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^4,x, algorithm="fricas")

[Out] -1/6*(3*b*x + 2*a)/x^3

giac [A] time = 1.38, size = 13, normalized size = 0.76

$$-\frac{3bx + 2a}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^4,x, algorithm="giac")

[Out] -1/6*(3*b*x + 2*a)/x^3

maple [A] time = 0.00, size = 14, normalized size = 0.82

$$-\frac{b}{2x^2} - \frac{a}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^4,x)

[Out] -1/3*a/x^3-1/2*b/x^2

maxima [A] time = 1.10, size = 13, normalized size = 0.76

$$-\frac{3bx + 2a}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^4,x, algorithm="maxima")

[Out] -1/6*(3*b*x + 2*a)/x^3

mupad [B] time = 0.03, size = 13, normalized size = 0.76

$$-\frac{2a + 3bx}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^4,x)
```

```
[Out] -(2*a + 3*b*x)/(6*x^3)
```

```
sympy [A] time = 0.13, size = 14, normalized size = 0.82
```

$$\frac{-2a - 3bx}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**4,x)
```

```
[Out] (-2*a - 3*b*x)/(6*x**3)
```

$$3.51 \quad \int \frac{a+bx}{x^5} dx$$

Optimal. Leaf size=17

$$-\frac{a}{4x^4} - \frac{b}{3x^3}$$

[Out] $-1/4*a/x^4-1/3*b/x^3$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$-\frac{a}{4x^4} - \frac{b}{3x^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x^5, x]

[Out] $-a/(4*x^4) - b/(3*x^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^5} dx &= \int \left(\frac{a}{x^5} + \frac{b}{x^4} \right) dx \\ &= -\frac{a}{4x^4} - \frac{b}{3x^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$-\frac{a}{4x^4} - \frac{b}{3x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x^5, x]

[Out] $-1/4*a/x^4 - b/(3*x^3)$

fricas [A] time = 0.38, size = 13, normalized size = 0.76

$$-\frac{4bx + 3a}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^5,x, algorithm="fricas")

[Out] -1/12*(4*b*x + 3*a)/x^4

giac [A] time = 1.68, size = 13, normalized size = 0.76

$$-\frac{4bx + 3a}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^5,x, algorithm="giac")

[Out] -1/12*(4*b*x + 3*a)/x^4

maple [A] time = 0.01, size = 14, normalized size = 0.82

$$-\frac{b}{3x^3} - \frac{a}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^5,x)

[Out] -1/4*a/x^4-1/3*b/x^3

maxima [A] time = 1.05, size = 13, normalized size = 0.76

$$-\frac{4bx + 3a}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^5,x, algorithm="maxima")

[Out] -1/12*(4*b*x + 3*a)/x^4

mupad [B] time = 0.03, size = 13, normalized size = 0.76

$$-\frac{3a + 4bx}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^5,x)
```

```
[Out] -(3*a + 4*b*x)/(12*x^4)
```

sympy [A] time = 0.16, size = 14, normalized size = 0.82

$$\frac{-3a - 4bx}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**5,x)
```

```
[Out] (-3*a - 4*b*x)/(12*x**4)
```

3.52 $\int x^3(a + bx)^2 dx$

Optimal. Leaf size=30

$$\frac{a^2x^4}{4} + \frac{2}{5}abx^5 + \frac{b^2x^6}{6}$$

[Out] $1/4*a^2*x^4+2/5*a*b*x^5+1/6*b^2*x^6$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2x^4}{4} + \frac{2}{5}abx^5 + \frac{b^2x^6}{6}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*(a + b*x)^2, x]$

[Out] $(a^2*x^4)/4 + (2*a*b*x^5)/5 + (b^2*x^6)/6$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^2 dx &= \int (a^2x^3 + 2abx^4 + b^2x^5) dx \\ &= \frac{a^2x^4}{4} + \frac{2}{5}abx^5 + \frac{b^2x^6}{6} \end{aligned}$$

Mathematica [A] time = 0.00, size = 30, normalized size = 1.00

$$\frac{a^2x^4}{4} + \frac{2}{5}abx^5 + \frac{b^2x^6}{6}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^3*(a + b*x)^2, x]$

[Out] $(a^2*x^4)/4 + (2*a*b*x^5)/5 + (b^2*x^6)/6$

fricas [A] time = 0.35, size = 24, normalized size = 0.80

$$\frac{1}{6}x^6b^2 + \frac{2}{5}x^5ba + \frac{1}{4}x^4a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2,x, algorithm="fricas")

[Out] 1/6*x^6*b^2 + 2/5*x^5*b*a + 1/4*x^4*a^2

giac [A] time = 1.61, size = 24, normalized size = 0.80

$$\frac{1}{6}b^2x^6 + \frac{2}{5}abx^5 + \frac{1}{4}a^2x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2,x, algorithm="giac")

[Out] 1/6*b^2*x^6 + 2/5*a*b*x^5 + 1/4*a^2*x^4

maple [A] time = 0.00, size = 25, normalized size = 0.83

$$\frac{1}{6}b^2x^6 + \frac{2}{5}abx^5 + \frac{1}{4}a^2x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^2,x)

[Out] 1/4*a^2*x^4+2/5*a*b*x^5+1/6*b^2*x^6

maxima [A] time = 1.20, size = 24, normalized size = 0.80

$$\frac{1}{6}b^2x^6 + \frac{2}{5}abx^5 + \frac{1}{4}a^2x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2,x, algorithm="maxima")

[Out] 1/6*b^2*x^6 + 2/5*a*b*x^5 + 1/4*a^2*x^4

mupad [B] time = 0.08, size = 24, normalized size = 0.80

$$\frac{a^2x^4}{4} + \frac{2abx^5}{5} + \frac{b^2x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(a + b*x)^2,x)`

[Out] $(a^2*x^4)/4 + (b^2*x^6)/6 + (2*a*b*x^5)/5$

sympy [A] time = 0.07, size = 26, normalized size = 0.87

$$\frac{a^2x^4}{4} + \frac{2abx^5}{5} + \frac{b^2x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(b*x+a)**2,x)`

[Out] $a**2*x**4/4 + 2*a*b*x**5/5 + b**2*x**6/6$

3.53 $\int x^2(a + bx)^2 dx$

Optimal. Leaf size=30

$$\frac{a^2x^3}{3} + \frac{1}{2}abx^4 + \frac{b^2x^5}{5}$$

[Out] $1/3*a^2*x^3+1/2*a*b*x^4+1/5*b^2*x^5$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2x^3}{3} + \frac{1}{2}abx^4 + \frac{b^2x^5}{5}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*(a + b*x)^2, x]$

[Out] $(a^2*x^3)/3 + (a*b*x^4)/2 + (b^2*x^5)/5$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] :> \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}[\{a, b, c, d, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0]) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^2 dx &= \int (a^2x^2 + 2abx^3 + b^2x^4) dx \\ &= \frac{a^2x^3}{3} + \frac{1}{2}abx^4 + \frac{b^2x^5}{5} \end{aligned}$$

Mathematica [A] time = 0.00, size = 30, normalized size = 1.00

$$\frac{a^2x^3}{3} + \frac{1}{2}abx^4 + \frac{b^2x^5}{5}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^2*(a + b*x)^2, x]$

[Out] $(a^2*x^3)/3 + (a*b*x^4)/2 + (b^2*x^5)/5$

fricas [A] time = 0.35, size = 24, normalized size = 0.80

$$\frac{1}{5}x^5b^2 + \frac{1}{2}x^4ba + \frac{1}{3}x^3a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2,x, algorithm="fricas")

[Out] 1/5*x^5*b^2 + 1/2*x^4*b*a + 1/3*x^3*a^2

giac [A] time = 1.02, size = 24, normalized size = 0.80

$$\frac{1}{5}b^2x^5 + \frac{1}{2}abx^4 + \frac{1}{3}a^2x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2,x, algorithm="giac")

[Out] 1/5*b^2*x^5 + 1/2*a*b*x^4 + 1/3*a^2*x^3

maple [A] time = 0.00, size = 25, normalized size = 0.83

$$\frac{1}{5}b^2x^5 + \frac{1}{2}abx^4 + \frac{1}{3}a^2x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^2,x)

[Out] 1/3*a^2*x^3+1/2*a*b*x^4+1/5*b^2*x^5

maxima [A] time = 1.05, size = 24, normalized size = 0.80

$$\frac{1}{5}b^2x^5 + \frac{1}{2}abx^4 + \frac{1}{3}a^2x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2,x, algorithm="maxima")

[Out] 1/5*b^2*x^5 + 1/2*a*b*x^4 + 1/3*a^2*x^3

mupad [B] time = 0.03, size = 24, normalized size = 0.80

$$\frac{a^2x^3}{3} + \frac{abx^4}{2} + \frac{b^2x^5}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*(a + b*x)^2,x)
```

```
[Out] (a^2*x^3)/3 + (b^2*x^5)/5 + (a*b*x^4)/2
```

sympy [A] time = 0.07, size = 24, normalized size = 0.80

$$\frac{a^2x^3}{3} + \frac{abx^4}{2} + \frac{b^2x^5}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*(b*x+a)**2,x)
```

```
[Out] a**2*x**3/3 + a*b*x**4/2 + b**2*x**5/5
```

3.54 $\int x(a + bx)^2 dx$

Optimal. Leaf size=30

$$\frac{a^2x^2}{2} + \frac{2}{3}abx^3 + \frac{b^2x^4}{4}$$

[Out] $1/2*a^2*x^2+2/3*a*b*x^3+1/4*b^2*x^4$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{a^2x^2}{2} + \frac{2}{3}abx^3 + \frac{b^2x^4}{4}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^2,x]

[Out] $(a^2*x^2)/2 + (2*a*b*x^3)/3 + (b^2*x^4)/4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x(a + bx)^2 dx &= \int (a^2x + 2abx^2 + b^2x^3) dx \\ &= \frac{a^2x^2}{2} + \frac{2}{3}abx^3 + \frac{b^2x^4}{4} \end{aligned}$$

Mathematica [A] time = 0.00, size = 30, normalized size = 1.00

$$\frac{a^2x^2}{2} + \frac{2}{3}abx^3 + \frac{b^2x^4}{4}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^2,x]

[Out] $(a^2*x^2)/2 + (2*a*b*x^3)/3 + (b^2*x^4)/4$

fricas [A] time = 0.34, size = 24, normalized size = 0.80

$$\frac{1}{4}x^4b^2 + \frac{2}{3}x^3ba + \frac{1}{2}x^2a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2,x, algorithm="fricas")

[Out] 1/4*x^4*b^2 + 2/3*x^3*b*a + 1/2*x^2*a^2

giac [A] time = 1.41, size = 24, normalized size = 0.80

$$\frac{1}{4}b^2x^4 + \frac{2}{3}abx^3 + \frac{1}{2}a^2x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2,x, algorithm="giac")

[Out] 1/4*b^2*x^4 + 2/3*a*b*x^3 + 1/2*a^2*x^2

maple [A] time = 0.00, size = 25, normalized size = 0.83

$$\frac{1}{4}b^2x^4 + \frac{2}{3}abx^3 + \frac{1}{2}a^2x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^2,x)

[Out] 1/2*a^2*x^2+2/3*a*b*x^3+1/4*b^2*x^4

maxima [A] time = 0.99, size = 24, normalized size = 0.80

$$\frac{1}{4}b^2x^4 + \frac{2}{3}abx^3 + \frac{1}{2}a^2x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2,x, algorithm="maxima")

[Out] 1/4*b^2*x^4 + 2/3*a*b*x^3 + 1/2*a^2*x^2

mupad [B] time = 0.03, size = 24, normalized size = 0.80

$$\frac{a^2x^2}{2} + \frac{2abx^3}{3} + \frac{b^2x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*(a + b*x)^2,x)
```

```
[Out] (a^2*x^2)/2 + (b^2*x^4)/4 + (2*a*b*x^3)/3
```

```
sympy [A] time = 0.07, size = 26, normalized size = 0.87
```

$$\frac{a^2x^2}{2} + \frac{2abx^3}{3} + \frac{b^2x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*(b*x+a)**2,x)
```

```
[Out] a**2*x**2/2 + 2*a*b*x**3/3 + b**2*x**4/4
```

3.55 $\int (a + bx)^2 dx$

Optimal. Leaf size=14

$$\frac{(a + bx)^3}{3b}$$

[Out] 1/3*(b*x+a)^3/b

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(a + bx)^3}{3b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2,x]

[Out] (a + b*x)^3/(3*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^2 dx = \frac{(a + bx)^3}{3b}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{(a + bx)^3}{3b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2,x]

[Out] (a + b*x)^3/(3*b)

fricas [A] time = 0.41, size = 20, normalized size = 1.43

$$\frac{1}{3}x^3b^2 + x^2ba + xa^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2,x, algorithm="fricas")

[Out] 1/3*x^3*b^2 + x^2*b*a + x*a^2

giac [A] time = 1.16, size = 12, normalized size = 0.86

$$\frac{(bx + a)^3}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2,x, algorithm="giac")

[Out] 1/3*(b*x + a)^3/b

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{(bx + a)^3}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2,x)

[Out] 1/3*(b*x+a)^3/b

maxima [A] time = 1.08, size = 20, normalized size = 1.43

$$\frac{1}{3}b^2x^3 + abx^2 + a^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2,x, algorithm="maxima")

[Out] 1/3*b^2*x^3 + a*b*x^2 + a^2*x

mupad [B] time = 0.03, size = 20, normalized size = 1.43

$$a^2x + abx^2 + \frac{b^2x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2,x)

[Out] a^2*x + (b^2*x^3)/3 + a*b*x^2

sympy [B] time = 0.07, size = 19, normalized size = 1.36

$$a^2x + abx^2 + \frac{b^2x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**2,x)
```

```
[Out] a**2*x + a*b*x**2 + b**2*x**3/3
```


$$3.56 \quad \int \frac{(a+bx)^2}{x} dx$$

Optimal. Leaf size=22

$$a^2 \log(x) + 2abx + \frac{b^2x^2}{2}$$

[Out] 2*a*b*x+1/2*b^2*x^2+a^2*ln(x)

Rubi [A] time = 0.01, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$a^2 \log(x) + 2abx + \frac{b^2x^2}{2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x, x]

[Out] 2*a*b*x + (b^2*x^2)/2 + a^2*Log[x]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x} dx &= \int \left(2ab + \frac{a^2}{x} + b^2x \right) dx \\ &= 2abx + \frac{b^2x^2}{2} + a^2 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 1.00

$$a^2 \log(x) + 2abx + \frac{b^2x^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x, x]

[Out] $2*a*b*x + (b^2*x^2)/2 + a^2*\text{Log}[x]$

fricas [A] time = 0.42, size = 20, normalized size = 0.91

$$\frac{1}{2}b^2x^2 + 2abx + a^2\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x,x, algorithm="fricas")`

[Out] $1/2*b^2*x^2 + 2*a*b*x + a^2*\log(x)$

giac [A] time = 1.35, size = 21, normalized size = 0.95

$$\frac{1}{2}b^2x^2 + 2abx + a^2\log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x,x, algorithm="giac")`

[Out] $1/2*b^2*x^2 + 2*a*b*x + a^2*\log(\text{abs}(x))$

maple [A] time = 0.00, size = 21, normalized size = 0.95

$$\frac{b^2x^2}{2} + a^2\ln(x) + 2abx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x,x)`

[Out] $2*a*b*x + 1/2*b^2*x^2 + a^2*\ln(x)$

maxima [A] time = 1.11, size = 20, normalized size = 0.91

$$\frac{1}{2}b^2x^2 + 2abx + a^2\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x,x, algorithm="maxima")`

[Out] $1/2*b^2*x^2 + 2*a*b*x + a^2*\log(x)$

mupad [B] time = 0.03, size = 20, normalized size = 0.91

$$a^2\ln(x) + \frac{b^2x^2}{2} + 2abx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x,x)`

[Out] $a^2 \log(x) + (b^2 x^2)/2 + 2*a*b*x$

sympy [A] time = 0.11, size = 20, normalized size = 0.91

$$a^2 \log(x) + 2abx + \frac{b^2 x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x,x)`

[Out] $a**2*\log(x) + 2*a*b*x + b**2*x**2/2$

$$3.57 \quad \int \frac{(a+bx)^2}{x^2} dx$$

Optimal. Leaf size=20

$$-\frac{a^2}{x} + 2ab \log(x) + b^2x$$

[Out] $-a^2/x + b^2*x + 2*a*b*\ln(x)$

Rubi [A] time = 0.01, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{x} + 2ab \log(x) + b^2x$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^2/x^2, x]$

[Out] $-(a^2/x) + b^2*x + 2*a*b*\text{Log}[x]$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^(m_.)*((c_.) + (d_.)*(x_.))^(n_.), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{IGtQ}[m, 0] \&\& (!\text{IntegerQ}[n] \|\| (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0]) \|\| \text{LtQ}[9*m + 5*(n + 1), 0] \|\| \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^2} dx &= \int \left(b^2 + \frac{a^2}{x^2} + \frac{2ab}{x} \right) dx \\ &= -\frac{a^2}{x} + b^2x + 2ab \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 20, normalized size = 1.00

$$-\frac{a^2}{x} + 2ab \log(x) + b^2x$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(a + b*x)^2/x^2, x]$

[Out] $-(a^2/x) + b^2*x + 2*a*b*\text{Log}[x]$

fricas [A] time = 0.41, size = 24, normalized size = 1.20

$$\frac{b^2x^2 + 2abx \log(x) - a^2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^2,x, algorithm="fricas")`

[Out] $(b^2*x^2 + 2*a*b*x*\log(x) - a^2)/x$

giac [A] time = 1.09, size = 21, normalized size = 1.05

$$b^2x + 2ab \log(|x|) - \frac{a^2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^2,x, algorithm="giac")`

[Out] $b^2*x + 2*a*b*\log(\text{abs}(x)) - a^2/x$

maple [A] time = 0.01, size = 21, normalized size = 1.05

$$2ab \ln(x) + b^2x - \frac{a^2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^2,x)`

[Out] $-a^2/x + b^2*x + 2*a*b*\ln(x)$

maxima [A] time = 1.10, size = 20, normalized size = 1.00

$$b^2x + 2ab \log(x) - \frac{a^2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^2,x, algorithm="maxima")`

[Out] $b^2*x + 2*a*b*\log(x) - a^2/x$

mupad [B] time = 0.07, size = 20, normalized size = 1.00

$$b^2x - \frac{a^2}{x} + 2ab \ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x^2,x)`

[Out] $b^2x - a^2/x + 2ab \log(x)$

sympy [A] time = 0.13, size = 17, normalized size = 0.85

$$-\frac{a^2}{x} + 2ab \log(x) + b^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**2,x)`

[Out] $-a^2/x + 2ab \log(x) + b^2x$

$$3.58 \quad \int \frac{(a+bx)^2}{x^3} dx$$

Optimal. Leaf size=24

$$-\frac{a^2}{2x^2} - \frac{2ab}{x} + b^2 \log(x)$$

[Out] $-1/2*a^2/x^2-2*a*b/x+b^2*\ln(x)$

Rubi [A] time = 0.01, antiderivative size = 24, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{2x^2} - \frac{2ab}{x} + b^2 \log(x)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^3,x]

[Out] $-a^2/(2*x^2) - (2*a*b)/x + b^2*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^3} dx &= \int \left(\frac{a^2}{x^3} + \frac{2ab}{x^2} + \frac{b^2}{x} \right) dx \\ &= -\frac{a^2}{2x^2} - \frac{2ab}{x} + b^2 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 1.00

$$-\frac{a^2}{2x^2} - \frac{2ab}{x} + b^2 \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^3,x]

[Out] $-1/2*a^2/x^2 - (2*a*b)/x + b^2*\text{Log}[x]$

fricas [A] time = 0.43, size = 26, normalized size = 1.08

$$\frac{2b^2x^2\log(x) - 4abx - a^2}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^3,x, algorithm="fricas")`

[Out] $1/2*(2*b^2*x^2*\log(x) - 4*a*b*x - a^2)/x^2$

giac [A] time = 1.18, size = 22, normalized size = 0.92

$$b^2 \log(|x|) - \frac{4abx + a^2}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^3,x, algorithm="giac")`

[Out] $b^2*\log(\text{abs}(x)) - 1/2*(4*a*b*x + a^2)/x^2$

maple [A] time = 0.01, size = 23, normalized size = 0.96

$$b^2 \ln(x) - \frac{2ab}{x} - \frac{a^2}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^3,x)`

[Out] $-1/2*a^2/x^2 - 2*a*b/x + b^2*\ln(x)$

maxima [A] time = 1.18, size = 21, normalized size = 0.88

$$b^2 \log(x) - \frac{4abx + a^2}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^3,x, algorithm="maxima")`

[Out] $b^2*\log(x) - 1/2*(4*a*b*x + a^2)/x^2$

mupad [B] time = 0.04, size = 23, normalized size = 0.96

$$b^2 \ln(x) - \frac{\frac{a^2}{2} + 2bxa}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^2/x^3,x)
```

```
[Out] b^2*log(x) - (a^2/2 + 2*a*b*x)/x^2
```

```
sympy [A] time = 0.17, size = 22, normalized size = 0.92
```

$$b^2 \log(x) + \frac{-a^2 - 4abx}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**2/x**3,x)
```

```
[Out] b**2*log(x) + (-a**2 - 4*a*b*x)/(2*x**2)
```

$$3.59 \quad \int \frac{(a+bx)^2}{x^4} dx$$

Optimal. Leaf size=17

$$-\frac{(a+bx)^3}{3ax^3}$$

[Out] $-1/3*(b*x+a)^3/x^3/a$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {37}

$$-\frac{(a+bx)^3}{3ax^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^4, x]

[Out] $-(a + b*x)^3/(3*a*x^3)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(a+bx)^2}{x^4} dx = -\frac{(a+bx)^3}{3ax^3}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 1.53

$$-\frac{a^2}{3x^3} - \frac{ab}{x^2} - \frac{b^2}{x}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^4, x]

[Out] $-1/3*a^2/x^3 - (a*b)/x^2 - b^2/x$

fricas [A] time = 0.44, size = 22, normalized size = 1.29

$$\frac{3b^2x^2 + 3abx + a^2}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^4,x, algorithm="fricas")

[Out] -1/3*(3*b^2*x^2 + 3*a*b*x + a^2)/x^3

giac [A] time = 1.48, size = 22, normalized size = 1.29

$$\frac{3b^2x^2 + 3abx + a^2}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^4,x, algorithm="giac")

[Out] -1/3*(3*b^2*x^2 + 3*a*b*x + a^2)/x^3

maple [A] time = 0.01, size = 25, normalized size = 1.47

$$-\frac{b^2}{x} - \frac{ab}{x^2} - \frac{a^2}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/x^4,x)

[Out] -a*b/x^2-b^2/x-1/3*a^2/x^3

maxima [A] time = 1.35, size = 22, normalized size = 1.29

$$\frac{3b^2x^2 + 3abx + a^2}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^4,x, algorithm="maxima")

[Out] -1/3*(3*b^2*x^2 + 3*a*b*x + a^2)/x^3

mupad [B] time = 0.04, size = 22, normalized size = 1.29

$$\frac{\frac{a^2}{3} + abx + b^2x^2}{x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^2/x^4,x)
```

```
[Out] -(a^2/3 + b^2*x^2 + a*b*x)/x^3
```

sympy [A] time = 0.18, size = 24, normalized size = 1.41

$$\frac{-a^2 - 3abx - 3b^2x^2}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**2/x**4,x)
```

```
[Out] (-a**2 - 3*a*b*x - 3*b**2*x**2)/(3*x**3)
```

$$3.60 \quad \int \frac{(a+bx)^2}{x^5} dx$$

Optimal. Leaf size=30

$$-\frac{a^2}{4x^4} - \frac{2ab}{3x^3} - \frac{b^2}{2x^2}$$

[Out] $-1/4*a^2/x^4-2/3*a*b/x^3-1/2*b^2/x^2$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{4x^4} - \frac{2ab}{3x^3} - \frac{b^2}{2x^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^5, x]

[Out] $-a^2/(4*x^4) - (2*a*b)/(3*x^3) - b^2/(2*x^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^5} dx &= \int \left(\frac{a^2}{x^5} + \frac{2ab}{x^4} + \frac{b^2}{x^3} \right) dx \\ &= -\frac{a^2}{4x^4} - \frac{2ab}{3x^3} - \frac{b^2}{2x^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 30, normalized size = 1.00

$$-\frac{a^2}{4x^4} - \frac{2ab}{3x^3} - \frac{b^2}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^5, x]

[Out] $-1/4*a^2/x^4 - (2*a*b)/(3*x^3) - b^2/(2*x^2)$

fricas [A] time = 0.45, size = 24, normalized size = 0.80

$$\frac{6b^2x^2 + 8abx + 3a^2}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^5,x, algorithm="fricas")`

[Out] $-1/12*(6*b^2*x^2 + 8*a*b*x + 3*a^2)/x^4$

giac [A] time = 1.12, size = 24, normalized size = 0.80

$$\frac{6b^2x^2 + 8abx + 3a^2}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^5,x, algorithm="giac")`

[Out] $-1/12*(6*b^2*x^2 + 8*a*b*x + 3*a^2)/x^4$

maple [A] time = 0.00, size = 25, normalized size = 0.83

$$-\frac{b^2}{2x^2} - \frac{2ab}{3x^3} - \frac{a^2}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^5,x)`

[Out] $-1/4*a^2/x^4 - 2/3*a*b/x^3 - 1/2*b^2/x^2$

maxima [A] time = 1.34, size = 24, normalized size = 0.80

$$\frac{6b^2x^2 + 8abx + 3a^2}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^5,x, algorithm="maxima")`

[Out] $-1/12*(6*b^2*x^2 + 8*a*b*x + 3*a^2)/x^4$

mupad [B] time = 0.03, size = 24, normalized size = 0.80

$$-\frac{\frac{a^2}{4} + \frac{2abx}{3} + \frac{b^2x^2}{2}}{x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x^5, x)`

[Out] $-(a^2/4 + (b^2*x^2)/2 + (2*a*b*x)/3)/x^4$

sympy [A] time = 0.19, size = 26, normalized size = 0.87

$$\frac{-3a^2 - 8abx - 6b^2x^2}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**5, x)`

[Out] $(-3*a**2 - 8*a*b*x - 6*b**2*x**2)/(12*x**4)$

$$3.61 \quad \int \frac{(a+bx)^2}{x^6} dx$$

Optimal. Leaf size=30

$$-\frac{a^2}{5x^5} - \frac{ab}{2x^4} - \frac{b^2}{3x^3}$$

[Out] $-1/5*a^2/x^5-1/2*a*b/x^4-1/3*b^2/x^3$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{5x^5} - \frac{ab}{2x^4} - \frac{b^2}{3x^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^6, x]

[Out] $-a^2/(5*x^5) - (a*b)/(2*x^4) - b^2/(3*x^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^6} dx &= \int \left(\frac{a^2}{x^6} + \frac{2ab}{x^5} + \frac{b^2}{x^4} \right) dx \\ &= -\frac{a^2}{5x^5} - \frac{ab}{2x^4} - \frac{b^2}{3x^3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$-\frac{a^2}{5x^5} - \frac{ab}{2x^4} - \frac{b^2}{3x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^6, x]

[Out] $-1/5*a^2/x^5 - (a*b)/(2*x^4) - b^2/(3*x^3)$

fricas [A] time = 0.45, size = 24, normalized size = 0.80

$$-\frac{10b^2x^2 + 15abx + 6a^2}{30x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^6,x, algorithm="fricas")`

[Out] $-1/30*(10*b^2*x^2 + 15*a*b*x + 6*a^2)/x^5$

giac [A] time = 1.19, size = 24, normalized size = 0.80

$$-\frac{10b^2x^2 + 15abx + 6a^2}{30x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^6,x, algorithm="giac")`

[Out] $-1/30*(10*b^2*x^2 + 15*a*b*x + 6*a^2)/x^5$

maple [A] time = 0.00, size = 25, normalized size = 0.83

$$-\frac{b^2}{3x^3} - \frac{ab}{2x^4} - \frac{a^2}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^6,x)`

[Out] $-1/5*a^2/x^5 - 1/2*a*b/x^4 - 1/3*b^2/x^3$

maxima [A] time = 1.33, size = 24, normalized size = 0.80

$$-\frac{10b^2x^2 + 15abx + 6a^2}{30x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^6,x, algorithm="maxima")`

[Out] $-1/30*(10*b^2*x^2 + 15*a*b*x + 6*a^2)/x^5$

mupad [B] time = 0.03, size = 24, normalized size = 0.80

$$-\frac{\frac{a^2}{5} + \frac{abx}{2} + \frac{b^2x^2}{3}}{x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x^6,x)`

[Out] $-(a^2/5 + (b^2*x^2)/3 + (a*b*x)/2)/x^5$

sympy [A] time = 0.19, size = 26, normalized size = 0.87

$$\frac{-6a^2 - 15abx - 10b^2x^2}{30x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**6,x)`

[Out] $(-6*a**2 - 15*a*b*x - 10*b**2*x**2)/(30*x**5)$

$$3.62 \quad \int \frac{(a+bx)^2}{x^7} dx$$

Optimal. Leaf size=30

$$-\frac{a^2}{6x^6} - \frac{2ab}{5x^5} - \frac{b^2}{4x^4}$$

[Out] $-1/6*a^2/x^6-2/5*a*b/x^5-1/4*b^2/x^4$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{6x^6} - \frac{2ab}{5x^5} - \frac{b^2}{4x^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^7, x]

[Out] $-a^2/(6*x^6) - (2*a*b)/(5*x^5) - b^2/(4*x^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^7} dx &= \int \left(\frac{a^2}{x^7} + \frac{2ab}{x^6} + \frac{b^2}{x^5} \right) dx \\ &= -\frac{a^2}{6x^6} - \frac{2ab}{5x^5} - \frac{b^2}{4x^4} \end{aligned}$$

Mathematica [A] time = 0.00, size = 30, normalized size = 1.00

$$-\frac{a^2}{6x^6} - \frac{2ab}{5x^5} - \frac{b^2}{4x^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^7, x]

[Out] $-1/6*a^2/x^6 - (2*a*b)/(5*x^5) - b^2/(4*x^4)$

fricas [A] time = 0.50, size = 24, normalized size = 0.80

$$-\frac{15b^2x^2 + 24abx + 10a^2}{60x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^7,x, algorithm="fricas")`

[Out] $-1/60*(15*b^2*x^2 + 24*a*b*x + 10*a^2)/x^6$

giac [A] time = 1.07, size = 24, normalized size = 0.80

$$-\frac{15b^2x^2 + 24abx + 10a^2}{60x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^7,x, algorithm="giac")`

[Out] $-1/60*(15*b^2*x^2 + 24*a*b*x + 10*a^2)/x^6$

maple [A] time = 0.00, size = 25, normalized size = 0.83

$$-\frac{b^2}{4x^4} - \frac{2ab}{5x^5} - \frac{a^2}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^7,x)`

[Out] $-1/6*a^2/x^6 - 2/5*a*b/x^5 - 1/4*b^2/x^4$

maxima [A] time = 1.35, size = 24, normalized size = 0.80

$$-\frac{15b^2x^2 + 24abx + 10a^2}{60x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^7,x, algorithm="maxima")`

[Out] $-1/60*(15*b^2*x^2 + 24*a*b*x + 10*a^2)/x^6$

mupad [B] time = 0.03, size = 24, normalized size = 0.80

$$-\frac{\frac{a^2}{6} + \frac{2abx}{5} + \frac{b^2x^2}{4}}{x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x^7,x)`

[Out] $-(a^2/6 + (b^2*x^2)/4 + (2*a*b*x)/5)/x^6$

sympy [A] time = 0.20, size = 26, normalized size = 0.87

$$\frac{-10a^2 - 24abx - 15b^2x^2}{60x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**7,x)`

[Out] $(-10*a**2 - 24*a*b*x - 15*b**2*x**2)/(60*x**6)$

$$3.63 \quad \int \frac{(a+bx)^2}{x^8} dx$$

Optimal. Leaf size=30

$$-\frac{a^2}{7x^7} - \frac{ab}{3x^6} - \frac{b^2}{5x^5}$$

[Out] $-1/7*a^2/x^7-1/3*a*b/x^6-1/5*b^2/x^5$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{7x^7} - \frac{ab}{3x^6} - \frac{b^2}{5x^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^8, x]

[Out] $-a^2/(7*x^7) - (a*b)/(3*x^6) - b^2/(5*x^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^8} dx &= \int \left(\frac{a^2}{x^8} + \frac{2ab}{x^7} + \frac{b^2}{x^6} \right) dx \\ &= -\frac{a^2}{7x^7} - \frac{ab}{3x^6} - \frac{b^2}{5x^5} \end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$-\frac{a^2}{7x^7} - \frac{ab}{3x^6} - \frac{b^2}{5x^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^8, x]

[Out] $-1/7*a^2/x^7 - (a*b)/(3*x^6) - b^2/(5*x^5)$

fricas [A] time = 0.43, size = 24, normalized size = 0.80

$$-\frac{21 b^2 x^2 + 35 a b x + 15 a^2}{105 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^8,x, algorithm="fricas")`

[Out] $-1/105*(21*b^2*x^2 + 35*a*b*x + 15*a^2)/x^7$

giac [A] time = 1.20, size = 24, normalized size = 0.80

$$-\frac{21 b^2 x^2 + 35 a b x + 15 a^2}{105 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^8,x, algorithm="giac")`

[Out] $-1/105*(21*b^2*x^2 + 35*a*b*x + 15*a^2)/x^7$

maple [A] time = 0.01, size = 25, normalized size = 0.83

$$-\frac{b^2}{5x^5} - \frac{ab}{3x^6} - \frac{a^2}{7x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^8,x)`

[Out] $-1/7*a^2/x^7 - 1/3*a*b/x^6 - 1/5*b^2/x^5$

maxima [A] time = 1.35, size = 24, normalized size = 0.80

$$-\frac{21 b^2 x^2 + 35 a b x + 15 a^2}{105 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^8,x, algorithm="maxima")`

[Out] $-1/105*(21*b^2*x^2 + 35*a*b*x + 15*a^2)/x^7$

mupad [B] time = 0.04, size = 24, normalized size = 0.80

$$-\frac{\frac{a^2}{7} + \frac{a b x}{3} + \frac{b^2 x^2}{5}}{x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x^8,x)`

[Out] $-(a^2/7 + (b^2*x^2)/5 + (a*b*x)/3)/x^7$

sympy [A] time = 0.21, size = 26, normalized size = 0.87

$$\frac{-15a^2 - 35abx - 21b^2x^2}{105x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**8,x)`

[Out] $(-15*a**2 - 35*a*b*x - 21*b**2*x**2)/(105*x**7)$

3.64 $\int x^4(a + bx)^3 dx$

Optimal. Leaf size=43

$$\frac{a^3x^5}{5} + \frac{1}{2}a^2bx^6 + \frac{3}{7}ab^2x^7 + \frac{b^3x^8}{8}$$

[Out] $1/5*a^3*x^5+1/2*a^2*b*x^6+3/7*a*b^2*x^7+1/8*b^3*x^8$

Rubi [A] time = 0.02, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{1}{2}a^2bx^6 + \frac{a^3x^5}{5} + \frac{3}{7}ab^2x^7 + \frac{b^3x^8}{8}$$

Antiderivative was successfully verified.

[In] Int[x^4*(a + b*x)^3,x]

[Out] $(a^3*x^5)/5 + (a^2*b*x^6)/2 + (3*a*b^2*x^7)/7 + (b^3*x^8)/8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^4(a + bx)^3 dx &= \int (a^3x^4 + 3a^2bx^5 + 3ab^2x^6 + b^3x^7) dx \\ &= \frac{a^3x^5}{5} + \frac{1}{2}a^2bx^6 + \frac{3}{7}ab^2x^7 + \frac{b^3x^8}{8} \end{aligned}$$

Mathematica [A] time = 0.00, size = 43, normalized size = 1.00

$$\frac{a^3x^5}{5} + \frac{1}{2}a^2bx^6 + \frac{3}{7}ab^2x^7 + \frac{b^3x^8}{8}$$

Antiderivative was successfully verified.

[In] Integrate[x^4*(a + b*x)^3,x]

[Out] $(a^3x^5)/5 + (a^2bx^6)/2 + (3a^2b^2x^7)/7 + (b^3x^8)/8$

fricas [A] time = 0.42, size = 35, normalized size = 0.81

$$\frac{1}{8}x^8b^3 + \frac{3}{7}x^7b^2a + \frac{1}{2}x^6ba^2 + \frac{1}{5}x^5a^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4*(b*x+a)^3,x, algorithm="fricas")`

[Out] $1/8*x^8*b^3 + 3/7*x^7*b^2*a + 1/2*x^6*b*a^2 + 1/5*x^5*a^3$

giac [A] time = 1.22, size = 35, normalized size = 0.81

$$\frac{1}{8}b^3x^8 + \frac{3}{7}ab^2x^7 + \frac{1}{2}a^2bx^6 + \frac{1}{5}a^3x^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4*(b*x+a)^3,x, algorithm="giac")`

[Out] $1/8*b^3*x^8 + 3/7*a*b^2*x^7 + 1/2*a^2*b*x^6 + 1/5*a^3*x^5$

maple [A] time = 0.00, size = 36, normalized size = 0.84

$$\frac{1}{8}b^3x^8 + \frac{3}{7}ab^2x^7 + \frac{1}{2}a^2bx^6 + \frac{1}{5}a^3x^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^4*(b*x+a)^3,x)`

[Out] $1/5*a^3*x^5+1/2*a^2*b*x^6+3/7*a*b^2*x^7+1/8*b^3*x^8$

maxima [A] time = 1.32, size = 35, normalized size = 0.81

$$\frac{1}{8}b^3x^8 + \frac{3}{7}ab^2x^7 + \frac{1}{2}a^2bx^6 + \frac{1}{5}a^3x^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4*(b*x+a)^3,x, algorithm="maxima")`

[Out] $1/8*b^3*x^8 + 3/7*a*b^2*x^7 + 1/2*a^2*b*x^6 + 1/5*a^3*x^5$

mupad [B] time = 0.04, size = 35, normalized size = 0.81

$$\frac{a^3x^5}{5} + \frac{a^2bx^6}{2} + \frac{3ab^2x^7}{7} + \frac{b^3x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^4*(a + b*x)^3,x)`

[Out] $(a^3x^5)/5 + (b^3x^8)/8 + (a^2bx^6)/2 + (3ab^2x^7)/7$

sympy [A] time = 0.08, size = 37, normalized size = 0.86

$$\frac{a^3x^5}{5} + \frac{a^2bx^6}{2} + \frac{3ab^2x^7}{7} + \frac{b^3x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**4*(b*x+a)**3,x)`

[Out] $a**3*x**5/5 + a**2*b*x**6/2 + 3*a*b**2*x**7/7 + b**3*x**8/8$

3.65 $\int x^3(a + bx)^3 dx$

Optimal. Leaf size=43

$$\frac{a^3x^4}{4} + \frac{3}{5}a^2bx^5 + \frac{1}{2}ab^2x^6 + \frac{b^3x^7}{7}$$

[Out] $1/4*a^3*x^4+3/5*a^2*b*x^5+1/2*a*b^2*x^6+1/7*b^3*x^7$

Rubi [A] time = 0.02, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3}{5}a^2bx^5 + \frac{a^3x^4}{4} + \frac{1}{2}ab^2x^6 + \frac{b^3x^7}{7}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^3,x]

[Out] $(a^3*x^4)/4 + (3*a^2*b*x^5)/5 + (a*b^2*x^6)/2 + (b^3*x^7)/7$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^3 dx &= \int (a^3x^3 + 3a^2bx^4 + 3ab^2x^5 + b^3x^6) dx \\ &= \frac{a^3x^4}{4} + \frac{3}{5}a^2bx^5 + \frac{1}{2}ab^2x^6 + \frac{b^3x^7}{7} \end{aligned}$$

Mathematica [A] time = 0.00, size = 43, normalized size = 1.00

$$\frac{a^3x^4}{4} + \frac{3}{5}a^2bx^5 + \frac{1}{2}ab^2x^6 + \frac{b^3x^7}{7}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^3,x]

[Out] $(a^3x^4)/4 + (3a^2bx^5)/5 + (ab^2x^6)/2 + (b^3x^7)/7$

fricas [A] time = 0.39, size = 35, normalized size = 0.81

$$\frac{1}{7}x^7b^3 + \frac{1}{2}x^6b^2a + \frac{3}{5}x^5ba^2 + \frac{1}{4}x^4a^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(b*x+a)^3,x, algorithm="fricas")`

[Out] $1/7*x^7*b^3 + 1/2*x^6*b^2*a + 3/5*x^5*b*a^2 + 1/4*x^4*a^3$

giac [A] time = 1.27, size = 35, normalized size = 0.81

$$\frac{1}{7}b^3x^7 + \frac{1}{2}ab^2x^6 + \frac{3}{5}a^2bx^5 + \frac{1}{4}a^3x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(b*x+a)^3,x, algorithm="giac")`

[Out] $1/7*b^3*x^7 + 1/2*a*b^2*x^6 + 3/5*a^2*b*x^5 + 1/4*a^3*x^4$

maple [A] time = 0.00, size = 36, normalized size = 0.84

$$\frac{1}{7}b^3x^7 + \frac{1}{2}ab^2x^6 + \frac{3}{5}a^2bx^5 + \frac{1}{4}a^3x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(b*x+a)^3,x)`

[Out] $1/4*a^3*x^4+3/5*a^2*b*x^5+1/2*a*b^2*x^6+1/7*b^3*x^7$

maxima [A] time = 1.35, size = 35, normalized size = 0.81

$$\frac{1}{7}b^3x^7 + \frac{1}{2}ab^2x^6 + \frac{3}{5}a^2bx^5 + \frac{1}{4}a^3x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(b*x+a)^3,x, algorithm="maxima")`

[Out] $1/7*b^3*x^7 + 1/2*a*b^2*x^6 + 3/5*a^2*b*x^5 + 1/4*a^3*x^4$

mupad [B] time = 0.04, size = 35, normalized size = 0.81

$$\frac{a^3x^4}{4} + \frac{3a^2bx^5}{5} + \frac{ab^2x^6}{2} + \frac{b^3x^7}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(a + b*x)^3,x)`

[Out] $(a^3x^4)/4 + (b^3x^7)/7 + (3a^2bx^5)/5 + (ab^2x^6)/2$

sympy [A] time = 0.07, size = 37, normalized size = 0.86

$$\frac{a^3x^4}{4} + \frac{3a^2bx^5}{5} + \frac{ab^2x^6}{2} + \frac{b^3x^7}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(b*x+a)**3,x)`

[Out] $a**3*x**4/4 + 3*a**2*b*x**5/5 + a*b**2*x**6/2 + b**3*x**7/7$

3.66 $\int x^2(a + bx)^3 dx$

Optimal. Leaf size=43

$$\frac{a^3x^3}{3} + \frac{3}{4}a^2bx^4 + \frac{3}{5}ab^2x^5 + \frac{b^3x^6}{6}$$

[Out] $1/3*a^3*x^3+3/4*a^2*b*x^4+3/5*a*b^2*x^5+1/6*b^3*x^6$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3}{4}a^2bx^4 + \frac{a^3x^3}{3} + \frac{3}{5}ab^2x^5 + \frac{b^3x^6}{6}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*x)^3,x]

[Out] $(a^3*x^3)/3 + (3*a^2*b*x^4)/4 + (3*a*b^2*x^5)/5 + (b^3*x^6)/6$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^3 dx &= \int (a^3x^2 + 3a^2bx^3 + 3ab^2x^4 + b^3x^5) dx \\ &= \frac{a^3x^3}{3} + \frac{3}{4}a^2bx^4 + \frac{3}{5}ab^2x^5 + \frac{b^3x^6}{6} \end{aligned}$$

Mathematica [A] time = 0.00, size = 43, normalized size = 1.00

$$\frac{a^3x^3}{3} + \frac{3}{4}a^2bx^4 + \frac{3}{5}ab^2x^5 + \frac{b^3x^6}{6}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^3,x]

[Out] $(a^3x^3)/3 + (3a^2bx^4)/4 + (3ab^2x^5)/5 + (b^3x^6)/6$

fricas [A] time = 0.37, size = 35, normalized size = 0.81

$$\frac{1}{6}x^6b^3 + \frac{3}{5}x^5b^2a + \frac{3}{4}x^4ba^2 + \frac{1}{3}x^3a^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(b*x+a)^3,x, algorithm="fricas")`

[Out] $1/6*x^6*b^3 + 3/5*x^5*b^2*a + 3/4*x^4*b*a^2 + 1/3*x^3*a^3$

giac [A] time = 1.22, size = 35, normalized size = 0.81

$$\frac{1}{6}b^3x^6 + \frac{3}{5}ab^2x^5 + \frac{3}{4}a^2bx^4 + \frac{1}{3}a^3x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(b*x+a)^3,x, algorithm="giac")`

[Out] $1/6*b^3*x^6 + 3/5*a*b^2*x^5 + 3/4*a^2*b*x^4 + 1/3*a^3*x^3$

maple [A] time = 0.00, size = 36, normalized size = 0.84

$$\frac{1}{6}b^3x^6 + \frac{3}{5}ab^2x^5 + \frac{3}{4}a^2bx^4 + \frac{1}{3}a^3x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(b*x+a)^3,x)`

[Out] $1/3*a^3*x^3+3/4*a^2*b*x^4+3/5*a*b^2*x^5+1/6*b^3*x^6$

maxima [A] time = 1.34, size = 35, normalized size = 0.81

$$\frac{1}{6}b^3x^6 + \frac{3}{5}ab^2x^5 + \frac{3}{4}a^2bx^4 + \frac{1}{3}a^3x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(b*x+a)^3,x, algorithm="maxima")`

[Out] $1/6*b^3*x^6 + 3/5*a*b^2*x^5 + 3/4*a^2*b*x^4 + 1/3*a^3*x^3$

mupad [B] time = 0.04, size = 35, normalized size = 0.81

$$\frac{a^3x^3}{3} + \frac{3a^2bx^4}{4} + \frac{3ab^2x^5}{5} + \frac{b^3x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(a + b*x)^3,x)`

[Out] $(a^3x^3)/3 + (b^3x^6)/6 + (3a^2bx^4)/4 + (3ab^2x^5)/5$

sympy [A] time = 0.07, size = 39, normalized size = 0.91

$$\frac{a^3x^3}{3} + \frac{3a^2bx^4}{4} + \frac{3ab^2x^5}{5} + \frac{b^3x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(b*x+a)**3,x)`

[Out] $a**3*x**3/3 + 3*a**2*b*x**4/4 + 3*a*b**2*x**5/5 + b**3*x**6/6$

3.67 $\int x(a + bx)^3 dx$

Optimal. Leaf size=30

$$\frac{(a + bx)^5}{5b^2} - \frac{a(a + bx)^4}{4b^2}$$

[Out] $-1/4*a*(b*x+a)^4/b^2+1/5*(b*x+a)^5/b^2$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{(a + bx)^5}{5b^2} - \frac{a(a + bx)^4}{4b^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^3,x]

[Out] $-(a*(a + b*x)^4)/(4*b^2) + (a + b*x)^5/(5*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x(a + bx)^3 dx &= \int \left(-\frac{a(a + bx)^3}{b} + \frac{(a + bx)^4}{b} \right) dx \\ &= -\frac{a(a + bx)^4}{4b^2} + \frac{(a + bx)^5}{5b^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 40, normalized size = 1.33

$$\frac{a^3x^2}{2} + a^2bx^3 + \frac{3}{4}ab^2x^4 + \frac{b^3x^5}{5}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^3,x]

[Out] $(a^3*x^2)/2 + a^2*b*x^3 + (3*a*b^2*x^4)/4 + (b^3*x^5)/5$

fricas [A] time = 0.41, size = 34, normalized size = 1.13

$$\frac{1}{5}x^5b^3 + \frac{3}{4}x^4b^2a + x^3ba^2 + \frac{1}{2}x^2a^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^3,x, algorithm="fricas")

[Out] 1/5*x^5*b^3 + 3/4*x^4*b^2*a + x^3*b*a^2 + 1/2*x^2*a^3

giac [A] time = 1.21, size = 34, normalized size = 1.13

$$\frac{1}{5}b^3x^5 + \frac{3}{4}ab^2x^4 + a^2bx^3 + \frac{1}{2}a^3x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^3,x, algorithm="giac")

[Out] 1/5*b^3*x^5 + 3/4*a*b^2*x^4 + a^2*b*x^3 + 1/2*a^3*x^2

maple [A] time = 0.00, size = 35, normalized size = 1.17

$$\frac{1}{5}b^3x^5 + \frac{3}{4}ab^2x^4 + a^2bx^3 + \frac{1}{2}a^3x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^3,x)

[Out] 1/5*b^3*x^5+3/4*a*b^2*x^4+a^2*b*x^3+1/2*a^3*x^2

maxima [A] time = 1.38, size = 34, normalized size = 1.13

$$\frac{1}{5}b^3x^5 + \frac{3}{4}ab^2x^4 + a^2bx^3 + \frac{1}{2}a^3x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^3,x, algorithm="maxima")

[Out] 1/5*b^3*x^5 + 3/4*a*b^2*x^4 + a^2*b*x^3 + 1/2*a^3*x^2

mupad [B] time = 0.04, size = 34, normalized size = 1.13

$$\frac{a^3x^2}{2} + a^2bx^3 + \frac{3ab^2x^4}{4} + \frac{b^3x^5}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(a + b*x)^3,x)`

[Out] $(a^3x^2)/2 + (b^3x^5)/5 + a^2bx^3 + (3ab^2x^4)/4$

sympy [A] time = 0.07, size = 36, normalized size = 1.20

$$\frac{a^3x^2}{2} + a^2bx^3 + \frac{3ab^2x^4}{4} + \frac{b^3x^5}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**3,x)`

[Out] $a**3*x**2/2 + a**2*b*x**3 + 3*a*b**2*x**4/4 + b**3*x**5/5$

3.68 $\int (a + bx)^3 dx$

Optimal. Leaf size=14

$$\frac{(a + bx)^4}{4b}$$

[Out] 1/4*(b*x+a)^4/b

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(a + bx)^4}{4b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3, x]

[Out] (a + b*x)^4/(4*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^3 dx = \frac{(a + bx)^4}{4b}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{(a + bx)^4}{4b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3, x]

[Out] (a + b*x)^4/(4*b)

fricas [B] time = 0.38, size = 31, normalized size = 2.21

$$\frac{1}{4}x^4b^3 + x^3b^2a + \frac{3}{2}x^2ba^2 + xa^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3,x, algorithm="fricas")

[Out] $1/4*x^4*b^3 + x^3*b^2*a + 3/2*x^2*b*a^2 + x*a^3$

giac [A] time = 1.36, size = 12, normalized size = 0.86

$$\frac{(bx + a)^4}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3,x, algorithm="giac")

[Out] $1/4*(b*x + a)^4/b$

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{(bx + a)^4}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3,x)

[Out] $1/4*(b*x+a)^4/b$

maxima [B] time = 1.39, size = 31, normalized size = 2.21

$$\frac{1}{4}b^3x^4 + ab^2x^3 + \frac{3}{2}a^2bx^2 + a^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3,x, algorithm="maxima")

[Out] $1/4*b^3*x^4 + a*b^2*x^3 + 3/2*a^2*b*x^2 + a^3*x$

mupad [B] time = 0.04, size = 31, normalized size = 2.21

$$a^3x + \frac{3a^2bx^2}{2} + ab^2x^3 + \frac{b^3x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3,x)

[Out] $a^3*x + (b^3*x^4)/4 + (3*a^2*b*x^2)/2 + a*b^2*x^3$

sympy [B] time = 0.07, size = 32, normalized size = 2.29

$$a^3x + \frac{3a^2bx^2}{2} + ab^2x^3 + \frac{b^3x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3,x)

[Out] a**3*x + 3*a**2*b*x**2/2 + a*b**2*x**3 + b**3*x**4/4

$$3.69 \quad \int \frac{(a+bx)^3}{x} dx$$

Optimal. Leaf size=35

$$a^3 \log(x) + 3a^2bx + \frac{3}{2}ab^2x^2 + \frac{b^3x^3}{3}$$

[Out] $3*a^2*b*x+3/2*a*b^2*x^2+1/3*b^3*x^3+a^3*\ln(x)$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$3a^2bx + a^3 \log(x) + \frac{3}{2}ab^2x^2 + \frac{b^3x^3}{3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x, x]

[Out] $3*a^2*b*x + (3*a*b^2*x^2)/2 + (b^3*x^3)/3 + a^3*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x} dx &= \int \left(3a^2b + \frac{a^3}{x} + 3ab^2x + b^3x^2 \right) dx \\ &= 3a^2bx + \frac{3}{2}ab^2x^2 + \frac{b^3x^3}{3} + a^3 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 35, normalized size = 1.00

$$a^3 \log(x) + 3a^2bx + \frac{3}{2}ab^2x^2 + \frac{b^3x^3}{3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x, x]

[Out] $3a^2bx + (3ab^2x^2)/2 + (b^3x^3)/3 + a^3\text{Log}[x]$

fricas [A] time = 0.51, size = 31, normalized size = 0.89

$$\frac{1}{3}b^3x^3 + \frac{3}{2}ab^2x^2 + 3a^2bx + a^3\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x,x, algorithm="fricas")`

[Out] $1/3*b^3*x^3 + 3/2*a*b^2*x^2 + 3*a^2*b*x + a^3*\log(x)$

giac [A] time = 0.95, size = 32, normalized size = 0.91

$$\frac{1}{3}b^3x^3 + \frac{3}{2}ab^2x^2 + 3a^2bx + a^3\log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x,x, algorithm="giac")`

[Out] $1/3*b^3*x^3 + 3/2*a*b^2*x^2 + 3*a^2*b*x + a^3*\log(\text{abs}(x))$

maple [A] time = 0.00, size = 32, normalized size = 0.91

$$\frac{b^3x^3}{3} + \frac{3ab^2x^2}{2} + a^3\ln(x) + 3a^2bx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3/x,x)`

[Out] $3a^2bx + 3/2ab^2x^2 + 1/3b^3x^3 + a^3\ln(x)$

maxima [A] time = 1.34, size = 31, normalized size = 0.89

$$\frac{1}{3}b^3x^3 + \frac{3}{2}ab^2x^2 + 3a^2bx + a^3\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x,x, algorithm="maxima")`

[Out] $1/3*b^3*x^3 + 3/2*a*b^2*x^2 + 3*a^2*b*x + a^3*\log(x)$

mupad [B] time = 0.03, size = 31, normalized size = 0.89

$$a^3\ln(x) + \frac{b^3x^3}{3} + \frac{3ab^2x^2}{2} + 3a^2bx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x,x)`

[Out] $a^3 \log(x) + (b^3 x^3)/3 + (3ab^2 x^2)/2 + 3a^2 b x$

sympy [A] time = 0.12, size = 34, normalized size = 0.97

$$a^3 \log(x) + 3a^2 b x + \frac{3ab^2 x^2}{2} + \frac{b^3 x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x,x)`

[Out] $a**3 \log(x) + 3*a**2*b*x + 3*a*b**2*x**2/2 + b**3*x**3/3$

$$3.70 \quad \int \frac{(a+bx)^3}{x^2} dx$$

Optimal. Leaf size=34

$$-\frac{a^3}{x} + 3a^2b \log(x) + 3ab^2x + \frac{b^3x^2}{2}$$

[Out] $-a^3/x + 3*a*b^2*x + 1/2*b^3*x^2 + 3*a^2*b*\ln(x)$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$3a^2b \log(x) - \frac{a^3}{x} + 3ab^2x + \frac{b^3x^2}{2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^2,x]

[Out] $-(a^3/x) + 3*a*b^2*x + (b^3*x^2)/2 + 3*a^2*b*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^2} dx &= \int \left(3ab^2 + \frac{a^3}{x^2} + \frac{3a^2b}{x} + b^3x \right) dx \\ &= -\frac{a^3}{x} + 3ab^2x + \frac{b^3x^2}{2} + 3a^2b \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 34, normalized size = 1.00

$$-\frac{a^3}{x} + 3a^2b \log(x) + 3ab^2x + \frac{b^3x^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^2,x]

[Out] $-(a^3/x) + 3*a*b^2*x + (b^3*x^2)/2 + 3*a^2*b*\text{Log}[x]$

fricas [A] time = 0.43, size = 36, normalized size = 1.06

$$\frac{b^3x^3 + 6ab^2x^2 + 6a^2bx \log(x) - 2a^3}{2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^2,x, algorithm="fricas")`

[Out] $1/2*(b^3*x^3 + 6*a*b^2*x^2 + 6*a^2*b*x*\log(x) - 2*a^3)/x$

giac [A] time = 1.36, size = 33, normalized size = 0.97

$$\frac{1}{2}b^3x^2 + 3ab^2x + 3a^2b \log(|x|) - \frac{a^3}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^2,x, algorithm="giac")`

[Out] $1/2*b^3*x^2 + 3*a*b^2*x + 3*a^2*b*\log(\text{abs}(x)) - a^3/x$

maple [A] time = 0.01, size = 33, normalized size = 0.97

$$\frac{b^3x^2}{2} + 3a^2b \ln(x) + 3ab^2x - \frac{a^3}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3/x^2,x)`

[Out] $-a^3/x + 3*a*b^2*x + 1/2*b^3*x^2 + 3*a^2*b*\ln(x)$

maxima [A] time = 1.29, size = 32, normalized size = 0.94

$$\frac{1}{2}b^3x^2 + 3ab^2x + 3a^2b \log(x) - \frac{a^3}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^2,x, algorithm="maxima")`

[Out] $1/2*b^3*x^2 + 3*a*b^2*x + 3*a^2*b*\log(x) - a^3/x$

mupad [B] time = 0.03, size = 32, normalized size = 0.94

$$\frac{b^3x^2}{2} - \frac{a^3}{x} + 3a^2b \ln(x) + 3ab^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^2,x)`

[Out] $(b^3x^2)/2 - a^3/x + 3a^2b\log(x) + 3ab^2x$

sympy [A] time = 0.13, size = 31, normalized size = 0.91

$$-\frac{a^3}{x} + 3a^2b \log(x) + 3ab^2x + \frac{b^3x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**2,x)`

[Out] $-a^3/x + 3a^2b\log(x) + 3ab^2x + b^3x^2/2$

$$3.71 \quad \int \frac{(a+bx)^3}{x^3} dx$$

Optimal. Leaf size=33

$$-\frac{a^3}{2x^2} - \frac{3a^2b}{x} + 3ab^2 \log(x) + b^3x$$

[Out] $-1/2*a^3/x^2-3*a^2*b/x+b^3*x+3*a*b^2*\ln(x)$

Rubi [A] time = 0.01, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{3a^2b}{x} - \frac{a^3}{2x^2} + 3ab^2 \log(x) + b^3x$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^3,x]

[Out] $-a^3/(2*x^2) - (3*a^2*b)/x + b^3*x + 3*a*b^2*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^3} dx &= \int \left(b^3 + \frac{a^3}{x^3} + \frac{3a^2b}{x^2} + \frac{3ab^2}{x} \right) dx \\ &= -\frac{a^3}{2x^2} - \frac{3a^2b}{x} + b^3x + 3ab^2 \log(x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 1.00

$$-\frac{a^3}{2x^2} - \frac{3a^2b}{x} + 3ab^2 \log(x) + b^3x$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^3,x]

[Out] $-1/2*a^3/x^2 - (3*a^2*b)/x + b^3*x + 3*a*b^2*\text{Log}[x]$

fricas [A] time = 0.52, size = 37, normalized size = 1.12

$$\frac{2b^3x^3 + 6ab^2x^2 \log(x) - 6a^2bx - a^3}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^3,x, algorithm="fricas")`

[Out] $1/2*(2*b^3*x^3 + 6*a*b^2*x^2*\log(x) - 6*a^2*b*x - a^3)/x^2$

giac [A] time = 1.18, size = 31, normalized size = 0.94

$$b^3x + 3ab^2 \log(|x|) - \frac{6a^2bx + a^3}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^3,x, algorithm="giac")`

[Out] $b^3*x + 3*a*b^2*\log(\text{abs}(x)) - 1/2*(6*a^2*b*x + a^3)/x^2$

maple [A] time = 0.00, size = 32, normalized size = 0.97

$$3ab^2 \ln(x) + b^3x - \frac{3a^2b}{x} - \frac{a^3}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3/x^3,x)`

[Out] $-1/2*a^3/x^2 - 3*a^2*b/x + b^3*x + 3*a*b^2*\ln(x)$

maxima [A] time = 1.34, size = 30, normalized size = 0.91

$$b^3x + 3ab^2 \log(x) - \frac{6a^2bx + a^3}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^3,x, algorithm="maxima")`

[Out] $b^3*x + 3*a*b^2*\log(x) - 1/2*(6*a^2*b*x + a^3)/x^2$

mupad [B] time = 0.03, size = 32, normalized size = 0.97

$$b^3x - \frac{\frac{a^3}{2} + 3bxa^2}{x^2} + 3ab^2 \ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^3,x)`

[Out] $b^3x - (a^3/2 + 3a^2bx)/x^2 + 3ab^2\log(x)$

sympy [A] time = 0.19, size = 32, normalized size = 0.97

$$3ab^2 \log(x) + b^3x + \frac{-a^3 - 6a^2bx}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**3,x)`

[Out] $3ab^2\log(x) + b^3x + (-a^3 - 6a^2bx)/(2x^2)$

$$3.72 \quad \int \frac{(a+bx)^3}{x^4} dx$$

Optimal. Leaf size=37

$$-\frac{a^3}{3x^3} - \frac{3a^2b}{2x^2} - \frac{3ab^2}{x} + b^3 \log(x)$$

[Out] $-1/3*a^3/x^3-3/2*a^2*b/x^2-3*a*b^2/x+b^3*\ln(x)$

Rubi [A] time = 0.01, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{3a^2b}{2x^2} - \frac{a^3}{3x^3} - \frac{3ab^2}{x} + b^3 \log(x)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^4, x]

[Out] $-a^3/(3*x^3) - (3*a^2*b)/(2*x^2) - (3*a*b^2)/x + b^3*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^4} dx &= \int \left(\frac{a^3}{x^4} + \frac{3a^2b}{x^3} + \frac{3ab^2}{x^2} + \frac{b^3}{x} \right) dx \\ &= -\frac{a^3}{3x^3} - \frac{3a^2b}{2x^2} - \frac{3ab^2}{x} + b^3 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 37, normalized size = 1.00

$$-\frac{a^3}{3x^3} - \frac{3a^2b}{2x^2} - \frac{3ab^2}{x} + b^3 \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^4, x]

[Out] $-1/3*a^3/x^3 - (3*a^2*b)/(2*x^2) - (3*a*b^2)/x + b^3*\text{Log}[x]$

fricas [A] time = 0.49, size = 37, normalized size = 1.00

$$\frac{6b^3x^3 \log(x) - 18ab^2x^2 - 9a^2bx - 2a^3}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^4,x, algorithm="fricas")`

[Out] $1/6*(6*b^3*x^3*\log(x) - 18*a*b^2*x^2 - 9*a^2*b*x - 2*a^3)/x^3$

giac [A] time = 1.14, size = 35, normalized size = 0.95

$$b^3 \log(|x|) - \frac{18ab^2x^2 + 9a^2bx + 2a^3}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^4,x, algorithm="giac")`

[Out] $b^3*\log(\text{abs}(x)) - 1/6*(18*a*b^2*x^2 + 9*a^2*b*x + 2*a^3)/x^3$

maple [A] time = 0.01, size = 34, normalized size = 0.92

$$b^3 \ln(x) - \frac{3ab^2}{x} - \frac{3a^2b}{2x^2} - \frac{a^3}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3/x^4,x)`

[Out] $-1/3*a^3/x^3 - 3/2*a^2*b/x^2 - 3*a*b^2/x + b^3*\ln(x)$

maxima [A] time = 1.30, size = 34, normalized size = 0.92

$$b^3 \log(x) - \frac{18ab^2x^2 + 9a^2bx + 2a^3}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^4,x, algorithm="maxima")`

[Out] $b^3*\log(x) - 1/6*(18*a*b^2*x^2 + 9*a^2*b*x + 2*a^3)/x^3$

mupad [B] time = 0.07, size = 34, normalized size = 0.92

$$b^3 \ln(x) - \frac{\frac{a^3}{3} + \frac{3a^2bx}{2} + 3ab^2x^2}{x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^4,x)`

[Out] $b^3 \log(x) - (a^3/3 + 3*a*b^2*x^2 + (3*a^2*b*x)/2)/x^3$

sympy [A] time = 0.24, size = 36, normalized size = 0.97

$$b^3 \log(x) + \frac{-2a^3 - 9a^2bx - 18ab^2x^2}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**4,x)`

[Out] $b**3*\log(x) + (-2*a**3 - 9*a**2*b*x - 18*a*b**2*x**2)/(6*x**3)$

$$3.73 \quad \int \frac{(a+bx)^3}{x^5} dx$$

Optimal. Leaf size=17

$$-\frac{(a+bx)^4}{4ax^4}$$

[Out] $-1/4*(b*x+a)^4/a/x^4$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {37}

$$-\frac{(a+bx)^4}{4ax^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^5, x]

[Out] $-(a + b*x)^4/(4*a*x^4)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(a+bx)^3}{x^5} dx = -\frac{(a+bx)^4}{4ax^4}$$

Mathematica [B] time = 0.00, size = 39, normalized size = 2.29

$$-\frac{a^3}{4x^4} - \frac{a^2b}{x^3} - \frac{3ab^2}{2x^2} - \frac{b^3}{x}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^5, x]

[Out] $-1/4*a^3/x^4 - (a^2*b)/x^3 - (3*a*b^2)/(2*x^2) - b^3/x$

fricas [B] time = 0.44, size = 33, normalized size = 1.94

$$-\frac{4b^3x^3 + 6ab^2x^2 + 4a^2bx + a^3}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^5,x, algorithm="fricas")

[Out] -1/4*(4*b^3*x^3 + 6*a*b^2*x^2 + 4*a^2*b*x + a^3)/x^4

giac [B] time = 1.29, size = 33, normalized size = 1.94

$$-\frac{4b^3x^3 + 6ab^2x^2 + 4a^2bx + a^3}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^5,x, algorithm="giac")

[Out] -1/4*(4*b^3*x^3 + 6*a*b^2*x^2 + 4*a^2*b*x + a^3)/x^4

maple [B] time = 0.01, size = 36, normalized size = 2.12

$$-\frac{b^3}{x} - \frac{3ab^2}{2x^2} - \frac{a^2b}{x^3} - \frac{a^3}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/x^5,x)

[Out] -a^2*b/x^3-1/4*a^3/x^4-b^3/x-3/2*a*b^2/x^2

maxima [B] time = 1.33, size = 33, normalized size = 1.94

$$-\frac{4b^3x^3 + 6ab^2x^2 + 4a^2bx + a^3}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^5,x, algorithm="maxima")

[Out] -1/4*(4*b^3*x^3 + 6*a*b^2*x^2 + 4*a^2*b*x + a^3)/x^4

mupad [B] time = 0.03, size = 33, normalized size = 1.94

$$-\frac{\frac{a^3}{4} + a^2bx + \frac{3ab^2x^2}{2} + b^3x^3}{x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^5,x)`

[Out] $-(a^3/4 + b^3*x^3 + (3*a*b^2*x^2)/2 + a^2*b*x)/x^4$

sympy [B] time = 0.26, size = 36, normalized size = 2.12

$$\frac{-a^3 - 4a^2bx - 6ab^2x^2 - 4b^3x^3}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**5,x)`

[Out] $(-a**3 - 4*a**2*b*x - 6*a*b**2*x**2 - 4*b**3*x**3)/(4*x**4)$

$$3.74 \quad \int \frac{(a+bx)^3}{x^6} dx$$

Optimal. Leaf size=36

$$\frac{b(a+bx)^4}{20a^2x^4} - \frac{(a+bx)^4}{5ax^5}$$

[Out] $-1/5*(b*x+a)^4/a/x^5+1/20*b*(b*x+a)^4/a^2/x^4$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{b(a+bx)^4}{20a^2x^4} - \frac{(a+bx)^4}{5ax^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^6, x]

[Out] $-(a + b*x)^4/(5*a*x^5) + (b*(a + b*x)^4)/(20*a^2*x^4)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{(a+bx)^3}{x^6} dx = -\frac{(a+bx)^4}{5ax^5} - \frac{b \int \frac{(a+bx)^3}{x^5} dx}{5a}$$

$$= -\frac{(a+bx)^4}{5ax^5} + \frac{b(a+bx)^4}{20a^2x^4}$$

Mathematica [A] time = 0.01, size = 41, normalized size = 1.14

$$-\frac{a^3}{5x^5} - \frac{3a^2b}{4x^4} - \frac{ab^2}{x^3} - \frac{b^3}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^6, x]

[Out] -1/5*a^3/x^5 - (3*a^2*b)/(4*x^4) - (a*b^2)/x^3 - b^3/(2*x^2)

fricas [A] time = 0.44, size = 35, normalized size = 0.97

$$-\frac{10b^3x^3 + 20ab^2x^2 + 15a^2bx + 4a^3}{20x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^6, x, algorithm="fricas")

[Out] -1/20*(10*b^3*x^3 + 20*a*b^2*x^2 + 15*a^2*b*x + 4*a^3)/x^5

giac [A] time = 1.13, size = 35, normalized size = 0.97

$$-\frac{10b^3x^3 + 20ab^2x^2 + 15a^2bx + 4a^3}{20x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^6, x, algorithm="giac")

[Out] -1/20*(10*b^3*x^3 + 20*a*b^2*x^2 + 15*a^2*b*x + 4*a^3)/x^5

maple [A] time = 0.00, size = 36, normalized size = 1.00

$$-\frac{b^3}{2x^2} - \frac{ab^2}{x^3} - \frac{3a^2b}{4x^4} - \frac{a^3}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3/x^6,x)`

[Out] $-1/5*a^3/x^5 - a*b^2/x^3 - 3/4*a^2*b/x^4 - 1/2*b^3/x^2$

maxima [A] time = 1.35, size = 35, normalized size = 0.97

$$-\frac{10b^3x^3 + 20ab^2x^2 + 15a^2bx + 4a^3}{20x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^6,x, algorithm="maxima")`

[Out] $-1/20*(10*b^3*x^3 + 20*a*b^2*x^2 + 15*a^2*b*x + 4*a^3)/x^5$

mupad [B] time = 0.03, size = 34, normalized size = 0.94

$$-\frac{\frac{a^3}{5} + \frac{3a^2bx}{4} + ab^2x^2 + \frac{b^3x^3}{2}}{x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^6,x)`

[Out] $-(a^3/5 + (b^3*x^3)/2 + a*b^2*x^2 + (3*a^2*b*x)/4)/x^5$

sympy [A] time = 0.25, size = 37, normalized size = 1.03

$$\frac{-4a^3 - 15a^2bx - 20ab^2x^2 - 10b^3x^3}{20x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**6,x)`

[Out] $(-4*a**3 - 15*a**2*b*x - 20*a*b**2*x**2 - 10*b**3*x**3)/(20*x**5)$

$$3.75 \quad \int \frac{(a+bx)^3}{x^7} dx$$

Optimal. Leaf size=43

$$-\frac{a^3}{6x^6} - \frac{3a^2b}{5x^5} - \frac{3ab^2}{4x^4} - \frac{b^3}{3x^3}$$

[Out] $-1/6*a^3/x^6-3/5*a^2*b/x^5-3/4*a*b^2/x^4-1/3*b^3/x^3$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{3a^2b}{5x^5} - \frac{a^3}{6x^6} - \frac{3ab^2}{4x^4} - \frac{b^3}{3x^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^7, x]

[Out] $-a^3/(6*x^6) - (3*a^2*b)/(5*x^5) - (3*a*b^2)/(4*x^4) - b^3/(3*x^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^7} dx &= \int \left(\frac{a^3}{x^7} + \frac{3a^2b}{x^6} + \frac{3ab^2}{x^5} + \frac{b^3}{x^4} \right) dx \\ &= -\frac{a^3}{6x^6} - \frac{3a^2b}{5x^5} - \frac{3ab^2}{4x^4} - \frac{b^3}{3x^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 43, normalized size = 1.00

$$-\frac{a^3}{6x^6} - \frac{3a^2b}{5x^5} - \frac{3ab^2}{4x^4} - \frac{b^3}{3x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^7, x]

[Out] $-1/6*a^3/x^6 - (3*a^2*b)/(5*x^5) - (3*a*b^2)/(4*x^4) - b^3/(3*x^3)$

fricas [A] time = 0.41, size = 35, normalized size = 0.81

$$\frac{20 b^3 x^3 + 45 a b^2 x^2 + 36 a^2 b x + 10 a^3}{60 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^7,x, algorithm="fricas")`

[Out] $-1/60*(20*b^3*x^3 + 45*a*b^2*x^2 + 36*a^2*b*x + 10*a^3)/x^6$

giac [A] time = 1.15, size = 35, normalized size = 0.81

$$\frac{20 b^3 x^3 + 45 a b^2 x^2 + 36 a^2 b x + 10 a^3}{60 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^7,x, algorithm="giac")`

[Out] $-1/60*(20*b^3*x^3 + 45*a*b^2*x^2 + 36*a^2*b*x + 10*a^3)/x^6$

maple [A] time = 0.01, size = 36, normalized size = 0.84

$$-\frac{b^3}{3x^3} - \frac{3ab^2}{4x^4} - \frac{3a^2b}{5x^5} - \frac{a^3}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3/x^7,x)`

[Out] $-1/6*a^3/x^6-3/5*a^2*b/x^5-3/4*a*b^2/x^4-1/3*b^3/x^3$

maxima [A] time = 1.35, size = 35, normalized size = 0.81

$$\frac{20 b^3 x^3 + 45 a b^2 x^2 + 36 a^2 b x + 10 a^3}{60 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^7,x, algorithm="maxima")`

[Out] $-1/60*(20*b^3*x^3 + 45*a*b^2*x^2 + 36*a^2*b*x + 10*a^3)/x^6$

mupad [B] time = 0.03, size = 35, normalized size = 0.81

$$\frac{\frac{a^3}{6} + \frac{3a^2bx}{5} + \frac{3ab^2x^2}{4} + \frac{b^3x^3}{3}}{x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^7,x)`

[Out] $-(a^3/6 + (b^3*x^3)/3 + (3*a*b^2*x^2)/4 + (3*a^2*b*x)/5)/x^6$

sympy [A] time = 0.34, size = 37, normalized size = 0.86

$$\frac{-10a^3 - 36a^2bx - 45ab^2x^2 - 20b^3x^3}{60x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**7,x)`

[Out] $(-10*a**3 - 36*a**2*b*x - 45*a*b**2*x**2 - 20*b**3*x**3)/(60*x**6)$

$$3.76 \quad \int \frac{(a+bx)^3}{x^8} dx$$

Optimal. Leaf size=43

$$-\frac{a^3}{7x^7} - \frac{a^2b}{2x^6} - \frac{3ab^2}{5x^5} - \frac{b^3}{4x^4}$$

[Out] $-1/7*a^3/x^7-1/2*a^2*b/x^6-3/5*a*b^2/x^5-1/4*b^3/x^4$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2b}{2x^6} - \frac{a^3}{7x^7} - \frac{3ab^2}{5x^5} - \frac{b^3}{4x^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^8,x]

[Out] $-a^3/(7*x^7) - (a^2*b)/(2*x^6) - (3*a*b^2)/(5*x^5) - b^3/(4*x^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^8} dx &= \int \left(\frac{a^3}{x^8} + \frac{3a^2b}{x^7} + \frac{3ab^2}{x^6} + \frac{b^3}{x^5} \right) dx \\ &= -\frac{a^3}{7x^7} - \frac{a^2b}{2x^6} - \frac{3ab^2}{5x^5} - \frac{b^3}{4x^4} \end{aligned}$$

Mathematica [A] time = 0.00, size = 43, normalized size = 1.00

$$-\frac{a^3}{7x^7} - \frac{a^2b}{2x^6} - \frac{3ab^2}{5x^5} - \frac{b^3}{4x^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^8,x]

[Out] $-1/7*a^3/x^7 - (a^2*b)/(2*x^6) - (3*a*b^2)/(5*x^5) - b^3/(4*x^4)$

fricas [A] time = 0.43, size = 35, normalized size = 0.81

$$\frac{35 b^3 x^3 + 84 a b^2 x^2 + 70 a^2 b x + 20 a^3}{140 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^8,x, algorithm="fricas")`

[Out] $-1/140*(35*b^3*x^3 + 84*a*b^2*x^2 + 70*a^2*b*x + 20*a^3)/x^7$

giac [A] time = 1.12, size = 35, normalized size = 0.81

$$\frac{35 b^3 x^3 + 84 a b^2 x^2 + 70 a^2 b x + 20 a^3}{140 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^8,x, algorithm="giac")`

[Out] $-1/140*(35*b^3*x^3 + 84*a*b^2*x^2 + 70*a^2*b*x + 20*a^3)/x^7$

maple [A] time = 0.00, size = 36, normalized size = 0.84

$$-\frac{b^3}{4x^4} - \frac{3ab^2}{5x^5} - \frac{a^2b}{2x^6} - \frac{a^3}{7x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3/x^8,x)`

[Out] $-1/7*a^3/x^7 - 1/2*a^2*b/x^6 - 3/5*a*b^2/x^5 - 1/4*b^3/x^4$

maxima [A] time = 1.35, size = 35, normalized size = 0.81

$$\frac{35 b^3 x^3 + 84 a b^2 x^2 + 70 a^2 b x + 20 a^3}{140 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^8,x, algorithm="maxima")`

[Out] $-1/140*(35*b^3*x^3 + 84*a*b^2*x^2 + 70*a^2*b*x + 20*a^3)/x^7$

mupad [B] time = 0.03, size = 35, normalized size = 0.81

$$\frac{\frac{a^3}{7} + \frac{a^2 b x}{2} + \frac{3 a b^2 x^2}{5} + \frac{b^3 x^3}{4}}{x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^8,x)`

[Out] $-(a^3/7 + (b^3*x^3)/4 + (3*a*b^2*x^2)/5 + (a^2*b*x)/2)/x^7$

sympy [A] time = 0.29, size = 37, normalized size = 0.86

$$\frac{-20a^3 - 70a^2bx - 84ab^2x^2 - 35b^3x^3}{140x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**8,x)`

[Out] $(-20*a**3 - 70*a**2*b*x - 84*a*b**2*x**2 - 35*b**3*x**3)/(140*x**7)$

3.77 $\int x^6(a + bx)^5 dx$

Optimal. Leaf size=66

$$\frac{a^5x^7}{7} + \frac{5}{8}a^4bx^8 + \frac{10}{9}a^3b^2x^9 + a^2b^3x^{10} + \frac{5}{11}ab^4x^{11} + \frac{b^5x^{12}}{12}$$

[Out] $1/7*a^5*x^7+5/8*a^4*b*x^8+10/9*a^3*b^2*x^9+a^2*b^3*x^{10}+5/11*a*b^4*x^{11}+1/12*b^5*x^{12}$

Rubi [A] time = 0.03, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$a^2b^3x^{10} + \frac{10}{9}a^3b^2x^9 + \frac{5}{8}a^4bx^8 + \frac{a^5x^7}{7} + \frac{5}{11}ab^4x^{11} + \frac{b^5x^{12}}{12}$$

Antiderivative was successfully verified.

[In] Int[x^6*(a + b*x)^5, x]

[Out] $(a^5*x^7)/7 + (5*a^4*b*x^8)/8 + (10*a^3*b^2*x^9)/9 + a^2*b^3*x^{10} + (5*a*b^4*x^{11})/11 + (b^5*x^{12})/12$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^6(a + bx)^5 dx &= \int (a^5x^6 + 5a^4bx^7 + 10a^3b^2x^8 + 10a^2b^3x^9 + 5ab^4x^{10} + b^5x^{11}) dx \\ &= \frac{a^5x^7}{7} + \frac{5}{8}a^4bx^8 + \frac{10}{9}a^3b^2x^9 + a^2b^3x^{10} + \frac{5}{11}ab^4x^{11} + \frac{b^5x^{12}}{12} \end{aligned}$$

Mathematica [A] time = 0.00, size = 66, normalized size = 1.00

$$\frac{a^5x^7}{7} + \frac{5}{8}a^4bx^8 + \frac{10}{9}a^3b^2x^9 + a^2b^3x^{10} + \frac{5}{11}ab^4x^{11} + \frac{b^5x^{12}}{12}$$

Antiderivative was successfully verified.

[In] Integrate[x^6*(a + b*x)^5,x]

[Out] (a^5*x^7)/7 + (5*a^4*b*x^8)/8 + (10*a^3*b^2*x^9)/9 + a^2*b^3*x^10 + (5*a*b^4*x^11)/11 + (b^5*x^12)/12

fricas [A] time = 0.50, size = 56, normalized size = 0.85

$$\frac{1}{12}x^{12}b^5 + \frac{5}{11}x^{11}b^4a + x^{10}b^3a^2 + \frac{10}{9}x^9b^2a^3 + \frac{5}{8}x^8ba^4 + \frac{1}{7}x^7a^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^5,x, algorithm="fricas")

[Out] 1/12*x^12*b^5 + 5/11*x^11*b^4*a + x^10*b^3*a^2 + 10/9*x^9*b^2*a^3 + 5/8*x^8*b*a^4 + 1/7*x^7*a^5

giac [A] time = 0.94, size = 56, normalized size = 0.85

$$\frac{1}{12}b^5x^{12} + \frac{5}{11}ab^4x^{11} + a^2b^3x^{10} + \frac{10}{9}a^3b^2x^9 + \frac{5}{8}a^4bx^8 + \frac{1}{7}a^5x^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^5,x, algorithm="giac")

[Out] 1/12*b^5*x^12 + 5/11*a*b^4*x^11 + a^2*b^3*x^10 + 10/9*a^3*b^2*x^9 + 5/8*a^4*b*x^8 + 1/7*a^5*x^7

maple [A] time = 0.01, size = 57, normalized size = 0.86

$$\frac{1}{12}b^5x^{12} + \frac{5}{11}ab^4x^{11} + a^2b^3x^{10} + \frac{10}{9}a^3b^2x^9 + \frac{5}{8}a^4bx^8 + \frac{1}{7}a^5x^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6*(b*x+a)^5,x)

[Out] 1/7*a^5*x^7+5/8*a^4*b*x^8+10/9*a^3*b^2*x^9+a^2*b^3*x^10+5/11*a*b^4*x^11+1/12*b^5*x^12

maxima [A] time = 1.38, size = 56, normalized size = 0.85

$$\frac{1}{12}b^5x^{12} + \frac{5}{11}ab^4x^{11} + a^2b^3x^{10} + \frac{10}{9}a^3b^2x^9 + \frac{5}{8}a^4bx^8 + \frac{1}{7}a^5x^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^5,x, algorithm="maxima")

[Out] $1/12*b^5*x^{12} + 5/11*a*b^4*x^{11} + a^2*b^3*x^{10} + 10/9*a^3*b^2*x^9 + 5/8*a^4*b*x^8 + 1/7*a^5*x^7$

mupad [B] time = 0.02, size = 56, normalized size = 0.85

$$\frac{a^5 x^7}{7} + \frac{5 a^4 b x^8}{8} + \frac{10 a^3 b^2 x^9}{9} + a^2 b^3 x^{10} + \frac{5 a b^4 x^{11}}{11} + \frac{b^5 x^{12}}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^6*(a + b*x)^5,x)`

[Out] $(a^5*x^7)/7 + (b^5*x^{12})/12 + (5*a^4*b*x^8)/8 + (5*a*b^4*x^{11})/11 + (10*a^3*b^2*x^9)/9 + a^2*b^3*x^{10}$

sympy [A] time = 0.09, size = 63, normalized size = 0.95

$$\frac{a^5 x^7}{7} + \frac{5 a^4 b x^8}{8} + \frac{10 a^3 b^2 x^9}{9} + a^2 b^3 x^{10} + \frac{5 a b^4 x^{11}}{11} + \frac{b^5 x^{12}}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**6*(b*x+a)**5,x)`

[Out] $a**5*x**7/7 + 5*a**4*b*x**8/8 + 10*a**3*b**2*x**9/9 + a**2*b**3*x**10 + 5*a*b**4*x**11/11 + b**5*x**12/12$

3.78 $\int x^5(a + bx)^5 dx$

Optimal. Leaf size=69

$$\frac{a^5x^6}{6} + \frac{5}{7}a^4bx^7 + \frac{5}{4}a^3b^2x^8 + \frac{10}{9}a^2b^3x^9 + \frac{1}{2}ab^4x^{10} + \frac{b^5x^{11}}{11}$$

[Out] $1/6*a^5*x^6+5/7*a^4*b*x^7+5/4*a^3*b^2*x^8+10/9*a^2*b^3*x^9+1/2*a*b^4*x^{10}+1/11*b^5*x^{11}$

Rubi [A] time = 0.03, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{10}{9}a^2b^3x^9 + \frac{5}{4}a^3b^2x^8 + \frac{5}{7}a^4bx^7 + \frac{a^5x^6}{6} + \frac{1}{2}ab^4x^{10} + \frac{b^5x^{11}}{11}$$

Antiderivative was successfully verified.

[In] Int[x^5*(a + b*x)^5,x]

[Out] $(a^5*x^6)/6 + (5*a^4*b*x^7)/7 + (5*a^3*b^2*x^8)/4 + (10*a^2*b^3*x^9)/9 + (a*b^4*x^{10})/2 + (b^5*x^{11})/11$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^5(a + bx)^5 dx &= \int (a^5x^5 + 5a^4bx^6 + 10a^3b^2x^7 + 10a^2b^3x^8 + 5ab^4x^9 + b^5x^{10}) dx \\ &= \frac{a^5x^6}{6} + \frac{5}{7}a^4bx^7 + \frac{5}{4}a^3b^2x^8 + \frac{10}{9}a^2b^3x^9 + \frac{1}{2}ab^4x^{10} + \frac{b^5x^{11}}{11} \end{aligned}$$

Mathematica [A] time = 0.00, size = 69, normalized size = 1.00

$$\frac{a^5x^6}{6} + \frac{5}{7}a^4bx^7 + \frac{5}{4}a^3b^2x^8 + \frac{10}{9}a^2b^3x^9 + \frac{1}{2}ab^4x^{10} + \frac{b^5x^{11}}{11}$$

Antiderivative was successfully verified.

[In] Integrate[x^5*(a + b*x)^5,x]

[Out] (a^5*x^6)/6 + (5*a^4*b*x^7)/7 + (5*a^3*b^2*x^8)/4 + (10*a^2*b^3*x^9)/9 + (a*b^4*x^10)/2 + (b^5*x^11)/11

fricas [A] time = 0.49, size = 57, normalized size = 0.83

$$\frac{1}{11}x^{11}b^5 + \frac{1}{2}x^{10}b^4a + \frac{10}{9}x^9b^3a^2 + \frac{5}{4}x^8b^2a^3 + \frac{5}{7}x^7ba^4 + \frac{1}{6}x^6a^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^5,x, algorithm="fricas")

[Out] 1/11*x^11*b^5 + 1/2*x^10*b^4*a + 10/9*x^9*b^3*a^2 + 5/4*x^8*b^2*a^3 + 5/7*x^7*b*a^4 + 1/6*x^6*a^5

giac [A] time = 1.20, size = 57, normalized size = 0.83

$$\frac{1}{11}b^5x^{11} + \frac{1}{2}ab^4x^{10} + \frac{10}{9}a^2b^3x^9 + \frac{5}{4}a^3b^2x^8 + \frac{5}{7}a^4bx^7 + \frac{1}{6}a^5x^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^5,x, algorithm="giac")

[Out] 1/11*b^5*x^11 + 1/2*a*b^4*x^10 + 10/9*a^2*b^3*x^9 + 5/4*a^3*b^2*x^8 + 5/7*a^4*b*x^7 + 1/6*a^5*x^6

maple [A] time = 0.00, size = 58, normalized size = 0.84

$$\frac{1}{11}b^5x^{11} + \frac{1}{2}ab^4x^{10} + \frac{10}{9}a^2b^3x^9 + \frac{5}{4}a^3b^2x^8 + \frac{5}{7}a^4bx^7 + \frac{1}{6}a^5x^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5*(b*x+a)^5,x)

[Out] 1/6*a^5*x^6+5/7*a^4*b*x^7+5/4*a^3*b^2*x^8+10/9*a^2*b^3*x^9+1/2*a*b^4*x^10+1/11*b^5*x^11

maxima [A] time = 1.36, size = 57, normalized size = 0.83

$$\frac{1}{11}b^5x^{11} + \frac{1}{2}ab^4x^{10} + \frac{10}{9}a^2b^3x^9 + \frac{5}{4}a^3b^2x^8 + \frac{5}{7}a^4bx^7 + \frac{1}{6}a^5x^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^5,x, algorithm="maxima")

[Out] $1/11*b^5*x^{11} + 1/2*a*b^4*x^{10} + 10/9*a^2*b^3*x^9 + 5/4*a^3*b^2*x^8 + 5/7*a^4*b*x^7 + 1/6*a^5*x^6$

mupad [B] time = 0.02, size = 57, normalized size = 0.83

$$\frac{a^5 x^6}{6} + \frac{5 a^4 b x^7}{7} + \frac{5 a^3 b^2 x^8}{4} + \frac{10 a^2 b^3 x^9}{9} + \frac{a b^4 x^{10}}{2} + \frac{b^5 x^{11}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^5*(a + b*x)^5,x)`

[Out] $(a^5*x^6)/6 + (b^5*x^{11})/11 + (5*a^4*b*x^7)/7 + (a*b^4*x^{10})/2 + (5*a^3*b^2*x^8)/4 + (10*a^2*b^3*x^9)/9$

sympy [A] time = 0.08, size = 65, normalized size = 0.94

$$\frac{a^5 x^6}{6} + \frac{5 a^4 b x^7}{7} + \frac{5 a^3 b^2 x^8}{4} + \frac{10 a^2 b^3 x^9}{9} + \frac{a b^4 x^{10}}{2} + \frac{b^5 x^{11}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**5*(b*x+a)**5,x)`

[Out] $a**5*x**6/6 + 5*a**4*b*x**7/7 + 5*a**3*b**2*x**8/4 + 10*a**2*b**3*x**9/9 + a*b**4*x**10/2 + b**5*x**11/11$

3.79 $\int x^4(a + bx)^5 dx$

Optimal. Leaf size=69

$$\frac{a^5x^5}{5} + \frac{5}{6}a^4bx^6 + \frac{10}{7}a^3b^2x^7 + \frac{5}{4}a^2b^3x^8 + \frac{5}{9}ab^4x^9 + \frac{b^5x^{10}}{10}$$

[Out] $1/5*a^5*x^5+5/6*a^4*b*x^6+10/7*a^3*b^2*x^7+5/4*a^2*b^3*x^8+5/9*a*b^4*x^9+1/10*b^5*x^{10}$

Rubi [A] time = 0.03, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{5}{4}a^2b^3x^8 + \frac{10}{7}a^3b^2x^7 + \frac{5}{6}a^4bx^6 + \frac{a^5x^5}{5} + \frac{5}{9}ab^4x^9 + \frac{b^5x^{10}}{10}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^4*(a + b*x)^5, x]$

[Out] $(a^5*x^5)/5 + (5*a^4*b*x^6)/6 + (10*a^3*b^2*x^7)/7 + (5*a^2*b^3*x^8)/4 + (5*a*b^4*x^9)/9 + (b^5*x^{10})/10$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^(m_.)*((c_.) + (d_.)*(x_.))^(n_.), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ $\text{FreeQ}\{a, b, c, d, n, x\} \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (\ !\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0]) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x^4(a + bx)^5 dx &= \int (a^5x^4 + 5a^4bx^5 + 10a^3b^2x^6 + 10a^2b^3x^7 + 5ab^4x^8 + b^5x^9) dx \\ &= \frac{a^5x^5}{5} + \frac{5}{6}a^4bx^6 + \frac{10}{7}a^3b^2x^7 + \frac{5}{4}a^2b^3x^8 + \frac{5}{9}ab^4x^9 + \frac{b^5x^{10}}{10} \end{aligned}$$

Mathematica [A] time = 0.00, size = 69, normalized size = 1.00

$$\frac{a^5x^5}{5} + \frac{5}{6}a^4bx^6 + \frac{10}{7}a^3b^2x^7 + \frac{5}{4}a^2b^3x^8 + \frac{5}{9}ab^4x^9 + \frac{b^5x^{10}}{10}$$

Antiderivative was successfully verified.

[In] Integrate[x^4*(a + b*x)^5,x]

[Out] (a^5*x^5)/5 + (5*a^4*b*x^6)/6 + (10*a^3*b^2*x^7)/7 + (5*a^2*b^3*x^8)/4 + (5*a*b^4*x^9)/9 + (b^5*x^10)/10

fricas [A] time = 0.41, size = 57, normalized size = 0.83

$$\frac{1}{10}x^{10}b^5 + \frac{5}{9}x^9b^4a + \frac{5}{4}x^8b^3a^2 + \frac{10}{7}x^7b^2a^3 + \frac{5}{6}x^6ba^4 + \frac{1}{5}x^5a^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^5,x, algorithm="fricas")

[Out] 1/10*x^10*b^5 + 5/9*x^9*b^4*a + 5/4*x^8*b^3*a^2 + 10/7*x^7*b^2*a^3 + 5/6*x^6*b*a^4 + 1/5*x^5*a^5

giac [A] time = 1.10, size = 57, normalized size = 0.83

$$\frac{1}{10}b^5x^{10} + \frac{5}{9}ab^4x^9 + \frac{5}{4}a^2b^3x^8 + \frac{10}{7}a^3b^2x^7 + \frac{5}{6}a^4bx^6 + \frac{1}{5}a^5x^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^5,x, algorithm="giac")

[Out] 1/10*b^5*x^10 + 5/9*a*b^4*x^9 + 5/4*a^2*b^3*x^8 + 10/7*a^3*b^2*x^7 + 5/6*a^4*b*x^6 + 1/5*a^5*x^5

maple [A] time = 0.00, size = 58, normalized size = 0.84

$$\frac{1}{10}b^5x^{10} + \frac{5}{9}ab^4x^9 + \frac{5}{4}a^2b^3x^8 + \frac{10}{7}a^3b^2x^7 + \frac{5}{6}a^4bx^6 + \frac{1}{5}a^5x^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*(b*x+a)^5,x)

[Out] 1/5*a^5*x^5+5/6*a^4*b*x^6+10/7*a^3*b^2*x^7+5/4*a^2*b^3*x^8+5/9*a*b^4*x^9+1/10*b^5*x^10

maxima [A] time = 1.47, size = 57, normalized size = 0.83

$$\frac{1}{10}b^5x^{10} + \frac{5}{9}ab^4x^9 + \frac{5}{4}a^2b^3x^8 + \frac{10}{7}a^3b^2x^7 + \frac{5}{6}a^4bx^6 + \frac{1}{5}a^5x^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^5,x, algorithm="maxima")

[Out] $1/10*b^5*x^{10} + 5/9*a*b^4*x^9 + 5/4*a^2*b^3*x^8 + 10/7*a^3*b^2*x^7 + 5/6*a^4*b*x^6 + 1/5*a^5*x^5$

mupad [B] time = 0.02, size = 57, normalized size = 0.83

$$\frac{a^5 x^5}{5} + \frac{5 a^4 b x^6}{6} + \frac{10 a^3 b^2 x^7}{7} + \frac{5 a^2 b^3 x^8}{4} + \frac{5 a b^4 x^9}{9} + \frac{b^5 x^{10}}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^4*(a + b*x)^5,x)`

[Out] $(a^5*x^5)/5 + (b^5*x^{10})/10 + (5*a^4*b*x^6)/6 + (5*a*b^4*x^9)/9 + (10*a^3*b^2*x^7)/7 + (5*a^2*b^3*x^8)/4$

sympy [A] time = 0.08, size = 66, normalized size = 0.96

$$\frac{a^5 x^5}{5} + \frac{5 a^4 b x^6}{6} + \frac{10 a^3 b^2 x^7}{7} + \frac{5 a^2 b^3 x^8}{4} + \frac{5 a b^4 x^9}{9} + \frac{b^5 x^{10}}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**4*(b*x+a)**5,x)`

[Out] $a**5*x**5/5 + 5*a**4*b*x**6/6 + 10*a**3*b**2*x**7/7 + 5*a**2*b**3*x**8/4 + 5*a*b**4*x**9/9 + b**5*x**10/10$

3.80 $\int x^3(a + bx)^5 dx$

Optimal. Leaf size=64

$$-\frac{a^3(a + bx)^6}{6b^4} + \frac{3a^2(a + bx)^7}{7b^4} + \frac{(a + bx)^9}{9b^4} - \frac{3a(a + bx)^8}{8b^4}$$

[Out] $-1/6*a^3*(b*x+a)^6/b^4+3/7*a^2*(b*x+a)^7/b^4-3/8*a*(b*x+a)^8/b^4+1/9*(b*x+a)^9/b^4$

Rubi [A] time = 0.03, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3a^2(a + bx)^7}{7b^4} - \frac{a^3(a + bx)^6}{6b^4} + \frac{(a + bx)^9}{9b^4} - \frac{3a(a + bx)^8}{8b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^5, x]

[Out] $-(a^3*(a + b*x)^6)/(6*b^4) + (3*a^2*(a + b*x)^7)/(7*b^4) - (3*a*(a + b*x)^8)/(8*b^4) + (a + b*x)^9/(9*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^5 dx &= \int \left(-\frac{a^3(a + bx)^5}{b^3} + \frac{3a^2(a + bx)^6}{b^3} - \frac{3a(a + bx)^7}{b^3} + \frac{(a + bx)^8}{b^3} \right) dx \\ &= -\frac{a^3(a + bx)^6}{6b^4} + \frac{3a^2(a + bx)^7}{7b^4} - \frac{3a(a + bx)^8}{8b^4} + \frac{(a + bx)^9}{9b^4} \end{aligned}$$

Mathematica [A] time = 0.00, size = 66, normalized size = 1.03

$$\frac{a^5 x^4}{4} + a^4 b x^5 + \frac{5}{3} a^3 b^2 x^6 + \frac{10}{7} a^2 b^3 x^7 + \frac{5}{8} a b^4 x^8 + \frac{b^5 x^9}{9}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^5,x]

[Out] (a^5*x^4)/4 + a^4*b*x^5 + (5*a^3*b^2*x^6)/3 + (10*a^2*b^3*x^7)/7 + (5*a*b^4*x^8)/8 + (b^5*x^9)/9

fricas [A] time = 0.40, size = 56, normalized size = 0.88

$$\frac{1}{9}x^9b^5 + \frac{5}{8}x^8b^4a + \frac{10}{7}x^7b^3a^2 + \frac{5}{3}x^6b^2a^3 + x^5ba^4 + \frac{1}{4}x^4a^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^5,x, algorithm="fricas")

[Out] 1/9*x^9*b^5 + 5/8*x^8*b^4*a + 10/7*x^7*b^3*a^2 + 5/3*x^6*b^2*a^3 + x^5*b*a^4 + 1/4*x^4*a^5

giac [A] time = 1.05, size = 56, normalized size = 0.88

$$\frac{1}{9}b^5x^9 + \frac{5}{8}ab^4x^8 + \frac{10}{7}a^2b^3x^7 + \frac{5}{3}a^3b^2x^6 + a^4bx^5 + \frac{1}{4}a^5x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^5,x, algorithm="giac")

[Out] 1/9*b^5*x^9 + 5/8*a*b^4*x^8 + 10/7*a^2*b^3*x^7 + 5/3*a^3*b^2*x^6 + a^4*b*x^5 + 1/4*a^5*x^4

maple [A] time = 0.00, size = 57, normalized size = 0.89

$$\frac{1}{9}b^5x^9 + \frac{5}{8}ab^4x^8 + \frac{10}{7}a^2b^3x^7 + \frac{5}{3}a^3b^2x^6 + a^4bx^5 + \frac{1}{4}a^5x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^5,x)

[Out] 1/9*b^5*x^9+5/8*a*b^4*x^8+10/7*a^2*b^3*x^7+5/3*a^3*b^2*x^6+a^4*b*x^5+1/4*a^5*x^4

maxima [A] time = 1.40, size = 56, normalized size = 0.88

$$\frac{1}{9}b^5x^9 + \frac{5}{8}ab^4x^8 + \frac{10}{7}a^2b^3x^7 + \frac{5}{3}a^3b^2x^6 + a^4bx^5 + \frac{1}{4}a^5x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^5,x, algorithm="maxima")

[Out] $\frac{1}{9}b^5x^9 + \frac{5}{8}a*b^4x^8 + \frac{10}{7}a^2*b^3x^7 + \frac{5}{3}a^3*b^2x^6 + a^4*b*x^5 + \frac{1}{4}a^5x^4$

mupad [B] time = 0.02, size = 56, normalized size = 0.88

$$\frac{a^5 x^4}{4} + a^4 b x^5 + \frac{5 a^3 b^2 x^6}{3} + \frac{10 a^2 b^3 x^7}{7} + \frac{5 a b^4 x^8}{8} + \frac{b^5 x^9}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(a + b*x)^5,x)

[Out] $(a^5x^4)/4 + (b^5x^9)/9 + a^4*b*x^5 + (5*a*b^4*x^8)/8 + (5*a^3*b^2*x^6)/3 + (10*a^2*b^3*x^7)/7$

sympy [A] time = 0.10, size = 63, normalized size = 0.98

$$\frac{a^5 x^4}{4} + a^4 b x^5 + \frac{5 a^3 b^2 x^6}{3} + \frac{10 a^2 b^3 x^7}{7} + \frac{5 a b^4 x^8}{8} + \frac{b^5 x^9}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**5,x)

[Out] $a**5*x**4/4 + a**4*b*x**5 + 5*a**3*b**2*x**6/3 + 10*a**2*b**3*x**7/7 + 5*a*b**4*x**8/8 + b**5*x**9/9$

3.81 $\int x^2(a + bx)^5 dx$

Optimal. Leaf size=47

$$\frac{a^2(a + bx)^6}{6b^3} + \frac{(a + bx)^8}{8b^3} - \frac{2a(a + bx)^7}{7b^3}$$

[Out] $1/6*a^2*(b*x+a)^6/b^3-2/7*a*(b*x+a)^7/b^3+1/8*(b*x+a)^8/b^3$

Rubi [A] time = 0.02, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2(a + bx)^6}{6b^3} + \frac{(a + bx)^8}{8b^3} - \frac{2a(a + bx)^7}{7b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*x)^5,x]

[Out] $(a^2*(a + b*x)^6)/(6*b^3) - (2*a*(a + b*x)^7)/(7*b^3) + (a + b*x)^8/(8*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^5 dx &= \int \left(\frac{a^2(a + bx)^5}{b^2} - \frac{2a(a + bx)^6}{b^2} + \frac{(a + bx)^7}{b^2} \right) dx \\ &= \frac{a^2(a + bx)^6}{6b^3} - \frac{2a(a + bx)^7}{7b^3} + \frac{(a + bx)^8}{8b^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 67, normalized size = 1.43

$$\frac{a^5 x^3}{3} + \frac{5}{4} a^4 b x^4 + 2 a^3 b^2 x^5 + \frac{5}{3} a^2 b^3 x^6 + \frac{5}{7} a b^4 x^7 + \frac{b^5 x^8}{8}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^5,x]

[Out] $(a^5*x^3)/3 + (5*a^4*b*x^4)/4 + 2*a^3*b^2*x^5 + (5*a^2*b^3*x^6)/3 + (5*a*b^4*x^7)/7 + (b^5*x^8)/8$

fricas [A] time = 0.41, size = 57, normalized size = 1.21

$$\frac{1}{8}x^8b^5 + \frac{5}{7}x^7b^4a + \frac{5}{3}x^6b^3a^2 + 2x^5b^2a^3 + \frac{5}{4}x^4ba^4 + \frac{1}{3}x^3a^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^5,x, algorithm="fricas")

[Out] $1/8*x^8*b^5 + 5/7*x^7*b^4*a + 5/3*x^6*b^3*a^2 + 2*x^5*b^2*a^3 + 5/4*x^4*b*a^4 + 1/3*x^3*a^5$

giac [A] time = 1.71, size = 57, normalized size = 1.21

$$\frac{1}{8}b^5x^8 + \frac{5}{7}ab^4x^7 + \frac{5}{3}a^2b^3x^6 + 2a^3b^2x^5 + \frac{5}{4}a^4bx^4 + \frac{1}{3}a^5x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^5,x, algorithm="giac")

[Out] $1/8*b^5*x^8 + 5/7*a*b^4*x^7 + 5/3*a^2*b^3*x^6 + 2*a^3*b^2*x^5 + 5/4*a^4*b*x^4 + 1/3*a^5*x^3$

maple [A] time = 0.00, size = 58, normalized size = 1.23

$$\frac{1}{8}b^5x^8 + \frac{5}{7}ab^4x^7 + \frac{5}{3}a^2b^3x^6 + 2a^3b^2x^5 + \frac{5}{4}a^4bx^4 + \frac{1}{3}a^5x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^5,x)

[Out] $1/8*b^5*x^8+5/7*a*b^4*x^7+5/3*a^2*b^3*x^6+2*a^3*b^2*x^5+5/4*a^4*b*x^4+1/3*a^5*x^3$

maxima [A] time = 1.32, size = 57, normalized size = 1.21

$$\frac{1}{8}b^5x^8 + \frac{5}{7}ab^4x^7 + \frac{5}{3}a^2b^3x^6 + 2a^3b^2x^5 + \frac{5}{4}a^4bx^4 + \frac{1}{3}a^5x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^5,x, algorithm="maxima")

[Out] $\frac{1}{8}b^5x^8 + \frac{5}{7}ab^4x^7 + \frac{5}{3}a^2b^3x^6 + 2a^3b^2x^5 + \frac{5}{4}a^4bx^4 + \frac{1}{3}a^5x^3$

mupad [B] time = 0.02, size = 57, normalized size = 1.21

$$\frac{a^5x^3}{3} + \frac{5a^4bx^4}{4} + 2a^3b^2x^5 + \frac{5a^2b^3x^6}{3} + \frac{5ab^4x^7}{7} + \frac{b^5x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(a + b*x)^5,x)`

[Out] $(a^5x^3)/3 + (b^5x^8)/8 + (5a^4bx^4)/4 + (5a^3b^2x^5)/3 + (5a^2b^3x^6)/3 + (5ab^4x^7)/7 + 2a^3b^2x^5$

sympy [A] time = 0.08, size = 65, normalized size = 1.38

$$\frac{a^5x^3}{3} + \frac{5a^4bx^4}{4} + 2a^3b^2x^5 + \frac{5a^2b^3x^6}{3} + \frac{5ab^4x^7}{7} + \frac{b^5x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(b*x+a)**5,x)`

[Out] $a**5*x**3/3 + 5*a**4*b*x**4/4 + 2*a**3*b**2*x**5 + 5*a**2*b**3*x**6/3 + 5*a**b**4*x**7/7 + b**5*x**8/8$

3.82 $\int x(a + bx)^5 dx$

Optimal. Leaf size=30

$$\frac{(a + bx)^7}{7b^2} - \frac{a(a + bx)^6}{6b^2}$$

[Out] $-1/6*a*(b*x+a)^6/b^2+1/7*(b*x+a)^7/b^2$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{(a + bx)^7}{7b^2} - \frac{a(a + bx)^6}{6b^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^5,x]

[Out] $-(a*(a + b*x)^6)/(6*b^2) + (a + b*x)^7/(7*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int x(a + bx)^5 dx &= \int \left(-\frac{a(a + bx)^5}{b} + \frac{(a + bx)^6}{b} \right) dx \\ &= -\frac{a(a + bx)^6}{6b^2} + \frac{(a + bx)^7}{7b^2} \end{aligned}$$

Mathematica [B] time = 0.00, size = 67, normalized size = 2.23

$$\frac{a^5 x^2}{2} + \frac{5}{3} a^4 b x^3 + \frac{5}{2} a^3 b^2 x^4 + 2 a^2 b^3 x^5 + \frac{5}{6} a b^4 x^6 + \frac{b^5 x^7}{7}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^5,x]

[Out] $(a^5x^2)/2 + (5a^4bx^3)/3 + (5a^3b^2x^4)/2 + 2a^2b^3x^5 + (5ab^4x^6)/6 + (b^5x^7)/7$

fricas [B] time = 0.40, size = 57, normalized size = 1.90

$$\frac{1}{7}x^7b^5 + \frac{5}{6}x^6b^4a + 2x^5b^3a^2 + \frac{5}{2}x^4b^2a^3 + \frac{5}{3}x^3ba^4 + \frac{1}{2}x^2a^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^5,x, algorithm="fricas")

[Out] $1/7*x^7*b^5 + 5/6*x^6*b^4*a + 2*x^5*b^3*a^2 + 5/2*x^4*b^2*a^3 + 5/3*x^3*b*a^4 + 1/2*x^2*a^5$

giac [B] time = 0.93, size = 57, normalized size = 1.90

$$\frac{1}{7}b^5x^7 + \frac{5}{6}ab^4x^6 + 2a^2b^3x^5 + \frac{5}{2}a^3b^2x^4 + \frac{5}{3}a^4bx^3 + \frac{1}{2}a^5x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^5,x, algorithm="giac")

[Out] $1/7*b^5*x^7 + 5/6*a*b^4*x^6 + 2*a^2*b^3*x^5 + 5/2*a^3*b^2*x^4 + 5/3*a^4*b*x^3 + 1/2*a^5*x^2$

maple [B] time = 0.00, size = 58, normalized size = 1.93

$$\frac{1}{7}b^5x^7 + \frac{5}{6}ab^4x^6 + 2a^2b^3x^5 + \frac{5}{2}a^3b^2x^4 + \frac{5}{3}a^4bx^3 + \frac{1}{2}a^5x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^5,x)

[Out] $1/7*b^5*x^7+5/6*a*b^4*x^6+2*a^2*b^3*x^5+5/2*a^3*b^2*x^4+5/3*a^4*b*x^3+1/2*a^5*x^2$

maxima [B] time = 1.31, size = 57, normalized size = 1.90

$$\frac{1}{7}b^5x^7 + \frac{5}{6}ab^4x^6 + 2a^2b^3x^5 + \frac{5}{2}a^3b^2x^4 + \frac{5}{3}a^4bx^3 + \frac{1}{2}a^5x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^5,x, algorithm="maxima")

[Out] $1/7*b^5*x^7 + 5/6*a*b^4*x^6 + 2*a^2*b^3*x^5 + 5/2*a^3*b^2*x^4 + 5/3*a^4*b*x^3 + 1/2*a^5*x^2$

mupad [B] time = 0.02, size = 57, normalized size = 1.90

$$\frac{a^5 x^2}{2} + \frac{5 a^4 b x^3}{3} + \frac{5 a^3 b^2 x^4}{2} + 2 a^2 b^3 x^5 + \frac{5 a b^4 x^6}{6} + \frac{b^5 x^7}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(a + b*x)^5,x)`

[Out] $(a^5*x^2)/2 + (b^5*x^7)/7 + (5*a^4*b*x^3)/3 + (5*a*b^4*x^6)/6 + (5*a^3*b^2*x^4)/2 + 2*a^2*b^3*x^5$

sympy [B] time = 0.08, size = 65, normalized size = 2.17

$$\frac{a^5 x^2}{2} + \frac{5 a^4 b x^3}{3} + \frac{5 a^3 b^2 x^4}{2} + 2 a^2 b^3 x^5 + \frac{5 a b^4 x^6}{6} + \frac{b^5 x^7}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**5,x)`

[Out] $a**5*x**2/2 + 5*a**4*b*x**3/3 + 5*a**3*b**2*x**4/2 + 2*a**2*b**3*x**5 + 5*a*b**4*x**6/6 + b**5*x**7/7$

3.83 $\int (a + bx)^5 dx$

Optimal. Leaf size=14

$$\frac{(a + bx)^6}{6b}$$

[Out] 1/6*(b*x+a)^6/b

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(a + bx)^6}{6b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5,x]

[Out] (a + b*x)^6/(6*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^5 dx = \frac{(a + bx)^6}{6b}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{(a + bx)^6}{6b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5,x]

[Out] (a + b*x)^6/(6*b)

fricas [B] time = 0.41, size = 53, normalized size = 3.79

$$\frac{1}{6}x^6b^5 + x^5b^4a + \frac{5}{2}x^4b^3a^2 + \frac{10}{3}x^3b^2a^3 + \frac{5}{2}x^2ba^4 + xa^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5,x, algorithm="fricas")

[Out] $\frac{1}{6}x^6b^5 + x^5b^4a + \frac{5}{2}x^4b^3a^2 + \frac{10}{3}x^3b^2a^3 + \frac{5}{2}x^2ba^4 + xa^5$

giac [A] time = 1.20, size = 12, normalized size = 0.86

$$\frac{(bx + a)^6}{6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5,x, algorithm="giac")

[Out] $\frac{1}{6}(bx + a)^6/b$

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{(bx + a)^6}{6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5,x)

[Out] $\frac{1}{6}(bx+a)^6/b$

maxima [B] time = 1.37, size = 53, normalized size = 3.79

$$\frac{1}{6}b^5x^6 + ab^4x^5 + \frac{5}{2}a^2b^3x^4 + \frac{10}{3}a^3b^2x^3 + \frac{5}{2}a^4bx^2 + a^5x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5,x, algorithm="maxima")

[Out] $\frac{1}{6}b^5x^6 + a^5x + \frac{5}{2}a^4bx^2 + \frac{10}{3}a^3b^2x^3 + \frac{5}{2}a^2b^3x^4 + ab^4x^5$

mupad [B] time = 0.02, size = 53, normalized size = 3.79

$$a^5x + \frac{5a^4bx^2}{2} + \frac{10a^3b^2x^3}{3} + \frac{5a^2b^3x^4}{2} + ab^4x^5 + \frac{b^5x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5,x)

[Out] $a^5x + (b^5x^6)/6 + (5a^4bx^2)/2 + ab^4x^5 + (10a^3b^2x^3)/3 + (5a^2b^3x^4)/2$

sympy [B] time = 0.08, size = 60, normalized size = 4.29

$$a^5x + \frac{5a^4bx^2}{2} + \frac{10a^3b^2x^3}{3} + \frac{5a^2b^3x^4}{2} + ab^4x^5 + \frac{b^5x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5,x)

[Out] $a**5*x + 5*a**4*b*x**2/2 + 10*a**3*b**2*x**3/3 + 5*a**2*b**3*x**4/2 + a*b**4*x**5 + b**5*x**6/6$

$$3.84 \quad \int \frac{(a+bx)^5}{x} dx$$

Optimal. Leaf size=59

$$a^5 \log(x) + 5a^4bx + 5a^3b^2x^2 + \frac{10}{3}a^2b^3x^3 + \frac{5}{4}ab^4x^4 + \frac{b^5x^5}{5}$$

[Out] 5*a^4*b*x+5*a^3*b^2*x^2+10/3*a^2*b^3*x^3+5/4*a*b^4*x^4+1/5*b^5*x^5+a^5*ln(x)

Rubi [A] time = 0.02, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$5a^3b^2x^2 + \frac{10}{3}a^2b^3x^3 + 5a^4bx + a^5 \log(x) + \frac{5}{4}ab^4x^4 + \frac{b^5x^5}{5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x, x]

[Out] 5*a^4*b*x + 5*a^3*b^2*x^2 + (10*a^2*b^3*x^3)/3 + (5*a*b^4*x^4)/4 + (b^5*x^5)/5 + a^5*Log[x]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x} dx &= \int \left(5a^4b + \frac{a^5}{x} + 10a^3b^2x + 10a^2b^3x^2 + 5ab^4x^3 + b^5x^4 \right) dx \\ &= 5a^4bx + 5a^3b^2x^2 + \frac{10}{3}a^2b^3x^3 + \frac{5}{4}ab^4x^4 + \frac{b^5x^5}{5} + a^5 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 59, normalized size = 1.00

$$a^5 \log(x) + 5a^4bx + 5a^3b^2x^2 + \frac{10}{3}a^2b^3x^3 + \frac{5}{4}ab^4x^4 + \frac{b^5x^5}{5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x, x]

[Out] $5*a^4*b*x + 5*a^3*b^2*x^2 + (10*a^2*b^3*x^3)/3 + (5*a*b^4*x^4)/4 + (b^5*x^5)/5 + a^5*\text{Log}[x]$

fricas [A] time = 0.44, size = 53, normalized size = 0.90

$$\frac{1}{5}b^5x^5 + \frac{5}{4}ab^4x^4 + \frac{10}{3}a^2b^3x^3 + 5a^3b^2x^2 + 5a^4bx + a^5\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x, x, algorithm="fricas")

[Out] $1/5*b^5*x^5 + 5/4*a*b^4*x^4 + 10/3*a^2*b^3*x^3 + 5*a^3*b^2*x^2 + 5*a^4*b*x + a^5*\log(x)$

giac [A] time = 1.12, size = 54, normalized size = 0.92

$$\frac{1}{5}b^5x^5 + \frac{5}{4}ab^4x^4 + \frac{10}{3}a^2b^3x^3 + 5a^3b^2x^2 + 5a^4bx + a^5\log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x, x, algorithm="giac")

[Out] $1/5*b^5*x^5 + 5/4*a*b^4*x^4 + 10/3*a^2*b^3*x^3 + 5*a^3*b^2*x^2 + 5*a^4*b*x + a^5*\log(\text{abs}(x))$

maple [A] time = 0.00, size = 54, normalized size = 0.92

$$\frac{b^5x^5}{5} + \frac{5ab^4x^4}{4} + \frac{10a^2b^3x^3}{3} + 5a^3b^2x^2 + a^5\ln(x) + 5a^4bx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x, x)

[Out] $5*a^4*b*x + 5*a^3*b^2*x^2 + 10/3*a^2*b^3*x^3 + 5/4*a*b^4*x^4 + 1/5*b^5*x^5 + a^5*\ln(x)$

maxima [A] time = 1.37, size = 53, normalized size = 0.90

$$\frac{1}{5}b^5x^5 + \frac{5}{4}ab^4x^4 + \frac{10}{3}a^2b^3x^3 + 5a^3b^2x^2 + 5a^4bx + a^5\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x,x, algorithm="maxima")

[Out] $1/5*b^5*x^5 + 5/4*a*b^4*x^4 + 10/3*a^2*b^3*x^3 + 5*a^3*b^2*x^2 + 5*a^4*b*x + a^5*\log(x)$

mupad [B] time = 0.03, size = 53, normalized size = 0.90

$$a^5 \ln(x) + \frac{b^5 x^5}{5} + \frac{5 a b^4 x^4}{4} + 5 a^3 b^2 x^2 + \frac{10 a^2 b^3 x^3}{3} + 5 a^4 b x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x,x)

[Out] $a^5*\log(x) + (b^5*x^5)/5 + (5*a*b^4*x^4)/4 + 5*a^3*b^2*x^2 + (10*a^2*b^3*x^3)/3 + 5*a^4*b*x$

sympy [A] time = 0.15, size = 60, normalized size = 1.02

$$a^5 \log(x) + 5a^4bx + 5a^3b^2x^2 + \frac{10a^2b^3x^3}{3} + \frac{5ab^4x^4}{4} + \frac{b^5x^5}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x,x)

[Out] $a**5*\log(x) + 5*a**4*b*x + 5*a**3*b**2*x**2 + 10*a**2*b**3*x**3/3 + 5*a*b**4*x**4/4 + b**5*x**5/5$

$$3.85 \quad \int \frac{(a+bx)^5}{x^2} dx$$

Optimal. Leaf size=58

$$-\frac{a^5}{x} + 5a^4b \log(x) + 10a^3b^2x + 5a^2b^3x^2 + \frac{5}{3}ab^4x^3 + \frac{b^5x^4}{4}$$

[Out] $-a^5/x+10*a^3*b^2*x+5*a^2*b^3*x^2+5/3*a*b^4*x^3+1/4*b^5*x^4+5*a^4*b*\ln(x)$

Rubi [A] time = 0.02, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$5a^2b^3x^2 + 10a^3b^2x + 5a^4b \log(x) - \frac{a^5}{x} + \frac{5}{3}ab^4x^3 + \frac{b^5x^4}{4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^2, x]

[Out] $-(a^5/x) + 10*a^3*b^2*x + 5*a^2*b^3*x^2 + (5*a*b^4*x^3)/3 + (b^5*x^4)/4 + 5*a^4*b*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^2} dx &= \int \left(10a^3b^2 + \frac{a^5}{x^2} + \frac{5a^4b}{x} + 10a^2b^3x + 5ab^4x^2 + b^5x^3 \right) dx \\ &= -\frac{a^5}{x} + 10a^3b^2x + 5a^2b^3x^2 + \frac{5}{3}ab^4x^3 + \frac{b^5x^4}{4} + 5a^4b \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 58, normalized size = 1.00

$$-\frac{a^5}{x} + 5a^4b \log(x) + 10a^3b^2x + 5a^2b^3x^2 + \frac{5}{3}ab^4x^3 + \frac{b^5x^4}{4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^2,x]

[Out] $-(a^5/x) + 10a^3b^2x + 5a^2b^3x^2 + (5ab^4x^3)/3 + (b^5x^4)/4 + 5a^4b \operatorname{Log}[x]$

fricas [A] time = 0.47, size = 59, normalized size = 1.02

$$\frac{3b^5x^5 + 20ab^4x^4 + 60a^2b^3x^3 + 120a^3b^2x^2 + 60a^4bx \log(x) - 12a^5}{12x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^2,x, algorithm="fricas")

[Out] $1/12*(3b^5x^5 + 20a*b^4x^4 + 60a^2b^3x^3 + 120a^3b^2x^2 + 60a^4*b*x*\log(x) - 12a^5)/x$

giac [A] time = 1.28, size = 55, normalized size = 0.95

$$\frac{1}{4}b^5x^4 + \frac{5}{3}ab^4x^3 + 5a^2b^3x^2 + 10a^3b^2x + 5a^4b \log(|x|) - \frac{a^5}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^2,x, algorithm="giac")

[Out] $1/4*b^5*x^4 + 5/3*a*b^4*x^3 + 5*a^2*b^3*x^2 + 10*a^3*b^2*x + 5*a^4*b*\log(\operatorname{abs}(x)) - a^5/x$

maple [A] time = 0.01, size = 55, normalized size = 0.95

$$\frac{b^5x^4}{4} + \frac{5ab^4x^3}{3} + 5a^2b^3x^2 + 5a^4b \ln(x) + 10a^3b^2x - \frac{a^5}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^2,x)

[Out] $-a^5/x + 10a^3b^2x + 5a^2b^3x^2 + 5/3ab^4x^3 + 1/4b^5x^4 + 5a^4b \ln(x)$

maxima [A] time = 1.40, size = 54, normalized size = 0.93

$$\frac{1}{4}b^5x^4 + \frac{5}{3}ab^4x^3 + 5a^2b^3x^2 + 10a^3b^2x + 5a^4b \log(x) - \frac{a^5}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^2,x, algorithm="maxima")

[Out] $\frac{1}{4}b^5x^4 + \frac{5}{3}ab^4x^3 + 5a^2b^3x^2 + 10a^3b^2x + 5a^4b\log(x) - a^5/x$

mupad [B] time = 0.03, size = 54, normalized size = 0.93

$$\frac{b^5 x^4}{4} - \frac{a^5}{x} + 10 a^3 b^2 x + \frac{5 a b^4 x^3}{3} + 5 a^4 b \ln(x) + 5 a^2 b^3 x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/x^2,x)`

[Out] $(b^5x^4)/4 - a^5/x + 10a^3b^2x + (5ab^4x^3)/3 + 5a^4b\log(x) + 5a^2b^3x^2$

sympy [A] time = 0.18, size = 56, normalized size = 0.97

$$-\frac{a^5}{x} + 5a^4b \log(x) + 10a^3b^2x + 5a^2b^3x^2 + \frac{5ab^4x^3}{3} + \frac{b^5x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/x**2,x)`

[Out] $-a**5/x + 5*a**4*b*\log(x) + 10*a**3*b**2*x + 5*a**2*b**3*x**2 + 5*a*b**4*x**3/3 + b**5*x**4/4$

$$3.86 \quad \int \frac{(a+bx)^5}{x^3} dx$$

Optimal. Leaf size=60

$$-\frac{a^5}{2x^2} - \frac{5a^4b}{x} + 10a^3b^2 \log(x) + 10a^2b^3x + \frac{5}{2}ab^4x^2 + \frac{b^5x^3}{3}$$

[Out] $-1/2*a^5/x^2-5*a^4*b/x+10*a^2*b^3*x+5/2*a*b^4*x^2+1/3*b^5*x^3+10*a^3*b^2*\ln(x)$

Rubi [A] time = 0.02, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$10a^2b^3x + 10a^3b^2 \log(x) - \frac{5a^4b}{x} - \frac{a^5}{2x^2} + \frac{5}{2}ab^4x^2 + \frac{b^5x^3}{3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^3, x]

[Out] $-a^5/(2*x^2) - (5*a^4*b)/x + 10*a^2*b^3*x + (5*a*b^4*x^2)/2 + (b^5*x^3)/3 + 10*a^3*b^2*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^3} dx &= \int \left(10a^2b^3 + \frac{a^5}{x^3} + \frac{5a^4b}{x^2} + \frac{10a^3b^2}{x} + 5ab^4x + b^5x^2 \right) dx \\ &= -\frac{a^5}{2x^2} - \frac{5a^4b}{x} + 10a^2b^3x + \frac{5}{2}ab^4x^2 + \frac{b^5x^3}{3} + 10a^3b^2 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 60, normalized size = 1.00

$$-\frac{a^5}{2x^2} - \frac{5a^4b}{x} + 10a^3b^2 \log(x) + 10a^2b^3x + \frac{5}{2}ab^4x^2 + \frac{b^5x^3}{3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^3,x]

[Out] $-1/2*a^5/x^2 - (5*a^4*b)/x + 10*a^2*b^3*x + (5*a*b^4*x^2)/2 + (b^5*x^3)/3 + 10*a^3*b^2*\text{Log}[x]$

fricas [A] time = 0.45, size = 59, normalized size = 0.98

$$\frac{2b^5x^5 + 15ab^4x^4 + 60a^2b^3x^3 + 60a^3b^2x^2 \log(x) - 30a^4bx - 3a^5}{6x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^3,x, algorithm="fricas")

[Out] $1/6*(2*b^5*x^5 + 15*a*b^4*x^4 + 60*a^2*b^3*x^3 + 60*a^3*b^2*x^2*\log(x) - 30*a^4*b*x - 3*a^5)/x^2$

giac [A] time = 1.19, size = 54, normalized size = 0.90

$$\frac{1}{3}b^5x^3 + \frac{5}{2}ab^4x^2 + 10a^2b^3x + 10a^3b^2 \log(|x|) - \frac{10a^4bx + a^5}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^3,x, algorithm="giac")

[Out] $1/3*b^5*x^3 + 5/2*a*b^4*x^2 + 10*a^2*b^3*x + 10*a^3*b^2*\log(\text{abs}(x)) - 1/2*(10*a^4*b*x + a^5)/x^2$

maple [A] time = 0.00, size = 55, normalized size = 0.92

$$\frac{b^5x^3}{3} + \frac{5ab^4x^2}{2} + 10a^3b^2 \ln(x) + 10a^2b^3x - \frac{5a^4b}{x} - \frac{a^5}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^3,x)

[Out] $-1/2*a^5/x^2 - 5*a^4*b/x + 10*a^2*b^3*x + 5/2*a*b^4*x^2 + 1/3*b^5*x^3 + 10*a^3*b^2*\ln(x)$

maxima [A] time = 1.36, size = 53, normalized size = 0.88

$$\frac{1}{3}b^5x^3 + \frac{5}{2}ab^4x^2 + 10a^2b^3x + 10a^3b^2 \log(x) - \frac{10a^4bx + a^5}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^3,x, algorithm="maxima")

[Out] $\frac{1}{3}b^5x^3 + \frac{5}{2}ab^4x^2 + 10a^2b^3x + 10a^3b^2\log(x) - \frac{1}{2}(10a^4bx + a^5)/x^2$

mupad [B] time = 0.03, size = 55, normalized size = 0.92

$$\frac{b^5 x^3}{3} - \frac{\frac{a^5}{2} + 5 b x a^4}{x^2} + 10 a^2 b^3 x + \frac{5 a b^4 x^2}{2} + 10 a^3 b^2 \ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^3,x)

[Out] $(b^5x^3)/3 - (a^5/2 + 5a^4bx)/x^2 + 10a^2b^3x + (5ab^4x^2)/2 + 10a^3b^2\log(x)$

sympy [A] time = 0.20, size = 60, normalized size = 1.00

$$10a^3b^2 \log(x) + 10a^2b^3x + \frac{5ab^4x^2}{2} + \frac{b^5x^3}{3} + \frac{-a^5 - 10a^4bx}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**3,x)

[Out] $10a**3*b**2*\log(x) + 10a**2*b**3*x + 5*a*b**4*x**2/2 + b**5*x**3/3 + (-a**5 - 10*a**4*b*x)/(2*x**2)$

$$3.87 \quad \int \frac{(a+bx)^5}{x^4} dx$$

Optimal. Leaf size=60

$$-\frac{a^5}{3x^3} - \frac{5a^4b}{2x^2} - \frac{10a^3b^2}{x} + 10a^2b^3 \log(x) + 5ab^4x + \frac{b^5x^2}{2}$$

[Out] $-1/3*a^5/x^3-5/2*a^4*b/x^2-10*a^3*b^2/x+5*a*b^4*x+1/2*b^5*x^2+10*a^2*b^3*\ln(x)$

Rubi [A] time = 0.02, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{10a^3b^2}{x} + 10a^2b^3 \log(x) - \frac{5a^4b}{2x^2} - \frac{a^5}{3x^3} + 5ab^4x + \frac{b^5x^2}{2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^4,x]

[Out] $-a^5/(3*x^3) - (5*a^4*b)/(2*x^2) - (10*a^3*b^2)/x + 5*a*b^4*x + (b^5*x^2)/2 + 10*a^2*b^3*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^4} dx &= \int \left(5ab^4 + \frac{a^5}{x^4} + \frac{5a^4b}{x^3} + \frac{10a^3b^2}{x^2} + \frac{10a^2b^3}{x} + b^5x \right) dx \\ &= -\frac{a^5}{3x^3} - \frac{5a^4b}{2x^2} - \frac{10a^3b^2}{x} + 5ab^4x + \frac{b^5x^2}{2} + 10a^2b^3 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 60, normalized size = 1.00

$$-\frac{a^5}{3x^3} - \frac{5a^4b}{2x^2} - \frac{10a^3b^2}{x} + 10a^2b^3 \log(x) + 5ab^4x + \frac{b^5x^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^4,x]

[Out] $-1/3*a^5/x^3 - (5*a^4*b)/(2*x^2) - (10*a^3*b^2)/x + 5*a*b^4*x + (b^5*x^2)/2 + 10*a^2*b^3*\text{Log}[x]$

fricas [A] time = 0.48, size = 59, normalized size = 0.98

$$\frac{3b^5x^5 + 30ab^4x^4 + 60a^2b^3x^3 \log(x) - 60a^3b^2x^2 - 15a^4bx - 2a^5}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^4,x, algorithm="fricas")

[Out] $1/6*(3*b^5*x^5 + 30*a*b^4*x^4 + 60*a^2*b^3*x^3*\log(x) - 60*a^3*b^2*x^2 - 15*a^4*b*x - 2*a^5)/x^3$

giac [A] time = 1.00, size = 56, normalized size = 0.93

$$\frac{1}{2}b^5x^2 + 5ab^4x + 10a^2b^3 \log(|x|) - \frac{60a^3b^2x^2 + 15a^4bx + 2a^5}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^4,x, algorithm="giac")

[Out] $1/2*b^5*x^2 + 5*a*b^4*x + 10*a^2*b^3*\log(\text{abs}(x)) - 1/6*(60*a^3*b^2*x^2 + 15*a^4*b*x + 2*a^5)/x^3$

maple [A] time = 0.01, size = 55, normalized size = 0.92

$$\frac{b^5x^2}{2} + 10a^2b^3 \ln(x) + 5ab^4x - \frac{10a^3b^2}{x} - \frac{5a^4b}{2x^2} - \frac{a^5}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^4,x)

[Out] $-1/3*a^5/x^3 - 5/2*a^4*b/x^2 - 10*a^3*b^2/x + 5*a*b^4*x + 1/2*b^5*x^2 + 10*a^2*b^3*\ln(x)$

maxima [A] time = 1.41, size = 55, normalized size = 0.92

$$\frac{1}{2}b^5x^2 + 5ab^4x + 10a^2b^3 \log(x) - \frac{60a^3b^2x^2 + 15a^4bx + 2a^5}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^4,x, algorithm="maxima")

[Out] $1/2*b^5*x^2 + 5*a*b^4*x + 10*a^2*b^3*\log(x) - 1/6*(60*a^3*b^2*x^2 + 15*a^4*b*x + 2*a^5)/x^3$

mupad [B] time = 0.04, size = 55, normalized size = 0.92

$$\frac{b^5 x^2}{2} - \frac{\frac{a^5}{3} + \frac{5a^4 b x}{2} + 10 a^3 b^2 x^2}{x^3} + 10 a^2 b^3 \ln(x) + 5 a b^4 x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^4,x)

[Out] $(b^5*x^2)/2 - (a^5/3 + 10*a^3*b^2*x^2 + (5*a^4*b*x)/2)/x^3 + 10*a^2*b^3*\log(x) + 5*a*b^4*x$

sympy [A] time = 0.26, size = 60, normalized size = 1.00

$$10a^2b^3 \log(x) + 5ab^4x + \frac{b^5x^2}{2} + \frac{-2a^5 - 15a^4bx - 60a^3b^2x^2}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**4,x)

[Out] $10*a**2*b**3*\log(x) + 5*a*b**4*x + b**5*x**2/2 + (-2*a**5 - 15*a**4*b*x - 60*a**3*b**2*x**2)/(6*x**3)$

$$3.88 \quad \int \frac{(a+bx)^5}{x^5} dx$$

Optimal. Leaf size=57

$$-\frac{a^5}{4x^4} - \frac{5a^4b}{3x^3} - \frac{5a^3b^2}{x^2} - \frac{10a^2b^3}{x} + 5ab^4 \log(x) + b^5x$$

[Out] $-1/4*a^5/x^4-5/3*a^4*b/x^3-5*a^3*b^2/x^2-10*a^2*b^3/x+b^5*x+5*a*b^4*\ln(x)$

Rubi [A] time = 0.02, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{5a^3b^2}{x^2} - \frac{10a^2b^3}{x} - \frac{5a^4b}{3x^3} - \frac{a^5}{4x^4} + 5ab^4 \log(x) + b^5x$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^5, x]

[Out] $-a^5/(4*x^4) - (5*a^4*b)/(3*x^3) - (5*a^3*b^2)/x^2 - (10*a^2*b^3)/x + b^5*x + 5*a*b^4*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^5} dx &= \int \left(b^5 + \frac{a^5}{x^5} + \frac{5a^4b}{x^4} + \frac{10a^3b^2}{x^3} + \frac{10a^2b^3}{x^2} + \frac{5ab^4}{x} \right) dx \\ &= -\frac{a^5}{4x^4} - \frac{5a^4b}{3x^3} - \frac{5a^3b^2}{x^2} - \frac{10a^2b^3}{x} + b^5x + 5ab^4 \log(x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 57, normalized size = 1.00

$$-\frac{a^5}{4x^4} - \frac{5a^4b}{3x^3} - \frac{5a^3b^2}{x^2} - \frac{10a^2b^3}{x} + 5ab^4 \log(x) + b^5x$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^5, x]

[Out] $-1/4*a^5/x^4 - (5*a^4*b)/(3*x^3) - (5*a^3*b^2)/x^2 - (10*a^2*b^3)/x + b^5*x + 5*a*b^4*\text{Log}[x]$

fricas [A] time = 0.44, size = 59, normalized size = 1.04

$$\frac{12 b^5 x^5 + 60 a b^4 x^4 \log(x) - 120 a^2 b^3 x^3 - 60 a^3 b^2 x^2 - 20 a^4 b x - 3 a^5}{12 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^5, x, algorithm="fricas")

[Out] $1/12*(12*b^5*x^5 + 60*a*b^4*x^4*\log(x) - 120*a^2*b^3*x^3 - 60*a^3*b^2*x^2 - 20*a^4*b*x - 3*a^5)/x^4$

giac [A] time = 1.38, size = 55, normalized size = 0.96

$$b^5 x + 5 a b^4 \log(|x|) - \frac{120 a^2 b^3 x^3 + 60 a^3 b^2 x^2 + 20 a^4 b x + 3 a^5}{12 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^5, x, algorithm="giac")

[Out] $b^5*x + 5*a*b^4*\log(\text{abs}(x)) - 1/12*(120*a^2*b^3*x^3 + 60*a^3*b^2*x^2 + 20*a^4*b*x + 3*a^5)/x^4$

maple [A] time = 0.01, size = 54, normalized size = 0.95

$$5 a b^4 \ln(x) + b^5 x - \frac{10 a^2 b^3}{x} - \frac{5 a^3 b^2}{x^2} - \frac{5 a^4 b}{3 x^3} - \frac{a^5}{4 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^5, x)

[Out] $-1/4*a^5/x^4 - 5/3*a^4*b/x^3 - 5*a^3*b^2/x^2 - 10*a^2*b^3/x + b^5*x + 5*a*b^4*\ln(x)$

maxima [A] time = 1.37, size = 54, normalized size = 0.95

$$b^5 x + 5 a b^4 \log(x) - \frac{120 a^2 b^3 x^3 + 60 a^3 b^2 x^2 + 20 a^4 b x + 3 a^5}{12 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^5, x, algorithm="maxima")

[Out] $b^5 x + 5 a b^4 \log(x) - \frac{1}{12} (120 a^2 b^3 x^3 + 60 a^3 b^2 x^2 + 20 a^4 b x + 3 a^5) / x^4$

mupad [B] time = 0.08, size = 54, normalized size = 0.95

$$b^5 x - \frac{\frac{a^5}{4} + \frac{5 a^4 b x}{3} + 5 a^3 b^2 x^2 + 10 a^2 b^3 x^3}{x^4} + 5 a b^4 \ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/x^5, x)`

[Out] $b^5 x - (a^5/4 + 5 a^3 b^2 x^2 + 10 a^2 b^3 x^3 + (5 a^4 b x)/3) / x^4 + 5 a b^4 \log(x)$

sympy [A] time = 0.29, size = 58, normalized size = 1.02

$$5 a b^4 \log(x) + b^5 x + \frac{-3 a^5 - 20 a^4 b x - 60 a^3 b^2 x^2 - 120 a^2 b^3 x^3}{12 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/x**5, x)`

[Out] $5 a b^4 \log(x) + b^5 x + (-3 a^5 - 20 a^4 b x - 60 a^3 b^2 x^2 - 120 a^2 b^3 x^3) / (12 x^4)$

$$3.89 \quad \int \frac{(a+bx)^5}{x^6} dx$$

Optimal. Leaf size=61

$$-\frac{a^5}{5x^5} - \frac{5a^4b}{4x^4} - \frac{10a^3b^2}{3x^3} - \frac{5a^2b^3}{x^2} - \frac{5ab^4}{x} + b^5 \log(x)$$

[Out] $-1/5*a^5/x^5-5/4*a^4*b/x^4-10/3*a^3*b^2/x^3-5*a^2*b^3/x^2-5*a*b^4/x+b^5*\ln(x)$

Rubi [A] time = 0.02, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{10a^3b^2}{3x^3} - \frac{5a^2b^3}{x^2} - \frac{5a^4b}{4x^4} - \frac{a^5}{5x^5} - \frac{5ab^4}{x} + b^5 \log(x)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^6, x]

[Out] $-a^5/(5*x^5) - (5*a^4*b)/(4*x^4) - (10*a^3*b^2)/(3*x^3) - (5*a^2*b^3)/x^2 - (5*a*b^4)/x + b^5*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^6} dx &= \int \left(\frac{a^5}{x^6} + \frac{5a^4b}{x^5} + \frac{10a^3b^2}{x^4} + \frac{10a^2b^3}{x^3} + \frac{5ab^4}{x^2} + \frac{b^5}{x} \right) dx \\ &= -\frac{a^5}{5x^5} - \frac{5a^4b}{4x^4} - \frac{10a^3b^2}{3x^3} - \frac{5a^2b^3}{x^2} - \frac{5ab^4}{x} + b^5 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 61, normalized size = 1.00

$$-\frac{a^5}{5x^5} - \frac{5a^4b}{4x^4} - \frac{10a^3b^2}{3x^3} - \frac{5a^2b^3}{x^2} - \frac{5ab^4}{x} + b^5 \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^6,x]

[Out] $-1/5*a^5/x^5 - (5*a^4*b)/(4*x^4) - (10*a^3*b^2)/(3*x^3) - (5*a^2*b^3)/x^2 - (5*a*b^4)/x + b^5*\text{Log}[x]$

fricas [A] time = 0.43, size = 59, normalized size = 0.97

$$\frac{60 b^5 x^5 \log(x) - 300 a b^4 x^4 - 300 a^2 b^3 x^3 - 200 a^3 b^2 x^2 - 75 a^4 b x - 12 a^5}{60 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^6,x, algorithm="fricas")

[Out] $1/60*(60*b^5*x^5*\log(x) - 300*a*b^4*x^4 - 300*a^2*b^3*x^3 - 200*a^3*b^2*x^2 - 75*a^4*b*x - 12*a^5)/x^5$

giac [A] time = 1.37, size = 57, normalized size = 0.93

$$b^5 \log(|x|) - \frac{300 a b^4 x^4 + 300 a^2 b^3 x^3 + 200 a^3 b^2 x^2 + 75 a^4 b x + 12 a^5}{60 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^6,x, algorithm="giac")

[Out] $b^5*\log(\text{abs}(x)) - 1/60*(300*a*b^4*x^4 + 300*a^2*b^3*x^3 + 200*a^3*b^2*x^2 + 75*a^4*b*x + 12*a^5)/x^5$

maple [A] time = 0.01, size = 56, normalized size = 0.92

$$b^5 \ln(x) - \frac{5 a b^4}{x} - \frac{5 a^2 b^3}{x^2} - \frac{10 a^3 b^2}{3 x^3} - \frac{5 a^4 b}{4 x^4} - \frac{a^5}{5 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^6,x)

[Out] $-1/5*a^5/x^5 - 5/4*a^4*b/x^4 - 10/3*a^3*b^2/x^3 - 5*a^2*b^3/x^2 - 5*a*b^4/x + b^5*\ln(x)$

maxima [A] time = 1.35, size = 56, normalized size = 0.92

$$b^5 \log(x) - \frac{300 a b^4 x^4 + 300 a^2 b^3 x^3 + 200 a^3 b^2 x^2 + 75 a^4 b x + 12 a^5}{60 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^6,x, algorithm="maxima")

[Out] $b^5 \log(x) - \frac{1}{60} (300 a^5 b^4 x^4 + 300 a^4 b^3 x^3 + 200 a^3 b^2 x^2 + 75 a^2 b x + 12 a^5) / x^5$

mupad [B] time = 0.04, size = 56, normalized size = 0.92

$$b^5 \ln(x) - \frac{\frac{a^5}{5} + \frac{5a^4bx}{4} + \frac{10a^3b^2x^2}{3} + 5a^2b^3x^3 + 5ab^4x^4}{x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^6,x)

[Out] $b^5 \log(x) - (a^5/5 + 5a^4bx + (10a^3b^2x^2)/3 + 5a^2b^3x^3 + (5a^4b^4x^4)/4) / x^5$

sympy [A] time = 0.36, size = 60, normalized size = 0.98

$$b^5 \log(x) + \frac{-12a^5 - 75a^4bx - 200a^3b^2x^2 - 300a^2b^3x^3 - 300ab^4x^4}{60x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**6,x)

[Out] $b^{**5} \log(x) + (-12a^{**5} - 75a^{**4} b x - 200a^{**3} b^{**2} x^{**2} - 300a^{**2} b^{**3} x^{**3} - 300a b^{**4} x^{**4}) / (60x^{**5})$

$$3.90 \quad \int \frac{(a+bx)^5}{x^7} dx$$

Optimal. Leaf size=17

$$-\frac{(a+bx)^6}{6ax^6}$$

[Out] $-1/6*(b*x+a)^6/a/x^6$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {37}

$$-\frac{(a+bx)^6}{6ax^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^7, x]

[Out] $-(a + b*x)^6/(6*a*x^6)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp [((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(a+bx)^5}{x^7} dx = -\frac{(a+bx)^6}{6ax^6}$$

Mathematica [B] time = 0.00, size = 65, normalized size = 3.82

$$-\frac{a^5}{6x^6} - \frac{a^4b}{x^5} - \frac{5a^3b^2}{2x^4} - \frac{10a^2b^3}{3x^3} - \frac{5ab^4}{2x^2} - \frac{b^5}{x}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^7, x]

[Out] $-1/6*a^5/x^6 - (a^4*b)/x^5 - (5*a^3*b^2)/(2*x^4) - (10*a^2*b^3)/(3*x^3) - (5*a*b^4)/(2*x^2) - b^5/x$

fricas [B] time = 0.43, size = 55, normalized size = 3.24

$$\frac{6b^5x^5 + 15ab^4x^4 + 20a^2b^3x^3 + 15a^3b^2x^2 + 6a^4bx + a^5}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^7,x, algorithm="fricas")

[Out] -1/6*(6*b^5*x^5 + 15*a*b^4*x^4 + 20*a^2*b^3*x^3 + 15*a^3*b^2*x^2 + 6*a^4*b*x + a^5)/x^6

giac [B] time = 0.94, size = 55, normalized size = 3.24

$$\frac{6b^5x^5 + 15ab^4x^4 + 20a^2b^3x^3 + 15a^3b^2x^2 + 6a^4bx + a^5}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^7,x, algorithm="giac")

[Out] -1/6*(6*b^5*x^5 + 15*a*b^4*x^4 + 20*a^2*b^3*x^3 + 15*a^3*b^2*x^2 + 6*a^4*b*x + a^5)/x^6

maple [B] time = 0.00, size = 58, normalized size = 3.41

$$-\frac{b^5}{x} - \frac{5ab^4}{2x^2} - \frac{10a^2b^3}{3x^3} - \frac{5a^3b^2}{2x^4} - \frac{a^4b}{x^5} - \frac{a^5}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^7,x)

[Out] -1/6*a^5/x^6-a^4*b/x^5-5/2*a^3*b^2/x^4-b^5/x-10/3*a^2*b^3/x^3-5/2*a*b^4/x^2

maxima [B] time = 1.30, size = 55, normalized size = 3.24

$$\frac{6b^5x^5 + 15ab^4x^4 + 20a^2b^3x^3 + 15a^3b^2x^2 + 6a^4bx + a^5}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^7,x, algorithm="maxima")

[Out] -1/6*(6*b^5*x^5 + 15*a*b^4*x^4 + 20*a^2*b^3*x^3 + 15*a^3*b^2*x^2 + 6*a^4*b*x + a^5)/x^6

mupad [B] time = 0.04, size = 55, normalized size = 3.24

$$\frac{\frac{a^5}{6} + a^4 b x + \frac{5a^3 b^2 x^2}{2} + \frac{10a^2 b^3 x^3}{3} + \frac{5ab^4 x^4}{2} + b^5 x^5}{x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^7, x)

[Out] $-(a^5/6 + b^5*x^5 + (5*a*b^4*x^4)/2 + (5*a^3*b^2*x^2)/2 + (10*a^2*b^3*x^3)/3 + a^4*b*x)/x^6$

sympy [B] time = 0.37, size = 60, normalized size = 3.53

$$\frac{-a^5 - 6a^4bx - 15a^3b^2x^2 - 20a^2b^3x^3 - 15ab^4x^4 - 6b^5x^5}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**7, x)

[Out] $(-a**5 - 6*a**4*b*x - 15*a**3*b**2*x**2 - 20*a**2*b**3*x**3 - 15*a*b**4*x**4 - 6*b**5*x**5)/(6*x**6)$

3.91 $\int \frac{(a+bx)^5}{x^8} dx$

Optimal. Leaf size=36

$$\frac{b(a+bx)^6}{42a^2x^6} - \frac{(a+bx)^6}{7ax^7}$$

[Out] $-1/7*(b*x+a)^6/a/x^7+1/42*b*(b*x+a)^6/a^2/x^6$

Rubi [A] time = 0.00, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{b(a+bx)^6}{42a^2x^6} - \frac{(a+bx)^6}{7ax^7}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^8, x]

[Out] $-(a + b*x)^6/(7*a*x^7) + (b*(a + b*x)^6)/(42*a^2*x^6)$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp
[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
+ d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^8} dx &= -\frac{(a+bx)^6}{7ax^7} - \frac{b \int \frac{(a+bx)^5}{x^7} dx}{7a} \\ &= -\frac{(a+bx)^6}{7ax^7} + \frac{b(a+bx)^6}{42a^2x^6} \end{aligned}$$

Mathematica [A] time = 0.00, size = 67, normalized size = 1.86

$$-\frac{a^5}{7x^7} - \frac{5a^4b}{6x^6} - \frac{2a^3b^2}{x^5} - \frac{5a^2b^3}{2x^4} - \frac{5ab^4}{3x^3} - \frac{b^5}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^8,x]

[Out] $-1/7*a^5/x^7 - (5*a^4*b)/(6*x^6) - (2*a^3*b^2)/x^5 - (5*a^2*b^3)/(2*x^4) - (5*a*b^4)/(3*x^3) - b^5/(2*x^2)$

fricas [A] time = 0.45, size = 57, normalized size = 1.58

$$\frac{21 b^5 x^5 + 70 a b^4 x^4 + 105 a^2 b^3 x^3 + 84 a^3 b^2 x^2 + 35 a^4 b x + 6 a^5}{42 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^8,x, algorithm="fricas")

[Out] $-1/42*(21*b^5*x^5 + 70*a*b^4*x^4 + 105*a^2*b^3*x^3 + 84*a^3*b^2*x^2 + 35*a^4*b*x + 6*a^5)/x^7$

giac [A] time = 1.12, size = 57, normalized size = 1.58

$$\frac{21 b^5 x^5 + 70 a b^4 x^4 + 105 a^2 b^3 x^3 + 84 a^3 b^2 x^2 + 35 a^4 b x + 6 a^5}{42 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^8,x, algorithm="giac")

[Out] $-1/42*(21*b^5*x^5 + 70*a*b^4*x^4 + 105*a^2*b^3*x^3 + 84*a^3*b^2*x^2 + 35*a^4*b*x + 6*a^5)/x^7$

maple [A] time = 0.01, size = 58, normalized size = 1.61

$$-\frac{b^5}{2x^2} - \frac{5ab^4}{3x^3} - \frac{5a^2b^3}{2x^4} - \frac{2a^3b^2}{x^5} - \frac{5a^4b}{6x^6} - \frac{a^5}{7x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^8,x)

[Out] $-2*a^3*b^2/x^5 - 1/7*a^5/x^7 - 5/2*a^2*b^3/x^4 - 5/6*a^4*b/x^6 - 5/3*a*b^4/x^3 - 1/2*b^5/x^2$

maxima [A] time = 1.36, size = 57, normalized size = 1.58

$$\frac{21 b^5 x^5 + 70 a b^4 x^4 + 105 a^2 b^3 x^3 + 84 a^3 b^2 x^2 + 35 a^4 b x + 6 a^5}{42 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^8,x, algorithm="maxima")

[Out] -1/42*(21*b^5*x^5 + 70*a*b^4*x^4 + 105*a^2*b^3*x^3 + 84*a^3*b^2*x^2 + 35*a^4*b*x + 6*a^5)/x^7

mupad [B] time = 0.07, size = 57, normalized size = 1.58

$$\frac{\frac{a^5}{7} + \frac{5a^4bx}{6} + 2a^3b^2x^2 + \frac{5a^2b^3x^3}{2} + \frac{5ab^4x^4}{3} + \frac{b^5x^5}{2}}{x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^8,x)

[Out] -(a^5/7 + (b^5*x^5)/2 + (5*a*b^4*x^4)/3 + 2*a^3*b^2*x^2 + (5*a^2*b^3*x^3)/2 + (5*a^4*b*x)/6)/x^7

sympy [B] time = 0.41, size = 61, normalized size = 1.69

$$\frac{-6a^5 - 35a^4bx - 84a^3b^2x^2 - 105a^2b^3x^3 - 70ab^4x^4 - 21b^5x^5}{42x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**8,x)

[Out] (-6*a**5 - 35*a**4*b*x - 84*a**3*b**2*x**2 - 105*a**2*b**3*x**3 - 70*a*b**4*x**4 - 21*b**5*x**5)/(42*x**7)

3.92

$$\int \frac{(a+bx)^5}{x^9} dx$$

Optimal. Leaf size=56

$$-\frac{b^2(a+bx)^6}{168a^3x^6} + \frac{b(a+bx)^6}{28a^2x^7} - \frac{(a+bx)^6}{8ax^8}$$

[Out] $-1/8*(b*x+a)^6/a/x^8+1/28*b*(b*x+a)^6/a^2/x^7-1/168*b^2*(b*x+a)^6/a^3/x^6$

Rubi [A] time = 0.01, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$-\frac{b^2(a+bx)^6}{168a^3x^6} + \frac{b(a+bx)^6}{28a^2x^7} - \frac{(a+bx)^6}{8ax^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^9, x]

[Out] $-(a + b*x)^6/(8*a*x^8) + (b*(a + b*x)^6)/(28*a^2*x^7) - (b^2*(a + b*x)^6)/(168*a^3*x^6)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^5}{x^9} dx &= -\frac{(a+bx)^6}{8ax^8} - \frac{b \int \frac{(a+bx)^5}{x^8} dx}{4a} \\
&= -\frac{(a+bx)^6}{8ax^8} + \frac{b(a+bx)^6}{28a^2x^7} + \frac{b^2 \int \frac{(a+bx)^5}{x^7} dx}{28a^2} \\
&= -\frac{(a+bx)^6}{8ax^8} + \frac{b(a+bx)^6}{28a^2x^7} - \frac{b^2(a+bx)^6}{168a^3x^6}
\end{aligned}$$

Mathematica [A] time = 0.00, size = 67, normalized size = 1.20

$$-\frac{a^5}{8x^8} - \frac{5a^4b}{7x^7} - \frac{5a^3b^2}{3x^6} - \frac{2a^2b^3}{x^5} - \frac{5ab^4}{4x^4} - \frac{b^5}{3x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^9, x]

[Out] -1/8*a^5/x^8 - (5*a^4*b)/(7*x^7) - (5*a^3*b^2)/(3*x^6) - (2*a^2*b^3)/x^5 - (5*a*b^4)/(4*x^4) - b^5/(3*x^3)

fricas [A] time = 0.43, size = 57, normalized size = 1.02

$$\frac{56b^5x^5 + 210ab^4x^4 + 336a^2b^3x^3 + 280a^3b^2x^2 + 120a^4bx + 21a^5}{168x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^9, x, algorithm="fricas")

[Out] -1/168*(56*b^5*x^5 + 210*a*b^4*x^4 + 336*a^2*b^3*x^3 + 280*a^3*b^2*x^2 + 120*a^4*b*x + 21*a^5)/x^8

giac [A] time = 1.10, size = 57, normalized size = 1.02

$$\frac{56b^5x^5 + 210ab^4x^4 + 336a^2b^3x^3 + 280a^3b^2x^2 + 120a^4bx + 21a^5}{168x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^9, x, algorithm="giac")

[Out] -1/168*(56*b^5*x^5 + 210*a*b^4*x^4 + 336*a^2*b^3*x^3 + 280*a^3*b^2*x^2 + 120*a^4*b*x + 21*a^5)/x^8

maple [A] time = 0.01, size = 58, normalized size = 1.04

$$-\frac{b^5}{3x^3} - \frac{5ab^4}{4x^4} - \frac{2a^2b^3}{x^5} - \frac{5a^3b^2}{3x^6} - \frac{5a^4b}{7x^7} - \frac{a^5}{8x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^9,x)

[Out] $-5/7*a^4*b/x^7 - 1/8*a^5/x^8 - 5/4*a*b^4/x^4 - 5/3*a^3*b^2/x^6 - 1/3*b^5/x^3 - 2*a^2*b^3/x^5$

maxima [A] time = 1.40, size = 57, normalized size = 1.02

$$\frac{56b^5x^5 + 210ab^4x^4 + 336a^2b^3x^3 + 280a^3b^2x^2 + 120a^4bx + 21a^5}{168x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^9,x, algorithm="maxima")

[Out] $-1/168*(56*b^5*x^5 + 210*a*b^4*x^4 + 336*a^2*b^3*x^3 + 280*a^3*b^2*x^2 + 120*a^4*b*x + 21*a^5)/x^8$

mupad [B] time = 0.04, size = 57, normalized size = 1.02

$$\frac{\frac{a^5}{8} + \frac{5a^4bx}{7} + \frac{5a^3b^2x^2}{3} + 2a^2b^3x^3 + \frac{5ab^4x^4}{4} + \frac{b^5x^5}{3}}{x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^9,x)

[Out] $-(a^5/8 + (b^5*x^5)/3 + (5*a*b^4*x^4)/4 + (5*a^3*b^2*x^2)/3 + 2*a^2*b^3*x^3 + (5*a^4*b*x)/7)/x^8$

sympy [A] time = 0.43, size = 61, normalized size = 1.09

$$\frac{-21a^5 - 120a^4bx - 280a^3b^2x^2 - 336a^2b^3x^3 - 210ab^4x^4 - 56b^5x^5}{168x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**9,x)

[Out] $(-21*a**5 - 120*a**4*b*x - 280*a**3*b**2*x**2 - 336*a**2*b**3*x**3 - 210*a*b**4*x**4 - 56*b**5*x**5)/(168*x**8)$

3.93 $\int \frac{(a+bx)^5}{x^{10}} dx$

Optimal. Leaf size=67

$$-\frac{a^5}{9x^9} - \frac{5a^4b}{8x^8} - \frac{10a^3b^2}{7x^7} - \frac{5a^2b^3}{3x^6} - \frac{ab^4}{x^5} - \frac{b^5}{4x^4}$$

[Out] $-1/9*a^5/x^9-5/8*a^4*b/x^8-10/7*a^3*b^2/x^7-5/3*a^2*b^3/x^6-a*b^4/x^5-1/4*b^5/x^4$

Rubi [A] time = 0.02, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{10a^3b^2}{7x^7} - \frac{5a^2b^3}{3x^6} - \frac{5a^4b}{8x^8} - \frac{a^5}{9x^9} - \frac{ab^4}{x^5} - \frac{b^5}{4x^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^10,x]

[Out] $-a^5/(9*x^9) - (5*a^4*b)/(8*x^8) - (10*a^3*b^2)/(7*x^7) - (5*a^2*b^3)/(3*x^6) - (a*b^4)/x^5 - b^5/(4*x^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^{10}} dx &= \int \left(\frac{a^5}{x^{10}} + \frac{5a^4b}{x^9} + \frac{10a^3b^2}{x^8} + \frac{10a^2b^3}{x^7} + \frac{5ab^4}{x^6} + \frac{b^5}{x^5} \right) dx \\ &= -\frac{a^5}{9x^9} - \frac{5a^4b}{8x^8} - \frac{10a^3b^2}{7x^7} - \frac{5a^2b^3}{3x^6} - \frac{ab^4}{x^5} - \frac{b^5}{4x^4} \end{aligned}$$

Mathematica [A] time = 0.01, size = 67, normalized size = 1.00

$$-\frac{a^5}{9x^9} - \frac{5a^4b}{8x^8} - \frac{10a^3b^2}{7x^7} - \frac{5a^2b^3}{3x^6} - \frac{ab^4}{x^5} - \frac{b^5}{4x^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^10,x]

[Out] $-1/9*a^5/x^9 - (5*a^4*b)/(8*x^8) - (10*a^3*b^2)/(7*x^7) - (5*a^2*b^3)/(3*x^6) - (a*b^4)/x^5 - b^5/(4*x^4)$

fricas [A] time = 0.46, size = 57, normalized size = 0.85

$$\frac{126 b^5 x^5 + 504 a b^4 x^4 + 840 a^2 b^3 x^3 + 720 a^3 b^2 x^2 + 315 a^4 b x + 56 a^5}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^10,x, algorithm="fricas")

[Out] $-1/504*(126*b^5*x^5 + 504*a*b^4*x^4 + 840*a^2*b^3*x^3 + 720*a^3*b^2*x^2 + 315*a^4*b*x + 56*a^5)/x^9$

giac [A] time = 1.21, size = 57, normalized size = 0.85

$$\frac{126 b^5 x^5 + 504 a b^4 x^4 + 840 a^2 b^3 x^3 + 720 a^3 b^2 x^2 + 315 a^4 b x + 56 a^5}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^10,x, algorithm="giac")

[Out] $-1/504*(126*b^5*x^5 + 504*a*b^4*x^4 + 840*a^2*b^3*x^3 + 720*a^3*b^2*x^2 + 315*a^4*b*x + 56*a^5)/x^9$

maple [A] time = 0.00, size = 58, normalized size = 0.87

$$-\frac{b^5}{4x^4} - \frac{ab^4}{x^5} - \frac{5a^2b^3}{3x^6} - \frac{10a^3b^2}{7x^7} - \frac{5a^4b}{8x^8} - \frac{a^5}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^10,x)

[Out] $-1/9*a^5/x^9 - 5/8*a^4*b/x^8 - 10/7*a^3*b^2/x^7 - 5/3*a^2*b^3/x^6 - a*b^4/x^5 - 1/4*b^5/x^4$

maxima [A] time = 1.33, size = 57, normalized size = 0.85

$$\frac{126 b^5 x^5 + 504 a b^4 x^4 + 840 a^2 b^3 x^3 + 720 a^3 b^2 x^2 + 315 a^4 b x + 56 a^5}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^10,x, algorithm="maxima")

[Out] $-1/504*(126*b^5*x^5 + 504*a*b^4*x^4 + 840*a^2*b^3*x^3 + 720*a^3*b^2*x^2 + 315*a^4*b*x + 56*a^5)/x^9$

mupad [B] time = 0.08, size = 56, normalized size = 0.84

$$\frac{\frac{a^5}{9} + \frac{5a^4bx}{8} + \frac{10a^3b^2x^2}{7} + \frac{5a^2b^3x^3}{3} + ab^4x^4 + \frac{b^5x^5}{4}}{x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^10,x)

[Out] $-(a^5/9 + (b^5*x^5)/4 + a*b^4*x^4 + (10*a^3*b^2*x^2)/7 + (5*a^2*b^3*x^3)/3 + (5*a^4*b*x)/8)/x^9$

sympy [A] time = 0.45, size = 61, normalized size = 0.91

$$\frac{-56a^5 - 315a^4bx - 720a^3b^2x^2 - 840a^2b^3x^3 - 504ab^4x^4 - 126b^5x^5}{504x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**10,x)

[Out] $(-56*a**5 - 315*a**4*b*x - 720*a**3*b**2*x**2 - 840*a**2*b**3*x**3 - 504*a*b**4*x**4 - 126*b**5*x**5)/(504*x**9)$

$$3.94 \quad \int \frac{(a+bx)^5}{x^{11}} dx$$

Optimal. Leaf size=69

$$-\frac{a^5}{10x^{10}} - \frac{5a^4b}{9x^9} - \frac{5a^3b^2}{4x^8} - \frac{10a^2b^3}{7x^7} - \frac{5ab^4}{6x^6} - \frac{b^5}{5x^5}$$

[Out] $-1/10*a^5/x^{10}-5/9*a^4*b/x^9-5/4*a^3*b^2/x^8-10/7*a^2*b^3/x^7-5/6*a*b^4/x^6-1/5*b^5/x^5$

Rubi [A] time = 0.02, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{5a^3b^2}{4x^8} - \frac{10a^2b^3}{7x^7} - \frac{5a^4b}{9x^9} - \frac{a^5}{10x^{10}} - \frac{5ab^4}{6x^6} - \frac{b^5}{5x^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^11, x]

[Out] $-a^5/(10*x^{10}) - (5*a^4*b)/(9*x^9) - (5*a^3*b^2)/(4*x^8) - (10*a^2*b^3)/(7*x^7) - (5*a*b^4)/(6*x^6) - b^5/(5*x^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^{11}} dx &= \int \left(\frac{a^5}{x^{11}} + \frac{5a^4b}{x^{10}} + \frac{10a^3b^2}{x^9} + \frac{10a^2b^3}{x^8} + \frac{5ab^4}{x^7} + \frac{b^5}{x^6} \right) dx \\ &= -\frac{a^5}{10x^{10}} - \frac{5a^4b}{9x^9} - \frac{5a^3b^2}{4x^8} - \frac{10a^2b^3}{7x^7} - \frac{5ab^4}{6x^6} - \frac{b^5}{5x^5} \end{aligned}$$

Mathematica [A] time = 0.00, size = 69, normalized size = 1.00

$$-\frac{a^5}{10x^{10}} - \frac{5a^4b}{9x^9} - \frac{5a^3b^2}{4x^8} - \frac{10a^2b^3}{7x^7} - \frac{5ab^4}{6x^6} - \frac{b^5}{5x^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^11,x]

[Out] $-1/10*a^5/x^{10} - (5*a^4*b)/(9*x^9) - (5*a^3*b^2)/(4*x^8) - (10*a^2*b^3)/(7*x^7) - (5*a*b^4)/(6*x^6) - b^5/(5*x^5)$

fricas [A] time = 0.42, size = 57, normalized size = 0.83

$$-\frac{252 b^5 x^5 + 1050 a b^4 x^4 + 1800 a^2 b^3 x^3 + 1575 a^3 b^2 x^2 + 700 a^4 b x + 126 a^5}{1260 x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^11,x, algorithm="fricas")

[Out] $-1/1260*(252*b^5*x^5 + 1050*a*b^4*x^4 + 1800*a^2*b^3*x^3 + 1575*a^3*b^2*x^2 + 700*a^4*b*x + 126*a^5)/x^{10}$

giac [A] time = 1.00, size = 57, normalized size = 0.83

$$-\frac{252 b^5 x^5 + 1050 a b^4 x^4 + 1800 a^2 b^3 x^3 + 1575 a^3 b^2 x^2 + 700 a^4 b x + 126 a^5}{1260 x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^11,x, algorithm="giac")

[Out] $-1/1260*(252*b^5*x^5 + 1050*a*b^4*x^4 + 1800*a^2*b^3*x^3 + 1575*a^3*b^2*x^2 + 700*a^4*b*x + 126*a^5)/x^{10}$

maple [A] time = 0.01, size = 58, normalized size = 0.84

$$-\frac{b^5}{5x^5} - \frac{5ab^4}{6x^6} - \frac{10a^2b^3}{7x^7} - \frac{5a^3b^2}{4x^8} - \frac{5a^4b}{9x^9} - \frac{a^5}{10x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^11,x)

[Out] $-1/10*a^5/x^{10} - 5/9*a^4*b/x^9 - 5/4*a^3*b^2/x^8 - 10/7*a^2*b^3/x^7 - 5/6*a*b^4/x^6 - 1/5*b^5/x^5$

maxima [A] time = 1.37, size = 57, normalized size = 0.83

$$-\frac{252 b^5 x^5 + 1050 a b^4 x^4 + 1800 a^2 b^3 x^3 + 1575 a^3 b^2 x^2 + 700 a^4 b x + 126 a^5}{1260 x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^11,x, algorithm="maxima")

[Out] $-1/1260*(252*b^5*x^5 + 1050*a*b^4*x^4 + 1800*a^2*b^3*x^3 + 1575*a^3*b^2*x^2 + 700*a^4*b*x + 126*a^5)/x^{10}$

mupad [B] time = 0.08, size = 57, normalized size = 0.83

$$\frac{\frac{a^5}{10} + \frac{5a^4bx}{9} + \frac{5a^3b^2x^2}{4} + \frac{10a^2b^3x^3}{7} + \frac{5ab^4x^4}{6} + \frac{b^5x^5}{5}}{x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^11,x)

[Out] $-(a^5/10 + (b^5*x^5)/5 + (5*a*b^4*x^4)/6 + (5*a^3*b^2*x^2)/4 + (10*a^2*b^3*x^3)/7 + (5*a^4*b*x)/9)/x^{10}$

sympy [A] time = 0.49, size = 61, normalized size = 0.88

$$\frac{-126a^5 - 700a^4bx - 1575a^3b^2x^2 - 1800a^2b^3x^3 - 1050ab^4x^4 - 252b^5x^5}{1260x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**11,x)

[Out] $(-126*a**5 - 700*a**4*b*x - 1575*a**3*b**2*x**2 - 1800*a**2*b**3*x**3 - 1050*a*b**4*x**4 - 252*b**5*x**5)/(1260*x**10)$

3.95

$$\int \frac{(a+bx)^5}{x^{12}} dx$$

Optimal. Leaf size=69

$$-\frac{a^5}{11x^{11}} - \frac{a^4b}{2x^{10}} - \frac{10a^3b^2}{9x^9} - \frac{5a^2b^3}{4x^8} - \frac{5ab^4}{7x^7} - \frac{b^5}{6x^6}$$

[Out] $-1/11*a^5/x^{11}-1/2*a^4*b/x^{10}-10/9*a^3*b^2/x^9-5/4*a^2*b^3/x^8-5/7*a*b^4/x^7-1/6*b^5/x^6$

Rubi [A] time = 0.02, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{10a^3b^2}{9x^9} - \frac{5a^2b^3}{4x^8} - \frac{a^4b}{2x^{10}} - \frac{a^5}{11x^{11}} - \frac{5ab^4}{7x^7} - \frac{b^5}{6x^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^12,x]

[Out] $-a^5/(11*x^{11}) - (a^4*b)/(2*x^{10}) - (10*a^3*b^2)/(9*x^9) - (5*a^2*b^3)/(4*x^8) - (5*a*b^4)/(7*x^7) - b^5/(6*x^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^{12}} dx &= \int \left(\frac{a^5}{x^{12}} + \frac{5a^4b}{x^{11}} + \frac{10a^3b^2}{x^{10}} + \frac{10a^2b^3}{x^9} + \frac{5ab^4}{x^8} + \frac{b^5}{x^7} \right) dx \\ &= -\frac{a^5}{11x^{11}} - \frac{a^4b}{2x^{10}} - \frac{10a^3b^2}{9x^9} - \frac{5a^2b^3}{4x^8} - \frac{5ab^4}{7x^7} - \frac{b^5}{6x^6} \end{aligned}$$

Mathematica [A] time = 0.00, size = 69, normalized size = 1.00

$$-\frac{a^5}{11x^{11}} - \frac{a^4b}{2x^{10}} - \frac{10a^3b^2}{9x^9} - \frac{5a^2b^3}{4x^8} - \frac{5ab^4}{7x^7} - \frac{b^5}{6x^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^12,x]

[Out] $-1/11*a^5/x^{11} - (a^4*b)/(2*x^{10}) - (10*a^3*b^2)/(9*x^9) - (5*a^2*b^3)/(4*x^8) - (5*a*b^4)/(7*x^7) - b^5/(6*x^6)$

fricas [A] time = 0.44, size = 57, normalized size = 0.83

$$\frac{462 b^5 x^5 + 1980 a b^4 x^4 + 3465 a^2 b^3 x^3 + 3080 a^3 b^2 x^2 + 1386 a^4 b x + 252 a^5}{2772 x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^12,x, algorithm="fricas")

[Out] $-1/2772*(462*b^5*x^5 + 1980*a*b^4*x^4 + 3465*a^2*b^3*x^3 + 3080*a^3*b^2*x^2 + 1386*a^4*b*x + 252*a^5)/x^{11}$

giac [A] time = 1.38, size = 57, normalized size = 0.83

$$\frac{462 b^5 x^5 + 1980 a b^4 x^4 + 3465 a^2 b^3 x^3 + 3080 a^3 b^2 x^2 + 1386 a^4 b x + 252 a^5}{2772 x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^12,x, algorithm="giac")

[Out] $-1/2772*(462*b^5*x^5 + 1980*a*b^4*x^4 + 3465*a^2*b^3*x^3 + 3080*a^3*b^2*x^2 + 1386*a^4*b*x + 252*a^5)/x^{11}$

maple [A] time = 0.01, size = 58, normalized size = 0.84

$$\frac{b^5}{6x^6} - \frac{5ab^4}{7x^7} - \frac{5a^2b^3}{4x^8} - \frac{10a^3b^2}{9x^9} - \frac{a^4b}{2x^{10}} - \frac{a^5}{11x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^12,x)

[Out] $-1/11*a^5/x^{11}-1/2*a^4*b/x^{10}-10/9*a^3*b^2/x^9-5/4*a^2*b^3/x^8-5/7*a*b^4/x^7-1/6*b^5/x^6$

maxima [A] time = 1.31, size = 57, normalized size = 0.83

$$\frac{462 b^5 x^5 + 1980 a b^4 x^4 + 3465 a^2 b^3 x^3 + 3080 a^3 b^2 x^2 + 1386 a^4 b x + 252 a^5}{2772 x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^12,x, algorithm="maxima")

[Out] $-1/2772*(462*b^5*x^5 + 1980*a*b^4*x^4 + 3465*a^2*b^3*x^3 + 3080*a^3*b^2*x^2 + 1386*a^4*b*x + 252*a^5)/x^{11}$

mupad [B] time = 0.04, size = 57, normalized size = 0.83

$$\frac{\frac{a^5}{11} + \frac{a^4 b x}{2} + \frac{10 a^3 b^2 x^2}{9} + \frac{5 a^2 b^3 x^3}{4} + \frac{5 a b^4 x^4}{7} + \frac{b^5 x^5}{6}}{x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^12,x)

[Out] $-(a^5/11 + (b^5*x^5)/6 + (5*a*b^4*x^4)/7 + (10*a^3*b^2*x^2)/9 + (5*a^2*b^3*x^3)/4 + (a^4*b*x)/2)/x^{11}$

sympy [A] time = 0.58, size = 61, normalized size = 0.88

$$\frac{-252a^5 - 1386a^4bx - 3080a^3b^2x^2 - 3465a^2b^3x^3 - 1980ab^4x^4 - 462b^5x^5}{2772x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**12,x)

[Out] $(-252*a**5 - 1386*a**4*b*x - 3080*a**3*b**2*x**2 - 3465*a**2*b**3*x**3 - 1980*a*b**4*x**4 - 462*b**5*x**5)/(2772*x**11)$

$$3.96 \quad \int \frac{(a+bx)^5}{x^{13}} dx$$

Optimal. Leaf size=67

$$-\frac{a^5}{12x^{12}} - \frac{5a^4b}{11x^{11}} - \frac{a^3b^2}{x^{10}} - \frac{10a^2b^3}{9x^9} - \frac{5ab^4}{8x^8} - \frac{b^5}{7x^7}$$

[Out] $-1/12*a^5/x^{12}-5/11*a^4*b/x^{11}-a^3*b^2/x^{10}-10/9*a^2*b^3/x^9-5/8*a*b^4/x^8-1/7*b^5/x^7$

Rubi [A] time = 0.02, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^3b^2}{x^{10}} - \frac{10a^2b^3}{9x^9} - \frac{5a^4b}{11x^{11}} - \frac{a^5}{12x^{12}} - \frac{5ab^4}{8x^8} - \frac{b^5}{7x^7}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^13, x]

[Out] $-a^5/(12*x^{12}) - (5*a^4*b)/(11*x^{11}) - (a^3*b^2)/x^{10} - (10*a^2*b^3)/(9*x^9) - (5*a*b^4)/(8*x^8) - b^5/(7*x^7)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^{13}} dx &= \int \left(\frac{a^5}{x^{13}} + \frac{5a^4b}{x^{12}} + \frac{10a^3b^2}{x^{11}} + \frac{10a^2b^3}{x^{10}} + \frac{5ab^4}{x^9} + \frac{b^5}{x^8} \right) dx \\ &= -\frac{a^5}{12x^{12}} - \frac{5a^4b}{11x^{11}} - \frac{a^3b^2}{x^{10}} - \frac{10a^2b^3}{9x^9} - \frac{5ab^4}{8x^8} - \frac{b^5}{7x^7} \end{aligned}$$

Mathematica [A] time = 0.00, size = 67, normalized size = 1.00

$$-\frac{a^5}{12x^{12}} - \frac{5a^4b}{11x^{11}} - \frac{a^3b^2}{x^{10}} - \frac{10a^2b^3}{9x^9} - \frac{5ab^4}{8x^8} - \frac{b^5}{7x^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^13,x]

[Out] $-1/12*a^5/x^{12} - (5*a^4*b)/(11*x^{11}) - (a^3*b^2)/x^{10} - (10*a^2*b^3)/(9*x^9) - (5*a*b^4)/(8*x^8) - b^5/(7*x^7)$

fricas [A] time = 0.44, size = 57, normalized size = 0.85

$$\frac{792 b^5 x^5 + 3465 a b^4 x^4 + 6160 a^2 b^3 x^3 + 5544 a^3 b^2 x^2 + 2520 a^4 b x + 462 a^5}{5544 x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^13,x, algorithm="fricas")

[Out] $-1/5544*(792*b^5*x^5 + 3465*a*b^4*x^4 + 6160*a^2*b^3*x^3 + 5544*a^3*b^2*x^2 + 2520*a^4*b*x + 462*a^5)/x^{12}$

giac [A] time = 1.23, size = 57, normalized size = 0.85

$$\frac{792 b^5 x^5 + 3465 a b^4 x^4 + 6160 a^2 b^3 x^3 + 5544 a^3 b^2 x^2 + 2520 a^4 b x + 462 a^5}{5544 x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^13,x, algorithm="giac")

[Out] $-1/5544*(792*b^5*x^5 + 3465*a*b^4*x^4 + 6160*a^2*b^3*x^3 + 5544*a^3*b^2*x^2 + 2520*a^4*b*x + 462*a^5)/x^{12}$

maple [A] time = 0.01, size = 58, normalized size = 0.87

$$-\frac{b^5}{7x^7} - \frac{5ab^4}{8x^8} - \frac{10a^2b^3}{9x^9} - \frac{a^3b^2}{x^{10}} - \frac{5a^4b}{11x^{11}} - \frac{a^5}{12x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^13,x)

[Out] $-1/12*a^5/x^{12}-5/11*a^4*b/x^{11}-a^3*b^2/x^{10}-10/9*a^2*b^3/x^9-5/8*a*b^4/x^8-1/7*b^5/x^7$

maxima [A] time = 1.36, size = 57, normalized size = 0.85

$$\frac{792 b^5 x^5 + 3465 a b^4 x^4 + 6160 a^2 b^3 x^3 + 5544 a^3 b^2 x^2 + 2520 a^4 b x + 462 a^5}{5544 x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^13,x, algorithm="maxima")

[Out] $-1/5544*(792*b^5*x^5 + 3465*a*b^4*x^4 + 6160*a^2*b^3*x^3 + 5544*a^3*b^2*x^2 + 2520*a^4*b*x + 462*a^5)/x^{12}$

mupad [B] time = 0.04, size = 56, normalized size = 0.84

$$\frac{\frac{a^5}{12} + \frac{5a^4bx}{11} + a^3b^2x^2 + \frac{10a^2b^3x^3}{9} + \frac{5ab^4x^4}{8} + \frac{b^5x^5}{7}}{x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^13,x)

[Out] $-(a^5/12 + (b^5*x^5)/7 + (5*a*b^4*x^4)/8 + a^3*b^2*x^2 + (10*a^2*b^3*x^3)/9 + (5*a^4*b*x)/11)/x^{12}$

sympy [A] time = 0.62, size = 61, normalized size = 0.91

$$\frac{-462a^5 - 2520a^4bx - 5544a^3b^2x^2 - 6160a^2b^3x^3 - 3465ab^4x^4 - 792b^5x^5}{5544x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**13,x)

[Out] $(-462*a**5 - 2520*a**4*b*x - 5544*a**3*b**2*x**2 - 6160*a**2*b**3*x**3 - 3465*a*b**4*x**4 - 792*b**5*x**5)/(5544*x**12)$

$$3.97 \quad \int \frac{(a+bx)^5}{x^{14}} dx$$

Optimal. Leaf size=67

$$-\frac{a^5}{13x^{13}} - \frac{5a^4b}{12x^{12}} - \frac{10a^3b^2}{11x^{11}} - \frac{a^2b^3}{x^{10}} - \frac{5ab^4}{9x^9} - \frac{b^5}{8x^8}$$

[Out] $-1/13*a^5/x^{13}-5/12*a^4*b/x^{12}-10/11*a^3*b^2/x^{11}-a^2*b^3/x^{10}-5/9*a*b^4/x^9-1/8*b^5/x^8$

Rubi [A] time = 0.02, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{10a^3b^2}{11x^{11}} - \frac{a^2b^3}{x^{10}} - \frac{5a^4b}{12x^{12}} - \frac{a^5}{13x^{13}} - \frac{5ab^4}{9x^9} - \frac{b^5}{8x^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^14,x]

[Out] $-a^5/(13*x^{13}) - (5*a^4*b)/(12*x^{12}) - (10*a^3*b^2)/(11*x^{11}) - (a^2*b^3)/x^{10} - (5*a*b^4)/(9*x^9) - b^5/(8*x^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^{14}} dx &= \int \left(\frac{a^5}{x^{14}} + \frac{5a^4b}{x^{13}} + \frac{10a^3b^2}{x^{12}} + \frac{10a^2b^3}{x^{11}} + \frac{5ab^4}{x^{10}} + \frac{b^5}{x^9} \right) dx \\ &= -\frac{a^5}{13x^{13}} - \frac{5a^4b}{12x^{12}} - \frac{10a^3b^2}{11x^{11}} - \frac{a^2b^3}{x^{10}} - \frac{5ab^4}{9x^9} - \frac{b^5}{8x^8} \end{aligned}$$

Mathematica [A] time = 0.00, size = 67, normalized size = 1.00

$$-\frac{a^5}{13x^{13}} - \frac{5a^4b}{12x^{12}} - \frac{10a^3b^2}{11x^{11}} - \frac{a^2b^3}{x^{10}} - \frac{5ab^4}{9x^9} - \frac{b^5}{8x^8}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^14,x]

[Out] $-1/13*a^5/x^{13} - (5*a^4*b)/(12*x^{12}) - (10*a^3*b^2)/(11*x^{11}) - (a^2*b^3)/x^{10} - (5*a*b^4)/(9*x^9) - b^5/(8*x^8)$

fricas [A] time = 0.43, size = 57, normalized size = 0.85

$$\frac{1287 b^5 x^5 + 5720 a b^4 x^4 + 10296 a^2 b^3 x^3 + 9360 a^3 b^2 x^2 + 4290 a^4 b x + 792 a^5}{10296 x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^14,x, algorithm="fricas")

[Out] $-1/10296*(1287*b^5*x^5 + 5720*a*b^4*x^4 + 10296*a^2*b^3*x^3 + 9360*a^3*b^2*x^2 + 4290*a^4*b*x + 792*a^5)/x^{13}$

giac [A] time = 1.12, size = 57, normalized size = 0.85

$$\frac{1287 b^5 x^5 + 5720 a b^4 x^4 + 10296 a^2 b^3 x^3 + 9360 a^3 b^2 x^2 + 4290 a^4 b x + 792 a^5}{10296 x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^14,x, algorithm="giac")

[Out] $-1/10296*(1287*b^5*x^5 + 5720*a*b^4*x^4 + 10296*a^2*b^3*x^3 + 9360*a^3*b^2*x^2 + 4290*a^4*b*x + 792*a^5)/x^{13}$

maple [A] time = 0.00, size = 58, normalized size = 0.87

$$\frac{b^5}{8x^8} - \frac{5ab^4}{9x^9} - \frac{a^2b^3}{x^{10}} - \frac{10a^3b^2}{11x^{11}} - \frac{5a^4b}{12x^{12}} - \frac{a^5}{13x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^14,x)

[Out] $-1/13*a^5/x^{13}-5/12*a^4*b/x^{12}-10/11*a^3*b^2/x^{11}-a^2*b^3/x^{10}-5/9*a*b^4/x^9-1/8*b^5/x^8$

maxima [A] time = 1.38, size = 57, normalized size = 0.85

$$\frac{1287 b^5 x^5 + 5720 a b^4 x^4 + 10296 a^2 b^3 x^3 + 9360 a^3 b^2 x^2 + 4290 a^4 b x + 792 a^5}{10296 x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^14,x, algorithm="maxima")

[Out] $-1/10296*(1287*b^5*x^5 + 5720*a*b^4*x^4 + 10296*a^2*b^3*x^3 + 9360*a^3*b^2*x^2 + 4290*a^4*b*x + 792*a^5)/x^{13}$

mupad [B] time = 0.04, size = 56, normalized size = 0.84

$$\frac{\frac{a^5}{13} + \frac{5a^4bx}{12} + \frac{10a^3b^2x^2}{11} + a^2b^3x^3 + \frac{5ab^4x^4}{9} + \frac{b^5x^5}{8}}{x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^14,x)

[Out] $-(a^5/13 + (b^5*x^5)/8 + (5*a*b^4*x^4)/9 + (10*a^3*b^2*x^2)/11 + a^2*b^3*x^3 + (5*a^4*b*x)/12)/x^{13}$

sympy [A] time = 0.62, size = 61, normalized size = 0.91

$$\frac{-792a^5 - 4290a^4bx - 9360a^3b^2x^2 - 10296a^2b^3x^3 - 5720ab^4x^4 - 1287b^5x^5}{10296x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**14,x)

[Out] $(-792*a**5 - 4290*a**4*b*x - 9360*a**3*b**2*x**2 - 10296*a**2*b**3*x**3 - 5720*a*b**4*x**4 - 1287*b**5*x**5)/(10296*x**13)$

3.98 $\int x^8(a + bx)^7 dx$

Optimal. Leaf size=95

$$\frac{a^7x^9}{9} + \frac{7}{10}a^6bx^{10} + \frac{21}{11}a^5b^2x^{11} + \frac{35}{12}a^4b^3x^{12} + \frac{35}{13}a^3b^4x^{13} + \frac{3}{2}a^2b^5x^{14} + \frac{7}{15}ab^6x^{15} + \frac{b^7x^{16}}{16}$$

[Out] 1/9*a^7*x^9+7/10*a^6*b*x^10+21/11*a^5*b^2*x^11+35/12*a^4*b^3*x^12+35/13*a^3*b^4*x^13+3/2*a^2*b^5*x^14+7/15*a*b^6*x^15+1/16*b^7*x^16

Rubi [A] time = 0.05, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3}{2}a^2b^5x^{14} + \frac{35}{13}a^3b^4x^{13} + \frac{35}{12}a^4b^3x^{12} + \frac{21}{11}a^5b^2x^{11} + \frac{7}{10}a^6bx^{10} + \frac{a^7x^9}{9} + \frac{7}{15}ab^6x^{15} + \frac{b^7x^{16}}{16}$$

Antiderivative was successfully verified.

[In] Int[x^8*(a + b*x)^7, x]

[Out] (a^7*x^9)/9 + (7*a^6*b*x^10)/10 + (21*a^5*b^2*x^11)/11 + (35*a^4*b^3*x^12)/12 + (35*a^3*b^4*x^13)/13 + (3*a^2*b^5*x^14)/2 + (7*a*b^6*x^15)/15 + (b^7*x^16)/16

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^8(a + bx)^7 dx &= \int (a^7x^8 + 7a^6bx^9 + 21a^5b^2x^{10} + 35a^4b^3x^{11} + 35a^3b^4x^{12} + 21a^2b^5x^{13} + 7ab^6x^{14} + b^7x^{15}) dx \\ &= \frac{a^7x^9}{9} + \frac{7}{10}a^6bx^{10} + \frac{21}{11}a^5b^2x^{11} + \frac{35}{12}a^4b^3x^{12} + \frac{35}{13}a^3b^4x^{13} + \frac{3}{2}a^2b^5x^{14} + \frac{7}{15}ab^6x^{15} + \frac{b^7x^{16}}{16} \end{aligned}$$

Mathematica [A] time = 0.00, size = 95, normalized size = 1.00

$$\frac{a^7x^9}{9} + \frac{7}{10}a^6bx^{10} + \frac{21}{11}a^5b^2x^{11} + \frac{35}{12}a^4b^3x^{12} + \frac{35}{13}a^3b^4x^{13} + \frac{3}{2}a^2b^5x^{14} + \frac{7}{15}ab^6x^{15} + \frac{b^7x^{16}}{16}$$

Antiderivative was successfully verified.

[In] Integrate[x^8*(a + b*x)^7,x]

[Out] (a^7*x^9)/9 + (7*a^6*b*x^10)/10 + (21*a^5*b^2*x^11)/11 + (35*a^4*b^3*x^12)/12 + (35*a^3*b^4*x^13)/13 + (3*a^2*b^5*x^14)/2 + (7*a*b^6*x^15)/15 + (b^7*x^16)/16

fricas [A] time = 0.41, size = 79, normalized size = 0.83

$$\frac{1}{16}x^{16}b^7 + \frac{7}{15}x^{15}b^6a + \frac{3}{2}x^{14}b^5a^2 + \frac{35}{13}x^{13}b^4a^3 + \frac{35}{12}x^{12}b^3a^4 + \frac{21}{11}x^{11}b^2a^5 + \frac{7}{10}x^{10}ba^6 + \frac{1}{9}x^9a^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8*(b*x+a)^7,x, algorithm="fricas")

[Out] 1/16*x^16*b^7 + 7/15*x^15*b^6*a + 3/2*x^14*b^5*a^2 + 35/13*x^13*b^4*a^3 + 35/12*x^12*b^3*a^4 + 21/11*x^11*b^2*a^5 + 7/10*x^10*b*a^6 + 1/9*x^9*a^7

giac [A] time = 0.95, size = 79, normalized size = 0.83

$$\frac{1}{16}b^7x^{16} + \frac{7}{15}ab^6x^{15} + \frac{3}{2}a^2b^5x^{14} + \frac{35}{13}a^3b^4x^{13} + \frac{35}{12}a^4b^3x^{12} + \frac{21}{11}a^5b^2x^{11} + \frac{7}{10}a^6bx^{10} + \frac{1}{9}a^7x^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8*(b*x+a)^7,x, algorithm="giac")

[Out] 1/16*b^7*x^16 + 7/15*a*b^6*x^15 + 3/2*a^2*b^5*x^14 + 35/13*a^3*b^4*x^13 + 35/12*a^4*b^3*x^12 + 21/11*a^5*b^2*x^11 + 7/10*a^6*b*x^10 + 1/9*a^7*x^9

maple [A] time = 0.00, size = 80, normalized size = 0.84

$$\frac{1}{16}b^7x^{16} + \frac{7}{15}ab^6x^{15} + \frac{3}{2}a^2b^5x^{14} + \frac{35}{13}a^3b^4x^{13} + \frac{35}{12}a^4b^3x^{12} + \frac{21}{11}a^5b^2x^{11} + \frac{7}{10}a^6bx^{10} + \frac{1}{9}a^7x^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^8*(b*x+a)^7,x)

[Out] 1/9*a^7*x^9+7/10*a^6*b*x^10+21/11*a^5*b^2*x^11+35/12*a^4*b^3*x^12+35/13*a^3*b^4*x^13+3/2*a^2*b^5*x^14+7/15*a*b^6*x^15+1/16*b^7*x^16

maxima [A] time = 1.40, size = 79, normalized size = 0.83

$$\frac{1}{16}b^7x^{16} + \frac{7}{15}ab^6x^{15} + \frac{3}{2}a^2b^5x^{14} + \frac{35}{13}a^3b^4x^{13} + \frac{35}{12}a^4b^3x^{12} + \frac{21}{11}a^5b^2x^{11} + \frac{7}{10}a^6bx^{10} + \frac{1}{9}a^7x^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8*(b*x+a)^7,x, algorithm="maxima")

[Out] 1/16*b^7*x^16 + 7/15*a*b^6*x^15 + 3/2*a^2*b^5*x^14 + 35/13*a^3*b^4*x^13 + 35/12*a^4*b^3*x^12 + 21/11*a^5*b^2*x^11 + 7/10*a^6*b*x^10 + 1/9*a^7*x^9

mupad [B] time = 0.15, size = 79, normalized size = 0.83

$$\frac{a^7 x^9}{9} + \frac{7 a^6 b x^{10}}{10} + \frac{21 a^5 b^2 x^{11}}{11} + \frac{35 a^4 b^3 x^{12}}{12} + \frac{35 a^3 b^4 x^{13}}{13} + \frac{3 a^2 b^5 x^{14}}{2} + \frac{7 a b^6 x^{15}}{15} + \frac{b^7 x^{16}}{16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^8*(a + b*x)^7,x)

[Out] (a^7*x^9)/9 + (b^7*x^16)/16 + (7*a^6*b*x^10)/10 + (7*a*b^6*x^15)/15 + (21*a^5*b^2*x^11)/11 + (35*a^4*b^3*x^12)/12 + (35*a^3*b^4*x^13)/13 + (3*a^2*b^5*x^14)/2

sympy [A] time = 0.10, size = 94, normalized size = 0.99

$$\frac{a^7 x^9}{9} + \frac{7 a^6 b x^{10}}{10} + \frac{21 a^5 b^2 x^{11}}{11} + \frac{35 a^4 b^3 x^{12}}{12} + \frac{35 a^3 b^4 x^{13}}{13} + \frac{3 a^2 b^5 x^{14}}{2} + \frac{7 a b^6 x^{15}}{15} + \frac{b^7 x^{16}}{16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**8*(b*x+a)**7,x)

[Out] a**7*x**9/9 + 7*a**6*b*x**10/10 + 21*a**5*b**2*x**11/11 + 35*a**4*b**3*x**12/12 + 35*a**3*b**4*x**13/13 + 3*a**2*b**5*x**14/2 + 7*a*b**6*x**15/15 + b**7*x**16/16

3.99 $\int x^7(a + bx)^7 dx$

Optimal. Leaf size=95

$$\frac{a^7 x^8}{8} + \frac{7}{9} a^6 b x^9 + \frac{21}{10} a^5 b^2 x^{10} + \frac{35}{11} a^4 b^3 x^{11} + \frac{35}{12} a^3 b^4 x^{12} + \frac{21}{13} a^2 b^5 x^{13} + \frac{1}{2} a b^6 x^{14} + \frac{b^7 x^{15}}{15}$$

[Out] $1/8*a^7*x^8+7/9*a^6*b*x^9+21/10*a^5*b^2*x^{10}+35/11*a^4*b^3*x^{11}+35/12*a^3*b^4*x^{12}+21/13*a^2*b^5*x^{13}+1/2*a*b^6*x^{14}+1/15*b^7*x^{15}$

Rubi [A] time = 0.04, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{21}{13} a^2 b^5 x^{13} + \frac{35}{12} a^3 b^4 x^{12} + \frac{35}{11} a^4 b^3 x^{11} + \frac{21}{10} a^5 b^2 x^{10} + \frac{7}{9} a^6 b x^9 + \frac{a^7 x^8}{8} + \frac{1}{2} a b^6 x^{14} + \frac{b^7 x^{15}}{15}$$

Antiderivative was successfully verified.

[In] Int[x^7*(a + b*x)^7, x]

[Out] $(a^7*x^8)/8 + (7*a^6*b*x^9)/9 + (21*a^5*b^2*x^{10})/10 + (35*a^4*b^3*x^{11})/11 + (35*a^3*b^4*x^{12})/12 + (21*a^2*b^5*x^{13})/13 + (a*b^6*x^{14})/2 + (b^7*x^{15})/15$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int x^7(a + bx)^7 dx &= \int (a^7 x^7 + 7a^6 b x^8 + 21a^5 b^2 x^9 + 35a^4 b^3 x^{10} + 35a^3 b^4 x^{11} + 21a^2 b^5 x^{12} + 7ab^6 x^{13} + b^7 x^{14}) dx \\ &= \frac{a^7 x^8}{8} + \frac{7}{9} a^6 b x^9 + \frac{21}{10} a^5 b^2 x^{10} + \frac{35}{11} a^4 b^3 x^{11} + \frac{35}{12} a^3 b^4 x^{12} + \frac{21}{13} a^2 b^5 x^{13} + \frac{1}{2} a b^6 x^{14} + \frac{b^7 x^{15}}{15} \end{aligned}$$

Mathematica [A] time = 0.00, size = 95, normalized size = 1.00

$$\frac{a^7 x^8}{8} + \frac{7}{9} a^6 b x^9 + \frac{21}{10} a^5 b^2 x^{10} + \frac{35}{11} a^4 b^3 x^{11} + \frac{35}{12} a^3 b^4 x^{12} + \frac{21}{13} a^2 b^5 x^{13} + \frac{1}{2} a b^6 x^{14} + \frac{b^7 x^{15}}{15}$$

Antiderivative was successfully verified.

[In] Integrate[x^7*(a + b*x)^7,x]

[Out] (a^7*x^8)/8 + (7*a^6*b*x^9)/9 + (21*a^5*b^2*x^10)/10 + (35*a^4*b^3*x^11)/11 + (35*a^3*b^4*x^12)/12 + (21*a^2*b^5*x^13)/13 + (a*b^6*x^14)/2 + (b^7*x^15)/15

fricas [A] time = 0.42, size = 79, normalized size = 0.83

$$\frac{1}{15}x^{15}b^7 + \frac{1}{2}x^{14}b^6a + \frac{21}{13}x^{13}b^5a^2 + \frac{35}{12}x^{12}b^4a^3 + \frac{35}{11}x^{11}b^3a^4 + \frac{21}{10}x^{10}b^2a^5 + \frac{7}{9}x^9ba^6 + \frac{1}{8}x^8a^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^7,x, algorithm="fricas")

[Out] 1/15*x^15*b^7 + 1/2*x^14*b^6*a + 21/13*x^13*b^5*a^2 + 35/12*x^12*b^4*a^3 + 35/11*x^11*b^3*a^4 + 21/10*x^10*b^2*a^5 + 7/9*x^9*b*a^6 + 1/8*x^8*a^7

giac [A] time = 0.99, size = 79, normalized size = 0.83

$$\frac{1}{15}b^7x^{15} + \frac{1}{2}ab^6x^{14} + \frac{21}{13}a^2b^5x^{13} + \frac{35}{12}a^3b^4x^{12} + \frac{35}{11}a^4b^3x^{11} + \frac{21}{10}a^5b^2x^{10} + \frac{7}{9}a^6bx^9 + \frac{1}{8}a^7x^8$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^7,x, algorithm="giac")

[Out] 1/15*b^7*x^15 + 1/2*a*b^6*x^14 + 21/13*a^2*b^5*x^13 + 35/12*a^3*b^4*x^12 + 35/11*a^4*b^3*x^11 + 21/10*a^5*b^2*x^10 + 7/9*a^6*b*x^9 + 1/8*a^7*x^8

maple [A] time = 0.00, size = 80, normalized size = 0.84

$$\frac{1}{15}b^7x^{15} + \frac{1}{2}ab^6x^{14} + \frac{21}{13}a^2b^5x^{13} + \frac{35}{12}a^3b^4x^{12} + \frac{35}{11}a^4b^3x^{11} + \frac{21}{10}a^5b^2x^{10} + \frac{7}{9}a^6bx^9 + \frac{1}{8}a^7x^8$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7*(b*x+a)^7,x)

[Out] 1/8*a^7*x^8+7/9*a^6*b*x^9+21/10*a^5*b^2*x^10+35/11*a^4*b^3*x^11+35/12*a^3*b^4*x^12+21/13*a^2*b^5*x^13+1/2*a*b^6*x^14+1/15*b^7*x^15

maxima [A] time = 1.30, size = 79, normalized size = 0.83

$$\frac{1}{15}b^7x^{15} + \frac{1}{2}ab^6x^{14} + \frac{21}{13}a^2b^5x^{13} + \frac{35}{12}a^3b^4x^{12} + \frac{35}{11}a^4b^3x^{11} + \frac{21}{10}a^5b^2x^{10} + \frac{7}{9}a^6bx^9 + \frac{1}{8}a^7x^8$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^7,x, algorithm="maxima")

[Out] 1/15*b^7*x^15 + 1/2*a*b^6*x^14 + 21/13*a^2*b^5*x^13 + 35/12*a^3*b^4*x^12 + 35/11*a^4*b^3*x^11 + 21/10*a^5*b^2*x^10 + 7/9*a^6*b*x^9 + 1/8*a^7*x^8

mupad [B] time = 0.07, size = 79, normalized size = 0.83

$$\frac{a^7 x^8}{8} + \frac{7 a^6 b x^9}{9} + \frac{21 a^5 b^2 x^{10}}{10} + \frac{35 a^4 b^3 x^{11}}{11} + \frac{35 a^3 b^4 x^{12}}{12} + \frac{21 a^2 b^5 x^{13}}{13} + \frac{a b^6 x^{14}}{2} + \frac{b^7 x^{15}}{15}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7*(a + b*x)^7,x)

[Out] (a^7*x^8)/8 + (b^7*x^15)/15 + (7*a^6*b*x^9)/9 + (a*b^6*x^14)/2 + (21*a^5*b^2*x^10)/10 + (35*a^4*b^3*x^11)/11 + (35*a^3*b^4*x^12)/12 + (21*a^2*b^5*x^13)/13

sympy [A] time = 0.09, size = 92, normalized size = 0.97

$$\frac{a^7 x^8}{8} + \frac{7 a^6 b x^9}{9} + \frac{21 a^5 b^2 x^{10}}{10} + \frac{35 a^4 b^3 x^{11}}{11} + \frac{35 a^3 b^4 x^{12}}{12} + \frac{21 a^2 b^5 x^{13}}{13} + \frac{a b^6 x^{14}}{2} + \frac{b^7 x^{15}}{15}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**7*(b*x+a)**7,x)

[Out] a**7*x**8/8 + 7*a**6*b*x**9/9 + 21*a**5*b**2*x**10/10 + 35*a**4*b**3*x**11/11 + 35*a**3*b**4*x**12/12 + 21*a**2*b**5*x**13/13 + a*b**6*x**14/2 + b**7*x**15/15

3.100 $\int x^6(a + bx)^7 dx$

Optimal. Leaf size=95

$$\frac{a^7x^7}{7} + \frac{7}{8}a^6bx^8 + \frac{7}{3}a^5b^2x^9 + \frac{7}{2}a^4b^3x^{10} + \frac{35}{11}a^3b^4x^{11} + \frac{7}{4}a^2b^5x^{12} + \frac{7}{13}ab^6x^{13} + \frac{b^7x^{14}}{14}$$

[Out] $1/7*a^7*x^7+7/8*a^6*b*x^8+7/3*a^5*b^2*x^9+7/2*a^4*b^3*x^{10}+35/11*a^3*b^4*x^{11}+7/4*a^2*b^5*x^{12}+7/13*a*b^6*x^{13}+1/14*b^7*x^{14}$

Rubi [A] time = 0.04, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{7}{4}a^2b^5x^{12} + \frac{35}{11}a^3b^4x^{11} + \frac{7}{2}a^4b^3x^{10} + \frac{7}{3}a^5b^2x^9 + \frac{7}{8}a^6bx^8 + \frac{a^7x^7}{7} + \frac{7}{13}ab^6x^{13} + \frac{b^7x^{14}}{14}$$

Antiderivative was successfully verified.

[In] Int[x^6*(a + b*x)^7,x]

[Out] $(a^7*x^7)/7 + (7*a^6*b*x^8)/8 + (7*a^5*b^2*x^9)/3 + (7*a^4*b^3*x^{10})/2 + (35*a^3*b^4*x^{11})/11 + (7*a^2*b^5*x^{12})/4 + (7*a*b^6*x^{13})/13 + (b^7*x^{14})/14$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^6(a + bx)^7 dx &= \int (a^7x^6 + 7a^6bx^7 + 21a^5b^2x^8 + 35a^4b^3x^9 + 35a^3b^4x^{10} + 21a^2b^5x^{11} + 7ab^6x^{12} + b^7x^{13}) dx \\ &= \frac{a^7x^7}{7} + \frac{7}{8}a^6bx^8 + \frac{7}{3}a^5b^2x^9 + \frac{7}{2}a^4b^3x^{10} + \frac{35}{11}a^3b^4x^{11} + \frac{7}{4}a^2b^5x^{12} + \frac{7}{13}ab^6x^{13} + \frac{b^7x^{14}}{14} \end{aligned}$$

Mathematica [A] time = 0.00, size = 95, normalized size = 1.00

$$\frac{a^7x^7}{7} + \frac{7}{8}a^6bx^8 + \frac{7}{3}a^5b^2x^9 + \frac{7}{2}a^4b^3x^{10} + \frac{35}{11}a^3b^4x^{11} + \frac{7}{4}a^2b^5x^{12} + \frac{7}{13}ab^6x^{13} + \frac{b^7x^{14}}{14}$$

Antiderivative was successfully verified.

[In] Integrate[x^6*(a + b*x)^7,x]

[Out] (a^7*x^7)/7 + (7*a^6*b*x^8)/8 + (7*a^5*b^2*x^9)/3 + (7*a^4*b^3*x^10)/2 + (3*5*a^3*b^4*x^11)/11 + (7*a^2*b^5*x^12)/4 + (7*a*b^6*x^13)/13 + (b^7*x^14)/14

fricas [A] time = 0.40, size = 79, normalized size = 0.83

$$\frac{1}{14}x^{14}b^7 + \frac{7}{13}x^{13}b^6a + \frac{7}{4}x^{12}b^5a^2 + \frac{35}{11}x^{11}b^4a^3 + \frac{7}{2}x^{10}b^3a^4 + \frac{7}{3}x^9b^2a^5 + \frac{7}{8}x^8ba^6 + \frac{1}{7}x^7a^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^7,x, algorithm="fricas")

[Out] 1/14*x^14*b^7 + 7/13*x^13*b^6*a + 7/4*x^12*b^5*a^2 + 35/11*x^11*b^4*a^3 + 7/2*x^10*b^3*a^4 + 7/3*x^9*b^2*a^5 + 7/8*x^8*b*a^6 + 1/7*x^7*a^7

giac [A] time = 1.01, size = 79, normalized size = 0.83

$$\frac{1}{14}b^7x^{14} + \frac{7}{13}ab^6x^{13} + \frac{7}{4}a^2b^5x^{12} + \frac{35}{11}a^3b^4x^{11} + \frac{7}{2}a^4b^3x^{10} + \frac{7}{3}a^5b^2x^9 + \frac{7}{8}a^6bx^8 + \frac{1}{7}a^7x^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^7,x, algorithm="giac")

[Out] 1/14*b^7*x^14 + 7/13*a*b^6*x^13 + 7/4*a^2*b^5*x^12 + 35/11*a^3*b^4*x^11 + 7/2*a^4*b^3*x^10 + 7/3*a^5*b^2*x^9 + 7/8*a^6*b*x^8 + 1/7*a^7*x^7

maple [A] time = 0.00, size = 80, normalized size = 0.84

$$\frac{1}{14}b^7x^{14} + \frac{7}{13}ab^6x^{13} + \frac{7}{4}a^2b^5x^{12} + \frac{35}{11}a^3b^4x^{11} + \frac{7}{2}a^4b^3x^{10} + \frac{7}{3}a^5b^2x^9 + \frac{7}{8}a^6bx^8 + \frac{1}{7}a^7x^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6*(b*x+a)^7,x)

[Out] 1/7*a^7*x^7+7/8*a^6*b*x^8+7/3*a^5*b^2*x^9+7/2*a^4*b^3*x^10+35/11*a^3*b^4*x^11+7/4*a^2*b^5*x^12+7/13*a*b^6*x^13+1/14*b^7*x^14

maxima [A] time = 1.29, size = 79, normalized size = 0.83

$$\frac{1}{14}b^7x^{14} + \frac{7}{13}ab^6x^{13} + \frac{7}{4}a^2b^5x^{12} + \frac{35}{11}a^3b^4x^{11} + \frac{7}{2}a^4b^3x^{10} + \frac{7}{3}a^5b^2x^9 + \frac{7}{8}a^6bx^8 + \frac{1}{7}a^7x^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^7,x, algorithm="maxima")

[Out] $1/14*b^7*x^{14} + 7/13*a*b^6*x^{13} + 7/4*a^2*b^5*x^{12} + 35/11*a^3*b^4*x^{11} + 7/2*a^4*b^3*x^{10} + 7/3*a^5*b^2*x^9 + 7/8*a^6*b*x^8 + 1/7*a^7*x^7$

mupad [B] time = 0.07, size = 79, normalized size = 0.83

$$\frac{a^7 x^7}{7} + \frac{7 a^6 b x^8}{8} + \frac{7 a^5 b^2 x^9}{3} + \frac{7 a^4 b^3 x^{10}}{2} + \frac{35 a^3 b^4 x^{11}}{11} + \frac{7 a^2 b^5 x^{12}}{4} + \frac{7 a b^6 x^{13}}{13} + \frac{b^7 x^{14}}{14}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^6*(a + b*x)^7,x)`

[Out] $(a^7*x^7)/7 + (b^7*x^{14})/14 + (7*a^6*b*x^8)/8 + (7*a*b^6*x^{13})/13 + (7*a^5*b^2*x^9)/3 + (7*a^4*b^3*x^{10})/2 + (35*a^3*b^4*x^{11})/11 + (7*a^2*b^5*x^{12})/4$

sympy [A] time = 0.11, size = 94, normalized size = 0.99

$$\frac{a^7 x^7}{7} + \frac{7 a^6 b x^8}{8} + \frac{7 a^5 b^2 x^9}{3} + \frac{7 a^4 b^3 x^{10}}{2} + \frac{35 a^3 b^4 x^{11}}{11} + \frac{7 a^2 b^5 x^{12}}{4} + \frac{7 a b^6 x^{13}}{13} + \frac{b^7 x^{14}}{14}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**6*(b*x+a)**7,x)`

[Out] $a**7*x**7/7 + 7*a**6*b*x**8/8 + 7*a**5*b**2*x**9/3 + 7*a**4*b**3*x**10/2 + 35*a**3*b**4*x**11/11 + 7*a**2*b**5*x**12/4 + 7*a*b**6*x**13/13 + b**7*x**14/14$

3.101 $\int x^5(a + bx)^7 dx$

Optimal. Leaf size=96

$$-\frac{a^5(a+bx)^8}{8b^6} + \frac{5a^4(a+bx)^9}{9b^6} - \frac{a^3(a+bx)^{10}}{b^6} + \frac{10a^2(a+bx)^{11}}{11b^6} + \frac{(a+bx)^{13}}{13b^6} - \frac{5a(a+bx)^{12}}{12b^6}$$

[Out] $-1/8*a^5*(b*x+a)^8/b^6+5/9*a^4*(b*x+a)^9/b^6-a^3*(b*x+a)^{10}/b^6+10/11*a^2*(b*x+a)^{11}/b^6-5/12*a*(b*x+a)^{12}/b^6+1/13*(b*x+a)^{13}/b^6$

Rubi [A] time = 0.04, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{10a^2(a+bx)^{11}}{11b^6} - \frac{a^3(a+bx)^{10}}{b^6} + \frac{5a^4(a+bx)^9}{9b^6} - \frac{a^5(a+bx)^8}{8b^6} + \frac{(a+bx)^{13}}{13b^6} - \frac{5a(a+bx)^{12}}{12b^6}$$

Antiderivative was successfully verified.

[In] Int[x^5*(a + b*x)^7, x]

[Out] $-(a^5*(a + b*x)^8)/(8*b^6) + (5*a^4*(a + b*x)^9)/(9*b^6) - (a^3*(a + b*x)^{10})/b^6 + (10*a^2*(a + b*x)^{11})/(11*b^6) - (5*a*(a + b*x)^{12})/(12*b^6) + (a + b*x)^{13}/(13*b^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^5(a + bx)^7 dx &= \int \left(-\frac{a^5(a+bx)^7}{b^5} + \frac{5a^4(a+bx)^8}{b^5} - \frac{10a^3(a+bx)^9}{b^5} + \frac{10a^2(a+bx)^{10}}{b^5} - \frac{5a(a+bx)^{11}}{b^5} + \frac{(a+bx)^{13}}{b^5} \right) dx \\ &= -\frac{a^5(a+bx)^8}{8b^6} + \frac{5a^4(a+bx)^9}{9b^6} - \frac{a^3(a+bx)^{10}}{b^6} + \frac{10a^2(a+bx)^{11}}{11b^6} - \frac{5a(a+bx)^{12}}{12b^6} + \frac{(a+bx)^{13}}{13b^6} \end{aligned}$$

Mathematica [A] time = 0.00, size = 92, normalized size = 0.96

$$\frac{a^7 x^6}{6} + a^6 b x^7 + \frac{21}{8} a^5 b^2 x^8 + \frac{35}{9} a^4 b^3 x^9 + \frac{7}{2} a^3 b^4 x^{10} + \frac{21}{11} a^2 b^5 x^{11} + \frac{7}{12} a b^6 x^{12} + \frac{b^7 x^{13}}{13}$$

Antiderivative was successfully verified.

[In] Integrate[x^5*(a + b*x)^7,x]

[Out] (a^7*x^6)/6 + a^6*b*x^7 + (21*a^5*b^2*x^8)/8 + (35*a^4*b^3*x^9)/9 + (7*a^3*b^4*x^10)/2 + (21*a^2*b^5*x^11)/11 + (7*a*b^6*x^12)/12 + (b^7*x^13)/13

fricas [A] time = 0.38, size = 78, normalized size = 0.81

$$\frac{1}{13}x^{13}b^7 + \frac{7}{12}x^{12}b^6a + \frac{21}{11}x^{11}b^5a^2 + \frac{7}{2}x^{10}b^4a^3 + \frac{35}{9}x^9b^3a^4 + \frac{21}{8}x^8b^2a^5 + x^7ba^6 + \frac{1}{6}x^6a^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^7,x, algorithm="fricas")

[Out] 1/13*x^13*b^7 + 7/12*x^12*b^6*a + 21/11*x^11*b^5*a^2 + 7/2*x^10*b^4*a^3 + 35/9*x^9*b^3*a^4 + 21/8*x^8*b^2*a^5 + x^7*b*a^6 + 1/6*x^6*a^7

giac [A] time = 1.08, size = 78, normalized size = 0.81

$$\frac{1}{13}b^7x^{13} + \frac{7}{12}ab^6x^{12} + \frac{21}{11}a^2b^5x^{11} + \frac{7}{2}a^3b^4x^{10} + \frac{35}{9}a^4b^3x^9 + \frac{21}{8}a^5b^2x^8 + a^6bx^7 + \frac{1}{6}a^7x^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^7,x, algorithm="giac")

[Out] 1/13*b^7*x^13 + 7/12*a*b^6*x^12 + 21/11*a^2*b^5*x^11 + 7/2*a^3*b^4*x^10 + 35/9*a^4*b^3*x^9 + 21/8*a^5*b^2*x^8 + a^6*b*x^7 + 1/6*a^7*x^6

maple [A] time = 0.00, size = 79, normalized size = 0.82

$$\frac{1}{13}b^7x^{13} + \frac{7}{12}ab^6x^{12} + \frac{21}{11}a^2b^5x^{11} + \frac{7}{2}a^3b^4x^{10} + \frac{35}{9}a^4b^3x^9 + \frac{21}{8}a^5b^2x^8 + a^6bx^7 + \frac{1}{6}a^7x^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5*(b*x+a)^7,x)

[Out] 1/13*b^7*x^13+7/12*a*b^6*x^12+21/11*a^2*b^5*x^11+7/2*a^3*b^4*x^10+35/9*a^4*b^3*x^9+21/8*a^5*b^2*x^8+a^6*b*x^7+1/6*a^7*x^6

maxima [A] time = 1.39, size = 78, normalized size = 0.81

$$\frac{1}{13}b^7x^{13} + \frac{7}{12}ab^6x^{12} + \frac{21}{11}a^2b^5x^{11} + \frac{7}{2}a^3b^4x^{10} + \frac{35}{9}a^4b^3x^9 + \frac{21}{8}a^5b^2x^8 + a^6bx^7 + \frac{1}{6}a^7x^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^7,x, algorithm="maxima")

[Out] 1/13*b^7*x^13 + 7/12*a*b^6*x^12 + 21/11*a^2*b^5*x^11 + 7/2*a^3*b^4*x^10 + 35/9*a^4*b^3*x^9 + 21/8*a^5*b^2*x^8 + a^6*b*x^7 + 1/6*a^7*x^6

mupad [B] time = 0.06, size = 78, normalized size = 0.81

$$\frac{a^7 x^6}{6} + a^6 b x^7 + \frac{21 a^5 b^2 x^8}{8} + \frac{35 a^4 b^3 x^9}{9} + \frac{7 a^3 b^4 x^{10}}{2} + \frac{21 a^2 b^5 x^{11}}{11} + \frac{7 a b^6 x^{12}}{12} + \frac{b^7 x^{13}}{13}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5*(a + b*x)^7,x)

[Out] (a^7*x^6)/6 + (b^7*x^13)/13 + a^6*b*x^7 + (7*a*b^6*x^12)/12 + (21*a^5*b^2*x^8)/8 + (35*a^4*b^3*x^9)/9 + (7*a^3*b^4*x^10)/2 + (21*a^2*b^5*x^11)/11

sympy [A] time = 0.11, size = 90, normalized size = 0.94

$$\frac{a^7 x^6}{6} + a^6 b x^7 + \frac{21 a^5 b^2 x^8}{8} + \frac{35 a^4 b^3 x^9}{9} + \frac{7 a^3 b^4 x^{10}}{2} + \frac{21 a^2 b^5 x^{11}}{11} + \frac{7 a b^6 x^{12}}{12} + \frac{b^7 x^{13}}{13}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5*(b*x+a)**7,x)

[Out] a**7*x**6/6 + a**6*b*x**7 + 21*a**5*b**2*x**8/8 + 35*a**4*b**3*x**9/9 + 7*a**3*b**4*x**10/2 + 21*a**2*b**5*x**11/11 + 7*a*b**6*x**12/12 + b**7*x**13/13

3.102 $\int x^4(a + bx)^7 dx$

Optimal. Leaf size=81

$$\frac{a^4(a + bx)^8}{8b^5} - \frac{4a^3(a + bx)^9}{9b^5} + \frac{3a^2(a + bx)^{10}}{5b^5} + \frac{(a + bx)^{12}}{12b^5} - \frac{4a(a + bx)^{11}}{11b^5}$$

[Out] $1/8*a^4*(b*x+a)^8/b^5-4/9*a^3*(b*x+a)^9/b^5+3/5*a^2*(b*x+a)^{10}/b^5-4/11*a*(b*x+a)^{11}/b^5+1/12*(b*x+a)^{12}/b^5$

Rubi [A] time = 0.04, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3a^2(a + bx)^{10}}{5b^5} - \frac{4a^3(a + bx)^9}{9b^5} + \frac{a^4(a + bx)^8}{8b^5} + \frac{(a + bx)^{12}}{12b^5} - \frac{4a(a + bx)^{11}}{11b^5}$$

Antiderivative was successfully verified.

[In] Int[x^4*(a + b*x)^7, x]

[Out] $(a^4*(a + b*x)^8)/(8*b^5) - (4*a^3*(a + b*x)^9)/(9*b^5) + (3*a^2*(a + b*x)^{10})/(5*b^5) - (4*a*(a + b*x)^{11})/(11*b^5) + (a + b*x)^{12}/(12*b^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^4(a + bx)^7 dx &= \int \left(\frac{a^4(a + bx)^7}{b^4} - \frac{4a^3(a + bx)^8}{b^4} + \frac{6a^2(a + bx)^9}{b^4} - \frac{4a(a + bx)^{10}}{b^4} + \frac{(a + bx)^{11}}{b^4} \right) dx \\ &= \frac{a^4(a + bx)^8}{8b^5} - \frac{4a^3(a + bx)^9}{9b^5} + \frac{3a^2(a + bx)^{10}}{5b^5} - \frac{4a(a + bx)^{11}}{11b^5} + \frac{(a + bx)^{12}}{12b^5} \end{aligned}$$

Mathematica [A] time = 0.00, size = 93, normalized size = 1.15

$$\frac{a^7 x^5}{5} + \frac{7}{6} a^6 b x^6 + 3 a^5 b^2 x^7 + \frac{35}{8} a^4 b^3 x^8 + \frac{35}{9} a^3 b^4 x^9 + \frac{21}{10} a^2 b^5 x^{10} + \frac{7}{11} a b^6 x^{11} + \frac{b^7 x^{12}}{12}$$

Antiderivative was successfully verified.

[In] Integrate[x^4*(a + b*x)^7,x]

[Out] (a^7*x^5)/5 + (7*a^6*b*x^6)/6 + 3*a^5*b^2*x^7 + (35*a^4*b^3*x^8)/8 + (35*a^3*b^4*x^9)/9 + (21*a^2*b^5*x^10)/10 + (7*a*b^6*x^11)/11 + (b^7*x^12)/12

fricas [A] time = 0.36, size = 79, normalized size = 0.98

$$\frac{1}{12}x^{12}b^7 + \frac{7}{11}x^{11}b^6a + \frac{21}{10}x^{10}b^5a^2 + \frac{35}{9}x^9b^4a^3 + \frac{35}{8}x^8b^3a^4 + 3x^7b^2a^5 + \frac{7}{6}x^6ba^6 + \frac{1}{5}x^5a^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^7,x, algorithm="fricas")

[Out] 1/12*x^12*b^7 + 7/11*x^11*b^6*a + 21/10*x^10*b^5*a^2 + 35/9*x^9*b^4*a^3 + 35/8*x^8*b^3*a^4 + 3*x^7*b^2*a^5 + 7/6*x^6*b*a^6 + 1/5*x^5*a^7

giac [A] time = 1.13, size = 79, normalized size = 0.98

$$\frac{1}{12}b^7x^{12} + \frac{7}{11}ab^6x^{11} + \frac{21}{10}a^2b^5x^{10} + \frac{35}{9}a^3b^4x^9 + \frac{35}{8}a^4b^3x^8 + 3a^5b^2x^7 + \frac{7}{6}a^6bx^6 + \frac{1}{5}a^7x^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^7,x, algorithm="giac")

[Out] 1/12*b^7*x^12 + 7/11*a*b^6*x^11 + 21/10*a^2*b^5*x^10 + 35/9*a^3*b^4*x^9 + 35/8*a^4*b^3*x^8 + 3*a^5*b^2*x^7 + 7/6*a^6*b*x^6 + 1/5*a^7*x^5

maple [A] time = 0.00, size = 80, normalized size = 0.99

$$\frac{1}{12}b^7x^{12} + \frac{7}{11}ab^6x^{11} + \frac{21}{10}a^2b^5x^{10} + \frac{35}{9}a^3b^4x^9 + \frac{35}{8}a^4b^3x^8 + 3a^5b^2x^7 + \frac{7}{6}a^6bx^6 + \frac{1}{5}a^7x^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*(b*x+a)^7,x)

[Out] 1/12*b^7*x^12+7/11*a*b^6*x^11+21/10*a^2*b^5*x^10+35/9*a^3*b^4*x^9+35/8*a^4*b^3*x^8+3*a^5*b^2*x^7+7/6*a^6*b*x^6+1/5*a^7*x^5

maxima [A] time = 1.35, size = 79, normalized size = 0.98

$$\frac{1}{12}b^7x^{12} + \frac{7}{11}ab^6x^{11} + \frac{21}{10}a^2b^5x^{10} + \frac{35}{9}a^3b^4x^9 + \frac{35}{8}a^4b^3x^8 + 3a^5b^2x^7 + \frac{7}{6}a^6bx^6 + \frac{1}{5}a^7x^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^7,x, algorithm="maxima")

[Out] 1/12*b^7*x^12 + 7/11*a*b^6*x^11 + 21/10*a^2*b^5*x^10 + 35/9*a^3*b^4*x^9 + 35/8*a^4*b^3*x^8 + 3*a^5*b^2*x^7 + 7/6*a^6*b*x^6 + 1/5*a^7*x^5

mupad [B] time = 0.06, size = 79, normalized size = 0.98

$$\frac{a^7 x^5}{5} + \frac{7a^6 b x^6}{6} + 3a^5 b^2 x^7 + \frac{35a^4 b^3 x^8}{8} + \frac{35a^3 b^4 x^9}{9} + \frac{21a^2 b^5 x^{10}}{10} + \frac{7ab^6 x^{11}}{11} + \frac{b^7 x^{12}}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*(a + b*x)^7,x)

[Out] (a^7*x^5)/5 + (b^7*x^12)/12 + (7*a^6*b*x^6)/6 + (7*a*b^6*x^11)/11 + 3*a^5*b^2*x^7 + (35*a^4*b^3*x^8)/8 + (35*a^3*b^4*x^9)/9 + (21*a^2*b^5*x^10)/10

sympy [A] time = 0.10, size = 92, normalized size = 1.14

$$\frac{a^7 x^5}{5} + \frac{7a^6 b x^6}{6} + 3a^5 b^2 x^7 + \frac{35a^4 b^3 x^8}{8} + \frac{35a^3 b^4 x^9}{9} + \frac{21a^2 b^5 x^{10}}{10} + \frac{7ab^6 x^{11}}{11} + \frac{b^7 x^{12}}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4*(b*x+a)**7,x)

[Out] a**7*x**5/5 + 7*a**6*b*x**6/6 + 3*a**5*b**2*x**7 + 35*a**4*b**3*x**8/8 + 35*a**3*b**4*x**9/9 + 21*a**2*b**5*x**10/10 + 7*a*b**6*x**11/11 + b**7*x**12/12

3.103 $\int x^3(a + bx)^7 dx$

Optimal. Leaf size=64

$$-\frac{a^3(a + bx)^8}{8b^4} + \frac{a^2(a + bx)^9}{3b^4} + \frac{(a + bx)^{11}}{11b^4} - \frac{3a(a + bx)^{10}}{10b^4}$$

[Out] $-1/8*a^3*(b*x+a)^8/b^4+1/3*a^2*(b*x+a)^9/b^4-3/10*a*(b*x+a)^{10}/b^4+1/11*(b*x+a)^{11}/b^4$

Rubi [A] time = 0.03, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2(a + bx)^9}{3b^4} - \frac{a^3(a + bx)^8}{8b^4} + \frac{(a + bx)^{11}}{11b^4} - \frac{3a(a + bx)^{10}}{10b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^7, x]

[Out] $-(a^3*(a + b*x)^8)/(8*b^4) + (a^2*(a + b*x)^9)/(3*b^4) - (3*a*(a + b*x)^{10})/(10*b^4) + (a + b*x)^{11}/(11*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^7 dx &= \int \left(-\frac{a^3(a + bx)^7}{b^3} + \frac{3a^2(a + bx)^8}{b^3} - \frac{3a(a + bx)^9}{b^3} + \frac{(a + bx)^{10}}{b^3} \right) dx \\ &= -\frac{a^3(a + bx)^8}{8b^4} + \frac{a^2(a + bx)^9}{3b^4} - \frac{3a(a + bx)^{10}}{10b^4} + \frac{(a + bx)^{11}}{11b^4} \end{aligned}$$

Mathematica [A] time = 0.00, size = 93, normalized size = 1.45

$$\frac{a^7 x^4}{4} + \frac{7}{5} a^6 b x^5 + \frac{7}{2} a^5 b^2 x^6 + 5 a^4 b^3 x^7 + \frac{35}{8} a^3 b^4 x^8 + \frac{7}{3} a^2 b^5 x^9 + \frac{7}{10} a b^6 x^{10} + \frac{b^7 x^{11}}{11}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^7,x]

[Out] (a^7*x^4)/4 + (7*a^6*b*x^5)/5 + (7*a^5*b^2*x^6)/2 + 5*a^4*b^3*x^7 + (35*a^3*b^4*x^8)/8 + (7*a^2*b^5*x^9)/3 + (7*a*b^6*x^10)/10 + (b^7*x^11)/11

fricas [A] time = 0.39, size = 79, normalized size = 1.23

$$\frac{1}{11}x^{11}b^7 + \frac{7}{10}x^{10}b^6a + \frac{7}{3}x^9b^5a^2 + \frac{35}{8}x^8b^4a^3 + 5x^7b^3a^4 + \frac{7}{2}x^6b^2a^5 + \frac{7}{5}x^5ba^6 + \frac{1}{4}x^4a^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^7,x, algorithm="fricas")

[Out] 1/11*x^11*b^7 + 7/10*x^10*b^6*a + 7/3*x^9*b^5*a^2 + 35/8*x^8*b^4*a^3 + 5*x^7*b^3*a^4 + 7/2*x^6*b^2*a^5 + 7/5*x^5*b*a^6 + 1/4*x^4*a^7

giac [A] time = 1.22, size = 79, normalized size = 1.23

$$\frac{1}{11}b^7x^{11} + \frac{7}{10}ab^6x^{10} + \frac{7}{3}a^2b^5x^9 + \frac{35}{8}a^3b^4x^8 + 5a^4b^3x^7 + \frac{7}{2}a^5b^2x^6 + \frac{7}{5}a^6bx^5 + \frac{1}{4}a^7x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^7,x, algorithm="giac")

[Out] 1/11*b^7*x^11 + 7/10*a*b^6*x^10 + 7/3*a^2*b^5*x^9 + 35/8*a^3*b^4*x^8 + 5*a^4*b^3*x^7 + 7/2*a^5*b^2*x^6 + 7/5*a^6*b*x^5 + 1/4*a^7*x^4

maple [A] time = 0.00, size = 80, normalized size = 1.25

$$\frac{1}{11}b^7x^{11} + \frac{7}{10}ab^6x^{10} + \frac{7}{3}a^2b^5x^9 + \frac{35}{8}a^3b^4x^8 + 5a^4b^3x^7 + \frac{7}{2}a^5b^2x^6 + \frac{7}{5}a^6bx^5 + \frac{1}{4}a^7x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^7,x)

[Out] 1/11*b^7*x^11+7/10*a*b^6*x^10+7/3*a^2*b^5*x^9+35/8*a^3*b^4*x^8+5*a^4*b^3*x^7+7/2*a^5*b^2*x^6+7/5*a^6*b*x^5+1/4*a^7*x^4

maxima [A] time = 1.34, size = 79, normalized size = 1.23

$$\frac{1}{11}b^7x^{11} + \frac{7}{10}ab^6x^{10} + \frac{7}{3}a^2b^5x^9 + \frac{35}{8}a^3b^4x^8 + 5a^4b^3x^7 + \frac{7}{2}a^5b^2x^6 + \frac{7}{5}a^6bx^5 + \frac{1}{4}a^7x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^7,x, algorithm="maxima")

[Out] 1/11*b^7*x^11 + 7/10*a*b^6*x^10 + 7/3*a^2*b^5*x^9 + 35/8*a^3*b^4*x^8 + 5*a^4*b^3*x^7 + 7/2*a^5*b^2*x^6 + 7/5*a^6*b*x^5 + 1/4*a^7*x^4

mupad [B] time = 0.10, size = 79, normalized size = 1.23

$$\frac{a^7 x^4}{4} + \frac{7 a^6 b x^5}{5} + \frac{7 a^5 b^2 x^6}{2} + 5 a^4 b^3 x^7 + \frac{35 a^3 b^4 x^8}{8} + \frac{7 a^2 b^5 x^9}{3} + \frac{7 a b^6 x^{10}}{10} + \frac{b^7 x^{11}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(a + b*x)^7,x)

[Out] (a^7*x^4)/4 + (b^7*x^11)/11 + (7*a^6*b*x^5)/5 + (7*a*b^6*x^10)/10 + (7*a^5*b^2*x^6)/2 + 5*a^4*b^3*x^7 + (35*a^3*b^4*x^8)/8 + (7*a^2*b^5*x^9)/3

sympy [A] time = 0.09, size = 92, normalized size = 1.44

$$\frac{a^7 x^4}{4} + \frac{7 a^6 b x^5}{5} + \frac{7 a^5 b^2 x^6}{2} + 5 a^4 b^3 x^7 + \frac{35 a^3 b^4 x^8}{8} + \frac{7 a^2 b^5 x^9}{3} + \frac{7 a b^6 x^{10}}{10} + \frac{b^7 x^{11}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**7,x)

[Out] a**7*x**4/4 + 7*a**6*b*x**5/5 + 7*a**5*b**2*x**6/2 + 5*a**4*b**3*x**7 + 35*a**3*b**4*x**8/8 + 7*a**2*b**5*x**9/3 + 7*a*b**6*x**10/10 + b**7*x**11/11

3.104 $\int x^2(a + bx)^7 dx$

Optimal. Leaf size=47

$$\frac{a^2(a + bx)^8}{8b^3} + \frac{(a + bx)^{10}}{10b^3} - \frac{2a(a + bx)^9}{9b^3}$$

[Out] $1/8*a^2*(b*x+a)^8/b^3-2/9*a*(b*x+a)^9/b^3+1/10*(b*x+a)^{10}/b^3$

Rubi [A] time = 0.02, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2(a + bx)^8}{8b^3} + \frac{(a + bx)^{10}}{10b^3} - \frac{2a(a + bx)^9}{9b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*x)^7,x]

[Out] $(a^2*(a + b*x)^8)/(8*b^3) - (2*a*(a + b*x)^9)/(9*b^3) + (a + b*x)^{10}/(10*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^7 dx &= \int \left(\frac{a^2(a + bx)^7}{b^2} - \frac{2a(a + bx)^8}{b^2} + \frac{(a + bx)^9}{b^2} \right) dx \\ &= \frac{a^2(a + bx)^8}{8b^3} - \frac{2a(a + bx)^9}{9b^3} + \frac{(a + bx)^{10}}{10b^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 93, normalized size = 1.98

$$\frac{a^7 x^3}{3} + \frac{7}{4} a^6 b x^4 + \frac{21}{5} a^5 b^2 x^5 + \frac{35}{6} a^4 b^3 x^6 + 5 a^3 b^4 x^7 + \frac{21}{8} a^2 b^5 x^8 + \frac{7}{9} a b^6 x^9 + \frac{b^7 x^{10}}{10}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^7,x]

[Out] (a^7*x^3)/3 + (7*a^6*b*x^4)/4 + (21*a^5*b^2*x^5)/5 + (35*a^4*b^3*x^6)/6 + 5*a^3*b^4*x^7 + (21*a^2*b^5*x^8)/8 + (7*a*b^6*x^9)/9 + (b^7*x^10)/10

fricas [A] time = 0.47, size = 79, normalized size = 1.68

$$\frac{1}{10}x^{10}b^7 + \frac{7}{9}x^9b^6a + \frac{21}{8}x^8b^5a^2 + 5x^7b^4a^3 + \frac{35}{6}x^6b^3a^4 + \frac{21}{5}x^5b^2a^5 + \frac{7}{4}x^4ba^6 + \frac{1}{3}x^3a^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^7,x, algorithm="fricas")

[Out] 1/10*x^10*b^7 + 7/9*x^9*b^6*a + 21/8*x^8*b^5*a^2 + 5*x^7*b^4*a^3 + 35/6*x^6*b^3*a^4 + 21/5*x^5*b^2*a^5 + 7/4*x^4*b*a^6 + 1/3*x^3*a^7

giac [A] time = 0.91, size = 79, normalized size = 1.68

$$\frac{1}{10}b^7x^{10} + \frac{7}{9}ab^6x^9 + \frac{21}{8}a^2b^5x^8 + 5a^3b^4x^7 + \frac{35}{6}a^4b^3x^6 + \frac{21}{5}a^5b^2x^5 + \frac{7}{4}a^6bx^4 + \frac{1}{3}a^7x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^7,x, algorithm="giac")

[Out] 1/10*b^7*x^10 + 7/9*a*b^6*x^9 + 21/8*a^2*b^5*x^8 + 5*a^3*b^4*x^7 + 35/6*a^4*b^3*x^6 + 21/5*a^5*b^2*x^5 + 7/4*a^6*b*x^4 + 1/3*a^7*x^3

maple [A] time = 0.00, size = 80, normalized size = 1.70

$$\frac{1}{10}b^7x^{10} + \frac{7}{9}ab^6x^9 + \frac{21}{8}a^2b^5x^8 + 5a^3b^4x^7 + \frac{35}{6}a^4b^3x^6 + \frac{21}{5}a^5b^2x^5 + \frac{7}{4}a^6bx^4 + \frac{1}{3}a^7x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^7,x)

[Out] 1/10*b^7*x^10+7/9*a*b^6*x^9+21/8*a^2*b^5*x^8+5*a^3*b^4*x^7+35/6*a^4*b^3*x^6+21/5*a^5*b^2*x^5+7/4*a^6*b*x^4+1/3*a^7*x^3

maxima [A] time = 1.33, size = 79, normalized size = 1.68

$$\frac{1}{10}b^7x^{10} + \frac{7}{9}ab^6x^9 + \frac{21}{8}a^2b^5x^8 + 5a^3b^4x^7 + \frac{35}{6}a^4b^3x^6 + \frac{21}{5}a^5b^2x^5 + \frac{7}{4}a^6bx^4 + \frac{1}{3}a^7x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^7,x, algorithm="maxima")

[Out] $1/10*b^7*x^{10} + 7/9*a*b^6*x^9 + 21/8*a^2*b^5*x^8 + 5*a^3*b^4*x^7 + 35/6*a^4*b^3*x^6 + 21/5*a^5*b^2*x^5 + 7/4*a^6*b*x^4 + 1/3*a^7*x^3$

mupad [B] time = 0.12, size = 31, normalized size = 0.66

$$\frac{(a + b x)^8 (8 a^2 - 64 a b x + 288 b^2 x^2)}{2880 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(a + b*x)^7,x)`

[Out] $((a + b*x)^8*(8*a^2 + 288*b^2*x^2 - 64*a*b*x))/(2880*b^3)$

sympy [B] time = 0.09, size = 92, normalized size = 1.96

$$\frac{a^7 x^3}{3} + \frac{7 a^6 b x^4}{4} + \frac{21 a^5 b^2 x^5}{5} + \frac{35 a^4 b^3 x^6}{6} + 5 a^3 b^4 x^7 + \frac{21 a^2 b^5 x^8}{8} + \frac{7 a b^6 x^9}{9} + \frac{b^7 x^{10}}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(b*x+a)**7,x)`

[Out] $a**7*x**3/3 + 7*a**6*b*x**4/4 + 21*a**5*b**2*x**5/5 + 35*a**4*b**3*x**6/6 + 5*a**3*b**4*x**7 + 21*a**2*b**5*x**8/8 + 7*a*b**6*x**9/9 + b**7*x**10/10$

3.105 $\int x(a + bx)^7 dx$

Optimal. Leaf size=30

$$\frac{(a + bx)^9}{9b^2} - \frac{a(a + bx)^8}{8b^2}$$

[Out] $-1/8*a*(b*x+a)^8/b^2+1/9*(b*x+a)^9/b^2$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{(a + bx)^9}{9b^2} - \frac{a(a + bx)^8}{8b^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^7, x]

[Out] $-(a*(a + b*x)^8)/(8*b^2) + (a + b*x)^9/(9*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x(a + bx)^7 dx &= \int \left(-\frac{a(a + bx)^7}{b} + \frac{(a + bx)^8}{b} \right) dx \\ &= -\frac{a(a + bx)^8}{8b^2} + \frac{(a + bx)^9}{9b^2} \end{aligned}$$

Mathematica [B] time = 0.00, size = 91, normalized size = 3.03

$$\frac{a^7 x^2}{2} + \frac{7}{3} a^6 b x^3 + \frac{21}{4} a^5 b^2 x^4 + 7 a^4 b^3 x^5 + \frac{35}{6} a^3 b^4 x^6 + 3 a^2 b^5 x^7 + \frac{7}{8} a b^6 x^8 + \frac{b^7 x^9}{9}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^7, x]

[Out] $(a^7x^2)/2 + (7a^6bx^3)/3 + (21a^5b^2x^4)/4 + 7a^4b^3x^5 + (35a^3b^4x^6)/6 + 3a^2b^5x^7 + (7a^6bx^8)/8 + (b^7x^9)/9$

fricas [B] time = 0.43, size = 79, normalized size = 2.63

$$\frac{1}{9}x^9b^7 + \frac{7}{8}x^8b^6a + 3x^7b^5a^2 + \frac{35}{6}x^6b^4a^3 + 7x^5b^3a^4 + \frac{21}{4}x^4b^2a^5 + \frac{7}{3}x^3ba^6 + \frac{1}{2}x^2a^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^7,x, algorithm="fricas")

[Out] $1/9*x^9*b^7 + 7/8*x^8*b^6*a + 3*x^7*b^5*a^2 + 35/6*x^6*b^4*a^3 + 7*x^5*b^3*a^4 + 21/4*x^4*b^2*a^5 + 7/3*x^3*b*a^6 + 1/2*x^2*a^7$

giac [B] time = 0.92, size = 79, normalized size = 2.63

$$\frac{1}{9}b^7x^9 + \frac{7}{8}ab^6x^8 + 3a^2b^5x^7 + \frac{35}{6}a^3b^4x^6 + 7a^4b^3x^5 + \frac{21}{4}a^5b^2x^4 + \frac{7}{3}a^6bx^3 + \frac{1}{2}a^7x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^7,x, algorithm="giac")

[Out] $1/9*b^7*x^9 + 7/8*a*b^6*x^8 + 3*a^2*b^5*x^7 + 35/6*a^3*b^4*x^6 + 7*a^4*b^3*x^5 + 21/4*a^5*b^2*x^4 + 7/3*a^6*b*x^3 + 1/2*a^7*x^2$

maple [B] time = 0.00, size = 80, normalized size = 2.67

$$\frac{1}{9}b^7x^9 + \frac{7}{8}ab^6x^8 + 3a^2b^5x^7 + \frac{35}{6}a^3b^4x^6 + 7a^4b^3x^5 + \frac{21}{4}a^5b^2x^4 + \frac{7}{3}a^6bx^3 + \frac{1}{2}a^7x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^7,x)

[Out] $1/9*b^7*x^9+7/8*a*b^6*x^8+3*a^2*b^5*x^7+35/6*a^3*b^4*x^6+7*a^4*b^3*x^5+21/4*a^5*b^2*x^4+7/3*a^6*b*x^3+1/2*a^7*x^2$

maxima [B] time = 1.35, size = 79, normalized size = 2.63

$$\frac{1}{9}b^7x^9 + \frac{7}{8}ab^6x^8 + 3a^2b^5x^7 + \frac{35}{6}a^3b^4x^6 + 7a^4b^3x^5 + \frac{21}{4}a^5b^2x^4 + \frac{7}{3}a^6bx^3 + \frac{1}{2}a^7x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^7,x, algorithm="maxima")

[Out] $1/9*b^7*x^9 + 7/8*a*b^6*x^8 + 3*a^2*b^5*x^7 + 35/6*a^3*b^4*x^6 + 7*a^4*b^3*x^5 + 21/4*a^5*b^2*x^4 + 7/3*a^6*b*x^3 + 1/2*a^7*x^2$

mupad [B] time = 0.12, size = 25, normalized size = 0.83

$$-\frac{2 \left(\frac{a(a+bx)^8}{16} - \frac{(a+bx)^9}{18} \right)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(a + b*x)^7,x)`

[Out] `-(2*((a*(a + b*x)^8)/16 - (a + b*x)^9/18))/b^2`

sympy [B] time = 0.09, size = 90, normalized size = 3.00

$$\frac{a^7x^2}{2} + \frac{7a^6bx^3}{3} + \frac{21a^5b^2x^4}{4} + 7a^4b^3x^5 + \frac{35a^3b^4x^6}{6} + 3a^2b^5x^7 + \frac{7ab^6x^8}{8} + \frac{b^7x^9}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**7,x)`

[Out] `a**7*x**2/2 + 7*a**6*b*x**3/3 + 21*a**5*b**2*x**4/4 + 7*a**4*b**3*x**5 + 35*a**3*b**4*x**6/6 + 3*a**2*b**5*x**7 + 7*a*b**6*x**8/8 + b**7*x**9/9`

3.106 $\int (a + bx)^7 dx$

Optimal. Leaf size=14

$$\frac{(a + bx)^8}{8b}$$

[Out] $1/8*(b*x+a)^8/b$

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(a + bx)^8}{8b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7, x]

[Out] (a + b*x)^8/(8*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^7 dx = \frac{(a + bx)^8}{8b}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{(a + bx)^8}{8b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7, x]

[Out] (a + b*x)^8/(8*b)

fricas [B] time = 0.41, size = 75, normalized size = 5.36

$$\frac{1}{8}x^8b^7 + x^7b^6a + \frac{7}{2}x^6b^5a^2 + 7x^5b^4a^3 + \frac{35}{4}x^4b^3a^4 + 7x^3b^2a^5 + \frac{7}{2}x^2ba^6 + xa^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7,x, algorithm="fricas")

[Out] $\frac{1}{8}x^8b^7 + x^7b^6a + \frac{7}{2}x^6b^5a^2 + 7x^5b^4a^3 + \frac{35}{4}x^4b^3a^4 + 7x^3b^2a^5 + \frac{7}{2}x^2b^1a^6 + xa^7$

giac [A] time = 1.06, size = 12, normalized size = 0.86

$$\frac{(bx + a)^8}{8b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7,x, algorithm="giac")

[Out] $\frac{1}{8}(bx + a)^8/b$

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{(bx + a)^8}{8b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7,x)

[Out] $\frac{1}{8}(bx+a)^8/b$

maxima [A] time = 1.39, size = 12, normalized size = 0.86

$$\frac{(bx + a)^8}{8b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7,x, algorithm="maxima")

[Out] $\frac{1}{8}(bx + a)^8/b$

mupad [B] time = 0.06, size = 75, normalized size = 5.36

$$a^7x + \frac{7a^6bx^2}{2} + 7a^5b^2x^3 + \frac{35a^4b^3x^4}{4} + 7a^3b^4x^5 + \frac{7a^2b^5x^6}{2} + ab^6x^7 + \frac{b^7x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7,x)

[Out] $a^7x + (b^7x^8)/8 + (7a^6bx^2)/2 + ab^6x^7 + 7a^5b^2x^3 + (35a^4b^3x^4)/4 + 7a^3b^4x^5 + (7a^2b^5x^6)/2$

sympy [B] time = 0.08, size = 83, normalized size = 5.93

$$a^7x + \frac{7a^6bx^2}{2} + 7a^5b^2x^3 + \frac{35a^4b^3x^4}{4} + 7a^3b^4x^5 + \frac{7a^2b^5x^6}{2} + ab^6x^7 + \frac{b^7x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7,x)

[Out] $a**7*x + 7*a**6*b*x**2/2 + 7*a**5*b**2*x**3 + 35*a**4*b**3*x**4/4 + 7*a**3*b**4*x**5 + 7*a**2*b**5*x**6/2 + a*b**6*x**7 + b**7*x**8/8$

$$3.107 \quad \int \frac{(a+bx)^7}{x} dx$$

Optimal. Leaf size=87

$$a^7 \log(x) + 7a^6bx + \frac{21}{2}a^5b^2x^2 + \frac{35}{3}a^4b^3x^3 + \frac{35}{4}a^3b^4x^4 + \frac{21}{5}a^2b^5x^5 + \frac{7}{6}ab^6x^6 + \frac{b^7x^7}{7}$$

[Out] $7*a^6*b*x+21/2*a^5*b^2*x^2+35/3*a^4*b^3*x^3+35/4*a^3*b^4*x^4+21/5*a^2*b^5*x^5+7/6*a*b^6*x^6+1/7*b^7*x^7+a^7*\ln(x)$

Rubi [A] time = 0.03, antiderivative size = 87, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{21}{2}a^5b^2x^2 + \frac{35}{3}a^4b^3x^3 + \frac{35}{4}a^3b^4x^4 + \frac{21}{5}a^2b^5x^5 + 7a^6bx + a^7 \log(x) + \frac{7}{6}ab^6x^6 + \frac{b^7x^7}{7}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x, x]

[Out] $7*a^6*b*x + (21*a^5*b^2*x^2)/2 + (35*a^4*b^3*x^3)/3 + (35*a^3*b^4*x^4)/4 + (21*a^2*b^5*x^5)/5 + (7*a*b^6*x^6)/6 + (b^7*x^7)/7 + a^7*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x} dx &= \int \left(7a^6b + \frac{a^7}{x} + 21a^5b^2x + 35a^4b^3x^2 + 35a^3b^4x^3 + 21a^2b^5x^4 + 7ab^6x^5 + b^7x^6 \right) dx \\ &= 7a^6bx + \frac{21}{2}a^5b^2x^2 + \frac{35}{3}a^4b^3x^3 + \frac{35}{4}a^3b^4x^4 + \frac{21}{5}a^2b^5x^5 + \frac{7}{6}ab^6x^6 + \frac{b^7x^7}{7} + a^7 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 87, normalized size = 1.00

$$a^7 \log(x) + 7a^6bx + \frac{21}{2}a^5b^2x^2 + \frac{35}{3}a^4b^3x^3 + \frac{35}{4}a^3b^4x^4 + \frac{21}{5}a^2b^5x^5 + \frac{7}{6}ab^6x^6 + \frac{b^7x^7}{7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x,x]

[Out] $7*a^6*b*x + (21*a^5*b^2*x^2)/2 + (35*a^4*b^3*x^3)/3 + (35*a^3*b^4*x^4)/4 + (21*a^2*b^5*x^5)/5 + (7*a*b^6*x^6)/6 + (b^7*x^7)/7 + a^7*\text{Log}[x]$

fricas [A] time = 0.45, size = 75, normalized size = 0.86

$$\frac{1}{7} b^7 x^7 + \frac{7}{6} a b^6 x^6 + \frac{21}{5} a^2 b^5 x^5 + \frac{35}{4} a^3 b^4 x^4 + \frac{35}{3} a^4 b^3 x^3 + \frac{21}{2} a^5 b^2 x^2 + 7 a^6 b x + a^7 \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x,x, algorithm="fricas")

[Out] $1/7*b^7*x^7 + 7/6*a*b^6*x^6 + 21/5*a^2*b^5*x^5 + 35/4*a^3*b^4*x^4 + 35/3*a^4*b^3*x^3 + 21/2*a^5*b^2*x^2 + 7*a^6*b*x + a^7*\log(x)$

giac [A] time = 1.30, size = 76, normalized size = 0.87

$$\frac{1}{7} b^7 x^7 + \frac{7}{6} a b^6 x^6 + \frac{21}{5} a^2 b^5 x^5 + \frac{35}{4} a^3 b^4 x^4 + \frac{35}{3} a^4 b^3 x^3 + \frac{21}{2} a^5 b^2 x^2 + 7 a^6 b x + a^7 \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x,x, algorithm="giac")

[Out] $1/7*b^7*x^7 + 7/6*a*b^6*x^6 + 21/5*a^2*b^5*x^5 + 35/4*a^3*b^4*x^4 + 35/3*a^4*b^3*x^3 + 21/2*a^5*b^2*x^2 + 7*a^6*b*x + a^7*\log(\text{abs}(x))$

maple [A] time = 0.00, size = 76, normalized size = 0.87

$$\frac{b^7 x^7}{7} + \frac{7 a b^6 x^6}{6} + \frac{21 a^2 b^5 x^5}{5} + \frac{35 a^3 b^4 x^4}{4} + \frac{35 a^4 b^3 x^3}{3} + \frac{21 a^5 b^2 x^2}{2} + a^7 \ln(x) + 7 a^6 b x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x,x)

[Out] $7*a^6*b*x+21/2*a^5*b^2*x^2+35/3*a^4*b^3*x^3+35/4*a^3*b^4*x^4+21/5*a^2*b^5*x^5+7/6*a*b^6*x^6+1/7*b^7*x^7+a^7*\ln(x)$

maxima [A] time = 1.34, size = 75, normalized size = 0.86

$$\frac{1}{7} b^7 x^7 + \frac{7}{6} a b^6 x^6 + \frac{21}{5} a^2 b^5 x^5 + \frac{35}{4} a^3 b^4 x^4 + \frac{35}{3} a^4 b^3 x^3 + \frac{21}{2} a^5 b^2 x^2 + 7 a^6 b x + a^7 \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x,x, algorithm="maxima")

[Out] $1/7*b^7*x^7 + 7/6*a*b^6*x^6 + 21/5*a^2*b^5*x^5 + 35/4*a^3*b^4*x^4 + 35/3*a^4*b^3*x^3 + 21/2*a^5*b^2*x^2 + 7*a^6*b*x + a^7*\log(x)$

mupad [B] time = 0.07, size = 75, normalized size = 0.86

$$a^7 \ln(x) + \frac{b^7 x^7}{7} + \frac{7 a b^6 x^6}{6} + \frac{21 a^5 b^2 x^2}{2} + \frac{35 a^4 b^3 x^3}{3} + \frac{35 a^3 b^4 x^4}{4} + \frac{21 a^2 b^5 x^5}{5} + 7 a^6 b x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x,x)

[Out] $a^7*\log(x) + (b^7*x^7)/7 + (7*a*b^6*x^6)/6 + (21*a^5*b^2*x^2)/2 + (35*a^4*b^3*x^3)/3 + (35*a^3*b^4*x^4)/4 + (21*a^2*b^5*x^5)/5 + 7*a^6*b*x$

sympy [A] time = 0.19, size = 88, normalized size = 1.01

$$a^7 \log(x) + 7a^6bx + \frac{21a^5b^2x^2}{2} + \frac{35a^4b^3x^3}{3} + \frac{35a^3b^4x^4}{4} + \frac{21a^2b^5x^5}{5} + \frac{7ab^6x^6}{6} + \frac{b^7x^7}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x,x)

[Out] $a**7*\log(x) + 7*a**6*b*x + 21*a**5*b**2*x**2/2 + 35*a**4*b**3*x**3/3 + 35*a**3*b**4*x**4/4 + 21*a**2*b**5*x**5/5 + 7*a*b**6*x**6/6 + b**7*x**7/7$

$$3.108 \quad \int \frac{(a+bx)^7}{x^2} dx$$

Optimal. Leaf size=86

$$-\frac{a^7}{x} + 7a^6b \log(x) + 21a^5b^2x + \frac{35}{2}a^4b^3x^2 + \frac{35}{3}a^3b^4x^3 + \frac{21}{4}a^2b^5x^4 + \frac{7}{5}ab^6x^5 + \frac{b^7x^6}{6}$$

[Out] $-a^7/x + 21a^5b^2x + 35/2a^4b^3x^2 + 35/3a^3b^4x^3 + 21/4a^2b^5x^4 + 7/5a^1b^6x^5 + 1/6b^7x^6 + 7a^6b \ln(x)$

Rubi [A] time = 0.03, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{35}{2}a^4b^3x^2 + \frac{35}{3}a^3b^4x^3 + \frac{21}{4}a^2b^5x^4 + 21a^5b^2x + 7a^6b \log(x) - \frac{a^7}{x} + \frac{7}{5}ab^6x^5 + \frac{b^7x^6}{6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^2, x]

[Out] $-(a^7/x) + 21a^5b^2x + (35a^4b^3x^2)/2 + (35a^3b^4x^3)/3 + (21a^2b^5x^4)/4 + (7a^1b^6x^5)/5 + (b^7x^6)/6 + 7a^6b \text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x^2} dx &= \int \left(21a^5b^2 + \frac{a^7}{x^2} + \frac{7a^6b}{x} + 35a^4b^3x + 35a^3b^4x^2 + 21a^2b^5x^3 + 7ab^6x^4 + b^7x^5 \right) dx \\ &= -\frac{a^7}{x} + 21a^5b^2x + \frac{35}{2}a^4b^3x^2 + \frac{35}{3}a^3b^4x^3 + \frac{21}{4}a^2b^5x^4 + \frac{7}{5}ab^6x^5 + \frac{b^7x^6}{6} + 7a^6b \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 86, normalized size = 1.00

$$-\frac{a^7}{x} + 7a^6b \log(x) + 21a^5b^2x + \frac{35}{2}a^4b^3x^2 + \frac{35}{3}a^3b^4x^3 + \frac{21}{4}a^2b^5x^4 + \frac{7}{5}ab^6x^5 + \frac{b^7x^6}{6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^2,x]

[Out] $-(a^7/x) + 21a^5b^2x + (35a^4b^3x^2)/2 + (35a^3b^4x^3)/3 + (21a^2b^5x^4)/4 + (7a^1b^6x^5)/5 + (b^7x^6)/6 + 7a^6b \operatorname{Log}[x]$

fricas [A] time = 0.44, size = 81, normalized size = 0.94

$$\frac{10b^7x^7 + 84ab^6x^6 + 315a^2b^5x^5 + 700a^3b^4x^4 + 1050a^4b^3x^3 + 1260a^5b^2x^2 + 420a^6bx \log(x) - 60a^7}{60x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^2,x, algorithm="fricas")

[Out] $1/60*(10*b^7*x^7 + 84*a*b^6*x^6 + 315*a^2*b^5*x^5 + 700*a^3*b^4*x^4 + 1050*a^4*b^3*x^3 + 1260*a^5*b^2*x^2 + 420*a^6*b*x*\log(x) - 60*a^7)/x$

giac [A] time = 1.12, size = 77, normalized size = 0.90

$$\frac{1}{6}b^7x^6 + \frac{7}{5}ab^6x^5 + \frac{21}{4}a^2b^5x^4 + \frac{35}{3}a^3b^4x^3 + \frac{35}{2}a^4b^3x^2 + 21a^5b^2x + 7a^6b \log(|x|) - \frac{a^7}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^2,x, algorithm="giac")

[Out] $1/6*b^7*x^6 + 7/5*a*b^6*x^5 + 21/4*a^2*b^5*x^4 + 35/3*a^3*b^4*x^3 + 35/2*a^4*b^3*x^2 + 21*a^5*b^2*x + 7*a^6*b*\log(\operatorname{abs}(x)) - a^7/x$

maple [A] time = 0.01, size = 77, normalized size = 0.90

$$\frac{b^7x^6}{6} + \frac{7ab^6x^5}{5} + \frac{21a^2b^5x^4}{4} + \frac{35a^3b^4x^3}{3} + \frac{35a^4b^3x^2}{2} + 7a^6b \ln(x) + 21a^5b^2x - \frac{a^7}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^2,x)

[Out] $-a^7/x + 21a^5b^2x + 35/2*a^4*b^3*x^2 + 35/3*a^3*b^4*x^3 + 21/4*a^2*b^5*x^4 + 7/5*a*b^6*x^5 + 1/6*b^7*x^6 + 7*a^6*b*\ln(x)$

maxima [A] time = 1.36, size = 76, normalized size = 0.88

$$\frac{1}{6}b^7x^6 + \frac{7}{5}ab^6x^5 + \frac{21}{4}a^2b^5x^4 + \frac{35}{3}a^3b^4x^3 + \frac{35}{2}a^4b^3x^2 + 21a^5b^2x + 7a^6b \log(x) - \frac{a^7}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^2,x, algorithm="maxima")

[Out] $1/6*b^7*x^6 + 7/5*a*b^6*x^5 + 21/4*a^2*b^5*x^4 + 35/3*a^3*b^4*x^3 + 35/2*a^4*b^3*x^2 + 21*a^5*b^2*x + 7*a^6*b*\log(x) - a^7/x$

mupad [B] time = 0.05, size = 76, normalized size = 0.88

$$\frac{b^7 x^6}{6} - \frac{a^7}{x} + 21 a^5 b^2 x + \frac{7 a b^6 x^5}{5} + 7 a^6 b \ln(x) + \frac{35 a^4 b^3 x^2}{2} + \frac{35 a^3 b^4 x^3}{3} + \frac{21 a^2 b^5 x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^2,x)

[Out] $(b^7*x^6)/6 - a^7/x + 21*a^5*b^2*x + (7*a*b^6*x^5)/5 + 7*a^6*b*\log(x) + (35*a^4*b^3*x^2)/2 + (35*a^3*b^4*x^3)/3 + (21*a^2*b^5*x^4)/4$

sympy [A] time = 0.20, size = 85, normalized size = 0.99

$$-\frac{a^7}{x} + 7a^6b \log(x) + 21a^5b^2x + \frac{35a^4b^3x^2}{2} + \frac{35a^3b^4x^3}{3} + \frac{21a^2b^5x^4}{4} + \frac{7ab^6x^5}{5} + \frac{b^7x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**2,x)

[Out] $-a**7/x + 7*a**6*b*\log(x) + 21*a**5*b**2*x + 35*a**4*b**3*x**2/2 + 35*a**3*b**4*x**3/3 + 21*a**2*b**5*x**4/4 + 7*a*b**6*x**5/5 + b**7*x**6/6$

$$3.109 \quad \int \frac{(a+bx)^7}{x^3} dx$$

Optimal. Leaf size=84

$$-\frac{a^7}{2x^2} - \frac{7a^6b}{x} + 21a^5b^2 \log(x) + 35a^4b^3x + \frac{35}{2}a^3b^4x^2 + 7a^2b^5x^3 + \frac{7}{4}ab^6x^4 + \frac{b^7x^5}{5}$$

[Out] $-1/2*a^7/x^2-7*a^6*b/x+35*a^4*b^3*x+35/2*a^3*b^4*x^2+7*a^2*b^5*x^3+7/4*a*b^6*x^4+1/5*b^7*x^5+21*a^5*b^2*\ln(x)$

Rubi [A] time = 0.03, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{35}{2}a^3b^4x^2 + 7a^2b^5x^3 + 35a^4b^3x + 21a^5b^2 \log(x) - \frac{7a^6b}{x} - \frac{a^7}{2x^2} + \frac{7}{4}ab^6x^4 + \frac{b^7x^5}{5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^3, x]

[Out] $-a^7/(2*x^2) - (7*a^6*b)/x + 35*a^4*b^3*x + (35*a^3*b^4*x^2)/2 + 7*a^2*b^5*x^3 + (7*a*b^6*x^4)/4 + (b^7*x^5)/5 + 21*a^5*b^2*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^7}{x^3} dx = \int \left(35a^4b^3 + \frac{a^7}{x^3} + \frac{7a^6b}{x^2} + \frac{21a^5b^2}{x} + 35a^3b^4x + 21a^2b^5x^2 + 7ab^6x^3 + b^7x^4 \right) dx$$

$$= -\frac{a^7}{2x^2} - \frac{7a^6b}{x} + 35a^4b^3x + \frac{35}{2}a^3b^4x^2 + 7a^2b^5x^3 + \frac{7}{4}ab^6x^4 + \frac{b^7x^5}{5} + 21a^5b^2 \log(x)$$

Mathematica [A] time = 0.00, size = 84, normalized size = 1.00

$$-\frac{a^7}{2x^2} - \frac{7a^6b}{x} + 21a^5b^2 \log(x) + 35a^4b^3x + \frac{35}{2}a^3b^4x^2 + 7a^2b^5x^3 + \frac{7}{4}ab^6x^4 + \frac{b^7x^5}{5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^3,x]

[Out] $-1/2*a^7/x^2 - (7*a^6*b)/x + 35*a^4*b^3*x + (35*a^3*b^4*x^2)/2 + 7*a^2*b^5*x^3 + (7*a*b^6*x^4)/4 + (b^7*x^5)/5 + 21*a^5*b^2*\text{Log}[x]$

fricas [A] time = 0.48, size = 81, normalized size = 0.96

$$\frac{4b^7x^7 + 35ab^6x^6 + 140a^2b^5x^5 + 350a^3b^4x^4 + 700a^4b^3x^3 + 420a^5b^2x^2 \log(x) - 140a^6bx - 10a^7}{20x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^3,x, algorithm="fricas")

[Out] $1/20*(4*b^7*x^7 + 35*a*b^6*x^6 + 140*a^2*b^5*x^5 + 350*a^3*b^4*x^4 + 700*a^4*b^3*x^3 + 420*a^5*b^2*x^2*\log(x) - 140*a^6*b*x - 10*a^7)/x^2$

giac [A] time = 1.06, size = 76, normalized size = 0.90

$$\frac{1}{5}b^7x^5 + \frac{7}{4}ab^6x^4 + 7a^2b^5x^3 + \frac{35}{2}a^3b^4x^2 + 35a^4b^3x + 21a^5b^2 \log(|x|) - \frac{14a^6bx + a^7}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^3,x, algorithm="giac")

[Out] $1/5*b^7*x^5 + 7/4*a*b^6*x^4 + 7*a^2*b^5*x^3 + 35/2*a^3*b^4*x^2 + 35*a^4*b^3*x + 21*a^5*b^2*\log(\text{abs}(x)) - 1/2*(14*a^6*b*x + a^7)/x^2$

maple [A] time = 0.01, size = 77, normalized size = 0.92

$$\frac{b^7x^5}{5} + \frac{7ab^6x^4}{4} + 7a^2b^5x^3 + \frac{35a^3b^4x^2}{2} + 21a^5b^2 \ln(x) + 35a^4b^3x - \frac{7a^6b}{x} - \frac{a^7}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^3,x)

[Out] $-1/2*a^7/x^2 - 7*a^6*b/x + 35*a^4*b^3*x + 35/2*a^3*b^4*x^2 + 7*a^2*b^5*x^3 + 7/4*a*b^6*x^4 + 1/5*b^7*x^5 + 21*a^5*b^2*\ln(x)$

maxima [A] time = 1.38, size = 75, normalized size = 0.89

$$\frac{1}{5}b^7x^5 + \frac{7}{4}ab^6x^4 + 7a^2b^5x^3 + \frac{35}{2}a^3b^4x^2 + 35a^4b^3x + 21a^5b^2 \log(x) - \frac{14a^6bx + a^7}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^3,x, algorithm="maxima")

[Out] $\frac{1}{5}b^7x^5 + \frac{7}{4}a^6bx^4 + 7a^5b^2x^3 + \frac{35}{2}a^4b^3x^2 + 35a^3b^4x + 21a^2b^5x + 21a^5b^2\log(x) - \frac{1}{2}(14a^6bx + a^7)/x^2$

mupad [B] time = 0.05, size = 77, normalized size = 0.92

$$\frac{b^7x^5}{5} - \frac{a^7}{2} + \frac{7bxa^6}{x^2} + 35a^4b^3x + \frac{7ab^6x^4}{4} + \frac{35a^3b^4x^2}{2} + 7a^2b^5x^3 + 21a^5b^2\ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^3,x)

[Out] $(b^7x^5)/5 - (a^7/2 + 7a^6bx)/x^2 + 35a^4b^3x + (7a^6bx^4)/4 + (35a^3b^4x^2)/2 + 7a^2b^5x^3 + 21a^5b^2\log(x)$

sympy [A] time = 0.25, size = 85, normalized size = 1.01

$$21a^5b^2\log(x) + 35a^4b^3x + \frac{35a^3b^4x^2}{2} + 7a^2b^5x^3 + \frac{7ab^6x^4}{4} + \frac{b^7x^5}{5} + \frac{-a^7 - 14a^6bx}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**3,x)

[Out] $21a^{**5}b^{**2}\log(x) + 35a^{**4}b^{**3}x + 35a^{**3}b^{**4}x^{**2}/2 + 7a^{**2}b^{**5}x^{**3} + 7a^{**6}b^{**4}x^{**4}/4 + b^{**7}x^{**5}/5 + (-a^{**7} - 14a^{**6}b^{**4}x)/(2x^{**2})$

$$3.110 \quad \int \frac{(a+bx)^7}{x^4} dx$$

Optimal. Leaf size=86

$$-\frac{a^7}{3x^3} - \frac{7a^6b}{2x^2} - \frac{21a^5b^2}{x} + 35a^4b^3 \log(x) + 35a^3b^4x + \frac{21}{2}a^2b^5x^2 + \frac{7}{3}ab^6x^3 + \frac{b^7x^4}{4}$$

[Out] $-1/3*a^7/x^3-7/2*a^6*b/x^2-21*a^5*b^2/x+35*a^3*b^4*x+21/2*a^2*b^5*x^2+7/3*a*b^6*x^3+1/4*b^7*x^4+35*a^4*b^3*\ln(x)$

Rubi [A] time = 0.03, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{21}{2}a^2b^5x^2 - \frac{21a^5b^2}{x} + 35a^3b^4x + 35a^4b^3 \log(x) - \frac{7a^6b}{2x^2} - \frac{a^7}{3x^3} + \frac{7}{3}ab^6x^3 + \frac{b^7x^4}{4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^4, x]

[Out] $-a^7/(3*x^3) - (7*a^6*b)/(2*x^2) - (21*a^5*b^2)/x + 35*a^3*b^4*x + (21*a^2*b^5*x^2)/2 + (7*a*b^6*x^3)/3 + (b^7*x^4)/4 + 35*a^4*b^3*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x^4} dx &= \int \left(35a^3b^4 + \frac{a^7}{x^4} + \frac{7a^6b}{x^3} + \frac{21a^5b^2}{x^2} + \frac{35a^4b^3}{x} + 21a^2b^5x + 7ab^6x^2 + b^7x^3 \right) dx \\ &= -\frac{a^7}{3x^3} - \frac{7a^6b}{2x^2} - \frac{21a^5b^2}{x} + 35a^3b^4x + \frac{21}{2}a^2b^5x^2 + \frac{7}{3}ab^6x^3 + \frac{b^7x^4}{4} + 35a^4b^3 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 86, normalized size = 1.00

$$-\frac{a^7}{3x^3} - \frac{7a^6b}{2x^2} - \frac{21a^5b^2}{x} + 35a^4b^3 \log(x) + 35a^3b^4x + \frac{21}{2}a^2b^5x^2 + \frac{7}{3}ab^6x^3 + \frac{b^7x^4}{4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^4, x]

[Out] $-1/3*a^7/x^3 - (7*a^6*b)/(2*x^2) - (21*a^5*b^2)/x + 35*a^3*b^4*x + (21*a^2*b^5*x^2)/2 + (7*a*b^6*x^3)/3 + (b^7*x^4)/4 + 35*a^4*b^3*\text{Log}[x]$

fricas [A] time = 0.50, size = 81, normalized size = 0.94

$$\frac{3 b^7 x^7 + 28 a b^6 x^6 + 126 a^2 b^5 x^5 + 420 a^3 b^4 x^4 + 420 a^4 b^3 x^3 \log(x) - 252 a^5 b^2 x^2 - 42 a^6 b x - 4 a^7}{12 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^4, x, algorithm="fricas")

[Out] $1/12*(3*b^7*x^7 + 28*a*b^6*x^6 + 126*a^2*b^5*x^5 + 420*a^3*b^4*x^4 + 420*a^4*b^3*x^3*\log(x) - 252*a^5*b^2*x^2 - 42*a^6*b*x - 4*a^7)/x^3$

giac [A] time = 1.09, size = 78, normalized size = 0.91

$$\frac{1}{4} b^7 x^4 + \frac{7}{3} a b^6 x^3 + \frac{21}{2} a^2 b^5 x^2 + 35 a^3 b^4 x + 35 a^4 b^3 \log(|x|) - \frac{126 a^5 b^2 x^2 + 21 a^6 b x + 2 a^7}{6 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^4, x, algorithm="giac")

[Out] $1/4*b^7*x^4 + 7/3*a*b^6*x^3 + 21/2*a^2*b^5*x^2 + 35*a^3*b^4*x + 35*a^4*b^3*\log(\text{abs}(x)) - 1/6*(126*a^5*b^2*x^2 + 21*a^6*b*x + 2*a^7)/x^3$

maple [A] time = 0.01, size = 77, normalized size = 0.90

$$\frac{b^7 x^4}{4} + \frac{7 a b^6 x^3}{3} + \frac{21 a^2 b^5 x^2}{2} + 35 a^3 b^4 \ln(x) + 35 a^4 b^3 x - \frac{21 a^5 b^2}{x} - \frac{7 a^6 b}{2 x^2} - \frac{a^7}{3 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^4, x)

[Out] $-1/3*a^7/x^3 - 7/2*a^6*b/x^2 - 21*a^5*b^2/x + 35*a^3*b^4*x + 21/2*a^2*b^5*x^2 + 7/3*a*b^6*x^3 + 1/4*b^7*x^4 + 35*a^4*b^3*\ln(x)$

maxima [A] time = 1.33, size = 77, normalized size = 0.90

$$\frac{1}{4} b^7 x^4 + \frac{7}{3} a b^6 x^3 + \frac{21}{2} a^2 b^5 x^2 + 35 a^3 b^4 x + 35 a^4 b^3 \log(x) - \frac{126 a^5 b^2 x^2 + 21 a^6 b x + 2 a^7}{6 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^4,x, algorithm="maxima")

[Out] $\frac{1}{4}b^7x^4 + \frac{7}{3}a^6b^6x^3 + \frac{21}{2}a^5b^5x^2 + 35a^4b^4x + 35a^3b^3\log(x) - \frac{1}{6}(126a^5b^2x^2 + 21a^6bx + 2a^7)/x^3$

mupad [B] time = 0.05, size = 77, normalized size = 0.90

$$\frac{b^7 x^4}{4} - \frac{\frac{a^7}{3} + \frac{7a^6 b x}{2} + 21 a^5 b^2 x^2}{x^3} + 35 a^3 b^4 x + \frac{7 a b^6 x^3}{3} + \frac{21 a^2 b^5 x^2}{2} + 35 a^4 b^3 \ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^4,x)

[Out] $(b^7x^4)/4 - (a^7/3 + 21a^5b^2x^2 + (7a^6bx)/2)/x^3 + 35a^3b^4x + (7a^6bx^3)/3 + (21a^2b^5x^2)/2 + 35a^4b^3\log(x)$

sympy [A] time = 0.31, size = 87, normalized size = 1.01

$$35a^4b^3 \log(x) + 35a^3b^4x + \frac{21a^2b^5x^2}{2} + \frac{7ab^6x^3}{3} + \frac{b^7x^4}{4} + \frac{-2a^7 - 21a^6bx - 126a^5b^2x^2}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**4,x)

[Out] $35a^{**4}b^{**3}\log(x) + 35a^{**3}b^{**4}x + 21a^{**2}b^{**5}x^{**2}/2 + 7a^*b^{**6}x^{**3}/3 + b^{**7}x^{**4}/4 + (-2a^{**7} - 21a^{**6}b*x - 126a^{**5}b^{**2}x^{**2})/(6x^{**3})$

$$3.111 \quad \int \frac{(a+bx)^7}{x^5} dx$$

Optimal. Leaf size=86

$$-\frac{a^7}{4x^4} - \frac{7a^6b}{3x^3} - \frac{21a^5b^2}{2x^2} - \frac{35a^4b^3}{x} + 35a^3b^4 \log(x) + 21a^2b^5x + \frac{7}{2}ab^6x^2 + \frac{b^7x^3}{3}$$

[Out] $-1/4*a^7/x^4-7/3*a^6*b/x^3-21/2*a^5*b^2/x^2-35*a^4*b^3/x+21*a^2*b^5*x+7/2*a*b^6*x^2+1/3*b^7*x^3+35*a^3*b^4*\ln(x)$

Rubi [A] time = 0.03, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{21a^5b^2}{2x^2} - \frac{35a^4b^3}{x} + 21a^2b^5x + 35a^3b^4 \log(x) - \frac{7a^6b}{3x^3} - \frac{a^7}{4x^4} + \frac{7}{2}ab^6x^2 + \frac{b^7x^3}{3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^5, x]

[Out] $-a^7/(4*x^4) - (7*a^6*b)/(3*x^3) - (21*a^5*b^2)/(2*x^2) - (35*a^4*b^3)/x + 21*a^2*b^5*x + (7*a*b^6*x^2)/2 + (b^7*x^3)/3 + 35*a^3*b^4*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x^5} dx &= \int \left(21a^2b^5 + \frac{a^7}{x^5} + \frac{7a^6b}{x^4} + \frac{21a^5b^2}{x^3} + \frac{35a^4b^3}{x^2} + \frac{35a^3b^4}{x} + 7ab^6x + b^7x^2 \right) dx \\ &= -\frac{a^7}{4x^4} - \frac{7a^6b}{3x^3} - \frac{21a^5b^2}{2x^2} - \frac{35a^4b^3}{x} + 21a^2b^5x + \frac{7}{2}ab^6x^2 + \frac{b^7x^3}{3} + 35a^3b^4 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 86, normalized size = 1.00

$$-\frac{a^7}{4x^4} - \frac{7a^6b}{3x^3} - \frac{21a^5b^2}{2x^2} - \frac{35a^4b^3}{x} + 35a^3b^4 \log(x) + 21a^2b^5x + \frac{7}{2}ab^6x^2 + \frac{b^7x^3}{3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^5,x]

[Out] $-1/4*a^7/x^4 - (7*a^6*b)/(3*x^3) - (21*a^5*b^2)/(2*x^2) - (35*a^4*b^3)/x + 21*a^2*b^5*x + (7*a*b^6*x^2)/2 + (b^7*x^3)/3 + 35*a^3*b^4*\text{Log}[x]$

fricas [A] time = 0.44, size = 81, normalized size = 0.94

$$\frac{4b^7x^7 + 42ab^6x^6 + 252a^2b^5x^5 + 420a^3b^4x^4 \log(x) - 420a^4b^3x^3 - 126a^5b^2x^2 - 28a^6bx - 3a^7}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^5,x, algorithm="fricas")

[Out] $1/12*(4*b^7*x^7 + 42*a*b^6*x^6 + 252*a^2*b^5*x^5 + 420*a^3*b^4*x^4*\log(x) - 420*a^4*b^3*x^3 - 126*a^5*b^2*x^2 - 28*a^6*b*x - 3*a^7)/x^4$

giac [A] time = 1.04, size = 78, normalized size = 0.91

$$\frac{1}{3}b^7x^3 + \frac{7}{2}ab^6x^2 + 21a^2b^5x + 35a^3b^4 \log(|x|) - \frac{420a^4b^3x^3 + 126a^5b^2x^2 + 28a^6bx + 3a^7}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^5,x, algorithm="giac")

[Out] $1/3*b^7*x^3 + 7/2*a*b^6*x^2 + 21*a^2*b^5*x + 35*a^3*b^4*\log(\text{abs}(x)) - 1/12*(420*a^4*b^3*x^3 + 126*a^5*b^2*x^2 + 28*a^6*b*x + 3*a^7)/x^4$

maple [A] time = 0.01, size = 77, normalized size = 0.90

$$\frac{b^7x^3}{3} + \frac{7ab^6x^2}{2} + 35a^3b^4 \ln(x) + 21a^2b^5x - \frac{35a^4b^3}{x} - \frac{21a^5b^2}{2x^2} - \frac{7a^6b}{3x^3} - \frac{a^7}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^5,x)

[Out] $-1/4*a^7/x^4 - 7/3*a^6*b/x^3 - 21/2*a^5*b^2/x^2 - 35*a^4*b^3/x + 21*a^2*b^5*x + 7/2*a*b^6*x^2 + 1/3*b^7*x^3 + 35*a^3*b^4*\ln(x)$

maxima [A] time = 1.40, size = 77, normalized size = 0.90

$$\frac{1}{3}b^7x^3 + \frac{7}{2}ab^6x^2 + 21a^2b^5x + 35a^3b^4 \log(x) - \frac{420a^4b^3x^3 + 126a^5b^2x^2 + 28a^6bx + 3a^7}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^5,x, algorithm="maxima")

[Out] $\frac{1}{3}b^7x^3 + \frac{7}{2}a^6bx^2 + 21a^5b^2x + 35a^4b^3x^3 + 35a^3b^4\log(x) - \frac{1}{12}(420a^4b^3x^3 + 126a^5b^2x^2 + 28a^6bx + 3a^7)/x^4$

mupad [B] time = 0.09, size = 77, normalized size = 0.90

$$\frac{b^7x^3}{3} - \frac{\frac{a^7}{4} + \frac{7a^6bx}{3} + \frac{21a^5b^2x^2}{2} + 35a^4b^3x^3}{x^4} + 21a^2b^5x + \frac{7ab^6x^2}{2} + 35a^3b^4\ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^5,x)

[Out] $\frac{(b^7x^3)/3 - (a^7/4 + (21a^5b^2x^2)/2 + 35a^4b^3x^3 + (7a^6bx)/3)/x^4 + 21a^2b^5x + (7a^6bx^2)/2 + 35a^3b^4\log(x)}$

sympy [A] time = 0.33, size = 85, normalized size = 0.99

$$35a^3b^4\log(x) + 21a^2b^5x + \frac{7ab^6x^2}{2} + \frac{b^7x^3}{3} + \frac{-3a^7 - 28a^6bx - 126a^5b^2x^2 - 420a^4b^3x^3}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**5,x)

[Out] $35a^{**3}b^{**4}\log(x) + 21a^{**2}b^{**5}x + 7a^6bx^{**2}/2 + b^{**7}x^{**3}/3 + (-3a^{**7} - 28a^{**6}bx - 126a^{**5}b^{**2}x^{**2} - 420a^{**4}b^{**3}x^{**3})/(12x^{**4})$

$$3.112 \quad \int \frac{(a+bx)^7}{x^6} dx$$

Optimal. Leaf size=84

$$-\frac{a^7}{5x^5} - \frac{7a^6b}{4x^4} - \frac{7a^5b^2}{x^3} - \frac{35a^4b^3}{2x^2} - \frac{35a^3b^4}{x} + 21a^2b^5 \log(x) + 7ab^6x + \frac{b^7x^2}{2}$$

[Out] $-1/5*a^7/x^5-7/4*a^6*b/x^4-7*a^5*b^2/x^3-35/2*a^4*b^3/x^2-35*a^3*b^4/x+7*a*b^6*x+1/2*b^7*x^2+21*a^2*b^5*\ln(x)$

Rubi [A] time = 0.03, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{7a^5b^2}{x^3} - \frac{35a^4b^3}{2x^2} - \frac{35a^3b^4}{x} + 21a^2b^5 \log(x) - \frac{7a^6b}{4x^4} - \frac{a^7}{5x^5} + 7ab^6x + \frac{b^7x^2}{2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^6, x]

[Out] $-a^7/(5*x^5) - (7*a^6*b)/(4*x^4) - (7*a^5*b^2)/x^3 - (35*a^4*b^3)/(2*x^2) - (35*a^3*b^4)/x + 7*a*b^6*x + (b^7*x^2)/2 + 21*a^2*b^5*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x^6} dx &= \int \left(7ab^6 + \frac{a^7}{x^6} + \frac{7a^6b}{x^5} + \frac{21a^5b^2}{x^4} + \frac{35a^4b^3}{x^3} + \frac{35a^3b^4}{x^2} + \frac{21a^2b^5}{x} + b^7x \right) dx \\ &= -\frac{a^7}{5x^5} - \frac{7a^6b}{4x^4} - \frac{7a^5b^2}{x^3} - \frac{35a^4b^3}{2x^2} - \frac{35a^3b^4}{x} + 7ab^6x + \frac{b^7x^2}{2} + 21a^2b^5 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 84, normalized size = 1.00

$$-\frac{a^7}{5x^5} - \frac{7a^6b}{4x^4} - \frac{7a^5b^2}{x^3} - \frac{35a^4b^3}{2x^2} - \frac{35a^3b^4}{x} + 21a^2b^5 \log(x) + 7ab^6x + \frac{b^7x^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^6, x]

[Out] $-1/5*a^7/x^5 - (7*a^6*b)/(4*x^4) - (7*a^5*b^2)/x^3 - (35*a^4*b^3)/(2*x^2) - (35*a^3*b^4)/x + 7*a*b^6*x + (b^7*x^2)/2 + 21*a^2*b^5*\text{Log}[x]$

fricas [A] time = 0.44, size = 81, normalized size = 0.96

$$\frac{10 b^7 x^7 + 140 a b^6 x^6 + 420 a^2 b^5 x^5 \log(x) - 700 a^3 b^4 x^4 - 350 a^4 b^3 x^3 - 140 a^5 b^2 x^2 - 35 a^6 b x - 4 a^7}{20 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^6, x, algorithm="fricas")

[Out] $1/20*(10*b^7*x^7 + 140*a*b^6*x^6 + 420*a^2*b^5*x^5*\log(x) - 700*a^3*b^4*x^4 - 350*a^4*b^3*x^3 - 140*a^5*b^2*x^2 - 35*a^6*b*x - 4*a^7)/x^5$

giac [A] time = 1.01, size = 78, normalized size = 0.93

$$\frac{1}{2} b^7 x^2 + 7 a b^6 x + 21 a^2 b^5 \log(|x|) - \frac{700 a^3 b^4 x^4 + 350 a^4 b^3 x^3 + 140 a^5 b^2 x^2 + 35 a^6 b x + 4 a^7}{20 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^6, x, algorithm="giac")

[Out] $1/2*b^7*x^2 + 7*a*b^6*x + 21*a^2*b^5*\log(\text{abs}(x)) - 1/20*(700*a^3*b^4*x^4 + 350*a^4*b^3*x^3 + 140*a^5*b^2*x^2 + 35*a^6*b*x + 4*a^7)/x^5$

maple [A] time = 0.01, size = 77, normalized size = 0.92

$$\frac{b^7 x^2}{2} + 21 a^2 b^5 \ln(x) + 7 a b^6 x - \frac{35 a^3 b^4}{x} - \frac{35 a^4 b^3}{2 x^2} - \frac{7 a^5 b^2}{x^3} - \frac{7 a^6 b}{4 x^4} - \frac{a^7}{5 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^6, x)

[Out] $-1/5*a^7/x^5 - 7/4*a^6*b/x^4 - 7*a^5*b^2/x^3 - 35/2*a^4*b^3/x^2 - 35*a^3*b^4/x + 7*a*b^6*x + 1/2*b^7*x^2 + 21*a^2*b^5*\ln(x)$

maxima [A] time = 1.38, size = 77, normalized size = 0.92

$$\frac{1}{2} b^7 x^2 + 7 a b^6 x + 21 a^2 b^5 \log(x) - \frac{700 a^3 b^4 x^4 + 350 a^4 b^3 x^3 + 140 a^5 b^2 x^2 + 35 a^6 b x + 4 a^7}{20 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^6,x, algorithm="maxima")

[Out] $\frac{1}{2}b^7x^2 + 7ab^6x + 21a^2b^5\log(x) - \frac{1}{20}(700a^3b^4x^4 + 350a^4b^3x^3 + 140a^5b^2x^2 + 35a^6bx + 4a^7)/x^5$

mupad [B] time = 0.11, size = 77, normalized size = 0.92

$$\frac{b^7 x^2}{2} - \frac{\frac{a^7}{5} + \frac{7a^6 b x}{4} + 7a^5 b^2 x^2 + \frac{35a^4 b^3 x^3}{2} + 35a^3 b^4 x^4}{x^5} + 21a^2 b^5 \ln(x) + 7ab^6 x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^6,x)

[Out] $(b^7x^2)/2 - (a^7/5 + 7a^5b^2x^2 + (35a^4b^3x^3)/2 + 35a^3b^4x^4 + (7a^6bx)/4)/x^5 + 21a^2b^5\log(x) + 7ab^6x$

sympy [A] time = 0.45, size = 83, normalized size = 0.99

$$21a^2b^5 \log(x) + 7ab^6x + \frac{b^7x^2}{2} + \frac{-4a^7 - 35a^6bx - 140a^5b^2x^2 - 350a^4b^3x^3 - 700a^3b^4x^4}{20x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**6,x)

[Out] $21a^{**2}b^{**5}\log(x) + 7a*b^{**6}x + b^{**7}x^{**2}/2 + (-4a^{**7} - 35a^{**6}b*x - 140a^{**5}b^{**2}x^{**2} - 350a^{**4}b^{**3}x^{**3} - 700a^{**3}b^{**4}x^{**4})/(20x^{**5})$

$$3.113 \quad \int \frac{(a+bx)^7}{x^7} dx$$

Optimal. Leaf size=85

$$-\frac{a^7}{6x^6} - \frac{7a^6b}{5x^5} - \frac{21a^5b^2}{4x^4} - \frac{35a^4b^3}{3x^3} - \frac{35a^3b^4}{2x^2} - \frac{21a^2b^5}{x} + 7ab^6 \log(x) + b^7x$$

[Out] $-1/6*a^7/x^6-7/5*a^6*b/x^5-21/4*a^5*b^2/x^4-35/3*a^4*b^3/x^3-35/2*a^3*b^4/x^2-21*a^2*b^5/x+b^7*x+7*a*b^6*\ln(x)$

Rubi [A] time = 0.03, antiderivative size = 85, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{21a^5b^2}{4x^4} - \frac{35a^4b^3}{3x^3} - \frac{35a^3b^4}{2x^2} - \frac{21a^2b^5}{x} - \frac{7a^6b}{5x^5} - \frac{a^7}{6x^6} + 7ab^6 \log(x) + b^7x$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^7, x]

[Out] $-a^7/(6*x^6) - (7*a^6*b)/(5*x^5) - (21*a^5*b^2)/(4*x^4) - (35*a^4*b^3)/(3*x^3) - (35*a^3*b^4)/(2*x^2) - (21*a^2*b^5)/x + b^7*x + 7*a*b^6*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x^7} dx &= \int \left(b^7 + \frac{a^7}{x^7} + \frac{7a^6b}{x^6} + \frac{21a^5b^2}{x^5} + \frac{35a^4b^3}{x^4} + \frac{35a^3b^4}{x^3} + \frac{21a^2b^5}{x^2} + \frac{7ab^6}{x} \right) dx \\ &= -\frac{a^7}{6x^6} - \frac{7a^6b}{5x^5} - \frac{21a^5b^2}{4x^4} - \frac{35a^4b^3}{3x^3} - \frac{35a^3b^4}{2x^2} - \frac{21a^2b^5}{x} + b^7x + 7ab^6 \log(x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 85, normalized size = 1.00

$$-\frac{a^7}{6x^6} - \frac{7a^6b}{5x^5} - \frac{21a^5b^2}{4x^4} - \frac{35a^4b^3}{3x^3} - \frac{35a^3b^4}{2x^2} - \frac{21a^2b^5}{x} + 7ab^6 \log(x) + b^7x$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^7,x]

[Out] $-1/6*a^7/x^6 - (7*a^6*b)/(5*x^5) - (21*a^5*b^2)/(4*x^4) - (35*a^4*b^3)/(3*x^3) - (35*a^3*b^4)/(2*x^2) - (21*a^2*b^5)/x + b^7*x + 7*a*b^6*\text{Log}[x]$

fricas [A] time = 0.40, size = 81, normalized size = 0.95

$$\frac{60 b^7 x^7 + 420 a b^6 x^6 \log(x) - 1260 a^2 b^5 x^5 - 1050 a^3 b^4 x^4 - 700 a^4 b^3 x^3 - 315 a^5 b^2 x^2 - 84 a^6 b x - 10 a^7}{60 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^7,x, algorithm="fricas")

[Out] $1/60*(60*b^7*x^7 + 420*a*b^6*x^6*\log(x) - 1260*a^2*b^5*x^5 - 1050*a^3*b^4*x^4 - 700*a^4*b^3*x^3 - 315*a^5*b^2*x^2 - 84*a^6*b*x - 10*a^7)/x^6$

giac [A] time = 0.99, size = 77, normalized size = 0.91

$$b^7 x + 7 a b^6 \log(|x|) - \frac{1260 a^2 b^5 x^5 + 1050 a^3 b^4 x^4 + 700 a^4 b^3 x^3 + 315 a^5 b^2 x^2 + 84 a^6 b x + 10 a^7}{60 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^7,x, algorithm="giac")

[Out] $b^7*x + 7*a*b^6*\log(\text{abs}(x)) - 1/60*(1260*a^2*b^5*x^5 + 1050*a^3*b^4*x^4 + 700*a^4*b^3*x^3 + 315*a^5*b^2*x^2 + 84*a^6*b*x + 10*a^7)/x^6$

maple [A] time = 0.01, size = 76, normalized size = 0.89

$$7 a b^6 \ln(x) + b^7 x - \frac{21 a^2 b^5}{x} - \frac{35 a^3 b^4}{2 x^2} - \frac{35 a^4 b^3}{3 x^3} - \frac{21 a^5 b^2}{4 x^4} - \frac{7 a^6 b}{5 x^5} - \frac{a^7}{6 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^7,x)

[Out] $-1/6*a^7/x^6-7/5*a^6*b/x^5-21/4*a^5*b^2/x^4-35/3*a^4*b^3/x^3-35/2*a^3*b^4/x^2-21*a^2*b^5/x+b^7*x+7*a*b^6*\ln(x)$

maxima [A] time = 1.38, size = 76, normalized size = 0.89

$$b^7 x + 7 a b^6 \log(x) - \frac{1260 a^2 b^5 x^5 + 1050 a^3 b^4 x^4 + 700 a^4 b^3 x^3 + 315 a^5 b^2 x^2 + 84 a^6 b x + 10 a^7}{60 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^7,x, algorithm="maxima")

[Out] $b^7x + 7ab^6\log(x) - \frac{1}{60}(1260a^2b^5x^5 + 1050a^3b^4x^4 + 700a^4b^3x^3 + 315a^5b^2x^2 + 84a^6bx + 10a^7)/x^6$

mupad [B] time = 0.11, size = 81, normalized size = 0.95

$$\frac{10a^7 - 60b^7x^7 + 315a^5b^2x^2 + 700a^4b^3x^3 + 1050a^3b^4x^4 + 1260a^2b^5x^5 + 84a^6bx - 420ab^6x^6 \ln(x)}{60x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^7,x)

[Out] $-(10a^7 - 60b^7x^7 + 315a^5b^2x^2 + 700a^4b^3x^3 + 1050a^3b^4x^4 + 1260a^2b^5x^5 + 84a^6bx - 420ab^6x^6 \log(x))/(60x^6)$

sympy [A] time = 0.60, size = 82, normalized size = 0.96

$$7ab^6 \log(x) + b^7x + \frac{-10a^7 - 84a^6bx - 315a^5b^2x^2 - 700a^4b^3x^3 - 1050a^3b^4x^4 - 1260a^2b^5x^5}{60x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**7,x)

[Out] $7a^7b^6\log(x) + b^7x + \frac{(-10a^7 - 84a^6bx - 315a^5b^2x^2 - 700a^4b^3x^3 - 1050a^3b^4x^4 - 1260a^2b^5x^5)}{(60x^6)}$

$$3.114 \quad \int \frac{(a+bx)^7}{x^8} dx$$

Optimal. Leaf size=89

$$-\frac{a^7}{7x^7} - \frac{7a^6b}{6x^6} - \frac{21a^5b^2}{5x^5} - \frac{35a^4b^3}{4x^4} - \frac{35a^3b^4}{3x^3} - \frac{21a^2b^5}{2x^2} - \frac{7ab^6}{x} + b^7 \log(x)$$

[Out] $-1/7*a^7/x^7-7/6*a^6*b/x^6-21/5*a^5*b^2/x^5-35/4*a^4*b^3/x^4-35/3*a^3*b^4/x^3-21/2*a^2*b^5/x^2-7*a*b^6/x+b^7*\ln(x)$

Rubi [A] time = 0.03, antiderivative size = 89, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{21a^5b^2}{5x^5} - \frac{35a^4b^3}{4x^4} - \frac{35a^3b^4}{3x^3} - \frac{21a^2b^5}{2x^2} - \frac{7a^6b}{6x^6} - \frac{a^7}{7x^7} - \frac{7ab^6}{x} + b^7 \log(x)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^8, x]

[Out] $-a^7/(7*x^7) - (7*a^6*b)/(6*x^6) - (21*a^5*b^2)/(5*x^5) - (35*a^4*b^3)/(4*x^4) - (35*a^3*b^4)/(3*x^3) - (21*a^2*b^5)/(2*x^2) - (7*a*b^6)/x + b^7*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x^8} dx &= \int \left(\frac{a^7}{x^8} + \frac{7a^6b}{x^7} + \frac{21a^5b^2}{x^6} + \frac{35a^4b^3}{x^5} + \frac{35a^3b^4}{x^4} + \frac{21a^2b^5}{x^3} + \frac{7ab^6}{x^2} + \frac{b^7}{x} \right) dx \\ &= -\frac{a^7}{7x^7} - \frac{7a^6b}{6x^6} - \frac{21a^5b^2}{5x^5} - \frac{35a^4b^3}{4x^4} - \frac{35a^3b^4}{3x^3} - \frac{21a^2b^5}{2x^2} - \frac{7ab^6}{x} + b^7 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 89, normalized size = 1.00

$$-\frac{a^7}{7x^7} - \frac{7a^6b}{6x^6} - \frac{21a^5b^2}{5x^5} - \frac{35a^4b^3}{4x^4} - \frac{35a^3b^4}{3x^3} - \frac{21a^2b^5}{2x^2} - \frac{7ab^6}{x} + b^7 \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^8,x]

[Out] $-1/7*a^7/x^7 - (7*a^6*b)/(6*x^6) - (21*a^5*b^2)/(5*x^5) - (35*a^4*b^3)/(4*x^4) - (35*a^3*b^4)/(3*x^3) - (21*a^2*b^5)/(2*x^2) - (7*a*b^6)/x + b^7*\text{Log}[x]$

fricas [A] time = 0.46, size = 81, normalized size = 0.91

$$\frac{420 b^7 x^7 \log(x) - 2940 a b^6 x^6 - 4410 a^2 b^5 x^5 - 4900 a^3 b^4 x^4 - 3675 a^4 b^3 x^3 - 1764 a^5 b^2 x^2 - 490 a^6 b x - 60 a^7}{420 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^8,x, algorithm="fricas")

[Out] $1/420*(420*b^7*x^7*\log(x) - 2940*a*b^6*x^6 - 4410*a^2*b^5*x^5 - 4900*a^3*b^4*x^4 - 3675*a^4*b^3*x^3 - 1764*a^5*b^2*x^2 - 490*a^6*b*x - 60*a^7)/x^7$

giac [A] time = 1.27, size = 79, normalized size = 0.89

$$b^7 \log(|x|) - \frac{2940 a b^6 x^6 + 4410 a^2 b^5 x^5 + 4900 a^3 b^4 x^4 + 3675 a^4 b^3 x^3 + 1764 a^5 b^2 x^2 + 490 a^6 b x + 60 a^7}{420 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^8,x, algorithm="giac")

[Out] $b^7*\log(\text{abs}(x)) - 1/420*(2940*a*b^6*x^6 + 4410*a^2*b^5*x^5 + 4900*a^3*b^4*x^4 + 3675*a^4*b^3*x^3 + 1764*a^5*b^2*x^2 + 490*a^6*b*x + 60*a^7)/x^7$

maple [A] time = 0.01, size = 78, normalized size = 0.88

$$b^7 \ln(x) - \frac{7a b^6}{x} - \frac{21a^2 b^5}{2x^2} - \frac{35a^3 b^4}{3x^3} - \frac{35a^4 b^3}{4x^4} - \frac{21a^5 b^2}{5x^5} - \frac{7a^6 b}{6x^6} - \frac{a^7}{7x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^8,x)

[Out] $-1/7*a^7/x^7 - 7/6*a^6*b/x^6 - 21/5*a^5*b^2/x^5 - 35/4*a^4*b^3/x^4 - 35/3*a^3*b^4/x^3 - 21/2*a^2*b^5/x^2 - 7*a*b^6/x + b^7*\ln(x)$

maxima [A] time = 1.36, size = 78, normalized size = 0.88

$$b^7 \log(x) - \frac{2940 a b^6 x^6 + 4410 a^2 b^5 x^5 + 4900 a^3 b^4 x^4 + 3675 a^4 b^3 x^3 + 1764 a^5 b^2 x^2 + 490 a^6 b x + 60 a^7}{420 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^8,x, algorithm="maxima")

[Out] $b^7 \log(x) - \frac{1}{420} (2940 a^6 b x^6 + 4410 a^5 b^2 x^5 + 4900 a^4 b^3 x^4 + 3675 a^3 b^4 x^3 + 1764 a^2 b^5 x^2 + 490 a b^6 x + 60 a^7) / x^7$

mupad [B] time = 0.07, size = 78, normalized size = 0.88

$$b^7 \ln(x) - \frac{\frac{a^7}{7} + \frac{7 a^6 b x}{6} + \frac{21 a^5 b^2 x^2}{5} + \frac{35 a^4 b^3 x^3}{4} + \frac{35 a^3 b^4 x^4}{3} + \frac{21 a^2 b^5 x^5}{2} + 7 a b^6 x^6}{x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^8,x)

[Out] $b^7 \log(x) - \frac{(a^7/7 + 7 a^6 b x + (21 a^5 b^2 x^2)/5 + (35 a^4 b^3 x^3)/4 + (35 a^3 b^4 x^4)/3 + (21 a^2 b^5 x^5)/2 + (7 a b^6 x)/6)}{x^7}$

sympy [A] time = 0.63, size = 83, normalized size = 0.93

$$b^7 \log(x) + \frac{-60 a^7 - 490 a^6 b x - 1764 a^5 b^2 x^2 - 3675 a^4 b^3 x^3 - 4900 a^3 b^4 x^4 - 4410 a^2 b^5 x^5 - 2940 a b^6 x^6}{420 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**8,x)

[Out] $b^7 \log(x) + \frac{(-60 a^7 - 490 a^6 b x - 1764 a^5 b^2 x^2 - 3675 a^4 b^3 x^3 - 4900 a^3 b^4 x^4 - 4410 a^2 b^5 x^5 - 2940 a b^6 x^6)}{(420 x^7)}$

$$3.115 \quad \int \frac{(a+bx)^7}{x^9} dx$$

Optimal. Leaf size=17

$$-\frac{(a+bx)^8}{8ax^8}$$

[Out] $-1/8*(b*x+a)^8/a/x^8$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {37}

$$-\frac{(a+bx)^8}{8ax^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^9, x]

[Out] $-(a + b*x)^8/(8*a*x^8)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(a+bx)^7}{x^9} dx = -\frac{(a+bx)^8}{8ax^8}$$

Mathematica [B] time = 0.00, size = 87, normalized size = 5.12

$$-\frac{a^7}{8x^8} - \frac{a^6b}{x^7} - \frac{7a^5b^2}{2x^6} - \frac{7a^4b^3}{x^5} - \frac{35a^3b^4}{4x^4} - \frac{7a^2b^5}{x^3} - \frac{7ab^6}{2x^2} - \frac{b^7}{x}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^9, x]

[Out] $-1/8*a^7/x^8 - (a^6*b)/x^7 - (7*a^5*b^2)/(2*x^6) - (7*a^4*b^3)/x^5 - (35*a^3*b^4)/(4*x^4) - (7*a^2*b^5)/x^3 - (7*a*b^6)/(2*x^2) - b^7/x$

fricas [B] time = 0.43, size = 77, normalized size = 4.53

$$\frac{8b^7x^7 + 28ab^6x^6 + 56a^2b^5x^5 + 70a^3b^4x^4 + 56a^4b^3x^3 + 28a^5b^2x^2 + 8a^6bx + a^7}{8x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^9,x, algorithm="fricas")

[Out] $-1/8*(8*b^7*x^7 + 28*a*b^6*x^6 + 56*a^2*b^5*x^5 + 70*a^3*b^4*x^4 + 56*a^4*b^3*x^3 + 28*a^5*b^2*x^2 + 8*a^6*b*x + a^7)/x^8$

giac [B] time = 0.92, size = 77, normalized size = 4.53

$$\frac{8b^7x^7 + 28ab^6x^6 + 56a^2b^5x^5 + 70a^3b^4x^4 + 56a^4b^3x^3 + 28a^5b^2x^2 + 8a^6bx + a^7}{8x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^9,x, algorithm="giac")

[Out] $-1/8*(8*b^7*x^7 + 28*a*b^6*x^6 + 56*a^2*b^5*x^5 + 70*a^3*b^4*x^4 + 56*a^4*b^3*x^3 + 28*a^5*b^2*x^2 + 8*a^6*b*x + a^7)/x^8$

maple [B] time = 0.00, size = 80, normalized size = 4.71

$$-\frac{b^7}{x} - \frac{7ab^6}{2x^2} - \frac{7a^2b^5}{x^3} - \frac{35a^3b^4}{4x^4} - \frac{7a^4b^3}{x^5} - \frac{7a^5b^2}{2x^6} - \frac{a^6b}{x^7} - \frac{a^7}{8x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^9,x)

[Out] $-7*a^4*b^3/x^5 - 1/8*a^7/x^8 - 7/2*a^5*b^2/x^6 - 35/4*a^3*b^4/x^4 - 7*a^2*b^5/x^3 - b^7/x - a^6*b/x^7 - 7/2*a*b^6/x^2$

maxima [B] time = 1.29, size = 77, normalized size = 4.53

$$\frac{8b^7x^7 + 28ab^6x^6 + 56a^2b^5x^5 + 70a^3b^4x^4 + 56a^4b^3x^3 + 28a^5b^2x^2 + 8a^6bx + a^7}{8x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^9,x, algorithm="maxima")

[Out] $-1/8*(8*b^7*x^7 + 28*a*b^6*x^6 + 56*a^2*b^5*x^5 + 70*a^3*b^4*x^4 + 56*a^4*b^3*x^3 + 28*a^5*b^2*x^2 + 8*a^6*b*x + a^7)/x^8$

mupad [B] time = 0.07, size = 77, normalized size = 4.53

$$\frac{\frac{a^7}{8} + a^6 b x + \frac{7 a^5 b^2 x^2}{2} + 7 a^4 b^3 x^3 + \frac{35 a^3 b^4 x^4}{4} + 7 a^2 b^5 x^5 + \frac{7 a b^6 x^6}{2} + b^7 x^7}{x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^7/x^9, x)`

[Out] $-(a^7/8 + b^7*x^7 + (7*a*b^6*x^6)/2 + (7*a^5*b^2*x^2)/2 + 7*a^4*b^3*x^3 + (35*a^3*b^4*x^4)/4 + 7*a^2*b^5*x^5 + a^6*b*x)/x^8$

sympy [B] time = 0.60, size = 83, normalized size = 4.88

$$\frac{-a^7 - 8a^6bx - 28a^5b^2x^2 - 56a^4b^3x^3 - 70a^3b^4x^4 - 56a^2b^5x^5 - 28ab^6x^6 - 8b^7x^7}{8x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**7/x**9, x)`

[Out] $(-a**7 - 8*a**6*b*x - 28*a**5*b**2*x**2 - 56*a**4*b**3*x**3 - 70*a**3*b**4*x**4 - 56*a**2*b**5*x**5 - 28*a*b**6*x**6 - 8*b**7*x**7)/(8*x**8)$

$$3.116 \quad \int \frac{(a+bx)^7}{x^{10}} dx$$

Optimal. Leaf size=36

$$\frac{b(a+bx)^8}{72a^2x^8} - \frac{(a+bx)^8}{9ax^9}$$

[Out] $-1/9*(b*x+a)^8/a/x^9+1/72*b*(b*x+a)^8/a^2/x^8$

Rubi [A] time = 0.00, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{b(a+bx)^8}{72a^2x^8} - \frac{(a+bx)^8}{9ax^9}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^10, x]

[Out] $-(a + b*x)^8/(9*a*x^9) + (b*(a + b*x)^8)/(72*a^2*x^8)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x^{10}} dx &= -\frac{(a+bx)^8}{9ax^9} - \frac{b \int \frac{(a+bx)^7}{x^9} dx}{9a} \\ &= -\frac{(a+bx)^8}{9ax^9} + \frac{b(a+bx)^8}{72a^2x^8} \end{aligned}$$

Mathematica [B] time = 0.00, size = 91, normalized size = 2.53

$$-\frac{a^7}{9x^9} - \frac{7a^6b}{8x^8} - \frac{3a^5b^2}{x^7} - \frac{35a^4b^3}{6x^6} - \frac{7a^3b^4}{x^5} - \frac{21a^2b^5}{4x^4} - \frac{7ab^6}{3x^3} - \frac{b^7}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^10,x]

[Out] $-1/9*a^7/x^9 - (7*a^6*b)/(8*x^8) - (3*a^5*b^2)/x^7 - (35*a^4*b^3)/(6*x^6) - (7*a^3*b^4)/x^5 - (21*a^2*b^5)/(4*x^4) - (7*a*b^6)/(3*x^3) - b^7/(2*x^2)$

fricas [B] time = 0.46, size = 79, normalized size = 2.19

$$\frac{36b^7x^7 + 168ab^6x^6 + 378a^2b^5x^5 + 504a^3b^4x^4 + 420a^4b^3x^3 + 216a^5b^2x^2 + 63a^6bx + 8a^7}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^10,x, algorithm="fricas")

[Out] $-1/72*(36*b^7*x^7 + 168*a*b^6*x^6 + 378*a^2*b^5*x^5 + 504*a^3*b^4*x^4 + 420*a^4*b^3*x^3 + 216*a^5*b^2*x^2 + 63*a^6*b*x + 8*a^7)/x^9$

giac [B] time = 1.01, size = 79, normalized size = 2.19

$$\frac{36b^7x^7 + 168ab^6x^6 + 378a^2b^5x^5 + 504a^3b^4x^4 + 420a^4b^3x^3 + 216a^5b^2x^2 + 63a^6bx + 8a^7}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^10,x, algorithm="giac")

[Out] $-1/72*(36*b^7*x^7 + 168*a*b^6*x^6 + 378*a^2*b^5*x^5 + 504*a^3*b^4*x^4 + 420*a^4*b^3*x^3 + 216*a^5*b^2*x^2 + 63*a^6*b*x + 8*a^7)/x^9$

maple [B] time = 0.01, size = 80, normalized size = 2.22

$$-\frac{b^7}{2x^2} - \frac{7ab^6}{3x^3} - \frac{21a^2b^5}{4x^4} - \frac{7a^3b^4}{x^5} - \frac{35a^4b^3}{6x^6} - \frac{3a^5b^2}{x^7} - \frac{7a^6b}{8x^8} - \frac{a^7}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^10,x)

[Out] $-7*a^3*b^4/x^5 - 35/6*a^4*b^3/x^6 - 1/2*b^7/x^2 - 7/8*a^6*b/x^8 - 3*a^5*b^2/x^7 - 21/4*a^2*b^5/x^4 - 7/3*a*b^6/x^3 - 1/9*a^7/x^9$

maxima [B] time = 1.31, size = 79, normalized size = 2.19

$$\frac{36 b^7 x^7 + 168 a b^6 x^6 + 378 a^2 b^5 x^5 + 504 a^3 b^4 x^4 + 420 a^4 b^3 x^3 + 216 a^5 b^2 x^2 + 63 a^6 b x + 8 a^7}{72 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^10,x, algorithm="maxima")

[Out] $-1/72*(36*b^7*x^7 + 168*a*b^6*x^6 + 378*a^2*b^5*x^5 + 504*a^3*b^4*x^4 + 420*a^4*b^3*x^3 + 216*a^5*b^2*x^2 + 63*a^6*b*x + 8*a^7)/x^9$

mupad [B] time = 0.09, size = 23, normalized size = 0.64

$$\frac{(8a - bx)(a + bx)^8}{72a^2x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^10,x)

[Out] $-((8*a - b*x)*(a + b*x)^8)/(72*a^2*x^9)$

sympy [B] time = 0.73, size = 85, normalized size = 2.36

$$\frac{-8a^7 - 63a^6bx - 216a^5b^2x^2 - 420a^4b^3x^3 - 504a^3b^4x^4 - 378a^2b^5x^5 - 168ab^6x^6 - 36b^7x^7}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**10,x)

[Out] $(-8*a**7 - 63*a**6*b*x - 216*a**5*b**2*x**2 - 420*a**4*b**3*x**3 - 504*a**3*b**4*x**4 - 378*a**2*b**5*x**5 - 168*a*b**6*x**6 - 36*b**7*x**7)/(72*x**9)$

$$3.117 \quad \int \frac{(a+bx)^7}{x^{11}} dx$$

Optimal. Leaf size=56

$$-\frac{b^2(a+bx)^8}{360a^3x^8} + \frac{b(a+bx)^8}{45a^2x^9} - \frac{(a+bx)^8}{10ax^{10}}$$

[Out] $-1/10*(b*x+a)^8/a/x^{10}+1/45*b*(b*x+a)^8/a^2/x^9-1/360*b^2*(b*x+a)^8/a^3/x^8$

Rubi [A] time = 0.01, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$-\frac{b^2(a+bx)^8}{360a^3x^8} + \frac{b(a+bx)^8}{45a^2x^9} - \frac{(a+bx)^8}{10ax^{10}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^11, x]

[Out] $-(a + b*x)^8/(10*a*x^{10}) + (b*(a + b*x)^8)/(45*a^2*x^9) - (b^2*(a + b*x)^8)/(360*a^3*x^8)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^7}{x^{11}} dx &= -\frac{(a+bx)^8}{10ax^{10}} - \frac{b \int \frac{(a+bx)^7}{x^{10}} dx}{5a} \\
&= -\frac{(a+bx)^8}{10ax^{10}} + \frac{b(a+bx)^8}{45a^2x^9} + \frac{b^2 \int \frac{(a+bx)^7}{x^9} dx}{45a^2} \\
&= -\frac{(a+bx)^8}{10ax^{10}} + \frac{b(a+bx)^8}{45a^2x^9} - \frac{b^2(a+bx)^8}{360a^3x^8}
\end{aligned}$$

Mathematica [A] time = 0.00, size = 93, normalized size = 1.66

$$-\frac{a^7}{10x^{10}} - \frac{7a^6b}{9x^9} - \frac{21a^5b^2}{8x^8} - \frac{5a^4b^3}{x^7} - \frac{35a^3b^4}{6x^6} - \frac{21a^2b^5}{5x^5} - \frac{7ab^6}{4x^4} - \frac{b^7}{3x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^11,x]

[Out] $-1/10*a^7/x^{10} - (7*a^6*b)/(9*x^9) - (21*a^5*b^2)/(8*x^8) - (5*a^4*b^3)/x^7 - (35*a^3*b^4)/(6*x^6) - (21*a^2*b^5)/(5*x^5) - (7*a*b^6)/(4*x^4) - b^7/(3*x^3)$

fricas [A] time = 0.43, size = 79, normalized size = 1.41

$$\frac{120 b^7 x^7 + 630 a b^6 x^6 + 1512 a^2 b^5 x^5 + 2100 a^3 b^4 x^4 + 1800 a^4 b^3 x^3 + 945 a^5 b^2 x^2 + 280 a^6 b x + 36 a^7}{360 x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^11,x, algorithm="fricas")

[Out] $-1/360*(120*b^7*x^7 + 630*a*b^6*x^6 + 1512*a^2*b^5*x^5 + 2100*a^3*b^4*x^4 + 1800*a^4*b^3*x^3 + 945*a^5*b^2*x^2 + 280*a^6*b*x + 36*a^7)/x^{10}$

giac [A] time = 1.06, size = 79, normalized size = 1.41

$$\frac{120 b^7 x^7 + 630 a b^6 x^6 + 1512 a^2 b^5 x^5 + 2100 a^3 b^4 x^4 + 1800 a^4 b^3 x^3 + 945 a^5 b^2 x^2 + 280 a^6 b x + 36 a^7}{360 x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^11,x, algorithm="giac")

[Out] $-1/360*(120*b^7*x^7 + 630*a*b^6*x^6 + 1512*a^2*b^5*x^5 + 2100*a^3*b^4*x^4 + 1800*a^4*b^3*x^3 + 945*a^5*b^2*x^2 + 280*a^6*b*x + 36*a^7)/x^{10}$

maple [A] time = 0.00, size = 80, normalized size = 1.43

$$\frac{b^7}{3x^3} - \frac{7ab^6}{4x^4} - \frac{21a^2b^5}{5x^5} - \frac{35a^3b^4}{6x^6} - \frac{5a^4b^3}{x^7} - \frac{21a^5b^2}{8x^8} - \frac{7a^6b}{9x^9} - \frac{a^7}{10x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^11,x)

[Out] $-21/5*a^2*b^5/x^5 - 21/8*a^5*b^2/x^8 - 35/6*a^3*b^4/x^6 - 1/10*a^7/x^{10} - 5*a^4*b^3/x^7 - 7/4*a*b^6/x^4 - 1/3*b^7/x^3 - 7/9*a^6*b/x^9$

maxima [A] time = 1.38, size = 79, normalized size = 1.41

$$\frac{120b^7x^7 + 630ab^6x^6 + 1512a^2b^5x^5 + 2100a^3b^4x^4 + 1800a^4b^3x^3 + 945a^5b^2x^2 + 280a^6bx + 36a^7}{360x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^11,x, algorithm="maxima")

[Out] $-1/360*(120*b^7*x^7 + 630*a*b^6*x^6 + 1512*a^2*b^5*x^5 + 2100*a^3*b^4*x^4 + 1800*a^4*b^3*x^3 + 945*a^5*b^2*x^2 + 280*a^6*b*x + 36*a^7)/x^{10}$

mupad [B] time = 0.11, size = 79, normalized size = 1.41

$$\frac{\frac{a^7}{10} + \frac{7a^6bx}{9} + \frac{21a^5b^2x^2}{8} + 5a^4b^3x^3 + \frac{35a^3b^4x^4}{6} + \frac{21a^2b^5x^5}{5} + \frac{7a^6bx^6}{4} + \frac{b^7x^7}{3}}{x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^11,x)

[Out] $-(a^7/10 + (b^7*x^7)/3 + (7*a*b^6*x^6)/4 + (21*a^5*b^2*x^2)/8 + 5*a^4*b^3*x^3 + (35*a^3*b^4*x^4)/6 + (21*a^2*b^5*x^5)/5 + (7*a^6*b*x)/9)/x^{10}$

sympy [A] time = 0.76, size = 85, normalized size = 1.52

$$\frac{-36a^7 - 280a^6bx - 945a^5b^2x^2 - 1800a^4b^3x^3 - 2100a^3b^4x^4 - 1512a^2b^5x^5 - 630ab^6x^6 - 120b^7x^7}{360x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**11,x)

[Out] $(-36*a**7 - 280*a**6*b*x - 945*a**5*b**2*x**2 - 1800*a**4*b**3*x**3 - 2100*a**3*b**4*x**4 - 1512*a**2*b**5*x**5 - 630*a*b**6*x**6 - 120*b**7*x**7)/(360*x**10)$

$$3.118 \quad \int \frac{(a+bx)^7}{x^{12}} dx$$

Optimal. Leaf size=76

$$\frac{b^3(a+bx)^8}{1320a^4x^8} - \frac{b^2(a+bx)^8}{165a^3x^9} + \frac{3b(a+bx)^8}{110a^2x^{10}} - \frac{(a+bx)^8}{11ax^{11}}$$

[Out] $-1/11*(b*x+a)^8/a/x^{11}+3/110*b*(b*x+a)^8/a^2/x^{10}-1/165*b^2*(b*x+a)^8/a^3/x^9+1/1320*b^3*(b*x+a)^8/a^4/x^8$

Rubi [A] time = 0.02, antiderivative size = 76, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{b^3(a+bx)^8}{1320a^4x^8} - \frac{b^2(a+bx)^8}{165a^3x^9} + \frac{3b(a+bx)^8}{110a^2x^{10}} - \frac{(a+bx)^8}{11ax^{11}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^12, x]

[Out] $-(a + b*x)^8/(11*a*x^{11}) + (3*b*(a + b*x)^8)/(110*a^2*x^{10}) - (b^2*(a + b*x)^8)/(165*a^3*x^9) + (b^3*(a + b*x)^8)/(1320*a^4*x^8)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^7}{x^{12}} dx &= -\frac{(a+bx)^8}{11ax^{11}} - \frac{(3b) \int \frac{(a+bx)^7}{x^{11}} dx}{11a} \\
&= -\frac{(a+bx)^8}{11ax^{11}} + \frac{3b(a+bx)^8}{110a^2x^{10}} + \frac{(3b^2) \int \frac{(a+bx)^7}{x^{10}} dx}{55a^2} \\
&= -\frac{(a+bx)^8}{11ax^{11}} + \frac{3b(a+bx)^8}{110a^2x^{10}} - \frac{b^2(a+bx)^8}{165a^3x^9} - \frac{b^3 \int \frac{(a+bx)^7}{x^9} dx}{165a^3} \\
&= -\frac{(a+bx)^8}{11ax^{11}} + \frac{3b(a+bx)^8}{110a^2x^{10}} - \frac{b^2(a+bx)^8}{165a^3x^9} + \frac{b^3(a+bx)^8}{1320a^4x^8}
\end{aligned}$$

Mathematica [A] time = 0.00, size = 93, normalized size = 1.22

$$-\frac{a^7}{11x^{11}} - \frac{7a^6b}{10x^{10}} - \frac{7a^5b^2}{3x^9} - \frac{35a^4b^3}{8x^8} - \frac{5a^3b^4}{x^7} - \frac{7a^2b^5}{2x^6} - \frac{7ab^6}{5x^5} - \frac{b^7}{4x^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^12,x]

[Out] -1/11*a^7/x^11 - (7*a^6*b)/(10*x^10) - (7*a^5*b^2)/(3*x^9) - (35*a^4*b^3)/(8*x^8) - (5*a^3*b^4)/x^7 - (7*a^2*b^5)/(2*x^6) - (7*a*b^6)/(5*x^5) - b^7/(4*x^4)

fricas [A] time = 0.46, size = 79, normalized size = 1.04

$$\frac{330 b^7 x^7 + 1848 a b^6 x^6 + 4620 a^2 b^5 x^5 + 6600 a^3 b^4 x^4 + 5775 a^4 b^3 x^3 + 3080 a^5 b^2 x^2 + 924 a^6 b x + 120 a^7}{1320 x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^12,x, algorithm="fricas")

[Out] -1/1320*(330*b^7*x^7 + 1848*a*b^6*x^6 + 4620*a^2*b^5*x^5 + 6600*a^3*b^4*x^4 + 5775*a^4*b^3*x^3 + 3080*a^5*b^2*x^2 + 924*a^6*b*x + 120*a^7)/x^11

giac [A] time = 1.15, size = 79, normalized size = 1.04

$$\frac{330 b^7 x^7 + 1848 a b^6 x^6 + 4620 a^2 b^5 x^5 + 6600 a^3 b^4 x^4 + 5775 a^4 b^3 x^3 + 3080 a^5 b^2 x^2 + 924 a^6 b x + 120 a^7}{1320 x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^12,x, algorithm="giac")

[Out] $-1/1320*(330*b^7*x^7 + 1848*a*b^6*x^6 + 4620*a^2*b^5*x^5 + 6600*a^3*b^4*x^4 + 5775*a^4*b^3*x^3 + 3080*a^5*b^2*x^2 + 924*a^6*b*x + 120*a^7)/x^{11}$

maple [A] time = 0.01, size = 80, normalized size = 1.05

$$\frac{b^7}{4x^4} - \frac{7ab^6}{5x^5} - \frac{7a^2b^5}{2x^6} - \frac{5a^3b^4}{x^7} - \frac{35a^4b^3}{8x^8} - \frac{7a^5b^2}{3x^9} - \frac{7a^6b}{10x^{10}} - \frac{a^7}{11x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^7/x^12,x)`

[Out] $-7/5*a*b^6/x^5 - 7/3*a^5*b^2/x^9 - 5*a^3*b^4/x^7 - 7/2*a^2*b^5/x^6 - 1/4*b^7/x^4 - 7/10*a^6*b/x^{10} - 1/11*a^7/x^{11} - 35/8*a^4*b^3/x^8$

maxima [A] time = 1.36, size = 79, normalized size = 1.04

$$\frac{330b^7x^7 + 1848ab^6x^6 + 4620a^2b^5x^5 + 6600a^3b^4x^4 + 5775a^4b^3x^3 + 3080a^5b^2x^2 + 924a^6bx + 120a^7}{1320x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^7/x^12,x, algorithm="maxima")`

[Out] $-1/1320*(330*b^7*x^7 + 1848*a*b^6*x^6 + 4620*a^2*b^5*x^5 + 6600*a^3*b^4*x^4 + 5775*a^4*b^3*x^3 + 3080*a^5*b^2*x^2 + 924*a^6*b*x + 120*a^7)/x^{11}$

mupad [B] time = 0.11, size = 79, normalized size = 1.04

$$\frac{\frac{a^7}{11} + \frac{7a^6bx}{10} + \frac{7a^5b^2x^2}{3} + \frac{35a^4b^3x^3}{8} + 5a^3b^4x^4 + \frac{7a^2b^5x^5}{2} + \frac{7ab^6x^6}{5} + \frac{b^7x^7}{4}}{x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^7/x^12,x)`

[Out] $-(a^7/11 + (b^7*x^7)/4 + (7*a*b^6*x^6)/5 + (7*a^5*b^2*x^2)/3 + (35*a^4*b^3*x^3)/8 + 5*a^3*b^4*x^4 + (7*a^2*b^5*x^5)/2 + (7*a^6*b*x)/10)/x^{11}$

sympy [A] time = 0.75, size = 85, normalized size = 1.12

$$\frac{-120a^7 - 924a^6bx - 3080a^5b^2x^2 - 5775a^4b^3x^3 - 6600a^3b^4x^4 - 4620a^2b^5x^5 - 1848ab^6x^6 - 330b^7x^7}{1320x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**7/x**12,x)`

[Out] $(-120*a**7 - 924*a**6*b*x - 3080*a**5*b**2*x**2 - 5775*a**4*b**3*x**3 - 6600*a**3*b**4*x**4 - 4620*a**2*b**5*x**5 - 1848*a*b**6*x**6 - 330*b**7*x**7)/(1320*x**11)$

$$3.119 \quad \int \frac{(a+bx)^7}{x^{13}} dx$$

Optimal. Leaf size=96

$$-\frac{b^4(a+bx)^8}{3960a^5x^8} + \frac{b^3(a+bx)^8}{495a^4x^9} - \frac{b^2(a+bx)^8}{110a^3x^{10}} + \frac{b(a+bx)^8}{33a^2x^{11}} - \frac{(a+bx)^8}{12ax^{12}}$$

[Out] $-1/12*(b*x+a)^8/a/x^{12}+1/33*b*(b*x+a)^8/a^2/x^{11}-1/110*b^2*(b*x+a)^8/a^3/x^{10}+1/495*b^3*(b*x+a)^8/a^4/x^9-1/3960*b^4*(b*x+a)^8/a^5/x^8$

Rubi [A] time = 0.03, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$-\frac{b^4(a+bx)^8}{3960a^5x^8} + \frac{b^3(a+bx)^8}{495a^4x^9} - \frac{b^2(a+bx)^8}{110a^3x^{10}} + \frac{b(a+bx)^8}{33a^2x^{11}} - \frac{(a+bx)^8}{12ax^{12}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^13,x]

[Out] $-(a + b*x)^8/(12*a*x^{12}) + (b*(a + b*x)^8)/(33*a^2*x^{11}) - (b^2*(a + b*x)^8)/(110*a^3*x^{10}) + (b^3*(a + b*x)^8)/(495*a^4*x^9) - (b^4*(a + b*x)^8)/(3960*a^5*x^8)$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^7}{x^{13}} dx &= -\frac{(a+bx)^8}{12ax^{12}} - \frac{b \int \frac{(a+bx)^7}{x^{12}} dx}{3a} \\
&= -\frac{(a+bx)^8}{12ax^{12}} + \frac{b(a+bx)^8}{33a^2x^{11}} + \frac{b^2 \int \frac{(a+bx)^7}{x^{11}} dx}{11a^2} \\
&= -\frac{(a+bx)^8}{12ax^{12}} + \frac{b(a+bx)^8}{33a^2x^{11}} - \frac{b^2(a+bx)^8}{110a^3x^{10}} - \frac{b^3 \int \frac{(a+bx)^7}{x^{10}} dx}{55a^3} \\
&= -\frac{(a+bx)^8}{12ax^{12}} + \frac{b(a+bx)^8}{33a^2x^{11}} - \frac{b^2(a+bx)^8}{110a^3x^{10}} + \frac{b^3(a+bx)^8}{495a^4x^9} + \frac{b^4 \int \frac{(a+bx)^7}{x^9} dx}{495a^4} \\
&= -\frac{(a+bx)^8}{12ax^{12}} + \frac{b(a+bx)^8}{33a^2x^{11}} - \frac{b^2(a+bx)^8}{110a^3x^{10}} + \frac{b^3(a+bx)^8}{495a^4x^9} - \frac{b^4(a+bx)^8}{3960a^5x^8}
\end{aligned}$$

Mathematica [A] time = 0.00, size = 93, normalized size = 0.97

$$-\frac{a^7}{12x^{12}} - \frac{7a^6b}{11x^{11}} - \frac{21a^5b^2}{10x^{10}} - \frac{35a^4b^3}{9x^9} - \frac{35a^3b^4}{8x^8} - \frac{3a^2b^5}{x^7} - \frac{7ab^6}{6x^6} - \frac{b^7}{5x^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^13,x]

[Out] $-1/12*a^7/x^{12} - (7*a^6*b)/(11*x^{11}) - (21*a^5*b^2)/(10*x^{10}) - (35*a^4*b^3)/(9*x^9) - (35*a^3*b^4)/(8*x^8) - (3*a^2*b^5)/x^7 - (7*a*b^6)/(6*x^6) - b^7/(5*x^5)$

fricas [A] time = 0.47, size = 79, normalized size = 0.82

$$\frac{792 b^7 x^7 + 4620 a b^6 x^6 + 11880 a^2 b^5 x^5 + 17325 a^3 b^4 x^4 + 15400 a^4 b^3 x^3 + 8316 a^5 b^2 x^2 + 2520 a^6 b x + 330 a^7}{3960 x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^13,x, algorithm="fricas")

[Out] $-1/3960*(792*b^7*x^7 + 4620*a*b^6*x^6 + 11880*a^2*b^5*x^5 + 17325*a^3*b^4*x^4 + 15400*a^4*b^3*x^3 + 8316*a^5*b^2*x^2 + 2520*a^6*b*x + 330*a^7)/x^{12}$

giac [A] time = 1.15, size = 79, normalized size = 0.82

$$\frac{792 b^7 x^7 + 4620 a b^6 x^6 + 11880 a^2 b^5 x^5 + 17325 a^3 b^4 x^4 + 15400 a^4 b^3 x^3 + 8316 a^5 b^2 x^2 + 2520 a^6 b x + 330 a^7}{3960 x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^13,x, algorithm="giac")

[Out] $-1/3960*(792*b^7*x^7 + 4620*a*b^6*x^6 + 11880*a^2*b^5*x^5 + 17325*a^3*b^4*x^4 + 15400*a^4*b^3*x^3 + 8316*a^5*b^2*x^2 + 2520*a^6*b*x + 330*a^7)/x^{12}$

maple [A] time = 0.01, size = 80, normalized size = 0.83

$$-\frac{b^7}{5x^5} - \frac{7ab^6}{6x^6} - \frac{3a^2b^5}{x^7} - \frac{35a^3b^4}{8x^8} - \frac{35a^4b^3}{9x^9} - \frac{21a^5b^2}{10x^{10}} - \frac{7a^6b}{11x^{11}} - \frac{a^7}{12x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^13,x)

[Out] $-1/5*b^7/x^5 - 7/6*a*b^6/x^6 - 35/8*a^2*b^5/x^8 - 7/11*a^3*b^4/x^{11} - 3*a^2*b^5/x^{7-3} - 5/9*a^4*b^3/x^9 - 21/10*a^5*b^2/x^{10} - 1/12*a^7/x^{12}$

maxima [A] time = 1.45, size = 79, normalized size = 0.82

$$\frac{792 b^7 x^7 + 4620 a b^6 x^6 + 11880 a^2 b^5 x^5 + 17325 a^3 b^4 x^4 + 15400 a^4 b^3 x^3 + 8316 a^5 b^2 x^2 + 2520 a^6 b x + 330 a^7}{3960 x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^13,x, algorithm="maxima")

[Out] $-1/3960*(792*b^7*x^7 + 4620*a*b^6*x^6 + 11880*a^2*b^5*x^5 + 17325*a^3*b^4*x^4 + 15400*a^4*b^3*x^3 + 8316*a^5*b^2*x^2 + 2520*a^6*b*x + 330*a^7)/x^{12}$

mupad [B] time = 0.07, size = 79, normalized size = 0.82

$$\frac{\frac{a^7}{12} + \frac{7a^6bx}{11} + \frac{21a^5b^2x^2}{10} + \frac{35a^4b^3x^3}{9} + \frac{35a^3b^4x^4}{8} + 3a^2b^5x^5 + \frac{7ab^6x^6}{6} + \frac{b^7x^7}{5}}{x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^13,x)

[Out] $-(a^7/12 + (b^7*x^7)/5 + (7*a*b^6*x^6)/6 + (21*a^5*b^2*x^2)/10 + (35*a^4*b^3*x^3)/9 + (35*a^3*b^4*x^4)/8 + 3*a^2*b^5*x^5 + (7*a^6*b*x)/11)/x^{12}$

sympy [A] time = 0.80, size = 85, normalized size = 0.89

$$\frac{-330a^7 - 2520a^6bx - 8316a^5b^2x^2 - 15400a^4b^3x^3 - 17325a^3b^4x^4 - 11880a^2b^5x^5 - 4620ab^6x^6 - 792b^7x^7}{3960x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**13,x)

[Out]
$$\frac{-330*a**7 - 2520*a**6*b*x - 8316*a**5*b**2*x**2 - 15400*a**4*b**3*x**3 - 17325*a**3*b**4*x**4 - 11880*a**2*b**5*x**5 - 4620*a*b**6*x**6 - 792*b**7*x**7}{3960*x**12}$$

$$3.120 \quad \int \frac{(a+bx)^7}{x^{14}} dx$$

Optimal. Leaf size=93

$$-\frac{a^7}{13x^{13}} - \frac{7a^6b}{12x^{12}} - \frac{21a^5b^2}{11x^{11}} - \frac{7a^4b^3}{2x^{10}} - \frac{35a^3b^4}{9x^9} - \frac{21a^2b^5}{8x^8} - \frac{ab^6}{x^7} - \frac{b^7}{6x^6}$$

[Out] $-1/13*a^7/x^{13}-7/12*a^6*b/x^{12}-21/11*a^5*b^2/x^{11}-7/2*a^4*b^3/x^{10}-35/9*a^3*b^4/x^9-21/8*a^2*b^5/x^8-a*b^6/x^7-1/6*b^7/x^6$

Rubi [A] time = 0.03, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{21a^5b^2}{11x^{11}} - \frac{7a^4b^3}{2x^{10}} - \frac{35a^3b^4}{9x^9} - \frac{21a^2b^5}{8x^8} - \frac{7a^6b}{12x^{12}} - \frac{a^7}{13x^{13}} - \frac{ab^6}{x^7} - \frac{b^7}{6x^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^14,x]

[Out] $-a^7/(13*x^{13}) - (7*a^6*b)/(12*x^{12}) - (21*a^5*b^2)/(11*x^{11}) - (7*a^4*b^3)/(2*x^{10}) - (35*a^3*b^4)/(9*x^9) - (21*a^2*b^5)/(8*x^8) - (a*b^6)/x^7 - b^7/(6*x^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x^{14}} dx &= \int \left(\frac{a^7}{x^{14}} + \frac{7a^6b}{x^{13}} + \frac{21a^5b^2}{x^{12}} + \frac{35a^4b^3}{x^{11}} + \frac{35a^3b^4}{x^{10}} + \frac{21a^2b^5}{x^9} + \frac{7ab^6}{x^8} + \frac{b^7}{x^7} \right) dx \\ &= -\frac{a^7}{13x^{13}} - \frac{7a^6b}{12x^{12}} - \frac{21a^5b^2}{11x^{11}} - \frac{7a^4b^3}{2x^{10}} - \frac{35a^3b^4}{9x^9} - \frac{21a^2b^5}{8x^8} - \frac{ab^6}{x^7} - \frac{b^7}{6x^6} \end{aligned}$$

Mathematica [A] time = 0.01, size = 93, normalized size = 1.00

$$-\frac{a^7}{13x^{13}} - \frac{7a^6b}{12x^{12}} - \frac{21a^5b^2}{11x^{11}} - \frac{7a^4b^3}{2x^{10}} - \frac{35a^3b^4}{9x^9} - \frac{21a^2b^5}{8x^8} - \frac{ab^6}{x^7} - \frac{b^7}{6x^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^14,x]

[Out]
$$-1/13*a^7/x^{13} - (7*a^6*b)/(12*x^{12}) - (21*a^5*b^2)/(11*x^{11}) - (7*a^4*b^3)/(2*x^{10}) - (35*a^3*b^4)/(9*x^9) - (21*a^2*b^5)/(8*x^8) - (a*b^6)/x^7 - b^7/(6*x^6)$$

fricas [A] time = 0.42, size = 79, normalized size = 0.85

$$\frac{1716 b^7 x^7 + 10296 a b^6 x^6 + 27027 a^2 b^5 x^5 + 40040 a^3 b^4 x^4 + 36036 a^4 b^3 x^3 + 19656 a^5 b^2 x^2 + 6006 a^6 b x + 792 a^7}{10296 x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^14,x, algorithm="fricas")

[Out]
$$-1/10296*(1716*b^7*x^7 + 10296*a*b^6*x^6 + 27027*a^2*b^5*x^5 + 40040*a^3*b^4*x^4 + 36036*a^4*b^3*x^3 + 19656*a^5*b^2*x^2 + 6006*a^6*b*x + 792*a^7)/x^{13}$$

giac [A] time = 1.04, size = 79, normalized size = 0.85

$$\frac{1716 b^7 x^7 + 10296 a b^6 x^6 + 27027 a^2 b^5 x^5 + 40040 a^3 b^4 x^4 + 36036 a^4 b^3 x^3 + 19656 a^5 b^2 x^2 + 6006 a^6 b x + 792 a^7}{10296 x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^14,x, algorithm="giac")

[Out]
$$-1/10296*(1716*b^7*x^7 + 10296*a*b^6*x^6 + 27027*a^2*b^5*x^5 + 40040*a^3*b^4*x^4 + 36036*a^4*b^3*x^3 + 19656*a^5*b^2*x^2 + 6006*a^6*b*x + 792*a^7)/x^{13}$$

maple [A] time = 0.00, size = 80, normalized size = 0.86

$$\frac{b^7}{6x^6} - \frac{ab^6}{x^7} - \frac{21a^2b^5}{8x^8} - \frac{35a^3b^4}{9x^9} - \frac{7a^4b^3}{2x^{10}} - \frac{21a^5b^2}{11x^{11}} - \frac{7a^6b}{12x^{12}} - \frac{a^7}{13x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^14,x)

[Out]
$$-1/13*a^7/x^{13} - 7/12*a^6*b/x^{12} - 21/11*a^5*b^2/x^{11} - 7/2*a^4*b^3/x^{10} - 35/9*a^3*b^4/x^9 - 21/8*a^2*b^5/x^8 - a*b^6/x^7 - 1/6*b^7/x^6$$

maxima [A] time = 1.37, size = 79, normalized size = 0.85

$$\frac{1716 b^7 x^7 + 10296 a b^6 x^6 + 27027 a^2 b^5 x^5 + 40040 a^3 b^4 x^4 + 36036 a^4 b^3 x^3 + 19656 a^5 b^2 x^2 + 6006 a^6 b x + 792 a^7}{10296 x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^14,x, algorithm="maxima")

[Out]
$$-1/10296*(1716*b^7*x^7 + 10296*a*b^6*x^6 + 27027*a^2*b^5*x^5 + 40040*a^3*b^4*x^4 + 36036*a^4*b^3*x^3 + 19656*a^5*b^2*x^2 + 6006*a^6*b*x + 792*a^7)/x^13$$

mupad [B] time = 0.07, size = 78, normalized size = 0.84

$$\frac{\frac{a^7}{13} + \frac{7a^6bx}{12} + \frac{21a^5b^2x^2}{11} + \frac{7a^4b^3x^3}{2} + \frac{35a^3b^4x^4}{9} + \frac{21a^2b^5x^5}{8} + ab^6x^6 + \frac{b^7x^7}{6}}{x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^14,x)

[Out]
$$-(a^7/13 + (b^7*x^7)/6 + a*b^6*x^6 + (21*a^5*b^2*x^2)/11 + (7*a^4*b^3*x^3)/2 + (35*a^3*b^4*x^4)/9 + (21*a^2*b^5*x^5)/8 + (7*a^6*b*x)/12)/x^{13}$$

sympy [A] time = 0.78, size = 85, normalized size = 0.91

$$\frac{-792a^7 - 6006a^6bx - 19656a^5b^2x^2 - 36036a^4b^3x^3 - 40040a^3b^4x^4 - 27027a^2b^5x^5 - 10296ab^6x^6 - 1716b^7x^7}{10296x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**14,x)

[Out]
$$(-792*a**7 - 6006*a**6*b*x - 19656*a**5*b**2*x**2 - 36036*a**4*b**3*x**3 - 40040*a**3*b**4*x**4 - 27027*a**2*b**5*x**5 - 10296*a*b**6*x**6 - 1716*b**7*x**7)/(10296*x**13)$$

$$3.121 \quad \int \frac{(a+bx)^7}{x^{15}} dx$$

Optimal. Leaf size=95

$$-\frac{a^7}{14x^{14}} - \frac{7a^6b}{13x^{13}} - \frac{7a^5b^2}{4x^{12}} - \frac{35a^4b^3}{11x^{11}} - \frac{7a^3b^4}{2x^{10}} - \frac{7a^2b^5}{3x^9} - \frac{7ab^6}{8x^8} - \frac{b^7}{7x^7}$$

[Out] $-1/14*a^7/x^{14}-7/13*a^6*b/x^{13}-7/4*a^5*b^2/x^{12}-35/11*a^4*b^3/x^{11}-7/2*a^3*b^4/x^{10}-7/3*a^2*b^5/x^9-7/8*a*b^6/x^8-1/7*b^7/x^7$

Rubi [A] time = 0.03, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{7a^5b^2}{4x^{12}} - \frac{35a^4b^3}{11x^{11}} - \frac{7a^3b^4}{2x^{10}} - \frac{7a^2b^5}{3x^9} - \frac{7a^6b}{13x^{13}} - \frac{a^7}{14x^{14}} - \frac{7ab^6}{8x^8} - \frac{b^7}{7x^7}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^15,x]

[Out] $-a^7/(14*x^{14}) - (7*a^6*b)/(13*x^{13}) - (7*a^5*b^2)/(4*x^{12}) - (35*a^4*b^3)/(11*x^{11}) - (7*a^3*b^4)/(2*x^{10}) - (7*a^2*b^5)/(3*x^9) - (7*a*b^6)/(8*x^8) - b^7/(7*x^7)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x^{15}} dx &= \int \left(\frac{a^7}{x^{15}} + \frac{7a^6b}{x^{14}} + \frac{21a^5b^2}{x^{13}} + \frac{35a^4b^3}{x^{12}} + \frac{35a^3b^4}{x^{11}} + \frac{21a^2b^5}{x^{10}} + \frac{7ab^6}{x^9} + \frac{b^7}{x^8} \right) dx \\ &= -\frac{a^7}{14x^{14}} - \frac{7a^6b}{13x^{13}} - \frac{7a^5b^2}{4x^{12}} - \frac{35a^4b^3}{11x^{11}} - \frac{7a^3b^4}{2x^{10}} - \frac{7a^2b^5}{3x^9} - \frac{7ab^6}{8x^8} - \frac{b^7}{7x^7} \end{aligned}$$

Mathematica [A] time = 0.00, size = 95, normalized size = 1.00

$$-\frac{a^7}{14x^{14}} - \frac{7a^6b}{13x^{13}} - \frac{7a^5b^2}{4x^{12}} - \frac{35a^4b^3}{11x^{11}} - \frac{7a^3b^4}{2x^{10}} - \frac{7a^2b^5}{3x^9} - \frac{7ab^6}{8x^8} - \frac{b^7}{7x^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^15,x]

[Out] $-1/14*a^7/x^{14} - (7*a^6*b)/(13*x^{13}) - (7*a^5*b^2)/(4*x^{12}) - (35*a^4*b^3)/(11*x^{11}) - (7*a^3*b^4)/(2*x^{10}) - (7*a^2*b^5)/(3*x^9) - (7*a*b^6)/(8*x^8) - b^7/(7*x^7)$

fricas [A] time = 0.45, size = 79, normalized size = 0.83

$$\frac{3432 b^7 x^7 + 21021 a b^6 x^6 + 56056 a^2 b^5 x^5 + 84084 a^3 b^4 x^4 + 76440 a^4 b^3 x^3 + 42042 a^5 b^2 x^2 + 12936 a^6 b x + 1716 a^7}{24024 x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^15,x, algorithm="fricas")

[Out] $-1/24024*(3432*b^7*x^7 + 21021*a*b^6*x^6 + 56056*a^2*b^5*x^5 + 84084*a^3*b^4*x^4 + 76440*a^4*b^3*x^3 + 42042*a^5*b^2*x^2 + 12936*a^6*b*x + 1716*a^7)/x^{14}$

giac [A] time = 0.89, size = 79, normalized size = 0.83

$$\frac{3432 b^7 x^7 + 21021 a b^6 x^6 + 56056 a^2 b^5 x^5 + 84084 a^3 b^4 x^4 + 76440 a^4 b^3 x^3 + 42042 a^5 b^2 x^2 + 12936 a^6 b x + 1716 a^7}{24024 x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^15,x, algorithm="giac")

[Out] $-1/24024*(3432*b^7*x^7 + 21021*a*b^6*x^6 + 56056*a^2*b^5*x^5 + 84084*a^3*b^4*x^4 + 76440*a^4*b^3*x^3 + 42042*a^5*b^2*x^2 + 12936*a^6*b*x + 1716*a^7)/x^{14}$

maple [A] time = 0.01, size = 80, normalized size = 0.84

$$\frac{b^7}{7x^7} - \frac{7ab^6}{8x^8} - \frac{7a^2b^5}{3x^9} - \frac{7a^3b^4}{2x^{10}} - \frac{35a^4b^3}{11x^{11}} - \frac{7a^5b^2}{4x^{12}} - \frac{7a^6b}{13x^{13}} - \frac{a^7}{14x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^15,x)

[Out] $-1/14*a^7/x^{14} - 7/13*a^6*b/x^{13} - 7/4*a^5*b^2/x^{12} - 35/11*a^4*b^3/x^{11} - 7/2*a^3*b^4/x^{10} - 7/3*a^2*b^5/x^9 - 7/8*a*b^6/x^8 - 1/7*b^7/x^7$

maxima [A] time = 1.34, size = 79, normalized size = 0.83

$$\frac{3432 b^7 x^7 + 21021 a b^6 x^6 + 56056 a^2 b^5 x^5 + 84084 a^3 b^4 x^4 + 76440 a^4 b^3 x^3 + 42042 a^5 b^2 x^2 + 12936 a^6 b x + 1716 a^7}{24024 x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^15,x, algorithm="maxima")

[Out]
$$-1/24024*(3432*b^7*x^7 + 21021*a*b^6*x^6 + 56056*a^2*b^5*x^5 + 84084*a^3*b^4*x^4 + 76440*a^4*b^3*x^3 + 42042*a^5*b^2*x^2 + 12936*a^6*b*x + 1716*a^7)/x^{14}$$

mupad [B] time = 0.07, size = 79, normalized size = 0.83

$$\frac{\frac{a^7}{14} + \frac{7a^6bx}{13} + \frac{7a^5b^2x^2}{4} + \frac{35a^4b^3x^3}{11} + \frac{7a^3b^4x^4}{2} + \frac{7a^2b^5x^5}{3} + \frac{7ab^6x^6}{8} + \frac{b^7x^7}{7}}{x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^15,x)

[Out]
$$-(a^7/14 + (b^7*x^7)/7 + (7*a*b^6*x^6)/8 + (7*a^5*b^2*x^2)/4 + (35*a^4*b^3*x^3)/11 + (7*a^3*b^4*x^4)/2 + (7*a^2*b^5*x^5)/3 + (7*a^6*b*x)/13)/x^{14}$$

sympy [A] time = 0.88, size = 85, normalized size = 0.89

$$\frac{-1716a^7 - 12936a^6bx - 42042a^5b^2x^2 - 76440a^4b^3x^3 - 84084a^3b^4x^4 - 56056a^2b^5x^5 - 21021ab^6x^6 - 3432b^7x^7}{24024x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**15,x)

[Out]
$$(-1716*a**7 - 12936*a**6*b*x - 42042*a**5*b**2*x**2 - 76440*a**4*b**3*x**3 - 84084*a**3*b**4*x**4 - 56056*a**2*b**5*x**5 - 21021*a*b**6*x**6 - 3432*b**7*x**7)/(24024*x**14)$$

$$3.122 \quad \int \frac{(a+bx)^7}{x^{16}} dx$$

Optimal. Leaf size=95

$$-\frac{a^7}{15x^{15}} - \frac{a^6b}{2x^{14}} - \frac{21a^5b^2}{13x^{13}} - \frac{35a^4b^3}{12x^{12}} - \frac{35a^3b^4}{11x^{11}} - \frac{21a^2b^5}{10x^{10}} - \frac{7ab^6}{9x^9} - \frac{b^7}{8x^8}$$

[Out] $-1/15*a^7/x^{15}-1/2*a^6*b/x^{14}-21/13*a^5*b^2/x^{13}-35/12*a^4*b^3/x^{12}-35/11*a^3*b^4/x^{11}-21/10*a^2*b^5/x^{10}-7/9*a*b^6/x^9-1/8*b^7/x^8$

Rubi [A] time = 0.03, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{21a^5b^2}{13x^{13}} - \frac{35a^4b^3}{12x^{12}} - \frac{35a^3b^4}{11x^{11}} - \frac{21a^2b^5}{10x^{10}} - \frac{a^6b}{2x^{14}} - \frac{a^7}{15x^{15}} - \frac{7ab^6}{9x^9} - \frac{b^7}{8x^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^16,x]

[Out] $-a^7/(15*x^{15}) - (a^6*b)/(2*x^{14}) - (21*a^5*b^2)/(13*x^{13}) - (35*a^4*b^3)/(12*x^{12}) - (35*a^3*b^4)/(11*x^{11}) - (21*a^2*b^5)/(10*x^{10}) - (7*a*b^6)/(9*x^9) - b^7/(8*x^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^7}{x^{16}} dx = \int \left(\frac{a^7}{x^{16}} + \frac{7a^6b}{x^{15}} + \frac{21a^5b^2}{x^{14}} + \frac{35a^4b^3}{x^{13}} + \frac{35a^3b^4}{x^{12}} + \frac{21a^2b^5}{x^{11}} + \frac{7ab^6}{x^{10}} + \frac{b^7}{x^9} \right) dx$$

$$= -\frac{a^7}{15x^{15}} - \frac{a^6b}{2x^{14}} - \frac{21a^5b^2}{13x^{13}} - \frac{35a^4b^3}{12x^{12}} - \frac{35a^3b^4}{11x^{11}} - \frac{21a^2b^5}{10x^{10}} - \frac{7ab^6}{9x^9} - \frac{b^7}{8x^8}$$

Mathematica [A] time = 0.00, size = 95, normalized size = 1.00

$$-\frac{a^7}{15x^{15}} - \frac{a^6b}{2x^{14}} - \frac{21a^5b^2}{13x^{13}} - \frac{35a^4b^3}{12x^{12}} - \frac{35a^3b^4}{11x^{11}} - \frac{21a^2b^5}{10x^{10}} - \frac{7ab^6}{9x^9} - \frac{b^7}{8x^8}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^16,x]

[Out] $-1/15*a^7/x^{15} - (a^6*b)/(2*x^{14}) - (21*a^5*b^2)/(13*x^{13}) - (35*a^4*b^3)/(12*x^{12}) - (35*a^3*b^4)/(11*x^{11}) - (21*a^2*b^5)/(10*x^{10}) - (7*a*b^6)/(9*x^9) - b^7/(8*x^8)$

fricas [A] time = 0.43, size = 79, normalized size = 0.83

$$\frac{6435 b^7 x^7 + 40040 a b^6 x^6 + 108108 a^2 b^5 x^5 + 163800 a^3 b^4 x^4 + 150150 a^4 b^3 x^3 + 83160 a^5 b^2 x^2 + 25740 a^6 b x + 3432 a^7}{51480 x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^16,x, algorithm="fricas")

[Out] $-1/51480*(6435*b^7*x^7 + 40040*a*b^6*x^6 + 108108*a^2*b^5*x^5 + 163800*a^3*b^4*x^4 + 150150*a^4*b^3*x^3 + 83160*a^5*b^2*x^2 + 25740*a^6*b*x + 3432*a^7)/x^{15}$

giac [A] time = 1.00, size = 79, normalized size = 0.83

$$\frac{6435 b^7 x^7 + 40040 a b^6 x^6 + 108108 a^2 b^5 x^5 + 163800 a^3 b^4 x^4 + 150150 a^4 b^3 x^3 + 83160 a^5 b^2 x^2 + 25740 a^6 b x + 3432 a^7}{51480 x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^16,x, algorithm="giac")

[Out] $-1/51480*(6435*b^7*x^7 + 40040*a*b^6*x^6 + 108108*a^2*b^5*x^5 + 163800*a^3*b^4*x^4 + 150150*a^4*b^3*x^3 + 83160*a^5*b^2*x^2 + 25740*a^6*b*x + 3432*a^7)/x^{15}$

maple [A] time = 0.00, size = 80, normalized size = 0.84

$$-\frac{b^7}{8x^8} - \frac{7ab^6}{9x^9} - \frac{21a^2b^5}{10x^{10}} - \frac{35a^3b^4}{11x^{11}} - \frac{35a^4b^3}{12x^{12}} - \frac{21a^5b^2}{13x^{13}} - \frac{a^6b}{2x^{14}} - \frac{a^7}{15x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^16,x)

[Out] $-1/15*a^7/x^{15} - 1/2*a^6*b/x^{14} - 21/13*a^5*b^2/x^{13} - 35/12*a^4*b^3/x^{12} - 35/11*a^3*b^4/x^{11} - 21/10*a^2*b^5/x^{10} - 7/9*a*b^6/x^9 - 1/8*b^7/x^8$

maxima [A] time = 1.39, size = 79, normalized size = 0.83

$$\frac{6435 b^7 x^7 + 40040 a b^6 x^6 + 108108 a^2 b^5 x^5 + 163800 a^3 b^4 x^4 + 150150 a^4 b^3 x^3 + 83160 a^5 b^2 x^2 + 25740 a^6 b x + 3432 a^7}{51480 x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^16,x, algorithm="maxima")

[Out] -1/51480*(6435*b^7*x^7 + 40040*a*b^6*x^6 + 108108*a^2*b^5*x^5 + 163800*a^3*b^4*x^4 + 150150*a^4*b^3*x^3 + 83160*a^5*b^2*x^2 + 25740*a^6*b*x + 3432*a^7)/x^15

mupad [B] time = 0.11, size = 79, normalized size = 0.83

$$\frac{\frac{a^7}{15} + \frac{a^6 b x}{2} + \frac{21 a^5 b^2 x^2}{13} + \frac{35 a^4 b^3 x^3}{12} + \frac{35 a^3 b^4 x^4}{11} + \frac{21 a^2 b^5 x^5}{10} + \frac{7 a b^6 x^6}{9} + \frac{b^7 x^7}{8}}{x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^16,x)

[Out] -(a^7/15 + (b^7*x^7)/8 + (7*a*b^6*x^6)/9 + (21*a^5*b^2*x^2)/13 + (35*a^4*b^3*x^3)/12 + (35*a^3*b^4*x^4)/11 + (21*a^2*b^5*x^5)/10 + (a^6*b*x)/2)/x^15

sympy [A] time = 0.88, size = 85, normalized size = 0.89

$$\frac{-3432a^7 - 25740a^6bx - 83160a^5b^2x^2 - 150150a^4b^3x^3 - 163800a^3b^4x^4 - 108108a^2b^5x^5 - 40040ab^6x^6 - 6435b^7x^7}{51480x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**16,x)

[Out] (-3432*a**7 - 25740*a**6*b*x - 83160*a**5*b**2*x**2 - 150150*a**4*b**3*x**3 - 163800*a**3*b**4*x**4 - 108108*a**2*b**5*x**5 - 40040*a*b**6*x**6 - 6435*b**7*x**7)/(51480*x**15)

3.123 $\int x^{11}(a + bx)^{10} dx$

Optimal. Leaf size=132

$$\frac{a^{10}x^{12}}{12} + \frac{10}{13}a^9bx^{13} + \frac{45}{14}a^8b^2x^{14} + 8a^7b^3x^{15} + \frac{105}{8}a^6b^4x^{16} + \frac{252}{17}a^5b^5x^{17} + \frac{35}{3}a^4b^6x^{18} + \frac{120}{19}a^3b^7x^{19} + \frac{9}{4}a^2b^8x^{20} + \frac{10}{21}ab^9x^{21} + \frac{1}{22}b^{10}x^{22}$$

[Out] 1/12*a^10*x^12+10/13*a^9*b*x^13+45/14*a^8*b^2*x^14+8*a^7*b^3*x^15+105/8*a^6*b^4*x^16+252/17*a^5*b^5*x^17+35/3*a^4*b^6*x^18+120/19*a^3*b^7*x^19+9/4*a^2*b^8*x^20+10/21*a*b^9*x^21+1/22*b^10*x^22

Rubi [A] time = 0.08, antiderivative size = 132, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{9}{4}a^2b^8x^{20} + \frac{120}{19}a^3b^7x^{19} + \frac{35}{3}a^4b^6x^{18} + \frac{252}{17}a^5b^5x^{17} + \frac{105}{8}a^6b^4x^{16} + 8a^7b^3x^{15} + \frac{45}{14}a^8b^2x^{14} + \frac{10}{13}a^9bx^{13} + \frac{a^{10}x^{12}}{12} + \frac{10}{21}ab^9x^{21} + \frac{1}{22}b^{10}x^{22}$$

Antiderivative was successfully verified.

[In] Int[x^11*(a + b*x)^10,x]

[Out] (a^10*x^12)/12 + (10*a^9*b*x^13)/13 + (45*a^8*b^2*x^14)/14 + 8*a^7*b^3*x^15 + (105*a^6*b^4*x^16)/8 + (252*a^5*b^5*x^17)/17 + (35*a^4*b^6*x^18)/3 + (120*a^3*b^7*x^19)/19 + (9*a^2*b^8*x^20)/4 + (10*a*b^9*x^21)/21 + (b^10*x^22)/22

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int x^{11}(a + bx)^{10} dx = \int (a^{10}x^{11} + 10a^9bx^{12} + 45a^8b^2x^{13} + 120a^7b^3x^{14} + 210a^6b^4x^{15} + 252a^5b^5x^{16} + 210a^4b^6x^{17} + 105a^3b^7x^{18} + 35a^2b^8x^{19} + 10ab^9x^{20} + b^{10}x^{21}) dx$$

$$= \frac{a^{10}x^{12}}{12} + \frac{10}{13}a^9bx^{13} + \frac{45}{14}a^8b^2x^{14} + 8a^7b^3x^{15} + \frac{105}{8}a^6b^4x^{16} + \frac{252}{17}a^5b^5x^{17} + \frac{35}{3}a^4b^6x^{18} + \frac{120}{19}a^3b^7x^{19} + \frac{9}{4}a^2b^8x^{20} + \frac{10}{21}ab^9x^{21} + \frac{1}{22}b^{10}x^{22}$$

Mathematica [A] time = 0.00, size = 132, normalized size = 1.00

$$\frac{a^{10}x^{12}}{12} + \frac{10}{13}a^9bx^{13} + \frac{45}{14}a^8b^2x^{14} + 8a^7b^3x^{15} + \frac{105}{8}a^6b^4x^{16} + \frac{252}{17}a^5b^5x^{17} + \frac{35}{3}a^4b^6x^{18} + \frac{120}{19}a^3b^7x^{19} + \frac{9}{4}a^2b^8x^{20} + \frac{10}{21}ab^9x^{21} + \frac{1}{22}b^{10}x^{22}$$

Antiderivative was successfully verified.

[In] Integrate[x¹¹*(a + b*x)¹⁰,x]

[Out] (a¹⁰*x¹²)/12 + (10*a⁹*b*x¹³)/13 + (45*a⁸*b²*x¹⁴)/14 + 8*a⁷*b³*x¹⁵ + (105*a⁶*b⁴*x¹⁶)/8 + (252*a⁵*b⁵*x¹⁷)/17 + (35*a⁴*b⁶*x¹⁸)/3 + (120*a³*b⁷*x¹⁹)/19 + (9*a²*b⁸*x²⁰)/4 + (10*a*b⁹*x²¹)/21 + (b¹⁰*x²²)/22

fricas [A] time = 0.41, size = 112, normalized size = 0.85

$$\frac{1}{22}x^{22}b^{10} + \frac{10}{21}x^{21}b^9a + \frac{9}{4}x^{20}b^8a^2 + \frac{120}{19}x^{19}b^7a^3 + \frac{35}{3}x^{18}b^6a^4 + \frac{252}{17}x^{17}b^5a^5 + \frac{105}{8}x^{16}b^4a^6 + 8x^{15}b^3a^7 + \frac{45}{14}x^{14}b^2a^8 + \frac{10}{13}x^{13}b^1a^9 + \frac{1}{12}x^{12}a^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x¹¹*(b*x+a)¹⁰,x, algorithm="fricas")

[Out] 1/22*x²²*b¹⁰ + 10/21*x²¹*b⁹*a + 9/4*x²⁰*b⁸*a² + 120/19*x¹⁹*b⁷*a³ + 35/3*x¹⁸*b⁶*a⁴ + 252/17*x¹⁷*b⁵*a⁵ + 105/8*x¹⁶*b⁴*a⁶ + 8*x¹⁵*b³*a⁷ + 45/14*x¹⁴*b²*a⁸ + 10/13*x¹³*b*a⁹ + 1/12*x¹²*a¹⁰

giac [A] time = 0.98, size = 112, normalized size = 0.85

$$\frac{1}{22}b^{10}x^{22} + \frac{10}{21}ab^9x^{21} + \frac{9}{4}a^2b^8x^{20} + \frac{120}{19}a^3b^7x^{19} + \frac{35}{3}a^4b^6x^{18} + \frac{252}{17}a^5b^5x^{17} + \frac{105}{8}a^6b^4x^{16} + 8a^7b^3x^{15} + \frac{45}{14}a^8b^2x^{14} + \frac{10}{13}a^9b^1x^{13} + \frac{1}{12}a^{10}x^{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x¹¹*(b*x+a)¹⁰,x, algorithm="giac")

[Out] 1/22*b¹⁰*x²² + 10/21*a*b⁹*x²¹ + 9/4*a²*b⁸*x²⁰ + 120/19*a³*b⁷*x¹⁹ + 35/3*a⁴*b⁶*x¹⁸ + 252/17*a⁵*b⁵*x¹⁷ + 105/8*a⁶*b⁴*x¹⁶ + 8*a⁷*b³*x¹⁵ + 45/14*a⁸*b²*x¹⁴ + 10/13*a⁹*b*x¹³ + 1/12*a¹⁰*x¹²

maple [A] time = 0.00, size = 113, normalized size = 0.86

$$\frac{1}{22}b^{10}x^{22} + \frac{10}{21}ab^9x^{21} + \frac{9}{4}a^2b^8x^{20} + \frac{120}{19}a^3b^7x^{19} + \frac{35}{3}a^4b^6x^{18} + \frac{252}{17}a^5b^5x^{17} + \frac{105}{8}a^6b^4x^{16} + 8a^7b^3x^{15} + \frac{45}{14}a^8b^2x^{14} + \frac{10}{13}a^9b^1x^{13} + \frac{1}{12}a^{10}x^{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x¹¹*(b*x+a)¹⁰,x)

[Out] 1/12*a¹⁰*x¹²+10/13*a⁹*b*x¹³+45/14*a⁸*b²*x¹⁴+8*a⁷*b³*x¹⁵+105/8*a⁶*b⁴*x¹⁶+252/17*a⁵*b⁵*x¹⁷+35/3*a⁴*b⁶*x¹⁸+120/19*a³*b⁷*x¹⁹+9/4*a²*b⁸*x²⁰+10/21*a*b⁹*x²¹+1/22*b¹⁰*x²²

maxima [A] time = 1.33, size = 112, normalized size = 0.85

$$\frac{1}{22} b^{10} x^{22} + \frac{10}{21} a b^9 x^{21} + \frac{9}{4} a^2 b^8 x^{20} + \frac{120}{19} a^3 b^7 x^{19} + \frac{35}{3} a^4 b^6 x^{18} + \frac{252}{17} a^5 b^5 x^{17} + \frac{105}{8} a^6 b^4 x^{16} + 8 a^7 b^3 x^{15} + \frac{45}{14} a^8 b^2 x^{14} +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x¹¹*(b*x+a)¹⁰,x, algorithm="maxima")

[Out] 1/22*b¹⁰*x²² + 10/21*a*b⁹*x²¹ + 9/4*a²*b⁸*x²⁰ + 120/19*a³*b⁷*x¹⁹ + 35/3*a⁴*b⁶*x¹⁸ + 252/17*a⁵*b⁵*x¹⁷ + 105/8*a⁶*b⁴*x¹⁶ + 8*a⁷*b³*x¹⁵ + 45/14*a⁸*b²*x¹⁴ + 10/13*a⁹*b*x¹³ + 1/12*a¹⁰*x¹²

mupad [B] time = 0.15, size = 112, normalized size = 0.85

$$\frac{a^{10} x^{12}}{12} + \frac{10 a^9 b x^{13}}{13} + \frac{45 a^8 b^2 x^{14}}{14} + 8 a^7 b^3 x^{15} + \frac{105 a^6 b^4 x^{16}}{8} + \frac{252 a^5 b^5 x^{17}}{17} + \frac{35 a^4 b^6 x^{18}}{3} + \frac{120 a^3 b^7 x^{19}}{19} + \frac{9 a^2 b^8 x^{20}}{4} +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x¹¹*(a + b*x)¹⁰,x)

[Out] (a¹⁰*x¹²)/12 + (b¹⁰*x²²)/22 + (10*a⁹*b*x¹³)/13 + (10*a*b⁹*x²¹)/21 + (45*a⁸*b²*x¹⁴)/14 + 8*a⁷*b³*x¹⁵ + (105*a⁶*b⁴*x¹⁶)/8 + (252*a⁵*b⁵*x¹⁷)/17 + (35*a⁴*b⁶*x¹⁸)/3 + (120*a³*b⁷*x¹⁹)/19 + (9*a²*b⁸*x²⁰)/4

sympy [A] time = 0.11, size = 133, normalized size = 1.01

$$\frac{a^{10} x^{12}}{12} + \frac{10 a^9 b x^{13}}{13} + \frac{45 a^8 b^2 x^{14}}{14} + 8 a^7 b^3 x^{15} + \frac{105 a^6 b^4 x^{16}}{8} + \frac{252 a^5 b^5 x^{17}}{17} + \frac{35 a^4 b^6 x^{18}}{3} + \frac{120 a^3 b^7 x^{19}}{19} + \frac{9 a^2 b^8 x^{20}}{4} + \frac{10 a b^9 x^{21}}{21} +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**11*(b*x+a)**10,x)

[Out] a**10*x**12/12 + 10*a**9*b*x**13/13 + 45*a**8*b**2*x**14/14 + 8*a**7*b**3*x**15 + 105*a**6*b**4*x**16/8 + 252*a**5*b**5*x**17/17 + 35*a**4*b**6*x**18/3 + 120*a**3*b**7*x**19/19 + 9*a**2*b**8*x**20/4 + 10*a*b**9*x**21/21 + b**10*x**22/22

3.124 $\int x^{10}(a + bx)^{10} dx$

Optimal. Leaf size=132

$$\frac{a^{10}x^{11}}{11} + \frac{5}{6}a^9bx^{12} + \frac{45}{13}a^8b^2x^{13} + \frac{60}{7}a^7b^3x^{14} + 14a^6b^4x^{15} + \frac{63}{4}a^5b^5x^{16} + \frac{210}{17}a^4b^6x^{17} + \frac{20}{3}a^3b^7x^{18} + \frac{45}{19}a^2b^8x^{19} + \frac{1}{2}ab^9x^{20}$$

[Out] 1/11*a^10*x^11+5/6*a^9*b*x^12+45/13*a^8*b^2*x^13+60/7*a^7*b^3*x^14+14*a^6*b^4*x^15+63/4*a^5*b^5*x^16+210/17*a^4*b^6*x^17+20/3*a^3*b^7*x^18+45/19*a^2*b^8*x^19+1/2*a*b^9*x^20+1/21*b^10*x^21

Rubi [A] time = 0.06, antiderivative size = 132, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{45}{19}a^2b^8x^{19} + \frac{20}{3}a^3b^7x^{18} + \frac{210}{17}a^4b^6x^{17} + \frac{63}{4}a^5b^5x^{16} + 14a^6b^4x^{15} + \frac{60}{7}a^7b^3x^{14} + \frac{45}{13}a^8b^2x^{13} + \frac{5}{6}a^9bx^{12} + \frac{a^{10}x^{11}}{11} + \frac{1}{2}ab^9x^{20}$$

Antiderivative was successfully verified.

[In] Int[x^10*(a + b*x)^10,x]

[Out] (a^10*x^11)/11 + (5*a^9*b*x^12)/6 + (45*a^8*b^2*x^13)/13 + (60*a^7*b^3*x^14)/7 + 14*a^6*b^4*x^15 + (63*a^5*b^5*x^16)/4 + (210*a^4*b^6*x^17)/17 + (20*a^3*b^7*x^18)/3 + (45*a^2*b^8*x^19)/19 + (a*b^9*x^20)/2 + (b^10*x^21)/21

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int x^{10}(a + bx)^{10} dx = \int (a^{10}x^{10} + 10a^9bx^{11} + 45a^8b^2x^{12} + 120a^7b^3x^{13} + 210a^6b^4x^{14} + 252a^5b^5x^{15} + 210a^4b^6x^{16} + \frac{a^{10}x^{11}}{11} + \frac{5}{6}a^9bx^{12} + \frac{45}{13}a^8b^2x^{13} + \frac{60}{7}a^7b^3x^{14} + 14a^6b^4x^{15} + \frac{63}{4}a^5b^5x^{16} + \frac{210}{17}a^4b^6x^{17} + \frac{20}{3}a^3b^7x^{18} + \frac{45}{19}a^2b^8x^{19} + \frac{1}{2}ab^9x^{20} + \frac{1}{21}b^{10}x^{21}) dx$$

Mathematica [A] time = 0.00, size = 132, normalized size = 1.00

$$\frac{a^{10}x^{11}}{11} + \frac{5}{6}a^9bx^{12} + \frac{45}{13}a^8b^2x^{13} + \frac{60}{7}a^7b^3x^{14} + 14a^6b^4x^{15} + \frac{63}{4}a^5b^5x^{16} + \frac{210}{17}a^4b^6x^{17} + \frac{20}{3}a^3b^7x^{18} + \frac{45}{19}a^2b^8x^{19} + \frac{1}{2}ab^9x^{20} + \frac{1}{21}b^{10}x^{21}$$

Antiderivative was successfully verified.

[In] Integrate[x^10*(a + b*x)^10,x]

[Out] (a^10*x^11)/11 + (5*a^9*b*x^12)/6 + (45*a^8*b^2*x^13)/13 + (60*a^7*b^3*x^14)/7 + 14*a^6*b^4*x^15 + (63*a^5*b^5*x^16)/4 + (210*a^4*b^6*x^17)/17 + (20*a^3*b^7*x^18)/3 + (45*a^2*b^8*x^19)/19 + (a*b^9*x^20)/2 + (b^10*x^21)/21

fricas [A] time = 0.61, size = 112, normalized size = 0.85

$$\frac{1}{21}x^{21}b^{10} + \frac{1}{2}x^{20}b^9a + \frac{45}{19}x^{19}b^8a^2 + \frac{20}{3}x^{18}b^7a^3 + \frac{210}{17}x^{17}b^6a^4 + \frac{63}{4}x^{16}b^5a^5 + 14x^{15}b^4a^6 + \frac{60}{7}x^{14}b^3a^7 + \frac{45}{13}x^{13}b^2a^8 + \frac{5}{6}x^{12}b^1a^9 + \frac{1}{21}x^{11}b^0a^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^10*(b*x+a)^10,x, algorithm="fricas")

[Out] 1/21*x^21*b^10 + 1/2*x^20*b^9*a + 45/19*x^19*b^8*a^2 + 20/3*x^18*b^7*a^3 + 210/17*x^17*b^6*a^4 + 63/4*x^16*b^5*a^5 + 14*x^15*b^4*a^6 + 60/7*x^14*b^3*a^7 + 45/13*x^13*b^2*a^8 + 5/6*x^12*b^1*a^9 + 1/11*x^11*a^10

giac [A] time = 0.99, size = 112, normalized size = 0.85

$$\frac{1}{21}b^{10}x^{21} + \frac{1}{2}ab^9x^{20} + \frac{45}{19}a^2b^8x^{19} + \frac{20}{3}a^3b^7x^{18} + \frac{210}{17}a^4b^6x^{17} + \frac{63}{4}a^5b^5x^{16} + 14a^6b^4x^{15} + \frac{60}{7}a^7b^3x^{14} + \frac{45}{13}a^8b^2x^{13} + \frac{5}{6}a^9b^1x^{12} + \frac{1}{21}a^{10}b^0x^{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^10*(b*x+a)^10,x, algorithm="giac")

[Out] 1/21*b^10*x^21 + 1/2*a*b^9*x^20 + 45/19*a^2*b^8*x^19 + 20/3*a^3*b^7*x^18 + 210/17*a^4*b^6*x^17 + 63/4*a^5*b^5*x^16 + 14*a^6*b^4*x^15 + 60/7*a^7*b^3*x^14 + 45/13*a^8*b^2*x^13 + 5/6*a^9*b^1*x^12 + 1/11*a^10*x^11

maple [A] time = 0.00, size = 113, normalized size = 0.86

$$\frac{1}{21}b^{10}x^{21} + \frac{1}{2}ab^9x^{20} + \frac{45}{19}a^2b^8x^{19} + \frac{20}{3}a^3b^7x^{18} + \frac{210}{17}a^4b^6x^{17} + \frac{63}{4}a^5b^5x^{16} + 14a^6b^4x^{15} + \frac{60}{7}a^7b^3x^{14} + \frac{45}{13}a^8b^2x^{13} + \frac{5}{6}a^9b^1x^{12} + \frac{1}{21}a^{10}b^0x^{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^10*(b*x+a)^10,x)

[Out] 1/11*a^10*x^11+5/6*a^9*b*x^12+45/13*a^8*b^2*x^13+60/7*a^7*b^3*x^14+14*a^6*b^4*x^15+63/4*a^5*b^5*x^16+210/17*a^4*b^6*x^17+20/3*a^3*b^7*x^18+45/19*a^2*b^8*x^19+1/2*a*b^9*x^20+1/21*b^10*x^21

maxima [A] time = 1.34, size = 112, normalized size = 0.85

$$\frac{1}{21}b^{10}x^{21} + \frac{1}{2}ab^9x^{20} + \frac{45}{19}a^2b^8x^{19} + \frac{20}{3}a^3b^7x^{18} + \frac{210}{17}a^4b^6x^{17} + \frac{63}{4}a^5b^5x^{16} + 14a^6b^4x^{15} + \frac{60}{7}a^7b^3x^{14} + \frac{45}{13}a^8b^2x^{13} + \frac{5}{6}a^9b^1x^{12} + \frac{1}{21}a^{10}b^0x^{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x¹⁰*(b*x+a)¹⁰,x, algorithm="maxima")

[Out] 1/21*b¹⁰*x²¹ + 1/2*a*b⁹*x²⁰ + 45/19*a²*b⁸*x¹⁹ + 20/3*a³*b⁷*x¹⁸ + 210/17*a⁴*b⁶*x¹⁷ + 63/4*a⁵*b⁵*x¹⁶ + 14*a⁶*b⁴*x¹⁵ + 60/7*a⁷*b³*x¹⁴ + 45/13*a⁸*b²*x¹³ + 5/6*a⁹*b*x¹² + 1/11*a¹⁰*x¹¹

mupad [B] time = 0.08, size = 112, normalized size = 0.85

$$\frac{a^{10}x^{11}}{11} + \frac{5a^9bx^{12}}{6} + \frac{45a^8b^2x^{13}}{13} + \frac{60a^7b^3x^{14}}{7} + 14a^6b^4x^{15} + \frac{63a^5b^5x^{16}}{4} + \frac{210a^4b^6x^{17}}{17} + \frac{20a^3b^7x^{18}}{3} + \frac{45a^2b^8x^{19}}{19}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x¹⁰*(a + b*x)¹⁰,x)

[Out] (a¹⁰*x¹¹)/11 + (b¹⁰*x²¹)/21 + (5*a⁹*b*x¹²)/6 + (a*b⁹*x²⁰)/2 + (45*a⁸*b²*x¹³)/13 + (60*a⁷*b³*x¹⁴)/7 + 14*a⁶*b⁴*x¹⁵ + (63*a⁵*b⁵*x¹⁶)/4 + (210*a⁴*b⁶*x¹⁷)/17 + (20*a³*b⁷*x¹⁸)/3 + (45*a²*b⁸*x¹⁹)/19

sympy [A] time = 0.11, size = 131, normalized size = 0.99

$$\frac{a^{10}x^{11}}{11} + \frac{5a^9bx^{12}}{6} + \frac{45a^8b^2x^{13}}{13} + \frac{60a^7b^3x^{14}}{7} + 14a^6b^4x^{15} + \frac{63a^5b^5x^{16}}{4} + \frac{210a^4b^6x^{17}}{17} + \frac{20a^3b^7x^{18}}{3} + \frac{45a^2b^8x^{19}}{19} + \frac{ab^9x^{20}}{2} + \frac{b^{10}x^{21}}{21}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**10*(b*x+a)**10,x)

[Out] a**10*x**11/11 + 5*a**9*b*x**12/6 + 45*a**8*b**2*x**13/13 + 60*a**7*b**3*x**14/7 + 14*a**6*b**4*x**15 + 63*a**5*b**5*x**16/4 + 210*a**4*b**6*x**17/17 + 20*a**3*b**7*x**18/3 + 45*a**2*b**8*x**19/19 + a*b**9*x**20/2 + b**10*x**21/21

3.125 $\int x^9(a + bx)^{10} dx$

Optimal. Leaf size=132

$$\frac{a^{10}x^{10}}{10} + \frac{10}{11}a^9bx^{11} + \frac{15}{4}a^8b^2x^{12} + \frac{120}{13}a^7b^3x^{13} + 15a^6b^4x^{14} + \frac{84}{5}a^5b^5x^{15} + \frac{105}{8}a^4b^6x^{16} + \frac{120}{17}a^3b^7x^{17} + \frac{5}{2}a^2b^8x^{18} + \frac{10}{19}ab^9x^{19} + \frac{1}{20}b^{10}x^{20}$$

[Out] 1/10*a^10*x^10+10/11*a^9*b*x^11+15/4*a^8*b^2*x^12+120/13*a^7*b^3*x^13+15*a^6*b^4*x^14+84/5*a^5*b^5*x^15+105/8*a^4*b^6*x^16+120/17*a^3*b^7*x^17+5/2*a^2*b^8*x^18+10/19*a*b^9*x^19+1/20*b^10*x^20

Rubi [A] time = 0.06, antiderivative size = 132, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{5}{2}a^2b^8x^{18} + \frac{120}{17}a^3b^7x^{17} + \frac{105}{8}a^4b^6x^{16} + \frac{84}{5}a^5b^5x^{15} + 15a^6b^4x^{14} + \frac{120}{13}a^7b^3x^{13} + \frac{15}{4}a^8b^2x^{12} + \frac{10}{11}a^9bx^{11} + \frac{a^{10}x^{10}}{10} + \frac{10}{19}ab^9x^{19} + \frac{1}{20}b^{10}x^{20}$$

Antiderivative was successfully verified.

[In] Int[x^9*(a + b*x)^10,x]

[Out] (a^10*x^10)/10 + (10*a^9*b*x^11)/11 + (15*a^8*b^2*x^12)/4 + (120*a^7*b^3*x^13)/13 + 15*a^6*b^4*x^14 + (84*a^5*b^5*x^15)/5 + (105*a^4*b^6*x^16)/8 + (120*a^3*b^7*x^17)/17 + (5*a^2*b^8*x^18)/2 + (10*a*b^9*x^19)/19 + (b^10*x^20)/20

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int x^9(a + bx)^{10} dx = \int (a^{10}x^9 + 10a^9bx^{10} + 45a^8b^2x^{11} + 120a^7b^3x^{12} + 210a^6b^4x^{13} + 252a^5b^5x^{14} + 210a^4b^6x^{15} + 105a^3b^7x^{16} + 35a^2b^8x^{17} + 5ab^9x^{18} + b^{10}x^{19}) dx$$

$$= \frac{a^{10}x^{10}}{10} + \frac{10}{11}a^9bx^{11} + \frac{15}{4}a^8b^2x^{12} + \frac{120}{13}a^7b^3x^{13} + 15a^6b^4x^{14} + \frac{84}{5}a^5b^5x^{15} + \frac{105}{8}a^4b^6x^{16} + \frac{120}{17}a^3b^7x^{17} + \frac{5}{2}a^2b^8x^{18} + \frac{10}{19}ab^9x^{19} + \frac{1}{20}b^{10}x^{20}$$

Mathematica [A] time = 0.00, size = 132, normalized size = 1.00

$$\frac{a^{10}x^{10}}{10} + \frac{10}{11}a^9bx^{11} + \frac{15}{4}a^8b^2x^{12} + \frac{120}{13}a^7b^3x^{13} + 15a^6b^4x^{14} + \frac{84}{5}a^5b^5x^{15} + \frac{105}{8}a^4b^6x^{16} + \frac{120}{17}a^3b^7x^{17} + \frac{5}{2}a^2b^8x^{18} + \frac{10}{19}ab^9x^{19} + \frac{1}{20}b^{10}x^{20}$$

Antiderivative was successfully verified.

[In] Integrate[x^9*(a + b*x)^10,x]

[Out] (a^10*x^10)/10 + (10*a^9*b*x^11)/11 + (15*a^8*b^2*x^12)/4 + (120*a^7*b^3*x^13)/13 + 15*a^6*b^4*x^14 + (84*a^5*b^5*x^15)/5 + (105*a^4*b^6*x^16)/8 + (120*a^3*b^7*x^17)/17 + (5*a^2*b^8*x^18)/2 + (10*a*b^9*x^19)/19 + (b^10*x^20)/20

fricas [A] time = 0.44, size = 112, normalized size = 0.85

$$\frac{1}{20}x^{20}b^{10} + \frac{10}{19}x^{19}b^9a + \frac{5}{2}x^{18}b^8a^2 + \frac{120}{17}x^{17}b^7a^3 + \frac{105}{8}x^{16}b^6a^4 + \frac{84}{5}x^{15}b^5a^5 + 15x^{14}b^4a^6 + \frac{120}{13}x^{13}b^3a^7 + \frac{15}{4}x^{12}b^2a^8 + \frac{10}{11}x^{11}ba^9 + \frac{1}{10}x^{10}a^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^9*(b*x+a)^10,x, algorithm="fricas")

[Out] 1/20*x^20*b^10 + 10/19*x^19*b^9*a + 5/2*x^18*b^8*a^2 + 120/17*x^17*b^7*a^3 + 105/8*x^16*b^6*a^4 + 84/5*x^15*b^5*a^5 + 15*x^14*b^4*a^6 + 120/13*x^13*b^3*a^7 + 15/4*x^12*b^2*a^8 + 10/11*x^11*b*a^9 + 1/10*x^10*a^10

giac [A] time = 1.12, size = 112, normalized size = 0.85

$$\frac{1}{20}b^{10}x^{20} + \frac{10}{19}ab^9x^{19} + \frac{5}{2}a^2b^8x^{18} + \frac{120}{17}a^3b^7x^{17} + \frac{105}{8}a^4b^6x^{16} + \frac{84}{5}a^5b^5x^{15} + 15a^6b^4x^{14} + \frac{120}{13}a^7b^3x^{13} + \frac{15}{4}a^8b^2x^{12} + \frac{10}{11}a^9bx^{11} + \frac{1}{10}a^{10}x^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^9*(b*x+a)^10,x, algorithm="giac")

[Out] 1/20*b^10*x^20 + 10/19*a*b^9*x^19 + 5/2*a^2*b^8*x^18 + 120/17*a^3*b^7*x^17 + 105/8*a^4*b^6*x^16 + 84/5*a^5*b^5*x^15 + 15*a^6*b^4*x^14 + 120/13*a^7*b^3*x^13 + 15/4*a^8*b^2*x^12 + 10/11*a^9*b*x^11 + 1/10*a^10*x^10

maple [A] time = 0.00, size = 113, normalized size = 0.86

$$\frac{1}{20}b^{10}x^{20} + \frac{10}{19}ab^9x^{19} + \frac{5}{2}a^2b^8x^{18} + \frac{120}{17}a^3b^7x^{17} + \frac{105}{8}a^4b^6x^{16} + \frac{84}{5}a^5b^5x^{15} + 15a^6b^4x^{14} + \frac{120}{13}a^7b^3x^{13} + \frac{15}{4}a^8b^2x^{12} + \frac{10}{11}a^9bx^{11} + \frac{1}{10}a^{10}x^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^9*(b*x+a)^10,x)

[Out] 1/10*a^10*x^10+10/11*a^9*b*x^11+15/4*a^8*b^2*x^12+120/13*a^7*b^3*x^13+15*a^6*b^4*x^14+84/5*a^5*b^5*x^15+105/8*a^4*b^6*x^16+120/17*a^3*b^7*x^17+5/2*a^2*b^8*x^18+10/19*a*b^9*x^19+1/20*b^10*x^20

maxima [A] time = 1.37, size = 112, normalized size = 0.85

$$\frac{1}{20} b^{10} x^{20} + \frac{10}{19} a b^9 x^{19} + \frac{5}{2} a^2 b^8 x^{18} + \frac{120}{17} a^3 b^7 x^{17} + \frac{105}{8} a^4 b^6 x^{16} + \frac{84}{5} a^5 b^5 x^{15} + 15 a^6 b^4 x^{14} + \frac{120}{13} a^7 b^3 x^{13} + \frac{15}{4} a^8 b^2 x^{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^9*(b*x+a)^10,x, algorithm="maxima")

[Out] 1/20*b^10*x^20 + 10/19*a*b^9*x^19 + 5/2*a^2*b^8*x^18 + 120/17*a^3*b^7*x^17 + 105/8*a^4*b^6*x^16 + 84/5*a^5*b^5*x^15 + 15*a^6*b^4*x^14 + 120/13*a^7*b^3*x^13 + 15/4*a^8*b^2*x^12 + 10/11*a^9*b*x^11 + 1/10*a^10*x^10

mupad [B] time = 0.12, size = 112, normalized size = 0.85

$$\frac{a^{10} x^{10}}{10} + \frac{10 a^9 b x^{11}}{11} + \frac{15 a^8 b^2 x^{12}}{4} + \frac{120 a^7 b^3 x^{13}}{13} + 15 a^6 b^4 x^{14} + \frac{84 a^5 b^5 x^{15}}{5} + \frac{105 a^4 b^6 x^{16}}{8} + \frac{120 a^3 b^7 x^{17}}{17} + \frac{5 a^2 b^8 x^{18}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^9*(a + b*x)^10,x)

[Out] (a^10*x^10)/10 + (b^10*x^20)/20 + (10*a^9*b*x^11)/11 + (10*a*b^9*x^19)/19 + (15*a^8*b^2*x^12)/4 + (120*a^7*b^3*x^13)/13 + 15*a^6*b^4*x^14 + (84*a^5*b^5*x^15)/5 + (105*a^4*b^6*x^16)/8 + (120*a^3*b^7*x^17)/17 + (5*a^2*b^8*x^18)/2

sympy [A] time = 0.10, size = 133, normalized size = 1.01

$$\frac{a^{10} x^{10}}{10} + \frac{10 a^9 b x^{11}}{11} + \frac{15 a^8 b^2 x^{12}}{4} + \frac{120 a^7 b^3 x^{13}}{13} + 15 a^6 b^4 x^{14} + \frac{84 a^5 b^5 x^{15}}{5} + \frac{105 a^4 b^6 x^{16}}{8} + \frac{120 a^3 b^7 x^{17}}{17} + \frac{5 a^2 b^8 x^{18}}{2} + \frac{10 a b^9 x^{19}}{19}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**9*(b*x+a)**10,x)

[Out] a**10*x**10/10 + 10*a**9*b*x**11/11 + 15*a**8*b**2*x**12/4 + 120*a**7*b**3*x**13/13 + 15*a**6*b**4*x**14 + 84*a**5*b**5*x**15/5 + 105*a**4*b**6*x**16/8 + 120*a**3*b**7*x**17/17 + 5*a**2*b**8*x**18/2 + 10*a*b**9*x**19/19 + b**10*x**20/20

3.126 $\int x^8(a + bx)^{10} dx$

Optimal. Leaf size=147

$$\frac{a^8(a + bx)^{11}}{11b^9} - \frac{2a^7(a + bx)^{12}}{3b^9} + \frac{28a^6(a + bx)^{13}}{13b^9} - \frac{4a^5(a + bx)^{14}}{b^9} + \frac{14a^4(a + bx)^{15}}{3b^9} - \frac{7a^3(a + bx)^{16}}{2b^9} + \frac{28a^2(a + bx)^{17}}{17b^9} + \frac{a(a + bx)^{18}}{19b^9}$$

[Out] $1/11*a^8*(b*x+a)^{11}/b^9 - 2/3*a^7*(b*x+a)^{12}/b^9 + 28/13*a^6*(b*x+a)^{13}/b^9 - 4*a^5*(b*x+a)^{14}/b^9 + 14/3*a^4*(b*x+a)^{15}/b^9 - 7/2*a^3*(b*x+a)^{16}/b^9 + 28/17*a^2*(b*x+a)^{17}/b^9 - 4/9*a*(b*x+a)^{18}/b^9 + 1/19*(b*x+a)^{19}/b^9$

Rubi [A] time = 0.06, antiderivative size = 147, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{28a^2(a + bx)^{17}}{17b^9} - \frac{7a^3(a + bx)^{16}}{2b^9} + \frac{14a^4(a + bx)^{15}}{3b^9} - \frac{4a^5(a + bx)^{14}}{b^9} + \frac{28a^6(a + bx)^{13}}{13b^9} - \frac{2a^7(a + bx)^{12}}{3b^9} + \frac{a^8(a + bx)^{11}}{11b^9} + \frac{a(a + bx)^{18}}{19b^9}$$

Antiderivative was successfully verified.

[In] Int[x^8*(a + b*x)^10,x]

[Out] $(a^8*(a + b*x)^{11})/(11*b^9) - (2*a^7*(a + b*x)^{12})/(3*b^9) + (28*a^6*(a + b*x)^{13})/(13*b^9) - (4*a^5*(a + b*x)^{14})/b^9 + (14*a^4*(a + b*x)^{15})/(3*b^9) - (7*a^3*(a + b*x)^{16})/(2*b^9) + (28*a^2*(a + b*x)^{17})/(17*b^9) - (4*a*(a + b*x)^{18})/(9*b^9) + (a + b*x)^{19}/(19*b^9)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^8(a + bx)^{10} dx &= \int \left(\frac{a^8(a + bx)^{10}}{b^8} - \frac{8a^7(a + bx)^{11}}{b^8} + \frac{28a^6(a + bx)^{12}}{b^8} - \frac{56a^5(a + bx)^{13}}{b^8} + \frac{70a^4(a + bx)^{14}}{b^8} - \frac{56a^3(a + bx)^{15}}{b^8} + \frac{28a^2(a + bx)^{16}}{b^8} - \frac{8a(a + bx)^{17}}{b^8} + \frac{a^8(a + bx)^{18}}{b^8} \right) dx \\ &= \frac{a^8(a + bx)^{11}}{11b^9} - \frac{2a^7(a + bx)^{12}}{3b^9} + \frac{28a^6(a + bx)^{13}}{13b^9} - \frac{4a^5(a + bx)^{14}}{b^9} + \frac{14a^4(a + bx)^{15}}{3b^9} - \frac{7a^3(a + bx)^{16}}{2b^9} + \frac{28a^2(a + bx)^{17}}{17b^9} - \frac{4a(a + bx)^{18}}{9b^9} + \frac{a^8(a + bx)^{19}}{19b^9} \end{aligned}$$

Mathematica [A] time = 0.00, size = 125, normalized size = 0.85

$$\frac{a^{10}x^9}{9} + a^9bx^{10} + \frac{45}{11}a^8b^2x^{11} + 10a^7b^3x^{12} + \frac{210}{13}a^6b^4x^{13} + 18a^5b^5x^{14} + 14a^4b^6x^{15} + \frac{15}{2}a^3b^7x^{16} + \frac{45}{17}a^2b^8x^{17} + \frac{5}{9}ab^9x^{18} + \frac{b^{10}x^{19}}{19}$$

Antiderivative was successfully verified.

[In] Integrate[x^8*(a + b*x)^10,x]

[Out] $(a^{10}x^9)/9 + a^9bx^{10} + (45a^8b^2x^{11})/11 + 10a^7b^3x^{12} + (210a^6b^4x^{13})/13 + 18a^5b^5x^{14} + 14a^4b^6x^{15} + (15a^3b^7x^{16})/2 + (45a^2b^8x^{17})/17 + (5ab^9x^{18})/9 + (b^{10}x^{19})/19$

fricas [A] time = 0.60, size = 111, normalized size = 0.76

$$\frac{1}{19}x^{19}b^{10} + \frac{5}{9}x^{18}b^9a + \frac{45}{17}x^{17}b^8a^2 + \frac{15}{2}x^{16}b^7a^3 + 14x^{15}b^6a^4 + 18x^{14}b^5a^5 + \frac{210}{13}x^{13}b^4a^6 + 10x^{12}b^3a^7 + \frac{45}{11}x^{11}b^2a^8 + x^{10}ba^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8*(b*x+a)^10,x, algorithm="fricas")

[Out] $1/19*x^{19}*b^{10} + 5/9*x^{18}*b^9*a + 45/17*x^{17}*b^8*a^2 + 15/2*x^{16}*b^7*a^3 + 14*x^{15}*b^6*a^4 + 18*x^{14}*b^5*a^5 + 210/13*x^{13}*b^4*a^6 + 10*x^{12}*b^3*a^7 + 45/11*x^{11}*b^2*a^8 + x^{10}*b*a^9 + 1/9*x^9*a^{10}$

giac [A] time = 1.01, size = 111, normalized size = 0.76

$$\frac{1}{19}b^{10}x^{19} + \frac{5}{9}ab^9x^{18} + \frac{45}{17}a^2b^8x^{17} + \frac{15}{2}a^3b^7x^{16} + 14a^4b^6x^{15} + 18a^5b^5x^{14} + \frac{210}{13}a^6b^4x^{13} + 10a^7b^3x^{12} + \frac{45}{11}a^8b^2x^{11} + a^9bx^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8*(b*x+a)^10,x, algorithm="giac")

[Out] $1/19*b^{10}*x^{19} + 5/9*a*b^9*x^{18} + 45/17*a^2*b^8*x^{17} + 15/2*a^3*b^7*x^{16} + 14*a^4*b^6*x^{15} + 18*a^5*b^5*x^{14} + 210/13*a^6*b^4*x^{13} + 10*a^7*b^3*x^{12} + 45/11*a^8*b^2*x^{11} + a^9*b*x^{10} + 1/9*a^{10}*x^9$

maple [A] time = 0.00, size = 112, normalized size = 0.76

$$\frac{1}{19}b^{10}x^{19} + \frac{5}{9}ab^9x^{18} + \frac{45}{17}a^2b^8x^{17} + \frac{15}{2}a^3b^7x^{16} + 14a^4b^6x^{15} + 18a^5b^5x^{14} + \frac{210}{13}a^6b^4x^{13} + 10a^7b^3x^{12} + \frac{45}{11}a^8b^2x^{11} + a^9bx^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^8*(b*x+a)^10,x)

[Out] $1/19*b^{10}*x^{19} + 5/9*a*b^9*x^{18} + 45/17*a^2*b^8*x^{17} + 15/2*a^3*b^7*x^{16} + 14*a^4*b^6*x^{15} + 18*a^5*b^5*x^{14} + 210/13*a^6*b^4*x^{13} + 10*a^7*b^3*x^{12} + 45/11*a^8*b^2*x^{11} + a^9*b*x^{10} + 1/9*a^{10}*x^9$

maxima [A] time = 1.36, size = 111, normalized size = 0.76

$$\frac{1}{19}b^{10}x^{19} + \frac{5}{9}ab^9x^{18} + \frac{45}{17}a^2b^8x^{17} + \frac{15}{2}a^3b^7x^{16} + 14a^4b^6x^{15} + 18a^5b^5x^{14} + \frac{210}{13}a^6b^4x^{13} + 10a^7b^3x^{12} + \frac{45}{11}a^8b^2x^{11} + a^9bx^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8*(b*x+a)^10,x, algorithm="maxima")

[Out] 1/19*b^10*x^19 + 5/9*a*b^9*x^18 + 45/17*a^2*b^8*x^17 + 15/2*a^3*b^7*x^16 + 14*a^4*b^6*x^15 + 18*a^5*b^5*x^14 + 210/13*a^6*b^4*x^13 + 10*a^7*b^3*x^12 + 45/11*a^8*b^2*x^11 + a^9*b*x^10 + 1/9*a^10*x^9

mupad [B] time = 0.09, size = 111, normalized size = 0.76

$$\frac{a^{10}x^9}{9} + a^9bx^{10} + \frac{45a^8b^2x^{11}}{11} + 10a^7b^3x^{12} + \frac{210a^6b^4x^{13}}{13} + 18a^5b^5x^{14} + 14a^4b^6x^{15} + \frac{15a^3b^7x^{16}}{2} + \frac{45a^2b^8x^{17}}{17} + \frac{5a^1b^9x^{18}}{19} + \frac{b^{10}x^{19}}{19}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^8*(a + b*x)^10,x)

[Out] (a^10*x^9)/9 + (b^10*x^19)/19 + a^9*b*x^10 + (5*a*b^9*x^18)/9 + (45*a^8*b^2*x^11)/11 + 10*a^7*b^3*x^12 + (210*a^6*b^4*x^13)/13 + 18*a^5*b^5*x^14 + 14*a^4*b^6*x^15 + (15*a^3*b^7*x^16)/2 + (45*a^2*b^8*x^17)/17

sympy [A] time = 0.11, size = 126, normalized size = 0.86

$$\frac{a^{10}x^9}{9} + a^9bx^{10} + \frac{45a^8b^2x^{11}}{11} + 10a^7b^3x^{12} + \frac{210a^6b^4x^{13}}{13} + 18a^5b^5x^{14} + 14a^4b^6x^{15} + \frac{15a^3b^7x^{16}}{2} + \frac{45a^2b^8x^{17}}{17} + \frac{5ab^9x^{18}}{9} + \frac{b^{10}x^{19}}{19}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**8*(b*x+a)**10,x)

[Out] a**10*x**9/9 + a**9*b*x**10 + 45*a**8*b**2*x**11/11 + 10*a**7*b**3*x**12 + 210*a**6*b**4*x**13/13 + 18*a**5*b**5*x**14 + 14*a**4*b**6*x**15 + 15*a**3*b**7*x**16/2 + 45*a**2*b**8*x**17/17 + 5*a*b**9*x**18/9 + b**10*x**19/19

3.127 $\int x^7(a + bx)^{10} dx$

Optimal. Leaf size=132

$$\frac{a^7(a+bx)^{11}}{11b^8} + \frac{7a^6(a+bx)^{12}}{12b^8} - \frac{21a^5(a+bx)^{13}}{13b^8} + \frac{5a^4(a+bx)^{14}}{2b^8} - \frac{7a^3(a+bx)^{15}}{3b^8} + \frac{21a^2(a+bx)^{16}}{16b^8} + \frac{(a+bx)^{18}}{18b^8} - \frac{7a(a+bx)^{19}}{19b^8}$$

[Out] $-1/11*a^7*(b*x+a)^{11}/b^8+7/12*a^6*(b*x+a)^{12}/b^8-21/13*a^5*(b*x+a)^{13}/b^8+5/2*a^4*(b*x+a)^{14}/b^8-7/3*a^3*(b*x+a)^{15}/b^8+21/16*a^2*(b*x+a)^{16}/b^8-7/17*a*(b*x+a)^{17}/b^8+1/18*(b*x+a)^{18}/b^8$

Rubi [A] time = 0.06, antiderivative size = 132, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{21a^2(a+bx)^{16}}{16b^8} - \frac{7a^3(a+bx)^{15}}{3b^8} + \frac{5a^4(a+bx)^{14}}{2b^8} - \frac{21a^5(a+bx)^{13}}{13b^8} + \frac{7a^6(a+bx)^{12}}{12b^8} - \frac{a^7(a+bx)^{11}}{11b^8} + \frac{(a+bx)^{18}}{18b^8} - \frac{7a(a+bx)^{19}}{19b^8}$$

Antiderivative was successfully verified.

[In] Int[x^7*(a + b*x)^10, x]

[Out] $-(a^7*(a + b*x)^{11})/(11*b^8) + (7*a^6*(a + b*x)^{12})/(12*b^8) - (21*a^5*(a + b*x)^{13})/(13*b^8) + (5*a^4*(a + b*x)^{14})/(2*b^8) - (7*a^3*(a + b*x)^{15})/(3*b^8) + (21*a^2*(a + b*x)^{16})/(16*b^8) - (7*a*(a + b*x)^{17})/(17*b^8) + (a + b*x)^{18}/(18*b^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^7(a + bx)^{10} dx &= \int \left(-\frac{a^7(a + bx)^{10}}{b^7} + \frac{7a^6(a + bx)^{11}}{b^7} - \frac{21a^5(a + bx)^{12}}{b^7} + \frac{35a^4(a + bx)^{13}}{b^7} - \frac{35a^3(a + bx)^{14}}{b^7} + \frac{7a^2(a + bx)^{15}}{b^7} - \frac{7a(a + bx)^{16}}{b^7} + \frac{(a + bx)^{17}}{b^7} \right) dx \\ &= -\frac{a^7(a + bx)^{11}}{11b^8} + \frac{7a^6(a + bx)^{12}}{12b^8} - \frac{21a^5(a + bx)^{13}}{13b^8} + \frac{5a^4(a + bx)^{14}}{2b^8} - \frac{7a^3(a + bx)^{15}}{3b^8} + \frac{21a^2(a + bx)^{16}}{16b^8} + \frac{(a + bx)^{18}}{18b^8} - \frac{7a(a + bx)^{19}}{19b^8} \end{aligned}$$

Mathematica [A] time = 0.00, size = 130, normalized size = 0.98

$$\frac{a^{10}x^8}{8} + \frac{10}{9}a^9bx^9 + \frac{9}{2}a^8b^2x^{10} + \frac{120}{11}a^7b^3x^{11} + \frac{35}{2}a^6b^4x^{12} + \frac{252}{13}a^5b^5x^{13} + 15a^4b^6x^{14} + 8a^3b^7x^{15} + \frac{45}{16}a^2b^8x^{16} + \frac{10}{17}ab^9x^{17} + \frac{b^{10}x^{18}}{18}$$

Antiderivative was successfully verified.

[In] Integrate[x^7*(a + b*x)^10,x]

[Out] (a^10*x^8)/8 + (10*a^9*b*x^9)/9 + (9*a^8*b^2*x^10)/2 + (120*a^7*b^3*x^11)/11 + (35*a^6*b^4*x^12)/2 + (252*a^5*b^5*x^13)/13 + 15*a^4*b^6*x^14 + 8*a^3*b^7*x^15 + (45*a^2*b^8*x^16)/16 + (10*a*b^9*x^17)/17 + (b^10*x^18)/18

fricas [A] time = 0.65, size = 112, normalized size = 0.85

$$\frac{1}{18}x^{18}b^{10} + \frac{10}{17}x^{17}b^9a + \frac{45}{16}x^{16}b^8a^2 + 8x^{15}b^7a^3 + 15x^{14}b^6a^4 + \frac{252}{13}x^{13}b^5a^5 + \frac{35}{2}x^{12}b^4a^6 + \frac{120}{11}x^{11}b^3a^7 + \frac{9}{2}x^{10}b^2a^8 + \frac{10}{9}x^9ba^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^10,x, algorithm="fricas")

[Out] 1/18*x^18*b^10 + 10/17*x^17*b^9*a + 45/16*x^16*b^8*a^2 + 8*x^15*b^7*a^3 + 15*x^14*b^6*a^4 + 252/13*x^13*b^5*a^5 + 35/2*x^12*b^4*a^6 + 120/11*x^11*b^3*a^7 + 9/2*x^10*b^2*a^8 + 10/9*x^9*b*a^9 + 1/8*x^8*a^10

giac [A] time = 0.84, size = 112, normalized size = 0.85

$$\frac{1}{18}b^{10}x^{18} + \frac{10}{17}ab^9x^{17} + \frac{45}{16}a^2b^8x^{16} + 8a^3b^7x^{15} + 15a^4b^6x^{14} + \frac{252}{13}a^5b^5x^{13} + \frac{35}{2}a^6b^4x^{12} + \frac{120}{11}a^7b^3x^{11} + \frac{9}{2}a^8b^2x^{10} + \frac{10}{9}a^9bx^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^10,x, algorithm="giac")

[Out] 1/18*b^10*x^18 + 10/17*a*b^9*x^17 + 45/16*a^2*b^8*x^16 + 8*a^3*b^7*x^15 + 15*a^4*b^6*x^14 + 252/13*a^5*b^5*x^13 + 35/2*a^6*b^4*x^12 + 120/11*a^7*b^3*x^11 + 9/2*a^8*b^2*x^10 + 10/9*a^9*b*x^9 + 1/8*a^10*x^8

maple [A] time = 0.00, size = 113, normalized size = 0.86

$$\frac{1}{18}b^{10}x^{18} + \frac{10}{17}ab^9x^{17} + \frac{45}{16}a^2b^8x^{16} + 8a^3b^7x^{15} + 15a^4b^6x^{14} + \frac{252}{13}a^5b^5x^{13} + \frac{35}{2}a^6b^4x^{12} + \frac{120}{11}a^7b^3x^{11} + \frac{9}{2}a^8b^2x^{10} + \frac{10}{9}a^9bx^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7*(b*x+a)^10,x)

[Out] 1/18*b^10*x^18+10/17*a*b^9*x^17+45/16*a^2*b^8*x^16+8*a^3*b^7*x^15+15*a^4*b^6*x^14+252/13*a^5*b^5*x^13+35/2*a^6*b^4*x^12+120/11*a^7*b^3*x^11+9/2*a^8*b^2*x^10+10/9*a^9*b*x^9+1/8*a^10*x^8

maxima [A] time = 1.34, size = 112, normalized size = 0.85

$$\frac{1}{18}b^{10}x^{18} + \frac{10}{17}ab^9x^{17} + \frac{45}{16}a^2b^8x^{16} + 8a^3b^7x^{15} + 15a^4b^6x^{14} + \frac{252}{13}a^5b^5x^{13} + \frac{35}{2}a^6b^4x^{12} + \frac{120}{11}a^7b^3x^{11} + \frac{9}{2}a^8b^2x^{10} + \frac{10}{9}a^9bx^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^10,x, algorithm="maxima")

[Out] $1/18*b^{10}*x^{18} + 10/17*a*b^9*x^{17} + 45/16*a^2*b^8*x^{16} + 8*a^3*b^7*x^{15} + 15*a^4*b^6*x^{14} + 252/13*a^5*b^5*x^{13} + 35/2*a^6*b^4*x^{12} + 120/11*a^7*b^3*x^{11} + 9/2*a^8*b^2*x^{10} + 10/9*a^9*b*x^9 + 1/8*a^{10}*x^8$

mupad [B] time = 0.08, size = 112, normalized size = 0.85

$$\frac{a^{10}x^8}{8} + \frac{10a^9bx^9}{9} + \frac{9a^8b^2x^{10}}{2} + \frac{120a^7b^3x^{11}}{11} + \frac{35a^6b^4x^{12}}{2} + \frac{252a^5b^5x^{13}}{13} + 15a^4b^6x^{14} + 8a^3b^7x^{15} + \frac{45a^2b^8x^{16}}{16} + \frac{10ab^9x^{17}}{17} + \frac{b^{10}x^{18}}{18}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7*(a + b*x)^10,x)

[Out] $(a^{10}*x^8)/8 + (b^{10}*x^{18})/18 + (10*a^9*b*x^9)/9 + (10*a*b^9*x^{17})/17 + (9*a^8*b^2*x^{10})/2 + (120*a^7*b^3*x^{11})/11 + (35*a^6*b^4*x^{12})/2 + (252*a^5*b^5*x^{13})/13 + 15*a^4*b^6*x^{14} + 8*a^3*b^7*x^{15} + (45*a^2*b^8*x^{16})/16$

sympy [A] time = 0.11, size = 131, normalized size = 0.99

$$\frac{a^{10}x^8}{8} + \frac{10a^9bx^9}{9} + \frac{9a^8b^2x^{10}}{2} + \frac{120a^7b^3x^{11}}{11} + \frac{35a^6b^4x^{12}}{2} + \frac{252a^5b^5x^{13}}{13} + 15a^4b^6x^{14} + 8a^3b^7x^{15} + \frac{45a^2b^8x^{16}}{16} + \frac{10ab^9x^{17}}{17} + \frac{b^{10}x^{18}}{18}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**7*(b*x+a)**10,x)

[Out] $a^{10}*x^{18}/8 + 10*a^9*b*x^{17}/9 + 9*a^8*b^2*x^{16}/2 + 120*a^7*b^3*x^{15}/11 + 35*a^6*b^4*x^{14}/2 + 252*a^5*b^5*x^{13}/13 + 15*a^4*b^6*x^{12} + 8*a^3*b^7*x^{11} + 45*a^2*b^8*x^{10}/16 + 10*a*b^9*x^9/17 + b^{10}*x^8/18$

3.128 $\int x^6(a + bx)^{10} dx$

Optimal. Leaf size=112

$$\frac{a^6(a + bx)^{11}}{11b^7} - \frac{a^5(a + bx)^{12}}{2b^7} + \frac{15a^4(a + bx)^{13}}{13b^7} - \frac{10a^3(a + bx)^{14}}{7b^7} + \frac{a^2(a + bx)^{15}}{b^7} + \frac{(a + bx)^{17}}{17b^7} - \frac{3a(a + bx)^{16}}{8b^7}$$

[Out] $1/11*a^6*(b*x+a)^{11}/b^7 - 1/2*a^5*(b*x+a)^{12}/b^7 + 15/13*a^4*(b*x+a)^{13}/b^7 - 10/7*a^3*(b*x+a)^{14}/b^7 + a^2*(b*x+a)^{15}/b^7 - 3/8*a*(b*x+a)^{16}/b^7 + 1/17*(b*x+a)^{17}/b^7$

Rubi [A] time = 0.05, antiderivative size = 112, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2(a + bx)^{15}}{b^7} - \frac{10a^3(a + bx)^{14}}{7b^7} + \frac{15a^4(a + bx)^{13}}{13b^7} - \frac{a^5(a + bx)^{12}}{2b^7} + \frac{a^6(a + bx)^{11}}{11b^7} + \frac{(a + bx)^{17}}{17b^7} - \frac{3a(a + bx)^{16}}{8b^7}$$

Antiderivative was successfully verified.

[In] Int[x^6*(a + b*x)^10, x]

[Out] $(a^6*(a + b*x)^{11})/(11*b^7) - (a^5*(a + b*x)^{12})/(2*b^7) + (15*a^4*(a + b*x)^{13})/(13*b^7) - (10*a^3*(a + b*x)^{14})/(7*b^7) + (a^2*(a + b*x)^{15})/b^7 - (3*a*(a + b*x)^{16})/(8*b^7) + (a + b*x)^{17}/(17*b^7)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^6(a + bx)^{10} dx &= \int \left(\frac{a^6(a + bx)^{10}}{b^6} - \frac{6a^5(a + bx)^{11}}{b^6} + \frac{15a^4(a + bx)^{12}}{b^6} - \frac{20a^3(a + bx)^{13}}{b^6} + \frac{15a^2(a + bx)^{14}}{b^6} - \frac{6a(a + bx)^{15}}{b^6} + \frac{(a + bx)^{16}}{b^6} \right) dx \\ &= \frac{a^6(a + bx)^{11}}{11b^7} - \frac{a^5(a + bx)^{12}}{2b^7} + \frac{15a^4(a + bx)^{13}}{13b^7} - \frac{10a^3(a + bx)^{14}}{7b^7} + \frac{a^2(a + bx)^{15}}{b^7} - \frac{3a(a + bx)^{16}}{8b^7} + \frac{(a + bx)^{17}}{17b^7} \end{aligned}$$

Mathematica [A] time = 0.00, size = 126, normalized size = 1.12

$$\frac{a^{10}x^7}{7} + \frac{5}{4}a^9bx^8 + 5a^8b^2x^9 + 12a^7b^3x^{10} + \frac{210}{11}a^6b^4x^{11} + 21a^5b^5x^{12} + \frac{210}{13}a^4b^6x^{13} + \frac{60}{7}a^3b^7x^{14} + 3a^2b^8x^{15} + \frac{5}{8}ab^9x^{16} + \frac{b^{10}x^{17}}{17}$$

Antiderivative was successfully verified.

[In] Integrate[x^6*(a + b*x)^10,x]

[Out] $(a^{10}x^7)/7 + (5a^9b^2x^8)/4 + 5a^8b^2x^9 + 12a^7b^3x^{10} + (210a^6b^4x^{11})/11 + 21a^5b^5x^{12} + (210a^4b^6x^{13})/13 + (60a^3b^7x^{14})/7 + 3a^2b^8x^{15} + (5a^2b^9x^{16})/8 + (b^{10}x^{17})/17$

fricas [A] time = 0.42, size = 112, normalized size = 1.00

$$\frac{1}{17}x^{17}b^{10} + \frac{5}{8}x^{16}b^9a + 3x^{15}b^8a^2 + \frac{60}{7}x^{14}b^7a^3 + \frac{210}{13}x^{13}b^6a^4 + 21x^{12}b^5a^5 + \frac{210}{11}x^{11}b^4a^6 + 12x^{10}b^3a^7 + 5x^9b^2a^8 + \frac{5}{4}x^8ba^9 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^10,x, algorithm="fricas")

[Out] $1/17*x^{17}*b^{10} + 5/8*x^{16}*b^9*a + 3*x^{15}*b^8*a^2 + 60/7*x^{14}*b^7*a^3 + 210/13*x^{13}*b^6*a^4 + 21*x^{12}*b^5*a^5 + 210/11*x^{11}*b^4*a^6 + 12*x^{10}*b^3*a^7 + 5*x^9*b^2*a^8 + 5/4*x^8*b*a^9 + 1/7*x^7*a^{10}$

giac [A] time = 1.10, size = 112, normalized size = 1.00

$$\frac{1}{17}b^{10}x^{17} + \frac{5}{8}ab^9x^{16} + 3a^2b^8x^{15} + \frac{60}{7}a^3b^7x^{14} + \frac{210}{13}a^4b^6x^{13} + 21a^5b^5x^{12} + \frac{210}{11}a^6b^4x^{11} + 12a^7b^3x^{10} + 5a^8b^2x^9 + \frac{5}{4}a^9bx^8 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^10,x, algorithm="giac")

[Out] $1/17*b^{10}*x^{17} + 5/8*a*b^9*x^{16} + 3*a^2*b^8*x^{15} + 60/7*a^3*b^7*x^{14} + 210/13*a^4*b^6*x^{13} + 21*a^5*b^5*x^{12} + 210/11*a^6*b^4*x^{11} + 12*a^7*b^3*x^{10} + 5*a^8*b^2*x^9 + 5/4*a^9*b*x^8 + 1/7*a^{10}*x^7$

maple [A] time = 0.00, size = 113, normalized size = 1.01

$$\frac{1}{17}b^{10}x^{17} + \frac{5}{8}ab^9x^{16} + 3a^2b^8x^{15} + \frac{60}{7}a^3b^7x^{14} + \frac{210}{13}a^4b^6x^{13} + 21a^5b^5x^{12} + \frac{210}{11}a^6b^4x^{11} + 12a^7b^3x^{10} + 5a^8b^2x^9 + \frac{5}{4}a^9bx^8 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6*(b*x+a)^10,x)

[Out] $1/17*b^{10}*x^{17} + 5/8*a*b^9*x^{16} + 3*a^2*b^8*x^{15} + 60/7*a^3*b^7*x^{14} + 210/13*a^4*b^6*x^{13} + 21*a^5*b^5*x^{12} + 210/11*a^6*b^4*x^{11} + 12*a^7*b^3*x^{10} + 5*a^8*b^2*x^9 + 5/4*a^9*b*x^8 + 1/7*a^{10}*x^7$

maxima [A] time = 1.38, size = 112, normalized size = 1.00

$$\frac{1}{17}b^{10}x^{17} + \frac{5}{8}ab^9x^{16} + 3a^2b^8x^{15} + \frac{60}{7}a^3b^7x^{14} + \frac{210}{13}a^4b^6x^{13} + 21a^5b^5x^{12} + \frac{210}{11}a^6b^4x^{11} + 12a^7b^3x^{10} + 5a^8b^2x^9 + \frac{5}{4}a^9bx^8 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^10,x, algorithm="maxima")

[Out] 1/17*b^10*x^17 + 5/8*a*b^9*x^16 + 3*a^2*b^8*x^15 + 60/7*a^3*b^7*x^14 + 210/13*a^4*b^6*x^13 + 21*a^5*b^5*x^12 + 210/11*a^6*b^4*x^11 + 12*a^7*b^3*x^10 + 5*a^8*b^2*x^9 + 5/4*a^9*b*x^8 + 1/7*a^10*x^7

mupad [B] time = 0.12, size = 112, normalized size = 1.00

$$\frac{a^{10}x^7}{7} + \frac{5a^9bx^8}{4} + 5a^8b^2x^9 + 12a^7b^3x^{10} + \frac{210a^6b^4x^{11}}{11} + 21a^5b^5x^{12} + \frac{210a^4b^6x^{13}}{13} + \frac{60a^3b^7x^{14}}{7} + 3a^2b^8x^{15} + \frac{5ab^9x^{16}}{8} + \frac{b^{10}x^{17}}{17}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6*(a + b*x)^10,x)

[Out] (a^10*x^7)/7 + (b^10*x^17)/17 + (5*a^9*b*x^8)/4 + (5*a*b^9*x^16)/8 + 5*a^8*b^2*x^9 + 12*a^7*b^3*x^10 + (210*a^6*b^4*x^11)/11 + 21*a^5*b^5*x^12 + (210*a^4*b^6*x^13)/13 + (60*a^3*b^7*x^14)/7 + 3*a^2*b^8*x^15

sympy [A] time = 0.10, size = 128, normalized size = 1.14

$$\frac{a^{10}x^7}{7} + \frac{5a^9bx^8}{4} + 5a^8b^2x^9 + 12a^7b^3x^{10} + \frac{210a^6b^4x^{11}}{11} + 21a^5b^5x^{12} + \frac{210a^4b^6x^{13}}{13} + \frac{60a^3b^7x^{14}}{7} + 3a^2b^8x^{15} + \frac{5ab^9x^{16}}{8} + \frac{b^{10}x^{17}}{17}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6*(b*x+a)**10,x)

[Out] a**10*x**7/7 + 5*a**9*b*x**8/4 + 5*a**8*b**2*x**9 + 12*a**7*b**3*x**10 + 210*a**6*b**4*x**11/11 + 21*a**5*b**5*x**12 + 210*a**4*b**6*x**13/13 + 60*a**3*b**7*x**14/7 + 3*a**2*b**8*x**15 + 5*a*b**9*x**16/8 + b**10*x**17/17

3.129 $\int x^5(a + bx)^{10} dx$

Optimal. Leaf size=98

$$-\frac{a^5(a + bx)^{11}}{11b^6} + \frac{5a^4(a + bx)^{12}}{12b^6} - \frac{10a^3(a + bx)^{13}}{13b^6} + \frac{5a^2(a + bx)^{14}}{7b^6} + \frac{(a + bx)^{16}}{16b^6} - \frac{a(a + bx)^{15}}{3b^6}$$

[Out] $-1/11*a^5*(b*x+a)^{11}/b^6+5/12*a^4*(b*x+a)^{12}/b^6-10/13*a^3*(b*x+a)^{13}/b^6+5/7*a^2*(b*x+a)^{14}/b^6-1/16*(b*x+a)^{16}/b^6-1/3*a*(b*x+a)^{15}/b^6$

Rubi [A] time = 0.05, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{5a^2(a + bx)^{14}}{7b^6} - \frac{10a^3(a + bx)^{13}}{13b^6} + \frac{5a^4(a + bx)^{12}}{12b^6} - \frac{a^5(a + bx)^{11}}{11b^6} + \frac{(a + bx)^{16}}{16b^6} - \frac{a(a + bx)^{15}}{3b^6}$$

Antiderivative was successfully verified.

[In] Int[x^5*(a + b*x)^10, x]

[Out] $-(a^5*(a + b*x)^{11})/(11*b^6) + (5*a^4*(a + b*x)^{12})/(12*b^6) - (10*a^3*(a + b*x)^{13})/(13*b^6) + (5*a^2*(a + b*x)^{14})/(7*b^6) - (a*(a + b*x)^{15})/(3*b^6) + (a + b*x)^{16}/(16*b^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^5(a + bx)^{10} dx &= \int \left(-\frac{a^5(a + bx)^{10}}{b^5} + \frac{5a^4(a + bx)^{11}}{b^5} - \frac{10a^3(a + bx)^{12}}{b^5} + \frac{10a^2(a + bx)^{13}}{b^5} - \frac{5a(a + bx)^{14}}{b^5} + \frac{(a + bx)^{15}}{b^5} \right) dx \\ &= -\frac{a^5(a + bx)^{11}}{11b^6} + \frac{5a^4(a + bx)^{12}}{12b^6} - \frac{10a^3(a + bx)^{13}}{13b^6} + \frac{5a^2(a + bx)^{14}}{7b^6} - \frac{a(a + bx)^{15}}{3b^6} + \frac{(a + bx)^{16}}{16b^6} \end{aligned}$$

Mathematica [A] time = 0.00, size = 132, normalized size = 1.35

$$\frac{a^{10}x^6}{6} + \frac{10}{7}a^9bx^7 + \frac{45}{8}a^8b^2x^8 + \frac{40}{3}a^7b^3x^9 + 21a^6b^4x^{10} + \frac{252}{11}a^5b^5x^{11} + \frac{35}{2}a^4b^6x^{12} + \frac{120}{13}a^3b^7x^{13} + \frac{45}{14}a^2b^8x^{14} + \frac{2}{3}ab^9x^{15} + \frac{b^{10}x^{16}}{16}$$

Antiderivative was successfully verified.

[In] Integrate[x^5*(a + b*x)^10,x]

[Out] $(a^{10}x^6)/6 + (10*a^9*b*x^7)/7 + (45*a^8*b^2*x^8)/8 + (40*a^7*b^3*x^9)/3 + 21*a^6*b^4*x^{10} + (252*a^5*b^5*x^{11})/11 + (35*a^4*b^6*x^{12})/2 + (120*a^3*b^7*x^{13})/13 + (45*a^2*b^8*x^{14})/14 + (2*a*b^9*x^{15})/3 + (b^{10}*x^{16})/16$

fricas [A] time = 0.42, size = 112, normalized size = 1.14

$$\frac{1}{16}x^{16}b^{10} + \frac{2}{3}x^{15}b^9a + \frac{45}{14}x^{14}b^8a^2 + \frac{120}{13}x^{13}b^7a^3 + \frac{35}{2}x^{12}b^6a^4 + \frac{252}{11}x^{11}b^5a^5 + 21x^{10}b^4a^6 + \frac{40}{3}x^9b^3a^7 + \frac{45}{8}x^8b^2a^8 + \frac{10}{7}x^7b^1a^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^10,x, algorithm="fricas")

[Out] $1/16*x^{16}*b^{10} + 2/3*x^{15}*b^9*a + 45/14*x^{14}*b^8*a^2 + 120/13*x^{13}*b^7*a^3 + 35/2*x^{12}*b^6*a^4 + 252/11*x^{11}*b^5*a^5 + 21*x^{10}*b^4*a^6 + 40/3*x^9*b^3*a^7 + 45/8*x^8*b^2*a^8 + 10/7*x^7*b*a^9 + 1/6*x^6*a^{10}$

giac [A] time = 1.14, size = 112, normalized size = 1.14

$$\frac{1}{16}b^{10}x^{16} + \frac{2}{3}ab^9x^{15} + \frac{45}{14}a^2b^8x^{14} + \frac{120}{13}a^3b^7x^{13} + \frac{35}{2}a^4b^6x^{12} + \frac{252}{11}a^5b^5x^{11} + 21a^6b^4x^{10} + \frac{40}{3}a^7b^3x^9 + \frac{45}{8}a^8b^2x^8 + \frac{10}{7}a^9b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^10,x, algorithm="giac")

[Out] $1/16*b^{10}*x^{16} + 2/3*a*b^9*x^{15} + 45/14*a^2*b^8*x^{14} + 120/13*a^3*b^7*x^{13} + 35/2*a^4*b^6*x^{12} + 252/11*a^5*b^5*x^{11} + 21*a^6*b^4*x^{10} + 40/3*a^7*b^3*x^9 + 45/8*a^8*b^2*x^8 + 10/7*a^9*b*x^7 + 1/6*a^{10}*x^6$

maple [A] time = 0.00, size = 113, normalized size = 1.15

$$\frac{1}{16}b^{10}x^{16} + \frac{2}{3}ab^9x^{15} + \frac{45}{14}a^2b^8x^{14} + \frac{120}{13}a^3b^7x^{13} + \frac{35}{2}a^4b^6x^{12} + \frac{252}{11}a^5b^5x^{11} + 21a^6b^4x^{10} + \frac{40}{3}a^7b^3x^9 + \frac{45}{8}a^8b^2x^8 + \frac{10}{7}a^9b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5*(b*x+a)^10,x)

[Out] $1/16*b^{10}*x^{16} + 2/3*a*b^9*x^{15} + 45/14*a^2*b^8*x^{14} + 120/13*a^3*b^7*x^{13} + 35/2*a^4*b^6*x^{12} + 252/11*a^5*b^5*x^{11} + 21*a^6*b^4*x^{10} + 40/3*a^7*b^3*x^9 + 45/8*a^8*b^2*x^8 + 10/7*a^9*b*x^7 + 1/6*a^{10}*x^6$

maxima [A] time = 1.36, size = 112, normalized size = 1.14

$$\frac{1}{16}b^{10}x^{16} + \frac{2}{3}ab^9x^{15} + \frac{45}{14}a^2b^8x^{14} + \frac{120}{13}a^3b^7x^{13} + \frac{35}{2}a^4b^6x^{12} + \frac{252}{11}a^5b^5x^{11} + 21a^6b^4x^{10} + \frac{40}{3}a^7b^3x^9 + \frac{45}{8}a^8b^2x^8 + \frac{10}{7}a^9b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x⁵*(b*x+a)¹⁰,x, algorithm="maxima")

[Out] 1/16*b¹⁰*x¹⁶ + 2/3*a*b⁹*x¹⁵ + 45/14*a²*b⁸*x¹⁴ + 120/13*a³*b⁷*x¹³
+ 35/2*a⁴*b⁶*x¹² + 252/11*a⁵*b⁵*x¹¹ + 21*a⁶*b⁴*x¹⁰ + 40/3*a⁷*b³*
x⁹ + 45/8*a⁸*b²*x⁸ + 10/7*a⁹*b*x⁷ + 1/6*a¹⁰*x⁶

mupad [B] time = 0.12, size = 112, normalized size = 1.14

$$\frac{a^{10}x^6}{6} + \frac{10a^9bx^7}{7} + \frac{45a^8b^2x^8}{8} + \frac{40a^7b^3x^9}{3} + 21a^6b^4x^{10} + \frac{252a^5b^5x^{11}}{11} + \frac{35a^4b^6x^{12}}{2} + \frac{120a^3b^7x^{13}}{13} + \frac{45a^2b^8x^{14}}{14}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x⁵*(a + b*x)¹⁰,x)

[Out] (a¹⁰*x⁶)/6 + (b¹⁰*x¹⁶)/16 + (10*a⁹*b*x⁷)/7 + (2*a*b⁹*x¹⁵)/3 + (45*a⁸*
b²*x⁸)/8 + (40*a⁷*b³*x⁹)/3 + 21*a⁶*b⁴*x¹⁰ + (252*a⁵*b⁵*x¹¹)/11 + (35*a⁴*
b⁶*x¹²)/2 + (120*a³*b⁷*x¹³)/13 + (45*a²*b⁸*x¹⁴)/14

sympy [A] time = 0.10, size = 133, normalized size = 1.36

$$\frac{a^{10}x^6}{6} + \frac{10a^9bx^7}{7} + \frac{45a^8b^2x^8}{8} + \frac{40a^7b^3x^9}{3} + 21a^6b^4x^{10} + \frac{252a^5b^5x^{11}}{11} + \frac{35a^4b^6x^{12}}{2} + \frac{120a^3b^7x^{13}}{13} + \frac{45a^2b^8x^{14}}{14} + \frac{2ab^9x^{15}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5*(b*x+a)**10,x)

[Out] a**10*x**6/6 + 10*a**9*b*x**7/7 + 45*a**8*b**2*x**8/8 + 40*a**7*b**3*x**9/3
+ 21*a**6*b**4*x**10 + 252*a**5*b**5*x**11/11 + 35*a**4*b**6*x**12/2 + 120
*a**3*b**7*x**13/13 + 45*a**2*b**8*x**14/14 + 2*a*b**9*x**15/3 + b**10*x**16/16

3.130 $\int x^4(a + bx)^{10} dx$

Optimal. Leaf size=81

$$\frac{a^4(a + bx)^{11}}{11b^5} - \frac{a^3(a + bx)^{12}}{3b^5} + \frac{6a^2(a + bx)^{13}}{13b^5} + \frac{(a + bx)^{15}}{15b^5} - \frac{2a(a + bx)^{14}}{7b^5}$$

[Out] $1/11*a^4*(b*x+a)^{11}/b^5-1/3*a^3*(b*x+a)^{12}/b^5+6/13*a^2*(b*x+a)^{13}/b^5-2/7*a*(b*x+a)^{14}/b^5+1/15*(b*x+a)^{15}/b^5$

Rubi [A] time = 0.04, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{6a^2(a + bx)^{13}}{13b^5} - \frac{a^3(a + bx)^{12}}{3b^5} + \frac{a^4(a + bx)^{11}}{11b^5} + \frac{(a + bx)^{15}}{15b^5} - \frac{2a(a + bx)^{14}}{7b^5}$$

Antiderivative was successfully verified.

[In] Int[x^4*(a + b*x)^10, x]

[Out] $(a^4*(a + b*x)^{11})/(11*b^5) - (a^3*(a + b*x)^{12})/(3*b^5) + (6*a^2*(a + b*x)^{13})/(13*b^5) - (2*a*(a + b*x)^{14})/(7*b^5) + (a + b*x)^{15}/(15*b^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^4(a + bx)^{10} dx &= \int \left(\frac{a^4(a + bx)^{10}}{b^4} - \frac{4a^3(a + bx)^{11}}{b^4} + \frac{6a^2(a + bx)^{12}}{b^4} - \frac{4a(a + bx)^{13}}{b^4} + \frac{(a + bx)^{14}}{b^4} \right) dx \\ &= \frac{a^4(a + bx)^{11}}{11b^5} - \frac{a^3(a + bx)^{12}}{3b^5} + \frac{6a^2(a + bx)^{13}}{13b^5} - \frac{2a(a + bx)^{14}}{7b^5} + \frac{(a + bx)^{15}}{15b^5} \end{aligned}$$

Mathematica [A] time = 0.00, size = 130, normalized size = 1.60

$$\frac{a^{10}x^5}{5} + \frac{5}{3}a^9bx^6 + \frac{45}{7}a^8b^2x^7 + 15a^7b^3x^8 + \frac{70}{3}a^6b^4x^9 + \frac{126}{5}a^5b^5x^{10} + \frac{210}{11}a^4b^6x^{11} + 10a^3b^7x^{12} + \frac{45}{13}a^2b^8x^{13} + \frac{5}{7}ab^9x^{14} + \frac{b^{10}x^{15}}{15}$$

Antiderivative was successfully verified.

[In] Integrate[x^4*(a + b*x)^10,x]

[Out] $(a^{10}x^5)/5 + (5a^9bx^6)/3 + (45a^8b^2x^7)/7 + 15a^7b^3x^8 + (70a^6b^4x^9)/3 + (126a^5b^5x^{10})/5 + (210a^4b^6x^{11})/11 + 10a^3b^7x^{12} + (45a^2b^8x^{13})/13 + (5ab^9x^{14})/7 + (b^{10}x^{15})/15$

fricas [A] time = 0.43, size = 112, normalized size = 1.38

$$\frac{1}{15}x^{15}b^{10} + \frac{5}{7}x^{14}b^9a + \frac{45}{13}x^{13}b^8a^2 + 10x^{12}b^7a^3 + \frac{210}{11}x^{11}b^6a^4 + \frac{126}{5}x^{10}b^5a^5 + \frac{70}{3}x^9b^4a^6 + 15x^8b^3a^7 + \frac{45}{7}x^7b^2a^8 + \frac{5}{3}x^6ba^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^10,x, algorithm="fricas")

[Out] $1/15*x^{15}*b^{10} + 5/7*x^{14}*b^9*a + 45/13*x^{13}*b^8*a^2 + 10*x^{12}*b^7*a^3 + 210/11*x^{11}*b^6*a^4 + 126/5*x^{10}*b^5*a^5 + 70/3*x^9*b^4*a^6 + 15*x^8*b^3*a^7 + 45/7*x^7*b^2*a^8 + 5/3*x^6*b*a^9 + 1/5*x^5*a^{10}$

giac [A] time = 1.06, size = 112, normalized size = 1.38

$$\frac{1}{15}b^{10}x^{15} + \frac{5}{7}ab^9x^{14} + \frac{45}{13}a^2b^8x^{13} + 10a^3b^7x^{12} + \frac{210}{11}a^4b^6x^{11} + \frac{126}{5}a^5b^5x^{10} + \frac{70}{3}a^6b^4x^9 + 15a^7b^3x^8 + \frac{45}{7}a^8b^2x^7 + \frac{5}{3}a^9bx^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^10,x, algorithm="giac")

[Out] $1/15*b^{10}*x^{15} + 5/7*a*b^9*x^{14} + 45/13*a^2*b^8*x^{13} + 10*a^3*b^7*x^{12} + 210/11*a^4*b^6*x^{11} + 126/5*a^5*b^5*x^{10} + 70/3*a^6*b^4*x^9 + 15*a^7*b^3*x^8 + 45/7*a^8*b^2*x^7 + 5/3*a^9*b*x^6 + 1/5*a^{10}*x^5$

maple [A] time = 0.00, size = 113, normalized size = 1.40

$$\frac{1}{15}b^{10}x^{15} + \frac{5}{7}ab^9x^{14} + \frac{45}{13}a^2b^8x^{13} + 10a^3b^7x^{12} + \frac{210}{11}a^4b^6x^{11} + \frac{126}{5}a^5b^5x^{10} + \frac{70}{3}a^6b^4x^9 + 15a^7b^3x^8 + \frac{45}{7}a^8b^2x^7 + \frac{5}{3}a^9bx^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*(b*x+a)^10,x)

[Out] $1/15*b^{10}*x^{15} + 5/7*a*b^9*x^{14} + 45/13*a^2*b^8*x^{13} + 10*a^3*b^7*x^{12} + 210/11*a^4*b^6*x^{11} + 126/5*a^5*b^5*x^{10} + 70/3*a^6*b^4*x^9 + 15*a^7*b^3*x^8 + 45/7*a^8*b^2*x^7 + 5/3*a^9*b*x^6 + 1/5*a^{10}*x^5$

maxima [A] time = 1.29, size = 112, normalized size = 1.38

$$\frac{1}{15}b^{10}x^{15} + \frac{5}{7}ab^9x^{14} + \frac{45}{13}a^2b^8x^{13} + 10a^3b^7x^{12} + \frac{210}{11}a^4b^6x^{11} + \frac{126}{5}a^5b^5x^{10} + \frac{70}{3}a^6b^4x^9 + 15a^7b^3x^8 + \frac{45}{7}a^8b^2x^7 + \frac{5}{3}a^9bx^6$$

3.131 $\int x^3(a + bx)^{10} dx$

Optimal. Leaf size=64

$$-\frac{a^3(a + bx)^{11}}{11b^4} + \frac{a^2(a + bx)^{12}}{4b^4} + \frac{(a + bx)^{14}}{14b^4} - \frac{3a(a + bx)^{13}}{13b^4}$$

[Out] $-1/11*a^3*(b*x+a)^{11}/b^4+1/4*a^2*(b*x+a)^{12}/b^4-3/13*a*(b*x+a)^{13}/b^4+1/14*(b*x+a)^{14}/b^4$

Rubi [A] time = 0.04, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2(a + bx)^{12}}{4b^4} - \frac{a^3(a + bx)^{11}}{11b^4} + \frac{(a + bx)^{14}}{14b^4} - \frac{3a(a + bx)^{13}}{13b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^10, x]

[Out] $-(a^3*(a + b*x)^{11})/(11*b^4) + (a^2*(a + b*x)^{12})/(4*b^4) - (3*a*(a + b*x)^{13})/(13*b^4) + (a + b*x)^{14}/(14*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^{10} dx &= \int \left(-\frac{a^3(a + bx)^{10}}{b^3} + \frac{3a^2(a + bx)^{11}}{b^3} - \frac{3a(a + bx)^{12}}{b^3} + \frac{(a + bx)^{13}}{b^3} \right) dx \\ &= -\frac{a^3(a + bx)^{11}}{11b^4} + \frac{a^2(a + bx)^{12}}{4b^4} - \frac{3a(a + bx)^{13}}{13b^4} + \frac{(a + bx)^{14}}{14b^4} \end{aligned}$$

Mathematica [A] time = 0.00, size = 128, normalized size = 2.00

$$\frac{a^{10}x^4}{4} + 2a^9bx^5 + \frac{15}{2}a^8b^2x^6 + \frac{120}{7}a^7b^3x^7 + \frac{105}{4}a^6b^4x^8 + 28a^5b^5x^9 + 21a^4b^6x^{10} + \frac{120}{11}a^3b^7x^{11} + \frac{15}{4}a^2b^8x^{12} + \frac{10}{13}ab^9x^{13} + \dots$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^10,x]

[Out] (a^10*x^4)/4 + 2*a^9*b*x^5 + (15*a^8*b^2*x^6)/2 + (120*a^7*b^3*x^7)/7 + (105*a^6*b^4*x^8)/4 + 28*a^5*b^5*x^9 + 21*a^4*b^6*x^10 + (120*a^3*b^7*x^11)/11 + (15*a^2*b^8*x^12)/4 + (10*a*b^9*x^13)/13 + (b^10*x^14)/14

fricas [A] time = 0.40, size = 112, normalized size = 1.75

$$\frac{1}{14}x^{14}b^{10} + \frac{10}{13}x^{13}b^9a + \frac{15}{4}x^{12}b^8a^2 + \frac{120}{11}x^{11}b^7a^3 + 21x^{10}b^6a^4 + 28x^9b^5a^5 + \frac{105}{4}x^8b^4a^6 + \frac{120}{7}x^7b^3a^7 + \frac{15}{2}x^6b^2a^8 + 2x^5ba^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^10,x, algorithm="fricas")

[Out] 1/14*x^14*b^10 + 10/13*x^13*b^9*a + 15/4*x^12*b^8*a^2 + 120/11*x^11*b^7*a^3 + 21*x^10*b^6*a^4 + 28*x^9*b^5*a^5 + 105/4*x^8*b^4*a^6 + 120/7*x^7*b^3*a^7 + 15/2*x^6*b^2*a^8 + 2*x^5*b*a^9 + 1/4*x^4*a^10

giac [A] time = 1.09, size = 112, normalized size = 1.75

$$\frac{1}{14}b^{10}x^{14} + \frac{10}{13}ab^9x^{13} + \frac{15}{4}a^2b^8x^{12} + \frac{120}{11}a^3b^7x^{11} + 21a^4b^6x^{10} + 28a^5b^5x^9 + \frac{105}{4}a^6b^4x^8 + \frac{120}{7}a^7b^3x^7 + \frac{15}{2}a^8b^2x^6 + 2a^9bx^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^10,x, algorithm="giac")

[Out] 1/14*b^10*x^14 + 10/13*a*b^9*x^13 + 15/4*a^2*b^8*x^12 + 120/11*a^3*b^7*x^11 + 21*a^4*b^6*x^10 + 28*a^5*b^5*x^9 + 105/4*a^6*b^4*x^8 + 120/7*a^7*b^3*x^7 + 15/2*a^8*b^2*x^6 + 2*a^9*b*x^5 + 1/4*a^10*x^4

maple [A] time = 0.00, size = 113, normalized size = 1.77

$$\frac{1}{14}b^{10}x^{14} + \frac{10}{13}ab^9x^{13} + \frac{15}{4}a^2b^8x^{12} + \frac{120}{11}a^3b^7x^{11} + 21a^4b^6x^{10} + 28a^5b^5x^9 + \frac{105}{4}a^6b^4x^8 + \frac{120}{7}a^7b^3x^7 + \frac{15}{2}a^8b^2x^6 + 2a^9bx^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^10,x)

[Out] 1/14*b^10*x^14+10/13*a*b^9*x^13+15/4*a^2*b^8*x^12+120/11*a^3*b^7*x^11+21*a^4*b^6*x^10+28*a^5*b^5*x^9+105/4*a^6*b^4*x^8+120/7*a^7*b^3*x^7+15/2*a^8*b^2*x^6+2*a^9*b*x^5+1/4*a^10*x^4

maxima [A] time = 1.36, size = 112, normalized size = 1.75

$$\frac{1}{14}b^{10}x^{14} + \frac{10}{13}ab^9x^{13} + \frac{15}{4}a^2b^8x^{12} + \frac{120}{11}a^3b^7x^{11} + 21a^4b^6x^{10} + 28a^5b^5x^9 + \frac{105}{4}a^6b^4x^8 + \frac{120}{7}a^7b^3x^7 + \frac{15}{2}a^8b^2x^6 + 2a^9bx^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^10,x, algorithm="maxima")

[Out] $1/14*b^{10}*x^{14} + 10/13*a*b^9*x^{13} + 15/4*a^2*b^8*x^{12} + 120/11*a^3*b^7*x^{11}$
 $+ 21*a^4*b^6*x^{10} + 28*a^5*b^5*x^9 + 105/4*a^6*b^4*x^8 + 120/7*a^7*b^3*x^7$
 $+ 15/2*a^8*b^2*x^6 + 2*a^9*b*x^5 + 1/4*a^{10}*x^4$

mupad [B] time = 0.12, size = 112, normalized size = 1.75

$$\frac{a^{10}x^4}{4} + 2a^9bx^5 + \frac{15a^8b^2x^6}{2} + \frac{120a^7b^3x^7}{7} + \frac{105a^6b^4x^8}{4} + 28a^5b^5x^9 + 21a^4b^6x^{10} + \frac{120a^3b^7x^{11}}{11} + \frac{15a^2b^8x^{12}}{4} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(a + b*x)^10,x)

[Out] $(a^{10}*x^4)/4 + (b^{10}*x^{14})/14 + 2*a^9*b*x^5 + (10*a*b^9*x^{13})/13 + (15*a^8*$
 $b^2*x^6)/2 + (120*a^7*b^3*x^7)/7 + (105*a^6*b^4*x^8)/4 + 28*a^5*b^5*x^9 + 2$
 $1*a^4*b^6*x^{10} + (120*a^3*b^7*x^{11})/11 + (15*a^2*b^8*x^{12})/4$

sympy [B] time = 0.12, size = 129, normalized size = 2.02

$$\frac{a^{10}x^4}{4} + 2a^9bx^5 + \frac{15a^8b^2x^6}{2} + \frac{120a^7b^3x^7}{7} + \frac{105a^6b^4x^8}{4} + 28a^5b^5x^9 + 21a^4b^6x^{10} + \frac{120a^3b^7x^{11}}{11} + \frac{15a^2b^8x^{12}}{4} + \frac{10ab^9x^{13}}{13} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**10,x)

[Out] $a^{10}*x^{14}/4 + 2*a^9*b*x^{13} + 15*a^8*b^2*x^{12}/2 + 120*a^7*b^3*x^{11}/7 +$
 $105*a^6*b^4*x^{10}/4 + 28*a^5*b^5*x^9 + 21*a^4*b^6*x^{10} + 120*a^3*b^7*x^{11}/11 +$
 $15*a^2*b^8*x^{12}/4 + 10*a*b^9*x^{13}/13 + b^{10}*x^{14}/14$

3.132 $\int x^2(a + bx)^{10} dx$

Optimal. Leaf size=47

$$\frac{a^2(a + bx)^{11}}{11b^3} + \frac{(a + bx)^{13}}{13b^3} - \frac{a(a + bx)^{12}}{6b^3}$$

[Out] $1/11*a^2*(b*x+a)^{11}/b^3-1/6*a*(b*x+a)^{12}/b^3+1/13*(b*x+a)^{13}/b^3$

Rubi [A] time = 0.03, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2(a + bx)^{11}}{11b^3} + \frac{(a + bx)^{13}}{13b^3} - \frac{a(a + bx)^{12}}{6b^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*(a + b*x)^{10}, x]$

[Out] $(a^2*(a + b*x)^{11})/(11*b^3) - (a*(a + b*x)^{12})/(6*b^3) + (a + b*x)^{13}/(13*b^3)$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0])) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^{10} dx &= \int \left(\frac{a^2(a + bx)^{10}}{b^2} - \frac{2a(a + bx)^{11}}{b^2} + \frac{(a + bx)^{12}}{b^2} \right) dx \\ &= \frac{a^2(a + bx)^{11}}{11b^3} - \frac{a(a + bx)^{12}}{6b^3} + \frac{(a + bx)^{13}}{13b^3} \end{aligned}$$

Mathematica [B] time = 0.00, size = 126, normalized size = 2.68

$$\frac{a^{10}x^3}{3} + \frac{5}{2}a^9bx^4 + 9a^8b^2x^5 + 20a^7b^3x^6 + 30a^6b^4x^7 + \frac{63}{2}a^5b^5x^8 + \frac{70}{3}a^4b^6x^9 + 12a^3b^7x^{10} + \frac{45}{11}a^2b^8x^{11} + \frac{5}{6}ab^9x^{12} + \frac{b^{10}x^{13}}{13}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^10,x]

[Out] $(a^{10}x^3)/3 + (5a^9b^2x^4)/2 + 9a^8b^3x^5 + 20a^7b^4x^6 + 30a^6b^5x^7 + (63a^5b^6x^8)/2 + (70a^4b^7x^9)/3 + 12a^3b^8x^{10} + (45a^2b^9x^{11})/11 + (5ab^{10}x^{12})/6 + (b^{11}x^{13})/13$

fricas [B] time = 0.41, size = 112, normalized size = 2.38

$$\frac{1}{13}x^{13}b^{10} + \frac{5}{6}x^{12}b^9a + \frac{45}{11}x^{11}b^8a^2 + 12x^{10}b^7a^3 + \frac{70}{3}x^9b^6a^4 + \frac{63}{2}x^8b^5a^5 + 30x^7b^4a^6 + 20x^6b^3a^7 + 9x^5b^2a^8 + \frac{5}{2}x^4ba^9 + \frac{1}{3}x^3a^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^10,x, algorithm="fricas")

[Out] $1/13*x^{13}*b^{10} + 5/6*x^{12}*b^9*a + 45/11*x^{11}*b^8*a^2 + 12*x^{10}*b^7*a^3 + 70/3*x^9*b^6*a^4 + 63/2*x^8*b^5*a^5 + 30*x^7*b^4*a^6 + 20*x^6*b^3*a^7 + 9*x^5*b^2*a^8 + 5/2*x^4*b*a^9 + 1/3*x^3*a^{10}$

giac [B] time = 1.18, size = 112, normalized size = 2.38

$$\frac{1}{13}b^{10}x^{13} + \frac{5}{6}ab^9x^{12} + \frac{45}{11}a^2b^8x^{11} + 12a^3b^7x^{10} + \frac{70}{3}a^4b^6x^9 + \frac{63}{2}a^5b^5x^8 + 30a^6b^4x^7 + 20a^7b^3x^6 + 9a^8b^2x^5 + \frac{5}{2}a^9bx^4 + \frac{1}{3}a^{10}x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^10,x, algorithm="giac")

[Out] $1/13*b^{10}*x^{13} + 5/6*a*b^9*x^{12} + 45/11*a^2*b^8*x^{11} + 12*a^3*b^7*x^{10} + 70/3*a^4*b^6*x^9 + 63/2*a^5*b^5*x^8 + 30*a^6*b^4*x^7 + 20*a^7*b^3*x^6 + 9*a^8*b^2*x^5 + 5/2*a^9*b*x^4 + 1/3*a^{10}*x^3$

maple [B] time = 0.00, size = 113, normalized size = 2.40

$$\frac{1}{13}b^{10}x^{13} + \frac{5}{6}ab^9x^{12} + \frac{45}{11}a^2b^8x^{11} + 12a^3b^7x^{10} + \frac{70}{3}a^4b^6x^9 + \frac{63}{2}a^5b^5x^8 + 30a^6b^4x^7 + 20a^7b^3x^6 + 9a^8b^2x^5 + \frac{5}{2}a^9bx^4 + \frac{1}{3}a^{10}x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^10,x)

[Out] $1/13*b^{10}*x^{13} + 5/6*a*b^9*x^{12} + 45/11*a^2*b^8*x^{11} + 12*a^3*b^7*x^{10} + 70/3*a^4*b^6*x^9 + 63/2*a^5*b^5*x^8 + 30*a^6*b^4*x^7 + 20*a^7*b^3*x^6 + 9*a^8*b^2*x^5 + 5/2*a^9*b*x^4 + 1/3*a^{10}*x^3$

maxima [B] time = 1.37, size = 112, normalized size = 2.38

$$\frac{1}{13}b^{10}x^{13} + \frac{5}{6}ab^9x^{12} + \frac{45}{11}a^2b^8x^{11} + 12a^3b^7x^{10} + \frac{70}{3}a^4b^6x^9 + \frac{63}{2}a^5b^5x^8 + 30a^6b^4x^7 + 20a^7b^3x^6 + 9a^8b^2x^5 + \frac{5}{2}a^9bx^4 + \frac{1}{3}a^{10}x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^10,x, algorithm="maxima")

[Out] $1/13*b^{10}*x^{13} + 5/6*a*b^9*x^{12} + 45/11*a^2*b^8*x^{11} + 12*a^3*b^7*x^{10} + 70/3*a^4*b^6*x^9 + 63/2*a^5*b^5*x^8 + 30*a^6*b^4*x^7 + 20*a^7*b^3*x^6 + 9*a^8*b^2*x^5 + 5/2*a^9*b*x^4 + 1/3*a^{10}*x^3$

mupad [B] time = 0.07, size = 31, normalized size = 0.66

$$\frac{(a + bx)^{11} (8a^2 - 88abx + 528b^2x^2)}{6864b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a + b*x)^10,x)

[Out] $((a + b*x)^{11}*(8*a^2 + 528*b^2*x^2 - 88*a*b*x))/(6864*b^3)$

sympy [B] time = 0.11, size = 128, normalized size = 2.72

$$\frac{a^{10}x^3}{3} + \frac{5a^9bx^4}{2} + 9a^8b^2x^5 + 20a^7b^3x^6 + 30a^6b^4x^7 + \frac{63a^5b^5x^8}{2} + \frac{70a^4b^6x^9}{3} + 12a^3b^7x^{10} + \frac{45a^2b^8x^{11}}{11} + \frac{5ab^9x^{12}}{6} + \frac{b^{10}x^{13}}{13}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)**10,x)

[Out] $a^{10}*x^{13}/3 + 5*a^9*b*x^{12}/2 + 9*a^8*b^2*x^{11} + 20*a^7*b^3*x^{10} + 30*a^6*b^4*x^9 + 63*a^5*b^5*x^8/2 + 70*a^4*b^6*x^7/3 + 12*a^3*b^7*x^{10} + 45*a^2*b^8*x^{11}/11 + 5*a*b^9*x^{12}/6 + b^{10}*x^{13}/13$

3.133 $\int x(a + bx)^{10} dx$

Optimal. Leaf size=30

$$\frac{(a + bx)^{12}}{12b^2} - \frac{a(a + bx)^{11}}{11b^2}$$

[Out] $-1/11*a*(b*x+a)^{11}/b^2+1/12*(b*x+a)^{12}/b^2$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{(a + bx)^{12}}{12b^2} - \frac{a(a + bx)^{11}}{11b^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^10, x]

[Out] $-(a*(a + b*x)^{11})/(11*b^2) + (a + b*x)^{12}/(12*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x(a + bx)^{10} dx &= \int \left(-\frac{a(a + bx)^{10}}{b} + \frac{(a + bx)^{11}}{b} \right) dx \\ &= -\frac{a(a + bx)^{11}}{11b^2} + \frac{(a + bx)^{12}}{12b^2} \end{aligned}$$

Mathematica [B] time = 0.00, size = 128, normalized size = 4.27

$$\frac{a^{10}x^2}{2} + \frac{10}{3}a^9bx^3 + \frac{45}{4}a^8b^2x^4 + 24a^7b^3x^5 + 35a^6b^4x^6 + 36a^5b^5x^7 + \frac{105}{4}a^4b^6x^8 + \frac{40}{3}a^3b^7x^9 + \frac{9}{2}a^2b^8x^{10} + \frac{10}{11}ab^9x^{11} + \frac{b^{10}x^{12}}{12}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^10, x]

[Out] $(a^{10}x^2)/2 + (10a^9bx^3)/3 + (45a^8b^2x^4)/4 + 24a^7b^3x^5 + 35a^6b^4x^6 + 36a^5b^5x^7 + (105a^4b^6x^8)/4 + (40a^3b^7x^9)/3 + (9a^2b^8x^{10})/2 + (10ab^9x^{11})/11 + (b^{10}x^{12})/12$

fricas [B] time = 0.38, size = 112, normalized size = 3.73

$$\frac{1}{12}x^{12}b^{10} + \frac{10}{11}x^{11}b^9a + \frac{9}{2}x^{10}b^8a^2 + \frac{40}{3}x^9b^7a^3 + \frac{105}{4}x^8b^6a^4 + 36x^7b^5a^5 + 35x^6b^4a^6 + 24x^5b^3a^7 + \frac{45}{4}x^4b^2a^8 + \frac{10}{3}x^3ba^9 + \frac{1}{2}x^2a^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^10,x, algorithm="fricas")

[Out] $1/12*x^{12}*b^{10} + 10/11*x^{11}*b^9*a + 9/2*x^{10}*b^8*a^2 + 40/3*x^9*b^7*a^3 + 105/4*x^8*b^6*a^4 + 36*x^7*b^5*a^5 + 35*x^6*b^4*a^6 + 24*x^5*b^3*a^7 + 45/4*x^4*b^2*a^8 + 10/3*x^3*b*a^9 + 1/2*x^2*a^{10}$

giac [B] time = 1.44, size = 112, normalized size = 3.73

$$\frac{1}{12}b^{10}x^{12} + \frac{10}{11}ab^9x^{11} + \frac{9}{2}a^2b^8x^{10} + \frac{40}{3}a^3b^7x^9 + \frac{105}{4}a^4b^6x^8 + 36a^5b^5x^7 + 35a^6b^4x^6 + 24a^7b^3x^5 + \frac{45}{4}a^8b^2x^4 + \frac{10}{3}a^9bx^3 + \frac{1}{2}a^{10}x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^10,x, algorithm="giac")

[Out] $1/12*b^{10}*x^{12} + 10/11*a*b^9*x^{11} + 9/2*a^2*b^8*x^{10} + 40/3*a^3*b^7*x^9 + 105/4*a^4*b^6*x^8 + 36*a^5*b^5*x^7 + 35*a^6*b^4*x^6 + 24*a^7*b^3*x^5 + 45/4*a^8*b^2*x^4 + 10/3*a^9*b*x^3 + 1/2*a^{10}*x^2$

maple [B] time = 0.00, size = 113, normalized size = 3.77

$$\frac{1}{12}b^{10}x^{12} + \frac{10}{11}ab^9x^{11} + \frac{9}{2}a^2b^8x^{10} + \frac{40}{3}a^3b^7x^9 + \frac{105}{4}a^4b^6x^8 + 36a^5b^5x^7 + 35a^6b^4x^6 + 24a^7b^3x^5 + \frac{45}{4}a^8b^2x^4 + \frac{10}{3}a^9bx^3 + \frac{1}{2}a^{10}x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^10,x)

[Out] $1/12*b^{10}*x^{12} + 10/11*a*b^9*x^{11} + 9/2*a^2*b^8*x^{10} + 40/3*a^3*b^7*x^9 + 105/4*a^4*b^6*x^8 + 36*a^5*b^5*x^7 + 35*a^6*b^4*x^6 + 24*a^7*b^3*x^5 + 45/4*a^8*b^2*x^4 + 10/3*a^9*b*x^3 + 1/2*a^{10}*x^2$

maxima [B] time = 1.35, size = 112, normalized size = 3.73

$$\frac{1}{12}b^{10}x^{12} + \frac{10}{11}ab^9x^{11} + \frac{9}{2}a^2b^8x^{10} + \frac{40}{3}a^3b^7x^9 + \frac{105}{4}a^4b^6x^8 + 36a^5b^5x^7 + 35a^6b^4x^6 + 24a^7b^3x^5 + \frac{45}{4}a^8b^2x^4 + \frac{10}{3}a^9bx^3 + \frac{1}{2}a^{10}x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^10,x, algorithm="maxima")

[Out] $1/12*b^{10}*x^{12} + 10/11*a*b^9*x^{11} + 9/2*a^2*b^8*x^{10} + 40/3*a^3*b^7*x^9 + 105/4*a^4*b^6*x^8 + 36*a^5*b^5*x^7 + 35*a^6*b^4*x^6 + 24*a^7*b^3*x^5 + 45/4*a^8*b^2*x^4 + 10/3*a^9*b*x^3 + 1/2*a^{10}*x^2$

mupad [B] time = 0.09, size = 25, normalized size = 0.83

$$-\frac{2 \left(\frac{a(a+bx)^{11}}{22} - \frac{(a+bx)^{12}}{24} \right)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a + b*x)^10,x)

[Out] $-(2*((a*(a + b*x)^{11})/22 - (a + b*x)^{12}/24))/b^2$

sympy [B] time = 0.11, size = 129, normalized size = 4.30

$$\frac{a^{10}x^2}{2} + \frac{10a^9bx^3}{3} + \frac{45a^8b^2x^4}{4} + 24a^7b^3x^5 + 35a^6b^4x^6 + 36a^5b^5x^7 + \frac{105a^4b^6x^8}{4} + \frac{40a^3b^7x^9}{3} + \frac{9a^2b^8x^{10}}{2} + \frac{10ab^9x^{11}}{11} + \frac{b^{10}x^{12}}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)**10,x)

[Out] $a^{10}*x^{12}/2 + 10*a^9*b*x^{11}/3 + 45*a^8*b^2*x^{10}/4 + 24*a^7*b^3*x^9 + 35*a^6*b^4*x^8 + 36*a^5*b^5*x^7 + 105*a^4*b^6*x^6/4 + 40*a^3*b^7*x^5 + 9*a^2*b^8*x^4/2 + 10*a*b^9*x^3/3 + 9*a^2*b^8*x^{10}/2 + 10*a*b^9*x^{11}/11 + b^{10}*x^{12}/12$

3.134 $\int (a + bx)^{10} dx$

Optimal. Leaf size=14

$$\frac{(a + bx)^{11}}{11b}$$

[Out] 1/11*(b*x+a)^11/b

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(a + bx)^{11}}{11b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10,x]

[Out] (a + b*x)^11/(11*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^{10} dx = \frac{(a + bx)^{11}}{11b}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{(a + bx)^{11}}{11b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10,x]

[Out] (a + b*x)^11/(11*b)

fricas [B] time = 0.38, size = 108, normalized size = 7.71

$$\frac{1}{11}x^{11}b^{10} + x^{10}b^9a + 5x^9b^8a^2 + 15x^8b^7a^3 + 30x^7b^6a^4 + 42x^6b^5a^5 + 42x^5b^4a^6 + 30x^4b^3a^7 + 15x^3b^2a^8 + 5x^2ba^9 + xa^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10,x, algorithm="fricas")

[Out] $1/11*x^{11}*b^{10} + x^{10}*b^9*a + 5*x^9*b^8*a^2 + 15*x^8*b^7*a^3 + 30*x^7*b^6*a^4 + 42*x^6*b^5*a^5 + 42*x^5*b^4*a^6 + 30*x^4*b^3*a^7 + 15*x^3*b^2*a^8 + 5*x^2*b*a^9 + x*a^{10}$

giac [A] time = 1.16, size = 12, normalized size = 0.86

$$\frac{(bx + a)^{11}}{11b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10,x, algorithm="giac")

[Out] $1/11*(b*x + a)^{11}/b$

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{(bx + a)^{11}}{11b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10,x)

[Out] $1/11*(b*x+a)^{11}/b$

maxima [A] time = 1.33, size = 12, normalized size = 0.86

$$\frac{(bx + a)^{11}}{11b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10,x, algorithm="maxima")

[Out] $1/11*(b*x + a)^{11}/b$

mupad [B] time = 0.11, size = 108, normalized size = 7.71

$$a^{10}x + 5a^9bx^2 + 15a^8b^2x^3 + 30a^7b^3x^4 + 42a^6b^4x^5 + 42a^5b^5x^6 + 30a^4b^6x^7 + 15a^3b^7x^8 + 5a^2b^8x^9 + ab^9x^{10} + \frac{b^{10}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^10,x)`

[Out] $a^{10}x + (b^{10}x^{11})/11 + 5a^9bx^2 + a^9b^2x^3 + 15a^8b^2x^3 + 30a^7b^3x^4 + 42a^6b^4x^5 + 42a^5b^5x^6 + 30a^4b^6x^7 + 15a^3b^7x^8 + 5a^2b^8x^9$

sympy [B] time = 0.11, size = 114, normalized size = 8.14

$$a^{10}x + 5a^9bx^2 + 15a^8b^2x^3 + 30a^7b^3x^4 + 42a^6b^4x^5 + 42a^5b^5x^6 + 30a^4b^6x^7 + 15a^3b^7x^8 + 5a^2b^8x^9 + ab^9x^{10} + \frac{b^{10}x^{11}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**10,x)`

[Out] $a^{10}x + 5a^9bx^2 + 15a^8b^2x^3 + 30a^7b^3x^4 + 42a^6b^4x^5 + 42a^5b^5x^6 + 30a^4b^6x^7 + 15a^3b^7x^8 + 5a^2b^8x^9 + a^9bx^{10} + \frac{b^{10}x^{11}}{11}$

$$3.135 \quad \int \frac{(a+bx)^{10}}{x} dx$$

Optimal. Leaf size=122

$$a^{10} \log(x) + 10a^9bx + \frac{45}{2}a^8b^2x^2 + 40a^7b^3x^3 + \frac{105}{2}a^6b^4x^4 + \frac{252}{5}a^5b^5x^5 + 35a^4b^6x^6 + \frac{120}{7}a^3b^7x^7 + \frac{45}{8}a^2b^8x^8 + \frac{10}{9}ab^9x^9 +$$

[Out] $10*a^9*b*x + 45/2*a^8*b^2*x^2 + 40*a^7*b^3*x^3 + 105/2*a^6*b^4*x^4 + 252/5*a^5*b^5*x^5 + 35*a^4*b^6*x^6 + 120/7*a^3*b^7*x^7 + 45/8*a^2*b^8*x^8 + 10/9*a*b^9*x^9 + 1/10*b^10*x^10 + a^10*\ln(x)$

Rubi [A] time = 0.04, antiderivative size = 122, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{45}{2}a^8b^2x^2 + 40a^7b^3x^3 + \frac{105}{2}a^6b^4x^4 + \frac{252}{5}a^5b^5x^5 + 35a^4b^6x^6 + \frac{120}{7}a^3b^7x^7 + \frac{45}{8}a^2b^8x^8 + 10a^9bx + a^{10} \log(x) + \frac{10}{9}ab^9x^9 +$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x, x]

[Out] $10*a^9*b*x + (45*a^8*b^2*x^2)/2 + 40*a^7*b^3*x^3 + (105*a^6*b^4*x^4)/2 + (252*a^5*b^5*x^5)/5 + 35*a^4*b^6*x^6 + (120*a^3*b^7*x^7)/7 + (45*a^2*b^8*x^8)/8 + (10*a*b^9*x^9)/9 + (b^10*x^10)/10 + a^10*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x} dx = \int \left(10a^9b + \frac{a^{10}}{x} + 45a^8b^2x + 120a^7b^3x^2 + 210a^6b^4x^3 + 252a^5b^5x^4 + 210a^4b^6x^5 + 120a^3b^7x^6 + 45a^2b^8x^7 + 10ab^9x^8 + \frac{b^{10}}{x} \right) dx$$

$$= 10a^9bx + \frac{45}{2}a^8b^2x^2 + 40a^7b^3x^3 + \frac{105}{2}a^6b^4x^4 + \frac{252}{5}a^5b^5x^5 + 35a^4b^6x^6 + \frac{120}{7}a^3b^7x^7 + \frac{45}{8}a^2b^8x^8 + \frac{10}{9}ab^9x^9 + \frac{b^{10}}{10} \log(x)$$

Mathematica [A] time = 0.00, size = 122, normalized size = 1.00

$$a^{10} \log(x) + 10a^9bx + \frac{45}{2}a^8b^2x^2 + 40a^7b^3x^3 + \frac{105}{2}a^6b^4x^4 + \frac{252}{5}a^5b^5x^5 + 35a^4b^6x^6 + \frac{120}{7}a^3b^7x^7 + \frac{45}{8}a^2b^8x^8 + \frac{10}{9}ab^9x^9 +$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x,x]

[Out] $10*a^9*b*x + (45*a^8*b^2*x^2)/2 + 40*a^7*b^3*x^3 + (105*a^6*b^4*x^4)/2 + (52*a^5*b^5*x^5)/5 + 35*a^4*b^6*x^6 + (120*a^3*b^7*x^7)/7 + (45*a^2*b^8*x^8)/8 + (10*a*b^9*x^9)/9 + (b^{10}*x^{10})/10 + a^{10}*Log[x]$

fricas [A] time = 0.44, size = 108, normalized size = 0.89

$$\frac{1}{10} b^{10} x^{10} + \frac{10}{9} a b^9 x^9 + \frac{45}{8} a^2 b^8 x^8 + \frac{120}{7} a^3 b^7 x^7 + 35 a^4 b^6 x^6 + \frac{252}{5} a^5 b^5 x^5 + \frac{105}{2} a^6 b^4 x^4 + 40 a^7 b^3 x^3 + \frac{45}{2} a^8 b^2 x^2 + 10 a^9 b x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x,x, algorithm="fricas")

[Out] $1/10*b^{10}*x^{10} + 10/9*a*b^9*x^9 + 45/8*a^2*b^8*x^8 + 120/7*a^3*b^7*x^7 + 35*a^4*b^6*x^6 + 252/5*a^5*b^5*x^5 + 105/2*a^6*b^4*x^4 + 40*a^7*b^3*x^3 + 45/2*a^8*b^2*x^2 + 10*a^9*b*x + a^{10}*log(x)$

giac [A] time = 1.08, size = 109, normalized size = 0.89

$$\frac{1}{10} b^{10} x^{10} + \frac{10}{9} a b^9 x^9 + \frac{45}{8} a^2 b^8 x^8 + \frac{120}{7} a^3 b^7 x^7 + 35 a^4 b^6 x^6 + \frac{252}{5} a^5 b^5 x^5 + \frac{105}{2} a^6 b^4 x^4 + 40 a^7 b^3 x^3 + \frac{45}{2} a^8 b^2 x^2 + 10 a^9 b x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x,x, algorithm="giac")

[Out] $1/10*b^{10}*x^{10} + 10/9*a*b^9*x^9 + 45/8*a^2*b^8*x^8 + 120/7*a^3*b^7*x^7 + 35*a^4*b^6*x^6 + 252/5*a^5*b^5*x^5 + 105/2*a^6*b^4*x^4 + 40*a^7*b^3*x^3 + 45/2*a^8*b^2*x^2 + 10*a^9*b*x + a^{10}*log(abs(x))$

maple [A] time = 0.00, size = 109, normalized size = 0.89

$$\frac{b^{10}x^{10}}{10} + \frac{10ab^9x^9}{9} + \frac{45a^2b^8x^8}{8} + \frac{120a^3b^7x^7}{7} + 35a^4b^6x^6 + \frac{252a^5b^5x^5}{5} + \frac{105a^6b^4x^4}{2} + 40a^7b^3x^3 + \frac{45a^8b^2x^2}{2} + a^{10}\ln(x) + 10a^9bx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x,x)

[Out] $10*a^9*b*x+45/2*a^8*b^2*x^2+40*a^7*b^3*x^3+105/2*a^6*b^4*x^4+252/5*a^5*b^5*x^5+35*a^4*b^6*x^6+120/7*a^3*b^7*x^7+45/8*a^2*b^8*x^8+10/9*a*b^9*x^9+1/10*b^{10}*x^{10}+a^{10}*ln(x)$

maxima [A] time = 1.39, size = 108, normalized size = 0.89

$$\frac{1}{10} b^{10} x^{10} + \frac{10}{9} a b^9 x^9 + \frac{45}{8} a^2 b^8 x^8 + \frac{120}{7} a^3 b^7 x^7 + 35 a^4 b^6 x^6 + \frac{252}{5} a^5 b^5 x^5 + \frac{105}{2} a^6 b^4 x^4 + 40 a^7 b^3 x^3 + \frac{45}{2} a^8 b^2 x^2 + 10 a^9 b x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x,x, algorithm="maxima")

[Out] $1/10*b^{10}*x^{10} + 10/9*a*b^9*x^9 + 45/8*a^2*b^8*x^8 + 120/7*a^3*b^7*x^7 + 35*a^4*b^6*x^6 + 252/5*a^5*b^5*x^5 + 105/2*a^6*b^4*x^4 + 40*a^7*b^3*x^3 + 45/2*a^8*b^2*x^2 + 10*a^9*b*x + a^{10}*\log(x)$

mupad [B] time = 0.08, size = 108, normalized size = 0.89

$$a^{10} \ln(x) + \frac{b^{10} x^{10}}{10} + \frac{10 a b^9 x^9}{9} + \frac{45 a^2 b^8 x^8}{2} + 40 a^3 b^7 x^7 + \frac{105 a^4 b^6 x^6}{2} + \frac{252 a^5 b^5 x^5}{5} + 35 a^6 b^4 x^4 + \frac{120 a^7 b^3 x^3}{7} + \frac{45 a^8 b^2 x^2}{2} + 10 a^9 b x + a^{10} \ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x,x)

[Out] $a^{10}*\log(x) + (b^{10}*x^{10})/10 + (10*a*b^9*x^9)/9 + (45*a^8*b^2*x^2)/2 + 40*a^7*b^3*x^3 + (105*a^6*b^4*x^4)/2 + (252*a^5*b^5*x^5)/5 + 35*a^4*b^6*x^6 + (120*a^3*b^7*x^7)/7 + (45*a^2*b^8*x^8)/8 + 10*a^9*b*x$

sympy [A] time = 0.26, size = 126, normalized size = 1.03

$$a^{10} \log(x) + 10 a^9 b x + \frac{45 a^8 b^2 x^2}{2} + 40 a^7 b^3 x^3 + \frac{105 a^6 b^4 x^4}{2} + \frac{252 a^5 b^5 x^5}{5} + 35 a^4 b^6 x^6 + \frac{120 a^3 b^7 x^7}{7} + \frac{45 a^2 b^8 x^8}{8} + \frac{10 a b^9 x^9}{9} + a^{10} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x,x)

[Out] $a^{10}*\log(x) + 10*a^{9}*b*x + 45*a^{8}*b^{2}*x^{2}/2 + 40*a^{7}*b^{3}*x^{3} + 105*a^{6}*b^{4}*x^{4}/2 + 252*a^{5}*b^{5}*x^{5}/5 + 35*a^{4}*b^{6}*x^{6} + 120*a^{3}*b^{7}*x^{7}/7 + 45*a^{2}*b^{8}*x^{8}/8 + 10*a*b^{9}*x^{9}/9 + b^{10}*x^{10}/10$

$$3.136 \quad \int \frac{(a+bx)^{10}}{x^2} dx$$

Optimal. Leaf size=115

$$-\frac{a^{10}}{x} + 10a^9b \log(x) + 45a^8b^2x + 60a^7b^3x^2 + 70a^6b^4x^3 + 63a^5b^5x^4 + 42a^4b^6x^5 + 20a^3b^7x^6 + \frac{45}{7}a^2b^8x^7 + \frac{5}{4}ab^9x^8 + \frac{b^{10}x^9}{9}$$

[Out] $-a^{10}/x + 45*a^8*b^2*x + 60*a^7*b^3*x^2 + 70*a^6*b^4*x^3 + 63*a^5*b^5*x^4 + 42*a^4*b^6*x^5 + 20*a^3*b^7*x^6 + 45/7*a^2*b^8*x^7 + 5/4*a*b^9*x^8 + 1/9*b^{10}*x^9 + 10*a^9*b*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$60a^7b^3x^2 + 70a^6b^4x^3 + 63a^5b^5x^4 + 42a^4b^6x^5 + 20a^3b^7x^6 + \frac{45}{7}a^2b^8x^7 + 45a^8b^2x + 10a^9b \log(x) - \frac{a^{10}}{x} + \frac{5}{4}ab^9x^8 + \frac{b^{10}x^9}{9}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^2, x]

[Out] $-(a^{10}/x) + 45*a^8*b^2*x + 60*a^7*b^3*x^2 + 70*a^6*b^4*x^3 + 63*a^5*b^5*x^4 + 42*a^4*b^6*x^5 + 20*a^3*b^7*x^6 + (45*a^2*b^8*x^7)/7 + (5*a*b^9*x^8)/4 + (b^{10}*x^9)/9 + 10*a^9*b*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^{10}}{x^2} dx &= \int \left(45a^8b^2 + \frac{a^{10}}{x^2} + \frac{10a^9b}{x} + 120a^7b^3x + 210a^6b^4x^2 + 252a^5b^5x^3 + 210a^4b^6x^4 + 120a^3b^7x^5 + \dots \right) dx \\ &= -\frac{a^{10}}{x} + 45a^8b^2x + 60a^7b^3x^2 + 70a^6b^4x^3 + 63a^5b^5x^4 + 42a^4b^6x^5 + 20a^3b^7x^6 + \frac{45}{7}a^2b^8x^7 + \frac{5}{4}ab^9x^8 + \frac{b^{10}x^9}{9} \end{aligned}$$

Mathematica [A] time = 0.01, size = 115, normalized size = 1.00

$$-\frac{a^{10}}{x} + 10a^9b \log(x) + 45a^8b^2x + 60a^7b^3x^2 + 70a^6b^4x^3 + 63a^5b^5x^4 + 42a^4b^6x^5 + 20a^3b^7x^6 + \frac{45}{7}a^2b^8x^7 + \frac{5}{4}ab^9x^8 + \frac{b^{10}x^9}{9}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^2,x]

[Out] $-(a^{10}/x) + 45*a^8*b^2*x + 60*a^7*b^3*x^2 + 70*a^6*b^4*x^3 + 63*a^5*b^5*x^4 + 42*a^4*b^6*x^5 + 20*a^3*b^7*x^6 + (45*a^2*b^8*x^7)/7 + (5*a*b^9*x^8)/4 + (b^{10}*x^9)/9 + 10*a^9*b*\text{Log}[x]$

fricas [A] time = 0.47, size = 114, normalized size = 0.99

$$\frac{28 b^{10} x^{10} + 315 a b^9 x^9 + 1620 a^2 b^8 x^8 + 5040 a^3 b^7 x^7 + 10584 a^4 b^6 x^6 + 15876 a^5 b^5 x^5 + 17640 a^6 b^4 x^4 + 15120 a^7 b^3 x^3 + 11340 a^8 b^2 x^2 + 2520 a^9 b x - 252 a^{10}}{252 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^2,x, algorithm="fricas")

[Out] $1/252*(28*b^{10}*x^{10} + 315*a*b^9*x^9 + 1620*a^2*b^8*x^8 + 5040*a^3*b^7*x^7 + 10584*a^4*b^6*x^6 + 15876*a^5*b^5*x^5 + 17640*a^6*b^4*x^4 + 15120*a^7*b^3*x^3 + 11340*a^8*b^2*x^2 + 2520*a^9*b*x*\log(x) - 252*a^{10})/x$

giac [A] time = 0.96, size = 110, normalized size = 0.96

$$\frac{1}{9} b^{10} x^9 + \frac{5}{4} a b^9 x^8 + \frac{45}{7} a^2 b^8 x^7 + 20 a^3 b^7 x^6 + 42 a^4 b^6 x^5 + 63 a^5 b^5 x^4 + 70 a^6 b^4 x^3 + 60 a^7 b^3 x^2 + 45 a^8 b^2 x + 10 a^9 b \log(|x|) - \frac{a^{10}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^2,x, algorithm="giac")

[Out] $1/9*b^{10}*x^9 + 5/4*a*b^9*x^8 + 45/7*a^2*b^8*x^7 + 20*a^3*b^7*x^6 + 42*a^4*b^6*x^5 + 63*a^5*b^5*x^4 + 70*a^6*b^4*x^3 + 60*a^7*b^3*x^2 + 45*a^8*b^2*x + 10*a^9*b*\log(\text{abs}(x)) - a^{10}/x$

maple [A] time = 0.01, size = 110, normalized size = 0.96

$$\frac{b^{10} x^9}{9} + \frac{5 a b^9 x^8}{4} + \frac{45 a^2 b^8 x^7}{7} + 20 a^3 b^7 x^6 + 42 a^4 b^6 x^5 + 63 a^5 b^5 x^4 + 70 a^6 b^4 x^3 + 60 a^7 b^3 x^2 + 10 a^9 b \ln(x) + 45 a^8 b^2 x - \frac{a^{10}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^2,x)

[Out] $-a^{10}/x + 45*a^8*b^2*x + 60*a^7*b^3*x^2 + 70*a^6*b^4*x^3 + 63*a^5*b^5*x^4 + 42*a^4*b^6*x^5 + 20*a^3*b^7*x^6 + 45/7*a^2*b^8*x^7 + 5/4*a*b^9*x^8 + 1/9*b^{10}*x^9 + 10*a^9*b*\ln(x)$

maxima [A] time = 1.35, size = 109, normalized size = 0.95

$$\frac{1}{9} b^{10} x^9 + \frac{5}{4} a b^9 x^8 + \frac{45}{7} a^2 b^8 x^7 + 20 a^3 b^7 x^6 + 42 a^4 b^6 x^5 + 63 a^5 b^5 x^4 + 70 a^6 b^4 x^3 + 60 a^7 b^3 x^2 + 45 a^8 b^2 x + 10 a^9 b \log(x) - \frac{a^{10}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^2,x, algorithm="maxima")

[Out] 1/9*b^10*x^9 + 5/4*a*b^9*x^8 + 45/7*a^2*b^8*x^7 + 20*a^3*b^7*x^6 + 42*a^4*b^6*x^5 + 63*a^5*b^5*x^4 + 70*a^6*b^4*x^3 + 60*a^7*b^3*x^2 + 45*a^8*b^2*x + 10*a^9*b*log(x) - a^10/x

mupad [B] time = 0.12, size = 109, normalized size = 0.95

$$\frac{b^{10} x^9}{9} - \frac{a^{10}}{x} + 45 a^8 b^2 x + \frac{5 a b^9 x^8}{4} + 10 a^9 b \ln(x) + 60 a^7 b^3 x^2 + 70 a^6 b^4 x^3 + 63 a^5 b^5 x^4 + 42 a^4 b^6 x^5 + 20 a^3 b^7 x^6 + \frac{45 a^{10}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^2,x)

[Out] (b^10*x^9)/9 - a^10/x + 45*a^8*b^2*x + (5*a*b^9*x^8)/4 + 10*a^9*b*log(x) + 60*a^7*b^3*x^2 + 70*a^6*b^4*x^3 + 63*a^5*b^5*x^4 + 42*a^4*b^6*x^5 + 20*a^3*b^7*x^6 + (45*a^2*b^8*x^7)/7

sympy [A] time = 0.27, size = 117, normalized size = 1.02

$$-\frac{a^{10}}{x} + 10 a^9 b \log(x) + 45 a^8 b^2 x + 60 a^7 b^3 x^2 + 70 a^6 b^4 x^3 + 63 a^5 b^5 x^4 + 42 a^4 b^6 x^5 + 20 a^3 b^7 x^6 + \frac{45 a^2 b^8 x^7}{7} + \frac{5 a b^9 x^8}{4} + \frac{b^{10} x^9}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**2,x)

[Out] -a**10/x + 10*a**9*b*log(x) + 45*a**8*b**2*x + 60*a**7*b**3*x**2 + 70*a**6*b**4*x**3 + 63*a**5*b**5*x**4 + 42*a**4*b**6*x**5 + 20*a**3*b**7*x**6 + 45*a**2*b**8*x**7/7 + 5*a*b**9*x**8/4 + b**10*x**9/9

$$3.137 \quad \int \frac{(a+bx)^{10}}{x^3} dx$$

Optimal. Leaf size=119

$$-\frac{a^{10}}{2x^2} - \frac{10a^9b}{x} + 45a^8b^2 \log(x) + 120a^7b^3x + 105a^6b^4x^2 + 84a^5b^5x^3 + \frac{105}{2}a^4b^6x^4 + 24a^3b^7x^5 + \frac{15}{2}a^2b^8x^6 + \frac{10}{7}ab^9x^7 + \frac{b^{10}}{8}x^8$$

[Out] $-1/2*a^{10}/x^2-10*a^9*b/x+120*a^7*b^3*x+105*a^6*b^4*x^2+84*a^5*b^5*x^3+105/2*a^4*b^6*x^4+24*a^3*b^7*x^5+15/2*a^2*b^8*x^6+10/7*a*b^9*x^7+1/8*b^{10}*x^8+45*a^8*b^2*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$105a^6b^4x^2+84a^5b^5x^3+\frac{105}{2}a^4b^6x^4+24a^3b^7x^5+\frac{15}{2}a^2b^8x^6+120a^7b^3x+45a^8b^2 \log(x)-\frac{10a^9b}{x}-\frac{a^{10}}{2x^2}+\frac{10}{7}ab^9x^7+\frac{b^{10}x^8}{8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^3, x]

[Out] $-a^{10}/(2*x^2) - (10*a^9*b)/x + 120*a^7*b^3*x + 105*a^6*b^4*x^2 + 84*a^5*b^5*x^3 + (105*a^4*b^6*x^4)/2 + 24*a^3*b^7*x^5 + (15*a^2*b^8*x^6)/2 + (10*a*b^9*x^7)/7 + (b^{10}*x^8)/8 + 45*a^8*b^2*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^3} dx = \int \left(120a^7b^3 + \frac{a^{10}}{x^3} + \frac{10a^9b}{x^2} + \frac{45a^8b^2}{x} + 210a^6b^4x + 252a^5b^5x^2 + 210a^4b^6x^3 + 120a^3b^7x^4 + 42a^2b^8x^5 + 10ab^9x^6 + \frac{b^{10}}{8}x^7 \right) dx$$

$$= -\frac{a^{10}}{2x^2} - \frac{10a^9b}{x} + 120a^7b^3x + 105a^6b^4x^2 + 84a^5b^5x^3 + \frac{105}{2}a^4b^6x^4 + 24a^3b^7x^5 + \frac{15}{2}a^2b^8x^6 + \frac{10}{7}ab^9x^7 + \frac{b^{10}x^8}{8}$$

Mathematica [A] time = 0.01, size = 119, normalized size = 1.00

$$-\frac{a^{10}}{2x^2} - \frac{10a^9b}{x} + 45a^8b^2 \log(x) + 120a^7b^3x + 105a^6b^4x^2 + 84a^5b^5x^3 + \frac{105}{2}a^4b^6x^4 + 24a^3b^7x^5 + \frac{15}{2}a^2b^8x^6 + \frac{10}{7}ab^9x^7 + \frac{b^{10}}{8}x^8$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^3, x]

[Out] $-1/2*a^{10}/x^2 - (10*a^9*b)/x + 120*a^7*b^3*x + 105*a^6*b^4*x^2 + 84*a^5*b^5*x^3 + (105*a^4*b^6*x^4)/2 + 24*a^3*b^7*x^5 + (15*a^2*b^8*x^6)/2 + (10*a*b^9*x^7)/7 + (b^{10}*x^8)/8 + 45*a^8*b^2*\text{Log}[x]$

fricas [A] time = 0.45, size = 114, normalized size = 0.96

$$\frac{7b^{10}x^{10} + 80ab^9x^9 + 420a^2b^8x^8 + 1344a^3b^7x^7 + 2940a^4b^6x^6 + 4704a^5b^5x^5 + 5880a^6b^4x^4 + 6720a^7b^3x^3 + 2520a^8b^2x^2 + 28a^9bx + a^{10}}{56x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^3, x, algorithm="fricas")

[Out] $1/56*(7*b^{10}*x^{10} + 80*a*b^9*x^9 + 420*a^2*b^8*x^8 + 1344*a^3*b^7*x^7 + 2940*a^4*b^6*x^6 + 4704*a^5*b^5*x^5 + 5880*a^6*b^4*x^4 + 6720*a^7*b^3*x^3 + 2520*a^8*b^2*x^2*\log(x) - 560*a^9*b*x - 28*a^{10})/x^2$

giac [A] time = 0.93, size = 109, normalized size = 0.92

$$\frac{1}{8}b^{10}x^8 + \frac{10}{7}ab^9x^7 + \frac{15}{2}a^2b^8x^6 + 24a^3b^7x^5 + \frac{105}{2}a^4b^6x^4 + 84a^5b^5x^3 + 105a^6b^4x^2 + 120a^7b^3x + 45a^8b^2 \log(|x|) - \frac{20a^9b}{2x} - \frac{a^{10}}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^3, x, algorithm="giac")

[Out] $1/8*b^{10}*x^8 + 10/7*a*b^9*x^7 + 15/2*a^2*b^8*x^6 + 24*a^3*b^7*x^5 + 105/2*a^4*b^6*x^4 + 84*a^5*b^5*x^3 + 105*a^6*b^4*x^2 + 120*a^7*b^3*x + 45*a^8*b^2*\log(\text{abs}(x)) - 1/2*(20*a^9*b*x + a^{10})/x^2$

maple [A] time = 0.01, size = 110, normalized size = 0.92

$$\frac{b^{10}x^8}{8} + \frac{10ab^9x^7}{7} + \frac{15a^2b^8x^6}{2} + 24a^3b^7x^5 + \frac{105a^4b^6x^4}{2} + 84a^5b^5x^3 + 105a^6b^4x^2 + 45a^8b^2 \ln(x) + 120a^7b^3x - \frac{10a^9b}{x} - \frac{a^{10}}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^3, x)

[Out] $-1/2*a^{10}/x^2 - 10*a^9*b/x + 120*a^7*b^3*x + 105*a^6*b^4*x^2 + 84*a^5*b^5*x^3 + 105/2*a^4*b^6*x^4 + 24*a^3*b^7*x^5 + 15/2*a^2*b^8*x^6 + 10/7*a*b^9*x^7 + 1/8*b^{10}*x^8 + 45*a^8*b^2*\ln(x)$

maxima [A] time = 1.44, size = 108, normalized size = 0.91

$$\frac{1}{8} b^{10} x^8 + \frac{10}{7} a b^9 x^7 + \frac{15}{2} a^2 b^8 x^6 + 24 a^3 b^7 x^5 + \frac{105}{2} a^4 b^6 x^4 + 84 a^5 b^5 x^3 + 105 a^6 b^4 x^2 + 120 a^7 b^3 x + 45 a^8 b^2 \log(x) - \frac{20 a^9 b}{2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^3,x, algorithm="maxima")

[Out] 1/8*b^10*x^8 + 10/7*a*b^9*x^7 + 15/2*a^2*b^8*x^6 + 24*a^3*b^7*x^5 + 105/2*a^4*b^6*x^4 + 84*a^5*b^5*x^3 + 105*a^6*b^4*x^2 + 120*a^7*b^3*x + 45*a^8*b^2*log(x) - 1/2*(20*a^9*b*x + a^10)/x^2

mupad [B] time = 0.07, size = 110, normalized size = 0.92

$$\frac{b^{10} x^8}{8} - \frac{a^{10}}{2} + \frac{10 b x a^9}{x^2} + 120 a^7 b^3 x + \frac{10 a b^9 x^7}{7} + 105 a^6 b^4 x^2 + 84 a^5 b^5 x^3 + \frac{105 a^4 b^6 x^4}{2} + 24 a^3 b^7 x^5 + \frac{15 a^2 b^8 x^6}{2} + 45 a^8 b^2 \log(x) - \frac{20 a^9 b}{2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^3,x)

[Out] (b^10*x^8)/8 - (a^10/2 + 10*a^9*b*x)/x^2 + 120*a^7*b^3*x + (10*a*b^9*x^7)/7 + 105*a^6*b^4*x^2 + 84*a^5*b^5*x^3 + (105*a^4*b^6*x^4)/2 + 24*a^3*b^7*x^5 + (15*a^2*b^8*x^6)/2 + 45*a^8*b^2*log(x)

sympy [A] time = 0.31, size = 122, normalized size = 1.03

$$45 a^8 b^2 \log(x) + 120 a^7 b^3 x + 105 a^6 b^4 x^2 + 84 a^5 b^5 x^3 + \frac{105 a^4 b^6 x^4}{2} + 24 a^3 b^7 x^5 + \frac{15 a^2 b^8 x^6}{2} + \frac{10 a b^9 x^7}{7} + \frac{b^{10} x^8}{8} + \frac{-a^{10} - 20 a^9 b}{2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**3,x)

[Out] 45*a**8*b**2*log(x) + 120*a**7*b**3*x + 105*a**6*b**4*x**2 + 84*a**5*b**5*x**3 + 105*a**4*b**6*x**4/2 + 24*a**3*b**7*x**5 + 15*a**2*b**8*x**6/2 + 10*a**b**9*x**7/7 + b**10*x**8/8 + (-a**10 - 20*a**9*b*x)/(2*x**2)

$$3.138 \quad \int \frac{(a+bx)^{10}}{x^4} dx$$

Optimal. Leaf size=115

$$-\frac{a^{10}}{3x^3} - \frac{5a^9b}{x^2} - \frac{45a^8b^2}{x} + 120a^7b^3 \log(x) + 210a^6b^4x + 126a^5b^5x^2 + 70a^4b^6x^3 + 30a^3b^7x^4 + 9a^2b^8x^5 + \frac{5}{3}ab^9x^6 + \frac{b^{10}x^7}{7}$$

[Out] $-1/3*a^{10}/x^3 - 5*a^9*b/x^2 - 45*a^8*b^2/x + 210*a^6*b^4*x + 126*a^5*b^5*x^2 + 70*a^4*b^6*x^3 + 30*a^3*b^7*x^4 + 9*a^2*b^8*x^5 + 5/3*a*b^9*x^6 + 1/7*b^{10}*x^7 + 120*a^7*b^3*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$126a^5b^5x^2 + 70a^4b^6x^3 + 30a^3b^7x^4 + 9a^2b^8x^5 - \frac{45a^8b^2}{x} + 210a^6b^4x + 120a^7b^3 \log(x) - \frac{5a^9b}{x^2} - \frac{a^{10}}{3x^3} + \frac{5}{3}ab^9x^6 + \frac{b^{10}x^7}{7}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^4, x]

[Out] $-a^{10}/(3*x^3) - (5*a^9*b)/x^2 - (45*a^8*b^2)/x + 210*a^6*b^4*x + 126*a^5*b^5*x^2 + 70*a^4*b^6*x^3 + 30*a^3*b^7*x^4 + 9*a^2*b^8*x^5 + (5*a*b^9*x^6)/3 + (b^{10}*x^7)/7 + 120*a^7*b^3*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^4} dx = \int \left(210a^6b^4 + \frac{a^{10}}{x^4} + \frac{10a^9b}{x^3} + \frac{45a^8b^2}{x^2} + \frac{120a^7b^3}{x} + 252a^5b^5x + 210a^4b^6x^2 + 120a^3b^7x^3 + 45a^2b^8x^4 + 15a^2b^8x^5 + 5ab^9x^6 + \frac{b^{10}x^7}{7} \right) dx$$

$$= -\frac{a^{10}}{3x^3} - \frac{5a^9b}{x^2} - \frac{45a^8b^2}{x} + 210a^6b^4x + 126a^5b^5x^2 + 70a^4b^6x^3 + 30a^3b^7x^4 + 9a^2b^8x^5 + \frac{5}{3}ab^9x^6 + \frac{b^{10}x^7}{7}$$

Mathematica [A] time = 0.01, size = 115, normalized size = 1.00

$$-\frac{a^{10}}{3x^3} - \frac{5a^9b}{x^2} - \frac{45a^8b^2}{x} + 120a^7b^3 \log(x) + 210a^6b^4x + 126a^5b^5x^2 + 70a^4b^6x^3 + 30a^3b^7x^4 + 9a^2b^8x^5 + \frac{5}{3}ab^9x^6 + \frac{b^{10}x^7}{7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^4,x]

[Out] $-1/3*a^{10}/x^3 - (5*a^9*b)/x^2 - (45*a^8*b^2)/x + 210*a^6*b^4*x + 126*a^5*b^5*x^2 + 70*a^4*b^6*x^3 + 30*a^3*b^7*x^4 + 9*a^2*b^8*x^5 + (5*a*b^9*x^6)/3 + (b^{10}*x^7)/7 + 120*a^7*b^3*\text{Log}[x]$

fricas [A] time = 0.43, size = 114, normalized size = 0.99

$$\frac{3b^{10}x^{10} + 35ab^9x^9 + 189a^2b^8x^8 + 630a^3b^7x^7 + 1470a^4b^6x^6 + 2646a^5b^5x^5 + 4410a^6b^4x^4 + 2520a^7b^3x^3 \log(x)}{21x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^4,x, algorithm="fricas")

[Out] $1/21*(3*b^{10}*x^{10} + 35*a*b^9*x^9 + 189*a^2*b^8*x^8 + 630*a^3*b^7*x^7 + 1470*a^4*b^6*x^6 + 2646*a^5*b^5*x^5 + 4410*a^6*b^4*x^4 + 2520*a^7*b^3*x^3*\log(x) - 945*a^8*b^2*x^2 - 105*a^9*b*x - 7*a^{10})/x^3$

giac [A] time = 1.14, size = 109, normalized size = 0.95

$$\frac{1}{7}b^{10}x^7 + \frac{5}{3}ab^9x^6 + 9a^2b^8x^5 + 30a^3b^7x^4 + 70a^4b^6x^3 + 126a^5b^5x^2 + 210a^6b^4x + 120a^7b^3 \log(|x|) - \frac{135a^8b^2x^2 + 15a^9}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^4,x, algorithm="giac")

[Out] $1/7*b^{10}*x^7 + 5/3*a*b^9*x^6 + 9*a^2*b^8*x^5 + 30*a^3*b^7*x^4 + 70*a^4*b^6*x^3 + 126*a^5*b^5*x^2 + 210*a^6*b^4*x + 120*a^7*b^3*\log(\text{abs}(x)) - 1/3*(135*a^8*b^2*x^2 + 15*a^9*b*x + a^{10})/x^3$

maple [A] time = 0.01, size = 110, normalized size = 0.96

$$\frac{b^{10}x^7}{7} + \frac{5ab^9x^6}{3} + 9a^2b^8x^5 + 30a^3b^7x^4 + 70a^4b^6x^3 + 126a^5b^5x^2 + 120a^7b^3 \ln(x) + 210a^6b^4x - \frac{45a^8b^2}{x} - \frac{5a^9b}{x^2} - \frac{a^{10}}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^4,x)

[Out] $-1/3*a^{10}/x^3 - 5*a^9*b/x^2 - 45*a^8*b^2/x + 210*a^6*b^4*x + 126*a^5*b^5*x^2 + 70*a^4*b^6*x^3 + 30*a^3*b^7*x^4 + 9*a^2*b^8*x^5 + 5/3*a*b^9*x^6 + 1/7*b^{10}*x^7 + 120*a^7*b^3*\ln(x)$

maxima [A] time = 1.37, size = 108, normalized size = 0.94

$$\frac{1}{7}b^{10}x^7 + \frac{5}{3}ab^9x^6 + 9a^2b^8x^5 + 30a^3b^7x^4 + 70a^4b^6x^3 + 126a^5b^5x^2 + 210a^6b^4x + 120a^7b^3 \log(x) - \frac{135a^8b^2x^2 + 15a^9bx}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^4,x, algorithm="maxima")

[Out] 1/7*b^10*x^7 + 5/3*a*b^9*x^6 + 9*a^2*b^8*x^5 + 30*a^3*b^7*x^4 + 70*a^4*b^6*x^3 + 126*a^5*b^5*x^2 + 210*a^6*b^4*x + 120*a^7*b^3*log(x) - 1/3*(135*a^8*b^2*x^2 + 15*a^9*b*x + a^10)/x^3

mupad [B] time = 0.06, size = 110, normalized size = 0.96

$$\frac{b^{10}x^7}{7} - \frac{a^{10}}{3} + \frac{5a^9bx + 45a^8b^2x^2}{x^3} + 210a^6b^4x + \frac{5ab^9x^6}{3} + 126a^5b^5x^2 + 70a^4b^6x^3 + 30a^3b^7x^4 + 9a^2b^8x^5 + 120a^7b^3 \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^4,x)

[Out] (b^10*x^7)/7 - (a^10/3 + 45*a^8*b^2*x^2 + 5*a^9*b*x)/x^3 + 210*a^6*b^4*x + (5*a*b^9*x^6)/3 + 126*a^5*b^5*x^2 + 70*a^4*b^6*x^3 + 30*a^3*b^7*x^4 + 9*a^2*b^8*x^5 + 120*a^7*b^3*log(x)

sympy [A] time = 0.34, size = 119, normalized size = 1.03

$$120a^7b^3 \log(x) + 210a^6b^4x + 126a^5b^5x^2 + 70a^4b^6x^3 + 30a^3b^7x^4 + 9a^2b^8x^5 + \frac{5ab^9x^6}{3} + \frac{b^{10}x^7}{7} + \frac{-a^{10} - 15a^9bx - 135a^8b^2x^2}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**4,x)

[Out] 120*a**7*b**3*log(x) + 210*a**6*b**4*x + 126*a**5*b**5*x**2 + 70*a**4*b**6*x**3 + 30*a**3*b**7*x**4 + 9*a**2*b**8*x**5 + 5*a*b**9*x**6/3 + b**10*x**7/7 + (-a**10 - 15*a**9*b*x - 135*a**8*b**2*x**2)/(3*x**3)

$$3.139 \quad \int \frac{(a+bx)^{10}}{x^5} dx$$

Optimal. Leaf size=119

$$-\frac{a^{10}}{4x^4} - \frac{10a^9b}{3x^3} - \frac{45a^8b^2}{2x^2} - \frac{120a^7b^3}{x} + 210a^6b^4 \log(x) + 252a^5b^5x + 105a^4b^6x^2 + 40a^3b^7x^3 + \frac{45}{4}a^2b^8x^4 + 2ab^9x^5 + \frac{b^{10}x^6}{6}$$

[Out] $-1/4*a^{10}/x^4-10/3*a^9*b/x^3-45/2*a^8*b^2/x^2-120*a^7*b^3/x+252*a^5*b^5*x+105*a^4*b^6*x^2+40*a^3*b^7*x^3+45/4*a^2*b^8*x^4+2*a*b^9*x^5+1/6*b^{10}*x^6+210*a^6*b^4*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{45a^8b^2}{2x^2} + 105a^4b^6x^2 + 40a^3b^7x^3 + \frac{45}{4}a^2b^8x^4 - \frac{120a^7b^3}{x} + 252a^5b^5x + 210a^6b^4 \log(x) - \frac{10a^9b}{3x^3} - \frac{a^{10}}{4x^4} + 2ab^9x^5 + \frac{b^{10}x^6}{6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^5, x]

[Out] $-a^{10}/(4*x^4) - (10*a^9*b)/(3*x^3) - (45*a^8*b^2)/(2*x^2) - (120*a^7*b^3)/x + 252*a^5*b^5*x + 105*a^4*b^6*x^2 + 40*a^3*b^7*x^3 + (45*a^2*b^8*x^4)/4 + 2*a*b^9*x^5 + (b^{10}*x^6)/6 + 210*a^6*b^4*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^5} dx = \int \left(252a^5b^5 + \frac{a^{10}}{x^5} + \frac{10a^9b}{x^4} + \frac{45a^8b^2}{x^3} + \frac{120a^7b^3}{x^2} + \frac{210a^6b^4}{x} + 210a^4b^6x + 120a^3b^7x^2 + 45a^2b^8x^3 + \frac{45}{4}a^2b^8x^4 + 2ab^9x^5 + \frac{b^{10}x^6}{6} \right) dx$$

$$= -\frac{a^{10}}{4x^4} - \frac{10a^9b}{3x^3} - \frac{45a^8b^2}{2x^2} - \frac{120a^7b^3}{x} + 252a^5b^5x + 105a^4b^6x^2 + 40a^3b^7x^3 + \frac{45}{4}a^2b^8x^4 + 2ab^9x^5 + \frac{b^{10}x^6}{6}$$

Mathematica [A] time = 0.01, size = 119, normalized size = 1.00

$$-\frac{a^{10}}{4x^4} - \frac{10a^9b}{3x^3} - \frac{45a^8b^2}{2x^2} - \frac{120a^7b^3}{x} + 210a^6b^4 \log(x) + 252a^5b^5x + 105a^4b^6x^2 + 40a^3b^7x^3 + \frac{45}{4}a^2b^8x^4 + 2ab^9x^5 + \frac{b^{10}x^6}{6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^5, x]

[Out] $-1/4*a^{10}/x^4 - (10*a^9*b)/(3*x^3) - (45*a^8*b^2)/(2*x^2) - (120*a^7*b^3)/x + 252*a^5*b^5*x + 105*a^4*b^6*x^2 + 40*a^3*b^7*x^3 + (45*a^2*b^8*x^4)/4 + 2*a*b^9*x^5 + (b^{10}*x^6)/6 + 210*a^6*b^4*\text{Log}[x]$

fricas [A] time = 0.47, size = 114, normalized size = 0.96

$$\frac{2b^{10}x^{10} + 24ab^9x^9 + 135a^2b^8x^8 + 480a^3b^7x^7 + 1260a^4b^6x^6 + 3024a^5b^5x^5 + 2520a^6b^4x^4 \log(x) - 1440a^7b^3x^3}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^5, x, algorithm="fricas")

[Out] $1/12*(2*b^{10}*x^{10} + 24*a*b^9*x^9 + 135*a^2*b^8*x^8 + 480*a^3*b^7*x^7 + 1260*a^4*b^6*x^6 + 3024*a^5*b^5*x^5 + 2520*a^6*b^4*x^4*\log(x) - 1440*a^7*b^3*x^3 - 270*a^8*b^2*x^2 - 40*a^9*b*x - 3*a^{10})/x^4$

giac [A] time = 1.12, size = 111, normalized size = 0.93

$$\frac{1}{6}b^{10}x^6 + 2ab^9x^5 + \frac{45}{4}a^2b^8x^4 + 40a^3b^7x^3 + 105a^4b^6x^2 + 252a^5b^5x + 210a^6b^4 \log(|x|) - \frac{1440a^7b^3x^3 + 270a^8b^2x^2 + 40a^9bx + 3a^{10}}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^5, x, algorithm="giac")

[Out] $1/6*b^{10}*x^6 + 2*a*b^9*x^5 + 45/4*a^2*b^8*x^4 + 40*a^3*b^7*x^3 + 105*a^4*b^6*x^2 + 252*a^5*b^5*x + 210*a^6*b^4*\log(\text{abs}(x)) - 1/12*(1440*a^7*b^3*x^3 + 270*a^8*b^2*x^2 + 40*a^9*b*x + 3*a^{10})/x^4$

maple [A] time = 0.01, size = 110, normalized size = 0.92

$$\frac{b^{10}x^6}{6} + 2ab^9x^5 + \frac{45a^2b^8x^4}{4} + 40a^3b^7x^3 + 105a^4b^6x^2 + 210a^6b^4 \ln(x) + 252a^5b^5x - \frac{120a^7b^3}{x} - \frac{45a^8b^2}{2x^2} - \frac{10a^9b}{3x^3} - \frac{a^{10}}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^5, x)

[Out] $-1/4*a^{10}/x^4 - 10/3*a^9*b/x^3 - 45/2*a^8*b^2/x^2 - 120*a^7*b^3/x + 252*a^5*b^5*x + 105*a^4*b^6*x^2 + 40*a^3*b^7*x^3 + 45/4*a^2*b^8*x^4 + 2*a*b^9*x^5 + 1/6*b^{10}*x^6 + 210*a^6*b^4*\ln(x)$

maxima [A] time = 1.27, size = 110, normalized size = 0.92

$$\frac{1}{6} b^{10} x^6 + 2 a b^9 x^5 + \frac{45}{4} a^2 b^8 x^4 + 40 a^3 b^7 x^3 + 105 a^4 b^6 x^2 + 252 a^5 b^5 x + 210 a^6 b^4 \log(x) - \frac{1440 a^7 b^3 x^3 + 270 a^8 b^2 x^2 + 40 a^9 b x + 3 a^{10}}{12 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^5,x, algorithm="maxima")

[Out] 1/6*b^10*x^6 + 2*a*b^9*x^5 + 45/4*a^2*b^8*x^4 + 40*a^3*b^7*x^3 + 105*a^4*b^6*x^2 + 252*a^5*b^5*x + 210*a^6*b^4*log(x) - 1/12*(1440*a^7*b^3*x^3 + 270*a^8*b^2*x^2 + 40*a^9*b*x + 3*a^10)/x^4

mupad [B] time = 0.10, size = 110, normalized size = 0.92

$$\frac{b^{10} x^6}{6} - \frac{\frac{a^{10}}{4} + \frac{10 a^9 b x}{3} + \frac{45 a^8 b^2 x^2}{2} + 120 a^7 b^3 x^3}{x^4} + 252 a^5 b^5 x + 2 a b^9 x^5 + 105 a^4 b^6 x^2 + 40 a^3 b^7 x^3 + \frac{45 a^2 b^8 x^4}{4} + 210 a^6 b^4 \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^5,x)

[Out] (b^10*x^6)/6 - (a^10/4 + (45*a^8*b^2*x^2)/2 + 120*a^7*b^3*x^3 + (10*a^9*b*x)/3)/x^4 + 252*a^5*b^5*x + 2*a*b^9*x^5 + 105*a^4*b^6*x^2 + 40*a^3*b^7*x^3 + (45*a^2*b^8*x^4)/4 + 210*a^6*b^4*log(x)

sympy [A] time = 0.44, size = 121, normalized size = 1.02

$$210 a^6 b^4 \log(x) + 252 a^5 b^5 x + 105 a^4 b^6 x^2 + 40 a^3 b^7 x^3 + \frac{45 a^2 b^8 x^4}{4} + 2 a b^9 x^5 + \frac{b^{10} x^6}{6} + \frac{-3 a^{10} - 40 a^9 b x - 270 a^8 b^2 x^2 - 1440 a^7 b^3 x^3 - 270 a^8 b^2 x^2 - 40 a^9 b x - 3 a^{10}}{12 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**5,x)

[Out] 210*a**6*b**4*log(x) + 252*a**5*b**5*x + 105*a**4*b**6*x**2 + 40*a**3*b**7*x**3 + 45*a**2*b**8*x**4/4 + 2*a*b**9*x**5 + b**10*x**6/6 + (-3*a**10 - 40*a**9*b*x - 270*a**8*b**2*x**2 - 1440*a**7*b**3*x**3)/(12*x**4)

$$3.140 \quad \int \frac{(a+bx)^{10}}{x^6} dx$$

Optimal. Leaf size=117

$$\frac{a^{10}}{5x^5} - \frac{5a^9b}{2x^4} - \frac{15a^8b^2}{x^3} - \frac{60a^7b^3}{x^2} - \frac{210a^6b^4}{x} + 252a^5b^5 \log(x) + 210a^4b^6x + 60a^3b^7x^2 + 15a^2b^8x^3 + \frac{5}{2}ab^9x^4 + \frac{b^{10}x^5}{5}$$

[Out] $-1/5*a^{10}/x^5 - 5/2*a^9*b/x^4 - 15*a^8*b^2/x^3 - 60*a^7*b^3/x^2 - 210*a^6*b^4/x + 210*a^4*b^6*x + 60*a^3*b^7*x^2 + 15*a^2*b^8*x^3 + 5/2*a*b^9*x^4 + 1/5*b^{10}*x^5 + 252*a^5*b^5*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 117, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{15a^8b^2}{x^3} - \frac{60a^7b^3}{x^2} + 60a^3b^7x^2 + 15a^2b^8x^3 - \frac{210a^6b^4}{x} + 210a^4b^6x + 252a^5b^5 \log(x) - \frac{5a^9b}{2x^4} - \frac{a^{10}}{5x^5} + \frac{5}{2}ab^9x^4 + \frac{b^{10}x^5}{5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^6, x]

[Out] $-a^{10}/(5*x^5) - (5*a^9*b)/(2*x^4) - (15*a^8*b^2)/x^3 - (60*a^7*b^3)/x^2 - (210*a^6*b^4)/x + 210*a^4*b^6*x + 60*a^3*b^7*x^2 + 15*a^2*b^8*x^3 + (5*a*b^9*x^4)/2 + (b^{10}*x^5)/5 + 252*a^5*b^5*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^6} dx = \int \left(210a^4b^6 + \frac{a^{10}}{x^6} + \frac{10a^9b}{x^5} + \frac{45a^8b^2}{x^4} + \frac{120a^7b^3}{x^3} + \frac{210a^6b^4}{x^2} + \frac{252a^5b^5}{x} + 120a^3b^7x + 45a^2b^8x^2 + 15a^2b^8x^3 + \frac{5}{2}ab^9x^4 + \frac{b^{10}x^5}{5} \right) dx$$

$$= -\frac{a^{10}}{5x^5} - \frac{5a^9b}{2x^4} - \frac{15a^8b^2}{x^3} - \frac{60a^7b^3}{x^2} - \frac{210a^6b^4}{x} + 210a^4b^6x + 60a^3b^7x^2 + 15a^2b^8x^3 + \frac{5}{2}ab^9x^4 + \frac{b^{10}x^5}{5}$$

Mathematica [A] time = 0.01, size = 117, normalized size = 1.00

$$\frac{a^{10}}{5x^5} - \frac{5a^9b}{2x^4} - \frac{15a^8b^2}{x^3} - \frac{60a^7b^3}{x^2} - \frac{210a^6b^4}{x} + 252a^5b^5 \log(x) + 210a^4b^6x + 60a^3b^7x^2 + 15a^2b^8x^3 + \frac{5}{2}ab^9x^4 + \frac{b^{10}x^5}{5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^6,x]

[Out] $-1/5*a^{10}/x^5 - (5*a^9*b)/(2*x^4) - (15*a^8*b^2)/x^3 - (60*a^7*b^3)/x^2 - (210*a^6*b^4)/x + 210*a^4*b^6*x + 60*a^3*b^7*x^2 + 15*a^2*b^8*x^3 + (5*a*b^9*x^4)/2 + (b^{10}*x^5)/5 + 252*a^5*b^5*\text{Log}[x]$

fricas [A] time = 0.47, size = 114, normalized size = 0.97

$$\frac{2b^{10}x^{10} + 25ab^9x^9 + 150a^2b^8x^8 + 600a^3b^7x^7 + 2100a^4b^6x^6 + 2520a^5b^5x^5 \log(x) - 2100a^6b^4x^4 - 600a^7b^3x^3}{10x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^6,x, algorithm="fricas")

[Out] $1/10*(2*b^{10}*x^{10} + 25*a*b^9*x^9 + 150*a^2*b^8*x^8 + 600*a^3*b^7*x^7 + 2100*a^4*b^6*x^6 + 2520*a^5*b^5*x^5*\log(x) - 2100*a^6*b^4*x^4 - 600*a^7*b^3*x^3 - 150*a^8*b^2*x^2 - 25*a^9*b*x - 2*a^{10})/x^5$

giac [A] time = 1.14, size = 111, normalized size = 0.95

$$\frac{1}{5}b^{10}x^5 + \frac{5}{2}ab^9x^4 + 15a^2b^8x^3 + 60a^3b^7x^2 + 210a^4b^6x + 252a^5b^5 \log(|x|) - \frac{2100a^6b^4x^4 + 600a^7b^3x^3 + 150a^8b^2x^2}{10x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^6,x, algorithm="giac")

[Out] $1/5*b^{10}*x^5 + 5/2*a*b^9*x^4 + 15*a^2*b^8*x^3 + 60*a^3*b^7*x^2 + 210*a^4*b^6*x + 252*a^5*b^5*\log(\text{abs}(x)) - 1/10*(2100*a^6*b^4*x^4 + 600*a^7*b^3*x^3 + 150*a^8*b^2*x^2 + 25*a^9*b*x + 2*a^{10})/x^5$

maple [A] time = 0.01, size = 110, normalized size = 0.94

$$\frac{b^{10}x^5}{5} + \frac{5ab^9x^4}{2} + 15a^2b^8x^3 + 60a^3b^7x^2 + 252a^5b^5 \ln(x) + 210a^4b^6x - \frac{210a^6b^4}{x} - \frac{60a^7b^3}{x^2} - \frac{15a^8b^2}{x^3} - \frac{5a^9b}{2x^4} - \frac{a^{10}}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^6,x)

[Out] $-1/5*a^{10}/x^5 - 5/2*a^9*b/x^4 - 15*a^8*b^2/x^3 - 60*a^7*b^3/x^2 - 210*a^6*b^4/x + 210*a^4*b^6*x + 60*a^3*b^7*x^2 + 15*a^2*b^8*x^3 + 5/2*a*b^9*x^4 + 1/5*b^{10}*x^5 + 252*a^5*b^5*\ln(x)$

maxima [A] time = 1.40, size = 110, normalized size = 0.94

$$\frac{1}{5} b^{10} x^5 + \frac{5}{2} a b^9 x^4 + 15 a^2 b^8 x^3 + 60 a^3 b^7 x^2 + 210 a^4 b^6 x + 252 a^5 b^5 \log(x) - \frac{2100 a^6 b^4 x^4 + 600 a^7 b^3 x^3 + 150 a^8 b^2 x^2 + 252 a^9 b x + 2 a^{10}}{10 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^6,x, algorithm="maxima")

[Out] 1/5*b^10*x^5 + 5/2*a*b^9*x^4 + 15*a^2*b^8*x^3 + 60*a^3*b^7*x^2 + 210*a^4*b^6*x + 252*a^5*b^5*log(x) - 1/10*(2100*a^6*b^4*x^4 + 600*a^7*b^3*x^3 + 150*a^8*b^2*x^2 + 25*a^9*b*x + 2*a^10)/x^5

mupad [B] time = 0.10, size = 110, normalized size = 0.94

$$\frac{b^{10} x^5}{5} - \frac{a^{10}}{5} + \frac{5 a^9 b x}{2} + 15 a^8 b^2 x^2 + 60 a^7 b^3 x^3 + 210 a^6 b^4 x^4}{x^5} + 210 a^4 b^6 x + \frac{5 a b^9 x^4}{2} + 60 a^3 b^7 x^2 + 15 a^2 b^8 x^3 + 252 a^5 b^5 \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^6,x)

[Out] (b^10*x^5)/5 - (a^10/5 + 15*a^8*b^2*x^2 + 60*a^7*b^3*x^3 + 210*a^6*b^4*x^4 + (5*a^9*b*x)/2)/x^5 + 210*a^4*b^6*x + (5*a*b^9*x^4)/2 + 60*a^3*b^7*x^2 + 15*a^2*b^8*x^3 + 252*a^5*b^5*log(x)

sympy [A] time = 0.57, size = 121, normalized size = 1.03

$$252 a^5 b^5 \log(x) + 210 a^4 b^6 x + 60 a^3 b^7 x^2 + 15 a^2 b^8 x^3 + \frac{5 a b^9 x^4}{2} + \frac{b^{10} x^5}{5} + \frac{-2 a^{10} - 25 a^9 b x - 150 a^8 b^2 x^2 - 600 a^7 b^3 x^3 - 2100 a^6 b^4 x^4}{10 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**6,x)

[Out] 252*a**5*b**5*log(x) + 210*a**4*b**6*x + 60*a**3*b**7*x**2 + 15*a**2*b**8*x**3 + 5*a*b**9*x**4/2 + b**10*x**5/5 + (-2*a**10 - 25*a**9*b*x - 150*a**8*b**2*x**2 - 600*a**7*b**3*x**3 - 2100*a**6*b**4*x**4)/(10*x**5)

$$3.141 \quad \int \frac{(a+bx)^{10}}{x^7} dx$$

Optimal. Leaf size=119

$$\frac{a^{10}}{6x^6} - \frac{2a^9b}{x^5} - \frac{45a^8b^2}{4x^4} - \frac{40a^7b^3}{x^3} - \frac{105a^6b^4}{x^2} - \frac{252a^5b^5}{x} + 210a^4b^6 \log(x) + 120a^3b^7x + \frac{45}{2}a^2b^8x^2 + \frac{10}{3}ab^9x^3 + \frac{b^{10}x^4}{4}$$

[Out] $-1/6*a^{10}/x^6 - 2*a^9*b/x^5 - 45/4*a^8*b^2/x^4 - 40*a^7*b^3/x^3 - 105*a^6*b^4/x^2 - 252*a^5*b^5/x + 120*a^3*b^7*x + 45/2*a^2*b^8*x^2 + 10/3*a*b^9*x^3 + 1/4*b^{10}*x^4 + 210*a^4*b^6*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{45a^8b^2}{4x^4} - \frac{40a^7b^3}{x^3} - \frac{105a^6b^4}{x^2} + \frac{45}{2}a^2b^8x^2 - \frac{252a^5b^5}{x} + 120a^3b^7x + 210a^4b^6 \log(x) - \frac{2a^9b}{x^5} - \frac{a^{10}}{6x^6} + \frac{10}{3}ab^9x^3 + \frac{b^{10}x^4}{4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^7, x]

[Out] $-a^{10}/(6*x^6) - (2*a^9*b)/x^5 - (45*a^8*b^2)/(4*x^4) - (40*a^7*b^3)/x^3 - (105*a^6*b^4)/x^2 - (252*a^5*b^5)/x + 120*a^3*b^7*x + (45*a^2*b^8*x^2)/2 + (10*a*b^9*x^3)/3 + (b^{10}*x^4)/4 + 210*a^4*b^6*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^7} dx = \int \left(120a^3b^7 + \frac{a^{10}}{x^7} + \frac{10a^9b}{x^6} + \frac{45a^8b^2}{x^5} + \frac{120a^7b^3}{x^4} + \frac{210a^6b^4}{x^3} + \frac{252a^5b^5}{x^2} + \frac{210a^4b^6}{x} + 45a^2b^8x \right) dx$$

$$= -\frac{a^{10}}{6x^6} - \frac{2a^9b}{x^5} - \frac{45a^8b^2}{4x^4} - \frac{40a^7b^3}{x^3} - \frac{105a^6b^4}{x^2} - \frac{252a^5b^5}{x} + 120a^3b^7x + \frac{45}{2}a^2b^8x^2 + \frac{10}{3}ab^9x^3$$

Mathematica [A] time = 0.01, size = 119, normalized size = 1.00

$$\frac{a^{10}}{6x^6} - \frac{2a^9b}{x^5} - \frac{45a^8b^2}{4x^4} - \frac{40a^7b^3}{x^3} - \frac{105a^6b^4}{x^2} - \frac{252a^5b^5}{x} + 210a^4b^6 \log(x) + 120a^3b^7x + \frac{45}{2}a^2b^8x^2 + \frac{10}{3}ab^9x^3 + \frac{b^{10}x^4}{4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^7, x]

[Out] $-1/6*a^{10}/x^6 - (2*a^9*b)/x^5 - (45*a^8*b^2)/(4*x^4) - (40*a^7*b^3)/x^3 - (105*a^6*b^4)/x^2 - (252*a^5*b^5)/x + 120*a^3*b^7*x + (45*a^2*b^8*x^2)/2 + (10*a*b^9*x^3)/3 + (b^{10}*x^4)/4 + 210*a^4*b^6*\text{Log}[x]$

fricas [A] time = 0.49, size = 114, normalized size = 0.96

$$\frac{3b^{10}x^{10} + 40ab^9x^9 + 270a^2b^8x^8 + 1440a^3b^7x^7 + 2520a^4b^6x^6 \log(x) - 3024a^5b^5x^5 - 1260a^6b^4x^4 - 480a^7b^3x^3}{12x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^7, x, algorithm="fricas")

[Out] $1/12*(3*b^{10}*x^{10} + 40*a*b^9*x^9 + 270*a^2*b^8*x^8 + 1440*a^3*b^7*x^7 + 2520*a^4*b^6*x^6*\log(x) - 3024*a^5*b^5*x^5 - 1260*a^6*b^4*x^4 - 480*a^7*b^3*x^3 - 135*a^8*b^2*x^2 - 24*a^9*b*x - 2*a^{10})/x^6$

giac [A] time = 1.24, size = 111, normalized size = 0.93

$$\frac{1}{4}b^{10}x^4 + \frac{10}{3}ab^9x^3 + \frac{45}{2}a^2b^8x^2 + 120a^3b^7x + 210a^4b^6 \log(|x|) - \frac{3024a^5b^5x^5 + 1260a^6b^4x^4 + 480a^7b^3x^3 + 135a^8b^2x^2}{12x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^7, x, algorithm="giac")

[Out] $1/4*b^{10}*x^4 + 10/3*a*b^9*x^3 + 45/2*a^2*b^8*x^2 + 120*a^3*b^7*x + 210*a^4*b^6*\log(\text{abs}(x)) - 1/12*(3024*a^5*b^5*x^5 + 1260*a^6*b^4*x^4 + 480*a^7*b^3*x^3 + 135*a^8*b^2*x^2 + 24*a^9*b*x + 2*a^{10})/x^6$

maple [A] time = 0.01, size = 110, normalized size = 0.92

$$\frac{b^{10}x^4}{4} + \frac{10ab^9x^3}{3} + \frac{45a^2b^8x^2}{2} + 210a^4b^6 \ln(x) + 120a^3b^7x - \frac{252a^5b^5}{x} - \frac{105a^6b^4}{x^2} - \frac{40a^7b^3}{x^3} - \frac{45a^8b^2}{4x^4} - \frac{2a^9b}{x^5} - \frac{a^{10}}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^7, x)

[Out] $-1/6*a^{10}/x^6 - 2*a^9*b/x^5 - 45/4*a^8*b^2/x^4 - 40*a^7*b^3/x^3 - 105*a^6*b^4/x^2 - 52*a^5*b^5/x + 120*a^3*b^7*x + 45/2*a^2*b^8*x^2 + 10/3*a*b^9*x^3 + 1/4*b^{10}*x^4 + 210*a^4*b^6*\ln(x)$

maxima [A] time = 1.37, size = 110, normalized size = 0.92

$$\frac{1}{4} b^{10} x^4 + \frac{10}{3} a b^9 x^3 + \frac{45}{2} a^2 b^8 x^2 + 120 a^3 b^7 x + 210 a^4 b^6 \log(x) - \frac{3024 a^5 b^5 x^5 + 1260 a^6 b^4 x^4 + 480 a^7 b^3 x^3 + 135 a^8 b^2 x^2}{12 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^7,x, algorithm="maxima")

[Out] 1/4*b^10*x^4 + 10/3*a*b^9*x^3 + 45/2*a^2*b^8*x^2 + 120*a^3*b^7*x + 210*a^4*b^6*log(x) - 1/12*(3024*a^5*b^5*x^5 + 1260*a^6*b^4*x^4 + 480*a^7*b^3*x^3 + 135*a^8*b^2*x^2 + 24*a^9*b*x + 2*a^10)/x^6

mupad [B] time = 0.05, size = 110, normalized size = 0.92

$$\frac{b^{10} x^4}{4} - \frac{a^{10}}{6} + 2 a^9 b x + \frac{45 a^8 b^2 x^2}{4} + 40 a^7 b^3 x^3 + 105 a^6 b^4 x^4 + 252 a^5 b^5 x^5}{x^6} + 120 a^3 b^7 x + \frac{10 a b^9 x^3}{3} + \frac{45 a^2 b^8 x^2}{2} +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^7,x)

[Out] (b^10*x^4)/4 - (a^10/6 + (45*a^8*b^2*x^2)/4 + 40*a^7*b^3*x^3 + 105*a^6*b^4*x^4 + 252*a^5*b^5*x^5 + 2*a^9*b*x)/x^6 + 120*a^3*b^7*x + (10*a*b^9*x^3)/3 + (45*a^2*b^8*x^2)/2 + 210*a^4*b^6*log(x)

sympy [A] time = 0.57, size = 122, normalized size = 1.03

$$210 a^4 b^6 \log(x) + 120 a^3 b^7 x + \frac{45 a^2 b^8 x^2}{2} + \frac{10 a b^9 x^3}{3} + \frac{b^{10} x^4}{4} + \frac{-2 a^{10} - 24 a^9 b x - 135 a^8 b^2 x^2 - 480 a^7 b^3 x^3 - 1260 a^6 b^4 x^4}{12 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**7,x)

[Out] 210*a**4*b**6*log(x) + 120*a**3*b**7*x + 45*a**2*b**8*x**2/2 + 10*a*b**9*x**3/3 + b**10*x**4/4 + (-2*a**10 - 24*a**9*b*x - 135*a**8*b**2*x**2 - 480*a**7*b**3*x**3 - 1260*a**6*b**4*x**4 - 3024*a**5*b**5*x**5)/(12*x**6)

$$3.142 \quad \int \frac{(a+bx)^{10}}{x^8} dx$$

Optimal. Leaf size=115

$$\frac{a^{10}}{7x^7} - \frac{5a^9b}{3x^6} - \frac{9a^8b^2}{x^5} - \frac{30a^7b^3}{x^4} - \frac{70a^6b^4}{x^3} - \frac{126a^5b^5}{x^2} - \frac{210a^4b^6}{x} + 120a^3b^7 \log(x) + 45a^2b^8x + 5ab^9x^2 + \frac{b^{10}x^3}{3}$$

[Out] $-1/7*a^{10}/x^7 - 5/3*a^9*b/x^6 - 9*a^8*b^2/x^5 - 30*a^7*b^3/x^4 - 70*a^6*b^4/x^3 - 126*a^5*b^5/x^2 - 210*a^4*b^6/x + 45*a^2*b^8*x + 5*a*b^9*x^2 + 1/3*b^{10}*x^3 + 120*a^3*b^7*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{9a^8b^2}{x^5} - \frac{30a^7b^3}{x^4} - \frac{70a^6b^4}{x^3} - \frac{126a^5b^5}{x^2} - \frac{210a^4b^6}{x} + 45a^2b^8x + 120a^3b^7 \log(x) - \frac{5a^9b}{3x^6} - \frac{a^{10}}{7x^7} + 5ab^9x^2 + \frac{b^{10}x^3}{3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^8, x]

[Out] $-a^{10}/(7*x^7) - (5*a^9*b)/(3*x^6) - (9*a^8*b^2)/x^5 - (30*a^7*b^3)/x^4 - (70*a^6*b^4)/x^3 - (126*a^5*b^5)/x^2 - (210*a^4*b^6)/x + 45*a^2*b^8*x + 5*a*b^9*x^2 + (b^{10}*x^3)/3 + 120*a^3*b^7*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^8} dx = \int \left(45a^2b^8 + \frac{a^{10}}{x^8} + \frac{10a^9b}{x^7} + \frac{45a^8b^2}{x^6} + \frac{120a^7b^3}{x^5} + \frac{210a^6b^4}{x^4} + \frac{252a^5b^5}{x^3} + \frac{210a^4b^6}{x^2} + \frac{120a^3b^7}{x} \right) dx$$

$$= -\frac{a^{10}}{7x^7} - \frac{5a^9b}{3x^6} - \frac{9a^8b^2}{x^5} - \frac{30a^7b^3}{x^4} - \frac{70a^6b^4}{x^3} - \frac{126a^5b^5}{x^2} - \frac{210a^4b^6}{x} + 45a^2b^8x + 5ab^9x^2 + \frac{b^{10}x^3}{3}$$

Mathematica [A] time = 0.01, size = 115, normalized size = 1.00

$$\frac{a^{10}}{7x^7} - \frac{5a^9b}{3x^6} - \frac{9a^8b^2}{x^5} - \frac{30a^7b^3}{x^4} - \frac{70a^6b^4}{x^3} - \frac{126a^5b^5}{x^2} - \frac{210a^4b^6}{x} + 120a^3b^7 \log(x) + 45a^2b^8x + 5ab^9x^2 + \frac{b^{10}x^3}{3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^8,x]

[Out] $-1/7*a^{10}/x^7 - (5*a^9*b)/(3*x^6) - (9*a^8*b^2)/x^5 - (30*a^7*b^3)/x^4 - (70*a^6*b^4)/x^3 - (126*a^5*b^5)/x^2 - (210*a^4*b^6)/x + 45*a^2*b^8*x + 5*a*b^9*x^2 + (b^{10}*x^3)/3 + 120*a^3*b^7*\text{Log}[x]$

fricas [A] time = 0.46, size = 114, normalized size = 0.99

$$\frac{7b^{10}x^{10} + 105ab^9x^9 + 945a^2b^8x^8 + 2520a^3b^7x^7 \log(x) - 4410a^4b^6x^6 - 2646a^5b^5x^5 - 1470a^6b^4x^4 - 630a^7b^3x^3 - 189a^8b^2x^2 - 35a^9bx - 3a^{10}}{21x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^8,x, algorithm="fricas")

[Out] $1/21*(7*b^{10}*x^{10} + 105*a*b^9*x^9 + 945*a^2*b^8*x^8 + 2520*a^3*b^7*x^7*\log(x) - 4410*a^4*b^6*x^6 - 2646*a^5*b^5*x^5 - 1470*a^6*b^4*x^4 - 630*a^7*b^3*x^3 - 189*a^8*b^2*x^2 - 35*a^9*b*x - 3*a^{10})/x^7$

giac [A] time = 1.10, size = 111, normalized size = 0.97

$$\frac{1}{3}b^{10}x^3 + 5ab^9x^2 + 45a^2b^8x + 120a^3b^7 \log(|x|) - \frac{4410a^4b^6x^6 + 2646a^5b^5x^5 + 1470a^6b^4x^4 + 630a^7b^3x^3 + 189a^8b^2x^2 + 35a^9bx + 3a^{10}}{21x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^8,x, algorithm="giac")

[Out] $1/3*b^{10}*x^3 + 5*a*b^9*x^2 + 45*a^2*b^8*x + 120*a^3*b^7*\log(\text{abs}(x)) - 1/21*(4410*a^4*b^6*x^6 + 2646*a^5*b^5*x^5 + 1470*a^6*b^4*x^4 + 630*a^7*b^3*x^3 + 189*a^8*b^2*x^2 + 35*a^9*b*x + 3*a^{10})/x^7$

maple [A] time = 0.01, size = 110, normalized size = 0.96

$$\frac{b^{10}x^3}{3} + 5ab^9x^2 + 120a^3b^7 \ln(x) + 45a^2b^8x - \frac{210a^4b^6}{x} - \frac{126a^5b^5}{x^2} - \frac{70a^6b^4}{x^3} - \frac{30a^7b^3}{x^4} - \frac{9a^8b^2}{x^5} - \frac{5a^9b}{3x^6} - \frac{a^{10}}{7x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^8,x)

[Out] $-1/7*a^{10}/x^7 - 5/3*a^9*b/x^6 - 9*a^8*b^2/x^5 - 30*a^7*b^3/x^4 - 70*a^6*b^4/x^3 - 126*a^5*b^5/x^2 - 210*a^4*b^6/x + 45*a^2*b^8*x + 5*a*b^9*x^2 + 1/3*b^{10}*x^3 + 120*a^3*b^7*\ln(x)$

maxima [A] time = 1.30, size = 110, normalized size = 0.96

$$\frac{1}{3}b^{10}x^3 + 5ab^9x^2 + 45a^2b^8x + 120a^3b^7 \log(x) - \frac{4410a^4b^6x^6 + 2646a^5b^5x^5 + 1470a^6b^4x^4 + 630a^7b^3x^3 + 189a^8b^2x^2 + 35a^9bx + 3a^{10}}{21x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^8,x, algorithm="maxima")

[Out] 1/3*b^10*x^3 + 5*a*b^9*x^2 + 45*a^2*b^8*x + 120*a^3*b^7*log(x) - 1/21*(4410*a^4*b^6*x^6 + 2646*a^5*b^5*x^5 + 1470*a^6*b^4*x^4 + 630*a^7*b^3*x^3 + 189*a^8*b^2*x^2 + 35*a^9*b*x + 3*a^10)/x^7

mupad [B] time = 0.10, size = 110, normalized size = 0.96

$$\frac{b^{10}x^3}{3} - \frac{\frac{a^{10}}{7} + \frac{5a^9bx}{3} + 9a^8b^2x^2 + 30a^7b^3x^3 + 70a^6b^4x^4 + 126a^5b^5x^5 + 210a^4b^6x^6}{x^7} + 45a^2b^8x + 5ab^9x^2 + 120a^3b^7 \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^8,x)

[Out] (b^10*x^3)/3 - (a^10/7 + 9*a^8*b^2*x^2 + 30*a^7*b^3*x^3 + 70*a^6*b^4*x^4 + 126*a^5*b^5*x^5 + 210*a^4*b^6*x^6 + (5*a^9*b*x)/3)/x^7 + 45*a^2*b^8*x + 5*a*b^9*x^2 + 120*a^3*b^7*log(x)

sympy [A] time = 0.70, size = 119, normalized size = 1.03

$$120a^3b^7 \log(x) + 45a^2b^8x + 5ab^9x^2 + \frac{b^{10}x^3}{3} + \frac{-3a^{10} - 35a^9bx - 189a^8b^2x^2 - 630a^7b^3x^3 - 1470a^6b^4x^4 - 2646a^5b^5x^5}{21x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**8,x)

[Out] 120*a**3*b**7*log(x) + 45*a**2*b**8*x + 5*a*b**9*x**2 + b**10*x**3/3 + (-3*a**10 - 35*a**9*b*x - 189*a**8*b**2*x**2 - 630*a**7*b**3*x**3 - 1470*a**6*b**4*x**4 - 2646*a**5*b**5*x**5 - 4410*a**4*b**6*x**6)/(21*x**7)

$$3.143 \quad \int \frac{(a+bx)^{10}}{x^9} dx$$

Optimal. Leaf size=119

$$\frac{a^{10}}{8x^8} - \frac{10a^9b}{7x^7} - \frac{15a^8b^2}{2x^6} - \frac{24a^7b^3}{x^5} - \frac{105a^6b^4}{2x^4} - \frac{84a^5b^5}{x^3} - \frac{105a^4b^6}{x^2} - \frac{120a^3b^7}{x} + 45a^2b^8 \log(x) + 10ab^9x + \frac{b^{10}x^2}{2}$$

[Out] $-1/8*a^{10}/x^8-10/7*a^9*b/x^7-15/2*a^8*b^2/x^6-24*a^7*b^3/x^5-105/2*a^6*b^4/x^4-84*a^5*b^5/x^3-105*a^4*b^6/x^2-120*a^3*b^7/x+10*a*b^9*x+1/2*b^{10}*x^2+45*a^2*b^8*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{15a^8b^2}{2x^6} - \frac{24a^7b^3}{x^5} - \frac{105a^6b^4}{2x^4} - \frac{84a^5b^5}{x^3} - \frac{105a^4b^6}{x^2} - \frac{120a^3b^7}{x} + 45a^2b^8 \log(x) - \frac{10a^9b}{7x^7} - \frac{a^{10}}{8x^8} + 10ab^9x + \frac{b^{10}x^2}{2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^9, x]

[Out] $-a^{10}/(8*x^8) - (10*a^9*b)/(7*x^7) - (15*a^8*b^2)/(2*x^6) - (24*a^7*b^3)/x^5 - (105*a^6*b^4)/(2*x^4) - (84*a^5*b^5)/x^3 - (105*a^4*b^6)/x^2 - (120*a^3*b^7)/x + 10*a*b^9*x + (b^{10}*x^2)/2 + 45*a^2*b^8*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^9} dx = \int \left(10ab^9 + \frac{a^{10}}{x^9} + \frac{10a^9b}{x^8} + \frac{45a^8b^2}{x^7} + \frac{120a^7b^3}{x^6} + \frac{210a^6b^4}{x^5} + \frac{252a^5b^5}{x^4} + \frac{210a^4b^6}{x^3} + \frac{120a^3b^7}{x^2} \right) dx$$

$$= -\frac{a^{10}}{8x^8} - \frac{10a^9b}{7x^7} - \frac{15a^8b^2}{2x^6} - \frac{24a^7b^3}{x^5} - \frac{105a^6b^4}{2x^4} - \frac{84a^5b^5}{x^3} - \frac{105a^4b^6}{x^2} - \frac{120a^3b^7}{x} + 10ab^9x + \frac{b^{10}x^2}{2}$$

Mathematica [A] time = 0.01, size = 119, normalized size = 1.00

$$\frac{a^{10}}{8x^8} - \frac{10a^9b}{7x^7} - \frac{15a^8b^2}{2x^6} - \frac{24a^7b^3}{x^5} - \frac{105a^6b^4}{2x^4} - \frac{84a^5b^5}{x^3} - \frac{105a^4b^6}{x^2} - \frac{120a^3b^7}{x} + 45a^2b^8 \log(x) + 10ab^9x + \frac{b^{10}x^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^9, x]

[Out] $-1/8*a^{10}/x^8 - (10*a^9*b)/(7*x^7) - (15*a^8*b^2)/(2*x^6) - (24*a^7*b^3)/x^5 - (105*a^6*b^4)/(2*x^4) - (84*a^5*b^5)/x^3 - (105*a^4*b^6)/x^2 - (120*a^3*b^7)/x + 10*a*b^9*x + (b^{10}*x^2)/2 + 45*a^2*b^8*\text{Log}[x]$

fricas [A] time = 0.45, size = 114, normalized size = 0.96

$$\frac{28b^{10}x^{10} + 560ab^9x^9 + 2520a^2b^8x^8 \log(x) - 6720a^3b^7x^7 - 5880a^4b^6x^6 - 4704a^5b^5x^5 - 2940a^6b^4x^4 - 1344a^7b^3x^3 + 420a^8b^2x^2 + 80a^9bx + 7a^{10}}{56x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^9, x, algorithm="fricas")

[Out] $1/56*(28*b^{10}*x^{10} + 560*a*b^9*x^9 + 2520*a^2*b^8*x^8*\log(x) - 6720*a^3*b^7*x^7 - 5880*a^4*b^6*x^6 - 4704*a^5*b^5*x^5 - 2940*a^6*b^4*x^4 - 1344*a^7*b^3*x^3 - 420*a^8*b^2*x^2 - 80*a^9*b*x - 7*a^{10})/x^8$

giac [A] time = 1.16, size = 111, normalized size = 0.93

$$\frac{1}{2}b^{10}x^2 + 10ab^9x + 45a^2b^8 \log(|x|) - \frac{6720a^3b^7x^7 + 5880a^4b^6x^6 + 4704a^5b^5x^5 + 2940a^6b^4x^4 + 1344a^7b^3x^3 + 420a^8b^2x^2 + 80a^9bx + 7a^{10}}{56x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^9, x, algorithm="giac")

[Out] $1/2*b^{10}*x^2 + 10*a*b^9*x + 45*a^2*b^8*\log(\text{abs}(x)) - 1/56*(6720*a^3*b^7*x^7 + 5880*a^4*b^6*x^6 + 4704*a^5*b^5*x^5 + 2940*a^6*b^4*x^4 + 1344*a^7*b^3*x^3 + 420*a^8*b^2*x^2 + 80*a^9*b*x + 7*a^{10})/x^8$

maple [A] time = 0.01, size = 110, normalized size = 0.92

$$\frac{b^{10}x^2}{2} + 45a^2b^8 \ln(x) + 10ab^9x - \frac{120a^3b^7}{x} - \frac{105a^4b^6}{x^2} - \frac{84a^5b^5}{x^3} - \frac{105a^6b^4}{2x^4} - \frac{24a^7b^3}{x^5} - \frac{15a^8b^2}{2x^6} - \frac{10a^9b}{7x^7} - \frac{a^{10}}{8x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^9, x)

[Out] $-1/8*a^{10}/x^8 - 10/7*a^9*b/x^7 - 15/2*a^8*b^2/x^6 - 24*a^7*b^3/x^5 - 105/2*a^6*b^4/x^4 - 84*a^5*b^5/x^3 - 105*a^4*b^6/x^2 - 120*a^3*b^7/x + 10*a*b^9*x + 1/2*b^{10}*x^2 + 45*a^2*b^8*\ln(x)$

maxima [A] time = 1.42, size = 110, normalized size = 0.92

$$\frac{1}{2} b^{10} x^2 + 10 a b^9 x + 45 a^2 b^8 \log(x) - \frac{6720 a^3 b^7 x^7 + 5880 a^4 b^6 x^6 + 4704 a^5 b^5 x^5 + 2940 a^6 b^4 x^4 + 1344 a^7 b^3 x^3 + 420 a^8 b^2 x^2 + 80 a^9 b x + 7 a^{10}}{56 x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^9,x, algorithm="maxima")

[Out] 1/2*b^10*x^2 + 10*a*b^9*x + 45*a^2*b^8*log(x) - 1/56*(6720*a^3*b^7*x^7 + 5880*a^4*b^6*x^6 + 4704*a^5*b^5*x^5 + 2940*a^6*b^4*x^4 + 1344*a^7*b^3*x^3 + 420*a^8*b^2*x^2 + 80*a^9*b*x + 7*a^10)/x^8

mupad [B] time = 0.07, size = 110, normalized size = 0.92

$$\frac{b^{10} x^2}{2} - \frac{\frac{a^{10}}{8} + \frac{10 a^9 b x}{7} + \frac{15 a^8 b^2 x^2}{2} + 24 a^7 b^3 x^3 + \frac{105 a^6 b^4 x^4}{2} + 84 a^5 b^5 x^5 + 105 a^4 b^6 x^6 + 120 a^3 b^7 x^7}{x^8} + 45 a^2 b^8 \ln$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^9,x)

[Out] (b^10*x^2)/2 - (a^10/8 + (15*a^8*b^2*x^2)/2 + 24*a^7*b^3*x^3 + (105*a^6*b^4*x^4)/2 + 84*a^5*b^5*x^5 + 105*a^4*b^6*x^6 + 120*a^3*b^7*x^7 + (10*a^9*b*x)/7)/x^8 + 45*a^2*b^8*log(x) + 10*a*b^9*x

sympy [A] time = 0.76, size = 119, normalized size = 1.00

$$45 a^2 b^8 \log(x) + 10 a b^9 x + \frac{b^{10} x^2}{2} + \frac{-7 a^{10} - 80 a^9 b x - 420 a^8 b^2 x^2 - 1344 a^7 b^3 x^3 - 2940 a^6 b^4 x^4 - 4704 a^5 b^5 x^5 - 5880 a^4 b^6 x^6 - 420 a^3 b^7 x^7 - 80 a^2 b^8 x^8 - 7 a^{10}}{56 x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**9,x)

[Out] 45*a**2*b**8*log(x) + 10*a*b**9*x + b**10*x**2/2 + (-7*a**10 - 80*a**9*b*x - 420*a**8*b**2*x**2 - 1344*a**7*b**3*x**3 - 2940*a**6*b**4*x**4 - 4704*a**5*b**5*x**5 - 5880*a**4*b**6*x**6 - 420*a**3*b**7*x**7 - 80*a**2*b**8*x**8 - 7*a**10)/(56*x**8)

$$3.144 \quad \int \frac{(a+bx)^{10}}{x^{10}} dx$$

Optimal. Leaf size=114

$$\frac{a^{10}}{9x^9} - \frac{5a^9b}{4x^8} - \frac{45a^8b^2}{7x^7} - \frac{20a^7b^3}{x^6} - \frac{42a^6b^4}{x^5} - \frac{63a^5b^5}{x^4} - \frac{70a^4b^6}{x^3} - \frac{60a^3b^7}{x^2} - \frac{45a^2b^8}{x} + 10ab^9 \log(x) + b^{10}x$$

[Out] $-1/9*a^{10}/x^9 - 5/4*a^9*b/x^8 - 45/7*a^8*b^2/x^7 - 20*a^7*b^3/x^6 - 42*a^6*b^4/x^5 - 63*a^5*b^5/x^4 - 70*a^4*b^6/x^3 - 60*a^3*b^7/x^2 - 45*a^2*b^8/x + b^{10}*x + 10*a*b^9*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 114, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{45a^8b^2}{7x^7} - \frac{20a^7b^3}{x^6} - \frac{42a^6b^4}{x^5} - \frac{63a^5b^5}{x^4} - \frac{70a^4b^6}{x^3} - \frac{60a^3b^7}{x^2} - \frac{45a^2b^8}{x} - \frac{5a^9b}{4x^8} - \frac{a^{10}}{9x^9} + 10ab^9 \log(x) + b^{10}x$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^10, x]

[Out] $-a^{10}/(9*x^9) - (5*a^9*b)/(4*x^8) - (45*a^8*b^2)/(7*x^7) - (20*a^7*b^3)/x^6 - (42*a^6*b^4)/x^5 - (63*a^5*b^5)/x^4 - (70*a^4*b^6)/x^3 - (60*a^3*b^7)/x^2 - (45*a^2*b^8)/x + b^{10}*x + 10*a*b^9*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^{10}}{x^{10}} dx &= \int \left(b^{10} + \frac{a^{10}}{x^{10}} + \frac{10a^9b}{x^9} + \frac{45a^8b^2}{x^8} + \frac{120a^7b^3}{x^7} + \frac{210a^6b^4}{x^6} + \frac{252a^5b^5}{x^5} + \frac{210a^4b^6}{x^4} + \frac{120a^3b^7}{x^3} + \frac{45a^2b^8}{x^2} + \frac{10ab^9}{x} + b^{10}x \right) dx \\ &= \frac{a^{10}}{9x^9} - \frac{5a^9b}{4x^8} - \frac{45a^8b^2}{7x^7} - \frac{20a^7b^3}{x^6} - \frac{42a^6b^4}{x^5} - \frac{63a^5b^5}{x^4} - \frac{70a^4b^6}{x^3} - \frac{60a^3b^7}{x^2} - \frac{45a^2b^8}{x} + b^{10}x + 10ab^9 \log(x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 114, normalized size = 1.00

$$\frac{a^{10}}{9x^9} - \frac{5a^9b}{4x^8} - \frac{45a^8b^2}{7x^7} - \frac{20a^7b^3}{x^6} - \frac{42a^6b^4}{x^5} - \frac{63a^5b^5}{x^4} - \frac{70a^4b^6}{x^3} - \frac{60a^3b^7}{x^2} - \frac{45a^2b^8}{x} + 10ab^9 \log(x) + b^{10}x$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^10,x]

[Out] $-1/9*a^{10}/x^9 - (5*a^9*b)/(4*x^8) - (45*a^8*b^2)/(7*x^7) - (20*a^7*b^3)/x^6 - (42*a^6*b^4)/x^5 - (63*a^5*b^5)/x^4 - (70*a^4*b^6)/x^3 - (60*a^3*b^7)/x^2 - (45*a^2*b^8)/x + b^{10}*x + 10*a*b^9*\text{Log}[x]$

fricas [A] time = 0.48, size = 114, normalized size = 1.00

$$\frac{252 b^{10} x^{10} + 2520 a b^9 x^9 \log(x) - 11340 a^2 b^8 x^8 - 15120 a^3 b^7 x^7 - 17640 a^4 b^6 x^6 - 15876 a^5 b^5 x^5 - 10584 a^6 b^4 x^4 - 5040 a^7 b^3 x^3 - 1620 a^8 b^2 x^2 - 315 a^9 b x - 28 a^{10}}{252 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^10,x, algorithm="fricas")

[Out] $1/252*(252*b^{10}*x^{10} + 2520*a*b^9*x^9*\log(x) - 11340*a^2*b^8*x^8 - 15120*a^3*b^7*x^7 - 17640*a^4*b^6*x^6 - 15876*a^5*b^5*x^5 - 10584*a^6*b^4*x^4 - 5040*a^7*b^3*x^3 - 1620*a^8*b^2*x^2 - 315*a^9*b*x - 28*a^{10})/x^9$

giac [A] time = 1.21, size = 110, normalized size = 0.96

$$b^{10}x+10ab^9\log(|x|)-\frac{11340a^2b^8x^8+15120a^3b^7x^7+17640a^4b^6x^6+15876a^5b^5x^5+10584a^6b^4x^4+5040a^7b^3x^3+1620a^8b^2x^2+315a^9bx-28a^{10}}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^10,x, algorithm="giac")

[Out] $b^{10}*x + 10*a*b^9*\log(\text{abs}(x)) - 1/252*(11340*a^2*b^8*x^8 + 15120*a^3*b^7*x^7 + 17640*a^4*b^6*x^6 + 15876*a^5*b^5*x^5 + 10584*a^6*b^4*x^4 + 5040*a^7*b^3*x^3 + 1620*a^8*b^2*x^2 + 315*a^9*b*x + 28*a^{10})/x^9$

maple [A] time = 0.01, size = 109, normalized size = 0.96

$$10a b^9 \ln(x) + b^{10} x - \frac{45 a^2 b^8}{x} - \frac{60 a^3 b^7}{x^2} - \frac{70 a^4 b^6}{x^3} - \frac{63 a^5 b^5}{x^4} - \frac{42 a^6 b^4}{x^5} - \frac{20 a^7 b^3}{x^6} - \frac{45 a^8 b^2}{7 x^7} - \frac{5 a^9 b}{4 x^8} - \frac{a^{10}}{9 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^10,x)

[Out] $-1/9*a^{10}/x^9 - 5/4*a^9*b/x^8 - 45/7*a^8*b^2/x^7 - 20*a^7*b^3/x^6 - 42*a^6*b^4/x^5 - 63*a^5*b^5/x^4 - 70*a^4*b^6/x^3 - 60*a^3*b^7/x^2 - 45*a^2*b^8/x + b^{10}*x + 10*a*b^9*\ln(x)$

maxima [A] time = 1.40, size = 109, normalized size = 0.96

$$b^{10}x + 10ab^9 \log(x) - \frac{11340a^2b^8x^8 + 15120a^3b^7x^7 + 17640a^4b^6x^6 + 15876a^5b^5x^5 + 10584a^6b^4x^4 + 5040a^7b^3x^3 + 1620a^8b^2x^2 + 315a^9bx + 28a^{10}}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^10,x, algorithm="maxima")

[Out] b^10*x + 10*a*b^9*log(x) - 1/252*(11340*a^2*b^8*x^8 + 15120*a^3*b^7*x^7 + 17640*a^4*b^6*x^6 + 15876*a^5*b^5*x^5 + 10584*a^6*b^4*x^4 + 5040*a^7*b^3*x^3 + 1620*a^8*b^2*x^2 + 315*a^9*b*x + 28*a^10)/x^9

mupad [B] time = 0.08, size = 114, normalized size = 1.00

$$\frac{\frac{a^{10}}{9} - b^{10}x^{10} + \frac{45a^8b^2x^2}{7} + 20a^7b^3x^3 + 42a^6b^4x^4 + 63a^5b^5x^5 + 70a^4b^6x^6 + 60a^3b^7x^7 + 45a^2b^8x^8 + \frac{5a^9bx}{4}}{x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^10,x)

[Out] -(a^10/9 - b^10*x^10 + (45*a^8*b^2*x^2)/7 + 20*a^7*b^3*x^3 + 42*a^6*b^4*x^4 + 63*a^5*b^5*x^5 + 70*a^4*b^6*x^6 + 60*a^3*b^7*x^7 + 45*a^2*b^8*x^8 + (5*a^9*b*x)/4 - 10*a*b^9*x^9*log(x))/x^9

sympy [A] time = 0.82, size = 117, normalized size = 1.03

$$10ab^9 \log(x) + b^{10}x + \frac{-28a^{10} - 315a^9bx - 1620a^8b^2x^2 - 5040a^7b^3x^3 - 10584a^6b^4x^4 - 15876a^5b^5x^5 - 17640a^4b^6x^6 - 15120a^3b^7x^7 - 11340a^2b^8x^8}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**10,x)

[Out] 10*a*b**9*log(x) + b**10*x + (-28*a**10 - 315*a**9*b*x - 1620*a**8*b**2*x**2 - 5040*a**7*b**3*x**3 - 10584*a**6*b**4*x**4 - 15876*a**5*b**5*x**5 - 17640*a**4*b**6*x**6 - 15120*a**3*b**7*x**7 - 11340*a**2*b**8*x**8)/(252*x**9)

$$3.145 \quad \int \frac{(a+bx)^{10}}{x^{11}} dx$$

Optimal. Leaf size=124

$$\frac{a^{10}}{10x^{10}} - \frac{10a^9b}{9x^9} + \frac{45a^8b^2}{8x^8} - \frac{120a^7b^3}{7x^7} + \frac{35a^6b^4}{x^6} - \frac{252a^5b^5}{5x^5} + \frac{105a^4b^6}{2x^4} - \frac{40a^3b^7}{x^3} + \frac{45a^2b^8}{2x^2} - \frac{10ab^9}{x} + b^{10} \log(x)$$

[Out] $-1/10*a^{10}/x^{10}-10/9*a^9*b/x^9-45/8*a^8*b^2/x^8-120/7*a^7*b^3/x^7-35*a^6*b^4/x^6-252/5*a^5*b^5/x^5-105/2*a^4*b^6/x^4-40*a^3*b^7/x^3-45/2*a^2*b^8/x^2-10*a*b^9/x+b^{10}*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 124, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{45a^8b^2}{8x^8} - \frac{120a^7b^3}{7x^7} + \frac{35a^6b^4}{x^6} - \frac{252a^5b^5}{5x^5} + \frac{105a^4b^6}{2x^4} - \frac{40a^3b^7}{x^3} + \frac{45a^2b^8}{2x^2} - \frac{10a^9b}{9x^9} - \frac{a^{10}}{10x^{10}} - \frac{10ab^9}{x} + b^{10} \log(x)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^11, x]

[Out] $-a^{10}/(10*x^{10}) - (10*a^9*b)/(9*x^9) - (45*a^8*b^2)/(8*x^8) - (120*a^7*b^3)/(7*x^7) - (35*a^6*b^4)/x^6 - (252*a^5*b^5)/(5*x^5) - (105*a^4*b^6)/(2*x^4) - (40*a^3*b^7)/x^3 - (45*a^2*b^8)/(2*x^2) - (10*a*b^9)/x + b^{10}*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^{11}} dx = \int \left(\frac{a^{10}}{x^{11}} + \frac{10a^9b}{x^{10}} + \frac{45a^8b^2}{x^9} + \frac{120a^7b^3}{x^8} + \frac{210a^6b^4}{x^7} + \frac{252a^5b^5}{x^6} + \frac{210a^4b^6}{x^5} + \frac{120a^3b^7}{x^4} + \frac{45a^2b^8}{x^3} + \frac{10ab^9}{x^2} + \frac{b^{10}}{x} \right) dx$$

$$= -\frac{a^{10}}{10x^{10}} - \frac{10a^9b}{9x^9} - \frac{45a^8b^2}{8x^8} - \frac{120a^7b^3}{7x^7} - \frac{35a^6b^4}{x^6} - \frac{252a^5b^5}{5x^5} - \frac{105a^4b^6}{2x^4} - \frac{40a^3b^7}{x^3} - \frac{45a^2b^8}{2x^2} - \frac{10ab^9}{x} + b^{10} \log(x)$$

Mathematica [A] time = 0.00, size = 124, normalized size = 1.00

$$\frac{a^{10}}{10x^{10}} - \frac{10a^9b}{9x^9} + \frac{45a^8b^2}{8x^8} - \frac{120a^7b^3}{7x^7} + \frac{35a^6b^4}{x^6} - \frac{252a^5b^5}{5x^5} + \frac{105a^4b^6}{2x^4} - \frac{40a^3b^7}{x^3} + \frac{45a^2b^8}{2x^2} - \frac{10ab^9}{x} + b^{10} \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^11,x]

[Out] $-1/10*a^{10}/x^{10} - (10*a^9*b)/(9*x^9) - (45*a^8*b^2)/(8*x^8) - (120*a^7*b^3)/(7*x^7) - (35*a^6*b^4)/x^6 - (252*a^5*b^5)/(5*x^5) - (105*a^4*b^6)/(2*x^4) - (40*a^3*b^7)/x^3 - (45*a^2*b^8)/(2*x^2) - (10*a*b^9)/x + b^{10}*Log[x]$

fricas [A] time = 0.45, size = 114, normalized size = 0.92

$$\frac{2520 b^{10} x^{10} \log(x) - 25200 a b^9 x^9 - 56700 a^2 b^8 x^8 - 100800 a^3 b^7 x^7 - 132300 a^4 b^6 x^6 - 127008 a^5 b^5 x^5 - 88200 a^6 b^4 x^4 + 43200 a^7 b^3 x^3 + 14175 a^8 b^2 x^2 + 2800 a^9 b x + 252 a^{10}}{2520 x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^11,x, algorithm="fricas")

[Out] $1/2520*(2520*b^{10}*x^{10}*log(x) - 25200*a*b^9*x^9 - 56700*a^2*b^8*x^8 - 100800*a^3*b^7*x^7 - 132300*a^4*b^6*x^6 - 127008*a^5*b^5*x^5 - 88200*a^6*b^4*x^4 - 43200*a^7*b^3*x^3 - 14175*a^8*b^2*x^2 - 2800*a^9*b*x - 252*a^{10})/x^{10}$

giac [A] time = 1.13, size = 112, normalized size = 0.90

$$b^{10} \log(|x|) - \frac{25200 a b^9 x^9 + 56700 a^2 b^8 x^8 + 100800 a^3 b^7 x^7 + 132300 a^4 b^6 x^6 + 127008 a^5 b^5 x^5 + 88200 a^6 b^4 x^4 + 43200 a^7 b^3 x^3 + 14175 a^8 b^2 x^2 + 2800 a^9 b x + 252 a^{10}}{2520 x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^11,x, algorithm="giac")

[Out] $b^{10}*log(abs(x)) - 1/2520*(25200*a*b^9*x^9 + 56700*a^2*b^8*x^8 + 100800*a^3*b^7*x^7 + 132300*a^4*b^6*x^6 + 127008*a^5*b^5*x^5 + 88200*a^6*b^4*x^4 + 43200*a^7*b^3*x^3 + 14175*a^8*b^2*x^2 + 2800*a^9*b*x + 252*a^{10})/x^{10}$

maple [A] time = 0.01, size = 111, normalized size = 0.90

$$b^{10} \ln(x) - \frac{10 a b^9}{x} - \frac{45 a^2 b^8}{2 x^2} - \frac{40 a^3 b^7}{x^3} - \frac{105 a^4 b^6}{2 x^4} - \frac{252 a^5 b^5}{5 x^5} - \frac{35 a^6 b^4}{x^6} - \frac{120 a^7 b^3}{7 x^7} - \frac{45 a^8 b^2}{8 x^8} - \frac{10 a^9 b}{9 x^9} - \frac{a^{10}}{10 x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^11,x)

[Out] $-1/10*a^{10}/x^{10} - 10/9*a^9*b/x^9 - 45/8*a^8*b^2/x^8 - 120/7*a^7*b^3/x^7 - 35*a^6*b^4/x^6 - 252/5*a^5*b^5/x^5 - 105/2*a^4*b^6/x^4 - 40*a^3*b^7/x^3 - 45/2*a^2*b^8/x^2 - 10*a*b^9/x + b^{10}*ln(x)$

maxima [A] time = 1.40, size = 111, normalized size = 0.90

$$b^{10} \log(x) - \frac{25200 ab^9 x^9 + 56700 a^2 b^8 x^8 + 100800 a^3 b^7 x^7 + 132300 a^4 b^6 x^6 + 127008 a^5 b^5 x^5 + 88200 a^6 b^4 x^4 + 43200 a^7 b^3 x^3 + 14175 a^8 b^2 x^2 + 2800 a^9 b x + 252 a^{10}}{2520 x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^11,x, algorithm="maxima")

[Out] b^10*log(x) - 1/2520*(25200*a*b^9*x^9 + 56700*a^2*b^8*x^8 + 100800*a^3*b^7*x^7 + 132300*a^4*b^6*x^6 + 127008*a^5*b^5*x^5 + 88200*a^6*b^4*x^4 + 43200*a^7*b^3*x^3 + 14175*a^8*b^2*x^2 + 2800*a^9*b*x + 252*a^10)/x^10

mupad [B] time = 0.07, size = 111, normalized size = 0.90

$$b^{10} \ln(x) - \frac{\frac{a^{10}}{10} + \frac{10 a^9 b x}{9} + \frac{45 a^8 b^2 x^2}{8} + \frac{120 a^7 b^3 x^3}{7} + 35 a^6 b^4 x^4 + \frac{252 a^5 b^5 x^5}{5} + \frac{105 a^4 b^6 x^6}{2} + 40 a^3 b^7 x^7 + \frac{45 a^2 b^8 x^8}{2} + 2800 a^9 b x + 252 a^{10}}{x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^11,x)

[Out] b^10*log(x) - (a^10/10 + 10*a*b^9*x^9 + (45*a^8*b^2*x^2)/8 + (120*a^7*b^3*x^3)/7 + 35*a^6*b^4*x^4 + (252*a^5*b^5*x^5)/5 + (105*a^4*b^6*x^6)/2 + 40*a^3*b^7*x^7 + (45*a^2*b^8*x^8)/2 + (10*a^9*b*x)/9)/x^10

sympy [A] time = 1.01, size = 119, normalized size = 0.96

$$b^{10} \log(x) + \frac{-252a^{10} - 2800a^9bx - 14175a^8b^2x^2 - 43200a^7b^3x^3 - 88200a^6b^4x^4 - 127008a^5b^5x^5 - 132300a^4b^6x^6 - 100800a^3b^7x^7 - 56700a^2b^8x^8 - 25200a^9bx - 252a^{10}}{2520x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**11,x)

[Out] b**10*log(x) + (-252*a**10 - 2800*a**9*b*x - 14175*a**8*b**2*x**2 - 43200*a**7*b**3*x**3 - 88200*a**6*b**4*x**4 - 127008*a**5*b**5*x**5 - 132300*a**4*b**6*x**6 - 100800*a**3*b**7*x**7 - 56700*a**2*b**8*x**8 - 25200*a*b**9*x**9)/(2520*x**10)

$$3.146 \quad \int \frac{(a+bx)^{10}}{x^{12}} dx$$

Optimal. Leaf size=17

$$-\frac{(a+bx)^{11}}{11ax^{11}}$$

[Out] $-1/11*(b*x+a)^{11}/a/x^{11}$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {37}

$$-\frac{(a+bx)^{11}}{11ax^{11}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{10}/x^{12}, x]$

[Out] $-(a + b*x)^{11}/(11*a*x^{11})$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)*(c + d*x)^{(n + 1)}}/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^{12}} dx = -\frac{(a+bx)^{11}}{11ax^{11}}$$

Mathematica [B] time = 0.01, size = 114, normalized size = 6.71

$$-\frac{a^{10}}{11x^{11}} - \frac{a^9b}{x^{10}} - \frac{5a^8b^2}{x^9} - \frac{15a^7b^3}{x^8} - \frac{30a^6b^4}{x^7} - \frac{42a^5b^5}{x^6} - \frac{42a^4b^6}{x^5} - \frac{30a^3b^7}{x^4} - \frac{15a^2b^8}{x^3} - \frac{5ab^9}{x^2} - \frac{b^{10}}{x}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(a + b*x)^{10}/x^{12}, x]$

[Out] $-1/11*a^{10}/x^{11} - (a^9*b)/x^{10} - (5*a^8*b^2)/x^9 - (15*a^7*b^3)/x^8 - (30*a^6*b^4)/x^7 - (42*a^5*b^5)/x^6 - (42*a^4*b^6)/x^5 - (30*a^3*b^7)/x^4 - (15*a^2*b^8)/x^3 - (5*a*b^9)/x^2 - b^{10}/x$

fricas [B] time = 0.43, size = 110, normalized size = 6.47

$$\frac{11 b^{10} x^{10} + 55 a b^9 x^9 + 165 a^2 b^8 x^8 + 330 a^3 b^7 x^7 + 462 a^4 b^6 x^6 + 462 a^5 b^5 x^5 + 330 a^6 b^4 x^4 + 165 a^7 b^3 x^3 + 55 a^8 b^2 x^2 + 11 a^9 b x + a^{10}}{11 x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^12,x, algorithm="fricas")

[Out] -1/11*(11*b^10*x^10 + 55*a*b^9*x^9 + 165*a^2*b^8*x^8 + 330*a^3*b^7*x^7 + 462*a^4*b^6*x^6 + 462*a^5*b^5*x^5 + 330*a^6*b^4*x^4 + 165*a^7*b^3*x^3 + 55*a^8*b^2*x^2 + 11*a^9*b*x + a^10)/x^11

giac [B] time = 1.06, size = 110, normalized size = 6.47

$$\frac{11 b^{10} x^{10} + 55 a b^9 x^9 + 165 a^2 b^8 x^8 + 330 a^3 b^7 x^7 + 462 a^4 b^6 x^6 + 462 a^5 b^5 x^5 + 330 a^6 b^4 x^4 + 165 a^7 b^3 x^3 + 55 a^8 b^2 x^2 + 11 a^9 b x + a^{10}}{11 x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^12,x, algorithm="giac")

[Out] -1/11*(11*b^10*x^10 + 55*a*b^9*x^9 + 165*a^2*b^8*x^8 + 330*a^3*b^7*x^7 + 462*a^4*b^6*x^6 + 462*a^5*b^5*x^5 + 330*a^6*b^4*x^4 + 165*a^7*b^3*x^3 + 55*a^8*b^2*x^2 + 11*a^9*b*x + a^10)/x^11

maple [B] time = 0.01, size = 113, normalized size = 6.65

$$\frac{b^{10}}{x} - \frac{5ab^9}{x^2} - \frac{15a^2b^8}{x^3} - \frac{30a^3b^7}{x^4} - \frac{42a^4b^6}{x^5} - \frac{42a^5b^5}{x^6} - \frac{30a^6b^4}{x^7} - \frac{15a^7b^3}{x^8} - \frac{5a^8b^2}{x^9} - \frac{a^9b}{x^{10}} - \frac{a^{10}}{11x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^12,x)

[Out] -1/11*a^10/x^11-42*a^5*b^5/x^6-5*a*b^9/x^2-5*a^8*b^2/x^9-15*a^2*b^8/x^3-30*a^3*b^7/x^4-42*a^4*b^6/x^5-b^10/x-a^9*b/x^10-30*a^6*b^4/x^7-15*a^7*b^3/x^8

maxima [B] time = 1.33, size = 110, normalized size = 6.47

$$\frac{11 b^{10} x^{10} + 55 a b^9 x^9 + 165 a^2 b^8 x^8 + 330 a^3 b^7 x^7 + 462 a^4 b^6 x^6 + 462 a^5 b^5 x^5 + 330 a^6 b^4 x^4 + 165 a^7 b^3 x^3 + 55 a^8 b^2 x^2 + 11 a^9 b x + a^{10}}{11 x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^12,x, algorithm="maxima")

[Out] $-1/11*(11*b^{10}*x^{10} + 55*a*b^9*x^9 + 165*a^2*b^8*x^8 + 330*a^3*b^7*x^7 + 462*a^4*b^6*x^6 + 462*a^5*b^5*x^5 + 330*a^6*b^4*x^4 + 165*a^7*b^3*x^3 + 55*a^8*b^2*x^2 + 11*a^9*b*x + a^{10})/x^{11}$

mupad [B] time = 0.13, size = 110, normalized size = 6.47

$$\frac{\frac{a^{10}}{11} + a^9 b x + 5 a^8 b^2 x^2 + 15 a^7 b^3 x^3 + 30 a^6 b^4 x^4 + 42 a^5 b^5 x^5 + 42 a^4 b^6 x^6 + 30 a^3 b^7 x^7 + 15 a^2 b^8 x^8 + 5 a b^9 x^9 + a^{10}}{x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^10/x^12,x)`

[Out] $-(a^{10}/11 + b^{10}*x^{10} + 5*a*b^9*x^9 + 5*a^8*b^2*x^2 + 15*a^7*b^3*x^3 + 30*a^6*b^4*x^4 + 42*a^5*b^5*x^5 + 42*a^4*b^6*x^6 + 30*a^3*b^7*x^7 + 15*a^2*b^8*x^8 + a^9*b*x)/x^{11}$

sympy [B] time = 1.03, size = 119, normalized size = 7.00

$$\frac{-a^{10} - 11a^9bx - 55a^8b^2x^2 - 165a^7b^3x^3 - 330a^6b^4x^4 - 462a^5b^5x^5 - 462a^4b^6x^6 - 330a^3b^7x^7 - 165a^2b^8x^8 - 55ab^9x^9 - a^{10}}{11x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**10/x**12,x)`

[Out] $(-a^{10} - 11a^9bx - 55a^8b^2x^2 - 165a^7b^3x^3 - 330a^6b^4x^4 - 462a^5b^5x^5 - 462a^4b^6x^6 - 330a^3b^7x^7 - 165a^2b^8x^8 - 55ab^9x^9 - a^{10})/(11x^{11})$

$$3.147 \quad \int \frac{(a+bx)^{10}}{x^{13}} dx$$

Optimal. Leaf size=36

$$\frac{b(a+bx)^{11}}{132a^2x^{11}} - \frac{(a+bx)^{11}}{12ax^{12}}$$

[Out] $-1/12*(b*x+a)^{11}/a/x^{12}+1/132*b*(b*x+a)^{11}/a^2/x^{11}$

Rubi [A] time = 0.00, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{b(a+bx)^{11}}{132a^2x^{11}} - \frac{(a+bx)^{11}}{12ax^{12}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^13,x]

[Out] $-(a + b*x)^{11}/(12*a*x^{12}) + (b*(a + b*x)^{11})/(132*a^2*x^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 (((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
 a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
 1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
 + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
 LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
 (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
 Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^{13}} dx = -\frac{(a+bx)^{11}}{12ax^{12}} - \frac{b \int \frac{(a+bx)^{10}}{x^{12}} dx}{12a}$$

$$= -\frac{(a+bx)^{11}}{12ax^{12}} + \frac{b(a+bx)^{11}}{132a^2x^{11}}$$

Mathematica [B] time = 0.00, size = 128, normalized size = 3.56

$$\frac{a^{10}}{12x^{12}} - \frac{10a^9b}{11x^{11}} - \frac{9a^8b^2}{2x^{10}} - \frac{40a^7b^3}{3x^9} - \frac{105a^6b^4}{4x^8} - \frac{36a^5b^5}{x^7} - \frac{35a^4b^6}{x^6} - \frac{24a^3b^7}{x^5} - \frac{45a^2b^8}{4x^4} - \frac{10ab^9}{3x^3} - \frac{b^{10}}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^13, x]

[Out] -1/12*a^10/x^12 - (10*a^9*b)/(11*x^11) - (9*a^8*b^2)/(2*x^10) - (40*a^7*b^3)/(3*x^9) - (105*a^6*b^4)/(4*x^8) - (36*a^5*b^5)/x^7 - (35*a^4*b^6)/x^6 - (24*a^3*b^7)/x^5 - (45*a^2*b^8)/(4*x^4) - (10*a*b^9)/(3*x^3) - b^10/(2*x^2)

fricas [B] time = 0.45, size = 112, normalized size = 3.11

$$\frac{66b^{10}x^{10} + 440ab^9x^9 + 1485a^2b^8x^8 + 3168a^3b^7x^7 + 4620a^4b^6x^6 + 4752a^5b^5x^5 + 3465a^6b^4x^4 + 1760a^7b^3x^3}{132x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^13, x, algorithm="fricas")

[Out] -1/132*(66*b^10*x^10 + 440*a*b^9*x^9 + 1485*a^2*b^8*x^8 + 3168*a^3*b^7*x^7 + 4620*a^4*b^6*x^6 + 4752*a^5*b^5*x^5 + 3465*a^6*b^4*x^4 + 1760*a^7*b^3*x^3 + 594*a^8*b^2*x^2 + 120*a^9*b*x + 11*a^10)/x^12

giac [B] time = 0.96, size = 112, normalized size = 3.11

$$\frac{66b^{10}x^{10} + 440ab^9x^9 + 1485a^2b^8x^8 + 3168a^3b^7x^7 + 4620a^4b^6x^6 + 4752a^5b^5x^5 + 3465a^6b^4x^4 + 1760a^7b^3x^3}{132x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^13, x, algorithm="giac")

[Out] -1/132*(66*b^10*x^10 + 440*a*b^9*x^9 + 1485*a^2*b^8*x^8 + 3168*a^3*b^7*x^7 + 4620*a^4*b^6*x^6 + 4752*a^5*b^5*x^5 + 3465*a^6*b^4*x^4 + 1760*a^7*b^3*x^3 + 594*a^8*b^2*x^2 + 120*a^9*b*x + 11*a^10)/x^12

maple [B] time = 0.00, size = 113, normalized size = 3.14

$$\frac{b^{10}}{2x^2} - \frac{10ab^9}{3x^3} - \frac{45a^2b^8}{4x^4} - \frac{24a^3b^7}{x^5} - \frac{35a^4b^6}{x^6} - \frac{36a^5b^5}{x^7} - \frac{105a^6b^4}{4x^8} - \frac{40a^7b^3}{3x^9} - \frac{9a^8b^2}{2x^{10}} - \frac{10a^9b}{11x^{11}} - \frac{a^{10}}{12x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^13,x)

[Out] $-35*a^4*b^6/x^6 - 10/11*a^9*b/x^{11} - 1/12*a^{10}/x^{12} - 40/3*a^7*b^3/x^9 - 10/3*a*b^9/x^3 - 45/4*a^2*b^8/x^4 - 1/2*b^{10}/x^2 - 24*a^3*b^7/x^5 - 9/2*a^8*b^2/x^{10} - 36*a^5*b^5/x^7 - 105/4*a^6*b^4/x^8$

maxima [B] time = 1.39, size = 112, normalized size = 3.11

$$\frac{66b^{10}x^{10} + 440ab^9x^9 + 1485a^2b^8x^8 + 3168a^3b^7x^7 + 4620a^4b^6x^6 + 4752a^5b^5x^5 + 3465a^6b^4x^4 + 1760a^7b^3x^3 + 594a^8b^2x^2 + 120a^9bx + 11a^{10}}{132x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^13,x, algorithm="maxima")

[Out] $-1/132*(66*b^{10}*x^{10} + 440*a*b^9*x^9 + 1485*a^2*b^8*x^8 + 3168*a^3*b^7*x^7 + 4620*a^4*b^6*x^6 + 4752*a^5*b^5*x^5 + 3465*a^6*b^4*x^4 + 1760*a^7*b^3*x^3 + 594*a^8*b^2*x^2 + 120*a^9*b*x + 11*a^{10})/x^{12}$

mupad [B] time = 0.10, size = 23, normalized size = 0.64

$$\frac{(11a - bx)(a + bx)^{11}}{132a^2x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^13,x)

[Out] $-((11*a - b*x)*(a + b*x)^{11})/(132*a^2*x^{12})$

sympy [B] time = 0.99, size = 121, normalized size = 3.36

$$\frac{-11a^{10} - 120a^9bx - 594a^8b^2x^2 - 1760a^7b^3x^3 - 3465a^6b^4x^4 - 4752a^5b^5x^5 - 4620a^4b^6x^6 - 3168a^3b^7x^7 - 1485a^2b^8x^8 - 440ab^9x^9 - 66b^{10}x^{10}}{132x^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**13,x)

[Out] $(-11*a^{10} - 120*a^{9}*b*x - 594*a^{8}*b^{2}*x^{2} - 1760*a^{7}*b^{3}*x^{3} - 3465*a^{6}*b^{4}*x^{4} - 4752*a^{5}*b^{5}*x^{5} - 4620*a^{4}*b^{6}*x^{6} - 3168*a^{3}*b^{7}*x^{7} - 1485*a^{2}*b^{8}*x^{8} - 440*a*b^{9}*x^{9} - 66*b^{10}*x^{10})/(132*x^{12})$

$$3.148 \quad \int \frac{(a+bx)^{10}}{x^{14}} dx$$

Optimal. Leaf size=56

$$-\frac{b^2(a+bx)^{11}}{858a^3x^{11}} + \frac{b(a+bx)^{11}}{78a^2x^{12}} - \frac{(a+bx)^{11}}{13ax^{13}}$$

[Out] $-1/13*(b*x+a)^{11}/a/x^{13}+1/78*b*(b*x+a)^{11}/a^2/x^{12}-1/858*b^2*(b*x+a)^{11}/a^3/x^{11}$

Rubi [A] time = 0.01, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$-\frac{b^2(a+bx)^{11}}{858a^3x^{11}} + \frac{b(a+bx)^{11}}{78a^2x^{12}} - \frac{(a+bx)^{11}}{13ax^{13}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^14, x]

[Out] $-(a + b*x)^{11}/(13*a*x^{13}) + (b*(a + b*x)^{11})/(78*a^2*x^{12}) - (b^2*(a + b*x)^{11})/(858*a^3*x^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{10}}{x^{14}} dx &= -\frac{(a+bx)^{11}}{13ax^{13}} - \frac{(2b) \int \frac{(a+bx)^{10}}{x^{13}} dx}{13a} \\
&= -\frac{(a+bx)^{11}}{13ax^{13}} + \frac{b(a+bx)^{11}}{78a^2x^{12}} + \frac{b^2 \int \frac{(a+bx)^{10}}{x^{12}} dx}{78a^2} \\
&= -\frac{(a+bx)^{11}}{13ax^{13}} + \frac{b(a+bx)^{11}}{78a^2x^{12}} - \frac{b^2(a+bx)^{11}}{858a^3x^{11}}
\end{aligned}$$

Mathematica [B] time = 0.01, size = 126, normalized size = 2.25

$$\frac{a^{10}}{13x^{13}} - \frac{5a^9b}{6x^{12}} - \frac{45a^8b^2}{11x^{11}} - \frac{12a^7b^3}{x^{10}} - \frac{70a^6b^4}{3x^9} - \frac{63a^5b^5}{2x^8} - \frac{30a^4b^6}{x^7} - \frac{20a^3b^7}{x^6} - \frac{9a^2b^8}{x^5} - \frac{5ab^9}{2x^4} - \frac{b^{10}}{3x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^14,x]

[Out] $-1/13*a^{10}/x^{13} - (5*a^9*b)/(6*x^{12}) - (45*a^8*b^2)/(11*x^{11}) - (12*a^7*b^3)/x^{10} - (70*a^6*b^4)/(3*x^9) - (63*a^5*b^5)/(2*x^8) - (30*a^4*b^6)/x^7 - (20*a^3*b^7)/x^6 - (9*a^2*b^8)/x^5 - (5*a*b^9)/(2*x^4) - b^{10}/(3*x^3)$

fricas [B] time = 0.46, size = 112, normalized size = 2.00

$$\frac{286 b^{10} x^{10} + 2145 a b^9 x^9 + 7722 a^2 b^8 x^8 + 17160 a^3 b^7 x^7 + 25740 a^4 b^6 x^6 + 27027 a^5 b^5 x^5 + 20020 a^6 b^4 x^4 + 10296 a^7 b^3 x^3 + 3510 a^8 b^2 x^2 + 715 a^9 b x + 66 a^{10}}{858 x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^14,x, algorithm="fricas")

[Out] $-1/858*(286*b^{10}*x^{10} + 2145*a*b^9*x^9 + 7722*a^2*b^8*x^8 + 17160*a^3*b^7*x^7 + 25740*a^4*b^6*x^6 + 27027*a^5*b^5*x^5 + 20020*a^6*b^4*x^4 + 10296*a^7*b^3*x^3 + 3510*a^8*b^2*x^2 + 715*a^9*b*x + 66*a^{10})/x^{13}$

giac [B] time = 1.03, size = 112, normalized size = 2.00

$$\frac{286 b^{10} x^{10} + 2145 a b^9 x^9 + 7722 a^2 b^8 x^8 + 17160 a^3 b^7 x^7 + 25740 a^4 b^6 x^6 + 27027 a^5 b^5 x^5 + 20020 a^6 b^4 x^4 + 10296 a^7 b^3 x^3 + 3510 a^8 b^2 x^2 + 715 a^9 b x + 66 a^{10}}{858 x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^14,x, algorithm="giac")

[Out] $-1/858*(286*b^{10}*x^{10} + 2145*a*b^9*x^9 + 7722*a^2*b^8*x^8 + 17160*a^3*b^7*x^7 + 25740*a^4*b^6*x^6 + 27027*a^5*b^5*x^5 + 20020*a^6*b^4*x^4 + 10296*a^7*b^3*x^3 + 3510*a^8*b^2*x^2 + 715*a^9*b*x + 66*a^{10})/x^{13}$

maple [B] time = 0.00, size = 113, normalized size = 2.02

$$\frac{b^{10}}{3x^3} - \frac{5ab^9}{2x^4} - \frac{9a^2b^8}{x^5} - \frac{20a^3b^7}{x^6} - \frac{30a^4b^6}{x^7} - \frac{63a^5b^5}{2x^8} - \frac{70a^6b^4}{3x^9} - \frac{12a^7b^3}{x^{10}} - \frac{45a^8b^2}{11x^{11}} - \frac{5a^9b}{6x^{12}} - \frac{a^{10}}{13x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^10/x^14,x)`

[Out] $-20*a^3*b^7/x^6 - 1/13*a^{10}/x^{13} - 70/3*a^6*b^4/x^9 - 9*a^2*b^8/x^5 - 1/3*b^{10}/x^3 - 45/11*a^8*b^2/x^{11} - 5/2*a*b^9/x^4 - 12*a^7*b^3/x^{10} - 5/6*a^9*b/x^{12} - 30*a^4*b^6/x^7 - 63/2*a^5*b^5/x^8$

maxima [B] time = 1.37, size = 112, normalized size = 2.00

$$\frac{286 b^{10} x^{10} + 2145 a b^9 x^9 + 7722 a^2 b^8 x^8 + 17160 a^3 b^7 x^7 + 25740 a^4 b^6 x^6 + 27027 a^5 b^5 x^5 + 20020 a^6 b^4 x^4 + 10296 a^7 b^3 x^3 + 3510 a^8 b^2 x^2 + 715 a^9 b x + 66 a^{10}}{858 x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^10/x^14,x, algorithm="maxima")`

[Out] $-1/858*(286*b^{10}*x^{10} + 2145*a*b^9*x^9 + 7722*a^2*b^8*x^8 + 17160*a^3*b^7*x^7 + 25740*a^4*b^6*x^6 + 27027*a^5*b^5*x^5 + 20020*a^6*b^4*x^4 + 10296*a^7*b^3*x^3 + 3510*a^8*b^2*x^2 + 715*a^9*b*x + 66*a^{10})/x^{13}$

mupad [B] time = 0.13, size = 112, normalized size = 2.00

$$\frac{\frac{a^{10}}{13} + \frac{5a^9bx}{6} + \frac{45a^8b^2x^2}{11} + 12a^7b^3x^3 + \frac{70a^6b^4x^4}{3} + \frac{63a^5b^5x^5}{2} + 30a^4b^6x^6 + 20a^3b^7x^7 + 9a^2b^8x^8 + \frac{5ab^9x^9}{2} + \frac{b^{10}}{3}}{x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^10/x^14,x)`

[Out] $-(a^{10}/13 + (b^{10}*x^{10})/3 + (5*a*b^9*x^9)/2 + (45*a^8*b^2*x^2)/11 + 12*a^7*b^3*x^3 + (70*a^6*b^4*x^4)/3 + (63*a^5*b^5*x^5)/2 + 30*a^4*b^6*x^6 + 20*a^3*b^7*x^7 + 9*a^2*b^8*x^8 + (5*a^9*b*x)/6)/x^{13}$

sympy [B] time = 1.22, size = 121, normalized size = 2.16

$$\frac{-66a^{10} - 715a^9bx - 3510a^8b^2x^2 - 10296a^7b^3x^3 - 20020a^6b^4x^4 - 27027a^5b^5x^5 - 25740a^4b^6x^6 - 17160a^3b^7x^7 - 715a^2b^8x^8 - 66a^{10}}{858x^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**10/x**14,x)
```

```
[Out] (-66*a**10 - 715*a**9*b*x - 3510*a**8*b**2*x**2 - 10296*a**7*b**3*x**3 - 20020*a**6*b**4*x**4 - 27027*a**5*b**5*x**5 - 25740*a**4*b**6*x**6 - 17160*a**3*b**7*x**7 - 7722*a**2*b**8*x**8 - 2145*a*b**9*x**9 - 286*b**10*x**10)/(858*x**13)
```

$$3.149 \quad \int \frac{(a+bx)^{10}}{x^{15}} dx$$

Optimal. Leaf size=76

$$\frac{b^3(a+bx)^{11}}{4004a^4x^{11}} - \frac{b^2(a+bx)^{11}}{364a^3x^{12}} + \frac{3b(a+bx)^{11}}{182a^2x^{13}} - \frac{(a+bx)^{11}}{14ax^{14}}$$

[Out] $-1/14*(b*x+a)^{11}/a/x^{14}+3/182*b*(b*x+a)^{11}/a^2/x^{13}-1/364*b^2*(b*x+a)^{11}/a^3/x^{12}+1/4004*b^3*(b*x+a)^{11}/a^4/x^{11}$

Rubi [A] time = 0.02, antiderivative size = 76, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{b^3(a+bx)^{11}}{4004a^4x^{11}} - \frac{b^2(a+bx)^{11}}{364a^3x^{12}} + \frac{3b(a+bx)^{11}}{182a^2x^{13}} - \frac{(a+bx)^{11}}{14ax^{14}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^15, x]

[Out] $-(a + b*x)^{11}/(14*a*x^{14}) + (3*b*(a + b*x)^{11})/(182*a^2*x^{13}) - (b^2*(a + b*x)^{11})/(364*a^3*x^{12}) + (b^3*(a + b*x)^{11})/(4004*a^4*x^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{10}}{x^{15}} dx &= -\frac{(a+bx)^{11}}{14ax^{14}} - \frac{(3b) \int \frac{(a+bx)^{10}}{x^{14}} dx}{14a} \\
&= -\frac{(a+bx)^{11}}{14ax^{14}} + \frac{3b(a+bx)^{11}}{182a^2x^{13}} + \frac{(3b^2) \int \frac{(a+bx)^{10}}{x^{13}} dx}{91a^2} \\
&= -\frac{(a+bx)^{11}}{14ax^{14}} + \frac{3b(a+bx)^{11}}{182a^2x^{13}} - \frac{b^2(a+bx)^{11}}{364a^3x^{12}} - \frac{b^3 \int \frac{(a+bx)^{10}}{x^{12}} dx}{364a^3} \\
&= -\frac{(a+bx)^{11}}{14ax^{14}} + \frac{3b(a+bx)^{11}}{182a^2x^{13}} - \frac{b^2(a+bx)^{11}}{364a^3x^{12}} + \frac{b^3(a+bx)^{11}}{4004a^4x^{11}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 128, normalized size = 1.68

$$\frac{a^{10}}{14x^{14}} - \frac{10a^9b}{13x^{13}} - \frac{15a^8b^2}{4x^{12}} - \frac{120a^7b^3}{11x^{11}} - \frac{21a^6b^4}{x^{10}} - \frac{28a^5b^5}{x^9} - \frac{105a^4b^6}{4x^8} - \frac{120a^3b^7}{7x^7} - \frac{15a^2b^8}{2x^6} - \frac{2ab^9}{x^5} - \frac{b^{10}}{4x^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^15, x]

[Out] $-1/14*a^{10}/x^{14} - (10*a^9*b)/(13*x^{13}) - (15*a^8*b^2)/(4*x^{12}) - (120*a^7*b^3)/(11*x^{11}) - (21*a^6*b^4)/x^{10} - (28*a^5*b^5)/x^9 - (105*a^4*b^6)/(4*x^8) - (120*a^3*b^7)/(7*x^7) - (15*a^2*b^8)/(2*x^6) - (2*a*b^9)/x^5 - b^{10}/(4*x^4)$

fricas [A] time = 0.46, size = 112, normalized size = 1.47

$$\frac{1001 b^{10} x^{10} + 8008 a b^9 x^9 + 30030 a^2 b^8 x^8 + 68640 a^3 b^7 x^7 + 105105 a^4 b^6 x^6 + 112112 a^5 b^5 x^5 + 84084 a^6 b^4 x^4 + 43680 a^7 b^3 x^3 + 15015 a^8 b^2 x^2 + 3080 a^9 b x + 286 a^{10}}{4004 x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^15, x, algorithm="fricas")

[Out] $-1/4004*(1001*b^{10}*x^{10} + 8008*a*b^9*x^9 + 30030*a^2*b^8*x^8 + 68640*a^3*b^7*x^7 + 105105*a^4*b^6*x^6 + 112112*a^5*b^5*x^5 + 84084*a^6*b^4*x^4 + 43680*a^7*b^3*x^3 + 15015*a^8*b^2*x^2 + 3080*a^9*b*x + 286*a^{10})/x^{14}$

giac [A] time = 0.89, size = 112, normalized size = 1.47

$$\frac{1001 b^{10} x^{10} + 8008 a b^9 x^9 + 30030 a^2 b^8 x^8 + 68640 a^3 b^7 x^7 + 105105 a^4 b^6 x^6 + 112112 a^5 b^5 x^5 + 84084 a^6 b^4 x^4 + 43680 a^7 b^3 x^3 + 15015 a^8 b^2 x^2 + 3080 a^9 b x + 286 a^{10}}{4004 x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^15,x, algorithm="giac")

[Out] $-1/4004*(1001*b^{10}*x^{10} + 8008*a*b^9*x^9 + 30030*a^2*b^8*x^8 + 68640*a^3*b^7*x^7 + 105105*a^4*b^6*x^6 + 112112*a^5*b^5*x^5 + 84084*a^6*b^4*x^4 + 43680*a^7*b^3*x^3 + 15015*a^8*b^2*x^2 + 3080*a^9*b*x + 286*a^{10})/x^{14}$

maple [A] time = 0.01, size = 113, normalized size = 1.49

$$\frac{b^{10}}{4x^4} - \frac{2ab^9}{x^5} - \frac{15a^2b^8}{2x^6} - \frac{120a^3b^7}{7x^7} - \frac{105a^4b^6}{4x^8} - \frac{28a^5b^5}{x^9} - \frac{21a^6b^4}{x^{10}} - \frac{120a^7b^3}{11x^{11}} - \frac{15a^8b^2}{4x^{12}} - \frac{10a^9b}{13x^{13}} - \frac{a^{10}}{14x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^15,x)

[Out] $-15/4*a^8*b^2/x^{12}-15/2*a^2*b^8/x^6-10/13*a^9*b/x^{13}-28*a^5*b^5/x^9-1/4*b^{10}/x^4-120/11*a^7*b^3/x^{11}-2*a*b^9/x^5-1/14*a^{10}/x^{14}-21*a^6*b^4/x^{10}-120/7*a^3*b^7/x^7-105/4*a^4*b^6/x^8$

maxima [A] time = 1.28, size = 112, normalized size = 1.47

$$\frac{1001 b^{10} x^{10} + 8008 a b^9 x^9 + 30030 a^2 b^8 x^8 + 68640 a^3 b^7 x^7 + 105105 a^4 b^6 x^6 + 112112 a^5 b^5 x^5 + 84084 a^6 b^4 x^4 + 43680 a^7 b^3 x^3 + 15015 a^8 b^2 x^2 + 3080 a^9 b x + 286 a^{10}}{4004 x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^15,x, algorithm="maxima")

[Out] $-1/4004*(1001*b^{10}*x^{10} + 8008*a*b^9*x^9 + 30030*a^2*b^8*x^8 + 68640*a^3*b^7*x^7 + 105105*a^4*b^6*x^6 + 112112*a^5*b^5*x^5 + 84084*a^6*b^4*x^4 + 43680*a^7*b^3*x^3 + 15015*a^8*b^2*x^2 + 3080*a^9*b*x + 286*a^{10})/x^{14}$

mupad [B] time = 0.09, size = 112, normalized size = 1.47

$$\frac{\frac{a^{10}}{14} + \frac{10 a^9 b x}{13} + \frac{15 a^8 b^2 x^2}{4} + \frac{120 a^7 b^3 x^3}{11} + 21 a^6 b^4 x^4 + 28 a^5 b^5 x^5 + \frac{105 a^4 b^6 x^6}{4} + \frac{120 a^3 b^7 x^7}{7} + \frac{15 a^2 b^8 x^8}{2} + 2 a b^9 x^9 + \frac{a^{10}}{14}}{x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^15,x)

[Out] $-(a^{10}/14 + (b^{10}*x^{10})/4 + 2*a*b^9*x^9 + (15*a^8*b^2*x^2)/4 + (120*a^7*b^3*x^3)/11 + 21*a^6*b^4*x^4 + 28*a^5*b^5*x^5 + (105*a^4*b^6*x^6)/4 + (120*a^3*b^7*x^7)/7 + (15*a^2*b^8*x^8)/2 + (10*a^9*b*x)/13)/x^{14}$

sympy [A] time = 1.10, size = 121, normalized size = 1.59

$$\frac{-286a^{10} - 3080a^9bx - 15015a^8b^2x^2 - 43680a^7b^3x^3 - 84084a^6b^4x^4 - 112112a^5b^5x^5 - 105105a^4b^6x^6 - 68640a^3b^7x^7 - 15015a^2b^8x^8 - 3080a^9bx + 286a^{10}}{4004x^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**10/x**15,x)
```

```
[Out] (-286*a**10 - 3080*a**9*b*x - 15015*a**8*b**2*x**2 - 43680*a**7*b**3*x**3 -  
84084*a**6*b**4*x**4 - 112112*a**5*b**5*x**5 - 105105*a**4*b**6*x**6 - 686  
40*a**3*b**7*x**7 - 30030*a**2*b**8*x**8 - 8008*a*b**9*x**9 - 1001*b**10*x*  
*10)/(4004*x**14)
```

$$3.150 \quad \int \frac{(a+bx)^{10}}{x^{16}} dx$$

Optimal. Leaf size=96

$$-\frac{b^4(a+bx)^{11}}{15015a^5x^{11}} + \frac{b^3(a+bx)^{11}}{1365a^4x^{12}} - \frac{2b^2(a+bx)^{11}}{455a^3x^{13}} + \frac{2b(a+bx)^{11}}{105a^2x^{14}} - \frac{(a+bx)^{11}}{15ax^{15}}$$

[Out] $-1/15*(b*x+a)^{11}/a/x^{15}+2/105*b*(b*x+a)^{11}/a^2/x^{14}-2/455*b^2*(b*x+a)^{11}/a^3/x^{13}+1/1365*b^3*(b*x+a)^{11}/a^4/x^{12}-1/15015*b^4*(b*x+a)^{11}/a^5/x^{11}$

Rubi [A] time = 0.03, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$-\frac{b^4(a+bx)^{11}}{15015a^5x^{11}} + \frac{b^3(a+bx)^{11}}{1365a^4x^{12}} - \frac{2b^2(a+bx)^{11}}{455a^3x^{13}} + \frac{2b(a+bx)^{11}}{105a^2x^{14}} - \frac{(a+bx)^{11}}{15ax^{15}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^16, x]

[Out] $-(a + b*x)^{11}/(15*a*x^{15}) + (2*b*(a + b*x)^{11})/(105*a^2*x^{14}) - (2*b^2*(a + b*x)^{11})/(455*a^3*x^{13}) + (b^3*(a + b*x)^{11})/(1365*a^4*x^{12}) - (b^4*(a + b*x)^{11})/(15015*a^5*x^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{10}}{x^{16}} dx &= -\frac{(a+bx)^{11}}{15ax^{15}} - \frac{(4b) \int \frac{(a+bx)^{10}}{x^{15}} dx}{15a} \\
&= -\frac{(a+bx)^{11}}{15ax^{15}} + \frac{2b(a+bx)^{11}}{105a^2x^{14}} + \frac{(2b^2) \int \frac{(a+bx)^{10}}{x^{14}} dx}{35a^2} \\
&= -\frac{(a+bx)^{11}}{15ax^{15}} + \frac{2b(a+bx)^{11}}{105a^2x^{14}} - \frac{2b^2(a+bx)^{11}}{455a^3x^{13}} - \frac{(4b^3) \int \frac{(a+bx)^{10}}{x^{13}} dx}{455a^3} \\
&= -\frac{(a+bx)^{11}}{15ax^{15}} + \frac{2b(a+bx)^{11}}{105a^2x^{14}} - \frac{2b^2(a+bx)^{11}}{455a^3x^{13}} + \frac{b^3(a+bx)^{11}}{1365a^4x^{12}} + \frac{b^4 \int \frac{(a+bx)^{10}}{x^{12}} dx}{1365a^4} \\
&= -\frac{(a+bx)^{11}}{15ax^{15}} + \frac{2b(a+bx)^{11}}{105a^2x^{14}} - \frac{2b^2(a+bx)^{11}}{455a^3x^{13}} + \frac{b^3(a+bx)^{11}}{1365a^4x^{12}} - \frac{b^4(a+bx)^{11}}{15015a^5x^{11}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 130, normalized size = 1.35

$$\frac{a^{10}}{15x^{15}} - \frac{5a^9b}{7x^{14}} - \frac{45a^8b^2}{13x^{13}} - \frac{10a^7b^3}{x^{12}} - \frac{210a^6b^4}{11x^{11}} - \frac{126a^5b^5}{5x^{10}} - \frac{70a^4b^6}{3x^9} - \frac{15a^3b^7}{x^8} - \frac{45a^2b^8}{7x^7} - \frac{5ab^9}{3x^6} - \frac{b^{10}}{5x^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^16, x]

[Out] $-1/15*a^{10}/x^{15} - (5*a^9*b)/(7*x^{14}) - (45*a^8*b^2)/(13*x^{13}) - (10*a^7*b^3)/x^{12} - (210*a^6*b^4)/(11*x^{11}) - (126*a^5*b^5)/(5*x^{10}) - (70*a^4*b^6)/(3*x^9) - (15*a^3*b^7)/x^8 - (45*a^2*b^8)/(7*x^7) - (5*a*b^9)/(3*x^6) - b^{10}/(5*x^5)$

fricas [A] time = 0.44, size = 112, normalized size = 1.17

$$\frac{3003b^{10}x^{10} + 25025ab^9x^9 + 96525a^2b^8x^8 + 225225a^3b^7x^7 + 350350a^4b^6x^6 + 378378a^5b^5x^5 + 286650a^6b^4x^4 + 150150a^7b^3x^3 + 51975a^8b^2x^2 + 10725a^9bx + 1001a^{10}}{15015x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^16, x, algorithm="fricas")

[Out] $-1/15015*(3003*b^{10}*x^{10} + 25025*a*b^9*x^9 + 96525*a^2*b^8*x^8 + 225225*a^3*b^7*x^7 + 350350*a^4*b^6*x^6 + 378378*a^5*b^5*x^5 + 286650*a^6*b^4*x^4 + 150150*a^7*b^3*x^3 + 51975*a^8*b^2*x^2 + 10725*a^9*b*x + 1001*a^{10})/x^{15}$

giac [A] time = 1.52, size = 112, normalized size = 1.17

$$\frac{3003b^{10}x^{10} + 25025ab^9x^9 + 96525a^2b^8x^8 + 225225a^3b^7x^7 + 350350a^4b^6x^6 + 378378a^5b^5x^5 + 286650a^6b^4x^4 + 150150a^7b^3x^3 + 51975a^8b^2x^2 + 10725a^9bx + 1001a^{10}}{15015x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^16,x, algorithm="giac")

[Out] $-1/15015*(3003*b^{10}*x^{10} + 25025*a*b^9*x^9 + 96525*a^2*b^8*x^8 + 225225*a^3*b^7*x^7 + 350350*a^4*b^6*x^6 + 378378*a^5*b^5*x^5 + 286650*a^6*b^4*x^4 + 150150*a^7*b^3*x^3 + 51975*a^8*b^2*x^2 + 10725*a^9*b*x + 1001*a^{10})/x^{15}$

maple [A] time = 0.01, size = 113, normalized size = 1.18

$$\frac{b^{10}}{5x^5} - \frac{5ab^9}{3x^6} - \frac{45a^2b^8}{7x^7} - \frac{15a^3b^7}{x^8} - \frac{70a^4b^6}{3x^9} - \frac{126a^5b^5}{5x^{10}} - \frac{210a^6b^4}{11x^{11}} - \frac{10a^7b^3}{x^{12}} - \frac{45a^8b^2}{13x^{13}} - \frac{5a^9b}{7x^{14}} - \frac{a^{10}}{15x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^16,x)

[Out] $-5/3*a*b^9/x^6 - 210/11*a^6*b^4/x^{11} - 70/3*a^4*b^6/x^9 - 1/5*b^{10}/x^5 - 45/13*a^8*b^2/x^{13} - 5/7*a^9*b/x^{14} - 10*a^7*b^3/x^{12} - 126/5*a^5*b^5/x^{10} - 1/15*a^{10}/x^{15} - 45/7*a^2*b^8/x^7 - 15*a^3*b^7/x^8$

maxima [A] time = 1.36, size = 112, normalized size = 1.17

$$\frac{3003 b^{10} x^{10} + 25025 a b^9 x^9 + 96525 a^2 b^8 x^8 + 225225 a^3 b^7 x^7 + 350350 a^4 b^6 x^6 + 378378 a^5 b^5 x^5 + 286650 a^6 b^4 x^4 + 150150 a^7 b^3 x^3 + 51975 a^8 b^2 x^2 + 10725 a^9 b x + 1001 a^{10}}{15015 x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^16,x, algorithm="maxima")

[Out] $-1/15015*(3003*b^{10}*x^{10} + 25025*a*b^9*x^9 + 96525*a^2*b^8*x^8 + 225225*a^3*b^7*x^7 + 350350*a^4*b^6*x^6 + 378378*a^5*b^5*x^5 + 286650*a^6*b^4*x^4 + 150150*a^7*b^3*x^3 + 51975*a^8*b^2*x^2 + 10725*a^9*b*x + 1001*a^{10})/x^{15}$

mupad [B] time = 0.13, size = 112, normalized size = 1.17

$$\frac{\frac{a^{10}}{15} + \frac{5a^9bx}{7} + \frac{45a^8b^2x^2}{13} + 10a^7b^3x^3 + \frac{210a^6b^4x^4}{11} + \frac{126a^5b^5x^5}{5} + \frac{70a^4b^6x^6}{3} + 15a^3b^7x^7 + \frac{45a^2b^8x^8}{7} + \frac{5ab^9x^9}{3} + \frac{b^{10}x^{10}}{5}}{x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^16,x)

[Out] $-(a^{10}/15 + (b^{10}*x^{10})/5 + (5*a*b^9*x^9)/3 + (45*a^8*b^2*x^2)/13 + 10*a^7*b^3*x^3 + (210*a^6*b^4*x^4)/11 + (126*a^5*b^5*x^5)/5 + (70*a^4*b^6*x^6)/3 + 15*a^3*b^7*x^7 + (45*a^2*b^8*x^8)/7 + (5*a^9*b*x)/7)/x^{15}$

sympy [A] time = 1.25, size = 121, normalized size = 1.26

$$\frac{-1001a^{10} - 10725a^9bx - 51975a^8b^2x^2 - 150150a^7b^3x^3 - 286650a^6b^4x^4 - 378378a^5b^5x^5 - 350350a^4b^6x^6 - 225225a^3b^7x^7 - 96525a^2b^8x^8 - 25025ab^9x^9 - 3003b^{10}x^{10}}{15015x^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**16,x)

[Out] (-1001*a**10 - 10725*a**9*b*x - 51975*a**8*b**2*x**2 - 150150*a**7*b**3*x**3 - 286650*a**6*b**4*x**4 - 378378*a**5*b**5*x**5 - 350350*a**4*b**6*x**6 - 225225*a**3*b**7*x**7 - 96525*a**2*b**8*x**8 - 25025*a*b**9*x**9 - 3003*b**10*x**10)/(15015*x**15)

$$3.151 \quad \int \frac{(a+bx)^{10}}{x^{17}} dx$$

Optimal. Leaf size=116

$$\frac{b^5(a+bx)^{11}}{48048a^6x^{11}} - \frac{b^4(a+bx)^{11}}{4368a^5x^{12}} + \frac{b^3(a+bx)^{11}}{728a^4x^{13}} - \frac{b^2(a+bx)^{11}}{168a^3x^{14}} + \frac{b(a+bx)^{11}}{48a^2x^{15}} - \frac{(a+bx)^{11}}{16ax^{16}}$$

[Out] $-1/16*(b*x+a)^{11}/a/x^{16}+1/48*b*(b*x+a)^{11}/a^2/x^{15}-1/168*b^2*(b*x+a)^{11}/a^3/x^{14}+1/728*b^3*(b*x+a)^{11}/a^4/x^{13}-1/4368*b^4*(b*x+a)^{11}/a^5/x^{12}+1/48048*b^5*(b*x+a)^{11}/a^6/x^{11}$

Rubi [A] time = 0.04, antiderivative size = 116, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{b^5(a+bx)^{11}}{48048a^6x^{11}} - \frac{b^4(a+bx)^{11}}{4368a^5x^{12}} + \frac{b^3(a+bx)^{11}}{728a^4x^{13}} - \frac{b^2(a+bx)^{11}}{168a^3x^{14}} + \frac{b(a+bx)^{11}}{48a^2x^{15}} - \frac{(a+bx)^{11}}{16ax^{16}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^17, x]

[Out] $-(a + b*x)^{11}/(16*a*x^{16}) + (b*(a + b*x)^{11})/(48*a^2*x^{15}) - (b^2*(a + b*x)^{11})/(168*a^3*x^{14}) + (b^3*(a + b*x)^{11})/(728*a^4*x^{13}) - (b^4*(a + b*x)^{11})/(4368*a^5*x^{12}) + (b^5*(a + b*x)^{11})/(48048*a^6*x^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{10}}{x^{17}} dx &= -\frac{(a+bx)^{11}}{16ax^{16}} - \frac{(5b) \int \frac{(a+bx)^{10}}{x^{16}} dx}{16a} \\
&= -\frac{(a+bx)^{11}}{16ax^{16}} + \frac{b(a+bx)^{11}}{48a^2x^{15}} + \frac{b^2 \int \frac{(a+bx)^{10}}{x^{15}} dx}{12a^2} \\
&= -\frac{(a+bx)^{11}}{16ax^{16}} + \frac{b(a+bx)^{11}}{48a^2x^{15}} - \frac{b^2(a+bx)^{11}}{168a^3x^{14}} - \frac{b^3 \int \frac{(a+bx)^{10}}{x^{14}} dx}{56a^3} \\
&= -\frac{(a+bx)^{11}}{16ax^{16}} + \frac{b(a+bx)^{11}}{48a^2x^{15}} - \frac{b^2(a+bx)^{11}}{168a^3x^{14}} + \frac{b^3(a+bx)^{11}}{728a^4x^{13}} + \frac{b^4 \int \frac{(a+bx)^{10}}{x^{13}} dx}{364a^4} \\
&= -\frac{(a+bx)^{11}}{16ax^{16}} + \frac{b(a+bx)^{11}}{48a^2x^{15}} - \frac{b^2(a+bx)^{11}}{168a^3x^{14}} + \frac{b^3(a+bx)^{11}}{728a^4x^{13}} - \frac{b^4(a+bx)^{11}}{4368a^5x^{12}} - \frac{b^5 \int \frac{(a+bx)^{10}}{x^{12}} dx}{4368a^5} \\
&= -\frac{(a+bx)^{11}}{16ax^{16}} + \frac{b(a+bx)^{11}}{48a^2x^{15}} - \frac{b^2(a+bx)^{11}}{168a^3x^{14}} + \frac{b^3(a+bx)^{11}}{728a^4x^{13}} - \frac{b^4(a+bx)^{11}}{4368a^5x^{12}} + \frac{b^5(a+bx)^{11}}{48048a^6x^{11}}
\end{aligned}$$

Mathematica [A] time = 0.00, size = 132, normalized size = 1.14

$$-\frac{a^{10}}{16x^{16}} - \frac{2a^9b}{3x^{15}} - \frac{45a^8b^2}{14x^{14}} - \frac{120a^7b^3}{13x^{13}} - \frac{35a^6b^4}{2x^{12}} - \frac{252a^5b^5}{11x^{11}} - \frac{21a^4b^6}{x^{10}} - \frac{40a^3b^7}{3x^9} - \frac{45a^2b^8}{8x^8} - \frac{10ab^9}{7x^7} - \frac{b^{10}}{6x^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^17, x]

[Out] $-1/16*a^{10}/x^{16} - (2*a^9*b)/(3*x^{15}) - (45*a^8*b^2)/(14*x^{14}) - (120*a^7*b^3)/(13*x^{13}) - (35*a^6*b^4)/(2*x^{12}) - (252*a^5*b^5)/(11*x^{11}) - (21*a^4*b^6)/x^{10} - (40*a^3*b^7)/(3*x^9) - (45*a^2*b^8)/(8*x^8) - (10*a*b^9)/(7*x^7) - b^{10}/(6*x^6)$

fricas [A] time = 0.54, size = 112, normalized size = 0.97

$$\frac{8008b^{10}x^{10} + 68640ab^9x^9 + 270270a^2b^8x^8 + 640640a^3b^7x^7 + 1009008a^4b^6x^6 + 1100736a^5b^5x^5 + 840840a^6b^4x^4 + 443520a^7b^3x^3 + 154440a^8b^2x^2 + 32032a^9b^1x + 3003a^{10}}{48048x^{16}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^17, x, algorithm="fricas")

[Out] $-1/48048*(8008*b^{10}*x^{10} + 68640*a*b^9*x^9 + 270270*a^2*b^8*x^8 + 640640*a^3*b^7*x^7 + 1009008*a^4*b^6*x^6 + 1100736*a^5*b^5*x^5 + 840840*a^6*b^4*x^4 + 443520*a^7*b^3*x^3 + 154440*a^8*b^2*x^2 + 32032*a^9*b*x + 3003*a^{10})/x^{16}$

giac [A] time = 1.10, size = 112, normalized size = 0.97

$$\frac{8008 b^{10} x^{10} + 68640 a b^9 x^9 + 270270 a^2 b^8 x^8 + 640640 a^3 b^7 x^7 + 1009008 a^4 b^6 x^6 + 1100736 a^5 b^5 x^5 + 840840 a^6 b^4 x^4 + 443520 a^7 b^3 x^3 + 154440 a^8 b^2 x^2 + 32032 a^9 b x + 3003 a^{10}}{48048 x^{16}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^17,x, algorithm="giac")

[Out] -1/48048*(8008*b^10*x^10 + 68640*a*b^9*x^9 + 270270*a^2*b^8*x^8 + 640640*a^3*b^7*x^7 + 1009008*a^4*b^6*x^6 + 1100736*a^5*b^5*x^5 + 840840*a^6*b^4*x^4 + 443520*a^7*b^3*x^3 + 154440*a^8*b^2*x^2 + 32032*a^9*b*x + 3003*a^10)/x^16

maple [A] time = 0.01, size = 113, normalized size = 0.97

$$\frac{b^{10}}{6x^6} - \frac{10ab^9}{7x^7} - \frac{45a^2b^8}{8x^8} - \frac{40a^3b^7}{3x^9} - \frac{21a^4b^6}{x^{10}} - \frac{252a^5b^5}{11x^{11}} - \frac{35a^6b^4}{2x^{12}} - \frac{120a^7b^3}{13x^{13}} - \frac{45a^8b^2}{14x^{14}} - \frac{2a^9b}{3x^{15}} - \frac{a^{10}}{16x^{16}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^17,x)

[Out] -1/6*b^10/x^6-120/13*a^7*b^3/x^13-40/3*a^3*b^7/x^9-252/11*a^5*b^5/x^11-45/14*a^8*b^2/x^14-1/16*a^10/x^16-21*a^4*b^6/x^10-2/3*a^9*b/x^15-10/7*a*b^9/x^7-45/8*a^2*b^8/x^8-35/2*a^6*b^4/x^12

maxima [A] time = 1.39, size = 112, normalized size = 0.97

$$\frac{8008 b^{10} x^{10} + 68640 a b^9 x^9 + 270270 a^2 b^8 x^8 + 640640 a^3 b^7 x^7 + 1009008 a^4 b^6 x^6 + 1100736 a^5 b^5 x^5 + 840840 a^6 b^4 x^4 + 443520 a^7 b^3 x^3 + 154440 a^8 b^2 x^2 + 32032 a^9 b x + 3003 a^{10}}{48048 x^{16}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^17,x, algorithm="maxima")

[Out] -1/48048*(8008*b^10*x^10 + 68640*a*b^9*x^9 + 270270*a^2*b^8*x^8 + 640640*a^3*b^7*x^7 + 1009008*a^4*b^6*x^6 + 1100736*a^5*b^5*x^5 + 840840*a^6*b^4*x^4 + 443520*a^7*b^3*x^3 + 154440*a^8*b^2*x^2 + 32032*a^9*b*x + 3003*a^10)/x^16

mupad [B] time = 0.13, size = 112, normalized size = 0.97

$$\frac{\frac{a^{10}}{16} + \frac{2a^9bx}{3} + \frac{45a^8b^2x^2}{14} + \frac{120a^7b^3x^3}{13} + \frac{35a^6b^4x^4}{2} + \frac{252a^5b^5x^5}{11} + 21a^4b^6x^6 + \frac{40a^3b^7x^7}{3} + \frac{45a^2b^8x^8}{8} + \frac{10ab^9x^9}{7} + \frac{b^{10}x^{10}}{6}}{x^{16}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^17,x)

[Out] $-(a^{10}/16 + (b^{10}x^{10})/6 + (10ab^9x^9)/7 + (45a^8b^2x^2)/14 + (120a^7b^3x^3)/13 + (35a^6b^4x^4)/2 + (252a^5b^5x^5)/11 + 21a^4b^6x^6 + (40a^3b^7x^7)/3 + (45a^2b^8x^8)/8 + (2a^9bx)/3)/x^{16}$

sympy [A] time = 1.27, size = 121, normalized size = 1.04

$$\frac{-3003a^{10} - 32032a^9bx - 154440a^8b^2x^2 - 443520a^7b^3x^3 - 840840a^6b^4x^4 - 1100736a^5b^5x^5 - 1009008a^4b^6x^6 - 640640a^3b^7x^7 - 270270a^2b^8x^8 - 68640ab^9x^9 - 8008b^{10}x^{10}}{48048x^{16}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**17,x)

[Out] $(-3003a^{10} - 32032a^9bx - 154440a^8b^2x^2 - 443520a^7b^3x^3 - 840840a^6b^4x^4 - 1100736a^5b^5x^5 - 1009008a^4b^6x^6 - 640640a^3b^7x^7 - 270270a^2b^8x^8 - 68640ab^9x^9 - 8008b^{10}x^{10})/(48048x^{16})$

$$3.152 \quad \int \frac{(a+bx)^{10}}{x^{18}} dx$$

Optimal. Leaf size=136

$$-\frac{b^6(a+bx)^{11}}{136136a^7x^{11}} + \frac{b^5(a+bx)^{11}}{12376a^6x^{12}} - \frac{3b^4(a+bx)^{11}}{6188a^5x^{13}} + \frac{b^3(a+bx)^{11}}{476a^4x^{14}} - \frac{b^2(a+bx)^{11}}{136a^3x^{15}} + \frac{3b(a+bx)^{11}}{136a^2x^{16}} - \frac{(a+bx)^{11}}{17ax^{17}}$$

[Out] $-1/17*(b*x+a)^{11}/a/x^{17}+3/136*b*(b*x+a)^{11}/a^2/x^{16}-1/136*b^2*(b*x+a)^{11}/a^3/x^{15}+1/476*b^3*(b*x+a)^{11}/a^4/x^{14}-3/6188*b^4*(b*x+a)^{11}/a^5/x^{13}+1/12376*b^5*(b*x+a)^{11}/a^6/x^{12}-1/136136*b^6*(b*x+a)^{11}/a^7/x^{11}$

Rubi [A] time = 0.05, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$-\frac{b^6(a+bx)^{11}}{136136a^7x^{11}} + \frac{b^5(a+bx)^{11}}{12376a^6x^{12}} - \frac{3b^4(a+bx)^{11}}{6188a^5x^{13}} + \frac{b^3(a+bx)^{11}}{476a^4x^{14}} - \frac{b^2(a+bx)^{11}}{136a^3x^{15}} + \frac{3b(a+bx)^{11}}{136a^2x^{16}} - \frac{(a+bx)^{11}}{17ax^{17}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^18, x]

[Out] $-(a + b*x)^{11}/(17*a*x^{17}) + (3*b*(a + b*x)^{11})/(136*a^2*x^{16}) - (b^2*(a + b*x)^{11})/(136*a^3*x^{15}) + (b^3*(a + b*x)^{11})/(476*a^4*x^{14}) - (3*b^4*(a + b*x)^{11})/(6188*a^5*x^{13}) + (b^5*(a + b*x)^{11})/(12376*a^6*x^{12}) - (b^6*(a + b*x)^{11})/(136136*a^7*x^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{10}}{x^{18}} dx &= -\frac{(a+bx)^{11}}{17ax^{17}} - \frac{(6b) \int \frac{(a+bx)^{10}}{x^{17}} dx}{17a} \\
&= -\frac{(a+bx)^{11}}{17ax^{17}} + \frac{3b(a+bx)^{11}}{136a^2x^{16}} + \frac{(15b^2) \int \frac{(a+bx)^{10}}{x^{16}} dx}{136a^2} \\
&= -\frac{(a+bx)^{11}}{17ax^{17}} + \frac{3b(a+bx)^{11}}{136a^2x^{16}} - \frac{b^2(a+bx)^{11}}{136a^3x^{15}} - \frac{b^3 \int \frac{(a+bx)^{10}}{x^{15}} dx}{34a^3} \\
&= -\frac{(a+bx)^{11}}{17ax^{17}} + \frac{3b(a+bx)^{11}}{136a^2x^{16}} - \frac{b^2(a+bx)^{11}}{136a^3x^{15}} + \frac{b^3(a+bx)^{11}}{476a^4x^{14}} + \frac{(3b^4) \int \frac{(a+bx)^{10}}{x^{14}} dx}{476a^4} \\
&= -\frac{(a+bx)^{11}}{17ax^{17}} + \frac{3b(a+bx)^{11}}{136a^2x^{16}} - \frac{b^2(a+bx)^{11}}{136a^3x^{15}} + \frac{b^3(a+bx)^{11}}{476a^4x^{14}} - \frac{3b^4(a+bx)^{11}}{6188a^5x^{13}} - \frac{(3b^5) \int \frac{(a+bx)^{10}}{x^{13}} dx}{3094a^5} \\
&= -\frac{(a+bx)^{11}}{17ax^{17}} + \frac{3b(a+bx)^{11}}{136a^2x^{16}} - \frac{b^2(a+bx)^{11}}{136a^3x^{15}} + \frac{b^3(a+bx)^{11}}{476a^4x^{14}} - \frac{3b^4(a+bx)^{11}}{6188a^5x^{13}} + \frac{b^5(a+bx)^{11}}{12376a^6x^{12}} + \dots \\
&= -\frac{(a+bx)^{11}}{17ax^{17}} + \frac{3b(a+bx)^{11}}{136a^2x^{16}} - \frac{b^2(a+bx)^{11}}{136a^3x^{15}} + \frac{b^3(a+bx)^{11}}{476a^4x^{14}} - \frac{3b^4(a+bx)^{11}}{6188a^5x^{13}} + \frac{b^5(a+bx)^{11}}{12376a^6x^{12}} - \dots
\end{aligned}$$

Mathematica [A] time = 0.01, size = 126, normalized size = 0.93

$$\frac{a^{10}}{17x^{17}} - \frac{5a^9b}{8x^{16}} - \frac{3a^8b^2}{x^{15}} - \frac{60a^7b^3}{7x^{14}} - \frac{210a^6b^4}{13x^{13}} - \frac{21a^5b^5}{x^{12}} - \frac{210a^4b^6}{11x^{11}} - \frac{12a^3b^7}{x^{10}} - \frac{5a^2b^8}{x^9} - \frac{5ab^9}{4x^8} - \frac{b^{10}}{7x^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^18,x]

[Out] $-1/17*a^{10}/x^{17} - (5*a^9*b)/(8*x^{16}) - (3*a^8*b^2)/x^{15} - (60*a^7*b^3)/(7*x^{14}) - (210*a^6*b^4)/(13*x^{13}) - (21*a^5*b^5)/x^{12} - (210*a^4*b^6)/(11*x^{11}) - (12*a^3*b^7)/x^{10} - (5*a^2*b^8)/x^9 - (5*a*b^9)/(4*x^8) - b^{10}/(7*x^7)$

fricas [A] time = 0.54, size = 112, normalized size = 0.82

$$\frac{19448 b^{10} x^{10} + 170170 a b^9 x^9 + 680680 a^2 b^8 x^8 + 1633632 a^3 b^7 x^7 + 2598960 a^4 b^6 x^6 + 2858856 a^5 b^5 x^5 + 2199120 a^6 b^4 x^4 + 1237600 a^7 b^3 x^3 + 518400 a^8 b^2 x^2 + 144000 a^9 b x + 19448 a^{10}}{136136 x^{17}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^18,x, algorithm="fricas")

[Out] $-1/136136*(19448*b^{10}*x^{10} + 170170*a*b^9*x^9 + 680680*a^2*b^8*x^8 + 1633632*a^3*b^7*x^7 + 2598960*a^4*b^6*x^6 + 2858856*a^5*b^5*x^5 + 2199120*a^6*b^4*x^4 + 1237600*a^7*b^3*x^3 + 518400*a^8*b^2*x^2 + 144000*a^9*b*x + 19448*a^{10})$

$*x^4 + 1166880*a^7*b^3*x^3 + 408408*a^8*b^2*x^2 + 85085*a^9*b*x + 8008*a^{10})/x^{17}$

giac [A] time = 1.15, size = 112, normalized size = 0.82

$$\frac{19448 b^{10} x^{10} + 170170 a b^9 x^9 + 680680 a^2 b^8 x^8 + 1633632 a^3 b^7 x^7 + 2598960 a^4 b^6 x^6 + 2858856 a^5 b^5 x^5 + 2199120 a^6 b^4 x^4 + 1166880 a^7 b^3 x^3 + 408408 a^8 b^2 x^2 + 85085 a^9 b x + 8008 a^{10}}{136136 x^{17}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^18,x, algorithm="giac")

[Out] -1/136136*(19448*b^10*x^10 + 170170*a*b^9*x^9 + 680680*a^2*b^8*x^8 + 1633632*a^3*b^7*x^7 + 2598960*a^4*b^6*x^6 + 2858856*a^5*b^5*x^5 + 2199120*a^6*b^4*x^4 + 1166880*a^7*b^3*x^3 + 408408*a^8*b^2*x^2 + 85085*a^9*b*x + 8008*a^10)/x^17

maple [A] time = 0.01, size = 113, normalized size = 0.83

$$\frac{b^{10}}{7x^7} - \frac{5ab^9}{4x^8} - \frac{5a^2b^8}{x^9} - \frac{12a^3b^7}{x^{10}} - \frac{210a^4b^6}{11x^{11}} - \frac{21a^5b^5}{x^{12}} - \frac{210a^6b^4}{13x^{13}} - \frac{60a^7b^3}{7x^{14}} - \frac{3a^8b^2}{x^{15}} - \frac{5a^9b}{8x^{16}} - \frac{a^{10}}{17x^{17}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^18,x)

[Out] -3*a^8*b^2/x^15-12*a^3*b^7/x^10-5*a^2*b^8/x^9-21*a^5*b^5/x^12-1/17*a^10/x^17-5/8*a^9*b/x^16-60/7*a^7*b^3/x^14-210/13*a^6*b^4/x^13-1/7*b^10/x^7-5/4*a*b^9/x^8-210/11*a^4*b^6/x^11

maxima [A] time = 1.40, size = 112, normalized size = 0.82

$$\frac{19448 b^{10} x^{10} + 170170 a b^9 x^9 + 680680 a^2 b^8 x^8 + 1633632 a^3 b^7 x^7 + 2598960 a^4 b^6 x^6 + 2858856 a^5 b^5 x^5 + 2199120 a^6 b^4 x^4 + 1166880 a^7 b^3 x^3 + 408408 a^8 b^2 x^2 + 85085 a^9 b x + 8008 a^{10}}{136136 x^{17}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^18,x, algorithm="maxima")

[Out] -1/136136*(19448*b^10*x^10 + 170170*a*b^9*x^9 + 680680*a^2*b^8*x^8 + 1633632*a^3*b^7*x^7 + 2598960*a^4*b^6*x^6 + 2858856*a^5*b^5*x^5 + 2199120*a^6*b^4*x^4 + 1166880*a^7*b^3*x^3 + 408408*a^8*b^2*x^2 + 85085*a^9*b*x + 8008*a^10)/x^17

mupad [B] time = 0.13, size = 112, normalized size = 0.82

$$\frac{\frac{a^{10}}{17} + \frac{5a^9bx}{8} + 3a^8b^2x^2 + \frac{60a^7b^3x^3}{7} + \frac{210a^6b^4x^4}{13} + 21a^5b^5x^5 + \frac{210a^4b^6x^6}{11} + 12a^3b^7x^7 + 5a^2b^8x^8 + \frac{5ab^9x^9}{4} + \frac{b^{10}}{17}}{x^{17}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^10/x^18,x)`

[Out] $-(a^{10}/17 + (b^{10}x^{10})/7 + (5ab^9x^9)/4 + 3a^8b^2x^2 + (60a^7b^3x^3)/7 + (210a^6b^4x^4)/13 + 21a^5b^5x^5 + (210a^4b^6x^6)/11 + 12a^3b^7x^7 + 5a^2b^8x^8 + (5a^9bx)/8)/x^{17}$

sympy [A] time = 1.33, size = 121, normalized size = 0.89

$$\frac{-8008a^{10} - 85085a^9bx - 408408a^8b^2x^2 - 1166880a^7b^3x^3 - 2199120a^6b^4x^4 - 2858856a^5b^5x^5 - 2598960a^4b^6x^6 - 1633632a^3b^7x^7 - 680680a^2b^8x^8 - 170170ab^9x^9 - 19448b^{10}x^{10}}{136136x^{17}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**10/x**18,x)`

[Out] $(-8008a^{10} - 85085a^9bx - 408408a^8b^2x^2 - 1166880a^7b^3x^3 - 2199120a^6b^4x^4 - 2858856a^5b^5x^5 - 2598960a^4b^6x^6 - 1633632a^3b^7x^7 - 680680a^2b^8x^8 - 170170ab^9x^9 - 19448b^{10}x^{10})/(136136x^{17})$

$$3.153 \quad \int \frac{(a+bx)^{10}}{x^{19}} dx$$

Optimal. Leaf size=130

$$-\frac{a^{10}}{18x^{18}} - \frac{10a^9b}{17x^{17}} - \frac{45a^8b^2}{16x^{16}} - \frac{8a^7b^3}{x^{15}} - \frac{15a^6b^4}{x^{14}} - \frac{252a^5b^5}{13x^{13}} - \frac{35a^4b^6}{2x^{12}} - \frac{120a^3b^7}{11x^{11}} - \frac{9a^2b^8}{2x^{10}} - \frac{10ab^9}{9x^9} - \frac{b^{10}}{8x^8}$$

[Out] $-1/18*a^{10}/x^{18}-10/17*a^9*b/x^{17}-45/16*a^8*b^2/x^{16}-8*a^7*b^3/x^{15}-15*a^6*b^4/x^{14}-252/13*a^5*b^5/x^{13}-35/2*a^4*b^6/x^{12}-120/11*a^3*b^7/x^{11}-9/2*a^2*b^8/x^{10}-10/9*a*b^9/x^9-1/8*b^{10}/x^8$

Rubi [A] time = 0.05, antiderivative size = 130, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{45a^8b^2}{16x^{16}} - \frac{8a^7b^3}{x^{15}} - \frac{15a^6b^4}{x^{14}} - \frac{252a^5b^5}{13x^{13}} - \frac{35a^4b^6}{2x^{12}} - \frac{120a^3b^7}{11x^{11}} - \frac{9a^2b^8}{2x^{10}} - \frac{10a^9b}{17x^{17}} - \frac{a^{10}}{18x^{18}} - \frac{10ab^9}{9x^9} - \frac{b^{10}}{8x^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^19, x]

[Out] $-a^{10}/(18*x^{18}) - (10*a^9*b)/(17*x^{17}) - (45*a^8*b^2)/(16*x^{16}) - (8*a^7*b^3)/x^{15} - (15*a^6*b^4)/x^{14} - (252*a^5*b^5)/(13*x^{13}) - (35*a^4*b^6)/(2*x^{12}) - (120*a^3*b^7)/(11*x^{11}) - (9*a^2*b^8)/(2*x^{10}) - (10*a*b^9)/(9*x^9) - b^{10}/(8*x^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^{19}} dx = \int \left(\frac{a^{10}}{x^{19}} + \frac{10a^9b}{x^{18}} + \frac{45a^8b^2}{x^{17}} + \frac{120a^7b^3}{x^{16}} + \frac{210a^6b^4}{x^{15}} + \frac{252a^5b^5}{x^{14}} + \frac{210a^4b^6}{x^{13}} + \frac{120a^3b^7}{x^{12}} + \frac{45a^2b^8}{x^{11}} + \frac{10ab^9}{x^{10}} + \frac{b^{10}}{x^9} \right) dx$$

$$= -\frac{a^{10}}{18x^{18}} - \frac{10a^9b}{17x^{17}} - \frac{45a^8b^2}{16x^{16}} - \frac{8a^7b^3}{x^{15}} - \frac{15a^6b^4}{x^{14}} - \frac{252a^5b^5}{13x^{13}} - \frac{35a^4b^6}{2x^{12}} - \frac{120a^3b^7}{11x^{11}} - \frac{9a^2b^8}{2x^{10}} - \frac{10ab^9}{9x^9} - \frac{b^{10}}{8x^8}$$

Mathematica [A] time = 0.00, size = 130, normalized size = 1.00

$$-\frac{a^{10}}{18x^{18}} - \frac{10a^9b}{17x^{17}} - \frac{45a^8b^2}{16x^{16}} - \frac{8a^7b^3}{x^{15}} - \frac{15a^6b^4}{x^{14}} - \frac{252a^5b^5}{13x^{13}} - \frac{35a^4b^6}{2x^{12}} - \frac{120a^3b^7}{11x^{11}} - \frac{9a^2b^8}{2x^{10}} - \frac{10ab^9}{9x^9} - \frac{b^{10}}{8x^8}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^19,x]

[Out] $-1/18*a^{10}/x^{18} - (10*a^9*b)/(17*x^{17}) - (45*a^8*b^2)/(16*x^{16}) - (8*a^7*b^3)/x^{15} - (15*a^6*b^4)/x^{14} - (252*a^5*b^5)/(13*x^{13}) - (35*a^4*b^6)/(2*x^{12}) - (120*a^3*b^7)/(11*x^{11}) - (9*a^2*b^8)/(2*x^{10}) - (10*a*b^9)/(9*x^9) - b^{10}/(8*x^8)$

fricas [A] time = 0.42, size = 112, normalized size = 0.86

$$\frac{43758 b^{10} x^{10} + 388960 a b^9 x^9 + 1575288 a^2 b^8 x^8 + 3818880 a^3 b^7 x^7 + 6126120 a^4 b^6 x^6 + 6785856 a^5 b^5 x^5 + 5250960 a^6 b^4 x^4 + 2800512 a^7 b^3 x^3 + 984555 a^8 b^2 x^2 + 205920 a^9 b x + 19448 a^{10}}{350064 x^{18}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^19,x, algorithm="fricas")

[Out] $-1/350064*(43758*b^{10}*x^{10} + 388960*a*b^9*x^9 + 1575288*a^2*b^8*x^8 + 3818880*a^3*b^7*x^7 + 6126120*a^4*b^6*x^6 + 6785856*a^5*b^5*x^5 + 5250960*a^6*b^4*x^4 + 2800512*a^7*b^3*x^3 + 984555*a^8*b^2*x^2 + 205920*a^9*b*x + 19448*a^{10})/x^{18}$

giac [A] time = 0.98, size = 112, normalized size = 0.86

$$\frac{43758 b^{10} x^{10} + 388960 a b^9 x^9 + 1575288 a^2 b^8 x^8 + 3818880 a^3 b^7 x^7 + 6126120 a^4 b^6 x^6 + 6785856 a^5 b^5 x^5 + 5250960 a^6 b^4 x^4 + 2800512 a^7 b^3 x^3 + 984555 a^8 b^2 x^2 + 205920 a^9 b x + 19448 a^{10}}{350064 x^{18}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^19,x, algorithm="giac")

[Out] $-1/350064*(43758*b^{10}*x^{10} + 388960*a*b^9*x^9 + 1575288*a^2*b^8*x^8 + 3818880*a^3*b^7*x^7 + 6126120*a^4*b^6*x^6 + 6785856*a^5*b^5*x^5 + 5250960*a^6*b^4*x^4 + 2800512*a^7*b^3*x^3 + 984555*a^8*b^2*x^2 + 205920*a^9*b*x + 19448*a^{10})/x^{18}$

maple [A] time = 0.01, size = 113, normalized size = 0.87

$$\frac{b^{10}}{8x^8} - \frac{10ab^9}{9x^9} - \frac{9a^2b^8}{2x^{10}} - \frac{120a^3b^7}{11x^{11}} - \frac{35a^4b^6}{2x^{12}} - \frac{252a^5b^5}{13x^{13}} - \frac{15a^6b^4}{x^{14}} - \frac{8a^7b^3}{x^{15}} - \frac{45a^8b^2}{16x^{16}} - \frac{10a^9b}{17x^{17}} - \frac{a^{10}}{18x^{18}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^19,x)

[Out] $-1/18*a^{10}/x^{18}-10/17*a^9*b/x^{17}-45/16*a^8*b^2/x^{16}-8*a^7*b^3/x^{15}-15*a^6*b^4/x^{14}-252/13*a^5*b^5/x^{13}-35/2*a^4*b^6/x^{12}-120/11*a^3*b^7/x^{11}-9/2*a^2*b^8/x^{10}-10/9*a*b^9/x^9-1/8*b^{10}/x^8$

maxima [A] time = 1.36, size = 112, normalized size = 0.86

$$\frac{43758 b^{10} x^{10} + 388960 a b^9 x^9 + 1575288 a^2 b^8 x^8 + 3818880 a^3 b^7 x^7 + 6126120 a^4 b^6 x^6 + 6785856 a^5 b^5 x^5 + 5250960 a^6 b^4 x^4 + 2800512 a^7 b^3 x^3 + 984555 a^8 b^2 x^2 + 205920 a^9 b x + 19448 a^{10}}{350064 x^{18}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^19,x, algorithm="maxima")

[Out] -1/350064*(43758*b^10*x^10 + 388960*a*b^9*x^9 + 1575288*a^2*b^8*x^8 + 3818880*a^3*b^7*x^7 + 6126120*a^4*b^6*x^6 + 6785856*a^5*b^5*x^5 + 5250960*a^6*b^4*x^4 + 2800512*a^7*b^3*x^3 + 984555*a^8*b^2*x^2 + 205920*a^9*b*x + 19448*a^10)/x^18

mupad [B] time = 0.10, size = 112, normalized size = 0.86

$$\frac{\frac{a^{10}}{18} + \frac{10 a^9 b x}{17} + \frac{45 a^8 b^2 x^2}{16} + 8 a^7 b^3 x^3 + 15 a^6 b^4 x^4 + \frac{252 a^5 b^5 x^5}{13} + \frac{35 a^4 b^6 x^6}{2} + \frac{120 a^3 b^7 x^7}{11} + \frac{9 a^2 b^8 x^8}{2} + \frac{10 a b^9 x^9}{9} + \frac{b^{10} x^{10}}{8}}{x^{18}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^19,x)

[Out] -(a^10/18 + (b^10*x^10)/8 + (10*a*b^9*x^9)/9 + (45*a^8*b^2*x^2)/16 + 8*a^7*b^3*x^3 + 15*a^6*b^4*x^4 + (252*a^5*b^5*x^5)/13 + (35*a^4*b^6*x^6)/2 + (120*a^3*b^7*x^7)/11 + (9*a^2*b^8*x^8)/2 + (10*a^9*b*x)/17)/x^18

sympy [A] time = 1.35, size = 121, normalized size = 0.93

$$\frac{-19448 a^{10} - 205920 a^9 b x - 984555 a^8 b^2 x^2 - 2800512 a^7 b^3 x^3 - 5250960 a^6 b^4 x^4 - 6785856 a^5 b^5 x^5 - 6126120 a^4 b^6 x^6 - 3818880 a^3 b^7 x^7 - 1575288 a^2 b^8 x^8 - 388960 a b^9 x^9 - 43758 b^{10} x^{10}}{350064 x^{18}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**19,x)

[Out] (-19448*a**10 - 205920*a**9*b*x - 984555*a**8*b**2*x**2 - 2800512*a**7*b**3*x**3 - 5250960*a**6*b**4*x**4 - 6785856*a**5*b**5*x**5 - 6126120*a**4*b**6*x**6 - 3818880*a**3*b**7*x**7 - 1575288*a**2*b**8*x**8 - 388960*a*b**9*x**9 - 43758*b**10*x**10)/(350064*x**18)

$$3.154 \quad \int \frac{(a+bx)^{10}}{x^{20}} dx$$

Optimal. Leaf size=126

$$\frac{a^{10}}{19x^{19}} - \frac{5a^9b}{9x^{18}} - \frac{45a^8b^2}{17x^{17}} - \frac{15a^7b^3}{2x^{16}} - \frac{14a^6b^4}{x^{15}} - \frac{18a^5b^5}{x^{14}} - \frac{210a^4b^6}{13x^{13}} - \frac{10a^3b^7}{x^{12}} - \frac{45a^2b^8}{11x^{11}} - \frac{ab^9}{x^{10}} - \frac{b^{10}}{9x^9}$$

[Out] $-1/19*a^{10}/x^{19}-5/9*a^9*b/x^{18}-45/17*a^8*b^2/x^{17}-15/2*a^7*b^3/x^{16}-14*a^6*b^4/x^{15}-18*a^5*b^5/x^{14}-210/13*a^4*b^6/x^{13}-10*a^3*b^7/x^{12}-45/11*a^2*b^8/x^{11}-a*b^9/x^{10}-1/9*b^{10}/x^9$

Rubi [A] time = 0.05, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{45a^8b^2}{17x^{17}} - \frac{15a^7b^3}{2x^{16}} - \frac{14a^6b^4}{x^{15}} - \frac{18a^5b^5}{x^{14}} - \frac{210a^4b^6}{13x^{13}} - \frac{10a^3b^7}{x^{12}} - \frac{45a^2b^8}{11x^{11}} - \frac{5a^9b}{9x^{18}} - \frac{a^{10}}{19x^{19}} - \frac{ab^9}{x^{10}} - \frac{b^{10}}{9x^9}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^20, x]

[Out] $-a^{10}/(19*x^{19}) - (5*a^9*b)/(9*x^{18}) - (45*a^8*b^2)/(17*x^{17}) - (15*a^7*b^3)/(2*x^{16}) - (14*a^6*b^4)/x^{15} - (18*a^5*b^5)/x^{14} - (210*a^4*b^6)/(13*x^{13}) - (10*a^3*b^7)/x^{12} - (45*a^2*b^8)/(11*x^{11}) - (a*b^9)/x^{10} - b^{10}/(9*x^9)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^{20}} dx = \int \left(\frac{a^{10}}{x^{20}} + \frac{10a^9b}{x^{19}} + \frac{45a^8b^2}{x^{18}} + \frac{120a^7b^3}{x^{17}} + \frac{210a^6b^4}{x^{16}} + \frac{252a^5b^5}{x^{15}} + \frac{210a^4b^6}{x^{14}} + \frac{120a^3b^7}{x^{13}} + \frac{45a^2b^8}{x^{12}} + \frac{5a^9b}{9x^{18}} - \frac{a^{10}}{19x^{19}} - \frac{45a^8b^2}{17x^{17}} - \frac{15a^7b^3}{2x^{16}} - \frac{14a^6b^4}{x^{15}} - \frac{18a^5b^5}{x^{14}} - \frac{210a^4b^6}{13x^{13}} - \frac{10a^3b^7}{x^{12}} - \frac{45a^2b^8}{11x^{11}} - \frac{ab^9}{x^{10}} - \frac{b^{10}}{9x^9} \right) dx$$

Mathematica [A] time = 0.01, size = 126, normalized size = 1.00

$$\frac{a^{10}}{19x^{19}} - \frac{5a^9b}{9x^{18}} - \frac{45a^8b^2}{17x^{17}} - \frac{15a^7b^3}{2x^{16}} - \frac{14a^6b^4}{x^{15}} - \frac{18a^5b^5}{x^{14}} - \frac{210a^4b^6}{13x^{13}} - \frac{10a^3b^7}{x^{12}} - \frac{45a^2b^8}{11x^{11}} - \frac{ab^9}{x^{10}} - \frac{b^{10}}{9x^9}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^20,x]

[Out] -1/19*a^10/x^19 - (5*a^9*b)/(9*x^18) - (45*a^8*b^2)/(17*x^17) - (15*a^7*b^3)/(2*x^16) - (14*a^6*b^4)/x^15 - (18*a^5*b^5)/x^14 - (210*a^4*b^6)/(13*x^13) - (10*a^3*b^7)/x^12 - (45*a^2*b^8)/(11*x^11) - (a*b^9)/x^10 - b^10/(9*x^9)

fricas [A] time = 0.45, size = 112, normalized size = 0.89

$$\frac{92378 b^{10} x^{10} + 831402 a b^9 x^9 + 3401190 a^2 b^8 x^8 + 8314020 a^3 b^7 x^7 + 13430340 a^4 b^6 x^6 + 14965236 a^5 b^5 x^5 + 11639628 a^6 b^4 x^4 + 6235515 a^7 b^3 x^3 + 2200770 a^8 b^2 x^2 + 461890 a^9 b x + 43758 a^{10}}{831402 x^{19}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^20,x, algorithm="fricas")

[Out] -1/831402*(92378*b^10*x^10 + 831402*a*b^9*x^9 + 3401190*a^2*b^8*x^8 + 8314020*a^3*b^7*x^7 + 13430340*a^4*b^6*x^6 + 14965236*a^5*b^5*x^5 + 11639628*a^6*b^4*x^4 + 6235515*a^7*b^3*x^3 + 2200770*a^8*b^2*x^2 + 461890*a^9*b*x + 43758*a^10)/x^19

giac [A] time = 1.11, size = 112, normalized size = 0.89

$$\frac{92378 b^{10} x^{10} + 831402 a b^9 x^9 + 3401190 a^2 b^8 x^8 + 8314020 a^3 b^7 x^7 + 13430340 a^4 b^6 x^6 + 14965236 a^5 b^5 x^5 + 11639628 a^6 b^4 x^4 + 6235515 a^7 b^3 x^3 + 2200770 a^8 b^2 x^2 + 461890 a^9 b x + 43758 a^{10}}{831402 x^{19}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^20,x, algorithm="giac")

[Out] -1/831402*(92378*b^10*x^10 + 831402*a*b^9*x^9 + 3401190*a^2*b^8*x^8 + 8314020*a^3*b^7*x^7 + 13430340*a^4*b^6*x^6 + 14965236*a^5*b^5*x^5 + 11639628*a^6*b^4*x^4 + 6235515*a^7*b^3*x^3 + 2200770*a^8*b^2*x^2 + 461890*a^9*b*x + 43758*a^10)/x^19

maple [A] time = 0.01, size = 113, normalized size = 0.90

$$\frac{b^{10}}{9x^9} - \frac{a b^9}{x^{10}} - \frac{45 a^2 b^8}{11 x^{11}} - \frac{10 a^3 b^7}{x^{12}} - \frac{210 a^4 b^6}{13 x^{13}} - \frac{18 a^5 b^5}{x^{14}} - \frac{14 a^6 b^4}{x^{15}} - \frac{15 a^7 b^3}{2 x^{16}} - \frac{45 a^8 b^2}{17 x^{17}} - \frac{5 a^9 b}{9 x^{18}} - \frac{a^{10}}{19 x^{19}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^20,x)

[Out] -1/19*a^10/x^19-5/9*a^9*b/x^18-45/17*a^8*b^2/x^17-15/2*a^7*b^3/x^16-14*a^6*b^4/x^15-18*a^5*b^5/x^14-210/13*a^4*b^6/x^13-10*a^3*b^7/x^12-45/11*a^2*b^8/x^11-a*b^9/x^10-1/9*b^10/x^9

maxima [A] time = 1.40, size = 112, normalized size = 0.89

$$\frac{92378 b^{10} x^{10} + 831402 a b^9 x^9 + 3401190 a^2 b^8 x^8 + 8314020 a^3 b^7 x^7 + 13430340 a^4 b^6 x^6 + 14965236 a^5 b^5 x^5 + 11639628 a^6 b^4 x^4 + 6235515 a^7 b^3 x^3 + 2200770 a^8 b^2 x^2 + 461890 a^9 b x + 43758 a^{10}}{831402 x^{19}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^20,x, algorithm="maxima")

[Out] -1/831402*(92378*b^10*x^10 + 831402*a*b^9*x^9 + 3401190*a^2*b^8*x^8 + 8314020*a^3*b^7*x^7 + 13430340*a^4*b^6*x^6 + 14965236*a^5*b^5*x^5 + 11639628*a^6*b^4*x^4 + 6235515*a^7*b^3*x^3 + 2200770*a^8*b^2*x^2 + 461890*a^9*b*x + 43758*a^10)/x^19

mupad [B] time = 0.14, size = 111, normalized size = 0.88

$$\frac{\frac{a^{10}}{19} + \frac{5a^9bx}{9} + \frac{45a^8b^2x^2}{17} + \frac{15a^7b^3x^3}{2} + 14a^6b^4x^4 + 18a^5b^5x^5 + \frac{210a^4b^6x^6}{13} + 10a^3b^7x^7 + \frac{45a^2b^8x^8}{11} + ab^9x^9 + \frac{b^{10}}{19}}{x^{19}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^20,x)

[Out] -(a^10/19 + (b^10*x^10)/9 + a*b^9*x^9 + (45*a^8*b^2*x^2)/17 + (15*a^7*b^3*x^3)/2 + 14*a^6*b^4*x^4 + 18*a^5*b^5*x^5 + (210*a^4*b^6*x^6)/13 + 10*a^3*b^7*x^7 + (45*a^2*b^8*x^8)/11 + (5*a^9*b*x)/9)/x^19

sympy [A] time = 1.42, size = 121, normalized size = 0.96

$$\frac{-43758a^{10} - 461890a^9bx - 2200770a^8b^2x^2 - 6235515a^7b^3x^3 - 11639628a^6b^4x^4 - 14965236a^5b^5x^5 - 13430340a^4b^6x^6 - 8314020a^3b^7x^7 - 3401190a^2b^8x^8 - 461890ab^9x^9 - 43758a^{10}}{831402x^{19}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**20,x)

[Out] (-43758*a**10 - 461890*a**9*b*x - 2200770*a**8*b**2*x**2 - 6235515*a**7*b**3*x**3 - 11639628*a**6*b**4*x**4 - 14965236*a**5*b**5*x**5 - 13430340*a**4*b**6*x**6 - 8314020*a**3*b**7*x**7 - 3401190*a**2*b**8*x**8 - 461890*a*b**9 - 43758*b**10*x**10)/(831402*x**19)

3.155 $\int c(a + bx) dx$

Optimal. Leaf size=15

$$\frac{c(a + bx)^2}{2b}$$

[Out] $1/2*c*(b*x+a)^2/b$

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {9}

$$\frac{c(a + bx)^2}{2b}$$

Antiderivative was successfully verified.

[In] Int[c*(a + b*x), x]

[Out] (c*(a + b*x)^2)/(2*b)

Rule 9

Int[(a_)*((b_) + (c_)*(x_)), x_Symbol] :> Simp[(a*(b + c*x)^2)/(2*c), x] / ; FreeQ[{a, b, c}, x]

Rubi steps

$$\int c(a + bx) dx = \frac{c(a + bx)^2}{2b}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 0.93

$$c\left(ax + \frac{bx^2}{2}\right)$$

Antiderivative was successfully verified.

[In] Integrate[c*(a + b*x), x]

[Out] c*(a*x + (b*x^2)/2)

fricas [A] time = 0.41, size = 12, normalized size = 0.80

$$\frac{1}{2}x^2cb + xca$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(c*(b*x+a),x, algorithm="fricas")

[Out] 1/2*x^2*c*b + x*c*a

giac [A] time = 1.09, size = 13, normalized size = 0.87

$$\frac{1}{2}(bx^2 + 2ax)c$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(c*(b*x+a),x, algorithm="giac")

[Out] 1/2*(b*x^2 + 2*a*x)*c

maple [A] time = 0.00, size = 13, normalized size = 0.87

$$\left(\frac{1}{2}bx^2 + ax\right)c$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(c*(b*x+a),x)

[Out] c*(1/2*b*x^2+a*x)

maxima [A] time = 1.36, size = 13, normalized size = 0.87

$$\frac{1}{2}(bx^2 + 2ax)c$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(c*(b*x+a),x, algorithm="maxima")

[Out] 1/2*(b*x^2 + 2*a*x)*c

mupad [B] time = 0.02, size = 11, normalized size = 0.73

$$\frac{cx(2a + bx)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(c*(a + b*x),x)

[Out] (c*x*(2*a + b*x))/2

sympy [A] time = 0.07, size = 12, normalized size = 0.80

$$acx + \frac{bcx^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(c*(b*x+a),x)

[Out] a*c*x + b*c*x**2/2

$$3.156 \quad \int \frac{(c+d)(a+bx)}{e} dx$$

Optimal. Leaf size=20

$$\frac{(c+d)(a+bx)^2}{2be}$$

[Out] 1/2*(c+d)*(b*x+a)^2/b/e

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.083$, Rules used = {9}

$$\frac{(c+d)(a+bx)^2}{2be}$$

Antiderivative was successfully verified.

[In] Int[((c + d)*(a + b*x))/e,x]

[Out] ((c + d)*(a + b*x)^2)/(2*b*e)

Rule 9

Int[(a_)*((b_) + (c_)*(x_)), x_Symbol] := Simp[(a*(b + c*x)^2)/(2*c), x] / ; FreeQ[{a, b, c}, x]

Rubi steps

$$\int \frac{(c+d)(a+bx)}{e} dx = \frac{(c+d)(a+bx)^2}{2be}$$

Mathematica [A] time = 0.00, size = 19, normalized size = 0.95

$$\frac{(c+d)\left(ax + \frac{bx^2}{2}\right)}{e}$$

Antiderivative was successfully verified.

[In] Integrate[((c + d)*(a + b*x))/e,x]

[Out] ((c + d)*(a*x + (b*x^2)/2))/e

fricas [A] time = 0.45, size = 27, normalized size = 1.35

$$\frac{(bc + bd)x^2 + 2(ac + ad)x}{2e}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d)*(b*x+a)/e,x, algorithm="fricas")

[Out] 1/2*((b*c + b*d)*x^2 + 2*(a*c + a*d)*x)/e

giac [A] time = 1.20, size = 17, normalized size = 0.85

$$\frac{1}{2} (bx^2 + 2ax)(c + d)e^{(-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d)*(b*x+a)/e,x, algorithm="giac")

[Out] 1/2*(b*x^2 + 2*a*x)*(c + d)*e^(-1)

maple [A] time = 0.00, size = 18, normalized size = 0.90

$$\frac{(c + d) \left(\frac{1}{2} b x^2 + a x \right)}{e}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c+d)*(b*x+a)/e,x)

[Out] (c+d)/e*(1/2*b*x^2+a*x)

maxima [A] time = 1.37, size = 18, normalized size = 0.90

$$\frac{(bx^2 + 2ax)(c + d)}{2e}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c+d)*(b*x+a)/e,x, algorithm="maxima")

[Out] 1/2*(b*x^2 + 2*a*x)*(c + d)/e

mupad [B] time = 0.07, size = 16, normalized size = 0.80

$$\frac{x (c + d) (2a + bx)}{2e}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c + d)*(a + b*x))/e,x)

[Out] $(x*(c + d)*(2*a + b*x))/(2*e)$

sympy [A] time = 0.08, size = 22, normalized size = 1.10

$$\frac{x^2 (bc + bd)}{2e} + \frac{x (ac + ad)}{e}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c+d)*(b*x+a)/e,x)`

[Out] $x**2*(b*c + b*d)/(2*e) + x*(a*c + a*d)/e$

$$3.157 \quad \int \frac{x^5}{a+bx} dx$$

Optimal. Leaf size=70

$$-\frac{a^5 \log(a+bx)}{b^6} + \frac{a^4 x}{b^5} - \frac{a^3 x^2}{2b^4} + \frac{a^2 x^3}{3b^3} - \frac{ax^4}{4b^2} + \frac{x^5}{5b}$$

[Out] $a^4 x/b^5 - 1/2 a^3 x^2/b^4 + 1/3 a^2 x^3/b^3 - 1/4 a x^4/b^2 + 1/5 x^5/b - a^5 \ln(bx+a)/b^6$

Rubi [A] time = 0.03, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^3 x^2}{2b^4} + \frac{a^2 x^3}{3b^3} + \frac{a^4 x}{b^5} - \frac{a^5 \log(a+bx)}{b^6} - \frac{ax^4}{4b^2} + \frac{x^5}{5b}$$

Antiderivative was successfully verified.

[In] Int[x^5/(a + b*x), x]

[Out] $(a^4 x)/b^5 - (a^3 x^2)/(2b^4) + (a^2 x^3)/(3b^3) - (a x^4)/(4b^2) + x^5/(5b) - (a^5 \text{Log}[a + b*x])/b^6$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^5}{a+bx} dx &= \int \left(\frac{a^4}{b^5} - \frac{a^3 x}{b^4} + \frac{a^2 x^2}{b^3} - \frac{ax^3}{b^2} + \frac{x^4}{b} - \frac{a^5}{b^5(a+bx)} \right) dx \\ &= \frac{a^4 x}{b^5} - \frac{a^3 x^2}{2b^4} + \frac{a^2 x^3}{3b^3} - \frac{ax^4}{4b^2} + \frac{x^5}{5b} - \frac{a^5 \log(a+bx)}{b^6} \end{aligned}$$

Mathematica [A] time = 0.00, size = 70, normalized size = 1.00

$$-\frac{a^5 \log(a+bx)}{b^6} + \frac{a^4 x}{b^5} - \frac{a^3 x^2}{2b^4} + \frac{a^2 x^3}{3b^3} - \frac{ax^4}{4b^2} + \frac{x^5}{5b}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/(a + b*x),x]

[Out] $(a^4*x)/b^5 - (a^3*x^2)/(2*b^4) + (a^2*x^3)/(3*b^3) - (a*x^4)/(4*b^2) + x^5/(5*b) - (a^5*\text{Log}[a + b*x])/b^6$

fricas [A] time = 0.44, size = 63, normalized size = 0.90

$$\frac{12 b^5 x^5 - 15 a b^4 x^4 + 20 a^2 b^3 x^3 - 30 a^3 b^2 x^2 + 60 a^4 b x - 60 a^5 \log(bx + a)}{60 b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a),x, algorithm="fricas")

[Out] $1/60*(12*b^5*x^5 - 15*a*b^4*x^4 + 20*a^2*b^3*x^3 - 30*a^3*b^2*x^2 + 60*a^4*b*x - 60*a^5*\log(b*x + a))/b^6$

giac [A] time = 1.00, size = 65, normalized size = 0.93

$$-\frac{a^5 \log(|bx + a|)}{b^6} + \frac{12 b^4 x^5 - 15 a b^3 x^4 + 20 a^2 b^2 x^3 - 30 a^3 b x^2 + 60 a^4 x}{60 b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a),x, algorithm="giac")

[Out] $-a^5*\log(\text{abs}(b*x + a))/b^6 + 1/60*(12*b^4*x^5 - 15*a*b^3*x^4 + 20*a^2*b^2*x^3 - 30*a^3*b*x^2 + 60*a^4*x)/b^5$

maple [A] time = 0.00, size = 63, normalized size = 0.90

$$\frac{x^5}{5b} - \frac{ax^4}{4b^2} + \frac{a^2x^3}{3b^3} - \frac{a^3x^2}{2b^4} - \frac{a^5 \ln(bx + a)}{b^6} + \frac{a^4x}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(b*x+a),x)

[Out] $a^4*x/b^5 - 1/2*a^3*x^2/b^4 + 1/3*a^2*x^3/b^3 - 1/4*a*x^4/b^2 + 1/5*x^5/b - a^5*\ln(b*x+a)/b^6$

maxima [A] time = 1.39, size = 64, normalized size = 0.91

$$-\frac{a^5 \log(bx + a)}{b^6} + \frac{12 b^4 x^5 - 15 a b^3 x^4 + 20 a^2 b^2 x^3 - 30 a^3 b x^2 + 60 a^4 x}{60 b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a),x, algorithm="maxima")

[Out] $-a^5 \log(bx + a)/b^6 + 1/60*(12*b^4*x^5 - 15*a*b^3*x^4 + 20*a^2*b^2*x^3 - 30*a^3*b*x^2 + 60*a^4*x)/b^5$

mupad [B] time = 0.08, size = 62, normalized size = 0.89

$$\frac{x^5}{5b} - \frac{a^5 \ln(ax + b)}{b^6} - \frac{ax^4}{4b^2} + \frac{a^4x}{b^5} + \frac{a^2x^3}{3b^3} - \frac{a^3x^2}{2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(a + b*x),x)

[Out] $x^5/(5*b) - (a^5*\log(a + b*x))/b^6 - (a*x^4)/(4*b^2) + (a^4*x)/b^5 + (a^2*x^3)/(3*b^3) - (a^3*x^2)/(2*b^4)$

sympy [A] time = 0.16, size = 61, normalized size = 0.87

$$-\frac{a^5 \log(ax + b)}{b^6} + \frac{a^4x}{b^5} - \frac{a^3x^2}{2b^4} + \frac{a^2x^3}{3b^3} - \frac{ax^4}{4b^2} + \frac{x^5}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5/(b*x+a),x)

[Out] $-a**5*\log(a + b*x)/b**6 + a**4*x/b**5 - a**3*x**2/(2*b**4) + a**2*x**3/(3*b**3) - a*x**4/(4*b**2) + x**5/(5*b)$

$$3.158 \quad \int \frac{x^4}{a+bx} dx$$

Optimal. Leaf size=57

$$\frac{a^4 \log(a+bx)}{b^5} - \frac{a^3x}{b^4} + \frac{a^2x^2}{2b^3} - \frac{ax^3}{3b^2} + \frac{x^4}{4b}$$

[Out] $-a^3x/b^4 + 1/2*a^2*x^2/b^3 - 1/3*a*x^3/b^2 + 1/4*x^4/b + a^4*\ln(b*x+a)/b^5$

Rubi [A] time = 0.02, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2x^2}{2b^3} - \frac{a^3x}{b^4} + \frac{a^4 \log(a+bx)}{b^5} - \frac{ax^3}{3b^2} + \frac{x^4}{4b}$$

Antiderivative was successfully verified.

[In] Int[x^4/(a + b*x), x]

[Out] $-((a^3*x)/b^4) + (a^2*x^2)/(2*b^3) - (a*x^3)/(3*b^2) + x^4/(4*b) + (a^4*Log[a + b*x])/b^5$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{a+bx} dx &= \int \left(-\frac{a^3}{b^4} + \frac{a^2x}{b^3} - \frac{ax^2}{b^2} + \frac{x^3}{b} + \frac{a^4}{b^4(a+bx)} \right) dx \\ &= -\frac{a^3x}{b^4} + \frac{a^2x^2}{2b^3} - \frac{ax^3}{3b^2} + \frac{x^4}{4b} + \frac{a^4 \log(a+bx)}{b^5} \end{aligned}$$

Mathematica [A] time = 0.00, size = 57, normalized size = 1.00

$$\frac{a^4 \log(a+bx)}{b^5} - \frac{a^3x}{b^4} + \frac{a^2x^2}{2b^3} - \frac{ax^3}{3b^2} + \frac{x^4}{4b}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/(a + b*x), x]

[Out] $-\frac{(a^3x)/b^4 + (a^2x^2)/(2b^3) - (ax^3)/(3b^2) + x^4/(4b) + (a^4 \text{Log}[a + bx])/b^5}$

fricas [A] time = 0.43, size = 52, normalized size = 0.91

$$\frac{3b^4x^4 - 4ab^3x^3 + 6a^2b^2x^2 - 12a^3bx + 12a^4 \log(bx + a)}{12b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a), x, algorithm="fricas")

[Out] $1/12*(3b^4x^4 - 4a*b^3x^3 + 6a^2*b^2x^2 - 12a^3*bx + 12a^4*\log(b*x + a))/b^5$

giac [A] time = 1.35, size = 53, normalized size = 0.93

$$\frac{a^4 \log(|bx + a|)}{b^5} + \frac{3b^3x^4 - 4ab^2x^3 + 6a^2bx^2 - 12a^3x}{12b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a), x, algorithm="giac")

[Out] $a^4*\log(\text{abs}(b*x + a))/b^5 + 1/12*(3*b^3*x^4 - 4*a*b^2*x^3 + 6*a^2*b*x^2 - 12*a^3*x)/b^4$

maple [A] time = 0.00, size = 52, normalized size = 0.91

$$\frac{x^4}{4b} - \frac{ax^3}{3b^2} + \frac{a^2x^2}{2b^3} + \frac{a^4 \ln(bx + a)}{b^5} - \frac{a^3x}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(b*x+a), x)

[Out] $-a^3x/b^4 + 1/2*a^2*x^2/b^3 - 1/3*a*x^3/b^2 + 1/4*x^4/b + a^4*\ln(b*x+a)/b^5$

maxima [A] time = 1.33, size = 52, normalized size = 0.91

$$\frac{a^4 \log(bx + a)}{b^5} + \frac{3b^3x^4 - 4ab^2x^3 + 6a^2bx^2 - 12a^3x}{12b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a), x, algorithm="maxima")

[Out] $a^4 \log(bx + a)/b^5 + 1/12*(3*b^3*x^4 - 4*a*b^2*x^3 + 6*a^2*b*x^2 - 12*a^3*x)/b^4$

mupad [B] time = 0.10, size = 51, normalized size = 0.89

$$\frac{x^4}{4b} + \frac{a^4 \ln(a + bx)}{b^5} - \frac{ax^3}{3b^2} - \frac{a^3x}{b^4} + \frac{a^2x^2}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^4/(a + b*x), x)`

[Out] $x^4/(4*b) + (a^4*\log(a + b*x))/b^5 - (a*x^3)/(3*b^2) - (a^3*x)/b^4 + (a^2*x^2)/(2*b^3)$

sympy [A] time = 0.15, size = 49, normalized size = 0.86

$$\frac{a^4 \log(a + bx)}{b^5} - \frac{a^3x}{b^4} + \frac{a^2x^2}{2b^3} - \frac{ax^3}{3b^2} + \frac{x^4}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**4/(b*x+a), x)`

[Out] $a**4*\log(a + b*x)/b**5 - a**3*x/b**4 + a**2*x**2/(2*b**3) - a*x**3/(3*b**2) + x**4/(4*b)$

$$3.159 \quad \int \frac{x^3}{a+bx} dx$$

Optimal. Leaf size=44

$$-\frac{a^3 \log(a+bx)}{b^4} + \frac{a^2x}{b^3} - \frac{ax^2}{2b^2} + \frac{x^3}{3b}$$

[Out] $a^2x/b^3 - 1/2*a*x^2/b^2 + 1/3*x^3/b - a^3*\ln(b*x+a)/b^4$

Rubi [A] time = 0.02, antiderivative size = 44, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2x}{b^3} - \frac{a^3 \log(a+bx)}{b^4} - \frac{ax^2}{2b^2} + \frac{x^3}{3b}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x), x]

[Out] $(a^2*x)/b^3 - (a*x^2)/(2*b^2) + x^3/(3*b) - (a^3*\text{Log}[a + b*x])/b^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{a+bx} dx &= \int \left(\frac{a^2}{b^3} - \frac{ax}{b^2} + \frac{x^2}{b} - \frac{a^3}{b^3(a+bx)} \right) dx \\ &= \frac{a^2x}{b^3} - \frac{ax^2}{2b^2} + \frac{x^3}{3b} - \frac{a^3 \log(a+bx)}{b^4} \end{aligned}$$

Mathematica [A] time = 0.00, size = 44, normalized size = 1.00

$$-\frac{a^3 \log(a+bx)}{b^4} + \frac{a^2x}{b^3} - \frac{ax^2}{2b^2} + \frac{x^3}{3b}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x), x]

[Out] $(a^2x)/b^3 - (ax^2)/(2b^2) + x^3/(3b) - (a^3\text{Log}[a + bx])/b^4$

fricas [A] time = 0.45, size = 41, normalized size = 0.93

$$\frac{2b^3x^3 - 3ab^2x^2 + 6a^2bx - 6a^3\log(bx + a)}{6b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3/(b*x+a),x, algorithm="fricas")`

[Out] $1/6*(2*b^3*x^3 - 3*a*b^2*x^2 + 6*a^2*b*x - 6*a^3*\log(b*x + a))/b^4$

giac [A] time = 1.05, size = 43, normalized size = 0.98

$$-\frac{a^3\log(|bx + a|)}{b^4} + \frac{2b^2x^3 - 3abx^2 + 6a^2x}{6b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3/(b*x+a),x, algorithm="giac")`

[Out] $-a^3*\log(\text{abs}(b*x + a))/b^4 + 1/6*(2*b^2*x^3 - 3*a*b*x^2 + 6*a^2*x)/b^3$

maple [A] time = 0.00, size = 41, normalized size = 0.93

$$\frac{x^3}{3b} - \frac{ax^2}{2b^2} - \frac{a^3\ln(bx + a)}{b^4} + \frac{a^2x}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3/(b*x+a),x)`

[Out] $a^2*x/b^3 - 1/2*a*x^2/b^2 + 1/3*x^3/b - a^3*\ln(b*x+a)/b^4$

maxima [A] time = 1.24, size = 42, normalized size = 0.95

$$-\frac{a^3\log(bx + a)}{b^4} + \frac{2b^2x^3 - 3abx^2 + 6a^2x}{6b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3/(b*x+a),x, algorithm="maxima")`

[Out] $-a^3*\log(b*x + a)/b^4 + 1/6*(2*b^2*x^3 - 3*a*b*x^2 + 6*a^2*x)/b^3$

mupad [B] time = 0.04, size = 40, normalized size = 0.91

$$\frac{x^3}{3b} - \frac{a^3\ln(a + bx)}{b^4} - \frac{ax^2}{2b^2} + \frac{a^2x}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3/(a + b*x),x)`

[Out] $x^3/(3*b) - (a^3*\log(a + b*x))/b^4 - (a*x^2)/(2*b^2) + (a^2*x)/b^3$

sympy [A] time = 0.14, size = 37, normalized size = 0.84

$$-\frac{a^3 \log(a + bx)}{b^4} + \frac{a^2 x}{b^3} - \frac{ax^2}{2b^2} + \frac{x^3}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3/(b*x+a),x)`

[Out] $-a**3*\log(a + b*x)/b**4 + a**2*x/b**3 - a*x**2/(2*b**2) + x**3/(3*b)$

$$3.160 \quad \int \frac{x^2}{a+bx} dx$$

Optimal. Leaf size=31

$$\frac{a^2 \log(a+bx)}{b^3} - \frac{ax}{b^2} + \frac{x^2}{2b}$$

[Out] $-a*x/b^2 + 1/2*x^2/b + a^2*\ln(b*x+a)/b^3$

Rubi [A] time = 0.01, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2 \log(a+bx)}{b^3} - \frac{ax}{b^2} + \frac{x^2}{2b}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*x), x]

[Out] $-((a*x)/b^2) + x^2/(2*b) + (a^2*\text{Log}[a + b*x])/b^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{a+bx} dx &= \int \left(-\frac{a}{b^2} + \frac{x}{b} + \frac{a^2}{b^2(a+bx)} \right) dx \\ &= -\frac{ax}{b^2} + \frac{x^2}{2b} + \frac{a^2 \log(a+bx)}{b^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 31, normalized size = 1.00

$$\frac{a^2 \log(a+bx)}{b^3} - \frac{ax}{b^2} + \frac{x^2}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x), x]

[Out] $-\left(\frac{a \cdot x}{b^2}\right) + \frac{x^2}{2 \cdot b} + \frac{a^2 \cdot \text{Log}[a + b \cdot x]}{b^3}$

fricas [A] time = 0.44, size = 29, normalized size = 0.94

$$\frac{b^2 x^2 - 2 a b x + 2 a^2 \log (b x + a)}{2 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2/(b*x+a),x, algorithm="fricas")`

[Out] $\frac{1}{2} \cdot (b^2 \cdot x^2 - 2 \cdot a \cdot b \cdot x + 2 \cdot a^2 \cdot \log (b \cdot x + a)) / b^3$

giac [A] time = 0.94, size = 30, normalized size = 0.97

$$\frac{a^2 \log (|b x + a|)}{b^3} + \frac{b x^2 - 2 a x}{2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2/(b*x+a),x, algorithm="giac")`

[Out] $a^2 \cdot \log (\text{abs}(b \cdot x + a)) / b^3 + \frac{1}{2} \cdot (b \cdot x^2 - 2 \cdot a \cdot x) / b^2$

maple [A] time = 0.00, size = 30, normalized size = 0.97

$$\frac{x^2}{2b} + \frac{a^2 \ln (b x + a)}{b^3} - \frac{a x}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/(b*x+a),x)`

[Out] $-a \cdot x / b^2 + \frac{1}{2} \cdot x^2 / b + a^2 \cdot \ln (b \cdot x + a) / b^3$

maxima [A] time = 1.37, size = 29, normalized size = 0.94

$$\frac{a^2 \log (b x + a)}{b^3} + \frac{b x^2 - 2 a x}{2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2/(b*x+a),x, algorithm="maxima")`

[Out] $a^2 \cdot \log (b \cdot x + a) / b^3 + \frac{1}{2} \cdot (b \cdot x^2 - 2 \cdot a \cdot x) / b^2$

mupad [B] time = 0.04, size = 29, normalized size = 0.94

$$\frac{2 a^2 \ln (a + b x) + b^2 x^2 - 2 a b x}{2 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2/(a + b*x),x)
```

```
[Out] (2*a^2*log(a + b*x) + b^2*x^2 - 2*a*b*x)/(2*b^3)
```

```
sympy [A] time = 0.13, size = 26, normalized size = 0.84
```

$$\frac{a^2 \log(a + bx)}{b^3} - \frac{ax}{b^2} + \frac{x^2}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2/(b*x+a),x)
```

```
[Out] a**2*log(a + b*x)/b**3 - a*x/b**2 + x**2/(2*b)
```

$$3.161 \quad \int \frac{x}{a+bx} dx$$

Optimal. Leaf size=18

$$\frac{x}{b} - \frac{a \log(a + bx)}{b^2}$$

[Out] x/b-a*ln(b*x+a)/b^2

Rubi [A] time = 0.01, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{x}{b} - \frac{a \log(a + bx)}{b^2}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x), x]

[Out] x/b - (a*Log[a + b*x])/b^2

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x}{a+bx} dx &= \int \left(\frac{1}{b} - \frac{a}{b(a+bx)} \right) dx \\ &= \frac{x}{b} - \frac{a \log(a+bx)}{b^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 18, normalized size = 1.00

$$\frac{x}{b} - \frac{a \log(a + bx)}{b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x), x]

[Out] x/b - (a*Log[a + b*x])/b^2

fricas [A] time = 0.44, size = 17, normalized size = 0.94

$$\frac{bx - a \log (bx + a)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a),x, algorithm="fricas")

[Out] (b*x - a*log(b*x + a))/b^2

giac [A] time = 1.02, size = 19, normalized size = 1.06

$$\frac{x}{b} - \frac{a \log (|bx + a|)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a),x, algorithm="giac")

[Out] x/b - a*log(abs(b*x + a))/b^2

maple [A] time = 0.00, size = 19, normalized size = 1.06

$$-\frac{a \ln (bx + a)}{b^2} + \frac{x}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(b*x+a),x)

[Out] x/b-a*ln(b*x+a)/b^2

maxima [A] time = 1.31, size = 18, normalized size = 1.00

$$\frac{x}{b} - \frac{a \log (bx + a)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a),x, algorithm="maxima")

[Out] x/b - a*log(b*x + a)/b^2

mupad [B] time = 0.08, size = 18, normalized size = 1.00

$$\frac{a \ln (a + bx) - bx}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x/(a + b*x),x)
```

```
[Out] -(a*log(a + b*x) - b*x)/b^2
```

sympy [A] time = 0.12, size = 14, normalized size = 0.78

$$-\frac{a \log(a + bx)}{b^2} + \frac{x}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x/(b*x+a),x)
```

```
[Out] -a*log(a + b*x)/b**2 + x/b
```

$$3.162 \quad \int \frac{1}{a+bx} dx$$

Optimal. Leaf size=10

$$\frac{\log(a+bx)}{b}$$

[Out] ln(b*x+a)/b

Rubi [A] time = 0.00, antiderivative size = 10, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {31}

$$\frac{\log(a+bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-1), x]

[Out] Log[a + b*x]/b

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \frac{1}{a+bx} dx = \frac{\log(a+bx)}{b}$$

Mathematica [A] time = 0.00, size = 10, normalized size = 1.00

$$\frac{\log(a+bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-1), x]

[Out] Log[a + b*x]/b

fricas [A] time = 0.45, size = 10, normalized size = 1.00

$$\frac{\log(bx+a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a),x, algorithm="fricas")

[Out] log(b*x + a)/b

giac [A] time = 0.92, size = 11, normalized size = 1.10

$$\frac{\log(|bx + a|)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a),x, algorithm="giac")

[Out] log(abs(b*x + a))/b

maple [A] time = 0.00, size = 11, normalized size = 1.10

$$\frac{\ln(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a),x)

[Out] ln(b*x+a)/b

maxima [A] time = 1.30, size = 10, normalized size = 1.00

$$\frac{\log(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a),x, algorithm="maxima")

[Out] log(b*x + a)/b

mupad [B] time = 0.02, size = 10, normalized size = 1.00

$$\frac{\ln(a + bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x),x)

[Out] log(a + b*x)/b

sympy [A] time = 0.07, size = 7, normalized size = 0.70

$$\frac{\log(a + bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a),x)

[Out] log(a + b*x)/b

$$3.163 \quad \int \frac{1}{x(a+bx)} dx$$

Optimal. Leaf size=18

$$\frac{\log(x)}{a} - \frac{\log(a+bx)}{a}$$

[Out] ln(x)/a-ln(b*x+a)/a

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.273$, Rules used = {36, 29, 31}

$$\frac{\log(x)}{a} - \frac{\log(a+bx)}{a}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a + b*x)),x]

[Out] Log[x]/a - Log[a + b*x]/a

Rule 29

Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]

Rule 31

Int[((a_) + (b_.)*(x_))^(n-1), x_Symbol] :> Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 36

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))), x_Symbol] :> Dist[b/(b*c - a*d), Int[1/(a + b*x), x], x] - Dist[d/(b*c - a*d), Int[1/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x(a+bx)} dx &= \frac{\int \frac{1}{x} dx}{a} - \frac{b \int \frac{1}{a+bx} dx}{a} \\ &= \frac{\log(x)}{a} - \frac{\log(a+bx)}{a} \end{aligned}$$

Mathematica [A] time = 0.00, size = 18, normalized size = 1.00

$$\frac{\log(x)}{a} - \frac{\log(a + bx)}{a}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)),x]

[Out] Log[x]/a - Log[a + b*x]/a

fricas [A] time = 0.47, size = 16, normalized size = 0.89

$$\frac{\log(bx + a) - \log(x)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a),x, algorithm="fricas")

[Out] -(log(b*x + a) - log(x))/a

giac [A] time = 1.10, size = 20, normalized size = 1.11

$$-\frac{\log(|bx + a|)}{a} + \frac{\log(|x|)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a),x, algorithm="giac")

[Out] -log(abs(b*x + a))/a + log(abs(x))/a

maple [A] time = 0.00, size = 19, normalized size = 1.06

$$\frac{\ln(x)}{a} - \frac{\ln(bx + a)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a),x)

[Out] ln(x)/a-ln(b*x+a)/a

maxima [A] time = 1.39, size = 18, normalized size = 1.00

$$-\frac{\log(bx + a)}{a} + \frac{\log(x)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a),x, algorithm="maxima")

[Out] $-\log(b*x + a)/a + \log(x)/a$

mupad [B] time = 0.09, size = 15, normalized size = 0.83

$$-\frac{2 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(a + b*x)),x)

[Out] $-(2*\operatorname{atanh}((2*b*x)/a + 1))/a$

sympy [A] time = 0.15, size = 10, normalized size = 0.56

$$\frac{\log(x) - \log\left(\frac{a}{b} + x\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a),x)

[Out] $(\log(x) - \log(a/b + x))/a$

$$3.164 \quad \int \frac{1}{x^2(a+bx)} dx$$

Optimal. Leaf size=28

$$-\frac{b \log(x)}{a^2} + \frac{b \log(a+bx)}{a^2} - \frac{1}{ax}$$

[Out] $-1/a/x - b*\ln(x)/a^2 + b*\ln(b*x+a)/a^2$

Rubi [A] time = 0.01, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{b \log(x)}{a^2} + \frac{b \log(a+bx)}{a^2} - \frac{1}{ax}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(a + b*x)),x]

[Out] $-(1/(a*x)) - (b*\text{Log}[x])/a^2 + (b*\text{Log}[a + b*x])/a^2$

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(a+bx)} dx &= \int \left(\frac{1}{ax^2} - \frac{b}{a^2x} + \frac{b^2}{a^2(a+bx)} \right) dx \\ &= -\frac{1}{ax} - \frac{b \log(x)}{a^2} + \frac{b \log(a+bx)}{a^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 28, normalized size = 1.00

$$-\frac{b \log(x)}{a^2} + \frac{b \log(a+bx)}{a^2} - \frac{1}{ax}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)),x]

[Out] $-(1/(a*x)) - (b*\text{Log}[x])/a^2 + (b*\text{Log}[a + b*x])/a^2$

fricas [A] time = 0.49, size = 26, normalized size = 0.93

$$\frac{bx \log (bx + a) - bx \log (x) - a}{a^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(b*x+a),x, algorithm="fricas")`

[Out] $(b*x*\log(b*x + a) - b*x*\log(x) - a)/(a^2*x)$

giac [A] time = 0.97, size = 30, normalized size = 1.07

$$\frac{b \log (|bx + a|)}{a^2} - \frac{b \log (|x|)}{a^2} - \frac{1}{ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(b*x+a),x, algorithm="giac")`

[Out] $b*\log(\text{abs}(b*x + a))/a^2 - b*\log(\text{abs}(x))/a^2 - 1/(a*x)$

maple [A] time = 0.01, size = 29, normalized size = 1.04

$$-\frac{b \ln (x)}{a^2} + \frac{b \ln (bx + a)}{a^2} - \frac{1}{ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^2/(b*x+a),x)`

[Out] $-1/a/x - b*\ln(x)/a^2 + b*\ln(b*x+a)/a^2$

maxima [A] time = 1.30, size = 28, normalized size = 1.00

$$\frac{b \log (bx + a)}{a^2} - \frac{b \log (x)}{a^2} - \frac{1}{ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(b*x+a),x, algorithm="maxima")`

[Out] $b*\log(b*x + a)/a^2 - b*\log(x)/a^2 - 1/(a*x)$

mupad [B] time = 0.05, size = 25, normalized size = 0.89

$$\frac{2 b \operatorname{atanh}\left(\frac{2 b x}{a} + 1\right)}{a^2} - \frac{1}{a x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^2*(a + b*x)),x)`

[Out] $(2*b*atanh((2*b*x)/a + 1))/a^2 - 1/(a*x)$

sympy [A] time = 0.20, size = 19, normalized size = 0.68

$$-\frac{1}{ax} + \frac{b\left(-\log(x) + \log\left(\frac{a}{b} + x\right)\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(b*x+a),x)`

[Out] $-1/(a*x) + b*(-\log(x) + \log(a/b + x))/a**2$

$$3.165 \quad \int \frac{1}{x^3(a+bx)} dx$$

Optimal. Leaf size=42

$$\frac{b^2 \log(x)}{a^3} - \frac{b^2 \log(a+bx)}{a^3} + \frac{b}{a^2 x} - \frac{1}{2ax^2}$$

[Out] $-1/2/a/x^2+b/a^2/x+b^2*\ln(x)/a^3-b^2*\ln(b*x+a)/a^3$

Rubi [A] time = 0.02, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{b^2 \log(x)}{a^3} - \frac{b^2 \log(a+bx)}{a^3} + \frac{b}{a^2 x} - \frac{1}{2ax^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/(x^3*(a + b*x)), x]$

[Out] $-1/(2*a*x^2) + b/(a^2*x) + (b^2*\text{Log}[x])/a^3 - (b^2*\text{Log}[a + b*x])/a^3$

Rule 44

$\text{Int}[(a_.) + (b_.)*(x_.)^{(m_.)}*((c_.) + (d_.)*(x_.)^{(n_.)}), x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^3(a+bx)} dx &= \int \left(\frac{1}{ax^3} - \frac{b}{a^2x^2} + \frac{b^2}{a^3x} - \frac{b^3}{a^3(a+bx)} \right) dx \\ &= -\frac{1}{2ax^2} + \frac{b}{a^2x} + \frac{b^2 \log(x)}{a^3} - \frac{b^2 \log(a+bx)}{a^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 42, normalized size = 1.00

$$\frac{b^2 \log(x)}{a^3} - \frac{b^2 \log(a+bx)}{a^3} + \frac{b}{a^2 x} - \frac{1}{2ax^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)),x]

[Out] $-1/2*1/(a*x^2) + b/(a^2*x) + (b^2*\text{Log}[x])/a^3 - (b^2*\text{Log}[a + b*x])/a^3$

fricas [A] time = 0.45, size = 41, normalized size = 0.98

$$\frac{2 b^2 x^2 \log (b x + a) - 2 b^2 x^2 \log (x) - 2 a b x + a^2}{2 a^3 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a),x, algorithm="fricas")

[Out] $-1/2*(2*b^2*x^2*\log(b*x + a) - 2*b^2*x^2*\log(x) - 2*a*b*x + a^2)/(a^3*x^2)$

giac [A] time = 1.02, size = 45, normalized size = 1.07

$$-\frac{b^2 \log (|b x + a|)}{a^3} + \frac{b^2 \log (|x|)}{a^3} + \frac{2 a b x - a^2}{2 a^3 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a),x, algorithm="giac")

[Out] $-b^2*\log(\text{abs}(b*x + a))/a^3 + b^2*\log(\text{abs}(x))/a^3 + 1/2*(2*a*b*x - a^2)/(a^3*x^2)$

maple [A] time = 0.01, size = 41, normalized size = 0.98

$$\frac{b^2 \ln (x)}{a^3} - \frac{b^2 \ln (b x + a)}{a^3} + \frac{b}{a^2 x} - \frac{1}{2 a x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a),x)

[Out] $-1/2/a/x^2+b/a^2/x+b^2*\ln(x)/a^3-b^2*\ln(b*x+a)/a^3$

maxima [A] time = 1.34, size = 40, normalized size = 0.95

$$-\frac{b^2 \log (b x + a)}{a^3} + \frac{b^2 \log (x)}{a^3} + \frac{2 b x - a}{2 a^2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a),x, algorithm="maxima")

[Out] $-b^2*\log(b*x + a)/a^3 + b^2*\log(x)/a^3 + 1/2*(2*b*x - a)/(a^2*x^2)$

mupad [B] time = 0.06, size = 38, normalized size = 0.90

$$-\frac{\frac{a^2}{2} - abx}{a^3 x^2} - \frac{2b^2 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^3*(a + b*x)),x)`

[Out] `-(a^2/2 - a*b*x)/(a^3*x^2) - (2*b^2*atanh((2*b*x)/a + 1))/a^3`

sympy [A] time = 0.22, size = 31, normalized size = 0.74

$$\frac{-a + 2bx}{2a^2x^2} + \frac{b^2 \left(\log(x) - \log\left(\frac{a}{b} + x\right) \right)}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**3/(b*x+a),x)`

[Out] `(-a + 2*b*x)/(2*a**2*x**2) + b**2*(log(x) - log(a/b + x))/a**3`

$$3.166 \quad \int \frac{1}{x^4(a+bx)} dx$$

Optimal. Leaf size=56

$$-\frac{b^3 \log(x)}{a^4} + \frac{b^3 \log(a+bx)}{a^4} - \frac{b^2}{a^3 x} + \frac{b}{2a^2 x^2} - \frac{1}{3ax^3}$$

[Out] $-1/3/x^3/a+1/2*b/a^2/x^2-b^2/a^3/x-b^3*\ln(x)/a^4+b^3*\ln(b*x+a)/a^4$

Rubi [A] time = 0.02, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{b^2}{a^3 x} - \frac{b^3 \log(x)}{a^4} + \frac{b^3 \log(a+bx)}{a^4} + \frac{b}{2a^2 x^2} - \frac{1}{3ax^3}$$

Antiderivative was successfully verified.

[In] Int[1/(x^4*(a + b*x)), x]

[Out] $-1/(3*a*x^3) + b/(2*a^2*x^2) - b^2/(a^3*x) - (b^3*\text{Log}[x])/a^4 + (b^3*\text{Log}[a + b*x])/a^4$

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^4(a+bx)} dx &= \int \left(\frac{1}{ax^4} - \frac{b}{a^2 x^3} + \frac{b^2}{a^3 x^2} - \frac{b^3}{a^4 x} + \frac{b^4}{a^4(a+bx)} \right) dx \\ &= -\frac{1}{3ax^3} + \frac{b}{2a^2 x^2} - \frac{b^2}{a^3 x} - \frac{b^3 \log(x)}{a^4} + \frac{b^3 \log(a+bx)}{a^4} \end{aligned}$$

Mathematica [A] time = 0.01, size = 56, normalized size = 1.00

$$-\frac{b^3 \log(x)}{a^4} + \frac{b^3 \log(a+bx)}{a^4} - \frac{b^2}{a^3 x} + \frac{b}{2a^2 x^2} - \frac{1}{3ax^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^4*(a + b*x)),x]

[Out] $-1/3*1/(a*x^3) + b/(2*a^2*x^2) - b^2/(a^3*x) - (b^3*\text{Log}[x])/a^4 + (b^3*\text{Log}[a + b*x])/a^4$

fricas [A] time = 0.50, size = 54, normalized size = 0.96

$$\frac{6b^3x^3 \log(bx + a) - 6b^3x^3 \log(x) - 6ab^2x^2 + 3a^2bx - 2a^3}{6a^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a),x, algorithm="fricas")

[Out] $1/6*(6*b^3*x^3*\log(b*x + a) - 6*b^3*x^3*\log(x) - 6*a*b^2*x^2 + 3*a^2*b*x - 2*a^3)/(a^4*x^3)$

giac [A] time = 1.07, size = 56, normalized size = 1.00

$$\frac{b^3 \log(|bx + a|)}{a^4} - \frac{b^3 \log(|x|)}{a^4} - \frac{6ab^2x^2 - 3a^2bx + 2a^3}{6a^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a),x, algorithm="giac")

[Out] $b^3*\log(\text{abs}(b*x + a))/a^4 - b^3*\log(\text{abs}(x))/a^4 - 1/6*(6*a*b^2*x^2 - 3*a^2*b*x + 2*a^3)/(a^4*x^3)$

maple [A] time = 0.01, size = 53, normalized size = 0.95

$$-\frac{b^3 \ln(x)}{a^4} + \frac{b^3 \ln(bx + a)}{a^4} - \frac{b^2}{a^3x} + \frac{b}{2a^2x^2} - \frac{1}{3ax^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^4/(b*x+a),x)

[Out] $-1/3/a/x^3 + 1/2*b/a^2/x^2 - b^2/a^3/x - b^3*\ln(x)/a^4 + b^3*\ln(b*x+a)/a^4$

maxima [A] time = 1.35, size = 51, normalized size = 0.91

$$\frac{b^3 \log(bx + a)}{a^4} - \frac{b^3 \log(x)}{a^4} - \frac{6b^2x^2 - 3abx + 2a^2}{6a^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a),x, algorithm="maxima")

[Out] $b^3 \log(bx + a)/a^4 - b^3 \log(x)/a^4 - 1/6(6b^2x^2 - 3abx + 2a^2)/(a^3x^3)$

mupad [B] time = 0.10, size = 48, normalized size = 0.86

$$\frac{2b^3 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^4} - \frac{\frac{a^3}{3} - \frac{a^2bx}{2} + ab^2x^2}{a^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^4*(a + b*x)),x)`

[Out] $(2b^3 \operatorname{atanh}((2bx)/a + 1))/a^4 - (a^3/3 + ab^2x^2 - (a^2bx)/2)/(a^4x^3)$

sympy [A] time = 0.24, size = 44, normalized size = 0.79

$$\frac{-2a^2 + 3abx - 6b^2x^2}{6a^3x^3} + \frac{b^3(-\log(x) + \log(\frac{a}{b} + x))}{a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**4/(b*x+a),x)`

[Out] $(-2a**2 + 3a*b*x - 6b**2*x**2)/(6*a**3*x**3) + b**3*(-\log(x) + \log(a/b + x))/a**4$

$$3.167 \quad \int \frac{1}{x^5(a+bx)} dx$$

Optimal. Leaf size=68

$$\frac{b^4 \log(x)}{a^5} - \frac{b^4 \log(a+bx)}{a^5} + \frac{b^3}{a^4 x} - \frac{b^2}{2a^3 x^2} + \frac{b}{3a^2 x^3} - \frac{1}{4ax^4}$$

[Out] $-1/4/a/x^4+1/3*b/a^2/x^3-1/2*b^2/a^3/x^2+b^3/a^4/x+b^4*\ln(x)/a^5-b^4*\ln(b*x+a)/a^5$

Rubi [A] time = 0.04, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{b^2}{2a^3 x^2} + \frac{b^3}{a^4 x} + \frac{b^4 \log(x)}{a^5} - \frac{b^4 \log(a+bx)}{a^5} + \frac{b}{3a^2 x^3} - \frac{1}{4ax^4}$$

Antiderivative was successfully verified.

[In] Int[1/(x^5*(a + b*x)),x]

[Out] $-1/(4*a*x^4) + b/(3*a^2*x^3) - b^2/(2*a^3*x^2) + b^3/(a^4*x) + (b^4*\text{Log}[x])/a^5 - (b^4*\text{Log}[a + b*x])/a^5$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^5(a+bx)} dx &= \int \left(\frac{1}{ax^5} - \frac{b}{a^2 x^4} + \frac{b^2}{a^3 x^3} - \frac{b^3}{a^4 x^2} + \frac{b^4}{a^5 x} - \frac{b^5}{a^5(a+bx)} \right) dx \\ &= -\frac{1}{4ax^4} + \frac{b}{3a^2 x^3} - \frac{b^2}{2a^3 x^2} + \frac{b^3}{a^4 x} + \frac{b^4 \log(x)}{a^5} - \frac{b^4 \log(a+bx)}{a^5} \end{aligned}$$

Mathematica [A] time = 0.00, size = 68, normalized size = 1.00

$$\frac{b^4 \log(x)}{a^5} - \frac{b^4 \log(a+bx)}{a^5} + \frac{b^3}{a^4 x} - \frac{b^2}{2a^3 x^2} + \frac{b}{3a^2 x^3} - \frac{1}{4ax^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^5*(a + b*x)),x]

[Out] $-1/4*1/(a*x^4) + b/(3*a^2*x^3) - b^2/(2*a^3*x^2) + b^3/(a^4*x) + (b^4*\text{Log}[x])/a^5 - (b^4*\text{Log}[a + b*x])/a^5$

fricas [A] time = 0.46, size = 65, normalized size = 0.96

$$\frac{12 b^4 x^4 \log(bx + a) - 12 b^4 x^4 \log(x) - 12 a b^3 x^3 + 6 a^2 b^2 x^2 - 4 a^3 b x + 3 a^4}{12 a^5 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a),x, algorithm="fricas")

[Out] $-1/12*(12*b^4*x^4*\log(b*x + a) - 12*b^4*x^4*\log(x) - 12*a*b^3*x^3 + 6*a^2*b^2*x^2 - 4*a^3*b*x + 3*a^4)/(a^5*x^4)$

giac [A] time = 1.06, size = 67, normalized size = 0.99

$$-\frac{b^4 \log(|bx + a|)}{a^5} + \frac{b^4 \log(|x|)}{a^5} + \frac{12 a b^3 x^3 - 6 a^2 b^2 x^2 + 4 a^3 b x - 3 a^4}{12 a^5 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a),x, algorithm="giac")

[Out] $-b^4*\log(\text{abs}(b*x + a))/a^5 + b^4*\log(\text{abs}(x))/a^5 + 1/12*(12*a*b^3*x^3 - 6*a^2*b^2*x^2 + 4*a^3*b*x - 3*a^4)/(a^5*x^4)$

maple [A] time = 0.01, size = 63, normalized size = 0.93

$$\frac{b^4 \ln(x)}{a^5} - \frac{b^4 \ln(bx + a)}{a^5} + \frac{b^3}{a^4 x} - \frac{b^2}{2 a^3 x^2} + \frac{b}{3 a^2 x^3} - \frac{1}{4 a x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^5/(b*x+a),x)

[Out] $-1/4/a/x^4+1/3*b/a^2/x^3-1/2*b^2/a^3/x^2+b^3/a^4/x+b^4*\ln(x)/a^5-b^4*\ln(b*x+a)/a^5$

maxima [A] time = 1.36, size = 62, normalized size = 0.91

$$-\frac{b^4 \log(bx + a)}{a^5} + \frac{b^4 \log(x)}{a^5} + \frac{12 b^3 x^3 - 6 a b^2 x^2 + 4 a^2 b x - 3 a^3}{12 a^4 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a),x, algorithm="maxima")

[Out] $-b^4 \log(bx + a)/a^5 + b^4 \log(x)/a^5 + 1/12(12b^3x^3 - 6ab^2x^2 + 4a^2bx - 3a^3)/(a^4x^4)$

mupad [B] time = 0.07, size = 60, normalized size = 0.88

$$\frac{\frac{a^4}{4} - \frac{a^3bx}{3} + \frac{a^2b^2x^2}{2} - ab^3x^3}{a^5x^4} - \frac{2b^4 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^5*(a + b*x)),x)

[Out] $-(a^4/4 - ab^3x^3 + (a^2b^2x^2)/2 - (a^3bx)/3)/(a^5x^4) - (2b^4 \operatorname{atanh}((2bx)/a + 1))/a^5$

sympy [A] time = 0.28, size = 56, normalized size = 0.82

$$\frac{-3a^3 + 4a^2bx - 6ab^2x^2 + 12b^3x^3}{12a^4x^4} + \frac{b^4 \left(\log(x) - \log\left(\frac{a}{b} + x\right)\right)}{a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**5/(b*x+a),x)

[Out] $(-3a**3 + 4a**2*b*x - 6*a*b**2*x**2 + 12*b**3*x**3)/(12*a**4*x**4) + b**4 * (\log(x) - \log(a/b + x))/a**5$

$$3.168 \quad \int \frac{x^6}{(a+bx)^2} dx$$

Optimal. Leaf size=81

$$-\frac{a^6}{b^7(a+bx)} - \frac{6a^5 \log(a+bx)}{b^7} + \frac{5a^4x}{b^6} - \frac{2a^3x^2}{b^5} + \frac{a^2x^3}{b^4} - \frac{ax^4}{2b^3} + \frac{x^5}{5b^2}$$

[Out] $5a^4x/b^6 - 2a^3x^2/b^5 + a^2x^3/b^4 - 1/2ax^4/b^3 + 1/5x^5/b^2 - a^6/b^7/(b*x+a) - 6a^5*ln(b*x+a)/b^7$

Rubi [A] time = 0.06, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{2a^3x^2}{b^5} + \frac{a^2x^3}{b^4} - \frac{a^6}{b^7(a+bx)} + \frac{5a^4x}{b^6} - \frac{6a^5 \log(a+bx)}{b^7} - \frac{ax^4}{2b^3} + \frac{x^5}{5b^2}$$

Antiderivative was successfully verified.

[In] Int[x^6/(a + b*x)^2, x]

[Out] $(5a^4x)/b^6 - (2a^3x^2)/b^5 + (a^2x^3)/b^4 - (ax^4)/(2b^3) + x^5/(5b^2) - a^6/(b^7*(a + b*x)) - (6a^5*Log[a + b*x])/b^7$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^6}{(a+bx)^2} dx &= \int \left(\frac{5a^4}{b^6} - \frac{4a^3x}{b^5} + \frac{3a^2x^2}{b^4} - \frac{2ax^3}{b^3} + \frac{x^4}{b^2} + \frac{a^6}{b^6(a+bx)^2} - \frac{6a^5}{b^6(a+bx)} \right) dx \\ &= \frac{5a^4x}{b^6} - \frac{2a^3x^2}{b^5} + \frac{a^2x^3}{b^4} - \frac{ax^4}{2b^3} + \frac{x^5}{5b^2} - \frac{a^6}{b^7(a+bx)} - \frac{6a^5 \log(a+bx)}{b^7} \end{aligned}$$

Mathematica [A] time = 0.02, size = 77, normalized size = 0.95

$$\frac{-\frac{10a^6}{a+bx} - 60a^5 \log(a+bx) + 50a^4bx - 20a^3b^2x^2 + 10a^2b^3x^3 - 5ab^4x^4 + 2b^5x^5}{10b^7}$$

Antiderivative was successfully verified.

[In] Integrate[x^6/(a + b*x)^2,x]

[Out] (50*a^4*b*x - 20*a^3*b^2*x^2 + 10*a^2*b^3*x^3 - 5*a*b^4*x^4 + 2*b^5*x^5 - (10*a^6)/(a + b*x) - 60*a^5*Log[a + b*x])/(10*b^7)

fricas [A] time = 0.46, size = 96, normalized size = 1.19

$$\frac{2b^6x^6 - 3ab^5x^5 + 5a^2b^4x^4 - 10a^3b^3x^3 + 30a^4b^2x^2 + 50a^5bx - 10a^6 - 60(a^5bx + a^6)\log(bx + a)}{10(b^8x + ab^7)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/10*(2*b^6*x^6 - 3*a*b^5*x^5 + 5*a^2*b^4*x^4 - 10*a^3*b^3*x^3 + 30*a^4*b^2*x^2 + 50*a^5*b*x - 10*a^6 - 60*(a^5*b*x + a^6)*log(b*x + a))/(b^8*x + a*b^7)

giac [A] time = 1.14, size = 103, normalized size = 1.27

$$-\frac{(bx+a)^5\left(\frac{15a}{bx+a} - \frac{50a^2}{(bx+a)^2} + \frac{100a^3}{(bx+a)^3} - \frac{150a^4}{(bx+a)^4} - 2\right)}{10b^7} + \frac{6a^5\log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b^7} - \frac{a^6}{(bx+a)b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^2,x, algorithm="giac")

[Out] -1/10*(b*x + a)^5*(15*a/(b*x + a) - 50*a^2/(b*x + a)^2 + 100*a^3/(b*x + a)^3 - 150*a^4/(b*x + a)^4 - 2)/b^7 + 6*a^5*log(abs(b*x + a)/((b*x + a)^2*abs(b)))/b^7 - a^6/((b*x + a)*b^7)

maple [A] time = 0.01, size = 78, normalized size = 0.96

$$\frac{x^5}{5b^2} - \frac{ax^4}{2b^3} + \frac{a^2x^3}{b^4} - \frac{2a^3x^2}{b^5} - \frac{a^6}{(bx+a)b^7} - \frac{6a^5\ln(bx+a)}{b^7} + \frac{5a^4x}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/(b*x+a)^2,x)

[Out] 5*a^4*x/b^6-2*a^3*x^2/b^5+a^2*x^3/b^4-1/2*a*x^4/b^3+1/5*x^5/b^2-a^6/b^7/(b*x+a)-6*a^5*ln(b*x+a)/b^7

maxima [A] time = 1.33, size = 82, normalized size = 1.01

$$-\frac{a^6}{b^8x + ab^7} - \frac{6a^5\log(bx + a)}{b^7} + \frac{2b^4x^5 - 5ab^3x^4 + 10a^2b^2x^3 - 20a^3bx^2 + 50a^4x}{10b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^2,x, algorithm="maxima")

[Out] $-a^6/(b^8x + a*b^7) - 6*a^5*\log(b*x + a)/b^7 + 1/10*(2*b^4*x^5 - 5*a*b^3*x^4 + 10*a^2*b^2*x^3 - 20*a^3*b*x^2 + 50*a^4*x)/b^6$

mupad [B] time = 0.14, size = 83, normalized size = 1.02

$$\frac{x^5}{5b^2} - \frac{6a^5 \ln(a+bx)}{b^7} - \frac{ax^4}{2b^3} + \frac{5a^4x}{b^6} + \frac{a^2x^3}{b^4} - \frac{2a^3x^2}{b^5} - \frac{a^6}{b(xb^7 + ab^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/(a + b*x)^2,x)

[Out] $x^5/(5*b^2) - (6*a^5*\log(a + b*x))/b^7 - (a*x^4)/(2*b^3) + (5*a^4*x)/b^6 + (a^2*x^3)/b^4 - (2*a^3*x^2)/b^5 - a^6/(b*(a*b^6 + b^7*x))$

sympy [A] time = 0.28, size = 78, normalized size = 0.96

$$-\frac{a^6}{ab^7 + b^8x} - \frac{6a^5 \log(a+bx)}{b^7} + \frac{5a^4x}{b^6} - \frac{2a^3x^2}{b^5} + \frac{a^2x^3}{b^4} - \frac{ax^4}{2b^3} + \frac{x^5}{5b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6/(b*x+a)**2,x)

[Out] $-a**6/(a*b**7 + b**8*x) - 6*a**5*\log(a + b*x)/b**7 + 5*a**4*x/b**6 - 2*a**3*x**2/b**5 + a**2*x**3/b**4 - a*x**4/(2*b**3) + x**5/(5*b**2)$

$$3.169 \quad \int \frac{x^5}{(a+bx)^2} dx$$

Optimal. Leaf size=72

$$\frac{a^5}{b^6(a+bx)} + \frac{5a^4 \log(a+bx)}{b^6} - \frac{4a^3x}{b^5} + \frac{3a^2x^2}{2b^4} - \frac{2ax^3}{3b^3} + \frac{x^4}{4b^2}$$

[Out] $-4*a^3*x/b^5+3/2*a^2*x^2/b^4-2/3*a*x^3/b^3+1/4*x^4/b^2+a^5/b^6/(b*x+a)+5*a^4*\ln(b*x+a)/b^6$

Rubi [A] time = 0.04, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3a^2x^2}{2b^4} + \frac{a^5}{b^6(a+bx)} - \frac{4a^3x}{b^5} + \frac{5a^4 \log(a+bx)}{b^6} - \frac{2ax^3}{3b^3} + \frac{x^4}{4b^2}$$

Antiderivative was successfully verified.

[In] Int[x^5/(a + b*x)^2,x]

[Out] $(-4*a^3*x)/b^5 + (3*a^2*x^2)/(2*b^4) - (2*a*x^3)/(3*b^3) + x^4/(4*b^2) + a^5/(b^6*(a + b*x)) + (5*a^4*Log[a + b*x])/b^6$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^5}{(a+bx)^2} dx &= \int \left(-\frac{4a^3}{b^5} + \frac{3a^2x}{b^4} - \frac{2ax^2}{b^3} + \frac{x^3}{b^2} - \frac{a^5}{b^5(a+bx)^2} + \frac{5a^4}{b^5(a+bx)} \right) dx \\ &= -\frac{4a^3x}{b^5} + \frac{3a^2x^2}{2b^4} - \frac{2ax^3}{3b^3} + \frac{x^4}{4b^2} + \frac{a^5}{b^6(a+bx)} + \frac{5a^4 \log(a+bx)}{b^6} \end{aligned}$$

Mathematica [A] time = 0.02, size = 66, normalized size = 0.92

$$\frac{\frac{12a^5}{a+bx} + 60a^4 \log(a+bx) - 48a^3bx + 18a^2b^2x^2 - 8ab^3x^3 + 3b^4x^4}{12b^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/(a + b*x)^2,x]

[Out] $(-48a^3bx + 18a^2b^2x^2 - 8ab^3x^3 + 3b^4x^4 + (12a^5)/(a + bx) + 60a^4\text{Log}[a + bx])/(12b^6)$

fricas [A] time = 0.44, size = 85, normalized size = 1.18

$$\frac{3b^5x^5 - 5ab^4x^4 + 10a^2b^3x^3 - 30a^3b^2x^2 - 48a^4bx + 12a^5 + 60(a^4bx + a^5)\log(bx + a)}{12(b^7x + ab^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^2,x, algorithm="fricas")

[Out] $1/12*(3*b^5*x^5 - 5*a*b^4*x^4 + 10*a^2*b^3*x^3 - 30*a^3*b^2*x^2 - 48*a^4*b*x + 12*a^5 + 60*(a^4*b*x + a^5)*\log(b*x + a))/(b^7*x + a*b^6)$

giac [A] time = 1.22, size = 90, normalized size = 1.25

$$-\frac{(bx + a)^4 \left(\frac{20a}{bx+a} - \frac{60a^2}{(bx+a)^2} + \frac{120a^3}{(bx+a)^3} - 3 \right)}{12b^6} - \frac{5a^4 \log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b^6} + \frac{a^5}{(bx+a)b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^2,x, algorithm="giac")

[Out] $-1/12*(b*x + a)^4*(20*a/(b*x + a) - 60*a^2/(b*x + a)^2 + 120*a^3/(b*x + a)^3 - 3)/b^6 - 5*a^4*\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b)))/b^6 + a^5/((b*x + a)*b^6)$

maple [A] time = 0.01, size = 67, normalized size = 0.93

$$\frac{x^4}{4b^2} - \frac{2ax^3}{3b^3} + \frac{3a^2x^2}{2b^4} + \frac{a^5}{(bx+a)b^6} + \frac{5a^4 \ln(bx+a)}{b^6} - \frac{4a^3x}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(b*x+a)^2,x)

[Out] $-4*a^3*x/b^5 + 3/2*a^2*x^2/b^4 - 2/3*a*x^3/b^3 + 1/4*x^4/b^2 + a^5/b^6/(b*x+a) + 5*a^4*\ln(b*x+a)/b^6$

maxima [A] time = 1.33, size = 70, normalized size = 0.97

$$\frac{a^5}{b^7x + ab^6} + \frac{5a^4 \log(bx + a)}{b^6} + \frac{3b^3x^4 - 8ab^2x^3 + 18a^2bx^2 - 48a^3x}{12b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^2,x, algorithm="maxima")

[Out] $a^5/(b^7*x + a*b^6) + 5*a^4*\log(b*x + a)/b^6 + 1/12*(3*b^3*x^4 - 8*a*b^2*x^3 + 18*a^2*b*x^2 - 48*a^3*x)/b^5$

mupad [B] time = 0.07, size = 72, normalized size = 1.00

$$\frac{x^4}{4b^2} + \frac{5a^4 \ln(ax + b)}{b^6} - \frac{2ax^3}{3b^3} - \frac{4a^3x}{b^5} + \frac{3a^2x^2}{2b^4} + \frac{a^5}{b(axb^6 + ab^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(a + b*x)^2,x)

[Out] $x^4/(4*b^2) + (5*a^4*\log(a + b*x))/b^6 - (2*a*x^3)/(3*b^3) - (4*a^3*x)/b^5 + (3*a^2*x^2)/(2*b^4) + a^5/(b*(a*b^5 + b^6*x))$

sympy [A] time = 0.25, size = 71, normalized size = 0.99

$$\frac{a^5}{ab^6 + b^7x} + \frac{5a^4 \log(ax + b)}{b^6} - \frac{4a^3x}{b^5} + \frac{3a^2x^2}{2b^4} - \frac{2ax^3}{3b^3} + \frac{x^4}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5/(b*x+a)**2,x)

[Out] $a**5/(a*b**6 + b**7*x) + 5*a**4*\log(a + b*x)/b**6 - 4*a**3*x/b**5 + 3*a**2*x**2/(2*b**4) - 2*a*x**3/(3*b**3) + x**4/(4*b**2)$

$$3.170 \quad \int \frac{x^4}{(a+bx)^2} dx$$

Optimal. Leaf size=58

$$-\frac{a^4}{b^5(a+bx)} - \frac{4a^3 \log(a+bx)}{b^5} + \frac{3a^2x}{b^4} - \frac{ax^2}{b^3} + \frac{x^3}{3b^2}$$

[Out] $3a^2x/b^4 - ax^2/b^3 + 1/3x^3/b^2 - a^4/b^5/(bx+a) - 4a^3 \ln(bx+a)/b^5$

Rubi [A] time = 0.03, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^4}{b^5(a+bx)} + \frac{3a^2x}{b^4} - \frac{4a^3 \log(a+bx)}{b^5} - \frac{ax^2}{b^3} + \frac{x^3}{3b^2}$$

Antiderivative was successfully verified.

[In] Int[x^4/(a + b*x)^2, x]

[Out] $(3a^2x)/b^4 - (ax^2)/b^3 + x^3/(3b^2) - a^4/(b^5(a + b*x)) - (4a^3 \text{Log}[a + b*x])/b^5$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{(a+bx)^2} dx &= \int \left(\frac{3a^2}{b^4} - \frac{2ax}{b^3} + \frac{x^2}{b^2} + \frac{a^4}{b^4(a+bx)^2} - \frac{4a^3}{b^4(a+bx)} \right) dx \\ &= \frac{3a^2x}{b^4} - \frac{ax^2}{b^3} + \frac{x^3}{3b^2} - \frac{a^4}{b^5(a+bx)} - \frac{4a^3 \log(a+bx)}{b^5} \end{aligned}$$

Mathematica [A] time = 0.02, size = 54, normalized size = 0.93

$$\frac{-\frac{3a^4}{a+bx} - 12a^3 \log(a+bx) + 9a^2bx - 3ab^2x^2 + b^3x^3}{3b^5}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/(a + b*x)^2,x]

[Out] (9*a^2*b*x - 3*a*b^2*x^2 + b^3*x^3 - (3*a^4)/(a + b*x) - 12*a^3*Log[a + b*x])/ (3*b^5)

fricas [A] time = 0.46, size = 73, normalized size = 1.26

$$\frac{b^4 x^4 - 2 a b^3 x^3 + 6 a^2 b^2 x^2 + 9 a^3 b x - 3 a^4 - 12 (a^3 b x + a^4) \log (b x + a)}{3 (b^6 x + a b^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/3*(b^4*x^4 - 2*a*b^3*x^3 + 6*a^2*b^2*x^2 + 9*a^3*b*x - 3*a^4 - 12*(a^3*b*x + a^4)*log(b*x + a))/(b^6*x + a*b^5)

giac [A] time = 1.07, size = 79, normalized size = 1.36

$$-\frac{(b x + a)^3 \left(\frac{6 a}{b x + a} - \frac{18 a^2}{(b x + a)^2} - 1 \right)}{3 b^5} + \frac{4 a^3 \log \left(\frac{|b x + a|}{(b x + a)^2 |b|} \right)}{b^5} - \frac{a^4}{(b x + a) b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^2,x, algorithm="giac")

[Out] -1/3*(b*x + a)^3*(6*a/(b*x + a) - 18*a^2/(b*x + a)^2 - 1)/b^5 + 4*a^3*log(abs(b*x + a)/((b*x + a)^2*abs(b)))/b^5 - a^4/((b*x + a)*b^5)

maple [A] time = 0.01, size = 57, normalized size = 0.98

$$\frac{x^3}{3b^2} - \frac{ax^2}{b^3} - \frac{a^4}{(bx+a)b^5} - \frac{4a^3 \ln(bx+a)}{b^5} + \frac{3a^2x}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(b*x+a)^2,x)

[Out] 3*a^2*x/b^4-a*x^2/b^3+1/3*x^3/b^2-a^4/b^5/(b*x+a)-4*a^3*ln(b*x+a)/b^5

maxima [A] time = 1.37, size = 59, normalized size = 1.02

$$-\frac{a^4}{b^6 x + a b^5} - \frac{4 a^3 \log (b x + a)}{b^5} + \frac{b^2 x^3 - 3 a b x^2 + 9 a^2 x}{3 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^2,x, algorithm="maxima")

[Out] $-a^4/(b^6*x + a*b^5) - 4*a^3*\log(b*x + a)/b^5 + 1/3*(b^2*x^3 - 3*a*b*x^2 + 9*a^2*x)/b^4$

mupad [B] time = 0.07, size = 62, normalized size = 1.07

$$\frac{x^3}{3b^2} - \frac{4a^3 \ln(a+bx)}{b^5} - \frac{ax^2}{b^3} + \frac{3a^2x}{b^4} - \frac{a^4}{b(xb^5 + ab^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(a + b*x)^2,x)

[Out] $x^3/(3*b^2) - (4*a^3*\log(a + b*x))/b^5 - (a*x^2)/b^3 + (3*a^2*x)/b^4 - a^4/(b*(a*b^4 + b^5*x))$

sympy [A] time = 0.22, size = 54, normalized size = 0.93

$$-\frac{a^4}{ab^5 + b^6x} - \frac{4a^3 \log(a+bx)}{b^5} + \frac{3a^2x}{b^4} - \frac{ax^2}{b^3} + \frac{x^3}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/(b*x+a)**2,x)

[Out] $-a**4/(a*b**5 + b**6*x) - 4*a**3*\log(a + b*x)/b**5 + 3*a**2*x/b**4 - a*x**2/b**3 + x**3/(3*b**2)$

$$3.171 \quad \int \frac{x^3}{(a+bx)^2} dx$$

Optimal. Leaf size=46

$$\frac{a^3}{b^4(a+bx)} + \frac{3a^2 \log(a+bx)}{b^4} - \frac{2ax}{b^3} + \frac{x^2}{2b^2}$$

[Out] $-2*a*x/b^3 + 1/2*x^2/b^2 + a^3/b^4/(b*x+a) + 3*a^2*\ln(b*x+a)/b^4$

Rubi [A] time = 0.03, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^3}{b^4(a+bx)} + \frac{3a^2 \log(a+bx)}{b^4} - \frac{2ax}{b^3} + \frac{x^2}{2b^2}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x)^2, x]

[Out] $(-2*a*x)/b^3 + x^2/(2*b^2) + a^3/(b^4*(a + b*x)) + (3*a^2*\text{Log}[a + b*x])/b^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(a+bx)^2} dx &= \int \left(-\frac{2a}{b^3} + \frac{x}{b^2} - \frac{a^3}{b^3(a+bx)^2} + \frac{3a^2}{b^3(a+bx)} \right) dx \\ &= -\frac{2ax}{b^3} + \frac{x^2}{2b^2} + \frac{a^3}{b^4(a+bx)} + \frac{3a^2 \log(a+bx)}{b^4} \end{aligned}$$

Mathematica [A] time = 0.01, size = 43, normalized size = 0.93

$$\frac{\frac{2a^3}{a+bx} + 6a^2 \log(a+bx) - 4abx + b^2x^2}{2b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x)^2,x]

[Out] $(-4*a*b*x + b^2*x^2 + (2*a^3)/(a + b*x) + 6*a^2*\text{Log}[a + b*x])/(2*b^4)$

fricas [A] time = 0.45, size = 62, normalized size = 1.35

$$\frac{b^3x^3 - 3ab^2x^2 - 4a^2bx + 2a^3 + 6(a^2bx + a^3)\log(bx + a)}{2(b^5x + ab^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^2,x, algorithm="fricas")

[Out] $1/2*(b^3*x^3 - 3*a*b^2*x^2 - 4*a^2*b*x + 2*a^3 + 6*(a^2*b*x + a^3)*\log(b*x + a))/(b^5*x + a*b^4)$

giac [A] time = 1.14, size = 66, normalized size = 1.43

$$-\frac{(bx + a)^2\left(\frac{6a}{bx+a} - 1\right)}{2b^4} - \frac{3a^2 \log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b^4} + \frac{a^3}{(bx + a)b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^2,x, algorithm="giac")

[Out] $-1/2*(b*x + a)^2*(6*a/(b*x + a) - 1)/b^4 - 3*a^2*\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b)))/b^4 + a^3/((b*x + a)*b^4)$

maple [A] time = 0.01, size = 45, normalized size = 0.98

$$\frac{x^2}{2b^2} + \frac{a^3}{(bx + a)b^4} + \frac{3a^2 \ln(bx + a)}{b^4} - \frac{2ax}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^2,x)

[Out] $-2*a*x/b^3 + 1/2*x^2/b^2 + a^3/b^4/(b*x+a) + 3*a^2*\ln(b*x+a)/b^4$

maxima [A] time = 1.36, size = 47, normalized size = 1.02

$$\frac{a^3}{b^5x + ab^4} + \frac{3a^2 \log(bx + a)}{b^4} + \frac{bx^2 - 4ax}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^2,x, algorithm="maxima")

[Out] $a^3/(b^5x + a*b^4) + 3*a^2*\log(b*x + a)/b^4 + 1/2*(b*x^2 - 4*a*x)/b^3$

mupad [B] time = 0.08, size = 50, normalized size = 1.09

$$\frac{x^2}{2b^2} + \frac{3a^2 \ln(a + bx)}{b^4} + \frac{a^3}{b(xb^4 + ab^3)} - \frac{2ax}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3/(a + b*x)^2,x)`

[Out] $x^2/(2*b^2) + (3*a^2*\log(a + b*x))/b^4 + a^3/(b*(a*b^3 + b^4*x)) - (2*a*x)/b^3$

sympy [A] time = 0.20, size = 44, normalized size = 0.96

$$\frac{a^3}{ab^4 + b^5x} + \frac{3a^2 \log(a + bx)}{b^4} - \frac{2ax}{b^3} + \frac{x^2}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3/(b*x+a)**2,x)`

[Out] $a**3/(a*b**4 + b**5*x) + 3*a**2*\log(a + b*x)/b**4 - 2*a*x/b**3 + x**2/(2*b**2)$

$$3.172 \quad \int \frac{x^2}{(a+bx)^2} dx$$

Optimal. Leaf size=33

$$-\frac{a^2}{b^3(a+bx)} - \frac{2a \log(a+bx)}{b^3} + \frac{x}{b^2}$$

[Out] $x/b^2 - a^2/b^3/(b*x+a) - 2*a*\ln(b*x+a)/b^3$

Rubi [A] time = 0.02, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{b^3(a+bx)} - \frac{2a \log(a+bx)}{b^3} + \frac{x}{b^2}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*x)^2, x]

[Out] $x/b^2 - a^2/(b^3*(a + b*x)) - (2*a*\text{Log}[a + b*x])/b^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(a+bx)^2} dx &= \int \left(\frac{1}{b^2} + \frac{a^2}{b^2(a+bx)^2} - \frac{2a}{b^2(a+bx)} \right) dx \\ &= \frac{x}{b^2} - \frac{a^2}{b^3(a+bx)} - \frac{2a \log(a+bx)}{b^3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 0.88

$$\frac{-\frac{a^2}{a+bx} - 2a \log(a+bx) + bx}{b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x)^2,x]

[Out] (b*x - a^2/(a + b*x) - 2*a*Log[a + b*x])/b^3

fricas [A] time = 0.45, size = 47, normalized size = 1.42

$$\frac{b^2x^2 + abx - a^2 - 2(abx + a^2) \log(bx + a)}{b^4x + ab^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^2,x, algorithm="fricas")

[Out] (b^2*x^2 + a*b*x - a^2 - 2*(a*b*x + a^2)*log(b*x + a))/(b^4*x + a*b^3)

giac [A] time = 1.15, size = 50, normalized size = 1.52

$$\frac{2a \log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b^3} + \frac{bx+a}{b^3} - \frac{a^2}{(bx+a)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^2,x, algorithm="giac")

[Out] 2*a*log(abs(b*x + a)/((b*x + a)^2*abs(b)))/b^3 + (b*x + a)/b^3 - a^2/((b*x + a)*b^3)

maple [A] time = 0.01, size = 34, normalized size = 1.03

$$-\frac{a^2}{(bx+a)b^3} - \frac{2a \ln(bx+a)}{b^3} + \frac{x}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^2,x)

[Out] x/b^2-a^2/b^3/(b*x+a)-2*a*ln(b*x+a)/b^3

maxima [A] time = 1.34, size = 36, normalized size = 1.09

$$-\frac{a^2}{b^4x + ab^3} + \frac{x}{b^2} - \frac{2a \log(bx + a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^2,x, algorithm="maxima")

[Out] -a^2/(b^4*x + a*b^3) + x/b^2 - 2*a*log(b*x + a)/b^3

mupad [B] time = 0.08, size = 36, normalized size = 1.09

$$\frac{x}{b^2} - \frac{a^2}{x b^4 + a b^3} - \frac{2 a \ln(a + b x)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/(a + b*x)^2,x)`

[Out] `x/b^2 - a^2/(a*b^3 + b^4*x) - (2*a*log(a + b*x))/b^3`

sympy [A] time = 0.17, size = 31, normalized size = 0.94

$$-\frac{a^2}{a b^3 + b^4 x} - \frac{2 a \log(a + b x)}{b^3} + \frac{x}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2/(b*x+a)**2,x)`

[Out] `-a**2/(a*b**3 + b**4*x) - 2*a*log(a + b*x)/b**3 + x/b**2`

$$3.173 \quad \int \frac{x}{(a+bx)^2} dx$$

Optimal. Leaf size=23

$$\frac{a}{b^2(a+bx)} + \frac{\log(a+bx)}{b^2}$$

[Out] a/b^2/(b*x+a)+ln(b*x+a)/b^2

Rubi [A] time = 0.01, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.111, Rules used = {43}

$$\frac{a}{b^2(a+bx)} + \frac{\log(a+bx)}{b^2}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x)^2,x]

[Out] a/(b^2*(a + b*x)) + Log[a + b*x]/b^2

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x}{(a+bx)^2} dx &= \int \left(-\frac{a}{b(a+bx)^2} + \frac{1}{b(a+bx)} \right) dx \\ &= \frac{a}{b^2(a+bx)} + \frac{\log(a+bx)}{b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 0.87

$$\frac{\frac{a}{a+bx} + \log(a+bx)}{b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x)^2,x]

[Out] $(a/(a + b*x) + \text{Log}[a + b*x])/b^2$

fricas [A] time = 0.45, size = 28, normalized size = 1.22

$$\frac{(bx + a) \log(bx + a) + a}{b^3x + ab^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^2,x, algorithm="fricas")`

[Out] $((b*x + a)*\log(b*x + a) + a)/(b^3*x + a*b^2)$

giac [A] time = 1.05, size = 42, normalized size = 1.83

$$-\frac{\frac{\log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b} - \frac{a}{(bx+a)b}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^2,x, algorithm="giac")`

[Out] $-(\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b))))/b - a/((b*x + a)*b))/b$

maple [A] time = 0.01, size = 24, normalized size = 1.04

$$\frac{a}{(bx + a)b^2} + \frac{\ln(bx + a)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(b*x+a)^2,x)`

[Out] $a/b^2/(b*x+a)+\ln(b*x+a)/b^2$

maxima [A] time = 1.32, size = 26, normalized size = 1.13

$$\frac{a}{b^3x + ab^2} + \frac{\log(bx + a)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^2,x, algorithm="maxima")`

[Out] $a/(b^3*x + a*b^2) + \log(b*x + a)/b^2$

mupad [B] time = 0.04, size = 23, normalized size = 1.00

$$\frac{\ln(a + bx)}{b^2} + \frac{a}{b^2 (a + bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a + b*x)^2,x)`

[Out] `log(a + b*x)/b^2 + a/(b^2*(a + b*x))`

sympy [A] time = 0.17, size = 20, normalized size = 0.87

$$\frac{a}{ab^2 + b^3x} + \frac{\log(a + bx)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)**2,x)`

[Out] `a/(a*b**2 + b**3*x) + log(a + b*x)/b**2`

$$3.174 \quad \int \frac{1}{(a+bx)^2} dx$$

Optimal. Leaf size=12

$$-\frac{1}{b(a+bx)}$$

[Out] -1/b/(b*x+a)

Rubi [A] time = 0.00, antiderivative size = 12, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$-\frac{1}{b(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-2), x]

[Out] -(1/(b*(a + b*x)))

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^2} dx = -\frac{1}{b(a+bx)}$$

Mathematica [A] time = 0.00, size = 12, normalized size = 1.00

$$-\frac{1}{b(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-2), x]

[Out] -(1/(b*(a + b*x)))

fricas [A] time = 0.44, size = 13, normalized size = 1.08

$$-\frac{1}{b^2x+ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2,x, algorithm="fricas")

[Out] -1/(b^2*x + a*b)

giac [A] time = 1.18, size = 12, normalized size = 1.00

$$-\frac{1}{(bx + a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2,x, algorithm="giac")

[Out] -1/((b*x + a)*b)

maple [A] time = 0.00, size = 13, normalized size = 1.08

$$-\frac{1}{(bx + a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2,x)

[Out] -1/b/(b*x+a)

maxima [A] time = 1.38, size = 12, normalized size = 1.00

$$-\frac{1}{(bx + a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2,x, algorithm="maxima")

[Out] -1/((b*x + a)*b)

mupad [B] time = 0.03, size = 12, normalized size = 1.00

$$-\frac{1}{b(a + bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x)^2,x)

[Out] -1/(b*(a + b*x))

sympy [A] time = 0.15, size = 10, normalized size = 0.83

$$-\frac{1}{ab + b^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2,x)

[Out] -1/(a*b + b**2*x)

$$3.175 \quad \int \frac{1}{x(a+bx)^2} dx$$

Optimal. Leaf size=29

$$-\frac{\log(a+bx)}{a^2} + \frac{\log(x)}{a^2} + \frac{1}{a(a+bx)}$$

[Out] 1/a/(b*x+a)+ln(x)/a^2-ln(b*x+a)/a^2

Rubi [A] time = 0.01, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{\log(a+bx)}{a^2} + \frac{\log(x)}{a^2} + \frac{1}{a(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a + b*x)^2), x]

[Out] 1/(a*(a + b*x)) + Log[x]/a^2 - Log[a + b*x]/a^2

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x(a+bx)^2} dx &= \int \left(\frac{1}{a^2x} - \frac{b}{a(a+bx)^2} - \frac{b}{a^2(a+bx)} \right) dx \\ &= \frac{1}{a(a+bx)} + \frac{\log(x)}{a^2} - \frac{\log(a+bx)}{a^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.83

$$\frac{\frac{a}{a+bx} - \log(a+bx) + \log(x)}{a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)^2),x]

[Out] (a/(a + b*x) + Log[x] - Log[a + b*x])/a^2

fricas [A] time = 0.46, size = 39, normalized size = 1.34

$$\frac{(bx + a) \log(bx + a) - (bx + a) \log(x) - a}{a^2bx + a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^2,x, algorithm="fricas")

[Out] -((b*x + a)*log(b*x + a) - (b*x + a)*log(x) - a)/(a^2*b*x + a^3)

giac [A] time = 1.00, size = 38, normalized size = 1.31

$$b \left(\frac{\log \left(\left| -\frac{a}{bx+a} + 1 \right| \right)}{a^2b} + \frac{1}{(bx + a)ab} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^2,x, algorithm="giac")

[Out] b*(log(abs(-a/(b*x + a) + 1)))/(a^2*b) + 1/((b*x + a)*a*b))

maple [A] time = 0.01, size = 30, normalized size = 1.03

$$\frac{1}{(bx + a)a} + \frac{\ln(x)}{a^2} - \frac{\ln(bx + a)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a)^2,x)

[Out] 1/a/(b*x+a)+ln(x)/a^2-ln(b*x+a)/a^2

maxima [A] time = 1.30, size = 28, normalized size = 0.97

$$\frac{1}{abx + a^2} - \frac{\log(bx + a)}{a^2} + \frac{\log(x)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^2,x, algorithm="maxima")

[Out] 1/(a*b*x + a^2) - log(b*x + a)/a^2 + log(x)/a^2

mupad [B] time = 0.12, size = 26, normalized size = 0.90

$$\frac{1}{a^2 + b x a} - \frac{\ln\left(\frac{a+bx}{x}\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(a + b*x)^2),x)

[Out] 1/(a^2 + a*b*x) - log((a + b*x)/x)/a^2

sympy [A] time = 0.22, size = 22, normalized size = 0.76

$$\frac{1}{a^2 + abx} + \frac{\log(x) - \log\left(\frac{a}{b} + x\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)**2,x)

[Out] 1/(a**2 + a*b*x) + (log(x) - log(a/b + x))/a**2

$$3.176 \quad \int \frac{1}{x^2(a+bx)^2} dx$$

Optimal. Leaf size=42

$$-\frac{2b \log(x)}{a^3} + \frac{2b \log(a+bx)}{a^3} - \frac{b}{a^2(a+bx)} - \frac{1}{a^2x}$$

[Out] $-1/a^2/x - b/a^2/(b*x+a) - 2*b*\ln(x)/a^3 + 2*b*\ln(b*x+a)/a^3$

Rubi [A] time = 0.02, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{b}{a^2(a+bx)} - \frac{2b \log(x)}{a^3} + \frac{2b \log(a+bx)}{a^3} - \frac{1}{a^2x}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(a + b*x)^2), x]

[Out] $-(1/(a^2*x)) - b/(a^2*(a + b*x)) - (2*b*Log[x])/a^3 + (2*b*Log[a + b*x])/a^3$

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(a+bx)^2} dx &= \int \left(\frac{1}{a^2x^2} - \frac{2b}{a^3x} + \frac{b^2}{a^2(a+bx)^2} + \frac{2b^2}{a^3(a+bx)} \right) dx \\ &= -\frac{1}{a^2x} - \frac{b}{a^2(a+bx)} - \frac{2b \log(x)}{a^3} + \frac{2b \log(a+bx)}{a^3} \end{aligned}$$

Mathematica [A] time = 0.04, size = 35, normalized size = 0.83

$$-\frac{a \left(\frac{b}{a+bx} + \frac{1}{x} \right) - 2b \log(a+bx) + 2b \log(x)}{a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)^2), x]

[Out] -((a*(x^(-1) + b/(a + b*x)) + 2*b*Log[x] - 2*b*Log[a + b*x])/a^3)

fricas [A] time = 0.47, size = 63, normalized size = 1.50

$$\frac{2 abx + a^2 - 2 (b^2x^2 + abx) \log (bx + a) + 2 (b^2x^2 + abx) \log (x)}{a^3bx^2 + a^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^2,x, algorithm="fricas")

[Out] -(2*a*b*x + a^2 - 2*(b^2*x^2 + a*b*x)*log(b*x + a) + 2*(b^2*x^2 + a*b*x)*log(x))/(a^3*b*x^2 + a^4*x)

giac [A] time = 1.22, size = 52, normalized size = 1.24

$$-\frac{2 b \log \left(\left| -\frac{a}{bx+a} + 1 \right| \right)}{a^3} - \frac{b}{(bx+a)a^2} + \frac{b}{a^3 \left(\frac{a}{bx+a} - 1 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^2,x, algorithm="giac")

[Out] -2*b*log(abs(-a/(b*x + a) + 1))/a^3 - b/((b*x + a)*a^2) + b/(a^3*(a/(b*x + a) - 1))

maple [A] time = 0.01, size = 43, normalized size = 1.02

$$-\frac{b}{(bx+a)a^2} - \frac{2b \ln(x)}{a^3} + \frac{2b \ln(bx+a)}{a^3} - \frac{1}{a^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^2,x)

[Out] -1/a^2/x-b/a^2/(b*x+a)-2*b*ln(x)/a^3+2*b*ln(b*x+a)/a^3

maxima [A] time = 1.39, size = 45, normalized size = 1.07

$$-\frac{2 bx + a}{a^2bx^2 + a^3x} + \frac{2 b \log (bx + a)}{a^3} - \frac{2 b \log (x)}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^2,x, algorithm="maxima")

[Out] $-(2*b*x + a)/(a^2*b*x^2 + a^3*x) + 2*b*\log(b*x + a)/a^3 - 2*b*\log(x)/a^3$

mupad [B] time = 0.12, size = 45, normalized size = 1.07

$$\frac{2b \ln\left(\frac{a+bx}{x}\right)}{a^3} - \frac{1}{ax(a+bx)} - \frac{2b}{a^2(a+bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(a + b*x)^2),x)

[Out] $(2*b*\log((a + b*x)/x))/a^3 - 1/(a*x*(a + b*x)) - (2*b)/(a^2*(a + b*x))$

sympy [A] time = 0.30, size = 37, normalized size = 0.88

$$\frac{-a - 2bx}{a^3x + a^2bx^2} + \frac{2b(-\log(x) + \log\left(\frac{a}{b} + x\right))}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/(b*x+a)**2,x)

[Out] $(-a - 2*b*x)/(a**3*x + a**2*b*x**2) + 2*b*(-\log(x) + \log(a/b + x))/a**3$

$$3.177 \quad \int \frac{1}{x^3(a+bx)^2} dx$$

Optimal. Leaf size=58

$$\frac{3b^2 \log(x)}{a^4} - \frac{3b^2 \log(a+bx)}{a^4} + \frac{b^2}{a^3(a+bx)} + \frac{2b}{a^3x} - \frac{1}{2a^2x^2}$$

[Out] $-1/2/a^2/x^2+2*b/a^3/x+b^2/a^3/(b*x+a)+3*b^2*\ln(x)/a^4-3*b^2*\ln(b*x+a)/a^4$

Rubi [A] time = 0.03, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{b^2}{a^3(a+bx)} + \frac{3b^2 \log(x)}{a^4} - \frac{3b^2 \log(a+bx)}{a^4} + \frac{2b}{a^3x} - \frac{1}{2a^2x^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(a + b*x)^2), x]

[Out] $-1/(2*a^2*x^2) + (2*b)/(a^3*x) + b^2/(a^3*(a + b*x)) + (3*b^2*\text{Log}[x])/a^4 - (3*b^2*\text{Log}[a + b*x])/a^4$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^3(a+bx)^2} dx &= \int \left(\frac{1}{a^2x^3} - \frac{2b}{a^3x^2} + \frac{3b^2}{a^4x} - \frac{b^3}{a^3(a+bx)^2} - \frac{3b^3}{a^4(a+bx)} \right) dx \\ &= -\frac{1}{2a^2x^2} + \frac{2b}{a^3x} + \frac{b^2}{a^3(a+bx)} + \frac{3b^2 \log(x)}{a^4} - \frac{3b^2 \log(a+bx)}{a^4} \end{aligned}$$

Mathematica [A] time = 0.05, size = 53, normalized size = 0.91

$$\frac{a \left(\frac{2b^2}{a+bx} - \frac{a}{x^2} + \frac{4b}{x} \right) - 6b^2 \log(a+bx) + 6b^2 \log(x)}{2a^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)^2),x]

[Out] (a*(-(a/x^2) + (4*b)/x + (2*b^2)/(a + b*x)) + 6*b^2*Log[x] - 6*b^2*Log[a + b*x])/(2*a^4)

fricas [A] time = 0.45, size = 86, normalized size = 1.48

$$\frac{6ab^2x^2 + 3a^2bx - a^3 - 6(b^3x^3 + ab^2x^2)\log(bx + a) + 6(b^3x^3 + ab^2x^2)\log(x)}{2(a^4bx^3 + a^5x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/2*(6*a*b^2*x^2 + 3*a^2*b*x - a^3 - 6*(b^3*x^3 + a*b^2*x^2)*log(b*x + a) + 6*(b^3*x^3 + a*b^2*x^2)*log(x))/(a^4*b*x^3 + a^5*x^2)

giac [A] time = 1.13, size = 74, normalized size = 1.28

$$\frac{3b^2 \log\left(\left|-\frac{a}{bx+a} + 1\right|\right)}{a^4} + \frac{b^2}{(bx+a)a^3} - \frac{\frac{6ab^2}{bx+a} - 5b^2}{2a^4\left(\frac{a}{bx+a} - 1\right)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^2,x, algorithm="giac")

[Out] 3*b^2*log(abs(-a/(b*x + a) + 1))/a^4 + b^2/((b*x + a)*a^3) - 1/2*(6*a*b^2/(b*x + a) - 5*b^2)/(a^4*(a/(b*x + a) - 1)^2)

maple [A] time = 0.01, size = 57, normalized size = 0.98

$$\frac{b^2}{(bx+a)a^3} + \frac{3b^2 \ln(x)}{a^4} - \frac{3b^2 \ln(bx+a)}{a^4} + \frac{2b}{a^3x} - \frac{1}{2a^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a)^2,x)

[Out] -1/2/a^2/x^2+2*b/a^3/x+b^2/a^3/(b*x+a)+3*b^2*ln(x)/a^4-3*b^2*ln(b*x+a)/a^4

maxima [A] time = 1.40, size = 64, normalized size = 1.10

$$\frac{6b^2x^2 + 3abx - a^2}{2(a^3bx^3 + a^4x^2)} - \frac{3b^2 \log(bx + a)}{a^4} + \frac{3b^2 \log(x)}{a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^2,x, algorithm="maxima")

[Out] $\frac{1}{2} \cdot \frac{6b^2x^2 + 3abx - a^2}{a^3bx^3 + a^4x^2} - \frac{3b^2 \log(bx + a)}{a^4} + \frac{3b^2 \log(x)}{a^4}$

mupad [B] time = 0.11, size = 57, normalized size = 0.98

$$\frac{\frac{3b^2x^2}{a^3} - \frac{1}{2a} + \frac{3bx}{2a^2}}{bx^3 + ax^2} - \frac{6b^2 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(a + b*x)^2),x)

[Out] $\left(\frac{3b^2x^2}{a^3} - \frac{1}{2a} + \frac{3bx}{2a^2}\right) / (ax^2 + bx^3) - \frac{6b^2 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^4}$

sympy [A] time = 0.31, size = 54, normalized size = 0.93

$$\frac{-a^2 + 3abx + 6b^2x^2}{2a^4x^2 + 2a^3bx^3} + \frac{3b^2 \left(\log(x) - \log\left(\frac{a}{b} + x\right)\right)}{a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(b*x+a)**2,x)

[Out] $\frac{-a^{**2} + 3a*b*x + 6*b^{**2}*x^{**2}}{(2*a^{**4}*x^{**2} + 2*a^{**3}*b*x^{**3})} + \frac{3*b^{**2}*(\log(x) - \log(a/b + x))}{a^{**4}}$

$$3.178 \quad \int \frac{1}{x^4(a+bx)^2} dx$$

Optimal. Leaf size=69

$$-\frac{4b^3 \log(x)}{a^5} + \frac{4b^3 \log(a+bx)}{a^5} - \frac{b^3}{a^4(a+bx)} - \frac{3b^2}{a^4x} + \frac{b}{a^3x^2} - \frac{1}{3a^2x^3}$$

[Out] $-1/3/a^2/x^3+b/a^3/x^2-3*b^2/a^4/x-b^3/a^4/(b*x+a)-4*b^3*\ln(x)/a^5+4*b^3*\ln(b*x+a)/a^5$

Rubi [A] time = 0.03, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{b^3}{a^4(a+bx)} - \frac{3b^2}{a^4x} - \frac{4b^3 \log(x)}{a^5} + \frac{4b^3 \log(a+bx)}{a^5} + \frac{b}{a^3x^2} - \frac{1}{3a^2x^3}$$

Antiderivative was successfully verified.

[In] Int[1/(x^4*(a + b*x)^2), x]

[Out] $-1/(3*a^2*x^3) + b/(a^3*x^2) - (3*b^2)/(a^4*x) - b^3/(a^4*(a + b*x)) - (4*b^3*\text{Log}[x])/a^5 + (4*b^3*\text{Log}[a + b*x])/a^5$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^4(a+bx)^2} dx &= \int \left(\frac{1}{a^2x^4} - \frac{2b}{a^3x^3} + \frac{3b^2}{a^4x^2} - \frac{4b^3}{a^5x} + \frac{b^4}{a^4(a+bx)^2} + \frac{4b^4}{a^5(a+bx)} \right) dx \\ &= -\frac{1}{3a^2x^3} + \frac{b}{a^3x^2} - \frac{3b^2}{a^4x} - \frac{b^3}{a^4(a+bx)} - \frac{4b^3 \log(x)}{a^5} + \frac{4b^3 \log(a+bx)}{a^5} \end{aligned}$$

Mathematica [A] time = 0.06, size = 66, normalized size = 0.96

$$-\frac{a(a^3-2a^2bx+6ab^2x^2+12b^3x^3)}{x^3(a+bx)} - \frac{12b^3 \log(a+bx) + 12b^3 \log(x)}{3a^5}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^4*(a + b*x)^2),x]

[Out] $-1/3*((a*(a^3 - 2*a^2*b*x + 6*a*b^2*x^2 + 12*b^3*x^3))/(x^3*(a + b*x)) + 12*b^3*Log[x] - 12*b^3*Log[a + b*x])/a^5$

fricas [A] time = 0.50, size = 95, normalized size = 1.38

$$\frac{12ab^3x^3 + 6a^2b^2x^2 - 2a^3bx + a^4 - 12(b^4x^4 + ab^3x^3)\log(bx + a) + 12(b^4x^4 + ab^3x^3)\log(x)}{3(a^5bx^4 + a^6x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^2,x, algorithm="fricas")

[Out] $-1/3*(12*a*b^3*x^3 + 6*a^2*b^2*x^2 - 2*a^3*b*x + a^4 - 12*(b^4*x^4 + a*b^3*x^3)*\log(b*x + a) + 12*(b^4*x^4 + a*b^3*x^3)*\log(x))/(a^5*b*x^4 + a^6*x^3)$

giac [A] time = 1.02, size = 90, normalized size = 1.30

$$-\frac{4b^3 \log\left(-\frac{a}{bx+a} + 1\right)}{a^5} - \frac{b^3}{(bx+a)a^4} - \frac{\frac{30ab^3}{bx+a} - \frac{18a^2b^3}{(bx+a)^2} - 13b^3}{3a^5\left(\frac{a}{bx+a} - 1\right)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^2,x, algorithm="giac")

[Out] $-4*b^3*\log(\text{abs}(-a/(b*x + a) + 1))/a^5 - b^3/((b*x + a)*a^4) - 1/3*(30*a*b^3/(b*x + a) - 18*a^2*b^3/(b*x + a)^2 - 13*b^3)/(a^5*(a/(b*x + a) - 1)^3)$

maple [A] time = 0.01, size = 68, normalized size = 0.99

$$-\frac{b^3}{(bx+a)a^4} - \frac{4b^3 \ln(x)}{a^5} + \frac{4b^3 \ln(bx+a)}{a^5} - \frac{3b^2}{a^4x} + \frac{b}{a^3x^2} - \frac{1}{3a^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^4/(b*x+a)^2,x)

[Out] $-1/3/a^2/x^3 + b/a^3/x^2 - 3*b^2/a^4/x - b^3/a^4/(b*x+a) - 4*b^3*\ln(x)/a^5 + 4*b^3*\ln(b*x+a)/a^5$

maxima [A] time = 1.41, size = 73, normalized size = 1.06

$$-\frac{12b^3x^3 + 6ab^2x^2 - 2a^2bx + a^3}{3(a^4bx^4 + a^5x^3)} + \frac{4b^3 \log(bx+a)}{a^5} - \frac{4b^3 \log(x)}{a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^2,x, algorithm="maxima")

[Out] $-1/3*(12*b^3*x^3 + 6*a*b^2*x^2 - 2*a^2*b*x + a^3)/(a^4*b*x^4 + a^5*x^3) + 4*b^3*\log(b*x + a)/a^5 - 4*b^3*\log(x)/a^5$

mupad [B] time = 0.08, size = 69, normalized size = 1.00

$$\frac{8b^3 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^5} - \frac{\frac{1}{3a} + \frac{2b^2x^2}{a^3} + \frac{4b^3x^3}{a^4} - \frac{2bx}{3a^2}}{bx^4 + ax^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^4*(a + b*x)^2),x)

[Out] $(8*b^3*\operatorname{atanh}((2*b*x)/a + 1))/a^5 - (1/(3*a) + (2*b^2*x^2)/a^3 + (4*b^3*x^3)/a^4 - (2*b*x)/(3*a^2))/(a*x^3 + b*x^4)$

sympy [A] time = 0.34, size = 66, normalized size = 0.96

$$\frac{-a^3 + 2a^2bx - 6ab^2x^2 - 12b^3x^3}{3a^5x^3 + 3a^4bx^4} + \frac{4b^3(-\log(x) + \log(\frac{a}{b} + x))}{a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**4/(b*x+a)**2,x)

[Out] $(-a**3 + 2*a**2*b*x - 6*a*b**2*x**2 - 12*b**3*x**3)/(3*a**5*x**3 + 3*a**4*b*x**4) + 4*b**3*(-\log(x) + \log(a/b + x))/a**5$

$$3.179 \quad \int \frac{1}{x^5(a+bx)^2} dx$$

Optimal. Leaf size=84

$$\frac{5b^4 \log(x)}{a^6} - \frac{5b^4 \log(a+bx)}{a^6} + \frac{b^4}{a^5(a+bx)} + \frac{4b^3}{a^5x} - \frac{3b^2}{2a^4x^2} + \frac{2b}{3a^3x^3} - \frac{1}{4a^2x^4}$$

[Out] $-1/4/a^2/x^4+2/3*b/a^3/x^3-3/2*b^2/a^4/x^2+4*b^3/a^5/x+b^4/a^5/(b*x+a)+5*b^4*\ln(x)/a^6-5*b^4*\ln(b*x+a)/a^6$

Rubi [A] time = 0.04, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{3b^2}{2a^4x^2} + \frac{b^4}{a^5(a+bx)} + \frac{4b^3}{a^5x} + \frac{5b^4 \log(x)}{a^6} - \frac{5b^4 \log(a+bx)}{a^6} + \frac{2b}{3a^3x^3} - \frac{1}{4a^2x^4}$$

Antiderivative was successfully verified.

[In] Int[1/(x^5*(a + b*x)^2), x]

[Out] $-1/(4*a^2*x^4) + (2*b)/(3*a^3*x^3) - (3*b^2)/(2*a^4*x^2) + (4*b^3)/(a^5*x) + b^4/(a^5*(a + b*x)) + (5*b^4*\text{Log}[x])/a^6 - (5*b^4*\text{Log}[a + b*x])/a^6$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{x^5(a+bx)^2} dx = \int \left(\frac{1}{a^2x^5} - \frac{2b}{a^3x^4} + \frac{3b^2}{a^4x^3} - \frac{4b^3}{a^5x^2} + \frac{5b^4}{a^6x} - \frac{b^5}{a^5(a+bx)^2} - \frac{5b^5}{a^6(a+bx)} \right) dx$$

$$= -\frac{1}{4a^2x^4} + \frac{2b}{3a^3x^3} - \frac{3b^2}{2a^4x^2} + \frac{4b^3}{a^5x} + \frac{b^4}{a^5(a+bx)} + \frac{5b^4 \log(x)}{a^6} - \frac{5b^4 \log(a+bx)}{a^6}$$

Mathematica [A] time = 0.04, size = 79, normalized size = 0.94

$$\frac{a(-3a^4+5a^3bx-10a^2b^2x^2+30ab^3x^3+60b^4x^4)}{x^4(a+bx)} - 60b^4 \log(a+bx) + 60b^4 \log(x)$$

$$12a^6$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^5*(a + b*x)^2),x]

[Out] ((a*(-3*a^4 + 5*a^3*b*x - 10*a^2*b^2*x^2 + 30*a*b^3*x^3 + 60*b^4*x^4))/(x^4*(a + b*x)) + 60*b^4*Log[x] - 60*b^4*Log[a + b*x])/(12*a^6)

fricas [A] time = 0.60, size = 108, normalized size = 1.29

$$\frac{60 ab^4 x^4 + 30 a^2 b^3 x^3 - 10 a^3 b^2 x^2 + 5 a^4 b x - 3 a^5 - 60 (b^5 x^5 + ab^4 x^4) \log (bx + a) + 60 (b^5 x^5 + ab^4 x^4) \log (x)}{12 (a^6 b x^5 + a^7 x^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/12*(60*a*b^4*x^4 + 30*a^2*b^3*x^3 - 10*a^3*b^2*x^2 + 5*a^4*b*x - 3*a^5 - 60*(b^5*x^5 + a*b^4*x^4)*log(b*x + a) + 60*(b^5*x^5 + a*b^4*x^4)*log(x))/(a^6*b*x^5 + a^7*x^4)

giac [A] time = 0.99, size = 104, normalized size = 1.24

$$\frac{5 b^4 \log \left(\left| -\frac{a}{bx+a} + 1 \right| \right)}{a^6} + \frac{b^4}{(bx+a)a^5} - \frac{\frac{260 ab^4}{bx+a} - \frac{300 a^2 b^4}{(bx+a)^2} + \frac{120 a^3 b^4}{(bx+a)^3} - 77 b^4}{12 a^6 \left(\frac{a}{bx+a} - 1 \right)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a)^2,x, algorithm="giac")

[Out] 5*b^4*log(abs(-a/(b*x + a) + 1))/a^6 + b^4/((b*x + a)*a^5) - 1/12*(260*a*b^4/(b*x + a) - 300*a^2*b^4/(b*x + a)^2 + 120*a^3*b^4/(b*x + a)^3 - 77*b^4)/(a^6*(a/(b*x + a) - 1)^4)

maple [A] time = 0.01, size = 79, normalized size = 0.94

$$\frac{b^4}{(bx+a)a^5} + \frac{5b^4 \ln(x)}{a^6} - \frac{5b^4 \ln(bx+a)}{a^6} + \frac{4b^3}{a^5 x} - \frac{3b^2}{2a^4 x^2} + \frac{2b}{3a^3 x^3} - \frac{1}{4a^2 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^5/(b*x+a)^2,x)

[Out] -1/4/a^2/x^4+2/3*b/a^3/x^3-3/2*b^2/a^4/x^2+4*b^3/a^5/x+b^4/a^5/(b*x+a)+5*b^4*ln(x)/a^6-5*b^4*ln(b*x+a)/a^6

maxima [A] time = 1.34, size = 86, normalized size = 1.02

$$\frac{60b^4x^4 + 30ab^3x^3 - 10a^2b^2x^2 + 5a^3bx - 3a^4}{12(a^5bx^5 + a^6x^4)} - \frac{5b^4 \log(bx + a)}{a^6} + \frac{5b^4 \log(x)}{a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a)^2,x, algorithm="maxima")

[Out] 1/12*(60*b^4*x^4 + 30*a*b^3*x^3 - 10*a^2*b^2*x^2 + 5*a^3*b*x - 3*a^4)/(a^5*b*x^5 + a^6*x^4) - 5*b^4*log(b*x + a)/a^6 + 5*b^4*log(x)/a^6

mupad [B] time = 0.12, size = 79, normalized size = 0.94

$$\frac{\frac{5b^3x^3}{2a^4} - \frac{5b^2x^2}{6a^3} - \frac{1}{4a} + \frac{5b^4x^4}{a^5} + \frac{5bx}{12a^2}}{bx^5 + ax^4} - \frac{10b^4 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^5*(a + b*x)^2),x)

[Out] ((5*b^3*x^3)/(2*a^4) - (5*b^2*x^2)/(6*a^3) - 1/(4*a) + (5*b^4*x^4)/a^5 + (5*b*x)/(12*a^2))/(a*x^4 + b*x^5) - (10*b^4*atanh((2*b*x)/a + 1))/a^6

sympy [A] time = 0.39, size = 80, normalized size = 0.95

$$\frac{-3a^4 + 5a^3bx - 10a^2b^2x^2 + 30ab^3x^3 + 60b^4x^4}{12a^6x^4 + 12a^5bx^5} + \frac{5b^4 \left(\log(x) - \log\left(\frac{a}{b} + x\right) \right)}{a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**5/(b*x+a)**2,x)

[Out] (-3*a**4 + 5*a**3*b*x - 10*a**2*b**2*x**2 + 30*a*b**3*x**3 + 60*b**4*x**4)/(12*a**6*x**4 + 12*a**5*b*x**5) + 5*b**4*(log(x) - log(a/b + x))/a**6

$$3.180 \quad \int \frac{x^7}{(a+bx)^3} dx$$

Optimal. Leaf size=99

$$\frac{a^7}{2b^8(a+bx)^2} - \frac{7a^6}{b^8(a+bx)} - \frac{21a^5 \log(a+bx)}{b^8} + \frac{15a^4x}{b^7} - \frac{5a^3x^2}{b^6} + \frac{2a^2x^3}{b^5} - \frac{3ax^4}{4b^4} + \frac{x^5}{5b^3}$$

[Out] $15a^4x/b^7 - 5a^3x^2/b^6 + 2a^2x^3/b^5 - 3/4ax^4/b^4 + 1/5x^5/b^3 + 1/2a^7/b^8/(b*x+a)^2 - 7a^6/b^8/(b*x+a) - 21a^5*\ln(b*x+a)/b^8$

Rubi [A] time = 0.07, antiderivative size = 99, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{5a^3x^2}{b^6} + \frac{2a^2x^3}{b^5} + \frac{a^7}{2b^8(a+bx)^2} - \frac{7a^6}{b^8(a+bx)} + \frac{15a^4x}{b^7} - \frac{21a^5 \log(a+bx)}{b^8} - \frac{3ax^4}{4b^4} + \frac{x^5}{5b^3}$$

Antiderivative was successfully verified.

[In] Int[x^7/(a + b*x)^3, x]

[Out] $(15a^4x)/b^7 - (5a^3x^2)/b^6 + (2a^2x^3)/b^5 - (3ax^4)/(4b^4) + x^5/(5b^3) + a^7/(2b^8(a + b*x)^2) - (7a^6)/(b^8(a + b*x)) - (21a^5*\text{Log}[a + b*x])/b^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^7}{(a+bx)^3} dx &= \int \left(\frac{15a^4}{b^7} - \frac{10a^3x}{b^6} + \frac{6a^2x^2}{b^5} - \frac{3ax^3}{b^4} + \frac{x^4}{b^3} - \frac{a^7}{b^7(a+bx)^3} + \frac{7a^6}{b^7(a+bx)^2} - \frac{21a^5}{b^7(a+bx)} \right) dx \\ &= \frac{15a^4x}{b^7} - \frac{5a^3x^2}{b^6} + \frac{2a^2x^3}{b^5} - \frac{3ax^4}{4b^4} + \frac{x^5}{5b^3} + \frac{a^7}{2b^8(a+bx)^2} - \frac{7a^6}{b^8(a+bx)} - \frac{21a^5 \log(a+bx)}{b^8} \end{aligned}$$

Mathematica [A] time = 0.03, size = 89, normalized size = 0.90

$$\frac{10a^7}{(a+bx)^2} - \frac{140a^6}{a+bx} - 420a^5 \log(a+bx) + 300a^4bx - 100a^3b^2x^2 + 40a^2b^3x^3 - 15ab^4x^4 + 4b^5x^5}{20b^8}$$

Antiderivative was successfully verified.

[In] Integrate[x^7/(a + b*x)^3,x]

[Out] (300*a^4*b*x - 100*a^3*b^2*x^2 + 40*a^2*b^3*x^3 - 15*a*b^4*x^4 + 4*b^5*x^5 + (10*a^7)/(a + b*x)^2 - (140*a^6)/(a + b*x) - 420*a^5*Log[a + b*x])/(20*b^8)

fricas [A] time = 0.58, size = 129, normalized size = 1.30

$$\frac{4b^7x^7 - 7ab^6x^6 + 14a^2b^5x^5 - 35a^3b^4x^4 + 140a^4b^3x^3 + 500a^5b^2x^2 + 160a^6bx - 130a^7 - 420(a^5b^2x^2 + 2a^6bx + a^7)\log(bx + a)}{20(b^{10}x^2 + 2ab^9x + a^2b^8)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^3,x, algorithm="fricas")

[Out] 1/20*(4*b^7*x^7 - 7*a*b^6*x^6 + 14*a^2*b^5*x^5 - 35*a^3*b^4*x^4 + 140*a^4*b^3*x^3 + 500*a^5*b^2*x^2 + 160*a^6*b*x - 130*a^7 - 420*(a^5*b^2*x^2 + 2*a^6*b*x + a^7)*log(b*x + a))/(b^10*x^2 + 2*a*b^9*x + a^2*b^8)

giac [A] time = 0.89, size = 95, normalized size = 0.96

$$-\frac{21a^5\log(|bx+a|)}{b^8} - \frac{14a^6bx + 13a^7}{2(bx+a)^2b^8} + \frac{4b^{12}x^5 - 15ab^{11}x^4 + 40a^2b^{10}x^3 - 100a^3b^9x^2 + 300a^4b^8x}{20b^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^3,x, algorithm="giac")

[Out] -21*a^5*log(abs(b*x + a))/b^8 - 1/2*(14*a^6*b*x + 13*a^7)/((b*x + a)^2*b^8) + 1/20*(4*b^12*x^5 - 15*a*b^11*x^4 + 40*a^2*b^10*x^3 - 100*a^3*b^9*x^2 + 300*a^4*b^8*x)/b^15

maple [A] time = 0.01, size = 94, normalized size = 0.95

$$\frac{x^5}{5b^3} - \frac{3ax^4}{4b^4} + \frac{2a^2x^3}{b^5} + \frac{a^7}{2(bx+a)^2b^8} - \frac{5a^3x^2}{b^6} - \frac{7a^6}{(bx+a)b^8} - \frac{21a^5\ln(bx+a)}{b^8} + \frac{15a^4x}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7/(b*x+a)^3,x)

[Out] 15*a^4*x/b^7 - 5*a^3*x^2/b^6 + 2*a^2*x^3/b^5 - 3/4*a*x^4/b^4 + 1/5*x^5/b^3 + 1/2*a^7/b^8 - (b*x+a)^2 - 7*a^6/b^8/(b*x+a) - 21*a^5*ln(b*x+a)/b^8

maxima [A] time = 1.39, size = 103, normalized size = 1.04

$$\frac{14 a^6 b x + 13 a^7}{2 (b^{10} x^2 + 2 a b^9 x + a^2 b^8)} - \frac{21 a^5 \log(bx + a)}{b^8} + \frac{4 b^4 x^5 - 15 a b^3 x^4 + 40 a^2 b^2 x^3 - 100 a^3 b x^2 + 300 a^4 x}{20 b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^3,x, algorithm="maxima")

[Out] $-1/2*(14*a^6*b*x + 13*a^7)/(b^{10}*x^2 + 2*a*b^9*x + a^2*b^8) - 21*a^5*\log(b*x + a)/b^8 + 1/20*(4*b^4*x^5 - 15*a*b^3*x^4 + 40*a^2*b^2*x^3 - 100*a^3*b*x^2 + 300*a^4*x)/b^7$

mupad [B] time = 0.23, size = 91, normalized size = 0.92

$$\frac{\frac{7a(a+bx)^4}{4} - \frac{(a+bx)^5}{5} - 7a^2(a+bx)^3 + \frac{35a^3(a+bx)^2}{2} + \frac{7a^6}{a+bx} - \frac{a^7}{2(a+bx)^2} + 21a^5 \ln(a+bx) - 35a^4bx}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7/(a + b*x)^3,x)

[Out] $-((7*a*(a + b*x)^4)/4 - (a + b*x)^5/5 - 7*a^2*(a + b*x)^3 + (35*a^3*(a + b*x)^2)/2 + (7*a^6)/(a + b*x) - a^7/(2*(a + b*x)^2) + 21*a^5*\log(a + b*x) - 35*a^4*b*x)/b^8$

sympy [A] time = 0.53, size = 109, normalized size = 1.10

$$-\frac{21a^5 \log(a + bx)}{b^8} + \frac{15a^4x}{b^7} - \frac{5a^3x^2}{b^6} + \frac{2a^2x^3}{b^5} - \frac{3ax^4}{4b^4} + \frac{-13a^7 - 14a^6bx}{2a^2b^8 + 4ab^9x + 2b^{10}x^2} + \frac{x^5}{5b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**7/(b*x+a)**3,x)

[Out] $-21*a**5*\log(a + b*x)/b**8 + 15*a**4*x/b**7 - 5*a**3*x**2/b**6 + 2*a**2*x**3/b**5 - 3*a*x**4/(4*b**4) + (-13*a**7 - 14*a**6*b*x)/(2*a**2*b**8 + 4*a*b**9*x + 2*b**10*x**2) + x**5/(5*b**3)$

$$3.181 \quad \int \frac{x^6}{(a+bx)^3} dx$$

Optimal. Leaf size=86

$$-\frac{a^6}{2b^7(a+bx)^2} + \frac{6a^5}{b^7(a+bx)} + \frac{15a^4 \log(a+bx)}{b^7} - \frac{10a^3x}{b^6} + \frac{3a^2x^2}{b^5} - \frac{ax^3}{b^4} + \frac{x^4}{4b^3}$$

[Out] $-10*a^3*x/b^6+3*a^2*x^2/b^5-a*x^3/b^4+1/4*x^4/b^3-1/2*a^6/b^7/(b*x+a)^2+6*a^5/b^7/(b*x+a)+15*a^4*\ln(b*x+a)/b^7$

Rubi [A] time = 0.05, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3a^2x^2}{b^5} - \frac{a^6}{2b^7(a+bx)^2} + \frac{6a^5}{b^7(a+bx)} - \frac{10a^3x}{b^6} + \frac{15a^4 \log(a+bx)}{b^7} - \frac{ax^3}{b^4} + \frac{x^4}{4b^3}$$

Antiderivative was successfully verified.

[In] Int[x^6/(a + b*x)^3, x]

[Out] $(-10*a^3*x)/b^6 + (3*a^2*x^2)/b^5 - (a*x^3)/b^4 + x^4/(4*b^3) - a^6/(2*b^7*(a + b*x)^2) + (6*a^5)/(b^7*(a + b*x)) + (15*a^4*\text{Log}[a + b*x])/b^7$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^6}{(a+bx)^3} dx &= \int \left(-\frac{10a^3}{b^6} + \frac{6a^2x}{b^5} - \frac{3ax^2}{b^4} + \frac{x^3}{b^3} + \frac{a^6}{b^6(a+bx)^3} - \frac{6a^5}{b^6(a+bx)^2} + \frac{15a^4}{b^6(a+bx)} \right) dx \\ &= -\frac{10a^3x}{b^6} + \frac{3a^2x^2}{b^5} - \frac{ax^3}{b^4} + \frac{x^4}{4b^3} - \frac{a^6}{2b^7(a+bx)^2} + \frac{6a^5}{b^7(a+bx)} + \frac{15a^4 \log(a+bx)}{b^7} \end{aligned}$$

Mathematica [A] time = 0.02, size = 77, normalized size = 0.90

$$\frac{-\frac{2a^6}{(a+bx)^2} + \frac{24a^5}{a+bx} + 60a^4 \log(a+bx) - 40a^3bx + 12a^2b^2x^2 - 4ab^3x^3 + b^4x^4}{4b^7}$$

Antiderivative was successfully verified.

[In] Integrate[x^6/(a + b*x)^3,x]

[Out] $(-40*a^3*b*x + 12*a^2*b^2*x^2 - 4*a*b^3*x^3 + b^4*x^4 - (2*a^6)/(a + b*x)^2 + (24*a^5)/(a + b*x) + 60*a^4*Log[a + b*x])/(4*b^7)$

fricas [A] time = 0.45, size = 117, normalized size = 1.36

$$\frac{b^6x^6 - 2ab^5x^5 + 5a^2b^4x^4 - 20a^3b^3x^3 - 68a^4b^2x^2 - 16a^5bx + 22a^6 + 60(a^4b^2x^2 + 2a^5bx + a^6)\log(bx + a)}{4(b^9x^2 + 2ab^8x + a^2b^7)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^3,x, algorithm="fricas")

[Out] $1/4*(b^6*x^6 - 2*a*b^5*x^5 + 5*a^2*b^4*x^4 - 20*a^3*b^3*x^3 - 68*a^4*b^2*x^2 - 16*a^5*b*x + 22*a^6 + 60*(a^4*b^2*x^2 + 2*a^5*b*x + a^6)*\log(b*x + a))/(b^9*x^2 + 2*a*b^8*x + a^2*b^7)$

giac [A] time = 1.15, size = 83, normalized size = 0.97

$$\frac{15a^4\log(|bx+a|)}{b^7} + \frac{12a^5bx + 11a^6}{2(bx+a)^2b^7} + \frac{b^9x^4 - 4ab^8x^3 + 12a^2b^7x^2 - 40a^3b^6x}{4b^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^3,x, algorithm="giac")

[Out] $15*a^4*\log(\text{abs}(b*x + a))/b^7 + 1/2*(12*a^5*b*x + 11*a^6)/((b*x + a)^2*b^7) + 1/4*(b^9*x^4 - 4*a*b^8*x^3 + 12*a^2*b^7*x^2 - 40*a^3*b^6*x)/b^{12}$

maple [A] time = 0.01, size = 83, normalized size = 0.97

$$\frac{x^4}{4b^3} - \frac{ax^3}{b^4} - \frac{a^6}{2(bx+a)^2b^7} + \frac{3a^2x^2}{b^5} + \frac{6a^5}{(bx+a)b^7} + \frac{15a^4\ln(bx+a)}{b^7} - \frac{10a^3x}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/(b*x+a)^3,x)

[Out] $-10*a^3*x/b^6 + 3*a^2*x^2/b^5 - a*x^3/b^4 + 1/4*x^4/b^3 - 1/2*a^6/b^7/(b*x+a)^2 + 6*a^5/b^7/(b*x+a) + 15*a^4*\ln(b*x+a)/b^7$

maxima [A] time = 1.40, size = 91, normalized size = 1.06

$$\frac{12a^5bx + 11a^6}{2(b^9x^2 + 2ab^8x + a^2b^7)} + \frac{15a^4\log(bx+a)}{b^7} + \frac{b^3x^4 - 4ab^2x^3 + 12a^2bx^2 - 40a^3x}{4b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^3,x, algorithm="maxima")

[Out] $\frac{1}{2} \cdot \frac{12a^5bx + 11a^6}{(b^9x^2 + 2ab^8x + a^2b^7)} + 15a^4 \log(bx + a) / b^7 + \frac{1}{4} \cdot \frac{(b^3x^4 - 4ab^2x^3 + 12a^2bx^2 - 40a^3x)}{b^6}$

mupad [B] time = 0.16, size = 78, normalized size = 0.91

$$\frac{\frac{(a+bx)^4}{4} - 2a(a+bx)^3 + \frac{15a^2(a+bx)^2}{2} + \frac{6a^5}{a+bx} - \frac{a^6}{2(a+bx)^2} + 15a^4 \ln(a+bx) - 20a^3bx}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/(a + b*x)^3,x)

[Out] $((a + bx)^{4/4} - 2a(a + bx)^3 + (15a^2(a + bx)^2)/2 + (6a^5)/(a + bx) - a^6/(2(a + bx)^2) + 15a^4 \log(a + bx) - 20a^3bx) / b^7$

sympy [A] time = 0.40, size = 92, normalized size = 1.07

$$\frac{15a^4 \log(a + bx)}{b^7} - \frac{10a^3x}{b^6} + \frac{3a^2x^2}{b^5} - \frac{ax^3}{b^4} + \frac{11a^6 + 12a^5bx}{2a^2b^7 + 4ab^8x + 2b^9x^2} + \frac{x^4}{4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6/(b*x+a)**3,x)

[Out] $15a^{**4} \log(a + b*x) / b^{**7} - 10a^{**3}x / b^{**6} + 3a^{**2}x^{**2} / b^{**5} - a^{**3}x^{**3} / b^{**4} + (11a^{**6} + 12a^{**5}b*x) / (2a^{**2}b^{**7} + 4a*b^{**8}x + 2b^{**9}x^{**2}) + x^{**4} / (4b^{**3})$

$$3.182 \quad \int \frac{x^5}{(a+bx)^3} dx$$

Optimal. Leaf size=77

$$\frac{a^5}{2b^6(a+bx)^2} - \frac{5a^4}{b^6(a+bx)} - \frac{10a^3 \log(a+bx)}{b^6} + \frac{6a^2x}{b^5} - \frac{3ax^2}{2b^4} + \frac{x^3}{3b^3}$$

[Out] $6*a^2*x/b^5 - 3/2*a*x^2/b^4 + 1/3*x^3/b^3 + 1/2*a^5/b^6/(b*x+a)^2 - 5*a^4/b^6/(b*x+a) - 10*a^3*\ln(b*x+a)/b^6$

Rubi [A] time = 0.05, antiderivative size = 77, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^5}{2b^6(a+bx)^2} - \frac{5a^4}{b^6(a+bx)} + \frac{6a^2x}{b^5} - \frac{10a^3 \log(a+bx)}{b^6} - \frac{3ax^2}{2b^4} + \frac{x^3}{3b^3}$$

Antiderivative was successfully verified.

[In] Int[x^5/(a + b*x)^3, x]

[Out] $(6*a^2*x)/b^5 - (3*a*x^2)/(2*b^4) + x^3/(3*b^3) + a^5/(2*b^6*(a + b*x)^2) - (5*a^4)/(b^6*(a + b*x)) - (10*a^3*\text{Log}[a + b*x])/b^6$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^5}{(a+bx)^3} dx &= \int \left(\frac{6a^2}{b^5} - \frac{3ax}{b^4} + \frac{x^2}{b^3} - \frac{a^5}{b^5(a+bx)^3} + \frac{5a^4}{b^5(a+bx)^2} - \frac{10a^3}{b^5(a+bx)} \right) dx \\ &= \frac{6a^2x}{b^5} - \frac{3ax^2}{2b^4} + \frac{x^3}{3b^3} + \frac{a^5}{2b^6(a+bx)^2} - \frac{5a^4}{b^6(a+bx)} - \frac{10a^3 \log(a+bx)}{b^6} \end{aligned}$$

Mathematica [A] time = 0.02, size = 67, normalized size = 0.87

$$\frac{\frac{3a^5}{(a+bx)^2} - \frac{30a^4}{a+bx} - 60a^3 \log(a+bx) + 36a^2bx - 9ab^2x^2 + 2b^3x^3}{6b^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/(a + b*x)^3,x]

[Out] (36*a^2*b*x - 9*a*b^2*x^2 + 2*b^3*x^3 + (3*a^5)/(a + b*x)^2 - (30*a^4)/(a + b*x) - 60*a^3*Log[a + b*x])/(6*b^6)

fricas [A] time = 0.45, size = 107, normalized size = 1.39

$$\frac{2b^5x^5 - 5ab^4x^4 + 20a^2b^3x^3 + 63a^3b^2x^2 + 6a^4bx - 27a^5 - 60(a^3b^2x^2 + 2a^4bx + a^5)\log(bx + a)}{6(b^8x^2 + 2ab^7x + a^2b^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^3,x, algorithm="fricas")

[Out] 1/6*(2*b^5*x^5 - 5*a*b^4*x^4 + 20*a^2*b^3*x^3 + 63*a^3*b^2*x^2 + 6*a^4*b*x - 27*a^5 - 60*(a^3*b^2*x^2 + 2*a^4*b*x + a^5)*log(b*x + a))/(b^8*x^2 + 2*a*b^7*x + a^2*b^6)

giac [A] time = 1.12, size = 73, normalized size = 0.95

$$-\frac{10a^3\log(|bx+a|)}{b^6} - \frac{10a^4bx + 9a^5}{2(bx+a)^2b^6} + \frac{2b^6x^3 - 9ab^5x^2 + 36a^2b^4x}{6b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^3,x, algorithm="giac")

[Out] -10*a^3*log(abs(b*x + a))/b^6 - 1/2*(10*a^4*b*x + 9*a^5)/((b*x + a)^2*b^6) + 1/6*(2*b^6*x^3 - 9*a*b^5*x^2 + 36*a^2*b^4*x)/b^9

maple [A] time = 0.01, size = 72, normalized size = 0.94

$$\frac{x^3}{3b^3} + \frac{a^5}{2(bx+a)^2b^6} - \frac{3ax^2}{2b^4} - \frac{5a^4}{(bx+a)b^6} - \frac{10a^3\ln(bx+a)}{b^6} + \frac{6a^2x}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(b*x+a)^3,x)

[Out] 6*a^2*x/b^5 - 3/2*a*x^2/b^4 + 1/3*x^3/b^3 + 1/2*a^5/b^6/(b*x+a)^2 - 5*a^4/b^6/(b*x+a) - 10*a^3*ln(b*x+a)/b^6

maxima [A] time = 1.36, size = 81, normalized size = 1.05

$$-\frac{10a^4bx + 9a^5}{2(b^8x^2 + 2ab^7x + a^2b^6)} - \frac{10a^3\log(bx+a)}{b^6} + \frac{2b^2x^3 - 9abx^2 + 36a^2x}{6b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x⁵/(b*x+a)³,x, algorithm="maxima")

[Out] $-1/2*(10*a^4*b*x + 9*a^5)/(b^8*x^2 + 2*a*b^7*x + a^2*b^6) - 10*a^3*\log(b*x + a)/b^6 + 1/6*(2*b^2*x^3 - 9*a*b*x^2 + 36*a^2*x)/b^5$

mupad [B] time = 0.12, size = 67, normalized size = 0.87

$$\frac{\frac{5a(a+bx)^2}{2} - \frac{(a+bx)^3}{3} + \frac{5a^4}{a+bx} - \frac{a^5}{2(a+bx)^2} + 10a^3 \ln(a+bx) - 10a^2bx}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x⁵/(a + b*x)³,x)

[Out] $-((5*a*(a + b*x)^2)/2 - (a + b*x)^3/3 + (5*a^4)/(a + b*x) - a^5/(2*(a + b*x)^2) + 10*a^3*\log(a + b*x) - 10*a^2*b*x)/b^6$

sympy [A] time = 0.36, size = 85, normalized size = 1.10

$$-\frac{10a^3 \log(a+bx)}{b^6} + \frac{6a^2x}{b^5} - \frac{3ax^2}{2b^4} + \frac{-9a^5 - 10a^4bx}{2a^2b^6 + 4ab^7x + 2b^8x^2} + \frac{x^3}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5/(b*x+a)**3,x)

[Out] $-10*a**3*\log(a + b*x)/b**6 + 6*a**2*x/b**5 - 3*a*x**2/(2*b**4) + (-9*a**5 - 10*a**4*b*x)/(2*a**2*b**6 + 4*a*b**7*x + 2*b**8*x**2) + x**3/(3*b**3)$

$$3.183 \quad \int \frac{x^4}{(a+bx)^3} dx$$

Optimal. Leaf size=64

$$-\frac{a^4}{2b^5(a+bx)^2} + \frac{4a^3}{b^5(a+bx)} + \frac{6a^2 \log(a+bx)}{b^5} - \frac{3ax}{b^4} + \frac{x^2}{2b^3}$$

[Out] $-3*a*x/b^4 + 1/2*x^2/b^3 - 1/2*a^4/b^5/(b*x+a)^2 + 4*a^3/b^5/(b*x+a) + 6*a^2*\ln(b*x+a)/b^5$

Rubi [A] time = 0.04, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^4}{2b^5(a+bx)^2} + \frac{4a^3}{b^5(a+bx)} + \frac{6a^2 \log(a+bx)}{b^5} - \frac{3ax}{b^4} + \frac{x^2}{2b^3}$$

Antiderivative was successfully verified.

[In] Int[x^4/(a + b*x)^3, x]

[Out] $(-3*a*x)/b^4 + x^2/(2*b^3) - a^4/(2*b^5*(a + b*x)^2) + (4*a^3)/(b^5*(a + b*x)) + (6*a^2*\text{Log}[a + b*x])/b^5$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{(a+bx)^3} dx &= \int \left(-\frac{3a}{b^4} + \frac{x}{b^3} + \frac{a^4}{b^4(a+bx)^3} - \frac{4a^3}{b^4(a+bx)^2} + \frac{6a^2}{b^4(a+bx)} \right) dx \\ &= -\frac{3ax}{b^4} + \frac{x^2}{2b^3} - \frac{a^4}{2b^5(a+bx)^2} + \frac{4a^3}{b^5(a+bx)} + \frac{6a^2 \log(a+bx)}{b^5} \end{aligned}$$

Mathematica [A] time = 0.02, size = 55, normalized size = 0.86

$$\frac{-\frac{a^4}{(a+bx)^2} + \frac{8a^3}{a+bx} + 12a^2 \log(a+bx) - 6abx + b^2x^2}{2b^5}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/(a + b*x)^3,x]

[Out] $(-6*a*b*x + b^2*x^2 - a^4/(a + b*x)^2 + (8*a^3)/(a + b*x) + 12*a^2*\text{Log}[a + b*x])/(2*b^5)$

fricas [A] time = 0.48, size = 95, normalized size = 1.48

$$\frac{b^4 x^4 - 4 a b^3 x^3 - 11 a^2 b^2 x^2 + 2 a^3 b x + 7 a^4 + 12 (a^2 b^2 x^2 + 2 a^3 b x + a^4) \log (b x + a)}{2 (b^7 x^2 + 2 a b^6 x + a^2 b^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^3,x, algorithm="fricas")

[Out] $1/2*(b^4*x^4 - 4*a*b^3*x^3 - 11*a^2*b^2*x^2 + 2*a^3*b*x + 7*a^4 + 12*(a^2*b^2*x^2 + 2*a^3*b*x + a^4)*\log(b*x + a))/(b^7*x^2 + 2*a*b^6*x + a^2*b^5)$

giac [A] time = 0.95, size = 61, normalized size = 0.95

$$\frac{6 a^2 \log (|b x + a|)}{b^5} + \frac{b^3 x^2 - 6 a b^2 x}{2 b^6} + \frac{8 a^3 b x + 7 a^4}{2 (b x + a)^2 b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^3,x, algorithm="giac")

[Out] $6*a^2*\log(\text{abs}(b*x + a))/b^5 + 1/2*(b^3*x^2 - 6*a*b^2*x)/b^6 + 1/2*(8*a^3*b*x + 7*a^4)/((b*x + a)^2*b^5)$

maple [A] time = 0.01, size = 61, normalized size = 0.95

$$-\frac{a^4}{2 (b x + a)^2 b^5} + \frac{x^2}{2 b^3} + \frac{4 a^3}{(b x + a) b^5} + \frac{6 a^2 \ln (b x + a)}{b^5} - \frac{3 a x}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(b*x+a)^3,x)

[Out] $-3*a*x/b^4 + 1/2*x^2/b^3 - 1/2*a^4/b^5/(b*x+a)^2 + 4*a^3/b^5/(b*x+a) + 6*a^2*\ln(b*x+a)/b^5$

maxima [A] time = 1.33, size = 69, normalized size = 1.08

$$\frac{8 a^3 b x + 7 a^4}{2 (b^7 x^2 + 2 a b^6 x + a^2 b^5)} + \frac{6 a^2 \log (b x + a)}{b^5} + \frac{b x^2 - 6 a x}{2 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^3,x, algorithm="maxima")

[Out] $\frac{1}{2}*(8*a^3*b*x + 7*a^4)/(b^7*x^2 + 2*a*b^6*x + a^2*b^5) + 6*a^2*\log(b*x + a)/b^5 + 1/2*(b*x^2 - 6*a*x)/b^4$

mupad [B] time = 0.08, size = 54, normalized size = 0.84

$$\frac{\frac{(a+bx)^2}{2} + \frac{4a^3}{a+bx} - \frac{a^4}{2(a+bx)^2} + 6a^2 \ln(a+bx) - 4abx}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(a + b*x)^3,x)

[Out] $((a + b*x)^2/2 + (4*a^3)/(a + b*x) - a^4/(2*(a + b*x)^2) + 6*a^2*\log(a + b*x) - 4*a*b*x)/b^5$

sympy [A] time = 0.34, size = 70, normalized size = 1.09

$$\frac{6a^2 \log(a+bx)}{b^5} - \frac{3ax}{b^4} + \frac{7a^4 + 8a^3bx}{2a^2b^5 + 4ab^6x + 2b^7x^2} + \frac{x^2}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/(b*x+a)**3,x)

[Out] $6*a**2*\log(a + b*x)/b**5 - 3*a*x/b**4 + (7*a**4 + 8*a**3*b*x)/(2*a**2*b**5 + 4*a*b**6*x + 2*b**7*x**2) + x**2/(2*b**3)$

$$3.184 \quad \int \frac{x^3}{(a+bx)^3} dx$$

Optimal. Leaf size=50

$$\frac{a^3}{2b^4(a+bx)^2} - \frac{3a^2}{b^4(a+bx)} - \frac{3a \log(a+bx)}{b^4} + \frac{x}{b^3}$$

[Out] $x/b^3 + 1/2*a^3/b^4/(b*x+a)^2 - 3*a^2/b^4/(b*x+a) - 3*a*\ln(b*x+a)/b^4$

Rubi [A] time = 0.03, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^3}{2b^4(a+bx)^2} - \frac{3a^2}{b^4(a+bx)} - \frac{3a \log(a+bx)}{b^4} + \frac{x}{b^3}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x)^3, x]

[Out] $x/b^3 + a^3/(2*b^4*(a + b*x)^2) - (3*a^2)/(b^4*(a + b*x)) - (3*a*\text{Log}[a + b*x])/b^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(a+bx)^3} dx &= \int \left(\frac{1}{b^3} - \frac{a^3}{b^3(a+bx)^3} + \frac{3a^2}{b^3(a+bx)^2} - \frac{3a}{b^3(a+bx)} \right) dx \\ &= \frac{x}{b^3} + \frac{a^3}{2b^4(a+bx)^2} - \frac{3a^2}{b^4(a+bx)} - \frac{3a \log(a+bx)}{b^4} \end{aligned}$$

Mathematica [A] time = 0.04, size = 40, normalized size = 0.80

$$-\frac{\frac{a^2(5a+6bx)}{(a+bx)^2} + 6a \log(a+bx) - 2bx}{2b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x)^3,x]

[Out] -1/2*(-2*b*x + (a^2*(5*a + 6*b*x))/(a + b*x)^2 + 6*a*Log[a + b*x])/b^4

fricas [A] time = 0.46, size = 83, normalized size = 1.66

$$\frac{2b^3x^3 + 4ab^2x^2 - 4a^2bx - 5a^3 - 6(ab^2x^2 + 2a^2bx + a^3)\log(bx + a)}{2(b^6x^2 + 2ab^5x + a^2b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^3,x, algorithm="fricas")

[Out] 1/2*(2*b^3*x^3 + 4*a*b^2*x^2 - 4*a^2*b*x - 5*a^3 - 6*(a*b^2*x^2 + 2*a^2*b*x + a^3)*log(b*x + a))/(b^6*x^2 + 2*a*b^5*x + a^2*b^4)

giac [A] time = 0.96, size = 44, normalized size = 0.88

$$\frac{x}{b^3} - \frac{3a \log(|bx + a|)}{b^4} - \frac{6a^2bx + 5a^3}{2(bx + a)^2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^3,x, algorithm="giac")

[Out] x/b^3 - 3*a*log(abs(b*x + a))/b^4 - 1/2*(6*a^2*b*x + 5*a^3)/((b*x + a)^2*b^4)

maple [A] time = 0.01, size = 49, normalized size = 0.98

$$\frac{a^3}{2(bx + a)^2b^4} - \frac{3a^2}{(bx + a)b^4} - \frac{3a \ln(bx + a)}{b^4} + \frac{x}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^3,x)

[Out] x/b^3+1/2*a^3/b^4/(b*x+a)^2-3*a^2/b^4/(b*x+a)-3*a*ln(b*x+a)/b^4

maxima [A] time = 1.31, size = 57, normalized size = 1.14

$$-\frac{6a^2bx + 5a^3}{2(b^6x^2 + 2ab^5x + a^2b^4)} + \frac{x}{b^3} - \frac{3a \log(bx + a)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^3,x, algorithm="maxima")

[Out] $-1/2*(6*a^2*b*x + 5*a^3)/(b^6*x^2 + 2*a*b^5*x + a^2*b^4) + x/b^3 - 3*a*\log(b*x + a)/b^4$

mupad [B] time = 0.15, size = 43, normalized size = 0.86

$$-\frac{3a \ln(a + bx) - bx + \frac{3a^2}{a+bx} - \frac{a^3}{2(a+bx)^2}}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(a + b*x)^3,x)

[Out] $-(3*a*\log(a + b*x) - b*x + (3*a^2)/(a + b*x) - a^3/(2*(a + b*x)^2))/b^4$

sympy [A] time = 0.31, size = 58, normalized size = 1.16

$$-\frac{3a \log(a + bx)}{b^4} + \frac{-5a^3 - 6a^2bx}{2a^2b^4 + 4ab^5x + 2b^6x^2} + \frac{x}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(b*x+a)**3,x)

[Out] $-3*a*\log(a + b*x)/b**4 + (-5*a**3 - 6*a**2*b*x)/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) + x/b**3$

$$3.185 \quad \int \frac{x^2}{(a+bx)^3} dx$$

Optimal. Leaf size=41

$$-\frac{a^2}{2b^3(a+bx)^2} + \frac{2a}{b^3(a+bx)} + \frac{\log(a+bx)}{b^3}$$

[Out] $-1/2*a^2/b^3/(b*x+a)^2+2*a/b^3/(b*x+a)+\ln(b*x+a)/b^3$

Rubi [A] time = 0.02, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{2b^3(a+bx)^2} + \frac{2a}{b^3(a+bx)} + \frac{\log(a+bx)}{b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*x)^3,x]

[Out] $-a^2/(2*b^3*(a + b*x)^2) + (2*a)/(b^3*(a + b*x)) + \text{Log}[a + b*x]/b^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(a+bx)^3} dx &= \int \left(\frac{a^2}{b^2(a+bx)^3} - \frac{2a}{b^2(a+bx)^2} + \frac{1}{b^2(a+bx)} \right) dx \\ &= -\frac{a^2}{2b^3(a+bx)^2} + \frac{2a}{b^3(a+bx)} + \frac{\log(a+bx)}{b^3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.80

$$\frac{\frac{a(3a+4bx)}{(a+bx)^2} + 2 \log(a+bx)}{2b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x)^3,x]

[Out] ((a*(3*a + 4*b*x))/(a + b*x)^2 + 2*Log[a + b*x])/(2*b^3)

fricas [A] time = 0.47, size = 61, normalized size = 1.49

$$\frac{4 abx + 3 a^2 + 2 (b^2 x^2 + 2 abx + a^2) \log (bx + a)}{2 (b^5 x^2 + 2 ab^4 x + a^2 b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^3,x, algorithm="fricas")

[Out] 1/2*(4*a*b*x + 3*a^2 + 2*(b^2*x^2 + 2*a*b*x + a^2)*log(b*x + a))/(b^5*x^2 + 2*a*b^4*x + a^2*b^3)

giac [A] time = 1.08, size = 37, normalized size = 0.90

$$\frac{\log (|bx + a|)}{b^3} + \frac{4 ax + \frac{3 a^2}{b}}{2 (bx + a)^2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^3,x, algorithm="giac")

[Out] log(abs(b*x + a))/b^3 + 1/2*(4*a*x + 3*a^2/b)/((b*x + a)^2*b^2)

maple [A] time = 0.01, size = 40, normalized size = 0.98

$$-\frac{a^2}{2 (bx + a)^2 b^3} + \frac{2a}{(bx + a) b^3} + \frac{\ln (bx + a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^3,x)

[Out] -1/2*a^2/b^3/(b*x+a)^2+2*a/b^3/(b*x+a)+ln(b*x+a)/b^3

maxima [A] time = 1.34, size = 48, normalized size = 1.17

$$\frac{4 abx + 3 a^2}{2 (b^5 x^2 + 2 ab^4 x + a^2 b^3)} + \frac{\log (bx + a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^3,x, algorithm="maxima")

[Out] $1/2*(4*a*b*x + 3*a^2)/(b^5*x^2 + 2*a*b^4*x + a^2*b^3) + \log(b*x + a)/b^3$

mupad [B] time = 0.09, size = 46, normalized size = 1.12

$$\frac{\ln(a + bx)}{b^3} + \frac{\frac{3a^2}{2b^3} + \frac{2ax}{b^2}}{a^2 + 2abx + b^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/(a + b*x)^3,x)`

[Out] $\log(a + b*x)/b^3 + ((3*a^2)/(2*b^3) + (2*a*x)/b^2)/(a^2 + b^2*x^2 + 2*a*b*x)$

sympy [A] time = 0.25, size = 46, normalized size = 1.12

$$\frac{3a^2 + 4abx}{2a^2b^3 + 4ab^4x + 2b^5x^2} + \frac{\log(a + bx)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2/(b*x+a)**3,x)`

[Out] $(3*a**2 + 4*a*b*x)/(2*a**2*b**3 + 4*a*b**4*x + 2*b**5*x**2) + \log(a + b*x)/b**3$

$$3.186 \quad \int \frac{x}{(a+bx)^3} dx$$

Optimal. Leaf size=17

$$\frac{x^2}{2a(a+bx)^2}$$

[Out] 1/2*x^2/a/(b*x+a)^2

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.111, Rules used = {37}

$$\frac{x^2}{2a(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x)^3,x]

[Out] x^2/(2*a*(a + b*x)^2)

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp [((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{x}{(a+bx)^3} dx = \frac{x^2}{2a(a+bx)^2}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 1.18

$$-\frac{a+2bx}{2b^2(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x)^3,x]

[Out] -1/2*(a + 2*b*x)/(b^2*(a + b*x)^2)

fricas [B] time = 0.48, size = 32, normalized size = 1.88

$$\frac{2bx + a}{2(b^4x^2 + 2ab^3x + a^2b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)^3,x, algorithm="fricas")

[Out] -1/2*(2*b*x + a)/(b^4*x^2 + 2*a*b^3*x + a^2*b^2)

giac [A] time = 1.14, size = 18, normalized size = 1.06

$$\frac{2bx + a}{2(bx + a)^2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)^3,x, algorithm="giac")

[Out] -1/2*(2*b*x + a)/((b*x + a)^2*b^2)

maple [A] time = 0.00, size = 27, normalized size = 1.59

$$\frac{a}{2(bx + a)^2b^2} - \frac{1}{(bx + a)b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(b*x+a)^3,x)

[Out] 1/2*a/b^2/(b*x+a)^2-1/b^2/(b*x+a)

maxima [B] time = 1.39, size = 32, normalized size = 1.88

$$\frac{2bx + a}{2(b^4x^2 + 2ab^3x + a^2b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)^3,x, algorithm="maxima")

[Out] -1/2*(2*b*x + a)/(b^4*x^2 + 2*a*b^3*x + a^2*b^2)

mupad [B] time = 0.07, size = 32, normalized size = 1.88

$$\frac{\frac{a}{2b^2} + \frac{x}{b}}{a^2 + 2abx + b^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a + b*x)^3,x)`

[Out] $-(a/(2*b^2) + x/b)/(a^2 + b^2*x^2 + 2*a*b*x)$

sympy [B] time = 0.20, size = 32, normalized size = 1.88

$$\frac{-a - 2bx}{2a^2b^2 + 4ab^3x + 2b^4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)**3,x)`

[Out] $(-a - 2*b*x)/(2*a**2*b**2 + 4*a*b**3*x + 2*b**4*x**2)$

$$3.187 \quad \int \frac{1}{(a+bx)^3} dx$$

Optimal. Leaf size=14

$$-\frac{1}{2b(a+bx)^2}$$

[Out] -1/2/b/(b*x+a)^2

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$-\frac{1}{2b(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-3), x]

[Out] -1/(2*b*(a + b*x)^2)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^3} dx = -\frac{1}{2b(a+bx)^2}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\frac{1}{2b(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-3), x]

[Out] -1/2*1/(b*(a + b*x)^2)

fricas [A] time = 0.48, size = 24, normalized size = 1.71

$$-\frac{1}{2(b^3x^2 + 2ab^2x + a^2b)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3,x, algorithm="fricas")

[Out] -1/2/(b^3*x^2 + 2*a*b^2*x + a^2*b)

giac [A] time = 0.95, size = 12, normalized size = 0.86

$$-\frac{1}{2(bx+a)^2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3,x, algorithm="giac")

[Out] -1/2/((b*x + a)^2*b)

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$-\frac{1}{2(bx+a)^2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^3,x)

[Out] -1/2/b/(b*x+a)^2

maxima [A] time = 1.29, size = 12, normalized size = 0.86

$$-\frac{1}{2(bx+a)^2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3,x, algorithm="maxima")

[Out] -1/2/((b*x + a)^2*b)

mupad [B] time = 0.07, size = 26, normalized size = 1.86

$$-\frac{1}{2a^2b + 4ab^2x + 2b^3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x)^3,x)

[Out] -1/((2*a^2*b + 2*b^3*x^2 + 4*a*b^2*x))

sympy [B] time = 0.21, size = 26, normalized size = 1.86

$$-\frac{1}{2a^2b + 4ab^2x + 2b^3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**3,x)

[Out] -1/(2*a**2*b + 4*a*b**2*x + 2*b**3*x**2)

$$3.188 \quad \int \frac{1}{x(a+bx)^3} dx$$

Optimal. Leaf size=43

$$-\frac{\log(a+bx)}{a^3} + \frac{\log(x)}{a^3} + \frac{1}{a^2(a+bx)} + \frac{1}{2a(a+bx)^2}$$

[Out] 1/2/a/(b*x+a)^2+1/a^2/(b*x+a)+ln(x)/a^3-ln(b*x+a)/a^3

Rubi [A] time = 0.02, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{1}{a^2(a+bx)} - \frac{\log(a+bx)}{a^3} + \frac{\log(x)}{a^3} + \frac{1}{2a(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a + b*x)^3), x]

[Out] 1/(2*a*(a + b*x)^2) + 1/(a^2*(a + b*x)) + Log[x]/a^3 - Log[a + b*x]/a^3

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x(a+bx)^3} dx &= \int \left(\frac{1}{a^3x} - \frac{b}{a(a+bx)^3} - \frac{b}{a^2(a+bx)^2} - \frac{b}{a^3(a+bx)} \right) dx \\ &= \frac{1}{2a(a+bx)^2} + \frac{1}{a^2(a+bx)} + \frac{\log(x)}{a^3} - \frac{\log(a+bx)}{a^3} \end{aligned}$$

Mathematica [A] time = 0.03, size = 37, normalized size = 0.86

$$\frac{\frac{a(3a+2bx)}{(a+bx)^2} - 2\log(a+bx) + 2\log(x)}{2a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)^3), x]

[Out] ((a*(3*a + 2*b*x))/(a + b*x)^2 + 2*Log[x] - 2*Log[a + b*x])/(2*a^3)

fricas [A] time = 0.45, size = 80, normalized size = 1.86

$$\frac{2 abx + 3 a^2 - 2 (b^2 x^2 + 2 abx + a^2) \log (bx + a) + 2 (b^2 x^2 + 2 abx + a^2) \log (x)}{2 (a^3 b^2 x^2 + 2 a^4 bx + a^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^3,x, algorithm="fricas")

[Out] 1/2*(2*a*b*x + 3*a^2 - 2*(b^2*x^2 + 2*a*b*x + a^2)*log(b*x + a) + 2*(b^2*x^2 + 2*a*b*x + a^2)*log(x))/(a^3*b^2*x^2 + 2*a^4*b*x + a^5)

giac [A] time = 1.03, size = 43, normalized size = 1.00

$$-\frac{\log (bx + a)}{a^3} + \frac{\log (|x|)}{a^3} + \frac{2 abx + 3 a^2}{2 (bx + a)^2 a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^3,x, algorithm="giac")

[Out] -log(abs(b*x + a))/a^3 + log(abs(x))/a^3 + 1/2*(2*a*b*x + 3*a^2)/((b*x + a)^2*a^3)

maple [A] time = 0.01, size = 42, normalized size = 0.98

$$\frac{1}{2 (bx + a)^2 a} + \frac{1}{(bx + a) a^2} + \frac{\ln (x)}{a^3} - \frac{\ln (bx + a)}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a)^3,x)

[Out] 1/2/a/(b*x+a)^2+1/a^2/(b*x+a)+ln(x)/a^3-ln(b*x+a)/a^3

maxima [A] time = 1.35, size = 51, normalized size = 1.19

$$\frac{2 bx + 3 a}{2 (a^2 b^2 x^2 + 2 a^3 bx + a^4)} - \frac{\log (bx + a)}{a^3} + \frac{\log (x)}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^3,x, algorithm="maxima")

[Out] $1/2*(2*b*x + 3*a)/(a^2*b^2*x^2 + 2*a^3*b*x + a^4) - \log(b*x + a)/a^3 + \log(x)/a^3$

mupad [B] time = 0.10, size = 43, normalized size = 1.00

$$\frac{\frac{1}{a^2+bx} - \frac{\ln\left(\frac{a+bx}{x}\right)}{a^2}}{a} + \frac{1}{2a(a+bx)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(a + b*x)^3), x)`

[Out] $(1/(a^2 + a*b*x) - \log((a + b*x)/x)/a^2)/a + 1/(2*a*(a + b*x)^2)$

sympy [A] time = 0.35, size = 46, normalized size = 1.07

$$\frac{3a + 2bx}{2a^4 + 4a^3bx + 2a^2b^2x^2} + \frac{\log(x) - \log\left(\frac{a}{b} + x\right)}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b*x+a)**3, x)`

[Out] $(3*a + 2*b*x)/(2*a**4 + 4*a**3*b*x + 2*a**2*b**2*x**2) + (\log(x) - \log(a/b + x))/a**3$

$$3.189 \quad \int \frac{1}{x^2(a+bx)^3} dx$$

Optimal. Leaf size=57

$$-\frac{3b \log(x)}{a^4} + \frac{3b \log(a+bx)}{a^4} - \frac{2b}{a^3(a+bx)} - \frac{1}{a^3x} - \frac{b}{2a^2(a+bx)^2}$$

[Out] $-1/a^3/x - 1/2*b/a^2/(b*x+a)^2 - 2*b/a^3/(b*x+a) - 3*b*\ln(x)/a^4 + 3*b*\ln(b*x+a)/a^4$

Rubi [A] time = 0.03, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{2b}{a^3(a+bx)} - \frac{b}{2a^2(a+bx)^2} - \frac{3b \log(x)}{a^4} + \frac{3b \log(a+bx)}{a^4} - \frac{1}{a^3x}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(a + b*x)^3), x]

[Out] $-(1/(a^3*x)) - b/(2*a^2*(a + b*x)^2) - (2*b)/(a^3*(a + b*x)) - (3*b*\text{Log}[x])/a^4 + (3*b*\text{Log}[a + b*x])/a^4$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(a+bx)^3} dx &= \int \left(\frac{1}{a^3x^2} - \frac{3b}{a^4x} + \frac{b^2}{a^2(a+bx)^3} + \frac{2b^2}{a^3(a+bx)^2} + \frac{3b^2}{a^4(a+bx)} \right) dx \\ &= -\frac{1}{a^3x} - \frac{b}{2a^2(a+bx)^2} - \frac{2b}{a^3(a+bx)} - \frac{3b \log(x)}{a^4} + \frac{3b \log(a+bx)}{a^4} \end{aligned}$$

Mathematica [A] time = 0.05, size = 53, normalized size = 0.93

$$-\frac{a(2a^2+9abx+6b^2x^2)}{x(a+bx)^2} - 6b \log(a+bx) + 6b \log(x)$$

$$2a^4$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)^3),x]

[Out] $-1/2*((a*(2*a^2 + 9*a*b*x + 6*b^2*x^2))/(x*(a + b*x)^2) + 6*b*\text{Log}[x] - 6*b*\text{Log}[a + b*x])/a^4$

fricas [A] time = 0.50, size = 109, normalized size = 1.91

$$\frac{6ab^2x^2 + 9a^2bx + 2a^3 - 6(b^3x^3 + 2ab^2x^2 + a^2bx)\log(bx + a) + 6(b^3x^3 + 2ab^2x^2 + a^2bx)\log(x)}{2(a^4b^2x^3 + 2a^5bx^2 + a^6x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^3,x, algorithm="fricas")

[Out] $-1/2*(6*a*b^2*x^2 + 9*a^2*b*x + 2*a^3 - 6*(b^3*x^3 + 2*a*b^2*x^2 + a^2*b*x)*\log(b*x + a) + 6*(b^3*x^3 + 2*a*b^2*x^2 + a^2*b*x)*\log(x))/(a^4*b^2*x^3 + 2*a^5*b*x^2 + a^6*x)$

giac [A] time = 1.07, size = 60, normalized size = 1.05

$$\frac{3b\log(|bx + a|)}{a^4} - \frac{3b\log(|x|)}{a^4} - \frac{6ab^2x^2 + 9a^2bx + 2a^3}{2(bx + a)^2a^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^3,x, algorithm="giac")

[Out] $3*b*\log(\text{abs}(b*x + a))/a^4 - 3*b*\log(\text{abs}(x))/a^4 - 1/2*(6*a*b^2*x^2 + 9*a^2*b*x + 2*a^3)/((b*x + a)^2*a^4*x)$

maple [A] time = 0.01, size = 56, normalized size = 0.98

$$-\frac{b}{2(bx + a)^2a^2} - \frac{2b}{(bx + a)a^3} - \frac{3b\ln(x)}{a^4} + \frac{3b\ln(bx + a)}{a^4} - \frac{1}{a^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^3,x)

[Out] $-1/a^3/x - 1/2*b/a^2/(b*x+a)^2 - 2*b/a^3/(b*x+a) - 3*b*\ln(x)/a^4 + 3*b*\ln(b*x+a)/a^4$

maxima [A] time = 1.32, size = 69, normalized size = 1.21

$$-\frac{6b^2x^2 + 9abx + 2a^2}{2(a^3b^2x^3 + 2a^4bx^2 + a^5x)} + \frac{3b\log(bx + a)}{a^4} - \frac{3b\log(x)}{a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^3,x, algorithm="maxima")

[Out] $-1/2*(6*b^2*x^2 + 9*a*b*x + 2*a^2)/(a^3*b^2*x^3 + 2*a^4*b*x^2 + a^5*x) + 3*b*\log(b*x + a)/a^4 - 3*b*\log(x)/a^4$

mupad [B] time = 0.11, size = 63, normalized size = 1.11

$$\frac{6b \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^4} - \frac{\frac{1}{a} + \frac{3b^2x^2}{a^3} + \frac{9bx}{2a^2}}{a^2x + 2abx^2 + b^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(a + b*x)^3),x)

[Out] $(6*b*\operatorname{atanh}((2*b*x)/a + 1))/a^4 - (1/a + (3*b^2*x^2)/a^3 + (9*b*x)/(2*a^2))/(a^2*x + b^2*x^3 + 2*a*b*x^2)$

sympy [A] time = 0.40, size = 66, normalized size = 1.16

$$\frac{-2a^2 - 9abx - 6b^2x^2}{2a^5x + 4a^4bx^2 + 2a^3b^2x^3} + \frac{3b(-\log(x) + \log(\frac{a}{b} + x))}{a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/(b*x+a)**3,x)

[Out] $(-2*a**2 - 9*a*b*x - 6*b**2*x**2)/(2*a**5*x + 4*a**4*b*x**2 + 2*a**3*b**2*x**3) + 3*b*(-\log(x) + \log(a/b + x))/a**4$

$$3.190 \quad \int \frac{1}{x^3(a+bx)^3} dx$$

Optimal. Leaf size=76

$$\frac{6b^2 \log(x)}{a^5} - \frac{6b^2 \log(a+bx)}{a^5} + \frac{3b^2}{a^4(a+bx)} + \frac{3b}{a^4x} + \frac{b^2}{2a^3(a+bx)^2} - \frac{1}{2a^3x^2}$$

[Out] $-1/2/a^3/x^2+3*b/a^4/x+1/2*b^2/a^3/(b*x+a)^2+3*b^2/a^4/(b*x+a)+6*b^2*\ln(x)/a^5-6*b^2*\ln(b*x+a)/a^5$

Rubi [A] time = 0.04, antiderivative size = 76, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{3b^2}{a^4(a+bx)} + \frac{b^2}{2a^3(a+bx)^2} + \frac{6b^2 \log(x)}{a^5} - \frac{6b^2 \log(a+bx)}{a^5} + \frac{3b}{a^4x} - \frac{1}{2a^3x^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(a + b*x)^3), x]

[Out] $-1/(2*a^3*x^2) + (3*b)/(a^4*x) + b^2/(2*a^3*(a + b*x)^2) + (3*b^2)/(a^4*(a + b*x)) + (6*b^2*\text{Log}[x])/a^5 - (6*b^2*\text{Log}[a + b*x])/a^5$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^3(a+bx)^3} dx &= \int \left(\frac{1}{a^3x^3} - \frac{3b}{a^4x^2} + \frac{6b^2}{a^5x} - \frac{b^3}{a^3(a+bx)^3} - \frac{3b^3}{a^4(a+bx)^2} - \frac{6b^3}{a^5(a+bx)} \right) dx \\ &= -\frac{1}{2a^3x^2} + \frac{3b}{a^4x} + \frac{b^2}{2a^3(a+bx)^2} + \frac{3b^2}{a^4(a+bx)} + \frac{6b^2 \log(x)}{a^5} - \frac{6b^2 \log(a+bx)}{a^5} \end{aligned}$$

Mathematica [A] time = 0.05, size = 68, normalized size = 0.89

$$\frac{\frac{a(-a^3+4a^2bx+18ab^2x^2+12b^3x^3)}{x^2(a+bx)^2} - 12b^2 \log(a+bx) + 12b^2 \log(x)}{2a^5}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)^3),x]

[Out] ((a*(-a^3 + 4*a^2*b*x + 18*a*b^2*x^2 + 12*b^3*x^3))/(x^2*(a + b*x)^2) + 12*b^2*Log[x] - 12*b^2*Log[a + b*x])/(2*a^5)

fricas [A] time = 0.54, size = 130, normalized size = 1.71

$$\frac{12 ab^3 x^3 + 18 a^2 b^2 x^2 + 4 a^3 b x - a^4 - 12 (b^4 x^4 + 2 ab^3 x^3 + a^2 b^2 x^2) \log(bx + a) + 12 (b^4 x^4 + 2 ab^3 x^3 + a^2 b^2 x^2) \log(x)}{2 (a^5 b^2 x^4 + 2 a^6 b x^3 + a^7 x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^3,x, algorithm="fricas")

[Out] 1/2*(12*a*b^3*x^3 + 18*a^2*b^2*x^2 + 4*a^3*b*x - a^4 - 12*(b^4*x^4 + 2*a*b^3*x^3 + a^2*b^2*x^2)*log(b*x + a) + 12*(b^4*x^4 + 2*a*b^3*x^3 + a^2*b^2*x^2)*log(x))/(a^5*b^2*x^4 + 2*a^6*b*x^3 + a^7*x^2)

giac [A] time = 1.39, size = 73, normalized size = 0.96

$$-\frac{6b^2 \log(|bx + a|)}{a^5} + \frac{6b^2 \log(|x|)}{a^5} + \frac{12b^3x^3 + 18ab^2x^2 + 4a^2bx - a^3}{2(bx^2 + ax)^2 a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^3,x, algorithm="giac")

[Out] -6*b^2*log(abs(b*x + a))/a^5 + 6*b^2*log(abs(x))/a^5 + 1/2*(12*b^3*x^3 + 18*a*b^2*x^2 + 4*a^2*b*x - a^3)/((b*x^2 + a*x)^2*a^4)

maple [A] time = 0.01, size = 73, normalized size = 0.96

$$\frac{b^2}{2(bx + a)^2 a^3} + \frac{3b^2}{(bx + a)a^4} + \frac{6b^2 \ln(x)}{a^5} - \frac{6b^2 \ln(bx + a)}{a^5} + \frac{3b}{a^4 x} - \frac{1}{2a^3 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a)^3,x)

[Out] -1/2/a^3/x^2+3*b/a^4/x+1/2*b^2/a^3/(b*x+a)^2+3*b^2/a^4/(b*x+a)+6*b^2*ln(x)/a^5-6*b^2*ln(b*x+a)/a^5

maxima [A] time = 1.37, size = 86, normalized size = 1.13

$$\frac{12 b^3 x^3 + 18 a b^2 x^2 + 4 a^2 b x - a^3}{2 (a^4 b^2 x^4 + 2 a^5 b x^3 + a^6 x^2)} - \frac{6 b^2 \log(bx + a)}{a^5} + \frac{6 b^2 \log(x)}{a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^3,x, algorithm="maxima")

[Out] $\frac{1}{2} \cdot (12 \cdot b^3 \cdot x^3 + 18 \cdot a \cdot b^2 \cdot x^2 + 4 \cdot a^2 \cdot b \cdot x - a^3) / (a^4 \cdot b^2 \cdot x^4 + 2 \cdot a^5 \cdot b \cdot x^3 + a^6 \cdot x^2) - 6 \cdot b^2 \cdot \log(b \cdot x + a) / a^5 + 6 \cdot b^2 \cdot \log(x) / a^5$

mupad [B] time = 0.12, size = 79, normalized size = 1.04

$$\frac{\frac{9b^2x^2}{a^3} - \frac{1}{2a} + \frac{6b^3x^3}{a^4} + \frac{2bx}{a^2}}{a^2x^2 + 2abx^3 + b^2x^4} - \frac{12b^2 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(a + b*x)^3),x)

[Out] $\left(\frac{9 \cdot b^2 \cdot x^2}{a^3} - \frac{1}{2 \cdot a} + \frac{6 \cdot b^3 \cdot x^3}{a^4} + \frac{2 \cdot b \cdot x}{a^2}\right) / (a^2 \cdot x^2 + b^2 \cdot x^4 + 2 \cdot a \cdot b \cdot x^3) - \frac{12 \cdot b^2 \cdot \operatorname{atanh}\left(\frac{2 \cdot b \cdot x}{a} + 1\right)}{a^5}$

sympy [A] time = 0.41, size = 78, normalized size = 1.03

$$\frac{-a^3 + 4a^2bx + 18ab^2x^2 + 12b^3x^3}{2a^6x^2 + 4a^5bx^3 + 2a^4b^2x^4} + \frac{6b^2 \left(\log(x) - \log\left(\frac{a}{b} + x\right)\right)}{a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(b*x+a)**3,x)

[Out] $(-a^{**3} + 4 \cdot a^{**2} \cdot b \cdot x + 18 \cdot a \cdot b^{**2} \cdot x^{**2} + 12 \cdot b^{**3} \cdot x^{**3}) / (2 \cdot a^{**6} \cdot x^{**2} + 4 \cdot a^{**5} \cdot b \cdot x^{**3} + 2 \cdot a^{**4} \cdot b^{**2} \cdot x^{**4}) + 6 \cdot b^{**2} \cdot (\log(x) - \log(a/b + x)) / a^{**5}$

$$3.191 \quad \int \frac{1}{x^4(a+bx)^3} dx$$

Optimal. Leaf size=89

$$-\frac{10b^3 \log(x)}{a^6} + \frac{10b^3 \log(a+bx)}{a^6} - \frac{4b^3}{a^5(a+bx)} - \frac{6b^2}{a^5x} - \frac{b^3}{2a^4(a+bx)^2} + \frac{3b}{2a^4x^2} - \frac{1}{3a^3x^3}$$

[Out] $-1/3/a^3/x^3+3/2*b/a^4/x^2-6*b^2/a^5/x-1/2*b^3/a^4/(b*x+a)^2-4*b^3/a^5/(b*x+a)-10*b^3*\ln(x)/a^6+10*b^3*\ln(b*x+a)/a^6$

Rubi [A] time = 0.05, antiderivative size = 89, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{4b^3}{a^5(a+bx)} - \frac{b^3}{2a^4(a+bx)^2} - \frac{6b^2}{a^5x} - \frac{10b^3 \log(x)}{a^6} + \frac{10b^3 \log(a+bx)}{a^6} + \frac{3b}{2a^4x^2} - \frac{1}{3a^3x^3}$$

Antiderivative was successfully verified.

[In] Int[1/(x^4*(a + b*x)^3), x]

[Out] $-1/(3*a^3*x^3) + (3*b)/(2*a^4*x^2) - (6*b^2)/(a^5*x) - b^3/(2*a^4*(a + b*x)^2) - (4*b^3)/(a^5*(a + b*x)) - (10*b^3*\text{Log}[x])/a^6 + (10*b^3*\text{Log}[a + b*x])/a^6$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^4(a+bx)^3} dx &= \int \left(\frac{1}{a^3x^4} - \frac{3b}{a^4x^3} + \frac{6b^2}{a^5x^2} - \frac{10b^3}{a^6x} + \frac{b^4}{a^4(a+bx)^3} + \frac{4b^4}{a^5(a+bx)^2} + \frac{10b^4}{a^6(a+bx)} \right) dx \\ &= -\frac{1}{3a^3x^3} + \frac{3b}{2a^4x^2} - \frac{6b^2}{a^5x} - \frac{b^3}{2a^4(a+bx)^2} - \frac{4b^3}{a^5(a+bx)} - \frac{10b^3 \log(x)}{a^6} + \frac{10b^3 \log(a+bx)}{a^6} \end{aligned}$$

Mathematica [A] time = 0.07, size = 79, normalized size = 0.89

$$\frac{a(2a^4-5a^3bx+20a^2b^2x^2+90ab^3x^3+60b^4x^4)}{x^3(a+bx)^2} - 60b^3 \log(a+bx) + 60b^3 \log(x)$$

$$6a^6$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^4*(a + b*x)^3),x]

[Out]
$$-1/6*((a*(2*a^4 - 5*a^3*b*x + 20*a^2*b^2*x^2 + 90*a*b^3*x^3 + 60*b^4*x^4))/(x^3*(a + b*x)^2) + 60*b^3*\text{Log}[x] - 60*b^3*\text{Log}[a + b*x])/a^6$$

fricas [A] time = 0.51, size = 141, normalized size = 1.58

$$\frac{60 ab^4 x^4 + 90 a^2 b^3 x^3 + 20 a^3 b^2 x^2 - 5 a^4 b x + 2 a^5 - 60 (b^5 x^5 + 2 a b^4 x^4 + a^2 b^3 x^3) \log(bx + a) + 60 (b^5 x^5 + 2 a b^4 x^4 + a^2 b^3 x^3) \log(x)}{6 (a^6 b^2 x^5 + 2 a^7 b x^4 + a^8 x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^3,x, algorithm="fricas")

[Out]
$$-1/6*(60*a*b^4*x^4 + 90*a^2*b^3*x^3 + 20*a^3*b^2*x^2 - 5*a^4*b*x + 2*a^5 - 60*(b^5*x^5 + 2*a*b^4*x^4 + a^2*b^3*x^3)*\log(b*x + a) + 60*(b^5*x^5 + 2*a*b^4*x^4 + a^2*b^3*x^3)*\log(x))/(a^6*b^2*x^5 + 2*a^7*b*x^4 + a^8*x^3)$$

giac [A] time = 0.94, size = 86, normalized size = 0.97

$$\frac{10 b^3 \log(|bx + a|)}{a^6} - \frac{10 b^3 \log(|x|)}{a^6} - \frac{60 ab^4 x^4 + 90 a^2 b^3 x^3 + 20 a^3 b^2 x^2 - 5 a^4 b x + 2 a^5}{6 (bx + a)^2 a^6 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^3,x, algorithm="giac")

[Out]
$$10*b^3*\log(\text{abs}(b*x + a))/a^6 - 10*b^3*\log(\text{abs}(x))/a^6 - 1/6*(60*a*b^4*x^4 + 90*a^2*b^3*x^3 + 20*a^3*b^2*x^2 - 5*a^4*b*x + 2*a^5)/((b*x + a)^2*a^6*x^3)$$

maple [A] time = 0.01, size = 84, normalized size = 0.94

$$-\frac{b^3}{2 (bx + a)^2 a^4} - \frac{4b^3}{(bx + a) a^5} - \frac{10b^3 \ln(x)}{a^6} + \frac{10b^3 \ln(bx + a)}{a^6} - \frac{6b^2}{a^5 x} + \frac{3b}{2a^4 x^2} - \frac{1}{3a^3 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^4/(b*x+a)^3,x)

[Out]
$$-1/3/a^3/x^3 + 3/2*b/a^4/x^2 - 6*b^2/a^5/x - 1/2*b^3/a^4/(b*x+a)^2 - 4*b^3/a^5/(b*x+a) - 10*b^3*\ln(x)/a^6 + 10*b^3*\ln(b*x+a)/a^6$$

maxima [A] time = 1.46, size = 97, normalized size = 1.09

$$-\frac{60 b^4 x^4 + 90 ab^3 x^3 + 20 a^2 b^2 x^2 - 5 a^3 b x + 2 a^4}{6 (a^5 b^2 x^5 + 2 a^6 b x^4 + a^7 x^3)} + \frac{10 b^3 \log(bx + a)}{a^6} - \frac{10 b^3 \log(x)}{a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^3,x, algorithm="maxima")

[Out] $-1/6*(60*b^4*x^4 + 90*a*b^3*x^3 + 20*a^2*b^2*x^2 - 5*a^3*b*x + 2*a^4)/(a^5*b^2*x^5 + 2*a^6*b*x^4 + a^7*x^3) + 10*b^3*\log(b*x + a)/a^6 - 10*b^3*\log(x)/a^6$

mupad [B] time = 0.13, size = 91, normalized size = 1.02

$$\frac{20b^3 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^6} - \frac{\frac{1}{3a} + \frac{10b^2x^2}{3a^3} + \frac{15b^3x^3}{a^4} + \frac{10b^4x^4}{a^5} - \frac{5bx}{6a^2}}{a^2x^3 + 2abx^4 + b^2x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^4*(a + b*x)^3),x)

[Out] $(20*b^3*\operatorname{atanh}((2*b*x)/a + 1))/a^6 - (1/(3*a) + (10*b^2*x^2)/(3*a^3) + (15*b^3*x^3)/a^4 + (10*b^4*x^4)/a^5 - (5*b*x)/(6*a^2))/(a^2*x^3 + b^2*x^5 + 2*a*b*x^4)$

sympy [A] time = 0.48, size = 92, normalized size = 1.03

$$\frac{-2a^4 + 5a^3bx - 20a^2b^2x^2 - 90ab^3x^3 - 60b^4x^4}{6a^7x^3 + 12a^6bx^4 + 6a^5b^2x^5} + \frac{10b^3(-\log(x) + \log\left(\frac{a}{b} + x\right))}{a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**4/(b*x+a)**3,x)

[Out] $(-2*a**4 + 5*a**3*b*x - 20*a**2*b**2*x**2 - 90*a*b**3*x**3 - 60*b**4*x**4)/(6*a**7*x**3 + 12*a**6*b*x**4 + 6*a**5*b**2*x**5) + 10*b**3*(-\log(x) + \log(a/b + x))/a**6$

$$3.192 \quad \int \frac{1}{x^5(a+bx)^3} dx$$

Optimal. Leaf size=97

$$\frac{15b^4 \log(x)}{a^7} - \frac{15b^4 \log(a+bx)}{a^7} + \frac{5b^4}{a^6(a+bx)} + \frac{10b^3}{a^6x} + \frac{b^4}{2a^5(a+bx)^2} - \frac{3b^2}{a^5x^2} + \frac{b}{a^4x^3} - \frac{1}{4a^3x^4}$$

[Out] $-1/4/a^3/x^4+b/a^4/x^3-3*b^2/a^5/x^2+10*b^3/a^6/x+1/2*b^4/a^5/(b*x+a)^2+5*b^4/a^6/(b*x+a)+15*b^4*\ln(x)/a^7-15*b^4*\ln(b*x+a)/a^7$

Rubi [A] time = 0.05, antiderivative size = 97, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{3b^2}{a^5x^2} + \frac{5b^4}{a^6(a+bx)} + \frac{b^4}{2a^5(a+bx)^2} + \frac{10b^3}{a^6x} + \frac{15b^4 \log(x)}{a^7} - \frac{15b^4 \log(a+bx)}{a^7} + \frac{b}{a^4x^3} - \frac{1}{4a^3x^4}$$

Antiderivative was successfully verified.

[In] Int[1/(x^5*(a + b*x)^3), x]

[Out] $-1/(4*a^3*x^4) + b/(a^4*x^3) - (3*b^2)/(a^5*x^2) + (10*b^3)/(a^6*x) + b^4/(2*a^5*(a + b*x)^2) + (5*b^4)/(a^6*(a + b*x)) + (15*b^4*\text{Log}[x])/a^7 - (15*b^4*\text{Log}[a + b*x])/a^7$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^5(a+bx)^3} dx &= \int \left(\frac{1}{a^3x^5} - \frac{3b}{a^4x^4} + \frac{6b^2}{a^5x^3} - \frac{10b^3}{a^6x^2} + \frac{15b^4}{a^7x} - \frac{b^5}{a^5(a+bx)^3} - \frac{5b^5}{a^6(a+bx)^2} - \frac{15b^5}{a^7(a+bx)} \right) dx \\ &= -\frac{1}{4a^3x^4} + \frac{b}{a^4x^3} - \frac{3b^2}{a^5x^2} + \frac{10b^3}{a^6x} + \frac{b^4}{2a^5(a+bx)^2} + \frac{5b^4}{a^6(a+bx)} + \frac{15b^4 \log(x)}{a^7} - \frac{15b^4 \log(a+bx)}{a^7} \end{aligned}$$

Mathematica [A] time = 0.06, size = 90, normalized size = 0.93

$$\frac{a(-a^5+2a^4bx-5a^3b^2x^2+20a^2b^3x^3+90ab^4x^4+60b^5x^5)}{x^4(a+bx)^2} - \frac{60b^4 \log(a+bx) + 60b^4 \log(x)}{4a^7}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^5*(a + b*x)^3), x]

[Out] ((a*(-a^5 + 2*a^4*b*x - 5*a^3*b^2*x^2 + 20*a^2*b^3*x^3 + 90*a*b^4*x^4 + 60*b^5*x^5))/(x^4*(a + b*x)^2) + 60*b^4*Log[x] - 60*b^4*Log[a + b*x])/(4*a^7)

fricas [A] time = 0.50, size = 152, normalized size = 1.57

$$\frac{60 ab^5 x^5 + 90 a^2 b^4 x^4 + 20 a^3 b^3 x^3 - 5 a^4 b^2 x^2 + 2 a^5 b x - a^6 - 60 (b^6 x^6 + 2 a b^5 x^5 + a^2 b^4 x^4) \log(bx + a) + 60 (b^6 x^6 + 2 a^7 b^2 x^6 + 2 a^8 b x^5 + a^9 x^4)}{4 (a^7 b^2 x^6 + 2 a^8 b x^5 + a^9 x^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a)^3,x, algorithm="fricas")

[Out] 1/4*(60*a*b^5*x^5 + 90*a^2*b^4*x^4 + 20*a^3*b^3*x^3 - 5*a^4*b^2*x^2 + 2*a^5*b*x - a^6 - 60*(b^6*x^6 + 2*a*b^5*x^5 + a^2*b^4*x^4)*log(b*x + a) + 60*(b^6*x^6 + 2*a*b^5*x^5 + a^2*b^4*x^4)*log(x))/(a^7*b^2*x^6 + 2*a^8*b*x^5 + a^9*x^4)

giac [A] time = 1.01, size = 97, normalized size = 1.00

$$-\frac{15 b^4 \log(|bx + a|)}{a^7} + \frac{15 b^4 \log(|x|)}{a^7} + \frac{60 ab^5 x^5 + 90 a^2 b^4 x^4 + 20 a^3 b^3 x^3 - 5 a^4 b^2 x^2 + 2 a^5 b x - a^6}{4 (bx + a)^2 a^7 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a)^3,x, algorithm="giac")

[Out] -15*b^4*log(abs(b*x + a))/a^7 + 15*b^4*log(abs(x))/a^7 + 1/4*(60*a*b^5*x^5 + 90*a^2*b^4*x^4 + 20*a^3*b^3*x^3 - 5*a^4*b^2*x^2 + 2*a^5*b*x - a^6)/((b*x + a)^2*a^7*x^4)

maple [A] time = 0.01, size = 94, normalized size = 0.97

$$\frac{b^4}{2 (bx + a)^2 a^5} + \frac{5b^4}{(bx + a) a^6} + \frac{15b^4 \ln(x)}{a^7} - \frac{15b^4 \ln(bx + a)}{a^7} + \frac{10b^3}{a^6 x} - \frac{3b^2}{a^5 x^2} + \frac{b}{a^4 x^3} - \frac{1}{4a^3 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^5/(b*x+a)^3,x)

[Out] -1/4/a^3/x^4+b/a^4/x^3-3*b^2/a^5/x^2+10*b^3/a^6/x+1/2*b^4/a^5/(b*x+a)^2+5*b^4/a^6/(b*x+a)+15*b^4*ln(x)/a^7-15*b^4*ln(b*x+a)/a^7

maxima [A] time = 1.35, size = 108, normalized size = 1.11

$$\frac{60 b^5 x^5 + 90 a b^4 x^4 + 20 a^2 b^3 x^3 - 5 a^3 b^2 x^2 + 2 a^4 b x - a^5}{4 (a^6 b^2 x^6 + 2 a^7 b x^5 + a^8 x^4)} - \frac{15 b^4 \log(bx + a)}{a^7} + \frac{15 b^4 \log(x)}{a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a)^3,x, algorithm="maxima")

[Out] 1/4*(60*b^5*x^5 + 90*a*b^4*x^4 + 20*a^2*b^3*x^3 - 5*a^3*b^2*x^2 + 2*a^4*b*x - a^5)/(a^6*b^2*x^6 + 2*a^7*b*x^5 + a^8*x^4) - 15*b^4*log(b*x + a)/a^7 + 15*b^4*log(x)/a^7

mupad [B] time = 0.09, size = 101, normalized size = 1.04

$$\frac{\frac{5 b^3 x^3}{a^4} - \frac{5 b^2 x^2}{4 a^3} - \frac{1}{4 a} + \frac{45 b^4 x^4}{2 a^5} + \frac{15 b^5 x^5}{a^6} + \frac{b x}{2 a^2}}{a^2 x^4 + 2 a b x^5 + b^2 x^6} - \frac{30 b^4 \operatorname{atanh}\left(\frac{2 b x}{a} + 1\right)}{a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^5*(a + b*x)^3),x)

[Out] ((5*b^3*x^3)/a^4 - (5*b^2*x^2)/(4*a^3) - 1/(4*a) + (45*b^4*x^4)/(2*a^5) + (15*b^5*x^5)/a^6 + (b*x)/(2*a^2))/(a^2*x^4 + b^2*x^6 + 2*a*b*x^5) - (30*b^4*atanh((2*b*x)/a + 1))/a^7

sympy [A] time = 0.48, size = 102, normalized size = 1.05

$$\frac{-a^5 + 2a^4bx - 5a^3b^2x^2 + 20a^2b^3x^3 + 90ab^4x^4 + 60b^5x^5}{4a^8x^4 + 8a^7bx^5 + 4a^6b^2x^6} + \frac{15b^4 (\log(x) - \log\left(\frac{a}{b} + x\right))}{a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**5/(b*x+a)**3,x)

[Out] (-a**5 + 2*a**4*b*x - 5*a**3*b**2*x**2 + 20*a**2*b**3*x**3 + 90*a*b**4*x**4 + 60*b**5*x**5)/(4*a**8*x**4 + 8*a**7*b*x**5 + 4*a**6*b**2*x**6) + 15*b**4*(log(x) - log(a/b + x))/a**7

$$3.193 \quad \int \frac{x^8}{(a+bx)^4} dx$$

Optimal. Leaf size=114

$$-\frac{a^8}{3b^9(a+bx)^3} + \frac{4a^7}{b^9(a+bx)^2} - \frac{28a^6}{b^9(a+bx)} - \frac{56a^5 \log(a+bx)}{b^9} + \frac{35a^4x}{b^8} - \frac{10a^3x^2}{b^7} + \frac{10a^2x^3}{3b^6} - \frac{ax^4}{b^5} + \frac{x^5}{5b^4}$$

[Out] $35*a^4*x/b^8 - 10*a^3*x^2/b^7 + 10/3*a^2*x^3/b^6 - a*x^4/b^5 + 1/5*x^5/b^4 - 1/3*a^8/b^9/(b*x+a)^3 + 4*a^7/b^9/(b*x+a)^2 - 28*a^6/b^9/(b*x+a) - 56*a^5*ln(b*x+a)/b^9$

Rubi [A] time = 0.09, antiderivative size = 114, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{10a^3x^2}{b^7} + \frac{10a^2x^3}{3b^6} - \frac{a^8}{3b^9(a+bx)^3} + \frac{4a^7}{b^9(a+bx)^2} - \frac{28a^6}{b^9(a+bx)} + \frac{35a^4x}{b^8} - \frac{56a^5 \log(a+bx)}{b^9} - \frac{ax^4}{b^5} + \frac{x^5}{5b^4}$$

Antiderivative was successfully verified.

[In] Int[x^8/(a + b*x)^4, x]

[Out] $(35*a^4*x)/b^8 - (10*a^3*x^2)/b^7 + (10*a^2*x^3)/(3*b^6) - (a*x^4)/b^5 + x^5/(5*b^4) - a^8/(3*b^9*(a + b*x)^3) + (4*a^7)/(b^9*(a + b*x)^2) - (28*a^6)/(b^9*(a + b*x)) - (56*a^5*Log[a + b*x])/b^9$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^8}{(a+bx)^4} dx &= \int \left(\frac{35a^4}{b^8} - \frac{20a^3x}{b^7} + \frac{10a^2x^2}{b^6} - \frac{4ax^3}{b^5} + \frac{x^4}{b^4} + \frac{a^8}{b^8(a+bx)^4} - \frac{8a^7}{b^8(a+bx)^3} + \frac{28a^6}{b^8(a+bx)^2} - \frac{56a^5 \log(a+bx)}{b^8(a+bx)} \right) dx \\ &= \frac{35a^4x}{b^8} - \frac{10a^3x^2}{b^7} + \frac{10a^2x^3}{3b^6} - \frac{ax^4}{b^5} + \frac{x^5}{5b^4} - \frac{a^8}{3b^9(a+bx)^3} + \frac{4a^7}{b^9(a+bx)^2} - \frac{28a^6}{b^9(a+bx)} - \frac{56a^5 \log(a+bx)}{b^9} \end{aligned}$$

Mathematica [A] time = 0.04, size = 101, normalized size = 0.89

$$-\frac{5a^8}{(a+bx)^3} + \frac{60a^7}{(a+bx)^2} - \frac{420a^6}{a+bx} - \frac{840a^5 \log(a+bx) + 525a^4bx - 150a^3b^2x^2 + 50a^2b^3x^3 - 15ab^4x^4 + 3b^5x^5}{15b^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^8/(a + b*x)^4,x]

[Out] (525*a^4*b*x - 150*a^3*b^2*x^2 + 50*a^2*b^3*x^3 - 15*a*b^4*x^4 + 3*b^5*x^5 - (5*a^8)/(a + b*x)^3 + (60*a^7)/(a + b*x)^2 - (420*a^6)/(a + b*x) - 840*a^5*Log[a + b*x])/(15*b^9)

fricas [A] time = 0.58, size = 162, normalized size = 1.42

$$\frac{3b^8x^8 - 6ab^7x^7 + 14a^2b^6x^6 - 42a^3b^5x^5 + 210a^4b^4x^4 + 1175a^5b^3x^3 + 1005a^6b^2x^2 - 255a^7bx - 365a^8 - 840(a^5b^3x^3 + 3a^6b^2x^2 + 3a^7bx + a^8)\log(bx + a)}{15(b^{12}x^3 + 3ab^{11}x^2 + 3a^2b^{10}x + a^3b^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8/(b*x+a)^4,x, algorithm="fricas")

[Out] 1/15*(3*b^8*x^8 - 6*a*b^7*x^7 + 14*a^2*b^6*x^6 - 42*a^3*b^5*x^5 + 210*a^4*b^4*x^4 + 1175*a^5*b^3*x^3 + 1005*a^6*b^2*x^2 - 255*a^7*b*x - 365*a^8 - 840*(a^5*b^3*x^3 + 3*a^6*b^2*x^2 + 3*a^7*b*x + a^8)*log(b*x + a))/(b^12*x^3 + 3*a*b^11*x^2 + 3*a^2*b^10*x + a^3*b^9)

giac [A] time = 1.11, size = 106, normalized size = 0.93

$$\frac{56a^5 \log(|bx + a|)}{b^9} - \frac{84a^6b^2x^2 + 156a^7bx + 73a^8}{3(bx + a)^3b^9} + \frac{3b^{16}x^5 - 15ab^{15}x^4 + 50a^2b^{14}x^3 - 150a^3b^{13}x^2 + 525a^4b^{12}x - 156a^5}{15b^{20}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8/(b*x+a)^4,x, algorithm="giac")

[Out] -56*a^5*log(abs(b*x + a))/b^9 - 1/3*(84*a^6*b^2*x^2 + 156*a^7*b*x + 73*a^8)/((b*x + a)^3*b^9) + 1/15*(3*b^16*x^5 - 15*a*b^15*x^4 + 50*a^2*b^14*x^3 - 150*a^3*b^13*x^2 + 525*a^4*b^12*x)/b^20

maple [A] time = 0.01, size = 109, normalized size = 0.96

$$\frac{x^5}{5b^4} - \frac{ax^4}{b^5} - \frac{a^8}{3(bx + a)^3b^9} + \frac{10a^2x^3}{3b^6} + \frac{4a^7}{(bx + a)^2b^9} - \frac{10a^3x^2}{b^7} - \frac{28a^6}{(bx + a)b^9} - \frac{56a^5 \ln(bx + a)}{b^9} + \frac{35a^4x}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^8/(b*x+a)^4,x)

[Out] 35*a^4*x/b^8 - 10*a^3*x^2/b^7 + 10/3*a^2*x^3/b^6 - a*x^4/b^5 + 1/5*x^5/b^4 - 1/3*a^8/b^9/(b*x+a)^3 + 4*a^7/b^9/(b*x+a)^2 - 28*a^6/b^9/(b*x+a) - 56*a^5*ln(b*x+a)/b^9

maxima [A] time = 1.44, size = 125, normalized size = 1.10

$$\frac{84 a^6 b^2 x^2 + 156 a^7 b x + 73 a^8}{3 (b^{12} x^3 + 3 a b^{11} x^2 + 3 a^2 b^{10} x + a^3 b^9)} - \frac{56 a^5 \log(bx + a)}{b^9} + \frac{3 b^4 x^5 - 15 a b^3 x^4 + 50 a^2 b^2 x^3 - 150 a^3 b x^2 + 525 a^4 x - 56 a^5}{15 b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8/(b*x+a)^4,x, algorithm="maxima")

[Out] -1/3*(84*a^6*b^2*x^2 + 156*a^7*b*x + 73*a^8)/(b^12*x^3 + 3*a*b^11*x^2 + 3*a^2*b^10*x + a^3*b^9) - 56*a^5*log(b*x + a)/b^9 + 1/15*(3*b^4*x^5 - 15*a*b^3*x^4 + 50*a^2*b^2*x^3 - 150*a^3*b*x^2 + 525*a^4*x)/b^8

mupad [B] time = 0.37, size = 103, normalized size = 0.90

$$\frac{2 a (a + b x)^4 - \frac{(a + b x)^5}{5} - \frac{28 a^2 (a + b x)^3}{3} + 28 a^3 (a + b x)^2 + \frac{28 a^6}{a + b x} - \frac{4 a^7}{(a + b x)^2} + \frac{a^8}{3 (a + b x)^3} + 56 a^5 \ln(a + b x) - 70 a^4 b x}{b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^8/(a + b*x)^4,x)

[Out] -(2*a*(a + b*x)^4 - (a + b*x)^5/5 - (28*a^2*(a + b*x)^3)/3 + 28*a^3*(a + b*x)^2 + (28*a^6)/(a + b*x) - (4*a^7)/(a + b*x)^2 + a^8/(3*(a + b*x)^3) + 56*a^5*log(a + b*x) - 70*a^4*b*x)/b^9

sympy [A] time = 0.52, size = 131, normalized size = 1.15

$$-\frac{56 a^5 \log(a + b x)}{b^9} + \frac{35 a^4 x}{b^8} - \frac{10 a^3 x^2}{b^7} + \frac{10 a^2 x^3}{3 b^6} - \frac{a x^4}{b^5} + \frac{-73 a^8 - 156 a^7 b x - 84 a^6 b^2 x^2}{3 a^3 b^9 + 9 a^2 b^{10} x + 9 a b^{11} x^2 + 3 b^{12} x^3} + \frac{x^5}{5 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**8/(b*x+a)**4,x)

[Out] -56*a**5*log(a + b*x)/b**9 + 35*a**4*x/b**8 - 10*a**3*x**2/b**7 + 10*a**2*x**3/(3*b**6) - a*x**4/b**5 + (-73*a**8 - 156*a**7*b*x - 84*a**6*b**2*x**2)/(3*a**3*b**9 + 9*a**2*b**10*x + 9*a*b**11*x**2 + 3*b**12*x**3) + x**5/(5*b**4)

$$3.194 \quad \int \frac{x^7}{(a+bx)^4} dx$$

Optimal. Leaf size=105

$$\frac{a^7}{3b^8(a+bx)^3} - \frac{7a^6}{2b^8(a+bx)^2} + \frac{21a^5}{b^8(a+bx)} + \frac{35a^4 \log(a+bx)}{b^8} - \frac{20a^3x}{b^7} + \frac{5a^2x^2}{b^6} - \frac{4ax^3}{3b^5} + \frac{x^4}{4b^4}$$

[Out] $-20*a^3*x/b^7+5*a^2*x^2/b^6-4/3*a*x^3/b^5+1/4*x^4/b^4+1/3*a^7/b^8/(b*x+a)^3-7/2*a^6/b^8/(b*x+a)^2+21*a^5/b^8/(b*x+a)+35*a^4*\ln(b*x+a)/b^8$

Rubi [A] time = 0.07, antiderivative size = 105, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{5a^2x^2}{b^6} + \frac{a^7}{3b^8(a+bx)^3} - \frac{7a^6}{2b^8(a+bx)^2} + \frac{21a^5}{b^8(a+bx)} - \frac{20a^3x}{b^7} + \frac{35a^4 \log(a+bx)}{b^8} - \frac{4ax^3}{3b^5} + \frac{x^4}{4b^4}$$

Antiderivative was successfully verified.

[In] Int[x^7/(a + b*x)^4, x]

[Out] $(-20*a^3*x)/b^7 + (5*a^2*x^2)/b^6 - (4*a*x^3)/(3*b^5) + x^4/(4*b^4) + a^7/(3*b^8*(a + b*x)^3) - (7*a^6)/(2*b^8*(a + b*x)^2) + (21*a^5)/(b^8*(a + b*x)) + (35*a^4*\text{Log}[a + b*x])/b^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^7}{(a+bx)^4} dx &= \int \left(-\frac{20a^3}{b^7} + \frac{10a^2x}{b^6} - \frac{4ax^2}{b^5} + \frac{x^3}{b^4} - \frac{a^7}{b^7(a+bx)^4} + \frac{7a^6}{b^7(a+bx)^3} - \frac{21a^5}{b^7(a+bx)^2} + \frac{35a^4}{b^7(a+bx)} \right) dx \\ &= -\frac{20a^3x}{b^7} + \frac{5a^2x^2}{b^6} - \frac{4ax^3}{3b^5} + \frac{x^4}{4b^4} + \frac{a^7}{3b^8(a+bx)^3} - \frac{7a^6}{2b^8(a+bx)^2} + \frac{21a^5}{b^8(a+bx)} + \frac{35a^4 \log(a+bx)}{b^8} \end{aligned}$$

Mathematica [A] time = 0.03, size = 90, normalized size = 0.86

$$\frac{4a^7}{(a+bx)^3} - \frac{42a^6}{(a+bx)^2} + \frac{252a^5}{a+bx} + 420a^4 \log(a+bx) - 240a^3bx + 60a^2b^2x^2 - 16ab^3x^3 + 3b^4x^4$$

$$12b^8$$

Antiderivative was successfully verified.

[In] Integrate[x^7/(a + b*x)^4,x]

[Out] $(-240*a^3*b*x + 60*a^2*b^2*x^2 - 16*a*b^3*x^3 + 3*b^4*x^4 + (4*a^7)/(a + b*x)^3 - (42*a^6)/(a + b*x)^2 + (252*a^5)/(a + b*x) + 420*a^4*\text{Log}[a + b*x])/ (12*b^8)$

fricas [A] time = 0.47, size = 151, normalized size = 1.44

$$\frac{3b^7x^7 - 7ab^6x^6 + 21a^2b^5x^5 - 105a^3b^4x^4 - 556a^4b^3x^3 - 408a^5b^2x^2 + 222a^6bx + 214a^7 + 420(a^4b^3x^3 + 3a^5b^2x^2)}{12(b^{11}x^3 + 3ab^{10}x^2 + 3a^2b^9x + a^3b^8)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^4,x, algorithm="fricas")

[Out] $1/12*(3*b^7*x^7 - 7*a*b^6*x^6 + 21*a^2*b^5*x^5 - 105*a^3*b^4*x^4 - 556*a^4*b^3*x^3 - 408*a^5*b^2*x^2 + 222*a^6*b*x + 214*a^7 + 420*(a^4*b^3*x^3 + 3*a^5*b^2*x^2 + 3*a^6*b*x + a^7)*\text{log}(b*x + a))/(b^{11}*x^3 + 3*a*b^{10}*x^2 + 3*a^2*b^9*x + a^3*b^8)$

giac [A] time = 1.01, size = 95, normalized size = 0.90

$$\frac{35a^4 \log(|bx + a|)}{b^8} + \frac{126a^5b^2x^2 + 231a^6bx + 107a^7}{6(bx + a)^3b^8} + \frac{3b^{12}x^4 - 16ab^{11}x^3 + 60a^2b^{10}x^2 - 240a^3b^9x}{12b^{16}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^4,x, algorithm="giac")

[Out] $35*a^4*\text{log}(\text{abs}(b*x + a))/b^8 + 1/6*(126*a^5*b^2*x^2 + 231*a^6*b*x + 107*a^7)/((b*x + a)^3*b^8) + 1/12*(3*b^{12}*x^4 - 16*a*b^{11}*x^3 + 60*a^2*b^{10}*x^2 - 240*a^3*b^9*x)/b^{16}$

maple [A] time = 0.01, size = 98, normalized size = 0.93

$$\frac{x^4}{4b^4} + \frac{a^7}{3(bx + a)^3b^8} - \frac{4ax^3}{3b^5} - \frac{7a^6}{2(bx + a)^2b^8} + \frac{5a^2x^2}{b^6} + \frac{21a^5}{(bx + a)b^8} + \frac{35a^4 \ln(bx + a)}{b^8} - \frac{20a^3x}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7/(b*x+a)^4,x)

[Out] $-20*a^3*x/b^7 + 5*a^2*x^2/b^6 - 4/3*a*x^3/b^5 + 1/4*x^4/b^4 + 1/3*a^7/b^8/(b*x+a)^3 - 7/2*a^6/b^8/(b*x+a)^2 + 21*a^5/b^8/(b*x+a) + 35*a^4*\ln(b*x+a)/b^8$

maxima [A] time = 1.39, size = 114, normalized size = 1.09

$$\frac{126 a^5 b^2 x^2 + 231 a^6 b x + 107 a^7}{6 (b^{11} x^3 + 3 a b^{10} x^2 + 3 a^2 b^9 x + a^3 b^8)} + \frac{35 a^4 \log(bx + a)}{b^8} + \frac{3 b^3 x^4 - 16 a b^2 x^3 + 60 a^2 b x^2 - 240 a^3 x}{12 b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^4,x, algorithm="maxima")

[Out] 1/6*(126*a^5*b^2*x^2 + 231*a^6*b*x + 107*a^7)/(b^11*x^3 + 3*a*b^10*x^2 + 3*a^2*b^9*x + a^3*b^8) + 35*a^4*log(b*x + a)/b^8 + 1/12*(3*b^3*x^4 - 16*a*b^2*x^3 + 60*a^2*b*x^2 - 240*a^3*x)/b^7

mupad [B] time = 0.22, size = 90, normalized size = 0.86

$$\frac{\frac{(a+bx)^4}{4} - \frac{7a(a+bx)^3}{3} + \frac{21a^2(a+bx)^2}{2} + \frac{21a^5}{a+bx} - \frac{7a^6}{2(a+bx)^2} + \frac{a^7}{3(a+bx)^3} + 35a^4 \ln(a+bx) - 35a^3bx}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7/(a + b*x)^4,x)

[Out] ((a + b*x)^4/4 - (7*a*(a + b*x)^3)/3 + (21*a^2*(a + b*x)^2)/2 + (21*a^5)/(a + b*x) - (7*a^6)/(2*(a + b*x)^2) + a^7/(3*(a + b*x)^3) + 35*a^4*log(a + b*x) - 35*a^3*b*x)/b^8

sympy [A] time = 0.48, size = 119, normalized size = 1.13

$$\frac{35a^4 \log(a + bx)}{b^8} - \frac{20a^3x}{b^7} + \frac{5a^2x^2}{b^6} - \frac{4ax^3}{3b^5} + \frac{107a^7 + 231a^6bx + 126a^5b^2x^2}{6a^3b^8 + 18a^2b^9x + 18ab^{10}x^2 + 6b^{11}x^3} + \frac{x^4}{4b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**7/(b*x+a)**4,x)

[Out] 35*a**4*log(a + b*x)/b**8 - 20*a**3*x/b**7 + 5*a**2*x**2/b**6 - 4*a*x**3/(3*b**5) + (107*a**7 + 231*a**6*b*x + 126*a**5*b**2*x**2)/(6*a**3*b**8 + 18*a**2*b**9*x + 18*a*b**10*x**2 + 6*b**11*x**3) + x**4/(4*b**4)

$$3.195 \quad \int \frac{x^6}{(a+bx)^4} dx$$

Optimal. Leaf size=90

$$-\frac{a^6}{3b^7(a+bx)^3} + \frac{3a^5}{b^7(a+bx)^2} - \frac{15a^4}{b^7(a+bx)} - \frac{20a^3 \log(a+bx)}{b^7} + \frac{10a^2x}{b^6} - \frac{2ax^2}{b^5} + \frac{x^3}{3b^4}$$

[Out] $10*a^2*x/b^6 - 2*a*x^2/b^5 + 1/3*x^3/b^4 - 1/3*a^6/b^7/(b*x+a)^3 + 3*a^5/b^7/(b*x+a)^2 - 15*a^4/b^7/(b*x+a) - 20*a^3*\ln(b*x+a)/b^7$

Rubi [A] time = 0.06, antiderivative size = 90, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^6}{3b^7(a+bx)^3} + \frac{3a^5}{b^7(a+bx)^2} - \frac{15a^4}{b^7(a+bx)} + \frac{10a^2x}{b^6} - \frac{20a^3 \log(a+bx)}{b^7} - \frac{2ax^2}{b^5} + \frac{x^3}{3b^4}$$

Antiderivative was successfully verified.

[In] Int[x^6/(a + b*x)^4, x]

[Out] $(10*a^2*x)/b^6 - (2*a*x^2)/b^5 + x^3/(3*b^4) - a^6/(3*b^7*(a + b*x)^3) + (3*a^5)/(b^7*(a + b*x)^2) - (15*a^4)/(b^7*(a + b*x)) - (20*a^3*\text{Log}[a + b*x])/b^7$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^6}{(a+bx)^4} dx &= \int \left(\frac{10a^2}{b^6} - \frac{4ax}{b^5} + \frac{x^2}{b^4} + \frac{a^6}{b^6(a+bx)^4} - \frac{6a^5}{b^6(a+bx)^3} + \frac{15a^4}{b^6(a+bx)^2} - \frac{20a^3}{b^6(a+bx)} \right) dx \\ &= \frac{10a^2x}{b^6} - \frac{2ax^2}{b^5} + \frac{x^3}{3b^4} - \frac{a^6}{3b^7(a+bx)^3} + \frac{3a^5}{b^7(a+bx)^2} - \frac{15a^4}{b^7(a+bx)} - \frac{20a^3 \log(a+bx)}{b^7} \end{aligned}$$

Mathematica [A] time = 0.02, size = 90, normalized size = 1.00

$$-\frac{a^6}{3b^7(a+bx)^3} + \frac{3a^5}{b^7(a+bx)^2} - \frac{15a^4}{b^7(a+bx)} - \frac{20a^3 \log(a+bx)}{b^7} + \frac{10a^2x}{b^6} - \frac{2ax^2}{b^5} + \frac{x^3}{3b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^6/(a + b*x)^4,x]

[Out] $(10*a^2*x)/b^6 - (2*a*x^2)/b^5 + x^3/(3*b^4) - a^6/(3*b^7*(a + b*x)^3) + (3*a^5)/(b^7*(a + b*x)^2) - (15*a^4)/(b^7*(a + b*x)) - (20*a^3*\text{Log}[a + b*x])/b^7$

fricas [A] time = 0.43, size = 139, normalized size = 1.54

$$\frac{b^6x^6 - 3ab^5x^5 + 15a^2b^4x^4 + 73a^3b^3x^3 + 39a^4b^2x^2 - 51a^5bx - 37a^6 - 60(a^3b^3x^3 + 3a^4b^2x^2 + 3a^5bx + a^6)\log(bx + a)}{3(b^{10}x^3 + 3ab^9x^2 + 3a^2b^8x + a^3b^7)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^4,x, algorithm="fricas")

[Out] $1/3*(b^6*x^6 - 3*a*b^5*x^5 + 15*a^2*b^4*x^4 + 73*a^3*b^3*x^3 + 39*a^4*b^2*x^2 - 51*a^5*b*x - 37*a^6 - 60*(a^3*b^3*x^3 + 3*a^4*b^2*x^2 + 3*a^5*b*x + a^6)*\log(b*x + a))/(b^{10}*x^3 + 3*a*b^9*x^2 + 3*a^2*b^8*x + a^3*b^7)$

giac [A] time = 1.11, size = 83, normalized size = 0.92

$$-\frac{20a^3\log(|bx+a|)}{b^7} - \frac{45a^4b^2x^2 + 81a^5bx + 37a^6}{3(bx+a)^3b^7} + \frac{b^8x^3 - 6ab^7x^2 + 30a^2b^6x}{3b^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^4,x, algorithm="giac")

[Out] $-20*a^3*\log(\text{abs}(b*x + a))/b^7 - 1/3*(45*a^4*b^2*x^2 + 81*a^5*b*x + 37*a^6)/((b*x + a)^3*b^7) + 1/3*(b^8*x^3 - 6*a*b^7*x^2 + 30*a^2*b^6*x)/b^{12}$

maple [A] time = 0.01, size = 87, normalized size = 0.97

$$-\frac{a^6}{3(bx+a)^3b^7} + \frac{x^3}{3b^4} + \frac{3a^5}{(bx+a)^2b^7} - \frac{2ax^2}{b^5} - \frac{15a^4}{(bx+a)b^7} - \frac{20a^3\ln(bx+a)}{b^7} + \frac{10a^2x}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/(b*x+a)^4,x)

[Out] $10*a^2*x/b^6 - 2*a*x^2/b^5 + 1/3*x^3/b^4 - 1/3*a^6/b^7/(b*x+a)^3 + 3*a^5/b^7/(b*x+a)^2 - 15*a^4/b^7/(b*x+a) - 20*a^3*\ln(b*x+a)/b^7$

maxima [A] time = 1.42, size = 102, normalized size = 1.13

$$-\frac{45a^4b^2x^2 + 81a^5bx + 37a^6}{3(b^{10}x^3 + 3ab^9x^2 + 3a^2b^8x + a^3b^7)} - \frac{20a^3\log(bx+a)}{b^7} + \frac{b^2x^3 - 6abx^2 + 30a^2x}{3b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^4,x, algorithm="maxima")

[Out] $-1/3*(45*a^4*b^2*x^2 + 81*a^5*b*x + 37*a^6)/(b^{10}*x^3 + 3*a*b^9*x^2 + 3*a^2*b^8*x + a^3*b^7) - 20*a^3*\log(b*x + a)/b^7 + 1/3*(b^2*x^3 - 6*a*b*x^2 + 30*a^2*x)/b^6$

mupad [B] time = 0.15, size = 79, normalized size = 0.88

$$\frac{3a(a+bx)^2 - \frac{(a+bx)^3}{3} + \frac{15a^4}{a+bx} - \frac{3a^5}{(a+bx)^2} + \frac{a^6}{3(a+bx)^3} + 20a^3 \ln(a+bx) - 15a^2bx}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/(a + b*x)^4,x)

[Out] $-(3*a*(a + b*x)^2 - (a + b*x)^3/3 + (15*a^4)/(a + b*x) - (3*a^5)/(a + b*x)^2 + a^6/(3*(a + b*x)^3) + 20*a^3*\log(a + b*x) - 15*a^2*b*x)/b^7$

sympy [A] time = 0.48, size = 107, normalized size = 1.19

$$-\frac{20a^3 \log(a+bx)}{b^7} + \frac{10a^2x}{b^6} - \frac{2ax^2}{b^5} + \frac{-37a^6 - 81a^5bx - 45a^4b^2x^2}{3a^3b^7 + 9a^2b^8x + 9ab^9x^2 + 3b^{10}x^3} + \frac{x^3}{3b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6/(b*x+a)**4,x)

[Out] $-20*a**3*\log(a + b*x)/b**7 + 10*a**2*x/b**6 - 2*a*x**2/b**5 + (-37*a**6 - 81*a**5*b*x - 45*a**4*b**2*x**2)/(3*a**3*b**7 + 9*a**2*b**8*x + 9*a*b**9*x**2 + 3*b**10*x**3) + x**3/(3*b**4)$

$$3.196 \quad \int \frac{x^5}{(a+bx)^4} dx$$

Optimal. Leaf size=81

$$\frac{a^5}{3b^6(a+bx)^3} - \frac{5a^4}{2b^6(a+bx)^2} + \frac{10a^3}{b^6(a+bx)} + \frac{10a^2 \log(a+bx)}{b^6} - \frac{4ax}{b^5} + \frac{x^2}{2b^4}$$

[Out] $-4*a*x/b^5 + 1/2*x^2/b^4 + 1/3*a^5/b^6/(b*x+a)^3 - 5/2*a^4/b^6/(b*x+a)^2 + 10*a^3/b^6/(b*x+a) + 10*a^2*\ln(b*x+a)/b^6$

Rubi [A] time = 0.05, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^5}{3b^6(a+bx)^3} - \frac{5a^4}{2b^6(a+bx)^2} + \frac{10a^3}{b^6(a+bx)} + \frac{10a^2 \log(a+bx)}{b^6} - \frac{4ax}{b^5} + \frac{x^2}{2b^4}$$

Antiderivative was successfully verified.

[In] Int[x^5/(a + b*x)^4, x]

[Out] $(-4*a*x)/b^5 + x^2/(2*b^4) + a^5/(3*b^6*(a + b*x)^3) - (5*a^4)/(2*b^6*(a + b*x)^2) + (10*a^3)/(b^6*(a + b*x)) + (10*a^2*\text{Log}[a + b*x])/b^6$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^5}{(a+bx)^4} dx &= \int \left(-\frac{4a}{b^5} + \frac{x}{b^4} - \frac{a^5}{b^5(a+bx)^4} + \frac{5a^4}{b^5(a+bx)^3} - \frac{10a^3}{b^5(a+bx)^2} + \frac{10a^2}{b^5(a+bx)} \right) dx \\ &= -\frac{4ax}{b^5} + \frac{x^2}{2b^4} + \frac{a^5}{3b^6(a+bx)^3} - \frac{5a^4}{2b^6(a+bx)^2} + \frac{10a^3}{b^6(a+bx)} + \frac{10a^2 \log(a+bx)}{b^6} \end{aligned}$$

Mathematica [A] time = 0.02, size = 68, normalized size = 0.84

$$\frac{\frac{2a^5}{(a+bx)^3} - \frac{15a^4}{(a+bx)^2} + \frac{60a^3}{a+bx} + 60a^2 \log(a+bx) - 24abx + 3b^2x^2}{6b^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/(a + b*x)^4,x]

[Out] $(-24*a*b*x + 3*b^2*x^2 + (2*a^5)/(a + b*x)^3 - (15*a^4)/(a + b*x)^2 + (60*a^3)/(a + b*x) + 60*a^2*\text{Log}[a + b*x])/(6*b^6)$

fricas [A] time = 0.44, size = 129, normalized size = 1.59

$$\frac{3b^5x^5 - 15ab^4x^4 - 63a^2b^3x^3 - 9a^3b^2x^2 + 81a^4bx + 47a^5 + 60(a^2b^3x^3 + 3a^3b^2x^2 + 3a^4bx + a^5)\log(bx + a)}{6(b^9x^3 + 3ab^8x^2 + 3a^2b^7x + a^3b^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^4,x, algorithm="fricas")

[Out] $1/6*(3*b^5*x^5 - 15*a*b^4*x^4 - 63*a^2*b^3*x^3 - 9*a^3*b^2*x^2 + 81*a^4*b*x + 47*a^5 + 60*(a^2*b^3*x^3 + 3*a^3*b^2*x^2 + 3*a^4*b*x + a^5)*\log(b*x + a))/(b^9*x^3 + 3*a*b^8*x^2 + 3*a^2*b^7*x + a^3*b^6)$

giac [A] time = 0.87, size = 72, normalized size = 0.89

$$\frac{10a^2\log(|bx+a|)}{b^6} + \frac{b^4x^2 - 8ab^3x}{2b^8} + \frac{60a^3b^2x^2 + 105a^4bx + 47a^5}{6(bx+a)^3b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^4,x, algorithm="giac")

[Out] $10*a^2*\log(\text{abs}(b*x + a))/b^6 + 1/2*(b^4*x^2 - 8*a*b^3*x)/b^8 + 1/6*(60*a^3*b^2*x^2 + 105*a^4*b*x + 47*a^5)/((b*x + a)^3*b^6)$

maple [A] time = 0.01, size = 76, normalized size = 0.94

$$\frac{a^5}{3(bx+a)^3b^6} - \frac{5a^4}{2(bx+a)^2b^6} + \frac{x^2}{2b^4} + \frac{10a^3}{(bx+a)b^6} + \frac{10a^2\ln(bx+a)}{b^6} - \frac{4ax}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(b*x+a)^4,x)

[Out] $-4*a*x/b^5 + 1/2*x^2/b^4 + 1/3*a^5/b^6/(b*x+a)^3 - 5/2*a^4/b^6/(b*x+a)^2 + 10*a^3/b^6/(b*x+a) + 10*a^2*\ln(b*x+a)/b^6$

maxima [A] time = 1.46, size = 91, normalized size = 1.12

$$\frac{60a^3b^2x^2 + 105a^4bx + 47a^5}{6(b^9x^3 + 3ab^8x^2 + 3a^2b^7x + a^3b^6)} + \frac{10a^2\log(bx+a)}{b^6} + \frac{bx^2 - 8ax}{2b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^4,x, algorithm="maxima")

[Out] $\frac{1}{6} \cdot (60 \cdot a^3 \cdot b^2 \cdot x^2 + 105 \cdot a^4 \cdot b \cdot x + 47 \cdot a^5) / (b^9 \cdot x^3 + 3 \cdot a \cdot b^8 \cdot x^2 + 3 \cdot a^2 \cdot b^7 \cdot x + a^3 \cdot b^6) + 10 \cdot a^2 \cdot \log(b \cdot x + a) / b^6 + 1/2 \cdot (b \cdot x^2 - 8 \cdot a \cdot x) / b^5$

mupad [B] time = 0.12, size = 66, normalized size = 0.81

$$\frac{\frac{(a+bx)^2}{2} + \frac{10a^3}{a+bx} - \frac{5a^4}{2(a+bx)^2} + \frac{a^5}{3(a+bx)^3} + 10a^2 \ln(a+bx) - 5abx}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(a + b*x)^4,x)

[Out] $((a + b \cdot x)^2 / 2 + (10 \cdot a^3) / (a + b \cdot x) - (5 \cdot a^4) / (2 \cdot (a + b \cdot x)^2) + a^5 / (3 \cdot (a + b \cdot x)^3) + 10 \cdot a^2 \cdot \log(a + b \cdot x) - 5 \cdot a \cdot b \cdot x) / b^6$

sympy [A] time = 0.46, size = 94, normalized size = 1.16

$$\frac{10a^2 \log(a+bx)}{b^6} - \frac{4ax}{b^5} + \frac{47a^5 + 105a^4bx + 60a^3b^2x^2}{6a^3b^6 + 18a^2b^7x + 18ab^8x^2 + 6b^9x^3} + \frac{x^2}{2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5/(b*x+a)**4,x)

[Out] $10 \cdot a^{**2} \cdot \log(a + b \cdot x) / b^{**6} - 4 \cdot a \cdot x / b^{**5} + (47 \cdot a^{**5} + 105 \cdot a^{**4} \cdot b \cdot x + 60 \cdot a^{**3} \cdot b^{**2} \cdot x^{**2}) / (6 \cdot a^{**3} \cdot b^{**6} + 18 \cdot a^{**2} \cdot b^{**7} \cdot x + 18 \cdot a \cdot b^{**8} \cdot x^{**2} + 6 \cdot b^{**9} \cdot x^{**3}) + x^{**2} / (2 \cdot b^{**4})$

$$3.197 \quad \int \frac{x^4}{(a+bx)^4} dx$$

Optimal. Leaf size=65

$$-\frac{a^4}{3b^5(a+bx)^3} + \frac{2a^3}{b^5(a+bx)^2} - \frac{6a^2}{b^5(a+bx)} - \frac{4a \log(a+bx)}{b^5} + \frac{x}{b^4}$$

[Out] $x/b^4 - 1/3*a^4/b^5/(b*x+a)^3 + 2*a^3/b^5/(b*x+a)^2 - 6*a^2/b^5/(b*x+a) - 4*a*\ln(b*x+a)/b^5$

Rubi [A] time = 0.04, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^4}{3b^5(a+bx)^3} + \frac{2a^3}{b^5(a+bx)^2} - \frac{6a^2}{b^5(a+bx)} - \frac{4a \log(a+bx)}{b^5} + \frac{x}{b^4}$$

Antiderivative was successfully verified.

[In] Int[x^4/(a + b*x)^4, x]

[Out] $x/b^4 - a^4/(3*b^5*(a + b*x)^3) + (2*a^3)/(b^5*(a + b*x)^2) - (6*a^2)/(b^5*(a + b*x)) - (4*a*\text{Log}[a + b*x])/b^5$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{(a+bx)^4} dx &= \int \left(\frac{1}{b^4} + \frac{a^4}{b^4(a+bx)^4} - \frac{4a^3}{b^4(a+bx)^3} + \frac{6a^2}{b^4(a+bx)^2} - \frac{4a}{b^4(a+bx)} \right) dx \\ &= \frac{x}{b^4} - \frac{a^4}{3b^5(a+bx)^3} + \frac{2a^3}{b^5(a+bx)^2} - \frac{6a^2}{b^5(a+bx)} - \frac{4a \log(a+bx)}{b^5} \end{aligned}$$

Mathematica [A] time = 0.05, size = 51, normalized size = 0.78

$$\frac{\frac{a^2(13a^2+30abx+18b^2x^2)}{(a+bx)^3} + 12a \log(a+bx) - 3bx}{3b^5}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/(a + b*x)^4,x]

[Out] $-1/3*(-3*b*x + (a^2*(13*a^2 + 30*a*b*x + 18*b^2*x^2))/(a + b*x)^3 + 12*a*\text{Log}[a + b*x])/b^5$

fricas [A] time = 0.43, size = 116, normalized size = 1.78

$$\frac{3b^4x^4 + 9ab^3x^3 - 9a^2b^2x^2 - 27a^3bx - 13a^4 - 12(ab^3x^3 + 3a^2b^2x^2 + 3a^3bx + a^4)\log(bx + a)}{3(b^8x^3 + 3ab^7x^2 + 3a^2b^6x + a^3b^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^4,x, algorithm="fricas")

[Out] $1/3*(3*b^4*x^4 + 9*a*b^3*x^3 - 9*a^2*b^2*x^2 - 27*a^3*b*x - 13*a^4 - 12*(a*b^3*x^3 + 3*a^2*b^2*x^2 + 3*a^3*b*x + a^4)*\log(b*x + a))/(b^8*x^3 + 3*a*b^7*x^2 + 3*a^2*b^6*x + a^3*b^5)$

giac [A] time = 0.86, size = 55, normalized size = 0.85

$$\frac{x}{b^4} - \frac{4a \log(|bx + a|)}{b^5} - \frac{18a^2b^2x^2 + 30a^3bx + 13a^4}{3(bx + a)^3b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^4,x, algorithm="giac")

[Out] $x/b^4 - 4*a*\log(\text{abs}(b*x + a))/b^5 - 1/3*(18*a^2*b^2*x^2 + 30*a^3*b*x + 13*a^4)/((b*x + a)^3*b^5)$

maple [A] time = 0.01, size = 64, normalized size = 0.98

$$-\frac{a^4}{3(bx + a)^3b^5} + \frac{2a^3}{(bx + a)^2b^5} - \frac{6a^2}{(bx + a)b^5} - \frac{4a \ln(bx + a)}{b^5} + \frac{x}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(b*x+a)^4,x)

[Out] $x/b^4 - 1/3*a^4/b^5/(b*x+a)^3 + 2*a^3/b^5/(b*x+a)^2 - 6*a^2/b^5/(b*x+a) - 4*a*\ln(b*x+a)/b^5$

maxima [A] time = 1.41, size = 79, normalized size = 1.22

$$-\frac{18a^2b^2x^2 + 30a^3bx + 13a^4}{3(b^8x^3 + 3ab^7x^2 + 3a^2b^6x + a^3b^5)} + \frac{x}{b^4} - \frac{4a \log(bx + a)}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^4,x, algorithm="maxima")

[Out] $-1/3*(18*a^2*b^2*x^2 + 30*a^3*b*x + 13*a^4)/(b^8*x^3 + 3*a*b^7*x^2 + 3*a^2*b^6*x + a^3*b^5) + x/b^4 - 4*a*\log(b*x + a)/b^5$

mupad [B] time = 0.17, size = 55, normalized size = 0.85

$$\frac{4a \ln(a + bx) - bx + \frac{6a^2}{a+bx} - \frac{2a^3}{(a+bx)^2} + \frac{a^4}{3(a+bx)^3}}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(a + b*x)^4,x)

[Out] $-(4*a*\log(a + b*x) - b*x + (6*a^2)/(a + b*x) - (2*a^3)/(a + b*x)^2 + a^4/(3*(a + b*x)^3))/b^5$

sympy [A] time = 0.40, size = 82, normalized size = 1.26

$$-\frac{4a \log(a + bx)}{b^5} + \frac{-13a^4 - 30a^3bx - 18a^2b^2x^2}{3a^3b^5 + 9a^2b^6x + 9ab^7x^2 + 3b^8x^3} + \frac{x}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/(b*x+a)**4,x)

[Out] $-4*a*\log(a + b*x)/b**5 + (-13*a**4 - 30*a**3*b*x - 18*a**2*b**2*x**2)/(3*a**3*b**5 + 9*a**2*b**6*x + 9*a*b**7*x**2 + 3*b**8*x**3) + x/b**4$

$$3.198 \quad \int \frac{x^3}{(a+bx)^4} dx$$

Optimal. Leaf size=58

$$\frac{a^3}{3b^4(a+bx)^3} - \frac{3a^2}{2b^4(a+bx)^2} + \frac{3a}{b^4(a+bx)} + \frac{\log(a+bx)}{b^4}$$

[Out] $1/3*a^3/b^4/(b*x+a)^3-3/2*a^2/b^4/(b*x+a)^2+3*a/b^4/(b*x+a)+\ln(b*x+a)/b^4$

Rubi [A] time = 0.03, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^3}{3b^4(a+bx)^3} - \frac{3a^2}{2b^4(a+bx)^2} + \frac{3a}{b^4(a+bx)} + \frac{\log(a+bx)}{b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x)^4, x]

[Out] $a^3/(3*b^4*(a + b*x)^3) - (3*a^2)/(2*b^4*(a + b*x)^2) + (3*a)/(b^4*(a + b*x)) + \text{Log}[a + b*x]/b^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(a+bx)^4} dx &= \int \left(-\frac{a^3}{b^3(a+bx)^4} + \frac{3a^2}{b^3(a+bx)^3} - \frac{3a}{b^3(a+bx)^2} + \frac{1}{b^3(a+bx)} \right) dx \\ &= \frac{a^3}{3b^4(a+bx)^3} - \frac{3a^2}{2b^4(a+bx)^2} + \frac{3a}{b^4(a+bx)} + \frac{\log(a+bx)}{b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 44, normalized size = 0.76

$$\frac{\frac{a(11a^2+27abx+18b^2x^2)}{(a+bx)^3} + 6 \log(a+bx)}{6b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x)^4,x]

[Out] ((a*(11*a^2 + 27*a*b*x + 18*b^2*x^2))/(a + b*x)^3 + 6*Log[a + b*x])/(6*b^4)

fricas [A] time = 0.45, size = 94, normalized size = 1.62

$$\frac{18 ab^2 x^2 + 27 a^2 b x + 11 a^3 + 6 (b^3 x^3 + 3 a b^2 x^2 + 3 a^2 b x + a^3) \log (b x + a)}{6 (b^7 x^3 + 3 a b^6 x^2 + 3 a^2 b^5 x + a^3 b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^4,x, algorithm="fricas")

[Out] 1/6*(18*a*b^2*x^2 + 27*a^2*b*x + 11*a^3 + 6*(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3)*log(b*x + a))/(b^7*x^3 + 3*a*b^6*x^2 + 3*a^2*b^5*x + a^3*b^4)

giac [A] time = 1.03, size = 46, normalized size = 0.79

$$\frac{\log (|b x + a|)}{b^4} + \frac{18 a b x^2 + 27 a^2 x + \frac{11 a^3}{b}}{6 (b x + a)^3 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^4,x, algorithm="giac")

[Out] log(abs(b*x + a))/b^4 + 1/6*(18*a*b*x^2 + 27*a^2*x + 11*a^3/b)/((b*x + a)^3*b^3)

maple [A] time = 0.01, size = 55, normalized size = 0.95

$$\frac{a^3}{3 (b x + a)^3 b^4} - \frac{3 a^2}{2 (b x + a)^2 b^4} + \frac{3 a}{(b x + a) b^4} + \frac{\ln (b x + a)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^4,x)

[Out] 1/3*a^3/b^4/(b*x+a)^3-3/2*a^2/b^4/(b*x+a)^2+3*a/b^4/(b*x+a)+ln(b*x+a)/b^4

maxima [A] time = 1.39, size = 70, normalized size = 1.21

$$\frac{18 a b^2 x^2 + 27 a^2 b x + 11 a^3}{6 (b^7 x^3 + 3 a b^6 x^2 + 3 a^2 b^5 x + a^3 b^4)} + \frac{\log (b x + a)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^4,x, algorithm="maxima")

[Out] 1/6*(18*a*b^2*x^2 + 27*a^2*b*x + 11*a^3)/(b^7*x^3 + 3*a*b^6*x^2 + 3*a^2*b^5*x + a^3*b^4) + log(b*x + a)/b^4

mupad [B] time = 0.07, size = 45, normalized size = 0.78

$$\frac{\ln(a + bx) + \frac{3a}{a+bx} - \frac{3a^2}{2(a+bx)^2} + \frac{a^3}{3(a+bx)^3}}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(a + b*x)^4,x)

[Out] (log(a + b*x) + (3*a)/(a + b*x) - (3*a^2)/(2*(a + b*x)^2) + a^3/(3*(a + b*x)^3))/b^4

sympy [A] time = 0.31, size = 70, normalized size = 1.21

$$\frac{11a^3 + 27a^2bx + 18ab^2x^2}{6a^3b^4 + 18a^2b^5x + 18ab^6x^2 + 6b^7x^3} + \frac{\log(a + bx)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(b*x+a)**4,x)

[Out] (11*a**3 + 27*a**2*b*x + 18*a*b**2*x**2)/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + log(a + b*x)/b**4

$$3.199 \quad \int \frac{x^2}{(a+bx)^4} dx$$

Optimal. Leaf size=17

$$\frac{x^3}{3a(a+bx)^3}$$

[Out] 1/3*x^3/a/(b*x+a)^3

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {37}

$$\frac{x^3}{3a(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*x)^4,x]

[Out] x^3/(3*a*(a + b*x)^3)

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{x^2}{(a+bx)^4} dx = \frac{x^3}{3a(a+bx)^3}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 1.82

$$\frac{a^2 + 3abx + 3b^2x^2}{3b^3(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x)^4,x]

[Out] -1/3*(a^2 + 3*a*b*x + 3*b^2*x^2)/(b^3*(a + b*x)^3)

fricas [B] time = 0.44, size = 54, normalized size = 3.18

$$\frac{3b^2x^2 + 3abx + a^2}{3(b^6x^3 + 3ab^5x^2 + 3a^2b^4x + a^3b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^4,x, algorithm="fricas")

[Out] -1/3*(3*b^2*x^2 + 3*a*b*x + a^2)/(b^6*x^3 + 3*a*b^5*x^2 + 3*a^2*b^4*x + a^3*b^3)

giac [A] time = 1.27, size = 29, normalized size = 1.71

$$\frac{3b^2x^2 + 3abx + a^2}{3(bx + a)^3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^4,x, algorithm="giac")

[Out] -1/3*(3*b^2*x^2 + 3*a*b*x + a^2)/((b*x + a)^3*b^3)

maple [B] time = 0.00, size = 41, normalized size = 2.41

$$-\frac{a^2}{3(bx + a)^3b^3} + \frac{a}{(bx + a)^2b^3} - \frac{1}{(bx + a)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^4,x)

[Out] a/b^3/(b*x+a)^2-1/3*a^2/b^3/(b*x+a)^3-1/b^3/(b*x+a)

maxima [B] time = 1.40, size = 54, normalized size = 3.18

$$\frac{3b^2x^2 + 3abx + a^2}{3(b^6x^3 + 3ab^5x^2 + 3a^2b^4x + a^3b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^4,x, algorithm="maxima")

[Out] -1/3*(3*b^2*x^2 + 3*a*b*x + a^2)/(b^6*x^3 + 3*a*b^5*x^2 + 3*a^2*b^4*x + a^3*b^3)

mupad [B] time = 0.09, size = 56, normalized size = 3.29

$$\frac{a^2 + 3abx + 3b^2x^2}{3a^3b^3 + 9a^2b^4x + 9ab^5x^2 + 3b^6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/(a + b*x)^4,x)`

[Out] `-(a^2 + 3*b^2*x^2 + 3*a*b*x)/(3*a^3*b^3 + 3*b^6*x^3 + 9*a^2*b^4*x + 9*a*b^5*x^2)`

sympy [B] time = 0.30, size = 56, normalized size = 3.29

$$\frac{-a^2 - 3abx - 3b^2x^2}{3a^3b^3 + 9a^2b^4x + 9ab^5x^2 + 3b^6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2/(b*x+a)**4,x)`

[Out] `(-a**2 - 3*a*b*x - 3*b**2*x**2)/(3*a**3*b**3 + 9*a**2*b**4*x + 9*a*b**5*x**2 + 3*b**6*x**3)`

$$3.200 \quad \int \frac{x}{(a+bx)^4} dx$$

Optimal. Leaf size=30

$$\frac{a}{3b^2(a+bx)^3} - \frac{1}{2b^2(a+bx)^2}$$

[Out] 1/3*a/b^2/(b*x+a)^3-1/2/b^2/(b*x+a)^2

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{a}{3b^2(a+bx)^3} - \frac{1}{2b^2(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x)^4,x]

[Out] a/(3*b^2*(a + b*x)^3) - 1/(2*b^2*(a + b*x)^2)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x}{(a+bx)^4} dx &= \int \left(-\frac{a}{b(a+bx)^4} + \frac{1}{b(a+bx)^3} \right) dx \\ &= \frac{a}{3b^2(a+bx)^3} - \frac{1}{2b^2(a+bx)^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 0.67

$$-\frac{a+3bx}{6b^2(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x)^4,x]

[Out] $-1/6*(a + 3*b*x)/(b^2*(a + b*x)^3)$

fricas [A] time = 0.46, size = 43, normalized size = 1.43

$$-\frac{3bx + a}{6(b^5x^3 + 3ab^4x^2 + 3a^2b^3x + a^3b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^4,x, algorithm="fricas")`

[Out] $-1/6*(3*b*x + a)/(b^5*x^3 + 3*a*b^4*x^2 + 3*a^2*b^3*x + a^3*b^2)$

giac [A] time = 1.01, size = 18, normalized size = 0.60

$$-\frac{3bx + a}{6(bx + a)^3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^4,x, algorithm="giac")`

[Out] $-1/6*(3*b*x + a)/((b*x + a)^3*b^2)$

maple [A] time = 0.00, size = 27, normalized size = 0.90

$$\frac{a}{3(bx + a)^3b^2} - \frac{1}{2(bx + a)^2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(b*x+a)^4,x)`

[Out] $1/3*a/b^2/(b*x+a)^3 - 1/2/b^2/(b*x+a)^2$

maxima [A] time = 1.37, size = 43, normalized size = 1.43

$$-\frac{3bx + a}{6(b^5x^3 + 3ab^4x^2 + 3a^2b^3x + a^3b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^4,x, algorithm="maxima")`

[Out] $-1/6*(3*b*x + a)/(b^5*x^3 + 3*a*b^4*x^2 + 3*a^2*b^3*x + a^3*b^2)$

mupad [B] time = 0.07, size = 44, normalized size = 1.47

$$-\frac{\frac{a}{6b^2} + \frac{x}{2b}}{a^3 + 3a^2bx + 3ab^2x^2 + b^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a + b*x)^4,x)`

[Out] `-(a/(6*b^2) + x/(2*b))/(a^3 + b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x)`

sympy [A] time = 0.32, size = 44, normalized size = 1.47

$$\frac{-a - 3bx}{6a^3b^2 + 18a^2b^3x + 18ab^4x^2 + 6b^5x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)**4,x)`

[Out] `(-a - 3*b*x)/(6*a**3*b**2 + 18*a**2*b**3*x + 18*a*b**4*x**2 + 6*b**5*x**3)`

$$3.201 \quad \int \frac{1}{(a+bx)^4} dx$$

Optimal. Leaf size=14

$$-\frac{1}{3b(a+bx)^3}$$

[Out] -1/3/b/(b*x+a)^3

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$-\frac{1}{3b(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-4), x]

[Out] -1/(3*b*(a + b*x)^3)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^4} dx = -\frac{1}{3b(a+bx)^3}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\frac{1}{3b(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-4), x]

[Out] -1/3*1/(b*(a + b*x)^3)

fricas [B] time = 0.41, size = 35, normalized size = 2.50

$$-\frac{1}{3(b^4x^3 + 3ab^3x^2 + 3a^2b^2x + a^3b)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^4,x, algorithm="fricas")

[Out] -1/3/(b^4*x^3 + 3*a*b^3*x^2 + 3*a^2*b^2*x + a^3*b)

giac [A] time = 1.02, size = 12, normalized size = 0.86

$$-\frac{1}{3(bx+a)^3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^4,x, algorithm="giac")

[Out] -1/3/((b*x + a)^3*b)

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$-\frac{1}{3(bx+a)^3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^4,x)

[Out] -1/3/b/(b*x+a)^3

maxima [A] time = 1.38, size = 12, normalized size = 0.86

$$-\frac{1}{3(bx+a)^3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^4,x, algorithm="maxima")

[Out] -1/3/((b*x + a)^3*b)

mupad [B] time = 0.08, size = 37, normalized size = 2.64

$$-\frac{1}{3a^3b + 9a^2b^2x + 9ab^3x^2 + 3b^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x)^4,x)

[Out] -1/(3*a^3*b + 3*b^4*x^3 + 9*a^2*b^2*x + 9*a*b^3*x^2)

sympy [B] time = 0.27, size = 37, normalized size = 2.64

$$-\frac{1}{3a^3b + 9a^2b^2x + 9ab^3x^2 + 3b^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**4,x)

[Out] -1/(3*a**3*b + 9*a**2*b**2*x + 9*a*b**3*x**2 + 3*b**4*x**3)

$$3.202 \quad \int \frac{1}{x(a+bx)^4} dx$$

Optimal. Leaf size=57

$$-\frac{\log(a+bx)}{a^4} + \frac{\log(x)}{a^4} + \frac{1}{a^3(a+bx)} + \frac{1}{2a^2(a+bx)^2} + \frac{1}{3a(a+bx)^3}$$

[Out] $1/3/a/(b*x+a)^3+1/2/a^2/(b*x+a)^2+1/a^3/(b*x+a)+\ln(x)/a^4-\ln(b*x+a)/a^4$

Rubi [A] time = 0.03, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{1}{a^3(a+bx)} + \frac{1}{2a^2(a+bx)^2} - \frac{\log(a+bx)}{a^4} + \frac{\log(x)}{a^4} + \frac{1}{3a(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a + b*x)^4), x]

[Out] $1/(3*a*(a + b*x)^3) + 1/(2*a^2*(a + b*x)^2) + 1/(a^3*(a + b*x)) + \text{Log}[x]/a^4 - \text{Log}[a + b*x]/a^4$

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x(a+bx)^4} dx &= \int \left(\frac{1}{a^4 x} - \frac{b}{a(a+bx)^4} - \frac{b}{a^2(a+bx)^3} - \frac{b}{a^3(a+bx)^2} - \frac{b}{a^4(a+bx)} \right) dx \\ &= \frac{1}{3a(a+bx)^3} + \frac{1}{2a^2(a+bx)^2} + \frac{1}{a^3(a+bx)} + \frac{\log(x)}{a^4} - \frac{\log(a+bx)}{a^4} \end{aligned}$$

Mathematica [A] time = 0.03, size = 48, normalized size = 0.84

$$\frac{a(11a^2+15abx+6b^2x^2)}{(a+bx)^3} - 6\log(a+bx) + 6\log(x)$$

$$6a^4$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)^4), x]

[Out] ((a*(11*a^2 + 15*a*b*x + 6*b^2*x^2))/(a + b*x)^3 + 6*Log[x] - 6*Log[a + b*x])/ (6*a^4)

fricas [B] time = 0.46, size = 124, normalized size = 2.18

$$\frac{6ab^2x^2 + 15a^2bx + 11a^3 - 6(b^3x^3 + 3ab^2x^2 + 3a^2bx + a^3)\log(bx + a) + 6(b^3x^3 + 3ab^2x^2 + 3a^2bx + a^3)\log(x)}{6(a^4b^3x^3 + 3a^5b^2x^2 + 3a^6bx + a^7)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^4,x, algorithm="fricas")

[Out] 1/6*(6*a*b^2*x^2 + 15*a^2*b*x + 11*a^3 - 6*(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3)*log(b*x + a) + 6*(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3)*log(x))/(a^4*b^3*x^3 + 3*a^5*b^2*x^2 + 3*a^6*b*x + a^7)

giac [A] time = 1.02, size = 54, normalized size = 0.95

$$-\frac{\log(|bx + a|)}{a^4} + \frac{\log(|x|)}{a^4} + \frac{6ab^2x^2 + 15a^2bx + 11a^3}{6(bx + a)^3a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^4,x, algorithm="giac")

[Out] -log(abs(b*x + a))/a^4 + log(abs(x))/a^4 + 1/6*(6*a*b^2*x^2 + 15*a^2*b*x + 11*a^3)/((b*x + a)^3*a^4)

maple [A] time = 0.01, size = 54, normalized size = 0.95

$$\frac{1}{3(bx + a)^3a} + \frac{1}{2(bx + a)^2a^2} + \frac{1}{(bx + a)a^3} + \frac{\ln(x)}{a^4} - \frac{\ln(bx + a)}{a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a)^4,x)

[Out] 1/3/a/(b*x+a)^3+1/2/a^2/(b*x+a)^2+1/a^3/(b*x+a)+ln(x)/a^4-ln(b*x+a)/a^4

maxima [A] time = 1.47, size = 73, normalized size = 1.28

$$\frac{6b^2x^2 + 15abx + 11a^2}{6(a^3b^3x^3 + 3a^4b^2x^2 + 3a^5bx + a^6)} - \frac{\log(bx + a)}{a^4} + \frac{\log(x)}{a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^4,x, algorithm="maxima")

[Out] $1/6*(6*b^2*x^2 + 15*a*b*x + 11*a^2)/(a^3*b^3*x^3 + 3*a^4*b^2*x^2 + 3*a^5*b*x + a^6) - \log(b*x + a)/a^4 + \log(x)/a^4$

mupad [B] time = 0.13, size = 60, normalized size = 1.05

$$\frac{\frac{1}{a^2+bx} - \frac{\ln\left(\frac{a+bx}{x}\right)}{a^2}}{a} + \frac{1}{2a(a+bx)^2} + \frac{1}{3a(a+bx)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(a + b*x)^4),x)

[Out] $((1/(a^2 + a*b*x) - \log((a + b*x)/x)/a^2)/a + 1/(2*a*(a + b*x)^2))/a + 1/(3*a*(a + b*x)^3)$

sympy [A] time = 0.44, size = 70, normalized size = 1.23

$$\frac{11a^2 + 15abx + 6b^2x^2}{6a^6 + 18a^5bx + 18a^4b^2x^2 + 6a^3b^3x^3} + \frac{\log(x) - \log\left(\frac{a}{b} + x\right)}{a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)**4,x)

[Out] $(11*a**2 + 15*a*b*x + 6*b**2*x**2)/(6*a**6 + 18*a**5*b*x + 18*a**4*b**2*x**2 + 6*a**3*b**3*x**3) + (\log(x) - \log(a/b + x))/a**4$

$$3.203 \quad \int \frac{1}{x^2(a+bx)^4} dx$$

Optimal. Leaf size=70

$$-\frac{4b \log(x)}{a^5} + \frac{4b \log(a+bx)}{a^5} - \frac{3b}{a^4(a+bx)} - \frac{1}{a^4x} - \frac{b}{a^3(a+bx)^2} - \frac{b}{3a^2(a+bx)^3}$$

[Out] $-1/a^4/x - 1/3*b/a^2/(b*x+a)^3 - b/a^3/(b*x+a)^2 - 3*b/a^4/(b*x+a) - 4*b*\ln(x)/a^5 + 4*b*\ln(b*x+a)/a^5$

Rubi [A] time = 0.04, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{3b}{a^4(a+bx)} - \frac{b}{a^3(a+bx)^2} - \frac{b}{3a^2(a+bx)^3} - \frac{4b \log(x)}{a^5} + \frac{4b \log(a+bx)}{a^5} - \frac{1}{a^4x}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(a + b*x)^4), x]

[Out] $-(1/(a^4*x)) - b/(3*a^2*(a + b*x)^3) - b/(a^3*(a + b*x)^2) - (3*b)/(a^4*(a + b*x)) - (4*b*\text{Log}[x])/a^5 + (4*b*\text{Log}[a + b*x])/a^5$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(a+bx)^4} dx &= \int \left(\frac{1}{a^4x^2} - \frac{4b}{a^5x} + \frac{b^2}{a^2(a+bx)^4} + \frac{2b^2}{a^3(a+bx)^3} + \frac{3b^2}{a^4(a+bx)^2} + \frac{4b^2}{a^5(a+bx)} \right) dx \\ &= -\frac{1}{a^4x} - \frac{b}{3a^2(a+bx)^3} - \frac{b}{a^3(a+bx)^2} - \frac{3b}{a^4(a+bx)} - \frac{4b \log(x)}{a^5} + \frac{4b \log(a+bx)}{a^5} \end{aligned}$$

Mathematica [A] time = 0.06, size = 64, normalized size = 0.91

$$\frac{\frac{a(3a^3+22a^2bx+30ab^2x^2+12b^3x^3)}{x(a+bx)^3} - 12b \log(a+bx) + 12b \log(x)}{3a^5}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)^4),x]

[Out] $-1/3*((a*(3*a^3 + 22*a^2*b*x + 30*a*b^2*x^2 + 12*b^3*x^3))/(x*(a + b*x)^3) + 12*b*\text{Log}[x] - 12*b*\text{Log}[a + b*x])/a^5$

fricas [B] time = 0.46, size = 153, normalized size = 2.19

$$\frac{12 ab^3 x^3 + 30 a^2 b^2 x^2 + 22 a^3 b x + 3 a^4 - 12 (b^4 x^4 + 3 ab^3 x^3 + 3 a^2 b^2 x^2 + a^3 b x) \log (bx + a) + 12 (b^4 x^4 + 3 ab^3 x^3 + 3 a^2 b^2 x^2 + a^3 b x) \log (x)}{3 (a^5 b^3 x^4 + 3 a^6 b^2 x^3 + 3 a^7 b x^2 + a^8 x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^4,x, algorithm="fricas")

[Out] $-1/3*(12*a*b^3*x^3 + 30*a^2*b^2*x^2 + 22*a^3*b*x + 3*a^4 - 12*(b^4*x^4 + 3*a*b^3*x^3 + 3*a^2*b^2*x^2 + a^3*b*x)*\log(b*x + a) + 12*(b^4*x^4 + 3*a*b^3*x^3 + 3*a^2*b^2*x^2 + a^3*b*x)*\log(x))/(a^5*b^3*x^4 + 3*a^6*b^2*x^3 + 3*a^7*b*x^2 + a^8*x)$

giac [A] time = 1.16, size = 71, normalized size = 1.01

$$\frac{4 b \log (|bx + a|)}{a^5} - \frac{4 b \log (|x|)}{a^5} - \frac{12 ab^3 x^3 + 30 a^2 b^2 x^2 + 22 a^3 b x + 3 a^4}{3 (bx + a)^3 a^5 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^4,x, algorithm="giac")

[Out] $4*b*\log(\text{abs}(b*x + a))/a^5 - 4*b*\log(\text{abs}(x))/a^5 - 1/3*(12*a*b^3*x^3 + 30*a^2*b^2*x^2 + 22*a^3*b*x + 3*a^4)/((b*x + a)^3*a^5*x)$

maple [A] time = 0.01, size = 69, normalized size = 0.99

$$-\frac{b}{3 (bx + a)^3 a^2} - \frac{b}{(bx + a)^2 a^3} - \frac{3b}{(bx + a) a^4} - \frac{4b \ln(x)}{a^5} + \frac{4b \ln (bx + a)}{a^5} - \frac{1}{a^4 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^4,x)

[Out] $-1/a^4/x - 1/3*b/a^2/(b*x+a)^3 - b/a^3/(b*x+a)^2 - 3*b/a^4/(b*x+a) - 4*b*\ln(x)/a^5 + 4*b*\ln(b*x+a)/a^5$

maxima [A] time = 1.40, size = 91, normalized size = 1.30

$$\frac{12 b^3 x^3 + 30 ab^2 x^2 + 22 a^2 b x + 3 a^3}{3 (a^4 b^3 x^4 + 3 a^5 b^2 x^3 + 3 a^6 b x^2 + a^7 x)} + \frac{4 b \log (bx + a)}{a^5} - \frac{4 b \log (x)}{a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^4,x, algorithm="maxima")

[Out] $-1/3*(12*b^3*x^3 + 30*a*b^2*x^2 + 22*a^2*b*x + 3*a^3)/(a^4*b^3*x^4 + 3*a^5*b^2*x^3 + 3*a^6*b*x^2 + a^7*x) + 4*b*\log(b*x + a)/a^5 - 4*b*\log(x)/a^5$

mupad [B] time = 0.08, size = 85, normalized size = 1.21

$$\frac{8b \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^5} - \frac{\frac{1}{a} + \frac{10b^2x^2}{a^3} + \frac{4b^3x^3}{a^4} + \frac{22bx}{3a^2}}{a^3x + 3a^2bx^2 + 3ab^2x^3 + b^3x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(a + b*x)^4),x)

[Out] $(8*b*\operatorname{atanh}((2*b*x)/a + 1))/a^5 - (1/a + (10*b^2*x^2)/a^3 + (4*b^3*x^3)/a^4 + (22*b*x)/(3*a^2))/(a^3*x + b^3*x^4 + 3*a^2*b*x^2 + 3*a*b^2*x^3)$

sympy [A] time = 0.46, size = 90, normalized size = 1.29

$$\frac{-3a^3 - 22a^2bx - 30ab^2x^2 - 12b^3x^3}{3a^7x + 9a^6bx^2 + 9a^5b^2x^3 + 3a^4b^3x^4} + \frac{4b(-\log(x) + \log(\frac{a}{b} + x))}{a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/(b*x+a)**4,x)

[Out] $(-3*a**3 - 22*a**2*b*x - 30*a*b**2*x**2 - 12*b**3*x**3)/(3*a**7*x + 9*a**6*b*x**2 + 9*a**5*b**2*x**3 + 3*a**4*b**3*x**4) + 4*b*(-\log(x) + \log(a/b + x))/a**5$

$$3.204 \quad \int \frac{1}{x^3(a+bx)^4} dx$$

Optimal. Leaf size=93

$$\frac{10b^2 \log(x)}{a^6} - \frac{10b^2 \log(a+bx)}{a^6} + \frac{6b^2}{a^5(a+bx)} + \frac{4b}{a^5x} + \frac{3b^2}{2a^4(a+bx)^2} - \frac{1}{2a^4x^2} + \frac{b^2}{3a^3(a+bx)^3}$$

[Out] $-1/2/a^4/x^2+4*b/a^5/x+1/3*b^2/a^3/(b*x+a)^3+3/2*b^2/a^4/(b*x+a)^2+6*b^2/a^5/(b*x+a)+10*b^2*\ln(x)/a^6-10*b^2*\ln(b*x+a)/a^6$

Rubi [A] time = 0.05, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{6b^2}{a^5(a+bx)} + \frac{3b^2}{2a^4(a+bx)^2} + \frac{b^2}{3a^3(a+bx)^3} + \frac{10b^2 \log(x)}{a^6} - \frac{10b^2 \log(a+bx)}{a^6} + \frac{4b}{a^5x} - \frac{1}{2a^4x^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(a + b*x)^4), x]

[Out] $-1/(2*a^4*x^2) + (4*b)/(a^5*x) + b^2/(3*a^3*(a + b*x)^3) + (3*b^2)/(2*a^4*(a + b*x)^2) + (6*b^2)/(a^5*(a + b*x)) + (10*b^2*\text{Log}[x])/a^6 - (10*b^2*\text{Log}[a + b*x])/a^6$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^3(a+bx)^4} dx &= \int \left(\frac{1}{a^4x^3} - \frac{4b}{a^5x^2} + \frac{10b^2}{a^6x} - \frac{b^3}{a^3(a+bx)^4} - \frac{3b^3}{a^4(a+bx)^3} - \frac{6b^3}{a^5(a+bx)^2} - \frac{10b^3}{a^6(a+bx)} \right) dx \\ &= -\frac{1}{2a^4x^2} + \frac{4b}{a^5x} + \frac{b^2}{3a^3(a+bx)^3} + \frac{3b^2}{2a^4(a+bx)^2} + \frac{6b^2}{a^5(a+bx)} + \frac{10b^2 \log(x)}{a^6} - \frac{10b^2 \log(a+bx)}{a^6} \end{aligned}$$

Mathematica [A] time = 0.06, size = 79, normalized size = 0.85

$$\frac{a(-3a^4+15a^3bx+110a^2b^2x^2+150ab^3x^3+60b^4x^4)}{x^2(a+bx)^3} - \frac{60b^2 \log(a+bx) + 60b^2 \log(x)}{6a^6}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)^4), x]

[Out] ((a*(-3*a^4 + 15*a^3*b*x + 110*a^2*b^2*x^2 + 150*a*b^3*x^3 + 60*b^4*x^4))/(x^2*(a + b*x)^3) + 60*b^2*Log[x] - 60*b^2*Log[a + b*x])/(6*a^6)

fricas [A] time = 0.48, size = 174, normalized size = 1.87

$$\frac{60 ab^4 x^4 + 150 a^2 b^3 x^3 + 110 a^3 b^2 x^2 + 15 a^4 b x - 3 a^5 - 60 (b^5 x^5 + 3 ab^4 x^4 + 3 a^2 b^3 x^3 + a^3 b^2 x^2) \log (bx + a) + 60}{6 (a^6 b^3 x^5 + 3 a^7 b^2 x^4 + 3 a^8 b x^3 + a^9 x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^4,x, algorithm="fricas")

[Out] 1/6*(60*a*b^4*x^4 + 150*a^2*b^3*x^3 + 110*a^3*b^2*x^2 + 15*a^4*b*x - 3*a^5 - 60*(b^5*x^5 + 3*a*b^4*x^4 + 3*a^2*b^3*x^3 + a^3*b^2*x^2)*log(b*x + a) + 60*(b^5*x^5 + 3*a*b^4*x^4 + 3*a^2*b^3*x^3 + a^3*b^2*x^2)*log(x))/(a^6*b^3*x^5 + 3*a^7*b^2*x^4 + 3*a^8*b*x^3 + a^9*x^2)

giac [A] time = 0.95, size = 86, normalized size = 0.92

$$-\frac{10 b^2 \log (|bx + a|)}{a^6} + \frac{10 b^2 \log (|x|)}{a^6} + \frac{60 ab^4 x^4 + 150 a^2 b^3 x^3 + 110 a^3 b^2 x^2 + 15 a^4 b x - 3 a^5}{6 (bx + a)^3 a^6 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^4,x, algorithm="giac")

[Out] -10*b^2*log(abs(b*x + a))/a^6 + 10*b^2*log(abs(x))/a^6 + 1/6*(60*a*b^4*x^4 + 150*a^2*b^3*x^3 + 110*a^3*b^2*x^2 + 15*a^4*b*x - 3*a^5)/((b*x + a)^3*a^6*x^2)

maple [A] time = 0.01, size = 88, normalized size = 0.95

$$\frac{b^2}{3 (bx + a)^3 a^3} + \frac{3b^2}{2 (bx + a)^2 a^4} + \frac{6b^2}{(bx + a) a^5} + \frac{10b^2 \ln(x)}{a^6} - \frac{10b^2 \ln (bx + a)}{a^6} + \frac{4b}{a^5 x} - \frac{1}{2a^4 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a)^4,x)

[Out] -1/2/a^4/x^2+4*b/a^5/x+1/3*b^2/a^3/(b*x+a)^3+3/2*b^2/a^4/(b*x+a)^2+6*b^2/a^5/(b*x+a)+10*b^2*ln(x)/a^6-10*b^2*ln(b*x+a)/a^6

maxima [A] time = 1.41, size = 108, normalized size = 1.16

$$\frac{60b^4x^4 + 150ab^3x^3 + 110a^2b^2x^2 + 15a^3bx - 3a^4}{6(a^5b^3x^5 + 3a^6b^2x^4 + 3a^7bx^3 + a^8x^2)} - \frac{10b^2 \log(bx + a)}{a^6} + \frac{10b^2 \log(x)}{a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^4,x, algorithm="maxima")

[Out] 1/6*(60*b^4*x^4 + 150*a*b^3*x^3 + 110*a^2*b^2*x^2 + 15*a^3*b*x - 3*a^4)/(a^5*b^3*x^5 + 3*a^6*b^2*x^4 + 3*a^7*b*x^3 + a^8*x^2) - 10*b^2*log(b*x + a)/a^6 + 10*b^2*log(x)/a^6

mupad [B] time = 0.14, size = 101, normalized size = 1.09

$$\frac{\frac{55b^2x^2}{3a^3} - \frac{1}{2a} + \frac{25b^3x^3}{a^4} + \frac{10b^4x^4}{a^5} + \frac{5bx}{2a^2}}{a^3x^2 + 3a^2bx^3 + 3ab^2x^4 + b^3x^5} - \frac{20b^2 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(a + b*x)^4),x)

[Out] ((55*b^2*x^2)/(3*a^3) - 1/(2*a) + (25*b^3*x^3)/a^4 + (10*b^4*x^4)/a^5 + (5*b*x)/(2*a^2))/(a^3*x^2 + b^3*x^5 + 3*a^2*b*x^3 + 3*a*b^2*x^4) - (20*b^2*atanh((2*b*x)/a + 1))/a^6

sympy [A] time = 0.56, size = 104, normalized size = 1.12

$$\frac{-3a^4 + 15a^3bx + 110a^2b^2x^2 + 150ab^3x^3 + 60b^4x^4}{6a^8x^2 + 18a^7bx^3 + 18a^6b^2x^4 + 6a^5b^3x^5} + \frac{10b^2(\log(x) - \log\left(\frac{a}{b} + x\right))}{a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(b*x+a)**4,x)

[Out] (-3*a**4 + 15*a**3*b*x + 110*a**2*b**2*x**2 + 150*a*b**3*x**3 + 60*b**4*x**4)/(6*a**8*x**2 + 18*a**7*b*x**3 + 18*a**6*b**2*x**4 + 6*a**5*b**3*x**5) + 10*b**2*(log(x) - log(a/b + x))/a**6

$$3.205 \quad \int \frac{1}{x^4(a+bx)^4} dx$$

Optimal. Leaf size=102

$$-\frac{20b^3 \log(x)}{a^7} + \frac{20b^3 \log(a+bx)}{a^7} - \frac{10b^3}{a^6(a+bx)} - \frac{10b^2}{a^6x} - \frac{2b^3}{a^5(a+bx)^2} + \frac{2b}{a^5x^2} - \frac{b^3}{3a^4(a+bx)^3} - \frac{1}{3a^4x^3}$$

[Out] $-1/3/a^4/x^3+2*b/a^5/x^2-10*b^2/a^6/x-1/3*b^3/a^4/(b*x+a)^3-2*b^3/a^5/(b*x+a)^2-10*b^3/a^6/(b*x+a)-20*b^3*\ln(x)/a^7+20*b^3*\ln(b*x+a)/a^7$

Rubi [A] time = 0.05, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{10b^3}{a^6(a+bx)} - \frac{2b^3}{a^5(a+bx)^2} - \frac{b^3}{3a^4(a+bx)^3} - \frac{10b^2}{a^6x} - \frac{20b^3 \log(x)}{a^7} + \frac{20b^3 \log(a+bx)}{a^7} + \frac{2b}{a^5x^2} - \frac{1}{3a^4x^3}$$

Antiderivative was successfully verified.

[In] Int[1/(x^4*(a + b*x)^4), x]

[Out] $-1/(3*a^4*x^3) + (2*b)/(a^5*x^2) - (10*b^2)/(a^6*x) - b^3/(3*a^4*(a + b*x)^3) - (2*b^3)/(a^5*(a + b*x)^2) - (10*b^3)/(a^6*(a + b*x)) - (20*b^3*\text{Log}[x])/a^7 + (20*b^3*\text{Log}[a + b*x])/a^7$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{x^4(a+bx)^4} dx = \int \left(\frac{1}{a^4x^4} - \frac{4b}{a^5x^3} + \frac{10b^2}{a^6x^2} - \frac{20b^3}{a^7x} + \frac{b^4}{a^4(a+bx)^4} + \frac{4b^4}{a^5(a+bx)^3} + \frac{10b^4}{a^6(a+bx)^2} + \frac{20b^4}{a^7(a+bx)} \right) dx$$

$$= -\frac{1}{3a^4x^3} + \frac{2b}{a^5x^2} - \frac{10b^2}{a^6x} - \frac{b^3}{3a^4(a+bx)^3} - \frac{2b^3}{a^5(a+bx)^2} - \frac{10b^3}{a^6(a+bx)} - \frac{20b^3 \log(x)}{a^7} + \frac{20b^3 \log(a+bx)}{a^7}$$

Mathematica [A] time = 0.06, size = 88, normalized size = 0.86

$$-\frac{a(a^5-3a^4bx+15a^3b^2x^2+110a^2b^3x^3+150ab^4x^4+60b^5x^5)}{x^3(a+bx)^3} - \frac{60b^3 \log(a+bx) + 60b^3 \log(x)}{3a^7}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^4*(a + b*x)^4), x]

[Out]
$$-1/3*((a*(a^5 - 3*a^4*b*x + 15*a^3*b^2*x^2 + 110*a^2*b^3*x^3 + 150*a*b^4*x^4 + 60*b^5*x^5))/(x^3*(a + b*x)^3) + 60*b^3*\text{Log}[x] - 60*b^3*\text{Log}[a + b*x])/a^7$$

fricas [A] time = 0.49, size = 183, normalized size = 1.79

$$\frac{60 ab^5 x^5 + 150 a^2 b^4 x^4 + 110 a^3 b^3 x^3 + 15 a^4 b^2 x^2 - 3 a^5 b x + a^6 - 60 (b^6 x^6 + 3 a b^5 x^5 + 3 a^2 b^4 x^4 + a^3 b^3 x^3) \log(bx + a)}{3 (a^7 b^3 x^6 + 3 a^8 b^2 x^5 + 3 a^9 b x^4 + a^{10} x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^4,x, algorithm="fricas")

[Out]
$$-1/3*(60*a*b^5*x^5 + 150*a^2*b^4*x^4 + 110*a^3*b^3*x^3 + 15*a^4*b^2*x^2 - 3*a^5*b*x + a^6 - 60*(b^6*x^6 + 3*a*b^5*x^5 + 3*a^2*b^4*x^4 + a^3*b^3*x^3)*\log(b*x + a) + 60*(b^6*x^6 + 3*a*b^5*x^5 + 3*a^2*b^4*x^4 + a^3*b^3*x^3)*\log(x))/(a^7*b^3*x^6 + 3*a^8*b^2*x^5 + 3*a^9*b*x^4 + a^{10}*x^3)$$

giac [A] time = 0.99, size = 93, normalized size = 0.91

$$\frac{20 b^3 \log(|bx + a|)}{a^7} - \frac{20 b^3 \log(|x|)}{a^7} - \frac{60 b^5 x^5 + 150 a b^4 x^4 + 110 a^2 b^3 x^3 + 15 a^3 b^2 x^2 - 3 a^4 b x + a^5}{3 (bx^2 + ax)^3 a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^4,x, algorithm="giac")

[Out]
$$20*b^3*\log(\text{abs}(b*x + a))/a^7 - 20*b^3*\log(\text{abs}(x))/a^7 - 1/3*(60*b^5*x^5 + 150*a*b^4*x^4 + 110*a^2*b^3*x^3 + 15*a^3*b^2*x^2 - 3*a^4*b*x + a^5)/((b*x^2 + a*x)^3*a^6)$$

maple [A] time = 0.01, size = 99, normalized size = 0.97

$$-\frac{b^3}{3 (bx + a)^3 a^4} - \frac{2b^3}{(bx + a)^2 a^5} - \frac{10b^3}{(bx + a) a^6} - \frac{20b^3 \ln(x)}{a^7} + \frac{20b^3 \ln(bx + a)}{a^7} - \frac{10b^2}{a^6 x} + \frac{2b}{a^5 x^2} - \frac{1}{3a^4 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^4/(b*x+a)^4,x)

[Out]
$$-1/3/a^4/x^3 + 2*b/a^5/x^2 - 10*b^2/a^6/x - 1/3*b^3/a^4/(b*x+a)^3 - 2*b^3/a^5/(b*x+a)^2 - 10*b^3/a^6/(b*x+a) - 20*b^3*\ln(x)/a^7 + 20*b^3*\ln(b*x+a)/a^7$$

maxima [A] time = 1.40, size = 117, normalized size = 1.15

$$\frac{60b^5x^5 + 150ab^4x^4 + 110a^2b^3x^3 + 15a^3b^2x^2 - 3a^4bx + a^5}{3(a^6b^3x^6 + 3a^7b^2x^5 + 3a^8bx^4 + a^9x^3)} + \frac{20b^3 \log(bx + a)}{a^7} - \frac{20b^3 \log(x)}{a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^4,x, algorithm="maxima")

[Out] -1/3*(60*b^5*x^5 + 150*a*b^4*x^4 + 110*a^2*b^3*x^3 + 15*a^3*b^2*x^2 - 3*a^4*b*x + a^5)/(a^6*b^3*x^6 + 3*a^7*b^2*x^5 + 3*a^8*b*x^4 + a^9*x^3) + 20*b^3*log(b*x + a)/a^7 - 20*b^3*log(x)/a^7

mupad [B] time = 0.10, size = 113, normalized size = 1.11

$$\frac{40b^3 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^7} - \frac{\frac{1}{3a} + \frac{5b^2x^2}{a^3} + \frac{110b^3x^3}{3a^4} + \frac{50b^4x^4}{a^5} + \frac{20b^5x^5}{a^6} - \frac{bx}{a^2}}{a^3x^3 + 3a^2bx^4 + 3ab^2x^5 + b^3x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^4*(a + b*x)^4),x)

[Out] (40*b^3*atanh((2*b*x)/a + 1))/a^7 - (1/(3*a) + (5*b^2*x^2)/a^3 + (110*b^3*x^3)/(3*a^4) + (50*b^4*x^4)/a^5 + (20*b^5*x^5)/a^6 - (b*x)/a^2)/(a^3*x^3 + b^3*x^6 + 3*a^2*b*x^4 + 3*a*b^2*x^5)

sympy [A] time = 0.53, size = 114, normalized size = 1.12

$$\frac{-a^5 + 3a^4bx - 15a^3b^2x^2 - 110a^2b^3x^3 - 150ab^4x^4 - 60b^5x^5}{3a^9x^3 + 9a^8bx^4 + 9a^7b^2x^5 + 3a^6b^3x^6} + \frac{20b^3(-\log(x) + \log\left(\frac{a}{b} + x\right))}{a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**4/(b*x+a)**4,x)

[Out] (-a**5 + 3*a**4*b*x - 15*a**3*b**2*x**2 - 110*a**2*b**3*x**3 - 150*a*b**4*x**4 - 60*b**5*x**5)/(3*a**9*x**3 + 9*a**8*b*x**4 + 9*a**7*b**2*x**5 + 3*a**6*b**3*x**6) + 20*b**3*(-log(x) + log(a/b + x))/a**7

$$3.206 \quad \int \frac{1}{x^5(a+bx)^4} dx$$

Optimal. Leaf size=117

$$\frac{35b^4 \log(x)}{a^8} - \frac{35b^4 \log(a+bx)}{a^8} + \frac{15b^4}{a^7(a+bx)} + \frac{20b^3}{a^7x} + \frac{5b^4}{2a^6(a+bx)^2} - \frac{5b^2}{a^6x^2} + \frac{b^4}{3a^5(a+bx)^3} + \frac{4b}{3a^5x^3} - \frac{1}{4a^4x^4}$$

[Out] $-1/4/a^4/x^4+4/3*b/a^5/x^3-5*b^2/a^6/x^2+20*b^3/a^7/x+1/3*b^4/a^5/(b*x+a)^3+5/2*b^4/a^6/(b*x+a)^2+15*b^4/a^7/(b*x+a)+35*b^4*ln(x)/a^8-35*b^4*ln(b*x+a)/a^8$

Rubi [A] time = 0.07, antiderivative size = 117, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{5b^2}{a^6x^2} + \frac{15b^4}{a^7(a+bx)} + \frac{5b^4}{2a^6(a+bx)^2} + \frac{b^4}{3a^5(a+bx)^3} + \frac{20b^3}{a^7x} + \frac{35b^4 \log(x)}{a^8} - \frac{35b^4 \log(a+bx)}{a^8} + \frac{4b}{3a^5x^3} - \frac{1}{4a^4x^4}$$

Antiderivative was successfully verified.

[In] Int[1/(x^5*(a + b*x)^4), x]

[Out] $-1/(4*a^4*x^4) + (4*b)/(3*a^5*x^3) - (5*b^2)/(a^6*x^2) + (20*b^3)/(a^7*x) + b^4/(3*a^5*(a + b*x)^3) + (5*b^4)/(2*a^6*(a + b*x)^2) + (15*b^4)/(a^7*(a + b*x)) + (35*b^4*Log[x])/a^8 - (35*b^4*Log[a + b*x])/a^8$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^5(a+bx)^4} dx &= \int \left(\frac{1}{a^4x^5} - \frac{4b}{a^5x^4} + \frac{10b^2}{a^6x^3} - \frac{20b^3}{a^7x^2} + \frac{35b^4}{a^8x} - \frac{b^5}{a^5(a+bx)^4} - \frac{5b^5}{a^6(a+bx)^3} - \frac{15b^5}{a^7(a+bx)^2} - \frac{35b^5}{a^8(a+bx)} \right) dx \\ &= -\frac{1}{4a^4x^4} + \frac{4b}{3a^5x^3} - \frac{5b^2}{a^6x^2} + \frac{20b^3}{a^7x} + \frac{b^4}{3a^5(a+bx)^3} + \frac{5b^4}{2a^6(a+bx)^2} + \frac{15b^4}{a^7(a+bx)} + \frac{35b^4 \log(x)}{a^8} \end{aligned}$$

Mathematica [A] time = 0.07, size = 101, normalized size = 0.86

$$\frac{a(-3a^6+7a^5bx-21a^4b^2x^2+105a^3b^3x^3+770a^2b^4x^4+1050ab^5x^5+420b^6x^6)}{x^4(a+bx)^3} - 420b^4 \log(a+bx) + 420b^4 \log(x)$$

$$12a^8$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^5*(a + b*x)^4), x]

[Out] ((a*(-3*a^6 + 7*a^5*b*x - 21*a^4*b^2*x^2 + 105*a^3*b^3*x^3 + 770*a^2*b^4*x^4 + 1050*a*b^5*x^5 + 420*b^6*x^6))/(x^4*(a + b*x)^3) + 420*b^4*Log[x] - 420*b^4*Log[a + b*x])/(12*a^8)

fricas [A] time = 0.45, size = 196, normalized size = 1.68

$$\frac{420 ab^6x^6 + 1050 a^2b^5x^5 + 770 a^3b^4x^4 + 105 a^4b^3x^3 - 21 a^5b^2x^2 + 7 a^6bx - 3 a^7 - 420 (b^7x^7 + 3 ab^6x^6 + 3 a^2b^5x^5)}{12 (a^8b^3x^7 + 3 a^9b^2x^6 + 3 a^{10}bx^5 + a^{11}x^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a)^4,x, algorithm="fricas")

[Out] 1/12*(420*a*b^6*x^6 + 1050*a^2*b^5*x^5 + 770*a^3*b^4*x^4 + 105*a^4*b^3*x^3 - 21*a^5*b^2*x^2 + 7*a^6*b*x - 3*a^7 - 420*(b^7*x^7 + 3*a*b^6*x^6 + 3*a^2*b^5*x^5 + a^3*b^4*x^4)*log(b*x + a) + 420*(b^7*x^7 + 3*a*b^6*x^6 + 3*a^2*b^5*x^5 + a^3*b^4*x^4)*log(x))/(a^8*b^3*x^7 + 3*a^9*b^2*x^6 + 3*a^10*b*x^5 + a^11*x^4)

giac [A] time = 1.00, size = 108, normalized size = 0.92

$$-\frac{35 b^4 \log(|bx + a|)}{a^8} + \frac{35 b^4 \log(|x|)}{a^8} + \frac{420 ab^6x^6 + 1050 a^2b^5x^5 + 770 a^3b^4x^4 + 105 a^4b^3x^3 - 21 a^5b^2x^2 + 7 a^6bx - 3 a^7}{12 (bx + a)^3 a^8 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a)^4,x, algorithm="giac")

[Out] -35*b^4*log(abs(b*x + a))/a^8 + 35*b^4*log(abs(x))/a^8 + 1/12*(420*a*b^6*x^6 + 1050*a^2*b^5*x^5 + 770*a^3*b^4*x^4 + 105*a^4*b^3*x^3 - 21*a^5*b^2*x^2 + 7*a^6*b*x - 3*a^7)/((b*x + a)^3*a^8*x^4)

maple [A] time = 0.01, size = 110, normalized size = 0.94

$$\frac{b^4}{3 (bx + a)^3 a^5} + \frac{5b^4}{2 (bx + a)^2 a^6} + \frac{15b^4}{(bx + a) a^7} + \frac{35b^4 \ln(x)}{a^8} - \frac{35b^4 \ln(bx + a)}{a^8} + \frac{20b^3}{a^7 x} - \frac{5b^2}{a^6 x^2} + \frac{4b}{3a^5 x^3} - \frac{1}{4a^4 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^5/(b*x+a)^4,x)

[Out] -1/4/a^4/x^4+4/3*b/a^5/x^3-5*b^2/a^6/x^2+20*b^3/a^7/x+1/3*b^4/a^5/(b*x+a)^3+5/2*b^4/a^6/(b*x+a)^2+15*b^4/a^7/(b*x+a)+35*b^4*ln(x)/a^8-35*b^4*ln(b*x+a)/a^8

maxima [A] time = 1.39, size = 130, normalized size = 1.11

$$\frac{420 b^6 x^6 + 1050 a b^5 x^5 + 770 a^2 b^4 x^4 + 105 a^3 b^3 x^3 - 21 a^4 b^2 x^2 + 7 a^5 b x - 3 a^6}{12 (a^7 b^3 x^7 + 3 a^8 b^2 x^6 + 3 a^9 b x^5 + a^{10} x^4)} - \frac{35 b^4 \log(bx + a)}{a^8} + \frac{35 b^4 \log(x)}{a^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(b*x+a)^4,x, algorithm="maxima")

[Out] 1/12*(420*b^6*x^6 + 1050*a*b^5*x^5 + 770*a^2*b^4*x^4 + 105*a^3*b^3*x^3 - 21*a^4*b^2*x^2 + 7*a^5*b*x - 3*a^6)/(a^7*b^3*x^7 + 3*a^8*b^2*x^6 + 3*a^9*b*x^5 + a^10*x^4) - 35*b^4*log(b*x + a)/a^8 + 35*b^4*log(x)/a^8

mupad [B] time = 0.17, size = 123, normalized size = 1.05

$$\frac{\frac{35 b^3 x^3}{4 a^4} - \frac{7 b^2 x^2}{4 a^3} - \frac{1}{4 a} + \frac{385 b^4 x^4}{6 a^5} + \frac{175 b^5 x^5}{2 a^6} + \frac{35 b^6 x^6}{a^7} + \frac{7 b x}{12 a^2}}{a^3 x^4 + 3 a^2 b x^5 + 3 a b^2 x^6 + b^3 x^7} - \frac{70 b^4 \operatorname{atanh}\left(\frac{2 b x}{a} + 1\right)}{a^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^5*(a + b*x)^4),x)

[Out] ((35*b^3*x^3)/(4*a^4) - (7*b^2*x^2)/(4*a^3) - 1/(4*a) + (385*b^4*x^4)/(6*a^5) + (175*b^5*x^5)/(2*a^6) + (35*b^6*x^6)/a^7 + (7*b*x)/(12*a^2))/(a^3*x^4 + b^3*x^7 + 3*a^2*b*x^5 + 3*a*b^2*x^6) - (70*b^4*atanh((2*b*x)/a + 1))/a^8

sympy [A] time = 0.58, size = 128, normalized size = 1.09

$$\frac{-3 a^6 + 7 a^5 b x - 21 a^4 b^2 x^2 + 105 a^3 b^3 x^3 + 770 a^2 b^4 x^4 + 1050 a b^5 x^5 + 420 b^6 x^6}{12 a^{10} x^4 + 36 a^9 b x^5 + 36 a^8 b^2 x^6 + 12 a^7 b^3 x^7} + \frac{35 b^4 (\log(x) - \log\left(\frac{a}{b} + x\right))}{a^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**5/(b*x+a)**4,x)

[Out] (-3*a**6 + 7*a**5*b*x - 21*a**4*b**2*x**2 + 105*a**3*b**3*x**3 + 770*a**2*b**4*x**4 + 1050*a*b**5*x**5 + 420*b**6*x**6)/(12*a**10*x**4 + 36*a**9*b*x**5 + 36*a**8*b**2*x**6 + 12*a**7*b**3*x**7) + 35*b**4*(log(x) - log(a/b + x))/a**8

3.207

$$\int \frac{x^{10}}{(a+bx)^7} dx$$

Optimal. Leaf size=150

$$-\frac{a^{10}}{6b^{11}(a+bx)^6} + \frac{2a^9}{b^{11}(a+bx)^5} - \frac{45a^8}{4b^{11}(a+bx)^4} + \frac{40a^7}{b^{11}(a+bx)^3} - \frac{105a^6}{b^{11}(a+bx)^2} + \frac{252a^5}{b^{11}(a+bx)} + \frac{210a^4 \log(a+bx)}{b^{11}} - \frac{84a^3}{b^{10}}$$

[Out] $-84*a^3*x/b^{10}+14*a^2*x^2/b^9-7/3*a*x^3/b^8+1/4*x^4/b^7-1/6*a^{10}/b^{11}/(b*x+a)^6+2*a^9/b^{11}/(b*x+a)^5-45/4*a^8/b^{11}/(b*x+a)^4+40*a^7/b^{11}/(b*x+a)^3-105*a^6/b^{11}/(b*x+a)^2+252*a^5/b^{11}/(b*x+a)+210*a^4*\ln(b*x+a)/b^{11}$

Rubi [A] time = 0.14, antiderivative size = 150, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{14a^2x^2}{b^9} - \frac{a^{10}}{6b^{11}(a+bx)^6} + \frac{2a^9}{b^{11}(a+bx)^5} - \frac{45a^8}{4b^{11}(a+bx)^4} + \frac{40a^7}{b^{11}(a+bx)^3} - \frac{105a^6}{b^{11}(a+bx)^2} + \frac{252a^5}{b^{11}(a+bx)} - \frac{84a^3x}{b^{10}} + \frac{210a^4 \log}{b^{11}}$$

Antiderivative was successfully verified.

[In] Int[x¹⁰/(a + b*x)⁷, x]

[Out] $(-84*a^3*x)/b^{10} + (14*a^2*x^2)/b^9 - (7*a*x^3)/(3*b^8) + x^4/(4*b^7) - a^{10}/(6*b^{11}*(a + b*x)^6) + (2*a^9)/(b^{11}*(a + b*x)^5) - (45*a^8)/(4*b^{11}*(a + b*x)^4) + (40*a^7)/(b^{11}*(a + b*x)^3) - (105*a^6)/(b^{11}*(a + b*x)^2) + (252*a^5)/(b^{11}*(a + b*x)) + (210*a^4*Log[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{x^{10}}{(a+bx)^7} dx = \int \left(-\frac{84a^3}{b^{10}} + \frac{28a^2x}{b^9} - \frac{7ax^2}{b^8} + \frac{x^3}{b^7} + \frac{a^{10}}{b^{10}(a+bx)^7} - \frac{10a^9}{b^{10}(a+bx)^6} + \frac{45a^8}{b^{10}(a+bx)^5} - \frac{120a^7}{b^{10}(a+bx)^4} \right. \\ \left. - \frac{84a^3x}{b^{10}} + \frac{14a^2x^2}{b^9} - \frac{7ax^3}{3b^8} + \frac{x^4}{4b^7} - \frac{a^{10}}{6b^{11}(a+bx)^6} + \frac{2a^9}{b^{11}(a+bx)^5} - \frac{45a^8}{4b^{11}(a+bx)^4} + \frac{40a^7}{b^{11}(a+bx)^3} \right) dx$$

Mathematica [A] time = 0.03, size = 139, normalized size = 0.93

$$\frac{2131a^{10} + 10266a^9bx + 18105a^8b^2x^2 + 11540a^7b^3x^3 - 3945a^6b^4x^4 - 9138a^5b^5x^5 - 4043a^4b^6x^6 + 2520a^4(a + bx)}{12b^{11}(a + bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^10/(a + b*x)^7,x]

[Out] (2131*a^10 + 10266*a^9*b*x + 18105*a^8*b^2*x^2 + 11540*a^7*b^3*x^3 - 3945*a^6*b^4*x^4 - 9138*a^5*b^5*x^5 - 4043*a^4*b^6*x^6 - 360*a^3*b^7*x^7 + 45*a^2*b^8*x^8 - 10*a*b^9*x^9 + 3*b^10*x^10 + 2520*a^4*(a + b*x)^6*Log[a + b*x])/ (12*b^11*(a + b*x)^6)

fricas [A] time = 0.49, size = 250, normalized size = 1.67

$$\frac{3b^{10}x^{10} - 10ab^9x^9 + 45a^2b^8x^8 - 360a^3b^7x^7 - 4043a^4b^6x^6 - 9138a^5b^5x^5 - 3945a^6b^4x^4 + 11540a^7b^3x^3 + 18105a^8b^2x^2 + 10266a^9bx + 2131a^{10}}{12(b^{17}x^6 + 6ab^{16}x^5 + 15a^2b^{15}x^4 + 20a^3b^{14}x^3 + 15a^4b^{13}x^2 + 6a^5b^{12}x + a^6b^{11})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^10/(b*x+a)^7,x, algorithm="fricas")

[Out] 1/12*(3*b^10*x^10 - 10*a*b^9*x^9 + 45*a^2*b^8*x^8 - 360*a^3*b^7*x^7 - 4043*a^4*b^6*x^6 - 9138*a^5*b^5*x^5 - 3945*a^6*b^4*x^4 + 11540*a^7*b^3*x^3 + 18105*a^8*b^2*x^2 + 10266*a^9*b*x + 2131*a^10 + 2520*(a^4*b^6*x^6 + 6*a^5*b^5*x^5 + 15*a^6*b^4*x^4 + 20*a^7*b^3*x^3 + 15*a^8*b^2*x^2 + 6*a^9*b*x + a^10)*log(b*x + a))/(b^17*x^6 + 6*a*b^16*x^5 + 15*a^2*b^15*x^4 + 20*a^3*b^14*x^3 + 15*a^4*b^13*x^2 + 6*a^5*b^12*x + a^6*b^11)

giac [A] time = 1.21, size = 128, normalized size = 0.85

$$\frac{210a^4 \log(|bx + a|)}{b^{11}} + \frac{3024a^5b^5x^5 + 13860a^6b^4x^4 + 25680a^7b^3x^3 + 23985a^8b^2x^2 + 11274a^9bx + 2131a^{10}}{12(bx + a)^6b^{11}} + \frac{3b^{10}x^{10} - 10ab^9x^9 + 45a^2b^8x^8 - 360a^3b^7x^7 - 4043a^4b^6x^6 - 9138a^5b^5x^5 - 3945a^6b^4x^4 + 11540a^7b^3x^3 + 18105a^8b^2x^2 + 10266a^9bx + 2131a^{10}}{12(b^{17}x^6 + 6ab^{16}x^5 + 15a^2b^{15}x^4 + 20a^3b^{14}x^3 + 15a^4b^{13}x^2 + 6a^5b^{12}x + a^6b^{11})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^10/(b*x+a)^7,x, algorithm="giac")

[Out] 210*a^4*log(abs(b*x + a))/b^11 + 1/12*(3024*a^5*b^5*x^5 + 13860*a^6*b^4*x^4 + 25680*a^7*b^3*x^3 + 23985*a^8*b^2*x^2 + 11274*a^9*b*x + 2131*a^10)/((b*x + a)^6*b^11) + 1/12*(3*b^21*x^4 - 28*a*b^20*x^3 + 168*a^2*b^19*x^2 - 1008*a^3*b^18*x)/b^28

maple [A] time = 0.01, size = 143, normalized size = 0.95

$$-\frac{a^{10}}{6(bx + a)^6b^{11}} + \frac{2a^9}{(bx + a)^5b^{11}} - \frac{45a^8}{4(bx + a)^4b^{11}} + \frac{x^4}{4b^7} + \frac{40a^7}{(bx + a)^3b^{11}} - \frac{7ax^3}{3b^8} - \frac{105a^6}{(bx + a)^2b^{11}} + \frac{14a^2x^2}{b^9} + \frac{252a^5}{(bx + a)b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^10/(b*x+a)^7,x)`

[Out] $-84a^3x/b^{10} + 14a^2x^2/b^9 - 7/3ax^3/b^8 + 1/4x^4/b^7 - 1/6a^{10}/b^{11}/(bx+a)^6 + 2a^9/b^{11}/(bx+a)^5 - 45/4a^8/b^{11}/(bx+a)^4 + 40a^7/b^{11}/(bx+a)^3 - 105a^6/b^{11}/(bx+a)^2 + 252a^5/b^{11}/(bx+a) + 210a^4 \ln(bx+a)/b^{11}$

maxima [A] time = 1.47, size = 180, normalized size = 1.20

$$\frac{3024a^5b^5x^5 + 13860a^6b^4x^4 + 25680a^7b^3x^3 + 23985a^8b^2x^2 + 11274a^9bx + 2131a^{10}}{12(b^{17}x^6 + 6ab^{16}x^5 + 15a^2b^{15}x^4 + 20a^3b^{14}x^3 + 15a^4b^{13}x^2 + 6a^5b^{12}x + a^6b^{11})} + \frac{210a^4 \log(bx+a)}{b^{11}} + \frac{3b^3x}{b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^10/(b*x+a)^7,x, algorithm="maxima")`

[Out] $1/12*(3024a^5b^5x^5 + 13860a^6b^4x^4 + 25680a^7b^3x^3 + 23985a^8b^2x^2 + 11274a^9bx + 2131a^{10})/(b^{17}x^6 + 6a^5b^{16}x^5 + 15a^4b^{15}x^4 + 20a^3b^{14}x^3 + 15a^2b^{13}x^2 + 6a^5b^{12}x + a^6b^{11}) + 210a^4 \log(bx+a)/b^{11} + 1/12*(3b^3x^4 - 28a^2b^2x^3 + 168a^2b^2x^2 - 1008a^3x)/b^{10}$

mupad [B] time = 1.09, size = 126, normalized size = 0.84

$$\frac{(a+bx)^4}{4} - \frac{10a(a+bx)^3}{3} + \frac{45a^2(a+bx)^2}{2} + \frac{252a^5}{a+bx} - \frac{105a^6}{(a+bx)^2} + \frac{40a^7}{(a+bx)^3} - \frac{45a^8}{4(a+bx)^4} + \frac{2a^9}{(a+bx)^5} - \frac{a^{10}}{6(a+bx)^6} + 210a^4 \ln(a+bx) - \frac{120a^3bx}{b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^10/(a+b*x)^7,x)`

[Out] $((a+b*x)^4/4 - (10*a*(a+b*x)^3)/3 + (45*a^2*(a+b*x)^2)/2 + (252*a^5)/(a+b*x) - (105*a^6)/(a+b*x)^2 + (40*a^7)/(a+b*x)^3 - (45*a^8)/(4*(a+b*x)^4) + (2*a^9)/(a+b*x)^5 - a^{10}/(6*(a+b*x)^6) + 210*a^4*\log(a+b*x) - 120*a^3*b*x)/b^{11}$

sympy [A] time = 0.93, size = 190, normalized size = 1.27

$$\frac{210a^4 \log(a+bx)}{b^{11}} - \frac{84a^3x}{b^{10}} + \frac{14a^2x^2}{b^9} - \frac{7ax^3}{3b^8} + \frac{2131a^{10} + 11274a^9bx + 23985a^8b^2x^2 + 25680a^7b^3x^3 + 13860a^6b^4x^4}{12a^6b^{11} + 72a^5b^{12}x + 180a^4b^{13}x^2 + 240a^3b^{14}x^3 + 180a^2b^{15}x^4 + 72ab^{16}x^5 + a^6b^{17}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**10/(b*x+a)**7,x)`

```
[Out] 210*a**4*log(a + b*x)/b**11 - 84*a**3*x/b**10 + 14*a**2*x**2/b**9 - 7*a*x**3/(3*b**8) + (2131*a**10 + 11274*a**9*b*x + 23985*a**8*b**2*x**2 + 25680*a**7*b**3*x**3 + 13860*a**6*b**4*x**4 + 3024*a**5*b**5*x**5)/(12*a**6*b**11 + 72*a**5*b**12*x + 180*a**4*b**13*x**2 + 240*a**3*b**14*x**3 + 180*a**2*b**15*x**4 + 72*a*b**16*x**5 + 12*b**17*x**6) + x**4/(4*b**7)
```

$$3.208 \quad \int \frac{x^9}{(a+bx)^7} dx$$

Optimal. Leaf size=139

$$\frac{a^9}{6b^{10}(a+bx)^6} - \frac{9a^8}{5b^{10}(a+bx)^5} + \frac{9a^7}{b^{10}(a+bx)^4} - \frac{28a^6}{b^{10}(a+bx)^3} + \frac{63a^5}{b^{10}(a+bx)^2} - \frac{126a^4}{b^{10}(a+bx)} - \frac{84a^3 \log(a+bx)}{b^{10}} + \frac{28a^2x}{b^9}$$

[Out] $28a^2x/b^9 - 7/2*a*x^2/b^8 + 1/3*x^3/b^7 + 1/6*a^9/b^{10}/(b*x+a)^6 - 9/5*a^8/b^{10}/(b*x+a)^5 + 9*a^7/b^{10}/(b*x+a)^4 - 28*a^6/b^{10}/(b*x+a)^3 + 63*a^5/b^{10}/(b*x+a)^2 - 126*a^4/b^{10}/(b*x+a) - 84*a^3*\ln(b*x+a)/b^{10}$

Rubi [A] time = 0.11, antiderivative size = 139, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^9}{6b^{10}(a+bx)^6} - \frac{9a^8}{5b^{10}(a+bx)^5} + \frac{9a^7}{b^{10}(a+bx)^4} - \frac{28a^6}{b^{10}(a+bx)^3} + \frac{63a^5}{b^{10}(a+bx)^2} - \frac{126a^4}{b^{10}(a+bx)} + \frac{28a^2x}{b^9} - \frac{84a^3 \log(a+bx)}{b^{10}}$$

Antiderivative was successfully verified.

[In] Int[x^9/(a + b*x)^7, x]

[Out] $(28a^2x)/b^9 - (7a*x^2)/(2*b^8) + x^3/(3*b^7) + a^9/(6*b^{10}*(a + b*x)^6) - (9*a^8)/(5*b^{10}*(a + b*x)^5) + (9*a^7)/(b^{10}*(a + b*x)^4) - (28*a^6)/(b^{10}*(a + b*x)^3) + (63*a^5)/(b^{10}*(a + b*x)^2) - (126*a^4)/(b^{10}*(a + b*x)) - (84*a^3*\text{Log}[a + b*x])/b^{10}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{x^9}{(a+bx)^7} dx = \int \left(\frac{28a^2}{b^9} - \frac{7ax}{b^8} + \frac{x^2}{b^7} - \frac{a^9}{b^9(a+bx)^7} + \frac{9a^8}{b^9(a+bx)^6} - \frac{36a^7}{b^9(a+bx)^5} + \frac{84a^6}{b^9(a+bx)^4} - \frac{126a^5}{b^9(a+bx)^3} \right. \\ \left. + \frac{28a^2x}{b^9} - \frac{7ax^2}{2b^8} + \frac{x^3}{3b^7} + \frac{a^9}{6b^{10}(a+bx)^6} - \frac{9a^8}{5b^{10}(a+bx)^5} + \frac{9a^7}{b^{10}(a+bx)^4} - \frac{28a^6}{b^{10}(a+bx)^3} + \frac{63a^5}{b^{10}(a+bx)^2} - \frac{126a^4}{b^{10}(a+bx)} - \frac{84a^3 \log(a+bx)}{b^{10}} \right) dx$$

Mathematica [A] time = 0.03, size = 128, normalized size = 0.92

$$\frac{2509a^9 + 12534a^8bx + 23775a^7b^2x^2 + 19100a^6b^3x^3 + 1725a^5b^4x^4 - 6870a^4b^5x^5 - 3665a^3b^6x^6 + 2520a^3(a + bx)^6}{30b^{10}(a + bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^9/(a + b*x)^7,x]

[Out]
$$-1/30*(2509*a^9 + 12534*a^8*b*x + 23775*a^7*b^2*x^2 + 19100*a^6*b^3*x^3 + 1725*a^5*b^4*x^4 - 6870*a^4*b^5*x^5 - 3665*a^3*b^6*x^6 - 360*a^2*b^7*x^7 + 45*a*b^8*x^8 - 10*b^9*x^9 + 2520*a^3*(a + b*x)^6*\text{Log}[a + b*x])/(b^{10}*(a + b*x)^6)$$

fricas [A] time = 0.47, size = 239, normalized size = 1.72

$$\frac{10b^9x^9 - 45ab^8x^8 + 360a^2b^7x^7 + 3665a^3b^6x^6 + 6870a^4b^5x^5 - 1725a^5b^4x^4 - 19100a^6b^3x^3 - 23775a^7b^2x^2 - 12534a^8bx + 2509a^9}{30(b^{16}x^6 + 6ab^{15}x^5 + 15a^2b^{14}x^4 + 20a^3b^{13}x^3 + 15a^4b^{12}x^2 + 6a^5b^{11}x + a^6b^{10})} \log(bx + a)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^9/(b*x+a)^7,x, algorithm="fricas")

[Out]
$$1/30*(10*b^9*x^9 - 45*a*b^8*x^8 + 360*a^2*b^7*x^7 + 3665*a^3*b^6*x^6 + 6870*a^4*b^5*x^5 - 1725*a^5*b^4*x^4 - 19100*a^6*b^3*x^3 - 23775*a^7*b^2*x^2 - 12534*a^8*b*x - 2509*a^9 - 2520*(a^3*b^6*x^6 + 6*a^4*b^5*x^5 + 15*a^5*b^4*x^4 + 20*a^6*b^3*x^3 + 15*a^7*b^2*x^2 + 6*a^8*b*x + a^9)*\text{log}(b*x + a))/(b^{16}*x^6 + 6*a*b^{15}*x^5 + 15*a^2*b^{14}*x^4 + 20*a^3*b^{13}*x^3 + 15*a^4*b^{12}*x^2 + 6*a^5*b^{11}*x + a^6*b^{10})$$

giac [A] time = 1.48, size = 117, normalized size = 0.84

$$\frac{84a^3 \log(|bx + a|)}{b^{10}} - \frac{3780a^4b^5x^5 + 17010a^5b^4x^4 + 31080a^6b^3x^3 + 28710a^7b^2x^2 + 13374a^8bx + 2509a^9}{30(bx + a)^6b^{10}} + \frac{2b^{10}}{30(bx + a)^6b^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^9/(b*x+a)^7,x, algorithm="giac")

[Out]
$$-84*a^3*\text{log}(\text{abs}(b*x + a))/b^{10} - 1/30*(3780*a^4*b^5*x^5 + 17010*a^5*b^4*x^4 + 31080*a^6*b^3*x^3 + 28710*a^7*b^2*x^2 + 13374*a^8*b*x + 2509*a^9)/((b*x + a)^6*b^{10}) + 1/6*(2*b^{14}*x^3 - 21*a*b^{13}*x^2 + 168*a^2*b^{12}*x)/b^{21}$$

maple [A] time = 0.01, size = 132, normalized size = 0.95

$$\frac{a^9}{6(bx + a)^6b^{10}} - \frac{9a^8}{5(bx + a)^5b^{10}} + \frac{9a^7}{(bx + a)^4b^{10}} - \frac{28a^6}{(bx + a)^3b^{10}} + \frac{x^3}{3b^7} + \frac{63a^5}{(bx + a)^2b^{10}} - \frac{7ax^2}{2b^8} - \frac{126a^4}{(bx + a)b^{10}} - \frac{84a^3 \ln(|bx + a|)}{b^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^9/(b*x+a)^7,x)`

[Out] $28*a^2*x/b^9 - 7/2*a*x^2/b^8 + 1/3*x^3/b^7 + 1/6*a^9/b^{10}/(b*x+a)^6 - 9/5*a^8/b^{10}/(b*x+a)^5 + 9*a^7/b^{10}/(b*x+a)^4 - 28*a^6/b^{10}/(b*x+a)^3 + 63*a^5/b^{10}/(b*x+a)^2 - 126*a^4/b^{10}/(b*x+a) - 84*a^3*\ln(b*x+a)/b^{10}$

maxima [A] time = 1.59, size = 169, normalized size = 1.22

$$\frac{3780 a^4 b^5 x^5 + 17010 a^5 b^4 x^4 + 31080 a^6 b^3 x^3 + 28710 a^7 b^2 x^2 + 13374 a^8 b x + 2509 a^9}{30 (b^{16} x^6 + 6 a b^{15} x^5 + 15 a^2 b^{14} x^4 + 20 a^3 b^{13} x^3 + 15 a^4 b^{12} x^2 + 6 a^5 b^{11} x + a^6 b^{10})} - \frac{84 a^3 \log(bx + a)}{b^{10}} + \frac{2 b^2 x^2}{b^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^9/(b*x+a)^7,x, algorithm="maxima")`

[Out] $-1/30*(3780*a^4*b^5*x^5 + 17010*a^5*b^4*x^4 + 31080*a^6*b^3*x^3 + 28710*a^7*b^2*x^2 + 13374*a^8*b*x + 2509*a^9)/(b^{16}*x^6 + 6*a*b^{15}*x^5 + 15*a^2*b^{14}*x^4 + 20*a^3*b^{13}*x^3 + 15*a^4*b^{12}*x^2 + 6*a^5*b^{11}*x + a^6*b^{10}) - 84*a^3*log(b*x + a)/b^{10} + 1/6*(2*b^2*x^3 - 21*a*b*x^2 + 168*a^2*x)/b^9$

mupad [B] time = 0.55, size = 115, normalized size = 0.83

$$\frac{\frac{9 a (a+b x)^2}{2} - \frac{(a+b x)^3}{3} + \frac{126 a^4}{a+b x} - \frac{63 a^5}{(a+b x)^2} + \frac{28 a^6}{(a+b x)^3} - \frac{9 a^7}{(a+b x)^4} + \frac{9 a^8}{5 (a+b x)^5} - \frac{a^9}{6 (a+b x)^6} + 84 a^3 \ln(a+b x) - 36 a^2 b x}{b^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^9/(a + b*x)^7,x)`

[Out] $-((9*a*(a + b*x)^2)/2 - (a + b*x)^3/3 + (126*a^4)/(a + b*x) - (63*a^5)/(a + b*x)^2 + (28*a^6)/(a + b*x)^3 - (9*a^7)/(a + b*x)^4 + (9*a^8)/(5*(a + b*x)^5) - a^9/(6*(a + b*x)^6) + 84*a^3*\log(a + b*x) - 36*a^2*b*x)/b^{10}$

sympy [A] time = 0.91, size = 180, normalized size = 1.29

$$-\frac{84 a^3 \log(a+b x)}{b^{10}} + \frac{28 a^2 x}{b^9} - \frac{7 a x^2}{2 b^8} + \frac{-2509 a^9 - 13374 a^8 b x - 28710 a^7 b^2 x^2 - 31080 a^6 b^3 x^3 - 17010 a^5 b^4 x^4 - 3780 a^4 b^5 x^5}{30 a^6 b^{10} + 180 a^5 b^{11} x + 450 a^4 b^{12} x^2 + 600 a^3 b^{13} x^3 + 450 a^2 b^{14} x^4 + 180 a b^{15} x^5 - 3780 a^4 b^5 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**9/(b*x+a)**7,x)`

[Out] $-84*a**3*\log(a + b*x)/b**10 + 28*a**2*x/b**9 - 7*a*x**2/(2*b**8) + (-2509*a**9 - 13374*a**8*b*x - 28710*a**7*b**2*x**2 - 31080*a**6*b**3*x**3 - 17010*a**5*b**4*x**4 - 3780*a**4*b**5*x**5)/(30*a**6*b**10 + 180*a**5*b**11*x + 450*a**4*b**12*x**2 + 600*a**3*b**13*x**3 + 450*a**2*b**14*x**4 + 180*a*b**15*x**5 + 30*b**16*x**6) + x**3/(3*b**7)$

$$3.209 \quad \int \frac{x^8}{(a+bx)^7} dx$$

Optimal. Leaf size=128

$$-\frac{a^8}{6b^9(a+bx)^6} + \frac{8a^7}{5b^9(a+bx)^5} - \frac{7a^6}{b^9(a+bx)^4} + \frac{56a^5}{3b^9(a+bx)^3} - \frac{35a^4}{b^9(a+bx)^2} + \frac{56a^3}{b^9(a+bx)} + \frac{28a^2 \log(a+bx)}{b^9} - \frac{7ax}{b^8} + \frac{x^2}{2b^7}$$

[Out] $-7*a*x/b^8 + 1/2*x^2/b^7 - 1/6*a^8/b^9/(b*x+a)^6 + 8/5*a^7/b^9/(b*x+a)^5 - 7*a^6/b^9/(b*x+a)^4 + 56/3*a^5/b^9/(b*x+a)^3 - 35*a^4/b^9/(b*x+a)^2 + 56*a^3/b^9/(b*x+a) + 28*a^2*\ln(b*x+a)/b^9$

Rubi [A] time = 0.09, antiderivative size = 128, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^8}{6b^9(a+bx)^6} + \frac{8a^7}{5b^9(a+bx)^5} - \frac{7a^6}{b^9(a+bx)^4} + \frac{56a^5}{3b^9(a+bx)^3} - \frac{35a^4}{b^9(a+bx)^2} + \frac{56a^3}{b^9(a+bx)} + \frac{28a^2 \log(a+bx)}{b^9} - \frac{7ax}{b^8} + \frac{x^2}{2b^7}$$

Antiderivative was successfully verified.

[In] Int[x^8/(a + b*x)^7, x]

[Out] $(-7*a*x)/b^8 + x^2/(2*b^7) - a^8/(6*b^9*(a + b*x)^6) + (8*a^7)/(5*b^9*(a + b*x)^5) - (7*a^6)/(b^9*(a + b*x)^4) + (56*a^5)/(3*b^9*(a + b*x)^3) - (35*a^4)/(b^9*(a + b*x)^2) + (56*a^3)/(b^9*(a + b*x)) + (28*a^2*\text{Log}[a + b*x])/b^9$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{x^8}{(a+bx)^7} dx = \int \left(-\frac{7a}{b^8} + \frac{x}{b^7} + \frac{a^8}{b^8(a+bx)^7} - \frac{8a^7}{b^8(a+bx)^6} + \frac{28a^6}{b^8(a+bx)^5} - \frac{56a^5}{b^8(a+bx)^4} + \frac{70a^4}{b^8(a+bx)^3} - \frac{56a^3}{b^8(a+bx)^2} + \frac{7ax}{b^8} + \frac{x^2}{2b^7} - \frac{a^8}{6b^9(a+bx)^6} + \frac{8a^7}{5b^9(a+bx)^5} - \frac{7a^6}{b^9(a+bx)^4} + \frac{56a^5}{3b^9(a+bx)^3} - \frac{35a^4}{b^9(a+bx)^2} + \frac{56a^3}{b^9(a+bx)} + \frac{28a^2 \log(a+bx)}{b^9} - \frac{7ax}{b^8} + \frac{x^2}{2b^7} \right) dx$$

Mathematica [A] time = 0.05, size = 104, normalized size = 0.81

$$\frac{-\frac{5a^8}{(a+bx)^6} + \frac{48a^7}{(a+bx)^5} - \frac{210a^6}{(a+bx)^4} + \frac{560a^5}{(a+bx)^3} - \frac{1050a^4}{(a+bx)^2} + \frac{1680a^3}{a+bx} + 840a^2 \log(a+bx) - 210abx + 15b^2x^2}{30b^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^8/(a + b*x)^7,x]

[Out] $(-210*a*b*x + 15*b^2*x^2 - (5*a^8)/(a + b*x)^6 + (48*a^7)/(a + b*x)^5 - (210*a^6)/(a + b*x)^4 + (560*a^5)/(a + b*x)^3 - (1050*a^4)/(a + b*x)^2 + (1680*a^3)/(a + b*x) + 840*a^2*\text{Log}[a + b*x])/(30*b^9)$

fricas [A] time = 0.47, size = 228, normalized size = 1.78

$$\frac{15 b^8 x^8 - 120 a b^7 x^7 - 1035 a^2 b^6 x^6 - 1170 a^3 b^5 x^5 + 3375 a^4 b^4 x^4 + 10100 a^5 b^3 x^3 + 10725 a^6 b^2 x^2 + 5298 a^7 b x + 1023 a^8}{30 (b^{15} x^6 + 6 a b^{14} x^5 + 15 a^2 b^{13} x^4 + 20 a^3 b^{12} x^3 + 15 a^4 b^{11} x^2 + 6 a^5 b^{10} x + a^6 b^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8/(b*x+a)^7,x, algorithm="fricas")

[Out] $1/30*(15*b^8*x^8 - 120*a*b^7*x^7 - 1035*a^2*b^6*x^6 - 1170*a^3*b^5*x^5 + 3375*a^4*b^4*x^4 + 10100*a^5*b^3*x^3 + 10725*a^6*b^2*x^2 + 5298*a^7*b*x + 1023*a^8 + 840*(a^2*b^6*x^6 + 6*a^3*b^5*x^5 + 15*a^4*b^4*x^4 + 20*a^5*b^3*x^3 + 15*a^6*b^2*x^2 + 6*a^7*b*x + a^8)*\text{log}(b*x + a))/(b^{15}*x^6 + 6*a*b^{14}*x^5 + 15*a^2*b^{13}*x^4 + 20*a^3*b^{12}*x^3 + 15*a^4*b^{11}*x^2 + 6*a^5*b^{10}*x + a^6*b^9)$

giac [A] time = 1.07, size = 105, normalized size = 0.82

$$\frac{28 a^2 \log(|bx + a|)}{b^9} + \frac{b^7 x^2 - 14 a b^6 x}{2 b^{14}} + \frac{1680 a^3 b^5 x^5 + 7350 a^4 b^4 x^4 + 13160 a^5 b^3 x^3 + 11970 a^6 b^2 x^2 + 5508 a^7 b x + 1023 a^8}{30 (bx + a)^6 b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8/(b*x+a)^7,x, algorithm="giac")

[Out] $28*a^2*\text{log}(\text{abs}(b*x + a))/b^9 + 1/2*(b^7*x^2 - 14*a*b^6*x)/b^{14} + 1/30*(1680*a^3*b^5*x^5 + 7350*a^4*b^4*x^4 + 13160*a^5*b^3*x^3 + 11970*a^6*b^2*x^2 + 5508*a^7*b*x + 1023*a^8)/((b*x + a)^6*b^9)$

maple [A] time = 0.01, size = 121, normalized size = 0.95

$$-\frac{a^8}{6 (bx + a)^6 b^9} + \frac{8a^7}{5 (bx + a)^5 b^9} - \frac{7a^6}{(bx + a)^4 b^9} + \frac{56a^5}{3 (bx + a)^3 b^9} - \frac{35a^4}{(bx + a)^2 b^9} + \frac{x^2}{2b^7} + \frac{56a^3}{(bx + a)b^9} + \frac{28a^2 \ln(bx + a)}{b^9} - \frac{7a}{b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^8/(b*x+a)^7,x)

[Out] $-7ax/b^8 + 1/2x^2/b^7 - 1/6a^8/b^9/(bx+a)^6 + 8/5a^7/b^9/(bx+a)^5 - 7a^6/b^9/(bx+a)^4 + 56/3a^5/b^9/(bx+a)^3 - 35a^4/b^9/(bx+a)^2 + 56a^3/b^9/(bx+a) + 28a^2 \ln(bx+a)/b^9$

maxima [A] time = 1.56, size = 157, normalized size = 1.23

$$\frac{1680a^3b^5x^5 + 7350a^4b^4x^4 + 13160a^5b^3x^3 + 11970a^6b^2x^2 + 5508a^7bx + 1023a^8}{30(b^{15}x^6 + 6ab^{14}x^5 + 15a^2b^{13}x^4 + 20a^3b^{12}x^3 + 15a^4b^{11}x^2 + 6a^5b^{10}x + a^6b^9)} + \frac{28a^2 \log(bx+a)}{b^9} + \frac{bx^2 - 14bx}{2b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8/(b*x+a)^7,x, algorithm="maxima")

[Out] $1/30*(1680a^3b^5x^5 + 7350a^4b^4x^4 + 13160a^5b^3x^3 + 11970a^6b^2x^2 + 5508a^7bx + 1023a^8)/(b^{15}x^6 + 6a*b^{14}x^5 + 15a^2*b^{13}x^4 + 20a^3*b^{12}x^3 + 15a^4*b^{11}x^2 + 6a^5*b^{10}x + a^6*b^9) + 28a^2 \log(bx+a)/b^9 + 1/2*(b*x^2 - 14*a*x)/b^8$

mupad [B] time = 0.18, size = 102, normalized size = 0.80

$$\frac{\frac{(a+bx)^2}{2} + \frac{56a^3}{a+bx} - \frac{35a^4}{(a+bx)^2} + \frac{56a^5}{3(a+bx)^3} - \frac{7a^6}{(a+bx)^4} + \frac{8a^7}{5(a+bx)^5} - \frac{a^8}{6(a+bx)^6} + 28a^2 \ln(a+bx) - 8abx}{b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^8/(a + b*x)^7,x)

[Out] $((a + b*x)^2/2 + (56*a^3)/(a + b*x) - (35*a^4)/(a + b*x)^2 + (56*a^5)/(3*(a + b*x)^3) - (7*a^6)/(a + b*x)^4 + (8*a^7)/(5*(a + b*x)^5) - a^8/(6*(a + b*x)^6) + 28*a^2*\log(a + b*x) - 8*a*b*x)/b^9$

sympy [A] time = 0.84, size = 165, normalized size = 1.29

$$\frac{28a^2 \log(a+bx)}{b^9} - \frac{7ax}{b^8} + \frac{1023a^8 + 5508a^7bx + 11970a^6b^2x^2 + 13160a^5b^3x^3 + 7350a^4b^4x^4 + 1680a^3b^5x^5}{30a^6b^9 + 180a^5b^{10}x + 450a^4b^{11}x^2 + 600a^3b^{12}x^3 + 450a^2b^{13}x^4 + 180ab^{14}x^5 + 30b^{15}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**8/(b*x+a)**7,x)

[Out] $28a**2*\log(a + b*x)/b**9 - 7*a*x/b**8 + (1023*a**8 + 5508*a**7*b*x + 11970*a**6*b**2*x**2 + 13160*a**5*b**3*x**3 + 7350*a**4*b**4*x**4 + 1680*a**3*b**5*x**5)/(30*a**6*b**9 + 180*a**5*b**10*x + 450*a**4*b**11*x**2 + 600*a**3*b**12*x**3 + 450*a**2*b**13*x**4 + 180*a*b**14*x**5 + 30*b**15*x**6) + x**2/(2*b**7)$

$$3.210 \quad \int \frac{x^7}{(a+bx)^7} dx$$

Optimal. Leaf size=118

$$\frac{a^7}{6b^8(a+bx)^6} - \frac{7a^6}{5b^8(a+bx)^5} + \frac{21a^5}{4b^8(a+bx)^4} - \frac{35a^4}{3b^8(a+bx)^3} + \frac{35a^3}{2b^8(a+bx)^2} - \frac{21a^2}{b^8(a+bx)} - \frac{7a \log(a+bx)}{b^8} + \frac{x}{b^7}$$

[Out] $x/b^7 + 1/6*a^7/b^8/(b*x+a)^6 - 7/5*a^6/b^8/(b*x+a)^5 + 21/4*a^5/b^8/(b*x+a)^4 - 35/3*a^4/b^8/(b*x+a)^3 + 35/2*a^3/b^8/(b*x+a)^2 - 21*a^2/b^8/(b*x+a) - 7*a*\ln(b*x+a)/b^8$

Rubi [A] time = 0.07, antiderivative size = 118, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^7}{6b^8(a+bx)^6} - \frac{7a^6}{5b^8(a+bx)^5} + \frac{21a^5}{4b^8(a+bx)^4} - \frac{35a^4}{3b^8(a+bx)^3} + \frac{35a^3}{2b^8(a+bx)^2} - \frac{21a^2}{b^8(a+bx)} - \frac{7a \log(a+bx)}{b^8} + \frac{x}{b^7}$$

Antiderivative was successfully verified.

[In] Int[x^7/(a + b*x)^7, x]

[Out] $x/b^7 + a^7/(6*b^8*(a + b*x)^6) - (7*a^6)/(5*b^8*(a + b*x)^5) + (21*a^5)/(4*b^8*(a + b*x)^4) - (35*a^4)/(3*b^8*(a + b*x)^3) + (35*a^3)/(2*b^8*(a + b*x)^2) - (21*a^2)/(b^8*(a + b*x)) - (7*a*\text{Log}[a + b*x])/b^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^7}{(a+bx)^7} dx &= \int \left(\frac{1}{b^7} - \frac{a^7}{b^7(a+bx)^7} + \frac{7a^6}{b^7(a+bx)^6} - \frac{21a^5}{b^7(a+bx)^5} + \frac{35a^4}{b^7(a+bx)^4} - \frac{35a^3}{b^7(a+bx)^3} + \frac{21a^2}{b^7(a+bx)^2} \right. \\ &= \frac{x}{b^7} + \frac{a^7}{6b^8(a+bx)^6} - \frac{7a^6}{5b^8(a+bx)^5} + \frac{21a^5}{4b^8(a+bx)^4} - \frac{35a^4}{3b^8(a+bx)^3} + \frac{35a^3}{2b^8(a+bx)^2} - \frac{21a^2}{b^8(a+bx)} \end{aligned}$$

Mathematica [A] time = 0.03, size = 104, normalized size = 0.88

$$\frac{669a^7 + 3594a^6bx + 7725a^5b^2x^2 + 8200a^4b^3x^3 + 4050a^3b^4x^4 + 360a^2b^5x^5 - 360ab^6x^6 + 420a(a+bx)^6 \log(a+bx)}{60b^8(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^7/(a + b*x)^7,x]

[Out]
$$-1/60*(669*a^7 + 3594*a^6*b*x + 7725*a^5*b^2*x^2 + 8200*a^4*b^3*x^3 + 4050*a^3*b^4*x^4 + 360*a^2*b^5*x^5 - 360*a*b^6*x^6 - 60*b^7*x^7 + 420*a*(a + b*x)^6*\text{Log}[a + b*x])/(b^8*(a + b*x)^6)$$

fricas [A] time = 0.44, size = 215, normalized size = 1.82

$$\frac{60 b^7 x^7 + 360 a b^6 x^6 - 360 a^2 b^5 x^5 - 4050 a^3 b^4 x^4 - 8200 a^4 b^3 x^3 - 7725 a^5 b^2 x^2 - 3594 a^6 b x - 669 a^7 - 420 (a b^6 x + a^2 b^5 x^2 + 15 a^3 b^4 x^3 + 20 a^4 b^3 x^4 + 15 a^5 b^2 x^5 + 6 a^6 b x^6 + a^7) \log(b x + a)}{60 (b^{14} x^6 + 6 a b^{13} x^5 + 15 a^2 b^{12} x^4 + 20 a^3 b^{11} x^3 + 15 a^4 b^{10} x^2 + 6 a^5 b^9 x + a^6 b^8)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^7,x, algorithm="fricas")

[Out]
$$1/60*(60*b^7*x^7 + 360*a*b^6*x^6 - 360*a^2*b^5*x^5 - 4050*a^3*b^4*x^4 - 8200*a^4*b^3*x^3 - 7725*a^5*b^2*x^2 - 3594*a^6*b*x - 669*a^7 - 420*(a*b^6*x^6 + 6*a^2*b^5*x^5 + 15*a^3*b^4*x^4 + 20*a^4*b^3*x^3 + 15*a^5*b^2*x^2 + 6*a^6*b*x + a^7)*\text{log}(b*x + a))/(b^{14}*x^6 + 6*a*b^{13}*x^5 + 15*a^2*b^{12}*x^4 + 20*a^3*b^{11}*x^3 + 15*a^4*b^{10}*x^2 + 6*a^5*b^9*x + a^6*b^8)$$

giac [A] time = 0.92, size = 88, normalized size = 0.75

$$\frac{x}{b^7} - \frac{7 a \log(|b x + a|)}{b^8} - \frac{1260 a^2 b^5 x^5 + 5250 a^3 b^4 x^4 + 9100 a^4 b^3 x^3 + 8085 a^5 b^2 x^2 + 3654 a^6 b x + 669 a^7}{60 (b x + a)^6 b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^7,x, algorithm="giac")

[Out]
$$x/b^7 - 7*a*\text{log}(\text{abs}(b*x + a))/b^8 - 1/60*(1260*a^2*b^5*x^5 + 5250*a^3*b^4*x^4 + 9100*a^4*b^3*x^3 + 8085*a^5*b^2*x^2 + 3654*a^6*b*x + 669*a^7)/((b*x + a)^6*b^8)$$

maple [A] time = 0.01, size = 109, normalized size = 0.92

$$\frac{a^7}{6 (b x + a)^6 b^8} - \frac{7 a^6}{5 (b x + a)^5 b^8} + \frac{21 a^5}{4 (b x + a)^4 b^8} - \frac{35 a^4}{3 (b x + a)^3 b^8} + \frac{35 a^3}{2 (b x + a)^2 b^8} - \frac{21 a^2}{(b x + a) b^8} - \frac{7 a \ln(b x + a)}{b^8} + \frac{x}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7/(b*x+a)^7,x)

[Out]
$$x/b^7 + 1/6*a^7/b^8/(b*x+a)^6 - 7/5*a^6/b^8/(b*x+a)^5 + 21/4*a^5/b^8/(b*x+a)^4 - 35/3*a^4/b^8/(b*x+a)^3 + 35/2*a^3/b^8/(b*x+a)^2 - 21*a^2/b^8/(b*x+a) - 7*a*\ln(b*x+a)/b^8$$

maxima [A] time = 1.49, size = 145, normalized size = 1.23

$$\frac{1260 a^2 b^5 x^5 + 5250 a^3 b^4 x^4 + 9100 a^4 b^3 x^3 + 8085 a^5 b^2 x^2 + 3654 a^6 b x + 669 a^7}{60 (b^{14} x^6 + 6 a b^{13} x^5 + 15 a^2 b^{12} x^4 + 20 a^3 b^{11} x^3 + 15 a^4 b^{10} x^2 + 6 a^5 b^9 x + a^6 b^8)} + \frac{x}{b^7} - \frac{7 a \log (b x + a)}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^7,x, algorithm="maxima")

[Out]
$$-1/60*(1260*a^2*b^5*x^5 + 5250*a^3*b^4*x^4 + 9100*a^4*b^3*x^3 + 8085*a^5*b^2*x^2 + 3654*a^6*b*x + 669*a^7)/(b^{14}*x^6 + 6*a*b^{13}*x^5 + 15*a^2*b^{12}*x^4 + 20*a^3*b^{11}*x^3 + 15*a^4*b^{10}*x^2 + 6*a^5*b^9*x + a^6*b^8) + x/b^7 - 7*a*\log(b*x + a)/b^8$$

mupad [B] time = 0.34, size = 91, normalized size = 0.77

$$\frac{7 a \ln (a + b x) - b x + \frac{21 a^2}{a+b x} - \frac{35 a^3}{2(a+b x)^2} + \frac{35 a^4}{3(a+b x)^3} - \frac{21 a^5}{4(a+b x)^4} + \frac{7 a^6}{5(a+b x)^5} - \frac{a^7}{6(a+b x)^6}}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7/(a + b*x)^7,x)

[Out]
$$-(7*a*\log(a + b*x) - b*x + (21*a^2)/(a + b*x) - (35*a^3)/(2*(a + b*x)^2) + (35*a^4)/(3*(a + b*x)^3) - (21*a^5)/(4*(a + b*x)^4) + (7*a^6)/(5*(a + b*x)^5) - a^7/(6*(a + b*x)^6))/b^8$$

sympy [A] time = 0.82, size = 153, normalized size = 1.30

$$-\frac{7 a \log (a + b x)}{b^8} + \frac{-669 a^7 - 3654 a^6 b x - 8085 a^5 b^2 x^2 - 9100 a^4 b^3 x^3 - 5250 a^3 b^4 x^4 - 1260 a^2 b^5 x^5}{60 a^6 b^8 + 360 a^5 b^9 x + 900 a^4 b^{10} x^2 + 1200 a^3 b^{11} x^3 + 900 a^2 b^{12} x^4 + 360 a b^{13} x^5 + 60 b^{14} x^6} + \frac{x}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**7/(b*x+a)**7,x)

[Out]
$$-7*a*\log(a + b*x)/b**8 + (-669*a**7 - 3654*a**6*b*x - 8085*a**5*b**2*x**2 - 9100*a**4*b**3*x**3 - 5250*a**3*b**4*x**4 - 1260*a**2*b**5*x**5)/(60*a**6*b**8 + 360*a**5*b**9*x + 900*a**4*b**10*x**2 + 1200*a**3*b**11*x**3 + 900*a**2*b**12*x**4 + 360*a*b**13*x**5 + 60*b**14*x**6) + x/b**7$$

$$3.211 \quad \int \frac{x^6}{(a+bx)^7} dx$$

Optimal. Leaf size=109

$$-\frac{a^6}{6b^7(a+bx)^6} + \frac{6a^5}{5b^7(a+bx)^5} - \frac{15a^4}{4b^7(a+bx)^4} + \frac{20a^3}{3b^7(a+bx)^3} - \frac{15a^2}{2b^7(a+bx)^2} + \frac{6a}{b^7(a+bx)} + \frac{\log(a+bx)}{b^7}$$

[Out] $-1/6*a^6/b^7/(b*x+a)^6+6/5*a^5/b^7/(b*x+a)^5-15/4*a^4/b^7/(b*x+a)^4+20/3*a^3/b^7/(b*x+a)^3-15/2*a^2/b^7/(b*x+a)^2+6*a/b^7/(b*x+a)+\ln(b*x+a)/b^7$

Rubi [A] time = 0.06, antiderivative size = 109, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^6}{6b^7(a+bx)^6} + \frac{6a^5}{5b^7(a+bx)^5} - \frac{15a^4}{4b^7(a+bx)^4} + \frac{20a^3}{3b^7(a+bx)^3} - \frac{15a^2}{2b^7(a+bx)^2} + \frac{6a}{b^7(a+bx)} + \frac{\log(a+bx)}{b^7}$$

Antiderivative was successfully verified.

[In] Int[x^6/(a + b*x)^7, x]

[Out] $-a^6/(6*b^7*(a + b*x)^6) + (6*a^5)/(5*b^7*(a + b*x)^5) - (15*a^4)/(4*b^7*(a + b*x)^4) + (20*a^3)/(3*b^7*(a + b*x)^3) - (15*a^2)/(2*b^7*(a + b*x)^2) + (6*a)/(b^7*(a + b*x)) + \text{Log}[a + b*x]/b^7$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^6}{(a+bx)^7} dx &= \int \left(\frac{a^6}{b^6(a+bx)^7} - \frac{6a^5}{b^6(a+bx)^6} + \frac{15a^4}{b^6(a+bx)^5} - \frac{20a^3}{b^6(a+bx)^4} + \frac{15a^2}{b^6(a+bx)^3} - \frac{6a}{b^6(a+bx)^2} + \frac{1}{b^6} \right) dx \\ &= -\frac{a^6}{6b^7(a+bx)^6} + \frac{6a^5}{5b^7(a+bx)^5} - \frac{15a^4}{4b^7(a+bx)^4} + \frac{20a^3}{3b^7(a+bx)^3} - \frac{15a^2}{2b^7(a+bx)^2} + \frac{6a}{b^7(a+bx)} + \frac{\log(a+bx)}{b^7} \end{aligned}$$

Mathematica [A] time = 0.02, size = 77, normalized size = 0.71

$$\frac{a(147a^5+822a^4bx+1875a^3b^2x^2+2200a^2b^3x^3+1350ab^4x^4+360b^5x^5)}{(a+bx)^6} + 60 \log(a+bx)$$

$$60b^7$$

Antiderivative was successfully verified.

[In] Integrate[x^6/(a + b*x)^7,x]

[Out] ((a*(147*a^5 + 822*a^4*b*x + 1875*a^3*b^2*x^2 + 2200*a^2*b^3*x^3 + 1350*a*b^4*x^4 + 360*b^5*x^5))/(a + b*x)^6 + 60*Log[a + b*x])/(60*b^7)

fricas [A] time = 0.47, size = 193, normalized size = 1.77

$$\frac{360 ab^5 x^5 + 1350 a^2 b^4 x^4 + 2200 a^3 b^3 x^3 + 1875 a^4 b^2 x^2 + 822 a^5 b x + 147 a^6 + 60 (b^6 x^6 + 6 a b^5 x^5 + 15 a^2 b^4 x^4 + 20 a^3 b^3 x^3 + 15 a^4 b^2 x^2 + 6 a^5 b x + a^6) \log(a + b x)}{60 (b^{13} x^6 + 6 a b^{12} x^5 + 15 a^2 b^{11} x^4 + 20 a^3 b^{10} x^3 + 15 a^4 b^9 x^2 + 6 a^5 b^8 x + a^6 b^7)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^7,x, algorithm="fricas")

[Out] 1/60*(360*a*b^5*x^5 + 1350*a^2*b^4*x^4 + 2200*a^3*b^3*x^3 + 1875*a^4*b^2*x^2 + 822*a^5*b*x + 147*a^6 + 60*(b^6*x^6 + 6*a*b^5*x^5 + 15*a^2*b^4*x^4 + 20*a^3*b^3*x^3 + 15*a^4*b^2*x^2 + 6*a^5*b*x + a^6)*log(b*x + a))/(b^13*x^6 + 6*a*b^12*x^5 + 15*a^2*b^11*x^4 + 20*a^3*b^10*x^3 + 15*a^4*b^9*x^2 + 6*a^5*b^8*x + a^6*b^7)

giac [A] time = 1.16, size = 79, normalized size = 0.72

$$\frac{\log(|bx + a|)}{b^7} + \frac{360 ab^4 x^5 + 1350 a^2 b^3 x^4 + 2200 a^3 b^2 x^3 + 1875 a^4 b x^2 + 822 a^5 x + \frac{147 a^6}{b}}{60 (bx + a)^6 b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^7,x, algorithm="giac")

[Out] log(abs(b*x + a))/b^7 + 1/60*(360*a*b^4*x^5 + 1350*a^2*b^3*x^4 + 2200*a^3*b^2*x^3 + 1875*a^4*b*x^2 + 822*a^5*x + 147*a^6/b)/((b*x + a)^6*b^6)

maple [A] time = 0.01, size = 100, normalized size = 0.92

$$-\frac{a^6}{6 (bx + a)^6 b^7} + \frac{6a^5}{5 (bx + a)^5 b^7} - \frac{15a^4}{4 (bx + a)^4 b^7} + \frac{20a^3}{3 (bx + a)^3 b^7} - \frac{15a^2}{2 (bx + a)^2 b^7} + \frac{6a}{(bx + a) b^7} + \frac{\ln(bx + a)}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/(b*x+a)^7,x)

[Out] -1/6*a^6/b^7/(b*x+a)^6+6/5*a^5/b^7/(b*x+a)^5-15/4*a^4/b^7/(b*x+a)^4+20/3*a^3/b^7/(b*x+a)^3-15/2*a^2/b^7/(b*x+a)^2+6*a/b^7/(b*x+a)+ln(b*x+a)/b^7

maxima [A] time = 1.45, size = 136, normalized size = 1.25

$$\frac{360 ab^5 x^5 + 1350 a^2 b^4 x^4 + 2200 a^3 b^3 x^3 + 1875 a^4 b^2 x^2 + 822 a^5 b x + 147 a^6}{60 (b^{13} x^6 + 6 ab^{12} x^5 + 15 a^2 b^{11} x^4 + 20 a^3 b^{10} x^3 + 15 a^4 b^9 x^2 + 6 a^5 b^8 x + a^6 b^7)} + \frac{\log(bx + a)}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^7,x, algorithm="maxima")

[Out] 1/60*(360*a*b^5*x^5 + 1350*a^2*b^4*x^4 + 2200*a^3*b^3*x^3 + 1875*a^4*b^2*x^2 + 822*a^5*b*x + 147*a^6)/(b^13*x^6 + 6*a*b^12*x^5 + 15*a^2*b^11*x^4 + 20*a^3*b^10*x^3 + 15*a^4*b^9*x^2 + 6*a^5*b^8*x + a^6*b^7) + log(b*x + a)/b^7

mupad [B] time = 0.11, size = 81, normalized size = 0.74

$$\frac{\ln(a + bx) + \frac{6a}{a+bx} - \frac{15a^2}{2(a+bx)^2} + \frac{20a^3}{3(a+bx)^3} - \frac{15a^4}{4(a+bx)^4} + \frac{6a^5}{5(a+bx)^5} - \frac{a^6}{6(a+bx)^6}}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/(a + b*x)^7,x)

[Out] (log(a + b*x) + (6*a)/(a + b*x) - (15*a^2)/(2*(a + b*x)^2) + (20*a^3)/(3*(a + b*x)^3) - (15*a^4)/(4*(a + b*x)^4) + (6*a^5)/(5*(a + b*x)^5) - a^6/(6*(a + b*x)^6))/b^7

sympy [A] time = 0.64, size = 141, normalized size = 1.29

$$\frac{147a^6 + 822a^5bx + 1875a^4b^2x^2 + 2200a^3b^3x^3 + 1350a^2b^4x^4 + 360ab^5x^5}{60a^6b^7 + 360a^5b^8x + 900a^4b^9x^2 + 1200a^3b^{10}x^3 + 900a^2b^{11}x^4 + 360ab^{12}x^5 + 60b^{13}x^6} + \frac{\log(a + bx)}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6/(b*x+a)**7,x)

[Out] (147*a**6 + 822*a**5*b*x + 1875*a**4*b**2*x**2 + 2200*a**3*b**3*x**3 + 1350*a**2*b**4*x**4 + 360*a*b**5*x**5)/(60*a**6*b**7 + 360*a**5*b**8*x + 900*a**4*b**9*x**2 + 1200*a**3*b**10*x**3 + 900*a**2*b**11*x**4 + 360*a*b**12*x**5 + 60*b**13*x**6) + log(a + b*x)/b**7

$$3.212 \quad \int \frac{x^5}{(a+bx)^7} dx$$

Optimal. Leaf size=17

$$\frac{x^6}{6a(a+bx)^6}$$

[Out] 1/6*x^6/a/(b*x+a)^6

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {37}

$$\frac{x^6}{6a(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Int[x^5/(a + b*x)^7, x]

[Out] x^6/(6*a*(a + b*x)^6)

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{x^5}{(a+bx)^7} dx = \frac{x^6}{6a(a+bx)^6}$$

Mathematica [B] time = 0.01, size = 64, normalized size = 3.76

$$\frac{a^5 + 6a^4bx + 15a^3b^2x^2 + 20a^2b^3x^3 + 15ab^4x^4 + 6b^5x^5}{6b^6(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/(a + b*x)^7, x]

[Out] -1/6*(a^5 + 6*a^4*b*x + 15*a^3*b^2*x^2 + 20*a^2*b^3*x^3 + 15*a*b^4*x^4 + 6*b^5*x^5)/(b^6*(a + b*x)^6)

fricas [B] time = 0.45, size = 120, normalized size = 7.06

$$\frac{6b^5x^5 + 15ab^4x^4 + 20a^2b^3x^3 + 15a^3b^2x^2 + 6a^4bx + a^5}{6(b^{12}x^6 + 6ab^{11}x^5 + 15a^2b^{10}x^4 + 20a^3b^9x^3 + 15a^4b^8x^2 + 6a^5b^7x + a^6b^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^7,x, algorithm="fricas")

[Out] $-1/6*(6*b^5*x^5 + 15*a*b^4*x^4 + 20*a^2*b^3*x^3 + 15*a^3*b^2*x^2 + 6*a^4*b*x + a^5)/(b^{12}*x^6 + 6*a*b^{11}*x^5 + 15*a^2*b^{10}*x^4 + 20*a^3*b^9*x^3 + 15*a^4*b^8*x^2 + 6*a^5*b^7*x + a^6*b^6)$

giac [B] time = 1.08, size = 62, normalized size = 3.65

$$\frac{6b^5x^5 + 15ab^4x^4 + 20a^2b^3x^3 + 15a^3b^2x^2 + 6a^4bx + a^5}{6(bx + a)^6b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^7,x, algorithm="giac")

[Out] $-1/6*(6*b^5*x^5 + 15*a*b^4*x^4 + 20*a^2*b^3*x^3 + 15*a^3*b^2*x^2 + 6*a^4*b*x + a^5)/((b*x + a)^6*b^6)$

maple [B] time = 0.00, size = 87, normalized size = 5.12

$$\frac{a^5}{6(bx + a)^6b^6} - \frac{a^4}{(bx + a)^5b^6} + \frac{5a^3}{2(bx + a)^4b^6} - \frac{10a^2}{3(bx + a)^3b^6} + \frac{5a}{2(bx + a)^2b^6} - \frac{1}{(bx + a)b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(b*x+a)^7,x)

[Out] $1/6*a^5/b^6/(b*x+a)^6+5/2*a/b^6/(b*x+a)^2-a^4/b^6/(b*x+a)^5+5/2*a^3/b^6/(b*x+a)^4-10/3*a^2/b^6/(b*x+a)^3-1/b^6/(b*x+a)$

maxima [B] time = 1.43, size = 120, normalized size = 7.06

$$\frac{6b^5x^5 + 15ab^4x^4 + 20a^2b^3x^3 + 15a^3b^2x^2 + 6a^4bx + a^5}{6(b^{12}x^6 + 6ab^{11}x^5 + 15a^2b^{10}x^4 + 20a^3b^9x^3 + 15a^4b^8x^2 + 6a^5b^7x + a^6b^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^7,x, algorithm="maxima")

[Out] $-1/6*(6*b^5*x^5 + 15*a*b^4*x^4 + 20*a^2*b^3*x^3 + 15*a^3*b^2*x^2 + 6*a^4*b*x + a^5)/(b^{12}*x^6 + 6*a*b^{11}*x^5 + 15*a^2*b^{10}*x^4 + 20*a^3*b^9*x^3 + 15*a^4*b^8*x^2 + 6*a^5*b^7*x + a^6*b^6)$

mupad [B] time = 0.12, size = 72, normalized size = 4.24

$$\frac{\frac{5a}{2(a+bx)^2} - \frac{1}{a+bx} - \frac{10a^2}{3(a+bx)^3} + \frac{5a^3}{2(a+bx)^4} - \frac{a^4}{(a+bx)^5} + \frac{a^5}{6(a+bx)^6}}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^5/(a + b*x)^7,x)`

[Out] $((5*a)/(2*(a + b*x)^2) - 1/(a + b*x) - (10*a^2)/(3*(a + b*x)^3) + (5*a^3)/(2*(a + b*x)^4) - a^4/(a + b*x)^5 + a^5/(6*(a + b*x)^6))/b^6$

sympy [B] time = 0.58, size = 128, normalized size = 7.53

$$\frac{-a^5 - 6a^4bx - 15a^3b^2x^2 - 20a^2b^3x^3 - 15ab^4x^4 - 6b^5x^5}{6a^6b^6 + 36a^5b^7x + 90a^4b^8x^2 + 120a^3b^9x^3 + 90a^2b^{10}x^4 + 36ab^{11}x^5 + 6b^{12}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**5/(b*x+a)**7,x)`

[Out] $(-a**5 - 6*a**4*b*x - 15*a**3*b**2*x**2 - 20*a**2*b**3*x**3 - 15*a*b**4*x**4 - 6*b**5*x**5)/(6*a**6*b**6 + 36*a**5*b**7*x + 90*a**4*b**8*x**2 + 120*a**3*b**9*x**3 + 90*a**2*b**10*x**4 + 36*a*b**11*x**5 + 6*b**12*x**6)$

$$3.213 \quad \int \frac{x^4}{(a+bx)^7} dx$$

Optimal. Leaf size=35

$$\frac{x^5}{30a^2(a+bx)^5} + \frac{x^5}{6a(a+bx)^6}$$

[Out] $1/6*x^5/a/(b*x+a)^6+1/30*x^5/a^2/(b*x+a)^5$

Rubi [A] time = 0.00, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{x^5}{30a^2(a+bx)^5} + \frac{x^5}{6a(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Int[x^4/(a + b*x)^7,x]

[Out] $x^5/(6*a*(a + b*x)^6) + x^5/(30*a^2*(a + b*x)^5)$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
  implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{x^4}{(a+bx)^7} dx = \frac{x^5}{6a(a+bx)^6} + \frac{\int \frac{x^4}{(a+bx)^6} dx}{6a}$$

$$= \frac{x^5}{6a(a+bx)^6} + \frac{x^5}{30a^2(a+bx)^5}$$

Mathematica [A] time = 0.01, size = 53, normalized size = 1.51

$$\frac{a^4 + 6a^3bx + 15a^2b^2x^2 + 20ab^3x^3 + 15b^4x^4}{30b^5(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/(a + b*x)^7, x]

[Out] -1/30*(a^4 + 6*a^3*b*x + 15*a^2*b^2*x^2 + 20*a*b^3*x^3 + 15*b^4*x^4)/(b^5*(a + b*x)^6)

fricas [B] time = 0.48, size = 109, normalized size = 3.11

$$\frac{15b^4x^4 + 20ab^3x^3 + 15a^2b^2x^2 + 6a^3bx + a^4}{30(b^{11}x^6 + 6ab^{10}x^5 + 15a^2b^9x^4 + 20a^3b^8x^3 + 15a^4b^7x^2 + 6a^5b^6x + a^6b^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^7, x, algorithm="fricas")

[Out] -1/30*(15*b^4*x^4 + 20*a*b^3*x^3 + 15*a^2*b^2*x^2 + 6*a^3*b*x + a^4)/(b^11*x^6 + 6*a*b^10*x^5 + 15*a^2*b^9*x^4 + 20*a^3*b^8*x^3 + 15*a^4*b^7*x^2 + 6*a^5*b^6*x + a^6*b^5)

giac [A] time = 1.14, size = 51, normalized size = 1.46

$$\frac{15b^4x^4 + 20ab^3x^3 + 15a^2b^2x^2 + 6a^3bx + a^4}{30(bx+a)^6b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^7, x, algorithm="giac")

[Out] -1/30*(15*b^4*x^4 + 20*a*b^3*x^3 + 15*a^2*b^2*x^2 + 6*a^3*b*x + a^4)/((b*x + a)^6*b^5)

maple [B] time = 0.01, size = 72, normalized size = 2.06

$$-\frac{a^4}{6(bx+a)^6 b^5} + \frac{4a^3}{5(bx+a)^5 b^5} - \frac{3a^2}{2(bx+a)^4 b^5} + \frac{4a}{3(bx+a)^3 b^5} - \frac{1}{2(bx+a)^2 b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(b*x+a)^7,x)

[Out] $-1/6*a^4/b^5/(b*x+a)^6 - 1/2/b^5/(b*x+a)^2 - 3/2*a^2/b^5/(b*x+a)^4 + 4/5*a^3/b^5/(b*x+a)^5 + 4/3*a/b^5/(b*x+a)^3$

maxima [B] time = 1.45, size = 109, normalized size = 3.11

$$\frac{15b^4x^4 + 20ab^3x^3 + 15a^2b^2x^2 + 6a^3bx + a^4}{30(b^{11}x^6 + 6ab^{10}x^5 + 15a^2b^9x^4 + 20a^3b^8x^3 + 15a^4b^7x^2 + 6a^5b^6x + a^6b^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^7,x, algorithm="maxima")

[Out] $-1/30*(15*b^4*x^4 + 20*a*b^3*x^3 + 15*a^2*b^2*x^2 + 6*a^3*b*x + a^4)/(b^{11}*x^6 + 6*a*b^{10}*x^5 + 15*a^2*b^9*x^4 + 20*a^3*b^8*x^3 + 15*a^4*b^7*x^2 + 6*a^5*b^6*x + a^6*b^5)$

mupad [B] time = 0.07, size = 22, normalized size = 0.63

$$\frac{x^5(6a+bx)}{30a^2(a+bx)^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(a+b*x)^7,x)

[Out] $(x^5*(6*a + b*x))/(30*a^2*(a + b*x)^6)$

sympy [B] time = 0.57, size = 116, normalized size = 3.31

$$\frac{-a^4 - 6a^3bx - 15a^2b^2x^2 - 20ab^3x^3 - 15b^4x^4}{30a^6b^5 + 180a^5b^6x + 450a^4b^7x^2 + 600a^3b^8x^3 + 450a^2b^9x^4 + 180ab^{10}x^5 + 30b^{11}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/(b*x+a)**7,x)

[Out] $(-a**4 - 6*a**3*b*x - 15*a**2*b**2*x**2 - 20*a*b**3*x**3 - 15*b**4*x**4)/(30*a**6*b**5 + 180*a**5*b**6*x + 450*a**4*b**7*x**2 + 600*a**3*b**8*x**3 + 450*a**2*b**9*x**4 + 180*a*b**10*x**5 + 30*b**11*x**6)$

$$3.214 \quad \int \frac{x^3}{(a+bx)^7} dx$$

Optimal. Leaf size=52

$$\frac{x^4}{60a^3(a+bx)^4} + \frac{x^4}{15a^2(a+bx)^5} + \frac{x^4}{6a(a+bx)^6}$$

[Out] $1/6*x^4/a/(b*x+a)^6+1/15*x^4/a^2/(b*x+a)^5+1/60*x^4/a^3/(b*x+a)^4$

Rubi [A] time = 0.03, antiderivative size = 64, normalized size of antiderivative = 1.23, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^3}{6b^4(a+bx)^6} - \frac{3a^2}{5b^4(a+bx)^5} + \frac{3a}{4b^4(a+bx)^4} - \frac{1}{3b^4(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x)^7,x]

[Out] $a^3/(6*b^4*(a + b*x)^6) - (3*a^2)/(5*b^4*(a + b*x)^5) + (3*a)/(4*b^4*(a + b*x)^4) - 1/(3*b^4*(a + b*x)^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(a+bx)^7} dx &= \int \left(-\frac{a^3}{b^3(a+bx)^7} + \frac{3a^2}{b^3(a+bx)^6} - \frac{3a}{b^3(a+bx)^5} + \frac{1}{b^3(a+bx)^4} \right) dx \\ &= \frac{a^3}{6b^4(a+bx)^6} - \frac{3a^2}{5b^4(a+bx)^5} + \frac{3a}{4b^4(a+bx)^4} - \frac{1}{3b^4(a+bx)^3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 42, normalized size = 0.81

$$-\frac{a^3 + 6a^2bx + 15ab^2x^2 + 20b^3x^3}{60b^4(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x)^7,x]

[Out] $-1/60*(a^3 + 6*a^2*b*x + 15*a*b^2*x^2 + 20*b^3*x^3)/(b^4*(a + b*x)^6)$

fricas [B] time = 0.44, size = 98, normalized size = 1.88

$$\frac{20 b^3 x^3 + 15 a b^2 x^2 + 6 a^2 b x + a^3}{60 (b^{10} x^6 + 6 a b^9 x^5 + 15 a^2 b^8 x^4 + 20 a^3 b^7 x^3 + 15 a^4 b^6 x^2 + 6 a^5 b^5 x + a^6 b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^7,x, algorithm="fricas")

[Out] $-1/60*(20*b^3*x^3 + 15*a*b^2*x^2 + 6*a^2*b*x + a^3)/(b^{10}*x^6 + 6*a*b^9*x^5 + 15*a^2*b^8*x^4 + 20*a^3*b^7*x^3 + 15*a^4*b^6*x^2 + 6*a^5*b^5*x + a^6*b^4)$

giac [A] time = 1.00, size = 40, normalized size = 0.77

$$\frac{20 b^3 x^3 + 15 a b^2 x^2 + 6 a^2 b x + a^3}{60 (b x + a)^6 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^7,x, algorithm="giac")

[Out] $-1/60*(20*b^3*x^3 + 15*a*b^2*x^2 + 6*a^2*b*x + a^3)/((b*x + a)^6*b^4)$

maple [A] time = 0.00, size = 57, normalized size = 1.10

$$\frac{a^3}{6 (b x + a)^6 b^4} - \frac{3 a^2}{5 (b x + a)^5 b^4} + \frac{3 a}{4 (b x + a)^4 b^4} - \frac{1}{3 (b x + a)^3 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^7,x)

[Out] $1/6*a^3/b^4/(b*x+a)^6-3/5*a^2/b^4/(b*x+a)^5+3/4*a/b^4/(b*x+a)^4-1/3/b^4/(b*x+a)^3$

maxima [B] time = 1.40, size = 98, normalized size = 1.88

$$\frac{20 b^3 x^3 + 15 a b^2 x^2 + 6 a^2 b x + a^3}{60 (b^{10} x^6 + 6 a b^9 x^5 + 15 a^2 b^8 x^4 + 20 a^3 b^7 x^3 + 15 a^4 b^6 x^2 + 6 a^5 b^5 x + a^6 b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^7,x, algorithm="maxima")

[Out] -1/60*(20*b^3*x^3 + 15*a*b^2*x^2 + 6*a^2*b*x + a^3)/(b^10*x^6 + 6*a*b^9*x^5 + 15*a^2*b^8*x^4 + 20*a^3*b^7*x^3 + 15*a^4*b^6*x^2 + 6*a^5*b^5*x + a^6*b^4)

mupad [B] time = 0.07, size = 48, normalized size = 0.92

$$\frac{\frac{3a}{4(a+bx)^4} - \frac{1}{3(a+bx)^3} - \frac{3a^2}{5(a+bx)^5} + \frac{a^3}{6(a+bx)^6}}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(a + b*x)^7,x)

[Out] ((3*a)/(4*(a + b*x)^4) - 1/(3*(a + b*x)^3) - (3*a^2)/(5*(a + b*x)^5) + a^3/(6*(a + b*x)^6))/b^4

sympy [B] time = 0.56, size = 104, normalized size = 2.00

$$\frac{-a^3 - 6a^2bx - 15ab^2x^2 - 20b^3x^3}{60a^6b^4 + 360a^5b^5x + 900a^4b^6x^2 + 1200a^3b^7x^3 + 900a^2b^8x^4 + 360ab^9x^5 + 60b^{10}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(b*x+a)**7,x)

[Out] (-a**3 - 6*a**2*b*x - 15*a*b**2*x**2 - 20*b**3*x**3)/(60*a**6*b**4 + 360*a**5*b**5*x + 900*a**4*b**6*x**2 + 1200*a**3*b**7*x**3 + 900*a**2*b**8*x**4 + 360*a*b**9*x**5 + 60*b**10*x**6)

$$3.215 \quad \int \frac{x^2}{(a+bx)^7} dx$$

Optimal. Leaf size=47

$$-\frac{a^2}{6b^3(a+bx)^6} + \frac{2a}{5b^3(a+bx)^5} - \frac{1}{4b^3(a+bx)^4}$$

[Out] $-1/6*a^2/b^3/(b*x+a)^6+2/5*a/b^3/(b*x+a)^5-1/4/b^3/(b*x+a)^4$

Rubi [A] time = 0.02, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{6b^3(a+bx)^6} + \frac{2a}{5b^3(a+bx)^5} - \frac{1}{4b^3(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*x)^7,x]

[Out] $-a^2/(6*b^3*(a + b*x)^6) + (2*a)/(5*b^3*(a + b*x)^5) - 1/(4*b^3*(a + b*x)^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(a+bx)^7} dx &= \int \left(\frac{a^2}{b^2(a+bx)^7} - \frac{2a}{b^2(a+bx)^6} + \frac{1}{b^2(a+bx)^5} \right) dx \\ &= -\frac{a^2}{6b^3(a+bx)^6} + \frac{2a}{5b^3(a+bx)^5} - \frac{1}{4b^3(a+bx)^4} \end{aligned}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 0.66

$$-\frac{a^2 + 6abx + 15b^2x^2}{60b^3(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x)^7,x]

[Out] -1/60*(a^2 + 6*a*b*x + 15*b^2*x^2)/(b^3*(a + b*x)^6)

fricas [B] time = 0.45, size = 87, normalized size = 1.85

$$\frac{15b^2x^2 + 6abx + a^2}{60(b^9x^6 + 6ab^8x^5 + 15a^2b^7x^4 + 20a^3b^6x^3 + 15a^4b^5x^2 + 6a^5b^4x + a^6b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^7,x, algorithm="fricas")

[Out] -1/60*(15*b^2*x^2 + 6*a*b*x + a^2)/(b^9*x^6 + 6*a*b^8*x^5 + 15*a^2*b^7*x^4 + 20*a^3*b^6*x^3 + 15*a^4*b^5*x^2 + 6*a^5*b^4*x + a^6*b^3)

giac [A] time = 1.00, size = 29, normalized size = 0.62

$$\frac{15b^2x^2 + 6abx + a^2}{60(bx + a)^6b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^7,x, algorithm="giac")

[Out] -1/60*(15*b^2*x^2 + 6*a*b*x + a^2)/((b*x + a)^6*b^3)

maple [A] time = 0.00, size = 42, normalized size = 0.89

$$-\frac{a^2}{6(bx + a)^6b^3} + \frac{2a}{5(bx + a)^5b^3} - \frac{1}{4(bx + a)^4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^7,x)

[Out] -1/6*a^2/b^3/(b*x+a)^6+2/5*a/b^3/(b*x+a)^5-1/4/b^3/(b*x+a)^4

maxima [B] time = 1.45, size = 87, normalized size = 1.85

$$\frac{15b^2x^2 + 6abx + a^2}{60(b^9x^6 + 6ab^8x^5 + 15a^2b^7x^4 + 20a^3b^6x^3 + 15a^4b^5x^2 + 6a^5b^4x + a^6b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^7,x, algorithm="maxima")

[Out] $-1/60*(15*b^2*x^2 + 6*a*b*x + a^2)/(b^9*x^6 + 6*a*b^8*x^5 + 15*a^2*b^7*x^4 + 20*a^3*b^6*x^3 + 15*a^4*b^5*x^2 + 6*a^5*b^4*x + a^6*b^3)$

mupad [B] time = 0.08, size = 31, normalized size = 0.66

$$-\frac{8a^2 + 48abx + 120b^2x^2}{480b^3(a+bx)^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(a + b*x)^7,x)

[Out] $-(8*a^2 + 120*b^2*x^2 + 48*a*b*x)/(480*b^3*(a + b*x)^6)$

sympy [B] time = 0.55, size = 92, normalized size = 1.96

$$\frac{-a^2 - 6abx - 15b^2x^2}{60a^6b^3 + 360a^5b^4x + 900a^4b^5x^2 + 1200a^3b^6x^3 + 900a^2b^7x^4 + 360ab^8x^5 + 60b^9x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(b*x+a)**7,x)

[Out] $(-a**2 - 6*a*b*x - 15*b**2*x**2)/(60*a**6*b**3 + 360*a**5*b**4*x + 900*a**4*b**5*x**2 + 1200*a**3*b**6*x**3 + 900*a**2*b**7*x**4 + 360*a*b**8*x**5 + 60*b**9*x**6)$

$$3.216 \quad \int \frac{x}{(a+bx)^7} dx$$

Optimal. Leaf size=30

$$\frac{a}{6b^2(a+bx)^6} - \frac{1}{5b^2(a+bx)^5}$$

[Out] 1/6*a/b^2/(b*x+a)^6-1/5/b^2/(b*x+a)^5

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{a}{6b^2(a+bx)^6} - \frac{1}{5b^2(a+bx)^5}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x)^7, x]

[Out] a/(6*b^2*(a + b*x)^6) - 1/(5*b^2*(a + b*x)^5)

Rule 43

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int
[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n},
x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && Le
Q[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])
```

Rubi steps

$$\begin{aligned} \int \frac{x}{(a+bx)^7} dx &= \int \left(-\frac{a}{b(a+bx)^7} + \frac{1}{b(a+bx)^6} \right) dx \\ &= \frac{a}{6b^2(a+bx)^6} - \frac{1}{5b^2(a+bx)^5} \end{aligned}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 0.67

$$-\frac{a+6bx}{30b^2(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x)^7, x]

[Out] $-1/30*(a + 6*b*x)/(b^2*(a + b*x)^6)$

fricas [B] time = 0.44, size = 76, normalized size = 2.53

$$-\frac{6bx + a}{30(b^8x^6 + 6ab^7x^5 + 15a^2b^6x^4 + 20a^3b^5x^3 + 15a^4b^4x^2 + 6a^5b^3x + a^6b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^7,x, algorithm="fricas")`

[Out] $-1/30*(6*b*x + a)/(b^8*x^6 + 6*a*b^7*x^5 + 15*a^2*b^6*x^4 + 20*a^3*b^5*x^3 + 15*a^4*b^4*x^2 + 6*a^5*b^3*x + a^6*b^2)$

giac [A] time = 1.39, size = 18, normalized size = 0.60

$$-\frac{6bx + a}{30(bx + a)^6b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^7,x, algorithm="giac")`

[Out] $-1/30*(6*b*x + a)/((b*x + a)^6*b^2)$

maple [A] time = 0.01, size = 27, normalized size = 0.90

$$\frac{a}{6(bx + a)^6b^2} - \frac{1}{5(bx + a)^5b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(b*x+a)^7,x)`

[Out] $1/6*a/b^2/(b*x+a)^6 - 1/5/b^2/(b*x+a)^5$

maxima [B] time = 1.37, size = 76, normalized size = 2.53

$$-\frac{6bx + a}{30(b^8x^6 + 6ab^7x^5 + 15a^2b^6x^4 + 20a^3b^5x^3 + 15a^4b^4x^2 + 6a^5b^3x + a^6b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^7,x, algorithm="maxima")`

[Out] $-1/30*(6*b*x + a)/(b^8*x^6 + 6*a*b^7*x^5 + 15*a^2*b^6*x^4 + 20*a^3*b^5*x^3 + 15*a^4*b^4*x^2 + 6*a^5*b^3*x + a^6*b^2)$

mupad [B] time = 0.10, size = 18, normalized size = 0.60

$$-\frac{a + 6bx}{30b^2(a + bx)^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a + b*x)^7,x)`

[Out] `-(a + 6*b*x)/(30*b^2*(a + b*x)^6)`

sympy [B] time = 0.50, size = 80, normalized size = 2.67

$$\frac{-a - 6bx}{30a^6b^2 + 180a^5b^3x + 450a^4b^4x^2 + 600a^3b^5x^3 + 450a^2b^6x^4 + 180ab^7x^5 + 30b^8x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)**7,x)`

[Out] `(-a - 6*b*x)/(30*a**6*b**2 + 180*a**5*b**3*x + 450*a**4*b**4*x**2 + 600*a**3*b**5*x**3 + 450*a**2*b**6*x**4 + 180*a*b**7*x**5 + 30*b**8*x**6)`

$$3.217 \quad \int \frac{1}{(a+bx)^7} dx$$

Optimal. Leaf size=14

$$-\frac{1}{6b(a+bx)^6}$$

[Out] -1/6/b/(b*x+a)^6

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.143, Rules used = {32}

$$-\frac{1}{6b(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-7), x]

[Out] -1/(6*b*(a + b*x)^6)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^7} dx = -\frac{1}{6b(a+bx)^6}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\frac{1}{6b(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-7), x]

[Out] -1/6*1/(b*(a + b*x)^6)

fricas [B] time = 0.48, size = 68, normalized size = 4.86

$$-\frac{1}{6(b^7x^6 + 6ab^6x^5 + 15a^2b^5x^4 + 20a^3b^4x^3 + 15a^4b^3x^2 + 6a^5b^2x + a^6b)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^7,x, algorithm="fricas")

[Out] $-1/6/(b^7*x^6 + 6*a*b^6*x^5 + 15*a^2*b^5*x^4 + 20*a^3*b^4*x^3 + 15*a^4*b^3*x^2 + 6*a^5*b^2*x + a^6*b)$

giac [A] time = 1.09, size = 12, normalized size = 0.86

$$-\frac{1}{6(bx+a)^6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^7,x, algorithm="giac")

[Out] $-1/6/((b*x + a)^6*b)$

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$-\frac{1}{6(bx+a)^6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^7,x)

[Out] $-1/6/b/(b*x+a)^6$

maxima [A] time = 1.41, size = 12, normalized size = 0.86

$$-\frac{1}{6(bx+a)^6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^7,x, algorithm="maxima")

[Out] $-1/6/((b*x + a)^6*b)$

mupad [B] time = 0.06, size = 70, normalized size = 5.00

$$-\frac{1}{6a^6b + 36a^5b^2x + 90a^4b^3x^2 + 120a^3b^4x^3 + 90a^2b^5x^4 + 36ab^6x^5 + 6b^7x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x)^7,x)

[Out] $-1/(6*a^6*b + 6*b^7*x^6 + 36*a^5*b^2*x + 36*a*b^6*x^5 + 90*a^4*b^3*x^2 + 120*a^3*b^4*x^3 + 90*a^2*b^5*x^4)$

sympy [B] time = 0.46, size = 73, normalized size = 5.21

$$\frac{1}{6a^6b + 36a^5b^2x + 90a^4b^3x^2 + 120a^3b^4x^3 + 90a^2b^5x^4 + 36ab^6x^5 + 6b^7x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**7,x)`

[Out] $-1/(6*a**6*b + 36*a**5*b**2*x + 90*a**4*b**3*x**2 + 120*a**3*b**4*x**3 + 90*a**2*b**5*x**4 + 36*a*b**6*x**5 + 6*b**7*x**6)$

$$3.218 \quad \int \frac{1}{x(a+bx)^7} dx$$

Optimal. Leaf size=99

$$-\frac{\log(a+bx)}{a^7} + \frac{\log(x)}{a^7} + \frac{1}{a^6(a+bx)} + \frac{1}{2a^5(a+bx)^2} + \frac{1}{3a^4(a+bx)^3} + \frac{1}{4a^3(a+bx)^4} + \frac{1}{5a^2(a+bx)^5} + \frac{1}{6a(a+bx)^6}$$

[Out] $1/6/a/(b*x+a)^6 + 1/5/a^2/(b*x+a)^5 + 1/4/a^3/(b*x+a)^4 + 1/3/a^4/(b*x+a)^3 + 1/2/a^5/(b*x+a)^2 + 1/a^6/(b*x+a) + \ln(x)/a^7 - \ln(b*x+a)/a^7$

Rubi [A] time = 0.05, antiderivative size = 99, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{1}{a^6(a+bx)} + \frac{1}{2a^5(a+bx)^2} + \frac{1}{3a^4(a+bx)^3} + \frac{1}{4a^3(a+bx)^4} + \frac{1}{5a^2(a+bx)^5} - \frac{\log(a+bx)}{a^7} + \frac{\log(x)}{a^7} + \frac{1}{6a(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a + b*x)^7), x]

[Out] $1/(6*a*(a + b*x)^6) + 1/(5*a^2*(a + b*x)^5) + 1/(4*a^3*(a + b*x)^4) + 1/(3*a^4*(a + b*x)^3) + 1/(2*a^5*(a + b*x)^2) + 1/(a^6*(a + b*x)) + \text{Log}[x]/a^7 - \text{Log}[a + b*x]/a^7$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{x(a+bx)^7} dx = \int \left(\frac{1}{a^7 x} - \frac{b}{a(a+bx)^7} - \frac{b}{a^2(a+bx)^6} - \frac{b}{a^3(a+bx)^5} - \frac{b}{a^4(a+bx)^4} - \frac{b}{a^5(a+bx)^3} - \frac{b}{a^6(a+bx)^2} \right) dx$$

$$= \frac{1}{6a(a+bx)^6} + \frac{1}{5a^2(a+bx)^5} + \frac{1}{4a^3(a+bx)^4} + \frac{1}{3a^4(a+bx)^3} + \frac{1}{2a^5(a+bx)^2} + \frac{1}{a^6(a+bx)} + \frac{\log(x)}{a^7} - \frac{\log(a+bx)}{a^7}$$

Mathematica [A] time = 0.06, size = 81, normalized size = 0.82

$$\frac{a(147a^5 + 522a^4bx + 855a^3b^2x^2 + 740a^2b^3x^3 + 330ab^4x^4 + 60b^5x^5)}{(a+bx)^6} - 60 \log(a+bx) + 60 \log(x)$$

$$60a^7$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)^7), x]

[Out] ((a*(147*a^5 + 522*a^4*b*x + 855*a^3*b^2*x^2 + 740*a^2*b^3*x^3 + 330*a*b^4*x^4 + 60*b^5*x^5))/(a + b*x)^6 + 60*Log[x] - 60*Log[a + b*x])/(60*a^7)

fricas [B] time = 0.46, size = 256, normalized size = 2.59

$$\frac{60 ab^5 x^5 + 330 a^2 b^4 x^4 + 740 a^3 b^3 x^3 + 855 a^4 b^2 x^2 + 522 a^5 b x + 147 a^6 - 60 (b^6 x^6 + 6 ab^5 x^5 + 15 a^2 b^4 x^4 + 20 a^3 b^3 x^3 + 15 a^4 b^2 x^2 + 6 a^5 b x + a^6)}{60 (a^7 b^6 x^6 + 6 a^8 b^5 x^5 + 15 a^9 b^4 x^4 + 20 a^{10} b^3 x^3 + 15 a^{11} b^2 x^2 + 6 a^{12} b x + a^{13})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^7,x, algorithm="fricas")

[Out] 1/60*(60*a*b^5*x^5 + 330*a^2*b^4*x^4 + 740*a^3*b^3*x^3 + 855*a^4*b^2*x^2 + 522*a^5*b*x + 147*a^6 - 60*(b^6*x^6 + 6*a*b^5*x^5 + 15*a^2*b^4*x^4 + 20*a^3*b^3*x^3 + 15*a^4*b^2*x^2 + 6*a^5*b*x + a^6)*log(b*x + a) + 60*(b^6*x^6 + 6*a*b^5*x^5 + 15*a^2*b^4*x^4 + 20*a^3*b^3*x^3 + 15*a^4*b^2*x^2 + 6*a^5*b*x + a^6)*log(x))/(a^7*b^6*x^6 + 6*a^8*b^5*x^5 + 15*a^9*b^4*x^4 + 20*a^10*b^3*x^3 + 15*a^11*b^2*x^2 + 6*a^12*b*x + a^13)

giac [A] time = 1.01, size = 87, normalized size = 0.88

$$\frac{\frac{\log(|bx + a|)}{a^7} + \frac{\log(|x|)}{a^7} + \frac{60 ab^5 x^5 + 330 a^2 b^4 x^4 + 740 a^3 b^3 x^3 + 855 a^4 b^2 x^2 + 522 a^5 b x + 147 a^6}{60 (bx + a)^6 a^7}}{60 (bx + a)^6 a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^7,x, algorithm="giac")

[Out] -log(abs(b*x + a))/a^7 + log(abs(x))/a^7 + 1/60*(60*a*b^5*x^5 + 330*a^2*b^4*x^4 + 740*a^3*b^3*x^3 + 855*a^4*b^2*x^2 + 522*a^5*b*x + 147*a^6)/((b*x + a)^6*a^7)

maple [A] time = 0.01, size = 90, normalized size = 0.91

$$\frac{1}{6 (bx + a)^6 a} + \frac{1}{5 (bx + a)^5 a^2} + \frac{1}{4 (bx + a)^4 a^3} + \frac{1}{3 (bx + a)^3 a^4} + \frac{1}{2 (bx + a)^2 a^5} + \frac{1}{(bx + a) a^6} + \frac{\ln(x)}{a^7} - \frac{\ln(bx + a)}{a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a)^7,x)

[Out] 1/6/a/(b*x+a)^6+1/5/a^2/(b*x+a)^5+1/4/a^3/(b*x+a)^4+1/3/a^4/(b*x+a)^3+1/2/a^5/(b*x+a)^2+1/a^6/(b*x+a)+ln(x)/a^7-ln(b*x+a)/a^7

maxima [A] time = 1.51, size = 139, normalized size = 1.40

$$\frac{60b^5x^5 + 330ab^4x^4 + 740a^2b^3x^3 + 855a^3b^2x^2 + 522a^4bx + 147a^5}{60(a^6b^6x^6 + 6a^7b^5x^5 + 15a^8b^4x^4 + 20a^9b^3x^3 + 15a^{10}b^2x^2 + 6a^{11}bx + a^{12})} - \frac{\log(bx + a)}{a^7} + \frac{\log(x)}{a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^7,x, algorithm="maxima")

[Out] 1/60*(60*b^5*x^5 + 330*a*b^4*x^4 + 740*a^2*b^3*x^3 + 855*a^3*b^2*x^2 + 522*a^4*b*x + 147*a^5)/(a^6*b^6*x^6 + 6*a^7*b^5*x^5 + 15*a^8*b^4*x^4 + 20*a^9*b^3*x^3 + 15*a^10*b^2*x^2 + 6*a^11*b*x + a^12) - log(b*x + a)/a^7 + log(x)/a^7

mupad [B] time = 0.45, size = 102, normalized size = 1.03

$$\frac{\ln\left(\frac{a+bx}{x}\right) - \frac{15b^2x^2}{2(a+bx)^2} + \frac{20b^3x^3}{3(a+bx)^3} - \frac{15b^4x^4}{4(a+bx)^4} + \frac{6b^5x^5}{5(a+bx)^5} - \frac{b^6x^6}{6(a+bx)^6} + \frac{6bx}{a+bx}}{a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(a + b*x)^7),x)

[Out] -(log((a + b*x)/x) - (15*b^2*x^2)/(2*(a + b*x)^2) + (20*b^3*x^3)/(3*(a + b*x)^3) - (15*b^4*x^4)/(4*(a + b*x)^4) + (6*b^5*x^5)/(5*(a + b*x)^5) - (b^6*x^6)/(6*(a + b*x)^6) + (6*b*x)/(a + b*x))/a^7

sympy [A] time = 0.68, size = 141, normalized size = 1.42

$$\frac{147a^5 + 522a^4bx + 855a^3b^2x^2 + 740a^2b^3x^3 + 330ab^4x^4 + 60b^5x^5}{60a^{12} + 360a^{11}bx + 900a^{10}b^2x^2 + 1200a^9b^3x^3 + 900a^8b^4x^4 + 360a^7b^5x^5 + 60a^6b^6x^6} + \frac{\log(x) - \log\left(\frac{a}{b} + x\right)}{a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)**7,x)

[Out] (147*a**5 + 522*a**4*b*x + 855*a**3*b**2*x**2 + 740*a**2*b**3*x**3 + 330*a*b**4*x**4 + 60*b**5*x**5)/(60*a**12 + 360*a**11*b*x + 900*a**10*b**2*x**2 + 1200*a**9*b**3*x**3 + 900*a**8*b**4*x**4 + 360*a**7*b**5*x**5 + 60*a**6*b**6*x**6) + (log(x) - log(a/b + x))/a**7

$$3.219 \quad \int \frac{1}{x^2(a+bx)^7} dx$$

Optimal. Leaf size=117

$$-\frac{7b \log(x)}{a^8} + \frac{7b \log(a+bx)}{a^8} - \frac{6b}{a^7(a+bx)} - \frac{1}{a^7 x} - \frac{5b}{2a^6(a+bx)^2} - \frac{4b}{3a^5(a+bx)^3} - \frac{3b}{4a^4(a+bx)^4} - \frac{2b}{5a^3(a+bx)^5} - \frac{b}{6a^2(a+bx)^6} - \frac{7b \log(x)}{a^8} + \frac{7b \log(a+bx)}{a^8}$$

[Out] $-1/a^7/x - 1/6*b/a^2/(b*x+a)^6 - 2/5*b/a^3/(b*x+a)^5 - 3/4*b/a^4/(b*x+a)^4 - 4/3*b/a^5/(b*x+a)^3 - 5/2*b/a^6/(b*x+a)^2 - 6*b/a^7/(b*x+a) - 7*b*\ln(x)/a^8 + 7*b*\ln(b*x+a)/a^8$

Rubi [A] time = 0.07, antiderivative size = 117, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{6b}{a^7(a+bx)} - \frac{5b}{2a^6(a+bx)^2} - \frac{4b}{3a^5(a+bx)^3} - \frac{3b}{4a^4(a+bx)^4} - \frac{2b}{5a^3(a+bx)^5} - \frac{b}{6a^2(a+bx)^6} - \frac{7b \log(x)}{a^8} + \frac{7b \log(a+bx)}{a^8}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(a + b*x)^7), x]

[Out] $-(1/(a^7*x)) - b/(6*a^2*(a + b*x)^6) - (2*b)/(5*a^3*(a + b*x)^5) - (3*b)/(4*a^4*(a + b*x)^4) - (4*b)/(3*a^5*(a + b*x)^3) - (5*b)/(2*a^6*(a + b*x)^2) - (6*b)/(a^7*(a + b*x)) - (7*b*\text{Log}[x])/a^8 + (7*b*\text{Log}[a + b*x])/a^8$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(a+bx)^7} dx &= \int \left(\frac{1}{a^7 x^2} - \frac{7b}{a^8 x} + \frac{b^2}{a^2(a+bx)^7} + \frac{2b^2}{a^3(a+bx)^6} + \frac{3b^2}{a^4(a+bx)^5} + \frac{4b^2}{a^5(a+bx)^4} + \frac{5b^2}{a^6(a+bx)^3} + \frac{6b^2}{a^7(a+bx)^2} \right) dx \\ &= -\frac{1}{a^7 x} - \frac{b}{6a^2(a+bx)^6} - \frac{2b}{5a^3(a+bx)^5} - \frac{3b}{4a^4(a+bx)^4} - \frac{4b}{3a^5(a+bx)^3} - \frac{5b}{2a^6(a+bx)^2} - \frac{6b}{a^7(a+bx)} + \frac{7b \log(a+bx)}{a^8} - \frac{7b \log(x)}{a^8} \end{aligned}$$

Mathematica [A] time = 0.09, size = 97, normalized size = 0.83

$$\frac{a(60a^6 + 1029a^5bx + 3654a^4b^2x^2 + 5985a^3b^3x^3 + 5180a^2b^4x^4 + 2310ab^5x^5 + 420b^6x^6)}{x(a+bx)^6} - 420b \log(a+bx) + 420b \log(x)$$

$$60a^8$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)^7),x]

[Out] $-1/60*((a*(60*a^6 + 1029*a^5*b*x + 3654*a^4*b^2*x^2 + 5985*a^3*b^3*x^3 + 5180*a^2*b^4*x^4 + 2310*a*b^5*x^5 + 420*b^6*x^6))/(x*(a + b*x)^6) + 420*b*\text{Log}[x] - 420*b*\text{Log}[a + b*x])/a^8$

fricas [B] time = 0.45, size = 285, normalized size = 2.44

$$\frac{420 ab^6 x^6 + 2310 a^2 b^5 x^5 + 5180 a^3 b^4 x^4 + 5985 a^4 b^3 x^3 + 3654 a^5 b^2 x^2 + 1029 a^6 b x + 60 a^7 - 420 (b^7 x^7 + 6 ab^6 x^6)}{60 (a^8 b^6 x^7 + 6 a^9 b^5 x^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^7,x, algorithm="fricas")

[Out] $-1/60*(420*a*b^6*x^6 + 2310*a^2*b^5*x^5 + 5180*a^3*b^4*x^4 + 5985*a^4*b^3*x^3 + 3654*a^5*b^2*x^2 + 1029*a^6*b*x + 60*a^7 - 420*(b^7*x^7 + 6*a*b^6*x^6 + 15*a^2*b^5*x^5 + 20*a^3*b^4*x^4 + 15*a^4*b^3*x^3 + 6*a^5*b^2*x^2 + a^6*b*x)*\text{log}(b*x + a) + 420*(b^7*x^7 + 6*a*b^6*x^6 + 15*a^2*b^5*x^5 + 20*a^3*b^4*x^4 + 15*a^4*b^3*x^3 + 6*a^5*b^2*x^2 + a^6*b*x)*\text{log}(x))/(a^8*b^6*x^7 + 6*a^9*b^5*x^6 + 15*a^{10}*b^4*x^5 + 20*a^{11}*b^3*x^4 + 15*a^{12}*b^2*x^3 + 6*a^{13}*b*x^2 + a^{14}*x)$

giac [A] time = 1.05, size = 104, normalized size = 0.89

$$\frac{7b \log(|bx + a|)}{a^8} - \frac{7b \log(|x|)}{a^8} - \frac{420 ab^6 x^6 + 2310 a^2 b^5 x^5 + 5180 a^3 b^4 x^4 + 5985 a^4 b^3 x^3 + 3654 a^5 b^2 x^2 + 1029 a^6 b x + 60 a^7}{60 (bx + a)^6 a^8 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^7,x, algorithm="giac")

[Out] $7*b*\text{log}(\text{abs}(b*x + a))/a^8 - 7*b*\text{log}(\text{abs}(x))/a^8 - 1/60*(420*a*b^6*x^6 + 2310*a^2*b^5*x^5 + 5180*a^3*b^4*x^4 + 5985*a^4*b^3*x^3 + 3654*a^5*b^2*x^2 + 1029*a^6*b*x + 60*a^7)/((b*x + a)^6*a^8*x)$

maple [A] time = 0.01, size = 108, normalized size = 0.92

$$\frac{b}{6 (bx + a)^6 a^2} - \frac{2b}{5 (bx + a)^5 a^3} - \frac{3b}{4 (bx + a)^4 a^4} - \frac{4b}{3 (bx + a)^3 a^5} - \frac{5b}{2 (bx + a)^2 a^6} - \frac{6b}{(bx + a) a^7} - \frac{7b \ln(x)}{a^8} + \frac{7b \ln(bx + a)}{a^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^7,x)

[Out] $-1/a^7/x - 1/6*b/a^2/(b*x+a)^6 - 2/5*b/a^3/(b*x+a)^5 - 3/4*b/a^4/(b*x+a)^4 - 4/3*b/a^5/(b*x+a)^3 - 5/2*b/a^6/(b*x+a)^2 - 6*b/a^7/(b*x+a) - 7*b*\ln(x)/a^8 + 7*b*\ln(b*x+a)/a^8$

maxima [A] time = 1.59, size = 157, normalized size = 1.34

$$\frac{420 b^6 x^6 + 2310 a b^5 x^5 + 5180 a^2 b^4 x^4 + 5985 a^3 b^3 x^3 + 3654 a^4 b^2 x^2 + 1029 a^5 b x + 60 a^6}{60 (a^7 b^6 x^7 + 6 a^8 b^5 x^6 + 15 a^9 b^4 x^5 + 20 a^{10} b^3 x^4 + 15 a^{11} b^2 x^3 + 6 a^{12} b x^2 + a^{13} x)} + \frac{7 b \log(bx + a)}{a^8} - \frac{7 b}{a^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^7,x, algorithm="maxima")

[Out] $-1/60*(420*b^6*x^6 + 2310*a*b^5*x^5 + 5180*a^2*b^4*x^4 + 5985*a^3*b^3*x^3 + 3654*a^4*b^2*x^2 + 1029*a^5*b*x + 60*a^6)/(a^7*b^6*x^7 + 6*a^8*b^5*x^6 + 15*a^9*b^4*x^5 + 20*a^{10}*b^3*x^4 + 15*a^{11}*b^2*x^3 + 6*a^{12}*b*x^2 + a^{13}*x) + 7*b*\log(b*x + a)/a^8 - 7*b*\log(x)/a^8$

mupad [B] time = 0.19, size = 151, normalized size = 1.29

$$\frac{14 b \operatorname{atanh}\left(\frac{2 b x}{a} + 1\right)}{a^8} - \frac{\frac{1}{a} + \frac{609 b^2 x^2}{10 a^3} + \frac{399 b^3 x^3}{4 a^4} + \frac{259 b^4 x^4}{3 a^5} + \frac{77 b^5 x^5}{2 a^6} + \frac{7 b^6 x^6}{a^7} + \frac{343 b x}{20 a^2}}{a^6 x + 6 a^5 b x^2 + 15 a^4 b^2 x^3 + 20 a^3 b^3 x^4 + 15 a^2 b^4 x^5 + 6 a b^5 x^6 + b^6 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(a + b*x)^7),x)

[Out] $(14*b*\operatorname{atanh}((2*b*x)/a + 1))/a^8 - (1/a + (609*b^2*x^2)/(10*a^3) + (399*b^3*x^3)/(4*a^4) + (259*b^4*x^4)/(3*a^5) + (77*b^5*x^5)/(2*a^6) + (7*b^6*x^6)/a^7 + (343*b*x)/(20*a^2))/(a^6*x + b^6*x^7 + 6*a^5*b*x^2 + 6*a*b^5*x^6 + 15*a^4*b^2*x^3 + 20*a^3*b^3*x^4 + 15*a^2*b^4*x^5)$

sympy [A] time = 0.80, size = 162, normalized size = 1.38

$$\frac{-60 a^6 - 1029 a^5 b x - 3654 a^4 b^2 x^2 - 5985 a^3 b^3 x^3 - 5180 a^2 b^4 x^4 - 2310 a b^5 x^5 - 420 b^6 x^6}{60 a^{13} x + 360 a^{12} b x^2 + 900 a^{11} b^2 x^3 + 1200 a^{10} b^3 x^4 + 900 a^9 b^4 x^5 + 360 a^8 b^5 x^6 + 60 a^7 b^6 x^7} + \frac{7 b (-\log(x) + \log(\frac{a}{b}))}{a^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/(b*x+a)**7,x)

[Out] $(-60*a**6 - 1029*a**5*b*x - 3654*a**4*b**2*x**2 - 5985*a**3*b**3*x**3 - 5180*a**2*b**4*x**4 - 2310*a*b**5*x**5 - 420*b**6*x**6)/(60*a**13*x + 360*a**12*b*x**2 + 900*a**11*b**2*x**3 + 1200*a**10*b**3*x**4 + 900*a**9*b**4*x**5 + 360*a**8*b**5*x**6 + 60*a**7*b**6*x**7) + 7*b*(-\log(x) + \log(a/b + x))/a**8$

$$3.220 \quad \int \frac{1}{x^3(a+bx)^7} dx$$

Optimal. Leaf size=144

$$\frac{28b^2 \log(x)}{a^9} - \frac{28b^2 \log(a+bx)}{a^9} + \frac{21b^2}{a^8(a+bx)} + \frac{7b}{a^8x} + \frac{15b^2}{2a^7(a+bx)^2} - \frac{1}{2a^7x^2} + \frac{10b^2}{3a^6(a+bx)^3} + \frac{3b^2}{2a^5(a+bx)^4} + \frac{3b^2}{5a^4(a+bx)^5}$$

[Out] $-1/2/a^7/x^2+7*b/a^8/x+1/6*b^2/a^3/(b*x+a)^6+3/5*b^2/a^4/(b*x+a)^5+3/2*b^2/a^5/(b*x+a)^4+10/3*b^2/a^6/(b*x+a)^3+15/2*b^2/a^7/(b*x+a)^2+21*b^2/a^8/(b*x+a)+28*b^2*\ln(x)/a^9-28*b^2*\ln(b*x+a)/a^9$

Rubi [A] time = 0.09, antiderivative size = 144, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{21b^2}{a^8(a+bx)} + \frac{15b^2}{2a^7(a+bx)^2} + \frac{10b^2}{3a^6(a+bx)^3} + \frac{3b^2}{2a^5(a+bx)^4} + \frac{3b^2}{5a^4(a+bx)^5} + \frac{b^2}{6a^3(a+bx)^6} + \frac{28b^2 \log(x)}{a^9} - \frac{28b^2 \log(a+bx)}{a^9}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(a + b*x)^7), x]

[Out] $-1/(2*a^7*x^2) + (7*b)/(a^8*x) + b^2/(6*a^3*(a + b*x)^6) + (3*b^2)/(5*a^4*(a + b*x)^5) + (3*b^2)/(2*a^5*(a + b*x)^4) + (10*b^2)/(3*a^6*(a + b*x)^3) + (15*b^2)/(2*a^7*(a + b*x)^2) + (21*b^2)/(a^8*(a + b*x)) + (28*b^2*Log[x])/a^9 - (28*b^2*Log[a + b*x])/a^9$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{x^3(a+bx)^7} dx = \int \left(\frac{1}{a^7x^3} - \frac{7b}{a^8x^2} + \frac{28b^2}{a^9x} - \frac{b^3}{a^3(a+bx)^7} - \frac{3b^3}{a^4(a+bx)^6} - \frac{6b^3}{a^5(a+bx)^5} - \frac{10b^3}{a^6(a+bx)^4} - \frac{15b^3}{a^7(a+bx)^3} \right) dx$$

$$= -\frac{1}{2a^7x^2} + \frac{7b}{a^8x} + \frac{b^2}{6a^3(a+bx)^6} + \frac{3b^2}{5a^4(a+bx)^5} + \frac{3b^2}{2a^5(a+bx)^4} + \frac{10b^2}{3a^6(a+bx)^3} + \frac{15b^2}{2a^7(a+bx)^2}$$

Mathematica [A] time = 0.07, size = 112, normalized size = 0.78

$$\frac{a(-15a^7 + 120a^6bx + 2058a^5b^2x^2 + 7308a^4b^3x^3 + 11970a^3b^4x^4 + 10360a^2b^5x^5 + 4620ab^6x^6 + 840b^7x^7)}{x^2(a+bx)^6} - 840b^2 \log(a+bx) + 840b^2 \log(x)$$

$$30a^9$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)^7),x]

[Out] ((a*(-15*a^7 + 120*a^6*b*x + 2058*a^5*b^2*x^2 + 7308*a^4*b^3*x^3 + 11970*a^3*b^4*x^4 + 10360*a^2*b^5*x^5 + 4620*a*b^6*x^6 + 840*b^7*x^7))/(x^2*(a + b*x)^6) + 840*b^2*Log[x] - 840*b^2*Log[a + b*x])/(30*a^9)

fricas [B] time = 0.51, size = 306, normalized size = 2.12

$$\frac{840 ab^7 x^7 + 4620 a^2 b^6 x^6 + 10360 a^3 b^5 x^5 + 11970 a^4 b^4 x^4 + 7308 a^5 b^3 x^3 + 2058 a^6 b^2 x^2 + 120 a^7 b x - 15 a^8 - 840}{30(a^9 b^6 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^7,x, algorithm="fricas")

[Out] 1/30*(840*a*b^7*x^7 + 4620*a^2*b^6*x^6 + 10360*a^3*b^5*x^5 + 11970*a^4*b^4*x^4 + 7308*a^5*b^3*x^3 + 2058*a^6*b^2*x^2 + 120*a^7*b*x - 15*a^8 - 840*(b^8*x^8 + 6*a*b^7*x^7 + 15*a^2*b^6*x^6 + 20*a^3*b^5*x^5 + 15*a^4*b^4*x^4 + 6*a^5*b^3*x^3 + a^6*b^2*x^2)*log(b*x + a) + 840*(b^8*x^8 + 6*a*b^7*x^7 + 15*a^2*b^6*x^6 + 20*a^3*b^5*x^5 + 15*a^4*b^4*x^4 + 6*a^5*b^3*x^3 + a^6*b^2*x^2)*log(x))/(a^9*b^6*x^8 + 6*a^10*b^5*x^7 + 15*a^11*b^4*x^6 + 20*a^12*b^3*x^5 + 15*a^13*b^2*x^4 + 6*a^14*b*x^3 + a^15*x^2)

giac [A] time = 1.27, size = 119, normalized size = 0.83

$$-\frac{28b^2 \log(|bx + a|)}{a^9} + \frac{28b^2 \log(|x|)}{a^9} + \frac{840 ab^7 x^7 + 4620 a^2 b^6 x^6 + 10360 a^3 b^5 x^5 + 11970 a^4 b^4 x^4 + 7308 a^5 b^3 x^3 + 2058 a^6 b^2 x^2 + 120 a^7 b x - 15 a^8}{30 (bx + a)^6 a^9 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^7,x, algorithm="giac")

[Out] -28*b^2*log(abs(b*x + a))/a^9 + 28*b^2*log(abs(x))/a^9 + 1/30*(840*a*b^7*x^7 + 4620*a^2*b^6*x^6 + 10360*a^3*b^5*x^5 + 11970*a^4*b^4*x^4 + 7308*a^5*b^3*x^3 + 2058*a^6*b^2*x^2 + 120*a^7*b*x - 15*a^8)/((b*x + a)^6*a^9*x^2)

maple [A] time = 0.01, size = 133, normalized size = 0.92

$$\frac{b^2}{6(bx+a)^6 a^3} + \frac{3b^2}{5(bx+a)^5 a^4} + \frac{3b^2}{2(bx+a)^4 a^5} + \frac{10b^2}{3(bx+a)^3 a^6} + \frac{15b^2}{2(bx+a)^2 a^7} + \frac{21b^2}{(bx+a) a^8} + \frac{28b^2 \ln(x)}{a^9} - \frac{28b^2 \ln(a+bx)}{a^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/x^3/(b*x+a)^7, x)$

[Out] $-1/2/a^7/x^2+7*b/a^8/x+1/6*b^2/a^3/(b*x+a)^6+3/5*b^2/a^4/(b*x+a)^5+3/2*b^2/a^5/(b*x+a)^4+10/3*b^2/a^6/(b*x+a)^3+15/2*b^2/a^7/(b*x+a)^2+21*b^2/a^8/(b*x+a)+28*b^2*\ln(x)/a^9-28*b^2*\ln(b*x+a)/a^9$

maxima [A] time = 1.55, size = 174, normalized size = 1.21

$$\frac{840 b^7 x^7 + 4620 a b^6 x^6 + 10360 a^2 b^5 x^5 + 11970 a^3 b^4 x^4 + 7308 a^4 b^3 x^3 + 2058 a^5 b^2 x^2 + 120 a^6 b x - 15 a^7}{30 (a^8 b^6 x^8 + 6 a^9 b^5 x^7 + 15 a^{10} b^4 x^6 + 20 a^{11} b^3 x^5 + 15 a^{12} b^2 x^4 + 6 a^{13} b x^3 + a^{14} x^2)} - \frac{28 b^2 \log(x)}{a^9} + \frac{28 b^2 \log(b x + a)}{a^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^3/(b*x+a)^7, x, \text{algorithm}="maxima")$

[Out] $1/30*(840*b^7*x^7 + 4620*a*b^6*x^6 + 10360*a^2*b^5*x^5 + 11970*a^3*b^4*x^4 + 7308*a^4*b^3*x^3 + 2058*a^5*b^2*x^2 + 120*a^6*b*x - 15*a^7)/(a^8*b^6*x^8 + 6*a^9*b^5*x^7 + 15*a^{10}*b^4*x^6 + 20*a^{11}*b^3*x^5 + 15*a^{12}*b^2*x^4 + 6*a^{13}*b*x^3 + a^{14}*x^2) - 28*b^2*\log(b*x + a)/a^9 + 28*b^2*\log(x)/a^9$

mupad [B] time = 0.21, size = 167, normalized size = 1.16

$$\frac{\frac{343 b^2 x^2}{5 a^3} - \frac{1}{2 a} + \frac{1218 b^3 x^3}{5 a^4} + \frac{399 b^4 x^4}{a^5} + \frac{1036 b^5 x^5}{3 a^6} + \frac{154 b^6 x^6}{a^7} + \frac{28 b^7 x^7}{a^8} + \frac{4 b x}{a^2}}{6 a^5 b x^3 + 15 a^4 b^2 x^4 + 20 a^3 b^3 x^5 + 15 a^2 b^4 x^6 + 6 a b^5 x^7 + b^6 x^8} - \frac{56 b^2 \operatorname{atanh}\left(\frac{2 b x}{a} + 1\right)}{a^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(x^3*(a + b*x)^7), x)$

[Out] $((343*b^2*x^2)/(5*a^3) - 1/(2*a) + (1218*b^3*x^3)/(5*a^4) + (399*b^4*x^4)/a^5 + (1036*b^5*x^5)/(3*a^6) + (154*b^6*x^6)/a^7 + (28*b^7*x^7)/a^8 + (4*b*x)/a^2)/(a^6*x^2 + b^6*x^8 + 6*a^5*b*x^3 + 6*a*b^5*x^7 + 15*a^4*b^2*x^4 + 20*a^3*b^3*x^5 + 15*a^2*b^4*x^6) - (56*b^2*\operatorname{atanh}((2*b*x)/a + 1))/a^9$

sympy [A] time = 0.84, size = 175, normalized size = 1.22

$$\frac{-15 a^7 + 120 a^6 b x + 2058 a^5 b^2 x^2 + 7308 a^4 b^3 x^3 + 11970 a^3 b^4 x^4 + 10360 a^2 b^5 x^5 + 4620 a b^6 x^6 + 840 b^7 x^7}{30 a^{14} x^2 + 180 a^{13} b x^3 + 450 a^{12} b^2 x^4 + 600 a^{11} b^3 x^5 + 450 a^{10} b^4 x^6 + 180 a^9 b^5 x^7 + 30 a^8 b^6 x^8} + \frac{28 b^2 (\log(x) + \log(b x + a))}{a^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^{**3}/(b*x+a)^{**7}, x)$

[Out] $(-15*a^{**7} + 120*a^{**6}*b*x + 2058*a^{**5}*b^{**2}*x^{**2} + 7308*a^{**4}*b^{**3}*x^{**3} + 11970*a^{**3}*b^{**4}*x^{**4} + 10360*a^{**2}*b^{**5}*x^{**5} + 4620*a*b^{**6}*x^{**6} + 840*b^{**7}*x^{**7})/30*(a^{14}*x^2 + 180*a^{13}*b*x^3 + 450*a^{12}*b^2*x^4 + 600*a^{11}*b^3*x^5 + 450*a^{10}*b^4*x^6 + 180*a^9*b^5*x^7 + 30*a^8*b^6*x^8) + 28*b^2*(\log(x) + \log(b*x+a))/a^9$

$$\frac{1}{(30a^{14}x^2 + 180a^{13}bx^3 + 450a^{12}b^2x^4 + 600a^{11}b^3x^5 + 450a^{10}b^4x^6 + 180a^9b^5x^7 + 30a^8b^6x^8) + 28b^2(\log(x) - \log(a/b + x))}a^9$$

Mathematica [A] time = 0.09, size = 123, normalized size = 0.78

$$\frac{a(10a^8 - 45a^7bx + 360a^6b^2x^2 + 6174a^5b^3x^3 + 21924a^4b^4x^4 + 35910a^3b^5x^5 + 31080a^2b^6x^6 + 13860ab^7x^7 + 2520b^8x^8)}{x^3(a+bx)^6} - 2520b^3 \log(a+bx) + 2520b^3 \log(a)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^4*(a + b*x)^7),x]

[Out] -1/30*((a*(10*a^8 - 45*a^7*b*x + 360*a^6*b^2*x^2 + 6174*a^5*b^3*x^3 + 21924*a^4*b^4*x^4 + 35910*a^3*b^5*x^5 + 31080*a^2*b^6*x^6 + 13860*a*b^7*x^7 + 2520*b^8*x^8))/(x^3*(a + b*x)^6) + 2520*b^3*Log[x] - 2520*b^3*Log[a + b*x])/a^10

fricas [B] time = 0.44, size = 317, normalized size = 2.02

$$\frac{2520 ab^8 x^8 + 13860 a^2 b^7 x^7 + 31080 a^3 b^6 x^6 + 35910 a^4 b^5 x^5 + 21924 a^5 b^4 x^4 + 6174 a^6 b^3 x^3 + 360 a^7 b^2 x^2 - 45 a^8 b x + 10 a^9}{(a + b x)^6 a^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^7,x, algorithm="fricas")

[Out] -1/30*(2520*a*b^8*x^8 + 13860*a^2*b^7*x^7 + 31080*a^3*b^6*x^6 + 35910*a^4*b^5*x^5 + 21924*a^5*b^4*x^4 + 6174*a^6*b^3*x^3 + 360*a^7*b^2*x^2 - 45*a^8*b*x + 10*a^9 - 2520*(b^9*x^9 + 6*a*b^8*x^8 + 15*a^2*b^7*x^7 + 20*a^3*b^6*x^6 + 15*a^4*b^5*x^5 + 6*a^5*b^4*x^4 + a^6*b^3*x^3)*log(b*x + a) + 2520*(b^9*x^9 + 6*a*b^8*x^8 + 15*a^2*b^7*x^7 + 20*a^3*b^6*x^6 + 15*a^4*b^5*x^5 + 6*a^5*b^4*x^4 + a^6*b^3*x^3)*log(x))/(a^10*b^6*x^9 + 6*a^11*b^5*x^8 + 15*a^12*b^4*x^7 + 20*a^13*b^3*x^6 + 15*a^14*b^2*x^5 + 6*a^15*b*x^4 + a^16*x^3)

giac [A] time = 1.25, size = 130, normalized size = 0.83

$$\frac{84 b^3 \log(|bx + a|)}{a^{10}} - \frac{84 b^3 \log(|x|)}{a^{10}} - \frac{2520 ab^8 x^8 + 13860 a^2 b^7 x^7 + 31080 a^3 b^6 x^6 + 35910 a^4 b^5 x^5 + 21924 a^5 b^4 x^4}{30 (bx + a)^6 a^{10} x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^7,x, algorithm="giac")

[Out] 84*b^3*log(abs(b*x + a))/a^10 - 84*b^3*log(abs(x))/a^10 - 1/30*(2520*a*b^8*x^8 + 13860*a^2*b^7*x^7 + 31080*a^3*b^6*x^6 + 35910*a^4*b^5*x^5 + 21924*a^5*b^4*x^4 + 6174*a^6*b^3*x^3 + 360*a^7*b^2*x^2 - 45*a^8*b*x + 10*a^9)/((b*x + a)^6*a^10*x^3)

maple [A] time = 0.01, size = 144, normalized size = 0.92

$$\frac{b^3}{6(bx+a)^6 a^4} - \frac{4b^3}{5(bx+a)^5 a^5} - \frac{5b^3}{2(bx+a)^4 a^6} - \frac{20b^3}{3(bx+a)^3 a^7} - \frac{35b^3}{2(bx+a)^2 a^8} - \frac{56b^3}{(bx+a) a^9} - \frac{84b^3 \ln(x)}{a^{10}} + \frac{84b^3 \ln(bx+a)}{a^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^4/(b*x+a)^7,x)

[Out] $-\frac{1}{3} \frac{b^3}{a^7 x^3} + \frac{7}{2} \frac{b^2}{a^8 x^2} - 28 \frac{b^2}{a^9 x} - \frac{1}{6} \frac{b^3}{a^4 (bx+a)^6} - \frac{4}{5} \frac{b^3}{a^5 (bx+a)^5} - \frac{5}{2} \frac{b^3}{a^6 (bx+a)^4} - \frac{20}{3} \frac{b^3}{a^7 (bx+a)^3} - \frac{35}{2} \frac{b^3}{a^8 (bx+a)^2} - 56 \frac{b^3}{a^9 (bx+a)} - 84 \frac{b^3 \ln(x)}{a^{10}} + 84 \frac{b^3 \ln(bx+a)}{a^{10}}$

maxima [A] time = 1.59, size = 185, normalized size = 1.18

$$\frac{2520 b^8 x^8 + 13860 a b^7 x^7 + 31080 a^2 b^6 x^6 + 35910 a^3 b^5 x^5 + 21924 a^4 b^4 x^4 + 6174 a^5 b^3 x^3 + 360 a^6 b^2 x^2 - 45 a^7 b x}{30 (a^9 b^6 x^9 + 6 a^{10} b^5 x^8 + 15 a^{11} b^4 x^7 + 20 a^{12} b^3 x^6 + 15 a^{13} b^2 x^5 + 6 a^{14} b x^4 + a^{15} x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^7,x, algorithm="maxima")

[Out] $-\frac{1}{30} \frac{(2520 b^8 x^8 + 13860 a b^7 x^7 + 31080 a^2 b^6 x^6 + 35910 a^3 b^5 x^5 + 21924 a^4 b^4 x^4 + 6174 a^5 b^3 x^3 + 360 a^6 b^2 x^2 - 45 a^7 b x + 10 a^8)}{(a^9 b^6 x^9 + 6 a^{10} b^5 x^8 + 15 a^{11} b^4 x^7 + 20 a^{12} b^3 x^6 + 15 a^{13} b^2 x^5 + 6 a^{14} b x^4 + a^{15} x^3)} + 84 \frac{b^3 \log(bx+a)}{a^{10}} - 84 \frac{b^3 \log(x)}{a^{10}}$

mupad [B] time = 0.31, size = 179, normalized size = 1.14

$$\frac{168 b^3 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^{10}} - \frac{\frac{1}{3a} + \frac{12b^2 x^2}{a^3} + \frac{1029b^3 x^3}{5a^4} + \frac{3654b^4 x^4}{5a^5} + \frac{1197b^5 x^5}{a^6} + \frac{1036b^6 x^6}{a^7} + \frac{462b^7 x^7}{a^8} + \frac{84b^8 x^8}{a^9} - \frac{3bx}{2a^2}}{a^6 x^3 + 6 a^5 b x^4 + 15 a^4 b^2 x^5 + 20 a^3 b^3 x^6 + 15 a^2 b^4 x^7 + 6 a b^5 x^8 + b^6 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^4*(a + b*x)^7),x)

[Out] $\frac{168 b^3 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^{10}} - \frac{1}{3a} + \frac{12 b^2 x^2}{a^3} + \frac{1029 b^3 x^3}{5 a^4} + \frac{3654 b^4 x^4}{5 a^5} + \frac{1197 b^5 x^5}{a^6} + \frac{1036 b^6 x^6}{a^7} + \frac{462 b^7 x^7}{a^8} + \frac{84 b^8 x^8}{a^9} - \frac{3 b x}{2 a^2} + \frac{b^6 x^9}{a^{10}}$

sympy [A] time = 0.99, size = 187, normalized size = 1.19

$$\frac{-10a^8 + 45a^7bx - 360a^6b^2x^2 - 6174a^5b^3x^3 - 21924a^4b^4x^4 - 35910a^3b^5x^5 - 31080a^2b^6x^6 - 13860ab^7x^7 - 2520b^8}{30a^{15}x^3 + 180a^{14}bx^4 + 450a^{13}b^2x^5 + 600a^{12}b^3x^6 + 450a^{11}b^4x^7 + 180a^{10}b^5x^8 + 30a^9b^6x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**4/(b*x+a)**7,x)
```

```
[Out] (-10*a**8 + 45*a**7*b*x - 360*a**6*b**2*x**2 - 6174*a**5*b**3*x**3 - 21924*  
a**4*b**4*x**4 - 35910*a**3*b**5*x**5 - 31080*a**2*b**6*x**6 - 13860*a*b**7  
*x**7 - 2520*b**8*x**8)/(30*a**15*x**3 + 180*a**14*b*x**4 + 450*a**13*b**2*  
x**5 + 600*a**12*b**3*x**6 + 450*a**11*b**4*x**7 + 180*a**10*b**5*x**8 + 30  
*a**9*b**6*x**9) + 84*b**3*(-log(x) + log(a/b + x))/a**10
```

$$3.222 \quad \int \frac{x^{12}}{(a+bx)^{10}} dx$$

Optimal. Leaf size=186

$$-\frac{a^{12}}{9b^{13}(a+bx)^9} + \frac{3a^{11}}{2b^{13}(a+bx)^8} - \frac{66a^{10}}{7b^{13}(a+bx)^7} + \frac{110a^9}{3b^{13}(a+bx)^6} - \frac{99a^8}{b^{13}(a+bx)^5} + \frac{198a^7}{b^{13}(a+bx)^4} - \frac{308a^6}{b^{13}(a+bx)^3} + \frac{396a^5}{b^{13}(a+bx)^2} - \frac{495a^4}{b^{13}(a+bx)} + \frac{220a^3 \ln(bx+a)}{b^{13}}$$

[Out] $55*a^2*x/b^{12} - 5*a*x^2/b^{11} + 1/3*x^3/b^{10} - 1/9*a^{12}/b^{13}/(b*x+a)^9 + 3/2*a^{11}/b^{13}/(b*x+a)^8 - 66/7*a^{10}/b^{13}/(b*x+a)^7 + 110/3*a^9/b^{13}/(b*x+a)^6 - 99*a^8/b^{13}/(b*x+a)^5 + 198*a^7/b^{13}/(b*x+a)^4 - 308*a^6/b^{13}/(b*x+a)^3 + 396*a^5/b^{13}/(b*x+a)^2 - 495*a^4/b^{13}/(b*x+a) - 220*a^3*\ln(b*x+a)/b^{13}$

Rubi [A] time = 0.18, antiderivative size = 186, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^{12}}{9b^{13}(a+bx)^9} + \frac{3a^{11}}{2b^{13}(a+bx)^8} - \frac{66a^{10}}{7b^{13}(a+bx)^7} + \frac{110a^9}{3b^{13}(a+bx)^6} - \frac{99a^8}{b^{13}(a+bx)^5} + \frac{198a^7}{b^{13}(a+bx)^4} - \frac{308a^6}{b^{13}(a+bx)^3} + \frac{396a^5}{b^{13}(a+bx)^2} - \frac{495a^4}{b^{13}(a+bx)} + \frac{220a^3 \ln(bx+a)}{b^{13}}$$

Antiderivative was successfully verified.

[In] Int[x^12/(a + b*x)^10, x]

[Out] $(55*a^2*x)/b^{12} - (5*a*x^2)/b^{11} + x^3/(3*b^{10}) - a^{12}/(9*b^{13}*(a + b*x)^9) + (3*a^{11})/(2*b^{13}*(a + b*x)^8) - (66*a^{10})/(7*b^{13}*(a + b*x)^7) + (110*a^9)/(3*b^{13}*(a + b*x)^6) - (99*a^8)/(b^{13}*(a + b*x)^5) + (198*a^7)/(b^{13}*(a + b*x)^4) - (308*a^6)/(b^{13}*(a + b*x)^3) + (396*a^5)/(b^{13}*(a + b*x)^2) - (495*a^4)/(b^{13}*(a + b*x)) - (220*a^3*\text{Log}[a + b*x])/b^{13}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{x^{12}}{(a+bx)^{10}} dx = \int \left(\frac{55a^2}{b^{12}} - \frac{10ax}{b^{11}} + \frac{x^2}{b^{10}} + \frac{a^{12}}{b^{12}(a+bx)^{10}} - \frac{12a^{11}}{b^{12}(a+bx)^9} + \frac{66a^{10}}{b^{12}(a+bx)^8} - \frac{220a^9}{b^{12}(a+bx)^7} + \frac{495a^8}{b^{12}(a+bx)^6} - \frac{308a^7}{b^{12}(a+bx)^5} + \frac{198a^6}{b^{12}(a+bx)^4} - \frac{99a^5}{b^{12}(a+bx)^3} + \frac{396a^4}{b^{12}(a+bx)^2} - \frac{220a^3 \ln(bx+a)}{b^{12}} \right) dx$$

$$= \frac{55a^2x}{b^{12}} - \frac{5ax^2}{b^{11}} + \frac{x^3}{3b^{10}} - \frac{a^{12}}{9b^{13}(a+bx)^9} + \frac{3a^{11}}{2b^{13}(a+bx)^8} - \frac{66a^{10}}{7b^{13}(a+bx)^7} + \frac{110a^9}{3b^{13}(a+bx)^6} - \frac{99a^8}{b^{13}(a+bx)^5} + \frac{198a^7}{b^{13}(a+bx)^4} - \frac{308a^6}{b^{13}(a+bx)^3} + \frac{396a^5}{b^{13}(a+bx)^2} - \frac{495a^4}{b^{13}(a+bx)} + \frac{220a^3 \ln(bx+a)}{b^{13}}$$

Mathematica [A] time = 0.05, size = 161, normalized size = 0.87

$$\frac{35201a^{12} + 289089a^{11}bx + 1031616a^{10}b^2x^2 + 2074464a^9b^3x^3 + 2529576a^8b^4x^4 + 1831032a^7b^5x^5 + 638568a^6b^6x^6 - 58968a^5b^7x^7 - 139482a^4b^8x^8 - 43218a^3b^9x^9 - 2772a^2b^{10}x^{10} + 252ab^{11}x^{11} - 42b^{12}x^{12} + 27720a^3(a + bx)^9 \operatorname{Log}[a + bx]}{b^{13}(a + bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^12/(a + b*x)^10,x]

[Out]
$$\frac{-1/126*(35201*a^{12} + 289089*a^{11}*b*x + 1031616*a^{10}*b^2*x^2 + 2074464*a^9*b^3*x^3 + 2529576*a^8*b^4*x^4 + 1831032*a^7*b^5*x^5 + 638568*a^6*b^6*x^6 - 58968*a^5*b^7*x^7 - 139482*a^4*b^8*x^8 - 43218*a^3*b^9*x^9 - 2772*a^2*b^{10}*x^{10} + 252*a*b^{11}*x^{11} - 42*b^{12}*x^{12} + 27720*a^3*(a + b*x)^9*\operatorname{Log}[a + b*x])}{b^{13}*(a + b*x)^9}$$

fricas [A] time = 0.47, size = 338, normalized size = 1.82

$$\frac{42b^{12}x^{12} - 252ab^{11}x^{11} + 2772a^2b^{10}x^{10} + 43218a^3b^9x^9 + 139482a^4b^8x^8 + 58968a^5b^7x^7 - 638568a^6b^6x^6 - 1831032a^7b^5x^5 - 2529576a^8b^4x^4 - 2074464a^9b^3x^3 - 1031616a^{10}b^2x^2 - 289089a^{11}bx - 35201a^{12} - 27720(a^3b^9x^9 + 9a^4b^8x^8 + 36a^5b^7x^7 + 84a^6b^6x^6 + 126a^7b^5x^5 + 126a^8b^4x^4 + 84a^9b^3x^3 + 36a^{10}b^2x^2 + 9a^{11}bx + a^{12})\log(bx + a)}{b^{22}x^9 + 9a^2b^{21}x^8 + 36a^3b^{20}x^7 + 84a^4b^{19}x^6 + 126a^5b^{18}x^5 + 126a^6b^{17}x^4 + 84a^7b^{16}x^3 + 36a^8b^{15}x^2 + 9a^9b^{14}x + a^9b^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^12/(b*x+a)^10,x, algorithm="fricas")

[Out]
$$\frac{1/126*(42*b^{12}*x^{12} - 252*a*b^{11}*x^{11} + 2772*a^2*b^{10}*x^{10} + 43218*a^3*b^9*x^9 + 139482*a^4*b^8*x^8 + 58968*a^5*b^7*x^7 - 638568*a^6*b^6*x^6 - 1831032*a^7*b^5*x^5 - 2529576*a^8*b^4*x^4 - 2074464*a^9*b^3*x^3 - 1031616*a^{10}*b^2*x^2 - 289089*a^{11}*b*x - 35201*a^{12} - 27720*(a^3*b^9*x^9 + 9*a^4*b^8*x^8 + 36*a^5*b^7*x^7 + 84*a^6*b^6*x^6 + 126*a^7*b^5*x^5 + 126*a^8*b^4*x^4 + 84*a^9*b^3*x^3 + 36*a^{10}*b^2*x^2 + 9*a^{11}*b*x + a^{12})*\log(b*x + a))}{b^{22}*x^9 + 9*a^2*b^{21}*x^8 + 36*a^3*b^{20}*x^7 + 84*a^4*b^{19}*x^6 + 126*a^5*b^{18}*x^5 + 126*a^6*b^{17}*x^4 + 84*a^7*b^{16}*x^3 + 36*a^8*b^{15}*x^2 + 9*a^9*b^{14}*x + a^9*b^{13}}$$

giac [A] time = 1.07, size = 149, normalized size = 0.80

$$\frac{220a^3 \log(|bx + a|)}{b^{13}} - \frac{62370a^4b^8x^8 + 449064a^5b^7x^7 + 1435896a^6b^6x^6 + 2652804a^7b^5x^5 + 3089394a^8b^4x^4 + 2318316a^9b^3x^3 + 1093356a^{10}b^2x^2 + 296019a^{11}bx + 35201a^{12}}{126(bx + a)^9b^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^12/(b*x+a)^10,x, algorithm="giac")

[Out]
$$-220*a^3*\log(\operatorname{abs}(b*x + a))/b^{13} - 1/126*(62370*a^4*b^8*x^8 + 449064*a^5*b^7*x^7 + 1435896*a^6*b^6*x^6 + 2652804*a^7*b^5*x^5 + 3089394*a^8*b^4*x^4 + 2318316*a^9*b^3*x^3 + 1093356*a^{10}*b^2*x^2 + 296019*a^{11}*b*x + 35201*a^{12})/((b*x + a)^9*b^{13}) + 1/3*(b^{20}*x^3 - 15*a*b^{19}*x^2 + 165*a^2*b^{18}*x)/b^{30}$$

maple [A] time = 0.01, size = 177, normalized size = 0.95

$$\frac{a^{12}}{9(bx+a)^9 b^{13}} + \frac{3a^{11}}{2(bx+a)^8 b^{13}} - \frac{66a^{10}}{7(bx+a)^7 b^{13}} + \frac{110a^9}{3(bx+a)^6 b^{13}} - \frac{99a^8}{(bx+a)^5 b^{13}} + \frac{198a^7}{(bx+a)^4 b^{13}} - \frac{308a^6}{(bx+a)^3 b^{13}} + \frac{x}{3b^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^12/(b*x+a)^10,x)

[Out] 55*a^2*x/b^12-5*a*x^2/b^11+1/3*x^3/b^10-1/9*a^12/b^13/(b*x+a)^9+3/2*a^11/b^13/(b*x+a)^8-66/7*a^10/b^13/(b*x+a)^7+110/3*a^9/b^13/(b*x+a)^6-99*a^8/b^13/(b*x+a)^5+198*a^7/b^13/(b*x+a)^4-308*a^6/b^13/(b*x+a)^3+396*a^5/b^13/(b*x+a)^2-495*a^4/b^13/(b*x+a)-220*a^3*ln(b*x+a)/b^13

maxima [A] time = 1.73, size = 234, normalized size = 1.26

$$\frac{62370 a^4 b^8 x^8 + 449064 a^5 b^7 x^7 + 1435896 a^6 b^6 x^6 + 2652804 a^7 b^5 x^5 + 3089394 a^8 b^4 x^4 + 2318316 a^9 b^3 x^3 + 1093356 a^{10} b^2 x^2 + 296019 a^{11} b x + 35201 a^{12}}{126 (b^{22} x^9 + 9 a b^{21} x^8 + 36 a^2 b^{20} x^7 + 84 a^3 b^{19} x^6 + 126 a^4 b^{18} x^5 + 126 a^5 b^{17} x^4 + 84 a^6 b^{16} x^3 + 36 a^7 b^{15} x^2 + 9 a^8 b^{14} x + a^9 b^{13})} - 220 a^3 \log(bx+a) / b^{13}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^12/(b*x+a)^10,x, algorithm="maxima")

[Out] -1/126*(62370*a^4*b^8*x^8 + 449064*a^5*b^7*x^7 + 1435896*a^6*b^6*x^6 + 2652804*a^7*b^5*x^5 + 3089394*a^8*b^4*x^4 + 2318316*a^9*b^3*x^3 + 1093356*a^10*b^2*x^2 + 296019*a^11*b*x + 35201*a^12)/(b^22*x^9 + 9*a*b^21*x^8 + 36*a^2*b^20*x^7 + 84*a^3*b^19*x^6 + 126*a^4*b^18*x^5 + 126*a^5*b^17*x^4 + 84*a^6*b^16*x^3 + 36*a^7*b^15*x^2 + 9*a^8*b^14*x + a^9*b^13) - 220*a^3*log(b*x + a)/b^13 + 1/3*(b^2*x^3 - 15*a*b*x^2 + 165*a^2*x)/b^12

mupad [B] time = 0.98, size = 151, normalized size = 0.81

$$\frac{6a(a+bx)^2 - \frac{(a+bx)^3}{3} + \frac{495a^4}{a+bx} - \frac{396a^5}{(a+bx)^2} + \frac{308a^6}{(a+bx)^3} - \frac{198a^7}{(a+bx)^4} + \frac{99a^8}{(a+bx)^5} - \frac{110a^9}{3(a+bx)^6} + \frac{66a^{10}}{7(a+bx)^7} - \frac{3a^{11}}{2(a+bx)^8} + \frac{a^{12}}{9(a+bx)^9}}{b^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^12/(a + b*x)^10,x)

[Out] -(6*a*(a + b*x)^2 - (a + b*x)^3/3 + (495*a^4)/(a + b*x) - (396*a^5)/(a + b*x)^2 + (308*a^6)/(a + b*x)^3 - (198*a^7)/(a + b*x)^4 + (99*a^8)/(a + b*x)^5 - (110*a^9)/(3*(a + b*x)^6) + (66*a^10)/(7*(a + b*x)^7) - (3*a^11)/(2*(a + b*x)^8) + a^12/(9*(a + b*x)^9) + 220*a^3*log(a + b*x) - 66*a^2*b*x)/b^13

sympy [A] time = 1.54, size = 250, normalized size = 1.34

$$\frac{220a^3 \log(a+bx)}{b^{13}} + \frac{55a^2x}{b^{12}} - \frac{5ax^2}{b^{11}} + \frac{-35201a^{12} - 296019a^{11}bx - 1093356a^{10}b^2x^2 - 2318316a^9b^3x^3 - 3089394a^8b^4x^4 - 2318316a^7b^5x^5 - 1093356a^6b^6x^6 - 3089394a^5b^7x^7 - 449064a^4b^8x^8 - 62370a^3b^9x^9}{126a^9b^{13} + 1134a^8b^{14}x + 4536a^7b^{15}x^2 + 10584a^6b^{16}x^3 + 15876a^5b^{17}x^4 + 1093356a^4b^{18}x^5 + 3089394a^3b^{19}x^6 + 62370a^2b^{20}x^7 + 449064ab^{21}x^8 + 62370b^{22}x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**12/(b*x+a)**10,x)`

[Out]
$$\begin{aligned} & -220*a**3*\log(a + b*x)/b**13 + 55*a**2*x/b**12 - 5*a*x**2/b**11 + (-35201*a \\ & **12 - 296019*a**11*b*x - 1093356*a**10*b**2*x**2 - 2318316*a**9*b**3*x**3 \\ & - 3089394*a**8*b**4*x**4 - 2652804*a**7*b**5*x**5 - 1435896*a**6*b**6*x**6 \\ & - 449064*a**5*b**7*x**7 - 62370*a**4*b**8*x**8)/(126*a**9*b**13 + 1134*a**8 \\ & *b**14*x + 4536*a**7*b**15*x**2 + 10584*a**6*b**16*x**3 + 15876*a**5*b**17* \\ & x**4 + 15876*a**4*b**18*x**5 + 10584*a**3*b**19*x**6 + 4536*a**2*b**20*x**7 \\ & + 1134*a*b**21*x**8 + 126*b**22*x**9) + x**3/(3*b**10) \end{aligned}$$

$$3.223 \quad \int \frac{x^{11}}{(a+bx)^{10}} dx$$

Optimal. Leaf size=177

$$\frac{a^{11}}{9b^{12}(a+bx)^9} - \frac{11a^{10}}{8b^{12}(a+bx)^8} + \frac{55a^9}{7b^{12}(a+bx)^7} - \frac{55a^8}{2b^{12}(a+bx)^6} + \frac{66a^7}{b^{12}(a+bx)^5} - \frac{231a^6}{2b^{12}(a+bx)^4} + \frac{154a^5}{b^{12}(a+bx)^3} - \frac{165a^4}{b^{12}(a+bx)^2} + \frac{165a^3}{b^{12}(a+bx)} - \frac{55a^2 \ln(bx+a)}{b^{12}}$$

[Out] $-10*a*x/b^{11} + 1/2*x^2/b^{10} + 1/9*a^{11}/b^{12}/(b*x+a)^9 - 11/8*a^{10}/b^{12}/(b*x+a)^8 + 55/7*a^9/b^{12}/(b*x+a)^7 - 55/2*a^8/b^{12}/(b*x+a)^6 + 66*a^7/b^{12}/(b*x+a)^5 - 231/2*a^6/b^{12}/(b*x+a)^4 + 154*a^5/b^{12}/(b*x+a)^3 - 165*a^4/b^{12}/(b*x+a)^2 + 165*a^3/b^{12}/(b*x+a) + 55*a^2*\ln(b*x+a)/b^{12}$

Rubi [A] time = 0.14, antiderivative size = 177, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^{11}}{9b^{12}(a+bx)^9} - \frac{11a^{10}}{8b^{12}(a+bx)^8} + \frac{55a^9}{7b^{12}(a+bx)^7} - \frac{55a^8}{2b^{12}(a+bx)^6} + \frac{66a^7}{b^{12}(a+bx)^5} - \frac{231a^6}{2b^{12}(a+bx)^4} + \frac{154a^5}{b^{12}(a+bx)^3} - \frac{165a^4}{b^{12}(a+bx)^2} + \frac{165a^3}{b^{12}(a+bx)} - \frac{55a^2 \ln(bx+a)}{b^{12}}$$

Antiderivative was successfully verified.

[In] Int[x^11/(a + b*x)^10, x]

[Out] $(-10*a*x)/b^{11} + x^2/(2*b^{10}) + a^{11}/(9*b^{12}*(a + b*x)^9) - (11*a^{10})/(8*b^{12}*(a + b*x)^8) + (55*a^9)/(7*b^{12}*(a + b*x)^7) - (55*a^8)/(2*b^{12}*(a + b*x)^6) + (66*a^7)/(b^{12}*(a + b*x)^5) - (231*a^6)/(2*b^{12}*(a + b*x)^4) + (154*a^5)/(b^{12}*(a + b*x)^3) - (165*a^4)/(b^{12}*(a + b*x)^2) + (165*a^3)/(b^{12}*(a + b*x)) + (55*a^2*\text{Log}[a + b*x])/b^{12}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{x^{11}}{(a+bx)^{10}} dx = \int \left(-\frac{10a}{b^{11}} + \frac{x}{b^{10}} - \frac{a^{11}}{b^{11}(a+bx)^{10}} + \frac{11a^{10}}{b^{11}(a+bx)^9} - \frac{55a^9}{b^{11}(a+bx)^8} + \frac{165a^8}{b^{11}(a+bx)^7} - \frac{330a^7}{b^{11}(a+bx)^6} \right. \\ \left. - \frac{10ax}{b^{11}} + \frac{x^2}{2b^{10}} + \frac{a^{11}}{9b^{12}(a+bx)^9} - \frac{11a^{10}}{8b^{12}(a+bx)^8} + \frac{55a^9}{7b^{12}(a+bx)^7} - \frac{55a^8}{2b^{12}(a+bx)^6} + \frac{66a^7}{b^{12}(a+bx)^5} - \frac{231a^6}{2b^{12}(a+bx)^4} + \frac{154a^5}{b^{12}(a+bx)^3} - \frac{165a^4}{b^{12}(a+bx)^2} + \frac{165a^3}{b^{12}(a+bx)} - \frac{55a^2 \ln(bx+a)}{b^{12}} \right) dx$$

Mathematica [A] time = 0.03, size = 150, normalized size = 0.85

$$\frac{42131a^{11} + 351459a^{10}bx + 1281096a^9b^2x^2 + 2656584a^8b^3x^3 + 3402756a^7b^4x^4 + 2704212a^6b^5x^5 + 1220688a^5b^6x^6 + 190512a^4b^7x^7 - 77112a^3b^8x^8 - 36288a^2b^9x^9 - 2772ab^{10}x^{10} + 252b^{11}x^{11} + 27720a^2(a + bx)^9 \operatorname{Log}[a + bx]}{504b^{12}(a + bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^11/(a + b*x)^10,x]

[Out] (42131*a^11 + 351459*a^10*b*x + 1281096*a^9*b^2*x^2 + 2656584*a^8*b^3*x^3 + 3402756*a^7*b^4*x^4 + 2704212*a^6*b^5*x^5 + 1220688*a^5*b^6*x^6 + 190512*a^4*b^7*x^7 - 77112*a^3*b^8*x^8 - 36288*a^2*b^9*x^9 - 2772*a*b^10*x^10 + 252*b^11*x^11 + 27720*a^2*(a + b*x)^9*Log[a + b*x])/(504*b^12*(a + b*x)^9)

fricas [A] time = 0.43, size = 327, normalized size = 1.85

$$\frac{252b^{11}x^{11} - 2772ab^{10}x^{10} - 36288a^2b^9x^9 - 77112a^3b^8x^8 + 190512a^4b^7x^7 + 1220688a^5b^6x^6 + 2704212a^6b^5x^5 + 1220688a^7b^4x^4 + 2656584a^8b^3x^3 + 3402756a^9b^2x^2 + 351459a^{10}bx + 42131a^{11} + 27720(a^2b^9x^9 + 9a^3b^8x^8 + 36a^4b^7x^7 + 84a^5b^6x^6 + 126a^6b^5x^5 + 126a^7b^4x^4 + 84a^8b^3x^3 + 36a^9b^2x^2 + 9a^{10}bx + a^{11}) \log(bx + a)}{504(b^{21}x^9 + 9a^2b^{20}x^8 + 36a^3b^{19}x^7 + 84a^4b^{18}x^6 + 126a^5b^{17}x^5 + 126a^6b^{16}x^4 + 84a^7b^{15}x^3 + 36a^8b^{14}x^2 + 9a^9b^{13}x + a^{10}b^{12})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^11/(b*x+a)^10,x, algorithm="fricas")

[Out] 1/504*(252*b^11*x^11 - 2772*a*b^10*x^10 - 36288*a^2*b^9*x^9 - 77112*a^3*b^8*x^8 + 190512*a^4*b^7*x^7 + 1220688*a^5*b^6*x^6 + 2704212*a^6*b^5*x^5 + 3402756*a^7*b^4*x^4 + 2656584*a^8*b^3*x^3 + 1281096*a^9*b^2*x^2 + 351459*a^10*b*x + 42131*a^11 + 27720*(a^2*b^9*x^9 + 9*a^3*b^8*x^8 + 36*a^4*b^7*x^7 + 84*a^5*b^6*x^6 + 126*a^6*b^5*x^5 + 126*a^7*b^4*x^4 + 84*a^8*b^3*x^3 + 36*a^9*b^2*x^2 + 9*a^10*b*x + a^11)*log(b*x + a))/(b^21*x^9 + 9*a^2*b^20*x^8 + 36*a^3*b^19*x^7 + 84*a^4*b^18*x^6 + 126*a^5*b^17*x^5 + 126*a^6*b^16*x^4 + 84*a^7*b^15*x^3 + 36*a^8*b^14*x^2 + 9*a^9*b^13*x + a^10*b^12)

giac [A] time = 1.70, size = 138, normalized size = 0.78

$$\frac{55a^2 \log(|bx + a|)}{b^{12}} + \frac{b^{10}x^2 - 20ab^9x}{2b^{20}} + \frac{83160a^3b^8x^8 + 582120a^4b^7x^7 + 1823976a^5b^6x^6 + 3318084a^6b^5x^5 + 3817044a^7b^4x^4 + 2835756a^8b^3x^3 + 1326204a^9b^2x^2 + 356499a^{10}bx + 42131a^{11}}{504(b^{21}x^9 + 9a^2b^{20}x^8 + 36a^3b^{19}x^7 + 84a^4b^{18}x^6 + 126a^5b^{17}x^5 + 126a^6b^{16}x^4 + 84a^7b^{15}x^3 + 36a^8b^{14}x^2 + 9a^9b^{13}x + a^{10}b^{12})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^11/(b*x+a)^10,x, algorithm="giac")

[Out] 55*a^2*log(abs(b*x + a))/b^12 + 1/2*(b^10*x^2 - 20*a*b^9*x)/b^20 + 1/504*(83160*a^3*b^8*x^8 + 582120*a^4*b^7*x^7 + 1823976*a^5*b^6*x^6 + 3318084*a^6*b^5*x^5 + 3817044*a^7*b^4*x^4 + 2835756*a^8*b^3*x^3 + 1326204*a^9*b^2*x^2 + 356499*a^{10}*b*x + 42131*a^{11})/((b*x + a)^9*b^{12})

maple [A] time = 0.01, size = 166, normalized size = 0.94

$$\frac{a^{11}}{9(bx+a)^9 b^{12}} - \frac{11a^{10}}{8(bx+a)^8 b^{12}} + \frac{55a^9}{7(bx+a)^7 b^{12}} - \frac{55a^8}{2(bx+a)^6 b^{12}} + \frac{66a^7}{(bx+a)^5 b^{12}} - \frac{231a^6}{2(bx+a)^4 b^{12}} + \frac{154a^5}{(bx+a)^3 b^{12}} - \frac{11a^4}{(bx+a)^2 b^{12}} + \frac{11a^3}{(bx+a) b^{12}} - \frac{11a^2}{b^{12}} + \frac{11a}{b^{12}} - \frac{11}{b^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x¹¹/(b*x+a)¹⁰,x)

[Out] -10*a*x/b¹¹+1/2*x²/b¹⁰+1/9*a¹¹/b¹²/(b*x+a)⁹-11/8*a¹⁰/b¹²/(b*x+a)⁸+55/7*a⁹/b¹²/(b*x+a)⁷-55/2*a⁸/b¹²/(b*x+a)⁶+66*a⁷/b¹²/(b*x+a)⁵-231/2*a⁶/b¹²/(b*x+a)⁴+154*a⁵/b¹²/(b*x+a)³-165*a⁴/b¹²/(b*x+a)²+165*a³/b¹²/(b*x+a)+55*a²*ln(b*x+a)/b¹²

maxima [A] time = 1.65, size = 223, normalized size = 1.26

$$\frac{83160 a^3 b^8 x^8 + 582120 a^4 b^7 x^7 + 1823976 a^5 b^6 x^6 + 3318084 a^6 b^5 x^5 + 3817044 a^7 b^4 x^4 + 2835756 a^8 b^3 x^3 + 1326204 a^9 b^2 x^2 + 356499 a^{10} b x + 42131 a^{11}}{504 (b^{21} x^9 + 9 a b^{20} x^8 + 36 a^2 b^{19} x^7 + 84 a^3 b^{18} x^6 + 126 a^4 b^{17} x^5 + 126 a^5 b^{16} x^4 + 84 a^6 b^{15} x^3 + 36 a^7 b^{14} x^2 + 9 a^8 b^{13} x + a^9 b^{12})} + 55 a^2 \ln(a + b x) / b^{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x¹¹/(b*x+a)¹⁰,x, algorithm="maxima")

[Out] 1/504*(83160*a³*b⁸*x⁸ + 582120*a⁴*b⁷*x⁷ + 1823976*a⁵*b⁶*x⁶ + 3318084*a⁶*b⁵*x⁵ + 3817044*a⁷*b⁴*x⁴ + 2835756*a⁸*b³*x³ + 1326204*a⁹*b²*x² + 356499*a¹⁰*b*x + 42131*a¹¹)/(b²¹*x⁹ + 9*a*b²⁰*x⁸ + 36*a²*b¹⁹*x⁷ + 84*a³*b¹⁸*x⁶ + 126*a⁴*b¹⁷*x⁵ + 126*a⁵*b¹⁶*x⁴ + 84*a⁶*b¹⁵*x³ + 36*a⁷*b¹⁴*x² + 9*a⁸*b¹³*x + a⁹*b¹²) + 55*a²*log(b*x + a)/b¹²

mupad [B] time = 0.23, size = 138, normalized size = 0.78

$$\frac{(a+bx)^2}{2} + \frac{165a^3}{a+bx} - \frac{165a^4}{(a+bx)^2} + \frac{154a^5}{(a+bx)^3} - \frac{231a^6}{2(a+bx)^4} + \frac{66a^7}{(a+bx)^5} - \frac{55a^8}{2(a+bx)^6} + \frac{55a^9}{7(a+bx)^7} - \frac{11a^{10}}{8(a+bx)^8} + \frac{a^{11}}{9(a+bx)^9} + 55a^2 \ln(a + b x) / b^{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x¹¹/(a + b*x)¹⁰,x)

[Out] ((a + b*x)²/2 + (165*a³)/(a + b*x) - (165*a⁴)/(a + b*x)² + (154*a⁵)/(a + b*x)³ - (231*a⁶)/(2*(a + b*x)⁴ + (66*a⁷)/(a + b*x)⁵ - (55*a⁸)/(2*(a + b*x)⁶ + (55*a⁹)/(7*(a + b*x)⁷ - (11*a¹⁰)/(8*(a + b*x)⁸ + a¹¹/(9*(a + b*x)⁹ + 55*a²*log(a + b*x) - 11*a*b*x)/b¹²

sympy [A] time = 1.48, size = 236, normalized size = 1.33

$$\frac{55a^2 \log(a + bx)}{b^{12}} - \frac{10ax}{b^{11}} + \frac{42131a^{11} + 356499a^{10}bx + 1326204a^9b^2x^2 + 2835756a^8b^3x^3 + 3817044a^7b^4x^4 + 3318084a^6b^5x^5 + 1823976a^5b^6x^6 + 582120a^4b^7x^7 + 83160a^3b^8x^8}{504a^9b^{12} + 4536a^8b^{13}x + 18144a^7b^{14}x^2 + 42336a^6b^{15}x^3 + 63504a^5b^{16}x^4 + 63504a^4b^{17}x^5 + 42336a^3b^{18}x^6 + 18144a^2b^{19}x^7 + 4536ab^{20}x^8 + 504b^{21}x^9} + 55a^2 \ln(a + b x) / b^{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**11/(b*x+a)**10,x)`

[Out] $55*a**2*\log(a + b*x)/b**12 - 10*a*x/b**11 + (42131*a**11 + 356499*a**10*b*x + 1326204*a**9*b**2*x**2 + 2835756*a**8*b**3*x**3 + 3817044*a**7*b**4*x**4 + 3318084*a**6*b**5*x**5 + 1823976*a**5*b**6*x**6 + 582120*a**4*b**7*x**7 + 83160*a**3*b**8*x**8)/(504*a**9*b**12 + 4536*a**8*b**13*x + 18144*a**7*b**14*x**2 + 42336*a**6*b**15*x**3 + 63504*a**5*b**16*x**4 + 63504*a**4*b**17*x**5 + 42336*a**3*b**18*x**6 + 18144*a**2*b**19*x**7 + 4536*a*b**20*x**8 + 504*b**21*x**9) + x**2/(2*b**10)$

$$3.224 \quad \int \frac{x^{10}}{(a+bx)^{10}} dx$$

Optimal. Leaf size=159

$$-\frac{a^{10}}{9b^{11}(a+bx)^9} + \frac{5a^9}{4b^{11}(a+bx)^8} - \frac{45a^8}{7b^{11}(a+bx)^7} + \frac{20a^7}{b^{11}(a+bx)^6} - \frac{42a^6}{b^{11}(a+bx)^5} + \frac{63a^5}{b^{11}(a+bx)^4} - \frac{70a^4}{b^{11}(a+bx)^3} + \frac{60a^3}{b^{11}(a+bx)^2} - \frac{45a^2}{b^{11}(a+bx)} - \frac{10a \ln(bx+a)}{b^{11}}$$

[Out] $x/b^{10} - 1/9*a^{10}/b^{11}/(b*x+a)^9 + 5/4*a^9/b^{11}/(b*x+a)^8 - 45/7*a^8/b^{11}/(b*x+a)^7 + 20*a^7/b^{11}/(b*x+a)^6 - 42*a^6/b^{11}/(b*x+a)^5 + 63*a^5/b^{11}/(b*x+a)^4 - 70*a^4/b^{11}/(b*x+a)^3 + 60*a^3/b^{11}/(b*x+a)^2 - 45*a^2/b^{11}/(b*x+a) - 10*a*\ln(b*x+a)/b^{11}$

Rubi [A] time = 0.12, antiderivative size = 159, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^{10}}{9b^{11}(a+bx)^9} + \frac{5a^9}{4b^{11}(a+bx)^8} - \frac{45a^8}{7b^{11}(a+bx)^7} + \frac{20a^7}{b^{11}(a+bx)^6} - \frac{42a^6}{b^{11}(a+bx)^5} + \frac{63a^5}{b^{11}(a+bx)^4} - \frac{70a^4}{b^{11}(a+bx)^3} + \frac{60a^3}{b^{11}(a+bx)^2} - \frac{45a^2}{b^{11}(a+bx)} - \frac{10a \ln(bx+a)}{b^{11}}$$

Antiderivative was successfully verified.

[In] Int[x^10/(a + b*x)^10,x]

[Out] $x/b^{10} - a^{10}/(9*b^{11}*(a + b*x)^9) + (5*a^9)/(4*b^{11}*(a + b*x)^8) - (45*a^8)/(7*b^{11}*(a + b*x)^7) + (20*a^7)/(b^{11}*(a + b*x)^6) - (42*a^6)/(b^{11}*(a + b*x)^5) + (63*a^5)/(b^{11}*(a + b*x)^4) - (70*a^4)/(b^{11}*(a + b*x)^3) + (60*a^3)/(b^{11}*(a + b*x)^2) - (45*a^2)/(b^{11}*(a + b*x)) - (10*a*\text{Log}[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{x^{10}}{(a+bx)^{10}} dx = \int \left(\frac{1}{b^{10}} + \frac{a^{10}}{b^{10}(a+bx)^{10}} - \frac{10a^9}{b^{10}(a+bx)^9} + \frac{45a^8}{b^{10}(a+bx)^8} - \frac{120a^7}{b^{10}(a+bx)^7} + \frac{210a^6}{b^{10}(a+bx)^6} - \frac{252a^5}{b^{10}(a+bx)^5} + \frac{210a^4}{b^{10}(a+bx)^4} - \frac{120a^3}{b^{10}(a+bx)^3} + \frac{45a^2}{b^{10}(a+bx)^2} - \frac{10a}{b^{10}(a+bx)} \right) dx$$

$$= \frac{x}{b^{10}} - \frac{a^{10}}{9b^{11}(a+bx)^9} + \frac{5a^9}{4b^{11}(a+bx)^8} - \frac{45a^8}{7b^{11}(a+bx)^7} + \frac{20a^7}{b^{11}(a+bx)^6} - \frac{42a^6}{b^{11}(a+bx)^5} + \frac{63a^5}{b^{11}(a+bx)^4} - \frac{70a^4}{b^{11}(a+bx)^3} + \frac{60a^3}{b^{11}(a+bx)^2} - \frac{45a^2}{b^{11}(a+bx)} - \frac{10a \ln(bx+a)}{b^{11}}$$

Mathematica [A] time = 0.03, size = 137, normalized size = 0.86

$$\frac{4861a^{10} + 41229a^9bx + 153576a^8b^2x^2 + 328104a^7b^3x^3 + 439236a^6b^4x^4 + 375732a^5b^5x^5 + 197568a^4b^6x^6 + 54432a^3b^7x^7 + 2268a^2b^8x^8 - 2268ab^9x^9 - 252b^{10}x^{10} + 2520a(a + bx)^9}{252b^{11}(a + bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^10/(a + b*x)^10,x]

[Out]
$$\frac{-1/252*(4861*a^{10} + 41229*a^9*b*x + 153576*a^8*b^2*x^2 + 328104*a^7*b^3*x^3 + 439236*a^6*b^4*x^4 + 375732*a^5*b^5*x^5 + 197568*a^4*b^6*x^6 + 54432*a^3*b^7*x^7 + 2268*a^2*b^8*x^8 - 2268*a*b^9*x^9 - 252*b^{10}*x^{10} + 2520*a*(a + b*x)^9*\text{Log}[a + b*x])}{(b^{11}*(a + b*x)^9)}$$

fricas [B] time = 0.47, size = 314, normalized size = 1.97

$$\frac{252b^{10}x^{10} + 2268ab^9x^9 - 2268a^2b^8x^8 - 54432a^3b^7x^7 - 197568a^4b^6x^6 - 375732a^5b^5x^5 - 439236a^6b^4x^4 - 328104a^7b^3x^3 - 153576a^8b^2x^2 - 41229a^9bx - 4861a^{10} - 2520a(a + bx)^9}{252(b^{20}x^9 + 9ab^{19}x^8 + 36a^2b^{18}x^7 + 84a^3b^{17}x^6 + 126a^4b^{16}x^5 + 126a^5b^{15}x^4 + 84a^6b^{14}x^3 + 36a^7b^{13}x^2 + 9a^8b^{12}x + a^9b^{11})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^10/(b*x+a)^10,x, algorithm="fricas")

[Out]
$$\frac{1/252*(252*b^{10}*x^{10} + 2268*a*b^9*x^9 - 2268*a^2*b^8*x^8 - 54432*a^3*b^7*x^7 - 197568*a^4*b^6*x^6 - 375732*a^5*b^5*x^5 - 439236*a^6*b^4*x^4 - 328104*a^7*b^3*x^3 - 153576*a^8*b^2*x^2 - 41229*a^9*b*x - 4861*a^{10} - 2520*(a*b^9*x^9 + 9*a^2*b^8*x^8 + 36*a^3*b^7*x^7 + 84*a^4*b^6*x^6 + 126*a^5*b^5*x^5 + 126*a^6*b^4*x^4 + 84*a^7*b^3*x^3 + 36*a^8*b^2*x^2 + 9*a^9*b*x + a^{10})*\text{log}(b*x + a))}{(b^{20}*x^9 + 9*a*b^{19}*x^8 + 36*a^2*b^{18}*x^7 + 84*a^3*b^{17}*x^6 + 126*a^4*b^{16}*x^5 + 126*a^5*b^{15}*x^4 + 84*a^6*b^{14}*x^3 + 36*a^7*b^{13}*x^2 + 9*a^8*b^{12}*x + a^9*b^{11})}$$

giac [A] time = 1.29, size = 121, normalized size = 0.76

$$\frac{x}{b^{10}} - \frac{10a \log(|bx + a|)}{b^{11}} - \frac{11340a^2b^8x^8 + 75600a^3b^7x^7 + 229320a^4b^6x^6 + 407484a^5b^5x^5 + 460404a^6b^4x^4 + 37176a^7b^3x^3 + 155844a^8b^2x^2 + 41481a^9bx + 4861a^{10}}{252(bx + a)^9b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^10/(b*x+a)^10,x, algorithm="giac")

[Out]
$$x/b^{10} - 10*a*\text{log}(\text{abs}(b*x + a))/b^{11} - 1/252*(11340*a^2*b^8*x^8 + 75600*a^3*b^7*x^7 + 229320*a^4*b^6*x^6 + 407484*a^5*b^5*x^5 + 460404*a^6*b^4*x^4 + 37176*a^7*b^3*x^3 + 155844*a^8*b^2*x^2 + 41481*a^9*b*x + 4861*a^{10})/((b*x + a)^9*b^{11})$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**10/(b*x+a)**10,x)
```

```
[Out] -10*a*log(a + b*x)/b**11 + (-4861*a**10 - 41481*a**9*b*x - 155844*a**8*b**2
*x**2 - 337176*a**7*b**3*x**3 - 460404*a**6*b**4*x**4 - 407484*a**5*b**5*x*
*5 - 229320*a**4*b**6*x**6 - 75600*a**3*b**7*x**7 - 11340*a**2*b**8*x**8)/(
252*a**9*b**11 + 2268*a**8*b**12*x + 9072*a**7*b**13*x**2 + 21168*a**6*b**1
4*x**3 + 31752*a**5*b**15*x**4 + 31752*a**4*b**16*x**5 + 21168*a**3*b**17*x
**6 + 9072*a**2*b**18*x**7 + 2268*a*b**19*x**8 + 252*b**20*x**9) + x/b**10
```

$$3.225 \quad \int \frac{x^9}{(a+bx)^{10}} dx$$

Optimal. Leaf size=154

$$\frac{a^9}{9b^{10}(a+bx)^9} - \frac{9a^8}{8b^{10}(a+bx)^8} + \frac{36a^7}{7b^{10}(a+bx)^7} - \frac{14a^6}{b^{10}(a+bx)^6} + \frac{126a^5}{5b^{10}(a+bx)^5} - \frac{63a^4}{2b^{10}(a+bx)^4} + \frac{28a^3}{b^{10}(a+bx)^3} - \frac{18a^2}{b^{10}(a+bx)^2} + \frac{9a}{b^{10}(a+bx)} + \frac{\ln(bx+a)}{b^{10}}$$

[Out] $1/9*a^9/b^{10}/(b*x+a)^9 - 9/8*a^8/b^{10}/(b*x+a)^8 + 36/7*a^7/b^{10}/(b*x+a)^7 - 14*a^6/b^{10}/(b*x+a)^6 + 126/5*a^5/b^{10}/(b*x+a)^5 - 63/2*a^4/b^{10}/(b*x+a)^4 + 28*a^3/b^{10}/(b*x+a)^3 - 18*a^2/b^{10}/(b*x+a)^2 + 9*a/b^{10}/(b*x+a) + \ln(b*x+a)/b^{10}$

Rubi [A] time = 0.11, antiderivative size = 154, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^9}{9b^{10}(a+bx)^9} - \frac{9a^8}{8b^{10}(a+bx)^8} + \frac{36a^7}{7b^{10}(a+bx)^7} - \frac{14a^6}{b^{10}(a+bx)^6} + \frac{126a^5}{5b^{10}(a+bx)^5} - \frac{63a^4}{2b^{10}(a+bx)^4} + \frac{28a^3}{b^{10}(a+bx)^3} - \frac{18a^2}{b^{10}(a+bx)^2} + \frac{9a}{b^{10}(a+bx)} + \frac{\ln(bx+a)}{b^{10}}$$

Antiderivative was successfully verified.

[In] Int[x^9/(a + b*x)^10, x]

[Out] $a^9/(9*b^{10}*(a + b*x)^9) - (9*a^8)/(8*b^{10}*(a + b*x)^8) + (36*a^7)/(7*b^{10}*(a + b*x)^7) - (14*a^6)/(b^{10}*(a + b*x)^6) + (126*a^5)/(5*b^{10}*(a + b*x)^5) - (63*a^4)/(2*b^{10}*(a + b*x)^4) + (28*a^3)/(b^{10}*(a + b*x)^3) - (18*a^2)/(b^{10}*(a + b*x)^2) + (9*a)/(b^{10}*(a + b*x)) + \text{Log}[a + b*x]/b^{10}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{x^9}{(a+bx)^{10}} dx = \int \left(-\frac{a^9}{b^9(a+bx)^{10}} + \frac{9a^8}{b^9(a+bx)^9} - \frac{36a^7}{b^9(a+bx)^8} + \frac{84a^6}{b^9(a+bx)^7} - \frac{126a^5}{b^9(a+bx)^6} + \frac{126a^4}{b^9(a+bx)^5} - \frac{63a^3}{b^9(a+bx)^4} + \frac{28a^2}{b^9(a+bx)^3} - \frac{9a}{b^9(a+bx)^2} + \frac{9}{b^9(a+bx)} \right) dx$$

$$= \frac{a^9}{9b^{10}(a+bx)^9} - \frac{9a^8}{8b^{10}(a+bx)^8} + \frac{36a^7}{7b^{10}(a+bx)^7} - \frac{14a^6}{b^{10}(a+bx)^6} + \frac{126a^5}{5b^{10}(a+bx)^5} - \frac{63a^4}{2b^{10}(a+bx)^4} + \frac{28a^3}{b^{10}(a+bx)^3} - \frac{18a^2}{b^{10}(a+bx)^2} + \frac{9a}{b^{10}(a+bx)} + \frac{\ln(bx+a)}{b^{10}}$$

Mathematica [A] time = 0.03, size = 111, normalized size = 0.72

$$\frac{a(7129a^8 + 61641a^7bx + 235224a^6b^2x^2 + 518616a^5b^3x^3 + 725004a^4b^4x^4 + 661500a^3b^5x^5 + 388080a^2b^6x^6 + 136080ab^7x^7 + 22680b^8x^8)}{2520b^{10}(a + bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^9/(a + b*x)^10,x]

[Out] (a*(7129*a^8 + 61641*a^7*b*x + 235224*a^6*b^2*x^2 + 518616*a^5*b^3*x^3 + 725004*a^4*b^4*x^4 + 661500*a^3*b^5*x^5 + 388080*a^2*b^6*x^6 + 136080*a*b^7*x^7 + 22680*b^8*x^8))/(2520*b^10*(a + b*x)^9) + Log[a + b*x]/b^10

fricas [B] time = 0.46, size = 292, normalized size = 1.90

$$\frac{22680ab^8x^8 + 136080a^2b^7x^7 + 388080a^3b^6x^6 + 661500a^4b^5x^5 + 725004a^5b^4x^4 + 518616a^6b^3x^3 + 235224a^7b^2x^2 + 61641a^8bx + 7129a^9}{2520(b^{19}x^9 + 9ab^{18}x^8 + 36a^2b^{17}x^7 + 84a^3b^{16}x^6 + 126a^4b^{15}x^5 + 126a^5b^{14}x^4 + 84a^6b^{13}x^3 + 36a^7b^{12}x^2 + 9a^8b^{11}x + a^9b^{10})} \log(bx + a)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^9/(b*x+a)^10,x, algorithm="fricas")

[Out] 1/2520*(22680*a*b^8*x^8 + 136080*a^2*b^7*x^7 + 388080*a^3*b^6*x^6 + 661500*a^4*b^5*x^5 + 725004*a^5*b^4*x^4 + 518616*a^6*b^3*x^3 + 235224*a^7*b^2*x^2 + 61641*a^8*b*x + 7129*a^9 + 2520*(b^9*x^9 + 9*a*b^8*x^8 + 36*a^2*b^7*x^7 + 84*a^3*b^6*x^6 + 126*a^4*b^5*x^5 + 126*a^5*b^4*x^4 + 84*a^6*b^3*x^3 + 36*a^7*b^2*x^2 + 9*a^8*b*x + a^9)*log(b*x + a))/(b^19*x^9 + 9*a*b^18*x^8 + 36*a^2*b^17*x^7 + 84*a^3*b^16*x^6 + 126*a^4*b^15*x^5 + 126*a^5*b^14*x^4 + 84*a^6*b^13*x^3 + 36*a^7*b^12*x^2 + 9*a^8*b^11*x + a^9*b^10)

giac [A] time = 1.22, size = 112, normalized size = 0.73

$$\frac{\log(|bx + a|)}{b^{10}} + \frac{22680ab^7x^8 + 136080a^2b^6x^7 + 388080a^3b^5x^6 + 661500a^4b^4x^5 + 725004a^5b^3x^4 + 518616a^6b^2x^3 + 61641a^8bx + 7129a^9}{2520(bx + a)^9b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^9/(b*x+a)^10,x, algorithm="giac")

[Out] log(abs(b*x + a))/b^10 + 1/2520*(22680*a*b^7*x^8 + 136080*a^2*b^6*x^7 + 388080*a^3*b^5*x^6 + 661500*a^4*b^4*x^5 + 725004*a^5*b^3*x^4 + 518616*a^6*b^2*x^3 + 235224*a^7*b*x^2 + 61641*a^8*x + 7129*a^9/b)/((b*x + a)^9*b^9)

maple [A] time = 0.01, size = 145, normalized size = 0.94

$$\frac{a^9}{9(bx + a)^9b^{10}} - \frac{9a^8}{8(bx + a)^8b^{10}} + \frac{36a^7}{7(bx + a)^7b^{10}} - \frac{14a^6}{(bx + a)^6b^{10}} + \frac{126a^5}{5(bx + a)^5b^{10}} - \frac{63a^4}{2(bx + a)^4b^{10}} + \frac{28a^3}{(bx + a)^3b^{10}} - \frac{9a^2}{(bx + a)^2b^{10}} + \frac{a}{(bx + a)b^{10}} + \frac{\log(bx + a)}{b^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^9/(b*x+a)^{10}, x)$

[Out] $\frac{1}{9}a^9/b^{10}/(b*x+a)^9 - 9/8a^8/b^{10}/(b*x+a)^8 + 36/7a^7/b^{10}/(b*x+a)^7 - 14a^6/b^{10}/(b*x+a)^6 + 126/5a^5/b^{10}/(b*x+a)^5 - 63/2a^4/b^{10}/(b*x+a)^4 + 28a^3/b^{10}/(b*x+a)^3 - 18a^2/b^{10}/(b*x+a)^2 + 9a/b^{10}/(b*x+a) + \ln(b*x+a)/b^{10}$

maxima [A] time = 1.60, size = 202, normalized size = 1.31

$$\frac{22680 ab^8 x^8 + 136080 a^2 b^7 x^7 + 388080 a^3 b^6 x^6 + 661500 a^4 b^5 x^5 + 725004 a^5 b^4 x^4 + 518616 a^6 b^3 x^3 + 235224 a^7 b^2 x^2 + 61641 a^8 b x + 7129 a^9}{2520 (b^{19} x^9 + 9 ab^{18} x^8 + 36 a^2 b^{17} x^7 + 84 a^3 b^{16} x^6 + 126 a^4 b^{15} x^5 + 126 a^5 b^{14} x^4 + 84 a^6 b^{13} x^3 + 36 a^7 b^{12} x^2 + 9 a^8 b^{11} x + a^9 b^{10})} + \frac{\ln(b*x+a)}{b^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^9/(b*x+a)^{10}, x, \text{algorithm}="maxima")$

[Out] $\frac{1}{2520} * (22680 * a * b^8 * x^8 + 136080 * a^2 * b^7 * x^7 + 388080 * a^3 * b^6 * x^6 + 661500 * a^4 * b^5 * x^5 + 725004 * a^5 * b^4 * x^4 + 518616 * a^6 * b^3 * x^3 + 235224 * a^7 * b^2 * x^2 + 61641 * a^8 * b * x + 7129 * a^9) / (b^{19} * x^9 + 9 * a * b^{18} * x^8 + 36 * a^2 * b^{17} * x^7 + 84 * a^3 * b^{16} * x^6 + 126 * a^4 * b^{15} * x^5 + 126 * a^5 * b^{14} * x^4 + 84 * a^6 * b^{13} * x^3 + 36 * a^7 * b^{12} * x^2 + 9 * a^8 * b^{11} * x + a^9 * b^{10}) + \log(b*x + a) / b^{10}$

mupad [B] time = 0.19, size = 117, normalized size = 0.76

$$\frac{\ln(a + bx) + \frac{9a}{a+bx} - \frac{18a^2}{(a+bx)^2} + \frac{28a^3}{(a+bx)^3} - \frac{63a^4}{2(a+bx)^4} + \frac{126a^5}{5(a+bx)^5} - \frac{14a^6}{(a+bx)^6} + \frac{36a^7}{7(a+bx)^7} - \frac{9a^8}{8(a+bx)^8} + \frac{a^9}{9(a+bx)^9}}{b^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^9/(a + b*x)^{10}, x)$

[Out] $(\log(a + b*x) + (9*a)/(a + b*x) - (18*a^2)/(a + b*x)^2 + (28*a^3)/(a + b*x)^3 - (63*a^4)/(2*(a + b*x)^4) + (126*a^5)/(5*(a + b*x)^5) - (14*a^6)/(a + b*x)^6 + (36*a^7)/(7*(a + b*x)^7) - (9*a^8)/(8*(a + b*x)^8) + a^9/(9*(a + b*x)^9))/b^{10}$

sympy [A] time = 1.11, size = 212, normalized size = 1.38

$$\frac{7129a^9 + 61641a^8bx + 235224a^7b^2x^2 + 518616a^6b^3x^3 + 725004a^5b^4x^4 + 661500a^4b^5x^5 + 388080a^3b^6x^6 + 136080a^2b^7x^7 + 22680ab^8x^8 + 7129a^9}{2520a^9b^{10} + 22680a^8b^{11}x + 90720a^7b^{12}x^2 + 211680a^6b^{13}x^3 + 317520a^5b^{14}x^4 + 317520a^4b^{15}x^5 + 211680a^3b^{16}x^6 + 90720a^2b^{17}x^7 + 136080ab^{18}x^8 + 7129a^9} + \frac{\ln(b*x+a)}{b^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x**9/(b*x+a)**10, x)$

```
[Out] (7129*a**9 + 61641*a**8*b*x + 235224*a**7*b**2*x**2 + 518616*a**6*b**3*x**3
+ 725004*a**5*b**4*x**4 + 661500*a**4*b**5*x**5 + 388080*a**3*b**6*x**6 +
136080*a**2*b**7*x**7 + 22680*a*b**8*x**8)/(2520*a**9*b**10 + 22680*a**8*b*
*11*x + 90720*a**7*b**12*x**2 + 211680*a**6*b**13*x**3 + 317520*a**5*b**14*
x**4 + 317520*a**4*b**15*x**5 + 211680*a**3*b**16*x**6 + 90720*a**2*b**17*x
**7 + 22680*a*b**18*x**8 + 2520*b**19*x**9) + log(a + b*x)/b**10
```

$$3.226 \quad \int \frac{x^8}{(a+bx)^{10}} dx$$

Optimal. Leaf size=17

$$\frac{x^9}{9a(a+bx)^9}$$

[Out] 1/9*x^9/a/(b*x+a)^9

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {37}

$$\frac{x^9}{9a(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Int[x^8/(a + b*x)^10,x]

[Out] x^9/(9*a*(a + b*x)^9)

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{x^8}{(a+bx)^{10}} dx = \frac{x^9}{9a(a+bx)^9}$$

Mathematica [B] time = 0.02, size = 97, normalized size = 5.71

$$\frac{a^8 + 9a^7bx + 36a^6b^2x^2 + 84a^5b^3x^3 + 126a^4b^4x^4 + 126a^3b^5x^5 + 84a^2b^6x^6 + 36ab^7x^7 + 9b^8x^8}{9b^9(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^8/(a + b*x)^10,x]

[Out] $-1/9*(a^8 + 9*a^7*b*x + 36*a^6*b^2*x^2 + 84*a^5*b^3*x^3 + 126*a^4*b^4*x^4 + 126*a^3*b^5*x^5 + 84*a^2*b^6*x^6 + 36*a*b^7*x^7 + 9*b^8*x^8)/(b^9*(a + b*x)^9)$

fricas [B] time = 0.45, size = 186, normalized size = 10.94

$$\frac{9b^8x^8 + 36ab^7x^7 + 84a^2b^6x^6 + 126a^3b^5x^5 + 126a^4b^4x^4 + 84a^5b^3x^3 + 36a^6b^2x^2 + 9a^7bx + a^8}{9(b^{18}x^9 + 9ab^{17}x^8 + 36a^2b^{16}x^7 + 84a^3b^{15}x^6 + 126a^4b^{14}x^5 + 126a^5b^{13}x^4 + 84a^6b^{12}x^3 + 36a^7b^{11}x^2 + 9a^8b^{10})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^8/(b*x+a)^10,x, algorithm="fricas")`

[Out] $-1/9*(9*b^8*x^8 + 36*a*b^7*x^7 + 84*a^2*b^6*x^6 + 126*a^3*b^5*x^5 + 126*a^4*b^4*x^4 + 84*a^5*b^3*x^3 + 36*a^6*b^2*x^2 + 9*a^7*b*x + a^8)/(b^{18}*x^9 + 9*a*b^{17}*x^8 + 36*a^2*b^{16}*x^7 + 84*a^3*b^{15}*x^6 + 126*a^4*b^{14}*x^5 + 126*a^5*b^{13}*x^4 + 84*a^6*b^{12}*x^3 + 36*a^7*b^{11}*x^2 + 9*a^8*b^{10}*x + a^9*b^9)$

giac [B] time = 1.23, size = 95, normalized size = 5.59

$$\frac{9b^8x^8 + 36ab^7x^7 + 84a^2b^6x^6 + 126a^3b^5x^5 + 126a^4b^4x^4 + 84a^5b^3x^3 + 36a^6b^2x^2 + 9a^7bx + a^8}{9(bx + a)^9b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^8/(b*x+a)^10,x, algorithm="giac")`

[Out] $-1/9*(9*b^8*x^8 + 36*a*b^7*x^7 + 84*a^2*b^6*x^6 + 126*a^3*b^5*x^5 + 126*a^4*b^4*x^4 + 84*a^5*b^3*x^3 + 36*a^6*b^2*x^2 + 9*a^7*b*x + a^8)/((b*x + a)^9*b^9)$

maple [B] time = 0.01, size = 131, normalized size = 7.71

$$-\frac{a^8}{9(bx + a)^9b^9} + \frac{a^7}{(bx + a)^8b^9} - \frac{4a^6}{(bx + a)^7b^9} + \frac{28a^5}{3(bx + a)^6b^9} - \frac{14a^4}{(bx + a)^5b^9} + \frac{14a^3}{(bx + a)^4b^9} - \frac{28a^2}{3(bx + a)^3b^9} + \frac{4a}{(bx + a)^2b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^8/(b*x+a)^10,x)`

[Out] $28/3*a^5/b^9/(b*x+a)^6+4*a/b^9/(b*x+a)^2-14*a^4/b^9/(b*x+a)^5+a^7/b^9/(b*x+a)^8-28/3*a^2/b^9/(b*x+a)^3+14*a^3/b^9/(b*x+a)^4-1/9*a^8/b^9/(b*x+a)^9-4*a^6/b^9/(b*x+a)^7-1/b^9/(b*x+a)$

maxima [B] time = 1.51, size = 186, normalized size = 10.94

$$\frac{9b^8x^8 + 36ab^7x^7 + 84a^2b^6x^6 + 126a^3b^5x^5 + 126a^4b^4x^4 + 84a^5b^3x^3 + 36a^6b^2x^2 + 9a^7bx + a^8}{9(b^{18}x^9 + 9ab^{17}x^8 + 36a^2b^{16}x^7 + 84a^3b^{15}x^6 + 126a^4b^{14}x^5 + 126a^5b^{13}x^4 + 84a^6b^{12}x^3 + 36a^7b^{11}x^2 + 9a^8b^{10})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8/(b*x+a)^10,x, algorithm="maxima")

[Out]
$$-1/9*(9*b^8*x^8 + 36*a*b^7*x^7 + 84*a^2*b^6*x^6 + 126*a^3*b^5*x^5 + 126*a^4*b^4*x^4 + 84*a^5*b^3*x^3 + 36*a^6*b^2*x^2 + 9*a^7*b*x + a^8)/(b^18*x^9 + 9*a*b^17*x^8 + 36*a^2*b^16*x^7 + 84*a^3*b^15*x^6 + 126*a^4*b^14*x^5 + 126*a^5*b^13*x^4 + 84*a^6*b^12*x^3 + 36*a^7*b^11*x^2 + 9*a^8*b^10*x + a^9*b^9)$$

mupad [B] time = 0.14, size = 107, normalized size = 6.29

$$\frac{\frac{1}{a+bx} - \frac{4a}{(a+bx)^2} + \frac{28a^2}{3(a+bx)^3} - \frac{14a^3}{(a+bx)^4} + \frac{14a^4}{(a+bx)^5} - \frac{28a^5}{3(a+bx)^6} + \frac{4a^6}{(a+bx)^7} - \frac{a^7}{(a+bx)^8} + \frac{a^8}{9(a+bx)^9}}{b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^8/(a + b*x)^10,x)

[Out]
$$-(1/(a + b*x) - (4*a)/(a + b*x)^2 + (28*a^2)/(3*(a + b*x)^3) - (14*a^3)/(a + b*x)^4 + (14*a^4)/(a + b*x)^5 - (28*a^5)/(3*(a + b*x)^6) + (4*a^6)/(a + b*x)^7 - a^7/(a + b*x)^8 + a^8/(9*(a + b*x)^9))/b^9$$

sympy [B] time = 0.98, size = 199, normalized size = 11.71

$$\frac{-a^8 - 9a^7bx - 36a^6b^2x^2 - 84a^5b^3x^3 - 126a^4b^4x^4 - 126a^3b^5x^5 - 84a^2b^6x^6 - 36ab^7x^7 - 9b^8x^8}{9a^9b^9 + 81a^8b^{10}x + 324a^7b^{11}x^2 + 756a^6b^{12}x^3 + 1134a^5b^{13}x^4 + 1134a^4b^{14}x^5 + 756a^3b^{15}x^6 + 324a^2b^{16}x^7 + 81ab^{17}x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**8/(b*x+a)**10,x)

[Out]
$$(-a^{**8} - 9*a^{**7}*b*x - 36*a^{**6}*b^{**2}*x^{**2} - 84*a^{**5}*b^{**3}*x^{**3} - 126*a^{**4}*b^{**4}*x^{**4} - 126*a^{**3}*b^{**5}*x^{**5} - 84*a^{**2}*b^{**6}*x^{**6} - 36*a*b^{**7}*x^{**7} - 9*b^{**8}*x^{**8})/(9*a^{**9}*b^{**9} + 81*a^{**8}*b^{**10}*x + 324*a^{**7}*b^{**11}*x^{**2} + 756*a^{**6}*b^{**12}*x^{**3} + 1134*a^{**5}*b^{**13}*x^{**4} + 1134*a^{**4}*b^{**14}*x^{**5} + 756*a^{**3}*b^{**15}*x^{**6} + 324*a^{**2}*b^{**16}*x^{**7} + 81*a*b^{**17}*x^{**8} + 9*b^{**18}*x^{**9})$$

$$3.227 \quad \int \frac{x^7}{(a+bx)^{10}} dx$$

Optimal. Leaf size=35

$$\frac{x^8}{72a^2(a+bx)^8} + \frac{x^8}{9a(a+bx)^9}$$

[Out] 1/9*x^8/a/(b*x+a)^9+1/72*x^8/a^2/(b*x+a)^8

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{x^8}{72a^2(a+bx)^8} + \frac{x^8}{9a(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Int[x^7/(a + b*x)^10,x]

[Out] x^8/(9*a*(a + b*x)^9) + x^8/(72*a^2*(a + b*x)^8)

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
  implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{x^7}{(a+bx)^{10}} dx = \frac{x^8}{9a(a+bx)^9} + \frac{\int \frac{x^7}{(a+bx)^9} dx}{9a}$$

$$= \frac{x^8}{9a(a+bx)^9} + \frac{x^8}{72a^2(a+bx)^8}$$

Mathematica [B] time = 0.01, size = 86, normalized size = 2.46

$$\frac{a^7 + 9a^6bx + 36a^5b^2x^2 + 84a^4b^3x^3 + 126a^3b^4x^4 + 126a^2b^5x^5 + 84ab^6x^6 + 36b^7x^7}{72b^8(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^7/(a + b*x)^10,x]

[Out] -1/72*(a^7 + 9*a^6*b*x + 36*a^5*b^2*x^2 + 84*a^4*b^3*x^3 + 126*a^3*b^4*x^4 + 126*a^2*b^5*x^5 + 84*a*b^6*x^6 + 36*b^7*x^7)/(b^8*(a + b*x)^9)

fricas [B] time = 0.47, size = 175, normalized size = 5.00

$$\frac{36b^7x^7 + 84ab^6x^6 + 126a^2b^5x^5 + 126a^3b^4x^4 + 84a^4b^3x^3 + 36a^5b^2x^2 + 9a^6bx + a^7}{72(b^{17}x^9 + 9ab^{16}x^8 + 36a^2b^{15}x^7 + 84a^3b^{14}x^6 + 126a^4b^{13}x^5 + 126a^5b^{12}x^4 + 84a^6b^{11}x^3 + 36a^7b^{10}x^2 + 9a^8b^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^10,x, algorithm="fricas")

[Out] -1/72*(36*b^7*x^7 + 84*a*b^6*x^6 + 126*a^2*b^5*x^5 + 126*a^3*b^4*x^4 + 84*a^4*b^3*x^3 + 36*a^5*b^2*x^2 + 9*a^6*b*x + a^7)/(b^17*x^9 + 9*a*b^16*x^8 + 36*a^2*b^15*x^7 + 84*a^3*b^14*x^6 + 126*a^4*b^13*x^5 + 126*a^5*b^12*x^4 + 84*a^6*b^11*x^3 + 36*a^7*b^10*x^2 + 9*a^8*b^9*x + a^9*b^8)

giac [B] time = 0.96, size = 84, normalized size = 2.40

$$\frac{36b^7x^7 + 84ab^6x^6 + 126a^2b^5x^5 + 126a^3b^4x^4 + 84a^4b^3x^3 + 36a^5b^2x^2 + 9a^6bx + a^7}{72(bx+a)^9b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^10,x, algorithm="giac")

[Out] -1/72*(36*b^7*x^7 + 84*a*b^6*x^6 + 126*a^2*b^5*x^5 + 126*a^3*b^4*x^4 + 84*a^4*b^3*x^3 + 36*a^5*b^2*x^2 + 9*a^6*b*x + a^7)/((b*x + a)^9*b^8)

maple [B] time = 0.01, size = 117, normalized size = 3.34

$$\frac{a^7}{9(bx+a)^9 b^8} - \frac{7a^6}{8(bx+a)^8 b^8} + \frac{3a^5}{(bx+a)^7 b^8} - \frac{35a^4}{6(bx+a)^6 b^8} + \frac{7a^3}{(bx+a)^5 b^8} - \frac{21a^2}{4(bx+a)^4 b^8} + \frac{7a}{3(bx+a)^3 b^8} - \frac{1}{2(bx+a)^2 b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7/(b*x+a)^10,x)

[Out] $-35/6*a^4/b^8/(b*x+a)^6 - 1/2/b^8/(b*x+a)^2 + 3*a^5/b^8/(b*x+a)^7 + 7*a^3/b^8/(b*x+a)^5 - 21/4*a^2/b^8/(b*x+a)^4 - 7/8*a^6/b^8/(b*x+a)^8 + 7/3*a/b^8/(b*x+a)^3 + 1/9*a^7/b^8/(b*x+a)^9$

maxima [B] time = 1.59, size = 175, normalized size = 5.00

$$\frac{36b^7x^7 + 84ab^6x^6 + 126a^2b^5x^5 + 126a^3b^4x^4 + 84a^4b^3x^3 + 36a^5b^2x^2 + 9a^6bx + a^7}{72(b^{17}x^9 + 9ab^{16}x^8 + 36a^2b^{15}x^7 + 84a^3b^{14}x^6 + 126a^4b^{13}x^5 + 126a^5b^{12}x^4 + 84a^6b^{11}x^3 + 36a^7b^{10}x^2 + 9a^8b^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7/(b*x+a)^10,x, algorithm="maxima")

[Out] $-1/72*(36*b^7*x^7 + 84*a*b^6*x^6 + 126*a^2*b^5*x^5 + 126*a^3*b^4*x^4 + 84*a^4*b^3*x^3 + 36*a^5*b^2*x^2 + 9*a^6*b*x + a^7)/(b^{17}*x^9 + 9*a*b^{16}*x^8 + 36*a^2*b^{15}*x^7 + 84*a^3*b^{14}*x^6 + 126*a^4*b^{13}*x^5 + 126*a^5*b^{12}*x^4 + 84*a^6*b^{11}*x^3 + 36*a^7*b^{10}*x^2 + 9*a^8*b^9*x + a^9*b^8)$

mupad [B] time = 0.13, size = 22, normalized size = 0.63

$$\frac{x^8 (9a + bx)}{72a^2 (a + bx)^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7/(a + b*x)^10,x)

[Out] $(x^8*(9*a + b*x))/(72*a^2*(a + b*x)^9)$

sympy [B] time = 1.00, size = 187, normalized size = 5.34

$$\frac{-a^7 - 9a^6bx - 36a^5b^2x^2 - 84a^4b^3x^3 - 126a^3b^4x^4 - 126a^2b^5x^5 - 84ab^6x^6 - 36b^7x^7}{72a^9b^8 + 648a^8b^9x + 2592a^7b^{10}x^2 + 6048a^6b^{11}x^3 + 9072a^5b^{12}x^4 + 9072a^4b^{13}x^5 + 6048a^3b^{14}x^6 + 2592a^2b^{15}x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**7/(b*x+a)**10,x)

```
[Out] (-a**7 - 9*a**6*b*x - 36*a**5*b**2*x**2 - 84*a**4*b**3*x**3 - 126*a**3*b**4*x**4 - 126*a**2*b**5*x**5 - 84*a*b**6*x**6 - 36*b**7*x**7)/(72*a**9*b**8 + 648*a**8*b**9*x + 2592*a**7*b**10*x**2 + 6048*a**6*b**11*x**3 + 9072*a**5*b**12*x**4 + 9072*a**4*b**13*x**5 + 6048*a**3*b**14*x**6 + 2592*a**2*b**15*x**7 + 648*a*b**16*x**8 + 72*b**17*x**9)
```

$$3.228 \quad \int \frac{x^6}{(a+bx)^{10}} dx$$

Optimal. Leaf size=52

$$\frac{x^7}{252a^3(a+bx)^7} + \frac{x^7}{36a^2(a+bx)^8} + \frac{x^7}{9a(a+bx)^9}$$

[Out] $1/9*x^7/a/(b*x+a)^9+1/36*x^7/a^2/(b*x+a)^8+1/252*x^7/a^3/(b*x+a)^7$

Rubi [A] time = 0.01, antiderivative size = 52, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{x^7}{252a^3(a+bx)^7} + \frac{x^7}{36a^2(a+bx)^8} + \frac{x^7}{9a(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Int[x^6/(a + b*x)^10,x]

[Out] $x^7/(9*a*(a + b*x)^9) + x^7/(36*a^2*(a + b*x)^8) + x^7/(252*a^3*(a + b*x)^7)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{x^6}{(a+bx)^{10}} dx &= \frac{x^7}{9a(a+bx)^9} + \frac{2 \int \frac{x^6}{(a+bx)^9} dx}{9a} \\
&= \frac{x^7}{9a(a+bx)^9} + \frac{x^7}{36a^2(a+bx)^8} + \frac{\int \frac{x^6}{(a+bx)^8} dx}{36a^2} \\
&= \frac{x^7}{9a(a+bx)^9} + \frac{x^7}{36a^2(a+bx)^8} + \frac{x^7}{252a^3(a+bx)^7}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 75, normalized size = 1.44

$$\frac{a^6 + 9a^5bx + 36a^4b^2x^2 + 84a^3b^3x^3 + 126a^2b^4x^4 + 126ab^5x^5 + 84b^6x^6}{252b^7(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^6/(a + b*x)^10,x]

[Out] -1/252*(a^6 + 9*a^5*b*x + 36*a^4*b^2*x^2 + 84*a^3*b^3*x^3 + 126*a^2*b^4*x^4 + 126*a*b^5*x^5 + 84*b^6*x^6)/(b^7*(a + b*x)^9)

fricas [B] time = 0.46, size = 164, normalized size = 3.15

$$\frac{84b^6x^6 + 126ab^5x^5 + 126a^2b^4x^4 + 84a^3b^3x^3 + 36a^4b^2x^2 + 9a^5bx + a^6}{252(b^{16}x^9 + 9ab^{15}x^8 + 36a^2b^{14}x^7 + 84a^3b^{13}x^6 + 126a^4b^{12}x^5 + 126a^5b^{11}x^4 + 84a^6b^{10}x^3 + 36a^7b^9x^2 + 9a^8b^8)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^10,x, algorithm="fricas")

[Out] -1/252*(84*b^6*x^6 + 126*a*b^5*x^5 + 126*a^2*b^4*x^4 + 84*a^3*b^3*x^3 + 36*a^4*b^2*x^2 + 9*a^5*b*x + a^6)/(b^16*x^9 + 9*a*b^15*x^8 + 36*a^2*b^14*x^7 + 84*a^3*b^13*x^6 + 126*a^4*b^12*x^5 + 126*a^5*b^11*x^4 + 84*a^6*b^10*x^3 + 36*a^7*b^9*x^2 + 9*a^8*b^8*x + a^9*b^7)

giac [A] time = 1.01, size = 73, normalized size = 1.40

$$\frac{84b^6x^6 + 126ab^5x^5 + 126a^2b^4x^4 + 84a^3b^3x^3 + 36a^4b^2x^2 + 9a^5bx + a^6}{252(bx+a)^9b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(b*x+a)^10,x, algorithm="giac")

[Out] $-1/252*(84*b^6*x^6 + 126*a*b^5*x^5 + 126*a^2*b^4*x^4 + 84*a^3*b^3*x^3 + 36*a^4*b^2*x^2 + 9*a^5*b*x + a^6)/((b*x + a)^9*b^7)$

maple [B] time = 0.01, size = 102, normalized size = 1.96

$$\frac{a^6}{9(bx+a)^9 b^7} + \frac{3a^5}{4(bx+a)^8 b^7} - \frac{15a^4}{7(bx+a)^7 b^7} + \frac{10a^3}{3(bx+a)^6 b^7} - \frac{3a^2}{(bx+a)^5 b^7} + \frac{3a}{2(bx+a)^4 b^7} - \frac{1}{3(bx+a)^3 b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^6/(b*x+a)^{10}, x)$

[Out] $10/3*a^3/b^7/(b*x+a)^6 - 3*a^2/b^7/(b*x+a)^5 + 3/4*a^5/b^7/(b*x+a)^8 + 3/2*a/b^7/(b*x+a)^4 - 1/3/b^7/(b*x+a)^3 - 1/9*a^6/b^7/(b*x+a)^9 - 15/7*a^4/b^7/(b*x+a)^7$

maxima [B] time = 1.49, size = 164, normalized size = 3.15

$$\frac{84 b^6 x^6 + 126 a b^5 x^5 + 126 a^2 b^4 x^4 + 84 a^3 b^3 x^3 + 36 a^4 b^2 x^2 + 9 a^5 b x + a^6}{252 (b^{16} x^9 + 9 a b^{15} x^8 + 36 a^2 b^{14} x^7 + 84 a^3 b^{13} x^6 + 126 a^4 b^{12} x^5 + 126 a^5 b^{11} x^4 + 84 a^6 b^{10} x^3 + 36 a^7 b^9 x^2 + 9 a^8 b x + a^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^6/(b*x+a)^{10}, x, \text{algorithm}="maxima")$

[Out] $-1/252*(84*b^6*x^6 + 126*a*b^5*x^5 + 126*a^2*b^4*x^4 + 84*a^3*b^3*x^3 + 36*a^4*b^2*x^2 + 9*a^5*b*x + a^6)/(b^{16}*x^9 + 9*a*b^{15}*x^8 + 36*a^2*b^{14}*x^7 + 84*a^3*b^{13}*x^6 + 126*a^4*b^{12}*x^5 + 126*a^5*b^{11}*x^4 + 84*a^6*b^{10}*x^3 + 36*a^7*b^9*x^2 + 9*a^8*b^8*x + a^9*b^7)$

mupad [B] time = 0.14, size = 85, normalized size = 1.63

$$\frac{\frac{1}{3(a+bx)^3} - \frac{3a}{2(a+bx)^4} + \frac{3a^2}{(a+bx)^5} - \frac{10a^3}{3(a+bx)^6} + \frac{15a^4}{7(a+bx)^7} - \frac{3a^5}{4(a+bx)^8} + \frac{a^6}{9(a+bx)^9}}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^6/(a + b*x)^{10}, x)$

[Out] $-(1/(3*(a + b*x)^3) - (3*a)/(2*(a + b*x)^4) + (3*a^2)/(a + b*x)^5 - (10*a^3)/(3*(a + b*x)^6) + (15*a^4)/(7*(a + b*x)^7) - (3*a^5)/(4*(a + b*x)^8) + a^6/(9*(a + b*x)^9))/b^7$

sympy [B] time = 0.91, size = 175, normalized size = 3.37

$$\frac{-a^6 - 9a^5bx - 36a^4b^2x^2 - 84a^3b^3x^3 - 126a^2b^4x^4 - 126ab^5x^5 - 84b^6x^6}{252a^9b^7 + 2268a^8b^8x + 9072a^7b^9x^2 + 21168a^6b^{10}x^3 + 31752a^5b^{11}x^4 + 31752a^4b^{12}x^5 + 21168a^3b^{13}x^6 + 9072a^2b^{14}x^7 + 252a^2b^{15}x^8 + 84a^2b^{16}x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**6/(b*x+a)**10,x)`

[Out]
$$\frac{-a^6 - 9a^5bx - 36a^4b^2x^2 - 84a^3b^3x^3 - 126a^2b^4x^4 - 126ab^5x^5 - 84b^6x^6}{(252a^9b^7 + 2268a^8b^8x + 9072a^7b^9x^2 + 21168a^6b^{10}x^3 + 31752a^5b^{11}x^4 + 31752a^4b^{12}x^5 + 21168a^3b^{13}x^6 + 9072a^2b^{14}x^7 + 2268ab^{15}x^8 + 252b^{16}x^9)}$$

$$3.229 \quad \int \frac{x^5}{(a+bx)^{10}} dx$$

Optimal. Leaf size=69

$$\frac{x^6}{504a^4(a+bx)^6} + \frac{x^6}{84a^3(a+bx)^7} + \frac{x^6}{24a^2(a+bx)^8} + \frac{x^6}{9a(a+bx)^9}$$

[Out] $1/9*x^6/a/(b*x+a)^9+1/24*x^6/a^2/(b*x+a)^8+1/84*x^6/a^3/(b*x+a)^7+1/504*x^6/a^4/(b*x+a)^6$

Rubi [A] time = 0.02, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{x^6}{504a^4(a+bx)^6} + \frac{x^6}{84a^3(a+bx)^7} + \frac{x^6}{24a^2(a+bx)^8} + \frac{x^6}{9a(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Int[x^5/(a + b*x)^10, x]

[Out] $x^6/(9*a*(a + b*x)^9) + x^6/(24*a^2*(a + b*x)^8) + x^6/(84*a^3*(a + b*x)^7) + x^6/(504*a^4*(a + b*x)^6)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[m] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{x^5}{(a+bx)^{10}} dx &= \frac{x^6}{9a(a+bx)^9} + \frac{\int \frac{x^5}{(a+bx)^9} dx}{3a} \\
&= \frac{x^6}{9a(a+bx)^9} + \frac{x^6}{24a^2(a+bx)^8} + \frac{\int \frac{x^5}{(a+bx)^8} dx}{12a^2} \\
&= \frac{x^6}{9a(a+bx)^9} + \frac{x^6}{24a^2(a+bx)^8} + \frac{x^6}{84a^3(a+bx)^7} + \frac{\int \frac{x^5}{(a+bx)^7} dx}{84a^3} \\
&= \frac{x^6}{9a(a+bx)^9} + \frac{x^6}{24a^2(a+bx)^8} + \frac{x^6}{84a^3(a+bx)^7} + \frac{x^6}{504a^4(a+bx)^6}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 64, normalized size = 0.93

$$\frac{a^5 + 9a^4bx + 36a^3b^2x^2 + 84a^2b^3x^3 + 126ab^4x^4 + 126b^5x^5}{504b^6(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/(a + b*x)^10,x]

[Out] -1/504*(a^5 + 9*a^4*b*x + 36*a^3*b^2*x^2 + 84*a^2*b^3*x^3 + 126*a*b^4*x^4 + 126*b^5*x^5)/(b^6*(a + b*x)^9)

fricas [B] time = 0.44, size = 153, normalized size = 2.22

$$\frac{126b^5x^5 + 126ab^4x^4 + 84a^2b^3x^3 + 36a^3b^2x^2 + 9a^4bx + a^5}{504(b^{15}x^9 + 9ab^{14}x^8 + 36a^2b^{13}x^7 + 84a^3b^{12}x^6 + 126a^4b^{11}x^5 + 126a^5b^{10}x^4 + 84a^6b^9x^3 + 36a^7b^8x^2 + 9a^8b^7x + a^9b^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^10,x, algorithm="fricas")

[Out] -1/504*(126*b^5*x^5 + 126*a*b^4*x^4 + 84*a^2*b^3*x^3 + 36*a^3*b^2*x^2 + 9*a^4*b*x + a^5)/(b^15*x^9 + 9*a*b^14*x^8 + 36*a^2*b^13*x^7 + 84*a^3*b^12*x^6 + 126*a^4*b^11*x^5 + 126*a^5*b^10*x^4 + 84*a^6*b^9*x^3 + 36*a^7*b^8*x^2 + 9*a^8*b^7*x + a^9*b^6)

giac [A] time = 0.90, size = 62, normalized size = 0.90

$$\frac{126b^5x^5 + 126ab^4x^4 + 84a^2b^3x^3 + 36a^3b^2x^2 + 9a^4bx + a^5}{504(bx+a)^9b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^10,x, algorithm="giac")

[Out] $-1/504*(126*b^5*x^5 + 126*a*b^4*x^4 + 84*a^2*b^3*x^3 + 36*a^3*b^2*x^2 + 9*a^4*b*x + a^5)/((b*x + a)^9*b^6)$

maple [A] time = 0.00, size = 86, normalized size = 1.25

$$\frac{a^5}{9(bx+a)^9 b^6} - \frac{5a^4}{8(bx+a)^8 b^6} + \frac{10a^3}{7(bx+a)^7 b^6} - \frac{5a^2}{3(bx+a)^6 b^6} + \frac{a}{(bx+a)^5 b^6} - \frac{1}{4(bx+a)^4 b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(b*x+a)^10,x)

[Out] $-5/3*a^2/b^6/(b*x+a)^6 - 1/4/b^6/(b*x+a)^4 + a/b^6/(b*x+a)^5 - 5/8*a^4/b^6/(b*x+a)^8 + 10/7*a^3/b^6/(b*x+a)^7 + 1/9*a^5/b^6/(b*x+a)^9$

maxima [B] time = 1.54, size = 153, normalized size = 2.22

$$\frac{126 b^5 x^5 + 126 a b^4 x^4 + 84 a^2 b^3 x^3 + 36 a^3 b^2 x^2 + 9 a^4 b x + a^5}{504 (b^{15} x^9 + 9 a b^{14} x^8 + 36 a^2 b^{13} x^7 + 84 a^3 b^{12} x^6 + 126 a^4 b^{11} x^5 + 126 a^5 b^{10} x^4 + 84 a^6 b^9 x^3 + 36 a^7 b^8 x^2 + 9 a^8 b^7 x + a^9 b^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^10,x, algorithm="maxima")

[Out] $-1/504*(126*b^5*x^5 + 126*a*b^4*x^4 + 84*a^2*b^3*x^3 + 36*a^3*b^2*x^2 + 9*a^4*b*x + a^5)/(b^{15}*x^9 + 9*a*b^{14}*x^8 + 36*a^2*b^{13}*x^7 + 84*a^3*b^{12}*x^6 + 126*a^4*b^{11}*x^5 + 126*a^5*b^{10}*x^4 + 84*a^6*b^9*x^3 + 36*a^7*b^8*x^2 + 9*a^8*b^7*x + a^9*b^6)$

mupad [B] time = 0.08, size = 71, normalized size = 1.03

$$\frac{\frac{a}{(a+bx)^5} - \frac{1}{4(a+bx)^4} - \frac{5a^2}{3(a+bx)^6} + \frac{10a^3}{7(a+bx)^7} - \frac{5a^4}{8(a+bx)^8} + \frac{a^5}{9(a+bx)^9}}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(a + b*x)^10,x)

[Out] $(a/(a + b*x)^5 - 1/(4*(a + b*x)^4) - (5*a^2)/(3*(a + b*x)^6) + (10*a^3)/(7*(a + b*x)^7) - (5*a^4)/(8*(a + b*x)^8) + a^5/(9*(a + b*x)^9))/b^6$

sympy [B] time = 0.84, size = 163, normalized size = 2.36

$$\frac{-a^5 - 9a^4bx - 36a^3b^2x^2 - 84a^2b^3x^3 - 126ab^4x^4 - 126b^5x^5}{504a^9b^6 + 4536a^8b^7x + 18144a^7b^8x^2 + 42336a^6b^9x^3 + 63504a^5b^{10}x^4 + 63504a^4b^{11}x^5 + 42336a^3b^{12}x^6 + 18144a^2b^{13}x^7 + 4536a^1b^{14}x^8 + 504a^0b^{15}x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5/(b*x+a)**10,x)
```

```
[Out] (-a**5 - 9*a**4*b*x - 36*a**3*b**2*x**2 - 84*a**2*b**3*x**3 - 126*a*b**4*x**4 - 126*b**5*x**5)/(504*a**9*b**6 + 4536*a**8*b**7*x + 18144*a**7*b**8*x**2 + 42336*a**6*b**9*x**3 + 63504*a**5*b**10*x**4 + 63504*a**4*b**11*x**5 + 42336*a**3*b**12*x**6 + 18144*a**2*b**13*x**7 + 4536*a*b**14*x**8 + 504*b**15*x**9)
```

$$3.230 \quad \int \frac{x^4}{(a+bx)^{10}} dx$$

Optimal. Leaf size=81

$$-\frac{a^4}{9b^5(a+bx)^9} + \frac{a^3}{2b^5(a+bx)^8} - \frac{6a^2}{7b^5(a+bx)^7} + \frac{2a}{3b^5(a+bx)^6} - \frac{1}{5b^5(a+bx)^5}$$

[Out] $-1/9*a^4/b^5/(b*x+a)^9+1/2*a^3/b^5/(b*x+a)^8-6/7*a^2/b^5/(b*x+a)^7+2/3*a/b^5/(b*x+a)^6-1/5/b^5/(b*x+a)^5$

Rubi [A] time = 0.04, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^4}{9b^5(a+bx)^9} + \frac{a^3}{2b^5(a+bx)^8} - \frac{6a^2}{7b^5(a+bx)^7} + \frac{2a}{3b^5(a+bx)^6} - \frac{1}{5b^5(a+bx)^5}$$

Antiderivative was successfully verified.

[In] Int[x^4/(a + b*x)^10, x]

[Out] $-a^4/(9*b^5*(a + b*x)^9) + a^3/(2*b^5*(a + b*x)^8) - (6*a^2)/(7*b^5*(a + b*x)^7) + (2*a)/(3*b^5*(a + b*x)^6) - 1/(5*b^5*(a + b*x)^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{(a+bx)^{10}} dx &= \int \left(\frac{a^4}{b^4(a+bx)^{10}} - \frac{4a^3}{b^4(a+bx)^9} + \frac{6a^2}{b^4(a+bx)^8} - \frac{4a}{b^4(a+bx)^7} + \frac{1}{b^4(a+bx)^6} \right) dx \\ &= -\frac{a^4}{9b^5(a+bx)^9} + \frac{a^3}{2b^5(a+bx)^8} - \frac{6a^2}{7b^5(a+bx)^7} + \frac{2a}{3b^5(a+bx)^6} - \frac{1}{5b^5(a+bx)^5} \end{aligned}$$

Mathematica [A] time = 0.01, size = 53, normalized size = 0.65

$$-\frac{a^4 + 9a^3bx + 36a^2b^2x^2 + 84ab^3x^3 + 126b^4x^4}{630b^5(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/(a + b*x)^10,x]

[Out] $-1/630*(a^4 + 9*a^3*b*x + 36*a^2*b^2*x^2 + 84*a*b^3*x^3 + 126*b^4*x^4)/(b^5*(a + b*x)^9)$

fricas [A] time = 0.44, size = 142, normalized size = 1.75

$$\frac{126 b^4 x^4 + 84 a b^3 x^3 + 36 a^2 b^2 x^2 + 9 a^3 b x + a^4}{630 (b^{14} x^9 + 9 a b^{13} x^8 + 36 a^2 b^{12} x^7 + 84 a^3 b^{11} x^6 + 126 a^4 b^{10} x^5 + 126 a^5 b^9 x^4 + 84 a^6 b^8 x^3 + 36 a^7 b^7 x^2 + 9 a^8 b^6 x + a^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^10,x, algorithm="fricas")

[Out] $-1/630*(126*b^4*x^4 + 84*a*b^3*x^3 + 36*a^2*b^2*x^2 + 9*a^3*b*x + a^4)/(b^14*x^9 + 9*a*b^13*x^8 + 36*a^2*b^12*x^7 + 84*a^3*b^11*x^6 + 126*a^4*b^10*x^5 + 126*a^5*b^9*x^4 + 84*a^6*b^8*x^3 + 36*a^7*b^7*x^2 + 9*a^8*b^6*x + a^9*b^5)$

giac [A] time = 1.22, size = 51, normalized size = 0.63

$$\frac{126 b^4 x^4 + 84 a b^3 x^3 + 36 a^2 b^2 x^2 + 9 a^3 b x + a^4}{630 (b x + a)^9 b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^10,x, algorithm="giac")

[Out] $-1/630*(126*b^4*x^4 + 84*a*b^3*x^3 + 36*a^2*b^2*x^2 + 9*a^3*b*x + a^4)/((b*x + a)^9*b^5)$

maple [A] time = 0.01, size = 72, normalized size = 0.89

$$-\frac{a^4}{9 (b x + a)^9 b^5} + \frac{a^3}{2 (b x + a)^8 b^5} - \frac{6 a^2}{7 (b x + a)^7 b^5} + \frac{2 a}{3 (b x + a)^6 b^5} - \frac{1}{5 (b x + a)^5 b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(b*x+a)^10,x)

[Out] $-1/9*a^4/b^5/(b*x+a)^9+1/2*a^3/b^5/(b*x+a)^8-6/7*a^2/b^5/(b*x+a)^7+2/3*a/b^5/(b*x+a)^6-1/5/b^5/(b*x+a)^5$

maxima [A] time = 1.46, size = 142, normalized size = 1.75

$$\frac{126 b^4 x^4 + 84 a b^3 x^3 + 36 a^2 b^2 x^2 + 9 a^3 b x + a^4}{630 (b^{14} x^9 + 9 a b^{13} x^8 + 36 a^2 b^{12} x^7 + 84 a^3 b^{11} x^6 + 126 a^4 b^{10} x^5 + 126 a^5 b^9 x^4 + 84 a^6 b^8 x^3 + 36 a^7 b^7 x^2 + 9 a^8 b^6 x + a^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^10,x, algorithm="maxima")

[Out]
$$-1/630*(126*b^4*x^4 + 84*a*b^3*x^3 + 36*a^2*b^2*x^2 + 9*a^3*b*x + a^4)/(b^14*x^9 + 9*a*b^13*x^8 + 36*a^2*b^12*x^7 + 84*a^3*b^11*x^6 + 126*a^4*b^10*x^5 + 126*a^5*b^9*x^4 + 84*a^6*b^8*x^3 + 36*a^7*b^7*x^2 + 9*a^8*b^6*x + a^9*b^5)$$

mupad [B] time = 0.08, size = 61, normalized size = 0.75

$$\frac{\frac{1}{5(a+bx)^5} - \frac{2a}{3(a+bx)^6} + \frac{6a^2}{7(a+bx)^7} - \frac{a^3}{2(a+bx)^8} + \frac{a^4}{9(a+bx)^9}}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(a + b*x)^10,x)

[Out]
$$-(1/(5*(a + b*x)^5) - (2*a)/(3*(a + b*x)^6) + (6*a^2)/(7*(a + b*x)^7) - a^3/(2*(a + b*x)^8) + a^4/(9*(a + b*x)^9))/b^5$$

sympy [B] time = 0.79, size = 151, normalized size = 1.86

$$\frac{-a^4 - 9a^3bx - 36a^2b^2x^2 - 84ab^3x^3 - 126b^4x^4}{630a^9b^5 + 5670a^8b^6x + 22680a^7b^7x^2 + 52920a^6b^8x^3 + 79380a^5b^9x^4 + 79380a^4b^{10}x^5 + 52920a^3b^{11}x^6 + 22680a^2b^{12}x^7 + 5670ab^{13}x^8 + 630b^{14}x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/(b*x+a)**10,x)

[Out]
$$(-a**4 - 9*a**3*b*x - 36*a**2*b**2*x**2 - 84*a*b**3*x**3 - 126*b**4*x**4)/(630*a**9*b**5 + 5670*a**8*b**6*x + 22680*a**7*b**7*x**2 + 52920*a**6*b**8*x**3 + 79380*a**5*b**9*x**4 + 79380*a**4*b**10*x**5 + 52920*a**3*b**11*x**6 + 22680*a**2*b**12*x**7 + 5670*a*b**13*x**8 + 630*b**14*x**9)$$

$$3.231 \quad \int \frac{x^3}{(a+bx)^{10}} dx$$

Optimal. Leaf size=64

$$\frac{a^3}{9b^4(a+bx)^9} - \frac{3a^2}{8b^4(a+bx)^8} + \frac{3a}{7b^4(a+bx)^7} - \frac{1}{6b^4(a+bx)^6}$$

[Out] $1/9*a^3/b^4/(b*x+a)^9 - 3/8*a^2/b^4/(b*x+a)^8 + 3/7*a/b^4/(b*x+a)^7 - 1/6/b^4/(b*x+a)^6$

Rubi [A] time = 0.03, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^3}{9b^4(a+bx)^9} - \frac{3a^2}{8b^4(a+bx)^8} + \frac{3a}{7b^4(a+bx)^7} - \frac{1}{6b^4(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x)^10, x]

[Out] $a^3/(9*b^4*(a + b*x)^9) - (3*a^2)/(8*b^4*(a + b*x)^8) + (3*a)/(7*b^4*(a + b*x)^7) - 1/(6*b^4*(a + b*x)^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(a+bx)^{10}} dx &= \int \left(-\frac{a^3}{b^3(a+bx)^{10}} + \frac{3a^2}{b^3(a+bx)^9} - \frac{3a}{b^3(a+bx)^8} + \frac{1}{b^3(a+bx)^7} \right) dx \\ &= \frac{a^3}{9b^4(a+bx)^9} - \frac{3a^2}{8b^4(a+bx)^8} + \frac{3a}{7b^4(a+bx)^7} - \frac{1}{6b^4(a+bx)^6} \end{aligned}$$

Mathematica [A] time = 0.01, size = 42, normalized size = 0.66

$$-\frac{a^3 + 9a^2bx + 36ab^2x^2 + 84b^3x^3}{504b^4(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x)^10,x]

[Out] $-1/504*(a^3 + 9*a^2*b*x + 36*a*b^2*x^2 + 84*b^3*x^3)/(b^4*(a + b*x)^9)$

fricas [B] time = 0.46, size = 131, normalized size = 2.05

$$\frac{84 b^3 x^3 + 36 a b^2 x^2 + 9 a^2 b x + a^3}{504 (b^{13} x^9 + 9 a b^{12} x^8 + 36 a^2 b^{11} x^7 + 84 a^3 b^{10} x^6 + 126 a^4 b^9 x^5 + 126 a^5 b^8 x^4 + 84 a^6 b^7 x^3 + 36 a^7 b^6 x^2 + 9 a^8 b^5 x + a^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^10,x, algorithm="fricas")

[Out] $-1/504*(84*b^3*x^3 + 36*a*b^2*x^2 + 9*a^2*b*x + a^3)/(b^{13}*x^9 + 9*a*b^{12}*x^8 + 36*a^2*b^{11}*x^7 + 84*a^3*b^{10}*x^6 + 126*a^4*b^9*x^5 + 126*a^5*b^8*x^4 + 84*a^6*b^7*x^3 + 36*a^7*b^6*x^2 + 9*a^8*b^5*x + a^9*b^4)$

giac [A] time = 1.12, size = 40, normalized size = 0.62

$$\frac{84 b^3 x^3 + 36 a b^2 x^2 + 9 a^2 b x + a^3}{504 (b x + a)^9 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^10,x, algorithm="giac")

[Out] $-1/504*(84*b^3*x^3 + 36*a*b^2*x^2 + 9*a^2*b*x + a^3)/((b*x + a)^9*b^4)$

maple [A] time = 0.00, size = 57, normalized size = 0.89

$$\frac{a^3}{9 (b x + a)^9 b^4} - \frac{3 a^2}{8 (b x + a)^8 b^4} + \frac{3 a}{7 (b x + a)^7 b^4} - \frac{1}{6 (b x + a)^6 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^10,x)

[Out] $1/9*a^3/b^4/(b*x+a)^9-3/8*a^2/b^4/(b*x+a)^8+3/7*a/b^4/(b*x+a)^7-1/6/b^4/(b*x+a)^6$

maxima [B] time = 1.48, size = 131, normalized size = 2.05

$$\frac{84 b^3 x^3 + 36 a b^2 x^2 + 9 a^2 b x + a^3}{504 (b^{13} x^9 + 9 a b^{12} x^8 + 36 a^2 b^{11} x^7 + 84 a^3 b^{10} x^6 + 126 a^4 b^9 x^5 + 126 a^5 b^8 x^4 + 84 a^6 b^7 x^3 + 36 a^7 b^6 x^2 + 9 a^8 b^5 x + a^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^10,x, algorithm="maxima")

[Out]
$$-1/504*(84*b^3*x^3 + 36*a*b^2*x^2 + 9*a^2*b*x + a^3)/(b^{13}*x^9 + 9*a*b^{12}*x^8 + 36*a^2*b^{11}*x^7 + 84*a^3*b^{10}*x^6 + 126*a^4*b^9*x^5 + 126*a^5*b^8*x^4 + 84*a^6*b^7*x^3 + 36*a^7*b^6*x^2 + 9*a^8*b^5*x + a^9*b^4)$$

mupad [B] time = 0.13, size = 48, normalized size = 0.75

$$\frac{\frac{3a}{7(a+bx)^7} - \frac{1}{6(a+bx)^6} - \frac{3a^2}{8(a+bx)^8} + \frac{a^3}{9(a+bx)^9}}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(a + b*x)^10,x)

[Out]
$$((3*a)/(7*(a + b*x)^7) - 1/(6*(a + b*x)^6) - (3*a^2)/(8*(a + b*x)^8) + a^3/(9*(a + b*x)^9))/b^4$$

sympy [B] time = 0.70, size = 139, normalized size = 2.17

$$\frac{-a^3 - 9a^2bx - 36ab^2x^2 - 84b^3x^3}{504a^9b^4 + 4536a^8b^5x + 18144a^7b^6x^2 + 42336a^6b^7x^3 + 63504a^5b^8x^4 + 63504a^4b^9x^5 + 42336a^3b^{10}x^6 + 18144a^2b^{11}x^7 + 4536ab^{12}x^8 + 504b^{13}x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(b*x+a)**10,x)

[Out]
$$(-a^{**3} - 9*a^{**2}*b*x - 36*a*b^{**2}*x^{**2} - 84*b^{**3}*x^{**3})/(504*a^{**9}*b^{**4} + 4536*a^{**8}*b^{**5}*x + 18144*a^{**7}*b^{**6}*x^{**2} + 42336*a^{**6}*b^{**7}*x^{**3} + 63504*a^{**5}*b^{**8}*x^{**4} + 63504*a^{**4}*b^{**9}*x^{**5} + 42336*a^{**3}*b^{**10}*x^{**6} + 18144*a^{**2}*b^{**11}*x^{**7} + 4536*a*b^{**12}*x^{**8} + 504*b^{**13}*x^{**9})$$

$$3.232 \quad \int \frac{x^2}{(a+bx)^{10}} dx$$

Optimal. Leaf size=47

$$-\frac{a^2}{9b^3(a+bx)^9} + \frac{a}{4b^3(a+bx)^8} - \frac{1}{7b^3(a+bx)^7}$$

[Out] $-1/9*a^2/b^3/(b*x+a)^9+1/4*a/b^3/(b*x+a)^8-1/7/b^3/(b*x+a)^7$

Rubi [A] time = 0.02, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{9b^3(a+bx)^9} + \frac{a}{4b^3(a+bx)^8} - \frac{1}{7b^3(a+bx)^7}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2/(a + b*x)^{10}, x]$

[Out] $-a^2/(9*b^3*(a + b*x)^9) + a/(4*b^3*(a + b*x)^8) - 1/(7*b^3*(a + b*x)^7)$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(a+bx)^{10}} dx &= \int \left(\frac{a^2}{b^2(a+bx)^{10}} - \frac{2a}{b^2(a+bx)^9} + \frac{1}{b^2(a+bx)^8} \right) dx \\ &= -\frac{a^2}{9b^3(a+bx)^9} + \frac{a}{4b^3(a+bx)^8} - \frac{1}{7b^3(a+bx)^7} \end{aligned}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 0.66

$$-\frac{a^2 + 9abx + 36b^2x^2}{252b^3(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x)^10,x]

[Out] $-1/252*(a^2 + 9*a*b*x + 36*b^2*x^2)/(b^3*(a + b*x)^9)$

fricas [B] time = 0.44, size = 120, normalized size = 2.55

$$\frac{36b^2x^2 + 9abx + a^2}{252(b^{12}x^9 + 9ab^{11}x^8 + 36a^2b^{10}x^7 + 84a^3b^9x^6 + 126a^4b^8x^5 + 126a^5b^7x^4 + 84a^6b^6x^3 + 36a^7b^5x^2 + 9a^8b^4x + a^9b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^10,x, algorithm="fricas")

[Out] $-1/252*(36*b^2*x^2 + 9*a*b*x + a^2)/(b^{12}*x^9 + 9*a*b^{11}*x^8 + 36*a^2*b^{10}*x^7 + 84*a^3*b^9*x^6 + 126*a^4*b^8*x^5 + 126*a^5*b^7*x^4 + 84*a^6*b^6*x^3 + 36*a^7*b^5*x^2 + 9*a^8*b^4*x + a^9*b^3)$

giac [A] time = 1.04, size = 29, normalized size = 0.62

$$\frac{36b^2x^2 + 9abx + a^2}{252(bx + a)^9b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^10,x, algorithm="giac")

[Out] $-1/252*(36*b^2*x^2 + 9*a*b*x + a^2)/((b*x + a)^9*b^3)$

maple [A] time = 0.00, size = 42, normalized size = 0.89

$$-\frac{a^2}{9(bx + a)^9b^3} + \frac{a}{4(bx + a)^8b^3} - \frac{1}{7(bx + a)^7b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^10,x)

[Out] $-1/9*a^2/b^3/(b*x+a)^9+1/4*a/b^3/(b*x+a)^8-1/7/b^3/(b*x+a)^7$

maxima [B] time = 1.42, size = 120, normalized size = 2.55

$$\frac{36b^2x^2 + 9abx + a^2}{252(b^{12}x^9 + 9ab^{11}x^8 + 36a^2b^{10}x^7 + 84a^3b^9x^6 + 126a^4b^8x^5 + 126a^5b^7x^4 + 84a^6b^6x^3 + 36a^7b^5x^2 + 9a^8b^4x + a^9b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^10,x, algorithm="maxima")

[Out] $-1/252*(36*b^2*x^2 + 9*a*b*x + a^2)/(b^{12}*x^9 + 9*a*b^{11}*x^8 + 36*a^2*b^{10}*x^7 + 84*a^3*b^9*x^6 + 126*a^4*b^8*x^5 + 126*a^5*b^7*x^4 + 84*a^6*b^6*x^3 + 36*a^7*b^5*x^2 + 9*a^8*b^4*x + a^9*b^3)$

mupad [B] time = 0.15, size = 31, normalized size = 0.66

$$\frac{8a^2 + 72abx + 288b^2x^2}{2016b^3(a+bx)^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/(a + b*x)^10,x)`

[Out] $-(8*a^2 + 288*b^2*x^2 + 72*a*b*x)/(2016*b^3*(a + b*x)^9)$

sympy [B] time = 0.68, size = 128, normalized size = 2.72

$$\frac{-a^2 - 9abx - 36b^2x^2}{252a^9b^3 + 2268a^8b^4x + 9072a^7b^5x^2 + 21168a^6b^6x^3 + 31752a^5b^7x^4 + 31752a^4b^8x^5 + 21168a^3b^9x^6 + 9072a^2b^{10}x^7 + 252ab^{11}x^8 + 252b^{12}x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2/(b*x+a)**10,x)`

[Out] $(-a^{**2} - 9*a*b*x - 36*b^{**2}*x^{**2})/(252*a^{**9}*b^{**3} + 2268*a^{**8}*b^{**4}*x + 9072*a^{**7}*b^{**5}*x^{**2} + 21168*a^{**6}*b^{**6}*x^{**3} + 31752*a^{**5}*b^{**7}*x^{**4} + 31752*a^{**4}*b^{**8}*x^{**5} + 21168*a^{**3}*b^{**9}*x^{**6} + 9072*a^{**2}*b^{**10}*x^{**7} + 2268*a*b^{**11}*x^{**8} + 252*b^{**12}*x^{**9})$

$$3.233 \quad \int \frac{x}{(a+bx)^{10}} dx$$

Optimal. Leaf size=30

$$\frac{a}{9b^2(a+bx)^9} - \frac{1}{8b^2(a+bx)^8}$$

[Out] 1/9*a/b^2/(b*x+a)^9-1/8/b^2/(b*x+a)^8

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{a}{9b^2(a+bx)^9} - \frac{1}{8b^2(a+bx)^8}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x)^10,x]

[Out] a/(9*b^2*(a + b*x)^9) - 1/(8*b^2*(a + b*x)^8)

Rule 43

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int
[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n},
x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && Le
Q[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])
```

Rubi steps

$$\begin{aligned} \int \frac{x}{(a+bx)^{10}} dx &= \int \left(-\frac{a}{b(a+bx)^{10}} + \frac{1}{b(a+bx)^9} \right) dx \\ &= \frac{a}{9b^2(a+bx)^9} - \frac{1}{8b^2(a+bx)^8} \end{aligned}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 0.67

$$-\frac{a+9bx}{72b^2(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x)^10,x]

[Out] $-1/72*(a + 9*b*x)/(b^2*(a + b*x)^9)$

fricas [B] time = 0.45, size = 109, normalized size = 3.63

$$\frac{9bx + a}{72(b^{11}x^9 + 9ab^{10}x^8 + 36a^2b^9x^7 + 84a^3b^8x^6 + 126a^4b^7x^5 + 126a^5b^6x^4 + 84a^6b^5x^3 + 36a^7b^4x^2 + 9a^8b^3x + a^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^10,x, algorithm="fricas")`

[Out] $-1/72*(9*b*x + a)/(b^{11}*x^9 + 9*a*b^{10}*x^8 + 36*a^2*b^9*x^7 + 84*a^3*b^8*x^6 + 126*a^4*b^7*x^5 + 126*a^5*b^6*x^4 + 84*a^6*b^5*x^3 + 36*a^7*b^4*x^2 + 9*a^8*b^3*x + a^9*b^2)$

giac [A] time = 1.04, size = 18, normalized size = 0.60

$$\frac{9bx + a}{72(bx + a)^9b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^10,x, algorithm="giac")`

[Out] $-1/72*(9*b*x + a)/((b*x + a)^9*b^2)$

maple [A] time = 0.00, size = 27, normalized size = 0.90

$$\frac{a}{9(bx + a)^9b^2} - \frac{1}{8(bx + a)^8b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(b*x+a)^10,x)`

[Out] $1/9*a/b^2/(b*x+a)^9 - 1/8/b^2/(b*x+a)^8$

maxima [B] time = 1.42, size = 109, normalized size = 3.63

$$\frac{9bx + a}{72(b^{11}x^9 + 9ab^{10}x^8 + 36a^2b^9x^7 + 84a^3b^8x^6 + 126a^4b^7x^5 + 126a^5b^6x^4 + 84a^6b^5x^3 + 36a^7b^4x^2 + 9a^8b^3x + a^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^10,x, algorithm="maxima")`

[Out] $-1/72*(9*b*x + a)/(b^{11}*x^9 + 9*a*b^{10}*x^8 + 36*a^2*b^9*x^7 + 84*a^3*b^8*x^6 + 126*a^4*b^7*x^5 + 126*a^5*b^6*x^4 + 84*a^6*b^5*x^3 + 36*a^7*b^4*x^2 + 9*a^8*b^3*x + a^9*b^2)$

mupad [B] time = 0.07, size = 18, normalized size = 0.60

$$-\frac{a + 9bx}{72b^2(a + bx)^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a + b*x)^10,x)`

[Out] $-(a + 9*b*x)/(72*b^2*(a + b*x)^9)$

sympy [B] time = 0.72, size = 116, normalized size = 3.87

$$\frac{-a - 9bx}{72a^9b^2 + 648a^8b^3x + 2592a^7b^4x^2 + 6048a^6b^5x^3 + 9072a^5b^6x^4 + 9072a^4b^7x^5 + 6048a^3b^8x^6 + 2592a^2b^9x^7 + 648a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)**10,x)`

[Out] $(-a - 9*b*x)/(72*a**9*b**2 + 648*a**8*b**3*x + 2592*a**7*b**4*x**2 + 6048*a**6*b**5*x**3 + 9072*a**5*b**6*x**4 + 9072*a**4*b**7*x**5 + 6048*a**3*b**8*x**6 + 2592*a**2*b**9*x**7 + 648*a*b**10*x**8 + 72*b**11*x**9)$

$$3.234 \quad \int \frac{1}{(a+bx)^{10}} dx$$

Optimal. Leaf size=14

$$-\frac{1}{9b(a+bx)^9}$$

[Out] -1/9/b/(b*x+a)^9

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$-\frac{1}{9b(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-10), x]

[Out] -1/(9*b*(a + b*x)^9)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^{10}} dx = -\frac{1}{9b(a+bx)^9}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\frac{1}{9b(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-10), x]

[Out] -1/9*1/(b*(a + b*x)^9)

fricas [B] time = 0.44, size = 101, normalized size = 7.21

$$\frac{1}{9(b^{10}x^9 + 9ab^9x^8 + 36a^2b^8x^7 + 84a^3b^7x^6 + 126a^4b^6x^5 + 126a^5b^5x^4 + 84a^6b^4x^3 + 36a^7b^3x^2 + 9a^8b^2x + a^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^10,x, algorithm="fricas")

[Out] $-1/9/(b^{10}x^9 + 9*a*b^9*x^8 + 36*a^2*b^8*x^7 + 84*a^3*b^7*x^6 + 126*a^4*b^6*x^5 + 126*a^5*b^5*x^4 + 84*a^6*b^4*x^3 + 36*a^7*b^3*x^2 + 9*a^8*b^2*x + a^9*b)$

giac [A] time = 1.03, size = 12, normalized size = 0.86

$$-\frac{1}{9(bx+a)^9b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^10,x, algorithm="giac")

[Out] $-1/9/((b*x + a)^9*b)$

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$-\frac{1}{9(bx+a)^9b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^10,x)

[Out] $-1/9/b/(b*x+a)^9$

maxima [A] time = 1.34, size = 12, normalized size = 0.86

$$-\frac{1}{9(bx+a)^9b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^10,x, algorithm="maxima")

[Out] $-1/9/((b*x + a)^9*b)$

mupad [B] time = 0.14, size = 103, normalized size = 7.36

$$\frac{1}{9a^9b + 81a^8b^2x + 324a^7b^3x^2 + 756a^6b^4x^3 + 1134a^5b^5x^4 + 1134a^4b^6x^5 + 756a^3b^7x^6 + 324a^2b^8x^7 + 81a^9b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(a + b*x)^10,x)`

[Out] $-1/(9*a^9*b + 9*b^{10}*x^9 + 81*a^8*b^2*x + 81*a*b^9*x^8 + 324*a^7*b^3*x^2 + 756*a^6*b^4*x^3 + 1134*a^5*b^5*x^4 + 1134*a^4*b^6*x^5 + 756*a^3*b^7*x^6 + 324*a^2*b^8*x^7)$

sympy [B] time = 0.67, size = 109, normalized size = 7.79

1

$9a^9b + 81a^8b^2x + 324a^7b^3x^2 + 756a^6b^4x^3 + 1134a^5b^5x^4 + 1134a^4b^6x^5 + 756a^3b^7x^6 + 324a^2b^8x^7 + 81ab^9x^8 +$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**10,x)`

[Out] $-1/(9*a**9*b + 81*a**8*b**2*x + 324*a**7*b**3*x**2 + 756*a**6*b**4*x**3 + 1134*a**5*b**5*x**4 + 1134*a**4*b**6*x**5 + 756*a**3*b**7*x**6 + 324*a**2*b**8*x**7 + 81*a*b**9*x**8 + 9*b**10*x**9)$

$$3.235 \quad \int \frac{1}{x(a+bx)^{10}} dx$$

Optimal. Leaf size=141

$$-\frac{\log(a+bx)}{a^{10}} + \frac{\log(x)}{a^{10}} + \frac{1}{a^9(a+bx)} + \frac{1}{2a^8(a+bx)^2} + \frac{1}{3a^7(a+bx)^3} + \frac{1}{4a^6(a+bx)^4} + \frac{1}{5a^5(a+bx)^5} + \frac{1}{6a^4(a+bx)^6} + \frac{1}{7a^3(a+bx)^7} + \frac{1}{8a^2(a+bx)^8} + \frac{1}{9a(a+bx)^9} + \frac{1}{10a^9(a+bx)^9}$$

[Out] $1/9/a/(b*x+a)^9 + 1/8/a^2/(b*x+a)^8 + 1/7/a^3/(b*x+a)^7 + 1/6/a^4/(b*x+a)^6 + 1/5/a^5/(b*x+a)^5 + 1/4/a^6/(b*x+a)^4 + 1/3/a^7/(b*x+a)^3 + 1/2/a^8/(b*x+a)^2 + 1/a^9/(b*x+a) + \ln(x)/a^{10} - \ln(b*x+a)/a^{10}$

Rubi [A] time = 0.07, antiderivative size = 141, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{1}{a^9(a+bx)} + \frac{1}{2a^8(a+bx)^2} + \frac{1}{3a^7(a+bx)^3} + \frac{1}{4a^6(a+bx)^4} + \frac{1}{5a^5(a+bx)^5} + \frac{1}{6a^4(a+bx)^6} + \frac{1}{7a^3(a+bx)^7} + \frac{1}{8a^2(a+bx)^8} + \frac{1}{9a(a+bx)^9} + \frac{1}{10a^9(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a + b*x)^10), x]

[Out] $1/(9*a*(a + b*x)^9) + 1/(8*a^2*(a + b*x)^8) + 1/(7*a^3*(a + b*x)^7) + 1/(6*a^4*(a + b*x)^6) + 1/(5*a^5*(a + b*x)^5) + 1/(4*a^6*(a + b*x)^4) + 1/(3*a^7*(a + b*x)^3) + 1/(2*a^8*(a + b*x)^2) + 1/(a^9*(a + b*x)) + \text{Log}[x]/a^{10} - \text{Log}[a + b*x]/a^{10}$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] & & ILtQ[m, 0] & & IntegerQ[n] & & !(IGtQ[n, 0] & & LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{x(a+bx)^{10}} dx = \int \left(\frac{1}{a^{10}x} - \frac{b}{a(a+bx)^{10}} - \frac{b}{a^2(a+bx)^9} - \frac{b}{a^3(a+bx)^8} - \frac{b}{a^4(a+bx)^7} - \frac{b}{a^5(a+bx)^6} - \frac{b}{a^6(a+bx)^5} - \frac{b}{a^7(a+bx)^4} - \frac{b}{a^8(a+bx)^3} - \frac{b}{a^9(a+bx)^2} - \frac{b}{a^{10}(a+bx)} \right) dx$$

$$= \frac{1}{9a(a+bx)^9} + \frac{1}{8a^2(a+bx)^8} + \frac{1}{7a^3(a+bx)^7} + \frac{1}{6a^4(a+bx)^6} + \frac{1}{5a^5(a+bx)^5} + \frac{1}{4a^6(a+bx)^4} + \frac{1}{3a^7(a+bx)^3} + \frac{1}{2a^8(a+bx)^2} + \frac{1}{a^9(a+bx)} + \frac{1}{10a^9(a+bx)^9}$$

Mathematica [A] time = 0.10, size = 127, normalized size = 0.90

$$-\frac{\log(a+bx)}{a^{10}} + \frac{\log(x)}{a^{10}} + \frac{280a^8 + 315a^7(a+bx) + 360a^6(a+bx)^2 + 420a^5(a+bx)^3 + 504a^4(a+bx)^4 + 630a^3(a+bx)^5 + 720a^2(a+bx)^6 + 840a(a+bx)^7 + 1080(a+bx)^8}{2520a^9(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)^10),x]

[Out] (280*a^8 + 315*a^7*(a + b*x) + 360*a^6*(a + b*x)^2 + 420*a^5*(a + b*x)^3 + 504*a^4*(a + b*x)^4 + 630*a^3*(a + b*x)^5 + 840*a^2*(a + b*x)^6 + 1260*a*(a + b*x)^7 + 2520*(a + b*x)^8)/(2520*a^9*(a + b*x)^9) + Log[x]/a^10 - Log[a + b*x]/a^10

fricas [B] time = 0.51, size = 388, normalized size = 2.75

$$2520 ab^8 x^8 + 21420 a^2 b^7 x^7 + 80220 a^3 b^6 x^6 + 173250 a^4 b^5 x^5 + 236754 a^5 b^4 x^4 + 210756 a^6 b^3 x^3 + 120564 a^7 b^2 x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^10,x, algorithm="fricas")

[Out] 1/2520*(2520*a*b^8*x^8 + 21420*a^2*b^7*x^7 + 80220*a^3*b^6*x^6 + 173250*a^4*b^5*x^5 + 236754*a^5*b^4*x^4 + 210756*a^6*b^3*x^3 + 120564*a^7*b^2*x^2 + 41481*a^8*b*x + 7129*a^9 - 2520*(b^9*x^9 + 9*a*b^8*x^8 + 36*a^2*b^7*x^7 + 84*a^3*b^6*x^6 + 126*a^4*b^5*x^5 + 126*a^5*b^4*x^4 + 84*a^6*b^3*x^3 + 36*a^7*b^2*x^2 + 9*a^8*b*x + a^9)*log(b*x + a) + 2520*(b^9*x^9 + 9*a*b^8*x^8 + 36*a^2*b^7*x^7 + 84*a^3*b^6*x^6 + 126*a^4*b^5*x^5 + 126*a^5*b^4*x^4 + 84*a^6*b^3*x^3 + 36*a^7*b^2*x^2 + 9*a^8*b*x + a^9)*log(x))/(a^10*b^9*x^9 + 9*a^11*b^8*x^8 + 36*a^12*b^7*x^7 + 84*a^13*b^6*x^6 + 126*a^14*b^5*x^5 + 126*a^15*b^4*x^4 + 84*a^16*b^3*x^3 + 36*a^17*b^2*x^2 + 9*a^18*b*x + a^19)

giac [A] time = 1.05, size = 120, normalized size = 0.85

$$-\frac{\log(|bx + a|)}{a^{10}} + \frac{\log(|x|)}{a^{10}} + \frac{2520 ab^8 x^8 + 21420 a^2 b^7 x^7 + 80220 a^3 b^6 x^6 + 173250 a^4 b^5 x^5 + 236754 a^5 b^4 x^4 + 210756 a^6 b^3 x^3 + 120564 a^7 b^2 x^2 + 41481 a^8 b x + 7129 a^9}{2520 (bx + a)^9 a^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^10,x, algorithm="giac")

[Out] -log(abs(b*x + a))/a^10 + log(abs(x))/a^10 + 1/2520*(2520*a*b^8*x^8 + 21420*a^2*b^7*x^7 + 80220*a^3*b^6*x^6 + 173250*a^4*b^5*x^5 + 236754*a^5*b^4*x^4 + 210756*a^6*b^3*x^3 + 120564*a^7*b^2*x^2 + 41481*a^8*b*x + 7129*a^9)/((b*x + a)^9*a^10)

maple [A] time = 0.01, size = 126, normalized size = 0.89

$$\frac{1}{9 (bx + a)^9 a} + \frac{1}{8 (bx + a)^8 a^2} + \frac{1}{7 (bx + a)^7 a^3} + \frac{1}{6 (bx + a)^6 a^4} + \frac{1}{5 (bx + a)^5 a^5} + \frac{1}{4 (bx + a)^4 a^6} + \frac{1}{3 (bx + a)^3 a^7} + \frac{1}{2 (bx + a)^2 a^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x/(b*x+a)^10,x)`

[Out] $\frac{1}{9} \frac{1}{a} (b*x+a)^{-9} + \frac{1}{8} \frac{1}{a^2} (b*x+a)^{-8} + \frac{1}{7} \frac{1}{a^3} (b*x+a)^{-7} + \frac{1}{6} \frac{1}{a^4} (b*x+a)^{-6} + \frac{1}{5} \frac{1}{a^5} (b*x+a)^{-5} + \frac{1}{4} \frac{1}{a^6} (b*x+a)^{-4} + \frac{1}{3} \frac{1}{a^7} (b*x+a)^{-3} + \frac{1}{2} \frac{1}{a^8} (b*x+a)^{-2} + \frac{1}{a^9} (b*x+a)^{-1} + \ln(x)/a^{10} - \ln(b*x+a)/a^{10}$

maxima [A] time = 1.75, size = 205, normalized size = 1.45

$$\frac{2520 b^8 x^8 + 21420 a b^7 x^7 + 80220 a^2 b^6 x^6 + 173250 a^3 b^5 x^5 + 236754 a^4 b^4 x^4 + 210756 a^5 b^3 x^3 + 120564 a^6 b^2 x^2 + 41481 a^7 b x + 7129 a^8}{2520 (a^9 b^9 x^9 + 9 a^{10} b^8 x^8 + 36 a^{11} b^7 x^7 + 84 a^{12} b^6 x^6 + 126 a^{13} b^5 x^5 + 126 a^{14} b^4 x^4 + 84 a^{15} b^3 x^3 + 36 a^{16} b^2 x^2 + 9 a^{17} b x + a^{18})} - \frac{\ln(b*x+a)}{a^{10}} + \frac{\ln(x)}{a^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b*x+a)^10,x, algorithm="maxima")`

[Out] $\frac{1}{2520} (2520 b^8 x^8 + 21420 a b^7 x^7 + 80220 a^2 b^6 x^6 + 173250 a^3 b^5 x^5 + 236754 a^4 b^4 x^4 + 210756 a^5 b^3 x^3 + 120564 a^6 b^2 x^2 + 41481 a^7 b x + 7129 a^8) / (a^9 b^9 x^9 + 9 a^{10} b^8 x^8 + 36 a^{11} b^7 x^7 + 84 a^{12} b^6 x^6 + 126 a^{13} b^5 x^5 + 126 a^{14} b^4 x^4 + 84 a^{15} b^3 x^3 + 36 a^{16} b^2 x^2 + 9 a^{17} b x + a^{18}) - \frac{\ln(b*x+a)}{a^{10}} + \frac{\ln(x)}{a^{10}}$

mupad [B] time = 0.76, size = 145, normalized size = 1.03

$$\frac{1}{9 a (a + b x)^9} \frac{\ln\left(\frac{a+b x}{x}\right) - \frac{14 b^2 x^2}{(a+b x)^2} + \frac{56 b^3 x^3}{3 (a+b x)^3} - \frac{35 b^4 x^4}{2 (a+b x)^4} + \frac{56 b^5 x^5}{5 (a+b x)^5} - \frac{14 b^6 x^6}{3 (a+b x)^6} + \frac{8 b^7 x^7}{7 (a+b x)^7} - \frac{b^8 x^8}{8 (a+b x)^8} + \frac{8 b x}{a+b x}}{a^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(a + b*x)^10),x)`

[Out] $\frac{1}{(9 a (a + b x)^9) - (\log((a + b x)/x) - (14 b^2 x^2)/(a + b x)^2 + (56 b^3 x^3)/(3 (a + b x)^3) - (35 b^4 x^4)/(2 (a + b x)^4) + (56 b^5 x^5)/(5 (a + b x)^5) - (14 b^6 x^6)/(3 (a + b x)^6) + (8 b^7 x^7)/(7 (a + b x)^7) - (b^8 x^8)/(8 (a + b x)^8) + (8 b x)/(a + b x)) / a^{10}}$

sympy [A] time = 1.02, size = 212, normalized size = 1.50

$$\frac{7129 a^8 + 41481 a^7 b x + 120564 a^6 b^2 x^2 + 210756 a^5 b^3 x^3 + 236754 a^4 b^4 x^4 + 173250 a^3 b^5 x^5 + 80220 a^2 b^6 x^6 + 41481 a b^7 x^7 + 7129 a^8}{2520 a^{18} + 22680 a^{17} b x + 90720 a^{16} b^2 x^2 + 211680 a^{15} b^3 x^3 + 317520 a^{14} b^4 x^4 + 317520 a^{13} b^5 x^5 + 211680 a^{12} b^6 x^6 + 90720 a^{11} b^7 x^7 + 7129 a^8} - \frac{\ln(b*x+a)}{a^{10}} + \frac{\ln(x)}{a^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b*x+a)**10,x)`

```
[Out] (7129*a**8 + 41481*a**7*b*x + 120564*a**6*b**2*x**2 + 210756*a**5*b**3*x**3
+ 236754*a**4*b**4*x**4 + 173250*a**3*b**5*x**5 + 80220*a**2*b**6*x**6 + 2
1420*a*b**7*x**7 + 2520*b**8*x**8)/(2520*a**18 + 22680*a**17*b*x + 90720*a*
*16*b**2*x**2 + 211680*a**15*b**3*x**3 + 317520*a**14*b**4*x**4 + 317520*a*
*13*b**5*x**5 + 211680*a**12*b**6*x**6 + 90720*a**11*b**7*x**7 + 22680*a**1
0*b**8*x**8 + 2520*a**9*b**9*x**9) + (log(x) - log(a/b + x))/a**10
```

$$3.236 \quad \int \frac{1}{x^2(a+bx)^{10}} dx$$

Optimal. Leaf size=158

$$-\frac{10b \log(x)}{a^{11}} + \frac{10b \log(a+bx)}{a^{11}} - \frac{9b}{a^{10}(a+bx)} - \frac{1}{a^{10}x} - \frac{4b}{a^9(a+bx)^2} - \frac{7b}{3a^8(a+bx)^3} - \frac{3b}{2a^7(a+bx)^4} - \frac{b}{a^6(a+bx)^5} - \frac{2}{3a^5(a+bx)^6}$$

[Out] $-1/a^{10}/x - 1/9*b/a^2/(b*x+a)^9 - 1/4*b/a^3/(b*x+a)^8 - 3/7*b/a^4/(b*x+a)^7 - 2/3*b/a^5/(b*x+a)^6 - b/a^6/(b*x+a)^5 - 3/2*b/a^7/(b*x+a)^4 - 7/3*b/a^8/(b*x+a)^3 - 4*b/a^9/(b*x+a)^2 - 9*b/a^{10}/(b*x+a) - 10*b*\ln(x)/a^{11} + 10*b*\ln(b*x+a)/a^{11}$

Rubi [A] time = 0.12, antiderivative size = 158, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{9b}{a^{10}(a+bx)} - \frac{4b}{a^9(a+bx)^2} - \frac{7b}{3a^8(a+bx)^3} - \frac{3b}{2a^7(a+bx)^4} - \frac{b}{a^6(a+bx)^5} - \frac{2b}{3a^5(a+bx)^6} - \frac{3b}{7a^4(a+bx)^7} - \frac{b}{4a^3(a+bx)^8}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(a + b*x)^10), x]

[Out] $-(1/(a^{10}x)) - b/(9*a^2*(a + b*x)^9) - b/(4*a^3*(a + b*x)^8) - (3*b)/(7*a^4*(a + b*x)^7) - (2*b)/(3*a^5*(a + b*x)^6) - b/(a^6*(a + b*x)^5) - (3*b)/(2*a^7*(a + b*x)^4) - (7*b)/(3*a^8*(a + b*x)^3) - (4*b)/(a^9*(a + b*x)^2) - (9*b)/(a^{10}*(a + b*x)) - (10*b*\text{Log}[x])/a^{11} + (10*b*\text{Log}[a + b*x])/a^{11}$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] & & ILtQ[m, 0] & & IntegerQ[n] & & !(IGtQ[n, 0] & & LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{x^2(a+bx)^{10}} dx = \int \left(\frac{1}{a^{10}x^2} - \frac{10b}{a^{11}x} + \frac{b^2}{a^2(a+bx)^{10}} + \frac{2b^2}{a^3(a+bx)^9} + \frac{3b^2}{a^4(a+bx)^8} + \frac{4b^2}{a^5(a+bx)^7} + \frac{5b^2}{a^6(a+bx)^6} \right) dx$$

$$= -\frac{1}{a^{10}x} - \frac{b}{9a^2(a+bx)^9} - \frac{b}{4a^3(a+bx)^8} - \frac{3b}{7a^4(a+bx)^7} - \frac{2b}{3a^5(a+bx)^6} - \frac{b}{a^6(a+bx)^5} - \frac{2}{2a^7(a+bx)^4}$$

Mathematica [A] time = 0.13, size = 130, normalized size = 0.82

$$\frac{a(252a^9 + 7129a^8bx + 41481a^7b^2x^2 + 120564a^6b^3x^3 + 210756a^5b^4x^4 + 236754a^4b^5x^5 + 173250a^3b^6x^6 + 80220a^2b^7x^7 + 21420ab^8x^8 + 2520b^9x^9)}{x(a+bx)^9} - 2520a^{11}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)^10),x]

[Out] $-1/252*((a*(252*a^9 + 7129*a^8*b*x + 41481*a^7*b^2*x^2 + 120564*a^6*b^3*x^3 + 210756*a^5*b^4*x^4 + 236754*a^4*b^5*x^5 + 173250*a^3*b^6*x^6 + 80220*a^2*b^7*x^7 + 21420*a*b^8*x^8 + 2520*b^9*x^9))/(x*(a + b*x)^9) + 2520*b*\text{Log}[x] - 2520*b*\text{Log}[a + b*x])/a^{11}$

fricas [B] time = 0.50, size = 417, normalized size = 2.64

$$\frac{2520 ab^9 x^9 + 21420 a^2 b^8 x^8 + 80220 a^3 b^7 x^7 + 173250 a^4 b^6 x^6 + 236754 a^5 b^5 x^5 + 210756 a^6 b^4 x^4 + 120564 a^7 b^3 x^3 + 41481 a^8 b^2 x^2 + 7129 a^9 b x + 2520 a^{10}}{x(a+bx)^9} - 2520 a^{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^10,x, algorithm="fricas")

[Out] $-1/252*(2520*a*b^9*x^9 + 21420*a^2*b^8*x^8 + 80220*a^3*b^7*x^7 + 173250*a^4*b^6*x^6 + 236754*a^5*b^5*x^5 + 210756*a^6*b^4*x^4 + 120564*a^7*b^3*x^3 + 41481*a^8*b^2*x^2 + 7129*a^9*b*x + 2520*a^{10} - 2520*(b^{10}*x^{10} + 9*a*b^9*x^9 + 36*a^2*b^8*x^8 + 84*a^3*b^7*x^7 + 126*a^4*b^6*x^6 + 126*a^5*b^5*x^5 + 84*a^6*b^4*x^4 + 36*a^7*b^3*x^3 + 9*a^8*b^2*x^2 + a^9*b*x)*\text{log}(b*x + a) + 2520*(b^{10}*x^{10} + 9*a*b^9*x^9 + 36*a^2*b^8*x^8 + 84*a^3*b^7*x^7 + 126*a^4*b^6*x^6 + 126*a^5*b^5*x^5 + 84*a^6*b^4*x^4 + 36*a^7*b^3*x^3 + 9*a^8*b^2*x^2 + a^9*b*x)*\text{log}(x))/(a^{11}*b^9*x^{10} + 9*a^{12}*b^8*x^9 + 36*a^{13}*b^7*x^8 + 84*a^{14}*b^6*x^7 + 126*a^{15}*b^5*x^6 + 126*a^{16}*b^4*x^5 + 84*a^{17}*b^3*x^4 + 36*a^{18}*b^2*x^3 + 9*a^{19}*b*x^2 + a^{20}*x)$

giac [A] time = 1.01, size = 137, normalized size = 0.87

$$\frac{10 b \log(|bx + a|)}{a^{11}} - \frac{10 b \log(|x|)}{a^{11}} - \frac{2520 ab^9 x^9 + 21420 a^2 b^8 x^8 + 80220 a^3 b^7 x^7 + 173250 a^4 b^6 x^6 + 236754 a^5 b^5 x^5 + 210756 a^6 b^4 x^4 + 120564 a^7 b^3 x^3 + 41481 a^8 b^2 x^2 + 7129 a^9 b x + 2520 a^{10}}{252 (bx + a)^9} - 2520 a^{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^10,x, algorithm="giac")

[Out] $10*b*\text{log}(\text{abs}(b*x + a))/a^{11} - 10*b*\text{log}(\text{abs}(x))/a^{11} - 1/252*(2520*a*b^9*x^9 + 21420*a^2*b^8*x^8 + 80220*a^3*b^7*x^7 + 173250*a^4*b^6*x^6 + 236754*a^5*$

$$\frac{b^5 x^5 + 210756 a^6 b^4 x^4 + 120564 a^7 b^3 x^3 + 41481 a^8 b^2 x^2 + 7129 a^9 b x + 252 a^{10}}{(b x + a)^9 a^{11} x}$$

maple [A] time = 0.01, size = 147, normalized size = 0.93

$$\frac{b}{9(bx+a)^9 a^2} - \frac{b}{4(bx+a)^8 a^3} - \frac{3b}{7(bx+a)^7 a^4} - \frac{2b}{3(bx+a)^6 a^5} - \frac{b}{(bx+a)^5 a^6} - \frac{3b}{2(bx+a)^4 a^7} - \frac{7b}{3(bx+a)^3 a^8} - \frac{4b}{(bx+a)^2 a^9} - \frac{10b \ln(x)}{a^{11}} + \frac{10b \ln(bx+a)}{a^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^10,x)

[Out] $-\frac{1}{a^{10}x} - \frac{1}{9b/a^2(bx+a)^9} - \frac{1}{4b/a^3(bx+a)^8} - \frac{3}{7b/a^4(bx+a)^7} - \frac{2}{3b/a^5(bx+a)^6} - \frac{b/a^6(bx+a)^5}{3/2b/a^7(bx+a)^4} - \frac{7/3b/a^8(bx+a)^3}{4b/a^9(bx+a)^2} - \frac{9b/a^{10}(bx+a)}{10b \ln(x)/a^{11} + 10b \ln(bx+a)/a^{11}}$

maxima [A] time = 1.71, size = 223, normalized size = 1.41

$$\frac{2520 b^9 x^9 + 21420 a b^8 x^8 + 80220 a^2 b^7 x^7 + 173250 a^3 b^6 x^6 + 236754 a^4 b^5 x^5 + 210756 a^5 b^4 x^4 + 120564 a^6 b^3 x^3 + 41481 a^7 b^2 x^2 + 7129 a^8 b x + 252 a^9}{252 (a^{10} b^9 x^{10} + 9 a^{11} b^8 x^9 + 36 a^{12} b^7 x^8 + 84 a^{13} b^6 x^7 + 126 a^{14} b^5 x^6 + 126 a^{15} b^4 x^5 + 84 a^{16} b^3 x^4 + 36 a^{17} b^2 x^3 + 9 a^{18} b x^2 + a^{19} x) + 10 b \log(bx+a) - 10 b \log(x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^10,x, algorithm="maxima")

[Out] $-\frac{1}{252} \frac{(2520 b^9 x^9 + 21420 a b^8 x^8 + 80220 a^2 b^7 x^7 + 173250 a^3 b^6 x^6 + 236754 a^4 b^5 x^5 + 210756 a^5 b^4 x^4 + 120564 a^6 b^3 x^3 + 41481 a^7 b^2 x^2 + 7129 a^8 b x + 252 a^9)}{(a^{10} b^9 x^{10} + 9 a^{11} b^8 x^9 + 36 a^{12} b^7 x^8 + 84 a^{13} b^6 x^7 + 126 a^{14} b^5 x^6 + 126 a^{15} b^4 x^5 + 84 a^{16} b^3 x^4 + 36 a^{17} b^2 x^3 + 9 a^{18} b x^2 + a^{19} x) + 10 b \log(bx+a) - 10 b \log(x)}$

mupad [B] time = 0.39, size = 217, normalized size = 1.37

$$\frac{20 b \operatorname{atanh}\left(\frac{2 b x}{a} + 1\right)}{a^{11}} - \frac{\frac{1}{a} + \frac{4609 b^2 x^2}{28 a^3} + \frac{3349 b^3 x^3}{7 a^4} + \frac{2509 b^4 x^4}{3 a^5} + \frac{1879 b^5 x^5}{2 a^6} + \frac{1375 b^6 x^6}{2 a^7} + \frac{955 b^7 x^7}{3 a^8} + \frac{85 b^8 x^8}{a^9} + \frac{10 b^9 x^9}{a^{10}} + \frac{7129 b x}{252 a^2}}{a^9 x + 9 a^8 b x^2 + 36 a^7 b^2 x^3 + 84 a^6 b^3 x^4 + 126 a^5 b^4 x^5 + 126 a^4 b^5 x^6 + 84 a^3 b^6 x^7 + 36 a^2 b^7 x^8 + 9 a b^8 x^9 + a^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(a + b*x)^10),x)

[Out] $\frac{20 b \operatorname{atanh}\left(\frac{2 b x}{a} + 1\right)}{a^{11}} - \frac{1}{a} - \frac{4609 b^2 x^2}{28 a^3} - \frac{3349 b^3 x^3}{7 a^4} - \frac{2509 b^4 x^4}{3 a^5} - \frac{1879 b^5 x^5}{2 a^6} - \frac{1375 b^6 x^6}{2 a^7} - \frac{955 b^7 x^7}{3 a^8} - \frac{85 b^8 x^8}{a^9} - \frac{10 b^9 x^9}{a^{10}} - \frac{7129 b x}{252 a^2} \frac{1}{a^9 x + 9 a^8 b x^2 + 36 a^7 b^2 x^3 + 84 a^6 b^3 x^4 + 126 a^5 b^4 x^5 + 126 a^4 b^5 x^6 + 84 a^3 b^6 x^7 + 36 a^2 b^7 x^8 + 9 a b^8 x^9 + a^9}$

$$36*a^7*b^2*x^3 + 84*a^6*b^3*x^4 + 126*a^5*b^4*x^5 + 126*a^4*b^5*x^6 + 84*a^3*b^6*x^7 + 36*a^2*b^7*x^8)$$

sympy [A] time = 1.15, size = 233, normalized size = 1.47

$$\frac{-252a^9 - 7129a^8bx - 41481a^7b^2x^2 - 120564a^6b^3x^3 - 210756a^5b^4x^4 - 236754a^4b^5x^5 - 173250a^3b^6x^6 - 80220a^2b^7x^7 - 21420ab^8x^8 - 2520b^9x^9}{252a^{19}x + 2268a^{18}bx^2 + 9072a^{17}b^2x^3 + 21168a^{16}b^3x^4 + 31752a^{15}b^4x^5 + 31752a^{14}b^5x^6 + 21168a^{13}b^6x^7 + 9072a^{12}b^7x^8 + 2268a^{11}b^8x^9 + 252a^{10}b^9x^{10}} + 10*b*(-\log(x) + \log(a/b + x))/a^{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/(b*x+a)**10,x)

[Out] (-252*a**9 - 7129*a**8*b*x - 41481*a**7*b**2*x**2 - 120564*a**6*b**3*x**3 - 210756*a**5*b**4*x**4 - 236754*a**4*b**5*x**5 - 173250*a**3*b**6*x**6 - 80220*a**2*b**7*x**7 - 21420*a*b**8*x**8 - 2520*b**9*x**9)/(252*a**19*x + 2268*a**18*b*x**2 + 9072*a**17*b**2*x**3 + 21168*a**16*b**3*x**4 + 31752*a**15*b**4*x**5 + 31752*a**14*b**5*x**6 + 21168*a**13*b**6*x**7 + 9072*a**12*b**7*x**8 + 2268*a**11*b**8*x**9 + 252*a**10*b**9*x**10) + 10*b*(-log(x) + log(a/b + x))/a**11

$$3.237 \quad \int \frac{1}{x^3(a+bx)^{10}} dx$$

Optimal. Leaf size=191

$$\frac{55b^2 \log(x)}{a^{12}} - \frac{55b^2 \log(a+bx)}{a^{12}} + \frac{45b^2}{a^{11}(a+bx)} + \frac{10b}{a^{11}x} + \frac{18b^2}{a^{10}(a+bx)^2} - \frac{1}{2a^{10}x^2} + \frac{28b^2}{3a^9(a+bx)^3} + \frac{21b^2}{4a^8(a+bx)^4} + \frac{3b^2}{a^7(a+bx)^5}$$

[Out] $-1/2/a^{10}/x^2+10*b/a^{11}/x+1/9*b^2/a^3/(b*x+a)^9+3/8*b^2/a^4/(b*x+a)^8+6/7*b^2/a^5/(b*x+a)^7+5/3*b^2/a^6/(b*x+a)^6+3*b^2/a^7/(b*x+a)^5+21/4*b^2/a^8/(b*x+a)^4+28/3*b^2/a^9/(b*x+a)^3+18*b^2/a^{10}/(b*x+a)^2+45*b^2/a^{11}/(b*x+a)+55*b^2*\ln(x)/a^{12}-55*b^2*\ln(b*x+a)/a^{12}$

Rubi [A] time = 0.14, antiderivative size = 191, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{45b^2}{a^{11}(a+bx)} + \frac{18b^2}{a^{10}(a+bx)^2} + \frac{28b^2}{3a^9(a+bx)^3} + \frac{21b^2}{4a^8(a+bx)^4} + \frac{3b^2}{a^7(a+bx)^5} + \frac{5b^2}{3a^6(a+bx)^6} + \frac{6b^2}{7a^5(a+bx)^7} + \frac{3b^2}{8a^4(a+bx)^8}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(a + b*x)^10), x]

[Out] $-1/(2*a^{10}*x^2) + (10*b)/(a^{11}*x) + b^2/(9*a^3*(a + b*x)^9) + (3*b^2)/(8*a^4*(a + b*x)^8) + (6*b^2)/(7*a^5*(a + b*x)^7) + (5*b^2)/(3*a^6*(a + b*x)^6) + (3*b^2)/(a^7*(a + b*x)^5) + (21*b^2)/(4*a^8*(a + b*x)^4) + (28*b^2)/(3*a^9*(a + b*x)^3) + (18*b^2)/(a^{10}*(a + b*x)^2) + (45*b^2)/(a^{11}*(a + b*x)) + (55*b^2*Log[x])/a^{12} - (55*b^2*Log[a + b*x])/a^{12}$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{x^3(a+bx)^{10}} dx = \int \left(\frac{1}{a^{10}x^3} - \frac{10b}{a^{11}x^2} + \frac{55b^2}{a^{12}x} - \frac{b^3}{a^3(a+bx)^{10}} - \frac{3b^3}{a^4(a+bx)^9} - \frac{6b^3}{a^5(a+bx)^8} - \frac{10b^3}{a^6(a+bx)^7} - \frac{3b^3}{a^7(a+bx)^6} \right) dx$$

$$= -\frac{1}{2a^{10}x^2} + \frac{10b}{a^{11}x} + \frac{b^2}{9a^3(a+bx)^9} + \frac{3b^2}{8a^4(a+bx)^8} + \frac{6b^2}{7a^5(a+bx)^7} + \frac{5b^2}{3a^6(a+bx)^6} + \frac{3b^2}{a^7(a+bx)^5}$$

Mathematica [A] time = 0.11, size = 145, normalized size = 0.76

$$\frac{a(-252a^{10}+2772a^9bx+78419a^8b^2x^2+456291a^7b^3x^3+1326204a^6b^4x^4+2318316a^5b^5x^5+2604294a^4b^6x^6+1905750a^3b^7x^7+882420a^2b^8x^8+235620ab^9x^9)}{x^2(a+bx)^9}$$

$$504a^{12}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)^10), x]

[Out] ((a*(-252*a^10 + 2772*a^9*b*x + 78419*a^8*b^2*x^2 + 456291*a^7*b^3*x^3 + 1326204*a^6*b^4*x^4 + 2318316*a^5*b^5*x^5 + 2604294*a^4*b^6*x^6 + 1905750*a^3*b^7*x^7 + 882420*a^2*b^8*x^8 + 235620*a*b^9*x^9 + 27720*b^10*x^10))/(x^2*(a + b*x)^9) + 27720*b^2*Log[x] - 27720*b^2*Log[a + b*x])/(504*a^12)

fricas [B] time = 0.49, size = 438, normalized size = 2.29

$$\frac{27720 ab^{10}x^{10} + 235620 a^2b^9x^9 + 882420 a^3b^8x^8 + 1905750 a^4b^7x^7 + 2604294 a^5b^6x^6 + 2318316 a^6b^5x^5 + 1326204 a^7b^4x^4 + 456291 a^8b^3x^3 + 78419 a^9b^2x^2 + 2772 a^{10}b x - 252 a^{11}}{504 a^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^10,x, algorithm="fricas")

[Out] 1/504*(27720*a*b^10*x^10 + 235620*a^2*b^9*x^9 + 882420*a^3*b^8*x^8 + 1905750*a^4*b^7*x^7 + 2604294*a^5*b^6*x^6 + 2318316*a^6*b^5*x^5 + 1326204*a^7*b^4*x^4 + 456291*a^8*b^3*x^3 + 78419*a^9*b^2*x^2 + 2772*a^10*b*x - 252*a^11 - 27720*(b^11*x^11 + 9*a*b^10*x^10 + 36*a^2*b^9*x^9 + 84*a^3*b^8*x^8 + 126*a^4*b^7*x^7 + 126*a^5*b^6*x^6 + 84*a^6*b^5*x^5 + 36*a^7*b^4*x^4 + 9*a^8*b^3*x^3 + a^9*b^2*x^2)*log(b*x + a) + 27720*(b^11*x^11 + 9*a*b^10*x^10 + 36*a^2*b^9*x^9 + 84*a^3*b^8*x^8 + 126*a^4*b^7*x^7 + 126*a^5*b^6*x^6 + 84*a^6*b^5*x^5 + 36*a^7*b^4*x^4 + 9*a^8*b^3*x^3 + a^9*b^2*x^2)*log(x))/(a^12*b^9*x^11 + 9*a^13*b^8*x^10 + 36*a^14*b^7*x^9 + 84*a^15*b^6*x^8 + 126*a^16*b^5*x^7 + 126*a^17*b^4*x^6 + 84*a^18*b^3*x^5 + 36*a^19*b^2*x^4 + 9*a^20*b*x^3 + a^21*x^2)

giac [A] time = 1.10, size = 152, normalized size = 0.80

$$-\frac{55b^2 \log(|bx + a|)}{a^{12}} + \frac{55b^2 \log(|x|)}{a^{12}} + \frac{27720 ab^{10}x^{10} + 235620 a^2b^9x^9 + 882420 a^3b^8x^8 + 1905750 a^4b^7x^7 + 2604294 a^5b^6x^6 + 2318316 a^6b^5x^5 + 1326204 a^7b^4x^4 + 456291 a^8b^3x^3 + 78419 a^9b^2x^2 + 2772 a^{10}b x - 252 a^{11}}{504 a^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^10,x, algorithm="giac")

[Out] -55*b^2*log(abs(b*x + a))/a^12 + 55*b^2*log(abs(x))/a^12 + 1/504*(27720*a*b^10*x^10 + 235620*a^2*b^9*x^9 + 882420*a^3*b^8*x^8 + 1905750*a^4*b^7*x^7 + 2604294*a^5*b^6*x^6 + 2318316*a^6*b^5*x^5 + 1326204*a^7*b^4*x^4 + 456291*a^8*b^3*x^3 + 78419*a^9*b^2*x^2 + 2772*a^10*b*x - 252*a^11)

$$2604294a^5b^6x^6 + 2318316a^6b^5x^5 + 1326204a^7b^4x^4 + 456291a^8b^3x^3 + 78419a^9b^2x^2 + 2772a^{10}bx - 252a^{11}) / ((bx + a)^9a^{12}x^2)$$

maple [A] time = 0.02, size = 178, normalized size = 0.93

$$\frac{b^2}{9(bx+a)^9a^3} + \frac{3b^2}{8(bx+a)^8a^4} + \frac{6b^2}{7(bx+a)^7a^5} + \frac{5b^2}{3(bx+a)^6a^6} + \frac{3b^2}{(bx+a)^5a^7} + \frac{21b^2}{4(bx+a)^4a^8} + \frac{28b^2}{3(bx+a)^3a^9} + \frac{11b^2}{(bx+a)^2a^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a)^10,x)

[Out] $-\frac{1}{2} \frac{1}{a^{10}x^2} + \frac{10b}{a^{11}x} + \frac{1}{9} \frac{b^2}{a^3(bx+a)^9} + \frac{3}{8} \frac{b^2}{a^4(bx+a)^8} + \frac{6}{7} \frac{b^2}{a^5(bx+a)^7} + \frac{5}{3} \frac{b^2}{a^6(bx+a)^6} + \frac{3}{2} \frac{b^2}{a^7(bx+a)^5} + \frac{21}{4} \frac{b^2}{a^8(bx+a)^4} + \frac{28}{3} \frac{b^2}{a^9(bx+a)^3} + \frac{18}{b} \frac{b^2}{a^{10}(bx+a)^2} + \frac{45}{a^{11}} \frac{b^2}{bx+a} + 55 \frac{b^2 \ln(x)}{a^{12}} - 55 \frac{b^2 \ln(bx+a)}{a^{12}}$

maxima [A] time = 1.71, size = 240, normalized size = 1.26

$$\frac{27720b^{10}x^{10} + 235620ab^9x^9 + 882420a^2b^8x^8 + 1905750a^3b^7x^7 + 2604294a^4b^6x^6 + 2318316a^5b^5x^5 + 1326204a^6b^4x^4 + 456291a^7b^3x^3 + 78419a^8b^2x^2 + 2772a^9bx - 252a^{10})}{504(a^{11}b^9x^{11} + 9a^{12}b^8x^{10} + 36a^{13}b^7x^9 + 84a^{14}b^6x^8 + 126a^{15}b^5x^7 + 126a^{16}b^4x^6 + 84a^{17}b^3x^5 + 36a^{18}b^2x^4 + 9a^{19}bx^3 + a^{20}x^2) - 55b^2 \log(bx+a)/a^{12} + 55b^2 \log(x)/a^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^10,x, algorithm="maxima")

[Out] $\frac{1}{504} \frac{(27720b^{10}x^{10} + 235620a^2b^8x^8 + 1905750a^3b^7x^7 + 2604294a^4b^6x^6 + 2318316a^5b^5x^5 + 1326204a^6b^4x^4 + 456291a^7b^3x^3 + 78419a^8b^2x^2 + 2772a^9bx - 252a^{10})}{(a^{11}b^9x^{11} + 9a^{12}b^8x^{10} + 36a^{13}b^7x^9 + 84a^{14}b^6x^8 + 126a^{15}b^5x^7 + 126a^{16}b^4x^6 + 84a^{17}b^3x^5 + 36a^{18}b^2x^4 + 9a^{19}bx^3 + a^{20}x^2) - 55b^2 \log(bx+a)/a^{12} + 55b^2 \log(x)/a^{12}}$

mupad [B] time = 0.44, size = 233, normalized size = 1.22

$$\frac{\frac{78419b^2x^2}{504a^3} - \frac{1}{2a} + \frac{50699b^3x^3}{56a^4} + \frac{36839b^4x^4}{14a^5} + \frac{27599b^5x^5}{6a^6} + \frac{20669b^6x^6}{4a^7} + \frac{15125b^7x^7}{4a^8} + \frac{10505b^8x^8}{6a^9} + \frac{935b^9x^9}{2a^{10}} + \frac{55b^{10}x^{10}}{a^{11}} + \frac{11b^{11}x^{11}}{a^{12}}}{a^9x^2 + 9a^8bx^3 + 36a^7b^2x^4 + 84a^6b^3x^5 + 126a^5b^4x^6 + 126a^4b^5x^7 + 84a^3b^6x^8 + 36a^2b^7x^9 + 9ab^8x^{10} + b^9x^{11}} - \frac{55b^2 \log(bx+a)}{a^{12}} + \frac{55b^2 \log(x)}{a^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(a + b*x)^10),x)

[Out] $\frac{(78419b^2x^2)/(504a^3) - 1/(2a) + (50699b^3x^3)/(56a^4) + (36839b^4x^4)/(14a^5) + (27599b^5x^5)/(6a^6) + (20669b^6x^6)/(4a^7) + (15125b^7x^7)/(4a^8) + (10505b^8x^8)/(6a^9) + (935b^9x^9)/(2a^{10}) + (55b^{10}x^{10})/a^{11} + (11b^{11}x^{11})/a^{12}}{a^9x^2 + 9a^8bx^3 + 36a^7b^2x^4 + 84a^6b^3x^5 + 126a^5b^4x^6 + 126a^4b^5x^7 + 84a^3b^6x^8 + 36a^2b^7x^9 + 9ab^8x^{10} + b^9x^{11}} - \frac{55b^2 \log(bx+a)}{a^{12}} + \frac{55b^2 \log(x)}{a^{12}}$

$$\frac{b^{10}x^{10}}{a^{11}} + \frac{(11bx)}{(2a^2)} \frac{1}{(a^9x^2 + b^9x^{11} + 9a^8bx^3 + 9ab^8x^{10} + 36a^7b^2x^4 + 84a^6b^3x^5 + 126a^5b^4x^6 + 126a^4b^5x^7 + 84a^3b^6x^8 + 36a^2b^7x^9)} - \frac{(110b^2 \operatorname{atanh}(\frac{2bx}{a+1}))}{a^{12}}$$

sympy [A] time = 1.18, size = 246, normalized size = 1.29

$$\frac{-252a^{10} + 2772a^9bx + 78419a^8b^2x^2 + 456291a^7b^3x^3 + 1326204a^6b^4x^4 + 2318316a^5b^5x^5 + 2604294a^4b^6x^6 + 1905750a^3b^7x^7 + 882420a^2b^8x^8 + 235620ab^9x^9 + 27720b^{10}x^{10}}{504a^{20}x^2 + 4536a^{19}bx^3 + 18144a^{18}b^2x^4 + 42336a^{17}b^3x^5 + 63504a^{16}b^4x^6 + 63504a^{15}b^5x^7 + 42336a^{14}b^6x^8 + 18144a^{13}b^7x^9 + 4536a^{12}b^8x^{10} + 504a^{11}b^9x^{11}} + 55b^2(\log(x) - \log(a/b + x))/a^{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(b*x+a)**10,x)

[Out] (-252*a**10 + 2772*a**9*b*x + 78419*a**8*b**2*x**2 + 456291*a**7*b**3*x**3 + 1326204*a**6*b**4*x**4 + 2318316*a**5*b**5*x**5 + 2604294*a**4*b**6*x**6 + 1905750*a**3*b**7*x**7 + 882420*a**2*b**8*x**8 + 235620*a*b**9*x**9 + 27720*b**10*x**10)/(504*a**20*x**2 + 4536*a**19*b*x**3 + 18144*a**18*b**2*x**4 + 42336*a**17*b**3*x**5 + 63504*a**16*b**4*x**6 + 63504*a**15*b**5*x**7 + 42336*a**14*b**6*x**8 + 18144*a**13*b**7*x**9 + 4536*a**12*b**8*x**10 + 504*a**11*b**9*x**11) + 55*b**2*(log(x) - log(a/b + x))/a**12

$$3.238 \quad \int \frac{1}{x^4(a+bx)^{10}} dx$$

Optimal. Leaf size=198

$$-\frac{220b^3 \log(x)}{a^{13}} + \frac{220b^3 \log(a+bx)}{a^{13}} - \frac{165b^3}{a^{12}(a+bx)} - \frac{55b^2}{a^{12}x} - \frac{60b^3}{a^{11}(a+bx)^2} + \frac{5b}{a^{11}x^2} - \frac{28b^3}{a^{10}(a+bx)^3} - \frac{1}{3a^{10}x^3} - \frac{14b^3}{a^9(a+bx)^4}$$

[Out] $-1/3/a^{10}/x^3+5*b/a^{11}/x^2-55*b^2/a^{12}/x-1/9*b^3/a^4/(b*x+a)^9-1/2*b^3/a^5/(b*x+a)^8-10/7*b^3/a^6/(b*x+a)^7-10/3*b^3/a^7/(b*x+a)^6-7*b^3/a^8/(b*x+a)^5-14*b^3/a^9/(b*x+a)^4-28*b^3/a^{10}/(b*x+a)^3-60*b^3/a^{11}/(b*x+a)^2-165*b^3/a^{12}/(b*x+a)-220*b^3*\ln(x)/a^{13}+220*b^3*\ln(b*x+a)/a^{13}$

Rubi [A] time = 0.16, antiderivative size = 198, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{165b^3}{a^{12}(a+bx)} - \frac{60b^3}{a^{11}(a+bx)^2} - \frac{28b^3}{a^{10}(a+bx)^3} - \frac{14b^3}{a^9(a+bx)^4} - \frac{7b^3}{a^8(a+bx)^5} - \frac{10b^3}{3a^7(a+bx)^6} - \frac{10b^3}{7a^6(a+bx)^7} - \frac{b^3}{2a^5(a+bx)^8}$$

Antiderivative was successfully verified.

[In] Int[1/(x^4*(a + b*x)^10), x]

[Out] $-1/(3*a^{10}*x^3) + (5*b)/(a^{11}*x^2) - (55*b^2)/(a^{12}*x) - b^3/(9*a^4*(a + b*x)^9) - b^3/(2*a^5*(a + b*x)^8) - (10*b^3)/(7*a^6*(a + b*x)^7) - (10*b^3)/(3*a^7*(a + b*x)^6) - (7*b^3)/(a^8*(a + b*x)^5) - (14*b^3)/(a^9*(a + b*x)^4) - (28*b^3)/(a^{10}*(a + b*x)^3) - (60*b^3)/(a^{11}*(a + b*x)^2) - (165*b^3)/(a^{12}*(a + b*x)) - (220*b^3*\text{Log}[x])/a^{13} + (220*b^3*\text{Log}[a + b*x])/a^{13}$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^4(a+bx)^{10}} dx &= \int \left(\frac{1}{a^{10}x^4} - \frac{10b}{a^{11}x^3} + \frac{55b^2}{a^{12}x^2} - \frac{220b^3}{a^{13}x} + \frac{b^4}{a^4(a+bx)^{10}} + \frac{4b^4}{a^5(a+bx)^9} + \frac{10b^4}{a^6(a+bx)^8} + \frac{20b^4}{a^7(a+bx)^7} \right. \\ &= -\frac{1}{3a^{10}x^3} + \frac{5b}{a^{11}x^2} - \frac{55b^2}{a^{12}x} - \frac{b^3}{9a^4(a+bx)^9} - \frac{b^3}{2a^5(a+bx)^8} - \frac{10b^3}{7a^6(a+bx)^7} - \frac{10b^3}{3a^7(a+bx)^6} - \frac{b^3}{2a^5(a+bx)^8} \end{aligned}$$

Mathematica [A] time = 0.12, size = 156, normalized size = 0.79

$$\frac{-27720b^3 \log(a + bx) + \frac{a(42a^{11} - 252a^{10}bx + 2772a^9b^2x^2 + 78419a^8b^3x^3 + 456291a^7b^4x^4 + 1326204a^6b^5x^5 + 2318316a^5b^6x^6 + 2604294a^4b^7x^7 + 1905750a^3b^8x^8 + 882420a^2b^9x^9 + 235620ab^{10}x^{10} + 27720b^{11}x^{11})}{x^3(a+bx)^9}}{126a^{13}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^4*(a + b*x)^10),x]

[Out] -1/126*((a*(42*a^11 - 252*a^10*b*x + 2772*a^9*b^2*x^2 + 78419*a^8*b^3*x^3 + 456291*a^7*b^4*x^4 + 1326204*a^6*b^5*x^5 + 2318316*a^5*b^6*x^6 + 2604294*a^4*b^7*x^7 + 1905750*a^3*b^8*x^8 + 882420*a^2*b^9*x^9 + 235620*a*b^10*x^10 + 27720*b^11*x^11))/(x^3*(a + b*x)^9) + 27720*b^3*Log[x] - 27720*b^3*Log[a + b*x])/a^13

fricas [B] time = 0.48, size = 449, normalized size = 2.27

$$\frac{27720 ab^{11}x^{11} + 235620 a^2b^{10}x^{10} + 882420 a^3b^9x^9 + 1905750 a^4b^8x^8 + 2604294 a^5b^7x^7 + 2318316 a^6b^6x^6 + 1905750 a^7b^5x^5 + 1326204 a^8b^4x^4 + 78419 a^9b^3x^3 + 2772 a^{10}b^2x^2 - 252 a^{11}bx + 42a^{12}}{a^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^10,x, algorithm="fricas")

[Out] -1/126*(27720*a*b^11*x^11 + 235620*a^2*b^10*x^10 + 882420*a^3*b^9*x^9 + 1905750*a^4*b^8*x^8 + 2604294*a^5*b^7*x^7 + 2318316*a^6*b^6*x^6 + 1326204*a^7*b^5*x^5 + 456291*a^8*b^4*x^4 + 78419*a^9*b^3*x^3 + 2772*a^10*b^2*x^2 - 252*a^11*b*x + 42*a^12 - 27720*(b^12*x^12 + 9*a*b^11*x^11 + 36*a^2*b^10*x^10 + 84*a^3*b^9*x^9 + 126*a^4*b^8*x^8 + 126*a^5*b^7*x^7 + 84*a^6*b^6*x^6 + 36*a^7*b^5*x^5 + 9*a^8*b^4*x^4 + a^9*b^3*x^3)*log(b*x + a) + 27720*(b^12*x^12 + 9*a*b^11*x^11 + 36*a^2*b^10*x^10 + 84*a^3*b^9*x^9 + 126*a^4*b^8*x^8 + 126*a^5*b^7*x^7 + 84*a^6*b^6*x^6 + 36*a^7*b^5*x^5 + 9*a^8*b^4*x^4 + a^9*b^3*x^3)*log(x))/(a^13*b^9*x^12 + 9*a^14*b^8*x^11 + 36*a^15*b^7*x^10 + 84*a^16*b^6*x^9 + 126*a^17*b^5*x^8 + 126*a^18*b^4*x^7 + 84*a^19*b^3*x^6 + 36*a^20*b^2*x^5 + 9*a^21*b*x^4 + a^22*x^3)

giac [A] time = 1.35, size = 163, normalized size = 0.82

$$\frac{220 b^3 \log(|bx + a|)}{a^{13}} - \frac{220 b^3 \log(|x|)}{a^{13}} - \frac{27720 ab^{11}x^{11} + 235620 a^2b^{10}x^{10} + 882420 a^3b^9x^9 + 1905750 a^4b^8x^8 + 2604294 a^5b^7x^7 + 2318316 a^6b^6x^6 + 1905750 a^7b^5x^5 + 1326204 a^8b^4x^4 + 78419 a^9b^3x^3 + 2772 a^{10}b^2x^2 - 252 a^{11}bx + 42a^{12}}{a^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^10,x, algorithm="giac")

[Out] $220*b^3*\log(\text{abs}(b*x + a))/a^{13} - 220*b^3*\log(\text{abs}(x))/a^{13} - 1/126*(27720*a*b^{11}*x^{11} + 235620*a^2*b^{10}*x^{10} + 882420*a^3*b^9*x^9 + 1905750*a^4*b^8*x^8 + 2604294*a^5*b^7*x^7 + 2318316*a^6*b^6*x^6 + 1326204*a^7*b^5*x^5 + 456291*a^8*b^4*x^4 + 78419*a^9*b^3*x^3 + 2772*a^{10}*b^2*x^2 - 252*a^{11}*b*x + 42*a^{12})/((b*x + a)^9*a^{13}*x^3)$

maple [A] time = 0.01, size = 189, normalized size = 0.95

$$\frac{b^3}{9(bx+a)^9 a^4} - \frac{b^3}{2(bx+a)^8 a^5} - \frac{10b^3}{7(bx+a)^7 a^6} - \frac{10b^3}{3(bx+a)^6 a^7} - \frac{7b^3}{(bx+a)^5 a^8} - \frac{14b^3}{(bx+a)^4 a^9} - \frac{28b^3}{(bx+a)^3 a^{10}} - \frac{60b^3}{(bx+a)^2 a^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/x^4/(b*x+a)^{10}, x)$

[Out] $-1/3/a^{10}/x^3+5*b/a^{11}/x^2-55*b^2/a^{12}/x-1/9*b^3/a^4/(b*x+a)^9-1/2*b^3/a^5/(b*x+a)^8-10/7*b^3/a^6/(b*x+a)^7-10/3*b^3/a^7/(b*x+a)^6-7*b^3/a^8/(b*x+a)^5-14*b^3/a^9/(b*x+a)^4-28*b^3/a^{10}/(b*x+a)^3-60*b^3/a^{11}/(b*x+a)^2-165*b^3/a^{12}/(b*x+a)-220*b^3*\ln(x)/a^{13}+220*b^3*\ln(b*x+a)/a^{13}$

maxima [A] time = 1.72, size = 251, normalized size = 1.27

$$\frac{27720 b^{11} x^{11} + 235620 a b^{10} x^{10} + 882420 a^2 b^9 x^9 + 1905750 a^3 b^8 x^8 + 2604294 a^4 b^7 x^7 + 2318316 a^5 b^6 x^6 + 1326204 a^6 b^5 x^5 + 456291 a^7 b^4 x^4 + 78419 a^8 b^3 x^3 + 2772 a^9 b^2 x^2 - 252 a^{10} b x + 42 a^{11}}{126 (a^{12} b^9 x^{12} + 9 a^{13} b^8 x^{11} + 36 a^{14} b^7 x^{10} + 84 a^{15} b^6 x^9 + 126 a^{16} b^5 x^8 + 126 a^{17} b^4 x^7 + 84 a^{18} b^3 x^6 + 36 a^{19} b^2 x^5 + 9 a^{20} b x^4 + a^{21} x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^4/(b*x+a)^{10}, x, \text{algorithm}="maxima")$

[Out] $-1/126*(27720*b^{11}*x^{11} + 235620*a*b^{10}*x^{10} + 882420*a^2*b^9*x^9 + 1905750*a^3*b^8*x^8 + 2604294*a^4*b^7*x^7 + 2318316*a^5*b^6*x^6 + 1326204*a^6*b^5*x^5 + 456291*a^7*b^4*x^4 + 78419*a^8*b^3*x^3 + 2772*a^9*b^2*x^2 - 252*a^{10}*b*x + 42*a^{11})/(a^{12}*b^9*x^{12} + 9*a^{13}*b^8*x^{11} + 36*a^{14}*b^7*x^{10} + 84*a^{15}*b^6*x^9 + 126*a^{16}*b^5*x^8 + 126*a^{17}*b^4*x^7 + 84*a^{18}*b^3*x^6 + 36*a^{19}*b^2*x^5 + 9*a^{20}*b*x^4 + a^{21}*x^3) + 220*b^3*\log(b*x + a)/a^{13} - 220*b^3*\log(x)/a^{13}$

mupad [B] time = 0.59, size = 245, normalized size = 1.24

$$\frac{440 b^3 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^{13}} - \frac{\frac{1}{3a} + \frac{22b^2x^2}{a^3} + \frac{78419b^3x^3}{126a^4} + \frac{50699b^4x^4}{14a^5} + \frac{73678b^5x^5}{7a^6} + \frac{55198b^6x^6}{3a^7} + \frac{20669b^7x^7}{a^8} + \frac{15125b^8x^8}{a^9} + \frac{2112b^9x^9}{a^{10}}}{a^9x^3 + 9a^8bx^4 + 36a^7b^2x^5 + 84a^6b^3x^6 + 126a^5b^4x^7 + 126a^4b^5x^8 + 84a^3b^6x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(x^4*(a + b*x)^{10}), x)$


```
[Out] (440*b^3*atanh((2*b*x)/a + 1))/a^13 - (1/(3*a) + (22*b^2*x^2)/a^3 + (78419*
b^3*x^3)/(126*a^4) + (50699*b^4*x^4)/(14*a^5) + (73678*b^5*x^5)/(7*a^6) + (
55198*b^6*x^6)/(3*a^7) + (20669*b^7*x^7)/a^8 + (15125*b^8*x^8)/a^9 + (21010
*b^9*x^9)/(3*a^10) + (1870*b^10*x^10)/a^11 + (220*b^11*x^11)/a^12 - (2*b*x)
/a^2)/(a^9*x^3 + b^9*x^12 + 9*a^8*b*x^4 + 9*a*b^8*x^11 + 36*a^7*b^2*x^5 + 8
4*a^6*b^3*x^6 + 126*a^5*b^4*x^7 + 126*a^4*b^5*x^8 + 84*a^3*b^6*x^9 + 36*a^2
*b^7*x^10)
```

sympy [A] time = 1.24, size = 258, normalized size = 1.30

$$\frac{-42a^{11} + 252a^{10}bx - 2772a^9b^2x^2 - 78419a^8b^3x^3 - 456291a^7b^4x^4 - 1326204a^6b^5x^5 - 2318316a^5b^6x^6 - 2604290a^4b^7x^7 - 1905750a^3b^8x^8 - 882420a^2b^9x^9 - 235620ab^{10}x^{10} - 27720b^{11}x^{11}}{126a^{21}x^3 + 1134a^{20}bx^4 + 4536a^{19}b^2x^5 + 10584a^{18}b^3x^6 + 15876a^{17}b^4x^7 + 15876a^{16}b^5x^8 + 10584a^{15}b^6x^9 + 4536a^{14}b^7x^{10} + 1134a^{13}b^8x^{11} + 126a^{12}b^9x^{12}} + 220b^3(-\log(x) + \log(a/b + x))/a^{13}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**4/(b*x+a)**10,x)
```

```
[Out] (-42*a**11 + 252*a**10*b*x - 2772*a**9*b**2*x**2 - 78419*a**8*b**3*x**3 - 4
56291*a**7*b**4*x**4 - 1326204*a**6*b**5*x**5 - 2318316*a**5*b**6*x**6 - 26
04294*a**4*b**7*x**7 - 1905750*a**3*b**8*x**8 - 882420*a**2*b**9*x**9 - 235
620*a*b**10*x**10 - 27720*b**11*x**11)/(126*a**21*x**3 + 1134*a**20*b*x**4
+ 4536*a**19*b**2*x**5 + 10584*a**18*b**3*x**6 + 15876*a**17*b**4*x**7 + 15
876*a**16*b**5*x**8 + 10584*a**15*b**6*x**9 + 4536*a**14*b**7*x**10 + 1134*
a**13*b**8*x**11 + 126*a**12*b**9*x**12) + 220*b**3*(-log(x) + log(a/b + x)
)/a**13
```

$$3.239 \quad \int \frac{(a+bx)^{12}}{x^{10}} dx$$

Optimal. Leaf size=141

$$\frac{a^{12}}{9x^9} - \frac{3a^{11}b}{2x^8} - \frac{66a^{10}b^2}{7x^7} - \frac{110a^9b^3}{3x^6} - \frac{99a^8b^4}{x^5} - \frac{198a^7b^5}{x^4} - \frac{308a^6b^6}{x^3} - \frac{396a^5b^7}{x^2} - \frac{495a^4b^8}{x} + 220a^3b^9 \log(x) + 66a^2b^{10}x + 6a$$

[Out] $-1/9*a^{12}/x^9 - 3/2*a^{11}*b/x^8 - 66/7*a^{10}*b^2/x^7 - 110/3*a^9*b^3/x^6 - 99*a^8*b^4/x^5 - 198*a^7*b^5/x^4 - 308*a^6*b^6/x^3 - 396*a^5*b^7/x^2 - 495*a^4*b^8/x + 66*a^2*b^{10}*x + 6*a^3*b^9*\ln(x)$

Rubi [A] time = 0.08, antiderivative size = 141, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{66a^{10}b^2}{7x^7} - \frac{110a^9b^3}{3x^6} - \frac{99a^8b^4}{x^5} - \frac{198a^7b^5}{x^4} - \frac{308a^6b^6}{x^3} - \frac{396a^5b^7}{x^2} - \frac{495a^4b^8}{x} + 66a^2b^{10}x + 220a^3b^9 \log(x) - \frac{3a^{11}b}{2x^8} - \frac{a^{12}}{9x^9} + 6a$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^12/x^10, x]

[Out] $-a^{12}/(9*x^9) - (3*a^{11}*b)/(2*x^8) - (66*a^{10}*b^2)/(7*x^7) - (110*a^9*b^3)/(3*x^6) - (99*a^8*b^4)/x^5 - (198*a^7*b^5)/x^4 - (308*a^6*b^6)/x^3 - (396*a^5*b^7)/x^2 - (495*a^4*b^8)/x + 66*a^2*b^{10}*x + 6*a*b^{11}*x^2 + (b^{12}*x^3)/3 + 220*a^3*b^9*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{12}}{x^{10}} dx = \int \left(66a^2b^{10} + \frac{a^{12}}{x^{10}} + \frac{12a^{11}b}{x^9} + \frac{66a^{10}b^2}{x^8} + \frac{220a^9b^3}{x^7} + \frac{495a^8b^4}{x^6} + \frac{792a^7b^5}{x^5} + \frac{924a^6b^6}{x^4} + \frac{792a^5b^7}{x^3} + \frac{495a^4b^8}{x^2} + \frac{198a^3b^9}{x} + 66a^2b^{10}x + 6a^3b^9 \log(x) \right) dx$$

Mathematica [A] time = 0.01, size = 141, normalized size = 1.00

$$\frac{a^{12}}{9x^9} - \frac{3a^{11}b}{2x^8} - \frac{66a^{10}b^2}{7x^7} - \frac{110a^9b^3}{3x^6} - \frac{99a^8b^4}{x^5} - \frac{198a^7b^5}{x^4} - \frac{308a^6b^6}{x^3} - \frac{396a^5b^7}{x^2} - \frac{495a^4b^8}{x} + 220a^3b^9 \log(x) + 66a^2b^{10}x + 6a$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^12/x^10,x]

[Out] $-1/9*a^{12}/x^9 - (3*a^{11}*b)/(2*x^8) - (66*a^{10}*b^2)/(7*x^7) - (110*a^9*b^3)/(3*x^6) - (99*a^8*b^4)/x^5 - (198*a^7*b^5)/x^4 - (308*a^6*b^6)/x^3 - (396*a^5*b^7)/x^2 - (495*a^4*b^8)/x + 66*a^2*b^{10}*x + 6*a*b^{11}*x^2 + (b^{12}*x^3)/3 + 220*a^3*b^9*\text{Log}[x]$

fricas [A] time = 0.48, size = 136, normalized size = 0.96

$$\frac{42 b^{12} x^{12} + 756 a b^{11} x^{11} + 8316 a^2 b^{10} x^{10} + 27720 a^3 b^9 x^9 \log(x) - 62370 a^4 b^8 x^8 - 49896 a^5 b^7 x^7 - 38808 a^6 b^6 x^6 - 24948 a^7 b^5 x^5 - 12474 a^8 b^4 x^4 - 4620 a^9 b^3 x^3 - 1188 a^{10} b^2 x^2 - 189 a^{11} b x - 14 a^{12}}{126 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^12/x^10,x, algorithm="fricas")

[Out] $1/126*(42*b^{12}*x^{12} + 756*a*b^{11}*x^{11} + 8316*a^2*b^{10}*x^{10} + 27720*a^3*b^9*x^9*\log(x) - 62370*a^4*b^8*x^8 - 49896*a^5*b^7*x^7 - 38808*a^6*b^6*x^6 - 24948*a^7*b^5*x^5 - 12474*a^8*b^4*x^4 - 4620*a^9*b^3*x^3 - 1188*a^{10}*b^2*x^2 - 189*a^{11}*b*x - 14*a^{12})/x^9$

giac [A] time = 1.14, size = 133, normalized size = 0.94

$$\frac{1}{3} b^{12} x^3 + 6 a b^{11} x^2 + 66 a^2 b^{10} x + 220 a^3 b^9 \log(|x|) - \frac{62370 a^4 b^8 x^8 + 49896 a^5 b^7 x^7 + 38808 a^6 b^6 x^6 + 24948 a^7 b^5 x^5 - 12474 a^8 b^4 x^4 - 4620 a^9 b^3 x^3 - 1188 a^{10} b^2 x^2 - 189 a^{11} b x - 14 a^{12}}{126 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^12/x^10,x, algorithm="giac")

[Out] $1/3*b^{12}*x^3 + 6*a*b^{11}*x^2 + 66*a^2*b^{10}*x + 220*a^3*b^9*\log(\text{abs}(x)) - 1/126*(62370*a^4*b^8*x^8 + 49896*a^5*b^7*x^7 + 38808*a^6*b^6*x^6 + 24948*a^7*b^5*x^5 + 12474*a^8*b^4*x^4 + 4620*a^9*b^3*x^3 + 1188*a^{10}*b^2*x^2 + 189*a^{11}*b*x + 14*a^{12})/x^9$

maple [A] time = 0.01, size = 132, normalized size = 0.94

$$\frac{b^{12} x^3}{3} + 6 a b^{11} x^2 + 220 a^3 b^9 \ln(x) + 66 a^2 b^{10} x - \frac{495 a^4 b^8}{x} - \frac{396 a^5 b^7}{x^2} - \frac{308 a^6 b^6}{x^3} - \frac{198 a^7 b^5}{x^4} - \frac{99 a^8 b^4}{x^5} - \frac{110 a^9 b^3}{3 x^6} - \frac{66 a^{10} b^2}{7 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^12/x^10,x)

[Out] $-1/9*a^{12}/x^9 - 3/2*a^{11}*b/x^8 - 66/7*a^{10}*b^2/x^7 - 110/3*a^9*b^3/x^6 - 99*a^8*b^4/x^5 - 198*a^7*b^5/x^4 - 308*a^6*b^6/x^3 - 396*a^5*b^7/x^2 - 495*a^4*b^8/x + 66*a^2*b^{10}*x + 6*a*b^{11}*x^2 + 1/3*b^{12}*x^3 + 220*a^3*b^9*\ln(x)$

maxima [A] time = 1.37, size = 132, normalized size = 0.94

$$\frac{1}{3} b^{12} x^3 + 6 a b^{11} x^2 + 66 a^2 b^{10} x + 220 a^3 b^9 \log(x) - \frac{62370 a^4 b^8 x^8 + 49896 a^5 b^7 x^7 + 38808 a^6 b^6 x^6 + 24948 a^7 b^5 x^5 + 12474 a^8 b^4 x^4 + 4620 a^9 b^3 x^3 + 1188 a^{10} b^2 x^2 + 189 a^{11} b x + 14 a^{12}}{126 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^12/x^10,x, algorithm="maxima")

[Out] 1/3*b^12*x^3 + 6*a*b^11*x^2 + 66*a^2*b^10*x + 220*a^3*b^9*log(x) - 1/126*(62370*a^4*b^8*x^8 + 49896*a^5*b^7*x^7 + 38808*a^6*b^6*x^6 + 24948*a^7*b^5*x^5 + 12474*a^8*b^4*x^4 + 4620*a^9*b^3*x^3 + 1188*a^10*b^2*x^2 + 189*a^11*b*x + 14*a^12)/x^9

mupad [B] time = 0.08, size = 132, normalized size = 0.94

$$\frac{b^{12} x^3}{3} - \frac{a^{12}}{9} + \frac{3 a^{11} b x}{2} + \frac{66 a^{10} b^2 x^2}{7} + \frac{110 a^9 b^3 x^3}{3} + 99 a^8 b^4 x^4 + 198 a^7 b^5 x^5 + 308 a^6 b^6 x^6 + 396 a^5 b^7 x^7 + 495 a^4 b^8 x^8 + \frac{12474 a^8 b^4 x^4 + 4620 a^9 b^3 x^3 + 1188 a^{10} b^2 x^2 + 189 a^{11} b x + 14 a^{12}}{126 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^12/x^10,x)

[Out] (b^12*x^3)/3 - (a^12/9 + (66*a^10*b^2*x^2)/7 + (110*a^9*b^3*x^3)/3 + 99*a^8*b^4*x^4 + 198*a^7*b^5*x^5 + 308*a^6*b^6*x^6 + 396*a^5*b^7*x^7 + 495*a^4*b^8*x^8 + (3*a^11*b*x)/2)/x^9 + 66*a^2*b^10*x + 6*a*b^11*x^2 + 220*a^3*b^9*log(x)

sympy [A] time = 0.91, size = 143, normalized size = 1.01

$$220 a^3 b^9 \log(x) + 66 a^2 b^{10} x + 6 a b^{11} x^2 + \frac{b^{12} x^3}{3} + \frac{-14 a^{12} - 189 a^{11} b x - 1188 a^{10} b^2 x^2 - 4620 a^9 b^3 x^3 - 12474 a^8 b^4 x^4 - 49896 a^7 b^5 x^5 - 38808 a^6 b^6 x^6 - 24948 a^5 b^7 x^7 - 12474 a^4 b^8 x^8 - 4620 a^3 b^9 x^9 - 1188 a^2 b^{10} x^2 - 189 a b^{11} x^2 - 14 a^{12}}{126 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**12/x**10,x)

[Out] 220*a**3*b**9*log(x) + 66*a**2*b**10*x + 6*a*b**11*x**2 + b**12*x**3/3 + (-14*a**12 - 189*a**11*b*x - 1188*a**10*b**2*x**2 - 4620*a**9*b**3*x**3 - 12474*a**8*b**4*x**4 - 49896*a**7*b**5*x**5 - 38808*a**6*b**6*x**6 - 24948*a**5*b**7*x**7 - 12474*a**4*b**8*x**8 - 4620*a**3*b**9*x**9 - 1188*a**2*b**10*x**2 - 189*a**11*b*x**2 - 14*a**12)/(126*x**9)

$$3.240 \quad \int \frac{(a+bx)^{11}}{x^{10}} dx$$

Optimal. Leaf size=132

$$\frac{a^{11}}{9x^9} - \frac{11a^{10}b}{8x^8} - \frac{55a^9b^2}{7x^7} - \frac{55a^8b^3}{2x^6} - \frac{66a^7b^4}{x^5} - \frac{231a^6b^5}{2x^4} - \frac{154a^5b^6}{x^3} - \frac{165a^4b^7}{x^2} - \frac{165a^3b^8}{x} + 55a^2b^9 \log(x) + 11ab^{10}x + \frac{b^{11}x}{2}$$

[Out] $-1/9*a^{11}/x^9-11/8*a^{10}*b/x^8-55/7*a^9*b^2/x^7-55/2*a^8*b^3/x^6-66*a^7*b^4/x^5-231/2*a^6*b^5/x^4-154*a^5*b^6/x^3-165*a^4*b^7/x^2-165*a^3*b^8/x+11*a*b^10*x+1/2*b^{11}*x^2+55*a^2*b^9*\ln(x)$

Rubi [A] time = 0.07, antiderivative size = 132, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{55a^9b^2}{7x^7} - \frac{55a^8b^3}{2x^6} - \frac{66a^7b^4}{x^5} - \frac{231a^6b^5}{2x^4} - \frac{154a^5b^6}{x^3} - \frac{165a^4b^7}{x^2} - \frac{165a^3b^8}{x} + 55a^2b^9 \log(x) - \frac{11a^{10}b}{8x^8} - \frac{a^{11}}{9x^9} + 11ab^{10}x + \frac{b^{11}x}{2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^11/x^10, x]

[Out] $-a^{11}/(9*x^9) - (11*a^{10}*b)/(8*x^8) - (55*a^9*b^2)/(7*x^7) - (55*a^8*b^3)/(2*x^6) - (66*a^7*b^4)/x^5 - (231*a^6*b^5)/(2*x^4) - (154*a^5*b^6)/x^3 - (165*a^4*b^7)/x^2 - (165*a^3*b^8)/x + 11*a*b^{10}*x + (b^{11}*x^2)/2 + 55*a^2*b^9*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{11}}{x^{10}} dx = \int \left(11ab^{10} + \frac{a^{11}}{x^{10}} + \frac{11a^{10}b}{x^9} + \frac{55a^9b^2}{x^8} + \frac{165a^8b^3}{x^7} + \frac{330a^7b^4}{x^6} + \frac{462a^6b^5}{x^5} + \frac{462a^5b^6}{x^4} + \frac{330a^4b^7}{x^3} + \frac{165a^3b^8}{x^2} + \frac{11ab^{10}x}{2} + \frac{b^{11}x^2}{2} \right) dx$$

Mathematica [A] time = 0.01, size = 132, normalized size = 1.00

$$\frac{a^{11}}{9x^9} - \frac{11a^{10}b}{8x^8} - \frac{55a^9b^2}{7x^7} - \frac{55a^8b^3}{2x^6} - \frac{66a^7b^4}{x^5} - \frac{231a^6b^5}{2x^4} - \frac{154a^5b^6}{x^3} - \frac{165a^4b^7}{x^2} - \frac{165a^3b^8}{x} + 55a^2b^9 \log(x) + 11ab^{10}x + \frac{b^{11}x}{2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^11/x^10, x]

[Out] $-1/9*a^{11}/x^9 - (11*a^{10}*b)/(8*x^8) - (55*a^9*b^2)/(7*x^7) - (55*a^8*b^3)/(2*x^6) - (66*a^7*b^4)/x^5 - (231*a^6*b^5)/(2*x^4) - (154*a^5*b^6)/x^3 - (165*a^4*b^7)/x^2 - (165*a^3*b^8)/x + 11*a*b^{10}*x + (b^{11}*x^2)/2 + 55*a^2*b^9*\text{Log}[x]$

fricas [A] time = 0.54, size = 125, normalized size = 0.95

$$\frac{252 b^{11} x^{11} + 5544 a b^{10} x^{10} + 27720 a^2 b^9 x^9 \log(x) - 83160 a^3 b^8 x^8 - 83160 a^4 b^7 x^7 - 77616 a^5 b^6 x^6 - 58212 a^6 b^5 x^5 - 3264 a^7 b^4 x^4 - 13860 a^8 b^3 x^3 - 3960 a^9 b^2 x^2 - 693 a^{10} b x - 56 a^{11}}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^11/x^10, x, algorithm="fricas")

[Out] $1/504*(252*b^{11}*x^{11} + 5544*a*b^{10}*x^{10} + 27720*a^2*b^9*x^9*\log(x) - 83160*a^3*b^8*x^8 - 83160*a^4*b^7*x^7 - 77616*a^5*b^6*x^6 - 58212*a^6*b^5*x^5 - 3264*a^7*b^4*x^4 - 13860*a^8*b^3*x^3 - 3960*a^9*b^2*x^2 - 693*a^{10}*b*x - 56*a^{11})/x^9$

giac [A] time = 1.28, size = 122, normalized size = 0.92

$$\frac{1}{2} b^{11} x^2 + 11 a b^{10} x + 55 a^2 b^9 \log(|x|) - \frac{83160 a^3 b^8 x^8 + 83160 a^4 b^7 x^7 + 77616 a^5 b^6 x^6 + 58212 a^6 b^5 x^5 + 33264 a^7 b^4 x^4 + 13860 a^8 b^3 x^3 + 3960 a^9 b^2 x^2 + 693 a^{10} b x + 56 a^{11}}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^11/x^10, x, algorithm="giac")

[Out] $1/2*b^{11}*x^2 + 11*a*b^{10}*x + 55*a^2*b^9*\log(\text{abs}(x)) - 1/504*(83160*a^3*b^8*x^8 + 83160*a^4*b^7*x^7 + 77616*a^5*b^6*x^6 + 58212*a^6*b^5*x^5 + 33264*a^7*b^4*x^4 + 13860*a^8*b^3*x^3 + 3960*a^9*b^2*x^2 + 693*a^{10}*b*x + 56*a^{11})/x^9$

maple [A] time = 0.01, size = 121, normalized size = 0.92

$$\frac{b^{11} x^2}{2} + 55 a^2 b^9 \ln(x) + 11 a b^{10} x - \frac{165 a^3 b^8}{x} - \frac{165 a^4 b^7}{x^2} - \frac{154 a^5 b^6}{x^3} - \frac{231 a^6 b^5}{2 x^4} - \frac{66 a^7 b^4}{x^5} - \frac{55 a^8 b^3}{2 x^6} - \frac{55 a^9 b^2}{7 x^7} - \frac{11 a^{10} b}{8 x^8} - \frac{a^{11}}{9 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^11/x^10, x)

[Out] $-1/9*a^{11}/x^9 - 11/8*a^{10}*b/x^8 - 55/7*a^9*b^2/x^7 - 55/2*a^8*b^3/x^6 - 66*a^7*b^4/x^5 - 231/2*a^6*b^5/x^4 - 154*a^5*b^6/x^3 - 165*a^4*b^7/x^2 - 165*a^3*b^8/x + 11*a*b^{10}*x + 1/2*b^{11}*x^2 + 55*a^2*b^9*\ln(x)$

maxima [A] time = 1.37, size = 121, normalized size = 0.92

$$\frac{1}{2} b^{11} x^2 + 11 a b^{10} x + 55 a^2 b^9 \log(x) - \frac{83160 a^3 b^8 x^8 + 83160 a^4 b^7 x^7 + 77616 a^5 b^6 x^6 + 58212 a^6 b^5 x^5 + 33264 a^7 b^4 x^4 + 13860 a^8 b^3 x^3 + 3960 a^9 b^2 x^2 + 693 a^{10} b x + 56 a^{11}}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^11/x^10,x, algorithm="maxima")

[Out] 1/2*b^11*x^2 + 11*a*b^10*x + 55*a^2*b^9*log(x) - 1/504*(83160*a^3*b^8*x^8 + 83160*a^4*b^7*x^7 + 77616*a^5*b^6*x^6 + 58212*a^6*b^5*x^5 + 33264*a^7*b^4*x^4 + 13860*a^8*b^3*x^3 + 3960*a^9*b^2*x^2 + 693*a^10*b*x + 56*a^11)/x^9

mupad [B] time = 0.09, size = 121, normalized size = 0.92

$$\frac{b^{11} x^2}{2} - \frac{a^{11}}{9} + \frac{11 a^{10} b x}{8} + \frac{55 a^9 b^2 x^2}{7} + \frac{55 a^8 b^3 x^3}{2} + 66 a^7 b^4 x^4 + \frac{231 a^6 b^5 x^5}{2} + 154 a^5 b^6 x^6 + 165 a^4 b^7 x^7 + 165 a^3 b^8 x^8 + \frac{56 a^{11}}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^11/x^10,x)

[Out] (b^11*x^2)/2 - (a^11/9 + (55*a^9*b^2*x^2)/7 + (55*a^8*b^3*x^3)/2 + 66*a^7*b^4*x^4 + (231*a^6*b^5*x^5)/2 + 154*a^5*b^6*x^6 + 165*a^4*b^7*x^7 + 165*a^3*b^8*x^8 + (11*a^10*b*x)/8)/x^9 + 55*a^2*b^9*log(x) + 11*a*b^10*x

sympy [A] time = 0.85, size = 131, normalized size = 0.99

$$55 a^2 b^9 \log(x) + 11 a b^{10} x + \frac{b^{11} x^2}{2} + \frac{-56 a^{11} - 693 a^{10} b x - 3960 a^9 b^2 x^2 - 13860 a^8 b^3 x^3 - 33264 a^7 b^4 x^4 - 58212 a^6 b^5 x^5 - 33264 a^5 b^6 x^6 - 77616 a^4 b^7 x^7 - 83160 a^3 b^8 x^8}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**11/x**10,x)

[Out] 55*a**2*b**9*log(x) + 11*a*b**10*x + b**11*x**2/2 + (-56*a**11 - 693*a**10*b*x - 3960*a**9*b**2*x**2 - 13860*a**8*b**3*x**3 - 33264*a**7*b**4*x**4 - 58212*a**6*b**5*x**5 - 77616*a**5*b**6*x**6 - 83160*a**4*b**7*x**7 - 83160*a**3*b**8*x**8)/(504*x**9)

$$3.241 \quad \int \frac{(a+bx)^{10}}{x^{10}} dx$$

Optimal. Leaf size=114

$$\frac{a^{10}}{9x^9} - \frac{5a^9b}{4x^8} - \frac{45a^8b^2}{7x^7} - \frac{20a^7b^3}{x^6} - \frac{42a^6b^4}{x^5} - \frac{63a^5b^5}{x^4} - \frac{70a^4b^6}{x^3} - \frac{60a^3b^7}{x^2} - \frac{45a^2b^8}{x} + 10ab^9 \log(x) + b^{10}x$$

[Out] $-1/9*a^{10}/x^9 - 5/4*a^9*b/x^8 - 45/7*a^8*b^2/x^7 - 20*a^7*b^3/x^6 - 42*a^6*b^4/x^5 - 63*a^5*b^5/x^4 - 70*a^4*b^6/x^3 - 60*a^3*b^7/x^2 - 45*a^2*b^8/x + b^{10}*x + 10*a*b^9*\ln(x)$

Rubi [A] time = 0.06, antiderivative size = 114, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{45a^8b^2}{7x^7} - \frac{20a^7b^3}{x^6} - \frac{42a^6b^4}{x^5} - \frac{63a^5b^5}{x^4} - \frac{70a^4b^6}{x^3} - \frac{60a^3b^7}{x^2} - \frac{45a^2b^8}{x} - \frac{5a^9b}{4x^8} - \frac{a^{10}}{9x^9} + 10ab^9 \log(x) + b^{10}x$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10/x^10,x]

[Out] $-a^{10}/(9*x^9) - (5*a^9*b)/(4*x^8) - (45*a^8*b^2)/(7*x^7) - (20*a^7*b^3)/x^6 - (42*a^6*b^4)/x^5 - (63*a^5*b^5)/x^4 - (70*a^4*b^6)/x^3 - (60*a^3*b^7)/x^2 - (45*a^2*b^8)/x + b^{10}*x + 10*a*b^9*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^{10}}{x^{10}} dx = \int \left(b^{10} + \frac{a^{10}}{x^{10}} + \frac{10a^9b}{x^9} + \frac{45a^8b^2}{x^8} + \frac{120a^7b^3}{x^7} + \frac{210a^6b^4}{x^6} + \frac{252a^5b^5}{x^5} + \frac{210a^4b^6}{x^4} + \frac{120a^3b^7}{x^3} + \frac{45a^2b^8}{x^2} + \frac{10ab^9}{x} + b^{10}x \right) dx$$

Mathematica [A] time = 0.01, size = 114, normalized size = 1.00

$$\frac{a^{10}}{9x^9} - \frac{5a^9b}{4x^8} - \frac{45a^8b^2}{7x^7} - \frac{20a^7b^3}{x^6} - \frac{42a^6b^4}{x^5} - \frac{63a^5b^5}{x^4} - \frac{70a^4b^6}{x^3} - \frac{60a^3b^7}{x^2} - \frac{45a^2b^8}{x} + 10ab^9 \log(x) + b^{10}x$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10/x^10,x]

[Out] $-1/9*a^{10}/x^9 - (5*a^9*b)/(4*x^8) - (45*a^8*b^2)/(7*x^7) - (20*a^7*b^3)/x^6 - (42*a^6*b^4)/x^5 - (63*a^5*b^5)/x^4 - (70*a^4*b^6)/x^3 - (60*a^3*b^7)/x^2 - (45*a^2*b^8)/x + b^{10}*x + 10*a*b^9*\text{Log}[x]$

fricas [A] time = 0.43, size = 114, normalized size = 1.00

$$\frac{252 b^{10} x^{10} + 2520 a b^9 x^9 \log(x) - 11340 a^2 b^8 x^8 - 15120 a^3 b^7 x^7 - 17640 a^4 b^6 x^6 - 15876 a^5 b^5 x^5 - 10584 a^6 b^4 x^4 - 5040 a^7 b^3 x^3 - 1620 a^8 b^2 x^2 - 315 a^9 b x - 28 a^{10}}{252 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^10,x, algorithm="fricas")

[Out] $1/252*(252*b^{10}*x^{10} + 2520*a*b^9*x^9*\log(x) - 11340*a^2*b^8*x^8 - 15120*a^3*b^7*x^7 - 17640*a^4*b^6*x^6 - 15876*a^5*b^5*x^5 - 10584*a^6*b^4*x^4 - 5040*a^7*b^3*x^3 - 1620*a^8*b^2*x^2 - 315*a^9*b*x - 28*a^{10})/x^9$

giac [A] time = 1.06, size = 110, normalized size = 0.96

$$b^{10}x+10ab^9\log(|x|)-\frac{11340a^2b^8x^8+15120a^3b^7x^7+17640a^4b^6x^6+15876a^5b^5x^5+10584a^6b^4x^4+5040a^7b^3x^3+1620a^8b^2x^2+315a^9bx-28a^{10}}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^10,x, algorithm="giac")

[Out] $b^{10}*x + 10*a*b^9*\log(\text{abs}(x)) - 1/252*(11340*a^2*b^8*x^8 + 15120*a^3*b^7*x^7 + 17640*a^4*b^6*x^6 + 15876*a^5*b^5*x^5 + 10584*a^6*b^4*x^4 + 5040*a^7*b^3*x^3 + 1620*a^8*b^2*x^2 + 315*a^9*b*x + 28*a^{10})/x^9$

maple [A] time = 0.00, size = 109, normalized size = 0.96

$$10ab^9\ln(x)+b^{10}x-\frac{45a^2b^8}{x}-\frac{60a^3b^7}{x^2}-\frac{70a^4b^6}{x^3}-\frac{63a^5b^5}{x^4}-\frac{42a^6b^4}{x^5}-\frac{20a^7b^3}{x^6}-\frac{45a^8b^2}{7x^7}-\frac{5a^9b}{4x^8}-\frac{a^{10}}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^10/x^10,x)

[Out] $10*a*b^9*\ln(x)+b^{10}*x-45*a^2*b^8/x-60*a^3*b^7/x^2-70*a^4*b^6/x^3-63*a^5*b^5/x^4-42*a^6*b^4/x^5-20*a^7*b^3/x^6-45/7*a^8*b^2/x^7-5/4*a^9*b/x^8-1/9*a^{10}/x^9$

maxima [A] time = 1.43, size = 109, normalized size = 0.96

$$b^{10}x + 10ab^9 \log(x) - \frac{11340a^2b^8x^8 + 15120a^3b^7x^7 + 17640a^4b^6x^6 + 15876a^5b^5x^5 + 10584a^6b^4x^4 + 5040a^7b^3x^3 + 1620a^8b^2x^2 + 315a^9bx + 28a^{10}}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10/x^10,x, algorithm="maxima")

[Out] b^10*x + 10*a*b^9*log(x) - 1/252*(11340*a^2*b^8*x^8 + 15120*a^3*b^7*x^7 + 17640*a^4*b^6*x^6 + 15876*a^5*b^5*x^5 + 10584*a^6*b^4*x^4 + 5040*a^7*b^3*x^3 + 1620*a^8*b^2*x^2 + 315*a^9*b*x + 28*a^10)/x^9

mupad [B] time = 0.00, size = 114, normalized size = 1.00

$$\frac{\frac{a^{10}}{9} - b^{10}x^{10} + \frac{45a^8b^2x^2}{7} + 20a^7b^3x^3 + 42a^6b^4x^4 + 63a^5b^5x^5 + 70a^4b^6x^6 + 60a^3b^7x^7 + 45a^2b^8x^8 + \frac{5a^9bx}{4}}{x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^10/x^10,x)

[Out] -(a^10/9 - b^10*x^10 + (45*a^8*b^2*x^2)/7 + 20*a^7*b^3*x^3 + 42*a^6*b^4*x^4 + 63*a^5*b^5*x^5 + 70*a^4*b^6*x^6 + 60*a^3*b^7*x^7 + 45*a^2*b^8*x^8 + (5*a^9*b*x)/4 - 10*a*b^9*x^9*log(x))/x^9

sympy [A] time = 0.86, size = 117, normalized size = 1.03

$$10ab^9 \log(x) + b^{10}x + \frac{-28a^{10} - 315a^9bx - 1620a^8b^2x^2 - 5040a^7b^3x^3 - 10584a^6b^4x^4 - 15876a^5b^5x^5 - 17640a^4b^6x^6 - 15120a^3b^7x^7 - 11340a^2b^8x^8}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10/x**10,x)

[Out] 10*a*b**9*log(x) + b**10*x + (-28*a**10 - 315*a**9*b*x - 1620*a**8*b**2*x**2 - 5040*a**7*b**3*x**3 - 10584*a**6*b**4*x**4 - 15876*a**5*b**5*x**5 - 17640*a**4*b**6*x**6 - 15120*a**3*b**7*x**7 - 11340*a**2*b**8*x**8)/(252*x**9)

$$3.242 \quad \int \frac{(a+bx)^9}{x^{10}} dx$$

Optimal. Leaf size=109

$$\frac{a^9}{9x^9} - \frac{9a^8b}{8x^8} - \frac{36a^7b^2}{7x^7} - \frac{14a^6b^3}{x^6} - \frac{126a^5b^4}{5x^5} - \frac{63a^4b^5}{2x^4} - \frac{28a^3b^6}{x^3} - \frac{18a^2b^7}{x^2} - \frac{9ab^8}{x} + b^9 \log(x)$$

[Out] $-1/9*a^9/x^9-9/8*a^8*b/x^8-36/7*a^7*b^2/x^7-14*a^6*b^3/x^6-126/5*a^5*b^4/x^5-63/2*a^4*b^5/x^4-28*a^3*b^6/x^3-18*a^2*b^7/x^2-9*a*b^8/x+b^9*\ln(x)$

Rubi [A] time = 0.05, antiderivative size = 109, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{36a^7b^2}{7x^7} - \frac{14a^6b^3}{x^6} - \frac{126a^5b^4}{5x^5} - \frac{63a^4b^5}{2x^4} - \frac{28a^3b^6}{x^3} - \frac{18a^2b^7}{x^2} - \frac{9a^8b}{8x^8} - \frac{a^9}{9x^9} - \frac{9ab^8}{x} + b^9 \log(x)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^9/x^10, x]

[Out] $-a^9/(9*x^9) - (9*a^8*b)/(8*x^8) - (36*a^7*b^2)/(7*x^7) - (14*a^6*b^3)/x^6 - (126*a^5*b^4)/(5*x^5) - (63*a^4*b^5)/(2*x^4) - (28*a^3*b^6)/x^3 - (18*a^2*b^7)/x^2 - (9*a*b^8)/x + b^9*\text{Log}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^9}{x^{10}} dx &= \int \left(\frac{a^9}{x^{10}} + \frac{9a^8b}{x^9} + \frac{36a^7b^2}{x^8} + \frac{84a^6b^3}{x^7} + \frac{126a^5b^4}{x^6} + \frac{126a^4b^5}{x^5} + \frac{84a^3b^6}{x^4} + \frac{36a^2b^7}{x^3} + \frac{9ab^8}{x^2} + \frac{b^9}{x} \right) dx \\ &= \frac{a^9}{9x^9} - \frac{9a^8b}{8x^8} - \frac{36a^7b^2}{7x^7} - \frac{14a^6b^3}{x^6} - \frac{126a^5b^4}{5x^5} - \frac{63a^4b^5}{2x^4} - \frac{28a^3b^6}{x^3} - \frac{18a^2b^7}{x^2} - \frac{9ab^8}{x} + b^9 \log(x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 109, normalized size = 1.00

$$\frac{a^9}{9x^9} - \frac{9a^8b}{8x^8} - \frac{36a^7b^2}{7x^7} - \frac{14a^6b^3}{x^6} - \frac{126a^5b^4}{5x^5} - \frac{63a^4b^5}{2x^4} - \frac{28a^3b^6}{x^3} - \frac{18a^2b^7}{x^2} - \frac{9ab^8}{x} + b^9 \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^9/x^10,x]

[Out] $-1/9*a^9/x^9 - (9*a^8*b)/(8*x^8) - (36*a^7*b^2)/(7*x^7) - (14*a^6*b^3)/x^6 - (126*a^5*b^4)/(5*x^5) - (63*a^4*b^5)/(2*x^4) - (28*a^3*b^6)/x^3 - (18*a^2*b^7)/x^2 - (9*a*b^8)/x + b^9*\text{Log}[x]$

fricas [A] time = 0.46, size = 103, normalized size = 0.94

$$\frac{2520 b^9 x^9 \log(x) - 22680 a b^8 x^8 - 45360 a^2 b^7 x^7 - 70560 a^3 b^6 x^6 - 79380 a^4 b^5 x^5 - 63504 a^5 b^4 x^4 - 35280 a^6 b^3 x^3 - 12960 a^7 b^2 x^2 - 2835 a^8 b x - 280 a^9}{2520 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^9/x^10,x, algorithm="fricas")

[Out] $1/2520*(2520*b^9*x^9*\log(x) - 22680*a*b^8*x^8 - 45360*a^2*b^7*x^7 - 70560*a^3*b^6*x^6 - 79380*a^4*b^5*x^5 - 63504*a^5*b^4*x^4 - 35280*a^6*b^3*x^3 - 12960*a^7*b^2*x^2 - 2835*a^8*b*x - 280*a^9)/x^9$

giac [A] time = 1.04, size = 101, normalized size = 0.93

$$b^9 \log(|x|) - \frac{22680 a b^8 x^8 + 45360 a^2 b^7 x^7 + 70560 a^3 b^6 x^6 + 79380 a^4 b^5 x^5 + 63504 a^5 b^4 x^4 + 35280 a^6 b^3 x^3 + 12960 a^7 b^2 x^2 + 2835 a^8 b x + 280 a^9}{2520 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^9/x^10,x, algorithm="giac")

[Out] $b^9*\log(\text{abs}(x)) - 1/2520*(22680*a*b^8*x^8 + 45360*a^2*b^7*x^7 + 70560*a^3*b^6*x^6 + 79380*a^4*b^5*x^5 + 63504*a^5*b^4*x^4 + 35280*a^6*b^3*x^3 + 12960*a^7*b^2*x^2 + 2835*a^8*b*x + 280*a^9)/x^9$

maple [A] time = 0.01, size = 100, normalized size = 0.92

$$b^9 \ln(x) - \frac{9 a b^8}{x} - \frac{18 a^2 b^7}{x^2} - \frac{28 a^3 b^6}{x^3} - \frac{63 a^4 b^5}{2 x^4} - \frac{126 a^5 b^4}{5 x^5} - \frac{14 a^6 b^3}{x^6} - \frac{36 a^7 b^2}{7 x^7} - \frac{9 a^8 b}{8 x^8} - \frac{a^9}{9 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^9/x^10,x)

[Out] $-1/9*a^9/x^9 - 9/8*a^8*b/x^8 - 36/7*a^7*b^2/x^7 - 14*a^6*b^3/x^6 - 126/5*a^5*b^4/x^5 - 63/2*a^4*b^5/x^4 - 28*a^3*b^6/x^3 - 18*a^2*b^7/x^2 - 9*a*b^8/x + b^9*\ln(x)$

maxima [A] time = 1.34, size = 100, normalized size = 0.92

$$b^9 \log(x) - \frac{22680 a b^8 x^8 + 45360 a^2 b^7 x^7 + 70560 a^3 b^6 x^6 + 79380 a^4 b^5 x^5 + 63504 a^5 b^4 x^4 + 35280 a^6 b^3 x^3 + 12960 a^7 b^2 x^2 + 2835 a^8 b x + 280 a^9}{2520 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^9/x^10,x, algorithm="maxima")

[Out] $b^9 \log(x) - \frac{1}{2520} (22680 a^8 b x^8 + 45360 a^7 b^2 x^7 + 70560 a^6 b^3 x^6 + 79380 a^5 b^4 x^5 + 63504 a^4 b^5 x^4 + 35280 a^3 b^6 x^3 + 12960 a^2 b^7 x^2 + 2835 a b^8 x + 280 a^9) / x^9$

mupad [B] time = 0.08, size = 100, normalized size = 0.92

$$b^9 \ln(x) - \frac{\frac{a^9}{9} + \frac{9a^8bx}{8} + \frac{36a^7b^2x^2}{7} + 14a^6b^3x^3 + \frac{126a^5b^4x^4}{5} + \frac{63a^4b^5x^5}{2} + 28a^3b^6x^6 + 18a^2b^7x^7 + 9ab^8x^8 + 280a^9}{x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^9/x^10,x)

[Out] $b^9 \log(x) - \frac{(a^9/9 + 9a^8bx^8 + (36a^7b^2x^2)/7 + 14a^6b^3x^3 + (126a^5b^4x^4)/5 + (63a^4b^5x^5)/2 + 28a^3b^6x^6 + 18a^2b^7x^7 + (9a^8bx)/8)}{x^9}$

sympy [A] time = 0.79, size = 107, normalized size = 0.98

$$b^9 \log(x) + \frac{-280a^9 - 2835a^8bx - 12960a^7b^2x^2 - 35280a^6b^3x^3 - 63504a^5b^4x^4 - 79380a^4b^5x^5 - 70560a^3b^6x^6 - 45360a^2b^7x^7 - 22680ab^8x^8 - 280a^9}{2520x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**9/x**10,x)

[Out] $b^{**9} \log(x) + \frac{(-280 a^{**9} - 2835 a^{**8} b x - 12960 a^{**7} b^{**2} x^{**2} - 35280 a^{**6} b^{**3} x^{**3} - 63504 a^{**5} b^{**4} x^{**4} - 79380 a^{**4} b^{**5} x^{**5} - 70560 a^{**3} b^{**6} x^{**6} - 45360 a^{**2} b^{**7} x^{**7} - 22680 a b^{**8} x^{**8})}{(2520 x^{**9})}$

$$3.243 \quad \int \frac{(a+bx)^8}{x^{10}} dx$$

Optimal. Leaf size=17

$$-\frac{(a+bx)^9}{9ax^9}$$

[Out] -1/9*(b*x+a)^9/a/x^9

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {37}

$$-\frac{(a+bx)^9}{9ax^9}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^8/x^10, x]

[Out] -(a + b*x)^9/(9*a*x^9)

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(a+bx)^8}{x^{10}} dx = -\frac{(a+bx)^9}{9ax^9}$$

Mathematica [B] time = 0.01, size = 96, normalized size = 5.65

$$-\frac{a^8}{9x^9} - \frac{a^7b}{x^8} - \frac{4a^6b^2}{x^7} - \frac{28a^5b^3}{3x^6} - \frac{14a^4b^4}{x^5} - \frac{14a^3b^5}{x^4} - \frac{28a^2b^6}{3x^3} - \frac{4ab^7}{x^2} - \frac{b^8}{x}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^8/x^10, x]

[Out] -1/9*a^8/x^9 - (a^7*b)/x^8 - (4*a^6*b^2)/x^7 - (28*a^5*b^3)/(3*x^6) - (14*a^4*b^4)/x^5 - (14*a^3*b^5)/x^4 - (28*a^2*b^6)/(3*x^3) - (4*a*b^7)/x^2 - b^8/x

fricas [B] time = 0.53, size = 88, normalized size = 5.18

$$\frac{9b^8x^8 + 36ab^7x^7 + 84a^2b^6x^6 + 126a^3b^5x^5 + 126a^4b^4x^4 + 84a^5b^3x^3 + 36a^6b^2x^2 + 9a^7bx + a^8}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8/x^10,x, algorithm="fricas")

[Out] $-1/9*(9*b^8*x^8 + 36*a*b^7*x^7 + 84*a^2*b^6*x^6 + 126*a^3*b^5*x^5 + 126*a^4*b^4*x^4 + 84*a^5*b^3*x^3 + 36*a^6*b^2*x^2 + 9*a^7*b*x + a^8)/x^9$

giac [B] time = 1.17, size = 88, normalized size = 5.18

$$\frac{9b^8x^8 + 36ab^7x^7 + 84a^2b^6x^6 + 126a^3b^5x^5 + 126a^4b^4x^4 + 84a^5b^3x^3 + 36a^6b^2x^2 + 9a^7bx + a^8}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8/x^10,x, algorithm="giac")

[Out] $-1/9*(9*b^8*x^8 + 36*a*b^7*x^7 + 84*a^2*b^6*x^6 + 126*a^3*b^5*x^5 + 126*a^4*b^4*x^4 + 84*a^5*b^3*x^3 + 36*a^6*b^2*x^2 + 9*a^7*b*x + a^8)/x^9$

maple [B] time = 0.01, size = 91, normalized size = 5.35

$$\frac{b^8}{x} - \frac{4ab^7}{x^2} - \frac{28a^2b^6}{3x^3} - \frac{14a^3b^5}{x^4} - \frac{14a^4b^4}{x^5} - \frac{28a^5b^3}{3x^6} - \frac{4a^6b^2}{x^7} - \frac{a^7b}{x^8} - \frac{a^8}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^8/x^10,x)

[Out] $-28/3*a^2*b^6/x^3 - b^8/x - 4*a*b^7/x^2 - 14*a^4*b^4/x^5 - 1/9*a^8/x^9 - a^7*b/x^8 - 28/3*a^5*b^3/x^6 - 14*a^3*b^5/x^4 - 4*a^6*b^2/x^7$

maxima [B] time = 1.34, size = 88, normalized size = 5.18

$$\frac{9b^8x^8 + 36ab^7x^7 + 84a^2b^6x^6 + 126a^3b^5x^5 + 126a^4b^4x^4 + 84a^5b^3x^3 + 36a^6b^2x^2 + 9a^7bx + a^8}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8/x^10,x, algorithm="maxima")

[Out] $-1/9*(9*b^8*x^8 + 36*a*b^7*x^7 + 84*a^2*b^6*x^6 + 126*a^3*b^5*x^5 + 126*a^4*b^4*x^4 + 84*a^5*b^3*x^3 + 36*a^6*b^2*x^2 + 9*a^7*b*x + a^8)/x^9$

mupad [B] time = 0.09, size = 88, normalized size = 5.18

$$\frac{\frac{a^8}{9} + a^7 b x + 4 a^6 b^2 x^2 + \frac{28 a^5 b^3 x^3}{3} + 14 a^4 b^4 x^4 + 14 a^3 b^5 x^5 + \frac{28 a^2 b^6 x^6}{3} + 4 a b^7 x^7 + b^8 x^8}{x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^8/x^10,x)

[Out] $-(a^8/9 + b^8*x^8 + 4*a*b^7*x^7 + 4*a^6*b^2*x^2 + (28*a^5*b^3*x^3)/3 + 14*a^4*b^4*x^4 + 14*a^3*b^5*x^5 + (28*a^2*b^6*x^6)/3 + a^7*b*x)/x^9$

sympy [B] time = 0.73, size = 95, normalized size = 5.59

$$\frac{-a^8 - 9a^7bx - 36a^6b^2x^2 - 84a^5b^3x^3 - 126a^4b^4x^4 - 126a^3b^5x^5 - 84a^2b^6x^6 - 36ab^7x^7 - 9b^8x^8}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**8/x**10,x)

[Out] $(-a**8 - 9*a**7*b*x - 36*a**6*b**2*x**2 - 84*a**5*b**3*x**3 - 126*a**4*b**4*x**4 - 126*a**3*b**5*x**5 - 84*a**2*b**6*x**6 - 36*a*b**7*x**7 - 9*b**8*x**8)/(9*x**9)$

$$3.244 \quad \int \frac{(a+bx)^7}{x^{10}} dx$$

Optimal. Leaf size=36

$$\frac{b(a+bx)^8}{72a^2x^8} - \frac{(a+bx)^8}{9ax^9}$$

[Out] $-1/9*(b*x+a)^8/a/x^9+1/72*b*(b*x+a)^8/a^2/x^8$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$\frac{b(a+bx)^8}{72a^2x^8} - \frac{(a+bx)^8}{9ax^9}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/x^10, x]

[Out] $-(a + b*x)^8/(9*a*x^9) + (b*(a + b*x)^8)/(72*a^2*x^8)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^7}{x^{10}} dx &= -\frac{(a+bx)^8}{9ax^9} - \frac{b \int \frac{(a+bx)^7}{x^9} dx}{9a} \\ &= -\frac{(a+bx)^8}{9ax^9} + \frac{b(a+bx)^8}{72a^2x^8} \end{aligned}$$

Mathematica [B] time = 0.00, size = 91, normalized size = 2.53

$$-\frac{a^7}{9x^9} - \frac{7a^6b}{8x^8} - \frac{3a^5b^2}{x^7} - \frac{35a^4b^3}{6x^6} - \frac{7a^3b^4}{x^5} - \frac{21a^2b^5}{4x^4} - \frac{7ab^6}{3x^3} - \frac{b^7}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/x^10,x]

[Out] $-\frac{1}{9}a^7/x^9 - \frac{7a^6b}{8x^8} - \frac{3a^5b^2}{x^7} - \frac{35a^4b^3}{6x^6} - \frac{7a^3b^4}{x^5} - \frac{21a^2b^5}{4x^4} - \frac{7ab^6}{3x^3} - \frac{b^7}{2x^2}$

fricas [B] time = 0.45, size = 79, normalized size = 2.19

$$\frac{36b^7x^7 + 168ab^6x^6 + 378a^2b^5x^5 + 504a^3b^4x^4 + 420a^4b^3x^3 + 216a^5b^2x^2 + 63a^6bx + 8a^7}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^10,x, algorithm="fricas")

[Out] $-\frac{1}{72}(36b^7x^7 + 168a^6b^6x^6 + 378a^5b^5x^5 + 504a^4b^4x^4 + 420a^3b^3x^3 + 216a^2b^2x^2 + 63a^6b^6x + 8a^7)/x^9$

giac [B] time = 1.04, size = 79, normalized size = 2.19

$$\frac{36b^7x^7 + 168ab^6x^6 + 378a^2b^5x^5 + 504a^3b^4x^4 + 420a^4b^3x^3 + 216a^5b^2x^2 + 63a^6bx + 8a^7}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^10,x, algorithm="giac")

[Out] $-\frac{1}{72}(36b^7x^7 + 168a^6b^6x^6 + 378a^5b^5x^5 + 504a^4b^4x^4 + 420a^3b^3x^3 + 216a^2b^2x^2 + 63a^6b^6x + 8a^7)/x^9$

maple [B] time = 0.00, size = 80, normalized size = 2.22

$$-\frac{b^7}{2x^2} - \frac{7ab^6}{3x^3} - \frac{21a^2b^5}{4x^4} - \frac{7a^3b^4}{x^5} - \frac{35a^4b^3}{6x^6} - \frac{3a^5b^2}{x^7} - \frac{7a^6b}{8x^8} - \frac{a^7}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/x^10,x)

[Out] $-\frac{1}{2}b^7/x^2 - \frac{7}{3}a^6b^6/x^3 - \frac{21}{4}a^5b^5/x^4 - \frac{7}{1}a^4b^4/x^5 - \frac{35}{6}a^3b^3/x^6 - \frac{7}{8}a^2b^2/x^7 - \frac{7}{8}a^6b^6/x^8 - \frac{1}{9}a^7/x^9$

maxima [B] time = 1.36, size = 79, normalized size = 2.19

$$\frac{36 b^7 x^7 + 168 a b^6 x^6 + 378 a^2 b^5 x^5 + 504 a^3 b^4 x^4 + 420 a^4 b^3 x^3 + 216 a^5 b^2 x^2 + 63 a^6 b x + 8 a^7}{72 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/x^10,x, algorithm="maxima")

[Out] $-1/72*(36*b^7*x^7 + 168*a*b^6*x^6 + 378*a^2*b^5*x^5 + 504*a^3*b^4*x^4 + 420*a^4*b^3*x^3 + 216*a^5*b^2*x^2 + 63*a^6*b*x + 8*a^7)/x^9$

mupad [B] time = 0.00, size = 23, normalized size = 0.64

$$\frac{(8a - bx)(a + bx)^8}{72a^2x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7/x^10,x)

[Out] $-((8*a - b*x)*(a + b*x)^8)/(72*a^2*x^9)$

sympy [B] time = 0.70, size = 85, normalized size = 2.36

$$\frac{-8a^7 - 63a^6bx - 216a^5b^2x^2 - 420a^4b^3x^3 - 504a^3b^4x^4 - 378a^2b^5x^5 - 168ab^6x^6 - 36b^7x^7}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7/x**10,x)

[Out] $(-8*a**7 - 63*a**6*b*x - 216*a**5*b**2*x**2 - 420*a**4*b**3*x**3 - 504*a**3*b**4*x**4 - 378*a**2*b**5*x**5 - 168*a*b**6*x**6 - 36*b**7*x**7)/(72*x**9)$

$$3.245 \quad \int \frac{(a+bx)^6}{x^{10}} dx$$

Optimal. Leaf size=56

$$-\frac{b^2(a+bx)^7}{252a^3x^7} + \frac{b(a+bx)^7}{36a^2x^8} - \frac{(a+bx)^7}{9ax^9}$$

[Out] $-1/9*(b*x+a)^7/a/x^9+1/36*b*(b*x+a)^7/a^2/x^8-1/252*b^2*(b*x+a)^7/a^3/x^7$

Rubi [A] time = 0.01, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {45, 37}

$$-\frac{b^2(a+bx)^7}{252a^3x^7} + \frac{b(a+bx)^7}{36a^2x^8} - \frac{(a+bx)^7}{9ax^9}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^6/x^10, x]

[Out] $-(a + b*x)^7/(9*a*x^9) + (b*(a + b*x)^7)/(36*a^2*x^8) - (b^2*(a + b*x)^7)/(252*a^3*x^7)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^6}{x^{10}} dx &= -\frac{(a+bx)^7}{9ax^9} - \frac{(2b) \int \frac{(a+bx)^6}{x^9} dx}{9a} \\
&= -\frac{(a+bx)^7}{9ax^9} + \frac{b(a+bx)^7}{36a^2x^8} + \frac{b^2 \int \frac{(a+bx)^6}{x^8} dx}{36a^2} \\
&= -\frac{(a+bx)^7}{9ax^9} + \frac{b(a+bx)^7}{36a^2x^8} - \frac{b^2(a+bx)^7}{252a^3x^7}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 80, normalized size = 1.43

$$\frac{a^6}{9x^9} - \frac{3a^5b}{4x^8} - \frac{15a^4b^2}{7x^7} - \frac{10a^3b^3}{3x^6} - \frac{3a^2b^4}{x^5} - \frac{3ab^5}{2x^4} - \frac{b^6}{3x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^6/x^10,x]

[Out] -1/9*a^6/x^9 - (3*a^5*b)/(4*x^8) - (15*a^4*b^2)/(7*x^7) - (10*a^3*b^3)/(3*x^6) - (3*a^2*b^4)/x^5 - (3*a*b^5)/(2*x^4) - b^6/(3*x^3)

fricas [A] time = 0.43, size = 68, normalized size = 1.21

$$\frac{84b^6x^6 + 378ab^5x^5 + 756a^2b^4x^4 + 840a^3b^3x^3 + 540a^4b^2x^2 + 189a^5bx + 28a^6}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6/x^10,x, algorithm="fricas")

[Out] -1/252*(84*b^6*x^6 + 378*a*b^5*x^5 + 756*a^2*b^4*x^4 + 840*a^3*b^3*x^3 + 540*a^4*b^2*x^2 + 189*a^5*b*x + 28*a^6)/x^9

giac [A] time = 1.02, size = 68, normalized size = 1.21

$$\frac{84b^6x^6 + 378ab^5x^5 + 756a^2b^4x^4 + 840a^3b^3x^3 + 540a^4b^2x^2 + 189a^5bx + 28a^6}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6/x^10,x, algorithm="giac")

[Out] -1/252*(84*b^6*x^6 + 378*a*b^5*x^5 + 756*a^2*b^4*x^4 + 840*a^3*b^3*x^3 + 540*a^4*b^2*x^2 + 189*a^5*b*x + 28*a^6)/x^9

maple [A] time = 0.01, size = 69, normalized size = 1.23

$$-\frac{b^6}{3x^3} - \frac{3ab^5}{2x^4} - \frac{3a^2b^4}{x^5} - \frac{10a^3b^3}{3x^6} - \frac{15a^4b^2}{7x^7} - \frac{3a^5b}{4x^8} - \frac{a^6}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^6/x^10,x)`

[Out] $-1/3*b^6/x^3-3*a^2*b^4/x^5-15/7*a^4*b^2/x^7-1/9*a^6/x^9-3/4*a^5*b/x^8-10/3*a^3*b^3/x^6-3/2*a*b^5/x^4$

maxima [A] time = 1.37, size = 68, normalized size = 1.21

$$-\frac{84b^6x^6 + 378ab^5x^5 + 756a^2b^4x^4 + 840a^3b^3x^3 + 540a^4b^2x^2 + 189a^5bx + 28a^6}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^6/x^10,x, algorithm="maxima")`

[Out] $-1/252*(84*b^6*x^6 + 378*a*b^5*x^5 + 756*a^2*b^4*x^4 + 840*a^3*b^3*x^3 + 540*a^4*b^2*x^2 + 189*a^5*b*x + 28*a^6)/x^9$

mupad [B] time = 0.10, size = 68, normalized size = 1.21

$$\frac{\frac{a^6}{9} + \frac{3a^5bx}{4} + \frac{15a^4b^2x^2}{7} + \frac{10a^3b^3x^3}{3} + 3a^2b^4x^4 + \frac{3ab^5x^5}{2} + \frac{b^6x^6}{3}}{x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^6/x^10,x)`

[Out] $-(a^6/9 + (b^6*x^6)/3 + (3*a*b^5*x^5)/2 + (15*a^4*b^2*x^2)/7 + (10*a^3*b^3*x^3)/3 + 3*a^2*b^4*x^4 + (3*a^5*b*x)/4)/x^9$

sympy [A] time = 0.56, size = 73, normalized size = 1.30

$$-\frac{28a^6 - 189a^5bx - 540a^4b^2x^2 - 840a^3b^3x^3 - 756a^2b^4x^4 - 378ab^5x^5 - 84b^6x^6}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**6/x**10,x)`

[Out] $(-28*a**6 - 189*a**5*b*x - 540*a**4*b**2*x**2 - 840*a**3*b**3*x**3 - 756*a**2*b**4*x**4 - 378*a*b**5*x**5 - 84*b**6*x**6)/(252*x**9)$

$$3.246 \quad \int \frac{(a+bx)^5}{x^{10}} dx$$

Optimal. Leaf size=67

$$-\frac{a^5}{9x^9} - \frac{5a^4b}{8x^8} - \frac{10a^3b^2}{7x^7} - \frac{5a^2b^3}{3x^6} - \frac{ab^4}{x^5} - \frac{b^5}{4x^4}$$

[Out] $-1/9*a^5/x^9-5/8*a^4*b/x^8-10/7*a^3*b^2/x^7-5/3*a^2*b^3/x^6-a*b^4/x^5-1/4*b^5/x^4$

Rubi [A] time = 0.02, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{10a^3b^2}{7x^7} - \frac{5a^2b^3}{3x^6} - \frac{5a^4b}{8x^8} - \frac{a^5}{9x^9} - \frac{ab^4}{x^5} - \frac{b^5}{4x^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/x^10, x]

[Out] $-a^5/(9*x^9) - (5*a^4*b)/(8*x^8) - (10*a^3*b^2)/(7*x^7) - (5*a^2*b^3)/(3*x^6) - (a*b^4)/x^5 - b^5/(4*x^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{x^{10}} dx &= \int \left(\frac{a^5}{x^{10}} + \frac{5a^4b}{x^9} + \frac{10a^3b^2}{x^8} + \frac{10a^2b^3}{x^7} + \frac{5ab^4}{x^6} + \frac{b^5}{x^5} \right) dx \\ &= -\frac{a^5}{9x^9} - \frac{5a^4b}{8x^8} - \frac{10a^3b^2}{7x^7} - \frac{5a^2b^3}{3x^6} - \frac{ab^4}{x^5} - \frac{b^5}{4x^4} \end{aligned}$$

Mathematica [A] time = 0.01, size = 67, normalized size = 1.00

$$-\frac{a^5}{9x^9} - \frac{5a^4b}{8x^8} - \frac{10a^3b^2}{7x^7} - \frac{5a^2b^3}{3x^6} - \frac{ab^4}{x^5} - \frac{b^5}{4x^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/x^10,x]

[Out] $-1/9*a^5/x^9 - (5*a^4*b)/(8*x^8) - (10*a^3*b^2)/(7*x^7) - (5*a^2*b^3)/(3*x^6) - (a*b^4)/x^5 - b^5/(4*x^4)$

fricas [A] time = 0.44, size = 57, normalized size = 0.85

$$\frac{126 b^5 x^5 + 504 a b^4 x^4 + 840 a^2 b^3 x^3 + 720 a^3 b^2 x^2 + 315 a^4 b x + 56 a^5}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^10,x, algorithm="fricas")

[Out] $-1/504*(126*b^5*x^5 + 504*a*b^4*x^4 + 840*a^2*b^3*x^3 + 720*a^3*b^2*x^2 + 315*a^4*b*x + 56*a^5)/x^9$

giac [A] time = 1.01, size = 57, normalized size = 0.85

$$\frac{126 b^5 x^5 + 504 a b^4 x^4 + 840 a^2 b^3 x^3 + 720 a^3 b^2 x^2 + 315 a^4 b x + 56 a^5}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^10,x, algorithm="giac")

[Out] $-1/504*(126*b^5*x^5 + 504*a*b^4*x^4 + 840*a^2*b^3*x^3 + 720*a^3*b^2*x^2 + 315*a^4*b*x + 56*a^5)/x^9$

maple [A] time = 0.00, size = 58, normalized size = 0.87

$$\frac{b^5}{4x^4} - \frac{ab^4}{x^5} - \frac{5a^2b^3}{3x^6} - \frac{10a^3b^2}{7x^7} - \frac{5a^4b}{8x^8} - \frac{a^5}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/x^10,x)

[Out] $-1/4*b^5/x^4 - a*b^4/x^5 - 5/3*a^2*b^3/x^6 - 10/7*a^3*b^2/x^7 - 5/8*a^4*b/x^8 - 1/9*a^5/x^9$

maxima [A] time = 1.36, size = 57, normalized size = 0.85

$$\frac{126 b^5 x^5 + 504 a b^4 x^4 + 840 a^2 b^3 x^3 + 720 a^3 b^2 x^2 + 315 a^4 b x + 56 a^5}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/x^10,x, algorithm="maxima")

[Out] $-1/504*(126*b^5*x^5 + 504*a*b^4*x^4 + 840*a^2*b^3*x^3 + 720*a^3*b^2*x^2 + 315*a^4*b*x + 56*a^5)/x^9$

mupad [B] time = 0.00, size = 56, normalized size = 0.84

$$\frac{\frac{a^5}{9} + \frac{5a^4bx}{8} + \frac{10a^3b^2x^2}{7} + \frac{5a^2b^3x^3}{3} + ab^4x^4 + \frac{b^5x^5}{4}}{x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/x^10,x)

[Out] $-(a^5/9 + (b^5*x^5)/4 + a*b^4*x^4 + (10*a^3*b^2*x^2)/7 + (5*a^2*b^3*x^3)/3 + (5*a^4*b*x)/8)/x^9$

sympy [A] time = 0.49, size = 61, normalized size = 0.91

$$\frac{-56a^5 - 315a^4bx - 720a^3b^2x^2 - 840a^2b^3x^3 - 504ab^4x^4 - 126b^5x^5}{504x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/x**10,x)

[Out] $(-56*a**5 - 315*a**4*b*x - 720*a**3*b**2*x**2 - 840*a**2*b**3*x**3 - 504*a*b**4*x**4 - 126*b**5*x**5)/(504*x**9)$

$$3.247 \quad \int \frac{(a+bx)^4}{x^{10}} dx$$

Optimal. Leaf size=56

$$-\frac{a^4}{9x^9} - \frac{a^3b}{2x^8} - \frac{6a^2b^2}{7x^7} - \frac{2ab^3}{3x^6} - \frac{b^4}{5x^5}$$

[Out] $-1/9*a^4/x^9-1/2*a^3*b/x^8-6/7*a^2*b^2/x^7-2/3*a*b^3/x^6-1/5*b^4/x^5$

Rubi [A] time = 0.02, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{6a^2b^2}{7x^7} - \frac{a^3b}{2x^8} - \frac{a^4}{9x^9} - \frac{2ab^3}{3x^6} - \frac{b^4}{5x^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4/x^10, x]

[Out] $-a^4/(9*x^9) - (a^3*b)/(2*x^8) - (6*a^2*b^2)/(7*x^7) - (2*a*b^3)/(3*x^6) - b^4/(5*x^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^4}{x^{10}} dx &= \int \left(\frac{a^4}{x^{10}} + \frac{4a^3b}{x^9} + \frac{6a^2b^2}{x^8} + \frac{4ab^3}{x^7} + \frac{b^4}{x^6} \right) dx \\ &= -\frac{a^4}{9x^9} - \frac{a^3b}{2x^8} - \frac{6a^2b^2}{7x^7} - \frac{2ab^3}{3x^6} - \frac{b^4}{5x^5} \end{aligned}$$

Mathematica [A] time = 0.01, size = 56, normalized size = 1.00

$$-\frac{a^4}{9x^9} - \frac{a^3b}{2x^8} - \frac{6a^2b^2}{7x^7} - \frac{2ab^3}{3x^6} - \frac{b^4}{5x^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4/x^10,x]

[Out] $-1/9*a^4/x^9 - (a^3*b)/(2*x^8) - (6*a^2*b^2)/(7*x^7) - (2*a*b^3)/(3*x^6) - b^4/(5*x^5)$

fricas [A] time = 0.46, size = 46, normalized size = 0.82

$$\frac{126 b^4 x^4 + 420 a b^3 x^3 + 540 a^2 b^2 x^2 + 315 a^3 b x + 70 a^4}{630 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/x^10,x, algorithm="fricas")

[Out] $-1/630*(126*b^4*x^4 + 420*a*b^3*x^3 + 540*a^2*b^2*x^2 + 315*a^3*b*x + 70*a^4)/x^9$

giac [A] time = 1.25, size = 46, normalized size = 0.82

$$\frac{126 b^4 x^4 + 420 a b^3 x^3 + 540 a^2 b^2 x^2 + 315 a^3 b x + 70 a^4}{630 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/x^10,x, algorithm="giac")

[Out] $-1/630*(126*b^4*x^4 + 420*a*b^3*x^3 + 540*a^2*b^2*x^2 + 315*a^3*b*x + 70*a^4)/x^9$

maple [A] time = 0.01, size = 47, normalized size = 0.84

$$-\frac{b^4}{5x^5} - \frac{2ab^3}{3x^6} - \frac{6a^2b^2}{7x^7} - \frac{a^3b}{2x^8} - \frac{a^4}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4/x^10,x)

[Out] $-1/9*a^4/x^9 - 1/2*a^3*b/x^8 - 6/7*a^2*b^2/x^7 - 2/3*a*b^3/x^6 - 1/5*b^4/x^5$

maxima [A] time = 1.34, size = 46, normalized size = 0.82

$$\frac{126 b^4 x^4 + 420 a b^3 x^3 + 540 a^2 b^2 x^2 + 315 a^3 b x + 70 a^4}{630 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/x^10,x, algorithm="maxima")

[Out] $-1/630*(126*b^4*x^4 + 420*a*b^3*x^3 + 540*a^2*b^2*x^2 + 315*a^3*b*x + 70*a^4)/x^9$

mupad [B] time = 0.03, size = 46, normalized size = 0.82

$$\frac{\frac{a^4}{9} + \frac{a^3 b x}{2} + \frac{6 a^2 b^2 x^2}{7} + \frac{2 a b^3 x^3}{3} + \frac{b^4 x^4}{5}}{x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^4/x^10,x)`

[Out] $-(a^4/9 + (b^4*x^4)/5 + (2*a*b^3*x^3)/3 + (6*a^2*b^2*x^2)/7 + (a^3*b*x)/2)/x^9$

sympy [A] time = 0.50, size = 49, normalized size = 0.88

$$\frac{-70a^4 - 315a^3bx - 540a^2b^2x^2 - 420ab^3x^3 - 126b^4x^4}{630x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**4/x**10,x)`

[Out] $(-70*a**4 - 315*a**3*b*x - 540*a**2*b**2*x**2 - 420*a*b**3*x**3 - 126*b**4*x**4)/(630*x**9)$

$$3.248 \quad \int \frac{(a+bx)^3}{x^{10}} dx$$

Optimal. Leaf size=43

$$-\frac{a^3}{9x^9} - \frac{3a^2b}{8x^8} - \frac{3ab^2}{7x^7} - \frac{b^3}{6x^6}$$

[Out] $-1/9*a^3/x^9-3/8*a^2*b/x^8-3/7*a*b^2/x^7-1/6*b^3/x^6$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{3a^2b}{8x^8} - \frac{a^3}{9x^9} - \frac{3ab^2}{7x^7} - \frac{b^3}{6x^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^10,x]

[Out] $-a^3/(9*x^9) - (3*a^2*b)/(8*x^8) - (3*a*b^2)/(7*x^7) - b^3/(6*x^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^{10}} dx &= \int \left(\frac{a^3}{x^{10}} + \frac{3a^2b}{x^9} + \frac{3ab^2}{x^8} + \frac{b^3}{x^7} \right) dx \\ &= -\frac{a^3}{9x^9} - \frac{3a^2b}{8x^8} - \frac{3ab^2}{7x^7} - \frac{b^3}{6x^6} \end{aligned}$$

Mathematica [A] time = 0.00, size = 43, normalized size = 1.00

$$-\frac{a^3}{9x^9} - \frac{3a^2b}{8x^8} - \frac{3ab^2}{7x^7} - \frac{b^3}{6x^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^10,x]

[Out] $-1/9*a^3/x^9 - (3*a^2*b)/(8*x^8) - (3*a*b^2)/(7*x^7) - b^3/(6*x^6)$

fricas [A] time = 0.47, size = 35, normalized size = 0.81

$$-\frac{84 b^3 x^3 + 216 a b^2 x^2 + 189 a^2 b x + 56 a^3}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^10,x, algorithm="fricas")`

[Out] $-1/504*(84*b^3*x^3 + 216*a*b^2*x^2 + 189*a^2*b*x + 56*a^3)/x^9$

giac [A] time = 1.09, size = 35, normalized size = 0.81

$$-\frac{84 b^3 x^3 + 216 a b^2 x^2 + 189 a^2 b x + 56 a^3}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^10,x, algorithm="giac")`

[Out] $-1/504*(84*b^3*x^3 + 216*a*b^2*x^2 + 189*a^2*b*x + 56*a^3)/x^9$

maple [A] time = 0.00, size = 36, normalized size = 0.84

$$-\frac{b^3}{6x^6} - \frac{3ab^2}{7x^7} - \frac{3a^2b}{8x^8} - \frac{a^3}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3/x^10,x)`

[Out] $-1/9*a^3/x^9 - 3/8*a^2*b/x^8 - 3/7*a*b^2/x^7 - 1/6*b^3/x^6$

maxima [A] time = 1.35, size = 35, normalized size = 0.81

$$-\frac{84 b^3 x^3 + 216 a b^2 x^2 + 189 a^2 b x + 56 a^3}{504 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3/x^10,x, algorithm="maxima")`

[Out] $-1/504*(84*b^3*x^3 + 216*a*b^2*x^2 + 189*a^2*b*x + 56*a^3)/x^9$

mupad [B] time = 0.03, size = 35, normalized size = 0.81

$$-\frac{\frac{a^3}{9} + \frac{3a^2bx}{8} + \frac{3ab^2x^2}{7} + \frac{b^3x^3}{6}}{x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^10, x)`

[Out] $-(a^3/9 + (b^3*x^3)/6 + (3*a*b^2*x^2)/7 + (3*a^2*b*x)/8)/x^9$

sympy [A] time = 0.38, size = 37, normalized size = 0.86

$$\frac{-56a^3 - 189a^2bx - 216ab^2x^2 - 84b^3x^3}{504x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**10, x)`

[Out] $(-56*a**3 - 189*a**2*b*x - 216*a*b**2*x**2 - 84*b**3*x**3)/(504*x**9)$

$$3.249 \quad \int \frac{(a+bx)^2}{x^{10}} dx$$

Optimal. Leaf size=30

$$-\frac{a^2}{9x^9} - \frac{ab}{4x^8} - \frac{b^2}{7x^7}$$

[Out] $-1/9*a^2/x^9-1/4*a*b/x^8-1/7*b^2/x^7$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^2}{9x^9} - \frac{ab}{4x^8} - \frac{b^2}{7x^7}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^10,x]

[Out] $-a^2/(9*x^9) - (a*b)/(4*x^8) - b^2/(7*x^7)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^{10}} dx &= \int \left(\frac{a^2}{x^{10}} + \frac{2ab}{x^9} + \frac{b^2}{x^8} \right) dx \\ &= -\frac{a^2}{9x^9} - \frac{ab}{4x^8} - \frac{b^2}{7x^7} \end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$-\frac{a^2}{9x^9} - \frac{ab}{4x^8} - \frac{b^2}{7x^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^10,x]

[Out] $-1/9*a^2/x^9 - (a*b)/(4*x^8) - b^2/(7*x^7)$

fricas [A] time = 0.43, size = 24, normalized size = 0.80

$$-\frac{36 b^2 x^2 + 63 a b x + 28 a^2}{252 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^10,x, algorithm="fricas")`

[Out] $-1/252*(36*b^2*x^2 + 63*a*b*x + 28*a^2)/x^9$

giac [A] time = 0.87, size = 24, normalized size = 0.80

$$-\frac{36 b^2 x^2 + 63 a b x + 28 a^2}{252 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^10,x, algorithm="giac")`

[Out] $-1/252*(36*b^2*x^2 + 63*a*b*x + 28*a^2)/x^9$

maple [A] time = 0.00, size = 25, normalized size = 0.83

$$-\frac{b^2}{7x^7} - \frac{ab}{4x^8} - \frac{a^2}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^10,x)`

[Out] $-1/9*a^2/x^9 - 1/4*a*b/x^8 - 1/7*b^2/x^7$

maxima [A] time = 1.34, size = 24, normalized size = 0.80

$$-\frac{36 b^2 x^2 + 63 a b x + 28 a^2}{252 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^10,x, algorithm="maxima")`

[Out] $-1/252*(36*b^2*x^2 + 63*a*b*x + 28*a^2)/x^9$

mupad [B] time = 0.04, size = 24, normalized size = 0.80

$$-\frac{\frac{a^2}{9} + \frac{abx}{4} + \frac{b^2x^2}{7}}{x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x^10,x)`

[Out] $-(a^2/9 + (b^2*x^2)/7 + (a*b*x)/4)/x^9$

sympy [A] time = 0.27, size = 26, normalized size = 0.87

$$\frac{-28a^2 - 63abx - 36b^2x^2}{252x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**10,x)`

[Out] $(-28*a**2 - 63*a*b*x - 36*b**2*x**2)/(252*x**9)$

$$3.250 \quad \int \frac{a+bx}{x^{10}} dx$$

Optimal. Leaf size=17

$$-\frac{a}{9x^9} - \frac{b}{8x^8}$$

[Out] $-1/9*a/x^9-1/8*b/x^8$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$-\frac{a}{9x^9} - \frac{b}{8x^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x^10,x]

[Out] $-a/(9*x^9) - b/(8*x^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^{10}} dx &= \int \left(\frac{a}{x^{10}} + \frac{b}{x^9} \right) dx \\ &= -\frac{a}{9x^9} - \frac{b}{8x^8} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$-\frac{a}{9x^9} - \frac{b}{8x^8}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x^10,x]

[Out] $-1/9*a/x^9 - b/(8*x^8)$

fricas [A] time = 0.46, size = 13, normalized size = 0.76

$$-\frac{9bx + 8a}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^10,x, algorithm="fricas")

[Out] -1/72*(9*b*x + 8*a)/x^9

giac [A] time = 1.00, size = 13, normalized size = 0.76

$$-\frac{9bx + 8a}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^10,x, algorithm="giac")

[Out] -1/72*(9*b*x + 8*a)/x^9

maple [A] time = 0.00, size = 14, normalized size = 0.82

$$-\frac{b}{8x^8} - \frac{a}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^10,x)

[Out] -1/9*a/x^9-1/8*b/x^8

maxima [A] time = 1.30, size = 13, normalized size = 0.76

$$-\frac{9bx + 8a}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^10,x, algorithm="maxima")

[Out] -1/72*(9*b*x + 8*a)/x^9

mupad [B] time = 0.03, size = 13, normalized size = 0.76

$$-\frac{8a + 9bx}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^10,x)
```

```
[Out] -(8*a + 9*b*x)/(72*x^9)
```

```
sympy [A] time = 0.21, size = 14, normalized size = 0.82
```

$$\frac{-8a - 9bx}{72x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**10,x)
```

```
[Out] (-8*a - 9*b*x)/(72*x**9)
```

$$3.251 \quad \int \frac{1}{x^{10}} dx$$

Optimal. Leaf size=7

$$-\frac{1}{9x^9}$$

[Out] -1/9/x^9

Rubi [A] time = 0.00, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 3, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {30}

$$-\frac{1}{9x^9}$$

Antiderivative was successfully verified.

[In] Int[x^(-10), x]

[Out] -1/(9*x^9)

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{10}} dx = -\frac{1}{9x^9}$$

Mathematica [A] time = 0.00, size = 7, normalized size = 1.00

$$-\frac{1}{9x^9}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-10), x]

[Out] -1/9*1/x^9

fricas [A] time = 0.45, size = 5, normalized size = 0.71

$$-\frac{1}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10,x, algorithm="fricas")

[Out] -1/9/x^9

giac [A] time = 1.04, size = 5, normalized size = 0.71

$$-\frac{1}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10,x, algorithm="giac")

[Out] -1/9/x^9

maple [A] time = 0.00, size = 6, normalized size = 0.86

$$-\frac{1}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^10,x)

[Out] -1/9/x^9

maxima [A] time = 1.32, size = 5, normalized size = 0.71

$$-\frac{1}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10,x, algorithm="maxima")

[Out] -1/9/x^9

mupad [B] time = 0.02, size = 5, normalized size = 0.71

$$-\frac{1}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^10,x)

[Out] -1/(9*x^9)

sympy [A] time = 0.07, size = 7, normalized size = 1.00

$$-\frac{1}{9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**10,x)

[Out] -1/(9*x**9)

$$3.252 \quad \int \frac{1}{x^{10}(a+bx)} dx$$

Optimal. Leaf size=134

$$-\frac{b^9 \log(x)}{a^{10}} + \frac{b^9 \log(a+bx)}{a^{10}} - \frac{b^8}{a^9 x} + \frac{b^7}{2a^8 x^2} - \frac{b^6}{3a^7 x^3} + \frac{b^5}{4a^6 x^4} - \frac{b^4}{5a^5 x^5} + \frac{b^3}{6a^4 x^6} - \frac{b^2}{7a^3 x^7} + \frac{b}{8a^2 x^8} - \frac{1}{9ax^9}$$

[Out] $-1/9/a/x^9 + 1/8*b/a^2/x^8 - 1/7*b^2/a^3/x^7 + 1/6*b^3/a^4/x^6 - 1/5*b^4/a^5/x^5 + 1/4*b^5/a^6/x^4 - 1/3*b^6/a^7/x^3 + 1/2*b^7/a^8/x^2 - b^8/a^9/x - b^9*\ln(x)/a^{10} + b^9*\ln(b*x+a)/a^{10}$

Rubi [A] time = 0.06, antiderivative size = 134, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{b^7}{2a^8 x^2} - \frac{b^6}{3a^7 x^3} + \frac{b^5}{4a^6 x^4} - \frac{b^4}{5a^5 x^5} + \frac{b^3}{6a^4 x^6} - \frac{b^2}{7a^3 x^7} - \frac{b^8}{a^9 x} - \frac{b^9 \log(x)}{a^{10}} + \frac{b^9 \log(a+bx)}{a^{10}} + \frac{b}{8a^2 x^8} - \frac{1}{9ax^9}$$

Antiderivative was successfully verified.

[In] Int[1/(x^10*(a + b*x)),x]

[Out] $-1/(9*a*x^9) + b/(8*a^2*x^8) - b^2/(7*a^3*x^7) + b^3/(6*a^4*x^6) - b^4/(5*a^5*x^5) + b^5/(4*a^6*x^4) - b^6/(3*a^7*x^3) + b^7/(2*a^8*x^2) - b^8/(a^9*x) - (b^9*\text{Log}[x])/a^{10} + (b^9*\text{Log}[a + b*x])/a^{10}$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^{10}(a+bx)} dx &= \int \left(\frac{1}{ax^{10}} - \frac{b}{a^2 x^9} + \frac{b^2}{a^3 x^8} - \frac{b^3}{a^4 x^7} + \frac{b^4}{a^5 x^6} - \frac{b^5}{a^6 x^5} + \frac{b^6}{a^7 x^4} - \frac{b^7}{a^8 x^3} + \frac{b^8}{a^9 x^2} - \frac{b^9}{a^{10} x} + \frac{b^{10}}{a^{10}(a+bx)} \right) dx \\ &= -\frac{1}{9ax^9} + \frac{b}{8a^2 x^8} - \frac{b^2}{7a^3 x^7} + \frac{b^3}{6a^4 x^6} - \frac{b^4}{5a^5 x^5} + \frac{b^5}{4a^6 x^4} - \frac{b^6}{3a^7 x^3} + \frac{b^7}{2a^8 x^2} - \frac{b^8}{a^9 x} - \frac{b^9 \log(x)}{a^{10}} + \end{aligned}$$

Mathematica [A] time = 0.01, size = 134, normalized size = 1.00

$$-\frac{b^9 \log(x)}{a^{10}} + \frac{b^9 \log(a+bx)}{a^{10}} - \frac{b^8}{a^9 x} + \frac{b^7}{2a^8 x^2} - \frac{b^6}{3a^7 x^3} + \frac{b^5}{4a^6 x^4} - \frac{b^4}{5a^5 x^5} + \frac{b^3}{6a^4 x^6} - \frac{b^2}{7a^3 x^7} + \frac{b}{8a^2 x^8} - \frac{1}{9ax^9}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^10*(a + b*x)),x]

[Out] $-1/9*1/(a*x^9) + b/(8*a^2*x^8) - b^2/(7*a^3*x^7) + b^3/(6*a^4*x^6) - b^4/(5*a^5*x^5) + b^5/(4*a^6*x^4) - b^6/(3*a^7*x^3) + b^7/(2*a^8*x^2) - b^8/(a^9*x) - (b^9*\text{Log}[x])/a^{10} + (b^9*\text{Log}[a + b*x])/a^{10}$

fricas [A] time = 0.50, size = 120, normalized size = 0.90

$$\frac{2520 b^9 x^9 \log(bx + a) - 2520 b^9 x^9 \log(x) - 2520 a b^8 x^8 + 1260 a^2 b^7 x^7 - 840 a^3 b^6 x^6 + 630 a^4 b^5 x^5 - 504 a^5 b^4 x^4 + 420 a^6 b^3 x^3 - 360 a^7 b^2 x^2 + 315 a^8 b x - 280 a^9}{2520 a^{10} x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10/(b*x+a),x, algorithm="fricas")

[Out] $1/2520*(2520*b^9*x^9*\log(b*x + a) - 2520*b^9*x^9*\log(x) - 2520*a*b^8*x^8 + 1260*a^2*b^7*x^7 - 840*a^3*b^6*x^6 + 630*a^4*b^5*x^5 - 504*a^5*b^4*x^4 + 420*a^6*b^3*x^3 - 360*a^7*b^2*x^2 + 315*a^8*b*x - 280*a^9)/(a^{10}*x^9)$

giac [A] time = 1.16, size = 122, normalized size = 0.91

$$\frac{b^9 \log(|bx + a|)}{a^{10}} - \frac{b^9 \log(|x|)}{a^{10}} - \frac{2520 a b^8 x^8 - 1260 a^2 b^7 x^7 + 840 a^3 b^6 x^6 - 630 a^4 b^5 x^5 + 504 a^5 b^4 x^4 - 420 a^6 b^3 x^3 + 315 a^8 b x - 280 a^9}{2520 a^{10} x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10/(b*x+a),x, algorithm="giac")

[Out] $b^9*\log(\text{abs}(b*x + a))/a^{10} - b^9*\log(\text{abs}(x))/a^{10} - 1/2520*(2520*a*b^8*x^8 - 1260*a^2*b^7*x^7 + 840*a^3*b^6*x^6 - 630*a^4*b^5*x^5 + 504*a^5*b^4*x^4 - 420*a^6*b^3*x^3 + 360*a^7*b^2*x^2 - 315*a^8*b*x + 280*a^9)/(a^{10}*x^9)$

maple [A] time = 0.01, size = 119, normalized size = 0.89

$$-\frac{b^9 \ln(x)}{a^{10}} + \frac{b^9 \ln(bx + a)}{a^{10}} - \frac{b^8}{a^9 x} + \frac{b^7}{2a^8 x^2} - \frac{b^6}{3a^7 x^3} + \frac{b^5}{4a^6 x^4} - \frac{b^4}{5a^5 x^5} + \frac{b^3}{6a^4 x^6} - \frac{b^2}{7a^3 x^7} + \frac{b}{8a^2 x^8} - \frac{1}{9a x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^10/(b*x+a),x)

[Out] $-1/9/a/x^9 + 1/8*b/a^2/x^8 - 1/7*b^2/a^3/x^7 + 1/6*b^3/a^4/x^6 - 1/5*b^4/a^5/x^5 + 1/4*b^5/a^6/x^4 - 1/3*b^6/a^7/x^3 + 1/2*b^7/a^8/x^2 - b^8/a^9/x - b^9*\ln(x)/a^{10} + b^9*\ln(b*x+a)/a^{10}$

maxima [A] time = 1.35, size = 117, normalized size = 0.87

$$\frac{b^9 \log(bx + a)}{a^{10}} - \frac{b^9 \log(x)}{a^{10}} - \frac{2520 b^8 x^8 - 1260 a b^7 x^7 + 840 a^2 b^6 x^6 - 630 a^3 b^5 x^5 + 504 a^4 b^4 x^4 - 420 a^5 b^3 x^3 + 360 a^6 b^2 x^2 - 315 a^7 b x + 280 a^8}{2520 a^9 x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10/(b*x+a),x, algorithm="maxima")

[Out] b^9*log(b*x + a)/a^10 - b^9*log(x)/a^10 - 1/2520*(2520*b^8*x^8 - 1260*a*b^7*x^7 + 840*a^2*b^6*x^6 - 630*a^3*b^5*x^5 + 504*a^4*b^4*x^4 - 420*a^5*b^3*x^3 + 360*a^6*b^2*x^2 - 315*a^7*b*x + 280*a^8)/(a^9*x^9)

mupad [B] time = 0.13, size = 114, normalized size = 0.85

$$\frac{280 a^9 + 2520 a b^8 x^8 - 5040 b^9 x^9 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right) + 360 a^7 b^2 x^2 - 420 a^6 b^3 x^3 + 504 a^5 b^4 x^4 - 630 a^4 b^5 x^5 + 840 a^3 b^6 x^6 - 1260 a^2 b^7 x^7 + 315 a b^8 x^8 - 280 a^8}{2520 a^{10} x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^10*(a + b*x)),x)

[Out] -(280*a^9 + 2520*a*b^8*x^8 - 5040*b^9*x^9*atanh((2*b*x)/a + 1) + 360*a^7*b^2*x^2 - 420*a^6*b^3*x^3 + 504*a^5*b^4*x^4 - 630*a^4*b^5*x^5 + 840*a^3*b^6*x^6 - 1260*a^2*b^7*x^7 - 315*a^8*b*x)/(2520*a^10*x^9)

sympy [A] time = 0.41, size = 116, normalized size = 0.87

$$\frac{-280a^8 + 315a^7bx - 360a^6b^2x^2 + 420a^5b^3x^3 - 504a^4b^4x^4 + 630a^3b^5x^5 - 840a^2b^6x^6 + 1260ab^7x^7 - 2520b^8x^8 + 280a^8}{2520a^9x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**10/(b*x+a),x)

[Out] (-280*a**8 + 315*a**7*b*x - 360*a**6*b**2*x**2 + 420*a**5*b**3*x**3 - 504*a**4*b**4*x**4 + 630*a**3*b**5*x**5 - 840*a**2*b**6*x**6 + 1260*a*b**7*x**7 - 2520*b**8*x**8)/(2520*a**9*x**9) + b**9*(-log(x) + log(a/b + x))/a**10

$$3.253 \quad \int \frac{1}{x^{10}(a+bx)^2} dx$$

Optimal. Leaf size=146

$$-\frac{10b^9 \log(x)}{a^{11}} + \frac{10b^9 \log(a+bx)}{a^{11}} - \frac{b^9}{a^{10}(a+bx)} - \frac{9b^8}{a^{10}x} + \frac{4b^7}{a^9x^2} - \frac{7b^6}{3a^8x^3} + \frac{3b^5}{2a^7x^4} - \frac{b^4}{a^6x^5} + \frac{2b^3}{3a^5x^6} - \frac{3b^2}{7a^4x^7} + \frac{b}{4a^3x^8} - \frac{1}{9a^2x^9}$$

[Out] $-1/9/a^2/x^9 + 1/4*b/a^3/x^8 - 3/7*b^2/a^4/x^7 + 2/3*b^3/a^5/x^6 - b^4/a^6/x^5 + 3/2*b^5/a^7/x^4 - 7/3*b^6/a^8/x^3 + 4*b^7/a^9/x^2 - 9*b^8/a^{10}/x - b^9/a^{10}/(b*x+a) - 10*b^9*\ln(x)/a^{11} + 10*b^9*\ln(b*x+a)/a^{11}$

Rubi [A] time = 0.09, antiderivative size = 146, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{4b^7}{a^9x^2} - \frac{7b^6}{3a^8x^3} + \frac{3b^5}{2a^7x^4} - \frac{b^4}{a^6x^5} + \frac{2b^3}{3a^5x^6} - \frac{3b^2}{7a^4x^7} - \frac{b^9}{a^{10}(a+bx)} - \frac{9b^8}{a^{10}x} - \frac{10b^9 \log(x)}{a^{11}} + \frac{10b^9 \log(a+bx)}{a^{11}} + \frac{b}{4a^3x^8} - \frac{1}{9a^2x^9}$$

Antiderivative was successfully verified.

[In] Int[1/(x^10*(a + b*x)^2), x]

[Out] $-1/(9*a^2*x^9) + b/(4*a^3*x^8) - (3*b^2)/(7*a^4*x^7) + (2*b^3)/(3*a^5*x^6) - b^4/(a^6*x^5) + (3*b^5)/(2*a^7*x^4) - (7*b^6)/(3*a^8*x^3) + (4*b^7)/(a^9*x^2) - (9*b^8)/(a^{10}*x) - b^9/(a^{10}*(a + b*x)) - (10*b^9*\text{Log}[x])/a^{11} + (10*b^9*\text{Log}[a + b*x])/a^{11}$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{x^{10}(a+bx)^2} dx = \int \left(\frac{1}{a^2x^{10}} - \frac{2b}{a^3x^9} + \frac{3b^2}{a^4x^8} - \frac{4b^3}{a^5x^7} + \frac{5b^4}{a^6x^6} - \frac{6b^5}{a^7x^5} + \frac{7b^6}{a^8x^4} - \frac{8b^7}{a^9x^3} + \frac{9b^8}{a^{10}x^2} - \frac{10b^9}{a^{11}x} + \frac{b^{10}}{a^{10}(a+bx)} \right) dx$$

$$= -\frac{1}{9a^2x^9} + \frac{b}{4a^3x^8} - \frac{3b^2}{7a^4x^7} + \frac{2b^3}{3a^5x^6} - \frac{b^4}{a^6x^5} + \frac{3b^5}{2a^7x^4} - \frac{7b^6}{3a^8x^3} + \frac{4b^7}{a^9x^2} - \frac{9b^8}{a^{10}x} - \frac{b^9}{a^{10}(a+bx)}$$

Mathematica [A] time = 0.09, size = 134, normalized size = 0.92

$$\frac{a(28a^9 - 35a^8bx + 45a^7b^2x^2 - 60a^6b^3x^3 + 84a^5b^4x^4 - 126a^4b^5x^5 + 210a^3b^6x^6 - 420a^2b^7x^7 + 1260ab^8x^8 + 2520b^9x^9)}{x^9(a+bx)} - 2520b^9 \log(a + bx) + 2520a^{11}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^10*(a + b*x)^2),x]

[Out] -1/252*((a*(28*a^9 - 35*a^8*b*x + 45*a^7*b^2*x^2 - 60*a^6*b^3*x^3 + 84*a^5*b^4*x^4 - 126*a^4*b^5*x^5 + 210*a^3*b^6*x^6 - 420*a^2*b^7*x^7 + 1260*a*b^8*x^8 + 2520*b^9*x^9))/(x^9*(a + b*x)) + 2520*b^9*Log[x] - 2520*b^9*Log[a + b*x])/a^11

fricas [A] time = 0.47, size = 163, normalized size = 1.12

$$\frac{2520ab^9x^9 + 1260a^2b^8x^8 - 420a^3b^7x^7 + 210a^4b^6x^6 - 126a^5b^5x^5 + 84a^6b^4x^4 - 60a^7b^3x^3 + 45a^8b^2x^2 - 35a^9b^1x^1}{252(a^{11}bx^{10} + a^{12}x^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10/(b*x+a)^2,x, algorithm="fricas")

[Out] -1/252*(2520*a*b^9*x^9 + 1260*a^2*b^8*x^8 - 420*a^3*b^7*x^7 + 210*a^4*b^6*x^6 - 126*a^5*b^5*x^5 + 84*a^6*b^4*x^4 - 60*a^7*b^3*x^3 + 45*a^8*b^2*x^2 - 35*a^9*b*x + 28*a^10 - 2520*(b^10*x^10 + a*b^9*x^9)*log(b*x + a) + 2520*(b^10*x^10 + a*b^9*x^9)*log(x))/(a^11*b*x^10 + a^12*x^9)

giac [A] time = 1.28, size = 180, normalized size = 1.23

$$\frac{10b^9 \log\left(\left|-\frac{a}{bx+a} + 1\right|\right)}{a^{11}} - \frac{b^9}{(bx+a)a^{10}} - \frac{\frac{41481ab^9}{bx+a} - \frac{155844a^2b^9}{(bx+a)^2} + \frac{337176a^3b^9}{(bx+a)^3} - \frac{460404a^4b^9}{(bx+a)^4} + \frac{407484a^5b^9}{(bx+a)^5} - \frac{229320a^6b^9}{(bx+a)^6} + \dots}{252a^{11}\left(\frac{a}{bx+a} - 1\right)^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10/(b*x+a)^2,x, algorithm="giac")

[Out] -10*b^9*log(abs(-a/(b*x + a) + 1))/a^11 - b^9/((b*x + a)*a^10) - 1/252*(41481*a*b^9/(b*x + a) - 155844*a^2*b^9/(b*x + a)^2 + 337176*a^3*b^9/(b*x + a)^3 - 460404*a^4*b^9/(b*x + a)^4 + 407484*a^5*b^9/(b*x + a)^5 - 229320*a^6*b^9/(b*x + a)^6 + 75600*a^7*b^9/(b*x + a)^7 - 11340*a^8*b^9/(b*x + a)^8 - 4861*b^9)/(a^11*(a/(b*x + a) - 1)^9)

maple [A] time = 0.01, size = 135, normalized size = 0.92

$$\frac{b^9}{(bx+a)a^{10}} - \frac{10b^9 \ln(x)}{a^{11}} + \frac{10b^9 \ln(bx+a)}{a^{11}} - \frac{9b^8}{a^{10}x} + \frac{4b^7}{a^9x^2} - \frac{7b^6}{3a^8x^3} + \frac{3b^5}{2a^7x^4} - \frac{b^4}{a^6x^5} + \frac{2b^3}{3a^5x^6} - \frac{3b^2}{7a^4x^7} + \frac{b}{4a^3x^8} - \frac{1}{9a^2x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^10/(b*x+a)^2,x)

[Out] $-1/9/a^2/x^9 + 1/4*b/a^3/x^8 - 3/7*b^2/a^4/x^7 + 2/3*b^3/a^5/x^6 - b^4/a^6/x^5 + 3/2*b^5/a^7/x^4 - 7/3*b^6/a^8/x^3 + 4*b^7/a^9/x^2 - 9*b^8/a^{10}/x - b^9/a^{10}/(b*x+a) - 10*b^9*\ln(x)/a^{11} + 10*b^9*\ln(b*x+a)/a^{11}$

maxima [A] time = 1.40, size = 141, normalized size = 0.97

$$\frac{2520b^9x^9 + 1260ab^8x^8 - 420a^2b^7x^7 + 210a^3b^6x^6 - 126a^4b^5x^5 + 84a^5b^4x^4 - 60a^6b^3x^3 + 45a^7b^2x^2 - 35a^8bx}{252(a^{10}bx^{10} + a^{11}x^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10/(b*x+a)^2,x, algorithm="maxima")

[Out] $-1/252*(2520*b^9*x^9 + 1260*a*b^8*x^8 - 420*a^2*b^7*x^7 + 210*a^3*b^6*x^6 - 126*a^4*b^5*x^5 + 84*a^5*b^4*x^4 - 60*a^6*b^3*x^3 + 45*a^7*b^2*x^2 - 35*a^8*b*x + 28*a^9)/(a^{10}*b*x^{10} + a^{11}*x^9) + 10*b^9*\log(b*x + a)/a^{11} - 10*b^9*\log(x)/a^{11}$

mupad [B] time = 0.08, size = 135, normalized size = 0.92

$$\frac{20b^9 \operatorname{atanh}\left(\frac{2bx}{a} + 1\right)}{a^{11}} - \frac{\frac{1}{9a} + \frac{5b^2x^2}{28a^3} - \frac{5b^3x^3}{21a^4} + \frac{b^4x^4}{3a^5} - \frac{b^5x^5}{2a^6} + \frac{5b^6x^6}{6a^7} - \frac{5b^7x^7}{3a^8} + \frac{5b^8x^8}{a^9} + \frac{10b^9x^9}{a^{10}} - \frac{5bx}{36a^2}}{bx^{10} + ax^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^10*(a + b*x)^2),x)

[Out] $(20*b^9*\operatorname{atanh}((2*b*x)/a + 1))/a^{11} - (1/(9*a) + (5*b^2*x^2)/(28*a^3) - (5*b^3*x^3)/(21*a^4) + (b^4*x^4)/(3*a^5) - (b^5*x^5)/(2*a^6) + (5*b^6*x^6)/(6*a^7) - (5*b^7*x^7)/(3*a^8) + (5*b^8*x^8)/a^9 + (10*b^9*x^9)/a^{10} - (5*b*x)/(36*a^2))/(a*x^9 + b*x^{10})$

sympy [A] time = 0.61, size = 139, normalized size = 0.95

$$\frac{-28a^9 + 35a^8bx - 45a^7b^2x^2 + 60a^6b^3x^3 - 84a^5b^4x^4 + 126a^4b^5x^5 - 210a^3b^6x^6 + 420a^2b^7x^7 - 1260ab^8x^8 - 2520b^9}{252a^{11}x^9 + 252a^{10}bx^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**10/(b*x+a)**2,x)
```

```
[Out] (-28*a**9 + 35*a**8*b*x - 45*a**7*b**2*x**2 + 60*a**6*b**3*x**3 - 84*a**5*b**4*x**4 + 126*a**4*b**5*x**5 - 210*a**3*b**6*x**6 + 420*a**2*b**7*x**7 - 1260*a*b**8*x**8 - 2520*b**9*x**9)/(252*a**11*x**9 + 252*a**10*b*x**10) + 10*b**9*(-log(x) + log(a/b + x))/a**11
```

$$3.254 \quad \int \frac{1}{x^{10}(a+bx)^3} dx$$

Optimal. Leaf size=163

$$-\frac{55b^9 \log(x)}{a^{12}} + \frac{55b^9 \log(a+bx)}{a^{12}} - \frac{10b^9}{a^{11}(a+bx)} - \frac{45b^8}{a^{11}x} - \frac{b^9}{2a^{10}(a+bx)^2} + \frac{18b^7}{a^{10}x^2} - \frac{28b^6}{3a^9x^3} + \frac{21b^5}{4a^8x^4} - \frac{3b^4}{a^7x^5} + \frac{5b^3}{3a^6x^6} - \frac{6b^2}{7a^5x^7}$$

[Out] $-1/9/a^3/x^9+3/8*b/a^4/x^8-6/7*b^2/a^5/x^7+5/3*b^3/a^6/x^6-3*b^4/a^7/x^5+21/4*b^5/a^8/x^4-28/3*b^6/a^9/x^3+18*b^7/a^{10}/x^2-45*b^8/a^{11}/x-1/2*b^9/a^{10}/(b*x+a)^2-10*b^9/a^{11}/(b*x+a)-55*b^9*\ln(x)/a^{12}+55*b^9*\ln(b*x+a)/a^{12}$

Rubi [A] time = 0.11, antiderivative size = 163, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{18b^7}{a^{10}x^2} - \frac{28b^6}{3a^9x^3} + \frac{21b^5}{4a^8x^4} - \frac{3b^4}{a^7x^5} + \frac{5b^3}{3a^6x^6} - \frac{6b^2}{7a^5x^7} - \frac{10b^9}{a^{11}(a+bx)} - \frac{b^9}{2a^{10}(a+bx)^2} - \frac{45b^8}{a^{11}x} - \frac{55b^9 \log(x)}{a^{12}} + \frac{55b^9 \log(a+bx)}{a^{12}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^10*(a + b*x)^3), x]

[Out] $-1/(9*a^3*x^9) + (3*b)/(8*a^4*x^8) - (6*b^2)/(7*a^5*x^7) + (5*b^3)/(3*a^6*x^6) - (3*b^4)/(a^7*x^5) + (21*b^5)/(4*a^8*x^4) - (28*b^6)/(3*a^9*x^3) + (18*b^7)/(a^{10}*x^2) - (45*b^8)/(a^{11}*x) - b^9/(2*a^{10}*(a + b*x)^2) - (10*b^9)/(a^{11}*(a + b*x)) - (55*b^9*\text{Log}[x])/a^{12} + (55*b^9*\text{Log}[a + b*x])/a^{12}$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{x^{10}(a+bx)^3} dx = \int \left(\frac{1}{a^3x^{10}} - \frac{3b}{a^4x^9} + \frac{6b^2}{a^5x^8} - \frac{10b^3}{a^6x^7} + \frac{15b^4}{a^7x^6} - \frac{21b^5}{a^8x^5} + \frac{28b^6}{a^9x^4} - \frac{36b^7}{a^{10}x^3} + \frac{45b^8}{a^{11}x^2} - \frac{55b^9}{a^{12}x} + \frac{b^{10}}{a^{10}(a+bx)} \right) dx$$

$$= -\frac{1}{9a^3x^9} + \frac{3b}{8a^4x^8} - \frac{6b^2}{7a^5x^7} + \frac{5b^3}{3a^6x^6} - \frac{3b^4}{a^7x^5} + \frac{21b^5}{4a^8x^4} - \frac{28b^6}{3a^9x^3} + \frac{18b^7}{a^{10}x^2} - \frac{45b^8}{a^{11}x} - \frac{b^9}{2a^{10}(a+bx)}$$

Mathematica [A] time = 0.11, size = 145, normalized size = 0.89

$$\frac{a(56a^{10} - 77a^9bx + 110a^8b^2x^2 - 165a^7b^3x^3 + 264a^6b^4x^4 - 462a^5b^5x^5 + 924a^4b^6x^6 - 2310a^3b^7x^7 + 9240a^2b^8x^8 + 41580ab^9x^9 + 27720b^{10}x^{10})}{x^9(a+bx)^2} - \frac{27720b^9}{504a^{12}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^10*(a + b*x)^3), x]

[Out]
$$-1/504*((a*(56*a^{10} - 77*a^9*b*x + 110*a^8*b^2*x^2 - 165*a^7*b^3*x^3 + 264*a^6*b^4*x^4 - 462*a^5*b^5*x^5 + 924*a^4*b^6*x^6 - 2310*a^3*b^7*x^7 + 9240*a^2*b^8*x^8 + 41580*a*b^9*x^9 + 27720*b^{10}*x^{10}))/x^9*(a + b*x)^2 + 27720*b^9*Log[x] - 27720*b^9*Log[a + b*x])/a^{12}$$

fricas [A] time = 0.48, size = 207, normalized size = 1.27

$$\frac{27720 ab^{10}x^{10} + 41580 a^2b^9x^9 + 9240 a^3b^8x^8 - 2310 a^4b^7x^7 + 924 a^5b^6x^6 - 462 a^6b^5x^5 + 264 a^7b^4x^4 - 165 a^8b^3x^3 + 110 a^9b^2x^2 - 77 a^{10}bx + 56 a^{11}}{504(a+bx)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10/(b*x+a)^3,x, algorithm="fricas")

[Out]
$$-1/504*(27720*a*b^{10}*x^{10} + 41580*a^2*b^9*x^9 + 9240*a^3*b^8*x^8 - 2310*a^4*b^7*x^7 + 924*a^5*b^6*x^6 - 462*a^6*b^5*x^5 + 264*a^7*b^4*x^4 - 165*a^8*b^3*x^3 + 110*a^9*b^2*x^2 - 77*a^{10}*b*x + 56*a^{11} - 27720*(b^{11}*x^{11} + 2*a*b^{10}*x^{10} + a^2*b^9*x^9)*log(b*x + a) + 27720*(b^{11}*x^{11} + 2*a*b^{10}*x^{10} + a^2*b^9*x^9)*log(x))/(a^{12}*b^2*x^{11} + 2*a^{13}*b*x^{10} + a^{14}*x^9)$$

giac [A] time = 1.13, size = 152, normalized size = 0.93

$$\frac{55 b^9 \log(|bx + a|)}{a^{12}} - \frac{55 b^9 \log(|x|)}{a^{12}} - \frac{27720 ab^{10}x^{10} + 41580 a^2b^9x^9 + 9240 a^3b^8x^8 - 2310 a^4b^7x^7 + 924 a^5b^6x^6 - 165 a^8b^3x^3 + 110 a^9b^2x^2 - 77 a^{10}bx + 56 a^{11}}{504 (bx + a)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^10/(b*x+a)^3,x, algorithm="giac")

[Out]
$$55*b^9*log(abs(b*x + a))/a^{12} - 55*b^9*log(abs(x))/a^{12} - 1/504*(27720*a*b^{10}*x^{10} + 41580*a^2*b^9*x^9 + 9240*a^3*b^8*x^8 - 2310*a^4*b^7*x^7 + 924*a^5*b^6*x^6 - 462*a^6*b^5*x^5 + 264*a^7*b^4*x^4 - 165*a^8*b^3*x^3 + 110*a^9*b^2*x^2 - 77*a^{10}*b*x + 56*a^{11})/((b*x + a)^2*a^{12}*x^9)$$

maple [A] time = 0.01, size = 150, normalized size = 0.92

$$\frac{b^9}{2(bx+a)^2 a^{10}} - \frac{10b^9}{(bx+a)a^{11}} - \frac{55b^9 \ln(x)}{a^{12}} + \frac{55b^9 \ln(bx+a)}{a^{12}} - \frac{45b^8}{a^{11}x} + \frac{18b^7}{a^{10}x^2} - \frac{28b^6}{3a^9x^3} + \frac{21b^5}{4a^8x^4} - \frac{3b^4}{a^7x^5} + \frac{5b^3}{3a^6x^6} - \frac{6b^2}{7a^5x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^10/(b*x+a)^3,x)`

[Out]
$$\frac{-1/9/a^3/x^9+3/8*b/a^4/x^8-6/7*b^2/a^5/x^7+5/3*b^3/a^6/x^6-3*b^4/a^7/x^5+21/4*b^5/a^8/x^4-28/3*b^6/a^9/x^3+18*b^7/a^10/x^2-45*b^8/a^11/x-1/2*b^9/a^10/(b*x+a)^2-10*b^9/a^11/(b*x+a)-55*b^9*\ln(x)/a^12+55*b^9*\ln(b*x+a)/a^12}{504(a^{11}b^2x^{11}+2a^{12}bx^{10}+a^{13}x^9)}$$

maxima [A] time = 1.43, size = 163, normalized size = 1.00

$$\frac{27720 b^{10} x^{10} + 41580 a b^9 x^9 + 9240 a^2 b^8 x^8 - 2310 a^3 b^7 x^7 + 924 a^4 b^6 x^6 - 462 a^5 b^5 x^5 + 264 a^6 b^4 x^4 - 165 a^7 b^3 x^3}{504 (a^{11} b^2 x^{11} + 2 a^{12} b x^{10} + a^{13} x^9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^10/(b*x+a)^3,x, algorithm="maxima")`

[Out]
$$\frac{-1/504*(27720*b^{10}*x^{10} + 41580*a*b^9*x^9 + 9240*a^2*b^8*x^8 - 2310*a^3*b^7*x^7 + 924*a^4*b^6*x^6 - 462*a^5*b^5*x^5 + 264*a^6*b^4*x^4 - 165*a^7*b^3*x^3 + 110*a^8*b^2*x^2 - 77*a^9*b*x + 56*a^{10})/(a^{11}*b^2*x^{11} + 2*a^{12}*b*x^{10} + a^{13}*x^9) + 55*b^9*\log(b*x + a)/a^{12} - 55*b^9*\log(x)/a^{12}}$$

mupad [B] time = 0.23, size = 157, normalized size = 0.96

$$\frac{110 b^9 \operatorname{atanh}\left(\frac{2 b x}{a} + 1\right)}{a^{12}} - \frac{\frac{1}{9 a} + \frac{55 b^2 x^2}{252 a^3} - \frac{55 b^3 x^3}{168 a^4} + \frac{11 b^4 x^4}{21 a^5} - \frac{11 b^5 x^5}{12 a^6} + \frac{11 b^6 x^6}{6 a^7} - \frac{55 b^7 x^7}{12 a^8} + \frac{55 b^8 x^8}{3 a^9} + \frac{165 b^9 x^9}{2 a^{10}} + \frac{55 b^{10} x^{10}}{a^{11}}}{a^2 x^9 + 2 a b x^{10} + b^2 x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^10*(a + b*x)^3),x)`

[Out]
$$(110*b^9*\operatorname{atanh}((2*b*x)/a + 1))/a^{12} - (1/(9*a) + (55*b^2*x^2)/(252*a^3) - (55*b^3*x^3)/(168*a^4) + (11*b^4*x^4)/(21*a^5) - (11*b^5*x^5)/(12*a^6) + (11*b^6*x^6)/(6*a^7) - (55*b^7*x^7)/(12*a^8) + (55*b^8*x^8)/(3*a^9) + (165*b^9*x^9)/(2*a^{10}) + (55*b^{10}*x^{10})/a^{11} - (11*b*x)/(72*a^2))/(a^2*x^9 + b^2*x^{11} + 2*a*b*x^{10})$$

sympy [A] time = 0.68, size = 163, normalized size = 1.00

$$\frac{-56a^{10} + 77a^9bx - 110a^8b^2x^2 + 165a^7b^3x^3 - 264a^6b^4x^4 + 462a^5b^5x^5 - 924a^4b^6x^6 + 2310a^3b^7x^7 - 9240a^2b^8x^8 - 55b^9\ln(x)}{504a^{13}x^9 + 1008a^{12}bx^{10} + 504a^{11}b^2x^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**10/(b*x+a)**3,x)`

```
[Out] (-56*a**10 + 77*a**9*b*x - 110*a**8*b**2*x**2 + 165*a**7*b**3*x**3 - 264*a*  
*6*b**4*x**4 + 462*a**5*b**5*x**5 - 924*a**4*b**6*x**6 + 2310*a**3*b**7*x**  
7 - 9240*a**2*b**8*x**8 - 41580*a*b**9*x**9 - 27720*b**10*x**10)/(504*a**13  
*x**9 + 1008*a**12*b*x**10 + 504*a**11*b**2*x**11) + 55*b**9*(-log(x) + log  
(a/b + x))/a**12
```

$$3.255 \quad \int \frac{1}{x(2+3x)} dx$$

Optimal. Leaf size=17

$$\frac{\log(x)}{2} - \frac{1}{2} \log(3x + 2)$$

[Out] 1/2*ln(x)-1/2*ln(2+3*x)

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.273$, Rules used = {36, 29, 31}

$$\frac{\log(x)}{2} - \frac{1}{2} \log(3x + 2)$$

Antiderivative was successfully verified.

[In] Int[1/(x*(2 + 3*x)),x]

[Out] Log[x]/2 - Log[2 + 3*x]/2

Rule 29

Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] :> Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 36

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))), x_Symbol] :> Dist[b/(b*c - a*d), Int[1/(a + b*x), x], x] - Dist[d/(b*c - a*d), Int[1/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x(2+3x)} dx &= \frac{1}{2} \int \frac{1}{x} dx - \frac{3}{2} \int \frac{1}{2+3x} dx \\ &= \frac{\log(x)}{2} - \frac{1}{2} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{\log(x)}{2} - \frac{1}{2} \log(3x + 2)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(2 + 3*x)),x]

[Out] Log[x]/2 - Log[2 + 3*x]/2

fricas [A] time = 0.46, size = 13, normalized size = 0.76

$$-\frac{1}{2} \log(3x + 2) + \frac{1}{2} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(2+3*x),x, algorithm="fricas")

[Out] -1/2*log(3*x + 2) + 1/2*log(x)

giac [A] time = 1.15, size = 15, normalized size = 0.88

$$-\frac{1}{2} \log(|3x + 2|) + \frac{1}{2} \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(2+3*x),x, algorithm="giac")

[Out] -1/2*log(abs(3*x + 2)) + 1/2*log(abs(x))

maple [A] time = 0.01, size = 14, normalized size = 0.82

$$\frac{\ln(x)}{2} - \frac{\ln(3x + 2)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(2+3*x),x)

[Out] 1/2*ln(x)-1/2*ln(2+3*x)

maxima [A] time = 1.34, size = 13, normalized size = 0.76

$$-\frac{1}{2} \log(3x + 2) + \frac{1}{2} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(2+3*x),x, algorithm="maxima")

[Out] -1/2*log(3*x + 2) + 1/2*log(x)

mupad [B] time = 0.17, size = 10, normalized size = 0.59

$$-\frac{\ln\left(\frac{2}{x} + 3\right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(3*x + 2)),x)

[Out] -log(2/x + 3)/2

sympy [A] time = 0.12, size = 12, normalized size = 0.71

$$\frac{\log(x)}{2} - \frac{\log\left(x + \frac{2}{3}\right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(2+3*x),x)

[Out] log(x)/2 - log(x + 2/3)/2

$$3.256 \quad \int \frac{1}{x(4+6x)} dx$$

Optimal. Leaf size=17

$$\frac{\log(x)}{4} - \frac{1}{4} \log(3x + 2)$$

[Out] 1/4*ln(x)-1/4*ln(2+3*x)

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.273$, Rules used = {36, 29, 31}

$$\frac{\log(x)}{4} - \frac{1}{4} \log(3x + 2)$$

Antiderivative was successfully verified.

[In] Int[1/(x*(4 + 6*x)),x]

[Out] Log[x]/4 - Log[2 + 3*x]/4

Rule 29

Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]

Rule 31

Int[((a_) + (b_.)*(x_))^-1, x_Symbol] :> Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 36

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))), x_Symbol] :> Dist[b/(b*c - a*d), Int[1/(a + b*x), x], x] - Dist[d/(b*c - a*d), Int[1/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x(4+6x)} dx &= \frac{1}{4} \int \frac{1}{x} dx - \frac{3}{2} \int \frac{1}{4+6x} dx \\ &= \frac{\log(x)}{4} - \frac{1}{4} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{\log(x)}{4} - \frac{1}{4} \log(3x + 2)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(4 + 6*x)),x]

[Out] Log[x]/4 - Log[2 + 3*x]/4

fricas [A] time = 0.53, size = 13, normalized size = 0.76

$$-\frac{1}{4} \log(3x + 2) + \frac{1}{4} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(4+6*x),x, algorithm="fricas")

[Out] -1/4*log(3*x + 2) + 1/4*log(x)

giac [A] time = 1.01, size = 15, normalized size = 0.88

$$-\frac{1}{4} \log(|3x + 2|) + \frac{1}{4} \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(4+6*x),x, algorithm="giac")

[Out] -1/4*log(abs(3*x + 2)) + 1/4*log(abs(x))

maple [A] time = 0.00, size = 14, normalized size = 0.82

$$\frac{\ln(x)}{4} - \frac{\ln(3x + 2)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(4+6*x),x)

[Out] 1/4*ln(x)-1/4*ln(3*x+2)

maxima [A] time = 1.29, size = 13, normalized size = 0.76

$$-\frac{1}{4} \log(3x + 2) + \frac{1}{4} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(4+6*x),x, algorithm="maxima")

[Out] -1/4*log(3*x + 2) + 1/4*log(x)

mupad [B] time = 0.14, size = 10, normalized size = 0.59

$$-\frac{\ln\left(\frac{4}{x} + 6\right)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(6*x + 4)),x)

[Out] -log(4/x + 6)/4

sympy [A] time = 0.12, size = 12, normalized size = 0.71

$$\frac{\log(x)}{4} - \frac{\log\left(x + \frac{2}{3}\right)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(4+6*x),x)

[Out] log(x)/4 - log(x + 2/3)/4

$$3.257 \quad \int \frac{1}{x^2(4+6x)} dx$$

Optimal. Leaf size=24

$$-\frac{1}{4x} - \frac{3 \log(x)}{8} + \frac{3}{8} \log(3x + 2)$$

[Out] -1/4/x-3/8*ln(x)+3/8*ln(2+3*x)

Rubi [A] time = 0.01, antiderivative size = 24, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{1}{4x} - \frac{3 \log(x)}{8} + \frac{3}{8} \log(3x + 2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(4 + 6*x)),x]

[Out] -1/(4*x) - (3*Log[x])/8 + (3*Log[2 + 3*x])/8

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(4+6x)} dx &= \int \left(\frac{1}{4x^2} - \frac{3}{8x} + \frac{9}{8(2+3x)} \right) dx \\ &= -\frac{1}{4x} - \frac{3 \log(x)}{8} + \frac{3}{8} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 1.00

$$-\frac{1}{4x} - \frac{3 \log(x)}{8} + \frac{3}{8} \log(3x + 2)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(4 + 6*x)),x]

[Out] $-1/4*1/x - (3*\text{Log}[x])/8 + (3*\text{Log}[2 + 3*x])/8$

fricas [A] time = 0.53, size = 21, normalized size = 0.88

$$\frac{3x \log(3x + 2) - 3x \log(x) - 2}{8x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(4+6*x),x, algorithm="fricas")`

[Out] $1/8*(3*x*\log(3*x + 2) - 3*x*\log(x) - 2)/x$

giac [A] time = 1.01, size = 20, normalized size = 0.83

$$-\frac{1}{4x} + \frac{3}{8} \log(|3x + 2|) - \frac{3}{8} \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(4+6*x),x, algorithm="giac")`

[Out] $-1/4/x + 3/8*\log(\text{abs}(3*x + 2)) - 3/8*\log(\text{abs}(x))$

maple [A] time = 0.01, size = 19, normalized size = 0.79

$$-\frac{3 \ln(x)}{8} + \frac{3 \ln(3x + 2)}{8} - \frac{1}{4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^2/(4+6*x),x)`

[Out] $-1/4/x - 3/8*\ln(x) + 3/8*\ln(3*x+2)$

maxima [A] time = 1.38, size = 18, normalized size = 0.75

$$-\frac{1}{4x} + \frac{3}{8} \log(3x + 2) - \frac{3}{8} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(4+6*x),x, algorithm="maxima")`

[Out] $-1/4/x + 3/8*\log(3*x + 2) - 3/8*\log(x)$

mupad [B] time = 0.05, size = 18, normalized size = 0.75

$$-\frac{3 \ln\left(\frac{x}{6x+4}\right)}{8} - \frac{1}{4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^2*(6*x + 4)),x)`

[Out] `-(3*log(x/(6*x + 4)))/8 - 1/(4*x)`

sympy [A] time = 0.14, size = 20, normalized size = 0.83

$$-\frac{3\log(x)}{8} + \frac{3\log\left(x + \frac{2}{3}\right)}{8} - \frac{1}{4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(4+6*x),x)`

[Out] `-3*log(x)/8 + 3*log(x + 2/3)/8 - 1/(4*x)`

$$3.258 \quad \int \frac{1}{x^3(4+6x)} dx$$

Optimal. Leaf size=31

$$-\frac{1}{8x^2} + \frac{3}{8x} + \frac{9 \log(x)}{16} - \frac{9}{16} \log(3x + 2)$$

[Out] $-1/8/x^2+3/8/x+9/16*\ln(x)-9/16*\ln(2+3*x)$

Rubi [A] time = 0.01, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{1}{8x^2} + \frac{3}{8x} + \frac{9 \log(x)}{16} - \frac{9}{16} \log(3x + 2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(4 + 6*x)),x]

[Out] $-1/(8*x^2) + 3/(8*x) + (9*\text{Log}[x])/16 - (9*\text{Log}[2 + 3*x])/16$

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{1}{x^3(4+6x)} dx &= \int \left(\frac{1}{4x^3} - \frac{3}{8x^2} + \frac{9}{16x} - \frac{27}{16(2+3x)} \right) dx \\ &= -\frac{1}{8x^2} + \frac{3}{8x} + \frac{9 \log(x)}{16} - \frac{9}{16} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 31, normalized size = 1.00

$$-\frac{1}{8x^2} + \frac{3}{8x} + \frac{9 \log(x)}{16} - \frac{9}{16} \log(3x + 2)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(4 + 6*x)),x]

[Out] $-1/8*1/x^2 + 3/(8*x) + (9*\text{Log}[x])/16 - (9*\text{Log}[2 + 3*x])/16$

fricas [A] time = 0.52, size = 28, normalized size = 0.90

$$-\frac{9x^2 \log(3x + 2) - 9x^2 \log(x) - 6x + 2}{16x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(4+6*x),x, algorithm="fricas")

[Out] $-1/16*(9*x^2*\log(3*x + 2) - 9*x^2*\log(x) - 6*x + 2)/x^2$

giac [A] time = 1.07, size = 25, normalized size = 0.81

$$\frac{3x - 1}{8x^2} - \frac{9}{16} \log(|3x + 2|) + \frac{9}{16} \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(4+6*x),x, algorithm="giac")

[Out] $1/8*(3*x - 1)/x^2 - 9/16*\log(\text{abs}(3*x + 2)) + 9/16*\log(\text{abs}(x))$

maple [A] time = 0.01, size = 24, normalized size = 0.77

$$\frac{9 \ln(x)}{16} - \frac{9 \ln(3x + 2)}{16} + \frac{3}{8x} - \frac{1}{8x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(4+6*x),x)

[Out] $-1/8/x^2+3/8/x+9/16*\ln(x)-9/16*\ln(3*x+2)$

maxima [A] time = 1.29, size = 23, normalized size = 0.74

$$\frac{3x - 1}{8x^2} - \frac{9}{16} \log(3x + 2) + \frac{9}{16} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(4+6*x),x, algorithm="maxima")

[Out] $1/8*(3*x - 1)/x^2 - 9/16*\log(3*x + 2) + 9/16*\log(x)$

mupad [B] time = 0.04, size = 18, normalized size = 0.58

$$\frac{\frac{3x}{8} - \frac{1}{8}}{x^2} - \frac{9 \operatorname{atanh}(3x + 1)}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^3*(6*x + 4)),x)`

[Out] `((3*x)/8 - 1/8)/x^2 - (9*atanh(3*x + 1))/8`

sympy [A] time = 0.15, size = 26, normalized size = 0.84

$$\frac{9 \log(x)}{16} - \frac{9 \log\left(x + \frac{2}{3}\right)}{16} + \frac{3x - 1}{8x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**3/(4+6*x),x)`

[Out] `9*log(x)/16 - 9*log(x + 2/3)/16 + (3*x - 1)/(8*x**2)`

$$3.259 \quad \int \frac{1}{x^4(4+6x)} dx$$

Optimal. Leaf size=38

$$-\frac{1}{12x^3} + \frac{3}{16x^2} - \frac{9}{16x} - \frac{27 \log(x)}{32} + \frac{27}{32} \log(3x+2)$$

[Out] $-1/12/x^3+3/16/x^2-9/16/x-27/32*\ln(x)+27/32*\ln(2+3*x)$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{3}{16x^2} - \frac{1}{12x^3} - \frac{9}{16x} - \frac{27 \log(x)}{32} + \frac{27}{32} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^4*(4 + 6*x)),x]

[Out] $-1/(12*x^3) + 3/(16*x^2) - 9/(16*x) - (27*\text{Log}[x])/32 + (27*\text{Log}[2 + 3*x])/32$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^4(4+6x)} dx &= \int \left(\frac{1}{4x^4} - \frac{3}{8x^3} + \frac{9}{16x^2} - \frac{27}{32x} + \frac{81}{32(2+3x)} \right) dx \\ &= -\frac{1}{12x^3} + \frac{3}{16x^2} - \frac{9}{16x} - \frac{27 \log(x)}{32} + \frac{27}{32} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 38, normalized size = 1.00

$$-\frac{1}{12x^3} + \frac{3}{16x^2} - \frac{9}{16x} - \frac{27 \log(x)}{32} + \frac{27}{32} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^4*(4 + 6*x)),x]

[Out] $-1/12*1/x^3 + 3/(16*x^2) - 9/(16*x) - (27*\text{Log}[x])/32 + (27*\text{Log}[2 + 3*x])/32$

fricas [A] time = 0.47, size = 33, normalized size = 0.87

$$\frac{81x^3 \log(3x + 2) - 81x^3 \log(x) - 54x^2 + 18x - 8}{96x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(4+6*x),x, algorithm="fricas")

[Out] $1/96*(81*x^3*\log(3*x + 2) - 81*x^3*\log(x) - 54*x^2 + 18*x - 8)/x^3$

giac [A] time = 1.03, size = 30, normalized size = 0.79

$$-\frac{27x^2 - 9x + 4}{48x^3} + \frac{27}{32} \log(|3x + 2|) - \frac{27}{32} \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(4+6*x),x, algorithm="giac")

[Out] $-1/48*(27*x^2 - 9*x + 4)/x^3 + 27/32*\log(\text{abs}(3*x + 2)) - 27/32*\log(\text{abs}(x))$

maple [A] time = 0.01, size = 29, normalized size = 0.76

$$-\frac{27 \ln(x)}{32} + \frac{27 \ln(3x + 2)}{32} - \frac{9}{16x} + \frac{3}{16x^2} - \frac{1}{12x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^4/(4+6*x),x)

[Out] $-1/12/x^3+3/16/x^2-9/16/x-27/32*\ln(x)+27/32*\ln(3*x+2)$

maxima [A] time = 1.35, size = 28, normalized size = 0.74

$$-\frac{27x^2 - 9x + 4}{48x^3} + \frac{27}{32} \log(3x + 2) - \frac{27}{32} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(4+6*x),x, algorithm="maxima")

[Out] $-1/48*(27*x^2 - 9*x + 4)/x^3 + 27/32*\log(3*x + 2) - 27/32*\log(x)$

mupad [B] time = 0.09, size = 24, normalized size = 0.63

$$\frac{27 \operatorname{atanh}(3x + 1)}{16} - \frac{\frac{9x^2}{16} - \frac{3x}{16} + \frac{1}{12}}{x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^4*(6*x + 4)),x)`

[Out] `(27*atanh(3*x + 1))/16 - ((9*x^2)/16 - (3*x)/16 + 1/12)/x^3`

sympy [A] time = 0.16, size = 31, normalized size = 0.82

$$-\frac{27 \log(x)}{32} + \frac{27 \log\left(x + \frac{2}{3}\right)}{32} + \frac{-27x^2 + 9x - 4}{48x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**4/(4+6*x),x)`

[Out] `-27*log(x)/32 + 27*log(x + 2/3)/32 + (-27*x**2 + 9*x - 4)/(48*x**3)`

$$3.260 \quad \int \frac{1}{x^5(4+6x)} dx$$

Optimal. Leaf size=45

$$-\frac{1}{16x^4} + \frac{1}{8x^3} - \frac{9}{32x^2} + \frac{27}{32x} + \frac{81 \log(x)}{64} - \frac{81}{64} \log(3x+2)$$

[Out] $-1/16/x^4+1/8/x^3-9/32/x^2+27/32/x+81/64*\ln(x)-81/64*\ln(2+3*x)$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{9}{32x^2} + \frac{1}{8x^3} - \frac{1}{16x^4} + \frac{27}{32x} + \frac{81 \log(x)}{64} - \frac{81}{64} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^5*(4 + 6*x)), x]

[Out] $-1/(16*x^4) + 1/(8*x^3) - 9/(32*x^2) + 27/(32*x) + (81*\text{Log}[x])/64 - (81*\text{Log}[2 + 3*x])/64$

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^5(4+6x)} dx &= \int \left(\frac{1}{4x^5} - \frac{3}{8x^4} + \frac{9}{16x^3} - \frac{27}{32x^2} + \frac{81}{64x} - \frac{243}{64(2+3x)} \right) dx \\ &= -\frac{1}{16x^4} + \frac{1}{8x^3} - \frac{9}{32x^2} + \frac{27}{32x} + \frac{81 \log(x)}{64} - \frac{81}{64} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.00, size = 45, normalized size = 1.00

$$-\frac{1}{16x^4} + \frac{1}{8x^3} - \frac{9}{32x^2} + \frac{27}{32x} + \frac{81 \log(x)}{64} - \frac{81}{64} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^5*(4 + 6*x)),x]

[Out] $-1/16*1/x^4 + 1/(8*x^3) - 9/(32*x^2) + 27/(32*x) + (81*\text{Log}[x])/64 - (81*\text{Log}[2 + 3*x])/64$

fricas [A] time = 0.48, size = 38, normalized size = 0.84

$$-\frac{81x^4 \log(3x+2) - 81x^4 \log(x) - 54x^3 + 18x^2 - 8x + 4}{64x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(4+6*x),x, algorithm="fricas")

[Out] $-1/64*(81*x^4*\log(3*x + 2) - 81*x^4*\log(x) - 54*x^3 + 18*x^2 - 8*x + 4)/x^4$

giac [A] time = 1.14, size = 35, normalized size = 0.78

$$\frac{27x^3 - 9x^2 + 4x - 2}{32x^4} - \frac{81}{64} \log(|3x+2|) + \frac{81}{64} \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(4+6*x),x, algorithm="giac")

[Out] $1/32*(27*x^3 - 9*x^2 + 4*x - 2)/x^4 - 81/64*\log(\text{abs}(3*x + 2)) + 81/64*\log(\text{abs}(x))$

maple [A] time = 0.01, size = 34, normalized size = 0.76

$$\frac{81 \ln(x)}{64} - \frac{81 \ln(3x+2)}{64} + \frac{27}{32x} - \frac{9}{32x^2} + \frac{1}{8x^3} - \frac{1}{16x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^5/(4+6*x),x)

[Out] $-1/16/x^4+1/8/x^3-9/32/x^2+27/32/x+81/64*\ln(x)-81/64*\ln(3*x+2)$

maxima [A] time = 1.32, size = 33, normalized size = 0.73

$$\frac{27x^3 - 9x^2 + 4x - 2}{32x^4} - \frac{81}{64} \log(3x+2) + \frac{81}{64} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(4+6*x),x, algorithm="maxima")

[Out] $1/32*(27*x^3 - 9*x^2 + 4*x - 2)/x^4 - 81/64*\log(3*x + 2) + 81/64*\log(x)$

mupad [B] time = 0.04, size = 28, normalized size = 0.62

$$\frac{\frac{27x^3}{32} - \frac{9x^2}{32} + \frac{x}{8} - \frac{1}{16}}{x^4} - \frac{81 \operatorname{atanh}(3x + 1)}{32}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^5*(6*x + 4)), x)`

[Out] $(x/8 - (9*x^2)/32 + (27*x^3)/32 - 1/16)/x^4 - (81*\operatorname{atanh}(3*x + 1))/32$

sympy [A] time = 0.17, size = 36, normalized size = 0.80

$$\frac{81 \log(x)}{64} - \frac{81 \log\left(x + \frac{2}{3}\right)}{64} + \frac{27x^3 - 9x^2 + 4x - 2}{32x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**5/(4+6*x), x)`

[Out] $81*\log(x)/64 - 81*\log(x + 2/3)/64 + (27*x**3 - 9*x**2 + 4*x - 2)/(32*x**4)$

$$3.261 \quad \int \frac{1}{x(4+6x)^2} dx$$

Optimal. Leaf size=28

$$\frac{1}{8(3x+2)} + \frac{\log(x)}{16} - \frac{1}{16} \log(3x+2)$$

[Out] 1/8/(2+3*x)+1/16*ln(x)-1/16*ln(2+3*x)

Rubi [A] time = 0.01, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{1}{8(3x+2)} + \frac{\log(x)}{16} - \frac{1}{16} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x*(4 + 6*x)^2), x]

[Out] 1/(8*(2 + 3*x)) + Log[x]/16 - Log[2 + 3*x]/16

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x(4+6x)^2} dx &= \int \left(\frac{1}{16x} - \frac{3}{8(2+3x)^2} - \frac{3}{16(2+3x)} \right) dx \\ &= \frac{1}{8(2+3x)} + \frac{\log(x)}{16} - \frac{1}{16} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 0.93

$$\frac{1}{16} \left(\frac{2}{3x+2} + \log(-6x) - \log(6x+4) \right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(4 + 6*x)^2),x]

[Out] (2/(2 + 3*x) + Log[-6*x] - Log[4 + 6*x])/16

fricas [A] time = 0.45, size = 32, normalized size = 1.14

$$\frac{(3x + 2)\log(3x + 2) - (3x + 2)\log(x) - 2}{16(3x + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(4+6*x)^2,x, algorithm="fricas")

[Out] -1/16*((3*x + 2)*log(3*x + 2) - (3*x + 2)*log(x) - 2)/(3*x + 2)

giac [A] time = 1.11, size = 25, normalized size = 0.89

$$\frac{1}{8(3x + 2)} + \frac{1}{16} \log\left(\left|-\frac{2}{3x + 2} + 1\right|\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(4+6*x)^2,x, algorithm="giac")

[Out] 1/8/(3*x + 2) + 1/16*log(abs(-2/(3*x + 2) + 1))

maple [A] time = 0.01, size = 23, normalized size = 0.82

$$\frac{\ln(x)}{16} - \frac{\ln(3x + 2)}{16} + \frac{1}{24x + 16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(4+6*x)^2,x)

[Out] 1/8/(3*x+2)+1/16*ln(x)-1/16*ln(3*x+2)

maxima [A] time = 1.37, size = 22, normalized size = 0.79

$$\frac{1}{8(3x + 2)} - \frac{1}{16} \log(3x + 2) + \frac{1}{16} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(4+6*x)^2,x, algorithm="maxima")

[Out] 1/8/(3*x + 2) - 1/16*log(3*x + 2) + 1/16*log(x)

mupad [B] time = 0.06, size = 20, normalized size = 0.71

$$\frac{1}{8(3x+2)} - \frac{\ln\left(\frac{6x+4}{x}\right)}{16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(6*x + 4)^2),x)`

[Out] `1/(8*(3*x + 2)) - log((6*x + 4)/x)/16`

sympy [A] time = 0.14, size = 19, normalized size = 0.68

$$\frac{\log(x)}{16} - \frac{\log\left(x + \frac{2}{3}\right)}{16} + \frac{1}{24x + 16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(4+6*x)**2,x)`

[Out] `log(x)/16 - log(x + 2/3)/16 + 1/(24*x + 16)`

$$3.262 \quad \int \frac{1}{x^2(4+6x)^2} dx$$

Optimal. Leaf size=35

$$-\frac{1}{16x} - \frac{3}{16(3x+2)} - \frac{3 \log(x)}{16} + \frac{3}{16} \log(3x+2)$$

[Out] -1/16/x-3/16/(2+3*x)-3/16*ln(x)+3/16*ln(2+3*x)

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{1}{16x} - \frac{3}{16(3x+2)} - \frac{3 \log(x)}{16} + \frac{3}{16} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(4 + 6*x)^2), x]

[Out] -1/(16*x) - 3/(16*(2 + 3*x)) - (3*Log[x])/16 + (3*Log[2 + 3*x])/16

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(4+6x)^2} dx &= \int \left(\frac{1}{16x^2} - \frac{3}{16x} + \frac{9}{16(2+3x)^2} + \frac{9}{16(2+3x)} \right) dx \\ &= -\frac{1}{16x} - \frac{3}{16(2+3x)} - \frac{3 \log(x)}{16} + \frac{3}{16} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 0.89

$$\frac{1}{16} \left(-\frac{1}{x} - \frac{3}{3x+2} - 3 \log(x) + 3 \log(3x+2) \right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(4 + 6*x)^2), x]

[Out] $(-x^{(-1)} - 3/(2 + 3*x) - 3*\text{Log}[x] + 3*\text{Log}[2 + 3*x])/16$

fricas [A] time = 0.50, size = 48, normalized size = 1.37

$$\frac{3(3x^2 + 2x)\log(3x + 2) - 3(3x^2 + 2x)\log(x) - 6x - 2}{16(3x^2 + 2x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(4+6*x)^2,x, algorithm="fricas")

[Out] $1/16*(3*(3*x^2 + 2*x)*\log(3*x + 2) - 3*(3*x^2 + 2*x)*\log(x) - 6*x - 2)/(3*x^2 + 2*x)$

giac [A] time = 0.95, size = 40, normalized size = 1.14

$$-\frac{3}{16(3x + 2)} + \frac{3}{32\left(\frac{2}{3x+2} - 1\right)} - \frac{3}{16} \log\left(\left|-\frac{2}{3x+2} + 1\right|\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(4+6*x)^2,x, algorithm="giac")

[Out] $-3/16/(3*x + 2) + 3/32/(2/(3*x + 2) - 1) - 3/16*\log(\text{abs}(-2/(3*x + 2) + 1))$

maple [A] time = 0.01, size = 28, normalized size = 0.80

$$-\frac{3 \ln(x)}{16} + \frac{3 \ln(3x + 2)}{16} - \frac{1}{16x} - \frac{3}{16(3x + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(4+6*x)^2,x)

[Out] $-1/16/x - 3/16/(3*x+2) - 3/16*\ln(x) + 3/16*\ln(3*x+2)$

maxima [A] time = 1.39, size = 31, normalized size = 0.89

$$-\frac{3x + 1}{8(3x^2 + 2x)} + \frac{3}{16} \log(3x + 2) - \frac{3}{16} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(4+6*x)^2,x, algorithm="maxima")

[Out] $-1/8*(3*x + 1)/(3*x^2 + 2*x) + 3/16*\log(3*x + 2) - 3/16*\log(x)$

mupad [B] time = 0.09, size = 34, normalized size = 0.97

$$\frac{3 \ln\left(\frac{6x+4}{x}\right)}{16} - \frac{3}{4(6x+4)} - \frac{1}{4x(6x+4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^2*(6*x + 4)^2),x)`

[Out] $(3*\log((6*x + 4)/x))/16 - 3/(4*(6*x + 4)) - 1/(4*x*(6*x + 4))$

sympy [A] time = 0.15, size = 31, normalized size = 0.89

$$\frac{-3x-1}{24x^2+16x} - \frac{3\log(x)}{16} + \frac{3\log\left(x + \frac{2}{3}\right)}{16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(4+6*x)**2,x)`

[Out] $(-3*x - 1)/(24*x**2 + 16*x) - 3*\log(x)/16 + 3*\log(x + 2/3)/16$

$$3.263 \quad \int \frac{1}{x^3(4+6x)^2} dx$$

Optimal. Leaf size=42

$$-\frac{1}{32x^2} + \frac{3}{16x} + \frac{9}{32(3x+2)} + \frac{27 \log(x)}{64} - \frac{27}{64} \log(3x+2)$$

[Out] $-1/32/x^2+3/16/x+9/32/(2+3*x)+27/64*\ln(x)-27/64*\ln(2+3*x)$

Rubi [A] time = 0.01, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{1}{32x^2} + \frac{3}{16x} + \frac{9}{32(3x+2)} + \frac{27 \log(x)}{64} - \frac{27}{64} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(4 + 6*x)^2), x]

[Out] $-1/(32*x^2) + 3/(16*x) + 9/(32*(2 + 3*x)) + (27*\text{Log}[x])/64 - (27*\text{Log}[2 + 3*x])/64$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] & & ILtQ[m, 0] & & IntegerQ[n] & & !(IGtQ[n, 0] & & LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^3(4+6x)^2} dx &= \int \left(\frac{1}{16x^3} - \frac{3}{16x^2} + \frac{27}{64x} - \frac{27}{32(2+3x)^2} - \frac{81}{64(2+3x)} \right) dx \\ &= -\frac{1}{32x^2} + \frac{3}{16x} + \frac{9}{32(2+3x)} + \frac{27 \log(x)}{64} - \frac{27}{64} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 36, normalized size = 0.86

$$\frac{1}{64} \left(-\frac{2}{x^2} + \frac{12}{x} + \frac{18}{3x+2} + 27 \log(x) - 27 \log(3x+2) \right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(4 + 6*x)^2),x]

[Out] (-2/x^2 + 12/x + 18/(2 + 3*x) + 27*Log[x] - 27*Log[2 + 3*x])/64

fricas [A] time = 0.47, size = 59, normalized size = 1.40

$$\frac{54x^2 - 27(3x^3 + 2x^2)\log(3x + 2) + 27(3x^3 + 2x^2)\log(x) + 18x - 4}{64(3x^3 + 2x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(4+6*x)^2,x, algorithm="fricas")

[Out] 1/64*(54*x^2 - 27*(3*x^3 + 2*x^2)*log(3*x + 2) + 27*(3*x^3 + 2*x^2)*log(x) + 18*x - 4)/(3*x^3 + 2*x^2)

giac [A] time = 0.94, size = 51, normalized size = 1.21

$$\frac{9}{32(3x + 2)} - \frac{9\left(\frac{12}{3x+2} - 5\right)}{128\left(\frac{2}{3x+2} - 1\right)^2} + \frac{27}{64} \log\left(\left|-\frac{2}{3x+2} + 1\right|\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(4+6*x)^2,x, algorithm="giac")

[Out] 9/32/(3*x + 2) - 9/128*(12/(3*x + 2) - 5)/(2/(3*x + 2) - 1)^2 + 27/64*log(abs(-2/(3*x + 2) + 1))

maple [A] time = 0.01, size = 33, normalized size = 0.79

$$\frac{27\ln(x)}{64} - \frac{27\ln(3x + 2)}{64} + \frac{3}{16x} - \frac{1}{32x^2} + \frac{9}{32(3x + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(4+6*x)^2,x)

[Out] -1/32/x^2+3/16/x+9/32/(3*x+2)+27/64*ln(x)-27/64*ln(3*x+2)

maxima [A] time = 1.31, size = 38, normalized size = 0.90

$$\frac{27x^2 + 9x - 2}{32(3x^3 + 2x^2)} - \frac{27}{64} \log(3x + 2) + \frac{27}{64} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(4+6*x)^2,x, algorithm="maxima")

[Out] 1/32*(27*x^2 + 9*x - 2)/(3*x^3 + 2*x^2) - 27/64*log(3*x + 2) + 27/64*log(x)

mupad [B] time = 0.04, size = 31, normalized size = 0.74

$$\frac{\frac{9x^2}{32} + \frac{3x}{32} - \frac{1}{48}}{x^3 + \frac{2x^2}{3}} - \frac{27 \operatorname{atanh}(3x + 1)}{32}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(6*x + 4)^2),x)

[Out] ((3*x)/32 + (9*x^2)/32 - 1/48)/((2*x^2)/3 + x^3) - (27*atanh(3*x + 1))/32

sympy [A] time = 0.16, size = 36, normalized size = 0.86

$$\frac{27 \log(x)}{64} - \frac{27 \log\left(x + \frac{2}{3}\right)}{64} + \frac{27x^2 + 9x - 2}{96x^3 + 64x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(4+6*x)**2,x)

[Out] 27*log(x)/64 - 27*log(x + 2/3)/64 + (27*x**2 + 9*x - 2)/(96*x**3 + 64*x**2)

$$3.264 \quad \int \frac{1}{x^4(4+6x)^2} dx$$

Optimal. Leaf size=49

$$-\frac{1}{48x^3} + \frac{3}{32x^2} - \frac{27}{64x} - \frac{27}{64(3x+2)} - \frac{27 \log(x)}{32} + \frac{27}{32} \log(3x+2)$$

[Out] $-1/48/x^3+3/32/x^2-27/64/x-27/64/(2+3*x)-27/32*\ln(x)+27/32*\ln(2+3*x)$

Rubi [A] time = 0.02, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{3}{32x^2} - \frac{1}{48x^3} - \frac{27}{64x} - \frac{27}{64(3x+2)} - \frac{27 \log(x)}{32} + \frac{27}{32} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^4*(4 + 6*x)^2), x]

[Out] $-1/(48*x^3) + 3/(32*x^2) - 27/(64*x) - 27/(64*(2 + 3*x)) - (27*\text{Log}[x])/32 + (27*\text{Log}[2 + 3*x])/32$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^4(4+6x)^2} dx &= \int \left(\frac{1}{16x^4} - \frac{3}{16x^3} + \frac{27}{64x^2} - \frac{27}{32x} + \frac{81}{64(2+3x)^2} + \frac{81}{32(2+3x)} \right) dx \\ &= -\frac{1}{48x^3} + \frac{3}{32x^2} - \frac{27}{64x} - \frac{27}{64(2+3x)} - \frac{27 \log(x)}{32} + \frac{27}{32} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.03, size = 44, normalized size = 0.90

$$\frac{1}{192} \left(-\frac{4(81x^3 + 27x^2 - 6x + 2)}{x^3(3x+2)} - 162 \log(x) + 162 \log(3x+2) \right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^4*(4 + 6*x)^2),x]

[Out] ((-4*(2 - 6*x + 27*x^2 + 81*x^3))/(x^3*(2 + 3*x)) - 162*Log[x] + 162*Log[2 + 3*x])/192

fricas [A] time = 0.44, size = 64, normalized size = 1.31

$$\frac{162x^3 + 54x^2 - 81(3x^4 + 2x^3)\log(3x + 2) + 81(3x^4 + 2x^3)\log(x) - 12x + 4}{96(3x^4 + 2x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(4+6*x)^2,x, algorithm="fricas")

[Out] -1/96*(162*x^3 + 54*x^2 - 81*(3*x^4 + 2*x^3)*log(3*x + 2) + 81*(3*x^4 + 2*x^3)*log(x) - 12*x + 4)/(3*x^4 + 2*x^3)

giac [A] time = 1.23, size = 60, normalized size = 1.22

$$-\frac{27}{64(3x + 2)} - \frac{9\left(\frac{60}{3x+2} - \frac{72}{(3x+2)^2} - 13\right)}{128\left(\frac{2}{3x+2} - 1\right)^3} - \frac{27}{32} \log\left(\left|-\frac{2}{3x+2} + 1\right|\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(4+6*x)^2,x, algorithm="giac")

[Out] -27/64/(3*x + 2) - 9/128*(60/(3*x + 2) - 72/(3*x + 2)^2 - 13)/(2/(3*x + 2) - 1)^3 - 27/32*log(abs(-2/(3*x + 2) + 1))

maple [A] time = 0.01, size = 38, normalized size = 0.78

$$-\frac{27 \ln(x)}{32} + \frac{27 \ln(3x + 2)}{32} - \frac{27}{64x} + \frac{3}{32x^2} - \frac{1}{48x^3} - \frac{27}{64(3x + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^4/(4+6*x)^2,x)

[Out] -1/48/x^3+3/32/x^2-27/64/x-27/64/(3*x+2)-27/32*ln(x)+27/32*ln(3*x+2)

maxima [A] time = 1.31, size = 43, normalized size = 0.88

$$-\frac{81x^3 + 27x^2 - 6x + 2}{48(3x^4 + 2x^3)} + \frac{27}{32} \log(3x + 2) - \frac{27}{32} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^4/(4+6*x)^2,x, algorithm="maxima")`

[Out] $-1/48*(81*x^3 + 27*x^2 - 6*x + 2)/(3*x^4 + 2*x^3) + 27/32*\log(3*x + 2) - 27/32*\log(x)$

mupad [B] time = 0.09, size = 37, normalized size = 0.76

$$\frac{27 \operatorname{atanh}(3x + 1)}{16} - \frac{\frac{9x^3}{16} + \frac{3x^2}{16} - \frac{x}{24} + \frac{1}{72}}{x^4 + \frac{2x^3}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^4*(6*x + 4)^2),x)`

[Out] $(27*\operatorname{atanh}(3*x + 1))/16 - ((3*x^2)/16 - x/24 + (9*x^3)/16 + 1/72)/((2*x^3)/3 + x^4)$

sympy [A] time = 0.17, size = 41, normalized size = 0.84

$$-\frac{27 \log(x)}{32} + \frac{27 \log\left(x + \frac{2}{3}\right)}{32} + \frac{-81x^3 - 27x^2 + 6x - 2}{144x^4 + 96x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**4/(4+6*x)**2,x)`

[Out] $-27*\log(x)/32 + 27*\log(x + 2/3)/32 + (-81*x**3 - 27*x**2 + 6*x - 2)/(144*x**4 + 96*x**3)$

$$3.265 \quad \int \frac{1}{x^5(4+6x)^2} dx$$

Optimal. Leaf size=56

$$-\frac{1}{64x^4} + \frac{1}{16x^3} - \frac{27}{128x^2} + \frac{27}{32x} + \frac{81}{128(3x+2)} + \frac{405 \log(x)}{256} - \frac{405}{256} \log(3x+2)$$

[Out] $-1/64/x^4+1/16/x^3-27/128/x^2+27/32/x+81/128/(2+3*x)+405/256*\ln(x)-405/256*\ln(2+3*x)$

Rubi [A] time = 0.02, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{27}{128x^2} + \frac{1}{16x^3} - \frac{1}{64x^4} + \frac{27}{32x} + \frac{81}{128(3x+2)} + \frac{405 \log(x)}{256} - \frac{405}{256} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^5*(4 + 6*x)^2), x]

[Out] $-1/(64*x^4) + 1/(16*x^3) - 27/(128*x^2) + 27/(32*x) + 81/(128*(2 + 3*x)) + (405*\text{Log}[x])/256 - (405*\text{Log}[2 + 3*x])/256$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^5(4+6x)^2} dx &= \int \left(\frac{1}{16x^5} - \frac{3}{16x^4} + \frac{27}{64x^3} - \frac{27}{32x^2} + \frac{405}{256x} - \frac{243}{128(2+3x)^2} - \frac{1215}{256(2+3x)} \right) dx \\ &= -\frac{1}{64x^4} + \frac{1}{16x^3} - \frac{27}{128x^2} + \frac{27}{32x} + \frac{81}{128(2+3x)} + \frac{405 \log(x)}{256} - \frac{405}{256} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 56, normalized size = 1.00

$$-\frac{1}{64x^4} + \frac{1}{16x^3} - \frac{27}{128x^2} + \frac{27}{32x} + \frac{81}{128(3x+2)} + \frac{405 \log(x)}{256} - \frac{405}{256} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^5*(4 + 6*x)^2),x]

[Out] $-1/64*1/x^4 + 1/(16*x^3) - 27/(128*x^2) + 27/(32*x) + 81/(128*(2 + 3*x)) + (405*\text{Log}[x])/256 - (405*\text{Log}[2 + 3*x])/256$

fricas [A] time = 0.49, size = 69, normalized size = 1.23

$$\frac{810x^4 + 270x^3 - 60x^2 - 405(3x^5 + 2x^4)\log(3x + 2) + 405(3x^5 + 2x^4)\log(x) + 20x - 8}{256(3x^5 + 2x^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(4+6*x)^2,x, algorithm="fricas")

[Out] $1/256*(810*x^4 + 270*x^3 - 60*x^2 - 405*(3*x^5 + 2*x^4)*\log(3*x + 2) + 405*(3*x^5 + 2*x^4)*\log(x) + 20*x - 8)/(3*x^5 + 2*x^4)$

giac [A] time = 1.15, size = 69, normalized size = 1.23

$$\frac{81}{128(3x + 2)} - \frac{27\left(\frac{520}{3x+2} - \frac{1200}{(3x+2)^2} + \frac{960}{(3x+2)^3} - 77\right)}{1024\left(\frac{2}{3x+2} - 1\right)^4} + \frac{405}{256} \log\left(\left|-\frac{2}{3x+2} + 1\right|\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(4+6*x)^2,x, algorithm="giac")

[Out] $81/128/(3*x + 2) - 27/1024*(520/(3*x + 2) - 1200/(3*x + 2)^2 + 960/(3*x + 2)^3 - 77)/(2/(3*x + 2) - 1)^4 + 405/256*\log(\text{abs}(-2/(3*x + 2) + 1))$

maple [A] time = 0.01, size = 43, normalized size = 0.77

$$\frac{405 \ln(x)}{256} - \frac{405 \ln(3x + 2)}{256} + \frac{27}{32x} - \frac{27}{128x^2} + \frac{1}{16x^3} - \frac{1}{64x^4} + \frac{81}{128(3x + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^5/(4+6*x)^2,x)

[Out] $-1/64/x^4 + 1/16/x^3 - 27/128/x^2 + 27/32/x + 81/128/(3*x+2) + 405/256*\ln(x) - 405/256*\ln(3*x+2)$

maxima [A] time = 1.36, size = 48, normalized size = 0.86

$$\frac{405x^4 + 135x^3 - 30x^2 + 10x - 4}{128(3x^5 + 2x^4)} - \frac{405}{256} \log(3x + 2) + \frac{405}{256} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(4+6*x)^2,x, algorithm="maxima")

[Out] 1/128*(405*x^4 + 135*x^3 - 30*x^2 + 10*x - 4)/(3*x^5 + 2*x^4) - 405/256*log(3*x + 2) + 405/256*log(x)

mupad [B] time = 0.09, size = 41, normalized size = 0.73

$$\frac{\frac{135x^4}{128} + \frac{45x^3}{128} - \frac{5x^2}{64} + \frac{5x}{192} - \frac{1}{96}}{x^5 + \frac{2x^4}{3}} - \frac{405 \operatorname{atanh}(3x + 1)}{128}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^5*(6*x + 4)^2),x)

[Out] ((5*x)/192 - (5*x^2)/64 + (45*x^3)/128 + (135*x^4)/128 - 1/96)/((2*x^4)/3 + x^5) - (405*atanh(3*x + 1))/128

sympy [A] time = 0.18, size = 46, normalized size = 0.82

$$\frac{405 \log(x)}{256} - \frac{405 \log\left(x + \frac{2}{3}\right)}{256} + \frac{405x^4 + 135x^3 - 30x^2 + 10x - 4}{384x^5 + 256x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**5/(4+6*x)**2,x)

[Out] 405*log(x)/256 - 405*log(x + 2/3)/256 + (405*x**4 + 135*x**3 - 30*x**2 + 10*x - 4)/(384*x**5 + 256*x**4)

$$3.266 \quad \int \frac{1}{x(4+6x)^3} dx$$

Optimal. Leaf size=39

$$\frac{1}{32(3x+2)} + \frac{1}{32(3x+2)^2} + \frac{\log(x)}{64} - \frac{1}{64} \log(3x+2)$$

[Out] 1/32/(2+3*x)^2+1/32/(2+3*x)+1/64*ln(x)-1/64*ln(2+3*x)

Rubi [A] time = 0.01, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{1}{32(3x+2)} + \frac{1}{32(3x+2)^2} + \frac{\log(x)}{64} - \frac{1}{64} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x*(4 + 6*x)^3), x]

[Out] 1/(32*(2 + 3*x)^2) + 1/(32*(2 + 3*x)) + Log[x]/64 - Log[2 + 3*x]/64

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x(4+6x)^3} dx &= \int \left(\frac{1}{64x} - \frac{3}{16(2+3x)^3} - \frac{3}{32(2+3x)^2} - \frac{3}{64(2+3x)} \right) dx \\ &= \frac{1}{32(2+3x)^2} + \frac{1}{32(2+3x)} + \frac{\log(x)}{64} - \frac{1}{64} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.02, size = 29, normalized size = 0.74

$$\frac{1}{64} \left(\frac{6(x+1)}{(3x+2)^2} + \log(-6x) - \log(6x+4) \right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(4 + 6*x)^3), x]

[Out] ((6*(1 + x))/(2 + 3*x)^2 + Log[-6*x] - Log[4 + 6*x])/64

fricas [A] time = 0.49, size = 50, normalized size = 1.28

$$\frac{(9x^2 + 12x + 4)\log(3x + 2) - (9x^2 + 12x + 4)\log(x) - 6x - 6}{64(9x^2 + 12x + 4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(4+6*x)^3,x, algorithm="fricas")

[Out] -1/64*((9*x^2 + 12*x + 4)*log(3*x + 2) - (9*x^2 + 12*x + 4)*log(x) - 6*x - 6)/(9*x^2 + 12*x + 4)

giac [A] time = 1.03, size = 27, normalized size = 0.69

$$\frac{3(x+1)}{32(3x+2)^2} - \frac{1}{64}\log(|3x+2|) + \frac{1}{64}\log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(4+6*x)^3,x, algorithm="giac")

[Out] 3/32*(x + 1)/(3*x + 2)^2 - 1/64*log(abs(3*x + 2)) + 1/64*log(abs(x))

maple [A] time = 0.01, size = 32, normalized size = 0.82

$$\frac{\ln(x)}{64} - \frac{\ln(3x+2)}{64} + \frac{1}{32(3x+2)^2} + \frac{1}{96x+64}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(4+6*x)^3,x)

[Out] 1/32/(3*x+2)^2+1/32/(3*x+2)+1/64*ln(x)-1/64*ln(3*x+2)

maxima [A] time = 1.39, size = 30, normalized size = 0.77

$$\frac{3(x+1)}{32(9x^2 + 12x + 4)} - \frac{1}{64}\log(3x+2) + \frac{1}{64}\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(4+6*x)^3,x, algorithm="maxima")

[Out] 3/32*(x + 1)/(9*x^2 + 12*x + 4) - 1/64*log(3*x + 2) + 1/64*log(x)

mupad [B] time = 0.13, size = 29, normalized size = 0.74

$$\frac{1}{32(3x+2)} - \frac{\ln\left(\frac{6x+4}{x}\right)}{64} + \frac{1}{8(6x+4)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(6*x + 4)^3), x)`

[Out] `1/(32*(3*x + 2)) - log((6*x + 4)/x)/64 + 1/(8*(6*x + 4)^2)`

sympy [A] time = 0.17, size = 27, normalized size = 0.69

$$\frac{3x+3}{288x^2+384x+128} + \frac{\log(x)}{64} - \frac{\log\left(x + \frac{2}{3}\right)}{64}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(4+6*x)**3, x)`

[Out] `(3*x + 3)/(288*x**2 + 384*x + 128) + log(x)/64 - log(x + 2/3)/64`

$$3.267 \quad \int \frac{1}{x^2(4+6x)^3} dx$$

Optimal. Leaf size=46

$$-\frac{1}{64x} - \frac{3}{32(3x+2)} - \frac{3}{64(3x+2)^2} - \frac{9\log(x)}{128} + \frac{9}{128}\log(3x+2)$$

[Out] -1/64/x-3/64/(2+3*x)^2-3/32/(2+3*x)-9/128*ln(x)+9/128*ln(2+3*x)

Rubi [A] time = 0.02, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{1}{64x} - \frac{3}{32(3x+2)} - \frac{3}{64(3x+2)^2} - \frac{9\log(x)}{128} + \frac{9}{128}\log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(4 + 6*x)^3), x]

[Out] -1/(64*x) - 3/(64*(2 + 3*x)^2) - 3/(32*(2 + 3*x)) - (9*Log[x])/128 + (9*Log[2 + 3*x])/128

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(4+6x)^3} dx &= \int \left(\frac{1}{64x^2} - \frac{9}{128x} + \frac{9}{32(2+3x)^3} + \frac{9}{32(2+3x)^2} + \frac{27}{128(2+3x)} \right) dx \\ &= -\frac{1}{64x} - \frac{3}{64(2+3x)^2} - \frac{3}{32(2+3x)} - \frac{9\log(x)}{128} + \frac{9}{128}\log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.02, size = 39, normalized size = 0.85

$$\frac{1}{128} \left(-\frac{2(27x^2 + 27x + 4)}{x(3x+2)^2} - 9\log(x) + 9\log(3x+2) \right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(4 + 6*x)^3),x]

[Out] ((-2*(4 + 27*x + 27*x^2))/(x*(2 + 3*x)^2) - 9*Log[x] + 9*Log[2 + 3*x])/128

fricas [A] time = 0.48, size = 68, normalized size = 1.48

$$\frac{54x^2 - 9(9x^3 + 12x^2 + 4x)\log(3x + 2) + 9(9x^3 + 12x^2 + 4x)\log(x) + 54x + 8}{128(9x^3 + 12x^2 + 4x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(4+6*x)^3,x, algorithm="fricas")

[Out] -1/128*(54*x^2 - 9*(9*x^3 + 12*x^2 + 4*x)*log(3*x + 2) + 9*(9*x^3 + 12*x^2 + 4*x)*log(x) + 54*x + 8)/(9*x^3 + 12*x^2 + 4*x)

giac [A] time = 0.89, size = 37, normalized size = 0.80

$$-\frac{27x^2 + 27x + 4}{64(3x + 2)^2x} + \frac{9}{128} \log(|3x + 2|) - \frac{9}{128} \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(4+6*x)^3,x, algorithm="giac")

[Out] -1/64*(27*x^2 + 27*x + 4)/((3*x + 2)^2*x) + 9/128*log(abs(3*x + 2)) - 9/128*log(abs(x))

maple [A] time = 0.01, size = 37, normalized size = 0.80

$$-\frac{9 \ln(x)}{128} + \frac{9 \ln(3x + 2)}{128} - \frac{1}{64x} - \frac{3}{64(3x + 2)^2} - \frac{3}{32(3x + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(4+6*x)^3,x)

[Out] -1/64/x-3/64/(3*x+2)^2-3/32/(3*x+2)-9/128*ln(x)+9/128*ln(3*x+2)

maxima [A] time = 1.39, size = 41, normalized size = 0.89

$$-\frac{27x^2 + 27x + 4}{64(9x^3 + 12x^2 + 4x)} + \frac{9}{128} \log(3x + 2) - \frac{9}{128} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(4+6*x)^3,x, algorithm="maxima")

[Out] $-1/64*(27*x^2 + 27*x + 4)/(9*x^3 + 12*x^2 + 4*x) + 9/128*\log(3*x + 2) - 9/128*\log(x)$

mupad [B] time = 0.09, size = 35, normalized size = 0.76

$$\frac{9 \operatorname{atanh}(3x + 1)}{64} - \frac{\frac{3x^2}{64} + \frac{3x}{64} + \frac{1}{144}}{x^3 + \frac{4x^2}{3} + \frac{4x}{9}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(6*x + 4)^3),x)

[Out] $(9*\operatorname{atanh}(3*x + 1))/64 - ((3*x)/64 + (3*x^2)/64 + 1/144)/((4*x)/9 + (4*x^2)/3 + x^3)$

sympy [A] time = 0.18, size = 41, normalized size = 0.89

$$\frac{-27x^2 - 27x - 4}{576x^3 + 768x^2 + 256x} - \frac{9 \log(x)}{128} + \frac{9 \log\left(x + \frac{2}{3}\right)}{128}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/(4+6*x)**3,x)

[Out] $(-27*x**2 - 27*x - 4)/(576*x**3 + 768*x**2 + 256*x) - 9*\log(x)/128 + 9*\log(x + 2/3)/128$

$$3.268 \quad \int \frac{1}{x^3(4+6x)^3} dx$$

Optimal. Leaf size=53

$$-\frac{1}{128x^2} + \frac{9}{128x} + \frac{27}{128(3x+2)} + \frac{9}{128(3x+2)^2} + \frac{27 \log(x)}{128} - \frac{27}{128} \log(3x+2)$$

[Out] -1/128/x^2+9/128/x+9/128/(2+3*x)^2+27/128/(2+3*x)+27/128*ln(x)-27/128*ln(2+3*x)

Rubi [A] time = 0.02, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{1}{128x^2} + \frac{9}{128x} + \frac{27}{128(3x+2)} + \frac{9}{128(3x+2)^2} + \frac{27 \log(x)}{128} - \frac{27}{128} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(4 + 6*x)^3), x]

[Out] -1/(128*x^2) + 9/(128*x) + 9/(128*(2 + 3*x)^2) + 27/(128*(2 + 3*x)) + (27*Log[x])/128 - (27*Log[2 + 3*x])/128

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^3(4+6x)^3} dx &= \int \left(\frac{1}{64x^3} - \frac{9}{128x^2} + \frac{27}{128x} - \frac{27}{64(2+3x)^3} - \frac{81}{128(2+3x)^2} - \frac{81}{128(2+3x)} \right) dx \\ &= -\frac{1}{128x^2} + \frac{9}{128x} + \frac{9}{128(2+3x)^2} + \frac{27}{128(2+3x)} + \frac{27 \log(x)}{128} - \frac{27}{128} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.02, size = 44, normalized size = 0.83

$$\frac{1}{128} \left(\frac{2(81x^3 + 81x^2 + 12x - 2)}{x^2(3x+2)^2} + 27 \log(x) - 27 \log(3x+2) \right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(4 + 6*x)^3),x]

[Out] ((2*(-2 + 12*x + 81*x^2 + 81*x^3))/(x^2*(2 + 3*x)^2) + 27*Log[x] - 27*Log[2 + 3*x])/128

fricas [A] time = 0.50, size = 79, normalized size = 1.49

$$\frac{162x^3 + 162x^2 - 27(9x^4 + 12x^3 + 4x^2)\log(3x + 2) + 27(9x^4 + 12x^3 + 4x^2)\log(x) + 24x - 4}{128(9x^4 + 12x^3 + 4x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(4+6*x)^3,x, algorithm="fricas")

[Out] 1/128*(162*x^3 + 162*x^2 - 27*(9*x^4 + 12*x^3 + 4*x^2)*log(3*x + 2) + 27*(9*x^4 + 12*x^3 + 4*x^2)*log(x) + 24*x - 4)/(9*x^4 + 12*x^3 + 4*x^2)

giac [A] time = 1.07, size = 43, normalized size = 0.81

$$\frac{81x^3 + 81x^2 + 12x - 2}{64(3x^2 + 2x)^2} - \frac{27}{128} \log(|3x + 2|) + \frac{27}{128} \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(4+6*x)^3,x, algorithm="giac")

[Out] 1/64*(81*x^3 + 81*x^2 + 12*x - 2)/(3*x^2 + 2*x)^2 - 27/128*log(abs(3*x + 2)) + 27/128*log(abs(x))

maple [A] time = 0.01, size = 42, normalized size = 0.79

$$\frac{27 \ln(x)}{128} - \frac{27 \ln(3x + 2)}{128} + \frac{9}{128x} - \frac{1}{128x^2} + \frac{9}{128(3x + 2)^2} + \frac{27}{128(3x + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(4+6*x)^3,x)

[Out] -1/128/x^2+9/128/x+9/128/(3*x+2)^2+27/128/(3*x+2)+27/128*ln(x)-27/128*ln(3*x+2)

maxima [A] time = 1.38, size = 48, normalized size = 0.91

$$\frac{81x^3 + 81x^2 + 12x - 2}{64(9x^4 + 12x^3 + 4x^2)} - \frac{27}{128} \log(3x + 2) + \frac{27}{128} \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(4+6*x)^3,x, algorithm="maxima")

[Out] 1/64*(81*x^3 + 81*x^2 + 12*x - 2)/(9*x^4 + 12*x^3 + 4*x^2) - 27/128*log(3*x + 2) + 27/128*log(x)

mupad [B] time = 0.09, size = 41, normalized size = 0.77

$$\frac{\frac{9x^3}{64} + \frac{9x^2}{64} + \frac{x}{48} - \frac{1}{288}}{x^4 + \frac{4x^3}{3} + \frac{4x^2}{9}} - \frac{27 \operatorname{atanh}(3x + 1)}{64}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(6*x + 4)^3),x)

[Out] (x/48 + (9*x^2)/64 + (9*x^3)/64 - 1/288)/((4*x^2)/9 + (4*x^3)/3 + x^4) - (27*atanh(3*x + 1))/64

sympy [A] time = 0.18, size = 46, normalized size = 0.87

$$\frac{27 \log(x)}{128} - \frac{27 \log\left(x + \frac{2}{3}\right)}{128} + \frac{81x^3 + 81x^2 + 12x - 2}{576x^4 + 768x^3 + 256x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(4+6*x)**3,x)

[Out] 27*log(x)/128 - 27*log(x + 2/3)/128 + (81*x**3 + 81*x**2 + 12*x - 2)/(576*x**4 + 768*x**3 + 256*x**2)

$$3.269 \quad \int \frac{1}{x^4(4+6x)^3} dx$$

Optimal. Leaf size=60

$$-\frac{1}{192x^3} + \frac{9}{256x^2} - \frac{27}{128x} - \frac{27}{64(3x+2)} - \frac{27}{256(3x+2)^2} - \frac{135 \log(x)}{256} + \frac{135}{256} \log(3x+2)$$

[Out] $-1/192/x^3+9/256/x^2-27/128/x-27/256/(2+3*x)^2-27/64/(2+3*x)-135/256*\ln(x)+135/256*\ln(2+3*x)$

Rubi [A] time = 0.02, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$\frac{9}{256x^2} - \frac{1}{192x^3} - \frac{27}{128x} - \frac{27}{64(3x+2)} - \frac{27}{256(3x+2)^2} - \frac{135 \log(x)}{256} + \frac{135}{256} \log(3x+2)$$

Antiderivative was successfully verified.

[In] Int[1/(x^4*(4 + 6*x)^3), x]

[Out] $-1/(192*x^3) + 9/(256*x^2) - 27/(128*x) - 27/(256*(2 + 3*x)^2) - 27/(64*(2 + 3*x)) - (135*\text{Log}[x])/256 + (135*\text{Log}[2 + 3*x])/256$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^4(4+6x)^3} dx &= \int \left(\frac{1}{64x^4} - \frac{9}{128x^3} + \frac{27}{128x^2} - \frac{135}{256x} + \frac{81}{128(2+3x)^3} + \frac{81}{64(2+3x)^2} + \frac{405}{256(2+3x)} \right) dx \\ &= -\frac{1}{192x^3} + \frac{9}{256x^2} - \frac{27}{128x} - \frac{27}{256(2+3x)^2} - \frac{27}{64(2+3x)} - \frac{135 \log(x)}{256} + \frac{135}{256} \log(2+3x) \end{aligned}$$

Mathematica [A] time = 0.02, size = 49, normalized size = 0.82

$$\frac{1}{768} \left(-\frac{2(1215x^4 + 1215x^3 + 180x^2 - 30x + 8)}{x^3(3x+2)^2} - 405 \log(x) + 405 \log(3x+2) \right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^4*(4 + 6*x)^3),x]

[Out] $((-2*(8 - 30*x + 180*x^2 + 1215*x^3 + 1215*x^4))/(x^3*(2 + 3*x)^2) - 405*\text{Log}[x] + 405*\text{Log}[2 + 3*x])/768$

fricas [A] time = 0.45, size = 84, normalized size = 1.40

$$\frac{2430x^4 + 2430x^3 + 360x^2 - 405(9x^5 + 12x^4 + 4x^3)\log(3x + 2) + 405(9x^5 + 12x^4 + 4x^3)\log(x) - 60x}{768(9x^5 + 12x^4 + 4x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(4+6*x)^3,x, algorithm="fricas")

[Out] $-1/768*(2430*x^4 + 2430*x^3 + 360*x^2 - 405*(9*x^5 + 12*x^4 + 4*x^3)*\log(3*x + 2) + 405*(9*x^5 + 12*x^4 + 4*x^3)*\log(x) - 60*x + 16)/(9*x^5 + 12*x^4 + 4*x^3)$

giac [A] time = 1.29, size = 47, normalized size = 0.78

$$\frac{1215x^4 + 1215x^3 + 180x^2 - 30x + 8}{384(3x + 2)^2x^3} + \frac{135}{256}\log(|3x + 2|) - \frac{135}{256}\log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(4+6*x)^3,x, algorithm="giac")

[Out] $-1/384*(1215*x^4 + 1215*x^3 + 180*x^2 - 30*x + 8)/((3*x + 2)^2*x^3) + 135/256*\log(\text{abs}(3*x + 2)) - 135/256*\log(\text{abs}(x))$

maple [A] time = 0.01, size = 47, normalized size = 0.78

$$-\frac{135\ln(x)}{256} + \frac{135\ln(3x + 2)}{256} - \frac{27}{128x} + \frac{9}{256x^2} - \frac{1}{192x^3} - \frac{27}{256(3x + 2)^2} - \frac{27}{64(3x + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^4/(4+6*x)^3,x)

[Out] $-1/192/x^3 + 9/256/x^2 - 27/128/x - 27/256/(3*x+2)^2 - 27/64/(3*x+2) - 135/256*\ln(x) + 135/256*\ln(3*x+2)$

maxima [A] time = 1.38, size = 53, normalized size = 0.88

$$-\frac{1215x^4 + 1215x^3 + 180x^2 - 30x + 8}{384(9x^5 + 12x^4 + 4x^3)} + \frac{135}{256}\log(3x + 2) - \frac{135}{256}\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(4+6*x)^3,x, algorithm="maxima")

[Out] -1/384*(1215*x^4 + 1215*x^3 + 180*x^2 - 30*x + 8)/(9*x^5 + 12*x^4 + 4*x^3) + 135/256*log(3*x + 2) - 135/256*log(x)

mupad [B] time = 0.05, size = 47, normalized size = 0.78

$$\frac{135 \operatorname{atanh}(3x + 1)}{128} - \frac{\frac{45x^4}{128} + \frac{45x^3}{128} + \frac{5x^2}{96} - \frac{5x}{576} + \frac{1}{432}}{x^5 + \frac{4x^4}{3} + \frac{4x^3}{9}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^4*(6*x + 4)^3),x)

[Out] (135*atanh(3*x + 1))/128 - ((5*x^2)/96 - (5*x)/576 + (45*x^3)/128 + (45*x^4)/128 + 1/432)/((4*x^3)/9 + (4*x^4)/3 + x^5)

sympy [A] time = 0.21, size = 51, normalized size = 0.85

$$-\frac{135 \log(x)}{256} + \frac{135 \log\left(x + \frac{2}{3}\right)}{256} + \frac{-1215x^4 - 1215x^3 - 180x^2 + 30x - 8}{3456x^5 + 4608x^4 + 1536x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**4/(4+6*x)**3,x)

[Out] -135*log(x)/256 + 135*log(x + 2/3)/256 + (-1215*x**4 - 1215*x**3 - 180*x**2 + 30*x - 8)/(3456*x**5 + 4608*x**4 + 1536*x**3)

$$3.270 \quad \int \frac{1}{x^5(4+6x)^3} dx$$

Optimal. Leaf size=67

$$-\frac{1}{256x^4} + \frac{3}{128x^3} - \frac{27}{256x^2} + \frac{135}{256x} + \frac{405}{512(3x+2)} + \frac{81}{512(3x+2)^2} + \frac{1215 \log(x)}{1024} - \frac{1215 \log(3x+2)}{1024}$$

[Out] $-1/256/x^4+3/128/x^3-27/256/x^2+135/256/x+81/512/(2+3*x)^2+405/512/(2+3*x)+1215/1024*\ln(x)-1215/1024*\ln(2+3*x)$

Rubi [A] time = 0.02, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-\frac{27}{256x^2} + \frac{3}{128x^3} - \frac{1}{256x^4} + \frac{135}{256x} + \frac{405}{512(3x+2)} + \frac{81}{512(3x+2)^2} + \frac{1215 \log(x)}{1024} - \frac{1215 \log(3x+2)}{1024}$$

Antiderivative was successfully verified.

[In] Int[1/(x^5*(4 + 6*x)^3), x]

[Out] $-1/(256*x^4) + 3/(128*x^3) - 27/(256*x^2) + 135/(256*x) + 81/(512*(2 + 3*x)^2) + 405/(512*(2 + 3*x)) + (1215*\text{Log}[x])/1024 - (1215*\text{Log}[2 + 3*x])/1024$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^5(4+6x)^3} dx &= \int \left(\frac{1}{64x^5} - \frac{9}{128x^4} + \frac{27}{128x^3} - \frac{135}{256x^2} + \frac{1215}{1024x} - \frac{243}{256(2+3x)^3} - \frac{1215}{512(2+3x)^2} - \frac{3645}{1024(2+3x)} \right) dx \\ &= -\frac{1}{256x^4} + \frac{3}{128x^3} - \frac{27}{256x^2} + \frac{135}{256x} + \frac{81}{512(2+3x)^2} + \frac{405}{512(2+3x)} + \frac{1215 \log(x)}{1024} - \frac{1215 \log(3x+2)}{1024} \end{aligned}$$

Mathematica [A] time = 0.02, size = 54, normalized size = 0.81

$$\frac{2(3645x^5+3645x^4+540x^3-90x^2+24x-8)}{x^4(3x+2)^2} + 1215 \log(x) - 1215 \log(3x+2)$$

1024

Antiderivative was successfully verified.

[In] Integrate[1/(x^5*(4 + 6*x)^3),x]

[Out] ((2*(-8 + 24*x - 90*x^2 + 540*x^3 + 3645*x^4 + 3645*x^5))/(x^4*(2 + 3*x)^2) + 1215*Log[x] - 1215*Log[2 + 3*x])/1024

fricas [A] time = 0.47, size = 89, normalized size = 1.33

$$\frac{7290x^5 + 7290x^4 + 1080x^3 - 180x^2 - 1215(9x^6 + 12x^5 + 4x^4)\log(3x + 2) + 1215(9x^6 + 12x^5 + 4x^4)\log(x)}{1024(9x^6 + 12x^5 + 4x^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(4+6*x)^3,x, algorithm="fricas")

[Out] 1/1024*(7290*x^5 + 7290*x^4 + 1080*x^3 - 180*x^2 - 1215*(9*x^6 + 12*x^5 + 4*x^4)*log(3*x + 2) + 1215*(9*x^6 + 12*x^5 + 4*x^4)*log(x) + 48*x - 16)/(9*x^6 + 12*x^5 + 4*x^4)

giac [A] time = 1.13, size = 52, normalized size = 0.78

$$\frac{3645x^5 + 3645x^4 + 540x^3 - 90x^2 + 24x - 8}{512(3x + 2)^2x^4} - \frac{1215}{1024}\log(|3x + 2|) + \frac{1215}{1024}\log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(4+6*x)^3,x, algorithm="giac")

[Out] 1/512*(3645*x^5 + 3645*x^4 + 540*x^3 - 90*x^2 + 24*x - 8)/((3*x + 2)^2*x^4) - 1215/1024*log(abs(3*x + 2)) + 1215/1024*log(abs(x))

maple [A] time = 0.01, size = 52, normalized size = 0.78

$$\frac{1215\ln(x)}{1024} - \frac{1215\ln(3x + 2)}{1024} + \frac{135}{256x} - \frac{27}{256x^2} + \frac{3}{128x^3} - \frac{1}{256x^4} + \frac{81}{512(3x + 2)^2} + \frac{405}{512(3x + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^5/(4+6*x)^3,x)

[Out] -1/256/x^4+3/128/x^3-27/256/x^2+135/256/x+81/512/(3*x+2)^2+405/512/(3*x+2)+1215/1024*ln(x)-1215/1024*ln(3*x+2)

maxima [A] time = 1.39, size = 58, normalized size = 0.87

$$\frac{3645x^5 + 3645x^4 + 540x^3 - 90x^2 + 24x - 8}{512(9x^6 + 12x^5 + 4x^4)} - \frac{1215}{1024}\log(3x + 2) + \frac{1215}{1024}\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^5/(4+6*x)^3,x, algorithm="maxima")

[Out] 1/512*(3645*x^5 + 3645*x^4 + 540*x^3 - 90*x^2 + 24*x - 8)/(9*x^6 + 12*x^5 + 4*x^4) - 1215/1024*log(3*x + 2) + 1215/1024*log(x)

mupad [B] time = 0.05, size = 51, normalized size = 0.76

$$\frac{\frac{405x^5}{512} + \frac{405x^4}{512} + \frac{15x^3}{128} - \frac{5x^2}{256} + \frac{x}{192} - \frac{1}{576}}{x^6 + \frac{4x^5}{3} + \frac{4x^4}{9}} - \frac{1215 \operatorname{atanh}(3x + 1)}{512}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^5*(6*x + 4)^3),x)

[Out] (x/192 - (5*x^2)/256 + (15*x^3)/128 + (405*x^4)/512 + (405*x^5)/512 - 1/576)/((4*x^4)/9 + (4*x^5)/3 + x^6) - (1215*atanh(3*x + 1))/512

sympy [A] time = 0.22, size = 56, normalized size = 0.84

$$\frac{1215 \log(x)}{1024} - \frac{1215 \log\left(x + \frac{2}{3}\right)}{1024} + \frac{3645x^5 + 3645x^4 + 540x^3 - 90x^2 + 24x - 8}{4608x^6 + 6144x^5 + 2048x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**5/(4+6*x)**3,x)

[Out] 1215*log(x)/1024 - 1215*log(x + 2/3)/1024 + (3645*x**5 + 3645*x**4 + 540*x**3 - 90*x**2 + 24*x - 8)/(4608*x**6 + 6144*x**5 + 2048*x**4)

$$3.271 \quad \int \frac{1}{2+2x} dx$$

Optimal. Leaf size=8

$$\frac{1}{2} \log(x+1)$$

[Out] 1/2*ln(1+x)

Rubi [A] time = 0.00, antiderivative size = 8, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {31}

$$\frac{1}{2} \log(x+1)$$

Antiderivative was successfully verified.

[In] Int[(2 + 2*x)^(-1), x]

[Out] Log[1 + x]/2

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \frac{1}{2+2x} dx = \frac{1}{2} \log(1+x)$$

Mathematica [A] time = 0.00, size = 10, normalized size = 1.25

$$\frac{1}{2} \log(2x+2)$$

Antiderivative was successfully verified.

[In] Integrate[(2 + 2*x)^(-1), x]

[Out] Log[2 + 2*x]/2

fricas [A] time = 0.51, size = 6, normalized size = 0.75

$$\frac{1}{2} \log(x+1)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(2*x+2),x, algorithm="fricas")

[Out] 1/2*log(x + 1)

giac [A] time = 0.90, size = 7, normalized size = 0.88

$$\frac{1}{2} \log(|x + 1|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(2*x+2),x, algorithm="giac")

[Out] 1/2*log(abs(x + 1))

maple [A] time = 0.00, size = 9, normalized size = 1.12

$$\frac{\ln(2x + 2)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(2+2*x),x)

[Out] 1/2*ln(2+2*x)

maxima [A] time = 1.34, size = 6, normalized size = 0.75

$$\frac{1}{2} \log(x + 1)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(2*x+2),x, algorithm="maxima")

[Out] 1/2*log(x + 1)

mupad [B] time = 0.15, size = 6, normalized size = 0.75

$$\frac{\ln(x + 1)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(2*x + 2),x)

[Out] log(x + 1)/2

sympy [A] time = 0.07, size = 7, normalized size = 0.88

$$\frac{\log(2x + 2)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(2*x+2),x)

[Out] log(2*x + 2)/2

$$3.272 \quad \int \frac{1}{4-6x} dx$$

Optimal. Leaf size=10

$$-\frac{1}{6} \log(2-3x)$$

[Out] -1/6*ln(2-3*x)

Rubi [A] time = 0.00, antiderivative size = 10, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {31}

$$-\frac{1}{6} \log(2-3x)$$

Antiderivative was successfully verified.

[In] Int[(4 - 6*x)^(-1), x]

[Out] -Log[2 - 3*x]/6

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \frac{1}{4-6x} dx = -\frac{1}{6} \log(2-3x)$$

Mathematica [A] time = 0.00, size = 10, normalized size = 1.00

$$-\frac{1}{6} \log(4-6x)$$

Antiderivative was successfully verified.

[In] Integrate[(4 - 6*x)^(-1), x]

[Out] -1/6*Log[4 - 6*x]

fricas [A] time = 0.49, size = 8, normalized size = 0.80

$$-\frac{1}{6} \log(3x-2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(4-6*x),x, algorithm="fricas")

[Out] -1/6*log(3*x - 2)

giac [A] time = 1.15, size = 9, normalized size = 0.90

$$-\frac{1}{6} \log(|3x - 2|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(4-6*x),x, algorithm="giac")

[Out] -1/6*log(abs(3*x - 2))

maple [A] time = 0.00, size = 9, normalized size = 0.90

$$-\frac{\ln(-6x + 4)}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(4-6*x),x)

[Out] -1/6*ln(4-6*x)

maxima [A] time = 1.34, size = 8, normalized size = 0.80

$$-\frac{1}{6} \log(3x - 2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(4-6*x),x, algorithm="maxima")

[Out] -1/6*log(3*x - 2)

mupad [B] time = 0.08, size = 6, normalized size = 0.60

$$-\frac{\ln\left(x - \frac{2}{3}\right)}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-1/(6*x - 4),x)

[Out] -log(x - 2/3)/6

sympy [A] time = 0.07, size = 8, normalized size = 0.80

$$-\frac{\log(6x - 4)}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(4-6*x),x)

[Out] -log(6*x - 4)/6

$$3.273 \quad \int \frac{1}{a + \sqrt{a}x} dx$$

Optimal. Leaf size=14

$$\frac{\log(\sqrt{a} + x)}{\sqrt{a}}$$

[Out] $\ln(x+a^{(1/2)})/a^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {31}

$$\frac{\log(\sqrt{a} + x)}{\sqrt{a}}$$

Antiderivative was successfully verified.

[In] `Int[(a + Sqrt[a]*x)^(-1), x]`

[Out] `Log[Sqrt[a] + x]/Sqrt[a]`

Rule 31

`Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]`

Rubi steps

$$\int \frac{1}{a + \sqrt{a}x} dx = \frac{\log(\sqrt{a} + x)}{\sqrt{a}}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.14

$$\frac{\log(\sqrt{a}x + a)}{\sqrt{a}}$$

Antiderivative was successfully verified.

[In] `Integrate[(a + Sqrt[a]*x)^(-1), x]`

[Out] `Log[a + Sqrt[a]*x]/Sqrt[a]`

fricas [A] time = 0.48, size = 10, normalized size = 0.71

$$\frac{\log(x + \sqrt{a})}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+x*a^(1/2)),x, algorithm="fricas")

[Out] log(x + sqrt(a))/sqrt(a)

giac [A] time = 1.28, size = 13, normalized size = 0.93

$$\frac{\log(|\sqrt{a}x + a|)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+x*a^(1/2)),x, algorithm="giac")

[Out] log(abs(sqrt(a)*x + a))/sqrt(a)

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{\ln(\sqrt{a}x + a)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a+x*a^(1/2)),x)

[Out] ln(a+x*a^(1/2))/a^(1/2)

maxima [A] time = 1.25, size = 12, normalized size = 0.86

$$\frac{\log(\sqrt{a}x + a)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+x*a^(1/2)),x, algorithm="maxima")

[Out] log(sqrt(a)*x + a)/sqrt(a)

mupad [B] time = 0.11, size = 10, normalized size = 0.71

$$\frac{\ln(x + \sqrt{a})}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(a + a^(1/2)*x),x)
```

```
[Out] log(x + a^(1/2))/a^(1/2)
```

sympy [A] time = 0.08, size = 14, normalized size = 1.00

$$\frac{\log(\sqrt{a}x + a)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a+x*a**(1/2)),x)
```

```
[Out] log(sqrt(a)*x + a)/sqrt(a)
```

$$3.274 \quad \int \frac{1}{a + \sqrt{-a}x} dx$$

Optimal. Leaf size=20

$$\frac{\log(\sqrt{-a}x + a)}{\sqrt{-a}}$$

[Out] $\ln(a+x*(-a)^{(1/2)})/(-a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {31}

$$\frac{\log(\sqrt{-a}x + a)}{\sqrt{-a}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + \text{Sqrt}[-a]*x)^{-1}, x]$

[Out] $\text{Log}[a + \text{Sqrt}[-a]*x]/\text{Sqrt}[-a]$

Rule 31

$\text{Int}[(a_ + (b_)*(x_))^{-1}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] \text{ /; FreeQ}\{a, b\}, x]$

Rubi steps

$$\int \frac{1}{a + \sqrt{-a}x} dx = \frac{\log(a + \sqrt{-a}x)}{\sqrt{-a}}$$

Mathematica [A] time = 0.00, size = 20, normalized size = 1.00

$$\frac{\log(\sqrt{-a}x + a)}{\sqrt{-a}}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(a + \text{Sqrt}[-a]*x)^{-1}, x]$

[Out] $\text{Log}[a + \text{Sqrt}[-a]*x]/\text{Sqrt}[-a]$

fricas [A] time = 0.49, size = 20, normalized size = 1.00

$$-\frac{\sqrt{-a} \log(x - \sqrt{-a})}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+x*(-a)^(1/2)),x, algorithm="fricas")

[Out] -sqrt(-a)*log(x - sqrt(-a))/a

giac [A] time = 1.10, size = 17, normalized size = 0.85

$$\frac{\log(|\sqrt{-a}x + a|)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+x*(-a)^(1/2)),x, algorithm="giac")

[Out] log(abs(sqrt(-a)*x + a))/sqrt(-a)

maple [A] time = 0.00, size = 17, normalized size = 0.85

$$\frac{\ln(a + \sqrt{-a}x)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a+x*(-a)^(1/2)),x)

[Out] ln(a+x*(-a)^(1/2))/(-a)^(1/2)

maxima [A] time = 1.37, size = 16, normalized size = 0.80

$$\frac{\log(\sqrt{-a}x + a)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+x*(-a)^(1/2)),x, algorithm="maxima")

[Out] log(sqrt(-a)*x + a)/sqrt(-a)

mupad [B] time = 0.11, size = 16, normalized size = 0.80

$$\frac{\ln(x - \sqrt{-a})}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(a + (-a)^(1/2)*x), x)
```

```
[Out] log(x - (-a)^(1/2))/(-a)^(1/2)
```

sympy [A] time = 0.08, size = 17, normalized size = 0.85

$$\frac{\log(a + x\sqrt{-a})}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a+x*(-a)**(1/2)), x)
```

```
[Out] log(a + x*sqrt(-a))/sqrt(-a)
```

$$3.275 \quad \int \frac{1}{a^2 + \sqrt{-a}x} dx$$

Optimal. Leaf size=22

$$\frac{\log(a^2 + \sqrt{-a}x)}{\sqrt{-a}}$$

[Out] $\ln(a^2+x*(-a)^{(1/2)})/(-a)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {31}

$$\frac{\log(a^2 + \sqrt{-a}x)}{\sqrt{-a}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a^2 + \text{Sqrt}[-a]*x)^{-1}, x]$

[Out] $\text{Log}[a^2 + \text{Sqrt}[-a]*x]/\text{Sqrt}[-a]$

Rule 31

$\text{Int}[(a_ + (b_.)*(x_))^{-1}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] /;$ $\text{FreeQ}[\{a, b\}, x]$

Rubi steps

$$\int \frac{1}{a^2 + \sqrt{-a}x} dx = \frac{\log(a^2 + \sqrt{-a}x)}{\sqrt{-a}}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 1.00

$$\frac{\log(a^2 + \sqrt{-a}x)}{\sqrt{-a}}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(a^2 + \text{Sqrt}[-a]*x)^{-1}, x]$

[Out] $\text{Log}[a^2 + \text{Sqrt}[-a]*x]/\text{Sqrt}[-a]$

fricas [A] time = 0.51, size = 21, normalized size = 0.95

$$-\frac{\sqrt{-a} \log(-\sqrt{-a} a + x)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a^2+x*(-a)^(1/2)),x, algorithm="fricas")

[Out] -sqrt(-a)*log(-sqrt(-a)*a + x)/a

giac [A] time = 0.93, size = 19, normalized size = 0.86

$$\frac{\log(|a^2 + \sqrt{-a} x|)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a^2+x*(-a)^(1/2)),x, algorithm="giac")

[Out] log(abs(a^2 + sqrt(-a)*x))/sqrt(-a)

maple [A] time = 0.00, size = 19, normalized size = 0.86

$$\frac{\ln(a^2 + \sqrt{-a} x)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a^2+(-a)^(1/2)*x),x)

[Out] ln(a^2+(-a)^(1/2)*x)/(-a)^(1/2)

maxima [A] time = 1.32, size = 18, normalized size = 0.82

$$\frac{\log(a^2 + \sqrt{-a} x)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a^2+x*(-a)^(1/2)),x, algorithm="maxima")

[Out] log(a^2 + sqrt(-a)*x)/sqrt(-a)

mupad [B] time = 0.05, size = 14, normalized size = 0.64

$$\frac{\ln(x + (-a)^{3/2})}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(a^2 + (-a)^(1/2)*x), x)
```

```
[Out] log(x + (-a)^(3/2))/(-a)^(1/2)
```

sympy [A] time = 0.08, size = 19, normalized size = 0.86

$$\frac{\log(a^2 + x\sqrt{-a})}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a**2+x*(-a)**(1/2)), x)
```

```
[Out] log(a**2 + x*sqrt(-a))/sqrt(-a)
```

$$3.276 \quad \int \frac{1}{a^3 + \sqrt{-a}x} dx$$

Optimal. Leaf size=22

$$\frac{\log(a^3 + \sqrt{-a}x)}{\sqrt{-a}}$$

[Out] $\ln(a^3+x*(-a)^{(1/2)})/(-a)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {31}

$$\frac{\log(a^3 + \sqrt{-a}x)}{\sqrt{-a}}$$

Antiderivative was successfully verified.

[In] Int[(a^3 + Sqrt[-a]*x)^(-1), x]

[Out] Log[a^3 + Sqrt[-a]*x]/Sqrt[-a]

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \frac{1}{a^3 + \sqrt{-a}x} dx = \frac{\log(a^3 + \sqrt{-a}x)}{\sqrt{-a}}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 1.00

$$\frac{\log(a^3 + \sqrt{-a}x)}{\sqrt{-a}}$$

Antiderivative was successfully verified.

[In] Integrate[(a^3 + Sqrt[-a]*x)^(-1), x]

[Out] Log[a^3 + Sqrt[-a]*x]/Sqrt[-a]

fricas [A] time = 0.48, size = 23, normalized size = 1.05

$$-\frac{\sqrt{-a} \log(-\sqrt{-a} a^2 + x)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a^3+x*(-a)^(1/2)),x, algorithm="fricas")

[Out] -sqrt(-a)*log(-sqrt(-a)*a^2 + x)/a

giac [A] time = 1.09, size = 19, normalized size = 0.86

$$\frac{\log(|a^3 + \sqrt{-a} x|)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a^3+x*(-a)^(1/2)),x, algorithm="giac")

[Out] log(abs(a^3 + sqrt(-a)*x))/sqrt(-a)

maple [A] time = 0.00, size = 19, normalized size = 0.86

$$\frac{\ln(a^3 + \sqrt{-a} x)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a^3+(-a)^(1/2)*x),x)

[Out] ln(a^3+(-a)^(1/2)*x)/(-a)^(1/2)

maxima [A] time = 1.31, size = 18, normalized size = 0.82

$$\frac{\log(a^3 + \sqrt{-a} x)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a^3+x*(-a)^(1/2)),x, algorithm="maxima")

[Out] log(a^3 + sqrt(-a)*x)/sqrt(-a)

mupad [B] time = 0.06, size = 16, normalized size = 0.73

$$\frac{\ln(x - (-a)^{5/2})}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(a^3 + (-a)^(1/2)*x),x)`

[Out] `log(x - (-a)^(5/2))/(-a)^(1/2)`

sympy [A] time = 0.08, size = 19, normalized size = 0.86

$$\frac{\log(a^3 + x\sqrt{-a})}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a**3+x*(-a)**(1/2)),x)`

[Out] `log(a**3 + x*sqrt(-a))/sqrt(-a)`

$$3.277 \quad \int \frac{1}{\frac{1}{a} + \sqrt{-a}x} dx$$

Optimal. Leaf size=21

$$\frac{\log(1 - (-a)^{3/2}x)}{\sqrt{-a}}$$

[Out] $\ln(1 - (-a)^{(3/2)*x}) / (-a)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {31}

$$\frac{\log(1 - (-a)^{3/2}x)}{\sqrt{-a}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a^{-1}) + \text{Sqrt}[-a]*x]^{-1}, x]$

[Out] $\text{Log}[1 - (-a)^{(3/2)*x}] / \text{Sqrt}[-a]$

Rule 31

$\text{Int}[(a_) + (b_.)*(x_)]^{-1}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] /; \text{FreeQ}[\{a, b\}, x]$

Rubi steps

$$\int \frac{1}{\frac{1}{a} + \sqrt{-a}x} dx = \frac{\log(1 - (-a)^{3/2}x)}{\sqrt{-a}}$$

Mathematica [A] time = 0.01, size = 21, normalized size = 1.00

$$\frac{\log(\sqrt{-a}ax + 1)}{\sqrt{-a}}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(a^{-1}) + \text{Sqrt}[-a]*x]^{-1}, x]$

[Out] $\text{Log}[1 + \text{Sqrt}[-a]*a*x] / \text{Sqrt}[-a]$

fricas [A] time = 0.49, size = 24, normalized size = 1.14

$$\frac{\sqrt{-a} \log(a^2 x - \sqrt{-a})}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1/a+x*(-a)^(1/2)),x, algorithm="fricas")

[Out] -sqrt(-a)*log(a^2*x - sqrt(-a))/a

giac [A] time = 1.04, size = 19, normalized size = 0.90

$$\frac{\log\left(\left|\sqrt{-a}x + \frac{1}{a}\right|\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1/a+x*(-a)^(1/2)),x, algorithm="giac")

[Out] log(abs(sqrt(-a)*x + 1/a))/sqrt(-a)

maple [A] time = 0.00, size = 19, normalized size = 0.90

$$\frac{\ln\left(\sqrt{-a}x + \frac{1}{a}\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(1/a+(-a)^(1/2)*x),x)

[Out] ln(1/a+(-a)^(1/2)*x)/(-a)^(1/2)

maxima [A] time = 1.33, size = 18, normalized size = 0.86

$$\frac{\log\left(\sqrt{-a}x + \frac{1}{a}\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1/a+x*(-a)^(1/2)),x, algorithm="maxima")

[Out] log(sqrt(-a)*x + 1/a)/sqrt(-a)

mupad [B] time = 0.15, size = 16, normalized size = 0.76

$$\frac{\ln\left(x - \frac{1}{(-a)^{3/2}}\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(1/a + (-a)^(1/2)*x), x)`

[Out] `log(x - 1/(-a)^(3/2))/(-a)^(1/2)`

sympy [A] time = 0.09, size = 19, normalized size = 0.90

$$\frac{\log(ax\sqrt{-a} + 1)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1/a+x*(-a)**(1/2)), x)`

[Out] `log(a*x*sqrt(-a) + 1)/sqrt(-a)`

$$3.278 \quad \int \frac{1}{\frac{1}{a^2} + \sqrt{-a}x} dx$$

Optimal. Leaf size=20

$$\frac{\log((-a)^{5/2}x + 1)}{\sqrt{-a}}$$

[Out] $\ln(1+(-a)^{(5/2)*x})/(-a)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {31}

$$\frac{\log((-a)^{5/2}x + 1)}{\sqrt{-a}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a^{-2}) + \text{Sqrt}[-a]*x]^{-1}, x]$

[Out] $\text{Log}[1 + (-a)^{(5/2)*x}]/\text{Sqrt}[-a]$

Rule 31

$\text{Int}[(a + b*x)^{-1}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] /; \text{FreeQ}\{a, b\}, x]$

Rubi steps

$$\int \frac{1}{\frac{1}{a^2} + \sqrt{-a}x} dx = \frac{\log(1 + (-a)^{5/2}x)}{\sqrt{-a}}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 1.10

$$\frac{\log\left(\frac{1}{a^2} + \sqrt{-a}x\right)}{\sqrt{-a}}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(a^{-2}) + \text{Sqrt}[-a]*x]^{-1}, x]$

[Out] $\text{Log}[a^{-2} + \text{Sqrt}[-a]*x]/\text{Sqrt}[-a]$

fricas [A] time = 0.49, size = 24, normalized size = 1.20

$$-\frac{\sqrt{-a} \log(a^3 x - \sqrt{-a})}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1/a^2+x*(-a)^(1/2)),x, algorithm="fricas")

[Out] -sqrt(-a)*log(a^3*x - sqrt(-a))/a

giac [A] time = 1.08, size = 19, normalized size = 0.95

$$\frac{\log\left(\left|\sqrt{-a}x + \frac{1}{a^2}\right|\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1/a^2+x*(-a)^(1/2)),x, algorithm="giac")

[Out] log(abs(sqrt(-a)*x + 1/a^2))/sqrt(-a)

maple [A] time = 0.00, size = 19, normalized size = 0.95

$$\frac{\ln\left(\sqrt{-a}x + \frac{1}{a^2}\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(1/a^2+(-a)^(1/2)*x),x)

[Out] ln(1/a^2+(-a)^(1/2)*x)/(-a)^(1/2)

maxima [A] time = 1.31, size = 18, normalized size = 0.90

$$\frac{\log\left(\sqrt{-a}x + \frac{1}{a^2}\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1/a^2+x*(-a)^(1/2)),x, algorithm="maxima")

[Out] log(sqrt(-a)*x + 1/a^2)/sqrt(-a)

mupad [B] time = 0.18, size = 14, normalized size = 0.70

$$\frac{\ln\left(x + \frac{1}{(-a)^{5/2}}\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(1/a^2 + (-a)^(1/2)*x),x)`

[Out] `log(x + 1/(-a)^(5/2))/(-a)^(1/2)`

sympy [A] time = 0.09, size = 20, normalized size = 1.00

$$\frac{\log\left(a^2x\sqrt{-a} + 1\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1/a**2+x*(-a)**(1/2)),x)`

[Out] `log(a**2*x*sqrt(-a) + 1)/sqrt(-a)`

$$3.279 \quad \int \frac{1}{x(1+bx)} dx$$

Optimal. Leaf size=11

$$\log(x) - \log(bx + 1)$$

[Out] ln(x)-ln(b*x+1)

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.273$, Rules used = {36, 29, 31}

$$\log(x) - \log(bx + 1)$$

Antiderivative was successfully verified.

[In] Int[1/(x*(1 + b*x)), x]

[Out] Log[x] - Log[1 + b*x]

Rule 29

Int[(x_)^(-1), x_Symbol] := Simp[Log[x], x]

Rule 31

Int[((a_) + (b_.)*(x_))^-1, x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 36

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))), x_Symbol] := Dist[b/(b*c - a*d), Int[1/(a + b*x), x], x] - Dist[d/(b*c - a*d), Int[1/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x(1+bx)} dx &= -\left(b \int \frac{1}{1+bx} dx\right) + \int \frac{1}{x} dx \\ &= \log(x) - \log(1+bx) \end{aligned}$$

Mathematica [A] time = 0.00, size = 11, normalized size = 1.00

$$\log(x) - \log(bx + 1)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(1 + b*x)),x]

[Out] Log[x] - Log[1 + b*x]

fricas [A] time = 0.46, size = 11, normalized size = 1.00

$$-\log(bx + 1) + \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+1),x, algorithm="fricas")

[Out] -log(b*x + 1) + log(x)

giac [A] time = 0.99, size = 13, normalized size = 1.18

$$-\log(|bx + 1|) + \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+1),x, algorithm="giac")

[Out] -log(abs(b*x + 1)) + log(abs(x))

maple [A] time = 0.00, size = 12, normalized size = 1.09

$$\ln(x) - \ln(bx + 1)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+1),x)

[Out] ln(x)-ln(b*x+1)

maxima [A] time = 1.31, size = 11, normalized size = 1.00

$$-\log(bx + 1) + \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+1),x, algorithm="maxima")

[Out] -log(b*x + 1) + log(x)

mupad [B] time = 0.10, size = 9, normalized size = 0.82

$$-2 \operatorname{atanh}(2bx + 1)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(x*(b*x + 1)),x)
```

```
[Out] -2*atanh(2*b*x + 1)
```

sympy [A] time = 0.14, size = 8, normalized size = 0.73

$$\log(x) - \log\left(x + \frac{1}{b}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x/(b*x+1),x)
```

```
[Out] log(x) - log(x + 1/b)
```

$$3.280 \quad \int \frac{1}{x(-1+bx)} dx$$

Optimal. Leaf size=12

$$\log(1 - bx) - \log(x)$$

[Out] $-\ln(x) + \ln(-b*x+1)$

Rubi [A] time = 0.00, antiderivative size = 12, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.273$, Rules used = {36, 29, 31}

$$\log(1 - bx) - \log(x)$$

Antiderivative was successfully verified.

[In] `Int[1/(x*(-1 + b*x)), x]`

[Out] `-Log[x] + Log[1 - b*x]`

Rule 29

`Int[(x_)^(-1), x_Symbol] := Simp[Log[x], x]`

Rule 31

`Int[((a_) + (b_)*(x_))^-1, x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]`

Rule 36

`Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))), x_Symbol] := Dist[b/(b*c - a*d), Int[1/(a + b*x), x], x] - Dist[d/(b*c - a*d), Int[1/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0]`

Rubi steps

$$\begin{aligned} \int \frac{1}{x(-1+bx)} dx &= b \int \frac{1}{-1+bx} dx - \int \frac{1}{x} dx \\ &= -\log(x) + \log(1 - bx) \end{aligned}$$

Mathematica [A] time = 0.00, size = 12, normalized size = 1.00

$$\log(1 - bx) - \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(-1 + b*x)),x]

[Out] -Log[x] + Log[1 - b*x]

fricas [A] time = 0.48, size = 11, normalized size = 0.92

$$\log(bx - 1) - \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-1),x, algorithm="fricas")

[Out] log(b*x - 1) - log(x)

giac [A] time = 1.02, size = 13, normalized size = 1.08

$$\log(|bx - 1|) - \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-1),x, algorithm="giac")

[Out] log(abs(b*x - 1)) - log(abs(x))

maple [A] time = 0.01, size = 12, normalized size = 1.00

$$-\ln(x) + \ln(bx - 1)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x-1),x)

[Out] ln(b*x-1)-ln(x)

maxima [A] time = 1.36, size = 11, normalized size = 0.92

$$\log(bx - 1) - \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-1),x, algorithm="maxima")

[Out] log(b*x - 1) - log(x)

mupad [B] time = 0.04, size = 9, normalized size = 0.75

$$-2 \operatorname{atanh}(2bx - 1)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(x*(b*x - 1)),x)
```

```
[Out] -2*atanh(2*b*x - 1)
```

sympy [A] time = 0.13, size = 8, normalized size = 0.67

$$-\log(x) + \log\left(x - \frac{1}{b}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x/(b*x-1),x)
```

```
[Out] -log(x) + log(x - 1/b)
```

$$3.281 \quad \int \frac{1}{x^2(1+bx)} dx$$

Optimal. Leaf size=19

$$-b \log(x) + b \log(bx + 1) - \frac{1}{x}$$

[Out] $-1/x - b \ln(x) + b \ln(b*x+1)$

Rubi [A] time = 0.01, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-b \log(x) + b \log(bx + 1) - \frac{1}{x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/(x^2*(1 + b*x)), x]$

[Out] $-x^{(-1)} - b*\text{Log}[x] + b*\text{Log}[1 + b*x]$

Rule 44

$\text{Int}[(a + (b \cdot x)^m) \cdot (c + (d \cdot x)^n), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b \cdot x)^m \cdot (c + d \cdot x)^n, x], x] /;$ FreeQ[{a, b, c, d}, x] & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(1+bx)} dx &= \int \left(\frac{1}{x^2} - \frac{b}{x} + \frac{b^2}{1+bx} \right) dx \\ &= -\frac{1}{x} - b \log(x) + b \log(1+bx) \end{aligned}$$

Mathematica [A] time = 0.00, size = 19, normalized size = 1.00

$$-b \log(x) + b \log(bx + 1) - \frac{1}{x}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/(x^2*(1 + b*x)), x]$

[Out] $-x^{(-1)} - b*\text{Log}[x] + b*\text{Log}[1 + b*x]$

fricas [A] time = 0.46, size = 21, normalized size = 1.11

$$\frac{bx \log(bx + 1) - bx \log(x) - 1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+1),x, algorithm="fricas")

[Out] (b*x*log(b*x + 1) - b*x*log(x) - 1)/x

giac [A] time = 0.92, size = 21, normalized size = 1.11

$$b \log(|bx + 1|) - b \log(|x|) - \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+1),x, algorithm="giac")

[Out] b*log(abs(b*x + 1)) - b*log(abs(x)) - 1/x

maple [A] time = 0.01, size = 20, normalized size = 1.05

$$-b \ln(x) + b \ln(bx + 1) - \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+1),x)

[Out] -1/x-b*ln(x)+b*ln(b*x+1)

maxima [A] time = 1.32, size = 19, normalized size = 1.00

$$b \log(bx + 1) - b \log(x) - \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+1),x, algorithm="maxima")

[Out] b*log(b*x + 1) - b*log(x) - 1/x

mupad [B] time = 0.04, size = 16, normalized size = 0.84

$$2b \operatorname{atanh}(2bx + 1) - \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(x^2*(b*x + 1)),x)
```

```
[Out] 2*b*atanh(2*b*x + 1) - 1/x
```

sympy [A] time = 0.18, size = 14, normalized size = 0.74

$$b \left(-\log(x) + \log\left(x + \frac{1}{b}\right) \right) - \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**2/(b*x+1),x)
```

```
[Out] b*(-log(x) + log(x + 1/b)) - 1/x
```

$$3.282 \quad \int \frac{1}{x^2(-1+bx)} dx$$

Optimal. Leaf size=18

$$-b \log(x) + b \log(1 - bx) + \frac{1}{x}$$

[Out] 1/x-b*ln(x)+b*ln(-b*x+1)

Rubi [A] time = 0.01, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {44}

$$-b \log(x) + b \log(1 - bx) + \frac{1}{x}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(-1 + b*x)),x]

[Out] x^(-1) - b*Log[x] + b*Log[1 - b*x]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(-1+bx)} dx &= \int \left(-\frac{1}{x^2} - \frac{b}{x} + \frac{b^2}{-1+bx} \right) dx \\ &= \frac{1}{x} - b \log(x) + b \log(1 - bx) \end{aligned}$$

Mathematica [A] time = 0.00, size = 18, normalized size = 1.00

$$-b \log(x) + b \log(1 - bx) + \frac{1}{x}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(-1 + b*x)),x]

[Out] x^(-1) - b*Log[x] + b*Log[1 - b*x]

fricas [A] time = 0.51, size = 21, normalized size = 1.17

$$\frac{bx \log (bx - 1) - bx \log (x) + 1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-1),x, algorithm="fricas")

[Out] (b*x*log(b*x - 1) - b*x*log(x) + 1)/x

giac [A] time = 1.14, size = 19, normalized size = 1.06

$$b \log (|bx - 1|) - b \log (|x|) + \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-1),x, algorithm="giac")

[Out] b*log(abs(b*x - 1)) - b*log(abs(x)) + 1/x

maple [A] time = 0.01, size = 18, normalized size = 1.00

$$-b \ln (x) + b \ln (bx - 1) + \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x-1),x)

[Out] b*ln(b*x-1)+1/x-b*ln(x)

maxima [A] time = 1.33, size = 17, normalized size = 0.94

$$b \log (bx - 1) - b \log (x) + \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-1),x, algorithm="maxima")

[Out] b*log(b*x - 1) - b*log(x) + 1/x

mupad [B] time = 0.03, size = 14, normalized size = 0.78

$$\frac{1}{x} - 2 b \operatorname{atanh} (2 b x - 1)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(x^2*(b*x - 1)),x)
```

```
[Out] 1/x - 2*b*atanh(2*b*x - 1)
```

sympy [A] time = 0.19, size = 14, normalized size = 0.78

$$b \left(-\log(x) + \log\left(x - \frac{1}{b}\right) \right) + \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**2/(b*x-1),x)
```

```
[Out] b*(-log(x) + log(x - 1/b)) + 1/x
```

$$3.283 \quad \int \left(\frac{b}{x} + \frac{1}{x^2(1+bx)} \right) dx$$

Optimal. Leaf size=14

$$b \log(bx + 1) - \frac{1}{x}$$

[Out] -1/x+b*ln(b*x+1)

Rubi [A] time = 0.01, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {44}

$$b \log(bx + 1) - \frac{1}{x}$$

Antiderivative was successfully verified.

[In] Int[b/x + 1/(x^2*(1 + b*x)), x]

[Out] -x^(-1) + b*Log[1 + b*x]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \left(\frac{b}{x} + \frac{1}{x^2(1+bx)} \right) dx &= b \log(x) + \int \frac{1}{x^2(1+bx)} dx \\ &= b \log(x) + \int \left(\frac{1}{x^2} - \frac{b}{x} + \frac{b^2}{1+bx} \right) dx \\ &= -\frac{1}{x} + b \log(1+bx) \end{aligned}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$b \log(bx + 1) - \frac{1}{x}$$

Antiderivative was successfully verified.

[In] Integrate[b/x + 1/(x^2*(1 + b*x)),x]

[Out] $-x^{-1} + b \cdot \text{Log}[1 + b \cdot x]$

fricas [A] time = 0.48, size = 15, normalized size = 1.07

$$\frac{bx \log (bx + 1) - 1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(b/x+1/x^2/(b*x+1),x, algorithm="fricas")

[Out] $(b \cdot x \cdot \log (b \cdot x + 1) - 1) / x$

giac [A] time = 1.25, size = 15, normalized size = 1.07

$$b \log (|bx + 1|) - \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(b/x+1/x^2/(b*x+1),x, algorithm="giac")

[Out] $b \cdot \log (\text{abs}(b \cdot x + 1)) - 1 / x$

maple [A] time = 0.00, size = 15, normalized size = 1.07

$$b \ln (bx + 1) - \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(b/x+1/x^2/(b*x+1),x)

[Out] $-1/x + b \cdot \ln (b \cdot x + 1)$

maxima [A] time = 1.32, size = 14, normalized size = 1.00

$$b \log (bx + 1) - \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(b/x+1/x^2/(b*x+1),x, algorithm="maxima")

[Out] $b \cdot \log (b \cdot x + 1) - 1 / x$

mupad [B] time = 0.04, size = 20, normalized size = 1.43

$$b \ln (x) + 2 b \operatorname{atanh} (2 b x + 1) - \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(x^2*(b*x + 1)) + b/x,x)
```

```
[Out] b*log(x) + 2*b*atanh(2*b*x + 1) - 1/x
```

sympy [A] time = 0.15, size = 10, normalized size = 0.71

$$b \log (bx + 1) - \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(b/x+1/x**2/(b*x+1),x)
```

```
[Out] b*log(b*x + 1) - 1/x
```

3.284 $\int x^3 \sqrt{a + bx} dx$

Optimal. Leaf size=72

$$-\frac{2a^3(a+bx)^{3/2}}{3b^4} + \frac{6a^2(a+bx)^{5/2}}{5b^4} + \frac{2(a+bx)^{9/2}}{9b^4} - \frac{6a(a+bx)^{7/2}}{7b^4}$$

[Out] $-2/3*a^3*(b*x+a)^{(3/2)}/b^4+6/5*a^2*(b*x+a)^{(5/2)}/b^4-6/7*a*(b*x+a)^{(7/2)}/b^4+2/9*(b*x+a)^{(9/2)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{6a^2(a+bx)^{5/2}}{5b^4} - \frac{2a^3(a+bx)^{3/2}}{3b^4} + \frac{2(a+bx)^{9/2}}{9b^4} - \frac{6a(a+bx)^{7/2}}{7b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*Sqrt[a + b*x], x]

[Out] $(-2*a^3*(a + b*x)^{(3/2)})/(3*b^4) + (6*a^2*(a + b*x)^{(5/2)})/(5*b^4) - (6*a*(a + b*x)^{(7/2)})/(7*b^4) + (2*(a + b*x)^{(9/2)})/(9*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3 \sqrt{a + bx} dx &= \int \left(-\frac{a^3 \sqrt{a + bx}}{b^3} + \frac{3a^2(a + bx)^{3/2}}{b^3} - \frac{3a(a + bx)^{5/2}}{b^3} + \frac{(a + bx)^{7/2}}{b^3} \right) dx \\ &= -\frac{2a^3(a + bx)^{3/2}}{3b^4} + \frac{6a^2(a + bx)^{5/2}}{5b^4} - \frac{6a(a + bx)^{7/2}}{7b^4} + \frac{2(a + bx)^{9/2}}{9b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.64

$$\frac{2(a + bx)^{3/2} (-16a^3 + 24a^2bx - 30ab^2x^2 + 35b^3x^3)}{315b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*Sqrt[a + b*x],x]

[Out] $(2*(a + b*x)^{(3/2)}*(-16*a^3 + 24*a^2*b*x - 30*a*b^2*x^2 + 35*b^3*x^3))/(315*b^4)$

fricas [A] time = 0.51, size = 53, normalized size = 0.74

$$\frac{2(35b^4x^4 + 5ab^3x^3 - 6a^2b^2x^2 + 8a^3bx - 16a^4)\sqrt{bx+a}}{315b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(1/2),x, algorithm="fricas")

[Out] $2/315*(35*b^4*x^4 + 5*a*b^3*x^3 - 6*a^2*b^2*x^2 + 8*a^3*b*x - 16*a^4)*\text{sqrt}(b*x + a)/b^4$

giac [B] time = 0.95, size = 116, normalized size = 1.61

$$2 \left(\frac{9 \left(5(bx+a)^{\frac{7}{2}} - 21(bx+a)^{\frac{5}{2}}a + 35(bx+a)^{\frac{3}{2}}a^2 - 35\sqrt{bx+a}a^3 \right) a}{b^3} + \frac{35(bx+a)^{\frac{9}{2}} - 180(bx+a)^{\frac{7}{2}}a + 378(bx+a)^{\frac{5}{2}}a^2 - 420(bx+a)^{\frac{3}{2}}a^3 + 315\sqrt{bx+a}a^4}{b^3} \right) / 315b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(1/2),x, algorithm="giac")

[Out] $2/315*(9*(5*(b*x + a)^{(7/2)} - 21*(b*x + a)^{(5/2)}*a + 35*(b*x + a)^{(3/2)}*a^2 - 35*\text{sqrt}(b*x + a)*a^3)*a/b^3 + (35*(b*x + a)^{(9/2)} - 180*(b*x + a)^{(7/2)}*a + 378*(b*x + a)^{(5/2)}*a^2 - 420*(b*x + a)^{(3/2)}*a^3 + 315*\text{sqrt}(b*x + a)*a^4)/b^3)/b$

maple [A] time = 0.02, size = 43, normalized size = 0.60

$$\frac{2(bx+a)^{\frac{3}{2}}(-35b^3x^3 + 30ab^2x^2 - 24a^2bx + 16a^3)}{315b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^(1/2),x)

[Out] $-2/315*(b*x+a)^{(3/2)}*(-35*b^3*x^3+30*a*b^2*x^2-24*a^2*b*x+16*a^3)/b^4$

maxima [A] time = 1.25, size = 56, normalized size = 0.78

$$\frac{2(bx+a)^{\frac{9}{2}}}{9b^4} - \frac{6(bx+a)^{\frac{7}{2}}a}{7b^4} + \frac{6(bx+a)^{\frac{5}{2}}a^2}{5b^4} - \frac{2(bx+a)^{\frac{3}{2}}a^3}{3b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(1/2),x, algorithm="maxima")

[Out] 2/9*(b*x + a)^(9/2)/b^4 - 6/7*(b*x + a)^(7/2)*a/b^4 + 6/5*(b*x + a)^(5/2)*a^2/b^4 - 2/3*(b*x + a)^(3/2)*a^3/b^4

mupad [B] time = 0.05, size = 56, normalized size = 0.78

$$\frac{2(a+bx)^{9/2}}{9b^4} - \frac{2a^3(a+bx)^{3/2}}{3b^4} + \frac{6a^2(a+bx)^{5/2}}{5b^4} - \frac{6a(a+bx)^{7/2}}{7b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(a + b*x)^(1/2),x)

[Out] (2*(a + b*x)^(9/2))/(9*b^4) - (2*a^3*(a + b*x)^(3/2))/(3*b^4) + (6*a^2*(a + b*x)^(5/2))/(5*b^4) - (6*a*(a + b*x)^(7/2))/(7*b^4)

sympy [B] time = 2.91, size = 1742, normalized size = 24.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**(1/2),x)

[Out] -32*a**(49/2)*sqrt(1 + b*x/a)/(315*a**20*b**4 + 1890*a**19*b**5*x + 4725*a**18*b**6*x**2 + 6300*a**17*b**7*x**3 + 4725*a**16*b**8*x**4 + 1890*a**15*b**9*x**5 + 315*a**14*b**10*x**6) + 32*a**(49/2)/(315*a**20*b**4 + 1890*a**19*b**5*x + 4725*a**18*b**6*x**2 + 6300*a**17*b**7*x**3 + 4725*a**16*b**8*x**4 + 1890*a**15*b**9*x**5 + 315*a**14*b**10*x**6) - 176*a**(47/2)*b*x*sqrt(1 + b*x/a)/(315*a**20*b**4 + 1890*a**19*b**5*x + 4725*a**18*b**6*x**2 + 6300*a**17*b**7*x**3 + 4725*a**16*b**8*x**4 + 1890*a**15*b**9*x**5 + 315*a**14*b**10*x**6) + 192*a**(47/2)*b*x/(315*a**20*b**4 + 1890*a**19*b**5*x + 4725*a**18*b**6*x**2 + 6300*a**17*b**7*x**3 + 4725*a**16*b**8*x**4 + 1890*a**15*b**9*x**5 + 315*a**14*b**10*x**6) - 396*a**(45/2)*b**2*x**2*sqrt(1 + b*x/a)/(315*a**20*b**4 + 1890*a**19*b**5*x + 4725*a**18*b**6*x**2 + 6300*a**17*b**7*x**3 + 4725*a**16*b**8*x**4 + 1890*a**15*b**9*x**5 + 315*a**14*b**10*x**6) + 480*a**(45/2)*b**2*x**2/(315*a**20*b**4 + 1890*a**19*b**5*x + 4725*a**18*b**6*x**2 + 6300*a**17*b**7*x**3 + 4725*a**16*b**8*x**4 + 1890*a**15*b**9*x**5 + 315*a**14*b**10*x**6)

$$\begin{aligned}
& 9x^{**5} + 315a^{**14}b^{**10}x^{**6}) - 462a^{**}(43/2)*b^{**3}x^{**3}\sqrt{1 + b*x/a)/(3 \\
& 15a^{**20}b^{**4} + 1890a^{**19}b^{**5}x + 4725a^{**18}b^{**6}x^{**2} + 6300a^{**17}b^{**7} \\
& x^{**3} + 4725a^{**16}b^{**8}x^{**4} + 1890a^{**15}b^{**9}x^{**5} + 315a^{**14}b^{**10}x^{**6}) \\
& + 640a^{**}(43/2)*b^{**3}x^{**3}/(315a^{**20}b^{**4} + 1890a^{**19}b^{**5}x + 4725a^{**18} \\
& b^{**6}x^{**2} + 6300a^{**17}b^{**7}x^{**3} + 4725a^{**16}b^{**8}x^{**4} + 1890a^{**15}b^{**9}x \\
& **5 + 315a^{**14}b^{**10}x^{**6}) - 210a^{**}(41/2)*b^{**4}x^{**4}\sqrt{1 + b*x/a)/(315* \\
& a^{**20}b^{**4} + 1890a^{**19}b^{**5}x + 4725a^{**18}b^{**6}x^{**2} + 6300a^{**17}b^{**7}x^{** \\
& 3 + 4725a^{**16}b^{**8}x^{**4} + 1890a^{**15}b^{**9}x^{**5} + 315a^{**14}b^{**10}x^{**6}) + 4 \\
& 80a^{**}(41/2)*b^{**4}x^{**4}/(315a^{**20}b^{**4} + 1890a^{**19}b^{**5}x + 4725a^{**18}b^{** \\
& 6x^{**2} + 6300a^{**17}b^{**7}x^{**3} + 4725a^{**16}b^{**8}x^{**4} + 1890a^{**15}b^{**9}x^{**5} \\
& + 315a^{**14}b^{**10}x^{**6}) + 378a^{**}(39/2)*b^{**5}x^{**5}\sqrt{1 + b*x/a)/(315a^{** \\
& 20}b^{**4} + 1890a^{**19}b^{**5}x + 4725a^{**18}b^{**6}x^{**2} + 6300a^{**17}b^{**7}x^{**3} + \\
& 4725a^{**16}b^{**8}x^{**4} + 1890a^{**15}b^{**9}x^{**5} + 315a^{**14}b^{**10}x^{**6}) + 192* \\
& a^{**}(39/2)*b^{**5}x^{**5}/(315a^{**20}b^{**4} + 1890a^{**19}b^{**5}x + 4725a^{**18}b^{**6}x \\
& **2 + 6300a^{**17}b^{**7}x^{**3} + 4725a^{**16}b^{**8}x^{**4} + 1890a^{**15}b^{**9}x^{**5} + \\
& 315a^{**14}b^{**10}x^{**6}) + 1134a^{**}(37/2)*b^{**6}x^{**6}\sqrt{1 + b*x/a)/(315a^{**20} \\
& *b^{**4} + 1890a^{**19}b^{**5}x + 4725a^{**18}b^{**6}x^{**2} + 6300a^{**17}b^{**7}x^{**3} + 4 \\
& 725a^{**16}b^{**8}x^{**4} + 1890a^{**15}b^{**9}x^{**5} + 315a^{**14}b^{**10}x^{**6}) + 32a^{**} \\
& (37/2)*b^{**6}x^{**6}/(315a^{**20}b^{**4} + 1890a^{**19}b^{**5}x + 4725a^{**18}b^{**6}x^{**2} \\
& + 6300a^{**17}b^{**7}x^{**3} + 4725a^{**16}b^{**8}x^{**4} + 1890a^{**15}b^{**9}x^{**5} + 315 \\
& *a^{**14}b^{**10}x^{**6}) + 1494a^{**}(35/2)*b^{**7}x^{**7}\sqrt{1 + b*x/a)/(315a^{**20}*b \\
& *4 + 1890a^{**19}b^{**5}x + 4725a^{**18}b^{**6}x^{**2} + 6300a^{**17}b^{**7}x^{**3} + 4725 \\
& *a^{**16}b^{**8}x^{**4} + 1890a^{**15}b^{**9}x^{**5} + 315a^{**14}b^{**10}x^{**6}) + 1098a^{**}(\\
& 33/2)*b^{**8}x^{**8}\sqrt{1 + b*x/a)/(315a^{**20}b^{**4} + 1890a^{**19}b^{**5}x + 4725* \\
& a^{**18}b^{**6}x^{**2} + 6300a^{**17}b^{**7}x^{**3} + 4725a^{**16}b^{**8}x^{**4} + 1890a^{**15} \\
& b^{**9}x^{**5} + 315a^{**14}b^{**10}x^{**6}) + 430a^{**}(31/2)*b^{**9}x^{**9}\sqrt{1 + b*x/a) \\
& /(315a^{**20}b^{**4} + 1890a^{**19}b^{**5}x + 4725a^{**18}b^{**6}x^{**2} + 6300a^{**17}b* \\
& *7x^{**3} + 4725a^{**16}b^{**8}x^{**4} + 1890a^{**15}b^{**9}x^{**5} + 315a^{**14}b^{**10}x^{** \\
& 6) + 70a^{**}(29/2)*b^{**10}x^{**10}\sqrt{1 + b*x/a)/(315a^{**20}b^{**4} + 1890a^{**19} \\
& b^{**5}x + 4725a^{**18}b^{**6}x^{**2} + 6300a^{**17}b^{**7}x^{**3} + 4725a^{**16}b^{**8}x^{**4} \\
& + 1890a^{**15}b^{**9}x^{**5} + 315a^{**14}b^{**10}x^{**6})
\end{aligned}$$

3.285 $\int x^2 \sqrt{a + bx} dx$

Optimal. Leaf size=53

$$\frac{2a^2(a + bx)^{3/2}}{3b^3} + \frac{2(a + bx)^{7/2}}{7b^3} - \frac{4a(a + bx)^{5/2}}{5b^3}$$

[Out] $2/3*a^2*(b*x+a)^{(3/2)}/b^3-4/5*a*(b*x+a)^{(5/2)}/b^3+2/7*(b*x+a)^{(7/2)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2a^2(a + bx)^{3/2}}{3b^3} + \frac{2(a + bx)^{7/2}}{7b^3} - \frac{4a(a + bx)^{5/2}}{5b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*Sqrt[a + b*x], x]

[Out] $(2*a^2*(a + b*x)^{(3/2)})/(3*b^3) - (4*a*(a + b*x)^{(5/2)})/(5*b^3) + (2*(a + b*x)^{(7/2)})/(7*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2 \sqrt{a + bx} dx &= \int \left(\frac{a^2 \sqrt{a + bx}}{b^2} - \frac{2a(a + bx)^{3/2}}{b^2} + \frac{(a + bx)^{5/2}}{b^2} \right) dx \\ &= \frac{2a^2(a + bx)^{3/2}}{3b^3} - \frac{4a(a + bx)^{5/2}}{5b^3} + \frac{2(a + bx)^{7/2}}{7b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.66

$$\frac{2(a + bx)^{3/2} (8a^2 - 12abx + 15b^2x^2)}{105b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*Sqrt[a + b*x], x]

[Out] $(2*(a + b*x)^{(3/2)}*(8*a^2 - 12*a*b*x + 15*b^2*x^2))/(105*b^3)$

fricas [A] time = 0.56, size = 42, normalized size = 0.79

$$\frac{2(15b^3x^3 + 3ab^2x^2 - 4a^2bx + 8a^3)\sqrt{bx+a}}{105b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(1/2), x, algorithm="fricas")

[Out] $2/105*(15*b^3*x^3 + 3*a*b^2*x^2 - 4*a^2*b*x + 8*a^3)*\text{sqrt}(b*x + a)/b^3$

giac [B] time = 1.03, size = 93, normalized size = 1.75

$$\frac{2 \left(\frac{7 \left(3(bx+a)^{\frac{5}{2}} - 10(bx+a)^{\frac{3}{2}}a + 15\sqrt{bx+a}a^2 \right) a}{b^2} + \frac{3 \left(5(bx+a)^{\frac{7}{2}} - 21(bx+a)^{\frac{5}{2}}a + 35(bx+a)^{\frac{3}{2}}a^2 - 35\sqrt{bx+a}a^3 \right)}{b^2} \right)}{105b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(1/2), x, algorithm="giac")

[Out] $2/105*(7*(3*(b*x + a)^{(5/2)} - 10*(b*x + a)^{(3/2)}*a + 15*\text{sqrt}(b*x + a)*a^2)*a/b^2 + 3*(5*(b*x + a)^{(7/2)} - 21*(b*x + a)^{(5/2)}*a + 35*(b*x + a)^{(3/2)}*a^2 - 35*\text{sqrt}(b*x + a)*a^3)/b^2)/b$

maple [A] time = 0.00, size = 32, normalized size = 0.60

$$\frac{2(bx+a)^{\frac{3}{2}}(15b^2x^2 - 12abx + 8a^2)}{105b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^(1/2), x)

[Out] $2/105*(b*x+a)^{(3/2)}*(15*b^2*x^2-12*a*b*x+8*a^2)/b^3$

maxima [A] time = 1.41, size = 41, normalized size = 0.77

$$\frac{2(bx+a)^{\frac{7}{2}}}{7b^3} - \frac{4(bx+a)^{\frac{5}{2}}a}{5b^3} + \frac{2(bx+a)^{\frac{3}{2}}a^2}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(1/2),x, algorithm="maxima")

[Out] $\frac{2}{7}*(b*x + a)^{(7/2)}/b^3 - \frac{4}{5}*(b*x + a)^{(5/2)}*a/b^3 + \frac{2}{3}*(b*x + a)^{(3/2)}*a^2/b^3$

mupad [B] time = 0.05, size = 37, normalized size = 0.70

$$\frac{30(a+bx)^{7/2} - 84a(a+bx)^{5/2} + 70a^2(a+bx)^{3/2}}{105b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a + b*x)^(1/2),x)

[Out] $(30*(a + b*x)^{(7/2)} - 84*a*(a + b*x)^{(5/2)} + 70*a^2*(a + b*x)^{(3/2)})/(105*b^3)$

sympy [B] time = 2.04, size = 666, normalized size = 12.57

$$\frac{16a^{\frac{23}{2}}\sqrt{1+\frac{bx}{a}}}{105a^8b^3 + 315a^7b^4x + 315a^6b^5x^2 + 105a^5b^6x^3} - \frac{16a^{\frac{23}{2}}}{105a^8b^3 + 315a^7b^4x + 315a^6b^5x^2 + 105a^5b^6x^3} + \frac{4}{105a^8b^3 + 315a^7b^4x + 315a^6b^5x^2 + 105a^5b^6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)**(1/2),x)

[Out] $16*a**(23/2)*sqrt(1 + b*x/a)/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3) - 16*a**(23/2)/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3) + 40*a**(21/2)*b*x*sqrt(1 + b*x/a)/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3) - 48*a**(21/2)*b*x/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3) + 30*a**(19/2)*b**2*x**2*sqrt(1 + b*x/a)/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3) - 48*a**(19/2)*b**2*x**2/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3) + 40*a**(17/2)*b**3*x**3*sqrt(1 + b*x/a)/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3) - 16*a**(17/2)*b**3*x**3/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3) + 100*a**(15/2)*b**4*x**4*sqrt(1 + b*x/a)/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3) + 96*a**(13/2)*b**5*x**5*sqrt(1 + b*x/a)/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3) + 30*a**(11/2)*b**6*x**6*sqrt(1 + b*x/a)/(105*a**8*b**3 + 315*a**7*b**4*x + 315*a**6*b**5*x**2 + 105*a**5*b**6*x**3)$

3.286 $\int x\sqrt{a+bx} dx$

Optimal. Leaf size=34

$$\frac{2(a+bx)^{5/2}}{5b^2} - \frac{2a(a+bx)^{3/2}}{3b^2}$$

[Out] $-2/3*a*(b*x+a)^{(3/2)}/b^2+2/5*(b*x+a)^{(5/2)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{2(a+bx)^{5/2}}{5b^2} - \frac{2a(a+bx)^{3/2}}{3b^2}$$

Antiderivative was successfully verified.

[In] Int[x*Sqrt[a + b*x],x]

[Out] $(-2*a*(a + b*x)^{(3/2)})/(3*b^2) + (2*(a + b*x)^{(5/2)})/(5*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int x\sqrt{a+bx} dx &= \int \left(-\frac{a\sqrt{a+bx}}{b} + \frac{(a+bx)^{3/2}}{b} \right) dx \\ &= -\frac{2a(a+bx)^{3/2}}{3b^2} + \frac{2(a+bx)^{5/2}}{5b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.71

$$\frac{2(a+bx)^{3/2}(3bx-2a)}{15b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*Sqrt[a + b*x],x]

[Out] $(2*(a + b*x)^{(3/2)}*(-2*a + 3*b*x))/(15*b^2)$

fricas [A] time = 0.52, size = 30, normalized size = 0.88

$$\frac{2(3b^2x^2 + abx - 2a^2)\sqrt{bx+a}}{15b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(1/2),x, algorithm="fricas")`

[Out] $2/15*(3*b^2*x^2 + a*b*x - 2*a^2)*\text{sqrt}(b*x + a)/b^2$

giac [B] time = 1.28, size = 66, normalized size = 1.94

$$\frac{2\left(\frac{5\left((bx+a)^{\frac{3}{2}}-3\sqrt{bx+a}a\right)a}{b} + \frac{3(bx+a)^{\frac{5}{2}}-10(bx+a)^{\frac{3}{2}}a+15\sqrt{bx+a}a^2}{b}\right)}{15b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(1/2),x, algorithm="giac")`

[Out] $2/15*(5*((b*x + a)^{(3/2)} - 3*\text{sqrt}(b*x + a)*a)*a/b + (3*(b*x + a)^{(5/2)} - 10*(b*x + a)^{(3/2)}*a + 15*\text{sqrt}(b*x + a)*a^2)/b)/b$

maple [A] time = 0.00, size = 21, normalized size = 0.62

$$-\frac{2(bx+a)^{\frac{3}{2}}(-3bx+2a)}{15b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)^(1/2),x)`

[Out] $-2/15*(b*x+a)^{(3/2)}*(-3*b*x+2*a)/b^2$

maxima [A] time = 1.31, size = 26, normalized size = 0.76

$$\frac{2(bx+a)^{\frac{5}{2}}}{5b^2} - \frac{2(bx+a)^{\frac{3}{2}}a}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] $2/5*(b*x + a)^{(5/2)}/b^2 - 2/3*(b*x + a)^{(3/2)}*a/b^2$

mupad [B] time = 0.03, size = 25, normalized size = 0.74

$$-\frac{10 a (a + b x)^{3/2} - 6 (a + b x)^{5/2}}{15 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(a + b*x)^(1/2), x)`

[Out] $-(10*a*(a + b*x)^{(3/2)} - 6*(a + b*x)^{(5/2)})/(15*b^2)$

sympy [B] time = 1.39, size = 202, normalized size = 5.94

$$-\frac{4a^{\frac{9}{2}}\sqrt{1+\frac{bx}{a}}}{15a^2b^2+15ab^3x} + \frac{4a^{\frac{9}{2}}}{15a^2b^2+15ab^3x} - \frac{2a^{\frac{7}{2}}bx\sqrt{1+\frac{bx}{a}}}{15a^2b^2+15ab^3x} + \frac{4a^{\frac{7}{2}}bx}{15a^2b^2+15ab^3x} + \frac{8a^{\frac{5}{2}}b^2x^2\sqrt{1+\frac{bx}{a}}}{15a^2b^2+15ab^3x} + \frac{6a^{\frac{3}{2}}b^3x^3\sqrt{1+\frac{bx}{a}}}{15a^2b^2+15ab^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**(1/2), x)`

[Out] $-4*a**(9/2)*\text{sqrt}(1 + b*x/a)/(15*a**2*b**2 + 15*a*b**3*x) + 4*a**(9/2)/(15*a**2*b**2 + 15*a*b**3*x) - 2*a**(7/2)*b*x*\text{sqrt}(1 + b*x/a)/(15*a**2*b**2 + 15*a*b**3*x) + 4*a**(7/2)*b*x/(15*a**2*b**2 + 15*a*b**3*x) + 8*a**(5/2)*b**2*x**2*\text{sqrt}(1 + b*x/a)/(15*a**2*b**2 + 15*a*b**3*x) + 6*a**(3/2)*b**3*x**3*\text{sqrt}(1 + b*x/a)/(15*a**2*b**2 + 15*a*b**3*x)$

3.287 $\int \sqrt{a + bx} dx$

Optimal. Leaf size=16

$$\frac{2(a + bx)^{3/2}}{3b}$$

[Out] $2/3*(b*x+a)^{(3/2)}/b$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{2(a + bx)^{3/2}}{3b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x], x]

[Out] $(2*(a + b*x)^{(3/2)})/(3*b)$

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \sqrt{a + bx} dx = \frac{2(a + bx)^{3/2}}{3b}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$\frac{2(a + bx)^{3/2}}{3b}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x], x]

[Out] $(2*(a + b*x)^{(3/2)})/(3*b)$

fricas [A] time = 0.52, size = 12, normalized size = 0.75

$$\frac{2(bx + a)^{\frac{3}{2}}}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2),x, algorithm="fricas")

[Out] 2/3*(b*x + a)^(3/2)/b

giac [A] time = 1.06, size = 12, normalized size = 0.75

$$\frac{2(bx + a)^{\frac{3}{2}}}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2),x, algorithm="giac")

[Out] 2/3*(b*x + a)^(3/2)/b

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{2(bx + a)^{\frac{3}{2}}}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2),x)

[Out] 2/3*(b*x+a)^(3/2)/b

maxima [A] time = 1.34, size = 12, normalized size = 0.75

$$\frac{2(bx + a)^{\frac{3}{2}}}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2),x, algorithm="maxima")

[Out] 2/3*(b*x + a)^(3/2)/b

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{2(a + bx)^{\frac{3}{2}}}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2),x)

[Out] $(2*(a + b*x)^{(3/2)})/(3*b)$

sympy [A] time = 0.07, size = 12, normalized size = 0.75

$$\frac{2(a + bx)^{\frac{3}{2}}}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/2),x)`

[Out] $2*(a + b*x)**(3/2)/(3*b)$

$$3.288 \quad \int \frac{\sqrt{a+bx}}{x} dx$$

Optimal. Leaf size=35

$$2\sqrt{a+bx} - 2\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)$$

[Out] $-2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})*a^{(1/2)}+2*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {50, 63, 208}

$$2\sqrt{a+bx} - 2\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[a + b*x]/x, x]`

[Out] $2*\operatorname{Sqrt}[a + b*x] - 2*\operatorname{Sqrt}[a]*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]]$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{a+bx}}{x} dx &= 2\sqrt{a+bx} + a \int \frac{1}{x\sqrt{a+bx}} dx \\
&= 2\sqrt{a+bx} + \frac{(2a) \operatorname{Subst}\left(\int \frac{1}{\frac{-a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{b} \\
&= 2\sqrt{a+bx} - 2\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 1.00

$$2\sqrt{a+bx} - 2\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/x,x]

[Out] 2*Sqrt[a + b*x] - 2*Sqrt[a]*ArcTanh[Sqrt[a + b*x]/Sqrt[a]]

fricas [A] time = 0.57, size = 73, normalized size = 2.09

$$\left[\sqrt{a} \log\left(\frac{bx - 2\sqrt{bx+a}\sqrt{a} + 2a}{x}\right) + 2\sqrt{bx+a}, 2\sqrt{-a} \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) + 2\sqrt{bx+a} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x,x, algorithm="fricas")

[Out] [sqrt(a)*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*sqrt(b*x + a), 2*sqrt(-a)*arctan(sqrt(b*x + a)*sqrt(-a)/a) + 2*sqrt(b*x + a)]

giac [A] time = 1.13, size = 32, normalized size = 0.91

$$\frac{2a \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} + 2\sqrt{bx+a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x,x, algorithm="giac")

[Out] $2*a*\arctan(\sqrt{b*x + a}/\sqrt{-a})/\sqrt{-a} + 2*\sqrt{b*x + a}$

maple [A] time = 0.01, size = 28, normalized size = 0.80

$$-2\sqrt{a} \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right) + 2\sqrt{bx+a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{int}((b*x+a)^{(1/2)}/x,x)$

[Out] $-2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})*a^{(1/2)}+2*(b*x+a)^{(1/2)}$

maxima [A] time = 2.92, size = 42, normalized size = 1.20

$$\sqrt{a} \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right) + 2\sqrt{bx+a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{integrate}((b*x+a)^{(1/2)}/x,x, \text{algorithm}="maxima")$

[Out] $\sqrt{a}*\log((\sqrt{b*x + a} - \sqrt{a})/(\sqrt{b*x + a} + \sqrt{a})) + 2*\sqrt{b*x + a}$

mupad [B] time = 0.09, size = 27, normalized size = 0.77

$$2\sqrt{a+bx} - 2\sqrt{a} \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{int}((a + b*x)^{(1/2)}/x,x)$

[Out] $2*(a + b*x)^{(1/2)} - 2*a^{(1/2)}*\operatorname{atanh}((a + b*x)^{(1/2)}/a^{(1/2)})$

sympy [B] time = 1.60, size = 68, normalized size = 1.94

$$-2\sqrt{a} \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) + \frac{2a}{\sqrt{b}\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{2\sqrt{b}\sqrt{x}}{\sqrt{\frac{a}{bx}+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{integrate}((b*x+a)**(1/2)/x,x)$

[Out] $-2*\sqrt{a}*\operatorname{asinh}(\sqrt{a}/(\sqrt{b}*\sqrt{x})) + 2*a/(\sqrt{b}*\sqrt{x}*\sqrt{a/(b*x + 1)}) + 2*\sqrt{b}*\sqrt{x}/\sqrt{a/(b*x + 1)}$

$$3.289 \quad \int \frac{\sqrt{a+bx}}{x^2} dx$$

Optimal. Leaf size=39

$$-\frac{\sqrt{a+bx}}{x} - \frac{b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

[Out] $-b \cdot \operatorname{arctanh}((b \cdot x + a)^{(1/2)} / a^{(1/2)}) / a^{(1/2)} - (b \cdot x + a)^{(1/2)} / x$

Rubi [A] time = 0.01, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {47, 63, 208}

$$-\frac{\sqrt{a+bx}}{x} - \frac{b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/x^2,x]

[Out] $-(\operatorname{Sqrt}[a + b \cdot x] / x) - (b \cdot \operatorname{ArcTanh}[\operatorname{Sqrt}[a + b \cdot x] / \operatorname{Sqrt}[a]]) / \operatorname{Sqrt}[a]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{a+bx}}{x^2} dx &= -\frac{\sqrt{a+bx}}{x} + \frac{1}{2}b \int \frac{1}{x\sqrt{a+bx}} dx \\
&= -\frac{\sqrt{a+bx}}{x} + \text{Subst} \left(\int \frac{1}{\frac{-a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx} \right) \\
&= -\frac{\sqrt{a+bx}}{x} - \frac{b \tanh^{-1} \left(\frac{\sqrt{a+bx}}{\sqrt{a}} \right)}{\sqrt{a}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 47, normalized size = 1.21

$$-\frac{bx\sqrt{\frac{bx}{a}+1} \tanh^{-1}\left(\sqrt{\frac{bx}{a}+1}\right) + a + bx}{x\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/x^2,x]

[Out] -((a + b*x + b*x*Sqrt[1 + (b*x)/a]*ArcTanh[Sqrt[1 + (b*x)/a]])/(x*Sqrt[a + b*x]))

fricas [A] time = 0.54, size = 93, normalized size = 2.38

$$\left[\frac{\sqrt{a} bx \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2\sqrt{bx+a} a}{2ax}, \frac{\sqrt{-a} bx \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) - \sqrt{bx+a} a}{ax} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^2,x, algorithm="fricas")

[Out] [1/2*(sqrt(a)*b*x*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) - 2*sqrt(b*x + a)*a)/(a*x), (sqrt(-a)*b*x*arctan(sqrt(b*x + a)*sqrt(-a)/a) - sqrt(b*x + a)*a)/(a*x)]

giac [A] time = 0.96, size = 41, normalized size = 1.05

$$\frac{\frac{b^2 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} - \frac{\sqrt{bx+a} b}{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^2,x, algorithm="giac")

[Out] (b^2*arctan(sqrt(b*x + a)/sqrt(-a))/sqrt(-a) - sqrt(b*x + a)*b/x)/b

maple [A] time = 0.01, size = 37, normalized size = 0.95

$$2 \left(-\frac{\operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{2\sqrt{a}} - \frac{\sqrt{bx+a}}{2bx} \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/x^2,x)

[Out] 2*b*(-1/2*(b*x+a)^(1/2)/x/b-1/2*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(1/2))

maxima [A] time = 2.87, size = 47, normalized size = 1.21

$$\frac{b \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{2\sqrt{a}} - \frac{\sqrt{bx+a}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^2,x, algorithm="maxima")

[Out] 1/2*b*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a)))/sqrt(a) - sqrt(b*x + a)/x

mupad [B] time = 0.05, size = 31, normalized size = 0.79

$$\frac{\sqrt{a+bx}}{x} - \frac{b \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/x^2,x)

[Out] - (a + b*x)^(1/2)/x - (b*atanh((a + b*x)^(1/2)/a^(1/2)))/a^(1/2)

sympy [A] time = 2.22, size = 44, normalized size = 1.13

$$-\frac{\sqrt{b} \sqrt{\frac{a}{bx} + 1}}{\sqrt{x}} - \frac{b \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b} \sqrt{x}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(1/2)/x**2,x)
```

```
[Out] -sqrt(b)*sqrt(a/(b*x) + 1)/sqrt(x) - b*asinh(sqrt(a)/(sqrt(b)*sqrt(x)))/sqrt(a)
```

$$3.290 \quad \int \frac{\sqrt{a+bx}}{x^3} dx$$

Optimal. Leaf size=65

$$\frac{b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{3/2}} - \frac{\sqrt{a+bx}}{2x^2} - \frac{b\sqrt{a+bx}}{4ax}$$

[Out] $1/4*b^2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(3/2)}-1/2*(b*x+a)^{(1/2)}/x^2-1/4*b*(b*x+a)^{(1/2)}/a/x$

Rubi [A] time = 0.02, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 51, 63, 208}

$$\frac{b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{3/2}} - \frac{\sqrt{a+bx}}{2x^2} - \frac{b\sqrt{a+bx}}{4ax}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/x^3, x]

[Out] $-\operatorname{Sqrt}[a + b*x]/(2*x^2) - (b*\operatorname{Sqrt}[a + b*x])/(4*a*x) + (b^2*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(4*a^{(3/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^(n), x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{a+bx}}{x^3} dx &= -\frac{\sqrt{a+bx}}{2x^2} + \frac{1}{4}b \int \frac{1}{x^2\sqrt{a+bx}} dx \\ &= -\frac{\sqrt{a+bx}}{2x^2} - \frac{b\sqrt{a+bx}}{4ax} - \frac{b^2 \int \frac{1}{x\sqrt{a+bx}} dx}{8a} \\ &= -\frac{\sqrt{a+bx}}{2x^2} - \frac{b\sqrt{a+bx}}{4ax} - \frac{b \operatorname{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{4a} \\ &= -\frac{\sqrt{a+bx}}{2x^2} - \frac{b\sqrt{a+bx}}{4ax} + \frac{b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{3/2}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.54

$$\frac{2b^2(a+bx)^{3/2} {}_2F_1\left(\frac{3}{2}, 3; \frac{5}{2}; \frac{bx}{a} + 1\right)}{3a^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[a + b*x]/x^3, x]
```

```
[Out] (-2*b^2*(a + b*x)^(3/2)*Hypergeometric2F1[3/2, 3, 5/2, 1 + (b*x)/a])/(3*a^3)
```

fricas [A] time = 0.56, size = 119, normalized size = 1.83

$$\left[\frac{\sqrt{a} b^2 x^2 \log\left(\frac{bx+2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2(abx+2a^2)\sqrt{bx+a}}{8a^2x^2}, -\frac{\sqrt{-a} b^2 x^2 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) + (abx+2a^2)\sqrt{bx+a}}{4a^2x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^3,x, algorithm="fricas")

[Out] [1/8*(sqrt(a)*b^2*x^2*log((b*x + 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) - 2*(a*b*x + 2*a^2)*sqrt(b*x + a))/(a^2*x^2), -1/4*(sqrt(-a)*b^2*x^2*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (a*b*x + 2*a^2)*sqrt(b*x + a))/(a^2*x^2)]

giac [A] time = 1.14, size = 66, normalized size = 1.02

$$-\frac{\frac{b^3 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}a} + \frac{(bx+a)^2 b^3 + \sqrt{bx+a} ab^3}{ab^2 x^2}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^3,x, algorithm="giac")

[Out] -1/4*(b^3*arctan(sqrt(b*x + a)/sqrt(-a))/(sqrt(-a)*a) + ((b*x + a)^(3/2)*b^3 + sqrt(b*x + a)*a*b^3)/(a*b^2*x^2))/b

maple [A] time = 0.01, size = 53, normalized size = 0.82

$$2 \left(\frac{\operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{8a^{\frac{3}{2}}} + \frac{\frac{(bx+a)^{\frac{3}{2}}}{8a} - \frac{\sqrt{bx+a}}{8}}{b^2 x^2} \right) b^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/x^3,x)

[Out] 2*b^2*((-1/8/a*(b*x+a)^(3/2)-1/8*(b*x+a)^(1/2))/x^2/b^2+1/8*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(3/2))

maxima [A] time = 3.03, size = 88, normalized size = 1.35

$$-\frac{b^2 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{8a^{\frac{3}{2}}} - \frac{(bx+a)^{\frac{3}{2}} b^2 + \sqrt{bx+a} ab^2}{4((bx+a)^2 a - 2(bx+a)a^2 + a^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^3,x, algorithm="maxima")

[Out] -1/8*b^2*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a)))/a^(3/2) - 1/4*((b*x + a)^(3/2)*b^2 + sqrt(b*x + a)*a*b^2)/((b*x + a)^2*a - 2*(b*x + a)*a^2 + a^3)

mupad [B] time = 0.07, size = 48, normalized size = 0.74

$$\frac{b^2 \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{3/2}} - \frac{(a+bx)^{3/2}}{4ax^2} - \frac{\sqrt{a+bx}}{4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/2)/x^3, x)`

[Out] $(b^2 \operatorname{atanh}((a + b*x)^{1/2}/a^{1/2}))/ (4*a^{3/2}) - (a + b*x)^{3/2}/(4*a*x^2) - (a + b*x)^{1/2}/(4*x^2)$

sympy [A] time = 4.02, size = 97, normalized size = 1.49

$$-\frac{a}{2\sqrt{b}x^2\sqrt{\frac{a}{bx}+1}} - \frac{3\sqrt{b}}{4x^2\sqrt{\frac{a}{bx}+1}} - \frac{b^{\frac{3}{2}}}{4a\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{b^2 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4a^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/2)/x**3, x)`

[Out] $-a/(2*\sqrt{b}*x**(5/2)*\sqrt{a/(b*x) + 1}) - 3*\sqrt{b}/(4*x**(3/2)*\sqrt{a/(b*x) + 1}) - b**(3/2)/(4*a*\sqrt{x}*\sqrt{a/(b*x) + 1}) + b**2*\operatorname{asinh}(\sqrt{a}/(\sqrt{b}*\sqrt{x}))/ (4*a**(3/2))$

$$3.291 \quad \int \frac{\sqrt{a+bx}}{x^4} dx$$

Optimal. Leaf size=87

$$-\frac{b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{5/2}} + \frac{b^2\sqrt{a+bx}}{8a^2x} - \frac{\sqrt{a+bx}}{3x^3} - \frac{b\sqrt{a+bx}}{12ax^2}$$

[Out] $-1/8*b^3*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(5/2)}-1/3*(b*x+a)^{(1/2)}/x^3-1/12*b*(b*x+a)^{(1/2)}/a/x^2+1/8*b^2*(b*x+a)^{(1/2)}/a^2/x$

Rubi [A] time = 0.03, antiderivative size = 87, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 51, 63, 208}

$$\frac{b^2\sqrt{a+bx}}{8a^2x} - \frac{b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{5/2}} - \frac{b\sqrt{a+bx}}{12ax^2} - \frac{\sqrt{a+bx}}{3x^3}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/x^4, x]

[Out] $-\operatorname{Sqrt}[a + b*x]/(3*x^3) - (b*\operatorname{Sqrt}[a + b*x])/(12*a*x^2) + (b^2*\operatorname{Sqrt}[a + b*x])/(8*a^2*x) - (b^3*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(8*a^{(5/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{a+bx}}{x^4} dx &= -\frac{\sqrt{a+bx}}{3x^3} + \frac{1}{6}b \int \frac{1}{x^3\sqrt{a+bx}} dx \\
&= -\frac{\sqrt{a+bx}}{3x^3} - \frac{b\sqrt{a+bx}}{12ax^2} - \frac{b^2 \int \frac{1}{x^2\sqrt{a+bx}} dx}{8a} \\
&= -\frac{\sqrt{a+bx}}{3x^3} - \frac{b\sqrt{a+bx}}{12ax^2} + \frac{b^2\sqrt{a+bx}}{8a^2x} + \frac{b^3 \int \frac{1}{x\sqrt{a+bx}} dx}{16a^2} \\
&= -\frac{\sqrt{a+bx}}{3x^3} - \frac{b\sqrt{a+bx}}{12ax^2} + \frac{b^2\sqrt{a+bx}}{8a^2x} + \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{8a^2} \\
&= -\frac{\sqrt{a+bx}}{3x^3} - \frac{b\sqrt{a+bx}}{12ax^2} + \frac{b^2\sqrt{a+bx}}{8a^2x} - \frac{b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{5/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.40

$$\frac{2b^3(a+bx)^{3/2} {}_2F_1\left(\frac{3}{2}, 4; \frac{5}{2}; \frac{bx}{a} + 1\right)}{3a^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[a + b*x]/x^4, x]
```

```
[Out] (2*b^3*(a + b*x)^(3/2)*Hypergeometric2F1[3/2, 4, 5/2, 1 + (b*x)/a])/(3*a^4)
```

fricas [A] time = 0.59, size = 145, normalized size = 1.67

$$\left[\frac{3\sqrt{a}b^3x^3 \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(3ab^2x^2 - 2a^2bx - 8a^3)\sqrt{bx+a}}{48a^3x^3}, \frac{3\sqrt{-a}b^3x^3 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) + (3ab^2x^2 - 2a^2bx - 8a^3)\sqrt{-a}}{24a^3x^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^4,x, algorithm="fricas")

[Out] [1/48*(3*sqrt(a)*b^3*x^3*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*(3*a*b^2*x^2 - 2*a^2*b*x - 8*a^3)*sqrt(b*x + a))/(a^3*x^3), 1/24*(3*sqrt(-a)*b^3*x^3*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (3*a*b^2*x^2 - 2*a^2*b*x - 8*a^3)*sqrt(b*x + a))/(a^3*x^3)]

giac [A] time = 1.23, size = 84, normalized size = 0.97

$$\frac{3b^4 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right) + \frac{3(bx+a)^2 b^4 - 8(bx+a)^2 ab^4 - 3\sqrt{bx+a} a^2 b^4}{a^2 b^3 x^3}}{\sqrt{-a} a^2} + \frac{3(bx+a)^2 b^4 - 8(bx+a)^2 ab^4 - 3\sqrt{bx+a} a^2 b^4}{24b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^4,x, algorithm="giac")

[Out] 1/24*(3*b^4*arctan(sqrt(b*x + a)/sqrt(-a))/(sqrt(-a)*a^2) + (3*(b*x + a)^(5/2)*b^4 - 8*(b*x + a)^(3/2)*a*b^4 - 3*sqrt(b*x + a)*a^2*b^4)/(a^2*b^3*x^3))/b

maple [A] time = 0.01, size = 65, normalized size = 0.75

$$2 \left(-\frac{\operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{16a^{\frac{5}{2}}} + \frac{-(bx+a)^{\frac{3}{2}}}{6a} + \frac{(bx+a)^{\frac{5}{2}}}{16a^2} - \frac{\sqrt{bx+a}}{16} \right) b^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/x^4,x)

[Out] 2*b^3*((1/16/a^2*(b*x+a)^(5/2)-1/6*(b*x+a)^(3/2)/a-1/16*(b*x+a)^(1/2))/x^3/b^3-1/16*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(5/2))

maxima [A] time = 3.02, size = 121, normalized size = 1.39

$$\frac{b^3 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{16a^{\frac{5}{2}}} + \frac{3(bx+a)^{\frac{5}{2}}b^3 - 8(bx+a)^{\frac{3}{2}}ab^3 - 3\sqrt{bx+a}a^2b^3}{24((bx+a)^3a^2 - 3(bx+a)^2a^3 + 3(bx+a)a^4 - a^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^4,x, algorithm="maxima")

[Out] $\frac{1}{16}b^3 \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right) / a^{5/2} + \frac{1}{24}(3(bx+a)^{5/2}b^3 - 8(bx+a)^{3/2}ab^3 - 3\sqrt{bx+a}a^2b^3) / ((bx+a)^3a^2 - 3(bx+a)^2a^3 + 3(bx+a)a^4 - a^5)$

mupad [B] time = 0.11, size = 66, normalized size = 0.76

$$\frac{(a+bx)^{5/2}}{8a^2x^3} - \frac{(a+bx)^{3/2}}{3ax^3} - \frac{\sqrt{a+bx}}{8x^3} + \frac{b^3 \operatorname{atan}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/x^4,x)

[Out] $(a + bx)^{5/2} / (8a^2x^3) - (a + bx)^{3/2} / (3ax^3) - (a + bx)^{1/2} / (8x^3) + (b^3 \operatorname{atan}((a + bx)^{1/2} / a^{1/2})) / (8a^{5/2})$

sympy [A] time = 6.68, size = 122, normalized size = 1.40

$$-\frac{a}{3\sqrt{b}x^2\sqrt{\frac{a}{bx}+1}} - \frac{5\sqrt{b}}{12x^2\sqrt{\frac{a}{bx}+1}} + \frac{b^{\frac{3}{2}}}{24ax^2\sqrt{\frac{a}{bx}+1}} + \frac{b^{\frac{5}{2}}}{8a^2\sqrt{x}\sqrt{\frac{a}{bx}+1}} - \frac{b^3 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{8a^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/x**4,x)

[Out] $-a / (3\sqrt{b}x^{7/2}\sqrt{a/(bx)+1}) - 5\sqrt{b} / (12x^{5/2}\sqrt{a/(bx)+1}) + b^{3/2} / (24ax^{3/2}\sqrt{a/(bx)+1}) + b^{5/2} / (8a^2x\sqrt{a/(bx)+1}) - b^3 \operatorname{asinh}(\sqrt{a}/(\sqrt{b}\sqrt{x})) / (8a^{5/2})$

3.292 $\int x^3(a + bx)^{3/2} dx$

Optimal. Leaf size=72

$$-\frac{2a^3(a + bx)^{5/2}}{5b^4} + \frac{6a^2(a + bx)^{7/2}}{7b^4} + \frac{2(a + bx)^{11/2}}{11b^4} - \frac{2a(a + bx)^{9/2}}{3b^4}$$

[Out] $-2/5*a^3*(b*x+a)^{(5/2)}/b^4+6/7*a^2*(b*x+a)^{(7/2)}/b^4-2/3*a*(b*x+a)^{(9/2)}/b^4+2/11*(b*x+a)^{(11/2)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{6a^2(a + bx)^{7/2}}{7b^4} - \frac{2a^3(a + bx)^{5/2}}{5b^4} + \frac{2(a + bx)^{11/2}}{11b^4} - \frac{2a(a + bx)^{9/2}}{3b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^(3/2), x]

[Out] $(-2*a^3*(a + b*x)^{(5/2)})/(5*b^4) + (6*a^2*(a + b*x)^{(7/2)})/(7*b^4) - (2*a*(a + b*x)^{(9/2)})/(3*b^4) + (2*(a + b*x)^{(11/2)})/(11*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^{3/2} dx &= \int \left(-\frac{a^3(a + bx)^{3/2}}{b^3} + \frac{3a^2(a + bx)^{5/2}}{b^3} - \frac{3a(a + bx)^{7/2}}{b^3} + \frac{(a + bx)^{9/2}}{b^3} \right) dx \\ &= -\frac{2a^3(a + bx)^{5/2}}{5b^4} + \frac{6a^2(a + bx)^{7/2}}{7b^4} - \frac{2a(a + bx)^{9/2}}{3b^4} + \frac{2(a + bx)^{11/2}}{11b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.64

$$\frac{2(a + bx)^{5/2} (-16a^3 + 40a^2bx - 70ab^2x^2 + 105b^3x^3)}{1155b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^(3/2), x]

[Out] (2*(a + b*x)^(5/2)*(-16*a^3 + 40*a^2*b*x - 70*a*b^2*x^2 + 105*b^3*x^3))/(1155*b^4)

fricas [A] time = 0.47, size = 64, normalized size = 0.89

$$\frac{2(105b^5x^5 + 140ab^4x^4 + 5a^2b^3x^3 - 6a^3b^2x^2 + 8a^4bx - 16a^5)\sqrt{bx+a}}{1155b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(3/2), x, algorithm="fricas")

[Out] 2/1155*(105*b^5*x^5 + 140*a*b^4*x^4 + 5*a^2*b^3*x^3 - 6*a^3*b^2*x^2 + 8*a^4*b*x - 16*a^5)*sqrt(b*x + a)/b^4

giac [B] time = 1.11, size = 193, normalized size = 2.68

$$2 \left(\frac{99 \left(5(bx+a)^{\frac{7}{2}} - 21(bx+a)^{\frac{5}{2}}a + 35(bx+a)^{\frac{3}{2}}a^2 - 35\sqrt{bx+a}a^3 \right) a^2}{b^3} + \frac{22 \left(35(bx+a)^{\frac{9}{2}} - 180(bx+a)^{\frac{7}{2}}a + 378(bx+a)^{\frac{5}{2}}a^2 - 420(bx+a)^{\frac{3}{2}}a^3 + 315\sqrt{bx+a}a^4 \right) a}{b^3} \right) / 3465b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(3/2), x, algorithm="giac")

[Out] 2/3465*(99*(5*(b*x + a)^(7/2) - 21*(b*x + a)^(5/2)*a + 35*(b*x + a)^(3/2)*a^2 - 35*sqrt(b*x + a)*a^3)*a^2/b^3 + 22*(35*(b*x + a)^(9/2) - 180*(b*x + a)^(7/2)*a + 378*(b*x + a)^(5/2)*a^2 - 420*(b*x + a)^(3/2)*a^3 + 315*sqrt(b*x + a)*a^4)*a/b^3 + 5*(63*(b*x + a)^(11/2) - 385*(b*x + a)^(9/2)*a + 990*(b*x + a)^(7/2)*a^2 - 1386*(b*x + a)^(5/2)*a^3 + 1155*(b*x + a)^(3/2)*a^4 - 693*sqrt(b*x + a)*a^5)/b^3/b

maple [A] time = 0.00, size = 43, normalized size = 0.60

$$\frac{2(bx+a)^{\frac{5}{2}}(-105b^3x^3 + 70ab^2x^2 - 40a^2bx + 16a^3)}{1155b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^(3/2), x)

[Out] -2/1155*(b*x+a)^(5/2)*(-105*b^3*x^3+70*a*b^2*x^2-40*a^2*b*x+16*a^3)/b^4

maxima [A] time = 1.35, size = 56, normalized size = 0.78

$$\frac{2(bx+a)^{\frac{11}{2}}}{11b^4} - \frac{2(bx+a)^{\frac{9}{2}}a}{3b^4} + \frac{6(bx+a)^{\frac{7}{2}}a^2}{7b^4} - \frac{2(bx+a)^{\frac{5}{2}}a^3}{5b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(3/2),x, algorithm="maxima")

[Out] 2/11*(b*x + a)^(11/2)/b^4 - 2/3*(b*x + a)^(9/2)*a/b^4 + 6/7*(b*x + a)^(7/2)*a^2/b^4 - 2/5*(b*x + a)^(5/2)*a^3/b^4

mupad [B] time = 0.05, size = 56, normalized size = 0.78

$$\frac{2(a+bx)^{11/2}}{11b^4} - \frac{2a^3(a+bx)^{5/2}}{5b^4} + \frac{6a^2(a+bx)^{7/2}}{7b^4} - \frac{2a(a+bx)^{9/2}}{3b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(a + b*x)^(3/2),x)

[Out] (2*(a + b*x)^(11/2))/(11*b^4) - (2*a^3*(a + b*x)^(5/2))/(5*b^4) + (6*a^2*(a + b*x)^(7/2))/(7*b^4) - (2*a*(a + b*x)^(9/2))/(3*b^4)

sympy [B] time = 3.20, size = 1742, normalized size = 24.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**(3/2),x)

[Out] -32*a**(51/2)*sqrt(1 + b*x/a)/(1155*a**20*b**4 + 6930*a**19*b**5*x + 17325*a**18*b**6*x**2 + 23100*a**17*b**7*x**3 + 17325*a**16*b**8*x**4 + 6930*a**15*b**9*x**5 + 1155*a**14*b**10*x**6) + 32*a**(51/2)/(1155*a**20*b**4 + 6930*a**19*b**5*x + 17325*a**18*b**6*x**2 + 23100*a**17*b**7*x**3 + 17325*a**16*b**8*x**4 + 6930*a**15*b**9*x**5 + 1155*a**14*b**10*x**6) - 176*a**(49/2)*b*x*sqrt(1 + b*x/a)/(1155*a**20*b**4 + 6930*a**19*b**5*x + 17325*a**18*b**6*x**2 + 23100*a**17*b**7*x**3 + 17325*a**16*b**8*x**4 + 6930*a**15*b**9*x**5 + 1155*a**14*b**10*x**6) + 192*a**(49/2)*b*x/(1155*a**20*b**4 + 6930*a**19*b**5*x + 17325*a**18*b**6*x**2 + 23100*a**17*b**7*x**3 + 17325*a**16*b**8*x**4 + 6930*a**15*b**9*x**5 + 1155*a**14*b**10*x**6) - 396*a**(47/2)*b**2*x**2*sqrt(1 + b*x/a)/(1155*a**20*b**4 + 6930*a**19*b**5*x + 17325*a**18*b**6*x**2 + 23100*a**17*b**7*x**3 + 17325*a**16*b**8*x**4 + 6930*a**15*b**9*x**5 + 1155*a**14*b**10*x**6) + 480*a**(47/2)*b**2*x**2/(1155*a**20*b**4 + 6930*a**19*b**5*x + 17325*a**18*b**6*x**2 + 23100*a**17*b**7*x**3 + 17325*a**16*b**8*x**4 + 6930*a**15*b**9*x**5 + 1155*a**14*b**10*x**6) + 480*a**(47/2)*b**2*x**2/(1155*a**20*b**4 + 6930*a**19*b**5*x + 17325*a**18*b**6*x**2 + 23100*a**17*b**7*x**3 + 17325*a**16*b**8*x**4 + 6930*a**15*b**9*x**5 + 1155*a**14*b**10*x**6)

$$\begin{aligned}
& 16b^{**8}x^{**4} + 6930a^{**15}b^{**9}x^{**5} + 1155a^{**14}b^{**10}x^{**6}) - 462a^{**}(45/2) \\
&)b^{**3}x^{**3}\sqrt{1 + b*x/a}/(1155a^{**20}b^{**4} + 6930a^{**19}b^{**5}x + 17325a^{**} \\
& *18b^{**6}x^{**2} + 23100a^{**17}b^{**7}x^{**3} + 17325a^{**16}b^{**8}x^{**4} + 6930a^{**15} \\
& b^{**9}x^{**5} + 1155a^{**14}b^{**10}x^{**6}) + 640a^{**}(45/2)b^{**3}x^{**3}/(1155a^{**20}b^{**} \\
& *4 + 6930a^{**19}b^{**5}x + 17325a^{**18}b^{**6}x^{**2} + 23100a^{**17}b^{**7}x^{**3} + 17 \\
& 325a^{**16}b^{**8}x^{**4} + 6930a^{**15}b^{**9}x^{**5} + 1155a^{**14}b^{**10}x^{**6}) + 480a \\
& ** (43/2)b^{**4}x^{**4}/(1155a^{**20}b^{**4} + 6930a^{**19}b^{**5}x + 17325a^{**18}b^{**6}x \\
& **2 + 23100a^{**17}b^{**7}x^{**3} + 17325a^{**16}b^{**8}x^{**4} + 6930a^{**15}b^{**9}x^{**5} \\
& + 1155a^{**14}b^{**10}x^{**6}) + 1848a^{**}(41/2)b^{**5}x^{**5}\sqrt{1 + b*x/a}/(1155a \\
& **20b^{**4} + 6930a^{**19}b^{**5}x + 17325a^{**18}b^{**6}x^{**2} + 23100a^{**17}b^{**7}x \\
& **3 + 17325a^{**16}b^{**8}x^{**4} + 6930a^{**15}b^{**9}x^{**5} + 1155a^{**14}b^{**10}x^{**6}) \\
& + 192a^{**}(41/2)b^{**5}x^{**5}/(1155a^{**20}b^{**4} + 6930a^{**19}b^{**5}x + 17325a^{**} \\
& 18b^{**6}x^{**2} + 23100a^{**17}b^{**7}x^{**3} + 17325a^{**16}b^{**8}x^{**4} + 6930a^{**15}b \\
& **9x^{**5} + 1155a^{**14}b^{**10}x^{**6}) + 5544a^{**}(39/2)b^{**6}x^{**6}\sqrt{1 + b*x/a} \\
&)/(1155a^{**20}b^{**4} + 6930a^{**19}b^{**5}x + 17325a^{**18}b^{**6}x^{**2} + 23100a^{**1} \\
& 7b^{**7}x^{**3} + 17325a^{**16}b^{**8}x^{**4} + 6930a^{**15}b^{**9}x^{**5} + 1155a^{**14}b^{**} \\
& 10x^{**6}) + 32a^{**}(39/2)b^{**6}x^{**6}/(1155a^{**20}b^{**4} + 6930a^{**19}b^{**5}x + 17 \\
& 325a^{**18}b^{**6}x^{**2} + 23100a^{**17}b^{**7}x^{**3} + 17325a^{**16}b^{**8}x^{**4} + 6930a \\
& **15b^{**9}x^{**5} + 1155a^{**14}b^{**10}x^{**6}) + 8844a^{**}(37/2)b^{**7}x^{**7}\sqrt{1 \\
& + b*x/a}/(1155a^{**20}b^{**4} + 6930a^{**19}b^{**5}x + 17325a^{**18}b^{**6}x^{**2} + 231 \\
& 00a^{**17}b^{**7}x^{**3} + 17325a^{**16}b^{**8}x^{**4} + 6930a^{**15}b^{**9}x^{**5} + 1155a^{**} \\
& *14b^{**10}x^{**6}) + 8448a^{**}(35/2)b^{**8}x^{**8}\sqrt{1 + b*x/a}/(1155a^{**20}b^{**4} \\
& + 6930a^{**19}b^{**5}x + 17325a^{**18}b^{**6}x^{**2} + 23100a^{**17}b^{**7}x^{**3} + 1732 \\
& 5a^{**16}b^{**8}x^{**4} + 6930a^{**15}b^{**9}x^{**5} + 1155a^{**14}b^{**10}x^{**6}) + 4840a^{**} \\
& *(33/2)b^{**9}x^{**9}\sqrt{1 + b*x/a}/(1155a^{**20}b^{**4} + 6930a^{**19}b^{**5}x + 17 \\
& 325a^{**18}b^{**6}x^{**2} + 23100a^{**17}b^{**7}x^{**3} + 17325a^{**16}b^{**8}x^{**4} + 6930a \\
& **15b^{**9}x^{**5} + 1155a^{**14}b^{**10}x^{**6}) + 1540a^{**}(31/2)b^{**10}x^{**10}\sqrt{(\\
& 1 + b*x/a)/(1155a^{**20}b^{**4} + 6930a^{**19}b^{**5}x + 17325a^{**18}b^{**6}x^{**2} + 2 \\
& 3100a^{**17}b^{**7}x^{**3} + 17325a^{**16}b^{**8}x^{**4} + 6930a^{**15}b^{**9}x^{**5} + 1155a \\
& **14b^{**10}x^{**6}) + 210a^{**}(29/2)b^{**11}x^{**11}\sqrt{1 + b*x/a}/(1155a^{**20}b \\
& **4 + 6930a^{**19}b^{**5}x + 17325a^{**18}b^{**6}x^{**2} + 23100a^{**17}b^{**7}x^{**3} + 1 \\
& 7325a^{**16}b^{**8}x^{**4} + 6930a^{**15}b^{**9}x^{**5} + 1155a^{**14}b^{**10}x^{**6})
\end{aligned}$$

3.293 $\int x^2(a + bx)^{3/2} dx$

Optimal. Leaf size=53

$$\frac{2a^2(a + bx)^{5/2}}{5b^3} + \frac{2(a + bx)^{9/2}}{9b^3} - \frac{4a(a + bx)^{7/2}}{7b^3}$$

[Out] $2/5*a^2*(b*x+a)^{(5/2)}/b^3-4/7*a*(b*x+a)^{(7/2)}/b^3+2/9*(b*x+a)^{(9/2)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2a^2(a + bx)^{5/2}}{5b^3} + \frac{2(a + bx)^{9/2}}{9b^3} - \frac{4a(a + bx)^{7/2}}{7b^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*(a + b*x)^{(3/2)}, x]$

[Out] $(2*a^2*(a + b*x)^{(5/2)})/(5*b^3) - (4*a*(a + b*x)^{(7/2)})/(7*b^3) + (2*(a + b*x)^{(9/2)})/(9*b^3)$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{IGtQ}[m, 0] \&\& (!\text{IntegerQ}[n] || (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0]) || \text{LtQ}[9*m + 5*(n + 1), 0] || \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^{3/2} dx &= \int \left(\frac{a^2(a + bx)^{3/2}}{b^2} - \frac{2a(a + bx)^{5/2}}{b^2} + \frac{(a + bx)^{7/2}}{b^2} \right) dx \\ &= \frac{2a^2(a + bx)^{5/2}}{5b^3} - \frac{4a(a + bx)^{7/2}}{7b^3} + \frac{2(a + bx)^{9/2}}{9b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.66

$$\frac{2(a + bx)^{5/2} (8a^2 - 20abx + 35b^2x^2)}{315b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^(3/2), x]

[Out] (2*(a + b*x)^(5/2)*(8*a^2 - 20*a*b*x + 35*b^2*x^2))/(315*b^3)

fricas [A] time = 0.48, size = 53, normalized size = 1.00

$$\frac{2(35b^4x^4 + 50ab^3x^3 + 3a^2b^2x^2 - 4a^3bx + 8a^4)\sqrt{bx+a}}{315b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(3/2), x, algorithm="fricas")

[Out] 2/315*(35*b^4*x^4 + 50*a*b^3*x^3 + 3*a^2*b^2*x^2 - 4*a^3*b*x + 8*a^4)*sqrt(b*x + a)/b^3

giac [B] time = 0.94, size = 156, normalized size = 2.94

$$2 \left(\frac{21 \left(3(bx+a)^{\frac{5}{2}} - 10(bx+a)^{\frac{3}{2}}a + 15\sqrt{bx+a}a^2 \right) a^2}{b^2} + \frac{18 \left(5(bx+a)^{\frac{7}{2}} - 21(bx+a)^{\frac{5}{2}}a + 35(bx+a)^{\frac{3}{2}}a^2 - 35\sqrt{bx+a}a^3 \right) a}{b^2} + \frac{35(bx+a)^{\frac{9}{2}} - 180(bx+a)^{\frac{7}{2}}a + 378a^2}{b^2} \right) / 315b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(3/2), x, algorithm="giac")

[Out] 2/315*(21*(3*(b*x + a)^(5/2) - 10*(b*x + a)^(3/2)*a + 15*sqrt(b*x + a)*a^2)*a^2/b^2 + 18*(5*(b*x + a)^(7/2) - 21*(b*x + a)^(5/2)*a + 35*(b*x + a)^(3/2))*a^2 - 35*sqrt(b*x + a)*a^3)*a/b^2 + (35*(b*x + a)^(9/2) - 180*(b*x + a)^(7/2)*a + 378*(b*x + a)^(5/2)*a^2 - 420*(b*x + a)^(3/2)*a^3 + 315*sqrt(b*x + a)*a^4)/b^2)/b

maple [A] time = 0.01, size = 32, normalized size = 0.60

$$\frac{2(bx+a)^{\frac{5}{2}}(35b^2x^2 - 20abx + 8a^2)}{315b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^(3/2), x)

[Out] 2/315*(b*x+a)^(5/2)*(35*b^2*x^2-20*a*b*x+8*a^2)/b^3

maxima [A] time = 1.35, size = 41, normalized size = 0.77

$$\frac{2(bx+a)^{\frac{9}{2}}}{9b^3} - \frac{4(bx+a)^{\frac{7}{2}}a}{7b^3} + \frac{2(bx+a)^{\frac{5}{2}}a^2}{5b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(3/2),x, algorithm="maxima")

[Out] $2/9*(b*x + a)^{(9/2)}/b^3 - 4/7*(b*x + a)^{(7/2)}*a/b^3 + 2/5*(b*x + a)^{(5/2)}*a^2/b^3$

mupad [B] time = 0.04, size = 37, normalized size = 0.70

$$\frac{70(a+bx)^{9/2} - 180a(a+bx)^{7/2} + 126a^2(a+bx)^{5/2}}{315b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a + b*x)^(3/2),x)

[Out] $(70*(a + b*x)^{(9/2)} - 180*a*(a + b*x)^{(7/2)} + 126*a^2*(a + b*x)^{(5/2)})/(315*b^3)$

sympy [B] time = 2.17, size = 733, normalized size = 13.83

$$\frac{16a^{\frac{25}{2}}\sqrt{1+\frac{bx}{a}}}{315a^8b^3 + 945a^7b^4x + 945a^6b^5x^2 + 315a^5b^6x^3} - \frac{16a^{\frac{25}{2}}}{315a^8b^3 + 945a^7b^4x + 945a^6b^5x^2 + 315a^5b^6x^3} + \frac{16a^{\frac{25}{2}}}{315a^8b^3 + 945a^7b^4x + 945a^6b^5x^2 + 315a^5b^6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)**(3/2),x)

[Out] $16*a**(25/2)*\text{sqrt}(1 + b*x/a)/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) - 16*a**(25/2)/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) + 40*a**(23/2)*b*x*\text{sqrt}(1 + b*x/a)/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) - 48*a**(23/2)*b*x/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) + 30*a**(21/2)*b**2*x**2*\text{sqrt}(1 + b*x/a)/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) - 48*a**(21/2)*b**2*x**2/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) + 110*a**(19/2)*b**3*x**3*\text{sqrt}(1 + b*x/a)/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) - 16*a**(19/2)*b**3*x**3/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) + 380*a**(17/2)*b**4*x**4*\text{sqrt}(1 + b*x/a)/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) + 516*a**(15/2)*b**5*x**5*\text{sqrt}(1 + b*x/a)/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) + 310*a**(13/2)*b**6*x**6*\text{sqrt}(1 + b*x/a)/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3) + 70*a**(11/2)*b**7*x**7*\text{sqrt}(1 + b*x/a)/(315*a**8*b**3 + 945*a**7*b**4*x + 945*a**6*b**5*x**2 + 315*a**5*b**6*x**3)$

3.294 $\int x(a + bx)^{3/2} dx$

Optimal. Leaf size=34

$$\frac{2(a + bx)^{7/2}}{7b^2} - \frac{2a(a + bx)^{5/2}}{5b^2}$$

[Out] $-2/5*a*(b*x+a)^{(5/2)}/b^2+2/7*(b*x+a)^{(7/2)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{2(a + bx)^{7/2}}{7b^2} - \frac{2a(a + bx)^{5/2}}{5b^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^(3/2), x]

[Out] $(-2*a*(a + b*x)^{(5/2)})/(5*b^2) + (2*(a + b*x)^{(7/2)})/(7*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x(a + bx)^{3/2} dx &= \int \left(-\frac{a(a + bx)^{3/2}}{b} + \frac{(a + bx)^{5/2}}{b} \right) dx \\ &= -\frac{2a(a + bx)^{5/2}}{5b^2} + \frac{2(a + bx)^{7/2}}{7b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.71

$$\frac{2(a + bx)^{5/2}(5bx - 2a)}{35b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^(3/2), x]

[Out] $(2*(a + b*x)^{(5/2)*(-2*a + 5*b*x)})/(35*b^2)$

fricas [A] time = 0.50, size = 41, normalized size = 1.21

$$\frac{2(5b^3x^3 + 8ab^2x^2 + a^2bx - 2a^3)\sqrt{bx+a}}{35b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(3/2),x, algorithm="fricas")`

[Out] $2/35*(5*b^3*x^3 + 8*a*b^2*x^2 + a^2*b*x - 2*a^3)*\text{sqrt}(b*x + a)/b^2$

giac [B] time = 1.24, size = 119, normalized size = 3.50

$$\frac{2 \left(\frac{35 \left((bx+a)^{\frac{3}{2}} - 3 \sqrt{bx+a} a \right) a^2}{b} + \frac{14 \left(3 (bx+a)^{\frac{5}{2}} - 10 (bx+a)^{\frac{3}{2}} a + 15 \sqrt{bx+a} a^2 \right) a}{b} + \frac{3 \left(5 (bx+a)^{\frac{7}{2}} - 21 (bx+a)^{\frac{5}{2}} a + 35 (bx+a)^{\frac{3}{2}} a^2 - 35 \sqrt{bx+a} a^3 \right)}{b} \right)}{105b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(3/2),x, algorithm="giac")`

[Out] $2/105*(35*((b*x + a)^{(3/2)} - 3*\text{sqrt}(b*x + a)*a)*a^2/b + 14*(3*(b*x + a)^{(5/2)} - 10*(b*x + a)^{(3/2)}*a + 15*\text{sqrt}(b*x + a)*a^2)*a/b + 3*(5*(b*x + a)^{(7/2)} - 21*(b*x + a)^{(5/2)}*a + 35*(b*x + a)^{(3/2)}*a^2 - 35*\text{sqrt}(b*x + a)*a^3)/b)$

maple [A] time = 0.00, size = 21, normalized size = 0.62

$$\frac{2(bx+a)^{\frac{5}{2}}(-5bx+2a)}{35b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)^(3/2),x)`

[Out] $-2/35*(b*x+a)^{(5/2)*(-5*b*x+2*a)}/b^2$

maxima [A] time = 1.35, size = 26, normalized size = 0.76

$$\frac{2(bx+a)^{\frac{7}{2}}}{7b^2} - \frac{2(bx+a)^{\frac{5}{2}}a}{5b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^(3/2),x, algorithm="maxima")

[Out] $\frac{2}{7}(bx + a)^{7/2}/b^2 - \frac{2}{5}(bx + a)^{5/2} * a/b^2$

mupad [B] time = 0.03, size = 25, normalized size = 0.74

$$-\frac{14a(a+bx)^{5/2} - 10(a+bx)^{7/2}}{35b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a + b*x)^(3/2),x)

[Out] $-(14*a*(a + b*x)^{5/2} - 10*(a + b*x)^{7/2})/(35*b^2)$

sympy [A] time = 0.74, size = 80, normalized size = 2.35

$$\begin{cases} -\frac{4a^3\sqrt{a+bx}}{35b^2} + \frac{2a^2x\sqrt{a+bx}}{35b} + \frac{16ax^2\sqrt{a+bx}}{35} + \frac{2bx^3\sqrt{a+bx}}{7} & \text{for } b \neq 0 \\ \frac{a^{\frac{3}{2}}x^2}{2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)**(3/2),x)

[Out] Piecewise((-4*a**3*sqrt(a + b*x)/(35*b**2) + 2*a**2*x*sqrt(a + b*x)/(35*b) + 16*a*x**2*sqrt(a + b*x)/35 + 2*b*x**3*sqrt(a + b*x)/7, Ne(b, 0)), (a**(3/2)*x**2/2, True))

3.295 $\int (a + bx)^{3/2} dx$

Optimal. Leaf size=16

$$\frac{2(a + bx)^{5/2}}{5b}$$

[Out] $2/5*(b*x+a)^{(5/2)}/b$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{2(a + bx)^{5/2}}{5b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2), x]

[Out] (2*(a + b*x)^(5/2))/(5*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^{3/2} dx = \frac{2(a + bx)^{5/2}}{5b}$$

Mathematica [A] time = 0.01, size = 16, normalized size = 1.00

$$\frac{2(a + bx)^{5/2}}{5b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2), x]

[Out] (2*(a + b*x)^(5/2))/(5*b)

fricas [B] time = 0.44, size = 28, normalized size = 1.75

$$\frac{2(b^2x^2 + 2abx + a^2)\sqrt{bx + a}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2),x, algorithm="fricas")

[Out] 2/5*(b^2*x^2 + 2*a*b*x + a^2)*sqrt(b*x + a)/b

giac [B] time = 1.13, size = 58, normalized size = 3.62

$$\frac{2 \left(3 (bx + a)^{\frac{5}{2}} - 10 (bx + a)^{\frac{3}{2}} a + 30 \sqrt{bx + a} a^2 + 10 \left((bx + a)^{\frac{3}{2}} - 3 \sqrt{bx + a} a \right) a \right)}{15b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2),x, algorithm="giac")

[Out] 2/15*(3*(b*x + a)^(5/2) - 10*(b*x + a)^(3/2)*a + 30*sqrt(b*x + a)*a^2 + 10*((b*x + a)^(3/2) - 3*sqrt(b*x + a)*a)*a)/b

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{2 (bx + a)^{\frac{5}{2}}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2),x)

[Out] 2/5*(b*x+a)^(5/2)/b

maxima [A] time = 1.29, size = 12, normalized size = 0.75

$$\frac{2 (bx + a)^{\frac{5}{2}}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2),x, algorithm="maxima")

[Out] 2/5*(b*x + a)^(5/2)/b

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{2 (a + bx)^{\frac{5}{2}}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(3/2),x)
```

```
[Out] (2*(a + b*x)^(5/2))/(5*b)
```

sympy [A] time = 0.07, size = 12, normalized size = 0.75

$$\frac{2(a + bx)^{\frac{5}{2}}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(3/2),x)
```

```
[Out] 2*(a + b*x)**(5/2)/(5*b)
```

$$3.296 \quad \int \frac{(a+bx)^{3/2}}{x} dx$$

Optimal. Leaf size=49

$$-2a^{3/2} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + 2a\sqrt{a+bx} + \frac{2}{3}(a+bx)^{3/2}$$

[Out] 2/3*(b*x+a)^(3/2)-2*a^(3/2)*arctanh((b*x+a)^(1/2)/a^(1/2))+2*a*(b*x+a)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {50, 63, 208}

$$-2a^{3/2} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + 2a\sqrt{a+bx} + \frac{2}{3}(a+bx)^{3/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)/x, x]

[Out] 2*a*Sqrt[a + b*x] + (2*(a + b*x)^(3/2))/3 - 2*a^(3/2)*ArcTanh[Sqrt[a + b*x]/Sqrt[a]]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

`Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{3/2}}{x} dx &= \frac{2}{3}(a+bx)^{3/2} + a \int \frac{\sqrt{a+bx}}{x} dx \\
 &= 2a\sqrt{a+bx} + \frac{2}{3}(a+bx)^{3/2} + a^2 \int \frac{1}{x\sqrt{a+bx}} dx \\
 &= 2a\sqrt{a+bx} + \frac{2}{3}(a+bx)^{3/2} + \frac{(2a^2) \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{b} \\
 &= 2a\sqrt{a+bx} + \frac{2}{3}(a+bx)^{3/2} - 2a^{3/2} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)
 \end{aligned}$$

Mathematica [A] time = 0.02, size = 44, normalized size = 0.90

$$\frac{2}{3}\sqrt{a+bx}(4a+bx) - 2a^{3/2} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/x,x]

[Out] (2*Sqrt[a + b*x]*(4*a + b*x))/3 - 2*a^(3/2)*ArcTanh[Sqrt[a + b*x]/Sqrt[a]]

fricas [A] time = 0.51, size = 88, normalized size = 1.80

$$\left[a^{\frac{3}{2}} \log\left(\frac{bx - 2\sqrt{bx+a}\sqrt{a} + 2a}{x}\right) + \frac{2}{3}(bx + 4a)\sqrt{bx+a}, 2\sqrt{-a}a \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) + \frac{2}{3}(bx + 4a)\sqrt{bx+a} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x,x, algorithm="fricas")

[Out] [a^(3/2)*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2/3*(b*x + 4*a)*sqrt(b*x + a), 2*sqrt(-a)*a*arctan(sqrt(b*x + a)*sqrt(-a)/a) + 2/3*(b*x + 4*a)*sqrt(b*x + a)]

giac [A] time = 1.08, size = 44, normalized size = 0.90

$$\frac{2a^2 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} + \frac{2}{3}(bx+a)^{\frac{3}{2}} + 2\sqrt{bx+a}a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x,x, algorithm="giac")

[Out] 2*a^2*arctan(sqrt(b*x + a)/sqrt(-a))/sqrt(-a) + 2/3*(b*x + a)^(3/2) + 2*sqrt(b*x + a)*a

maple [A] time = 0.01, size = 38, normalized size = 0.78

$$-2a^{\frac{3}{2}} \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right) + 2\sqrt{bx+a}a + \frac{2(bx+a)^{\frac{3}{2}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/x,x)

[Out] 2/3*(b*x+a)^(3/2)-2*a^(3/2)*arctanh((b*x+a)^(1/2)/a^(1/2))+2*a*(b*x+a)^(1/2)

maxima [A] time = 2.94, size = 52, normalized size = 1.06

$$a^{\frac{3}{2}} \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right) + \frac{2}{3}(bx+a)^{\frac{3}{2}} + 2\sqrt{bx+a}a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x,x, algorithm="maxima")

[Out] a^(3/2)*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a))) + 2/3*(b*x + a)^(3/2) + 2*sqrt(b*x + a)*a

mupad [B] time = 0.04, size = 37, normalized size = 0.76

$$2a\sqrt{a+bx} + \frac{2(a+bx)^{3/2}}{3} - 2a^{3/2} \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/x,x)

[Out] $2*a*(a + b*x)^{(1/2)} + (2*(a + b*x)^{(3/2)})/3 - 2*a^{(3/2)}*atanh((a + b*x)^{(1/2)}/a^{(1/2)})$

sympy [A] time = 2.29, size = 71, normalized size = 1.45

$$\frac{8a^{\frac{3}{2}}\sqrt{1 + \frac{bx}{a}}}{3} + a^{\frac{3}{2}}\log\left(\frac{bx}{a}\right) - 2a^{\frac{3}{2}}\log\left(\sqrt{1 + \frac{bx}{a}} + 1\right) + \frac{2\sqrt{a}bx\sqrt{1 + \frac{bx}{a}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/x,x)

[Out] $8*a^{(3/2)}*\sqrt{1 + b*x/a}/3 + a^{(3/2)}*\log(b*x/a) - 2*a^{(3/2)}*\log(\sqrt{1 + b*x/a} + 1) + 2*\sqrt{a}*b*x*\sqrt{1 + b*x/a}/3$

$$3.297 \quad \int \frac{(a+bx)^{3/2}}{x^2} dx$$

Optimal. Leaf size=51

$$-\frac{(a+bx)^{3/2}}{x} + 3b\sqrt{a+bx} - 3\sqrt{a}b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)$$

[Out] $-(b*x+a)^{(3/2)}/x-3*b*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})*a^{(1/2)}+3*b*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 208}

$$-\frac{(a+bx)^{3/2}}{x} + 3b\sqrt{a+bx} - 3\sqrt{a}b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)/x^2, x]

[Out] $3*b*\operatorname{Sqrt}[a + b*x] - (a + b*x)^{(3/2)}/x - 3*\operatorname{Sqrt}[a]*b*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]]$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63


```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{x^2} dx &= -\frac{(a+bx)^{3/2}}{x} + \frac{1}{2}(3b) \int \frac{\sqrt{a+bx}}{x} dx \\
&= 3b\sqrt{a+bx} - \frac{(a+bx)^{3/2}}{x} + \frac{1}{2}(3ab) \int \frac{1}{x\sqrt{a+bx}} dx \\
&= 3b\sqrt{a+bx} - \frac{(a+bx)^{3/2}}{x} + (3a) \operatorname{Subst} \left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx} \right) \\
&= 3b\sqrt{a+bx} - \frac{(a+bx)^{3/2}}{x} - 3\sqrt{a} b \tanh^{-1} \left(\frac{\sqrt{a+bx}}{\sqrt{a}} \right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.65

$$\frac{2b(a+bx)^{5/2} {}_2F_1\left(2, \frac{5}{2}; \frac{7}{2}; \frac{bx}{a} + 1\right)}{5a^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/x^2,x]

[Out] (2*b*(a + b*x)^(5/2)*Hypergeometric2F1[2, 5/2, 7/2, 1 + (b*x)/a])/(5*a^2)

fricas [A] time = 0.47, size = 102, normalized size = 2.00

$$\left[\frac{3\sqrt{a}bx \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(2bx-a)\sqrt{bx+a}}{2x}, \frac{3\sqrt{-a}bx \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) + (2bx-a)\sqrt{bx+a}}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^2,x, algorithm="fricas")

[Out] [1/2*(3*sqrt(a)*b*x*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*(2*b*x - a)*sqrt(b*x + a))/x, (3*sqrt(-a)*b*x*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (2*b*x - a)*sqrt(b*x + a))/x]

giac [A] time = 1.04, size = 56, normalized size = 1.10

$$\frac{\frac{3ab^2 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} + 2\sqrt{bx+a}b^2 - \frac{\sqrt{bx+a}ab}{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^2,x, algorithm="giac")

[Out] (3*a*b^2*arctan(sqrt(b*x + a)/sqrt(-a))/sqrt(-a) + 2*sqrt(b*x + a)*b^2 - sqrt(b*x + a)*a*b/x)/b

maple [A] time = 0.01, size = 47, normalized size = 0.92

$$2 \left(\left(-\frac{3 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{2\sqrt{a}} - \frac{\sqrt{bx+a}}{2bx} \right) a + \sqrt{bx+a} \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/x^2,x)

[Out] 2*b*((b*x+a)^(1/2)+a*(-1/2*(b*x+a)^(1/2)/b/x-3/2*arctanh((b*x+a)^(1/2)/a^(1/2)))/a^(1/2))

maxima [A] time = 2.87, size = 58, normalized size = 1.14

$$\frac{3}{2} \sqrt{a} b \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right) + 2\sqrt{bx+a}b - \frac{\sqrt{bx+a}a}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^2,x, algorithm="maxima")

[Out] 3/2*sqrt(a)*b*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a))) + 2*sqrt(b*x + a)*b - sqrt(b*x + a)*a/x

mupad [B] time = 0.10, size = 42, normalized size = 0.82

$$2b\sqrt{a+bx} - 3\sqrt{a}b \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) - \frac{a\sqrt{a+bx}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(3/2)/x^2, x)`

[Out] `2*b*(a + b*x)^(1/2) - 3*a^(1/2)*b*atanh((a + b*x)^(1/2)/a^(1/2)) - (a*(a + b*x)^(1/2))/x`

sympy [B] time = 2.66, size = 92, normalized size = 1.80

$$-3\sqrt{a}b \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) - \frac{a^2}{\sqrt{b}x^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}} + \frac{a\sqrt{b}}{\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{2b^{\frac{3}{2}}\sqrt{x}}{\sqrt{\frac{a}{bx}+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(3/2)/x**2, x)`

[Out] `-3*sqrt(a)*b*asinh(sqrt(a)/(sqrt(b)*sqrt(x))) - a**2/(sqrt(b)*x**(3/2)*sqrt(a/(b*x) + 1)) + a*sqrt(b)/(sqrt(x)*sqrt(a/(b*x) + 1)) + 2*b**(3/2)*sqrt(x)/sqrt(a/(b*x) + 1)`

$$3.298 \quad \int \frac{(a+bx)^{3/2}}{x^3} dx$$

Optimal. Leaf size=62

$$-\frac{3b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4\sqrt{a}} - \frac{(a+bx)^{3/2}}{2x^2} - \frac{3b\sqrt{a+bx}}{4x}$$

[Out] $-1/2*(b*x+a)^{(3/2)}/x^2-3/4*b^2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(1/2)}-3/4*b*(b*x+a)^{(1/2)}/x$

Rubi [A] time = 0.02, antiderivative size = 62, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {47, 63, 208}

$$-\frac{3b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4\sqrt{a}} - \frac{(a+bx)^{3/2}}{2x^2} - \frac{3b\sqrt{a+bx}}{4x}$$

Antiderivative was successfully verified.

[In] `Int[(a + b*x)^(3/2)/x^3, x]`

[Out] $(-3*b*\operatorname{Sqrt}[a + b*x])/(4*x) - (a + b*x)^{(3/2)}/(2*x^2) - (3*b^2*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(4*\operatorname{Sqrt}[a])$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

`Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{3/2}}{x^3} dx &= -\frac{(a+bx)^{3/2}}{2x^2} + \frac{1}{4}(3b) \int \frac{\sqrt{a+bx}}{x^2} dx \\
 &= -\frac{3b\sqrt{a+bx}}{4x} - \frac{(a+bx)^{3/2}}{2x^2} + \frac{1}{8}(3b^2) \int \frac{1}{x\sqrt{a+bx}} dx \\
 &= -\frac{3b\sqrt{a+bx}}{4x} - \frac{(a+bx)^{3/2}}{2x^2} + \frac{1}{4}(3b) \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right) \\
 &= -\frac{3b\sqrt{a+bx}}{4x} - \frac{(a+bx)^{3/2}}{2x^2} - \frac{3b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4\sqrt{a}}
 \end{aligned}$$

Mathematica [A] time = 0.03, size = 68, normalized size = 1.10

$$\frac{2a^2 + 3b^2x^2\sqrt{\frac{bx}{a}} + 1 \tanh^{-1}\left(\sqrt{\frac{bx}{a}} + 1\right) + 7abx + 5b^2x^2}{4x^2\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] `Integrate[(a + b*x)^(3/2)/x^3, x]`

[Out] `-1/4*(2*a^2 + 7*a*b*x + 5*b^2*x^2 + 3*b^2*x^2*Sqrt[1 + (b*x)/a]*ArcTanh[Sqrt[1 + (b*x)/a]])/(x^2*Sqrt[a + b*x])`

fricas [A] time = 0.52, size = 124, normalized size = 2.00

$$\left[\frac{3\sqrt{a}b^2x^2 \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2(5abx + 2a^2)\sqrt{bx+a}}{8ax^2}, \frac{3\sqrt{-a}b^2x^2 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) - (5abx + 2a^2)\sqrt{-a}}{4ax^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/2)/x^3, x, algorithm="fricas")`

[Out] `[1/8*(3*sqrt(a)*b^2*x^2*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) - 2*(5*a*b*x + 2*a^2)*sqrt(b*x + a))/(a*x^2), 1/4*(3*sqrt(-a)*b^2*x^2*arctan(sqrt(b*x + a)*sqrt(-a)/a) - (5*a*b*x + 2*a^2)*sqrt(b*x + a))/(a*x^2)]`

giac [A] time = 1.29, size = 64, normalized size = 1.03

$$\frac{3b^3 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right) - \frac{5(bx+a)^{\frac{3}{2}}b^3 - 3\sqrt{bx+a}ab^3}{b^2x^2}}{4b\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^3,x, algorithm="giac")

[Out] 1/4*(3*b^3*arctan(sqrt(b*x + a)/sqrt(-a))/sqrt(-a) - (5*(b*x + a)^(3/2)*b^3 - 3*sqrt(b*x + a)*a*b^3)/(b^2*x^2))/b

maple [A] time = 0.01, size = 51, normalized size = 0.82

$$2 \left(-\frac{3 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{8\sqrt{a}} + \frac{3\sqrt{bx+a}a - 5(bx+a)^{\frac{3}{2}}}{8b^2x^2} \right) b^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/x^3,x)

[Out] 2*b^2*((-5/8*(b*x+a)^(3/2)+3/8*(b*x+a)^(1/2)*a)/x^2/b^2-3/8*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(1/2))

maxima [A] time = 2.98, size = 86, normalized size = 1.39

$$\frac{3b^2 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right) - \frac{5(bx+a)^{\frac{3}{2}}b^2 - 3\sqrt{bx+a}ab^2}{4((bx+a)^2 - 2(bx+a)a + a^2)}}{8\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^3,x, algorithm="maxima")

[Out] 3/8*b^2*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a)))/sqrt(a) - 1/4*(5*(b*x + a)^(3/2)*b^2 - 3*sqrt(b*x + a)*a*b^2)/((b*x + a)^2 - 2*(b*x + a)*a + a^2)

mupad [B] time = 0.06, size = 46, normalized size = 0.74

$$\frac{3a\sqrt{a+bx}}{4x^2} - \frac{3b^2 \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4\sqrt{a}} - \frac{5(a+bx)^{3/2}}{4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(3/2)/x^3,x)`

[Out] $(3*a*(a + b*x)^{(1/2)})/(4*x^2) - (3*b^2*\operatorname{atanh}((a + b*x)^{(1/2)}/a^{(1/2)}))/(4*a^{(1/2)}) - (5*(a + b*x)^{(3/2)})/(4*x^2)$

sympy [A] time = 3.28, size = 76, normalized size = 1.23

$$-\frac{a\sqrt{b}\sqrt{\frac{a}{bx}+1}}{2x^{\frac{3}{2}}}-\frac{5b^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}}{4\sqrt{x}}-\frac{3b^2\operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(3/2)/x**3,x)`

[Out] $-a*\sqrt{b}*\sqrt{a/(b*x) + 1}/(2*x^{(3/2)}) - 5*b^{(3/2)}*\sqrt{a/(b*x) + 1}/(4*\sqrt{x}) - 3*b^{(3/2)}*\operatorname{asinh}(\sqrt{a}/(\sqrt{b}*\sqrt{x}))/4*\sqrt{a}$

$$3.299 \quad \int \frac{(a+bx)^{3/2}}{x^4} dx$$

Optimal. Leaf size=84

$$\frac{b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{3/2}} - \frac{b^2 \sqrt{a+bx}}{8ax} - \frac{(a+bx)^{3/2}}{3x^3} - \frac{b\sqrt{a+bx}}{4x^2}$$

[Out] $-1/3*(b*x+a)^{(3/2)}/x^3+1/8*b^3*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(3/2)}-1/4*b*(b*x+a)^{(1/2)}/x^2-1/8*b^2*(b*x+a)^{(1/2)}/a/x$

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 51, 63, 208}

$$\frac{b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{3/2}} - \frac{b^2 \sqrt{a+bx}}{8ax} - \frac{b\sqrt{a+bx}}{4x^2} - \frac{(a+bx)^{3/2}}{3x^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)/x^4, x]

[Out] $-(b*\operatorname{Sqrt}[a + b*x])/(4*x^2) - (b^2*\operatorname{Sqrt}[a + b*x])/(8*a*x) - (a + b*x)^{(3/2)}/(3*x^3) + (b^3*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(8*a^{(3/2)})$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(IleQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63


```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{x^4} dx &= -\frac{(a+bx)^{3/2}}{3x^3} + \frac{1}{2}b \int \frac{\sqrt{a+bx}}{x^3} dx \\
&= -\frac{b\sqrt{a+bx}}{4x^2} - \frac{(a+bx)^{3/2}}{3x^3} + \frac{1}{8}b^2 \int \frac{1}{x^2\sqrt{a+bx}} dx \\
&= -\frac{b\sqrt{a+bx}}{4x^2} - \frac{b^2\sqrt{a+bx}}{8ax} - \frac{(a+bx)^{3/2}}{3x^3} - \frac{b^3 \int \frac{1}{x\sqrt{a+bx}} dx}{16a} \\
&= -\frac{b\sqrt{a+bx}}{4x^2} - \frac{b^2\sqrt{a+bx}}{8ax} - \frac{(a+bx)^{3/2}}{3x^3} - \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{8a} \\
&= -\frac{b\sqrt{a+bx}}{4x^2} - \frac{b^2\sqrt{a+bx}}{8ax} - \frac{(a+bx)^{3/2}}{3x^3} + \frac{b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{3/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.42

$$\frac{2b^3(a+bx)^{5/2} {}_2F_1\left(\frac{5}{2}, 4; \frac{7}{2}; \frac{bx}{a} + 1\right)}{5a^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*x)^(3/2)/x^4, x]
```

```
[Out] (2*b^3*(a + b*x)^(5/2)*Hypergeometric2F1[5/2, 4, 7/2, 1 + (b*x)/a])/(5*a^4)
```

fricas [A] time = 0.54, size = 145, normalized size = 1.73

$$\left[\frac{3\sqrt{a}b^3x^3 \log\left(\frac{bx+2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2(3ab^2x^2 + 14a^2bx + 8a^3)\sqrt{bx+a}}{48a^2x^3}, \frac{3\sqrt{-a}b^3x^3 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) + (3a^2x^2 + 14a^2bx + 8a^3)\sqrt{bx+a}}{24a^2x^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^4,x, algorithm="fricas")

[Out] [1/48*(3*sqrt(a)*b^3*x^3*log((b*x + 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) - 2*(3*a*b^2*x^2 + 14*a^2*b*x + 8*a^3)*sqrt(b*x + a))/(a^2*x^3), -1/24*(3*sqrt(-a)*b^3*x^3*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (3*a*b^2*x^2 + 14*a^2*b*x + 8*a^3)*sqrt(b*x + a))/(a^2*x^3)]

giac [A] time = 1.16, size = 84, normalized size = 1.00

$$\frac{\frac{3b^4 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}a} + \frac{3(bx+a)^5 b^4 + 8(bx+a)^2 ab^4 - 3\sqrt{bx+a} a^2 b^4}{ab^3 x^3}}{24b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^4,x, algorithm="giac")

[Out] -1/24*(3*b^4*arctan(sqrt(b*x + a)/sqrt(-a))/(sqrt(-a)*a) + (3*(b*x + a)^(5/2)*b^4 + 8*(b*x + a)^(3/2)*a*b^4 - 3*sqrt(b*x + a)*a^2*b^4)/(a*b^3*x^3))/b

maple [A] time = 0.01, size = 63, normalized size = 0.75

$$2 \left(\frac{\operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{16a^{\frac{3}{2}}} + \frac{\frac{\sqrt{bx+a}a}{16} - \frac{(bx+a)^{\frac{5}{2}}}{16a} - \frac{(bx+a)^{\frac{3}{2}}}{6}}{b^3 x^3} \right) b^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/x^4,x)

[Out] 2*b^3*((-1/16/a*(b*x+a)^(5/2)-1/6*(b*x+a)^(3/2)+1/16*(b*x+a)^(1/2)*a)/x^3/b^3+1/16*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(3/2))

maxima [A] time = 3.05, size = 119, normalized size = 1.42

$$\frac{b^3 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{16a^{\frac{3}{2}}} - \frac{3(bx+a)^{\frac{5}{2}}b^3 + 8(bx+a)^{\frac{3}{2}}ab^3 - 3\sqrt{bx+a}a^2b^3}{24((bx+a)^3a - 3(bx+a)^2a^2 + 3(bx+a)a^3 - a^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^4,x, algorithm="maxima")

[Out]
$$-1/16*b^3*\log((\sqrt{b*x+a})-\sqrt{a})/(\sqrt{b*x+a}+\sqrt{a}))/a^{3/2}$$

$$-1/24*(3*(b*x+a)^{5/2}*b^3+8*(b*x+a)^{3/2}*a*b^3-3*\sqrt{b*x+a}*a^2*b^3)/((b*x+a)^3*a-3*(b*x+a)^2*a^2+3*(b*x+a)*a^3-a^4)$$

mupad [B] time = 0.10, size = 64, normalized size = 0.76

$$\frac{a\sqrt{a+bx}}{8x^3} - \frac{(a+bx)^{5/2}}{8ax^3} - \frac{(a+bx)^{3/2}}{3x^3} - \frac{b^3 \operatorname{atan}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{3/2}} 1i$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/x^4,x)

[Out]
$$(a*(a+b*x)^{(1/2)})/(8*x^3) - (a+b*x)^{(5/2)}/(8*a*x^3) - (b^3*\operatorname{atan}(((a+b*x)^{(1/2)}*1i)/a^{(1/2)})*1i)/(8*a^{(3/2)}) - (a+b*x)^{(3/2)}/(3*x^3)$$

sympy [A] time = 5.84, size = 124, normalized size = 1.48

$$-\frac{a^2}{3\sqrt{b}x^2\sqrt{\frac{a}{bx}+1}} - \frac{11a\sqrt{b}}{12x^2\sqrt{\frac{a}{bx}+1}} - \frac{17b^{\frac{3}{2}}}{24x^2\sqrt{\frac{a}{bx}+1}} - \frac{b^{\frac{5}{2}}}{8a\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{b^3 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{8a^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/x**4,x)

[Out]
$$-a^{**2}/(3*\sqrt{b}*x^{**7/2}*\sqrt{a/(b*x)+1}) - 11*a*\sqrt{b}/(12*x^{**5/2}*\sqrt{a/(b*x)+1}) - 17*b^{**3/2}/(24*x^{**3/2}*\sqrt{a/(b*x)+1}) - b^{**5/2}/(8*a*\sqrt{x}*\sqrt{a/(b*x)+1}) + b^{**3}*\operatorname{asinh}(\sqrt{a}/(\sqrt{b}*\sqrt{x}))/8*a^{**3/2}$$

3.300 $\int x^3(a + bx)^{5/2} dx$

Optimal. Leaf size=72

$$-\frac{2a^3(a + bx)^{7/2}}{7b^4} + \frac{2a^2(a + bx)^{9/2}}{3b^4} + \frac{2(a + bx)^{13/2}}{13b^4} - \frac{6a(a + bx)^{11/2}}{11b^4}$$

[Out] $-2/7*a^3*(b*x+a)^{(7/2)}/b^4+2/3*a^2*(b*x+a)^{(9/2)}/b^4-6/11*a*(b*x+a)^{(11/2)}/b^4+2/13*(b*x+a)^{(13/2)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2a^2(a + bx)^{9/2}}{3b^4} - \frac{2a^3(a + bx)^{7/2}}{7b^4} + \frac{2(a + bx)^{13/2}}{13b^4} - \frac{6a(a + bx)^{11/2}}{11b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^(5/2), x]

[Out] $(-2*a^3*(a + b*x)^{(7/2)})/(7*b^4) + (2*a^2*(a + b*x)^{(9/2)})/(3*b^4) - (6*a*(a + b*x)^{(11/2)})/(11*b^4) + (2*(a + b*x)^{(13/2)})/(13*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^{5/2} dx &= \int \left(-\frac{a^3(a + bx)^{5/2}}{b^3} + \frac{3a^2(a + bx)^{7/2}}{b^3} - \frac{3a(a + bx)^{9/2}}{b^3} + \frac{(a + bx)^{11/2}}{b^3} \right) dx \\ &= -\frac{2a^3(a + bx)^{7/2}}{7b^4} + \frac{2a^2(a + bx)^{9/2}}{3b^4} - \frac{6a(a + bx)^{11/2}}{11b^4} + \frac{2(a + bx)^{13/2}}{13b^4} \end{aligned}$$

Mathematica [A] time = 0.03, size = 46, normalized size = 0.64

$$\frac{2(a + bx)^{7/2} (-16a^3 + 56a^2bx - 126ab^2x^2 + 231b^3x^3)}{3003b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^(5/2),x]

[Out] $(2*(a + b*x)^(7/2)*(-16*a^3 + 56*a^2*b*x - 126*a*b^2*x^2 + 231*b^3*x^3))/(3003*b^4)$

fricas [A] time = 0.48, size = 75, normalized size = 1.04

$$\frac{2(231b^6x^6 + 567ab^5x^5 + 371a^2b^4x^4 + 5a^3b^3x^3 - 6a^4b^2x^2 + 8a^5bx - 16a^6)\sqrt{bx+a}}{3003b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(5/2),x, algorithm="fricas")

[Out] $2/3003*(231*b^6*x^6 + 567*a*b^5*x^5 + 371*a^2*b^4*x^4 + 5*a^3*b^3*x^3 - 6*a^4*b^2*x^2 + 8*a^5*b*x - 16*a^6)*\text{sqrt}(b*x + a)/b^4$

giac [B] time = 1.16, size = 281, normalized size = 3.90

$$2 \left(\frac{429 \left(5(bx+a)^{\frac{7}{2}} - 21(bx+a)^{\frac{5}{2}}a + 35(bx+a)^{\frac{3}{2}}a^2 - 35\sqrt{bx+a}a^3 \right) a^3}{b^3} + \frac{143 \left(35(bx+a)^{\frac{9}{2}} - 180(bx+a)^{\frac{7}{2}}a + 378(bx+a)^{\frac{5}{2}}a^2 - 420(bx+a)^{\frac{3}{2}}a^3 + 315\sqrt{bx+a}a^4 \right) a^3}{b^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(5/2),x, algorithm="giac")

[Out] $2/15015*(429*(5*(b*x + a)^(7/2) - 21*(b*x + a)^(5/2)*a + 35*(b*x + a)^(3/2)*a^2 - 35*\text{sqrt}(b*x + a)*a^3)*a^3/b^3 + 143*(35*(b*x + a)^(9/2) - 180*(b*x + a)^(7/2)*a + 378*(b*x + a)^(5/2)*a^2 - 420*(b*x + a)^(3/2)*a^3 + 315*\text{sqrt}(b*x + a)*a^4)*a^2/b^3 + 65*(63*(b*x + a)^(11/2) - 385*(b*x + a)^(9/2)*a + 990*(b*x + a)^(7/2)*a^2 - 1386*(b*x + a)^(5/2)*a^3 + 1155*(b*x + a)^(3/2)*a^4 - 693*\text{sqrt}(b*x + a)*a^5)*a/b^3 + 5*(231*(b*x + a)^(13/2) - 1638*(b*x + a)^(11/2)*a + 5005*(b*x + a)^(9/2)*a^2 - 8580*(b*x + a)^(7/2)*a^3 + 9009*(b*x + a)^(5/2)*a^4 - 6006*(b*x + a)^(3/2)*a^5 + 3003*\text{sqrt}(b*x + a)*a^6)/b^3)/b$

maple [A] time = 0.01, size = 43, normalized size = 0.60

$$\frac{2(bx+a)^{\frac{7}{2}}(-231b^3x^3 + 126ab^2x^2 - 56a^2bx + 16a^3)}{3003b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^(5/2),x)

[Out] $-2/3003*(b*x+a)^{(7/2)*(-231*b^3*x^3+126*a*b^2*x^2-56*a^2*b*x+16*a^3)}/b^4$

maxima [A] time = 1.35, size = 56, normalized size = 0.78

$$\frac{2(bx+a)^{\frac{13}{2}}}{13b^4} - \frac{6(bx+a)^{\frac{11}{2}}a}{11b^4} + \frac{2(bx+a)^{\frac{9}{2}}a^2}{3b^4} - \frac{2(bx+a)^{\frac{7}{2}}a^3}{7b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(b*x+a)^(5/2),x, algorithm="maxima")`

[Out] $2/13*(b*x+a)^{(13/2)}/b^4 - 6/11*(b*x+a)^{(11/2)}*a/b^4 + 2/3*(b*x+a)^{(9/2)}*a^2/b^4 - 2/7*(b*x+a)^{(7/2)}*a^3/b^4$

mapad [B] time = 0.05, size = 56, normalized size = 0.78

$$\frac{2(a+bx)^{13/2}}{13b^4} - \frac{2a^3(a+bx)^{7/2}}{7b^4} + \frac{2a^2(a+bx)^{9/2}}{3b^4} - \frac{6a(a+bx)^{11/2}}{11b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(a+b*x)^(5/2),x)`

[Out] $(2*(a+b*x)^{(13/2)})/(13*b^4) - (2*a^3*(a+b*x)^{(7/2)})/(7*b^4) + (2*a^2*(a+b*x)^{(9/2)})/(3*b^4) - (6*a*(a+b*x)^{(11/2)})/(11*b^4)$

sympy [A] time = 4.47, size = 146, normalized size = 2.03

$$\begin{cases} -\frac{32a^6\sqrt{a+bx}}{3003b^4} + \frac{16a^5x\sqrt{a+bx}}{3003b^3} - \frac{4a^4x^2\sqrt{a+bx}}{1001b^2} + \frac{10a^3x^3\sqrt{a+bx}}{3003b} + \frac{106a^2x^4\sqrt{a+bx}}{429} + \frac{54abx^5\sqrt{a+bx}}{143} + \frac{2b^2x^6\sqrt{a+bx}}{13} & \text{for } b \neq 0 \\ \frac{5}{4}a^{\frac{5}{2}}x^4 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(b*x+a)**(5/2),x)`

[Out] `Piecewise((-32*a**6*sqrt(a+b*x)/(3003*b**4) + 16*a**5*x*sqrt(a+b*x)/(3003*b**3) - 4*a**4*x**2*sqrt(a+b*x)/(1001*b**2) + 10*a**3*x**3*sqrt(a+b*x)/(3003*b) + 106*a**2*x**4*sqrt(a+b*x)/429 + 54*a*b*x**5*sqrt(a+b*x)/143 + 2*b**2*x**6*sqrt(a+b*x)/13, Ne(b, 0)), (a**(5/2)*x**4/4, True))`

3.301 $\int x^2(a + bx)^{5/2} dx$

Optimal. Leaf size=53

$$\frac{2a^2(a + bx)^{7/2}}{7b^3} + \frac{2(a + bx)^{11/2}}{11b^3} - \frac{4a(a + bx)^{9/2}}{9b^3}$$

[Out] $2/7*a^2*(b*x+a)^{(7/2)}/b^3-4/9*a*(b*x+a)^{(9/2)}/b^3+2/11*(b*x+a)^{(11/2)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2a^2(a + bx)^{7/2}}{7b^3} + \frac{2(a + bx)^{11/2}}{11b^3} - \frac{4a(a + bx)^{9/2}}{9b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*x)^(5/2), x]

[Out] $(2*a^2*(a + b*x)^{(7/2)})/(7*b^3) - (4*a*(a + b*x)^{(9/2)})/(9*b^3) + (2*(a + b*x)^{(11/2)})/(11*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^{5/2} dx &= \int \left(\frac{a^2(a + bx)^{5/2}}{b^2} - \frac{2a(a + bx)^{7/2}}{b^2} + \frac{(a + bx)^{9/2}}{b^2} \right) dx \\ &= \frac{2a^2(a + bx)^{7/2}}{7b^3} - \frac{4a(a + bx)^{9/2}}{9b^3} + \frac{2(a + bx)^{11/2}}{11b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.66

$$\frac{2(a + bx)^{7/2} (8a^2 - 28abx + 63b^2x^2)}{693b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^(5/2), x]

[Out] (2*(a + b*x)^(7/2)*(8*a^2 - 28*a*b*x + 63*b^2*x^2))/(693*b^3)

fricas [A] time = 0.44, size = 64, normalized size = 1.21

$$\frac{2(63b^5x^5 + 161ab^4x^4 + 113a^2b^3x^3 + 3a^3b^2x^2 - 4a^4bx + 8a^5)\sqrt{bx+a}}{693b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(5/2), x, algorithm="fricas")

[Out] 2/693*(63*b^5*x^5 + 161*a*b^4*x^4 + 113*a^2*b^3*x^3 + 3*a^3*b^2*x^2 - 4*a^4*b*x + 8*a^5)*sqrt(b*x + a)/b^3

giac [B] time = 1.09, size = 233, normalized size = 4.40

$$2 \left(\frac{231 \left(3(bx+a)^{\frac{5}{2}} - 10(bx+a)^{\frac{3}{2}}a + 15\sqrt{bx+a}a^2 \right) a^3}{b^2} + \frac{297 \left(5(bx+a)^{\frac{7}{2}} - 21(bx+a)^{\frac{5}{2}}a + 35(bx+a)^{\frac{3}{2}}a^2 - 35\sqrt{bx+a}a^3 \right) a^2}{b^2} + \frac{33 \left(35(bx+a)^{\frac{9}{2}} - 180(bx+a)^{\frac{7}{2}}a + 378(bx+a)^{\frac{5}{2}}a^2 - 420(bx+a)^{\frac{3}{2}}a^3 + 315\sqrt{bx+a}a^4 \right) a}{b^2} \right) / b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(5/2), x, algorithm="giac")

[Out] 2/3465*(231*(3*(b*x + a)^(5/2) - 10*(b*x + a)^(3/2)*a + 15*sqrt(b*x + a)*a^2)*a^3/b^2 + 297*(5*(b*x + a)^(7/2) - 21*(b*x + a)^(5/2)*a + 35*(b*x + a)^(3/2)*a^2 - 35*sqrt(b*x + a)*a^3)*a^2/b^2 + 33*(35*(b*x + a)^(9/2) - 180*(b*x + a)^(7/2)*a + 378*(b*x + a)^(5/2)*a^2 - 420*(b*x + a)^(3/2)*a^3 + 315*sqrt(b*x + a)*a^4)*a/b^2 + 5*(63*(b*x + a)^(11/2) - 385*(b*x + a)^(9/2)*a + 990*(b*x + a)^(7/2)*a^2 - 1386*(b*x + a)^(5/2)*a^3 + 1155*(b*x + a)^(3/2)*a^4 - 693*sqrt(b*x + a)*a^5)/b^2)/b

maple [A] time = 0.00, size = 32, normalized size = 0.60

$$\frac{2(bx+a)^{\frac{7}{2}}(63b^2x^2 - 28abx + 8a^2)}{693b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^(5/2), x)

[Out] 2/693*(b*x+a)^(7/2)*(63*b^2*x^2-28*a*b*x+8*a^2)/b^3

maxima [A] time = 1.37, size = 41, normalized size = 0.77

$$\frac{2 (bx + a)^{\frac{11}{2}}}{11 b^3} - \frac{4 (bx + a)^{\frac{9}{2}} a}{9 b^3} + \frac{2 (bx + a)^{\frac{7}{2}} a^2}{7 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(5/2),x, algorithm="maxima")

[Out] 2/11*(b*x + a)^(11/2)/b^3 - 4/9*(b*x + a)^(9/2)*a/b^3 + 2/7*(b*x + a)^(7/2)*a^2/b^3

mupad [B] time = 0.04, size = 37, normalized size = 0.70

$$\frac{126 (a + bx)^{11/2} - 308 a (a + bx)^{9/2} + 198 a^2 (a + bx)^{7/2}}{693 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a + b*x)^(5/2),x)

[Out] (126*(a + b*x)^(11/2) - 308*a*(a + b*x)^(9/2) + 198*a^2*(a + b*x)^(7/2))/(693*b^3)

sympy [A] time = 3.77, size = 124, normalized size = 2.34

$$\begin{cases} \frac{16a^5\sqrt{a+bx}}{693b^3} - \frac{8a^4x\sqrt{a+bx}}{693b^2} + \frac{2a^3x^2\sqrt{a+bx}}{231b} + \frac{226a^2x^3\sqrt{a+bx}}{693} + \frac{46abx^4\sqrt{a+bx}}{99} + \frac{2b^2x^5\sqrt{a+bx}}{11} & \text{for } b \neq 0 \\ \frac{a^2x^3}{3} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)**(5/2),x)

[Out] Piecewise((16*a**5*sqrt(a + b*x)/(693*b**3) - 8*a**4*x*sqrt(a + b*x)/(693*b**2) + 2*a**3*x**2*sqrt(a + b*x)/(231*b) + 226*a**2*x**3*sqrt(a + b*x)/693 + 46*a*b*x**4*sqrt(a + b*x)/99 + 2*b**2*x**5*sqrt(a + b*x)/11, Ne(b, 0)), (a**5/2*x**3/3, True))

3.302 $\int x(a + bx)^{5/2} dx$

Optimal. Leaf size=34

$$\frac{2(a + bx)^{9/2}}{9b^2} - \frac{2a(a + bx)^{7/2}}{7b^2}$$

[Out] $-2/7*a*(b*x+a)^{(7/2)}/b^2+2/9*(b*x+a)^{(9/2)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{2(a + bx)^{9/2}}{9b^2} - \frac{2a(a + bx)^{7/2}}{7b^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^(5/2), x]

[Out] $(-2*a*(a + b*x)^{(7/2)})/(7*b^2) + (2*(a + b*x)^{(9/2)})/(9*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x(a + bx)^{5/2} dx &= \int \left(-\frac{a(a + bx)^{5/2}}{b} + \frac{(a + bx)^{7/2}}{b} \right) dx \\ &= -\frac{2a(a + bx)^{7/2}}{7b^2} + \frac{2(a + bx)^{9/2}}{9b^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 24, normalized size = 0.71

$$\frac{2(a + bx)^{7/2}(7bx - 2a)}{63b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^(5/2), x]

[Out] $(2*(a + b*x)^{(7/2)}*(-2*a + 7*b*x))/(63*b^2)$

fricas [A] time = 0.49, size = 52, normalized size = 1.53

$$\frac{2(7b^4x^4 + 19ab^3x^3 + 15a^2b^2x^2 + a^3bx - 2a^4)\sqrt{bx+a}}{63b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(5/2),x, algorithm="fricas")`

[Out] $2/63*(7*b^4*x^4 + 19*a*b^3*x^3 + 15*a^2*b^2*x^2 + a^3*b*x - 2*a^4)*\text{sqrt}(b*x + a)/b^2$

giac [B] time = 1.15, size = 182, normalized size = 5.35

$$2 \left(\frac{105 \left((bx+a)^{\frac{3}{2}} - 3\sqrt{bx+a} \right) a^3}{b} + \frac{63 \left(3(bx+a)^{\frac{5}{2}} - 10(bx+a)^{\frac{3}{2}}a + 15\sqrt{bx+a}a^2 \right) a^2}{b} + \frac{27 \left(5(bx+a)^{\frac{7}{2}} - 21(bx+a)^{\frac{5}{2}}a + 35(bx+a)^{\frac{3}{2}}a^2 - 35\sqrt{bx+a}a^3 \right) a}{b} \right) / 315b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(5/2),x, algorithm="giac")`

[Out] $2/315*(105*((b*x + a)^{(3/2)} - 3*\text{sqrt}(b*x + a)*a)*a^3/b + 63*(3*(b*x + a)^{(5/2)} - 10*(b*x + a)^{(3/2)}*a + 15*\text{sqrt}(b*x + a)*a^2)*a^2/b + 27*(5*(b*x + a)^{(7/2)} - 21*(b*x + a)^{(5/2)}*a + 35*(b*x + a)^{(3/2)}*a^2 - 35*\text{sqrt}(b*x + a)*a^3)*a/b + (35*(b*x + a)^{(9/2)} - 180*(b*x + a)^{(7/2)}*a + 378*(b*x + a)^{(5/2)}*a^2 - 420*(b*x + a)^{(3/2)}*a^3 + 315*\text{sqrt}(b*x + a)*a^4)/b)/b$

maple [A] time = 0.00, size = 21, normalized size = 0.62

$$\frac{2(bx+a)^{\frac{7}{2}}(-7bx+2a)}{63b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)^(5/2),x)`

[Out] $-2/63*(b*x+a)^{(7/2)}*(-7*b*x+2*a)/b^2$

maxima [A] time = 1.37, size = 26, normalized size = 0.76

$$\frac{2(bx+a)^{\frac{9}{2}}}{9b^2} - \frac{2(bx+a)^{\frac{7}{2}}a}{7b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^(5/2),x, algorithm="maxima")

[Out] $2/9*(b*x + a)^{(9/2)}/b^2 - 2/7*(b*x + a)^{(7/2)}*a/b^2$

mupad [B] time = 0.03, size = 25, normalized size = 0.74

$$-\frac{18a(a+bx)^{7/2} - 14(a+bx)^{9/2}}{63b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a + b*x)^(5/2),x)

[Out] $-(18*a*(a + b*x)^{(7/2)} - 14*(a + b*x)^{(9/2)})/(63*b^2)$

sympy [A] time = 2.60, size = 102, normalized size = 3.00

$$\begin{cases} -\frac{4a^4\sqrt{a+bx}}{63b^2} + \frac{2a^3x\sqrt{a+bx}}{63b} + \frac{10a^2x^2\sqrt{a+bx}}{21} + \frac{38abx^3\sqrt{a+bx}}{63} + \frac{2b^2x^4\sqrt{a+bx}}{9} & \text{for } b \neq 0 \\ \frac{a^2x^2}{2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)**(5/2),x)

[Out] Piecewise((-4*a**4*sqrt(a + b*x)/(63*b**2) + 2*a**3*x*sqrt(a + b*x)/(63*b) + 10*a**2*x**2*sqrt(a + b*x)/21 + 38*a*b*x**3*sqrt(a + b*x)/63 + 2*b**2*x**4*sqrt(a + b*x)/9, Ne(b, 0)), (a**(5/2)*x**2/2, True))

3.303 $\int (a + bx)^{5/2} dx$

Optimal. Leaf size=16

$$\frac{2(a + bx)^{7/2}}{7b}$$

[Out] $2/7*(b*x+a)^{(7/2)}/b$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{2(a + bx)^{7/2}}{7b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2), x]

[Out] (2*(a + b*x)^(7/2))/(7*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^{5/2} dx = \frac{2(a + bx)^{7/2}}{7b}$$

Mathematica [A] time = 0.01, size = 16, normalized size = 1.00

$$\frac{2(a + bx)^{7/2}}{7b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2), x]

[Out] (2*(a + b*x)^(7/2))/(7*b)

fricas [B] time = 0.43, size = 39, normalized size = 2.44

$$\frac{2(b^3x^3 + 3ab^2x^2 + 3a^2bx + a^3)\sqrt{bx + a}}{7b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2),x, algorithm="fricas")

[Out] $2/7*(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3)*\text{sqrt}(b*x + a)/b$

giac [B] time = 0.98, size = 95, normalized size = 5.94

$$\frac{2 \left(5 (bx + a)^{\frac{7}{2}} - 21 (bx + a)^{\frac{5}{2}} a + 35 (bx + a)^{\frac{3}{2}} a^2 + 35 \left((bx + a)^{\frac{3}{2}} - 3 \sqrt{bx + a} a \right) a^2 + 7 \left(3 (bx + a)^{\frac{5}{2}} - 10 (bx + a)^{\frac{3}{2}} a \right) \right)}{35 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2),x, algorithm="giac")

[Out] $2/35*(5*(b*x + a)^{(7/2)} - 21*(b*x + a)^{(5/2)}*a + 35*(b*x + a)^{(3/2)}*a^2 + 3*5*((b*x + a)^{(3/2)} - 3*\text{sqrt}(b*x + a)*a)*a^2 + 7*(3*(b*x + a)^{(5/2)} - 10*(b*x + a)^{(3/2)}*a + 15*\text{sqrt}(b*x + a)*a^2)*a)/b$

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{2 (bx + a)^{\frac{7}{2}}}{7b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2),x)

[Out] $2/7*(b*x+a)^{(7/2)}/b$

maxima [A] time = 1.34, size = 12, normalized size = 0.75

$$\frac{2 (bx + a)^{\frac{7}{2}}}{7b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2),x, algorithm="maxima")

[Out] $2/7*(b*x + a)^{(7/2)}/b$

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{2 (a + bx)^{7/2}}{7b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(5/2),x)
```

```
[Out] (2*(a + b*x)^(7/2))/(7*b)
```

sympy [A] time = 0.08, size = 12, normalized size = 0.75

$$\frac{2(a + bx)^{\frac{7}{2}}}{7b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(5/2),x)
```

```
[Out] 2*(a + b*x)**(7/2)/(7*b)
```

$$3.304 \quad \int \frac{(a+bx)^{5/2}}{x} dx$$

Optimal. Leaf size=65

$$-2a^{5/2} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + 2a^2\sqrt{a+bx} + \frac{2}{3}a(a+bx)^{3/2} + \frac{2}{5}(a+bx)^{5/2}$$

[Out] $2/3*a*(b*x+a)^{(3/2)}+2/5*(b*x+a)^{(5/2)}-2*a^{(5/2)}*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})+2*a^2*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {50, 63, 208}

$$2a^2\sqrt{a+bx} - 2a^{5/2} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + \frac{2}{3}a(a+bx)^{3/2} + \frac{2}{5}(a+bx)^{5/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2)/x, x]

[Out] $2*a^2*\operatorname{Sqrt}[a + b*x] + (2*a*(a + b*x)^{(3/2)})/3 + (2*(a + b*x)^{(5/2)})/5 - 2*a^{(5/2)}*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]]$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{5/2}}{x} dx &= \frac{2}{5}(a+bx)^{5/2} + a \int \frac{(a+bx)^{3/2}}{x} dx \\
 &= \frac{2}{3}a(a+bx)^{3/2} + \frac{2}{5}(a+bx)^{5/2} + a^2 \int \frac{\sqrt{a+bx}}{x} dx \\
 &= 2a^2\sqrt{a+bx} + \frac{2}{3}a(a+bx)^{3/2} + \frac{2}{5}(a+bx)^{5/2} + a^3 \int \frac{1}{x\sqrt{a+bx}} dx \\
 &= 2a^2\sqrt{a+bx} + \frac{2}{3}a(a+bx)^{3/2} + \frac{2}{5}(a+bx)^{5/2} + \frac{(2a^3) \operatorname{Subst}\left(\int \frac{1}{\frac{-a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{b} \\
 &= 2a^2\sqrt{a+bx} + \frac{2}{3}a(a+bx)^{3/2} + \frac{2}{5}(a+bx)^{5/2} - 2a^{5/2} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)
 \end{aligned}$$

Mathematica [A] time = 0.05, size = 58, normalized size = 0.89

$$-2a^{5/2} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + \frac{2}{3}a\sqrt{a+bx}(4a+bx) + \frac{2}{5}(a+bx)^{5/2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/x, x]

[Out] (2*(a + b*x)^(5/2))/5 + (2*a*Sqrt[a + b*x]*(4*a + b*x))/3 - 2*a^(5/2)*ArcTanh[Sqrt[a + b*x]/Sqrt[a]]

fricas [A] time = 0.48, size = 114, normalized size = 1.75

$$\left[a^{\frac{5}{2}} \log\left(\frac{bx - 2\sqrt{bx+a}\sqrt{a} + 2a}{x}\right) + \frac{2}{15}(3b^2x^2 + 11abx + 23a^2)\sqrt{bx+a}, 2\sqrt{-a}a^2 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) \right] +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x,x, algorithm="fricas")

[Out] [a^(5/2)*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2/15*(3*b^2*x^2 + 11*a*b*x + 23*a^2)*sqrt(b*x + a), 2*sqrt(-a)*a^2*arctan(sqrt(b*x + a)*sqrt(-a)/a) + 2/15*(3*b^2*x^2 + 11*a*b*x + 23*a^2)*sqrt(b*x + a)]

giac [A] time = 1.03, size = 56, normalized size = 0.86

$$\frac{2a^3 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} + \frac{2}{5}(bx+a)^{\frac{5}{2}} + \frac{2}{3}(bx+a)^{\frac{3}{2}}a + 2\sqrt{bx+a}a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x,x, algorithm="giac")

[Out] 2*a^3*arctan(sqrt(b*x + a)/sqrt(-a))/sqrt(-a) + 2/5*(b*x + a)^(5/2) + 2/3*(b*x + a)^(3/2)*a + 2*sqrt(b*x + a)*a^2

maple [A] time = 0.01, size = 50, normalized size = 0.77

$$-2a^{\frac{5}{2}} \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right) + 2\sqrt{bx+a}a^2 + \frac{2(bx+a)^{\frac{3}{2}}a}{3} + \frac{2(bx+a)^{\frac{5}{2}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/x,x)

[Out] 2/3*a*(b*x+a)^(3/2)+2/5*(b*x+a)^(5/2)-2*a^(5/2)*arctanh((b*x+a)^(1/2)/a^(1/2))+2*a^2*(b*x+a)^(1/2)

maxima [A] time = 3.02, size = 64, normalized size = 0.98

$$a^{\frac{5}{2}} \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right) + \frac{2}{5}(bx+a)^{\frac{5}{2}} + \frac{2}{3}(bx+a)^{\frac{3}{2}}a + 2\sqrt{bx+a}a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x,x, algorithm="maxima")

[Out] a^(5/2)*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a))) + 2/5*(b*x + a)^(5/2) + 2/3*(b*x + a)^(3/2)*a + 2*sqrt(b*x + a)*a^2

mupad [B] time = 0.05, size = 52, normalized size = 0.80

$$\frac{2a(a+bx)^{3/2}}{3} + \frac{2(a+bx)^{5/2}}{5} + 2a^2\sqrt{a+bx} + a^{5/2} \operatorname{atan}\left(\frac{\sqrt{a+bx} \operatorname{li}}{\sqrt{a}}\right) 2i$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)/x,x)

[Out] $(2*a*(a + b*x)^{(3/2)})/3 + (2*(a + b*x)^{(5/2)})/5 + 2*a^2*(a + b*x)^{(1/2)} + a^{(5/2)}*atan(((a + b*x)^{(1/2)}*1i)/a^{(1/2)})*2i$

sympy [A] time = 4.12, size = 97, normalized size = 1.49

$$\frac{46a^{\frac{5}{2}}\sqrt{1 + \frac{bx}{a}}}{15} + a^{\frac{5}{2}}\log\left(\frac{bx}{a}\right) - 2a^{\frac{5}{2}}\log\left(\sqrt{1 + \frac{bx}{a}} + 1\right) + \frac{22a^{\frac{3}{2}}bx\sqrt{1 + \frac{bx}{a}}}{15} + \frac{2\sqrt{a}b^2x^2\sqrt{1 + \frac{bx}{a}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)/x,x)

[Out] $46*a^{(5/2)}*\sqrt{1 + b*x/a}/15 + a^{(5/2)}*\log(b*x/a) - 2*a^{(5/2)}*\log(\sqrt{1 + b*x/a} + 1) + 22*a^{(3/2)}*b*x*\sqrt{1 + b*x/a}/15 + 2*\sqrt{a}*b^{*2}*x^{*2}*\sqrt{1 + b*x/a}/5$

$$3.305 \quad \int \frac{(a+bx)^{5/2}}{x^2} dx$$

Optimal. Leaf size=66

$$-5a^{3/2}b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) - \frac{(a+bx)^{5/2}}{x} + \frac{5}{3}b(a+bx)^{3/2} + 5ab\sqrt{a+bx}$$

[Out] $5/3*b*(b*x+a)^{(3/2)}-(b*x+a)^{(5/2)}/x-5*a^{(3/2)}*b*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})+5*a*b*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 208}

$$-5a^{3/2}b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) - \frac{(a+bx)^{5/2}}{x} + \frac{5}{3}b(a+bx)^{3/2} + 5ab\sqrt{a+bx}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2)/x^2, x]

[Out] $5*a*b*\operatorname{Sqrt}[a + b*x] + (5*b*(a + b*x)^{(3/2)})/3 - (a + b*x)^{(5/2)}/x - 5*a^{(3/2)}*b*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{x^2} dx &= -\frac{(a+bx)^{5/2}}{x} + \frac{1}{2}(5b) \int \frac{(a+bx)^{3/2}}{x} dx \\
&= \frac{5}{3}b(a+bx)^{3/2} - \frac{(a+bx)^{5/2}}{x} + \frac{1}{2}(5ab) \int \frac{\sqrt{a+bx}}{x} dx \\
&= 5ab\sqrt{a+bx} + \frac{5}{3}b(a+bx)^{3/2} - \frac{(a+bx)^{5/2}}{x} + \frac{1}{2}(5a^2b) \int \frac{1}{x\sqrt{a+bx}} dx \\
&= 5ab\sqrt{a+bx} + \frac{5}{3}b(a+bx)^{3/2} - \frac{(a+bx)^{5/2}}{x} + (5a^2) \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right) \\
&= 5ab\sqrt{a+bx} + \frac{5}{3}b(a+bx)^{3/2} - \frac{(a+bx)^{5/2}}{x} - 5a^{3/2}b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.50

$$\frac{2b(a+bx)^{7/2} {}_2F_1\left(2, \frac{7}{2}; \frac{9}{2}; \frac{bx}{a} + 1\right)}{7a^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*x)^(5/2)/x^2,x]
```

```
[Out] (2*b*(a + b*x)^(7/2)*Hypergeometric2F1[2, 7/2, 9/2, 1 + (b*x)/a])/(7*a^2)
```

fricas [A] time = 0.48, size = 126, normalized size = 1.91

$$\left[\frac{15 a^{\frac{3}{2}} b x \log\left(\frac{b x - 2 \sqrt{b x + a} \sqrt{a + 2 a}}{x}\right) + 2 \left(2 b^2 x^2 + 14 a b x - 3 a^2\right) \sqrt{b x + a}}{6 x}, \frac{15 \sqrt{-a} a b x \arctan\left(\frac{\sqrt{b x + a} \sqrt{-a}}{a}\right) + \left(2 b^2 x^2\right)}{3 x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^2,x, algorithm="fricas")

[Out] [1/6*(15*a^(3/2)*b*x*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*(2*b^2*x^2 + 14*a*b*x - 3*a^2)*sqrt(b*x + a))/x, 1/3*(15*sqrt(-a)*a*b*x*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (2*b^2*x^2 + 14*a*b*x - 3*a^2)*sqrt(b*x + a))/x]

giac [A] time = 1.09, size = 74, normalized size = 1.12

$$\frac{15 a^2 b^2 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right) + 2 (bx + a)^{\frac{3}{2}} b^2 + 12 \sqrt{bx + a} a b^2 - \frac{3 \sqrt{bx+a} a^2 b}{x}}{3 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^2,x, algorithm="giac")

[Out] 1/3*(15*a^2*b^2*arctan(sqrt(b*x + a)/sqrt(-a))/sqrt(-a) + 2*(b*x + a)^(3/2)*b^2 + 12*sqrt(b*x + a)*a*b^2 - 3*sqrt(b*x + a)*a^2*b/x)/b

maple [A] time = 0.01, size = 61, normalized size = 0.92

$$2 \left(\left(-\frac{5 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{2\sqrt{a}} - \frac{\sqrt{bx+a}}{2bx} \right) a^2 + 2\sqrt{bx+a} a + \frac{(bx+a)^{\frac{3}{2}}}{3} \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/x^2,x)

[Out] 2*b*(1/3*(b*x+a)^(3/2)+2*(b*x+a)^(1/2)*a+a^2*(-1/2*(b*x+a)^(1/2)/b/x-5/2*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(1/2)))

maxima [A] time = 2.94, size = 71, normalized size = 1.08

$$\frac{5}{2} a^{\frac{3}{2}} b \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right) + \frac{2}{3} (bx + a)^{\frac{3}{2}} b + 4 \sqrt{bx + a} a b - \frac{\sqrt{bx + a} a^2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^2,x, algorithm="maxima")

[Out] 5/2*a^(3/2)*b*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a))) + 2/3*(b*x + a)^(3/2)*b + 4*sqrt(b*x + a)*a*b - sqrt(b*x + a)*a^2/x

mupad [B] time = 0.11, size = 58, normalized size = 0.88

$$\frac{2b(a+bx)^{3/2}}{3} - \frac{a^2\sqrt{a+bx}}{x} + 4ab\sqrt{a+bx} + a^{3/2}b \operatorname{atan}\left(\frac{\sqrt{a+bx} \operatorname{1i}}{\sqrt{a}}\right) 5i$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(5/2)/x^2,x)`

[Out] $(2*b*(a + b*x)^{(3/2)})/3 - (a^2*(a + b*x)^{(1/2)})/x + a^{(3/2)}*b*\operatorname{atan}(((a + b*x)^{(1/2)}*1i)/a^{(1/2)})*5i + 4*a*b*(a + b*x)^{(1/2)}$

sympy [A] time = 3.75, size = 99, normalized size = 1.50

$$-\frac{a^{\frac{5}{2}}\sqrt{1+\frac{bx}{a}}}{x} + \frac{14a^{\frac{3}{2}}b\sqrt{1+\frac{bx}{a}}}{3} + \frac{5a^{\frac{3}{2}}b\log\left(\frac{bx}{a}\right)}{2} - 5a^{\frac{3}{2}}b\log\left(\sqrt{1+\frac{bx}{a}}+1\right) + \frac{2\sqrt{a}b^2x\sqrt{1+\frac{bx}{a}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(5/2)/x**2,x)`

[Out] $-a^{(5/2)}*\operatorname{sqrt}(1 + b*x/a)/x + 14*a^{(3/2)}*b*\operatorname{sqrt}(1 + b*x/a)/3 + 5*a^{(3/2)}*b*\log(b*x/a)/2 - 5*a^{(3/2)}*b*\log(\operatorname{sqrt}(1 + b*x/a) + 1) + 2*\operatorname{sqrt}(a)*b^{*2}*x*\operatorname{sqrt}(1 + b*x/a)/3$

$$3.306 \quad \int \frac{(a+bx)^{5/2}}{x^3} dx$$

Optimal. Leaf size=78

$$\frac{15}{4}b^2\sqrt{a+bx} - \frac{15}{4}\sqrt{a}b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) - \frac{(a+bx)^{5/2}}{2x^2} - \frac{5b(a+bx)^{3/2}}{4x}$$

[Out] $-5/4*b*(b*x+a)^{(3/2)}/x-1/2*(b*x+a)^{(5/2)}/x^2-15/4*b^2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})*a^{(1/2)}+15/4*b^2*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 208}

$$\frac{15}{4}b^2\sqrt{a+bx} - \frac{15}{4}\sqrt{a}b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) - \frac{(a+bx)^{5/2}}{2x^2} - \frac{5b(a+bx)^{3/2}}{4x}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}/x^3, x]$

[Out] $(15*b^2*\operatorname{Sqrt}[a + b*x])/4 - (5*b*(a + b*x)^{(3/2)})/(4*x) - (a + b*x)^{(5/2)}/(2*x^2) - (15*\operatorname{Sqrt}[a]*b^2*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/4$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(IntegerQ[n] \&\& !IntegerQ[m]) \&\& !(IntegerQ[m + n + 2, 0] \&\& (FractionQ[m] || GeQ[2*n + m + 1, 0])) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{NeQ}[m + n + 1, 0] \&\& !(IGtQ[m, 0] \&\& (!IntegerQ[n] || (GtQ[m, 0] \&\& LtQ[m - n, 0]))) \&\& !ILtQ[m + n + 2, 0] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63


```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{x^3} dx &= -\frac{(a+bx)^{5/2}}{2x^2} + \frac{1}{4}(5b) \int \frac{(a+bx)^{3/2}}{x^2} dx \\
&= -\frac{5b(a+bx)^{3/2}}{4x} - \frac{(a+bx)^{5/2}}{2x^2} + \frac{1}{8}(15b^2) \int \frac{\sqrt{a+bx}}{x} dx \\
&= \frac{15}{4}b^2\sqrt{a+bx} - \frac{5b(a+bx)^{3/2}}{4x} - \frac{(a+bx)^{5/2}}{2x^2} + \frac{1}{8}(15ab^2) \int \frac{1}{x\sqrt{a+bx}} dx \\
&= \frac{15}{4}b^2\sqrt{a+bx} - \frac{5b(a+bx)^{3/2}}{4x} - \frac{(a+bx)^{5/2}}{2x^2} + \frac{1}{4}(15ab) \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right) \\
&= \frac{15}{4}b^2\sqrt{a+bx} - \frac{5b(a+bx)^{3/2}}{4x} - \frac{(a+bx)^{5/2}}{2x^2} - \frac{15}{4}\sqrt{a}b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.45

$$-\frac{2b^2(a+bx)^{7/2} {}_2F_1\left(3, \frac{7}{2}; \frac{9}{2}; \frac{bx}{a} + 1\right)}{7a^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/x^3, x]

[Out] (-2*b^2*(a + b*x)^(7/2)*Hypergeometric2F1[3, 7/2, 9/2, 1 + (b*x)/a])/(7*a^3)

fricas [A] time = 0.49, size = 133, normalized size = 1.71

$$\left[\frac{15\sqrt{a}b^2x^2 \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(8b^2x^2 - 9abx - 2a^2)\sqrt{bx+a}}{8x^2}, \frac{15\sqrt{-a}b^2x^2 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) + (8b^2x^2 - 9abx - 2a^2)\sqrt{-a}}{4x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^3,x, algorithm="fricas")

[Out] [1/8*(15*sqrt(a)*b^2*x^2*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*(8*b^2*x^2 - 9*a*b*x - 2*a^2)*sqrt(b*x + a))/x^2, 1/4*(15*sqrt(-a)*b^2*x^2*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (8*b^2*x^2 - 9*a*b*x - 2*a^2)*sqrt(b*x + a))/x^2]

giac [A] time = 1.12, size = 80, normalized size = 1.03

$$\frac{15ab^3 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right) + 8\sqrt{bx+a}b^3 - \frac{9(bx+a)^{\frac{3}{2}}ab^3 - 7\sqrt{bx+a}a^2b^3}{b^2x^2}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^3,x, algorithm="giac")

[Out] 1/4*(15*a*b^3*arctan(sqrt(b*x + a)/sqrt(-a))/sqrt(-a) + 8*sqrt(b*x + a)*b^3 - (9*(b*x + a)^(3/2)*a*b^3 - 7*sqrt(b*x + a)*a^2*b^3)/(b^2*x^2))/b

maple [A] time = 0.01, size = 61, normalized size = 0.78

$$2 \left(\left(\frac{15 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{8\sqrt{a}} + \frac{7\sqrt{bx+a}a - \frac{9(bx+a)^{\frac{3}{2}}}{8}}{b^2x^2} \right) a + \sqrt{bx+a} \right) b^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/x^3,x)

[Out] 2*b^2*((b*x+a)^(1/2)+a*((-9/8*(b*x+a)^(3/2)+7/8*(b*x+a)^(1/2)*a)/x^2/b^2-15/8*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(1/2)))

maxima [A] time = 2.94, size = 101, normalized size = 1.29

$$\frac{15}{8}\sqrt{a}b^2 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right) + 2\sqrt{bx+a}b^2 - \frac{9(bx+a)^{\frac{3}{2}}ab^2 - 7\sqrt{bx+a}a^2b^2}{4((bx+a)^2 - 2(bx+a)a + a^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^3,x, algorithm="maxima")

[Out] $15/8*\sqrt{a}*b^2*\log((\sqrt{b*x + a} - \sqrt{a})/(\sqrt{b*x + a} + \sqrt{a})) + 2*\sqrt{b*x + a}*b^2 - 1/4*(9*(b*x + a)^{(3/2)}*a*b^2 - 7*\sqrt{b*x + a}*a^2*b^2)/((b*x + a)^2 - 2*(b*x + a)*a + a^2)$

mupad [B] time = 0.05, size = 64, normalized size = 0.82

$$2b^2\sqrt{a+bx} + \frac{7a^2\sqrt{a+bx}}{4x^2} - \frac{9a(a+bx)^{3/2}}{4x^2} + \frac{\sqrt{a}b^2\operatorname{atan}\left(\frac{\sqrt{a+bx}1i}{\sqrt{a}}\right)15i}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{int}((a + b*x)^{(5/2)}/x^3, x)$

[Out] $2*b^2*(a + b*x)^{(1/2)} + (7*a^2*(a + b*x)^{(1/2)})/(4*x^2) + (a^{(1/2)}*b^2*\operatorname{atan}(((a + b*x)^{(1/2)}*1i)/a^{(1/2)})*15i)/4 - (9*a*(a + b*x)^{(3/2)})/(4*x^2)$

sympy [A] time = 4.30, size = 126, normalized size = 1.62

$$\frac{15\sqrt{a}b^2\operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4} - \frac{a^3}{2\sqrt{b}x^2\sqrt{\frac{a}{bx}+1}} - \frac{11a^2\sqrt{b}}{4x^2\sqrt{\frac{a}{bx}+1}} - \frac{ab^{\frac{3}{2}}}{4\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{2b^{\frac{5}{2}}\sqrt{x}}{\sqrt{\frac{a}{bx}+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{integrate}((b*x+a)**(5/2)/x**3, x)$

[Out] $-15*\sqrt{a}*b**2*\operatorname{asinh}(\sqrt{a}/(\sqrt{b}*\sqrt{x}))/4 - a**3/(2*\sqrt{b}*x**(5/2)*\sqrt{a/(b*x) + 1}) - 11*a**2*\sqrt{b}/(4*x**(3/2)*\sqrt{a/(b*x) + 1}) - a*b**(3/2)/(4*\sqrt{x}*\sqrt{a/(b*x) + 1}) + 2*b**(5/2)*\sqrt{x}/\sqrt{a/(b*x) + 1}$

$$3.307 \quad \int \frac{(a+bx)^{5/2}}{x^4} dx$$

Optimal. Leaf size=81

$$-\frac{5b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8\sqrt{a}} - \frac{5b^2\sqrt{a+bx}}{8x} - \frac{(a+bx)^{5/2}}{3x^3} - \frac{5b(a+bx)^{3/2}}{12x^2}$$

[Out] $-5/12*b*(b*x+a)^{(3/2)}/x^2-1/3*(b*x+a)^{(5/2)}/x^3-5/8*b^3*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(1/2)}-5/8*b^2*(b*x+a)^{(1/2)}/x$

Rubi [A] time = 0.02, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {47, 63, 208}

$$-\frac{5b^2\sqrt{a+bx}}{8x} - \frac{5b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8\sqrt{a}} - \frac{5b(a+bx)^{3/2}}{12x^2} - \frac{(a+bx)^{5/2}}{3x^3}$$

Antiderivative was successfully verified.

[In] `Int[(a + b*x)^(5/2)/x^4, x]`

[Out] $(-5*b^2*\operatorname{Sqrt}[a + b*x])/(8*x) - (5*b*(a + b*x)^{(3/2)})/(12*x^2) - (a + b*x)^{(5/2)}/(3*x^3) - (5*b^3*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(8*\operatorname{Sqrt}[a])$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{5/2}}{x^4} dx &= -\frac{(a+bx)^{5/2}}{3x^3} + \frac{1}{6}(5b) \int \frac{(a+bx)^{3/2}}{x^3} dx \\
 &= -\frac{5b(a+bx)^{3/2}}{12x^2} - \frac{(a+bx)^{5/2}}{3x^3} + \frac{1}{8}(5b^2) \int \frac{\sqrt{a+bx}}{x^2} dx \\
 &= -\frac{5b^2\sqrt{a+bx}}{8x} - \frac{5b(a+bx)^{3/2}}{12x^2} - \frac{(a+bx)^{5/2}}{3x^3} + \frac{1}{16}(5b^3) \int \frac{1}{x\sqrt{a+bx}} dx \\
 &= -\frac{5b^2\sqrt{a+bx}}{8x} - \frac{5b(a+bx)^{3/2}}{12x^2} - \frac{(a+bx)^{5/2}}{3x^3} + \frac{1}{8}(5b^2) \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right) \\
 &= -\frac{5b^2\sqrt{a+bx}}{8x} - \frac{5b(a+bx)^{3/2}}{12x^2} - \frac{(a+bx)^{5/2}}{3x^3} - \frac{5b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8\sqrt{a}}
 \end{aligned}$$

Mathematica [A] time = 0.04, size = 79, normalized size = 0.98

$$\frac{8a^3 + 34a^2bx + 15b^3x^3\sqrt{\frac{bx}{a} + 1} \tanh^{-1}\left(\sqrt{\frac{bx}{a} + 1}\right) + 59ab^2x^2 + 33b^3x^3}{24x^3\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/x^4, x]

[Out] -1/24*(8*a^3 + 34*a^2*b*x + 59*a*b^2*x^2 + 33*b^3*x^3 + 15*b^3*x^3*Sqrt[1 + (b*x)/a]*ArcTanh[Sqrt[1 + (b*x)/a]])/(x^3*Sqrt[a + b*x])

fricas [A] time = 0.49, size = 146, normalized size = 1.80

$$\left[\frac{15\sqrt{a}b^3x^3 \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2(33ab^2x^2 + 26a^2bx + 8a^3)\sqrt{bx+a}}{48ax^3}, \frac{15\sqrt{-a}b^3x^3 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right)}{24} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^4, x, algorithm="fricas")

[Out] $[1/48*(15*\sqrt{a}*b^3*x^3*\log((b*x - 2*\sqrt{b*x + a})*\sqrt{a} + 2*a)/x) - 2*(33*a*b^2*x^2 + 26*a^2*b*x + 8*a^3)*\sqrt{b*x + a})/(a*x^3), 1/24*(15*\sqrt{-a}*b^3*x^3*\arctan(\sqrt{b*x + a}*\sqrt{-a}/a) - (33*a*b^2*x^2 + 26*a^2*b*x + 8*a^3)*\sqrt{b*x + a})/(a*x^3)]$

giac [A] time = 1.13, size = 79, normalized size = 0.98

$$\frac{15b^4 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} - \frac{33(bx+a)^{\frac{5}{2}}b^4 - 40(bx+a)^{\frac{3}{2}}ab^4 + 15\sqrt{bx+a}a^2b^4}{b^3x^3}$$

$$24b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^4,x, algorithm="giac")

[Out] $1/24*(15*b^4*\arctan(\sqrt{b*x + a}/\sqrt{-a})/\sqrt{-a} - (33*(b*x + a)^{(5/2)}*b^4 - 40*(b*x + a)^{(3/2)}*a*b^4 + 15*\sqrt{b*x + a}*a^2*b^4)/(b^3*x^3))/b$

maple [A] time = 0.01, size = 63, normalized size = 0.78

$$2 \left(-\frac{5 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{16\sqrt{a}} + \frac{-\frac{5\sqrt{bx+a}a^2}{16} + \frac{5(bx+a)^{\frac{3}{2}}a}{6} - \frac{11(bx+a)^{\frac{5}{2}}}{16}}{b^3x^3} \right) b^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/x^4,x)

[Out] $2*b^3*((-11/16*(b*x+a)^{(5/2)}+5/6*(b*x+a)^{(3/2)}*a-5/16*(b*x+a)^{(1/2)}*a^2)/x^3/b^3-5/16*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(1/2)})$

maxima [A] time = 2.99, size = 115, normalized size = 1.42

$$\frac{5b^3 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{16\sqrt{a}} - \frac{33(bx+a)^{\frac{5}{2}}b^3 - 40(bx+a)^{\frac{3}{2}}ab^3 + 15\sqrt{bx+a}a^2b^3}{24((bx+a)^3 - 3(bx+a)^2a + 3(bx+a)a^2 - a^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^4,x, algorithm="maxima")

[Out] $5/16*b^3*\log((\sqrt{b*x + a} - \sqrt{a})/(\sqrt{b*x + a} + \sqrt{a}))/\sqrt{a} - 1/24*(33*(b*x + a)^{(5/2)}*b^3 - 40*(b*x + a)^{(3/2)}*a*b^3 + 15*\sqrt{b*x + a}*a^2*b^3)/(b*x + a)^3 - 3*(b*x + a)^2*a + 3*(b*x + a)*a^2 - a^3)$

mupad [B] time = 0.05, size = 64, normalized size = 0.79

$$\frac{5a(a+bx)^{3/2}}{3x^3} - \frac{5a^2\sqrt{a+bx}}{8x^3} - \frac{11(a+bx)^{5/2}}{8x^3} + \frac{b^3 \operatorname{atan}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) 5i}{8\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(5/2)/x^4,x)`

[Out] $(b^3 \operatorname{atan}((a + b*x)^{(1/2)} * i) / a^{(1/2)}) * 5i / (8 * a^{(1/2)}) - (5 * a^2 * (a + b*x)^{(1/2)}) / (8 * x^3) - (11 * (a + b*x)^{(5/2)}) / (8 * x^3) + (5 * a * (a + b*x)^{(3/2)}) / (3 * x^3)$

sympy [A] time = 5.16, size = 104, normalized size = 1.28

$$-\frac{a^2 \sqrt{b} \sqrt{\frac{a}{bx} + 1}}{3x^{\frac{5}{2}}} - \frac{13ab^{\frac{3}{2}} \sqrt{\frac{a}{bx} + 1}}{12x^{\frac{3}{2}}} - \frac{11b^{\frac{5}{2}} \sqrt{\frac{a}{bx} + 1}}{8\sqrt{x}} - \frac{5b^3 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{8\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(5/2)/x**4,x)`

[Out] $-a**2 * \operatorname{sqrt}(b) * \operatorname{sqrt}(a/(b*x) + 1) / (3 * x**(5/2)) - 13 * a * b**(3/2) * \operatorname{sqrt}(a/(b*x) + 1) / (12 * x**(3/2)) - 11 * b**(5/2) * \operatorname{sqrt}(a/(b*x) + 1) / (8 * \operatorname{sqrt}(x)) - 5 * b**3 * \operatorname{asin}(\operatorname{sqrt}(a) / (\operatorname{sqrt}(b) * \operatorname{sqrt}(x))) / (8 * \operatorname{sqrt}(a))$

$$3.308 \quad \int \frac{(a+bx)^{5/2}}{x^5} dx$$

Optimal. Leaf size=103

$$\frac{5b^4 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{64a^{3/2}} - \frac{5b^3\sqrt{a+bx}}{64ax} - \frac{5b^2\sqrt{a+bx}}{32x^2} - \frac{(a+bx)^{5/2}}{4x^4} - \frac{5b(a+bx)^{3/2}}{24x^3}$$

[Out] $-5/24*b*(b*x+a)^{(3/2)}/x^3-1/4*(b*x+a)^{(5/2)}/x^4+5/64*b^4*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(3/2)}-5/32*b^2*(b*x+a)^{(1/2)}/x^2-5/64*b^3*(b*x+a)^{(1/2)}/a/x$

Rubi [A] time = 0.03, antiderivative size = 103, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 51, 63, 208}

$$\frac{5b^4 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{64a^{3/2}} - \frac{5b^2\sqrt{a+bx}}{32x^2} - \frac{5b^3\sqrt{a+bx}}{64ax} - \frac{5b(a+bx)^{3/2}}{24x^3} - \frac{(a+bx)^{5/2}}{4x^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2)/x^5, x]

[Out] $(-5*b^2*\operatorname{Sqrt}[a + b*x])/(32*x^2) - (5*b^3*\operatorname{Sqrt}[a + b*x])/(64*a*x) - (5*b*(a + b*x)^{(3/2)})/(24*x^3) - (a + b*x)^{(5/2)}/(4*x^4) + (5*b^4*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(64*a^{(3/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63


```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{x^5} dx &= -\frac{(a+bx)^{5/2}}{4x^4} + \frac{1}{8}(5b) \int \frac{(a+bx)^{3/2}}{x^4} dx \\
&= -\frac{5b(a+bx)^{3/2}}{24x^3} - \frac{(a+bx)^{5/2}}{4x^4} + \frac{1}{16}(5b^2) \int \frac{\sqrt{a+bx}}{x^3} dx \\
&= -\frac{5b^2\sqrt{a+bx}}{32x^2} - \frac{5b(a+bx)^{3/2}}{24x^3} - \frac{(a+bx)^{5/2}}{4x^4} + \frac{1}{64}(5b^3) \int \frac{1}{x^2\sqrt{a+bx}} dx \\
&= -\frac{5b^2\sqrt{a+bx}}{32x^2} - \frac{5b^3\sqrt{a+bx}}{64ax} - \frac{5b(a+bx)^{3/2}}{24x^3} - \frac{(a+bx)^{5/2}}{4x^4} - \frac{(5b^4) \int \frac{1}{x\sqrt{a+bx}} dx}{128a} \\
&= -\frac{5b^2\sqrt{a+bx}}{32x^2} - \frac{5b^3\sqrt{a+bx}}{64ax} - \frac{5b(a+bx)^{3/2}}{24x^3} - \frac{(a+bx)^{5/2}}{4x^4} - \frac{(5b^3) \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{\frac{a+bx}{a}}\right)}{64a} \\
&= -\frac{5b^2\sqrt{a+bx}}{32x^2} - \frac{5b^3\sqrt{a+bx}}{64ax} - \frac{5b(a+bx)^{3/2}}{24x^3} - \frac{(a+bx)^{5/2}}{4x^4} + \frac{5b^4 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{64a^{3/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.34

$$-\frac{2b^4(a+bx)^{7/2} {}_2F_1\left(\frac{7}{2}, 5; \frac{9}{2}; \frac{bx}{a} + 1\right)}{7a^5}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*x)^(5/2)/x^5, x]
```

```
[Out] (-2*b^4*(a + b*x)^(7/2)*Hypergeometric2F1[7/2, 5, 9/2, 1 + (b*x)/a])/(7*a^5)
```

fricas [A] time = 0.50, size = 167, normalized size = 1.62

$$\left[\frac{15 \sqrt{a} b^4 x^4 \log\left(\frac{bx+2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2(15 ab^3 x^3 + 118 a^2 b^2 x^2 + 136 a^3 b x + 48 a^4) \sqrt{bx+a}}{384 a^2 x^4}, \frac{15 \sqrt{-a} b^4 x^4 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) + (15 a^2 b^3 x^3 + 118 a^2 b^2 x^2 + 136 a^3 b x + 48 a^4) \sqrt{bx+a}}{192 a^2 x^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^5,x, algorithm="fricas")

[Out] [1/384*(15*sqrt(a)*b^4*x^4*log((b*x + 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) - 2*(15*a*b^3*x^3 + 118*a^2*b^2*x^2 + 136*a^3*b*x + 48*a^4)*sqrt(b*x + a))/(a^2*x^4), -1/192*(15*sqrt(-a)*b^4*x^4*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (15*a*b^3*x^3 + 118*a^2*b^2*x^2 + 136*a^3*b*x + 48*a^4)*sqrt(b*x + a))/(a^2*x^4)]

giac [A] time = 1.09, size = 99, normalized size = 0.96

$$-\frac{\frac{15 b^5 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} + \frac{15 (bx+a)^{\frac{7}{2}} b^5 + 73 (bx+a)^{\frac{5}{2}} a b^5 - 55 (bx+a)^{\frac{3}{2}} a^2 b^5 + 15 \sqrt{bx+a} a^3 b^5}{ab^4 x^4}}{192 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^5,x, algorithm="giac")

[Out] -1/192*(15*b^5*arctan(sqrt(b*x + a)/sqrt(-a))/(sqrt(-a)*a) + (15*(b*x + a)^(7/2)*b^5 + 73*(b*x + a)^(5/2)*a*b^5 - 55*(b*x + a)^(3/2)*a^2*b^5 + 15*sqrt(b*x + a)*a^3*b^5)/(a*b^4*x^4))/b

maple [A] time = 0.01, size = 75, normalized size = 0.73

$$2 \left(\frac{5 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{128 a^{\frac{3}{2}}} + \frac{-\frac{5 \sqrt{bx+a} a^2}{128} + \frac{55 (bx+a)^{\frac{3}{2}} a}{384} - \frac{5 (bx+a)^{\frac{7}{2}}}{128 a} - \frac{73 (bx+a)^{\frac{5}{2}}}{384}}{b^4 x^4} \right) b^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/x^5,x)

[Out] 2*b^4*((-5/128/a*(b*x+a)^(7/2)-73/384*(b*x+a)^(5/2)+55/384*(b*x+a)^(3/2)*a-5/128*(b*x+a)^(1/2)*a^2)/x^4/b^4+5/128*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(3/2))

maxima [A] time = 2.93, size = 144, normalized size = 1.40

$$\frac{5b^4 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{128a^{\frac{3}{2}}} - \frac{15(bx+a)^{\frac{7}{2}}b^4 + 73(bx+a)^{\frac{5}{2}}ab^4 - 55(bx+a)^{\frac{3}{2}}a^2b^4 + 15\sqrt{bx+a}a^3b^4}{192\left((bx+a)^4a - 4(bx+a)^3a^2 + 6(bx+a)^2a^3 - 4(bx+a)a^4 + a^5\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^5,x, algorithm="maxima")

[Out] $-5/128*b^4*\log((\text{sqrt}(b*x + a) - \text{sqrt}(a))/(\text{sqrt}(b*x + a) + \text{sqrt}(a)))/a^{(3/2)}$
 $- 1/192*(15*(b*x + a)^{(7/2)}*b^4 + 73*(b*x + a)^{(5/2)}*a*b^4 - 55*(b*x + a)^{(3/2)}*a^2*b^4 + 15*\text{sqrt}(b*x + a)*a^3*b^4)/((b*x + a)^4*a - 4*(b*x + a)^3*a^2 + 6*(b*x + a)^2*a^3 - 4*(b*x + a)*a^4 + a^5)$

mupad [B] time = 0.11, size = 79, normalized size = 0.77

$$\frac{55a(a+bx)^{3/2}}{192x^4} - \frac{5a^2\sqrt{a+bx}}{64x^4} - \frac{5(a+bx)^{7/2}}{64ax^4} - \frac{73(a+bx)^{5/2}}{192x^4} - \frac{b^4 \operatorname{atan}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) 5i}{64a^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)/x^5,x)

[Out] $(55*a*(a + b*x)^{(3/2)})/(192*x^4) - (5*a^2*(a + b*x)^{(1/2)})/(64*x^4) - (5*(a + b*x)^{(7/2)})/(64*a*x^4) - (b^4*\operatorname{atan}(((a + b*x)^{(1/2)}*1i)/a^{(1/2)})*5i)/(64*a^{(3/2)}) - (73*(a + b*x)^{(5/2)})/(192*x^4)$

sympy [A] time = 8.36, size = 155, normalized size = 1.50

$$\frac{a^3}{4\sqrt{b}x^{\frac{9}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{23a^2\sqrt{b}}{24x^{\frac{7}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{127ab^{\frac{3}{2}}}{96x^{\frac{5}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{133b^{\frac{5}{2}}}{192x^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{5b^{\frac{7}{2}}}{64a\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{5b^4 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{64a^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)/x**5,x)

[Out] $-a^{**3}/(4*\text{sqrt}(b)*x^{**9/2}*\text{sqrt}(a/(b*x) + 1)) - 23*a^{**2}*\text{sqrt}(b)/(24*x^{**7/2}*\text{sqrt}(a/(b*x) + 1)) - 127*a*b^{**3/2}/(96*x^{**5/2}*\text{sqrt}(a/(b*x) + 1)) - 133*b^{**5/2}/(192*x^{**3/2}*\text{sqrt}(a/(b*x) + 1)) - 5*b^{**7/2}/(64*a*\text{sqrt}(x)*\text{sqrt}(a/(b*x) + 1)) + 5*b^{**4}*\operatorname{asinh}(\text{sqrt}(a)/(\text{sqrt}(b)*\text{sqrt}(x)))/(64*a^{**3/2})$

3.309 $\int x^7(a+bx)^{9/2} dx$

Optimal. Leaf size=146

$$-\frac{2a^7(a+bx)^{11/2}}{11b^8} + \frac{14a^6(a+bx)^{13/2}}{13b^8} - \frac{14a^5(a+bx)^{15/2}}{5b^8} + \frac{70a^4(a+bx)^{17/2}}{17b^8} - \frac{70a^3(a+bx)^{19/2}}{19b^8} + \frac{2a^2(a+bx)^{21/2}}{b^8} + \frac{2(a+bx)^{23/2}}{25b^8}$$

[Out] $-2/11*a^7*(b*x+a)^{(11/2)}/b^8+14/13*a^6*(b*x+a)^{(13/2)}/b^8-14/5*a^5*(b*x+a)^{(15/2)}/b^8+70/17*a^4*(b*x+a)^{(17/2)}/b^8-70/19*a^3*(b*x+a)^{(19/2)}/b^8+2*a^2*(b*x+a)^{(21/2)}/b^8-14/23*a*(b*x+a)^{(23/2)}/b^8+2/25*(b*x+a)^{(25/2)}/b^8$

Rubi [A] time = 0.04, antiderivative size = 146, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2a^2(a+bx)^{21/2}}{b^8} - \frac{70a^3(a+bx)^{19/2}}{19b^8} + \frac{70a^4(a+bx)^{17/2}}{17b^8} - \frac{14a^5(a+bx)^{15/2}}{5b^8} + \frac{14a^6(a+bx)^{13/2}}{13b^8} - \frac{2a^7(a+bx)^{11/2}}{11b^8} + \frac{2(a+bx)^{23/2}}{25b^8}$$

Antiderivative was successfully verified.

[In] Int[x^7*(a + b*x)^(9/2), x]

[Out] $(-2*a^7*(a + b*x)^{(11/2)})/(11*b^8) + (14*a^6*(a + b*x)^{(13/2)})/(13*b^8) - (14*a^5*(a + b*x)^{(15/2)})/(5*b^8) + (70*a^4*(a + b*x)^{(17/2)})/(17*b^8) - (70*a^3*(a + b*x)^{(19/2)})/(19*b^8) + (2*a^2*(a + b*x)^{(21/2)})/b^8 - (14*a*(a + b*x)^{(23/2)})/(23*b^8) + (2*(a + b*x)^{(25/2)})/(25*b^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^7(a+bx)^{9/2} dx &= \int \left(-\frac{a^7(a+bx)^{9/2}}{b^7} + \frac{7a^6(a+bx)^{11/2}}{b^7} - \frac{21a^5(a+bx)^{13/2}}{b^7} + \frac{35a^4(a+bx)^{15/2}}{b^7} - \frac{35a^3(a+bx)^{17/2}}{b^7} \right. \\ &= -\frac{2a^7(a+bx)^{11/2}}{11b^8} + \frac{14a^6(a+bx)^{13/2}}{13b^8} - \frac{14a^5(a+bx)^{15/2}}{5b^8} + \frac{70a^4(a+bx)^{17/2}}{17b^8} - \frac{70a^3(a+bx)^{19/2}}{19b^8} \end{aligned}$$

Mathematica [A] time = 0.05, size = 90, normalized size = 0.62

$$\frac{2(a+bx)^{11/2}(-2048a^7 + 11264a^6bx - 36608a^5b^2x^2 + 91520a^4b^3x^3 - 194480a^3b^4x^4 + 369512a^2b^5x^5 - 646646ab^6x^6 + 26558675b^8)}{26558675b^8}$$

Antiderivative was successfully verified.

[In] Integrate[x^7*(a + b*x)^(9/2),x]

[Out] $(2*(a + b*x)^{(11/2)}*(-2048*a^7 + 11264*a^6*b*x - 36608*a^5*b^2*x^2 + 91520*a^4*b^3*x^3 - 194480*a^3*b^4*x^4 + 369512*a^2*b^5*x^5 - 646646*a*b^6*x^6 + 1062347*b^7*x^7))/(26558675*b^8)$

fricas [A] time = 0.46, size = 141, normalized size = 0.97

$$\frac{2(1062347 b^{12} x^{12} + 4665089 a b^{11} x^{11} + 7759752 a^2 b^{10} x^{10} + 5810090 a^3 b^9 x^9 + 1659515 a^4 b^8 x^8 + 429 a^5 b^7 x^7 - 462 a^6 b^6 x^6 + 504 a^7 b^5 x^5 - 560 a^8 b^4 x^4 + 640 a^9 b^3 x^3 - 768 a^{10} b^2 x^2 + 1024 a^{11} b x - 2048 a^{12}) \sqrt{b x + a}}{26558675 b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^(9/2),x, algorithm="fricas")

[Out] $2/26558675*(1062347*b^{12}*x^{12} + 4665089*a*b^{11}*x^{11} + 7759752*a^2*b^{10}*x^{10} + 5810090*a^3*b^9*x^9 + 1659515*a^4*b^8*x^8 + 429*a^5*b^7*x^7 - 462*a^6*b^6*x^6 + 504*a^7*b^5*x^5 - 560*a^8*b^4*x^4 + 640*a^9*b^3*x^3 - 768*a^{10}*b^2*x^2 + 1024*a^{11}*b*x - 2048*a^{12})*\text{sqrt}(b*x + a)/b^8$

giac [B] time = 1.14, size = 781, normalized size = 5.35

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^(9/2),x, algorithm="giac")

[Out] $2/1673196525*(260015*(429*(b*x + a)^{(15/2)} - 3465*(b*x + a)^{(13/2)}*a + 12285*(b*x + a)^{(11/2)}*a^2 - 25025*(b*x + a)^{(9/2)}*a^3 + 32175*(b*x + a)^{(7/2)}*a^4 - 27027*(b*x + a)^{(5/2)}*a^5 + 15015*(b*x + a)^{(3/2)}*a^6 - 6435*\text{sqrt}(b*x + a)*a^7)*a^5/b^7 + 76475*(6435*(b*x + a)^{(17/2)} - 58344*(b*x + a)^{(15/2)}*a + 235620*(b*x + a)^{(13/2)}*a^2 - 556920*(b*x + a)^{(11/2)}*a^3 + 850850*(b*x + a)^{(9/2)}*a^4 - 875160*(b*x + a)^{(7/2)}*a^5 + 612612*(b*x + a)^{(5/2)}*a^6 - 291720*(b*x + a)^{(3/2)}*a^7 + 109395*\text{sqrt}(b*x + a)*a^8)*a^4/b^7 + 72450*(12155*(b*x + a)^{(19/2)} - 122265*(b*x + a)^{(17/2)}*a + 554268*(b*x + a)^{(15/2)}*a^2 - 1492260*(b*x + a)^{(13/2)}*a^3 + 2645370*(b*x + a)^{(11/2)}*a^4 - 3233230*(b*x + a)^{(9/2)}*a^5 + 2771340*(b*x + a)^{(7/2)}*a^6 - 1662804*(b*x + a)^{(5/2)}*a^7 + 692835*(b*x + a)^{(3/2)}*a^8 - 230945*\text{sqrt}(b*x + a)*a^9)*a^3/b^7 + 17250*(46189*(b*x + a)^{(21/2)} - 510510*(b*x + a)^{(19/2)}*a + 2567565*(b*x + a)^{(17/2)}*a^2 - 7759752*(b*x + a)^{(15/2)}*a^3 + 15668730*(b*x + a)^{(13/2)}*a^4 - 22221108*(b*x + a)^{(11/2)}*a^5 + 22632610*(b*x + a)^{(9/2)}*a^6 - 16628040*(b*x + a)^{(7/2)}*a^7 + 8729721*(b*x + a)^{(5/2)}*a^8 - 3233230*(b*x + a)^{(3/2)}*a^9 + 969969*\text{sqrt}(b*x + a)*a^{10})*a^2/b^7 + 4125*(88179*(b*x + a)^{(23/2)} - 1062347*(b*x + a)^{(21/2)}*a + 5870865*(b*x + a)^{(19/2)}*a^2 - 19684665*(b*x +$

$$a^{(17/2)}*a^3 + 44618574*(b*x + a)^{(15/2)}*a^4 - 72076158*(b*x + a)^{(13/2)}*a^5 + 85180914*(b*x + a)^{(11/2)}*a^6 - 74364290*(b*x + a)^{(9/2)}*a^7 + 47805615*(b*x + a)^{(7/2)}*a^8 - 22309287*(b*x + a)^{(5/2)}*a^9 + 7436429*(b*x + a)^{(3/2)}*a^{10} - 2028117*\sqrt{b*x + a}*a^{11}*a/b^7 + 99*(676039*(b*x + a)^{(25/2)} - 8817900*(b*x + a)^{(23/2)}*a + 53117350*(b*x + a)^{(21/2)}*a^2 - 195695500*(b*x + a)^{(19/2)}*a^3 + 492116625*(b*x + a)^{(17/2)}*a^4 - 892371480*(b*x + a)^{(15/2)}*a^5 + 1201269300*(b*x + a)^{(13/2)}*a^6 - 1216870200*(b*x + a)^{(11/2)}*a^7 + 929553625*(b*x + a)^{(9/2)}*a^8 - 531173500*(b*x + a)^{(7/2)}*a^9 + 223092870*(b*x + a)^{(5/2)}*a^{10} - 67603900*(b*x + a)^{(3/2)}*a^{11} + 16900975*\sqrt{b*x + a}*a^{12})/b^7)/b$$

maple [A] time = 0.01, size = 87, normalized size = 0.60

$$\frac{2(bx + a)^{\frac{11}{2}} \left(-1062347b^7x^7 + 646646ab^6x^6 - 369512a^2b^5x^5 + 194480a^3b^4x^4 - 91520a^4b^3x^3 + 36608a^5b^2x^2 - 2048a^6bx + 2048a^7 \right)}{26558675b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7*(b*x+a)^(9/2), x)

[Out] $-2/26558675*(b*x+a)^{(11/2)}*(-1062347*b^7*x^7+646646*a*b^6*x^6-369512*a^2*b^5*x^5+194480*a^3*b^4*x^4-91520*a^4*b^3*x^3+36608*a^5*b^2*x^2-11264*a^6*b*x+2048*a^7)/b^8$

maxima [A] time = 1.33, size = 116, normalized size = 0.79

$$\frac{2(bx + a)^{\frac{25}{2}}}{25b^8} - \frac{14(bx + a)^{\frac{23}{2}}a}{23b^8} + \frac{2(bx + a)^{\frac{21}{2}}a^2}{b^8} - \frac{70(bx + a)^{\frac{19}{2}}a^3}{19b^8} + \frac{70(bx + a)^{\frac{17}{2}}a^4}{17b^8} - \frac{14(bx + a)^{\frac{15}{2}}a^5}{5b^8} + \frac{14(bx + a)^{\frac{13}{2}}a^6}{13b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^(9/2), x, algorithm="maxima")

[Out] $2/25*(b*x + a)^{(25/2)}/b^8 - 14/23*(b*x + a)^{(23/2)}*a/b^8 + 2*(b*x + a)^{(21/2)}*a^2/b^8 - 70/19*(b*x + a)^{(19/2)}*a^3/b^8 + 70/17*(b*x + a)^{(17/2)}*a^4/b^8 - 14/5*(b*x + a)^{(15/2)}*a^5/b^8 + 14/13*(b*x + a)^{(13/2)}*a^6/b^8 - 2/11*(b*x + a)^{(11/2)}*a^7/b^8$

mupad [B] time = 0.04, size = 116, normalized size = 0.79

$$\frac{2(a + bx)^{25/2}}{25b^8} - \frac{2a^7(a + bx)^{11/2}}{11b^8} + \frac{14a^6(a + bx)^{13/2}}{13b^8} - \frac{14a^5(a + bx)^{15/2}}{5b^8} + \frac{70a^4(a + bx)^{17/2}}{17b^8} - \frac{70a^3(a + bx)^{19/2}}{19b^8} + \frac{2a^2(a + bx)^{21/2}}{2b^8} - \frac{2a(a + bx)^{23/2}}{23b^8} + \frac{2(a + bx)^{25/2}}{25b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7*(a + b*x)^(9/2), x)

```
[Out] (2*(a + b*x)^(25/2))/(25*b^8) - (2*a^7*(a + b*x)^(11/2))/(11*b^8) + (14*a^6
*(a + b*x)^(13/2))/(13*b^8) - (14*a^5*(a + b*x)^(15/2))/(5*b^8) + (70*a^4*(
a + b*x)^(17/2))/(17*b^8) - (70*a^3*(a + b*x)^(19/2))/(19*b^8) + (2*a^2*(a
+ b*x)^(21/2))/b^8 - (14*a*(a + b*x)^(23/2))/(23*b^8)
```

```
sympy [A] time = 40.30, size = 279, normalized size = 1.91
```

$$\left\{ \begin{array}{l} -\frac{4096a^{12}\sqrt{a+bx}}{26558675b^8} + \frac{2048a^{11}x\sqrt{a+bx}}{26558675b^7} - \frac{1536a^{10}x^2\sqrt{a+bx}}{26558675b^6} + \frac{256a^9x^3\sqrt{a+bx}}{5311735b^5} - \frac{224a^8x^4\sqrt{a+bx}}{5311735b^4} + \frac{1008a^7x^5\sqrt{a+bx}}{26558675b^3} - \frac{84a^6x^6\sqrt{a+bx}}{2414425b^2} + \dots \\ \frac{9}{8}a^{\frac{9}{2}}x^8 \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**7*(b*x+a)**(9/2),x)
```

```
[Out] Piecewise((-4096*a**12*sqrt(a + b*x)/(26558675*b**8) + 2048*a**11*x*sqrt(a
+ b*x)/(26558675*b**7) - 1536*a**10*x**2*sqrt(a + b*x)/(26558675*b**6) + 25
6*a**9*x**3*sqrt(a + b*x)/(5311735*b**5) - 224*a**8*x**4*sqrt(a + b*x)/(531
1735*b**4) + 1008*a**7*x**5*sqrt(a + b*x)/(26558675*b**3) - 84*a**6*x**6*sq
rt(a + b*x)/(2414425*b**2) + 6*a**5*x**7*sqrt(a + b*x)/(185725*b) + 4642*a*
*4*x**8*sqrt(a + b*x)/37145 + 956*a**3*b*x**9*sqrt(a + b*x)/2185 + 336*a**2
*b**2*x**10*sqrt(a + b*x)/575 + 202*a*b**3*x**11*sqrt(a + b*x)/575 + 2*b**4
*x**12*sqrt(a + b*x)/25, Ne(b, 0)), (a**(9/2)*x**8/8, True))
```

3.310 $\int x^6(a + bx)^{9/2} dx$

Optimal. Leaf size=127

$$\frac{2a^6(a + bx)^{11/2}}{11b^7} - \frac{12a^5(a + bx)^{13/2}}{13b^7} + \frac{2a^4(a + bx)^{15/2}}{b^7} - \frac{40a^3(a + bx)^{17/2}}{17b^7} + \frac{30a^2(a + bx)^{19/2}}{19b^7} + \frac{2(a + bx)^{23/2}}{23b^7} - \frac{4a(a + bx)}{7b^7}$$

[Out] $2/11*a^6*(b*x+a)^{(11/2)}/b^7-12/13*a^5*(b*x+a)^{(13/2)}/b^7+2*a^4*(b*x+a)^{(15/2)}/b^7-40/17*a^3*(b*x+a)^{(17/2)}/b^7+30/19*a^2*(b*x+a)^{(19/2)}/b^7-4/7*a*(b*x+a)^{(21/2)}/b^7+2/23*(b*x+a)^{(23/2)}/b^7$

Rubi [A] time = 0.04, antiderivative size = 127, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{30a^2(a + bx)^{19/2}}{19b^7} - \frac{40a^3(a + bx)^{17/2}}{17b^7} + \frac{2a^4(a + bx)^{15/2}}{b^7} - \frac{12a^5(a + bx)^{13/2}}{13b^7} + \frac{2a^6(a + bx)^{11/2}}{11b^7} + \frac{2(a + bx)^{23/2}}{23b^7} - \frac{4a(a + bx)}{7b^7}$$

Antiderivative was successfully verified.

[In] Int[x^6*(a + b*x)^(9/2), x]

[Out] $(2*a^6*(a + b*x)^{(11/2)})/(11*b^7) - (12*a^5*(a + b*x)^{(13/2)})/(13*b^7) + (2*a^4*(a + b*x)^{(15/2)})/b^7 - (40*a^3*(a + b*x)^{(17/2)})/(17*b^7) + (30*a^2*(a + b*x)^{(19/2)})/(19*b^7) - (4*a*(a + b*x)^{(21/2)})/(7*b^7) + (2*(a + b*x)^{(23/2)})/(23*b^7)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int x^6(a + bx)^{9/2} dx &= \int \left(\frac{a^6(a + bx)^{9/2}}{b^6} - \frac{6a^5(a + bx)^{11/2}}{b^6} + \frac{15a^4(a + bx)^{13/2}}{b^6} - \frac{20a^3(a + bx)^{15/2}}{b^6} + \frac{15a^2(a + bx)^{17/2}}{b^6} \right. \\ &= \frac{2a^6(a + bx)^{11/2}}{11b^7} - \frac{12a^5(a + bx)^{13/2}}{13b^7} + \frac{2a^4(a + bx)^{15/2}}{b^7} - \frac{40a^3(a + bx)^{17/2}}{17b^7} + \frac{30a^2(a + bx)^{19/2}}{19b^7} \end{aligned}$$

Mathematica [A] time = 0.04, size = 79, normalized size = 0.62

$$\frac{2(a + bx)^{11/2} (1024a^6 - 5632a^5bx + 18304a^4b^2x^2 - 45760a^3b^3x^3 + 97240a^2b^4x^4 - 184756ab^5x^5 + 323323b^6x^6)}{7436429b^7}$$

Antiderivative was successfully verified.

[In] Integrate[x^6*(a + b*x)^(9/2),x]

[Out] $(2*(a + b*x)^{(11/2)}*(1024*a^6 - 5632*a^5*b*x + 18304*a^4*b^2*x^2 - 45760*a^3*b^3*x^3 + 97240*a^2*b^4*x^4 - 184756*a*b^5*x^5 + 323323*b^6*x^6))/(7436429*b^7)$

fricas [A] time = 0.47, size = 130, normalized size = 1.02

$$\frac{2(323323 b^{11} x^{11} + 1431859 a b^{10} x^{10} + 2406690 a^2 b^9 x^9 + 1826110 a^3 b^8 x^8 + 530959 a^4 b^7 x^7 + 231 a^5 b^6 x^6 - 252 a^6 b^5 x^5 + 280 a^7 b^4 x^4 - 320 a^8 b^3 x^3 + 384 a^9 b^2 x^2 - 512 a^{10} b x + 1024 a^{11}) \sqrt{b x + a}}{7436429 b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^(9/2),x, algorithm="fricas")

[Out] $2/7436429*(323323*b^{11}*x^{11} + 1431859*a*b^{10}*x^{10} + 2406690*a^2*b^9*x^9 + 1826110*a^3*b^8*x^8 + 530959*a^4*b^7*x^7 + 231*a^5*b^6*x^6 - 252*a^6*b^5*x^5 + 280*a^7*b^4*x^4 - 320*a^8*b^3*x^3 + 384*a^9*b^2*x^2 - 512*a^{10}*b*x + 1024*a^{11})*\sqrt{b*x + a}/b^7$

giac [B] time = 1.32, size = 709, normalized size = 5.58

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^(9/2),x, algorithm="giac")

[Out] $2/66927861*(22287*(231*(b*x + a)^{(13/2)} - 1638*(b*x + a)^{(11/2)}*a + 5005*(b*x + a)^{(9/2)}*a^2 - 8580*(b*x + a)^{(7/2)}*a^3 + 9009*(b*x + a)^{(5/2)}*a^4 - 6006*(b*x + a)^{(3/2)}*a^5 + 3003*\sqrt{b*x + a}*a^6)*a^5/b^6 + 52003*(429*(b*x + a)^{(15/2)} - 3465*(b*x + a)^{(13/2)}*a + 12285*(b*x + a)^{(11/2)}*a^2 - 25025*(b*x + a)^{(9/2)}*a^3 + 32175*(b*x + a)^{(7/2)}*a^4 - 27027*(b*x + a)^{(5/2)}*a^5 + 15015*(b*x + a)^{(3/2)}*a^6 - 6435*\sqrt{b*x + a}*a^7)*a^4/b^6 + 6118*(6435*(b*x + a)^{(17/2)} - 58344*(b*x + a)^{(15/2)}*a + 235620*(b*x + a)^{(13/2)}*a^2 - 556920*(b*x + a)^{(11/2)}*a^3 + 850850*(b*x + a)^{(9/2)}*a^4 - 875160*(b*x + a)^{(7/2)}*a^5 + 612612*(b*x + a)^{(5/2)}*a^6 - 291720*(b*x + a)^{(3/2)}*a^7 + 109395*\sqrt{b*x + a}*a^8)*a^3/b^6 + 2898*(12155*(b*x + a)^{(19/2)} - 122265*(b*x + a)^{(17/2)}*a + 554268*(b*x + a)^{(15/2)}*a^2 - 1492260*(b*x + a)^{(13/2)}*a^3 + 2645370*(b*x + a)^{(11/2)}*a^4 - 3233230*(b*x + a)^{(9/2)}*a^5 + 2771340*(b*x + a)^{(7/2)}*a^6 - 1662804*(b*x + a)^{(5/2)}*a^7 + 692835*(b*x + a)^{(3/2)}*a^8 - 230945*\sqrt{b*x + a}*a^9)*a^2/b^6 + 345*(46189*(b*x + a)^{(21/2)} - 510510*(b*x + a)^{(19/2)}*a + 2567565*(b*x + a)^{(17/2)}*a^2 - 7759752*(b*x + a)^{(15/2)}*a^3 + 15668730*(b*x + a)^{(13/2)}*a^4 - 22221108*(b*x + a)^{(11/2)}*a^5 + 22632610*(b*x + a)^{(9/2)}*a^6 - 16628040*(b*x + a)^{(7/2)}*a^7 + 8729721*(b*x$

$$\begin{aligned} &+ a^{(5/2)} * a^8 - 3233230 * (b*x + a)^{(3/2)} * a^9 + 969969 * \sqrt{b*x + a} * a^{10} * a \\ &/b^6 + 33 * (88179 * (b*x + a)^{(23/2)} - 1062347 * (b*x + a)^{(21/2)} * a + 5870865 * (b \\ &*x + a)^{(19/2)} * a^2 - 19684665 * (b*x + a)^{(17/2)} * a^3 + 44618574 * (b*x + a)^{(15 \\ &/2)} * a^4 - 72076158 * (b*x + a)^{(13/2)} * a^5 + 85180914 * (b*x + a)^{(11/2)} * a^6 - 7 \\ &4364290 * (b*x + a)^{(9/2)} * a^7 + 47805615 * (b*x + a)^{(7/2)} * a^8 - 22309287 * (b*x \\ &+ a)^{(5/2)} * a^9 + 7436429 * (b*x + a)^{(3/2)} * a^{10} - 2028117 * \sqrt{b*x + a} * a^{11} \\ &/b^6) / b \end{aligned}$$

maple [A] time = 0.01, size = 76, normalized size = 0.60

$$\frac{2 (bx + a)^{\frac{11}{2}} (323323x^6b^6 - 184756ax^5b^5 + 97240a^2x^4b^4 - 45760a^3x^3b^3 + 18304a^4x^2b^2 - 5632a^5xb + 1024a^6)}{7436429b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6*(b*x+a)^(9/2),x)

[Out] 2/7436429*(b*x+a)^(11/2)*(323323*b^6*x^6-184756*a*b^5*x^5+97240*a^2*b^4*x^4-45760*a^3*b^3*x^3+18304*a^4*b^2*x^2-5632*a^5*b*x+1024*a^6)/b^7

maxima [A] time = 1.34, size = 101, normalized size = 0.80

$$\frac{2 (bx + a)^{\frac{23}{2}}}{23 b^7} - \frac{4 (bx + a)^{\frac{21}{2}} a}{7 b^7} + \frac{30 (bx + a)^{\frac{19}{2}} a^2}{19 b^7} - \frac{40 (bx + a)^{\frac{17}{2}} a^3}{17 b^7} + \frac{2 (bx + a)^{\frac{15}{2}} a^4}{b^7} - \frac{12 (bx + a)^{\frac{13}{2}} a^5}{13 b^7} + \frac{2 (bx + a)^{\frac{11}{2}} a^6}{11 b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^(9/2),x, algorithm="maxima")

[Out] 2/23*(b*x + a)^(23/2)/b^7 - 4/7*(b*x + a)^(21/2)*a/b^7 + 30/19*(b*x + a)^(19/2)*a^2/b^7 - 40/17*(b*x + a)^(17/2)*a^3/b^7 + 2*(b*x + a)^(15/2)*a^4/b^7 - 12/13*(b*x + a)^(13/2)*a^5/b^7 + 2/11*(b*x + a)^(11/2)*a^6/b^7

mupad [B] time = 0.03, size = 101, normalized size = 0.80

$$\frac{2 (a + bx)^{23/2}}{23 b^7} + \frac{2 a^6 (a + bx)^{11/2}}{11 b^7} - \frac{12 a^5 (a + bx)^{13/2}}{13 b^7} + \frac{2 a^4 (a + bx)^{15/2}}{b^7} - \frac{40 a^3 (a + bx)^{17/2}}{17 b^7} + \frac{30 a^2 (a + bx)^{19/2}}{19 b^7} - \frac{4 a (a + bx)^{21/2}}{7 b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6*(a + b*x)^(9/2),x)

[Out] (2*(a + b*x)^(23/2))/(23*b^7) + (2*a^6*(a + b*x)^(11/2))/(11*b^7) - (12*a^5*(a + b*x)^(13/2))/(13*b^7) + (2*a^4*(a + b*x)^(15/2))/b^7 - (40*a^3*(a + b*x)^(17/2))/(17*b^7) + (30*a^2*(a + b*x)^(19/2))/(19*b^7) - (4*a*(a + b*x)^(21/2))/(7*b^7)

sympy [A] time = 36.61, size = 257, normalized size = 2.02

$$\left\{ \begin{array}{l} \frac{2048a^{11}\sqrt{a+bx}}{7436429b^7} - \frac{1024a^{10}x\sqrt{a+bx}}{7436429b^6} + \frac{768a^9x^2\sqrt{a+bx}}{7436429b^5} - \frac{640a^8x^3\sqrt{a+bx}}{7436429b^4} + \frac{80a^7x^4\sqrt{a+bx}}{1062347b^3} - \frac{72a^6x^5\sqrt{a+bx}}{1062347b^2} + \frac{6a^5x^6\sqrt{a+bx}}{96577b} + \frac{7426a^4x^7}{52003} \\ \frac{a^{\frac{9}{2}}x^7}{7} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6*(b*x+a)**(9/2),x)

[Out] Piecewise((2048*a**11*sqrt(a + b*x)/(7436429*b**7) - 1024*a**10*x*sqrt(a + b*x)/(7436429*b**6) + 768*a**9*x**2*sqrt(a + b*x)/(7436429*b**5) - 640*a**8*x**3*sqrt(a + b*x)/(7436429*b**4) + 80*a**7*x**4*sqrt(a + b*x)/(1062347*b**3) - 72*a**6*x**5*sqrt(a + b*x)/(1062347*b**2) + 6*a**5*x**6*sqrt(a + b*x)/(96577*b) + 7426*a**4*x**7*sqrt(a + b*x)/52003 + 25540*a**3*b*x**8*sqrt(a + b*x)/52003 + 1980*a**2*b**2*x**9*sqrt(a + b*x)/3059 + 62*a*b**3*x**10*sqrt(a + b*x)/161 + 2*b**4*x**11*sqrt(a + b*x)/23, Ne(b, 0)), (a**(9/2)*x**7/7, True))

3.311 $\int x^5(a + bx)^{9/2} dx$

Optimal. Leaf size=110

$$-\frac{2a^5(a+bx)^{11/2}}{11b^6} + \frac{10a^4(a+bx)^{13/2}}{13b^6} - \frac{4a^3(a+bx)^{15/2}}{3b^6} + \frac{20a^2(a+bx)^{17/2}}{17b^6} + \frac{2(a+bx)^{21/2}}{21b^6} - \frac{10a(a+bx)^{19/2}}{19b^6}$$

[Out] $-2/11*a^5*(b*x+a)^{(11/2)}/b^6+10/13*a^4*(b*x+a)^{(13/2)}/b^6-4/3*a^3*(b*x+a)^{(15/2)}/b^6+20/17*a^2*(b*x+a)^{(17/2)}/b^6-10/19*a*(b*x+a)^{(19/2)}/b^6+2/21*(b*x+a)^{(21/2)}/b^6$

Rubi [A] time = 0.03, antiderivative size = 110, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{20a^2(a+bx)^{17/2}}{17b^6} - \frac{4a^3(a+bx)^{15/2}}{3b^6} + \frac{10a^4(a+bx)^{13/2}}{13b^6} - \frac{2a^5(a+bx)^{11/2}}{11b^6} + \frac{2(a+bx)^{21/2}}{21b^6} - \frac{10a(a+bx)^{19/2}}{19b^6}$$

Antiderivative was successfully verified.

[In] Int[x^5*(a + b*x)^(9/2), x]

[Out] $(-2*a^5*(a + b*x)^{(11/2)})/(11*b^6) + (10*a^4*(a + b*x)^{(13/2)})/(13*b^6) - (4*a^3*(a + b*x)^{(15/2)})/(3*b^6) + (20*a^2*(a + b*x)^{(17/2)})/(17*b^6) - (10*a*(a + b*x)^{(19/2)})/(19*b^6) + (2*(a + b*x)^{(21/2)})/(21*b^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int x^5(a + bx)^{9/2} dx &= \int \left(-\frac{a^5(a + bx)^{9/2}}{b^5} + \frac{5a^4(a + bx)^{11/2}}{b^5} - \frac{10a^3(a + bx)^{13/2}}{b^5} + \frac{10a^2(a + bx)^{15/2}}{b^5} - \frac{5a(a + bx)^{17/2}}{b^5} \right. \\ &= -\frac{2a^5(a + bx)^{11/2}}{11b^6} + \frac{10a^4(a + bx)^{13/2}}{13b^6} - \frac{4a^3(a + bx)^{15/2}}{3b^6} + \frac{20a^2(a + bx)^{17/2}}{17b^6} - \frac{10a(a + bx)^{19/2}}{19b^6} \end{aligned}$$

Mathematica [A] time = 0.04, size = 68, normalized size = 0.62

$$\frac{2(a + bx)^{11/2} (-256a^5 + 1408a^4bx - 4576a^3b^2x^2 + 11440a^2b^3x^3 - 24310ab^4x^4 + 46189b^5x^5)}{969969b^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^5*(a + b*x)^(9/2),x]

[Out] $(2*(a + b*x)^{(11/2)}*(-256*a^5 + 1408*a^4*b*x - 4576*a^3*b^2*x^2 + 11440*a^2*b^3*x^3 - 24310*a*b^4*x^4 + 46189*b^5*x^5))/(969969*b^6)$

fricas [A] time = 0.56, size = 119, normalized size = 1.08

$$\frac{2(46189 b^{10} x^{10} + 206635 a b^9 x^9 + 351780 a^2 b^8 x^8 + 271414 a^3 b^7 x^7 + 80773 a^4 b^6 x^6 + 63 a^5 b^5 x^5 - 70 a^6 b^4 x^4 + 80 a^7 b^3 x^3 - 96 a^8 b^2 x^2 + 128 a^9 b x - 256 a^{10}) \sqrt{b x + a}}{969969 b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^(9/2),x, algorithm="fricas")

[Out] $2/969969*(46189*b^{10}*x^{10} + 206635*a*b^9*x^9 + 351780*a^2*b^8*x^8 + 271414*a^3*b^7*x^7 + 80773*a^4*b^6*x^6 + 63*a^5*b^5*x^5 - 70*a^6*b^4*x^4 + 80*a^7*b^3*x^3 - 96*a^8*b^2*x^2 + 128*a^9*b*x - 256*a^{10})*\sqrt{b*x + a}/b^6$

giac [B] time = 1.05, size = 637, normalized size = 5.79

$$2 \left(\frac{4199 \left(63 (bx+a)^{\frac{11}{2}} - 385 (bx+a)^{\frac{9}{2}} a + 990 (bx+a)^{\frac{7}{2}} a^2 - 1386 (bx+a)^{\frac{5}{2}} a^3 + 1155 (bx+a)^{\frac{3}{2}} a^4 - 693 \sqrt{bx+a} a^5 \right) a^5}{b^5} + \frac{4845 \left(231 (bx+a)^{\frac{13}{2}} - 1638 (bx+a)^{\frac{11}{2}} \right) a^5}{b^5} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^(9/2),x, algorithm="giac")

[Out] $2/2909907*(4199*(63*(b*x + a)^{(11/2)} - 385*(b*x + a)^{(9/2)}*a + 990*(b*x + a)^{(7/2)}*a^2 - 1386*(b*x + a)^{(5/2)}*a^3 + 1155*(b*x + a)^{(3/2)}*a^4 - 693*\sqrt{b*x + a}*a^5)*a^5/b^5 + 4845*(231*(b*x + a)^{(13/2)} - 1638*(b*x + a)^{(11/2)})*a + 5005*(b*x + a)^{(9/2)}*a^2 - 8580*(b*x + a)^{(7/2)}*a^3 + 9009*(b*x + a)^{(5/2)}*a^4 - 6006*(b*x + a)^{(3/2)}*a^5 + 3003*\sqrt{b*x + a}*a^6)*a^4/b^5 + 4522*(429*(b*x + a)^{(15/2)} - 3465*(b*x + a)^{(13/2)}*a + 12285*(b*x + a)^{(11/2)}*a^2 - 25025*(b*x + a)^{(9/2)}*a^3 + 32175*(b*x + a)^{(7/2)}*a^4 - 27027*(b*x + a)^{(5/2)}*a^5 + 15015*(b*x + a)^{(3/2)}*a^6 - 6435*\sqrt{b*x + a}*a^7)*a^3/b^5 + 266*(6435*(b*x + a)^{(17/2)} - 58344*(b*x + a)^{(15/2)}*a + 235620*(b*x + a)^{(13/2)}*a^2 - 556920*(b*x + a)^{(11/2)}*a^3 + 850850*(b*x + a)^{(9/2)}*a^4 - 875160*(b*x + a)^{(7/2)}*a^5 + 612612*(b*x + a)^{(5/2)}*a^6 - 291720*(b*x + a)^{(3/2)}*a^7 + 109395*\sqrt{b*x + a}*a^8)*a^2/b^5 + 63*(12155*(b*x + a)^{(19/2)} - 122265*(b*x + a)^{(17/2)}*a + 554268*(b*x + a)^{(15/2)}*a^2 - 1492260*(b*x + a)^{(13/2)}*a^3 + 2645370*(b*x + a)^{(11/2)}*a^4 - 3233230*(b*x + a)^{(9/2)}*a^5 + 2771340*(b*x + a)^{(7/2)}*a^6 - 1662804*(b*x + a)^{(5/2)}*a^7 + 692835*(b*x + a)^{(3/2)}*a^8)*a/b^5$

$$\begin{aligned} &)^{(3/2)} * a^8 - 230945 * \sqrt{b*x + a} * a^9 * a / b^5 + 3 * (46189 * (b*x + a)^{(21/2)} - \\ &510510 * (b*x + a)^{(19/2)} * a + 2567565 * (b*x + a)^{(17/2)} * a^2 - 7759752 * (b*x + \\ &a)^{(15/2)} * a^3 + 15668730 * (b*x + a)^{(13/2)} * a^4 - 22221108 * (b*x + a)^{(11/2)} * a \\ &^5 + 22632610 * (b*x + a)^{(9/2)} * a^6 - 16628040 * (b*x + a)^{(7/2)} * a^7 + 8729721 * \\ &(b*x + a)^{(5/2)} * a^8 - 3233230 * (b*x + a)^{(3/2)} * a^9 + 969969 * \sqrt{b*x + a} * a^ \\ &10) / b^5) / b \end{aligned}$$

maple [A] time = 0.01, size = 65, normalized size = 0.59

$$\frac{2(bx+a)^{\frac{11}{2}}(-46189b^5x^5+24310ab^4x^4-11440a^2b^3x^3+4576a^3b^2x^2-1408a^4bx+256a^5)}{969969b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5*(b*x+a)^(9/2),x)

[Out] -2/969969*(b*x+a)^(11/2)*(-46189*b^5*x^5+24310*a*b^4*x^4-11440*a^2*b^3*x^3+4576*a^3*b^2*x^2-1408*a^4*b*x+256*a^5)/b^6

maxima [A] time = 1.35, size = 86, normalized size = 0.78

$$\frac{2(bx+a)^{\frac{21}{2}}}{21b^6} - \frac{10(bx+a)^{\frac{19}{2}}a}{19b^6} + \frac{20(bx+a)^{\frac{17}{2}}a^2}{17b^6} - \frac{4(bx+a)^{\frac{15}{2}}a^3}{3b^6} + \frac{10(bx+a)^{\frac{13}{2}}a^4}{13b^6} - \frac{2(bx+a)^{\frac{11}{2}}a^5}{11b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^(9/2),x, algorithm="maxima")

[Out] 2/21*(b*x + a)^(21/2)/b^6 - 10/19*(b*x + a)^(19/2)*a/b^6 + 20/17*(b*x + a)^(17/2)*a^2/b^6 - 4/3*(b*x + a)^(15/2)*a^3/b^6 + 10/13*(b*x + a)^(13/2)*a^4/b^6 - 2/11*(b*x + a)^(11/2)*a^5/b^6

mupad [B] time = 0.03, size = 86, normalized size = 0.78

$$\frac{2(a+bx)^{21/2}}{21b^6} - \frac{2a^5(a+bx)^{11/2}}{11b^6} + \frac{10a^4(a+bx)^{13/2}}{13b^6} - \frac{4a^3(a+bx)^{15/2}}{3b^6} + \frac{20a^2(a+bx)^{17/2}}{17b^6} - \frac{10a(a+bx)^{19/2}}{19b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5*(a + b*x)^(9/2),x)

[Out] (2*(a + b*x)^(21/2))/(21*b^6) - (2*a^5*(a + b*x)^(11/2))/(11*b^6) + (10*a^4*(a + b*x)^(13/2))/(13*b^6) - (4*a^3*(a + b*x)^(15/2))/(3*b^6) + (20*a^2*(a + b*x)^(17/2))/(17*b^6) - (10*a*(a + b*x)^(19/2))/(19*b^6)

sympy [A] time = 28.76, size = 235, normalized size = 2.14

$$\left\{ \begin{array}{l} -\frac{512a^{10}\sqrt{a+bx}}{969969b^6} + \frac{256a^9x\sqrt{a+bx}}{969969b^5} - \frac{64a^8x^2\sqrt{a+bx}}{323323b^4} + \frac{160a^7x^3\sqrt{a+bx}}{969969b^3} - \frac{20a^6x^4\sqrt{a+bx}}{138567b^2} + \frac{6a^5x^5\sqrt{a+bx}}{46189b} + \frac{2098a^4x^6\sqrt{a+bx}}{12597} + \frac{3796a^3bx^7}{6783} \\ \frac{a^{\frac{9}{2}}x^6}{6} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5*(b*x+a)**(9/2),x)

[Out] Piecewise((-512*a**10*sqrt(a + b*x)/(969969*b**6) + 256*a**9*x*sqrt(a + b*x)/(969969*b**5) - 64*a**8*x**2*sqrt(a + b*x)/(323323*b**4) + 160*a**7*x**3*sqrt(a + b*x)/(969969*b**3) - 20*a**6*x**4*sqrt(a + b*x)/(138567*b**2) + 6*a**5*x**5*sqrt(a + b*x)/(46189*b) + 2098*a**4*x**6*sqrt(a + b*x)/12597 + 3796*a**3*b*x**7*sqrt(a + b*x)/6783 + 1640*a**2*b**2*x**8*sqrt(a + b*x)/2261 + 170*a*b**3*x**9*sqrt(a + b*x)/399 + 2*b**4*x**10*sqrt(a + b*x)/21, Ne(b, 0)), (a**(9/2)*x**6/6, True))

3.312 $\int x^4(a + bx)^{9/2} dx$

Optimal. Leaf size=91

$$\frac{2a^4(a + bx)^{11/2}}{11b^5} - \frac{8a^3(a + bx)^{13/2}}{13b^5} + \frac{4a^2(a + bx)^{15/2}}{5b^5} + \frac{2(a + bx)^{19/2}}{19b^5} - \frac{8a(a + bx)^{17/2}}{17b^5}$$

[Out] $2/11*a^4*(b*x+a)^{(11/2)}/b^5-8/13*a^3*(b*x+a)^{(13/2)}/b^5+4/5*a^2*(b*x+a)^{(15/2)}/b^5-8/17*a*(b*x+a)^{(17/2)}/b^5+2/19*(b*x+a)^{(19/2)}/b^5$

Rubi [A] time = 0.02, antiderivative size = 91, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{4a^2(a + bx)^{15/2}}{5b^5} - \frac{8a^3(a + bx)^{13/2}}{13b^5} + \frac{2a^4(a + bx)^{11/2}}{11b^5} + \frac{2(a + bx)^{19/2}}{19b^5} - \frac{8a(a + bx)^{17/2}}{17b^5}$$

Antiderivative was successfully verified.

[In] Int [x^4*(a + b*x)^(9/2), x]

[Out] $(2*a^4*(a + b*x)^{(11/2)})/(11*b^5) - (8*a^3*(a + b*x)^{(13/2)})/(13*b^5) + (4*a^2*(a + b*x)^{(15/2)})/(5*b^5) - (8*a*(a + b*x)^{(17/2)})/(17*b^5) + (2*(a + b*x)^{(19/2)})/(19*b^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^4(a + bx)^{9/2} dx &= \int \left(\frac{a^4(a + bx)^{9/2}}{b^4} - \frac{4a^3(a + bx)^{11/2}}{b^4} + \frac{6a^2(a + bx)^{13/2}}{b^4} - \frac{4a(a + bx)^{15/2}}{b^4} + \frac{(a + bx)^{17/2}}{b^4} \right) dx \\ &= \frac{2a^4(a + bx)^{11/2}}{11b^5} - \frac{8a^3(a + bx)^{13/2}}{13b^5} + \frac{4a^2(a + bx)^{15/2}}{5b^5} - \frac{8a(a + bx)^{17/2}}{17b^5} + \frac{2(a + bx)^{19/2}}{19b^5} \end{aligned}$$

Mathematica [A] time = 0.03, size = 57, normalized size = 0.63

$$\frac{2(a + bx)^{11/2} (128a^4 - 704a^3bx + 2288a^2b^2x^2 - 5720ab^3x^3 + 12155b^4x^4)}{230945b^5}$$

Antiderivative was successfully verified.

[In] Integrate[x^4*(a + b*x)^(9/2),x]

[Out] $(2*(a + b*x)^(11/2)*(128*a^4 - 704*a^3*b*x + 2288*a^2*b^2*x^2 - 5720*a*b^3*x^3 + 12155*b^4*x^4))/(230945*b^5)$

fricas [A] time = 0.52, size = 108, normalized size = 1.19

$$\frac{2(12155 b^9 x^9 + 55055 a b^8 x^8 + 95238 a^2 b^7 x^7 + 75086 a^3 b^6 x^6 + 23063 a^4 b^5 x^5 + 35 a^5 b^4 x^4 - 40 a^6 b^3 x^3 + 48 a^7 b^2 x^2 - 64 a^8 b x + 128 a^9) \sqrt{b x + a}}{230945 b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^(9/2),x, algorithm="fricas")

[Out] $2/230945*(12155*b^9*x^9 + 55055*a*b^8*x^8 + 95238*a^2*b^7*x^7 + 75086*a^3*b^6*x^6 + 23063*a^4*b^5*x^5 + 35*a^5*b^4*x^4 - 40*a^6*b^3*x^3 + 48*a^7*b^2*x^2 - 64*a^8*b*x + 128*a^9)*\sqrt{b*x + a}/b^5$

giac [B] time = 1.12, size = 565, normalized size = 6.21

$$2 \left(\frac{46189 \left(35 (b x + a)^{\frac{9}{2}} - 180 (b x + a)^{\frac{7}{2}} a + 378 (b x + a)^{\frac{5}{2}} a^2 - 420 (b x + a)^{\frac{3}{2}} a^3 + 315 \sqrt{b x + a} a^4 \right) a^5}{b^4} + \frac{104975 \left(63 (b x + a)^{\frac{11}{2}} - 385 (b x + a)^{\frac{9}{2}} a + 990 (b x + a)^{\frac{7}{2}} a^2 - 1386 (b x + a)^{\frac{5}{2}} a^3 + 1155 (b x + a)^{\frac{3}{2}} a^4 - 693 \sqrt{b x + a} a^5 \right) a^4}{b^4} + 48450 \left(231 (b x + a)^{\frac{13}{2}} - 1638 (b x + a)^{\frac{11}{2}} a + 5005 (b x + a)^{\frac{9}{2}} a^2 - 8580 (b x + a)^{\frac{7}{2}} a^3 + 9009 (b x + a)^{\frac{5}{2}} a^4 - 6006 (b x + a)^{\frac{3}{2}} a^5 + 3003 \sqrt{b x + a} a^6 \right) a^3}{b^4} + 22610 \left(429 (b x + a)^{\frac{15}{2}} - 3465 (b x + a)^{\frac{13}{2}} a + 12285 (b x + a)^{\frac{11}{2}} a^2 - 25025 (b x + a)^{\frac{9}{2}} a^3 + 32175 (b x + a)^{\frac{7}{2}} a^4 - 27027 (b x + a)^{\frac{5}{2}} a^5 + 15015 (b x + a)^{\frac{3}{2}} a^6 - 6435 \sqrt{b x + a} a^7 \right) a^2}{b^4} + 665 \left(6435 (b x + a)^{\frac{17}{2}} - 58344 (b x + a)^{\frac{15}{2}} a + 235620 (b x + a)^{\frac{13}{2}} a^2 - 556920 (b x + a)^{\frac{11}{2}} a^3 + 850850 (b x + a)^{\frac{9}{2}} a^4 - 875160 (b x + a)^{\frac{7}{2}} a^5 + 612612 (b x + a)^{\frac{5}{2}} a^6 - 291720 (b x + a)^{\frac{3}{2}} a^7 + 109395 \sqrt{b x + a} a^8 \right) a}{b^4} + 63 \left(12155 (b x + a)^{\frac{19}{2}} - 122265 (b x + a)^{\frac{17}{2}} a + 554268 (b x + a)^{\frac{15}{2}} a^2 - 1492260 (b x + a)^{\frac{13}{2}} a^3 \right) a^5 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^(9/2),x, algorithm="giac")

[Out] $2/14549535*(46189*(35*(b*x + a)^(9/2) - 180*(b*x + a)^(7/2)*a + 378*(b*x + a)^(5/2)*a^2 - 420*(b*x + a)^(3/2)*a^3 + 315*\sqrt{b*x + a}*a^4)*a^5/b^4 + 104975*(63*(b*x + a)^(11/2) - 385*(b*x + a)^(9/2)*a + 990*(b*x + a)^(7/2)*a^2 - 1386*(b*x + a)^(5/2)*a^3 + 1155*(b*x + a)^(3/2)*a^4 - 693*\sqrt{b*x + a}*a^5)*a^4/b^4 + 48450*(231*(b*x + a)^(13/2) - 1638*(b*x + a)^(11/2)*a + 5005*(b*x + a)^(9/2)*a^2 - 8580*(b*x + a)^(7/2)*a^3 + 9009*(b*x + a)^(5/2)*a^4 - 6006*(b*x + a)^(3/2)*a^5 + 3003*\sqrt{b*x + a}*a^6)*a^3/b^4 + 22610*(429*(b*x + a)^(15/2) - 3465*(b*x + a)^(13/2)*a + 12285*(b*x + a)^(11/2)*a^2 - 25025*(b*x + a)^(9/2)*a^3 + 32175*(b*x + a)^(7/2)*a^4 - 27027*(b*x + a)^(5/2)*a^5 + 15015*(b*x + a)^(3/2)*a^6 - 6435*\sqrt{b*x + a}*a^7)*a^2/b^4 + 665*(6435*(b*x + a)^(17/2) - 58344*(b*x + a)^(15/2)*a + 235620*(b*x + a)^(13/2)*a^2 - 556920*(b*x + a)^(11/2)*a^3 + 850850*(b*x + a)^(9/2)*a^4 - 875160*(b*x + a)^(7/2)*a^5 + 612612*(b*x + a)^(5/2)*a^6 - 291720*(b*x + a)^(3/2)*a^7 + 109395*\sqrt{b*x + a}*a^8)*a/b^4 + 63*(12155*(b*x + a)^(19/2) - 122265*(b*x + a)^(17/2)*a + 554268*(b*x + a)^(15/2)*a^2 - 1492260*(b*x + a)^(13/2)*a^3)$

$$3 + 2645370*(b*x + a)^{(11/2)}*a^4 - 3233230*(b*x + a)^{(9/2)}*a^5 + 2771340*(b*x + a)^{(7/2)}*a^6 - 1662804*(b*x + a)^{(5/2)}*a^7 + 692835*(b*x + a)^{(3/2)}*a^8 - 230945*\sqrt{b*x + a}*a^9/b^4)/b$$

maple [A] time = 0.01, size = 54, normalized size = 0.59

$$\frac{2(bx + a)^{\frac{11}{2}} (12155x^4b^4 - 5720ax^3b^3 + 2288a^2x^2b^2 - 704a^3xb + 128a^4)}{230945b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*(b*x+a)^(9/2), x)

[Out] 2/230945*(b*x+a)^(11/2)*(12155*b^4*x^4-5720*a*b^3*x^3+2288*a^2*b^2*x^2-704*a^3*b*x+128*a^4)/b^5

maxima [A] time = 1.36, size = 71, normalized size = 0.78

$$\frac{2(bx + a)^{\frac{19}{2}}}{19b^5} - \frac{8(bx + a)^{\frac{17}{2}}a}{17b^5} + \frac{4(bx + a)^{\frac{15}{2}}a^2}{5b^5} - \frac{8(bx + a)^{\frac{13}{2}}a^3}{13b^5} + \frac{2(bx + a)^{\frac{11}{2}}a^4}{11b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^(9/2), x, algorithm="maxima")

[Out] 2/19*(b*x + a)^(19/2)/b^5 - 8/17*(b*x + a)^(17/2)*a/b^5 + 4/5*(b*x + a)^(15/2)*a^2/b^5 - 8/13*(b*x + a)^(13/2)*a^3/b^5 + 2/11*(b*x + a)^(11/2)*a^4/b^5

mupad [B] time = 0.02, size = 71, normalized size = 0.78

$$\frac{2(a + bx)^{19/2}}{19b^5} + \frac{2a^4(a + bx)^{11/2}}{11b^5} - \frac{8a^3(a + bx)^{13/2}}{13b^5} + \frac{4a^2(a + bx)^{15/2}}{5b^5} - \frac{8a(a + bx)^{17/2}}{17b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*(a + b*x)^(9/2), x)

[Out] (2*(a + b*x)^(19/2))/(19*b^5) + (2*a^4*(a + b*x)^(11/2))/(11*b^5) - (8*a^3*(a + b*x)^(13/2))/(13*b^5) + (4*a^2*(a + b*x)^(15/2))/(5*b^5) - (8*a*(a + b*x)^(17/2))/(17*b^5)

sympy [A] time = 25.70, size = 212, normalized size = 2.33

$$\left\{ \begin{array}{l} \frac{256a^9\sqrt{a+bx}}{230945b^5} - \frac{128a^8x\sqrt{a+bx}}{230945b^4} + \frac{96a^7x^2\sqrt{a+bx}}{230945b^3} - \frac{16a^6x^3\sqrt{a+bx}}{46189b^2} + \frac{14a^5x^4\sqrt{a+bx}}{46189b} + \frac{46126a^4x^5\sqrt{a+bx}}{230945} + \frac{13652a^3bx^6\sqrt{a+bx}}{20995} + \frac{1332a^2b^2x^7\sqrt{a+bx}}{104975} \\ \frac{9}{5}a^2x^5 \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*(b*x+a)**(9/2),x)
```

```
[Out] Piecewise((256*a**9*sqrt(a + b*x)/(230945*b**5) - 128*a**8*x*sqrt(a + b*x)/
(230945*b**4) + 96*a**7*x**2*sqrt(a + b*x)/(230945*b**3) - 16*a**6*x**3*sqrt
(a + b*x)/(46189*b**2) + 14*a**5*x**4*sqrt(a + b*x)/(46189*b) + 46126*a**4
*x**5*sqrt(a + b*x)/230945 + 13652*a**3*b*x**6*sqrt(a + b*x)/20995 + 1332*a
**2*b**2*x**7*sqrt(a + b*x)/1615 + 154*a*b**3*x**8*sqrt(a + b*x)/323 + 2*b*
*4*x**9*sqrt(a + b*x)/19, Ne(b, 0)), (a**(9/2)*x**5/5, True))
```

3.313 $\int x^3(a + bx)^{9/2} dx$

Optimal. Leaf size=72

$$-\frac{2a^3(a + bx)^{11/2}}{11b^4} + \frac{6a^2(a + bx)^{13/2}}{13b^4} + \frac{2(a + bx)^{17/2}}{17b^4} - \frac{2a(a + bx)^{15/2}}{5b^4}$$

[Out] $-2/11*a^3*(b*x+a)^{(11/2)}/b^4+6/13*a^2*(b*x+a)^{(13/2)}/b^4-2/5*a*(b*x+a)^{(15/2)}/b^4+2/17*(b*x+a)^{(17/2)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{6a^2(a + bx)^{13/2}}{13b^4} - \frac{2a^3(a + bx)^{11/2}}{11b^4} + \frac{2(a + bx)^{17/2}}{17b^4} - \frac{2a(a + bx)^{15/2}}{5b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^(9/2), x]

[Out] $(-2*a^3*(a + b*x)^{(11/2)})/(11*b^4) + (6*a^2*(a + b*x)^{(13/2)})/(13*b^4) - (2*a*(a + b*x)^{(15/2)})/(5*b^4) + (2*(a + b*x)^{(17/2)})/(17*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^{9/2} dx &= \int \left(-\frac{a^3(a + bx)^{9/2}}{b^3} + \frac{3a^2(a + bx)^{11/2}}{b^3} - \frac{3a(a + bx)^{13/2}}{b^3} + \frac{(a + bx)^{15/2}}{b^3} \right) dx \\ &= -\frac{2a^3(a + bx)^{11/2}}{11b^4} + \frac{6a^2(a + bx)^{13/2}}{13b^4} - \frac{2a(a + bx)^{15/2}}{5b^4} + \frac{2(a + bx)^{17/2}}{17b^4} \end{aligned}$$

Mathematica [A] time = 0.03, size = 46, normalized size = 0.64

$$\frac{2(a + bx)^{11/2} (-16a^3 + 88a^2bx - 286ab^2x^2 + 715b^3x^3)}{12155b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^(9/2),x]

[Out] (2*(a + b*x)^(11/2)*(-16*a^3 + 88*a^2*b*x - 286*a*b^2*x^2 + 715*b^3*x^3))/(12155*b^4)

fricas [A] time = 0.46, size = 97, normalized size = 1.35

$$\frac{2(715b^8x^8 + 3289ab^7x^7 + 5808a^2b^6x^6 + 4714a^3b^5x^5 + 1515a^4b^4x^4 + 5a^5b^3x^3 - 6a^6b^2x^2 + 8a^7bx - 16a^8)\sqrt{b}}{12155b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(9/2),x, algorithm="fricas")

[Out] 2/12155*(715*b^8*x^8 + 3289*a*b^7*x^7 + 5808*a^2*b^6*x^6 + 4714*a^3*b^5*x^5 + 1515*a^4*b^4*x^4 + 5*a^5*b^3*x^3 - 6*a^6*b^2*x^2 + 8*a^7*b*x - 16*a^8)*sqrt(b*x + a)/b^4

giac [B] time = 1.10, size = 493, normalized size = 6.85

$$2 \left(\frac{21879 \left(5(bx+a)^{\frac{7}{2}} - 21(bx+a)^{\frac{5}{2}}a + 35(bx+a)^{\frac{3}{2}}a^2 - 35\sqrt{bx+a}a^3 \right) a^5}{b^3} + \frac{12155 \left(35(bx+a)^{\frac{9}{2}} - 180(bx+a)^{\frac{7}{2}}a + 378(bx+a)^{\frac{5}{2}}a^2 - 420(bx+a)^{\frac{3}{2}}a^3 + 315\sqrt{bx+a}a^4 \right)}{b^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(9/2),x, algorithm="giac")

[Out] 2/765765*(21879*(5*(b*x + a)^(7/2) - 21*(b*x + a)^(5/2)*a + 35*(b*x + a)^(3/2)*a^2 - 35*sqrt(b*x + a)*a^3)*a^5/b^3 + 12155*(35*(b*x + a)^(9/2) - 180*(b*x + a)^(7/2)*a + 378*(b*x + a)^(5/2)*a^2 - 420*(b*x + a)^(3/2)*a^3 + 315*sqrt(b*x + a)*a^4)*a^4/b^3 + 11050*(63*(b*x + a)^(11/2) - 385*(b*x + a)^(9/2)*a + 990*(b*x + a)^(7/2)*a^2 - 1386*(b*x + a)^(5/2)*a^3 + 1155*(b*x + a)^(3/2)*a^4 - 693*sqrt(b*x + a)*a^5)*a^3/b^3 + 2550*(231*(b*x + a)^(13/2) - 1638*(b*x + a)^(11/2)*a + 5005*(b*x + a)^(9/2)*a^2 - 8580*(b*x + a)^(7/2)*a^3 + 9009*(b*x + a)^(5/2)*a^4 - 6006*(b*x + a)^(3/2)*a^5 + 3003*sqrt(b*x + a)*a^6)*a^2/b^3 + 595*(429*(b*x + a)^(15/2) - 3465*(b*x + a)^(13/2)*a + 12285*(b*x + a)^(11/2)*a^2 - 25025*(b*x + a)^(9/2)*a^3 + 32175*(b*x + a)^(7/2)*a^4 - 27027*(b*x + a)^(5/2)*a^5 + 15015*(b*x + a)^(3/2)*a^6 - 6435*sqrt(b*x + a)*a^7)*a/b^3 + 7*(6435*(b*x + a)^(17/2) - 58344*(b*x + a)^(15/2)*a + 235620*(b*x + a)^(13/2)*a^2 - 556920*(b*x + a)^(11/2)*a^3 + 850850*(b*x + a)^(9/2)*a^4 - 875160*(b*x + a)^(7/2)*a^5 + 612612*(b*x + a)^(5/2)*a^6 - 291720*(b*x + a)^(3/2)*a^7 + 109395*sqrt(b*x + a)*a^8)/b^3)/b

maple [A] time = 0.01, size = 43, normalized size = 0.60

$$\frac{2(bx + a)^{\frac{11}{2}} \left(-715b^3x^3 + 286ab^2x^2 - 88a^2bx + 16a^3 \right)}{12155b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(b*x+a)^(9/2),x)`

[Out] $-2/12155*(b*x+a)^{(11/2)}*(-715*b^3*x^3+286*a*b^2*x^2-88*a^2*b*x+16*a^3)/b^4$

maxima [A] time = 1.29, size = 56, normalized size = 0.78

$$\frac{2(bx + a)^{\frac{17}{2}}}{17b^4} - \frac{2(bx + a)^{\frac{15}{2}}a}{5b^4} + \frac{6(bx + a)^{\frac{13}{2}}a^2}{13b^4} - \frac{2(bx + a)^{\frac{11}{2}}a^3}{11b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(b*x+a)^(9/2),x, algorithm="maxima")`

[Out] $2/17*(b*x + a)^{(17/2)}/b^4 - 2/5*(b*x + a)^{(15/2)}*a/b^4 + 6/13*(b*x + a)^{(13/2)}*a^2/b^4 - 2/11*(b*x + a)^{(11/2)}*a^3/b^4$

mupad [B] time = 0.04, size = 56, normalized size = 0.78

$$\frac{2(a + bx)^{17/2}}{17b^4} - \frac{2a^3(a + bx)^{11/2}}{11b^4} + \frac{6a^2(a + bx)^{13/2}}{13b^4} - \frac{2a(a + bx)^{15/2}}{5b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(a + b*x)^(9/2),x)`

[Out] $(2*(a + b*x)^{(17/2)})/(17*b^4) - (2*a^3*(a + b*x)^{(11/2)})/(11*b^4) + (6*a^2*(a + b*x)^{(13/2)})/(13*b^4) - (2*a*(a + b*x)^{(15/2)})/(5*b^4)$

sympy [A] time = 20.35, size = 190, normalized size = 2.64

$$\left\{ \begin{array}{l} -\frac{32a^8\sqrt{a+bx}}{12155b^4} + \frac{16a^7x\sqrt{a+bx}}{12155b^3} - \frac{12a^6x^2\sqrt{a+bx}}{12155b^2} + \frac{2a^5x^3\sqrt{a+bx}}{2431b} + \frac{606a^4x^4\sqrt{a+bx}}{2431} + \frac{9428a^3bx^5\sqrt{a+bx}}{12155} + \frac{1056a^2b^2x^6\sqrt{a+bx}}{1105} + \frac{46ab^3x^7\sqrt{a+bx}}{85} \\ \frac{9}{4}a^2x^4 \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(b*x+a)**(9/2),x)`

```
[Out] Piecewise((-32*a**8*sqrt(a + b*x)/(12155*b**4) + 16*a**7*x*sqrt(a + b*x)/(12155*b**3) - 12*a**6*x**2*sqrt(a + b*x)/(12155*b**2) + 2*a**5*x**3*sqrt(a + b*x)/(2431*b) + 606*a**4*x**4*sqrt(a + b*x)/2431 + 9428*a**3*b*x**5*sqrt(a + b*x)/12155 + 1056*a**2*b**2*x**6*sqrt(a + b*x)/1105 + 46*a*b**3*x**7*sqrt(a + b*x)/85 + 2*b**4*x**8*sqrt(a + b*x)/17, Ne(b, 0)), (a**(9/2)*x**4/4, True))
```

3.314 $\int x^2(a + bx)^{9/2} dx$

Optimal. Leaf size=53

$$\frac{2a^2(a + bx)^{11/2}}{11b^3} + \frac{2(a + bx)^{15/2}}{15b^3} - \frac{4a(a + bx)^{13/2}}{13b^3}$$

[Out] $2/11*a^2*(b*x+a)^{(11/2)}/b^3-4/13*a*(b*x+a)^{(13/2)}/b^3+2/15*(b*x+a)^{(15/2)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2a^2(a + bx)^{11/2}}{11b^3} + \frac{2(a + bx)^{15/2}}{15b^3} - \frac{4a(a + bx)^{13/2}}{13b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*x)^(9/2), x]

[Out] $(2*a^2*(a + b*x)^{(11/2)})/(11*b^3) - (4*a*(a + b*x)^{(13/2)})/(13*b^3) + (2*(a + b*x)^{(15/2)})/(15*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^{9/2} dx &= \int \left(\frac{a^2(a + bx)^{9/2}}{b^2} - \frac{2a(a + bx)^{11/2}}{b^2} + \frac{(a + bx)^{13/2}}{b^2} \right) dx \\ &= \frac{2a^2(a + bx)^{11/2}}{11b^3} - \frac{4a(a + bx)^{13/2}}{13b^3} + \frac{2(a + bx)^{15/2}}{15b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.66

$$\frac{2(a + bx)^{11/2} (8a^2 - 44abx + 143b^2x^2)}{2145b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^(9/2),x]

[Out] (2*(a + b*x)^(11/2)*(8*a^2 - 44*a*b*x + 143*b^2*x^2))/(2145*b^3)

fricas [B] time = 0.46, size = 86, normalized size = 1.62

$$\frac{2 \left(143 b^7 x^7 + 671 a b^6 x^6 + 1218 a^2 b^5 x^5 + 1030 a^3 b^4 x^4 + 355 a^4 b^3 x^3 + 3 a^5 b^2 x^2 - 4 a^6 b x + 8 a^7 \right) \sqrt{b x + a}}{2145 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(9/2),x, algorithm="fricas")

[Out] 2/2145*(143*b^7*x^7 + 671*a*b^6*x^6 + 1218*a^2*b^5*x^5 + 1030*a^3*b^4*x^4 + 355*a^4*b^3*x^3 + 3*a^5*b^2*x^2 - 4*a^6*b*x + 8*a^7)*sqrt(b*x + a)/b^3

giac [B] time = 1.06, size = 421, normalized size = 7.94

$$2 \left(\frac{3003 \left(3 (b x + a)^{\frac{5}{2}} - 10 (b x + a)^{\frac{3}{2}} a + 15 \sqrt{b x + a} a^2 \right) a^5}{b^2} + \frac{6435 \left(5 (b x + a)^{\frac{7}{2}} - 21 (b x + a)^{\frac{5}{2}} a + 35 (b x + a)^{\frac{3}{2}} a^2 - 35 \sqrt{b x + a} a^3 \right) a^4}{b^2} + \frac{1430 \left(35 (b x + a)^{\frac{9}{2}} - 180 (b x + a)^{\frac{7}{2}} a + 378 (b x + a)^{\frac{5}{2}} a^2 - 420 (b x + a)^{\frac{3}{2}} a^3 + 315 \sqrt{b x + a} a^4 \right) a^3}{b^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(9/2),x, algorithm="giac")

[Out] 2/45045*(3003*(3*(b*x + a)^(5/2) - 10*(b*x + a)^(3/2)*a + 15*sqrt(b*x + a)*a^2)*a^5/b^2 + 6435*(5*(b*x + a)^(7/2) - 21*(b*x + a)^(5/2)*a + 35*(b*x + a)^(3/2)*a^2 - 35*sqrt(b*x + a)*a^3)*a^4/b^2 + 1430*(35*(b*x + a)^(9/2) - 180*(b*x + a)^(7/2)*a + 378*(b*x + a)^(5/2)*a^2 - 420*(b*x + a)^(3/2)*a^3 + 315*sqrt(b*x + a)*a^4)*a^3/b^2 + 650*(63*(b*x + a)^(11/2) - 385*(b*x + a)^(9/2)*a + 990*(b*x + a)^(7/2)*a^2 - 1386*(b*x + a)^(5/2)*a^3 + 1155*(b*x + a)^(3/2)*a^4 - 693*sqrt(b*x + a)*a^5)*a^2/b^2 + 75*(231*(b*x + a)^(13/2) - 1638*(b*x + a)^(11/2)*a + 5005*(b*x + a)^(9/2)*a^2 - 8580*(b*x + a)^(7/2)*a^3 + 9009*(b*x + a)^(5/2)*a^4 - 6006*(b*x + a)^(3/2)*a^5 + 3003*sqrt(b*x + a)*a^6)*a/b^2 + 7*(429*(b*x + a)^(15/2) - 3465*(b*x + a)^(13/2)*a + 12285*(b*x + a)^(11/2)*a^2 - 25025*(b*x + a)^(9/2)*a^3 + 32175*(b*x + a)^(7/2)*a^4 - 27027*(b*x + a)^(5/2)*a^5 + 15015*(b*x + a)^(3/2)*a^6 - 6435*sqrt(b*x + a)*a^7)/b^2)/b

maple [A] time = 0.00, size = 32, normalized size = 0.60

$$\frac{2 (b x + a)^{\frac{11}{2}} (143 b^2 x^2 - 44 a b x + 8 a^2)}{2145 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(b*x+a)^(9/2),x)`

[Out] $2/2145*(b*x+a)^{(11/2)}*(143*b^2*x^2-44*a*b*x+8*a^2)/b^3$

maxima [A] time = 1.34, size = 41, normalized size = 0.77

$$\frac{2(bx+a)^{\frac{15}{2}}}{15b^3} - \frac{4(bx+a)^{\frac{13}{2}}a}{13b^3} + \frac{2(bx+a)^{\frac{11}{2}}a^2}{11b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(b*x+a)^(9/2),x, algorithm="maxima")`

[Out] $2/15*(b*x+a)^{(15/2)}/b^3 - 4/13*(b*x+a)^{(13/2)}*a/b^3 + 2/11*(b*x+a)^{(11/2)}*a^2/b^3$

mupad [B] time = 0.04, size = 36, normalized size = 0.68

$$\frac{\frac{2(a+bx)^{15/2}}{15} - \frac{4a(a+bx)^{13/2}}{13} + \frac{2a^2(a+bx)^{11/2}}{11}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(a+b*x)^(9/2),x)`

[Out] $((2*(a+b*x)^{(15/2)})/15 - (4*a*(a+b*x)^{(13/2)})/13 + (2*a^2*(a+b*x)^{(11/2)})/11)/b^3$

sympy [A] time = 16.86, size = 168, normalized size = 3.17

$$\left\{ \begin{array}{l} \frac{16a^7\sqrt{a+bx}}{2145b^3} - \frac{8a^6x\sqrt{a+bx}}{2145b^2} + \frac{2a^5x^2\sqrt{a+bx}}{715b} + \frac{142a^4x^3\sqrt{a+bx}}{429} + \frac{412a^3bx^4\sqrt{a+bx}}{429} + \frac{812a^2b^2x^5\sqrt{a+bx}}{715} + \frac{122ab^3x^6\sqrt{a+bx}}{195} + \frac{2b^4x^7\sqrt{a+bx}}{15} \\ \frac{9}{3} \\ \frac{a^2x^3}{3} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(b*x+a)**(9/2),x)`

[Out] `Piecewise((16*a**7*sqrt(a+b*x)/(2145*b**3) - 8*a**6*x*sqrt(a+b*x)/(2145*b**2) + 2*a**5*x**2*sqrt(a+b*x)/(715*b) + 142*a**4*x**3*sqrt(a+b*x)/429 + 412*a**3*b*x**4*sqrt(a+b*x)/429 + 812*a**2*b**2*x**5*sqrt(a+b*x)/715 + 122*a*b**3*x**6*sqrt(a+b*x)/195 + 2*b**4*x**7*sqrt(a+b*x)/15, Ne(b, 0)), (a**(9/2)*x**3/3, True))`

3.315 $\int x(a + bx)^{9/2} dx$

Optimal. Leaf size=34

$$\frac{2(a + bx)^{13/2}}{13b^2} - \frac{2a(a + bx)^{11/2}}{11b^2}$$

[Out] $-2/11*a*(b*x+a)^{(11/2)}/b^2+2/13*(b*x+a)^{(13/2)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{2(a + bx)^{13/2}}{13b^2} - \frac{2a(a + bx)^{11/2}}{11b^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^(9/2), x]

[Out] $(-2*a*(a + b*x)^{(11/2)})/(11*b^2) + (2*(a + b*x)^{(13/2)})/(13*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x(a + bx)^{9/2} dx &= \int \left(-\frac{a(a + bx)^{9/2}}{b} + \frac{(a + bx)^{11/2}}{b} \right) dx \\ &= -\frac{2a(a + bx)^{11/2}}{11b^2} + \frac{2(a + bx)^{13/2}}{13b^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 24, normalized size = 0.71

$$\frac{2(a + bx)^{11/2}(11bx - 2a)}{143b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^(9/2), x]

[Out] $(2*(a + b*x)^{(11/2)*(-2*a + 11*b*x))/(143*b^2)$

fricas [B] time = 0.47, size = 74, normalized size = 2.18

$$\frac{2(11b^6x^6 + 53ab^5x^5 + 100a^2b^4x^4 + 90a^3b^3x^3 + 35a^4b^2x^2 + a^5bx - 2a^6)\sqrt{bx+a}}{143b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(9/2),x, algorithm="fricas")`

[Out] $2/143*(11*b^6*x^6 + 53*a*b^5*x^5 + 100*a^2*b^4*x^4 + 90*a^3*b^3*x^3 + 35*a^4*b^2*x^2 + a^5*b*x - 2*a^6)*\text{sqrt}(b*x + a)/b^2$

giac [B] time = 1.27, size = 347, normalized size = 10.21

$$2 \left(\frac{3003 \left((bx+a)^{\frac{3}{2}} - 3\sqrt{bx+a} \right) a^5}{b} + \frac{3003 \left(3(bx+a)^{\frac{5}{2}} - 10(bx+a)^{\frac{3}{2}}a + 15\sqrt{bx+a}a^2 \right) a^4}{b} + \frac{2574 \left(5(bx+a)^{\frac{7}{2}} - 21(bx+a)^{\frac{5}{2}}a + 35(bx+a)^{\frac{3}{2}}a^2 - 35\sqrt{bx+a}a^3 \right)}{b} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(9/2),x, algorithm="giac")`

[Out] $2/9009*(3003*((b*x + a)^{(3/2)} - 3*\text{sqrt}(b*x + a)*a)*a^5/b + 3003*(3*(b*x + a)^{(5/2)} - 10*(b*x + a)^{(3/2)}*a + 15*\text{sqrt}(b*x + a)*a^2)*a^4/b + 2574*(5*(b*x + a)^{(7/2)} - 21*(b*x + a)^{(5/2)}*a + 35*(b*x + a)^{(3/2)}*a^2 - 35*\text{sqrt}(b*x + a)*a^3)*a^3/b + 286*(35*(b*x + a)^{(9/2)} - 180*(b*x + a)^{(7/2)}*a + 378*(b*x + a)^{(5/2)}*a^2 - 420*(b*x + a)^{(3/2)}*a^3 + 315*\text{sqrt}(b*x + a)*a^4)*a^2/b + 65*(63*(b*x + a)^{(11/2)} - 385*(b*x + a)^{(9/2)}*a + 990*(b*x + a)^{(7/2)}*a^2 - 1386*(b*x + a)^{(5/2)}*a^3 + 1155*(b*x + a)^{(3/2)}*a^4 - 693*\text{sqrt}(b*x + a)*a^5)*a/b + 3*(231*(b*x + a)^{(13/2)} - 1638*(b*x + a)^{(11/2)}*a + 5005*(b*x + a)^{(9/2)}*a^2 - 8580*(b*x + a)^{(7/2)}*a^3 + 9009*(b*x + a)^{(5/2)}*a^4 - 6006*(b*x + a)^{(3/2)}*a^5 + 3003*\text{sqrt}(b*x + a)*a^6)/b/b$

maple [A] time = 0.00, size = 21, normalized size = 0.62

$$\frac{2(bx+a)^{\frac{11}{2}}(-11bx+2a)}{143b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)^(9/2),x)`

[Out] $-2/143*(b*x+a)^{(11/2)*(-11*b*x+2*a)/b^2$

maxima [A] time = 1.36, size = 26, normalized size = 0.76

$$\frac{2 (bx + a)^{\frac{13}{2}}}{13 b^2} - \frac{2 (bx + a)^{\frac{11}{2}} a}{11 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^(9/2),x, algorithm="maxima")

[Out] 2/13*(b*x + a)^(13/2)/b^2 - 2/11*(b*x + a)^(11/2)*a/b^2

mupad [B] time = 0.03, size = 25, normalized size = 0.74

$$\frac{26 a (a + b x)^{11/2} - 22 (a + b x)^{13/2}}{143 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a + b*x)^(9/2),x)

[Out] -(26*a*(a + b*x)^(11/2) - 22*(a + b*x)^(13/2))/(143*b^2)

sympy [A] time = 14.85, size = 146, normalized size = 4.29

$$\begin{cases} -\frac{4a^6\sqrt{a+bx}}{143b^2} + \frac{2a^5x\sqrt{a+bx}}{143b} + \frac{70a^4x^2\sqrt{a+bx}}{143} + \frac{180a^3bx^3\sqrt{a+bx}}{143} + \frac{200a^2b^2x^4\sqrt{a+bx}}{143} + \frac{106ab^3x^5\sqrt{a+bx}}{143} + \frac{2b^4x^6\sqrt{a+bx}}{13} & \text{for } b \neq 0 \\ \frac{9}{2}a^2x^2 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)**(9/2),x)

[Out] Piecewise((-4*a**6*sqrt(a + b*x)/(143*b**2) + 2*a**5*x*sqrt(a + b*x)/(143*b) + 70*a**4*x**2*sqrt(a + b*x)/143 + 180*a**3*b*x**3*sqrt(a + b*x)/143 + 200*a**2*b**2*x**4*sqrt(a + b*x)/143 + 106*a*b**3*x**5*sqrt(a + b*x)/143 + 2*b**4*x**6*sqrt(a + b*x)/13, Ne(b, 0)), (a**(9/2)*x**2/2, True))

3.316 $\int (a + bx)^{9/2} dx$

Optimal. Leaf size=16

$$\frac{2(a + bx)^{11/2}}{11b}$$

[Out] 2/11*(b*x+a)^(11/2)/b

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{2(a + bx)^{11/2}}{11b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(9/2), x]

[Out] (2*(a + b*x)^(11/2))/(11*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^{9/2} dx = \frac{2(a + bx)^{11/2}}{11b}$$

Mathematica [A] time = 0.01, size = 16, normalized size = 1.00

$$\frac{2(a + bx)^{11/2}}{11b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(9/2), x]

[Out] (2*(a + b*x)^(11/2))/(11*b)

fricas [B] time = 0.47, size = 61, normalized size = 3.81

$$\frac{2(b^5x^5 + 5ab^4x^4 + 10a^2b^3x^3 + 10a^3b^2x^2 + 5a^4bx + a^5)\sqrt{bx + a}}{11b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2),x, algorithm="fricas")

[Out] $2/11*(b^5*x^5 + 5*a*b^4*x^4 + 10*a^2*b^3*x^3 + 10*a^3*b^2*x^2 + 5*a^4*b*x + a^5)*\text{sqrt}(b*x + a)/b$

giac [B] time = 0.99, size = 229, normalized size = 14.31

$$2 \left(63 (bx + a)^{\frac{11}{2}} - 385 (bx + a)^{\frac{9}{2}} a + 990 (bx + a)^{\frac{7}{2}} a^2 - 1386 (bx + a)^{\frac{5}{2}} a^3 + 1155 (bx + a)^{\frac{3}{2}} a^4 + 1155 \left((bx + a)^{\frac{3}{2}} - \right. \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2),x, algorithm="giac")

[Out] $2/693*(63*(b*x + a)^{(11/2)} - 385*(b*x + a)^{(9/2)}*a + 990*(b*x + a)^{(7/2)}*a^2 - 1386*(b*x + a)^{(5/2)}*a^3 + 1155*(b*x + a)^{(3/2)}*a^4 + 1155*((b*x + a)^{(3/2)} - 3*\text{sqrt}(b*x + a)*a)*a^4 + 462*(3*(b*x + a)^{(5/2)} - 10*(b*x + a)^{(3/2)})*a + 15*\text{sqrt}(b*x + a)*a^2)*a^3 + 198*(5*(b*x + a)^{(7/2)} - 21*(b*x + a)^{(5/2)})*a + 35*(b*x + a)^{(3/2)}*a^2 - 35*\text{sqrt}(b*x + a)*a^3)*a^2 + 11*(35*(b*x + a)^{(9/2)} - 180*(b*x + a)^{(7/2)}*a + 378*(b*x + a)^{(5/2)}*a^2 - 420*(b*x + a)^{(3/2)}*a^3 + 315*\text{sqrt}(b*x + a)*a^4)*a)/b$

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{2 (bx + a)^{\frac{11}{2}}}{11b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(9/2),x)

[Out] $2/11*(b*x+a)^{(11/2)}/b$

maxima [A] time = 1.34, size = 12, normalized size = 0.75

$$\frac{2 (bx + a)^{\frac{11}{2}}}{11b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2),x, algorithm="maxima")

[Out] $2/11*(b*x + a)^{(11/2)}/b$

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{2(a + bx)^{11/2}}{11b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(9/2), x)`

[Out] `(2*(a + b*x)^(11/2))/(11*b)`

sympy [A] time = 0.08, size = 12, normalized size = 0.75

$$\frac{2(a + bx)^{\frac{11}{2}}}{11b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(9/2), x)`

[Out] `2*(a + b*x)**(11/2)/(11*b)`

$$3.317 \quad \int \frac{(a+bx)^{9/2}}{x} dx$$

Optimal. Leaf size=97

$$-2a^{9/2} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + 2a^4\sqrt{a+bx} + \frac{2}{3}a^3(a+bx)^{3/2} + \frac{2}{5}a^2(a+bx)^{5/2} + \frac{2}{7}a(a+bx)^{7/2} + \frac{2}{9}(a+bx)^{9/2}$$

[Out] $2/3*a^3*(b*x+a)^{(3/2)}+2/5*a^2*(b*x+a)^{(5/2)}+2/7*a*(b*x+a)^{(7/2)}+2/9*(b*x+a)^{(9/2)}-2*a^{(9/2)}*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})+2*a^4*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 97, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {50, 63, 208}

$$2a^4\sqrt{a+bx} + \frac{2}{3}a^3(a+bx)^{3/2} + \frac{2}{5}a^2(a+bx)^{5/2} - 2a^{9/2} \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + \frac{2}{7}a(a+bx)^{7/2} + \frac{2}{9}(a+bx)^{9/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(9/2)/x, x]

[Out] $2*a^4*\operatorname{Sqrt}[a + b*x] + (2*a^3*(a + b*x)^{(3/2)})/3 + (2*a^2*(a + b*x)^{(5/2)})/5 + (2*a*(a + b*x)^{(7/2)})/7 + (2*(a + b*x)^{(9/2)})/9 - 2*a^{(9/2)}*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]]$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{9/2}}{x} dx &= \frac{2}{9}(a+bx)^{9/2} + a \int \frac{(a+bx)^{7/2}}{x} dx \\
 &= \frac{2}{7}a(a+bx)^{7/2} + \frac{2}{9}(a+bx)^{9/2} + a^2 \int \frac{(a+bx)^{5/2}}{x} dx \\
 &= \frac{2}{5}a^2(a+bx)^{5/2} + \frac{2}{7}a(a+bx)^{7/2} + \frac{2}{9}(a+bx)^{9/2} + a^3 \int \frac{(a+bx)^{3/2}}{x} dx \\
 &= \frac{2}{3}a^3(a+bx)^{3/2} + \frac{2}{5}a^2(a+bx)^{5/2} + \frac{2}{7}a(a+bx)^{7/2} + \frac{2}{9}(a+bx)^{9/2} + a^4 \int \frac{\sqrt{a+bx}}{x} dx \\
 &= 2a^4\sqrt{a+bx} + \frac{2}{3}a^3(a+bx)^{3/2} + \frac{2}{5}a^2(a+bx)^{5/2} + \frac{2}{7}a(a+bx)^{7/2} + \frac{2}{9}(a+bx)^{9/2} + a^5 \int \frac{1}{x\sqrt{a+bx}} dx \\
 &= 2a^4\sqrt{a+bx} + \frac{2}{3}a^3(a+bx)^{3/2} + \frac{2}{5}a^2(a+bx)^{5/2} + \frac{2}{7}a(a+bx)^{7/2} + \frac{2}{9}(a+bx)^{9/2} + \frac{(2a^5) \operatorname{Subst}}{x\sqrt{a+bx}} \\
 &= 2a^4\sqrt{a+bx} + \frac{2}{3}a^3(a+bx)^{3/2} + \frac{2}{5}a^2(a+bx)^{5/2} + \frac{2}{7}a(a+bx)^{7/2} + \frac{2}{9}(a+bx)^{9/2} - 2a^{9/2} \tanh^{-1} \left(\frac{\sqrt{a+bx}}{\sqrt{a}} \right)
 \end{aligned}$$

Mathematica [A] time = 0.09, size = 78, normalized size = 0.80

$$\frac{2}{315} \sqrt{a+bx} (563a^4 + 506a^3bx + 408a^2b^2x^2 + 185ab^3x^3 + 35b^4x^4) - 2a^{9/2} \tanh^{-1} \left(\frac{\sqrt{a+bx}}{\sqrt{a}} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(9/2)/x, x]

[Out] (2*Sqrt[a + b*x]*(563*a^4 + 506*a^3*b*x + 408*a^2*b^2*x^2 + 185*a*b^3*x^3 + 35*b^4*x^4))/315 - 2*a^(9/2)*ArcTanh[Sqrt[a + b*x]/Sqrt[a]]

fricas [A] time = 0.50, size = 158, normalized size = 1.63

$$\left[a^{\frac{9}{2}} \log \left(\frac{bx - 2\sqrt{bx+a}\sqrt{a} + 2a}{x} \right) + \frac{2}{315} (35b^4x^4 + 185ab^3x^3 + 408a^2b^2x^2 + 506a^3bx + 563a^4) \sqrt{bx+a}, 2\sqrt{bx+a} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x,x, algorithm="fricas")

[Out] [a^(9/2)*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2/315*(35*b^4*x^4 + 185*a*b^3*x^3 + 408*a^2*b^2*x^2 + 506*a^3*b*x + 563*a^4)*sqrt(b*x + a), 2*sqrt(-a)*a^4*arctan(sqrt(b*x + a)*sqrt(-a)/a) + 2/315*(35*b^4*x^4 + 185*a*b^3*x^3 + 408*a^2*b^2*x^2 + 506*a^3*b*x + 563*a^4)*sqrt(b*x + a)]

giac [A] time = 1.23, size = 80, normalized size = 0.82

$$\frac{2a^5 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} + \frac{2}{9}(bx+a)^{\frac{9}{2}} + \frac{2}{7}(bx+a)^{\frac{7}{2}}a + \frac{2}{5}(bx+a)^{\frac{5}{2}}a^2 + \frac{2}{3}(bx+a)^{\frac{3}{2}}a^3 + 2\sqrt{bx+a}a^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x,x, algorithm="giac")

[Out] 2*a^5*arctan(sqrt(b*x + a)/sqrt(-a))/sqrt(-a) + 2/9*(b*x + a)^(9/2) + 2/7*(b*x + a)^(7/2)*a + 2/5*(b*x + a)^(5/2)*a^2 + 2/3*(b*x + a)^(3/2)*a^3 + 2*sqrt(b*x + a)*a^4

maple [A] time = 0.01, size = 74, normalized size = 0.76

$$-2a^{\frac{9}{2}} \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right) + 2\sqrt{bx+a}a^4 + \frac{2(bx+a)^{\frac{3}{2}}a^3}{3} + \frac{2(bx+a)^{\frac{5}{2}}a^2}{5} + \frac{2(bx+a)^{\frac{7}{2}}a}{7} + \frac{2(bx+a)^{\frac{9}{2}}}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(9/2)/x,x)

[Out] 2/3*a^3*(b*x+a)^(3/2)+2/5*a^2*(b*x+a)^(5/2)+2/7*a*(b*x+a)^(7/2)+2/9*(b*x+a)^(9/2)-2*a^(9/2)*arctanh((b*x+a)^(1/2)/a^(1/2))+2*a^4*(b*x+a)^(1/2)

maxima [A] time = 2.94, size = 88, normalized size = 0.91

$$a^{\frac{9}{2}} \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right) + \frac{2}{9}(bx+a)^{\frac{9}{2}} + \frac{2}{7}(bx+a)^{\frac{7}{2}}a + \frac{2}{5}(bx+a)^{\frac{5}{2}}a^2 + \frac{2}{3}(bx+a)^{\frac{3}{2}}a^3 + 2\sqrt{bx+a}a^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x,x, algorithm="maxima")

[Out] a^(9/2)*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a))) + 2/9*(b*x + a)^(9/2) + 2/7*(b*x + a)^(7/2)*a + 2/5*(b*x + a)^(5/2)*a^2 + 2/3*(b*x + a)^(3/2)*a^3 + 2*sqrt(b*x + a)*a^4

mupad [B] time = 0.04, size = 76, normalized size = 0.78

$$\frac{2a(a+bx)^{7/2}}{7} + \frac{2(a+bx)^{9/2}}{9} + 2a^4\sqrt{a+bx} + \frac{2a^3(a+bx)^{3/2}}{3} + \frac{2a^2(a+bx)^{5/2}}{5} + a^{9/2} \operatorname{atan}\left(\frac{\sqrt{a+bx} \operatorname{li}}{\sqrt{a}}\right) 2i$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(9/2)/x,x)`

[Out] $(2*a*(a + b*x)^{(7/2)})/7 + (2*(a + b*x)^{(9/2)})/9 + 2*a^4*(a + b*x)^{(1/2)} + (2*a^3*(a + b*x)^{(3/2)})/3 + (2*a^2*(a + b*x)^{(5/2)})/5 + a^{(9/2)}*atan(((a + b*x)^{(1/2)}*1i)/a^{(1/2)})*2i$

sympy [A] time = 11.10, size = 148, normalized size = 1.53

$$\frac{1126a^{\frac{9}{2}}\sqrt{1+\frac{bx}{a}}}{315} + a^{\frac{9}{2}} \log\left(\frac{bx}{a}\right) - 2a^{\frac{9}{2}} \log\left(\sqrt{1+\frac{bx}{a}} + 1\right) + \frac{1012a^{\frac{7}{2}}bx\sqrt{1+\frac{bx}{a}}}{315} + \frac{272a^{\frac{5}{2}}b^2x^2\sqrt{1+\frac{bx}{a}}}{105} + \frac{74a^{\frac{3}{2}}b^3x^3\sqrt{1+\frac{bx}{a}}}{63}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(9/2)/x,x)`

[Out] $1126*a^{(9/2)}*\sqrt{1 + b*x/a}/315 + a^{(9/2)}*\log(b*x/a) - 2*a^{(9/2)}*\log(\sqrt{1 + b*x/a} + 1) + 1012*a^{(7/2)}*b*x*\sqrt{1 + b*x/a}/315 + 272*a^{(5/2)}*b**2*x**2*\sqrt{1 + b*x/a}/105 + 74*a^{(3/2)}*b**3*x**3*\sqrt{1 + b*x/a}/63 + 2 * \sqrt{a}*b**4*x**4*\sqrt{1 + b*x/a}/9$

$$3.318 \quad \int \frac{(a+bx)^{9/2}}{x^2} dx$$

Optimal. Leaf size=98

$$-9a^{7/2}b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + 9a^3b\sqrt{a+bx} + 3a^2b(a+bx)^{3/2} - \frac{(a+bx)^{9/2}}{x} + \frac{9}{7}b(a+bx)^{7/2} + \frac{9}{5}ab(a+bx)^{5/2}$$

[Out] $3*a^2*b*(b*x+a)^{(3/2)}+9/5*a*b*(b*x+a)^{(5/2)}+9/7*b*(b*x+a)^{(7/2)}-(b*x+a)^{(9/2)}/x-9*a^{(7/2)}*b*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})+9*a^3*b*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 208}

$$3a^2b(a+bx)^{3/2} + 9a^3b\sqrt{a+bx} - 9a^{7/2}b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) - \frac{(a+bx)^{9/2}}{x} + \frac{9}{7}b(a+bx)^{7/2} + \frac{9}{5}ab(a+bx)^{5/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(9/2)/x^2, x]

[Out] $9*a^3*b*\operatorname{Sqrt}[a + b*x] + 3*a^2*b*(a + b*x)^{(3/2)} + (9*a*b*(a + b*x)^{(5/2)})/5 + (9*b*(a + b*x)^{(7/2)})/7 - (a + b*x)^{(9/2)}/x - 9*a^{(7/2)}*b*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{9/2}}{x^2} dx &= -\frac{(a+bx)^{9/2}}{x} + \frac{1}{2}(9b) \int \frac{(a+bx)^{7/2}}{x} dx \\
&= \frac{9}{7}b(a+bx)^{7/2} - \frac{(a+bx)^{9/2}}{x} + \frac{1}{2}(9ab) \int \frac{(a+bx)^{5/2}}{x} dx \\
&= \frac{9}{5}ab(a+bx)^{5/2} + \frac{9}{7}b(a+bx)^{7/2} - \frac{(a+bx)^{9/2}}{x} + \frac{1}{2}(9a^2b) \int \frac{(a+bx)^{3/2}}{x} dx \\
&= 3a^2b(a+bx)^{3/2} + \frac{9}{5}ab(a+bx)^{5/2} + \frac{9}{7}b(a+bx)^{7/2} - \frac{(a+bx)^{9/2}}{x} + \frac{1}{2}(9a^3b) \int \frac{\sqrt{a+bx}}{x} dx \\
&= 9a^3b\sqrt{a+bx} + 3a^2b(a+bx)^{3/2} + \frac{9}{5}ab(a+bx)^{5/2} + \frac{9}{7}b(a+bx)^{7/2} - \frac{(a+bx)^{9/2}}{x} + \frac{1}{2}(9a^4b) \int \frac{1}{x} dx \\
&= 9a^3b\sqrt{a+bx} + 3a^2b(a+bx)^{3/2} + \frac{9}{5}ab(a+bx)^{5/2} + \frac{9}{7}b(a+bx)^{7/2} - \frac{(a+bx)^{9/2}}{x} + (9a^4) \text{Subst} \\
&= 9a^3b\sqrt{a+bx} + 3a^2b(a+bx)^{3/2} + \frac{9}{5}ab(a+bx)^{5/2} + \frac{9}{7}b(a+bx)^{7/2} - \frac{(a+bx)^{9/2}}{x} - 9a^{7/2}b \tanh^{-1}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.34

$$\frac{2b(a+bx)^{11/2} {}_2F_1\left(2, \frac{11}{2}; \frac{13}{2}; \frac{bx}{a} + 1\right)}{11a^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*x)^(9/2)/x^2, x]
```

```
[Out] (2*b*(a + b*x)^(11/2)*Hypergeometric2F1[2, 11/2, 13/2, 1 + (b*x)/a])/(11*a^2)
```

fricas [A] time = 0.47, size = 172, normalized size = 1.76

$$\left[\frac{315 a^{\frac{7}{2}} b x \log\left(\frac{b x - 2 \sqrt{b x + a} \sqrt{a} + 2 a}{x}\right) + 2 \left(10 b^4 x^4 + 58 a b^3 x^3 + 156 a^2 b^2 x^2 + 388 a^3 b x - 35 a^4\right) \sqrt{b x + a}}{70 x}, \frac{315 \sqrt{-a} a^{\frac{7}{2}}}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^2,x, algorithm="fricas")

[Out] [1/70*(315*a^(7/2)*b*x*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*(10*b^4*x^4 + 58*a*b^3*x^3 + 156*a^2*b^2*x^2 + 388*a^3*b*x - 35*a^4)*sqrt(b*x + a))/x, 1/35*(315*sqrt(-a)*a^3*b*x*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (10*b^4*x^4 + 58*a*b^3*x^3 + 156*a^2*b^2*x^2 + 388*a^3*b*x - 35*a^4)*sqrt(b*x + a))/x]

giac [A] time = 1.43, size = 104, normalized size = 1.06

$$\frac{\frac{315 a^4 b^2 \arctan\left(\frac{\sqrt{b x + a}}{\sqrt{-a}}\right)}{\sqrt{-a}} + 10 (b x + a)^{\frac{7}{2}} b^2 + 28 (b x + a)^{\frac{5}{2}} a b^2 + 70 (b x + a)^{\frac{3}{2}} a^2 b^2 + 280 \sqrt{b x + a} a^3 b^2 - \frac{35 \sqrt{b x + a} a^4 b}{x}}{35 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^2,x, algorithm="giac")

[Out] 1/35*(315*a^4*b^2*arctan(sqrt(b*x + a)/sqrt(-a))/sqrt(-a) + 10*(b*x + a)^(7/2)*b^2 + 28*(b*x + a)^(5/2)*a*b^2 + 70*(b*x + a)^(3/2)*a^2*b^2 + 280*sqrt(b*x + a)*a^3*b^2 - 35*sqrt(b*x + a)*a^4*b/x)/b

maple [A] time = 0.01, size = 84, normalized size = 0.86

$$2 \left(\left(\frac{9 \operatorname{arctanh}\left(\frac{\sqrt{b x + a}}{\sqrt{a}}\right)}{2 \sqrt{a}} - \frac{\sqrt{b x + a}}{2 b x} \right) a^4 + 4 \sqrt{b x + a} a^3 + (b x + a)^{\frac{3}{2}} a^2 + \frac{2 (b x + a)^{\frac{5}{2}} a}{5} + \frac{(b x + a)^{\frac{7}{2}}}{7} \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(9/2)/x^2,x)

[Out] 2*b*(1/7*(b*x+a)^(7/2)+2/5*a*(b*x+a)^(5/2)+a^2*(b*x+a)^(3/2)+4*(b*x+a)^(1/2))*a^3+a^4*(-1/2*(b*x+a)^(1/2)/b/x-9/2*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(1/2))

maxima [A] time = 2.97, size = 97, normalized size = 0.99

$$\frac{9}{2} a^{\frac{7}{2}} b \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right) + \frac{2}{7} (bx+a)^{\frac{7}{2}} b + \frac{4}{5} (bx+a)^{\frac{5}{2}} ab + 2 (bx+a)^{\frac{3}{2}} a^2 b + 8 \sqrt{bx+a} a^3 b - \frac{\sqrt{bx+a} a^4}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^2,x, algorithm="maxima")

[Out] 9/2*a^(7/2)*b*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a))) + 2/7*(b*x + a)^(7/2)*b + 4/5*(b*x + a)^(5/2)*a*b + 2*(b*x + a)^(3/2)*a^2*b + 8*sqrt(b*x + a)*a^3*b - sqrt(b*x + a)*a^4/x

mupad [B] time = 0.04, size = 84, normalized size = 0.86

$$\frac{2b(a+bx)^{7/2}}{7} - \frac{a^4\sqrt{a+bx}}{x} + \frac{4ab(a+bx)^{5/2}}{5} + 8a^3b\sqrt{a+bx} + 2a^2b(a+bx)^{3/2} + a^{7/2}b \operatorname{atan}\left(\frac{\sqrt{a+bx} \operatorname{li}}{\sqrt{a}}\right) 9i$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(9/2)/x^2,x)

[Out] (2*b*(a + b*x)^(7/2))/7 - (a^4*(a + b*x)^(1/2))/x + a^(7/2)*b*atan(((a + b*x)^(1/2)*1i)/a^(1/2))*9i + (4*a*b*(a + b*x)^(5/2))/5 + 8*a^3*b*(a + b*x)^(1/2) + 2*a^2*b*(a + b*x)^(3/2)

sympy [A] time = 9.92, size = 150, normalized size = 1.53

$$-\frac{a^{\frac{9}{2}}\sqrt{1+\frac{bx}{a}}}{x} + \frac{388a^{\frac{7}{2}}b\sqrt{1+\frac{bx}{a}}}{35} + \frac{9a^{\frac{7}{2}}b\log\left(\frac{bx}{a}\right)}{2} - 9a^{\frac{7}{2}}b\log\left(\sqrt{1+\frac{bx}{a}}+1\right) + \frac{156a^{\frac{5}{2}}b^2x\sqrt{1+\frac{bx}{a}}}{35} + \frac{58a^{\frac{3}{2}}b^3x^2\sqrt{1+\frac{bx}{a}}}{35}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(9/2)/x**2,x)

[Out] -a**(9/2)*sqrt(1 + b*x/a)/x + 388*a**(7/2)*b*sqrt(1 + b*x/a)/35 + 9*a**(7/2)*b*log(b*x/a)/2 - 9*a**(7/2)*b*log(sqrt(1 + b*x/a) + 1) + 156*a**(5/2)*b**2*x*sqrt(1 + b*x/a)/35 + 58*a**(3/2)*b**3*x**2*sqrt(1 + b*x/a)/35 + 2*sqrt(a)*b**4*x**3*sqrt(1 + b*x/a)/7

$$3.319 \quad \int \frac{(a+bx)^{9/2}}{x^3} dx$$

Optimal. Leaf size=114

$$-\frac{63}{4}a^{5/2}b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + \frac{63}{4}a^2b^2\sqrt{a+bx} + \frac{63}{20}b^2(a+bx)^{5/2} + \frac{21}{4}ab^2(a+bx)^{3/2} - \frac{(a+bx)^{9/2}}{2x^2} - \frac{9b(a+bx)^{7/2}}{4x}$$

[Out] $21/4*a*b^2*(b*x+a)^{(3/2)}+63/20*b^2*(b*x+a)^{(5/2)}-9/4*b*(b*x+a)^{(7/2)}/x-1/2*(b*x+a)^{(9/2)}/x^2-63/4*a^{(5/2)}*b^2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})+63/4*a^2*b^2*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 114, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 208}

$$\frac{63}{4}a^2b^2\sqrt{a+bx} - \frac{63}{4}a^{5/2}b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + \frac{63}{20}b^2(a+bx)^{5/2} + \frac{21}{4}ab^2(a+bx)^{3/2} - \frac{(a+bx)^{9/2}}{2x^2} - \frac{9b(a+bx)^{7/2}}{4x}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(9/2)/x^3, x]

[Out] $(63*a^2*b^2*\operatorname{Sqrt}[a + b*x])/4 + (21*a*b^2*(a + b*x)^{(3/2)})/4 + (63*b^2*(a + b*x)^{(5/2)})/20 - (9*b*(a + b*x)^{(7/2)})/(4*x) - (a + b*x)^{(9/2)}/(2*x^2) - (63*a^{(5/2)}*b^2*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/4$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{9/2}}{x^3} dx &= -\frac{(a+bx)^{9/2}}{2x^2} + \frac{1}{4}(9b) \int \frac{(a+bx)^{7/2}}{x^2} dx \\
&= -\frac{9b(a+bx)^{7/2}}{4x} - \frac{(a+bx)^{9/2}}{2x^2} + \frac{1}{8}(63b^2) \int \frac{(a+bx)^{5/2}}{x} dx \\
&= \frac{63}{20}b^2(a+bx)^{5/2} - \frac{9b(a+bx)^{7/2}}{4x} - \frac{(a+bx)^{9/2}}{2x^2} + \frac{1}{8}(63ab^2) \int \frac{(a+bx)^{3/2}}{x} dx \\
&= \frac{21}{4}ab^2(a+bx)^{3/2} + \frac{63}{20}b^2(a+bx)^{5/2} - \frac{9b(a+bx)^{7/2}}{4x} - \frac{(a+bx)^{9/2}}{2x^2} + \frac{1}{8}(63a^2b^2) \int \frac{\sqrt{a+bx}}{x} dx \\
&= \frac{63}{4}a^2b^2\sqrt{a+bx} + \frac{21}{4}ab^2(a+bx)^{3/2} + \frac{63}{20}b^2(a+bx)^{5/2} - \frac{9b(a+bx)^{7/2}}{4x} - \frac{(a+bx)^{9/2}}{2x^2} + \frac{1}{8}(63a^2b^2) \int \frac{\sqrt{a+bx}}{x} dx \\
&= \frac{63}{4}a^2b^2\sqrt{a+bx} + \frac{21}{4}ab^2(a+bx)^{3/2} + \frac{63}{20}b^2(a+bx)^{5/2} - \frac{9b(a+bx)^{7/2}}{4x} - \frac{(a+bx)^{9/2}}{2x^2} + \frac{1}{4}(63a^2b^2) \int \frac{\sqrt{a+bx}}{x} dx \\
&= \frac{63}{4}a^2b^2\sqrt{a+bx} + \frac{21}{4}ab^2(a+bx)^{3/2} + \frac{63}{20}b^2(a+bx)^{5/2} - \frac{9b(a+bx)^{7/2}}{4x} - \frac{(a+bx)^{9/2}}{2x^2} - \frac{63}{4}a^2b^2 \int \frac{\sqrt{a+bx}}{x} dx
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.31

$$-\frac{2b^2(a+bx)^{11/2} {}_2F_1\left(3, \frac{11}{2}; \frac{13}{2}; \frac{bx}{a} + 1\right)}{11a^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*x)^(9/2)/x^3, x]
```

[Out] $(-2*b^2*(a + b*x)^{(11/2)}*Hypergeometric2F1[3, 11/2, 13/2, 1 + (b*x)/a])/(11*a^3)$

fricas [A] time = 0.48, size = 180, normalized size = 1.58

$$\left[\frac{315 a^{\frac{5}{2}} b^2 x^2 \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(8b^4x^4 + 56ab^3x^3 + 288a^2b^2x^2 - 85a^3bx - 10a^4)\sqrt{bx+a} + 315\sqrt{-a}a^2}{40x^2}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^3,x, algorithm="fricas")

[Out] $[1/40*(315*a^{(5/2)}*b^2*x^2*\log((b*x - 2*\sqrt{b*x + a})*\sqrt{a} + 2*a)/x) + 2*(8*b^4*x^4 + 56*a*b^3*x^3 + 288*a^2*b^2*x^2 - 85*a^3*b*x - 10*a^4)*\sqrt{b*x + a})/x^2, 1/20*(315*\sqrt{-a}*a^2*b^2*x^2*\arctan(\sqrt{b*x + a}*\sqrt{-a}/a) + (8*b^4*x^4 + 56*a*b^3*x^3 + 288*a^2*b^2*x^2 - 85*a^3*b*x - 10*a^4)*\sqrt{b*x + a})/x^2]$

giac [A] time = 1.10, size = 112, normalized size = 0.98

$$\frac{315 a^3 b^3 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right) + 8 (bx+a)^{\frac{5}{2}} b^3 + 40 (bx+a)^{\frac{3}{2}} a b^3 + 240 \sqrt{bx+a} a^2 b^3 - \frac{5(17(bx+a)^{\frac{3}{2}} a^3 b^3 - 15 \sqrt{bx+a} a^4 b^3)}{b^2 x^2}}{20 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^3,x, algorithm="giac")

[Out] $1/20*(315*a^3*b^3*\arctan(\sqrt{b*x + a}/\sqrt{-a})/\sqrt{-a} + 8*(b*x + a)^{(5/2)}*b^3 + 40*(b*x + a)^{(3/2)}*a*b^3 + 240*\sqrt{b*x + a}*a^2*b^3 - 5*(17*(b*x + a)^{(3/2)}*a^3*b^3 - 15*\sqrt{b*x + a}*a^4*b^3)/(b^2*x^2))/b$

maple [A] time = 0.01, size = 86, normalized size = 0.75

$$2 \left(\left(-\frac{63 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{8\sqrt{a}} + \frac{15\sqrt{bx+a}a - 17(bx+a)^{\frac{3}{2}}}{8b^2x^2} \right) a^3 + 6\sqrt{bx+a}a^2 + (bx+a)^{\frac{3}{2}}a + \frac{(bx+a)^{\frac{5}{2}}}{5} \right) b^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(9/2)/x^3,x)

[Out] $2*b^2*(1/5*(b*x+a)^{(5/2)}+(b*x+a)^{(3/2)}*a+6*(b*x+a)^{(1/2)}*a^2+a^3*((-17/8*(b*x+a)^{(3/2)}+15/8*(b*x+a)^{(1/2)}*a)/x^2/b^2-63/8*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)}))/a^{(1/2)})$

maxima [A] time = 2.95, size = 131, normalized size = 1.15

$$\frac{63}{8} a^{\frac{5}{2}} b^2 \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right) + \frac{2}{5} (bx+a)^{\frac{5}{2}} b^2 + 2 (bx+a)^{\frac{3}{2}} a b^2 + 12 \sqrt{bx+a} a^2 b^2 - \frac{17 (bx+a)^{\frac{3}{2}} a^3 b^2 - 15 \sqrt{bx+a} a^4 b^2}{4 ((bx+a)^2 - 2 (bx+a)a + a^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^3,x, algorithm="maxima")

[Out] 63/8*a^(5/2)*b^2*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a))) + 2/5*(b*x + a)^(5/2)*b^2 + 2*(b*x + a)^(3/2)*a*b^2 + 12*sqrt(b*x + a)*a^2*b^2 - 1/4*(17*(b*x + a)^(3/2)*a^3*b^2 - 15*sqrt(b*x + a)*a^4*b^2)/((b*x + a)^2 - 2*(b*x + a)*a + a^2)

mupad [B] time = 0.05, size = 117, normalized size = 1.03

$$\frac{2 b^2 (a + b x)^{5/2}}{5} + \frac{\frac{15 a^4 b^2 \sqrt{a+b x}}{4} - \frac{17 a^3 b^2 (a+b x)^{3/2}}{4}}{(a + b x)^2 - 2 a (a + b x) + a^2} + 12 a^2 b^2 \sqrt{a + b x} + 2 a b^2 (a + b x)^{3/2} + \frac{a^{5/2} b^2 \operatorname{atan}\left(\frac{\sqrt{a+b x}}{\sqrt{a}}\right)}{4} 63i$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(9/2)/x^3,x)

[Out] (2*b^2*(a + b*x)^(5/2))/5 + ((15*a^4*b^2*(a + b*x)^(1/2))/4 - (17*a^3*b^2*(a + b*x)^(3/2))/4)/((a + b*x)^2 - 2*a*(a + b*x) + a^2) + 12*a^2*b^2*(a + b*x)^(1/2) + (a^(5/2)*b^2*atan((a + b*x)^(1/2)*1i)/a^(1/2))*63i/4 + 2*a*b^2*(a + b*x)^(3/2)

sympy [A] time = 8.99, size = 184, normalized size = 1.61

$$-\frac{63a^{\frac{5}{2}}b^2 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4} - \frac{a^5}{2\sqrt{b}x^{\frac{5}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{19a^4\sqrt{b}}{4x^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}} + \frac{203a^3b^{\frac{3}{2}}}{20\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{86a^2b^{\frac{5}{2}}\sqrt{x}}{5\sqrt{\frac{a}{bx}+1}} + \frac{16ab^{\frac{7}{2}}x^{\frac{3}{2}}}{5\sqrt{\frac{a}{bx}+1}} + \frac{2b^2x^{\frac{5}{2}}}{5\sqrt{\frac{a}{bx}+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(9/2)/x**3,x)

[Out] -63*a**(5/2)*b**2*asinh(sqrt(a)/(sqrt(b)*sqrt(x)))/4 - a**5/(2*sqrt(b)*x**(5/2)*sqrt(a/(b*x) + 1)) - 19*a**4*sqrt(b)/(4*x**(3/2)*sqrt(a/(b*x) + 1)) + 203*a**3*b**(3/2)/(20*sqrt(x)*sqrt(a/(b*x) + 1)) + 86*a**2*b**(5/2)*sqrt(x)/(5*sqrt(a/(b*x) + 1)) + 16*a*b**(7/2)*x**(3/2)/(5*sqrt(a/(b*x) + 1)) + 2*b**(9/2)*x**(5/2)/(5*sqrt(a/(b*x) + 1))

$$3.320 \quad \int \frac{(a+bx)^{9/2}}{x^4} dx$$

Optimal. Leaf size=114

$$-\frac{105}{8}a^{3/2}b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) + \frac{35}{8}b^3(a+bx)^{3/2} + \frac{105}{8}ab^3\sqrt{a+bx} - \frac{21b^2(a+bx)^{5/2}}{8x} - \frac{(a+bx)^{9/2}}{3x^3} - \frac{3b(a+bx)^{7/2}}{4x^2}$$

[Out] 35/8*b^3*(b*x+a)^(3/2)-21/8*b^2*(b*x+a)^(5/2)/x-3/4*b*(b*x+a)^(7/2)/x^2-1/3*(b*x+a)^(9/2)/x^3-105/8*a^(3/2)*b^3*arctanh((b*x+a)^(1/2)/a^(1/2))+105/8*a*b^3*(b*x+a)^(1/2)

Rubi [A] time = 0.04, antiderivative size = 114, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 208}

$$-\frac{105}{8}a^{3/2}b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) - \frac{21b^2(a+bx)^{5/2}}{8x} + \frac{35}{8}b^3(a+bx)^{3/2} + \frac{105}{8}ab^3\sqrt{a+bx} - \frac{(a+bx)^{9/2}}{3x^3} - \frac{3b(a+bx)^{7/2}}{4x^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(9/2)/x^4,x]

[Out] (105*a*b^3*Sqrt[a + b*x])/8 + (35*b^3*(a + b*x)^(3/2))/8 - (21*b^2*(a + b*x)^(5/2))/(8*x) - (3*b*(a + b*x)^(7/2))/(4*x^2) - (a + b*x)^(9/2)/(3*x^3) - (105*a^(3/2)*b^3*ArcTanh[Sqrt[a + b*x]/Sqrt[a]])/8

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{9/2}}{x^4} dx &= -\frac{(a+bx)^{9/2}}{3x^3} + \frac{1}{2}(3b) \int \frac{(a+bx)^{7/2}}{x^3} dx \\
&= -\frac{3b(a+bx)^{7/2}}{4x^2} - \frac{(a+bx)^{9/2}}{3x^3} + \frac{1}{8}(21b^2) \int \frac{(a+bx)^{5/2}}{x^2} dx \\
&= -\frac{21b^2(a+bx)^{5/2}}{8x} - \frac{3b(a+bx)^{7/2}}{4x^2} - \frac{(a+bx)^{9/2}}{3x^3} + \frac{1}{16}(105b^3) \int \frac{(a+bx)^{3/2}}{x} dx \\
&= \frac{35}{8}b^3(a+bx)^{3/2} - \frac{21b^2(a+bx)^{5/2}}{8x} - \frac{3b(a+bx)^{7/2}}{4x^2} - \frac{(a+bx)^{9/2}}{3x^3} + \frac{1}{16}(105ab^3) \int \frac{\sqrt{a+bx}}{x} dx \\
&= \frac{105}{8}ab^3\sqrt{a+bx} + \frac{35}{8}b^3(a+bx)^{3/2} - \frac{21b^2(a+bx)^{5/2}}{8x} - \frac{3b(a+bx)^{7/2}}{4x^2} - \frac{(a+bx)^{9/2}}{3x^3} + \frac{1}{16}(105a^2b^3) \int \frac{1}{x} dx \\
&= \frac{105}{8}ab^3\sqrt{a+bx} + \frac{35}{8}b^3(a+bx)^{3/2} - \frac{21b^2(a+bx)^{5/2}}{8x} - \frac{3b(a+bx)^{7/2}}{4x^2} - \frac{(a+bx)^{9/2}}{3x^3} + \frac{1}{8}(105a^2b^3) \ln|x| \\
&= \frac{105}{8}ab^3\sqrt{a+bx} + \frac{35}{8}b^3(a+bx)^{3/2} - \frac{21b^2(a+bx)^{5/2}}{8x} - \frac{3b(a+bx)^{7/2}}{4x^2} - \frac{(a+bx)^{9/2}}{3x^3} - \frac{105}{8}a^2b^3 \ln|x|
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.31

$$\frac{2b^3(a+bx)^{11/2} {}_2F_1\left(4, \frac{11}{2}; \frac{13}{2}; \frac{bx}{a} + 1\right)}{11a^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(9/2)/x^4, x]

[Out] $(2*b^3*(a + b*x)^{(11/2)}*Hypergeometric2F1[4, 11/2, 13/2, 1 + (b*x)/a])/(11*a^4)$

fricas [A] time = 0.48, size = 178, normalized size = 1.56

$$\left[\frac{315 a^{\frac{3}{2}} b^3 x^3 \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(16b^4x^4 + 208ab^3x^3 - 165a^2b^2x^2 - 50a^3bx - 8a^4)\sqrt{bx+a}}{48x^3}, \frac{315\sqrt{-a}a}{\dots} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(9/2)/x^4,x, algorithm="fricas")`

[Out] $[1/48*(315*a^{(3/2)}*b^3*x^3*\log((b*x - 2*\sqrt{b*x + a})*\sqrt{a} + 2*a)/x) + 2*(16*b^4*x^4 + 208*a*b^3*x^3 - 165*a^2*b^2*x^2 - 50*a^3*b*x - 8*a^4)*\sqrt{b*x + a})/x^3, 1/24*(315*\sqrt{-a}*a*b^3*x^3*\arctan(\sqrt{b*x + a}*\sqrt{-a}/a) + (16*b^4*x^4 + 208*a*b^3*x^3 - 165*a^2*b^2*x^2 - 50*a^3*b*x - 8*a^4)*\sqrt{b*x + a})/x^3]$

giac [A] time = 1.10, size = 112, normalized size = 0.98

$$\frac{315 a^2 b^4 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} + 16 (bx + a)^{\frac{3}{2}} b^4 + 192 \sqrt{bx + a} a b^4 - \frac{165 (bx+a)^{\frac{5}{2}} a^2 b^4 - 280 (bx+a)^{\frac{3}{2}} a^3 b^4 + 123 \sqrt{bx+a} a^4 b^4}{b^3 x^3}}{24 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(9/2)/x^4,x, algorithm="giac")`

[Out] $1/24*(315*a^2*b^4*\arctan(\sqrt{b*x + a}/\sqrt{-a})/\sqrt{-a} + 16*(b*x + a)^{(3/2)}*b^4 + 192*\sqrt{b*x + a}*a*b^4 - (165*(b*x + a)^{(5/2)}*a^2*b^4 - 280*(b*x + a)^{(3/2)}*a^3*b^4 + 123*\sqrt{b*x + a}*a^4*b^4)/(b^3*x^3))/b$

maple [A] time = 0.01, size = 87, normalized size = 0.76

$$2 \left(\left(-\frac{105 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{16\sqrt{a}} + \frac{-\frac{41\sqrt{bx+a}a^2}{16} + \frac{35(bx+a)^{\frac{3}{2}}a}{6} - \frac{55(bx+a)^{\frac{5}{2}}}{16}}{b^3x^3} \right) a^2 + 4\sqrt{bx+a}a + \frac{(bx+a)^{\frac{3}{2}}}{3} \right) b^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(9/2)/x^4,x)`

[Out] $2*b^3*(1/3*(b*x+a)^{(3/2)}+4*(b*x+a)^{(1/2)}*a+a^2*((-55/16*(b*x+a)^{(5/2)}+35/6*(b*x+a)^{(3/2)}*a-41/16*(b*x+a)^{(1/2)}*a^2)/x^3/b^3-105/16*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)}))/a^{(1/2)})$

maxima [A] time = 2.94, size = 145, normalized size = 1.27

$$\frac{105}{16} a^{\frac{3}{2}} b^3 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right) + \frac{2}{3} (bx+a)^{\frac{3}{2}} b^3 + 8 \sqrt{bx+a} a b^3 - \frac{165 (bx+a)^{\frac{5}{2}} a^2 b^3 - 280 (bx+a)^{\frac{3}{2}} a^3 b^3 + 123 \sqrt{bx+a} a^4 b^3}{24 \left((bx+a)^3 - 3 (bx+a)^2 a + 3 (bx+a) a^2 - a^3 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^4,x, algorithm="maxima")

[Out] 105/16*a^(3/2)*b^3*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a))) + 2/3*(b*x + a)^(3/2)*b^3 + 8*sqrt(b*x + a)*a*b^3 - 1/24*(165*(b*x + a)^(5/2)*a^2*b^3 - 280*(b*x + a)^(3/2)*a^3*b^3 + 123*sqrt(b*x + a)*a^4*b^3)/((b*x + a)^3 - 3*(b*x + a)^2*a + 3*(b*x + a)*a^2 - a^3)

mupad [B] time = 0.12, size = 131, normalized size = 1.15

$$\frac{2b^3(a+bx)^{3/2}}{3} + \frac{\frac{41a^4b^3\sqrt{a+bx}}{8} - \frac{35a^3b^3(a+bx)^{3/2}}{3} + \frac{55a^2b^3(a+bx)^{5/2}}{8}}{3a(a+bx)^2 - 3a^2(a+bx) - (a+bx)^3 + a^3} + 8ab^3\sqrt{a+bx} + \frac{a^{3/2}b^3 \operatorname{atan}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8} 105i$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(9/2)/x^4,x)

[Out] (2*b^3*(a + b*x)^(3/2))/3 + ((41*a^4*b^3*(a + b*x)^(1/2))/8 - (35*a^3*b^3*(a + b*x)^(3/2))/3 + (55*a^2*b^3*(a + b*x)^(5/2))/8)/(3*a*(a + b*x)^2 - 3*a^2*(a + b*x) - (a + b*x)^3 + a^3) + (a^(3/2)*b^3*atan(((a + b*x)^(1/2)*1i)/a^(1/2)))/8 + 8*a*b^3*(a + b*x)^(1/2)

sympy [A] time = 7.91, size = 184, normalized size = 1.61

$$\frac{105a^{\frac{3}{2}}b^3 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{8} - \frac{a^5}{3\sqrt{b}x^{\frac{7}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{29a^4\sqrt{b}}{12x^{\frac{5}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{215a^3b^{\frac{3}{2}}}{24x^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}} + \frac{43a^2b^{\frac{5}{2}}}{24\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{28ab^{\frac{7}{2}}\sqrt{x}}{3\sqrt{\frac{a}{bx}+1}} + \frac{2b^{\frac{9}{2}}x^{\frac{9}{2}}}{3\sqrt{\frac{a}{bx}+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(9/2)/x**4,x)

[Out] -105*a**(3/2)*b**3*asinh(sqrt(a)/(sqrt(b)*sqrt(x)))/8 - a**5/(3*sqrt(b)*x**(7/2)*sqrt(a/(b*x) + 1)) - 29*a**4*sqrt(b)/(12*x**(5/2)*sqrt(a/(b*x) + 1)) - 215*a**3*b**(3/2)/(24*x**(3/2)*sqrt(a/(b*x) + 1)) + 43*a**2*b**(5/2)/(24*sqrt(x)*sqrt(a/(b*x) + 1)) + 28*a*b**(7/2)*sqrt(x)/(3*sqrt(a/(b*x) + 1)) + 2*b**(9/2)*x**(3/2)/(3*sqrt(a/(b*x) + 1))

$$3.321 \quad \int \frac{(a+bx)^{9/2}}{x^5} dx$$

Optimal. Leaf size=116

$$\frac{315}{64}b^4\sqrt{a+bx} - \frac{315}{64}\sqrt{a}b^4 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) - \frac{105b^3(a+bx)^{3/2}}{64x} - \frac{21b^2(a+bx)^{5/2}}{32x^2} - \frac{(a+bx)^{9/2}}{4x^4} - \frac{3b(a+bx)^{7/2}}{8x^3}$$

[Out] $-105/64*b^3*(b*x+a)^{(3/2)}/x-21/32*b^2*(b*x+a)^{(5/2)}/x^2-3/8*b*(b*x+a)^{(7/2)}/x^3-1/4*(b*x+a)^{(9/2)}/x^4-315/64*b^4*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})*a^{(1/2)}+315/64*b^4*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 116, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 208}

$$-\frac{21b^2(a+bx)^{5/2}}{32x^2} - \frac{105b^3(a+bx)^{3/2}}{64x} + \frac{315}{64}b^4\sqrt{a+bx} - \frac{315}{64}\sqrt{a}b^4 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right) - \frac{(a+bx)^{9/2}}{4x^4} - \frac{3b(a+bx)^{7/2}}{8x^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(9/2)/x^5, x]

[Out] $(315*b^4*\operatorname{Sqrt}[a + b*x])/64 - (105*b^3*(a + b*x)^{(3/2)})/(64*x) - (21*b^2*(a + b*x)^{(5/2)})/(32*x^2) - (3*b*(a + b*x)^{(7/2)})/(8*x^3) - (a + b*x)^{(9/2)}/(4*x^4) - (315*\operatorname{Sqrt}[a]*b^4*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/64$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{9/2}}{x^5} dx &= -\frac{(a+bx)^{9/2}}{4x^4} + \frac{1}{8}(9b) \int \frac{(a+bx)^{7/2}}{x^4} dx \\
&= -\frac{3b(a+bx)^{7/2}}{8x^3} - \frac{(a+bx)^{9/2}}{4x^4} + \frac{1}{16}(21b^2) \int \frac{(a+bx)^{5/2}}{x^3} dx \\
&= -\frac{21b^2(a+bx)^{5/2}}{32x^2} - \frac{3b(a+bx)^{7/2}}{8x^3} - \frac{(a+bx)^{9/2}}{4x^4} + \frac{1}{64}(105b^3) \int \frac{(a+bx)^{3/2}}{x^2} dx \\
&= -\frac{105b^3(a+bx)^{3/2}}{64x} - \frac{21b^2(a+bx)^{5/2}}{32x^2} - \frac{3b(a+bx)^{7/2}}{8x^3} - \frac{(a+bx)^{9/2}}{4x^4} + \frac{1}{128}(315b^4) \int \frac{\sqrt{a+bx}}{x} dx \\
&= \frac{315}{64}b^4\sqrt{a+bx} - \frac{105b^3(a+bx)^{3/2}}{64x} - \frac{21b^2(a+bx)^{5/2}}{32x^2} - \frac{3b(a+bx)^{7/2}}{8x^3} - \frac{(a+bx)^{9/2}}{4x^4} + \frac{1}{128}(315b^4) \int \frac{\sqrt{a+bx}}{x} dx \\
&= \frac{315}{64}b^4\sqrt{a+bx} - \frac{105b^3(a+bx)^{3/2}}{64x} - \frac{21b^2(a+bx)^{5/2}}{32x^2} - \frac{3b(a+bx)^{7/2}}{8x^3} - \frac{(a+bx)^{9/2}}{4x^4} + \frac{1}{64}(315b^4) \int \frac{\sqrt{a+bx}}{x} dx \\
&= \frac{315}{64}b^4\sqrt{a+bx} - \frac{105b^3(a+bx)^{3/2}}{64x} - \frac{21b^2(a+bx)^{5/2}}{32x^2} - \frac{3b(a+bx)^{7/2}}{8x^3} - \frac{(a+bx)^{9/2}}{4x^4} - \frac{315}{64}b^4\sqrt{a+bx}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.30

$$-\frac{2b^4(a+bx)^{11/2} {}_2F_1\left(5, \frac{11}{2}; \frac{13}{2}; \frac{bx}{a} + 1\right)}{11a^5}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*x)^(9/2)/x^5, x]
```

[Out] $(-2*b^4*(a + b*x)^{(11/2)}*Hypergeometric2F1[5, 11/2, 13/2, 1 + (b*x)/a])/(11*a^5)$

fricas [A] time = 0.55, size = 177, normalized size = 1.53

$$\left[\frac{315 \sqrt{a} b^4 x^4 \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(128 b^4 x^4 - 325 ab^3 x^3 - 210 a^2 b^2 x^2 - 88 a^3 bx - 16 a^4) \sqrt{bx+a}}{128 x^4}, \frac{315 \sqrt{-a} \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right) + 2(128 b^4 x^4 - 325 a b^3 x^3 - 210 a^2 b^2 x^2 - 88 a^3 b x - 16 a^4) \sqrt{-a}}{128 x^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(9/2)/x^5,x, algorithm="fricas")`

[Out] $\frac{1}{128} (315 \sqrt{a} b^4 x^4 \log((b*x - 2*\sqrt{b*x + a})*\sqrt{a} + 2*a)/x) + 2*(128*b^4*x^4 - 325*a*b^3*x^3 - 210*a^2*b^2*x^2 - 88*a^3*b*x - 16*a^4)*\sqrt{-a} \arctan(\sqrt{b*x + a})/x^4 + 1/64*(315*\sqrt{-a}*b^4*x^4*\arctan(\sqrt{b*x + a})*\sqrt{-a}/a) + (128*b^4*x^4 - 325*a*b^3*x^3 - 210*a^2*b^2*x^2 - 88*a^3*b*x - 16*a^4)*\sqrt{b*x + a}/x^4$

giac [A] time = 1.22, size = 110, normalized size = 0.95

$$\frac{315 ab^5 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} + 128 \sqrt{bx+a} b^5 - \frac{325 (bx+a)^{\frac{7}{2}} ab^5 - 765 (bx+a)^{\frac{5}{2}} a^2 b^5 + 643 (bx+a)^{\frac{3}{2}} a^3 b^5 - 187 \sqrt{bx+a} a^4 b^5}{b^4 x^4}}{64 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(9/2)/x^5,x, algorithm="giac")`

[Out] $\frac{1}{64} (315*a*b^5*\arctan(\sqrt{b*x + a}/\sqrt{-a})/\sqrt{-a} + 128*\sqrt{b*x + a} *b^5 - (325*(b*x + a)^{(7/2)}*a*b^5 - 765*(b*x + a)^{(5/2)}*a^2*b^5 + 643*(b*x + a)^{(3/2)}*a^3*b^5 - 187*\sqrt{b*x + a}*a^4*b^5)/(b^4*x^4))/b$

maple [A] time = 0.01, size = 85, normalized size = 0.73

$$2 \left(\left(-\frac{315 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{128 \sqrt{a}} + \frac{187 \sqrt{bx+a} a^3}{128} - \frac{643 (bx+a)^{\frac{3}{2}} a^2}{128} + \frac{765 (bx+a)^{\frac{5}{2}} a}{128} - \frac{325 (bx+a)^{\frac{7}{2}}}{128} \right) a + \sqrt{bx+a} \right) b^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(9/2)/x^5,x)`

[Out] $2*b^4*((b*x+a)^{(1/2)}+a*((-325/128*(b*x+a)^{(7/2)}+765/128*(b*x+a)^{(5/2)}*a-643/128*(b*x+a)^{(3/2)}*a^2+187/128*(b*x+a)^{(1/2)}*a^3)/x^4/b^4-315/128*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(1/2)})$

maxima [A] time = 2.96, size = 155, normalized size = 1.34

$$\frac{315}{128} \sqrt{a} b^4 \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right) + 2\sqrt{bx+a} b^4 - \frac{325 (bx+a)^{\frac{7}{2}} a b^4 - 765 (bx+a)^{\frac{5}{2}} a^2 b^4 + 643 (bx+a)^{\frac{3}{2}} a^3 b^4 - 187 \sqrt{bx+a} a^4}{64 \left((bx+a)^4 - 4(bx+a)^3 a + 6(bx+a)^2 a^2 - 4(bx+a) a^3 + a^4 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^5,x, algorithm="maxima")

[Out] 315/128*sqrt(a)*b^4*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a))) + 2*sqrt(b*x + a)*b^4 - 1/64*(325*(b*x + a)^(7/2)*a*b^4 - 765*(b*x + a)^(5/2)*a^2*b^4 + 643*(b*x + a)^(3/2)*a^3*b^4 - 187*sqrt(b*x + a)*a^4*b^4)/((b*x + a)^4 - 4*(b*x + a)^3*a + 6*(b*x + a)^2*a^2 - 4*(b*x + a)*a^3 + a^4)

mupad [B] time = 0.06, size = 94, normalized size = 0.81

$$2b^4 \sqrt{a+bx} + \frac{187a^4 \sqrt{a+bx}}{64x^4} - \frac{643a^3(a+bx)^{3/2}}{64x^4} + \frac{765a^2(a+bx)^{5/2}}{64x^4} - \frac{325a(a+bx)^{7/2}}{64x^4} + \frac{\sqrt{a} b^4 \operatorname{atan}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{64}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(9/2)/x^5,x)

[Out] 2*b^4*(a + b*x)^(1/2) + (187*a^4*(a + b*x)^(1/2))/(64*x^4) - (643*a^3*(a + b*x)^(3/2))/(64*x^4) + (765*a^2*(a + b*x)^(5/2))/(64*x^4) + (a^(1/2)*b^4*atan((a + b*x)^(1/2)*1i/a^(1/2))*315i)/64 - (325*a*(a + b*x)^(7/2))/(64*x^4)

sympy [A] time = 8.55, size = 182, normalized size = 1.57

$$\frac{315\sqrt{a}b^4 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{64} - \frac{a^5}{4\sqrt{b}x^{\frac{9}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{13a^4\sqrt{b}}{8x^{\frac{7}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{149a^3b^{\frac{3}{2}}}{32x^{\frac{5}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{535a^2b^{\frac{5}{2}}}{64x^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{197ab^{\frac{7}{2}}}{64\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{2b^{\frac{9}{2}}}{\sqrt{\frac{a}{bx}+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(9/2)/x**5,x)

[Out] -315*sqrt(a)*b**4*asinh(sqrt(a)/(sqrt(b)*sqrt(x)))/64 - a**5/(4*sqrt(b)*x**(9/2)*sqrt(a/(b*x) + 1)) - 13*a**4*sqrt(b)/(8*x**(7/2)*sqrt(a/(b*x) + 1)) - 149*a**3*b**(3/2)/(32*x**(5/2)*sqrt(a/(b*x) + 1)) - 535*a**2*b**(5/2)/(64*x**(3/2)*sqrt(a/(b*x) + 1)) - 197*a*b**(7/2)/(64*sqrt(x)*sqrt(a/(b*x) + 1)) + 2*b**(9/2)*sqrt(x)/sqrt(a/(b*x) + 1)

$$3.322 \quad \int \frac{(a+bx)^{9/2}}{x^6} dx$$

Optimal. Leaf size=119

$$\frac{63b^5 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{128\sqrt{a}} - \frac{63b^4\sqrt{a+bx}}{128x} - \frac{21b^3(a+bx)^{3/2}}{64x^2} - \frac{21b^2(a+bx)^{5/2}}{80x^3} - \frac{(a+bx)^{9/2}}{5x^5} - \frac{9b(a+bx)^{7/2}}{40x^4}$$

[Out] $-21/64*b^3*(b*x+a)^{(3/2)}/x^2-21/80*b^2*(b*x+a)^{(5/2)}/x^3-9/40*b*(b*x+a)^{(7/2)}/x^4-1/5*(b*x+a)^{(9/2)}/x^5-63/128*b^5*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(1/2)}-63/128*b^4*(b*x+a)^{(1/2)}/x$

Rubi [A] time = 0.04, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {47, 63, 208}

$$\frac{21b^3(a+bx)^{3/2}}{64x^2} - \frac{21b^2(a+bx)^{5/2}}{80x^3} - \frac{63b^4\sqrt{a+bx}}{128x} - \frac{63b^5 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{128\sqrt{a}} - \frac{9b(a+bx)^{7/2}}{40x^4} - \frac{(a+bx)^{9/2}}{5x^5}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(9/2)}/x^6, x]$

[Out] $(-63*b^4*\operatorname{Sqrt}[a + b*x])/(128*x) - (21*b^3*(a + b*x)^{(3/2)})/(64*x^2) - (21*b^2*(a + b*x)^{(5/2)})/(80*x^3) - (9*b*(a + b*x)^{(7/2)})/(40*x^4) - (a + b*x)^{(9/2)}/(5*x^5) - (63*b^5*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(128*\operatorname{Sqrt}[a])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{GtQ}[n, 0] \ \&\& \ \operatorname{LtQ}[m, -1] \ \&\& \ !(\operatorname{IntegerQ}[n] \ \&\& \ !\operatorname{IntegerQ}[m]) \ \&\& \ !(\operatorname{ILeQ}[m + n + 2, 0] \ \&\& \ (\operatorname{FractionQ}[m] \ || \ \operatorname{GeQ}[2*n + m + 1, 0])) \ \& \ \& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{LtQ}[-1, m, 0] \ \&\& \ \operatorname{LeQ}[-1, n, 0] \ \&\& \ \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{9/2}}{x^6} dx &= -\frac{(a+bx)^{9/2}}{5x^5} + \frac{1}{10}(9b) \int \frac{(a+bx)^{7/2}}{x^5} dx \\
 &= -\frac{9b(a+bx)^{7/2}}{40x^4} - \frac{(a+bx)^{9/2}}{5x^5} + \frac{1}{80}(63b^2) \int \frac{(a+bx)^{5/2}}{x^4} dx \\
 &= -\frac{21b^2(a+bx)^{5/2}}{80x^3} - \frac{9b(a+bx)^{7/2}}{40x^4} - \frac{(a+bx)^{9/2}}{5x^5} + \frac{1}{32}(21b^3) \int \frac{(a+bx)^{3/2}}{x^3} dx \\
 &= -\frac{21b^3(a+bx)^{3/2}}{64x^2} - \frac{21b^2(a+bx)^{5/2}}{80x^3} - \frac{9b(a+bx)^{7/2}}{40x^4} - \frac{(a+bx)^{9/2}}{5x^5} + \frac{1}{128}(63b^4) \int \frac{\sqrt{a+bx}}{x^2} dx \\
 &= -\frac{63b^4\sqrt{a+bx}}{128x} - \frac{21b^3(a+bx)^{3/2}}{64x^2} - \frac{21b^2(a+bx)^{5/2}}{80x^3} - \frac{9b(a+bx)^{7/2}}{40x^4} - \frac{(a+bx)^{9/2}}{5x^5} + \frac{1}{256}(63b^4) \int \frac{1}{x} dx \\
 &= -\frac{63b^4\sqrt{a+bx}}{128x} - \frac{21b^3(a+bx)^{3/2}}{64x^2} - \frac{21b^2(a+bx)^{5/2}}{80x^3} - \frac{9b(a+bx)^{7/2}}{40x^4} - \frac{(a+bx)^{9/2}}{5x^5} + \frac{1}{128}(63b^4) \ln|x| \\
 &= -\frac{63b^4\sqrt{a+bx}}{128x} - \frac{21b^3(a+bx)^{3/2}}{64x^2} - \frac{21b^2(a+bx)^{5/2}}{80x^3} - \frac{9b(a+bx)^{7/2}}{40x^4} - \frac{(a+bx)^{9/2}}{5x^5} - \frac{63b^4 \tan^{-1}\left(\sqrt{\frac{bx+a}{a}}\right)}{128}
 \end{aligned}$$

Mathematica [A] time = 0.04, size = 101, normalized size = 0.85

$$\frac{128a^5 + 784a^4bx + 2024a^3b^2x^2 + 2858a^2b^3x^3 + 315b^5x^5 \sqrt{\frac{bx}{a} + 1} \tanh^{-1}\left(\sqrt{\frac{bx}{a} + 1}\right) + 2455ab^4x^4 + 965b^5x^5}{640x^5\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(9/2)/x^6, x]

[Out] -1/640*(128*a^5 + 784*a^4*b*x + 2024*a^3*b^2*x^2 + 2858*a^2*b^3*x^3 + 2455*a*b^4*x^4 + 965*b^5*x^5 + 315*b^5*x^5*Sqrt[1 + (b*x)/a]*ArcTanh[Sqrt[1 + (b*x)/a]])/(x^5*Sqrt[a + b*x])

fricas [A] time = 0.55, size = 190, normalized size = 1.60

$$\left[\frac{315 \sqrt{a} b^5 x^5 \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2(965 ab^4 x^4 + 1490 a^2 b^3 x^3 + 1368 a^3 b^2 x^2 + 656 a^4 bx + 128 a^5) \sqrt{bx+a}}{1280 ax^5}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^6,x, algorithm="fricas")

[Out] $\left[\frac{1}{1280} \cdot (315 \sqrt{a} \cdot b^5 x^5 \log((b x - 2 \sqrt{b x + a}) \sqrt{a} + 2 a) / x) - 2 \cdot (965 a b^4 x^4 + 1490 a^2 b^3 x^3 + 1368 a^3 b^2 x^2 + 656 a^4 b x + 128 a^5) \sqrt{b x + a} \right] / (a x^5), \frac{1}{640} \cdot (315 \sqrt{-a} \cdot b^5 x^5 \arctan(\sqrt{b x + a}) \sqrt{-a} / a) - (965 a b^4 x^4 + 1490 a^2 b^3 x^3 + 1368 a^3 b^2 x^2 + 656 a^4 b x + 128 a^5) \sqrt{b x + a} \right] / (a x^5]$

giac [A] time = 1.19, size = 109, normalized size = 0.92

$$\frac{\frac{315 b^6 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}} - \frac{965 (bx+a)^2 b^6 - 2370 (bx+a)^2 a b^6 + 2688 (bx+a)^2 a^2 b^6 - 1470 (bx+a)^3 a^3 b^6 + 315 \sqrt{bx+a} a^4 b^6}{b^5 x^5}}{640 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^6,x, algorithm="giac")

[Out] $\frac{1}{640} \cdot (315 b^6 \arctan(\sqrt{b x + a} / \sqrt{-a}) / \sqrt{-a} - (965 (b x + a)^{9/2} b^6 - 2370 (b x + a)^{7/2} a b^6 + 2688 (b x + a)^{5/2} a^2 b^6 - 1470 (b x + a)^{3/2} a^3 b^6 + 315 \sqrt{b x + a} a^4 b^6) / (b^5 x^5)) / b$

maple [A] time = 0.01, size = 87, normalized size = 0.73

$$2 \left(-\frac{63 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{256 \sqrt{a}} + \frac{-\frac{63 \sqrt{bx+a} a^4}{256} + \frac{147 (bx+a)^3 a^3}{128} - \frac{21 (bx+a)^5 a^2}{10} + \frac{237 (bx+a)^7 a}{128} - \frac{193 (bx+a)^9}{256}}{b^5 x^5} \right) b^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(9/2)/x^6,x)

[Out] $2 b^5 \cdot \left((-193/256 \cdot (b x + a)^{9/2} + 237/128 \cdot (b x + a)^{7/2} \cdot a - 21/10 \cdot (b x + a)^{5/2} \cdot a^2 + 147/128 \cdot (b x + a)^{3/2} \cdot a^3 - 63/256 \cdot (b x + a)^{1/2} \cdot a^4) / x^5 / b^5 - 63/256 \cdot \operatorname{arctanh}((b x + a)^{1/2} / a^{1/2}) / a^{1/2} \right)$

maxima [A] time = 2.97, size = 169, normalized size = 1.42

$$\frac{63 b^5 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{256 \sqrt{a}} - \frac{965 (bx+a)^2 b^5 - 2370 (bx+a)^2 a b^5 + 2688 (bx+a)^2 a^2 b^5 - 1470 (bx+a)^3 a^3 b^5 + 315 \sqrt{bx+a} a^4 b^6}{640 \left((bx+a)^5 - 5 (bx+a)^4 a + 10 (bx+a)^3 a^2 - 10 (bx+a)^2 a^3 + 5 (bx+a) a^4 - a^5 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^6,x, algorithm="maxima")

[Out] $\frac{63}{256}b^5 \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right) / \sqrt{a} - \frac{1}{640}(965(bx+a)^{9/2}b^5 - 2370(bx+a)^{7/2}ab^5 + 2688(bx+a)^{5/2}a^2b^5 - 1470(bx+a)^{3/2}a^3b^5 + 315\sqrt{bx+a}a^4b^5) / ((bx+a)^5 - 5(bx+a)^4a + 10(bx+a)^3a^2 - 10(bx+a)^2a^3 + 5(bx+a)a^4 - a^5)$

mupad [B] time = 0.12, size = 94, normalized size = 0.79

$$\frac{147a^3(a+bx)^{3/2}}{64x^5} - \frac{63a^4\sqrt{a+bx}}{128x^5} - \frac{193(a+bx)^{9/2}}{128x^5} - \frac{21a^2(a+bx)^{5/2}}{5x^5} + \frac{237a(a+bx)^{7/2}}{64x^5} + \frac{b^5 \operatorname{atan}\left(\frac{\sqrt{a+bx} - 1i}{\sqrt{a}}\right)}{128\sqrt{a}} 63i$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(9/2)/x^6,x)

[Out] $\frac{147a^3(a+bx)^{3/2}}{(64x^5)} - \frac{63a^4(a+bx)^{1/2}}{(128x^5)} - \frac{193(a+bx)^{9/2}}{(128x^5)} - \frac{21a^2(a+bx)^{5/2}}{(5x^5)} + \frac{b^5 \operatorname{atan}\left(\frac{(a+bx)^{1/2} - 1i}{a^{1/2}}\right)}{(128a^{1/2})} + \frac{237a(a+bx)^{7/2}}{(64x^5)}$

sympy [A] time = 10.25, size = 158, normalized size = 1.33

$$\frac{a^4\sqrt{b}\sqrt{\frac{a}{bx}+1}}{5x^{\frac{9}{2}}} - \frac{41a^3b^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}}{40x^{\frac{7}{2}}} - \frac{171a^2b^{\frac{5}{2}}\sqrt{\frac{a}{bx}+1}}{80x^{\frac{5}{2}}} - \frac{149ab^{\frac{7}{2}}\sqrt{\frac{a}{bx}+1}}{64x^{\frac{3}{2}}} - \frac{193b^{\frac{9}{2}}\sqrt{\frac{a}{bx}+1}}{128\sqrt{x}} - \frac{63b^5 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{128\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(9/2)/x**6,x)

[Out] $-a^{**4}\sqrt{b}\sqrt{a/(b*x) + 1}/(5*x^{**}(9/2)) - 41*a^{**3}b^{**}(3/2)\sqrt{a/(b*x) + 1}/(40*x^{**}(7/2)) - 171*a^{**2}b^{**}(5/2)\sqrt{a/(b*x) + 1}/(80*x^{**}(5/2)) - 149*a*b^{**}(7/2)\sqrt{a/(b*x) + 1}/(64*x^{**}(3/2)) - 193*b^{**}(9/2)\sqrt{a/(b*x) + 1}/(128*\sqrt{x}) - 63*b^{**5}\operatorname{asinh}(\sqrt{a}/(\sqrt{b}\sqrt{x}))/128*\sqrt{a}$

$$3.323 \quad \int \frac{(a+bx)^{9/2}}{x^7} dx$$

Optimal. Leaf size=141

$$\frac{21b^6 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{512a^{3/2}} - \frac{21b^5\sqrt{a+bx}}{512ax} - \frac{21b^4\sqrt{a+bx}}{256x^2} - \frac{7b^3(a+bx)^{3/2}}{64x^3} - \frac{21b^2(a+bx)^{5/2}}{160x^4} - \frac{(a+bx)^{9/2}}{6x^6} - \frac{3b(a+bx)^{7/2}}{20x^5}$$

[Out] $-7/64*b^3*(b*x+a)^{(3/2)}/x^3-21/160*b^2*(b*x+a)^{(5/2)}/x^4-3/20*b*(b*x+a)^{(7/2)}/x^5-1/6*(b*x+a)^{(9/2)}/x^6+21/512*b^6*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(3/2)}-21/256*b^4*(b*x+a)^{(1/2)}/x^2-21/512*b^5*(b*x+a)^{(1/2)}/a/x$

Rubi [A] time = 0.05, antiderivative size = 141, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 51, 63, 208}

$$\frac{21b^6 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{512a^{3/2}} - \frac{21b^4\sqrt{a+bx}}{256x^2} - \frac{7b^3(a+bx)^{3/2}}{64x^3} - \frac{21b^2(a+bx)^{5/2}}{160x^4} - \frac{21b^5\sqrt{a+bx}}{512ax} - \frac{3b(a+bx)^{7/2}}{20x^5} - \frac{(a+bx)^{9/2}}{6x^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(9/2)/x^7, x]

[Out] $(-21*b^4*\operatorname{Sqrt}[a + b*x])/(256*x^2) - (21*b^5*\operatorname{Sqrt}[a + b*x])/(512*a*x) - (7*b^3*(a + b*x)^{(3/2)})/(64*x^3) - (21*b^2*(a + b*x)^{(5/2)})/(160*x^4) - (3*b*(a + b*x)^{(7/2)})/(20*x^5) - (a + b*x)^{(9/2)}/(6*x^6) + (21*b^6*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(512*a^{(3/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I

ntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{9/2}}{x^7} dx &= -\frac{(a+bx)^{9/2}}{6x^6} + \frac{1}{4}(3b) \int \frac{(a+bx)^{7/2}}{x^6} dx \\
 &= -\frac{3b(a+bx)^{7/2}}{20x^5} - \frac{(a+bx)^{9/2}}{6x^6} + \frac{1}{40} (21b^2) \int \frac{(a+bx)^{5/2}}{x^5} dx \\
 &= -\frac{21b^2(a+bx)^{5/2}}{160x^4} - \frac{3b(a+bx)^{7/2}}{20x^5} - \frac{(a+bx)^{9/2}}{6x^6} + \frac{1}{64} (21b^3) \int \frac{(a+bx)^{3/2}}{x^4} dx \\
 &= -\frac{7b^3(a+bx)^{3/2}}{64x^3} - \frac{21b^2(a+bx)^{5/2}}{160x^4} - \frac{3b(a+bx)^{7/2}}{20x^5} - \frac{(a+bx)^{9/2}}{6x^6} + \frac{1}{128} (21b^4) \int \frac{\sqrt{a+bx}}{x^3} dx \\
 &= -\frac{21b^4\sqrt{a+bx}}{256x^2} - \frac{7b^3(a+bx)^{3/2}}{64x^3} - \frac{21b^2(a+bx)^{5/2}}{160x^4} - \frac{3b(a+bx)^{7/2}}{20x^5} - \frac{(a+bx)^{9/2}}{6x^6} + \frac{1}{512} (21b^5) \int \frac{1}{x^2} dx \\
 &= -\frac{21b^4\sqrt{a+bx}}{256x^2} - \frac{21b^5\sqrt{a+bx}}{512ax} - \frac{7b^3(a+bx)^{3/2}}{64x^3} - \frac{21b^2(a+bx)^{5/2}}{160x^4} - \frac{3b(a+bx)^{7/2}}{20x^5} - \frac{(a+bx)^{9/2}}{6x^6} \\
 &= -\frac{21b^4\sqrt{a+bx}}{256x^2} - \frac{21b^5\sqrt{a+bx}}{512ax} - \frac{7b^3(a+bx)^{3/2}}{64x^3} - \frac{21b^2(a+bx)^{5/2}}{160x^4} - \frac{3b(a+bx)^{7/2}}{20x^5} - \frac{(a+bx)^{9/2}}{6x^6} \\
 &= -\frac{21b^4\sqrt{a+bx}}{256x^2} - \frac{21b^5\sqrt{a+bx}}{512ax} - \frac{7b^3(a+bx)^{3/2}}{64x^3} - \frac{21b^2(a+bx)^{5/2}}{160x^4} - \frac{3b(a+bx)^{7/2}}{20x^5} - \frac{(a+bx)^{9/2}}{6x^6}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.25

$$\frac{2b^6(a+bx)^{11/2} {}_2F_1\left(\frac{11}{2}, 7; \frac{13}{2}; \frac{bx}{a} + 1\right)}{11a^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(9/2)/x^7,x]

[Out] $(-2*b^6*(a + b*x)^{(11/2)}*Hypergeometric2F1[11/2, 7, 13/2, 1 + (b*x)/a])/(11*a^7)$

fricas [A] time = 0.47, size = 211, normalized size = 1.50

$$\left[\frac{315 \sqrt{a} b^6 x^6 \log\left(\frac{bx+2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2(315 ab^5 x^5 + 4910 a^2 b^4 x^4 + 11432 a^3 b^3 x^3 + 12144 a^4 b^2 x^2 + 6272 a^5 b x + 1280 a^6)}{15360 a^2 x^6} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^7,x, algorithm="fricas")

[Out] $[1/15360*(315*\sqrt{a}*b^6*x^6*\log((b*x + 2*\sqrt{b*x + a})*\sqrt{a} + 2*a)/x) - 2*(315*a*b^5*x^5 + 4910*a^2*b^4*x^4 + 11432*a^3*b^3*x^3 + 12144*a^4*b^2*x^2 + 6272*a^5*b*x + 1280*a^6)*\sqrt{b*x + a})/(a^2*x^6), -1/7680*(315*\sqrt{-a}*b^6*x^6*\arctan(\sqrt{b*x + a}*\sqrt{-a}/a) + (315*a*b^5*x^5 + 4910*a^2*b^4*x^4 + 11432*a^3*b^3*x^3 + 12144*a^4*b^2*x^2 + 6272*a^5*b*x + 1280*a^6)*\sqrt{b*x + a})/(a^2*x^6)]$

giac [A] time = 1.04, size = 129, normalized size = 0.91

$$\frac{\frac{315 b^7 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a} a} + \frac{315 (bx+a)^{\frac{11}{2}} b^7 + 3335 (bx+a)^{\frac{9}{2}} a b^7 - 5058 (bx+a)^{\frac{7}{2}} a^2 b^7 + 4158 (bx+a)^{\frac{5}{2}} a^3 b^7 - 1785 (bx+a)^{\frac{3}{2}} a^4 b^7 + 315 \sqrt{bx+a} a^5 b^7}{ab^6 x^6}}{7680 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^7,x, algorithm="giac")

[Out] $-1/7680*(315*b^7*\arctan(\sqrt{b*x + a}/\sqrt{-a})/(\sqrt{-a}*a) + (315*(b*x + a)^{(11/2)}*b^7 + 3335*(b*x + a)^{(9/2)}*a*b^7 - 5058*(b*x + a)^{(7/2)}*a^2*b^7 + 4158*(b*x + a)^{(5/2)}*a^3*b^7 - 1785*(b*x + a)^{(3/2)}*a^4*b^7 + 315*\sqrt{b*x + a}*a^5*b^7)/(a*b^6*x^6))/b$

maple [A] time = 0.01, size = 99, normalized size = 0.70

$$2 \left(\frac{21 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{1024 a^{\frac{3}{2}}} + \frac{-\frac{21 \sqrt{bx+a} a^4}{1024} + \frac{119 (bx+a)^{\frac{3}{2}} a^3}{1024} - \frac{693 (bx+a)^{\frac{5}{2}} a^2}{2560} + \frac{843 (bx+a)^{\frac{7}{2}} a}{2560} - \frac{21 (bx+a)^{\frac{11}{2}}}{1024 a} - \frac{667 (bx+a)^{\frac{9}{2}}}{3072}}{b^6 x^6} \right) b^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x+a)^{(9/2)}/x^7, x)$

[Out] $2*b^6*((-21/1024/a*(b*x+a)^{(11/2)}-667/3072*(b*x+a)^{(9/2)}+843/2560*(b*x+a)^{(7/2)}*a-693/2560*(b*x+a)^{(5/2)}*a^2+119/1024*(b*x+a)^{(3/2)}*a^3-21/1024*(b*x+a)^{(1/2)}*a^4)/x^6/b^6+21/1024*\text{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(3/2)}$

maxima [A] time = 3.03, size = 198, normalized size = 1.40

$$\frac{21 b^6 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{1024 a^{\frac{3}{2}}}-\frac{315 (bx+a)^{\frac{11}{2}} b^6+3335 (bx+a)^{\frac{9}{2}} a b^6-5058 (bx+a)^{\frac{7}{2}} a^2 b^6+4158 (bx+a)^{\frac{5}{2}} a^3 b^6-1785 (bx+a)^{\frac{3}{2}} a^4 b^6+315 \sqrt{bx+a} a^5 b^6}{7680\left((bx+a)^6 a-6(bx+a)^5 a^2+15(bx+a)^4 a^3-20(bx+a)^3 a^4+15(bx+a)^2 a^5-6(bx+a) a^6+a^7\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)^{(9/2)}/x^7, x, \text{algorithm}="maxima")$

[Out] $-21/1024*b^6*\log((\text{sqrt}(b*x+a)-\text{sqrt}(a))/(\text{sqrt}(b*x+a)+\text{sqrt}(a)))/a^{(3/2)}-1/7680*(315*(b*x+a)^{(11/2)}*b^6+3335*(b*x+a)^{(9/2)}*a*b^6-5058*(b*x+a)^{(7/2)}*a^2*b^6+4158*(b*x+a)^{(5/2)}*a^3*b^6-1785*(b*x+a)^{(3/2)}*a^4*b^6+315*\text{sqrt}(b*x+a)*a^5*b^6)/((b*x+a)^6*a-6*(b*x+a)^5*a^2+15*(b*x+a)^4*a^3-20*(b*x+a)^3*a^4+15*(b*x+a)^2*a^5-6*(b*x+a)*a^6+a^7)$

mupad [B] time = 0.13, size = 109, normalized size = 0.77

$$\frac{119 a^3 (a+b x)^{3/2}}{512 x^6}-\frac{21 a^4 \sqrt{a+b x}}{512 x^6}-\frac{667 (a+b x)^{9/2}}{1536 x^6}-\frac{693 a^2 (a+b x)^{5/2}}{1280 x^6}-\frac{21 (a+b x)^{11/2}}{512 a x^6}+\frac{843 a (a+b x)^{7/2}}{1280 x^6}-\frac{b^6 \text{atan}\left(\frac{\sqrt{a+b x}-\sqrt{a}}{\sqrt{a+b x}+\sqrt{a}}\right)}{512 a^2 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a+b*x)^{(9/2)}/x^7, x)$

[Out] $(119*a^3*(a+b*x)^{(3/2)})/(512*x^6)-(21*a^4*(a+b*x)^{(1/2)})/(512*x^6)-(667*(a+b*x)^{(9/2)})/(1536*x^6)-(693*a^2*(a+b*x)^{(5/2)})/(1280*x^6)-(21*(a+b*x)^{(11/2)})/(512*a*x^6)-(b^6*\text{atan}(((a+b*x)^{(1/2)}*1i)/a^{(1/2)})*21i)/(512*a^{(3/2)})+(843*a*(a+b*x)^{(7/2)})/(1280*x^6)$

sympy [A] time = 15.69, size = 209, normalized size = 1.48

$$\frac{a^5}{6\sqrt{b}x^{\frac{13}{2}}\sqrt{\frac{a}{bx}+1}}-\frac{59a^4\sqrt{b}}{60x^{\frac{11}{2}}\sqrt{\frac{a}{bx}+1}}-\frac{1151a^3b^{\frac{3}{2}}}{480x^{\frac{9}{2}}\sqrt{\frac{a}{bx}+1}}-\frac{2947a^2b^{\frac{5}{2}}}{960x^{\frac{7}{2}}\sqrt{\frac{a}{bx}+1}}-\frac{8171ab^{\frac{7}{2}}}{3840x^{\frac{5}{2}}\sqrt{\frac{a}{bx}+1}}-\frac{1045b^{\frac{9}{2}}}{1536x^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}}-\frac{b^6\text{atan}\left(\frac{\sqrt{\frac{a}{bx}+1}-1}{\sqrt{\frac{a}{bx}+1}+1}\right)}{512a^2x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)**(9/2)/x**7, x)$

```
[Out] -a**5/(6*sqrt(b)*x**(13/2)*sqrt(a/(b*x) + 1)) - 59*a**4*sqrt(b)/(60*x**(11/2)*sqrt(a/(b*x) + 1)) - 1151*a**3*b**(3/2)/(480*x**(9/2)*sqrt(a/(b*x) + 1)) - 2947*a**2*b**(5/2)/(960*x**(7/2)*sqrt(a/(b*x) + 1)) - 8171*a*b**(7/2)/(3840*x**(5/2)*sqrt(a/(b*x) + 1)) - 1045*b**(9/2)/(1536*x**(3/2)*sqrt(a/(b*x) + 1)) - 21*b**(11/2)/(512*a*sqrt(x)*sqrt(a/(b*x) + 1)) + 21*b**6*asinh(sqrt(a)/(sqrt(b)*sqrt(x)))/(512*a**(3/2))
```

$$3.324 \quad \int \frac{(a+bx)^{9/2}}{x^8} dx$$

Optimal. Leaf size=163

$$-\frac{9b^7 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{1024a^{5/2}} + \frac{9b^6\sqrt{a+bx}}{1024a^2x} - \frac{3b^5\sqrt{a+bx}}{512ax^2} - \frac{3b^4\sqrt{a+bx}}{128x^3} - \frac{3b^3(a+bx)^{3/2}}{64x^4} - \frac{3b^2(a+bx)^{5/2}}{40x^5} - \frac{(a+bx)^{9/2}}{7x^7} - \frac{3b(a+bx)^{7/2}}{28x^6}$$

[Out] $-3/64*b^3*(b*x+a)^{(3/2)}/x^4-3/40*b^2*(b*x+a)^{(5/2)}/x^5-3/28*b*(b*x+a)^{(7/2)}/x^6-1/7*(b*x+a)^{(9/2)}/x^7-9/1024*b^7*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(5/2)}$
 $-3/128*b^4*(b*x+a)^{(1/2)}/x^3-3/512*b^5*(b*x+a)^{(1/2)}/a/x^2+9/1024*b^6*(b*x+a)^{(1/2)}/a^2/x$

Rubi [A] time = 0.07, antiderivative size = 163, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 51, 63, 208}

$$\frac{9b^6\sqrt{a+bx}}{1024a^2x} - \frac{9b^7 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{1024a^{5/2}} - \frac{3b^5\sqrt{a+bx}}{512ax^2} - \frac{3b^4\sqrt{a+bx}}{128x^3} - \frac{3b^3(a+bx)^{3/2}}{64x^4} - \frac{3b^2(a+bx)^{5/2}}{40x^5} - \frac{3b(a+bx)^{7/2}}{28x^6} - \frac{(a+bx)^{9/2}}{7x^7}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(9/2)/x^8, x]

[Out] $(-3*b^4*\operatorname{Sqrt}[a + b*x])/(128*x^3) - (3*b^5*\operatorname{Sqrt}[a + b*x])/(512*a*x^2) + (9*b^6*\operatorname{Sqrt}[a + b*x])/(1024*a^2*x) - (3*b^3*(a + b*x)^{(3/2)})/(64*x^4) - (3*b^2*(a + b*x)^{(5/2)})/(40*x^5) - (3*b*(a + b*x)^{(7/2)})/(28*x^6) - (a + b*x)^{(9/2)}/(7*x^7) - (9*b^7*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(1024*a^{(5/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IleQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I

ntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{9/2}}{x^8} dx &= -\frac{(a+bx)^{9/2}}{7x^7} + \frac{1}{14}(9b) \int \frac{(a+bx)^{7/2}}{x^7} dx \\
 &= -\frac{3b(a+bx)^{7/2}}{28x^6} - \frac{(a+bx)^{9/2}}{7x^7} + \frac{1}{8}(3b^2) \int \frac{(a+bx)^{5/2}}{x^6} dx \\
 &= -\frac{3b^2(a+bx)^{5/2}}{40x^5} - \frac{3b(a+bx)^{7/2}}{28x^6} - \frac{(a+bx)^{9/2}}{7x^7} + \frac{1}{16}(3b^3) \int \frac{(a+bx)^{3/2}}{x^5} dx \\
 &= -\frac{3b^3(a+bx)^{3/2}}{64x^4} - \frac{3b^2(a+bx)^{5/2}}{40x^5} - \frac{3b(a+bx)^{7/2}}{28x^6} - \frac{(a+bx)^{9/2}}{7x^7} + \frac{1}{128}(9b^4) \int \frac{\sqrt{a+bx}}{x^4} dx \\
 &= -\frac{3b^4\sqrt{a+bx}}{128x^3} - \frac{3b^3(a+bx)^{3/2}}{64x^4} - \frac{3b^2(a+bx)^{5/2}}{40x^5} - \frac{3b(a+bx)^{7/2}}{28x^6} - \frac{(a+bx)^{9/2}}{7x^7} + \frac{1}{256}(3b^5) \int \frac{1}{x^3} dx \\
 &= -\frac{3b^4\sqrt{a+bx}}{128x^3} - \frac{3b^5\sqrt{a+bx}}{512ax^2} - \frac{3b^3(a+bx)^{3/2}}{64x^4} - \frac{3b^2(a+bx)^{5/2}}{40x^5} - \frac{3b(a+bx)^{7/2}}{28x^6} - \frac{(a+bx)^{9/2}}{7x^7} \\
 &= -\frac{3b^4\sqrt{a+bx}}{128x^3} - \frac{3b^5\sqrt{a+bx}}{512ax^2} + \frac{9b^6\sqrt{a+bx}}{1024a^2x} - \frac{3b^3(a+bx)^{3/2}}{64x^4} - \frac{3b^2(a+bx)^{5/2}}{40x^5} - \frac{3b(a+bx)^{7/2}}{28x^6} \\
 &= -\frac{3b^4\sqrt{a+bx}}{128x^3} - \frac{3b^5\sqrt{a+bx}}{512ax^2} + \frac{9b^6\sqrt{a+bx}}{1024a^2x} - \frac{3b^3(a+bx)^{3/2}}{64x^4} - \frac{3b^2(a+bx)^{5/2}}{40x^5} - \frac{3b(a+bx)^{7/2}}{28x^6} \\
 &= -\frac{3b^4\sqrt{a+bx}}{128x^3} - \frac{3b^5\sqrt{a+bx}}{512ax^2} + \frac{9b^6\sqrt{a+bx}}{1024a^2x} - \frac{3b^3(a+bx)^{3/2}}{64x^4} - \frac{3b^2(a+bx)^{5/2}}{40x^5} - \frac{3b(a+bx)^{7/2}}{28x^6}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.21

$$\frac{2b^7(a+bx)^{11/2} {}_2F_1\left(\frac{11}{2}, 8; \frac{13}{2}; \frac{bx}{a} + 1\right)}{11a^8}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(9/2)/x^8, x]

[Out] (2*b^7*(a + b*x)^(11/2)*Hypergeometric2F1[11/2, 8, 13/2, 1 + (b*x)/a])/(11*a^8)

fricas [A] time = 0.50, size = 233, normalized size = 1.43

$$\left[\frac{315 \sqrt{a} b^7 x^7 \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(315 ab^6 x^6 - 210 a^2 b^5 x^5 - 14168 a^3 b^4 x^4 - 39056 a^4 b^3 x^3 - 44928 a^5 b^2 x^2 - 24320 a^6 b x - 5120 a^7) \sqrt{bx+a}}{71680 a^3 x^7} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^8, x, algorithm="fricas")

[Out] [1/71680*(315*sqrt(a)*b^7*x^7*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*(315*a*b^6*x^6 - 210*a^2*b^5*x^5 - 14168*a^3*b^4*x^4 - 39056*a^4*b^3*x^3 - 44928*a^5*b^2*x^2 - 24320*a^6*b*x - 5120*a^7)*sqrt(b*x + a))/(a^3*x^7), 1/35840*(315*sqrt(-a)*b^7*x^7*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (315*a*b^6*x^6 - 210*a^2*b^5*x^5 - 14168*a^3*b^4*x^4 - 39056*a^4*b^3*x^3 - 44928*a^5*b^2*x^2 - 24320*a^6*b*x - 5120*a^7)*sqrt(b*x + a))/(a^3*x^7)]

giac [A] time = 0.95, size = 144, normalized size = 0.88

$$\frac{315 b^8 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a^2}} + \frac{315 (bx+a)^{\frac{13}{2}} b^8 - 2100 (bx+a)^{\frac{11}{2}} a b^8 - 8393 (bx+a)^{\frac{9}{2}} a^2 b^8 + 9216 (bx+a)^{\frac{7}{2}} a^3 b^8 - 5943 (bx+a)^{\frac{5}{2}} a^4 b^8 + 2100 (bx+a)^{\frac{3}{2}} a^5 b^8 - 315 \sqrt{bx+a} a^6 b^8}{a^2 b^7 x^7}$$

35840 b

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/x^8, x, algorithm="giac")

[Out] 1/35840*(315*b^8*arctan(sqrt(b*x + a)/sqrt(-a))/(sqrt(-a)*a^2) + (315*(b*x + a)^(13/2)*b^8 - 2100*(b*x + a)^(11/2)*a*b^8 - 8393*(b*x + a)^(9/2)*a^2*b^8 + 9216*(b*x + a)^(7/2)*a^3*b^8 - 5943*(b*x + a)^(5/2)*a^4*b^8 + 2100*(b*x + a)^(3/2)*a^5*b^8 - 315*sqrt(b*x + a)*a^6*b^8)/(a^2*b^7*x^7)/b

maple [A] time = 0.01, size = 111, normalized size = 0.68

$$2 \left(\frac{9 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{2048a^{\frac{5}{2}}} + \frac{-\frac{9\sqrt{bx+a}a^4}{2048} + \frac{15(bx+a)^{\frac{3}{2}}a^3}{512} - \frac{849(bx+a)^{\frac{5}{2}}a^2}{10240} + \frac{9(bx+a)^{\frac{7}{2}}a}{70} - \frac{15(bx+a)^{\frac{11}{2}}}{512a} + \frac{9(bx+a)^{\frac{13}{2}}}{2048a^2} - \frac{1199(bx+a)^{\frac{9}{2}}}{10240}}{b^7x^7} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(9/2)/x^8,x)`

[Out] $2*b^7*((9/2048/a^2*(b*x+a)^{(13/2)}-15/512*(b*x+a)^{(11/2)}/a-1199/10240*(b*x+a)^{(9/2)}+9/70*(b*x+a)^{(7/2)}*a-849/10240*(b*x+a)^{(5/2)}*a^2+15/512*(b*x+a)^{(3/2)}*a^3-9/2048*(b*x+a)^{(1/2)}*a^4)/x^7/b^7-9/2048*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(5/2)}$

maxima [A] time = 3.08, size = 229, normalized size = 1.40

$$\frac{9b^7 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{2048a^{\frac{5}{2}}} + \frac{315(bx+a)^{\frac{13}{2}}b^7 - 2100(bx+a)^{\frac{11}{2}}ab^7 - 8393(bx+a)^{\frac{9}{2}}a^2b^7 + 9216(bx+a)^{\frac{7}{2}}a^3b^7 - 5943(bx+a)^{\frac{5}{2}}a^4b^7 + 2100(bx+a)^{\frac{3}{2}}a^5b^7 - 315\sqrt{bx+a}a^6b^7}{35840\left((bx+a)^7a^2 - 7(bx+a)^6a^3 + 21(bx+a)^5a^4 - 35(bx+a)^4a^5 + 35(bx+a)^3a^6 - 21(bx+a)^2a^7 + 7(bx+a)a^8 - a^9\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(9/2)/x^8,x, algorithm="maxima")`

[Out] $9/2048*b^7*\log((\sqrt{b*x+a}-\sqrt{a})/(\sqrt{b*x+a}+\sqrt{a}))/a^{(5/2)} + 1/35840*(315*(b*x+a)^{(13/2)}*b^7 - 2100*(b*x+a)^{(11/2)}*a*b^7 - 8393*(b*x+a)^{(9/2)}*a^2*b^7 + 9216*(b*x+a)^{(7/2)}*a^3*b^7 - 5943*(b*x+a)^{(5/2)}*a^4*b^7 + 2100*(b*x+a)^{(3/2)}*a^5*b^7 - 315*\sqrt{b*x+a}*a^6*b^7)/((b*x+a)^7*a^2 - 7*(b*x+a)^6*a^3 + 21*(b*x+a)^5*a^4 - 35*(b*x+a)^4*a^5 + 35*(b*x+a)^3*a^6 - 21*(b*x+a)^2*a^7 + 7*(b*x+a)*a^8 - a^9)$

mupad [B] time = 0.13, size = 124, normalized size = 0.76

$$\frac{15a^3(a+bx)^{3/2}}{256x^7} - \frac{9a^4\sqrt{a+bx}}{1024x^7} - \frac{1199(a+bx)^{9/2}}{5120x^7} - \frac{849a^2(a+bx)^{5/2}}{5120x^7} - \frac{15(a+bx)^{11/2}}{256ax^7} + \frac{9(a+bx)^{13/2}}{1024a^2x^7} + \frac{9a(a+bx)^{9/2}}{35x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*x)^(9/2)/x^8,x)`

[Out] $(15*a^3*(a+b*x)^{(3/2)})/(256*x^7) - (9*a^4*(a+b*x)^{(1/2)})/(1024*x^7) - (1199*(a+b*x)^{(9/2)})/(5120*x^7) - (849*a^2*(a+b*x)^{(5/2)})/(5120*x^7) - (15*(a+b*x)^{(11/2)})/(256*a*x^7) + (9*(a+b*x)^{(13/2)})/(1024*a^2*x^7) + (9*a*(a+b*x)^{(9/2)})/(35*x^7)$

$\frac{7 \operatorname{atan}\left(\frac{(a + bx)^{1/2} i}{a^{1/2}}\right) i}{1024 a^{5/2}} + \frac{9 a (a + bx)^{7/2}}{35 x^7}$

sympy [A] time = 22.20, size = 236, normalized size = 1.45

$$\frac{a^5}{7\sqrt{b}x^{\frac{15}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{23a^4\sqrt{b}}{28x^{\frac{13}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{541a^3b^{\frac{3}{2}}}{280x^{\frac{11}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{5249a^2b^{\frac{5}{2}}}{2240x^{\frac{9}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{6653ab^{\frac{7}{2}}}{4480x^{\frac{7}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{1027b^{\frac{9}{2}}}{2560x^{\frac{5}{2}}\sqrt{\frac{a}{bx}+1}} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(9/2)/x**8,x)

[Out] $-a^{5/2}/(7\sqrt{b}x^{15/2}\sqrt{a/(bx)+1}) - 23a^{4/2}\sqrt{b}/(28x^{13/2}\sqrt{a/(bx)+1}) - 541a^{3/2}b^{3/2}/(280x^{11/2}\sqrt{a/(bx)+1}) - 5249a^{2/2}b^{5/2}/(2240x^{9/2}\sqrt{a/(bx)+1}) - 6653a^{1/2}b^{7/2}/(4480x^{7/2}\sqrt{a/(bx)+1}) - 1027b^{9/2}/(2560x^{5/2}\sqrt{a/(bx)+1}) + 3b^{11/2}/(1024ax^{3/2}\sqrt{a/(bx)+1}) + 9b^{13/2}/(1024a^2x\sqrt{a/(bx)+1}) - 9b^{7/2}\operatorname{asinh}(\sqrt{a}/(\sqrt{b}\sqrt{x}))/1024a^{5/2}$

$$3.325 \quad \int \frac{\sqrt{-a+bx}}{x} dx$$

Optimal. Leaf size=39

$$2\sqrt{bx-a} - 2\sqrt{a} \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)$$

[Out] $-2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})*a^{(1/2)}+2*(b*x-a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 63, 205}

$$2\sqrt{bx-a} - 2\sqrt{a} \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[-a + b*x]/x, x]

[Out] $2*\text{Sqrt}[-a + b*x] - 2*\text{Sqrt}[a]*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]]$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{-a+bx}}{x} dx &= 2\sqrt{-a+bx} - a \int \frac{1}{x\sqrt{-a+bx}} dx \\
&= 2\sqrt{-a+bx} - \frac{(2a) \operatorname{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx}\right)}{b} \\
&= 2\sqrt{-a+bx} - 2\sqrt{a} \tan^{-1}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 1.00

$$2\sqrt{bx-a} - 2\sqrt{a} \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[-a + b*x]/x,x]

[Out] 2*Sqrt[-a + b*x] - 2*Sqrt[a]*ArcTan[Sqrt[-a + b*x]/Sqrt[a]]

fricas [A] time = 0.54, size = 78, normalized size = 2.00

$$\left[\sqrt{-a} \log\left(\frac{bx - 2\sqrt{bx-a}\sqrt{-a} - 2a}{x}\right) + 2\sqrt{bx-a}, -2\sqrt{a} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2\sqrt{bx-a} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(1/2)/x,x, algorithm="fricas")

[Out] [sqrt(-a)*log((b*x - 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) + 2*sqrt(b*x - a), -2*sqrt(a)*arctan(sqrt(b*x - a)/sqrt(a)) + 2*sqrt(b*x - a)]

giac [A] time = 1.14, size = 31, normalized size = 0.79

$$-2\sqrt{a} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2\sqrt{bx-a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(1/2)/x,x, algorithm="giac")

[Out] -2*sqrt(a)*arctan(sqrt(b*x - a)/sqrt(a)) + 2*sqrt(b*x - a)

maple [A] time = 0.01, size = 32, normalized size = 0.82

$$-2\sqrt{a} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2\sqrt{bx-a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x-a)^(1/2)/x,x)

[Out] -2*arctan((b*x-a)^(1/2)/a^(1/2))*a^(1/2)+2*(b*x-a)^(1/2)

maxima [A] time = 2.94, size = 31, normalized size = 0.79

$$-2\sqrt{a} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2\sqrt{bx-a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(1/2)/x,x, algorithm="maxima")

[Out] -2*sqrt(a)*arctan(sqrt(b*x - a)/sqrt(a)) + 2*sqrt(b*x - a)

mupad [B] time = 0.09, size = 31, normalized size = 0.79

$$2\sqrt{bx-a} - 2\sqrt{a} \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x - a)^(1/2)/x,x)

[Out] 2*(b*x - a)^(1/2) - 2*a^(1/2)*atan((b*x - a)^(1/2)/a^(1/2))

sympy [B] time = 1.74, size = 148, normalized size = 3.79

$$\begin{cases} -2i\sqrt{a} \operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) + \frac{2ia}{\sqrt{b}\sqrt{x}\sqrt{\frac{a}{bx}-1}} - \frac{2i\sqrt{b}\sqrt{x}}{\sqrt{\frac{a}{bx}-1}} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ 2\sqrt{a} \operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) - \frac{2a}{\sqrt{b}\sqrt{x}\sqrt{-\frac{a}{bx}+1}} + \frac{2\sqrt{b}\sqrt{x}}{\sqrt{-\frac{a}{bx}+1}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)**(1/2)/x,x)

```
[Out] Piecewise((-2*I*sqrt(a)*acosh(sqrt(a)/(sqrt(b)*sqrt(x))) + 2*I*a/(sqrt(b)*sqrt(x)*sqrt(a/(b*x) - 1)) - 2*I*sqrt(b)*sqrt(x)/sqrt(a/(b*x) - 1), Abs(a/(b*x)) > 1), (2*sqrt(a)*asin(sqrt(a)/(sqrt(b)*sqrt(x))) - 2*a/(sqrt(b)*sqrt(x)*sqrt(-a/(b*x) + 1)) + 2*sqrt(b)*sqrt(x)/sqrt(-a/(b*x) + 1), True))
```

$$3.326 \quad \int \frac{\sqrt{-a+bx}}{x^2} dx$$

Optimal. Leaf size=42

$$\frac{b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}} - \frac{\sqrt{bx-a}}{x}$$

[Out] $b \arctan((b*x-a)^{(1/2)/a^{(1/2)})/a^{(1/2)} - (b*x-a)^{(1/2)}/x$

Rubi [A] time = 0.01, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 63, 205}

$$\frac{b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}} - \frac{\sqrt{bx-a}}{x}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[-a + b*x]/x^2,x]

[Out] $-(\text{Sqrt}[-a + b*x]/x) + (b*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]])/\text{Sqrt}[a]$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{-a+bx}}{x^2} dx &= -\frac{\sqrt{-a+bx}}{x} + \frac{1}{2}b \int \frac{1}{x\sqrt{-a+bx}} dx \\
&= -\frac{\sqrt{-a+bx}}{x} + \text{Subst} \left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx} \right) \\
&= -\frac{\sqrt{-a+bx}}{x} + \frac{b \tan^{-1} \left(\frac{\sqrt{-a+bx}}{\sqrt{a}} \right)}{\sqrt{a}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 52, normalized size = 1.24

$$\frac{-bx\sqrt{1-\frac{bx}{a}} \tanh^{-1} \left(\sqrt{1-\frac{bx}{a}} \right) + a - bx}{x\sqrt{bx-a}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[-a + b*x]/x^2,x]

[Out] (a - b*x - b*x*Sqrt[1 - (b*x)/a]*ArcTanh[Sqrt[1 - (b*x)/a]])/(x*Sqrt[-a + b*x])

fricas [A] time = 0.49, size = 98, normalized size = 2.33

$$\left[\frac{\sqrt{-a} bx \log \left(\frac{bx-2\sqrt{bx-a}\sqrt{-a}-2a}{x} \right) + 2\sqrt{bx-a} a}{2ax}, \frac{\sqrt{a} bx \arctan \left(\frac{\sqrt{bx-a}}{\sqrt{a}} \right) - \sqrt{bx-a} a}{ax} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(1/2)/x^2,x, algorithm="fricas")

[Out] [-1/2*(sqrt(-a)*b*x*log((b*x - 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) + 2*sqrt(b*x - a)*a)/(a*x), (sqrt(a)*b*x*arctan(sqrt(b*x - a)/sqrt(a)) - sqrt(b*x - a)*a)/(a*x)]

giac [A] time = 1.08, size = 41, normalized size = 0.98

$$\frac{\frac{b^2 \arctan \left(\frac{\sqrt{bx-a}}{\sqrt{a}} \right)}{\sqrt{a}} - \frac{\sqrt{bx-a} b}{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(1/2)/x^2,x, algorithm="giac")

[Out] (b^2*arctan(sqrt(b*x - a)/sqrt(a))/sqrt(a) - sqrt(b*x - a)*b/x)/b

maple [A] time = 0.01, size = 35, normalized size = 0.83

$$\frac{b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}} - \frac{\sqrt{bx-a}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x-a)^(1/2)/x^2,x)

[Out] b*arctan((b*x-a)^(1/2)/a^(1/2))/a^(1/2)-(b*x-a)^(1/2)/x

maxima [A] time = 2.94, size = 34, normalized size = 0.81

$$\frac{b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}} - \frac{\sqrt{bx-a}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(1/2)/x^2,x, algorithm="maxima")

[Out] b*arctan(sqrt(b*x - a)/sqrt(a))/sqrt(a) - sqrt(b*x - a)/x

mupad [B] time = 0.10, size = 34, normalized size = 0.81

$$\frac{b \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}} - \frac{\sqrt{bx-a}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x - a)^(1/2)/x^2,x)

[Out] (b*atan((b*x - a)^(1/2)/a^(1/2)))/a^(1/2) - (b*x - a)^(1/2)/x

sympy [A] time = 2.14, size = 121, normalized size = 2.88

$$\left\{ \begin{array}{l} -\frac{ia}{\sqrt{b}x^2\sqrt{\frac{a}{bx}-1}} + \frac{i\sqrt{b}}{\sqrt{x}\sqrt{\frac{a}{bx}-1}} + \frac{ib \operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{a}} \quad \text{for } \left|\frac{a}{bx}\right| > 1 \\ -\frac{\sqrt{b}\sqrt{-\frac{a}{bx}+1}}{\sqrt{x}} - \frac{b \operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{a}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x-a)**(1/2)/x**2,x)
```

```
[Out] Piecewise((-I*a/(sqrt(b)*x**(3/2)*sqrt(a/(b*x) - 1)) + I*sqrt(b)/(sqrt(x)*sqrt(a/(b*x) - 1)) + I*b*acosh(sqrt(a)/(sqrt(b)*sqrt(x)))/sqrt(a), Abs(a/(b*x)) > 1), (-sqrt(b)*sqrt(-a/(b*x) + 1)/sqrt(x) - b*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/sqrt(a), True))
```

$$3.327 \quad \int \frac{\sqrt{-a+bx}}{x^3} dx$$

Optimal. Leaf size=71

$$\frac{b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{3/2}} - \frac{\sqrt{bx-a}}{2x^2} + \frac{b\sqrt{bx-a}}{4ax}$$

[Out] $1/4*b^2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(3/2)}-1/2*(b*x-a)^{(1/2)}/x^2+1/4*b*(b*x-a)^{(1/2)}/a/x$

Rubi [A] time = 0.02, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 51, 63, 205}

$$\frac{b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{3/2}} - \frac{\sqrt{bx-a}}{2x^2} + \frac{b\sqrt{bx-a}}{4ax}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[-a + b*x]/x^3,x]

[Out] $-\text{Sqrt}[-a + b*x]/(2*x^2) + (b*\text{Sqrt}[-a + b*x])/(4*a*x) + (b^2*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]])/(4*a^{(3/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^(n), x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{-a+bx}}{x^3} dx &= -\frac{\sqrt{-a+bx}}{2x^2} + \frac{1}{4}b \int \frac{1}{x^2\sqrt{-a+bx}} dx \\ &= -\frac{\sqrt{-a+bx}}{2x^2} + \frac{b\sqrt{-a+bx}}{4ax} + \frac{b^2 \int \frac{1}{x\sqrt{-a+bx}} dx}{8a} \\ &= -\frac{\sqrt{-a+bx}}{2x^2} + \frac{b\sqrt{-a+bx}}{4ax} + \frac{b \operatorname{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx}\right)}{4a} \\ &= -\frac{\sqrt{-a+bx}}{2x^2} + \frac{b\sqrt{-a+bx}}{4ax} + \frac{b^2 \tan^{-1}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)}{4a^{3/2}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 38, normalized size = 0.54

$$\frac{2b^2(bx-a)^{3/2} {}_2F_1\left(\frac{3}{2}, 3; \frac{5}{2}; 1 - \frac{bx}{a}\right)}{3a^3}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[-a + b*x]/x^3, x]

[Out] (2*b^2*(-a + b*x)^(3/2)*Hypergeometric2F1[3/2, 3, 5/2, 1 - (b*x)/a])/(3*a^3)

fricas [A] time = 0.49, size = 124, normalized size = 1.75

$$\left[-\frac{\sqrt{-a} b^2 x^2 \log\left(\frac{bx-2\sqrt{bx-a}\sqrt{-a-2a}}{x}\right) - 2(abx-2a^2)\sqrt{bx-a}}{8a^2x^2}, \frac{\sqrt{a} b^2 x^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + (abx-2a^2)\sqrt{bx-a}}{4a^2x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(1/2)/x^3,x, algorithm="fricas")

[Out] $[-1/8*(\sqrt{-a})b^2x^2*\log((b*x - 2*\sqrt{b*x - a})*\sqrt{-a} - 2*a)/x) - 2*(a*b*x - 2*a^2)*\sqrt{b*x - a})/(a^2*x^2), 1/4*(\sqrt{a})b^2*x^2*\arctan(\sqrt{b*x - a}/\sqrt{a}) + (a*b*x - 2*a^2)*\sqrt{b*x - a})/(a^2*x^2)]$

giac [A] time = 1.08, size = 66, normalized size = 0.93

$$\frac{\frac{b^3 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{3}{2}}} + \frac{(bx-a)^{\frac{3}{2}}b^3 - \sqrt{bx-a}ab^3}{ab^2x^2}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(1/2)/x^3,x, algorithm="giac")

[Out] $1/4*(b^3*\arctan(\sqrt{b*x - a}/\sqrt{a}))/a^{(3/2)} + ((b*x - a)^{(3/2)}*b^3 - \sqrt{b*x - a}*a*b^3)/(a*b^2*x^2))/b$

maple [A] time = 0.01, size = 55, normalized size = 0.77

$$\frac{b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{\frac{3}{2}}} - \frac{\sqrt{bx-a}}{4x^2} + \frac{(bx-a)^{\frac{3}{2}}}{4ax^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x-a)^(1/2)/x^3,x)

[Out] $1/4/x^2/a*(b*x-a)^{(3/2)}-1/4*(b*x-a)^{(1/2)}/x^2+1/4*b^2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(3/2)}$

maxima [A] time = 2.96, size = 83, normalized size = 1.17

$$\frac{b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{\frac{3}{2}}} + \frac{(bx-a)^{\frac{3}{2}}b^2 - \sqrt{bx-a}ab^2}{4((bx-a)^2a + 2(bx-a)a^2 + a^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(1/2)/x^3,x, algorithm="maxima")

[Out] $1/4*b^2*\arctan(\sqrt{b*x - a}/\sqrt{a}))/a^{(3/2)} + 1/4*((b*x - a)^{(3/2)}*b^2 - \sqrt{b*x - a}*a*b^2)/((b*x - a)^2*a + 2*(b*x - a)*a^2 + a^3)$

mupad [B] time = 0.10, size = 54, normalized size = 0.76

$$\frac{b^2 \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{3/2}} - \frac{\sqrt{bx-a}}{4x^2} + \frac{(bx-a)^{3/2}}{4ax^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x - a)^(1/2)/x^3,x)`

[Out] $(b^2 \operatorname{atan}((b*x - a)^{(1/2)}/a^{(1/2)}))/(4*a^{(3/2)}) - (b*x - a)^{(1/2)}/(4*x^2) + (b*x - a)^{(3/2)}/(4*a*x^2)$

sympy [A] time = 4.16, size = 207, normalized size = 2.92

$$\begin{cases} -\frac{ia}{2\sqrt{b}x^2\sqrt{\frac{a}{bx}-1}} + \frac{3i\sqrt{b}}{4x^2\sqrt{\frac{a}{bx}-1}} - \frac{ib^{\frac{3}{2}}}{4a\sqrt{x}\sqrt{\frac{a}{bx}-1}} + \frac{ib^2 \operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4a^{\frac{3}{2}}} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ \frac{a}{2\sqrt{b}x^2\sqrt{-\frac{a}{bx}+1}} - \frac{3\sqrt{b}}{4x^2\sqrt{-\frac{a}{bx}+1}} + \frac{b^{\frac{3}{2}}}{4a\sqrt{x}\sqrt{-\frac{a}{bx}+1}} - \frac{b^2 \operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4a^{\frac{3}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x-a)**(1/2)/x**3,x)`

[Out] `Piecewise((-I*a/(2*sqrt(b)*x**(5/2)*sqrt(a/(b*x) - 1)) + 3*I*sqrt(b)/(4*x**(3/2)*sqrt(a/(b*x) - 1)) - I*b**(3/2)/(4*a*sqrt(x)*sqrt(a/(b*x) - 1)) + I*b**2*acosh(sqrt(a)/(sqrt(b)*sqrt(x)))/(4*a**(3/2)), Abs(a/(b*x)) > 1), (a/(2*sqrt(b)*x**(5/2)*sqrt(-a/(b*x) + 1)) - 3*sqrt(b)/(4*x**(3/2)*sqrt(-a/(b*x) + 1)) + b**(3/2)/(4*a*sqrt(x)*sqrt(-a/(b*x) + 1)) - b**2*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/(4*a**(3/2)), True))`

$$3.328 \quad \int \frac{(-a+bx)^{3/2}}{x} dx$$

Optimal. Leaf size=55

$$2a^{3/2} \tan^{-1} \left(\frac{\sqrt{bx-a}}{\sqrt{a}} \right) - 2a\sqrt{bx-a} + \frac{2}{3}(bx-a)^{3/2}$$

[Out] $2/3*(b*x-a)^{(3/2)}+2*a^{(3/2)}*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})-2*a*(b*x-a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 55, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 63, 205}

$$2a^{3/2} \tan^{-1} \left(\frac{\sqrt{bx-a}}{\sqrt{a}} \right) - 2a\sqrt{bx-a} + \frac{2}{3}(bx-a)^{3/2}$$

Antiderivative was successfully verified.

[In] Int[(-a + b*x)^(3/2)/x,x]

[Out] $-2*a*\text{Sqrt}[-a + b*x] + (2*(-a + b*x)^{(3/2)})/3 + 2*a^{(3/2)}*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]]$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
\int \frac{(-a + bx)^{3/2}}{x} dx &= \frac{2}{3}(-a + bx)^{3/2} - a \int \frac{\sqrt{-a + bx}}{x} dx \\
&= -2a\sqrt{-a + bx} + \frac{2}{3}(-a + bx)^{3/2} + a^2 \int \frac{1}{x\sqrt{-a + bx}} dx \\
&= -2a\sqrt{-a + bx} + \frac{2}{3}(-a + bx)^{3/2} + \frac{(2a^2) \text{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a + bx}\right)}{b} \\
&= -2a\sqrt{-a + bx} + \frac{2}{3}(-a + bx)^{3/2} + 2a^{3/2} \tan^{-1}\left(\frac{\sqrt{-a + bx}}{\sqrt{a}}\right)
\end{aligned}$$

Mathematica [A] time = 0.02, size = 48, normalized size = 0.87

$$2a^{3/2} \tan^{-1}\left(\frac{\sqrt{bx - a}}{\sqrt{a}}\right) + \frac{2}{3}(bx - 4a)\sqrt{bx - a}$$

Antiderivative was successfully verified.

[In] Integrate[(-a + b*x)^(3/2)/x,x]

[Out] (2*(-4*a + b*x)*Sqrt[-a + b*x])/3 + 2*a^(3/2)*ArcTan[Sqrt[-a + b*x]/Sqrt[a]]

fricas [A] time = 0.52, size = 93, normalized size = 1.69

$$\left[\sqrt{-a} a \log\left(\frac{bx + 2\sqrt{bx - a}\sqrt{-a} - 2a}{x}\right) + \frac{2}{3}\sqrt{bx - a}(bx - 4a), 2a^{3/2} \arctan\left(\frac{\sqrt{bx - a}}{\sqrt{a}}\right) + \frac{2}{3}\sqrt{bx - a}(bx - 4a) \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(3/2)/x,x, algorithm="fricas")

[Out] [sqrt(-a)*a*log((b*x + 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) + 2/3*sqrt(b*x - a)*(b*x - 4*a), 2*a^(3/2)*arctan(sqrt(b*x - a)/sqrt(a)) + 2/3*sqrt(b*x - a)*(b*x - 4*a)]

giac [A] time = 1.06, size = 43, normalized size = 0.78

$$2a^{3/2} \arctan\left(\frac{\sqrt{bx - a}}{\sqrt{a}}\right) + \frac{2}{3}(bx - a)^{3/2} - 2\sqrt{bx - a}a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(3/2)/x,x, algorithm="giac")

[Out] $2*a^{3/2}*arctan(\sqrt{b*x - a}/\sqrt{a}) + 2/3*(b*x - a)^{3/2} - 2*\sqrt{b*x - a}*a$

maple [A] time = 0.01, size = 44, normalized size = 0.80

$$2a^{\frac{3}{2}} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - 2\sqrt{bx-a}a + \frac{2(bx-a)^{\frac{3}{2}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x-a)^(3/2)/x,x)

[Out] $2/3*(b*x-a)^{3/2}+2*a^{3/2}*arctan((b*x-a)^{1/2}/a^{1/2})-2*a*(b*x-a)^{1/2}$

maxima [A] time = 3.02, size = 43, normalized size = 0.78

$$2a^{\frac{3}{2}} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + \frac{2}{3}(bx-a)^{\frac{3}{2}} - 2\sqrt{bx-a}a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(3/2)/x,x, algorithm="maxima")

[Out] $2*a^{3/2}*arctan(\sqrt{b*x - a}/\sqrt{a}) + 2/3*(b*x - a)^{3/2} - 2*\sqrt{b*x - a}*a$

mupad [B] time = 0.04, size = 43, normalized size = 0.78

$$2a^{3/2} \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - 2a\sqrt{bx-a} + \frac{2(bx-a)^{3/2}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x - a)^(3/2)/x,x)

[Out] $2*a^{3/2}*atan((b*x - a)^{1/2}/a^{1/2}) - 2*a*(b*x - a)^{1/2} + (2*(b*x - a)^{3/2})/3$

sympy [C] time = 2.46, size = 187, normalized size = 3.40

$$\left\{ \begin{array}{ll} -\frac{8a^{\frac{3}{2}}\sqrt{-1+\frac{bx}{a}}}{3} - ia^{\frac{3}{2}}\log\left(\frac{bx}{a}\right) + 2ia^{\frac{3}{2}}\log\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) - 2a^{\frac{3}{2}}\operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) + \frac{2\sqrt{a}bx\sqrt{-1+\frac{bx}{a}}}{3} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{8ia^{\frac{3}{2}}\sqrt{1-\frac{bx}{a}}}{3} - ia^{\frac{3}{2}}\log\left(\frac{bx}{a}\right) + 2ia^{\frac{3}{2}}\log\left(\sqrt{1-\frac{bx}{a}} + 1\right) + \frac{2i\sqrt{a}bx\sqrt{1-\frac{bx}{a}}}{3} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)**(3/2)/x,x)

[Out] Piecewise((-8*a**(3/2)*sqrt(-1 + b*x/a)/3 - I*a**(3/2)*log(b*x/a) + 2*I*a**(3/2)*log(sqrt(b)*sqrt(x)/sqrt(a)) - 2*a**(3/2)*asin(sqrt(a)/(sqrt(b)*sqrt(x))) + 2*sqrt(a)*b*x*sqrt(-1 + b*x/a)/3, Abs(b*x/a) > 1), (-8*I*a**(3/2)*sqrt(1 - b*x/a)/3 - I*a**(3/2)*log(b*x/a) + 2*I*a**(3/2)*log(sqrt(1 - b*x/a) + 1) + 2*I*sqrt(a)*b*x*sqrt(1 - b*x/a)/3, True))

$$3.329 \quad \int \frac{(-a+bx)^{3/2}}{x^2} dx$$

Optimal. Leaf size=57

$$-\frac{(bx-a)^{3/2}}{x} + 3b\sqrt{bx-a} - 3\sqrt{a}b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)$$

[Out] $-(b*x-a)^{(3/2)}/x-3*b*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})*a^{(1/2)}+3*b*(b*x-a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 63, 205}

$$-\frac{(bx-a)^{3/2}}{x} + 3b\sqrt{bx-a} - 3\sqrt{a}b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)$$

Antiderivative was successfully verified.

[In] Int[(-a + b*x)^(3/2)/x^2,x]

[Out] $3*b*\text{Sqrt}[-a + b*x] - (-a + b*x)^{(3/2)}/x - 3*\text{Sqrt}[a]*b*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^(n), x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(-a + bx)^{3/2}}{x^2} dx &= -\frac{(-a + bx)^{3/2}}{x} + \frac{1}{2}(3b) \int \frac{\sqrt{-a + bx}}{x} dx \\
&= 3b\sqrt{-a + bx} - \frac{(-a + bx)^{3/2}}{x} - \frac{1}{2}(3ab) \int \frac{1}{x\sqrt{-a + bx}} dx \\
&= 3b\sqrt{-a + bx} - \frac{(-a + bx)^{3/2}}{x} - (3a) \operatorname{Subst} \left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a + bx} \right) \\
&= 3b\sqrt{-a + bx} - \frac{(-a + bx)^{3/2}}{x} - 3\sqrt{a}b \tan^{-1} \left(\frac{\sqrt{-a + bx}}{\sqrt{a}} \right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 36, normalized size = 0.63

$$\frac{2b(bx - a)^{5/2} {}_2F_1\left(2, \frac{5}{2}; \frac{7}{2}; 1 - \frac{bx}{a}\right)}{5a^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(-a + b*x)^(3/2)/x^2, x]
```

```
[Out] (2*b*(-a + b*x)^(5/2)*Hypergeometric2F1[2, 5/2, 7/2, 1 - (b*x)/a])/(5*a^2)
```

fricas [A] time = 0.48, size = 105, normalized size = 1.84

$$\left[\frac{3\sqrt{-a}bx \log\left(\frac{bx-2\sqrt{bx-a}\sqrt{-a}-2a}{x}\right) + 2(2bx+a)\sqrt{bx-a}}{2x}, -\frac{3\sqrt{a}bx \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - (2bx+a)\sqrt{bx-a}}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(3/2)/x^2,x, algorithm="fricas")

[Out] [1/2*(3*sqrt(-a)*b*x*log((b*x - 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) + 2*(2*b*x + a)*sqrt(b*x - a))/x, -(3*sqrt(a)*b*x*arctan(sqrt(b*x - a)/sqrt(a)) - (2*b*x + a)*sqrt(b*x - a))/x]

giac [A] time = 0.96, size = 58, normalized size = 1.02

$$\frac{3\sqrt{a}b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - 2\sqrt{bx-a}b^2 - \frac{\sqrt{bx-a}ab}{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(3/2)/x^2,x, algorithm="giac")

[Out] -(3*sqrt(a)*b^2*arctan(sqrt(b*x - a)/sqrt(a)) - 2*sqrt(b*x - a)*b^2 - sqrt(b*x - a)*a*b/x)/b

maple [A] time = 0.01, size = 48, normalized size = 0.84

$$-3\sqrt{a}b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2\sqrt{bx-a}b + \frac{\sqrt{bx-a}a}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x-a)^(3/2)/x^2,x)

[Out] 2*b*(b*x-a)^(1/2)+a*(b*x-a)^(1/2)/x-3*b*arctan((b*x-a)^(1/2)/a^(1/2))*a^(1/2)

maxima [A] time = 3.00, size = 47, normalized size = 0.82

$$-3\sqrt{a}b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2\sqrt{bx-a}b + \frac{\sqrt{bx-a}a}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(3/2)/x^2,x, algorithm="maxima")

[Out] -3*sqrt(a)*b*arctan(sqrt(b*x - a)/sqrt(a)) + 2*sqrt(b*x - a)*b + sqrt(b*x - a)*a/x

mupad [B] time = 0.04, size = 47, normalized size = 0.82

$$2b\sqrt{bx-a} + \frac{a\sqrt{bx-a}}{x} - 3\sqrt{a}b \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x - a)^(3/2)/x^2,x)`

[Out] $2*b*(b*x - a)^{(1/2)} + (a*(b*x - a)^{(1/2)})/x - 3*a^{(1/2)}*b*\operatorname{atan}((b*x - a)^{(1/2)}/a^{(1/2)})$

sympy [B] time = 2.84, size = 197, normalized size = 3.46

$$\begin{cases} -3i\sqrt{a}b \operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) + \frac{ia^2}{\sqrt{b}x^2\sqrt{\frac{a}{bx}-1}} + \frac{ia\sqrt{b}}{\sqrt{x}\sqrt{\frac{a}{bx}-1}} - \frac{2ib^{\frac{3}{2}}\sqrt{x}}{\sqrt{\frac{a}{bx}-1}} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ 3\sqrt{a}b \operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) - \frac{a^2}{\sqrt{b}x^2\sqrt{-\frac{a}{bx}+1}} - \frac{a\sqrt{b}}{\sqrt{x}\sqrt{-\frac{a}{bx}+1}} + \frac{2b^{\frac{3}{2}}\sqrt{x}}{\sqrt{-\frac{a}{bx}+1}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x-a)**(3/2)/x**2,x)`

[Out] `Piecewise((-3*I*sqrt(a)*b*acosh(sqrt(a)/(sqrt(b)*sqrt(x))) + I*a**2/(sqrt(b)*x**(3/2)*sqrt(a/(b*x) - 1)) + I*a*sqrt(b)/(sqrt(x)*sqrt(a/(b*x) - 1)) - 2*I*b**(3/2)*sqrt(x)/sqrt(a/(b*x) - 1), Abs(a/(b*x)) > 1), (3*sqrt(a)*b*asin(sqrt(a)/(sqrt(b)*sqrt(x))) - a**2/(sqrt(b)*x**(3/2)*sqrt(-a/(b*x) + 1)) - a*sqrt(b)/(sqrt(x)*sqrt(-a/(b*x) + 1)) + 2*b**(3/2)*sqrt(x)/sqrt(-a/(b*x) + 1), True))`

$$3.330 \quad \int \frac{(-a+bx)^{3/2}}{x^3} dx$$

Optimal. Leaf size=68

$$\frac{3b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4\sqrt{a}} - \frac{(bx-a)^{3/2}}{2x^2} - \frac{3b\sqrt{bx-a}}{4x}$$

[Out] $-1/2*(b*x-a)^{(3/2)}/x^2+3/4*b^2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(1/2)}-3/4*b*(b*x-a)^{(1/2)}/x$

Rubi [A] time = 0.01, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 63, 205}

$$\frac{3b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4\sqrt{a}} - \frac{(bx-a)^{3/2}}{2x^2} - \frac{3b\sqrt{bx-a}}{4x}$$

Antiderivative was successfully verified.

[In] Int[(-a + b*x)^(3/2)/x^3, x]

[Out] $(-3*b*\text{Sqrt}[-a + b*x])/(4*x) - (-a + b*x)^{(3/2)}/(2*x^2) + (3*b^2*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]])/(4*\text{Sqrt}[a])$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(-a+bx)^{3/2}}{x^3} dx &= -\frac{(-a+bx)^{3/2}}{2x^2} + \frac{1}{4}(3b) \int \frac{\sqrt{-a+bx}}{x^2} dx \\
 &= -\frac{3b\sqrt{-a+bx}}{4x} - \frac{(-a+bx)^{3/2}}{2x^2} + \frac{1}{8}(3b^2) \int \frac{1}{x\sqrt{-a+bx}} dx \\
 &= -\frac{3b\sqrt{-a+bx}}{4x} - \frac{(-a+bx)^{3/2}}{2x^2} + \frac{1}{4}(3b) \operatorname{Subst} \left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx} \right) \\
 &= -\frac{3b\sqrt{-a+bx}}{4x} - \frac{(-a+bx)^{3/2}}{2x^2} + \frac{3b^2 \tan^{-1} \left(\frac{\sqrt{-a+bx}}{\sqrt{a}} \right)}{4\sqrt{a}}
 \end{aligned}$$

Mathematica [A] time = 0.03, size = 72, normalized size = 1.06

$$\frac{2a^2 + 3b^2x^2\sqrt{1-\frac{bx}{a}} \tanh^{-1} \left(\sqrt{1-\frac{bx}{a}} \right) - 7abx + 5b^2x^2}{4x^2\sqrt{bx-a}}$$

Antiderivative was successfully verified.

[In] Integrate[(-a + b*x)^(3/2)/x^3, x]

[Out] -1/4*(2*a^2 - 7*a*b*x + 5*b^2*x^2 + 3*b^2*x^2*Sqrt[1 - (b*x)/a]*ArcTanh[Sqrt[1 - (b*x)/a]])/(x^2*Sqrt[-a + b*x])

fricas [A] time = 0.52, size = 129, normalized size = 1.90

$$\left[\frac{3\sqrt{-a}b^2x^2 \log\left(\frac{bx-2\sqrt{bx-a}\sqrt{-a}-2a}{x}\right) + 2(5abx-2a^2)\sqrt{bx-a}}{8ax^2}, \frac{3\sqrt{a}b^2x^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - (5abx-2a^2)\sqrt{bx-a}}{4ax^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(3/2)/x^3, x, algorithm="fricas")

[Out] [-1/8*(3*sqrt(-a)*b^2*x^2*log((b*x - 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) + 2*(5*a*b*x - 2*a^2)*sqrt(b*x - a))/(a*x^2), 1/4*(3*sqrt(a)*b^2*x^2*arctan(sqrt(b*x - a)/sqrt(a)) - (5*a*b*x - 2*a^2)*sqrt(b*x - a))/(a*x^2)]

giac [A] time = 0.95, size = 66, normalized size = 0.97

$$\frac{\frac{3b^3 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}} - \frac{5(bx-a)^{\frac{3}{2}}b^3 + 3\sqrt{bx-a}ab^3}{b^2x^2}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(3/2)/x^3,x, algorithm="giac")

[Out] 1/4*(3*b^3*arctan(sqrt(b*x - a)/sqrt(a))/sqrt(a) - (5*(b*x - a)^(3/2)*b^3 + 3*sqrt(b*x - a)*a*b^3)/(b^2*x^2))/b

maple [A] time = 0.01, size = 53, normalized size = 0.78

$$\frac{3b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4\sqrt{a}} - \frac{3\sqrt{bx-a}a}{4x^2} - \frac{5(bx-a)^{\frac{3}{2}}}{4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x-a)^(3/2)/x^3,x)

[Out] -5/4*(b*x-a)^(3/2)/x^2-3/4/x^2*(b*x-a)^(1/2)*a+3/4*b^2*arctan((b*x-a)^(1/2)/a^(1/2))/a^(1/2)

maxima [A] time = 3.02, size = 80, normalized size = 1.18

$$\frac{3b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4\sqrt{a}} - \frac{5(bx-a)^{\frac{3}{2}}b^2 + 3\sqrt{bx-a}ab^2}{4((bx-a)^2 + 2(bx-a)a + a^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(3/2)/x^3,x, algorithm="maxima")

[Out] 3/4*b^2*arctan(sqrt(b*x - a)/sqrt(a))/sqrt(a) - 1/4*(5*(b*x - a)^(3/2)*b^2 + 3*sqrt(b*x - a)*a*b^2)/((b*x - a)^2 + 2*(b*x - a)*a + a^2)

mupad [B] time = 0.10, size = 52, normalized size = 0.76

$$\frac{3b^2 \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4\sqrt{a}} - \frac{5(bx-a)^{3/2}}{4x^2} - \frac{3a\sqrt{bx-a}}{4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((b*x - a)^(3/2)/x^3,x)
```

```
[Out] (3*b^2*atan((b*x - a)^(1/2)/a^(1/2)))/(4*a^(1/2)) - (5*(b*x - a)^(3/2))/(4*x^2) - (3*a*(b*x - a)^(1/2))/(4*x^2)
```

sympy [A] time = 3.30, size = 190, normalized size = 2.79

$$\left\{ \begin{array}{ll} \frac{ia^2}{2\sqrt{b}x^2\sqrt{\frac{a}{bx}-1}} - \frac{7ia\sqrt{b}}{4x^2\sqrt{\frac{a}{bx}-1}} + \frac{5ib^{\frac{3}{2}}}{4\sqrt{x}\sqrt{\frac{a}{bx}-1}} + \frac{3ib^2\operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4\sqrt{a}} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ \frac{a\sqrt{b}\sqrt{-\frac{a}{bx}+1}}{2x^{\frac{3}{2}}} - \frac{5b^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}}{4\sqrt{x}} - \frac{3b^2\operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4\sqrt{a}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x-a)**(3/2)/x**3,x)
```

```
[Out] Piecewise((I*a**2/(2*sqrt(b)*x**(5/2)*sqrt(a/(b*x) - 1)) - 7*I*a*sqrt(b)/(4*x**(3/2)*sqrt(a/(b*x) - 1)) + 5*I*b**(3/2)/(4*sqrt(x)*sqrt(a/(b*x) - 1)) + 3*I*b**2*acosh(sqrt(a)/(sqrt(b)*sqrt(x)))/(4*sqrt(a)), Abs(a/(b*x)) > 1), (a*sqrt(b)*sqrt(-a/(b*x) + 1)/(2*x**(3/2)) - 5*b**(3/2)*sqrt(-a/(b*x) + 1)/(4*sqrt(x)) - 3*b**2*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/(4*sqrt(a)), True))
```

$$3.331 \quad \int \frac{(-a+bx)^{5/2}}{x} dx$$

Optimal. Leaf size=73

$$-2a^{5/2} \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2a^2\sqrt{bx-a} - \frac{2}{3}a(bx-a)^{3/2} + \frac{2}{5}(bx-a)^{5/2}$$

[Out] $-2/3*a*(b*x-a)^{(3/2)}+2/5*(b*x-a)^{(5/2)}-2*a^{(5/2)}*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})+2*a^2*(b*x-a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 73, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 63, 205}

$$2a^2\sqrt{bx-a} - 2a^{5/2} \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - \frac{2}{3}a(bx-a)^{3/2} + \frac{2}{5}(bx-a)^{5/2}$$

Antiderivative was successfully verified.

[In] Int[(-a + b*x)^(5/2)/x,x]

[Out] $2*a^2*\text{Sqrt}[-a + b*x] - (2*a*(-a + b*x)^{(3/2)})/3 + (2*(-a + b*x)^{(5/2)})/5 - 2*a^{(5/2)}*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]]$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(-a+bx)^{5/2}}{x} dx &= \frac{2}{5}(-a+bx)^{5/2} - a \int \frac{(-a+bx)^{3/2}}{x} dx \\
 &= -\frac{2}{3}a(-a+bx)^{3/2} + \frac{2}{5}(-a+bx)^{5/2} + a^2 \int \frac{\sqrt{-a+bx}}{x} dx \\
 &= 2a^2\sqrt{-a+bx} - \frac{2}{3}a(-a+bx)^{3/2} + \frac{2}{5}(-a+bx)^{5/2} - a^3 \int \frac{1}{x\sqrt{-a+bx}} dx \\
 &= 2a^2\sqrt{-a+bx} - \frac{2}{3}a(-a+bx)^{3/2} + \frac{2}{5}(-a+bx)^{5/2} - \frac{(2a^3) \text{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx}\right)}{b} \\
 &= 2a^2\sqrt{-a+bx} - \frac{2}{3}a(-a+bx)^{3/2} + \frac{2}{5}(-a+bx)^{5/2} - 2a^{5/2} \tan^{-1}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)
 \end{aligned}$$

Mathematica [A] time = 0.03, size = 60, normalized size = 0.82

$$\frac{2}{15}\sqrt{bx-a}(23a^2-11abx+3b^2x^2)-2a^{5/2}\tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(-a + b*x)^(5/2)/x, x]

[Out] (2*Sqrt[-a + b*x]*(23*a^2 - 11*a*b*x + 3*b^2*x^2))/15 - 2*a^(5/2)*ArcTan[Sqrt[-a + b*x]/Sqrt[a]]

fricas [A] time = 0.53, size = 119, normalized size = 1.63

$$\left[\sqrt{-a}a^2\log\left(\frac{bx-2\sqrt{bx-a}\sqrt{-a}-2a}{x}\right)+\frac{2}{15}(3b^2x^2-11abx+23a^2)\sqrt{bx-a}, -2a^{\frac{5}{2}}\arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)+\frac{2}{15}\right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(5/2)/x, x, algorithm="fricas")

[Out] [sqrt(-a)*a^2*log((b*x - 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) + 2/15*(3*b^2*x^2 - 11*a*b*x + 23*a^2)*sqrt(b*x - a), -2*a^(5/2)*arctan(sqrt(b*x - a)/sqrt(a)) + 2/15*(3*b^2*x^2 - 11*a*b*x + 23*a^2)*sqrt(b*x - a)]

giac [A] time = 1.22, size = 57, normalized size = 0.78

$$-2a^{\frac{5}{2}} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + \frac{2}{5}(bx-a)^{\frac{5}{2}} - \frac{2}{3}(bx-a)^{\frac{3}{2}}a + 2\sqrt{bx-a}a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(5/2)/x,x, algorithm="giac")

[Out] $-2*a^{(5/2)}*\arctan(\text{sqrt}(b*x - a)/\text{sqrt}(a)) + 2/5*(b*x - a)^{(5/2)} - 2/3*(b*x - a)^{(3/2)}*a + 2*\text{sqrt}(b*x - a)*a^2$

maple [A] time = 0.01, size = 58, normalized size = 0.79

$$-2a^{\frac{5}{2}} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2\sqrt{bx-a}a^2 - \frac{2(bx-a)^{\frac{3}{2}}a}{3} + \frac{2(bx-a)^{\frac{5}{2}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x-a)^(5/2)/x,x)

[Out] $-2/3*a*(b*x-a)^{(3/2)}+2/5*(b*x-a)^{(5/2)}-2*a^{(5/2)}*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})+2*a^2*(b*x-a)^{(1/2)}$

maxima [A] time = 2.92, size = 57, normalized size = 0.78

$$-2a^{\frac{5}{2}} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + \frac{2}{5}(bx-a)^{\frac{5}{2}} - \frac{2}{3}(bx-a)^{\frac{3}{2}}a + 2\sqrt{bx-a}a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(5/2)/x,x, algorithm="maxima")

[Out] $-2*a^{(5/2)}*\arctan(\text{sqrt}(b*x - a)/\text{sqrt}(a)) + 2/5*(b*x - a)^{(5/2)} - 2/3*(b*x - a)^{(3/2)}*a + 2*\text{sqrt}(b*x - a)*a^2$

mupad [B] time = 0.04, size = 57, normalized size = 0.78

$$\frac{2(bx-a)^{5/2}}{5} - \frac{2a(bx-a)^{3/2}}{3} - 2a^{5/2} \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2a^2\sqrt{bx-a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x - a)^(5/2)/x,x)

[Out] $(2*(b*x - a)^{(5/2)})/5 - (2*a*(b*x - a)^{(3/2)})/3 - 2*a^{(5/2)}*atan((b*x - a)^{(1/2)}/a^{(1/2)}) + 2*a^2*(b*x - a)^{(1/2)}$

sympy [C] time = 4.24, size = 240, normalized size = 3.29

$$\left\{ \begin{array}{l} \frac{46a^{\frac{5}{2}}\sqrt{-1+\frac{bx}{a}}}{15} + ia^{\frac{5}{2}}\log\left(\frac{bx}{a}\right) - 2ia^{\frac{5}{2}}\log\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) + 2a^{\frac{5}{2}}\operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) - \frac{22a^{\frac{3}{2}}bx\sqrt{-1+\frac{bx}{a}}}{15} + \frac{2\sqrt{a}b^2x^2\sqrt{-1+\frac{bx}{a}}}{5} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ \frac{46ia^{\frac{5}{2}}\sqrt{1-\frac{bx}{a}}}{15} + ia^{\frac{5}{2}}\log\left(\frac{bx}{a}\right) - 2ia^{\frac{5}{2}}\log\left(\sqrt{1-\frac{bx}{a}} + 1\right) - \frac{22ia^{\frac{3}{2}}bx\sqrt{1-\frac{bx}{a}}}{15} + \frac{2i\sqrt{a}b^2x^2\sqrt{1-\frac{bx}{a}}}{5} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x-a)**(5/2)/x,x)`

[Out] `Piecewise((46*a**(5/2)*sqrt(-1 + b*x/a)/15 + I*a**(5/2)*log(b*x/a) - 2*I*a**
*(5/2)*log(sqrt(b)*sqrt(x)/sqrt(a)) + 2*a**(5/2)*asin(sqrt(a)/(sqrt(b)*sqrt
(x))) - 22*a**(3/2)*b*x*sqrt(-1 + b*x/a)/15 + 2*sqrt(a)*b**2*x**2*sqrt(-1 +
b*x/a)/5, Abs(b*x/a) > 1), (46*I*a**(5/2)*sqrt(1 - b*x/a)/15 + I*a**(5/2)*
log(b*x/a) - 2*I*a**(5/2)*log(sqrt(1 - b*x/a) + 1) - 22*I*a**(3/2)*b*x*sqrt
(1 - b*x/a)/15 + 2*I*sqrt(a)*b**2*x**2*sqrt(1 - b*x/a)/5, True))`

$$3.332 \quad \int \frac{(-a+bx)^{5/2}}{x^2} dx$$

Optimal. Leaf size=74

$$5a^{3/2}b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - \frac{(bx-a)^{5/2}}{x} + \frac{5}{3}b(bx-a)^{3/2} - 5ab\sqrt{bx-a}$$

[Out] $5/3*b*(b*x-a)^{(3/2)}-(b*x-a)^{(5/2)}/x+5*a^{(3/2)}*b*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})-5*a*b*(b*x-a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 63, 205}

$$5a^{3/2}b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - \frac{(bx-a)^{5/2}}{x} + \frac{5}{3}b(bx-a)^{3/2} - 5ab\sqrt{bx-a}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(-a + b*x)^{(5/2)}/x^2, x]$

[Out] $-5*a*b*\text{Sqrt}[-a + b*x] + (5*b*(-a + b*x)^{(3/2)})/3 - (-a + b*x)^{(5/2)}/x + 5*a^{(3/2)}*b*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]]$

Rule 47

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \text{Dist}[(d*n)/(b*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(-a + bx)^{5/2}}{x^2} dx &= -\frac{(-a + bx)^{5/2}}{x} + \frac{1}{2}(5b) \int \frac{(-a + bx)^{3/2}}{x} dx \\
&= \frac{5}{3}b(-a + bx)^{3/2} - \frac{(-a + bx)^{5/2}}{x} - \frac{1}{2}(5ab) \int \frac{\sqrt{-a + bx}}{x} dx \\
&= -5ab\sqrt{-a + bx} + \frac{5}{3}b(-a + bx)^{3/2} - \frac{(-a + bx)^{5/2}}{x} + \frac{1}{2}(5a^2b) \int \frac{1}{x\sqrt{-a + bx}} dx \\
&= -5ab\sqrt{-a + bx} + \frac{5}{3}b(-a + bx)^{3/2} - \frac{(-a + bx)^{5/2}}{x} + (5a^2) \text{Subst} \left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a + bx} \right) \\
&= -5ab\sqrt{-a + bx} + \frac{5}{3}b(-a + bx)^{3/2} - \frac{(-a + bx)^{5/2}}{x} + 5a^{3/2}b \tan^{-1} \left(\frac{\sqrt{-a + bx}}{\sqrt{a}} \right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 36, normalized size = 0.49

$$\frac{2b(bx - a)^{7/2} {}_2F_1\left(2, \frac{7}{2}; \frac{9}{2}; 1 - \frac{bx}{a}\right)}{7a^2}$$

Antiderivative was successfully verified.

[In] Integrate[(-a + b*x)^(5/2)/x^2, x]

[Out] (2*b*(-a + b*x)^(7/2)*Hypergeometric2F1[2, 7/2, 9/2, 1 - (b*x)/a])/(7*a^2)

fricas [A] time = 0.50, size = 131, normalized size = 1.77

$$\left[\frac{15\sqrt{-a} abx \log\left(\frac{bx+2\sqrt{bx-a}\sqrt{-a-2a}}{x}\right) + 2(2b^2x^2 - 14abx - 3a^2)\sqrt{bx-a}}{6x}, \frac{15a^{\frac{3}{2}}bx \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + (2b^2x^2 - 14abx - 3a^2)\sqrt{bx-a}}{3x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(5/2)/x^2,x, algorithm="fricas")

[Out] $\frac{1}{6}*(15*\sqrt{-a})*a*b*x*\log((b*x + 2*\sqrt{b*x - a})*\sqrt{-a} - 2*a)/x + 2*(2*b^2*x^2 - 14*a*b*x - 3*a^2)*\sqrt{b*x - a})/x, \frac{1}{3}*(15*a^{(3/2)}*b*x*\arctan(\sqrt{b*x - a}/\sqrt{a}) + (2*b^2*x^2 - 14*a*b*x - 3*a^2)*\sqrt{b*x - a})/x]$

giac [A] time = 1.02, size = 75, normalized size = 1.01

$$\frac{15 a^{\frac{3}{2}} b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2 (bx-a)^{\frac{3}{2}} b^2 - 12 \sqrt{bx-a} ab^2 - \frac{3 \sqrt{bx-a} a^2 b}{x}}{3 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(5/2)/x^2,x, algorithm="giac")

[Out] $\frac{1}{3}*(15*a^{(3/2)}*b^2*\arctan(\sqrt{b*x - a}/\sqrt{a}) + 2*(b*x - a)^{(3/2)}*b^2 - 12*\sqrt{b*x - a}*a*b^2 - 3*\sqrt{b*x - a}*a^2*b/x)/b$

maple [A] time = 0.01, size = 64, normalized size = 0.86

$$5 a^{\frac{3}{2}} b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - 4 \sqrt{bx-a} ab - \frac{\sqrt{bx-a} a^2}{x} + \frac{2 (bx-a)^{\frac{3}{2}} b}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x-a)^(5/2)/x^2,x)

[Out] $\frac{2}{3}*b*(b*x-a)^{(3/2)}-4*a*b*(b*x-a)^{(1/2)}-a^2*(b*x-a)^{(1/2)}/x+5*a^{(3/2)}*b*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})$

maxima [A] time = 3.05, size = 63, normalized size = 0.85

$$5 a^{\frac{3}{2}} b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + \frac{2}{3} (bx-a)^{\frac{3}{2}} b - 4 \sqrt{bx-a} ab - \frac{\sqrt{bx-a} a^2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(5/2)/x^2,x, algorithm="maxima")

[Out] $5*a^{(3/2)}*b*\arctan(\sqrt{b*x - a}/\sqrt{a}) + 2/3*(b*x - a)^{(3/2)}*b - 4*\sqrt{b*x - a}*a*b - \sqrt{b*x - a}*a^2/x$

mupad [B] time = 0.10, size = 63, normalized size = 0.85

$$\frac{2 b (b x - a)^{3/2}}{3} - \frac{a^2 \sqrt{b x - a}}{x} + 5 a^{3/2} b \operatorname{atan}\left(\frac{\sqrt{b x - a}}{\sqrt{a}}\right) - 4 a b \sqrt{b x - a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x - a)^(5/2)/x^2,x)`

[Out] $(2*b*(b*x - a)^{(3/2)})/3 - (a^2*(b*x - a)^{(1/2)})/x + 5*a^{(3/2)}*b*atan((b*x - a)^{(1/2)}/a^{(1/2)}) - 4*a*b*(b*x - a)^{(1/2)}$

sympy [C] time = 3.69, size = 245, normalized size = 3.31

$$\left\{ \begin{array}{l} -\frac{a^{\frac{5}{2}}\sqrt{-1+\frac{bx}{a}}}{x} - \frac{14a^{\frac{3}{2}}b\sqrt{-1+\frac{bx}{a}}}{3} - \frac{5ia^{\frac{3}{2}}b\log\left(\frac{bx}{a}\right)}{2} + 5ia^{\frac{3}{2}}b\log\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) - 5a^{\frac{3}{2}}b\operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) + \frac{2\sqrt{a}b^2x\sqrt{-1+\frac{bx}{a}}}{3} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{ia^{\frac{5}{2}}\sqrt{1-\frac{bx}{a}}}{x} - \frac{14ia^{\frac{3}{2}}b\sqrt{1-\frac{bx}{a}}}{3} - \frac{5ia^{\frac{3}{2}}b\log\left(\frac{bx}{a}\right)}{2} + 5ia^{\frac{3}{2}}b\log\left(\sqrt{1-\frac{bx}{a}}+1\right) + \frac{2i\sqrt{a}b^2x\sqrt{1-\frac{bx}{a}}}{3} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x-a)**(5/2)/x**2,x)`

[Out] `Piecewise((-a**(5/2)*sqrt(-1 + b*x/a)/x - 14*a**(3/2)*b*sqrt(-1 + b*x/a)/3 - 5*I*a**(3/2)*b*log(b*x/a)/2 + 5*I*a**(3/2)*b*log(sqrt(b)*sqrt(x)/sqrt(a)) - 5*a**(3/2)*b*asin(sqrt(a)/(sqrt(b)*sqrt(x))) + 2*sqrt(a)*b**2*x*sqrt(-1 + b*x/a)/3, Abs(b*x/a) > 1), (-I*a**(5/2)*sqrt(1 - b*x/a)/x - 14*I*a**(3/2)*b*sqrt(1 - b*x/a)/3 - 5*I*a**(3/2)*b*log(b*x/a)/2 + 5*I*a**(3/2)*b*log(sqrt(1 - b*x/a) + 1) + 2*I*sqrt(a)*b**2*x*sqrt(1 - b*x/a)/3, True))`

$$3.333 \quad \int \frac{(-a+bx)^{5/2}}{x^3} dx$$

Optimal. Leaf size=86

$$\frac{15}{4}b^2\sqrt{bx-a} - \frac{15}{4}\sqrt{a}b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - \frac{(bx-a)^{5/2}}{2x^2} - \frac{5b(bx-a)^{3/2}}{4x}$$

[Out] $-5/4*b*(b*x-a)^{(3/2)}/x-1/2*(b*x-a)^{(5/2)}/x^2-15/4*b^2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})*a^{(1/2)}+15/4*b^2*(b*x-a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 63, 205}

$$\frac{15}{4}b^2\sqrt{bx-a} - \frac{15}{4}\sqrt{a}b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - \frac{(bx-a)^{5/2}}{2x^2} - \frac{5b(bx-a)^{3/2}}{4x}$$

Antiderivative was successfully verified.

[In] Int[(-a + b*x)^(5/2)/x^3,x]

[Out] $(15*b^2*\text{Sqrt}[-a + b*x])/4 - (5*b*(-a + b*x)^{(3/2)})/(4*x) - (-a + b*x)^{(5/2)}/(2*x^2) - (15*\text{Sqrt}[a]*b^2*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]])/4$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^(n), x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(-a + bx)^{5/2}}{x^3} dx &= -\frac{(-a + bx)^{5/2}}{2x^2} + \frac{1}{4}(5b) \int \frac{(-a + bx)^{3/2}}{x^2} dx \\
&= -\frac{5b(-a + bx)^{3/2}}{4x} - \frac{(-a + bx)^{5/2}}{2x^2} + \frac{1}{8}(15b^2) \int \frac{\sqrt{-a + bx}}{x} dx \\
&= \frac{15}{4}b^2\sqrt{-a + bx} - \frac{5b(-a + bx)^{3/2}}{4x} - \frac{(-a + bx)^{5/2}}{2x^2} - \frac{1}{8}(15ab^2) \int \frac{1}{x\sqrt{-a + bx}} dx \\
&= \frac{15}{4}b^2\sqrt{-a + bx} - \frac{5b(-a + bx)^{3/2}}{4x} - \frac{(-a + bx)^{5/2}}{2x^2} - \frac{1}{4}(15ab) \operatorname{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a + bx}\right) \\
&= \frac{15}{4}b^2\sqrt{-a + bx} - \frac{5b(-a + bx)^{3/2}}{4x} - \frac{(-a + bx)^{5/2}}{2x^2} - \frac{15}{4}\sqrt{a}b^2 \tan^{-1}\left(\frac{\sqrt{-a + bx}}{\sqrt{a}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 38, normalized size = 0.44

$$\frac{2b^2(bx - a)^{7/2} {}_2F_1\left(3, \frac{7}{2}; \frac{9}{2}; 1 - \frac{bx}{a}\right)}{7a^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(-a + b*x)^(5/2)/x^3, x]
```

```
[Out] (2*b^2*(-a + b*x)^(7/2)*Hypergeometric2F1[3, 7/2, 9/2, 1 - (b*x)/a])/(7*a^3)
```

fricas [A] time = 0.51, size = 139, normalized size = 1.62

$$\left[\frac{15\sqrt{-a}b^2x^2 \log\left(\frac{bx-2\sqrt{bx-a}\sqrt{-a}-2a}{x}\right) + 2(8b^2x^2 + 9abx - 2a^2)\sqrt{bx-a}}{8x^2}, -\frac{15\sqrt{a}b^2x^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - (8b^2x^2 - 15abx + 2a^2)\sqrt{bx-a}}{4x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(5/2)/x^3,x, algorithm="fricas")

[Out] $[1/8*(15*\sqrt{-a}*b^2*x^2*\log((b*x - 2*\sqrt{b*x - a})*\sqrt{-a} - 2*a)/x) + 2*(8*b^2*x^2 + 9*a*b*x - 2*a^2)*\sqrt{b*x - a})/x^2, -1/4*(15*\sqrt{a}*b^2*x^2*\arctan(\sqrt{b*x - a}/\sqrt{a}) - (8*b^2*x^2 + 9*a*b*x - 2*a^2)*\sqrt{b*x - a})/x^2]$

giac [A] time = 1.04, size = 83, normalized size = 0.97

$$\frac{15\sqrt{a}b^3\arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) - 8\sqrt{bx-a}b^3 - \frac{9(bx-a)^{\frac{3}{2}}ab^3 + 7\sqrt{bx-a}a^2b^3}{b^2x^2}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(5/2)/x^3,x, algorithm="giac")

[Out] $-1/4*(15*\sqrt{a}*b^3*\arctan(\sqrt{b*x - a}/\sqrt{a}) - 8*\sqrt{b*x - a}*b^3 - (9*(b*x - a)^{(3/2)}*a*b^3 + 7*\sqrt{b*x - a}*a^2*b^3)/(b^2*x^2))/b$

maple [A] time = 0.01, size = 70, normalized size = 0.81

$$-\frac{15\sqrt{a}b^2\arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4} + 2\sqrt{bx-a}b^2 + \frac{7\sqrt{bx-a}a^2}{4x^2} + \frac{9(bx-a)^{\frac{3}{2}}a}{4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x-a)^(5/2)/x^3,x)

[Out] $2*b^2*(b*x-a)^{(1/2)}+9/4*a/x^2*(b*x-a)^{(3/2)}+7/4/x^2*(b*x-a)^{(1/2)}*a^2-15/4*b^2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})*a^{(1/2)}$

maxima [A] time = 2.92, size = 97, normalized size = 1.13

$$-\frac{15}{4}\sqrt{a}b^2\arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + 2\sqrt{bx-a}b^2 + \frac{9(bx-a)^{\frac{3}{2}}ab^2 + 7\sqrt{bx-a}a^2b^2}{4((bx-a)^2 + 2(bx-a)a + a^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x-a)^(5/2)/x^3,x, algorithm="maxima")

[Out] $-15/4*\sqrt{a}*b^2*\arctan(\sqrt{b*x - a}/\sqrt{a}) + 2*\sqrt{b*x - a}*b^2 + 1/4*(9*(b*x - a)^{(3/2)}*a*b^2 + 7*\sqrt{b*x - a}*a^2*b^2)/((b*x - a)^2 + 2*(b*x - a)*a + a^2)$

mupad [B] time = 0.09, size = 69, normalized size = 0.80

$$2b^2 \sqrt{bx-a} - \frac{15\sqrt{a} b^2 \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4} + \frac{9a(bx-a)^{3/2}}{4x^2} + \frac{7a^2 \sqrt{bx-a}}{4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x - a)^(5/2)/x^3,x)`

[Out] $2*b^2*(b*x - a)^{(1/2)} - (15*a^{(1/2)}*b^2*\operatorname{atan}((b*x - a)^{(1/2)}/a^{(1/2)}))/4 + (9*a*(b*x - a)^{(3/2)})/(4*x^2) + (7*a^2*(b*x - a)^{(1/2)})/(4*x^2)$

sympy [A] time = 3.93, size = 267, normalized size = 3.10

$$\left\{ \begin{array}{l} -\frac{15i\sqrt{a}b^2 \operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4} - \frac{ia^3}{2\sqrt{b}x^2\sqrt{\frac{a}{bx}-1}} + \frac{11ia^2\sqrt{b}}{4x^2\sqrt{\frac{a}{bx}-1}} - \frac{iab^{\frac{3}{2}}}{4\sqrt{x}\sqrt{\frac{a}{bx}-1}} - \frac{2ib^{\frac{5}{2}}\sqrt{x}}{\sqrt{\frac{a}{bx}-1}} \quad \text{for } \left|\frac{a}{bx}\right| > 1 \\ \frac{15\sqrt{a}b^2 \operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4} + \frac{a^3}{2\sqrt{b}x^2\sqrt{-\frac{a}{bx}+1}} - \frac{11a^2\sqrt{b}}{4x^2\sqrt{-\frac{a}{bx}+1}} + \frac{ab^{\frac{3}{2}}}{4\sqrt{x}\sqrt{-\frac{a}{bx}+1}} + \frac{2b^{\frac{5}{2}}\sqrt{x}}{\sqrt{-\frac{a}{bx}+1}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x-a)**(5/2)/x**3,x)`

[Out] `Piecewise((-15*I*sqrt(a)*b**2*acosh(sqrt(a)/(sqrt(b)*sqrt(x)))/4 - I*a**3/(2*sqrt(b)*x**(5/2)*sqrt(a/(b*x) - 1)) + 11*I*a**2*sqrt(b)/(4*x**(3/2)*sqrt(a/(b*x) - 1)) - I*a*b**(3/2)/(4*sqrt(x)*sqrt(a/(b*x) - 1)) - 2*I*b**(5/2)*sqrt(x)/sqrt(a/(b*x) - 1), Abs(a/(b*x)) > 1), (15*sqrt(a)*b**2*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/4 + a**3/(2*sqrt(b)*x**(5/2)*sqrt(-a/(b*x) + 1)) - 11*a**2*sqrt(b)/(4*x**(3/2)*sqrt(-a/(b*x) + 1)) + a*b**(3/2)/(4*sqrt(x)*sqrt(-a/(b*x) + 1)) + 2*b**(5/2)*sqrt(x)/sqrt(-a/(b*x) + 1), True))`

$$3.334 \quad \int \frac{x^4}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=89

$$\frac{2a^4\sqrt{a+bx}}{b^5} - \frac{8a^3(a+bx)^{3/2}}{3b^5} + \frac{12a^2(a+bx)^{5/2}}{5b^5} + \frac{2(a+bx)^{9/2}}{9b^5} - \frac{8a(a+bx)^{7/2}}{7b^5}$$

[Out] $-8/3*a^3*(b*x+a)^{(3/2)}/b^5+12/5*a^2*(b*x+a)^{(5/2)}/b^5-8/7*a*(b*x+a)^{(7/2)}/b^5+2/9*(b*x+a)^{(9/2)}/b^5+2*a^4*(b*x+a)^{(1/2)}/b^5$

Rubi [A] time = 0.02, antiderivative size = 89, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{12a^2(a+bx)^{5/2}}{5b^5} - \frac{8a^3(a+bx)^{3/2}}{3b^5} + \frac{2a^4\sqrt{a+bx}}{b^5} + \frac{2(a+bx)^{9/2}}{9b^5} - \frac{8a(a+bx)^{7/2}}{7b^5}$$

Antiderivative was successfully verified.

[In] Int[x^4/Sqrt[a + b*x], x]

[Out] $(2*a^4*\text{Sqrt}[a + b*x])/b^5 - (8*a^3*(a + b*x)^{(3/2)})/(3*b^5) + (12*a^2*(a + b*x)^{(5/2)})/(5*b^5) - (8*a*(a + b*x)^{(7/2)})/(7*b^5) + (2*(a + b*x)^{(9/2)})/(9*b^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{\sqrt{a+bx}} dx &= \int \left(\frac{a^4}{b^4\sqrt{a+bx}} - \frac{4a^3\sqrt{a+bx}}{b^4} + \frac{6a^2(a+bx)^{3/2}}{b^4} - \frac{4a(a+bx)^{5/2}}{b^4} + \frac{(a+bx)^{7/2}}{b^4} \right) dx \\ &= \frac{2a^4\sqrt{a+bx}}{b^5} - \frac{8a^3(a+bx)^{3/2}}{3b^5} + \frac{12a^2(a+bx)^{5/2}}{5b^5} - \frac{8a(a+bx)^{7/2}}{7b^5} + \frac{2(a+bx)^{9/2}}{9b^5} \end{aligned}$$

Mathematica [A] time = 0.03, size = 57, normalized size = 0.64

$$\frac{2\sqrt{a+bx} (128a^4 - 64a^3bx + 48a^2b^2x^2 - 40ab^3x^3 + 35b^4x^4)}{315b^5}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/Sqrt[a + b*x], x]

[Out] (2*sqrt[a + b*x]*(128*a^4 - 64*a^3*b*x + 48*a^2*b^2*x^2 - 40*a*b^3*x^3 + 35*b^4*x^4))/(315*b^5)

fricas [A] time = 0.79, size = 53, normalized size = 0.60

$$\frac{2(35b^4x^4 - 40ab^3x^3 + 48a^2b^2x^2 - 64a^3bx + 128a^4)\sqrt{bx+a}}{315b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] 2/315*(35*b^4*x^4 - 40*a*b^3*x^3 + 48*a^2*b^2*x^2 - 64*a^3*b*x + 128*a^4)*sqrt(b*x + a)/b^5

giac [A] time = 1.04, size = 61, normalized size = 0.69

$$\frac{2\left(35(bx+a)^{\frac{9}{2}} - 180(bx+a)^{\frac{7}{2}}a + 378(bx+a)^{\frac{5}{2}}a^2 - 420(bx+a)^{\frac{3}{2}}a^3 + 315\sqrt{bx+a}a^4\right)}{315b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^(1/2), x, algorithm="giac")

[Out] 2/315*(35*(b*x + a)^(9/2) - 180*(b*x + a)^(7/2)*a + 378*(b*x + a)^(5/2)*a^2 - 420*(b*x + a)^(3/2)*a^3 + 315*sqrt(b*x + a)*a^4)/b^5

maple [A] time = 0.01, size = 54, normalized size = 0.61

$$\frac{2\sqrt{bx+a}\left(35x^4b^4 - 40ax^3b^3 + 48a^2x^2b^2 - 64a^3xb + 128a^4\right)}{315b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(b*x+a)^(1/2), x)

[Out] 2/315*(b*x+a)^(1/2)*(35*b^4*x^4-40*a*b^3*x^3+48*a^2*b^2*x^2-64*a^3*b*x+128*a^4)/b^5

maxima [A] time = 1.34, size = 71, normalized size = 0.80

$$\frac{2(bx+a)^{\frac{9}{2}}}{9b^5} - \frac{8(bx+a)^{\frac{7}{2}}a}{7b^5} + \frac{12(bx+a)^{\frac{5}{2}}a^2}{5b^5} - \frac{8(bx+a)^{\frac{3}{2}}a^3}{3b^5} + \frac{2\sqrt{bx+a}a^4}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] $2/9*(b*x + a)^{(9/2)}/b^5 - 8/7*(b*x + a)^{(7/2)}*a/b^5 + 12/5*(b*x + a)^{(5/2)}*a^2/b^5 - 8/3*(b*x + a)^{(3/2)}*a^3/b^5 + 2*\sqrt{b*x + a}*a^4/b^5$

mupad [B] time = 0.02, size = 71, normalized size = 0.80

$$\frac{2(a+bx)^{9/2}}{9b^5} + \frac{2a^4\sqrt{a+bx}}{b^5} - \frac{8a^3(a+bx)^{3/2}}{3b^5} + \frac{12a^2(a+bx)^{5/2}}{5b^5} - \frac{8a(a+bx)^{7/2}}{7b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(a + b*x)^(1/2),x)

[Out] $(2*(a + b*x)^{(9/2)})/(9*b^5) + (2*a^4*(a + b*x)^{(1/2)})/b^5 - (8*a^3*(a + b*x)^{(3/2)})/(3*b^5) + (12*a^2*(a + b*x)^{(5/2)})/(5*b^5) - (8*a*(a + b*x)^{(7/2)})/(7*b^5)$

sympy [B] time = 4.84, size = 3755, normalized size = 42.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/(b*x+a)**(1/2),x)

[Out] $256*a**(89/2)*\sqrt{1 + b*x/a}/(315*a**40*b**5 + 3150*a**39*b**6*x + 14175*a**38*b**7*x**2 + 37800*a**37*b**8*x**3 + 66150*a**36*b**9*x**4 + 79380*a**35*b**10*x**5 + 66150*a**34*b**11*x**6 + 37800*a**33*b**12*x**7 + 14175*a**32*b**13*x**8 + 3150*a**31*b**14*x**9 + 315*a**30*b**15*x**10) - 256*a**(89/2)/(315*a**40*b**5 + 3150*a**39*b**6*x + 14175*a**38*b**7*x**2 + 37800*a**37*b**8*x**3 + 66150*a**36*b**9*x**4 + 79380*a**35*b**10*x**5 + 66150*a**34*b**11*x**6 + 37800*a**33*b**12*x**7 + 14175*a**32*b**13*x**8 + 3150*a**31*b**14*x**9 + 315*a**30*b**15*x**10) + 2432*a**(87/2)*b*x*\sqrt{1 + b*x/a}/(315*a**40*b**5 + 3150*a**39*b**6*x + 14175*a**38*b**7*x**2 + 37800*a**37*b**8*x**3 + 66150*a**36*b**9*x**4 + 79380*a**35*b**10*x**5 + 66150*a**34*b**11*x**6 + 37800*a**33*b**12*x**7 + 14175*a**32*b**13*x**8 + 3150*a**31*b**14*x**9 + 315*a**30*b**15*x**10) + 10336*a**(85/2)*b**2*x**2*\sqrt{1 + b*x/a}/(315*a**40*b**5 + 3150*a**39*b**6*x + 14175*a**38*b**7*x**2 + 37800*a**37*b**8*x**3 + 66150*a**36*b**9*x**4 + 79380*a**35*b**10*x**5 + 66150*a**34*b**11*x**6 + 37800*a**33*b**12*x**7 + 14175*a**32*b**13*x**8 + 3150*a**31*b**14*x**9 + 315*a**30*b**15*x**10)$

$$\begin{aligned}
& x^{10}) - 11520a^{85/2}b^2x^2/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) + 25840a^{83/2}b^3x^3\sqrt{1 + b^2x/a}/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) - 30720a^{83/2}b^3x^3/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) + 41990a^{81/2}b^4x^4\sqrt{1 + b^2x/a}/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) - 53760a^{81/2}b^4x^4/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) + 46252a^{79/2}b^5x^5\sqrt{1 + b^2x/a}/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) - 64512a^{79/2}b^5x^5/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) + 35214a^{77/2}b^6x^6\sqrt{1 + b^2x/a}/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) - 53760a^{77/2}b^6x^6/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) + 19632a^{75/2}b^7x^7\sqrt{1 + b^2x/a}/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) - 30720a^{75/2}b^7x^7/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) + 10860a^{73/2}b^8x^8\sqrt{1 + b^2x/a}/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10}) + 10860a^{73/2}b^8x^8/(315a^{40}b^5 + 3150a^{39}b^6x + 14175a^{38}b^7x^2 + 37800a^{37}b^8x^3 + 66150a^{36}b^9x^4 + 79380a^{35}b^{10}x^5 + 66150a^{34}b^{11}x^6 + 37800a^{33}b^{12}x^7 + 14175a^{32}b^{13}x^8 + 3150a^{31}b^{14}x^9 + 315a^{30}b^{15}x^{10})
\end{aligned}$$

$$\begin{aligned}
& + 79380*a^{35}*b^{10}*x^5 + 66150*a^{34}*b^{11}*x^6 + 37800*a^{33}*b^{12}*x^7 \\
& + 14175*a^{32}*b^{13}*x^8 + 3150*a^{31}*b^{14}*x^9 + 315*a^{30}*b^{15}*x^{10}) - \\
& 11520*a^{(73/2)}*b^8*x^8/(315*a^{40}*b^5 + 3150*a^{39}*b^6*x + 14175*a^{38}*b^7*x^2 + 37800*a^{37}*b^8*x^3 + 66150*a^{36}*b^9*x^4 + 79380*a^{35}*b^{10}*x^5 + 66150*a^{34}*b^{11}*x^6 + 37800*a^{33}*b^{12}*x^7 + 14175*a^{32}*b^{13}*x^8 + 3150*a^{31}*b^{14}*x^9 + 315*a^{30}*b^{15}*x^{10}) + 9160*a^{(71/2)}*b^9*x^9*\sqrt{1 + b*x/a}/(315*a^{40}*b^5 + 3150*a^{39}*b^6*x + 14175*a^{38}*b^7*x^2 + 37800*a^{37}*b^8*x^3 + 66150*a^{36}*b^9*x^4 + 79380*a^{35}*b^{10}*x^5 + 66150*a^{34}*b^{11}*x^6 + 37800*a^{33}*b^{12}*x^7 + 14175*a^{32}*b^{13}*x^8 + 3150*a^{31}*b^{14}*x^9 + 315*a^{30}*b^{15}*x^{10}) - 2560*a^{(71/2)}*b^9*x^9/(315*a^{40}*b^5 + 3150*a^{39}*b^6*x + 14175*a^{38}*b^7*x^2 + 37800*a^{37}*b^8*x^3 + 66150*a^{36}*b^9*x^4 + 79380*a^{35}*b^{10}*x^5 + 66150*a^{34}*b^{11}*x^6 + 37800*a^{33}*b^{12}*x^7 + 14175*a^{32}*b^{13}*x^8 + 3150*a^{31}*b^{14}*x^9 + 315*a^{30}*b^{15}*x^{10}) + 8396*a^{(69/2)}*b^{10}*x^{10}*\sqrt{1 + b*x/a}/(315*a^{40}*b^5 + 3150*a^{39}*b^6*x + 14175*a^{38}*b^7*x^2 + 37800*a^{37}*b^8*x^3 + 66150*a^{36}*b^9*x^4 + 79380*a^{35}*b^{10}*x^5 + 66150*a^{34}*b^{11}*x^6 + 37800*a^{33}*b^{12}*x^7 + 14175*a^{32}*b^{13}*x^8 + 3150*a^{31}*b^{14}*x^9 + 315*a^{30}*b^{15}*x^{10}) - 256*a^{(69/2)}*b^{10}*x^{10}/(315*a^{40}*b^5 + 3150*a^{39}*b^6*x + 14175*a^{38}*b^7*x^2 + 37800*a^{37}*b^8*x^3 + 66150*a^{36}*b^9*x^4 + 79380*a^{35}*b^{10}*x^5 + 66150*a^{34}*b^{11}*x^6 + 37800*a^{33}*b^{12}*x^7 + 14175*a^{32}*b^{13}*x^8 + 3150*a^{31}*b^{14}*x^9 + 315*a^{30}*b^{15}*x^{10}) + 5632*a^{(67/2)}*b^{11}*x^{11}*\sqrt{1 + b*x/a}/(315*a^{40}*b^5 + 3150*a^{39}*b^6*x + 14175*a^{38}*b^7*x^2 + 37800*a^{37}*b^8*x^3 + 66150*a^{36}*b^9*x^4 + 79380*a^{35}*b^{10}*x^5 + 66150*a^{34}*b^{11}*x^6 + 37800*a^{33}*b^{12}*x^7 + 14175*a^{32}*b^{13}*x^8 + 3150*a^{31}*b^{14}*x^9 + 315*a^{30}*b^{15}*x^{10}) + 2446*a^{(65/2)}*b^{12}*x^{12}*\sqrt{1 + b*x/a}/(315*a^{40}*b^5 + 3150*a^{39}*b^6*x + 14175*a^{38}*b^7*x^2 + 37800*a^{37}*b^8*x^3 + 66150*a^{36}*b^9*x^4 + 79380*a^{35}*b^{10}*x^5 + 66150*a^{34}*b^{11}*x^6 + 37800*a^{33}*b^{12}*x^7 + 14175*a^{32}*b^{13}*x^8 + 3150*a^{31}*b^{14}*x^9 + 315*a^{30}*b^{15}*x^{10}) + 620*a^{(63/2)}*b^{13}*x^{13}*\sqrt{1 + b*x/a}/(315*a^{40}*b^5 + 3150*a^{39}*b^6*x + 14175*a^{38}*b^7*x^2 + 37800*a^{37}*b^8*x^3 + 66150*a^{36}*b^9*x^4 + 79380*a^{35}*b^{10}*x^5 + 66150*a^{34}*b^{11}*x^6 + 37800*a^{33}*b^{12}*x^7 + 14175*a^{32}*b^{13}*x^8 + 3150*a^{31}*b^{14}*x^9 + 315*a^{30}*b^{15}*x^{10}) + 70*a^{(61/2)}*b^{14}*x^{14}*\sqrt{1 + b*x/a}/(315*a^{40}*b^5 + 3150*a^{39}*b^6*x + 14175*a^{38}*b^7*x^2 + 37800*a^{37}*b^8*x^3 + 66150*a^{36}*b^9*x^4 + 79380*a^{35}*b^{10}*x^5 + 66150*a^{34}*b^{11}*x^6 + 37800*a^{33}*b^{12}*x^7 + 14175*a^{32}*b^{13}*x^8 + 3150*a^{31}*b^{14}*x^9 + 315*a^{30}*b^{15}*x^{10})
\end{aligned}$$

$$3.335 \quad \int \frac{x^3}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=68

$$-\frac{2a^3\sqrt{a+bx}}{b^4} + \frac{2a^2(a+bx)^{3/2}}{b^4} + \frac{2(a+bx)^{7/2}}{7b^4} - \frac{6a(a+bx)^{5/2}}{5b^4}$$

[Out] $2a^2(bx+a)^{(3/2)}/b^4 - 6/5a*(bx+a)^{(5/2)}/b^4 + 2/7*(bx+a)^{(7/2)}/b^4 - 2a^3*(bx+a)^{(1/2)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2a^2(a+bx)^{3/2}}{b^4} - \frac{2a^3\sqrt{a+bx}}{b^4} + \frac{2(a+bx)^{7/2}}{7b^4} - \frac{6a(a+bx)^{5/2}}{5b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3/Sqrt[a + b*x], x]

[Out] $(-2a^3\sqrt{a+bx})/b^4 + (2a^2(a+bx)^{(3/2)})/b^4 - (6a*(a+bx)^{(5/2)})/(5*b^4) + (2*(a+bx)^{(7/2)})/(7*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{\sqrt{a+bx}} dx &= \int \left(-\frac{a^3}{b^3\sqrt{a+bx}} + \frac{3a^2\sqrt{a+bx}}{b^3} - \frac{3a(a+bx)^{3/2}}{b^3} + \frac{(a+bx)^{5/2}}{b^3} \right) dx \\ &= -\frac{2a^3\sqrt{a+bx}}{b^4} + \frac{2a^2(a+bx)^{3/2}}{b^4} - \frac{6a(a+bx)^{5/2}}{5b^4} + \frac{2(a+bx)^{7/2}}{7b^4} \end{aligned}$$

Mathematica [A] time = 0.03, size = 46, normalized size = 0.68

$$\frac{2\sqrt{a+bx}(-16a^3 + 8a^2bx - 6ab^2x^2 + 5b^3x^3)}{35b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/Sqrt[a + b*x], x]

[Out] (2*Sqrt[a + b*x]*(-16*a^3 + 8*a^2*b*x - 6*a*b^2*x^2 + 5*b^3*x^3))/(35*b^4)

fricas [A] time = 0.44, size = 42, normalized size = 0.62

$$\frac{2(5b^3x^3 - 6ab^2x^2 + 8a^2bx - 16a^3)\sqrt{bx+a}}{35b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] 2/35*(5*b^3*x^3 - 6*a*b^2*x^2 + 8*a^2*b*x - 16*a^3)*sqrt(b*x + a)/b^4

giac [A] time = 1.21, size = 49, normalized size = 0.72

$$\frac{2\left(5(bx+a)^{\frac{7}{2}} - 21(bx+a)^{\frac{5}{2}}a + 35(bx+a)^{\frac{3}{2}}a^2 - 35\sqrt{bx+a}a^3\right)}{35b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(1/2), x, algorithm="giac")

[Out] 2/35*(5*(b*x + a)^(7/2) - 21*(b*x + a)^(5/2)*a + 35*(b*x + a)^(3/2)*a^2 - 35*sqrt(b*x + a)*a^3)/b^4

maple [A] time = 0.00, size = 43, normalized size = 0.63

$$\frac{2\sqrt{bx+a}(-5b^3x^3 + 6ab^2x^2 - 8a^2bx + 16a^3)}{35b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^(1/2), x)

[Out] -2/35*(b*x+a)^(1/2)*(-5*b^3*x^3+6*a*b^2*x^2-8*a^2*b*x+16*a^3)/b^4

maxima [A] time = 1.25, size = 56, normalized size = 0.82

$$\frac{2(bx+a)^{\frac{7}{2}}}{7b^4} - \frac{6(bx+a)^{\frac{5}{2}}a}{5b^4} + \frac{2(bx+a)^{\frac{3}{2}}a^2}{b^4} - \frac{2\sqrt{bx+a}a^3}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] $\frac{2}{7}*(b*x + a)^{(7/2)}/b^4 - \frac{6}{5}*(b*x + a)^{(5/2)}*a/b^4 + 2*(b*x + a)^{(3/2)}*a^2/b^4 - 2*\text{sqrt}(b*x + a)*a^3/b^4$

mupad [B] time = 0.05, size = 56, normalized size = 0.82

$$\frac{2(a+bx)^{7/2}}{7b^4} - \frac{2a^3\sqrt{a+bx}}{b^4} + \frac{2a^2(a+bx)^{3/2}}{b^4} - \frac{6a(a+bx)^{5/2}}{5b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(a + b*x)^(1/2),x)

[Out] $\frac{2*(a + b*x)^{(7/2))}}{(7*b^4)} - \frac{(2*a^3*(a + b*x)^{(1/2))}}{b^4} + \frac{(2*a^2*(a + b*x)^{(3/2))}}{b^4} - \frac{(6*a*(a + b*x)^{(5/2))}}{(5*b^4)}$

sympy [B] time = 2.70, size = 1640, normalized size = 24.12

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(b*x+a)**(1/2),x)

[Out] $-32*a^{(47/2)}*\text{sqrt}(1 + b*x/a)/(35*a^{20}*b^{**4} + 210*a^{19}*b^{**5}*x + 525*a^{18}*b^{**6}*x^{**2} + 700*a^{17}*b^{**7}*x^{**3} + 525*a^{16}*b^{**8}*x^{**4} + 210*a^{15}*b^{**9}*x^{**5} + 35*a^{14}*b^{**10}*x^{**6}) + 32*a^{(47/2)}/(35*a^{20}*b^{**4} + 210*a^{19}*b^{**5}*x + 525*a^{18}*b^{**6}*x^{**2} + 700*a^{17}*b^{**7}*x^{**3} + 525*a^{16}*b^{**8}*x^{**4} + 210*a^{15}*b^{**9}*x^{**5} + 35*a^{14}*b^{**10}*x^{**6}) - 176*a^{(45/2)}*b*x*\text{sqrt}(1 + b*x/a)/(35*a^{20}*b^{**4} + 210*a^{19}*b^{**5}*x + 525*a^{18}*b^{**6}*x^{**2} + 700*a^{17}*b^{**7}*x^{**3} + 525*a^{16}*b^{**8}*x^{**4} + 210*a^{15}*b^{**9}*x^{**5} + 35*a^{14}*b^{**10}*x^{**6}) + 192*a^{(45/2)}*b*x/(35*a^{20}*b^{**4} + 210*a^{19}*b^{**5}*x + 525*a^{18}*b^{**6}*x^{**2} + 700*a^{17}*b^{**7}*x^{**3} + 525*a^{16}*b^{**8}*x^{**4} + 210*a^{15}*b^{**9}*x^{**5} + 35*a^{14}*b^{**10}*x^{**6}) - 396*a^{(43/2)}*b^{**2}*x^{**2}*\text{sqrt}(1 + b*x/a)/(35*a^{20}*b^{**4} + 210*a^{19}*b^{**5}*x + 525*a^{18}*b^{**6}*x^{**2} + 700*a^{17}*b^{**7}*x^{**3} + 525*a^{16}*b^{**8}*x^{**4} + 210*a^{15}*b^{**9}*x^{**5} + 35*a^{14}*b^{**10}*x^{**6}) + 480*a^{(43/2)}*b^{**2}*x^{**2}/(35*a^{20}*b^{**4} + 210*a^{19}*b^{**5}*x + 525*a^{18}*b^{**6}*x^{**2} + 700*a^{17}*b^{**7}*x^{**3} + 525*a^{16}*b^{**8}*x^{**4} + 210*a^{15}*b^{**9}*x^{**5} + 35*a^{14}*b^{**10}*x^{**6}) - 462*a^{(41/2)}*b^{**3}*x^{**3}*\text{sqrt}(1 + b*x/a)/(35*a^{20}*b^{**4} + 210*a^{19}*b^{**5}*x + 525*a^{18}*b^{**6}*x^{**2} + 700*a^{17}*b^{**7}*x^{**3} + 525*a^{16}*b^{**8}*x^{**4} + 210*a^{15}*b^{**9}*x^{**5} + 35*a^{14}*b^{**10}*x^{**6}) + 640*a^{(41/2)}*b^{**3}*x^{**3}/(35*a^{20}*b^{**4} + 210*a^{19}*b^{**5}*x + 525*a^{18}*b^{**6}*x^{**2} + 700*a^{17}*b^{**7}*x^{**3} + 525*a^{16}*b^{**8}*x^{**4} + 210*a^{15}*b^{**9}*x^{**5} + 35*a^{14}*b^{**10}*x^{**6}) - 280*a^{(39/2)}*b^{**4}*x^{**4}*\text{sqrt}(1 + b*x/a)/(35*a^{20}*b^{**4} + 210*a^{19}*b^{**5}*x + 525*a^{18}*b^{**6}*x^{**2} + 700*a^{17}*b^{**7}*x^{**3} + 525*a^{16}*b^{**8}*x^{**4} + 210*a^{15}*b^{**9}*x^{**5} + 35*a^{14}*b^{**10}*x^{**6}) + 480*a^{(39/2)}*b^{**4}*x^{**4}/(35*a^{20}*b^{**4} + 210*a^{19}*b^{**5}*x + 525*$

$$\begin{aligned}
& a^{18}b^6x^2 + 700a^{17}b^7x^3 + 525a^{16}b^8x^4 + 210a^{15}b^9x^5 + 35a^{14}b^{10}x^6) - 42a^{17/2}b^5x^5\sqrt{1 + b^2x/a}/(35a^{20}b^4 + 210a^{19}b^5x + 525a^{18}b^6x^2 + 700a^{17}b^7x^3 + 525a^{16}b^8x^4 + 210a^{15}b^9x^5 + 35a^{14}b^{10}x^6) + 192a^{17/2}b^5x^5/(35a^{20}b^4 + 210a^{19}b^5x + 525a^{18}b^6x^2 + 700a^{17}b^7x^3 + 525a^{16}b^8x^4 + 210a^{15}b^9x^5 + 35a^{14}b^{10}x^6) + 84a^{15/2}b^6x^6\sqrt{1 + b^2x/a}/(35a^{20}b^4 + 210a^{19}b^5x + 525a^{18}b^6x^2 + 700a^{17}b^7x^3 + 525a^{16}b^8x^4 + 210a^{15}b^9x^5 + 35a^{14}b^{10}x^6) + 32a^{15/2}b^6x^6/(35a^{20}b^4 + 210a^{19}b^5x + 525a^{18}b^6x^2 + 700a^{17}b^7x^3 + 525a^{16}b^8x^4 + 210a^{15}b^9x^5 + 35a^{14}b^{10}x^6) + 94a^{13/2}b^7x^7\sqrt{1 + b^2x/a}/(35a^{20}b^4 + 210a^{19}b^5x + 525a^{18}b^6x^2 + 700a^{17}b^7x^3 + 525a^{16}b^8x^4 + 210a^{15}b^9x^5 + 35a^{14}b^{10}x^6) + 48a^{11/2}b^8x^8\sqrt{1 + b^2x/a}/(35a^{20}b^4 + 210a^{19}b^5x + 525a^{18}b^6x^2 + 700a^{17}b^7x^3 + 525a^{16}b^8x^4 + 210a^{15}b^9x^5 + 35a^{14}b^{10}x^6) + 10a^{9/2}b^9x^9\sqrt{1 + b^2x/a}/(35a^{20}b^4 + 210a^{19}b^5x + 525a^{18}b^6x^2 + 700a^{17}b^7x^3 + 525a^{16}b^8x^4 + 210a^{15}b^9x^5 + 35a^{14}b^{10}x^6)
\end{aligned}$$

$$3.336 \quad \int \frac{x^2}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=51

$$\frac{2a^2\sqrt{a+bx}}{b^3} + \frac{2(a+bx)^{5/2}}{5b^3} - \frac{4a(a+bx)^{3/2}}{3b^3}$$

[Out] $-4/3*a*(b*x+a)^{(3/2)}/b^3+2/5*(b*x+a)^{(5/2)}/b^3+2*a^2*(b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2a^2\sqrt{a+bx}}{b^3} + \frac{2(a+bx)^{5/2}}{5b^3} - \frac{4a(a+bx)^{3/2}}{3b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/Sqrt[a + b*x], x]

[Out] $(2*a^2*\text{Sqrt}[a + b*x])/b^3 - (4*a*(a + b*x)^{(3/2)})/(3*b^3) + (2*(a + b*x)^{(5/2)})/(5*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sqrt{a+bx}} dx &= \int \left(\frac{a^2}{b^2\sqrt{a+bx}} - \frac{2a\sqrt{a+bx}}{b^2} + \frac{(a+bx)^{3/2}}{b^2} \right) dx \\ &= \frac{2a^2\sqrt{a+bx}}{b^3} - \frac{4a(a+bx)^{3/2}}{3b^3} + \frac{2(a+bx)^{5/2}}{5b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.69

$$\frac{2\sqrt{a+bx} (8a^2 - 4abx + 3b^2x^2)}{15b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/Sqrt[a + b*x], x]

[Out] (2*Sqrt[a + b*x]*(8*a^2 - 4*a*b*x + 3*b^2*x^2))/(15*b^3)

fricas [A] time = 0.45, size = 31, normalized size = 0.61

$$\frac{2(3b^2x^2 - 4abx + 8a^2)\sqrt{bx + a}}{15b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] 2/15*(3*b^2*x^2 - 4*a*b*x + 8*a^2)*sqrt(b*x + a)/b^3

giac [A] time = 1.34, size = 37, normalized size = 0.73

$$\frac{2\left(3(bx + a)^{\frac{5}{2}} - 10(bx + a)^{\frac{3}{2}}a + 15\sqrt{bx + a}a^2\right)}{15b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(1/2), x, algorithm="giac")

[Out] 2/15*(3*(b*x + a)^(5/2) - 10*(b*x + a)^(3/2)*a + 15*sqrt(b*x + a)*a^2)/b^3

maple [A] time = 0.00, size = 32, normalized size = 0.63

$$\frac{2\sqrt{bx + a} (3b^2x^2 - 4abx + 8a^2)}{15b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^(1/2), x)

[Out] 2/15*(b*x+a)^(1/2)*(3*b^2*x^2-4*a*b*x+8*a^2)/b^3

maxima [A] time = 1.32, size = 41, normalized size = 0.80

$$\frac{2(bx + a)^{\frac{5}{2}}}{5b^3} - \frac{4(bx + a)^{\frac{3}{2}}a}{3b^3} + \frac{2\sqrt{bx + a}a^2}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(1/2), x, algorithm="maxima")

[Out] $2/5*(b*x + a)^{(5/2)}/b^3 - 4/3*(b*x + a)^{(3/2)}*a/b^3 + 2*\sqrt{b*x + a}*a^2/b^3$

mupad [B] time = 0.04, size = 37, normalized size = 0.73

$$\frac{6(a+bx)^{5/2} - 20a(a+bx)^{3/2} + 30a^2\sqrt{a+bx}}{15b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/(a + b*x)^(1/2), x)`

[Out] $(6*(a + b*x)^{(5/2)} - 20*a*(a + b*x)^{(3/2)} + 30*a^2*(a + b*x)^{(1/2)})/(15*b^3)$

sympy [B] time = 1.77, size = 600, normalized size = 11.76

$$\frac{16a^{\frac{21}{2}}\sqrt{1+\frac{bx}{a}}}{15a^8b^3 + 45a^7b^4x + 45a^6b^5x^2 + 15a^5b^6x^3} - \frac{16a^{\frac{21}{2}}}{15a^8b^3 + 45a^7b^4x + 45a^6b^5x^2 + 15a^5b^6x^3} + \frac{40a^{\frac{19}{2}}bx\sqrt{1+\frac{bx}{a}}}{15a^8b^3 + 45a^7b^4x + 45a^6b^5x^2 + 15a^5b^6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2/(b*x+a)**(1/2), x)`

[Out] $16*a^{(21/2)}*\sqrt{1 + b*x/a}/(15*a^{(8)}*b^{(3)} + 45*a^{(7)}*b^{(4)}*x + 45*a^{(6)}*b^{(5)}*x^{(2)} + 15*a^{(5)}*b^{(6)}*x^{(3)}) - 16*a^{(21/2)}/(15*a^{(8)}*b^{(3)} + 45*a^{(7)}*b^{(4)}*x + 45*a^{(6)}*b^{(5)}*x^{(2)} + 15*a^{(5)}*b^{(6)}*x^{(3)}) + 40*a^{(19/2)}*b*x*\sqrt{1 + b*x/a}/(15*a^{(8)}*b^{(3)} + 45*a^{(7)}*b^{(4)}*x + 45*a^{(6)}*b^{(5)}*x^{(2)} + 15*a^{(5)}*b^{(6)}*x^{(3)}) - 48*a^{(19/2)}*b*x/(15*a^{(8)}*b^{(3)} + 45*a^{(7)}*b^{(4)}*x + 45*a^{(6)}*b^{(5)}*x^{(2)} + 15*a^{(5)}*b^{(6)}*x^{(3)}) + 30*a^{(17/2)}*b^{(2)}*x^{(2)}*\sqrt{1 + b*x/a}/(15*a^{(8)}*b^{(3)} + 45*a^{(7)}*b^{(4)}*x + 45*a^{(6)}*b^{(5)}*x^{(2)} + 15*a^{(5)}*b^{(6)}*x^{(3)}) - 48*a^{(17/2)}*b^{(2)}*x^{(2)}/(15*a^{(8)}*b^{(3)} + 45*a^{(7)}*b^{(4)}*x + 45*a^{(6)}*b^{(5)}*x^{(2)} + 15*a^{(5)}*b^{(6)}*x^{(3)}) + 10*a^{(15/2)}*b^{(3)}*x^{(3)}*\sqrt{1 + b*x/a}/(15*a^{(8)}*b^{(3)} + 45*a^{(7)}*b^{(4)}*x + 45*a^{(6)}*b^{(5)}*x^{(2)} + 15*a^{(5)}*b^{(6)}*x^{(3)}) - 16*a^{(15/2)}*b^{(3)}*x^{(3)}/(15*a^{(8)}*b^{(3)} + 45*a^{(7)}*b^{(4)}*x + 45*a^{(6)}*b^{(5)}*x^{(2)} + 15*a^{(5)}*b^{(6)}*x^{(3)}) + 10*a^{(13/2)}*b^{(4)}*x^{(4)}*\sqrt{1 + b*x/a}/(15*a^{(8)}*b^{(3)} + 45*a^{(7)}*b^{(4)}*x + 45*a^{(6)}*b^{(5)}*x^{(2)} + 15*a^{(5)}*b^{(6)}*x^{(3)}) + 6*a^{(11/2)}*b^{(5)}*x^{(5)}*\sqrt{1 + b*x/a}/(15*a^{(8)}*b^{(3)} + 45*a^{(7)}*b^{(4)}*x + 45*a^{(6)}*b^{(5)}*x^{(2)} + 15*a^{(5)}*b^{(6)}*x^{(3)})$

$$3.337 \quad \int \frac{x}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=32

$$\frac{2(a+bx)^{3/2}}{3b^2} - \frac{2a\sqrt{a+bx}}{b^2}$$

[Out] $2/3*(b*x+a)^{(3/2)}/b^2-2*a*(b*x+a)^{(1/2)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{2(a+bx)^{3/2}}{3b^2} - \frac{2a\sqrt{a+bx}}{b^2}$$

Antiderivative was successfully verified.

[In] Int[x/Sqrt[a + b*x], x]

[Out] $(-2*a*\text{Sqrt}[a + b*x])/b^2 + (2*(a + b*x)^{(3/2)})/(3*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x}{\sqrt{a+bx}} dx &= \int \left(-\frac{a}{b\sqrt{a+bx}} + \frac{\sqrt{a+bx}}{b} \right) dx \\ &= -\frac{2a\sqrt{a+bx}}{b^2} + \frac{2(a+bx)^{3/2}}{3b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.72

$$\frac{2(bx-2a)\sqrt{a+bx}}{3b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x/Sqrt[a + b*x], x]

[Out] $(2*(-2*a + b*x)*\text{Sqrt}[a + b*x])/(3*b^2)$

fricas [A] time = 0.43, size = 19, normalized size = 0.59

$$\frac{2\sqrt{bx+a}(bx-2a)}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(1/2),x, algorithm="fricas")`

[Out] $2/3*\text{sqrt}(b*x + a)*(b*x - 2*a)/b^2$

giac [A] time = 1.01, size = 23, normalized size = 0.72

$$\frac{2\left((bx+a)^{\frac{3}{2}} - 3\sqrt{bx+a}a\right)}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(1/2),x, algorithm="giac")`

[Out] $2/3*((b*x + a)^{(3/2)} - 3*\text{sqrt}(b*x + a)*a)/b^2$

maple [A] time = 0.00, size = 21, normalized size = 0.66

$$-\frac{2\sqrt{bx+a}(-bx+2a)}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(b*x+a)^(1/2),x)`

[Out] $-2/3*(b*x+a)^{(1/2)}*(-b*x+2*a)/b^2$

maxima [A] time = 1.32, size = 26, normalized size = 0.81

$$\frac{2(bx+a)^{\frac{3}{2}}}{3b^2} - \frac{2\sqrt{bx+a}a}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] $2/3*(b*x + a)^{(3/2)}/b^2 - 2*\text{sqrt}(b*x + a)*a/b^2$

mupad [B] time = 0.03, size = 25, normalized size = 0.78

$$\frac{6a\sqrt{a+bx} - 2(a+bx)^{3/2}}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a + b*x)^(1/2), x)`

[Out] `-(6*a*(a + b*x)^(1/2) - 2*(a + b*x)^(3/2))/(3*b^2)`

sympy [B] time = 1.16, size = 162, normalized size = 5.06

$$-\frac{4a^{\frac{7}{2}}\sqrt{1+\frac{bx}{a}}}{3a^2b^2+3ab^3x} + \frac{4a^{\frac{7}{2}}}{3a^2b^2+3ab^3x} - \frac{2a^{\frac{5}{2}}bx\sqrt{1+\frac{bx}{a}}}{3a^2b^2+3ab^3x} + \frac{4a^{\frac{5}{2}}bx}{3a^2b^2+3ab^3x} + \frac{2a^{\frac{3}{2}}b^2x^2\sqrt{1+\frac{bx}{a}}}{3a^2b^2+3ab^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)**(1/2), x)`

[Out] `-4*a**(7/2)*sqrt(1 + b*x/a)/(3*a**2*b**2 + 3*a*b**3*x) + 4*a**(7/2)/(3*a**2*b**2 + 3*a*b**3*x) - 2*a**(5/2)*b*x*sqrt(1 + b*x/a)/(3*a**2*b**2 + 3*a*b**3*x) + 4*a**(5/2)*b*x/(3*a**2*b**2 + 3*a*b**3*x) + 2*a**(3/2)*b**2*x**2*sqrt(1 + b*x/a)/(3*a**2*b**2 + 3*a*b**3*x)`

$$3.338 \quad \int \frac{1}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=14

$$\frac{2\sqrt{a+bx}}{b}$$

[Out] 2*(b*x+a)^(1/2)/b

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{2\sqrt{a+bx}}{b}$$

Antiderivative was successfully verified.

[In] Int[1/Sqrt[a + b*x], x]

[Out] (2*Sqrt[a + b*x])/b

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt{a+bx}} dx = \frac{2\sqrt{a+bx}}{b}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{2\sqrt{a+bx}}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/Sqrt[a + b*x], x]

[Out] (2*Sqrt[a + b*x])/b

fricas [A] time = 0.44, size = 12, normalized size = 0.86

$$\frac{2\sqrt{bx+a}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] 2*sqrt(b*x + a)/b

giac [A] time = 0.99, size = 12, normalized size = 0.86

$$\frac{2\sqrt{bx+a}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2),x, algorithm="giac")

[Out] 2*sqrt(b*x + a)/b

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{2\sqrt{bx+a}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2),x)

[Out] 2*(b*x+a)^(1/2)/b

maxima [A] time = 1.30, size = 12, normalized size = 0.86

$$\frac{2\sqrt{bx+a}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] 2*sqrt(b*x + a)/b

mupad [B] time = 0.02, size = 12, normalized size = 0.86

$$\frac{2\sqrt{a+bx}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(a + b*x)^(1/2),x)
```

```
[Out] (2*(a + b*x)^(1/2))/b
```

sympy [A] time = 0.07, size = 10, normalized size = 0.71

$$\frac{2\sqrt{a + bx}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(1/2),x)
```

```
[Out] 2*sqrt(a + b*x)/b
```


$$3.339 \quad \int \frac{1}{x\sqrt{a+bx}} dx$$

Optimal. Leaf size=23

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

[Out] $-2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {63, 208}

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/(x*\operatorname{Sqrt}[a + b*x]), x]$

[Out] $(-2*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/\operatorname{Sqrt}[a]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n}, x], x, (a + b*x)^{(1/p)}], x]] /;$ $\operatorname{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{LtQ}[-1, m, 0] \ \&\& \ \operatorname{LeQ}[-1, n, 0] \ \&\& \ \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 208

$\operatorname{Int}[(a_. + (b_.)*(x_.)^2)^{-1}, x_Symbol] := \operatorname{Simp}[(\operatorname{Rt}[-(a/b), 2]*\operatorname{ArcTanh}[x/\operatorname{Rt}[-(a/b), 2]])/a, x] /;$ $\operatorname{FreeQ}[\{a, b\}, x] \ \&\& \ \operatorname{NegQ}[a/b]$

Rubi steps

$$\int \frac{1}{x\sqrt{a+bx}} dx = \frac{2 \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{b}$$

$$= -\frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Mathematica [A] time = 0.00, size = 23, normalized size = 1.00

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*Sqrt[a + b*x]),x]

[Out] (-2*ArcTanh[Sqrt[a + b*x]/Sqrt[a]])/Sqrt[a]

fricas [A] time = 0.43, size = 56, normalized size = 2.43

$$\left[\frac{\log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a}+2a}{x}\right)}{\sqrt{a}}, \frac{2\sqrt{-a}\arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right)}{a} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x)/sqrt(a), 2*sqrt(-a)*arctan(sqrt(b*x + a)*sqrt(-a)/a)/a]

giac [A] time = 1.24, size = 21, normalized size = 0.91

$$\frac{2 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(1/2),x, algorithm="giac")

[Out] $2 \arctan(\sqrt{bx+a}/\sqrt{-a})/\sqrt{-a}$

maple [A] time = 0.01, size = 18, normalized size = 0.78

$$-\frac{2 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x/(b*x+a)^(1/2),x)`

[Out] $-2 \operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(1/2)}$

maxima [A] time = 2.94, size = 32, normalized size = 1.39

$$\frac{\log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] $\log((\sqrt{bx+a}-\sqrt{a})/(\sqrt{bx+a}+\sqrt{a}))/\sqrt{a}$

mupad [B] time = 0.06, size = 17, normalized size = 0.74

$$-\frac{2 \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(a+b*x)^(1/2)),x)`

[Out] $-(2 \operatorname{atanh}((a+b*x)^{(1/2)}/a^{(1/2)}))/a^{(1/2)}$

sympy [A] time = 1.11, size = 24, normalized size = 1.04

$$-\frac{2 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b*x+a)**(1/2),x)`

[Out] $-2 \operatorname{asinh}(\sqrt{a}/(\sqrt{b}\sqrt{x}))/\sqrt{a}$

$$3.340 \quad \int \frac{1}{x^2 \sqrt{a+bx}} dx$$

Optimal. Leaf size=41

$$\frac{b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{3/2}} - \frac{\sqrt{a+bx}}{ax}$$

[Out] b*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(3/2)-(b*x+a)^(1/2)/a/x

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 208}

$$\frac{b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{3/2}} - \frac{\sqrt{a+bx}}{ax}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*Sqrt[a + b*x]),x]

[Out] -(Sqrt[a + b*x]/(a*x)) + (b*ArcTanh[Sqrt[a + b*x]/Sqrt[a]])/a^(3/2)

Rule 51

```
Int[((a_.) + (b_.)*(x_)^(m_))*((c_.) + (d_.)*(x_)^(n_)), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_)^(m_))*((c_.) + (d_.)*(x_)^(n_)), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^2 \sqrt{a+bx}} dx &= -\frac{\sqrt{a+bx}}{ax} - \frac{b \int \frac{1}{x \sqrt{a+bx}} dx}{2a} \\
&= -\frac{\sqrt{a+bx}}{ax} - \frac{\text{Subst} \left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx} \right)}{a} \\
&= -\frac{\sqrt{a+bx}}{ax} + \frac{b \tanh^{-1} \left(\frac{\sqrt{a+bx}}{\sqrt{a}} \right)}{a^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.06, size = 47, normalized size = 1.15

$$\frac{\sqrt{a+bx} \left(\frac{b \tanh^{-1} \left(\sqrt{\frac{bx}{a}+1} \right)}{\sqrt{\frac{bx}{a}+1}} - \frac{a}{x} \right)}{a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*Sqrt[a + b*x]),x]

[Out] (Sqrt[a + b*x]*(-(a/x) + (b*ArcTanh[Sqrt[1 + (b*x)/a]]))/Sqrt[1 + (b*x)/a])/a^2

fricas [A] time = 0.44, size = 93, normalized size = 2.27

$$\left[\frac{\sqrt{a} bx \log \left(\frac{bx+2 \sqrt{bx+a} \sqrt{a}+2a}{x} \right) - 2 \sqrt{bx+a} a}{2 a^2 x}, -\frac{\sqrt{-a} bx \arctan \left(\frac{\sqrt{bx+a} \sqrt{-a}}{a} \right) + \sqrt{bx+a} a}{a^2 x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [1/2*(sqrt(a)*b*x*log((b*x + 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) - 2*sqrt(b*x + a)*a)/(a^2*x), -(sqrt(-a)*b*x*arctan(sqrt(b*x + a)*sqrt(-a)/a) + sqrt(b*x + a)*a)/(a^2*x)]

giac [A] time = 1.07, size = 47, normalized size = 1.15

$$-\frac{\frac{b^2 \arctan \left(\frac{\sqrt{bx+a}}{\sqrt{-a}} \right)}{\sqrt{-a} a} + \frac{\sqrt{bx+a} b}{ax}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(1/2),x, algorithm="giac")

[Out] $-(b^2 \arctan(\sqrt{bx+a}/\sqrt{-a})/(\sqrt{-a} * a) + \sqrt{bx+a} * b / (a * x)) / b$

maple [A] time = 0.01, size = 40, normalized size = 0.98

$$2 \left(\frac{\operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{2a^{\frac{3}{2}}} - \frac{\sqrt{bx+a}}{2abx} \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^(1/2),x)

[Out] $2 * b * (-1/2 * (b * x + a)^{(1/2)} / a * x / b + 1/2 * \operatorname{arctanh}((b * x + a)^{(1/2)} / a^{(1/2)}) / a^{(3/2)})$

maxima [A] time = 3.00, size = 60, normalized size = 1.46

$$-\frac{\sqrt{bx+a} b}{(bx+a)a - a^2} - \frac{b \log\left(\frac{\sqrt{bx+a} - \sqrt{a}}{\sqrt{bx+a} + \sqrt{a}}\right)}{2a^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] $-\sqrt{bx+a} * b / ((b * x + a) * a - a^2) - 1/2 * b * \log((\sqrt{bx+a} - \sqrt{a}) / (\sqrt{bx+a} + \sqrt{a})) / a^{(3/2)}$

mapad [B] time = 0.11, size = 33, normalized size = 0.80

$$\frac{b \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{3/2}} - \frac{\sqrt{a+bx}}{a x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(a + b*x)^(1/2)),x)

[Out] $(b * \operatorname{atanh}((a + b * x)^{(1/2)} / a^{(1/2)})) / a^{(3/2)} - (a + b * x)^{(1/2)} / (a * x)$

sympy [A] time = 2.30, size = 44, normalized size = 1.07

$$-\frac{\sqrt{b} \sqrt{\frac{a}{bx} + 1}}{a \sqrt{x}} + \frac{b \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b} \sqrt{x}}\right)}{a^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**2/(b*x+a)**(1/2),x)
```

```
[Out] -sqrt(b)*sqrt(a/(b*x) + 1)/(a*sqrt(x)) + b*asinh(sqrt(a)/(sqrt(b)*sqrt(x)))/a**(3/2)
```

$$3.341 \quad \int \frac{1}{x^3 \sqrt{a+bx}} dx$$

Optimal. Leaf size=68

$$-\frac{3b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{5/2}} + \frac{3b\sqrt{a+bx}}{4a^2x} - \frac{\sqrt{a+bx}}{2ax^2}$$

[Out] $-3/4*b^2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(5/2)}-1/2*(b*x+a)^{(1/2)}/a/x^2+3/4*b*(b*x+a)^{(1/2)}/a^2/x$

Rubi [A] time = 0.02, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 208}

$$-\frac{3b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{5/2}} + \frac{3b\sqrt{a+bx}}{4a^2x} - \frac{\sqrt{a+bx}}{2ax^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*sqrt[a + b*x]),x]

[Out] $-\operatorname{Sqrt}[a + b*x]/(2*a*x^2) + (3*b*\operatorname{Sqrt}[a + b*x])/(4*a^2*x) - (3*b^2*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(4*a^{(5/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^3 \sqrt{a+bx}} dx &= -\frac{\sqrt{a+bx}}{2ax^2} - \frac{(3b) \int \frac{1}{x^2 \sqrt{a+bx}} dx}{4a} \\
 &= -\frac{\sqrt{a+bx}}{2ax^2} + \frac{3b\sqrt{a+bx}}{4a^2x} + \frac{(3b^2) \int \frac{1}{x\sqrt{a+bx}} dx}{8a^2} \\
 &= -\frac{\sqrt{a+bx}}{2ax^2} + \frac{3b\sqrt{a+bx}}{4a^2x} + \frac{(3b) \text{Subst}\left(\int \frac{1}{\frac{-a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{4a^2} \\
 &= -\frac{\sqrt{a+bx}}{2ax^2} + \frac{3b\sqrt{a+bx}}{4a^2x} - \frac{3b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.49

$$-\frac{2b^2\sqrt{a+bx} {}_2F_1\left(\frac{1}{2}, 3; \frac{3}{2}; \frac{bx}{a} + 1\right)}{a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*Sqrt[a + b*x]),x]

[Out] (-2*b^2*Sqrt[a + b*x]*Hypergeometric2F1[1/2, 3, 3/2, 1 + (b*x)/a])/a^3

fricas [A] time = 0.49, size = 123, normalized size = 1.81

$$\left[\frac{3\sqrt{a}b^2x^2 \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(3abx-2a^2)\sqrt{bx+a}}{8a^3x^2}, \frac{3\sqrt{-a}b^2x^2 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) + (3abx-2a^2)\sqrt{-a}}{4a^3x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [1/8*(3*sqrt(a)*b^2*x^2*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*(3*a*b*x - 2*a^2)*sqrt(b*x + a))/(a^3*x^2), 1/4*(3*sqrt(-a)*b^2*x^2*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (3*a*b*x - 2*a^2)*sqrt(b*x + a))/(a^3*x^2)]

giac [A] time = 1.19, size = 69, normalized size = 1.01

$$\frac{3b^3 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}a^2} + \frac{3(bx+a)^{\frac{3}{2}}b^3 - 5\sqrt{bx+a}ab^3}{a^2b^2x^2}$$

$$4b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(1/2),x, algorithm="giac")

[Out] 1/4*(3*b^3*arctan(sqrt(b*x + a)/sqrt(-a))/(sqrt(-a)*a^2) + (3*(b*x + a)^(3/2)*b^3 - 5*sqrt(b*x + a)*a*b^3)/(a^2*b^2*x^2))/b

maple [A] time = 0.01, size = 66, normalized size = 0.97

$$2 \left(\frac{3 \left(\frac{\operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{2a^{\frac{3}{2}}} - \frac{\sqrt{bx+a}}{2abx} \right)}{4a} - \frac{\sqrt{bx+a}}{4a b^2 x^2} \right) b^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a)^(1/2),x)

[Out] 2*b^2*(-1/4*(b*x+a)^(1/2)/a/x^2/b^2-3/4/a*(-1/2*(b*x+a)^(1/2)/a/b/x+1/2*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(3/2))

maxima [A] time = 2.92, size = 92, normalized size = 1.35

$$\frac{3b^2 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{8a^{\frac{5}{2}}} + \frac{3(bx+a)^{\frac{3}{2}}b^2 - 5\sqrt{bx+a}ab^2}{4((bx+a)^2a^2 - 2(bx+a)a^3 + a^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] 3/8*b^2*log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a)))/a^(5/2) + 1/4*(3*(b*x + a)^(3/2)*b^2 - 5*sqrt(b*x + a)*a*b^2)/((b*x + a)^2*a^2 - 2*(b*x + a)*a^3 + a^4)

mupad [B] time = 0.06, size = 51, normalized size = 0.75

$$\frac{3(a+bx)^{3/2}}{4a^2x^2} - \frac{5\sqrt{a+bx}}{4ax^2} - \frac{3b^2 \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^3*(a + b*x)^(1/2)),x)`

[Out] $(3*(a + b*x)^{(3/2)})/(4*a^2*x^2) - (5*(a + b*x)^{(1/2)})/(4*a*x^2) - (3*b^2*atanh((a + b*x)^{(1/2)}/a^{(1/2)}))/(4*a^{(5/2)})$

sympy [A] time = 4.37, size = 102, normalized size = 1.50

$$-\frac{1}{2\sqrt{b}x^{\frac{5}{2}}\sqrt{\frac{a}{bx}+1}} + \frac{\sqrt{b}}{4ax^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}} + \frac{3b^{\frac{3}{2}}}{4a^2\sqrt{x}\sqrt{\frac{a}{bx}+1}} - \frac{3b^2 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4a^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**3/(b*x+a)**(1/2),x)`

[Out] $-1/(2*\sqrt{b}*x^{(5/2)}*\sqrt{a/(b*x) + 1}) + \sqrt{b}/(4*a*x^{(3/2)}*\sqrt{a/(b*x) + 1}) + 3*b^{(3/2)}/(4*a^{(5/2)}*\sqrt{x}*\sqrt{a/(b*x) + 1}) - 3*b^{(3/2)}*asinh(\sqrt{a}/(\sqrt{b}*\sqrt{x}))/4*a^{(5/2)}$

$$3.342 \quad \int \frac{1}{x^4 \sqrt{a+bx}} dx$$

Optimal. Leaf size=90

$$\frac{5b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{7/2}} - \frac{5b^2 \sqrt{a+bx}}{8a^3 x} + \frac{5b \sqrt{a+bx}}{12a^2 x^2} - \frac{\sqrt{a+bx}}{3ax^3}$$

[Out] $5/8*b^3*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(7/2)}-1/3*(b*x+a)^{(1/2)}/x^3/a+5/12*b*(b*x+a)^{(1/2)}/a^2/x^2-5/8*b^2*(b*x+a)^{(1/2)}/a^3/x$

Rubi [A] time = 0.03, antiderivative size = 90, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 208}

$$-\frac{5b^2 \sqrt{a+bx}}{8a^3 x} + \frac{5b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{7/2}} + \frac{5b \sqrt{a+bx}}{12a^2 x^2} - \frac{\sqrt{a+bx}}{3ax^3}$$

Antiderivative was successfully verified.

[In] Int[1/(x^4*Sqrt[a + b*x]),x]

[Out] $-\operatorname{Sqrt}[a + b*x]/(3*a*x^3) + (5*b*\operatorname{Sqrt}[a + b*x])/(12*a^2*x^2) - (5*b^2*\operatorname{Sqrt}[a + b*x])/(8*a^3*x) + (5*b^3*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(8*a^{(7/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^4 \sqrt{a+bx}} dx &= -\frac{\sqrt{a+bx}}{3ax^3} - \frac{(5b) \int \frac{1}{x^3 \sqrt{a+bx}} dx}{6a} \\
 &= -\frac{\sqrt{a+bx}}{3ax^3} + \frac{5b\sqrt{a+bx}}{12a^2x^2} + \frac{(5b^2) \int \frac{1}{x^2 \sqrt{a+bx}} dx}{8a^2} \\
 &= -\frac{\sqrt{a+bx}}{3ax^3} + \frac{5b\sqrt{a+bx}}{12a^2x^2} - \frac{5b^2\sqrt{a+bx}}{8a^3x} - \frac{(5b^3) \int \frac{1}{x \sqrt{a+bx}} dx}{16a^3} \\
 &= -\frac{\sqrt{a+bx}}{3ax^3} + \frac{5b\sqrt{a+bx}}{12a^2x^2} - \frac{5b^2\sqrt{a+bx}}{8a^3x} - \frac{(5b^2) \text{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{8a^3} \\
 &= -\frac{\sqrt{a+bx}}{3ax^3} + \frac{5b\sqrt{a+bx}}{12a^2x^2} - \frac{5b^2\sqrt{a+bx}}{8a^3x} + \frac{5b^3 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.37

$$\frac{2b^3\sqrt{a+bx} {}_2F_1\left(\frac{1}{2}, 4; \frac{3}{2}; \frac{bx}{a} + 1\right)}{a^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^4*Sqrt[a + b*x]),x]

[Out] (2*b^3*Sqrt[a + b*x]*Hypergeometric2F1[1/2, 4, 3/2, 1 + (b*x)/a])/a^4

fricas [A] time = 0.48, size = 145, normalized size = 1.61

$$\left[\frac{15\sqrt{a}b^3x^3 \log\left(\frac{bx+2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2(15ab^2x^2 - 10a^2bx + 8a^3)\sqrt{bx+a}}{48a^4x^3}, -\frac{15\sqrt{-a}b^3x^3 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right)}{24a^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] $\left[\frac{1}{48} \cdot (15 \sqrt{a} \cdot b^3 x^3 \log((b x + 2 \sqrt{b x + a}) \sqrt{a} + 2 a) / x) - 2 \cdot (15 a \cdot b^2 x^2 - 10 a^2 b x + 8 a^3) \sqrt{b x + a} / (a^4 x^3), -1/24 \cdot (15 \sqrt{-a} \cdot b^3 x^3 \arctan(\sqrt{b x + a} \sqrt{-a} / a) + (15 a \cdot b^2 x^2 - 10 a^2 b x + 8 a^3) \sqrt{b x + a}) / (a^4 x^3) \right]$

giac [A] time = 0.91, size = 84, normalized size = 0.93

$$\frac{15 b^4 \arctan\left(\frac{\sqrt{b x + a}}{\sqrt{-a}}\right)}{\sqrt{-a} a^3} + \frac{15 (b x + a)^{\frac{5}{2}} b^4 - 40 (b x + a)^{\frac{3}{2}} a b^4 + 33 \sqrt{b x + a} a^2 b^4}{a^3 b^3 x^3}$$

$$24 b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^4/(b*x+a)^(1/2),x, algorithm="giac")`

[Out] $-1/24 \cdot (15 b^4 \arctan(\sqrt{b x + a} / \sqrt{-a}) / (\sqrt{-a} a^3) + (15 (b x + a)^{(5/2)} b^4 - 40 (b x + a)^{(3/2)} a b^4 + 33 \sqrt{b x + a} a^2 b^4) / (a^3 b^3 x^3)) / b$

maple [A] time = 0.01, size = 90, normalized size = 1.00

$$\left(\frac{5 \left(\frac{3 \left(\frac{\operatorname{arctanh}\left(\frac{\sqrt{b x + a}}{\sqrt{a}}\right)}{2 a^{\frac{3}{2}}} - \frac{\sqrt{b x + a}}{2 a b x} \right)}{4 a} - \frac{\sqrt{b x + a}}{4 a b^2 x^2} \right)}{6 a} - \frac{\sqrt{b x + a}}{6 a b^3 x^3} \right) b^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^4/(b*x+a)^(1/2),x)`

[Out] $2 b^3 \cdot (-1/6 \cdot (b x + a)^{(1/2)} / a / x^3 / b^3 - 5/6 \cdot a \cdot (-1/4 \cdot (b x + a)^{(1/2)} / a / b^2 / x^2 - 3/4 \cdot a \cdot (-1/2 \cdot (b x + a)^{(1/2)} / a / b / x + 1/2 \cdot \operatorname{arctanh}((b x + a)^{(1/2)} / a^{(1/2)}) / a^{(3/2)}))$

maxima [A] time = 2.92, size = 121, normalized size = 1.34

$$\frac{5 b^3 \log\left(\frac{\sqrt{b x + a} - \sqrt{a}}{\sqrt{b x + a} + \sqrt{a}}\right)}{16 a^{\frac{7}{2}}} - \frac{15 (b x + a)^{\frac{5}{2}} b^3 - 40 (b x + a)^{\frac{3}{2}} a b^3 + 33 \sqrt{b x + a} a^2 b^3}{24 \left((b x + a)^3 a^3 - 3 (b x + a)^2 a^4 + 3 (b x + a) a^5 - a^6 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^4/(b*x+a)^(1/2),x, algorithm="maxima")

[Out]
$$-5/16*b^3*\log((\sqrt{b*x+a}-\sqrt{a})/(\sqrt{b*x+a}+\sqrt{a}))/a^{(7/2)} - 1/24*(15*(b*x+a)^{(5/2)}*b^3 - 40*(b*x+a)^{(3/2)}*a*b^3 + 33*\sqrt{b*x+a})*a^2*b^3/((b*x+a)^3*a^3 - 3*(b*x+a)^2*a^4 + 3*(b*x+a)*a^5 - a^6)$$

mupad [B] time = 0.05, size = 69, normalized size = 0.77

$$\frac{5(a+bx)^{3/2}}{3a^2x^3} - \frac{11\sqrt{a+bx}}{8ax^3} - \frac{5(a+bx)^{5/2}}{8a^3x^3} - \frac{b^3 \operatorname{atan}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{8a^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^4*(a+b*x)^(1/2)),x)

[Out]
$$(5*(a+b*x)^{(3/2)})/(3*a^2*x^3) - (11*(a+b*x)^{(1/2)})/(8*a*x^3) - (5*(a+b*x)^{(5/2)})/(8*a^3*x^3) - (b^3*\operatorname{atan}(((a+b*x)^{(1/2)}*1i)/a^{(1/2)})*5i)/(8*a^{(7/2)})$$

sympy [A] time = 7.02, size = 129, normalized size = 1.43

$$-\frac{1}{3\sqrt{b}x^2\sqrt{\frac{a}{bx}+1}} + \frac{\sqrt{b}}{12ax^2\sqrt{\frac{a}{bx}+1}} - \frac{5b^{\frac{3}{2}}}{24a^2x^2\sqrt{\frac{a}{bx}+1}} - \frac{5b^{\frac{5}{2}}}{8a^3\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{5b^3 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{8a^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**4/(b*x+a)**(1/2),x)

[Out]
$$-1/(3*\sqrt{b}*x^{(7/2)}*\sqrt{a/(b*x)+1}) + \sqrt{b}/(12*a*x^{(5/2)}*\sqrt{a/(b*x)+1}) - 5*b^{(3/2)}/(24*a^{(2)}*x^{(3/2)}*\sqrt{a/(b*x)+1}) - 5*b^{(5/2)}/(8*a^{(3)}*\sqrt{x}*\sqrt{a/(b*x)+1}) + 5*b^{(3)}*\operatorname{asinh}(\sqrt{a}/(\sqrt{b}*\sqrt{x}))/ (8*a^{(7/2)})$$

$$3.343 \quad \int \frac{x^4}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=85

$$-\frac{2a^4}{b^5\sqrt{a+bx}} - \frac{8a^3\sqrt{a+bx}}{b^5} + \frac{4a^2(a+bx)^{3/2}}{b^5} - \frac{8a(a+bx)^{5/2}}{5b^5} + \frac{2(a+bx)^{7/2}}{7b^5}$$

[Out] $4a^2(bx+a)^{(3/2)}/b^5-8/5a*(bx+a)^{(5/2)}/b^5+2/7*(bx+a)^{(7/2)}/b^5-2a^4/b^5/(bx+a)^{(1/2)}-8a^3*(bx+a)^{(1/2)}/b^5$

Rubi [A] time = 0.02, antiderivative size = 85, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{2a^4}{b^5\sqrt{a+bx}} - \frac{8a^3\sqrt{a+bx}}{b^5} + \frac{4a^2(a+bx)^{3/2}}{b^5} - \frac{8a(a+bx)^{5/2}}{5b^5} + \frac{2(a+bx)^{7/2}}{7b^5}$$

Antiderivative was successfully verified.

[In] Int[x^4/(a + b*x)^(3/2), x]

[Out] $(-2a^4)/(b^5*\text{Sqrt}[a + b*x]) - (8a^3*\text{Sqrt}[a + b*x])/b^5 + (4a^2*(a + b*x)^(3/2))/b^5 - (8a*(a + b*x)^(5/2))/(5*b^5) + (2*(a + b*x)^(7/2))/(7*b^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{(a+bx)^{3/2}} dx &= \int \left(\frac{a^4}{b^4(a+bx)^{3/2}} - \frac{4a^3}{b^4\sqrt{a+bx}} + \frac{6a^2\sqrt{a+bx}}{b^4} - \frac{4a(a+bx)^{3/2}}{b^4} + \frac{(a+bx)^{5/2}}{b^4} \right) dx \\ &= -\frac{2a^4}{b^5\sqrt{a+bx}} - \frac{8a^3\sqrt{a+bx}}{b^5} + \frac{4a^2(a+bx)^{3/2}}{b^5} - \frac{8a(a+bx)^{5/2}}{5b^5} + \frac{2(a+bx)^{7/2}}{7b^5} \end{aligned}$$

Mathematica [A] time = 0.03, size = 57, normalized size = 0.67

$$\frac{2(-128a^4 - 64a^3bx + 16a^2b^2x^2 - 8ab^3x^3 + 5b^4x^4)}{35b^5\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/(a + b*x)^(3/2), x]

[Out] (2*(-128*a^4 - 64*a^3*b*x + 16*a^2*b^2*x^2 - 8*a*b^3*x^3 + 5*b^4*x^4))/(35*b^5*Sqrt[a + b*x])

fricas [A] time = 0.42, size = 63, normalized size = 0.74

$$\frac{2(5b^4x^4 - 8ab^3x^3 + 16a^2b^2x^2 - 64a^3bx - 128a^4)\sqrt{bx+a}}{35(b^6x + ab^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^(3/2), x, algorithm="fricas")

[Out] 2/35*(5*b^4*x^4 - 8*a*b^3*x^3 + 16*a^2*b^2*x^2 - 64*a^3*b*x - 128*a^4)*sqrt(b*x + a)/(b^6*x + a*b^5)

giac [A] time = 1.25, size = 77, normalized size = 0.91

$$-\frac{2a^4}{\sqrt{bx+ab^5}} + \frac{2\left(5(bx+a)^{\frac{7}{2}}b^{30} - 28(bx+a)^{\frac{5}{2}}ab^{30} + 70(bx+a)^{\frac{3}{2}}a^2b^{30} - 140\sqrt{bx+a}a^3b^{30}\right)}{35b^{35}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^(3/2), x, algorithm="giac")

[Out] -2*a^4/(sqrt(b*x + a)*b^5) + 2/35*(5*(b*x + a)^(7/2)*b^30 - 28*(b*x + a)^(5/2)*a*b^30 + 70*(b*x + a)^(3/2)*a^2*b^30 - 140*sqrt(b*x + a)*a^3*b^30)/b^35

maple [A] time = 0.01, size = 54, normalized size = 0.64

$$\frac{2(-5x^4b^4 + 8ax^3b^3 - 16a^2x^2b^2 + 64a^3xb + 128a^4)}{35\sqrt{bx+a}b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(b*x+a)^(3/2), x)

[Out] -2/35/(b*x+a)^(1/2)*(-5*b^4*x^4+8*a*b^3*x^3-16*a^2*b^2*x^2+64*a^3*b*x+128*a^4)/b^5

maxima [A] time = 1.33, size = 71, normalized size = 0.84

$$\frac{2(bx+a)^{\frac{7}{2}}}{7b^5} - \frac{8(bx+a)^{\frac{5}{2}}a}{5b^5} + \frac{4(bx+a)^{\frac{3}{2}}a^2}{b^5} - \frac{8\sqrt{bx+a}a^3}{b^5} - \frac{2a^4}{\sqrt{bx+a}b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] $\frac{2}{7}*(b*x + a)^{(7/2)}/b^5 - \frac{8}{5}*(b*x + a)^{(5/2)}*a/b^5 + 4*(b*x + a)^{(3/2)}*a^2/b^5 - 8*\sqrt{b*x + a}*a^3/b^5 - 2*a^4/(\sqrt{b*x + a}*b^5)$

mupad [B] time = 0.03, size = 71, normalized size = 0.84

$$\frac{2(a+bx)^{7/2}}{7b^5} - \frac{8a^3\sqrt{a+bx}}{b^5} + \frac{4a^2(a+bx)^{3/2}}{b^5} - \frac{2a^4}{b^5\sqrt{a+bx}} - \frac{8a(a+bx)^{5/2}}{5b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(a + b*x)^(3/2),x)

[Out] $(2*(a + b*x)^{(7/2)})/(7*b^5) - (8*a^3*(a + b*x)^{(1/2)})/b^5 + (4*a^2*(a + b*x)^{(3/2)})/b^5 - (2*a^4)/(b^5*(a + b*x)^{(1/2)}) - (8*a*(a + b*x)^{(5/2)})/(5*b^5)$

sympy [B] time = 4.81, size = 3606, normalized size = 42.42

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/(b*x+a)**(3/2),x)

[Out] $-256*a^{(87/2)}*\sqrt{1 + b*x/a}/(35*a^{40}*b^{55} + 350*a^{39}*b^{56}*x + 1575*a^{38}*b^{57}*x^2 + 4200*a^{37}*b^{58}*x^3 + 7350*a^{36}*b^{59}*x^4 + 8820*a^{35}*b^{60}*x^5 + 7350*a^{34}*b^{61}*x^6 + 4200*a^{33}*b^{62}*x^7 + 1575*a^{32}*b^{63}*x^8 + 350*a^{31}*b^{64}*x^9 + 35*a^{30}*b^{65}*x^{10}) + 256*a^{(87/2)}/(35*a^{40}*b^{55} + 350*a^{39}*b^{56}*x + 1575*a^{38}*b^{57}*x^2 + 4200*a^{37}*b^{58}*x^3 + 7350*a^{36}*b^{59}*x^4 + 8820*a^{35}*b^{60}*x^5 + 7350*a^{34}*b^{61}*x^6 + 4200*a^{33}*b^{62}*x^7 + 1575*a^{32}*b^{63}*x^8 + 350*a^{31}*b^{64}*x^9 + 35*a^{30}*b^{65}*x^{10}) - 2432*a^{(85/2)}*b*x*\sqrt{1 + b*x/a}/(35*a^{40}*b^{55} + 350*a^{39}*b^{56}*x + 1575*a^{38}*b^{57}*x^2 + 4200*a^{37}*b^{58}*x^3 + 7350*a^{36}*b^{59}*x^4 + 8820*a^{35}*b^{60}*x^5 + 7350*a^{34}*b^{61}*x^6 + 4200*a^{33}*b^{62}*x^7 + 1575*a^{32}*b^{63}*x^8 + 350*a^{31}*b^{64}*x^9 + 35*a^{30}*b^{65}*x^{10}) + 2560*a^{(85/2)}*b*x/(35*a^{40}*b^{55} + 350*a^{39}*b^{56}*x + 1575*a^{38}*b^{57}*x^2 + 4200*a^{37}*b^{58}*x^3 + 7350*a^{36}*b^{59}*x^4 + 8820*a^{35}*b^{60}*x^5 + 7350*a^{34}*b^{61}*x^6 + 4200*a^{33}*b^{62}*x^7 + 1575*a^{32}*b^{63}*x^8 + 350*a^{31}*b^{64}*x^9 + 35*a^{30}*b^{65}*x^{10}) - 10336*a^{(83/2)}*b^2*x^2*\sqrt{1 + b*x/a}/(35*a^{40}*b^{55} + 350*a^{39}*b^{56}*x + 1575*a^{38}*b^{57}*x^2 + 4200*a^{37}*b^{58}*x^3 + 7350*a^{36}*b^{59}*x^4 + 8820*a^{35}*b^{60}*x^5 + 7350*a^{34}*b^{61}*x^6 + 4200*a^{33}*b^{62}*x^7 + 1575*a^{32}*b^{63}*x^8 + 350*a^{31}*b^{64}*x^9 + 35*a^{30}*b^{65}*x^{10}) + 11520*a^{(83/2)}*b^2*x^2/(35*a^{40}*b^{55} + 3$

$$\begin{aligned}
& 50a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10} \\
& - 25840a^{30}(81/2)b^3x^3\sqrt{1 + b^2x/a}/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& + 30720a^{30}(81/2)b^3x^3/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& - 41990a^{30}(79/2)b^4x^4\sqrt{1 + b^2x/a}/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& + 53760a^{30}(79/2)b^4x^4/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& - 46182a^{30}(77/2)b^5x^5\sqrt{1 + b^2x/a}/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& + 64512a^{30}(77/2)b^5x^5/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& - 34584a^{30}(75/2)b^6x^6\sqrt{1 + b^2x/a}/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& + 53760a^{30}(75/2)b^6x^6/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& - 17112a^{30}(73/2)b^7x^7\sqrt{1 + b^2x/a}/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& + 30720a^{30}(73/2)b^7x^7/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& - 4980a^{30}(71/2)b^8x^8\sqrt{1 + b^2x/a}/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10}) \\
& + 11520a^{30}(71/2)b^8x^8/(35a^{40}b^5 + 350a^{39}b^6x + 1575a^{38}b^7x^2 + 4200a^{37}b^8x^3 + 7350a^{36}b^9x^4 + 8820a^{35}b^{10}x^5 + 7350a^{34}b^{11}x^6 + 4200a^{33}b^{12}x^7 + 1575a^{32}b^{13}x^8 + 350a^{31}b^{14}x^9 + 35a^{30}b^{15}x^{10})
\end{aligned}$$

$$\begin{aligned}
& b^{**5} + 350*a^{**39}*b^{**6}*x + 1575*a^{**38}*b^{**7}*x^{**2} + 4200*a^{**37}*b^{**8}*x^{**3} + 7350*a^{**36}*b^{**9}*x^{**4} + 8820*a^{**35}*b^{**10}*x^{**5} + 7350*a^{**34}*b^{**11}*x^{**6} + 4200*a^{**33}*b^{**12}*x^{**7} + 1575*a^{**32}*b^{**13}*x^{**8} + 350*a^{**31}*b^{**14}*x^{**9} + 35*a^{**30}*b^{**15}*x^{**10} \\
& - 340*a^{**69/2}*b^{**9}*x^{**9}*sqrt(1 + b*x/a)/(35*a^{**40}*b^{**5} + 350*a^{**39}*b^{**6}*x + 1575*a^{**38}*b^{**7}*x^{**2} + 4200*a^{**37}*b^{**8}*x^{**3} + 7350*a^{**36}*b^{**9}*x^{**4} + 8820*a^{**35}*b^{**10}*x^{**5} + 7350*a^{**34}*b^{**11}*x^{**6} + 4200*a^{**33}*b^{**12}*x^{**7} + 1575*a^{**32}*b^{**13}*x^{**8} + 350*a^{**31}*b^{**14}*x^{**9} + 35*a^{**30}*b^{**15}*x^{**10}) \\
& + 2560*a^{**69/2}*b^{**9}*x^{**9}/(35*a^{**40}*b^{**5} + 350*a^{**39}*b^{**6}*x + 1575*a^{**38}*b^{**7}*x^{**2} + 4200*a^{**37}*b^{**8}*x^{**3} + 7350*a^{**36}*b^{**9}*x^{**4} + 8820*a^{**35}*b^{**10}*x^{**5} + 7350*a^{**34}*b^{**11}*x^{**6} + 4200*a^{**33}*b^{**12}*x^{**7} + 1575*a^{**32}*b^{**13}*x^{**8} + 350*a^{**31}*b^{**14}*x^{**9} + 35*a^{**30}*b^{**15}*x^{**10}) \\
& + 424*a^{**67/2}*b^{**10}*x^{**10}*sqrt(1 + b*x/a)/(35*a^{**40}*b^{**5} + 350*a^{**39}*b^{**6}*x + 1575*a^{**38}*b^{**7}*x^{**2} + 4200*a^{**37}*b^{**8}*x^{**3} + 7350*a^{**36}*b^{**9}*x^{**4} + 8820*a^{**35}*b^{**10}*x^{**5} + 7350*a^{**34}*b^{**11}*x^{**6} + 4200*a^{**33}*b^{**12}*x^{**7} + 1575*a^{**32}*b^{**13}*x^{**8} + 350*a^{**31}*b^{**14}*x^{**9} + 35*a^{**30}*b^{**15}*x^{**10}) \\
& + 256*a^{**67/2}*b^{**10}*x^{**10}/(35*a^{**40}*b^{**5} + 350*a^{**39}*b^{**6}*x + 1575*a^{**38}*b^{**7}*x^{**2} + 4200*a^{**37}*b^{**8}*x^{**3} + 7350*a^{**36}*b^{**9}*x^{**4} + 8820*a^{**35}*b^{**10}*x^{**5} + 7350*a^{**34}*b^{**11}*x^{**6} + 4200*a^{**33}*b^{**12}*x^{**7} + 1575*a^{**32}*b^{**13}*x^{**8} + 350*a^{**31}*b^{**14}*x^{**9} + 35*a^{**30}*b^{**15}*x^{**10}) \\
& + 248*a^{**65/2}*b^{**11}*x^{**11}*sqrt(1 + b*x/a)/(35*a^{**40}*b^{**5} + 350*a^{**39}*b^{**6}*x + 1575*a^{**38}*b^{**7}*x^{**2} + 4200*a^{**37}*b^{**8}*x^{**3} + 7350*a^{**36}*b^{**9}*x^{**4} + 8820*a^{**35}*b^{**10}*x^{**5} + 7350*a^{**34}*b^{**11}*x^{**6} + 4200*a^{**33}*b^{**12}*x^{**7} + 1575*a^{**32}*b^{**13}*x^{**8} + 350*a^{**31}*b^{**14}*x^{**9} + 35*a^{**30}*b^{**15}*x^{**10}) \\
& + 74*a^{**63/2}*b^{**12}*x^{**12}*sqrt(1 + b*x/a)/(35*a^{**40}*b^{**5} + 350*a^{**39}*b^{**6}*x + 1575*a^{**38}*b^{**7}*x^{**2} + 4200*a^{**37}*b^{**8}*x^{**3} + 7350*a^{**36}*b^{**9}*x^{**4} + 8820*a^{**35}*b^{**10}*x^{**5} + 7350*a^{**34}*b^{**11}*x^{**6} + 4200*a^{**33}*b^{**12}*x^{**7} + 1575*a^{**32}*b^{**13}*x^{**8} + 350*a^{**31}*b^{**14}*x^{**9} + 35*a^{**30}*b^{**15}*x^{**10}) \\
& + 10*a^{**61/2}*b^{**13}*x^{**13}*sqrt(1 + b*x/a)/(35*a^{**40}*b^{**5} + 350*a^{**39}*b^{**6}*x + 1575*a^{**38}*b^{**7}*x^{**2} + 4200*a^{**37}*b^{**8}*x^{**3} + 7350*a^{**36}*b^{**9}*x^{**4} + 8820*a^{**35}*b^{**10}*x^{**5} + 7350*a^{**34}*b^{**11}*x^{**6} + 4200*a^{**33}*b^{**12}*x^{**7} + 1575*a^{**32}*b^{**13}*x^{**8} + 350*a^{**31}*b^{**14}*x^{**9} + 35*a^{**30}*b^{**15}*x^{**10})
\end{aligned}$$

$$3.344 \quad \int \frac{x^3}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=66

$$\frac{2a^3}{b^4\sqrt{a+bx}} + \frac{6a^2\sqrt{a+bx}}{b^4} - \frac{2a(a+bx)^{3/2}}{b^4} + \frac{2(a+bx)^{5/2}}{5b^4}$$

[Out] $-2*a*(b*x+a)^{(3/2)}/b^4+2/5*(b*x+a)^{(5/2)}/b^4+2*a^3/b^4/(b*x+a)^{(1/2)}+6*a^2*(b*x+a)^{(1/2)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2a^3}{b^4\sqrt{a+bx}} + \frac{6a^2\sqrt{a+bx}}{b^4} - \frac{2a(a+bx)^{3/2}}{b^4} + \frac{2(a+bx)^{5/2}}{5b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x)^(3/2), x]

[Out] $(2*a^3)/(b^4*\text{Sqrt}[a + b*x]) + (6*a^2*\text{Sqrt}[a + b*x])/b^4 - (2*a*(a + b*x)^{(3/2)}/b^4 + (2*(a + b*x)^{(5/2)})/(5*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(a+bx)^{3/2}} dx &= \int \left(-\frac{a^3}{b^3(a+bx)^{3/2}} + \frac{3a^2}{b^3\sqrt{a+bx}} - \frac{3a\sqrt{a+bx}}{b^3} + \frac{(a+bx)^{3/2}}{b^3} \right) dx \\ &= \frac{2a^3}{b^4\sqrt{a+bx}} + \frac{6a^2\sqrt{a+bx}}{b^4} - \frac{2a(a+bx)^{3/2}}{b^4} + \frac{2(a+bx)^{5/2}}{5b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 0.68

$$\frac{2(16a^3 + 8a^2bx - 2ab^2x^2 + b^3x^3)}{5b^4\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x)^(3/2), x]

[Out] (2*(16*a^3 + 8*a^2*b*x - 2*a*b^2*x^2 + b^3*x^3))/(5*b^4*Sqrt[a + b*x])

fricas [A] time = 0.45, size = 51, normalized size = 0.77

$$\frac{2(b^3x^3 - 2ab^2x^2 + 8a^2bx + 16a^3)\sqrt{bx + a}}{5(b^5x + ab^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(3/2), x, algorithm="fricas")

[Out] 2/5*(b^3*x^3 - 2*a*b^2*x^2 + 8*a^2*b*x + 16*a^3)*sqrt(b*x + a)/(b^5*x + a*b^4)

giac [A] time = 1.10, size = 61, normalized size = 0.92

$$\frac{2a^3}{\sqrt{bx + a}b^4} + \frac{2\left((bx + a)^{\frac{5}{2}}b^{16} - 5(bx + a)^{\frac{3}{2}}ab^{16} + 15\sqrt{bx + a}a^2b^{16}\right)}{5b^{20}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(3/2), x, algorithm="giac")

[Out] 2*a^3/(sqrt(b*x + a)*b^4) + 2/5*((b*x + a)^(5/2)*b^16 - 5*(b*x + a)^(3/2)*a*b^16 + 15*sqrt(b*x + a)*a^2*b^16)/b^20

maple [A] time = 0.01, size = 42, normalized size = 0.64

$$\frac{\frac{2}{5}b^3x^3 - \frac{4}{5}ab^2x^2 + \frac{16}{5}a^2bx + \frac{32}{5}a^3}{b^4\sqrt{bx + a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^(3/2), x)

[Out] 2/5/(b*x+a)^(1/2)*(b^3*x^3-2*a*b^2*x^2+8*a^2*b*x+16*a^3)/b^4

maxima [A] time = 1.38, size = 56, normalized size = 0.85

$$\frac{2(bx + a)^{\frac{5}{2}}}{5b^4} - \frac{2(bx + a)^{\frac{3}{2}}a}{b^4} + \frac{6\sqrt{bx + a}a^2}{b^4} + \frac{2a^3}{\sqrt{bx + a}b^4}$$

$$\begin{aligned}
& 9x^{**5} + 5a^{**14}b^{**10}x^{**6}) - 480a^{**}(37/2)*b^{**4}x^{**4}/(5a^{**20}b^{**4} + 30a^{**19}b^{**5}x + 75a^{**18}b^{**6}x^{**2} + 100a^{**17}b^{**7}x^{**3} + 75a^{**16}b^{**8}x^{**4} \\
& + 30a^{**15}b^{**9}x^{**5} + 5a^{**14}b^{**10}x^{**6}) + 92a^{**}(35/2)*b^{**5}x^{**5}\sqrt{1 + b*x/a}/(5a^{**20}b^{**4} + 30a^{**19}b^{**5}x + 75a^{**18}b^{**6}x^{**2} + 100a^{**17}b^{**7}x^{**3} + 75a^{**16}b^{**8}x^{**4} + 30a^{**15}b^{**9}x^{**5} + 5a^{**14}b^{**10}x^{**6}) - \\
& 192a^{**}(35/2)*b^{**5}x^{**5}/(5a^{**20}b^{**4} + 30a^{**19}b^{**5}x + 75a^{**18}b^{**6}x^{**2} + 100a^{**17}b^{**7}x^{**3} + 75a^{**16}b^{**8}x^{**4} + 30a^{**15}b^{**9}x^{**5} + 5a^{**14}b^{**10}x^{**6}) + 16a^{**}(33/2)*b^{**6}x^{**6}\sqrt{1 + b*x/a}/(5a^{**20}b^{**4} + 30a^{**19}b^{**5}x + 75a^{**18}b^{**6}x^{**2} + 100a^{**17}b^{**7}x^{**3} + 75a^{**16}b^{**8}x^{**4} + 30a^{**15}b^{**9}x^{**5} + 5a^{**14}b^{**10}x^{**6}) - 32a^{**}(33/2)*b^{**6}x^{**6}/(5a^{**20}b^{**4} + 30a^{**19}b^{**5}x + 75a^{**18}b^{**6}x^{**2} + 100a^{**17}b^{**7}x^{**3} + 75a^{**16}b^{**8}x^{**4} + 30a^{**15}b^{**9}x^{**5} + 5a^{**14}b^{**10}x^{**6}) + 6a^{**}(31/2)*b^{**7}x^{**7}\sqrt{1 + b*x/a}/(5a^{**20}b^{**4} + 30a^{**19}b^{**5}x + 75a^{**18}b^{**6}x^{**2} + 100a^{**17}b^{**7}x^{**3} + 75a^{**16}b^{**8}x^{**4} + 30a^{**15}b^{**9}x^{**5} + 5a^{**14}b^{**10}x^{**6}) + 2a^{**}(29/2)*b^{**8}x^{**8}\sqrt{1 + b*x/a}/(5a^{**20}b^{**4} + 30a^{**19}b^{**5}x + 75a^{**18}b^{**6}x^{**2} + 100a^{**17}b^{**7}x^{**3} + 75a^{**16}b^{**8}x^{**4} + 30a^{**15}b^{**9}x^{**5} + 5a^{**14}b^{**10}x^{**6})
\end{aligned}$$

$$3.345 \quad \int \frac{x^2}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=49

$$-\frac{2a^2}{b^3\sqrt{a+bx}} - \frac{4a\sqrt{a+bx}}{b^3} + \frac{2(a+bx)^{3/2}}{3b^3}$$

[Out] $2/3*(b*x+a)^{(3/2)}/b^3-2*a^2/b^3/(b*x+a)^{(1/2)}-4*a*(b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{2a^2}{b^3\sqrt{a+bx}} - \frac{4a\sqrt{a+bx}}{b^3} + \frac{2(a+bx)^{3/2}}{3b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*x)^(3/2), x]

[Out] $(-2*a^2)/(b^3*sqrt[a + b*x]) - (4*a*sqrt[a + b*x])/b^3 + (2*(a + b*x)^{(3/2)})/(3*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(a+bx)^{3/2}} dx &= \int \left(\frac{a^2}{b^2(a+bx)^{3/2}} - \frac{2a}{b^2\sqrt{a+bx}} + \frac{\sqrt{a+bx}}{b^2} \right) dx \\ &= -\frac{2a^2}{b^3\sqrt{a+bx}} - \frac{4a\sqrt{a+bx}}{b^3} + \frac{2(a+bx)^{3/2}}{3b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 34, normalized size = 0.69

$$\frac{2(-8a^2 - 4abx + b^2x^2)}{3b^3\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x)^(3/2), x]

[Out] (2*(-8*a^2 - 4*a*b*x + b^2*x^2))/(3*b^3*Sqrt[a + b*x])

fricas [A] time = 0.45, size = 40, normalized size = 0.82

$$\frac{2(b^2x^2 - 4abx - 8a^2)\sqrt{bx + a}}{3(b^4x + ab^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(3/2), x, algorithm="fricas")

[Out] 2/3*(b^2*x^2 - 4*a*b*x - 8*a^2)*sqrt(b*x + a)/(b^4*x + a*b^3)

giac [A] time = 1.14, size = 46, normalized size = 0.94

$$-\frac{2a^2}{\sqrt{bx + a}b^3} + \frac{2\left((bx + a)^{\frac{3}{2}}b^6 - 6\sqrt{bx + a}ab^6\right)}{3b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(3/2), x, algorithm="giac")

[Out] -2*a^2/(sqrt(b*x + a)*b^3) + 2/3*((b*x + a)^(3/2)*b^6 - 6*sqrt(b*x + a)*a*b^6)/b^9

maple [A] time = 0.01, size = 32, normalized size = 0.65

$$\frac{2(-b^2x^2 + 4abx + 8a^2)}{3\sqrt{bx + a}b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^(3/2), x)

[Out] -2/3/(b*x+a)^(1/2)*(-b^2*x^2+4*a*b*x+8*a^2)/b^3

maxima [A] time = 1.29, size = 41, normalized size = 0.84

$$\frac{2(bx + a)^{\frac{3}{2}}}{3b^3} - \frac{4\sqrt{bx + a}a}{b^3} - \frac{2a^2}{\sqrt{bx + a}b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] $\frac{2}{3}*(b*x + a)^{(3/2)}/b^3 - 4*\sqrt{b*x + a}*a/b^3 - 2*a^2/(\sqrt{b*x + a})*b^3)$

mupad [B] time = 0.04, size = 35, normalized size = 0.71

$$\frac{12 a (a + b x) - 2 (a + b x)^2 + 6 a^2}{3 b^3 \sqrt{a + b x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(a + b*x)^(3/2),x)

[Out] $-(12*a*(a + b*x) - 2*(a + b*x)^2 + 6*a^2)/(3*b^3*(a + b*x)^{(1/2)})$

sympy [B] time = 1.83, size = 534, normalized size = 10.90

$$\frac{16a^{\frac{19}{2}}\sqrt{1+\frac{bx}{a}}}{3a^8b^3+9a^7b^4x+9a^6b^5x^2+3a^5b^6x^3} + \frac{16a^{\frac{19}{2}}}{3a^8b^3+9a^7b^4x+9a^6b^5x^2+3a^5b^6x^3} - \frac{40a^{\frac{17}{2}}bx\sqrt{1+\frac{bx}{a}}}{3a^8b^3+9a^7b^4x+9a^6b^5x^2+3a^5b^6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(b*x+a)**(3/2),x)

[Out] $-16*a**(19/2)*\sqrt{1 + b*x/a}/(3*a**8*b**3 + 9*a**7*b**4*x + 9*a**6*b**5*x**2 + 3*a**5*b**6*x**3) + 16*a**(19/2)/(3*a**8*b**3 + 9*a**7*b**4*x + 9*a**6*b**5*x**2 + 3*a**5*b**6*x**3) - 40*a**(17/2)*b*x*\sqrt{1 + b*x/a}/(3*a**8*b**3 + 9*a**7*b**4*x + 9*a**6*b**5*x**2 + 3*a**5*b**6*x**3) + 48*a**(17/2)*b*x/(3*a**8*b**3 + 9*a**7*b**4*x + 9*a**6*b**5*x**2 + 3*a**5*b**6*x**3) - 30*a**(15/2)*b**2*x**2*\sqrt{1 + b*x/a}/(3*a**8*b**3 + 9*a**7*b**4*x + 9*a**6*b**5*x**2 + 3*a**5*b**6*x**3) + 48*a**(15/2)*b**2*x**2/(3*a**8*b**3 + 9*a**7*b**4*x + 9*a**6*b**5*x**2 + 3*a**5*b**6*x**3) - 4*a**(13/2)*b**3*x**3*\sqrt{1 + b*x/a}/(3*a**8*b**3 + 9*a**7*b**4*x + 9*a**6*b**5*x**2 + 3*a**5*b**6*x**3) + 16*a**(13/2)*b**3*x**3/(3*a**8*b**3 + 9*a**7*b**4*x + 9*a**6*b**5*x**2 + 3*a**5*b**6*x**3) + 2*a**(11/2)*b**4*x**4*\sqrt{1 + b*x/a}/(3*a**8*b**3 + 9*a**7*b**4*x + 9*a**6*b**5*x**2 + 3*a**5*b**6*x**3)$

$$3.346 \quad \int \frac{x}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=30

$$\frac{2a}{b^2\sqrt{a+bx}} + \frac{2\sqrt{a+bx}}{b^2}$$

[Out] 2*a/b^2/(b*x+a)^(1/2)+2*(b*x+a)^(1/2)/b^2

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{2a}{b^2\sqrt{a+bx}} + \frac{2\sqrt{a+bx}}{b^2}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x)^(3/2), x]

[Out] (2*a)/(b^2*Sqrt[a + b*x]) + (2*Sqrt[a + b*x])/b^2

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x}{(a+bx)^{3/2}} dx &= \int \left(-\frac{a}{b(a+bx)^{3/2}} + \frac{1}{b\sqrt{a+bx}} \right) dx \\ &= \frac{2a}{b^2\sqrt{a+bx}} + \frac{2\sqrt{a+bx}}{b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 21, normalized size = 0.70

$$\frac{2(2a+bx)}{b^2\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x)^(3/2),x]

[Out] (2*(2*a + b*x))/(b^2*Sqrt[a + b*x])

fricas [A] time = 0.48, size = 29, normalized size = 0.97

$$\frac{2(bx + 2a)\sqrt{bx + a}}{b^3x + ab^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] 2*(b*x + 2*a)*sqrt(b*x + a)/(b^3*x + a*b^2)

giac [A] time = 1.00, size = 29, normalized size = 0.97

$$\frac{2\left(\frac{\sqrt{bx+a}}{b} + \frac{a}{\sqrt{bx+ab}}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)^(3/2),x, algorithm="giac")

[Out] 2*(sqrt(b*x + a)/b + a/(sqrt(b*x + a)*b))/b

maple [A] time = 0.00, size = 20, normalized size = 0.67

$$\frac{2bx + 4a}{b^2\sqrt{bx + a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(b*x+a)^(3/2),x)

[Out] 2/(b*x+a)^(1/2)*(b*x+2*a)/b^2

maxima [A] time = 1.32, size = 26, normalized size = 0.87

$$\frac{2\sqrt{bx + a}}{b^2} + \frac{2a}{\sqrt{bx + a}b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] 2*sqrt(b*x + a)/b^2 + 2*a/(sqrt(b*x + a)*b^2)

mupad [B] time = 0.09, size = 19, normalized size = 0.63

$$\frac{4a + 2bx}{b^2 \sqrt{a + bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a + b*x)^(3/2), x)`

[Out] `(4*a + 2*b*x)/(b^2*(a + b*x)^(1/2))`

sympy [A] time = 0.67, size = 37, normalized size = 1.23

$$\begin{cases} \frac{4a}{b^2 \sqrt{a+bx}} + \frac{2x}{b \sqrt{a+bx}} & \text{for } b \neq 0 \\ \frac{x^2}{2a^{\frac{3}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)**(3/2), x)`

[Out] `Piecewise((4*a/(b**2*sqrt(a + b*x)) + 2*x/(b*sqrt(a + b*x)), Ne(b, 0)), (x**2/(2*a**(3/2)), True))`

$$3.347 \quad \int \frac{1}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=14

$$-\frac{2}{b\sqrt{a+bx}}$$

[Out] -2/b/(b*x+a)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$-\frac{2}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-3/2), x]

[Out] -2/(b*Sqrt[a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^{3/2}} dx = -\frac{2}{b\sqrt{a+bx}}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\frac{2}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-3/2), x]

[Out] -2/(b*Sqrt[a + b*x])

fricas [A] time = 0.46, size = 20, normalized size = 1.43

$$-\frac{2\sqrt{bx+a}}{b^2x+ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] -2*sqrt(b*x + a)/(b^2*x + a*b)

giac [A] time = 1.24, size = 12, normalized size = 0.86

$$-\frac{2}{\sqrt{bx + a} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2),x, algorithm="giac")

[Out] -2/(sqrt(b*x + a)*b)

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$-\frac{2}{\sqrt{bx + a} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2),x)

[Out] -2/b/(b*x+a)^(1/2)

maxima [A] time = 1.34, size = 12, normalized size = 0.86

$$-\frac{2}{\sqrt{bx + a} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] -2/(sqrt(b*x + a)*b)

mupad [B] time = 0.02, size = 12, normalized size = 0.86

$$-\frac{2}{b\sqrt{a + bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x)^(3/2),x)

[Out] $-2/(b*(a + b*x)^{(1/2)})$

sympy [A] time = 0.07, size = 12, normalized size = 0.86

$$-\frac{2}{b\sqrt{a + bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(3/2),x)`

[Out] $-2/(b*\text{sqrt}(a + b*x))$

$$3.348 \quad \int \frac{1}{x(a+bx)^{3/2}} dx$$

Optimal. Leaf size=38

$$\frac{2}{a\sqrt{a+bx}} - \frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{3/2}}$$

[Out] $-2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(3/2)}+2/a/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 208}

$$\frac{2}{a\sqrt{a+bx}} - \frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{3/2}}$$

Antiderivative was successfully verified.

[In] `Int[1/(x*(a + b*x)^(3/2)),x]`

[Out] $2/(a*\operatorname{Sqrt}[a + b*x]) - (2*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/a^{3/2}$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x(a+bx)^{3/2}} dx &= \frac{2}{a\sqrt{a+bx}} + \frac{\int \frac{1}{x\sqrt{a+bx}} dx}{a} \\
&= \frac{2}{a\sqrt{a+bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{\frac{-a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{ab} \\
&= \frac{2}{a\sqrt{a+bx}} - \frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{3/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.79

$$\frac{{}_2F_1\left(-\frac{1}{2}, 1; \frac{1}{2}; \frac{bx}{a} + 1\right)}{a\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)^(3/2)),x]

[Out] (2*Hypergeometric2F1[-1/2, 1, 1/2, 1 + (b*x)/a])/(a*Sqrt[a + b*x])

fricas [A] time = 0.46, size = 110, normalized size = 2.89

$$\left[\frac{(bx+a)\sqrt{a} \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a}+2a}{x}\right) + 2\sqrt{bx+a}a}{a^2bx+a^3}, \frac{2\left((bx+a)\sqrt{-a} \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right) + \sqrt{bx+a}a\right)}{a^2bx+a^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] [((b*x + a)*sqrt(a)*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*sqrt(b*x + a)*a)/(a^2*b*x + a^3), 2*((b*x + a)*sqrt(-a)*arctan(sqrt(b*x + a)*sqrt(-a)/a) + sqrt(b*x + a)*a)/(a^2*b*x + a^3)]

giac [A] time = 1.07, size = 37, normalized size = 0.97

$$\frac{2 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}a} + \frac{2}{\sqrt{bx+a}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(3/2),x, algorithm="giac")

[Out] 2*arctan(sqrt(b*x + a)/sqrt(-a))/(sqrt(-a)*a) + 2/(sqrt(b*x + a)*a)

maple [A] time = 0.01, size = 31, normalized size = 0.82

$$-\frac{2 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{a^{\frac{3}{2}}} + \frac{2}{\sqrt{bx+a} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a)^(3/2),x)

[Out] -2*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(3/2)+2/a/(b*x+a)^(1/2)

maxima [A] time = 2.93, size = 45, normalized size = 1.18

$$\frac{\log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{a^{\frac{3}{2}}} + \frac{2}{\sqrt{bx+a} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a)))/a^(3/2) + 2/(sqrt(b*x + a)*a)

mupad [B] time = 0.04, size = 30, normalized size = 0.79

$$\frac{2}{a \sqrt{a+bx}} - \frac{2 \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(a + b*x)^(3/2)),x)

[Out] 2/(a*(a + b*x)^(1/2)) - (2*atanh((a + b*x)^(1/2)/a^(1/2)))/a^(3/2)

sympy [B] time = 1.87, size = 146, normalized size = 3.84

$$\frac{2a^3 \sqrt{1 + \frac{bx}{a}}}{a^{\frac{9}{2}} + a^{\frac{7}{2}} bx} + \frac{a^3 \log\left(\frac{bx}{a}\right)}{a^{\frac{9}{2}} + a^{\frac{7}{2}} bx} - \frac{2a^3 \log\left(\sqrt{1 + \frac{bx}{a}} + 1\right)}{a^{\frac{9}{2}} + a^{\frac{7}{2}} bx} + \frac{a^2 bx \log\left(\frac{bx}{a}\right)}{a^{\frac{9}{2}} + a^{\frac{7}{2}} bx} - \frac{2a^2 bx \log\left(\sqrt{1 + \frac{bx}{a}} + 1\right)}{a^{\frac{9}{2}} + a^{\frac{7}{2}} bx}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x/(b*x+a)**(3/2),x)
```

```
[Out] 2*a**3*sqrt(1 + b*x/a)/(a**(9/2) + a**(7/2)*b*x) + a**3*log(b*x/a)/(a**(9/2)
) + a**(7/2)*b*x) - 2*a**3*log(sqrt(1 + b*x/a) + 1)/(a**(9/2) + a**(7/2)*b*
x) + a**2*b*x*log(b*x/a)/(a**(9/2) + a**(7/2)*b*x) - 2*a**2*b*x*log(sqrt(1
+ b*x/a) + 1)/(a**(9/2) + a**(7/2)*b*x)
```

$$3.349 \quad \int \frac{1}{x^2(a+bx)^{3/2}} dx$$

Optimal. Leaf size=57

$$\frac{3b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{3b}{a^2\sqrt{a+bx}} - \frac{1}{ax\sqrt{a+bx}}$$

[Out] $3*b*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(5/2)}-3*b/a^2/(b*x+a)^{(1/2)}-1/a/x/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 59, normalized size of antiderivative = 1.04, number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 208}

$$-\frac{3\sqrt{a+bx}}{a^2x} + \frac{3b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{5/2}} + \frac{2}{ax\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] `Int[1/(x^2*(a + b*x)^(3/2)),x]`

[Out] $2/(a*x*\operatorname{Sqrt}[a + b*x]) - (3*\operatorname{Sqrt}[a + b*x])/(a^2*x) + (3*b*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/a^{(5/2)}$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^2(a+bx)^{3/2}} dx &= \frac{2}{ax\sqrt{a+bx}} + \frac{3 \int \frac{1}{x^2\sqrt{a+bx}} dx}{a} \\
 &= \frac{2}{ax\sqrt{a+bx}} - \frac{3\sqrt{a+bx}}{a^2x} - \frac{(3b) \int \frac{1}{x\sqrt{a+bx}} dx}{2a^2} \\
 &= \frac{2}{ax\sqrt{a+bx}} - \frac{3\sqrt{a+bx}}{a^2x} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{a^2} \\
 &= \frac{2}{ax\sqrt{a+bx}} - \frac{3\sqrt{a+bx}}{a^2x} + \frac{3b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 31, normalized size = 0.54

$$\frac{2b {}_2F_1\left(-\frac{1}{2}, 2; \frac{1}{2}; \frac{bx}{a} + 1\right)}{a^2\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)^(3/2)), x]

[Out] (-2*b*Hypergeometric2F1[-1/2, 2, 1/2, 1 + (b*x)/a])/(a^2*Sqrt[a + b*x])

fricas [A] time = 0.50, size = 151, normalized size = 2.65

$$\left[\frac{3(b^2x^2 + abx)\sqrt{a} \log\left(\frac{bx+2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2(3abx + a^2)\sqrt{bx+a}}{2(a^3bx^2 + a^4x)}, -\frac{3(b^2x^2 + abx)\sqrt{-a} \arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right)}{a^3bx^2 + a^4x} \right] +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(3/2), x, algorithm="fricas")

[Out] [1/2*(3*(b^2*x^2 + a*b*x)*sqrt(a)*log((b*x + 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) - 2*(3*a*b*x + a^2)*sqrt(b*x + a))/(a^3*b*x^2 + a^4*x), -(3*(b^2*x^2 +

$a*b*x)*\sqrt{-a}*\arctan(\sqrt{b*x + a}*\sqrt{-a}/a) + (3*a*b*x + a^2)*\sqrt{b*x + a})/(a^3*b*x^2 + a^4*x)]$

giac [A] time = 0.90, size = 64, normalized size = 1.12

$$-\frac{3b \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a} a^2} - \frac{3(bx+a)b - 2ab}{\left((bx+a)^2 - \sqrt{bx+a} a\right) a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(3/2),x, algorithm="giac")

[Out] $-3*b*\arctan(\sqrt{b*x + a}/\sqrt{-a})/(\sqrt{-a}*a^2) - (3*(b*x + a)*b - 2*a*b)/(((b*x + a)^{(3/2)} - \sqrt{b*x + a})*a^2)$

maple [A] time = 0.01, size = 55, normalized size = 0.96

$$2 \left(-\frac{1}{\sqrt{bx+a} a^2} - \frac{-\frac{3 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{2\sqrt{a}} + \frac{\sqrt{bx+a}}{2bx}}{a^2} \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^(3/2),x)

[Out] $2*b*(-1/a^2/(b*x+a)^{(1/2)}-1/a^2*(1/2*(b*x+a)^{(1/2)}/b/x-3/2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)))/a^{(1/2))})$

maxima [A] time = 3.01, size = 76, normalized size = 1.33

$$-\frac{3(bx+a)b - 2ab}{(bx+a)^2 a^2 - \sqrt{bx+a} a^3} - \frac{3b \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{2a^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] $-(3*(b*x + a)*b - 2*a*b)/((b*x + a)^{(3/2)}*a^2 - \sqrt{b*x + a}*a^3) - 3/2*b*\log((\sqrt{b*x + a} - \sqrt{a})/(\sqrt{b*x + a} + \sqrt{a}))/a^{(5/2)}$

mupad [B] time = 0.12, size = 60, normalized size = 1.05

$$\frac{3b \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{\frac{2b}{a} - \frac{3b(a+bx)}{a^2}}{a\sqrt{a+bx} - (a+bx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^2*(a + b*x)^(3/2)),x)`

[Out] $(3*b*\operatorname{atanh}((a + b*x)^{1/2}/a^{1/2}))/a^{5/2} - ((2*b)/a - (3*b*(a + b*x))/a^2)/(a*(a + b*x)^{1/2} - (a + b*x)^{3/2})$

sympy [A] time = 3.41, size = 73, normalized size = 1.28

$$-\frac{1}{a\sqrt{b}x^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}} - \frac{3\sqrt{b}}{a^2\sqrt{x}\sqrt{\frac{a}{bx}+1}} + \frac{3b\operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{a^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(b*x+a)**(3/2),x)`

[Out] $-1/(a*\sqrt{b}*x^{3/2}*\sqrt{a/(b*x) + 1}) - 3*\sqrt{b}/(a**2*\sqrt{x}*\sqrt{a/(b*x) + 1}) + 3*b*\operatorname{asinh}(\sqrt{a}/(\sqrt{b}*\sqrt{x}))/a^{5/2}$

$$3.350 \quad \int \frac{1}{x^3(a+bx)^{3/2}} dx$$

Optimal. Leaf size=87

$$-\frac{15b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{7/2}} + \frac{15b^2}{4a^3\sqrt{a+bx}} + \frac{5b}{4a^2x\sqrt{a+bx}} - \frac{1}{2ax^2\sqrt{a+bx}}$$

[Out] $-15/4*b^2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(7/2)}+15/4*b^2/a^3/(b*x+a)^{(1/2)}$
 $-1/2/a/x^2/(b*x+a)^{(1/2)}+5/4*b/a^2/x/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 85, normalized size of antiderivative = 0.98,
 number of steps used = 5, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} =$
 0.231, Rules used = {51, 63, 208}

$$-\frac{15b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{7/2}} - \frac{5\sqrt{a+bx}}{2a^2x^2} + \frac{15b\sqrt{a+bx}}{4a^3x} + \frac{2}{ax^2\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(a + b*x)^(3/2)),x]

[Out] $2/(a*x^2*\operatorname{Sqrt}[a + b*x]) - (5*\operatorname{Sqrt}[a + b*x])/(2*a^2*x^2) + (15*b*\operatorname{Sqrt}[a + b*x])/(4*a^3*x) - (15*b^2*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/(4*a^{(7/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
 ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
 m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
 [n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
 ntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
 {p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
 (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
 [b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
 ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^3(a+bx)^{3/2}} dx &= \frac{2}{ax^2\sqrt{a+bx}} + \frac{5 \int \frac{1}{x^3\sqrt{a+bx}} dx}{a} \\
 &= \frac{2}{ax^2\sqrt{a+bx}} - \frac{5\sqrt{a+bx}}{2a^2x^2} - \frac{(15b) \int \frac{1}{x^2\sqrt{a+bx}} dx}{4a^2} \\
 &= \frac{2}{ax^2\sqrt{a+bx}} - \frac{5\sqrt{a+bx}}{2a^2x^2} + \frac{15b\sqrt{a+bx}}{4a^3x} + \frac{(15b^2) \int \frac{1}{x\sqrt{a+bx}} dx}{8a^3} \\
 &= \frac{2}{ax^2\sqrt{a+bx}} - \frac{5\sqrt{a+bx}}{2a^2x^2} + \frac{15b\sqrt{a+bx}}{4a^3x} + \frac{(15b) \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{4a^3} \\
 &= \frac{2}{ax^2\sqrt{a+bx}} - \frac{5\sqrt{a+bx}}{2a^2x^2} + \frac{15b\sqrt{a+bx}}{4a^3x} - \frac{15b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.38

$$\frac{2b^2 {}_2F_1\left(-\frac{1}{2}, 3; \frac{1}{2}; \frac{bx}{a} + 1\right)}{a^3\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)^(3/2)), x]

[Out] (2*b^2*Hypergeometric2F1[-1/2, 3, 1/2, 1 + (b*x)/a])/(a^3*Sqrt[a + b*x])

fricas [A] time = 0.47, size = 189, normalized size = 2.17

$$\left[\frac{15(b^3x^3 + ab^2x^2)\sqrt{a} \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(15ab^2x^2 + 5a^2bx - 2a^3)\sqrt{bx+a} - 15(b^3x^3 + ab^2x^2)\sqrt{-a}}{8(a^4bx^3 + a^5x^2)}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] [1/8*(15*(b^3*x^3 + a*b^2*x^2)*sqrt(a)*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*(15*a*b^2*x^2 + 5*a^2*b*x - 2*a^3)*sqrt(b*x + a))/(a^4*b*x^3 + a^5*x^2), 1/4*(15*(b^3*x^3 + a*b^2*x^2)*sqrt(-a)*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (15*a*b^2*x^2 + 5*a^2*b*x - 2*a^3)*sqrt(b*x + a))/(a^4*b*x^3 + a^5*x^2)]

giac [A] time = 1.05, size = 80, normalized size = 0.92

$$\frac{15b^2 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{4\sqrt{-a}a^3} + \frac{2b^2}{\sqrt{bx+a}a^3} + \frac{7(bx+a)^{\frac{3}{2}}b^2 - 9\sqrt{bx+a}ab^2}{4a^3b^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(3/2),x, algorithm="giac")

[Out] 15/4*b^2*arctan(sqrt(b*x + a)/sqrt(-a))/(sqrt(-a)*a^3) + 2*b^2/(sqrt(b*x + a)*a^3) + 1/4*(7*(b*x + a)^(3/2)*b^2 - 9*sqrt(b*x + a)*a*b^2)/(a^3*b^2*x^2)

maple [A] time = 0.01, size = 67, normalized size = 0.77

$$2 \left(\frac{1}{\sqrt{bx+a}a^3} + \frac{\frac{15 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{8\sqrt{a}} + \frac{-\frac{9\sqrt{bx+a}a}{8} + \frac{7(bx+a)^{\frac{3}{2}}}{8}}{b^2x^2}}{a^3} \right) b^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a)^(3/2),x)

[Out] 2*b^2*(1/a^3/(b*x+a)^(1/2)+1/a^3*((7/8*(b*x+a)^(3/2)-9/8*(b*x+a)^(1/2)*a)/x^2/b^2-15/8*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(1/2)))

maxima [A] time = 3.06, size = 108, normalized size = 1.24

$$\frac{15(bx+a)^2b^2 - 25(bx+a)ab^2 + 8a^2b^2}{4\left((bx+a)^{\frac{5}{2}}a^3 - 2(bx+a)^{\frac{3}{2}}a^4 + \sqrt{bx+a}a^5\right)} + \frac{15b^2 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{8a^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] $\frac{1}{4} \cdot (15 \cdot (b \cdot x + a)^2 \cdot b^2 - 25 \cdot (b \cdot x + a) \cdot a \cdot b^2 + 8 \cdot a^2 \cdot b^2) / ((b \cdot x + a)^{(5/2)} \cdot a^3 - 2 \cdot (b \cdot x + a)^{(3/2)} \cdot a^4 + \sqrt{b \cdot x + a} \cdot a^5) + \frac{15}{8} \cdot b^2 \cdot \log((\sqrt{b \cdot x + a} - \sqrt{a}) / (\sqrt{b \cdot x + a} + \sqrt{a})) / a^{(7/2)}$

mupad [B] time = 0.06, size = 90, normalized size = 1.03

$$\frac{\frac{2b^2}{a} + \frac{15b^2(a+bx)^2}{4a^3} - \frac{25b^2(a+bx)}{4a^2}}{(a+bx)^{5/2} - 2a(a+bx)^{3/2} + a^2\sqrt{a+bx}} - \frac{15b^2 \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^3*(a + b*x)^(3/2)),x)`

[Out] $((2 \cdot b^2) / a + (15 \cdot b^2 \cdot (a + b \cdot x)^2) / (4 \cdot a^3) - (25 \cdot b^2 \cdot (a + b \cdot x)) / (4 \cdot a^2)) / ((a + b \cdot x)^{(5/2)} - 2 \cdot a \cdot (a + b \cdot x)^{(3/2)} + a^2 \cdot (a + b \cdot x)^{(1/2)}) - (15 \cdot b^2 \cdot \operatorname{atanh}(a + b \cdot x)^{(1/2)} / a^{(1/2)}) / (4 \cdot a^{(7/2)})$

sympy [A] time = 5.98, size = 107, normalized size = 1.23

$$-\frac{1}{2a\sqrt{b}x^{\frac{5}{2}}\sqrt{\frac{a}{bx}+1}} + \frac{5\sqrt{b}}{4a^2x^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}} + \frac{15b^{\frac{3}{2}}}{4a^3\sqrt{x}\sqrt{\frac{a}{bx}+1}} - \frac{15b^2 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4a^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**3/(b*x+a)**(3/2),x)`

[Out] $-1 / (2 \cdot a \cdot \sqrt{b} \cdot x^{(5/2)} \cdot \sqrt{a / (b \cdot x) + 1}) + 5 \cdot \sqrt{b} / (4 \cdot a^{(2)} \cdot x^{(3/2)} \cdot \sqrt{a / (b \cdot x) + 1}) + 15 \cdot b^{(3/2)} / (4 \cdot a^{(3)} \cdot \sqrt{x} \cdot \sqrt{a / (b \cdot x) + 1}) - 15 \cdot b^{(2)} \cdot \operatorname{asinh}(\sqrt{a} / (\sqrt{b} \cdot \sqrt{x})) / (4 \cdot a^{(7/2)})$

$$3.351 \quad \int \frac{x^4}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=87

$$-\frac{2a^4}{3b^5(a+bx)^{3/2}} + \frac{8a^3}{b^5\sqrt{a+bx}} + \frac{12a^2\sqrt{a+bx}}{b^5} - \frac{8a(a+bx)^{3/2}}{3b^5} + \frac{2(a+bx)^{5/2}}{5b^5}$$

[Out] $-2/3*a^4/b^5/(b*x+a)^{(3/2)}-8/3*a*(b*x+a)^{(3/2)}/b^5+2/5*(b*x+a)^{(5/2)}/b^5+8*a^3/b^5/(b*x+a)^{(1/2)}+12*a^2*(b*x+a)^{(1/2)}/b^5$

Rubi [A] time = 0.02, antiderivative size = 87, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{2a^4}{3b^5(a+bx)^{3/2}} + \frac{8a^3}{b^5\sqrt{a+bx}} + \frac{12a^2\sqrt{a+bx}}{b^5} - \frac{8a(a+bx)^{3/2}}{3b^5} + \frac{2(a+bx)^{5/2}}{5b^5}$$

Antiderivative was successfully verified.

[In] Int[x^4/(a + b*x)^(5/2), x]

[Out] $(-2*a^4)/(3*b^5*(a + b*x)^{(3/2)}) + (8*a^3)/(b^5*\text{Sqrt}[a + b*x]) + (12*a^2*\text{Sqrt}[a + b*x])/b^5 - (8*a*(a + b*x)^{(3/2)})/(3*b^5) + (2*(a + b*x)^{(5/2)})/(5*b^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{(a+bx)^{5/2}} dx &= \int \left(\frac{a^4}{b^4(a+bx)^{5/2}} - \frac{4a^3}{b^4(a+bx)^{3/2}} + \frac{6a^2}{b^4\sqrt{a+bx}} - \frac{4a\sqrt{a+bx}}{b^4} + \frac{(a+bx)^{3/2}}{b^4} \right) dx \\ &= -\frac{2a^4}{3b^5(a+bx)^{3/2}} + \frac{8a^3}{b^5\sqrt{a+bx}} + \frac{12a^2\sqrt{a+bx}}{b^5} - \frac{8a(a+bx)^{3/2}}{3b^5} + \frac{2(a+bx)^{5/2}}{5b^5} \end{aligned}$$

Mathematica [A] time = 0.03, size = 57, normalized size = 0.66

$$\frac{2(128a^4 + 192a^3bx + 48a^2b^2x^2 - 8ab^3x^3 + 3b^4x^4)}{15b^5(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/(a + b*x)^(5/2), x]

[Out] $(2*(128*a^4 + 192*a^3*b*x + 48*a^2*b^2*x^2 - 8*a*b^3*x^3 + 3*b^4*x^4))/(15*b^5*(a + b*x)^(3/2))$

fricas [A] time = 0.44, size = 74, normalized size = 0.85

$$\frac{2(3b^4x^4 - 8ab^3x^3 + 48a^2b^2x^2 + 192a^3bx + 128a^4)\sqrt{bx+a}}{15(b^7x^2 + 2ab^6x + a^2b^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] $2/15*(3*b^4*x^4 - 8*a*b^3*x^3 + 48*a^2*b^2*x^2 + 192*a^3*b*x + 128*a^4)*\text{sqrt}(b*x + a)/(b^7*x^2 + 2*a*b^6*x + a^2*b^5)$

giac [A] time = 1.08, size = 75, normalized size = 0.86

$$\frac{2(12(bx+a)a^3 - a^4)}{3(bx+a)^3b^5} + \frac{2(3(bx+a)^{\frac{5}{2}}b^{20} - 20(bx+a)^{\frac{3}{2}}ab^{20} + 90\sqrt{bx+a}a^2b^{20})}{15b^{25}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^(5/2), x, algorithm="giac")

[Out] $2/3*(12*(b*x + a)*a^3 - a^4)/((b*x + a)^(3/2)*b^5) + 2/15*(3*(b*x + a)^(5/2)*b^{20} - 20*(b*x + a)^(3/2)*a*b^{20} + 90*\text{sqrt}(b*x + a)*a^2*b^{20})/b^{25}$

maple [A] time = 0.00, size = 54, normalized size = 0.62

$$\frac{\frac{2}{5}x^4b^4 - \frac{16}{15}ax^3b^3 + \frac{32}{5}a^2x^2b^2 + \frac{128}{5}a^3xb + \frac{256}{15}a^4}{(bx+a)^{\frac{3}{2}}b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(b*x+a)^(5/2), x)

[Out] $2/15/(b*x+a)^(3/2)*(3*b^4*x^4-8*a*b^3*x^3+48*a^2*b^2*x^2+192*a^3*b*x+128*a^4)/b^5$

maxima [A] time = 1.35, size = 71, normalized size = 0.82

$$\frac{2(bx+a)^{\frac{5}{2}}}{5b^5} - \frac{8(bx+a)^{\frac{3}{2}}a}{3b^5} + \frac{12\sqrt{bx+a}a^2}{b^5} + \frac{8a^3}{\sqrt{bx+a}b^5} - \frac{2a^4}{3(bx+a)^{\frac{3}{2}}b^5}$$

$$\begin{aligned}
& *6*x + 675*a**38*b**7*x**2 + 1800*a**37*b**8*x**3 + 3150*a**36*b**9*x**4 + \\
& 3780*a**35*b**10*x**5 + 3150*a**34*b**11*x**6 + 1800*a**33*b**12*x**7 + 675 \\
& *a**32*b**13*x**8 + 150*a**31*b**14*x**9 + 15*a**30*b**15*x**10) + 25840*a* \\
& *(79/2)*b**3*x**3*sqrt(1 + b*x/a)/(15*a**40*b**5 + 150*a**39*b**6*x + 675*a \\
& **38*b**7*x**2 + 1800*a**37*b**8*x**3 + 3150*a**36*b**9*x**4 + 3780*a**35*b \\
& **10*x**5 + 3150*a**34*b**11*x**6 + 1800*a**33*b**12*x**7 + 675*a**32*b**13 \\
& *x**8 + 150*a**31*b**14*x**9 + 15*a**30*b**15*x**10) - 30720*a***(79/2)*b**3 \\
& *x**3/(15*a**40*b**5 + 150*a**39*b**6*x + 675*a**38*b**7*x**2 + 1800*a**37* \\
& b**8*x**3 + 3150*a**36*b**9*x**4 + 3780*a**35*b**10*x**5 + 3150*a**34*b**11 \\
& *x**6 + 1800*a**33*b**12*x**7 + 675*a**32*b**13*x**8 + 150*a**31*b**14*x**9 \\
& + 15*a**30*b**15*x**10) + 41990*a***(77/2)*b**4*x**4*sqrt(1 + b*x/a)/(15*a* \\
& **40*b**5 + 150*a**39*b**6*x + 675*a**38*b**7*x**2 + 1800*a**37*b**8*x**3 + \\
& 3150*a**36*b**9*x**4 + 3780*a**35*b**10*x**5 + 3150*a**34*b**11*x**6 + 1800 \\
& *a**33*b**12*x**7 + 675*a**32*b**13*x**8 + 150*a**31*b**14*x**9 + 15*a**30* \\
& b**15*x**10) - 53760*a***(77/2)*b**4*x**4/(15*a**40*b**5 + 150*a**39*b**6*x \\
& + 675*a**38*b**7*x**2 + 1800*a**37*b**8*x**3 + 3150*a**36*b**9*x**4 + 3780* \\
& a**35*b**10*x**5 + 3150*a**34*b**11*x**6 + 1800*a**33*b**12*x**7 + 675*a**3 \\
& 2*b**13*x**8 + 150*a**31*b**14*x**9 + 15*a**30*b**15*x**10) + 46192*a***(75/ \\
& 2)*b**5*x**5*sqrt(1 + b*x/a)/(15*a**40*b**5 + 150*a**39*b**6*x + 675*a**38* \\
& b**7*x**2 + 1800*a**37*b**8*x**3 + 3150*a**36*b**9*x**4 + 3780*a**35*b**10* \\
& x**5 + 3150*a**34*b**11*x**6 + 1800*a**33*b**12*x**7 + 675*a**32*b**13*x**8 \\
& + 150*a**31*b**14*x**9 + 15*a**30*b**15*x**10) - 64512*a***(75/2)*b**5*x**5 \\
& /(15*a**40*b**5 + 150*a**39*b**6*x + 675*a**38*b**7*x**2 + 1800*a**37*b**8* \\
& x**3 + 3150*a**36*b**9*x**4 + 3780*a**35*b**10*x**5 + 3150*a**34*b**11*x**6 \\
& + 1800*a**33*b**12*x**7 + 675*a**32*b**13*x**8 + 150*a**31*b**14*x**9 + 15 \\
& *a**30*b**15*x**10) + 34664*a***(73/2)*b**6*x**6*sqrt(1 + b*x/a)/(15*a**40*b \\
& **5 + 150*a**39*b**6*x + 675*a**38*b**7*x**2 + 1800*a**37*b**8*x**3 + 3150* \\
& a**36*b**9*x**4 + 3780*a**35*b**10*x**5 + 3150*a**34*b**11*x**6 + 1800*a**3 \\
& 3*b**12*x**7 + 675*a**32*b**13*x**8 + 150*a**31*b**14*x**9 + 15*a**30*b**15 \\
& *x**10) - 53760*a***(73/2)*b**6*x**6/(15*a**40*b**5 + 150*a**39*b**6*x + 675 \\
& *a**38*b**7*x**2 + 1800*a**37*b**8*x**3 + 3150*a**36*b**9*x**4 + 3780*a**35 \\
& *b**10*x**5 + 3150*a**34*b**11*x**6 + 1800*a**33*b**12*x**7 + 675*a**32*b** \\
& 13*x**8 + 150*a**31*b**14*x**9 + 15*a**30*b**15*x**10) + 17392*a***(71/2)*b* \\
& *7*x**7*sqrt(1 + b*x/a)/(15*a**40*b**5 + 150*a**39*b**6*x + 675*a**38*b**7* \\
& x**2 + 1800*a**37*b**8*x**3 + 3150*a**36*b**9*x**4 + 3780*a**35*b**10*x**5 \\
& + 3150*a**34*b**11*x**6 + 1800*a**33*b**12*x**7 + 675*a**32*b**13*x**8 + 15 \\
& 0*a**31*b**14*x**9 + 15*a**30*b**15*x**10) - 30720*a***(71/2)*b**7*x**7/(15* \\
& a**40*b**5 + 150*a**39*b**6*x + 675*a**38*b**7*x**2 + 1800*a**37*b**8*x**3 \\
& + 3150*a**36*b**9*x**4 + 3780*a**35*b**10*x**5 + 3150*a**34*b**11*x**6 + 18 \\
& 00*a**33*b**12*x**7 + 675*a**32*b**13*x**8 + 150*a**31*b**14*x**9 + 15*a**3 \\
& 0*b**15*x**10) + 5540*a***(69/2)*b**8*x**8*sqrt(1 + b*x/a)/(15*a**40*b**5 + \\
& 150*a**39*b**6*x + 675*a**38*b**7*x**2 + 1800*a**37*b**8*x**3 + 3150*a**36* \\
& b**9*x**4 + 3780*a**35*b**10*x**5 + 3150*a**34*b**11*x**6 + 1800*a**33*b**1 \\
& 2*x**7 + 675*a**32*b**13*x**8 + 150*a**31*b**14*x**9 + 15*a**30*b**15*x**10 \\
&) - 11520*a***(69/2)*b**8*x**8/(15*a**40*b**5 + 150*a**39*b**6*x + 675*a**38
\end{aligned}$$

$$\begin{aligned}
& *b^{**7}x^{**2} + 1800*a^{**37}*b^{**8}x^{**3} + 3150*a^{**36}*b^{**9}x^{**4} + 3780*a^{**35}*b^{**10} \\
& *x^{**5} + 3150*a^{**34}*b^{**11}x^{**6} + 1800*a^{**33}*b^{**12}x^{**7} + 675*a^{**32}*b^{**13}x^{**8} \\
& + 150*a^{**31}*b^{**14}x^{**9} + 15*a^{**30}*b^{**15}x^{**10}) + 1040*a^{**}(67/2)*b^{**9}x^{**9} \\
& *sqrt(1 + b*x/a)/(15*a^{**40}*b^{**5} + 150*a^{**39}*b^{**6}x + 675*a^{**38}*b^{**7}x^{**2} + \\
& 1800*a^{**37}*b^{**8}x^{**3} + 3150*a^{**36}*b^{**9}x^{**4} + 3780*a^{**35}*b^{**10}x^{**5} + 3150* \\
& a^{**34}*b^{**11}x^{**6} + 1800*a^{**33}*b^{**12}x^{**7} + 675*a^{**32}*b^{**13}x^{**8} + 150*a^{**31} \\
& *b^{**14}x^{**9} + 15*a^{**30}*b^{**15}x^{**10}) - 2560*a^{**}(67/2)*b^{**9}x^{**9}/(15*a^{**40}*b^{** \\
& *5 + 150*a^{**39}*b^{**6}x + 675*a^{**38}*b^{**7}x^{**2} + 1800*a^{**37}*b^{**8}x^{**3} + 3150*a \\
& **36*b^{**9}x^{**4} + 3780*a^{**35}*b^{**10}x^{**5} + 3150*a^{**34}*b^{**11}x^{**6} + 1800*a^{**33} \\
& *b^{**12}x^{**7} + 675*a^{**32}*b^{**13}x^{**8} + 150*a^{**31}*b^{**14}x^{**9} + 15*a^{**30}*b^{**15}x^{**10} \\
& + 136*a^{**}(65/2)*b^{**10}x^{**10}*sqrt(1 + b*x/a)/(15*a^{**40}*b^{**5} + 150*a^{**39}*b^{**6}x + 675*a^{**38}*b^{**7}x^{**2} \\
& + 1800*a^{**37}*b^{**8}x^{**3} + 3150*a^{**36}*b^{**9}x^{**4} + 3780*a^{**35}*b^{**10}x^{**5} + 3150*a^{**34}*b^{**11}x^{**6} \\
& + 1800*a^{**33}*b^{**12}x^{**7} + 675*a^{**32}*b^{**13}x^{**8} + 150*a^{**31}*b^{**14}x^{**9} + 15*a^{**30}*b^{**15}x^{**10}) - 256 \\
& *a^{**}(65/2)*b^{**10}x^{**10}/(15*a^{**40}*b^{**5} + 150*a^{**39}*b^{**6}x + 675*a^{**38}*b^{**7}x^{**2} \\
& + 1800*a^{**37}*b^{**8}x^{**3} + 3150*a^{**36}*b^{**9}x^{**4} + 3780*a^{**35}*b^{**10}x^{**5} + 3150*a^{**34}*b^{**11}x^{**6} \\
& + 1800*a^{**33}*b^{**12}x^{**7} + 675*a^{**32}*b^{**13}x^{**8} + 150*a^{**31}*b^{**14}x^{**9} + 15*a^{**30}*b^{**15}x^{**10}) + 32*a^{**}(63/2)*b^{**11}x^{**11}*sqrt(1 \\
& + b*x/a)/(15*a^{**40}*b^{**5} + 150*a^{**39}*b^{**6}x + 675*a^{**38}*b^{**7}x^{**2} + 1800*a^{**37}*b^{**8}x^{**3} \\
& + 3150*a^{**36}*b^{**9}x^{**4} + 3780*a^{**35}*b^{**10}x^{**5} + 3150*a^{**34}*b^{**11}x^{**6} + 1800*a^{**33}*b^{**12}x^{**7} \\
& + 675*a^{**32}*b^{**13}x^{**8} + 150*a^{**31}*b^{**14}x^{**9} + 15*a^{**30}*b^{**15}x^{**10}) + 6*a^{**}(61/2)*b^{**12}x^{**12}*sqrt(1 + b*x/a)/(15* \\
& a^{**40}*b^{**5} + 150*a^{**39}*b^{**6}x + 675*a^{**38}*b^{**7}x^{**2} + 1800*a^{**37}*b^{**8}x^{**3} \\
& + 3150*a^{**36}*b^{**9}x^{**4} + 3780*a^{**35}*b^{**10}x^{**5} + 3150*a^{**34}*b^{**11}x^{**6} + 18 \\
& 00*a^{**33}*b^{**12}x^{**7} + 675*a^{**32}*b^{**13}x^{**8} + 150*a^{**31}*b^{**14}x^{**9} + 15*a^{**30} \\
& *b^{**15}x^{**10})
\end{aligned}$$

$$3.352 \quad \int \frac{x^3}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=68

$$\frac{2a^3}{3b^4(a+bx)^{3/2}} - \frac{6a^2}{b^4\sqrt{a+bx}} - \frac{6a\sqrt{a+bx}}{b^4} + \frac{2(a+bx)^{3/2}}{3b^4}$$

[Out] $2/3*a^3/b^4/(b*x+a)^{(3/2)}+2/3*(b*x+a)^{(3/2)}/b^4-6*a^2/b^4/(b*x+a)^{(1/2)}-6*a*(b*x+a)^{(1/2)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2a^3}{3b^4(a+bx)^{3/2}} - \frac{6a^2}{b^4\sqrt{a+bx}} - \frac{6a\sqrt{a+bx}}{b^4} + \frac{2(a+bx)^{3/2}}{3b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x)^(5/2), x]

[Out] $(2*a^3)/(3*b^4*(a + b*x)^{(3/2)}) - (6*a^2)/(b^4*sqrt[a + b*x]) - (6*a*sqrt[a + b*x])/b^4 + (2*(a + b*x)^{(3/2)})/(3*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(a+bx)^{5/2}} dx &= \int \left(-\frac{a^3}{b^3(a+bx)^{5/2}} + \frac{3a^2}{b^3(a+bx)^{3/2}} - \frac{3a}{b^3\sqrt{a+bx}} + \frac{\sqrt{a+bx}}{b^3} \right) dx \\ &= \frac{2a^3}{3b^4(a+bx)^{3/2}} - \frac{6a^2}{b^4\sqrt{a+bx}} - \frac{6a\sqrt{a+bx}}{b^4} + \frac{2(a+bx)^{3/2}}{3b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 0.66

$$\frac{2(-16a^3 - 24a^2bx - 6ab^2x^2 + b^3x^3)}{3b^4(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x)^(5/2), x]

[Out] (2*(-16*a^3 - 24*a^2*b*x - 6*a*b^2*x^2 + b^3*x^3))/(3*b^4*(a + b*x)^(3/2))

fricas [A] time = 0.47, size = 62, normalized size = 0.91

$$\frac{2(b^3x^3 - 6ab^2x^2 - 24a^2bx - 16a^3)\sqrt{bx+a}}{3(b^6x^2 + 2ab^5x + a^2b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] 2/3*(b^3*x^3 - 6*a*b^2*x^2 - 24*a^2*b*x - 16*a^3)*sqrt(b*x + a)/(b^6*x^2 + 2*a*b^5*x + a^2*b^4)

giac [A] time = 1.03, size = 59, normalized size = 0.87

$$-\frac{2(9(bx+a)a^2 - a^3)}{3(bx+a)^{\frac{3}{2}}b^4} + \frac{2((bx+a)^{\frac{3}{2}}b^8 - 9\sqrt{bx+a}ab^8)}{3b^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(5/2), x, algorithm="giac")

[Out] -2/3*(9*(b*x + a)*a^2 - a^3)/((b*x + a)^(3/2)*b^4) + 2/3*((b*x + a)^(3/2)*b^8 - 9*sqrt(b*x + a)*a*b^8)/b^12

maple [A] time = 0.01, size = 43, normalized size = 0.63

$$\frac{2(-b^3x^3 + 6ab^2x^2 + 24a^2bx + 16a^3)}{3(bx+a)^{\frac{3}{2}}b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^(5/2), x)

[Out] -2/3/(b*x+a)^(3/2)*(-b^3*x^3+6*a*b^2*x^2+24*a^2*b*x+16*a^3)/b^4

maxima [A] time = 1.25, size = 56, normalized size = 0.82

$$\frac{2(bx+a)^{\frac{3}{2}}}{3b^4} - \frac{6\sqrt{bx+a}a}{b^4} - \frac{6a^2}{\sqrt{bx+a}b^4} + \frac{2a^3}{3(bx+a)^{\frac{3}{2}}b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] $\frac{2}{3}*(b*x + a)^{(3/2)}/b^4 - 6*\sqrt{b*x + a}*a/b^4 - 6*a^2/(\sqrt{b*x + a})*b^4 + 2/3*a^3/((b*x + a)^{(3/2)}*b^4)$

mupad [B] time = 0.04, size = 47, normalized size = 0.69

$$\frac{18 a (a + b x)^2 + 18 a^2 (a + b x) - 2 (a + b x)^3 - 2 a^3}{3 b^4 (a + b x)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(a + b*x)^(5/2),x)

[Out] $-(18*a*(a + b*x)^2 + 18*a^2*(a + b*x) - 2*(a + b*x)^3 - 2*a^3)/(3*b^4*(a + b*x)^{(3/2)})$

sympy [A] time = 1.20, size = 163, normalized size = 2.40

$$\begin{cases} \frac{32a^3}{3ab^4\sqrt{a+bx}+3b^5x\sqrt{a+bx}} - \frac{48a^2bx}{3ab^4\sqrt{a+bx}+3b^5x\sqrt{a+bx}} - \frac{12ab^2x^2}{3ab^4\sqrt{a+bx}+3b^5x\sqrt{a+bx}} + \frac{2b^3x^3}{3ab^4\sqrt{a+bx}+3b^5x\sqrt{a+bx}} & \text{for } b \neq 0 \\ \frac{x^4}{4a^2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(b*x+a)**(5/2),x)

[Out] Piecewise((-32*a**3/(3*a*b**4*sqrt(a + b*x) + 3*b**5*x*sqrt(a + b*x)) - 48*a**2*b*x/(3*a*b**4*sqrt(a + b*x) + 3*b**5*x*sqrt(a + b*x)) - 12*a*b**2*x**2/(3*a*b**4*sqrt(a + b*x) + 3*b**5*x*sqrt(a + b*x)) + 2*b**3*x**3/(3*a*b**4*sqrt(a + b*x) + 3*b**5*x*sqrt(a + b*x)), Ne(b, 0)), (x**4/(4*a**(5/2)), True))

$$3.353 \quad \int \frac{x^2}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=49

$$-\frac{2a^2}{3b^3(a+bx)^{3/2}} + \frac{4a}{b^3\sqrt{a+bx}} + \frac{2\sqrt{a+bx}}{b^3}$$

[Out] $-2/3*a^2/b^3/(b*x+a)^{(3/2)}+4*a/b^3/(b*x+a)^{(1/2)}+2*(b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{2a^2}{3b^3(a+bx)^{3/2}} + \frac{4a}{b^3\sqrt{a+bx}} + \frac{2\sqrt{a+bx}}{b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*x)^(5/2), x]

[Out] $(-2*a^2)/(3*b^3*(a + b*x)^{(3/2)}) + (4*a)/(b^3*sqrt[a + b*x]) + (2*sqrt[a + b*x])/b^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(a+bx)^{5/2}} dx &= \int \left(\frac{a^2}{b^2(a+bx)^{5/2}} - \frac{2a}{b^2(a+bx)^{3/2}} + \frac{1}{b^2\sqrt{a+bx}} \right) dx \\ &= -\frac{2a^2}{3b^3(a+bx)^{3/2}} + \frac{4a}{b^3\sqrt{a+bx}} + \frac{2\sqrt{a+bx}}{b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.71

$$\frac{2(8a^2 + 12abx + 3b^2x^2)}{3b^3(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x)^(5/2),x]

[Out] (2*(8*a^2 + 12*a*b*x + 3*b^2*x^2))/(3*b^3*(a + b*x)^(3/2))

fricas [A] time = 0.44, size = 52, normalized size = 1.06

$$\frac{2(3b^2x^2 + 12abx + 8a^2)\sqrt{bx + a}}{3(b^5x^2 + 2ab^4x + a^2b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(5/2),x, algorithm="fricas")

[Out] 2/3*(3*b^2*x^2 + 12*a*b*x + 8*a^2)*sqrt(b*x + a)/(b^5*x^2 + 2*a*b^4*x + a^2*b^3)

giac [A] time = 0.94, size = 39, normalized size = 0.80

$$\frac{2\sqrt{bx + a}}{b^3} + \frac{2(6(bx + a)a - a^2)}{3(bx + a)^{\frac{3}{2}}b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(5/2),x, algorithm="giac")

[Out] 2*sqrt(b*x + a)/b^3 + 2/3*(6*(b*x + a)*a - a^2)/((b*x + a)^(3/2)*b^3)

maple [A] time = 0.00, size = 32, normalized size = 0.65

$$\frac{2b^2x^2 + 8abx + \frac{16}{3}a^2}{b^3(bx + a)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^(5/2),x)

[Out] 2/3/(b*x+a)^(3/2)*(3*b^2*x^2+12*a*b*x+8*a^2)/b^3

maxima [A] time = 1.33, size = 41, normalized size = 0.84

$$\frac{2\sqrt{bx + a}}{b^3} + \frac{4a}{\sqrt{bx + a}b^3} - \frac{2a^2}{3(bx + a)^{\frac{3}{2}}b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] 2*sqrt(b*x + a)/b^3 + 4*a/(sqrt(b*x + a)*b^3) - 2/3*a^2/((b*x + a)^(3/2)*b^3)

mupad [B] time = 0.08, size = 35, normalized size = 0.71

$$\frac{6(a+bx)^2 + 12a(a+bx) - 2a^2}{3b^3(a+bx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(a + b*x)^(5/2),x)

[Out] (6*(a + b*x)^2 + 12*a*(a + b*x) - 2*a^2)/(3*b^3*(a + b*x)^(3/2))

sympy [A] time = 1.28, size = 121, normalized size = 2.47

$$\begin{cases} \frac{16a^2}{3ab^3\sqrt{a+bx}+3b^4x\sqrt{a+bx}} + \frac{24abx}{3ab^3\sqrt{a+bx}+3b^4x\sqrt{a+bx}} + \frac{6b^2x^2}{3ab^3\sqrt{a+bx}+3b^4x\sqrt{a+bx}} & \text{for } b \neq 0 \\ \frac{x^3}{3a^{\frac{5}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(b*x+a)**(5/2),x)

[Out] Piecewise((16*a**2/(3*a*b**3*sqrt(a + b*x) + 3*b**4*x*sqrt(a + b*x)) + 24*a*b*x/(3*a*b**3*sqrt(a + b*x) + 3*b**4*x*sqrt(a + b*x)) + 6*b**2*x**2/(3*a*b**3*sqrt(a + b*x) + 3*b**4*x*sqrt(a + b*x)), Ne(b, 0)), (x**3/(3*a**(5/2)), True))

$$3.354 \quad \int \frac{x}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=32

$$\frac{2a}{3b^2(a+bx)^{3/2}} - \frac{2}{b^2\sqrt{a+bx}}$$

[Out] $2/3*a/b^2/(b*x+a)^{(3/2)}-2/b^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{2a}{3b^2(a+bx)^{3/2}} - \frac{2}{b^2\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x)^(5/2), x]

[Out] $(2*a)/(3*b^2*(a + b*x)^{(3/2)}) - 2/(b^2*\text{Sqrt}[a + b*x])$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x}{(a+bx)^{5/2}} dx &= \int \left(-\frac{a}{b(a+bx)^{5/2}} + \frac{1}{b(a+bx)^{3/2}} \right) dx \\ &= \frac{2a}{3b^2(a+bx)^{3/2}} - \frac{2}{b^2\sqrt{a+bx}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.75

$$\frac{2(2a + 3bx)}{3b^2(a + bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x)^(5/2), x]

[Out] $(-2*(2*a + 3*b*x))/(3*b^2*(a + b*x)^(3/2))$

fricas [A] time = 0.44, size = 41, normalized size = 1.28

$$-\frac{2(3bx + 2a)\sqrt{bx + a}}{3(b^4x^2 + 2ab^3x + a^2b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(5/2),x, algorithm="fricas")`

[Out] $-2/3*(3*b*x + 2*a)*\text{sqrt}(b*x + a)/(b^4*x^2 + 2*a*b^3*x + a^2*b^2)$

giac [A] time = 1.06, size = 20, normalized size = 0.62

$$-\frac{2(3bx + 2a)}{3(bx + a)^{\frac{3}{2}}b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(5/2),x, algorithm="giac")`

[Out] $-2/3*(3*b*x + 2*a)/((b*x + a)^(3/2)*b^2)$

maple [A] time = 0.00, size = 21, normalized size = 0.66

$$-\frac{2(3bx + 2a)}{3(bx + a)^{\frac{3}{2}}b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(b*x+a)^(5/2),x)`

[Out] $-2/3/(b*x+a)^(3/2)*(3*b*x+2*a)/b^2$

maxima [A] time = 1.34, size = 26, normalized size = 0.81

$$-\frac{2}{\sqrt{bx + a}b^2} + \frac{2a}{3(bx + a)^{\frac{3}{2}}b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(5/2),x, algorithm="maxima")`

[Out] $-2/(\text{sqrt}(b*x + a)*b^2) + 2/3*a/((b*x + a)^(3/2)*b^2)$

mupad [B] time = 0.03, size = 20, normalized size = 0.62

$$-\frac{4a + 6bx}{3b^2(a + bx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a + b*x)^(5/2), x)`

[Out] `-(4*a + 6*b*x)/(3*b^2*(a + b*x)^(3/2))`

sympy [A] time = 1.13, size = 80, normalized size = 2.50

$$\begin{cases} -\frac{4a}{3ab^2\sqrt{a+bx}+3b^3x\sqrt{a+bx}} - \frac{6bx}{3ab^2\sqrt{a+bx}+3b^3x\sqrt{a+bx}} & \text{for } b \neq 0 \\ \frac{x^2}{2a^2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)**(5/2), x)`

[Out] `Piecewise((-4*a/(3*a*b**2*sqrt(a + b*x) + 3*b**3*x*sqrt(a + b*x)) - 6*b*x/(3*a*b**2*sqrt(a + b*x) + 3*b**3*x*sqrt(a + b*x)), Ne(b, 0)), (x**2/(2*a**(5/2)), True))`

$$3.355 \quad \int \frac{1}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=16

$$-\frac{2}{3b(a+bx)^{3/2}}$$

[Out] -2/3/b/(b*x+a)^(3/2)

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$-\frac{2}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-5/2), x]

[Out] -2/(3*b*(a + b*x)^(3/2))

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^{5/2}} dx = -\frac{2}{3b(a+bx)^{3/2}}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$-\frac{2}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-5/2), x]

[Out] -2/(3*b*(a + b*x)^(3/2))

fricas [B] time = 0.48, size = 31, normalized size = 1.94

$$-\frac{2\sqrt{bx+a}}{3(b^3x^2+2ab^2x+a^2b)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2),x, algorithm="fricas")

[Out] -2/3*sqrt(b*x + a)/(b^3*x^2 + 2*a*b^2*x + a^2*b)

giac [A] time = 1.04, size = 12, normalized size = 0.75

$$-\frac{2}{3(bx+a)^{\frac{3}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2),x, algorithm="giac")

[Out] -2/3/((b*x + a)^(3/2)*b)

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$-\frac{2}{3(bx+a)^{\frac{3}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2),x)

[Out] -2/3/b/(b*x+a)^(3/2)

maxima [A] time = 1.31, size = 12, normalized size = 0.75

$$-\frac{2}{3(bx+a)^{\frac{3}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] -2/3/((b*x + a)^(3/2)*b)

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$-\frac{2}{3b(a+bx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x)^(5/2),x)

[Out] $-2/(3*b*(a + b*x)^{(3/2)})$

sympy [A] time = 0.07, size = 14, normalized size = 0.88

$$-\frac{2}{3b(a+bx)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/2),x)`

[Out] $-2/(3*b*(a + b*x)**(3/2))$

$$3.356 \quad \int \frac{1}{x(a+bx)^{5/2}} dx$$

Optimal. Leaf size=54

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{5/2}} + \frac{2}{a^2\sqrt{a+bx}} + \frac{2}{3a(a+bx)^{3/2}}$$

[Out] $2/3/a/(b*x+a)^{(3/2)}-2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(5/2)}+2/a^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 208}

$$\frac{2}{a^2\sqrt{a+bx}} - \frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{5/2}} + \frac{2}{3a(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a + b*x)^(5/2)),x]

[Out] $2/(3*a*(a + b*x)^{(3/2)}) + 2/(a^2*\operatorname{Sqrt}[a + b*x]) - (2*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/a^{(5/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x(a+bx)^{5/2}} dx &= \frac{2}{3a(a+bx)^{3/2}} + \frac{\int \frac{1}{x(a+bx)^{3/2}} dx}{a} \\
 &= \frac{2}{3a(a+bx)^{3/2}} + \frac{2}{a^2\sqrt{a+bx}} + \frac{\int \frac{1}{x\sqrt{a+bx}} dx}{a^2} \\
 &= \frac{2}{3a(a+bx)^{3/2}} + \frac{2}{a^2\sqrt{a+bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{a^2b} \\
 &= \frac{2}{3a(a+bx)^{3/2}} + \frac{2}{a^2\sqrt{a+bx}} - \frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 32, normalized size = 0.59

$$\frac{{}_2F_1\left(-\frac{3}{2}, 1; -\frac{1}{2}; \frac{bx}{a} + 1\right)}{3a(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)^(5/2)), x]

[Out] (2*Hypergeometric2F1[-3/2, 1, -1/2, 1 + (b*x)/a])/(3*a*(a + b*x)^(3/2))

fricas [B] time = 0.49, size = 177, normalized size = 3.28

$$\left[\frac{3(b^2x^2 + 2abx + a^2)\sqrt{a} \log\left(\frac{bx - 2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(3abx + 4a^2)\sqrt{bx+a}}{3(a^3b^2x^2 + 2a^4bx + a^5)}, \frac{2\left(3(b^2x^2 + 2abx + a^2)\sqrt{-a} \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)\right)}{3(a^3b^2x^2 + 2a^4bx + a^5)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] [1/3*(3*(b^2*x^2 + 2*a*b*x + a^2)*sqrt(a)*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*(3*a*b*x + 4*a^2)*sqrt(b*x + a))/(a^3*b^2*x^2 + 2*a^4*b*x +

a^5), $2/3*(3*(b^2*x^2 + 2*a*b*x + a^2)*\sqrt{-a}*\arctan(\sqrt{b*x + a}*\sqrt{-a})/a) + (3*a*b*x + 4*a^2)*\sqrt{b*x + a})/(a^3*b^2*x^2 + 2*a^4*b*x + a^5)]$

giac [A] time = 1.00, size = 45, normalized size = 0.83

$$\frac{2 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a} a^2} + \frac{2(3bx + 4a)}{3(bx + a)^{\frac{3}{2}} a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(5/2),x, algorithm="giac")

[Out] $2*\arctan(\sqrt{b*x + a}/\sqrt{-a})/(\sqrt{-a}*a^2) + 2/3*(3*b*x + 4*a)/((b*x + a)^(3/2)*a^2)$

maple [A] time = 0.01, size = 43, normalized size = 0.80

$$\frac{2}{3(bx + a)^{\frac{3}{2}} a} - \frac{2 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{a^{\frac{5}{2}}} + \frac{2}{\sqrt{bx + a} a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a)^(5/2),x)

[Out] $2/3/a/(b*x+a)^(3/2)-2*\operatorname{arctanh}((b*x+a)^(1/2)/a^(1/2))/a^(5/2)+2/(b*x+a)^(1/2)/a^2$

maxima [A] time = 2.91, size = 53, normalized size = 0.98

$$\frac{\log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{a^{\frac{5}{2}}} + \frac{2(3bx + 4a)}{3(bx + a)^{\frac{3}{2}} a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] $\log((\sqrt{b*x + a} - \sqrt{a})/(\sqrt{b*x + a} + \sqrt{a}))/a^(5/2) + 2/3*(3*b*x + 4*a)/((b*x + a)^(3/2)*a^2)$

mupad [B] time = 0.05, size = 42, normalized size = 0.78

$$\frac{\frac{2(a+bx)}{a^2} + \frac{2}{3a}}{(a+bx)^{3/2}} - \frac{2 \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(a + b*x)^(5/2)),x)`

[Out] $((2*(a + b*x))/a^2 + 2/(3*a))/(a + b*x)^{(3/2)} - (2*\operatorname{atanh}((a + b*x)^{(1/2)}/a^{(1/2)}))/a^{(5/2)}$

sympy [B] time = 2.99, size = 697, normalized size = 12.91

$$\frac{8a^7 \sqrt{1 + \frac{bx}{a}}}{3a^{\frac{19}{2}} + 9a^{\frac{17}{2}}bx + 9a^{\frac{15}{2}}b^2x^2 + 3a^{\frac{13}{2}}b^3x^3} + \frac{3a^7 \log\left(\frac{bx}{a}\right)}{3a^{\frac{19}{2}} + 9a^{\frac{17}{2}}bx + 9a^{\frac{15}{2}}b^2x^2 + 3a^{\frac{13}{2}}b^3x^3} - \frac{6a^7 \log\left(\sqrt{1 + \frac{bx}{a}} + 1\right)}{3a^{\frac{19}{2}} + 9a^{\frac{17}{2}}bx + 9a^{\frac{15}{2}}b^2x^2 + 3a^{\frac{13}{2}}b^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b*x+a)**(5/2),x)`

[Out] $8*a^{**7}*\sqrt{1 + b*x/a}/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3}) + 3*a^{**7}*\log(b*x/a)/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3}) - 6*a^{**7}*\log(\sqrt{1 + b*x/a} + 1)/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3}) + 14*a^{**6}*b*x*\sqrt{1 + b*x/a}/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3}) + 9*a^{**6}*b*x*\log(b*x/a)/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3}) - 18*a^{**6}*b*x*\log(\sqrt{1 + b*x/a} + 1)/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3}) + 6*a^{**5}*b^{**2}*x^{**2}*\sqrt{1 + b*x/a}/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3}) + 9*a^{**5}*b^{**2}*x^{**2}*\log(b*x/a)/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3}) - 18*a^{**5}*b^{**2}*x^{**2}*\log(\sqrt{1 + b*x/a} + 1)/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3}) + 3*a^{**4}*b^{**3}*x^{**3}*\log(b*x/a)/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3}) - 6*a^{**4}*b^{**3}*x^{**3}*\log(\sqrt{1 + b*x/a} + 1)/(3*a^{**}(19/2) + 9*a^{**}(17/2)*b*x + 9*a^{**}(15/2)*b^{**2}*x^{**2} + 3*a^{**}(13/2)*b^{**3}*x^{**3})$

$$3.357 \quad \int \frac{1}{x^2(a+bx)^{5/2}} dx$$

Optimal. Leaf size=74

$$\frac{5b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{7/2}} - \frac{5b}{a^3\sqrt{a+bx}} - \frac{5b}{3a^2(a+bx)^{3/2}} - \frac{1}{ax(a+bx)^{3/2}}$$

[Out] $-5/3*b/a^2/(b*x+a)^{(3/2)}-1/a/x/(b*x+a)^{(3/2)}+5*b*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(7/2)}-5*b/a^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.08, number of steps used = 5, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 208}

$$-\frac{5\sqrt{a+bx}}{a^3x} + \frac{10}{3a^2x\sqrt{a+bx}} + \frac{5b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{7/2}} + \frac{2}{3ax(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(a + b*x)^(5/2)), x]

[Out] $2/(3*a*x*(a + b*x)^{(3/2)}) + 10/(3*a^2*x*\operatorname{Sqrt}[a + b*x]) - (5*\operatorname{Sqrt}[a + b*x])/ (a^3*x) + (5*b*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/a^{(7/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^2(a+bx)^{5/2}} dx &= \frac{2}{3ax(a+bx)^{3/2}} + \frac{5 \int \frac{1}{x^2(a+bx)^{3/2}} dx}{3a} \\
 &= \frac{2}{3ax(a+bx)^{3/2}} + \frac{10}{3a^2x\sqrt{a+bx}} + \frac{5 \int \frac{1}{x^2\sqrt{a+bx}} dx}{a^2} \\
 &= \frac{2}{3ax(a+bx)^{3/2}} + \frac{10}{3a^2x\sqrt{a+bx}} - \frac{5\sqrt{a+bx}}{a^3x} - \frac{(5b) \int \frac{1}{x\sqrt{a+bx}} dx}{2a^3} \\
 &= \frac{2}{3ax(a+bx)^{3/2}} + \frac{10}{3a^2x\sqrt{a+bx}} - \frac{5\sqrt{a+bx}}{a^3x} - \frac{5 \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{a^3} \\
 &= \frac{2}{3ax(a+bx)^{3/2}} + \frac{10}{3a^2x\sqrt{a+bx}} - \frac{5\sqrt{a+bx}}{a^3x} + \frac{5b \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.45

$$-\frac{2b {}_2F_1\left(-\frac{3}{2}, 2; -\frac{1}{2}; \frac{bx}{a} + 1\right)}{3a^2(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)^(5/2)), x]

[Out] (-2*b*Hypergeometric2F1[-3/2, 2, -1/2, 1 + (b*x)/a])/(3*a^2*(a + b*x)^(3/2))

fricas [A] time = 0.49, size = 221, normalized size = 2.99

$$\left[\frac{15(b^3x^3 + 2ab^2x^2 + a^2bx)\sqrt{a} \log\left(\frac{bx+2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) - 2(15ab^2x^2 + 20a^2bx + 3a^3)\sqrt{bx+a}}{6(a^4b^2x^3 + 2a^5bx^2 + a^6x)}, -\frac{15(b^3x^3 + 2ab^2x^2 + a^2bx)\sqrt{a}}{6(a^4b^2x^3 + 2a^5bx^2 + a^6x)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(5/2),x, algorithm="fricas")

[Out] [1/6*(15*(b^3*x^3 + 2*a*b^2*x^2 + a^2*b*x)*sqrt(a)*log((b*x + 2*sqrt(b*x + a))*sqrt(a) + 2*a)/x) - 2*(15*a*b^2*x^2 + 20*a^2*b*x + 3*a^3)*sqrt(b*x + a))/(a^4*b^2*x^3 + 2*a^5*b*x^2 + a^6*x), -1/3*(15*(b^3*x^3 + 2*a*b^2*x^2 + a^2*b*x)*sqrt(-a)*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (15*a*b^2*x^2 + 20*a^2*b*x + 3*a^3)*sqrt(b*x + a))/(a^4*b^2*x^3 + 2*a^5*b*x^2 + a^6*x)]

giac [A] time = 1.03, size = 65, normalized size = 0.88

$$-\frac{5b \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a} a^3} - \frac{2(6(bx+a)b + ab)}{3(bx+a)^{\frac{3}{2}} a^3} - \frac{\sqrt{bx+a}}{a^3 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(5/2),x, algorithm="giac")

[Out] -5*b*arctan(sqrt(b*x + a)/sqrt(-a))/(sqrt(-a)*a^3) - 2/3*(6*(b*x + a)*b + a*b)/((b*x + a)^(3/2)*a^3) - sqrt(b*x + a)/(a^3*x)

maple [A] time = 0.01, size = 67, normalized size = 0.91

$$2 \left(-\frac{1}{3(bx+a)^{\frac{3}{2}} a^2} - \frac{2}{\sqrt{bx+a} a^3} - \frac{5 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{2\sqrt{a} a^3} + \frac{\sqrt{bx+a}}{2bx} \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^(5/2),x)

[Out] 2*b*(-1/3/a^2/(b*x+a)^(3/2)-2/(b*x+a)^(1/2)/a^3-1/a^3*(1/2*(b*x+a)^(1/2)/b/x-5/2*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(1/2)))

maxima [A] time = 3.03, size = 89, normalized size = 1.20

$$-\frac{15(bx+a)^2 b - 10(bx+a)ab - 2a^2 b}{3\left((bx+a)^{\frac{5}{2}} a^3 - (bx+a)^{\frac{3}{2}} a^4\right)} - \frac{5b \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{2a^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] $-1/3*(15*(b*x + a)^2*b - 10*(b*x + a)*a*b - 2*a^2*b)/((b*x + a)^{(5/2)}*a^3 - (b*x + a)^{(3/2)}*a^4) - 5/2*b*\log((\sqrt{b*x + a}) - \sqrt{a})/(\sqrt{b*x + a} + \sqrt{a})/a^{(7/2)}$

mupad [B] time = 0.11, size = 73, normalized size = 0.99

$$\frac{5 b \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{a^{7/2}} - \frac{\frac{2b}{3a} + \frac{10b(a+bx)}{3a^2} - \frac{5b(a+bx)^2}{a^3}}{a(a+bx)^{3/2} - (a+bx)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{int}(1/(x^2*(a + b*x)^{(5/2})), x)$

[Out] $(5*b*\operatorname{atanh}((a + b*x)^{(1/2)}/a^{(1/2)}))/a^{(7/2)} - ((2*b)/(3*a) + (10*b*(a + b*x))/(3*a^2) - (5*b*(a + b*x)^2)/a^3)/(a*(a + b*x)^{(3/2)} - (a + b*x)^{(5/2)})$

sympy [B] time = 5.60, size = 818, normalized size = 11.05

$$\frac{6a^{17}\sqrt{1+\frac{bx}{a}}}{6a^{\frac{39}{2}}x + 18a^{\frac{37}{2}}bx^2 + 18a^{\frac{35}{2}}b^2x^3 + 6a^{\frac{33}{2}}b^3x^4} - \frac{46a^{16}bx\sqrt{1+\frac{bx}{a}}}{6a^{\frac{39}{2}}x + 18a^{\frac{37}{2}}bx^2 + 18a^{\frac{35}{2}}b^2x^3 + 6a^{\frac{33}{2}}b^3x^4} - \frac{15a^{16}bx}{6a^{\frac{39}{2}}x + 18a^{\frac{37}{2}}bx^2 + 18a^{\frac{35}{2}}b^2x^3 + 6a^{\frac{33}{2}}b^3x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{integrate}(1/x^{**2}/(b*x+a)^{(5/2}), x)$

[Out] $-6*a^{**17}*\sqrt{1 + b*x/a}/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) - 46*a^{**16}*b*x*\sqrt{1 + b*x/a}/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) - 15*a^{**16}*b*x*\log(b*x/a)/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) + 30*a^{**16}*b*x*\log(\sqrt{1 + b*x/a} + 1)/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) - 70*a^{**15}*b^{**2}*x^{**2}*\sqrt{1 + b*x/a}/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) - 45*a^{**15}*b^{**2}*x^{**2}*\log(b*x/a)/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) + 90*a^{**15}*b^{**2}*x^{**2}*\log(\sqrt{1 + b*x/a} + 1)/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) - 30*a^{**14}*b^{**3}*x^{**3}*\sqrt{1 + b*x/a}/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) - 45*a^{**14}*b^{**3}*x^{**3}*\log(b*x/a)/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) + 90*a^{**14}*b^{**3}*x^{**3}*\log(\sqrt{1 + b*x/a} + 1)/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) - 15*a^{**13}*b^{**4}*x^{**4}*\log(b*x/a)/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4}) + 30*a^{**13}*b^{**4}*x^{**4}*\log(\sqrt{1 + b*x/a} + 1)/(6*a^{**}(39/2)*x + 18*a^{**}(37/2)*b*x^{**2} + 18*a^{**}(35/2)*b^{**2}*x^{**3} + 6*a^{**}(33/2)*b^{**3}*x^{**4})$

$$3.358 \quad \int \frac{1}{x^3(a+bx)^{5/2}} dx$$

Optimal. Leaf size=106

$$-\frac{35b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{9/2}} + \frac{35b^2}{4a^4\sqrt{a+bx}} + \frac{35b^2}{12a^3(a+bx)^{3/2}} + \frac{7b}{4a^2x(a+bx)^{3/2}} - \frac{1}{2ax^2(a+bx)^{3/2}}$$

[Out] 35/12*b^2/a^3/(b*x+a)^(3/2)-1/2/a/x^2/(b*x+a)^(3/2)+7/4*b/a^2/x/(b*x+a)^(3/2)-35/4*b^2*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(9/2)+35/4*b^2/a^4/(b*x+a)^(1/2)

Rubi [A] time = 0.03, antiderivative size = 106, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 208}

$$-\frac{35b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{9/2}} - \frac{35\sqrt{a+bx}}{6a^3x^2} + \frac{14}{3a^2x^2\sqrt{a+bx}} + \frac{35b\sqrt{a+bx}}{4a^4x} + \frac{2}{3ax^2(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(a + b*x)^(5/2)),x]

[Out] 2/(3*a*x^2*(a + b*x)^(3/2)) + 14/(3*a^2*x^2*Sqrt[a + b*x]) - (35*Sqrt[a + b*x])/(6*a^3*x^2) + (35*b*Sqrt[a + b*x])/(4*a^4*x) - (35*b^2*ArcTanh[Sqrt[a + b*x]/Sqrt[a]])/(4*a^(9/2))

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^3(a+bx)^{5/2}} dx &= \frac{2}{3ax^2(a+bx)^{3/2}} + \frac{7 \int \frac{1}{x^3(a+bx)^{3/2}} dx}{3a} \\
 &= \frac{2}{3ax^2(a+bx)^{3/2}} + \frac{14}{3a^2x^2\sqrt{a+bx}} + \frac{35 \int \frac{1}{x^3\sqrt{a+bx}} dx}{3a^2} \\
 &= \frac{2}{3ax^2(a+bx)^{3/2}} + \frac{14}{3a^2x^2\sqrt{a+bx}} - \frac{35\sqrt{a+bx}}{6a^3x^2} - \frac{(35b) \int \frac{1}{x^2\sqrt{a+bx}} dx}{4a^3} \\
 &= \frac{2}{3ax^2(a+bx)^{3/2}} + \frac{14}{3a^2x^2\sqrt{a+bx}} - \frac{35\sqrt{a+bx}}{6a^3x^2} + \frac{35b\sqrt{a+bx}}{4a^4x} + \frac{(35b^2) \int \frac{1}{x\sqrt{a+bx}} dx}{8a^4} \\
 &= \frac{2}{3ax^2(a+bx)^{3/2}} + \frac{14}{3a^2x^2\sqrt{a+bx}} - \frac{35\sqrt{a+bx}}{6a^3x^2} + \frac{35b\sqrt{a+bx}}{4a^4x} + \frac{(35b) \operatorname{Subst}\left(\int \frac{1}{-\frac{a}{b} + \frac{x^2}{b}} dx\right)}{4a^4} \\
 &= \frac{2}{3ax^2(a+bx)^{3/2}} + \frac{14}{3a^2x^2\sqrt{a+bx}} - \frac{35\sqrt{a+bx}}{6a^3x^2} + \frac{35b\sqrt{a+bx}}{4a^4x} - \frac{35b^2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{9/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.33

$$\frac{2b^2 {}_2F_1\left(-\frac{3}{2}, 3; -\frac{1}{2}; \frac{bx}{a} + 1\right)}{3a^3(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)^(5/2)), x]

[Out] (2*b^2*Hypergeometric2F1[-3/2, 3, -1/2, 1 + (b*x)/a])/(3*a^3*(a + b*x)^(3/2))

fricas [A] time = 0.48, size = 255, normalized size = 2.41

$$\left[\frac{105(b^4x^4 + 2ab^3x^3 + a^2b^2x^2)\sqrt{a} \log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right) + 2(105ab^3x^3 + 140a^2b^2x^2 + 21a^3bx - 6a^4)\sqrt{bx+a}}{24(a^5b^2x^4 + 2a^6bx^3 + a^7x^2)} \right],$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(5/2),x, algorithm="fricas")

[Out] [1/24*(105*(b^4*x^4 + 2*a*b^3*x^3 + a^2*b^2*x^2)*sqrt(a)*log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x) + 2*(105*a*b^3*x^3 + 140*a^2*b^2*x^2 + 21*a^3*b*x - 6*a^4)*sqrt(b*x + a))/(a^5*b^2*x^4 + 2*a^6*b*x^3 + a^7*x^2), 1/12*(105*(b^4*x^4 + 2*a*b^3*x^3 + a^2*b^2*x^2)*sqrt(-a)*arctan(sqrt(b*x + a)*sqrt(-a)/a) + (105*a*b^3*x^3 + 140*a^2*b^2*x^2 + 21*a^3*b*x - 6*a^4)*sqrt(b*x + a))/(a^5*b^2*x^4 + 2*a^6*b*x^3 + a^7*x^2)]

giac [A] time = 0.99, size = 93, normalized size = 0.88

$$\frac{35b^2 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{4\sqrt{-a}a^4} + \frac{2(9(bx+a)b^2 + ab^2)}{3(bx+a)^{\frac{3}{2}}a^4} + \frac{11(bx+a)^{\frac{3}{2}}b^2 - 13\sqrt{bx+a}ab^2}{4a^4b^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(5/2),x, algorithm="giac")

[Out] 35/4*b^2*arctan(sqrt(b*x + a)/sqrt(-a))/(sqrt(-a)*a^4) + 2/3*(9*(b*x + a)*b^2 + a*b^2)/((b*x + a)^(3/2)*a^4) + 1/4*(11*(b*x + a)^(3/2)*b^2 - 13*sqrt(b*x + a)*a*b^2)/(a^4*b^2*x^2)

maple [A] time = 0.02, size = 80, normalized size = 0.75

$$2 \left(\frac{1}{3(bx+a)^{\frac{3}{2}}a^3} + \frac{3}{\sqrt{bx+a}a^4} + \frac{-\frac{35 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{8\sqrt{a}} + \frac{-13\sqrt{bx+a}a + 11(bx+a)^{\frac{3}{2}}}{8}}{a^4} \right) b^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a)^(5/2),x)

[Out] 2*b^2*(3/a^4/(b*x+a)^(1/2)+1/3/a^3/(b*x+a)^(3/2)+1/a^4*((11/8*(b*x+a)^(3/2)-13/8*(b*x+a)^(1/2)*a)/x^2/b^2-35/8*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(1/2))

maxima [A] time = 3.00, size = 123, normalized size = 1.16

$$\frac{105(bx+a)^3b^2 - 175(bx+a)^2ab^2 + 56(bx+a)a^2b^2 + 8a^3b^2}{12\left((bx+a)^{\frac{7}{2}}a^4 - 2(bx+a)^{\frac{5}{2}}a^5 + (bx+a)^{\frac{3}{2}}a^6\right)} + \frac{35b^2 \log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{8a^{\frac{9}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] $\frac{1}{12} \cdot (105 \cdot (b \cdot x + a)^3 \cdot b^2 - 175 \cdot (b \cdot x + a)^2 \cdot a \cdot b^2 + 56 \cdot (b \cdot x + a) \cdot a^2 \cdot b^2 + 8 \cdot a^3 \cdot b^2) / ((b \cdot x + a)^{7/2} \cdot a^4 - 2 \cdot (b \cdot x + a)^{5/2} \cdot a^5 + (b \cdot x + a)^{3/2} \cdot a^6) + 35/8 \cdot b^2 \cdot \log((\sqrt{b \cdot x + a} - \sqrt{a}) / (\sqrt{b \cdot x + a} + \sqrt{a})) / a^{9/2}$

mpad [B] time = 0.12, size = 105, normalized size = 0.99

$$\frac{\frac{2b^2}{3a} - \frac{175b^2(a+bx)^2}{12a^3} + \frac{35b^2(a+bx)^3}{4a^4} + \frac{14b^2(a+bx)}{3a^2}}{(a+bx)^{7/2} - 2a(a+bx)^{5/2} + a^2(a+bx)^{3/2}} - \frac{35b^2 \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{4a^{9/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(a + b*x)^(5/2)),x)

[Out] $((2 \cdot b^2) / (3 \cdot a) - (175 \cdot b^2 \cdot (a + b \cdot x)^2) / (12 \cdot a^3) + (35 \cdot b^2 \cdot (a + b \cdot x)^3) / (4 \cdot a^4) + (14 \cdot b^2 \cdot (a + b \cdot x)) / (3 \cdot a^2)) / ((a + b \cdot x)^{7/2} - 2 \cdot a \cdot (a + b \cdot x)^{5/2} + a^2 \cdot (a + b \cdot x)^{3/2}) - (35 \cdot b^2 \cdot \operatorname{atanh}((a + b \cdot x)^{1/2} / a^{1/2})) / (4 \cdot a^{9/2})$

sympy [B] time = 8.57, size = 464, normalized size = 4.38

$$-\frac{6a^{\frac{89}{2}}b^{75}x^{75}}{12a^{\frac{93}{2}}b^{\frac{151}{2}}x^{\frac{155}{2}}\sqrt{\frac{a}{bx}+1}} + \frac{21a^{\frac{87}{2}}b^{76}x^{76}}{12a^{\frac{93}{2}}b^{\frac{151}{2}}x^{\frac{155}{2}}\sqrt{\frac{a}{bx}+1}} + \frac{12a^{\frac{91}{2}}b^{\frac{153}{2}}x^{\frac{157}{2}}\sqrt{\frac{a}{bx}+1}}{12a^{\frac{93}{2}}b^{\frac{151}{2}}x^{\frac{155}{2}}\sqrt{\frac{a}{bx}+1}} + \frac{12a^{\frac{91}{2}}b^{\frac{153}{2}}x^{\frac{157}{2}}\sqrt{\frac{a}{bx}+1}}{12a^{\frac{93}{2}}b^{\frac{151}{2}}x^{\frac{155}{2}}\sqrt{\frac{a}{bx}+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(b*x+a)**(5/2),x)

[Out] $-6 \cdot a^{89/2} \cdot b^{75} \cdot x^{75} / (12 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2} \cdot \sqrt{a/(b \cdot x) + 1}) + 12 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \sqrt{a/(b \cdot x) + 1}) + 21 \cdot a^{87/2} \cdot b^{76} \cdot x^{76} / (12 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2} \cdot \sqrt{a/(b \cdot x) + 1}) + 12 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \sqrt{a/(b \cdot x) + 1}) + 140 \cdot a^{85/2} \cdot b^{77} \cdot x^{77} / (12 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2} \cdot \sqrt{a/(b \cdot x) + 1}) + 12 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \sqrt{a/(b \cdot x) + 1}) + 105 \cdot a^{83/2} \cdot b^{78} \cdot x^{78} / (12 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2} \cdot \sqrt{a/(b \cdot x) + 1}) + 12 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \sqrt{a/(b \cdot x) + 1}) - 105 \cdot a^{41} \cdot b^{157/2} \cdot x^{157/2} \cdot \sqrt{a/(b \cdot x) + 1} \cdot \operatorname{asinh}(\sqrt{a}/(\sqrt{b} \cdot \sqrt{x})) / (12 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2} \cdot \sqrt{a/(b \cdot x) + 1}) + 12 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \sqrt{a/(b \cdot x) + 1}) - 105 \cdot a^{41} \cdot b^{157/2} \cdot x^{157/2} \cdot \sqrt{a/(b \cdot x) + 1} \cdot \operatorname{asinh}(\sqrt{a}/(\sqrt{b} \cdot \sqrt{x})) / (12 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2} \cdot \sqrt{a/(b \cdot x) + 1}) + 12 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \sqrt{a/(b \cdot x) + 1})$

$$3.359 \quad \int \frac{1}{x\sqrt{-a+bx}} dx$$

Optimal. Leaf size=25

$$\frac{2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}}$$

[Out] 2*arctan((b*x-a)^(1/2)/a^(1/2))/a^(1/2)

Rubi [A] time = 0.01, antiderivative size = 25, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {63, 205}

$$\frac{2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*Sqrt[-a + b*x]),x]

[Out] (2*ArcTan[Sqrt[-a + b*x]/Sqrt[a]])/Sqrt[a]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\int \frac{1}{x\sqrt{-a+bx}} dx = \frac{2 \operatorname{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx}\right)}{b}$$

$$= \frac{2 \tan^{-1}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 1.00

$$\frac{2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*Sqrt[-a + b*x]),x]

[Out] (2*ArcTan[Sqrt[-a + b*x]/Sqrt[a]])/Sqrt[a]

fricas [A] time = 0.45, size = 58, normalized size = 2.32

$$\left[\frac{\sqrt{-a} \log\left(\frac{bx-2\sqrt{bx-a}\sqrt{-a}-2a}{x}\right)}{a}, \frac{2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(1/2),x, algorithm="fricas")

[Out] [-sqrt(-a)*log((b*x - 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x)/a, 2*arctan(sqrt(b*x - a)/sqrt(a))/sqrt(a)]

giac [A] time = 0.99, size = 19, normalized size = 0.76

$$\frac{2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(1/2),x, algorithm="giac")

[Out] $2 \arctan(\sqrt{bx-a}/\sqrt{a})/\sqrt{a}$

maple [A] time = 0.00, size = 20, normalized size = 0.80

$$\frac{2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/x/(b*x-a)^{(1/2)}, x)$

[Out] $2 \arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(1/2)}$

maxima [A] time = 2.99, size = 19, normalized size = 0.76

$$\frac{2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x/(b*x-a)^{(1/2)}, x, \text{algorithm}="maxima")$

[Out] $2 \arctan(\sqrt{bx-a}/\sqrt{a})/\sqrt{a}$

mupad [B] time = 0.05, size = 19, normalized size = 0.76

$$\frac{2 \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(x*(b*x-a)^{(1/2)}), x)$

[Out] $(2 \operatorname{atan}((b*x-a)^{(1/2)}/a^{(1/2)}))/a^{(1/2)}$

sympy [A] time = 1.23, size = 54, normalized size = 2.16

$$\begin{cases} \frac{2i \operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{a}} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ -\frac{2 \operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{a}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x/(b*x-a)**(1/2),x)
```

```
[Out] Piecewise((2*I*acosh(sqrt(a)/(sqrt(b)*sqrt(x)))/sqrt(a), Abs(a/(b*x)) > 1),  
(-2*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/sqrt(a), True))
```

$$3.360 \quad \int \frac{1}{x^2 \sqrt{-a+bx}} dx$$

Optimal. Leaf size=44

$$\frac{b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{3/2}} + \frac{\sqrt{bx-a}}{ax}$$

[Out] b*arctan((b*x-a)^(1/2)/a^(1/2))/a^(3/2)+(b*x-a)^(1/2)/a/x

Rubi [A] time = 0.01, antiderivative size = 44, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 205}

$$\frac{b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{3/2}} + \frac{\sqrt{bx-a}}{ax}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*Sqrt[-a + b*x]),x]

[Out] Sqrt[-a + b*x]/(a*x) + (b*ArcTan[Sqrt[-a + b*x]/Sqrt[a]])/a^(3/2)

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^2 \sqrt{-a+bx}} dx &= \frac{\sqrt{-a+bx}}{ax} + \frac{b \int \frac{1}{x \sqrt{-a+bx}} dx}{2a} \\
&= \frac{\sqrt{-a+bx}}{ax} + \frac{\text{Subst} \left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx} \right)}{a} \\
&= \frac{\sqrt{-a+bx}}{ax} + \frac{b \tan^{-1} \left(\frac{\sqrt{-a+bx}}{\sqrt{a}} \right)}{a^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.06, size = 53, normalized size = 1.20

$$\frac{b\sqrt{bx-a} \left(\frac{a}{bx} + \frac{\tanh^{-1} \left(\sqrt{1-\frac{bx}{a}} \right)}{\sqrt{1-\frac{bx}{a}}} \right)}{a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*Sqrt[-a + b*x]),x]

[Out] (b*Sqrt[-a + b*x]*(a/(b*x) + ArcTanh[Sqrt[1 - (b*x)/a]]/Sqrt[1 - (b*x)/a]))/a^2

fricas [A] time = 0.45, size = 97, normalized size = 2.20

$$\left[\frac{\sqrt{-a} bx \log \left(\frac{bx-2\sqrt{bx-a}\sqrt{-a}-2a}{x} \right) - 2\sqrt{bx-a} a}{2a^2x}, \frac{\sqrt{a} bx \arctan \left(\frac{\sqrt{bx-a}}{\sqrt{a}} \right) + \sqrt{bx-a} a}{a^2x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(1/2),x, algorithm="fricas")

[Out] [-1/2*(sqrt(-a)*b*x*log((b*x - 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) - 2*sqrt(b*x - a)*a)/(a^2*x), (sqrt(a)*b*x*arctan(sqrt(b*x - a)/sqrt(a)) + sqrt(b*x - a)*a)/(a^2*x)]

giac [A] time = 0.89, size = 43, normalized size = 0.98

$$\frac{\frac{b^2 \arctan \left(\frac{\sqrt{bx-a}}{\sqrt{a}} \right)}{a^{3/2}} + \frac{\sqrt{bx-a} b}{ax}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(1/2),x, algorithm="giac")

[Out] (b^2*arctan(sqrt(b*x - a)/sqrt(a))/a^(3/2) + sqrt(b*x - a)*b/(a*x))/b

maple [A] time = 0.01, size = 37, normalized size = 0.84

$$\frac{b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{3}{2}}} + \frac{\sqrt{bx-a}}{ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x-a)^(1/2),x)

[Out] b*arctan((b*x-a)^(1/2)/a^(1/2))/a^(3/2)+(b*x-a)^(1/2)/a/x

maxima [A] time = 2.98, size = 46, normalized size = 1.05

$$\frac{\sqrt{bx-a} b}{(bx-a)a + a^2} + \frac{b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(1/2),x, algorithm="maxima")

[Out] sqrt(b*x - a)*b/((b*x - a)*a + a^2) + b*arctan(sqrt(b*x - a)/sqrt(a))/a^(3/2)

mupad [B] time = 0.04, size = 36, normalized size = 0.82

$$\frac{\sqrt{bx-a}}{ax} + \frac{b \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(b*x - a)^(1/2)),x)

[Out] (b*x - a)^(1/2)/(a*x) + (b*atan((b*x - a)^(1/2)/a^(1/2)))/a^(3/2)

sympy [B] time = 2.46, size = 121, normalized size = 2.75

$$\begin{cases} \frac{i\sqrt{b}\sqrt{\frac{a}{bx}-1}}{a\sqrt{x}} + \frac{ib \operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{a^{\frac{3}{2}}} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ -\frac{1}{\sqrt{b}x^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}} + \frac{\sqrt{b}}{a\sqrt{x}\sqrt{-\frac{a}{bx}+1}} - \frac{b \operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{a^{\frac{3}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/(b*x-a)**(1/2),x)

[Out] Piecewise((I*sqrt(b)*sqrt(a/(b*x) - 1)/(a*sqrt(x)) + I*b*acosh(sqrt(a)/(sqrt(b)*sqrt(x)))/a**(3/2), Abs(a/(b*x)) > 1), (-1/(sqrt(b)*x**(3/2)*sqrt(-a/(b*x) + 1)) + sqrt(b)/(a*sqrt(x)*sqrt(-a/(b*x) + 1)) - b*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/a**(3/2), True))

$$3.361 \quad \int \frac{1}{x^3 \sqrt{-a+bx}} dx$$

Optimal. Leaf size=74

$$\frac{3b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{5/2}} + \frac{3b\sqrt{bx-a}}{4a^2x} + \frac{\sqrt{bx-a}}{2ax^2}$$

[Out] $3/4*b^2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(5/2)}+1/2*(b*x-a)^{(1/2)}/a/x^2+3/4*b*(b*x-a)^{(1/2)}/a^2/x$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 205}

$$\frac{3b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{5/2}} + \frac{3b\sqrt{bx-a}}{4a^2x} + \frac{\sqrt{bx-a}}{2ax^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*sqrt[-a + b*x]),x]

[Out] Sqrt[-a + b*x]/(2*a*x^2) + (3*b*Sqrt[-a + b*x])/(4*a^2*x) + (3*b^2*ArcTan[Sqrt[-a + b*x]/Sqrt[a]])/(4*a^(5/2))

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^3 \sqrt{-a+bx}} dx &= \frac{\sqrt{-a+bx}}{2ax^2} + \frac{(3b) \int \frac{1}{x^2 \sqrt{-a+bx}} dx}{4a} \\
 &= \frac{\sqrt{-a+bx}}{2ax^2} + \frac{3b\sqrt{-a+bx}}{4a^2x} + \frac{(3b^2) \int \frac{1}{x\sqrt{-a+bx}} dx}{8a^2} \\
 &= \frac{\sqrt{-a+bx}}{2ax^2} + \frac{3b\sqrt{-a+bx}}{4a^2x} + \frac{(3b) \text{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx}\right)}{4a^2} \\
 &= \frac{\sqrt{-a+bx}}{2ax^2} + \frac{3b\sqrt{-a+bx}}{4a^2x} + \frac{3b^2 \tan^{-1}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)}{4a^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 36, normalized size = 0.49

$$\frac{2b^2\sqrt{bx-a} {}_2F_1\left(\frac{1}{2}, 3; \frac{3}{2}; 1 - \frac{bx}{a}\right)}{a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*Sqrt[-a + b*x]),x]

[Out] (2*b^2*Sqrt[-a + b*x]*Hypergeometric2F1[1/2, 3, 3/2, 1 - (b*x)/a])/a^3

fricas [A] time = 0.46, size = 128, normalized size = 1.73

$$\left[\frac{3\sqrt{-a}b^2x^2 \log\left(\frac{bx-2\sqrt{bx-a}\sqrt{-a-2a}}{x}\right) - 2(3abx+2a^2)\sqrt{bx-a}}{8a^3x^2}, \frac{3\sqrt{a}b^2x^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + (3abx+2a^2)\sqrt{bx-a}}{4a^3x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(1/2),x, algorithm="fricas")

[Out] [-1/8*(3*sqrt(-a)*b^2*x^2*log((b*x - 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) - 2*(3*a*b*x + 2*a^2)*sqrt(b*x - a))/(a^3*x^2), 1/4*(3*sqrt(a)*b^2*x^2*arctan(sqrt(b*x - a)/sqrt(a)) + (3*a*b*x + 2*a^2)*sqrt(b*x - a))/(a^3*x^2)]

giac [A] time = 0.97, size = 68, normalized size = 0.92

$$\frac{\frac{3b^3 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{5}{2}}} + \frac{3(bx-a)^{\frac{3}{2}}b^3 + 5\sqrt{bx-a}ab^3}{a^2b^2x^2}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(1/2),x, algorithm="giac")

[Out] 1/4*(3*b^3*arctan(sqrt(b*x - a)/sqrt(a))/a^(5/2) + (3*(b*x - a)^(3/2)*b^3 + 5*sqrt(b*x - a)*a*b^3)/(a^2*b^2*x^2))/b

maple [A] time = 0.01, size = 59, normalized size = 0.80

$$\frac{3b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{\frac{5}{2}}} + \frac{3\sqrt{bx-a}b}{4a^2x} + \frac{\sqrt{bx-a}}{2ax^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x-a)^(1/2),x)

[Out] 3/4*b^2*arctan((b*x-a)^(1/2)/a^(1/2))/a^(5/2)+1/2*(b*x-a)^(1/2)/a/x^2+3/4*b*(b*x-a)^(1/2)/a^2/x

maxima [A] time = 2.96, size = 86, normalized size = 1.16

$$\frac{3b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{\frac{5}{2}}} + \frac{3(bx-a)^{\frac{3}{2}}b^2 + 5\sqrt{bx-a}ab^2}{4((bx-a)^2a^2 + 2(bx-a)a^3 + a^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(1/2),x, algorithm="maxima")

[Out] 3/4*b^2*arctan(sqrt(b*x - a)/sqrt(a))/a^(5/2) + 1/4*(3*(b*x - a)^(3/2)*b^2 + 5*sqrt(b*x - a)*a*b^2)/((b*x - a)^2*a^2 + 2*(b*x - a)*a^3 + a^4)

mupad [B] time = 0.05, size = 57, normalized size = 0.77

$$\frac{3b^2 \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{5/2}} + \frac{5\sqrt{bx-a}}{4ax^2} + \frac{3(bx-a)^{3/2}}{4a^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^3*(b*x - a)^(1/2)),x)`

[Out] $(3*b^2*\operatorname{atan}((b*x - a)^{1/2}/a^{1/2}))/ (4*a^{5/2}) + (5*(b*x - a)^{1/2})/ (4*a*x^2) + (3*(b*x - a)^{3/2})/ (4*a^2*x^2)$

sympy [A] time = 4.20, size = 216, normalized size = 2.92

$$\left\{ \begin{array}{l} \frac{i}{2\sqrt{b}x^2\sqrt{\frac{a}{bx}-1}} + \frac{i\sqrt{b}}{4ax^2\sqrt{\frac{a}{bx}-1}} - \frac{3ib^{\frac{3}{2}}}{4a^2\sqrt{x}\sqrt{\frac{a}{bx}-1}} + \frac{3ib^2\operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4a^{\frac{5}{2}}} \quad \text{for } \left|\frac{a}{bx}\right| > 1 \\ -\frac{1}{2\sqrt{b}x^2\sqrt{-\frac{a}{bx}+1}} - \frac{\sqrt{b}}{4ax^2\sqrt{-\frac{a}{bx}+1}} + \frac{3b^{\frac{3}{2}}}{4a^2\sqrt{x}\sqrt{-\frac{a}{bx}+1}} - \frac{3b^2\operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4a^{\frac{5}{2}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**3/(b*x-a)**(1/2),x)`

[Out] `Piecewise((I/(2*sqrt(b)*x**(5/2)*sqrt(a/(b*x) - 1)) + I*sqrt(b)/(4*a*x**(3/2)*sqrt(a/(b*x) - 1)) - 3*I*b**(3/2)/(4*a**2*sqrt(x)*sqrt(a/(b*x) - 1)) + 3*I*b**2*acosh(sqrt(a)/(sqrt(b)*sqrt(x)))/(4*a**(5/2)), Abs(a/(b*x)) > 1), (-1/(2*sqrt(b)*x**(5/2)*sqrt(-a/(b*x) + 1)) - sqrt(b)/(4*a*x**(3/2)*sqrt(-a/(b*x) + 1)) + 3*b**(3/2)/(4*a**2*sqrt(x)*sqrt(-a/(b*x) + 1)) - 3*b**2*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/(4*a**(5/2)), True))`

$$3.362 \quad \int \frac{1}{x(-a+bx)^{3/2}} dx$$

Optimal. Leaf size=42

$$-\frac{2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{3/2}} - \frac{2}{a\sqrt{bx-a}}$$

[Out] $-2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(3/2)}-2/a/(b*x-a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 205}

$$-\frac{2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{3/2}} - \frac{2}{a\sqrt{bx-a}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(-a + b*x)^(3/2)),x]

[Out] $-2/(a*\text{Sqrt}[-a + b*x]) - (2*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]])/a^{(3/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
\int \frac{1}{x(-a+bx)^{3/2}} dx &= -\frac{2}{a\sqrt{-a+bx}} - \frac{\int \frac{1}{x\sqrt{-a+bx}} dx}{a} \\
&= -\frac{2}{a\sqrt{-a+bx}} - \frac{2 \operatorname{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx}\right)}{ab} \\
&= -\frac{2}{a\sqrt{-a+bx}} - \frac{2 \tan^{-1}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)}{a^{3/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.79

$$-\frac{{}_2F_1\left(-\frac{1}{2}, 1; \frac{1}{2}; 1 - \frac{bx}{a}\right)}{a\sqrt{bx-a}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(-a + b*x)^(3/2)),x]

[Out] (-2*Hypergeometric2F1[-1/2, 1, 1/2, 1 - (b*x)/a])/(a*Sqrt[-a + b*x])

fricas [A] time = 0.48, size = 124, normalized size = 2.95

$$\left[-\frac{(bx-a)\sqrt{-a} \log\left(\frac{bx+2\sqrt{bx-a}\sqrt{-a}-2a}{x}\right) + 2\sqrt{bx-a}a}{a^2bx-a^3}, -\frac{2\left((bx-a)\sqrt{a} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + \sqrt{bx-a}a\right)}{a^2bx-a^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(3/2),x, algorithm="fricas")

[Out] [-(b*x - a)*sqrt(-a)*log((b*x + 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) + 2*sqrt(b*x - a)*a/(a^2*b*x - a^3), -2*((b*x - a)*sqrt(a)*arctan(sqrt(b*x - a)/sqrt(a)) + sqrt(b*x - a)*a)/(a^2*b*x - a^3)]

giac [A] time = 1.02, size = 34, normalized size = 0.81

$$-\frac{2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{3}{2}}} - \frac{2}{\sqrt{bx-a}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(3/2),x, algorithm="giac")

[Out] $-2*\arctan(\sqrt{b*x - a}/\sqrt{a})/a^{3/2} - 2/(\sqrt{b*x - a}*a)$

maple [A] time = 0.01, size = 35, normalized size = 0.83

$$-\frac{2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{3}{2}}} - \frac{2}{\sqrt{bx-a} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x-a)^(3/2),x)

[Out] $-2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(3/2)}-2/a/(b*x-a)^{(1/2)}$

maxima [A] time = 2.97, size = 34, normalized size = 0.81

$$-\frac{2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{3}{2}}} - \frac{2}{\sqrt{bx-a} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(3/2),x, algorithm="maxima")

[Out] $-2*\arctan(\sqrt{b*x - a}/\sqrt{a})/a^{3/2} - 2/(\sqrt{b*x - a}*a)$

mupad [B] time = 0.10, size = 34, normalized size = 0.81

$$-\frac{2 \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{3/2}} - \frac{2}{a \sqrt{bx-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(b*x - a)^(3/2)),x)

[Out] $-(2*\operatorname{atan}((b*x - a)^{(1/2)}/a^{(1/2)}))/a^{(3/2)} - 2/(a*(b*x - a)^{(1/2)})$

sympy [C] time = 2.20, size = 478, normalized size = 11.38

$$\left\{ \begin{array}{l} \frac{2ia^3\sqrt{-1+\frac{bx}{a}}}{ia^{\frac{9}{2}}-ia^{\frac{7}{2}}bx} - \frac{a^3\log\left(\frac{bx}{a}\right)}{ia^{\frac{9}{2}}-ia^{\frac{7}{2}}bx} + \frac{2a^3\log\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{ia^{\frac{9}{2}}-ia^{\frac{7}{2}}bx} + \frac{2ia^3\operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{ia^{\frac{9}{2}}-ia^{\frac{7}{2}}bx} + \frac{a^2bx\log\left(\frac{bx}{a}\right)}{ia^{\frac{9}{2}}-ia^{\frac{7}{2}}bx} - \frac{2a^2bx\log\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{ia^{\frac{9}{2}}-ia^{\frac{7}{2}}bx} - \frac{2ia^2bx\operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{ia^{\frac{9}{2}}-ia^{\frac{7}{2}}bx} \\ \frac{2a^3\sqrt{1-\frac{bx}{a}}}{-ia^{\frac{9}{2}}+ia^{\frac{7}{2}}bx} + \frac{a^3\log\left(\frac{bx}{a}\right)}{-ia^{\frac{9}{2}}+ia^{\frac{7}{2}}bx} - \frac{2a^3\log\left(\sqrt{1-\frac{bx}{a}}+1\right)}{-ia^{\frac{9}{2}}+ia^{\frac{7}{2}}bx} - \frac{i\pi a^3}{-ia^{\frac{9}{2}}+ia^{\frac{7}{2}}bx} - \frac{a^2bx\log\left(\frac{bx}{a}\right)}{-ia^{\frac{9}{2}}+ia^{\frac{7}{2}}bx} + \frac{2a^2bx\log\left(\sqrt{1-\frac{bx}{a}}+1\right)}{-ia^{\frac{9}{2}}+ia^{\frac{7}{2}}bx} + \frac{i\pi a^2bx}{-ia^{\frac{9}{2}}+ia^{\frac{7}{2}}bx} \end{array} \right.$$

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Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)**(3/2),x)

[Out] Piecewise((2*I*a**3*sqrt(-1 + b*x/a)/(I*a**(9/2) - I*a**(7/2)*b*x) - a**3*log(b*x/a)/(I*a**(9/2) - I*a**(7/2)*b*x) + 2*a**3*log(sqrt(b)*sqrt(x)/sqrt(a))/(I*a**(9/2) - I*a**(7/2)*b*x) + 2*I*a**3*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/(I*a**(9/2) - I*a**(7/2)*b*x) + a**2*b*x*log(b*x/a)/(I*a**(9/2) - I*a**(7/2)*b*x) - 2*a**2*b*x*log(sqrt(b)*sqrt(x)/sqrt(a))/(I*a**(9/2) - I*a**(7/2)*b*x) - 2*I*a**2*b*x*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/(I*a**(9/2) - I*a**(7/2)*b*x), Abs(b*x/a) > 1), (2*a**3*sqrt(1 - b*x/a)/(-I*a**(9/2) + I*a**(7/2)*b*x) + a**3*log(b*x/a)/(-I*a**(9/2) + I*a**(7/2)*b*x) - 2*a**3*log(sqrt(1 - b*x/a) + 1)/(-I*a**(9/2) + I*a**(7/2)*b*x) - I*pi*a**3/(-I*a**(9/2) + I*a**(7/2)*b*x) - a**2*b*x*log(b*x/a)/(-I*a**(9/2) + I*a**(7/2)*b*x) + 2*a**2*b*x*log(sqrt(1 - b*x/a) + 1)/(-I*a**(9/2) + I*a**(7/2)*b*x) + I*pi*a**2*b*x/(-I*a**(9/2) + I*a**(7/2)*b*x), True))

$$3.363 \quad \int \frac{1}{x^2(-a+bx)^{3/2}} dx$$

Optimal. Leaf size=62

$$-\frac{3b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{3b}{a^2\sqrt{bx-a}} + \frac{1}{ax\sqrt{bx-a}}$$

[Out] $-3*b*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(5/2)}-3*b/a^2/(b*x-a)^{(1/2)}+1/a/x/(b*x-a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 65, normalized size of antiderivative = 1.05, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 205}

$$\frac{3\sqrt{bx-a}}{a^2x} - \frac{3b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{2}{ax\sqrt{bx-a}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(-a + b*x)^(3/2)),x]

[Out] $-2/(a*x*\text{Sqrt}[-a + b*x]) - (3*\text{Sqrt}[-a + b*x])/(a^2*x) - (3*b*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]])/a^{(5/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^2(-a+bx)^{3/2}} dx &= -\frac{2}{ax\sqrt{-a+bx}} - \frac{3 \int \frac{1}{x^2\sqrt{-a+bx}} dx}{a} \\
 &= -\frac{2}{ax\sqrt{-a+bx}} - \frac{3\sqrt{-a+bx}}{a^2x} - \frac{(3b) \int \frac{1}{x\sqrt{-a+bx}} dx}{2a^2} \\
 &= -\frac{2}{ax\sqrt{-a+bx}} - \frac{3\sqrt{-a+bx}}{a^2x} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx}\right)}{a^2} \\
 &= -\frac{2}{ax\sqrt{-a+bx}} - \frac{3\sqrt{-a+bx}}{a^2x} - \frac{3b \tan^{-1}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)}{a^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 34, normalized size = 0.55

$$\frac{2b {}_2F_1\left(-\frac{1}{2}, 2; \frac{1}{2}; 1 - \frac{bx}{a}\right)}{a^2\sqrt{bx-a}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(-a + b*x)^(3/2)),x]

[Out] (-2*b*Hypergeometric2F1[-1/2, 2, 1/2, 1 - (b*x)/a])/(a^2*Sqrt[-a + b*x])

fricas [A] time = 0.54, size = 164, normalized size = 2.65

$$\left[\frac{3(b^2x^2 - abx)\sqrt{-a} \log\left(\frac{bx+2\sqrt{bx-a}\sqrt{-a}-2a}{x}\right) + 2(3abx - a^2)\sqrt{bx-a}}{2(a^3bx^2 - a^4x)}, \frac{3(b^2x^2 - abx)\sqrt{a} \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right) + (3}{a^3bx^2 - a^4x} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(3/2),x, algorithm="fricas")

[Out] [-1/2*(3*(b^2*x^2 - a*b*x)*sqrt(-a)*log((b*x + 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) + 2*(3*a*b*x - a^2)*sqrt(b*x - a))/(a^3*b*x^2 - a^4*x), -(3*(b^2*x^2

$- a*b*x)*\sqrt{a}*\arctan(\sqrt{b*x - a}/\sqrt{a}) + (3*a*b*x - a^2)*\sqrt{b*x - a})/(a^3*b*x^2 - a^4*x)]$

giac [A] time = 1.01, size = 64, normalized size = 1.03

$$-\frac{3 b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{5}{2}}}-\frac{3 (bx-a) b+2 a b}{\left((bx-a)^{\frac{3}{2}}+\sqrt{bx-a} a\right) a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(3/2),x, algorithm="giac")

[Out] $-3*b*\arctan(\sqrt{b*x - a}/\sqrt{a})/a^{5/2} - (3*(b*x - a)*b + 2*a*b)/(((b*x - a)^{3/2} + \sqrt{b*x - a})*a^2)$

maple [A] time = 0.01, size = 54, normalized size = 0.87

$$-\frac{3 b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{5}{2}}}-\frac{2 b}{\sqrt{bx-a} a^2}-\frac{\sqrt{bx-a}}{a^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x-a)^(3/2),x)

[Out] $-2*b/a^2/(b*x-a)^{1/2}-1/a^2*(b*x-a)^{1/2}/x-3*b*\arctan((b*x-a)^{1/2}/a^{1/2})/a^{5/2}$

maxima [A] time = 3.02, size = 67, normalized size = 1.08

$$\frac{3 (bx-a) b+2 a b}{(bx-a)^{\frac{3}{2}} a^2+\sqrt{bx-a} a^3}-\frac{3 b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(3/2),x, algorithm="maxima")

[Out] $-(3*(b*x - a)*b + 2*a*b)/((b*x - a)^{3/2}*a^2 + \sqrt{b*x - a}*a^3) - 3*b*\arctan(\sqrt{b*x - a}/\sqrt{a})/a^{5/2}$

mupad [B] time = 0.06, size = 52, normalized size = 0.84

$$\frac{1}{a x \sqrt{b x-a}}-\frac{3 b}{a^2 \sqrt{b x-a}}-\frac{3 b \operatorname{atan}\left(\frac{\sqrt{b x-a}}{\sqrt{a}}\right)}{a^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^2*(b*x - a)^(3/2)),x)`

[Out] $1/(a*x*(b*x - a)^{(1/2)}) - (3*b)/(a^2*(b*x - a)^{(1/2)}) - (3*b*atan((b*x - a)^{(1/2)}/a^{(1/2)}))/a^{(5/2)}$

sympy [A] time = 3.50, size = 156, normalized size = 2.52

$$\left\{ \begin{array}{l} -\frac{i}{a\sqrt{b}x^{\frac{3}{2}}\sqrt{\frac{a}{bx}-1}} + \frac{3i\sqrt{b}}{a^2\sqrt{x}\sqrt{\frac{a}{bx}-1}} - \frac{3ib\operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{a^{\frac{5}{2}}} \quad \text{for } \left|\frac{a}{bx}\right| > 1 \\ \frac{1}{a\sqrt{b}x^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}} - \frac{3\sqrt{b}}{a^2\sqrt{x}\sqrt{-\frac{a}{bx}+1}} + \frac{3b\operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{a^{\frac{5}{2}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(b*x-a)**(3/2),x)`

[Out] `Piecewise((-I/(a*sqrt(b)*x**(3/2)*sqrt(a/(b*x) - 1)) + 3*I*sqrt(b)/(a**2*sqrt(x)*sqrt(a/(b*x) - 1)) - 3*I*b*acosh(sqrt(a)/(sqrt(b)*sqrt(x)))/a**(5/2), Abs(a/(b*x)) > 1), (1/(a*sqrt(b)*x**(3/2)*sqrt(-a/(b*x) + 1)) - 3*sqrt(b)/(a**2*sqrt(x)*sqrt(-a/(b*x) + 1)) + 3*b*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/a**(5/2), True))`

$$3.364 \quad \int \frac{1}{x^3(-a+bx)^{3/2}} dx$$

Optimal. Leaf size=95

$$-\frac{15b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{7/2}} - \frac{15b^2}{4a^3\sqrt{bx-a}} + \frac{5b}{4a^2x\sqrt{bx-a}} + \frac{1}{2ax^2\sqrt{bx-a}}$$

[Out] $-15/4*b^2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(7/2)}-15/4*b^2/a^3/(b*x-a)^{(1/2)}+1/2/a/x^2/(b*x-a)^{(1/2)}+5/4*b/a^2/x/(b*x-a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 93, normalized size of antiderivative = 0.98, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 205}

$$-\frac{15b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{7/2}} - \frac{5\sqrt{bx-a}}{2a^2x^2} - \frac{15b\sqrt{bx-a}}{4a^3x} - \frac{2}{ax^2\sqrt{bx-a}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(-a + b*x)^(3/2)),x]

[Out] $-2/(a*x^2*\text{Sqrt}[-a + b*x]) - (5*\text{Sqrt}[-a + b*x])/(2*a^2*x^2) - (15*b*\text{Sqrt}[-a + b*x])/(4*a^3*x) - (15*b^2*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]])/(4*a^{(7/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^3(-a+bx)^{3/2}} dx &= -\frac{2}{ax^2\sqrt{-a+bx}} - \frac{5 \int \frac{1}{x^3\sqrt{-a+bx}} dx}{a} \\
 &= -\frac{2}{ax^2\sqrt{-a+bx}} - \frac{5\sqrt{-a+bx}}{2a^2x^2} - \frac{(15b) \int \frac{1}{x^2\sqrt{-a+bx}} dx}{4a^2} \\
 &= -\frac{2}{ax^2\sqrt{-a+bx}} - \frac{5\sqrt{-a+bx}}{2a^2x^2} - \frac{15b\sqrt{-a+bx}}{4a^3x} - \frac{(15b^2) \int \frac{1}{x\sqrt{-a+bx}} dx}{8a^3} \\
 &= -\frac{2}{ax^2\sqrt{-a+bx}} - \frac{5\sqrt{-a+bx}}{2a^2x^2} - \frac{15b\sqrt{-a+bx}}{4a^3x} - \frac{(15b) \operatorname{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx}\right)}{4a^3} \\
 &= -\frac{2}{ax^2\sqrt{-a+bx}} - \frac{5\sqrt{-a+bx}}{2a^2x^2} - \frac{15b\sqrt{-a+bx}}{4a^3x} - \frac{15b^2 \tan^{-1}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)}{4a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 36, normalized size = 0.38

$$-\frac{2b^2 {}_2F_1\left(-\frac{1}{2}, 3; \frac{1}{2}; 1 - \frac{bx}{a}\right)}{a^3\sqrt{bx-a}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(-a + b*x)^(3/2)), x]

[Out] (-2*b^2*Hypergeometric2F1[-1/2, 3, 1/2, 1 - (b*x)/a])/(a^3*sqrt[-a + b*x])

fricas [A] time = 0.50, size = 198, normalized size = 2.08

$$\left[\frac{15(b^3x^3 - ab^2x^2)\sqrt{-a} \log\left(\frac{bx+2\sqrt{bx-a}\sqrt{-a}-2a}{x}\right) + 2(15ab^2x^2 - 5a^2bx - 2a^3)\sqrt{bx-a} - 15(b^3x^3 - ab^2x^2)\sqrt{a}}{8(a^4bx^3 - a^5x^2)}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(3/2),x, algorithm="fricas")

[Out] [-1/8*(15*(b^3*x^3 - a*b^2*x^2)*sqrt(-a)*log((b*x + 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) + 2*(15*a*b^2*x^2 - 5*a^2*b*x - 2*a^3)*sqrt(b*x - a))/(a^4*b*x^3 - a^5*x^2), -1/4*(15*(b^3*x^3 - a*b^2*x^2)*sqrt(a)*arctan(sqrt(b*x - a)/sqrt(a)) + (15*a*b^2*x^2 - 5*a^2*b*x - 2*a^3)*sqrt(b*x - a))/(a^4*b*x^3 - a^5*x^2)]

giac [A] time = 1.01, size = 81, normalized size = 0.85

$$-\frac{15b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{\frac{7}{2}}} - \frac{2b^2}{\sqrt{bx-a}a^3} - \frac{7(bx-a)^{\frac{3}{2}}b^2 + 9\sqrt{bx-a}ab^2}{4a^3b^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(3/2),x, algorithm="giac")

[Out] -15/4*b^2*arctan(sqrt(b*x - a)/sqrt(a))/a^(7/2) - 2*b^2/(sqrt(b*x - a)*a^3) - 1/4*(7*(b*x - a)^(3/2)*b^2 + 9*sqrt(b*x - a)*a*b^2)/(a^3*b^2*x^2)

maple [A] time = 0.01, size = 75, normalized size = 0.79

$$-\frac{15b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{\frac{7}{2}}} - \frac{2b^2}{\sqrt{bx-a}a^3} - \frac{9\sqrt{bx-a}}{4a^2x^2} - \frac{7(bx-a)^{\frac{3}{2}}}{4a^3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x-a)^(3/2),x)

[Out] -2*b^2/a^3/(b*x-a)^(1/2)-7/4/a^3/x^2*(b*x-a)^(3/2)-9/4/a^2/x^2*(b*x-a)^(1/2)-15/4*b^2*arctan((b*x-a)^(1/2)/a^(1/2))/a^(7/2)

maxima [A] time = 2.93, size = 104, normalized size = 1.09

$$-\frac{15(bx-a)^2b^2 + 25(bx-a)ab^2 + 8a^2b^2}{4\left((bx-a)^{\frac{5}{2}}a^3 + 2(bx-a)^{\frac{3}{2}}a^4 + \sqrt{bx-a}a^5\right)} - \frac{15b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(3/2),x, algorithm="maxima")

[Out] -1/4*(15*(b*x - a)^2*b^2 + 25*(b*x - a)*a*b^2 + 8*a^2*b^2)/((b*x - a)^(5/2)*a^3 + 2*(b*x - a)^(3/2)*a^4 + sqrt(b*x - a)*a^5) - 15/4*b^2*arctan(sqrt(b*x - a)/sqrt(a))/a^(7/2)

mupad [B] time = 0.13, size = 101, normalized size = 1.06

$$\frac{\frac{2b^2}{a} + \frac{15b^2(a-bx)^2}{4a^3} - \frac{25b^2(a-bx)}{4a^2}}{2a(bx-a)^{3/2} + (bx-a)^{5/2} + a^2\sqrt{bx-a}} - \frac{15b^2 \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^3*(b*x - a)^(3/2)), x)`

[Out] `- ((2*b^2)/a + (15*b^2*(a - b*x)^2)/(4*a^3) - (25*b^2*(a - b*x))/(4*a^2))/(2*a*(b*x - a)^(3/2) + (b*x - a)^(5/2) + a^2*(b*x - a)^(1/2)) - (15*b^2*atan((b*x - a)^(1/2)/a^(1/2)))/(4*a^(7/2))`

sympy [A] time = 5.57, size = 226, normalized size = 2.38

$$\left\{ \begin{array}{l} -\frac{i}{2a\sqrt{b}x^2\sqrt{\frac{a}{bx}-1}} - \frac{5i\sqrt{b}}{4a^2x^2\sqrt{\frac{a}{bx}-1}} + \frac{15ib^{\frac{3}{2}}}{4a^3\sqrt{x}\sqrt{\frac{a}{bx}-1}} - \frac{15ib^2 \operatorname{acosh}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4a^{\frac{7}{2}}} \quad \text{for } \left|\frac{a}{bx}\right| > 1 \\ \frac{1}{2a\sqrt{b}x^2\sqrt{-\frac{a}{bx}+1}} + \frac{5\sqrt{b}}{4a^2x^2\sqrt{-\frac{a}{bx}+1}} - \frac{15b^{\frac{3}{2}}}{4a^3\sqrt{x}\sqrt{-\frac{a}{bx}+1}} + \frac{15b^2 \operatorname{asin}\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right)}{4a^{\frac{7}{2}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**3/(b*x-a)**(3/2), x)`

[Out] `Piecewise((-I/(2*a*sqrt(b)*x**(5/2)*sqrt(a/(b*x) - 1)) - 5*I*sqrt(b)/(4*a**2*x**(3/2)*sqrt(a/(b*x) - 1)) + 15*I*b**(3/2)/(4*a**3*sqrt(x)*sqrt(a/(b*x) - 1)) - 15*I*b**2*acosh(sqrt(a)/(sqrt(b)*sqrt(x)))/(4*a**(7/2)), Abs(a/(b*x)) > 1), (1/(2*a*sqrt(b)*x**(5/2)*sqrt(-a/(b*x) + 1)) + 5*sqrt(b)/(4*a**2*x**(3/2)*sqrt(-a/(b*x) + 1)) - 15*b**(3/2)/(4*a**3*sqrt(x)*sqrt(-a/(b*x) + 1)) + 15*b**2*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/(4*a**(7/2)), True))`

$$3.365 \quad \int \frac{1}{x(-a+bx)^{5/2}} dx$$

Optimal. Leaf size=60

$$\frac{2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{5/2}} + \frac{2}{a^2\sqrt{bx-a}} - \frac{2}{3a(bx-a)^{3/2}}$$

[Out] $-2/3/a/(b*x-a)^{(3/2)}+2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(5/2)}+2/a^2/(b*x-a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 205}

$$\frac{2}{a^2\sqrt{bx-a}} + \frac{2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{2}{3a(bx-a)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(-a + b*x)^(5/2)),x]

[Out] $-2/(3*a*(-a + b*x)^{(3/2)}) + 2/(a^2*\text{Sqrt}[-a + b*x]) + (2*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]])/a^{(5/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x(-a+bx)^{5/2}} dx &= -\frac{2}{3a(-a+bx)^{3/2}} - \frac{\int \frac{1}{x(-a+bx)^{3/2}} dx}{a} \\
 &= -\frac{2}{3a(-a+bx)^{3/2}} + \frac{2}{a^2\sqrt{-a+bx}} + \frac{\int \frac{1}{x\sqrt{-a+bx}} dx}{a^2} \\
 &= -\frac{2}{3a(-a+bx)^{3/2}} + \frac{2}{a^2\sqrt{-a+bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx}\right)}{a^2 b} \\
 &= -\frac{2}{3a(-a+bx)^{3/2}} + \frac{2}{a^2\sqrt{-a+bx}} + \frac{2 \tan^{-1}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)}{a^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.58

$$-\frac{{}_2F_1\left(-\frac{3}{2}, 1; -\frac{1}{2}; 1 - \frac{bx}{a}\right)}{3a(bx-a)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(-a + b*x)^(5/2)), x]

[Out] (-2*Hypergeometric2F1[-3/2, 1, -1/2, 1 - (b*x)/a])/(3*a*(-a + b*x)^(3/2))

fricas [A] time = 0.48, size = 182, normalized size = 3.03

$$\left[\frac{3(b^2x^2 - 2abx + a^2)\sqrt{-a} \log\left(\frac{bx - 2\sqrt{bx-a}\sqrt{-a} - 2a}{x}\right) - 2(3abx - 4a^2)\sqrt{bx-a}}{3(a^3b^2x^2 - 2a^4bx + a^5)}, \frac{2\left(3(b^2x^2 - 2abx + a^2)\sqrt{a} \operatorname{arctan}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)\right)}{3(a^3b^2x^2 - 2a^4bx + a^5)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(5/2), x, algorithm="fricas")

[Out] [-1/3*(3*(b^2*x^2 - 2*a*b*x + a^2)*sqrt(-a)*log((b*x - 2*sqrt(b*x - a)*sqrt(-a) - 2*a)/x) - 2*(3*a*b*x - 4*a^2)*sqrt(b*x - a))/(a^3*b^2*x^2 - 2*a^4*b*

$x + a^5$), $2/3*(3*(b^2*x^2 - 2*a*b*x + a^2)*\sqrt{a}*\arctan(\sqrt{b*x - a}/\sqrt{a}) + (3*a*b*x - 4*a^2)*\sqrt{b*x - a})/(a^3*b^2*x^2 - 2*a^4*b*x + a^5)$]

giac [A] time = 1.06, size = 42, normalized size = 0.70

$$\frac{2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{5}{2}}} + \frac{2(3bx-4a)}{3(bx-a)^{\frac{3}{2}}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(5/2),x, algorithm="giac")

[Out] $2*\arctan(\sqrt{b*x - a}/\sqrt{a})/a^{(5/2)} + 2/3*(3*b*x - 4*a)/((b*x - a)^{(3/2)}*a^2)$

maple [A] time = 0.01, size = 49, normalized size = 0.82

$$-\frac{2}{3(bx-a)^{\frac{3}{2}}a} + \frac{2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{5}{2}}} + \frac{2}{\sqrt{bx-a}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x-a)^(5/2),x)

[Out] $-2/3/a/(b*x-a)^{(3/2)}+2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(5/2)}+2/a^2/(b*x-a)^{(1/2)}$

maxima [A] time = 2.94, size = 42, normalized size = 0.70

$$\frac{2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{5}{2}}} + \frac{2(3bx-4a)}{3(bx-a)^{\frac{3}{2}}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(5/2),x, algorithm="maxima")

[Out] $2*\arctan(\sqrt{b*x - a}/\sqrt{a})/a^{(5/2)} + 2/3*(3*b*x - 4*a)/((b*x - a)^{(3/2)}*a^2)$

mupad [B] time = 0.09, size = 48, normalized size = 0.80

$$\frac{2 \operatorname{atan}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{\frac{2(a-bx)}{a^2} + \frac{2}{3a}}{(bx-a)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(x*(b*x - a)^(5/2)),x)
```

```
[Out] (2*atan((b*x - a)^(1/2)/a^(1/2)))/a^(5/2) - ((2*(a - b*x))/a^2 + 2/(3*a))/(b*x - a)^(3/2)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x/(b*x-a)**(5/2),x)
```

```
[Out] Timed out
```

$$3.366 \quad \int \frac{1}{x^2(-a+bx)^{5/2}} dx$$

Optimal. Leaf size=81

$$\frac{5b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{7/2}} + \frac{5b}{a^3\sqrt{bx-a}} - \frac{5b}{3a^2(bx-a)^{3/2}} + \frac{1}{ax(bx-a)^{3/2}}$$

[Out] $-5/3*b/a^2/(b*x-a)^{(3/2)}+1/a/x/(b*x-a)^{(3/2)}+5*b*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(7/2)}+5*b/a^3/(b*x-a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 88, normalized size of antiderivative = 1.09, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 205}

$$\frac{5\sqrt{bx-a}}{a^3x} + \frac{10}{3a^2x\sqrt{bx-a}} + \frac{5b \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{7/2}} - \frac{2}{3ax(bx-a)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(-a + b*x)^(5/2)),x]

[Out] $-2/(3*a*x*(-a + b*x)^{(3/2)}) + 10/(3*a^2*x*\text{Sqrt}[-a + b*x]) + (5*\text{Sqrt}[-a + b*x])/a^{(3*x)} + (5*b*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]])/a^{(7/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^2(-a+bx)^{5/2}} dx &= -\frac{2}{3ax(-a+bx)^{3/2}} - \frac{5 \int \frac{1}{x^2(-a+bx)^{3/2}} dx}{3a} \\
 &= -\frac{2}{3ax(-a+bx)^{3/2}} + \frac{10}{3a^2x\sqrt{-a+bx}} + \frac{5 \int \frac{1}{x^2\sqrt{-a+bx}} dx}{a^2} \\
 &= -\frac{2}{3ax(-a+bx)^{3/2}} + \frac{10}{3a^2x\sqrt{-a+bx}} + \frac{5\sqrt{-a+bx}}{a^3x} + \frac{(5b) \int \frac{1}{x\sqrt{-a+bx}} dx}{2a^3} \\
 &= -\frac{2}{3ax(-a+bx)^{3/2}} + \frac{10}{3a^2x\sqrt{-a+bx}} + \frac{5\sqrt{-a+bx}}{a^3x} + \frac{5 \operatorname{Subst}\left(\int \frac{1}{\frac{a}{b} + \frac{x^2}{b}} dx, x, \sqrt{-a+bx}\right)}{a^3} \\
 &= -\frac{2}{3ax(-a+bx)^{3/2}} + \frac{10}{3a^2x\sqrt{-a+bx}} + \frac{5\sqrt{-a+bx}}{a^3x} + \frac{5b \tan^{-1}\left(\frac{\sqrt{-a+bx}}{\sqrt{a}}\right)}{a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 36, normalized size = 0.44

$$-\frac{2b {}_2F_1\left(-\frac{3}{2}, 2; -\frac{1}{2}; 1 - \frac{bx}{a}\right)}{3a^2(bx-a)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(-a + b*x)^(5/2)), x]

[Out] (-2*b*Hypergeometric2F1[-3/2, 2, -1/2, 1 - (b*x)/a])/(3*a^2*(-a + b*x)^(3/2))

fricas [A] time = 0.48, size = 226, normalized size = 2.79

$$\left[\frac{15(b^3x^3 - 2ab^2x^2 + a^2bx)\sqrt{-a} \log\left(\frac{bx-2\sqrt{bx-a}\sqrt{-a}-2a}{x}\right) - 2(15ab^2x^2 - 20a^2bx + 3a^3)\sqrt{bx-a}}{6(a^4b^2x^3 - 2a^5bx^2 + a^6x)}, \frac{15(b^3x^3 - 2ab^2x^2 + a^2bx)\sqrt{-a}}{6(a^4b^2x^3 - 2a^5bx^2 + a^6x)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(5/2),x, algorithm="fricas")

[Out] $[-1/6*(15*(b^3*x^3 - 2*a*b^2*x^2 + a^2*b*x)*\sqrt{-a}*\log((b*x - 2*\sqrt{b*x - a})*\sqrt{-a} - 2*a)/x) - 2*(15*a*b^2*x^2 - 20*a^2*b*x + 3*a^3)*\sqrt{b*x - a}]/(a^4*b^2*x^3 - 2*a^5*b*x^2 + a^6*x), 1/3*(15*(b^3*x^3 - 2*a*b^2*x^2 + a^2*b*x)*\sqrt{a}*\arctan(\sqrt{b*x - a}/\sqrt{a}) + (15*a*b^2*x^2 - 20*a^2*b*x + 3*a^3)*\sqrt{b*x - a})/(a^4*b^2*x^3 - 2*a^5*b*x^2 + a^6*x)]$

giac [A] time = 1.00, size = 66, normalized size = 0.81

$$\frac{5b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{7}{2}}} + \frac{2(6(bx-a)b - ab)}{3(bx-a)^{\frac{3}{2}}a^3} + \frac{\sqrt{bx-a}}{a^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(5/2),x, algorithm="giac")

[Out] $5*b*\arctan(\sqrt{b*x - a}/\sqrt{a})/a^{(7/2)} + 2/3*(6*(b*x - a)*b - a*b)/((b*x - a)^{(3/2)}*a^3) + \sqrt{b*x - a}/(a^3*x)$

maple [A] time = 0.01, size = 68, normalized size = 0.84

$$-\frac{2b}{3(bx-a)^{\frac{3}{2}}a^2} + \frac{5b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{7}{2}}} + \frac{4b}{\sqrt{bx-a}a^3} + \frac{\sqrt{bx-a}}{a^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x-a)^(5/2),x)

[Out] $-2/3*b/a^2/(b*x-a)^{(3/2)}+4*b/a^3/(b*x-a)^{(1/2)}+1/a^3*(b*x-a)^{(1/2)}/x+5*b*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(7/2)}$

maxima [A] time = 2.93, size = 82, normalized size = 1.01

$$\frac{15(bx-a)^2b + 10(bx-a)ab - 2a^2b}{3\left((bx-a)^{\frac{5}{2}}a^3 + (bx-a)^{\frac{3}{2}}a^4\right)} + \frac{5b \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{a^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(5/2),x, algorithm="maxima")

[Out] $1/3*(15*(b*x - a)^2*b + 10*(b*x - a)*a*b - 2*a^2*b)/((b*x - a)^{(5/2)}*a^3 + (b*x - a)^{(3/2)}*a^4) + 5*b*\arctan(\sqrt{b*x - a}/\sqrt{a})/a^{(7/2)}$

mupad [B] time = 0.12, size = 70, normalized size = 0.86

$$\frac{1}{a x (b x - a)^{3/2}} - \frac{20 b}{3 a^2 (b x - a)^{3/2}} + \frac{5 b \operatorname{atan}\left(\frac{\sqrt{b x - a}}{\sqrt{a}}\right)}{a^{7/2}} + \frac{5 b^2 x}{a^3 (b x - a)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^2*(b*x - a)^(5/2)),x)`

[Out] `1/(a*x*(b*x - a)^(3/2)) - (20*b)/(3*a^2*(b*x - a)^(3/2)) + (5*b*atan((b*x - a)^(1/2)/a^(1/2)))/a^(7/2) + (5*b^2*x)/(a^3*(b*x - a)^(3/2))`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(b*x-a)**(5/2),x)`

[Out] Timed out

$$3.367 \quad \int \frac{1}{x^3(-a+bx)^{5/2}} dx$$

Optimal. Leaf size=116

$$\frac{35b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{9/2}} + \frac{35b^2}{4a^4\sqrt{bx-a}} - \frac{35b^2}{12a^3(bx-a)^{3/2}} + \frac{7b}{4a^2x(bx-a)^{3/2}} + \frac{1}{2ax^2(bx-a)^{3/2}}$$

[Out] $-35/12*b^2/a^3/(b*x-a)^{(3/2)}+1/2/a/x^2/(b*x-a)^{(3/2)}+7/4*b/a^2/x/(b*x-a)^{(3/2)}+35/4*b^2*\arctan((b*x-a)^{(1/2)}/a^{(1/2)})/a^{(9/2)}+35/4*b^2/a^4/(b*x-a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 116, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 205}

$$\frac{35b^2 \tan^{-1}\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{9/2}} + \frac{35\sqrt{bx-a}}{6a^3x^2} + \frac{14}{3a^2x^2\sqrt{bx-a}} + \frac{35b\sqrt{bx-a}}{4a^4x} - \frac{2}{3ax^2(bx-a)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(-a + b*x)^(5/2)), x]

[Out] $-2/(3*a*x^2*(-a + b*x)^{(3/2)}) + 14/(3*a^2*x^2*\text{Sqrt}[-a + b*x]) + (35*\text{Sqrt}[-a + b*x])/(6*a^3*x^2) + (35*b*\text{Sqrt}[-a + b*x])/(4*a^4*x) + (35*b^2*\text{ArcTan}[\text{Sqrt}[-a + b*x]/\text{Sqrt}[a]])/(4*a^{(9/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^3(-a+bx)^{5/2}} dx &= -\frac{2}{3ax^2(-a+bx)^{3/2}} - \frac{7 \int \frac{1}{x^3(-a+bx)^{3/2}} dx}{3a} \\
 &= -\frac{2}{3ax^2(-a+bx)^{3/2}} + \frac{14}{3a^2x^2\sqrt{-a+bx}} + \frac{35 \int \frac{1}{x^3\sqrt{-a+bx}} dx}{3a^2} \\
 &= -\frac{2}{3ax^2(-a+bx)^{3/2}} + \frac{14}{3a^2x^2\sqrt{-a+bx}} + \frac{35\sqrt{-a+bx}}{6a^3x^2} + \frac{(35b) \int \frac{1}{x^2\sqrt{-a+bx}} dx}{4a^3} \\
 &= -\frac{2}{3ax^2(-a+bx)^{3/2}} + \frac{14}{3a^2x^2\sqrt{-a+bx}} + \frac{35\sqrt{-a+bx}}{6a^3x^2} + \frac{35b\sqrt{-a+bx}}{4a^4x} + \frac{(35b^2) \int \frac{1}{x\sqrt{-a+bx}} dx}{8a^4} \\
 &= -\frac{2}{3ax^2(-a+bx)^{3/2}} + \frac{14}{3a^2x^2\sqrt{-a+bx}} + \frac{35\sqrt{-a+bx}}{6a^3x^2} + \frac{35b\sqrt{-a+bx}}{4a^4x} + \frac{(35b) \operatorname{Subst}\left(\int \frac{1}{\sqrt{-a+bx}} dx\right)}{8a^4} \\
 &= -\frac{2}{3ax^2(-a+bx)^{3/2}} + \frac{14}{3a^2x^2\sqrt{-a+bx}} + \frac{35\sqrt{-a+bx}}{6a^3x^2} + \frac{35b\sqrt{-a+bx}}{4a^4x} + \frac{35b^2 \tan^{-1}\left(\frac{\sqrt{-a+bx}}{x}\right)}{4a^{9/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 38, normalized size = 0.33

$$-\frac{2b^2 {}_2F_1\left(-\frac{3}{2}, 3; -\frac{1}{2}; 1 - \frac{bx}{a}\right)}{3a^3(bx-a)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(-a + b*x)^(5/2)), x]

[Out] (-2*b^2*Hypergeometric2F1[-3/2, 3, -1/2, 1 - (b*x)/a])/(3*a^3*(-a + b*x)^(3/2))

fricas [A] time = 0.47, size = 260, normalized size = 2.24

$$\left[\frac{105(b^4x^4 - 2ab^3x^3 + a^2b^2x^2)\sqrt{-a} \log\left(\frac{bx-2\sqrt{bx-a}\sqrt{-a}-2a}{x}\right) - 2(105ab^3x^3 - 140a^2b^2x^2 + 21a^3bx + 6a^4)\sqrt{bx-a}}{24(a^5b^2x^4 - 2a^6bx^3 + a^7x^2)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(5/2),x, algorithm="fricas")

[Out] $[-1/24*(105*(b^4*x^4 - 2*a*b^3*x^3 + a^2*b^2*x^2)*\sqrt{-a}*\log((b*x - 2*\sqrt{a}*(b*x - a)*\sqrt{-a} - 2*a)/x) - 2*(105*a*b^3*x^3 - 140*a^2*b^2*x^2 + 21*a^3*b*x + 6*a^4)*\sqrt{b*x - a})/(a^5*b^2*x^4 - 2*a^6*b*x^3 + a^7*x^2), 1/12*(105*(b^4*x^4 - 2*a*b^3*x^3 + a^2*b^2*x^2)*\sqrt{a}*\arctan(\sqrt{b*x - a}/\sqrt{a})) + (105*a*b^3*x^3 - 140*a^2*b^2*x^2 + 21*a^3*b*x + 6*a^4)*\sqrt{b*x - a})/(a^5*b^2*x^4 - 2*a^6*b*x^3 + a^7*x^2)]$

giac [A] time = 0.90, size = 97, normalized size = 0.84

$$\frac{35b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{\frac{9}{2}}} + \frac{2(9(bx-a)b^2 - ab^2)}{3(bx-a)^{\frac{3}{2}}a^4} + \frac{11(bx-a)^{\frac{3}{2}}b^2 + 13\sqrt{bx-a}ab^2}{4a^4b^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(5/2),x, algorithm="giac")

[Out] $35/4*b^2*\arctan(\sqrt{b*x - a}/\sqrt{a})/a^{9/2} + 2/3*(9*(b*x - a)*b^2 - a*b^2)/((b*x - a)^{3/2}*a^4) + 1/4*(11*(b*x - a)^{3/2}*b^2 + 13*\sqrt{b*x - a}*a*b^2)/(a^4*b^2*x^2)$

maple [A] time = 0.02, size = 92, normalized size = 0.79

$$-\frac{2b^2}{3(bx-a)^{\frac{3}{2}}a^3} + \frac{35b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{\frac{9}{2}}} + \frac{6b^2}{\sqrt{bx-a}a^4} + \frac{13\sqrt{bx-a}}{4a^3x^2} + \frac{11(bx-a)^{\frac{3}{2}}}{4a^4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x-a)^(5/2),x)

[Out] $-2/3*b^2/a^3/(b*x-a)^{3/2}+6*b^2/a^4/(b*x-a)^{1/2}+11/4/a^4/x^2*(b*x-a)^{3/2}+13/4/a^3/x^2*(b*x-a)^{1/2}+35/4*b^2*\arctan((b*x-a)^{1/2}/a^{1/2})/a^{9/2}$

maxima [A] time = 2.87, size = 121, normalized size = 1.04

$$\frac{105(bx-a)^3b^2 + 175(bx-a)^2ab^2 + 56(bx-a)a^2b^2 - 8a^3b^2}{12\left((bx-a)^{\frac{7}{2}}a^4 + 2(bx-a)^{\frac{5}{2}}a^5 + (bx-a)^{\frac{3}{2}}a^6\right)} + \frac{35b^2 \arctan\left(\frac{\sqrt{bx-a}}{\sqrt{a}}\right)}{4a^{\frac{9}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(5/2),x, algorithm="maxima")

[Out] $\frac{1}{12} \cdot (105 \cdot (b \cdot x - a)^3 \cdot b^2 + 175 \cdot (b \cdot x - a)^2 \cdot a \cdot b^2 + 56 \cdot (b \cdot x - a) \cdot a^2 \cdot b^2 - 8 \cdot a^3 \cdot b^2) / ((b \cdot x - a)^{7/2} \cdot a^4 + 2 \cdot (b \cdot x - a)^{5/2} \cdot a^5 + (b \cdot x - a)^{3/2} \cdot a^6) + 35/4 \cdot b^2 \cdot \arctan(\sqrt{b \cdot x - a} / \sqrt{a}) / a^{9/2}$

mupad [B] time = 0.07, size = 117, normalized size = 1.01

$$\frac{35 b^2 \operatorname{atan}\left(\frac{\sqrt{b x-a}}{\sqrt{a}}\right)}{4 a^{9/2}} - \frac{\frac{2 b^2}{3 a} - \frac{175 b^2 (a-b x)^2}{12 a^3} + \frac{35 b^2 (a-b x)^3}{4 a^4} + \frac{14 b^2 (a-b x)}{3 a^2}}{2 a (b x-a)^{5/2} + (b x-a)^{7/2} + a^2 (b x-a)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(b*x - a)^(5/2)),x)

[Out] $(35 \cdot b^2 \cdot \operatorname{atan}((b \cdot x - a)^{1/2} / a^{1/2})) / (4 \cdot a^{9/2}) - ((2 \cdot b^2) / (3 \cdot a) - (175 \cdot b^2 \cdot (a - b \cdot x)^2) / (12 \cdot a^3) + (35 \cdot b^2 \cdot (a - b \cdot x)^3) / (4 \cdot a^4) + (14 \cdot b^2 \cdot (a - b \cdot x)) / (3 \cdot a^2)) / (2 \cdot a \cdot (b \cdot x - a)^{5/2} + (b \cdot x - a)^{7/2} + a^2 \cdot (b \cdot x - a)^{3/2})$

sympy [B] time = 11.22, size = 1108, normalized size = 9.55

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(b*x-a)**(5/2),x)

[Out] Piecewise(($(12 \cdot I \cdot a^{89/2} \cdot b^{75} \cdot x^{75} / (24 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2}) \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 24 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) + 42 \cdot I \cdot a^{87/2} \cdot b^{76} \cdot x^{76} / (24 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2}) \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 24 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 280 \cdot I \cdot a^{85/2} \cdot b^{77} \cdot x^{77} / (24 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2}) \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 24 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) + 210 \cdot I \cdot a^{83/2} \cdot b^{78} \cdot x^{78} / (24 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2}) \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 24 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) + 210 \cdot I \cdot a^{42} \cdot b^{155/2} \cdot x^{155/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) \cdot \operatorname{acosh}(\operatorname{sqrt}(a) / (\operatorname{sqrt}(b) \cdot \operatorname{sqrt}(x))) / (24 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2}) \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 24 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 105 \cdot \pi \cdot a^{42} \cdot b^{155/2} \cdot x^{155/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) / (24 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2}) \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 24 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 210 \cdot I \cdot a^{41} \cdot b^{157/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) \cdot \operatorname{acosh}(\operatorname{sqrt}(a) / (\operatorname{sqrt}(b) \cdot \operatorname{sqrt}(x))) / (24 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2}) \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 24 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) + 105 \cdot \pi \cdot a^{41} \cdot b^{157/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) / (24 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2}) \cdot \operatorname{sqrt}(a / (b \cdot x) - 1) - 24 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(a / (b \cdot x) - 1)$), Abs(a/(b*x)) > 1), (- $6 \cdot a^{89/2} \cdot b^{75} \cdot x^{75} / (12 \cdot a^{93/2} \cdot b^{151/2} \cdot x^{155/2}) \cdot \operatorname{sqrt}(-a / (b \cdot x) + 1) - 12 \cdot a^{91/2} \cdot b^{153/2} \cdot x^{157/2} \cdot \operatorname{sqrt}(-a / (b \cdot x) + 1)$))

```

/2)*sqrt(-a/(b*x) + 1)) - 21*a**(87/2)*b**76*x**76/(12*a**(93/2)*b**(151/2)
*x**(155/2)*sqrt(-a/(b*x) + 1) - 12*a**(91/2)*b**(153/2)*x**(157/2)*sqrt(-a
/(b*x) + 1)) + 140*a**(85/2)*b**77*x**77/(12*a**(93/2)*b**(151/2)*x**(155/2)
)*sqrt(-a/(b*x) + 1) - 12*a**(91/2)*b**(153/2)*x**(157/2)*sqrt(-a/(b*x) + 1
)) - 105*a**(83/2)*b**78*x**78/(12*a**(93/2)*b**(151/2)*x**(155/2)*sqrt(-a/
(b*x) + 1) - 12*a**(91/2)*b**(153/2)*x**(157/2)*sqrt(-a/(b*x) + 1)) - 105*a
**42*b**(155/2)*x**(155/2)*sqrt(-a/(b*x) + 1)*asin(sqrt(a)/(sqrt(b)*sqrt(x)
))/(12*a**(93/2)*b**(151/2)*x**(155/2)*sqrt(-a/(b*x) + 1) - 12*a**(91/2)*b*
*(153/2)*x**(157/2)*sqrt(-a/(b*x) + 1)) + 105*a**41*b**(157/2)*x**(157/2)*s
qrt(-a/(b*x) + 1)*asin(sqrt(a)/(sqrt(b)*sqrt(x)))/(12*a**(93/2)*b**(151/2)*
x**(155/2)*sqrt(-a/(b*x) + 1) - 12*a**(91/2)*b**(153/2)*x**(157/2)*sqrt(-a/
(b*x) + 1)), True))

```

$$3.368 \quad \int \frac{x^{-1+m}(2am+b(-1+2m)x)}{2(a+bx)^{3/2}} dx$$

Optimal. Leaf size=13

$$\frac{x^m}{\sqrt{a+bx}}$$

[Out] $x^m/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 31, $\frac{\text{number of rules}}{\text{integrand size}} = 0.065$, Rules used = {12, 74}

$$\frac{x^m}{\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x^{(-1+m)}*(2*a*m + b*(-1+2*m)*x))/(2*(a + b*x)^{(3/2)}), x]$

[Out] $x^m/\text{Sqrt}[a + b*x]$

Rule 12

$\text{Int}[(a_*)(u_), x_Symbol] \rightarrow \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \ \&\& \ !\text{MatchQ}[u, (b_*)(v_)] /; \text{FreeQ}[b, x]$

Rule 74

$\text{Int}[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^{(n_.)}*((e_.) + (f_.)*(x_))^{(p_.)}, x_Symbol] \rightarrow \text{Simp}[(b*(c + d*x)^{(n+1)}*(e + f*x)^{(p+1)})/(d*f*(n+p+2)), x] /; \text{FreeQ}[\{a, b, c, d, e, f, n, p\}, x] \ \&\& \ \text{NeQ}[n+p+2, 0] \ \&\& \ \text{EqQ}[a*d*f*(n+p+2) - b*(d*e*(n+1) + c*f*(p+1)), 0]$

Rubi steps

$$\begin{aligned} \int \frac{x^{-1+m}(2am+b(-1+2m)x)}{2(a+bx)^{3/2}} dx &= \frac{1}{2} \int \frac{x^{-1+m}(2am+b(-1+2m)x)}{(a+bx)^{3/2}} dx \\ &= \frac{x^m}{\sqrt{a+bx}} \end{aligned}$$

Mathematica [A] time = 0.04, size = 13, normalized size = 1.00

$$\frac{x^m}{\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^(-1 + m)*(2*a*m + b*(-1 + 2*m)*x))/(2*(a + b*x)^(3/2)),x]

[Out] x^m/Sqrt[a + b*x]

fricas [A] time = 0.48, size = 14, normalized size = 1.08

$$\frac{xx^{m-1}}{\sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/2*x^(-1+m)*(2*a*m+b*(-1+2*m)*x)/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] x*x^(m - 1)/sqrt(b*x + a)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(b(2m-1)x + 2am)x^{m-1}}{2(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/2*x^(-1+m)*(2*a*m+b*(-1+2*m)*x)/(b*x+a)^(3/2),x, algorithm="giac")

[Out] integrate(1/2*(b*(2*m - 1)*x + 2*a*m)*x^(m - 1)/(b*x + a)^(3/2), x)

maple [A] time = 0.01, size = 12, normalized size = 0.92

$$\frac{x^m}{\sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/2*x^(-1+m)*(2*a*m+b*(-1+2*m)*x)/(b*x+a)^(3/2), x)

[Out] x^m/(b*x+a)^(1/2)

maxima [A] time = 1.87, size = 11, normalized size = 0.85

$$\frac{x^m}{\sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/2*x^(-1+m)*(2*a*m+b*(-1+2*m)*x)/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] x^m/sqrt(b*x + a)

mupad [B] time = 0.41, size = 11, normalized size = 0.85

$$\frac{x^m}{\sqrt{a + bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^(m - 1)*(2*a*m + b*x*(2*m - 1)))/(2*(a + b*x)^(3/2)),x)

[Out] x^m/(a + b*x)^(1/2)

sympy [C] time = 84.07, size = 78, normalized size = 6.00

$$\frac{mx^m\Gamma(m) {}_2F_1\left(\frac{3}{2}, m \left| \frac{bx e^{i\pi}}{a} \right. \right)}{\sqrt{a}\Gamma(m+1)} + \frac{bxx^m(2m-1)\Gamma(m+1) {}_2F_1\left(\frac{3}{2}, m+1 \left| \frac{bx e^{i\pi}}{a} \right. \right)}{2a^{\frac{3}{2}}\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/2*x**(-1+m)*(2*a*m+b*(-1+2*m)*x)/(b*x+a)**(3/2),x)

[Out] m*x**m*gamma(m)*hyper((3/2, m), (m + 1,), b*x*exp_polar(I*pi)/a)/(sqrt(a)*gamma(m + 1)) + b*x*x**m*(2*m - 1)*gamma(m + 1)*hyper((3/2, m + 1), (m + 2,), b*x*exp_polar(I*pi)/a)/(2*a**(3/2)*gamma(m + 2))

$$3.369 \quad \int \left(-\frac{bx^m}{2(a+bx)^{3/2}} + \frac{mx^{-1+m}}{\sqrt{a+bx}} \right) dx$$

Optimal. Leaf size=13

$$\frac{x^m}{\sqrt{a+bx}}$$

[Out] $x^m/(b*x+a)^{(1/2)}$

Rubi [C] time = 0.04, antiderivative size = 92, normalized size of antiderivative = 7.08, number of steps used = 5, number of rules used = 2, integrand size = 34, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {67, 65}

$$\frac{x^m \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(-\frac{1}{2}, -m; \frac{1}{2}; \frac{bx}{a} + 1\right)}{\sqrt{a+bx}} - \frac{2mx^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, 1-m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{a}$$

Antiderivative was successfully verified.

[In] $\text{Int}[-(b*x^m)/(2*(a + b*x)^{(3/2)}) + (m*x^{(-1 + m)})/\text{Sqrt}[a + b*x], x]$

[Out] $(x^m * \text{Hypergeometric2F1}[-1/2, -m, 1/2, 1 + (b*x)/a]) / ((-(b*x)/a))^m * \text{Sqrt}[a + b*x] - (2*m*x^m * \text{Sqrt}[a + b*x] * \text{Hypergeometric2F1}[1/2, 1 - m, 3/2, 1 + (b*x)/a]) / (a * (-(b*x)/a))^m$

Rule 65

$\text{Int}[(b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}), x_Symbol] \rightarrow \text{Simp}[(c + d*x)^{(n + 1)} * \text{Hypergeometric2F1}[-m, n + 1, n + 2, 1 + (d*x)/c]) / (d*(n + 1) * (-(d/(b*c)))^m), x] /;$ $\text{FreeQ}\{b, c, d, m, n\}, x \ \&\& \ !\text{IntegerQ}[n] \ \&\& \ (\text{IntegerQ}[m] \ || \ \text{GtQ}[-(d/(b*c)), 0])$

Rule 67

$\text{Int}[(b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}), x_Symbol] \rightarrow \text{Dist}[(c + d*x)^m * \text{IntPart}[m] * (b*x)^{\text{FracPart}[m]} / (-(d*x)/c)^{\text{FracPart}[m]}, \text{Int}[(c + d*x)^n, x], x] /;$ $\text{FreeQ}\{b, c, d, m, n\}, x \ \&\& \ !\text{IntegerQ}[m] \ \&\& \ !\text{IntegerQ}[n] \ \&\& \ !\text{GtQ}[c, 0] \ \&\& \ !\text{GtQ}[-(d/(b*c)), 0]$

Rubi steps

$$\begin{aligned}
\int \left(-\frac{bx^m}{2(a+bx)^{3/2}} + \frac{mx^{-1+m}}{\sqrt{a+bx}} \right) dx &= -\left(\frac{1}{2}b \int \frac{x^m}{(a+bx)^{3/2}} dx \right) + m \int \frac{x^{-1+m}}{\sqrt{a+bx}} dx \\
&= -\left(\frac{1}{2} \left(bx^m \left(-\frac{bx}{a} \right)^{-m} \right) \int \frac{\left(-\frac{bx}{a} \right)^m}{(a+bx)^{3/2}} dx \right) - \frac{\left(bmx^m \left(-\frac{bx}{a} \right)^{-m} \right) \int \frac{\left(-\frac{bx}{a} \right)^{-1+m}}{\sqrt{a+bx}} dx}{a} \\
&= \frac{x^m \left(-\frac{bx}{a} \right)^{-m} {}_2F_1 \left(-\frac{1}{2}, -m; \frac{1}{2}; 1 + \frac{bx}{a} \right)}{\sqrt{a+bx}} - \frac{2mx^m \left(-\frac{bx}{a} \right)^{-m} \sqrt{a+bx} {}_2F_1 \left(\frac{1}{2}, 1-m; \frac{3}{2}; 1 + \frac{bx}{a} \right)}{a}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 13, normalized size = 1.00

$$\frac{x^m}{\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[-1/2*(b*x^m)/(a + b*x)^(3/2) + (m*x^(-1 + m))/Sqrt[a + b*x],x]

[Out] x^m/Sqrt[a + b*x]

fricas [A] time = 0.52, size = 11, normalized size = 0.85

$$\frac{x^m}{\sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-1/2*b*x^m/(b*x+a)^(3/2)+m*x^(-1+m)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] x^m/sqrt(b*x + a)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{mx^{m-1}}{\sqrt{bx+a}} - \frac{bx^m}{2(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-1/2*b*x^m/(b*x+a)^(3/2)+m*x^(-1+m)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] integrate($m*x^{(m-1)}/\sqrt{b*x+a} - 1/2*b*x^m/(b*x+a)^{(3/2)}$, x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int -\frac{b x^m}{2(bx+a)^{\frac{3}{2}}} + \frac{m x^{m-1}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int($-1/2*b*x^m/(b*x+a)^{(3/2)}+m*x^{(-1+m)}/(b*x+a)^{(1/2)}$, x)

[Out] int($-1/2*b*x^m/(b*x+a)^{(3/2)}+m*x^{(-1+m)}/(b*x+a)^{(1/2)}$, x)

maxima [A] time = 1.86, size = 11, normalized size = 0.85

$$\frac{x^m}{\sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate($-1/2*b*x^m/(b*x+a)^{(3/2)}+m*x^{(-1+m)}/(b*x+a)^{(1/2)}$, x, algorithm="maxima")

[Out] $x^m/\sqrt{b*x+a}$

mupad [F] time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{m x^{m-1}}{\sqrt{a+bx}} - \frac{b x^m}{2(a+bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int($(m*x^{(m-1)})/(a+b*x)^{(1/2)} - (b*x^m)/(2*(a+b*x)^{(3/2)}$, x)

[Out] int($(m*x^{(m-1)})/(a+b*x)^{(1/2)} - (b*x^m)/(2*(a+b*x)^{(3/2)}$, x)

sympy [C] time = 5.34, size = 73, normalized size = 5.62

$$\frac{m x^m \Gamma(m) {}_2F_1\left(\frac{1}{2}, m \left| \frac{b x e^{i\pi}}{a} \right. \right)}{\sqrt{a} \Gamma(m+1)} - \frac{b x x^m \Gamma(m+1) {}_2F_1\left(\frac{3}{2}, m+1 \left| \frac{b x e^{i\pi}}{a} \right. \right)}{2 a^{\frac{3}{2}} \Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate($-1/2*b*x**m/(b*x+a)**(3/2)+m*x**(-1+m)/(b*x+a)**(1/2)$, x)

```
[Out] m*x**m*gamma(m)*hyper((1/2, m), (m + 1,), b*x*exp_polar(I*pi)/a)/(sqrt(a)*g  
amma(m + 1)) - b*x*x**m*gamma(m + 1)*hyper((3/2, m + 1), (m + 2,), b*x*exp_  
polar(I*pi)/a)/(2*a**(3/2)*gamma(m + 2))
```

$$3.370 \quad \int x^{\frac{1-n}{2} + \frac{1}{2}(-3+n)} \frac{dx}{\sqrt{a+bx}}$$

Optimal. Leaf size=23

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

[Out] $-2*\operatorname{arctanh}((b*x+a)^{(1/2)}/a^{(1/2)})/a^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 29, $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$, Rules used = {7, 63, 208}

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{((1-n)/2 + (-3+n)/2)}/\operatorname{Sqrt}[a + b*x], x]$

[Out] $(-2*\operatorname{ArcTanh}[\operatorname{Sqrt}[a + b*x]/\operatorname{Sqrt}[a]])/\operatorname{Sqrt}[a]$

Rule 7

$\operatorname{Int}[(u_.)*(Px_.)^{(p_)}, x_Symbol] \rightarrow \operatorname{Int}[u*Px^{\operatorname{Simplify}[p]}, x] /; \operatorname{PolyQ}[Px, x] \&\& \operatorname{!RationalQ}[p] \&\& \operatorname{FreeQ}[p, x] \&\& \operatorname{RationalQ}[\operatorname{Simplify}[p]]$

Rule 63

$\operatorname{Int}[(a_.) + (b_.)*(x_.)^{(m_)}*((c_.) + (d_.)*(x_.)^{(n_)}), x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /; \operatorname{FreeQ}\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 208

$\operatorname{Int}[(a_.) + (b_.)*(x_.)^2)^{-1}, x_Symbol] \rightarrow \operatorname{Simp}[(\operatorname{Rt}[-(a/b), 2]*\operatorname{ArcTanh}[x/\operatorname{Rt}[-(a/b), 2]])/a, x] /; \operatorname{FreeQ}\{a, b\}, x] \&\& \operatorname{NegQ}[a/b]$

Rubi steps

$$\begin{aligned}
\int x^{\frac{1-n}{2} + \frac{1}{2}(-3+n)} \frac{1}{\sqrt{a+bx}} dx &= \int \frac{1}{x\sqrt{a+bx}} dx \\
&= \frac{2 \operatorname{Subst}\left(\int \frac{1}{\frac{-a}{b} + \frac{x^2}{b}} dx, x, \sqrt{a+bx}\right)}{b} \\
&= -\frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}
\end{aligned}$$

Mathematica [A] time = 0.00, size = 23, normalized size = 1.00

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(((1 - n)/2 + (-3 + n)/2)/Sqrt[a + b*x], x]

[Out] (-2*ArcTanh[Sqrt[a + b*x]/Sqrt[a]])/Sqrt[a]

fricas [A] time = 0.46, size = 56, normalized size = 2.43

$$\left[\frac{\log\left(\frac{bx-2\sqrt{bx+a}\sqrt{a+2a}}{x}\right)}{\sqrt{a}}, \frac{2\sqrt{-a}\arctan\left(\frac{\sqrt{bx+a}\sqrt{-a}}{a}\right)}{a} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [log((b*x - 2*sqrt(b*x + a)*sqrt(a) + 2*a)/x)/sqrt(a), 2*sqrt(-a)*arctan(sqrt(b*x + a)*sqrt(-a)/a)/a]

giac [A] time = 0.85, size = 21, normalized size = 0.91

$$\frac{2 \arctan\left(\frac{\sqrt{bx+a}}{\sqrt{-a}}\right)}{\sqrt{-a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(1/2),x, algorithm="giac")

[Out] 2*arctan(sqrt(b*x + a)/sqrt(-a))/sqrt(-a)

maple [A] time = 0.00, size = 18, normalized size = 0.78

$$\frac{2 \operatorname{arctanh}\left(\frac{\sqrt{bx+a}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a)^(1/2),x)

[Out] -2*arctanh((b*x+a)^(1/2)/a^(1/2))/a^(1/2)

maxima [A] time = 2.99, size = 32, normalized size = 1.39

$$\frac{\log\left(\frac{\sqrt{bx+a}-\sqrt{a}}{\sqrt{bx+a}+\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] log((sqrt(b*x + a) - sqrt(a))/(sqrt(b*x + a) + sqrt(a)))/sqrt(a)

mupad [B] time = 0.00, size = 17, normalized size = 0.74

$$\frac{2 \operatorname{atanh}\left(\frac{\sqrt{a+bx}}{\sqrt{a}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(a + b*x)^(1/2)),x)

[Out] -(2*atanh((a + b*x)^(1/2)/a^(1/2)))/a^(1/2)

sympy [A] time = 1.09, size = 24, normalized size = 1.04

$$\frac{2 \operatorname{asinh}\left(\frac{\sqrt{a}}{\sqrt{b} \sqrt{x}}\right)}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)**(1/2),x)

[Out] -2*asinh(sqrt(a)/(sqrt(b)*sqrt(x)))/sqrt(a)

3.371 $\int x^3 \sqrt[3]{a + bx} dx$

Optimal. Leaf size=72

$$-\frac{3a^3(a+bx)^{4/3}}{4b^4} + \frac{9a^2(a+bx)^{7/3}}{7b^4} + \frac{3(a+bx)^{13/3}}{13b^4} - \frac{9a(a+bx)^{10/3}}{10b^4}$$

[Out] $-3/4*a^3*(b*x+a)^{(4/3)}/b^4+9/7*a^2*(b*x+a)^{(7/3)}/b^4-9/10*a*(b*x+a)^{(10/3)}/b^4+3/13*(b*x+a)^{(13/3)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9a^2(a+bx)^{7/3}}{7b^4} - \frac{3a^3(a+bx)^{4/3}}{4b^4} + \frac{3(a+bx)^{13/3}}{13b^4} - \frac{9a(a+bx)^{10/3}}{10b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^(1/3), x]

[Out] $(-3*a^3*(a + b*x)^{(4/3)})/(4*b^4) + (9*a^2*(a + b*x)^{(7/3)})/(7*b^4) - (9*a*(a + b*x)^{(10/3)})/(10*b^4) + (3*(a + b*x)^{(13/3)})/(13*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3 \sqrt[3]{a + bx} dx &= \int \left(-\frac{a^3 \sqrt[3]{a + bx}}{b^3} + \frac{3a^2(a + bx)^{4/3}}{b^3} - \frac{3a(a + bx)^{7/3}}{b^3} + \frac{(a + bx)^{10/3}}{b^3} \right) dx \\ &= -\frac{3a^3(a + bx)^{4/3}}{4b^4} + \frac{9a^2(a + bx)^{7/3}}{7b^4} - \frac{9a(a + bx)^{10/3}}{10b^4} + \frac{3(a + bx)^{13/3}}{13b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.64

$$\frac{3(a + bx)^{4/3} (-81a^3 + 108a^2bx - 126ab^2x^2 + 140b^3x^3)}{1820b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^(1/3),x]

[Out] (3*(a + b*x)^(4/3)*(-81*a^3 + 108*a^2*b*x - 126*a*b^2*x^2 + 140*b^3*x^3))/(1820*b^4)

fricas [A] time = 0.45, size = 53, normalized size = 0.74

$$\frac{3 \left(140 b^4 x^4 + 14 a b^3 x^3 - 18 a^2 b^2 x^2 + 27 a^3 b x - 81 a^4 \right) (b x + a)^{\frac{1}{3}}}{1820 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(1/3),x, algorithm="fricas")

[Out] 3/1820*(140*b^4*x^4 + 14*a*b^3*x^3 - 18*a^2*b^2*x^2 + 27*a^3*b*x - 81*a^4)*(b*x + a)^(1/3)/b^4

giac [B] time = 0.87, size = 117, normalized size = 1.62

$$\frac{3 \left(\frac{13 \left(14 (b x + a)^{\frac{10}{3}} - 60 (b x + a)^{\frac{7}{3}} a + 105 (b x + a)^{\frac{4}{3}} a^2 - 140 (b x + a)^{\frac{1}{3}} a^3 \right) a}{b^3} + \frac{4 \left(35 (b x + a)^{\frac{13}{3}} - 182 (b x + a)^{\frac{10}{3}} a + 390 (b x + a)^{\frac{7}{3}} a^2 - 455 (b x + a)^{\frac{4}{3}} a^3 + 455 (b x + a)^{\frac{1}{3}} a^4 \right)}{b^3} \right)}{1820 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(1/3),x, algorithm="giac")

[Out] 3/1820*(13*(14*(b*x + a)^(10/3) - 60*(b*x + a)^(7/3)*a + 105*(b*x + a)^(4/3)*a^2 - 140*(b*x + a)^(1/3)*a^3)*a/b^3 + 4*(35*(b*x + a)^(13/3) - 182*(b*x + a)^(10/3)*a + 390*(b*x + a)^(7/3)*a^2 - 455*(b*x + a)^(4/3)*a^3 + 455*(b*x + a)^(1/3)*a^4)/b^3)/b

maple [A] time = 0.00, size = 43, normalized size = 0.60

$$\frac{3 (b x + a)^{\frac{4}{3}} \left(-140 b^3 x^3 + 126 a b^2 x^2 - 108 a^2 b x + 81 a^3 \right)}{1820 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^(1/3),x)

[Out] -3/1820*(b*x+a)^(4/3)*(-140*b^3*x^3+126*a*b^2*x^2-108*a^2*b*x+81*a^3)/b^4

maxima [A] time = 1.39, size = 56, normalized size = 0.78

$$\frac{3(bx+a)^{\frac{13}{3}}}{13b^4} - \frac{9(bx+a)^{\frac{10}{3}}a}{10b^4} + \frac{9(bx+a)^{\frac{7}{3}}a^2}{7b^4} - \frac{3(bx+a)^{\frac{4}{3}}a^3}{4b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(1/3),x, algorithm="maxima")

[Out] 3/13*(b*x + a)^(13/3)/b^4 - 9/10*(b*x + a)^(10/3)*a/b^4 + 9/7*(b*x + a)^(7/3)*a^2/b^4 - 3/4*(b*x + a)^(4/3)*a^3/b^4

mupad [B] time = 0.05, size = 56, normalized size = 0.78

$$\frac{3(a+bx)^{13/3}}{13b^4} - \frac{3a^3(a+bx)^{4/3}}{4b^4} + \frac{9a^2(a+bx)^{7/3}}{7b^4} - \frac{9a(a+bx)^{10/3}}{10b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(a + b*x)^(1/3),x)

[Out] (3*(a + b*x)^(13/3))/(13*b^4) - (3*a^3*(a + b*x)^(4/3))/(4*b^4) + (9*a^2*(a + b*x)^(7/3))/(7*b^4) - (9*a*(a + b*x)^(10/3))/(10*b^4)

sympy [B] time = 2.83, size = 1742, normalized size = 24.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**(1/3),x)

[Out] -243*a**(73/3)*(1 + b*x/a)**(1/3)/(1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6) + 243*a**(73/3)/(1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6) - 1377*a**(70/3)*b*x*(1 + b*x/a)**(1/3)/(1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6) + 1458*a**(70/3)*b*x/(1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6) - 3213*a**(67/3)*b**2*x**2*(1 + b*x/a)**(1/3)/(1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6) + 3645*a**(67/3)*b**2*x**2/(1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a

$$\begin{aligned}
& **17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14 \\
& *b**10*x**6) - 3927*a**(64/3)*b**3*x**3*(1 + b*x/a)**(1/3)/(1820*a**20*b**4 \\
& + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + 273 \\
& 00*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6) + 4860* \\
& a**(64/3)*b**3*x**3/(1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b** \\
& 6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x \\
& **5 + 1820*a**14*b**10*x**6) - 2163*a**(61/3)*b**4*x**4*(1 + b*x/a)**(1/3)/ \\
& (1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17 \\
& *b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b** \\
& 10*x**6) + 3645*a**(61/3)*b**4*x**4/(1820*a**20*b**4 + 10920*a**19*b**5*x + \\
& 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10 \\
& 920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6) + 1827*a**(58/3)*b**5*x**5*(1 \\
& + b*x/a)**(1/3)/(1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x \\
& *2 + 36400*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 \\
& + 1820*a**14*b**10*x**6) + 1458*a**(58/3)*b**5*x**5/(1820*a**20*b**4 + 1092 \\
& 0*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**1 \\
& 6*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6) + 6573*a**(55/ \\
& 3)*b**6*x**6*(1 + b*x/a)**(1/3)/(1820*a**20*b**4 + 10920*a**19*b**5*x + 273 \\
& 00*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920* \\
& a**15*b**9*x**5 + 1820*a**14*b**10*x**6) + 243*a**(55/3)*b**6*x**6/(1820*a \\
& *20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x \\
& *3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6) \\
& + 8787*a**(52/3)*b**7*x**7*(1 + b*x/a)**(1/3)/(1820*a**20*b**4 + 10920*a** \\
& 19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**16*b** \\
& 8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6) + 6498*a**(49/3)*b \\
& *8*x**8*(1 + b*x/a)**(1/3)/(1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a \\
& *18*b**6*x**2 + 36400*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15 \\
& *b**9*x**5 + 1820*a**14*b**10*x**6) + 2562*a**(46/3)*b**9*x**9*(1 + b*x/a)* \\
& *(1/3)/(1820*a**20*b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 3640 \\
& 0*a**17*b**7*x**3 + 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a \\
& *14*b**10*x**6) + 420*a**(43/3)*b**10*x**10*(1 + b*x/a)**(1/3)/(1820*a**20* \\
& b**4 + 10920*a**19*b**5*x + 27300*a**18*b**6*x**2 + 36400*a**17*b**7*x**3 + \\
& 27300*a**16*b**8*x**4 + 10920*a**15*b**9*x**5 + 1820*a**14*b**10*x**6)
\end{aligned}$$

3.372 $\int x^2 \sqrt[3]{a + bx} dx$

Optimal. Leaf size=53

$$\frac{3a^2(a + bx)^{4/3}}{4b^3} + \frac{3(a + bx)^{10/3}}{10b^3} - \frac{6a(a + bx)^{7/3}}{7b^3}$$

[Out] $3/4*a^2*(b*x+a)^{(4/3)}/b^3-6/7*a*(b*x+a)^{(7/3)}/b^3+3/10*(b*x+a)^{(10/3)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3a^2(a + bx)^{4/3}}{4b^3} + \frac{3(a + bx)^{10/3}}{10b^3} - \frac{6a(a + bx)^{7/3}}{7b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*x)^(1/3), x]

[Out] $(3*a^2*(a + b*x)^{(4/3)})/(4*b^3) - (6*a*(a + b*x)^{(7/3)})/(7*b^3) + (3*(a + b*x)^{(10/3)})/(10*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2 \sqrt[3]{a + bx} dx &= \int \left(\frac{a^2 \sqrt[3]{a + bx}}{b^2} - \frac{2a(a + bx)^{4/3}}{b^2} + \frac{(a + bx)^{7/3}}{b^2} \right) dx \\ &= \frac{3a^2(a + bx)^{4/3}}{4b^3} - \frac{6a(a + bx)^{7/3}}{7b^3} + \frac{3(a + bx)^{10/3}}{10b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.66

$$\frac{3(a + bx)^{4/3} (9a^2 - 12abx + 14b^2x^2)}{140b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^(1/3),x]

[Out] (3*(a + b*x)^(4/3)*(9*a^2 - 12*a*b*x + 14*b^2*x^2))/(140*b^3)

fricas [A] time = 0.48, size = 42, normalized size = 0.79

$$\frac{3(14b^3x^3 + 2ab^2x^2 - 3a^2bx + 9a^3)(bx + a)^{\frac{1}{3}}}{140b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(1/3),x, algorithm="fricas")

[Out] 3/140*(14*b^3*x^3 + 2*a*b^2*x^2 - 3*a^2*b*x + 9*a^3)*(b*x + a)^(1/3)/b^3

giac [B] time = 0.83, size = 92, normalized size = 1.74

$$\frac{3\left(\frac{10\left(2(bx+a)^{\frac{7}{3}}-7(bx+a)^{\frac{4}{3}}a+14(bx+a)^{\frac{1}{3}}a^2\right)a}{b^2} + \frac{14(bx+a)^{\frac{10}{3}}-60(bx+a)^{\frac{7}{3}}a+105(bx+a)^{\frac{4}{3}}a^2-140(bx+a)^{\frac{1}{3}}a^3}{b^2}\right)}{140b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(1/3),x, algorithm="giac")

[Out] 3/140*(10*(2*(b*x + a)^(7/3) - 7*(b*x + a)^(4/3)*a + 14*(b*x + a)^(1/3)*a^2)*a/b^2 + (14*(b*x + a)^(10/3) - 60*(b*x + a)^(7/3)*a + 105*(b*x + a)^(4/3)*a^2 - 140*(b*x + a)^(1/3)*a^3)/b^2)/b

maple [A] time = 0.01, size = 32, normalized size = 0.60

$$\frac{3(bx + a)^{\frac{4}{3}}(14b^2x^2 - 12abx + 9a^2)}{140b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^(1/3),x)

[Out] 3/140*(b*x+a)^(4/3)*(14*b^2*x^2-12*a*b*x+9*a^2)/b^3

maxima [A] time = 1.30, size = 41, normalized size = 0.77

$$\frac{3(bx + a)^{\frac{10}{3}}}{10b^3} - \frac{6(bx + a)^{\frac{7}{3}}a}{7b^3} + \frac{3(bx + a)^{\frac{4}{3}}a^2}{4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(1/3),x, algorithm="maxima")

[Out] $\frac{3}{10}(b*x + a)^{(10/3)}/b^3 - \frac{6}{7}(b*x + a)^{(7/3)}*a/b^3 + \frac{3}{4}(b*x + a)^{(4/3)}*a^2/b^3$

mupad [B] time = 0.04, size = 37, normalized size = 0.70

$$\frac{42(a+bx)^{10/3} - 120a(a+bx)^{7/3} + 105a^2(a+bx)^{4/3}}{140b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a + b*x)^(1/3),x)

[Out] $\frac{(42*(a + b*x)^{(10/3)} - 120*a*(a + b*x)^{(7/3)} + 105*a^2*(a + b*x)^{(4/3)})}{(140*b^3)}$

sympy [B] time = 1.86, size = 666, normalized size = 12.57

$$\frac{27a^{\frac{34}{3}} \sqrt[3]{1 + \frac{bx}{a}}}{140a^8b^3 + 420a^7b^4x + 420a^6b^5x^2 + 140a^5b^6x^3} - \frac{27a^{\frac{34}{3}}}{140a^8b^3 + 420a^7b^4x + 420a^6b^5x^2 + 140a^5b^6x^3} + \frac{7}{140a^8b^3 + 420a^7b^4x + 420a^6b^5x^2 + 140a^5b^6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)**(1/3),x)

[Out] $27*a^{(34/3)}*(1 + b*x/a)^{(1/3)}/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3}) - 27*a^{(34/3)}/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3}) + 72*a^{(31/3)}*b*x*(1 + b*x/a)^{(1/3)}/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3}) - 81*a^{(31/3)}*b*x/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3}) + 60*a^{(28/3)}*b^{**2}*x^{**2}*(1 + b*x/a)^{(1/3)}/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3}) - 81*a^{(28/3)}*b^{**2}*x^{**2}/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3}) + 60*a^{(25/3)}*b^{**3}*x^{**3}*(1 + b*x/a)^{(1/3)}/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3}) - 27*a^{(25/3)}*b^{**3}*x^{**3}/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3}) + 135*a^{(22/3)}*b^{**4}*x^{**4}*(1 + b*x/a)^{(1/3)}/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3}) + 132*a^{(19/3)}*b^{**5}*x^{**5}*(1 + b*x/a)^{(1/3)}/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3}) + 42*a^{(16/3)}*b^{**6}*x^{**6}*(1 + b*x/a)^{(1/3)}/(140*a^{**8}*b^{**3} + 420*a^{**7}*b^{**4}*x + 420*a^{**6}*b^{**5}*x^{**2} + 140*a^{**5}*b^{**6}*x^{**3})$

3.373 $\int x \sqrt[3]{a + bx} dx$

Optimal. Leaf size=34

$$\frac{3(a + bx)^{7/3}}{7b^2} - \frac{3a(a + bx)^{4/3}}{4b^2}$$

[Out] $-3/4*a*(b*x+a)^{(4/3)}/b^2+3/7*(b*x+a)^{(7/3)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3(a + bx)^{7/3}}{7b^2} - \frac{3a(a + bx)^{4/3}}{4b^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*(a + b*x)^{(1/3)}, x]$

[Out] $(-3*a*(a + b*x)^{(4/3)})/(4*b^2) + (3*(a + b*x)^{(7/3)})/(7*b^2)$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (\ !\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0]) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x \sqrt[3]{a + bx} dx &= \int \left(-\frac{a \sqrt[3]{a + bx}}{b} + \frac{(a + bx)^{4/3}}{b} \right) dx \\ &= -\frac{3a(a + bx)^{4/3}}{4b^2} + \frac{3(a + bx)^{7/3}}{7b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.71

$$\frac{3(a + bx)^{4/3}(4bx - 3a)}{28b^2}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x*(a + b*x)^{(1/3)}, x]$

[Out] $(3*(a + b*x)^{(4/3)}*(-3*a + 4*b*x))/(28*b^2)$

fricas [A] time = 0.49, size = 30, normalized size = 0.88

$$\frac{3(4b^2x^2 + abx - 3a^2)(bx + a)^{\frac{1}{3}}}{28b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(1/3),x, algorithm="fricas")`

[Out] $3/28*(4*b^2*x^2 + a*b*x - 3*a^2)*(b*x + a)^{(1/3)}/b^2$

giac [B] time = 1.04, size = 67, normalized size = 1.97

$$3 \left(\frac{7 \left((bx+a)^{\frac{4}{3}} - 4(bx+a)^{\frac{1}{3}}a \right) a}{b} + \frac{2 \left(2(bx+a)^{\frac{7}{3}} - 7(bx+a)^{\frac{4}{3}}a + 14(bx+a)^{\frac{1}{3}}a^2 \right)}{b} \right) / 28b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(1/3),x, algorithm="giac")`

[Out] $3/28*(7*((b*x + a)^{(4/3)} - 4*(b*x + a)^{(1/3)}*a)*a/b + 2*(2*(b*x + a)^{(7/3)} - 7*(b*x + a)^{(4/3)}*a + 14*(b*x + a)^{(1/3)}*a^2)/b)/b$

maple [A] time = 0.00, size = 21, normalized size = 0.62

$$\frac{3(bx + a)^{\frac{4}{3}}(-4bx + 3a)}{28b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)^(1/3),x)`

[Out] $-3/28*(b*x+a)^{(4/3)}*(-4*b*x+3*a)/b^2$

maxima [A] time = 1.29, size = 26, normalized size = 0.76

$$\frac{3(bx + a)^{\frac{7}{3}}}{7b^2} - \frac{3(bx + a)^{\frac{4}{3}}a}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(1/3),x, algorithm="maxima")`

[Out] $3/7*(b*x + a)^{(7/3)}/b^2 - 3/4*(b*x + a)^{(4/3)}*a/b^2$

mupad [B] time = 0.03, size = 25, normalized size = 0.74

$$\frac{21 a (a + b x)^{4/3} - 12 (a + b x)^{7/3}}{28 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(a + b*x)^(1/3), x)`

[Out] $-(21*a*(a + b*x)^{(4/3)} - 12*(a + b*x)^{(7/3)})/(28*b^2)$

sympy [B] time = 1.20, size = 202, normalized size = 5.94

$$\frac{9a^{\frac{13}{3}}\sqrt[3]{1 + \frac{bx}{a}}}{28a^2b^2 + 28ab^3x} + \frac{9a^{\frac{13}{3}}}{28a^2b^2 + 28ab^3x} - \frac{6a^{\frac{10}{3}}bx\sqrt[3]{1 + \frac{bx}{a}}}{28a^2b^2 + 28ab^3x} + \frac{9a^{\frac{10}{3}}bx}{28a^2b^2 + 28ab^3x} + \frac{15a^{\frac{7}{3}}b^2x^2\sqrt[3]{1 + \frac{bx}{a}}}{28a^2b^2 + 28ab^3x} + \frac{12a^{\frac{4}{3}}b^3x^3\sqrt[3]{1 + \frac{bx}{a}}}{28a^2b^2 + 28ab^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**(1/3), x)`

[Out] $-9*a**(13/3)*(1 + b*x/a)**(1/3)/(28*a**2*b**2 + 28*a*b**3*x) + 9*a**(13/3)/(28*a**2*b**2 + 28*a*b**3*x) - 6*a**(10/3)*b*x*(1 + b*x/a)**(1/3)/(28*a**2*b**2 + 28*a*b**3*x) + 9*a**(10/3)*b*x/(28*a**2*b**2 + 28*a*b**3*x) + 15*a**(7/3)*b**2*x**2*(1 + b*x/a)**(1/3)/(28*a**2*b**2 + 28*a*b**3*x) + 12*a**(4/3)*b**3*x**3*(1 + b*x/a)**(1/3)/(28*a**2*b**2 + 28*a*b**3*x)$

3.374 $\int \sqrt[3]{a + bx} dx$

Optimal. Leaf size=16

$$\frac{3(a + bx)^{4/3}}{4b}$$

[Out] $3/4*(b*x+a)^{(4/3)}/b$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{3(a + bx)^{4/3}}{4b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/3), x]

[Out] (3*(a + b*x)^(4/3))/(4*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \sqrt[3]{a + bx} dx = \frac{3(a + bx)^{4/3}}{4b}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$\frac{3(a + bx)^{4/3}}{4b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/3), x]

[Out] (3*(a + b*x)^(4/3))/(4*b)

fricas [A] time = 0.49, size = 12, normalized size = 0.75

$$\frac{3(bx + a)^{4/3}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/3),x, algorithm="fricas")`

[Out] $3/4*(b*x + a)^{(4/3)}/b$

giac [A] time = 0.89, size = 12, normalized size = 0.75

$$\frac{3 (bx + a)^{\frac{4}{3}}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/3),x, algorithm="giac")`

[Out] $3/4*(b*x + a)^{(4/3)}/b$

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{3 (bx + a)^{\frac{4}{3}}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(1/3),x)`

[Out] $3/4*(b*x+a)^{(4/3)}/b$

maxima [A] time = 1.26, size = 12, normalized size = 0.75

$$\frac{3 (bx + a)^{\frac{4}{3}}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/3),x, algorithm="maxima")`

[Out] $3/4*(b*x + a)^{(4/3)}/b$

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{3 (a + bx)^{\frac{4}{3}}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/3),x)`

[Out] $(3*(a + b*x)^{(4/3)})/(4*b)$

sympy [A] time = 0.07, size = 12, normalized size = 0.75

$$\frac{3(a + bx)^{\frac{4}{3}}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/3),x)`

[Out] $3*(a + b*x)^{(4/3)}/(4*b)$

$$3.375 \quad \int \frac{\sqrt[3]{a+bx}}{x} dx$$

Optimal. Leaf size=91

$$3\sqrt[3]{a+bx} + \frac{3}{2}\sqrt[3]{a} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) - \sqrt{3} \sqrt[3]{a} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3} \sqrt[3]{a}}\right) - \frac{1}{2}\sqrt[3]{a} \log(x)$$

[Out] $3*(b*x+a)^{(1/3)}-1/2*a^{(1/3)}*\ln(x)+3/2*a^{(1/3)}*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})-a^{(1/3)}*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)}*3^{(1/2)})*3^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 91, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {50, 57, 617, 204, 31}

$$3\sqrt[3]{a+bx} + \frac{3}{2}\sqrt[3]{a} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) - \sqrt{3} \sqrt[3]{a} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3} \sqrt[3]{a}}\right) - \frac{1}{2}\sqrt[3]{a} \log(x)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/3)/x, x]

[Out] $3*(a + b*x)^{(1/3)} - \text{Sqrt}[3]*a^{(1/3)}*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})] - (a^{(1/3)}*\text{Log}[x])/2 + (3*a^{(1/3)}*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)})]/2$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 50

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 57

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2), x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)]], x, (c + d*x)^(1/3))]

3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x
)] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt[3]{a+bx}}{x} dx &= 3\sqrt[3]{a+bx} + a \int \frac{1}{x(a+bx)^{2/3}} dx \\ &= 3\sqrt[3]{a+bx} - \frac{1}{2}\sqrt[3]{a} \log(x) - \frac{1}{2}(3\sqrt[3]{a}) \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a}-x} dx, x, \sqrt[3]{a+bx}\right) - \frac{1}{2}(3a^{2/3}) \operatorname{Subst}\left(\int \frac{1}{a-x^2} dx, x, \sqrt[3]{a+bx}\right) \\ &= 3\sqrt[3]{a+bx} - \frac{1}{2}\sqrt[3]{a} \log(x) + \frac{3}{2}\sqrt[3]{a} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) + (3\sqrt[3]{a}) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}\right) \\ &= 3\sqrt[3]{a+bx} - \sqrt{3}\sqrt[3]{a} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right) - \frac{1}{2}\sqrt[3]{a} \log(x) + \frac{3}{2}\sqrt[3]{a} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) \end{aligned}$$

Mathematica [A] time = 0.05, size = 113, normalized size = 1.24

$$-\frac{1}{2}\sqrt[3]{a} \log\left(a^{2/3} + \sqrt[3]{a}\sqrt[3]{a+bx} + (a+bx)^{2/3}\right) + 3\sqrt[3]{a+bx} + \sqrt[3]{a} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) - \sqrt{3}\sqrt[3]{a} \tan^{-1}\left(\frac{\frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}} + 1}{\sqrt{3}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/3)/x, x]

[Out] $3*(a + b*x)^{(1/3)} - \text{Sqrt}[3]*a^{(1/3)}*\text{ArcTan}[(1 + (2*(a + b*x)^{(1/3}))/a^{(1/3)})/\text{Sqrt}[3]] + a^{(1/3)}*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}] - (a^{(1/3)}*\text{Log}[a^{(2/3)} + a^{(1/3)}*(a + b*x)^{(1/3)} + (a + b*x)^{(2/3)}])/2$

fricas [A] time = 0.49, size = 91, normalized size = 1.00

$$-\sqrt{3} a^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}(bx+a)^{\frac{1}{3}}a^{\frac{2}{3}} + \sqrt{3}a}{3a}\right) - \frac{1}{2} a^{\frac{1}{3}} \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right) + a^{\frac{1}{3}} \log\left((bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right) + 3(bx+a)^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/3)/x,x, algorithm="fricas")`

[Out] $-\text{sqrt}(3)*a^{(1/3)}*\arctan(1/3*(2*\text{sqrt}(3)*(b*x + a)^{(1/3)}*a^{(2/3)} + \text{sqrt}(3)*a)/a) - 1/2*a^{(1/3)}*\log((b*x + a)^{(2/3)} + (b*x + a)^{(1/3)}*a^{(1/3)} + a^{(2/3)}) + a^{(1/3)}*\log((b*x + a)^{(1/3)} - a^{(1/3)}) + 3*(b*x + a)^{(1/3)}$

giac [A] time = 2.37, size = 87, normalized size = 0.96

$$-\sqrt{3} a^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}} + a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right) - \frac{1}{2} a^{\frac{1}{3}} \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right) + a^{\frac{1}{3}} \log\left(\left|(bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right) + 3(bx+a)^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/3)/x,x, algorithm="giac")`

[Out] $-\text{sqrt}(3)*a^{(1/3)}*\arctan(1/3*\text{sqrt}(3)*(2*(b*x + a)^{(1/3)} + a^{(1/3)})/a^{(1/3)}) - 1/2*a^{(1/3)}*\log((b*x + a)^{(2/3)} + (b*x + a)^{(1/3)}*a^{(1/3)} + a^{(2/3)}) + a^{(1/3)}*\log(\text{abs}((b*x + a)^{(1/3)} - a^{(1/3)})) + 3*(b*x + a)^{(1/3)}$

maple [A] time = 0.01, size = 85, normalized size = 0.93

$$-\sqrt{3} a^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}} + 1\right)}{3}\right) + a^{\frac{1}{3}} \ln\left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}\right) - \frac{a^{\frac{1}{3}} \ln\left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}}\right)}{2} + 3(bx+a)^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(1/3)/x,x)`

[Out] $3*(b*x+a)^{(1/3)}+a^{(1/3)}*\ln((b*x+a)^{(1/3)}-a^{(1/3)})-1/2*a^{(1/3)}*\ln((b*x+a)^{(2/3)}+a^{(1/3)}*(b*x+a)^{(1/3)}+a^{(2/3)})-a^{(1/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2/a^{(1/3)}*(b*x+a)^{(1/3)}+1))$

maxima [A] time = 3.08, size = 86, normalized size = 0.95

$$-\sqrt{3} a^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right) - \frac{1}{2} a^{\frac{1}{3}} \log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right) + a^{\frac{1}{3}} \log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right) + 3(bx+a)^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/x,x, algorithm="maxima")

[Out] -sqrt(3)*a^(1/3)*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3)) - 1/2*a^(1/3)*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + a^(1/3)*log((b*x + a)^(1/3) - a^(1/3)) + 3*(b*x + a)^(1/3)

mupad [B] time = 0.12, size = 107, normalized size = 1.18

$$a^{1/3} \ln\left(9a(a+bx)^{1/3} - 9a^{4/3}\right) + 3(a+bx)^{1/3} + \frac{a^{1/3} \ln\left(9a(a+bx)^{1/3} - \frac{9a^{4/3}(-1+\sqrt{3}i)}{2}\right) (-1+\sqrt{3}i)}{2} - \frac{a^{1/3} \ln\left(9a(a+bx)^{1/3} - 9a^{4/3}\right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/3)/x,x)

[Out] a^(1/3)*log(9*a*(a + b*x)^(1/3) - 9*a^(4/3)) + 3*(a + b*x)^(1/3) + (a^(1/3)*log(9*a*(a + b*x)^(1/3) - (9*a^(4/3)*(3^(1/2)*1i - 1))/2)*(3^(1/2)*1i - 1))/2 - (a^(1/3)*log(9*a*(a + b*x)^(1/3) + (9*a^(4/3)*(3^(1/2)*1i + 1))/2)*(3^(1/2)*1i + 1))/2

sympy [C] time = 2.02, size = 180, normalized size = 1.98

$$\frac{4\sqrt[3]{a} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{4}{3}\right)}{3\Gamma\left(\frac{7}{3}\right)} + \frac{4\sqrt[3]{a} e^{-\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x} e^{\frac{2i\pi}{3}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{4}{3}\right)}{3\Gamma\left(\frac{7}{3}\right)} + \frac{4\sqrt[3]{a} e^{\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x} e^{\frac{4i\pi}{3}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{4}{3}\right)}{3\Gamma\left(\frac{7}{3}\right)} + \frac{4\sqrt[3]{a} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{4}{3}\right)}{3\Gamma\left(\frac{7}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/3)/x,x)

[Out] 4*a**(1/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(4/3)/(3*gamma(7/3)) + 4*a**(1/3)*exp(-2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(2*I*pi/3)/a**(1/3))*gamma(4/3)/(3*gamma(7/3)) + 4*a**(1/3)*exp(2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(4*I*pi/3)/a**(1/3))*gamma(4/3)/(3*gamma(7/3)) + 4*b**(1/3)*(a/b + x)**(1/3)*gamma(4/3)/gamma(7/3)

$$3.376 \quad \int \frac{\sqrt[3]{a+bx}}{x^2} dx$$

Optimal. Leaf size=97

$$-\frac{b \log(x)}{6a^{2/3}} + \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{2/3}} - \frac{b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{2/3}} - \frac{\sqrt[3]{a+bx}}{x}$$

[Out] $-(b*x+a)^{(1/3)}/x-1/6*b*\ln(x)/a^{(2/3)}+1/2*b*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(2/3)}$
 $-1/3*b*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}})/a^{(2/3)*3^{(1/2)}}$

Rubi [A] time = 0.03, antiderivative size = 97, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {47, 57, 617, 204, 31}

$$-\frac{b \log(x)}{6a^{2/3}} + \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{2/3}} - \frac{b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{2/3}} - \frac{\sqrt[3]{a+bx}}{x}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/3)/x^2,x]

[Out] $-((a + b*x)^{(1/3)}/x) - (b*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/(\text{Sqrt}[3]*a^{(2/3)}) - (b*\text{Log}[x])/((6*a^{(2/3)}) + (b*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}])/(2*a^{(2/3)}))$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 57

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2),
x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x
])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt[3]{a+bx}}{x^2} dx &= -\frac{\sqrt[3]{a+bx}}{x} + \frac{1}{3}b \int \frac{1}{x(a+bx)^{2/3}} dx \\ &= -\frac{\sqrt[3]{a+bx}}{x} - \frac{b \log(x)}{6a^{2/3}} - \frac{b \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a}-x} dx, x, \sqrt[3]{a+bx}\right)}{2a^{2/3}} - \frac{b \operatorname{Subst}\left(\int \frac{1}{a^{2/3}+\sqrt[3]{a}x+x^2} dx, x, \sqrt[3]{a+bx}\right)}{2\sqrt[3]{a}} \\ &= -\frac{\sqrt[3]{a+bx}}{x} - \frac{b \log(x)}{6a^{2/3}} + \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{2/3}} + \frac{b \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}\right)}{a^{2/3}} \\ &= -\frac{\sqrt[3]{a+bx}}{x} - \frac{b \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3} a^{2/3}} - \frac{b \log(x)}{6a^{2/3}} + \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{2/3}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.34

$$\frac{3b(a+bx)^{4/3} {}_2F_1\left(\frac{4}{3}, 2; \frac{7}{3}; \frac{bx}{a} + 1\right)}{4a^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/3)/x^2,x]

[Out] (3*b*(a + b*x)^(4/3)*Hypergeometric2F1[4/3, 2, 7/3, 1 + (b*x)/a])/(4*a^2)

fricas [A] time = 0.46, size = 139, normalized size = 1.43

$$\frac{2\sqrt{3}(a^2)^{\frac{1}{6}}abx \arctan\left(\frac{(a^2)^{\frac{1}{6}}\left(\sqrt{3}(a^2)^{\frac{1}{3}}a + 2\sqrt{3}(a^2)^{\frac{2}{3}}(bx+a)^{\frac{1}{3}}\right)}{3a^2}\right) + (a^2)^{\frac{2}{3}}bx \log\left((bx+a)^{\frac{2}{3}}a + (a^2)^{\frac{1}{3}}a + (a^2)^{\frac{2}{3}}(bx+a)^{\frac{1}{3}}\right)}{6a^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/x^2,x, algorithm="fricas")

[Out] -1/6*(2*sqrt(3)*(a^2)^(1/6)*a*b*x*arctan(1/3*(a^2)^(1/6)*(sqrt(3)*(a^2)^(1/3)*a + 2*sqrt(3)*(a^2)^(2/3)*(b*x + a)^(1/3))/a^2) + (a^2)^(2/3)*b*x*log((b*x + a)^(2/3)*a + (a^2)^(1/3)*a + (a^2)^(2/3)*(b*x + a)^(1/3)) - 2*(a^2)^(2/3)*b*x*log((b*x + a)^(1/3)*a - (a^2)^(2/3)) + 6*(b*x + a)^(1/3)*a^2/(a^2*x)

giac [A] time = 2.55, size = 105, normalized size = 1.08

$$\frac{2\sqrt{3}b^2 \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{\frac{2}{a^{\frac{2}{3}}}} + \frac{b^2 \log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)}{\frac{2}{a^{\frac{2}{3}}}} - \frac{2b^2 \log\left(\left|(bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right|\right)}{\frac{2}{a^{\frac{2}{3}}}} + \frac{6(bx+a)^{\frac{1}{3}}b}{x}}{6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/x^2,x, algorithm="giac")

[Out] -1/6*(2*sqrt(3)*b^2*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3)))/a^(2/3) + b^2*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(2/3) - 2*b^2*log(abs((b*x + a)^(1/3) - a^(1/3)))/a^(2/3) + 6*(b*x + a)^(1/3)*b/x/b

maple [A] time = 0.01, size = 92, normalized size = 0.95

$$\frac{\sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)}{3a^{\frac{2}{3}}} + \frac{b \ln\left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}\right)}{3a^{\frac{2}{3}}} - \frac{b \ln\left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}}\right)}{6a^{\frac{2}{3}}} - \frac{(bx+a)^{\frac{1}{3}}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x+a)^{(1/3)}/x^2, x)$

[Out] $-(b*x+a)^{(1/3)}/x+1/3*b/a^{(2/3)}*\ln(-a^{(1/3)}+(b*x+a)^{(1/3)})-1/6*b/a^{(2/3)}*\ln(a^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+(b*x+a)^{(2/3)})-1/3*b/a^{(2/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2*(b*x+a)^{(1/3)}/a^{(1/3)}+1))$

maxima [A] time = 2.96, size = 93, normalized size = 0.96

$$\frac{\sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{3a^{\frac{2}{3}}} - \frac{b \log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)}{6a^{\frac{2}{3}}} + \frac{b \log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)}{3a^{\frac{2}{3}}} - \frac{(bx+a)^{\frac{1}{3}}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)^{(1/3)}/x^2, x, \text{algorithm}="maxima")$

[Out] $-1/3*\sqrt{3}*b*\arctan(1/3*\sqrt{3}*(2*(b*x+a)^{(1/3)}+a^{(1/3)})/a^{(1/3)})/a^{(2/3)}-1/6*b*\log((b*x+a)^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+a^{(2/3)})/a^{(2/3)}+1/3*b*\log((b*x+a)^{(1/3)}-a^{(1/3)})/a^{(2/3)}-(b*x+a)^{(1/3)}/x$

mupad [B] time = 0.07, size = 117, normalized size = 1.21

$$\frac{b \ln\left(3b(a+bx)^{1/3}-3a^{1/3}b\right)}{3a^{2/3}} - \frac{(a+bx)^{1/3}}{x} - \frac{\ln\left(\frac{3a^{1/3}(b-\sqrt{3}bi)}{2}+3b(a+bx)^{1/3}\right)(b-\sqrt{3}bi)}{6a^{2/3}} - \frac{\ln\left(\frac{3a^{1/3}(b+\sqrt{3}bi)}{2}+3b(a+bx)^{1/3}\right)(b+\sqrt{3}bi)}{6a^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a+b*x)^{(1/3)}/x^2, x)$

[Out] $(b*\log(3*b*(a+b*x)^{(1/3)}-3*a^{(1/3)}*b))/(3*a^{(2/3)})-(a+b*x)^{(1/3)}/x-(\log((3*a^{(1/3)}*(b-3^{(1/2)}*b*1i))/2+3*b*(a+b*x)^{(1/3)}*(b-3^{(1/2)}*b*1i)))/(6*a^{(2/3)})-(\log((3*a^{(1/3)}*(b+3^{(1/2)}*b*1i))/2+3*b*(a+b*x)^{(1/3)}*(b+3^{(1/2)}*b*1i)))/(6*a^{(2/3)})$

sympy [C] time = 2.19, size = 643, normalized size = 6.63

$$\frac{4a^{\frac{7}{3}}be^{\frac{2i\pi}{3}}\log\left(1-\frac{\sqrt[3]{b}\sqrt[3]{\frac{a}{b}+x}}{\sqrt[3]{a}}\right)\Gamma\left(\frac{4}{3}\right)}{9a^3e^{\frac{2i\pi}{3}}\Gamma\left(\frac{7}{3}\right)-9a^2b\left(\frac{a}{b}+x\right)e^{\frac{2i\pi}{3}}\Gamma\left(\frac{7}{3}\right)} + \frac{4a^{\frac{7}{3}}b\log\left(1-\frac{\sqrt[3]{b}\sqrt[3]{\frac{a}{b}+xe^{\frac{2i\pi}{3}}}}{\sqrt[3]{a}}\right)\Gamma\left(\frac{4}{3}\right)}{9a^3e^{\frac{2i\pi}{3}}\Gamma\left(\frac{7}{3}\right)-9a^2b\left(\frac{a}{b}+x\right)e^{\frac{2i\pi}{3}}\Gamma\left(\frac{7}{3}\right)} + \frac{4a^{\frac{7}{3}}be^{-\frac{2i\pi}{3}}\log\left(1-\frac{\sqrt[3]{b}\sqrt[3]{\frac{a}{b}+xe^{\frac{4i\pi}{3}}}}{\sqrt[3]{a}}\right)\Gamma\left(\frac{4}{3}\right)}{9a^3e^{-\frac{2i\pi}{3}}\Gamma\left(\frac{7}{3}\right)-9a^2b\left(\frac{a}{b}+x\right)e^{-\frac{2i\pi}{3}}\Gamma\left(\frac{7}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/3)/x**2,x)

[Out] $4a^{7/3}b \exp(2I\pi/3) \log(1 - b^{1/3}(a/b + x)^{1/3}/a^{1/3}) \operatorname{gamma}(4/3) / (9a^{3/3} \exp(2I\pi/3) \operatorname{gamma}(7/3) - 9a^{2/3}b(a/b + x) \exp(2I\pi/3) \operatorname{gamma}(7/3)) + 4a^{7/3}b \log(1 - b^{1/3}(a/b + x)^{1/3} \exp_{\text{polar}}(2I\pi/3)/a^{1/3}) \operatorname{gamma}(4/3) / (9a^{3/3} \exp(2I\pi/3) \operatorname{gamma}(7/3) - 9a^{2/3}b(a/b + x) \exp(2I\pi/3) \operatorname{gamma}(7/3)) + 4a^{7/3}b \exp(-2I\pi/3) \log(1 - b^{1/3}(a/b + x)^{1/3} \exp_{\text{polar}}(4I\pi/3)/a^{1/3}) \operatorname{gamma}(4/3) / (9a^{3/3} \exp(2I\pi/3) \operatorname{gamma}(7/3) - 9a^{2/3}b(a/b + x) \exp(2I\pi/3) \operatorname{gamma}(7/3)) - 4a^{4/3}b^2(a/b + x) \exp(2I\pi/3) \log(1 - b^{1/3}(a/b + x)^{1/3}/a^{1/3}) \operatorname{gamma}(4/3) / (9a^{3/3} \exp(2I\pi/3) \operatorname{gamma}(7/3) - 9a^{2/3}b(a/b + x) \exp(2I\pi/3) \operatorname{gamma}(7/3)) - 4a^{4/3}b^2(a/b + x) \log(1 - b^{1/3}(a/b + x)^{1/3} \exp_{\text{polar}}(2I\pi/3)/a^{1/3}) \operatorname{gamma}(4/3) / (9a^{3/3} \exp(2I\pi/3) \operatorname{gamma}(7/3) - 9a^{2/3}b(a/b + x) \exp(2I\pi/3) \operatorname{gamma}(7/3)) - 4a^{4/3}b^2(a/b + x) \exp(-2I\pi/3) \log(1 - b^{1/3}(a/b + x)^{1/3} \exp_{\text{polar}}(4I\pi/3)/a^{1/3}) \operatorname{gamma}(4/3) / (9a^{3/3} \exp(2I\pi/3) \operatorname{gamma}(7/3) - 9a^{2/3}b(a/b + x) \exp(2I\pi/3) \operatorname{gamma}(7/3)) + 12a^{2/3}b^{4/3}(a/b + x)^{1/3} \exp(2I\pi/3) \operatorname{gamma}(4/3) / (9a^{3/3} \exp(2I\pi/3) \operatorname{gamma}(7/3) - 9a^{2/3}b(a/b + x) \exp(2I\pi/3) \operatorname{gamma}(7/3))$

$$3.377 \quad \int \frac{\sqrt[3]{a+bx}}{x^3} dx$$

Optimal. Leaf size=127

$$\frac{b^2 \log(x)}{18a^{5/3}} - \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{5/3}} + \frac{b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{5/3}} - \frac{\sqrt[3]{a+bx}}{2x^2} - \frac{b\sqrt[3]{a+bx}}{6ax}$$

[Out] $-1/2*(b*x+a)^{(1/3)}/x^2-1/6*b*(b*x+a)^{(1/3)}/a/x+1/18*b^2*\ln(x)/a^{(5/3)}-1/6*b^2*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(5/3)}+1/9*b^2*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}}/a^{(5/3)*3^{(1/2)}})$

Rubi [A] time = 0.05, antiderivative size = 127, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.462$, Rules used = {47, 51, 57, 617, 204, 31}

$$\frac{b^2 \log(x)}{18a^{5/3}} - \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{5/3}} + \frac{b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{5/3}} - \frac{\sqrt[3]{a+bx}}{2x^2} - \frac{b\sqrt[3]{a+bx}}{6ax}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/3)/x^3, x]

[Out] $-(a + b*x)^{(1/3)}/(2*x^2) - (b*(a + b*x)^{(1/3)})/(6*a*x) + (b^2*ArcTan[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(Sqrt[3]*a^{(1/3)})])/(3*Sqrt[3]*a^{(5/3)}) + (b^2*Log[x])/(18*a^{(5/3)}) - (b^2*Log[a^{(1/3)} - (a + b*x)^{(1/3)}])/(6*a^{(5/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 51


```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 57

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2),
x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/
3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x
])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[3]{a+bx}}{x^3} dx &= -\frac{\sqrt[3]{a+bx}}{2x^2} + \frac{1}{6}b \int \frac{1}{x^2(a+bx)^{2/3}} dx \\
&= -\frac{\sqrt[3]{a+bx}}{2x^2} - \frac{b\sqrt[3]{a+bx}}{6ax} - \frac{b^2 \int \frac{1}{x(a+bx)^{2/3}} dx}{9a} \\
&= -\frac{\sqrt[3]{a+bx}}{2x^2} - \frac{b\sqrt[3]{a+bx}}{6ax} + \frac{b^2 \log(x)}{18a^{5/3}} + \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{6a^{5/3}} + \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{a^{2/3} + \sqrt[3]{a}} dx, x, \sqrt[3]{a+bx}\right)}{6a^{5/3}} \\
&= -\frac{\sqrt[3]{a+bx}}{2x^2} - \frac{b\sqrt[3]{a+bx}}{6ax} + \frac{b^2 \log(x)}{18a^{5/3}} - \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{5/3}} - \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2}{\sqrt[3]{a+bx}}\right)}{3a^{5/3}} \\
&= -\frac{\sqrt[3]{a+bx}}{2x^2} - \frac{b\sqrt[3]{a+bx}}{6ax} + \frac{b^2 \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{3\sqrt{3}a^{5/3}} + \frac{b^2 \log(x)}{18a^{5/3}} - \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{5/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.28

$$\frac{3b^2(a+bx)^{4/3} {}_2F_1\left(\frac{4}{3}, 3; \frac{7}{3}; \frac{bx}{a} + 1\right)}{4a^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/3)/x^3, x]

[Out] (-3*b^2*(a + b*x)^(4/3)*Hypergeometric2F1[4/3, 3, 7/3, 1 + (b*x)/a])/(4*a^3)

fricas [A] time = 0.49, size = 187, normalized size = 1.47

$$\frac{2\sqrt{3}ab^2x^2\sqrt{-(-a^2)^{\frac{1}{3}}}\arctan\left(\frac{\left(\sqrt{3}(-a^2)^{\frac{1}{3}}a-2\sqrt{3}(-a^2)^{\frac{2}{3}}(bx+a)^{\frac{1}{3}}\right)\sqrt{-(-a^2)^{\frac{1}{3}}}}{3a^2}\right)+(-a^2)^{\frac{2}{3}}b^2x^2\log\left((bx+a)^{\frac{2}{3}}a-(-a^2)^{\frac{1}{3}}a\right)}{18a^3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/x^3,x, algorithm="fricas")

[Out] 1/18*(2*sqrt(3)*a*b^2*x^2*sqrt(-(-a^2)^(1/3))*arctan(-1/3*(sqrt(3)*(-a^2)^(1/3)*a - 2*sqrt(3)*(-a^2)^(2/3)*(b*x + a)^(1/3))*sqrt(-(-a^2)^(1/3))/a^2) +

$$(-a^2)^{2/3} * b^2 * x^2 * \log((b*x + a)^{2/3} * a - (-a^2)^{1/3} * a + (-a^2)^{2/3} * (b*x + a)^{1/3}) - 2 * (-a^2)^{2/3} * b^2 * x^2 * \log((b*x + a)^{1/3} * a - (-a^2)^{2/3}) - 3 * (a^2 * b * x + 3 * a^3) * (b*x + a)^{1/3} / (a^3 * x^2)$$

giac [A] time = 2.43, size = 128, normalized size = 1.01

$$\frac{2\sqrt{3}b^3 \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{a^{\frac{5}{3}}} + \frac{b^3 \log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)}{a^{\frac{5}{3}}} - \frac{2b^3 \log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)}{a^{\frac{5}{3}}} - \frac{3\left((bx+a)^{\frac{4}{3}}b^3+2(bx+a)^{\frac{1}{3}}ab^3\right)}{ab^2x^2}$$

$18b$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/x^3,x, algorithm="giac")

[Out] 1/18*(2*sqrt(3)*b^3*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3)))/a^(5/3) + b^3*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(5/3) - 2*b^3*log(abs((b*x + a)^(1/3) - a^(1/3)))/a^(5/3) - 3*((b*x + a)^(4/3)*b^3 + 2*(b*x + a)^(1/3)*a*b^3)/(a*b^2*x^2)/b

maple [A] time = 0.01, size = 113, normalized size = 0.89

$$\frac{\sqrt{3} b^2 \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)}{9a^{\frac{5}{3}}} + \frac{b^2 \ln\left(-a^{\frac{1}{3}} + (bx + a)^{\frac{1}{3}}\right)}{9a^{\frac{5}{3}}} + \frac{b^2 \ln\left(a^{\frac{2}{3}} + (bx + a)^{\frac{1}{3}} a^{\frac{1}{3}} + (bx + a)^{\frac{2}{3}}\right)}{18a^{\frac{5}{3}}} - \frac{(bx + a)^{\frac{1}{3}}}{3x^2} - \frac{(bx + a)^{\frac{4}{3}}}{6a^{\frac{5}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/3)/x^3,x)

[Out] -1/6/x^2/a*(b*x+a)^(4/3)-1/3*(b*x+a)^(1/3)/x^2-1/9*b^2/a^(5/3)*ln(-a^(1/3)+(b*x+a)^(1/3))+1/18*b^2/a^(5/3)*ln(a^(2/3)+(b*x+a)^(1/3)*a^(1/3)+(b*x+a)^(2/3))+1/9*b^2/a^(5/3)*3^(1/2)*arctan(1/3*3^(1/2)*(2*(b*x+a)^(1/3)/a^(1/3)+1))

maxima [A] time = 2.99, size = 139, normalized size = 1.09

$$\frac{\sqrt{3} b^2 \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{9a^{\frac{5}{3}}} + \frac{b^2 \log\left((bx + a)^{\frac{2}{3}} + (bx + a)^{\frac{1}{3}} a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{18a^{\frac{5}{3}}} - \frac{b^2 \log\left((bx + a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right)}{9a^{\frac{5}{3}}} - \frac{(bx + a)^{\frac{4}{3}}}{6((bx + a)^2 a^{\frac{5}{3}})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/x^3,x, algorithm="maxima")

[Out] $\frac{1}{9}\sqrt{3}b^2\arctan\left(\frac{1}{3}\sqrt{3}\frac{(2(bx+a)^{1/3}+a^{1/3})}{a^{1/3}}\right)/a^{5/3} + \frac{1}{18}b^2\log\left(\frac{(bx+a)^{2/3}+(bx+a)^{1/3}a^{1/3}+a^{2/3}}{a^{5/3}}\right) - \frac{1}{9}b^2\log\left(\frac{(bx+a)^{1/3}-a^{1/3}}{a^{5/3}}\right) - \frac{1}{6}\frac{(bx+a)^{4/3}b^2+2(bx+a)^{1/3}ab^2}{(bx+a)^2a-2(bx+a)a^2+a^3}$

mupad [B] time = 0.23, size = 196, normalized size = 1.54

$$\frac{b^2 \ln\left(\frac{b^2}{(-a)^{2/3}} - \frac{b^2(a+bx)^{1/3}}{a}\right)}{9(-a)^{5/3}} - \frac{\ln\left(\frac{b^2+\sqrt{3}b^2i}{2(-a)^{2/3}} + \frac{b^2(a+bx)^{1/3}}{a}\right) (b^2 + \sqrt{3}b^2i)}{18(-a)^{5/3}} - \frac{\frac{b^2(a+bx)^{1/3}}{3} + \frac{b^2(a+bx)^{4/3}}{6a}}{(a+bx)^2 - 2a(a+bx) + a^2} + \frac{b^2 \ln\left(\frac{b^2}{(-a)^{2/3}} - \frac{b^2(a+bx)^{1/3}}{a}\right)}{9(-a)^{5/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/3)/x^3,x)

[Out] $(b^2\log(b^2/(-a)^{2/3} - (b^2(a+bx)^{1/3})/a))/(9(-a)^{5/3}) - (\log((3^{1/2}b^2i + b^2)/(2(-a)^{2/3}) + (b^2(a+bx)^{1/3})/a)*(3^{1/2}b^2i + b^2))/(18(-a)^{5/3}) - ((b^2(a+bx)^{1/3})/3 + (b^2(a+bx)^{4/3})/(6a))/((a+bx)^2 - 2a(a+bx) + a^2) + (b^2\log((b^2(a+bx)^{1/3})/a - (b^2((3^{1/2}i)/2 - 1/2))/(-a)^{2/3})*((3^{1/2}i)/2 - 1/2))/(9(-a)^{5/3})$

sympy [C] time = 2.58, size = 2266, normalized size = 17.84

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/3)/x**3,x)

[Out] $-4a^{16/3}b^2\exp(2I\pi/3)\log(1 - b^{1/3}(a/b + x)^{1/3}/a^{1/3})\gamma(4/3)/(27a^7\exp(2I\pi/3)\gamma(7/3) - 81a^6b(a/b + x)\exp(2I\pi/3)\gamma(7/3) + 81a^5b^2(a/b + x)^2\exp(2I\pi/3)\gamma(7/3) - 27a^4b^3(a/b + x)^3\exp(2I\pi/3)\gamma(7/3) - 4a^{16/3}b^2\log(1 - b^{1/3}(a/b + x)^{1/3}\exp_{\text{polar}}(2I\pi/3)/a^{1/3})\gamma(4/3)/(27a^7\exp(2I\pi/3)\gamma(7/3) - 81a^6b(a/b + x)\exp(2I\pi/3)\gamma(7/3) + 81a^5b^2(a/b + x)^2\exp(2I\pi/3)\gamma(7/3) - 27a^4b^3(a/b + x)^3\exp(2I\pi/3)\gamma(7/3) - 4a^{16/3}b^2\exp(-2I\pi/3)\log(1 - b^{1/3}(a/b + x)^{1/3}\exp_{\text{polar}}(4I\pi/3)/a^{1/3})\gamma(4/3)/(27a^7\exp(2I\pi/3)\gamma(7/3) - 81a^6b(a/b + x)\exp(2I\pi/3)\gamma(7/3) + 81a^5b^2(a/b + x)^2\exp(2I\pi/3)\gamma(7/3) - 27a^4b^3(a/b + x)^3\exp(2I\pi/3)\gamma(7/3) - 4a^{16/3}b^2\exp(2I\pi/3)\log(1 - b^{1/3}(a/b + x)^{1/3}/a^{1/3})\gamma(4/3)/(27a^7\exp(2I\pi/3)\gamma(7/3) - 81a^6b(a/b + x)\exp(2I\pi/3)\gamma(7/3) + 81a^5b^2(a/b + x)^2\exp(2I\pi/3)\gamma(7/3) - 27a^4b^3(a/b + x)^3\exp(2I\pi/3)\gamma(7/3)$

$$p(2*I*pi/3)*gamma(7/3) - 27*a**4*b**3*(a/b + x)**3*exp(2*I*pi/3)*gamma(7/3)$$

3.378 $\int x^3(a + bx)^{2/3} dx$

Optimal. Leaf size=72

$$-\frac{3a^3(a + bx)^{5/3}}{5b^4} + \frac{9a^2(a + bx)^{8/3}}{8b^4} + \frac{3(a + bx)^{14/3}}{14b^4} - \frac{9a(a + bx)^{11/3}}{11b^4}$$

[Out] $-3/5*a^3*(b*x+a)^{(5/3)}/b^4+9/8*a^2*(b*x+a)^{(8/3)}/b^4-9/11*a*(b*x+a)^{(11/3)}/b^4+3/14*(b*x+a)^{(14/3)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9a^2(a + bx)^{8/3}}{8b^4} - \frac{3a^3(a + bx)^{5/3}}{5b^4} + \frac{3(a + bx)^{14/3}}{14b^4} - \frac{9a(a + bx)^{11/3}}{11b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^(2/3), x]

[Out] $(-3*a^3*(a + b*x)^{(5/3)})/(5*b^4) + (9*a^2*(a + b*x)^{(8/3)})/(8*b^4) - (9*a*(a + b*x)^{(11/3)})/(11*b^4) + (3*(a + b*x)^{(14/3)})/(14*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^{2/3} dx &= \int \left(-\frac{a^3(a + bx)^{2/3}}{b^3} + \frac{3a^2(a + bx)^{5/3}}{b^3} - \frac{3a(a + bx)^{8/3}}{b^3} + \frac{(a + bx)^{11/3}}{b^3} \right) dx \\ &= -\frac{3a^3(a + bx)^{5/3}}{5b^4} + \frac{9a^2(a + bx)^{8/3}}{8b^4} - \frac{9a(a + bx)^{11/3}}{11b^4} + \frac{3(a + bx)^{14/3}}{14b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.64

$$\frac{3(a + bx)^{5/3} (-81a^3 + 135a^2bx - 180ab^2x^2 + 220b^3x^3)}{3080b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^(2/3), x]

[Out] (3*(a + b*x)^(5/3)*(-81*a^3 + 135*a^2*b*x - 180*a*b^2*x^2 + 220*b^3*x^3))/(3080*b^4)

fricas [A] time = 0.49, size = 53, normalized size = 0.74

$$\frac{3(220b^4x^4 + 40ab^3x^3 - 45a^2b^2x^2 + 54a^3bx - 81a^4)(bx + a)^{\frac{2}{3}}}{3080b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(2/3), x, algorithm="fricas")

[Out] 3/3080*(220*b^4*x^4 + 40*a*b^3*x^3 - 45*a^2*b^2*x^2 + 54*a^3*b*x - 81*a^4)*(b*x + a)^(2/3)/b^4

giac [B] time = 1.12, size = 117, normalized size = 1.62

$$3 \frac{7 \left(40 (bx+a)^{\frac{11}{3}} - 165 (bx+a)^{\frac{8}{3}} a + 264 (bx+a)^{\frac{5}{3}} a^2 - 220 (bx+a)^{\frac{2}{3}} a^3 \right) a}{b^3} + \frac{2 \left(110 (bx+a)^{\frac{14}{3}} - 560 (bx+a)^{\frac{11}{3}} a + 1155 (bx+a)^{\frac{8}{3}} a^2 - 1232 (bx+a)^{\frac{5}{3}} a^3 + 770 (bx+a)^{\frac{2}{3}} a^4 \right)}{b^3}}{3080b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(2/3), x, algorithm="giac")

[Out] 3/3080*(7*(40*(b*x + a)^(11/3) - 165*(b*x + a)^(8/3)*a + 264*(b*x + a)^(5/3))*a^2 - 220*(b*x + a)^(2/3)*a^3)*a/b^3 + 2*(110*(b*x + a)^(14/3) - 560*(b*x + a)^(11/3)*a + 1155*(b*x + a)^(8/3)*a^2 - 1232*(b*x + a)^(5/3)*a^3 + 770*(b*x + a)^(2/3)*a^4)/b^3)/b

maple [A] time = 0.00, size = 43, normalized size = 0.60

$$\frac{3(bx + a)^{\frac{5}{3}}(-220b^3x^3 + 180ab^2x^2 - 135a^2bx + 81a^3)}{3080b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^(2/3), x)

[Out] -3/3080*(b*x+a)^(5/3)*(-220*b^3*x^3+180*a*b^2*x^2-135*a^2*b*x+81*a^3)/b^4

maxima [A] time = 1.36, size = 56, normalized size = 0.78

$$\frac{3(bx+a)^{\frac{14}{3}}}{14b^4} - \frac{9(bx+a)^{\frac{11}{3}}a}{11b^4} + \frac{9(bx+a)^{\frac{8}{3}}a^2}{8b^4} - \frac{3(bx+a)^{\frac{5}{3}}a^3}{5b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(2/3),x, algorithm="maxima")

[Out] 3/14*(b*x + a)^(14/3)/b^4 - 9/11*(b*x + a)^(11/3)*a/b^4 + 9/8*(b*x + a)^(8/3)*a^2/b^4 - 3/5*(b*x + a)^(5/3)*a^3/b^4

mupad [B] time = 0.05, size = 56, normalized size = 0.78

$$\frac{3(a+bx)^{14/3}}{14b^4} - \frac{3a^3(a+bx)^{5/3}}{5b^4} + \frac{9a^2(a+bx)^{8/3}}{8b^4} - \frac{9a(a+bx)^{11/3}}{11b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(a + b*x)^(2/3),x)

[Out] (3*(a + b*x)^(14/3))/(14*b^4) - (3*a^3*(a + b*x)^(5/3))/(5*b^4) + (9*a^2*(a + b*x)^(8/3))/(8*b^4) - (9*a*(a + b*x)^(11/3))/(11*b^4)

sympy [B] time = 3.07, size = 1742, normalized size = 24.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**(2/3),x)

[Out] -243*a**(74/3)*(1 + b*x/a)**(2/3)/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6) + 243*a**(74/3)/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6) - 1296*a**(71/3)*b*x*(1 + b*x/a)**(2/3)/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6) + 1458*a**(71/3)*b*x/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6) - 2808*a**(68/3)*b**2*x**2*(1 + b*x/a)**(2/3)/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6) + 3645*a**(68/3)*b**2*x**2/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a

$$\begin{aligned}
& **17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14 \\
& *b**10*x**6) - 3120*a**(65/3)*b**3*x**3*(1 + b*x/a)**(2/3)/(3080*a**20*b**4 \\
& + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 462 \\
& 00*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6) + 4860* \\
& a**(65/3)*b**3*x**3/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b** \\
& 6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x \\
& **5 + 3080*a**14*b**10*x**6) - 1050*a**(62/3)*b**4*x**4*(1 + b*x/a)**(2/3)/ \\
& (3080*a**20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17 \\
& *b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b** \\
& 10*x**6) + 3645*a**(62/3)*b**4*x**4/(3080*a**20*b**4 + 18480*a**19*b**5*x + \\
& 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18 \\
& 480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6) + 4032*a**(59/3)*b**5*x**5*(1 \\
& + b*x/a)**(2/3)/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x \\
& **2 + 61600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 \\
& + 3080*a**14*b**10*x**6) + 1458*a**(59/3)*b**5*x**5/(3080*a**20*b**4 + 1848 \\
& 0*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**1 \\
& 6*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6) + 11004*a**(56 \\
& /3)*b**6*x**6*(1 + b*x/a)**(2/3)/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46 \\
& 200*a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480 \\
& *a**15*b**9*x**5 + 3080*a**14*b**10*x**6) + 243*a**(56/3)*b**6*x**6/(3080*a \\
& **20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x \\
& **3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6 \\
&) + 14352*a**(53/3)*b**7*x**7*(1 + b*x/a)**(2/3)/(3080*a**20*b**4 + 18480*a \\
& **19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**16*b \\
& **8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6) + 10485*a**(50/3) \\
& *b**8*x**8*(1 + b*x/a)**(2/3)/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46200 \\
& *a**18*b**6*x**2 + 61600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a \\
& **15*b**9*x**5 + 3080*a**14*b**10*x**6) + 4080*a**(47/3)*b**9*x**9*(1 + b*x/ \\
& a)**(2/3)/(3080*a**20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 6 \\
& 1600*a**17*b**7*x**3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080 \\
& *a**14*b**10*x**6) + 660*a**(44/3)*b**10*x**10*(1 + b*x/a)**(2/3)/(3080*a** \\
& 20*b**4 + 18480*a**19*b**5*x + 46200*a**18*b**6*x**2 + 61600*a**17*b**7*x** \\
& 3 + 46200*a**16*b**8*x**4 + 18480*a**15*b**9*x**5 + 3080*a**14*b**10*x**6)
\end{aligned}$$

3.379 $\int x^2(a + bx)^{2/3} dx$

Optimal. Leaf size=53

$$\frac{3a^2(a + bx)^{5/3}}{5b^3} + \frac{3(a + bx)^{11/3}}{11b^3} - \frac{3a(a + bx)^{8/3}}{4b^3}$$

[Out] $3/5*a^2*(b*x+a)^{(5/3)}/b^3-3/4*a*(b*x+a)^{(8/3)}/b^3+3/11*(b*x+a)^{(11/3)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3a^2(a + bx)^{5/3}}{5b^3} + \frac{3(a + bx)^{11/3}}{11b^3} - \frac{3a(a + bx)^{8/3}}{4b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*x)^(2/3), x]

[Out] $(3*a^2*(a + b*x)^{(5/3)})/(5*b^3) - (3*a*(a + b*x)^{(8/3)})/(4*b^3) + (3*(a + b*x)^{(11/3)})/(11*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^{2/3} dx &= \int \left(\frac{a^2(a + bx)^{2/3}}{b^2} - \frac{2a(a + bx)^{5/3}}{b^2} + \frac{(a + bx)^{8/3}}{b^2} \right) dx \\ &= \frac{3a^2(a + bx)^{5/3}}{5b^3} - \frac{3a(a + bx)^{8/3}}{4b^3} + \frac{3(a + bx)^{11/3}}{11b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.66

$$\frac{3(a + bx)^{5/3} (9a^2 - 15abx + 20b^2x^2)}{220b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^(2/3), x]

[Out] $(3*(a + b*x)^(5/3)*(9*a^2 - 15*a*b*x + 20*b^2*x^2))/(220*b^3)$

fricas [A] time = 0.47, size = 42, normalized size = 0.79

$$\frac{3(20b^3x^3 + 5ab^2x^2 - 6a^2bx + 9a^3)(bx + a)^{\frac{2}{3}}}{220b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(2/3), x, algorithm="fricas")

[Out] $3/220*(20*b^3*x^3 + 5*a*b^2*x^2 - 6*a^2*b*x + 9*a^3)*(b*x + a)^(2/3)/b^3$

giac [B] time = 0.83, size = 92, normalized size = 1.74

$$3 \left(\frac{11 \left(5(bx+a)^{\frac{8}{3}} - 16(bx+a)^{\frac{5}{3}}a + 20(bx+a)^{\frac{2}{3}}a^2 \right) a}{b^2} + \frac{40(bx+a)^{\frac{11}{3}} - 165(bx+a)^{\frac{8}{3}}a + 264(bx+a)^{\frac{5}{3}}a^2 - 220(bx+a)^{\frac{2}{3}}a^3}{b^2} \right) / 440b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(2/3), x, algorithm="giac")

[Out] $3/440*(11*(5*(b*x + a)^(8/3) - 16*(b*x + a)^(5/3)*a + 20*(b*x + a)^(2/3)*a^2)*a/b^2 + (40*(b*x + a)^(11/3) - 165*(b*x + a)^(8/3)*a + 264*(b*x + a)^(5/3)*a^2 - 220*(b*x + a)^(2/3)*a^3)/b^2)/b$

maple [A] time = 0.01, size = 32, normalized size = 0.60

$$\frac{3(bx + a)^{\frac{5}{3}}(20b^2x^2 - 15abx + 9a^2)}{220b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^(2/3), x)

[Out] $3/220*(b*x+a)^(5/3)*(20*b^2*x^2-15*a*b*x+9*a^2)/b^3$

maxima [A] time = 1.35, size = 41, normalized size = 0.77

$$\frac{3(bx + a)^{\frac{11}{3}}}{11b^3} - \frac{3(bx + a)^{\frac{8}{3}}a}{4b^3} + \frac{3(bx + a)^{\frac{5}{3}}a^2}{5b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(2/3),x, algorithm="maxima")

[Out] $\frac{3}{11}(b*x + a)^{(11/3)}/b^3 - \frac{3}{4}(b*x + a)^{(8/3)}*a/b^3 + \frac{3}{5}(b*x + a)^{(5/3)}*a^2/b^3$

mupad [B] time = 0.04, size = 37, normalized size = 0.70

$$\frac{60(a+bx)^{11/3} - 165a(a+bx)^{8/3} + 132a^2(a+bx)^{5/3}}{220b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a + b*x)^(2/3),x)

[Out] $(60*(a + b*x)^{(11/3)} - 165*a*(a + b*x)^{(8/3)} + 132*a^2*(a + b*x)^{(5/3)})/(220*b^3)$

sympy [B] time = 1.94, size = 666, normalized size = 12.57

$$\frac{27a^{\frac{35}{3}} \left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3} - \frac{27a^{\frac{35}{3}}}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3} + \frac{63a^{\frac{32}{3}}(1 + \frac{bx}{a})^{\frac{2}{3}}}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3} - \frac{81a^{\frac{32}{3}}bx}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3} + \frac{42a^{\frac{29}{3}}b^2x^2(1 + \frac{bx}{a})^{\frac{2}{3}}}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3} - \frac{81a^{\frac{29}{3}}b^2x^2}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3} + \frac{78a^{\frac{26}{3}}b^3x^3(1 + \frac{bx}{a})^{\frac{2}{3}}}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3} - \frac{27a^{\frac{26}{3}}b^3x^3}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3} + \frac{207a^{\frac{23}{3}}b^4x^4(1 + \frac{bx}{a})^{\frac{2}{3}}}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3} + \frac{195a^{\frac{20}{3}}b^5x^5(1 + \frac{bx}{a})^{\frac{2}{3}}}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3} + \frac{60a^{\frac{17}{3}}b^6x^6(1 + \frac{bx}{a})^{\frac{2}{3}}}{220a^8b^3 + 660a^7b^4x + 660a^6b^5x^2 + 220a^5b^6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)**(2/3),x)

[Out] $27*a^{(35/3)}*(1 + b*x/a)^{(2/3)}/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3}) - 27*a^{(35/3)}/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3}) + 63*a^{(32/3)}*b*x*(1 + b*x/a)^{(2/3)}/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3}) - 81*a^{(32/3)}*b*x/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3}) + 42*a^{(29/3)}*b^{**2}*x^{**2}*(1 + b*x/a)^{(2/3)}/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3}) - 81*a^{(29/3)}*b^{**2}*x^{**2}/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3}) + 78*a^{(26/3)}*b^{**3}*x^{**3}*(1 + b*x/a)^{(2/3)}/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3}) - 27*a^{(26/3)}*b^{**3}*x^{**3}/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3}) + 207*a^{(23/3)}*b^{**4}*x^{**4}*(1 + b*x/a)^{(2/3)}/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3}) + 195*a^{(20/3)}*b^{**5}*x^{**5}*(1 + b*x/a)^{(2/3)}/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3}) + 60*a^{(17/3)}*b^{**6}*x^{**6}*(1 + b*x/a)^{(2/3)}/(220*a^{**8}*b^{**3} + 660*a^{**7}*b^{**4}*x + 660*a^{**6}*b^{**5}*x^{**2} + 220*a^{**5}*b^{**6}*x^{**3})$

3.380 $\int x(a + bx)^{2/3} dx$

Optimal. Leaf size=34

$$\frac{3(a + bx)^{8/3}}{8b^2} - \frac{3a(a + bx)^{5/3}}{5b^2}$$

[Out] $-3/5*a*(b*x+a)^{(5/3)}/b^2+3/8*(b*x+a)^{(8/3)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3(a + bx)^{8/3}}{8b^2} - \frac{3a(a + bx)^{5/3}}{5b^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^(2/3), x]

[Out] $(-3*a*(a + b*x)^{(5/3)})/(5*b^2) + (3*(a + b*x)^{(8/3)})/(8*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x(a + bx)^{2/3} dx &= \int \left(-\frac{a(a + bx)^{2/3}}{b} + \frac{(a + bx)^{5/3}}{b} \right) dx \\ &= -\frac{3a(a + bx)^{5/3}}{5b^2} + \frac{3(a + bx)^{8/3}}{8b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.71

$$\frac{3(a + bx)^{5/3}(5bx - 3a)}{40b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^(2/3), x]

[Out] $(3*(a + b*x)^{(5/3)*(-3*a + 5*b*x))/(40*b^2)$

fricas [A] time = 0.48, size = 31, normalized size = 0.91

$$\frac{3(5b^2x^2 + 2abx - 3a^2)(bx + a)^{\frac{2}{3}}}{40b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(2/3),x, algorithm="fricas")`

[Out] $3/40*(5*b^2*x^2 + 2*a*b*x - 3*a^2)*(b*x + a)^{(2/3)}/b^2$

giac [B] time = 0.89, size = 68, normalized size = 2.00

$$\frac{3 \left(\frac{4 \left(2(bx+a)^{\frac{5}{3}} - 5(bx+a)^{\frac{2}{3}}a \right) a}{b} + \frac{5(bx+a)^{\frac{8}{3}} - 16(bx+a)^{\frac{5}{3}}a + 20(bx+a)^{\frac{2}{3}}a^2}{b} \right)}{40b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(2/3),x, algorithm="giac")`

[Out] $3/40*(4*(2*(b*x + a)^{(5/3)} - 5*(b*x + a)^{(2/3)}*a)*a/b + (5*(b*x + a)^{(8/3)} - 16*(b*x + a)^{(5/3)}*a + 20*(b*x + a)^{(2/3)}*a^2)/b)$

maple [A] time = 0.00, size = 21, normalized size = 0.62

$$\frac{3(bx + a)^{\frac{5}{3}}(-5bx + 3a)}{40b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)^(2/3),x)`

[Out] $-3/40*(b*x+a)^{(5/3)*(-5*b*x+3*a)}/b^2$

maxima [A] time = 1.35, size = 26, normalized size = 0.76

$$\frac{3(bx + a)^{\frac{8}{3}}}{8b^2} - \frac{3(bx + a)^{\frac{5}{3}}a}{5b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(2/3),x, algorithm="maxima")`

[Out] $3/8*(b*x + a)^{(8/3)}/b^2 - 3/5*(b*x + a)^{(5/3)}*a/b^2$

mupad [B] time = 0.03, size = 25, normalized size = 0.74

$$-\frac{24a(a+bx)^{5/3} - 15(a+bx)^{8/3}}{40b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(a + b*x)^(2/3), x)`

[Out] $-(24*a*(a + b*x)^{(5/3)} - 15*(a + b*x)^{(8/3)})/(40*b^2)$

sympy [B] time = 1.28, size = 202, normalized size = 5.94

$$-\frac{9a^{\frac{14}{3}}\left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{40a^2b^2 + 40ab^3x} + \frac{9a^{\frac{14}{3}}}{40a^2b^2 + 40ab^3x} - \frac{3a^{\frac{11}{3}}bx\left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{40a^2b^2 + 40ab^3x} + \frac{9a^{\frac{11}{3}}bx}{40a^2b^2 + 40ab^3x} + \frac{21a^{\frac{8}{3}}b^2x^2\left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{40a^2b^2 + 40ab^3x} + \frac{15a^{\frac{5}{3}}b^3x^3\left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{40a^2b^2 + 40ab^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**(2/3), x)`

[Out] $-9*a^{14/3}*(1 + b*x/a)^{2/3}/(40*a^{14/3} + 40*a*b^{11/3}*x) + 9*a^{14/3}/(40*a^{14/3} + 40*a*b^{11/3}*x) - 3*a^{11/3}*b*x*(1 + b*x/a)^{2/3}/(40*a^{14/3} + 40*a*b^{11/3}*x) + 9*a^{11/3}*b*x/(40*a^{14/3} + 40*a*b^{11/3}*x) + 21*a^{8/3}*b^2*x^2*(1 + b*x/a)^{2/3}/(40*a^{14/3} + 40*a*b^{11/3}*x) + 15*a^{5/3}*b^3*x^3*(1 + b*x/a)^{2/3}/(40*a^{14/3} + 40*a*b^{11/3}*x)$

3.381 $\int (a + bx)^{2/3} dx$

Optimal. Leaf size=16

$$\frac{3(a + bx)^{5/3}}{5b}$$

[Out] $3/5*(b*x+a)^{(5/3)}/b$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{3(a + bx)^{5/3}}{5b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(2/3), x]

[Out] (3*(a + b*x)^(5/3))/(5*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^{2/3} dx = \frac{3(a + bx)^{5/3}}{5b}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$\frac{3(a + bx)^{5/3}}{5b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(2/3), x]

[Out] (3*(a + b*x)^(5/3))/(5*b)

fricas [A] time = 0.48, size = 12, normalized size = 0.75

$$\frac{3(bx + a)^{5/3}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3),x, algorithm="fricas")

[Out] 3/5*(b*x + a)^(5/3)/b

giac [A] time = 1.14, size = 12, normalized size = 0.75

$$\frac{3(bx + a)^{\frac{5}{3}}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3),x, algorithm="giac")

[Out] 3/5*(b*x + a)^(5/3)/b

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{3(bx + a)^{\frac{5}{3}}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(2/3),x)

[Out] 3/5*(b*x+a)^(5/3)/b

maxima [A] time = 1.29, size = 12, normalized size = 0.75

$$\frac{3(bx + a)^{\frac{5}{3}}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3),x, algorithm="maxima")

[Out] 3/5*(b*x + a)^(5/3)/b

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{3(a + bx)^{\frac{5}{3}}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(2/3),x)

[Out] $(3*(a + b*x)^{(5/3)})/(5*b)$

sympy [A] time = 0.06, size = 12, normalized size = 0.75

$$\frac{3(a + bx)^{\frac{5}{3}}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(2/3),x)`

[Out] $3*(a + b*x)**(5/3)/(5*b)$

$$3.382 \quad \int \frac{(a+bx)^{2/3}}{x} dx$$

Optimal. Leaf size=92

$$\frac{3}{2}a^{2/3} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) + \sqrt{3} a^{2/3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right) - \frac{1}{2}a^{2/3} \log(x) + \frac{3}{2}(a+bx)^{2/3}$$

[Out] $3/2*(b*x+a)^{(2/3)}-1/2*a^{(2/3)}*\ln(x)+3/2*a^{(2/3)}*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})+a^{(2/3)}*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)}*3^{(1/2)})*3^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {50, 55, 617, 204, 31}

$$\frac{3}{2}a^{2/3} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) + \sqrt{3} a^{2/3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right) - \frac{1}{2}a^{2/3} \log(x) + \frac{3}{2}(a+bx)^{2/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(2/3)/x, x]

[Out] $(3*(a + b*x)^{(2/3)})/2 + \text{Sqrt}[3]*a^{(2/3)}*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})] - (a^{(2/3)}*\text{Log}[x])/2 + (3*a^{(2/3)}*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}])/2$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 55

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)],

$x] - \text{Dist}[3/(2*b*q), \text{Subst}[\text{Int}[1/(q - x), x], x, (c + d*x)^{(1/3)}], x)] /;$
 $\text{FreeQ}\{a, b, c, d, x\} \ \&\& \ \text{PosQ}[(b*c - a*d)/b]$

Rule 204

$\text{Int}[(a_ + (b_)*(x_)^2)^{-1}, x_Symbol] \text{ :> } -\text{Simp}[\text{ArcTan}[(\text{Rt}[-b, 2]*x)/\text{Rt}[-a, 2]]/(\text{Rt}[-a, 2]*\text{Rt}[-b, 2]), x] /;$
 $\text{FreeQ}\{a, b, x\} \ \&\& \ \text{PosQ}[a/b] \ \&\& \ (\text{LtQ}[a, 0] \ || \ \text{LtQ}[b, 0])$

Rule 617

$\text{Int}[(a_ + (b_)*(x_) + (c_)*(x_)^2)^{-1}, x_Symbol] \text{ :> } \text{With}\{q = 1 - 4*S$
 $\text{implify}[(a*c)/b^2]\}, \text{Dist}[-2/b, \text{Subst}[\text{Int}[1/(q - x^2), x], x, 1 + (2*c*x)/b$
 $], x] /;$
 $\text{RationalQ}[q] \ \&\& \ (\text{EqQ}[q^2, 1] \ || \ !\text{RationalQ}[b^2 - 4*a*c]) /;$
 $\text{FreeQ}\{a, b, c, x\} \ \&\& \ \text{NeQ}[b^2 - 4*a*c, 0]$

Rubi steps

$$\begin{aligned} \int \frac{(a + bx)^{2/3}}{x} dx &= \frac{3}{2}(a + bx)^{2/3} + a \int \frac{1}{x\sqrt[3]{a + bx}} dx \\ &= \frac{3}{2}(a + bx)^{2/3} - \frac{1}{2}a^{2/3} \log(x) - \frac{1}{2}(3a^{2/3}) \text{Subst}\left(\int \frac{1}{\sqrt[3]{a} - x} dx, x, \sqrt[3]{a + bx}\right) + \frac{1}{2}(3a) \text{Subst}\left(\int \frac{1}{-3 - x^2} dx, x, \sqrt[3]{a + bx}\right) \\ &= \frac{3}{2}(a + bx)^{2/3} - \frac{1}{2}a^{2/3} \log(x) + \frac{3}{2}a^{2/3} \log\left(\sqrt[3]{a} - \sqrt[3]{a + bx}\right) - (3a^{2/3}) \text{Subst}\left(\int \frac{1}{-3 - x^2} dx, x, \sqrt[3]{a + bx}\right) \\ &= \frac{3}{2}(a + bx)^{2/3} + \sqrt{3} a^{2/3} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right) - \frac{1}{2}a^{2/3} \log(x) + \frac{3}{2}a^{2/3} \log\left(\sqrt[3]{a} - \sqrt[3]{a + bx}\right) \end{aligned}$$

Mathematica [A] time = 0.04, size = 86, normalized size = 0.93

$$\frac{3}{2} \left(a^{2/3} \log\left(\sqrt[3]{a} - \sqrt[3]{a + bx}\right) + (a + bx)^{2/3} \right) + \sqrt{3} a^{2/3} \tan^{-1}\left(\frac{\frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}} + 1}{\sqrt{3}}\right) - \frac{1}{2} a^{2/3} \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(2/3)/x,x]

[Out] $\text{Sqrt}[3]*a^{(2/3)}*\text{ArcTan}[(1 + (2*(a + b*x)^{(1/3}))/a^{(1/3}))/\text{Sqrt}[3]] - (a^{(2/3)})*\text{Log}[x])/2 + (3*((a + b*x)^{(2/3)} + a^{(2/3)}*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}]))/2$

fricas [A] time = 0.48, size = 110, normalized size = 1.20

$$\sqrt{3} (a^2)^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3} a + 2 \sqrt{3} (a^2)^{\frac{1}{3}} (bx + a)^{\frac{1}{3}}}{3 a}\right) - \frac{1}{2} (a^2)^{\frac{1}{3}} \log\left((bx + a)^{\frac{2}{3}} a + (a^2)^{\frac{1}{3}} a + (a^2)^{\frac{2}{3}} (bx + a)^{\frac{1}{3}}\right) + (a^2)^{\frac{1}{3}} \log\left(\left|(bx + a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right) + \frac{3}{2} (bx + a)^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(2/3)/x,x, algorithm="fricas")`

[Out] $\text{sqrt}(3)*(a^2)^{(1/3)}*\text{arctan}(1/3*\text{sqrt}(3)*a + 2*\text{sqrt}(3)*(a^2)^{(1/3)}*(b*x + a)^{(1/3}))/a - 1/2*(a^2)^{(1/3)}*\text{log}((b*x + a)^{(2/3)}*a + (a^2)^{(1/3)}*a + (a^2)^{(2/3)}*(b*x + a)^{(1/3})) + (a^2)^{(1/3)}*\text{log}((b*x + a)^{(1/3)}*a - (a^2)^{(2/3)}) + 3/2*(b*x + a)^{(2/3)}$

giac [A] time = 2.20, size = 86, normalized size = 0.93

$$\sqrt{3} a^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3} \left(2 (bx + a)^{\frac{1}{3}} + a^{\frac{1}{3}}\right)}{3 a^{\frac{1}{3}}}\right) - \frac{1}{2} a^{\frac{2}{3}} \log\left((bx + a)^{\frac{2}{3}} + (bx + a)^{\frac{1}{3}} a^{\frac{1}{3}} + a^{\frac{2}{3}}\right) + a^{\frac{2}{3}} \log\left(\left|(bx + a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right) + \frac{3}{2} (bx + a)^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(2/3)/x,x, algorithm="giac")`

[Out] $\text{sqrt}(3)*a^{(2/3)}*\text{arctan}(1/3*\text{sqrt}(3)*(2*(b*x + a)^{(1/3)} + a^{(1/3}))/a^{(1/3)}) - 1/2*a^{(2/3)}*\text{log}((b*x + a)^{(2/3)} + (b*x + a)^{(1/3)}*a^{(1/3)} + a^{(2/3)}) + a^{(2/3)}*\text{log}(\text{abs}((b*x + a)^{(1/3)} - a^{(1/3)})) + 3/2*(b*x + a)^{(2/3)}$

maple [A] time = 0.00, size = 84, normalized size = 0.91

$$\sqrt{3} a^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3} \left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}} + 1\right)}{3}\right) + a^{\frac{2}{3}} \ln\left(-a^{\frac{1}{3}} + (bx + a)^{\frac{1}{3}}\right) - \frac{a^{\frac{2}{3}} \ln\left(a^{\frac{2}{3}} + (bx + a)^{\frac{1}{3}} a^{\frac{1}{3}} + (bx + a)^{\frac{2}{3}}\right)}{2} + \frac{3 (bx + a)^{\frac{2}{3}}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(2/3)/x,x)`

[Out] $3/2*(b*x+a)^{(2/3)}+a^{(2/3)}*\ln(-a^{(1/3)}+(b*x+a)^{(1/3)})-1/2*a^{(2/3)}*\ln(a^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+(b*x+a)^{(2/3)})+a^{(2/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2*(b*x+a)^{(1/3)}/a^{(1/3)}+1))$

maxima [A] time = 2.97, size = 85, normalized size = 0.92

$$\sqrt{3} a^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right) - \frac{1}{2} a^{\frac{2}{3}} \log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right) + a^{\frac{2}{3}} \log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right) + \frac{3}{2} (b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/x,x, algorithm="maxima")

[Out] $\sqrt{3}*a^{(2/3)}*\arctan(1/3*\sqrt{3}*(2*(b*x+a)^{(1/3)}+a^{(1/3)})/a^{(1/3)}) - 1/2*a^{(2/3)}*\log((b*x+a)^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+a^{(2/3)}) + a^{(2/3)}*\log((b*x+a)^{(1/3)}-a^{(1/3)}) + 3/2*(b*x+a)^{(2/3)}$

mupad [B] time = 0.11, size = 117, normalized size = 1.27

$$\frac{3(a+bx)^{2/3}}{2} + a^{2/3} \ln\left(9a^2(a+bx)^{1/3} - 9a^{7/3}\right) + \frac{a^{2/3} \ln\left(9a^2(a+bx)^{1/3} - \frac{9a^{7/3}(-1+\sqrt{3}i)^2}{4}\right) (-1+\sqrt{3}i) a^{2/3}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(2/3)/x,x)

[Out] $(3*(a+bx)^{(2/3)})/2 + a^{(2/3)}*\log(9*a^2*(a+bx)^{(1/3)} - 9*a^{(7/3)}) + (a^{(2/3)}*\log(9*a^2*(a+bx)^{(1/3)} - (9*a^{(7/3)}*(3^{(1/2)}*1i - 1)^2)/4)*(3^{(1/2)}*1i - 1))/2 - (a^{(2/3)}*\log(9*a^2*(a+bx)^{(1/3)} - (9*a^{(7/3)}*(3^{(1/2)}*1i + 1)^2)/4)*(3^{(1/2)}*1i + 1))/2$

sympy [C] time = 2.06, size = 182, normalized size = 1.98

$$\frac{5a^{\frac{2}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b}+x}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{5}{3}\right)}{3\Gamma\left(\frac{8}{3}\right)} + \frac{5a^{\frac{2}{3}} e^{\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b}+x} e^{\frac{2i\pi}{3}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{5}{3}\right)}{3\Gamma\left(\frac{8}{3}\right)} + \frac{5a^{\frac{2}{3}} e^{-\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b}+x} e^{\frac{4i\pi}{3}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{5}{3}\right)}{3\Gamma\left(\frac{8}{3}\right)} + \frac{5b^{\frac{2}{3}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(2/3)/x,x)

[Out] $5*a^{(2/3)}*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}/a^{(1/3)})*\gamma(5/3)/(3*\gamma(8/3)) + 5*a^{(2/3)}*\exp(2*I*pi/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_pola$

$$\begin{aligned} & r(2I\pi/3)/a^{1/3})\gamma(5/3)/(3\gamma(8/3)) + 5a^{2/3}\exp(-2I\pi/3) \\ & * \log(1 - b^{1/3}(a/b + x)^{1/3}\exp_{\text{polar}}(4I\pi/3)/a^{1/3})\gamma(5/3) \\ & / (3\gamma(8/3)) + 5b^{2/3}(a/b + x)^{2/3}\gamma(5/3)/(2\gamma(8/3)) \end{aligned}$$

$$3.383 \quad \int \frac{(a+bx)^{2/3}}{x^2} dx$$

Optimal. Leaf size=94

$$-\frac{(a+bx)^{2/3}}{x} - \frac{b \log(x)}{3\sqrt[3]{a}} + \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{\sqrt[3]{a}} + \frac{2b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}\sqrt[3]{a}}$$

[Out] $-(b*x+a)^{(2/3)}/x-1/3*b*\ln(x)/a^{(1/3)}+b*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(1/3)}+2/3*b*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}}/a^{(1/3)*3^{(1/2)}})$

Rubi [A] time = 0.03, antiderivative size = 94, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {47, 55, 617, 204, 31}

$$-\frac{(a+bx)^{2/3}}{x} - \frac{b \log(x)}{3\sqrt[3]{a}} + \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{\sqrt[3]{a}} + \frac{2b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}\sqrt[3]{a}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(2/3)/x^2,x]

[Out] $-((a + b*x)^{(2/3)}/x) + (2*b*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})]/(\text{Sqrt}[3]*a^{(1/3)}))/(\text{Sqrt}[3]*a^{(1/3)}) - (b*\text{Log}[x])/((3*a^{(1/3)}) + (b*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}])/a^{(1/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 55

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x]

```
] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)],
x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x]) /;
FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c]) /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{2/3}}{x^2} dx &= -\frac{(a+bx)^{2/3}}{x} + \frac{1}{3}(2b) \int \frac{1}{x\sqrt[3]{a+bx}} dx \\
 &= -\frac{(a+bx)^{2/3}}{x} - \frac{b \log(x)}{3\sqrt[3]{a}} + b \operatorname{Subst}\left(\int \frac{1}{a^{2/3} + \sqrt[3]{a}x + x^2} dx, x, \sqrt[3]{a+bx}\right) - \frac{b \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{\sqrt[3]{a}} \\
 &= -\frac{(a+bx)^{2/3}}{x} - \frac{b \log(x)}{3\sqrt[3]{a}} + \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{\sqrt[3]{a}} - \frac{(2b) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}\right)}{\sqrt[3]{a}} \\
 &= -\frac{(a+bx)^{2/3}}{x} + \frac{2b \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3}\sqrt[3]{a}} - \frac{b \log(x)}{3\sqrt[3]{a}} + \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{\sqrt[3]{a}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.35

$$\frac{3b(a+bx)^{5/3} {}_2F_1\left(\frac{5}{3}, 2; \frac{8}{3}; \frac{bx}{a} + 1\right)}{5a^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(2/3)/x^2,x]

[Out] (3*b*(a + b*x)^(5/3)*Hypergeometric2F1[5/3, 2, 8/3, 1 + (b*x)/a])/(5*a^2)

fricas [A] time = 0.53, size = 252, normalized size = 2.68

$$\frac{3 \sqrt{\frac{1}{3}} abx \sqrt{-\frac{1}{a^{\frac{2}{3}}}} \log \left(\frac{2bx+3 \sqrt{\frac{1}{3}} \left(2(bx+a)^{\frac{2}{3}} a^{\frac{2}{3}} - (bx+a)^{\frac{1}{3}} a - a^{\frac{4}{3}} \right) \sqrt{-\frac{1}{a^{\frac{2}{3}}}} - 3(bx+a)^{\frac{1}{3}} a^{\frac{2}{3}} + 3a}{x} \right) - a^{\frac{2}{3}} bx \log \left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a \right)}{3ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/x^2,x, algorithm="fricas")

[Out] [1/3*(3*sqrt(1/3)*a*b*x*sqrt(-1/a^(2/3))*log((2*b*x + 3*sqrt(1/3)*(2*(b*x + a)^(2/3)*a^(2/3) - (b*x + a)^(1/3)*a - a^(4/3))*sqrt(-1/a^(2/3)) - 3*(b*x + a)^(1/3)*a^(2/3) + 3*a)/x) - a^(2/3)*b*x*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + 2*a^(2/3)*b*x*log((b*x + a)^(1/3) - a^(1/3)) - 3*(b*x + a)^(2/3)*a)/(a*x), 1/3*(6*sqrt(1/3)*a^(2/3)*b*x*arctan(sqrt(1/3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3)) - a^(2/3)*b*x*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + 2*a^(2/3)*b*x*log((b*x + a)^(1/3) - a^(1/3)) - 3*(b*x + a)^(2/3)*a)/(a*x)]

giac [A] time = 2.29, size = 106, normalized size = 1.13

$$\frac{2 \sqrt{3} b^2 \arctan \left(\frac{\sqrt{3} \left(2(bx+a)^{\frac{1}{3}} + a^{\frac{1}{3}} \right)}{3 a^{\frac{1}{3}}} \right)}{\frac{1}{a^{\frac{1}{3}}}} - \frac{b^2 \log \left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + a^{\frac{2}{3}} \right)}{\frac{1}{a^{\frac{1}{3}}}} + \frac{2 b^2 \log \left(\left| (bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}} \right| \right)}{\frac{1}{a^{\frac{1}{3}}}} - \frac{3 (bx+a)^{\frac{2}{3}} b}{x}}{3 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/x^2,x, algorithm="giac")

[Out] 1/3*(2*sqrt(3)*b^2*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3))/a^(1/3) - b^2*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(1/3) + 2*b^2*log(abs((b*x + a)^(1/3) - a^(1/3)))/a^(1/3) - 3*(b*x + a)^(2/3)*b/x)/b

maple [A] time = 0.01, size = 92, normalized size = 0.98

$$\frac{2\sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)}{3a^{\frac{1}{3}}} + \frac{2b \ln\left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}} - \frac{b \ln\left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}}\right)}{3a^{\frac{1}{3}}} - \frac{(bx+a)^{\frac{2}{3}}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(2/3)/x^2,x)

[Out] -(b*x+a)^(2/3)/x+2/3*b/a^(1/3)*ln(-a^(1/3)+(b*x+a)^(1/3))-1/3*b/a^(1/3)*ln(a^(2/3)+(b*x+a)^(1/3)*a^(1/3)+(b*x+a)^(2/3))+2/3*b*3^(1/2)/a^(1/3)*arctan(1/3*3^(1/2)*(2*(b*x+a)^(1/3)/a^(1/3)+1))

maxima [A] time = 2.98, size = 93, normalized size = 0.99

$$\frac{2\sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{3a^{\frac{1}{3}}} - \frac{b \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{3a^{\frac{1}{3}}} + \frac{2b \log\left((bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}} - \frac{(bx+a)^{\frac{2}{3}}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/x^2,x, algorithm="maxima")

[Out] 2/3*sqrt(3)*b*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3))/a^(1/3) - 1/3*b*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(1/3) + 2/3*b*log((b*x + a)^(1/3) - a^(1/3))/a^(1/3) - (b*x + a)^(2/3)/x

mupad [B] time = 0.11, size = 127, normalized size = 1.35

$$\frac{2b \ln\left(4a^{1/3}b^2 - 4b^2(a+bx)^{1/3}\right)}{3a^{1/3}} - \frac{(a+bx)^{2/3}}{x} - \frac{\ln\left(a^{1/3}(b - \sqrt{3}b1i)^2 - 4b^2(a+bx)^{1/3}\right)}{3a^{1/3}} - \frac{(b - \sqrt{3}b1i) \ln\left(a^{1/3}\right)}{3a^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(2/3)/x^2,x)

[Out] (2*b*log(4*a^(1/3)*b^2 - 4*b^2*(a + b*x)^(1/3)))/(3*a^(1/3)) - (a + b*x)^(2/3)/x - (log(a^(1/3)*(b - 3^(1/2)*b*1i)^2 - 4*b^2*(a + b*x)^(1/3))*(b - 3^(1/2)*b*1i))/(3*a^(1/3)) - (log(a^(1/3)*(b + 3^(1/2)*b*1i)^2 - 4*b^2*(a + b*x)^(1/3))*(b + 3^(1/2)*b*1i))/(3*a^(1/3))

sympy [C] time = 2.24, size = 643, normalized size = 6.84

$$\frac{10a^{\frac{8}{3}}be^{\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{5}{3}\right)}{9a^3e^{\frac{2i\pi}{3}} \Gamma\left(\frac{8}{3}\right) - 9a^2b\left(\frac{a}{b} + x\right)e^{\frac{2i\pi}{3}} \Gamma\left(\frac{8}{3}\right)} + \frac{10a^{\frac{8}{3}}be^{-\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + xe^{\frac{2i\pi}{3}}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{5}{3}\right)}{9a^3e^{\frac{2i\pi}{3}} \Gamma\left(\frac{8}{3}\right) - 9a^2b\left(\frac{a}{b} + x\right)e^{\frac{2i\pi}{3}} \Gamma\left(\frac{8}{3}\right)} + \frac{10a^{\frac{8}{3}}b \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + xe^{\frac{4i\pi}{3}}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{5}{3}\right)}{9a^3e^{\frac{2i\pi}{3}} \Gamma\left(\frac{8}{3}\right) - 9a^2b\left(\frac{a}{b} + x\right)e^{\frac{2i\pi}{3}} \Gamma\left(\frac{8}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(2/3)/x**2,x)

[Out] $10*a^{8/3}*b*\exp(2*I*pi/3)*\log(1 - b^{1/3}*(a/b + x)^{1/3}/a^{1/3})*\text{gamma}(5/3)/(9*a^{3/3}*\exp(2*I*pi/3)*\text{gamma}(8/3) - 9*a^{2/3}*b*(a/b + x)*\exp(2*I*pi/3)*\text{gamma}(8/3)) + 10*a^{8/3}*b*\exp(-2*I*pi/3)*\log(1 - b^{1/3}*(a/b + x)^{1/3}/a^{1/3})*\exp_polar(2*I*pi/3)/a^{1/3})*\text{gamma}(5/3)/(9*a^{3/3}*\exp(2*I*pi/3)*\text{gamma}(8/3) - 9*a^{2/3}*b*(a/b + x)*\exp(2*I*pi/3)*\text{gamma}(8/3)) + 10*a^{8/3}*b*\log(1 - b^{1/3}*(a/b + x)^{1/3}/a^{1/3})*\exp_polar(4*I*pi/3)/a^{1/3})*\text{gamma}(5/3)/(9*a^{3/3}*\exp(2*I*pi/3)*\text{gamma}(8/3) - 9*a^{2/3}*b*(a/b + x)*\exp(2*I*pi/3)*\text{gamma}(8/3)) - 10*a^{5/3}*b^{2/3}*(a/b + x)*\exp(2*I*pi/3)*\log(1 - b^{1/3}*(a/b + x)^{1/3}/a^{1/3})*\text{gamma}(5/3)/(9*a^{3/3}*\exp(2*I*pi/3)*\text{gamma}(8/3) - 9*a^{2/3}*b*(a/b + x)*\exp(2*I*pi/3)*\text{gamma}(8/3)) - 10*a^{5/3}*b^{2/3}*(a/b + x)*\exp(-2*I*pi/3)*\log(1 - b^{1/3}*(a/b + x)^{1/3}/a^{1/3})*\exp_polar(2*I*pi/3)/a^{1/3})*\text{gamma}(5/3)/(9*a^{3/3}*\exp(2*I*pi/3)*\text{gamma}(8/3) - 9*a^{2/3}*b*(a/b + x)*\exp(2*I*pi/3)*\text{gamma}(8/3)) - 10*a^{5/3}*b^{2/3}*(a/b + x)*\log(1 - b^{1/3}*(a/b + x)^{1/3}/a^{1/3})*\exp_polar(4*I*pi/3)/a^{1/3})*\text{gamma}(5/3)/(9*a^{3/3}*\exp(2*I*pi/3)*\text{gamma}(8/3) - 9*a^{2/3}*b*(a/b + x)*\exp(2*I*pi/3)*\text{gamma}(8/3)) + 15*a^{2/3}*b^{5/3}*(a/b + x)^{2/3}*\exp(2*I*pi/3)*\text{gamma}(5/3)/(9*a^{3/3}*\exp(2*I*pi/3)*\text{gamma}(8/3) - 9*a^{2/3}*b*(a/b + x)*\exp(2*I*pi/3)*\text{gamma}(8/3))$

$$3.384 \quad \int \frac{(a+bx)^{2/3}}{x^3} dx$$

Optimal. Leaf size=127

$$\frac{b^2 \log(x)}{18a^{4/3}} - \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{4/3}} - \frac{b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{4/3}} - \frac{(a+bx)^{2/3}}{2x^2} - \frac{b(a+bx)^{2/3}}{3ax}$$

[Out] $-1/2*(b*x+a)^{(2/3)}/x^2-1/3*b*(b*x+a)^{(2/3)}/a/x+1/18*b^2*\ln(x)/a^{(4/3)}-1/6*b^{2*}\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(4/3)}-1/9*b^2*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}}/a^{(4/3)*3^{(1/2)}})$

Rubi [A] time = 0.05, antiderivative size = 127, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.462$, Rules used = {47, 51, 55, 617, 204, 31}

$$\frac{b^2 \log(x)}{18a^{4/3}} - \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{4/3}} - \frac{b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{4/3}} - \frac{(a+bx)^{2/3}}{2x^2} - \frac{b(a+bx)^{2/3}}{3ax}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(2/3)/x^3, x]

[Out] $-(a + b*x)^{(2/3)}/(2*x^2) - (b*(a + b*x)^{(2/3)})/(3*a*x) - (b^2*ArcTan[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(Sqrt[3]*a^{(1/3)})])/(3*Sqrt[3]*a^{(4/3)}) + (b^2*Log[x])/(18*a^{(4/3)}) - (b^2*Log[a^{(1/3)} - (a + b*x)^{(1/3)}])/(6*a^{(4/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] :> Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 55

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x
] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)],
x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])] /;
FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{2/3}}{x^3} dx &= -\frac{(a+bx)^{2/3}}{2x^2} + \frac{1}{3}b \int \frac{1}{x^2 \sqrt[3]{a+bx}} dx \\
&= -\frac{(a+bx)^{2/3}}{2x^2} - \frac{b(a+bx)^{2/3}}{3ax} - \frac{b^2 \int \frac{1}{x \sqrt[3]{a+bx}} dx}{9a} \\
&= -\frac{(a+bx)^{2/3}}{2x^2} - \frac{b(a+bx)^{2/3}}{3ax} + \frac{b^2 \log(x)}{18a^{4/3}} + \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{6a^{4/3}} - \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{6a^{4/3}} \\
&= -\frac{(a+bx)^{2/3}}{2x^2} - \frac{b(a+bx)^{2/3}}{3ax} + \frac{b^2 \log(x)}{18a^{4/3}} - \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{4/3}} + \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{a+bx}\right)}{3a^{4/3}} \\
&= -\frac{(a+bx)^{2/3}}{2x^2} - \frac{b(a+bx)^{2/3}}{3ax} - \frac{b^2 \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{3\sqrt{3}a^{4/3}} + \frac{b^2 \log(x)}{18a^{4/3}} - \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{4/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.28

$$-\frac{3b^2(a+bx)^{5/3} {}_2F_1\left(\frac{5}{3}, 3; \frac{8}{3}; \frac{bx}{a} + 1\right)}{5a^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(2/3)/x^3, x]

[Out] (-3*b^2*(a + b*x)^(5/3)*Hypergeometric2F1[5/3, 3, 8/3, 1 + (b*x)/a])/(5*a^3)

fricas [A] time = 0.51, size = 350, normalized size = 2.76

$$\left[3 \sqrt{\frac{1}{3}} ab^2 x^2 \sqrt{\frac{(-a)^{1/3}}{a}} \log \left(\frac{2bx-3 \sqrt{\frac{1}{3}} \left(2(bx+a)^{2/3} (-a)^{2/3} - (bx+a)^{1/3} a + (-a)^{1/3} a \right) \sqrt{\frac{(-a)^{1/3}}{a}} - 3(bx+a)^{1/3} (-a)^{2/3} + 3a}{x}} \right) + (-a)^{2/3} b^2 x^2 \log((bx+a)^{1/3}) \right] / 18a^2 x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/x^3,x, algorithm="fricas")

[Out] [1/18*(3*sqrt(1/3)*a*b^2*x^2*sqrt((-a)^(1/3)/a)*log((2*b*x - 3*sqrt(1/3)*(2*(b*x + a)^(2/3)*(-a)^(2/3) - (b*x + a)^(1/3)*a + (-a)^(1/3)*a)*sqrt((-a)^(1/3)/a) - 3*(b*x + a)^(1/3)*(-a)^(2/3) + 3*a)/x) + (-a)^(2/3)*b^2*x^2*log((b*x + a)^(2/3) - (b*x + a)^(1/3)*(-a)^(1/3) + (-a)^(2/3)) - 2*(-a)^(2/3)*b^2*x^2*log((b*x + a)^(1/3) + (-a)^(1/3)) - 3*(2*a*b*x + 3*a^2)*(b*x + a)^(2/3))/(a^2*x^2), -1/18*(6*sqrt(1/3)*a*b^2*x^2*sqrt(-(-a)^(1/3)/a)*arctan(sqrt(1/3)*(2*(b*x + a)^(1/3) - (-a)^(1/3))*sqrt(-(-a)^(1/3)/a)) - (-a)^(2/3)*b^2*x^2*log((b*x + a)^(2/3) - (b*x + a)^(1/3)*(-a)^(1/3) + (-a)^(2/3)) + 2*(-a)^(2/3)*b^2*x^2*log((b*x + a)^(1/3) + (-a)^(1/3)) + 3*(2*a*b*x + 3*a^2)*(b*x + a)^(2/3))/(a^2*x^2)]

giac [A] time = 2.47, size = 129, normalized size = 1.02

$$\frac{2\sqrt{3}b^3 \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right) - b^3 \log\left(\frac{(bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}}{a^{\frac{4}{3}}}\right) + 2b^3 \log\left(\frac{(bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}}{a^{\frac{4}{3}}}\right) + \frac{3\left(2(bx+a)^{\frac{5}{3}}b^3+(bx+a)^{\frac{2}{3}}ab^3\right)}{ab^2x^2}}{18b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/x^3,x, algorithm="giac")

[Out] -1/18*(2*sqrt(3)*b^3*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3))/a^(4/3) - b^3*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(4/3) + 2*b^3*log(abs((b*x + a)^(1/3) - a^(1/3)))/a^(4/3) + 3*(2*(b*x + a)^(5/3)*b^3 + (b*x + a)^(2/3)*a*b^3)/(a*b^2*x^2)/b

maple [A] time = 0.01, size = 113, normalized size = 0.89

$$\frac{\sqrt{3} b^2 \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right) - b^2 \ln\left(-a^{\frac{1}{3}}+(bx+a)^{\frac{1}{3}}\right) + b^2 \ln\left(a^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+(bx+a)^{\frac{2}{3}}\right) - \frac{(bx+a)^{\frac{2}{3}}}{6x^2}}{9a^{\frac{4}{3}} - 9a^{\frac{4}{3}} + 18a^{\frac{4}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(2/3)/x^3,x)

[Out] -1/3/x^2/a*(b*x+a)^(5/3)-1/6*(b*x+a)^(2/3)/x^2-1/9*b^2/a^(4/3)*ln(-a^(1/3)+(b*x+a)^(1/3))+1/18*b^2/a^(4/3)*ln(a^(2/3)+(b*x+a)^(1/3)*a^(1/3)+(b*x+a)^(2/3))

/3)) - 1/9*b^2/a^(4/3)*3^(1/2)*arctan(1/3*3^(1/2)*(2*(b*x+a)^(1/3)/a^(1/3)+1))

maxima [A] time = 2.98, size = 139, normalized size = 1.09

$$\frac{\sqrt{3} b^2 \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{9a^{\frac{4}{3}}} + \frac{b^2 \log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)}{18a^{\frac{4}{3}}} - \frac{b^2 \log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)}{9a^{\frac{4}{3}}} - \frac{2(bx+a)^{\frac{5}{3}}}{6((bx+a)^2 a^{\frac{1}{3}})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/x^3,x, algorithm="maxima")

[Out] -1/9*sqrt(3)*b^2*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3))/a^(4/3) + 1/18*b^2*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(4/3) - 1/9*b^2*log((b*x + a)^(1/3) - a^(1/3))/a^(4/3) - 1/6*(2*(b*x + a)^(5/3)*b^2 + (b*x + a)^(2/3)*a*b^2)/((b*x + a)^2*a - 2*(b*x + a)*a^2 + a^3)

mupad [B] time = 0.33, size = 194, normalized size = 1.53

$$\frac{(-1)^{1/3} b^2 \ln\left((a+bx)^{1/3} - (-1)^{2/3} a^{1/3}\right)}{9a^{4/3}} - \frac{\frac{b^2(a+bx)^{2/3}}{6} + \frac{b^2(a+bx)^{5/3}}{3a}}{(a+bx)^2 - 2a(a+bx) + a^2} + \frac{(-1)^{1/3} b^2 \ln\left(\frac{b^4(a+bx)^{1/3}}{9a^2} - \frac{(-1)^{2/3} b^4\left(-\frac{1}{2} + \frac{\sqrt{3}}{2}\right)}{9a^{5/3}}\right)}{9a^{4/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(2/3)/x^3,x)

[Out] ((-1)^(1/3)*b^2*log((a + b*x)^(1/3) - (-1)^(2/3)*a^(1/3))/(9*a^(4/3)) - ((b^2*(a + b*x)^(2/3))/6 + (b^2*(a + b*x)^(5/3))/(3*a))/((a + b*x)^2 - 2*a*(a + b*x) + a^2) + ((-1)^(1/3)*b^2*log((b^4*(a + b*x)^(1/3))/(9*a^2) - ((-1)^(2/3)*b^4*((3^(1/2)*1i)/2 - 1/2)^2)/(9*a^(5/3)))*((3^(1/2)*1i)/2 - 1/2)/(9*a^(4/3)) - ((-1)^(1/3)*b^2*log((b^4*(a + b*x)^(1/3))/(9*a^2) - ((-1)^(2/3)*b^4*((3^(1/2)*1i)/2 + 1/2)^2)/(9*a^(5/3)))*((3^(1/2)*1i)/2 + 1/2)/(9*a^(4/3))

sympy [C] time = 2.65, size = 2266, normalized size = 17.84

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

$$\begin{aligned}
& a/b + x)^{**3} \exp(2*I*pi/3) \gamma(8/3) + 10*a^{**8/3} * b^{**5} (a/b + x)^{**3} \log(1 \\
& - b^{**1/3} (a/b + x)^{**1/3} \exp_polar(4*I*pi/3) / a^{**1/3}) \gamma(5/3) / (54*a \\
& **7 \exp(2*I*pi/3) \gamma(8/3) - 162*a^{**6} * b (a/b + x) \exp(2*I*pi/3) \gamma(8/3 \\
&) + 162*a^{**5} * b^{**2} (a/b + x)^{**2} \exp(2*I*pi/3) \gamma(8/3) - 54*a^{**4} * b^{**3} (a/b \\
& + x)^{**3} \exp(2*I*pi/3) \gamma(8/3) - 15*a^{**5} * b^{**8/3} (a/b + x)^{**2/3} \exp(\\
& 2*I*pi/3) \gamma(5/3) / (54*a^{**7} \exp(2*I*pi/3) \gamma(8/3) - 162*a^{**6} * b (a/b + \\
& x) \exp(2*I*pi/3) \gamma(8/3) + 162*a^{**5} * b^{**2} (a/b + x)^{**2} \exp(2*I*pi/3) \gamma \\
& a(8/3) - 54*a^{**4} * b^{**3} (a/b + x)^{**3} \exp(2*I*pi/3) \gamma(8/3)) - 15*a^{**4} * b^{** \\
& (11/3) (a/b + x)^{**5/3} \exp(2*I*pi/3) \gamma(5/3) / (54*a^{**7} \exp(2*I*pi/3) \gamma \\
& a(8/3) - 162*a^{**6} * b (a/b + x) \exp(2*I*pi/3) \gamma(8/3) + 162*a^{**5} * b^{**2} (a/b \\
& + x)^{**2} \exp(2*I*pi/3) \gamma(8/3) - 54*a^{**4} * b^{**3} (a/b + x)^{**3} \exp(2*I*pi/3) \\
& * \gamma(8/3)) + 30*a^{**3} * b^{**14/3} (a/b + x)^{**8/3} \exp(2*I*pi/3) \gamma(5/3) / \\
& (54*a^{**7} \exp(2*I*pi/3) \gamma(8/3) - 162*a^{**6} * b (a/b + x) \exp(2*I*pi/3) \gamma \\
& a(8/3) + 162*a^{**5} * b^{**2} (a/b + x)^{**2} \exp(2*I*pi/3) \gamma(8/3) - 54*a^{**4} * b^{**3} \\
& * (a/b + x)^{**3} \exp(2*I*pi/3) \gamma(8/3))
\end{aligned}$$

3.385 $\int x^3(a + bx)^{4/3} dx$

Optimal. Leaf size=72

$$-\frac{3a^3(a + bx)^{7/3}}{7b^4} + \frac{9a^2(a + bx)^{10/3}}{10b^4} + \frac{3(a + bx)^{16/3}}{16b^4} - \frac{9a(a + bx)^{13/3}}{13b^4}$$

[Out] $-3/7*a^3*(b*x+a)^{(7/3)}/b^4+9/10*a^2*(b*x+a)^{(10/3)}/b^4-9/13*a*(b*x+a)^{(13/3)}/b^4+3/16*(b*x+a)^{(16/3)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9a^2(a + bx)^{10/3}}{10b^4} - \frac{3a^3(a + bx)^{7/3}}{7b^4} + \frac{3(a + bx)^{16/3}}{16b^4} - \frac{9a(a + bx)^{13/3}}{13b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^(4/3), x]

[Out] $(-3*a^3*(a + b*x)^{(7/3)})/(7*b^4) + (9*a^2*(a + b*x)^{(10/3)})/(10*b^4) - (9*a*(a + b*x)^{(13/3)})/(13*b^4) + (3*(a + b*x)^{(16/3)})/(16*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^{4/3} dx &= \int \left(-\frac{a^3(a + bx)^{4/3}}{b^3} + \frac{3a^2(a + bx)^{7/3}}{b^3} - \frac{3a(a + bx)^{10/3}}{b^3} + \frac{(a + bx)^{13/3}}{b^3} \right) dx \\ &= -\frac{3a^3(a + bx)^{7/3}}{7b^4} + \frac{9a^2(a + bx)^{10/3}}{10b^4} - \frac{9a(a + bx)^{13/3}}{13b^4} + \frac{3(a + bx)^{16/3}}{16b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.64

$$\frac{3(a + bx)^{7/3} (-81a^3 + 189a^2bx - 315ab^2x^2 + 455b^3x^3)}{7280b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^(4/3), x]

[Out] (3*(a + b*x)^(7/3)*(-81*a^3 + 189*a^2*b*x - 315*a*b^2*x^2 + 455*b^3*x^3))/(7280*b^4)

fricas [A] time = 0.50, size = 64, normalized size = 0.89

$$\frac{3 \left(455 b^5 x^5 + 595 a b^4 x^4 + 14 a^2 b^3 x^3 - 18 a^3 b^2 x^2 + 27 a^4 b x - 81 a^5 \right) (b x + a)^{\frac{1}{3}}}{7280 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(4/3), x, algorithm="fricas")

[Out] 3/7280*(455*b^5*x^5 + 595*a*b^4*x^4 + 14*a^2*b^3*x^3 - 18*a^3*b^2*x^2 + 27*a^4*b*x - 81*a^5)*(b*x + a)^(1/3)/b^4

giac [B] time = 1.22, size = 193, normalized size = 2.68

$$3 \left(\frac{52 \left(14 (b x + a)^{\frac{10}{3}} - 60 (b x + a)^{\frac{7}{3}} a + 105 (b x + a)^{\frac{4}{3}} a^2 - 140 (b x + a)^{\frac{1}{3}} a^3 \right) a^2}{b^3} + \frac{32 \left(35 (b x + a)^{\frac{13}{3}} - 182 (b x + a)^{\frac{10}{3}} a + 390 (b x + a)^{\frac{7}{3}} a^2 - 455 (b x + a)^{\frac{4}{3}} a^3 + 455 (b x + a)^{\frac{1}{3}} a^4 \right) a}{b^3} \right) / 7280 b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(4/3), x, algorithm="giac")

[Out] 3/7280*(52*(14*(b*x + a)^(10/3) - 60*(b*x + a)^(7/3)*a + 105*(b*x + a)^(4/3)*a^2 - 140*(b*x + a)^(1/3)*a^3)*a^2/b^3 + 32*(35*(b*x + a)^(13/3) - 182*(b*x + a)^(10/3)*a + 390*(b*x + a)^(7/3)*a^2 - 455*(b*x + a)^(4/3)*a^3 + 455*(b*x + a)^(1/3)*a^4)*a/b^3 + 5*(91*(b*x + a)^(16/3) - 560*(b*x + a)^(13/3)*a + 1456*(b*x + a)^(10/3)*a^2 - 2080*(b*x + a)^(7/3)*a^3 + 1820*(b*x + a)^(4/3)*a^4 - 1456*(b*x + a)^(1/3)*a^5)/b^3)/b

maple [A] time = 0.01, size = 43, normalized size = 0.60

$$\frac{3 (b x + a)^{\frac{7}{3}} \left(-455 b^3 x^3 + 315 a b^2 x^2 - 189 a^2 b x + 81 a^3 \right)}{7280 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^(4/3), x)

[Out] -3/7280*(b*x+a)^(7/3)*(-455*b^3*x^3+315*a*b^2*x^2-189*a^2*b*x+81*a^3)/b^4

maxima [A] time = 1.36, size = 56, normalized size = 0.78

$$\frac{3(bx+a)^{\frac{16}{3}}}{16b^4} - \frac{9(bx+a)^{\frac{13}{3}}a}{13b^4} + \frac{9(bx+a)^{\frac{10}{3}}a^2}{10b^4} - \frac{3(bx+a)^{\frac{7}{3}}a^3}{7b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^(4/3),x, algorithm="maxima")

[Out] 3/16*(b*x + a)^(16/3)/b^4 - 9/13*(b*x + a)^(13/3)*a/b^4 + 9/10*(b*x + a)^(10/3)*a^2/b^4 - 3/7*(b*x + a)^(7/3)*a^3/b^4

mupad [B] time = 0.05, size = 56, normalized size = 0.78

$$\frac{3(a+bx)^{16/3}}{16b^4} - \frac{3a^3(a+bx)^{7/3}}{7b^4} + \frac{9a^2(a+bx)^{10/3}}{10b^4} - \frac{9a(a+bx)^{13/3}}{13b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(a + b*x)^(4/3),x)

[Out] (3*(a + b*x)^(16/3))/(16*b^4) - (3*a^3*(a + b*x)^(7/3))/(7*b^4) + (9*a^2*(a + b*x)^(10/3))/(10*b^4) - (9*a*(a + b*x)^(13/3))/(13*b^4)

sympy [B] time = 3.18, size = 1844, normalized size = 25.61

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**(4/3),x)

[Out] -243*a**(76/3)*(1 + b*x/a)**(1/3)/(7280*a**20*b**4 + 43680*a**19*b**5*x + 109200*a**18*b**6*x**2 + 145600*a**17*b**7*x**3 + 109200*a**16*b**8*x**4 + 43680*a**15*b**9*x**5 + 7280*a**14*b**10*x**6) + 243*a**(76/3)/(7280*a**20*b**4 + 43680*a**19*b**5*x + 109200*a**18*b**6*x**2 + 145600*a**17*b**7*x**3 + 109200*a**16*b**8*x**4 + 43680*a**15*b**9*x**5 + 7280*a**14*b**10*x**6) - 1377*a**(73/3)*b*x*(1 + b*x/a)**(1/3)/(7280*a**20*b**4 + 43680*a**19*b**5*x + 109200*a**18*b**6*x**2 + 145600*a**17*b**7*x**3 + 109200*a**16*b**8*x**4 + 43680*a**15*b**9*x**5 + 7280*a**14*b**10*x**6) + 1458*a**(73/3)*b*x/(7280*a**20*b**4 + 43680*a**19*b**5*x + 109200*a**18*b**6*x**2 + 145600*a**17*b**7*x**3 + 109200*a**16*b**8*x**4 + 43680*a**15*b**9*x**5 + 7280*a**14*b**10*x**6) - 3213*a**(70/3)*b**2*x**2*(1 + b*x/a)**(1/3)/(7280*a**20*b**4 + 43680*a**19*b**5*x + 109200*a**18*b**6*x**2 + 145600*a**17*b**7*x**3 + 109200*a**16*b**8*x**4 + 43680*a**15*b**9*x**5 + 7280*a**14*b**10*x**6) + 3645*a**(70/3)*b**2*x**2/(7280*a**20*b**4 + 43680*a**19*b**5*x + 109200*a**18*b**6*x**2 + 145600*a**17*b**7*x**3 + 109200*a**16*b**8*x**4 + 43680*a**15*b**9*x**5 + 7280*a**14*b**10*x**6)

$$\begin{aligned}
& 6x^{**2} + 145600a^{**17}b^{**7}x^{**3} + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9} \\
& x^{**5} + 7280a^{**14}b^{**10}x^{**6}) - 3927a^{**67/3}b^{**3}x^{**3}(1 + b*x/a)^{(1/3)} \\
&)/(7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} \\
& + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6}) + 4860a^{**67/3}b^{**3}x^{**3} \\
& / (7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} \\
& + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6}) - 798a^{**64/3}b^{**4}x^{**4} \\
& **4(1 + b*x/a)^{(1/3)} / (7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} \\
& + 145600a^{**17}b^{**7}x^{**3} + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6}) \\
& + 3645a^{**64/3}b^{**4}x^{**4} / (7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} \\
& + 145600a^{**17}b^{**7}x^{**3} + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6}) \\
& + 11382a^{**61/3}b^{**5}x^{**5}(1 + b*x/a)^{(1/3)} / (7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x \\
& + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} \\
& + 7280a^{**14}b^{**10}x^{**6}) + 1458a^{**61/3}b^{**5}x^{**5} / (7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x \\
& + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} \\
& + 7280a^{**14}b^{**10}x^{**6}) + 35238a^{**58/3}b^{**6}x^{**6}(1 + b*x/a)^{(1/3)} / (7280a^{**20}b^{**4} \\
& + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} + 109200a^{**16}b^{**8}x^{**4} \\
& + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6}) + 243a^{**58/3}b^{**6}x^{**6} / (7280a^{**20}b^{**4} \\
& + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} + 109200a^{**16}b^{**8}x^{**4} \\
& + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6}) + 56562a^{**55/3}b^{**7}x^{**7}(1 + b*x/a)^{(1/3)} \\
& / (7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} \\
& + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6}) + 54273a^{**52/3}b^{**8}x^{**8} \\
& (1 + b*x/a)^{(1/3)} / (7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} \\
& + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6}) + 31227a^{**49/3}b^{**9}x^{**9} \\
& (1 + b*x/a)^{(1/3)} / (7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} \\
& + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6}) + 9975a^{**46/3}b^{**10}x^{**10} \\
& (1 + b*x/a)^{(1/3)} / (7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} \\
& + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6}) + 1365a^{**43/3}b^{**11}x^{**11} \\
& (1 + b*x/a)^{(1/3)} / (7280a^{**20}b^{**4} + 43680a^{**19}b^{**5}x + 109200a^{**18}b^{**6}x^{**2} + 145600a^{**17}b^{**7}x^{**3} \\
& + 109200a^{**16}b^{**8}x^{**4} + 43680a^{**15}b^{**9}x^{**5} + 7280a^{**14}b^{**10}x^{**6})
\end{aligned}$$

3.386 $\int x^2(a + bx)^{4/3} dx$

Optimal. Leaf size=53

$$\frac{3a^2(a + bx)^{7/3}}{7b^3} + \frac{3(a + bx)^{13/3}}{13b^3} - \frac{3a(a + bx)^{10/3}}{5b^3}$$

[Out] $3/7*a^2*(b*x+a)^{(7/3)}/b^3-3/5*a*(b*x+a)^{(10/3)}/b^3+3/13*(b*x+a)^{(13/3)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3a^2(a + bx)^{7/3}}{7b^3} + \frac{3(a + bx)^{13/3}}{13b^3} - \frac{3a(a + bx)^{10/3}}{5b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*x)^(4/3), x]

[Out] $(3*a^2*(a + b*x)^{(7/3)})/(7*b^3) - (3*a*(a + b*x)^{(10/3)})/(5*b^3) + (3*(a + b*x)^{(13/3)})/(13*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^{4/3} dx &= \int \left(\frac{a^2(a + bx)^{4/3}}{b^2} - \frac{2a(a + bx)^{7/3}}{b^2} + \frac{(a + bx)^{10/3}}{b^2} \right) dx \\ &= \frac{3a^2(a + bx)^{7/3}}{7b^3} - \frac{3a(a + bx)^{10/3}}{5b^3} + \frac{3(a + bx)^{13/3}}{13b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.66

$$\frac{3(a + bx)^{7/3} (9a^2 - 21abx + 35b^2x^2)}{455b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^(4/3), x]

[Out] $(3*(a + b*x)^(7/3)*(9*a^2 - 21*a*b*x + 35*b^2*x^2))/(455*b^3)$

fricas [A] time = 0.52, size = 53, normalized size = 1.00

$$\frac{3(35b^4x^4 + 49ab^3x^3 + 2a^2b^2x^2 - 3a^3bx + 9a^4)(bx + a)^{\frac{1}{3}}}{455b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(4/3), x, algorithm="fricas")

[Out] $3/455*(35*b^4*x^4 + 49*a*b^3*x^3 + 2*a^2*b^2*x^2 - 3*a^3*b*x + 9*a^4)*(b*x + a)^(1/3)/b^3$

giac [B] time = 0.98, size = 157, normalized size = 2.96

$$3 \left(\frac{65 \left(2(bx+a)^{\frac{7}{3}} - 7(bx+a)^{\frac{4}{3}}a + 14(bx+a)^{\frac{1}{3}}a^2 \right) a^2}{b^2} + \frac{13 \left(14(bx+a)^{\frac{10}{3}} - 60(bx+a)^{\frac{7}{3}}a + 105(bx+a)^{\frac{4}{3}}a^2 - 140(bx+a)^{\frac{1}{3}}a^3 \right) a}{b^2} + \frac{2 \left(35(bx+a)^{\frac{13}{3}} - 182(bx+a)^{\frac{10}{3}}a + 390(bx+a)^{\frac{7}{3}}a^2 - 455(bx+a)^{\frac{4}{3}}a^3 + 455(bx+a)^{\frac{1}{3}}a^4 \right)}{b^2} \right) / 910b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(4/3), x, algorithm="giac")

[Out] $3/910*(65*(2*(b*x + a)^(7/3) - 7*(b*x + a)^(4/3)*a + 14*(b*x + a)^(1/3)*a^2)*a^2/b^2 + 13*(14*(b*x + a)^(10/3) - 60*(b*x + a)^(7/3)*a + 105*(b*x + a)^(4/3)*a^2 - 140*(b*x + a)^(1/3)*a^3)*a/b^2 + 2*(35*(b*x + a)^(13/3) - 182*(b*x + a)^(10/3)*a + 390*(b*x + a)^(7/3)*a^2 - 455*(b*x + a)^(4/3)*a^3 + 455*(b*x + a)^(1/3)*a^4)/b^2)/b$

maple [A] time = 0.00, size = 32, normalized size = 0.60

$$\frac{3(bx + a)^{\frac{7}{3}}(35b^2x^2 - 21abx + 9a^2)}{455b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^(4/3), x)

[Out] $3/455*(b*x+a)^(7/3)*(35*b^2*x^2-21*a*b*x+9*a^2)/b^3$

maxima [A] time = 1.30, size = 41, normalized size = 0.77

$$\frac{3(bx + a)^{\frac{13}{3}}}{13b^3} - \frac{3(bx + a)^{\frac{10}{3}}a}{5b^3} + \frac{3(bx + a)^{\frac{7}{3}}a^2}{7b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^(4/3),x, algorithm="maxima")

[Out] $3/13*(b*x + a)^{(13/3)}/b^3 - 3/5*(b*x + a)^{(10/3)}*a/b^3 + 3/7*(b*x + a)^{(7/3)}*a^2/b^3$

mupad [B] time = 0.04, size = 37, normalized size = 0.70

$$\frac{105(a+bx)^{13/3} - 273a(a+bx)^{10/3} + 195a^2(a+bx)^{7/3}}{455b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a + b*x)^(4/3),x)

[Out] $(105*(a + b*x)^{(13/3)} - 273*a*(a + b*x)^{(10/3)} + 195*a^2*(a + b*x)^{(7/3)})/(455*b^3)$

sympy [B] time = 2.16, size = 733, normalized size = 13.83

$$\frac{27a^{\frac{37}{3}} \sqrt[3]{1 + \frac{bx}{a}}}{455a^8b^3 + 1365a^7b^4x + 1365a^6b^5x^2 + 455a^5b^6x^3} - \frac{27a^{\frac{37}{3}}}{455a^8b^3 + 1365a^7b^4x + 1365a^6b^5x^2 + 455a^5b^6x^3} + \frac{1}{455a^8b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)**(4/3),x)

[Out] $27*a^{(37/3)}*(1 + b*x/a)^{(1/3)}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) - 27*a^{(37/3)}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) + 72*a^{(34/3)}*b*x*(1 + b*x/a)^{(1/3)}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) - 81*a^{(34/3)}*b*x/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) + 60*a^{(31/3)}*b^{**2}*x^{**2}*(1 + b*x/a)^{(1/3)}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) - 81*a^{(31/3)}*b^{**2}*x^{**2}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) + 165*a^{(28/3)}*b^{**3}*x^{**3}*(1 + b*x/a)^{(1/3)}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) - 27*a^{(28/3)}*b^{**3}*x^{**3}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) + 555*a^{(25/3)}*b^{**4}*x^{**4}*(1 + b*x/a)^{(1/3)}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) + 762*a^{(22/3)}*b^{**5}*x^{**5}*(1 + b*x/a)^{(1/3)}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) + 462*a^{(19/3)}*b^{**6}*x^{**6}*(1 + b*x/a)^{(1/3)}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3}) + 105*a^{(16/3)}*b^{**7}*x^{**7}*(1 + b*x/a)^{(1/3)}/(455*a^{**8}*b^{**3} + 1365*a^{**7}*b^{**4}*x + 1365*a^{**6}*b^{**5}*x^{**2} + 455*a^{**5}*b^{**6}*x^{**3})$

3.387 $\int x(a + bx)^{4/3} dx$

Optimal. Leaf size=34

$$\frac{3(a + bx)^{10/3}}{10b^2} - \frac{3a(a + bx)^{7/3}}{7b^2}$$

[Out] $-3/7*a*(b*x+a)^{(7/3)}/b^2+3/10*(b*x+a)^{(10/3)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3(a + bx)^{10/3}}{10b^2} - \frac{3a(a + bx)^{7/3}}{7b^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^(4/3), x]

[Out] $(-3*a*(a + b*x)^{(7/3)})/(7*b^2) + (3*(a + b*x)^{(10/3)})/(10*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x(a + bx)^{4/3} dx &= \int \left(-\frac{a(a + bx)^{4/3}}{b} + \frac{(a + bx)^{7/3}}{b} \right) dx \\ &= -\frac{3a(a + bx)^{7/3}}{7b^2} + \frac{3(a + bx)^{10/3}}{10b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.71

$$\frac{3(a + bx)^{7/3}(7bx - 3a)}{70b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^(4/3), x]

[Out] $(3*(a + b*x)^{(7/3)*(-3*a + 7*b*x)})/(70*b^2)$

fricas [A] time = 0.45, size = 41, normalized size = 1.21

$$\frac{3(7b^3x^3 + 11ab^2x^2 + a^2bx - 3a^3)(bx + a)^{\frac{1}{3}}}{70b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(4/3),x, algorithm="fricas")`

[Out] $3/70*(7*b^3*x^3 + 11*a*b^2*x^2 + a^2*b*x - 3*a^3)*(b*x + a)^{(1/3)}/b^2$

giac [B] time = 1.02, size = 118, normalized size = 3.47

$$3 \left(\frac{35 \left((bx+a)^{\frac{4}{3}} - 4(bx+a)^{\frac{1}{3}}a \right) a^2}{b} + \frac{20 \left(2(bx+a)^{\frac{7}{3}} - 7(bx+a)^{\frac{4}{3}}a + 14(bx+a)^{\frac{1}{3}}a^2 \right) a}{b} + \frac{14(bx+a)^{\frac{10}{3}} - 60(bx+a)^{\frac{7}{3}}a + 105(bx+a)^{\frac{4}{3}}a^2 - 140(bx+a)^{\frac{1}{3}}a^3}{b} \right) \frac{1}{140b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^(4/3),x, algorithm="giac")`

[Out] $3/140*(35*((b*x + a)^{(4/3)} - 4*(b*x + a)^{(1/3)}*a)*a^2/b + 20*(2*(b*x + a)^{(7/3)} - 7*(b*x + a)^{(4/3)}*a + 14*(b*x + a)^{(1/3)}*a^2)*a/b + (14*(b*x + a)^{(10/3)} - 60*(b*x + a)^{(7/3)}*a + 105*(b*x + a)^{(4/3)}*a^2 - 140*(b*x + a)^{(1/3)}*a^3)/b)/b$

maple [A] time = 0.00, size = 21, normalized size = 0.62

$$\frac{3(bx + a)^{\frac{7}{3}}(-7bx + 3a)}{70b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)^(4/3),x)`

[Out] $-3/70*(b*x+a)^{(7/3)*(-7*b*x+3*a)}/b^2$

maxima [A] time = 1.29, size = 26, normalized size = 0.76

$$\frac{3(bx + a)^{\frac{10}{3}}}{10b^2} - \frac{3(bx + a)^{\frac{7}{3}}a}{7b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^(4/3),x, algorithm="maxima")

[Out] $\frac{3}{10}(bx + a)^{10/3}/b^2 - \frac{3}{7}(bx + a)^{7/3} * a/b^2$

mupad [B] time = 0.03, size = 25, normalized size = 0.74

$$-\frac{30 a (a + b x)^{7/3} - 21 (a + b x)^{10/3}}{70 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a + b*x)^(4/3),x)

[Out] $-(30*a*(a + b*x)^{7/3} - 21*(a + b*x)^{10/3})/(70*b^2)$

sympy [A] time = 1.49, size = 80, normalized size = 2.35

$$\begin{cases} -\frac{9a^3 \sqrt[3]{a+bx}}{70b^2} + \frac{3a^2x \sqrt[3]{a+bx}}{70b} + \frac{33ax^2 \sqrt[3]{a+bx}}{70} + \frac{3bx^3 \sqrt[3]{a+bx}}{10} & \text{for } b \neq 0 \\ \frac{a^{\frac{4}{3}}x^2}{2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)**(4/3),x)

[Out] Piecewise((-9*a**3*(a + b*x)**(1/3)/(70*b**2) + 3*a**2*x*(a + b*x)**(1/3)/(70*b) + 33*a*x**2*(a + b*x)**(1/3)/70 + 3*b*x**3*(a + b*x)**(1/3)/10, Ne(b, 0)), (a**(4/3)*x**2/2, True))

3.388 $\int (a + bx)^{4/3} dx$

Optimal. Leaf size=16

$$\frac{3(a + bx)^{7/3}}{7b}$$

[Out] 3/7*(b*x+a)^(7/3)/b

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{3(a + bx)^{7/3}}{7b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(4/3), x]

[Out] (3*(a + b*x)^(7/3))/(7*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^{4/3} dx = \frac{3(a + bx)^{7/3}}{7b}$$

Mathematica [A] time = 0.01, size = 16, normalized size = 1.00

$$\frac{3(a + bx)^{7/3}}{7b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(4/3), x]

[Out] (3*(a + b*x)^(7/3))/(7*b)

fricas [B] time = 0.51, size = 28, normalized size = 1.75

$$\frac{3(b^2x^2 + 2abx + a^2)(bx + a)^{\frac{1}{3}}}{7b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3),x, algorithm="fricas")

[Out] $3/7*(b^2*x^2 + 2*a*b*x + a^2)*(b*x + a)^{(1/3)}/b$

giac [B] time = 1.25, size = 58, normalized size = 3.62

$$\frac{3 \left(2 (bx + a)^{\frac{7}{3}} - 7 (bx + a)^{\frac{4}{3}} a + 28 (bx + a)^{\frac{1}{3}} a^2 + 7 \left((bx + a)^{\frac{4}{3}} - 4 (bx + a)^{\frac{1}{3}} a \right) a \right)}{14b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3),x, algorithm="giac")

[Out] $3/14*(2*(b*x + a)^{(7/3)} - 7*(b*x + a)^{(4/3)}*a + 28*(b*x + a)^{(1/3)}*a^2 + 7*((b*x + a)^{(4/3)} - 4*(b*x + a)^{(1/3)}*a)*a)/b$

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{3 (bx + a)^{\frac{7}{3}}}{7b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(4/3),x)

[Out] $3/7*(b*x+a)^{(7/3)}/b$

maxima [A] time = 1.33, size = 12, normalized size = 0.75

$$\frac{3 (bx + a)^{\frac{7}{3}}}{7b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3),x, algorithm="maxima")

[Out] $3/7*(b*x + a)^{(7/3)}/b$

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{3 (a + bx)^{7/3}}{7b}$$

Verification of antiderivative is not currently implemented for this CAS.


```
[In] int((a + b*x)^(4/3),x)
```

```
[Out] (3*(a + b*x)^(7/3))/(7*b)
```

sympy [A] time = 0.07, size = 12, normalized size = 0.75

$$\frac{3(a + bx)^{\frac{7}{3}}}{7b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(4/3),x)
```

```
[Out] 3*(a + b*x)**(7/3)/(7*b)
```

$$3.389 \quad \int \frac{(a+bx)^{4/3}}{x} dx$$

Optimal. Leaf size=105

$$\frac{3}{2}a^{4/3} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) - \sqrt{3}a^{4/3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right) - \frac{1}{2}a^{4/3} \log(x) + 3a\sqrt[3]{a+bx} + \frac{3}{4}(a+bx)^{4/3}$$

[Out] 3*a*(b*x+a)^(1/3)+3/4*(b*x+a)^(4/3)-1/2*a^(4/3)*ln(x)+3/2*a^(4/3)*ln(a^(1/3)-(b*x+a)^(1/3))-a^(4/3)*arctan(1/3*(a^(1/3)+2*(b*x+a)^(1/3))/a^(1/3)*3^(1/2))*3^(1/2)

Rubi [A] time = 0.04, antiderivative size = 105, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {50, 57, 617, 204, 31}

$$\frac{3}{2}a^{4/3} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) - \sqrt{3}a^{4/3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right) - \frac{1}{2}a^{4/3} \log(x) + 3a\sqrt[3]{a+bx} + \frac{3}{4}(a+bx)^{4/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(4/3)/x, x]

[Out] 3*a*(a + b*x)^(1/3) + (3*(a + b*x)^(4/3))/4 - Sqrt[3]*a^(4/3)*ArcTan[(a^(1/3) + 2*(a + b*x)^(1/3))/(Sqrt[3]*a^(1/3))] - (a^(4/3)*Log[x])/2 + (3*a^(4/3))*Log[a^(1/3) - (a + b*x)^(1/3)]/2

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 57

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2),

$x] + (-\text{Dist}[3/(2*b*q), \text{Subst}[\text{Int}[1/(q^2 + q*x + x^2)], x], x, (c + d*x)^{(1/3)}], x] - \text{Dist}[3/(2*b*q^2), \text{Subst}[\text{Int}[1/(q - x)], x], x, (c + d*x)^{(1/3)}], x]) /; \text{FreeQ}[\{a, b, c, d\}, x] \&\& \text{PosQ}[(b*c - a*d)/b]$

Rule 204

$\text{Int}[(a_ + (b_)*(x_)^2)^{-1}, x_Symbol] := -\text{Simp}[\text{ArcTan}[\text{Rt}[-b, 2]*x]/\text{Rt}[-a, 2]]/(\text{Rt}[-a, 2]*\text{Rt}[-b, 2]), x] /; \text{FreeQ}[\{a, b\}, x] \&\& \text{PosQ}[a/b] \&\& (\text{LtQ}[a, 0] \parallel \text{LtQ}[b, 0])$

Rule 617

$\text{Int}[(a_ + (b_)*(x_) + (c_)*(x_)^2)^{-1}, x_Symbol] := \text{With}[\{q = 1 - 4*S\text{implify}[(a*c)/b^2]\}, \text{Dist}[-2/b, \text{Subst}[\text{Int}[1/(q - x^2)], x], x, 1 + (2*c*x)/b], x] /; \text{RationalQ}[q] \&\& (\text{EqQ}[q^2, 1] \parallel \text{!RationalQ}[b^2 - 4*a*c]) /; \text{FreeQ}[\{a, b, c\}, x] \&\& \text{NeQ}[b^2 - 4*a*c, 0]$

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^{4/3}}{x} dx &= \frac{3}{4}(a+bx)^{4/3} + a \int \frac{\sqrt[3]{a+bx}}{x} dx \\ &= 3a\sqrt[3]{a+bx} + \frac{3}{4}(a+bx)^{4/3} + a^2 \int \frac{1}{x(a+bx)^{2/3}} dx \\ &= 3a\sqrt[3]{a+bx} + \frac{3}{4}(a+bx)^{4/3} - \frac{1}{2}a^{4/3} \log(x) - \frac{1}{2}(3a^{4/3}) \text{Subst}\left(\int \frac{1}{\sqrt[3]{a}-x} dx, x, \sqrt[3]{a+bx}\right) - \frac{1}{2} \\ &= 3a\sqrt[3]{a+bx} + \frac{3}{4}(a+bx)^{4/3} - \frac{1}{2}a^{4/3} \log(x) + \frac{3}{2}a^{4/3} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) + (3a^{4/3}) \text{Subst}\left(\int \dots\right) \\ &= 3a\sqrt[3]{a+bx} + \frac{3}{4}(a+bx)^{4/3} - \sqrt{3} a^{4/3} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right) - \frac{1}{2}a^{4/3} \log(x) + \frac{3}{2}a^{4/3} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) \end{aligned}$$

Mathematica [A] time = 0.03, size = 130, normalized size = 1.24

$$\frac{1}{4} \left(4a^{4/3} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) - 2a^{4/3} \log\left(a^{2/3} + \sqrt[3]{a} \sqrt[3]{a+bx} + (a+bx)^{2/3}\right) - 4\sqrt{3} a^{4/3} \tan^{-1}\left(\frac{\frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}} + 1}{\sqrt{3}}\right) + 15 \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(4/3)/x,x]

[Out] (15*a*(a + b*x)^(1/3) + 3*b*x*(a + b*x)^(1/3) - 4*Sqrt[3]*a^(4/3)*ArcTan[(1 + (2*(a + b*x)^(1/3))/a^(1/3))/Sqrt[3]] + 4*a^(4/3)*Log[a^(1/3) - (a + b*x)^(1/3)] - 2*a^(4/3)*Log[a^(2/3) + a^(1/3)*(a + b*x)^(1/3) + (a + b*x)^(2/3)])/4

fricas [A] time = 0.51, size = 98, normalized size = 0.93

$$-\sqrt{3} a^{\frac{4}{3}} \arctan\left(\frac{2\sqrt{3}(bx+a)^{\frac{1}{3}}a^{\frac{2}{3}} + \sqrt{3}a}{3a}\right) - \frac{1}{2} a^{\frac{4}{3}} \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right) + a^{\frac{4}{3}} \log\left((bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right) + \frac{3}{4} (bx+a)^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/x,x, algorithm="fricas")

[Out] -sqrt(3)*a^(4/3)*arctan(1/3*(2*sqrt(3)*(b*x + a)^(1/3)*a^(2/3) + sqrt(3)*a)/a) - 1/2*a^(4/3)*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + a^(4/3)*log((b*x + a)^(1/3) - a^(1/3)) + 3/4*(b*x + 5*a)*(b*x + a)^(1/3)

giac [A] time = 2.02, size = 97, normalized size = 0.92

$$-\sqrt{3} a^{\frac{4}{3}} \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}} + a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right) - \frac{1}{2} a^{\frac{4}{3}} \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right) + a^{\frac{4}{3}} \log\left(\left|(bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right) + \frac{3}{4} (bx+a)^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/x,x, algorithm="giac")

[Out] -sqrt(3)*a^(4/3)*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3)) - 1/2*a^(4/3)*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + a^(4/3)*log(abs((b*x + a)^(1/3) - a^(1/3))) + 3/4*(b*x + a)^(4/3) + 3*(b*x + a)^(1/3)*a

maple [A] time = 0.01, size = 95, normalized size = 0.90

$$-\sqrt{3} a^{\frac{4}{3}} \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}} + 1\right)}{3}\right) + a^{\frac{4}{3}} \ln\left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}\right) - \frac{a^{\frac{4}{3}} \ln\left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}}\right)}{2} + 3(bx+a)^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(4/3)/x,x)

[Out] $3/4*(b*x+a)^{(4/3)}+3*a*(b*x+a)^{(1/3)}+a^{(4/3)}*\ln(-a^{(1/3)}+(b*x+a)^{(1/3)})-1/2*a^{(4/3)}*\ln(a^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+(b*x+a)^{(2/3)})-a^{(4/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2*(b*x+a)^{(1/3)}/a^{(1/3)}+1))$

maxima [A] time = 3.03, size = 96, normalized size = 0.91

$$-\sqrt{3}a^{\frac{4}{3}}\arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)-\frac{1}{2}a^{\frac{4}{3}}\log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)+a^{\frac{4}{3}}\log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)+\frac{3}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/x,x, algorithm="maxima")

[Out] $-\sqrt{3}*a^{(4/3)}*\arctan(1/3*\sqrt{3}*(2*(b*x+a)^{(1/3)}+a^{(1/3)})/a^{(1/3)})-1/2*a^{(4/3)}*\log((b*x+a)^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+a^{(2/3)})+a^{(4/3)}*\log((b*x+a)^{(1/3)}-a^{(1/3)})+3/4*(b*x+a)^{(4/3)}+3*(b*x+a)^{(1/3)}*a$

mupad [B] time = 0.06, size = 123, normalized size = 1.17

$$3a(a+bx)^{1/3}+\frac{3(a+bx)^{4/3}}{4}+a^{4/3}\ln\left(9a^2(a+bx)^{1/3}-9a^{7/3}\right)+\frac{a^{4/3}\ln\left(\frac{9a^{7/3}(-1+\sqrt{3}i)}{2}-9a^2(a+bx)^{1/3}\right)}{2}(-1$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(4/3)/x,x)

[Out] $3*a*(a+b*x)^{(1/3)}+(3*(a+b*x)^{(4/3)})/4+a^{(4/3)}*\log(9*a^2*(a+b*x)^{(1/3)}-9*a^{(7/3)})+(a^{(4/3)}*\log((9*a^{(7/3)}*(3^{(1/2)}*1i-1))/2-9*a^2*(a+b*x)^{(1/3)}*(3^{(1/2)}*1i-1))/2-(a^{(4/3)}*\log((9*a^{(7/3)}*(3^{(1/2)}*1i+1))/2+9*a^2*(a+b*x)^{(1/3)}*(3^{(1/2)}*1i+1))/2$

sympy [C] time = 2.39, size = 209, normalized size = 1.99

$$\frac{7a^{\frac{4}{3}}\log\left(1-\frac{\sqrt[3]{b}\sqrt[3]{\frac{a}{b}+x}}{\sqrt[3]{a}}\right)\Gamma\left(\frac{7}{3}\right)}{3\Gamma\left(\frac{10}{3}\right)}+\frac{7a^{\frac{4}{3}}e^{-\frac{2i\pi}{3}}\log\left(1-\frac{\sqrt[3]{b}\sqrt[3]{\frac{a}{b}+xe^{\frac{2i\pi}{3}}}}{\sqrt[3]{a}}\right)\Gamma\left(\frac{7}{3}\right)}{3\Gamma\left(\frac{10}{3}\right)}+\frac{7a^{\frac{4}{3}}e^{\frac{2i\pi}{3}}\log\left(1-\frac{\sqrt[3]{b}\sqrt[3]{\frac{a}{b}+xe^{\frac{4i\pi}{3}}}}{\sqrt[3]{a}}\right)\Gamma\left(\frac{7}{3}\right)}{3\Gamma\left(\frac{10}{3}\right)}+\frac{7a^{\frac{4}{3}}\log\left(1-\frac{\sqrt[3]{b}\sqrt[3]{\frac{a}{b}+x}}{\sqrt[3]{a}}\right)\Gamma\left(\frac{7}{3}\right)}{3\Gamma\left(\frac{10}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(4/3)/x,x)

```
[Out] 7*a**(4/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(7/3)/(3*gamma(
10/3)) + 7*a**(4/3)*exp(-2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_po
lar(2*I*pi/3)/a**(1/3))*gamma(7/3)/(3*gamma(10/3)) + 7*a**(4/3)*exp(2*I*pi/
3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(4*I*pi/3)/a**(1/3))*gamma(7/
3)/(3*gamma(10/3)) + 7*a*b**(1/3)*(a/b + x)**(1/3)*gamma(7/3)/gamma(10/3) +
7*b**(4/3)*(a/b + x)**(4/3)*gamma(7/3)/(4*gamma(10/3))
```

$$3.390 \quad \int \frac{(a+bx)^{4/3}}{x^2} dx$$

Optimal. Leaf size=107

$$-\frac{(a+bx)^{4/3}}{x} + 4b\sqrt[3]{a+bx} - \frac{2}{3}\sqrt[3]{a}b \log(x) + 2\sqrt[3]{a}b \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) - \frac{4\sqrt[3]{a}b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}}$$

[Out] 4*b*(b*x+a)^(1/3)-(b*x+a)^(4/3)/x-2/3*a^(1/3)*b*ln(x)+2*a^(1/3)*b*ln(a^(1/3)-(b*x+a)^(1/3))-4/3*a^(1/3)*b*arctan(1/3*(a^(1/3)+2*(b*x+a)^(1/3))/a^(1/3)*3^(1/2))*3^(1/2)

Rubi [A] time = 0.04, antiderivative size = 107, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.462$, Rules used = {47, 50, 57, 617, 204, 31}

$$-\frac{(a+bx)^{4/3}}{x} + 4b\sqrt[3]{a+bx} - \frac{2}{3}\sqrt[3]{a}b \log(x) + 2\sqrt[3]{a}b \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) - \frac{4\sqrt[3]{a}b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(4/3)/x^2, x]

[Out] 4*b*(a + b*x)^(1/3) - (a + b*x)^(4/3)/x - (4*a^(1/3)*b*ArcTan[(a^(1/3) + 2*(a + b*x)^(1/3))/(Sqrt[3]*a^(1/3))])/Sqrt[3] - (2*a^(1/3)*b*Log[x])/3 + 2*a^(1/3)*b*Log[a^(1/3) - (a + b*x)^(1/3)]

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 57

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2),
x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/
3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x
])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{4/3}}{x^2} dx &= -\frac{(a+bx)^{4/3}}{x} + \frac{1}{3}(4b) \int \frac{\sqrt[3]{a+bx}}{x} dx \\
&= 4b\sqrt[3]{a+bx} - \frac{(a+bx)^{4/3}}{x} + \frac{1}{3}(4ab) \int \frac{1}{x(a+bx)^{2/3}} dx \\
&= 4b\sqrt[3]{a+bx} - \frac{(a+bx)^{4/3}}{x} - \frac{2}{3}\sqrt[3]{a}b \log(x) - (2\sqrt[3]{a}b) \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a}-x} dx, x, \sqrt[3]{a+bx}\right) - (2\sqrt[3]{a}b) \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a}+x} dx, x, \sqrt[3]{a+bx}\right) \\
&= 4b\sqrt[3]{a+bx} - \frac{(a+bx)^{4/3}}{x} - \frac{2}{3}\sqrt[3]{a}b \log(x) + 2\sqrt[3]{a}b \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) + (4\sqrt[3]{a}b) \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a}+x} dx, x, \sqrt[3]{a+bx}\right) \\
&= 4b\sqrt[3]{a+bx} - \frac{(a+bx)^{4/3}}{x} - \frac{4\sqrt[3]{a}b \tan^{-1}\left(\frac{1+2\sqrt[3]{a+bx}}{\sqrt[3]{a}}\right)}{\sqrt{3}} - \frac{2}{3}\sqrt[3]{a}b \log(x) + 2\sqrt[3]{a}b \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.31

$$\frac{3b(a+bx)^{7/3} {}_2F_1\left(2, \frac{7}{3}; \frac{10}{3}; \frac{bx}{a} + 1\right)}{7a^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(4/3)/x^2,x]

[Out] (3*b*(a + b*x)^(7/3)*Hypergeometric2F1[2, 7/3, 10/3, 1 + (b*x)/a])/(7*a^2)

fricas [A] time = 0.51, size = 111, normalized size = 1.04

$$\frac{4\sqrt{3}a^{1/3}bx \arctan\left(\frac{2\sqrt{3}(bx+a)^{1/3}a^{2/3}+\sqrt{3}a}{3a}\right) + 2a^{1/3}bx \log\left((bx+a)^{2/3} + (bx+a)^{1/3}a^{1/3} + a^{2/3}\right) - 4a^{1/3}bx \log\left((bx+a)^{1/3} - a^{1/3}\right)}{3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/x^2,x, algorithm="fricas")

[Out] -1/3*(4*sqrt(3)*a^(1/3)*b*x*arctan(1/3*(2*sqrt(3)*(b*x + a)^(1/3)*a^(2/3) + sqrt(3)*a)/a) + 2*a^(1/3)*b*x*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) - 4*a^(1/3)*b*x*log((b*x + a)^(1/3) - a^(1/3)) - 3*(3*b*x - a)*(b*x + a)^(1/3)/x

giac [A] time = 2.35, size = 119, normalized size = 1.11

$$\frac{4\sqrt{3}a^{\frac{1}{3}}b^2 \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right) + 2a^{\frac{1}{3}}b^2 \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right) - 4a^{\frac{1}{3}}b^2 \log\left(\left|(bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right)}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/x^2,x, algorithm="giac")

[Out] $-\frac{1}{3}*(4*\sqrt{3}*a^{(1/3)}*b^2*\arctan(1/3*\sqrt{3}*(2*(b*x + a)^{(1/3)} + a^{(1/3)})/a^{(1/3)}) + 2*a^{(1/3)}*b^2*\log((b*x + a)^{(2/3)} + (b*x + a)^{(1/3)}*a^{(1/3)} + a^{(2/3)}) - 4*a^{(1/3)}*b^2*\log(\text{abs}((b*x + a)^{(1/3)} - a^{(1/3)})) - 9*(b*x + a)^{(1/3)}*b^2 + 3*(b*x + a)^{(1/3)}*a*b/x)/b$

maple [A] time = 0.01, size = 103, normalized size = 0.96

$$\frac{4\sqrt{3}a^{\frac{1}{3}}b \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)}{3} + \frac{4a^{\frac{1}{3}}b \ln\left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}\right)}{3} - \frac{2a^{\frac{1}{3}}b \ln\left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}}\right)}{3} + 3(bx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(4/3)/x^2,x)

[Out] $3*b*(b*x+a)^{(1/3)}-a*(b*x+a)^{(1/3)}/x+4/3*b*a^{(1/3)}*\ln(-a^{(1/3)}+(b*x+a)^{(1/3)})-2/3*b*a^{(1/3)}*\ln(a^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+(b*x+a)^{(2/3)})-4/3*b*a^{(1/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2*(b*x+a)^{(1/3)}/a^{(1/3)}+1))$

maxima [A] time = 3.03, size = 104, normalized size = 0.97

$$-\frac{4}{3}\sqrt{3}a^{\frac{1}{3}}b \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right) - \frac{2}{3}a^{\frac{1}{3}}b \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right) + \frac{4}{3}a^{\frac{1}{3}}b \log\left((bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/x^2,x, algorithm="maxima")

[Out] $-\frac{4}{3}*\sqrt{3}*a^{(1/3)}*b*\arctan(1/3*\sqrt{3}*(2*(b*x + a)^{(1/3)} + a^{(1/3)})/a^{(1/3)}) - 2/3*a^{(1/3)}*b*\log((b*x + a)^{(2/3)} + (b*x + a)^{(1/3)}*a^{(1/3)} + a^{(2/3)})$

3)) + 4/3*a^(1/3)*b*log((b*x + a)^(1/3) - a^(1/3)) + 3*(b*x + a)^(1/3)*b - (b*x + a)^(1/3)*a/x

mupad [B] time = 0.07, size = 131, normalized size = 1.22

$$3b(a+bx)^{1/3} + \frac{4a^{1/3}b \ln(12a^{4/3}b - 12ab(a+bx)^{1/3})}{3} - \frac{a(a+bx)^{1/3}}{x} + \frac{2a^{1/3}b \ln(12ab(a+bx)^{1/3} - 6a^{4/3}b)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(4/3)/x^2,x)

[Out] 3*b*(a + b*x)^(1/3) + (4*a^(1/3)*b*log(12*a^(4/3)*b - 12*a*b*(a + b*x)^(1/3)))/3 - (a*(a + b*x)^(1/3))/x + (2*a^(1/3)*b*log(12*a*b*(a + b*x)^(1/3) - 6*a^(4/3)*b*(3^(1/2)*1i - 1))*(3^(1/2)*1i - 1))/3 - (2*a^(1/3)*b*log(12*a*b*(a + b*x)^(1/3) + 6*a^(4/3)*b*(3^(1/2)*1i + 1))*(3^(1/2)*1i + 1))/3

sympy [C] time = 2.58, size = 719, normalized size = 6.72

$$\frac{28a^{10/3}be^{2i\pi/3} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b}+x}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{7}{3}\right)}{9a^3e^{2i\pi/3} \Gamma\left(\frac{10}{3}\right) - 9a^2b\left(\frac{a}{b} + x\right)e^{2i\pi/3} \Gamma\left(\frac{10}{3}\right)} + \frac{28a^{10/3}b \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b}+x}e^{2i\pi/3}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{7}{3}\right)}{9a^3e^{2i\pi/3} \Gamma\left(\frac{10}{3}\right) - 9a^2b\left(\frac{a}{b} + x\right)e^{2i\pi/3} \Gamma\left(\frac{10}{3}\right)} + \frac{28a^{10/3}be^{-2i\pi/3} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b}+x}}{\sqrt[3]{a}}\right)}{9a^3e^{2i\pi/3} \Gamma\left(\frac{10}{3}\right) - 9a^2b\left(\frac{a}{b} + x\right)e^{2i\pi/3} \Gamma\left(\frac{10}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(4/3)/x**2,x)

[Out] 28*a**(10/3)*b*exp(2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(7/3)/(9*a**3*exp(2*I*pi/3)*gamma(10/3) - 9*a**2*b*(a/b + x)*exp(2*I*pi/3)*gamma(10/3)) + 28*a**(10/3)*b*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(2*I*pi/3)/a**(1/3))*gamma(7/3)/(9*a**3*exp(2*I*pi/3)*gamma(10/3) - 9*a**2*b*(a/b + x)*exp(2*I*pi/3)*gamma(10/3)) + 28*a**(10/3)*b*exp(-2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(4*I*pi/3)/a**(1/3))*gamma(7/3)/(9*a**3*exp(2*I*pi/3)*gamma(10/3) - 9*a**2*b*(a/b + x)*exp(2*I*pi/3)*gamma(10/3)) - 28*a**(7/3)*b**2*(a/b + x)*exp(2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(7/3)/(9*a**3*exp(2*I*pi/3)*gamma(10/3) - 9*a**2*b*(a/b + x)*exp(2*I*pi/3)*gamma(10/3)) - 28*a**(7/3)*b**2*(a/b + x)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(2*I*pi/3)/a**(1/3))*gamma(7/3)/(9*a**3*exp(2*I*pi/3)*gamma(10/3) - 9*a**2*b*(a/b + x)*exp(2*I*pi/3)*gamma(10/3)) - 28*a**(7/3)*b**2*(a/b + x)*exp(-2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(4*I*pi/3)/a**(1/3))*gamma(7/3)/(9*a**3*exp(2*I*pi/3)*gamma(10/3) - 9*a**2*b*(a/b + x)*exp(2*I*pi/3)*gamma(10/3)) + 84*a**3*b**(4/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(7/3)/(9*a**3*exp(2*I*pi/3)*gamma(10/3) - 9*a**2*b*(a/b + x)*exp(2*I*pi/3)*gamma(10/3)) - 63*a**2*b**(7/3)*(a/b + x)**(4/3)*

$$\exp(2I\pi/3)*\text{gamma}(7/3)/(9*a**3*\exp(2I\pi/3)*\text{gamma}(10/3) - 9*a**2*b*(a/b + x)*\exp(2I\pi/3)*\text{gamma}(10/3))$$

$$3.391 \quad \int \frac{(a+bx)^{4/3}}{x^3} dx$$

Optimal. Leaf size=124

$$-\frac{b^2 \log(x)}{9a^{2/3}} + \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{3a^{2/3}} - \frac{2b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{2/3}} - \frac{(a+bx)^{4/3}}{2x^2} - \frac{2b\sqrt[3]{a+bx}}{3x}$$

[Out] $-2/3*b*(b*x+a)^{(1/3)}/x-1/2*(b*x+a)^{(4/3)}/x^2-1/9*b^2*\ln(x)/a^{(2/3)}+1/3*b^2*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(2/3)}-2/9*b^2*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}})/a^{(2/3)*3^{(1/2)}}$

Rubi [A] time = 0.04, antiderivative size = 124, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {47, 57, 617, 204, 31}

$$-\frac{b^2 \log(x)}{9a^{2/3}} + \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{3a^{2/3}} - \frac{2b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{2/3}} - \frac{(a+bx)^{4/3}}{2x^2} - \frac{2b\sqrt[3]{a+bx}}{3x}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(4/3)/x^3, x]

[Out] $(-2*b*(a + b*x)^{(1/3)})/(3*x) - (a + b*x)^{(4/3)}/(2*x^2) - (2*b^2*ArcTan[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(Sqrt[3]*a^{(1/3)})])/(3*Sqrt[3]*a^{(2/3)}) - (b^2*Log[x])/(9*a^{(2/3)}) + (b^2*Log[a^{(1/3)} - (a + b*x)^{(1/3)}])/(3*a^{(2/3)})$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 57

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2),
x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/
3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x
])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{4/3}}{x^3} dx &= -\frac{(a+bx)^{4/3}}{2x^2} + \frac{1}{3}(2b) \int \frac{\sqrt[3]{a+bx}}{x^2} dx \\
&= -\frac{2b\sqrt[3]{a+bx}}{3x} - \frac{(a+bx)^{4/3}}{2x^2} + \frac{1}{9}(2b^2) \int \frac{1}{x(a+bx)^{2/3}} dx \\
&= -\frac{2b\sqrt[3]{a+bx}}{3x} - \frac{(a+bx)^{4/3}}{2x^2} - \frac{b^2 \log(x)}{9a^{2/3}} - \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{3a^{2/3}} - \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{a^2} dx, x, \sqrt[3]{a+bx}\right)}{3a^{2/3}} \\
&= -\frac{2b\sqrt[3]{a+bx}}{3x} - \frac{(a+bx)^{4/3}}{2x^2} - \frac{b^2 \log(x)}{9a^{2/3}} + \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{3a^{2/3}} + \frac{(2b^2) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{a+bx}\right)}{3a^{2/3}} \\
&= -\frac{2b\sqrt[3]{a+bx}}{3x} - \frac{(a+bx)^{4/3}}{2x^2} - \frac{2b^2 \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{3\sqrt{3}a^{2/3}} - \frac{b^2 \log(x)}{9a^{2/3}} + \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{3a^{2/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.28

$$-\frac{3b^2(a+bx)^{7/3} {}_2F_1\left(\frac{7}{3}, 3; \frac{10}{3}; \frac{bx}{a} + 1\right)}{7a^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(4/3)/x^3,x]

[Out] $(-3*b^2*(a + b*x)^{(7/3)}*Hypergeometric2F1[7/3, 3, 10/3, 1 + (b*x)/a])/(7*a^3)$

fricas [A] time = 0.50, size = 162, normalized size = 1.31

$$\frac{4\sqrt{3}(a^2)^{\frac{1}{6}}ab^2x^2 \arctan\left(\frac{(a^2)^{\frac{1}{6}}\left(\sqrt{3}(a^2)^{\frac{1}{3}}a+2\sqrt{3}(a^2)^{\frac{2}{3}}(bx+a)^{\frac{1}{3}}\right)}{3a^2}\right) + 2(a^2)^{\frac{2}{3}}b^2x^2 \log\left((bx+a)^{\frac{2}{3}}a + (a^2)^{\frac{1}{3}}a + (a^2)^{\frac{2}{3}}(bx+a)\right)}{18a^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/x^3,x, algorithm="fricas")

[Out] $-1/18*(4*\sqrt{3}*(a^2)^{(1/6)}*a*b^2*x^2*\arctan(1/3*(a^2)^{(1/6)}*(\sqrt{3}*(a^2)^{(1/3)}*a + 2*\sqrt{3}*(a^2)^{(2/3)}*(b*x + a)^{(1/3)})/a^2) + 2*(a^2)^{(2/3)}*b^2*x^2*\log((b*x + a)^{(2/3)}*a + (a^2)^{(1/3)}*a + (a^2)^{(2/3)}*(b*x + a)^{(1/3)}) - 4*(a^2)^{(2/3)}*b^2*x^2*\log((b*x + a)^{(1/3)}*a - (a^2)^{(2/3)}) + 3*(7*a^2*b*x + 3*a^3)*(b*x + a)^{(1/3)}/(a^2*x^2)$

giac [A] time = 1.94, size = 127, normalized size = 1.02

$$\frac{4\sqrt{3}b^3 \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right) + 2b^3 \log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right) - 4b^3 \log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right) + 3\left(7(bx+a)^{\frac{4}{3}}b^3-4(bx+a)^{\frac{1}{3}}ab^3\right)}{18b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/x^3,x, algorithm="giac")

[Out] $-1/18*(4*\sqrt{3}*b^3*\arctan(1/3*\sqrt{3}*(2*(b*x + a)^{(1/3)} + a^{(1/3)})/a^{(1/3)})/a^{(2/3)} + 2*b^3*\log((b*x + a)^{(2/3)} + (b*x + a)^{(1/3)}*a^{(1/3)} + a^{(2/3)})/a^{(2/3)} - 4*b^3*\log(\text{abs}((b*x + a)^{(1/3)} - a^{(1/3)}))/a^{(2/3)} + 3*(7*(b*x + a)^{(4/3)}*b^3 - 4*(b*x + a)^{(1/3)}*a*b^3)/(b^2*x^2)/b$

maple [A] time = 0.01, size = 111, normalized size = 0.90

$$\frac{2\sqrt{3} b^2 \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)}{9a^{\frac{2}{3}}} + \frac{2b^2 \ln\left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}\right)}{9a^{\frac{2}{3}}} - \frac{b^2 \ln\left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}}\right)}{9a^{\frac{2}{3}}} + \frac{2(bx+a)^{\frac{1}{3}}}{3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(4/3)/x^3,x)

[Out] -7/6*(b*x+a)^(4/3)/x^2+2/3/x^2*(b*x+a)^(1/3)*a+2/9*b^2/a^(2/3)*ln(-a^(1/3)+(b*x+a)^(1/3))-1/9*b^2/a^(2/3)*ln(a^(2/3)+(b*x+a)^(1/3)*a^(1/3)+(b*x+a)^(2/3))-2/9*b^2/a^(2/3)*3^(1/2)*arctan(1/3*3^(1/2)*(2*(b*x+a)^(1/3)/a^(1/3)+1))

maxima [A] time = 3.06, size = 136, normalized size = 1.10

$$\frac{2\sqrt{3}b^2 \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{9a^{\frac{2}{3}}} - \frac{b^2 \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{9a^{\frac{2}{3}}} + \frac{2b^2 \log\left((bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right)}{9a^{\frac{2}{3}}} - \frac{7(bx+a)^{\frac{1}{3}}}{6((bx+a)^{\frac{2}{3}})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/x^3,x, algorithm="maxima")

[Out] -2/9*sqrt(3)*b^2*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3))/a^(2/3) - 1/9*b^2*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(2/3) + 2/9*b^2*log((b*x + a)^(1/3) - a^(1/3))/a^(2/3) - 1/6*(7*(b*x + a)^(4/3)*b^2 - 4*(b*x + a)^(1/3)*a*b^2)/((b*x + a)^2 - 2*(b*x + a)*a + a^2)

mupad [B] time = 0.12, size = 174, normalized size = 1.40

$$\frac{2b^2 \ln\left(2b^2(a+bx)^{1/3} - 2a^{1/3}b^2\right)}{9a^{2/3}} - \frac{\frac{7b^2(a+bx)^{4/3}}{6} - \frac{2ab^2(a+bx)^{1/3}}{3}}{(a+bx)^2 - 2a(a+bx) + a^2} - \frac{\ln\left(2b^2(a+bx)^{1/3} + a^{1/3}(b^2 + \sqrt{3}b^2i)\right)}{9a^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(4/3)/x^3,x)

[Out] (2*b^2*log(2*b^2*(a + b*x)^(1/3) - 2*a^(1/3)*b^2))/(9*a^(2/3)) - ((7*b^2*(a + b*x)^(4/3))/6 - (2*a*b^2*(a + b*x)^(1/3))/3)/((a + b*x)^2 - 2*a*(a + b*x) + a^2) - (log(2*b^2*(a + b*x)^(1/3) + a^(1/3)*(3^(1/2)*b^2*i + b^2)))*(3^

$$\frac{(1/2)*b^{2*1i + b^2}}{(9*a^{(2/3)})} + (b^2*\log(2*b^2*(a + b*x)^{(1/3)} - 9*a^{(1/3)}*b^2*((3^{(1/2)*1i})/9 - 1/9))*((3^{(1/2)*1i})/9 - 1/9))/a^{(2/3)}$$

sympy [C] time = 2.74, size = 2266, normalized size = 18.27

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(4/3)/x**3,x)

[Out] $28*a^{(19/3)}*b^{**2}*\exp(2*I*pi/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}/a^{(1/3)})$
 $*\gamma(7/3)/(54*a^{**7}*\exp(2*I*pi/3)*\gamma(10/3) - 162*a^{**6}*b*(a/b + x)*\exp(2$
 $*I*pi/3)*\gamma(10/3) + 162*a^{**5}*b^{**2}*(a/b + x)^{**2}*\exp(2*I*pi/3)*\gamma(10/3)$
 $- 54*a^{**4}*b^{**3}*(a/b + x)^{**3}*\exp(2*I*pi/3)*\gamma(10/3)) + 28*a^{(19/3)}*b^{**2}$
 $*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_polar(2*I*pi/3)/a^{(1/3)})*\gamma(7/3)$
 $/(54*a^{**7}*\exp(2*I*pi/3)*\gamma(10/3) - 162*a^{**6}*b*(a/b + x)*\exp(2*I*pi/3)*\gamma$
 $mma(10/3) + 162*a^{**5}*b^{**2}*(a/b + x)^{**2}*\exp(2*I*pi/3)*\gamma(10/3) - 54*a^{**4}$
 $*b^{**3}*(a/b + x)^{**3}*\exp(2*I*pi/3)*\gamma(10/3)) + 28*a^{(19/3)}*b^{**2}*\exp(-2*I*p$
 $i/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_polar(4*I*pi/3)/a^{(1/3)})*\gamma($
 $7/3)/(54*a^{**7}*\exp(2*I*pi/3)*\gamma(10/3) - 162*a^{**6}*b*(a/b + x)*\exp(2*I*pi/3)$
 $)*\gamma(10/3) + 162*a^{**5}*b^{**2}*(a/b + x)^{**2}*\exp(2*I*pi/3)*\gamma(10/3) - 54*a$
 $**4*b^{**3}*(a/b + x)^{**3}*\exp(2*I*pi/3)*\gamma(10/3)) - 84*a^{(16/3)}*b^{**3}*(a/b +$
 $x)*\exp(2*I*pi/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}/a^{(1/3)})*\gamma(7/3)/(5$
 $4*a^{**7}*\exp(2*I*pi/3)*\gamma(10/3) - 162*a^{**6}*b*(a/b + x)*\exp(2*I*pi/3)*\gamma$
 $(10/3) + 162*a^{**5}*b^{**2}*(a/b + x)^{**2}*\exp(2*I*pi/3)*\gamma(10/3) - 54*a^{**4}*b^{**$
 $3*(a/b + x)^{**3}*\exp(2*I*pi/3)*\gamma(10/3)) - 84*a^{(16/3)}*b^{**3}*(a/b + x)*\log$
 $(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_polar(2*I*pi/3)/a^{(1/3)})*\gamma(7/3)/(54$
 $*a^{**7}*\exp(2*I*pi/3)*\gamma(10/3) - 162*a^{**6}*b*(a/b + x)*\exp(2*I*pi/3)*\gamma($
 $10/3) + 162*a^{**5}*b^{**2}*(a/b + x)^{**2}*\exp(2*I*pi/3)*\gamma(10/3) - 54*a^{**4}*b^{**3}$
 $*(a/b + x)^{**3}*\exp(2*I*pi/3)*\gamma(10/3)) - 84*a^{(16/3)}*b^{**3}*(a/b + x)*\exp(-$
 $2*I*pi/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_polar(4*I*pi/3)/a^{(1/3)})*$
 $\gamma(7/3)/(54*a^{**7}*\exp(2*I*pi/3)*\gamma(10/3) - 162*a^{**6}*b*(a/b + x)*\exp(2*$
 $I*pi/3)*\gamma(10/3) + 162*a^{**5}*b^{**2}*(a/b + x)^{**2}*\exp(2*I*pi/3)*\gamma(10/3)$
 $- 54*a^{**4}*b^{**3}*(a/b + x)^{**3}*\exp(2*I*pi/3)*\gamma(10/3)) + 84*a^{(13/3)}*b^{**4}$
 $(a/b + x)^{**2}*\exp(2*I*pi/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}/a^{(1/3)})*\gamma$
 $a(7/3)/(54*a^{**7}*\exp(2*I*pi/3)*\gamma(10/3) - 162*a^{**6}*b*(a/b + x)*\exp(2*I*pi$
 $/3)*\gamma(10/3) + 162*a^{**5}*b^{**2}*(a/b + x)^{**2}*\exp(2*I*pi/3)*\gamma(10/3) - 54$
 $*a^{**4}*b^{**3}*(a/b + x)^{**3}*\exp(2*I*pi/3)*\gamma(10/3)) + 84*a^{(13/3)}*b^{**4}*(a/b$
 $+ x)^{**2}*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_polar(2*I*pi/3)/a^{(1/3)})*\gamma$
 $mma(7/3)/(54*a^{**7}*\exp(2*I*pi/3)*\gamma(10/3) - 162*a^{**6}*b*(a/b + x)*\exp(2*I*$
 $pi/3)*\gamma(10/3) + 162*a^{**5}*b^{**2}*(a/b + x)^{**2}*\exp(2*I*pi/3)*\gamma(10/3) -$
 $54*a^{**4}*b^{**3}*(a/b + x)^{**3}*\exp(2*I*pi/3)*\gamma(10/3)) + 84*a^{(13/3)}*b^{**4}*(a$
 $/b + x)^{**2}*\exp(-2*I*pi/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_polar(4*I*p$
 $i/3)/a^{(1/3)})*\gamma(7/3)/(54*a^{**7}*\exp(2*I*pi/3)*\gamma(10/3) - 162*a^{**6}*b*($
 $a/b + x)*\exp(2*I*pi/3)*\gamma(10/3) + 162*a^{**5}*b^{**2}*(a/b + x)^{**2}*\exp(2*I*pi/$

$$\begin{aligned}
& 3) * \gamma(10/3) - 54 * a^{**4} * b^{**3} * (a/b + x)^{**3} * \exp(2 * I * \pi / 3) * \gamma(10/3)) - 28 * \\
& a^{**10/3} * b^{**5} * (a/b + x)^{**3} * \exp(2 * I * \pi / 3) * \log(1 - b^{**1/3} * (a/b + x)^{**1/3}) \\
& / a^{**1/3}) * \gamma(7/3) / (54 * a^{**7} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 162 * a^{**6} * b * (a/b \\
& + x) * \exp(2 * I * \pi / 3) * \gamma(10/3) + 162 * a^{**5} * b^{**2} * (a/b + x)^{**2} * \exp(2 * I * \pi / 3) * \gamma \\
& (10/3) - 54 * a^{**4} * b^{**3} * (a/b + x)^{**3} * \exp(2 * I * \pi / 3) * \gamma(10/3)) - 28 * a^{**10/3} * b^{**5} * (a/b + x)^{**3} * \log(1 - b^{**1/3} * (a/b + x)^{**1/3}) * \exp_polar(2 * I * \pi / 3) / a^{**1/3}) * \gamma(7/3) / (54 * a^{**7} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 162 * a^{**6} * b * (a/b + x) * \exp(2 * I * \pi / 3) * \gamma(10/3) + 162 * a^{**5} * b^{**2} * (a/b + x)^{**2} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 54 * a^{**4} * b^{**3} * (a/b + x)^{**3} * \exp(2 * I * \pi / 3) * \gamma(10/3)) - 28 * a^{**10/3} * b^{**5} * (a/b + x)^{**3} * \exp(-2 * I * \pi / 3) * \log(1 - b^{**1/3} * (a/b + x)^{**1/3}) * \exp_polar(4 * I * \pi / 3) / a^{**1/3}) * \gamma(7/3) / (54 * a^{**7} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 162 * a^{**6} * b * (a/b + x) * \exp(2 * I * \pi / 3) * \gamma(10/3) + 162 * a^{**5} * b^{**2} * (a/b + x)^{**2} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 54 * a^{**4} * b^{**3} * (a/b + x)^{**3} * \exp(2 * I * \pi / 3) * \gamma(10/3)) + 84 * a^{**6} * b^{**7/3} * (a/b + x)^{**1/3} * \exp(2 * I * \pi / 3) * \gamma(7/3) / (54 * a^{**7} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 162 * a^{**6} * b * (a/b + x) * \exp(2 * I * \pi / 3) * \gamma(10/3) + 162 * a^{**5} * b^{**2} * (a/b + x)^{**2} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 54 * a^{**4} * b^{**3} * (a/b + x)^{**3} * \exp(2 * I * \pi / 3) * \gamma(10/3)) - 231 * a^{**5} * b^{**10/3} * (a/b + x)^{**4/3} * \exp(2 * I * \pi / 3) * \gamma(7/3) / (54 * a^{**7} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 162 * a^{**6} * b * (a/b + x) * \exp(2 * I * \pi / 3) * \gamma(10/3) + 162 * a^{**5} * b^{**2} * (a/b + x)^{**2} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 54 * a^{**4} * b^{**3} * (a/b + x)^{**3} * \exp(2 * I * \pi / 3) * \gamma(10/3)) + 147 * a^{**4} * b^{**13/3} * (a/b + x)^{**7/3} * \exp(2 * I * \pi / 3) * \gamma(7/3) / (54 * a^{**7} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 162 * a^{**6} * b * (a/b + x) * \exp(2 * I * \pi / 3) * \gamma(10/3) + 162 * a^{**5} * b^{**2} * (a/b + x)^{**2} * \exp(2 * I * \pi / 3) * \gamma(10/3) - 54 * a^{**4} * b^{**3} * (a/b + x)^{**3} * \exp(2 * I * \pi / 3) * \gamma(10/3))
\end{aligned}$$

$$3.392 \quad \int \frac{x^3}{\sqrt[3]{a+bx}} dx$$

Optimal. Leaf size=72

$$-\frac{3a^3(a+bx)^{2/3}}{2b^4} + \frac{9a^2(a+bx)^{5/3}}{5b^4} + \frac{3(a+bx)^{11/3}}{11b^4} - \frac{9a(a+bx)^{8/3}}{8b^4}$$

[Out] $-3/2*a^3*(b*x+a)^{(2/3)}/b^4+9/5*a^2*(b*x+a)^{(5/3)}/b^4-9/8*a*(b*x+a)^{(8/3)}/b^4+3/11*(b*x+a)^{(11/3)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9a^2(a+bx)^{5/3}}{5b^4} - \frac{3a^3(a+bx)^{2/3}}{2b^4} + \frac{3(a+bx)^{11/3}}{11b^4} - \frac{9a(a+bx)^{8/3}}{8b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x)^(1/3), x]

[Out] $(-3*a^3*(a + b*x)^{(2/3)})/(2*b^4) + (9*a^2*(a + b*x)^{(5/3)})/(5*b^4) - (9*a*(a + b*x)^{(8/3)})/(8*b^4) + (3*(a + b*x)^{(11/3)})/(11*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{\sqrt[3]{a+bx}} dx &= \int \left(-\frac{a^3}{b^3\sqrt[3]{a+bx}} + \frac{3a^2(a+bx)^{2/3}}{b^3} - \frac{3a(a+bx)^{5/3}}{b^3} + \frac{(a+bx)^{8/3}}{b^3} \right) dx \\ &= -\frac{3a^3(a+bx)^{2/3}}{2b^4} + \frac{9a^2(a+bx)^{5/3}}{5b^4} - \frac{9a(a+bx)^{8/3}}{8b^4} + \frac{3(a+bx)^{11/3}}{11b^4} \end{aligned}$$

Mathematica [A] time = 0.03, size = 46, normalized size = 0.64

$$\frac{3(a+bx)^{2/3}(-81a^3 + 54a^2bx - 45ab^2x^2 + 40b^3x^3)}{440b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x)^(1/3), x]

[Out] $(3*(a + b*x)^{(2/3)*(-81*a^3 + 54*a^2*b*x - 45*a*b^2*x^2 + 40*b^3*x^3))/(440*b^4)$

fricas [A] time = 0.60, size = 42, normalized size = 0.58

$$\frac{3(40b^3x^3 - 45ab^2x^2 + 54a^2bx - 81a^3)(bx + a)^{\frac{2}{3}}}{440b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(1/3), x, algorithm="fricas")

[Out] $3/440*(40*b^3*x^3 - 45*a*b^2*x^2 + 54*a^2*b*x - 81*a^3)*(b*x + a)^{(2/3)}/b^4$

giac [A] time = 0.90, size = 49, normalized size = 0.68

$$\frac{3\left(40(bx + a)^{\frac{11}{3}} - 165(bx + a)^{\frac{8}{3}}a + 264(bx + a)^{\frac{5}{3}}a^2 - 220(bx + a)^{\frac{2}{3}}a^3\right)}{440b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(1/3), x, algorithm="giac")

[Out] $3/440*(40*(b*x + a)^{(11/3)} - 165*(b*x + a)^{(8/3)}*a + 264*(b*x + a)^{(5/3)}*a^2 - 220*(b*x + a)^{(2/3)}*a^3)/b^4$

maple [A] time = 0.00, size = 43, normalized size = 0.60

$$-\frac{3(bx + a)^{\frac{2}{3}}(-40b^3x^3 + 45ab^2x^2 - 54a^2bx + 81a^3)}{440b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^(1/3), x)

[Out] $-3/440*(b*x+a)^{(2/3)*(-40*b^3*x^3+45*a*b^2*x^2-54*a^2*b*x+81*a^3)}/b^4$

maxima [A] time = 1.31, size = 56, normalized size = 0.78

$$\frac{3(bx + a)^{\frac{11}{3}}}{11b^4} - \frac{9(bx + a)^{\frac{8}{3}}a}{8b^4} + \frac{9(bx + a)^{\frac{5}{3}}a^2}{5b^4} - \frac{3(bx + a)^{\frac{2}{3}}a^3}{2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(1/3),x, algorithm="maxima")

[Out] $\frac{3}{11}*(b*x + a)^{(11/3)}/b^4 - \frac{9}{8}*(b*x + a)^{(8/3)}*a/b^4 + \frac{9}{5}*(b*x + a)^{(5/3)}*a^2/b^4 - \frac{3}{2}*(b*x + a)^{(2/3)}*a^3/b^4$

mupad [B] time = 0.04, size = 56, normalized size = 0.78

$$\frac{3(a+bx)^{11/3}}{11b^4} - \frac{3a^3(a+bx)^{2/3}}{2b^4} + \frac{9a^2(a+bx)^{5/3}}{5b^4} - \frac{9a(a+bx)^{8/3}}{8b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(a + b*x)^(1/3),x)

[Out] $\frac{3*(a + b*x)^{(11/3)}}{(11*b^4)} - \frac{3*a^3*(a + b*x)^{(2/3)}}{(2*b^4)} + \frac{9*a^2*(a + b*x)^{(5/3)}}{(5*b^4)} - \frac{9*a*(a + b*x)^{(8/3)}}{(8*b^4)}$

sympy [B] time = 2.78, size = 1640, normalized size = 22.78

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(b*x+a)**(1/3),x)

[Out] $-243*a^{(71/3)}*(1 + b*x/a)^{(2/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 243*a^{(71/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) - 1296*a^{(68/3)}*b*x*(1 + b*x/a)^{(2/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 1458*a^{(68/3)}*b*x/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) - 2808*a^{(65/3)}*b^2*x^2*(1 + b*x/a)^{(2/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 3645*a^{(65/3)}*b^2*x^2/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) - 3120*a^{(62/3)}*b^3*x^3*(1 + b*x/a)^{(2/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 4860*a^{(62/3)}*b^3*x^3/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) - 1710*a^{(59/3)}*b^4*x^4*(1 + b*x/a)^{(2/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 4860*a^{(59/3)}*b^4*x^4/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6)$

$$\begin{aligned}
& 40*a^{14}*b^{10}*x^6) + 3645*a^{59/3}*b^4*x^4/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 72*a^{56/3}*b^5*x^5*(1 + b*x/a)^{(2/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 1458*a^{56/3}*b^5*x^5/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 1104*a^{53/3}*b^6*x^6*(1 + b*x/a)^{(2/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 243*a^{53/3}*b^6*x^6/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 1152*a^{50/3}*b^7*x^7*(1 + b*x/a)^{(2/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 585*a^{47/3}*b^8*x^8*(1 + b*x/a)^{(2/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6) + 120*a^{44/3}*b^9*x^9*(1 + b*x/a)^{(2/3)}/(440*a^{20}*b^4 + 2640*a^{19}*b^5*x + 6600*a^{18}*b^6*x^2 + 8800*a^{17}*b^7*x^3 + 6600*a^{16}*b^8*x^4 + 2640*a^{15}*b^9*x^5 + 440*a^{14}*b^{10}*x^6)
\end{aligned}$$

$$3.393 \quad \int \frac{x^2}{\sqrt[3]{a+bx}} dx$$

Optimal. Leaf size=53

$$\frac{3a^2(a+bx)^{2/3}}{2b^3} + \frac{3(a+bx)^{8/3}}{8b^3} - \frac{6a(a+bx)^{5/3}}{5b^3}$$

[Out] $3/2*a^2*(b*x+a)^{(2/3)}/b^3-6/5*a*(b*x+a)^{(5/3)}/b^3+3/8*(b*x+a)^{(8/3)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3a^2(a+bx)^{2/3}}{2b^3} + \frac{3(a+bx)^{8/3}}{8b^3} - \frac{6a(a+bx)^{5/3}}{5b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*x)^(1/3), x]

[Out] $(3*a^2*(a + b*x)^{(2/3)})/(2*b^3) - (6*a*(a + b*x)^{(5/3)})/(5*b^3) + (3*(a + b*x)^{(8/3)})/(8*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sqrt[3]{a+bx}} dx &= \int \left(\frac{a^2}{b^2 \sqrt[3]{a+bx}} - \frac{2a(a+bx)^{2/3}}{b^2} + \frac{(a+bx)^{5/3}}{b^2} \right) dx \\ &= \frac{3a^2(a+bx)^{2/3}}{2b^3} - \frac{6a(a+bx)^{5/3}}{5b^3} + \frac{3(a+bx)^{8/3}}{8b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.66

$$\frac{3(a+bx)^{2/3} (9a^2 - 6abx + 5b^2x^2)}{40b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x)^(1/3), x]

[Out] (3*(a + b*x)^(2/3)*(9*a^2 - 6*a*b*x + 5*b^2*x^2))/(40*b^3)

fricas [A] time = 0.51, size = 31, normalized size = 0.58

$$\frac{3(5b^2x^2 - 6abx + 9a^2)(bx + a)^{\frac{2}{3}}}{40b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(1/3), x, algorithm="fricas")

[Out] 3/40*(5*b^2*x^2 - 6*a*b*x + 9*a^2)*(b*x + a)^(2/3)/b^3

giac [A] time = 0.91, size = 37, normalized size = 0.70

$$\frac{3\left(5(bx + a)^{\frac{8}{3}} - 16(bx + a)^{\frac{5}{3}}a + 20(bx + a)^{\frac{2}{3}}a^2\right)}{40b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(1/3), x, algorithm="giac")

[Out] 3/40*(5*(b*x + a)^(8/3) - 16*(b*x + a)^(5/3)*a + 20*(b*x + a)^(2/3)*a^2)/b^3

maple [A] time = 0.00, size = 32, normalized size = 0.60

$$\frac{3(bx + a)^{\frac{2}{3}}(5b^2x^2 - 6abx + 9a^2)}{40b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^(1/3), x)

[Out] 3/40*(b*x+a)^(2/3)*(5*b^2*x^2-6*a*b*x+9*a^2)/b^3

maxima [A] time = 1.38, size = 41, normalized size = 0.77

$$\frac{3(bx + a)^{\frac{8}{3}}}{8b^3} - \frac{6(bx + a)^{\frac{5}{3}}a}{5b^3} + \frac{3(bx + a)^{\frac{2}{3}}a^2}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(1/3),x, algorithm="maxima")

[Out] $\frac{3}{8}*(b*x + a)^{(8/3)}/b^3 - \frac{6}{5}*(b*x + a)^{(5/3)}*a/b^3 + \frac{3}{2}*(b*x + a)^{(2/3)}*a^2/b^3$

mupad [B] time = 0.04, size = 37, normalized size = 0.70

$$\frac{15(a+bx)^{8/3} - 48a(a+bx)^{5/3} + 60a^2(a+bx)^{2/3}}{40b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(a + b*x)^(1/3),x)

[Out] $(15*(a + b*x)^{(8/3)} - 48*a*(a + b*x)^{(5/3)} + 60*a^2*(a + b*x)^{(2/3)})/(40*b^3)$

sympy [B] time = 1.77, size = 600, normalized size = 11.32

$$\frac{27a^{\frac{32}{3}} \left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{40a^8b^3 + 120a^7b^4x + 120a^6b^5x^2 + 40a^5b^6x^3} - \frac{27a^{\frac{32}{3}}}{40a^8b^3 + 120a^7b^4x + 120a^6b^5x^2 + 40a^5b^6x^3} + \frac{63a^{\frac{29}{3}}b}{40a^8b^3 + 120a^7b^4x + 120a^6b^5x^2 + 40a^5b^6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(b*x+a)**(1/3),x)

[Out] $27*a^{(32/3)}*(1 + b*x/a)^{(2/3)}/(40*a^{**8}*b^{**3} + 120*a^{**7}*b^{**4}*x + 120*a^{**6}*b^{**5}*x^{**2} + 40*a^{**5}*b^{**6}*x^{**3}) - 27*a^{(32/3)}/(40*a^{**8}*b^{**3} + 120*a^{**7}*b^{**4}*x + 120*a^{**6}*b^{**5}*x^{**2} + 40*a^{**5}*b^{**6}*x^{**3}) + 63*a^{(29/3)}*b*x*(1 + b*x/a)^{(2/3)}/(40*a^{**8}*b^{**3} + 120*a^{**7}*b^{**4}*x + 120*a^{**6}*b^{**5}*x^{**2} + 40*a^{**5}*b^{**6}*x^{**3}) - 81*a^{(29/3)}*b*x/(40*a^{**8}*b^{**3} + 120*a^{**7}*b^{**4}*x + 120*a^{**6}*b^{**5}*x^{**2} + 40*a^{**5}*b^{**6}*x^{**3}) + 42*a^{(26/3)}*b^{**2}*x^{**2}*(1 + b*x/a)^{(2/3)}/(40*a^{**8}*b^{**3} + 120*a^{**7}*b^{**4}*x + 120*a^{**6}*b^{**5}*x^{**2} + 40*a^{**5}*b^{**6}*x^{**3}) - 81*a^{(26/3)}*b^{**2}*x^{**2}/(40*a^{**8}*b^{**3} + 120*a^{**7}*b^{**4}*x + 120*a^{**6}*b^{**5}*x^{**2} + 40*a^{**5}*b^{**6}*x^{**3}) + 18*a^{(23/3)}*b^{**3}*x^{**3}*(1 + b*x/a)^{(2/3)}/(40*a^{**8}*b^{**3} + 120*a^{**7}*b^{**4}*x + 120*a^{**6}*b^{**5}*x^{**2} + 40*a^{**5}*b^{**6}*x^{**3}) - 27*a^{(23/3)}*b^{**3}*x^{**3}/(40*a^{**8}*b^{**3} + 120*a^{**7}*b^{**4}*x + 120*a^{**6}*b^{**5}*x^{**2} + 40*a^{**5}*b^{**6}*x^{**3}) + 27*a^{(20/3)}*b^{**4}*x^{**4}*(1 + b*x/a)^{(2/3)}/(40*a^{**8}*b^{**3} + 120*a^{**7}*b^{**4}*x + 120*a^{**6}*b^{**5}*x^{**2} + 40*a^{**5}*b^{**6}*x^{**3}) + 15*a^{(17/3)}*b^{**5}*x^{**5}*(1 + b*x/a)^{(2/3)}/(40*a^{**8}*b^{**3} + 120*a^{**7}*b^{**4}*x + 120*a^{**6}*b^{**5}*x^{**2} + 40*a^{**5}*b^{**6}*x^{**3})$

$$3.394 \quad \int \frac{x}{\sqrt[3]{a+bx}} dx$$

Optimal. Leaf size=34

$$\frac{3(a+bx)^{5/3}}{5b^2} - \frac{3a(a+bx)^{2/3}}{2b^2}$$

[Out] $-3/2*a*(b*x+a)^{(2/3)}/b^2+3/5*(b*x+a)^{(5/3)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3(a+bx)^{5/3}}{5b^2} - \frac{3a(a+bx)^{2/3}}{2b^2}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x)^(1/3), x]

[Out] $(-3*a*(a + b*x)^{(2/3)})/(2*b^2) + (3*(a + b*x)^{(5/3)})/(5*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x}{\sqrt[3]{a+bx}} dx &= \int \left(-\frac{a}{b\sqrt[3]{a+bx}} + \frac{(a+bx)^{2/3}}{b} \right) dx \\ &= -\frac{3a(a+bx)^{2/3}}{2b^2} + \frac{3(a+bx)^{5/3}}{5b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.71

$$\frac{3(a+bx)^{2/3}(2bx-3a)}{10b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x)^(1/3), x]

[Out] $(3*(a + b*x)^{(2/3)}*(-3*a + 2*b*x))/(10*b^2)$

fricas [A] time = 0.48, size = 20, normalized size = 0.59

$$\frac{3(2bx - 3a)(bx + a)^{\frac{2}{3}}}{10b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(1/3),x, algorithm="fricas")`

[Out] $3/10*(2*b*x - 3*a)*(b*x + a)^{(2/3)}/b^2$

giac [A] time = 0.90, size = 25, normalized size = 0.74

$$\frac{3\left(2(bx + a)^{\frac{5}{3}} - 5(bx + a)^{\frac{2}{3}}a\right)}{10b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(1/3),x, algorithm="giac")`

[Out] $3/10*(2*(b*x + a)^{(5/3)} - 5*(b*x + a)^{(2/3)}*a)/b^2$

maple [A] time = 0.00, size = 21, normalized size = 0.62

$$-\frac{3(bx + a)^{\frac{2}{3}}(-2bx + 3a)}{10b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(b*x+a)^(1/3),x)`

[Out] $-3/10*(b*x+a)^{(2/3)}*(-2*b*x+3*a)/b^2$

maxima [A] time = 1.30, size = 26, normalized size = 0.76

$$\frac{3(bx + a)^{\frac{5}{3}}}{5b^2} - \frac{3(bx + a)^{\frac{2}{3}}a}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(1/3),x, algorithm="maxima")`

[Out] $3/5*(b*x + a)^{(5/3)}/b^2 - 3/2*(b*x + a)^{(2/3)}*a/b^2$

mupad [B] time = 0.03, size = 25, normalized size = 0.74

$$\frac{15a(a+bx)^{2/3} - 6(a+bx)^{5/3}}{10b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a + b*x)^(1/3), x)`

[Out] `-(15*a*(a + b*x)^(2/3) - 6*(a + b*x)^(5/3))/(10*b^2)`

sympy [B] time = 1.16, size = 162, normalized size = 4.76

$$-\frac{9a^{\frac{11}{3}} \left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{10a^2b^2 + 10ab^3x} + \frac{9a^{\frac{11}{3}}}{10a^2b^2 + 10ab^3x} - \frac{3a^{\frac{8}{3}}bx \left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{10a^2b^2 + 10ab^3x} + \frac{9a^{\frac{8}{3}}bx}{10a^2b^2 + 10ab^3x} + \frac{6a^{\frac{5}{3}}b^2x^2 \left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{10a^2b^2 + 10ab^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)**(1/3), x)`

[Out] `-9*a**(11/3)*(1 + b*x/a)**(2/3)/(10*a**2*b**2 + 10*a*b**3*x) + 9*a**(11/3)/(10*a**2*b**2 + 10*a*b**3*x) - 3*a**(8/3)*b*x*(1 + b*x/a)**(2/3)/(10*a**2*b**2 + 10*a*b**3*x) + 9*a**(8/3)*b*x/(10*a**2*b**2 + 10*a*b**3*x) + 6*a**(5/3)*b**2*x**2*(1 + b*x/a)**(2/3)/(10*a**2*b**2 + 10*a*b**3*x)`

$$3.395 \quad \int \frac{1}{\sqrt[3]{a+bx}} dx$$

Optimal. Leaf size=16

$$\frac{3(a+bx)^{2/3}}{2b}$$

[Out] 3/2*(b*x+a)^(2/3)/b

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.111, Rules used = {32}

$$\frac{3(a+bx)^{2/3}}{2b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-1/3), x]

[Out] (3*(a + b*x)^(2/3))/(2*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt[3]{a+bx}} dx = \frac{3(a+bx)^{2/3}}{2b}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$\frac{3(a+bx)^{2/3}}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-1/3), x]

[Out] (3*(a + b*x)^(2/3))/(2*b)

fricas [A] time = 0.52, size = 12, normalized size = 0.75

$$\frac{3(bx+a)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3),x, algorithm="fricas")

[Out] 3/2*(b*x + a)^(2/3)/b

giac [A] time = 0.97, size = 12, normalized size = 0.75

$$\frac{3(bx + a)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3),x, algorithm="giac")

[Out] 3/2*(b*x + a)^(2/3)/b

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{3(bx + a)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/3),x)

[Out] 3/2*(b*x+a)^(2/3)/b

maxima [A] time = 1.32, size = 12, normalized size = 0.75

$$\frac{3(bx + a)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3),x, algorithm="maxima")

[Out] 3/2*(b*x + a)^(2/3)/b

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{3(a + bx)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x)^(1/3),x)

[Out] $(3*(a + b*x)^{(2/3)})/(2*b)$

sympy [A] time = 0.06, size = 12, normalized size = 0.75

$$\frac{3(a + bx)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/3),x)`

[Out] $3*(a + b*x)**(2/3)/(2*b)$

$$3.396 \quad \int \frac{1}{x \sqrt[3]{a+bx}} dx$$

Optimal. Leaf size=79

$$\frac{3 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2\sqrt[3]{a}} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt[3]{a}} - \frac{\log(x)}{2\sqrt[3]{a}}$$

[Out] $-1/2*\ln(x)/a^{(1/3)}+3/2*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(1/3)}+\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}})*3^{(1/2)}/a^{(1/3)}$

Rubi [A] time = 0.03, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {55, 617, 204, 31}

$$\frac{3 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2\sqrt[3]{a}} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt[3]{a}} - \frac{\log(x)}{2\sqrt[3]{a}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a + b*x)^(1/3)),x]

[Out] $(\text{Sqrt}[3]*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/a^{(1/3)} - \text{Log}[x]/(2*a^{(1/3)}) + (3*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}])/(2*a^{(1/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(−1), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 55

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_.)*(x_)^2)^(−1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x\sqrt[3]{a+bx}} dx &= -\frac{\log(x)}{2\sqrt[3]{a}} + \frac{3}{2} \text{Subst}\left(\int \frac{1}{a^{2/3} + \sqrt[3]{a}x + x^2} dx, x, \sqrt[3]{a+bx}\right) - \frac{3 \text{Subst}\left(\int \frac{1}{\sqrt[3]{a}-x} dx, x, \sqrt[3]{a+bx}\right)}{2\sqrt[3]{a}} \\ &= -\frac{\log(x)}{2\sqrt[3]{a}} + \frac{3 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2\sqrt[3]{a}} - \frac{3 \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}\right)}{\sqrt[3]{a}} \\ &= \frac{\sqrt{3} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt[3]{a}} - \frac{\log(x)}{2\sqrt[3]{a}} + \frac{3 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2\sqrt[3]{a}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 66, normalized size = 0.84

$$\frac{3 \log(\sqrt[3]{a} - \sqrt[3]{a+bx}) + 2\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}} + 1\right) - \log(x)}{2\sqrt[3]{a}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)^(1/3)),x]

[Out] (2*Sqrt[3]*ArcTan[(1 + (2*(a + b*x)^(1/3))/a^(1/3))/Sqrt[3]] - Log[x] + 3*Log[a^(1/3) - (a + b*x)^(1/3)])/(2*a^(1/3))

fricas [A] time = 0.55, size = 213, normalized size = 2.70

$$\frac{\sqrt{3} a \sqrt{-\frac{1}{2} \frac{1}{a^{\frac{2}{3}}}} \log \left(\frac{2bx + \sqrt{3} \left(2(bx+a)^{\frac{2}{3}} a^{\frac{2}{3}} - (bx+a)^{\frac{1}{3}} a - a^{\frac{4}{3}} \right) \sqrt{-\frac{1}{2} \frac{1}{a^{\frac{2}{3}}}} - 3(bx+a)^{\frac{1}{3}} a^{\frac{2}{3}} + 3a}{x} \right)}{2a} - a^{\frac{2}{3}} \log \left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + a^{\frac{2}{3}} \right) +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(1/3),x, algorithm="fricas")

[Out] [1/2*(sqrt(3)*a*sqrt(-1/a^(2/3))*log((2*b*x + sqrt(3)*(2*(b*x + a)^(2/3)*a^(2/3) - (b*x + a)^(1/3)*a - a^(4/3))*sqrt(-1/a^(2/3)) - 3*(b*x + a)^(1/3)*a^(2/3) + 3*a)/x) - a^(2/3)*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + 2*a^(2/3)*log((b*x + a)^(1/3) - a^(1/3)))/a, 1/2*(2*sqrt(3)*a^(2/3)*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3)) - a^(2/3)*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + 2*a^(2/3)*log((b*x + a)^(1/3) - a^(1/3)))/a]

giac [A] time = 2.37, size = 77, normalized size = 0.97

$$\frac{\sqrt{3} \arctan \left(\frac{\sqrt{3} \left(2(bx+a)^{\frac{1}{3}} + a^{\frac{1}{3}} \right)}{3a^{\frac{1}{3}}} \right)}{a^{\frac{1}{3}}} - \frac{\log \left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + a^{\frac{2}{3}} \right)}{2a^{\frac{1}{3}}} + \frac{\log \left(\left| (bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}} \right| \right)}{a^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(1/3),x, algorithm="giac")

[Out] sqrt(3)*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3))/a^(1/3) - 1/2*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(1/3) + log(abs((b*x + a)^(1/3) - a^(1/3)))/a^(1/3)

maple [A] time = 0.00, size = 75, normalized size = 0.95

$$\frac{\sqrt{3} \arctan \left(\frac{\sqrt{3} \left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}} + 1 \right)}{3} \right)}{a^{\frac{1}{3}}} + \frac{\ln \left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}} \right)}{a^{\frac{1}{3}}} - \frac{\ln \left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}} \right)}{2a^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x/(b*x+a)^(1/3),x)`

[Out] $1/a^{1/3}*\ln(-a^{1/3}+(b*x+a)^{1/3})-1/2/a^{1/3}*\ln(a^{2/3}+(b*x+a)^{1/3})*a^{1/3}+(b*x+a)^{2/3}+3^{1/2}/a^{1/3}*\arctan(1/3*3^{1/2}*(2*(b*x+a)^{1/3}/a^{1/3}+1))$

maxima [A] time = 2.93, size = 76, normalized size = 0.96

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{a^{\frac{1}{3}}} - \frac{\log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)}{2a^{\frac{1}{3}}} + \frac{\log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)}{a^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b*x+a)^(1/3),x, algorithm="maxima")`

[Out] $\sqrt{3}*\arctan(1/3*\sqrt{3}*(2*(b*x+a)^{1/3}+a^{1/3})/a^{1/3})/a^{1/3}-1/2*\log((b*x+a)^{2/3}+(b*x+a)^{1/3}*a^{1/3}+a^{2/3})/a^{1/3}+\log((b*x+a)^{1/3}-a^{1/3})/a^{1/3}$

mupad [B] time = 0.09, size = 99, normalized size = 1.25

$$\frac{\ln\left(9(a+bx)^{1/3}-9a^{1/3}\right)}{a^{1/3}} + \frac{\ln\left(9(a+bx)^{1/3}-\frac{9a^{1/3}(-1+\sqrt{3}i)^2}{4}\right)(-1+\sqrt{3}i)}{2a^{1/3}} - \frac{\ln\left(9(a+bx)^{1/3}-\frac{9a^{1/3}(1+\sqrt{3}i)^2}{4}\right)}{2a^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(a+b*x)^(1/3)),x)`

[Out] $\log(9*(a+b*x)^{1/3}-9*a^{1/3})/a^{1/3}+(\log(9*(a+b*x)^{1/3}-(9*a^{1/3}*(3^{1/2}*1i-1)^2/4)*(3^{1/2}*1i-1))/(2*a^{1/3})-(\log(9*(a+b*x)^{1/3}-(9*a^{1/3}*(3^{1/2}*1i+1)^2/4)*(3^{1/2}*1i+1))/(2*a^{1/3}))$

sympy [C] time = 1.88, size = 155, normalized size = 1.96

$$\frac{2\log\left(1-\frac{\sqrt[3]{b}\sqrt[3]{\frac{a}{b}+x}}{\sqrt[3]{a}}\right)\Gamma\left(\frac{2}{3}\right)}{3\sqrt[3]{a}\Gamma\left(\frac{5}{3}\right)} + \frac{2e^{\frac{2i\pi}{3}}\log\left(1-\frac{\sqrt[3]{b}\sqrt[3]{\frac{a}{b}+xe^{\frac{2i\pi}{3}}}}{\sqrt[3]{a}}\right)\Gamma\left(\frac{2}{3}\right)}{3\sqrt[3]{a}\Gamma\left(\frac{5}{3}\right)} + \frac{2e^{-\frac{2i\pi}{3}}\log\left(1-\frac{\sqrt[3]{b}\sqrt[3]{\frac{a}{b}+xe^{\frac{4i\pi}{3}}}}{\sqrt[3]{a}}\right)\Gamma\left(\frac{2}{3}\right)}{3\sqrt[3]{a}\Gamma\left(\frac{5}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x/(b*x+a)**(1/3),x)
```

```
[Out] 2*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(2/3)/(3*a**(1/3)*gamma(5/3)) + 2*exp(2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(2*I*pi/3)/a**(1/3))*gamma(2/3)/(3*a**(1/3)*gamma(5/3)) + 2*exp(-2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(4*I*pi/3)/a**(1/3))*gamma(2/3)/(3*a**(1/3)*gamma(5/3))
```

$$3.397 \quad \int \frac{1}{x^2 \sqrt[3]{a+bx}} dx$$

Optimal. Leaf size=100

$$\frac{b \log(x)}{6a^{4/3}} - \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{4/3}} - \frac{b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{4/3}} - \frac{(a+bx)^{2/3}}{ax}$$

[Out] $-(b*x+a)^{(2/3)}/a/x+1/6*b*\ln(x)/a^{(4/3)}-1/2*b*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(4/3)}-1/3*b*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}})/a^{(4/3)*3^{(1/2)}}$

Rubi [A] time = 0.03, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 55, 617, 204, 31}

$$\frac{b \log(x)}{6a^{4/3}} - \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{4/3}} - \frac{b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{4/3}} - \frac{(a+bx)^{2/3}}{ax}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(a + b*x)^(1/3)),x]

[Out] $-((a + b*x)^{(2/3)}/(a*x)) - (b*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})]/(\text{Sqrt}[3]*a^{(1/3)}))/(\text{Sqrt}[3]*a^{(4/3)}) + (b*\text{Log}[x])/(6*a^{(4/3)}) - (b*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}])/(2*a^{(4/3)})$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 55

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x
] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)],
x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])] /;
FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^2 \sqrt[3]{a+bx}} dx &= -\frac{(a+bx)^{2/3}}{ax} - \frac{b \int \frac{1}{x \sqrt[3]{a+bx}} dx}{3a} \\
&= -\frac{(a+bx)^{2/3}}{ax} + \frac{b \log(x)}{6a^{4/3}} + \frac{b \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{2a^{4/3}} - \frac{b \operatorname{Subst}\left(\int \frac{1}{a^{2/3} + \sqrt[3]{a}x + x^2} dx, x, \sqrt[3]{a+bx}\right)}{2a} \\
&= -\frac{(a+bx)^{2/3}}{ax} + \frac{b \log(x)}{6a^{4/3}} - \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{4/3}} + \frac{b \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}\right)}{a^{4/3}} \\
&= -\frac{(a+bx)^{2/3}}{ax} - \frac{b \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3} a^{4/3}} + \frac{b \log(x)}{6a^{4/3}} - \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{4/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.33

$$\frac{3b(a+bx)^{2/3} {}_2F_1\left(\frac{2}{3}, 2; \frac{5}{3}; \frac{bx}{a} + 1\right)}{2a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)^(1/3)),x]

[Out] (3*b*(a + b*x)^(2/3)*Hypergeometric2F1[2/3, 2, 5/3, 1 + (b*x)/a])/(2*a^2)

fricas [A] time = 0.51, size = 306, normalized size = 3.06

$$\frac{3\sqrt{\frac{1}{3}}abx\sqrt{\frac{(-a)^{\frac{1}{3}}}{a}}\log\left(\frac{2bx-3\sqrt{\frac{1}{3}}\left(2(bx+a)^{\frac{2}{3}}(-a)^{\frac{2}{3}}-(bx+a)^{\frac{1}{3}}a+(-a)^{\frac{1}{3}}a\right)\sqrt{\frac{(-a)^{\frac{1}{3}}}{a}}-3(bx+a)^{\frac{1}{3}}(-a)^{\frac{2}{3}}+3a}{x}}{(-a)^{\frac{2}{3}}bx\log\left((bx+a)^{\frac{2}{3}}\right)}\right)}{6a^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(1/3),x, algorithm="fricas")

[Out] [1/6*(3*sqrt(1/3)*a*b*x*sqrt((-a)^(1/3)/a)*log((2*b*x - 3*sqrt(1/3)*(2*(b*x + a)^(2/3)*(-a)^(2/3) - (b*x + a)^(1/3)*a + (-a)^(1/3)*a)*sqrt((-a)^(1/3)/a) - 3*(b*x + a)^(1/3)*(-a)^(2/3) + 3*a)/x) + (-a)^(2/3)*b*x*log((b*x + a)^(2/3) - (b*x + a)^(1/3)*(-a)^(1/3) + (-a)^(2/3)) - 2*(-a)^(2/3)*b*x*log((b*x + a)^(1/3) + (-a)^(1/3)) - 6*(b*x + a)^(2/3)*a)/(a^2*x), -1/6*(6*sqrt(1/3)*a*b*x*sqrt(-(-a)^(1/3)/a)*arctan(sqrt(1/3)*(2*(b*x + a)^(1/3) - (-a)^(1/3))*sqrt(-(-a)^(1/3)/a)) - (-a)^(2/3)*b*x*log((b*x + a)^(2/3) - (b*x + a)^(1/3)*(-a)^(1/3) + (-a)^(2/3)) + 2*(-a)^(2/3)*b*x*log((b*x + a)^(1/3) + (-a)^(1/3)) + 6*(b*x + a)^(2/3)*a)/(a^2*x)]

giac [A] time = 2.45, size = 109, normalized size = 1.09

$$\frac{2\sqrt{3}b^2\arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{a^{\frac{4}{3}}}-\frac{b^2\log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)}{a^{\frac{4}{3}}}+\frac{2b^2\log\left(\left|(bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right|\right)}{a^{\frac{4}{3}}}+\frac{6(bx+a)^{\frac{2}{3}}b}{ax}}{6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(1/3),x, algorithm="giac")

[Out] -1/6*(2*sqrt(3)*b^2*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3)))/a^(4/3) - b^2*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(4/3) + 2*b^2*log(abs((b*x + a)^(1/3) - a^(1/3)))/a^(4/3) + 6*(b*x + a)^(2/3)*b/(a*x)/b

maple [A] time = 0.01, size = 95, normalized size = 0.95

$$\frac{\sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)}{3a^{\frac{4}{3}}}-\frac{b \ln\left(-a^{\frac{1}{3}}+(bx+a)^{\frac{1}{3}}\right)}{3a^{\frac{4}{3}}}+\frac{b \ln\left(a^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+(bx+a)^{\frac{2}{3}}\right)}{6a^{\frac{4}{3}}}-\frac{(bx+a)^{\frac{2}{3}}}{ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^(1/3),x)

[Out] $-(b*x+a)^{(2/3)}/a/x-1/3*b/a^{(4/3)}*\ln(-a^{(1/3)}+(b*x+a)^{(1/3)})+1/6*b/a^{(4/3)}*\ln(a^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+(b*x+a)^{(2/3)})-1/3*b/a^{(4/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2*(b*x+a)^{(1/3)}/a^{(1/3)}+1))$

maxima [A] time = 3.00, size = 106, normalized size = 1.06

$$\frac{\sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{3a^{\frac{4}{3}}}-\frac{(bx+a)^{\frac{2}{3}}b}{(bx+a)a-a^2}+\frac{b \log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)}{6a^{\frac{4}{3}}}-\frac{b \log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)}{3a^{\frac{4}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(1/3),x, algorithm="maxima")

[Out] $-1/3*\sqrt{3}*b*\arctan(1/3*\sqrt{3}*(2*(b*x+a)^{(1/3)}+a^{(1/3)})/a^{(1/3)})/a^{(4/3)}-(b*x+a)^{(2/3)}*b/((b*x+a)*a-a^2)+1/6*b*\log((b*x+a)^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+a^{(2/3)})/a^{(4/3)}-1/3*b*\log((b*x+a)^{(1/3)}-a^{(1/3)})/a^{(4/3)}$

mupad [B] time = 0.14, size = 130, normalized size = 1.30

$$\frac{(a+bx)^{2/3}}{ax}+\frac{\ln\left(\frac{(b-\sqrt{3}bi)^2}{4a^{5/3}}-\frac{b^2(a+bx)^{1/3}}{a^2}\right)(b-\sqrt{3}bi)}{6a^{4/3}}+\frac{\ln\left(\frac{(b+\sqrt{3}bi)^2}{4a^{5/3}}-\frac{b^2(a+bx)^{1/3}}{a^2}\right)(b+\sqrt{3}bi)}{6a^{4/3}}-\frac{b \ln((a+bx)^{1/3}-a^{1/3})}{3a^{4/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(a+b*x)^(1/3)),x)

[Out] $(\log((b-3^{(1/2)}*b*1i)^2/(4*a^{(5/3)}))-(b^2*(a+b*x)^{(1/3)})/a^2)*(b-3^{(1/2)}*b*1i)/(6*a^{(4/3)})-(a+b*x)^{(2/3)}/(a*x)+(\log((b+3^{(1/2)}*b*1i)^2/(4*a^{(5/3)}))-(b^2*(a+b*x)^{(1/3)})/a^2)*(b+3^{(1/2)}*b*1i)/(6*a^{(4/3)})$

$$\frac{/(4*a^{(5/3)}) - (b^2*(a + b*x)^{(1/3)})/a^2*(b + 3^{(1/2)*b*1i)))/(6*a^{(4/3)}) - (b*\log((a + b*x)^{(1/3)} - a^{(1/3)})))/(3*a^{(4/3)})}$$

sympy [C] time = 2.20, size = 831, normalized size = 8.31

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/(b*x+a)**(1/3),x)

[Out]
$$\begin{aligned} & -2*a^{(5/3)}*b^{(7/3)}*(a/b + x)^{(4/3)}*\exp(2*I*pi/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}/a^{(1/3)})*\gamma(2/3)/(9*a^{(3/3)}*b^{(4/3)}*(a/b + x)^{(4/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & - 9*a^{(2/3)}*b^{(7/3)}*(a/b + x)^{(7/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & - 2*a^{(5/3)}*b^{(7/3)}*(a/b + x)^{(4/3)}*\exp(-2*I*pi/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_polar(2*I*pi/3)/a^{(1/3)})*\gamma(2/3)/(9*a^{(3/3)}*b^{(4/3)}*(a/b + x)^{(4/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & - 9*a^{(2/3)}*b^{(7/3)}*(a/b + x)^{(7/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & - 2*a^{(5/3)}*b^{(7/3)}*(a/b + x)^{(4/3)}*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_polar(4*I*pi/3)/a^{(1/3)})*\gamma(2/3)/(9*a^{(3/3)}*b^{(4/3)}*(a/b + x)^{(4/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & - 9*a^{(2/3)}*b^{(7/3)}*(a/b + x)^{(7/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & + 2*a^{(2/3)}*b^{(10/3)}*(a/b + x)^{(7/3)}*\exp(2*I*pi/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}/a^{(1/3)})*\gamma(2/3)/(9*a^{(3/3)}*b^{(4/3)}*(a/b + x)^{(4/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & - 9*a^{(2/3)}*b^{(7/3)}*(a/b + x)^{(7/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & + 2*a^{(2/3)}*b^{(10/3)}*(a/b + x)^{(7/3)}*\exp(-2*I*pi/3)*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_polar(2*I*pi/3)/a^{(1/3)})*\gamma(2/3)/(9*a^{(3/3)}*b^{(4/3)}*(a/b + x)^{(4/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & - 9*a^{(2/3)}*b^{(7/3)}*(a/b + x)^{(7/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & + 2*a^{(2/3)}*b^{(10/3)}*(a/b + x)^{(7/3)}*\log(1 - b^{(1/3)}*(a/b + x)^{(1/3)}*\exp_polar(4*I*pi/3)/a^{(1/3)})*\gamma(2/3)/(9*a^{(3/3)}*b^{(4/3)}*(a/b + x)^{(4/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & - 9*a^{(2/3)}*b^{(7/3)}*(a/b + x)^{(7/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & + 6*a*b^{(3/3)}*(a/b + x)^{(2/3)}*\exp(2*I*pi/3)*\gamma(2/3)/(9*a^{(3/3)}*b^{(4/3)}*(a/b + x)^{(4/3)}*\exp(2*I*pi/3)*\gamma(5/3) \\ & - 9*a^{(2/3)}*b^{(7/3)}*(a/b + x)^{(7/3)}*\exp(2*I*pi/3)*\gamma(5/3) \end{aligned}$$

$$3.398 \quad \int \frac{1}{x^3 \sqrt[3]{a+bx}} dx$$

Optimal. Leaf size=130

$$-\frac{b^2 \log(x)}{9a^{7/3}} + \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{3a^{7/3}} + \frac{2b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{7/3}} + \frac{2b(a+bx)^{2/3}}{3a^2x} - \frac{(a+bx)^{2/3}}{2ax^2}$$

[Out] $-1/2*(b*x+a)^{(2/3)}/a/x^2+2/3*b*(b*x+a)^{(2/3)}/a^2/x-1/9*b^2*\ln(x)/a^{(7/3)}+1/3*b^2*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(7/3)}+2/9*b^2*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}})/a^{(7/3)*3^{(1/2)}}$

Rubi [A] time = 0.05, antiderivative size = 130, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 55, 617, 204, 31}

$$-\frac{b^2 \log(x)}{9a^{7/3}} + \frac{b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{3a^{7/3}} + \frac{2b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{7/3}} + \frac{2b(a+bx)^{2/3}}{3a^2x} - \frac{(a+bx)^{2/3}}{2ax^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(a + b*x)^(1/3)),x]

[Out] $-(a + b*x)^{(2/3)}/(2*a*x^2) + (2*b*(a + b*x)^{(2/3)})/(3*a^2*x) + (2*b^2*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/(3*\text{Sqrt}[3]*a^{(7/3)}) - (b^2*\text{Log}[x])/(9*a^{(7/3)}) + (b^2*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}])/(3*a^{(7/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 55

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x
] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)],
x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])) /;
FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c]) /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^3 \sqrt[3]{a+bx}} dx &= -\frac{(a+bx)^{2/3}}{2ax^2} - \frac{(2b) \int \frac{1}{x^2 \sqrt[3]{a+bx}} dx}{3a} \\
&= -\frac{(a+bx)^{2/3}}{2ax^2} + \frac{2b(a+bx)^{2/3}}{3a^2x} + \frac{(2b^2) \int \frac{1}{x \sqrt[3]{a+bx}} dx}{9a^2} \\
&= -\frac{(a+bx)^{2/3}}{2ax^2} + \frac{2b(a+bx)^{2/3}}{3a^2x} - \frac{b^2 \log(x)}{9a^{7/3}} - \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{3a^{7/3}} + \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{a+bx}\right)}{3a^{7/3}} \\
&= -\frac{(a+bx)^{2/3}}{2ax^2} + \frac{2b(a+bx)^{2/3}}{3a^2x} - \frac{b^2 \log(x)}{9a^{7/3}} + \frac{b^2 \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)}{3a^{7/3}} - \frac{(2b^2) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{a+bx}\right)}{3a^{7/3}} \\
&= -\frac{(a+bx)^{2/3}}{2ax^2} + \frac{2b(a+bx)^{2/3}}{3a^2x} + \frac{2b^2 \tan^{-1}\left(\frac{1 + 2\sqrt[3]{a+bx}}{\sqrt[3]{a}}\right)}{3\sqrt{3}a^{7/3}} - \frac{b^2 \log(x)}{9a^{7/3}} + \frac{b^2 \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)}{3a^{7/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.27

$$\frac{3b^2(a+bx)^{2/3} {}_2F_1\left(\frac{2}{3}, 3; \frac{5}{3}; \frac{bx}{a} + 1\right)}{2a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)^(1/3)),x]

[Out] (-3*b^2*(a + b*x)^(2/3)*Hypergeometric2F1[2/3, 3, 5/3, 1 + (b*x)/a])/(2*a^3)

fricas [A] time = 0.53, size = 296, normalized size = 2.28

$$\frac{6\sqrt{\frac{1}{3}}ab^2x^2\sqrt{-\frac{1}{a^3}}\log\left(\frac{2bx+3\sqrt{\frac{1}{3}}\left(2(bx+a)^{\frac{2}{3}}a^{\frac{2}{3}}-(bx+a)^{\frac{1}{3}}a^{\frac{4}{3}}\right)\sqrt{-\frac{1}{2}-3(bx+a)^{\frac{1}{3}}a^{\frac{2}{3}}+3a}}{x}}\right)-2a^{\frac{2}{3}}b^2x^2\log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{2}{3}}\right)}{18a^3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(1/3),x, algorithm="fricas")

[Out] [1/18*(6*sqrt(1/3)*a*b^2*x^2*sqrt(-1/a^(2/3))*log((2*b*x + 3*sqrt(1/3))*(2*(b*x + a)^(2/3)*a^(2/3) - (b*x + a)^(1/3)*a - a^(4/3))*sqrt(-1/a^(2/3)) - 3*(b*x + a)^(1/3)*a^(2/3) + 3*a)/x - 2*a^(2/3)*b^2*x^2*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + 4*a^(2/3)*b^2*x^2*log((b*x + a)^(1/3) - a^(1/3)) + 3*(4*a*b*x - 3*a^2)*(b*x + a)^(2/3))/(a^3*x^2), 1/18*(12*sqrt(1/3)*a^(2/3)*b^2*x^2*arctan(sqrt(1/3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3)) - 2*a^(2/3)*b^2*x^2*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + 4*a^(2/3)*b^2*x^2*log((b*x + a)^(1/3) - a^(1/3)) + 3*(4*a*b*x - 3*a^2)*(b*x + a)^(2/3))/(a^3*x^2)]

giac [A] time = 2.24, size = 130, normalized size = 1.00

$$\frac{4\sqrt{3}b^3\arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{a^{\frac{7}{3}}}-\frac{2b^3\log\left(\frac{(bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}}{a^{\frac{1}{3}}}\right)}{a^{\frac{7}{3}}}+\frac{4b^3\log\left(\frac{(bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}}{a^{\frac{1}{3}}}\right)}{a^{\frac{7}{3}}}+\frac{3\left(4(bx+a)^{\frac{5}{3}}b^3-7(bx+a)^{\frac{2}{3}}ab^3\right)}{a^2b^2x^2}$$

18b

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(1/3),x, algorithm="giac")

[Out] $\frac{1}{18} \cdot (4 \cdot \sqrt{3} \cdot b^3 \cdot \arctan(\frac{1}{3} \cdot \sqrt{3} \cdot (2 \cdot (b \cdot x + a)^{1/3} + a^{1/3}))) / a^{1/3} - 2 \cdot b^3 \cdot \log((b \cdot x + a)^{2/3} + (b \cdot x + a)^{1/3} \cdot a^{1/3} + a^{2/3})) / a^{7/3} + 4 \cdot b^3 \cdot \log(\text{abs}((b \cdot x + a)^{1/3} - a^{1/3})) / a^{7/3} + 3 \cdot (4 \cdot (b \cdot x + a)^{5/3} \cdot b^3 - 7 \cdot (b \cdot x + a)^{2/3} \cdot a \cdot b^3) / (a^2 \cdot b^2 \cdot x^2) / b$

maple [A] time = 0.01, size = 117, normalized size = 0.90

$$\frac{2\sqrt{3} b^2 \arctan\left(\frac{\sqrt{3} \left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}} + 1\right)}{3}\right)}{9a^{\frac{7}{3}}} + \frac{2b^2 \ln\left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}\right)}{9a^{\frac{7}{3}}} - \frac{b^2 \ln\left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}}\right)}{9a^{\frac{7}{3}}} + \frac{2(bx+a)^{\frac{2}{3}}}{3a^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a)^(1/3),x)

[Out] $-1/2 \cdot (b \cdot x + a)^{2/3} / a / x^2 + 2/3 \cdot b \cdot (b \cdot x + a)^{2/3} / a^2 / x + 2/9 \cdot b^2 / a^{7/3} \cdot \ln(-a^{1/3} + (b \cdot x + a)^{1/3}) - 1/9 \cdot b^2 / a^{7/3} \cdot \ln(a^{2/3} + (b \cdot x + a)^{1/3} \cdot a^{1/3} + (b \cdot x + a)^{2/3}) + 2/9 \cdot b^2 / a^{7/3} \cdot 3^{1/2} \cdot \arctan(1/3 \cdot 3^{1/2} \cdot (2 \cdot (b \cdot x + a)^{1/3} / a^{1/3} + 1))$

maxima [A] time = 3.03, size = 142, normalized size = 1.09

$$\frac{2\sqrt{3} b^2 \arctan\left(\frac{\sqrt{3} \left(2 \frac{(bx+a)^{\frac{1}{3}}}{3a^{\frac{1}{3}}} + a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{9a^{\frac{7}{3}}} - \frac{b^2 \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{9a^{\frac{7}{3}}} + \frac{2b^2 \log\left((bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right)}{9a^{\frac{7}{3}}} + \frac{4(bx+a)^{\frac{2}{3}}}{6((bx+a)^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(1/3),x, algorithm="maxima")

[Out] $\frac{2}{9} \cdot \sqrt{3} \cdot b^2 \cdot \arctan(\frac{1}{3} \cdot \sqrt{3} \cdot (2 \cdot (b \cdot x + a)^{1/3} + a^{1/3})) / a^{7/3} - \frac{1}{9} \cdot b^2 \cdot \log((b \cdot x + a)^{2/3} + (b \cdot x + a)^{1/3} \cdot a^{1/3} + a^{2/3}) / a^{7/3} + \frac{2}{9} \cdot b^2 \cdot \log((b \cdot x + a)^{1/3} - a^{1/3}) / a^{7/3} + \frac{1}{6} \cdot (4 \cdot (b \cdot x + a)^{5/3} \cdot b^2 - 7 \cdot (b \cdot x + a)^{2/3} \cdot a \cdot b^2) / ((b \cdot x + a)^2 \cdot a^2 - 2 \cdot (b \cdot x + a) \cdot a^3 + a^4)$

mupad [B] time = 0.23, size = 182, normalized size = 1.40

$$\frac{2b^2 \ln\left((a+bx)^{1/3} - a^{1/3}\right)}{9a^{7/3}} - \frac{\frac{7b^2(a+bx)^{2/3}}{6a} - \frac{2b^2(a+bx)^{5/3}}{3a^2}}{(a+bx)^2 - 2a(a+bx) + a^2} - \frac{\ln\left(\frac{4b^4(a+bx)^{1/3}}{9a^4} - \frac{(b^2 + \sqrt{3}b^2i)^2}{9a^{11/3}}\right)}{9a^{7/3}} (b^2 + \sqrt{3}b^2i) + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(a + b*x)^(1/3)), x)

[Out] (2*b^2*log((a + b*x)^(1/3) - a^(1/3)))/(9*a^(7/3)) - ((7*b^2*(a + b*x)^(2/3))/(6*a) - (2*b^2*(a + b*x)^(5/3))/(3*a^2))/((a + b*x)^2 - 2*a*(a + b*x) + a^2) - (log((4*b^4*(a + b*x)^(1/3))/(9*a^4) - (3^(1/2)*b^2*i + b^2)^2/(9*a^(11/3))))*(3^(1/2)*b^2*i + b^2)/(9*a^(7/3)) + (b^2*log((4*b^4*(a + b*x)^(1/3))/(9*a^4) - (9*b^4*((3^(1/2)*i)/9 - 1/9)^2)/a^(11/3))*((3^(1/2)*i)/9 - 1/9))/a^(7/3)

sympy [C] time = 2.59, size = 2730, normalized size = 21.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(b*x+a)**(1/3), x)

[Out] 4*a**(14/3)*b**(10/3)*(a/b + x)**(4/3)*exp(2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(2/3)/(27*a**7*b**(4/3)*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(5/3) - 81*a**6*b**(7/3)*(a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(5/3) + 81*a**5*b**(10/3)*(a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(5/3) - 27*a**4*b**(13/3)*(a/b + x)**(13/3)*exp(2*I*pi/3)*gamma(5/3)) + 4*a**(14/3)*b**(10/3)*(a/b + x)**(4/3)*exp(-2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(2/3)/(27*a**7*b**(4/3)*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(5/3) - 81*a**6*b**(7/3)*(a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(5/3) + 81*a**5*b**(10/3)*(a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(5/3) - 27*a**4*b**(13/3)*(a/b + x)**(13/3)*exp(2*I*pi/3)*gamma(5/3)) + 4*a**(14/3)*b**(10/3)*(a/b + x)**(4/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(2/3)/(27*a**7*b**(4/3)*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(5/3) - 81*a**6*b**(7/3)*(a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(5/3) + 81*a**5*b**(10/3)*(a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(5/3) - 27*a**4*b**(13/3)*(a/b + x)**(13/3)*exp(2*I*pi/3)*gamma(5/3)) - 12*a**(11/3)*b**(13/3)*(a/b + x)**(7/3)*exp(2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(2/3)/(27*a**7*b**(4/3)*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(5/3) - 81*a**6*b**(7/3)*(a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(5/3) + 81*a**5*b**(10/3)*(a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(5/3) - 27*a**4*b**(13/3)*(a/b + x)**(13/3)*exp(2*I*pi/3)*gamma(5/3))

$$\begin{aligned}
& (13/3) * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 12 * a^{11/3} * b^{13/3} * (a/b + x)^{7/3} * \\
& \exp(-2 * I * \pi / 3) * \log(1 - b^{1/3} * (a/b + x)^{1/3} * \exp_{\text{polar}}(2 * I * \pi / 3) / a^{1/3}) * \text{gamma}(2/3) / (27 * a^{7/3} * b^{4/3} * (a/b + x)^{4/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) \\
& - 81 * a^{6/3} * b^{7/3} * (a/b + x)^{7/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) + 81 * a^{5/3} * b^{10/3} * (a/b + x)^{10/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 27 * a^{4/3} * b^{13/3} * (a/b + \\
& x)^{13/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 12 * a^{11/3} * b^{13/3} * (a/b + x)^{7/3} * \log(1 - b^{1/3} * (a/b + x)^{1/3} * \exp_{\text{polar}}(4 * I * \pi / 3) / a^{1/3}) * \text{gamma}(\\
& 2/3) / (27 * a^{7/3} * b^{4/3} * (a/b + x)^{4/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 81 * a^{6/3} * \\
& b^{7/3} * (a/b + x)^{7/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) + 81 * a^{5/3} * b^{10/3} * (a/b \\
& + x)^{10/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 27 * a^{4/3} * b^{13/3} * (a/b + x)^{13/3} \\
&) * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) + 12 * a^{8/3} * b^{16/3} * (a/b + x)^{10/3} * \exp(2 \\
& * I * \pi / 3) * \log(1 - b^{1/3} * (a/b + x)^{1/3} / a^{1/3}) * \text{gamma}(2/3) / (27 * a^{7/3} * b^{ \\
& * (4/3) * (a/b + x)^{4/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 81 * a^{6/3} * b^{7/3} * (a/b + \\
& x)^{7/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) + 81 * a^{5/3} * b^{10/3} * (a/b + x)^{10/3} * \exp \\
& (2 * I * \pi / 3) * \text{gamma}(5/3) - 27 * a^{4/3} * b^{13/3} * (a/b + x)^{13/3} * \exp(2 * I * \pi / 3) * \\
& \text{gamma}(5/3) + 12 * a^{8/3} * b^{16/3} * (a/b + x)^{10/3} * \exp(-2 * I * \pi / 3) * \log(1 \\
& - b^{1/3} * (a/b + x)^{1/3} * \exp_{\text{polar}}(2 * I * \pi / 3) / a^{1/3}) * \text{gamma}(2/3) / (27 * a^{ \\
& * 7/3} * b^{4/3} * (a/b + x)^{4/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 81 * a^{6/3} * b^{7/3} * (a \\
& / b + x)^{7/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) + 81 * a^{5/3} * b^{10/3} * (a/b + x)^{10/ \\
& 3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 27 * a^{4/3} * b^{13/3} * (a/b + x)^{13/3} * \exp(2 * I * \pi \\
& / 3) * \text{gamma}(5/3) + 12 * a^{8/3} * b^{16/3} * (a/b + x)^{10/3} * \log(1 - b^{1/3} \\
& * (a/b + x)^{1/3} * \exp_{\text{polar}}(4 * I * \pi / 3) / a^{1/3}) * \text{gamma}(2/3) / (27 * a^{7/3} * b^{4/3} \\
&) * (a/b + x)^{4/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 81 * a^{6/3} * b^{7/3} * (a/b + x)^{7/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) + 81 * a^{5/3} * b^{10/3} * (a/b + x)^{10/3} * \exp(2 * I \\
& * \pi / 3) * \text{gamma}(5/3) - 27 * a^{4/3} * b^{13/3} * (a/b + x)^{13/3} * \exp(2 * I * \pi / 3) * \text{gamma} \\
& (5/3) - 4 * a^{5/3} * b^{19/3} * (a/b + x)^{13/3} * \exp(2 * I * \pi / 3) * \log(1 - b^{1/3} * (a/b + x)^{1/3} / a^{1/3}) * \text{gamma}(2/3) / (27 * a^{7/3} * b^{4/3} * (a/b + x)^{4/3} \\
&) * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 81 * a^{6/3} * b^{7/3} * (a/b + x)^{7/3} * \exp(2 * I * \pi / 3) \\
&) * \text{gamma}(5/3) + 81 * a^{5/3} * b^{10/3} * (a/b + x)^{10/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) \\
& - 27 * a^{4/3} * b^{13/3} * (a/b + x)^{13/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 4 * a^{5/ \\
& 3} * b^{19/3} * (a/b + x)^{13/3} * \exp(-2 * I * \pi / 3) * \log(1 - b^{1/3} * (a/b + x)^{1/3} * \exp_{\text{polar}}(2 * I * \pi / 3) / a^{1/3}) * \text{gamma}(2/3) / (27 * a^{7/3} * b^{4/3} * (a/b + x)^{4/3} \\
&) * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 81 * a^{6/3} * b^{7/3} * (a/b + x)^{7/3} * \exp(2 * I * \pi \\
& / 3) * \text{gamma}(5/3) + 81 * a^{5/3} * b^{10/3} * (a/b + x)^{10/3} * \exp(2 * I * \pi / 3) * \text{gamma}(\\
& 5/3) - 27 * a^{4/3} * b^{13/3} * (a/b + x)^{13/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 4 * a^{ \\
& * (5/3) * b^{19/3} * (a/b + x)^{13/3} * \log(1 - b^{1/3} * (a/b + x)^{1/3} * \exp_{\text{polar}}(4 * I * \pi / 3) / a^{1/3}) * \text{gamma}(2/3) / (27 * a^{7/3} * b^{4/3} * (a/b + x)^{4/3} * \exp(2 \\
& * I * \pi / 3) * \text{gamma}(5/3) - 81 * a^{6/3} * b^{7/3} * (a/b + x)^{7/3} * \exp(2 * I * \pi / 3) * \text{gamma} \\
& (5/3) + 81 * a^{5/3} * b^{10/3} * (a/b + x)^{10/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 27 * a \\
& ^{4/3} * b^{13/3} * (a/b + x)^{13/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 21 * a^{4/3} * b^{13/3} * (a \\
& / b + x)^2 * \exp(2 * I * \pi / 3) * \text{gamma}(2/3) / (27 * a^{7/3} * b^{4/3} * (a/b + x)^{4/3} * \exp(\\
& 2 * I * \pi / 3) * \text{gamma}(5/3) - 81 * a^{6/3} * b^{7/3} * (a/b + x)^{7/3} * \exp(2 * I * \pi / 3) * \text{gamma} \\
& a(5/3) + 81 * a^{5/3} * b^{10/3} * (a/b + x)^{10/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) - 27 * \\
& a^{4/3} * b^{13/3} * (a/b + x)^{13/3} * \exp(2 * I * \pi / 3) * \text{gamma}(5/3) + 33 * a^{3/3} * b^{15/3} * (\\
& a/b + x)^3 * \exp(2 * I * \pi / 3) * \text{gamma}(2/3) / (27 * a^{7/3} * b^{4/3} * (a/b + x)^{4/3} * \exp
\end{aligned}$$

$$\begin{aligned}
& (2I\pi/3)*\text{gamma}(5/3) - 81*a**6*b**(7/3)*(a/b + x)**(7/3)*\exp(2I\pi/3)*\text{gamma}(5/3) \\
& + 81*a**5*b**(10/3)*(a/b + x)**(10/3)*\exp(2I\pi/3)*\text{gamma}(5/3) - 27 \\
& *a**4*b**(13/3)*(a/b + x)**(13/3)*\exp(2I\pi/3)*\text{gamma}(5/3) - 12*a**2*b**6* \\
& (a/b + x)**4*\exp(2I\pi/3)*\text{gamma}(2/3)/(27*a**7*b**(4/3)*(a/b + x)**(4/3)*\exp(2I\pi/3)*\text{gamma}(5/3) \\
& - 81*a**6*b**(7/3)*(a/b + x)**(7/3)*\exp(2I\pi/3)*\text{gamma}(5/3) + 81*a**5*b**(10/3)*(a/b + x)**(10/3)*\exp(2I\pi/3)*\text{gamma}(5/3) - 27 \\
& *a**4*b**(13/3)*(a/b + x)**(13/3)*\exp(2I\pi/3)*\text{gamma}(5/3)
\end{aligned}$$

$$3.399 \quad \int \frac{x^3}{\sqrt[3]{-a+bx}} dx$$

Optimal. Leaf size=80

$$\frac{3a^3(bx-a)^{2/3}}{2b^4} + \frac{9a^2(bx-a)^{5/3}}{5b^4} + \frac{3(bx-a)^{11/3}}{11b^4} + \frac{9a(bx-a)^{8/3}}{8b^4}$$

[Out] $3/2*a^3*(b*x-a)^{(2/3)}/b^4+9/5*a^2*(b*x-a)^{(5/3)}/b^4+9/8*a*(b*x-a)^{(8/3)}/b^4+3/11*(b*x-a)^{(11/3)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{9a^2(bx-a)^{5/3}}{5b^4} + \frac{3a^3(bx-a)^{2/3}}{2b^4} + \frac{3(bx-a)^{11/3}}{11b^4} + \frac{9a(bx-a)^{8/3}}{8b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3/(-a + b*x)^(1/3), x]

[Out] $(3*a^3*(-a + b*x)^{(2/3)})/(2*b^4) + (9*a^2*(-a + b*x)^{(5/3)})/(5*b^4) + (9*a*(-a + b*x)^{(8/3)})/(8*b^4) + (3*(-a + b*x)^{(11/3)})/(11*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{\sqrt[3]{-a+bx}} dx &= \int \left(\frac{a^3}{b^3 \sqrt[3]{-a+bx}} + \frac{3a^2(-a+bx)^{2/3}}{b^3} + \frac{3a(-a+bx)^{5/3}}{b^3} + \frac{(-a+bx)^{8/3}}{b^3} \right) dx \\ &= \frac{3a^3(-a+bx)^{2/3}}{2b^4} + \frac{9a^2(-a+bx)^{5/3}}{5b^4} + \frac{9a(-a+bx)^{8/3}}{8b^4} + \frac{3(-a+bx)^{11/3}}{11b^4} \end{aligned}$$

Mathematica [A] time = 0.03, size = 48, normalized size = 0.60

$$\frac{3(bx-a)^{2/3} (81a^3 + 54a^2bx + 45ab^2x^2 + 40b^3x^3)}{440b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(-a + b*x)^(1/3), x]

[Out] (3*(-a + b*x)^(2/3)*(81*a^3 + 54*a^2*b*x + 45*a*b^2*x^2 + 40*b^3*x^3))/(440*b^4)

fricas [A] time = 0.50, size = 44, normalized size = 0.55

$$\frac{3 \left(40 b^3 x^3 + 45 a b^2 x^2 + 54 a^2 b x + 81 a^3 \right) (b x - a)^{\frac{2}{3}}}{440 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x-a)^(1/3), x, algorithm="fricas")

[Out] 3/440*(40*b^3*x^3 + 45*a*b^2*x^2 + 54*a^2*b*x + 81*a^3)*(b*x - a)^(2/3)/b^4

giac [A] time = 1.07, size = 57, normalized size = 0.71

$$\frac{3 \left(40 (b x - a)^{\frac{11}{3}} + 165 (b x - a)^{\frac{8}{3}} a + 264 (b x - a)^{\frac{5}{3}} a^2 + 220 (b x - a)^{\frac{2}{3}} a^3 \right)}{440 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x-a)^(1/3), x, algorithm="giac")

[Out] 3/440*(40*(b*x - a)^(11/3) + 165*(b*x - a)^(8/3)*a + 264*(b*x - a)^(5/3)*a^2 + 220*(b*x - a)^(2/3)*a^3)/b^4

maple [A] time = 0.00, size = 45, normalized size = 0.56

$$\frac{3 \left(40 b^3 x^3 + 45 a b^2 x^2 + 54 a^2 b x + 81 a^3 \right) (b x - a)^{\frac{2}{3}}}{440 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x-a)^(1/3), x)

[Out] 3/440*(40*b^3*x^3+45*a*b^2*x^2+54*a^2*b*x+81*a^3)/b^4*(b*x-a)^(2/3)

maxima [A] time = 1.34, size = 64, normalized size = 0.80

$$\frac{3 (b x - a)^{\frac{11}{3}}}{11 b^4} + \frac{9 (b x - a)^{\frac{8}{3}} a}{8 b^4} + \frac{9 (b x - a)^{\frac{5}{3}} a^2}{5 b^4} + \frac{3 (b x - a)^{\frac{2}{3}} a^3}{2 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x-a)^(1/3),x, algorithm="maxima")

[Out] $\frac{3}{11}(bx - a)^{11/3}/b^4 + \frac{9}{8}(bx - a)^{8/3}a/b^4 + \frac{9}{5}(bx - a)^{5/3}a^2/b^4 + \frac{3}{2}(bx - a)^{2/3}a^3/b^4$

mupad [B] time = 0.05, size = 64, normalized size = 0.80

$$\frac{3(bx - a)^{11/3}}{11b^4} + \frac{9a(bx - a)^{8/3}}{8b^4} + \frac{3a^3(bx - a)^{2/3}}{2b^4} + \frac{9a^2(bx - a)^{5/3}}{5b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x - a)^(1/3),x)

[Out] $\frac{3(bx - a)^{11/3}}{11b^4} + \frac{9a(bx - a)^{8/3}}{8b^4} + \frac{3a^3(bx - a)^{2/3}}{2b^4} + \frac{9a^2(bx - a)^{5/3}}{5b^4}$

sympy [C] time = 2.98, size = 4974, normalized size = 62.18

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(b*x-a)**(1/3),x)

[Out] Piecewise(($243a^{71/3}(-1 + bx/a)^{2/3}\exp(i\pi/3)/(440a^{20}b^4\exp(i\pi/3) - 2640a^{19}b^5x\exp(i\pi/3) + 6600a^{18}b^6x^2\exp(i\pi/3) - 8800a^{17}b^7x^3\exp(i\pi/3) + 6600a^{16}b^8x^4\exp(i\pi/3) - 2640a^{15}b^9x^5\exp(i\pi/3) + 440a^{14}b^{10}x^6\exp(i\pi/3)$) + $243a^{71/3}/(440a^{20}b^4\exp(i\pi/3) - 2640a^{19}b^5x\exp(i\pi/3) + 6600a^{18}b^6x^2\exp(i\pi/3) - 8800a^{17}b^7x^3\exp(i\pi/3) + 6600a^{16}b^8x^4\exp(i\pi/3) - 2640a^{15}b^9x^5\exp(i\pi/3) + 440a^{14}b^{10}x^6\exp(i\pi/3)$) - $1296a^{68/3}bx(-1 + bx/a)^{2/3}\exp(i\pi/3)/(440a^{20}b^4\exp(i\pi/3) - 2640a^{19}b^5x\exp(i\pi/3) + 6600a^{18}b^6x^2\exp(i\pi/3) - 8800a^{17}b^7x^3\exp(i\pi/3) + 6600a^{16}b^8x^4\exp(i\pi/3) - 2640a^{15}b^9x^5\exp(i\pi/3) + 440a^{14}b^{10}x^6\exp(i\pi/3)$) - $1458a^{68/3}bx/(440a^{20}b^4\exp(i\pi/3) - 2640a^{19}b^5x\exp(i\pi/3) + 6600a^{18}b^6x^2\exp(i\pi/3) - 8800a^{17}b^7x^3\exp(i\pi/3) + 6600a^{16}b^8x^4\exp(i\pi/3) - 2640a^{15}b^9x^5\exp(i\pi/3) + 440a^{14}b^{10}x^6\exp(i\pi/3)$) + $2808a^{65/3}b^2x^2(-1 + bx/a)^{2/3}\exp(i\pi/3)/(440a^{20}b^4\exp(i\pi/3) - 2640a^{19}b^5x\exp(i\pi/3) + 6600a^{18}b^6x^2\exp(i\pi/3) - 8800a^{17}b^7x^3\exp(i\pi/3) + 6600a^{16}b^8x^4\exp(i\pi/3) - 2640a^{15}b^9x^5\exp(i\pi/3) + 440a^{14}b^{10}x^6\exp(i\pi/3)$) + $3645a^{65/3}b^2x^2/(440a^{20}b^4\exp(i\pi/3) - 2640a^{19}b^5x\exp(i\pi/3) + 6600a^{18}b^6x^2\exp(i\pi/3) - 8800a^{17}b^7x^3\exp(i\pi/3) + 6600a^{16}b^8x^4\exp(i\pi/3) - 2640a^{15}b^9x^5\exp(i\pi/3) + 440a^{14}b^{10}x^6\exp(i\pi/3)$) -

$$\begin{aligned}
& 3120*a^{62/3}*b^3*x^3*(-1 + b*x/a)^{(2/3)}*exp(I*pi/3)/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)) - 4860*a^{62/3}*b^3*x^3/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)) + 1710*a^{59/3}*b^4*x^4*(-1 + b*x/a)^{(2/3)}*exp(I*pi/3)/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)) + 3645*a^{59/3}*b^4*x^4/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)) + 72*a^{56/3}*b^5*x^5*(-1 + b*x/a)^{(2/3)}*exp(I*pi/3)/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)) - 1458*a^{56/3}*b^5*x^5/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)) - 1104*a^{53/3}*b^6*x^6*(-1 + b*x/a)^{(2/3)}*exp(I*pi/3)/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)) + 243*a^{53/3}*b^6*x^6/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)) + 1152*a^{50/3}*b^7*x^7*(-1 + b*x/a)^{(2/3)}*exp(I*pi/3)/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)) - 585*a^{47/3}*b^8*x^8*(-1 + b*x/a)^{(2/3)}*exp(I*pi/3)/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)) + 120*a^{44/3}*b^9*x^9*(-1 + b*x/a)^{(2/3)}*exp(I*pi/3)/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3)), Abs(b*x/a) > 1), (-243*a^{71/3}*(1 - b*x/a)^{(2/3)}/(440*a^{20}*b^4*exp(I*pi/3) - 2640*a^{19}*b^5*x*exp(I*pi/3) + 6600*a^{18}*b^6*x^2*exp(I*pi/3) - 8800*a^{17}*b^7*x^3*exp(I*pi/3) + 6600*a^{16}*b^8*x^4*exp(I*pi/3) - 2640*a^{15}*b^9*x^5*exp(I*pi/3) + 440*a^{14}*b^{10}*x^6*exp(I*pi/3))
\end{aligned}$$

$$\begin{aligned}
& *b^{10}x^6 \exp(I\pi/3) + 243a^{71/3}/(440a^{20}b^4 \exp(I\pi/3) - 2640 \\
& *a^{19}b^5x \exp(I\pi/3) + 6600a^{18}b^6x^2 \exp(I\pi/3) - 8800a^{17}b \\
& **7x^3 \exp(I\pi/3) + 6600a^{16}b^8x^4 \exp(I\pi/3) - 2640a^{15}b^9x \\
& **5 \exp(I\pi/3) + 440a^{14}b^{10}x^6 \exp(I\pi/3) + 1296a^{68/3}bx(1 \\
& - bx/a)^{2/3}/(440a^{20}b^4 \exp(I\pi/3) - 2640a^{19}b^5x \exp(I\pi/3) \\
&) + 6600a^{18}b^6x^2 \exp(I\pi/3) - 8800a^{17}b^7x^3 \exp(I\pi/3) + 6 \\
& 600a^{16}b^8x^4 \exp(I\pi/3) - 2640a^{15}b^9x^5 \exp(I\pi/3) + 440a^* \\
& *14b^{10}x^6 \exp(I\pi/3) - 1458a^{68/3}bx/(440a^{20}b^4 \exp(I\pi/3) \\
&) - 2640a^{19}b^5x \exp(I\pi/3) + 6600a^{18}b^6x^2 \exp(I\pi/3) - 8800 \\
& *a^{17}b^7x^3 \exp(I\pi/3) + 6600a^{16}b^8x^4 \exp(I\pi/3) - 2640a^{15} \\
& *b^9x^5 \exp(I\pi/3) + 440a^{14}b^{10}x^6 \exp(I\pi/3) - 2808a^{65/3} \\
&)b^2x^2(1 - bx/a)^{2/3}/(440a^{20}b^4 \exp(I\pi/3) - 2640a^{19}b^5 \\
& *x \exp(I\pi/3) + 6600a^{18}b^6x^2 \exp(I\pi/3) - 8800a^{17}b^7x^3 \exp \\
& \exp(I\pi/3) + 6600a^{16}b^8x^4 \exp(I\pi/3) - 2640a^{15}b^9x^5 \exp(I\pi \\
& /3) + 440a^{14}b^{10}x^6 \exp(I\pi/3) + 3645a^{65/3}b^2x^2/(440a^* \\
& **20b^4 \exp(I\pi/3) - 2640a^{19}b^5x \exp(I\pi/3) + 6600a^{18}b^6x^* \\
& 2 \exp(I\pi/3) - 8800a^{17}b^7x^3 \exp(I\pi/3) + 6600a^{16}b^8x^4 \exp \\
& (I\pi/3) - 2640a^{15}b^9x^5 \exp(I\pi/3) + 440a^{14}b^{10}x^6 \exp(I\pi \\
& /3) + 3120a^{62/3}b^3x^3(1 - bx/a)^{2/3}/(440a^{20}b^4 \exp(I\pi \\
& /3) - 2640a^{19}b^5x \exp(I\pi/3) + 6600a^{18}b^6x^2 \exp(I\pi/3) - 88 \\
& 00a^{17}b^7x^3 \exp(I\pi/3) + 6600a^{16}b^8x^4 \exp(I\pi/3) - 2640a^* \\
& *15b^9x^5 \exp(I\pi/3) + 440a^{14}b^{10}x^6 \exp(I\pi/3) - 4860a^{62 \\
& /3}b^3x^3/(440a^{20}b^4 \exp(I\pi/3) - 2640a^{19}b^5x \exp(I\pi/3) + \\
& 6600a^{18}b^6x^2 \exp(I\pi/3) - 8800a^{17}b^7x^3 \exp(I\pi/3) + 6600 \\
& *a^{16}b^8x^4 \exp(I\pi/3) - 2640a^{15}b^9x^5 \exp(I\pi/3) + 440a^{14} \\
& *b^{10}x^6 \exp(I\pi/3) - 1710a^{59/3}b^4x^4(1 - bx/a)^{2/3}/(440 \\
& *a^{20}b^4 \exp(I\pi/3) - 2640a^{19}b^5x \exp(I\pi/3) + 6600a^{18}b^6x^* \\
& **2 \exp(I\pi/3) - 8800a^{17}b^7x^3 \exp(I\pi/3) + 6600a^{16}b^8x^4 \exp \\
& \exp(I\pi/3) - 2640a^{15}b^9x^5 \exp(I\pi/3) + 440a^{14}b^{10}x^6 \exp(I\pi \\
& /3) + 3645a^{59/3}b^4x^4/(440a^{20}b^4 \exp(I\pi/3) - 2640a^{19}b^* \\
& **5x \exp(I\pi/3) + 6600a^{18}b^6x^2 \exp(I\pi/3) - 8800a^{17}b^7x^* \\
& 3 \exp(I\pi/3) + 6600a^{16}b^8x^4 \exp(I\pi/3) - 2640a^{15}b^9x^5 \exp \\
& (I\pi/3) + 440a^{14}b^{10}x^6 \exp(I\pi/3) - 72a^{56/3}b^5x^5(1 - \\
& bx/a)^{2/3}/(440a^{20}b^4 \exp(I\pi/3) - 2640a^{19}b^5x \exp(I\pi/3) + \\
& 6600a^{18}b^6x^2 \exp(I\pi/3) - 8800a^{17}b^7x^3 \exp(I\pi/3) + 6600 \\
& *a^{16}b^8x^4 \exp(I\pi/3) - 2640a^{15}b^9x^5 \exp(I\pi/3) + 440a^{14} \\
& *b^{10}x^6 \exp(I\pi/3) - 1458a^{56/3}b^5x^5/(440a^{20}b^4 \exp(I\pi \\
& /3) - 2640a^{19}b^5x \exp(I\pi/3) + 6600a^{18}b^6x^2 \exp(I\pi/3) - 8 \\
& 800a^{17}b^7x^3 \exp(I\pi/3) + 6600a^{16}b^8x^4 \exp(I\pi/3) - 2640a^* \\
& **15b^9x^5 \exp(I\pi/3) + 440a^{14}b^{10}x^6 \exp(I\pi/3) + 1104a^{53/3} \\
&)b^6x^6(1 - bx/a)^{2/3}/(440a^{20}b^4 \exp(I\pi/3) - 2640a^{19}b^* \\
& **5x \exp(I\pi/3) + 6600a^{18}b^6x^2 \exp(I\pi/3) - 8800a^{17}b^7x^* \\
& 3 \exp(I\pi/3) + 6600a^{16}b^8x^4 \exp(I\pi/3) - 2640a^{15}b^9x^5 \exp \\
& (I\pi/3) + 440a^{14}b^{10}x^6 \exp(I\pi/3) + 243a^{53/3}b^6x^6/(440 \\
& *a^{20}b^4 \exp(I\pi/3) - 2640a^{19}b^5x \exp(I\pi/3) + 6600a^{18}b^6x^
\end{aligned}$$

```

**2*exp(I*pi/3) - 8800*a**17*b**7*x**3*exp(I*pi/3) + 6600*a**16*b**8*x**4*exp(I*pi/3) - 2640*a**15*b**9*x**5*exp(I*pi/3) + 440*a**14*b**10*x**6*exp(I*pi/3)) - 1152*a**(50/3)*b**7*x**7*(1 - b*x/a)**(2/3)/(440*a**20*b**4*exp(I*pi/3) - 2640*a**19*b**5*x*exp(I*pi/3) + 6600*a**18*b**6*x**2*exp(I*pi/3) - 8800*a**17*b**7*x**3*exp(I*pi/3) + 6600*a**16*b**8*x**4*exp(I*pi/3) - 2640*a**15*b**9*x**5*exp(I*pi/3) + 440*a**14*b**10*x**6*exp(I*pi/3)) + 585*a**(47/3)*b**8*x**8*(1 - b*x/a)**(2/3)/(440*a**20*b**4*exp(I*pi/3) - 2640*a**19*b**5*x*exp(I*pi/3) + 6600*a**18*b**6*x**2*exp(I*pi/3) - 8800*a**17*b**7*x**3*exp(I*pi/3) + 6600*a**16*b**8*x**4*exp(I*pi/3) - 2640*a**15*b**9*x**5*exp(I*pi/3) + 440*a**14*b**10*x**6*exp(I*pi/3)) - 120*a**(44/3)*b**9*x**9*(1 - b*x/a)**(2/3)/(440*a**20*b**4*exp(I*pi/3) - 2640*a**19*b**5*x*exp(I*pi/3) + 6600*a**18*b**6*x**2*exp(I*pi/3) - 8800*a**17*b**7*x**3*exp(I*pi/3) + 6600*a**16*b**8*x**4*exp(I*pi/3) - 2640*a**15*b**9*x**5*exp(I*pi/3) + 440*a**14*b**10*x**6*exp(I*pi/3)), True)

```

$$3.400 \quad \int \frac{x^2}{\sqrt[3]{-a+bx}} dx$$

Optimal. Leaf size=59

$$\frac{3a^2(bx-a)^{2/3}}{2b^3} + \frac{3(bx-a)^{8/3}}{8b^3} + \frac{6a(bx-a)^{5/3}}{5b^3}$$

[Out] $3/2*a^2*(b*x-a)^{(2/3)}/b^3+6/5*a*(b*x-a)^{(5/3)}/b^3+3/8*(b*x-a)^{(8/3)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{3a^2(bx-a)^{2/3}}{2b^3} + \frac{3(bx-a)^{8/3}}{8b^3} + \frac{6a(bx-a)^{5/3}}{5b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/(-a + b*x)^(1/3), x]

[Out] $(3*a^2*(-a + b*x)^{(2/3)})/(2*b^3) + (6*a*(-a + b*x)^{(5/3)})/(5*b^3) + (3*(-a + b*x)^{(8/3)})/(8*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sqrt[3]{-a+bx}} dx &= \int \left(\frac{a^2}{b^2 \sqrt[3]{-a+bx}} + \frac{2a(-a+bx)^{2/3}}{b^2} + \frac{(-a+bx)^{5/3}}{b^2} \right) dx \\ &= \frac{3a^2(-a+bx)^{2/3}}{2b^3} + \frac{6a(-a+bx)^{5/3}}{5b^3} + \frac{3(-a+bx)^{8/3}}{8b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 37, normalized size = 0.63

$$\frac{3(bx-a)^{2/3} (9a^2 + 6abx + 5b^2x^2)}{40b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(-a + b*x)^(1/3), x]

[Out] (3*(-a + b*x)^(2/3)*(9*a^2 + 6*a*b*x + 5*b^2*x^2))/(40*b^3)

fricas [A] time = 0.49, size = 33, normalized size = 0.56

$$\frac{3(5b^2x^2 + 6abx + 9a^2)(bx - a)^{\frac{2}{3}}}{40b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x-a)^(1/3), x, algorithm="fricas")

[Out] 3/40*(5*b^2*x^2 + 6*a*b*x + 9*a^2)*(b*x - a)^(2/3)/b^3

giac [A] time = 1.07, size = 43, normalized size = 0.73

$$\frac{3\left(5(bx - a)^{\frac{8}{3}} + 16(bx - a)^{\frac{5}{3}}a + 20(bx - a)^{\frac{2}{3}}a^2\right)}{40b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x-a)^(1/3), x, algorithm="giac")

[Out] 3/40*(5*(b*x - a)^(8/3) + 16*(b*x - a)^(5/3)*a + 20*(b*x - a)^(2/3)*a^2)/b^3

maple [A] time = 0.00, size = 34, normalized size = 0.58

$$\frac{3(5b^2x^2 + 6abx + 9a^2)(bx - a)^{\frac{2}{3}}}{40b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x-a)^(1/3), x)

[Out] 3/40*(5*b^2*x^2+6*a*b*x+9*a^2)/b^3*(b*x-a)^(2/3)

maxima [A] time = 1.33, size = 47, normalized size = 0.80

$$\frac{3(bx - a)^{\frac{8}{3}}}{8b^3} + \frac{6(bx - a)^{\frac{5}{3}}a}{5b^3} + \frac{3(bx - a)^{\frac{2}{3}}a^2}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x-a)^(1/3),x, algorithm="maxima")

[Out] $\frac{3}{8}*(b*x - a)^{(8/3)}/b^3 + \frac{6}{5}*(b*x - a)^{(5/3)}*a/b^3 + \frac{3}{2}*(b*x - a)^{(2/3)}*a^2/b^3$

mupad [B] time = 0.04, size = 43, normalized size = 0.73

$$\frac{48 a (b x - a)^{5/3} + 15 (b x - a)^{8/3} + 60 a^2 (b x - a)^{2/3}}{40 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x - a)^(1/3),x)

[Out] $(48*a*(b*x - a)^{(5/3)} + 15*(b*x - a)^{(8/3)} + 60*a^2*(b*x - a)^{(2/3)})/(40*b^3)$

sympy [C] time = 1.90, size = 1326, normalized size = 22.47

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(b*x-a)**(1/3),x)

[Out] Piecewise((-27*a**(32/3)*(-1 + b*x/a)**(2/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) + 27*a**(32/3)*exp(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) + 63*a**(29/3)*b*x*(-1 + b*x/a)**(2/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) - 81*a**(29/3)*b*x*exp(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) - 42*a**(26/3)*b**2*x**2*(-1 + b*x/a)**(2/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) + 81*a**(26/3)*b**2*x**2*exp(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) + 18*a**(23/3)*b**3*x**3*(-1 + b*x/a)**(2/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) - 27*a**(23/3)*b**3*x**3*exp(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) - 27*a**(20/3)*b**4*x**4*(-1 + b*x/a)**(2/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) + 15*a**(17/3)*b**5*x**5*(-1 + b*x/a)**(2/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3), Abs(b*x/a) > 1), (-27*a**(32/3)*(1 - b*x/a)**(2/3)*exp(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) + 27*a**(32/3)*exp(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) + 63*a**(29/3)*b*x*(1 - b*x/a)**(2/3)*exp(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) - 81*a**(29/3)*b*x*exp(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) - 42*a**(26/3)*b

```

**2*x**2*(1 - b*x/a)**(2/3)*exp(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x
- 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) + 81*a**(26/3)*b**2*x**2*exp(2*I*
pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*
x**3) + 18*a**(23/3)*b**3*x**3*(1 - b*x/a)**(2/3)*exp(2*I*pi/3)/(-40*a**8*b
**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3) - 27*a**(23
/3)*b**3*x**3*exp(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**
5*x**2 + 40*a**5*b**6*x**3) - 27*a**(20/3)*b**4*x**4*(1 - b*x/a)**(2/3)*exp
(2*I*pi/3)/(-40*a**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*
b**6*x**3) + 15*a**(17/3)*b**5*x**5*(1 - b*x/a)**(2/3)*exp(2*I*pi/3)/(-40*a
**8*b**3 + 120*a**7*b**4*x - 120*a**6*b**5*x**2 + 40*a**5*b**6*x**3), True)
)

```

$$3.401 \quad \int \frac{x}{\sqrt[3]{-a+bx}} dx$$

Optimal. Leaf size=38

$$\frac{3(bx-a)^{5/3}}{5b^2} + \frac{3a(bx-a)^{2/3}}{2b^2}$$

[Out] $3/2*a*(b*x-a)^{(2/3)}/b^2+3/5*(b*x-a)^{(5/3)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3(bx-a)^{5/3}}{5b^2} + \frac{3a(bx-a)^{2/3}}{2b^2}$$

Antiderivative was successfully verified.

[In] Int[x/(-a + b*x)^(1/3), x]

[Out] $(3*a*(-a + b*x)^{(2/3)})/(2*b^2) + (3*(-a + b*x)^{(5/3)})/(5*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x}{\sqrt[3]{-a+bx}} dx &= \int \left(\frac{a}{b\sqrt[3]{-a+bx}} + \frac{(-a+bx)^{2/3}}{b} \right) dx \\ &= \frac{3a(-a+bx)^{2/3}}{2b^2} + \frac{3(-a+bx)^{5/3}}{5b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 0.68

$$\frac{3(bx-a)^{2/3}(3a+2bx)}{10b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x/(-a + b*x)^(1/3), x]

[Out] $(3*(-a + b*x)^{(2/3)}*(3*a + 2*b*x))/(10*b^2)$

fricas [A] time = 0.60, size = 22, normalized size = 0.58

$$\frac{3(2bx + 3a)(bx - a)^{\frac{2}{3}}}{10b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x-a)^(1/3),x, algorithm="fricas")`

[Out] $3/10*(2*b*x + 3*a)*(b*x - a)^{(2/3)}/b^2$

giac [A] time = 0.98, size = 29, normalized size = 0.76

$$\frac{3\left(2(bx - a)^{\frac{5}{3}} + 5(bx - a)^{\frac{2}{3}}a\right)}{10b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x-a)^(1/3),x, algorithm="giac")`

[Out] $3/10*(2*(b*x - a)^{(5/3)} + 5*(b*x - a)^{(2/3)}*a)/b^2$

maple [A] time = 0.00, size = 23, normalized size = 0.61

$$\frac{3(2bx + 3a)(bx - a)^{\frac{2}{3}}}{10b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(b*x-a)^(1/3),x)`

[Out] $3/10*(2*b*x+3*a)/b^2*(b*x-a)^{(2/3)}$

maxima [A] time = 1.34, size = 30, normalized size = 0.79

$$\frac{3(bx - a)^{\frac{5}{3}}}{5b^2} + \frac{3(bx - a)^{\frac{2}{3}}a}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x-a)^(1/3),x, algorithm="maxima")`

[Out] $3/5*(b*x - a)^{(5/3)}/b^2 + 3/2*(b*x - a)^{(2/3)}*a/b^2$

mupad [B] time = 0.03, size = 29, normalized size = 0.76

$$\frac{15 a (b x - a)^{2/3} + 6 (b x - a)^{5/3}}{10 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(b*x - a)^(1/3), x)

[Out] (15*a*(b*x - a)^(2/3) + 6*(b*x - a)^(5/3))/(10*b^2)

sympy [C] time = 1.26, size = 486, normalized size = 12.79

$$\left\{ \begin{array}{l} \frac{9a^{\frac{11}{3}} \left(-1 + \frac{bx}{a}\right)^{\frac{2}{3}} e^{\frac{i\pi}{3}}}{-10a^2b^2e^{\frac{i\pi}{3}} + 10ab^3xe^{\frac{i\pi}{3}}} - \frac{9a^{\frac{11}{3}}}{-10a^2b^2e^{\frac{i\pi}{3}} + 10ab^3xe^{\frac{i\pi}{3}}} + \frac{3a^{\frac{8}{3}}bx \left(-1 + \frac{bx}{a}\right)^{\frac{2}{3}} e^{\frac{i\pi}{3}}}{-10a^2b^2e^{\frac{i\pi}{3}} + 10ab^3xe^{\frac{i\pi}{3}}} + \frac{9a^{\frac{8}{3}}bx}{-10a^2b^2e^{\frac{i\pi}{3}} + 10ab^3xe^{\frac{i\pi}{3}}} + \frac{6a^{\frac{5}{3}}b^2x^2 \left(-1 + \frac{bx}{a}\right)^{\frac{2}{3}} e^{\frac{i\pi}{3}}}{-10a^2b^2e^{\frac{i\pi}{3}} + 10ab^3xe^{\frac{i\pi}{3}}} \\ \frac{9a^{\frac{11}{3}} \left(1 - \frac{bx}{a}\right)^{\frac{2}{3}}}{-10a^2b^2e^{\frac{i\pi}{3}} + 10ab^3xe^{\frac{i\pi}{3}}} - \frac{9a^{\frac{11}{3}}}{-10a^2b^2e^{\frac{i\pi}{3}} + 10ab^3xe^{\frac{i\pi}{3}}} - \frac{3a^{\frac{8}{3}}bx \left(1 - \frac{bx}{a}\right)^{\frac{2}{3}}}{-10a^2b^2e^{\frac{i\pi}{3}} + 10ab^3xe^{\frac{i\pi}{3}}} + \frac{9a^{\frac{8}{3}}bx}{-10a^2b^2e^{\frac{i\pi}{3}} + 10ab^3xe^{\frac{i\pi}{3}}} - \frac{6a^{\frac{5}{3}}b^2x^2 \left(1 - \frac{bx}{a}\right)^{\frac{2}{3}}}{-10a^2b^2e^{\frac{i\pi}{3}} + 10ab^3xe^{\frac{i\pi}{3}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x-a)**(1/3), x)

[Out] Piecewise((-9*a**(11/3)*(-1 + b*x/a)**(2/3)*exp(I*pi/3)/(-10*a**2*b**2*exp(I*pi/3) + 10*a*b**3*x*exp(I*pi/3)) - 9*a**(11/3)/(-10*a**2*b**2*exp(I*pi/3) + 10*a*b**3*x*exp(I*pi/3)) + 3*a**(8/3)*b*x*(-1 + b*x/a)**(2/3)*exp(I*pi/3)/(-10*a**2*b**2*exp(I*pi/3) + 10*a*b**3*x*exp(I*pi/3)) + 9*a**(8/3)*b*x/(-10*a**2*b**2*exp(I*pi/3) + 10*a*b**3*x*exp(I*pi/3)) + 6*a**(5/3)*b**2*x**2*(-1 + b*x/a)**(2/3)*exp(I*pi/3)/(-10*a**2*b**2*exp(I*pi/3) + 10*a*b**3*x*exp(I*pi/3)), Abs(b*x/a) > 1), (9*a**(11/3)*(1 - b*x/a)**(2/3)/(-10*a**2*b**2*exp(I*pi/3) + 10*a*b**3*x*exp(I*pi/3)) - 9*a**(11/3)/(-10*a**2*b**2*exp(I*pi/3) + 10*a*b**3*x*exp(I*pi/3)) - 3*a**(8/3)*b*x*(1 - b*x/a)**(2/3)/(-10*a**2*b**2*exp(I*pi/3) + 10*a*b**3*x*exp(I*pi/3)) + 9*a**(8/3)*b*x/(-10*a**2*b**2*exp(I*pi/3) + 10*a*b**3*x*exp(I*pi/3)) - 6*a**(5/3)*b**2*x**2*(1 - b*x/a)**(2/3)/(-10*a**2*b**2*exp(I*pi/3) + 10*a*b**3*x*exp(I*pi/3)), True))

$$3.402 \quad \int \frac{1}{\sqrt[3]{-a+bx}} dx$$

Optimal. Leaf size=18

$$\frac{3(bx - a)^{2/3}}{2b}$$

[Out] 3/2*(b*x-a)^(2/3)/b

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {32}

$$\frac{3(bx - a)^{2/3}}{2b}$$

Antiderivative was successfully verified.

[In] Int[(-a + b*x)^(-1/3), x]

[Out] (3*(-a + b*x)^(2/3))/(2*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt[3]{-a+bx}} dx = \frac{3(-a+bx)^{2/3}}{2b}$$

Mathematica [A] time = 0.00, size = 18, normalized size = 1.00

$$\frac{3(bx - a)^{2/3}}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[(-a + b*x)^(-1/3), x]

[Out] (3*(-a + b*x)^(2/3))/(2*b)

fricas [A] time = 0.55, size = 14, normalized size = 0.78

$$\frac{3(bx - a)^{2/3}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-a)^(1/3),x, algorithm="fricas")`

[Out] $3/2*(b*x - a)^{(2/3)}/b$

giac [A] time = 1.02, size = 14, normalized size = 0.78

$$\frac{3(bx - a)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-a)^(1/3),x, algorithm="giac")`

[Out] $3/2*(b*x - a)^{(2/3)}/b$

maple [A] time = 0.00, size = 15, normalized size = 0.83

$$\frac{3(bx - a)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x-a)^(1/3),x)`

[Out] $3/2*(b*x-a)^{(2/3)}/b$

maxima [A] time = 1.32, size = 14, normalized size = 0.78

$$\frac{3(bx - a)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-a)^(1/3),x, algorithm="maxima")`

[Out] $3/2*(b*x - a)^{(2/3)}/b$

mupad [B] time = 0.02, size = 14, normalized size = 0.78

$$\frac{3(bx - a)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x - a)^(1/3),x)`

[Out] $(3*(b*x - a)^{(2/3)})/(2*b)$

sympy [A] time = 0.07, size = 12, normalized size = 0.67

$$\frac{3(-a + bx)^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-a)**(1/3),x)`

[Out] $3*(-a + b*x)^{(2/3)}/(2*b)$

$$3.403 \quad \int \frac{1}{x \sqrt[3]{-a+bx}} dx$$

Optimal. Leaf size=82

$$-\frac{3 \log(\sqrt[3]{bx-a} + \sqrt[3]{a})}{2\sqrt[3]{a}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{bx-a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt[3]{a}} + \frac{\log(x)}{2\sqrt[3]{a}}$$

[Out] $1/2*\ln(x)/a^{(1/3)}-3/2*\ln(a^{(1/3)}+(b*x-a)^{(1/3)})/a^{(1/3)}-\arctan(1/3*(a^{(1/3)}-2*(b*x-a)^{(1/3)})/a^{(1/3)*3^{(1/2)}})*3^{(1/2)}/a^{(1/3)}$

Rubi [A] time = 0.03, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {56, 617, 204, 31}

$$-\frac{3 \log(\sqrt[3]{bx-a} + \sqrt[3]{a})}{2\sqrt[3]{a}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{bx-a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt[3]{a}} + \frac{\log(x)}{2\sqrt[3]{a}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(-a + b*x)^(1/3)),x]

[Out] $-\left(\frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{a^{1/3}-2(-a+bx)^{1/3}}{\sqrt{3}a^{1/3}}\right]}{a^{1/3}}\right) + \frac{\log(x)}{2a^{1/3}} - \frac{3 \log[a^{1/3} + (-a+bx)^{1/3}]}{2a^{1/3}}$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 56

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])]/; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[Rt[-b, 2]*x]/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x\sqrt{-a+bx}} dx &= \frac{\log(x)}{2\sqrt[3]{a}} + \frac{3}{2} \text{Subst} \left(\int \frac{1}{a^{2/3} - \sqrt[3]{a}x + x^2} dx, x, \sqrt[3]{-a+bx} \right) - \frac{3 \text{Subst} \left(\int \frac{1}{\sqrt[3]{a}+x} dx, x, \sqrt[3]{-a+bx} \right)}{2\sqrt[3]{a}} \\ &= \frac{\log(x)}{2\sqrt[3]{a}} - \frac{3 \log(\sqrt[3]{a} + \sqrt[3]{-a+bx})}{2\sqrt[3]{a}} + \frac{3 \text{Subst} \left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{-a+bx}}{\sqrt[3]{a}} \right)}{\sqrt[3]{a}} \\ &= -\frac{\sqrt{3} \tan^{-1} \left(\frac{1 - \frac{2\sqrt[3]{-a+bx}}{\sqrt[3]{a}}}{\sqrt{3}} \right)}{\sqrt[3]{a}} + \frac{\log(x)}{2\sqrt[3]{a}} - \frac{3 \log(\sqrt[3]{a} + \sqrt[3]{-a+bx})}{2\sqrt[3]{a}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.43

$$\frac{3(bx-a)^{2/3} {}_2F_1\left(\frac{2}{3}, 1; \frac{5}{3}; 1 - \frac{bx}{a}\right)}{2a}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(-a + b*x)^(1/3)), x]

[Out] (3*(-a + b*x)^(2/3)*Hypergeometric2F1[2/3, 1, 5/3, 1 - (b*x)/a])/(2*a)

fricas [A] time = 0.54, size = 285, normalized size = 3.48

$$\left[\frac{\sqrt{3} a \sqrt{\frac{(-a)^{\frac{1}{3}}}{a}} \log \left(\frac{2bx + \sqrt{3} \left(2(bx-a)^{\frac{2}{3}} (-a)^{\frac{2}{3}} + (bx-a)^{\frac{1}{3}} a + (-a)^{\frac{1}{3}} a \right) \sqrt{\frac{(-a)^{\frac{1}{3}}}{a}} - 3(bx-a)^{\frac{1}{3}} (-a)^{\frac{2}{3}} - 3a}{x}} \right)}{2a} + (-a)^{\frac{2}{3}} \log \left((bx-a)^{\frac{2}{3}} + (bx-a) \right) \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(1/3),x, algorithm="fricas")

[Out] $\frac{1}{2} \cdot \frac{\sqrt{3} \cdot a \cdot \sqrt{(-a)^{1/3}/a} \cdot \log((2 \cdot b \cdot x + \sqrt{3}) \cdot (2 \cdot (b \cdot x - a)^{2/3} \cdot (-a)^{2/3} + (b \cdot x - a)^{1/3} \cdot a + (-a)^{1/3} \cdot a) \cdot \sqrt{(-a)^{1/3}/a} - 3 \cdot (b \cdot x - a)^{1/3} \cdot (-a)^{2/3} - 3 \cdot a)/x) + (-a)^{2/3} \cdot \log((b \cdot x - a)^{2/3} + (b \cdot x - a)^{1/3} \cdot (-a)^{1/3} + (-a)^{2/3}) - 2 \cdot (-a)^{2/3} \cdot \log((b \cdot x - a)^{1/3} - (-a)^{1/3})}{a} + \frac{1}{2} \cdot \frac{2 \cdot \sqrt{3} \cdot a \cdot \sqrt{-(-a)^{1/3}/a} \cdot \arctan(1/3 \cdot \sqrt{3} \cdot (2 \cdot (b \cdot x - a)^{1/3} + (-a)^{1/3}) \cdot \sqrt{-(-a)^{1/3}/a}) + (-a)^{2/3} \cdot \log((b \cdot x - a)^{2/3} + (b \cdot x - a)^{1/3} \cdot (-a)^{1/3} + (-a)^{2/3}) - 2 \cdot (-a)^{2/3} \cdot \log((b \cdot x - a)^{1/3} - (-a)^{1/3})}{a}$

giac [A] time = 2.51, size = 112, normalized size = 1.37

$$\frac{\sqrt{3} (-a)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3} \left(2 (bx-a)^{\frac{1}{3}} + (-a)^{\frac{1}{3}}\right)}{3 (-a)^{\frac{1}{3}}}\right)}{a} + \frac{(-a)^{\frac{2}{3}} \log\left((bx-a)^{\frac{2}{3}} + (bx-a)^{\frac{1}{3}} (-a)^{\frac{1}{3}} + (-a)^{\frac{2}{3}}\right)}{2a} - \frac{(-a)^{\frac{2}{3}} \log\left(\left|bx-a\right|\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(1/3),x, algorithm="giac")

[Out] $-\frac{\sqrt{3} \cdot (-a)^{2/3} \cdot \arctan(1/3 \cdot \sqrt{3} \cdot (2 \cdot (b \cdot x - a)^{1/3} + (-a)^{1/3}) / (-a)^{1/3})}{a} + \frac{1}{2} \cdot \frac{(-a)^{2/3} \cdot \log((b \cdot x - a)^{2/3} + (b \cdot x - a)^{1/3} \cdot (-a)^{1/3} + (-a)^{2/3})}{a} - \frac{(-a)^{2/3} \cdot \log(\text{abs}((b \cdot x - a)^{1/3} - (-a)^{1/3}))}{a}$

maple [A] time = 0.01, size = 83, normalized size = 1.01

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3} \left(\frac{2(bx-a)^{\frac{1}{3}}}{a^{\frac{1}{3}}} - 1\right)}{3}\right)}{a^{\frac{1}{3}}} - \frac{\ln\left(a^{\frac{1}{3}} + (bx-a)^{\frac{1}{3}}\right)}{a^{\frac{1}{3}}} + \frac{\ln\left(a^{\frac{2}{3}} - (bx-a)^{\frac{1}{3}} a^{\frac{1}{3}} + (bx-a)^{\frac{2}{3}}\right)}{2a^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x-a)^(1/3),x)

[Out] $-\ln(a^{1/3} + (b \cdot x - a)^{1/3}) / a^{1/3} + 1/2 \cdot \ln((b \cdot x - a)^{2/3} - a^{1/3} \cdot (b \cdot x - a)^{1/3} + a^{2/3}) / a^{1/3} + 3^{1/2} / a^{1/3} \cdot \arctan(1/3 \cdot 3^{1/2} \cdot (2/a^{1/3} \cdot (b \cdot x - a)^{1/3} - 1))$

maxima [A] time = 3.01, size = 86, normalized size = 1.05

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2(bx-a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{a^{\frac{1}{3}}} + \frac{\log\left((bx-a)^{\frac{2}{3}} - (bx-a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{2a^{\frac{1}{3}}} - \frac{\log\left((bx-a)^{\frac{1}{3}} + a^{\frac{1}{3}}\right)}{a^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)^(1/3),x, algorithm="maxima")

[Out] sqrt(3)*arctan(1/3*sqrt(3)*(2*(b*x - a)^(1/3) - a^(1/3))/a^(1/3))/a^(1/3) + 1/2*log((b*x - a)^(2/3) - (b*x - a)^(1/3)*a^(1/3) + a^(2/3))/a^(1/3) - log((b*x - a)^(1/3) + a^(1/3))/a^(1/3)

mupad [B] time = 0.09, size = 117, normalized size = 1.43

$$\frac{\ln\left(9(bx-a)^{1/3} - 9(-a)^{1/3}\right)}{(-a)^{1/3}} + \frac{\ln\left(9(bx-a)^{1/3} - \frac{9(-a)^{1/3}(-1+\sqrt{3}i)^2}{4}\right)(-1+\sqrt{3}i)}{2(-a)^{1/3}} - \frac{\ln\left(9(bx-a)^{1/3} - \frac{9(-a)^{1/3}(1+\sqrt{3}i)^2}{4}\right)(1+\sqrt{3}i)}{2(-a)^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(b*x - a)^(1/3)),x)

[Out] log(9*(b*x - a)^(1/3) - 9*(-a)^(1/3))/(-a)^(1/3) + (log(9*(b*x - a)^(1/3) - 9*(-a)^(1/3)*(3^(1/2)*1i - 1)^2/4)*(3^(1/2)*1i - 1))/(2*(-a)^(1/3)) - (log(9*(b*x - a)^(1/3) - 9*(-a)^(1/3)*(3^(1/2)*1i + 1)^2/4)*(3^(1/2)*1i + 1))/(2*(-a)^(1/3))

sympy [C] time = 1.88, size = 160, normalized size = 1.95

$$\frac{2e^{-\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{-a}{b} + x e^{\frac{i\pi}{3}}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{2}{3}\right)}{3\sqrt[3]{a} \Gamma\left(\frac{5}{3}\right)} - \frac{2 \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{-a}{b} + x e^{i\pi}}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{2}{3}\right)}{3\sqrt[3]{a} \Gamma\left(\frac{5}{3}\right)} - \frac{2e^{\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{-a}{b} + x e^{\frac{5i\pi}{3}}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{2}{3}\right)}{3\sqrt[3]{a} \Gamma\left(\frac{5}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x-a)**(1/3),x)

[Out] -2*exp(-2*I*pi/3)*log(1 - b**(1/3)*(-a/b + x)**(1/3)*exp_polar(I*pi/3)/a**(1/3))*gamma(2/3)/(3*a**(1/3)*gamma(5/3)) - 2*log(1 - b**(1/3)*(-a/b + x)**(1/3)*exp_polar(I*pi)/a**(1/3))*gamma(2/3)/(3*a**(1/3)*gamma(5/3)) - 2*exp(2*I*pi/3)*log(1 - b**(1/3)*(-a/b + x)**(1/3)*exp_polar(5*I*pi/3)/a**(1/3))*gamma(2/3)/(3*a**(1/3)*gamma(5/3))

$$3.404 \quad \int \frac{1}{x^2 \sqrt[3]{-a+bx}} dx$$

Optimal. Leaf size=103

$$\frac{b \log(x)}{6a^{4/3}} - \frac{b \log(\sqrt[3]{bx-a} + \sqrt[3]{a})}{2a^{4/3}} - \frac{b \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{bx-a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{4/3}} + \frac{(bx-a)^{2/3}}{ax}$$

[Out] (b*x-a)^(2/3)/a/x+1/6*b*ln(x)/a^(4/3)-1/2*b*ln(a^(1/3)+(b*x-a)^(1/3))/a^(4/3)-1/3*b*arctan(1/3*(a^(1/3)-2*(b*x-a)^(1/3))/a^(1/3)*3^(1/2))/a^(4/3)*3^(1/2)

Rubi [A] time = 0.03, antiderivative size = 103, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {51, 56, 617, 204, 31}

$$\frac{b \log(x)}{6a^{4/3}} - \frac{b \log(\sqrt[3]{bx-a} + \sqrt[3]{a})}{2a^{4/3}} - \frac{b \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{bx-a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{4/3}} + \frac{(bx-a)^{2/3}}{ax}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(-a + b*x)^(1/3)),x]

[Out] (-a + b*x)^(2/3)/(a*x) - (b*ArcTan[(a^(1/3) - 2*(-a + b*x)^(1/3))/(Sqrt[3]*a^(1/3))]/(Sqrt[3]*a^(4/3)) + (b*Log[x])/(6*a^(4/3)) - (b*Log[a^(1/3) + (-a + b*x)^(1/3)])/(2*a^(4/3))

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]) /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c]) /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^2 \sqrt[3]{-a+bx}} dx &= \frac{(-a+bx)^{2/3}}{ax} + \frac{b \int \frac{1}{x \sqrt[3]{-a+bx}} dx}{3a} \\
&= \frac{(-a+bx)^{2/3}}{ax} + \frac{b \log(x)}{6a^{4/3}} - \frac{b \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a+bx}} dx, x, \sqrt[3]{-a+bx}\right)}{2a^{4/3}} + \frac{b \operatorname{Subst}\left(\int \frac{1}{a^{2/3} - \sqrt[3]{a+bx} x^2} dx, x, \sqrt[3]{-a+bx}\right)}{2a} \\
&= \frac{(-a+bx)^{2/3}}{ax} + \frac{b \log(x)}{6a^{4/3}} - \frac{b \log\left(\sqrt[3]{a} + \sqrt[3]{-a+bx}\right)}{2a^{4/3}} + \frac{b \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{-a+bx}}{\sqrt[3]{a}}\right)}{a^{4/3}} \\
&= \frac{(-a+bx)^{2/3}}{ax} - \frac{b \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{-a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3} a^{4/3}} + \frac{b \log(x)}{6a^{4/3}} - \frac{b \log\left(\sqrt[3]{a} + \sqrt[3]{-a+bx}\right)}{2a^{4/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 36, normalized size = 0.35

$$\frac{3b(bx-a)^{2/3} {}_2F_1\left(\frac{2}{3}, 2; \frac{5}{3}; 1 - \frac{bx}{a}\right)}{2a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(-a + b*x)^(1/3)),x]

[Out] (3*b*(-a + b*x)^(2/3)*Hypergeometric2F1[2/3, 2, 5/3, 1 - (b*x)/a])/(2*a^2)

fricas [A] time = 0.65, size = 328, normalized size = 3.18

$$\frac{3 \sqrt{\frac{1}{3}} abx \sqrt{\frac{(-a)^{\frac{1}{3}}}{a}} \log \left(\frac{2bx+3 \sqrt{\frac{1}{3}} \left(2(bx-a)^{\frac{2}{3}}(-a)^{\frac{2}{3}}+(bx-a)^{\frac{1}{3}}a+(-a)^{\frac{1}{3}}a \right) \sqrt{\frac{(-a)^{\frac{1}{3}}}{a}} - 3(bx-a)^{\frac{1}{3}}(-a)^{\frac{2}{3}}-3a}{x}} \right) + (-a)^{\frac{2}{3}} bx \log \left((bx-a)^{\frac{2}{3}} \right)}{6a^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(1/3),x, algorithm="fricas")

[Out] [1/6*(3*sqrt(1/3)*a*b*x*sqrt((-a)^(1/3)/a)*log((2*b*x + 3*sqrt(1/3)*(2*(b*x - a)^(2/3)*(-a)^(2/3) + (b*x - a)^(1/3)*a + (-a)^(1/3)*a)*sqrt((-a)^(1/3)/a) - 3*(b*x - a)^(1/3)*(-a)^(2/3) - 3*a)/x) + (-a)^(2/3)*b*x*log((b*x - a)^(2/3) + (b*x - a)^(1/3)*(-a)^(1/3) + (-a)^(2/3)) - 2*(-a)^(2/3)*b*x*log((b*x - a)^(1/3) - (-a)^(1/3)) + 6*(b*x - a)^(2/3)*a)/(a^2*x), 1/6*(6*sqrt(1/3)*a*b*x*sqrt((-a)^(1/3)/a)*arctan(sqrt(1/3)*(2*(b*x - a)^(1/3) + (-a)^(1/3))*sqrt((-a)^(1/3)/a)) + (-a)^(2/3)*b*x*log((b*x - a)^(2/3) + (b*x - a)^(1/3)*(-a)^(1/3) + (-a)^(2/3)) - 2*(-a)^(2/3)*b*x*log((b*x - a)^(1/3) - (-a)^(1/3)) + 6*(b*x - a)^(2/3)*a)/(a^2*x)]

giac [A] time = 2.43, size = 144, normalized size = 1.40

$$\frac{2 \sqrt{3} b^2 \arctan \left(\frac{\sqrt{3} \left(2(bx-a)^{\frac{1}{3}}+(-a)^{\frac{1}{3}} \right)}{3(-a)^{\frac{1}{3}}} \right)}{(-a)^{\frac{1}{3}} a} - \frac{b^2 \log \left((bx-a)^{\frac{2}{3}}+(bx-a)^{\frac{1}{3}}(-a)^{\frac{1}{3}}+(-a)^{\frac{2}{3}} \right)}{(-a)^{\frac{1}{3}} a} - \frac{2(-a)^{\frac{2}{3}} b^2 \log \left(\left((bx-a)^{\frac{1}{3}}-(-a)^{\frac{1}{3}} \right) \right)}{a^2} + \frac{6(bx-a)^{\frac{2}{3}} b}{ax}}{6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(1/3),x, algorithm="giac")

[Out] 1/6*(2*sqrt(3)*b^2*arctan(1/3*sqrt(3)*(2*(b*x - a)^(1/3) + (-a)^(1/3))/((-a)^(1/3)))/((-a)^(1/3))/((-a)^(1/3)*a) - b^2*log((b*x - a)^(2/3) + (b*x - a)^(1/3)*(-a)^(1/3) + (-a)^(2/3))/((-a)^(1/3)*a) - 2*(-a)^(2/3)*b^2*log(abs((b*x - a)^(1/3) - (-a)^(1/3)))/a^2 + 6*(b*x - a)^(2/3)*b/(a*x))/b

maple [A] time = 0.01, size = 103, normalized size = 1.00

$$\frac{\sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx-a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}-1\right)}{3}\right)}{3a^{\frac{4}{3}}}-\frac{b \ln\left(a^{\frac{1}{3}}+(bx-a)^{\frac{1}{3}}\right)}{3a^{\frac{4}{3}}}+\frac{b \ln\left(a^{\frac{2}{3}}-(bx-a)^{\frac{1}{3}}a^{\frac{1}{3}}+(bx-a)^{\frac{2}{3}}\right)}{6a^{\frac{4}{3}}}+\frac{(bx-a)^{\frac{2}{3}}}{ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x-a)^(1/3),x)

[Out] (b*x-a)^(2/3)/a/x-1/3*b*ln(a^(1/3)+(b*x-a)^(1/3))/a^(4/3)+1/6*b/a^(4/3)*ln(a^(2/3)-(b*x-a)^(1/3)*a^(1/3)+(b*x-a)^(2/3))+1/3*b/a^(4/3)*3^(1/2)*arctan(1/3*3^(1/2)*(2*(b*x-a)^(1/3)/a^(1/3)-1))

maxima [A] time = 2.99, size = 116, normalized size = 1.13

$$\frac{\sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(2(bx-a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{3a^{\frac{4}{3}}}+\frac{(bx-a)^{\frac{2}{3}}b}{(bx-a)a+a^2}+\frac{b \log\left((bx-a)^{\frac{2}{3}}-(bx-a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)}{6a^{\frac{4}{3}}}-\frac{b \log\left((bx-a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{4}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x-a)^(1/3),x, algorithm="maxima")

[Out] 1/3*sqrt(3)*b*arctan(1/3*sqrt(3)*(2*(b*x - a)^(1/3) - a^(1/3))/a^(1/3))/a^(4/3) + (b*x - a)^(2/3)*b/((b*x - a)*a + a^2) + 1/6*b*log((b*x - a)^(2/3) - (b*x - a)^(1/3)*a^(1/3) + a^(2/3))/a^(4/3) - 1/3*b*log((b*x - a)^(1/3) + a^(1/3))/a^(4/3)

mupad [B] time = 0.18, size = 133, normalized size = 1.29

$$\frac{(bx-a)^{2/3}}{ax}-\frac{b \ln\left((bx-a)^{1/3}+a^{1/3}\right)}{3a^{4/3}}+\frac{\ln\left(\frac{(b-\sqrt{3} b 1i)^2}{4a^{5/3}}+\frac{b^2(bx-a)^{1/3}}{a^2}\right)(b-\sqrt{3} b 1i)}{6a^{4/3}}+\frac{\ln\left(\frac{(b+\sqrt{3} b 1i)^2}{4a^{5/3}}+\frac{b^2(bx-a)^{1/3}}{a^2}\right)(b+\sqrt{3} b 1i)}{6a^{4/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(b*x - a)^(1/3)),x)

[Out] (b*x - a)^(2/3)/(a*x) - (b*log((b*x - a)^(1/3) + a^(1/3)))/(3*a^(4/3)) + (1/3)*log((b - 3^(1/2)*b*1i)^2/(4*a^(5/3)) + (b^2*(b*x - a)^(1/3))/a^2)/(b - 3^(1/2)*b*1i) + (1/3)*log((b + 3^(1/2)*b*1i)^2/(4*a^(5/3)) + (b^2*(b*x - a)^(1/3))/a^2)/(b + 3^(1/2)*b*1i)

$$2) * b * 1i) / (6 * a^{(4/3)}) + (\log((b + 3^{(1/2)} * b * 1i)^2 / (4 * a^{(5/3)}) + (b^2 * (b * x - a)^{(1/3)}) / a^2) * (b + 3^{(1/2)} * b * 1i)) / (6 * a^{(4/3)})$$

sympy [C] time = 2.24, size = 838, normalized size = 8.14

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/(b*x-a)**(1/3),x)

[Out]
$$\begin{aligned} & -2 * a^{(5/3)} * b^{(7/3)} * (-a/b + x)^{(4/3)} * \log(1 - b^{(1/3)} * (-a/b + x)^{(1/3)} * \exp_{\text{polar}}(I * \pi / 3) / a^{(1/3)}) * \gamma(2/3) / (9 * a^{(3)} * b^{(4/3)} * (-a/b + x)^{(4/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3) + 9 * a^{(2)} * b^{(7/3)} * (-a/b + x)^{(7/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3)) \\ & - 2 * a^{(5/3)} * b^{(7/3)} * (-a/b + x)^{(4/3)} * \exp(2 * I * \pi / 3) * \log(1 - b^{(1/3)} * (-a/b + x)^{(1/3)} * \exp_{\text{polar}}(I * \pi) / a^{(1/3)}) * \gamma(2/3) / (9 * a^{(3)} * b^{(4/3)} * (-a/b + x)^{(4/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3) + 9 * a^{(2)} * b^{(7/3)} * (-a/b + x)^{(7/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3)) \\ & - 2 * a^{(5/3)} * b^{(7/3)} * (-a/b + x)^{(4/3)} * \exp(2 * I * \pi / 3) * \log(1 - b^{(1/3)} * (-a/b + x)^{(1/3)} * \exp_{\text{polar}}(5 * I * \pi / 3) / a^{(1/3)}) * \gamma(2/3) / (9 * a^{(3)} * b^{(4/3)} * (-a/b + x)^{(4/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3) + 9 * a^{(2)} * b^{(7/3)} * (-a/b + x)^{(7/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3)) \\ & - 2 * a^{(2/3)} * b^{(10/3)} * (-a/b + x)^{(7/3)} * \log(1 - b^{(1/3)} * (-a/b + x)^{(1/3)} * \exp_{\text{polar}}(I * \pi) / a^{(1/3)}) * \gamma(2/3) / (9 * a^{(3)} * b^{(4/3)} * (-a/b + x)^{(4/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3) + 9 * a^{(2)} * b^{(7/3)} * (-a/b + x)^{(7/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3)) \\ & - 2 * a^{(2/3)} * b^{(10/3)} * (-a/b + x)^{(7/3)} * \exp(2 * I * \pi / 3) * \log(1 - b^{(1/3)} * (-a/b + x)^{(1/3)} * \exp_{\text{polar}}(5 * I * \pi / 3) / a^{(1/3)}) * \gamma(2/3) / (9 * a^{(3)} * b^{(4/3)} * (-a/b + x)^{(4/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3) + 9 * a^{(2)} * b^{(7/3)} * (-a/b + x)^{(7/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3)) \\ & + 6 * a * b^{(3)} * (-a/b + x)^{(2)} * \exp(2 * I * \pi / 3) * \gamma(2/3) / (9 * a^{(3)} * b^{(4/3)} * (-a/b + x)^{(4/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3) + 9 * a^{(2)} * b^{(7/3)} * (-a/b + x)^{(7/3)} * \exp(2 * I * \pi / 3) * \gamma(5/3)) \end{aligned}$$

$$3.405 \quad \int \frac{1}{x^3 \sqrt[3]{-a+bx}} dx$$

Optimal. Leaf size=136

$$\frac{b^2 \log(x)}{9a^{7/3}} - \frac{b^2 \log(\sqrt[3]{bx-a} + \sqrt[3]{a})}{3a^{7/3}} - \frac{2b^2 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{bx-a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{7/3}} + \frac{2b(bx-a)^{2/3}}{3a^2x} + \frac{(bx-a)^{2/3}}{2ax^2}$$

[Out] 1/2*(b*x-a)^(2/3)/a/x^2+2/3*b*(b*x-a)^(2/3)/a^2/x+1/9*b^2*ln(x)/a^(7/3)-1/3*b^2*ln(a^(1/3)+(b*x-a)^(1/3))/a^(7/3)-2/9*b^2*arctan(1/3*(a^(1/3)-2*(b*x-a)^(1/3))/a^(1/3)*3^(1/2))/a^(7/3)*3^(1/2)

Rubi [A] time = 0.04, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {51, 56, 617, 204, 31}

$$\frac{b^2 \log(x)}{9a^{7/3}} - \frac{b^2 \log(\sqrt[3]{bx-a} + \sqrt[3]{a})}{3a^{7/3}} - \frac{2b^2 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{bx-a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{7/3}} + \frac{2b(bx-a)^{2/3}}{3a^2x} + \frac{(bx-a)^{2/3}}{2ax^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(-a + b*x)^(1/3)),x]

[Out] (-a + b*x)^(2/3)/(2*a*x^2) + (2*b*(-a + b*x)^(2/3))/(3*a^2*x) - (2*b^2*ArcTan[(a^(1/3) - 2*(-a + b*x)^(1/3))/(Sqrt[3]*a^(1/3))]/(3*Sqrt[3]*a^(7/3)) + (b^2*Log[x])/(9*a^(7/3)) - (b^2*Log[a^(1/3) + (-a + b*x)^(1/3)]/(3*a^(7/3)))

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])) /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^3 \sqrt[3]{-a+bx}} dx &= \frac{(-a+bx)^{2/3}}{2ax^2} + \frac{(2b) \int \frac{1}{x^2 \sqrt[3]{-a+bx}} dx}{3a} \\
&= \frac{(-a+bx)^{2/3}}{2ax^2} + \frac{2b(-a+bx)^{2/3}}{3a^2x} + \frac{(2b^2) \int \frac{1}{x \sqrt[3]{-a+bx}} dx}{9a^2} \\
&= \frac{(-a+bx)^{2/3}}{2ax^2} + \frac{2b(-a+bx)^{2/3}}{3a^2x} + \frac{b^2 \log(x)}{9a^{7/3}} - \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a+x}} dx, x, \sqrt[3]{-a+bx}\right)}{3a^{7/3}} + \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a+x}} dx, x, \sqrt[3]{-a+bx}\right)}{3a^{7/3}} \\
&= \frac{(-a+bx)^{2/3}}{2ax^2} + \frac{2b(-a+bx)^{2/3}}{3a^2x} + \frac{b^2 \log(x)}{9a^{7/3}} - \frac{b^2 \log(\sqrt[3]{a} + \sqrt[3]{-a+bx})}{3a^{7/3}} + \frac{(2b^2) \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a+x}} dx, x, \sqrt[3]{-a+bx}\right)}{3a^{7/3}} \\
&= \frac{(-a+bx)^{2/3}}{2ax^2} + \frac{2b(-a+bx)^{2/3}}{3a^2x} - \frac{2b^2 \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{-a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{3\sqrt{3}a^{7/3}} + \frac{b^2 \log(x)}{9a^{7/3}} - \frac{b^2 \log(\sqrt[3]{a} + \sqrt[3]{-a+bx})}{3a^{7/3}} + \frac{b^2 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a+x}} dx, x, \sqrt[3]{-a+bx}\right)}{3a^{7/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 38, normalized size = 0.28

$$\frac{3b^2(bx-a)^{2/3} {}_2F_1\left(\frac{2}{3}, 3; \frac{5}{3}; 1 - \frac{bx}{a}\right)}{2a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(-a + b*x)^(1/3)),x]

[Out] (3*b^2*(-a + b*x)^(2/3)*Hypergeometric2F1[2/3, 3, 5/3, 1 - (b*x)/a])/(2*a^3)

fricas [A] time = 0.56, size = 374, normalized size = 2.75

$$\left[\frac{6\sqrt{\frac{1}{3}}ab^2x^2\sqrt{\frac{(-a)^{\frac{1}{3}}}{a}} \log\left(\frac{2bx+3\sqrt{\frac{1}{3}}\left(2(bx-a)^{\frac{2}{3}}(-a)^{\frac{2}{3}}+(bx-a)^{\frac{1}{3}}a+(-a)^{\frac{1}{3}}a\right)\sqrt{\frac{(-a)^{\frac{1}{3}}}{a}}-3(bx-a)^{\frac{1}{3}}(-a)^{\frac{2}{3}}-3a}{x}}{x}\right)}{18a^3x^2} + 2(-a)^{\frac{2}{3}}b^2x^2 \log\left(\frac{bx-a}{a}\right) \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(1/3),x, algorithm="fricas")

[Out] [1/18*(6*sqrt(1/3)*a*b^2*x^2*sqrt((-a)^(1/3)/a)*log((2*b*x + 3*sqrt(1/3))*(2*(b*x - a)^(2/3)*(-a)^(2/3) + (b*x - a)^(1/3)*a + (-a)^(1/3)*a)*sqrt((-a)^(1/3)/a) - 3*(b*x - a)^(1/3)*(-a)^(2/3) - 3*a)/x) + 2*(-a)^(2/3)*b^2*x^2*log((b*x - a)^(2/3) + (b*x - a)^(1/3)*(-a)^(1/3) + (-a)^(2/3)) - 4*(-a)^(2/3)*b^2*x^2*log((b*x - a)^(1/3) - (-a)^(1/3)) + 3*(4*a*b*x + 3*a^2)*(b*x - a)^(2/3))/(a^3*x^2), 1/18*(12*sqrt(1/3)*a*b^2*x^2*sqrt((-a)^(1/3)/a)*arctan(sqrt(1/3)*(2*(b*x - a)^(1/3) + (-a)^(1/3))*sqrt(-(-a)^(1/3)/a) + 2*(-a)^(2/3)*b^2*x^2*log((b*x - a)^(2/3) + (b*x - a)^(1/3)*(-a)^(1/3) + (-a)^(2/3)) - 4*(-a)^(2/3)*b^2*x^2*log((b*x - a)^(1/3) - (-a)^(1/3)) + 3*(4*a*b*x + 3*a^2)*(b*x - a)^(2/3))/(a^3*x^2)]

giac [A] time = 2.24, size = 167, normalized size = 1.23

$$\frac{4\sqrt{3}b^3 \arctan\left(\frac{\sqrt{3}\left(2(bx-a)^{\frac{1}{3}}+(-a)^{\frac{1}{3}}\right)}{3(-a)^{\frac{1}{3}}}\right)}{(-a)^{\frac{1}{3}}a^2} - \frac{2b^3 \log\left(\frac{(bx-a)^{\frac{2}{3}}+(bx-a)^{\frac{1}{3}}(-a)^{\frac{1}{3}}+(-a)^{\frac{2}{3}}}{(-a)^{\frac{1}{3}}a^2}\right)}{(-a)^{\frac{1}{3}}a^2} - \frac{4(-a)^{\frac{2}{3}}b^3 \log\left(\frac{(bx-a)^{\frac{1}{3}}-(-a)^{\frac{1}{3}}}{a^3}\right)}{a^3} + \frac{3\left(4(bx-a)^{\frac{5}{3}}b^3+7(bx-a)^{\frac{2}{3}}b^2\right)}{a^2b^2x^2}$$

18b

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(1/3),x, algorithm="giac")

[Out] $\frac{1}{18} \cdot (4 \cdot \sqrt{3} \cdot b^3 \cdot \arctan(\frac{1}{3} \cdot \sqrt{3} \cdot (2 \cdot (b \cdot x - a)^{1/3} + (-a)^{1/3})) / (-a)^{1/3}) / ((-a)^{1/3} \cdot a^2) - 2 \cdot b^3 \cdot \log((b \cdot x - a)^{2/3} + (b \cdot x - a)^{1/3} \cdot (-a)^{1/3} + (-a)^{2/3}) / ((-a)^{1/3} \cdot a^2) - 4 \cdot (-a)^{2/3} \cdot b^3 \cdot \log(\text{abs}((b \cdot x - a)^{1/3} - (-a)^{1/3})) / a^3 + 3 \cdot (4 \cdot (b \cdot x - a)^{5/3} \cdot b^3 + 7 \cdot (b \cdot x - a)^{2/3} \cdot a \cdot b^3) / (a^2 \cdot b^2 \cdot x^2) / b$

maple [A] time = 0.01, size = 128, normalized size = 0.94

$$\frac{2\sqrt{3} b^2 \arctan\left(\frac{\sqrt{3} \left(\frac{2(bx-a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}-1\right)}{3}\right)}{9a^{\frac{7}{3}}} - \frac{2b^2 \ln\left(a^{\frac{1}{3}} + (bx-a)^{\frac{1}{3}}\right)}{9a^{\frac{7}{3}}} + \frac{b^2 \ln\left(a^{\frac{2}{3}} - (bx-a)^{\frac{1}{3}} a^{\frac{1}{3}} + (bx-a)^{\frac{2}{3}}\right)}{9a^{\frac{7}{3}}} + \frac{2(bx-a)^{\frac{2}{3}} b}{3a^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x-a)^(1/3),x)

[Out] $\frac{1}{2} \cdot (b \cdot x - a)^{2/3} / a \cdot x^2 + 2/3 \cdot b \cdot (b \cdot x - a)^{2/3} / a^2 \cdot x - 2/9 \cdot b^2 \cdot \ln(a^{1/3} + (b \cdot x - a)^{1/3}) / a^{7/3} + 1/9 \cdot b^2 / a^{7/3} \cdot \ln(a^{2/3} - (b \cdot x - a)^{1/3} \cdot a^{1/3} + (b \cdot x - a)^{2/3}) + 2/9 \cdot b^2 / a^{7/3} \cdot 3^{1/2} \cdot \arctan(1/3 \cdot 3^{1/2} \cdot (2 \cdot (b \cdot x - a)^{1/3} / a^{1/3} - 1))$

maxima [A] time = 3.09, size = 159, normalized size = 1.17

$$\frac{2\sqrt{3} b^2 \arctan\left(\frac{\sqrt{3} \left(2 \frac{(bx-a)^{\frac{1}{3}}}{3a^{\frac{1}{3}}}-a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{9a^{\frac{7}{3}}} + \frac{b^2 \log\left((bx-a)^{\frac{2}{3}} - (bx-a)^{\frac{1}{3}} a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{9a^{\frac{7}{3}}} - \frac{2b^2 \log\left((bx-a)^{\frac{1}{3}} + a^{\frac{1}{3}}\right)}{9a^{\frac{7}{3}}} + \frac{4(bx-a)^{\frac{2}{3}}}{6(bx-a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x-a)^(1/3),x, algorithm="maxima")

[Out] $\frac{2}{9} \cdot \sqrt{3} \cdot b^2 \cdot \arctan(\frac{1}{3} \cdot \sqrt{3} \cdot (2 \cdot (b \cdot x - a)^{1/3} - a^{1/3})) / a^{1/3} / a^{7/3} + 1/9 \cdot b^2 \cdot \log((b \cdot x - a)^{2/3} - (b \cdot x - a)^{1/3} \cdot a^{1/3} + a^{2/3}) / a^{7/3} - 2/9 \cdot b^2 \cdot \log((b \cdot x - a)^{1/3} + a^{1/3}) / a^{7/3} + 1/6 \cdot (4 \cdot (b \cdot x - a)^{5/3} \cdot b^2 + 7 \cdot (b \cdot x - a)^{2/3} \cdot a \cdot b^2) / ((b \cdot x - a)^2 \cdot a^2 + 2 \cdot (b \cdot x - a) \cdot a^3 + a^4)$

mupad [B] time = 0.22, size = 216, normalized size = 1.59

$$\frac{\frac{7b^2(bx-a)^{2/3}}{6a} + \frac{2b^2(bx-a)^{5/3}}{3a^2}}{(a-bx)^2 - 2a(a-bx) + a^2} \frac{\ln\left(\frac{4b^4(bx-a)^{1/3}}{9a^4} - \frac{(b^2 + \sqrt{3}b^2i)^2}{9(-a)^{11/3}}\right) (b^2 + \sqrt{3}b^2i)}{9(-a)^{7/3}} + \frac{2b^2 \ln\left(\frac{4b^4(bx-a)^{1/3}}{9a^4} - \frac{4b^4}{9(-a)^{11/3}}\right)}{9(-a)^{7/3}} +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(b*x - a)^(1/3)),x)

[Out] ((7*b^2*(b*x - a)^(2/3))/(6*a) + (2*b^2*(b*x - a)^(5/3))/(3*a^2))/((a - b*x)^2 - 2*a*(a - b*x) + a^2) - (log((4*b^4*(b*x - a)^(1/3))/(9*a^4) - (3^(1/2)*b^2*i + b^2)^2/(9*(-a)^(11/3))))*(3^(1/2)*b^2*i + b^2)/(9*(-a)^(7/3)) + (2*b^2*log((4*b^4*(b*x - a)^(1/3))/(9*a^4) - (4*b^4)/(9*(-a)^(11/3))))/(9*(-a)^(7/3)) + (b^2*log((4*b^4*(b*x - a)^(1/3))/(9*a^4) - (9*b^4*((3^(1/2)*i)/9 - 1/9)^2)/(-a)^(11/3))*((3^(1/2)*i)/9 - 1/9))/(-a)^(7/3)

sympy [C] time = 2.62, size = 2744, normalized size = 20.18

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(b*x-a)**(1/3),x)

[Out] -4*a**(14/3)*b**(10/3)*(-a/b + x)**(4/3)*log(1 - b**(1/3)*(-a/b + x)**(1/3))*exp_polar(I*pi/3)/a**(1/3)*gamma(2/3)/(27*a**7*b**(4/3)*(-a/b + x)**(4/3))*exp(2*I*pi/3)*gamma(5/3) + 81*a**6*b**(7/3)*(-a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(5/3) + 81*a**5*b**(10/3)*(-a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(5/3) + 27*a**4*b**(13/3)*(-a/b + x)**(13/3)*exp(2*I*pi/3)*gamma(5/3) - 4*a**(14/3)*b**(10/3)*(-a/b + x)**(4/3)*exp(2*I*pi/3)*log(1 - b**(1/3)*(-a/b + x)**(1/3))*exp_polar(I*pi)/a**(1/3)*gamma(2/3)/(27*a**7*b**(4/3)*(-a/b + x)**(4/3))*exp(2*I*pi/3)*gamma(5/3) + 81*a**6*b**(7/3)*(-a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(5/3) + 81*a**5*b**(10/3)*(-a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(5/3) + 27*a**4*b**(13/3)*(-a/b + x)**(13/3)*exp(2*I*pi/3)*gamma(5/3) - 4*a**(14/3)*b**(10/3)*(-a/b + x)**(4/3)*exp(-2*I*pi/3)*log(1 - b**(1/3)*(-a/b + x)**(1/3))*exp_polar(5*I*pi/3)/a**(1/3)*gamma(2/3)/(27*a**7*b**(4/3)*(-a/b + x)**(4/3))*exp(2*I*pi/3)*gamma(5/3) + 81*a**6*b**(7/3)*(-a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(5/3) + 81*a**5*b**(10/3)*(-a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(5/3) + 27*a**4*b**(13/3)*(-a/b + x)**(13/3)*exp(2*I*pi/3)*gamma(5/3) - 12*a**(11/3)*b**(13/3)*(-a/b + x)**(7/3)*log(1 - b**(1/3)*(-a/b + x)**(1/3))*exp_polar(I*pi/3)/a**(1/3)*gamma(2/3)/(27*a**7*b**(4/3)*(-a/b + x)**(4/3))*exp(2*I*pi/3)*gamma(5/3) + 81*a**6*b**(7/3)*(-a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(5/3) + 81*a**5*b**(10/3)*(-a/b + x)**(10/3)*exp(2*I*pi/3)*

$$\begin{aligned}
& \gamma(5/3) + 27a^{**4}b^{**}(13/3)*(-a/b + x)^{**}(13/3)*\exp(2I\pi/3)*\gamma(5/3) \\
& - 12a^{**}(11/3)*b^{**}(13/3)*(-a/b + x)^{**}(7/3)*\exp(2I\pi/3)*\log(1 - b^{**}(1/3)* \\
& (-a/b + x)^{**}(1/3)*\exp_polar(I\pi)/a^{**}(1/3))*\gamma(2/3)/(27a^{**7}b^{**}(4/3)*(- \\
& a/b + x)^{**}(4/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**6}b^{**}(7/3)*(-a/b + x)^{**}(7/ \\
& 3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**5}b^{**}(10/3)*(-a/b + x)^{**}(10/3)*\exp(2I\pi \\
& /3)*\gamma(5/3) + 27a^{**4}b^{**}(13/3)*(-a/b + x)^{**}(13/3)*\exp(2I\pi/3)*\gamma \\
& (5/3) - 12a^{**}(11/3)*b^{**}(13/3)*(-a/b + x)^{**}(7/3)*\exp(-2I\pi/3)*\log(1 - b \\
& ^{**}(1/3)*(-a/b + x)^{**}(1/3)*\exp_polar(5I\pi/3)/a^{**}(1/3))*\gamma(2/3)/(27a^{**7} \\
& b^{**}(4/3)*(-a/b + x)^{**}(4/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**6}b^{**}(7/3)*(-a/ \\
& b + x)^{**}(7/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**5}b^{**}(10/3)*(-a/b + x)^{**}(10/ \\
& 3)*\exp(2I\pi/3)*\gamma(5/3) + 27a^{**4}b^{**}(13/3)*(-a/b + x)^{**}(13/3)*\exp(2I\pi \\
& /3)*\gamma(5/3) - 12a^{**}(8/3)*b^{**}(16/3)*(-a/b + x)^{**}(10/3)*\log(1 - b^{**}(1/ \\
& 3)*(-a/b + x)^{**}(1/3)*\exp_polar(I\pi)/a^{**}(1/3))*\gamma(2/3)/(27a^{**7}b^{**}(4/ \\
& 3)*(-a/b + x)^{**}(4/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**6}b^{**}(7/3)*(-a/b + x) \\
& ^{**}(7/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**5}b^{**}(10/3)*(-a/b + x)^{**}(10/3)*\exp \\
& (2I\pi/3)*\gamma(5/3) + 27a^{**4}b^{**}(13/3)*(-a/b + x)^{**}(13/3)*\exp(2I\pi/3)* \\
& \gamma(5/3) - 12a^{**}(8/3)*b^{**}(16/3)*(-a/b + x)^{**}(10/3)*\exp(2I\pi/3)*\log(1 \\
& - b^{**}(1/3)*(-a/b + x)^{**}(1/3)*\exp_polar(I\pi)/a^{**}(1/3))*\gamma(2/3)/(27a^{**7} \\
& b^{**}(4/3)*(-a/b + x)^{**}(4/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**6}b^{**}(7/3)*(-a/ \\
& b + x)^{**}(7/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**5}b^{**}(10/3)*(-a/b + x)^{**}(10/ \\
& 3)*\exp(2I\pi/3)*\gamma(5/3) + 27a^{**4}b^{**}(13/3)*(-a/b + x)^{**}(13/3)*\exp(2I\pi \\
& /3)*\gamma(5/3) - 12a^{**}(8/3)*b^{**}(16/3)*(-a/b + x)^{**}(10/3)*\exp(-2I\pi/3) \\
& *\log(1 - b^{**}(1/3)*(-a/b + x)^{**}(1/3)*\exp_polar(5I\pi/3)/a^{**}(1/3))*\gamma(2/3) \\
&)/(27a^{**7}b^{**}(4/3)*(-a/b + x)^{**}(4/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**6}b^{**} \\
& *(7/3)*(-a/b + x)^{**}(7/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**5}b^{**}(10/3)*(-a/b \\
& + x)^{**}(10/3)*\exp(2I\pi/3)*\gamma(5/3) + 27a^{**4}b^{**}(13/3)*(-a/b + x)^{**}(13/ \\
& 3)*\exp(2I\pi/3)*\gamma(5/3) - 4a^{**}(5/3)*b^{**}(19/3)*(-a/b + x)^{**}(13/3)*\log(\\
& 1 - b^{**}(1/3)*(-a/b + x)^{**}(1/3)*\exp_polar(I\pi)/a^{**}(1/3))*\gamma(2/3)/(27a \\
& ^{**7}b^{**}(4/3)*(-a/b + x)^{**}(4/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**6}b^{**}(7/3)* \\
& (-a/b + x)^{**}(7/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**5}b^{**}(10/3)*(-a/b + x)^{**} \\
& (10/3)*\exp(2I\pi/3)*\gamma(5/3) + 27a^{**4}b^{**}(13/3)*(-a/b + x)^{**}(13/3)*\exp(\\
& 2I\pi/3)*\gamma(5/3) - 4a^{**}(5/3)*b^{**}(19/3)*(-a/b + x)^{**}(13/3)*\exp(2I\pi/ \\
& 3)*\log(1 - b^{**}(1/3)*(-a/b + x)^{**}(1/3)*\exp_polar(I\pi)/a^{**}(1/3))*\gamma(2/3)/ \\
& (27a^{**7}b^{**}(4/3)*(-a/b + x)^{**}(4/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**6}b^{**}(\\
& 7/3)*(-a/b + x)^{**}(7/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**5}b^{**}(10/3)*(-a/b + \\
& x)^{**}(10/3)*\exp(2I\pi/3)*\gamma(5/3) + 27a^{**4}b^{**}(13/3)*(-a/b + x)^{**}(13/3) \\
& *\exp(2I\pi/3)*\gamma(5/3) - 4a^{**}(5/3)*b^{**}(19/3)*(-a/b + x)^{**}(13/3)*\exp(-2 \\
& I\pi/3)*\log(1 - b^{**}(1/3)*(-a/b + x)^{**}(1/3)*\exp_polar(5I\pi/3)/a^{**}(1/3))*\gamma \\
& (2/3)/(27a^{**7}b^{**}(4/3)*(-a/b + x)^{**}(4/3)*\exp(2I\pi/3)*\gamma(5/3) + 81 \\
& a^{**6}b^{**}(7/3)*(-a/b + x)^{**}(7/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**5}b^{**}(10/ \\
& 3)*(-a/b + x)^{**}(10/3)*\exp(2I\pi/3)*\gamma(5/3) + 27a^{**4}b^{**}(13/3)*(-a/b + \\
& x)^{**}(13/3)*\exp(2I\pi/3)*\gamma(5/3) + 21a^{**4}b^{**4}*(-a/b + x)^{**2}*\exp(2I\pi \\
& /3)*\gamma(2/3)/(27a^{**7}b^{**}(4/3)*(-a/b + x)^{**}(4/3)*\exp(2I\pi/3)*\gamma(5/3) \\
&) + 81a^{**6}b^{**}(7/3)*(-a/b + x)^{**}(7/3)*\exp(2I\pi/3)*\gamma(5/3) + 81a^{**5}b \\
& ^{**}(10/3)*(-a/b + x)^{**}(10/3)*\exp(2I\pi/3)*\gamma(5/3) + 27a^{**4}b^{**}(13/3)*(-
\end{aligned}$$

$$\begin{aligned}
& a/b + x)^{(13/3)} \exp(2I\pi/3) \gamma(5/3)) + 33a^{*3}b^{*5}(-a/b + x)^{*3} \exp \\
& (2I\pi/3) \gamma(2/3) / (27a^{*7}b^{*4}(-a/b + x)^{*4} \exp(2I\pi/3) \gamma(5/3) + 81a^{*6}b^{*7}(-a/b + x)^{*7} \exp(2I\pi/3) \gamma(5/3) + 81a^{*5}b^{*10}(-a/b + x)^{*10} \exp(2I\pi/3) \gamma(5/3) + 27a^{*4}b^{*13} \\
& (-a/b + x)^{*13} \exp(2I\pi/3) \gamma(5/3)) + 12a^{*2}b^{*6}(-a/b + x)^{*4} \exp(2I\pi/3) \gamma(2/3) / (27a^{*7}b^{*4}(-a/b + x)^{*4} \exp(2I\pi/3) \gamma(5/3) + 81a^{*6}b^{*7}(-a/b + x)^{*7} \exp(2I\pi/3) \gamma(5/3) \\
& + 81a^{*5}b^{*10}(-a/b + x)^{*10} \exp(2I\pi/3) \gamma(5/3) + 27a^{*4}b^{*13} \\
& (-a/b + x)^{*13} \exp(2I\pi/3) \gamma(5/3))
\end{aligned}$$

$$3.406 \quad \int \frac{x^3}{(a+bx)^{2/3}} dx$$

Optimal. Leaf size=70

$$-\frac{3a^3\sqrt[3]{a+bx}}{b^4} + \frac{9a^2(a+bx)^{4/3}}{4b^4} + \frac{3(a+bx)^{10/3}}{10b^4} - \frac{9a(a+bx)^{7/3}}{7b^4}$$

[Out] $-3a^3(b*x+a)^{(1/3)}/b^4+9/4*a^2*(b*x+a)^{(4/3)}/b^4-9/7*a*(b*x+a)^{(7/3)}/b^4+3/10*(b*x+a)^{(10/3)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9a^2(a+bx)^{4/3}}{4b^4} - \frac{3a^3\sqrt[3]{a+bx}}{b^4} + \frac{3(a+bx)^{10/3}}{10b^4} - \frac{9a(a+bx)^{7/3}}{7b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x)^(2/3), x]

[Out] $(-3*a^3*(a + b*x)^{(1/3)})/b^4 + (9*a^2*(a + b*x)^{(4/3)})/(4*b^4) - (9*a*(a + b*x)^{(7/3)})/(7*b^4) + (3*(a + b*x)^{(10/3)})/(10*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(a+bx)^{2/3}} dx &= \int \left(-\frac{a^3}{b^3(a+bx)^{2/3}} + \frac{3a^2\sqrt[3]{a+bx}}{b^3} - \frac{3a(a+bx)^{4/3}}{b^3} + \frac{(a+bx)^{7/3}}{b^3} \right) dx \\ &= -\frac{3a^3\sqrt[3]{a+bx}}{b^4} + \frac{9a^2(a+bx)^{4/3}}{4b^4} - \frac{9a(a+bx)^{7/3}}{7b^4} + \frac{3(a+bx)^{10/3}}{10b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.66

$$\frac{3\sqrt[3]{a+bx} \left(-81a^3 + 27a^2bx - 18ab^2x^2 + 14b^3x^3 \right)}{140b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x)^(2/3), x]

[Out] (3*(a + b*x)^(1/3)*(-81*a^3 + 27*a^2*b*x - 18*a*b^2*x^2 + 14*b^3*x^3))/(140*b^4)

fricas [A] time = 0.48, size = 42, normalized size = 0.60

$$\frac{3 \left(14 b^3 x^3 - 18 a b^2 x^2 + 27 a^2 b x - 81 a^3 \right) (b x + a)^{\frac{1}{3}}}{140 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(2/3), x, algorithm="fricas")

[Out] 3/140*(14*b^3*x^3 - 18*a*b^2*x^2 + 27*a^2*b*x - 81*a^3)*(b*x + a)^(1/3)/b^4

giac [A] time = 1.03, size = 49, normalized size = 0.70

$$\frac{3 \left(14 (b x + a)^{\frac{10}{3}} - 60 (b x + a)^{\frac{7}{3}} a + 105 (b x + a)^{\frac{4}{3}} a^2 - 140 (b x + a)^{\frac{1}{3}} a^3 \right)}{140 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(2/3), x, algorithm="giac")

[Out] 3/140*(14*(b*x + a)^(10/3) - 60*(b*x + a)^(7/3)*a + 105*(b*x + a)^(4/3)*a^2 - 140*(b*x + a)^(1/3)*a^3)/b^4

maple [A] time = 0.01, size = 43, normalized size = 0.61

$$-\frac{3 (b x + a)^{\frac{1}{3}} \left(-14 b^3 x^3 + 18 a b^2 x^2 - 27 a^2 b x + 81 a^3 \right)}{140 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^(2/3), x)

[Out] -3/140*(b*x+a)^(1/3)*(-14*b^3*x^3+18*a*b^2*x^2-27*a^2*b*x+81*a^3)/b^4

maxima [A] time = 1.34, size = 56, normalized size = 0.80

$$\frac{3 (b x + a)^{\frac{10}{3}}}{10 b^4} - \frac{9 (b x + a)^{\frac{7}{3}} a}{7 b^4} + \frac{9 (b x + a)^{\frac{4}{3}} a^2}{4 b^4} - \frac{3 (b x + a)^{\frac{1}{3}} a^3}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(2/3),x, algorithm="maxima")

[Out] $\frac{3}{10}*(b*x + a)^{(10/3)}/b^4 - \frac{9}{7}*(b*x + a)^{(7/3)}*a/b^4 + \frac{9}{4}*(b*x + a)^{(4/3)}*a^2/b^4 - 3*(b*x + a)^{(1/3)}*a^3/b^4$

mupad [B] time = 0.05, size = 56, normalized size = 0.80

$$\frac{3(a+bx)^{10/3}}{10b^4} - \frac{3a^3(a+bx)^{1/3}}{b^4} + \frac{9a^2(a+bx)^{4/3}}{4b^4} - \frac{9a(a+bx)^{7/3}}{7b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(a + b*x)^(2/3),x)

[Out] $\frac{3*(a + b*x)^{(10/3)}}{(10*b^4)} - \frac{3*a^3*(a + b*x)^{(1/3)}}{b^4} + \frac{9*a^2*(a + b*x)^{(4/3)}}{(4*b^4)} - \frac{9*a*(a + b*x)^{(7/3)}}{(7*b^4)}$

sympy [B] time = 2.79, size = 1640, normalized size = 23.43

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(b*x+a)**(2/3),x)

[Out] $-243*a**(70/3)*(1 + b*x/a)**(1/3)/(140*a**20*b**4 + 840*a**19*b**5*x + 2100*a**18*b**6*x**2 + 2800*a**17*b**7*x**3 + 2100*a**16*b**8*x**4 + 840*a**15*b**9*x**5 + 140*a**14*b**10*x**6) + 243*a**(70/3)/(140*a**20*b**4 + 840*a**19*b**5*x + 2100*a**18*b**6*x**2 + 2800*a**17*b**7*x**3 + 2100*a**16*b**8*x**4 + 840*a**15*b**9*x**5 + 140*a**14*b**10*x**6) - 1377*a**(67/3)*b*x*(1 + b*x/a)**(1/3)/(140*a**20*b**4 + 840*a**19*b**5*x + 2100*a**18*b**6*x**2 + 2800*a**17*b**7*x**3 + 2100*a**16*b**8*x**4 + 840*a**15*b**9*x**5 + 140*a**14*b**10*x**6) + 1458*a**(67/3)*b*x/(140*a**20*b**4 + 840*a**19*b**5*x + 2100*a**18*b**6*x**2 + 2800*a**17*b**7*x**3 + 2100*a**16*b**8*x**4 + 840*a**15*b**9*x**5 + 140*a**14*b**10*x**6) - 3213*a**(64/3)*b**2*x**2*(1 + b*x/a)**(1/3)/(140*a**20*b**4 + 840*a**19*b**5*x + 2100*a**18*b**6*x**2 + 2800*a**17*b**7*x**3 + 2100*a**16*b**8*x**4 + 840*a**15*b**9*x**5 + 140*a**14*b**10*x**6) + 3645*a**(64/3)*b**2*x**2/(140*a**20*b**4 + 840*a**19*b**5*x + 2100*a**18*b**6*x**2 + 2800*a**17*b**7*x**3 + 2100*a**16*b**8*x**4 + 840*a**15*b**9*x**5 + 140*a**14*b**10*x**6) - 3927*a**(61/3)*b**3*x**3*(1 + b*x/a)**(1/3)/(140*a**20*b**4 + 840*a**19*b**5*x + 2100*a**18*b**6*x**2 + 2800*a**17*b**7*x**3 + 2100*a**16*b**8*x**4 + 840*a**15*b**9*x**5 + 140*a**14*b**10*x**6) + 4860*a**(61/3)*b**3*x**3/(140*a**20*b**4 + 840*a**19*b**5*x + 2100*a**18*b**6*x**2 + 2800*a**17*b**7*x**3 + 2100*a**16*b**8*x**4 + 840*a**15*b**9*x**5 + 140*a**14*b**10*x**6) - 2583*a**(58/3)*b**4*x**4*(1 + b*x/a)**(1/3)/(140*a**20*b**4 + 840*a**19*b**5*x + 2100*a**18*b**6*x**2 + 2800*a**17*b**7*x**3 + 2100*a**16*b**8*x**4 + 840*a**15*b**9*x**5 + 140*a**14*b**10*x**6)$

$$\begin{aligned}
& 6) + 3645*a^{58/3}*b^4*x^4/(140*a^{20}*b^4 + 840*a^{19}*b^5*x + 2100*a^{18}*b^6*x^2 + 2800*a^{17}*b^7*x^3 + 2100*a^{16}*b^8*x^4 + 840*a^{15}*b^9*x^5 + 140*a^{14}*b^{10}*x^6) - 693*a^{55/3}*b^5*x^5*(1 + b*x/a)^{(1/3)}/ \\
& (140*a^{20}*b^4 + 840*a^{19}*b^5*x + 2100*a^{18}*b^6*x^2 + 2800*a^{17}*b^7*x^3 + 2100*a^{16}*b^8*x^4 + 840*a^{15}*b^9*x^5 + 140*a^{14}*b^{10}*x^6) \\
& + 1458*a^{55/3}*b^5*x^5/(140*a^{20}*b^4 + 840*a^{19}*b^5*x + 2100*a^{18}*b^6*x^2 + 2800*a^{17}*b^7*x^3 + 2100*a^{16}*b^8*x^4 + 840*a^{15}*b^9*x^5 + 140*a^{14}*b^{10}*x^6) \\
& + 273*a^{52/3}*b^6*x^6*(1 + b*x/a)^{(1/3)}/(140*a^{20}*b^4 + 840*a^{19}*b^5*x + 2100*a^{18}*b^6*x^2 + 2800*a^{17}*b^7*x^3 + 2100*a^{16}*b^8*x^4 + 840*a^{15}*b^9*x^5 + 140*a^{14}*b^{10}*x^6) + 2 \\
& 43*a^{52/3}*b^6*x^6/(140*a^{20}*b^4 + 840*a^{19}*b^5*x + 2100*a^{18}*b^6*x^2 + 2800*a^{17}*b^7*x^3 + 2100*a^{16}*b^8*x^4 + 840*a^{15}*b^9*x^5 + 140*a^{14}*b^{10}*x^6) + 387*a^{49/3}*b^7*x^7*(1 + b*x/a)^{(1/3)}/(140*a^{20}*b^4 + 840*a^{19}*b^5*x + 2100*a^{18}*b^6*x^2 + 2800*a^{17}*b^7*x^3 + 2100*a^{16}*b^8*x^4 + 840*a^{15}*b^9*x^5 + 140*a^{14}*b^{10}*x^6) + 198*a^{46/3}*b^8*x^8*(1 + b*x/a)^{(1/3)}/(140*a^{20}*b^4 + 840*a^{19}*b^5*x + 2100*a^{18}*b^6*x^2 + 2800*a^{17}*b^7*x^3 + 2100*a^{16}*b^8*x^4 + 840*a^{15}*b^9*x^5 + 140*a^{14}*b^{10}*x^6) + 42*a^{43/3}*b^9*x^9*(1 + b*x/a)^{(1/3)}/(140*a^{20}*b^4 + 840*a^{19}*b^5*x + 2100*a^{18}*b^6*x^2 + 2800*a^{17}*b^7*x^3 + 2100*a^{16}*b^8*x^4 + 840*a^{15}*b^9*x^5 + 140*a^{14}*b^{10}*x^6)
\end{aligned}$$

$$3.407 \quad \int \frac{x^2}{(a+bx)^{2/3}} dx$$

Optimal. Leaf size=51

$$\frac{3a^2\sqrt[3]{a+bx}}{b^3} + \frac{3(a+bx)^{7/3}}{7b^3} - \frac{3a(a+bx)^{4/3}}{2b^3}$$

[Out] $3a^2(b*x+a)^{(1/3)}/b^3-3/2*a*(b*x+a)^{(4/3)}/b^3+3/7*(b*x+a)^{(7/3)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3a^2\sqrt[3]{a+bx}}{b^3} + \frac{3(a+bx)^{7/3}}{7b^3} - \frac{3a(a+bx)^{4/3}}{2b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*x)^(2/3), x]

[Out] $(3*a^2*(a + b*x)^{(1/3)})/b^3 - (3*a*(a + b*x)^{(4/3)})/(2*b^3) + (3*(a + b*x)^{(7/3)})/(7*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(a+bx)^{2/3}} dx &= \int \left(\frac{a^2}{b^2(a+bx)^{2/3}} - \frac{2a\sqrt[3]{a+bx}}{b^2} + \frac{(a+bx)^{4/3}}{b^2} \right) dx \\ &= \frac{3a^2\sqrt[3]{a+bx}}{b^3} - \frac{3a(a+bx)^{4/3}}{2b^3} + \frac{3(a+bx)^{7/3}}{7b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.69

$$\frac{3\sqrt[3]{a+bx} (9a^2 - 3abx + 2b^2x^2)}{14b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x)^(2/3), x]

[Out] (3*(a + b*x)^(1/3)*(9*a^2 - 3*a*b*x + 2*b^2*x^2))/(14*b^3)

fricas [A] time = 0.41, size = 31, normalized size = 0.61

$$\frac{3(2b^2x^2 - 3abx + 9a^2)(bx + a)^{\frac{1}{3}}}{14b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(2/3), x, algorithm="fricas")

[Out] 3/14*(2*b^2*x^2 - 3*a*b*x + 9*a^2)*(b*x + a)^(1/3)/b^3

giac [A] time = 0.90, size = 37, normalized size = 0.73

$$\frac{3\left(2(bx + a)^{\frac{7}{3}} - 7(bx + a)^{\frac{4}{3}}a + 14(bx + a)^{\frac{1}{3}}a^2\right)}{14b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(2/3), x, algorithm="giac")

[Out] 3/14*(2*(b*x + a)^(7/3) - 7*(b*x + a)^(4/3)*a + 14*(b*x + a)^(1/3)*a^2)/b^3

maple [A] time = 0.00, size = 32, normalized size = 0.63

$$\frac{3(bx + a)^{\frac{1}{3}}(2b^2x^2 - 3abx + 9a^2)}{14b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^(2/3), x)

[Out] 3/14*(b*x+a)^(1/3)*(2*b^2*x^2-3*a*b*x+9*a^2)/b^3

maxima [A] time = 1.31, size = 41, normalized size = 0.80

$$\frac{3(bx + a)^{\frac{7}{3}}}{7b^3} - \frac{3(bx + a)^{\frac{4}{3}}a}{2b^3} + \frac{3(bx + a)^{\frac{1}{3}}a^2}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(2/3),x, algorithm="maxima")

[Out] $\frac{3}{7}(b*x + a)^{7/3}/b^3 - \frac{3}{2}(b*x + a)^{4/3}*a/b^3 + 3*(b*x + a)^{1/3}*a^2/b^3$

mupad [B] time = 0.04, size = 37, normalized size = 0.73

$$\frac{6(a+bx)^{7/3} - 21a(a+bx)^{4/3} + 42a^2(a+bx)^{1/3}}{14b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(a + b*x)^(2/3),x)

[Out] $(6*(a + b*x)^{7/3} - 21*a*(a + b*x)^{4/3} + 42*a^2*(a + b*x)^{1/3})/(14*b^3)$

sympy [B] time = 1.82, size = 600, normalized size = 11.76

$$\frac{27a^{\frac{31}{3}} \sqrt[3]{1 + \frac{bx}{a}}}{14a^8b^3 + 42a^7b^4x + 42a^6b^5x^2 + 14a^5b^6x^3} - \frac{27a^{\frac{31}{3}}}{14a^8b^3 + 42a^7b^4x + 42a^6b^5x^2 + 14a^5b^6x^3} + \frac{72a^{\frac{28}{3}} bx \sqrt[3]{1 + \frac{bx}{a}}}{14a^8b^3 + 42a^7b^4x + 42a^6b^5x^2 + 14a^5b^6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(b*x+a)**(2/3),x)

[Out] $27*a**(31/3)*(1 + b*x/a)**(1/3)/(14*a**8*b**3 + 42*a**7*b**4*x + 42*a**6*b**5*x**2 + 14*a**5*b**6*x**3) - 27*a**(31/3)/(14*a**8*b**3 + 42*a**7*b**4*x + 42*a**6*b**5*x**2 + 14*a**5*b**6*x**3) + 72*a**(28/3)*b*x*(1 + b*x/a)**(1/3)/(14*a**8*b**3 + 42*a**7*b**4*x + 42*a**6*b**5*x**2 + 14*a**5*b**6*x**3) - 81*a**(28/3)*b*x/(14*a**8*b**3 + 42*a**7*b**4*x + 42*a**6*b**5*x**2 + 14*a**5*b**6*x**3) + 60*a**(25/3)*b**2*x**2*(1 + b*x/a)**(1/3)/(14*a**8*b**3 + 42*a**7*b**4*x + 42*a**6*b**5*x**2 + 14*a**5*b**6*x**3) - 81*a**(25/3)*b**2*x**2/(14*a**8*b**3 + 42*a**7*b**4*x + 42*a**6*b**5*x**2 + 14*a**5*b**6*x**3) + 18*a**(22/3)*b**3*x**3*(1 + b*x/a)**(1/3)/(14*a**8*b**3 + 42*a**7*b**4*x + 42*a**6*b**5*x**2 + 14*a**5*b**6*x**3) - 27*a**(22/3)*b**3*x**3/(14*a**8*b**3 + 42*a**7*b**4*x + 42*a**6*b**5*x**2 + 14*a**5*b**6*x**3) + 9*a**(19/3)*b**4*x**4*(1 + b*x/a)**(1/3)/(14*a**8*b**3 + 42*a**7*b**4*x + 42*a**6*b**5*x**2 + 14*a**5*b**6*x**3) + 6*a**(16/3)*b**5*x**5*(1 + b*x/a)**(1/3)/(14*a**8*b**3 + 42*a**7*b**4*x + 42*a**6*b**5*x**2 + 14*a**5*b**6*x**3)$

$$3.408 \quad \int \frac{x}{(a+bx)^{2/3}} dx$$

Optimal. Leaf size=32

$$\frac{3(a+bx)^{4/3}}{4b^2} - \frac{3a\sqrt[3]{a+bx}}{b^2}$$

[Out] $-3*a*(b*x+a)^{(1/3)}/b^2+3/4*(b*x+a)^{(4/3)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3(a+bx)^{4/3}}{4b^2} - \frac{3a\sqrt[3]{a+bx}}{b^2}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x)^(2/3), x]

[Out] $(-3*a*(a + b*x)^{(1/3)})/b^2 + (3*(a + b*x)^{(4/3)})/(4*b^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{x}{(a+bx)^{2/3}} dx &= \int \left(-\frac{a}{b(a+bx)^{2/3}} + \frac{\sqrt[3]{a+bx}}{b} \right) dx \\ &= -\frac{3a\sqrt[3]{a+bx}}{b^2} + \frac{3(a+bx)^{4/3}}{4b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.72

$$\frac{3(bx-3a)\sqrt[3]{a+bx}}{4b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x)^(2/3), x]

[Out] $(3*(-3*a + b*x)*(a + b*x)^{(1/3)})/(4*b^2)$

fricas [A] time = 0.46, size = 19, normalized size = 0.59

$$\frac{3 (bx + a)^{\frac{1}{3}} (bx - 3a)}{4 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(2/3),x, algorithm="fricas")`

[Out] $3/4*(b*x + a)^{(1/3)}*(b*x - 3*a)/b^2$

giac [A] time = 0.89, size = 23, normalized size = 0.72

$$\frac{3 \left((bx + a)^{\frac{4}{3}} - 4 (bx + a)^{\frac{1}{3}} a \right)}{4 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(2/3),x, algorithm="giac")`

[Out] $3/4*((b*x + a)^{(4/3)} - 4*(b*x + a)^{(1/3)}*a)/b^2$

maple [A] time = 0.00, size = 21, normalized size = 0.66

$$-\frac{3 (bx + a)^{\frac{1}{3}} (-bx + 3a)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(b*x+a)^(2/3),x)`

[Out] $-3/4*(b*x+a)^{(1/3)}*(-b*x+3*a)/b^2$

maxima [A] time = 1.34, size = 26, normalized size = 0.81

$$\frac{3 (bx + a)^{\frac{4}{3}}}{4 b^2} - \frac{3 (bx + a)^{\frac{1}{3}} a}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(2/3),x, algorithm="maxima")`

[Out] $3/4*(b*x + a)^{(4/3)}/b^2 - 3*(b*x + a)^{(1/3)}*a/b^2$

mupad [B] time = 0.03, size = 25, normalized size = 0.78

$$\frac{12 a (a + b x)^{1/3} - 3 (a + b x)^{4/3}}{4 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(a + b*x)^(2/3), x)

[Out] -(12*a*(a + b*x)^(1/3) - 3*(a + b*x)^(4/3))/(4*b^2)

sympy [B] time = 1.19, size = 162, normalized size = 5.06

$$-\frac{9a^{\frac{10}{3}}\sqrt[3]{1+\frac{bx}{a}}}{4a^2b^2+4ab^3x} + \frac{9a^{\frac{10}{3}}}{4a^2b^2+4ab^3x} - \frac{6a^{\frac{7}{3}}bx\sqrt[3]{1+\frac{bx}{a}}}{4a^2b^2+4ab^3x} + \frac{9a^{\frac{7}{3}}bx}{4a^2b^2+4ab^3x} + \frac{3a^{\frac{4}{3}}b^2x^2\sqrt[3]{1+\frac{bx}{a}}}{4a^2b^2+4ab^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)**(2/3), x)

[Out] -9*a**(10/3)*(1 + b*x/a)**(1/3)/(4*a**2*b**2 + 4*a*b**3*x) + 9*a**(10/3)/(4*a**2*b**2 + 4*a*b**3*x) - 6*a**(7/3)*b*x*(1 + b*x/a)**(1/3)/(4*a**2*b**2 + 4*a*b**3*x) + 9*a**(7/3)*b*x/(4*a**2*b**2 + 4*a*b**3*x) + 3*a**(4/3)*b**2*x**2*(1 + b*x/a)**(1/3)/(4*a**2*b**2 + 4*a*b**3*x)

$$3.409 \quad \int \frac{1}{(a+bx)^{2/3}} dx$$

Optimal. Leaf size=14

$$\frac{3\sqrt[3]{a+bx}}{b}$$

[Out] 3*(b*x+a)^(1/3)/b

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{3\sqrt[3]{a+bx}}{b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-2/3), x]

[Out] (3*(a + b*x)^(1/3))/b

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^{2/3}} dx = \frac{3\sqrt[3]{a+bx}}{b}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{3\sqrt[3]{a+bx}}{b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-2/3), x]

[Out] (3*(a + b*x)^(1/3))/b

fricas [A] time = 0.41, size = 12, normalized size = 0.86

$$\frac{3(bx + a)^{\frac{1}{3}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(2/3),x, algorithm="fricas")

[Out] 3*(b*x + a)^(1/3)/b

giac [A] time = 0.98, size = 12, normalized size = 0.86

$$\frac{3(bx + a)^{\frac{1}{3}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(2/3),x, algorithm="giac")

[Out] 3*(b*x + a)^(1/3)/b

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{3(bx + a)^{\frac{1}{3}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(2/3),x)

[Out] 3*(b*x+a)^(1/3)/b

maxima [A] time = 1.30, size = 12, normalized size = 0.86

$$\frac{3(bx + a)^{\frac{1}{3}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(2/3),x, algorithm="maxima")

[Out] 3*(b*x + a)^(1/3)/b

mupad [B] time = 0.02, size = 12, normalized size = 0.86

$$\frac{3(a + bx)^{\frac{1}{3}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(a + b*x)^(2/3), x)
```

```
[Out] (3*(a + b*x)^(1/3))/b
```

sympy [A] time = 0.06, size = 10, normalized size = 0.71

$$\frac{3\sqrt[3]{a + bx}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(2/3), x)
```

```
[Out] 3*(a + b*x)**(1/3)/b
```

$$3.410 \quad \int \frac{1}{x(a+bx)^{2/3}} dx$$

Optimal. Leaf size=80

$$\frac{3 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{2/3}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{a^{2/3}} - \frac{\log(x)}{2a^{2/3}}$$

[Out] $-1/2*\ln(x)/a^{(2/3)}+3/2*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(2/3)}-\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}}*3^{(1/2)}/a^{(2/3)})$

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {57, 617, 204, 31}

$$\frac{3 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{2/3}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{a^{2/3}} - \frac{\log(x)}{2a^{2/3}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a + b*x)^(2/3)),x]

[Out] $-((\text{Sqrt}[3]*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/a^{(2/3)}) - \text{Log}[x]/(2*a^{(2/3)}) + (3*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}])/(2*a^{(2/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 57

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2), x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_.)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x(a+bx)^{2/3}} dx &= -\frac{\log(x)}{2a^{2/3}} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a}-x} dx, x, \sqrt[3]{a+bx}\right)}{2a^{2/3}} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{a^{2/3} + \sqrt[3]{a}xx^2} dx, x, \sqrt[3]{a+bx}\right)}{2\sqrt[3]{a}} \\ &= -\frac{\log(x)}{2a^{2/3}} + \frac{3 \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)}{2a^{2/3}} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}\right)}{a^{2/3}} \\ &= -\frac{\sqrt{3} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{a^{2/3}} - \frac{\log(x)}{2a^{2/3}} + \frac{3 \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)}{2a^{2/3}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 93, normalized size = 1.16

$$\frac{\log\left(a^{2/3} + \sqrt[3]{a} \sqrt[3]{a+bx} + (a+bx)^{2/3}\right) - 2 \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right) + 2\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + 1}{\sqrt{3}}\right)}{2a^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)^(2/3)), x]

[Out] -1/2*(2*Sqrt[3]*ArcTan[(1 + (2*(a + b*x)^(1/3))/a^(1/3))/Sqrt[3]] - 2*Log[a^(1/3) - (a + b*x)^(1/3)] + Log[a^(2/3) + a^(1/3)*(a + b*x)^(1/3) + (a + b*x)^(2/3)])/a^(2/3)

fricas [B] time = 0.48, size = 115, normalized size = 1.44

$$\frac{2\sqrt{3}(a^2)^{\frac{1}{6}}a \arctan\left(\frac{\sqrt{3}(a^2)^{\frac{1}{6}}\left((a^2)^{\frac{1}{3}}a + 2(a^2)^{\frac{2}{3}}(bx+a)^{\frac{1}{3}}\right)}{3a^2}\right) + (a^2)^{\frac{2}{3}} \log\left((bx+a)^{\frac{2}{3}}a + (a^2)^{\frac{1}{3}}a + (a^2)^{\frac{2}{3}}(bx+a)^{\frac{1}{3}}\right) - 2(a^2)^{\frac{2}{3}} \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(2/3),x, algorithm="fricas")

[Out] $-1/2*(2*\sqrt{3}*(a^2)^{(1/6)}*a*\arctan(1/3*\sqrt{3}*(a^2)^{(1/6)}*((a^2)^{(1/3)}*a + 2*(a^2)^{(2/3)}*(b*x + a)^{(1/3)})/a^2) + (a^2)^{(2/3)}*\log((b*x + a)^{(2/3)}*a + (a^2)^{(1/3)}*a + (a^2)^{(2/3)}*(b*x + a)^{(1/3)}) - 2*(a^2)^{(2/3)}*\log((b*x + a)^{(1/3)}*a - (a^2)^{(2/3)})/a^2$

giac [A] time = 2.32, size = 78, normalized size = 0.98

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{a^{\frac{2}{3}}} - \frac{\log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{2a^{\frac{2}{3}}} + \frac{\log\left(\left|(bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right)}{a^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(2/3),x, algorithm="giac")

[Out] $-\sqrt{3}*\arctan(1/3*\sqrt{3}*(2*(b*x + a)^{(1/3)} + a^{(1/3)})/a^{(1/3)})/a^{(2/3)} - 1/2*\log((b*x + a)^{(2/3)} + (b*x + a)^{(1/3)}*a^{(1/3)} + a^{(2/3)})/a^{(2/3)} + \log(\text{abs}((b*x + a)^{(1/3)} - a^{(1/3)}))/a^{(2/3)}$

maple [A] time = 0.00, size = 76, normalized size = 0.95

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)}{a^{\frac{2}{3}}} + \frac{\ln\left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}\right)}{a^{\frac{2}{3}}} - \frac{\ln\left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}}\right)}{2a^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a)^(2/3),x)

[Out] $1/a^{(2/3)}*\ln(-a^{(1/3)}+(b*x+a)^{(1/3)})-1/2/a^{(2/3)}*\ln(a^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+(b*x+a)^{(2/3)})-1/a^{(2/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2*(b*x+a)^{(1/3)}/a^{(1/3)}+1))$

maxima [A] time = 2.87, size = 77, normalized size = 0.96

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{a^{\frac{2}{3}}} - \frac{\log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{2a^{\frac{2}{3}}} + \frac{\log\left(\left|(bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right)}{a^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(2/3),x, algorithm="maxima")

[Out] $-\sqrt{3} \arctan\left(\frac{1}{3}\sqrt{3} \frac{(2(bx+a)^{1/3} + a^{1/3})}{a^{1/3}}\right) a^{2/3} - \frac{1}{2} \log\left(\frac{(bx+a)^{2/3} + (bx+a)^{1/3} a^{1/3} + a^{2/3}}{a^{2/3}}\right) + \log\left(\frac{(bx+a)^{1/3} - a^{1/3}}{a^{2/3}}\right)$

mupad [B] time = 0.17, size = 95, normalized size = 1.19

$$\frac{\ln\left(9(a+bx)^{1/3} - 9a^{1/3}\right)}{a^{2/3}} + \frac{\ln\left(\frac{9a^{1/3}(-1+\sqrt{3}i)}{2} - 9(a+bx)^{1/3}\right)(-1+\sqrt{3}i)}{2a^{2/3}} - \frac{\ln\left(\frac{9a^{1/3}(1+\sqrt{3}i)}{2} + 9(a+bx)^{1/3}\right)}{2a^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(a + b*x)^(2/3)),x)

[Out] $\log\left(\frac{9(a+bx)^{1/3} - 9a^{1/3}}{a^{2/3}}\right) + \frac{\log\left(\frac{9a^{1/3}(3^{1/2}i - 1)}{2} - 9(a+bx)^{1/3}\right)(3^{1/2}i - 1)}{2a^{2/3}} - \frac{\log\left(\frac{9a^{1/3}(3^{1/2}i + 1)}{2} + 9(a+bx)^{1/3}\right)(3^{1/2}i + 1)}{2a^{2/3}}$

sympy [C] time = 1.93, size = 150, normalized size = 1.88

$$\frac{\log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{1}{3}\right)}{3a^{\frac{2}{3}} \Gamma\left(\frac{4}{3}\right)} + \frac{e^{-\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x} e^{\frac{2i\pi}{3}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{1}{3}\right)}{3a^{\frac{2}{3}} \Gamma\left(\frac{4}{3}\right)} + \frac{e^{\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x} e^{\frac{4i\pi}{3}}}{\sqrt[3]{a}}\right) \Gamma\left(\frac{1}{3}\right)}{3a^{\frac{2}{3}} \Gamma\left(\frac{4}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)**(2/3),x)

[Out] $\log\left(1 - b^{1/3} \frac{(a/b + x)^{1/3}}{a^{1/3}}\right) \frac{\Gamma(1/3)}{(3a^{2/3}) \Gamma(4/3)} + \exp(-2i\pi/3) \log\left(1 - b^{1/3} \frac{(a/b + x)^{1/3}}{a^{1/3}}\right) \frac{\exp(i\pi/3) \Gamma(1/3)}{(3a^{2/3}) \Gamma(4/3)} + \exp(2i\pi/3) \log\left(1 - b^{1/3} \frac{(a/b + x)^{1/3}}{a^{1/3}}\right) \frac{\exp(i\pi/3) \Gamma(1/3)}{(3a^{2/3}) \Gamma(4/3)}$

$$3.411 \quad \int \frac{1}{x^2(a+bx)^{2/3}} dx$$

Optimal. Leaf size=98

$$\frac{b \log(x)}{3a^{5/3}} - \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{a^{5/3}} + \frac{2b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{5/3}} - \frac{\sqrt[3]{a+bx}}{ax}$$

[Out] $-(b*x+a)^{(1/3)}/a/x+1/3*b*\ln(x)/a^{(5/3)}-b*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(5/3)}+2/3*b*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)}*3^{(1/2)})/a^{(5/3)}*3^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 57, 617, 204, 31}

$$\frac{b \log(x)}{3a^{5/3}} - \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{a^{5/3}} + \frac{2b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{5/3}} - \frac{\sqrt[3]{a+bx}}{ax}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(a + b*x)^(2/3)), x]

[Out] $-\left(\frac{(a + b*x)^{(1/3)}}{(a*x)} + \frac{(2*b*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})]/(\text{Sqrt}[3]*a^{(1/3)})]}{(\text{Sqrt}[3]*a^{(5/3)})} + \frac{(b*\text{Log}[x])}{(3*a^{(5/3)})} - \frac{(b*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)})]}{a^{(5/3)}}\right)$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 57

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2),

$x] + (-\text{Dist}[3/(2*b*q), \text{Subst}[\text{Int}[1/(q^2 + q*x + x^2)], x], x, (c + d*x)^{(1/3)}], x] - \text{Dist}[3/(2*b*q^2), \text{Subst}[\text{Int}[1/(q - x)], x], x, (c + d*x)^{(1/3)}], x]) /; \text{FreeQ}\{a, b, c, d\}, x \ \&\& \ \text{PosQ}[(b*c - a*d)/b]$

Rule 204

$\text{Int}[(a_ + (b_)*(x_)^2)^{-1}, x_Symbol] := -\text{Simp}[\text{ArcTan}[\text{Rt}[-b, 2]*x]/\text{Rt}[-a, 2]]/(\text{Rt}[-a, 2]*\text{Rt}[-b, 2]), x] /; \text{FreeQ}\{a, b\}, x \ \&\& \ \text{PosQ}[a/b] \ \&\& \ (\text{LtQ}[a, 0] \ || \ \text{LtQ}[b, 0])$

Rule 617

$\text{Int}[(a_ + (b_)*(x_) + (c_)*(x_)^2)^{-1}, x_Symbol] := \text{With}\{q = 1 - 4*S \text{implify}[(a*c)/b^2]\}, \text{Dist}[-2/b, \text{Subst}[\text{Int}[1/(q - x^2)], x], x, 1 + (2*c*x)/b], x] /; \text{RationalQ}[q] \ \&\& \ (\text{EqQ}[q^2, 1] \ || \ !\text{RationalQ}[b^2 - 4*a*c]) /; \text{FreeQ}\{a, b, c\}, x \ \&\& \ \text{NeQ}[b^2 - 4*a*c, 0]$

Rubi steps

$$\begin{aligned} \int \frac{1}{x^2(a+bx)^{2/3}} dx &= -\frac{\sqrt[3]{a+bx}}{ax} - \frac{(2b) \int \frac{1}{x(a+bx)^{2/3}} dx}{3a} \\ &= -\frac{\sqrt[3]{a+bx}}{ax} + \frac{b \log(x)}{3a^{5/3}} + \frac{b \text{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{a^{5/3}} + \frac{b \text{Subst}\left(\int \frac{1}{a^{2/3} + \sqrt[3]{a}x + x^2} dx, x, \right)}{a^{4/3}} \\ &= -\frac{\sqrt[3]{a+bx}}{ax} + \frac{b \log(x)}{3a^{5/3}} - \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{a^{5/3}} - \frac{(2b) \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}\right)}{a^{5/3}} \\ &= -\frac{\sqrt[3]{a+bx}}{ax} + \frac{2b \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3}a^{5/3}} + \frac{b \log(x)}{3a^{5/3}} - \frac{b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{a^{5/3}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 31, normalized size = 0.32

$$\frac{3b\sqrt[3]{a+bx} {}_2F_1\left(\frac{1}{3}, 2; \frac{4}{3}; \frac{bx}{a} + 1\right)}{a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)^(2/3)),x]

[Out] $(3*b*(a + b*x)^{1/3}*Hypergeometric2F1[1/3, 2, 4/3, 1 + (b*x)/a])/a^2$

fricas [B] time = 0.45, size = 166, normalized size = 1.69

$$\frac{2\sqrt{3}abx\sqrt{-(-a^2)^{\frac{1}{3}}}\arctan\left(-\frac{\left(\sqrt{3}(-a^2)^{\frac{1}{3}}a-2\sqrt{3}(-a^2)^{\frac{2}{3}}(bx+a)^{\frac{1}{3}}\right)\sqrt{-(-a^2)^{\frac{1}{3}}}}{3a^2}\right)+(-a^2)^{\frac{2}{3}}bx\log\left((bx+a)^{\frac{2}{3}}a-(-a^2)^{\frac{1}{3}}a+\right)}{3a^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(b*x+a)^(2/3),x, algorithm="fricas")`

[Out] $\frac{1}{3}*(2*\sqrt{3}*a*b*x*\sqrt{-(-a^2)^{1/3}}*\arctan(-1/3*(\sqrt{3}*(-a^2)^{1/3}*a-2*\sqrt{3}*(-a^2)^{2/3}*(b*x+a)^{1/3}))*\sqrt{-(-a^2)^{1/3}}/a^2+(a^2)^{2/3}*b*x*\log((b*x+a)^{2/3}*a-(-a^2)^{1/3}*a+(a^2)^{2/3}*(b*x+a)^{1/3}))-2*(-a^2)^{2/3}*b*x*\log((b*x+a)^{1/3}*a-(-a^2)^{2/3}))-3*(b*x+a)^{1/3}*a^2/(a^3*x)$

giac [A] time = 2.37, size = 108, normalized size = 1.10

$$\frac{2\sqrt{3}b^2\arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)+b^2\log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)-2b^2\log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)-\frac{3(bx+a)^{\frac{1}{3}}b}{ax}}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(b*x+a)^(2/3),x, algorithm="giac")`

[Out] $\frac{1}{3}*(2*\sqrt{3}*b^2*\arctan(1/3*\sqrt{3}*(2*(b*x+a)^{1/3}+a^{1/3}))/a^{1/3})/a^{5/3}+b^2*\log((b*x+a)^{2/3}+(b*x+a)^{1/3}*a^{1/3}+a^{2/3}))/a^{5/3}-2*b^2*\log(\text{abs}((b*x+a)^{1/3}-a^{1/3}))/a^{5/3}-3*(b*x+a)^{1/3}*b/(a*x))/b$

maple [A] time = 0.01, size = 95, normalized size = 0.97

$$\frac{2\sqrt{3}b\arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)+2b\ln\left(-a^{\frac{1}{3}}+(bx+a)^{\frac{1}{3}}\right)+b\ln\left(a^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+(bx+a)^{\frac{2}{3}}\right)}{3a^{\frac{5}{3}}}-\frac{3(bx+a)^{\frac{1}{3}}b}{ax}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^2/(b*x+a)^(2/3),x)`

[Out] $-(b*x+a)^{(1/3)}/a/x-2/3*b/a^{(5/3)}*\ln(-a^{(1/3)}+(b*x+a)^{(1/3)})+1/3*b/a^{(5/3)}*\ln(a^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+(b*x+a)^{(2/3)})+2/3*b/a^{(5/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2*(b*x+a)^{(1/3)}/a^{(1/3)}+1))$

maxima [A] time = 2.95, size = 106, normalized size = 1.08

$$\frac{2\sqrt{3}b\arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{3a^{\frac{5}{3}}}-\frac{(bx+a)^{\frac{1}{3}}b}{(bx+a)a-a^2}+\frac{b\log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)}{3a^{\frac{5}{3}}}-\frac{2b\log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)}{3a^{\frac{5}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(b*x+a)^(2/3),x, algorithm="maxima")`

[Out] $2/3*\sqrt{3}*b*\arctan(1/3*\sqrt{3}*(2*(b*x+a)^{(1/3)}+a^{(1/3)})/a^{(1/3)})/a^{(5/3)}-(b*x+a)^{(1/3)}*b/((b*x+a)*a-a^2)+1/3*b*\log((b*x+a)^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+a^{(2/3)})/a^{(5/3)}-2/3*b*\log((b*x+a)^{(1/3)}-a^{(1/3)})/a^{(5/3)}$

mupad [B] time = 0.13, size = 122, normalized size = 1.24

$$-\frac{(a+bx)^{1/3}}{ax}+\frac{\ln\left(\frac{3(b-\sqrt{3}bi)}{a^{2/3}}+\frac{6b(a+bx)^{1/3}}{a}\right)(b-\sqrt{3}bi)}{3a^{5/3}}+\frac{\ln\left(\frac{3(b+\sqrt{3}bi)}{a^{2/3}}+\frac{6b(a+bx)^{1/3}}{a}\right)(b+\sqrt{3}bi)}{3a^{5/3}}-2b\ln\left(\frac{(a+bx)^{1/3}}{a}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^2*(a+b*x)^(2/3)),x)`

[Out] $(\log((3*(b-3^{(1/2)}*b*1i))/a^{(2/3)}+(6*b*(a+b*x)^{(1/3)})/a)*(b-3^{(1/2)}*b*1i))/(3*a^{(5/3)})-(a+b*x)^{(1/3)}/(a*x)+(\log((3*(b+3^{(1/2)}*b*1i))/a^{(2/3)}+(6*b*(a+b*x)^{(1/3)})/a)*(b+3^{(1/2)}*b*1i))/(3*a^{(5/3)})-(2*b*\log((a+b*x)^{(1/3)}-a^{(1/3)}))/(3*a^{(5/3)})$

sympy [C] time = 2.27, size = 830, normalized size = 8.47

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(b*x+a)**(2/3),x)`

[Out] $-2*a^{(4/3)}*b^{(5/3)}*(a/b+x)^{(2/3)}*\exp(2*I*pi/3)*\log(1-b^{(1/3)}*(a/b+x)^{(1/3)}/a^{(1/3)})*\gamma(1/3)/(9*a^{(3/3)}*b^{(2/3)}*(a/b+x)^{(2/3)}*\exp(2*I*pi/3))$

$$\begin{aligned}
& i/3) * \text{gamma}(4/3) - 9 * a^{**2} * b^{**5/3} * (a/b + x)^{**5/3} * \exp(2 * I * \text{pi}/3) * \text{gamma}(4/3) \\
&) - 2 * a^{**4/3} * b^{**5/3} * (a/b + x)^{**2/3} * \log(1 - b^{**1/3} * (a/b + x)^{**1/3}) * \\
& \exp_polar(2 * I * \text{pi}/3) / a^{**1/3}) * \text{gamma}(1/3) / (9 * a^{**3} * b^{**2/3} * (a/b + x)^{**2/3} * \\
& \exp(2 * I * \text{pi}/3) * \text{gamma}(4/3) - 9 * a^{**2} * b^{**5/3} * (a/b + x)^{**5/3} * \exp(2 * I * \text{pi}/3) * \text{g} \\
& \text{amma}(4/3)) - 2 * a^{**4/3} * b^{**5/3} * (a/b + x)^{**2/3} * \exp(-2 * I * \text{pi}/3) * \log(1 - b * \\
& * (1/3) * (a/b + x)^{**1/3}) * \exp_polar(4 * I * \text{pi}/3) / a^{**1/3}) * \text{gamma}(1/3) / (9 * a^{**3} * b * \\
& * (2/3) * (a/b + x)^{**2/3} * \exp(2 * I * \text{pi}/3) * \text{gamma}(4/3) - 9 * a^{**2} * b^{**5/3} * (a/b + x) \\
&)^{**5/3} * \exp(2 * I * \text{pi}/3) * \text{gamma}(4/3)) + 2 * a^{**1/3} * b^{**8/3} * (a/b + x)^{**5/3} * e \\
& xp(2 * I * \text{pi}/3) * \log(1 - b^{**1/3} * (a/b + x)^{**1/3}) / a^{**1/3}) * \text{gamma}(1/3) / (9 * a^{**3} \\
& * b^{**2/3} * (a/b + x)^{**2/3} * \exp(2 * I * \text{pi}/3) * \text{gamma}(4/3) - 9 * a^{**2} * b^{**5/3} * (a/b \\
& + x)^{**5/3} * \exp(2 * I * \text{pi}/3) * \text{gamma}(4/3)) + 2 * a^{**1/3} * b^{**8/3} * (a/b + x)^{**5/3} \\
&) * \log(1 - b^{**1/3} * (a/b + x)^{**1/3}) * \exp_polar(2 * I * \text{pi}/3) / a^{**1/3}) * \text{gamma}(1/3 \\
&) / (9 * a^{**3} * b^{**2/3} * (a/b + x)^{**2/3} * \exp(2 * I * \text{pi}/3) * \text{gamma}(4/3) - 9 * a^{**2} * b^{**5} \\
& /3) * (a/b + x)^{**5/3} * \exp(2 * I * \text{pi}/3) * \text{gamma}(4/3)) + 2 * a^{**1/3} * b^{**8/3} * (a/b + \\
& x)^{**5/3} * \exp(-2 * I * \text{pi}/3) * \log(1 - b^{**1/3} * (a/b + x)^{**1/3}) * \exp_polar(4 * I * p \\
& i/3) / a^{**1/3}) * \text{gamma}(1/3) / (9 * a^{**3} * b^{**2/3} * (a/b + x)^{**2/3} * \exp(2 * I * \text{pi}/3) * \text{g} \\
& \text{amma}(4/3) - 9 * a^{**2} * b^{**5/3} * (a/b + x)^{**5/3} * \exp(2 * I * \text{pi}/3) * \text{gamma}(4/3)) + 3 * \\
& a * b^{**2} * (a/b + x) * \exp(2 * I * \text{pi}/3) * \text{gamma}(1/3) / (9 * a^{**3} * b^{**2/3} * (a/b + x)^{**2/3} \\
& * \exp(2 * I * \text{pi}/3) * \text{gamma}(4/3) - 9 * a^{**2} * b^{**5/3} * (a/b + x)^{**5/3} * \exp(2 * I * \text{pi}/3) * \\
& \text{gamma}(4/3))
\end{aligned}$$

$$3.412 \quad \int \frac{1}{x^3(a+bx)^{2/3}} dx$$

Optimal. Leaf size=130

$$-\frac{5b^2 \log(x)}{18a^{8/3}} + \frac{5b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{8/3}} - \frac{5b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{8/3}} + \frac{5b\sqrt[3]{a+bx}}{6a^2x} - \frac{\sqrt[3]{a+bx}}{2ax^2}$$

[Out] $-1/2*(b*x+a)^{(1/3)}/a/x^2+5/6*b*(b*x+a)^{(1/3)}/a^2/x-5/18*b^2*\ln(x)/a^{(8/3)}+5/6*b^2*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(8/3)}-5/9*b^2*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}})/a^{(8/3)*3^{(1/2)}}$

Rubi [A] time = 0.05, antiderivative size = 130, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 57, 617, 204, 31}

$$-\frac{5b^2 \log(x)}{18a^{8/3}} + \frac{5b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{8/3}} - \frac{5b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{8/3}} + \frac{5b\sqrt[3]{a+bx}}{6a^2x} - \frac{\sqrt[3]{a+bx}}{2ax^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(a + b*x)^(2/3)), x]

[Out] $-(a + b*x)^{(1/3)}/(2*a*x^2) + (5*b*(a + b*x)^{(1/3)})/(6*a^2*x) - (5*b^2*ArcTan[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(Sqrt[3]*a^{(1/3)})])/(3*Sqrt[3]*a^{(8/3)}) - (5*b^2*Log[x])/(18*a^{(8/3)}) + (5*b^2*Log[a^{(1/3)} - (a + b*x)^{(1/3)}])/(6*a^{(8/3)})$

Rule 31

Int[((a_.) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 57

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2),
x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x
])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^3(a+bx)^{2/3}} dx &= -\frac{\sqrt[3]{a+bx}}{2ax^2} - \frac{(5b) \int \frac{1}{x^2(a+bx)^{2/3}} dx}{6a} \\
&= -\frac{\sqrt[3]{a+bx}}{2ax^2} + \frac{5b\sqrt[3]{a+bx}}{6a^2x} + \frac{(5b^2) \int \frac{1}{x(a+bx)^{2/3}} dx}{9a^2} \\
&= -\frac{\sqrt[3]{a+bx}}{2ax^2} + \frac{5b\sqrt[3]{a+bx}}{6a^2x} - \frac{5b^2 \log(x)}{18a^{8/3}} - \frac{(5b^2) \text{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{6a^{8/3}} - \frac{(5b^2) \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{a+bx}\right)}{3a^{8/3}} \\
&= -\frac{\sqrt[3]{a+bx}}{2ax^2} + \frac{5b\sqrt[3]{a+bx}}{6a^2x} - \frac{5b^2 \log(x)}{18a^{8/3}} + \frac{5b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{8/3}} + \frac{(5b^2) \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{a+bx}\right)}{3a^{8/3}} \\
&= -\frac{\sqrt[3]{a+bx}}{2ax^2} + \frac{5b\sqrt[3]{a+bx}}{6a^2x} - \frac{5b^2 \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{3\sqrt{3}a^{8/3}} - \frac{5b^2 \log(x)}{18a^{8/3}} + \frac{5b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{6a^{8/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.25

$$-\frac{3b^2\sqrt[3]{a+bx} {}_2F_1\left(\frac{1}{3}, 3; \frac{4}{3}; \frac{bx}{a} + 1\right)}{a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)^(2/3)),x]

[Out] (-3*b^2*(a + b*x)^(1/3)*Hypergeometric2F1[1/3, 3, 4/3, 1 + (b*x)/a])/a^3

fricas [A] time = 0.43, size = 162, normalized size = 1.25

$$\frac{10\sqrt{3}\left(a^2\right)^{\frac{1}{6}}ab^2x^2\arctan\left(\frac{\left(a^2\right)^{\frac{1}{6}}\left(\sqrt{3}\left(a^2\right)^{\frac{1}{3}}a+2\sqrt{3}\left(a^2\right)^{\frac{2}{3}}(bx+a)^{\frac{1}{3}}\right)}{3a^2}\right)+5\left(a^2\right)^{\frac{2}{3}}b^2x^2\log\left(\left(bx+a\right)^{\frac{2}{3}}a+\left(a^2\right)^{\frac{1}{3}}a+\left(a^2\right)^{\frac{2}{3}}(bx+a)\right)}{18a^4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(2/3),x, algorithm="fricas")

[Out] -1/18*(10*sqrt(3)*(a^2)^(1/6)*a*b^2*x^2*arctan(1/3*(a^2)^(1/6)*(sqrt(3)*(a^2)^(1/3)*a + 2*sqrt(3)*(a^2)^(2/3)*(b*x + a)^(1/3))/a^2) + 5*(a^2)^(2/3)*b^2*x^2*log((b*x + a)^(2/3)*a + (a^2)^(1/3)*a + (a^2)^(2/3)*(b*x + a)^(1/3)) - 10*(a^2)^(2/3)*b^2*x^2*log((b*x + a)^(1/3)*a - (a^2)^(2/3)) - 3*(5*a^2*b*x - 3*a^3)*(b*x + a)^(1/3))/(a^4*x^2)

giac [A] time = 2.05, size = 130, normalized size = 1.00

$$\frac{10\sqrt{3}b^3\arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)+5b^3\log\left(\frac{(bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}}{a^{\frac{1}{3}}}\right)-10b^3\log\left(\frac{(bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}}{a^{\frac{1}{3}}}\right)-3\left(5(bx+a)^{\frac{4}{3}}b^3-8(bx+a)^{\frac{1}{3}}ab^3\right)}{18b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(2/3),x, algorithm="giac")

[Out] -1/18*(10*sqrt(3)*b^3*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3)))/a^(8/3) + 5*b^3*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)))/a^(8/3) - 10*b^3*log(abs((b*x + a)^(1/3) - a^(1/3)))/a^(8/3) - 3*(5*(b*x + a)^(4/3)*b^3 - 8*(b*x + a)^(1/3)*a*b^3)/(a^2*b^2*x^2)/b

maple [A] time = 0.01, size = 117, normalized size = 0.90

$$\frac{5\sqrt{3}b^2\arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)+5b^2\ln\left(-a^{\frac{1}{3}}+(bx+a)^{\frac{1}{3}}\right)-5b^2\ln\left(a^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+(bx+a)^{\frac{2}{3}}\right)+\frac{5(bx+a)}{6a^2x}}{9a^{\frac{8}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^3/(b*x+a)^(2/3),x)`

[Out]
$$-1/2*(b*x+a)^{(1/3)}/a/x^2+5/6*b*(b*x+a)^{(1/3)}/a^2/x+5/9*b^2/a^{(8/3)}*\ln(-a^{(1/3)}+(b*x+a)^{(1/3)})-5/18*b^2/a^{(8/3)}*\ln(a^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+(b*x+a)^{(2/3)})-5/9*b^2/a^{(8/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2*(b*x+a)^{(1/3)}/a^{(1/3)}+1))$$

maxima [A] time = 3.04, size = 142, normalized size = 1.09

$$\frac{5\sqrt{3}b^2 \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{9a^{\frac{8}{3}}} - \frac{5b^2 \log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+a^{\frac{2}{3}}\right)}{18a^{\frac{8}{3}}} + \frac{5b^2 \log\left((bx+a)^{\frac{1}{3}}-a^{\frac{1}{3}}\right)}{9a^{\frac{8}{3}}} + \frac{5(bx+a)^{\frac{1}{3}}}{6(bx+a)^{\frac{8}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^3/(b*x+a)^(2/3),x, algorithm="maxima")`

[Out]
$$-5/9*\sqrt{3}*b^2*\arctan(1/3*\sqrt{3}*(2*(b*x+a)^{(1/3)}+a^{(1/3)})/a^{(1/3)})/a^{(8/3)}-5/18*b^2*\log((b*x+a)^{(2/3)}+(b*x+a)^{(1/3)}*a^{(1/3)}+a^{(2/3)})/a^{(8/3)}+5/9*b^2*\log((b*x+a)^{(1/3)}-a^{(1/3)})/a^{(8/3)}+1/6*(5*(b*x+a)^{(4/3)}*b^2-8*(b*x+a)^{(1/3)}*a*b^2)/((b*x+a)^2*a^2-2*(b*x+a)*a^3+a^4)$$

mapad [B] time = 0.13, size = 175, normalized size = 1.35

$$\frac{5b^2 \ln\left((a+bx)^{1/3}-a^{1/3}\right)}{9a^{8/3}} - \frac{\frac{4b^2(a+bx)^{1/3}}{3a} - \frac{5b^2(a+bx)^{4/3}}{6a^2}}{(a+bx)^2-2a(a+bx)+a^2} + \frac{5b^2 \ln\left(\frac{5b^2(a+bx)^{1/3}}{a^2} - \frac{5b^2\left(-\frac{1}{2}+\frac{\sqrt{3}1i}{2}\right)}{a^{5/3}}\right)\left(-\frac{1}{2}+\frac{\sqrt{3}1i}{2}\right)}{9a^{8/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^3*(a+b*x)^(2/3)),x)`

[Out]
$$(5*b^2*\log((a+b*x)^{(1/3)}-a^{(1/3)}))/(9*a^{(8/3)}) - ((4*b^2*(a+b*x)^{(1/3)})/(3*a) - (5*b^2*(a+b*x)^{(4/3)})/(6*a^2))/((a+b*x)^2-2*a*(a+b*x)+a^2) + (5*b^2*\log((5*b^2*(a+b*x)^{(1/3)})/a^2 - (5*b^2*((3^{(1/2)}*1i)/2 - 1/2))/a^{(5/3)}))*((3^{(1/2)}*1i)/2 - 1/2))/(9*a^{(8/3)}) - (5*b^2*\log((5*b^2*(a+b*x)^{(1/3)})/a^2 + (5*b^2*((3^{(1/2)}*1i)/2 + 1/2))/a^{(5/3)}))*((3^{(1/2)}*1i)/2 + 1/2))/(9*a^{(8/3)})$$

sympy [C] time = 2.73, size = 2728, normalized size = 20.98

result too large to display

$$\begin{aligned}
& a/b + x)^{(2/3)} \exp(2I\pi/3) \gamma(4/3) - 162a^{**6}b^{**}(5/3)(a/b + x)^{(5/3)} \\
& \exp(2I\pi/3) \gamma(4/3) + 162a^{**5}b^{**}(8/3)(a/b + x)^{(8/3)} \exp(2I\pi/3) \gamma(4/3) \\
& - 54a^{**4}b^{**}(11/3)(a/b + x)^{(11/3)} \exp(2I\pi/3) \gamma(4/3) - 10a^{**}(4/3)b^{**}(17/3) \\
& (a/b + x)^{(11/3)} \exp(2I\pi/3) \log(1 - b^{**}(1/3)) (a/b + x)^{(1/3)} / a^{**}(1/3) \gamma(1/3) \\
& / (54a^{**7}b^{**}(2/3)(a/b + x)^{(2/3)} \exp(2I\pi/3) \gamma(4/3) - 162a^{**6}b^{**}(5/3) \\
& (a/b + x)^{(5/3)} \exp(2I\pi/3) \gamma(4/3) + 162a^{**5}b^{**}(8/3)(a/b + x)^{(8/3)} \\
& \exp(2I\pi/3) \gamma(4/3) - 54a^{**4}b^{**}(11/3)(a/b + x)^{(11/3)} \exp(2I\pi/3) \gamma(4/3) \\
& - 10a^{**}(4/3)b^{**}(17/3)(a/b + x)^{(11/3)} \log(1 - b^{**}(1/3)) (a/b + x)^{(1/3)} \\
& \exp_{\text{polar}}(2I\pi/3) / a^{**}(1/3) \gamma(1/3) / (54a^{**7}b^{**}(2/3)(a/b + x)^{(2/3)} \exp(2I\pi/3) \\
& \gamma(4/3) - 162a^{**6}b^{**}(5/3)(a/b + x)^{(5/3)} \exp(2I\pi/3) \gamma(4/3) \\
& + 162a^{**5}b^{**}(8/3)(a/b + x)^{(8/3)} \exp(2I\pi/3) \gamma(4/3) - 54a^{**4}b^{**} \\
& (11/3)(a/b + x)^{(11/3)} \exp(2I\pi/3) \gamma(4/3) - 10a^{**}(4/3)b^{**}(17/3) \\
& (a/b + x)^{(11/3)} \exp(-2I\pi/3) \log(1 - b^{**}(1/3)) (a/b + x)^{(1/3)} \exp_{\text{polar}} \\
& (4I\pi/3) / a^{**}(1/3) \gamma(1/3) / (54a^{**7}b^{**}(2/3)(a/b + x)^{(2/3)} \exp(2I\pi/3) \\
& \gamma(4/3) - 162a^{**6}b^{**}(5/3)(a/b + x)^{(5/3)} \exp(2I\pi/3) \gamma(4/3) \\
& + 162a^{**5}b^{**}(8/3)(a/b + x)^{(8/3)} \exp(2I\pi/3) \gamma(4/3) - 54a^{**4}b^{**} \\
& (11/3)(a/b + x)^{(11/3)} \exp(2I\pi/3) \gamma(4/3) - 24a^{**4}b^{**3}(a/b + x) \\
& \exp(2I\pi/3) \gamma(1/3) / (54a^{**7}b^{**}(2/3)(a/b + x)^{(2/3)} \exp(2I\pi/3) \gamma(4/3) \\
& - 162a^{**6}b^{**}(5/3)(a/b + x)^{(5/3)} \exp(2I\pi/3) \gamma(4/3) + 162a^{**5}b^{**} \\
& (8/3)(a/b + x)^{(8/3)} \exp(2I\pi/3) \gamma(4/3) - 54a^{**4}b^{**}(11/3)(a/b + x) \\
& (11/3) \exp(2I\pi/3) \gamma(4/3) + 39a^{**3}b^{**4}(a/b + x)^{**2} \exp(2I\pi/3) \gamma(1/3) \\
& / (54a^{**7}b^{**}(2/3)(a/b + x)^{(2/3)} \exp(2I\pi/3) \gamma(4/3) - 162a^{**6}b^{**}(5/3) \\
& (a/b + x)^{(5/3)} \exp(2I\pi/3) \gamma(4/3) + 162a^{**5}b^{**}(8/3)(a/b + x)^{(8/3)} \\
& \exp(2I\pi/3) \gamma(4/3) - 54a^{**4}b^{**}(11/3)(a/b + x)^{(11/3)} \exp(2I\pi/3) \gamma(4/3) \\
& - 15a^{**2}b^{**5}(a/b + x)^{**3} \exp(2I\pi/3) \gamma(1/3) / (54a^{**7}b^{**}(2/3)(a/b + x) \\
& (2/3) \exp(2I\pi/3) \gamma(4/3) - 162a^{**6}b^{**}(5/3)(a/b + x)^{(5/3)} \exp(2I\pi/3) \gamma(4/3) \\
& + 162a^{**5}b^{**}(8/3)(a/b + x)^{(8/3)} \exp(2I\pi/3) \gamma(4/3) - 54a^{**4}b^{**} \\
& (11/3)(a/b + x)^{(11/3)} \exp(2I\pi/3) \gamma(4/3)
\end{aligned}$$

$$3.413 \quad \int \frac{x^3}{(a+bx)^{4/3}} dx$$

Optimal. Leaf size=70

$$\frac{3a^3}{b^4 \sqrt[3]{a+bx}} + \frac{9a^2(a+bx)^{2/3}}{2b^4} - \frac{9a(a+bx)^{5/3}}{5b^4} + \frac{3(a+bx)^{8/3}}{8b^4}$$

[Out] $3*a^3/b^4/(b*x+a)^{(1/3)}+9/2*a^2*(b*x+a)^{(2/3)}/b^4-9/5*a*(b*x+a)^{(5/3)}/b^4+3/8*(b*x+a)^{(8/3)}/b^4$

Rubi [A] time = 0.02, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3a^3}{b^4 \sqrt[3]{a+bx}} + \frac{9a^2(a+bx)^{2/3}}{2b^4} - \frac{9a(a+bx)^{5/3}}{5b^4} + \frac{3(a+bx)^{8/3}}{8b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3/(a + b*x)^(4/3), x]

[Out] $(3*a^3)/(b^4*(a + b*x)^{(1/3)}) + (9*a^2*(a + b*x)^{(2/3)})/(2*b^4) - (9*a*(a + b*x)^{(5/3)})/(5*b^4) + (3*(a + b*x)^{(8/3)})/(8*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(a+bx)^{4/3}} dx &= \int \left(-\frac{a^3}{b^3(a+bx)^{4/3}} + \frac{3a^2}{b^3 \sqrt[3]{a+bx}} - \frac{3a(a+bx)^{2/3}}{b^3} + \frac{(a+bx)^{5/3}}{b^3} \right) dx \\ &= \frac{3a^3}{b^4 \sqrt[3]{a+bx}} + \frac{9a^2(a+bx)^{2/3}}{2b^4} - \frac{9a(a+bx)^{5/3}}{5b^4} + \frac{3(a+bx)^{8/3}}{8b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.66

$$\frac{3(81a^3 + 27a^2bx - 9ab^2x^2 + 5b^3x^3)}{40b^4 \sqrt[3]{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(a + b*x)^(4/3), x]

[Out] (3*(81*a^3 + 27*a^2*b*x - 9*a*b^2*x^2 + 5*b^3*x^3))/(40*b^4*(a + b*x)^(1/3))

fricas [A] time = 0.42, size = 52, normalized size = 0.74

$$\frac{3(5b^3x^3 - 9ab^2x^2 + 27a^2bx + 81a^3)(bx + a)^{\frac{2}{3}}}{40(b^5x + ab^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(4/3), x, algorithm="fricas")

[Out] 3/40*(5*b^3*x^3 - 9*a*b^2*x^2 + 27*a^2*b*x + 81*a^3)*(b*x + a)^(2/3)/(b^5*x + a*b^4)

giac [A] time = 1.10, size = 62, normalized size = 0.89

$$\frac{3a^3}{(bx + a)^{\frac{1}{3}}b^4} + \frac{3\left(5(bx + a)^{\frac{8}{3}}b^{28} - 24(bx + a)^{\frac{5}{3}}ab^{28} + 60(bx + a)^{\frac{2}{3}}a^2b^{28}\right)}{40b^{32}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(4/3), x, algorithm="giac")

[Out] 3*a^3/((b*x + a)^(1/3)*b^4) + 3/40*(5*(b*x + a)^(8/3)*b^28 - 24*(b*x + a)^(5/3)*a*b^28 + 60*(b*x + a)^(2/3)*a^2*b^28)/b^32

maple [A] time = 0.00, size = 43, normalized size = 0.61

$$\frac{\frac{3}{8}b^3x^3 - \frac{27}{40}ab^2x^2 + \frac{81}{40}a^2bx + \frac{243}{40}a^3}{(bx + a)^{\frac{1}{3}}b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^(4/3), x)

[Out] 3/40/(b*x+a)^(1/3)*(5*b^3*x^3-9*a*b^2*x^2+27*a^2*b*x+81*a^3)/b^4

maxima [A] time = 1.36, size = 56, normalized size = 0.80

$$\frac{3(bx + a)^{\frac{8}{3}}}{8b^4} - \frac{9(bx + a)^{\frac{5}{3}}a}{5b^4} + \frac{9(bx + a)^{\frac{2}{3}}a^2}{2b^4} + \frac{3a^3}{(bx + a)^{\frac{1}{3}}b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^(4/3),x, algorithm="maxima")

[Out] $\frac{3}{8}*(b*x + a)^{(8/3)}/b^4 - \frac{9}{5}*(b*x + a)^{(5/3)}*a/b^4 + \frac{9}{2}*(b*x + a)^{(2/3)}*a^2/b^4 + \frac{3*a^3}{(b*x + a)^{(1/3)}*b^4}$

mupad [B] time = 0.05, size = 56, normalized size = 0.80

$$\frac{3(a+bx)^{8/3}}{8b^4} + \frac{9a^2(a+bx)^{2/3}}{2b^4} + \frac{3a^3}{b^4(a+bx)^{1/3}} - \frac{9a(a+bx)^{5/3}}{5b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(a + b*x)^(4/3),x)

[Out] $\frac{3*(a + b*x)^{(8/3)}}{(8*b^4)} + \frac{(9*a^2*(a + b*x)^{(2/3)})}{(2*b^4)} + \frac{(3*a^3)}{(b^4*(a + b*x)^{(1/3)})} - \frac{(9*a*(a + b*x)^{(5/3)})}{(5*b^4)}$

sympy [B] time = 2.89, size = 1538, normalized size = 21.97

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(b*x+a)**(4/3),x)

[Out] $243*a**(68/3)*(1 + b*x/a)**(2/3)/(40*a**20*b**4 + 240*a**19*b**5*x + 600*a**18*b**6*x**2 + 800*a**17*b**7*x**3 + 600*a**16*b**8*x**4 + 240*a**15*b**9*x**5 + 40*a**14*b**10*x**6) - 243*a**(68/3)/(40*a**20*b**4 + 240*a**19*b**5*x + 600*a**18*b**6*x**2 + 800*a**17*b**7*x**3 + 600*a**16*b**8*x**4 + 240*a**15*b**9*x**5 + 40*a**14*b**10*x**6) + 1296*a**(65/3)*b*x*(1 + b*x/a)**(2/3)/(40*a**20*b**4 + 240*a**19*b**5*x + 600*a**18*b**6*x**2 + 800*a**17*b**7*x**3 + 600*a**16*b**8*x**4 + 240*a**15*b**9*x**5 + 40*a**14*b**10*x**6) - 1458*a**(65/3)*b*x/(40*a**20*b**4 + 240*a**19*b**5*x + 600*a**18*b**6*x**2 + 800*a**17*b**7*x**3 + 600*a**16*b**8*x**4 + 240*a**15*b**9*x**5 + 40*a**14*b**10*x**6) + 2808*a**(62/3)*b**2*x**2*(1 + b*x/a)**(2/3)/(40*a**20*b**4 + 240*a**19*b**5*x + 600*a**18*b**6*x**2 + 800*a**17*b**7*x**3 + 600*a**16*b**8*x**4 + 240*a**15*b**9*x**5 + 40*a**14*b**10*x**6) - 3645*a**(62/3)*b**2*x**2/(40*a**20*b**4 + 240*a**19*b**5*x + 600*a**18*b**6*x**2 + 800*a**17*b**7*x**3 + 600*a**16*b**8*x**4 + 240*a**15*b**9*x**5 + 40*a**14*b**10*x**6) + 3120*a**(59/3)*b**3*x**3*(1 + b*x/a)**(2/3)/(40*a**20*b**4 + 240*a**19*b**5*x + 600*a**18*b**6*x**2 + 800*a**17*b**7*x**3 + 600*a**16*b**8*x**4 + 240*a**15*b**9*x**5 + 40*a**14*b**10*x**6) - 4860*a**(59/3)*b**3*x**3/(40*a**20*b**4 + 240*a**19*b**5*x + 600*a**18*b**6*x**2 + 800*a**17*b**7*x**3 + 600*a**16*b**8*x**4 + 240*a**15*b**9*x**5 + 40*a**14*b**10*x**6) + 1830*a**18*b**6*x**2/(40*a**20*b**4 + 240*a**19*b**5*x + 600*a**18*b**6*x**2 + 800*a**17*b**7*x**3 + 600*a**16*b**8*x**4 + 240*a**15*b**9*x**5 + 40*a**14*b**10*x**6)$

$$\begin{aligned}
& * (56/3) * b^{**4} * x^{**4} * (1 + b*x/a)^{(2/3)} / (40*a^{**20}*b^{**4} + 240*a^{**19}*b^{**5}*x + 600*a^{**18}*b^{**6}*x^{**2} + 800*a^{**17}*b^{**7}*x^{**3} + 600*a^{**16}*b^{**8}*x^{**4} + 240*a^{**15}*b^{**9}*x^{**5} + 40*a^{**14}*b^{**10}*x^{**6}) - 3645*a^{**20}*(56/3)*b^{**4}*x^{**4} / (40*a^{**20}*b^{**4} + 240*a^{**19}*b^{**5}*x + 600*a^{**18}*b^{**6}*x^{**2} + 800*a^{**17}*b^{**7}*x^{**3} + 600*a^{**16}*b^{**8}*x^{**4} + 240*a^{**15}*b^{**9}*x^{**5} + 40*a^{**14}*b^{**10}*x^{**6}) + 528*a^{**20}*(53/3)*b^{**5}*x^{**5} * (1 + b*x/a)^{(2/3)} / (40*a^{**20}*b^{**4} + 240*a^{**19}*b^{**5}*x + 600*a^{**18}*b^{**6}*x^{**2} + 800*a^{**17}*b^{**7}*x^{**3} + 600*a^{**16}*b^{**8}*x^{**4} + 240*a^{**15}*b^{**9}*x^{**5} + 40*a^{**14}*b^{**10}*x^{**6}) - 1458*a^{**20}*(53/3)*b^{**5}*x^{**5} / (40*a^{**20}*b^{**4} + 240*a^{**19}*b^{**5}*x + 600*a^{**18}*b^{**6}*x^{**2} + 800*a^{**17}*b^{**7}*x^{**3} + 600*a^{**16}*b^{**8}*x^{**4} + 240*a^{**15}*b^{**9}*x^{**5} + 40*a^{**14}*b^{**10}*x^{**6}) + 96*a^{**20}*(50/3)*b^{**6}*x^{**6} * (1 + b*x/a)^{(2/3)} / (40*a^{**20}*b^{**4} + 240*a^{**19}*b^{**5}*x + 600*a^{**18}*b^{**6}*x^{**2} + 800*a^{**17}*b^{**7}*x^{**3} + 600*a^{**16}*b^{**8}*x^{**4} + 240*a^{**15}*b^{**9}*x^{**5} + 40*a^{**14}*b^{**10}*x^{**6}) - 243*a^{**20}*(50/3)*b^{**6}*x^{**6} / (40*a^{**20}*b^{**4} + 240*a^{**19}*b^{**5}*x + 600*a^{**18}*b^{**6}*x^{**2} + 800*a^{**17}*b^{**7}*x^{**3} + 600*a^{**16}*b^{**8}*x^{**4} + 240*a^{**15}*b^{**9}*x^{**5} + 40*a^{**14}*b^{**10}*x^{**6}) + 48*a^{**20}*(47/3)*b^{**7}*x^{**7} * (1 + b*x/a)^{(2/3)} / (40*a^{**20}*b^{**4} + 240*a^{**19}*b^{**5}*x + 600*a^{**18}*b^{**6}*x^{**2} + 800*a^{**17}*b^{**7}*x^{**3} + 600*a^{**16}*b^{**8}*x^{**4} + 240*a^{**15}*b^{**9}*x^{**5} + 40*a^{**14}*b^{**10}*x^{**6}) + 15*a^{**20}*(44/3)*b^{**8}*x^{**8} * (1 + b*x/a)^{(2/3)} / (40*a^{**20}*b^{**4} + 240*a^{**19}*b^{**5}*x + 600*a^{**18}*b^{**6}*x^{**2} + 800*a^{**17}*b^{**7}*x^{**3} + 600*a^{**16}*b^{**8}*x^{**4} + 240*a^{**15}*b^{**9}*x^{**5} + 40*a^{**14}*b^{**10}*x^{**6})
\end{aligned}$$

$$3.414 \quad \int \frac{x^2}{(a+bx)^{4/3}} dx$$

Optimal. Leaf size=49

$$-\frac{3a^2}{b^3\sqrt[3]{a+bx}} - \frac{3a(a+bx)^{2/3}}{b^3} + \frac{3(a+bx)^{5/3}}{5b^3}$$

[Out] $-3*a^2/b^3/(b*x+a)^{(1/3)}-3*a*(b*x+a)^{(2/3)}/b^3+3/5*(b*x+a)^{(5/3)}/b^3$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{3a^2}{b^3\sqrt[3]{a+bx}} - \frac{3a(a+bx)^{2/3}}{b^3} + \frac{3(a+bx)^{5/3}}{5b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*x)^(4/3), x]

[Out] $(-3*a^2)/(b^3*(a + b*x)^{(1/3)}) - (3*a*(a + b*x)^{(2/3)})/b^3 + (3*(a + b*x)^{(5/3)})/(5*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(a+bx)^{4/3}} dx &= \int \left(\frac{a^2}{b^2(a+bx)^{4/3}} - \frac{2a}{b^2\sqrt[3]{a+bx}} + \frac{(a+bx)^{2/3}}{b^2} \right) dx \\ &= -\frac{3a^2}{b^3\sqrt[3]{a+bx}} - \frac{3a(a+bx)^{2/3}}{b^3} + \frac{3(a+bx)^{5/3}}{5b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 34, normalized size = 0.69

$$\frac{3(-9a^2 - 3abx + b^2x^2)}{5b^3\sqrt[3]{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*x)^(4/3), x]

[Out] (3*(-9*a^2 - 3*a*b*x + b^2*x^2))/(5*b^3*(a + b*x)^(1/3))

fricas [A] time = 0.42, size = 40, normalized size = 0.82

$$\frac{3(b^2x^2 - 3abx - 9a^2)(bx + a)^{\frac{2}{3}}}{5(b^4x + ab^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(4/3), x, algorithm="fricas")

[Out] 3/5*(b^2*x^2 - 3*a*b*x - 9*a^2)*(b*x + a)^(2/3)/(b^4*x + a*b^3)

giac [A] time = 1.00, size = 46, normalized size = 0.94

$$-\frac{3a^2}{(bx+a)^{\frac{1}{3}}b^3} + \frac{3\left((bx+a)^{\frac{5}{3}}b^{12} - 5(bx+a)^{\frac{2}{3}}ab^{12}\right)}{5b^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(4/3), x, algorithm="giac")

[Out] -3*a^2/((b*x + a)^(1/3)*b^3) + 3/5*((b*x + a)^(5/3)*b^12 - 5*(b*x + a)^(2/3)*a*b^12)/b^15

maple [A] time = 0.01, size = 32, normalized size = 0.65

$$-\frac{3(-b^2x^2 + 3abx + 9a^2)}{5(bx+a)^{\frac{1}{3}}b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(b*x+a)^(4/3), x)

[Out] -3/5/(b*x+a)^(1/3)*(-b^2*x^2+3*a*b*x+9*a^2)/b^3

maxima [A] time = 1.33, size = 41, normalized size = 0.84

$$\frac{3(bx+a)^{\frac{5}{3}}}{5b^3} - \frac{3(bx+a)^{\frac{2}{3}}a}{b^3} - \frac{3a^2}{(bx+a)^{\frac{1}{3}}b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^(4/3),x, algorithm="maxima")

[Out] $3/5*(b*x + a)^{(5/3)}/b^3 - 3*(b*x + a)^{(2/3)}*a/b^3 - 3*a^2/((b*x + a)^{(1/3)}*b^3)$

mupad [B] time = 0.04, size = 35, normalized size = 0.71

$$\frac{15 a (a + b x) - 3 (a + b x)^2 + 15 a^2}{5 b^3 (a + b x)^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(a + b*x)^(4/3),x)

[Out] $-(15*a*(a + b*x) - 3*(a + b*x)^2 + 15*a^2)/(5*b^3*(a + b*x)^{(1/3)})$

sympy [B] time = 1.88, size = 534, normalized size = 10.90

$$\frac{27a^{\frac{29}{3}} \left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{5a^8b^3 + 15a^7b^4x + 15a^6b^5x^2 + 5a^5b^6x^3} + \frac{27a^{\frac{29}{3}}}{5a^8b^3 + 15a^7b^4x + 15a^6b^5x^2 + 5a^5b^6x^3} - \frac{63a^{\frac{26}{3}}bx \left(1 + \frac{bx}{a}\right)^{\frac{2}{3}}}{5a^8b^3 + 15a^7b^4x + 15a^6b^5x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(b*x+a)**(4/3),x)

[Out] $-27*a**(29/3)*(1 + b*x/a)**(2/3)/(5*a**8*b**3 + 15*a**7*b**4*x + 15*a**6*b**5*x**2 + 5*a**5*b**6*x**3) + 27*a**(29/3)/(5*a**8*b**3 + 15*a**7*b**4*x + 15*a**6*b**5*x**2 + 5*a**5*b**6*x**3) - 63*a**(26/3)*b*x*(1 + b*x/a)**(2/3)/(5*a**8*b**3 + 15*a**7*b**4*x + 15*a**6*b**5*x**2 + 5*a**5*b**6*x**3) + 81*a**(26/3)*b*x/(5*a**8*b**3 + 15*a**7*b**4*x + 15*a**6*b**5*x**2 + 5*a**5*b**6*x**3) - 42*a**(23/3)*b**2*x**2*(1 + b*x/a)**(2/3)/(5*a**8*b**3 + 15*a**7*b**4*x + 15*a**6*b**5*x**2 + 5*a**5*b**6*x**3) + 81*a**(23/3)*b**2*x**2/(5*a**8*b**3 + 15*a**7*b**4*x + 15*a**6*b**5*x**2 + 5*a**5*b**6*x**3) - 3*a***(20/3)*b**3*x**3*(1 + b*x/a)**(2/3)/(5*a**8*b**3 + 15*a**7*b**4*x + 15*a**6*b**5*x**2 + 5*a**5*b**6*x**3) + 27*a**(20/3)*b**3*x**3/(5*a**8*b**3 + 15*a**7*b**4*x + 15*a**6*b**5*x**2 + 5*a**5*b**6*x**3) + 3*a***(17/3)*b**4*x**4*(1 + b*x/a)**(2/3)/(5*a**8*b**3 + 15*a**7*b**4*x + 15*a**6*b**5*x**2 + 5*a**5*b**6*x**3)$

$$3.415 \quad \int \frac{x}{(a+bx)^{4/3}} dx$$

Optimal. Leaf size=32

$$\frac{3a}{b^2 \sqrt[3]{a+bx}} + \frac{3(a+bx)^{2/3}}{2b^2}$$

[Out] $3*a/b^2/(b*x+a)^{(1/3)}+3/2*(b*x+a)^{(2/3)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3a}{b^2 \sqrt[3]{a+bx}} + \frac{3(a+bx)^{2/3}}{2b^2}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*x)^(4/3), x]

[Out] (3*a)/(b^2*(a + b*x)^(1/3)) + (3*(a + b*x)^(2/3))/(2*b^2)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x}{(a+bx)^{4/3}} dx &= \int \left(-\frac{a}{b(a+bx)^{4/3}} + \frac{1}{b\sqrt[3]{a+bx}} \right) dx \\ &= \frac{3a}{b^2 \sqrt[3]{a+bx}} + \frac{3(a+bx)^{2/3}}{2b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.72

$$\frac{3(3a+bx)}{2b^2 \sqrt[3]{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*x)^(4/3), x]

[Out] $(3*(3*a + b*x))/(2*b^2*(a + b*x)^(1/3))$

fricas [A] time = 0.53, size = 29, normalized size = 0.91

$$\frac{3 (bx + 3a)(bx + a)^{\frac{2}{3}}}{2 (b^3x + ab^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(4/3),x, algorithm="fricas")`

[Out] $3/2*(b*x + 3*a)*(b*x + a)^(2/3)/(b^3*x + a*b^2)$

giac [A] time = 0.93, size = 30, normalized size = 0.94

$$\frac{3 \left(\frac{(bx+a)^{\frac{2}{3}}}{b} + \frac{2a}{(bx+a)^{\frac{1}{3}}b} \right)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(4/3),x, algorithm="giac")`

[Out] $3/2*((b*x + a)^(2/3)/b + 2*a/((b*x + a)^(1/3)*b))/b$

maple [A] time = 0.00, size = 20, normalized size = 0.62

$$\frac{\frac{3bx}{2} + \frac{9a}{2}}{(bx + a)^{\frac{1}{3}} b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(b*x+a)^(4/3),x)`

[Out] $3/2/(b*x+a)^(1/3)*(b*x+3*a)/b^2$

maxima [A] time = 1.30, size = 26, normalized size = 0.81

$$\frac{3 (bx + a)^{\frac{2}{3}}}{2 b^2} + \frac{3 a}{(bx + a)^{\frac{1}{3}} b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)^(4/3),x, algorithm="maxima")`

[Out] $3/2*(b*x + a)^{(2/3)}/b^2 + 3*a/((b*x + a)^{(1/3)}*b^2)$

mupad [B] time = 0.03, size = 20, normalized size = 0.62

$$\frac{9a + 3bx}{2b^2(a + bx)^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a + b*x)^(4/3), x)`

[Out] $(9*a + 3*b*x)/(2*b^2*(a + b*x)^{(1/3)})$

sympy [A] time = 0.72, size = 41, normalized size = 1.28

$$\begin{cases} \frac{9a}{2b^2\sqrt[3]{a+bx}} + \frac{3x}{2b\sqrt[3]{a+bx}} & \text{for } b \neq 0 \\ \frac{x^2}{2a^{3/4}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(b*x+a)**(4/3), x)`

[Out] `Piecewise((9*a/(2*b**2*(a + b*x)**(1/3)) + 3*x/(2*b*(a + b*x)**(1/3)), Ne(b, 0)), (x**2/(2*a**(4/3)), True))`

$$3.416 \quad \int \frac{1}{(a+bx)^{4/3}} dx$$

Optimal. Leaf size=14

$$-\frac{3}{b\sqrt[3]{a+bx}}$$

[Out] -3/b/(b*x+a)^(1/3)

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$-\frac{3}{b\sqrt[3]{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-4/3), x]

[Out] -3/(b*(a + b*x)^(1/3))

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^{4/3}} dx = -\frac{3}{b\sqrt[3]{a+bx}}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\frac{3}{b\sqrt[3]{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-4/3), x]

[Out] -3/(b*(a + b*x)^(1/3))

fricas [A] time = 0.43, size = 20, normalized size = 1.43

$$-\frac{3(bx+a)^{\frac{2}{3}}}{b^2x+ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(4/3),x, algorithm="fricas")

[Out] -3*(b*x + a)^(2/3)/(b^2*x + a*b)

giac [A] time = 0.76, size = 12, normalized size = 0.86

$$-\frac{3}{(bx + a)^{\frac{1}{3}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(4/3),x, algorithm="giac")

[Out] -3/((b*x + a)^(1/3)*b)

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$-\frac{3}{(bx + a)^{\frac{1}{3}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(4/3),x)

[Out] -3/b/(b*x+a)^(1/3)

maxima [A] time = 1.35, size = 12, normalized size = 0.86

$$-\frac{3}{(bx + a)^{\frac{1}{3}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(4/3),x, algorithm="maxima")

[Out] -3/((b*x + a)^(1/3)*b)

mupad [B] time = 0.02, size = 12, normalized size = 0.86

$$-\frac{3}{b(a + bx)^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x)^(4/3),x)

[Out] $-3/(b*(a + b*x)^{(1/3)})$

sympy [A] time = 0.07, size = 12, normalized size = 0.86

$$-\frac{3}{b\sqrt[3]{a + bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(4/3),x)`

[Out] $-3/(b*(a + b*x)**(1/3))$

$$3.417 \quad \int \frac{1}{x(a+bx)^{4/3}} dx$$

Optimal. Leaf size=93

$$\frac{3 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{4/3}} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{a^{4/3}} - \frac{\log(x)}{2a^{4/3}} + \frac{3}{a\sqrt[3]{a+bx}}$$

[Out] 3/a/(b*x+a)^(1/3)-1/2*ln(x)/a^(4/3)+3/2*ln(a^(1/3)-(b*x+a)^(1/3))/a^(4/3)+arctan(1/3*(a^(1/3)+2*(b*x+a)^(1/3))/a^(1/3)*3^(1/2))*3^(1/2)/a^(4/3)

Rubi [A] time = 0.03, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 55, 617, 204, 31}

$$\frac{3 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{2a^{4/3}} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{a^{4/3}} - \frac{\log(x)}{2a^{4/3}} + \frac{3}{a\sqrt[3]{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a + b*x)^(4/3)),x]

[Out] 3/(a*(a + b*x)^(1/3)) + (Sqrt[3]*ArcTan[(a^(1/3) + 2*(a + b*x)^(1/3))/(Sqrt[3]*a^(1/3))])/a^(4/3) - Log[x]/(2*a^(4/3)) + (3*Log[a^(1/3) - (a + b*x)^(1/3)])/(2*a^(4/3))

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 55

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x]

```
] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)],
x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])) /;
FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])) /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x(a+bx)^{4/3}} dx &= \frac{3}{a\sqrt[3]{a+bx}} + \frac{\int \frac{1}{x\sqrt[3]{a+bx}} dx}{a} \\
 &= \frac{3}{a\sqrt[3]{a+bx}} - \frac{\log(x)}{2a^{4/3}} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a}-x} dx, x, \sqrt[3]{a+bx}\right)}{2a^{4/3}} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{a^{2/3}+\sqrt[3]{a}x+x^2} dx, x, \sqrt[3]{a+bx}\right)}{2a} \\
 &= \frac{3}{a\sqrt[3]{a+bx}} - \frac{\log(x)}{2a^{4/3}} + \frac{3 \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)}{2a^{4/3}} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}\right)}{a^{4/3}} \\
 &= \frac{3}{a\sqrt[3]{a+bx}} + \frac{\sqrt{3} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{a^{4/3}} - \frac{\log(x)}{2a^{4/3}} + \frac{3 \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)}{2a^{4/3}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.32

$$\frac{{}_3F_1\left(-\frac{1}{3}, 1; \frac{2}{3}; \frac{bx}{a} + 1\right)}{a\sqrt[3]{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a + b*x)^(4/3)),x]

[Out] (3*Hypergeometric2F1[-1/3, 1, 2/3, 1 + (b*x)/a])/(a*(a + b*x)^(1/3))

fricas [A] time = 0.45, size = 285, normalized size = 3.06

$$\frac{\sqrt{3}(abx + a^2)\sqrt{-\frac{1}{a^3}} \log\left(\frac{2bx + \sqrt{3}\left(2(bx+a)^{\frac{2}{3}}a^{\frac{2}{3}} - (bx+a)^{\frac{1}{3}}a - a^{\frac{4}{3}}\right)\sqrt{-\frac{1}{a^3}} - 3(bx+a)^{\frac{1}{3}}a^{\frac{2}{3}} + 3a}{x}}{\right) - (bx+a)a^{\frac{2}{3}} \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{2(a^2bx + a^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(4/3),x, algorithm="fricas")

[Out] [1/2*(sqrt(3)*(a*b*x + a^2)*sqrt(-1/a^(2/3))*log((2*b*x + sqrt(3)*(2*(b*x + a)^(2/3)*a^(2/3) - (b*x + a)^(1/3)*a - a^(4/3))*sqrt(-1/a^(2/3)) - 3*(b*x + a)^(1/3)*a^(2/3) + 3*a)/x) - (b*x + a)*a^(2/3)*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + 2*(b*x + a)*a^(2/3)*log((b*x + a)^(1/3) - a^(1/3)) + 6*(b*x + a)^(2/3)*a/(a^2*b*x + a^3), -1/2*((b*x + a)*a^(2/3)*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) - 2*(b*x + a)*a^(2/3)*log((b*x + a)^(1/3) - a^(1/3)) - 2*sqrt(3)*(a*b*x + a^2)*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3))/a^(1/3) - 6*(b*x + a)^(2/3)*a/(a^2*b*x + a^3)]

giac [A] time = 2.38, size = 89, normalized size = 0.96

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{a^{\frac{4}{3}}} - \frac{\log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{2a^{\frac{4}{3}}} + \frac{\log\left(\left|(bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right)}{a^{\frac{4}{3}}} + \frac{3}{(bx+a)^{\frac{1}{3}}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(4/3),x, algorithm="giac")

[Out] sqrt(3)*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3))/a^(4/3) - 1/2*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(4/3) + log(abs((b*x + a)^(1/3) - a^(1/3)))/a^(4/3) + 3/((b*x + a)^(1/3)*a)

maple [A] time = 0.01, size = 87, normalized size = 0.94

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)}{a^{\frac{4}{3}}} + \frac{\ln\left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}\right)}{a^{\frac{4}{3}}} - \frac{\ln\left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}}\right)}{2a^{\frac{4}{3}}} + \frac{3}{(bx+a)^{\frac{1}{3}}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a)^(4/3),x)

[Out] 3/a/(b*x+a)^(1/3)+1/a^(4/3)*ln(-a^(1/3)+(b*x+a)^(1/3))-1/2/a^(4/3)*ln(a^(2/3)+(b*x+a)^(1/3)*a^(1/3)+(b*x+a)^(2/3))+1/a^(4/3)*3^(1/2)*arctan(1/3*3^(1/2)*(2*(b*x+a)^(1/3)/a^(1/3)+1))

maxima [A] time = 3.03, size = 88, normalized size = 0.95

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{a^{\frac{4}{3}}} - \frac{\log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{2a^{\frac{4}{3}}} + \frac{\log\left((bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right)}{a^{\frac{4}{3}}} + \frac{3}{(bx+a)^{\frac{1}{3}}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^(4/3),x, algorithm="maxima")

[Out] sqrt(3)*arctan(1/3*sqrt(3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3))/a^(4/3) - 1/2*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3))/a^(4/3) + log((b*x + a)^(1/3) - a^(1/3))/a^(4/3) + 3/((b*x + a)^(1/3)*a)

mupad [B] time = 0.06, size = 114, normalized size = 1.23

$$\frac{\ln\left(9a(a+bx)^{1/3} - 9a^{4/3}\right)}{a^{4/3}} + \frac{3}{a(a+bx)^{1/3}} + \frac{\ln\left(9a(a+bx)^{1/3} - \frac{9a^{4/3}(-1+\sqrt{3}i)^2}{4}\right)}{2a^{4/3}} - \frac{\ln\left(9a(a+bx)^{1/3} - (9a^{4/3})(3^{1/2}i - 1)^2/4\right)}{2a^{4/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(a + b*x)^(4/3)),x)

[Out] log(9*a*(a + b*x)^(1/3) - 9*a^(4/3))/a^(4/3) + 3/(a*(a + b*x)^(1/3)) + (log(9*a*(a + b*x)^(1/3) - (9*a^(4/3)*(3^(1/2)*1i - 1)^2)/4)/(3^(1/2)*1i - 1)/

$$(2*a^{(4/3)}) - (\log(9*a*(a + b*x)^{(1/3)} - (9*a^{(4/3)}*(3^{(1/2)}*1i + 1)^2)/4)*(3^{(1/2)}*1i + 1))/(2*a^{(4/3)})$$

sympy [C] time = 2.21, size = 184, normalized size = 1.98

$$\frac{\Gamma\left(-\frac{1}{3}\right) \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x}}{\sqrt[3]{a}}\right) \Gamma\left(-\frac{1}{3}\right) e^{\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x} e^{\frac{2i\pi}{3}}}{\sqrt[3]{a}}\right) \Gamma\left(-\frac{1}{3}\right) e^{-\frac{2i\pi}{3}} \log\left(1 - \frac{\sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x} e^{\frac{4i\pi}{3}}}{\sqrt[3]{a}}\right) \Gamma\left(-\frac{1}{3}\right)}{a \sqrt[3]{b} \sqrt[3]{\frac{a}{b} + x} \Gamma\left(\frac{2}{3}\right) - 3a^{\frac{4}{3}} \Gamma\left(\frac{2}{3}\right) - 3a^{\frac{4}{3}} \Gamma\left(\frac{2}{3}\right) - 3a^{\frac{4}{3}} \Gamma\left(\frac{2}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)**(4/3),x)

[Out] -gamma(-1/3)/(a*b**(1/3)*(a/b + x)**(1/3)*gamma(2/3)) - log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(-1/3)/(3*a**(4/3)*gamma(2/3)) - exp(2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(2*I*pi/3)/a**(1/3))*gamma(-1/3)/(3*a**(4/3)*gamma(2/3)) - exp(-2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(4*I*pi/3)/a**(1/3))*gamma(-1/3)/(3*a**(4/3)*gamma(2/3))

$$3.418 \quad \int \frac{1}{x^2(a+bx)^{4/3}} dx$$

Optimal. Leaf size=113

$$\frac{2b \log(x)}{3a^{7/3}} - \frac{2b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{a^{7/3}} - \frac{4b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{7/3}} - \frac{4b}{a^2\sqrt[3]{a+bx}} - \frac{1}{ax\sqrt[3]{a+bx}}$$

[Out] $-4*b/a^2/(b*x+a)^{(1/3)}-1/a/x/(b*x+a)^{(1/3)}+2/3*b*\ln(x)/a^{(7/3)}-2*b*\ln(a^{(1/3)}-(b*x+a)^{(1/3)})/a^{(7/3)}-4/3*b*\arctan(1/3*(a^{(1/3)}+2*(b*x+a)^{(1/3)})/a^{(1/3)}*3^{(1/2)})/a^{(7/3)}*3^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 115, normalized size of antiderivative = 1.02, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 55, 617, 204, 31}

$$-\frac{4(a+bx)^{2/3}}{a^2x} + \frac{2b \log(x)}{3a^{7/3}} - \frac{2b \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{a^{7/3}} - \frac{4b \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{7/3}} + \frac{3}{ax\sqrt[3]{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*(a + b*x)^(4/3)), x]

[Out] $3/(a*x*(a + b*x)^{(1/3)}) - (4*(a + b*x)^{(2/3)})/(a^2*x) - (4*b*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})]) / (\text{Sqrt}[3]*a^{(7/3)}) + (2*b*\text{Log}[x]) / (3*a^{(7/3)}) - (2*b*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}]) / a^{(7/3)}$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 55

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x
] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)],
x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])] /;
FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^2(a+bx)^{4/3}} dx &= \frac{3}{ax\sqrt[3]{a+bx}} + \frac{4 \int \frac{1}{x^2\sqrt[3]{a+bx}} dx}{a} \\
&= \frac{3}{ax\sqrt[3]{a+bx}} - \frac{4(a+bx)^{2/3}}{a^2x} - \frac{(4b) \int \frac{1}{x\sqrt[3]{a+bx}} dx}{3a^2} \\
&= \frac{3}{ax\sqrt[3]{a+bx}} - \frac{4(a+bx)^{2/3}}{a^2x} + \frac{2b \log(x)}{3a^{7/3}} + \frac{(2b) \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{a^{7/3}} - \frac{(2b) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{a+bx}\right)}{a^{7/3}} \\
&= \frac{3}{ax\sqrt[3]{a+bx}} - \frac{4(a+bx)^{2/3}}{a^2x} + \frac{2b \log(x)}{3a^{7/3}} - \frac{2b \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)}{a^{7/3}} + \frac{(4b) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{a+bx}\right)}{a^{7/3}} \\
&= \frac{3}{ax\sqrt[3]{a+bx}} - \frac{4(a+bx)^{2/3}}{a^2x} - \frac{4b \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3}a^{7/3}} + \frac{2b \log(x)}{3a^{7/3}} - \frac{2b \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)}{a^{7/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 31, normalized size = 0.27

$$\frac{3b {}_2F_1\left(-\frac{1}{3}, 2; \frac{2}{3}; \frac{bx}{a} + 1\right)}{a^2 \sqrt[3]{a + bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*(a + b*x)^(4/3)),x]

[Out] (-3*b*Hypergeometric2F1[-1/3, 2, 2/3, 1 + (b*x)/a])/(a^2*(a + b*x)^(1/3))

fricas [B] time = 0.59, size = 407, normalized size = 3.60

$$\left[6 \sqrt{\frac{1}{3}} (ab^2x^2 + a^2bx) \sqrt{\frac{(-a)^{\frac{1}{3}}}{a}} \log \left(\frac{2bx - 3 \sqrt{\frac{1}{3}} \left(2(bx+a)^{\frac{2}{3}} (-a)^{\frac{2}{3}} - (bx+a)^{\frac{1}{3}} a + (-a)^{\frac{1}{3}} a \right) \sqrt{\frac{(-a)^{\frac{1}{3}}}{a}} - 3(bx+a)^{\frac{1}{3}} (-a)^{\frac{2}{3}} + 3a}{x} \right) + 2(b^2x^2 + abx) \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(4/3),x, algorithm="fricas")

[Out] [1/3*(6*sqrt(1/3)*(a*b^2*x^2 + a^2*b*x)*sqrt((-a)^(1/3)/a)*log((2*b*x - 3*sqrt(1/3)*(2*(b*x + a)^(2/3)*(-a)^(2/3) - (b*x + a)^(1/3)*a + (-a)^(1/3)*a)*sqrt((-a)^(1/3)/a) - 3*(b*x + a)^(1/3)*(-a)^(2/3) + 3*a)/x) + 2*(b^2*x^2 + a*b*x)*(-a)^(2/3)*log((b*x + a)^(2/3) - (b*x + a)^(1/3)*(-a)^(1/3) + (-a)^(2/3)) - 4*(b^2*x^2 + a*b*x)*(-a)^(2/3)*log((b*x + a)^(1/3) + (-a)^(1/3)) - 3*(4*a*b*x + a^2)*(b*x + a)^(2/3))/(a^3*b*x^2 + a^4*x), -1/3*(12*sqrt(1/3)*(a*b^2*x^2 + a^2*b*x)*sqrt(-(-a)^(1/3)/a)*arctan(sqrt(1/3)*(2*(b*x + a)^(1/3) - (-a)^(1/3))*sqrt(-(-a)^(1/3)/a)) - 2*(b^2*x^2 + a*b*x)*(-a)^(2/3)*log((b*x + a)^(2/3) - (b*x + a)^(1/3)*(-a)^(1/3) + (-a)^(2/3)) + 4*(b^2*x^2 + a*b*x)*(-a)^(2/3)*log((b*x + a)^(1/3) + (-a)^(1/3)) + 3*(4*a*b*x + a^2)*(b*x + a)^(2/3))/(a^3*b*x^2 + a^4*x)]

giac [A] time = 2.40, size = 120, normalized size = 1.06

$$\frac{4 \sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{3a^{\frac{7}{3}}} + \frac{2b \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{3a^{\frac{7}{3}}} - \frac{4b \log\left(\left|(bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right)}{3a^{\frac{7}{3}}} - \frac{4\left(\left|(bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right)}{\left((bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(4/3),x, algorithm="giac")

[Out]
$$-4/3*\sqrt{3}*b*\arctan(1/3*\sqrt{3}*(2*(b*x + a)^{1/3} + a^{1/3})/a^{1/3})/a^{7/3} + 2/3*b*\log((b*x + a)^{2/3} + (b*x + a)^{1/3}*a^{1/3} + a^{2/3})/a^{7/3} - 4/3*b*\log(\text{abs}((b*x + a)^{1/3} - a^{1/3}))/a^{7/3} - (4*(b*x + a)*b - 3*a*b)/(((b*x + a)^{4/3} - (b*x + a)^{1/3}*a)*a^2)$$

maple [A] time = 0.01, size = 108, normalized size = 0.96

$$\frac{4\sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)}{3a^{\frac{7}{3}}} - \frac{4b \ln\left(-a^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}\right)}{3a^{\frac{7}{3}}} + \frac{2b \ln\left(a^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}} a^{\frac{1}{3}} + (bx+a)^{\frac{2}{3}}\right)}{3a^{\frac{7}{3}}} - \frac{3b}{(bx+a)^{\frac{1}{3}} a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^(4/3),x)

[Out]
$$-3*b/a^{2/3}/(b*x+a)^{1/3}-1/a^{2/3}*(b*x+a)^{2/3}/x-4/3*b/a^{7/3}*\ln(-a^{1/3}+(b*x+a)^{1/3})+2/3*b/a^{7/3}*\ln(a^{2/3}+(b*x+a)^{1/3}*a^{1/3}+(b*x+a)^{2/3})-4/3*b/a^{7/3}*3^{1/2}*\arctan(1/3*3^{1/2}*(2*(b*x+a)^{1/3}/a^{1/3}+1))$$

maxima [A] time = 2.99, size = 122, normalized size = 1.08

$$\frac{4\sqrt{3} b \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{3a^{\frac{7}{3}}} - \frac{4(bx+a)b - 3ab}{(bx+a)^{\frac{4}{3}}a^2 - (bx+a)^{\frac{1}{3}}a^3} + \frac{2b \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{3a^{\frac{7}{3}}} - \frac{4b \log\left(\dots\right)}{3a^{\frac{7}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^(4/3),x, algorithm="maxima")

[Out]
$$-4/3*\sqrt{3}*b*\arctan(1/3*\sqrt{3}*(2*(b*x + a)^{1/3} + a^{1/3})/a^{1/3})/a^{7/3} - (4*(b*x + a)*b - 3*a*b)/((b*x + a)^{4/3}*a^2 - (b*x + a)^{1/3}*a^3) + 2/3*b*\log((b*x + a)^{2/3} + (b*x + a)^{1/3}*a^{1/3} + a^{2/3})/a^{7/3} - 4/3*b*\log((b*x + a)^{1/3} - a^{1/3})/a^{7/3}$$

mupad [B] time = 0.07, size = 173, normalized size = 1.53

$$\frac{\frac{3b}{a} - \frac{4b(a+bx)}{a^2}}{a(a+bx)^{1/3} - (a+bx)^{4/3}} + \frac{\ln\left(a^{7/3}\left(2b - \sqrt{3} b 2i\right)^2 - 16a^2 b^2 (a+bx)^{1/3}\right) (2b - \sqrt{3} b 2i)}{3a^{7/3}} + \frac{\ln\left(a^{7/3}\left(2b + \sqrt{3} b 2i\right)^2 - 16a^2 b^2 (a+bx)^{1/3}\right) (2b + \sqrt{3} b 2i)}{3a^{7/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(x^2*(a + b*x)^(4/3)),x)
```

```
[Out] (log(a^(7/3)*(2*b - 3^(1/2)*b*2i)^2 - 16*a^2*b^2*(a + b*x)^(1/3))*(2*b - 3^(1/2)*b*2i))/(3*a^(7/3)) - ((3*b)/a - (4*b*(a + b*x))/a^2)/(a*(a + b*x)^(1/3) - (a + b*x)^(4/3)) + (log(a^(7/3)*(2*b + 3^(1/2)*b*2i)^2 - 16*a^2*b^2*(a + b*x)^(1/3))*(2*b + 3^(1/2)*b*2i))/(3*a^(7/3)) - (4*b*log(16*a^(7/3)*b^2 - 16*a^2*b^2*(a + b*x)^(1/3)))/(3*a^(7/3))
```

sympy [C] time = 2.52, size = 857, normalized size = 7.58

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**2/(b*x+a)**(4/3),x)
```

```
[Out] -9*a**(4/3)*b**(2/3)*exp(2*I*pi/3)*gamma(-1/3)/(-9*a**(10/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 9*a**(7/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3)) + 12*a**(1/3)*b**(5/3)*(a/b + x)*exp(2*I*pi/3)*gamma(-1/3)/(-9*a**(10/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 9*a**(7/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3)) - 4*a*b*(a/b + x)**(1/3)*exp(2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(-1/3)/(-9*a**(10/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 9*a**(7/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3)) - 4*a*b*(a/b + x)**(1/3)*exp(-2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(2*I*pi/3)/a**(1/3))*gamma(-1/3)/(-9*a**(10/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 9*a**(7/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3)) - 4*a*b*(a/b + x)**(1/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(4*I*pi/3)/a**(1/3))*gamma(-1/3)/(-9*a**(10/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 9*a**(7/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3)) + 4*b**2*(a/b + x)**(4/3)*exp(2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(-1/3)/(-9*a**(10/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 9*a**(7/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3)) + 4*b**2*(a/b + x)**(4/3)*exp(-2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(2*I*pi/3)/a**(1/3))*gamma(-1/3)/(-9*a**(10/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 9*a**(7/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3)) + 4*b**2*(a/b + x)**(4/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)*exp_polar(4*I*pi/3)/a**(1/3))*gamma(-1/3)/(-9*a**(10/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 9*a**(7/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3))
```

$$3.419 \quad \int \frac{1}{x^3(a+bx)^{4/3}} dx$$

Optimal. Leaf size=149

$$-\frac{7b^2 \log(x)}{9a^{10/3}} + \frac{7b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{3a^{10/3}} + \frac{14b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{10/3}} + \frac{14b^2}{3a^3\sqrt[3]{a+bx}} + \frac{7b}{6a^2x\sqrt[3]{a+bx}} - \frac{1}{2ax^2\sqrt[3]{a+bx}}$$

[Out] $14/3*b^2/a^3/(b*x+a)^{(1/3)} - 1/2/a/x^2/(b*x+a)^{(1/3)} + 7/6*b/a^2/x/(b*x+a)^{(1/3)}$
 $- 7/9*b^2*\ln(x)/a^{(10/3)} + 7/3*b^2*\ln(a^{(1/3)} - (b*x+a)^{(1/3)})/a^{(10/3)} + 14/9*b^2*$
 $2*\arctan(1/3*(a^{(1/3)} + 2*(b*x+a)^{(1/3)})/a^{(1/3)*3^{(1/2)}})/a^{(10/3)*3^{(1/2)}}$

Rubi [A] time = 0.06, antiderivative size = 147, normalized size of antiderivative = 0.99, number of steps used = 7, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 55, 617, 204, 31}

$$-\frac{7b^2 \log(x)}{9a^{10/3}} + \frac{7b^2 \log(\sqrt[3]{a} - \sqrt[3]{a+bx})}{3a^{10/3}} + \frac{14b^2 \tan^{-1}\left(\frac{2\sqrt[3]{a+bx} + \sqrt[3]{a}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{10/3}} - \frac{7(a+bx)^{2/3}}{2a^2x^2} + \frac{14b(a+bx)^{2/3}}{3a^3x} + \frac{3}{ax^2\sqrt[3]{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*(a + b*x)^(4/3)), x]

[Out] $3/(a*x^2*(a + b*x)^{(1/3)}) - (7*(a + b*x)^{(2/3)})/(2*a^2*x^2) + (14*b*(a + b*x)^{(2/3)})/(3*a^3*x) + (14*b^2*\text{ArcTan}[(a^{(1/3)} + 2*(a + b*x)^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/(3*\text{Sqrt}[3]*a^{(10/3)}) - (7*b^2*\text{Log}[x])/(9*a^{(10/3)}) + (7*b^2*\text{Log}[a^{(1/3)} - (a + b*x)^{(1/3)}])/(3*a^{(10/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 55

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x
] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)],
x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])) /;
FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c]) /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^3(a+bx)^{4/3}} dx &= \frac{3}{ax^2\sqrt[3]{a+bx}} + \frac{7 \int \frac{1}{x^3\sqrt[3]{a+bx}} dx}{a} \\
&= \frac{3}{ax^2\sqrt[3]{a+bx}} - \frac{7(a+bx)^{2/3}}{2a^2x^2} - \frac{(14b) \int \frac{1}{x^2\sqrt[3]{a+bx}} dx}{3a^2} \\
&= \frac{3}{ax^2\sqrt[3]{a+bx}} - \frac{7(a+bx)^{2/3}}{2a^2x^2} + \frac{14b(a+bx)^{2/3}}{3a^3x} + \frac{(14b^2) \int \frac{1}{x\sqrt[3]{a+bx}} dx}{9a^3} \\
&= \frac{3}{ax^2\sqrt[3]{a+bx}} - \frac{7(a+bx)^{2/3}}{2a^2x^2} + \frac{14b(a+bx)^{2/3}}{3a^3x} - \frac{7b^2 \log(x)}{9a^{10/3}} - \frac{(7b^2) \text{Subst}\left(\int \frac{1}{\sqrt[3]{a-x}} dx, x, \sqrt[3]{a+bx}\right)}{3a^{10/3}} \\
&= \frac{3}{ax^2\sqrt[3]{a+bx}} - \frac{7(a+bx)^{2/3}}{2a^2x^2} + \frac{14b(a+bx)^{2/3}}{3a^3x} - \frac{7b^2 \log(x)}{9a^{10/3}} + \frac{7b^2 \log\left(\sqrt[3]{a} - \sqrt[3]{a+bx}\right)}{3a^{10/3}} \\
&= \frac{3}{ax^2\sqrt[3]{a+bx}} - \frac{7(a+bx)^{2/3}}{2a^2x^2} + \frac{14b(a+bx)^{2/3}}{3a^3x} + \frac{14b^2 \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a+bx}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{3\sqrt{3}a^{10/3}} - \frac{7b^2 \log(x)}{9a^{10/3}} + \frac{7b^2}{9a^{10/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 33, normalized size = 0.22

$$\frac{3b^2 {}_2F_1\left(-\frac{1}{3}, 3; \frac{2}{3}; \frac{bx}{a} + 1\right)}{a^3 \sqrt[3]{a + bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*(a + b*x)^(4/3)),x]

[Out] (3*b^2*Hypergeometric2F1[-1/3, 3, 2/3, 1 + (b*x)/a])/(a^3*(a + b*x)^(1/3))

fricas [A] time = 0.62, size = 407, normalized size = 2.73

$$\frac{42 \sqrt{\frac{1}{3}} (ab^3x^3 + a^2b^2x^2) \sqrt{-\frac{1}{2} \frac{1}{a^3}} \log\left(\frac{2bx+3 \sqrt{\frac{1}{3}} \left(2(bx+a)^{\frac{2}{3}} a^{\frac{2}{3}} - (bx+a)^{\frac{1}{3}} a - a^{\frac{4}{3}}\right) \sqrt{-\frac{1}{2} \frac{1}{a^3}} - 3(bx+a)^{\frac{1}{3}} a^{\frac{2}{3}} + 3a}}{x}\right) - 14(b^3x^3 + ab^2x^2)a^{\frac{2}{3}}}{18(a^{\frac{2}{3}})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(4/3),x, algorithm="fricas")

[Out] [1/18*(42*sqrt(1/3)*(a*b^3*x^3 + a^2*b^2*x^2)*sqrt(-1/a^(2/3))*log((2*b*x + 3*sqrt(1/3)*(2*(b*x + a)^(2/3)*a^(2/3) - (b*x + a)^(1/3)*a - a^(4/3))*sqrt(-1/a^(2/3)) - 3*(b*x + a)^(1/3)*a^(2/3) + 3*a)/x) - 14*(b^3*x^3 + a*b^2*x^2)*a^(2/3)*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) + 28*(b^3*x^3 + a*b^2*x^2)*a^(2/3)*log((b*x + a)^(1/3) - a^(1/3)) + 3*(28*a*b^2*x^2 + 7*a^2*b*x - 3*a^3)*(b*x + a)^(2/3))/(a^4*b*x^3 + a^5*x^2), -1/18*(14*(b^3*x^3 + a*b^2*x^2)*a^(2/3)*log((b*x + a)^(2/3) + (b*x + a)^(1/3)*a^(1/3) + a^(2/3)) - 28*(b^3*x^3 + a*b^2*x^2)*a^(2/3)*log((b*x + a)^(1/3) - a^(1/3)) - 84*sqrt(1/3)*(a*b^3*x^3 + a^2*b^2*x^2)*arctan(sqrt(1/3)*(2*(b*x + a)^(1/3) + a^(1/3))/a^(1/3))/a^(1/3) - 3*(28*a*b^2*x^2 + 7*a^2*b*x - 3*a^3)*(b*x + a)^(2/3))/(a^4*b*x^3 + a^5*x^2)]

giac [A] time = 2.59, size = 140, normalized size = 0.94

$$\frac{14 \sqrt{3} b^2 \arctan\left(\frac{\sqrt{3}\left(2(bx+a)^{\frac{1}{3}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{9a^{\frac{10}{3}}} - \frac{7b^2 \log\left((bx+a)^{\frac{2}{3}} + (bx+a)^{\frac{1}{3}}a^{\frac{1}{3}} + a^{\frac{2}{3}}\right)}{9a^{\frac{10}{3}}} + \frac{14b^2 \log\left(\left|(bx+a)^{\frac{1}{3}} - a^{\frac{1}{3}}\right|\right)}{9a^{\frac{10}{3}}} + \frac{3}{(bx+a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(4/3),x, algorithm="giac")

[Out] $14/9\sqrt{3}b^2\arctan(1/3\sqrt{3}*(2*(b*x+a)^{1/3}+a^{1/3})/a^{1/3})/a^{10/3}-7/9*b^2*\log((b*x+a)^{2/3}+(b*x+a)^{1/3}*a^{1/3}+a^{2/3})/a^{10/3}+14/9*b^2*\log(\text{abs}((b*x+a)^{1/3}-a^{1/3}))/a^{10/3}+3*b^2/((b*x+a)^{1/3}*a^3)+1/6*(10*(b*x+a)^{5/3}*b^2-13*(b*x+a)^{2/3}*a*b^2)/(a^3*b^2*x^2)$

maple [A] time = 0.01, size = 131, normalized size = 0.88

$$\frac{14\sqrt{3}b^2\arctan\left(\frac{\sqrt{3}\left(\frac{2(bx+a)^{\frac{1}{3}}}{a^{\frac{1}{3}}}+1\right)}{3}\right)}{9a^{\frac{10}{3}}} + \frac{14b^2\ln\left(-a^{\frac{1}{3}}+(bx+a)^{\frac{1}{3}}\right)}{9a^{\frac{10}{3}}} - \frac{7b^2\ln\left(a^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+(bx+a)^{\frac{2}{3}}\right)}{9a^{\frac{10}{3}}} + \frac{3b^2}{(bx+a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a)^(4/3),x)

[Out] $3*b^2/a^3/(b*x+a)^{1/3}+5/3/a^3/x^2*(b*x+a)^{5/3}-13/6/a^2/x^2*(b*x+a)^{2/3}+14/9*b^2/a^{10/3}*\ln(-a^{1/3}+(b*x+a)^{1/3})-7/9*b^2/a^{10/3}*\ln(a^{2/3}+(b*x+a)^{1/3}*a^{1/3}+(b*x+a)^{2/3})+14/9*b^2/a^{10/3}*3^{1/2}*\arctan(1/3*3^{1/2}*(2*(b*x+a)^{1/3}/a^{1/3}+1))$

maxima [A] time = 2.96, size = 158, normalized size = 1.06

$$\frac{14\sqrt{3}b^2\arctan\left(\frac{\sqrt{3}\left(2\frac{(bx+a)^{\frac{1}{3}}}{3a^{\frac{1}{3}}}+a^{\frac{1}{3}}\right)}{3a^{\frac{1}{3}}}\right)}{9a^{\frac{10}{3}}} + \frac{28(bx+a)^2b^2-49(bx+a)ab^2+18a^2b^2}{6\left((bx+a)^{\frac{7}{3}}a^3-2(bx+a)^{\frac{4}{3}}a^4+(bx+a)^{\frac{1}{3}}a^5\right)} - \frac{7b^2\log\left((bx+a)^{\frac{2}{3}}+(bx+a)^{\frac{1}{3}}a^{\frac{1}{3}}+(bx+a)^{\frac{2}{3}}\right)}{9a^{\frac{10}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)^(4/3),x, algorithm="maxima")

[Out] $14/9\sqrt{3}b^2\arctan(1/3\sqrt{3}*(2*(b*x+a)^{1/3}+a^{1/3})/a^{1/3})/a^{10/3}+1/6*(28*(b*x+a)^2*b^2-49*(b*x+a)*a*b^2+18*a^2*b^2)/((b*x+a)^{7/3}*a^3-2*(b*x+a)^{4/3}*a^4+(b*x+a)^{1/3}*a^5)-7/9*b^2*\log((b*x+a)^{2/3}+(b*x+a)^{1/3}*a^{1/3}+a^{2/3})/a^{10/3}+14/9*b^2*\log((b*x+a)^{1/3}-a^{1/3})/a^{10/3}$

mupad [B] time = 0.13, size = 221, normalized size = 1.48

$$\frac{\frac{3b^2}{a} + \frac{14b^2(a+bx)^2}{3a^3} - \frac{49b^2(a+bx)}{6a^2}}{(a+bx)^{7/3} - 2a(a+bx)^{4/3} + a^2(a+bx)^{1/3}} + \frac{\ln\left(588a^3b^4(a+bx)^{1/3} - 3a^{10/3}\left(-7b^2 + \sqrt{3}b^27i\right)^2\right)\left(-7b^2 + \sqrt{3}b^27i\right)}{9a^{10/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(a + b*x)^(4/3)),x)

[Out] ((3*b^2)/a + (14*b^2*(a + b*x)^2)/(3*a^3) - (49*b^2*(a + b*x))/(6*a^2))/((a + b*x)^(7/3) - 2*a*(a + b*x)^(4/3) + a^2*(a + b*x)^(1/3)) + (log(588*a^3*b^4*(a + b*x)^(1/3) - 3*a^(10/3)*(3^(1/2)*b^2*7i - 7*b^2)^2)*(3^(1/2)*b^2*7i - 7*b^2))/(9*a^(10/3)) - (log(588*a^3*b^4*(a + b*x)^(1/3) - 3*a^(10/3)*(3^(1/2)*b^2*7i + 7*b^2)^2)*(3^(1/2)*b^2*7i + 7*b^2))/(9*a^(10/3)) + (14*b^2*log(588*a^3*b^4*(a + b*x)^(1/3) - 588*a^(10/3)*b^4))/(9*a^(10/3))

sympy [C] time = 3.19, size = 2793, normalized size = 18.74

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(b*x+a)**(4/3),x)

[Out] 54*a**(13/3)*b**(5/3)*exp(2*I*pi/3)*gamma(-1/3)/(-54*a**(22/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 162*a**(19/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3) - 162*a**(16/3)*b**2*(a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(2/3) + 54*a**(13/3)*b**3*(a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(2/3)) - 201*a**(10/3)*b**(8/3)*(a/b + x)*exp(2*I*pi/3)*gamma(-1/3)/(-54*a**(22/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 162*a**(19/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3) - 162*a**(16/3)*b**2*(a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(2/3) + 54*a**(13/3)*b**3*(a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(2/3)) + 231*a**(7/3)*b**(11/3)*(a/b + x)**2*exp(2*I*pi/3)*gamma(-1/3)/(-54*a**(22/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 162*a**(19/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3) - 162*a**(16/3)*b**2*(a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(2/3) + 54*a**(13/3)*b**3*(a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(2/3)) - 84*a**(4/3)*b**(14/3)*(a/b + x)**3*exp(2*I*pi/3)*gamma(-1/3)/(-54*a**(22/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 162*a**(19/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3) - 162*a**(16/3)*b**2*(a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(2/3) + 54*a**(13/3)*b**3*(a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(2/3)) + 28*a**4*b**2*(a/b + x)**(1/3)*exp(2*I*pi/3)*log(1 - b**(1/3)*(a/b + x)**(1/3)/a**(1/3))*gamma(-1/3)/(-54*a**(22/3)*(a/b + x)**(1/3)*exp(2*I*pi/3)*gamma(2/3) + 162*a**(19/3)*b*(a/b + x)**(4/3)*exp(2*I*pi/3)*gamma(2/3) - 162*a**(16/3)*b**2*(a/b + x)**(7/3)*exp(2*I*pi/3)*gamma(2/3) + 54*a**(13/3)*b**3*(a/b + x)**(10/3)*exp(2*I*pi/3)*gamma(2/3)) + 28*a**4*b**2*(a

$$\begin{aligned}
& /b + x)^{(1/3)} \exp(-2I\pi/3) \log(1 - b^{(1/3)}(a/b + x)^{(1/3)} \exp_{\text{polar}}(2 \\
& *I\pi/3)/a^{(1/3)}) \gamma(-1/3) / (-54a^{(22/3)}(a/b + x)^{(1/3)} \exp(2I\pi/3) \\
&) \gamma(2/3) + 162a^{(19/3)} b(a/b + x)^{(4/3)} \exp(2I\pi/3) \gamma(2/3) - \\
& 162a^{(16/3)} b^2(a/b + x)^{(7/3)} \exp(2I\pi/3) \gamma(2/3) + 54a^{(13/3)} \\
& *b^3(a/b + x)^{(10/3)} \exp(2I\pi/3) \gamma(2/3) + 28a^4 b^2(a/b + x) \\
& * (1/3) \log(1 - b^{(1/3)}(a/b + x)^{(1/3)} \exp_{\text{polar}}(4I\pi/3)/a^{(1/3)}) \gamma \\
& a(-1/3) / (-54a^{(22/3)}(a/b + x)^{(1/3)} \exp(2I\pi/3) \gamma(2/3) + 162a^{(19/3)} \\
& *b(a/b + x)^{(4/3)} \exp(2I\pi/3) \gamma(2/3) - 162a^{(16/3)} b^2(a/b \\
& + x)^{(7/3)} \exp(2I\pi/3) \gamma(2/3) + 54a^{(13/3)} b^3(a/b + x)^{(10/3)} \\
& * \exp(2I\pi/3) \gamma(2/3) - 84a^3 b^3(a/b + x)^{(4/3)} \exp(2I\pi/3) \log \\
& (1 - b^{(1/3)}(a/b + x)^{(1/3)}/a^{(1/3)}) \gamma(-1/3) / (-54a^{(22/3)}(a/b + \\
& x)^{(1/3)} \exp(2I\pi/3) \gamma(2/3) + 162a^{(19/3)} b(a/b + x)^{(4/3)} \exp(\\
& 2I\pi/3) \gamma(2/3) - 162a^{(16/3)} b^2(a/b + x)^{(7/3)} \exp(2I\pi/3) \gamma \\
& a(2/3) + 54a^{(13/3)} b^3(a/b + x)^{(10/3)} \exp(2I\pi/3) \gamma(2/3) - \\
& 84a^3 b^3(a/b + x)^{(4/3)} \exp(-2I\pi/3) \log(1 - b^{(1/3)}(a/b + x)^{(1 \\
& /3)} \exp_{\text{polar}}(2I\pi/3)/a^{(1/3)}) \gamma(-1/3) / (-54a^{(22/3)}(a/b + x)^{(1/ \\
& 3)} \exp(2I\pi/3) \gamma(2/3) + 162a^{(19/3)} b(a/b + x)^{(4/3)} \exp(2I\pi/3) \\
&) \gamma(2/3) - 162a^{(16/3)} b^2(a/b + x)^{(7/3)} \exp(2I\pi/3) \gamma(2/3) \\
& + 54a^{(13/3)} b^3(a/b + x)^{(10/3)} \exp(2I\pi/3) \gamma(2/3) - 84a^3 b^3 \\
& (a/b + x)^{(4/3)} \log(1 - b^{(1/3)}(a/b + x)^{(1/3)} \exp_{\text{polar}}(4I\pi/3) \\
& /a^{(1/3)}) \gamma(-1/3) / (-54a^{(22/3)}(a/b + x)^{(1/3)} \exp(2I\pi/3) \gamma(2 \\
& /3) + 162a^{(19/3)} b(a/b + x)^{(4/3)} \exp(2I\pi/3) \gamma(2/3) - 162a^{(16/3)} \\
& *b^2(a/b + x)^{(7/3)} \exp(2I\pi/3) \gamma(2/3) + 54a^{(13/3)} b^3(a \\
& /b + x)^{(10/3)} \exp(2I\pi/3) \gamma(2/3) + 84a^2 b^4(a/b + x)^{(7/3)} e \\
& xp(2I\pi/3) \log(1 - b^{(1/3)}(a/b + x)^{(1/3)}/a^{(1/3)}) \gamma(-1/3) / (-54a \\
& ** (22/3) (a/b + x)^{(1/3)} \exp(2I\pi/3) \gamma(2/3) + 162a^{(19/3)} b(a/b + \\
& x)^{(4/3)} \exp(2I\pi/3) \gamma(2/3) - 162a^{(16/3)} b^2(a/b + x)^{(7/3)} e \\
& xp(2I\pi/3) \gamma(2/3) + 54a^{(13/3)} b^3(a/b + x)^{(10/3)} \exp(2I\pi/3) \\
& * \gamma(2/3) + 84a^2 b^4(a/b + x)^{(7/3)} \exp(-2I\pi/3) \log(1 - b^{(1/3) \\
&) (a/b + x)^{(1/3)} \exp_{\text{polar}}(2I\pi/3)/a^{(1/3)}) \gamma(-1/3) / (-54a^{(22/3) \\
&) (a/b + x)^{(1/3)} \exp(2I\pi/3) \gamma(2/3) + 162a^{(19/3)} b(a/b + x)^{(4/ \\
& 3)} \exp(2I\pi/3) \gamma(2/3) - 162a^{(16/3)} b^2(a/b + x)^{(7/3)} \exp(2I\pi \\
& i/3) \gamma(2/3) + 54a^{(13/3)} b^3(a/b + x)^{(10/3)} \exp(2I\pi/3) \gamma(2 \\
& /3) + 84a^2 b^4(a/b + x)^{(7/3)} \log(1 - b^{(1/3)}(a/b + x)^{(1/3)} \exp_{ \\
& polar}(4I\pi/3)/a^{(1/3)}) \gamma(-1/3) / (-54a^{(22/3)}(a/b + x)^{(1/3)} \exp(2 \\
& *I\pi/3) \gamma(2/3) + 162a^{(19/3)} b(a/b + x)^{(4/3)} \exp(2I\pi/3) \gamma(2 \\
& /3) - 162a^{(16/3)} b^2(a/b + x)^{(7/3)} \exp(2I\pi/3) \gamma(2/3) + 54a^ \\
& * (13/3) b^3(a/b + x)^{(10/3)} \exp(2I\pi/3) \gamma(2/3) - 28a b^5(a/b + \\
& x)^{(10/3)} \exp(2I\pi/3) \log(1 - b^{(1/3)}(a/b + x)^{(1/3)}/a^{(1/3)}) \gamma \\
& (-1/3) / (-54a^{(22/3)}(a/b + x)^{(1/3)} \exp(2I\pi/3) \gamma(2/3) + 162a^{(1 \\
& 9/3)} b(a/b + x)^{(4/3)} \exp(2I\pi/3) \gamma(2/3) - 162a^{(16/3)} b^2(a/b \\
& + x)^{(7/3)} \exp(2I\pi/3) \gamma(2/3) + 54a^{(13/3)} b^3(a/b + x)^{(10/3)} \\
& * \exp(2I\pi/3) \gamma(2/3) - 28a b^5(a/b + x)^{(10/3)} \exp(-2I\pi/3) \log(\\
& 1 - b^{(1/3)}(a/b + x)^{(1/3)} \exp_{\text{polar}}(2I\pi/3)/a^{(1/3)}) \gamma(-1/3) / (-5 \\
& 4a^{(22/3)}(a/b + x)^{(1/3)} \exp(2I\pi/3) \gamma(2/3) + 162a^{(19/3)} b(a/
\end{aligned}$$

$$\begin{aligned}
& b + x)^{(4/3)} \exp(2I\pi/3) \gamma(2/3) - 162 a^{(16/3)} b^{(2)} (a/b + x)^{(7/3)} \\
& \exp(2I\pi/3) \gamma(2/3) + 54 a^{(13/3)} b^{(3)} (a/b + x)^{(10/3)} \exp(2I\pi/3) \gamma(2/3) \\
& - 28 a b^{(5)} (a/b + x)^{(10/3)} \log(1 - b^{(1/3)} (a/b + x)^{(1/3)} \exp_{\text{polar}}(4I\pi/3) / a^{(1/3)}) \gamma(-1/3) / (-54 a^{(22/3)} (a/b + x)^{(1/3)} \exp(2I\pi/3) \gamma(2/3) + 162 a^{(19/3)} b (a/b + x)^{(4/3)} \exp(2I\pi/3) \gamma(2/3) - 162 a^{(16/3)} b^{(2)} (a/b + x)^{(7/3)} \exp(2I\pi/3) \gamma(2/3) + 54 a^{(13/3)} b^{(3)} (a/b + x)^{(10/3)} \exp(2I\pi/3) \gamma(2/3))
\end{aligned}$$

$$3.420 \quad \int \frac{1}{x \sqrt[3]{a^3 + b^3 x}} dx$$

Optimal. Leaf size=71

$$\frac{3 \log\left(a - \sqrt[3]{a^3 + b^3 x}\right)}{2a} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3 + b^3 x} + a}{\sqrt{3}a}\right)}{a} - \frac{\log(x)}{2a}$$

[Out] $-1/2*\ln(x)/a+3/2*\ln(a-(b^3*x+a^3)^{(1/3)})/a+\arctan(1/3*(a+2*(b^3*x+a^3)^{(1/3}))/a*3^{(1/2)})*3^{(1/2)}/a$

Rubi [A] time = 0.03, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {55, 617, 204, 31}

$$\frac{3 \log\left(a - \sqrt[3]{a^3 + b^3 x}\right)}{2a} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3 + b^3 x} + a}{\sqrt{3}a}\right)}{a} - \frac{\log(x)}{2a}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a^3 + b^3*x)^(1/3)),x]

[Out] (Sqrt[3]*ArcTan[(a + 2*(a^3 + b^3*x)^(1/3))/(Sqrt[3]*a)])/a - Log[x]/(2*a) + (3*Log[a - (a^3 + b^3*x)^(1/3)])/(2*a)

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 55

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)]], x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x\sqrt[3]{a^3 + b^3x}} dx &= -\frac{\log(x)}{2a} + \frac{3}{2} \text{Subst} \left(\int \frac{1}{a^2 + ax + x^2} dx, x, \sqrt[3]{a^3 + b^3x} \right) - \frac{3 \text{Subst} \left(\int \frac{1}{a-x} dx, x, \sqrt[3]{a^3 + b^3x} \right)}{2a} \\ &= -\frac{\log(x)}{2a} + \frac{3 \log \left(a - \sqrt[3]{a^3 + b^3x} \right)}{2a} - \frac{3 \text{Subst} \left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a^3 + b^3x}}{a} \right)}{a} \\ &= \frac{\sqrt{3} \tan^{-1} \left(\frac{1 + \frac{2\sqrt[3]{a^3 + b^3x}}{a}}{\sqrt{3}} \right)}{a} - \frac{\log(x)}{2a} + \frac{3 \log \left(a - \sqrt[3]{a^3 + b^3x} \right)}{2a} \end{aligned}$$

Mathematica [A] time = 0.02, size = 66, normalized size = 0.93

$$\frac{3 \log \left(a - \sqrt[3]{a^3 + b^3x} \right) + 2\sqrt{3} \tan^{-1} \left(\frac{2\sqrt[3]{a^3 + b^3x} + a}{\sqrt{3}a} \right) - \log(x)}{2a}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a^3 + b^3*x)^(1/3)),x]

[Out] (2*Sqrt[3]*ArcTan[(a + 2*(a^3 + b^3*x)^(1/3))/(Sqrt[3]*a)] - Log[x] + 3*Log[a - (a^3 + b^3*x)^(1/3)])/(2*a)

fricas [A] time = 0.50, size = 88, normalized size = 1.24

$$\frac{2\sqrt{3} \arctan \left(\frac{\sqrt{3}a + 2\sqrt{3}(b^3x + a^3)^{\frac{1}{3}}}{3a} \right) - \log \left(a^2 + (b^3x + a^3)^{\frac{1}{3}}a + (b^3x + a^3)^{\frac{2}{3}} \right) + 2 \log \left(-a + (b^3x + a^3)^{\frac{1}{3}} \right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b^3*x+a^3)^(1/3),x, algorithm="fricas")

[Out] $\frac{1}{2} \cdot (2 \cdot \sqrt{3} \cdot \arctan(1/3 \cdot (\sqrt{3} \cdot a + 2 \cdot \sqrt{3} \cdot (b^3 x + a^3)^{1/3})) / a) - \log(a^2 + (b^3 x + a^3)^{1/3} \cdot a + (b^3 x + a^3)^{2/3}) + 2 \cdot \log(-a + (b^3 x + a^3)^{1/3}) / a$

giac [A] time = 1.03, size = 87, normalized size = 1.23

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a+2\left(b^3x+a^3\right)^{\frac{1}{3}}\right)}{3a}\right)}{a} - \frac{\log\left(a^2 + \left(b^3x+a^3\right)^{\frac{1}{3}}a + \left(b^3x+a^3\right)^{\frac{2}{3}}\right)}{2a} + \frac{\log\left(\left|-a + \left(b^3x+a^3\right)^{\frac{1}{3}}\right|\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b^3*x+a^3)^(1/3),x, algorithm="giac")`

[Out] $\frac{\sqrt{3} \cdot \arctan(1/3 \cdot \sqrt{3} \cdot (a + 2 \cdot (b^3 x + a^3)^{1/3}) / a) / a - 1/2 \cdot \log(a^2 + (b^3 x + a^3)^{1/3} \cdot a + (b^3 x + a^3)^{2/3}) / a + \log(\text{abs}(-a + (b^3 x + a^3)^{1/3})) / a}$

maple [A] time = 0.01, size = 87, normalized size = 1.23

$$\frac{\sqrt{3} \arctan\left(\frac{\left(a+2\left(b^3x+a^3\right)^{\frac{1}{3}}\right)\sqrt{3}}{3a}\right)}{a} + \frac{\ln\left(-a + \left(b^3x+a^3\right)^{\frac{1}{3}}\right)}{a} - \frac{\ln\left(a^2 + \left(b^3x+a^3\right)^{\frac{1}{3}}a + \left(b^3x+a^3\right)^{\frac{2}{3}}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x/(b^3*x+a^3)^(1/3),x)`

[Out] $\frac{1}{a} \cdot \ln((b^3 x + a^3)^{1/3} - a) - \frac{1}{2} \cdot \frac{1}{a} \cdot \ln((b^3 x + a^3)^{2/3} + (b^3 x + a^3)^{1/3} \cdot a + a^2) + \arctan(1/3 \cdot (a + 2 \cdot (b^3 x + a^3)^{1/3}) / a) \cdot 3^{1/2} / a$

maxima [A] time = 3.09, size = 86, normalized size = 1.21

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a+2\left(b^3x+a^3\right)^{\frac{1}{3}}\right)}{3a}\right)}{a} - \frac{\log\left(a^2 + \left(b^3x+a^3\right)^{\frac{1}{3}}a + \left(b^3x+a^3\right)^{\frac{2}{3}}\right)}{2a} + \frac{\log\left(-a + \left(b^3x+a^3\right)^{\frac{1}{3}}\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b^3*x+a^3)^(1/3),x, algorithm="maxima")`

[Out] $\sqrt{3} \arctan(1/3 \sqrt{3} (a + 2(b^3 x + a^3)^{1/3})/a)/a - 1/2 \log(a^2 + (b^3 x + a^3)^{1/3} a + (b^3 x + a^3)^{2/3})/a + \log(-a + (b^3 x + a^3)^{1/3})/a$

mupad [B] time = 0.10, size = 105, normalized size = 1.48

$$\frac{\ln\left(9\left(a^3 + x b^3\right)^{1/3} - 9a\right)}{a} + \frac{\ln\left(9\left(a^3 + x b^3\right)^{1/3} - \frac{9a(-1+\sqrt{3}1i)^2}{4}\right)(-1+\sqrt{3}1i)}{2a} - \frac{\ln\left(9\left(a^3 + x b^3\right)^{1/3} - \frac{9a(1+\sqrt{3}1i)^2}{4}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(b^3*x + a^3)^(1/3)),x)`

[Out] $\log(9*(b^3*x + a^3)^{1/3} - 9*a)/a + (\log(9*(b^3*x + a^3)^{1/3} - (9*a*(3^{1/2}*1i - 1)^2/4)*(3^{1/2}*1i - 1))/(2*a) - (\log(9*(b^3*x + a^3)^{1/3} - (9*a*(3^{1/2}*1i + 1)^2/4)*(3^{1/2}*1i + 1))/(2*a)$

sympy [C] time = 2.13, size = 138, normalized size = 1.94

$$\frac{e^{\frac{i\pi}{3}} \log\left(-\frac{ae^{\frac{2i\pi}{3}}}{b\sqrt[3]{\frac{a^3}{b^3}+x}} + 1\right) \Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)} + \frac{e^{-\frac{i\pi}{3}} \log\left(-\frac{ae^{\frac{4i\pi}{3}}}{b\sqrt[3]{\frac{a^3}{b^3}+x}} + 1\right) \Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)} - \frac{\log\left(-\frac{ae^{2i\pi}}{b\sqrt[3]{\frac{a^3}{b^3}+x}} + 1\right) \Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b**3*x+a**3)**(1/3),x)`

[Out] $\exp(I*\pi/3)*\log(-a*\exp_polar(2*I*\pi/3)/(b*(a**3/b**3 + x)**(1/3)) + 1)*\gamma(-1/3)/(3*a*\gamma(2/3)) + \exp(-I*\pi/3)*\log(-a*\exp_polar(4*I*\pi/3)/(b*(a**3/b**3 + x)**(1/3)) + 1)*\gamma(-1/3)/(3*a*\gamma(2/3)) - \log(-a*\exp_polar(2*I*\pi)/(b*(a**3/b**3 + x)**(1/3)) + 1)*\gamma(-1/3)/(3*a*\gamma(2/3))$

$$3.421 \quad \int \frac{1}{x \sqrt[3]{a^3 - b^3 x}} dx$$

Optimal. Leaf size=73

$$\frac{3 \log\left(a - \sqrt[3]{a^3 - b^3 x}\right)}{2a} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3 - b^3 x} + a}{\sqrt{3}a}\right)}{a} - \frac{\log(x)}{2a}$$

[Out] $-1/2*\ln(x)/a+3/2*\ln(a-(-b^3*x+a^3)^(1/3))/a+\arctan(1/3*(a+2*(-b^3*x+a^3)^(1/3))/a*3^(1/2))*3^(1/2)/a$

Rubi [A] time = 0.03, antiderivative size = 73, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {55, 617, 204, 31}

$$\frac{3 \log\left(a - \sqrt[3]{a^3 - b^3 x}\right)}{2a} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3 - b^3 x} + a}{\sqrt{3}a}\right)}{a} - \frac{\log(x)}{2a}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a^3 - b^3*x)^(1/3)),x]

[Out] (Sqrt[3]*ArcTan[(a + 2*(a^3 - b^3*x)^(1/3))/(Sqrt[3]*a)]/a - Log[x]/(2*a) + (3*Log[a - (a^3 - b^3*x)^(1/3)])/(2*a)

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 55

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)]], x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x\sqrt[3]{a^3 - b^3x}} dx &= -\frac{\log(x)}{2a} + \frac{3}{2} \text{Subst}\left(\int \frac{1}{a^2 + ax + x^2} dx, x, \sqrt[3]{a^3 - b^3x}\right) - \frac{3 \text{Subst}\left(\int \frac{1}{a-x} dx, x, \sqrt[3]{a^3 - b^3x}\right)}{2a} \\ &= -\frac{\log(x)}{2a} + \frac{3 \log\left(a - \sqrt[3]{a^3 - b^3x}\right)}{2a} - \frac{3 \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a^3 - b^3x}}{a}\right)}{a} \\ &= \frac{\sqrt{3} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a^3 - b^3x}}{a}}{\sqrt{3}}\right)}{a} - \frac{\log(x)}{2a} + \frac{3 \log\left(a - \sqrt[3]{a^3 - b^3x}\right)}{2a} \end{aligned}$$

Mathematica [A] time = 0.02, size = 68, normalized size = 0.93

$$\frac{3 \log\left(a - \sqrt[3]{a^3 - b^3x}\right) + 2\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3 - b^3x} + a}{\sqrt{3}a}\right) - \log(x)}{2a}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a^3 - b^3*x)^(1/3)),x]

[Out] (2*Sqrt[3]*ArcTan[(a + 2*(a^3 - b^3*x)^(1/3))/(Sqrt[3]*a)] - Log[x] + 3*Log[a - (a^3 - b^3*x)^(1/3)])/(2*a)

fricas [A] time = 0.59, size = 92, normalized size = 1.26

$$\frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}a+2\sqrt{3}(-b^3x+a^3)^{\frac{1}{3}}}{3a}\right) - \log\left(a^2 + (-b^3x+a^3)^{\frac{1}{3}}a + (-b^3x+a^3)^{\frac{2}{3}}\right) + 2 \log\left(-a + (-b^3x+a^3)^{\frac{1}{3}}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(-b^3*x+a^3)^(1/3),x, algorithm="fricas")

[Out] $\frac{1}{2} \cdot (2 \cdot \sqrt{3} \cdot \arctan(1/3 \cdot (\sqrt{3} \cdot a + 2 \cdot \sqrt{3} \cdot (-b^3 x + a^3)^{1/3})/a) - \log(a^2 + (-b^3 x + a^3)^{1/3} \cdot a + (-b^3 x + a^3)^{2/3})) + 2 \cdot \log(-a + (-b^3 x + a^3)^{1/3})/a$

giac [A] time = 0.77, size = 91, normalized size = 1.25

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a+2(-b^3x+a^3)^{\frac{1}{3}}\right)}{3a}\right)}{a} - \frac{\log\left(a^2 + (-b^3x+a^3)^{\frac{1}{3}}a + (-b^3x+a^3)^{\frac{2}{3}}\right)}{2a} + \frac{\log\left(-a + (-b^3x+a^3)^{\frac{1}{3}}\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(-b^3*x+a^3)^(1/3),x, algorithm="giac")`

[Out] $\sqrt{3} \cdot \arctan(1/3 \cdot \sqrt{3} \cdot (a + 2 \cdot (-b^3 x + a^3)^{1/3})/a)/a - 1/2 \cdot \log(a^2 + (-b^3 x + a^3)^{1/3} \cdot a + (-b^3 x + a^3)^{2/3})/a + \log(\text{abs}(-a + (-b^3 x + a^3)^{1/3}))/a$

maple [A] time = 0.00, size = 91, normalized size = 1.25

$$\frac{\sqrt{3} \arctan\left(\frac{\left(a+2(-b^3x+a^3)^{\frac{1}{3}}\right)\sqrt{3}}{3a}\right)}{a} + \frac{\ln\left(-a + (-b^3x+a^3)^{\frac{1}{3}}\right)}{a} - \frac{\ln\left(a^2 + (-b^3x+a^3)^{\frac{1}{3}}a + (-b^3x+a^3)^{\frac{2}{3}}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x/(-b^3*x+a^3)^(1/3),x)`

[Out] $\frac{1}{a} \cdot \ln((-b^3 x + a^3)^{1/3} - a) - \frac{1}{2} \cdot \frac{1}{a} \cdot \ln((-b^3 x + a^3)^{2/3} + (-b^3 x + a^3)^{1/3} \cdot a + a^2) + \arctan(1/3 \cdot (a + 2 \cdot (-b^3 x + a^3)^{1/3})/a) \cdot 3^{1/2}/a$

maxima [A] time = 2.99, size = 90, normalized size = 1.23

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a+2(-b^3x+a^3)^{\frac{1}{3}}\right)}{3a}\right)}{a} - \frac{\log\left(a^2 + (-b^3x+a^3)^{\frac{1}{3}}a + (-b^3x+a^3)^{\frac{2}{3}}\right)}{2a} + \frac{\log\left(-a + (-b^3x+a^3)^{\frac{1}{3}}\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(-b^3*x+a^3)^(1/3),x, algorithm="maxima")`

[Out] $\sqrt{3} \arctan\left(\frac{1}{3}\sqrt{3}\left(\frac{a + 2(-b^3x + a^3)^{1/3}}{a}\right) - \frac{1}{2}\log\left(\frac{a^2 + (-b^3x + a^3)^{1/3}a + (-b^3x + a^3)^{2/3}}{a}\right) + \log\left(\frac{-a + (-b^3x + a^3)^{1/3}}{a}\right)\right)$

mupad [B] time = 0.13, size = 108, normalized size = 1.48

$$\frac{\ln\left(9\left(a^3 - b^3x\right)^{1/3} - 9a\right)}{a} + \frac{\ln\left(9\left(a^3 - b^3x\right)^{1/3} - \frac{9a(-1+\sqrt{3}1i)^2}{4}\right)(-1+\sqrt{3}1i)}{2a} - \frac{\ln\left(9\left(a^3 - b^3x\right)^{1/3} - \frac{9a(1+\sqrt{3}1i)^2}{4}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(x*(a^3 - b^3*x)^{1/3}), x)$

[Out] $\log\left(\frac{9(a^3 - b^3x)^{1/3} - 9a}{a}\right) + \frac{\log\left(\frac{9(a^3 - b^3x)^{1/3} - (9a*(3^{1/2}*1i - 1)^2/4)}{a}\right)*(3^{1/2}*1i - 1)}{2a} - \frac{\log\left(\frac{9(a^3 - b^3x)^{1/3} - (9a*(3^{1/2}*1i + 1)^2/4)}{a}\right)*(3^{1/2}*1i + 1)}{2a}$

sympy [C] time = 1.89, size = 136, normalized size = 1.86

$$\frac{e^{-\frac{2i\pi}{3}} \log\left(-\frac{ae^{\frac{i\pi}{3}}}{b\sqrt[3]{\frac{a^3}{b^3}+x}} + 1\right) \Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)} + \frac{e^{-\frac{i\pi}{3}} \log\left(-\frac{ae^{i\pi}}{b\sqrt[3]{\frac{a^3}{b^3}+x}} + 1\right) \Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)} - \frac{\log\left(-\frac{ae^{\frac{5i\pi}{3}}}{b\sqrt[3]{\frac{a^3}{b^3}+x}} + 1\right) \Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x/(-b**3*x+a**3)**(1/3), x)$

[Out] $-\exp(-2*I*\pi/3)*\log(-a*\exp_polar(I*\pi/3)/(b*(-a**3/b**3 + x)**(1/3)) + 1)*\gamma(-1/3)/(3*a*\gamma(2/3)) + \exp(-I*\pi/3)*\log(-a*\exp_polar(I*\pi)/(b*(-a**3/b**3 + x)**(1/3)) + 1)*\gamma(-1/3)/(3*a*\gamma(2/3)) - \log(-a*\exp_polar(5*I*\pi/3)/(b*(-a**3/b**3 + x)**(1/3)) + 1)*\gamma(-1/3)/(3*a*\gamma(2/3))$

$$3.422 \quad \int \frac{1}{x \sqrt[3]{-a^3 + b^3 x}} dx$$

Optimal. Leaf size=74

$$-\frac{3 \log\left(\sqrt[3]{b^3 x - a^3} + a\right)}{2a} - \frac{\sqrt{3} \tan^{-1}\left(\frac{a - 2\sqrt[3]{b^3 x - a^3}}{\sqrt{3}a}\right)}{a} + \frac{\log(x)}{2a}$$

[Out] $1/2*\ln(x)/a - 3/2*\ln(a + (b^3*x - a^3)^{(1/3)})/a - \arctan(1/3*(a - 2*(b^3*x - a^3)^{(1/3)})/a) * 3^{(1/2)}/a$

Rubi [A] time = 0.03, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {56, 617, 204, 31}

$$-\frac{3 \log\left(\sqrt[3]{b^3 x - a^3} + a\right)}{2a} - \frac{\sqrt{3} \tan^{-1}\left(\frac{a - 2\sqrt[3]{b^3 x - a^3}}{\sqrt{3}a}\right)}{a} + \frac{\log(x)}{2a}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(-a^3 + b^3*x)^(1/3)),x]

[Out] $-\left(\frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{a - 2(-a^3 + b^3 x)^{1/3}}{\sqrt{3}a}\right]}{a}\right) + \frac{\operatorname{Log}[x]}{2a} - \frac{3 \operatorname{Log}[a + (-a^3 + b^3 x)^{1/3}]}{2a}$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 56

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])]/; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[Rt[-b, 2]*x]/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
 implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{x\sqrt[3]{-a^3 + b^3x}} dx &= \frac{\log(x)}{2a} + \frac{3}{2} \text{Subst} \left(\int \frac{1}{a^2 - ax + x^2} dx, x, \sqrt[3]{-a^3 + b^3x} \right) - \frac{3 \text{Subst} \left(\int \frac{1}{a+x} dx, x, \sqrt[3]{-a^3 + b^3x} \right)}{2a} \\ &= \frac{\log(x)}{2a} - \frac{3 \log \left(a + \sqrt[3]{-a^3 + b^3x} \right)}{2a} + \frac{3 \text{Subst} \left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{-a^3 + b^3x}}{a} \right)}{a} \\ &= -\frac{\sqrt{3} \tan^{-1} \left(\frac{1 - \frac{2\sqrt[3]{-a^3 + b^3x}}{a}}{\sqrt{3}} \right)}{a} + \frac{\log(x)}{2a} - \frac{3 \log \left(a + \sqrt[3]{-a^3 + b^3x} \right)}{2a} \end{aligned}$$

Mathematica [C] time = 0.01, size = 41, normalized size = 0.55

$$\frac{3(b^3x - a^3)^{2/3} {}_2F_1\left(\frac{2}{3}, 1; \frac{5}{3}; 1 - \frac{b^3x}{a^3}\right)}{2a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(-a^3 + b^3*x)^(1/3)),x]

[Out] (3*(-a^3 + b^3*x)^(2/3)*Hypergeometric2F1[2/3, 1, 5/3, 1 - (b^3*x)/a^3])/(2*a^3)

fricas [A] time = 0.71, size = 93, normalized size = 1.26

$$\frac{2\sqrt{3} \arctan\left(-\frac{\sqrt{3}a - 2\sqrt{3}(b^3x - a^3)^{1/3}}{3a}\right) + \log\left(a^2 - (b^3x - a^3)^{1/3}a + (b^3x - a^3)^{2/3}\right) - 2 \log\left(a + (b^3x - a^3)^{1/3}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b^3*x-a^3)^(1/3),x, algorithm="fricas")

[Out] $\frac{1}{2} \cdot (2 \cdot \sqrt{3} \cdot \arctan(-\frac{1}{3} \cdot (\sqrt{3} \cdot a - 2 \cdot \sqrt{3} \cdot (b^3 x - a^3)^{1/3})) / a) + \log(a^2 - (b^3 x - a^3)^{1/3} \cdot a + (b^3 x - a^3)^{2/3}) - 2 \cdot \log(a + (b^3 x - a^3)^{1/3}) / a$

giac [A] time = 1.07, size = 95, normalized size = 1.28

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a-2\left(b^3x-a^3\right)^{\frac{1}{3}}\right)}{3a}\right)}{a} + \frac{\log\left(a^2 - \left(b^3x - a^3\right)^{\frac{1}{3}}a + \left(b^3x - a^3\right)^{\frac{2}{3}}\right)}{2a} - \frac{\log\left(a + \left(b^3x - a^3\right)^{\frac{1}{3}}\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b^3*x-a^3)^(1/3),x, algorithm="giac")`

[Out] $\frac{\sqrt{3} \cdot \arctan(-\frac{1}{3} \cdot \sqrt{3} \cdot (a - 2 \cdot (b^3 x - a^3)^{1/3})) / a}{a} + \frac{1}{2} \cdot \log(a^2 - (b^3 x - a^3)^{1/3} \cdot a + (b^3 x - a^3)^{2/3}) / a - \log(\text{abs}(a + (b^3 x - a^3)^{1/3})) / a$

maple [A] time = 0.01, size = 97, normalized size = 1.31

$$\frac{\sqrt{3} \arctan\left(\frac{\left(-a+2\left(b^3x-a^3\right)^{\frac{1}{3}}\right)\sqrt{3}}{3a}\right)}{a} - \frac{\ln\left(a + \left(b^3x - a^3\right)^{\frac{1}{3}}\right)}{a} + \frac{\ln\left(a^2 - \left(b^3x - a^3\right)^{\frac{1}{3}}a + \left(b^3x - a^3\right)^{\frac{2}{3}}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x/(b^3*x-a^3)^(1/3),x)`

[Out] $\frac{1}{2} \cdot \frac{a \cdot \ln((b^3 x - a^3)^{2/3} - (b^3 x - a^3)^{1/3} \cdot a + a^2) + 1/a \cdot 3^{1/2} \cdot \arctan(1/3 \cdot (2 \cdot (b^3 x - a^3)^{1/3} - a) \cdot 3^{1/2} / a) - \ln(a + (b^3 x - a^3)^{1/3})}{a}$

maxima [A] time = 2.90, size = 94, normalized size = 1.27

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a-2\left(b^3x-a^3\right)^{\frac{1}{3}}\right)}{3a}\right)}{a} + \frac{\log\left(a^2 - \left(b^3x - a^3\right)^{\frac{1}{3}}a + \left(b^3x - a^3\right)^{\frac{2}{3}}\right)}{2a} - \frac{\log\left(a + \left(b^3x - a^3\right)^{\frac{1}{3}}\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b^3*x-a^3)^(1/3),x, algorithm="maxima")`

[Out] $\sqrt{3} \arctan(-1/3 \sqrt{3} (a - 2(b^3 x - a^3)^{1/3})/a) / a + 1/2 \log(a^2 - (b^3 x - a^3)^{1/3} a + (b^3 x - a^3)^{2/3}) / a - \log(a + (b^3 x - a^3)^{1/3}) / a$

mupad [B] time = 0.11, size = 112, normalized size = 1.51

$$\frac{\ln\left(9a + 9(b^3x - a^3)^{1/3}\right)}{a} - \frac{\ln\left(\frac{9a(-1+\sqrt{3}i)^2}{4} + 9(b^3x - a^3)^{1/3}\right)}{2a} + \frac{\ln\left(\frac{9a(1+\sqrt{3}i)^2}{4} + 9(b^3x - a^3)^{1/3}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(b^3*x - a^3)^(1/3)),x)`

[Out] $(\log((9a(3^{1/2}i + 1)^2/4 + 9(b^3x - a^3)^{1/3})*(3^{1/2}i + 1)) / (2a) - (\log((9a(3^{1/2}i - 1)^2/4 + 9(b^3x - a^3)^{1/3})*(3^{1/2}i - 1)) / (2a) - \log(9a + 9(b^3x - a^3)^{1/3}) / a$

sympy [C] time = 1.82, size = 134, normalized size = 1.81

$$-\frac{e^{-\frac{i\pi}{3}} \log\left(-\frac{ae^{\frac{i\pi}{3}}}{b\sqrt[3]{\frac{a^3}{b^3}+x}} + 1\right) \Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)} + \frac{\log\left(-\frac{ae^{i\pi}}{b\sqrt[3]{-\frac{a^3}{b^3}+x}} + 1\right) \Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)} - \frac{e^{\frac{i\pi}{3}} \log\left(-\frac{ae^{\frac{5i\pi}{3}}}{b\sqrt[3]{\frac{a^3}{b^3}+x}} + 1\right) \Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b**3*x-a**3)**(1/3),x)`

[Out] $-\exp(-I\pi/3) \log(-a \exp_{\text{polar}}(I\pi/3) / (b(-a^{**3}/b^{**3} + x)^{**}(1/3)) + 1) * \text{gamma}(-1/3) / (3a * \text{gamma}(2/3)) + \log(-a \exp_{\text{polar}}(I\pi) / (b(-a^{**3}/b^{**3} + x)^{**}(1/3)) + 1) * \text{gamma}(-1/3) / (3a * \text{gamma}(2/3)) - \exp(I\pi/3) \log(-a \exp_{\text{polar}}(5I\pi/3) / (b(-a^{**3}/b^{**3} + x)^{**}(1/3)) + 1) * \text{gamma}(-1/3) / (3a * \text{gamma}(2/3))$

$$3.423 \quad \int \frac{1}{x \sqrt[3]{-a^3 - b^3 x}} dx$$

Optimal. Leaf size=76

$$-\frac{3 \log\left(\sqrt[3]{-a^3 - b^3 x} + a\right)}{2a} - \frac{\sqrt{3} \tan^{-1}\left(\frac{a - 2\sqrt[3]{-a^3 - b^3 x}}{\sqrt{3}a}\right)}{a} + \frac{\log(x)}{2a}$$

[Out] 1/2*ln(x)/a-3/2*ln(a+(-b^3*x-a^3)^(1/3))/a-arctan(1/3*(a-2*(-b^3*x-a^3)^(1/3))/a*3^(1/2))*3^(1/2)/a

Rubi [A] time = 0.03, antiderivative size = 76, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {56, 617, 204, 31}

$$-\frac{3 \log\left(\sqrt[3]{-a^3 - b^3 x} + a\right)}{2a} - \frac{\sqrt{3} \tan^{-1}\left(\frac{a - 2\sqrt[3]{-a^3 - b^3 x}}{\sqrt{3}a}\right)}{a} + \frac{\log(x)}{2a}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(-a^3 - b^3*x)^(1/3)),x]

[Out] -((Sqrt[3]*ArcTan[(a - 2*(-a^3 - b^3*x)^(1/3))/(Sqrt[3]*a)]/a) + Log[x]/(2*a) - (3*Log[a + (-a^3 - b^3*x)^(1/3)])/(2*a))

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 56

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])]/; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{x\sqrt[3]{-a^3 - b^3x}} dx &= \frac{\log(x)}{2a} + \frac{3}{2} \text{Subst} \left(\int \frac{1}{a^2 - ax + x^2} dx, x, \sqrt[3]{-a^3 - b^3x} \right) - \frac{3 \text{Subst} \left(\int \frac{1}{a+x} dx, x, \sqrt[3]{-a^3 - b^3x} \right)}{2a} \\ &= \frac{\log(x)}{2a} - \frac{3 \log \left(a + \sqrt[3]{-a^3 - b^3x} \right)}{2a} + \frac{3 \text{Subst} \left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{-a^3 - b^3x}}{a} \right)}{a} \\ &= -\frac{\sqrt{3} \tan^{-1} \left(\frac{1 - \frac{2\sqrt[3]{-a^3 - b^3x}}{a}}{\sqrt{3}} \right)}{a} + \frac{\log(x)}{2a} - \frac{3 \log \left(a + \sqrt[3]{-a^3 - b^3x} \right)}{2a} \end{aligned}$$

Mathematica [C] time = 0.01, size = 41, normalized size = 0.54

$$\frac{3(-a^3 - b^3x)^{2/3} {}_2F_1\left(\frac{2}{3}, 1; \frac{5}{3}; \frac{xb^3}{a^3} + 1\right)}{2a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(-a^3 - b^3*x)^(1/3)),x]

[Out] (3*(-a^3 - b^3*x)^(2/3)*Hypergeometric2F1[2/3, 1, 5/3, 1 + (b^3*x)/a^3])/(2*a^3)

fricas [A] time = 0.44, size = 97, normalized size = 1.28

$$\frac{2\sqrt{3} \arctan\left(-\frac{\sqrt{3}a - 2\sqrt{3}(-b^3x - a^3)^{\frac{1}{3}}}{3a}\right) + \log\left(a^2 - (-b^3x - a^3)^{\frac{1}{3}}a + (-b^3x - a^3)^{\frac{2}{3}}\right) - 2 \log\left(a + (-b^3x - a^3)^{\frac{1}{3}}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(-b^3*x-a^3)^(1/3),x, algorithm="fricas")

[Out] $\frac{1}{2} \cdot (2 \cdot \sqrt{3} \cdot \arctan(-\frac{1}{3} \cdot (\sqrt{3} \cdot a - 2 \cdot \sqrt{3} \cdot (-b^3 x - a^3)^{1/3})) / a + \log(a^2 - (-b^3 x - a^3)^{1/3} \cdot a + (-b^3 x - a^3)^{2/3})) - 2 \cdot \log(a + (-b^3 x - a^3)^{1/3}) / a$

giac [A] time = 1.00, size = 99, normalized size = 1.30

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a-2(-b^3x-a^3)^{\frac{1}{3}}\right)}{3a}\right)}{a} + \frac{\log\left(a^2 - (-b^3x - a^3)^{\frac{1}{3}}a + (-b^3x - a^3)^{\frac{2}{3}}\right)}{2a} - \frac{\log\left(a + (-b^3x - a^3)^{\frac{1}{3}}\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(-b^3*x-a^3)^(1/3),x, algorithm="giac")`

[Out] $\sqrt{3} \cdot \arctan(-\frac{1}{3} \cdot \sqrt{3} \cdot (a - 2 \cdot (-b^3 x - a^3)^{1/3}) / a) / a + \frac{1}{2} \cdot \log(a^2 - (-b^3 x - a^3)^{1/3} \cdot a + (-b^3 x - a^3)^{2/3}) / a - \log(\text{abs}(a + (-b^3 x - a^3)^{1/3})) / a$

maple [A] time = 0.00, size = 101, normalized size = 1.33

$$\frac{\sqrt{3} \arctan\left(\frac{\left(-a+2(-b^3x-a^3)^{\frac{1}{3}}\right)\sqrt{3}}{3a}\right)}{a} - \frac{\ln\left(a + (-b^3x - a^3)^{\frac{1}{3}}\right)}{a} + \frac{\ln\left(a^2 - (-b^3x - a^3)^{\frac{1}{3}}a + (-b^3x - a^3)^{\frac{2}{3}}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x/(-b^3*x-a^3)^(1/3),x)`

[Out] $\frac{1}{2} \cdot \frac{1}{a} \cdot \ln((-b^3 x - a^3)^{2/3} - (-b^3 x - a^3)^{1/3} \cdot a + a^2) + \frac{1}{a} \cdot 3^{1/2} \cdot \arctan(1/3 \cdot (2 \cdot (-b^3 x - a^3)^{1/3} - a) \cdot 3^{1/2} / a) - \ln(a + (-b^3 x - a^3)^{1/3}) / a$

maxima [A] time = 2.92, size = 98, normalized size = 1.29

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a-2(-b^3x-a^3)^{\frac{1}{3}}\right)}{3a}\right)}{a} + \frac{\log\left(a^2 - (-b^3x - a^3)^{\frac{1}{3}}a + (-b^3x - a^3)^{\frac{2}{3}}\right)}{2a} - \frac{\log\left(a + (-b^3x - a^3)^{\frac{1}{3}}\right)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(-b^3*x-a^3)^(1/3),x, algorithm="maxima")`

[Out] $\sqrt{3} \arctan(-1/3 \sqrt{3}) (a - 2(-b^3 x - a^3)^{1/3})/a + 1/2 \log(a^2 - (-b^3 x - a^3)^{1/3} a + (-b^3 x - a^3)^{2/3})/a - \log(a + (-b^3 x - a^3)^{1/3})/a$

mupad [B] time = 0.07, size = 115, normalized size = 1.51

$$\frac{\ln\left(9a + 9(-a^3 - xb^3)^{1/3}\right)}{a} - \frac{\ln\left(\frac{9a(-1+\sqrt{3}1i)^2}{4} + 9(-a^3 - xb^3)^{1/3}\right)(-1+\sqrt{3}1i)}{2a} + \frac{\ln\left(\frac{9a(1+\sqrt{3}1i)^2}{4} + 9(-a^3 - xb^3)^{1/3}\right)(-1-\sqrt{3}1i)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(-b^3*x - a^3)^(1/3)),x)`

[Out] $(\log((9a(3^{1/2}1i + 1)^2)/4 + 9(-b^3x - a^3)^{1/3})(3^{1/2}1i + 1))/(2a) - (\log((9a(3^{1/2}1i - 1)^2)/4 + 9(-b^3x - a^3)^{1/3})(3^{1/2}1i - 1))/(2a) - \log(9a + 9(-b^3x - a^3)^{1/3})/a$

sympy [C] time = 1.83, size = 139, normalized size = 1.83

$$\frac{\log\left(-\frac{ae^{\frac{2i\pi}{3}}}{b\sqrt[3]{\frac{a^3}{b^3}+x}}+1\right)\Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)} - \frac{e^{\frac{i\pi}{3}}\log\left(-\frac{ae^{\frac{4i\pi}{3}}}{b\sqrt[3]{\frac{a^3}{b^3}+x}}+1\right)\Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)} + \frac{e^{\frac{2i\pi}{3}}\log\left(-\frac{ae^{2i\pi}}{b\sqrt[3]{\frac{a^3}{b^3}+x}}+1\right)\Gamma\left(-\frac{1}{3}\right)}{3a\Gamma\left(\frac{2}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(-b**3*x-a**3)**(1/3),x)`

[Out] $\log(-a \exp_{\text{polar}}(2I\pi/3)/(b(a^3/b^3 + x)^{1/3}) + 1) \gamma(-1/3)/(3a \gamma(2/3)) - \exp(I\pi/3) \log(-a \exp_{\text{polar}}(4I\pi/3)/(b(a^3/b^3 + x)^{1/3}) + 1) \gamma(-1/3)/(3a \gamma(2/3)) + \exp(2I\pi/3) \log(-a \exp_{\text{polar}}(2I\pi)/(b(a^3/b^3 + x)^{1/3}) + 1) \gamma(-1/3)/(3a \gamma(2/3))$

$$3.424 \quad \int \frac{1}{x(a^3 + b^3x)^{2/3}} dx$$

Optimal. Leaf size=72

$$-\frac{\log(x)}{2a^2} + \frac{3 \log\left(a - \sqrt[3]{a^3 + b^3x}\right)}{2a^2} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3 + b^3x} + a}{\sqrt{3}a}\right)}{a^2}$$

[Out] $-1/2*\ln(x)/a^2+3/2*\ln(a-(b^3*x+a^3)^{(1/3)})/a^2-\arctan(1/3*(a+2*(b^3*x+a^3)^{(1/3)})/a*\sqrt[3]{a^3+b^3x})/\sqrt[3]{a^3+b^3x}/a^2$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {57, 617, 204, 31}

$$\frac{3 \log\left(a - \sqrt[3]{a^3 + b^3x}\right)}{2a^2} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3 + b^3x} + a}{\sqrt{3}a}\right)}{a^2} - \frac{\log(x)}{2a^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a^3 + b^3*x)^(2/3)),x]

[Out] $-\left(\frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{a + 2\sqrt[3]{a^3 + b^3x}}{\sqrt{3}a}\right]}{a^2}\right) - \frac{\operatorname{Log}[x]}{2a^2} + \frac{3 \operatorname{Log}\left[a - \sqrt[3]{a^3 + b^3x}\right]}{2a^2}$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 57

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2), x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[Rt[-b, 2]*x]/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x(a^3 + b^3x)^{2/3}} dx &= -\frac{\log(x)}{2a^2} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{a-x} dx, x, \sqrt[3]{a^3 + b^3x}\right)}{2a^2} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{a^2+ax+x^2} dx, x, \sqrt[3]{a^3 + b^3x}\right)}{2a} \\ &= -\frac{\log(x)}{2a^2} + \frac{3 \log\left(a - \sqrt[3]{a^3 + b^3x}\right)}{2a^2} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a^3+b^3x}}{a}\right)}{a^2} \\ &= -\frac{\sqrt{3} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a^3+b^3x}}{a}}{\sqrt{3}}\right)}{a^2} - \frac{\log(x)}{2a^2} + \frac{3 \log\left(a - \sqrt[3]{a^3 + b^3x}\right)}{2a^2} \end{aligned}$$

Mathematica [A] time = 0.03, size = 95, normalized size = 1.32

$$\frac{-2 \log\left(a - \sqrt[3]{a^3 + b^3x}\right) + 2\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3+b^3x}+a}{\sqrt{3}a}\right) + \log\left(a\sqrt[3]{a^3 + b^3x} + (a^3 + b^3x)^{2/3} + a^2\right)}{2a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a^3 + b^3*x)^(2/3)), x]

[Out] -1/2*(2*Sqrt[3]*ArcTan[(a + 2*(a^3 + b^3*x)^(1/3))/(Sqrt[3]*a)] - 2*Log[a - (a^3 + b^3*x)^(1/3)] + Log[a^2 + a*(a^3 + b^3*x)^(1/3) + (a^3 + b^3*x)^(2/3)])/a^2

fricas [A] time = 0.44, size = 86, normalized size = 1.19

$$\frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}a+2\sqrt{3}(b^3x+a^3)^{\frac{1}{3}}}{3a}\right) + \log\left(a^2 + (b^3x+a^3)^{\frac{1}{3}}a + (b^3x+a^3)^{\frac{2}{3}}\right) - 2 \log\left(-a + (b^3x+a^3)^{\frac{1}{3}}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b^3*x+a^3)^(2/3),x, algorithm="fricas")

[Out] $-\frac{1}{2} \cdot (2 \cdot \sqrt{3} \cdot \arctan(\frac{1}{3} \cdot (\sqrt{3} \cdot a + 2 \cdot \sqrt{3} \cdot (b^3 x + a^3)^{1/3})) / a) + \log(a^2 + (b^3 x + a^3)^{1/3} \cdot a + (b^3 x + a^3)^{2/3}) - 2 \cdot \log(-a + (b^3 x + a^3)^{1/3}) / a^2$

giac [A] time = 1.00, size = 88, normalized size = 1.22

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a+2\left(b^3x+a^3\right)^{\frac{1}{3}}\right)}{3a}\right)}{a^2} - \frac{\log\left(a^2 + \left(b^3x+a^3\right)^{\frac{1}{3}}a + \left(b^3x+a^3\right)^{\frac{2}{3}}\right)}{2a^2} + \frac{\log\left(\left|-a + \left(b^3x+a^3\right)^{\frac{1}{3}}\right|\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b^3*x+a^3)^(2/3),x, algorithm="giac")

[Out] $-\frac{\sqrt{3} \cdot \arctan(\frac{1}{3} \cdot \sqrt{3} \cdot (a + 2 \cdot (b^3 x + a^3)^{1/3})) / a}{a^2} - \frac{1}{2} \cdot \log(a^2 + (b^3 x + a^3)^{1/3} \cdot a + (b^3 x + a^3)^{2/3}) / a^2 + \log(\text{abs}(-a + (b^3 x + a^3)^{1/3})) / a^2$

maple [A] time = 0.01, size = 88, normalized size = 1.22

$$\frac{\sqrt{3} \arctan\left(\frac{\left(a+2\left(b^3x+a^3\right)^{\frac{1}{3}}\right)\sqrt{3}}{3a}\right)}{a^2} + \frac{\ln\left(-a + \left(b^3x+a^3\right)^{\frac{1}{3}}\right)}{a^2} - \frac{\ln\left(a^2 + \left(b^3x+a^3\right)^{\frac{1}{3}}a + \left(b^3x+a^3\right)^{\frac{2}{3}}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b^3*x+a^3)^(2/3),x)

[Out] $\frac{1}{a^2} \cdot \ln(-a + (b^3 x + a^3)^{1/3}) - \frac{1}{2} \cdot \frac{\ln(a^2 + (b^3 x + a^3)^{1/3} \cdot a + (b^3 x + a^3)^{2/3})}{a^2} - \frac{\arctan(\frac{1}{3} \cdot (a + 2 \cdot (b^3 x + a^3)^{1/3})) \cdot 3^{1/2} / a}{3^{1/2} / a^2}$

maxima [A] time = 2.88, size = 87, normalized size = 1.21

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a+2\left(b^3x+a^3\right)^{\frac{1}{3}}\right)}{3a}\right)}{a^2} - \frac{\log\left(a^2 + \left(b^3x+a^3\right)^{\frac{1}{3}}a + \left(b^3x+a^3\right)^{\frac{2}{3}}\right)}{2a^2} + \frac{\log\left(-a + \left(b^3x+a^3\right)^{\frac{1}{3}}\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b^3*x+a^3)^(2/3),x, algorithm="maxima")

[Out] $-\sqrt{3} \arctan\left(\frac{1}{3}\sqrt{3}\right) \frac{(a + 2(b^3x + a^3)^{1/3})/a}{a^2} - \frac{1}{2} \log\left(\frac{a^2 + (b^3x + a^3)^{1/3}a + (b^3x + a^3)^{2/3}}{a^2} + \log\left(\frac{-a + (b^3x + a^3)^{1/3}}{a^2}\right)\right)$

mupad [B] time = 0.14, size = 101, normalized size = 1.40

$$\frac{\ln\left(9a - 9(a^3 + xb^3)^{1/3}\right)}{a^2} + \frac{\ln\left(9(a^3 + xb^3)^{1/3} - \frac{9a(-1+\sqrt{3}1i)}{2}\right)}{2a^2} - \frac{\ln\left(9(a^3 + xb^3)^{1/3} + \frac{9a(1+\sqrt{3}1i)}{2}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(b^3*x + a^3)^(2/3)),x)`

[Out] $\log(9a - 9(b^3x + a^3)^{1/3})/a^2 + (\log(9(b^3x + a^3)^{1/3}) - (9a(3^{1/2}1i - 1))/2) \cdot (3^{1/2}1i - 1)/(2a^2) - (\log(9(b^3x + a^3)^{1/3}) + (9a(3^{1/2}1i + 1))/2) \cdot (3^{1/2}1i + 1)/(2a^2)$

sympy [C] time = 1.86, size = 134, normalized size = 1.86

$$\frac{\log\left(1 - \frac{b\sqrt[3]{\frac{a^3}{b^3} + x}}{a}\right) \Gamma\left(\frac{1}{3}\right)}{3a^2 \Gamma\left(\frac{4}{3}\right)} + \frac{e^{-\frac{2i\pi}{3}} \log\left(1 - \frac{b\sqrt[3]{\frac{a^3}{b^3} + x} e^{\frac{2i\pi}{3}}}{a}\right) \Gamma\left(\frac{1}{3}\right)}{3a^2 \Gamma\left(\frac{4}{3}\right)} + \frac{e^{\frac{2i\pi}{3}} \log\left(1 - \frac{b\sqrt[3]{\frac{a^3}{b^3} + x} e^{\frac{4i\pi}{3}}}{a}\right) \Gamma\left(\frac{1}{3}\right)}{3a^2 \Gamma\left(\frac{4}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b**3*x+a**3)**(2/3),x)`

[Out] $\log(1 - b(a^3/b^3 + x)^{1/3}/a) \gamma(1/3)/(3a^2 \gamma(4/3)) + \exp(-i\pi/3) \log(1 - b(a^3/b^3 + x)^{1/3} \exp_{\text{polar}}(2i\pi/3)/a) \gamma(1/3)/(3a^2 \gamma(4/3)) + \exp(2i\pi/3) \log(1 - b(a^3/b^3 + x)^{1/3} \exp_{\text{polar}}(4i\pi/3)/a) \gamma(1/3)/(3a^2 \gamma(4/3))$

$$3.425 \quad \int \frac{1}{x(a^3 - b^3x)^{2/3}} dx$$

Optimal. Leaf size=74

$$-\frac{\log(x)}{2a^2} + \frac{3 \log\left(a - \sqrt[3]{a^3 - b^3x}\right)}{2a^2} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3 - b^3x} + a}{\sqrt{3}a}\right)}{a^2}$$

[Out] $-1/2*\ln(x)/a^2+3/2*\ln(a-(-b^3*x+a^3)^{(1/3)})/a^2-\arctan(1/3*(a+2*(-b^3*x+a^3)^{(1/3)})/a*\sqrt[3]{a^3-b^3x})/a^2$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {57, 617, 204, 31}

$$\frac{3 \log\left(a - \sqrt[3]{a^3 - b^3x}\right)}{2a^2} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3 - b^3x} + a}{\sqrt{3}a}\right)}{a^2} - \frac{\log(x)}{2a^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(a^3 - b^3*x)^(2/3)),x]

[Out] $-\left(\frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{a + 2\sqrt[3]{a^3 - b^3x}}{\sqrt{3}a}\right]}{a^2}\right) - \frac{\operatorname{Log}[x]}{2a^2} + \frac{3 \operatorname{Log}\left[a - \sqrt[3]{a^3 - b^3x}\right]}{2a^2}$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 57

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2), x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])]) /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[Rt[-b, 2]*x]/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x(a^3 - b^3x)^{2/3}} dx &= -\frac{\log(x)}{2a^2} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{a-x} dx, x, \sqrt[3]{a^3 - b^3x}\right)}{2a^2} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{a^2+ax+x^2} dx, x, \sqrt[3]{a^3 - b^3x}\right)}{2a} \\ &= -\frac{\log(x)}{2a^2} + \frac{3 \log\left(a - \sqrt[3]{a^3 - b^3x}\right)}{2a^2} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{a^3 - b^3x}}{a}\right)}{a^2} \\ &= -\frac{\sqrt{3} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{a^3 - b^3x}}{a}}{\sqrt{3}}\right)}{a^2} - \frac{\log(x)}{2a^2} + \frac{3 \log\left(a - \sqrt[3]{a^3 - b^3x}\right)}{2a^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 99, normalized size = 1.34

$$\frac{-2 \log\left(a - \sqrt[3]{a^3 - b^3x}\right) + 2\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{a^3 - b^3x} + a}{\sqrt{3}a}\right) + \log\left(a\sqrt[3]{a^3 - b^3x} + (a^3 - b^3x)^{2/3} + a^2\right)}{2a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(a^3 - b^3*x)^(2/3)), x]

[Out] -1/2*(2*Sqrt[3]*ArcTan[(a + 2*(a^3 - b^3*x)^(1/3))/(Sqrt[3]*a)] - 2*Log[a - (a^3 - b^3*x)^(1/3)] + Log[a^2 + a*(a^3 - b^3*x)^(1/3) + (a^3 - b^3*x)^(2/3)])/a^2

fricas [A] time = 0.45, size = 90, normalized size = 1.22

$$\frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}a+2\sqrt{3}(-b^3x+a^3)^{\frac{1}{3}}}{3a}\right) + \log\left(a^2 + (-b^3x+a^3)^{\frac{1}{3}}a + (-b^3x+a^3)^{\frac{2}{3}}\right) - 2 \log\left(-a + (-b^3x+a^3)^{\frac{1}{3}}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(-b^3*x+a^3)^(2/3),x, algorithm="fricas")

[Out] $-\frac{1}{2} \cdot (2 \cdot \sqrt{3} \cdot \arctan(\frac{1}{3} \cdot (\sqrt{3} \cdot a + 2 \cdot \sqrt{3} \cdot (-b^3 x + a^3)^{1/3})) / a) + \log(a^2 + (-b^3 x + a^3)^{1/3} \cdot a + (-b^3 x + a^3)^{2/3}) - 2 \cdot \log(-a + (-b^3 x + a^3)^{1/3}) / a^2$

giac [A] time = 1.09, size = 92, normalized size = 1.24

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a+2(-b^3x+a^3)^{\frac{1}{3}}\right)}{3a}\right)}{a^2} - \frac{\log\left(a^2 + (-b^3x+a^3)^{\frac{1}{3}}a + (-b^3x+a^3)^{\frac{2}{3}}\right)}{2a^2} + \frac{\log\left(\left|-a + (-b^3x+a^3)^{\frac{1}{3}}\right|\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(-b^3*x+a^3)^(2/3),x, algorithm="giac")

[Out] $-\frac{\sqrt{3} \cdot \arctan(\frac{1}{3} \cdot \sqrt{3} \cdot (a + 2 \cdot (-b^3 x + a^3)^{1/3})) / a}{a^2} - \frac{1}{2} \cdot \log(a^2 + (-b^3 x + a^3)^{1/3} \cdot a + (-b^3 x + a^3)^{2/3}) / a^2 + \log(\text{abs}(-a + (-b^3 x + a^3)^{1/3})) / a^2$

maple [A] time = 0.00, size = 92, normalized size = 1.24

$$\frac{\sqrt{3} \arctan\left(\frac{\left(a+2(-b^3x+a^3)^{\frac{1}{3}}\right)\sqrt{3}}{3a}\right)}{a^2} + \frac{\ln\left(-a + (-b^3x+a^3)^{\frac{1}{3}}\right)}{a^2} - \frac{\ln\left(a^2 + (-b^3x+a^3)^{\frac{1}{3}}a + (-b^3x+a^3)^{\frac{2}{3}}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(-b^3*x+a^3)^(2/3),x)

[Out] $\frac{1}{a^2} \cdot \ln(-a + (-b^3 x + a^3)^{1/3}) - \frac{1}{2} \cdot \frac{\ln(a^2 + (-b^3 x + a^3)^{1/3} \cdot a + (-b^3 x + a^3)^{2/3})}{a^2} - \frac{\arctan(\frac{1}{3} \cdot (a + 2 \cdot (-b^3 x + a^3)^{1/3})) \cdot 3^{1/2}}{a^2}$

maxima [A] time = 2.98, size = 91, normalized size = 1.23

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a+2(-b^3x+a^3)^{\frac{1}{3}}\right)}{3a}\right)}{a^2} - \frac{\log\left(a^2 + (-b^3x+a^3)^{\frac{1}{3}}a + (-b^3x+a^3)^{\frac{2}{3}}\right)}{2a^2} + \frac{\log\left(-a + (-b^3x+a^3)^{\frac{1}{3}}\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(-b^3*x+a^3)^(2/3),x, algorithm="maxima")

[Out] $-\sqrt{3} \arctan\left(\frac{1}{3}\sqrt{3}(a + 2(-b^3x + a^3)^{1/3})/a\right)/a^2 - \frac{1}{2}\log(a^2 + (-b^3x + a^3)^{1/3})a + (-b^3x + a^3)^{2/3}/a^2 + \log(-a + (-b^3x + a^3)^{1/3})/a^2$

mupad [B] time = 0.11, size = 104, normalized size = 1.41

$$\frac{\ln\left(9a - 9(a^3 - b^3x)^{1/3}\right)}{a^2} + \frac{\ln\left(9(a^3 - b^3x)^{1/3} - \frac{9a(-1 + \sqrt{3}1i)}{2}\right)(-1 + \sqrt{3}1i)}{2a^2} - \frac{\ln\left(9(a^3 - b^3x)^{1/3} + \frac{9a(1 + \sqrt{3}1i)}{2}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(a^3 - b^3*x)^(2/3)),x)`

[Out] $\log(9a - 9(a^3 - b^3x)^{1/3})/a^2 + (\log(9(a^3 - b^3x)^{1/3}) - (9a*(3^{1/2}*1i - 1))/2)*(3^{1/2}*1i - 1)/(2*a^2) - (\log(9(a^3 - b^3x)^{1/3}) + (9a*(3^{1/2}*1i + 1))/2)*(3^{1/2}*1i + 1)/(2*a^2)$

sympy [C] time = 1.92, size = 136, normalized size = 1.84

$$\frac{\log\left(1 - \frac{b\sqrt[3]{-\frac{a^3}{b^3} + xe^{\frac{i\pi}{3}}}}{a}\right)\Gamma\left(\frac{1}{3}\right)}{3a^2\Gamma\left(\frac{4}{3}\right)} - \frac{e^{\frac{i\pi}{3}}\log\left(1 - \frac{b\sqrt[3]{-\frac{a^3}{b^3} + xe^{i\pi}}}}{a}\right)\Gamma\left(\frac{1}{3}\right)}{3a^2\Gamma\left(\frac{4}{3}\right)} + \frac{e^{\frac{2i\pi}{3}}\log\left(1 - \frac{b\sqrt[3]{-\frac{a^3}{b^3} + xe^{\frac{5i\pi}{3}}}}{a}\right)\Gamma\left(\frac{1}{3}\right)}{3a^2\Gamma\left(\frac{4}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(-b**3*x+a**3)**(2/3),x)`

[Out] $\log(1 - b*(-a**3/b**3 + x)**(1/3)*\exp_polar(I*pi/3)/a)*\gamma(1/3)/(3*a**2*\gamma(4/3)) - \exp(I*pi/3)*\log(1 - b*(-a**3/b**3 + x)**(1/3)*\exp_polar(I*pi)/a)*\gamma(1/3)/(3*a**2*\gamma(4/3)) + \exp(2*I*pi/3)*\log(1 - b*(-a**3/b**3 + x)**(1/3)*\exp_polar(5*I*pi/3)/a)*\gamma(1/3)/(3*a**2*\gamma(4/3))$

$$3.426 \quad \int \frac{1}{x(-a^3+b^3x)^{2/3}} dx$$

Optimal. Leaf size=74

$$-\frac{\log(x)}{2a^2} + \frac{3 \log\left(\sqrt[3]{b^3x-a^3} + a\right)}{2a^2} - \frac{\sqrt{3} \tan^{-1}\left(\frac{a-2\sqrt[3]{b^3x-a^3}}{\sqrt{3}a}\right)}{a^2}$$

[Out] $-1/2*\ln(x)/a^2+3/2*\ln(a+(\sqrt[3]{b^3*x-a^3})^{1/3})/a^2-\arctan(1/3*(a-2*(\sqrt[3]{b^3*x-a^3})^{1/3})/a*\sqrt[3]{1/2})*\sqrt[3]{1/2}/a^2$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {58, 617, 204, 31}

$$\frac{3 \log\left(\sqrt[3]{b^3x-a^3} + a\right)}{2a^2} - \frac{\sqrt{3} \tan^{-1}\left(\frac{a-2\sqrt[3]{b^3x-a^3}}{\sqrt{3}a}\right)}{a^2} - \frac{\log(x)}{2a^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(-a^3 + b^3*x)^(2/3)),x]

[Out] $-\left(\frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{a-2\sqrt[3]{b^3x-a^3}}{\sqrt{3}a}\right]}{a^2}\right) - \frac{\operatorname{Log}[x]}{(2a^2) + (3 \operatorname{Log}[a + (\sqrt[3]{b^3x-a^3})^{1/3}])/(2a^2)}$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 58

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]) /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[Rt[-b, 2]*x]/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x(-a^3 + b^3x)^{2/3}} dx &= -\frac{\log(x)}{2a^2} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{a+x} dx, x, \sqrt[3]{-a^3 + b^3x}\right)}{2a^2} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{a^2 - ax + x^2} dx, x, \sqrt[3]{-a^3 + b^3x}\right)}{2a} \\ &= -\frac{\log(x)}{2a^2} + \frac{3 \log\left(a + \sqrt[3]{-a^3 + b^3x}\right)}{2a^2} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{-a^3 + b^3x}}{a}\right)}{a^2} \\ &= -\frac{\sqrt{3} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{-a^3 + b^3x}}{a}}{\sqrt{3}}\right)}{a^2} - \frac{\log(x)}{2a^2} + \frac{3 \log\left(a + \sqrt[3]{-a^3 + b^3x}\right)}{2a^2} \end{aligned}$$

Mathematica [A] time = 0.03, size = 108, normalized size = 1.46

$$\frac{\log\left(\sqrt[3]{b^3x - a^3} + a\right)}{a^2} - \frac{\log\left(-a\sqrt[3]{b^3x - a^3} + (b^3x - a^3)^{2/3} + a^2\right)}{2a^2} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{b^3x - a^3} - a}{\sqrt{3}a}\right)}{a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(-a^3 + b^3*x)^(2/3)), x]

[Out] (Sqrt[3]*ArcTan[(-a + 2*(-a^3 + b^3*x)^(1/3))/(Sqrt[3]*a)]/a^2 + Log[a + (-a^3 + b^3*x)^(1/3)]/a^2 - Log[a^2 - a*(-a^3 + b^3*x)^(1/3) + (-a^3 + b^3*x)^(2/3)]/(2*a^2)

fricas [A] time = 0.43, size = 95, normalized size = 1.28

$$\frac{2\sqrt{3} \arctan\left(-\frac{\sqrt{3}a - 2\sqrt{3}(b^3x - a^3)^{1/3}}{3a}\right) - \log\left(a^2 - (b^3x - a^3)^{1/3}a + (b^3x - a^3)^{2/3}\right) + 2 \log\left(a + (b^3x - a^3)^{1/3}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b^3*x-a^3)^(2/3),x, algorithm="fricas")

[Out] $\frac{1}{2} \cdot (2 \cdot \sqrt{3} \cdot \arctan(-\frac{1}{3} \cdot (\sqrt{3} \cdot a - 2 \cdot \sqrt{3} \cdot (b^3 x - a^3)^{1/3})) / a) - \log(a^2 - (b^3 x - a^3)^{1/3} \cdot a + (b^3 x - a^3)^{2/3}) + 2 \cdot \log(a + (b^3 x - a^3)^{1/3})) / a^2$

giac [A] time = 0.99, size = 94, normalized size = 1.27

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a-2\left(b^3x-a^3\right)^{\frac{1}{3}}\right)}{3a}\right)}{a^2} - \frac{\log\left(a^2 - \left(b^3x - a^3\right)^{\frac{1}{3}}a + \left(b^3x - a^3\right)^{\frac{2}{3}}\right)}{2a^2} + \frac{\log\left(a + \left(b^3x - a^3\right)^{\frac{1}{3}}\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b^3*x-a^3)^(2/3),x, algorithm="giac")

[Out] $\frac{\sqrt{3} \cdot \arctan(-\frac{1}{3} \cdot \sqrt{3} \cdot (a - 2 \cdot (b^3 x - a^3)^{1/3})) / a}{a^2} - \frac{1}{2} \cdot \log(a^2 - (b^3 x - a^3)^{1/3} \cdot a + (b^3 x - a^3)^{2/3}) / a^2 + \log(\text{abs}(a + (b^3 x - a^3)^{1/3})) / a^2$

maple [A] time = 0.01, size = 96, normalized size = 1.30

$$\frac{\sqrt{3} \arctan\left(\frac{\left(-a+2\left(b^3x-a^3\right)^{\frac{1}{3}}\right)\sqrt{3}}{3a}\right)}{a^2} + \frac{\ln\left(a + \left(b^3x - a^3\right)^{\frac{1}{3}}\right)}{a^2} - \frac{\ln\left(a^2 - \left(b^3x - a^3\right)^{\frac{1}{3}}a + \left(b^3x - a^3\right)^{\frac{2}{3}}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b^3*x-a^3)^(2/3),x)

[Out] $-\frac{1}{2} \cdot \frac{\ln(a^2 - (b^3 x - a^3)^{1/3} \cdot a + (b^3 x - a^3)^{2/3})}{a^2} + \frac{1}{a^2} \cdot \frac{3^{1/2} \cdot \arctan\left(\frac{1}{3} \cdot (-a + 2 \cdot (b^3 x - a^3)^{1/3}) \cdot 3^{1/2}\right)}{a} + \frac{\ln(a + (b^3 x - a^3)^{1/3})}{a^2}$

maxima [A] time = 2.95, size = 93, normalized size = 1.26

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a-2\left(b^3x-a^3\right)^{\frac{1}{3}}\right)}{3a}\right)}{a^2} - \frac{\log\left(a^2 - \left(b^3x - a^3\right)^{\frac{1}{3}}a + \left(b^3x - a^3\right)^{\frac{2}{3}}\right)}{2a^2} + \frac{\log\left(a + \left(b^3x - a^3\right)^{\frac{1}{3}}\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b^3*x-a^3)^(2/3),x, algorithm="maxima")

[Out] $\sqrt{3} \arctan(-1/3 \sqrt{3} (a - 2(b^3 x - a^3)^{1/3})/a) / a^2 - 1/2 \log(a^2 - (b^3 x - a^3)^{1/3} a + (b^3 x - a^3)^{2/3}) / a^2 + \log(a + (b^3 x - a^3)^{1/3}) / a^2$

mupad [B] time = 0.16, size = 107, normalized size = 1.45

$$\frac{\ln\left(9a + 9(b^3 x - a^3)^{1/3}\right)}{a^2} + \frac{\ln\left(9(b^3 x - a^3)^{1/3} + \frac{9a(-1 + \sqrt{3} 1i)}{2}\right)}{2a^2} - \frac{\ln\left(9(b^3 x - a^3)^{1/3} - \frac{9a(1 + \sqrt{3} 1i)}{2}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(b^3*x - a^3)^(2/3)),x)`

[Out] $\log(9a + 9(b^3 x - a^3)^{1/3}) / a^2 + (\log(9(b^3 x - a^3)^{1/3} + (9a*(3^{1/2}*1i - 1))/2) * (3^{1/2}*1i - 1)) / (2*a^2) - (\log(9(b^3 x - a^3)^{1/3} - (9a*(3^{1/2}*1i + 1))/2) * (3^{1/2}*1i + 1)) / (2*a^2)$

sympy [C] time = 1.98, size = 134, normalized size = 1.81

$$\frac{e^{-\frac{i\pi}{3}} \log\left(1 - \frac{b^3 \sqrt{-\frac{a^3}{b^3} + x} e^{\frac{i\pi}{3}}}{a}\right) \Gamma\left(\frac{1}{3}\right)}{3a^2 \Gamma\left(\frac{4}{3}\right)} + \frac{\log\left(1 - \frac{b^3 \sqrt{-\frac{a^3}{b^3} + x} e^{i\pi}}{a}\right) \Gamma\left(\frac{1}{3}\right)}{3a^2 \Gamma\left(\frac{4}{3}\right)} - \frac{e^{\frac{i\pi}{3}} \log\left(1 - \frac{b^3 \sqrt{-\frac{a^3}{b^3} + x} e^{\frac{5i\pi}{3}}}{a}\right) \Gamma\left(\frac{1}{3}\right)}{3a^2 \Gamma\left(\frac{4}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b**3*x-a**3)**(2/3),x)`

[Out] $-\exp(-I\pi/3) \log(1 - b*(-a**3/b**3 + x)**(1/3) \exp_polar(I\pi/3)/a) * \gamma(1/3) / (3*a**2*\gamma(4/3)) + \log(1 - b*(-a**3/b**3 + x)**(1/3) \exp_polar(I\pi)/a) * \gamma(1/3) / (3*a**2*\gamma(4/3)) - \exp(I\pi/3) \log(1 - b*(-a**3/b**3 + x)**(1/3) \exp_polar(5*I\pi/3)/a) * \gamma(1/3) / (3*a**2*\gamma(4/3))$

$$3.427 \quad \int \frac{1}{x(-a^3 - b^3x)^{2/3}} dx$$

Optimal. Leaf size=76

$$-\frac{\log(x)}{2a^2} + \frac{3 \log\left(\sqrt[3]{-a^3 - b^3x} + a\right)}{2a^2} - \frac{\sqrt{3} \tan^{-1}\left(\frac{a-2\sqrt[3]{-a^3 - b^3x}}{\sqrt{3}a}\right)}{a^2}$$

[Out] $-1/2*\ln(x)/a^2+3/2*\ln(a+(-b^3*x-a^3)^{(1/3)})/a^2-\arctan(1/3*(a-2*(-b^3*x-a^3)^{(1/3)})/a*\sqrt{3})/\sqrt{3}/a^2$

Rubi [A] time = 0.02, antiderivative size = 76, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {58, 617, 204, 31}

$$\frac{3 \log\left(\sqrt[3]{-a^3 - b^3x} + a\right)}{2a^2} - \frac{\sqrt{3} \tan^{-1}\left(\frac{a-2\sqrt[3]{-a^3 - b^3x}}{\sqrt{3}a}\right)}{a^2} - \frac{\log(x)}{2a^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(-a^3 - b^3*x)^(2/3)),x]

[Out] $-\left(\frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{a - 2(-a^3 - b^3x)^{1/3}}{\sqrt{3}a}\right]}{a^2}\right) - \frac{\operatorname{Log}[x]}{(2a^2) + (3 \operatorname{Log}[a + (-a^3 - b^3x)^{1/3}])/(2a^2)}$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 58

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]) /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[Rt[-b, 2]*x]/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x(-a^3 - b^3x)^{2/3}} dx &= -\frac{\log(x)}{2a^2} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{a+x} dx, x, \sqrt[3]{-a^3 - b^3x}\right)}{2a^2} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{a^2 - ax + x^2} dx, x, \sqrt[3]{-a^3 - b^3x}\right)}{2a} \\ &= -\frac{\log(x)}{2a^2} + \frac{3 \log\left(a + \sqrt[3]{-a^3 - b^3x}\right)}{2a^2} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{-a^3 - b^3x}}{a}\right)}{a^2} \\ &= -\frac{\sqrt{3} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{-a^3 - b^3x}}{a}}{\sqrt{3}}\right)}{a^2} - \frac{\log(x)}{2a^2} + \frac{3 \log\left(a + \sqrt[3]{-a^3 - b^3x}\right)}{2a^2} \end{aligned}$$

Mathematica [A] time = 0.03, size = 112, normalized size = 1.47

$$\frac{\log\left(\sqrt[3]{-a^3 - b^3x} + a\right)}{a^2} - \frac{\log\left(-a\sqrt[3]{-a^3 - b^3x} + (-a^3 - b^3x)^{2/3} + a^2\right)}{2a^2} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{-a^3 - b^3x} - a}{\sqrt{3}a}\right)}{a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(-a^3 - b^3*x)^(2/3)), x]

[Out] (Sqrt[3]*ArcTan[(-a + 2*(-a^3 - b^3*x)^(1/3))/(Sqrt[3]*a)]/a^2 + Log[a + (-a^3 - b^3*x)^(1/3)]/a^2 - Log[a^2 - a*(-a^3 - b^3*x)^(1/3) + (-a^3 - b^3*x)^(2/3)]/(2*a^2)

fricas [A] time = 0.44, size = 99, normalized size = 1.30

$$\frac{2\sqrt{3} \arctan\left(-\frac{\sqrt{3}a - 2\sqrt{3}(-b^3x - a^3)^{1/3}}{3a}\right) - \log\left(a^2 - (-b^3x - a^3)^{1/3}a + (-b^3x - a^3)^{2/3}\right) + 2 \log\left(a + (-b^3x - a^3)^{1/3}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(-b^3*x-a^3)^(2/3),x, algorithm="fricas")

[Out] $\frac{1}{2} * (2 * \sqrt{3} * \arctan(-\frac{1}{3} * (\sqrt{3} * a - 2 * \sqrt{3} * (-b^3 * x - a^3)^{1/3})) / a - \log(a^2 - (-b^3 * x - a^3)^{1/3} * a + (-b^3 * x - a^3)^{2/3})) + 2 * \log(a + (-b^3 * x - a^3)^{1/3})) / a^2$

giac [A] time = 1.07, size = 98, normalized size = 1.29

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a-2(-b^3x-a^3)^{\frac{1}{3}}\right)}{3a}\right)}{a^2} - \frac{\log\left(a^2 - (-b^3x - a^3)^{\frac{1}{3}}a + (-b^3x - a^3)^{\frac{2}{3}}\right)}{2a^2} + \frac{\log\left(a + (-b^3x - a^3)^{\frac{1}{3}}\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(-b^3*x-a^3)^(2/3),x, algorithm="giac")

[Out] $\sqrt{3} * \arctan(-\frac{1}{3} * \sqrt{3} * (a - 2 * (-b^3 * x - a^3)^{1/3})) / a / a^2 - \frac{1}{2} * \log(a^2 - (-b^3 * x - a^3)^{1/3} * a + (-b^3 * x - a^3)^{2/3}) / a^2 + \log(\text{abs}(a + (-b^3 * x - a^3)^{1/3})) / a^2$

maple [A] time = 0.00, size = 100, normalized size = 1.32

$$\frac{\sqrt{3} \arctan\left(\frac{\left(-a+2(-b^3x-a^3)^{\frac{1}{3}}\right)\sqrt{3}}{3a}\right)}{a^2} + \frac{\ln\left(a + (-b^3x - a^3)^{\frac{1}{3}}\right)}{a^2} - \frac{\ln\left(a^2 - (-b^3x - a^3)^{\frac{1}{3}}a + (-b^3x - a^3)^{\frac{2}{3}}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(-b^3*x-a^3)^(2/3),x)

[Out] $-\frac{1}{2} * a^{-2} * \ln(a^2 - (-b^3 * x - a^3)^{1/3} * a + (-b^3 * x - a^3)^{2/3}) + \frac{1}{a^2} * 3^{1/2} * \arctan(\frac{1}{3} * (-a + 2 * (-b^3 * x - a^3)^{1/3})) * 3^{1/2} / a + \ln(a + (-b^3 * x - a^3)^{1/3}) / a^2$

maxima [A] time = 2.89, size = 97, normalized size = 1.28

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(a-2(-b^3x-a^3)^{\frac{1}{3}}\right)}{3a}\right)}{a^2} - \frac{\log\left(a^2 - (-b^3x - a^3)^{\frac{1}{3}}a + (-b^3x - a^3)^{\frac{2}{3}}\right)}{2a^2} + \frac{\log\left(a + (-b^3x - a^3)^{\frac{1}{3}}\right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(-b^3*x-a^3)^(2/3),x, algorithm="maxima")

[Out] $\sqrt{3} \arctan(-1/3 \sqrt{3} (a - 2(-b^3 x - a^3)^{1/3})/a) / a^2 - 1/2 \log(a^2 - (-b^3 x - a^3)^{1/3} a + (-b^3 x - a^3)^{2/3}) / a^2 + \log(a + (-b^3 x - a^3)^{1/3}) / a^2$

mupad [B] time = 0.16, size = 110, normalized size = 1.45

$$\frac{\ln\left(9a + 9(-a^3 - xb^3)^{1/3}\right)}{a^2} + \frac{\ln\left(9(-a^3 - xb^3)^{1/3} + \frac{9a(-1 + \sqrt{3}1i)}{2}\right)(-1 + \sqrt{3}1i)}{2a^2} - \frac{\ln\left(9(-a^3 - xb^3)^{1/3} - \frac{9a(1 + \sqrt{3}1i)}{2}\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(-b^3*x - a^3)^(2/3)),x)`

[Out] $\log(9a + 9(-b^3 x - a^3)^{1/3}) / a^2 + (\log(9(-b^3 x - a^3)^{1/3}) + (9a(3^{1/2}1i - 1))/2) * (3^{1/2}1i - 1) / (2a^2) - (\log(9(-b^3 x - a^3)^{1/3}) - (9a(3^{1/2}1i + 1))/2) * (3^{1/2}1i + 1) / (2a^2)$

sympy [C] time = 1.90, size = 133, normalized size = 1.75

$$\frac{e^{-\frac{2i\pi}{3}} \log\left(1 - \frac{b\sqrt[3]{\frac{a^3}{b^3} + x}}{a}\right) \Gamma\left(\frac{1}{3}\right)}{3a^2 \Gamma\left(\frac{4}{3}\right)} - \frac{e^{-\frac{i\pi}{3}} \log\left(1 - \frac{b\sqrt[3]{\frac{a^3}{b^3} + xe^{\frac{2i\pi}{3}}}}{a}\right) \Gamma\left(\frac{1}{3}\right)}{3a^2 \Gamma\left(\frac{4}{3}\right)} + \frac{\log\left(1 - \frac{b\sqrt[3]{\frac{a^3}{b^3} + xe^{\frac{4i\pi}{3}}}}{a}\right) \Gamma\left(\frac{1}{3}\right)}{3a^2 \Gamma\left(\frac{4}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(-b**3*x-a**3)**(2/3),x)`

[Out] $\exp(-2I\pi/3) \log(1 - b(a^3/b^3 + x)^{1/3}/a) \gamma(1/3) / (3a^2 \gamma(4/3)) - \exp(-I\pi/3) \log(1 - b(a^3/b^3 + x)^{1/3}) \exp_{\text{polar}}(2I\pi/3) / a \gamma(1/3) / (3a^2 \gamma(4/3)) + \log(1 - b(a^3/b^3 + x)^{1/3}) \exp_{\text{polar}}(4I\pi/3) / a \gamma(1/3) / (3a^2 \gamma(4/3))$

3.428 $\int x^m(a + bx) dx$

Optimal. Leaf size=25

$$\frac{ax^{m+1}}{m+1} + \frac{bx^{m+2}}{m+2}$$

[Out] $a*x^{(1+m)}/(1+m)+b*x^{(2+m)}/(2+m)$

Rubi [A] time = 0.01, antiderivative size = 25, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{ax^{m+1}}{m+1} + \frac{bx^{m+2}}{m+2}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x), x]

[Out] (a*x^(1 + m))/(1 + m) + (b*x^(2 + m))/(2 + m)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^m(a + bx) dx &= \int (ax^m + bx^{1+m}) dx \\ &= \frac{ax^{1+m}}{1+m} + \frac{bx^{2+m}}{2+m} \end{aligned}$$

Mathematica [A] time = 0.02, size = 22, normalized size = 0.88

$$x^{m+1} \left(\frac{a}{m+1} + \frac{bx}{m+2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x), x]

[Out] x^(1 + m)*(a/(1 + m) + (b*x)/(2 + m))

fricas [A] time = 0.44, size = 33, normalized size = 1.32

$$\frac{((bm + b)x^2 + (am + 2a)x)x^m}{m^2 + 3m + 2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a),x, algorithm="fricas")

[Out] ((b*m + b)*x^2 + (a*m + 2*a)*x)*x^m/(m^2 + 3*m + 2)

giac [A] time = 1.01, size = 43, normalized size = 1.72

$$\frac{bmx^2x^m + amxx^m + bx^2x^m + 2axx^m}{m^2 + 3m + 2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a),x, algorithm="giac")

[Out] (b*m*x^2*x^m + a*m*x*x^m + b*x^2*x^m + 2*a*x*x^m)/(m^2 + 3*m + 2)

maple [A] time = 0.00, size = 31, normalized size = 1.24

$$\frac{(bmx + am + bx + 2a)x^{m+1}}{(m + 2)(m + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(b*x+a),x)

[Out] x^(1+m)*(b*m*x+a*m+b*x+2*a)/(2+m)/(1+m)

maxima [A] time = 1.34, size = 25, normalized size = 1.00

$$\frac{bx^{m+2}}{m+2} + \frac{ax^{m+1}}{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a),x, algorithm="maxima")

[Out] b*x^(m + 2)/(m + 2) + a*x^(m + 1)/(m + 1)

mupad [B] time = 0.31, size = 30, normalized size = 1.20

$$\frac{x^{m+1} (2a + am + bx + bmx)}{m^2 + 3m + 2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(a + b*x), x)`

[Out] $(x^{(m + 1)}*(2*a + a*m + b*x + b*m*x))/(3*m + m^2 + 2)$

sympy [A] time = 0.30, size = 87, normalized size = 3.48

$$\begin{cases} -\frac{a}{x} + b \log(x) & \text{for } m = -2 \\ a \log(x) + bx & \text{for } m = -1 \\ \frac{amx^m}{m^2+3m+2} + \frac{2axx^m}{m^2+3m+2} + \frac{bmx^2x^m}{m^2+3m+2} + \frac{bx^2x^m}{m^2+3m+2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m*(b*x+a), x)`

[Out] `Piecewise((-a/x + b*log(x), Eq(m, -2)), (a*log(x) + b*x, Eq(m, -1)), (a*m*x*x**m/(m**2 + 3*m + 2) + 2*a*x*x**m/(m**2 + 3*m + 2) + b*m*x**2*x**m/(m**2 + 3*m + 2) + b*x**2*x**m/(m**2 + 3*m + 2), True))`

$$3.429 \quad \int x^{5/2}(a + bx) dx$$

Optimal. Leaf size=21

$$\frac{2}{7}ax^{7/2} + \frac{2}{9}bx^{9/2}$$

[Out] $2/7*a*x^{(7/2)}+2/9*b*x^{(9/2)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{2}{7}ax^{7/2} + \frac{2}{9}bx^{9/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(5/2)}*(a + b*x), x]$

[Out] $(2*a*x^{(7/2)})/7 + (2*b*x^{(9/2)})/9$

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^{5/2}(a + bx) dx &= \int (ax^{5/2} + bx^{7/2}) dx \\ &= \frac{2}{7}ax^{7/2} + \frac{2}{9}bx^{9/2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 0.81

$$\frac{2}{63}x^{7/2}(9a + 7bx)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(5/2)}*(a + b*x), x]$

[Out] $(2*x^{(7/2)}*(9*a + 7*b*x))/63$

fricas [A] time = 0.46, size = 18, normalized size = 0.86

$$\frac{2}{63} (7bx^4 + 9ax^3)\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a),x, algorithm="fricas")

[Out] 2/63*(7*b*x^4 + 9*a*x^3)*sqrt(x)

giac [A] time = 0.83, size = 13, normalized size = 0.62

$$\frac{2}{9}bx^{\frac{9}{2}} + \frac{2}{7}ax^{\frac{7}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a),x, algorithm="giac")

[Out] 2/9*b*x^(9/2) + 2/7*a*x^(7/2)

maple [A] time = 0.00, size = 14, normalized size = 0.67

$$\frac{2(7bx + 9a)x^{\frac{7}{2}}}{63}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(b*x+a),x)

[Out] 2/63*x^(7/2)*(7*b*x+9*a)

maxima [A] time = 1.33, size = 13, normalized size = 0.62

$$\frac{2}{9}bx^{\frac{9}{2}} + \frac{2}{7}ax^{\frac{7}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a),x, algorithm="maxima")

[Out] 2/9*b*x^(9/2) + 2/7*a*x^(7/2)

mupad [B] time = 0.09, size = 13, normalized size = 0.62

$$\frac{2x^{7/2}(9a + 7bx)}{63}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(5/2)*(a + b*x), x)
```

```
[Out] (2*x^(7/2)*(9*a + 7*b*x))/63
```

sympy [A] time = 1.59, size = 19, normalized size = 0.90

$$\frac{2ax^{\frac{7}{2}}}{7} + \frac{2bx^{\frac{9}{2}}}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(5/2)*(b*x+a), x)
```

```
[Out] 2*a*x**(7/2)/7 + 2*b*x**(9/2)/9
```


3.430 $\int x^{3/2}(a + bx) dx$

Optimal. Leaf size=21

$$\frac{2}{5}ax^{5/2} + \frac{2}{7}bx^{7/2}$$

[Out] $2/5*a*x^{(5/2)}+2/7*b*x^{(7/2)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{2}{5}ax^{5/2} + \frac{2}{7}bx^{7/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(3/2)}*(a + b*x), x]$

[Out] $(2*a*x^{(5/2)})/5 + (2*b*x^{(7/2)})/7$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^{3/2}(a + bx) dx &= \int (ax^{3/2} + bx^{5/2}) dx \\ &= \frac{2}{5}ax^{5/2} + \frac{2}{7}bx^{7/2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 0.81

$$\frac{2}{35}x^{5/2}(7a + 5bx)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(3/2)}*(a + b*x), x]$

[Out] $(2*x^{(5/2)}*(7*a + 5*b*x))/35$

fricas [A] time = 0.42, size = 18, normalized size = 0.86

$$\frac{2}{35} (5bx^3 + 7ax^2)\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a),x, algorithm="fricas")

[Out] 2/35*(5*b*x^3 + 7*a*x^2)*sqrt(x)

giac [A] time = 0.88, size = 13, normalized size = 0.62

$$\frac{2}{7}bx^{\frac{7}{2}} + \frac{2}{5}ax^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a),x, algorithm="giac")

[Out] 2/7*b*x^(7/2) + 2/5*a*x^(5/2)

maple [A] time = 0.00, size = 14, normalized size = 0.67

$$\frac{2(5bx + 7a)x^{\frac{5}{2}}}{35}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(b*x+a),x)

[Out] 2/35*x^(5/2)*(5*b*x+7*a)

maxima [A] time = 1.29, size = 13, normalized size = 0.62

$$\frac{2}{7}bx^{\frac{7}{2}} + \frac{2}{5}ax^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a),x, algorithm="maxima")

[Out] 2/7*b*x^(7/2) + 2/5*a*x^(5/2)

mupad [B] time = 0.03, size = 13, normalized size = 0.62

$$\frac{2x^{5/2}(7a + 5bx)}{35}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(3/2)*(a + b*x), x)
```

```
[Out] (2*x^(5/2)*(7*a + 5*b*x))/35
```

sympy [A] time = 0.55, size = 19, normalized size = 0.90

$$\frac{2ax^{\frac{5}{2}}}{5} + \frac{2bx^{\frac{7}{2}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(3/2)*(b*x+a), x)
```

```
[Out] 2*a*x**(5/2)/5 + 2*b*x**(7/2)/7
```

3.431 $\int \sqrt{x} (a + bx) dx$

Optimal. Leaf size=21

$$\frac{2}{3}ax^{3/2} + \frac{2}{5}bx^{5/2}$$

[Out] $2/3*a*x^{(3/2)}+2/5*b*x^{(5/2)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{2}{3}ax^{3/2} + \frac{2}{5}bx^{5/2}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[x]*(a + b*x), x]`

[Out] $(2*a*x^{(3/2)})/3 + (2*b*x^{(5/2)})/5$

Rule 43

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int
[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n},
x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && Le
Q[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])
```

Rubi steps

$$\begin{aligned} \int \sqrt{x} (a + bx) dx &= \int (a\sqrt{x} + bx^{3/2}) dx \\ &= \frac{2}{3}ax^{3/2} + \frac{2}{5}bx^{5/2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 0.81

$$\frac{2}{15}x^{3/2}(5a + 3bx)$$

Antiderivative was successfully verified.

[In] `Integrate[Sqrt[x]*(a + b*x), x]`

[Out] $(2*x^{(3/2)}*(5*a + 3*b*x))/15$

fricas [A] time = 0.44, size = 16, normalized size = 0.76

$$\frac{2}{15} (3bx^2 + 5ax)\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*x^(1/2),x, algorithm="fricas")

[Out] 2/15*(3*b*x^2 + 5*a*x)*sqrt(x)

giac [A] time = 0.86, size = 13, normalized size = 0.62

$$\frac{2}{5}bx^{\frac{5}{2}} + \frac{2}{3}ax^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*x^(1/2),x, algorithm="giac")

[Out] 2/5*b*x^(5/2) + 2/3*a*x^(3/2)

maple [A] time = 0.00, size = 14, normalized size = 0.67

$$\frac{2(3bx + 5a)x^{\frac{3}{2}}}{15}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*x^(1/2),x)

[Out] 2/15*x^(3/2)*(3*b*x+5*a)

maxima [A] time = 1.34, size = 13, normalized size = 0.62

$$\frac{2}{5}bx^{\frac{5}{2}} + \frac{2}{3}ax^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*x^(1/2),x, algorithm="maxima")

[Out] 2/5*b*x^(5/2) + 2/3*a*x^(3/2)

mupad [B] time = 0.02, size = 13, normalized size = 0.62

$$\frac{2x^{3/2}(5a + 3bx)}{15}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(1/2)*(a + b*x),x)
```

```
[Out] (2*x^(3/2)*(5*a + 3*b*x))/15
```

sympy [A] time = 1.62, size = 19, normalized size = 0.90

$$\frac{2ax^{\frac{3}{2}}}{3} + \frac{2bx^{\frac{5}{2}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)*x**(1/2),x)
```

```
[Out] 2*a*x**(3/2)/3 + 2*b*x**(5/2)/5
```

$$3.432 \quad \int \frac{a+bx}{\sqrt{x}} dx$$

Optimal. Leaf size=19

$$2a\sqrt{x} + \frac{2}{3}bx^{3/2}$$

[Out] $2/3*b*x^{(3/2)}+2*a*x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$2a\sqrt{x} + \frac{2}{3}bx^{3/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/Sqrt[x], x]

[Out] $2*a*\text{Sqrt}[x] + (2*b*x^{(3/2)})/3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{\sqrt{x}} dx &= \int \left(\frac{a}{\sqrt{x}} + b\sqrt{x} \right) dx \\ &= 2a\sqrt{x} + \frac{2}{3}bx^{3/2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 0.84

$$\frac{2}{3}\sqrt{x}(3a + bx)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/Sqrt[x], x]

[Out] $(2\sqrt{x}(3a + bx))/3$

fricas [A] time = 0.43, size = 12, normalized size = 0.63

$$\frac{2}{3}(bx + 3a)\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(1/2),x, algorithm="fricas")`

[Out] $2/3*(b*x + 3*a)*\text{sqrt}(x)$

giac [A] time = 1.08, size = 13, normalized size = 0.68

$$\frac{2}{3}bx^{\frac{3}{2}} + 2a\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(1/2),x, algorithm="giac")`

[Out] $2/3*b*x^{(3/2)} + 2*a*\text{sqrt}(x)$

maple [A] time = 0.00, size = 13, normalized size = 0.68

$$\frac{2(bx + 3a)\sqrt{x}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/x^(1/2),x)`

[Out] $2/3*x^{(1/2)}*(b*x+3*a)$

maxima [A] time = 1.32, size = 13, normalized size = 0.68

$$\frac{2}{3}bx^{\frac{3}{2}} + 2a\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(1/2),x, algorithm="maxima")`

[Out] $2/3*b*x^{(3/2)} + 2*a*\text{sqrt}(x)$

mupad [B] time = 0.03, size = 12, normalized size = 0.63

$$\frac{2\sqrt{x}(3a + bx)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^(1/2), x)
```

```
[Out] (2*x^(1/2)*(3*a + b*x))/3
```

```
sympy [A] time = 0.16, size = 17, normalized size = 0.89
```

$$2a\sqrt{x} + \frac{2bx^{\frac{3}{2}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**(1/2), x)
```

```
[Out] 2*a*sqrt(x) + 2*b*x**(3/2)/3
```

$$3.433 \quad \int \frac{a+bx}{x^{3/2}} dx$$

Optimal. Leaf size=17

$$2b\sqrt{x} - \frac{2a}{\sqrt{x}}$$

[Out] $-2*a/x^{(1/2)}+2*b*x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$2b\sqrt{x} - \frac{2a}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x^(3/2), x]

[Out] (-2*a)/Sqrt[x] + 2*b*Sqrt[x]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^{3/2}} dx &= \int \left(\frac{a}{x^{3/2}} + \frac{b}{\sqrt{x}} \right) dx \\ &= -\frac{2a}{\sqrt{x}} + 2b\sqrt{x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 14, normalized size = 0.82

$$\frac{2(bx - a)}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x^(3/2), x]

[Out] $(2*(-a + b*x))/\text{Sqrt}[x]$

fricas [A] time = 0.45, size = 12, normalized size = 0.71

$$\frac{2(bx - a)}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(3/2),x, algorithm="fricas")`

[Out] $2*(b*x - a)/\text{sqrt}(x)$

giac [A] time = 0.92, size = 13, normalized size = 0.76

$$2b\sqrt{x} - \frac{2a}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(3/2),x, algorithm="giac")`

[Out] $2*b*\text{sqrt}(x) - 2*a/\text{sqrt}(x)$

maple [A] time = 0.00, size = 12, normalized size = 0.71

$$-\frac{2(-bx + a)}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/x^(3/2),x)`

[Out] $-2*(-b*x+a)/x^(1/2)$

maxima [A] time = 1.33, size = 13, normalized size = 0.76

$$2b\sqrt{x} - \frac{2a}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(3/2),x, algorithm="maxima")`

[Out] $2*b*\text{sqrt}(x) - 2*a/\text{sqrt}(x)$

mupad [B] time = 0.03, size = 11, normalized size = 0.65

$$-\frac{2(a - bx)}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^(3/2), x)
```

```
[Out] -(2*(a - b*x))/x^(1/2)
```

sympy [A] time = 0.35, size = 15, normalized size = 0.88

$$-\frac{2a}{\sqrt{x}} + 2b\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**(3/2), x)
```

```
[Out] -2*a/sqrt(x) + 2*b*sqrt(x)
```

$$3.434 \quad \int \frac{a+bx}{x^{5/2}} dx$$

Optimal. Leaf size=19

$$-\frac{2a}{3x^{3/2}} - \frac{2b}{\sqrt{x}}$$

[Out] $-2/3*a/x^{(3/2)}-2*b/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{2a}{3x^{3/2}} - \frac{2b}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x^(5/2), x]

[Out] $(-2*a)/(3*x^{(3/2)}) - (2*b)/\text{Sqrt}[x]$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^{5/2}} dx &= \int \left(\frac{a}{x^{5/2}} + \frac{b}{x^{3/2}} \right) dx \\ &= -\frac{2a}{3x^{3/2}} - \frac{2b}{\sqrt{x}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 15, normalized size = 0.79

$$-\frac{2(a+3bx)}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x^(5/2), x]

[Out] $(-2*(a + 3*b*x))/(3*x^(3/2))$

fricas [A] time = 0.42, size = 11, normalized size = 0.58

$$-\frac{2(3bx + a)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(5/2),x, algorithm="fricas")`

[Out] $-2/3*(3*b*x + a)/x^(3/2)$

giac [A] time = 0.97, size = 11, normalized size = 0.58

$$-\frac{2(3bx + a)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(5/2),x, algorithm="giac")`

[Out] $-2/3*(3*b*x + a)/x^(3/2)$

maple [A] time = 0.00, size = 12, normalized size = 0.63

$$-\frac{2(3bx + a)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/x^(5/2),x)`

[Out] $-2/3*(3*b*x+a)/x^(3/2)$

maxima [A] time = 1.36, size = 11, normalized size = 0.58

$$-\frac{2(3bx + a)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(5/2),x, algorithm="maxima")`

[Out] $-2/3*(3*b*x + a)/x^(3/2)$

mupad [B] time = 0.03, size = 13, normalized size = 0.68

$$-\frac{2a + 6bx}{3x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/x^(5/2), x)`

[Out] `-(2*a + 6*b*x)/(3*x^(3/2))`

sympy [A] time = 0.56, size = 19, normalized size = 1.00

$$-\frac{2a}{3x^{3/2}} - \frac{2b}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x**(5/2), x)`

[Out] `-2*a/(3*x**(3/2)) - 2*b/sqrt(x)`

3.435 $\int x^m(a + bx)^2 dx$

Optimal. Leaf size=43

$$\frac{a^2x^{m+1}}{m+1} + \frac{2abx^{m+2}}{m+2} + \frac{b^2x^{m+3}}{m+3}$$

[Out] $a^2x^{(1+m)/(1+m)+2a*b*x^{(2+m)/(2+m)}+b^2*x^{(3+m)/(3+m)}$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2x^{m+1}}{m+1} + \frac{2abx^{m+2}}{m+2} + \frac{b^2x^{m+3}}{m+3}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x)^2,x]

[Out] $(a^2*x^{(1+m)/(1+m)} + (2*a*b*x^{(2+m)/(2+m)}) + (b^2*x^{(3+m)/(3+m)})/(3+m)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^m(a + bx)^2 dx &= \int (a^2x^m + 2abx^{1+m} + b^2x^{2+m}) dx \\ &= \frac{a^2x^{1+m}}{1+m} + \frac{2abx^{2+m}}{2+m} + \frac{b^2x^{3+m}}{3+m} \end{aligned}$$

Mathematica [A] time = 0.03, size = 38, normalized size = 0.88

$$x^{m+1} \left(\frac{a^2}{m+1} + \frac{2abx}{m+2} + \frac{b^2x^2}{m+3} \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x)^2,x]

[Out] $x^{(1+m)}(a^2/(1+m) + (2abx)/(2+m) + (b^2x^2)/(3+m))$

fricas [A] time = 0.44, size = 85, normalized size = 1.98

$$\frac{((b^2m^2 + 3b^2m + 2b^2)x^3 + 2(abm^2 + 4abm + 3ab)x^2 + (a^2m^2 + 5a^2m + 6a^2)x)x^m}{m^3 + 6m^2 + 11m + 6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m*(b*x+a)^2,x, algorithm="fricas")`

[Out] $((b^2m^2 + 3b^2m + 2b^2)x^3 + 2(a^2m^2 + 4a^2m + 3a^2b)x^2 + (a^2m^2 + 5a^2m + 6a^2b)x)x^m/(m^3 + 6m^2 + 11m + 6)$

giac [B] time = 1.10, size = 117, normalized size = 2.72

$$\frac{b^2m^2x^3x^m + 2abm^2x^2x^m + 3b^2mx^3x^m + a^2m^2xx^m + 8abmx^2x^m + 2b^2x^3x^m + 5a^2mxx^m + 6abx^2x^m + 6a^2xx^m}{m^3 + 6m^2 + 11m + 6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m*(b*x+a)^2,x, algorithm="giac")`

[Out] $(b^2m^2x^3x^m + 2a^2b^2m^2x^2x^m + 3b^2m^2x^3x^m + a^2m^2x^2x^m + 8a^2b^2m^2x^2x^m + 2b^2m^2x^3x^m + 5a^2m^2x^2x^m + 6a^2b^2m^2x^2x^m + 6a^2m^2x^2x^m)/(m^3 + 6m^2 + 11m + 6)$

maple [A] time = 0.00, size = 87, normalized size = 2.02

$$\frac{(b^2m^2x^2 + 2abm^2x + 3b^2mx^2 + a^2m^2 + 8abmx + 2b^2x^2 + 5a^2m + 6abx + 6a^2)x^{m+1}}{(m+3)(m+2)(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(b*x+a)^2,x)`

[Out] $x^{(m+1)}(b^2m^2x^2+2a^2b^2m^2x+3b^2m^2x^2+a^2m^2+8a^2b^2m^2x+2b^2m^2x^2+5a^2m^2+6a^2b^2x+6a^2)/(3+m)/(m+2)/(m+1)$

maxima [A] time = 1.36, size = 43, normalized size = 1.00

$$\frac{b^2x^{m+3}}{m+3} + \frac{2abx^{m+2}}{m+2} + \frac{a^2x^{m+1}}{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m*(b*x+a)^2,x, algorithm="maxima")`

[Out] $b^2 x^{m+3}/(m+3) + 2abx^{m+2}/(m+2) + a^2 x^{m+1}/(m+1)$

mupad [B] time = 0.42, size = 93, normalized size = 2.16

$$x^m \left(\frac{a^2 x (m^2 + 5m + 6)}{m^3 + 6m^2 + 11m + 6} + \frac{b^2 x^3 (m^2 + 3m + 2)}{m^3 + 6m^2 + 11m + 6} + \frac{2abx^2 (m^2 + 4m + 3)}{m^3 + 6m^2 + 11m + 6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(a + b*x)^2, x)`

[Out] $x^m * ((a^2 x (5m + m^2 + 6)) / (11m + 6m^2 + m^3 + 6) + (b^2 x^3 (3m + m^2 + 2)) / (11m + 6m^2 + m^3 + 6) + (2abx^2 (4m + m^2 + 3)) / (11m + 6m^2 + m^3 + 6))$

sympy [A] time = 0.53, size = 299, normalized size = 6.95

$$\left\{ \begin{array}{l} -\frac{a^2}{2x^2} - \frac{2ab}{x} + b^2 \log(x) \\ -\frac{a^2}{x} + 2ab \log(x) + b^2 x \\ a^2 \log(x) + 2abx + \frac{b^2 x^2}{2} \\ \frac{a^2 m^2 x x^m}{m^3 + 6m^2 + 11m + 6} + \frac{5a^2 m x x^m}{m^3 + 6m^2 + 11m + 6} + \frac{6a^2 x x^m}{m^3 + 6m^2 + 11m + 6} + \frac{2ab m^2 x^2 x^m}{m^3 + 6m^2 + 11m + 6} + \frac{8ab m x^2 x^m}{m^3 + 6m^2 + 11m + 6} + \frac{6ab x^2 x^m}{m^3 + 6m^2 + 11m + 6} + \frac{b^2 m^2 x^3 x^m}{m^3 + 6m^2 + 11m + 6} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m*(b*x+a)**2, x)`

[Out] `Piecewise((-a**2/(2*x**2) - 2*a*b/x + b**2*log(x), Eq(m, -3)), (-a**2/x + 2*a*b*log(x) + b**2*x, Eq(m, -2)), (a**2*log(x) + 2*a*b*x + b**2*x**2/2, Eq(m, -1)), (a**2*m**2*x*x**m/(m**3 + 6*m**2 + 11*m + 6) + 5*a**2*m*x*x**m/(m**3 + 6*m**2 + 11*m + 6) + 6*a**2*x*x**m/(m**3 + 6*m**2 + 11*m + 6) + 2*a*b*m**2*x**2*x**m/(m**3 + 6*m**2 + 11*m + 6) + 8*a*b*m*x**2*x**m/(m**3 + 6*m**2 + 11*m + 6) + 6*a*b*x**2*x**m/(m**3 + 6*m**2 + 11*m + 6) + b**2*m**2*x**3*x**m/(m**3 + 6*m**2 + 11*m + 6) + 3*b**2*m*x**3*x**m/(m**3 + 6*m**2 + 11*m + 6) + 2*b**2*x**3*x**m/(m**3 + 6*m**2 + 11*m + 6), True))`

3.436 $\int x^{5/2}(a + bx)^2 dx$

Optimal. Leaf size=36

$$\frac{2}{7}a^2x^{7/2} + \frac{4}{9}abx^{9/2} + \frac{2}{11}b^2x^{11/2}$$

[Out] $2/7*a^2*x^{(7/2)}+4/9*a*b*x^{(9/2)}+2/11*b^2*x^{(11/2)}$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2}{7}a^2x^{7/2} + \frac{4}{9}abx^{9/2} + \frac{2}{11}b^2x^{11/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(5/2)}*(a + b*x)^2, x]$

[Out] $(2*a^2*x^{(7/2)})/7 + (4*a*b*x^{(9/2)})/9 + (2*b^2*x^{(11/2)})/11$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^{5/2}(a + bx)^2 dx &= \int (a^2x^{5/2} + 2abx^{7/2} + b^2x^{9/2}) dx \\ &= \frac{2}{7}a^2x^{7/2} + \frac{4}{9}abx^{9/2} + \frac{2}{11}b^2x^{11/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.78

$$\frac{2}{693}x^{7/2}(99a^2 + 154abx + 63b^2x^2)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(5/2)}*(a + b*x)^2, x]$

[Out] $(2*x^{(7/2)}*(99*a^2 + 154*a*b*x + 63*b^2*x^2))/693$

fricas [A] time = 0.41, size = 29, normalized size = 0.81

$$\frac{2}{693} (63 b^2 x^5 + 154 a b x^4 + 99 a^2 x^3) \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] 2/693*(63*b^2*x^5 + 154*a*b*x^4 + 99*a^2*x^3)*sqrt(x)

giac [A] time = 1.16, size = 24, normalized size = 0.67

$$\frac{2}{11} b^2 x^{\frac{11}{2}} + \frac{4}{9} a b x^{\frac{9}{2}} + \frac{2}{7} a^2 x^{\frac{7}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^2,x, algorithm="giac")

[Out] 2/11*b^2*x^(11/2) + 4/9*a*b*x^(9/2) + 2/7*a^2*x^(7/2)

maple [A] time = 0.00, size = 25, normalized size = 0.69

$$\frac{2 (63 b^2 x^2 + 154 a b x + 99 a^2) x^{\frac{7}{2}}}{693}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(b*x+a)^2,x)

[Out] 2/693*x^(7/2)*(63*b^2*x^2+154*a*b*x+99*a^2)

maxima [A] time = 1.27, size = 24, normalized size = 0.67

$$\frac{2}{11} b^2 x^{\frac{11}{2}} + \frac{4}{9} a b x^{\frac{9}{2}} + \frac{2}{7} a^2 x^{\frac{7}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^2,x, algorithm="maxima")

[Out] 2/11*b^2*x^(11/2) + 4/9*a*b*x^(9/2) + 2/7*a^2*x^(7/2)

mupad [B] time = 0.10, size = 24, normalized size = 0.67

$$\frac{2 x^{7/2} (99 a^2 + 154 a b x + 63 b^2 x^2)}{693}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/2)*(a + b*x)^2,x)`

[Out] `(2*x^(7/2)*(99*a^2 + 63*b^2*x^2 + 154*a*b*x))/693`

sympy [A] time = 2.60, size = 34, normalized size = 0.94

$$\frac{2a^2x^{\frac{7}{2}}}{7} + \frac{4abx^{\frac{9}{2}}}{9} + \frac{2b^2x^{\frac{11}{2}}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/2)*(b*x+a)**2,x)`

[Out] `2*a**2*x**(7/2)/7 + 4*a*b*x**(9/2)/9 + 2*b**2*x**(11/2)/11`

3.437 $\int x^{3/2}(a + bx)^2 dx$

Optimal. Leaf size=36

$$\frac{2}{5}a^2x^{5/2} + \frac{4}{7}abx^{7/2} + \frac{2}{9}b^2x^{9/2}$$

[Out] $2/5*a^2*x^{(5/2)}+4/7*a*b*x^{(7/2)}+2/9*b^2*x^{(9/2)}$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2}{5}a^2x^{5/2} + \frac{4}{7}abx^{7/2} + \frac{2}{9}b^2x^{9/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(3/2)}*(a + b*x)^2, x]$

[Out] $(2*a^2*x^{(5/2)})/5 + (4*a*b*x^{(7/2)})/7 + (2*b^2*x^{(9/2)})/9$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^{3/2}(a + bx)^2 dx &= \int (a^2x^{3/2} + 2abx^{5/2} + b^2x^{7/2}) dx \\ &= \frac{2}{5}a^2x^{5/2} + \frac{4}{7}abx^{7/2} + \frac{2}{9}b^2x^{9/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.78

$$\frac{2}{315}x^{5/2}(63a^2 + 90abx + 35b^2x^2)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(3/2)}*(a + b*x)^2, x]$

[Out] $(2*x^{(5/2)}*(63*a^2 + 90*a*b*x + 35*b^2*x^2))/315$

fricas [A] time = 0.42, size = 29, normalized size = 0.81

$$\frac{2}{315} (35 b^2 x^4 + 90 a b x^3 + 63 a^2 x^2) \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] 2/315*(35*b^2*x^4 + 90*a*b*x^3 + 63*a^2*x^2)*sqrt(x)

giac [A] time = 1.12, size = 24, normalized size = 0.67

$$\frac{2}{9} b^2 x^{\frac{9}{2}} + \frac{4}{7} a b x^{\frac{7}{2}} + \frac{2}{5} a^2 x^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^2,x, algorithm="giac")

[Out] 2/9*b^2*x^(9/2) + 4/7*a*b*x^(7/2) + 2/5*a^2*x^(5/2)

maple [A] time = 0.00, size = 25, normalized size = 0.69

$$\frac{2(35b^2x^2 + 90abx + 63a^2)x^{\frac{5}{2}}}{315}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(b*x+a)^2,x)

[Out] 2/315*x^(5/2)*(35*b^2*x^2+90*a*b*x+63*a^2)

maxima [A] time = 1.32, size = 24, normalized size = 0.67

$$\frac{2}{9} b^2 x^{\frac{9}{2}} + \frac{4}{7} a b x^{\frac{7}{2}} + \frac{2}{5} a^2 x^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^2,x, algorithm="maxima")

[Out] 2/9*b^2*x^(9/2) + 4/7*a*b*x^(7/2) + 2/5*a^2*x^(5/2)

mupad [B] time = 0.04, size = 24, normalized size = 0.67

$$\frac{2x^{5/2}(63a^2 + 90abx + 35b^2x^2)}{315}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)*(a + b*x)^2,x)`

[Out] `(2*x^(5/2)*(63*a^2 + 35*b^2*x^2 + 90*a*b*x))/315`

sympy [A] time = 1.03, size = 34, normalized size = 0.94

$$\frac{2a^2x^{\frac{5}{2}}}{5} + \frac{4abx^{\frac{7}{2}}}{7} + \frac{2b^2x^{\frac{9}{2}}}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)*(b*x+a)**2,x)`

[Out] `2*a**2*x**(5/2)/5 + 4*a*b*x**(7/2)/7 + 2*b**2*x**(9/2)/9`

3.438 $\int \sqrt{x} (a + bx)^2 dx$

Optimal. Leaf size=36

$$\frac{2}{3}a^2x^{3/2} + \frac{4}{5}abx^{5/2} + \frac{2}{7}b^2x^{7/2}$$

[Out] $2/3*a^2*x^{(3/2)}+4/5*a*b*x^{(5/2)}+2/7*b^2*x^{(7/2)}$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2}{3}a^2x^{3/2} + \frac{4}{5}abx^{5/2} + \frac{2}{7}b^2x^{7/2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*(a + b*x)^2,x]

[Out] $(2*a^2*x^{(3/2)})/3 + (4*a*b*x^{(5/2)})/5 + (2*b^2*x^{(7/2)})/7$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \sqrt{x} (a + bx)^2 dx &= \int (a^2\sqrt{x} + 2abx^{3/2} + b^2x^{5/2}) dx \\ &= \frac{2}{3}a^2x^{3/2} + \frac{4}{5}abx^{5/2} + \frac{2}{7}b^2x^{7/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.78

$$\frac{2}{105}x^{3/2} (35a^2 + 42abx + 15b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*(a + b*x)^2,x]

[Out] $(2*x^{(3/2)}*(35*a^2 + 42*a*b*x + 15*b^2*x^2))/105$

fricas [A] time = 0.43, size = 27, normalized size = 0.75

$$\frac{2}{105} (15 b^2 x^3 + 42 a b x^2 + 35 a^2 x) \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*x^(1/2),x, algorithm="fricas")

[Out] 2/105*(15*b^2*x^3 + 42*a*b*x^2 + 35*a^2*x)*sqrt(x)

giac [A] time = 0.90, size = 24, normalized size = 0.67

$$\frac{2}{7} b^2 x^{\frac{7}{2}} + \frac{4}{5} a b x^{\frac{5}{2}} + \frac{2}{3} a^2 x^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*x^(1/2),x, algorithm="giac")

[Out] 2/7*b^2*x^(7/2) + 4/5*a*b*x^(5/2) + 2/3*a^2*x^(3/2)

maple [A] time = 0.00, size = 25, normalized size = 0.69

$$\frac{2 (15 b^2 x^2 + 42 a b x + 35 a^2) x^{\frac{3}{2}}}{105}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*x^(1/2),x)

[Out] 2/105*x^(3/2)*(15*b^2*x^2+42*a*b*x+35*a^2)

maxima [A] time = 1.29, size = 24, normalized size = 0.67

$$\frac{2}{7} b^2 x^{\frac{7}{2}} + \frac{4}{5} a b x^{\frac{5}{2}} + \frac{2}{3} a^2 x^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*x^(1/2),x, algorithm="maxima")

[Out] 2/7*b^2*x^(7/2) + 4/5*a*b*x^(5/2) + 2/3*a^2*x^(3/2)

mupad [B] time = 0.04, size = 24, normalized size = 0.67

$$\frac{2 x^{3/2} (35 a^2 + 42 a b x + 15 b^2 x^2)}{105}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(1/2)*(a + b*x)^2,x)
```

```
[Out] (2*x^(3/2)*(35*a^2 + 15*b^2*x^2 + 42*a*b*x))/105
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**2*x**(1/2),x)
```

```
[Out] Timed out
```

$$3.439 \quad \int \frac{(a+bx)^2}{\sqrt{x}} dx$$

Optimal. Leaf size=34

$$2a^2\sqrt{x} + \frac{4}{3}abx^{3/2} + \frac{2}{5}b^2x^{5/2}$$

[Out] $4/3*a*b*x^{(3/2)}+2/5*b^2*x^{(5/2)}+2*a^2*x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$2a^2\sqrt{x} + \frac{4}{3}abx^{3/2} + \frac{2}{5}b^2x^{5/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/Sqrt[x], x]

[Out] $2*a^2*\text{Sqrt}[x] + (4*a*b*x^{(3/2)})/3 + (2*b^2*x^{(5/2)})/5$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{\sqrt{x}} dx &= \int \left(\frac{a^2}{\sqrt{x}} + 2ab\sqrt{x} + b^2x^{3/2} \right) dx \\ &= 2a^2\sqrt{x} + \frac{4}{3}abx^{3/2} + \frac{2}{5}b^2x^{5/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.82

$$\frac{2}{15}\sqrt{x} (15a^2 + 10abx + 3b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/Sqrt[x], x]

[Out] $(2\sqrt{x}(15a^2 + 10abx + 3b^2x^2))/15$

fricas [A] time = 0.41, size = 24, normalized size = 0.71

$$\frac{2}{15} (3b^2x^2 + 10abx + 15a^2)\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^(1/2),x, algorithm="fricas")`

[Out] $2/15*(3*b^2*x^2 + 10*a*b*x + 15*a^2)*\text{sqrt}(x)$

giac [A] time = 0.92, size = 24, normalized size = 0.71

$$\frac{2}{5} b^2 x^{\frac{5}{2}} + \frac{4}{3} abx^{\frac{3}{2}} + 2a^2\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^(1/2),x, algorithm="giac")`

[Out] $2/5*b^2*x^(5/2) + 4/3*a*b*x^(3/2) + 2*a^2*\text{sqrt}(x)$

maple [A] time = 0.00, size = 25, normalized size = 0.74

$$\frac{2(3b^2x^2 + 10abx + 15a^2)\sqrt{x}}{15}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^(1/2),x)`

[Out] $2/15*x^(1/2)*(3*b^2*x^2+10*a*b*x+15*a^2)$

maxima [A] time = 1.38, size = 24, normalized size = 0.71

$$\frac{2}{5} b^2 x^{\frac{5}{2}} + \frac{4}{3} abx^{\frac{3}{2}} + 2a^2\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^(1/2),x, algorithm="maxima")`

[Out] $2/5*b^2*x^(5/2) + 4/3*a*b*x^(3/2) + 2*a^2*\text{sqrt}(x)$

mupad [B] time = 0.04, size = 24, normalized size = 0.71

$$\frac{2\sqrt{x}(15a^2 + 10abx + 3b^2x^2)}{15}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x^(1/2), x)`

[Out] `(2*x^(1/2)*(15*a^2 + 3*b^2*x^2 + 10*a*b*x))/15`

sympy [A] time = 0.26, size = 32, normalized size = 0.94

$$2a^2\sqrt{x} + \frac{4abx^{\frac{3}{2}}}{3} + \frac{2b^2x^{\frac{5}{2}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**(1/2), x)`

[Out] `2*a**2*sqrt(x) + 4*a*b*x**(3/2)/3 + 2*b**2*x**(5/2)/5`

$$3.440 \quad \int \frac{(a+bx)^2}{x^{3/2}} dx$$

Optimal. Leaf size=32

$$-\frac{2a^2}{\sqrt{x}} + 4ab\sqrt{x} + \frac{2}{3}b^2x^{3/2}$$

[Out] $2/3*b^2*x^{(3/2)}-2*a^2/x^{(1/2)}+4*a*b*x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{2a^2}{\sqrt{x}} + 4ab\sqrt{x} + \frac{2}{3}b^2x^{3/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^(3/2), x]

[Out] $(-2*a^2)/\text{Sqrt}[x] + 4*a*b*\text{Sqrt}[x] + (2*b^2*x^{(3/2)})/3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^{3/2}} dx &= \int \left(\frac{a^2}{x^{3/2}} + \frac{2ab}{\sqrt{x}} + b^2\sqrt{x} \right) dx \\ &= -\frac{2a^2}{\sqrt{x}} + 4ab\sqrt{x} + \frac{2}{3}b^2x^{3/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.84

$$\frac{2(-3a^2 + 6abx + b^2x^2)}{3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^(3/2), x]

[Out] (2*(-3*a^2 + 6*a*b*x + b^2*x^2))/(3*Sqrt[x])

fricas [A] time = 0.43, size = 23, normalized size = 0.72

$$\frac{2(b^2x^2 + 6abx - 3a^2)}{3\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(3/2), x, algorithm="fricas")

[Out] 2/3*(b^2*x^2 + 6*a*b*x - 3*a^2)/sqrt(x)

giac [A] time = 1.02, size = 24, normalized size = 0.75

$$\frac{2}{3}b^2x^{\frac{3}{2}} + 4ab\sqrt{x} - \frac{2a^2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(3/2), x, algorithm="giac")

[Out] 2/3*b^2*x^(3/2) + 4*a*b*sqrt(x) - 2*a^2/sqrt(x)

maple [A] time = 0.00, size = 25, normalized size = 0.78

$$\frac{2(-b^2x^2 - 6abx + 3a^2)}{3\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/x^(3/2), x)

[Out] -2/3*(-b^2*x^2-6*a*b*x+3*a^2)/x^(1/2)

maxima [A] time = 1.32, size = 24, normalized size = 0.75

$$\frac{2}{3}b^2x^{\frac{3}{2}} + 4ab\sqrt{x} - \frac{2a^2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(3/2), x, algorithm="maxima")

[Out] 2/3*b^2*x^(3/2) + 4*a*b*sqrt(x) - 2*a^2/sqrt(x)

mupad [B] time = 0.03, size = 24, normalized size = 0.75

$$\frac{-6a^2 + 12abx + 2b^2x^2}{3\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x^(3/2), x)`

[Out] `(2*b^2*x^2 - 6*a^2 + 12*a*b*x)/(3*x^(1/2))`

sympy [A] time = 0.43, size = 31, normalized size = 0.97

$$-\frac{2a^2}{\sqrt{x}} + 4ab\sqrt{x} + \frac{2b^2x^{\frac{3}{2}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**(3/2), x)`

[Out] `-2*a**2/sqrt(x) + 4*a*b*sqrt(x) + 2*b**2*x**(3/2)/3`

$$3.441 \quad \int \frac{(a+bx)^2}{x^{5/2}} dx$$

Optimal. Leaf size=32

$$-\frac{2a^2}{3x^{3/2}} - \frac{4ab}{\sqrt{x}} + 2b^2\sqrt{x}$$

[Out] $-2/3*a^2/x^{(3/2)}-4*a*b/x^{(1/2)}+2*b^2*x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{2a^2}{3x^{3/2}} - \frac{4ab}{\sqrt{x}} + 2b^2\sqrt{x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^2/x^{(5/2)}, x]$

[Out] $(-2*a^2)/(3*x^{(3/2)}) - (4*a*b)/\text{Sqrt}[x] + 2*b^2*\text{Sqrt}[x]$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)*((c_. + (d_.)*(x_))^{(n_.)}, x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x\} \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{IGtQ}[m, 0] \&\& (!\text{IntegerQ}[n] || (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0]) || \text{LtQ}[9*m + 5*(n + 1), 0] || \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^{5/2}} dx &= \int \left(\frac{a^2}{x^{5/2}} + \frac{2ab}{x^{3/2}} + \frac{b^2}{\sqrt{x}} \right) dx \\ &= -\frac{2a^2}{3x^{3/2}} - \frac{4ab}{\sqrt{x}} + 2b^2\sqrt{x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 0.81

$$-\frac{2(a^2 + 6abx - 3b^2x^2)}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^(5/2),x]

[Out] (-2*(a^2 + 6*a*b*x - 3*b^2*x^2))/(3*x^(3/2))

fricas [A] time = 0.44, size = 24, normalized size = 0.75

$$\frac{2(3b^2x^2 - 6abx - a^2)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(5/2),x, algorithm="fricas")

[Out] 2/3*(3*b^2*x^2 - 6*a*b*x - a^2)/x^(3/2)

giac [A] time = 1.00, size = 23, normalized size = 0.72

$$2b^2\sqrt{x} - \frac{2(6abx + a^2)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(5/2),x, algorithm="giac")

[Out] 2*b^2*sqrt(x) - 2/3*(6*a*b*x + a^2)/x^(3/2)

maple [A] time = 0.00, size = 23, normalized size = 0.72

$$-\frac{2(-3b^2x^2 + 6abx + a^2)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/x^(5/2),x)

[Out] -2/3*(-3*b^2*x^2+6*a*b*x+a^2)/x^(3/2)

maxima [A] time = 1.29, size = 23, normalized size = 0.72

$$2b^2\sqrt{x} - \frac{2(6abx + a^2)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(5/2),x, algorithm="maxima")

[Out] $2b^2\sqrt{x} - \frac{2}{3}(6abx + a^2)/x^{3/2}$

mupad [B] time = 0.03, size = 24, normalized size = 0.75

$$\frac{2a^2 + 12abx - 6b^2x^2}{3x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x^(5/2), x)`

[Out] $-(2a^2 - 6b^2x^2 + 12abx)/(3x^{3/2})$

sympy [A] time = 0.59, size = 31, normalized size = 0.97

$$-\frac{2a^2}{3x^{3/2}} - \frac{4ab}{\sqrt{x}} + 2b^2\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**(5/2), x)`

[Out] $-2a^2/(3x^{3/2}) - 4ab/\sqrt{x} + 2b^2\sqrt{x}$

3.442 $\int x^m(a + bx)^3 dx$

Optimal. Leaf size=61

$$\frac{a^3x^{m+1}}{m+1} + \frac{3a^2bx^{m+2}}{m+2} + \frac{3ab^2x^{m+3}}{m+3} + \frac{b^3x^{m+4}}{m+4}$$

[Out] $a^3x^{(1+m)}/(1+m)+3*a^2*b*x^{(2+m)}/(2+m)+3*a*b^2*x^{(3+m)}/(3+m)+b^3*x^{(4+m)}/(4+m)$

Rubi [A] time = 0.02, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3a^2bx^{m+2}}{m+2} + \frac{a^3x^{m+1}}{m+1} + \frac{3ab^2x^{m+3}}{m+3} + \frac{b^3x^{m+4}}{m+4}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x)^3,x]

[Out] $(a^3*x^{(1+m)})/(1+m) + (3*a^2*b*x^{(2+m)})/(2+m) + (3*a*b^2*x^{(3+m)})/(3+m) + (b^3*x^{(4+m)})/(4+m)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^m(a + bx)^3 dx &= \int (a^3x^m + 3a^2bx^{1+m} + 3ab^2x^{2+m} + b^3x^{3+m}) dx \\ &= \frac{a^3x^{1+m}}{1+m} + \frac{3a^2bx^{2+m}}{2+m} + \frac{3ab^2x^{3+m}}{3+m} + \frac{b^3x^{4+m}}{4+m} \end{aligned}$$

Mathematica [A] time = 0.03, size = 54, normalized size = 0.89

$$x^{m+1} \left(\frac{a^3}{m+1} + \frac{3a^2bx}{m+2} + \frac{3ab^2x^2}{m+3} + \frac{b^3x^3}{m+4} \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x)^3,x]

[Out] $x^{(1+m)}*(a^3/(1+m) + (3*a^2*b*x)/(2+m) + (3*a*b^2*x^2)/(3+m) + (b^3*x^3)/(4+m))$

fricas [B] time = 0.44, size = 157, normalized size = 2.57

$$\frac{((b^3 m^3 + 6 b^3 m^2 + 11 b^3 m + 6 b^3)x^4 + 3(ab^2 m^3 + 7 ab^2 m^2 + 14 ab^2 m + 8 ab^2)x^3 + 3(a^2 b m^3 + 8 a^2 b m^2 + 19 a^2 b m + 12 a^2 b)x^2 + (a^3 m^3 + 9 a^3 m^2 + 26 a^3 m + 24 a^3)x)x^m}{m^4 + 10 m^3 + 35 m^2 + 50 m + 24}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^3,x, algorithm="fricas")

[Out] $((b^3 m^3 + 6 b^3 m^2 + 11 b^3 m + 6 b^3)x^4 + 3(a^2 b m^3 + 7 a^2 b m^2 + 14 a^2 b m + 8 a^2 b)x^3 + 3(a^3 m^3 + 9 a^3 m^2 + 26 a^3 m + 24 a^3)x^2 + (a^3 m^3 + 9 a^3 m^2 + 26 a^3 m + 24 a^3)x)x^m/(m^4 + 10 m^3 + 35 m^2 + 50 m + 24)$

giac [B] time = 1.03, size = 224, normalized size = 3.67

$$\frac{b^3 m^3 x^4 x^m + 3 a b^2 m^3 x^3 x^m + 6 b^3 m^2 x^4 x^m + 3 a^2 b m^3 x^2 x^m + 21 a b^2 m^2 x^3 x^m + 11 b^3 m x^4 x^m + a^3 m^3 x x^m + 24 a^2 b m^2 x^2 x^m}{m^4 + 10 m^3 + 35 m^2 + 50 m + 24}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^3,x, algorithm="giac")

[Out] $(b^3 m^3 x^4 x^m + 3 a^2 b^2 m^3 x^3 x^m + 6 b^3 m^2 x^4 x^m + 3 a^2 b m^3 x^2 x^m + 21 a^2 b^2 m^2 x^3 x^m + 11 b^3 m^2 x^4 x^m + a^3 m^3 x^2 x^m + 24 a^2 b m^2 x^3 x^m + 42 a^2 b^2 m^2 x^3 x^m + 6 b^3 m^3 x^4 x^m + 9 a^3 m^2 x^2 x^m + 57 a^2 b^2 m^2 x^3 x^m + 24 a^2 b^2 m^2 x^3 x^m + 26 a^3 m^2 x^2 x^m + 36 a^2 b^2 m^2 x^3 x^m + 24 a^3 m^2 x^2 x^m)/(m^4 + 10 m^3 + 35 m^2 + 50 m + 24)$

maple [B] time = 0.00, size = 170, normalized size = 2.79

$$\frac{(b^3 m^3 x^3 + 3 a b^2 m^3 x^2 + 6 b^3 m^2 x^3 + 3 a^2 b m^3 x + 21 a b^2 m^2 x^2 + 11 b^3 m x^3 + a^3 m^3 + 24 a^2 b m^2 x + 42 a b^2 m x^2 + 6 b^3 x^3)}{(m+4)(m+3)(m+2)(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(b*x+a)^3,x)

[Out] $x^{(m+1)}*(b^3 m^3 x^3 + 3 a^2 b^2 m^3 x^2 + 6 b^3 m^2 x^3 + 3 a^2 b m^3 x + 21 a^2 b^2 m^2 x^2 + 11 b^3 m^2 x^3 + a^3 m^3 + 24 a^2 b m^2 x + 42 a^2 b^2 m^2 x^2 + 6 b^3 m^3 x^3 + 9 a^3 m^2 x^2 + 57 a^2 b^2 m^2 x^3 + 24 a^2 b^2 m^2 x^3 + 26 a^3 m^2 x^2 + 36 a^2 b^2 m^2 x^3 + 24 a^3 m^2 x^2)/(4+m)/(m+3)/(m+2)/(m+1)$

maxima [A] time = 1.36, size = 61, normalized size = 1.00

$$\frac{b^3 x^{m+4}}{m+4} + \frac{3ab^2 x^{m+3}}{m+3} + \frac{3a^2 b x^{m+2}}{m+2} + \frac{a^3 x^{m+1}}{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^3,x, algorithm="maxima")

[Out] b^3*x^(m + 4)/(m + 4) + 3*a*b^2*x^(m + 3)/(m + 3) + 3*a^2*b*x^(m + 2)/(m + 2) + a^3*x^(m + 1)/(m + 1)

mupad [B] time = 0.39, size = 167, normalized size = 2.74

$$x^m \left(\frac{a^3 x (m^3 + 9m^2 + 26m + 24)}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{b^3 x^4 (m^3 + 6m^2 + 11m + 6)}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{3ab^2 x^3 (m^3 + 7m^2 + 14m + 8)}{m^4 + 10m^3 + 35m^2 + 50m + 24} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(a + b*x)^3,x)

[Out] x^m*((a^3*x*(26*m + 9*m^2 + m^3 + 24))/(50*m + 35*m^2 + 10*m^3 + m^4 + 24) + (b^3*x^4*(11*m + 6*m^2 + m^3 + 6))/(50*m + 35*m^2 + 10*m^3 + m^4 + 24) + (3*a*b^2*x^3*(14*m + 7*m^2 + m^3 + 8))/(50*m + 35*m^2 + 10*m^3 + m^4 + 24) + (3*a^2*b*x^2*(19*m + 8*m^2 + m^3 + 12))/(50*m + 35*m^2 + 10*m^3 + m^4 + 24))

sympy [A] time = 0.88, size = 663, normalized size = 10.87

$$\left\{ \begin{array}{l} -\frac{a^3}{3x^3} - \frac{3a^2b}{2x^2} - \frac{3ab^2}{x} + b^3 \log(x) \\ -\frac{a^3}{2x^2} - \frac{3a^2b}{x} + 3ab^2 \log(x) + b^3 x \\ -\frac{a^3}{x} + 3a^2b \log(x) + 3ab^2 x + \frac{b^3 x^2}{2} \\ a^3 \log(x) + 3a^2bx + \frac{3ab^2 x^2}{2} + \frac{b^3 x^3}{3} \\ \frac{a^3 m^3 x x^m}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{9a^3 m^2 x x^m}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{26a^3 m x x^m}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{24a^3 x x^m}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{3a^2 b m^3 x^2 x^m}{m^4 + 10m^3 + 35m^2 + 50m + 24} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*(b*x+a)**3,x)

[Out] Piecewise((-a**3/(3*x**3) - 3*a**2*b/(2*x**2) - 3*a*b**2/x + b**3*log(x), Eq(m, -4)), (-a**3/(2*x**2) - 3*a**2*b/x + 3*a*b**2*log(x) + b**3*x, Eq(m, -

$3)), (-a^{3}/x + 3a^{2}b \log(x) + 3ab^{2}x + b^{3}x^{2}/2, \text{Eq}(m, -2)), (a^{3} \log(x) + 3a^{2}bx + 3ab^{2}x^{2}/2 + b^{3}x^{3}/3, \text{Eq}(m, -1)), (a^{3}m^{3}x^{3}x^{3}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 9a^{3}m^{2}x^{2}x^{2}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 26a^{3}m^{2}x^{2}x^{2}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 24a^{3}x^{2}x^{2}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 3a^{2}b^{3}x^{2}x^{2}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 24a^{2}b^{3}m^{2}x^{2}x^{2}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 57a^{2}b^{3}m^{2}x^{2}x^{2}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 36a^{2}b^{3}x^{2}x^{2}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 3ab^{2}m^{3}x^{3}x^{3}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 21ab^{2}m^{2}x^{3}x^{3}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 42ab^{2}m^{2}x^{3}x^{3}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 24ab^{2}x^{3}x^{3}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + b^{3}m^{3}x^{4}x^{4}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 6b^{3}m^{2}x^{4}x^{4}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 11b^{3}m^{2}x^{4}x^{4}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24) + 6b^{3}x^{4}x^{4}m/(m^{4} + 10m^{3} + 35m^{2} + 50m + 24), \text{True}))$

3.443 $\int x^{5/2}(a + bx)^3 dx$

Optimal. Leaf size=51

$$\frac{2}{7}a^3x^{7/2} + \frac{2}{3}a^2bx^{9/2} + \frac{6}{11}ab^2x^{11/2} + \frac{2}{13}b^3x^{13/2}$$

[Out] $2/7*a^3*x^(7/2)+2/3*a^2*b*x^(9/2)+6/11*a*b^2*x^(11/2)+2/13*b^3*x^(13/2)$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{2}{3}a^2bx^{9/2} + \frac{2}{7}a^3x^{7/2} + \frac{6}{11}ab^2x^{11/2} + \frac{2}{13}b^3x^{13/2}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)*(a + b*x)^3,x]

[Out] $(2*a^3*x^(7/2))/7 + (2*a^2*b*x^(9/2))/3 + (6*a*b^2*x^(11/2))/11 + (2*b^3*x^(13/2))/13$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^{5/2}(a + bx)^3 dx &= \int (a^3x^{5/2} + 3a^2bx^{7/2} + 3ab^2x^{9/2} + b^3x^{11/2}) dx \\ &= \frac{2}{7}a^3x^{7/2} + \frac{2}{3}a^2bx^{9/2} + \frac{6}{11}ab^2x^{11/2} + \frac{2}{13}b^3x^{13/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.76

$$\frac{2x^{7/2} (429a^3 + 1001a^2bx + 819ab^2x^2 + 231b^3x^3)}{3003}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*(a + b*x)^3,x]

[Out] (2*x^(7/2)*(429*a^3 + 1001*a^2*b*x + 819*a*b^2*x^2 + 231*b^3*x^3))/3003

fricas [A] time = 0.45, size = 40, normalized size = 0.78

$$\frac{2}{3003} (231 b^3 x^6 + 819 a b^2 x^5 + 1001 a^2 b x^4 + 429 a^3 x^3) \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^3,x, algorithm="fricas")

[Out] 2/3003*(231*b^3*x^6 + 819*a*b^2*x^5 + 1001*a^2*b*x^4 + 429*a^3*x^3)*sqrt(x)

giac [A] time = 0.99, size = 35, normalized size = 0.69

$$\frac{2}{13} b^3 x^{\frac{13}{2}} + \frac{6}{11} a b^2 x^{\frac{11}{2}} + \frac{2}{3} a^2 b x^{\frac{9}{2}} + \frac{2}{7} a^3 x^{\frac{7}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^3,x, algorithm="giac")

[Out] 2/13*b^3*x^(13/2) + 6/11*a*b^2*x^(11/2) + 2/3*a^2*b*x^(9/2) + 2/7*a^3*x^(7/2)

maple [A] time = 0.00, size = 36, normalized size = 0.71

$$\frac{2(231b^3x^3 + 819ab^2x^2 + 1001a^2bx + 429a^3)x^{\frac{7}{2}}}{3003}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(b*x+a)^3,x)

[Out] 2/3003*x^(7/2)*(231*b^3*x^3+819*a*b^2*x^2+1001*a^2*b*x+429*a^3)

maxima [A] time = 1.34, size = 35, normalized size = 0.69

$$\frac{2}{13} b^3 x^{\frac{13}{2}} + \frac{6}{11} a b^2 x^{\frac{11}{2}} + \frac{2}{3} a^2 b x^{\frac{9}{2}} + \frac{2}{7} a^3 x^{\frac{7}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^3,x, algorithm="maxima")

[Out] 2/13*b^3*x^(13/2) + 6/11*a*b^2*x^(11/2) + 2/3*a^2*b*x^(9/2) + 2/7*a^3*x^(7/2)

mupad [B] time = 0.04, size = 35, normalized size = 0.69

$$\frac{2a^3x^{7/2}}{7} + \frac{2b^3x^{13/2}}{13} + \frac{2a^2bx^{9/2}}{3} + \frac{6ab^2x^{11/2}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(a + b*x)^3,x)

[Out] (2*a^3*x^(7/2))/7 + (2*b^3*x^(13/2))/13 + (2*a^2*b*x^(9/2))/3 + (6*a*b^2*x^(11/2))/11

sympy [A] time = 3.88, size = 49, normalized size = 0.96

$$\frac{2a^3x^{\frac{7}{2}}}{7} + \frac{2a^2bx^{\frac{9}{2}}}{3} + \frac{6ab^2x^{\frac{11}{2}}}{11} + \frac{2b^3x^{\frac{13}{2}}}{13}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)*(b*x+a)**3,x)

[Out] 2*a**3*x**(7/2)/7 + 2*a**2*b*x**(9/2)/3 + 6*a*b**2*x**(11/2)/11 + 2*b**3*x***(13/2)/13

3.444 $\int x^{3/2}(a + bx)^3 dx$

Optimal. Leaf size=51

$$\frac{2}{5}a^3x^{5/2} + \frac{6}{7}a^2bx^{7/2} + \frac{2}{3}ab^2x^{9/2} + \frac{2}{11}b^3x^{11/2}$$

[Out] $2/5*a^3*x^{(5/2)}+6/7*a^2*b*x^{(7/2)}+2/3*a*b^2*x^{(9/2)}+2/11*b^3*x^{(11/2)}$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{6}{7}a^2bx^{7/2} + \frac{2}{5}a^3x^{5/2} + \frac{2}{3}ab^2x^{9/2} + \frac{2}{11}b^3x^{11/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(3/2)}*(a + b*x)^3, x]$

[Out] $(2*a^3*x^{(5/2)})/5 + (6*a^2*b*x^{(7/2)})/7 + (2*a*b^2*x^{(9/2)})/3 + (2*b^3*x^{(11/2)})/11$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)}*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{IGtQ}[m, 0] \&\& (!\text{IntegerQ}[n] || (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0])) || \text{LtQ}[9*m + 5*(n + 1), 0] || \text{GtQ}[m + n + 2, 0]$

Rubi steps

$$\begin{aligned} \int x^{3/2}(a + bx)^3 dx &= \int (a^3x^{3/2} + 3a^2bx^{5/2} + 3ab^2x^{7/2} + b^3x^{9/2}) dx \\ &= \frac{2}{5}a^3x^{5/2} + \frac{6}{7}a^2bx^{7/2} + \frac{2}{3}ab^2x^{9/2} + \frac{2}{11}b^3x^{11/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.76

$$\frac{2x^{5/2} (231a^3 + 495a^2bx + 385ab^2x^2 + 105b^3x^3)}{1155}$$

1155

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*(a + b*x)^3,x]

[Out] (2*x^(5/2)*(231*a^3 + 495*a^2*b*x + 385*a*b^2*x^2 + 105*b^3*x^3))/1155

fricas [A] time = 0.44, size = 40, normalized size = 0.78

$$\frac{2}{1155} (105 b^3 x^5 + 385 a b^2 x^4 + 495 a^2 b x^3 + 231 a^3 x^2) \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^3,x, algorithm="fricas")

[Out] 2/1155*(105*b^3*x^5 + 385*a*b^2*x^4 + 495*a^2*b*x^3 + 231*a^3*x^2)*sqrt(x)

giac [A] time = 0.99, size = 35, normalized size = 0.69

$$\frac{2}{11} b^3 x^{\frac{11}{2}} + \frac{2}{3} a b^2 x^{\frac{9}{2}} + \frac{6}{7} a^2 b x^{\frac{7}{2}} + \frac{2}{5} a^3 x^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^3,x, algorithm="giac")

[Out] 2/11*b^3*x^(11/2) + 2/3*a*b^2*x^(9/2) + 6/7*a^2*b*x^(7/2) + 2/5*a^3*x^(5/2)

maple [A] time = 0.00, size = 36, normalized size = 0.71

$$\frac{2 (105 b^3 x^3 + 385 a b^2 x^2 + 495 a^2 b x + 231 a^3) x^{\frac{5}{2}}}{1155}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(b*x+a)^3,x)

[Out] 2/1155*x^(5/2)*(105*b^3*x^3+385*a*b^2*x^2+495*a^2*b*x+231*a^3)

maxima [A] time = 1.34, size = 35, normalized size = 0.69

$$\frac{2}{11} b^3 x^{\frac{11}{2}} + \frac{2}{3} a b^2 x^{\frac{9}{2}} + \frac{6}{7} a^2 b x^{\frac{7}{2}} + \frac{2}{5} a^3 x^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^3,x, algorithm="maxima")

[Out] 2/11*b^3*x^(11/2) + 2/3*a*b^2*x^(9/2) + 6/7*a^2*b*x^(7/2) + 2/5*a^3*x^(5/2)

mupad [B] time = 0.05, size = 35, normalized size = 0.69

$$\frac{2a^3x^{5/2}}{5} + \frac{2b^3x^{11/2}}{11} + \frac{6a^2bx^{7/2}}{7} + \frac{2ab^2x^{9/2}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)*(a + b*x)^3,x)`

[Out] $(2*a^3*x^{(5/2)})/5 + (2*b^3*x^{(11/2)})/11 + (6*a^2*b*x^{(7/2)})/7 + (2*a*b^2*x^{(9/2)})/3$

sympy [A] time = 1.70, size = 49, normalized size = 0.96

$$\frac{2a^3x^{\frac{5}{2}}}{5} + \frac{6a^2bx^{\frac{7}{2}}}{7} + \frac{2ab^2x^{\frac{9}{2}}}{3} + \frac{2b^3x^{\frac{11}{2}}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)*(b*x+a)**3,x)`

[Out] $2*a**3*x**(5/2)/5 + 6*a**2*b*x**(7/2)/7 + 2*a*b**2*x**(9/2)/3 + 2*b**3*x**(11/2)/11$

3.445 $\int \sqrt{x} (a + bx)^3 dx$

Optimal. Leaf size=51

$$\frac{2}{3}a^3x^{3/2} + \frac{6}{5}a^2bx^{5/2} + \frac{6}{7}ab^2x^{7/2} + \frac{2}{9}b^3x^{9/2}$$

[Out] $2/3*a^3*x^{(3/2)}+6/5*a^2*b*x^{(5/2)}+6/7*a*b^2*x^{(7/2)}+2/9*b^3*x^{(9/2)}$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{6}{5}a^2bx^{5/2} + \frac{2}{3}a^3x^{3/2} + \frac{6}{7}ab^2x^{7/2} + \frac{2}{9}b^3x^{9/2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*(a + b*x)^3,x]

[Out] $(2*a^3*x^{(3/2)})/3 + (6*a^2*b*x^{(5/2)})/5 + (6*a*b^2*x^{(7/2)})/7 + (2*b^3*x^{(9/2)})/9$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \sqrt{x} (a + bx)^3 dx &= \int (a^3\sqrt{x} + 3a^2bx^{3/2} + 3ab^2x^{5/2} + b^3x^{7/2}) dx \\ &= \frac{2}{3}a^3x^{3/2} + \frac{6}{5}a^2bx^{5/2} + \frac{6}{7}ab^2x^{7/2} + \frac{2}{9}b^3x^{9/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.76

$$\frac{2}{315}x^{3/2} (105a^3 + 189a^2bx + 135ab^2x^2 + 35b^3x^3)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*(a + b*x)^3,x]

[Out] (2*x^(3/2)*(105*a^3 + 189*a^2*b*x + 135*a*b^2*x^2 + 35*b^3*x^3))/315

fricas [A] time = 0.43, size = 38, normalized size = 0.75

$$\frac{2}{315} (35b^3x^4 + 135ab^2x^3 + 189a^2bx^2 + 105a^3x) \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*x^(1/2),x, algorithm="fricas")

[Out] 2/315*(35*b^3*x^4 + 135*a*b^2*x^3 + 189*a^2*b*x^2 + 105*a^3*x)*sqrt(x)

giac [A] time = 1.08, size = 35, normalized size = 0.69

$$\frac{2}{9} b^3 x^{\frac{9}{2}} + \frac{6}{7} a b^2 x^{\frac{7}{2}} + \frac{6}{5} a^2 b x^{\frac{5}{2}} + \frac{2}{3} a^3 x^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*x^(1/2),x, algorithm="giac")

[Out] 2/9*b^3*x^(9/2) + 6/7*a*b^2*x^(7/2) + 6/5*a^2*b*x^(5/2) + 2/3*a^3*x^(3/2)

maple [A] time = 0.00, size = 36, normalized size = 0.71

$$\frac{2(35b^3x^3 + 135ab^2x^2 + 189a^2bx + 105a^3)x^{\frac{3}{2}}}{315}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3*x^(1/2),x)

[Out] 2/315*x^(3/2)*(35*b^3*x^3+135*a*b^2*x^2+189*a^2*b*x+105*a^3)

maxima [A] time = 1.26, size = 35, normalized size = 0.69

$$\frac{2}{9} b^3 x^{\frac{9}{2}} + \frac{6}{7} a b^2 x^{\frac{7}{2}} + \frac{6}{5} a^2 b x^{\frac{5}{2}} + \frac{2}{3} a^3 x^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*x^(1/2),x, algorithm="maxima")

[Out] 2/9*b^3*x^(9/2) + 6/7*a*b^2*x^(7/2) + 6/5*a^2*b*x^(5/2) + 2/3*a^3*x^(3/2)

mupad [B] time = 0.04, size = 35, normalized size = 0.69

$$\frac{2a^3x^{3/2}}{3} + \frac{2b^3x^{9/2}}{9} + \frac{6a^2bx^{5/2}}{5} + \frac{6ab^2x^{7/2}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)*(a + b*x)^3,x)`

[Out] $(2*a^3*x^{(3/2)})/3 + (2*b^3*x^{(9/2)})/9 + (6*a^2*b*x^{(5/2)})/5 + (6*a*b^2*x^{(7/2)})/7$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3*x**(1/2),x)`

[Out] Timed out

$$3.446 \quad \int \frac{(a+bx)^3}{\sqrt{x}} dx$$

Optimal. Leaf size=47

$$2a^3\sqrt{x} + 2a^2bx^{3/2} + \frac{6}{5}ab^2x^{5/2} + \frac{2}{7}b^3x^{7/2}$$

[Out] $2*a^2*b*x^{(3/2)}+6/5*a*b^2*x^{(5/2)}+2/7*b^3*x^{(7/2)}+2*a^3*x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$2a^2bx^{3/2} + 2a^3\sqrt{x} + \frac{6}{5}ab^2x^{5/2} + \frac{2}{7}b^3x^{7/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/Sqrt[x], x]

[Out] $2*a^3*\text{Sqrt}[x] + 2*a^2*b*x^{(3/2)} + (6*a*b^2*x^{(5/2)})/5 + (2*b^3*x^{(7/2)})/7$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{\sqrt{x}} dx &= \int \left(\frac{a^3}{\sqrt{x}} + 3a^2b\sqrt{x} + 3ab^2x^{3/2} + b^3x^{5/2} \right) dx \\ &= 2a^3\sqrt{x} + 2a^2bx^{3/2} + \frac{6}{5}ab^2x^{5/2} + \frac{2}{7}b^3x^{7/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.83

$$\frac{2}{35}\sqrt{x} (35a^3 + 35a^2bx + 21ab^2x^2 + 5b^3x^3)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/Sqrt[x],x]

[Out] (2*Sqrt[x]*(35*a^3 + 35*a^2*b*x + 21*a*b^2*x^2 + 5*b^3*x^3))/35

fricas [A] time = 0.42, size = 35, normalized size = 0.74

$$\frac{2}{35} (5b^3x^3 + 21ab^2x^2 + 35a^2bx + 35a^3)\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(1/2),x, algorithm="fricas")

[Out] 2/35*(5*b^3*x^3 + 21*a*b^2*x^2 + 35*a^2*b*x + 35*a^3)*sqrt(x)

giac [A] time = 0.94, size = 35, normalized size = 0.74

$$\frac{2}{7}b^3x^{\frac{7}{2}} + \frac{6}{5}ab^2x^{\frac{5}{2}} + 2a^2bx^{\frac{3}{2}} + 2a^3\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(1/2),x, algorithm="giac")

[Out] 2/7*b^3*x^(7/2) + 6/5*a*b^2*x^(5/2) + 2*a^2*b*x^(3/2) + 2*a^3*sqrt(x)

maple [A] time = 0.00, size = 36, normalized size = 0.77

$$\frac{2(5b^3x^3 + 21ab^2x^2 + 35a^2bx + 35a^3)\sqrt{x}}{35}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/x^(1/2),x)

[Out] 2/35*x^(1/2)*(5*b^3*x^3+21*a*b^2*x^2+35*a^2*b*x+35*a^3)

maxima [A] time = 1.35, size = 35, normalized size = 0.74

$$\frac{2}{7}b^3x^{\frac{7}{2}} + \frac{6}{5}ab^2x^{\frac{5}{2}} + 2a^2bx^{\frac{3}{2}} + 2a^3\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(1/2),x, algorithm="maxima")

[Out] 2/7*b^3*x^(7/2) + 6/5*a*b^2*x^(5/2) + 2*a^2*b*x^(3/2) + 2*a^3*sqrt(x)

mupad [B] time = 0.04, size = 35, normalized size = 0.74

$$2a^3\sqrt{x} + \frac{2b^3x^{7/2}}{7} + 2a^2bx^{3/2} + \frac{6ab^2x^{5/2}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^(1/2), x)`

[Out] `2*a^3*x^(1/2) + (2*b^3*x^(7/2))/7 + 2*a^2*b*x^(3/2) + (6*a*b^2*x^(5/2))/5`

sympy [A] time = 0.44, size = 46, normalized size = 0.98

$$2a^3\sqrt{x} + 2a^2bx^{\frac{3}{2}} + \frac{6ab^2x^{\frac{5}{2}}}{5} + \frac{2b^3x^{\frac{7}{2}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**(1/2), x)`

[Out] `2*a**3*sqrt(x) + 2*a**2*b*x**(3/2) + 6*a*b**2*x**(5/2)/5 + 2*b**3*x**(7/2)/7`

$$3.447 \quad \int \frac{(a+bx)^3}{x^{3/2}} dx$$

Optimal. Leaf size=45

$$-\frac{2a^3}{\sqrt{x}} + 6a^2b\sqrt{x} + 2ab^2x^{3/2} + \frac{2}{5}b^3x^{5/2}$$

[Out] $2*a*b^2*x^{(3/2)}+2/5*b^3*x^{(5/2)}-2*a^3/x^{(1/2)}+6*a^2*b*x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$6a^2b\sqrt{x} - \frac{2a^3}{\sqrt{x}} + 2ab^2x^{3/2} + \frac{2}{5}b^3x^{5/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^(3/2), x]

[Out] $(-2*a^3)/\text{Sqrt}[x] + 6*a^2*b*\text{Sqrt}[x] + 2*a*b^2*x^{(3/2)} + (2*b^3*x^{(5/2)})/5$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^{3/2}} dx &= \int \left(\frac{a^3}{x^{3/2}} + \frac{3a^2b}{\sqrt{x}} + 3ab^2\sqrt{x} + b^3x^{3/2} \right) dx \\ &= -\frac{2a^3}{\sqrt{x}} + 6a^2b\sqrt{x} + 2ab^2x^{3/2} + \frac{2}{5}b^3x^{5/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 38, normalized size = 0.84

$$\frac{2(-5a^3 + 15a^2bx + 5ab^2x^2 + b^3x^3)}{5\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^(3/2), x]

[Out] (2*(-5*a^3 + 15*a^2*b*x + 5*a*b^2*x^2 + b^3*x^3))/(5*sqrt(x))

fricas [A] time = 0.41, size = 34, normalized size = 0.76

$$\frac{2(b^3x^3 + 5ab^2x^2 + 15a^2bx - 5a^3)}{5\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(3/2), x, algorithm="fricas")

[Out] 2/5*(b^3*x^3 + 5*a*b^2*x^2 + 15*a^2*b*x - 5*a^3)/sqrt(x)

giac [A] time = 1.03, size = 35, normalized size = 0.78

$$\frac{2}{5}b^3x^{\frac{5}{2}} + 2ab^2x^{\frac{3}{2}} + 6a^2b\sqrt{x} - \frac{2a^3}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(3/2), x, algorithm="giac")

[Out] 2/5*b^3*x^(5/2) + 2*a*b^2*x^(3/2) + 6*a^2*b*sqrt(x) - 2*a^3/sqrt(x)

maple [A] time = 0.00, size = 36, normalized size = 0.80

$$\frac{2(-b^3x^3 - 5ab^2x^2 - 15a^2bx + 5a^3)}{5\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/x^(3/2), x)

[Out] -2/5*(-b^3*x^3-5*a*b^2*x^2-15*a^2*b*x+5*a^3)/x^(1/2)

maxima [A] time = 1.36, size = 35, normalized size = 0.78

$$\frac{2}{5}b^3x^{\frac{5}{2}} + 2ab^2x^{\frac{3}{2}} + 6a^2b\sqrt{x} - \frac{2a^3}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(3/2), x, algorithm="maxima")

[Out] $2/5*b^3*x^{(5/2)} + 2*a*b^2*x^{(3/2)} + 6*a^2*b*\text{sqrt}(x) - 2*a^3/\text{sqrt}(x)$

mupad [B] time = 0.05, size = 35, normalized size = 0.78

$$\frac{2b^3x^{5/2}}{5} - \frac{2a^3}{\sqrt{x}} + 6a^2b\sqrt{x} + 2ab^2x^{3/2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^(3/2), x)`

[Out] $(2*b^3*x^{(5/2)})/5 - (2*a^3)/x^{(1/2)} + 6*a^2*b*x^{(1/2)} + 2*a*b^2*x^{(3/2)}$

sympy [A] time = 0.64, size = 44, normalized size = 0.98

$$-\frac{2a^3}{\sqrt{x}} + 6a^2b\sqrt{x} + 2ab^2x^{3/2} + \frac{2b^3x^{5/2}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**(3/2), x)`

[Out] $-2*a**3/\text{sqrt}(x) + 6*a**2*b*\text{sqrt}(x) + 2*a*b**2*x**(3/2) + 2*b**3*x**(5/2)/5$

$$3.448 \quad \int \frac{(a+bx)^3}{x^{5/2}} dx$$

Optimal. Leaf size=47

$$-\frac{2a^3}{3x^{3/2}} - \frac{6a^2b}{\sqrt{x}} + 6ab^2\sqrt{x} + \frac{2}{3}b^3x^{3/2}$$

[Out] $-2/3*a^3/x^{(3/2)}+2/3*b^3*x^{(3/2)}-6*a^2*b/x^{(1/2)}+6*a*b^2*x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{6a^2b}{\sqrt{x}} - \frac{2a^3}{3x^{3/2}} + 6ab^2\sqrt{x} + \frac{2}{3}b^3x^{3/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^3/x^{(5/2)}, x]$

[Out] $(-2*a^3)/(3*x^{(3/2)}) - (6*a^2*b)/\text{Sqrt}[x] + 6*a*b^2*\text{Sqrt}[x] + (2*b^3*x^{(3/2)})/3$

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n, x\} \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0]) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^{5/2}} dx &= \int \left(\frac{a^3}{x^{5/2}} + \frac{3a^2b}{x^{3/2}} + \frac{3ab^2}{\sqrt{x}} + b^3\sqrt{x} \right) dx \\ &= -\frac{2a^3}{3x^{3/2}} - \frac{6a^2b}{\sqrt{x}} + 6ab^2\sqrt{x} + \frac{2}{3}b^3x^{3/2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 38, normalized size = 0.81

$$\frac{2(-a^3 - 9a^2bx + 9ab^2x^2 + b^3x^3)}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^(5/2),x]

[Out] (2*(-a^3 - 9*a^2*b*x + 9*a*b^2*x^2 + b^3*x^3))/(3*x^(3/2))

fricas [A] time = 0.44, size = 34, normalized size = 0.72

$$\frac{2(b^3x^3 + 9ab^2x^2 - 9a^2bx - a^3)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(5/2),x, algorithm="fricas")

[Out] 2/3*(b^3*x^3 + 9*a*b^2*x^2 - 9*a^2*b*x - a^3)/x^(3/2)

giac [A] time = 1.07, size = 34, normalized size = 0.72

$$\frac{2}{3}b^3x^{\frac{3}{2}} + 6ab^2\sqrt{x} - \frac{2(9a^2bx + a^3)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(5/2),x, algorithm="giac")

[Out] 2/3*b^3*x^(3/2) + 6*a*b^2*sqrt(x) - 2/3*(9*a^2*b*x + a^3)/x^(3/2)

maple [A] time = 0.00, size = 34, normalized size = 0.72

$$-\frac{2(-b^3x^3 - 9ab^2x^2 + 9a^2bx + a^3)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/x^(5/2),x)

[Out] -2/3*(-b^3*x^3-9*a*b^2*x^2+9*a^2*b*x+a^3)/x^(3/2)

maxima [A] time = 1.37, size = 34, normalized size = 0.72

$$\frac{2}{3}b^3x^{\frac{3}{2}} + 6ab^2\sqrt{x} - \frac{2(9a^2bx + a^3)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(5/2),x, algorithm="maxima")

[Out] $\frac{2}{3}b^3x^{3/2} + 6ab^2\sqrt{x} - \frac{2}{3}(9a^2bx + a^3)/x^{3/2}$

mupad [B] time = 0.04, size = 35, normalized size = 0.74

$$\frac{2a^3 + 18a^2bx - 18ab^2x^2 - 2b^3x^3}{3x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^(5/2), x)`

[Out] $-(2a^3 - 2b^3x^3 - 18a^2bx^2 + 18a^2b^2x)/(3x^{3/2})$

sympy [A] time = 0.78, size = 46, normalized size = 0.98

$$-\frac{2a^3}{3x^{3/2}} - \frac{6a^2b}{\sqrt{x}} + 6ab^2\sqrt{x} + \frac{2b^3x^{3/2}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**(5/2), x)`

[Out] $-2a^3/(3x^{3/2}) - 6a^2b/\sqrt{x} + 6a^2b^2\sqrt{x} + 2b^3x^{3/2}/3$

$$3.449 \quad \int \frac{x^{5/2}}{a+bx} dx$$

Optimal. Leaf size=68

$$-\frac{2a^{5/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}} + \frac{2a^2\sqrt{x}}{b^3} - \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b}$$

[Out] $-2/3*a*x^{(3/2)}/b^2+2/5*x^{(5/2)}/b-2*a^{(5/2)}*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/b^{(7/2)}+2*a^2*x^{(1/2)}/b^3$

Rubi [A] time = 0.03, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {50, 63, 205}

$$\frac{2a^2\sqrt{x}}{b^3} - \frac{2a^{5/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}} - \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)/(a + b*x), x]

[Out] $(2*a^2*\text{Sqrt}[x])/b^3 - (2*a*x^{(3/2)})/(3*b^2) + (2*x^{(5/2)})/(5*b) - (2*a^{(5/2)})*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a])/b^{(7/2)}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{x^{5/2}}{a+bx} dx &= \frac{2x^{5/2}}{5b} - \frac{a \int \frac{x^{3/2}}{a+bx} dx}{b} \\
 &= -\frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b} + \frac{a^2 \int \frac{\sqrt{x}}{a+bx} dx}{b^2} \\
 &= \frac{2a^2\sqrt{x}}{b^3} - \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b} - \frac{a^3 \int \frac{1}{\sqrt{x}(a+bx)} dx}{b^3} \\
 &= \frac{2a^2\sqrt{x}}{b^3} - \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b} - \frac{(2a^3) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{b^3} \\
 &= \frac{2a^2\sqrt{x}}{b^3} - \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b} - \frac{2a^{5/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}}
 \end{aligned}$$

Mathematica [A] time = 0.03, size = 61, normalized size = 0.90

$$\frac{2\sqrt{x} (15a^2 - 5abx + 3b^2x^2)}{15b^3} - \frac{2a^{5/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/(a + b*x), x]

[Out] (2*Sqrt[x]*(15*a^2 - 5*a*b*x + 3*b^2*x^2))/(15*b^3) - (2*a^(5/2)*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/b^(7/2)

fricas [A] time = 0.44, size = 132, normalized size = 1.94

$$\left[\frac{15a^2\sqrt{\frac{-a}{b}} \log\left(\frac{bx-2b\sqrt{x}\sqrt{\frac{-a}{b}}-a}{bx+a}\right) + 2(3b^2x^2 - 5abx + 15a^2)\sqrt{x}}{15b^3}, - \frac{2\left(15a^2\sqrt{\frac{a}{b}} \arctan\left(\frac{b\sqrt{x}\sqrt{\frac{a}{b}}}{a}\right) - (3b^2x^2 - 5abx)\right)}{15b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a),x, algorithm="fricas")

[Out] [1/15*(15*a^2*sqrt(-a/b)*log((b*x - 2*b*sqrt(x)*sqrt(-a/b) - a)/(b*x + a)) + 2*(3*b^2*x^2 - 5*a*b*x + 15*a^2)*sqrt(x))/b^3, -2/15*(15*a^2*sqrt(a/b)*arctan(b*sqrt(x)*sqrt(a/b)/a) - (3*b^2*x^2 - 5*a*b*x + 15*a^2)*sqrt(x))/b^3]

giac [A] time = 0.87, size = 59, normalized size = 0.87

$$-\frac{2a^3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}b^3} + \frac{2\left(3b^4x^{\frac{5}{2}} - 5ab^3x^{\frac{3}{2}} + 15a^2b^2\sqrt{x}\right)}{15b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a),x, algorithm="giac")

[Out] -2*a^3*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*b^3) + 2/15*(3*b^4*x^(5/2) - 5*a*b^3*x^(3/2) + 15*a^2*b^2*sqrt(x))/b^5

maple [A] time = 0.01, size = 54, normalized size = 0.79

$$\frac{2x^{\frac{5}{2}}}{5b} - \frac{2a^3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}b^3} - \frac{2ax^{\frac{3}{2}}}{3b^2} + \frac{2a^2\sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x+a),x)

[Out] 2/5*x^(5/2)/b-2/3*a*x^(3/2)/b^2+2*a^2*x^(1/2)/b^3-2*a^3/b^3/(a*b)^(1/2)*arctan(x^(1/2)*b/(a*b)^(1/2))

maxima [A] time = 3.01, size = 54, normalized size = 0.79

$$-\frac{2a^3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}b^3} + \frac{2\left(3b^2x^{\frac{5}{2}} - 5abx^{\frac{3}{2}} + 15a^2\sqrt{x}\right)}{15b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a),x, algorithm="maxima")

[Out] -2*a^3*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*b^3) + 2/15*(3*b^2*x^(5/2) - 5*a*b*x^(3/2) + 15*a^2*sqrt(x))/b^3

mupad [B] time = 0.06, size = 48, normalized size = 0.71

$$\frac{2x^{5/2}}{5b} - \frac{2ax^{3/2}}{3b^2} + \frac{2a^2\sqrt{x}}{b^3} - \frac{2a^{5/2} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/2)/(a + b*x), x)`

[Out] $(2*x^{(5/2)})/(5*b) - (2*a*x^{(3/2)})/(3*b^2) + (2*a^2*x^{(1/2)})/b^3 - (2*a^{(5/2)})*atan((b^{(1/2)}*x^{(1/2)})/a^{(1/2)})/b^{(7/2)}$

sympy [A] time = 7.30, size = 121, normalized size = 1.78

$$\left\{ \begin{array}{ll} \frac{ia^{\frac{5}{2}} \log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{b^4 \sqrt{\frac{1}{b}}} - \frac{ia^{\frac{5}{2}} \log\left(i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{b^4 \sqrt{\frac{1}{b}}} + \frac{2a^2 \sqrt{x}}{b^3} - \frac{2ax^{\frac{3}{2}}}{3b^2} + \frac{2x^{\frac{5}{2}}}{5b} & \text{for } b \neq 0 \\ \frac{2x^{\frac{7}{2}}}{7a} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/2)/(b*x+a), x)`

[Out] `Piecewise((I*a**(5/2)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(b**4*sqrt(1/b)) - I*a**(5/2)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(b**4*sqrt(1/b)) + 2*a**2*sqrt(x)/b**3 - 2*a*x**(3/2)/(3*b**2) + 2*x**(5/2)/(5*b), Ne(b, 0)), (2*x**(7/2)/(7*a), True))`

$$3.450 \quad \int \frac{x^{3/2}}{a+bx} dx$$

Optimal. Leaf size=53

$$\frac{2a^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} - \frac{2a\sqrt{x}}{b^2} + \frac{2x^{3/2}}{3b}$$

[Out] $2/3*x^{(3/2)}/b+2*a^{(3/2)}*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/b^{(5/2)}-2*a*x^{(1/2)}/b^2$

Rubi [A] time = 0.02, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {50, 63, 205}

$$\frac{2a^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} - \frac{2a\sqrt{x}}{b^2} + \frac{2x^{3/2}}{3b}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)/(a + b*x), x]

[Out] $(-2*a*\text{Sqrt}[x])/b^2 + (2*x^{(3/2)})/(3*b) + (2*a^{(3/2)}*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/ \text{Sqrt}[a]])/b^{(5/2)}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

`Int[((a_) + (b_)*(x)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{x^{3/2}}{a+bx} dx &= \frac{2x^{3/2}}{3b} - \frac{a \int \frac{\sqrt{x}}{a+bx} dx}{b} \\
 &= -\frac{2a\sqrt{x}}{b^2} + \frac{2x^{3/2}}{3b} + \frac{a^2 \int \frac{1}{\sqrt{x}(a+bx)} dx}{b^2} \\
 &= -\frac{2a\sqrt{x}}{b^2} + \frac{2x^{3/2}}{3b} + \frac{(2a^2) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{b^2} \\
 &= -\frac{2a\sqrt{x}}{b^2} + \frac{2x^{3/2}}{3b} + \frac{2a^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.02, size = 49, normalized size = 0.92

$$\frac{2a^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} + \frac{2\sqrt{x}(bx-3a)}{3b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/(a + b*x), x]

[Out] (2*Sqrt[x]*(-3*a + b*x))/(3*b^2) + (2*a^(3/2)*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/b^(5/2)

fricas [A] time = 0.46, size = 103, normalized size = 1.94

$$\left[\frac{3a\sqrt{-\frac{a}{b}} \log\left(\frac{bx+2b\sqrt{x}\sqrt{-\frac{a}{b}}-a}{bx+a}\right) + 2(bx-3a)\sqrt{x}}{3b^2}, \frac{2\left(3a\sqrt{\frac{a}{b}} \arctan\left(\frac{b\sqrt{x}\sqrt{\frac{a}{b}}}{a}\right) + (bx-3a)\sqrt{x}\right)}{3b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a), x, algorithm="fricas")

[Out] $[1/3*(3*a*\sqrt{-a/b}*\log((b*x + 2*b*\sqrt{x})*\sqrt{-a/b} - a)/(b*x + a)) + 2*(b*x - 3*a)*\sqrt{x})/b^2, 2/3*(3*a*\sqrt{a/b}*\arctan(b*\sqrt{x})*\sqrt{a/b}/a) + (b*x - 3*a)*\sqrt{x})/b^2]$

giac [A] time = 1.24, size = 45, normalized size = 0.85

$$\frac{2a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^2} + \frac{2\left(b^2 x^{\frac{3}{2}} - 3ab\sqrt{x}\right)}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)/(b*x+a),x, algorithm="giac")`

[Out] $2*a^2*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*b^2) + 2/3*(b^2*x^{(3/2)} - 3*a*b*\sqrt{x})/b^3$

maple [A] time = 0.01, size = 43, normalized size = 0.81

$$\frac{2a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^2} + \frac{2x^{\frac{3}{2}}}{3b} - \frac{2a\sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(b*x+a),x)`

[Out] $2/3*x^{(3/2)}/b-2*a*x^{(1/2)}/b^2+2*a^2/b^2/(a*b)^{(1/2)}*\arctan(1/(a*b)^{(1/2)}*b*x^{(1/2)})$

maxima [A] time = 2.94, size = 42, normalized size = 0.79

$$\frac{2a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^2} + \frac{2\left(bx^{\frac{3}{2}} - 3a\sqrt{x}\right)}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)/(b*x+a),x, algorithm="maxima")`

[Out] $2*a^2*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*b^2) + 2/3*(b*x^{(3/2)} - 3*a*\sqrt{x})/b^2$

mupad [B] time = 0.05, size = 37, normalized size = 0.70

$$\frac{2x^{3/2}}{3b} - \frac{2a\sqrt{x}}{b^2} + \frac{2a^{3/2} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(a + b*x), x)`

[Out] $(2*x^{(3/2)})/(3*b) - (2*a*x^{(1/2)})/b^2 + (2*a^{(3/2)}*atan((b^{(1/2)}*x^{(1/2)})/a^{(1/2)}))/b^{(5/2)}$

sympy [A] time = 1.93, size = 105, normalized size = 1.98

$$\begin{cases} -\frac{ia^{\frac{3}{2}} \log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{b^3\sqrt{\frac{1}{b}}} + \frac{ia^{\frac{3}{2}} \log\left(i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{b^3\sqrt{\frac{1}{b}}} - \frac{2a\sqrt{x}}{b^2} + \frac{2x^{\frac{3}{2}}}{3b} & \text{for } b \neq 0 \\ \frac{2x^{\frac{5}{2}}}{5a} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(b*x+a), x)`

[Out] `Piecewise((-I*a**(3/2)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(b**3*sqrt(1/b)) + I*a**(3/2)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(b**3*sqrt(1/b)) - 2*a*sqrt(x)/b**2 + 2*x**(3/2)/(3*b), Ne(b, 0)), (2*x**(5/2)/(5*a), True))`

$$3.451 \quad \int \frac{\sqrt{x}}{a+bx} dx$$

Optimal. Leaf size=40

$$\frac{2\sqrt{x}}{b} - \frac{2\sqrt{a} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}}$$

[Out] $-2*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})*a^{(1/2)}/b^{(3/2)}+2*x^{(1/2)}/b$

Rubi [A] time = 0.01, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {50, 63, 205}

$$\frac{2\sqrt{x}}{b} - \frac{2\sqrt{a} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(a + b*x), x]

[Out] $(2*\text{Sqrt}[x])/b - (2*\text{Sqrt}[a]*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a]])/b^{(3/2)}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{x}}{a+bx} dx &= \frac{2\sqrt{x}}{b} - \frac{a \int \frac{1}{\sqrt{x}(a+bx)} dx}{b} \\
&= \frac{2\sqrt{x}}{b} - \frac{(2a) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{b} \\
&= \frac{2\sqrt{x}}{b} - \frac{2\sqrt{a} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 1.00

$$\frac{2\sqrt{x}}{b} - \frac{2\sqrt{a} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(a + b*x), x]

[Out] (2*Sqrt[x])/b - (2*Sqrt[a]*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/b^(3/2)

fricas [A] time = 0.49, size = 85, normalized size = 2.12

$$\left[\frac{\sqrt{\frac{-a}{b}} \log\left(\frac{bx - 2b\sqrt{x}\sqrt{\frac{-a}{b}} - a}{bx+a}\right) + 2\sqrt{x}}{b}, -\frac{2\left(\sqrt{\frac{a}{b}} \arctan\left(\frac{b\sqrt{x}\sqrt{\frac{a}{b}}}{a}\right) - \sqrt{x}\right)}{b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a), x, algorithm="fricas")

[Out] [(sqrt(-a/b)*log((b*x - 2*b*sqrt(x)*sqrt(-a/b) - a)/(b*x + a)) + 2*sqrt(x))/b, -2*(sqrt(a/b)*arctan(b*sqrt(x)*sqrt(a/b)/a) - sqrt(x))/b]

giac [A] time = 0.99, size = 31, normalized size = 0.78

$$-\frac{2a \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}b} + \frac{2\sqrt{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a),x, algorithm="giac")

[Out] $-2*a*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*b) + 2*\sqrt{x}/b$

maple [A] time = 0.01, size = 32, normalized size = 0.80

$$-\frac{2a \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b} + \frac{2\sqrt{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x+a),x)

[Out] $2*x^(1/2)/b-2*a/b/(a*b)^(1/2)*\arctan(1/(a*b)^(1/2)*b*x^(1/2))$

maxima [A] time = 2.97, size = 31, normalized size = 0.78

$$-\frac{2 a \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b} + \frac{2\sqrt{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a),x, algorithm="maxima")

[Out] $-2*a*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*b) + 2*\sqrt{x}/b$

mupad [B] time = 0.04, size = 28, normalized size = 0.70

$$\frac{2\sqrt{x}}{b} - \frac{2\sqrt{a} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(a + b*x),x)

[Out] $(2*x^(1/2))/b - (2*a^(1/2)*\operatorname{atan}((b^(1/2)*x^(1/2))/a^(1/2)))/b^(3/2)$

sympy [A] time = 0.72, size = 92, normalized size = 2.30

$$\left\{ \begin{array}{ll} \frac{i\sqrt{a} \log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{b^2\sqrt{\frac{1}{b}}} - \frac{i\sqrt{a} \log\left(i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{b^2\sqrt{\frac{1}{b}}} + \frac{2\sqrt{x}}{b} & \text{for } b \neq 0 \\ \frac{2x^{\frac{3}{2}}}{3a} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(1/2)/(b*x+a),x)
```

```
[Out] Piecewise((I*sqrt(a)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(b**2*sqrt(1/b)) -  
I*sqrt(a)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(b**2*sqrt(1/b)) + 2*sqrt(x)/  
b, Ne(b, 0)), (2*x**(3/2)/(3*a), True))
```

$$3.452 \quad \int \frac{1}{\sqrt{x}(a+bx)} dx$$

Optimal. Leaf size=29

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{a} \sqrt{b}}$$

[Out] 2*arctan(b^(1/2)*x^(1/2)/a^(1/2))/a^(1/2)/b^(1/2)

Rubi [A] time = 0.01, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {63, 205}

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{a} \sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(a + b*x)),x]

[Out] (2*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[a]*Sqrt[b])

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{x}(a+bx)} dx &= 2 \text{Subst} \left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x} \right) \\ &= \frac{2 \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{a} \sqrt{b}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 1.00

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{a} \sqrt{b}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(a + b*x)),x]

[Out] (2*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[a]*Sqrt[b])

fricas [A] time = 0.47, size = 68, normalized size = 2.34

$$\left[-\frac{\sqrt{-ab} \log\left(\frac{bx-a-2\sqrt{-ab}\sqrt{x}}{bx+a}\right)}{ab}, -\frac{2\sqrt{ab} \arctan\left(\frac{\sqrt{ab}}{b\sqrt{x}}\right)}{ab} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/x^(1/2),x, algorithm="fricas")

[Out] [-sqrt(-a*b)*log((b*x - a - 2*sqrt(-a*b)*sqrt(x))/(b*x + a))/(a*b), -2*sqrt(a*b)*arctan(sqrt(a*b)/(b*sqrt(x)))/(a*b)]

giac [A] time = 0.95, size = 18, normalized size = 0.62

$$\frac{2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/x^(1/2),x, algorithm="giac")

[Out] 2*arctan(b*sqrt(x)/sqrt(a*b))/sqrt(a*b)

maple [A] time = 0.01, size = 19, normalized size = 0.66

$$\frac{2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)/x^(1/2),x)

[Out] $2/(a*b)^{(1/2)}*\arctan(1/(a*b)^{(1/2)}*b*x^{(1/2)})$

maxima [A] time = 2.93, size = 18, normalized size = 0.62

$$\frac{2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/x^(1/2),x, algorithm="maxima")`

[Out] $2*\arctan(b*\sqrt{x}/\sqrt{a*b})/\sqrt{a*b}$

mupad [B] time = 0.04, size = 19, normalized size = 0.66

$$\frac{2 \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a} \sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(a + b*x)),x)`

[Out] $(2*\operatorname{atan}((b^{(1/2)}*x^{(1/2)})/a^{(1/2)}))/(a^{(1/2)}*b^{(1/2)})$

sympy [A] time = 1.29, size = 94, normalized size = 3.24

$$\begin{cases} \frac{\infty}{\sqrt{x}} & \text{for } a = 0 \wedge b = 0 \\ -\frac{2}{b\sqrt{x}} & \text{for } a = 0 \\ \frac{2\sqrt{x}}{a} & \text{for } b = 0 \\ -\frac{i \log\left(-i\sqrt{a} \sqrt{\frac{1}{b}} + \sqrt{x}\right)}{\sqrt{a}b\sqrt{\frac{1}{b}}} + \frac{i \log\left(i\sqrt{a} \sqrt{\frac{1}{b}} + \sqrt{x}\right)}{\sqrt{a}b\sqrt{\frac{1}{b}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/x**(1/2),x)`

[Out] `Piecewise((zoo/sqrt(x), Eq(a, 0) & Eq(b, 0)), (-2/(b*sqrt(x)), Eq(a, 0)), (2*sqrt(x)/a, Eq(b, 0)), (-I*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(sqrt(a)*b*sqrt(1/b)) + I*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(sqrt(a)*b*sqrt(1/b)), True))`

$$3.453 \quad \int \frac{1}{x^{3/2}(a+bx)} dx$$

Optimal. Leaf size=40

$$-\frac{2\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}} - \frac{2}{a\sqrt{x}}$$

[Out] $-2*\arctan(b^{(1/2)*x^{(1/2)}/a^{(1/2)})*b^{(1/2)}/a^{(3/2)}-2/a/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 205}

$$-\frac{2\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}} - \frac{2}{a\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(a + b*x)),x]

[Out] $-2/(a*\text{Sqrt}[x]) - (2*\text{Sqrt}[b]*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/ \text{Sqrt}[a]])/a^{(3/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{3/2}(a+bx)} dx &= -\frac{2}{a\sqrt{x}} - \frac{b \int \frac{1}{\sqrt{x}(a+bx)} dx}{a} \\
&= -\frac{2}{a\sqrt{x}} - \frac{(2b) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{a} \\
&= -\frac{2}{a\sqrt{x}} - \frac{2\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 25, normalized size = 0.62

$$-\frac{{}_2F_1\left(-\frac{1}{2}, 1; \frac{1}{2}; -\frac{bx}{a}\right)}{a\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(a + b*x)),x]

[Out] (-2*Hypergeometric2F1[-1/2, 1, 1/2, -((b*x)/a)])/(a*Sqrt[x])

fricas [A] time = 0.47, size = 93, normalized size = 2.32

$$\left[\frac{x\sqrt{-\frac{b}{a}} \log\left(\frac{bx-2a\sqrt{x}\sqrt{-\frac{b}{a}}-a}{bx+a}\right) - 2\sqrt{x}}{ax}, \frac{2\left(x\sqrt{\frac{b}{a}} \arctan\left(\frac{a\sqrt{\frac{b}{a}}}{b\sqrt{x}}\right) - \sqrt{x}\right)}{ax} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a),x, algorithm="fricas")

[Out] [(x*sqrt(-b/a)*log((b*x - 2*a*sqrt(x)*sqrt(-b/a) - a)/(b*x + a)) - 2*sqrt(x))/(a*x), 2*(x*sqrt(b/a)*arctan(a*sqrt(b/a)/(b*sqrt(x))) - sqrt(x))/(a*x)]

giac [A] time = 1.00, size = 31, normalized size = 0.78

$$-\frac{2b \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}a} - \frac{2}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a),x, algorithm="giac")

[Out] $-2*b*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*a) - 2/(a*\sqrt{x})$

maple [A] time = 0.01, size = 32, normalized size = 0.80

$$-\frac{2b \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a} - \frac{2}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2)/(b*x+a),x)

[Out] $-2/a/x^{(1/2)}-2/a*b/(a*b)^{(1/2)}*\arctan(1/(a*b)^{(1/2)}*b*x^{(1/2)})$

maxima [A] time = 2.88, size = 31, normalized size = 0.78

$$-\frac{2 b \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a} - \frac{2}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a),x, algorithm="maxima")

[Out] $-2*b*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*a) - 2/(a*\sqrt{x})$

mupad [B] time = 0.04, size = 28, normalized size = 0.70

$$-\frac{2}{a\sqrt{x}} - \frac{2\sqrt{b} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(3/2)*(a + b*x)),x)

[Out] $-2/(a*x^{(1/2)}) - (2*b^{(1/2)}*\operatorname{atan}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)}))/a^{(3/2)}$

sympy [A] time = 2.77, size = 102, normalized size = 2.55

$$\left\{ \begin{array}{ll} \frac{\infty}{x^{\frac{3}{2}}} & \text{for } a = 0 \wedge b = 0 \\ -\frac{2}{a\sqrt{x}} & \text{for } b = 0 \\ -\frac{2}{3bx^{\frac{3}{2}}} & \text{for } a = 0 \\ -\frac{2}{a\sqrt{x}} + \frac{i \log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{3}{2}}\sqrt{\frac{1}{b}}} - \frac{i \log\left(i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{3}{2}}\sqrt{\frac{1}{b}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(3/2)/(b*x+a),x)

[Out] Piecewise((zoo/x**(3/2), Eq(a, 0) & Eq(b, 0)), (-2/(a*sqrt(x)), Eq(b, 0)), (-2/(3*b*x**(3/2)), Eq(a, 0)), (-2/(a*sqrt(x)) + I*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(3/2)*sqrt(1/b)) - I*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(3/2)*sqrt(1/b)), True))

$$3.454 \quad \int \frac{1}{x^{5/2}(a+bx)} dx$$

Optimal. Leaf size=53

$$\frac{2b^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}} + \frac{2b}{a^2\sqrt{x}} - \frac{2}{3ax^{3/2}}$$

[Out] $-2/3/a/x^{(3/2)}+2*b^{(3/2)}*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/a^{(5/2)}+2*b/a^2/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 205}

$$\frac{2b^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}} + \frac{2b}{a^2\sqrt{x}} - \frac{2}{3ax^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(a + b*x)),x]

[Out] $-2/(3*a*x^{(3/2)}) + (2*b)/(a^2*\text{Sqrt}[x]) + (2*b^{(3/2)}*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a]])/a^{(5/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

`Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{5/2}(a+bx)} dx &= -\frac{2}{3ax^{3/2}} - \frac{b \int \frac{1}{x^{3/2}(a+bx)} dx}{a} \\
 &= -\frac{2}{3ax^{3/2}} + \frac{2b}{a^2\sqrt{x}} + \frac{b^2 \int \frac{1}{\sqrt{x}(a+bx)} dx}{a^2} \\
 &= -\frac{2}{3ax^{3/2}} + \frac{2b}{a^2\sqrt{x}} + \frac{(2b^2) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{a^2} \\
 &= -\frac{2}{3ax^{3/2}} + \frac{2b}{a^2\sqrt{x}} + \frac{2b^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 27, normalized size = 0.51

$$-\frac{{}_2F_1\left(-\frac{3}{2}, 1; -\frac{1}{2}; -\frac{bx}{a}\right)}{3ax^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(a + b*x)), x]

[Out] (-2*Hypergeometric2F1[-3/2, 1, -1/2, -(b*x)/a])/(3*a*x^(3/2))

fricas [A] time = 0.46, size = 118, normalized size = 2.23

$$\left[\frac{3bx^2\sqrt{-\frac{b}{a}} \log\left(\frac{bx+2a\sqrt{x}\sqrt{\frac{b}{a}-a}}{bx+a}\right) + 2(3bx-a)\sqrt{x}}{3a^2x^2}, -\frac{2\left(3bx^2\sqrt{\frac{b}{a}} \arctan\left(\frac{a\sqrt{\frac{b}{a}}}{b\sqrt{x}}\right) - (3bx-a)\sqrt{x}\right)}{3a^2x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a), x, algorithm="fricas")

[Out] $[1/3*(3*b*x^2*\sqrt{-b/a}*\log((b*x + 2*a*\sqrt{x})*\sqrt{-b/a} - a)/(b*x + a) + 2*(3*b*x - a)*\sqrt{x})/(a^2*x^2), -2/3*(3*b*x^2*\sqrt{b/a}*\arctan(a*\sqrt{b/a}/(b*\sqrt{x})) - (3*b*x - a)*\sqrt{x})/(a^2*x^2)]$

giac [A] time = 1.16, size = 41, normalized size = 0.77

$$\frac{2b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^2} + \frac{2(3bx - a)}{3a^2 x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2)/(b*x+a),x, algorithm="giac")`

[Out] $2*b^2*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*a^2) + 2/3*(3*b*x - a)/(a^2*x^{(3/2)})$

maple [A] time = 0.01, size = 43, normalized size = 0.81

$$\frac{2b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^2} + \frac{2b}{a^2 \sqrt{x}} - \frac{2}{3a x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/2)/(b*x+a),x)`

[Out] $-2/3/a/x^{(3/2)}+2*b/a^2/x^{(1/2)}+2/a^2*b^2/(a*b)^{(1/2)}*\arctan(1/(a*b)^{(1/2)}*b*x^{(1/2)})$

maxima [A] time = 3.02, size = 41, normalized size = 0.77

$$\frac{2b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^2} + \frac{2(3bx - a)}{3a^2 x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2)/(b*x+a),x, algorithm="maxima")`

[Out] $2*b^2*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*a^2) + 2/3*(3*b*x - a)/(a^2*x^{(3/2)})$

mupad [B] time = 0.10, size = 38, normalized size = 0.72

$$\frac{2b^{3/2} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{2}{3a} - \frac{2bx}{a^2 x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/2)*(a + b*x)),x)`

[Out] $(2*b^{(3/2)}*atan((b^{(1/2)}*x^{(1/2)})/a^{(1/2)}))/a^{(5/2)} - (2/(3*a) - (2*b*x)/a^2)/x^{(3/2)}$

sympy [A] time = 7.83, size = 121, normalized size = 2.28

$$\left\{ \begin{array}{ll} \frac{\infty}{x^2} & \text{for } a = 0 \wedge b = 0 \\ -\frac{2}{3ax^2} & \text{for } b = 0 \\ -\frac{2}{5bx^2} & \text{for } a = 0 \\ -\frac{2}{3ax^2} + \frac{2b}{a^2\sqrt{x}} - \frac{ib \log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{5}{2}}\sqrt{\frac{1}{b}}} + \frac{ib \log\left(i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{5}{2}}\sqrt{\frac{1}{b}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(b*x+a),x)`

[Out] `Piecewise((zoo/x**(5/2), Eq(a, 0) & Eq(b, 0)), (-2/(3*a*x**(3/2)), Eq(b, 0)), (-2/(5*b*x**(5/2)), Eq(a, 0)), (-2/(3*a*x**(3/2)) + 2*b/(a**2*sqrt(x)) - I*b*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(5/2)*sqrt(1/b)) + I*b*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(5/2)*sqrt(1/b)), True))`

$$3.455 \quad \int \frac{1}{x^{7/2}(a+bx)} dx$$

Optimal. Leaf size=68

$$-\frac{2b^{5/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}} - \frac{2b^2}{a^3\sqrt{x}} + \frac{2b}{3a^2x^{3/2}} - \frac{2}{5ax^{5/2}}$$

[Out] $-2/5/a/x^{(5/2)}+2/3*b/a^2/x^{(3/2)}-2*b^{(5/2)}*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/a^{(7/2)}-2*b^2/a^3/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 205}

$$-\frac{2b^2}{a^3\sqrt{x}} - \frac{2b^{5/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}} + \frac{2b}{3a^2x^{3/2}} - \frac{2}{5ax^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(7/2)*(a + b*x)),x]

[Out] $-2/(5*a*x^{(5/2)}) + (2*b)/(3*a^2*x^{(3/2)}) - (2*b^2)/(a^3*\text{Sqrt}[x]) - (2*b^{(5/2)}* \text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/ \text{Sqrt}[a]])/a^{(7/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

`Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{7/2}(a+bx)} dx &= -\frac{2}{5ax^{5/2}} - \frac{b \int \frac{1}{x^{5/2}(a+bx)} dx}{a} \\
 &= -\frac{2}{5ax^{5/2}} + \frac{2b}{3a^2x^{3/2}} + \frac{b^2 \int \frac{1}{x^{3/2}(a+bx)} dx}{a^2} \\
 &= -\frac{2}{5ax^{5/2}} + \frac{2b}{3a^2x^{3/2}} - \frac{2b^2}{a^3\sqrt{x}} - \frac{b^3 \int \frac{1}{\sqrt{x}(a+bx)} dx}{a^3} \\
 &= -\frac{2}{5ax^{5/2}} + \frac{2b}{3a^2x^{3/2}} - \frac{2b^2}{a^3\sqrt{x}} - \frac{(2b^3) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{a^3} \\
 &= -\frac{2}{5ax^{5/2}} + \frac{2b}{3a^2x^{3/2}} - \frac{2b^2}{a^3\sqrt{x}} - \frac{2b^{5/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 27, normalized size = 0.40

$$\frac{{}_2F_1\left(-\frac{5}{2}, 1; -\frac{3}{2}; -\frac{bx}{a}\right)}{5ax^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(7/2)*(a + b*x)), x]

[Out] (-2*Hypergeometric2F1[-5/2, 1, -3/2, -((b*x)/a)])/(5*a*x^(5/2))

fricas [A] time = 0.46, size = 144, normalized size = 2.12

$$\left[\frac{15 b^2 x^3 \sqrt{-\frac{b}{a}} \log\left(\frac{bx-2a\sqrt{x}\sqrt{-\frac{b}{a}}-a}{bx+a}\right) - 2(15 b^2 x^2 - 5 abx + 3 a^2)\sqrt{x}}{15 a^3 x^3}, \frac{2\left(15 b^2 x^3 \sqrt{\frac{b}{a}} \arctan\left(\frac{a\sqrt{\frac{b}{a}}}{b\sqrt{x}}\right) - (15 b^2 x^2 - 5 abx + 3 a^2)\sqrt{x}\right)}{15 a^3 x^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+a),x, algorithm="fricas")

[Out] [1/15*(15*b^2*x^3*sqrt(-b/a)*log((b*x - 2*a*sqrt(x)*sqrt(-b/a) - a)/(b*x + a)) - 2*(15*b^2*x^2 - 5*a*b*x + 3*a^2)*sqrt(x))/(a^3*x^3), 2/15*(15*b^2*x^3*sqrt(b/a)*arctan(a*sqrt(b/a)/(b*sqrt(x))) - (15*b^2*x^2 - 5*a*b*x + 3*a^2)*sqrt(x))/(a^3*x^3)]

giac [A] time = 0.99, size = 52, normalized size = 0.76

$$\frac{2b^3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^3} - \frac{2(15b^2x^2 - 5abx + 3a^2)}{15a^3x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+a),x, algorithm="giac")

[Out] -2*b^3*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a^3) - 2/15*(15*b^2*x^2 - 5*a*b*x + 3*a^2)/(a^3*x^(5/2))

maple [A] time = 0.01, size = 54, normalized size = 0.79

$$-\frac{2b^3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^3} - \frac{2b^2}{a^3\sqrt{x}} + \frac{2b}{3a^2x^{\frac{3}{2}}} - \frac{2}{5ax^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(7/2)/(b*x+a),x)

[Out] -2/5/a/x^(5/2)-2*b^2/a^3/x^(1/2)+2/3*b/a^2/x^(3/2)-2/a^3*b^3/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.91, size = 52, normalized size = 0.76

$$\frac{2b^3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^3} - \frac{2(15b^2x^2 - 5abx + 3a^2)}{15a^3x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+a),x, algorithm="maxima")

[Out] -2*b^3*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a^3) - 2/15*(15*b^2*x^2 - 5*a*b*x + 3*a^2)/(a^3*x^(5/2))

mupad [B] time = 0.11, size = 49, normalized size = 0.72

$$-\frac{\frac{2}{5a} + \frac{2b^2x^2}{a^3} - \frac{2bx}{3a^2}}{x^{5/2}} - \frac{2b^{5/2} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(7/2)*(a + b*x)),x)`

[Out] $-\left(\frac{2}{5a} + \frac{2b^2x^2}{a^3} - \frac{2bx}{3a^2}\right)/x^{5/2} - \frac{2b^{5/2} \operatorname{atan}\left(\frac{b^{1/2}x^{1/2}}{a^{1/2}}\right)}{a^{7/2}}$

sympy [A] time = 24.82, size = 139, normalized size = 2.04

$$\left\{ \begin{array}{ll} \frac{\infty}{x^2} & \text{for } a = 0 \wedge b = 0 \\ -\frac{2}{7bx^2} & \text{for } a = 0 \\ -\frac{2}{5ax^2} & \text{for } b = 0 \\ -\frac{2}{5ax^2} + \frac{2b}{3a^2x^3} - \frac{2b^2}{a^3\sqrt{x}} + \frac{ib^2 \log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{7}{2}}\sqrt{\frac{1}{b}}} - \frac{ib^2 \log\left(i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{7}{2}}\sqrt{\frac{1}{b}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(7/2)/(b*x+a),x)`

[Out] `Piecewise((zoo/x**(7/2), Eq(a, 0) & Eq(b, 0)), (-2/(7*b*x**(7/2)), Eq(a, 0)), (-2/(5*a*x**(5/2)), Eq(b, 0)), (-2/(5*a*x**(5/2)) + 2*b/(3*a**2*x**(3/2)) - 2*b**2/(a**3*sqrt(x)) + I*b**2*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(7/2)*sqrt(1/b)) - I*b**2*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(7/2)*sqrt(1/b)), True))`

$$3.456 \quad \int \frac{x^{5/2}}{(a+bx)^2} dx$$

Optimal. Leaf size=70

$$\frac{5a^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}} - \frac{5a\sqrt{x}}{b^3} - \frac{x^{5/2}}{b(a+bx)} + \frac{5x^{3/2}}{3b^2}$$

[Out] $5/3*x^{(3/2)}/b^2-x^{(5/2)}/b/(b*x+a)+5*a^{(3/2)}*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/b^{(7/2)}-5*a*x^{(1/2)}/b^3$

Rubi [A] time = 0.02, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 205}

$$\frac{5a^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}} - \frac{5a\sqrt{x}}{b^3} - \frac{x^{5/2}}{b(a+bx)} + \frac{5x^{3/2}}{3b^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(5/2)}/(a + b*x)^2, x]$

[Out] $(-5*a*\text{Sqrt}[x])/b^3 + (5*x^{(3/2)})/(3*b^2) - x^{(5/2)}/(b*(a + b*x)) + (5*a^{(3/2)}*2)*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/(\text{Sqrt}[a])]/b^{(7/2)}$

Rule 47

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \text{Dist}[(d*n)/(b*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(a+bx)^2} dx &= -\frac{x^{5/2}}{b(a+bx)} + \frac{5 \int \frac{x^{3/2}}{a+bx} dx}{2b} \\
&= \frac{5x^{3/2}}{3b^2} - \frac{x^{5/2}}{b(a+bx)} - \frac{(5a) \int \frac{\sqrt{x}}{a+bx} dx}{2b^2} \\
&= -\frac{5a\sqrt{x}}{b^3} + \frac{5x^{3/2}}{3b^2} - \frac{x^{5/2}}{b(a+bx)} + \frac{(5a^2) \int \frac{1}{\sqrt{x}(a+bx)} dx}{2b^3} \\
&= -\frac{5a\sqrt{x}}{b^3} + \frac{5x^{3/2}}{3b^2} - \frac{x^{5/2}}{b(a+bx)} + \frac{(5a^2) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{b^3} \\
&= -\frac{5a\sqrt{x}}{b^3} + \frac{5x^{3/2}}{3b^2} - \frac{x^{5/2}}{b(a+bx)} + \frac{5a^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.39

$$\frac{2x^{7/2} {}_2F_1\left(2, \frac{7}{2}; \frac{9}{2}; -\frac{bx}{a}\right)}{7a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/(a + b*x)^2, x]

[Out] (2*x^(7/2)*Hypergeometric2F1[2, 7/2, 9/2, -(b*x)/a])/(7*a^2)

fricas [A] time = 0.47, size = 161, normalized size = 2.30

$$\left[\frac{15 (abx + a^2) \sqrt{-\frac{a}{b}} \log\left(\frac{bx + 2b\sqrt{x} \sqrt{-\frac{a}{b}} - a}{bx + a}\right) + 2 (2b^2x^2 - 10abx - 15a^2) \sqrt{x}}{6 (b^4x + ab^3)}, \frac{15 (abx + a^2) \sqrt{\frac{a}{b}} \arctan\left(\frac{b\sqrt{x} \sqrt{\frac{a}{b}}}{a}\right) + (2b^2x^2 - 10abx - 15a^2) \sqrt{x}}{3 (b^4x + ab^3)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] [1/6*(15*(a*b*x + a^2)*sqrt(-a/b)*log((b*x + 2*b*sqrt(x)*sqrt(-a/b) - a)/(b*x + a)) + 2*(2*b^2*x^2 - 10*a*b*x - 15*a^2)*sqrt(x))/(b^4*x + a*b^3), 1/3*(15*(a*b*x + a^2)*sqrt(a/b)*arctan(b*sqrt(x)*sqrt(a/b)/a) + (2*b^2*x^2 - 10*a*b*x - 15*a^2)*sqrt(x))/(b^4*x + a*b^3)]

giac [A] time = 0.93, size = 65, normalized size = 0.93

$$\frac{5a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^3} - \frac{a^2 \sqrt{x}}{(bx + a)b^3} + \frac{2(b^4x^{\frac{3}{2}} - 6ab^3\sqrt{x})}{3b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^2,x, algorithm="giac")

[Out] 5*a^2*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*b^3) - a^2*sqrt(x)/((b*x + a)*b^3) + 2/3*(b^4*x^(3/2) - 6*a*b^3*sqrt(x))/b^6

maple [A] time = 0.01, size = 61, normalized size = 0.87

$$\frac{5a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^3} - \frac{a^2 \sqrt{x}}{(bx + a)b^3} + \frac{2x^{\frac{3}{2}}}{3b^2} - \frac{4a\sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x+a)^2,x)

[Out] 2/3*x^(3/2)/b^2-4*a*x^(1/2)/b^3-1/b^3*a^2*x^(1/2)/(b*x+a)+5/b^3*a^2/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.96, size = 63, normalized size = 0.90

$$-\frac{a^2 \sqrt{x}}{b^4x + ab^3} + \frac{5a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^3} + \frac{2(bx^{\frac{3}{2}} - 6a\sqrt{x})}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^2,x, algorithm="maxima")

[Out] $-a^2\sqrt{x}/(b^4x + a*b^3) + 5*a^2*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b} * b^3) + 2/3*(b*x^{3/2} - 6*a*\sqrt{x})/b^3$

mupad [B] time = 0.11, size = 58, normalized size = 0.83

$$\frac{2x^{3/2}}{3b^2} - \frac{4a\sqrt{x}}{b^3} - \frac{a^2\sqrt{x}}{xb^4 + ab^3} + \frac{5a^{3/2}\operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(a + b*x)^2,x)

[Out] $(2*x^{3/2})/(3*b^2) - (4*a*x^{1/2})/b^3 - (a^2*x^{1/2})/(a*b^3 + b^4*x) + (5*a^{3/2}*atan((b^{1/2}*x^{1/2})/a^{1/2}))/b^{7/2}$

sympy [A] time = 24.57, size = 479, normalized size = 6.84

$$\left\{ \begin{array}{l} \infty x^2 \\ \frac{2x^2}{7a^2} \\ \frac{2x^2}{3b^2} \\ -\frac{30ia^{\frac{5}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{6ia^{\frac{3}{2}}b^4\sqrt{\frac{1}{b}}+6i\sqrt{a}b^5x\sqrt{\frac{1}{b}}} - \frac{20ia^{\frac{3}{2}}b^2x^2\sqrt{\frac{1}{b}}}{6ia^{\frac{3}{2}}b^4\sqrt{\frac{1}{b}}+6i\sqrt{a}b^5x\sqrt{\frac{1}{b}}} + \frac{4i\sqrt{a}b^3x^2\sqrt{\frac{1}{b}}}{6ia^{\frac{3}{2}}b^4\sqrt{\frac{1}{b}}+6i\sqrt{a}b^5x\sqrt{\frac{1}{b}}} + \frac{15a^3\log\left(-i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{6ia^{\frac{3}{2}}b^4\sqrt{\frac{1}{b}}+6i\sqrt{a}b^5x\sqrt{\frac{1}{b}}} - \frac{15a^3\log\left(i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{6ia^{\frac{3}{2}}b^4\sqrt{\frac{1}{b}}+6i\sqrt{a}b^5x\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(b*x+a)**2,x)

[Out] Piecewise((zoo*x**(3/2), Eq(a, 0) & Eq(b, 0)), (2*x**(7/2)/(7*a**2), Eq(b, 0)), (2*x**(3/2)/(3*b**2), Eq(a, 0)), (-30*I*a**(5/2)*b*sqrt(x)*sqrt(1/b)/(6*I*a**(3/2)*b**4*sqrt(1/b) + 6*I*sqrt(a)*b**5*x*sqrt(1/b)) - 20*I*a**(3/2)*b**2*x**(3/2)*sqrt(1/b)/(6*I*a**(3/2)*b**4*sqrt(1/b) + 6*I*sqrt(a)*b**5*x*sqrt(1/b)) + 4*I*sqrt(a)*b**3*x**(5/2)*sqrt(1/b)/(6*I*a**(3/2)*b**4*sqrt(1/b) + 6*I*sqrt(a)*b**5*x*sqrt(1/b)) + 15*a**3*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(6*I*a**(3/2)*b**4*sqrt(1/b) + 6*I*sqrt(a)*b**5*x*sqrt(1/b)) - 15*a**3*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(6*I*a**(3/2)*b**4*sqrt(1/b) + 6*I*sqrt(a)*b**5*x*sqrt(1/b)) + 15*a**2*b*x*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(6

```
*I*a**(3/2)*b**4*sqrt(1/b) + 6*I*sqrt(a)*b**5*x*sqrt(1/b)) - 15*a**2*b*x*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(6*I*a**(3/2)*b**4*sqrt(1/b) + 6*I*sqrt(a)*b**5*x*sqrt(1/b)), True))
```

$$3.457 \quad \int \frac{x^{3/2}}{(a+bx)^2} dx$$

Optimal. Leaf size=57

$$-\frac{3\sqrt{a} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} - \frac{x^{3/2}}{b(a+bx)} + \frac{3\sqrt{x}}{b^2}$$

[Out] $-x^{(3/2)}/b/(b*x+a)-3*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})*a^{(1/2)}/b^{(5/2)}+3*x^{(1/2)}/b^2$

Rubi [A] time = 0.02, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 205}

$$-\frac{3\sqrt{a} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} - \frac{x^{3/2}}{b(a+bx)} + \frac{3\sqrt{x}}{b^2}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)/(a + b*x)^2,x]

[Out] (3*Sqrt[x])/b^2 - x^(3/2)/(b*(a + b*x)) - (3*Sqrt[a]*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/b^(5/2)

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned} \int \frac{x^{3/2}}{(a+bx)^2} dx &= -\frac{x^{3/2}}{b(a+bx)} + \frac{3}{2b} \int \frac{\sqrt{x}}{a+bx} dx \\ &= \frac{3\sqrt{x}}{b^2} - \frac{x^{3/2}}{b(a+bx)} - \frac{(3a) \int \frac{1}{\sqrt{x}(a+bx)} dx}{2b^2} \\ &= \frac{3\sqrt{x}}{b^2} - \frac{x^{3/2}}{b(a+bx)} - \frac{(3a) \operatorname{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{b^2} \\ &= \frac{3\sqrt{x}}{b^2} - \frac{x^{3/2}}{b(a+bx)} - \frac{3\sqrt{a} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} \end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.47

$$\frac{2x^{5/2} {}_2F_1\left(2, \frac{5}{2}; \frac{7}{2}; -\frac{bx}{a}\right)}{5a^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(3/2)/(a + b*x)^2, x]
```

```
[Out] (2*x^(5/2)*Hypergeometric2F1[2, 5/2, 7/2, -(b*x)/a])/(5*a^2)
```

fricas [A] time = 0.44, size = 134, normalized size = 2.35

$$\left[\frac{3(bx+a)\sqrt{-\frac{a}{b}} \log\left(\frac{bx-2b\sqrt{x}\sqrt{-\frac{a}{b}}-a}{bx+a}\right) + 2(2bx+3a)\sqrt{x}}{2(b^3x+ab^2)}, -\frac{3(bx+a)\sqrt{\frac{a}{b}} \arctan\left(\frac{b\sqrt{x}\sqrt{\frac{a}{b}}}{a}\right) - (2bx+3a)\sqrt{x}}{b^3x+ab^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] [1/2*(3*(b*x + a)*sqrt(-a/b)*log((b*x - 2*b*sqrt(x)*sqrt(-a/b) - a)/(b*x + a)) + 2*(2*b*x + 3*a)*sqrt(x))/(b^3*x + a*b^2), -(3*(b*x + a)*sqrt(a/b)*arc tan(b*sqrt(x)*sqrt(a/b)/a) - (2*b*x + 3*a)*sqrt(x))/(b^3*x + a*b^2)]

giac [A] time = 0.96, size = 46, normalized size = 0.81

$$-\frac{3 a \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^2} + \frac{a\sqrt{x}}{(bx+a)b^2} + \frac{2\sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^2,x, algorithm="giac")

[Out] -3*a*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*b^2) + a*sqrt(x)/((b*x + a)*b^2) + 2*sqrt(x)/b^2

maple [A] time = 0.01, size = 47, normalized size = 0.82

$$-\frac{3a \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^2} + \frac{a\sqrt{x}}{(bx+a)b^2} + \frac{2\sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(b*x+a)^2,x)

[Out] 2*x^(1/2)/b^2+1/b^2*a*x^(1/2)/(b*x+a)-3/b^2*a/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.91, size = 49, normalized size = 0.86

$$\frac{a\sqrt{x}}{b^3x+ab^2} - \frac{3 a \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^2} + \frac{2\sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^2,x, algorithm="maxima")

[Out] a*sqrt(x)/(b^3*x + a*b^2) - 3*a*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*b^2) + 2*sqrt(x)/b^2

mupad [B] time = 0.12, size = 46, normalized size = 0.81

$$\frac{2\sqrt{x}}{b^2} + \frac{a\sqrt{x}}{xb^3 + ab^2} - \frac{3\sqrt{a} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(a + b*x)^2,x)`

[Out] $(2*x^{(1/2)})/b^2 + (a*x^{(1/2)})/(a*b^2 + b^3*x) - (3*a^{(1/2)}*atan((b^{(1/2)}*x^{(1/2)})/a^{(1/2)}))/b^{(5/2)}$

sympy [A] time = 9.18, size = 411, normalized size = 7.21

$$\left\{ \begin{array}{l} \infty\sqrt{x} \\ \frac{2x^2}{5a^2} \\ \frac{2\sqrt{x}}{b^2} \\ \frac{6ia^{\frac{3}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{2ia^{\frac{3}{2}}b^3\sqrt{\frac{1}{b}}+2i\sqrt{a}b^4x\sqrt{\frac{1}{b}}} + \frac{4i\sqrt{a}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{2ia^{\frac{3}{2}}b^3\sqrt{\frac{1}{b}}+2i\sqrt{a}b^4x\sqrt{\frac{1}{b}}} - \frac{3a^2 \log\left(-i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{3}{2}}b^3\sqrt{\frac{1}{b}}+2i\sqrt{a}b^4x\sqrt{\frac{1}{b}}} + \frac{3a^2 \log\left(i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{3}{2}}b^3\sqrt{\frac{1}{b}}+2i\sqrt{a}b^4x\sqrt{\frac{1}{b}}} - \frac{3abx \log\left(-i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{3}{2}}b^3\sqrt{\frac{1}{b}}+2i\sqrt{a}b^4x\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(b*x+a)**2,x)`

[Out] `Piecewise((zoo*sqrt(x), Eq(a, 0) & Eq(b, 0)), (2*x**(5/2)/(5*a**2), Eq(b, 0)), (2*sqrt(x)/b**2, Eq(a, 0)), (6*I*a**(3/2)*b*sqrt(x)*sqrt(1/b)/(2*I*a**(3/2)*b**3*sqrt(1/b) + 2*I*sqrt(a)*b**4*x*sqrt(1/b)) + 4*I*sqrt(a)*b**2*x**(3/2)*sqrt(1/b)/(2*I*a**(3/2)*b**3*sqrt(1/b) + 2*I*sqrt(a)*b**4*x*sqrt(1/b)) - 3*a**2*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(3/2)*b**3*sqrt(1/b) + 2*I*sqrt(a)*b**4*x*sqrt(1/b)) + 3*a**2*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(3/2)*b**3*sqrt(1/b) + 2*I*sqrt(a)*b**4*x*sqrt(1/b)) - 3*a*b*x*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(3/2)*b**3*sqrt(1/b) + 2*I*sqrt(a)*b**4*x*sqrt(1/b)) + 3*a*b*x*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(3/2)*b**3*sqrt(1/b) + 2*I*sqrt(a)*b**4*x*sqrt(1/b)), True))`

$$3.458 \quad \int \frac{\sqrt{x}}{(a+bx)^2} dx$$

Optimal. Leaf size=46

$$\frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}b^{3/2}} - \frac{\sqrt{x}}{b(a+bx)}$$

[Out] arctan(b^(1/2)*x^(1/2)/a^(1/2))/b^(3/2)/a^(1/2)-x^(1/2)/b/(b*x+a)

Rubi [A] time = 0.01, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {47, 63, 205}

$$\frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}b^{3/2}} - \frac{\sqrt{x}}{b(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(a + b*x)^2,x]

[Out] -(Sqrt[x]/(b*(a + b*x))) + ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]]/(Sqrt[a]*b^(3/2))

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{x}}{(a+bx)^2} dx &= -\frac{\sqrt{x}}{b(a+bx)} + \frac{\int \frac{1}{\sqrt{x}(a+bx)} dx}{2b} \\
&= -\frac{\sqrt{x}}{b(a+bx)} + \frac{\text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{b} \\
&= -\frac{\sqrt{x}}{b(a+bx)} + \frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 1.00

$$\frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}b^{3/2}} - \frac{\sqrt{x}}{b(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(a + b*x)^2, x]

[Out] -(Sqrt[x]/(b*(a + b*x))) + ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]]/(Sqrt[a]*b^(3/2))

fricas [A] time = 0.46, size = 115, normalized size = 2.50

$$\left[-\frac{2ab\sqrt{x} + \sqrt{-ab}(bx+a) \log\left(\frac{bx-a-2\sqrt{-ab}\sqrt{x}}{bx+a}\right)}{2(ab^3x + a^2b^2)}, -\frac{ab\sqrt{x} + \sqrt{ab}(bx+a) \arctan\left(\frac{\sqrt{ab}}{b\sqrt{x}}\right)}{ab^3x + a^2b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^2, x, algorithm="fricas")

[Out] [-1/2*(2*a*b*sqrt(x) + sqrt(-a*b)*(b*x + a)*log((b*x - a - 2*sqrt(-a*b)*sqrt(x))/(b*x + a)))/(a*b^3*x + a^2*b^2), -(a*b*sqrt(x) + sqrt(a*b)*(b*x + a)*arctan(sqrt(a*b)/(b*sqrt(x))))/(a*b^3*x + a^2*b^2)]

giac [A] time = 0.90, size = 36, normalized size = 0.78

$$\frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}b} - \frac{\sqrt{x}}{(bx+a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^2,x, algorithm="giac")

[Out] arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*b) - sqrt(x)/((b*x + a)*b)

maple [A] time = 0.01, size = 37, normalized size = 0.80

$$\frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b} - \frac{\sqrt{x}}{(bx + a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x+a)^2,x)

[Out] -x^(1/2)/b/(b*x+a)+1/b/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.94, size = 37, normalized size = 0.80

$$-\frac{\sqrt{x}}{b^2x + ab} + \frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^2,x, algorithm="maxima")

[Out] -sqrt(x)/(b^2*x + a*b) + arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*b)

mupad [B] time = 0.04, size = 34, normalized size = 0.74

$$\frac{\operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a} b^{3/2}} - \frac{\sqrt{x}}{b(a + bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(a + b*x)^2,x)

[Out] atan((b^(1/2)*x^(1/2))/a^(1/2))/(a^(1/2)*b^(3/2)) - x^(1/2)/(b*(a + b*x))

sympy [A] time = 4.45, size = 337, normalized size = 7.33

$$\left\{ \begin{array}{l} \frac{\infty}{\sqrt{x}} \\ \frac{2x^{\frac{3}{2}}}{3a^2} \\ -\frac{2}{b^2\sqrt{x}} \\ -\frac{2i\sqrt{a}b\sqrt{x}\sqrt{\frac{1}{b}}}{2ia^{\frac{3}{2}}b^2\sqrt{\frac{1}{b}}+2i\sqrt{a}b^3x\sqrt{\frac{1}{b}}} + \frac{a\log\left(-i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{3}{2}}b^2\sqrt{\frac{1}{b}}+2i\sqrt{a}b^3x\sqrt{\frac{1}{b}}} - \frac{a\log\left(i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{3}{2}}b^2\sqrt{\frac{1}{b}}+2i\sqrt{a}b^3x\sqrt{\frac{1}{b}}} + \frac{bx\log\left(-i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{3}{2}}b^2\sqrt{\frac{1}{b}}+2i\sqrt{a}b^3x\sqrt{\frac{1}{b}}} - \frac{bx\log\left(i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{3}{2}}b^2\sqrt{\frac{1}{b}}+2i\sqrt{a}b^3x\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(1/2)/(b*x+a)**2,x)

[Out] Piecewise((zoo/sqrt(x), Eq(a, 0) & Eq(b, 0)), (2*x**(3/2)/(3*a**2), Eq(b, 0)), (-2/(b**2*sqrt(x)), Eq(a, 0)), (-2*I*sqrt(a)*b*sqrt(x)*sqrt(1/b)/(2*I*a**(3/2)*b**2*sqrt(1/b) + 2*I*sqrt(a)*b**3*x*sqrt(1/b)) + a*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(3/2)*b**2*sqrt(1/b) + 2*I*sqrt(a)*b**3*x*sqrt(1/b)) - a*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(3/2)*b**2*sqrt(1/b) + 2*I*sqrt(a)*b**3*x*sqrt(1/b)) + b*x*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(3/2)*b**2*sqrt(1/b) + 2*I*sqrt(a)*b**3*x*sqrt(1/b)) - b*x*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(3/2)*b**2*sqrt(1/b) + 2*I*sqrt(a)*b**3*x*sqrt(1/b)), True))

$$3.459 \quad \int \frac{1}{\sqrt{x}(a+bx)^2} dx$$

Optimal. Leaf size=45

$$\frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}\sqrt{b}} + \frac{\sqrt{x}}{a(a+bx)}$$

[Out] arctan(b^(1/2)*x^(1/2)/a^(1/2))/a^(3/2)/b^(1/2)+x^(1/2)/a/(b*x+a)

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 205}

$$\frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}\sqrt{b}} + \frac{\sqrt{x}}{a(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(a + b*x)^2), x]

[Out] Sqrt[x]/(a*(a + b*x)) + ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]]/(a^(3/2)*Sqrt[b])

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt{x}(a+bx)^2} dx &= \frac{\sqrt{x}}{a(a+bx)} + \frac{\int \frac{1}{\sqrt{x}(a+bx)} dx}{2a} \\
&= \frac{\sqrt{x}}{a(a+bx)} + \frac{\text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{a} \\
&= \frac{\sqrt{x}}{a(a+bx)} + \frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}\sqrt{b}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 1.00

$$\frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}\sqrt{b}} + \frac{\sqrt{x}}{a^2 + abx}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(a + b*x)^2), x]

[Out] Sqrt[x]/(a^2 + a*b*x) + ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]]/(a^(3/2)*Sqrt[b])

fricas [A] time = 0.45, size = 116, normalized size = 2.58

$$\left[\frac{2ab\sqrt{x} - \sqrt{-ab}(bx+a) \log\left(\frac{bx-a-2\sqrt{-ab}\sqrt{x}}{bx+a}\right)}{2(a^2b^2x + a^3b)}, \frac{ab\sqrt{x} - \sqrt{ab}(bx+a) \arctan\left(\frac{\sqrt{ab}}{b\sqrt{x}}\right)}{a^2b^2x + a^3b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/x^(1/2), x, algorithm="fricas")

[Out] [1/2*(2*a*b*sqrt(x) - sqrt(-a*b)*(b*x + a)*log((b*x - a - 2*sqrt(-a*b)*sqrt(x))/(b*x + a)))/(a^2*b^2*x + a^3*b), (a*b*sqrt(x) - sqrt(a*b)*(b*x + a)*arctan(sqrt(a*b)/(b*sqrt(x))))/(a^2*b^2*x + a^3*b)]

giac [A] time = 0.89, size = 35, normalized size = 0.78

$$\frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}a} + \frac{\sqrt{x}}{(bx+a)a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/x^(1/2),x, algorithm="giac")

[Out] arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a) + sqrt(x)/((b*x + a)*a)

maple [A] time = 0.01, size = 36, normalized size = 0.80

$$\frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a} + \frac{\sqrt{x}}{(bx + a) a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/x^(1/2),x)

[Out] x^(1/2)/a/(b*x+a)+1/a/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.92, size = 35, normalized size = 0.78

$$\frac{\sqrt{x}}{abx + a^2} + \frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/x^(1/2),x, algorithm="maxima")

[Out] sqrt(x)/(a*b*x + a^2) + arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a)

mupad [B] time = 0.09, size = 33, normalized size = 0.73

$$\frac{\sqrt{x}}{a(a + bx)} + \frac{\operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/2)*(a + b*x)^2),x)

[Out] x^(1/2)/(a*(a + b*x)) + atan((b^(1/2)*x^(1/2))/a^(1/2))/(a^(3/2)*b^(1/2))

sympy [A] time = 7.53, size = 328, normalized size = 7.29

$$\left\{ \begin{array}{l} \frac{\infty}{3} \\ x^2 \\ \frac{2\sqrt{x}}{a^2} \\ \frac{2}{3b^2x^2} \\ \frac{2i\sqrt{a}b\sqrt{x}\sqrt{\frac{1}{b}}}{2ia^{\frac{5}{2}}b\sqrt{\frac{1}{b}}+2ia^{\frac{3}{2}}b^2x\sqrt{\frac{1}{b}}} + \frac{a\log\left(-i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{5}{2}}b\sqrt{\frac{1}{b}}+2ia^{\frac{3}{2}}b^2x\sqrt{\frac{1}{b}}} - \frac{a\log\left(i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{5}{2}}b\sqrt{\frac{1}{b}}+2ia^{\frac{3}{2}}b^2x\sqrt{\frac{1}{b}}} + \frac{bx\log\left(-i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{5}{2}}b\sqrt{\frac{1}{b}}+2ia^{\frac{3}{2}}b^2x\sqrt{\frac{1}{b}}} - \frac{bx\log\left(i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2ia^{\frac{5}{2}}b\sqrt{\frac{1}{b}}+2ia^{\frac{3}{2}}b^2x\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2/x**(1/2),x)

[Out] Piecewise((zoo/x**(3/2), Eq(a, 0) & Eq(b, 0)), (2*sqrt(x)/a**2, Eq(b, 0)), (-2/(3*b**2*x**(3/2)), Eq(a, 0)), (2*I*sqrt(a)*b*sqrt(x)*sqrt(1/b)/(2*I*a**(5/2)*b*sqrt(1/b) + 2*I*a**(3/2)*b**2*x*sqrt(1/b)) + a*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(5/2)*b*sqrt(1/b) + 2*I*a**(3/2)*b**2*x*sqrt(1/b)) - a*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(5/2)*b*sqrt(1/b) + 2*I*a**(3/2)*b**2*x*sqrt(1/b)) + b*x*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(5/2)*b*sqrt(1/b) + 2*I*a**(3/2)*b**2*x*sqrt(1/b)) - b*x*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(5/2)*b*sqrt(1/b) + 2*I*a**(3/2)*b**2*x*sqrt(1/b)), True))

$$3.460 \quad \int \frac{1}{x^{3/2}(a+bx)^2} dx$$

Optimal. Leaf size=56

$$-\frac{3\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{3}{a^2\sqrt{x}} + \frac{1}{a\sqrt{x}(a+bx)}$$

[Out] $-3*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})*b^{(1/2)}/a^{(5/2)}-3/a^2/x^{(1/2)}+1/a/(b*x+a)/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 205}

$$-\frac{3\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{3}{a^2\sqrt{x}} + \frac{1}{a\sqrt{x}(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(a + b*x)^2), x]

[Out] $-3/(a^2*\text{Sqrt}[x]) + 1/(a*\text{Sqrt}[x]*(a + b*x)) - (3*\text{Sqrt}[b]*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a]])/a^{(5/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

`Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{3/2}(a+bx)^2} dx &= \frac{1}{a\sqrt{x}(a+bx)} + \frac{3 \int \frac{1}{x^{3/2}(a+bx)} dx}{2a} \\
 &= -\frac{3}{a^2\sqrt{x}} + \frac{1}{a\sqrt{x}(a+bx)} - \frac{(3b) \int \frac{1}{\sqrt{x}(a+bx)} dx}{2a^2} \\
 &= -\frac{3}{a^2\sqrt{x}} + \frac{1}{a\sqrt{x}(a+bx)} - \frac{(3b) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{a^2} \\
 &= -\frac{3}{a^2\sqrt{x}} + \frac{1}{a\sqrt{x}(a+bx)} - \frac{3\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.00, size = 25, normalized size = 0.45

$$-\frac{{}_2F_1\left(-\frac{1}{2}, 2; \frac{1}{2}; -\frac{bx}{a}\right)}{a^2\sqrt{x}}$$

Antiderivative was successfully verified.

[In] `Integrate[1/(x^(3/2)*(a + b*x)^2), x]`

[Out] `(-2*Hypergeometric2F1[-1/2, 2, 1/2, -((b*x)/a)])/(a^2*Sqrt[x])`

fricas [A] time = 0.44, size = 147, normalized size = 2.62

$$\left[\frac{3(bx^2 + ax)\sqrt{-\frac{b}{a}} \log\left(\frac{bx - 2a\sqrt{x}\sqrt{-\frac{b}{a}} - a}{bx+a}\right) - 2(3bx + 2a)\sqrt{x}}{2(a^2bx^2 + a^3x)}, \frac{3(bx^2 + ax)\sqrt{\frac{b}{a}} \arctan\left(\frac{a\sqrt{\frac{b}{a}}}{b\sqrt{x}}\right) - (3bx + 2a)\sqrt{x}}{a^2bx^2 + a^3x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(b*x+a)^2, x, algorithm="fricas")`

[Out] $[1/2*(3*(b*x^2 + a*x)*\sqrt{-b/a}*\log((b*x - 2*a*\sqrt{x})*\sqrt{-b/a} - a)/(b*x + a)) - 2*(3*b*x + 2*a)*\sqrt{x})/(a^2*b*x^2 + a^3*x), (3*(b*x^2 + a*x)*\sqrt{b/a}*\arctan(a*\sqrt{b/a}/(b*\sqrt{x}))) - (3*b*x + 2*a)*\sqrt{x})/(a^2*b*x^2 + a^3*x)]$

giac [A] time = 1.01, size = 49, normalized size = 0.88

$$-\frac{3b \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^2} - \frac{3bx + 2a}{\left(bx^{\frac{3}{2}} + a\sqrt{x}\right)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(b*x+a)^2,x, algorithm="giac")`

[Out] $-3*b*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*a^2) - (3*b*x + 2*a)/((b*x^{(3/2)} + a*\sqrt{x})*a^2)$

maple [A] time = 0.01, size = 48, normalized size = 0.86

$$-\frac{3b \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^2} - \frac{b\sqrt{x}}{(bx + a)a^2} - \frac{2}{a^2\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(3/2)/(b*x+a)^2,x)`

[Out] $-2/a^2/x^{(1/2)} - 1/a^2*b*x^{(1/2)}/(b*x+a) - 3/a^2*b/(a*b)^{(1/2)}*\arctan(1/(a*b)^{(1/2)}*b*x^{(1/2)})$

maxima [A] time = 2.94, size = 51, normalized size = 0.91

$$-\frac{3bx + 2a}{a^2bx^{\frac{3}{2}} + a^3\sqrt{x}} - \frac{3b \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(b*x+a)^2,x, algorithm="maxima")`

[Out] $-(3*b*x + 2*a)/(a^2*b*x^{(3/2)} + a^3*\sqrt{x}) - 3*b*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*a^2)$

mupad [B] time = 0.12, size = 48, normalized size = 0.86

$$-\frac{\frac{2}{a} + \frac{3bx}{a^2}}{a\sqrt{x} + bx^{3/2}} - \frac{3\sqrt{b} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(a + b*x)^2), x)`

[Out] $-\frac{2}{a + (3bx)/a^2} / (ax^{1/2} + bx^{3/2}) - \frac{(3b^{1/2}) \operatorname{atan}((b^{1/2})x^{1/2}) / a^{1/2}}{a^{5/2}}$

sympy [A] time = 17.73, size = 434, normalized size = 7.75

$$\left\{ \begin{array}{l} \frac{\infty}{x^2} \\ -\frac{2}{5b^2x^2} \\ -\frac{2}{a^2\sqrt{x}} \\ -\frac{4ia^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{2ia^{\frac{7}{2}}\sqrt{x}\sqrt{\frac{1}{b}} + 2ia^{\frac{5}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}}} - \frac{6i\sqrt{a}bx\sqrt{\frac{1}{b}}}{2ia^{\frac{7}{2}}\sqrt{x}\sqrt{\frac{1}{b}} + 2ia^{\frac{5}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}}} - \frac{3a\sqrt{x}\log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{2ia^{\frac{7}{2}}\sqrt{x}\sqrt{\frac{1}{b}} + 2ia^{\frac{5}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}}} + \frac{3a\sqrt{x}\log\left(i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{2ia^{\frac{7}{2}}\sqrt{x}\sqrt{\frac{1}{b}} + 2ia^{\frac{5}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}}} - \frac{3bx^{\frac{3}{2}}\log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{2ia^{\frac{7}{2}}\sqrt{x}\sqrt{\frac{1}{b}} + 2ia^{\frac{5}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(b*x+a)**2, x)`

[Out] `Piecewise((zoo/x**(5/2), Eq(a, 0) & Eq(b, 0)), (-2/(5*b**2*x**(5/2)), Eq(a, 0)), (-2/(a**2*sqrt(x)), Eq(b, 0)), (-4*I*a**(3/2)*sqrt(1/b)/(2*I*a**(7/2)*sqrt(x)*sqrt(1/b) + 2*I*a**(5/2)*b*x**(3/2)*sqrt(1/b)) - 6*I*sqrt(a)*b*x*sqrt(1/b)/(2*I*a**(7/2)*sqrt(x)*sqrt(1/b) + 2*I*a**(5/2)*b*x**(3/2)*sqrt(1/b)) - 3*a*sqrt(x)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(7/2)*sqrt(x)*sqrt(1/b) + 2*I*a**(5/2)*b*x**(3/2)*sqrt(1/b)) + 3*a*sqrt(x)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(7/2)*sqrt(x)*sqrt(1/b) + 2*I*a**(5/2)*b*x**(3/2)*sqrt(1/b)) - 3*b*x**(3/2)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(7/2)*sqrt(x)*sqrt(1/b) + 2*I*a**(5/2)*b*x**(3/2)*sqrt(1/b)) + 3*b*x**(3/2)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(2*I*a**(7/2)*sqrt(x)*sqrt(1/b) + 2*I*a**(5/2)*b*x**(3/2)*sqrt(1/b)), True))`

$$3.461 \quad \int \frac{1}{x^{5/2}(a+bx)^2} dx$$

Optimal. Leaf size=69

$$\frac{5b^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}} + \frac{5b}{a^3\sqrt{x}} - \frac{5}{3a^2x^{3/2}} + \frac{1}{ax^{3/2}(a+bx)}$$

[Out] $-5/3/a^2/x^{(3/2)}+1/a/x^{(3/2)}/(b*x+a)+5*b^{(3/2)}*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/a^{(7/2)}+5*b/a^3/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 205}

$$\frac{5b^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}} + \frac{5b}{a^3\sqrt{x}} - \frac{5}{3a^2x^{3/2}} + \frac{1}{ax^{3/2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(a + b*x)^2), x]

[Out] $-5/(3*a^2*x^{(3/2)}) + (5*b)/(a^3*\text{Sqrt}[x]) + 1/(a*x^{(3/2)}*(a + b*x)) + (5*b^{(3/2)}*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a]])/a^{(7/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{5/2}(a+bx)^2} dx &= \frac{1}{ax^{3/2}(a+bx)} + \frac{5 \int \frac{1}{x^{5/2}(a+bx)} dx}{2a} \\
 &= -\frac{5}{3a^2x^{3/2}} + \frac{1}{ax^{3/2}(a+bx)} - \frac{(5b) \int \frac{1}{x^{3/2}(a+bx)} dx}{2a^2} \\
 &= -\frac{5}{3a^2x^{3/2}} + \frac{5b}{a^3\sqrt{x}} + \frac{1}{ax^{3/2}(a+bx)} + \frac{(5b^2) \int \frac{1}{\sqrt{x}(a+bx)} dx}{2a^3} \\
 &= -\frac{5}{3a^2x^{3/2}} + \frac{5b}{a^3\sqrt{x}} + \frac{1}{ax^{3/2}(a+bx)} + \frac{(5b^2) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{a^3} \\
 &= -\frac{5}{3a^2x^{3/2}} + \frac{5b}{a^3\sqrt{x}} + \frac{1}{ax^{3/2}(a+bx)} + \frac{5b^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 27, normalized size = 0.39

$$-\frac{{}_2F_1\left(-\frac{3}{2}, 2; -\frac{1}{2}; -\frac{bx}{a}\right)}{3a^2x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(a + b*x)^2), x]

[Out] (-2*Hypergeometric2F1[-3/2, 2, -1/2, -(b*x)/a])/(3*a^2*x^(3/2))

fricas [A] time = 0.46, size = 184, normalized size = 2.67

$$\left[\frac{15(b^2x^3 + abx^2)\sqrt{-\frac{b}{a}} \log\left(\frac{bx+2a\sqrt{x}\sqrt{-\frac{b}{a}}-a}{bx+a}\right) + 2(15b^2x^2 + 10abx - 2a^2)\sqrt{x}}{6(a^3bx^3 + a^4x^2)}, -\frac{15(b^2x^3 + abx^2)\sqrt{\frac{b}{a}} \arctan\left(\frac{a\sqrt{\frac{b}{a}}}{b\sqrt{x}}\right)}{3(a^3bx^3 + a^4x^2)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] [1/6*(15*(b^2*x^3 + a*b*x^2)*sqrt(-b/a)*log((b*x + 2*a*sqrt(x))*sqrt(-b/a) - a)/(b*x + a)) + 2*(15*b^2*x^2 + 10*a*b*x - 2*a^2)*sqrt(x))/(a^3*b*x^3 + a^4*x^2), -1/3*(15*(b^2*x^3 + a*b*x^2)*sqrt(b/a)*arctan(a*sqrt(b/a)/(b*sqrt(x)))) - (15*b^2*x^2 + 10*a*b*x - 2*a^2)*sqrt(x))/(a^3*b*x^3 + a^4*x^2)]

giac [A] time = 0.96, size = 58, normalized size = 0.84

$$\frac{5b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^3} + \frac{b^2\sqrt{x}}{(bx+a)a^3} + \frac{2(6bx-a)}{3a^3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^2,x, algorithm="giac")

[Out] 5*b^2*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a^3) + b^2*sqrt(x)/((b*x + a)*a^3) + 2/3*(6*b*x - a)/(a^3*x^(3/2))

maple [A] time = 0.02, size = 60, normalized size = 0.87

$$\frac{5b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^3} + \frac{b^2\sqrt{x}}{(bx+a)a^3} + \frac{4b}{a^3\sqrt{x}} - \frac{2}{3a^2x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(5/2)/(b*x+a)^2,x)

[Out] -2/3/a^2/x^(3/2)+4*b/a^3/x^(1/2)+1/a^3*b^2*x^(1/2)/(b*x+a)+5/a^3*b^2/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.88, size = 64, normalized size = 0.93

$$\frac{15b^2x^2 + 10abx - 2a^2}{3\left(a^3bx^{\frac{5}{2}} + a^4x^{\frac{3}{2}}\right)} + \frac{5b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^2,x, algorithm="maxima")

[Out] 1/3*(15*b^2*x^2 + 10*a*b*x - 2*a^2)/(a^3*b*x^(5/2) + a^4*x^(3/2)) + 5*b^2*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a^3)

mupad [B] time = 0.15, size = 58, normalized size = 0.84

$$\frac{\frac{5b^2x^2}{a^3} - \frac{2}{3a} + \frac{10bx}{3a^2}}{ax^{3/2} + bx^{5/2}} + \frac{5b^{3/2} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/2)*(a + b*x)^2), x)`

[Out] $((5b^2x^2)/a^3 - 2/(3a) + (10bx)/(3a^2))/(ax^{3/2} + bx^{5/2}) + (5b^{3/2} \operatorname{atan}((b^{1/2}x^{1/2})/a^{1/2}))/a^{7/2}$

sympy [A] time = 50.52, size = 507, normalized size = 7.35

$$\left\{ \begin{array}{l} \frac{\infty}{7} \\ x^2 \\ -\frac{2}{3a^2x^2} \\ -\frac{2}{7b^2x^2} \\ -\frac{4ia^{\frac{5}{2}}\sqrt{\frac{1}{b}}}{6ia^{\frac{9}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 6ia^{\frac{7}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}}} + \frac{20ia^{\frac{3}{2}}bx\sqrt{\frac{1}{b}}}{6ia^{\frac{9}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 6ia^{\frac{7}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}}} + \frac{30i\sqrt{a}b^2x^2\sqrt{\frac{1}{b}}}{6ia^{\frac{9}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 6ia^{\frac{7}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}}} + \frac{15abx^{\frac{3}{2}}\log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{6ia^{\frac{9}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 6ia^{\frac{7}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}}} - \frac{15abx^{\frac{3}{2}}\log\left(i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{6ia^{\frac{9}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 6ia^{\frac{7}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(b*x+a)**2, x)`

[Out] `Piecewise((zoo/x**(7/2), Eq(a, 0) & Eq(b, 0)), (-2/(3*a**2*x**(3/2)), Eq(b, 0)), (-2/(7*b**2*x**(7/2)), Eq(a, 0)), (-4*I*a**(5/2)*sqrt(1/b)/(6*I*a**(9/2)*x**(3/2)*sqrt(1/b) + 6*I*a**(7/2)*b*x**(5/2)*sqrt(1/b)) + 20*I*a**(3/2)*b*x*sqrt(1/b)/(6*I*a**(9/2)*x**(3/2)*sqrt(1/b) + 6*I*a**(7/2)*b*x**(5/2)*sqrt(1/b)) + 30*I*sqrt(a)*b**2*x**2*sqrt(1/b)/(6*I*a**(9/2)*x**(3/2)*sqrt(1/b) + 6*I*a**(7/2)*b*x**(5/2)*sqrt(1/b)) + 15*a*b*x**(3/2)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(6*I*a**(9/2)*x**(3/2)*sqrt(1/b) + 6*I*a**(7/2)*b*x**(5/2)*sqrt(1/b)) - 15*a*b*x**(3/2)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(6*I*a**(9/2)*x**(3/2)*sqrt(1/b) + 6*I*a**(7/2)*b*x**(5/2)*sqrt(1/b)) + 15*b**2*x**(5/2)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(6*I*a**(9/2)*x**(3/2)*sqrt(1/b) + 6*I*a**(7/2)*b*x**(5/2)*sqrt(1/b)) - 15*b**2*x**(5/2)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(6*I*a**(9/2)*x**(3/2)*sqrt(1/b) + 6*I*a**(7/2)*b*x**(5/2)*sqrt(1/b)), True))`

$$3.462 \quad \int \frac{x^{7/2}}{(a+bx)^3} dx$$

Optimal. Leaf size=95

$$\frac{35a^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{9/2}} - \frac{35a\sqrt{x}}{4b^4} - \frac{7x^{5/2}}{4b^2(a+bx)} - \frac{x^{7/2}}{2b(a+bx)^2} + \frac{35x^{3/2}}{12b^3}$$

[Out] 35/12*x^(3/2)/b^3-1/2*x^(7/2)/b/(b*x+a)^2-7/4*x^(5/2)/b^2/(b*x+a)+35/4*a^(3/2)*arctan(b^(1/2)*x^(1/2)/a^(1/2))/b^(9/2)-35/4*a*x^(1/2)/b^4

Rubi [A] time = 0.03, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 205}

$$\frac{35a^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{9/2}} - \frac{7x^{5/2}}{4b^2(a+bx)} - \frac{35a\sqrt{x}}{4b^4} - \frac{x^{7/2}}{2b(a+bx)^2} + \frac{35x^{3/2}}{12b^3}$$

Antiderivative was successfully verified.

[In] Int[x^(7/2)/(a + b*x)^3,x]

[Out] (-35*a*Sqrt[x])/(4*b^4) + (35*x^(3/2))/(12*b^3) - x^(7/2)/(2*b*(a + b*x)^2) - (7*x^(5/2))/(4*b^2*(a + b*x)) + (35*a^(3/2)*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(4*b^(9/2))

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{7/2}}{(a+bx)^3} dx &= -\frac{x^{7/2}}{2b(a+bx)^2} + \frac{7 \int \frac{x^{5/2}}{(a+bx)^2} dx}{4b} \\
&= -\frac{x^{7/2}}{2b(a+bx)^2} - \frac{7x^{5/2}}{4b^2(a+bx)} + \frac{35 \int \frac{x^{3/2}}{a+bx} dx}{8b^2} \\
&= \frac{35x^{3/2}}{12b^3} - \frac{x^{7/2}}{2b(a+bx)^2} - \frac{7x^{5/2}}{4b^2(a+bx)} - \frac{(35a) \int \frac{\sqrt{x}}{a+bx} dx}{8b^3} \\
&= -\frac{35a\sqrt{x}}{4b^4} + \frac{35x^{3/2}}{12b^3} - \frac{x^{7/2}}{2b(a+bx)^2} - \frac{7x^{5/2}}{4b^2(a+bx)} + \frac{(35a^2) \int \frac{1}{\sqrt{x}(a+bx)} dx}{8b^4} \\
&= -\frac{35a\sqrt{x}}{4b^4} + \frac{35x^{3/2}}{12b^3} - \frac{x^{7/2}}{2b(a+bx)^2} - \frac{7x^{5/2}}{4b^2(a+bx)} + \frac{(35a^2) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{4b^4} \\
&= -\frac{35a\sqrt{x}}{4b^4} + \frac{35x^{3/2}}{12b^3} - \frac{x^{7/2}}{2b(a+bx)^2} - \frac{7x^{5/2}}{4b^2(a+bx)} + \frac{35a^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{9/2}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.28

$$\frac{2x^{9/2} {}_2F_1\left(3, \frac{9}{2}; \frac{11}{2}; -\frac{bx}{a}\right)}{9a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(7/2)/(a + b*x)^3, x]

[Out] $(2*x^{(9/2)}*Hypergeometric2F1[3, 9/2, 11/2, -((b*x)/a)])/(9*a^3)$

fricas [A] time = 0.48, size = 227, normalized size = 2.39

$$\left[\frac{105 (ab^2x^2 + 2a^2bx + a^3) \sqrt{-\frac{a}{b}} \log\left(\frac{bx+2b\sqrt{x}\sqrt{-\frac{a}{b}}-a}{bx+a}\right) + 2(8b^3x^3 - 56ab^2x^2 - 175a^2bx - 105a^3)\sqrt{x}}{24(b^6x^2 + 2ab^5x + a^2b^4)}, \frac{105(ab^2x^2 + 2a^2bx + a^3)\sqrt{-\frac{a}{b}}}{24(b^6x^2 + 2ab^5x + a^2b^4)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(7/2)/(b*x+a)^3,x, algorithm="fricas")`

[Out] $[1/24*(105*(a*b^2*x^2 + 2*a^2*b*x + a^3)*\sqrt{-a/b}*\log((b*x + 2*b*\sqrt{x})*\sqrt{-a/b} - a)/(b*x + a) + 2*(8*b^3*x^3 - 56*a*b^2*x^2 - 175*a^2*b*x - 105*a^3)*\sqrt{x})/(b^6*x^2 + 2*a*b^5*x + a^2*b^4), 1/12*(105*(a*b^2*x^2 + 2*a^2*b*x + a^3)*\sqrt{a/b}*\arctan(b*\sqrt{x}*\sqrt{a/b}/a) + (8*b^3*x^3 - 56*a*b^2*x^2 - 175*a^2*b*x - 105*a^3)*\sqrt{x})/(b^6*x^2 + 2*a*b^5*x + a^2*b^4)]$

giac [A] time = 1.03, size = 77, normalized size = 0.81

$$\frac{35a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}b^4} - \frac{13a^2bx^{\frac{3}{2}} + 11a^3\sqrt{x}}{4(bx+a)^2b^4} + \frac{2(b^6x^{\frac{3}{2}} - 9ab^5\sqrt{x})}{3b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(7/2)/(b*x+a)^3,x, algorithm="giac")`

[Out] $35/4*a^2*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*b^4) - 1/4*(13*a^2*b*x^{(3/2)} + 11*a^3*\sqrt{x})/((b*x + a)^2*b^4) + 2/3*(b^6*x^{(3/2)} - 9*a*b^5*\sqrt{x})/b^9$

maple [A] time = 0.02, size = 79, normalized size = 0.83

$$-\frac{13a^2x^{\frac{3}{2}}}{4(bx+a)^2b^3} - \frac{11a^3\sqrt{x}}{4(bx+a)^2b^4} + \frac{35a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}b^4} + \frac{2x^{\frac{3}{2}}}{3b^3} - \frac{6a\sqrt{x}}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(7/2)/(b*x+a)^3,x)`

[Out] $2/3*x^{(3/2)}/b^3-6*a*x^{(1/2)}/b^4-13/4/b^3*a^2/(b*x+a)^2*x^{(3/2)}-11/4/b^4*a^3/(b*x+a)^2*x^{(1/2)}+35/4/b^4*a^2/(a*b)^{(1/2)}*\arctan(1/(a*b)^{(1/2)}*b*x^{(1/2)})$

maxima [A] time = 3.07, size = 86, normalized size = 0.91

$$-\frac{13 a^2 b x^{\frac{3}{2}} + 11 a^3 \sqrt{x}}{4 (b^6 x^2 + 2 a b^5 x + a^2 b^4)} + \frac{35 a^2 \arctan\left(\frac{b \sqrt{x}}{\sqrt{a b}}\right)}{4 \sqrt{a b} b^4} + \frac{2 (b x^{\frac{3}{2}} - 9 a \sqrt{x})}{3 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(7/2)/(b*x+a)^3,x, algorithm="maxima")

[Out] -1/4*(13*a^2*b*x^(3/2) + 11*a^3*sqrt(x))/(b^6*x^2 + 2*a*b^5*x + a^2*b^4) + 35/4*a^2*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*b^4) + 2/3*(b*x^(3/2) - 9*a*sqrt(x))/b^4

mupad [B] time = 0.12, size = 81, normalized size = 0.85

$$\frac{2 x^{3/2}}{3 b^3} - \frac{\frac{11 a^3 \sqrt{x}}{4} + \frac{13 a^2 b x^{3/2}}{4}}{a^2 b^4 + 2 a b^5 x + b^6 x^2} - \frac{6 a \sqrt{x}}{b^4} + \frac{35 a^{3/2} \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{4 b^{9/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(7/2)/(a + b*x)^3,x)

[Out] (2*x^(3/2))/(3*b^3) - ((11*a^3*x^(1/2))/4 + (13*a^2*b*x^(3/2))/4)/(a^2*b^4 + b^6*x^2 + 2*a*b^5*x) - (6*a*x^(1/2))/b^4 + (35*a^(3/2)*atan((b^(1/2)*x^(1/2))/a^(1/2)))/(4*b^(9/2))

sympy [A] time = 135.24, size = 906, normalized size = 9.54

$$\left\{ \begin{array}{l} \infty x^{\frac{3}{2}} \\ \frac{2x^{\frac{9}{2}}}{9a^3} \\ \frac{2x^{\frac{3}{2}}}{3b^3} \end{array} \right\} - \frac{210ia^{\frac{7}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{24ia^{\frac{5}{2}}b^5\sqrt{\frac{1}{b}} + 48ia^{\frac{3}{2}}b^6x\sqrt{\frac{1}{b}} + 24i\sqrt{a}b^7x^2\sqrt{\frac{1}{b}}} - \frac{350ia^{\frac{5}{2}}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{24ia^{\frac{5}{2}}b^5\sqrt{\frac{1}{b}} + 48ia^{\frac{3}{2}}b^6x\sqrt{\frac{1}{b}} + 24i\sqrt{a}b^7x^2\sqrt{\frac{1}{b}}} - \frac{112ia^{\frac{3}{2}}b^3x^{\frac{5}{2}}\sqrt{\frac{1}{b}}}{24ia^{\frac{5}{2}}b^5\sqrt{\frac{1}{b}} + 48ia^{\frac{3}{2}}b^6x\sqrt{\frac{1}{b}} + 24i\sqrt{a}b^7x^2\sqrt{\frac{1}{b}}} +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(7/2)/(b*x+a)**3,x)

[Out] Piecewise((zoo*x**(3/2), Eq(a, 0) & Eq(b, 0)), (2*x**(9/2)/(9*a**3), Eq(b, 0)), (2*x**(3/2)/(3*b**3), Eq(a, 0)), (-210*I*a**(7/2)*b*sqrt(x)*sqrt(1/b)/

```

(24*I*a**(5/2)*b**5*sqrt(1/b) + 48*I*a**(3/2)*b**6*x*sqrt(1/b) + 24*I*sqrt(
a)*b**7*x**2*sqrt(1/b)) - 350*I*a**(5/2)*b**2*x**(3/2)*sqrt(1/b)/(24*I*a**(
5/2)*b**5*sqrt(1/b) + 48*I*a**(3/2)*b**6*x*sqrt(1/b) + 24*I*sqrt(a)*b**7*x*
**2*sqrt(1/b)) - 112*I*a**(3/2)*b**3*x**(5/2)*sqrt(1/b)/(24*I*a**(5/2)*b**5*
sqrt(1/b) + 48*I*a**(3/2)*b**6*x*sqrt(1/b) + 24*I*sqrt(a)*b**7*x**2*sqrt(1/
b)) + 16*I*sqrt(a)*b**4*x**(7/2)*sqrt(1/b)/(24*I*a**(5/2)*b**5*sqrt(1/b) +
48*I*a**(3/2)*b**6*x*sqrt(1/b) + 24*I*sqrt(a)*b**7*x**2*sqrt(1/b)) + 105*a
**4*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(5/2)*b**5*sqrt(1/b) + 48*I
*a**(3/2)*b**6*x*sqrt(1/b) + 24*I*sqrt(a)*b**7*x**2*sqrt(1/b)) - 105*a**4*1
og(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(5/2)*b**5*sqrt(1/b) + 48*I*a**(
3/2)*b**6*x*sqrt(1/b) + 24*I*sqrt(a)*b**7*x**2*sqrt(1/b)) + 210*a**3*b*x*lo
g(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(5/2)*b**5*sqrt(1/b) + 48*I*a**(
3/2)*b**6*x*sqrt(1/b) + 24*I*sqrt(a)*b**7*x**2*sqrt(1/b)) - 210*a**3*b*x*lo
g(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(5/2)*b**5*sqrt(1/b) + 48*I*a**(3
/2)*b**6*x*sqrt(1/b) + 24*I*sqrt(a)*b**7*x**2*sqrt(1/b)) + 105*a**2*b**2*x*
**2*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(5/2)*b**5*sqrt(1/b) + 48*I
*a**(3/2)*b**6*x*sqrt(1/b) + 24*I*sqrt(a)*b**7*x**2*sqrt(1/b)) - 105*a**2*b
**2*x**2*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(5/2)*b**5*sqrt(1/b) +
48*I*a**(3/2)*b**6*x*sqrt(1/b) + 24*I*sqrt(a)*b**7*x**2*sqrt(1/b)), True))

```

$$3.463 \quad \int \frac{x^{5/2}}{(a+bx)^3} dx$$

Optimal. Leaf size=82

$$-\frac{15\sqrt{a} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{7/2}} - \frac{5x^{3/2}}{4b^2(a+bx)} - \frac{x^{5/2}}{2b(a+bx)^2} + \frac{15\sqrt{x}}{4b^3}$$

[Out] $-1/2*x^{(5/2)}/b/(b*x+a)^2-5/4*x^{(3/2)}/b^2/(b*x+a)-15/4*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})*a^{(1/2)}/b^{(7/2)}+15/4*x^{(1/2)}/b^3$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 50, 63, 205}

$$-\frac{5x^{3/2}}{4b^2(a+bx)} - \frac{15\sqrt{a} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{7/2}} - \frac{x^{5/2}}{2b(a+bx)^2} + \frac{15\sqrt{x}}{4b^3}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)/(a + b*x)^3, x]

[Out] $(15*\text{Sqrt}[x])/(4*b^3) - x^{(5/2)}/(2*b*(a + b*x)^2) - (5*x^{(3/2)})/(4*b^2*(a + b*x)) - (15*\text{Sqrt}[a]*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a]])/(4*b^{(7/2)})$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(a+bx)^3} dx &= -\frac{x^{5/2}}{2b(a+bx)^2} + \frac{5 \int \frac{x^{3/2}}{(a+bx)^2} dx}{4b} \\
&= -\frac{x^{5/2}}{2b(a+bx)^2} - \frac{5x^{3/2}}{4b^2(a+bx)} + \frac{15 \int \frac{\sqrt{x}}{a+bx} dx}{8b^2} \\
&= \frac{15\sqrt{x}}{4b^3} - \frac{x^{5/2}}{2b(a+bx)^2} - \frac{5x^{3/2}}{4b^2(a+bx)} - \frac{(15a) \int \frac{1}{\sqrt{x}(a+bx)} dx}{8b^3} \\
&= \frac{15\sqrt{x}}{4b^3} - \frac{x^{5/2}}{2b(a+bx)^2} - \frac{5x^{3/2}}{4b^2(a+bx)} - \frac{(15a) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{4b^3} \\
&= \frac{15\sqrt{x}}{4b^3} - \frac{x^{5/2}}{2b(a+bx)^2} - \frac{5x^{3/2}}{4b^2(a+bx)} - \frac{15\sqrt{a} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.33

$$\frac{2x^{7/2} {}_2F_1\left(3, \frac{7}{2}; \frac{9}{2}; -\frac{bx}{a}\right)}{7a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/(a + b*x)^3,x]

[Out] (2*x^(7/2)*Hypergeometric2F1[3, 7/2, 9/2, -((b*x)/a)])/(7*a^3)

fricas [A] time = 0.46, size = 200, normalized size = 2.44

$$\left[\frac{15 (b^2 x^2 + 2 abx + a^2) \sqrt{-\frac{a}{b}} \log\left(\frac{bx - 2b\sqrt{x} \sqrt{-\frac{a}{b}} - a}{bx + a}\right) + 2 (8b^2 x^2 + 25 abx + 15 a^2) \sqrt{x}}{8 (b^5 x^2 + 2 ab^4 x + a^2 b^3)}, -\frac{15 (b^2 x^2 + 2 abx + a^2) \sqrt{\frac{a}{b}}}{4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^3,x, algorithm="fricas")

[Out] [1/8*(15*(b^2*x^2 + 2*a*b*x + a^2)*sqrt(-a/b)*log((b*x - 2*b*sqrt(x)*sqrt(-a/b) - a)/(b*x + a)) + 2*(8*b^2*x^2 + 25*a*b*x + 15*a^2)*sqrt(x))/(b^5*x^2 + 2*a*b^4*x + a^2*b^3), -1/4*(15*(b^2*x^2 + 2*a*b*x + a^2)*sqrt(a/b)*arctan(b*sqrt(x)*sqrt(a/b)/a) - (8*b^2*x^2 + 25*a*b*x + 15*a^2)*sqrt(x))/(b^5*x^2 + 2*a*b^4*x + a^2*b^3)]

giac [A] time = 0.95, size = 59, normalized size = 0.72

$$-\frac{15 a \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4 \sqrt{ab} b^3} + \frac{2 \sqrt{x}}{b^3} + \frac{9 abx^{\frac{3}{2}} + 7 a^2 \sqrt{x}}{4 (bx + a)^2 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^3,x, algorithm="giac")

[Out] -15/4*a*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*b^3) + 2*sqrt(x)/b^3 + 1/4*(9*a*b*x^(3/2) + 7*a^2*sqrt(x))/((b*x + a)^2*b^3)

maple [A] time = 0.02, size = 66, normalized size = 0.80

$$\frac{9 a x^{\frac{3}{2}}}{4 (bx + a)^2 b^2} + \frac{7 a^2 \sqrt{x}}{4 (bx + a)^2 b^3} - \frac{15 a \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4 \sqrt{ab} b^3} + \frac{2 \sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x+a)^3,x)

[Out] 2*x^(1/2)/b^3+9/4/b^2*a/(b*x+a)^2*x^(3/2)+7/4/b^3*a^2/(b*x+a)^2*x^(1/2)-15/4/b^3*a/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.94, size = 73, normalized size = 0.89

$$\frac{9 abx^{\frac{3}{2}} + 7 a^2 \sqrt{x}}{4 (b^5 x^2 + 2 ab^4 x + a^2 b^3)} - \frac{15 a \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4 \sqrt{ab} b^3} + \frac{2 \sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^3,x, algorithm="maxima")

[Out] $\frac{1}{4}*(9*a*b*x^{(3/2)} + 7*a^2*\sqrt{x})/(b^5*x^2 + 2*a*b^4*x + a^2*b^3) - \frac{15}{4}*a*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*b^3) + 2*\sqrt{x}/b^3$

mupad [B] time = 0.14, size = 69, normalized size = 0.84

$$\frac{\frac{7a^2\sqrt{x}}{4} + \frac{9abx^{3/2}}{4}}{a^2b^3 + 2ab^4x + b^5x^2} + \frac{2\sqrt{x}}{b^3} - \frac{15\sqrt{a}\operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(a + b*x)^3,x)

[Out] $((7*a^2*x^{(1/2)})/4 + (9*a*b*x^{(3/2)})/4)/(a^2*b^3 + b^5*x^2 + 2*a*b^4*x) + (2*x^{(1/2)})/b^3 - (15*a^{(1/2)}*\operatorname{atan}((b^{(1/2)}*x^{(1/2)})/a^{(1/2)}))/(4*b^{(7/2)})$

sympy [A] time = 53.29, size = 816, normalized size = 9.95

$$\left\{ \begin{array}{l} \infty\sqrt{x} \\ \frac{7}{2x^2} \\ \frac{7}{7a^3} \\ \frac{2\sqrt{x}}{b^3} \end{array} \right. \left\{ \begin{array}{l} \frac{30ia^{\frac{5}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{8ia^{\frac{5}{2}}b^4\sqrt{\frac{1}{b}} + 16ia^{\frac{3}{2}}b^5x\sqrt{\frac{1}{b}} + 8i\sqrt{a}b^6x^2\sqrt{\frac{1}{b}}} + \frac{50ia^{\frac{3}{2}}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{8ia^{\frac{5}{2}}b^4\sqrt{\frac{1}{b}} + 16ia^{\frac{3}{2}}b^5x\sqrt{\frac{1}{b}} + 8i\sqrt{a}b^6x^2\sqrt{\frac{1}{b}}} + \frac{16i\sqrt{a}b^3x^{\frac{5}{2}}\sqrt{\frac{1}{b}}}{8ia^{\frac{5}{2}}b^4\sqrt{\frac{1}{b}} + 16ia^{\frac{3}{2}}b^5x\sqrt{\frac{1}{b}} + 8i\sqrt{a}b^6x^2\sqrt{\frac{1}{b}}} - \frac{5}{8ia^{\frac{5}{2}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(b*x+a)**3,x)

[Out] Piecewise((zoo*sqrt(x), Eq(a, 0) & Eq(b, 0)), (2*x**(7/2)/(7*a**3), Eq(b, 0)), (2*sqrt(x)/b**3, Eq(a, 0)), (30*I*a**(5/2)*b*sqrt(x)*sqrt(1/b)/(8*I*a**(5/2)*b**4*sqrt(1/b) + 16*I*a**(3/2)*b**5*x*sqrt(1/b) + 8*I*sqrt(a)*b**6*x**2*sqrt(1/b)) + 50*I*a**(3/2)*b**2*x**(3/2)*sqrt(1/b)/(8*I*a**(5/2)*b**4*sqrt(1/b) + 16*I*a**(3/2)*b**5*x*sqrt(1/b) + 8*I*sqrt(a)*b**6*x**2*sqrt(1/b)) + 16*I*sqrt(a)*b**3*x**(5/2)*sqrt(1/b)/(8*I*a**(5/2)*b**4*sqrt(1/b) + 16*I*a**(3/2)*b**5*x*sqrt(1/b) + 8*I*sqrt(a)*b**6*x**2*sqrt(1/b)) - 15*a**3*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(5/2)*b**4*sqrt(1/b) + 16*I*a**(3/2)*b**5*x*sqrt(1/b) + 8*I*sqrt(a)*b**6*x**2*sqrt(1/b)) + 15*a**3*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(5/2)*b**4*sqrt(1/b) + 16*I*a**(3/2)*b**5*x*sqrt(1/b) + 8*I*sqrt(a)*b**6*x**2*sqrt(1/b))

```

x*sqrt(1/b) + 8*I*sqrt(a)*b**6*x**2*sqrt(1/b)) - 30*a**2*b*x*log(-I*sqrt(a)
*sqrt(1/b) + sqrt(x))/(8*I*a**(5/2)*b**4*sqrt(1/b) + 16*I*a**(3/2)*b**5*x*s
qrt(1/b) + 8*I*sqrt(a)*b**6*x**2*sqrt(1/b)) + 30*a**2*b*x*log(I*sqrt(a)*sqr
t(1/b) + sqrt(x))/(8*I*a**(5/2)*b**4*sqrt(1/b) + 16*I*a**(3/2)*b**5*x*sqrt(
1/b) + 8*I*sqrt(a)*b**6*x**2*sqrt(1/b)) - 15*a*b**2*x**2*log(-I*sqrt(a)*sqr
t(1/b) + sqrt(x))/(8*I*a**(5/2)*b**4*sqrt(1/b) + 16*I*a**(3/2)*b**5*x*sqrt(
1/b) + 8*I*sqrt(a)*b**6*x**2*sqrt(1/b)) + 15*a*b**2*x**2*log(I*sqrt(a)*sqrt
(1/b) + sqrt(x))/(8*I*a**(5/2)*b**4*sqrt(1/b) + 16*I*a**(3/2)*b**5*x*sqrt(1
/b) + 8*I*sqrt(a)*b**6*x**2*sqrt(1/b)), True))

```


$$3.464 \quad \int \frac{x^{3/2}}{(a+bx)^3} dx$$

Optimal. Leaf size=70

$$\frac{3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{a}b^{5/2}} - \frac{3\sqrt{x}}{4b^2(a+bx)} - \frac{x^{3/2}}{2b(a+bx)^2}$$

[Out] $-1/2*x^{(3/2)}/b/(b*x+a)^2+3/4*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/b^{(5/2)}/a^{(1/2)}$
 $-3/4*x^{(1/2)}/b^2/(b*x+a)$

Rubi [A] time = 0.02, antiderivative size = 70, normalized size of antiderivative = 1.00,
 number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} =$
 0.231, Rules used = {47, 63, 205}

$$-\frac{3\sqrt{x}}{4b^2(a+bx)} + \frac{3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{a}b^{5/2}} - \frac{x^{3/2}}{2b(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)/(a + b*x)^3,x]

[Out] $-x^{(3/2)}/(2*b*(a + b*x)^2) - (3*\text{Sqrt}[x])/(4*b^2*(a + b*x)) + (3*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a]])/(4*\text{Sqrt}[a]*b^{(5/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 ((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
 nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
 NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
 rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
 & IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
 {p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
 (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
 [b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
 ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{x^{3/2}}{(a+bx)^3} dx &= -\frac{x^{3/2}}{2b(a+bx)^2} + \frac{3 \int \frac{\sqrt{x}}{(a+bx)^2} dx}{4b} \\
 &= -\frac{x^{3/2}}{2b(a+bx)^2} - \frac{3\sqrt{x}}{4b^2(a+bx)} + \frac{3 \int \frac{1}{\sqrt{x}(a+bx)} dx}{8b^2} \\
 &= -\frac{x^{3/2}}{2b(a+bx)^2} - \frac{3\sqrt{x}}{4b^2(a+bx)} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{4b^2} \\
 &= -\frac{x^{3/2}}{2b(a+bx)^2} - \frac{3\sqrt{x}}{4b^2(a+bx)} + \frac{3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{a}b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.03, size = 59, normalized size = 0.84

$$\frac{3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{a}b^{5/2}} - \frac{\sqrt{x}(3a+5bx)}{4b^2(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/(a + b*x)^3, x]

[Out] -1/4*(Sqrt[x]*(3*a + 5*b*x))/(b^2*(a + b*x)^2) + (3*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(4*Sqrt[a]*b^(5/2))

fricas [A] time = 0.45, size = 185, normalized size = 2.64

$$\left[\frac{3(b^2x^2 + 2abx + a^2)\sqrt{-ab} \log\left(\frac{bx-a-2\sqrt{-ab}\sqrt{x}}{bx+a}\right) + 2(5ab^2x + 3a^2b)\sqrt{x}}{8(ab^5x^2 + 2a^2b^4x + a^3b^3)}, -\frac{3(b^2x^2 + 2abx + a^2)\sqrt{ab} \arctan\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4(ab^5x^2 + 2a^2b^4x + a^3b^3)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^3, x, algorithm="fricas")

[Out] [-1/8*(3*(b^2*x^2 + 2*a*b*x + a^2)*sqrt(-a*b)*log((b*x - a - 2*sqrt(-a*b)*sqrt(x))/(b*x + a)) + 2*(5*a*b^2*x + 3*a^2*b)*sqrt(x))/(a*b^5*x^2 + 2*a^2*b^4x + a^3*b^3) + 3*atan(sqrt(b)*sqrt(x)/sqrt(a))/(4*sqrt(a)*b^(5/2))]

$4*x + a^3*b^3$), $-1/4*(3*(b^2*x^2 + 2*a*b*x + a^2)*\sqrt{a*b}*\arctan(\sqrt{a*b}/(b*\sqrt{x}))) + (5*a*b^2*x + 3*a^2*b)*\sqrt{x}/(a*b^5*x^2 + 2*a^2*b^4*x + a^3*b^3)]$

giac [A] time = 0.91, size = 47, normalized size = 0.67

$$\frac{3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4 \sqrt{ab} b^2} - \frac{5 b x^{\frac{3}{2}} + 3 a \sqrt{x}}{4 (b x + a)^2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^3,x, algorithm="giac")

[Out] $3/4*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*b^2) - 1/4*(5*b*x^{(3/2)} + 3*a*\sqrt{x})/((b*x + a)^2*b^2)$

maple [A] time = 0.01, size = 50, normalized size = 0.71

$$\frac{3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab} b^2} + \frac{-\frac{5x^{\frac{3}{2}}}{4b} - \frac{3a\sqrt{x}}{4b^2}}{(bx + a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(b*x+a)^3,x)

[Out] $2*(-5/8/b*x^{(3/2)}-3/8*a/b^2*x^{(1/2)})/(b*x+a)^2+3/4/b^2/(a*b)^{(1/2)*\arctan(1/(a*b)^{(1/2)*b*x^{(1/2)})}$

maxima [A] time = 2.96, size = 61, normalized size = 0.87

$$-\frac{5 b x^{\frac{3}{2}} + 3 a \sqrt{x}}{4 (b^4 x^2 + 2 a b^3 x + a^2 b^2)} + \frac{3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4 \sqrt{ab} b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^3,x, algorithm="maxima")

[Out] $-1/4*(5*b*x^{(3/2)} + 3*a*\sqrt{x})/(b^4*x^2 + 2*a*b^3*x + a^2*b^2) + 3/4*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b}*b^2)$

mupad [B] time = 0.13, size = 58, normalized size = 0.83

$$\frac{3 \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{4 \sqrt{a} b^{5/2}} - \frac{\frac{5 x^{3/2}}{4 b} + \frac{3 a \sqrt{x}}{4 b^2}}{a^2 + 2 a b x + b^2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(a + b*x)^3,x)`

[Out] $(3*\operatorname{atan}((b^{1/2}*x^{1/2})/a^{1/2}))/((4*a^{1/2}*b^{5/2}) - ((5*x^{3/2}))/((4*b) + (3*a*x^{1/2}))/((4*b^2)))/(a^2 + b^2*x^2 + 2*a*b*x)$

sympy [A] time = 29.37, size = 726, normalized size = 10.37

$$\left\{ \begin{array}{l} \frac{\infty}{\sqrt{x}} \\ \frac{2x^{\frac{5}{2}}}{5a^3} \\ \frac{2}{b^3\sqrt{x}} \end{array} \right. - \frac{6ia^{\frac{3}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{8ia^{\frac{5}{2}}b^3\sqrt{\frac{1}{b}}+16ia^{\frac{3}{2}}b^4x\sqrt{\frac{1}{b}}+8i\sqrt{a}b^5x^2\sqrt{\frac{1}{b}}} - \frac{10i\sqrt{a}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{8ia^{\frac{5}{2}}b^3\sqrt{\frac{1}{b}}+16ia^{\frac{3}{2}}b^4x\sqrt{\frac{1}{b}}+8i\sqrt{a}b^5x^2\sqrt{\frac{1}{b}}} + \frac{3a^2\log\left(-i\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{8ia^{\frac{5}{2}}b^3\sqrt{\frac{1}{b}}+16ia^{\frac{3}{2}}b^4x\sqrt{\frac{1}{b}}+8i\sqrt{a}b^5x^2\sqrt{\frac{1}{b}}} - \frac{5}{8ia^{\frac{5}{2}}b^3\sqrt{\frac{1}{b}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(b*x+a)**3,x)`

[Out] `Piecewise((zoo/sqrt(x), Eq(a, 0) & Eq(b, 0)), (2*x**(5/2)/(5*a**3), Eq(b, 0)), (-2/(b**3*sqrt(x)), Eq(a, 0)), (-6*I*a**(3/2)*b*sqrt(x)*sqrt(1/b)/(8*I*a**(5/2)*b**3*sqrt(1/b) + 16*I*a**(3/2)*b**4*x*sqrt(1/b) + 8*I*sqrt(a)*b**5*x**2*sqrt(1/b)) - 10*I*sqrt(a)*b**2*x**(3/2)*sqrt(1/b)/(8*I*a**(5/2)*b**3*sqrt(1/b) + 16*I*a**(3/2)*b**4*x*sqrt(1/b) + 8*I*sqrt(a)*b**5*x**2*sqrt(1/b)) + 3*a**2*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(5/2)*b**3*sqrt(1/b) + 16*I*a**(3/2)*b**4*x*sqrt(1/b) + 8*I*sqrt(a)*b**5*x**2*sqrt(1/b)) - 3*a**2*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(5/2)*b**3*sqrt(1/b) + 16*I*a**(3/2)*b**4*x*sqrt(1/b) + 8*I*sqrt(a)*b**5*x**2*sqrt(1/b)) + 6*a*b*x*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(5/2)*b**3*sqrt(1/b) + 16*I*a**(3/2)*b**4*x*sqrt(1/b) + 8*I*sqrt(a)*b**5*x**2*sqrt(1/b)) - 6*a*b*x*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(5/2)*b**3*sqrt(1/b) + 16*I*a**(3/2)*b**4*x*sqrt(1/b) + 8*I*sqrt(a)*b**5*x**2*sqrt(1/b)) + 3*b**2*x**2*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(5/2)*b**3*sqrt(1/b) + 16*I*a**(3/2)*b**4*x*sqrt(1/b) + 8*I*sqrt(a)*b**5*x**2*sqrt(1/b)) - 3*b**2*x**2*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(5/2)*b**3*sqrt(1/b) + 16*I*a**(3/2)*b**4*x*sqrt(1/b) + 8*I*sqrt(a)*b**5*x**2*sqrt(1/b)), True))`

$$3.465 \quad \int \frac{\sqrt{x}}{(a+bx)^3} dx$$

Optimal. Leaf size=73

$$\frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{3/2}b^{3/2}} + \frac{\sqrt{x}}{4ab(a+bx)} - \frac{\sqrt{x}}{2b(a+bx)^2}$$

[Out] 1/4*arctan(b^(1/2)*x^(1/2)/a^(1/2))/a^(3/2)/b^(3/2)-1/2*x^(1/2)/b/(b*x+a)^2+1/4*x^(1/2)/a/b/(b*x+a)

Rubi [A] time = 0.02, antiderivative size = 73, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 51, 63, 205}

$$\frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{3/2}b^{3/2}} + \frac{\sqrt{x}}{4ab(a+bx)} - \frac{\sqrt{x}}{2b(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(a + b*x)^3,x]

[Out] -Sqrt[x]/(2*b*(a + b*x)^2) + Sqrt[x]/(4*a*b*(a + b*x)) + ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]]/(4*a^(3/2)*b^(3/2))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a
/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{x}}{(a+bx)^3} dx &= -\frac{\sqrt{x}}{2b(a+bx)^2} + \frac{\int \frac{1}{\sqrt{x}(a+bx)^2} dx}{4b} \\ &= -\frac{\sqrt{x}}{2b(a+bx)^2} + \frac{\sqrt{x}}{4ab(a+bx)} + \frac{\int \frac{1}{\sqrt{x}(a+bx)} dx}{8ab} \\ &= -\frac{\sqrt{x}}{2b(a+bx)^2} + \frac{\sqrt{x}}{4ab(a+bx)} + \frac{\text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{4ab} \\ &= -\frac{\sqrt{x}}{2b(a+bx)^2} + \frac{\sqrt{x}}{4ab(a+bx)} + \frac{\tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{3/2}b^{3/2}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 27, normalized size = 0.37

$$\frac{2x^{3/2} {}_2F_1\left(\frac{3}{2}, 3; \frac{5}{2}; -\frac{bx}{a}\right)}{3a^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[x]/(a + b*x)^3, x]
```

```
[Out] (2*x^(3/2)*Hypergeometric2F1[3/2, 3, 5/2, -(b*x)/a])/(3*a^3)
```

fricas [A] time = 0.44, size = 186, normalized size = 2.55

$$\left[\frac{(b^2x^2 + 2abx + a^2)\sqrt{-ab} \log\left(\frac{bx-a-2\sqrt{-ab}\sqrt{x}}{bx+a}\right) - 2(ab^2x - a^2b)\sqrt{x}}{8(a^2b^4x^2 + 2a^3b^3x + a^4b^2)}, \frac{(b^2x^2 + 2abx + a^2)\sqrt{ab} \arctan\left(\frac{\sqrt{ab}}{b\sqrt{x}}\right) -}{4(a^2b^4x^2 + 2a^3b^3x + a^4b^2)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^3,x, algorithm="fricas")

[Out] [-1/8*((b^2*x^2 + 2*a*b*x + a^2)*sqrt(-a*b)*log((b*x - a - 2*sqrt(-a*b))*sqrt(x))/(b*x + a)) - 2*(a*b^2*x - a^2*b)*sqrt(x)/(a^2*b^4*x^2 + 2*a^3*b^3*x + a^4*b^2), -1/4*((b^2*x^2 + 2*a*b*x + a^2)*sqrt(a*b)*arctan(sqrt(a*b)/(b*sqrt(x))) - (a*b^2*x - a^2*b)*sqrt(x))/(a^2*b^4*x^2 + 2*a^3*b^3*x + a^4*b^2)]

giac [A] time = 1.07, size = 52, normalized size = 0.71

$$\frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}ab} + \frac{bx^{\frac{3}{2}} - a\sqrt{x}}{4(bx+a)^2ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^3,x, algorithm="giac")

[Out] 1/4*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a*b) + 1/4*(b*x^(3/2) - a*sqrt(x))/((b*x + a)^2*a*b)

maple [A] time = 0.01, size = 52, normalized size = 0.71

$$\frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}ab} + \frac{\frac{x^{\frac{3}{2}}}{4a} - \frac{\sqrt{x}}{4b}}{(bx+a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x+a)^3,x)

[Out] 2*(1/8/a*x^(3/2)-1/8/b*x^(1/2))/(b*x+a)^2+1/4/b/a/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 3.01, size = 64, normalized size = 0.88

$$\frac{bx^{\frac{3}{2}} - a\sqrt{x}}{4(ab^3x^2 + 2a^2b^2x + a^3b)} + \frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^3,x, algorithm="maxima")

[Out] 1/4*(b*x^(3/2) - a*sqrt(x))/(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b) + 1/4*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a*b)

mupad [B] time = 0.13, size = 56, normalized size = 0.77

$$\frac{\frac{x^{3/2}}{4a} - \frac{\sqrt{x}}{4b}}{a^2 + 2abx + b^2x^2} + \frac{\operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{3/2}b^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)/(a + b*x)^3,x)`

[Out] $(x^{3/2}/(4*a) - x^{1/2}/(4*b))/(a^2 + b^2*x^2 + 2*a*b*x) + \operatorname{atan}((b^{1/2}) * x^{1/2})/a^{3/2} * b^{3/2}$

sympy [A] time = 15.27, size = 721, normalized size = 9.88

$$\left\{ \begin{array}{l} \frac{\infty}{3} \\ x^2 \\ \frac{3}{2x^2} \\ \frac{3}{3a^3} \\ -\frac{2}{3b^3x^2} \\ -\frac{2ia^{\frac{3}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{8ia^{\frac{7}{2}}b^2\sqrt{\frac{1}{b}} + 16ia^{\frac{5}{2}}b^3x\sqrt{\frac{1}{b}} + 8ia^{\frac{3}{2}}b^4x^2\sqrt{\frac{1}{b}}} + \frac{2i\sqrt{a}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{8ia^{\frac{7}{2}}b^2\sqrt{\frac{1}{b}} + 16ia^{\frac{5}{2}}b^3x\sqrt{\frac{1}{b}} + 8ia^{\frac{3}{2}}b^4x^2\sqrt{\frac{1}{b}}} + \frac{a^2 \log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{8ia^{\frac{7}{2}}b^2\sqrt{\frac{1}{b}} + 16ia^{\frac{5}{2}}b^3x\sqrt{\frac{1}{b}} + 8ia^{\frac{3}{2}}b^4x^2\sqrt{\frac{1}{b}}} - \frac{7}{8ia^{\frac{7}{2}}b^2} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)/(b*x+a)**3,x)`

[Out] `Piecewise((zoo/x**(3/2), Eq(a, 0) & Eq(b, 0)), (2*x**(3/2)/(3*a**3), Eq(b, 0)), (-2/(3*b**3*x**(3/2)), Eq(a, 0)), (-2*I*a**(3/2)*b*sqrt(x)*sqrt(1/b)/(8*I*a**(7/2)*b**2*sqrt(1/b) + 16*I*a**(5/2)*b**3*x*sqrt(1/b) + 8*I*a**(3/2)*b**4*x**2*sqrt(1/b)) + 2*I*sqrt(a)*b**2*x**(3/2)*sqrt(1/b)/(8*I*a**(7/2)*b**2*sqrt(1/b) + 16*I*a**(5/2)*b**3*x*sqrt(1/b) + 8*I*a**(3/2)*b**4*x**2*sqrt(1/b)) + a**2*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(7/2)*b**2*sqrt(1/b) + 16*I*a**(5/2)*b**3*x*sqrt(1/b) + 8*I*a**(3/2)*b**4*x**2*sqrt(1/b)) - a**2*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(7/2)*b**2*sqrt(1/b) + 16*I*a**(5/2)*b**3*x*sqrt(1/b) + 8*I*a**(3/2)*b**4*x**2*sqrt(1/b)) + 2*a*b*x*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(7/2)*b**2*sqrt(1/b) + 16*I*a**(5/2)*b**3*x*sqrt(1/b) + 8*I*a**(3/2)*b**4*x**2*sqrt(1/b)) - 2*a*b*x*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(7/2)*b**2*sqrt(1/b) + 16*I*a**(5/2)*b**3*x*sqrt(1/b) + 8*I*a**(3/2)*b**4*x**2*sqrt(1/b)) + b**2*x**2*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(7/2)*b**2*sqrt(1/b) + 16*I*a**(5/2)*b**3*x*sqrt(1/b) + 8*I*a**(3/2)*b**4*x**2*sqrt(1/b)) - b**2*x**2*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(7/2)*b**2*sqrt(1/b) + 16*I*a**(5/2)*b**3*x*sqrt(1/b) + 8*I*a**(3/2)*b**4*x**2*sqrt(1/b))`


```
rt(1/b) + sqrt(x))/(8*I*a**(7/2)*b**2*sqrt(1/b) + 16*I*a**(5/2)*b**3*x*sqrt  
(1/b) + 8*I*a**(3/2)*b**4*x**2*sqrt(1/b)), True))
```

$$3.466 \quad \int \frac{1}{\sqrt{x}(a+bx)^3} dx$$

Optimal. Leaf size=70

$$\frac{3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{5/2}\sqrt{b}} + \frac{3\sqrt{x}}{4a^2(a+bx)} + \frac{\sqrt{x}}{2a(a+bx)^2}$$

[Out] $3/4*\arctan(b^{(1/2)*x^{(1/2)}/a^{(1/2)})/a^{(5/2)}/b^{(1/2)}+1/2*x^{(1/2)}/a/(b*x+a)^2$
 $+3/4*x^{(1/2)}/a^2/(b*x+a)$

Rubi [A] time = 0.02, antiderivative size = 70, normalized size of antiderivative = 1.00,
 number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} =$
 0.231, Rules used = {51, 63, 205}

$$\frac{3\sqrt{x}}{4a^2(a+bx)} + \frac{3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{5/2}\sqrt{b}} + \frac{\sqrt{x}}{2a(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(a + b*x)^3), x]

[Out] Sqrt[x]/(2*a*(a + b*x)^2) + (3*Sqrt[x])/(4*a^2*(a + b*x)) + (3*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(4*a^(5/2)*Sqrt[b])

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

`Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{1}{\sqrt{x}(a+bx)^3} dx &= \frac{\sqrt{x}}{2a(a+bx)^2} + \frac{3 \int \frac{1}{\sqrt{x}(a+bx)^2} dx}{4a} \\
 &= \frac{\sqrt{x}}{2a(a+bx)^2} + \frac{3\sqrt{x}}{4a^2(a+bx)} + \frac{3 \int \frac{1}{\sqrt{x}(a+bx)} dx}{8a^2} \\
 &= \frac{\sqrt{x}}{2a(a+bx)^2} + \frac{3\sqrt{x}}{4a^2(a+bx)} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{4a^2} \\
 &= \frac{\sqrt{x}}{2a(a+bx)^2} + \frac{3\sqrt{x}}{4a^2(a+bx)} + \frac{3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{5/2}\sqrt{b}}
 \end{aligned}$$

Mathematica [C] time = 0.00, size = 25, normalized size = 0.36

$$\frac{2\sqrt{x} {}_2F_1\left(\frac{1}{2}, 3; \frac{3}{2}; -\frac{bx}{a}\right)}{a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(a + b*x)^3), x]

[Out] (2*Sqrt[x]*Hypergeometric2F1[1/2, 3, 3/2, -(b*x)/a])/a^3

fricas [A] time = 0.46, size = 186, normalized size = 2.66

$$\left[\frac{3(b^2x^2 + 2abx + a^2)\sqrt{-ab} \log\left(\frac{bx-a-2\sqrt{-ab}\sqrt{x}}{bx+a}\right) - 2(3ab^2x + 5a^2b)\sqrt{x}}{8(a^3b^3x^2 + 2a^4b^2x + a^5b)}, \frac{3(b^2x^2 + 2abx + a^2)\sqrt{ab} \arctan\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4(a^3b^3x^2 + 2a^4b^2x + a^5b)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/x^(1/2), x, algorithm="fricas")

[Out] [-1/8*(3*(b^2*x^2 + 2*a*b*x + a^2)*sqrt(-a*b)*log((b*x - a - 2*sqrt(-a*b)*sqrt(x))/(b*x + a)) - 2*(3*a*b^2*x + 5*a^2*b)*sqrt(x))/(a^3*b^3*x^2 + 2*a^4*b^2*x + a^5*b), -1/4*(3*(b^2*x^2 + 2*a*b*x + a^2)*sqrt(a*b)*arctan(sqrt(a*b)

)/(b*sqrt(x))) - (3*a*b^2*x + 5*a^2*b)*sqrt(x))/(a^3*b^3*x^2 + 2*a^4*b^2*x + a^5*b)]

giac [A] time = 0.86, size = 47, normalized size = 0.67

$$\frac{3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}a^2} + \frac{3bx^{\frac{3}{2}} + 5a\sqrt{x}}{4(bx+a)^2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/x^(1/2),x, algorithm="giac")

[Out] 3/4*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a^2) + 1/4*(3*b*x^(3/2) + 5*a*sqrt(x))/((b*x + a)^2*a^2)

maple [A] time = 0.01, size = 53, normalized size = 0.76

$$\frac{\sqrt{x}}{2(bx+a)^2a} + \frac{3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}a^2} + \frac{3\sqrt{x}}{4(bx+a)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^3/x^(1/2),x)

[Out] 1/2*x^(1/2)/a/(b*x+a)^2+3/4*x^(1/2)/a^2/(b*x+a)+3/4/a^2/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.96, size = 60, normalized size = 0.86

$$\frac{3bx^{\frac{3}{2}} + 5a\sqrt{x}}{4(a^2b^2x^2 + 2a^3bx + a^4)} + \frac{3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/x^(1/2),x, algorithm="maxima")

[Out] 1/4*(3*b*x^(3/2) + 5*a*sqrt(x))/(a^2*b^2*x^2 + 2*a^3*b*x + a^4) + 3/4*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a^2)

mupad [B] time = 0.13, size = 57, normalized size = 0.81

$$\frac{\frac{5\sqrt{x}}{4a} + \frac{3bx^{3/2}}{4a^2}}{a^2 + 2abx + b^2x^2} + \frac{3 \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{5/2}\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(a + b*x)^3), x)`

[Out] $((5*x^{(1/2)})/(4*a) + (3*b*x^{(3/2)})/(4*a^2))/(a^2 + b^2*x^2 + 2*a*b*x) + (3*atan((b^{(1/2)}*x^{(1/2)})/a^{(1/2)}))/(4*a^{(5/2)}*b^{(1/2)})$

sympy [A] time = 25.69, size = 712, normalized size = 10.17

$$\left(\begin{array}{l} \frac{\infty}{5} \\ x^2 \\ -\frac{2}{5b^3x^2} \\ \frac{2\sqrt{x}}{a^3} \end{array} \right) + \frac{10ia^{\frac{3}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{8ia^{\frac{9}{2}}b\sqrt{\frac{1}{b}} + 16ia^{\frac{7}{2}}b^2x\sqrt{\frac{1}{b}} + 8ia^{\frac{5}{2}}b^3x^2\sqrt{\frac{1}{b}}} + \frac{6i\sqrt{a}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{8ia^{\frac{9}{2}}b\sqrt{\frac{1}{b}} + 16ia^{\frac{7}{2}}b^2x\sqrt{\frac{1}{b}} + 8ia^{\frac{5}{2}}b^3x^2\sqrt{\frac{1}{b}}} + \frac{3a^2 \log\left(-i\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{8ia^{\frac{9}{2}}b\sqrt{\frac{1}{b}} + 16ia^{\frac{7}{2}}b^2x\sqrt{\frac{1}{b}} + 8ia^{\frac{5}{2}}b^3x^2\sqrt{\frac{1}{b}}} - \frac{3}{8ia^{\frac{9}{2}}b\sqrt{\frac{1}{b}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**3/x**(1/2), x)`

[Out] `Piecewise((zoo/x**(5/2), Eq(a, 0) & Eq(b, 0)), (-2/(5*b**3*x**(5/2)), Eq(a, 0)), (2*sqrt(x)/a**3, Eq(b, 0)), (10*I*a**(3/2)*b*sqrt(x)*sqrt(1/b)/(8*I*a**(9/2)*b*sqrt(1/b) + 16*I*a**(7/2)*b**2*x*sqrt(1/b) + 8*I*a**(5/2)*b**3*x**2*sqrt(1/b) + 6*I*sqrt(a)*b**2*x**(3/2)*sqrt(1/b)/(8*I*a**(9/2)*b*sqrt(1/b) + 16*I*a**(7/2)*b**2*x*sqrt(1/b) + 8*I*a**(5/2)*b**3*x**2*sqrt(1/b)) + 3*a**2*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(9/2)*b*sqrt(1/b) + 16*I*a**(7/2)*b**2*x*sqrt(1/b) + 8*I*a**(5/2)*b**3*x**2*sqrt(1/b)) - 3*a**2*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(9/2)*b*sqrt(1/b) + 16*I*a**(7/2)*b**2*x*sqrt(1/b) + 8*I*a**(5/2)*b**3*x**2*sqrt(1/b)) + 6*a*b*x*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(9/2)*b*sqrt(1/b) + 16*I*a**(7/2)*b**2*x*sqrt(1/b) + 8*I*a**(5/2)*b**3*x**2*sqrt(1/b)) - 6*a*b*x*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(9/2)*b*sqrt(1/b) + 16*I*a**(7/2)*b**2*x*sqrt(1/b) + 8*I*a**(5/2)*b**3*x**2*sqrt(1/b)) + 3*b**2*x**2*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(9/2)*b*sqrt(1/b) + 16*I*a**(7/2)*b**2*x*sqrt(1/b) + 8*I*a**(5/2)*b**3*x**2*sqrt(1/b)) - 3*b**2*x**2*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(9/2)*b*sqrt(1/b) + 16*I*a**(7/2)*b**2*x*sqrt(1/b) + 8*I*a**(5/2)*b**3*x**2*sqrt(1/b)), True))`

$$3.467 \quad \int \frac{1}{x^{3/2}(a+bx)^3} dx$$

Optimal. Leaf size=82

$$-\frac{15\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{7/2}} - \frac{15}{4a^3\sqrt{x}} + \frac{5}{4a^2\sqrt{x}(a+bx)} + \frac{1}{2a\sqrt{x}(a+bx)^2}$$

[Out] $-15/4*\arctan(b^{(1/2)*x^{(1/2)}/a^{(1/2)})*b^{(1/2)}/a^{(7/2)}-15/4/a^3/x^{(1/2)}+1/2/a/(b*x+a)^2/x^{(1/2)}+5/4/a^2/(b*x+a)/x^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 205}

$$\frac{5}{4a^2\sqrt{x}(a+bx)} - \frac{15\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{7/2}} - \frac{15}{4a^3\sqrt{x}} + \frac{1}{2a\sqrt{x}(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(a + b*x)^3), x]

[Out] $-15/(4*a^3*\text{Sqrt}[x]) + 1/(2*a*\text{Sqrt}[x]*(a + b*x)^2) + 5/(4*a^2*\text{Sqrt}[x]*(a + b*x)) - (15*\text{Sqrt}[b]*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/(\text{Sqrt}[a])])/(4*a^{(7/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

`Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{3/2}(a+bx)^3} dx &= \frac{1}{2a\sqrt{x}(a+bx)^2} + \frac{5 \int \frac{1}{x^{3/2}(a+bx)^2} dx}{4a} \\
 &= \frac{1}{2a\sqrt{x}(a+bx)^2} + \frac{5}{4a^2\sqrt{x}(a+bx)} + \frac{15 \int \frac{1}{x^{3/2}(a+bx)} dx}{8a^2} \\
 &= -\frac{15}{4a^3\sqrt{x}} + \frac{1}{2a\sqrt{x}(a+bx)^2} + \frac{5}{4a^2\sqrt{x}(a+bx)} - \frac{(15b) \int \frac{1}{\sqrt{x}(a+bx)} dx}{8a^3} \\
 &= -\frac{15}{4a^3\sqrt{x}} + \frac{1}{2a\sqrt{x}(a+bx)^2} + \frac{5}{4a^2\sqrt{x}(a+bx)} - \frac{(15b) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{4a^3} \\
 &= -\frac{15}{4a^3\sqrt{x}} + \frac{1}{2a\sqrt{x}(a+bx)^2} + \frac{5}{4a^2\sqrt{x}(a+bx)} - \frac{15\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 25, normalized size = 0.30

$$-\frac{{}_2F_1\left(-\frac{1}{2}, 3; \frac{1}{2}; -\frac{bx}{a}\right)}{a^3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(a + b*x)^3), x]

[Out] (-2*Hypergeometric2F1[-1/2, 3, 1/2, -(b*x)/a])/(a^3*Sqrt[x])

fricas [A] time = 0.48, size = 214, normalized size = 2.61

$$\left[\frac{15(b^2x^3 + 2abx^2 + a^2x)\sqrt{-\frac{b}{a}} \log\left(\frac{bx - 2a\sqrt{x}\sqrt{-\frac{b}{a}} - a}{bx+a}\right) - 2(15b^2x^2 + 25abx + 8a^2)\sqrt{x}}{8(a^3b^2x^3 + 2a^4bx^2 + a^5x)}, \frac{15(b^2x^3 + 2abx^2 + a^2x)}{4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a)^3,x, algorithm="fricas")

[Out] [1/8*(15*(b^2*x^3 + 2*a*b*x^2 + a^2*x)*sqrt(-b/a)*log((b*x - 2*a*sqrt(x))*sqrt(-b/a) - a)/(b*x + a)) - 2*(15*b^2*x^2 + 25*a*b*x + 8*a^2)*sqrt(x))/(a^3*b^2*x^3 + 2*a^4*b*x^2 + a^5*x), 1/4*(15*(b^2*x^3 + 2*a*b*x^2 + a^2*x)*sqrt(b/a)*arctan(a*sqrt(b/a)/(b*sqrt(x))) - (15*b^2*x^2 + 25*a*b*x + 8*a^2)*sqrt(x))/(a^3*b^2*x^3 + 2*a^4*b*x^2 + a^5*x)]

giac [A] time = 1.14, size = 59, normalized size = 0.72

$$-\frac{15 b \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4 \sqrt{ab} a^3} - \frac{2}{a^3 \sqrt{x}} - \frac{7 b^2 x^{\frac{3}{2}} + 9 ab \sqrt{x}}{4 (bx + a)^2 a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a)^3,x, algorithm="giac")

[Out] -15/4*b*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a^3) - 2/(a^3*sqrt(x)) - 1/4*(7*b^2*x^(3/2) + 9*a*b*sqrt(x))/((b*x + a)^2*a^3)

maple [A] time = 0.02, size = 66, normalized size = 0.80

$$-\frac{7 b^2 x^{\frac{3}{2}}}{4 (bx + a)^2 a^3} - \frac{9 b \sqrt{x}}{4 (bx + a)^2 a^2} - \frac{15 b \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4 \sqrt{ab} a^3} - \frac{2}{a^3 \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2)/(b*x+a)^3,x)

[Out] -2/a^3/x^(1/2)-7/4/a^3*b^2/(b*x+a)^2*x^(3/2)-9/4/a^2*b/(b*x+a)^2*x^(1/2)-15/4/a^3*b/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.99, size = 73, normalized size = 0.89

$$-\frac{15 b^2 x^2 + 25 abx + 8 a^2}{4 \left(a^3 b^2 x^{\frac{5}{2}} + 2 a^4 b x^{\frac{3}{2}} + a^5 \sqrt{x} \right)} - \frac{15 b \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4 \sqrt{ab} a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a)^3,x, algorithm="maxima")

[Out] -1/4*(15*b^2*x^2 + 25*a*b*x + 8*a^2)/(a^3*b^2*x^(5/2) + 2*a^4*b*x^(3/2) + a^5*sqrt(x)) - 15/4*b*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a^3)

mupad [B] time = 0.15, size = 70, normalized size = 0.85

$$-\frac{\frac{2}{a} + \frac{15b^2x^2}{4a^3} + \frac{25bx}{4a^2}}{a^2\sqrt{x} + b^2x^{5/2} + 2abx^{3/2}} - \frac{15\sqrt{b} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(a + b*x)^3), x)`

[Out] $-(2/a + (15*b^2*x^2)/(4*a^3) + (25*b*x)/(4*a^2))/(a^2*x^{1/2} + b^2*x^{5/2}) + 2*a*b*x^{3/2} - (15*b^{1/2}*atan((b^{1/2}*x^{1/2})/a^{1/2}))/ (4*a^{7/2})$

sympy [A] time = 54.35, size = 865, normalized size = 10.55

$$\left\{ \begin{array}{l} \frac{\infty}{7} \\ x^2 \\ -\frac{2}{a^3\sqrt{x}} \\ -\frac{2}{7b^3x^2} \end{array} \right\} - \frac{16ia^{\frac{5}{2}}\sqrt{\frac{1}{b}}}{8ia^{\frac{11}{2}}\sqrt{x}\sqrt{\frac{1}{b}} + 16ia^{\frac{9}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 8ia^{\frac{7}{2}}b^2x^{\frac{5}{2}}\sqrt{\frac{1}{b}}} - \frac{50ia^{\frac{3}{2}}bx\sqrt{\frac{1}{b}}}{8ia^{\frac{11}{2}}\sqrt{x}\sqrt{\frac{1}{b}} + 16ia^{\frac{9}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 8ia^{\frac{7}{2}}b^2x^{\frac{5}{2}}\sqrt{\frac{1}{b}}} - \frac{30i\sqrt{a}b^2x^2\sqrt{\frac{1}{b}}}{8ia^{\frac{11}{2}}\sqrt{x}\sqrt{\frac{1}{b}} + 16ia^{\frac{9}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 8ia^{\frac{7}{2}}b^2x^{\frac{5}{2}}\sqrt{\frac{1}{b}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(b*x+a)**3, x)`

[Out] `Piecewise((zoo/x**(7/2), Eq(a, 0) & Eq(b, 0)), (-2/(a**3*sqrt(x)), Eq(b, 0)), (-2/(7*b**3*x**(7/2)), Eq(a, 0)), (-16*I*a**(5/2)*sqrt(1/b)/(8*I*a**(11/2)*sqrt(x)*sqrt(1/b) + 16*I*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*I*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) - 50*I*a**(3/2)*b*x*sqrt(1/b)/(8*I*a**(11/2)*sqrt(x)*sqrt(1/b) + 16*I*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*I*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) - 30*I*sqrt(a)*b**2*x**2*sqrt(1/b)/(8*I*a**(11/2)*sqrt(x)*sqrt(1/b) + 16*I*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*I*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) - 15*a**2*sqrt(x)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(11/2)*sqrt(x)*sqrt(1/b) + 16*I*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*I*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) + 15*a**2*sqrt(x)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(11/2)*sqrt(x)*sqrt(1/b) + 16*I*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*I*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) - 30*a*b*x**(3/2)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(11/2)*sqrt(x)*sqrt(1/b) + 16*I*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*I*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) + 30*a*b*x**(3/2)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(11/2)*sqrt(x)*sqrt(1/b) + 16*I*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*I*a**(7/2)*b**2*x**(5/2)*sqrt(1/b))`

```

rt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(11/2)*sqrt(x)*sqrt(1/b) + 16*I*a**(9/2)
*b*x**(3/2)*sqrt(1/b) + 8*I*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) - 15*b**2*x**
(5/2)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(11/2)*sqrt(x)*sqrt(1/b)
+ 16*I*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*I*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)
) + 15*b**2*x**(5/2)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(8*I*a**(11/2)*sqrt
(x)*sqrt(1/b) + 16*I*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*I*a**(7/2)*b**2*x**
(5/2)*sqrt(1/b)), True))

```

$$3.468 \quad \int \frac{1}{x^{5/2}(a+bx)^3} dx$$

Optimal. Leaf size=95

$$\frac{35b^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{9/2}} + \frac{35b}{4a^4\sqrt{x}} - \frac{35}{12a^3x^{3/2}} + \frac{7}{4a^2x^{3/2}(a+bx)} + \frac{1}{2ax^{3/2}(a+bx)^2}$$

[Out] $-35/12/a^3/x^{(3/2)}+1/2/a/x^{(3/2)}/(b*x+a)^2+7/4/a^2/x^{(3/2)}/(b*x+a)+35/4*b^{(3/2)}*\arctan(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/a^{(9/2)}+35/4*b/a^4/x^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {51, 63, 205}

$$\frac{35b^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{9/2}} + \frac{7}{4a^2x^{3/2}(a+bx)} + \frac{35b}{4a^4\sqrt{x}} - \frac{35}{12a^3x^{3/2}} + \frac{1}{2ax^{3/2}(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(a + b*x)^3), x]

[Out] $-35/(12*a^3*x^{(3/2)}) + (35*b)/(4*a^4*\text{Sqrt}[x]) + 1/(2*a*x^{(3/2)}*(a + b*x)^2) + 7/(4*a^2*x^{(3/2)}*(a + b*x)) + (35*b^{(3/2)}*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/ \text{Sqrt}[a]])/(4*a^{(9/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{5/2}(a+bx)^3} dx &= \frac{1}{2ax^{3/2}(a+bx)^2} + \frac{7 \int \frac{1}{x^{5/2}(a+bx)^2} dx}{4a} \\
 &= \frac{1}{2ax^{3/2}(a+bx)^2} + \frac{7}{4a^2x^{3/2}(a+bx)} + \frac{35 \int \frac{1}{x^{5/2}(a+bx)} dx}{8a^2} \\
 &= -\frac{35}{12a^3x^{3/2}} + \frac{1}{2ax^{3/2}(a+bx)^2} + \frac{7}{4a^2x^{3/2}(a+bx)} - \frac{(35b) \int \frac{1}{x^{3/2}(a+bx)} dx}{8a^3} \\
 &= -\frac{35}{12a^3x^{3/2}} + \frac{35b}{4a^4\sqrt{x}} + \frac{1}{2ax^{3/2}(a+bx)^2} + \frac{7}{4a^2x^{3/2}(a+bx)} + \frac{(35b^2) \int \frac{1}{\sqrt{x}(a+bx)} dx}{8a^4} \\
 &= -\frac{35}{12a^3x^{3/2}} + \frac{35b}{4a^4\sqrt{x}} + \frac{1}{2ax^{3/2}(a+bx)^2} + \frac{7}{4a^2x^{3/2}(a+bx)} + \frac{(35b^2) \text{Subst}\left(\int \frac{1}{a+bx^2} dx, x, \sqrt{x}\right)}{4a^4} \\
 &= -\frac{35}{12a^3x^{3/2}} + \frac{35b}{4a^4\sqrt{x}} + \frac{1}{2ax^{3/2}(a+bx)^2} + \frac{7}{4a^2x^{3/2}(a+bx)} + \frac{35b^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{9/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 27, normalized size = 0.28

$$-\frac{{}_2F_1\left(-\frac{3}{2}, 3; -\frac{1}{2}; -\frac{bx}{a}\right)}{3a^3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(a + b*x)^3), x]

[Out] (-2*Hypergeometric2F1[-3/2, 3, -1/2, -((b*x)/a)])/(3*a^3*x^(3/2))

fricas [A] time = 0.45, size = 250, normalized size = 2.63

$$\left[\frac{105(b^3x^4 + 2ab^2x^3 + a^2bx^2)\sqrt{-\frac{b}{a}} \log\left(\frac{bx+2a\sqrt{x}\sqrt{-\frac{b}{a}}-a}{bx+a}\right) + 2(105b^3x^3 + 175ab^2x^2 + 56a^2bx - 8a^3)\sqrt{x} - 105(b^3x^4 + 2ab^2x^3 + a^2bx^2)}{24(a^4b^2x^4 + 2a^5bx^3 + a^6x^2)}, - \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^3,x, algorithm="fricas")

[Out] [1/24*(105*(b^3*x^4 + 2*a*b^2*x^3 + a^2*b*x^2)*sqrt(-b/a)*log((b*x + 2*a*sqrt(x)*sqrt(-b/a) - a)/(b*x + a)) + 2*(105*b^3*x^3 + 175*a*b^2*x^2 + 56*a^2*b*x - 8*a^3)*sqrt(x))/(a^4*b^2*x^4 + 2*a^5*b*x^3 + a^6*x^2), -1/12*(105*(b^3*x^4 + 2*a*b^2*x^3 + a^2*b*x^2)*sqrt(b/a)*arctan(a*sqrt(b/a)/(b*sqrt(x))) - (105*b^3*x^3 + 175*a*b^2*x^2 + 56*a^2*b*x - 8*a^3)*sqrt(x))/(a^4*b^2*x^4 + 2*a^5*b*x^3 + a^6*x^2)]

giac [A] time = 1.10, size = 71, normalized size = 0.75

$$\frac{35b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}a^4} + \frac{2(9bx - a)}{3a^4x^{\frac{3}{2}}} + \frac{11b^3x^{\frac{3}{2}} + 13ab^2\sqrt{x}}{4(bx + a)^2a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^3,x, algorithm="giac")

[Out] 35/4*b^2*arctan(b*sqrt(x)/sqrt(a*b))/(sqrt(a*b)*a^4) + 2/3*(9*b*x - a)/(a^4*x^(3/2)) + 1/4*(11*b^3*x^(3/2) + 13*a*b^2*sqrt(x))/((b*x + a)^2*a^4)

maple [A] time = 0.02, size = 79, normalized size = 0.83

$$\frac{11b^3x^{\frac{3}{2}}}{4(bx + a)^2a^4} + \frac{13b^2\sqrt{x}}{4(bx + a)^2a^3} + \frac{35b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}a^4} + \frac{6b}{a^4\sqrt{x}} - \frac{2}{3a^3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(5/2)/(b*x+a)^3,x)

[Out] -2/3/a^3/x^(3/2)+6*b/a^4/x^(1/2)+11/4/a^4*b^3/(b*x+a)^2*x^(3/2)+13/4/a^3*b^2/(b*x+a)^2*x^(1/2)+35/4/a^4*b^2/(a*b)^(1/2)*arctan(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.98, size = 86, normalized size = 0.91

$$\frac{105b^3x^3 + 175ab^2x^2 + 56a^2bx - 8a^3}{12\left(a^4b^2x^{\frac{7}{2}} + 2a^5bx^{\frac{5}{2}} + a^6x^{\frac{3}{2}}\right)} + \frac{35b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^3,x, algorithm="maxima")

[Out] $1/12*(105*b^3*x^3 + 175*a*b^2*x^2 + 56*a^2*b*x - 8*a^3)/(a^4*b^2*x^{(7/2)} + 2*a^5*b*x^{(5/2)} + a^6*x^{(3/2)}) + 35/4*b^2*\arctan(b*\sqrt{x}/\sqrt{a*b})/(\sqrt{a*b})*a^4$

mupad [B] time = 0.16, size = 80, normalized size = 0.84

$$\frac{\frac{175b^2x^2}{12a^3} - \frac{2}{3a} + \frac{35b^3x^3}{4a^4} + \frac{14bx}{3a^2}}{a^2x^{3/2} + b^2x^{7/2} + 2abx^{5/2}} + \frac{35b^{3/2} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{9/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/2)*(a + b*x)^3), x)`

[Out] $((175*b^2*x^2)/(12*a^3) - 2/(3*a) + (35*b^3*x^3)/(4*a^4) + (14*b*x)/(3*a^2))/(a^2*x^{(3/2)} + b^2*x^{(7/2)} + 2*a*b*x^{(5/2)}) + (35*b^{(3/2)}*\operatorname{atan}(b^{(1/2)}*x^{(1/2)})/a^{(1/2)})/(4*a^{(9/2)})$

sympy [A] time = 138.08, size = 962, normalized size = 10.13

$$\left\{ \begin{array}{l} \frac{\infty}{9} \\ x^2 \\ - \frac{2}{3a^3x^2} \\ \frac{2}{9b^3x^2} \end{array} \right\} - \frac{16ia^{\frac{7}{2}}\sqrt{\frac{1}{b}}}{24ia^{\frac{13}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 48ia^{\frac{11}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}} + 24ia^{\frac{9}{2}}b^2x^{\frac{7}{2}}\sqrt{\frac{1}{b}}} + \frac{112ia^{\frac{5}{2}}bx\sqrt{\frac{1}{b}}}{24ia^{\frac{13}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 48ia^{\frac{11}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}} + 24ia^{\frac{9}{2}}b^2x^{\frac{7}{2}}\sqrt{\frac{1}{b}}} + \frac{350ia^{\frac{3}{2}}b^2x^2\sqrt{\frac{1}{b}}}{24ia^{\frac{13}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 48ia^{\frac{11}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}} + 24ia^{\frac{9}{2}}b^2x^{\frac{7}{2}}\sqrt{\frac{1}{b}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(b*x+a)**3, x)`

[Out] $\operatorname{Piecewise}((\operatorname{zoo}/x^{(9/2)}, \operatorname{Eq}(a, 0) \ \& \ \operatorname{Eq}(b, 0)), (-2/(3*a^{**3}*x^{(3/2)}), \operatorname{Eq}(b, 0)), (-2/(9*b^{**3}*x^{(9/2)}), \operatorname{Eq}(a, 0)), (-16*I*a^{(7/2)}*\sqrt{1/b}/(24*I*a^{(13/2)}*x^{(3/2)}*\sqrt{1/b} + 48*I*a^{(11/2)}*b*x^{(5/2)}*\sqrt{1/b} + 24*I*a^{(9/2)}*b^{**2}*x^{(7/2)}*\sqrt{1/b})) + 112*I*a^{(5/2)}*b*x*\sqrt{1/b}/(24*I*a^{(13/2)}*x^{(3/2)}*\sqrt{1/b} + 48*I*a^{(11/2)}*b*x^{(5/2)}*\sqrt{1/b} + 24*I*a^{(9/2)}*b^{**2}*x^{(7/2)}*\sqrt{1/b})) + 350*I*a^{(3/2)}*b^{**2}*x^2*\sqrt{1/b}/(24*I*a^{(13/2)}*x^{(3/2)}*\sqrt{1/b} + 48*I*a^{(11/2)}*b*x^{(5/2)}*\sqrt{1/b} + 24*I*a^{(9/2)}*b^{**2}*x^{(7/2)}*\sqrt{1/b})) + 210*I*\sqrt{a}*b^{**3}*x^{**3}*\sqrt{1/b}/(24*I*a^{(13/2)}*x^{(3/2)}*\sqrt{1/b} + 48*I*a^{(11/2)}*b*x^{(5/2)}*\sqrt{1/b} + 24*I*a^{(9/2)}*b^{**2}*x^{(7/2)}*\sqrt{1/b})) + 105*a^{**2}*b*x^{(3/2)}*\log(-I*\sqrt{a}*\sqrt{1/b} +$

```

sqrt(x))/(24*I*a**(13/2)*x**(3/2)*sqrt(1/b) + 48*I*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*I*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) - 105*a**2*b*x**(3/2)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(13/2)*x**(3/2)*sqrt(1/b) + 48*I*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*I*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) + 210*a*b**2*x**(5/2)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(13/2)*x**(3/2)*sqrt(1/b) + 48*I*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*I*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) - 210*a*b**2*x**(5/2)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(13/2)*x**(3/2)*sqrt(1/b) + 48*I*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*I*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) + 105*b**3*x**(7/2)*log(-I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(13/2)*x**(3/2)*sqrt(1/b) + 48*I*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*I*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) - 105*b**3*x**(7/2)*log(I*sqrt(a)*sqrt(1/b) + sqrt(x))/(24*I*a**(13/2)*x**(3/2)*sqrt(1/b) + 48*I*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*I*a**(9/2)*b**2*x**(7/2)*sqrt(1/b))
, True))

```

$$3.469 \quad \int \frac{x^{5/2}}{-a+bx} dx$$

Optimal. Leaf size=68

$$-\frac{2a^{5/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}} + \frac{2a^2\sqrt{x}}{b^3} + \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b}$$

[Out] $2/3*a*x^{(3/2)}/b^2+2/5*x^{(5/2)}/b-2*a^{(5/2)}*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/b^{(7/2)}+2*a^2*x^{(1/2)}/b^3$

Rubi [A] time = 0.02, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 63, 208}

$$\frac{2a^2\sqrt{x}}{b^3} - \frac{2a^{5/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}} + \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)/(-a + b*x), x]

[Out] $(2*a^2*\operatorname{Sqrt}[x])/b^3 + (2*a*x^{(3/2)})/(3*b^2) + (2*x^{(5/2)})/(5*b) - (2*a^{(5/2)})*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/(\operatorname{Sqrt}[a])]/b^{(7/2)}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{x^{5/2}}{-a+bx} dx &= \frac{2x^{5/2}}{5b} + \frac{a \int \frac{x^{3/2}}{-a+bx} dx}{b} \\
 &= \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b} + \frac{a^2 \int \frac{\sqrt{x}}{-a+bx} dx}{b^2} \\
 &= \frac{2a^2\sqrt{x}}{b^3} + \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b} + \frac{a^3 \int \frac{1}{\sqrt{x}(-a+bx)} dx}{b^3} \\
 &= \frac{2a^2\sqrt{x}}{b^3} + \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b} + \frac{(2a^3) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{b^3} \\
 &= \frac{2a^2\sqrt{x}}{b^3} + \frac{2ax^{3/2}}{3b^2} + \frac{2x^{5/2}}{5b} - \frac{2a^{5/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}}
 \end{aligned}$$

Mathematica [A] time = 0.03, size = 61, normalized size = 0.90

$$\frac{2\sqrt{x} (15a^2 + 5abx + 3b^2x^2)}{15b^3} - \frac{2a^{5/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/(-a + b*x), x]

[Out] (2*sqrt[x]*(15*a^2 + 5*a*b*x + 3*b^2*x^2))/(15*b^3) - (2*a^(5/2)*ArcTanh[(Sqrt[b]*sqrt[x])/sqrt[a]])/b^(7/2)

fricas [A] time = 0.43, size = 131, normalized size = 1.93

$$\left[\frac{15 a^2 \sqrt{\frac{a}{b}} \log\left(\frac{bx-2b\sqrt{x}\sqrt{\frac{a}{b}}+a}{bx-a}\right) + 2(3b^2x^2 + 5abx + 15a^2)\sqrt{x}}{15b^3}, \frac{2\left(15a^2\sqrt{-\frac{a}{b}} \arctan\left(\frac{b\sqrt{x}\sqrt{-\frac{a}{b}}}{a}\right) + (3b^2x^2 + 5abx + 15a^2)\sqrt{x}\right)}{15b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x-a),x, algorithm="fricas")

[Out] [1/15*(15*a^2*sqrt(a/b)*log((b*x - 2*b*sqrt(x)*sqrt(a/b) + a)/(b*x - a)) + 2*(3*b^2*x^2 + 5*a*b*x + 15*a^2)*sqrt(x))/b^3, 2/15*(15*a^2*sqrt(-a/b)*arctan(b*sqrt(x)*sqrt(-a/b)/a) + (3*b^2*x^2 + 5*a*b*x + 15*a^2)*sqrt(x))/b^3]

giac [A] time = 1.03, size = 61, normalized size = 0.90

$$\frac{2a^3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab} b^3} + \frac{2\left(3b^4x^{\frac{5}{2}} + 5ab^3x^{\frac{3}{2}} + 15a^2b^2\sqrt{x}\right)}{15b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x-a),x, algorithm="giac")

[Out] 2*a^3*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*b^3) + 2/15*(3*b^4*x^(5/2) + 5*a*b^3*x^(3/2) + 15*a^2*b^2*sqrt(x))/b^5

maple [A] time = 0.01, size = 54, normalized size = 0.79

$$-\frac{2a^3 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^3} + \frac{\frac{2b^2x^{\frac{5}{2}}}{5} + \frac{2abx^{\frac{3}{2}}}{3} + 2a^2\sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x-a),x)

[Out] 2/b^3*(1/5*b^2*x^(5/2)+1/3*a*b*x^(3/2)+a^2*x^(1/2))-2*a^3/b^3/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.94, size = 70, normalized size = 1.03

$$\frac{a^3 \log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{\sqrt{ab} b^3} + \frac{2\left(3b^2x^{\frac{5}{2}} + 5abx^{\frac{3}{2}} + 15a^2\sqrt{x}\right)}{15b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x-a),x, algorithm="maxima")

[Out] a^3*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*b^3) + 2/15*(3*b^2*x^(5/2) + 5*a*b*x^(3/2) + 15*a^2*sqrt(x))/b^3

mupad [B] time = 0.15, size = 51, normalized size = 0.75

$$\frac{2x^{5/2}}{5b} + \frac{2ax^{3/2}}{3b^2} + \frac{2a^2\sqrt{x}}{b^3} + \frac{a^{5/2} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-x^(5/2)/(a - b*x), x)`

[Out] $(2*x^{(5/2)})/(5*b) + (2*a*x^{(3/2)})/(3*b^2) + (2*a^2*x^{(1/2)})/b^3 + (a^{(5/2)}*atan((b^{(1/2)}*x^{(1/2)}*1i)/a^{(1/2)})*2i)/b^{(7/2)}$

sympy [A] time = 7.10, size = 116, normalized size = 1.71

$$\left\{ \begin{array}{ll} \frac{a^{\frac{5}{2}} \log\left(-\sqrt{a} \sqrt{\frac{1}{b}} + \sqrt{x}\right)}{b^4 \sqrt{\frac{1}{b}}} - \frac{a^{\frac{5}{2}} \log\left(\sqrt{a} \sqrt{\frac{1}{b}} + \sqrt{x}\right)}{b^4 \sqrt{\frac{1}{b}}} + \frac{2a^2 \sqrt{x}}{b^3} + \frac{2ax^{\frac{3}{2}}}{3b^2} + \frac{2x^{\frac{5}{2}}}{5b} & \text{for } b \neq 0 \\ -\frac{2x^{\frac{7}{2}}}{7a} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/2)/(b*x-a), x)`

[Out] `Piecewise((a**(5/2)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(b**4*sqrt(1/b)) - a*(5/2)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(b**4*sqrt(1/b)) + 2*a**2*sqrt(x)/b**3 + 2*a*x**(3/2)/(3*b**2) + 2*x**(5/2)/(5*b), Ne(b, 0)), (-2*x**(7/2)/(7*a), True))`

$$3.470 \quad \int \frac{x^{3/2}}{-a+bx} dx$$

Optimal. Leaf size=53

$$-\frac{2a^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} + \frac{2a\sqrt{x}}{b^2} + \frac{2x^{3/2}}{3b}$$

[Out] $2/3*x^{(3/2)}/b-2*a^{(3/2)*\arctanh(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/b^{(5/2)}+2*a*x^{(1/2)}/b^2$

Rubi [A] time = 0.02, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 63, 208}

$$-\frac{2a^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} + \frac{2a\sqrt{x}}{b^2} + \frac{2x^{3/2}}{3b}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)/(-a + b*x), x]

[Out] $(2*a*\text{Sqrt}[x])/b^2 + (2*x^{(3/2)})/(3*b) - (2*a^{(3/2)}*\text{ArcTanh}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a]])/b^{(5/2)}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

`Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{x^{3/2}}{-a+bx} dx &= \frac{2x^{3/2}}{3b} + \frac{a \int \frac{\sqrt{x}}{-a+bx} dx}{b} \\
 &= \frac{2a\sqrt{x}}{b^2} + \frac{2x^{3/2}}{3b} + \frac{a^2 \int \frac{1}{\sqrt{x}(-a+bx)} dx}{b^2} \\
 &= \frac{2a\sqrt{x}}{b^2} + \frac{2x^{3/2}}{3b} + \frac{(2a^2) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{b^2} \\
 &= \frac{2a\sqrt{x}}{b^2} + \frac{2x^{3/2}}{3b} - \frac{2a^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.02, size = 49, normalized size = 0.92

$$\frac{2\sqrt{x}(3a+bx)}{3b^2} - \frac{2a^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/(-a + b*x), x]

[Out] (2*Sqrt[x]*(3*a + b*x))/(3*b^2) - (2*a^(3/2)*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/b^(5/2)

fricas [A] time = 0.46, size = 103, normalized size = 1.94

$$\left[\frac{3a\sqrt{\frac{a}{b}} \log\left(\frac{bx-2b\sqrt{x}\sqrt{\frac{a}{b}}+a}{bx-a}\right) + 2(bx+3a)\sqrt{x}}{3b^2}, \frac{2\left(3a\sqrt{-\frac{a}{b}} \arctan\left(\frac{b\sqrt{x}\sqrt{-\frac{a}{b}}}{a}\right) + (bx+3a)\sqrt{x}\right)}{3b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x-a), x, algorithm="fricas")

[Out] $[1/3*(3*a*\sqrt{a/b}*\log((b*x - 2*b*\sqrt{x})*\sqrt{a/b} + a)/(b*x - a)) + 2*(b*x + 3*a)*\sqrt{x}]/b^2, 2/3*(3*a*\sqrt{-a/b}*\arctan(b*\sqrt{x}*\sqrt{-a/b}/a) + (b*x + 3*a)*\sqrt{x})/b^2]$

giac [A] time = 0.94, size = 47, normalized size = 0.89

$$\frac{2a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab} b^2} + \frac{2\left(b^2 x^{\frac{3}{2}} + 3ab\sqrt{x}\right)}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)/(b*x-a),x, algorithm="giac")`

[Out] $2*a^2*\arctan(b*\sqrt{x}/\sqrt{-a*b})/(\sqrt{-a*b}*b^2) + 2/3*(b^2*x^(3/2) + 3*a*b*\sqrt{x})/b^3$

maple [A] time = 0.01, size = 43, normalized size = 0.81

$$-\frac{2a^2 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b^2} + \frac{\frac{2bx^{\frac{3}{2}}}{3} + 2a\sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(b*x-a),x)`

[Out] $2/b^2*(1/3*b*x^(3/2)+a*x^(1/2))-2*a^2/b^2/(a*b)^(1/2)*\operatorname{arctanh}(1/(a*b)^(1/2)*b*x^(1/2))$

maxima [A] time = 2.92, size = 58, normalized size = 1.09

$$\frac{a^2 \log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{\sqrt{ab} b^2} + \frac{2\left(bx^{\frac{3}{2}} + 3a\sqrt{x}\right)}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)/(b*x-a),x, algorithm="maxima")`

[Out] $a^2*\log((b*\sqrt{x} - \sqrt{a*b})/(b*\sqrt{x} + \sqrt{a*b}))/(\sqrt{a*b}*b^2) + 2/3*(b*x^(3/2) + 3*a*\sqrt{x})/b^2$

mupad [B] time = 0.11, size = 37, normalized size = 0.70

$$\frac{2x^{3/2}}{3b} + \frac{2a\sqrt{x}}{b^2} - \frac{2a^{3/2} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-x^(3/2)/(a - b*x), x)`

[Out] $(2*x^{(3/2)})/(3*b) + (2*a*x^{(1/2)})/b^2 - (2*a^{(3/2)}*atanh((b^{(1/2)}*x^{(1/2)})/a^{(1/2)}))/b^{(5/2)}$

sympy [A] time = 1.87, size = 100, normalized size = 1.89

$$\left\{ \begin{array}{ll} \frac{a^{\frac{3}{2}} \log\left(-\sqrt{a} \sqrt{\frac{1}{b}} + \sqrt{x}\right)}{b^3 \sqrt{\frac{1}{b}}} - \frac{a^{\frac{3}{2}} \log\left(\sqrt{a} \sqrt{\frac{1}{b}} + \sqrt{x}\right)}{b^3 \sqrt{\frac{1}{b}}} + \frac{2a\sqrt{x}}{b^2} + \frac{2x^{\frac{3}{2}}}{3b} & \text{for } b \neq 0 \\ -\frac{2x^{\frac{5}{2}}}{5a} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(b*x-a), x)`

[Out] `Piecewise((a**(3/2)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(b**3*sqrt(1/b)) - a**
*(3/2)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(b**3*sqrt(1/b)) + 2*a*sqrt(x)/b**2
+ 2*x**(3/2)/(3*b), Ne(b, 0)), (-2*x**(5/2)/(5*a), True))`

$$3.471 \quad \int \frac{\sqrt{x}}{-a+bx} dx$$

Optimal. Leaf size=40

$$\frac{2\sqrt{x}}{b} - \frac{2\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}}$$

[Out] $-2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})*a^{(1/2)}/b^{(3/2)}+2*x^{(1/2)}/b$

Rubi [A] time = 0.01, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 63, 208}

$$\frac{2\sqrt{x}}{b} - \frac{2\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[x]/(-a + b*x), x]`

[Out] $(2*\operatorname{Sqrt}[x])/b - (2*\operatorname{Sqrt}[a]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a]])/b^{(3/2)}$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt{x}}{-a+bx} dx &= \frac{2\sqrt{x}}{b} + \frac{a \int \frac{1}{\sqrt{x}(-a+bx)} dx}{b} \\
 &= \frac{2\sqrt{x}}{b} + \frac{(2a) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{b} \\
 &= \frac{2\sqrt{x}}{b} - \frac{2\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}}
 \end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 1.00

$$\frac{2\sqrt{x}}{b} - \frac{2\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(-a + b*x),x]

[Out] (2*Sqrt[x])/b - (2*Sqrt[a]*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/b^(3/2)

fricas [A] time = 0.46, size = 83, normalized size = 2.08

$$\left[\frac{\sqrt{\frac{a}{b}} \log\left(\frac{bx-2b\sqrt{x}\sqrt{\frac{a}{b}}+a}{bx-a}\right) + 2\sqrt{x}}{b}, \frac{2\left(\sqrt{-\frac{a}{b}} \arctan\left(\frac{b\sqrt{x}\sqrt{-\frac{a}{b}}}{a}\right) + \sqrt{x}\right)}{b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x-a),x, algorithm="fricas")

[Out] [(sqrt(a/b)*log((b*x - 2*b*sqrt(x)*sqrt(a/b) + a)/(b*x - a)) + 2*sqrt(x))/b, 2*(sqrt(-a/b)*arctan(b*sqrt(x)*sqrt(-a/b)/a) + sqrt(x))/b]

giac [A] time = 1.04, size = 33, normalized size = 0.82

$$\frac{2a \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab}b} + \frac{2\sqrt{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x-a),x, algorithm="giac")

[Out] 2*a*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*b) + 2*sqrt(x)/b

maple [A] time = 0.00, size = 32, normalized size = 0.80

$$-\frac{2a \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b} + \frac{2\sqrt{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x-a),x)

[Out] 2/b*x^(1/2)-2*a/b/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 3.08, size = 47, normalized size = 1.18

$$\frac{a \log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{\sqrt{ab} b} + \frac{2\sqrt{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x-a),x, algorithm="maxima")

[Out] a*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*b) + 2*sqrt(x)/b

mupad [B] time = 0.11, size = 28, normalized size = 0.70

$$\frac{2\sqrt{x}}{b} - \frac{2\sqrt{a} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-x^(1/2)/(a - b*x),x)

[Out] (2*x^(1/2))/b - (2*a^(1/2)*atanh((b^(1/2)*x^(1/2))/a^(1/2)))/b^(3/2)

sympy [A] time = 0.71, size = 87, normalized size = 2.18

$$\left\{ \begin{array}{ll} \frac{\sqrt{a} \log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{b^2\sqrt{\frac{1}{b}}} - \frac{\sqrt{a} \log\left(\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{b^2\sqrt{\frac{1}{b}}} + \frac{2\sqrt{x}}{b} & \text{for } b \neq 0 \\ -\frac{2x^{\frac{3}{2}}}{3a} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(1/2)/(b*x-a),x)
```

```
[Out] Piecewise((sqrt(a)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(b**2*sqrt(1/b)) - sqrt(a)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(b**2*sqrt(1/b)) + 2*sqrt(x)/b, Ne(b, 0)), (-2*x**(3/2)/(3*a), True))
```

$$3.472 \quad \int \frac{1}{\sqrt{x}(-a+bx)} dx$$

Optimal. Leaf size=29

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}\sqrt{b}}$$

[Out] $-2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/a^{(1/2)}/b^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {63, 208}

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}\sqrt{b}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/(\operatorname{Sqrt}[x]*(-a + b*x)), x]$

[Out] $(-2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a]])/(\operatorname{Sqrt}[a]*\operatorname{Sqrt}[b])$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_)^m)*((c_.) + (d_.)*(x_)^n), x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{p*(m+1)-1}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /; \operatorname{FreeQ}[\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 208

$\operatorname{Int}[(a_. + (b_.)*(x_)^2)^{-1}, x_Symbol] \rightarrow \operatorname{Simp}[(\operatorname{Rt}[-(a/b), 2]*\operatorname{ArcTanh}[x/\operatorname{Rt}[-(a/b), 2]])/a, x] /; \operatorname{FreeQ}[\{a, b\}, x] \&\& \operatorname{NegQ}[a/b]$

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{x}(-a+bx)} dx &= 2 \operatorname{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right) \\ &= -\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}\sqrt{b}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 1.00

$$\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(-a + b*x)),x]

[Out] (-2*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[a]*Sqrt[b])

fricas [A] time = 0.45, size = 67, normalized size = 2.31

$$\left[\frac{\sqrt{ab} \log\left(\frac{bx+a-2\sqrt{ab}\sqrt{x}}{bx-a}\right)}{ab}, \frac{2\sqrt{-ab} \arctan\left(\frac{\sqrt{-ab}}{b\sqrt{x}}\right)}{ab} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-a)/x^(1/2),x, algorithm="fricas")

[Out] [sqrt(a*b)*log((b*x + a - 2*sqrt(a*b)*sqrt(x))/(b*x - a))/(a*b), 2*sqrt(-a*b)*arctan(sqrt(-a*b)/(b*sqrt(x)))/(a*b)]

giac [A] time = 1.00, size = 20, normalized size = 0.69

$$\frac{2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-a)/x^(1/2),x, algorithm="giac")

[Out] 2*arctan(b*sqrt(x)/sqrt(-a*b))/sqrt(-a*b)

maple [A] time = 0.00, size = 19, normalized size = 0.66

$$\frac{2 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x-a)/x^(1/2),x)

[Out] $-2/(a*b)^{(1/2)}*\operatorname{arctanh}(1/(a*b)^{(1/2)}*b*x^{(1/2)})$

maxima [A] time = 3.03, size = 34, normalized size = 1.17

$$\frac{\log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{\sqrt{ab}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-a)/x^(1/2),x, algorithm="maxima")`

[Out] $\log((b*\sqrt{x} - \sqrt{a*b})/(b*\sqrt{x} + \sqrt{a*b}))/\sqrt{a*b}$

mupad [B] time = 0.13, size = 19, normalized size = 0.66

$$-\frac{2 \operatorname{atanh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a} \sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-1/(x^(1/2)*(a - b*x)),x)`

[Out] $-(2*\operatorname{atanh}((b^{(1/2)}*x^{(1/2)})/a^{(1/2)}))/(a^{(1/2)}*b^{(1/2)})$

sympy [A] time = 1.25, size = 88, normalized size = 3.03

$$\left\{ \begin{array}{ll} \frac{\infty}{\sqrt{x}} & \text{for } a = 0 \wedge b = 0 \\ -\frac{2}{b\sqrt{x}} & \text{for } a = 0 \\ -\frac{2\sqrt{x}}{a} & \text{for } b = 0 \\ \frac{\log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{\sqrt{a}b\sqrt{\frac{1}{b}}} - \frac{\log\left(\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{\sqrt{a}b\sqrt{\frac{1}{b}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-a)/x**(1/2),x)`

[Out] `Piecewise((zoo/sqrt(x), Eq(a, 0) & Eq(b, 0)), (-2/(b*sqrt(x)), Eq(a, 0)), (-2*sqrt(x)/a, Eq(b, 0)), (log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(sqrt(a)*b*sqrt(1/b)) - log(sqrt(a)*sqrt(1/b) + sqrt(x))/(sqrt(a)*b*sqrt(1/b)), True))`

$$3.473 \quad \int \frac{1}{x^{3/2}(-a+bx)} dx$$

Optimal. Leaf size=40

$$\frac{2}{a\sqrt{x}} - \frac{2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}}$$

[Out] $-2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})*b^{(1/2)}/a^{(3/2)}+2/a/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 208}

$$\frac{2}{a\sqrt{x}} - \frac{2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/(x^{(3/2)}*(-a + b*x)), x]$

[Out] $2/(a*\operatorname{Sqrt}[x]) - (2*\operatorname{Sqrt}[b]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a]])/a^{(3/2)}$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)} / ((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*(m+n+2)) / ((b*c - a*d)*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^n, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, n\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{LtQ}[m, -1] \ \&\& !(\operatorname{LtQ}[n, -1] \ \&\& (\operatorname{EqQ}[a, 0] \ \|\ (\operatorname{NeQ}[c, 0] \ \&\& \operatorname{LtQ}[m - n, 0] \ \&\& \operatorname{IntegerQ}[n]))) \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{LtQ}[-1, m, 0] \ \&\& \operatorname{LeQ}[-1, n, 0] \ \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 208

$\operatorname{Int}[(a_. + (b_.)*(x_)^2)^{-1}, x_Symbol] \rightarrow \operatorname{Simp}[(\operatorname{Rt}[-(a/b), 2]*\operatorname{ArcTanh}[x/\operatorname{Rt}[-(a/b), 2]])/a, x] /;$ $\operatorname{FreeQ}\{a, b\}, x \ \&\& \operatorname{NegQ}[a/b]$

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{3/2}(-a+bx)} dx &= \frac{2}{a\sqrt{x}} + \frac{b \int \frac{1}{\sqrt{x}(-a+bx)} dx}{a} \\
&= \frac{2}{a\sqrt{x}} + \frac{(2b) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{a} \\
&= \frac{2}{a\sqrt{x}} - \frac{2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 24, normalized size = 0.60

$$\frac{{}_2F_1\left(-\frac{1}{2}, 1; \frac{1}{2}; \frac{bx}{a}\right)}{a\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(-a + b*x)),x]

[Out] (2*Hypergeometric2F1[-1/2, 1, 1/2, (b*x)/a])/(a*Sqrt[x])

fricas [A] time = 0.44, size = 91, normalized size = 2.28

$$\left[\frac{x\sqrt{\frac{b}{a}} \log\left(\frac{bx-2a\sqrt{x}\sqrt{\frac{b}{a}}+a}{bx-a}\right) + 2\sqrt{x}}{ax}, \frac{2\left(x\sqrt{\frac{-b}{a}} \arctan\left(\frac{a\sqrt{\frac{-b}{a}}}{b\sqrt{x}}\right) + \sqrt{x}\right)}{ax} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x-a),x, algorithm="fricas")

[Out] [(x*sqrt(b/a)*log((b*x - 2*a*sqrt(x)*sqrt(b/a) + a)/(b*x - a)) + 2*sqrt(x))/(a*x), 2*(x*sqrt(-b/a)*arctan(a*sqrt(-b/a)/(b*sqrt(x))) + sqrt(x))/(a*x)]

giac [A] time = 1.02, size = 33, normalized size = 0.82

$$\frac{2b \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab}a} + \frac{2}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x-a),x, algorithm="giac")

[Out] 2*b*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*a) + 2/(a*sqrt(x))

maple [A] time = 0.01, size = 32, normalized size = 0.80

$$-\frac{2b \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a} + \frac{2}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2)/(b*x-a),x)

[Out] -2/a*b/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2))+2/a/x^(1/2)

maxima [A] time = 2.87, size = 47, normalized size = 1.18

$$\frac{b \log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{\sqrt{ab} a} + \frac{2}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x-a),x, algorithm="maxima")

[Out] b*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*a) + 2/(a*sqrt(x))

mupad [B] time = 0.06, size = 28, normalized size = 0.70

$$\frac{2}{a\sqrt{x}} - \frac{2\sqrt{b} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-1/(x^(3/2)*(a - b*x)),x)

[Out] 2/(a*x^(1/2)) - (2*b^(1/2)*atanh((b^(1/2)*x^(1/2))/a^(1/2)))/a^(3/2)

sympy [A] time = 2.76, size = 94, normalized size = 2.35

$$\left\{ \begin{array}{ll} \frac{\infty}{x^2} & \text{for } a = 0 \wedge b = 0 \\ \frac{2}{a\sqrt{x}} & \text{for } b = 0 \\ -\frac{2}{3bx^{\frac{3}{2}}} & \text{for } a = 0 \\ \frac{2}{a\sqrt{x}} + \frac{\log\left(-\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{3}{2}}\sqrt{\frac{1}{b}}} - \frac{\log\left(\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{3}{2}}\sqrt{\frac{1}{b}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(3/2)/(b*x-a),x)

[Out] Piecewise((zoo/x**(3/2), Eq(a, 0) & Eq(b, 0)), (2/(a*sqrt(x)), Eq(b, 0)), (-2/(3*b*x**(3/2)), Eq(a, 0)), (2/(a*sqrt(x)) + log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(3/2)*sqrt(1/b)) - log(sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(3/2)*sqrt(1/b)), True))

$$3.474 \quad \int \frac{1}{x^{5/2}(-a+bx)} dx$$

Optimal. Leaf size=53

$$-\frac{2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}} + \frac{2b}{a^2\sqrt{x}} + \frac{2}{3ax^{3/2}}$$

[Out] $2/3/a/x^{(3/2)}-2*b^{(3/2)}*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/a^{(5/2)}+2*b/a^2/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 208}

$$-\frac{2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}} + \frac{2b}{a^2\sqrt{x}} + \frac{2}{3ax^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(-a + b*x)),x]

[Out] $2/(3*a*x^{(3/2)}) + (2*b)/(a^2*\operatorname{Sqrt}[x]) - (2*b^{(3/2)}*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a]])/a^{(5/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{5/2}(-a+bx)} dx &= \frac{2}{3ax^{3/2}} + \frac{b \int \frac{1}{x^{3/2}(-a+bx)} dx}{a} \\
 &= \frac{2}{3ax^{3/2}} + \frac{2b}{a^2\sqrt{x}} + \frac{b^2 \int \frac{1}{\sqrt{x}(-a+bx)} dx}{a^2} \\
 &= \frac{2}{3ax^{3/2}} + \frac{2b}{a^2\sqrt{x}} + \frac{(2b^2) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{a^2} \\
 &= \frac{2}{3ax^{3/2}} + \frac{2b}{a^2\sqrt{x}} - \frac{2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.00, size = 26, normalized size = 0.49

$$\frac{{}_2F_1\left(-\frac{3}{2}, 1; -\frac{1}{2}; \frac{bx}{a}\right)}{3ax^{3/2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[1/(x^(5/2)*(-a + b*x)),x]
```

```
[Out] (2*Hypergeometric2F1[-3/2, 1, -1/2, (b*x)/a])/(3*a*x^(3/2))
```

fricas [A] time = 0.45, size = 113, normalized size = 2.13

$$\left[\frac{3bx^2\sqrt{\frac{b}{a}} \log\left(\frac{bx-2a\sqrt{x}\sqrt{\frac{b}{a}+a}}{bx-a}\right) + 2(3bx+a)\sqrt{x}}{3a^2x^2}, \frac{2\left(3bx^2\sqrt{-\frac{b}{a}} \arctan\left(\frac{a\sqrt{-\frac{b}{a}}}{b\sqrt{x}}\right) + (3bx+a)\sqrt{x}\right)}{3a^2x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x^(5/2)/(b*x-a),x, algorithm="fricas")
```

[Out] $[1/3*(3*b*x^2*\sqrt{b/a}*\log((b*x - 2*a*\sqrt{x})*\sqrt{b/a} + a)/(b*x - a)) + 2*(3*b*x + a)*\sqrt{x})/(a^2*x^2), 2/3*(3*b*x^2*\sqrt{-b/a}*\arctan(a*\sqrt{-b/a)/(b*\sqrt{x})) + (3*b*x + a)*\sqrt{x})/(a^2*x^2)]$

giac [A] time = 0.98, size = 41, normalized size = 0.77

$$\frac{2b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab} a^2} + \frac{2(3bx + a)}{3a^2 x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2)/(b*x-a),x, algorithm="giac")`

[Out] $2*b^2*\arctan(b*\sqrt{x}/\sqrt{-a*b})/(\sqrt{-a*b}*a^2) + 2/3*(3*b*x + a)/(a^2*x^{(3/2)})$

maple [A] time = 0.01, size = 43, normalized size = 0.81

$$-\frac{2b^2 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^2} + \frac{2b}{a^2\sqrt{x}} + \frac{2}{3a x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/2)/(b*x-a),x)`

[Out] $-2/a^2*b^2/(a*b)^{(1/2)}*\operatorname{arctanh}(1/(a*b)^{(1/2)}*b*x^{(1/2)})+2/3/a/x^{(3/2)}+2/a^2*b/x^{(1/2)}$

maxima [A] time = 2.96, size = 55, normalized size = 1.04

$$\frac{b^2 \log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{\sqrt{ab} a^2} + \frac{2(3bx + a)}{3a^2 x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2)/(b*x-a),x, algorithm="maxima")`

[Out] $b^2*\log((b*\sqrt{x} - \sqrt{a*b})/(b*\sqrt{x} + \sqrt{a*b}))/(\sqrt{a*b}*a^2) + 2/3*(3*b*x + a)/(a^2*x^{(3/2)})$

mupad [B] time = 0.12, size = 37, normalized size = 0.70

$$\frac{\frac{2}{3a} + \frac{2bx}{a^2}}{x^{3/2}} - \frac{2b^{3/2} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-1/(x^(5/2)*(a - b*x)),x)`

[Out] $(2/(3*a) + (2*b*x)/a^2)/x^{3/2} - (2*b^{3/2}*atanh((b^{1/2}*x^{1/2})/a^{1/2}))/a^{5/2}$

sympy [A] time = 7.67, size = 112, normalized size = 2.11

$$\left\{ \begin{array}{ll} \frac{\infty}{x^2} & \text{for } a = 0 \wedge b = 0 \\ \frac{2}{3ax^2} & \text{for } b = 0 \\ -\frac{2}{5bx^2} & \text{for } a = 0 \\ \frac{2}{3ax^2} + \frac{2b}{a^2\sqrt{x}} + \frac{b \log\left(-\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{5}{2}}\sqrt{\frac{1}{b}}} - \frac{b \log\left(\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{5}{2}}\sqrt{\frac{1}{b}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(b*x-a),x)`

[Out] `Piecewise((zoo/x**(5/2), Eq(a, 0) & Eq(b, 0)), (2/(3*a*x**(3/2)), Eq(b, 0)), (-2/(5*b*x**(5/2)), Eq(a, 0)), (2/(3*a*x**(3/2)) + 2*b/(a**2*sqrt(x)) + b*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(5/2)*sqrt(1/b)) - b*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(5/2)*sqrt(1/b)), True))`

$$3.475 \quad \int \frac{1}{x^{7/2}(-a+bx)} dx$$

Optimal. Leaf size=68

$$-\frac{2b^{5/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}} + \frac{2b^2}{a^3\sqrt{x}} + \frac{2b}{3a^2x^{3/2}} + \frac{2}{5ax^{5/2}}$$

[Out] $2/5/a/x^{(5/2)}+2/3*b/a^2/x^{(3/2)}-2*b^{(5/2)}*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/a^{(7/2)}+2*b^2/a^3/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 208}

$$\frac{2b^2}{a^3\sqrt{x}} - \frac{2b^{5/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}} + \frac{2b}{3a^2x^{3/2}} + \frac{2}{5ax^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(7/2)*(-a + b*x)),x]

[Out] $2/(5*a*x^{(5/2)}) + (2*b)/(3*a^2*x^{(3/2)}) + (2*b^2)/(a^3*\operatorname{Sqrt}[x]) - (2*b^{(5/2)})*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a]]/a^{(7/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{7/2}(-a+bx)} dx &= \frac{2}{5ax^{5/2}} + \frac{b \int \frac{1}{x^{5/2}(-a+bx)} dx}{a} \\
 &= \frac{2}{5ax^{5/2}} + \frac{2b}{3a^2x^{3/2}} + \frac{b^2 \int \frac{1}{x^{3/2}(-a+bx)} dx}{a^2} \\
 &= \frac{2}{5ax^{5/2}} + \frac{2b}{3a^2x^{3/2}} + \frac{2b^2}{a^3\sqrt{x}} + \frac{b^3 \int \frac{1}{\sqrt{x}(-a+bx)} dx}{a^3} \\
 &= \frac{2}{5ax^{5/2}} + \frac{2b}{3a^2x^{3/2}} + \frac{2b^2}{a^3\sqrt{x}} + \frac{(2b^3) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{a^3} \\
 &= \frac{2}{5ax^{5/2}} + \frac{2b}{3a^2x^{3/2}} + \frac{2b^2}{a^3\sqrt{x}} - \frac{2b^{5/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 26, normalized size = 0.38

$$\frac{{}_2F_1\left(-\frac{5}{2}, 1; -\frac{3}{2}; \frac{bx}{a}\right)}{5ax^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(7/2)*(-a + b*x)), x]

[Out] (2*Hypergeometric2F1[-5/2, 1, -3/2, (b*x)/a])/(5*a*x^(5/2))

fricas [A] time = 0.46, size = 143, normalized size = 2.10

$$\left[\frac{15b^2x^3\sqrt{\frac{b}{a}} \log\left(\frac{bx-2a\sqrt{x}\sqrt{\frac{b}{a}+a}}{bx-a}\right) + 2(15b^2x^2 + 5abx + 3a^2)\sqrt{x}}{15a^3x^3}, \frac{2\left(15b^2x^3\sqrt{-\frac{b}{a}} \arctan\left(\frac{a\sqrt{-\frac{b}{a}}}{b\sqrt{x}}\right) + (15b^2x^2 + 5abx + 3a^2)\sqrt{x}\right)}{15a^3x^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x-a),x, algorithm="fricas")

[Out] [1/15*(15*b^2*x^3*sqrt(b/a)*log((b*x - 2*a*sqrt(x))*sqrt(b/a) + a)/(b*x - a) + 2*(15*b^2*x^2 + 5*a*b*x + 3*a^2)*sqrt(x))/(a^3*x^3), 2/15*(15*b^2*x^3*sqrt(-b/a)*arctan(a*sqrt(-b/a)/(b*sqrt(x))) + (15*b^2*x^2 + 5*a*b*x + 3*a^2)*sqrt(x))/(a^3*x^3)]

giac [A] time = 0.97, size = 54, normalized size = 0.79

$$\frac{2b^3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab} a^3} + \frac{2(15b^2x^2 + 5abx + 3a^2)}{15a^3x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x-a),x, algorithm="giac")

[Out] 2*b^3*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*a^3) + 2/15*(15*b^2*x^2 + 5*a*b*x + 3*a^2)/(a^3*x^(5/2))

maple [A] time = 0.01, size = 54, normalized size = 0.79

$$-\frac{2b^3 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a^3} + \frac{2b^2}{a^3\sqrt{x}} + \frac{2b}{3a^2x^{\frac{3}{2}}} + \frac{2}{5ax^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(7/2)/(b*x-a),x)

[Out] -2/a^3*b^3/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2))+2/5/a/x^(5/2)+2/a^3*b^2/x^(1/2)+2/3/a^2*b/x^(3/2)

maxima [A] time = 2.98, size = 68, normalized size = 1.00

$$\frac{b^3 \log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{\sqrt{ab} a^3} + \frac{2(15b^2x^2 + 5abx + 3a^2)}{15a^3x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x-a),x, algorithm="maxima")

[Out] b^3*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*a^3) + 2/15*(15*b^2*x^2 + 5*a*b*x + 3*a^2)/(a^3*x^(5/2))

mupad [B] time = 0.13, size = 48, normalized size = 0.71

$$\frac{\frac{2}{5a} + \frac{2b^2x^2}{a^3} + \frac{2bx}{3a^2}}{x^{5/2}} - \frac{2b^{5/2} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-1/(x^(7/2)*(a - b*x)),x)`

[Out] $(2/(5*a) + (2*b^2*x^2)/a^3 + (2*b*x)/(3*a^2))/x^{(5/2)} - (2*b^{(5/2)}*atanh((b^{(1/2)}*x^{(1/2)})/a^{(1/2)}))/a^{(7/2)}$

sympy [A] time = 24.44, size = 131, normalized size = 1.93

$$\left\{ \begin{array}{ll} \frac{\infty}{7} & \text{for } a = 0 \wedge b = 0 \\ x^2 & \\ -\frac{2}{7} & \text{for } a = 0 \\ 7bx^2 & \\ \frac{2}{5} & \text{for } b = 0 \\ 5ax^2 & \\ \frac{2}{5ax^2} + \frac{2b}{3a^2x^{\frac{3}{2}}} + \frac{2b^2}{a^3\sqrt{x}} + \frac{b^2 \log\left(-\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{7}{2}}\sqrt{\frac{1}{b}}} - \frac{b^2 \log\left(\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{a^{\frac{7}{2}}\sqrt{\frac{1}{b}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(7/2)/(b*x-a),x)`

[Out] `Piecewise((zoo/x**(7/2), Eq(a, 0) & Eq(b, 0)), (-2/(7*b*x**(7/2)), Eq(a, 0)), (2/(5*a*x**(5/2)), Eq(b, 0)), (2/(5*a*x**(5/2)) + 2*b/(3*a**2*x**(3/2)) + 2*b**2/(a**3*sqrt(x)) + b**2*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(7/2)*sqrt(1/b)) - b**2*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(a**(7/2)*sqrt(1/b)), True))`

$$3.476 \quad \int \frac{x^{5/2}}{(-a+bx)^2} dx$$

Optimal. Leaf size=70

$$-\frac{5a^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}} + \frac{5a\sqrt{x}}{b^3} + \frac{x^{5/2}}{b(a-bx)} + \frac{5x^{3/2}}{3b^2}$$

[Out] $5/3*x^{(3/2)}/b^2+x^{(5/2)}/b/(-b*x+a)-5*a^{(3/2)}*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/b^{(7/2)}+5*a*x^{(1/2)}/b^3$

Rubi [A] time = 0.02, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 63, 208}

$$-\frac{5a^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}} + \frac{5a\sqrt{x}}{b^3} + \frac{x^{5/2}}{b(a-bx)} + \frac{5x^{3/2}}{3b^2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(5/2)}/(-a + b*x)^2, x]$

[Out] $(5*a*\operatorname{Sqrt}[x])/b^3 + (5*x^{(3/2)})/(3*b^2) + x^{(5/2)}/(b*(a - b*x)) - (5*a^{(3/2)})*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a]]/b^{(7/2)}$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\}$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\}$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{NeQ}[m + n + 1, 0]$ && $!(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] \mid\mid (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m - n, 0])))$ && $!\operatorname{ILtQ}[m + n + 2, 0]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(-a + bx)^2} dx &= \frac{x^{5/2}}{b(a - bx)} + \frac{5 \int \frac{x^{3/2}}{-a + bx} dx}{2b} \\
&= \frac{5x^{3/2}}{3b^2} + \frac{x^{5/2}}{b(a - bx)} + \frac{(5a) \int \frac{\sqrt{x}}{-a + bx} dx}{2b^2} \\
&= \frac{5a\sqrt{x}}{b^3} + \frac{5x^{3/2}}{3b^2} + \frac{x^{5/2}}{b(a - bx)} + \frac{(5a^2) \int \frac{1}{\sqrt{x}(-a + bx)} dx}{2b^3} \\
&= \frac{5a\sqrt{x}}{b^3} + \frac{5x^{3/2}}{3b^2} + \frac{x^{5/2}}{b(a - bx)} + \frac{(5a^2) \text{Subst}\left(\int \frac{1}{-a + bx^2} dx, x, \sqrt{x}\right)}{b^3} \\
&= \frac{5a\sqrt{x}}{b^3} + \frac{5x^{3/2}}{3b^2} + \frac{x^{5/2}}{b(a - bx)} - \frac{5a^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 26, normalized size = 0.37

$$\frac{2x^{7/2} {}_2F_1\left(2, \frac{7}{2}; \frac{9}{2}; \frac{bx}{a}\right)}{7a^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(5/2)/(-a + b*x)^2, x]
```

```
[Out] (2*x^(7/2)*Hypergeometric2F1[2, 7/2, 9/2, (b*x)/a])/(7*a^2)
```

fricas [A] time = 0.48, size = 167, normalized size = 2.39

$$\left[\frac{15(abx - a^2)\sqrt{\frac{a}{b}} \log\left(\frac{bx - 2b\sqrt{x}\sqrt{\frac{a}{b}} + a}{bx - a}\right) + 2(2b^2x^2 + 10abx - 15a^2)\sqrt{x}}{6(b^4x - ab^3)}, \frac{15(abx - a^2)\sqrt{-\frac{a}{b}} \arctan\left(\frac{b\sqrt{x}\sqrt{-\frac{a}{b}}}{a}\right) + \dots}{3(b^4x - ab^3)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x-a)^2,x, algorithm="fricas")

[Out] [1/6*(15*(a*b*x - a^2)*sqrt(a/b)*log((b*x - 2*b*sqrt(x)*sqrt(a/b) + a)/(b*x - a)) + 2*(2*b^2*x^2 + 10*a*b*x - 15*a^2)*sqrt(x))/(b^4*x - a*b^3), 1/3*(15*(a*b*x - a^2)*sqrt(-a/b)*arctan(b*sqrt(x)*sqrt(-a/b)/a) + (2*b^2*x^2 + 10*a*b*x - 15*a^2)*sqrt(x))/(b^4*x - a*b^3)]

giac [A] time = 0.98, size = 69, normalized size = 0.99

$$\frac{5a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab}b^3} - \frac{a^2\sqrt{x}}{(bx-a)b^3} + \frac{2(b^4x^{\frac{3}{2}} + 6ab^3\sqrt{x})}{3b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x-a)^2,x, algorithm="giac")

[Out] 5*a^2*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*b^3) - a^2*sqrt(x)/((b*x - a)*b^3) + 2/3*(b^4*x^(3/2) + 6*a*b^3*sqrt(x))/b^6

maple [A] time = 0.01, size = 61, normalized size = 0.87

$$\frac{2\left(-\frac{5 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{2\sqrt{ab}} - \frac{\sqrt{x}}{2(bx-a)}\right)a^2}{b^3} + \frac{\frac{2bx^{\frac{3}{2}}}{3} + 4a\sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x-a)^2,x)

[Out] 2/b^3*(1/3*b*x^(3/2)+2*a*x^(1/2))+2/b^3*a^2*(-1/2*x^(1/2)/(b*x-a)-5/2/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2)))

maxima [A] time = 3.06, size = 81, normalized size = 1.16

$$-\frac{a^2\sqrt{x}}{b^4x - ab^3} + \frac{5a^2 \log\left(\frac{b\sqrt{x} - \sqrt{ab}}{b\sqrt{x} + \sqrt{ab}}\right)}{2\sqrt{ab}b^3} + \frac{2(bx^{\frac{3}{2}} + 6a\sqrt{x})}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x-a)^2,x, algorithm="maxima")

[Out] $-a^2\sqrt{x}/(b^4x - a*b^3) + 5/2*a^2*\log((b*\sqrt{x} - \sqrt{a*b})/(b*\sqrt{x} + \sqrt{a*b}))/(\sqrt{a*b}*b^3) + 2/3*(b*x^{(3/2)} + 6*a*\sqrt{x})/b^3$

mupad [B] time = 0.07, size = 61, normalized size = 0.87

$$\frac{2x^{3/2}}{3b^2} + \frac{4a\sqrt{x}}{b^3} + \frac{a^2\sqrt{x}}{ab^3 - b^4x} + \frac{a^{3/2} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) 5i}{b^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(a - b*x)^2,x)

[Out] $(2*x^{(3/2)})/(3*b^2) + (4*a*x^{(1/2)})/b^3 + (a^2*x^{(1/2)})/(a*b^3 - b^4*x) + (a^{(3/2)}*\operatorname{atan}((b^{(1/2)}*x^{(1/2)}*1i)/a^{(1/2)})*5i)/b^{(7/2)}$

sympy [A] time = 24.75, size = 444, normalized size = 6.34

$$\left\{ \begin{array}{l} \propto x^{\frac{3}{2}} \\ \frac{2x^{\frac{7}{2}}}{7a^2} \\ \frac{2x^{\frac{3}{2}}}{3b^2} \\ -\frac{30a^{\frac{5}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{-6a^{\frac{3}{2}}b^4\sqrt{\frac{1}{b}}+6\sqrt{a}b^5x\sqrt{\frac{1}{b}}} + \frac{20a^{\frac{3}{2}}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{-6a^{\frac{3}{2}}b^4\sqrt{\frac{1}{b}}+6\sqrt{a}b^5x\sqrt{\frac{1}{b}}} + \frac{4\sqrt{a}b^3x^{\frac{5}{2}}\sqrt{\frac{1}{b}}}{-6a^{\frac{3}{2}}b^4\sqrt{\frac{1}{b}}+6\sqrt{a}b^5x\sqrt{\frac{1}{b}}} - \frac{15a^3\log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-6a^{\frac{3}{2}}b^4\sqrt{\frac{1}{b}}+6\sqrt{a}b^5x\sqrt{\frac{1}{b}}} + \frac{15a^3\log\left(\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-6a^{\frac{3}{2}}b^4\sqrt{\frac{1}{b}}+6\sqrt{a}b^5x\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(b*x-a)**2,x)

[Out] Piecewise((zoo*x**(3/2), Eq(a, 0) & Eq(b, 0)), (2*x**(7/2)/(7*a**2), Eq(b, 0)), (2*x**(3/2)/(3*b**2), Eq(a, 0)), (-30*a**(5/2)*b*sqrt(x)*sqrt(1/b)/(-6*a**(3/2)*b**4*sqrt(1/b) + 6*sqrt(a)*b**5*x*sqrt(1/b)) + 20*a**(3/2)*b**2*x**(3/2)*sqrt(1/b)/(-6*a**(3/2)*b**4*sqrt(1/b) + 6*sqrt(a)*b**5*x*sqrt(1/b)) + 4*sqrt(a)*b**3*x**(5/2)*sqrt(1/b)/(-6*a**(3/2)*b**4*sqrt(1/b) + 6*sqrt(a)*b**5*x*sqrt(1/b)) - 15*a**3*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(-6*a**(3/2)*b**4*sqrt(1/b) + 6*sqrt(a)*b**5*x*sqrt(1/b)) + 15*a**3*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(-6*a**(3/2)*b**4*sqrt(1/b) + 6*sqrt(a)*b**5*x*sqrt(1/b)) + 15*a**2*b*x*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(-6*a**(3/2)*b**4*sqrt(1/b) + 6*sqrt(a)*b**5*x*sqrt(1/b)) - 15*a**2*b*x*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(-6*a**(3/2)*b**4*sqrt(1/b) + 6*sqrt(a)*b**5*x*sqrt(1/b)), True))

$$3.477 \quad \int \frac{x^{3/2}}{(-a+bx)^2} dx$$

Optimal. Leaf size=57

$$-\frac{3\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} + \frac{x^{3/2}}{b(a-bx)} + \frac{3\sqrt{x}}{b^2}$$

[Out] $x^{(3/2)}/b/(-b*x+a)-3*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})*a^{(1/2)}/b^{(5/2)}+3*x^{(1/2)}/b^2$

Rubi [A] time = 0.02, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 63, 208}

$$-\frac{3\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} + \frac{x^{3/2}}{b(a-bx)} + \frac{3\sqrt{x}}{b^2}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)/(-a + b*x)^2,x]

[Out] (3*Sqrt[x])/b^2 + x^(3/2)/(b*(a - b*x)) - (3*Sqrt[a]*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/b^(5/2)

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^(n), x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned} \int \frac{x^{3/2}}{(-a+bx)^2} dx &= \frac{x^{3/2}}{b(a-bx)} + \frac{3 \int \frac{\sqrt{x}}{-a+bx} dx}{2b} \\ &= \frac{3\sqrt{x}}{b^2} + \frac{x^{3/2}}{b(a-bx)} + \frac{(3a) \int \frac{1}{\sqrt{x}(-a+bx)} dx}{2b^2} \\ &= \frac{3\sqrt{x}}{b^2} + \frac{x^{3/2}}{b(a-bx)} + \frac{(3a) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{b^2} \\ &= \frac{3\sqrt{x}}{b^2} + \frac{x^{3/2}}{b(a-bx)} - \frac{3\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}} \end{aligned}$$

Mathematica [C] time = 0.00, size = 26, normalized size = 0.46

$$\frac{2x^{5/2} {}_2F_1\left(2, \frac{5}{2}; \frac{7}{2}; \frac{bx}{a}\right)}{5a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/(-a + b*x)^2, x]

[Out] (2*x^(5/2)*Hypergeometric2F1[2, 5/2, 7/2, (b*x)/a])/(5*a^2)

fricas [A] time = 0.46, size = 138, normalized size = 2.42

$$\left[\frac{3(bx-a)\sqrt{\frac{a}{b}} \log\left(\frac{bx-2b\sqrt{x}\sqrt{\frac{a}{b}}+a}{bx-a}\right) + 2(2bx-3a)\sqrt{x}}{2(b^3x-ab^2)}, \frac{3(bx-a)\sqrt{-\frac{a}{b}} \arctan\left(\frac{b\sqrt{x}\sqrt{\frac{a}{b}}}{a}\right) + (2bx-3a)\sqrt{x}}{b^3x-ab^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x-a)^2,x, algorithm="fricas")

[Out] [1/2*(3*(b*x - a)*sqrt(a/b)*log((b*x - 2*b*sqrt(x)*sqrt(a/b) + a)/(b*x - a) + 2*(2*b*x - 3*a)*sqrt(x))/(b^3*x - a*b^2), (3*(b*x - a)*sqrt(-a/b)*arctan(b*sqrt(x)*sqrt(-a/b)/a) + (2*b*x - 3*a)*sqrt(x))/(b^3*x - a*b^2)]

giac [A] time = 0.98, size = 51, normalized size = 0.89

$$\frac{3 a \arctan\left(\frac{b \sqrt{x}}{\sqrt{-a b}}\right)}{\sqrt{-a b} b^2} - \frac{a \sqrt{x}}{(b x - a) b^2} + \frac{2 \sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x-a)^2,x, algorithm="giac")

[Out] 3*a*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*b^2) - a*sqrt(x)/((b*x - a)*b^2) + 2*sqrt(x)/b^2

maple [A] time = 0.01, size = 49, normalized size = 0.86

$$\frac{2 \left(-\frac{3 \operatorname{arctanh}\left(\frac{b \sqrt{x}}{\sqrt{a b}}\right)}{2 \sqrt{a b}} - \frac{\sqrt{x}}{2(b x - a)} \right) a}{b^2} + \frac{2 \sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(b*x-a)^2,x)

[Out] 2/b^2*x^(1/2)+2*a/b^2*(-1/2/(b*x-a)*x^(1/2)-3/2/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2)))

maxima [A] time = 2.92, size = 68, normalized size = 1.19

$$-\frac{a \sqrt{x}}{b^3 x - a b^2} + \frac{3 a \log\left(\frac{b \sqrt{x} - \sqrt{a b}}{b \sqrt{x} + \sqrt{a b}}\right)}{2 \sqrt{a b} b^2} + \frac{2 \sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x-a)^2,x, algorithm="maxima")

[Out] -a*sqrt(x)/(b^3*x - a*b^2) + 3/2*a*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*b^2) + 2*sqrt(x)/b^2

mupad [B] time = 0.11, size = 47, normalized size = 0.82

$$\frac{2\sqrt{x}}{b^2} + \frac{a\sqrt{x}}{ab^2 - b^3x} - \frac{3\sqrt{a} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(a - b*x)^2,x)`

[Out] $(2x^{(1/2)})/b^2 + (a*x^{(1/2)})/(a*b^2 - b^3*x) - (3*a^{(1/2)}*atanh((b^{(1/2)}*x^{(1/2)})/a^{(1/2)}))/b^{(5/2)}$

sympy [A] time = 9.13, size = 381, normalized size = 6.68

$$\left\{ \begin{array}{l} \infty\sqrt{x} \\ \frac{2x^2}{5a^2} \\ \frac{2\sqrt{x}}{b^2} \\ -\frac{6a^{\frac{3}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{-2a^{\frac{3}{2}}b^3\sqrt{\frac{1}{b}}+2\sqrt{a}b^4x\sqrt{\frac{1}{b}}} + \frac{4\sqrt{a}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{-2a^{\frac{3}{2}}b^3\sqrt{\frac{1}{b}}+2\sqrt{a}b^4x\sqrt{\frac{1}{b}}} - \frac{3a^2\log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{3}{2}}b^3\sqrt{\frac{1}{b}}+2\sqrt{a}b^4x\sqrt{\frac{1}{b}}} + \frac{3a^2\log\left(\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{3}{2}}b^3\sqrt{\frac{1}{b}}+2\sqrt{a}b^4x\sqrt{\frac{1}{b}}} + \frac{3abx\log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{3}{2}}b^3\sqrt{\frac{1}{b}}+2\sqrt{a}b^4x\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(b*x-a)**2,x)`

[Out] `Piecewise((zoo*sqrt(x), Eq(a, 0) & Eq(b, 0)), (2*x**(5/2)/(5*a**2), Eq(b, 0)), (2*sqrt(x)/b**2, Eq(a, 0)), (-6*a**(3/2)*b*sqrt(x)*sqrt(1/b)/(-2*a**(3/2)*b**3*sqrt(1/b) + 2*sqrt(a)*b**4*x*sqrt(1/b)) + 4*sqrt(a)*b**2*x**(3/2)*sqrt(1/b)/(-2*a**(3/2)*b**3*sqrt(1/b) + 2*sqrt(a)*b**4*x*sqrt(1/b)) - 3*a**2*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(3/2)*b**3*sqrt(1/b) + 2*sqrt(a)*b**4*x*sqrt(1/b)) + 3*a**2*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(3/2)*b**3*sqrt(1/b) + 2*sqrt(a)*b**4*x*sqrt(1/b)) + 3*a*b*x*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(3/2)*b**3*sqrt(1/b) + 2*sqrt(a)*b**4*x*sqrt(1/b)) - 3*a*b*x*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(3/2)*b**3*sqrt(1/b) + 2*sqrt(a)*b**4*x*sqrt(1/b)), True))`

$$3.478 \quad \int \frac{\sqrt{x}}{(-a+bx)^2} dx$$

Optimal. Leaf size=47

$$\frac{\sqrt{x}}{b(a-bx)} - \frac{\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}b^{3/2}}$$

[Out] $-\operatorname{arctanh}(b^{(1/2)}x^{(1/2)}/a^{(1/2)})/b^{(3/2)}/a^{(1/2)}+x^{(1/2)}/b/(-b*x+a)$

Rubi [A] time = 0.01, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 63, 208}

$$\frac{\sqrt{x}}{b(a-bx)} - \frac{\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}b^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(-a + b*x)^2,x]

[Out] Sqrt[x]/(b*(a - b*x)) - ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]]/(Sqrt[a]*b^(3/2))

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{x}}{(-a+bx)^2} dx &= \frac{\sqrt{x}}{b(a-bx)} + \frac{\int \frac{1}{\sqrt{x}(-a+bx)} dx}{2b} \\ &= \frac{\sqrt{x}}{b(a-bx)} + \frac{\text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{b} \\ &= \frac{\sqrt{x}}{b(a-bx)} - \frac{\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}b^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.02, size = 61, normalized size = 1.30

$$\frac{\sqrt{a}\sqrt{b}\sqrt{x} + (bx-a)\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a}b^{3/2}(a-bx)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(-a + b*x)^2, x]

[Out] (Sqrt[a]*Sqrt[b]*Sqrt[x] + (-a + b*x)*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[a]*b^(3/2)*(a - b*x))

fricas [A] time = 0.45, size = 123, normalized size = 2.62

$$\left[-\frac{2ab\sqrt{x} - \sqrt{ab}(bx-a)\log\left(\frac{bx+a-2\sqrt{ab}\sqrt{x}}{bx-a}\right)}{2(ab^3x - a^2b^2)}, -\frac{ab\sqrt{x} - \sqrt{-ab}(bx-a)\arctan\left(\frac{\sqrt{-ab}}{b\sqrt{x}}\right)}{ab^3x - a^2b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x-a)^2, x, algorithm="fricas")

[Out] [-1/2*(2*a*b*sqrt(x) - sqrt(a*b)*(b*x - a)*log((b*x + a - 2*sqrt(a*b)*sqrt(x))/(b*x - a)))/(a*b^3*x - a^2*b^2), -(a*b*sqrt(x) - sqrt(-a*b)*(b*x - a)*arctan(sqrt(-a*b)/(b*sqrt(x))))/(a*b^3*x - a^2*b^2)]

giac [A] time = 1.06, size = 40, normalized size = 0.85

$$\frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab}b} - \frac{\sqrt{x}}{(bx-a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x-a)^2,x, algorithm="giac")

[Out] arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*b) - sqrt(x)/((b*x - a)*b)

maple [A] time = 0.01, size = 40, normalized size = 0.85

$$-\frac{\operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} b} - \frac{\sqrt{x}}{(bx - a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x-a)^2,x)

[Out] -1/b*x^(1/2)/(b*x-a)-1/b/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.99, size = 56, normalized size = 1.19

$$-\frac{\sqrt{x}}{b^2x - ab} + \frac{\log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{2\sqrt{ab} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x-a)^2,x, algorithm="maxima")

[Out] -sqrt(x)/(b^2*x - a*b) + 1/2*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*b)

mupad [B] time = 0.11, size = 35, normalized size = 0.74

$$\frac{\sqrt{x}}{b(a - bx)} - \frac{\operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{a} b^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(a - b*x)^2,x)

[Out] x^(1/2)/(b*(a - b*x)) - atanh((b^(1/2)*x^(1/2))/a^(1/2))/(a^(1/2)*b^(3/2))

sympy [A] time = 4.43, size = 311, normalized size = 6.62

$$\left\{ \begin{array}{l} \frac{\infty}{\sqrt{x}} \\ \frac{2x^{\frac{3}{2}}}{3a^2} \\ -\frac{2}{b^2\sqrt{x}} \\ -\frac{2\sqrt{a}b\sqrt{x}\sqrt{\frac{1}{b}}}{-2a^{\frac{3}{2}}b^2\sqrt{\frac{1}{b}}+2\sqrt{a}b^3x\sqrt{\frac{1}{b}}} - \frac{a\log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{3}{2}}b^2\sqrt{\frac{1}{b}}+2\sqrt{a}b^3x\sqrt{\frac{1}{b}}} + \frac{a\log\left(\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{3}{2}}b^2\sqrt{\frac{1}{b}}+2\sqrt{a}b^3x\sqrt{\frac{1}{b}}} + \frac{bx\log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{3}{2}}b^2\sqrt{\frac{1}{b}}+2\sqrt{a}b^3x\sqrt{\frac{1}{b}}} - \frac{bx\log\left(\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{3}{2}}b^2\sqrt{\frac{1}{b}}+2\sqrt{a}b^3x\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(1/2)/(b*x-a)**2,x)

[Out] Piecewise((zoo/sqrt(x), Eq(a, 0) & Eq(b, 0)), (2*x**(3/2)/(3*a**2), Eq(b, 0)), (-2/(b**2*sqrt(x)), Eq(a, 0)), (-2*sqrt(a)*b*sqrt(x)*sqrt(1/b)/(-2*a**(3/2)*b**2*sqrt(1/b) + 2*sqrt(a)*b**3*x*sqrt(1/b)) - a*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(3/2)*b**2*sqrt(1/b) + 2*sqrt(a)*b**3*x*sqrt(1/b)) + a*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(3/2)*b**2*sqrt(1/b) + 2*sqrt(a)*b**3*x*sqrt(1/b)) + b*x*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(3/2)*b**2*sqrt(1/b) + 2*sqrt(a)*b**3*x*sqrt(1/b)) - b*x*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(3/2)*b**2*sqrt(1/b) + 2*sqrt(a)*b**3*x*sqrt(1/b)), True))

$$3.479 \quad \int \frac{1}{\sqrt{x}(-a+bx)^2} dx$$

Optimal. Leaf size=46

$$\frac{\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}\sqrt{b}} + \frac{\sqrt{x}}{a(a-bx)}$$

[Out] arctanh(b^(1/2)*x^(1/2)/a^(1/2))/a^(3/2)/b^(1/2)+x^(1/2)/a/(-b*x+a)

Rubi [A] time = 0.01, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 208}

$$\frac{\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}\sqrt{b}} + \frac{\sqrt{x}}{a(a-bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(-a + b*x)^2),x]

[Out] Sqrt[x]/(a*(a - b*x)) + ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]]/(a^(3/2)*Sqrt[b])

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt{x}(-a+bx)^2} dx &= \frac{\sqrt{x}}{a(a-bx)} - \frac{\int \frac{1}{\sqrt{x}(-a+bx)} dx}{2a} \\
&= \frac{\sqrt{x}}{a(a-bx)} - \frac{\text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{a} \\
&= \frac{\sqrt{x}}{a(a-bx)} + \frac{\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}\sqrt{b}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 1.00

$$\frac{\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}\sqrt{b}} + \frac{\sqrt{x}}{a^2 - abx}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(-a + b*x)^2), x]

[Out] Sqrt[x]/(a^2 - a*b*x) + ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]]/(a^(3/2)*Sqrt[b])

fricas [A] time = 0.48, size = 122, normalized size = 2.65

$$\left[\frac{2ab\sqrt{x} - \sqrt{ab}(bx-a)\log\left(\frac{bx+a+2\sqrt{ab}\sqrt{x}}{bx-a}\right)}{2(a^2b^2x - a^3b)}, -\frac{ab\sqrt{x} + \sqrt{-ab}(bx-a)\arctan\left(\frac{\sqrt{-ab}}{b\sqrt{x}}\right)}{a^2b^2x - a^3b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-a)^2/x^(1/2), x, algorithm="fricas")

[Out] [-1/2*(2*a*b*sqrt(x) - sqrt(a*b)*(b*x - a)*log((b*x + a + 2*sqrt(a*b)*sqrt(x))/(b*x - a)))/(a^2*b^2*x - a^3*b), -(a*b*sqrt(x) + sqrt(-a*b)*(b*x - a)*arctan(sqrt(-a*b)/(b*sqrt(x))))/(a^2*b^2*x - a^3*b)]

giac [A] time = 0.88, size = 41, normalized size = 0.89

$$-\frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab}a} - \frac{\sqrt{x}}{(bx-a)a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-a)^2/x^(1/2),x, algorithm="giac")

[Out] $-\arctan(b\sqrt{x}/\sqrt{-a*b})/(\sqrt{-a*b}*a) - \sqrt{x}/((b*x - a)*a)$

maple [A] time = 0.01, size = 39, normalized size = 0.85

$$\frac{\operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{\sqrt{ab} a} - \frac{\sqrt{x}}{(bx - a) a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x-a)^2/x^(1/2),x)

[Out] $-x^{(1/2)}/a/(b*x-a)+1/a/(a*b)^{(1/2)}*\operatorname{arctanh}(1/(a*b)^{(1/2)}*b*x^{(1/2)})$

maxima [A] time = 2.97, size = 56, normalized size = 1.22

$$-\frac{\sqrt{x}}{abx - a^2} - \frac{\log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{2\sqrt{ab} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-a)^2/x^(1/2),x, algorithm="maxima")

[Out] $-\sqrt{x}/(a*b*x - a^2) - 1/2*\log((b*\sqrt{x} - \sqrt{a*b})/(b*\sqrt{x} + \sqrt{a*b}))/(\sqrt{a*b}*a)$

mupad [B] time = 0.05, size = 34, normalized size = 0.74

$$\frac{\sqrt{x}}{a(a - bx)} + \frac{\operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{3/2}\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/2)*(a - b*x)^2),x)

[Out] $x^{(1/2)}/(a*(a - b*x)) + \operatorname{atanh}((b^{(1/2)}*x^{(1/2)})/a^{(1/2)})/(a^{(3/2)}*b^{(1/2)})$

sympy [A] time = 7.41, size = 303, normalized size = 6.59

$$\left\{ \begin{array}{l} \frac{\infty}{3} \\ x^2 \\ \frac{2\sqrt{x}}{a^2} \\ -\frac{2}{3b^2x^2} \\ -\frac{2\sqrt{a}b\sqrt{x}\sqrt{\frac{1}{b}}}{-2a^{\frac{5}{2}}b\sqrt{\frac{1}{b}}+2a^{\frac{3}{2}}b^2x\sqrt{\frac{1}{b}}} + \frac{a\log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{5}{2}}b\sqrt{\frac{1}{b}}+2a^{\frac{3}{2}}b^2x\sqrt{\frac{1}{b}}} - \frac{a\log\left(\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{5}{2}}b\sqrt{\frac{1}{b}}+2a^{\frac{3}{2}}b^2x\sqrt{\frac{1}{b}}} - \frac{bx\log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{5}{2}}b\sqrt{\frac{1}{b}}+2a^{\frac{3}{2}}b^2x\sqrt{\frac{1}{b}}} + \frac{bx\log\left(\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{-2a^{\frac{5}{2}}b\sqrt{\frac{1}{b}}+2a^{\frac{3}{2}}b^2x\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-a)**2/x**(1/2),x)

[Out] Piecewise((zoo/x**(3/2), Eq(a, 0) & Eq(b, 0)), (2*sqrt(x)/a**2, Eq(b, 0)), (-2/(3*b**2*x**(3/2)), Eq(a, 0)), (-2*sqrt(a)*b*sqrt(x)*sqrt(1/b)/(-2*a**(5/2)*b*sqrt(1/b) + 2*a**(3/2)*b**2*x*sqrt(1/b)) + a*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(5/2)*b*sqrt(1/b) + 2*a**(3/2)*b**2*x*sqrt(1/b)) - a*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(5/2)*b*sqrt(1/b) + 2*a**(3/2)*b**2*x*sqrt(1/b)) - b*x*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(5/2)*b*sqrt(1/b) + 2*a**(3/2)*b**2*x*sqrt(1/b)) + b*x*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(-2*a**(5/2)*b*sqrt(1/b) + 2*a**(3/2)*b**2*x*sqrt(1/b)), True))

$$3.480 \quad \int \frac{1}{x^{3/2}(-a+bx)^2} dx$$

Optimal. Leaf size=57

$$\frac{3\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{3}{a^2\sqrt{x}} + \frac{1}{a\sqrt{x}(a-bx)}$$

[Out] $3*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})*b^{(1/2)}/a^{(5/2)}-3/a^2/x^{(1/2)}+1/a/(-b*x+a)/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 208}

$$\frac{3\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{3}{a^2\sqrt{x}} + \frac{1}{a\sqrt{x}(a-bx)}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/(x^{(3/2)}*(-a + b*x)^2), x]$

[Out] $-3/(a^2*\operatorname{Sqrt}[x]) + 1/(a*\operatorname{Sqrt}[x]*(a - b*x)) + (3*\operatorname{Sqrt}[b]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a]])/a^{(5/2)}$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)} / ((b*c - a*d)*(m + 1)), x] - \operatorname{Dist}[(d*(m + n + 2)) / ((b*c - a*d)*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x] /; \operatorname{FreeQ}\{a, b, c, d, n\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{LtQ}[n, -1] \&\& (\operatorname{EqQ}[a, 0] \mid\mid (\operatorname{NeQ}[c, 0] \&\& \operatorname{LtQ}[m - n, 0] \&\& \operatorname{IntegerQ}[n]))) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[p = \operatorname{Denominator}[m], \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /; \operatorname{FreeQ}\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{3/2}(-a+bx)^2} dx &= \frac{1}{a\sqrt{x}(a-bx)} - \frac{3 \int \frac{1}{x^{3/2}(-a+bx)} dx}{2a} \\
 &= -\frac{3}{a^2\sqrt{x}} + \frac{1}{a\sqrt{x}(a-bx)} - \frac{(3b) \int \frac{1}{\sqrt{x}(-a+bx)} dx}{2a^2} \\
 &= -\frac{3}{a^2\sqrt{x}} + \frac{1}{a\sqrt{x}(a-bx)} - \frac{(3b) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{a^2} \\
 &= -\frac{3}{a^2\sqrt{x}} + \frac{1}{a\sqrt{x}(a-bx)} + \frac{3\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 24, normalized size = 0.42

$$-\frac{{}_2F_1\left(-\frac{1}{2}, 2; \frac{1}{2}; \frac{bx}{a}\right)}{a^2\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(-a + b*x)^2), x]

[Out] (-2*Hypergeometric2F1[-1/2, 2, 1/2, (b*x)/a])/(a^2*Sqrt[x])

fricas [A] time = 0.46, size = 151, normalized size = 2.65

$$\left[\frac{3(bx^2 - ax)\sqrt{\frac{b}{a}} \log\left(\frac{bx+2a\sqrt{x}\sqrt{\frac{b}{a}}+a}{bx-a}\right) - 2(3bx - 2a)\sqrt{x}}{2(a^2bx^2 - a^3x)}, -\frac{3(bx^2 - ax)\sqrt{-\frac{b}{a}} \arctan\left(\frac{a\sqrt{-\frac{b}{a}}}{b\sqrt{x}}\right) + (3bx - 2a)\sqrt{x}}{a^2bx^2 - a^3x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x-a)^2,x, algorithm="fricas")

[Out] $\left[\frac{1}{2} \cdot (3 \cdot (b \cdot x^2 - a \cdot x) \cdot \sqrt{b/a}) \cdot \log((b \cdot x + 2 \cdot a \cdot \sqrt{x}) \cdot \sqrt{b/a} + a) / (b \cdot x - a) - 2 \cdot (3 \cdot b \cdot x - 2 \cdot a) \cdot \sqrt{x} / (a^2 \cdot b \cdot x^2 - a^3 \cdot x), - (3 \cdot (b \cdot x^2 - a \cdot x) \cdot \sqrt{-b/a}) \cdot \arctan(a \cdot \sqrt{-b/a} / (b \cdot \sqrt{x})) + (3 \cdot b \cdot x - 2 \cdot a) \cdot \sqrt{x} / (a^2 \cdot b \cdot x^2 - a^3 \cdot x) \right]$

giac [A] time = 1.01, size = 52, normalized size = 0.91

$$-\frac{3 b \arctan\left(\frac{b \sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab} a^2} - \frac{3 b x - 2 a}{\left(b x^{\frac{3}{2}} - a \sqrt{x}\right) a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(b*x-a)^2,x, algorithm="giac")`

[Out] $-3 \cdot b \cdot \arctan(b \cdot \sqrt{x} / \sqrt{-a \cdot b}) / (\sqrt{-a \cdot b} \cdot a^2) - (3 \cdot b \cdot x - 2 \cdot a) / ((b \cdot x^{3/2} - a \cdot \sqrt{x}) \cdot a^2)$

maple [A] time = 0.01, size = 49, normalized size = 0.86

$$-\frac{2 \left(-\frac{3 \operatorname{arctanh}\left(\frac{b \sqrt{x}}{\sqrt{ab}}\right)}{2 \sqrt{ab}} + \frac{\sqrt{x}}{2 b x - 2 a} \right) b}{a^2} - \frac{2}{a^2 \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(3/2)/(b*x-a)^2,x)`

[Out] $-2/a^2 \cdot b \cdot (1/2 / (b \cdot x - a) \cdot x^{1/2} - 3/2 / (a \cdot b)^{1/2} \cdot \operatorname{arctanh}(1/(a \cdot b)^{1/2}) \cdot b \cdot x^{1/2}) - 2/a^2 \cdot x^{1/2}$

maxima [A] time = 3.00, size = 69, normalized size = 1.21

$$-\frac{3 b x - 2 a}{a^2 b x^{\frac{3}{2}} - a^3 \sqrt{x}} - \frac{3 b \log\left(\frac{b \sqrt{x} - \sqrt{ab}}{b \sqrt{x} + \sqrt{ab}}\right)}{2 \sqrt{ab} a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(b*x-a)^2,x, algorithm="maxima")`

[Out] $-(3 \cdot b \cdot x - 2 \cdot a) / (a^2 \cdot b \cdot x^{3/2} - a^3 \cdot \sqrt{x}) - 3/2 \cdot b \cdot \log((b \cdot \sqrt{x} - \sqrt{a \cdot b}) / (b \cdot \sqrt{x} + \sqrt{a \cdot b})) / (\sqrt{a \cdot b} \cdot a^2)$

mupad [B] time = 0.07, size = 49, normalized size = 0.86

$$\frac{3\sqrt{b} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{5/2}} - \frac{\frac{2}{a} - \frac{3bx}{a^2}}{a\sqrt{x} - bx^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(a - b*x)^2), x)`

[Out] $(3*b^{(1/2)*\operatorname{atanh}((b^{(1/2)*x^{(1/2)}})/a^{(1/2)}))/a^{(5/2)} - (2/a - (3*b*x)/a^2)/(a*x^{(1/2)} - b*x^{(3/2)})$

sympy [A] time = 17.54, size = 403, normalized size = 7.07

$$\left\{ \begin{array}{l} \frac{\infty}{x^2} \\ -\frac{2}{a^2\sqrt{x}} \\ -\frac{2}{5b^2x^2} \\ -\frac{4a^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{2a^{\frac{7}{2}}\sqrt{x}\sqrt{\frac{1}{b}}-2a^{\frac{5}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}}} + \frac{6\sqrt{a}bx\sqrt{\frac{1}{b}}}{2a^{\frac{7}{2}}\sqrt{x}\sqrt{\frac{1}{b}}-2a^{\frac{5}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}}} - \frac{3a\sqrt{x}\log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2a^{\frac{7}{2}}\sqrt{x}\sqrt{\frac{1}{b}}-2a^{\frac{5}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}}} + \frac{3a\sqrt{x}\log\left(\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2a^{\frac{7}{2}}\sqrt{x}\sqrt{\frac{1}{b}}-2a^{\frac{5}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}}} + \frac{3bx^{\frac{3}{2}}\log\left(-\sqrt{a}\sqrt{\frac{1}{b}}+\sqrt{x}\right)}{2a^{\frac{7}{2}}\sqrt{x}\sqrt{\frac{1}{b}}-2a^{\frac{5}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(b*x-a)**2, x)`

[Out] `Piecewise((zoo/x**(5/2), Eq(a, 0) & Eq(b, 0)), (-2/(a**2*sqrt(x)), Eq(b, 0)), (-2/(5*b**2*x**(5/2)), Eq(a, 0)), (-4*a**(3/2)*sqrt(1/b)/(2*a**(7/2)*sqrt(x)*sqrt(1/b) - 2*a**(5/2)*b*x**(3/2)*sqrt(1/b)) + 6*sqrt(a)*b*x*sqrt(1/b)/(2*a**(7/2)*sqrt(x)*sqrt(1/b) - 2*a**(5/2)*b*x**(3/2)*sqrt(1/b)) - 3*a*sqrt(x)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(2*a**(7/2)*sqrt(x)*sqrt(1/b) - 2*a**(5/2)*b*x**(3/2)*sqrt(1/b)) + 3*a*sqrt(x)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(2*a**(7/2)*sqrt(x)*sqrt(1/b) - 2*a**(5/2)*b*x**(3/2)*sqrt(1/b)) + 3*b*x**(3/2)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(2*a**(7/2)*sqrt(x)*sqrt(1/b) - 2*a**(5/2)*b*x**(3/2)*sqrt(1/b)) - 3*b*x**(3/2)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(2*a**(7/2)*sqrt(x)*sqrt(1/b) - 2*a**(5/2)*b*x**(3/2)*sqrt(1/b)), True))`

$$3.481 \quad \int \frac{1}{x^{5/2}(-a+bx)^2} dx$$

Optimal. Leaf size=70

$$\frac{5b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}} - \frac{5b}{a^3\sqrt{x}} - \frac{5}{3a^2x^{3/2}} + \frac{1}{ax^{3/2}(a-bx)}$$

[Out] $-5/3/a^2/x^{(3/2)}+1/a/x^{(3/2)}/(-b*x+a)+5*b^{(3/2)}*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/a^{(7/2)}-5*b/a^3/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 208}

$$\frac{5b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}} - \frac{5b}{a^3\sqrt{x}} - \frac{5}{3a^2x^{3/2}} + \frac{1}{ax^{3/2}(a-bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(-a + b*x)^2), x]

[Out] $-5/(3*a^2*x^{(3/2)}) - (5*b)/(a^3*\operatorname{Sqrt}[x]) + 1/(a*x^{(3/2)}*(a - b*x)) + (5*b^{(3/2)}*\operatorname{ArcTanh}[\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x)]/\operatorname{Sqrt}[a])/a^{(7/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{5/2}(-a+bx)^2} dx &= \frac{1}{ax^{3/2}(a-bx)} - \frac{5 \int \frac{1}{x^{5/2}(-a+bx)} dx}{2a} \\
 &= -\frac{5}{3a^2x^{3/2}} + \frac{1}{ax^{3/2}(a-bx)} - \frac{(5b) \int \frac{1}{x^{3/2}(-a+bx)} dx}{2a^2} \\
 &= -\frac{5}{3a^2x^{3/2}} - \frac{5b}{a^3\sqrt{x}} + \frac{1}{ax^{3/2}(a-bx)} - \frac{(5b^2) \int \frac{1}{\sqrt{x}(-a+bx)} dx}{2a^3} \\
 &= -\frac{5}{3a^2x^{3/2}} - \frac{5b}{a^3\sqrt{x}} + \frac{1}{ax^{3/2}(a-bx)} - \frac{(5b^2) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{a^3} \\
 &= -\frac{5}{3a^2x^{3/2}} - \frac{5b}{a^3\sqrt{x}} + \frac{1}{ax^{3/2}(a-bx)} + \frac{5b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 26, normalized size = 0.37

$$-\frac{{}_2F_1\left(-\frac{3}{2}, 2; -\frac{1}{2}; \frac{bx}{a}\right)}{3a^2x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(-a + b*x)^2), x]

[Out] (-2*Hypergeometric2F1[-3/2, 2, -1/2, (b*x)/a])/(3*a^2*x^(3/2))

fricas [A] time = 0.45, size = 187, normalized size = 2.67

$$\left[\frac{15(b^2x^3 - abx^2)\sqrt{\frac{b}{a}} \log\left(\frac{bx+2a\sqrt{x}\sqrt{\frac{b}{a}}+a}{bx-a}\right) - 2(15b^2x^2 - 10abx - 2a^2)\sqrt{x}}{6(a^3bx^3 - a^4x^2)}, -\frac{15(b^2x^3 - abx^2)\sqrt{-\frac{b}{a}} \arctan\left(\frac{a\sqrt{-\frac{b}{a}}}{b\sqrt{x}}\right)}{3(a^3bx^3 - a^4x^2)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x-a)^2,x, algorithm="fricas")

[Out] [1/6*(15*(b^2*x^3 - a*b*x^2)*sqrt(b/a)*log((b*x + 2*a*sqrt(x)*sqrt(b/a) + a)/(b*x - a)) - 2*(15*b^2*x^2 - 10*a*b*x - 2*a^2)*sqrt(x))/(a^3*b*x^3 - a^4*x^2), -1/3*(15*(b^2*x^3 - a*b*x^2)*sqrt(-b/a)*arctan(a*sqrt(-b/a)/(b*sqrt(x)))) + (15*b^2*x^2 - 10*a*b*x - 2*a^2)*sqrt(x))/(a^3*b*x^3 - a^4*x^2)]

giac [A] time = 0.93, size = 61, normalized size = 0.87

$$-\frac{5b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{\sqrt{-ab}a^3} - \frac{b^2\sqrt{x}}{(bx-a)a^3} - \frac{2(6bx+a)}{3a^3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x-a)^2,x, algorithm="giac")

[Out] -5*b^2*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*a^3) - b^2*sqrt(x)/((b*x - a)*a^3) - 2/3*(6*b*x + a)/(a^3*x^(3/2))

maple [A] time = 0.02, size = 60, normalized size = 0.86

$$-\frac{2\left(-\frac{5 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{2\sqrt{ab}} + \frac{\sqrt{x}}{2bx-2a}\right)b^2}{a^3} - \frac{4b}{a^3\sqrt{x}} - \frac{2}{3a^2x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(5/2)/(b*x-a)^2,x)

[Out] -2/a^3*b^2*(1/2/(b*x-a)*x^(1/2)-5/2/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2)))-2/3/a^2/x^(3/2)-4/a^3*b/x^(1/2)

maxima [A] time = 3.00, size = 82, normalized size = 1.17

$$-\frac{15b^2x^2 - 10abx - 2a^2}{3\left(a^3bx^{\frac{5}{2}} - a^4x^{\frac{3}{2}}\right)} - \frac{5b^2 \log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{2\sqrt{ab}a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x-a)^2,x, algorithm="maxima")

[Out] -1/3*(15*b^2*x^2 - 10*a*b*x - 2*a^2)/(a^3*b*x^(5/2) - a^4*x^(3/2)) - 5/2*b^2*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*a^3)

mupad [B] time = 0.14, size = 60, normalized size = 0.86

$$\frac{5b^{3/2} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{a^{7/2}} - \frac{\frac{2}{3a} - \frac{5b^2x^2}{a^3} + \frac{10bx}{3a^2}}{ax^{3/2} - bx^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/2)*(a - b*x)^2), x)`

[Out] $(5*b^{3/2}*\operatorname{atanh}((b^{1/2}*x^{1/2})/a^{1/2}))/a^{7/2} - (2/(3*a) - (5*b^2*x^2)/a^3 + (10*b*x)/(3*a^2))/(a*x^{3/2} - b*x^{5/2})$

sympy [A] time = 50.25, size = 471, normalized size = 6.73

$$\left\{ \begin{array}{l} \frac{\infty}{7} \\ x^2 \\ -\frac{2}{7b^2x^2} \\ -\frac{2}{3a^2x^2} \\ -\frac{4a^{\frac{5}{2}}\sqrt{\frac{1}{b}}}{6a^{\frac{9}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} - 6a^{\frac{7}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}}} - \frac{20a^{\frac{3}{2}}bx\sqrt{\frac{1}{b}}}{6a^{\frac{9}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} - 6a^{\frac{7}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}}} + \frac{30\sqrt{a}b^2x^2\sqrt{\frac{1}{b}}}{6a^{\frac{9}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} - 6a^{\frac{7}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}}} - \frac{15abx^{\frac{3}{2}}\log\left(-\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{6a^{\frac{9}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} - 6a^{\frac{7}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}}} + \frac{15abx^{\frac{3}{2}}\log\left(\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{6a^{\frac{9}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} - 6a^{\frac{7}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(b*x-a)**2, x)`

[Out] `Piecewise((zoo/x**(7/2), Eq(a, 0) & Eq(b, 0)), (-2/(7*b**2*x**(7/2)), Eq(a, 0)), (-2/(3*a**2*x**(3/2)), Eq(b, 0)), (-4*a**(5/2)*sqrt(1/b)/(6*a**(9/2)*x**(3/2)*sqrt(1/b) - 6*a**(7/2)*b*x**(5/2)*sqrt(1/b)) - 20*a**(3/2)*b*x*sqrt(1/b)/(6*a**(9/2)*x**(3/2)*sqrt(1/b) - 6*a**(7/2)*b*x**(5/2)*sqrt(1/b)) + 30*sqrt(a)*b**2*x**2*sqrt(1/b)/(6*a**(9/2)*x**(3/2)*sqrt(1/b) - 6*a**(7/2)*b*x**(5/2)*sqrt(1/b)) - 15*a*b*x**(3/2)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(6*a**(9/2)*x**(3/2)*sqrt(1/b) - 6*a**(7/2)*b*x**(5/2)*sqrt(1/b)) + 15*a*b*x**(3/2)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(6*a**(9/2)*x**(3/2)*sqrt(1/b) - 6*a**(7/2)*b*x**(5/2)*sqrt(1/b)) + 15*b**2*x**(5/2)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(6*a**(9/2)*x**(3/2)*sqrt(1/b) - 6*a**(7/2)*b*x**(5/2)*sqrt(1/b)) - 15*b**2*x**(5/2)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(6*a**(9/2)*x**(3/2)*sqrt(1/b) - 6*a**(7/2)*b*x**(5/2)*sqrt(1/b)), True))`

$$3.482 \quad \int \frac{x^{7/2}}{(-a+bx)^3} dx$$

Optimal. Leaf size=97

$$-\frac{35a^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{9/2}} + \frac{35a\sqrt{x}}{4b^4} + \frac{7x^{5/2}}{4b^2(a-bx)} - \frac{x^{7/2}}{2b(a-bx)^2} + \frac{35x^{3/2}}{12b^3}$$

[Out] 35/12*x^(3/2)/b^3-1/2*x^(7/2)/b/(-b*x+a)^2+7/4*x^(5/2)/b^2/(-b*x+a)-35/4*a^(3/2)*arctanh(b^(1/2)*x^(1/2)/a^(1/2))/b^(9/2)+35/4*a*x^(1/2)/b^4

Rubi [A] time = 0.03, antiderivative size = 97, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 63, 208}

$$-\frac{35a^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{9/2}} + \frac{7x^{5/2}}{4b^2(a-bx)} + \frac{35a\sqrt{x}}{4b^4} - \frac{x^{7/2}}{2b(a-bx)^2} + \frac{35x^{3/2}}{12b^3}$$

Antiderivative was successfully verified.

[In] Int[x^(7/2)/(-a + b*x)^3,x]

[Out] (35*a*Sqrt[x])/(4*b^4) + (35*x^(3/2))/(12*b^3) - x^(7/2)/(2*b*(a - b*x)^2) + (7*x^(5/2))/(4*b^2*(a - b*x)) - (35*a^(3/2)*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(4*b^(9/2))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{7/2}}{(-a+bx)^3} dx &= -\frac{x^{7/2}}{2b(a-bx)^2} + \frac{7 \int \frac{x^{5/2}}{(-a+bx)^2} dx}{4b} \\
&= -\frac{x^{7/2}}{2b(a-bx)^2} + \frac{7x^{5/2}}{4b^2(a-bx)} + \frac{35 \int \frac{x^{3/2}}{-a+bx} dx}{8b^2} \\
&= \frac{35x^{3/2}}{12b^3} - \frac{x^{7/2}}{2b(a-bx)^2} + \frac{7x^{5/2}}{4b^2(a-bx)} + \frac{(35a) \int \frac{\sqrt{x}}{-a+bx} dx}{8b^3} \\
&= \frac{35a\sqrt{x}}{4b^4} + \frac{35x^{3/2}}{12b^3} - \frac{x^{7/2}}{2b(a-bx)^2} + \frac{7x^{5/2}}{4b^2(a-bx)} + \frac{(35a^2) \int \frac{1}{\sqrt{x}(-a+bx)} dx}{8b^4} \\
&= \frac{35a\sqrt{x}}{4b^4} + \frac{35x^{3/2}}{12b^3} - \frac{x^{7/2}}{2b(a-bx)^2} + \frac{7x^{5/2}}{4b^2(a-bx)} + \frac{(35a^2) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{4b^4} \\
&= \frac{35a\sqrt{x}}{4b^4} + \frac{35x^{3/2}}{12b^3} - \frac{x^{7/2}}{2b(a-bx)^2} + \frac{7x^{5/2}}{4b^2(a-bx)} - \frac{35a^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{9/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 26, normalized size = 0.27

$$-\frac{2x^{9/2} {}_2F_1\left(3, \frac{9}{2}; \frac{11}{2}; \frac{bx}{a}\right)}{9a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(7/2)/(-a + b*x)^3, x]

[Out] $(-2*x^{(9/2)}*Hypergeometric2F1[3, 9/2, 11/2, (b*x)/a])/(9*a^3)$

fricas [A] time = 0.46, size = 227, normalized size = 2.34

$$\left[\frac{105 (ab^2x^2 - 2a^2bx + a^3) \sqrt{\frac{a}{b}} \log\left(\frac{bx - 2b\sqrt{x} \sqrt{\frac{a}{b}} + a}{bx - a}\right) + 2(8b^3x^3 + 56ab^2x^2 - 175a^2bx + 105a^3) \sqrt{x}}{24(b^6x^2 - 2ab^5x + a^2b^4)}, \frac{105(ab^2x^2 - 2a^2bx + a^3) \sqrt{\frac{a}{b}} \log\left(\frac{bx - 2b\sqrt{x} \sqrt{\frac{a}{b}} + a}{bx - a}\right) + 2(8b^3x^3 + 56ab^2x^2 - 175a^2bx + 105a^3) \sqrt{x}}{24(b^6x^2 - 2ab^5x + a^2b^4)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(7/2)/(b*x-a)^3,x, algorithm="fricas")`

[Out] $[1/24*(105*(a*b^2*x^2 - 2*a^2*b*x + a^3)*\sqrt{a/b}*\log((b*x - 2*b*\sqrt{x})*\sqrt{a/b} + a)/(b*x - a)) + 2*(8*b^3*x^3 + 56*a*b^2*x^2 - 175*a^2*b*x + 105*a^3)*\sqrt{x})/(b^6*x^2 - 2*a*b^5*x + a^2*b^4), 1/12*(105*(a*b^2*x^2 - 2*a^2*b*x + a^3)*\sqrt{-a/b}*\arctan(b*\sqrt{x}*\sqrt{-a/b}/a) + (8*b^3*x^3 + 56*a*b^2*x^2 - 175*a^2*b*x + 105*a^3)*\sqrt{x})/(b^6*x^2 - 2*a*b^5*x + a^2*b^4)]$

giac [A] time = 1.03, size = 81, normalized size = 0.84

$$\frac{35a^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{4\sqrt{-ab}b^4} - \frac{13a^2bx^{\frac{3}{2}} - 11a^3\sqrt{x}}{4(bx - a)^2b^4} + \frac{2(b^6x^{\frac{3}{2}} + 9ab^5\sqrt{x})}{3b^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(7/2)/(b*x-a)^3,x, algorithm="giac")`

[Out] $35/4*a^2*\arctan(b*\sqrt{x}/\sqrt{-a*b})/(\sqrt{-a*b}*b^4) - 1/4*(13*a^2*b*x^{(3/2)} - 11*a^3*\sqrt{x})/((b*x - a)^2*b^4) + 2/3*(b^6*x^{(3/2)} + 9*a*b^5*\sqrt{x})/b^9$

maple [A] time = 0.02, size = 70, normalized size = 0.72

$$\frac{2\left(-\frac{35 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{8\sqrt{ab}} + \frac{-\frac{13bx^{\frac{3}{2}}}{8} + \frac{11a\sqrt{x}}{8}}{(bx-a)^2}\right)a^2}{b^4} + \frac{\frac{2bx^{\frac{3}{2}}}{3} + 6a\sqrt{x}}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(7/2)/(b*x-a)^3,x)`

[Out] $2/b^4*(1/3*b*x^{(3/2)}+3*a*x^{(1/2)})+2/b^4*a^2*((-13/8*b*x^{(3/2)}+11/8*a*x^{(1/2)})/(b*x-a)^2-35/8/(a*b)^{(1/2)}*\operatorname{arctanh}(1/(a*b)^{(1/2)}*b*x^{(1/2)}))$

maxima [A] time = 2.99, size = 103, normalized size = 1.06

$$-\frac{13a^2bx^{\frac{3}{2}} - 11a^3\sqrt{x}}{4(b^6x^2 - 2ab^5x + a^2b^4)} + \frac{35a^2 \log\left(\frac{b\sqrt{x} - \sqrt{ab}}{b\sqrt{x} + \sqrt{ab}}\right)}{8\sqrt{ab}b^4} + \frac{2(bx^{\frac{3}{2}} + 9a\sqrt{x})}{3b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(7/2)/(b*x-a)^3,x, algorithm="maxima")

[Out] -1/4*(13*a^2*b*x^(3/2) - 11*a^3*sqrt(x))/(b^6*x^2 - 2*a*b^5*x + a^2*b^4) + 35/8*a^2*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*b^4) + 2/3*(b*x^(3/2) + 9*a*sqrt(x))/b^4

mupad [B] time = 0.14, size = 83, normalized size = 0.86

$$\frac{\frac{11a^3\sqrt{x}}{4} - \frac{13a^2bx^{3/2}}{4}}{a^2b^4 - 2ab^5x + b^6x^2} + \frac{2x^{3/2}}{3b^3} + \frac{6a\sqrt{x}}{b^4} + \frac{a^{3/2} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{9/2}} 35i$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-x^(7/2)/(a - b*x)^3,x)

[Out] ((11*a^3*x^(1/2))/4 - (13*a^2*b*x^(3/2))/4)/(a^2*b^4 + b^6*x^2 - 2*a*b^5*x) + (2*x^(3/2))/(3*b^3) + (6*a*x^(1/2))/b^4 + (a^(3/2)*atan((b^(1/2)*x^(1/2))*1i)/a^(1/2))*35i)/(4*b^(9/2))

sympy [A] time = 136.15, size = 840, normalized size = 8.66

$$\left\{ \begin{array}{l} \infty x^{\frac{3}{2}} \\ \frac{2x^{\frac{9}{2}}}{9a^3} \\ \frac{2x^{\frac{3}{2}}}{3b^3} \\ \frac{210a^{\frac{7}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{24a^{\frac{5}{2}}b^5\sqrt{\frac{1}{b}} - 48a^{\frac{3}{2}}b^6x\sqrt{\frac{1}{b}} + 24\sqrt{a}b^7x^2\sqrt{\frac{1}{b}}} - \frac{350a^{\frac{5}{2}}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{24a^{\frac{5}{2}}b^5\sqrt{\frac{1}{b}} - 48a^{\frac{3}{2}}b^6x\sqrt{\frac{1}{b}} + 24\sqrt{a}b^7x^2\sqrt{\frac{1}{b}}} + \frac{112a^{\frac{3}{2}}b^3x^{\frac{5}{2}}\sqrt{\frac{1}{b}}}{24a^{\frac{5}{2}}b^5\sqrt{\frac{1}{b}} - 48a^{\frac{3}{2}}b^6x\sqrt{\frac{1}{b}} + 24\sqrt{a}b^7x^2\sqrt{\frac{1}{b}}} + \frac{5}{24a^{\frac{5}{2}}b} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(7/2)/(b*x-a)**3,x)

[Out] Piecewise((zoo*x**(3/2), Eq(a, 0) & Eq(b, 0)), (-2*x**(9/2)/(9*a**3), Eq(b, 0)), (2*x**(3/2)/(3*b**3), Eq(a, 0)), (210*a**(7/2)*b*sqrt(x)*sqrt(1/b)/(2

```

4*a**(5/2)*b**5*sqrt(1/b) - 48*a**(3/2)*b**6*x*sqrt(1/b) + 24*sqrt(a)*b**7*
x**2*sqrt(1/b)) - 350*a**(5/2)*b**2*x**(3/2)*sqrt(1/b)/(24*a**(5/2)*b**5*sq
rt(1/b) - 48*a**(3/2)*b**6*x*sqrt(1/b) + 24*sqrt(a)*b**7*x**2*sqrt(1/b)) +
112*a**(3/2)*b**3*x**(5/2)*sqrt(1/b)/(24*a**(5/2)*b**5*sqrt(1/b) - 48*a**(3
/2)*b**6*x*sqrt(1/b) + 24*sqrt(a)*b**7*x**2*sqrt(1/b)) + 16*sqrt(a)*b**4*x*
*(7/2)*sqrt(1/b)/(24*a**(5/2)*b**5*sqrt(1/b) - 48*a**(3/2)*b**6*x*sqrt(1/b)
+ 24*sqrt(a)*b**7*x**2*sqrt(1/b)) + 105*a**4*log(-sqrt(a)*sqrt(1/b) + sqrt
(x))/(24*a**(5/2)*b**5*sqrt(1/b) - 48*a**(3/2)*b**6*x*sqrt(1/b) + 24*sqrt(a
)*b**7*x**2*sqrt(1/b)) - 105*a**4*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(24*a**(
5/2)*b**5*sqrt(1/b) - 48*a**(3/2)*b**6*x*sqrt(1/b) + 24*sqrt(a)*b**7*x**2*s
qrt(1/b)) - 210*a**3*b*x*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(24*a**(5/2)*b**
5*sqrt(1/b) - 48*a**(3/2)*b**6*x*sqrt(1/b) + 24*sqrt(a)*b**7*x**2*sqrt(1/b)
) + 210*a**3*b*x*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(24*a**(5/2)*b**5*sqrt(1/
b) - 48*a**(3/2)*b**6*x*sqrt(1/b) + 24*sqrt(a)*b**7*x**2*sqrt(1/b)) + 105*a
**2*b**2*x**2*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(24*a**(5/2)*b**5*sqrt(1/b)
- 48*a**(3/2)*b**6*x*sqrt(1/b) + 24*sqrt(a)*b**7*x**2*sqrt(1/b)) - 105*a**
2*b**2*x**2*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(24*a**(5/2)*b**5*sqrt(1/b) -
48*a**(3/2)*b**6*x*sqrt(1/b) + 24*sqrt(a)*b**7*x**2*sqrt(1/b)), True))

```

$$3.483 \quad \int \frac{x^{5/2}}{(-a+bx)^3} dx$$

Optimal. Leaf size=84

$$-\frac{15\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{7/2}} + \frac{5x^{3/2}}{4b^2(a-bx)} - \frac{x^{5/2}}{2b(a-bx)^2} + \frac{15\sqrt{x}}{4b^3}$$

[Out] $-1/2*x^{(5/2)}/b/(-b*x+a)^2+5/4*x^{(3/2)}/b^2/(-b*x+a)-15/4*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})*a^{(1/2)}/b^{(7/2)}+15/4*x^{(1/2)}/b^3$

Rubi [A] time = 0.03, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 63, 208}

$$\frac{5x^{3/2}}{4b^2(a-bx)} - \frac{15\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{7/2}} - \frac{x^{5/2}}{2b(a-bx)^2} + \frac{15\sqrt{x}}{4b^3}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)/(-a + b*x)^3,x]

[Out] $(15*\operatorname{Sqrt}[x])/(4*b^3) - x^{(5/2)}/(2*b*(a - b*x)^2) + (5*x^{(3/2)})/(4*b^2*(a - b*x)) - (15*\operatorname{Sqrt}[a]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a]])/(4*b^{(7/2)})$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63


```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(-a+bx)^3} dx &= -\frac{x^{5/2}}{2b(a-bx)^2} + \frac{5 \int \frac{x^{3/2}}{(-a+bx)^2} dx}{4b} \\
&= -\frac{x^{5/2}}{2b(a-bx)^2} + \frac{5x^{3/2}}{4b^2(a-bx)} + \frac{15 \int \frac{\sqrt{x}}{-a+bx} dx}{8b^2} \\
&= \frac{15\sqrt{x}}{4b^3} - \frac{x^{5/2}}{2b(a-bx)^2} + \frac{5x^{3/2}}{4b^2(a-bx)} + \frac{(15a) \int \frac{1}{\sqrt{x}(-a+bx)} dx}{8b^3} \\
&= \frac{15\sqrt{x}}{4b^3} - \frac{x^{5/2}}{2b(a-bx)^2} + \frac{5x^{3/2}}{4b^2(a-bx)} + \frac{(15a) \operatorname{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{4b^3} \\
&= \frac{15\sqrt{x}}{4b^3} - \frac{x^{5/2}}{2b(a-bx)^2} + \frac{5x^{3/2}}{4b^2(a-bx)} - \frac{15\sqrt{a} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 26, normalized size = 0.31

$$-\frac{2x^{7/2} {}_2F_1\left(3, \frac{7}{2}; \frac{9}{2}; \frac{bx}{a}\right)}{7a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/(-a + b*x)^3,x]

[Out] (-2*x^(7/2)*Hypergeometric2F1[3, 7/2, 9/2, (b*x)/a])/(7*a^3)

fricas [A] time = 0.48, size = 199, normalized size = 2.37

$$\left[\frac{15 (b^2 x^2 - 2 abx + a^2) \sqrt{\frac{a}{b}} \log\left(\frac{bx - 2b\sqrt{x}\sqrt{\frac{a}{b}} + a}{bx - a}\right) + 2 (8b^2 x^2 - 25 abx + 15a^2) \sqrt{x}}{8 (b^5 x^2 - 2 ab^4 x + a^2 b^3)}, \frac{15 (b^2 x^2 - 2 abx + a^2) \sqrt{-\frac{a}{b}} \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{4 (b^5 x^2 - 2 ab^4 x + a^2 b^3)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x-a)^3,x, algorithm="fricas")

[Out] [1/8*(15*(b^2*x^2 - 2*a*b*x + a^2)*sqrt(a/b)*log((b*x - 2*b*sqrt(x)*sqrt(a/b) + a)/(b*x - a)) + 2*(8*b^2*x^2 - 25*a*b*x + 15*a^2)*sqrt(x))/(b^5*x^2 - 2*a*b^4*x + a^2*b^3), 1/4*(15*(b^2*x^2 - 2*a*b*x + a^2)*sqrt(-a/b)*arctan(b*sqrt(x)*sqrt(-a/b)/a) + (8*b^2*x^2 - 25*a*b*x + 15*a^2)*sqrt(x))/(b^5*x^2 - 2*a*b^4*x + a^2*b^3)]

giac [A] time = 0.95, size = 63, normalized size = 0.75

$$\frac{15 a \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{4 \sqrt{-ab} b^3} + \frac{2 \sqrt{x}}{b^3} - \frac{9 abx^{\frac{3}{2}} - 7 a^2 \sqrt{x}}{4 (bx - a)^2 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x-a)^3,x, algorithm="giac")

[Out] 15/4*a*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*b^3) + 2*sqrt(x)/b^3 - 1/4*(9*a*b*x^(3/2) - 7*a^2*sqrt(x))/((b*x - a)^2*b^3)

maple [A] time = 0.01, size = 58, normalized size = 0.69

$$\frac{2 \left(-\frac{15 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{8 \sqrt{ab}} + \frac{-\frac{9bx^{\frac{3}{2}}}{8} + \frac{7a\sqrt{x}}{8}}{(bx-a)^2} \right) a}{b^3} + \frac{2\sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x-a)^3,x)

[Out] 2/b^3*x^(1/2)+2/b^3*a*((-9/8*b*x^(3/2)+7/8*a*x^(1/2))/(b*x-a)^2-15/8/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2)))

maxima [A] time = 3.00, size = 90, normalized size = 1.07

$$-\frac{9abx^{\frac{3}{2}} - 7a^2\sqrt{x}}{4(b^5x^2 - 2ab^4x + a^2b^3)} + \frac{15a \log\left(\frac{b\sqrt{x} - \sqrt{ab}}{b\sqrt{x} + \sqrt{ab}}\right)}{8\sqrt{ab}b^3} + \frac{2\sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x-a)^3,x, algorithm="maxima")

[Out] -1/4*(9*a*b*x^(3/2) - 7*a^2*sqrt(x))/(b^5*x^2 - 2*a*b^4*x + a^2*b^3) + 15/8*a*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*b^3) + 2*sqrt(x)/b^3

mupad [B] time = 0.06, size = 69, normalized size = 0.82

$$\frac{\frac{7a^2\sqrt{x}}{4} - \frac{9abx^{3/2}}{4}}{a^2b^3 - 2ab^4x + b^5x^2} + \frac{2\sqrt{x}}{b^3} - \frac{15\sqrt{a} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-x^(5/2)/(a - b*x)^3,x)

[Out] ((7*a^2*x^(1/2))/4 - (9*a*b*x^(3/2))/4)/(a^2*b^3 + b^5*x^2 - 2*a*b^4*x) + (2*x^(1/2))/b^3 - (15*a^(1/2)*atanh((b^(1/2)*x^(1/2))/a^(1/2)))/(4*b^(7/2))

sympy [A] time = 53.45, size = 756, normalized size = 9.00

$$\left\{ \begin{array}{l} \infty\sqrt{x} \\ \frac{2\sqrt{x}}{b^3} \\ -\frac{2x^{\frac{7}{2}}}{7a^3} \\ \frac{30a^{\frac{5}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{8a^{\frac{5}{2}}b^4\sqrt{\frac{1}{b}} - 16a^{\frac{3}{2}}b^5x\sqrt{\frac{1}{b}} + 8\sqrt{a}b^6x^2\sqrt{\frac{1}{b}}} - \frac{50a^{\frac{3}{2}}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{8a^{\frac{5}{2}}b^4\sqrt{\frac{1}{b}} - 16a^{\frac{3}{2}}b^5x\sqrt{\frac{1}{b}} + 8\sqrt{a}b^6x^2\sqrt{\frac{1}{b}}} + \frac{16\sqrt{a}b^3x^{\frac{5}{2}}\sqrt{\frac{1}{b}}}{8a^{\frac{5}{2}}b^4\sqrt{\frac{1}{b}} - 16a^{\frac{3}{2}}b^5x\sqrt{\frac{1}{b}} + 8\sqrt{a}b^6x^2\sqrt{\frac{1}{b}}} + \frac{15a^{\frac{5}{2}}}{8a^{\frac{5}{2}}b^4\sqrt{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(b*x-a)**3,x)

[Out] Piecewise((zoo*sqrt(x), Eq(a, 0) & Eq(b, 0)), (2*sqrt(x)/b**3, Eq(a, 0)), (-2*x**(7/2)/(7*a**3), Eq(b, 0)), (30*a**(5/2)*b*sqrt(x)*sqrt(1/b)/(8*a**(5/2)

```

2)*b**4*sqrt(1/b) - 16*a**(3/2)*b**5*x*sqrt(1/b) + 8*sqrt(a)*b**6*x**2*sqrt
(1/b)) - 50*a**(3/2)*b**2*x**(3/2)*sqrt(1/b)/(8*a**(5/2)*b**4*sqrt(1/b) - 1
6*a**(3/2)*b**5*x*sqrt(1/b) + 8*sqrt(a)*b**6*x**2*sqrt(1/b)) + 16*sqrt(a)*b
**3*x**(5/2)*sqrt(1/b)/(8*a**(5/2)*b**4*sqrt(1/b) - 16*a**(3/2)*b**5*x*sqrt
(1/b) + 8*sqrt(a)*b**6*x**2*sqrt(1/b)) + 15*a**3*log(-sqrt(a)*sqrt(1/b) + s
qrt(x))/(8*a**(5/2)*b**4*sqrt(1/b) - 16*a**(3/2)*b**5*x*sqrt(1/b) + 8*sqrt(
a)*b**6*x**2*sqrt(1/b)) - 15*a**3*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5
/2)*b**4*sqrt(1/b) - 16*a**(3/2)*b**5*x*sqrt(1/b) + 8*sqrt(a)*b**6*x**2*sqr
t(1/b)) - 30*a**2*b*x*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5/2)*b**4*sq
rt(1/b) - 16*a**(3/2)*b**5*x*sqrt(1/b) + 8*sqrt(a)*b**6*x**2*sqrt(1/b)) + 3
0*a**2*b*x*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5/2)*b**4*sqrt(1/b) - 16
*a**(3/2)*b**5*x*sqrt(1/b) + 8*sqrt(a)*b**6*x**2*sqrt(1/b)) + 15*a*b**2*x**
2*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5/2)*b**4*sqrt(1/b) - 16*a**(3/2
)*b**5*x*sqrt(1/b) + 8*sqrt(a)*b**6*x**2*sqrt(1/b)) - 15*a*b**2*x**2*log(sq
rt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5/2)*b**4*sqrt(1/b) - 16*a**(3/2)*b**5*x*
sqrt(1/b) + 8*sqrt(a)*b**6*x**2*sqrt(1/b)), True))

```

$$3.484 \quad \int \frac{x^{3/2}}{(-a+bx)^3} dx$$

Optimal. Leaf size=72

$$-\frac{3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{a}b^{5/2}} + \frac{3\sqrt{x}}{4b^2(a-bx)} - \frac{x^{3/2}}{2b(a-bx)^2}$$

[Out] $-1/2*x^{(3/2)}/b/(-b*x+a)^2-3/4*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/b^{(5/2)}/a^{(1/2)}+3/4*x^{(1/2)}/b^2/(-b*x+a)$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 63, 208}

$$\frac{3\sqrt{x}}{4b^2(a-bx)} - \frac{3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{a}b^{5/2}} - \frac{x^{3/2}}{2b(a-bx)^2}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)/(-a + b*x)^3, x]

[Out] $-x^{(3/2)}/(2*b*(a-b*x)^2) + (3*\operatorname{Sqrt}[x])/(4*b^2*(a-b*x)) - (3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a]])/(4*\operatorname{Sqrt}[a]*b^{(5/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{x^{3/2}}{(-a+bx)^3} dx &= -\frac{x^{3/2}}{2b(a-bx)^2} + \frac{3 \int \frac{\sqrt{x}}{(-a+bx)^2} dx}{4b} \\
 &= -\frac{x^{3/2}}{2b(a-bx)^2} + \frac{3\sqrt{x}}{4b^2(a-bx)} + \frac{3 \int \frac{1}{\sqrt{x}(-a+bx)} dx}{8b^2} \\
 &= -\frac{x^{3/2}}{2b(a-bx)^2} + \frac{3\sqrt{x}}{4b^2(a-bx)} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{4b^2} \\
 &= -\frac{x^{3/2}}{2b(a-bx)^2} + \frac{3\sqrt{x}}{4b^2(a-bx)} - \frac{3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{a}b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.04, size = 60, normalized size = 0.83

$$\frac{\sqrt{x}(3a-5bx)}{4b^2(a-bx)^2} - \frac{3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{a}b^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/(-a + b*x)^3, x]

[Out] (Sqrt[x]*(3*a - 5*b*x))/(4*b^2*(a - b*x)^2) - (3*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(4*Sqrt[a]*b^(5/2))

fricas [A] time = 0.45, size = 186, normalized size = 2.58

$$\left[\frac{3(b^2x^2 - 2abx + a^2)\sqrt{ab} \log\left(\frac{bx+a-2\sqrt{ab}\sqrt{x}}{bx-a}\right) - 2(5ab^2x - 3a^2b)\sqrt{x}}{8(ab^5x^2 - 2a^2b^4x + a^3b^3)}, \frac{3(b^2x^2 - 2abx + a^2)\sqrt{-ab} \arctan\left(\frac{\sqrt{-ab}}{b\sqrt{x}}\right)}{4(ab^5x^2 - 2a^2b^4x + a^3b^3)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x-a)^3,x, algorithm="fricas")

[Out] [1/8*(3*(b^2*x^2 - 2*a*b*x + a^2)*sqrt(a*b)*log((b*x + a - 2*sqrt(a*b)*sqrt(x))/(b*x - a)) - 2*(5*a*b^2*x - 3*a^2*b)*sqrt(x))/(a*b^5*x^2 - 2*a^2*b^4*x

+ a³b³), 1/4*(3*(b²*x² - 2*a*b*x + a²)*sqrt(-a*b)*arctan(sqrt(-a*b)/(b*sqrt(x))) - (5*a*b²*x - 3*a²*b)*sqrt(x))/(a*b⁵*x² - 2*a²*b⁴*x + a³*b³)]

giac [A] time = 0.92, size = 51, normalized size = 0.71

$$\frac{3 \operatorname{arctan}\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{4\sqrt{-ab}b^2} - \frac{5bx^{\frac{3}{2}} - 3a\sqrt{x}}{4(bx-a)^2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x-a)^3,x, algorithm="giac")

[Out] 3/4*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*b²) - 1/4*(5*b*x^(3/2) - 3*a*sqrt(x))/((b*x - a)^2*b²)

maple [A] time = 0.01, size = 52, normalized size = 0.72

$$-\frac{3 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}b^2} + \frac{-\frac{5x^{\frac{3}{2}}}{4b} + \frac{3a\sqrt{x}}{4b^2}}{(bx-a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(b*x-a)^3,x)

[Out] 2*(-5/8/b*x^(3/2)+3/8*a/b^2*x^(1/2))/(b*x-a)^2-3/4/b^2/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.99, size = 78, normalized size = 1.08

$$-\frac{5bx^{\frac{3}{2}} - 3a\sqrt{x}}{4(b^4x^2 - 2ab^3x + a^2b^2)} + \frac{3 \log\left(\frac{b\sqrt{x} - \sqrt{ab}}{b\sqrt{x} + \sqrt{ab}}\right)}{8\sqrt{ab}b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x-a)^3,x, algorithm="maxima")

[Out] -1/4*(5*b*x^(3/2) - 3*a*sqrt(x))/(b^4*x^2 - 2*a*b^3*x + a^2*b^2) + 3/8*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*b^2)

mupad [B] time = 0.14, size = 58, normalized size = 0.81

$$-\frac{\frac{5x^{3/2}}{4b} - \frac{3a\sqrt{x}}{4b^2}}{a^2 - 2abx + b^2x^2} - \frac{3 \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{a}b^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-x^(3/2)/(a - b*x)^3,x)`

[Out] $-\left(\frac{5x^{3/2}}{4b} - \frac{3ax^{1/2}}{4b^2}\right)/(a^2 + b^2x^2 - 2abx) - \left(3\operatorname{atanh}\left(\frac{b^{1/2}x^{1/2}}{a^{1/2}}\right)\right)/(4a^{1/2}b^{5/2})$

sympy [A] time = 29.25, size = 673, normalized size = 9.35

$$\left\{ \begin{array}{l} \frac{\infty}{\sqrt{x}} \\ \frac{2x^2}{5a^3} \\ \frac{2}{b^3\sqrt{x}} \end{array} \right. \left[\frac{6a^{\frac{3}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{8a^{\frac{5}{2}}b^3\sqrt{\frac{1}{b}} - 16a^{\frac{3}{2}}b^4x\sqrt{\frac{1}{b}} + 8\sqrt{a}b^5x^2\sqrt{\frac{1}{b}}} - \frac{10\sqrt{a}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{8a^{\frac{5}{2}}b^3\sqrt{\frac{1}{b}} - 16a^{\frac{3}{2}}b^4x\sqrt{\frac{1}{b}} + 8\sqrt{a}b^5x^2\sqrt{\frac{1}{b}}} + \frac{3a^2\log\left(-\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{8a^{\frac{5}{2}}b^3\sqrt{\frac{1}{b}} - 16a^{\frac{3}{2}}b^4x\sqrt{\frac{1}{b}} + 8\sqrt{a}b^5x^2\sqrt{\frac{1}{b}}} - \frac{3a^2\log\left(\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{8a^{\frac{5}{2}}b^3\sqrt{\frac{1}{b}} - 16a^{\frac{3}{2}}b^4x\sqrt{\frac{1}{b}} + 8\sqrt{a}b^5x^2\sqrt{\frac{1}{b}}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(b*x-a)**3,x)`

[Out] `Piecewise((zoo/sqrt(x), Eq(a, 0) & Eq(b, 0)), (-2*x**(5/2)/(5*a**3), Eq(b, 0)), (-2/(b**3*sqrt(x)), Eq(a, 0)), (6*a**(3/2)*b*sqrt(x)*sqrt(1/b)/(8*a**(5/2)*b**3*sqrt(1/b) - 16*a**(3/2)*b**4*x*sqrt(1/b) + 8*sqrt(a)*b**5*x**2*sqrt(1/b)) - 10*sqrt(a)*b**2*x**(3/2)*sqrt(1/b)/(8*a**(5/2)*b**3*sqrt(1/b) - 16*a**(3/2)*b**4*x*sqrt(1/b) + 8*sqrt(a)*b**5*x**2*sqrt(1/b)) + 3*a**2*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5/2)*b**3*sqrt(1/b) - 16*a**(3/2)*b**4*x*sqrt(1/b) + 8*sqrt(a)*b**5*x**2*sqrt(1/b)) - 3*a**2*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5/2)*b**3*sqrt(1/b) - 16*a**(3/2)*b**4*x*sqrt(1/b) + 8*sqrt(a)*b**5*x**2*sqrt(1/b)) - 6*a*b*x*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5/2)*b**3*sqrt(1/b) - 16*a**(3/2)*b**4*x*sqrt(1/b) + 8*sqrt(a)*b**5*x**2*sqrt(1/b)) + 6*a*b*x*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5/2)*b**3*sqrt(1/b) - 16*a**(3/2)*b**4*x*sqrt(1/b) + 8*sqrt(a)*b**5*x**2*sqrt(1/b)) + 3*b**2*x**2*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5/2)*b**3*sqrt(1/b) - 16*a**(3/2)*b**4*x*sqrt(1/b) + 8*sqrt(a)*b**5*x**2*sqrt(1/b)) - 3*b**2*x**2*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(5/2)*b**3*sqrt(1/b) - 16*a**(3/2)*b**4*x*sqrt(1/b) + 8*sqrt(a)*b**5*x**2*sqrt(1/b)), True))`

$$3.485 \quad \int \frac{\sqrt{x}}{(-a+bx)^3} dx$$

Optimal. Leaf size=75

$$\frac{\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{3/2}b^{3/2}} + \frac{\sqrt{x}}{4ab(a-bx)} - \frac{\sqrt{x}}{2b(a-bx)^2}$$

[Out] 1/4*arctanh(b^(1/2)*x^(1/2)/a^(1/2))/a^(3/2)/b^(3/2)-1/2*x^(1/2)/b/(-b*x+a)
^2+1/4*x^(1/2)/a/b/(-b*x+a)

Rubi [A] time = 0.02, antiderivative size = 75, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 51, 63, 208}

$$\frac{\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{3/2}b^{3/2}} + \frac{\sqrt{x}}{4ab(a-bx)} - \frac{\sqrt{x}}{2b(a-bx)^2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(-a + b*x)^3,x]

[Out] -Sqrt[x]/(2*b*(a - b*x)^2) + Sqrt[x]/(4*a*b*(a - b*x)) + ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]]/(4*a^(3/2)*b^(3/2))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{x}}{(-a+bx)^3} dx &= -\frac{\sqrt{x}}{2b(a-bx)^2} + \frac{\int \frac{1}{\sqrt{x}(-a+bx)^2} dx}{4b} \\ &= -\frac{\sqrt{x}}{2b(a-bx)^2} + \frac{\sqrt{x}}{4ab(a-bx)} - \frac{\int \frac{1}{\sqrt{x}(-a+bx)} dx}{8ab} \\ &= -\frac{\sqrt{x}}{2b(a-bx)^2} + \frac{\sqrt{x}}{4ab(a-bx)} - \frac{\text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{4ab} \\ &= -\frac{\sqrt{x}}{2b(a-bx)^2} + \frac{\sqrt{x}}{4ab(a-bx)} + \frac{\tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{3/2}b^{3/2}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 26, normalized size = 0.35

$$-\frac{2x^{3/2} {}_2F_1\left(\frac{3}{2}, 3; \frac{5}{2}; \frac{bx}{a}\right)}{3a^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[x]/(-a + b*x)^3, x]
```

```
[Out] (-2*x^(3/2)*Hypergeometric2F1[3/2, 3, 5/2, (b*x)/a])/(3*a^3)
```

fricas [A] time = 0.45, size = 183, normalized size = 2.44

$$\left[\frac{(b^2x^2 - 2abx + a^2)\sqrt{ab} \log\left(\frac{bx+a+2\sqrt{ab}\sqrt{x}}{bx-a}\right) - 2(ab^2x + a^2b)\sqrt{x}}{8(a^2b^4x^2 - 2a^3b^3x + a^4b^2)}, -\frac{(b^2x^2 - 2abx + a^2)\sqrt{-ab} \arctan\left(\frac{\sqrt{-ab}}{b\sqrt{x}}\right) + (a^2b^2x + a^3b)}{4(a^2b^4x^2 - 2a^3b^3x + a^4b^2)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x-a)^3,x, algorithm="fricas")

[Out] [1/8*((b^2*x^2 - 2*a*b*x + a^2)*sqrt(a*b)*log((b*x + a + 2*sqrt(a*b)*sqrt(x))/(b*x - a)) - 2*(a*b^2*x + a^2*b)*sqrt(x))/(a^2*b^4*x^2 - 2*a^3*b^3*x + a^4*b^2), -1/4*((b^2*x^2 - 2*a*b*x + a^2)*sqrt(-a*b)*arctan(sqrt(-a*b)/(b*sqrt(x))) + (a*b^2*x + a^2*b)*sqrt(x))/(a^2*b^4*x^2 - 2*a^3*b^3*x + a^4*b^2)]

giac [A] time = 0.93, size = 55, normalized size = 0.73

$$-\frac{\arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{4\sqrt{-ab}ab} - \frac{bx^{\frac{3}{2}} + a\sqrt{x}}{4(bx-a)^2ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x-a)^3,x, algorithm="giac")

[Out] -1/4*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*a*b) - 1/4*(b*x^(3/2) + a*sqrt(x))/((b*x - a)^2*a*b)

maple [A] time = 0.01, size = 54, normalized size = 0.72

$$\frac{\operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{4\sqrt{ab}ab} + \frac{-\frac{x^{\frac{3}{2}}}{4a} - \frac{\sqrt{x}}{4b}}{(bx-a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x-a)^3,x)

[Out] 2*(-1/8/a*x^(3/2)-1/8/b*x^(1/2))/(b*x-a)^2+1/4/b/a/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2))

maxima [A] time = 2.85, size = 80, normalized size = 1.07

$$-\frac{bx^{\frac{3}{2}} + a\sqrt{x}}{4(ab^3x^2 - 2a^2b^2x + a^3b)} - \frac{\log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{8\sqrt{ab}ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x-a)^3,x, algorithm="maxima")

[Out] -1/4*(b*x^(3/2) + a*sqrt(x))/(a*b^3*x^2 - 2*a^2*b^2*x + a^3*b) - 1/8*log((b*sqrt(x) - sqrt(a*b))/(b*sqrt(x) + sqrt(a*b)))/(sqrt(a*b)*a*b)

mupad [B] time = 0.14, size = 57, normalized size = 0.76

$$\frac{\operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{3/2}b^{3/2}} - \frac{\frac{x^{3/2}}{4a} + \frac{\sqrt{x}}{4b}}{a^2 - 2abx + b^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-x^(1/2)/(a - b*x)^3,x)`

[Out] `atanh((b^(1/2)*x^(1/2))/a^(1/2))/(4*a^(3/2)*b^(3/2)) - (x^(3/2)/(4*a) + x^(1/2)/(4*b))/(a^2 + b^2*x^2 - 2*a*b*x)`

sympy [A] time = 15.19, size = 668, normalized size = 8.91

$$\left\{ \begin{array}{l} \frac{\infty}{x^2} \\ \frac{2x^2}{3a^3} \\ \frac{2}{3b^3x^2} \end{array} \right\} - \frac{2a^{\frac{3}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{8a^{\frac{7}{2}}b^2\sqrt{\frac{1}{b}} - 16a^{\frac{5}{2}}b^3x\sqrt{\frac{1}{b}} + 8a^{\frac{3}{2}}b^4x^2\sqrt{\frac{1}{b}}} - \frac{2\sqrt{a}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{8a^{\frac{7}{2}}b^2\sqrt{\frac{1}{b}} - 16a^{\frac{5}{2}}b^3x\sqrt{\frac{1}{b}} + 8a^{\frac{3}{2}}b^4x^2\sqrt{\frac{1}{b}}} - \frac{a^2 \log\left(-\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{8a^{\frac{7}{2}}b^2\sqrt{\frac{1}{b}} - 16a^{\frac{5}{2}}b^3x\sqrt{\frac{1}{b}} + 8a^{\frac{3}{2}}b^4x^2\sqrt{\frac{1}{b}}} + \frac{a^2 \log\left(-\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{8a^{\frac{7}{2}}b^2\sqrt{\frac{1}{b}} - 16a^{\frac{5}{2}}b^3x\sqrt{\frac{1}{b}} + 8a^{\frac{3}{2}}b^4x^2\sqrt{\frac{1}{b}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)/(b*x-a)**3,x)`

[Out] `Piecewise((zoo/x**(3/2), Eq(a, 0) & Eq(b, 0)), (-2*x**(3/2)/(3*a**3), Eq(b, 0)), (-2/(3*b**3*x**(3/2)), Eq(a, 0)), (-2*a**(3/2)*b*sqrt(x)*sqrt(1/b)/(8*a**(7/2)*b**2*sqrt(1/b) - 16*a**(5/2)*b**3*x*sqrt(1/b) + 8*a**(3/2)*b**4*x**2*sqrt(1/b)) - 2*sqrt(a)*b**2*x**(3/2)*sqrt(1/b)/(8*a**(7/2)*b**2*sqrt(1/b) - 16*a**(5/2)*b**3*x*sqrt(1/b) + 8*a**(3/2)*b**4*x**2*sqrt(1/b)) - a**2*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(7/2)*b**2*sqrt(1/b) - 16*a**(5/2)*b**3*x*sqrt(1/b) + 8*a**(3/2)*b**4*x**2*sqrt(1/b)) + a**2*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(7/2)*b**2*sqrt(1/b) - 16*a**(5/2)*b**3*x*sqrt(1/b) + 8*a**(3/2)*b**4*x**2*sqrt(1/b)) + 2*a*b*x*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(7/2)*b**2*sqrt(1/b) - 16*a**(5/2)*b**3*x*sqrt(1/b) + 8*a**(3/2)*b**4*x**2*sqrt(1/b)) - 2*a*b*x*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(7/2)*b**2*sqrt(1/b) - 16*a**(5/2)*b**3*x*sqrt(1/b) + 8*a**(3/2)*b**4*x**2*sqrt(1/b)) - b**2*x**2*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(7/2)*b**2*sqrt(1/b) - 16*a**(5/2)*b**3*x*sqrt(1/b) + 8*a**(3/2)*b**4*x**2*sqrt(1/b)) + b**2*x**2*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(7/2)*b**2*sqrt(1/b) - 16*a**(5/2)*b**3*x*sqrt(1/b) + 8*a**(3/2)*b**4*x**2*sqrt(1/b)), True))`

$$3.486 \quad \int \frac{1}{\sqrt{x}(-a+bx)^3} dx$$

Optimal. Leaf size=72

$$-\frac{3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{5/2}\sqrt{b}} - \frac{3\sqrt{x}}{4a^2(a-bx)} - \frac{\sqrt{x}}{2a(a-bx)^2}$$

[Out] $-3/4*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})/a^{(5/2)}/b^{(1/2)}-1/2*x^{(1/2)}/a/(-b*x+a)^2-3/4*x^{(1/2)}/a^2/(-b*x+a)$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 208}

$$-\frac{3\sqrt{x}}{4a^2(a-bx)} - \frac{3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{5/2}\sqrt{b}} - \frac{\sqrt{x}}{2a(a-bx)^2}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(-a + b*x)^3), x]

[Out] $-\operatorname{Sqrt}[x]/(2*a*(a-b*x)^2) - (3*\operatorname{Sqrt}[x])/(4*a^2*(a-b*x)) - (3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a]])/(4*a^{(5/2)}*\operatorname{Sqrt}[b])$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{\sqrt{x}(-a+bx)^3} dx &= -\frac{\sqrt{x}}{2a(a-bx)^2} - \frac{3 \int \frac{1}{\sqrt{x}(-a+bx)^2} dx}{4a} \\
 &= -\frac{\sqrt{x}}{2a(a-bx)^2} - \frac{3\sqrt{x}}{4a^2(a-bx)} + \frac{3 \int \frac{1}{\sqrt{x}(-a+bx)} dx}{8a^2} \\
 &= -\frac{\sqrt{x}}{2a(a-bx)^2} - \frac{3\sqrt{x}}{4a^2(a-bx)} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{4a^2} \\
 &= -\frac{\sqrt{x}}{2a(a-bx)^2} - \frac{3\sqrt{x}}{4a^2(a-bx)} - \frac{3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{5/2}\sqrt{b}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 24, normalized size = 0.33

$$-\frac{2\sqrt{x} {}_2F_1\left(\frac{1}{2}, 3; \frac{3}{2}; \frac{bx}{a}\right)}{a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(-a + b*x)^3), x]

[Out] (-2*Sqrt[x]*Hypergeometric2F1[1/2, 3, 3/2, (b*x)/a])/a^3

fricas [A] time = 0.45, size = 185, normalized size = 2.57

$$\left[\frac{3(b^2x^2 - 2abx + a^2)\sqrt{ab} \log\left(\frac{bx+a-2\sqrt{ab}\sqrt{x}}{bx-a}\right) + 2(3ab^2x - 5a^2b)\sqrt{x}}{8(a^3b^3x^2 - 2a^4b^2x + a^5b)}, \frac{3(b^2x^2 - 2abx + a^2)\sqrt{-ab} \arctan\left(\frac{\sqrt{-ab}}{b\sqrt{x}}\right)}{4(a^3b^3x^2 - 2a^4b^2x + a^5b)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-a)^3/x^(1/2), x, algorithm="fricas")

[Out] [1/8*(3*(b^2*x^2 - 2*a*b*x + a^2)*sqrt(a*b)*log((b*x + a - 2*sqrt(a*b)*sqrt(x))/(b*x - a)) + 2*(3*a*b^2*x - 5*a^2*b)*sqrt(x))/(a^3*b^3*x^2 - 2*a^4*b^2*x + a^5*b), 1/4*(3*(b^2*x^2 - 2*a*b*x + a^2)*sqrt(-a*b)*arctan(sqrt(-a*b)/

$(b\sqrt{x})) + (3ab^2x - 5a^2b)\sqrt{x}/(a^3b^3x^2 - 2a^4b^2x + a^5b)]$

giac [A] time = 1.15, size = 51, normalized size = 0.71

$$\frac{3 \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{4\sqrt{-ab}a^2} + \frac{3bx^{\frac{3}{2}} - 5a\sqrt{x}}{4(bx-a)^2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-a)^3/x^(1/2),x, algorithm="giac")

[Out] $3/4*\arctan(b*\sqrt{x}/\sqrt{-a*b})/(\sqrt{-a*b}*a^2) + 1/4*(3*b*x^{(3/2)} - 5*a*\sqrt{x})/((b*x - a)^2*a^2)$

maple [A] time = 0.01, size = 63, normalized size = 0.88

$$-\frac{\sqrt{x}}{2(bx-a)^2a} - \frac{3\left(\frac{\operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{2\sqrt{ab}a} - \frac{\sqrt{x}}{2(bx-a)a}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x-a)^3/x^(1/2),x)

[Out] $-1/2*x^{(1/2)}/a/(b*x-a)^2-3/2/a*(-1/2/(b*x-a)/a*x^{(1/2)}+1/2/a/(a*b)^{(1/2)*\arctanh(1/(a*b)^{(1/2)*b*x^{(1/2)})})$

maxima [A] time = 2.88, size = 77, normalized size = 1.07

$$\frac{3bx^{\frac{3}{2}} - 5a\sqrt{x}}{4(a^2b^2x^2 - 2a^3bx + a^4)} + \frac{3 \log\left(\frac{b\sqrt{x} - \sqrt{ab}}{b\sqrt{x} + \sqrt{ab}}\right)}{8\sqrt{ab}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-a)^3/x^(1/2),x, algorithm="maxima")

[Out] $1/4*(3*b*x^{(3/2)} - 5*a*\sqrt{x})/(a^2*b^2*x^2 - 2*a^3*b*x + a^4) + 3/8*\log((b*\sqrt{x} - \sqrt{a*b})/(b*\sqrt{x} + \sqrt{a*b}))/(\sqrt{a*b}*a^2)$

mupad [B] time = 0.13, size = 58, normalized size = 0.81

$$-\frac{\frac{5\sqrt{x}}{4a} - \frac{3bx^{3/2}}{4a^2}}{a^2 - 2abx + b^2x^2} - \frac{3 \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{5/2}\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-1/(x^(1/2)*(a - b*x)^3), x)`

[Out] $-\left(\frac{5x^{1/2}}{4a} - \frac{3bx^{3/2}}{4a^2}\right)/(a^2 + b^2x^2 - 2abx) - \left(3\operatorname{atanh}\left(\frac{b^{1/2}x^{1/2}}{a^{1/2}}\right)\right)/(4a^{5/2}b^{1/2})$

sympy [A] time = 25.67, size = 660, normalized size = 9.17

$$\left\{ \begin{array}{l} \frac{\infty}{5} \\ x^2 \\ -\frac{2\sqrt{x}}{a^3} \\ -\frac{2}{5b^3x^2} \end{array} \right. - \frac{10a^{\frac{3}{2}}b\sqrt{x}\sqrt{\frac{1}{b}}}{8a^{\frac{9}{2}}b\sqrt{\frac{1}{b}} - 16a^{\frac{7}{2}}b^2x\sqrt{\frac{1}{b}} + 8a^{\frac{5}{2}}b^3x^2\sqrt{\frac{1}{b}}} + \frac{6\sqrt{a}b^2x^{\frac{3}{2}}\sqrt{\frac{1}{b}}}{8a^{\frac{9}{2}}b\sqrt{\frac{1}{b}} - 16a^{\frac{7}{2}}b^2x\sqrt{\frac{1}{b}} + 8a^{\frac{5}{2}}b^3x^2\sqrt{\frac{1}{b}}} + \frac{3a^2\log\left(-\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{8a^{\frac{9}{2}}b\sqrt{\frac{1}{b}} - 16a^{\frac{7}{2}}b^2x\sqrt{\frac{1}{b}} + 8a^{\frac{5}{2}}b^3x^2\sqrt{\frac{1}{b}}} - \frac{3a^2\log\left(\sqrt{a}\sqrt{\frac{1}{b}} + \sqrt{x}\right)}{8a^{\frac{9}{2}}b\sqrt{\frac{1}{b}} - 16a^{\frac{7}{2}}b^2x\sqrt{\frac{1}{b}} + 8a^{\frac{5}{2}}b^3x^2\sqrt{\frac{1}{b}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-a)**3/x**(1/2), x)`

[Out] `Piecewise((zoo/x**(5/2), Eq(a, 0) & Eq(b, 0)), (-2*sqrt(x)/a**3, Eq(b, 0)), (-2/(5*b**3*x**(5/2)), Eq(a, 0)), (-10*a**(3/2)*b*sqrt(x)*sqrt(1/b)/(8*a**(9/2)*b*sqrt(1/b) - 16*a**(7/2)*b**2*x*sqrt(1/b) + 8*a**(5/2)*b**3*x**2*sqrt(1/b)) + 6*sqrt(a)*b**2*x**(3/2)*sqrt(1/b)/(8*a**(9/2)*b*sqrt(1/b) - 16*a**(7/2)*b**2*x*sqrt(1/b) + 8*a**(5/2)*b**3*x**2*sqrt(1/b)) + 3*a**2*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(9/2)*b*sqrt(1/b) - 16*a**(7/2)*b**2*x*sqrt(1/b) + 8*a**(5/2)*b**3*x**2*sqrt(1/b)) - 3*a**2*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(9/2)*b*sqrt(1/b) - 16*a**(7/2)*b**2*x*sqrt(1/b) + 8*a**(5/2)*b**3*x**2*sqrt(1/b)) - 6*a*b*x*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(9/2)*b*sqrt(1/b) - 16*a**(7/2)*b**2*x*sqrt(1/b) + 8*a**(5/2)*b**3*x**2*sqrt(1/b)) + 6*a*b*x*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(9/2)*b*sqrt(1/b) - 16*a**(7/2)*b**2*x*sqrt(1/b) + 8*a**(5/2)*b**3*x**2*sqrt(1/b)) + 3*b**2*x**2*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(9/2)*b*sqrt(1/b) - 16*a**(7/2)*b**2*x*sqrt(1/b) + 8*a**(5/2)*b**3*x**2*sqrt(1/b)) - 3*b**2*x**2*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(9/2)*b*sqrt(1/b) - 16*a**(7/2)*b**2*x*sqrt(1/b) + 8*a**(5/2)*b**3*x**2*sqrt(1/b)), True))`

$$3.487 \quad \int \frac{1}{x^{3/2}(-a+bx)^3} dx$$

Optimal. Leaf size=84

$$-\frac{15\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{7/2}} + \frac{15}{4a^3\sqrt{x}} - \frac{5}{4a^2\sqrt{x}(a-bx)} - \frac{1}{2a\sqrt{x}(a-bx)^2}$$

[Out] $-15/4*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/a^{(1/2)})*b^{(1/2)}/a^{(7/2)}+15/4/a^3/x^{(1/2)}-1/2/a/(-b*x+a)^2/x^{(1/2)}-5/4/a^2/(-b*x+a)/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 208}

$$-\frac{5}{4a^2\sqrt{x}(a-bx)} - \frac{15\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{7/2}} + \frac{15}{4a^3\sqrt{x}} - \frac{1}{2a\sqrt{x}(a-bx)^2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/(x^{(3/2)}*(-a + b*x)^3), x]$

[Out] $15/(4*a^3*\operatorname{Sqrt}[x]) - 1/(2*a*\operatorname{Sqrt}[x]*(a - b*x)^2) - 5/(4*a^2*\operatorname{Sqrt}[x]*(a - b*x)) - (15*\operatorname{Sqrt}[b]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/ \operatorname{Sqrt}[a]])/(4*a^{(7/2)})$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)} / ((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*(m+n+2)) / ((b*c - a*d)*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^n, x] /; \operatorname{FreeQ}\{a, b, c, d, n\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{LtQ}[n, -1] \&\& (\operatorname{EqQ}[a, 0] \mid\mid (\operatorname{NeQ}[c, 0] \&\& \operatorname{LtQ}[m - n, 0] \&\& \operatorname{IntegerQ}[n]))) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /; \operatorname{FreeQ}\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{3/2}(-a+bx)^3} dx &= -\frac{1}{2a\sqrt{x}(a-bx)^2} - \frac{5 \int \frac{1}{x^{3/2}(-a+bx)^2} dx}{4a} \\
 &= -\frac{1}{2a\sqrt{x}(a-bx)^2} - \frac{5}{4a^2\sqrt{x}(a-bx)} + \frac{15 \int \frac{1}{x^{3/2}(-a+bx)} dx}{8a^2} \\
 &= \frac{15}{4a^3\sqrt{x}} - \frac{1}{2a\sqrt{x}(a-bx)^2} - \frac{5}{4a^2\sqrt{x}(a-bx)} + \frac{(15b) \int \frac{1}{\sqrt{x}(-a+bx)} dx}{8a^3} \\
 &= \frac{15}{4a^3\sqrt{x}} - \frac{1}{2a\sqrt{x}(a-bx)^2} - \frac{5}{4a^2\sqrt{x}(a-bx)} + \frac{(15b) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{4a^3} \\
 &= \frac{15}{4a^3\sqrt{x}} - \frac{1}{2a\sqrt{x}(a-bx)^2} - \frac{5}{4a^2\sqrt{x}(a-bx)} - \frac{15\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 24, normalized size = 0.29

$$\frac{{}_2F_1\left(-\frac{1}{2}, 3; \frac{1}{2}; \frac{bx}{a}\right)}{a^3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(-a + b*x)^3), x]

[Out] (2*Hypergeometric2F1[-1/2, 3, 1/2, (b*x)/a])/(a^3*sqrt[x])

fricas [A] time = 0.45, size = 213, normalized size = 2.54

$$\left[\frac{15(b^2x^3 - 2abx^2 + a^2x)\sqrt{\frac{b}{a}} \log\left(\frac{bx - 2a\sqrt{x}\sqrt{\frac{b}{a}} + a}{bx - a}\right) + 2(15b^2x^2 - 25abx + 8a^2)\sqrt{x}}{8(a^3b^2x^3 - 2a^4bx^2 + a^5x)}, \frac{15(b^2x^3 - 2abx^2 + a^2x)\sqrt{-\frac{b}{a}}}{4(a^3b^2x^3 - 2a^4bx^2 + a^5x)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x-a)^3,x, algorithm="fricas")

[Out] [1/8*(15*(b^2*x^3 - 2*a*b*x^2 + a^2*x)*sqrt(b/a)*log((b*x - 2*a*sqrt(x))*sqrt(b/a) + a)/(b*x - a)) + 2*(15*b^2*x^2 - 25*a*b*x + 8*a^2)*sqrt(x))/(a^3*b^2*x^3 - 2*a^4*b*x^2 + a^5*x), 1/4*(15*(b^2*x^3 - 2*a*b*x^2 + a^2*x)*sqrt(-b/a)*arctan(a*sqrt(-b/a)/(b*sqrt(x))) + (15*b^2*x^2 - 25*a*b*x + 8*a^2)*sqrt(x))/(a^3*b^2*x^3 - 2*a^4*b*x^2 + a^5*x)]

giac [A] time = 1.05, size = 63, normalized size = 0.75

$$\frac{15 b \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{4 \sqrt{-ab} a^3} + \frac{2}{a^3 \sqrt{x}} + \frac{7 b^2 x^{\frac{3}{2}} - 9 ab \sqrt{x}}{4 (bx - a)^2 a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x-a)^3,x, algorithm="giac")

[Out] 15/4*b*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*a^3) + 2/(a^3*sqrt(x)) + 1/4*(7*b^2*x^(3/2) - 9*a*b*sqrt(x))/((b*x - a)^2*a^3)

maple [A] time = 0.02, size = 58, normalized size = 0.69

$$\frac{2 \left(-\frac{15 \operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{8\sqrt{ab}} + \frac{\frac{7bx^{\frac{3}{2}}}{8} - \frac{9a\sqrt{x}}{8}}{(bx-a)^2} \right) b}{a^3} + \frac{2}{a^3 \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2)/(b*x-a)^3,x)

[Out] 2/a^3*b*((7/8*b*x^(3/2)-9/8*a*x^(1/2))/(b*x-a)^2-15/8/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2)))+2/a^3/x^(1/2)

maxima [A] time = 2.93, size = 90, normalized size = 1.07

$$\frac{15 b^2 x^2 - 25 abx + 8 a^2}{4 \left(a^3 b^2 x^{\frac{5}{2}} - 2 a^4 b x^{\frac{3}{2}} + a^5 \sqrt{x} \right)} + \frac{15 b \log\left(\frac{b\sqrt{x} - \sqrt{ab}}{b\sqrt{x} + \sqrt{ab}}\right)}{8 \sqrt{ab} a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x-a)^3,x, algorithm="maxima")

[Out] $\frac{1}{4} \cdot (15b^2x^2 - 25abx + 8a^2) / (a^3b^2x^{5/2} - 2a^4bx^{3/2} + a^5\sqrt{x}) + \frac{15}{8}b \cdot \log((b\sqrt{x} - \sqrt{ab}) / (b\sqrt{x} + \sqrt{ab})) / (\sqrt{ab}a^3)$

mupad [B] time = 0.15, size = 69, normalized size = 0.82

$$\frac{\frac{2}{a} + \frac{15b^2x^2}{4a^3} - \frac{25bx}{4a^2}}{a^2\sqrt{x} + b^2x^{5/2} - 2abx^{3/2}} - \frac{15\sqrt{b} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-1/(x^(3/2)*(a - b*x)^3), x)`

[Out] $(2/a + (15b^2x^2)/(4a^3) - (25bx)/(4a^2)) / (a^2x^{1/2} + b^2x^{5/2} - 2abx^{3/2}) - (15b^{1/2} \operatorname{atanh}(b^{1/2}x^{1/2}/a^{1/2})) / (4a^{7/2})$

sympy [A] time = 54.56, size = 802, normalized size = 9.55

$$\left\{ \begin{array}{l} \frac{\infty}{7} \\ x^2 \\ \frac{2}{a^3\sqrt{x}} \\ \frac{2}{7b^3x^2} \end{array} \right\} \frac{16a^{\frac{5}{2}}\sqrt{\frac{1}{b}}}{8a^{\frac{11}{2}}\sqrt{x}\sqrt{\frac{1}{b}} - 16a^{\frac{9}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 8a^{\frac{7}{2}}b^2x^{\frac{5}{2}}\sqrt{\frac{1}{b}}} - \frac{50a^{\frac{3}{2}}bx\sqrt{\frac{1}{b}}}{8a^{\frac{11}{2}}\sqrt{x}\sqrt{\frac{1}{b}} - 16a^{\frac{9}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 8a^{\frac{7}{2}}b^2x^{\frac{5}{2}}\sqrt{\frac{1}{b}}} + \frac{30\sqrt{a}b^2x^2\sqrt{\frac{1}{b}}}{8a^{\frac{11}{2}}\sqrt{x}\sqrt{\frac{1}{b}} - 16a^{\frac{9}{2}}bx^{\frac{3}{2}}\sqrt{\frac{1}{b}} + 8a^{\frac{7}{2}}b^2x^{\frac{5}{2}}\sqrt{\frac{1}{b}}} + \frac{11}{8a^{\frac{11}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(b*x-a)**3, x)`

[Out] `Piecewise((zoo/x**(7/2), Eq(a, 0) & Eq(b, 0)), (2/(a**3*sqrt(x)), Eq(b, 0)), (-2/(7*b**3*x**(7/2)), Eq(a, 0)), (16*a**(5/2)*sqrt(1/b)/(8*a**(11/2)*sqrt(x)*sqrt(1/b) - 16*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) - 50*a**(3/2)*b*x*sqrt(1/b)/(8*a**(11/2)*sqrt(x)*sqrt(1/b) - 16*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) + 30*sqrt(a)*b**2*x**2*sqrt(1/b)/(8*a**(11/2)*sqrt(x)*sqrt(1/b) - 16*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) + 15*a**2*sqrt(x)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(11/2)*sqrt(x)*sqrt(1/b) - 16*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) - 15*a**2*sqrt(x)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(11/2)*sqrt(x)*sqrt(1/b) - 16*`

```

a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) - 30*a*
b*x**(3/2)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(11/2)*sqrt(x)*sqrt(1/b)
- 16*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*a**(7/2)*b**2*x**(5/2)*sqrt(1/b)) +
30*a*b*x**(3/2)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(11/2)*sqrt(x)*sqrt
(1/b) - 16*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*a**(7/2)*b**2*x**(5/2)*sqrt(1/
b)) + 15*b**2*x**(5/2)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(11/2)*sqrt(
x)*sqrt(1/b) - 16*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*a**(7/2)*b**2*x**(5/2)*
sqrt(1/b)) - 15*b**2*x**(5/2)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(8*a**(11/2)
*sqrt(x)*sqrt(1/b) - 16*a**(9/2)*b*x**(3/2)*sqrt(1/b) + 8*a**(7/2)*b**2*x**
(5/2)*sqrt(1/b)), True))

```

$$3.488 \quad \int \frac{1}{x^{5/2}(-a+bx)^3} dx$$

Optimal. Leaf size=97

$$-\frac{35b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{9/2}} + \frac{35b}{4a^4\sqrt{x}} + \frac{35}{12a^3x^{3/2}} - \frac{7}{4a^2x^{3/2}(a-bx)} - \frac{1}{2ax^{3/2}(a-bx)^2}$$

[Out] 35/12/a^3/x^(3/2)-1/2/a/x^(3/2)/(-b*x+a)^2-7/4/a^2/x^(3/2)/(-b*x+a)-35/4*b^(3/2)*arctanh(b^(1/2)*x^(1/2)/a^(1/2))/a^(9/2)+35/4*b/a^4/x^(1/2)

Rubi [A] time = 0.03, antiderivative size = 97, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 63, 208}

$$-\frac{35b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{9/2}} - \frac{7}{4a^2x^{3/2}(a-bx)} + \frac{35b}{4a^4\sqrt{x}} + \frac{35}{12a^3x^{3/2}} - \frac{1}{2ax^{3/2}(a-bx)^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(-a + b*x)^3),x]

[Out] 35/(12*a^3*x^(3/2)) + (35*b)/(4*a^4*Sqrt[x]) - 1/(2*a*x^(3/2)*(a - b*x)^2) - 7/(4*a^2*x^(3/2)*(a - b*x)) - (35*b^(3/2)*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(4*a^(9/2))

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{5/2}(-a+bx)^3} dx &= -\frac{1}{2ax^{3/2}(a-bx)^2} - \frac{7 \int \frac{1}{x^{5/2}(-a+bx)^2} dx}{4a} \\
 &= -\frac{1}{2ax^{3/2}(a-bx)^2} - \frac{7}{4a^2x^{3/2}(a-bx)} + \frac{35 \int \frac{1}{x^{5/2}(-a+bx)} dx}{8a^2} \\
 &= \frac{35}{12a^3x^{3/2}} - \frac{1}{2ax^{3/2}(a-bx)^2} - \frac{7}{4a^2x^{3/2}(a-bx)} + \frac{(35b) \int \frac{1}{x^{3/2}(-a+bx)} dx}{8a^3} \\
 &= \frac{35}{12a^3x^{3/2}} + \frac{35b}{4a^4\sqrt{x}} - \frac{1}{2ax^{3/2}(a-bx)^2} - \frac{7}{4a^2x^{3/2}(a-bx)} + \frac{(35b^2) \int \frac{1}{\sqrt{x}(-a+bx)} dx}{8a^4} \\
 &= \frac{35}{12a^3x^{3/2}} + \frac{35b}{4a^4\sqrt{x}} - \frac{1}{2ax^{3/2}(a-bx)^2} - \frac{7}{4a^2x^{3/2}(a-bx)} + \frac{(35b^2) \text{Subst}\left(\int \frac{1}{-a+bx^2} dx, x, \sqrt{x}\right)}{4a^4} \\
 &= \frac{35}{12a^3x^{3/2}} + \frac{35b}{4a^4\sqrt{x}} - \frac{1}{2ax^{3/2}(a-bx)^2} - \frac{7}{4a^2x^{3/2}(a-bx)} - \frac{35b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{9/2}}
 \end{aligned}$$

Mathematica [C] time = 0.00, size = 26, normalized size = 0.27

$$\frac{{}_2F_1\left(-\frac{3}{2}, 3; -\frac{1}{2}; \frac{bx}{a}\right)}{3a^3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(-a + b*x)^3), x]

[Out] (2*Hypergeometric2F1[-3/2, 3, -1/2, (b*x)/a])/(3*a^3*x^(3/2))

fricas [A] time = 0.49, size = 249, normalized size = 2.57

$$\left[\frac{105(b^3x^4 - 2ab^2x^3 + a^2bx^2)\sqrt{\frac{b}{a}} \log\left(\frac{bx - 2a\sqrt{x}\sqrt{\frac{b}{a}} + a}{bx - a}\right) + 2(105b^3x^3 - 175ab^2x^2 + 56a^2bx + 8a^3)\sqrt{x} - 105(b^3x^4 - 2ab^2x^3 + a^2bx^2)}{24(a^4b^2x^4 - 2a^5bx^3 + a^6x^2)}, \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x-a)^3,x, algorithm="fricas")

[Out] [1/24*(105*(b^3*x^4 - 2*a*b^2*x^3 + a^2*b*x^2)*sqrt(b/a)*log((b*x - 2*a*sqrt(x)*sqrt(b/a) + a)/(b*x - a)) + 2*(105*b^3*x^3 - 175*a*b^2*x^2 + 56*a^2*b*x + 8*a^3)*sqrt(x))/(a^4*b^2*x^4 - 2*a^5*b*x^3 + a^6*x^2), 1/12*(105*(b^3*x^4 - 2*a*b^2*x^3 + a^2*b*x^2)*sqrt(-b/a)*arctan(a*sqrt(-b/a)/(b*sqrt(x))) + (105*b^3*x^3 - 175*a*b^2*x^2 + 56*a^2*b*x + 8*a^3)*sqrt(x))/(a^4*b^2*x^4 - 2*a^5*b*x^3 + a^6*x^2)]

giac [A] time = 1.04, size = 73, normalized size = 0.75

$$\frac{35b^2 \arctan\left(\frac{b\sqrt{x}}{\sqrt{-ab}}\right)}{4\sqrt{-ab}a^4} + \frac{2(9bx+a)}{3a^4x^{\frac{3}{2}}} + \frac{11b^3x^{\frac{3}{2}} - 13ab^2\sqrt{x}}{4(bx-a)^2a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x-a)^3,x, algorithm="giac")

[Out] 35/4*b^2*arctan(b*sqrt(x)/sqrt(-a*b))/(sqrt(-a*b)*a^4) + 2/3*(9*b*x + a)/(a^4*x^(3/2)) + 1/4*(11*b^3*x^(3/2) - 13*a*b^2*sqrt(x))/((b*x - a)^2*a^4)

maple [A] time = 0.02, size = 69, normalized size = 0.71

$$\frac{2\left(-\frac{35\operatorname{arctanh}\left(\frac{b\sqrt{x}}{\sqrt{ab}}\right)}{8\sqrt{ab}} + \frac{\frac{11bx^{\frac{3}{2}}}{8} - \frac{13a\sqrt{x}}{8}}{(bx-a)^2}\right)b^2}{a^4} + \frac{6b}{a^4\sqrt{x}} + \frac{2}{3a^3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(5/2)/(b*x-a)^3,x)

[Out] 2/a^4*b^2*((11/8*b*x^(3/2)-13/8*a*x^(1/2))/(b*x-a)^2-35/8/(a*b)^(1/2)*arctanh(1/(a*b)^(1/2)*b*x^(1/2)))+2/3/a^3/x^(3/2)+6/a^4*b/x^(1/2)

maxima [A] time = 2.95, size = 103, normalized size = 1.06

$$\frac{105b^3x^3 - 175ab^2x^2 + 56a^2bx + 8a^3}{12\left(a^4b^2x^{\frac{7}{2}} - 2a^5bx^{\frac{5}{2}} + a^6x^{\frac{3}{2}}\right)} + \frac{35b^2 \log\left(\frac{b\sqrt{x}-\sqrt{ab}}{b\sqrt{x}+\sqrt{ab}}\right)}{8\sqrt{ab}a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x-a)^3,x, algorithm="maxima")

[Out] $\frac{1}{12} \cdot \frac{105b^3x^3 - 175a^2b^2x^2 + 56a^2bx + 8a^3}{a^4b^2x^{7/2} - 2a^5b^2x^{5/2} + a^6x^{3/2}} + \frac{35}{8} \cdot \frac{b^2 \log((b\sqrt{x} - \sqrt{ab})/(b\sqrt{x} + \sqrt{ab}))}{(\sqrt{ab})a^4}$

mupad [B] time = 0.17, size = 80, normalized size = 0.82

$$\frac{\frac{2}{3a} - \frac{175b^2x^2}{12a^3} + \frac{35b^3x^3}{4a^4} + \frac{14bx}{3a^2}}{a^2x^{3/2} + b^2x^{7/2} - 2abx^{5/2}} - \frac{35b^{3/2} \operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4a^{9/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-1/(x^(5/2)*(a - b*x)^3),x)

[Out] $\frac{2}{3a} - \frac{175b^2x^2}{12a^3} + \frac{35b^3x^3}{4a^4} + \frac{14bx}{3a^2} \bigg/ (a^2x^{3/2} + b^2x^{7/2} - 2a^2bx^{5/2}) - \frac{35b^{3/2} \operatorname{atanh}(b^{1/2}x^{1/2}/a^{1/2})}{4a^{9/2}}$

sympy [A] time = 138.88, size = 892, normalized size = 9.20

$$\left(\begin{array}{l} \frac{\infty}{x^2} \\ \frac{2}{3a^3x^2} \\ \frac{2}{9b^3x^2} \end{array} \right) + \frac{16a^{\frac{7}{2}}\sqrt{\frac{1}{b}}}{24a^{\frac{13}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} - 48a^{\frac{11}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}} + 24a^{\frac{9}{2}}b^2x^{\frac{7}{2}}\sqrt{\frac{1}{b}}} + \frac{112a^{\frac{5}{2}}bx\sqrt{\frac{1}{b}}}{24a^{\frac{13}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} - 48a^{\frac{11}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}} + 24a^{\frac{9}{2}}b^2x^{\frac{7}{2}}\sqrt{\frac{1}{b}}} - \frac{350a^{\frac{3}{2}}b^2x^2\sqrt{\frac{1}{b}}}{24a^{\frac{13}{2}}x^{\frac{3}{2}}\sqrt{\frac{1}{b}} - 48a^{\frac{11}{2}}bx^{\frac{5}{2}}\sqrt{\frac{1}{b}} + 24a^{\frac{9}{2}}b^2x^{\frac{7}{2}}\sqrt{\frac{1}{b}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(5/2)/(b*x-a)**3,x)

[Out] Piecewise((zoo/x**(9/2), Eq(a, 0) & Eq(b, 0)), (2/(3*a**3*x**(3/2)), Eq(b, 0)), (-2/(9*b**3*x**(9/2)), Eq(a, 0)), (16*a**(7/2)*sqrt(1/b)/(24*a**(13/2)*x**(3/2)*sqrt(1/b) - 48*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) + 112*a**(5/2)*b*x*sqrt(1/b)/(24*a**(13/2)*x**(3/2)*sqrt(1/b) - 48*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) - 350*a**(3/2)*b**2*x**2*sqrt(1/b)/(24*a**(13/2)*x**(3/2)*sqrt(1/b) - 48*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) + 210*sqrt(a)*b**3*x**3*sqrt(1/b)/(24*a**(13/2)*x**(3/2)*sqrt(1/b) - 48*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) + 105*a*

```

*2*b*x**(3/2)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/(24*a**(13/2)*x**(3/2)*sqrt
(1/b) - 48*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*a**(9/2)*b**2*x**(7/2)*sqrt(
1/b)) - 105*a**2*b*x**(3/2)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(24*a**(13/2)*
x**(3/2)*sqrt(1/b) - 48*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*a**(9/2)*b**2*x
**(7/2)*sqrt(1/b)) - 210*a*b**2*x**(5/2)*log(-sqrt(a)*sqrt(1/b) + sqrt(x))/
(24*a**(13/2)*x**(3/2)*sqrt(1/b) - 48*a**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*a
**(9/2)*b**2*x**(7/2)*sqrt(1/b)) + 210*a*b**2*x**(5/2)*log(sqrt(a)*sqrt(1/b
) + sqrt(x))/(24*a**(13/2)*x**(3/2)*sqrt(1/b) - 48*a**(11/2)*b*x**(5/2)*sqr
t(1/b) + 24*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) + 105*b**3*x**(7/2)*log(-sqrt
(a)*sqrt(1/b) + sqrt(x))/(24*a**(13/2)*x**(3/2)*sqrt(1/b) - 48*a**(11/2)*b*
x**(5/2)*sqrt(1/b) + 24*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)) - 105*b**3*x**(7/
2)*log(sqrt(a)*sqrt(1/b) + sqrt(x))/(24*a**(13/2)*x**(3/2)*sqrt(1/b) - 48*a
**(11/2)*b*x**(5/2)*sqrt(1/b) + 24*a**(9/2)*b**2*x**(7/2)*sqrt(1/b)), True)
)

```

3.489 $\int x^{5/2} \sqrt{a+bx} dx$

Optimal. Leaf size=122

$$-\frac{5a^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{64b^{7/2}} + \frac{5a^3 \sqrt{x} \sqrt{a+bx}}{64b^3} - \frac{5a^2 x^{3/2} \sqrt{a+bx}}{96b^2} + \frac{ax^{5/2} \sqrt{a+bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a+bx}$$

[Out] $-5/64*a^4*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(7/2)}-5/96*a^2*x^{(3/2)}*(b*x+a)^{(1/2)}/b^2+1/24*a*x^{(5/2)}*(b*x+a)^{(1/2)}/b+1/4*x^{(7/2)}*(b*x+a)^{(1/2)}+5/64*a^3*x^{(1/2)}*(b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.04, antiderivative size = 122, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$-\frac{5a^2 x^{3/2} \sqrt{a+bx}}{96b^2} + \frac{5a^3 \sqrt{x} \sqrt{a+bx}}{64b^3} - \frac{5a^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{64b^{7/2}} + \frac{ax^{5/2} \sqrt{a+bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a+bx}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(5/2)}*\operatorname{Sqrt}[a + b*x], x]$

[Out] $(5*a^3*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(64*b^3) - (5*a^2*x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/(96*b^2) + (a*x^{(5/2)}*\operatorname{Sqrt}[a + b*x])/(24*b) + (x^{(7/2)}*\operatorname{Sqrt}[a + b*x])/4 - (5*a^4*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(64*b^{(7/2)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n)}/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[p = \operatorname{Denominator}[m], \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int x^{5/2} \sqrt{a+bx} \, dx &= \frac{1}{4} x^{7/2} \sqrt{a+bx} + \frac{1}{8} a \int \frac{x^{5/2}}{\sqrt{a+bx}} \, dx \\
 &= \frac{ax^{5/2} \sqrt{a+bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a+bx} - \frac{(5a^2) \int \frac{x^{3/2}}{\sqrt{a+bx}} \, dx}{48b} \\
 &= -\frac{5a^2 x^{3/2} \sqrt{a+bx}}{96b^2} + \frac{ax^{5/2} \sqrt{a+bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a+bx} + \frac{(5a^3) \int \frac{\sqrt{x}}{\sqrt{a+bx}} \, dx}{64b^2} \\
 &= \frac{5a^3 \sqrt{x} \sqrt{a+bx}}{64b^3} - \frac{5a^2 x^{3/2} \sqrt{a+bx}}{96b^2} + \frac{ax^{5/2} \sqrt{a+bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a+bx} - \frac{(5a^4) \int \frac{1}{\sqrt{x} \sqrt{a+bx}} \, dx}{128b^3} \\
 &= \frac{5a^3 \sqrt{x} \sqrt{a+bx}}{64b^3} - \frac{5a^2 x^{3/2} \sqrt{a+bx}}{96b^2} + \frac{ax^{5/2} \sqrt{a+bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a+bx} - \frac{(5a^4) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx}} \, dx\right)}{64b^3} \\
 &= \frac{5a^3 \sqrt{x} \sqrt{a+bx}}{64b^3} - \frac{5a^2 x^{3/2} \sqrt{a+bx}}{96b^2} + \frac{ax^{5/2} \sqrt{a+bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a+bx} - \frac{(5a^4) \operatorname{Subst}\left(\int \frac{1}{1-bx^2} \, dx\right)}{64b^3} \\
 &= \frac{5a^3 \sqrt{x} \sqrt{a+bx}}{64b^3} - \frac{5a^2 x^{3/2} \sqrt{a+bx}}{96b^2} + \frac{ax^{5/2} \sqrt{a+bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a+bx} - \frac{5a^4 \tanh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a+bx}}\right)}{64b^{7/2}}
 \end{aligned}$$

Mathematica [A] time = 0.18, size = 96, normalized size = 0.79

$$\frac{\sqrt{a+bx} \left(\sqrt{b} \sqrt{x} (15a^3 - 10a^2bx + 8ab^2x^2 + 48b^3x^3) - \frac{15a^{7/2} \sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{\frac{bx}{a}+1}} \right)}{192b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*Sqrt[a + b*x], x]

[Out] $(\sqrt{a + bx} * (\sqrt{b} * \sqrt{x} * (15a^3 - 10a^2bx + 8ab^2x^2 + 48b^3x^3) - (15a^{7/2}) * \text{ArcSinh}[(\sqrt{b} * \sqrt{x}) / \sqrt{a}]) / \sqrt{1 + (bx)/a})) / (192b^{7/2})$

fricas [A] time = 0.45, size = 162, normalized size = 1.33

$$\left[\frac{15a^4\sqrt{b} \log(2bx - 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(48b^4x^3 + 8ab^3x^2 - 10a^2b^2x + 15a^3b)\sqrt{bx+a}\sqrt{x}}{384b^4}, \frac{15a^4\sqrt{-b}}{384b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/2)*(b*x+a)^(1/2),x, algorithm="fricas")`

[Out] $[1/384*(15a^4*\sqrt{b}*\log(2*bx - 2*\sqrt{bx+a}*\sqrt{b}*\sqrt{x} + a) + 2*(48*b^4*x^3 + 8*a*b^3*x^2 - 10*a^2*b^2*x + 15*a^3*b)*\sqrt{bx+a}*\sqrt{x})/b^4, 1/192*(15*a^4*\sqrt{-b}*\arctan(\sqrt{bx+a}*\sqrt{-b}/(b*\sqrt{x}))) + (48*b^4*x^3 + 8*a*b^3*x^2 - 10*a^2*b^2*x + 15*a^3*b)*\sqrt{bx+a}*\sqrt{x})/b^4]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/2)*(b*x+a)^(1/2),x, algorithm="giac")`

[Out] Timed out

maple [A] time = 0.01, size = 120, normalized size = 0.98

$$\frac{(bx+a)^{\frac{3}{2}}x^{\frac{5}{2}}}{4b} - \frac{5\sqrt{bx+a}x a^4 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{128\sqrt{bx+a}b^{\frac{7}{2}}\sqrt{x}} - \frac{5\sqrt{bx+a}a^3\sqrt{x}}{64b^3} - \frac{5(bx+a)^{\frac{3}{2}}ax^{\frac{3}{2}}}{24b^2} + \frac{5(bx+a)^{\frac{3}{2}}a^2\sqrt{x}}{32b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/2)*(b*x+a)^(1/2),x)`

[Out] $1/4/b*x^{5/2}*(b*x+a)^{3/2} - 5/24*a/b^2*x^{3/2}*(b*x+a)^{3/2} + 5/32*a^2/b^3*x^{1/2}*(b*x+a)^{3/2} - 5/64*a^3*x^{1/2}*(b*x+a)^{1/2}/b^3 - 5/128*a^4/b^{7/2}*(x*(b*x+a))^{1/2}/(b*x+a)^{1/2}/x^{1/2}*\ln((1/2*a+b*x)/b^{1/2}+(b*x^2+a*x)^{1/2})$

maxima [B] time = 2.95, size = 178, normalized size = 1.46

$$\frac{5a^4 \log\left(-\frac{\sqrt{b}-\sqrt{bx+a}}{\sqrt{x}}\right)}{128b^{\frac{7}{2}}} + \frac{\frac{15\sqrt{bx+a}a^4b^3}{\sqrt{x}} + \frac{73(bx+a)^{\frac{3}{2}}a^4b^2}{x^{\frac{3}{2}}} - \frac{55(bx+a)^{\frac{5}{2}}a^4b}{x^{\frac{5}{2}}} + \frac{15(bx+a)^{\frac{7}{2}}a^4}{x^{\frac{7}{2}}}}{192\left(b^7 - \frac{4(bx+a)b^6}{x} + \frac{6(bx+a)^2b^5}{x^2} - \frac{4(bx+a)^3b^4}{x^3} + \frac{(bx+a)^4b^3}{x^4}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^(1/2),x, algorithm="maxima")

[Out] 5/128*a^4*log(-(sqrt(b) - sqrt(b*x + a))/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x))/b^(7/2) + 1/192*(15*sqrt(b*x + a)*a^4*b^3/sqrt(x) + 73*(b*x + a)^(3/2)*a^4*b^2/x^(3/2) - 55*(b*x + a)^(5/2)*a^4*b/x^(5/2) + 15*(b*x + a)^(7/2)*a^4/x^(7/2))/(b^7 - 4*(b*x + a)*b^6/x + 6*(b*x + a)^2*b^5/x^2 - 4*(b*x + a)^3*b^4/x^3 + (b*x + a)^4*b^3/x^4)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} \sqrt{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(a + b*x)^(1/2),x)

[Out] int(x^(5/2)*(a + b*x)^(1/2), x)

sympy [A] time = 11.70, size = 153, normalized size = 1.25

$$\frac{5a^{\frac{7}{2}}\sqrt{x}}{64b^3\sqrt{1+\frac{bx}{a}}} + \frac{5a^{\frac{5}{2}}x^{\frac{3}{2}}}{192b^2\sqrt{1+\frac{bx}{a}}} - \frac{a^{\frac{3}{2}}x^{\frac{5}{2}}}{96b\sqrt{1+\frac{bx}{a}}} + \frac{7\sqrt{a}x^{\frac{7}{2}}}{24\sqrt{1+\frac{bx}{a}}} - \frac{5a^4 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{64b^{\frac{7}{2}}} + \frac{bx^{\frac{9}{2}}}{4\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)*(b*x+a)**(1/2),x)

[Out] 5*a**(7/2)*sqrt(x)/(64*b**3*sqrt(1 + b*x/a)) + 5*a**(5/2)*x**(3/2)/(192*b**2*sqrt(1 + b*x/a)) - a**(3/2)*x**(5/2)/(96*b*sqrt(1 + b*x/a)) + 7*sqrt(a)*x**(7/2)/(24*sqrt(1 + b*x/a)) - 5*a**4*asinh(sqrt(b)*sqrt(x)/sqrt(a))/(64*b**3*(7/2)) + b*x**(9/2)/(4*sqrt(a)*sqrt(1 + b*x/a))

3.490 $\int x^{3/2} \sqrt{a + bx} dx$

Optimal. Leaf size=98

$$\frac{a^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{8b^{5/2}} - \frac{a^2\sqrt{x}\sqrt{a+bx}}{8b^2} + \frac{ax^{3/2}\sqrt{a+bx}}{12b} + \frac{1}{3}x^{5/2}\sqrt{a+bx}$$

[Out] $1/8*a^3*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(5/2)}+1/12*a*x^{(3/2)}*(b*x+a)^{(1/2)}/b+1/3*x^{(5/2)}*(b*x+a)^{(1/2)}-1/8*a^2*x^{(1/2)}*(b*x+a)^{(1/2)}/b^2$

Rubi [A] time = 0.03, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$-\frac{a^2\sqrt{x}\sqrt{a+bx}}{8b^2} + \frac{a^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{8b^{5/2}} + \frac{ax^{3/2}\sqrt{a+bx}}{12b} + \frac{1}{3}x^{5/2}\sqrt{a+bx}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(3/2)}*\operatorname{Sqrt}[a + b*x], x]$

[Out] $-(a^2*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(8*b^2) + (a*x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/(12*b) + (x^{(5/2)}*\operatorname{Sqrt}[a + b*x])/3 + (a^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(8*b^{(5/2)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{GtQ}[n, 0] \ \&\& \operatorname{NeQ}[m + n + 1, 0] \ \&\& \operatorname{!(IGtQ}[m, 0] \ \&\& (\operatorname{!IntegerQ}[n] \ || (\operatorname{GtQ}[m, 0] \ \&\& \operatorname{LtQ}[m - n, 0])) \ \&\& \operatorname{!ILtQ}[m + 2, 0] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x])$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{LtQ}[-1, m, 0] \ \&\& \operatorname{LeQ}[-1, n, 0] \ \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int x^{3/2} \sqrt{a+bx} \, dx &= \frac{1}{3} x^{5/2} \sqrt{a+bx} + \frac{1}{6} a \int \frac{x^{3/2}}{\sqrt{a+bx}} \, dx \\
 &= \frac{ax^{3/2} \sqrt{a+bx}}{12b} + \frac{1}{3} x^{5/2} \sqrt{a+bx} - \frac{a^2 \int \frac{\sqrt{x}}{\sqrt{a+bx}} \, dx}{8b} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a+bx}}{8b^2} + \frac{ax^{3/2} \sqrt{a+bx}}{12b} + \frac{1}{3} x^{5/2} \sqrt{a+bx} + \frac{a^3 \int \frac{1}{\sqrt{x} \sqrt{a+bx}} \, dx}{16b^2} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a+bx}}{8b^2} + \frac{ax^{3/2} \sqrt{a+bx}}{12b} + \frac{1}{3} x^{5/2} \sqrt{a+bx} + \frac{a^3 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} \, dx, x, \sqrt{x}\right)}{8b^2} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a+bx}}{8b^2} + \frac{ax^{3/2} \sqrt{a+bx}}{12b} + \frac{1}{3} x^{5/2} \sqrt{a+bx} + \frac{a^3 \operatorname{Subst}\left(\int \frac{1}{1-bx^2} \, dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right)}{8b^2} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a+bx}}{8b^2} + \frac{ax^{3/2} \sqrt{a+bx}}{12b} + \frac{1}{3} x^{5/2} \sqrt{a+bx} + \frac{a^3 \tanh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a+bx}}\right)}{8b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.11, size = 85, normalized size = 0.87

$$\frac{\sqrt{a+bx} \left(\frac{3a^{5/2} \sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{\frac{bx}{a}+1}} + \sqrt{b} \sqrt{x} (-3a^2 + 2abx + 8b^2x^2) \right)}{24b^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*Sqrt[a + b*x], x]

[Out] (Sqrt[a + b*x]*(Sqrt[b]*Sqrt[x]*(-3*a^2 + 2*a*b*x + 8*b^2*x^2) + (3*a^(5/2)*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 + (b*x)/a])/(24*b^(5/2))

fricas [A] time = 0.44, size = 141, normalized size = 1.44

$$\left[\frac{3 a^3 \sqrt{b} \log(2 b x + 2 \sqrt{b x + a} \sqrt{b} \sqrt{x} + a) + 2 (8 b^3 x^2 + 2 a b^2 x - 3 a^2 b) \sqrt{b x + a} \sqrt{x}}{48 b^3}, - \frac{3 a^3 \sqrt{-b} \arctan\left(\frac{\sqrt{b x + a}}{b \sqrt{x}}\right)}{b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [1/48*(3*a^3*sqrt(b)*log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(8*b^3*x^2 + 2*a*b^2*x - 3*a^2*b)*sqrt(b*x + a)*sqrt(x))/b^3, -1/24*(3*a^3*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) - (8*b^3*x^2 + 2*a*b^2*x - 3*a^2*b)*sqrt(b*x + a)*sqrt(x))/b^3]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.00, size = 102, normalized size = 1.04

$$\frac{\sqrt{b x + a} x a^3 \ln\left(\frac{b x + \frac{a}{2}}{\sqrt{b}} + \sqrt{b x^2 + a x}\right)}{16 \sqrt{b x + a} b^{\frac{5}{2}} \sqrt{x}} + \frac{\sqrt{b x + a} a^2 \sqrt{x}}{8 b^2} + \frac{(b x + a)^{\frac{3}{2}} x^{\frac{3}{2}}}{3 b} - \frac{(b x + a)^{\frac{3}{2}} a \sqrt{x}}{4 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(b*x+a)^(1/2),x)

[Out] 1/3/b*x^(3/2)*(b*x+a)^(3/2)-1/4*a/b^2*x^(1/2)*(b*x+a)^(3/2)+1/8*a^2*x^(1/2)*(b*x+a)^(1/2)/b^2+1/16*a^3/b^(5/2)*((b*x+a)*x)^(1/2)/(b*x+a)^(1/2)/x^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))

maxima [B] time = 3.04, size = 146, normalized size = 1.49

$$-\frac{a^3 \log\left(-\frac{\sqrt{b}-\sqrt{b x+a}}{\sqrt{x}}\right)}{16 b^{\frac{5}{2}}}-\frac{\frac{3 \sqrt{b x+a} a^3 b^2}{\sqrt{x}}+\frac{8(b x+a)^{\frac{3}{2}} a^3 b}{x^{\frac{3}{2}}}-\frac{3(b x+a)^{\frac{5}{2}} a^3}{x^{\frac{5}{2}}}}{24\left(b^5-\frac{3(b x+a) b^4}{x}+\frac{3(b x+a)^2 b^3}{x^2}-\frac{(b x+a)^3 b^2}{x^3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^(1/2),x, algorithm="maxima")

[Out]
$$-1/16*a^3*\log(-(\sqrt{b} - \sqrt{b*x + a})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x + a})/\sqrt{x} - 1/24*(3*\sqrt{b*x + a}*a^3*b^2/\sqrt{x} + 8*(b*x + a)^{3/2})*a^3*b/x^{3/2} - 3*(b*x + a)^{5/2}*a^3/x^{5/2})/(b^5 - 3*(b*x + a)*b^4/x + 3*(b*x + a)^2*b^3/x^2 - (b*x + a)^3*b^2/x^3)$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} \sqrt{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(a + b*x)^(1/2),x)

[Out] int(x^(3/2)*(a + b*x)^(1/2), x)

sympy [A] time = 6.38, size = 122, normalized size = 1.24

$$-\frac{a^{\frac{5}{2}}\sqrt{x}}{8b^2\sqrt{1+\frac{bx}{a}}} - \frac{a^{\frac{3}{2}}x^{\frac{3}{2}}}{24b\sqrt{1+\frac{bx}{a}}} + \frac{5\sqrt{a}x^{\frac{5}{2}}}{12\sqrt{1+\frac{bx}{a}}} + \frac{a^3 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8b^{\frac{5}{2}}} + \frac{bx^{\frac{7}{2}}}{3\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)*(b*x+a)**(1/2),x)

[Out]
$$-a^{5/2}*\sqrt{x}/(8*b^{5/2}*\sqrt{1 + b*x/a}) - a^{3/2}*x^{3/2}/(24*b*\sqrt{1 + b*x/a}) + 5*\sqrt{a}*x^{5/2}/(12*\sqrt{1 + b*x/a}) + a^{3/2}*\operatorname{asinh}(\sqrt{b}*\sqrt{x}/\sqrt{a})/(8*b^{5/2}) + b*x^{7/2}/(3*\sqrt{a}*\sqrt{1 + b*x/a})$$

3.491 $\int \sqrt{x} \sqrt{a + bx} dx$

Optimal. Leaf size=74

$$-\frac{a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^{3/2}} + \frac{1}{2}x^{3/2}\sqrt{a+bx} + \frac{a\sqrt{x}\sqrt{a+bx}}{4b}$$

[Out] $-1/4*a^2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(3/2)}+1/2*x^{(3/2)}*(b*x+a)^{(1/2)}+1/4*a*x^{(1/2)}*(b*x+a)^{(1/2)}/b$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$-\frac{a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^{3/2}} + \frac{1}{2}x^{3/2}\sqrt{a+bx} + \frac{a\sqrt{x}\sqrt{a+bx}}{4b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*Sqrt[a + b*x], x]

[Out] $(a*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(4*b) + (x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/2 - (a^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(4*b^{(3/2)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[Rt[-b, 2]*x]/Rt[a, 2])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt

Q[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \sqrt{x} \sqrt{a+bx} \, dx &= \frac{1}{2} x^{3/2} \sqrt{a+bx} + \frac{1}{4} a \int \frac{\sqrt{x}}{\sqrt{a+bx}} \, dx \\
 &= \frac{a\sqrt{x} \sqrt{a+bx}}{4b} + \frac{1}{2} x^{3/2} \sqrt{a+bx} - \frac{a^2 \int \frac{1}{\sqrt{x} \sqrt{a+bx}} \, dx}{8b} \\
 &= \frac{a\sqrt{x} \sqrt{a+bx}}{4b} + \frac{1}{2} x^{3/2} \sqrt{a+bx} - \frac{a^2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} \, dx, x, \sqrt{x}\right)}{4b} \\
 &= \frac{a\sqrt{x} \sqrt{a+bx}}{4b} + \frac{1}{2} x^{3/2} \sqrt{a+bx} - \frac{a^2 \operatorname{Subst}\left(\int \frac{1}{1-bx^2} \, dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right)}{4b} \\
 &= \frac{a\sqrt{x} \sqrt{a+bx}}{4b} + \frac{1}{2} x^{3/2} \sqrt{a+bx} - \frac{a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^{3/2}}
 \end{aligned}$$

Mathematica [A] time = 0.11, size = 72, normalized size = 0.97

$$\frac{\sqrt{a+bx} \left(\sqrt{b}\sqrt{x}(a+2bx) - \frac{a^{3/2} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{\frac{bx}{a}+1}} \right)}{4b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*Sqrt[a + b*x], x]

[Out] (Sqrt[a + b*x]*(Sqrt[b]*Sqrt[x]*(a + 2*b*x) - (a^(3/2)*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 + (b*x)/a]))/(4*b^(3/2))

fricas [A] time = 0.45, size = 114, normalized size = 1.54

$$\left[\frac{a^2 \sqrt{b} \log(2bx - 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(2b^2x + ab)\sqrt{bx+a}\sqrt{x}}{8b^2}, \frac{a^2 \sqrt{-b} \arctan\left(\frac{\sqrt{bx+a}\sqrt{-b}}{b\sqrt{x}}\right) + (2b^2x + ab)}{4b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [1/8*(a^2*sqrt(b)*log(2*b*x - 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(2*b^2*x + a*b)*sqrt(b*x + a)*sqrt(x))/b^2, 1/4*(a^2*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) + (2*b^2*x + a*b)*sqrt(b*x + a)*sqrt(x))/b^2]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 81, normalized size = 1.09

$$\frac{\sqrt{bx+a} x^{\frac{3}{2}}}{2} - \frac{\sqrt{(bx+a)x} a^2 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{8\sqrt{bx+a} b^{\frac{3}{2}}\sqrt{x}} + \frac{\sqrt{bx+a} a\sqrt{x}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)*(b*x+a)^(1/2),x)

[Out] 1/2*x^(3/2)*(b*x+a)^(1/2)+1/4*a*x^(1/2)*(b*x+a)^(1/2)/b-1/8*a^2/b^(3/2)*((b*x+a)*x)^(1/2)/x^(1/2)/(b*x+a)^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))

maxima [B] time = 2.96, size = 108, normalized size = 1.46

$$\frac{a^2 \log\left(-\frac{\sqrt{b}-\sqrt{bx+a}}{\sqrt{x}}\right)}{8b^{\frac{3}{2}}} + \frac{\frac{\sqrt{bx+a} a^2 b}{\sqrt{x}} + \frac{(bx+a)^{\frac{3}{2}} a^2}{x^2}}{4\left(b^3 - \frac{2(bx+a)b^2}{x} + \frac{(bx+a)^2 b}{x^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(b*x+a)^(1/2),x, algorithm="maxima")

[Out] 1/8*a^2*log(-(sqrt(b) - sqrt(b*x + a)/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x)))/b^(3/2) + 1/4*(sqrt(b*x + a)*a^2*b/sqrt(x) + (b*x + a)^(3/2)*a^2/x^(3/2))/(b^3 - 2*(b*x + a)*b^2/x + (b*x + a)^2*b/x^2)

mupad [B] time = 0.15, size = 52, normalized size = 0.70

$$\sqrt{x} \left(\frac{x}{2} + \frac{a}{4b} \right) \sqrt{a+bx} - \frac{a^2 \ln(a + 2bx + 2\sqrt{b}\sqrt{x}\sqrt{a+bx})}{8b^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)*(a + b*x)^(1/2), x)`

[Out] `x^(1/2)*(x/2 + a/(4*b))*(a + b*x)^(1/2) - (a^2*log(a + 2*b*x + 2*b^(1/2)*x^(1/2)*(a + b*x)^(1/2)))/(8*b^(3/2))`

sympy [A] time = 3.57, size = 97, normalized size = 1.31

$$\frac{a^{\frac{3}{2}}\sqrt{x}}{4b\sqrt{1+\frac{bx}{a}}} + \frac{3\sqrt{a}x^{\frac{3}{2}}}{4\sqrt{1+\frac{bx}{a}}} - \frac{a^2 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{\frac{3}{2}}} + \frac{bx^{\frac{5}{2}}}{2\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)*(b*x+a)**(1/2), x)`

[Out] `a**(3/2)*sqrt(x)/(4*b*sqrt(1 + b*x/a)) + 3*sqrt(a)*x**(3/2)/(4*sqrt(1 + b*x/a)) - a**2*asinh(sqrt(b)*sqrt(x)/sqrt(a))/(4*b**(3/2)) + b*x**(5/2)/(2*sqrt(a)*sqrt(1 + b*x/a))`

$$3.492 \quad \int \frac{\sqrt{a+bx}}{\sqrt{x}} dx$$

Optimal. Leaf size=44

$$\sqrt{x} \sqrt{a+bx} + \frac{a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{\sqrt{b}}$$

[Out] a*arctanh(b^(1/2)*x^(1/2)/(b*x+a)^(1/2))/b^(1/2)+x^(1/2)*(b*x+a)^(1/2)

Rubi [A] time = 0.02, antiderivative size = 44, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$\sqrt{x} \sqrt{a+bx} + \frac{a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/Sqrt[x], x]

[Out] Sqrt[x]*Sqrt[a + b*x] + (a*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a + b*x]])/Sqrt[b]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[Rt[-b, 2]*x]/Rt[a, 2])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt

Q[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{a+bx}}{\sqrt{x}} dx &= \sqrt{x} \sqrt{a+bx} + \frac{1}{2}a \int \frac{1}{\sqrt{x} \sqrt{a+bx}} dx \\ &= \sqrt{x} \sqrt{a+bx} + a \operatorname{Subst} \left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x} \right) \\ &= \sqrt{x} \sqrt{a+bx} + a \operatorname{Subst} \left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}} \right) \\ &= \sqrt{x} \sqrt{a+bx} + \frac{a \tanh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a+bx}} \right)}{\sqrt{b}} \end{aligned}$$

Mathematica [A] time = 0.09, size = 62, normalized size = 1.41

$$\frac{a^{3/2} \sqrt{\frac{bx}{a}+1} \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right) + \sqrt{x} (a+bx)}{\sqrt{b} \sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/Sqrt[x], x]

[Out] (Sqrt[x]*(a + b*x) + (a^(3/2)*Sqrt[1 + (b*x)/a]*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[b])/Sqrt[a + b*x]

fricas [A] time = 0.45, size = 93, normalized size = 2.11

$$\left[\frac{a\sqrt{b} \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2\sqrt{bx+a}b\sqrt{x}}{2b}, -\frac{a\sqrt{-b} \arctan\left(\frac{\sqrt{bx+a}\sqrt{-b}}{b\sqrt{x}}\right) - \sqrt{bx+a}b\sqrt{x}}{b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(1/2),x, algorithm="fricas")

[Out] [1/2*(a*sqrt(b)*log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*sqrt(b*x + a)*b*sqrt(x))/b, -(a*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) - sqrt(b*x + a)*b*sqrt(x))/b]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.00, size = 62, normalized size = 1.41

$$\frac{\sqrt{(bx+a)x} a \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{2\sqrt{bx+a} \sqrt{b} \sqrt{x}} + \sqrt{bx+a} \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/x^(1/2),x)

[Out] x^(1/2)*(b*x+a)^(1/2)+1/2*a*((b*x+a)*x)^(1/2)/(b*x+a)^(1/2)/x^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))/b^(1/2)

maxima [B] time = 2.99, size = 70, normalized size = 1.59

$$-\frac{a \log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+a}}{\sqrt{x}}}\right)}{2\sqrt{b}} - \frac{\sqrt{bx+a} a}{\left(b-\frac{bx+a}{x}\right)\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(1/2),x, algorithm="maxima")

[Out] -1/2*a*log(-(sqrt(b) - sqrt(b*x + a)/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x)))/sqrt(b) - sqrt(b*x + a)*a/((b - (b*x + a)/x)*sqrt(x))

mupad [B] time = 0.68, size = 41, normalized size = 0.93

$$\sqrt{x} \sqrt{a+bx} + \frac{2a \operatorname{atanh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a+bx}-\sqrt{a}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/2)/x^(1/2), x)`

[Out] $x^{1/2}*(a + b*x)^{1/2} + (2*a*atanh((b^{1/2}*x^{1/2})/((a + b*x)^{1/2} - a^{1/2}))))/b^{1/2}$

sympy [A] time = 1.92, size = 42, normalized size = 0.95

$$\sqrt{a} \sqrt{x} \sqrt{1 + \frac{bx}{a}} + \frac{a \operatorname{asinh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/2)/x**(1/2), x)`

[Out] $\sqrt{a}*\sqrt{x}*\sqrt{1 + b*x/a} + a*\operatorname{asinh}(\sqrt{b}*\sqrt{x}/\sqrt{a})/\sqrt{b}$

$$3.493 \quad \int \frac{\sqrt{a+bx}}{x^{3/2}} dx$$

Optimal. Leaf size=45

$$2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right) - \frac{2\sqrt{a+bx}}{\sqrt{x}}$$

[Out] $2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)/(b*x+a)^{(1/2)})*b^{(1/2)}-2*(b*x+a)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 63, 217, 206}

$$2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right) - \frac{2\sqrt{a+bx}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/x^(3/2), x]

[Out] $(-2*\operatorname{Sqrt}[a + b*x])/ \operatorname{Sqrt}[x] + 2*\operatorname{Sqrt}[b]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/ \operatorname{Sqrt}[a + b*x]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt

$Q[a, 0] \parallel \text{LtQ}[b, 0]$

Rule 217

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^2], x_Symbol] \rightarrow \text{Subst}[\text{Int}[1/(1 - b*x^2), x], x, x/\text{Sqrt}[a + b*x^2]] /; \text{FreeQ}[\{a, b\}, x] \ \&\amp; \ !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{a+bx}}{x^{3/2}} dx &= -\frac{2\sqrt{a+bx}}{\sqrt{x}} + b \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx \\ &= -\frac{2\sqrt{a+bx}}{\sqrt{x}} + (2b) \text{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right) \\ &= -\frac{2\sqrt{a+bx}}{\sqrt{x}} + (2b) \text{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right) \\ &= -\frac{2\sqrt{a+bx}}{\sqrt{x}} + 2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right) \end{aligned}$$

Mathematica [A] time = 0.10, size = 64, normalized size = 1.42

$$\frac{2\left(\sqrt{a}\sqrt{b}\sqrt{\frac{bx}{a}+1} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) - \frac{a+bx}{\sqrt{x}}\right)}{\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/x^(3/2), x]

[Out] (2*(-((a + b*x)/Sqrt[x]) + Sqrt[a]*Sqrt[b]*Sqrt[1 + (b*x)/a]*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]]))/Sqrt[a + b*x]

fricas [A] time = 0.44, size = 89, normalized size = 1.98

$$\left[\frac{\sqrt{b}x \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) - 2\sqrt{bx+a}\sqrt{x}}{x}, -\frac{2\left(\sqrt{-b}x \arctan\left(\frac{\sqrt{bx+a}\sqrt{-b}}{b\sqrt{x}}\right) + \sqrt{bx+a}\sqrt{x}\right)}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(3/2), x, algorithm="fricas")

[Out] $[(\sqrt{b} \cdot x \cdot \log(2 \cdot b \cdot x + 2 \cdot \sqrt{b \cdot x + a}) \cdot \sqrt{b} \cdot \sqrt{x} + a) - 2 \cdot \sqrt{b \cdot x + a} \cdot \sqrt{x}) / x, -2 \cdot (\sqrt{-b} \cdot x \cdot \arctan(\sqrt{b \cdot x + a}) \cdot \sqrt{-b} / (b \cdot \sqrt{x})) + \sqrt{b \cdot x + a} \cdot \sqrt{x}) / x]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)/x^(3/2),x, algorithm="giac")`

[Out] Timed out

maple [A] time = 0.04, size = 61, normalized size = 1.36

$$\frac{\sqrt{(bx+a)x} \sqrt{b} \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{\sqrt{bx+a} \sqrt{x}} - \frac{2\sqrt{bx+a}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(1/2)/x^(3/2),x)`

[Out] $-2 \cdot (b \cdot x + a)^{1/2} / x^{1/2} + b^{1/2} \cdot \ln\left(\frac{(b \cdot x + 1/2 \cdot a)^{1/2}}{b^{1/2}} + (b \cdot x^2 + a \cdot x)^{1/2}\right) \cdot ((b \cdot x + a) \cdot x)^{1/2} / (b \cdot x + a)^{1/2} / x^{1/2}$

maxima [A] time = 3.00, size = 54, normalized size = 1.20

$$-\sqrt{b} \log\left(-\frac{\sqrt{b} - \frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+a}}{\sqrt{x}}}\right) - \frac{2\sqrt{bx+a}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)/x^(3/2),x, algorithm="maxima")`

[Out] $-\sqrt{b} \cdot \log\left(-\frac{\sqrt{b} - \sqrt{b \cdot x + a} / \sqrt{x}}{\sqrt{b} + \sqrt{b \cdot x + a} / \sqrt{x}}\right) - 2 \cdot \sqrt{b \cdot x + a} / \sqrt{x}$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{a + bx}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/2)/x^(3/2), x)`

[Out] `int((a + b*x)^(1/2)/x^(3/2), x)`

sympy [A] time = 1.56, size = 68, normalized size = 1.51

$$-\frac{2\sqrt{a}}{\sqrt{x}\sqrt{1+\frac{bx}{a}}} + 2\sqrt{b} \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) - \frac{2b\sqrt{x}}{\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/2)/x**(3/2), x)`

[Out] `-2*sqrt(a)/(sqrt(x)*sqrt(1 + b*x/a)) + 2*sqrt(b)*asinh(sqrt(b)*sqrt(x)/sqrt(a)) - 2*b*sqrt(x)/(sqrt(a)*sqrt(1 + b*x/a))`

$$3.494 \quad \int \frac{\sqrt{a+bx}}{x^{5/2}} dx$$

Optimal. Leaf size=21

$$-\frac{2(a+bx)^{3/2}}{3ax^{3/2}}$$

[Out] $-2/3*(b*x+a)^{(3/2)}/a/x^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$-\frac{2(a+bx)^{3/2}}{3ax^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/x^(5/2), x]

[Out] $(-2*(a + b*x)^{(3/2)})/(3*a*x^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{a+bx}}{x^{5/2}} dx = -\frac{2(a+bx)^{3/2}}{3ax^{3/2}}$$

Mathematica [A] time = 0.01, size = 21, normalized size = 1.00

$$-\frac{2(a+bx)^{3/2}}{3ax^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/x^(5/2), x]

[Out] $(-2*(a + b*x)^{(3/2)})/(3*a*x^{(3/2)})$

fricas [A] time = 0.41, size = 15, normalized size = 0.71

$$-\frac{2(bx+a)^{\frac{3}{2}}}{3ax^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(5/2),x, algorithm="fricas")

[Out] -2/3*(b*x + a)^(3/2)/(a*x^(3/2))

giac [B] time = 1.33, size = 33, normalized size = 1.57

$$-\frac{2(bx+a)^{\frac{3}{2}}b^4}{3((bx+a)b-ab)^{\frac{3}{2}}a|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(5/2),x, algorithm="giac")

[Out] -2/3*(b*x + a)^(3/2)*b^4/(((b*x + a)*b - a*b)^(3/2)*a*abs(b))

maple [A] time = 0.00, size = 16, normalized size = 0.76

$$-\frac{2(bx+a)^{\frac{3}{2}}}{3ax^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/x^(5/2),x)

[Out] -2/3*(b*x+a)^(3/2)/a/x^(3/2)

maxima [A] time = 1.36, size = 15, normalized size = 0.71

$$-\frac{2(bx+a)^{\frac{3}{2}}}{3ax^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(5/2),x, algorithm="maxima")

[Out] -2/3*(b*x + a)^(3/2)/(a*x^(3/2))

mupad [B] time = 0.24, size = 21, normalized size = 1.00

$$-\frac{\left(\frac{2bx}{3a} + \frac{2}{3}\right) \sqrt{a+bx}}{x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/2)/x^(5/2), x)`

[Out] `-(((2*b*x)/(3*a) + 2/3)*(a + b*x)^(1/2))/x^(3/2)`

sympy [B] time = 1.46, size = 41, normalized size = 1.95

$$-\frac{2\sqrt{b}\sqrt{\frac{a}{bx}+1}}{3x} - \frac{2b^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}}{3a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/2)/x**(5/2), x)`

[Out] `-2*sqrt(b)*sqrt(a/(b*x) + 1)/(3*x) - 2*b**(3/2)*sqrt(a/(b*x) + 1)/(3*a)`

$$3.495 \quad \int \frac{\sqrt{a+bx}}{x^{7/2}} dx$$

Optimal. Leaf size=44

$$\frac{4b(a+bx)^{3/2}}{15a^2x^{3/2}} - \frac{2(a+bx)^{3/2}}{5ax^{5/2}}$$

[Out] $-2/5*(b*x+a)^{(3/2)}/a/x^{(5/2)}+4/15*b*(b*x+a)^{(3/2)}/a^2/x^{(3/2)}$

Rubi [A] time = 0.01, antiderivative size = 44, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{4b(a+bx)^{3/2}}{15a^2x^{3/2}} - \frac{2(a+bx)^{3/2}}{5ax^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/x^(7/2), x]

[Out] $(-2*(a + b*x)^{(3/2)})/(5*a*x^{(5/2)}) + (4*b*(a + b*x)^{(3/2)})/(15*a^2*x^{(3/2)})$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{\sqrt{a+bx}}{x^{7/2}} dx = -\frac{2(a+bx)^{3/2}}{5ax^{5/2}} - \frac{(2b) \int \frac{\sqrt{a+bx}}{x^{5/2}} dx}{5a}$$

$$= -\frac{2(a+bx)^{3/2}}{5ax^{5/2}} + \frac{4b(a+bx)^{3/2}}{15a^2x^{3/2}}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 0.66

$$-\frac{2(3a-2bx)(a+bx)^{3/2}}{15a^2x^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/x^(7/2), x]

[Out] (-2*(3*a - 2*b*x)*(a + b*x)^(3/2))/(15*a^2*x^(5/2))

fricas [A] time = 0.43, size = 34, normalized size = 0.77

$$\frac{2(2b^2x^2 - abx - 3a^2)\sqrt{bx+a}}{15a^2x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(7/2), x, algorithm="fricas")

[Out] 2/15*(2*b^2*x^2 - a*b*x - 3*a^2)*sqrt(b*x + a)/(a^2*x^(5/2))

giac [A] time = 1.10, size = 50, normalized size = 1.14

$$\frac{2\left(\frac{2(bx+a)b^5}{a^2} - \frac{5b^5}{a}\right)(bx+a)^{\frac{3}{2}}b}{15((bx+a)b - ab)^{\frac{5}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(7/2), x, algorithm="giac")

[Out] 2/15*(2*(b*x + a)*b^5/a^2 - 5*b^5/a)*(b*x + a)^(3/2)*b/(((b*x + a)*b - a*b)^(5/2)*abs(b))

maple [A] time = 0.00, size = 24, normalized size = 0.55

$$-\frac{2(bx+a)^{\frac{3}{2}}(-2bx+3a)}{15a^2x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(1/2)/x^(7/2),x)`

[Out] $-2/15*(b*x+a)^{(3/2)*(-2*b*x+3*a)/x^{(5/2)}/a^2$

maxima [A] time = 1.29, size = 31, normalized size = 0.70

$$\frac{2 \left(\frac{5(bx+a)^{\frac{3}{2}} b}{x^2} - \frac{3(bx+a)^{\frac{5}{2}}}{x^2} \right)}{15a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)/x^(7/2),x, algorithm="maxima")`

[Out] $2/15*(5*(b*x + a)^{(3/2)*b/x^{(3/2)} - 3*(b*x + a)^{(5/2)/x^{(5/2)})/a^2$

mupad [B] time = 0.25, size = 32, normalized size = 0.73

$$-\frac{\sqrt{a+bx} \left(\frac{2bx}{15a} - \frac{4b^2x^2}{15a^2} + \frac{2}{5} \right)}{x^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/2)/x^(7/2),x)`

[Out] $-((a + b*x)^{(1/2)*((2*b*x)/(15*a) - (4*b^2*x^2)/(15*a^2) + 2/5))/x^{(5/2)}$

sympy [A] time = 4.88, size = 65, normalized size = 1.48

$$-\frac{2\sqrt{b}\sqrt{\frac{a}{bx}+1}}{5x^2} - \frac{2b^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}}{15ax} + \frac{4b^{\frac{5}{2}}\sqrt{\frac{a}{bx}+1}}{15a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/2)/x**(7/2),x)`

[Out] $-2*\sqrt{b}*\sqrt{a/(b*x) + 1}/(5*x**2) - 2*b**(3/2)*\sqrt{a/(b*x) + 1}/(15*a*x) + 4*b**(5/2)*\sqrt{a/(b*x) + 1}/(15*a**2)$

$$3.496 \quad \int \frac{\sqrt{a+bx}}{x^{9/2}} dx$$

Optimal. Leaf size=68

$$-\frac{16b^2(a+bx)^{3/2}}{105a^3x^{3/2}} + \frac{8b(a+bx)^{3/2}}{35a^2x^{5/2}} - \frac{2(a+bx)^{3/2}}{7ax^{7/2}}$$

[Out] $-2/7*(b*x+a)^{(3/2)}/a/x^{(7/2)}+8/35*b*(b*x+a)^{(3/2)}/a^2/x^{(5/2)}-16/105*b^2*(b*x+a)^{(3/2)}/a^3/x^{(3/2)}$

Rubi [A] time = 0.01, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{16b^2(a+bx)^{3/2}}{105a^3x^{3/2}} + \frac{8b(a+bx)^{3/2}}{35a^2x^{5/2}} - \frac{2(a+bx)^{3/2}}{7ax^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/x^(9/2), x]

[Out] $(-2*(a + b*x)^{(3/2)})/(7*a*x^{(7/2)}) + (8*b*(a + b*x)^{(3/2)})/(35*a^2*x^{(5/2)}) - (16*b^2*(a + b*x)^{(3/2)})/(105*a^3*x^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{a+bx}}{x^{9/2}} dx &= -\frac{2(a+bx)^{3/2}}{7ax^{7/2}} - \frac{(4b) \int \frac{\sqrt{a+bx}}{x^{7/2}} dx}{7a} \\
&= -\frac{2(a+bx)^{3/2}}{7ax^{7/2}} + \frac{8b(a+bx)^{3/2}}{35a^2x^{5/2}} + \frac{(8b^2) \int \frac{\sqrt{a+bx}}{x^{5/2}} dx}{35a^2} \\
&= -\frac{2(a+bx)^{3/2}}{7ax^{7/2}} + \frac{8b(a+bx)^{3/2}}{35a^2x^{5/2}} - \frac{16b^2(a+bx)^{3/2}}{105a^3x^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 0.59

$$-\frac{2(a+bx)^{3/2}(15a^2-12abx+8b^2x^2)}{105a^3x^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/x^(9/2), x]

[Out] (-2*(a + b*x)^(3/2)*(15*a^2 - 12*a*b*x + 8*b^2*x^2))/(105*a^3*x^(7/2))

fricas [A] time = 0.42, size = 45, normalized size = 0.66

$$-\frac{2(8b^3x^3 - 4ab^2x^2 + 3a^2bx + 15a^3)\sqrt{bx+a}}{105a^3x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(9/2), x, algorithm="fricas")

[Out] -2/105*(8*b^3*x^3 - 4*a*b^2*x^2 + 3*a^2*b*x + 15*a^3)*sqrt(b*x + a)/(a^3*x^(7/2))

giac [A] time = 0.97, size = 66, normalized size = 0.97

$$-\frac{2\left(\frac{35b^7}{a} + 4\left(\frac{2(bx+a)b^7}{a^3} - \frac{7b^7}{a^2}\right)(bx+a)\right)(bx+a)^{\frac{3}{2}}b}{105((bx+a)b - ab)^{\frac{7}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(9/2), x, algorithm="giac")

[Out] -2/105*(35*b^7/a + 4*(2*(b*x + a)*b^7/a^3 - 7*b^7/a^2)*(b*x + a))*(b*x + a)^(3/2)*b/(((b*x + a)*b - a*b)^(7/2)*abs(b))

maple [A] time = 0.00, size = 35, normalized size = 0.51

$$\frac{2(bx+a)^{\frac{3}{2}}(8b^2x^2-12abx+15a^2)}{105a^3x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/x^(9/2),x)

[Out] -2/105*(b*x+a)^(3/2)*(8*b^2*x^2-12*a*b*x+15*a^2)/x^(7/2)/a^3

maxima [A] time = 1.35, size = 46, normalized size = 0.68

$$\frac{2\left(\frac{35(bx+a)^{\frac{3}{2}}b^2}{x^{\frac{3}{2}}}-\frac{42(bx+a)^{\frac{5}{2}}b}{x^{\frac{5}{2}}}+\frac{15(bx+a)^{\frac{7}{2}}}{x^{\frac{7}{2}}}\right)}{105a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/x^(9/2),x, algorithm="maxima")

[Out] -2/105*(35*(b*x + a)^(3/2)*b^2/x^(3/2) - 42*(b*x + a)^(5/2)*b/x^(5/2) + 15*(b*x + a)^(7/2)/x^(7/2))/a^3

mupad [B] time = 0.26, size = 43, normalized size = 0.63

$$\frac{\sqrt{a+bx}\left(\frac{16b^3x^3}{105a^3}-\frac{8b^2x^2}{105a^2}+\frac{2bx}{35a}+\frac{2}{7}\right)}{x^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/x^(9/2),x)

[Out] -((a + b*x)^(1/2)*((16*b^3*x^3)/(105*a^3) - (8*b^2*x^2)/(105*a^2) + (2*b*x)/(35*a) + 2/7))/x^(7/2)

sympy [B] time = 13.77, size = 347, normalized size = 5.10

$$\frac{30a^5b^{\frac{9}{2}}\sqrt{\frac{a}{bx}+1}}{105a^5b^4x^3+210a^4b^5x^4+105a^3b^6x^5}-\frac{66a^4b^{\frac{11}{2}}x\sqrt{\frac{a}{bx}+1}}{105a^5b^4x^3+210a^4b^5x^4+105a^3b^6x^5}-\frac{34a^3b^{\frac{13}{2}}x^2\sqrt{\frac{a}{bx}+1}}{105a^5b^4x^3+210a^4b^5x^4+105a^3b^6x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/x**(9/2),x)

```
[Out] -30*a**5*b**(9/2)*sqrt(a/(b*x) + 1)/(105*a**5*b**4*x**3 + 210*a**4*b**5*x**
4 + 105*a**3*b**6*x**5) - 66*a**4*b**(11/2)*x*sqrt(a/(b*x) + 1)/(105*a**5*b
**4*x**3 + 210*a**4*b**5*x**4 + 105*a**3*b**6*x**5) - 34*a**3*b**(13/2)*x**
2*sqrt(a/(b*x) + 1)/(105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 + 105*a**3*b**
6*x**5) - 6*a**2*b**(15/2)*x**3*sqrt(a/(b*x) + 1)/(105*a**5*b**4*x**3 + 210
*a**4*b**5*x**4 + 105*a**3*b**6*x**5) - 24*a*b**(17/2)*x**4*sqrt(a/(b*x) +
1)/(105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 + 105*a**3*b**6*x**5) - 16*b**
(19/2)*x**5*sqrt(a/(b*x) + 1)/(105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 + 105
*a**3*b**6*x**5)
```


3.497 $\int x^{5/2} \sqrt{a - bx} dx$

Optimal. Leaf size=127

$$\frac{5a^4 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{64b^{7/2}} - \frac{5a^3 \sqrt{x} \sqrt{a-bx}}{64b^3} - \frac{5a^2 x^{3/2} \sqrt{a-bx}}{96b^2} - \frac{ax^{5/2} \sqrt{a-bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a-bx}$$

[Out] $5/64*a^4*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(7/2)}-5/96*a^2*x^{(3/2)}*(-b*x+a)^{(1/2)}/b^2-1/24*a*x^{(5/2)}*(-b*x+a)^{(1/2)}/b+1/4*x^{(7/2)}*(-b*x+a)^{(1/2)}-5/64*a^3*x^{(1/2)}*(-b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.04, antiderivative size = 127, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$-\frac{5a^2 x^{3/2} \sqrt{a-bx}}{96b^2} - \frac{5a^3 \sqrt{x} \sqrt{a-bx}}{64b^3} + \frac{5a^4 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{64b^{7/2}} - \frac{ax^{5/2} \sqrt{a-bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a-bx}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)*Sqrt[a - b*x],x]

[Out] $(-5*a^3*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(64*b^3) - (5*a^2*x^{(3/2)}*\text{Sqrt}[a - b*x])/(96*b^2) - (a*x^{(5/2)}*\text{Sqrt}[a - b*x])/(24*b) + (x^{(7/2)}*\text{Sqrt}[a - b*x])/4 + (5*a^4*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(64*b^{(7/2)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

```
Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
 \int x^{5/2} \sqrt{a-bx} \, dx &= \frac{1}{4} x^{7/2} \sqrt{a-bx} + \frac{1}{8} a \int \frac{x^{5/2}}{\sqrt{a-bx}} \, dx \\
 &= -\frac{ax^{5/2} \sqrt{a-bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a-bx} + \frac{(5a^2) \int \frac{x^{3/2}}{\sqrt{a-bx}} \, dx}{48b} \\
 &= -\frac{5a^2 x^{3/2} \sqrt{a-bx}}{96b^2} - \frac{ax^{5/2} \sqrt{a-bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a-bx} + \frac{(5a^3) \int \frac{\sqrt{x}}{\sqrt{a-bx}} \, dx}{64b^2} \\
 &= -\frac{5a^3 \sqrt{x} \sqrt{a-bx}}{64b^3} - \frac{5a^2 x^{3/2} \sqrt{a-bx}}{96b^2} - \frac{ax^{5/2} \sqrt{a-bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a-bx} + \frac{(5a^4) \int \frac{1}{\sqrt{x} \sqrt{a-bx}} \, dx}{128b^3} \\
 &= -\frac{5a^3 \sqrt{x} \sqrt{a-bx}}{64b^3} - \frac{5a^2 x^{3/2} \sqrt{a-bx}}{96b^2} - \frac{ax^{5/2} \sqrt{a-bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a-bx} + \frac{(5a^4) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a-bx}} \, dx\right)}{64b^3} \\
 &= -\frac{5a^3 \sqrt{x} \sqrt{a-bx}}{64b^3} - \frac{5a^2 x^{3/2} \sqrt{a-bx}}{96b^2} - \frac{ax^{5/2} \sqrt{a-bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a-bx} + \frac{(5a^4) \operatorname{Subst}\left(\int \frac{1}{1+bx} \, dx\right)}{64b^3} \\
 &= -\frac{5a^3 \sqrt{x} \sqrt{a-bx}}{64b^3} - \frac{5a^2 x^{3/2} \sqrt{a-bx}}{96b^2} - \frac{ax^{5/2} \sqrt{a-bx}}{24b} + \frac{1}{4} x^{7/2} \sqrt{a-bx} + \frac{5a^4 \tan^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a-bx}}\right)}{64b^{7/2}}
 \end{aligned}$$

Mathematica [A] time = 0.14, size = 98, normalized size = 0.77

$$\frac{\sqrt{a-bx} \left(\frac{15a^{7/2} \sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{1-\frac{bx}{a}}} + \sqrt{b} \sqrt{x} (-15a^3 - 10a^2 bx - 8ab^2 x^2 + 48b^3 x^3) \right)}{192b^{7/2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(5/2)*Sqrt[a - b*x], x]
```

[Out] $(\sqrt{a - bx} * (\sqrt{b} * \sqrt{x} * (-15a^3 - 10a^2bx - 8ab^2x^2 + 48b^3x^3) + (15a^{7/2} * \text{ArcSin}[(\sqrt{b} * \sqrt{x}) / \sqrt{a}]) / \sqrt{1 - (bx)/a})) / (192b^{7/2})$

fricas [A] time = 0.45, size = 164, normalized size = 1.29

$$\left[\frac{15a^4\sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) - 2(48b^4x^3 - 8ab^3x^2 - 10a^2b^2x - 15a^3b)\sqrt{-bx+a}\sqrt{x}}{384b^4}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/2)*(-b*x+a)^(1/2),x, algorithm="fricas")`

[Out] $[-1/384*(15a^4*\sqrt{-b}*\log(-2bx + 2*\sqrt{-bx+a}*\sqrt{-b}*\sqrt{x} + a) - 2*(48b^4*x^3 - 8a*b^3*x^2 - 10a^2*b^2*x - 15a^3*b)*\sqrt{-bx+a}*\sqrt{x})/b^4, -1/192*(15a^4*\sqrt{b}*\arctan(\sqrt{-bx+a}/(\sqrt{b}*\sqrt{x})) - (48b^4*x^3 - 8a*b^3*x^2 - 10a^2*b^2*x - 15a^3*b)*\sqrt{-bx+a}*\sqrt{x})/b^4]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/2)*(-b*x+a)^(1/2),x, algorithm="giac")`

[Out] Timed out

maple [A] time = 0.01, size = 127, normalized size = 1.00

$$-\frac{(-bx+a)^{\frac{3}{2}}x^{\frac{5}{2}}}{4b} + \frac{5\sqrt{-bx+a}x a^4 \arctan\left(\frac{(x-\frac{a}{2b})\sqrt{b}}{\sqrt{-bx+a}}\right)}{128\sqrt{-bx+a}b^{\frac{7}{2}}\sqrt{x}} + \frac{5\sqrt{-bx+a}a^3\sqrt{x}}{64b^3} - \frac{5(-bx+a)^{\frac{3}{2}}ax^{\frac{3}{2}}}{24b^2} - \frac{5(-bx+a)^{\frac{3}{2}}a^2}{32b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/2)*(-b*x+a)^(1/2),x)`

[Out] $-1/4/b*x^{5/2}*(-b*x+a)^{3/2} - 5/24*a/b^2*x^{3/2}*(-b*x+a)^{3/2} - 5/32*a^2/b^3*x^{1/2}*(-b*x+a)^{3/2} + 5/64*a^3*x^{1/2}*(-b*x+a)^{1/2}/b^3 + 5/128*a^4/b^{7/2}*(x*(-b*x+a))^{1/2}/(-b*x+a)^{1/2}/x^{1/2}*\arctan(b^{1/2}*(x-1/2*a/b)/(-b*x^2+a*x)^{1/2})$

maxima [A] time = 3.01, size = 170, normalized size = 1.34

$$-\frac{5a^4 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{64b^{\frac{7}{2}}} + \frac{15\sqrt{-bx+a}a^4b^3}{\sqrt{x}} - \frac{73(-bx+a)^{\frac{3}{2}}a^4b^2}{x^{\frac{3}{2}}} - \frac{55(-bx+a)^{\frac{5}{2}}a^4b}{x^{\frac{5}{2}}} - \frac{15(-bx+a)^{\frac{7}{2}}a^4}{x^{\frac{7}{2}}}$$

$$192\left(b^7 - \frac{4(bx-a)b^6}{x} + \frac{6(bx-a)^2b^5}{x^2} - \frac{4(bx-a)^3b^4}{x^3} + \frac{(bx-a)^4b^3}{x^4}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(-b*x+a)^(1/2),x, algorithm="maxima")

[Out] $-5/64*a^4*\arctan(\sqrt{-b*x + a}/(\sqrt{b}*\sqrt{x}))/b^{(7/2)} + 1/192*(15*\sqrt{-b*x + a}*a^4*b^3/\sqrt{x} - 73*(-b*x + a)^{(3/2)}*a^4*b^2/x^{(3/2)} - 55*(-b*x + a)^{(5/2)}*a^4*b/x^{(5/2)} - 15*(-b*x + a)^{(7/2)}*a^4/x^{(7/2)})/(b^7 - 4*(b*x - a)*b^6/x + 6*(b*x - a)^2*b^5/x^2 - 4*(b*x - a)^3*b^4/x^3 + (b*x - a)^4*b^3/x^4)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} \sqrt{a - bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(a - b*x)^(1/2),x)

[Out] int(x^(5/2)*(a - b*x)^(1/2), x)

sympy [A] time = 11.65, size = 323, normalized size = 2.54

$$\left\{ \begin{array}{l} \frac{5ia^{\frac{7}{2}}\sqrt{x}}{64b^3\sqrt{-1+\frac{bx}{a}}} - \frac{5ia^{\frac{5}{2}}x^{\frac{3}{2}}}{192b^2\sqrt{-1+\frac{bx}{a}}} - \frac{ia^{\frac{3}{2}}x^{\frac{5}{2}}}{96b\sqrt{-1+\frac{bx}{a}}} - \frac{7i\sqrt{a}x^{\frac{7}{2}}}{24\sqrt{-1+\frac{bx}{a}}} - \frac{5ia^4 \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{64b^{\frac{7}{2}}} + \frac{ibx^{\frac{9}{2}}}{4\sqrt{a}\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{5a^{\frac{7}{2}}\sqrt{x}}{64b^3\sqrt{1-\frac{bx}{a}}} + \frac{5a^{\frac{5}{2}}x^{\frac{3}{2}}}{192b^2\sqrt{1-\frac{bx}{a}}} + \frac{a^{\frac{3}{2}}x^{\frac{5}{2}}}{96b\sqrt{1-\frac{bx}{a}}} + \frac{7\sqrt{a}x^{\frac{7}{2}}}{24\sqrt{1-\frac{bx}{a}}} + \frac{5a^4 \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{64b^{\frac{7}{2}}} - \frac{bx^{\frac{9}{2}}}{4\sqrt{a}\sqrt{1-\frac{bx}{a}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)*(-b*x+a)**(1/2),x)

[Out] Piecewise((5*I*a**(7/2)*sqrt(x)/(64*b**3*sqrt(-1 + b*x/a)) - 5*I*a**(5/2)*x**(3/2)/(192*b**2*sqrt(-1 + b*x/a)) - I*a**(3/2)*x**(5/2)/(96*b*sqrt(-1 + b*x/a)) - 7*I*sqrt(a)*x**(7/2)/(24*sqrt(-1 + b*x/a)) - 5*I*a**4*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(64*b**(7/2)) + I*b*x**(9/2)/(4*sqrt(a)*sqrt(-1 + b*x/a))

```
), Abs(b*x/a) > 1), (-5*a**(7/2)*sqrt(x)/(64*b**3*sqrt(1 - b*x/a)) + 5*a**  
5/2)*x**(3/2)/(192*b**2*sqrt(1 - b*x/a)) + a**(3/2)*x**(5/2)/(96*b*sqrt(1 -  
b*x/a)) + 7*sqrt(a)*x**(7/2)/(24*sqrt(1 - b*x/a)) + 5*a**4*asin(sqrt(b)*sq  
rt(x)/sqrt(a))/(64*b**(7/2)) - b*x**(9/2)/(4*sqrt(a)*sqrt(1 - b*x/a)), True  
)
```

3.498 $\int x^{3/2} \sqrt{a - bx} dx$

Optimal. Leaf size=102

$$\frac{a^3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{8b^{5/2}} - \frac{a^2\sqrt{x}\sqrt{a-bx}}{8b^2} - \frac{ax^{3/2}\sqrt{a-bx}}{12b} + \frac{1}{3}x^{5/2}\sqrt{a-bx}$$

[Out] $1/8*a^3*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(5/2)}-1/12*a*x^{(3/2)}*(-b*x+a)^{(1/2)}/b+1/3*x^{(5/2)}*(-b*x+a)^{(1/2)}-1/8*a^2*x^{(1/2)}*(-b*x+a)^{(1/2)}/b^2$

Rubi [A] time = 0.03, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$-\frac{a^2\sqrt{x}\sqrt{a-bx}}{8b^2} + \frac{a^3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{8b^{5/2}} - \frac{ax^{3/2}\sqrt{a-bx}}{12b} + \frac{1}{3}x^{5/2}\sqrt{a-bx}$$

Antiderivative was successfully verified.

[In] `Int[x^(3/2)*Sqrt[a - b*x], x]`

[Out] $-(a^2*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(8*b^2) - (a*x^{(3/2)}*\text{Sqrt}[a - b*x])/(12*b) + (x^{(5/2)}*\text{Sqrt}[a - b*x])/3 + (a^3*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(8*b^{(5/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

`Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])`

Rule 217

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]`

Rubi steps

$$\begin{aligned}
 \int x^{3/2} \sqrt{a-bx} \, dx &= \frac{1}{3} x^{5/2} \sqrt{a-bx} + \frac{1}{6} a \int \frac{x^{3/2}}{\sqrt{a-bx}} \, dx \\
 &= -\frac{ax^{3/2} \sqrt{a-bx}}{12b} + \frac{1}{3} x^{5/2} \sqrt{a-bx} + \frac{a^2 \int \frac{\sqrt{x}}{\sqrt{a-bx}} \, dx}{8b} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a-bx}}{8b^2} - \frac{ax^{3/2} \sqrt{a-bx}}{12b} + \frac{1}{3} x^{5/2} \sqrt{a-bx} + \frac{a^3 \int \frac{1}{\sqrt{x} \sqrt{a-bx}} \, dx}{16b^2} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a-bx}}{8b^2} - \frac{ax^{3/2} \sqrt{a-bx}}{12b} + \frac{1}{3} x^{5/2} \sqrt{a-bx} + \frac{a^3 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} \, dx, x, \sqrt{x}\right)}{8b^2} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a-bx}}{8b^2} - \frac{ax^{3/2} \sqrt{a-bx}}{12b} + \frac{1}{3} x^{5/2} \sqrt{a-bx} + \frac{a^3 \operatorname{Subst}\left(\int \frac{1}{1+bx^2} \, dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right)}{8b^2} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a-bx}}{8b^2} - \frac{ax^{3/2} \sqrt{a-bx}}{12b} + \frac{1}{3} x^{5/2} \sqrt{a-bx} + \frac{a^3 \tan^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a-bx}}\right)}{8b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.12, size = 87, normalized size = 0.85

$$\frac{\sqrt{a-bx} \left(\frac{3a^{5/2} \sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{1-\frac{bx}{a}}} + \sqrt{b} \sqrt{x} (-3a^2 - 2abx + 8b^2x^2) \right)}{24b^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*Sqrt[a - b*x], x]

[Out] (Sqrt[a - b*x]*(Sqrt[b]*Sqrt[x]*(-3*a^2 - 2*a*b*x + 8*b^2*x^2) + (3*a^(5/2)*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 - (b*x)/a])/(24*b^(5/2))

fricas [A] time = 0.44, size = 142, normalized size = 1.39

$$\left[\frac{3 a^3 \sqrt{-b} \log(-2 b x + 2 \sqrt{-b x + a} \sqrt{-b} \sqrt{x} + a) - 2 (8 b^3 x^2 - 2 a b^2 x - 3 a^2 b) \sqrt{-b x + a} \sqrt{x}}{48 b^3}, \frac{3 a^3 \sqrt{b} \arctan\left(\frac{(x - \frac{a}{2b}) \sqrt{b}}{\sqrt{-b x^2 + a x}}\right)}{16 \sqrt{-b x + a} b^{\frac{5}{2}} \sqrt{x}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+a)^(1/2),x, algorithm="fricas")

[Out] [-1/48*(3*a^3*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*(8*b^3*x^2 - 2*a*b^2*x - 3*a^2*b)*sqrt(-b*x + a)*sqrt(x))/b^3, -1/24*(3*a^3*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - (8*b^3*x^2 - 2*a*b^2*x - 3*a^2*b)*sqrt(-b*x + a)*sqrt(x))/b^3]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 108, normalized size = 1.06

$$\frac{\sqrt{-b x + a} x a^3 \arctan\left(\frac{(x - \frac{a}{2b}) \sqrt{b}}{\sqrt{-b x^2 + a x}}\right)}{16 \sqrt{-b x + a} b^{\frac{5}{2}} \sqrt{x}} + \frac{\sqrt{-b x + a} a^2 \sqrt{x}}{8 b^2} - \frac{(-b x + a)^{\frac{3}{2}} x^{\frac{3}{2}}}{3 b} - \frac{(-b x + a)^{\frac{3}{2}} a \sqrt{x}}{4 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(-b*x+a)^(1/2),x)

[Out] -1/3/b*x^(3/2)*(-b*x+a)^(3/2)-1/4*a/b^2*x^(1/2)*(-b*x+a)^(3/2)+1/8*a^2*x^(1/2)*(-b*x+a)^(1/2)/b^2+1/16*a^3/b^(5/2)*((-b*x+a)*x)^(1/2)/(-b*x+a)^(1/2)/x^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))

maxima [A] time = 2.99, size = 135, normalized size = 1.32

$$-\frac{a^3 \arctan\left(\frac{\sqrt{-b x + a}}{\sqrt{b} \sqrt{x}}\right)}{8 b^{\frac{5}{2}}} + \frac{\frac{3 \sqrt{-b x + a} a^3 b^2}{\sqrt{x}} - \frac{8 (-b x + a)^{\frac{3}{2}} a^3 b}{x^{\frac{3}{2}}} - \frac{3 (-b x + a)^{\frac{5}{2}} a^3}{x^{\frac{5}{2}}}}{24 \left(b^5 - \frac{3 (b x - a) b^4}{x} + \frac{3 (b x - a)^2 b^3}{x^2} - \frac{(b x - a)^3 b^2}{x^3} \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+a)^(1/2),x, algorithm="maxima")

[Out] $-1/8*a^3*\arctan(\sqrt{-b*x + a}/(\sqrt{b}*\sqrt{x}))/b^{5/2} + 1/24*(3*\sqrt{-b*x + a})*a^3*b^2/\sqrt{x} - 8*(-b*x + a)^{(3/2)}*a^3*b/x^{(3/2)} - 3*(-b*x + a)^{(5/2)}*a^3/x^{(5/2)}/(b^5 - 3*(b*x - a)*b^4/x + 3*(b*x - a)^2*b^3/x^2 - (b*x - a)^3*b^2/x^3)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} \sqrt{a - bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(a - b*x)^(1/2),x)

[Out] int(x^(3/2)*(a - b*x)^(1/2), x)

sympy [A] time = 6.33, size = 260, normalized size = 2.55

$$\begin{cases} \frac{ia^{\frac{5}{2}}\sqrt{x}}{8b^2\sqrt{-1+\frac{bx}{a}}} - \frac{ia^{\frac{3}{2}}x^{\frac{3}{2}}}{24b\sqrt{-1+\frac{bx}{a}}} - \frac{5i\sqrt{a}x^{\frac{5}{2}}}{12\sqrt{-1+\frac{bx}{a}}} - \frac{ia^3\operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8b^{\frac{5}{2}}} + \frac{ibx^{\frac{7}{2}}}{3\sqrt{a}\sqrt{-1+\frac{bx}{a}}} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{a^{\frac{5}{2}}\sqrt{x}}{8b^2\sqrt{1-\frac{bx}{a}}} + \frac{a^{\frac{3}{2}}x^{\frac{3}{2}}}{24b\sqrt{1-\frac{bx}{a}}} + \frac{5\sqrt{a}x^{\frac{5}{2}}}{12\sqrt{1-\frac{bx}{a}}} + \frac{a^3\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8b^{\frac{5}{2}}} - \frac{bx^{\frac{7}{2}}}{3\sqrt{a}\sqrt{1-\frac{bx}{a}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)*(-b*x+a)**(1/2),x)

[Out] Piecewise((I*a**(5/2)*sqrt(x)/(8*b**2*sqrt(-1 + b*x/a)) - I*a**(3/2)*x**(3/2)/(24*b*sqrt(-1 + b*x/a)) - 5*I*sqrt(a)*x**(5/2)/(12*sqrt(-1 + b*x/a)) - I*a**3*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(8*b**(5/2)) + I*b*x**(7/2)/(3*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (-a**(5/2)*sqrt(x)/(8*b**2*sqrt(1 - b*x/a)) + a**(3/2)*x**(3/2)/(24*b*sqrt(1 - b*x/a)) + 5*sqrt(a)*x**(5/2)/(12*sqrt(1 - b*x/a)) + a**3*asin(sqrt(b)*sqrt(x)/sqrt(a))/(8*b**(5/2)) - b*x**(7/2)/(3*sqrt(a)*sqrt(1 - b*x/a)), True))

3.499 $\int \sqrt{x} \sqrt{a - bx} dx$

Optimal. Leaf size=77

$$\frac{a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^{3/2}} + \frac{1}{2}x^{3/2}\sqrt{a-bx} - \frac{a\sqrt{x}\sqrt{a-bx}}{4b}$$

[Out] $1/4*a^2*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(3/2)}+1/2*x^{(3/2)}*(-b*x+a)^{(1/2)}-1/4*a*x^{(1/2)}*(-b*x+a)^{(1/2)}/b$

Rubi [A] time = 0.02, antiderivative size = 77, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$\frac{a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^{3/2}} + \frac{1}{2}x^{3/2}\sqrt{a-bx} - \frac{a\sqrt{x}\sqrt{a-bx}}{4b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*Sqrt[a - b*x], x]

[Out] $-(a*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(4*b) + (x^{(3/2)}*\text{Sqrt}[a - b*x])/2 + (a^2*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(4*b^{(3/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
```

, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \sqrt{x} \sqrt{a-bx} \, dx &= \frac{1}{2} x^{3/2} \sqrt{a-bx} + \frac{1}{4} a \int \frac{\sqrt{x}}{\sqrt{a-bx}} \, dx \\
 &= -\frac{a\sqrt{x}\sqrt{a-bx}}{4b} + \frac{1}{2} x^{3/2} \sqrt{a-bx} + \frac{a^2 \int \frac{1}{\sqrt{x}\sqrt{a-bx}} \, dx}{8b} \\
 &= -\frac{a\sqrt{x}\sqrt{a-bx}}{4b} + \frac{1}{2} x^{3/2} \sqrt{a-bx} + \frac{a^2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} \, dx, x, \sqrt{x}\right)}{4b} \\
 &= -\frac{a\sqrt{x}\sqrt{a-bx}}{4b} + \frac{1}{2} x^{3/2} \sqrt{a-bx} + \frac{a^2 \operatorname{Subst}\left(\int \frac{1}{1+bx^2} \, dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right)}{4b} \\
 &= -\frac{a\sqrt{x}\sqrt{a-bx}}{4b} + \frac{1}{2} x^{3/2} \sqrt{a-bx} + \frac{a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^{3/2}}
 \end{aligned}$$

Mathematica [A] time = 0.10, size = 75, normalized size = 0.97

$$\frac{\sqrt{a-bx} \left(\frac{a^{3/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{1-\frac{bx}{a}}} + \sqrt{b}\sqrt{x}(2bx-a) \right)}{4b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*Sqrt[a - b*x], x]

[Out] (Sqrt[a - b*x]*(Sqrt[b]*Sqrt[x]*(-a + 2*b*x) + (a^(3/2)*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 - (b*x)/a]))/(4*b^(3/2))

fricas [A] time = 0.46, size = 118, normalized size = 1.53

$$\left[\frac{a^2 \sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) - 2(2b^2x - ab)\sqrt{-bx+a}\sqrt{x}}{8b^2}, \frac{a^2 \sqrt{b} \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right) - (2b}{4b^2} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(-b*x+a)^(1/2),x, algorithm="fricas")

[Out] [-1/8*(a^2*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*(2*b^2*x - a*b)*sqrt(-b*x + a)*sqrt(x))/b^2, -1/4*(a^2*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - (2*b^2*x - a*b)*sqrt(-b*x + a)*sqrt(x))/b^2]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(-b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 86, normalized size = 1.12

$$\frac{\sqrt{-bx+a} x^{\frac{3}{2}}}{2} + \frac{\sqrt{-bx+a} x a^2 \arctan\left(\frac{\left(x-\frac{a}{2b}\right)\sqrt{b}}{\sqrt{-bx+a}}\right)}{8\sqrt{-bx+a} b^{\frac{3}{2}}\sqrt{x}} - \frac{\sqrt{-bx+a} a\sqrt{x}}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)*(-b*x+a)^(1/2),x)

[Out] 1/2*x^(3/2)*(-b*x+a)^(1/2)-1/4*a*x^(1/2)*(-b*x+a)^(1/2)/b+1/8*a^2/b^(3/2)*((-b*x+a)*x)^(1/2)/x^(1/2)/(-b*x+a)^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2))*b^(1/2))

maxima [A] time = 2.97, size = 95, normalized size = 1.23

$$-\frac{a^2 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{4b^{\frac{3}{2}}} + \frac{\frac{\sqrt{-bx+a} a^2 b}{\sqrt{x}} - \frac{(-bx+a)^{\frac{3}{2}} a^2}{x^{\frac{3}{2}}}}{4\left(b^3 - \frac{2(bx-a)b^2}{x} + \frac{(bx-a)^2 b}{x^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(-b*x+a)^(1/2),x, algorithm="maxima")

[Out] -1/4*a^2*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/b^(3/2) + 1/4*(sqrt(-b*x + a)*a^2*b/sqrt(x) - (-b*x + a)^(3/2)*a^2/x^(3/2))/(b^3 - 2*(b*x - a)*b^2/x + (b*x - a)^2*b/x^2)

mupad [B] time = 0.08, size = 58, normalized size = 0.75

$$\sqrt{x} \left(\frac{x}{2} - \frac{a}{4b} \right) \sqrt{a-bx} - \frac{a^2 \ln(a - 2bx + 2\sqrt{-b} \sqrt{x} \sqrt{a-bx})}{8(-b)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)*(a - b*x)^(1/2),x)`

[Out] `x^(1/2)*(x/2 - a/(4*b))*(a - b*x)^(1/2) - (a^2*log(a - 2*b*x + 2*(-b)^(1/2)*x^(1/2)*(a - b*x)^(1/2)))/(8*(-b)^(3/2))`

sympy [A] time = 3.60, size = 207, normalized size = 2.69

$$\begin{cases} \frac{ia^2 \sqrt{x}}{4b \sqrt{-1 + \frac{bx}{a}}} - \frac{3i \sqrt{a} x^{\frac{3}{2}}}{4 \sqrt{-1 + \frac{bx}{a}}} - \frac{ia^2 \operatorname{acosh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{4b^{\frac{3}{2}}} + \frac{ibx^{\frac{5}{2}}}{2\sqrt{a} \sqrt{-1 + \frac{bx}{a}}} & \text{for } \left| \frac{bx}{a} \right| > 1 \\ -\frac{a^2 \sqrt{x}}{4b \sqrt{1 - \frac{bx}{a}}} + \frac{3\sqrt{a} x^{\frac{3}{2}}}{4 \sqrt{1 - \frac{bx}{a}}} + \frac{a^2 \operatorname{asin}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{4b^{\frac{3}{2}}} - \frac{bx^{\frac{5}{2}}}{2\sqrt{a} \sqrt{1 - \frac{bx}{a}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)*(-b*x+a)**(1/2),x)`

[Out] `Piecewise((I*a**(3/2)*sqrt(x)/(4*b*sqrt(-1 + b*x/a)) - 3*I*sqrt(a)*x**(3/2)/(4*sqrt(-1 + b*x/a)) - I*a**2*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(4*b**(3/2)) + I*b*x**(5/2)/(2*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (-a**(3/2)*sqrt(x)/(4*b*sqrt(1 - b*x/a)) + 3*sqrt(a)*x**(3/2)/(4*sqrt(1 - b*x/a)) + a**2*asin(sqrt(b)*sqrt(x)/sqrt(a))/(4*b**(3/2)) - b*x**(5/2)/(2*sqrt(a)*sqrt(1 - b*x/a)), True)`

$$3.500 \quad \int \frac{\sqrt{a-bx}}{\sqrt{x}} dx$$

Optimal. Leaf size=46

$$\sqrt{x} \sqrt{a-bx} + \frac{a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{\sqrt{b}}$$

[Out] a*arctan(b^(1/2)*x^(1/2)/(-b*x+a)^(1/2))/b^(1/2)+x^(1/2)*(-b*x+a)^(1/2)

Rubi [A] time = 0.02, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$\sqrt{x} \sqrt{a-bx} + \frac{a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a - b*x]/Sqrt[x],x]

[Out] Sqrt[x]*Sqrt[a - b*x] + (a*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a - b*x]])/Sqrt[b]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
```

, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{a-bx}}{\sqrt{x}} dx &= \sqrt{x} \sqrt{a-bx} + \frac{1}{2} a \int \frac{1}{\sqrt{x} \sqrt{a-bx}} dx \\ &= \sqrt{x} \sqrt{a-bx} + a \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x} \right) \\ &= \sqrt{x} \sqrt{a-bx} + a \operatorname{Subst} \left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}} \right) \\ &= \sqrt{x} \sqrt{a-bx} + \frac{a \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a-bx}} \right)}{\sqrt{b}} \end{aligned}$$

Mathematica [A] time = 0.09, size = 65, normalized size = 1.41

$$\frac{\frac{a^{3/2} \sqrt{1-\frac{bx}{a}} \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{b}} + \sqrt{x}(a-bx)}{\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a - b*x]/Sqrt[x], x]

[Out] (Sqrt[x]*(a - b*x) + (a^(3/2)*Sqrt[1 - (b*x)/a]*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[b])/Sqrt[a - b*x]

fricas [A] time = 0.50, size = 94, normalized size = 2.04

$$\left[\frac{a\sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) - 2\sqrt{-bx+a}b\sqrt{x}}{2b}, -\frac{a\sqrt{b} \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right) - \sqrt{-bx+a}b\sqrt{x}}{b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(1/2),x, algorithm="fricas")

[Out] [-1/2*(a*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*sqrt(-b*x + a)*b*sqrt(x))/b, -(a*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - sqrt(-b*x + a)*b*sqrt(x))/b]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.00, size = 66, normalized size = 1.43

$$\frac{\sqrt{-bx+a} x a \arctan\left(\frac{(x-\frac{a}{2b})\sqrt{b}}{\sqrt{-bx^2+ax}}\right)}{2\sqrt{-bx+a} \sqrt{b} \sqrt{x}} + \sqrt{-bx+a} \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+a)^(1/2)/x^(1/2),x)

[Out] x^(1/2)*(-b*x+a)^(1/2)+1/2*a*((-b*x+a)*x)^(1/2)/((-b*x+a)^(1/2)/x^(1/2)/b^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))

maxima [A] time = 2.90, size = 52, normalized size = 1.13

$$-\frac{a \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b} \sqrt{x}}\right)}{\sqrt{b}} + \frac{\sqrt{-bx+a} a}{\left(b - \frac{bx-a}{x}\right) \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(1/2),x, algorithm="maxima")

[Out] -a*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/sqrt(b) + sqrt(-b*x + a)*a/((b - (b*x - a)/x)*sqrt(x))

mupad [B] time = 0.59, size = 43, normalized size = 0.93

$$\sqrt{x} \sqrt{a - bx} + \frac{2 a \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a - bx} - \sqrt{a}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - b*x)^(1/2)/x^(1/2), x)`

[Out] $x^{1/2}*(a - b*x)^{1/2} + (2*a*atan((b^{1/2}*x^{1/2})/((a - b*x)^{1/2} - a^{1/2}))) / b^{1/2}$

sympy [A] time = 1.96, size = 119, normalized size = 2.59

$$\left\{ \begin{array}{ll} -\frac{i\sqrt{a}\sqrt{x}}{\sqrt{-1+\frac{bx}{a}}} - \frac{ia \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{b}} + \frac{ibx^{\frac{3}{2}}}{\sqrt{a}\sqrt{-1+\frac{bx}{a}}} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ \sqrt{a}\sqrt{x}\sqrt{1-\frac{bx}{a}} + \frac{a \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{b}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+a)**(1/2)/x**(1/2), x)`

[Out] `Piecewise((-I*sqrt(a)*sqrt(x)/sqrt(-1 + b*x/a) - I*a*acosh(sqrt(b)*sqrt(x)/sqrt(a))/sqrt(b) + I*b*x**(3/2)/(sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (sqrt(a)*sqrt(x)*sqrt(1 - b*x/a) + a*asin(sqrt(b)*sqrt(x)/sqrt(a))/sqrt(b), True))`

$$3.501 \quad \int \frac{\sqrt{a-bx}}{x^{3/2}} dx$$

Optimal. Leaf size=47

$$-\frac{2\sqrt{a-bx}}{\sqrt{x}} - 2\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)$$

[Out] $-2*\arctan(b^{(1/2)*x^{(1/2)/(-b*x+a)^{(1/2))}*b^{(1/2)}-2*(-b*x+a)^{(1/2)/x^{(1/2)}}$

Rubi [A] time = 0.02, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {47, 63, 217, 203}

$$-\frac{2\sqrt{a-bx}}{\sqrt{x}} - 2\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a - b*x]/x^(3/2), x]

[Out] $(-2*\text{Sqrt}[a - b*x])/\text{Sqrt}[x] - 2*\text{Sqrt}[b]*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]]$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
```

, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{a-bx}}{x^{3/2}} dx &= -\frac{2\sqrt{a-bx}}{\sqrt{x}} - b \int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx \\ &= -\frac{2\sqrt{a-bx}}{\sqrt{x}} - (2b) \text{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x}\right) \\ &= -\frac{2\sqrt{a-bx}}{\sqrt{x}} - (2b) \text{Subst}\left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right) \\ &= -\frac{2\sqrt{a-bx}}{\sqrt{x}} - 2\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right) \end{aligned}$$

Mathematica [A] time = 0.06, size = 69, normalized size = 1.47

$$\frac{2\left(\sqrt{a}\sqrt{b}\sqrt{x}\sqrt{1-\frac{bx}{a}}\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) + a - bx\right)}{\sqrt{x}\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a - b*x]/x^(3/2), x]

[Out] (-2*(a - b*x + Sqrt[a]*Sqrt[b]*Sqrt[x]*Sqrt[1 - (b*x)/a]*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[x]*Sqrt[a - b*x])

fricas [A] time = 0.44, size = 91, normalized size = 1.94

$$\left[\frac{\sqrt{-b}x \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) - 2\sqrt{-bx+a}\sqrt{x}}{x}, \frac{2\left(\sqrt{b}x \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right) - \sqrt{-bx+a}\sqrt{x}\right)}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(3/2), x, algorithm="fricas")

[Out] [(sqrt(-b)*x*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*sqrt(-b*x + a)*sqrt(x))/x, 2*(sqrt(b)*x*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - sqrt(-b*x + a)*sqrt(x))/x]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(3/2),x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{-bx+a}}{x^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+a)^(1/2)/x^(3/2),x)

[Out] int((-b*x+a)^(1/2)/x^(3/2),x)

maxima [A] time = 2.93, size = 35, normalized size = 0.74

$$2\sqrt{b} \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right) - \frac{2\sqrt{-bx+a}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(3/2),x, algorithm="maxima")

[Out] 2*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - 2*sqrt(-b*x + a)/sqrt(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{a-bx}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - b*x)^(1/2)/x^(3/2),x)

[Out] int((a - b*x)^(1/2)/x^(3/2), x)

sympy [A] time = 1.70, size = 148, normalized size = 3.15

$$\begin{cases} \frac{2i\sqrt{a}}{\sqrt{x}\sqrt{-1+\frac{bx}{a}}} + 2i\sqrt{b} \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) - \frac{2ib\sqrt{x}}{\sqrt{a}\sqrt{-1+\frac{bx}{a}}} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{2\sqrt{a}}{\sqrt{x}\sqrt{1-\frac{bx}{a}}} - 2\sqrt{b} \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) + \frac{2b\sqrt{x}}{\sqrt{a}\sqrt{1-\frac{bx}{a}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+a)**(1/2)/x**(3/2),x)`

[Out] `Piecewise((2*I*sqrt(a)/(sqrt(x)*sqrt(-1 + b*x/a)) + 2*I*sqrt(b)*acosh(sqrt(b)*sqrt(x)/sqrt(a)) - 2*I*b*sqrt(x)/(sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (-2*sqrt(a)/(sqrt(x)*sqrt(1 - b*x/a)) - 2*sqrt(b)*asin(sqrt(b)*sqrt(x)/sqrt(a)) + 2*b*sqrt(x)/(sqrt(a)*sqrt(1 - b*x/a)), True))`

$$3.502 \quad \int \frac{\sqrt{a-bx}}{x^{5/2}} dx$$

Optimal. Leaf size=22

$$-\frac{2(a-bx)^{3/2}}{3ax^{3/2}}$$

[Out] $-2/3*(-b*x+a)^{(3/2)}/a/x^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {37}

$$-\frac{2(a-bx)^{3/2}}{3ax^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a - b*x]/x^(5/2), x]

[Out] $(-2*(a - b*x)^{(3/2)})/(3*a*x^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{a-bx}}{x^{5/2}} dx = -\frac{2(a-bx)^{3/2}}{3ax^{3/2}}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 1.00

$$-\frac{2(a-bx)^{3/2}}{3ax^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a - b*x]/x^(5/2), x]

[Out] $(-2*(a - b*x)^{(3/2)})/(3*a*x^{(3/2)})$

fricas [A] time = 0.44, size = 23, normalized size = 1.05

$$\frac{2(bx - a)\sqrt{-bx + a}}{3ax^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(5/2),x, algorithm="fricas")

[Out] 2/3*(b*x - a)*sqrt(-b*x + a)/(a*x^(3/2))

giac [B] time = 1.40, size = 42, normalized size = 1.91

$$\frac{2(bx - a)\sqrt{-bx + a}b^4}{3((bx - a)b + ab)^{\frac{3}{2}}a|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(5/2),x, algorithm="giac")

[Out] 2/3*(b*x - a)*sqrt(-b*x + a)*b^4/(((b*x - a)*b + a*b)^(3/2)*a*abs(b))

maple [A] time = 0.00, size = 17, normalized size = 0.77

$$-\frac{2(-bx + a)^{\frac{3}{2}}}{3ax^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+a)^(1/2)/x^(5/2),x)

[Out] -2/3*(-b*x+a)^(3/2)/a/x^(3/2)

maxima [A] time = 1.31, size = 16, normalized size = 0.73

$$-\frac{2(-bx + a)^{\frac{3}{2}}}{3ax^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(5/2),x, algorithm="maxima")

[Out] -2/3*(-b*x + a)^(3/2)/(a*x^(3/2))

mupad [B] time = 0.24, size = 21, normalized size = 0.95

$$\frac{\left(\frac{2bx}{3a} - \frac{2}{3}\right) \sqrt{a-bx}}{x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - b*x)^(1/2)/x^(5/2), x)`

[Out] `((2*b*x)/(3*a) - 2/3)*(a - b*x)^(1/2)/x^(3/2)`

sympy [B] time = 1.55, size = 88, normalized size = 4.00

$$\begin{cases} -\frac{2\sqrt{b}\sqrt{\frac{a}{bx}-1}}{3x} + \frac{2b^{\frac{3}{2}}\sqrt{\frac{a}{bx}-1}}{3a} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ -\frac{2i\sqrt{b}\sqrt{-\frac{a}{bx}+1}}{3x} + \frac{2ib^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}}{3a} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+a)**(1/2)/x**(5/2), x)`

[Out] `Piecewise((-2*sqrt(b)*sqrt(a/(b*x) - 1)/(3*x) + 2*b**(3/2)*sqrt(a/(b*x) - 1)/(3*a), Abs(a/(b*x)) > 1), (-2*I*sqrt(b)*sqrt(-a/(b*x) + 1)/(3*x) + 2*I*b**(3/2)*sqrt(-a/(b*x) + 1)/(3*a), True))`

$$3.503 \quad \int \frac{\sqrt{a-bx}}{x^{7/2}} dx$$

Optimal. Leaf size=46

$$-\frac{4b(a-bx)^{3/2}}{15a^2x^{3/2}} - \frac{2(a-bx)^{3/2}}{5ax^{5/2}}$$

[Out] $-2/5*(-b*x+a)^{(3/2)}/a/x^{(5/2)}-4/15*b*(-b*x+a)^{(3/2)}/a^2/x^{(3/2)}$

Rubi [A] time = 0.01, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{4b(a-bx)^{3/2}}{15a^2x^{3/2}} - \frac{2(a-bx)^{3/2}}{5ax^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a - b*x]/x^(7/2), x]

[Out] $(-2*(a - b*x)^{(3/2)})/(5*a*x^{(5/2)}) - (4*b*(a - b*x)^{(3/2)})/(15*a^2*x^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{\sqrt{a-bx}}{x^{7/2}} dx = -\frac{2(a-bx)^{3/2}}{5ax^{5/2}} + \frac{(2b) \int \frac{\sqrt{a-bx}}{x^{5/2}} dx}{5a}$$

$$= -\frac{2(a-bx)^{3/2}}{5ax^{5/2}} - \frac{4b(a-bx)^{3/2}}{15a^2x^{3/2}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 0.65

$$-\frac{2(a-bx)^{3/2}(3a+2bx)}{15a^2x^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a - b*x]/x^(7/2), x]

[Out] (-2*(a - b*x)^(3/2)*(3*a + 2*b*x))/(15*a^2*x^(5/2))

fricas [A] time = 0.45, size = 34, normalized size = 0.74

$$\frac{2(2b^2x^2 + abx - 3a^2)\sqrt{-bx + a}}{15a^2x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(7/2), x, algorithm="fricas")

[Out] 2/15*(2*b^2*x^2 + a*b*x - 3*a^2)*sqrt(-b*x + a)/(a^2*x^(5/2))

giac [A] time = 1.38, size = 61, normalized size = 1.33

$$\frac{2\left(\frac{(bx-a)b^5}{a^2} + \frac{5b^5}{a}\right)(bx-a)\sqrt{-bx+a}b}{15((bx-a)b+ab)^{\frac{5}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(7/2), x, algorithm="giac")

[Out] 2/15*(2*(b*x - a)*b^5/a^2 + 5*b^5/a)*(b*x - a)*sqrt(-b*x + a)*b/(((b*x - a)*b + a*b)^(5/2)*abs(b))

maple [A] time = 0.00, size = 25, normalized size = 0.54

$$-\frac{2(-bx+a)^{\frac{3}{2}}(2bx+3a)}{15a^2x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-b*x+a)^(1/2)/x^(7/2),x)`

[Out] $-2/15*(-b*x+a)^{(3/2)}*(2*b*x+3*a)/x^{(5/2)}/a^2$

maxima [A] time = 1.34, size = 33, normalized size = 0.72

$$\frac{2 \left(\frac{5(-bx+a)^{\frac{3}{2}}b}{x^2} + \frac{3(-bx+a)^{\frac{5}{2}}}{x^2} \right)}{15a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+a)^(1/2)/x^(7/2),x, algorithm="maxima")`

[Out] $-2/15*(5*(-b*x + a)^{(3/2)}*b/x^{(3/2)} + 3*(-b*x + a)^{(5/2)}/x^{(5/2)})/a^2$

mupad [B] time = 0.25, size = 32, normalized size = 0.70

$$\frac{\sqrt{a-bx} \left(\frac{4b^2x^2}{15a^2} + \frac{2bx}{15a} - \frac{2}{5} \right)}{x^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a-b*x)^(1/2)/x^(7/2),x)`

[Out] $((a-b*x)^{(1/2)}*((4*b^2*x^2)/(15*a^2) + (2*b*x)/(15*a) - 2/5))/x^{(5/2)}$

sympy [A] time = 5.01, size = 241, normalized size = 5.24

$$\begin{cases} -\frac{2\sqrt{b}\sqrt{\frac{a}{bx}-1}}{5x^2} + \frac{2b^{\frac{3}{2}}\sqrt{\frac{a}{bx}-1}}{15ax} + \frac{4b^{\frac{5}{2}}\sqrt{\frac{a}{bx}-1}}{15a^2} & \text{for } \left| \frac{a}{bx} \right| > 1 \\ \frac{6ia^3b^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}}{x(-15a^3bx+15a^2b^2x^2)} - \frac{8ia^2b^{\frac{5}{2}}\sqrt{-\frac{a}{bx}+1}}{-15a^3bx+15a^2b^2x^2} - \frac{2iab^{\frac{7}{2}}x\sqrt{-\frac{a}{bx}+1}}{-15a^3bx+15a^2b^2x^2} + \frac{4ib^{\frac{9}{2}}x^2\sqrt{-\frac{a}{bx}+1}}{-15a^3bx+15a^2b^2x^2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+a)**(1/2)/x**(7/2),x)`

[Out] `Piecewise((-2*sqrt(b)*sqrt(a/(b*x) - 1)/(5*x**2) + 2*b**(3/2)*sqrt(a/(b*x) - 1)/(15*a*x) + 4*b**(5/2)*sqrt(a/(b*x) - 1)/(15*a**2), Abs(a/(b*x)) > 1), (6*I*a**3*b**(3/2)*sqrt(-a/(b*x) + 1)/(x*(-15*a**3*b*x + 15*a**2*b**2*x**2)) - 8*I*a**2*b**(5/2)*sqrt(-a/(b*x) + 1)/(-15*a**3*b*x + 15*a**2*b**2*x**2) - 2*I*a*b**(7/2)*x*sqrt(-a/(b*x) + 1)/(-15*a**3*b*x + 15*a**2*b**2*x**2) + 4*I*b**(9/2)*x**2*sqrt(-a/(b*x) + 1)/(-15*a**3*b*x + 15*a**2*b**2*x**2), True))`

$$3.504 \quad \int \frac{\sqrt{a-bx}}{x^{9/2}} dx$$

Optimal. Leaf size=71

$$-\frac{16b^2(a-bx)^{3/2}}{105a^3x^{3/2}} - \frac{8b(a-bx)^{3/2}}{35a^2x^{5/2}} - \frac{2(a-bx)^{3/2}}{7ax^{7/2}}$$

[Out] $-2/7*(-b*x+a)^{(3/2)}/a/x^{(7/2)}-8/35*b*(-b*x+a)^{(3/2)}/a^2/x^{(5/2)}-16/105*b^2*(-b*x+a)^{(3/2)}/a^3/x^{(3/2)}$

Rubi [A] time = 0.01, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{16b^2(a-bx)^{3/2}}{105a^3x^{3/2}} - \frac{8b(a-bx)^{3/2}}{35a^2x^{5/2}} - \frac{2(a-bx)^{3/2}}{7ax^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a - b*x]/x^(9/2), x]

[Out] $(-2*(a - b*x)^{(3/2)})/(7*a*x^{(7/2)}) - (8*b*(a - b*x)^{(3/2)})/(35*a^2*x^{(5/2)}) - (16*b^2*(a - b*x)^{(3/2)})/(105*a^3*x^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{a-bx}}{x^{9/2}} dx &= -\frac{2(a-bx)^{3/2}}{7ax^{7/2}} + \frac{(4b) \int \frac{\sqrt{a-bx}}{x^{7/2}} dx}{7a} \\
&= -\frac{2(a-bx)^{3/2}}{7ax^{7/2}} - \frac{8b(a-bx)^{3/2}}{35a^2x^{5/2}} + \frac{(8b^2) \int \frac{\sqrt{a-bx}}{x^{5/2}} dx}{35a^2} \\
&= -\frac{2(a-bx)^{3/2}}{7ax^{7/2}} - \frac{8b(a-bx)^{3/2}}{35a^2x^{5/2}} - \frac{16b^2(a-bx)^{3/2}}{105a^3x^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 41, normalized size = 0.58

$$-\frac{2(a-bx)^{3/2}(15a^2+12abx+8b^2x^2)}{105a^3x^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a - b*x]/x^(9/2), x]

[Out] (-2*(a - b*x)^(3/2)*(15*a^2 + 12*a*b*x + 8*b^2*x^2))/(105*a^3*x^(7/2))

fricas [A] time = 0.46, size = 46, normalized size = 0.65

$$\frac{2(8b^3x^3 + 4ab^2x^2 + 3a^2bx - 15a^3)\sqrt{-bx+a}}{105a^3x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(9/2), x, algorithm="fricas")

[Out] 2/105*(8*b^3*x^3 + 4*a*b^2*x^2 + 3*a^2*b*x - 15*a^3)*sqrt(-b*x + a)/(a^3*x^(7/2))

giac [A] time = 1.34, size = 79, normalized size = 1.11

$$\frac{2\left(\frac{35b^7}{a} + 4\left(\frac{2(bx-a)b^7}{a^3} + \frac{7b^7}{a^2}\right)(bx-a)\right)(bx-a)\sqrt{-bx+a}b}{105((bx-a)b+ab)^{\frac{7}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(1/2)/x^(9/2), x, algorithm="giac")

[Out] 2/105*(35*b^7/a + 4*(2*(b*x - a)*b^7/a^3 + 7*b^7/a^2)*(b*x - a))*(b*x - a)*sqrt(-b*x + a)*b/(((b*x - a)*b + a*b)^(7/2)*abs(b))

maple [A] time = 0.00, size = 36, normalized size = 0.51

$$\frac{2(-bx+a)^{\frac{3}{2}}(8b^2x^2+12abx+15a^2)}{105a^3x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-b*x+a)^(1/2)/x^(9/2),x)`

[Out] `-2/105*(-b*x+a)^(3/2)*(8*b^2*x^2+12*a*b*x+15*a^2)/x^(7/2)/a^3`

maxima [A] time = 1.35, size = 49, normalized size = 0.69

$$\frac{2\left(\frac{35(-bx+a)^{\frac{3}{2}}b^2}{x^{\frac{3}{2}}} + \frac{42(-bx+a)^{\frac{5}{2}}b}{x^{\frac{5}{2}}} + \frac{15(-bx+a)^{\frac{7}{2}}}{x^{\frac{7}{2}}}\right)}{105a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+a)^(1/2)/x^(9/2),x, algorithm="maxima")`

[Out] `-2/105*(35*(-b*x + a)^(3/2)*b^2/x^(3/2) + 42*(-b*x + a)^(5/2)*b/x^(5/2) + 15*(-b*x + a)^(7/2)/x^(7/2))/a^3`

mupad [B] time = 0.27, size = 43, normalized size = 0.61

$$\frac{\sqrt{a-bx}\left(\frac{8b^2x^2}{105a^2} + \frac{16b^3x^3}{105a^3} + \frac{2bx}{35a} - \frac{2}{7}\right)}{x^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - b*x)^(1/2)/x^(9/2),x)`

[Out] `((a - b*x)^(1/2)*((8*b^2*x^2)/(105*a^2) + (16*b^3*x^3)/(105*a^3) + (2*b*x)/(35*a) - 2/7))/x^(7/2)`

sympy [B] time = 26.81, size = 707, normalized size = 9.96

$$\left\{ \begin{array}{l} \frac{30a^5b^{\frac{9}{2}}\sqrt{\frac{a}{bx}-1}}{-105a^5b^4x^3+210a^4b^5x^4-105a^3b^6x^5} - \frac{66a^4b^{\frac{11}{2}}x\sqrt{\frac{a}{bx}-1}}{-105a^5b^4x^3+210a^4b^5x^4-105a^3b^6x^5} + \frac{34a^3b^{\frac{13}{2}}x^2\sqrt{\frac{a}{bx}-1}}{-105a^5b^4x^3+210a^4b^5x^4-105a^3b^6x^5} - \frac{6a^2b^{\frac{15}{2}}x^3\sqrt{\frac{a}{bx}-1}}{-105a^5b^4x^3+210a^4b^5x^4-105a^3b^6x^5} \\ \frac{30ia^5b^{\frac{9}{2}}\sqrt{-\frac{a}{bx}+1}}{-105a^5b^4x^3+210a^4b^5x^4-105a^3b^6x^5} - \frac{66ia^4b^{\frac{11}{2}}x\sqrt{-\frac{a}{bx}+1}}{-105a^5b^4x^3+210a^4b^5x^4-105a^3b^6x^5} + \frac{34ia^3b^{\frac{13}{2}}x^2\sqrt{-\frac{a}{bx}+1}}{-105a^5b^4x^3+210a^4b^5x^4-105a^3b^6x^5} - \frac{6ia^2b^{\frac{15}{2}}x^3\sqrt{-\frac{a}{bx}+1}}{-105a^5b^4x^3+210a^4b^5x^4-105a^3b^6x^5} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)**(1/2)/x**(9/2),x)

[Out] Piecewise((30*a**5*b**(9/2)*sqrt(a/(b*x) - 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5) - 66*a**4*b**(11/2)*x*sqrt(a/(b*x) - 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5) + 34*a**3*b**(13/2)*x**2*sqrt(a/(b*x) - 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5) - 6*a**2*b**(15/2)*x**3*sqrt(a/(b*x) - 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5) + 24*a*b**(17/2)*x**4*sqrt(a/(b*x) - 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5) - 16*b**(19/2)*x**5*sqrt(a/(b*x) - 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5), Abs(a/(b*x)) > 1), (30*I*a**5*b**(9/2)*sqrt(-a/(b*x) + 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5) - 66*I*a**4*b**(11/2)*x*sqrt(-a/(b*x) + 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5) + 34*I*a**3*b**(13/2)*x**2*sqrt(-a/(b*x) + 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5) - 6*I*a**2*b**(15/2)*x**3*sqrt(-a/(b*x) + 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5) + 24*I*a*b**(17/2)*x**4*sqrt(-a/(b*x) + 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5) - 16*I*b**(19/2)*x**5*sqrt(-a/(b*x) + 1)/(-105*a**5*b**4*x**3 + 210*a**4*b**5*x**4 - 105*a**3*b**6*x**5), True))

3.505 $\int x^{5/2} \sqrt{2 + bx} dx$

Optimal. Leaf size=108

$$-\frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}} + \frac{5\sqrt{x}\sqrt{bx+2}}{8b^3} - \frac{5x^{3/2}\sqrt{bx+2}}{24b^2} + \frac{1}{4}x^{7/2}\sqrt{bx+2} + \frac{x^{5/2}\sqrt{bx+2}}{12b}$$

[Out] $-5/4*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(7/2)}-5/24*x^{(3/2)}*(b*x+2)^{(1/2)}/b^2+1/12*x^{(5/2)}*(b*x+2)^{(1/2)}/b+1/4*x^{(7/2)}*(b*x+2)^{(1/2)}+5/8*x^{(1/2)}*(b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.03, antiderivative size = 108, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{5x^{3/2}\sqrt{bx+2}}{24b^2} + \frac{5\sqrt{x}\sqrt{bx+2}}{8b^3} - \frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}} + \frac{1}{4}x^{7/2}\sqrt{bx+2} + \frac{x^{5/2}\sqrt{bx+2}}{12b}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(5/2)}*\operatorname{Sqrt}[2 + b*x], x]$

[Out] $(5*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/(8*b^3) - (5*x^{(3/2)}*\operatorname{Sqrt}[2 + b*x])/(24*b^2) + (x^{(5/2)}*\operatorname{Sqrt}[2 + b*x])/(12*b) + (x^{(7/2)}*\operatorname{Sqrt}[2 + b*x])/4 - (5*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]])/(4*b^{(7/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] :> Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :- Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned}
 \int x^{5/2} \sqrt{2+bx} \, dx &= \frac{1}{4} x^{7/2} \sqrt{2+bx} + \frac{1}{4} \int \frac{x^{5/2}}{\sqrt{2+bx}} \, dx \\
 &= \frac{x^{5/2} \sqrt{2+bx}}{12b} + \frac{1}{4} x^{7/2} \sqrt{2+bx} - \frac{5 \int \frac{x^{3/2}}{\sqrt{2+bx}} \, dx}{12b} \\
 &= -\frac{5x^{3/2} \sqrt{2+bx}}{24b^2} + \frac{x^{5/2} \sqrt{2+bx}}{12b} + \frac{1}{4} x^{7/2} \sqrt{2+bx} + \frac{5 \int \frac{\sqrt{x}}{\sqrt{2+bx}} \, dx}{8b^2} \\
 &= \frac{5\sqrt{x} \sqrt{2+bx}}{8b^3} - \frac{5x^{3/2} \sqrt{2+bx}}{24b^2} + \frac{x^{5/2} \sqrt{2+bx}}{12b} + \frac{1}{4} x^{7/2} \sqrt{2+bx} - \frac{5 \int \frac{1}{\sqrt{x} \sqrt{2+bx}} \, dx}{8b^3} \\
 &= \frac{5\sqrt{x} \sqrt{2+bx}}{8b^3} - \frac{5x^{3/2} \sqrt{2+bx}}{24b^2} + \frac{x^{5/2} \sqrt{2+bx}}{12b} + \frac{1}{4} x^{7/2} \sqrt{2+bx} - \frac{5 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} \, dx, x\right)}{4b^3} \\
 &= \frac{5\sqrt{x} \sqrt{2+bx}}{8b^3} - \frac{5x^{3/2} \sqrt{2+bx}}{24b^2} + \frac{x^{5/2} \sqrt{2+bx}}{12b} + \frac{1}{4} x^{7/2} \sqrt{2+bx} - \frac{5 \sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}}
 \end{aligned}$$

Mathematica [A] time = 0.05, size = 70, normalized size = 0.65

$$\frac{\sqrt{x} \sqrt{bx+2} (6b^3x^3 + 2b^2x^2 - 5bx + 15)}{24b^3} - \frac{5 \sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*Sqrt[2 + b*x], x]

[Out] (Sqrt[x]*Sqrt[2 + b*x]*(15 - 5*b*x + 2*b^2*x^2 + 6*b^3*x^3))/(24*b^3) - (5*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(4*b^(7/2))

fricas [A] time = 0.46, size = 140, normalized size = 1.30

$$\left[\frac{(6b^4x^3 + 2b^3x^2 - 5b^2x + 15b)\sqrt{bx+2}\sqrt{x} + 15\sqrt{b} \log(bx - \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{24b^4}, \frac{(6b^4x^3 + 2b^3x^2 - 5b^2x - 15b)\sqrt{bx+2}\sqrt{x} + 15\sqrt{b} \log(bx - \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{24b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(5/2)*(b*x+2)^(1/2),x, algorithm="fricas")
```

```
[Out] [1/24*((6*b^4*x^3 + 2*b^3*x^2 - 5*b^2*x + 15*b)*sqrt(b*x + 2)*sqrt(x) + 15*sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^4, 1/24*((6*b^4*x^3 + 2*b^3*x^2 - 5*b^2*x + 15*b)*sqrt(b*x + 2)*sqrt(x) + 30*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))))/b^4]
```

```
giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00
```

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(5/2)*(b*x+2)^(1/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [59.8656459 874,25.8388736797]Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [33.9285577983,15.451549686]Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [59.8656459 874,25.8388736797]Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [33.9285577983,15.451549686]Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [33.9285577983,15.451549686]
```

Warning, choosing root of [1,0,-4, [1,1,-4, [1,0,-4, [0,1,-8, [0,0,0, [6, [2,2,4, [2,1,6, [2,0,4, [1,2,28, [1,1,8, [1,0,6, [0,2,8, [0,1,24, [0,0,0, [4, [3,3,4, [3,2,4, [3,1,-4, [3,0,-4, [2,3,-64, [2,2,20, [2,1,8, [2,0,4, [1,3,20, [1,2,-128, [1,1,16, [1,0,-4, [0,3,8, [0,2,16, [0,1,-32, [0,0,0, [1, [4,4,-4, [4,3,6, [4,2,-4, [4,1,1, [4,0,-4, [3,4,12, [3,3,-20, [3,2,20, [3,1,-8, [3,0,6, [2,4,-20, [2,3,46, [2,2,-40, [2,1,24, [2,0,-4, [1,4,20, [1,3,-40, [1,2,48, [1,1,-32, [1,0,1, [0,4,-8, [0,3,24, [0,2,-32, [0,1,6, [0,0,6]] at parameters values [54.7579903365,81.9516051291] Warning, choosing root of [1,0,-4, [1,1,-4, [1,0,-4, [0,1,-8, [0,0,0, [6, [2,2,4, [2,1,6, [2,0,4, [1,2,28, [1,1,8, [1,0,6, [0,2,8, [0,1,24, [0,0,0, [4, [3,3,4, [3,2,4, [3,1,-4, [3,0,-4, [2,3,-64, [2,2,20, [2,1,8, [2,0,4, [1,3,20, [1,2,-128, [1,1,16, [1,0,-4, [0,3,8, [0,2,16, [0,1,-32, [0,0,0, [1, [4,4,-4, [4,3,6, [4,2,-4, [4,1,1, [4,0,-4, [3,4,12, [3,3,-20, [3,2,20, [3,1,-8, [3,0,6, [2,4,-20, [2,3,46, [2,2,-40, [2,1,24, [2,0,-4, [1,4,20, [1,3,-40, [1,2,48, [1,1,-32, [1,0,1, [0,4,-8, [0,3,24, [0,2,-32, [0,1,16, [0,0,6]] at parameters values [18.4052062202,51.6443148847] $1/b * (2*b*abs(b)/b^2 * (2*((90*b^{11}/1440/b^{14}*sqrt(b*x+2)*sqrt(b*x+2)-750*b^{11}/1440/b^{14})*sqrt(b*x+2)*sqrt(b*x+2)+2445*b^{11}/1440/b^{14})*sqrt(b*x+2)*sqrt(b*x+2)-4185*b^{11}/1440/b^{14})*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)-35/8/b^2/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))+4*abs(b)/b^2 * (2*((12*b^5/144/b^7*sqrt(b*x+2)*sqrt(b*x+2)-78*b^5/144/b^7)*sqrt(b*x+2)*sqrt(b*x+2)+198*b^5/144/b^7)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)+5/2/b/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))$

maple [A] time = 0.01, size = 108, normalized size = 1.00

$$\frac{(bx+2)^{\frac{3}{2}}x^{\frac{5}{2}}}{4b} - \frac{5(bx+2)^{\frac{3}{2}}x^{\frac{3}{2}}}{12b^2} + \frac{5(bx+2)^{\frac{3}{2}}\sqrt{x}}{8b^3} - \frac{5\sqrt{bx+2}\sqrt{x}}{8b^3} - \frac{5\sqrt{(bx+2)x}\ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{8\sqrt{bx+2}b^{\frac{7}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{(5/2)}*(b*x+2)^{(1/2)}, x)$

[Out] $1/4/b*x^{(5/2)}*(b*x+2)^{(3/2)}-5/12/b^2*x^{(3/2)}*(b*x+2)^{(3/2)}+5/8/b^3*x^{(1/2)}*(b*x+2)^{(3/2)}-5/8*x^{(1/2)}*(b*x+2)^{(1/2)}/b^3-5/8/b^{(7/2)}*(x*(b*x+2))^{(1/2)}/(b*x+2)^{(1/2)}/x^{(1/2)}*ln((b*x+1)/b^{(1/2)}+(b*x^2+2*x)^{(1/2)})$

maxima [B] time = 3.03, size = 163, normalized size = 1.51

$$\frac{\frac{15\sqrt{bx+2}b^3}{\sqrt{x}} + \frac{73(bx+2)^{\frac{3}{2}}b^2}{x^{\frac{3}{2}}} - \frac{55(bx+2)^{\frac{5}{2}}b}{x^{\frac{5}{2}}} + \frac{15(bx+2)^{\frac{7}{2}}}{x^{\frac{7}{2}}}{12\left(b^7 - \frac{4(bx+2)b^6}{x} + \frac{6(bx+2)^2b^5}{x^2} - \frac{4(bx+2)^3b^4}{x^3} + \frac{(bx+2)^4b^3}{x^4}\right)} + \frac{5 \log\left(-\frac{\sqrt{b}-\sqrt{bx+2}}{\sqrt{x}}\right)}{8b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+2)^(1/2),x, algorithm="maxima")

[Out] 1/12*(15*sqrt(b*x + 2)*b^3/sqrt(x) + 73*(b*x + 2)^(3/2)*b^2/x^(3/2) - 55*(b*x + 2)^(5/2)*b/x^(5/2) + 15*(b*x + 2)^(7/2)/x^(7/2))/(b^7 - 4*(b*x + 2)*b^6/x + 6*(b*x + 2)^2*b^5/x^2 - 4*(b*x + 2)^3*b^4/x^3 + (b*x + 2)^4*b^3/x^4) + 5/8*log(-(sqrt(b) - sqrt(b*x + 2)/sqrt(x))/(sqrt(b) + sqrt(b*x + 2)/sqrt(x)))/b^(7/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} \sqrt{bx+2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(b*x + 2)^(1/2), x)

[Out] int(x^(5/2)*(b*x + 2)^(1/2), x)

sympy [A] time = 10.12, size = 117, normalized size = 1.08

$$\frac{bx^{\frac{9}{2}}}{4\sqrt{bx+2}} + \frac{7x^{\frac{7}{2}}}{12\sqrt{bx+2}} - \frac{x^{\frac{5}{2}}}{24b\sqrt{bx+2}} + \frac{5x^{\frac{3}{2}}}{24b^2\sqrt{bx+2}} + \frac{5\sqrt{x}}{4b^3\sqrt{bx+2}} - \frac{5 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)*(b*x+2)**(1/2),x)

[Out] b*x**(9/2)/(4*sqrt(b*x + 2)) + 7*x**(7/2)/(12*sqrt(b*x + 2)) - x**(5/2)/(24*b*sqrt(b*x + 2)) + 5*x**(3/2)/(24*b**2*sqrt(b*x + 2)) + 5*sqrt(x)/(4*b**3*sqrt(b*x + 2)) - 5*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(7/2))

3.506 $\int x^{3/2} \sqrt{2 + bx} dx$

Optimal. Leaf size=84

$$\frac{\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{\sqrt{x}\sqrt{bx+2}}{2b^2} + \frac{1}{3}x^{5/2}\sqrt{bx+2} + \frac{x^{3/2}\sqrt{bx+2}}{6b}$$

[Out] arcsinh(1/2*b^(1/2)*x^(1/2)*2^(1/2))/b^(5/2)+1/6*x^(3/2)*(b*x+2)^(1/2)/b+1/3*x^(5/2)*(b*x+2)^(1/2)-1/2*x^(1/2)*(b*x+2)^(1/2)/b^2

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{\sqrt{x}\sqrt{bx+2}}{2b^2} + \frac{\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{1}{3}x^{5/2}\sqrt{bx+2} + \frac{x^{3/2}\sqrt{bx+2}}{6b}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)*Sqrt[2 + b*x], x]

[Out] -(Sqrt[x]*Sqrt[2 + b*x])/(2*b^2) + (x^(3/2)*Sqrt[2 + b*x])/(6*b) + (x^(5/2)*Sqrt[2 + b*x])/3 + ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]]/b^(5/2)

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 215

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned}
\int x^{3/2}\sqrt{2+bx} \, dx &= \frac{1}{3}x^{5/2}\sqrt{2+bx} + \frac{1}{3}\int \frac{x^{3/2}}{\sqrt{2+bx}} \, dx \\
&= \frac{x^{3/2}\sqrt{2+bx}}{6b} + \frac{1}{3}x^{5/2}\sqrt{2+bx} - \frac{\int \frac{\sqrt{x}}{\sqrt{2+bx}} \, dx}{2b} \\
&= -\frac{\sqrt{x}\sqrt{2+bx}}{2b^2} + \frac{x^{3/2}\sqrt{2+bx}}{6b} + \frac{1}{3}x^{5/2}\sqrt{2+bx} + \frac{\int \frac{1}{\sqrt{x}\sqrt{2+bx}} \, dx}{2b^2} \\
&= -\frac{\sqrt{x}\sqrt{2+bx}}{2b^2} + \frac{x^{3/2}\sqrt{2+bx}}{6b} + \frac{1}{3}x^{5/2}\sqrt{2+bx} + \frac{\text{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} \, dx, x, \sqrt{x}\right)}{b^2} \\
&= -\frac{\sqrt{x}\sqrt{2+bx}}{2b^2} + \frac{x^{3/2}\sqrt{2+bx}}{6b} + \frac{1}{3}x^{5/2}\sqrt{2+bx} + \frac{\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 58, normalized size = 0.69

$$\frac{\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{\sqrt{x}\sqrt{bx+2}(2b^2x^2+bx-3)}{6b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*Sqrt[2 + b*x], x]

[Out] (Sqrt[x]*Sqrt[2 + b*x]*(-3 + b*x + 2*b^2*x^2))/(6*b^2) + ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]]/b^(5/2)

fricas [A] time = 0.46, size = 121, normalized size = 1.44

$$\left[\frac{(2b^3x^2 + b^2x - 3b)\sqrt{bx+2}\sqrt{x} + 3\sqrt{b}\log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{6b^3}, \frac{(2b^3x^2 + b^2x - 3b)\sqrt{bx+2}\sqrt{x} - 6\sqrt{b}\log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{6b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+2)^(1/2), x, algorithm="fricas")

[Out] [1/6*((2*b^3*x^2 + b^2*x - 3*b)*sqrt(b*x + 2)*sqrt(x) + 3*sqrt(b)*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^3, 1/6*((2*b^3*x^2 + b^2*x - 3*b)*sqrt(b*x + 2)*sqrt(x) - 6*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x)))/b^3]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+2)^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [59.8656459874,25.8388736797]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [33.9285577983,15.451549686]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{-40,[2,2]%%}+%%{46,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}]

20, [2, 3]%%}+%%{-46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{-24, [2, 0]%%}+%%{-4, [1, 4]%%}+%%{-20, [1, 3]%%}+%%{-40, [1, 2]%%}+%%{-48, [1, 1]%%}+%%{-32, [1, 0]%%}+%%{-1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{-24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{-16, [0, 0]%%}] at parameters values [54.7579903365, 81.9516051291] Warning, choosing root of [1, 0, %%{-4, [1, 1]%%}+%%{-4, [1, 0]%%}+%%{-4, [0, 1]%%}+%%{-8, [0, 0]%%}, 0, %%{-6, [2, 2]%%}+%%{-4, [2, 1]%%}+%%{-6, [2, 0]%%}+%%{-4, [1, 2]%%}+%%{-28, [1, 1]%%}+%%{-8, [1, 0]%%}+%%{-6, [0, 2]%%}+%%{-8, [0, 1]%%}+%%{-24, [0, 0]%%}, 0, %%{-4, [3, 3]%%}+%%{-4, [3, 2]%%}+%%{-4, [3, 1]%%}+%%{-4, [3, 0]%%}+%%{-4, [2, 3]%%}+%%{-64, [2, 2]%%}+%%{-20, [2, 1]%%}+%%{-8, [2, 0]%%}+%%{-4, [1, 3]%%}+%%{-20, [1, 2]%%}+%%{-128, [1, 1]%%}+%%{-16, [1, 0]%%}+%%{-4, [0, 3]%%}+%%{-8, [0, 2]%%}+%%{-16, [0, 1]%%}+%%{-32, [0, 0]%%}, 0, %%{-1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{-6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{-1, [4, 0]%%}+%%{-4, [3, 4]%%}+%%{-12, [3, 3]%%}+%%{-20, [3, 2]%%}+%%{-20, [3, 1]%%}+%%{-8, [3, 0]%%}+%%{-6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{-46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{-24, [2, 0]%%}+%%{-4, [1, 4]%%}+%%{-20, [1, 3]%%}+%%{-40, [1, 2]%%}+%%{-48, [1, 1]%%}+%%{-32, [1, 0]%%}+%%{-1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{-24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{-16, [0, 0]%%}] at parameters values [18.4052062202, 51.6443148847] $1/b*(2*b*abs(b)/b^2*(2*((12*b^5/144/b^7*\sqrt{b*x+2})*\sqrt{b*x+2}-78*b^5/144/b^7)*\sqrt{b*x+2}*\sqrt{b*x+2}+198*b^5/144/b^7)*\sqrt{b*x+2}*\sqrt{b*(b*x+2)-2*b}+5/2/b/\sqrt{b}*\ln(abs(\sqrt{b*(b*x+2)-2*b}-\sqrt{b}*\sqrt{b*x+2}))) + 4*abs(b)/b^2/b*(2*(1/8*\sqrt{b*x+2}*\sqrt{b*x+2}-5/8)*\sqrt{b*x+2}*\sqrt{b*(b*x+2)-2*b}-6*b/4/\sqrt{b}*\ln(abs(\sqrt{b*(b*x+2)-2*b}-\sqrt{b}*\sqrt{b*x+2}))))$

maple [A] time = 0.00, size = 93, normalized size = 1.11

$$\frac{(bx+2)^{\frac{3}{2}}x^{\frac{3}{2}}}{3b} - \frac{(bx+2)^{\frac{3}{2}}\sqrt{x}}{2b^2} + \frac{\sqrt{bx+2}\sqrt{x}}{2b^2} + \frac{\sqrt{(bx+2)x}\ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{2\sqrt{bx+2}b^{\frac{5}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{(3/2)}*(b*x+2)^{(1/2)}, x)$

[Out] $1/3/b*x^{(3/2)}*(b*x+2)^{(3/2)}-1/2/b^2*x^{(1/2)}*(b*x+2)^{(3/2)}+1/2*x^{(1/2)}*(b*x+2)^{(1/2)}/b^2+1/2/b^{(5/2)}*((b*x+2)*x)^{(1/2)}/(b*x+2)^{(1/2)}/x^{(1/2)}*\ln((b*x+1)/b^{(1/2)}+(b*x^2+2*x)^{(1/2)})$

maxima [B] time = 3.02, size = 134, normalized size = 1.60

$$-\frac{\frac{3\sqrt{bx+2}b^2}{\sqrt{x}} + \frac{8(bx+2)^{\frac{3}{2}}b}{x^2} - \frac{3(bx+2)^{\frac{5}{2}}}{x^2}}{3\left(b^5 - \frac{3(bx+2)b^4}{x} + \frac{3(bx+2)^2b^3}{x^2} - \frac{(bx+2)^3b^2}{x^3}\right)} - \frac{\log\left(-\frac{\sqrt{b}-\sqrt{bx+2}}{\sqrt{x}}\right)}{2b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+2)^(1/2),x, algorithm="maxima")

[Out]
$$-1/3*(3*\sqrt{b*x + 2}*b^2/\sqrt{x} + 8*(b*x + 2)^{(3/2)}*b/x^{(3/2)} - 3*(b*x + 2)^{(5/2)}/x^{(5/2)})/(b^5 - 3*(b*x + 2)*b^4/x + 3*(b*x + 2)^2*b^3/x^2 - (b*x + 2)^3*b^2/x^3) - 1/2*\log(-(\sqrt{b} - \sqrt{b*x + 2})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x + 2}/\sqrt{x}))/b^{(5/2)}$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} \sqrt{bx + 2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(b*x + 2)^(1/2),x)

[Out] int(x^(3/2)*(b*x + 2)^(1/2), x)

sympy [A] time = 5.22, size = 90, normalized size = 1.07

$$\frac{bx^{\frac{7}{2}}}{3\sqrt{bx+2}} + \frac{5x^{\frac{5}{2}}}{6\sqrt{bx+2}} - \frac{x^{\frac{3}{2}}}{6b\sqrt{bx+2}} - \frac{\sqrt{x}}{b^2\sqrt{bx+2}} + \frac{\operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)*(b*x+2)**(1/2),x)

[Out]
$$b*x^{(7/2)}/(3*\sqrt{b*x + 2}) + 5*x^{(5/2)}/(6*\sqrt{b*x + 2}) - x^{(3/2)}/(6*b*\sqrt{b*x + 2}) - \sqrt{x}/(b**2*\sqrt{b*x + 2}) + \operatorname{asinh}(\sqrt{2}*\sqrt{b}*\sqrt{x})/2/b^{(5/2)}$$

3.507 $\int \sqrt{x} \sqrt{2 + bx} dx$

Optimal. Leaf size=64

$$-\frac{\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} + \frac{1}{2}x^{3/2}\sqrt{bx+2} + \frac{\sqrt{x}\sqrt{bx+2}}{2b}$$

[Out] $-\operatorname{arcsinh}(1/2*b^{(1/2)*x^{(1/2)}*2^{(1/2)})/b^{(3/2)}+1/2*x^{(3/2)}*(b*x+2)^{(1/2)}+1/2*x^{(1/2)}*(b*x+2)^{(1/2)}/b$

Rubi [A] time = 0.01, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} + \frac{1}{2}x^{3/2}\sqrt{bx+2} + \frac{\sqrt{x}\sqrt{bx+2}}{2b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*Sqrt[2 + b*x], x]

[Out] $(\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/(2*b) + (x^{(3/2)}*\operatorname{Sqrt}[2 + b*x])/2 - \operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]]/b^{(3/2)}$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned}
\int \sqrt{x} \sqrt{2+bx} dx &= \frac{1}{2} x^{3/2} \sqrt{2+bx} + \frac{1}{2} \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx \\
&= \frac{\sqrt{x} \sqrt{2+bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2+bx} - \frac{\int \frac{1}{\sqrt{x} \sqrt{2+bx}} dx}{2b} \\
&= \frac{\sqrt{x} \sqrt{2+bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2+bx} - \frac{\text{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right)}{b} \\
&= \frac{\sqrt{x} \sqrt{2+bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2+bx} - \frac{\sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 51, normalized size = 0.80

$$\frac{\sqrt{x}(bx+1)\sqrt{bx+2}}{2b} - \frac{\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*Sqrt[2 + b*x], x]

[Out] (Sqrt[x]*(1 + b*x)*Sqrt[2 + b*x])/(2*b) - ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]]/b^(3/2)

fricas [A] time = 0.45, size = 101, normalized size = 1.58

$$\left[\frac{(b^2x + b)\sqrt{bx+2}\sqrt{x} + \sqrt{b} \log(bx - \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{2b^2}, \frac{(b^2x + b)\sqrt{bx+2}\sqrt{x} + 2\sqrt{-b} \arctan\left(\frac{\sqrt{bx+2}\sqrt{-b}}{b\sqrt{x}}\right)}{2b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(b*x+2)^(1/2), x, algorithm="fricas")

[Out] [1/2*((b^2*x + b)*sqrt(b*x + 2)*sqrt(x) + sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^2, 1/2*((b^2*x + b)*sqrt(b*x + 2)*sqrt(x) + 2*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))))/b^2]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(1/2)*(b*x+2)^(1/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [59.8656459874,25.8388736797]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [33.9285577983,15.451549686]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [54.7579903365,81.9516051291]Warning, cho
```

osing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [18.4052062202,51.6443148847] $1/b*(2*b*abs(b)/b^2/b*(2*(1/8*sqrt(b*x+2)*sqrt(b*x+2)-5/8)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)-6*b/4/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))+4*abs(b)/b^2*(1/2*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)+2*b/2/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))$

maple [A] time = 0.00, size = 75, normalized size = 1.17

$$\frac{\sqrt{bx+2} x^{\frac{3}{2}}}{2} + \frac{\sqrt{bx+2} \sqrt{x}}{2b} - \frac{\sqrt{(bx+2)x} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{2\sqrt{bx+2} b^{\frac{3}{2}} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)*(b*x+2)^(1/2),x)

[Out] $1/2*x^{(3/2)}*(b*x+2)^{(1/2)}+1/2*x^{(1/2)}*(b*x+2)^{(1/2)}/b-1/2/b^{(3/2)}*((b*x+2)*x)^{(1/2)}/(b*x+2)^{(1/2)}/x^{(1/2)}*ln((b*x+1)/b^{(1/2)}+(b*x^2+2*x)^{(1/2)})$

maxima [B] time = 2.91, size = 98, normalized size = 1.53

$$\frac{\frac{\sqrt{bx+2}b}{\sqrt{x}} + \frac{(bx+2)^{\frac{3}{2}}}{x^{\frac{3}{2}}}}{b^3 - \frac{2(bx+2)b^2}{x} + \frac{(bx+2)^2b}{x^2}} + \frac{\log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{2b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(b*x+2)^(1/2),x, algorithm="maxima")

[Out] $(sqrt(b*x+2)*b/sqrt(x) + (b*x+2)^{(3/2)}/x^{(3/2)})/(b^3 - 2*(b*x+2)*b^2/x + (b*x+2)^2*b/x^2) + 1/2*log(-(sqrt(b) - sqrt(b*x+2)/sqrt(x))/(sqrt(b) + sqrt(b*x+2)/sqrt(x)))/b^{(3/2)}$

mupad [B] time = 0.10, size = 46, normalized size = 0.72

$$\sqrt{x} \left(\frac{x}{2} + \frac{1}{2b} \right) \sqrt{bx+2} - \frac{\ln(bx + \sqrt{b} \sqrt{x} \sqrt{bx+2} + 1)}{2b^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)*(b*x + 2)^(1/2), x)`

[Out] `x^(1/2)*(x/2 + 1/(2*b))*(b*x + 2)^(1/2) - log(b*x + b^(1/2)*x^(1/2)*(b*x + 2)^(1/2) + 1)/(2*b^(3/2))`

sympy [A] time = 2.91, size = 71, normalized size = 1.11

$$\frac{bx^{\frac{5}{2}}}{2\sqrt{bx+2}} + \frac{3x^{\frac{3}{2}}}{2\sqrt{bx+2}} + \frac{\sqrt{x}}{b\sqrt{bx+2}} - \frac{\operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)*(b*x+2)**(1/2), x)`

[Out] `b*x**(5/2)/(2*sqrt(b*x + 2)) + 3*x**(3/2)/(2*sqrt(b*x + 2)) + sqrt(x)/(b*sqrt(b*x + 2)) - asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2)`

$$3.508 \quad \int \frac{\sqrt{2+bx}}{\sqrt{x}} dx$$

Optimal. Leaf size=40

$$\sqrt{x} \sqrt{bx+2} + \frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

[Out] $2*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)*2^{(1/2)}}/b^{(1/2)}+x^{(1/2)}*(b*x+2)^{(1/2)})$

Rubi [A] time = 0.01, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$\sqrt{x} \sqrt{bx+2} + \frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[2 + b*x]/Sqrt[x], x]

[Out] Sqrt[x]*Sqrt[2 + b*x] + (2*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{2+bx}}{\sqrt{x}} dx &= \sqrt{x} \sqrt{2+bx} + \int \frac{1}{\sqrt{x} \sqrt{2+bx}} dx \\
&= \sqrt{x} \sqrt{2+bx} + 2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x} \right) \\
&= \sqrt{x} \sqrt{2+bx} + \frac{2 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 1.00

$$\sqrt{x} \sqrt{bx+2} + \frac{2 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[2 + b*x]/Sqrt[x], x]

[Out] Sqrt[x]*Sqrt[2 + b*x] + (2*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

fricas [A] time = 0.49, size = 86, normalized size = 2.15

$$\left[\frac{\sqrt{bx+2} b \sqrt{x} + \sqrt{b} \log(bx + \sqrt{bx+2} \sqrt{b} \sqrt{x} + 1)}{b}, \frac{\sqrt{bx+2} b \sqrt{x} - 2 \sqrt{-b} \arctan\left(\frac{\sqrt{bx+2} \sqrt{-b}}{b \sqrt{x}}\right)}{b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(1/2), x, algorithm="fricas")

[Out] [(sqrt(b*x + 2)*b*sqrt(x) + sqrt(b)*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b, (sqrt(b*x + 2)*b*sqrt(x) - 2*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))))/b]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(1/2), x, algorithm="giac")


```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [85.3561567818,61.7937478349]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [71.707969239,78.6493344628]1/abs(b)*b^2/b*(1/b*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)-2/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2)))
```

maple [A] time = 0.00, size = 58, normalized size = 1.45

$$\sqrt{bx+2} \sqrt{x} + \frac{\sqrt{(bx+2)x} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{\sqrt{bx+2} \sqrt{b} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+2)^(1/2)/x^(1/2),x)

[Out] x^(1/2)*(b*x+2)^(1/2)+((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)/x^(1/2)*ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))/b^(1/2)

maxima [B] time = 2.96, size = 68, normalized size = 1.70

$$\frac{\log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{\sqrt{b}} - \frac{2\sqrt{bx+2}}{\left(b-\frac{bx+2}{x}\right)\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(1/2),x, algorithm="maxima")

[Out] -log(-(sqrt(b) - sqrt(b*x + 2)/sqrt(x))/(sqrt(b) + sqrt(b*x + 2)/sqrt(x)))/sqrt(b) - 2*sqrt(b*x + 2)/((b - (b*x + 2)/x)*sqrt(x))

mupad [B] time = 0.62, size = 40, normalized size = 1.00

$$\sqrt{x}\sqrt{bx+2} - \frac{4\operatorname{atanh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}-\sqrt{bx+2}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x + 2)^(1/2)/x^(1/2),x)

[Out] x^(1/2)*(b*x + 2)^(1/2) - (4*atanh((b^(1/2)*x^(1/2))/(2^(1/2) - (b*x + 2)^(1/2))))/b^(1/2)

sympy [A] time = 1.65, size = 37, normalized size = 0.92

$$\sqrt{x}\sqrt{bx+2} + \frac{2\operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)**(1/2)/x**(1/2),x)

[Out] sqrt(x)*sqrt(b*x + 2) + 2*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/sqrt(b)

$$3.509 \quad \int \frac{\sqrt{2+bx}}{x^{3/2}} dx$$

Optimal. Leaf size=41

$$2\sqrt{b} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right) - \frac{2\sqrt{bx+2}}{\sqrt{x}}$$

[Out] $2*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})*b^{(1/2)}-2*(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 54, 215}

$$2\sqrt{b} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right) - \frac{2\sqrt{bx+2}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[2 + b*x]/x^(3/2), x]

[Out] $(-2*\operatorname{Sqrt}[2 + b*x])/ \operatorname{Sqrt}[x] + 2*\operatorname{Sqrt}[b]*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/ \operatorname{Sqrt}[2]]$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{2+bx}}{x^{3/2}} dx &= -\frac{2\sqrt{2+bx}}{\sqrt{x}} + b \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx \\
&= -\frac{2\sqrt{2+bx}}{\sqrt{x}} + (2b) \text{Subst} \left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x} \right) \\
&= -\frac{2\sqrt{2+bx}}{\sqrt{x}} + 2\sqrt{b} \sinh^{-1} \left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}} \right)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 41, normalized size = 1.00

$$2\sqrt{b} \sinh^{-1} \left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}} \right) - \frac{2\sqrt{bx+2}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[2 + b*x]/x^(3/2), x]

[Out] (-2*Sqrt[2 + b*x])/Sqrt[x] + 2*Sqrt[b]*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]]

fricas [A] time = 0.48, size = 87, normalized size = 2.12

$$\left[\frac{\sqrt{b}x \log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1) - 2\sqrt{bx+2}\sqrt{x}}{x}, -\frac{2\left(\sqrt{-b}x \arctan\left(\frac{\sqrt{bx+2}\sqrt{-b}}{b\sqrt{x}}\right) + \sqrt{bx+2}\sqrt{x}\right)}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(3/2), x, algorithm="fricas")

[Out] [(sqrt(b)*x*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1) - 2*sqrt(b*x + 2)*sqrt(x))/x, -2*(sqrt(-b)*x*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))) + sqrt(b*x + 2)*sqrt(x))/x]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(3/2), x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%

$\} + \{ -8, [0, 0] \}, 0, \{ 6, [2, 2] \} + \{ 4, [2, 1] \} + \{ 6, [2, 0] \} + \{ 4, [1, 2] \} + \{ 28, [1, 1] \} + \{ 8, [1, 0] \} + \{ 6, [0, 2] \} + \{ 8, [0, 1] \} + \{ 24, [0, 0] \}, 0, \{ -4, [3, 3] \} + \{ 4, [3, 2] \} + \{ 4, [3, 1] \} + \{ -4, [3, 0] \} + \{ 4, [2, 3] \} + \{ -64, [2, 2] \} + \{ -20, [2, 1] \} + \{ 8, [2, 0] \} + \{ 4, [1, 3] \} + \{ 20, [1, 2] \} + \{ -128, [1, 1] \} + \{ 16, [1, 0] \} + \{ -4, [0, 3] \} + \{ 8, [0, 2] \} + \{ 16, [0, 1] \} + \{ -32, [0, 0] \}, 0, \{ 1, [4, 4] \} + \{ -4, [4, 3] \} + \{ 6, [4, 2] \} + \{ -4, [4, 1] \} + \{ 1, [4, 0] \} + \{ -4, [3, 4] \} + \{ 12, [3, 3] \} + \{ -20, [3, 2] \} + \{ 20, [3, 1] \} + \{ -8, [3, 0] \} + \{ 6, [2, 4] \} + \{ -20, [2, 3] \} + \{ 46, [2, 2] \} + \{ -40, [2, 1] \} + \{ 24, [2, 0] \} + \{ -4, [1, 4] \} + \{ 20, [1, 3] \} + \{ -40, [1, 2] \} + \{ 48, [1, 1] \} + \{ -32, [1, 0] \} + \{ 1, [0, 4] \} + \{ -8, [0, 3] \} + \{ 24, [0, 2] \} + \{ -32, [0, 1] \} + \{ 16, [0, 0] \}$ at parameters values [85.3561567 818,61.7937478349] Warning, choosing root of $\{ -4, [1, 1] \} + \{ -4, [1, 0] \} + \{ -4, [0, 1] \} + \{ -8, [0, 0] \}, 0, \{ 6, [2, 2] \} + \{ 4, [2, 1] \} + \{ 6, [2, 0] \} + \{ 4, [1, 2] \} + \{ 28, [1, 1] \} + \{ 8, [1, 0] \} + \{ 6, [0, 2] \} + \{ 8, [0, 1] \} + \{ 24, [0, 0] \}, 0, \{ -4, [3, 3] \} + \{ 4, [3, 2] \} + \{ 4, [3, 1] \} + \{ -4, [3, 0] \} + \{ 4, [2, 3] \} + \{ -64, [2, 2] \} + \{ 20, [2, 1] \} + \{ 8, [2, 0] \} + \{ 4, [1, 3] \} + \{ 20, [1, 2] \} + \{ -128, [1, 1] \} + \{ 16, [1, 0] \} + \{ -4, [0, 3] \} + \{ 8, [0, 2] \} + \{ 16, [0, 1] \} + \{ -32, [0, 0] \}, 0, \{ 1, [4, 4] \} + \{ -4, [4, 3] \} + \{ 6, [4, 2] \} + \{ -4, [4, 1] \} + \{ 1, [4, 0] \} + \{ -4, [3, 4] \} + \{ 12, [3, 3] \} + \{ -20, [3, 2] \} + \{ 20, [3, 1] \} + \{ -8, [3, 0] \} + \{ 6, [2, 4] \} + \{ -20, [2, 3] \} + \{ 46, [2, 2] \} + \{ -40, [2, 1] \} + \{ 24, [2, 0] \} + \{ -4, [1, 4] \} + \{ 20, [1, 3] \} + \{ -40, [1, 2] \} + \{ 48, [1, 1] \} + \{ -32, [1, 0] \} + \{ 1, [0, 4] \} + \{ -8, [0, 3] \} + \{ 24, [0, 2] \} + \{ -32, [0, 1] \} + \{ 16, [0, 0] \}$ at parameters values [71.707969239, 78.6493344628] $b/\text{abs}(b) * b^2/b * (-2 * \text{sqrt}(b*x+2) * \text{sqrt}(b*(b*x+2) - 2*b) / (b*(b*x+2) - 2*b) - 2/\text{sqrt}(b) * \ln(\text{abs}(\text{sqrt}(b*(b*x+2) - 2*b) - \text{sqrt}(b) * \text{sqrt}(b*x+2))))$

maple [A] time = 0.02, size = 59, normalized size = 1.44

$$\frac{\sqrt{bx+2} x \sqrt{b} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{\sqrt{bx+2} \sqrt{x}} - \frac{2\sqrt{bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x+2)^{(1/2)}/x^{(3/2)}, x)$

[Out] $-2*(b*x+2)^{(1/2)}/x^{(1/2)} + b^{(1/2)} * \ln((b*x+1)/b^{(1/2)} + (b*x^2+2*x)^{(1/2)}) * ((b*x+2)*x)^{(1/2)}/(b*x+2)^{(1/2)}/x^{(1/2)}$

maxima [A] time = 2.95, size = 54, normalized size = 1.32

$$-\sqrt{b} \log\left(-\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right) - \frac{2\sqrt{bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(3/2),x, algorithm="maxima")

[Out] -sqrt(b)*log(-(sqrt(b) - sqrt(b*x + 2)/sqrt(x))/(sqrt(b) + sqrt(b*x + 2)/sqrt(x))) - 2*sqrt(b*x + 2)/sqrt(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{bx+2}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x + 2)^(1/2)/x^(3/2), x)

[Out] int((b*x + 2)^(1/2)/x^(3/2), x)

sympy [A] time = 1.43, size = 48, normalized size = 1.17

$$-2\sqrt{b}\sqrt{1+\frac{2}{bx}} - \sqrt{b}\log\left(\frac{1}{bx}\right) + 2\sqrt{b}\log\left(\sqrt{1+\frac{2}{bx}}+1\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)**(1/2)/x**(3/2),x)

[Out] -2*sqrt(b)*sqrt(1 + 2/(b*x)) - sqrt(b)*log(1/(b*x)) + 2*sqrt(b)*log(sqrt(1 + 2/(b*x)) + 1)

$$3.510 \quad \int \frac{\sqrt{2+bx}}{x^{5/2}} dx$$

Optimal. Leaf size=18

$$-\frac{(bx+2)^{3/2}}{3x^{3/2}}$$

[Out] $-1/3*(b*x+2)^{(3/2)}/x^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$-\frac{(bx+2)^{3/2}}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[2 + b*x]/x^(5/2), x]

[Out] $-(2 + b*x)^{(3/2)}/(3*x^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{2+bx}}{x^{5/2}} dx = -\frac{(2+bx)^{3/2}}{3x^{3/2}}$$

Mathematica [A] time = 0.01, size = 18, normalized size = 1.00

$$-\frac{(bx+2)^{3/2}}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[2 + b*x]/x^(5/2), x]

[Out] $-1/3*(2 + b*x)^{(3/2)}/x^{(3/2)}$

fricas [A] time = 0.42, size = 12, normalized size = 0.67

$$-\frac{(bx+2)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(5/2),x, algorithm="fricas")

[Out] -1/3*(b*x + 2)^(3/2)/x^(3/2)

giac [B] time = 1.15, size = 29, normalized size = 1.61

$$-\frac{(bx+2)^{\frac{3}{2}}b^4}{3((bx+2)b-2b)^{\frac{3}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(5/2),x, algorithm="giac")

[Out] -1/3*(b*x + 2)^(3/2)*b^4/(((b*x + 2)*b - 2*b)^(3/2)*abs(b))

maple [A] time = 0.00, size = 13, normalized size = 0.72

$$-\frac{(bx+2)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+2)^(1/2)/x^(5/2),x)

[Out] -1/3*(b*x+2)^(3/2)/x^(3/2)

maxima [A] time = 1.31, size = 12, normalized size = 0.67

$$-\frac{(bx+2)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(5/2),x, algorithm="maxima")

[Out] -1/3*(b*x + 2)^(3/2)/x^(3/2)

mupad [B] time = 0.21, size = 18, normalized size = 1.00

$$-\frac{\sqrt{bx+2} \left(\frac{bx}{3} + \frac{2}{3} \right)}{x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x + 2)^(1/2)/x^(5/2), x)`

[Out] `-((b*x + 2)^(1/2)*((b*x)/3 + 2/3))/x^(3/2)`

sympy [B] time = 1.45, size = 37, normalized size = 2.06

$$-\frac{b^{\frac{3}{2}} \sqrt{1 + \frac{2}{bx}}}{3} - \frac{2\sqrt{b} \sqrt{1 + \frac{2}{bx}}}{3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)**(1/2)/x**(5/2), x)`

[Out] `-b**(3/2)*sqrt(1 + 2/(b*x))/3 - 2*sqrt(b)*sqrt(1 + 2/(b*x))/(3*x)`

$$3.511 \quad \int \frac{\sqrt{2+bx}}{x^{7/2}} dx$$

Optimal. Leaf size=38

$$\frac{b(bx+2)^{3/2}}{15x^{3/2}} - \frac{(bx+2)^{3/2}}{5x^{5/2}}$$

[Out] $-1/5*(b*x+2)^{(3/2)}/x^{(5/2)}+1/15*b*(b*x+2)^{(3/2)}/x^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{b(bx+2)^{3/2}}{15x^{3/2}} - \frac{(bx+2)^{3/2}}{5x^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[2 + b*x]/x^(7/2), x]

[Out] $-(2 + b*x)^{(3/2)}/(5*x^{(5/2)}) + (b*(2 + b*x)^{(3/2)})/(15*x^{(3/2)})$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{\sqrt{2+bx}}{x^{7/2}} dx = -\frac{(2+bx)^{3/2}}{5x^{5/2}} - \frac{1}{5}b \int \frac{\sqrt{2+bx}}{x^{5/2}} dx$$

$$= -\frac{(2+bx)^{3/2}}{5x^{5/2}} + \frac{b(2+bx)^{3/2}}{15x^{3/2}}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.61

$$\frac{(bx-3)(bx+2)^{3/2}}{15x^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[2 + b*x]/x^(7/2), x]

[Out] ((-3 + b*x)*(2 + b*x)^(3/2))/(15*x^(5/2))

fricas [A] time = 0.42, size = 25, normalized size = 0.66

$$\frac{(b^2x^2 - bx - 6)\sqrt{bx + 2}}{15x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(7/2), x, algorithm="fricas")

[Out] 1/15*(b^2*x^2 - b*x - 6)*sqrt(b*x + 2)/x^(5/2)

giac [A] time = 1.09, size = 42, normalized size = 1.11

$$\frac{((bx+2)b^5 - 5b^5)(bx+2)^{\frac{3}{2}}b}{15((bx+2)b - 2b)^{\frac{5}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(7/2), x, algorithm="giac")

[Out] 1/15*((b*x + 2)*b^5 - 5*b^5)*(b*x + 2)^(3/2)*b/(((b*x + 2)*b - 2*b)^(5/2)*abs(b))

maple [A] time = 0.00, size = 18, normalized size = 0.47

$$\frac{(bx+2)^{\frac{3}{2}}(bx-3)}{15x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+2)^(1/2)/x^(7/2),x)`

[Out] $1/15*(b*x+2)^{(3/2)}*(b*x-3)/x^{(5/2)}$

maxima [A] time = 1.32, size = 26, normalized size = 0.68

$$\frac{(bx+2)^{\frac{3}{2}}b}{6x^{\frac{3}{2}}} - \frac{(bx+2)^{\frac{5}{2}}}{10x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)^(1/2)/x^(7/2),x, algorithm="maxima")`

[Out] $1/6*(b*x+2)^{(3/2)}*b/x^{(3/2)} - 1/10*(b*x+2)^{(5/2)}/x^{(5/2)}$

mupad [B] time = 0.22, size = 26, normalized size = 0.68

$$-\frac{\sqrt{bx+2} \left(-\frac{b^2x^2}{15} + \frac{bx}{15} + \frac{2}{5} \right)}{x^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+2)^(1/2)/x^(7/2),x)`

[Out] $-((b*x+2)^{(1/2)}*((b*x)/15 - (b^2*x^2)/15 + 2/5))/x^{(5/2)}$

sympy [A] time = 4.72, size = 56, normalized size = 1.47

$$\frac{b^{\frac{5}{2}}\sqrt{1+\frac{2}{bx}}}{15} - \frac{b^{\frac{3}{2}}\sqrt{1+\frac{2}{bx}}}{15x} - \frac{2\sqrt{b}\sqrt{1+\frac{2}{bx}}}{5x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)**(1/2)/x**(7/2),x)`

[Out] $b^{(5/2)}*\sqrt{1+2/(b*x)}/15 - b^{(3/2)}*\sqrt{1+2/(b*x)}/(15*x) - 2*\sqrt{b}*\sqrt{1+2/(b*x)}/(5*x**2)$

$$3.512 \quad \int \frac{\sqrt{2+bx}}{x^{9/2}} dx$$

Optimal. Leaf size=59

$$-\frac{2b^2(bx+2)^{3/2}}{105x^{3/2}} + \frac{2b(bx+2)^{3/2}}{35x^{5/2}} - \frac{(bx+2)^{3/2}}{7x^{7/2}}$$

[Out] $-1/7*(b*x+2)^{(3/2)}/x^{(7/2)}+2/35*b*(b*x+2)^{(3/2)}/x^{(5/2)}-2/105*b^2*(b*x+2)^{(3/2)}/x^{(3/2)}$

Rubi [A] time = 0.01, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{2b^2(bx+2)^{3/2}}{105x^{3/2}} + \frac{2b(bx+2)^{3/2}}{35x^{5/2}} - \frac{(bx+2)^{3/2}}{7x^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[2 + b*x]/x^(9/2), x]

[Out] $-(2 + b*x)^{(3/2)}/(7*x^{(7/2)}) + (2*b*(2 + b*x)^{(3/2)})/(35*x^{(5/2)}) - (2*b^2*(2 + b*x)^{(3/2)})/(105*x^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{2+bx}}{x^{9/2}} dx &= -\frac{(2+bx)^{3/2}}{7x^{7/2}} - \frac{1}{7}(2b) \int \frac{\sqrt{2+bx}}{x^{7/2}} dx \\
&= -\frac{(2+bx)^{3/2}}{7x^{7/2}} + \frac{2b(2+bx)^{3/2}}{35x^{5/2}} + \frac{1}{35}(2b^2) \int \frac{\sqrt{2+bx}}{x^{5/2}} dx \\
&= -\frac{(2+bx)^{3/2}}{7x^{7/2}} + \frac{2b(2+bx)^{3/2}}{35x^{5/2}} - \frac{2b^2(2+bx)^{3/2}}{105x^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 0.54

$$-\frac{(bx+2)^{3/2}(2b^2x^2-6bx+15)}{105x^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[2 + b*x]/x^(9/2), x]

[Out] -1/105*((2 + b*x)^(3/2)*(15 - 6*b*x + 2*b^2*x^2))/x^(7/2)

fricas [A] time = 0.43, size = 34, normalized size = 0.58

$$-\frac{(2b^3x^3 - 2b^2x^2 + 3bx + 30)\sqrt{bx+2}}{105x^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(9/2), x, algorithm="fricas")

[Out] -1/105*(2*b^3*x^3 - 2*b^2*x^2 + 3*b*x + 30)*sqrt(b*x + 2)/x^(7/2)

giac [A] time = 1.11, size = 55, normalized size = 0.93

$$-\frac{(35b^7 + 2((bx+2)b^7 - 7b^7)(bx+2))(bx+2)^{3/2}b}{105((bx+2)b - 2b)^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(1/2)/x^(9/2), x, algorithm="giac")

[Out] -1/105*(35*b^7 + 2*((b*x + 2)*b^7 - 7*b^7)*(b*x + 2))*(b*x + 2)^(3/2)*b/(((b*x + 2)*b - 2*b)^(7/2)*abs(b))

maple [A] time = 0.00, size = 27, normalized size = 0.46

$$\frac{(bx + 2)^{\frac{3}{2}} (2b^2x^2 - 6bx + 15)}{105x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+2)^(1/2)/x^(9/2), x)`

[Out] `-1/105*(b*x+2)^(3/2)*(2*b^2*x^2-6*b*x+15)/x^(7/2)`

maxima [A] time = 1.27, size = 41, normalized size = 0.69

$$-\frac{(bx + 2)^{\frac{3}{2}} b^2}{12x^{\frac{3}{2}}} + \frac{(bx + 2)^{\frac{5}{2}} b}{10x^{\frac{5}{2}}} - \frac{(bx + 2)^{\frac{7}{2}}}{28x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)^(1/2)/x^(9/2), x, algorithm="maxima")`

[Out] `-1/12*(b*x + 2)^(3/2)*b^2/x^(3/2) + 1/10*(b*x + 2)^(5/2)*b/x^(5/2) - 1/28*(b*x + 2)^(7/2)/x^(7/2)`

mupad [B] time = 0.22, size = 34, normalized size = 0.58

$$-\frac{\sqrt{bx + 2} \left(\frac{2b^3x^3}{105} - \frac{2b^2x^2}{105} + \frac{bx}{35} + \frac{2}{7} \right)}{x^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x + 2)^(1/2)/x^(9/2), x)`

[Out] `-((b*x + 2)^(1/2)*((b*x)/35 - (2*b^2*x^2)/105 + (2*b^3*x^3)/105 + 2/7))/x^(7/2)`

sympy [B] time = 13.80, size = 270, normalized size = 4.58

$$\frac{2b^{\frac{19}{2}}x^5\sqrt{1+\frac{2}{bx}}}{105b^6x^5+420b^5x^4+420b^4x^3} - \frac{6b^{\frac{17}{2}}x^4\sqrt{1+\frac{2}{bx}}}{105b^6x^5+420b^5x^4+420b^4x^3} - \frac{3b^{\frac{15}{2}}x^3\sqrt{1+\frac{2}{bx}}}{105b^6x^5+420b^5x^4+420b^4x^3} - \frac{34b^{\frac{13}{2}}x^2\sqrt{1+\frac{2}{bx}}}{105b^6x^5+420b^5x^4+420b^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)**(1/2)/x**(9/2), x)`

```
[Out] -2*b**(19/2)*x**5*sqrt(1 + 2/(b*x))/(105*b**6*x**5 + 420*b**5*x**4 + 420*b*  
*4*x**3) - 6*b**(17/2)*x**4*sqrt(1 + 2/(b*x))/(105*b**6*x**5 + 420*b**5*x**  
4 + 420*b**4*x**3) - 3*b**(15/2)*x**3*sqrt(1 + 2/(b*x))/(105*b**6*x**5 + 42  
0*b**5*x**4 + 420*b**4*x**3) - 34*b**(13/2)*x**2*sqrt(1 + 2/(b*x))/(105*b**  
6*x**5 + 420*b**5*x**4 + 420*b**4*x**3) - 132*b**(11/2)*x*sqrt(1 + 2/(b*x))  
/(105*b**6*x**5 + 420*b**5*x**4 + 420*b**4*x**3) - 120*b**(9/2)*sqrt(1 + 2/  
(b*x))/(105*b**6*x**5 + 420*b**5*x**4 + 420*b**4*x**3)
```


3.513 $\int x^{5/2} \sqrt{2-bx} dx$

Optimal. Leaf size=112

$$\frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}} - \frac{5\sqrt{x}\sqrt{2-bx}}{8b^3} - \frac{5x^{3/2}\sqrt{2-bx}}{24b^2} + \frac{1}{4}x^{7/2}\sqrt{2-bx} - \frac{x^{5/2}\sqrt{2-bx}}{12b}$$

[Out] $5/4*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(7/2)}-5/24*x^{(3/2)}*(-b*x+2)^{(1/2)}/b^2-1/12*x^{(5/2)}*(-b*x+2)^{(1/2)}/b+1/4*x^{(7/2)}*(-b*x+2)^{(1/2)}-5/8*x^{(1/2)}*(-b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.03, antiderivative size = 112, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$-\frac{5x^{3/2}\sqrt{2-bx}}{24b^2} - \frac{5\sqrt{x}\sqrt{2-bx}}{8b^3} + \frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}} + \frac{1}{4}x^{7/2}\sqrt{2-bx} - \frac{x^{5/2}\sqrt{2-bx}}{12b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(5/2)}*\text{Sqrt}[2 - b*x], x]$

[Out] $(-5*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/(8*b^3) - (5*x^{(3/2)}*\text{Sqrt}[2 - b*x])/(24*b^2) - (x^{(5/2)}*\text{Sqrt}[2 - b*x])/(12*b) + (x^{(7/2)}*\text{Sqrt}[2 - b*x])/4 + (5*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/(4*b^{(7/2)})$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

$\text{Int}[1/(\text{Sqrt}[(a_.) + (b_.)*(x_)]*\text{Sqrt}[(c_.) + (d_.)*(x_)]), x_Symbol] \rightarrow \text{Dist}[2/\text{Sqrt}[b], \text{Subst}[\text{Int}[1/\text{Sqrt}[b*c - a*d + d*x^2], x], x, \text{Sqrt}[a + b*x]], x] /;$ FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
 \int x^{5/2} \sqrt{2-bx} \, dx &= \frac{1}{4} x^{7/2} \sqrt{2-bx} + \frac{1}{4} \int \frac{x^{5/2}}{\sqrt{2-bx}} \, dx \\
 &= -\frac{x^{5/2} \sqrt{2-bx}}{12b} + \frac{1}{4} x^{7/2} \sqrt{2-bx} + \frac{5 \int \frac{x^{3/2}}{\sqrt{2-bx}} \, dx}{12b} \\
 &= -\frac{5x^{3/2} \sqrt{2-bx}}{24b^2} - \frac{x^{5/2} \sqrt{2-bx}}{12b} + \frac{1}{4} x^{7/2} \sqrt{2-bx} + \frac{5 \int \frac{\sqrt{x}}{\sqrt{2-bx}} \, dx}{8b^2} \\
 &= -\frac{5\sqrt{x} \sqrt{2-bx}}{8b^3} - \frac{5x^{3/2} \sqrt{2-bx}}{24b^2} - \frac{x^{5/2} \sqrt{2-bx}}{12b} + \frac{1}{4} x^{7/2} \sqrt{2-bx} + \frac{5 \int \frac{1}{\sqrt{x} \sqrt{2-bx}} \, dx}{8b^3} \\
 &= -\frac{5\sqrt{x} \sqrt{2-bx}}{8b^3} - \frac{5x^{3/2} \sqrt{2-bx}}{24b^2} - \frac{x^{5/2} \sqrt{2-bx}}{12b} + \frac{1}{4} x^{7/2} \sqrt{2-bx} + \frac{5 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} \, dx, x\right)}{4b^3} \\
 &= -\frac{5\sqrt{x} \sqrt{2-bx}}{8b^3} - \frac{5x^{3/2} \sqrt{2-bx}}{24b^2} - \frac{x^{5/2} \sqrt{2-bx}}{12b} + \frac{1}{4} x^{7/2} \sqrt{2-bx} + \frac{5 \sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}}
 \end{aligned}$$

Mathematica [A] time = 0.04, size = 71, normalized size = 0.63

$$\frac{5 \sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}} + \frac{\sqrt{x} \sqrt{2-bx} (6b^3x^3 - 2b^2x^2 - 5bx - 15)}{24b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*Sqrt[2 - b*x], x]

[Out] (Sqrt[x]*Sqrt[2 - b*x]*(-15 - 5*b*x - 2*b^2*x^2 + 6*b^3*x^3))/(24*b^3) + (5*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(4*b^(7/2))

fricas [A] time = 0.44, size = 141, normalized size = 1.26

$$\left[\frac{(6b^4x^3 - 2b^3x^2 - 5b^2x - 15b)\sqrt{-bx+2}\sqrt{x} - 15\sqrt{-b} \log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1)}{24b^4}, \frac{(6b^4x^3 - 2b^3x^2 - 5b^2x - 15b)\sqrt{-bx+2}\sqrt{x} - 15\sqrt{-b} \log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1)}{24b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(5/2)*(-b*x+2)^(1/2),x, algorithm="fricas")
```

```
[Out] [1/24*((6*b^4*x^3 - 2*b^3*x^2 - 5*b^2*x - 15*b)*sqrt(-b*x + 2)*sqrt(x) - 15
*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^4, 1/24*((6*b^
4*x^3 - 2*b^3*x^2 - 5*b^2*x - 15*b)*sqrt(-b*x + 2)*sqrt(x) - 30*sqrt(b)*arc
tan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))))/b^4]
```

```
giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00
```

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(5/2)*(-b*x+2)^(1/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warni
ng, choosing root of [1,0,%%{4, [1,1]%%}+%%{4, [1,0]%%}+%%{-4, [0,1]%%}+
%%{-8, [0,0]%%}, 0, %%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{-4, [
1,2]%%}+%%{-28, [1,1]%%}+%%{-8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}
+%%{24, [0,0]%%}, 0, %%{4, [3,3]%%}+%%{-4, [3,2]%%}+%%{-4, [3,1]%%}+%%{4
, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%
}+%%{-4, [1,3]%%}+%%{-20, [1,2]%%}+%%{128, [1,1]%%}+%%{-16, [1,0]%%}+
%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0, %%{1,
[4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}
+%%{4, [3,4]%%}+%%{-12, [3,3]%%}+%%{20, [3,2]%%}+%%{-20, [3,1]%%}+%%{8
, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]
%%}+%%{24, [2,0]%%}+%%{4, [1,4]%%}+%%{-20, [1,3]%%}+%%{40, [1,2]%%}+%%
{-48, [1,1]%%}+%%{32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0
,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [-41.13435
40126,25.8388736797]Warning, choosing root of [1,0,%%{4, [1,1]%%}+%%{4, [1
,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0, %%{6, [2,2]%%}+%%{4, [2,1]%%}
+%%{6, [2,0]%%}+%%{-4, [1,2]%%}+%%{-28, [1,1]%%}+%%{-8, [1,0]%%}+%%{6,
[0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0, %%{4, [3,3]%%}+%%{-4, [3,2]%%
}+%%{-4, [3,1]%%}+%%{4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{2
0, [2,1]%%}+%%{8, [2,0]%%}+%%{-4, [1,3]%%}+%%{-20, [1,2]%%}+%%{128, [1,1
]%%}+%%{-16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+
%%{-32, [0,0]%%}, 0, %%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4,
[4,1]%%}+%%{1, [4,0]%%}+%%{4, [3,4]%%}+%%{-12, [3,3]%%}+%%{20, [3,2]%%
}+%%{-20, [3,1]%%}+%%{8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{4
6, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{4, [1,4]%%}+%%{-20, [1,3
]%%}+%%{40, [1,2]%%}+%%{-48, [1,1]%%}+%%{32, [1,0]%%}+%%{1, [0,4]%%}+
%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at par
ameters values [-67.0714422017,15.451549686]Warning, choosing root of [1,0,
%%{4, [1,1]%%}+%%{4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0, %%{6, [
2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{-4, [1,2]%%}+%%{-28, [1,1]%%}
+%%{-8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0, %%{4,
```

[3, 3]%%}+%%{-4, [3, 2]%%}+%%{-4, [3, 1]%%}+%%{4, [3, 0]%%}+%%{4, [2, 3]%%}+%%{-64, [2, 2]%%}+%%{20, [2, 1]%%}+%%{8, [2, 0]%%}+%%{-4, [1, 3]%%}+%%{-20, [1, 2]%%}+%%{128, [1, 1]%%}+%%{-16, [1, 0]%%}+%%{-4, [0, 3]%%}+%%{8, [0, 2]%%}+%%{16, [0, 1]%%}+%%{-32, [0, 0]%%}, 0, %%{1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{1, [4, 0]%%}+%%{4, [3, 4]%%}+%%{-12, [3, 3]%%}+%%{20, [3, 2]%%}+%%{-20, [3, 1]%%}+%%{8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{4, [1, 4]%%}+%%{-20, [1, 3]%%}+%%{40, [1, 2]%%}+%%{-48, [1, 1]%%}+%%{32, [1, 0]%%}+%%{1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{16, [0, 0]%%}] at parameters values [-46.2420096635, 81.9516051291] Warning, choosing root of [1, 0, %%{4, [1, 1]%%}+%%{4, [1, 0]%%}+%%{-4, [0, 1]%%}+%%{-8, [0, 0]%%}, 0, %%{6, [2, 2]%%}+%%{4, [2, 1]%%}+%%{6, [2, 0]%%}+%%{-4, [1, 2]%%}+%%{-28, [1, 1]%%}+%%{-8, [1, 0]%%}+%%{6, [0, 2]%%}+%%{8, [0, 1]%%}+%%{24, [0, 0]%%}, 0, %%{4, [3, 3]%%}+%%{-4, [3, 2]%%}+%%{-4, [3, 1]%%}+%%{4, [3, 0]%%}+%%{4, [2, 3]%%}+%%{-64, [2, 2]%%}+%%{20, [2, 1]%%}+%%{8, [2, 0]%%}+%%{-4, [1, 3]%%}+%%{-20, [1, 2]%%}+%%{128, [1, 1]%%}+%%{-16, [1, 0]%%}+%%{-4, [0, 3]%%}+%%{8, [0, 2]%%}+%%{16, [0, 1]%%}+%%{-32, [0, 0]%%}, 0, %%{1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{1, [4, 0]%%}+%%{4, [3, 4]%%}+%%{-12, [3, 3]%%}+%%{20, [3, 2]%%}+%%{-20, [3, 1]%%}+%%{8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{4, [1, 4]%%}+%%{-20, [1, 3]%%}+%%{40, [1, 2]%%}+%%{-48, [1, 1]%%}+%%{32, [1, 0]%%}+%%{1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{16, [0, 0]%%}] at parameters values [-82.5947937798, 51.6443148847] $\frac{1}{b} * (2 * b * \text{abs}(b) / b^2 * (2 * ((-90 * b^{11} / 1440 / b^{14} * \sqrt{-b * x + 2}) * \sqrt{-b * x + 2} + 750 * b^{11} / 1440 / b^{14}) * \sqrt{-b * x + 2}) * \sqrt{-b * x + 2} - 2445 * b^{11} / 1440 / b^{14}) * \sqrt{-b * x + 2}) * \sqrt{-b * x + 2} + 4185 * b^{11} / 1440 / b^{14}) * \sqrt{-b * x + 2}) * \sqrt{-b * (-b * x + 2) + 2 * b} - 35 / 8 / b^2 / \sqrt{-b} * \ln(\text{abs}(\sqrt{-b * (-b * x + 2) + 2 * b} - \sqrt{-b} * \sqrt{-b * x + 2})) - 4 * \text{abs}(b) / b^2 * (2 * ((12 * b^5 / 144 / b^7 * \sqrt{-b * x + 2}) * \sqrt{-b * x + 2} - 78 * b^5 / 144 / b^7) * \sqrt{-b * x + 2}) * \sqrt{-b * x + 2} + 198 * b^5 / 144 / b^7) * \sqrt{-b * x + 2}) * \sqrt{-b * (-b * x + 2) + 2 * b} - 5 / 2 / b / \sqrt{-b} * \ln(\text{abs}(\sqrt{-b * (-b * x + 2) + 2 * b} - \sqrt{-b} * \sqrt{-b * x + 2}))))$

maple [A] time = 0.01, size = 116, normalized size = 1.04

$$\frac{(-bx + 2)^{\frac{3}{2}} x^{\frac{5}{2}}}{4b} - \frac{5(-bx + 2)^{\frac{3}{2}} x^{\frac{3}{2}}}{12b^2} - \frac{5(-bx + 2)^{\frac{3}{2}} \sqrt{x}}{8b^3} + \frac{5\sqrt{-bx + 2} \sqrt{x}}{8b^3} + \frac{5\sqrt{-bx + 2} x \arctan\left(\frac{(x - \frac{1}{b})\sqrt{b}}{\sqrt{-bx^2 + 2x}}\right)}{8\sqrt{-bx + 2} b^{\frac{7}{2}} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{(5/2)} * (-b * x + 2)^{(1/2)}, x)$

[Out] $-1/4/b * x^{(5/2)} * (-b * x + 2)^{(3/2)} - 5/12/b^2 * x^{(3/2)} * (-b * x + 2)^{(3/2)} - 5/8/b^3 * x^{(1/2)} * (-b * x + 2)^{(3/2)} + 5/8 * x^{(1/2)} * (-b * x + 2)^{(1/2)} / b^3 + 5/8/b^{(7/2)} * ((-b * x + 2) * x)^{(1/2)} / (-b * x + 2)^{(1/2)} / x^{(1/2)} * \arctan(b^{(1/2)} * (x - 1/b) / (-b * x^2 + 2 * x)^{(1/2)})$

maxima [A] time = 2.93, size = 147, normalized size = 1.31

$$\frac{\frac{15\sqrt{-bx+2}b^3}{\sqrt{x}} - \frac{73(-bx+2)^{\frac{3}{2}}b^2}{x^{\frac{3}{2}}} - \frac{55(-bx+2)^{\frac{5}{2}}b}{x^{\frac{5}{2}}} - \frac{15(-bx+2)^{\frac{7}{2}}}{x^{\frac{7}{2}}}}{12\left(b^7 - \frac{4(bx-2)b^6}{x} + \frac{6(bx-2)^2b^5}{x^2} - \frac{4(bx-2)^3b^4}{x^3} + \frac{(bx-2)^4b^3}{x^4}\right)} - \frac{5 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{4b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(-b*x+2)^(1/2),x, algorithm="maxima")

[Out] 1/12*(15*sqrt(-b*x + 2)*b^3/sqrt(x) - 73*(-b*x + 2)^(3/2)*b^2/x^(3/2) - 55*(-b*x + 2)^(5/2)*b/x^(5/2) - 15*(-b*x + 2)^(7/2)/x^(7/2))/(b^7 - 4*(b*x - 2)*b^6/x + 6*(b*x - 2)^2*b^5/x^2 - 4*(b*x - 2)^3*b^4/x^3 + (b*x - 2)^4*b^3/x^4) - 5/4*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/b^(7/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} \sqrt{2 - bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(2 - b*x)^(1/2),x)

[Out] int(x^(5/2)*(2 - b*x)^(1/2), x)

sympy [A] time = 9.92, size = 252, normalized size = 2.25

$$\begin{cases} \frac{ibx^{\frac{9}{2}}}{4\sqrt{bx-2}} - \frac{7ix^{\frac{7}{2}}}{12\sqrt{bx-2}} - \frac{5ix^{\frac{5}{2}}}{24b\sqrt{bx-2}} - \frac{5ix^{\frac{3}{2}}}{24b^2\sqrt{bx-2}} + \frac{5i\sqrt{x}}{4b^3\sqrt{bx-2}} - \frac{5i\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{7}{2}}} & \text{for } \frac{|bx|}{2} > 1 \\ -\frac{bx^{\frac{9}{2}}}{4\sqrt{-bx+2}} + \frac{7x^{\frac{7}{2}}}{12\sqrt{-bx+2}} + \frac{5x^{\frac{5}{2}}}{24b\sqrt{-bx+2}} + \frac{5x^{\frac{3}{2}}}{24b^2\sqrt{-bx+2}} - \frac{5\sqrt{x}}{4b^3\sqrt{-bx+2}} + \frac{5\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{7}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)*(-b*x+2)**(1/2),x)

[Out] Piecewise((I*b*x**(9/2)/(4*sqrt(b*x - 2)) - 7*I*x**(7/2)/(12*sqrt(b*x - 2)) - I*x**(5/2)/(24*b*sqrt(b*x - 2)) - 5*I*x**(3/2)/(24*b**2*sqrt(b*x - 2)) + 5*I*sqrt(x)/(4*b**3*sqrt(b*x - 2)) - 5*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(7/2)), Abs(b*x)/2 > 1), (-b*x**(9/2)/(4*sqrt(-b*x + 2)) + 7*x**(7/2)/(12*sqrt(-b*x + 2)) + x**(5/2)/(24*b*sqrt(-b*x + 2)) + 5*x**(3/2)/(24*b**2*sqrt(-b*x + 2)) - 5*sqrt(x)/(4*b**3*sqrt(-b*x + 2)) + 5*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(7/2)), True))

3.514 $\int x^{3/2} \sqrt{2 - bx} dx$

Optimal. Leaf size=87

$$\frac{\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{\sqrt{x}\sqrt{2-bx}}{2b^2} + \frac{1}{3}x^{5/2}\sqrt{2-bx} - \frac{x^{3/2}\sqrt{2-bx}}{6b}$$

[Out] arcsin(1/2*b^(1/2)*x^(1/2)*2^(1/2))/b^(5/2)-1/6*x^(3/2)*(-b*x+2)^(1/2)/b+1/3*x^(5/2)*(-b*x+2)^(1/2)-1/2*x^(1/2)*(-b*x+2)^(1/2)/b^2

Rubi [A] time = 0.02, antiderivative size = 87, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$-\frac{\sqrt{x}\sqrt{2-bx}}{2b^2} + \frac{\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{1}{3}x^{5/2}\sqrt{2-bx} - \frac{x^{3/2}\sqrt{2-bx}}{6b}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)*Sqrt[2 - b*x], x]

[Out] -(Sqrt[x]*Sqrt[2 - b*x])/(2*b^2) - (x^(3/2)*Sqrt[2 - b*x])/(6*b) + (x^(5/2)*Sqrt[2 - b*x])/3 + ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]]/b^(5/2)

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int x^{3/2}\sqrt{2-bx} dx &= \frac{1}{3}x^{5/2}\sqrt{2-bx} + \frac{1}{3}\int \frac{x^{3/2}}{\sqrt{2-bx}} dx \\
&= -\frac{x^{3/2}\sqrt{2-bx}}{6b} + \frac{1}{3}x^{5/2}\sqrt{2-bx} + \frac{\int \frac{\sqrt{x}}{\sqrt{2-bx}} dx}{2b} \\
&= -\frac{\sqrt{x}\sqrt{2-bx}}{2b^2} - \frac{x^{3/2}\sqrt{2-bx}}{6b} + \frac{1}{3}x^{5/2}\sqrt{2-bx} + \frac{\int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx}{2b^2} \\
&= -\frac{\sqrt{x}\sqrt{2-bx}}{2b^2} - \frac{x^{3/2}\sqrt{2-bx}}{6b} + \frac{1}{3}x^{5/2}\sqrt{2-bx} + \frac{\text{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\
&= -\frac{\sqrt{x}\sqrt{2-bx}}{2b^2} - \frac{x^{3/2}\sqrt{2-bx}}{6b} + \frac{1}{3}x^{5/2}\sqrt{2-bx} + \frac{\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 60, normalized size = 0.69

$$\frac{\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{\sqrt{x}\sqrt{2-bx}(2b^2x^2 - bx - 3)}{6b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*Sqrt[2 - b*x], x]

[Out] (Sqrt[x]*Sqrt[2 - b*x]*(-3 - b*x + 2*b^2*x^2))/(6*b^2) + ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]]/b^(5/2)

fricas [A] time = 0.45, size = 125, normalized size = 1.44

$$\left[\frac{(2b^3x^2 - b^2x - 3b)\sqrt{-bx+2}\sqrt{x} - 3\sqrt{-b}\log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1)}{6b^3}, \frac{(2b^3x^2 - b^2x - 3b)\sqrt{-bx+2}}{6b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+2)^(1/2), x, algorithm="fricas")

[Out] [1/6*((2*b^3*x^2 - b^2*x - 3*b)*sqrt(-b*x + 2)*sqrt(x) - 3*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^3, 1/6*((2*b^3*x^2 - b^2*x - 3*b)*sqrt(-b*x + 2)*sqrt(x) - 6*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))))/b^3]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+2)^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of $[1,0, \{4, [1,1]\} + \{4, [1,0]\} + \{-4, [0,1]\} + \{-8, [0,0]\}, 0, \{6, [2,2]\} + \{4, [2,1]\} + \{6, [2,0]\} + \{-4, [1,2]\} + \{-28, [1,1]\} + \{-8, [1,0]\} + \{6, [0,2]\} + \{8, [0,1]\} + \{24, [0,0]\}, 0, \{4, [3,3]\} + \{-4, [3,2]\} + \{-4, [3,1]\} + \{4, [3,0]\} + \{4, [2,3]\} + \{-64, [2,2]\} + \{20, [2,1]\} + \{8, [2,0]\} + \{-4, [1,3]\} + \{-20, [1,2]\} + \{128, [1,1]\} + \{-16, [1,0]\} + \{-4, [0,3]\} + \{8, [0,2]\} + \{16, [0,1]\} + \{-32, [0,0]\}, 0, \{1, [4,4]\} + \{-4, [4,3]\} + \{6, [4,2]\} + \{-4, [4,1]\} + \{1, [4,0]\} + \{4, [3,4]\} + \{-12, [3,3]\} + \{20, [3,2]\} + \{-20, [3,1]\} + \{8, [3,0]\} + \{6, [2,4]\} + \{-20, [2,3]\} + \{46, [2,2]\} + \{-40, [2,1]\} + \{24, [2,0]\} + \{4, [1,4]\} + \{-20, [1,3]\} + \{40, [1,2]\} + \{-48, [1,1]\} + \{32, [1,0]\} + \{1, [0,4]\} + \{-8, [0,3]\} + \{24, [0,2]\} + \{-32, [0,1]\} + \{16, [0,0]\}$ at parameters values $[-41.1343540126, 25.8388736797]$ Warning, choosing root of $[1,0, \{4, [1,1]\} + \{4, [1,0]\} + \{-4, [0,1]\} + \{-8, [0,0]\}, 0, \{6, [2,2]\} + \{4, [2,1]\} + \{6, [2,0]\} + \{-4, [1,2]\} + \{-28, [1,1]\} + \{-8, [1,0]\} + \{6, [0,2]\} + \{8, [0,1]\} + \{24, [0,0]\}, 0, \{4, [3,3]\} + \{-4, [3,2]\} + \{-4, [3,1]\} + \{4, [3,0]\} + \{4, [2,3]\} + \{-64, [2,2]\} + \{20, [2,1]\} + \{8, [2,0]\} + \{-4, [1,3]\} + \{-20, [1,2]\} + \{128, [1,1]\} + \{-16, [1,0]\} + \{-4, [0,3]\} + \{8, [0,2]\} + \{16, [0,1]\} + \{-32, [0,0]\}, 0, \{1, [4,4]\} + \{-4, [4,3]\} + \{6, [4,2]\} + \{-4, [4,1]\} + \{1, [4,0]\} + \{4, [3,4]\} + \{-12, [3,3]\} + \{20, [3,2]\} + \{-20, [3,1]\} + \{8, [3,0]\} + \{6, [2,4]\} + \{-20, [2,3]\} + \{46, [2,2]\} + \{-40, [2,1]\} + \{24, [2,0]\} + \{4, [1,4]\} + \{-20, [1,3]\} + \{40, [1,2]\} + \{-48, [1,1]\} + \{32, [1,0]\} + \{1, [0,4]\} + \{-8, [0,3]\} + \{24, [0,2]\} + \{-32, [0,1]\} + \{16, [0,0]\}$ at parameters values $[-67.0714422017, 15.451549686]$ Warning, choosing root of $[1,0, \{4, [1,1]\} + \{4, [1,0]\} + \{-4, [0,1]\} + \{-8, [0,0]\}, 0, \{6, [2,2]\} + \{4, [2,1]\} + \{6, [2,0]\} + \{-4, [1,2]\} + \{-28, [1,1]\} + \{-8, [1,0]\} + \{6, [0,2]\} + \{8, [0,1]\} + \{24, [0,0]\}, 0, \{4, [3,3]\} + \{-4, [3,2]\} + \{-4, [3,1]\} + \{4, [3,0]\} + \{4, [2,3]\} + \{-64, [2,2]\} + \{20, [2,1]\} + \{8, [2,0]\} + \{-4, [1,3]\} + \{-20, [1,2]\} + \{128, [1,1]\} + \{-16, [1,0]\} + \{-4, [0,3]\} + \{8, [0,2]\} + \{16, [0,1]\} + \{-32, [0,0]\}, 0, \{1, [4,4]\} + \{-4, [4,3]\} + \{6, [4,2]\} + \{-4, [4,1]\} + \{1, [4,0]\} + \{4, [3,4]\} + \{-12, [3,3]\} + \{20, [3,2]\} + \{-20, [3,1]\} + \{8, [3,0]\} + \{6, [2,4]\} + \{-20, [2,3]\} + \{46, [2,2]\} + \{-40, [2,1]\} + \{24, [2,0]\} + \{4, [1,4]\} + \{-20, [1,3]\} + \{40, [1,2]\} + \{-48, [1,1]\} + \{32, [1,0]\} + \{1, [0,4]\} + \{-8, [0,3]\} + \{24, [0,2]\} + \{-32, [0,1]\} + \{16, [0,0]\}$

Warning, choosing root of [1,0,4,1,1]+4, [1,0]+-4, [0,1]+-8, [0,0], 0, 6, [2,2]+4, [2,1]+6, [2,0]+-4, [1,2]+-28, [1,1]+-8, [1,0]+6, [0,2]+8, [0,1]+24, [0,0], 0, 4, [3,3]+-4, [3,2]+-4, [3,1]+4, [3,0]+4, [2,3]+-64, [2,2]+20, [2,1]+8, [2,0]+-4, [1,3]+-20, [1,2]+128, [1,1]+-16, [1,0]+-4, [0,3]+8, [0,2]+16, [0,1]+-32, [0,0], 0, 1, [4,4]+-4, [4,3]+6, [4,2]+-4, [4,1]+1, [4,0]+4, [3,4]+-12, [3,3]+20, [3,2]+-20, [3,1]+8, [3,0]+6, [2,4]+-20, [2,3]+46, [2,2]+-40, [2,1]+24, [2,0]+4, [1,4]+-20, [1,3]+40, [1,2]+-48, [1,1]+32, [1,0]+1, [0,4]+-8, [0,3]+24, [0,2]+-32, [0,1]+16, [0,0]] at parameters values [-46.2420096635,81.9516051291]

Warning, choosing root of [1,0,4,1,1]+4, [1,0]+-4, [0,1]+-8, [0,0], 0, 6, [2,2]+4, [2,1]+6, [2,0]+-4, [1,2]+-28, [1,1]+-8, [1,0]+6, [0,2]+8, [0,1]+24, [0,0], 0, 4, [3,3]+-4, [3,2]+-4, [3,1]+4, [3,0]+4, [2,3]+-64, [2,2]+20, [2,1]+8, [2,0]+-4, [1,3]+-20, [1,2]+128, [1,1]+-16, [1,0]+-4, [0,3]+8, [0,2]+16, [0,1]+-32, [0,0], 0, 1, [4,4]+-4, [4,3]+6, [4,2]+-4, [4,1]+1, [4,0]+4, [3,4]+-12, [3,3]+20, [3,2]+-20, [3,1]+8, [3,0]+6, [2,4]+-20, [2,3]+46, [2,2]+-40, [2,1]+24, [2,0]+4, [1,4]+-20, [1,3]+40, [1,2]+-48, [1,1]+32, [1,0]+1, [0,4]+-8, [0,3]+24, [0,2]+-32, [0,1]+16, [0,0]] at parameters values [-82.5947937798,51.6443148847]

$$1/b*(2*b*abs(b)/b^2*(2*((12*b^5/144/b^7*\sqrt{-b*x+2})*\sqrt{-b*x+2}-78*b^5/144/b^7)*\sqrt{-b*x+2}*\sqrt{-b*x+2}+198*b^5/144/b^7)*\sqrt{-b*x+2}*\sqrt{-b*(-b*x+2)+2*b}-5/2/b/\sqrt{-b}*\ln(abs(\sqrt{-b*(-b*x+2)+2*b}-\sqrt{-b}*\sqrt{-b*x+2}))))+4*abs(b)/b^2/b*(2*(1/8*\sqrt{-b*x+2}*\sqrt{-b*x+2}-5/8)*\sqrt{-b*x+2}*\sqrt{-b*(-b*x+2)+2*b}+6*b/4/\sqrt{-b}*\ln(abs(\sqrt{-b*(-b*x+2)+2*b}-\sqrt{-b}*\sqrt{-b*x+2}))))$$

maple [A] time = 0.00, size = 100, normalized size = 1.15

$$-\frac{(-bx+2)^{\frac{3}{2}}x^{\frac{3}{2}}}{3b}-\frac{(-bx+2)^{\frac{3}{2}}\sqrt{x}}{2b^2}+\frac{\sqrt{-bx+2}\sqrt{x}}{2b^2}+\frac{\sqrt{(-bx+2)x}\arctan\left(\frac{(x-\frac{1}{b})\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{2\sqrt{-bx+2}b^2\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(-b*x+2)^(1/2),x)

[Out] $-1/3/b*x^{3/2}*(-b*x+2)^{3/2}-1/2/b^2*x^{1/2}*(-b*x+2)^{3/2}+1/2*x^{1/2}*(-b*x+2)^{1/2}/b^2+1/2/b^{5/2}*((-b*x+2)*x)^{1/2}/(-b*x+2)^{1/2}/x^{1/2}*\arctan((x-1/b)/(-b*x^2+2*x)^{1/2}*b^{1/2})$

maxima [A] time = 2.98, size = 117, normalized size = 1.34

$$\frac{\frac{3\sqrt{-bx+2}b^2}{\sqrt{x}}-\frac{8(-bx+2)^{\frac{3}{2}}b}{x^2}-\frac{3(-bx+2)^{\frac{5}{2}}}{x^2}}{3\left(b^5-\frac{3(bx-2)b^4}{x}+\frac{3(bx-2)^2b^3}{x^2}-\frac{(bx-2)^3b^2}{x^3}\right)}-\frac{\arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+2)^(1/2),x, algorithm="maxima")

[Out] 1/3*(3*sqrt(-b*x + 2)*b^2/sqrt(x) - 8*(-b*x + 2)^(3/2)*b/x^(3/2) - 3*(-b*x + 2)^(5/2)/x^(5/2))/(b^5 - 3*(b*x - 2)*b^4/x + 3*(b*x - 2)^2*b^3/x^2 - (b*x - 2)^3*b^2/x^3) - arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/b^(5/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} \sqrt{2 - bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(2 - b*x)^(1/2),x)

[Out] int(x^(3/2)*(2 - b*x)^(1/2), x)

sympy [A] time = 5.29, size = 196, normalized size = 2.25

$$\left\{ \begin{array}{ll} \frac{ibx^{\frac{7}{2}}}{3\sqrt{bx-2}} - \frac{5ix^{\frac{5}{2}}}{6\sqrt{bx-2}} - \frac{ix^{\frac{3}{2}}}{6b\sqrt{bx-2}} + \frac{i\sqrt{x}}{b^2\sqrt{bx-2}} - \frac{i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{5}{2}}} & \text{for } \frac{|bx|}{2} > 1 \\ -\frac{bx^{\frac{7}{2}}}{3\sqrt{-bx+2}} + \frac{5x^{\frac{5}{2}}}{6\sqrt{-bx+2}} + \frac{x^{\frac{3}{2}}}{6b\sqrt{-bx+2}} - \frac{\sqrt{x}}{b^2\sqrt{-bx+2}} + \frac{\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{5}{2}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)*(-b*x+2)**(1/2),x)

[Out] Piecewise((I*b*x**(7/2)/(3*sqrt(b*x - 2)) - 5*I*x**(5/2)/(6*sqrt(b*x - 2)) - I*x**(3/2)/(6*b*sqrt(b*x - 2)) + I*sqrt(x)/(b**2*sqrt(b*x - 2)) - I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(5/2), Abs(b*x)/2 > 1), (-b*x**(7/2)/(3*sqrt(-b*x + 2)) + 5*x**(5/2)/(6*sqrt(-b*x + 2)) + x**(3/2)/(6*b*sqrt(-b*x + 2)) - sqrt(x)/(b**2*sqrt(-b*x + 2)) + asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(5/2), True))

3.515 $\int \sqrt{x} \sqrt{2 - bx} dx$

Optimal. Leaf size=65

$$\frac{\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} + \frac{1}{2}x^{3/2}\sqrt{2-bx} - \frac{\sqrt{x}\sqrt{2-bx}}{2b}$$

[Out] arcsin(1/2*b^(1/2)*x^(1/2)*2^(1/2))/b^(3/2)+1/2*x^(3/2)*(-b*x+2)^(1/2)-1/2*x^(1/2)*(-b*x+2)^(1/2)/b

Rubi [A] time = 0.01, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$\frac{\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} + \frac{1}{2}x^{3/2}\sqrt{2-bx} - \frac{\sqrt{x}\sqrt{2-bx}}{2b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*Sqrt[2 - b*x],x]

[Out] -(Sqrt[x]*Sqrt[2 - b*x])/(2*b) + (x^(3/2)*Sqrt[2 - b*x])/2 + ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]]/b^(3/2)

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \sqrt{x} \sqrt{2-bx} \, dx &= \frac{1}{2} x^{3/2} \sqrt{2-bx} + \frac{1}{2} \int \frac{\sqrt{x}}{\sqrt{2-bx}} \, dx \\
&= -\frac{\sqrt{x} \sqrt{2-bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2-bx} + \frac{\int \frac{1}{\sqrt{x} \sqrt{2-bx}} \, dx}{2b} \\
&= -\frac{\sqrt{x} \sqrt{2-bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2-bx} + \frac{\text{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} \, dx, x, \sqrt{x}\right)}{b} \\
&= -\frac{\sqrt{x} \sqrt{2-bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2-bx} + \frac{\sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 51, normalized size = 0.78

$$\frac{\sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} + \frac{\sqrt{x} \sqrt{2-bx} (bx-1)}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*Sqrt[2 - b*x], x]

[Out] (Sqrt[x]*Sqrt[2 - b*x]*(-1 + b*x))/(2*b) + ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]]/b^(3/2)

fricas [A] time = 0.46, size = 107, normalized size = 1.65

$$\left[\frac{(b^2x - b)\sqrt{-bx + 2} \sqrt{x} - \sqrt{-b} \log(-bx + \sqrt{-bx + 2} \sqrt{-b} \sqrt{x} + 1)}{2b^2}, \frac{(b^2x - b)\sqrt{-bx + 2} \sqrt{x} - 2\sqrt{b} \arctan\left(\frac{\sqrt{-bx + 2} \sqrt{x}}{\sqrt{b}}\right)}{2b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(-b*x+2)^(1/2), x, algorithm="fricas")

[Out] [1/2*((b^2*x - b)*sqrt(-b*x + 2)*sqrt(x) - sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^2, 1/2*((b^2*x - b)*sqrt(-b*x + 2)*sqrt(x) - 2*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))))/b^2]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(1/2)*(-b*x+2)^(1/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-41.1343540126,25.8388736797]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-67.0714422017,15.451549686]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-46.2420096635,81.9516051291]Warning
```

g, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-82.594793 7798,51.6443148847] 1/b*(-2*b*abs(b)/b^2/b*(2*(1/8*sqrt(-b*x+2)*sqrt(-b*x+2)-5/8)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)+6*b/4/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b))-sqrt(-b)*sqrt(-b*x+2))))-4*abs(b)/b^2*(1/2*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)-2*b/2/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b))-sqrt(-b)*sqrt(-b*x+2))))))

maple [A] time = 0.00, size = 81, normalized size = 1.25

$$\frac{\sqrt{-bx+2} x^{\frac{3}{2}}}{2} - \frac{\sqrt{-bx+2} \sqrt{x}}{2b} + \frac{\sqrt{-bx+2} x \arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{2\sqrt{-bx+2} b^{\frac{3}{2}} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)*(-b*x+2)^(1/2),x)

[Out] 1/2*x^(3/2)*(-b*x+2)^(1/2)-1/2*x^(1/2)*(-b*x+2)^(1/2)/b+1/2/b^(3/2)*((-b*x+2)*x)^(1/2)/(-b*x+2)^(1/2)/x^(1/2)*arctan((x-1/b)/(-b*x^2+2*x)^(1/2)*b^(1/2))

maxima [A] time = 2.95, size = 81, normalized size = 1.25

$$\frac{\frac{\sqrt{-bx+2}b}{\sqrt{x}} - \frac{(-bx+2)^{\frac{3}{2}}}{x^{\frac{3}{2}}}}{b^3 - \frac{2(bx-2)b^2}{x} + \frac{(bx-2)^2b}{x^2}} - \frac{\arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(-b*x+2)^(1/2),x, algorithm="maxima")

[Out] (sqrt(-b*x + 2)*b/sqrt(x) - (-b*x + 2)^(3/2)/x^(3/2))/(b^3 - 2*(b*x - 2)*b^2/x + (b*x - 2)^2*b/x^2) - arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/b^(3/2)

mupad [B] time = 0.10, size = 53, normalized size = 0.82

$$\sqrt{x} \left(\frac{x}{2} - \frac{1}{2b} \right) \sqrt{2-bx} - \frac{\ln(\sqrt{-b} \sqrt{x} \sqrt{2-bx} - bx + 1)}{2(-b)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)*(2 - b*x)^(1/2),x)`

[Out] $x^{1/2}*(x/2 - 1/(2*b))*(2 - b*x)^{1/2} - \log((-b)^{1/2}*x^{1/2}*(2 - b*x)^{1/2} - b*x + 1)/(2*(-b)^{3/2})$

sympy [A] time = 2.94, size = 156, normalized size = 2.40

$$\begin{cases} \frac{ibx^{\frac{5}{2}}}{2\sqrt{bx-2}} - \frac{3ix^{\frac{3}{2}}}{2\sqrt{bx-2}} + \frac{i\sqrt{x}}{b\sqrt{bx-2}} - \frac{i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}} & \text{for } \frac{|bx|}{2} > 1 \\ -\frac{bx^{\frac{5}{2}}}{2\sqrt{-bx+2}} + \frac{3x^{\frac{3}{2}}}{2\sqrt{-bx+2}} - \frac{\sqrt{x}}{b\sqrt{-bx+2}} + \frac{\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)*(-b*x+2)**(1/2),x)`

[Out] `Piecewise((I*b*x**(5/2)/(2*sqrt(b*x - 2)) - 3*I*x**(3/2)/(2*sqrt(b*x - 2)) + I*sqrt(x)/(b*sqrt(b*x - 2)) - I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2), Abs(b*x)/2 > 1), (-b*x**(5/2)/(2*sqrt(-b*x + 2)) + 3*x**(3/2)/(2*sqrt(-b*x + 2)) - sqrt(x)/(b*sqrt(-b*x + 2)) + asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2), True))`

$$3.516 \quad \int \frac{\sqrt{2-bx}}{\sqrt{x}} dx$$

Optimal. Leaf size=41

$$\sqrt{x} \sqrt{2-bx} + \frac{2 \sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

[Out] 2*arcsin(1/2*b^(1/2)*x^(1/2)*2^(1/2))/b^(1/2)+x^(1/2)*(-b*x+2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$\sqrt{x} \sqrt{2-bx} + \frac{2 \sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[2 - b*x]/Sqrt[x],x]

[Out] Sqrt[x]*Sqrt[2 - b*x] + (2*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{2-bx}}{\sqrt{x}} dx &= \sqrt{x} \sqrt{2-bx} + \int \frac{1}{\sqrt{x} \sqrt{2-bx}} dx \\
&= \sqrt{x} \sqrt{2-bx} + 2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x} \right) \\
&= \sqrt{x} \sqrt{2-bx} + \frac{2 \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 41, normalized size = 1.00

$$\sqrt{x} \sqrt{2-bx} + \frac{2 \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[2 - b*x]/Sqrt[x], x]

[Out] Sqrt[x]*Sqrt[2 - b*x] + (2*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

fricas [A] time = 0.46, size = 89, normalized size = 2.17

$$\left[\frac{\sqrt{-bx+2} b \sqrt{x} - \sqrt{-b} \log(-bx + \sqrt{-bx+2} \sqrt{-b} \sqrt{x} + 1)}{b}, \frac{\sqrt{-bx+2} b \sqrt{x} - 2 \sqrt{b} \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b} \sqrt{x}}\right)}{b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(1/2), x, algorithm="fricas")

[Out] [(sqrt(-b*x + 2)*b*sqrt(x) - sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b, (sqrt(-b*x + 2)*b*sqrt(x) - 2*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))))/b]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(1/2), x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of $[1,0,4,1,1] + 4[1,0] - 4[0,1] - 8[0,0], 0, 6[2,2] + 4[2,1] + 6[2,0] - 4[1,2] - 28[1,1] - 8[1,0] + 6[0,2] + 8[0,1] + 24[0,0], 0, 4[3,3] - 4[3,2] - 4[3,1] + 4[3,0] + 4[2,3] - 64[2,2] + 20[2,1] + 8[2,0] - 4[1,3] - 20[1,2] + 128[1,1] - 16[1,0] - 4[0,3] + 8[0,2] + 16[0,1] - 32[0,0], 0, 1[4,4] - 4[4,3] + 6[4,2] - 4[4,1] + 1[4,0] + 4[3,4] - 12[3,3] + 20[3,2] - 20[3,1] + 8[3,0] + 6[2,4] - 20[2,3] + 46[2,2] - 40[2,1] + 24[2,0] + 4[1,4] - 20[1,3] + 40[1,2] - 48[1,1] + 32[1,0] + 1[0,4] - 8[0,3] + 24[0,2] - 32[0,1] + 16[0,0]$ at parameters values $[-15.6438432182, 61.7937478349]$ Warning, choosing root of $[1,0,4,1,1] + 4[1,0] - 4[0,1] - 8[0,0], 0, 6[2,2] + 4[2,1] + 6[2,0] - 4[1,2] - 28[1,1] - 8[1,0] + 6[0,2] + 8[0,1] + 24[0,0], 0, 4[3,3] - 4[3,2] - 4[3,1] + 4[3,0] + 4[2,3] - 64[2,2] + 20[2,1] + 8[2,0] - 4[1,3] - 20[1,2] + 128[1,1] - 16[1,0] - 4[0,3] + 8[0,2] + 16[0,1] - 32[0,0], 0, 1[4,4] - 4[4,3] + 6[4,2] - 4[4,1] + 1[4,0] + 4[3,4] - 12[3,3] + 20[3,2] - 20[3,1] + 8[3,0] + 6[2,4] - 20[2,3] + 46[2,2] - 40[2,1] + 24[2,0] + 4[1,4] - 20[1,3] + 40[1,2] - 48[1,1] + 32[1,0] + 1[0,4] - 8[0,3] + 24[0,2] - 32[0,1] + 16[0,0]$ at parameters values $[-29.292030761, 78.6493344628]$ $1/\text{abs}(b) \cdot b^2/b \cdot (1/b \cdot \sqrt{-bx+2}) \cdot \sqrt{-bx+2} + 2/\sqrt{-b} \cdot \ln(\text{abs}(\sqrt{-b(-bx+2)+2b}) - \sqrt{-b} \cdot \sqrt{-bx+2}))$

maple [B] time = 0.00, size = 63, normalized size = 1.54

$$\sqrt{-bx+2} \sqrt{x} + \frac{\sqrt{-bx+2} x \arctan\left(\frac{(x-\frac{1}{b})\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{\sqrt{-bx+2} \sqrt{b} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((-b*x+2)^{(1/2)}/x^{(1/2)}, x)$

[Out] $x^{(1/2)} * (-b*x+2)^{(1/2)} + ((-b*x+2)*x)^{(1/2)} / (-b*x+2)^{(1/2)} / x^{(1/2)} / b^{(1/2)} * \text{arctan}((x-1/b) / (-b*x^2+2*x)^{(1/2)} * b^{(1/2)})$

maxima [A] time = 2.91, size = 49, normalized size = 1.20

$$-\frac{2 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{b}} + \frac{2\sqrt{-bx+2}}{\left(b - \frac{bx-2}{x}\right)\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(1/2),x, algorithm="maxima")

[Out] -2*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/sqrt(b) + 2*sqrt(-b*x + 2)/((b - (b*x - 2)/x)*sqrt(x))

mupad [B] time = 0.56, size = 42, normalized size = 1.02

$$\sqrt{x} \sqrt{2-bx} - \frac{4 \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}-\sqrt{2-bx}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((2 - b*x)^(1/2)/x^(1/2),x)

[Out] x^(1/2)*(2 - b*x)^(1/2) - (4*atan((b^(1/2)*x^(1/2))/(2^(1/2) - (2 - b*x)^(1/2))))/b^(1/2)

sympy [A] time = 1.71, size = 121, normalized size = 2.95

$$\begin{cases} \frac{ibx^{\frac{3}{2}}}{\sqrt{bx-2}} - \frac{2i\sqrt{x}}{\sqrt{bx-2}} - \frac{2i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}} & \text{for } \frac{|bx|}{2} > 1 \\ -\frac{bx^{\frac{3}{2}}}{\sqrt{-bx+2}} + \frac{2\sqrt{x}}{\sqrt{-bx+2}} + \frac{2 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)**(1/2)/x**(1/2),x)

[Out] Piecewise((I*b*x**(3/2)/sqrt(b*x - 2) - 2*I*sqrt(x)/sqrt(b*x - 2) - 2*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/sqrt(b), Abs(b*x)/2 > 1), (-b*x**(3/2)/sqrt(-b*x + 2) + 2*sqrt(x)/sqrt(-b*x + 2) + 2*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/sqrt(b), True))

$$3.517 \quad \int \frac{\sqrt{2-bx}}{x^{3/2}} dx$$

Optimal. Leaf size=42

$$-\frac{2\sqrt{2-bx}}{\sqrt{x}} - 2\sqrt{b} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)$$

[Out] $-2*\arcsin(1/2*b^{(1/2)*x^{(1/2)}*2^{(1/2)})*b^{(1/2)}-2*(-b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {47, 54, 216}

$$-\frac{2\sqrt{2-bx}}{\sqrt{x}} - 2\sqrt{b} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[2 - b*x]/x^(3/2), x]

[Out] $(-2*\text{Sqrt}[2 - b*x])/\text{Sqrt}[x] - 2*\text{Sqrt}[b]*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]]$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{2-bx}}{x^{3/2}} dx &= -\frac{2\sqrt{2-bx}}{\sqrt{x}} - b \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx \\
&= -\frac{2\sqrt{2-bx}}{\sqrt{x}} - (2b) \text{Subst} \left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x} \right) \\
&= -\frac{2\sqrt{2-bx}}{\sqrt{x}} - 2\sqrt{b} \sin^{-1} \left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}} \right)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 42, normalized size = 1.00

$$-\frac{2\sqrt{2-bx}}{\sqrt{x}} - 2\sqrt{b} \sin^{-1} \left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}} \right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[2 - b*x]/x^(3/2), x]

[Out] (-2*Sqrt[2 - b*x])/Sqrt[x] - 2*Sqrt[b]*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]]

fricas [A] time = 0.48, size = 90, normalized size = 2.14

$$\left[\frac{\sqrt{-b}x \log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1) - 2\sqrt{-bx+2}\sqrt{x}}{x}, \frac{2\left(\sqrt{b}x \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) - \sqrt{-bx+2}\sqrt{x}\right)}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(3/2), x, algorithm="fricas")

[Out] [(sqrt(-b)*x*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1) - 2*sqrt(-b*x + 2)*sqrt(x))/x, 2*(sqrt(b)*x*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) - sqrt(-b*x + 2)*sqrt(x))/x]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(3/2), x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of $[1, 0, \{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}]$ at parameters values $[-15.6438432182, 61.7937478349]$ Warning, choosing root of $[1, 0, \{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}]$ at parameters values $[-29.292030761, 78.6493344628]$ $-b/\text{abs}(b) * b^2/b * (2 * \text{sqrt}(-b*x+2) * \text{sqrt}(-b*(-b*x+2)+2*b) / (-b*(-b*x+2)+2*b) + 2/\text{sqrt}(-b) * \ln(\text{abs}(\text{sqrt}(-b*(-b*x+2)+2*b)) - \text{sqrt}(-b) * \text{sqrt}(-b*x+2)))$

maple [B] time = 0.04, size = 90, normalized size = 2.14

$$\frac{\sqrt{-bx+2} x \sqrt{b} \arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{\sqrt{-bx+2} \sqrt{x}} + \frac{2(bx-2)\sqrt{-bx+2}x}{\sqrt{-(bx-2)x} \sqrt{-bx+2} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((-b*x+2)^{(1/2)}/x^{(3/2)}, x)$

[Out] $2*(b*x-2)/(-x*(b*x-2))^{(1/2)}*((-b*x+2)*x)^{(1/2)}/(-b*x+2)^{(1/2)}/x^{(1/2)}-b^{(1/2)}*\arctan((x-1/b)/(-b*x^2+2*x)^{(1/2)}*b^{(1/2)})*((-b*x+2)*x)^{(1/2)}/(-b*x+2)^{(1/2)}/x^{(1/2)}$

maxima [A] time = 3.01, size = 35, normalized size = 0.83

$$2\sqrt{b} \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) - \frac{2\sqrt{-bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(3/2),x, algorithm="maxima")

[Out] 2*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) - 2*sqrt(-b*x + 2)/sqrt(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{2-bx}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((2 - b*x)^(1/2)/x^(3/2),x)

[Out] int((2 - b*x)^(1/2)/x^(3/2), x)

sympy [C] time = 1.58, size = 136, normalized size = 3.24

$$\begin{cases} -2\sqrt{b}\sqrt{-1 + \frac{2}{bx}} - i\sqrt{b}\log\left(\frac{1}{bx}\right) + 2i\sqrt{b}\log\left(\frac{1}{\sqrt{b}\sqrt{x}}\right) - 2\sqrt{b}\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right) & \text{for } \frac{2}{|bx|} > 1 \\ -2i\sqrt{b}\sqrt{1 - \frac{2}{bx}} - i\sqrt{b}\log\left(\frac{1}{bx}\right) + 2i\sqrt{b}\log\left(\sqrt{1 - \frac{2}{bx}} + 1\right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)**(1/2)/x**(3/2),x)

[Out] Piecewise((-2*sqrt(b)*sqrt(-1 + 2/(b*x)) - I*sqrt(b)*log(1/(b*x)) + 2*I*sqrt(b)*log(1/(sqrt(b)*sqrt(x))) - 2*sqrt(b)*asin(sqrt(2)*sqrt(b)*sqrt(x)/2), 2/Abs(b*x) > 1), (-2*I*sqrt(b)*sqrt(1 - 2/(b*x)) - I*sqrt(b)*log(1/(b*x)) + 2*I*sqrt(b)*log(sqrt(1 - 2/(b*x)) + 1), True))

$$3.518 \quad \int \frac{\sqrt{2-bx}}{x^{5/2}} dx$$

Optimal. Leaf size=19

$$-\frac{(2-bx)^{3/2}}{3x^{3/2}}$$

[Out] $-1/3*(-b*x+2)^{(3/2)}/x^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {37}

$$-\frac{(2-bx)^{3/2}}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[2 - b*x]/x^(5/2), x]

[Out] $-(2 - b*x)^{(3/2)}/(3*x^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{2-bx}}{x^{5/2}} dx = -\frac{(2-bx)^{3/2}}{3x^{3/2}}$$

Mathematica [A] time = 0.01, size = 19, normalized size = 1.00

$$-\frac{(2-bx)^{3/2}}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[2 - b*x]/x^(5/2), x]

[Out] $-1/3*(2 - b*x)^{(3/2)}/x^{(3/2)}$

fricas [A] time = 0.44, size = 18, normalized size = 0.95

$$\frac{(bx - 2)\sqrt{-bx + 2}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(5/2),x, algorithm="fricas")

[Out] 1/3*(b*x - 2)*sqrt(-b*x + 2)/x^(3/2)

giac [B] time = 1.12, size = 35, normalized size = 1.84

$$\frac{(bx - 2)\sqrt{-bx + 2}b^4}{3((bx - 2)b + 2b)^{\frac{3}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(5/2),x, algorithm="giac")

[Out] 1/3*(b*x - 2)*sqrt(-b*x + 2)*b^4/(((b*x - 2)*b + 2*b)^(3/2)*abs(b))

maple [A] time = 0.00, size = 14, normalized size = 0.74

$$-\frac{(-bx + 2)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+2)^(1/2)/x^(5/2),x)

[Out] -1/3*(-b*x+2)^(3/2)/x^(3/2)

maxima [A] time = 1.28, size = 13, normalized size = 0.68

$$-\frac{(-bx + 2)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(5/2),x, algorithm="maxima")

[Out] -1/3*(-b*x + 2)^(3/2)/x^(3/2)

mupad [B] time = 0.22, size = 18, normalized size = 0.95

$$\frac{\sqrt{2-bx} \left(\frac{bx}{3} - \frac{2}{3} \right)}{x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((2 - b*x)^(1/2)/x^(5/2), x)`

[Out] `((2 - b*x)^(1/2)*((b*x)/3 - 2/3))/x^(3/2)`

sympy [B] time = 1.51, size = 82, normalized size = 4.32

$$\begin{cases} \frac{b^{3/2} \sqrt{-1 + \frac{2}{bx}}}{3} - \frac{2\sqrt{b} \sqrt{-1 + \frac{2}{bx}}}{3x} & \text{for } \frac{2}{|bx|} > 1 \\ \frac{ib^{3/2} \sqrt{1 - \frac{2}{bx}}}{3} - \frac{2i\sqrt{b} \sqrt{1 - \frac{2}{bx}}}{3x} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+2)**(1/2)/x**(5/2), x)`

[Out] `Piecewise((b**(3/2)*sqrt(-1 + 2/(b*x)))/3 - 2*sqrt(b)*sqrt(-1 + 2/(b*x))/(3*x), 2/Abs(b*x) > 1), (I*b**(3/2)*sqrt(1 - 2/(b*x)))/3 - 2*I*sqrt(b)*sqrt(1 - 2/(b*x))/(3*x), True)`

$$3.519 \quad \int \frac{\sqrt{2-bx}}{x^{7/2}} dx$$

Optimal. Leaf size=40

$$-\frac{b(2-bx)^{3/2}}{15x^{3/2}} - \frac{(2-bx)^{3/2}}{5x^{5/2}}$$

[Out] $-1/5*(-b*x+2)^{(3/2)}/x^{(5/2)}-1/15*b*(-b*x+2)^{(3/2)}/x^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{b(2-bx)^{3/2}}{15x^{3/2}} - \frac{(2-bx)^{3/2}}{5x^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[2 - b*x]/x^(7/2), x]

[Out] $-(2 - b*x)^{(3/2)}/(5*x^{(5/2)}) - (b*(2 - b*x)^{(3/2)})/(15*x^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{\sqrt{2-bx}}{x^{7/2}} dx = -\frac{(2-bx)^{3/2}}{5x^{5/2}} + \frac{1}{5}b \int \frac{\sqrt{2-bx}}{x^{5/2}} dx$$

$$= -\frac{(2-bx)^{3/2}}{5x^{5/2}} - \frac{b(2-bx)^{3/2}}{15x^{3/2}}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.60

$$-\frac{(2-bx)^{3/2}(bx+3)}{15x^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[2 - b*x]/x^(7/2), x]

[Out] -1/15*((2 - b*x)^(3/2)*(3 + b*x))/x^(5/2)

fricas [A] time = 0.41, size = 25, normalized size = 0.62

$$\frac{(b^2x^2 + bx - 6)\sqrt{-bx + 2}}{15x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(7/2), x, algorithm="fricas")

[Out] 1/15*(b^2*x^2 + b*x - 6)*sqrt(-b*x + 2)/x^(5/2)

giac [A] time = 0.85, size = 48, normalized size = 1.20

$$\frac{((bx-2)b^5 + 5b^5)(bx-2)\sqrt{-bx+2}b}{15((bx-2)b + 2b)^{\frac{5}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(7/2), x, algorithm="giac")

[Out] 1/15*((b*x - 2)*b^5 + 5*b^5)*(b*x - 2)*sqrt(-b*x + 2)*b/(((b*x - 2)*b + 2*b)^(5/2)*abs(b))

maple [A] time = 0.00, size = 19, normalized size = 0.48

$$-\frac{(bx+3)(-bx+2)^{\frac{3}{2}}}{15x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-b*x+2)^(1/2)/x^(7/2),x)`

[Out] $-1/15*(b*x+3)*(-b*x+2)^{(3/2)}/x^{(5/2)}$

maxima [A] time = 1.33, size = 28, normalized size = 0.70

$$\frac{(-bx+2)^{\frac{3}{2}}b}{6x^{\frac{3}{2}}} - \frac{(-bx+2)^{\frac{5}{2}}}{10x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+2)^(1/2)/x^(7/2),x, algorithm="maxima")`

[Out] $-1/6*(-b*x+2)^{(3/2)}*b/x^{(3/2)} - 1/10*(-b*x+2)^{(5/2)}/x^{(5/2)}$

mupad [B] time = 0.22, size = 26, normalized size = 0.65

$$\frac{\sqrt{2-bx} \left(\frac{b^2x^2}{15} + \frac{bx}{15} - \frac{2}{5} \right)}{x^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((2-b*x)^(1/2)/x^(7/2),x)`

[Out] $((2-b*x)^{(1/2)}*((b*x)/15 + (b^2*x^2)/15 - 2/5))/x^{(5/2)}$

sympy [A] time = 4.91, size = 194, normalized size = 4.85

$$\begin{cases} \frac{b^{\frac{5}{2}}\sqrt{-1+\frac{2}{bx}}}{15} + \frac{b^{\frac{3}{2}}\sqrt{-1+\frac{2}{bx}}}{15x} - \frac{2\sqrt{b}\sqrt{-1+\frac{2}{bx}}}{5x^2} & \text{for } \frac{2}{|bx|} > 1 \\ -\frac{ib^{\frac{9}{2}}x^2\sqrt{1-\frac{2}{bx}}}{-15b^2x^2+30bx} + \frac{ib^{\frac{7}{2}}x\sqrt{1-\frac{2}{bx}}}{-15b^2x^2+30bx} + \frac{8ib^{\frac{5}{2}}\sqrt{1-\frac{2}{bx}}}{-15b^2x^2+30bx} - \frac{12ib^{\frac{3}{2}}\sqrt{1-\frac{2}{bx}}}{x(-15b^2x^2+30bx)} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+2)**(1/2)/x**(7/2),x)`

[Out] `Piecewise((b**(5/2)*sqrt(-1+2/(b*x))/15 + b**(3/2)*sqrt(-1+2/(b*x))/(15*x) - 2*sqrt(b)*sqrt(-1+2/(b*x))/(5*x**2), 2/Abs(b*x) > 1), (-I*b**(9/2)*x**2*sqrt(1-2/(b*x))/(-15*b**2*x**2+30*b*x) + I*b**(7/2)*x*sqrt(1-2/(b*x))/(-15*b**2*x**2+30*b*x) + 8*I*b**(5/2)*sqrt(1-2/(b*x))/(-15*b**2*x**2+30*b*x) - 12*I*b**(3/2)*sqrt(1-2/(b*x))/(x*(-15*b**2*x**2+30*b*x)), True))`

$$3.520 \quad \int \frac{\sqrt{2-bx}}{x^{9/2}} dx$$

Optimal. Leaf size=62

$$-\frac{2b^2(2-bx)^{3/2}}{105x^{3/2}} - \frac{2b(2-bx)^{3/2}}{35x^{5/2}} - \frac{(2-bx)^{3/2}}{7x^{7/2}}$$

[Out] $-1/7*(-b*x+2)^{(3/2)}/x^{(7/2)}-2/35*b*(-b*x+2)^{(3/2)}/x^{(5/2)}-2/105*b^2*(-b*x+2)^{(3/2)}/x^{(3/2)}$

Rubi [A] time = 0.01, antiderivative size = 62, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{2b^2(2-bx)^{3/2}}{105x^{3/2}} - \frac{2b(2-bx)^{3/2}}{35x^{5/2}} - \frac{(2-bx)^{3/2}}{7x^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[2 - b*x]/x^(9/2), x]

[Out] $-(2 - b*x)^{(3/2)}/(7*x^{(7/2)}) - (2*b*(2 - b*x)^{(3/2)})/(35*x^{(5/2)}) - (2*b^2*(2 - b*x)^{(3/2)})/(105*x^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{ a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{2-bx}}{x^{9/2}} dx &= -\frac{(2-bx)^{3/2}}{7x^{7/2}} + \frac{1}{7}(2b) \int \frac{\sqrt{2-bx}}{x^{7/2}} dx \\
&= -\frac{(2-bx)^{3/2}}{7x^{7/2}} - \frac{2b(2-bx)^{3/2}}{35x^{5/2}} + \frac{1}{35}(2b^2) \int \frac{\sqrt{2-bx}}{x^{5/2}} dx \\
&= -\frac{(2-bx)^{3/2}}{7x^{7/2}} - \frac{2b(2-bx)^{3/2}}{35x^{5/2}} - \frac{2b^2(2-bx)^{3/2}}{105x^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.53

$$-\frac{(2-bx)^{3/2}(2b^2x^2+6bx+15)}{105x^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[2 - b*x]/x^(9/2), x]

[Out] -1/105*((2 - b*x)^(3/2)*(15 + 6*b*x + 2*b^2*x^2))/x^(7/2)

fricas [A] time = 0.42, size = 35, normalized size = 0.56

$$\frac{(2b^3x^3 + 2b^2x^2 + 3bx - 30)\sqrt{-bx + 2}}{105x^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(9/2), x, algorithm="fricas")

[Out] 1/105*(2*b^3*x^3 + 2*b^2*x^2 + 3*b*x - 30)*sqrt(-b*x + 2)/x^(7/2)

giac [A] time = 0.98, size = 61, normalized size = 0.98

$$\frac{(35b^7 + 2((bx-2)b^7 + 7b^7)(bx-2))(bx-2)\sqrt{-bx+2}b}{105((bx-2)b + 2b)^{7/2}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(1/2)/x^(9/2), x, algorithm="giac")

[Out] 1/105*(35*b^7 + 2*((b*x - 2)*b^7 + 7*b^7)*(b*x - 2))*(b*x - 2)*sqrt(-b*x + 2)*b/(((b*x - 2)*b + 2*b)^(7/2)*abs(b))

maple [A] time = 0.00, size = 28, normalized size = 0.45

$$\frac{(2b^2x^2 + 6bx + 15)(-bx + 2)^{\frac{3}{2}}}{105x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-b*x+2)^(1/2)/x^(9/2),x)`

[Out] `-1/105*(2*b^2*x^2+6*b*x+15)*(-b*x+2)^(3/2)/x^(7/2)`

maxima [A] time = 1.31, size = 44, normalized size = 0.71

$$-\frac{(-bx + 2)^{\frac{3}{2}}b^2}{12x^{\frac{3}{2}}} - \frac{(-bx + 2)^{\frac{5}{2}}b}{10x^{\frac{5}{2}}} - \frac{(-bx + 2)^{\frac{7}{2}}}{28x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+2)^(1/2)/x^(9/2),x, algorithm="maxima")`

[Out] `-1/12*(-b*x + 2)^(3/2)*b^2/x^(3/2) - 1/10*(-b*x + 2)^(5/2)*b/x^(5/2) - 1/28*(-b*x + 2)^(7/2)/x^(7/2)`

mupad [B] time = 0.22, size = 34, normalized size = 0.55

$$\frac{\sqrt{2 - bx} \left(\frac{2b^3x^3}{105} + \frac{2b^2x^2}{105} + \frac{bx}{35} - \frac{2}{7} \right)}{x^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((2 - b*x)^(1/2)/x^(9/2),x)`

[Out] `((2 - b*x)^(1/2)*((b*x)/35 + (2*b^2*x^2)/105 + (2*b^3*x^3)/105 - 2/7))/x^(7/2)`

sympy [B] time = 24.60, size = 554, normalized size = 8.94

$$\left\{ \begin{array}{l} -\frac{2b^{\frac{19}{2}}x^5\sqrt{-1+\frac{2}{bx}}}{-105b^6x^5+420b^5x^4-420b^4x^3} + \frac{6b^{\frac{17}{2}}x^4\sqrt{-1+\frac{2}{bx}}}{-105b^6x^5+420b^5x^4-420b^4x^3} - \frac{3b^{\frac{15}{2}}x^3\sqrt{-1+\frac{2}{bx}}}{-105b^6x^5+420b^5x^4-420b^4x^3} + \frac{34b^{\frac{13}{2}}x^2\sqrt{-1+\frac{2}{bx}}}{-105b^6x^5+420b^5x^4-420b^4x^3} - \frac{132b^{\frac{11}{2}}}{-105b^6x^5+420b^5x^4-420b^4x^3} \\ -\frac{2ib^{\frac{19}{2}}x^5\sqrt{1-\frac{2}{bx}}}{-105b^6x^5+420b^5x^4-420b^4x^3} + \frac{6ib^{\frac{17}{2}}x^4\sqrt{1-\frac{2}{bx}}}{-105b^6x^5+420b^5x^4-420b^4x^3} - \frac{3ib^{\frac{15}{2}}x^3\sqrt{1-\frac{2}{bx}}}{-105b^6x^5+420b^5x^4-420b^4x^3} + \frac{34ib^{\frac{13}{2}}x^2\sqrt{1-\frac{2}{bx}}}{-105b^6x^5+420b^5x^4-420b^4x^3} - \frac{132ib^{\frac{11}{2}}}{-105b^6x^5+420b^5x^4-420b^4x^3} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)**(1/2)/x**(9/2),x)

[Out] Piecewise((-2*b**(19/2)*x**5*sqrt(-1 + 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3) + 6*b**(17/2)*x**4*sqrt(-1 + 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3) - 3*b**(15/2)*x**3*sqrt(-1 + 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3) + 34*b**(13/2)*x**2*sqrt(-1 + 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3) - 132*b**(11/2)*x*sqrt(-1 + 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3) + 120*b**(9/2)*sqrt(-1 + 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3), 2/Abs(b*x) > 1), (-2*I*b**(19/2)*x**5*sqrt(1 - 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3) + 6*I*b**(17/2)*x**4*sqrt(1 - 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3) - 3*I*b**(15/2)*x**3*sqrt(1 - 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3) + 34*I*b**(13/2)*x**2*sqrt(1 - 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3) - 132*I*b**(11/2)*x*sqrt(1 - 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3) + 120*I*b**(9/2)*sqrt(1 - 2/(b*x))/(-105*b**6*x**5 + 420*b**5*x**4 - 420*b**4*x**3), True))

3.521 $\int x^{5/2}(a + bx)^{3/2} dx$

Optimal. Leaf size=143

$$-\frac{3a^5 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{128b^{7/2}} + \frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^3} - \frac{a^3x^{3/2}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{5/2}\sqrt{a+bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a+bx} + \frac{1}{5}x^{7/2}(a+bx)^{3/2}$$

[Out] $1/5*x^{(7/2)}*(b*x+a)^{(3/2)}-3/128*a^5*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(7/2)}-1/64*a^3*x^{(3/2)}*(b*x+a)^{(1/2)}/b^2+1/80*a^2*x^{(5/2)}*(b*x+a)^{(1/2)}/b+3/40*a*x^{(7/2)}*(b*x+a)^{(1/2)}+3/128*a^4*x^{(1/2)}*(b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.05, antiderivative size = 143, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$-\frac{a^3x^{3/2}\sqrt{a+bx}}{64b^2} + \frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^3} - \frac{3a^5 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{128b^{7/2}} + \frac{a^2x^{5/2}\sqrt{a+bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a+bx} + \frac{1}{5}x^{7/2}(a+bx)^{3/2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(5/2)}*(a + b*x)^{(3/2)}, x]$

[Out] $(3*a^4*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(128*b^3) - (a^3*x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/(64*b^2) + (a^2*x^{(5/2)}*\operatorname{Sqrt}[a + b*x])/(80*b) + (3*a*x^{(7/2)}*\operatorname{Sqrt}[a + b*x])/40 + (x^{(7/2)}*(a + b*x)^{(3/2)})/5 - (3*a^5*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(128*b^{(7/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int x^{5/2}(a+bx)^{3/2} dx &= \frac{1}{5}x^{7/2}(a+bx)^{3/2} + \frac{1}{10}(3a) \int x^{5/2}\sqrt{a+bx} dx \\
 &= \frac{3}{40}ax^{7/2}\sqrt{a+bx} + \frac{1}{5}x^{7/2}(a+bx)^{3/2} + \frac{1}{80}(3a^2) \int \frac{x^{5/2}}{\sqrt{a+bx}} dx \\
 &= \frac{a^2x^{5/2}\sqrt{a+bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a+bx} + \frac{1}{5}x^{7/2}(a+bx)^{3/2} - \frac{a^3 \int \frac{x^{3/2}}{\sqrt{a+bx}} dx}{32b} \\
 &= -\frac{a^3x^{3/2}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{5/2}\sqrt{a+bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a+bx} + \frac{1}{5}x^{7/2}(a+bx)^{3/2} + \frac{(3a^4) \int \frac{\sqrt{x}}{\sqrt{a+bx}} dx}{128b^2} \\
 &= \frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^3} - \frac{a^3x^{3/2}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{5/2}\sqrt{a+bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a+bx} + \frac{1}{5}x^{7/2}(a+bx)^{3/2} \\
 &= \frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^3} - \frac{a^3x^{3/2}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{5/2}\sqrt{a+bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a+bx} + \frac{1}{5}x^{7/2}(a+bx)^{3/2} \\
 &= \frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^3} - \frac{a^3x^{3/2}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{5/2}\sqrt{a+bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a+bx} + \frac{1}{5}x^{7/2}(a+bx)^{3/2} \\
 &= \frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^3} - \frac{a^3x^{3/2}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{5/2}\sqrt{a+bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a+bx} + \frac{1}{5}x^{7/2}(a+bx)^{3/2}
 \end{aligned}$$

Mathematica [A] time = 0.21, size = 107, normalized size = 0.75

$$\frac{\sqrt{a+bx} \left(\sqrt{b}\sqrt{x} (15a^4 - 10a^3bx + 8a^2b^2x^2 + 176ab^3x^3 + 128b^4x^4) - \frac{15a^{9/2} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{\frac{bx}{a}+1}} \right)}{640b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*(a + b*x)^(3/2),x]

[Out] (Sqrt[a + b*x]*(Sqrt[b]*Sqrt[x]*(15*a^4 - 10*a^3*b*x + 8*a^2*b^2*x^2 + 176*a*b^3*x^3 + 128*b^4*x^4) - (15*a^(9/2)*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 + (b*x)/a]))/(640*b^(7/2))

fricas [A] time = 0.44, size = 184, normalized size = 1.29

$$\frac{15 a^5 \sqrt{b} \log(2 b x - 2 \sqrt{b x + a} \sqrt{b} \sqrt{x} + a) + 2 (128 b^5 x^4 + 176 a b^4 x^3 + 8 a^2 b^3 x^2 - 10 a^3 b^2 x + 15 a^4 b) \sqrt{b x + a} \sqrt{x}}{1280 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^(3/2),x, algorithm="fricas")

[Out] [1/1280*(15*a^5*sqrt(b)*log(2*b*x - 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(128*b^5*x^4 + 176*a*b^4*x^3 + 8*a^2*b^3*x^2 - 10*a^3*b^2*x + 15*a^4*b)*sqrt(b*x + a)*sqrt(x))/b^4, 1/640*(15*a^5*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) + (128*b^5*x^4 + 176*a*b^4*x^3 + 8*a^2*b^3*x^2 - 10*a^3*b^2*x + 15*a^4*b)*sqrt(b*x + a)*sqrt(x))/b^4]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^(3/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 138, normalized size = 0.97

$$\frac{3\sqrt{bx+a} x a^5 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{256\sqrt{bx+a} b^{\frac{7}{2}}\sqrt{x}} - \frac{3\sqrt{bx+a} a^4\sqrt{x}}{128b^3} + \frac{(bx+a)^{\frac{5}{2}} x^{\frac{5}{2}}}{5b} - \frac{(bx+a)^{\frac{3}{2}} a^3\sqrt{x}}{64b^3} - \frac{(bx+a)^{\frac{5}{2}} a x^{\frac{3}{2}}}{8b^2} + \frac{(bx+a)^{\frac{7}{2}}}{128b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(b*x+a)^(3/2),x)

[Out] 1/5/b*x^(5/2)*(b*x+a)^(5/2)-1/8*a/b^2*x^(3/2)*(b*x+a)^(5/2)+1/16*a^2/b^3*x^(1/2)*(b*x+a)^(5/2)-1/64*a^3/b^3*(b*x+a)^(3/2)*x^(1/2)-3/128*a^4*x^(1/2)*(b*x+a)^(3/2)

$(bx+a)^{1/2}/b^3 - 3/256 a^5/b^{7/2} * ((bx+a)*x)^{1/2}/(bx+a)^{1/2}/x^{1/2} * \ln((bx+1/2*a)/b^{1/2} + (bx^2+ax)^{1/2})$

maxima [B] time = 2.96, size = 212, normalized size = 1.48

$$\frac{3a^5 \log\left(\frac{\sqrt{b} - \frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+a}}{\sqrt{x}}}\right)}{256b^{\frac{7}{2}}} + \frac{\frac{15\sqrt{bx+a}a^5b^4}{\sqrt{x}} - \frac{70(bx+a)^{\frac{3}{2}}a^5b^3}{x^{\frac{3}{2}}} - \frac{128(bx+a)^{\frac{5}{2}}a^5b^2}{x^{\frac{5}{2}}} + \frac{70(bx+a)^{\frac{7}{2}}a^5b}{x^{\frac{7}{2}}} - \frac{15(bx+a)^{\frac{9}{2}}a^5}{x^{\frac{9}{2}}}}{640\left(b^8 - \frac{5(bx+a)b^7}{x} + \frac{10(bx+a)^2b^6}{x^2} - \frac{10(bx+a)^3b^5}{x^3} + \frac{5(bx+a)^4b^4}{x^4} - \frac{(bx+a)^5b^3}{x^5}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^(3/2),x, algorithm="maxima")

[Out] $3/256*a^5*\log(-(\sqrt{b} - \sqrt{bx+a})/\sqrt{x})/(\sqrt{b} + \sqrt{bx+a})/\sqrt{x})/b^{7/2} + 1/640*(15*\sqrt{bx+a}*a^5*b^4/\sqrt{x} - 70*(bx+a)^{(3/2)}*a^5*b^3/x^{3/2} - 128*(bx+a)^{(5/2)}*a^5*b^2/x^{5/2} + 70*(bx+a)^{(7/2)}*a^5*b/x^{7/2} - 15*(bx+a)^{(9/2)}*a^5/x^{9/2})/(b^8 - 5*(bx+a)*b^7/x + 10*(bx+a)^2*b^6/x^2 - 10*(bx+a)^3*b^5/x^3 + 5*(bx+a)^4*b^4/x^4 - (bx+a)^5*b^3/x^5)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} (a + bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(a + b*x)^(3/2),x)

[Out] int(x^(5/2)*(a + b*x)^(3/2), x)

sympy [A] time = 17.71, size = 178, normalized size = 1.24

$$\frac{3a^{\frac{9}{2}}\sqrt{x}}{128b^3\sqrt{1+\frac{bx}{a}}} + \frac{a^{\frac{7}{2}}x^{\frac{3}{2}}}{128b^2\sqrt{1+\frac{bx}{a}}} - \frac{a^{\frac{5}{2}}x^{\frac{5}{2}}}{320b\sqrt{1+\frac{bx}{a}}} + \frac{23a^{\frac{3}{2}}x^{\frac{7}{2}}}{80\sqrt{1+\frac{bx}{a}}} + \frac{19\sqrt{a}bx^{\frac{9}{2}}}{40\sqrt{1+\frac{bx}{a}}} - \frac{3a^5 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{128b^{\frac{7}{2}}} + \frac{b^2x^{\frac{11}{2}}}{5\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)*(b*x+a)**(3/2),x)

[Out] $3*a^{9/2}*\sqrt{x}/(128*b^{3/2}*\sqrt{1+b*x/a}) + a^{7/2}*x^{3/2}/(128*b^{3/2}*\sqrt{1+b*x/a}) - a^{5/2}*x^{5/2}/(320*b*\sqrt{1+b*x/a}) + 23*a^{3/2}*x^{7/2}/(80*\sqrt{1+b*x/a}) + 19*\sqrt{a}*b*x^{9/2}/(40*\sqrt{1+b*x/a}) - 3*a^5*\operatorname{asinh}(\sqrt{b}*\sqrt{x}/\sqrt{a})/(128*b^{7/2}) + b^2*x^{11/2}/(5*\sqrt{a}*\sqrt{1+b*x/a})$

3.522 $\int x^{3/2}(a + bx)^{3/2} dx$

Optimal. Leaf size=119

$$\frac{3a^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{64b^{5/2}} - \frac{3a^3\sqrt{x}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{3/2}\sqrt{a+bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a+bx} + \frac{1}{4}x^{5/2}(a+bx)^{3/2}$$

[Out] $1/4*x^{(5/2)}*(b*x+a)^{(3/2)}+3/64*a^4*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(5/2)}+1/32*a^2*x^{(3/2)}*(b*x+a)^{(1/2)}/b+1/8*a*x^{(5/2)}*(b*x+a)^{(1/2)}-3/64*a^3*x^{(1/2)}*(b*x+a)^{(1/2)}/b^2$

Rubi [A] time = 0.04, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$-\frac{3a^3\sqrt{x}\sqrt{a+bx}}{64b^2} + \frac{3a^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{64b^{5/2}} + \frac{a^2x^{3/2}\sqrt{a+bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a+bx} + \frac{1}{4}x^{5/2}(a+bx)^{3/2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(3/2)}*(a + b*x)^{(3/2)}, x]$

[Out] $(-3*a^3*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(64*b^2) + (a^2*x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/(32*b) + (a*x^{(5/2)}*\operatorname{Sqrt}[a + b*x])/8 + (x^{(5/2)}*(a + b*x)^{(3/2)})/4 + (3*a^4*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(64*b^{(5/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]]/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int x^{3/2}(a+bx)^{3/2} dx &= \frac{1}{4}x^{5/2}(a+bx)^{3/2} + \frac{1}{8}(3a) \int x^{3/2}\sqrt{a+bx} dx \\
 &= \frac{1}{8}ax^{5/2}\sqrt{a+bx} + \frac{1}{4}x^{5/2}(a+bx)^{3/2} + \frac{1}{16}a^2 \int \frac{x^{3/2}}{\sqrt{a+bx}} dx \\
 &= \frac{a^2x^{3/2}\sqrt{a+bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a+bx} + \frac{1}{4}x^{5/2}(a+bx)^{3/2} - \frac{(3a^3) \int \frac{\sqrt{x}}{\sqrt{a+bx}} dx}{64b} \\
 &= -\frac{3a^3\sqrt{x}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{3/2}\sqrt{a+bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a+bx} + \frac{1}{4}x^{5/2}(a+bx)^{3/2} + \frac{(3a^4) \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx}{128b^2} \\
 &= -\frac{3a^3\sqrt{x}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{3/2}\sqrt{a+bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a+bx} + \frac{1}{4}x^{5/2}(a+bx)^{3/2} + \frac{(3a^4) \text{Subst}\left(\int \frac{1}{\sqrt{u}} du, u, a+bx\right)}{128b^2} \\
 &= -\frac{3a^3\sqrt{x}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{3/2}\sqrt{a+bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a+bx} + \frac{1}{4}x^{5/2}(a+bx)^{3/2} + \frac{(3a^4) \text{Subst}\left(\int \frac{1}{\sqrt{u}} du, u, a+bx\right)}{128b^2} \\
 &= -\frac{3a^3\sqrt{x}\sqrt{a+bx}}{64b^2} + \frac{a^2x^{3/2}\sqrt{a+bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a+bx} + \frac{1}{4}x^{5/2}(a+bx)^{3/2} + \frac{3a^4 \tanh^{-1}\left(\frac{\sqrt{bx}}{\sqrt{a+bx}}\right)}{64b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.13, size = 96, normalized size = 0.81

$$\frac{\sqrt{a+bx} \left(\frac{3a^{7/2} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{\frac{bx}{a}+1}} + \sqrt{b}\sqrt{x}(-3a^3 + 2a^2bx + 24ab^2x^2 + 16b^3x^3) \right)}{64b^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*(a + b*x)^(3/2), x]

[Out] $(\sqrt{a + bx} * (\sqrt{b} * \sqrt{x} * (-3a^3 + 2a^2bx + 24ab^2x^2 + 16b^3x^3) + (3a^{7/2} * \text{ArcSinh}[(\sqrt{b} * \sqrt{x}) / \sqrt{a}]) / \sqrt{1 + (bx)/a})) / (64b^{5/2})$

fricas [A] time = 0.45, size = 163, normalized size = 1.37

$$\left[\frac{3a^4\sqrt{b} \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(16b^4x^3 + 24ab^3x^2 + 2a^2b^2x - 3a^3b)\sqrt{bx+a}\sqrt{x}}{128b^3}, -\frac{3a^4\sqrt{-b} \arctan(\sqrt{bx+a}\sqrt{-b}/(\sqrt{b}\sqrt{x}))}{128b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)*(b*x+a)^(3/2),x, algorithm="fricas")`

[Out] $[1/128*(3a^4*\sqrt{b}*\log(2bx + 2*\sqrt{bx+a}*\sqrt{b}*\sqrt{x} + a) + 2*(16b^4*x^3 + 24a*b^3*x^2 + 2a^2*b^2*x - 3a^3*b)*\sqrt{bx+a}*\sqrt{x})/b^3, -1/64*(3a^4*\sqrt{-b}*\arctan(\sqrt{bx+a}*\sqrt{-b}/(\sqrt{b}*\sqrt{x}))) - (16*b^4*x^3 + 24a*b^3*x^2 + 2a^2*b^2*x - 3a^3*b)*\sqrt{bx+a}*\sqrt{x})/b^3]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)*(b*x+a)^(3/2),x, algorithm="giac")`

[Out] Timed out

maple [A] time = 0.01, size = 120, normalized size = 1.01

$$\frac{3\sqrt{(bx+a)x} a^4 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{128\sqrt{bx+a} b^{\frac{5}{2}}\sqrt{x}} + \frac{3\sqrt{bx+a} a^3\sqrt{x}}{64b^2} + \frac{(bx+a)^{\frac{3}{2}} a^2\sqrt{x}}{32b^2} + \frac{(bx+a)^{\frac{5}{2}} x^{\frac{3}{2}}}{4b} - \frac{(bx+a)^{\frac{5}{2}} a\sqrt{x}}{8b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)*(b*x+a)^(3/2),x)`

[Out] $1/4/b*x^{3/2}*(b*x+a)^{5/2} - 1/8*a/b^2*x^{1/2}*(b*x+a)^{5/2} + 1/32*a^2/b^2*(b*x+a)^{3/2}*x^{1/2} + 3/64*a^3*x^{1/2}*(b*x+a)^{1/2}/b^2 + 3/128*a^4/b^{5/2}*((b*x+a)*x)^{1/2}/(b*x+a)^{1/2}/x^{1/2} * \ln((b*x+1/2*a)/b^{1/2} + (b*x^2+a*x)^{1/2})$

maxima [B] time = 2.96, size = 178, normalized size = 1.50

$$\frac{3a^4 \log\left(-\frac{\sqrt{b}-\sqrt{bx+a}}{\sqrt{x}}\right)}{128b^{\frac{5}{2}}} - \frac{\frac{3\sqrt{bx+a}a^4b^3}{\sqrt{x}} - \frac{11(bx+a)^{\frac{3}{2}}a^4b^2}{x^{\frac{3}{2}}} - \frac{11(bx+a)^{\frac{5}{2}}a^4b}{x^{\frac{5}{2}}} + \frac{3(bx+a)^{\frac{7}{2}}a^4}{x^{\frac{7}{2}}}}{64\left(b^6 - \frac{4(bx+a)b^5}{x} + \frac{6(bx+a)^2b^4}{x^2} - \frac{4(bx+a)^3b^3}{x^3} + \frac{(bx+a)^4b^2}{x^4}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^(3/2),x, algorithm="maxima")

[Out] $-3/128*a^4*\log(-(\text{sqrt}(b) - \text{sqrt}(b*x + a))/\text{sqrt}(x))/(\text{sqrt}(b) + \text{sqrt}(b*x + a)/\text{sqrt}(x))/b^{5/2} - 1/64*(3*\text{sqrt}(b*x + a)*a^4*b^3/\text{sqrt}(x) - 11*(b*x + a)^{(3/2)}*a^4*b^2/x^{3/2} - 11*(b*x + a)^{(5/2)}*a^4*b/x^{5/2} + 3*(b*x + a)^{(7/2)}*a^4/x^{7/2})/(b^6 - 4*(b*x + a)*b^5/x + 6*(b*x + a)^2*b^4/x^2 - 4*(b*x + a)^3*b^3/x^3 + (b*x + a)^4*b^2/x^4)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} (a + bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(a + b*x)^(3/2),x)

[Out] int(x^(3/2)*(a + b*x)^(3/2), x)

sympy [A] time = 9.28, size = 153, normalized size = 1.29

$$-\frac{3a^{\frac{7}{2}}\sqrt{x}}{64b^2\sqrt{1+\frac{bx}{a}}} - \frac{a^{\frac{5}{2}}x^{\frac{3}{2}}}{64b\sqrt{1+\frac{bx}{a}}} + \frac{13a^{\frac{3}{2}}x^{\frac{5}{2}}}{32\sqrt{1+\frac{bx}{a}}} + \frac{5\sqrt{a}bx^{\frac{7}{2}}}{8\sqrt{1+\frac{bx}{a}}} + \frac{3a^4 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{64b^{\frac{5}{2}}} + \frac{b^2x^{\frac{9}{2}}}{4\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)*(b*x+a)**(3/2),x)

[Out] $-3*a^{7/2}*\text{sqrt}(x)/(64*b^{5/2}*\text{sqrt}(1 + b*x/a)) - a^{5/2}*x^{3/2}/(64*b*\text{sqrt}(1 + b*x/a)) + 13*a^{3/2}*x^{5/2}/(32*\text{sqrt}(1 + b*x/a)) + 5*\text{sqrt}(a)*b*x^{7/2}/(8*\text{sqrt}(1 + b*x/a)) + 3*a^{4/2}*\text{asinh}(\text{sqrt}(b)*\text{sqrt}(x)/\text{sqrt}(a))/(64*b^{5/2}) + b^{2/2}*x^{9/2}/(4*\text{sqrt}(a)*\text{sqrt}(1 + b*x/a))$

3.523 $\int \sqrt{x} (a + bx)^{3/2} dx$

Optimal. Leaf size=95

$$-\frac{a^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{8b^{3/2}} + \frac{a^2\sqrt{x}\sqrt{a+bx}}{8b} + \frac{1}{4}ax^{3/2}\sqrt{a+bx} + \frac{1}{3}x^{3/2}(a+bx)^{3/2}$$

[Out] $\frac{1}{3}x^{3/2}(b*x+a)^{3/2}-\frac{1}{8}a^3*\operatorname{arctanh}(b^{1/2}*x^{1/2}/(b*x+a)^{1/2})/b^{3/2}+\frac{1}{4}a^2*x^{3/2}*(b*x+a)^{1/2}+\frac{1}{8}a^2*x^{1/2}*(b*x+a)^{3/2}/b$

Rubi [A] time = 0.03, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$-\frac{a^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{8b^{3/2}} + \frac{a^2\sqrt{x}\sqrt{a+bx}}{8b} + \frac{1}{4}ax^{3/2}\sqrt{a+bx} + \frac{1}{3}x^{3/2}(a+bx)^{3/2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*(a + b*x)^(3/2), x]

[Out] $\frac{(a^2*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])}{(8*b)} + \frac{(a*x^{3/2}*\operatorname{Sqrt}[a + b*x])}{4} + \frac{(x^{3/2}*(a + b*x)^{3/2})}{3} - \frac{(a^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])}{(8*b^{3/2})}$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \sqrt{x} (a + bx)^{3/2} dx &= \frac{1}{3} x^{3/2} (a + bx)^{3/2} + \frac{1}{2} a \int \sqrt{x} \sqrt{a + bx} dx \\
 &= \frac{1}{4} a x^{3/2} \sqrt{a + bx} + \frac{1}{3} x^{3/2} (a + bx)^{3/2} + \frac{1}{8} a^2 \int \frac{\sqrt{x}}{\sqrt{a + bx}} dx \\
 &= \frac{a^2 \sqrt{x} \sqrt{a + bx}}{8b} + \frac{1}{4} a x^{3/2} \sqrt{a + bx} + \frac{1}{3} x^{3/2} (a + bx)^{3/2} - \frac{a^3 \int \frac{1}{\sqrt{x} \sqrt{a + bx}} dx}{16b} \\
 &= \frac{a^2 \sqrt{x} \sqrt{a + bx}}{8b} + \frac{1}{4} a x^{3/2} \sqrt{a + bx} + \frac{1}{3} x^{3/2} (a + bx)^{3/2} - \frac{a^3 \text{Subst}\left(\int \frac{1}{\sqrt{a + bx^2}} dx, x, \sqrt{x}\right)}{8b} \\
 &= \frac{a^2 \sqrt{x} \sqrt{a + bx}}{8b} + \frac{1}{4} a x^{3/2} \sqrt{a + bx} + \frac{1}{3} x^{3/2} (a + bx)^{3/2} - \frac{a^3 \text{Subst}\left(\int \frac{1}{1 - bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a + bx}}\right)}{8b} \\
 &= \frac{a^2 \sqrt{x} \sqrt{a + bx}}{8b} + \frac{1}{4} a x^{3/2} \sqrt{a + bx} + \frac{1}{3} x^{3/2} (a + bx)^{3/2} - \frac{a^3 \tanh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a + bx}}\right)}{8b^{3/2}}
 \end{aligned}$$

Mathematica [A] time = 0.11, size = 85, normalized size = 0.89

$$\frac{\sqrt{a + bx} \left(\sqrt{b} \sqrt{x} (3a^2 + 14abx + 8b^2x^2) - \frac{3a^{5/2} \sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{\frac{bx}{a} + 1}} \right)}{24b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*(a + b*x)^(3/2), x]

[Out] (Sqrt[a + b*x]*(Sqrt[b]*Sqrt[x]*(3*a^2 + 14*a*b*x + 8*b^2*x^2) - (3*a^(5/2)*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 + (b*x)/a]))/(24*b^(3/2))

fricas [A] time = 0.45, size = 140, normalized size = 1.47

$$\left[\frac{3 a^3 \sqrt{b} \log \left(2 b x - 2 \sqrt{b x + a} \sqrt{b} \sqrt{x} + a \right) + 2 \left(8 b^3 x^2 + 14 a b^2 x + 3 a^2 b \right) \sqrt{b x + a} \sqrt{x}}{48 b^2}, \frac{3 a^3 \sqrt{-b} \arctan \left(\frac{\sqrt{b x + a} \sqrt{-b}}{b \sqrt{x}} \right)}{b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*x^(1/2),x, algorithm="fricas")

[Out] [1/48*(3*a^3*sqrt(b)*log(2*b*x - 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(8*b^3*x^2 + 14*a*b^2*x + 3*a^2*b)*sqrt(b*x + a)*sqrt(x))/b^2, 1/24*(3*a^3*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x)))) + (8*b^3*x^2 + 14*a*b^2*x + 3*a^2*b)*sqrt(b*x + a)*sqrt(x))/b^2]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*x^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 96, normalized size = 1.01

$$\frac{\sqrt{b x + a} a x^{\frac{3}{2}}}{4} - \frac{\sqrt{(b x + a) x} a^3 \ln \left(\frac{b x + \frac{a}{2}}{\sqrt{b}} + \sqrt{b x^2 + a x} \right)}{16 \sqrt{b x + a} b^{\frac{3}{2}} \sqrt{x}} + \frac{\sqrt{b x + a} a^2 \sqrt{x}}{8 b} + \frac{(b x + a)^{\frac{3}{2}} x^{\frac{3}{2}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)*x^(1/2),x)

[Out] 1/3*x^(3/2)*(b*x+a)^(3/2)+1/4*a*x^(3/2)*(b*x+a)^(1/2)+1/8*a^2*x^(1/2)*(b*x+a)^(1/2)/b-1/16*a^3/b^(3/2)*((b*x+a)*x)^(1/2)/x^(1/2)/(b*x+a)^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))

maxima [B] time = 3.02, size = 144, normalized size = 1.52

$$\frac{a^3 \log \left(-\frac{\sqrt{b} - \frac{\sqrt{b x + a}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{b x + a}}{\sqrt{x}}} \right)}{16 b^{\frac{3}{2}}} + \frac{\frac{3 \sqrt{b x + a} a^3 b^2}{\sqrt{x}} - \frac{8 (b x + a)^{\frac{3}{2}} a^3 b}{x^{\frac{3}{2}}} - \frac{3 (b x + a)^{\frac{5}{2}} a^3}{x^{\frac{5}{2}}}}{24 \left(b^4 - \frac{3 (b x + a) b^3}{x} + \frac{3 (b x + a)^2 b^2}{x^2} - \frac{(b x + a)^3 b}{x^3} \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*x^(1/2),x, algorithm="maxima")

[Out] $\frac{1}{16}a^3 \log\left(\frac{-\sqrt{b} - \sqrt{bx+a}}{\sqrt{x}}\right) / (\sqrt{b} + \sqrt{bx+a}) / \sqrt{x} + \frac{1}{24}(3\sqrt{bx+a}a^3b^2/\sqrt{x} - 8(bx+a)^{3/2}a^3b/x^{3/2} - 3(bx+a)^{5/2}a^3/x^{5/2}) / (b^4 - 3(bx+a)b^3/x + 3(bx+a)^2b^2/x^2 - (bx+a)^3b/x^3)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{x} (a + bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)*(a + b*x)^(3/2),x)

[Out] int(x^(1/2)*(a + b*x)^(3/2), x)

sympy [A] time = 5.59, size = 124, normalized size = 1.31

$$\frac{a^{\frac{5}{2}}\sqrt{x}}{8b\sqrt{1+\frac{bx}{a}}} + \frac{17a^{\frac{3}{2}}x^{\frac{3}{2}}}{24\sqrt{1+\frac{bx}{a}}} + \frac{11\sqrt{a}bx^{\frac{5}{2}}}{12\sqrt{1+\frac{bx}{a}}} - \frac{a^3 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8b^{\frac{3}{2}}} + \frac{b^2x^{\frac{7}{2}}}{3\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)*x**(1/2),x)

[Out] $a^{5/2}\sqrt{x}/(8b\sqrt{1+b*x/a}) + 17a^{3/2}x^{3/2}/(24\sqrt{1+b*x/a}) + 11\sqrt{a}bx^{5/2}/(12\sqrt{1+b*x/a}) - a^3\operatorname{asinh}(\sqrt{b}\sqrt{x}/\sqrt{a})/(8b^{3/2}) + b^2x^{7/2}/(3\sqrt{a}\sqrt{1+b*x/a})$

$$3.524 \quad \int \frac{(a+bx)^{3/2}}{\sqrt{x}} dx$$

Optimal. Leaf size=71

$$\frac{3a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4\sqrt{b}} + \frac{3}{4}a\sqrt{x}\sqrt{a+bx} + \frac{1}{2}\sqrt{x}(a+bx)^{3/2}$$

[Out] $3/4*a^2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(1/2)}+1/2*(b*x+a)^{(3/2)}*x^{(1/2)}+3/4*a*x^{(1/2)}*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$\frac{3a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4\sqrt{b}} + \frac{3}{4}a\sqrt{x}\sqrt{a+bx} + \frac{1}{2}\sqrt{x}(a+bx)^{3/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)/Sqrt[x], x]

[Out] $(3*a*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/4 + (\operatorname{Sqrt}[x]*(a + b*x)^{(3/2)})/2 + (3*a^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/(\operatorname{Sqrt}[a + b*x])])/(4*\operatorname{Sqrt}[b])$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]]/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{3/2}}{\sqrt{x}} dx &= \frac{1}{2} \sqrt{x} (a+bx)^{3/2} + \frac{1}{4} (3a) \int \frac{\sqrt{a+bx}}{\sqrt{x}} dx \\
 &= \frac{3}{4} a \sqrt{x} \sqrt{a+bx} + \frac{1}{2} \sqrt{x} (a+bx)^{3/2} + \frac{1}{8} (3a^2) \int \frac{1}{\sqrt{x} \sqrt{a+bx}} dx \\
 &= \frac{3}{4} a \sqrt{x} \sqrt{a+bx} + \frac{1}{2} \sqrt{x} (a+bx)^{3/2} + \frac{1}{4} (3a^2) \text{Subst} \left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x} \right) \\
 &= \frac{3}{4} a \sqrt{x} \sqrt{a+bx} + \frac{1}{2} \sqrt{x} (a+bx)^{3/2} + \frac{1}{4} (3a^2) \text{Subst} \left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}} \right) \\
 &= \frac{3}{4} a \sqrt{x} \sqrt{a+bx} + \frac{1}{2} \sqrt{x} (a+bx)^{3/2} + \frac{3a^2 \tanh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a+bx}} \right)}{4\sqrt{b}}
 \end{aligned}$$

Mathematica [A] time = 0.10, size = 69, normalized size = 0.97

$$\frac{1}{4} \sqrt{a+bx} \left(\frac{3a^{3/2} \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{b} \sqrt{\frac{bx}{a}} + 1} + \sqrt{x} (5a + 2bx) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/Sqrt[x], x]

[Out] (Sqrt[a + b*x]*(Sqrt[x]*(5*a + 2*b*x) + (3*a^(3/2)*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[b]*Sqrt[1 + (b*x)/a]))) / 4

fricas [A] time = 0.47, size = 119, normalized size = 1.68

$$\left[\frac{3a^2 \sqrt{b} \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(2b^2x + 5ab)\sqrt{bx+a}\sqrt{x}}{8b}, -\frac{3a^2 \sqrt{-b} \arctan\left(\frac{\sqrt{bx+a}\sqrt{-b}}{b\sqrt{x}}\right) - (2b}{4b} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^(1/2),x, algorithm="fricas")

[Out] [1/8*(3*a^2*sqrt(b)*log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(2*b^2*x + 5*a*b)*sqrt(b*x + a)*sqrt(x))/b, -1/4*(3*a^2*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) - (2*b^2*x + 5*a*b)*sqrt(b*x + a)*sqrt(x))/b]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 78, normalized size = 1.10

$$\frac{3\sqrt{bx+a} x a^2 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{8\sqrt{bx+a} \sqrt{b} \sqrt{x}} + \frac{3\sqrt{bx+a} a\sqrt{x}}{4} + \frac{(bx+a)^{\frac{3}{2}} \sqrt{x}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/x^(1/2),x)

[Out] 1/2*(b*x+a)^(3/2)*x^(1/2)+3/4*a*x^(1/2)*(b*x+a)^(1/2)+3/8*a^2*((b*x+a)*x)^(1/2)/(b*x+a)^(1/2)/x^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))/b^(1/2)

maxima [B] time = 2.99, size = 107, normalized size = 1.51

$$-\frac{3a^2 \log\left(-\frac{\sqrt{b}-\sqrt{bx+a}}{\sqrt{x}}\right)}{8\sqrt{b}} - \frac{\frac{3\sqrt{bx+a}a^2b}{\sqrt{x}} - \frac{5(bx+a)^{\frac{3}{2}}a^2}{x^{\frac{3}{2}}}}{4\left(b^2 - \frac{2(bx+a)b}{x} + \frac{(bx+a)^2}{x^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^(1/2),x, algorithm="maxima")

[Out] -3/8*a^2*log(-sqrt(b) - sqrt(b*x + a)/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x))/sqrt(b) - 1/4*(3*sqrt(b*x + a)*a^2*b/sqrt(x) - 5*(b*x + a)^(3/2)*a^2/x^(3/2))/(b^2 - 2*(b*x + a)*b/x + (b*x + a)^2/x^2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{3/2}}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(3/2)/x^(1/2), x)`

[Out] `int((a + b*x)^(3/2)/x^(1/2), x)`

sympy [A] time = 3.17, size = 75, normalized size = 1.06

$$\frac{5a^{\frac{3}{2}}\sqrt{x}\sqrt{1+\frac{bx}{a}}}{4} + \frac{\sqrt{a}bx^{\frac{3}{2}}\sqrt{1+\frac{bx}{a}}}{2} + \frac{3a^2 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(3/2)/x**(1/2), x)`

[Out] `5*a**(3/2)*sqrt(x)*sqrt(1 + b*x/a)/4 + sqrt(a)*b*x**(3/2)*sqrt(1 + b*x/a)/2 + 3*a**2*asinh(sqrt(b)*sqrt(x)/sqrt(a))/(4*sqrt(b))`

$$3.525 \quad \int \frac{(a+bx)^{3/2}}{x^{3/2}} dx$$

Optimal. Leaf size=63

$$-\frac{2(a+bx)^{3/2}}{\sqrt{x}} + 3b\sqrt{x}\sqrt{a+bx} + 3a\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)$$

[Out] $3*a*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})*b^{(1/2)}-2*(b*x+a)^{(3/2)}/x^{(1/2)}+3*b*x^{(1/2)}*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {47, 50, 63, 217, 206}

$$-\frac{2(a+bx)^{3/2}}{\sqrt{x}} + 3b\sqrt{x}\sqrt{a+bx} + 3a\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}/x^{(3/2)}, x]$

[Out] $3*b*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x] - (2*(a + b*x)^{(3/2)})/\operatorname{Sqrt}[x] + 3*a*\operatorname{Sqrt}[b]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]]$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(IntegerQ[n] \&\& !IntegerQ[m]) \&\& !(IntegerQ[m + n + 2, 0] \&\& (FractionQ[m] || GeQ[2*n + m + 1, 0])) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{NeQ}[m + n + 1, 0] \&\& !(IGtQ[m, 0] \&\& (!IntegerQ[n] || (GtQ[m, 0] \&\& LtQ[m - n, 0]))) \&\& !ILtQ[m + n + 2, 0] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{x^{3/2}} dx &= -\frac{2(a+bx)^{3/2}}{\sqrt{x}} + (3b) \int \frac{\sqrt{a+bx}}{\sqrt{x}} dx \\
&= 3b\sqrt{x}\sqrt{a+bx} - \frac{2(a+bx)^{3/2}}{\sqrt{x}} + \frac{1}{2}(3ab) \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx \\
&= 3b\sqrt{x}\sqrt{a+bx} - \frac{2(a+bx)^{3/2}}{\sqrt{x}} + (3ab) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right) \\
&= 3b\sqrt{x}\sqrt{a+bx} - \frac{2(a+bx)^{3/2}}{\sqrt{x}} + (3ab) \operatorname{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right) \\
&= 3b\sqrt{x}\sqrt{a+bx} - \frac{2(a+bx)^{3/2}}{\sqrt{x}} + 3a\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 46, normalized size = 0.73

$$\frac{2a\sqrt{a+bx} {}_2F_1\left(-\frac{3}{2}, -\frac{1}{2}; \frac{1}{2}; -\frac{bx}{a}\right)}{\sqrt{x}\sqrt{\frac{bx}{a}+1}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*x)^(3/2)/x^(3/2), x]
```

[Out] $(-2*a*\sqrt{a + b*x}*Hypergeometric2F1[-3/2, -1/2, 1/2, -(b*x)/a]) / (\sqrt{x}*\sqrt{1 + (b*x)/a})$

fricas [A] time = 0.53, size = 109, normalized size = 1.73

$$\left[\frac{3 a \sqrt{b} x \log \left(2 b x + 2 \sqrt{b x + a} \sqrt{b} \sqrt{x} + a \right) + 2 \sqrt{b x + a} (b x - 2 a) \sqrt{x}}{2 x}, -\frac{3 a \sqrt{-b} x \arctan \left(\frac{\sqrt{b x + a} \sqrt{-b}}{b \sqrt{x}} \right) - \sqrt{b x + a}}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^(3/2),x, algorithm="fricas")

[Out] $[1/2*(3*a*\sqrt{b}*x*\log(2*b*x + 2*\sqrt{b*x + a})*\sqrt{b}*\sqrt{x} + a) + 2*\sqrt{b*x + a}*(b*x - 2*a)*\sqrt{x})/x, -(3*a*\sqrt{-b}*x*\arctan(\sqrt{b*x + a}*\sqrt{-b}/(b*\sqrt{x}))) - \sqrt{b*x + a}*(b*x - 2*a)*\sqrt{x})/x]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^(3/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.02, size = 71, normalized size = 1.13

$$\frac{3\sqrt{(bx+a)x} a\sqrt{b} \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{2\sqrt{bx+a}\sqrt{x}} - \frac{\sqrt{bx+a}(-bx+2a)}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/x^(3/2),x)

[Out] $-(b*x+a)^{(1/2)}*(-b*x+2*a)/x^{(1/2)}+3/2*a*b^{(1/2)}*\ln((b*x+1/2*a)/b^{(1/2)}+(b*x^2+a*x)^{(1/2)})*((b*x+a)*x)^{(1/2)}/(b*x+a)^{(1/2)}/x^{(1/2)}$

maxima [A] time = 2.99, size = 84, normalized size = 1.33

$$-\frac{3}{2} a \sqrt{b} \log \left(-\frac{\sqrt{b} - \frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+a}}{\sqrt{x}}} \right) - \frac{2 \sqrt{bx+a} a}{\sqrt{x}} - \frac{\sqrt{bx+a} a b}{\left(b - \frac{bx+a}{x}\right) \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^(3/2),x, algorithm="maxima")

[Out] $-3/2*a*\sqrt{b}*\log(-(\sqrt{b} - \sqrt{b*x + a})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x + a})/\sqrt{x}) - 2*\sqrt{b*x + a}*a/\sqrt{x} - \sqrt{b*x + a}*a*b/((b - (b*x + a)/x)*\sqrt{x})$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^{3/2}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/x^(3/2),x)

[Out] int((a + b*x)^(3/2)/x^(3/2), x)

sympy [A] time = 2.72, size = 92, normalized size = 1.46

$$-\frac{2a^{\frac{3}{2}}}{\sqrt{x}\sqrt{1+\frac{bx}{a}}} - \frac{\sqrt{a}b\sqrt{x}}{\sqrt{1+\frac{bx}{a}}} + 3a\sqrt{b} \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) + \frac{b^2x^{\frac{3}{2}}}{\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/x**(3/2),x)

[Out] $-2*a**(3/2)/(\sqrt{x}*\sqrt{1 + b*x/a}) - \sqrt{a}*b*\sqrt{x}/\sqrt{1 + b*x/a} + 3*a*\sqrt{b}*\operatorname{asinh}(\sqrt{b}*\sqrt{x}/\sqrt{a}) + b**2*x**(3/2)/(\sqrt{a}*\sqrt{1 + b*x/a})$

$$3.526 \quad \int \frac{(a+bx)^{3/2}}{x^{5/2}} dx$$

Optimal. Leaf size=64

$$2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right) - \frac{2(a+bx)^{3/2}}{3x^{3/2}} - \frac{2b\sqrt{a+bx}}{\sqrt{x}}$$

[Out] $-2/3*(b*x+a)^{(3/2)}/x^{(3/2)}+2*b^{(3/2)}*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})$
 $-2*b*(b*x+a)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 63, 217, 206}

$$2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right) - \frac{2(a+bx)^{3/2}}{3x^{3/2}} - \frac{2b\sqrt{a+bx}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] `Int[(a + b*x)^(3/2)/x^(5/2), x]`

[Out] `(-2*b*Sqrt[a + b*x])/Sqrt[x] - (2*(a + b*x)^(3/2))/(3*x^(3/2)) + 2*b^(3/2)*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a + b*x]]`

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[Rt[-b, 2]*x]/
Rt[a, 2])]/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
```

Q[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{3/2}}{x^{5/2}} dx &= -\frac{2(a+bx)^{3/2}}{3x^{3/2}} + b \int \frac{\sqrt{a+bx}}{x^{3/2}} dx \\
 &= -\frac{2b\sqrt{a+bx}}{\sqrt{x}} - \frac{2(a+bx)^{3/2}}{3x^{3/2}} + b^2 \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx \\
 &= -\frac{2b\sqrt{a+bx}}{\sqrt{x}} - \frac{2(a+bx)^{3/2}}{3x^{3/2}} + (2b^2) \text{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right) \\
 &= -\frac{2b\sqrt{a+bx}}{\sqrt{x}} - \frac{2(a+bx)^{3/2}}{3x^{3/2}} + (2b^2) \text{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right) \\
 &= -\frac{2b\sqrt{a+bx}}{\sqrt{x}} - \frac{2(a+bx)^{3/2}}{3x^{3/2}} + 2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 48, normalized size = 0.75

$$\frac{2a\sqrt{a+bx} {}_2F_1\left(-\frac{3}{2}, -\frac{3}{2}; -\frac{1}{2}; -\frac{bx}{a}\right)}{3x^{3/2}\sqrt{\frac{bx}{a}+1}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/x^(5/2), x]

[Out] (-2*a*Sqrt[a + b*x]*Hypergeometric2F1[-3/2, -3/2, -1/2, -(b*x)/a])/(3*x^(3/2)*Sqrt[1 + (b*x)/a])

fricas [A] time = 0.47, size = 109, normalized size = 1.70

$$\left[\frac{3b^2x^2 \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) - 2(4bx + a)\sqrt{bx+a}\sqrt{x}}{3x^2}, -\frac{2\left(3\sqrt{-b}bx^2 \arctan\left(\frac{\sqrt{bx+a}\sqrt{-b}}{b\sqrt{x}}\right) + (4bx\right)}{3x^2} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^(5/2),x, algorithm="fricas")

[Out] [1/3*(3*b^(3/2)*x^2*log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) - 2*(4*b*x + a)*sqrt(b*x + a)*sqrt(x))/x^2, -2/3*(3*sqrt(-b)*b*x^2*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) + (4*b*x + a)*sqrt(b*x + a)*sqrt(x))/x^2]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^(5/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.02, size = 67, normalized size = 1.05

$$\frac{\sqrt{bx+a} x b^{\frac{3}{2}} \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{\sqrt{bx+a} \sqrt{x}} - \frac{2\sqrt{bx+a} (4bx+a)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/x^(5/2),x)

[Out] -2/3*(b*x+a)^(1/2)*(4*b*x+a)/x^(3/2)+b^(3/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))*((b*x+a)*x)^(1/2)/(b*x+a)^(1/2)/x^(1/2)

maxima [A] time = 2.93, size = 67, normalized size = 1.05

$$-b^{\frac{3}{2}} \log\left(\frac{\sqrt{b} - \frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+a}}{\sqrt{x}}}\right) - \frac{2\sqrt{bx+a} b}{\sqrt{x}} - \frac{2(bx+a)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/x^(5/2),x, algorithm="maxima")

[Out] -b^(3/2)*log(-(sqrt(b) - sqrt(b*x + a)/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x))) - 2*sqrt(b*x + a)*b/sqrt(x) - 2/3*(b*x + a)^(3/2)/x^(3/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a+bx)^{3/2}}{x^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(3/2)/x^(5/2), x)`

[Out] `int((a + b*x)^(3/2)/x^(5/2), x)`

sympy [A] time = 3.04, size = 71, normalized size = 1.11

$$-\frac{2a\sqrt{b}\sqrt{\frac{a}{bx}+1}}{3x} - \frac{8b^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}}{3} - b^{\frac{3}{2}}\log\left(\frac{a}{bx}\right) + 2b^{\frac{3}{2}}\log\left(\sqrt{\frac{a}{bx}+1} + 1\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(3/2)/x**(5/2), x)`

[Out] `-2*a*sqrt(b)*sqrt(a/(b*x) + 1)/(3*x) - 8*b**(3/2)*sqrt(a/(b*x) + 1)/3 - b**
(3/2)*log(a/(b*x)) + 2*b**(3/2)*log(sqrt(a/(b*x) + 1) + 1)`

3.527 $\int x^{5/2}(a - bx)^{3/2} dx$

Optimal. Leaf size=149

$$\frac{3a^5 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{128b^{7/2}} - \frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^3} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{5/2}\sqrt{a-bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a-bx} + \frac{1}{5}x^{7/2}(a-bx)^{3/2}$$

[Out] $1/5*x^{(7/2)}*(-b*x+a)^{(3/2)}+3/128*a^5*\arctan(b^{(1/2)}*x^{(1/2)}/(-b*x+a)^{(1/2)})/b^{(7/2)}-1/64*a^3*x^{(3/2)}*(-b*x+a)^{(1/2)}/b^2-1/80*a^2*x^{(5/2)}*(-b*x+a)^{(1/2)}/b+3/40*a*x^{(7/2)}*(-b*x+a)^{(1/2)}-3/128*a^4*x^{(1/2)}*(-b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.05, antiderivative size = 149, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$-\frac{a^3x^{3/2}\sqrt{a-bx}}{64b^2} - \frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^3} + \frac{3a^5 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{128b^{7/2}} - \frac{a^2x^{5/2}\sqrt{a-bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a-bx} + \frac{1}{5}x^{7/2}(a-bx)^{3/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(5/2)}*(a - b*x)^{(3/2)}, x]$

[Out] $(-3*a^4*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(128*b^3) - (a^3*x^{(3/2)}*\text{Sqrt}[a - b*x])/(64*b^2) - (a^2*x^{(5/2)}*\text{Sqrt}[a - b*x])/(80*b) + (3*a*x^{(7/2)}*\text{Sqrt}[a - b*x])/40 + (x^{(7/2)}*(a - b*x)^{(3/2)})/5 + (3*a^5*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(128*b^{(7/2)})$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int x^{5/2}(a-bx)^{3/2} dx &= \frac{1}{5}x^{7/2}(a-bx)^{3/2} + \frac{1}{10}(3a) \int x^{5/2}\sqrt{a-bx} dx \\
 &= \frac{3}{40}ax^{7/2}\sqrt{a-bx} + \frac{1}{5}x^{7/2}(a-bx)^{3/2} + \frac{1}{80}(3a^2) \int \frac{x^{5/2}}{\sqrt{a-bx}} dx \\
 &= -\frac{a^2x^{5/2}\sqrt{a-bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a-bx} + \frac{1}{5}x^{7/2}(a-bx)^{3/2} + \frac{a^3 \int \frac{x^{3/2}}{\sqrt{a-bx}} dx}{32b} \\
 &= -\frac{a^3x^{3/2}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{5/2}\sqrt{a-bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a-bx} + \frac{1}{5}x^{7/2}(a-bx)^{3/2} + \frac{(3a^4) \int \frac{\sqrt{x}}{\sqrt{a-bx}} dx}{128b^2} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^3} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{5/2}\sqrt{a-bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a-bx} + \frac{1}{5}x^{7/2}(a-bx)^{3/2} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^3} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{5/2}\sqrt{a-bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a-bx} + \frac{1}{5}x^{7/2}(a-bx)^{3/2} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^3} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{5/2}\sqrt{a-bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a-bx} + \frac{1}{5}x^{7/2}(a-bx)^{3/2} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^3} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{5/2}\sqrt{a-bx}}{80b} + \frac{3}{40}ax^{7/2}\sqrt{a-bx} + \frac{1}{5}x^{7/2}(a-bx)^{3/2}
 \end{aligned}$$

Mathematica [A] time = 0.17, size = 110, normalized size = 0.74

$$\frac{\sqrt{a-bx} \left(\frac{15a^{9/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{1-\frac{bx}{a}}} - \sqrt{b}\sqrt{x} (15a^4 + 10a^3bx + 8a^2b^2x^2 - 176ab^3x^3 + 128b^4x^4) \right)}{640b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*(a - b*x)^(3/2), x]

[Out] (Sqrt[a - b*x]*(-(Sqrt[b]*Sqrt[x]*(15*a^4 + 10*a^3*b*x + 8*a^2*b^2*x^2 - 17*6*a*b^3*x^3 + 128*b^4*x^4)) + (15*a^(9/2)*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 - (b*x)/a]))/(640*b^(7/2))

fricas [A] time = 0.48, size = 185, normalized size = 1.24

$$\left[\frac{15 a^5 \sqrt{-b} \log\left(-2 b x + 2 \sqrt{-b x + a} \sqrt{-b} \sqrt{x} + a\right) + 2\left(128 b^5 x^4 - 176 a b^4 x^3 + 8 a^2 b^3 x^2 + 10 a^3 b^2 x + 15 a^4 b\right) \sqrt{-b x + a}}{1280 b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(-b*x+a)^(3/2), x, algorithm="fricas")

[Out] [-1/1280*(15*a^5*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) + 2*(128*b^5*x^4 - 176*a*b^4*x^3 + 8*a^2*b^3*x^2 + 10*a^3*b^2*x + 15*a^4*b)*sqrt(-b*x + a)*sqrt(x))/b^4, -1/640*(15*a^5*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) + (128*b^5*x^4 - 176*a*b^4*x^3 + 8*a^2*b^3*x^2 + 10*a^3*b^2*x + 15*a^4*b)*sqrt(-b*x + a)*sqrt(x))/b^4]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(-b*x+a)^(3/2), x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 146, normalized size = 0.98

$$\frac{3\sqrt{-bx+a} x a^5 \arctan\left(\frac{\left(x-\frac{a}{2b}\right)\sqrt{b}}{\sqrt{-bx^2+ax}}\right)}{256\sqrt{-bx+a} b^{\frac{7}{2}}\sqrt{x}} + \frac{3\sqrt{-bx+a} a^4 \sqrt{x}}{128b^3} - \frac{(-bx+a)^{\frac{5}{2}} x^{\frac{5}{2}}}{5b} + \frac{(-bx+a)^{\frac{3}{2}} a^3 \sqrt{x}}{64b^3} - \frac{(-bx+a)^{\frac{5}{2}} a x^{\frac{3}{2}}}{8b^2} - \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(-b*x+a)^(3/2), x)

[Out] -1/5/b*x^(5/2)*(-b*x+a)^(5/2)-1/8*a/b^2*x^(3/2)*(-b*x+a)^(5/2)-1/16*a^2/b^3*x^(1/2)*(-b*x+a)^(5/2)+1/64*a^3/b^3*(-b*x+a)^(3/2)*x^(1/2)+3/128*a^4*x^(1/2)

2)*(-b*x+a)^(1/2)/b^3+3/256*a^5/b^(7/2)*((-b*x+a)*x)^(1/2)/(-b*x+a)^(1/2)/x
^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))

maxima [A] time = 3.12, size = 207, normalized size = 1.39

$$-\frac{3a^5 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{128b^{\frac{7}{2}}} + \frac{\frac{15\sqrt{-bx+a}a^5b^4}{\sqrt{x}} + \frac{70(-bx+a)^{\frac{3}{2}}a^5b^3}{x^{\frac{3}{2}}} - \frac{128(-bx+a)^{\frac{5}{2}}a^5b^2}{x^{\frac{5}{2}}} - \frac{70(-bx+a)^{\frac{7}{2}}a^5b}{x^{\frac{7}{2}}} - \frac{15(-bx+a)^{\frac{9}{2}}a^5}{x^{\frac{9}{2}}}}{640\left(b^8 - \frac{5(bx-a)b^7}{x} + \frac{10(bx-a)^2b^6}{x^2} - \frac{10(bx-a)^3b^5}{x^3} + \frac{5(bx-a)^4b^4}{x^4} - \frac{(bx-a)^5b^3}{x^5}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(-b*x+a)^(3/2),x, algorithm="maxima")

[Out] -3/128*a^5*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/b^(7/2) + 1/640*(15*sqrt(-b*x + a)*a^5*b^4/sqrt(x) + 70*(-b*x + a)^(3/2)*a^5*b^3/x^(3/2) - 128*(-b*x + a)^(5/2)*a^5*b^2/x^(5/2) - 70*(-b*x + a)^(7/2)*a^5*b/x^(7/2) - 15*(-b*x + a)^(9/2)*a^5/x^(9/2))/(b^8 - 5*(b*x - a)*b^7/x + 10*(b*x - a)^2*b^6/x^2 - 10*(b*x - a)^3*b^5/x^3 + 5*(b*x - a)^4*b^4/x^4 - (b*x - a)^5*b^3/x^5)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} (a - bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(a - b*x)^(3/2),x)

[Out] int(x^(5/2)*(a - b*x)^(3/2), x)

sympy [A] time = 17.69, size = 376, normalized size = 2.52

$$\left\{ \begin{array}{l} \frac{3ia^{\frac{9}{2}}\sqrt{x}}{128b^3\sqrt{-1+\frac{bx}{a}}} - \frac{ia^{\frac{7}{2}}x^{\frac{3}{2}}}{128b^2\sqrt{-1+\frac{bx}{a}}} - \frac{ia^{\frac{5}{2}}x^{\frac{5}{2}}}{320b\sqrt{-1+\frac{bx}{a}}} - \frac{23ia^{\frac{3}{2}}x^{\frac{7}{2}}}{80\sqrt{-1+\frac{bx}{a}}} + \frac{19i\sqrt{a}bx^{\frac{9}{2}}}{40\sqrt{-1+\frac{bx}{a}}} - \frac{3ia^5\operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{128b^{\frac{7}{2}}} - \frac{ib^2x^{\frac{11}{2}}}{5\sqrt{a}\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{3a^{\frac{9}{2}}\sqrt{x}}{128b^3\sqrt{1-\frac{bx}{a}}} + \frac{a^{\frac{7}{2}}x^{\frac{3}{2}}}{128b^2\sqrt{1-\frac{bx}{a}}} + \frac{a^{\frac{5}{2}}x^{\frac{5}{2}}}{320b\sqrt{1-\frac{bx}{a}}} + \frac{23a^{\frac{3}{2}}x^{\frac{7}{2}}}{80\sqrt{1-\frac{bx}{a}}} - \frac{19\sqrt{a}bx^{\frac{9}{2}}}{40\sqrt{1-\frac{bx}{a}}} + \frac{3a^5\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{128b^{\frac{7}{2}}} + \frac{b^2x^{\frac{11}{2}}}{5\sqrt{a}\sqrt{1-\frac{bx}{a}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)*(-b*x+a)**(3/2),x)

[Out] Piecewise((3*I*a**(9/2)*sqrt(x)/(128*b**3*sqrt(-1 + b*x/a)) - I*a**(7/2)*x**(3/2)/(128*b**2*sqrt(-1 + b*x/a)) - I*a**(5/2)*x**(5/2)/(320*b*sqrt(-1 + b

```

*x/a)) - 23*I*a**(3/2)*x**(7/2)/(80*sqrt(-1 + b*x/a)) + 19*I*sqrt(a)*b*x**(
9/2)/(40*sqrt(-1 + b*x/a)) - 3*I*a**5*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(128*b
**(7/2)) - I*b**2*x**(11/2)/(5*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1),
(-3*a**(9/2)*sqrt(x)/(128*b**3*sqrt(1 - b*x/a)) + a**(7/2)*x**(3/2)/(128*b*
*2*sqrt(1 - b*x/a)) + a**(5/2)*x**(5/2)/(320*b*sqrt(1 - b*x/a)) + 23*a**(3/
2)*x**(7/2)/(80*sqrt(1 - b*x/a)) - 19*sqrt(a)*b*x**(9/2)/(40*sqrt(1 - b*x/a
)) + 3*a**5*asin(sqrt(b)*sqrt(x)/sqrt(a))/(128*b**(7/2)) + b**2*x**(11/2)/(
5*sqrt(a)*sqrt(1 - b*x/a)), True))

```

3.528 $\int x^{3/2}(a - bx)^{3/2} dx$

Optimal. Leaf size=124

$$\frac{3a^4 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{64b^{5/2}} - \frac{3a^3\sqrt{x}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{3/2}\sqrt{a-bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a-bx} + \frac{1}{4}x^{5/2}(a-bx)^{3/2}$$

[Out] $1/4*x^{(5/2)}*(-b*x+a)^{(3/2)}+3/64*a^4*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(5/2)}-1/32*a^2*x^{(3/2)}*(-b*x+a)^{(1/2)}/b+1/8*a*x^{(5/2)}*(-b*x+a)^{(1/2)}-3/64*a^3*x^{(1/2)}*(-b*x+a)^{(1/2)}/b^2$

Rubi [A] time = 0.04, antiderivative size = 124, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$-\frac{3a^3\sqrt{x}\sqrt{a-bx}}{64b^2} + \frac{3a^4 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{64b^{5/2}} - \frac{a^2x^{3/2}\sqrt{a-bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a-bx} + \frac{1}{4}x^{5/2}(a-bx)^{3/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(3/2)}*(a - b*x)^{(3/2)}, x]$

[Out] $(-3*a^3*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(64*b^2) - (a^2*x^{(3/2)}*\text{Sqrt}[a - b*x])/(32*b) + (a*x^{(5/2)}*\text{Sqrt}[a - b*x])/8 + (x^{(5/2)}*(a - b*x)^{(3/2)})/4 + (3*a^4*\text{ArcT an}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(64*b^{(5/2)})$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
 \int x^{3/2}(a-bx)^{3/2} dx &= \frac{1}{4}x^{5/2}(a-bx)^{3/2} + \frac{1}{8}(3a) \int x^{3/2}\sqrt{a-bx} dx \\
 &= \frac{1}{8}ax^{5/2}\sqrt{a-bx} + \frac{1}{4}x^{5/2}(a-bx)^{3/2} + \frac{1}{16}a^2 \int \frac{x^{3/2}}{\sqrt{a-bx}} dx \\
 &= -\frac{a^2x^{3/2}\sqrt{a-bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a-bx} + \frac{1}{4}x^{5/2}(a-bx)^{3/2} + \frac{(3a^3) \int \frac{\sqrt{x}}{\sqrt{a-bx}} dx}{64b} \\
 &= -\frac{3a^3\sqrt{x}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{3/2}\sqrt{a-bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a-bx} + \frac{1}{4}x^{5/2}(a-bx)^{3/2} + \frac{(3a^4) \int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx}{128b^2} \\
 &= -\frac{3a^3\sqrt{x}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{3/2}\sqrt{a-bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a-bx} + \frac{1}{4}x^{5/2}(a-bx)^{3/2} + \frac{(3a^4) \text{Subst}\left(\int \frac{1}{\sqrt{u}} du\right)}{64b^2} \\
 &= -\frac{3a^3\sqrt{x}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{3/2}\sqrt{a-bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a-bx} + \frac{1}{4}x^{5/2}(a-bx)^{3/2} + \frac{(3a^4) \text{Subst}\left(\int \frac{1}{\sqrt{u}} du\right)}{64b^2} \\
 &= -\frac{3a^3\sqrt{x}\sqrt{a-bx}}{64b^2} - \frac{a^2x^{3/2}\sqrt{a-bx}}{32b} + \frac{1}{8}ax^{5/2}\sqrt{a-bx} + \frac{1}{4}x^{5/2}(a-bx)^{3/2} + \frac{3a^4 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{64b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.15, size = 99, normalized size = 0.80

$$\frac{\sqrt{a-bx} \left(\frac{3a^{7/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{1-\frac{bx}{a}}} - \sqrt{b}\sqrt{x} (3a^3 + 2a^2bx - 24ab^2x^2 + 16b^3x^3) \right)}{64b^{5/2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(3/2)*(a - b*x)^(3/2), x]
```


[Out] $(\sqrt{a - bx} * (-(\sqrt{b} * \sqrt{x} * (3a^3 + 2a^2bx - 24ab^2x^2 + 16b^3x^3)) + (3a^{7/2} * \text{ArcSin}[(\sqrt{b} * \sqrt{x}) / \sqrt{a}]) / \sqrt{1 - (bx)/a})) / (64b^{5/2})$

fricas [A] time = 0.44, size = 163, normalized size = 1.31

$$\left[\frac{3a^4\sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) + 2(16b^4x^3 - 24ab^3x^2 + 2a^2b^2x + 3a^3b)\sqrt{-bx+a}\sqrt{x}}{128b^3}, - \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)*(-b*x+a)^(3/2),x, algorithm="fricas")`

[Out] $[-1/128*(3a^4*\sqrt{-b}*\log(-2*bx + 2*\sqrt{-bx+a}*\sqrt{-b}*\sqrt{x} + a) + 2*(16*b^4*x^3 - 24*a*b^3*x^2 + 2*a^2*b^2*x + 3*a^3*b)*\sqrt{-bx+a}*\sqrt{x})/b^3, -1/64*(3a^4*\sqrt{b}*\arctan(\sqrt{-bx+a}/(\sqrt{b}*\sqrt{x}))) + (16*b^4*x^3 - 24*a*b^3*x^2 + 2*a^2*b^2*x + 3*a^3*b)*\sqrt{-bx+a}*\sqrt{x})/b^3]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)*(-b*x+a)^(3/2),x, algorithm="giac")`

[Out] Timed out

maple [A] time = 0.01, size = 127, normalized size = 1.02

$$\frac{3\sqrt{-bx+a}x a^4 \arctan\left(\frac{(x-\frac{a}{2b})\sqrt{b}}{\sqrt{-bx^2+ax}}\right)}{128\sqrt{-bx+a} b^{\frac{5}{2}}\sqrt{x}} + \frac{3\sqrt{-bx+a} a^3\sqrt{x}}{64b^2} + \frac{(-bx+a)^{\frac{3}{2}} a^2\sqrt{x}}{32b^2} - \frac{(-bx+a)^{\frac{5}{2}} x^{\frac{3}{2}}}{4b} - \frac{(-bx+a)^{\frac{5}{2}} a\sqrt{x}}{8b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)*(-b*x+a)^(3/2),x)`

[Out] $-1/4/b*x^{3/2}*(-b*x+a)^{5/2} - 1/8*a/b^2*x^{1/2}*(-b*x+a)^{5/2} + 1/32*a^2/b^2*(-b*x+a)^{3/2}*x^{1/2} + 3/64*a^3*x^{1/2}*(-b*x+a)^{1/2}/b^2 + 3/128*a^4/b^{5/2}*((-b*x+a)*x)^{1/2}/(-b*x+a)^{1/2}/x^{1/2}*\arctan((x-1/2*a/b)/(-b*x^2+a*x)^{1/2})*b^{1/2}$

maxima [A] time = 2.97, size = 170, normalized size = 1.37

$$-\frac{3a^4 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{64b^{\frac{5}{2}}} + \frac{3\sqrt{-bx+a}a^4b^3}{\sqrt{x}} + \frac{11(-bx+a)^{\frac{3}{2}}a^4b^2}{x^{\frac{3}{2}}} - \frac{11(-bx+a)^{\frac{5}{2}}a^4b}{x^{\frac{5}{2}}} - \frac{3(-bx+a)^{\frac{7}{2}}a^4}{x^{\frac{7}{2}}}$$

$$64\left(b^6 - \frac{4(bx-a)b^5}{x} + \frac{6(bx-a)^2b^4}{x^2} - \frac{4(bx-a)^3b^3}{x^3} + \frac{(bx-a)^4b^2}{x^4}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+a)^(3/2),x, algorithm="maxima")

[Out] -3/64*a^4*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/b^(5/2) + 1/64*(3*sqrt(-b*x + a)*a^4*b^3/sqrt(x) + 11*(-b*x + a)^(3/2)*a^4*b^2/x^(3/2) - 11*(-b*x + a)^(5/2)*a^4*b/x^(5/2) - 3*(-b*x + a)^(7/2)*a^4/x^(7/2))/(b^6 - 4*(b*x - a)*b^5/x + 6*(b*x - a)^2*b^4/x^2 - 4*(b*x - a)^3*b^3/x^3 + (b*x - a)^4*b^2/x^4)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} (a - bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(a - b*x)^(3/2),x)

[Out] int(x^(3/2)*(a - b*x)^(3/2), x)

sympy [A] time = 9.06, size = 323, normalized size = 2.60

$$\left\{ \begin{array}{l} \frac{3ia^{\frac{7}{2}}\sqrt{x}}{64b^2\sqrt{-1+\frac{bx}{a}}} - \frac{5a^{\frac{5}{2}}x^{\frac{3}{2}}}{64b\sqrt{-1+\frac{bx}{a}}} - \frac{13ia^{\frac{3}{2}}x^{\frac{5}{2}}}{32\sqrt{-1+\frac{bx}{a}}} + \frac{5i\sqrt{a}bx^{\frac{7}{2}}}{8\sqrt{-1+\frac{bx}{a}}} - \frac{3ia^4 \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{64b^{\frac{5}{2}}} - \frac{ib^2x^{\frac{9}{2}}}{4\sqrt{a}\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{3a^{\frac{7}{2}}\sqrt{x}}{64b^2\sqrt{1-\frac{bx}{a}}} + \frac{5a^{\frac{5}{2}}x^{\frac{3}{2}}}{64b\sqrt{1-\frac{bx}{a}}} + \frac{13a^{\frac{3}{2}}x^{\frac{5}{2}}}{32\sqrt{1-\frac{bx}{a}}} - \frac{5\sqrt{a}bx^{\frac{7}{2}}}{8\sqrt{1-\frac{bx}{a}}} + \frac{3a^4 \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{64b^{\frac{5}{2}}} + \frac{b^2x^{\frac{9}{2}}}{4\sqrt{a}\sqrt{1-\frac{bx}{a}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)*(-b*x+a)**(3/2),x)

[Out] Piecewise((3*I*a**(7/2)*sqrt(x)/(64*b**2*sqrt(-1 + b*x/a)) - I*a**(5/2)*x**(3/2)/(64*b*sqrt(-1 + b*x/a)) - 13*I*a**(3/2)*x**(5/2)/(32*sqrt(-1 + b*x/a)) + 5*I*sqrt(a)*b*x**(7/2)/(8*sqrt(-1 + b*x/a)) - 3*I*a**4*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(64*b**(5/2)) - I*b**2*x**(9/2)/(4*sqrt(a)*sqrt(-1 + b*x/a))

```
, Abs(b*x/a) > 1), (-3*a**(7/2)*sqrt(x)/(64*b**2*sqrt(1 - b*x/a)) + a**(5/2)
)*x**(3/2)/(64*b*sqrt(1 - b*x/a)) + 13*a**(3/2)*x**(5/2)/(32*sqrt(1 - b*x/a
)) - 5*sqrt(a)*b*x**(7/2)/(8*sqrt(1 - b*x/a)) + 3*a**4*asin(sqrt(b)*sqrt(x)
/sqrt(a))/(64*b**(5/2)) + b**2*x**(9/2)/(4*sqrt(a)*sqrt(1 - b*x/a)), True))
```

3.529 $\int \sqrt{x} (a - bx)^{3/2} dx$

Optimal. Leaf size=99

$$\frac{a^3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{8b^{3/2}} - \frac{a^2\sqrt{x}\sqrt{a-bx}}{8b} + \frac{1}{4}ax^{3/2}\sqrt{a-bx} + \frac{1}{3}x^{3/2}(a-bx)^{3/2}$$

[Out] $1/3*x^{(3/2)}*(-b*x+a)^{(3/2)}+1/8*a^3*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(3/2)}+1/4*a*x^{(3/2)}*(-b*x+a)^{(1/2)}-1/8*a^2*x^{(1/2)}*(-b*x+a)^{(1/2)}/b$

Rubi [A] time = 0.03, antiderivative size = 99, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$\frac{a^3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{8b^{3/2}} - \frac{a^2\sqrt{x}\sqrt{a-bx}}{8b} + \frac{1}{4}ax^{3/2}\sqrt{a-bx} + \frac{1}{3}x^{3/2}(a-bx)^{3/2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*(a - b*x)^(3/2), x]

[Out] $-(a^2*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(8*b) + (a*x^{(3/2)}*\text{Sqrt}[a - b*x])/4 + (x^{(3/2)}*(a - b*x)^{(3/2)})/3 + (a^3*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(8*b^{(3/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

`Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])`

Rule 217

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]`

Rubi steps

$$\begin{aligned}
 \int \sqrt{x} (a - bx)^{3/2} dx &= \frac{1}{3} x^{3/2} (a - bx)^{3/2} + \frac{1}{2} a \int \sqrt{x} \sqrt{a - bx} dx \\
 &= \frac{1}{4} a x^{3/2} \sqrt{a - bx} + \frac{1}{3} x^{3/2} (a - bx)^{3/2} + \frac{1}{8} a^2 \int \frac{\sqrt{x}}{\sqrt{a - bx}} dx \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a - bx}}{8b} + \frac{1}{4} a x^{3/2} \sqrt{a - bx} + \frac{1}{3} x^{3/2} (a - bx)^{3/2} + \frac{a^3 \int \frac{1}{\sqrt{x} \sqrt{a - bx}} dx}{16b} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a - bx}}{8b} + \frac{1}{4} a x^{3/2} \sqrt{a - bx} + \frac{1}{3} x^{3/2} (a - bx)^{3/2} + \frac{a^3 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a - bx^2}} dx, x, \sqrt{x}\right)}{8b} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a - bx}}{8b} + \frac{1}{4} a x^{3/2} \sqrt{a - bx} + \frac{1}{3} x^{3/2} (a - bx)^{3/2} + \frac{a^3 \operatorname{Subst}\left(\int \frac{1}{1 + bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a - bx}}\right)}{8b} \\
 &= -\frac{a^2 \sqrt{x} \sqrt{a - bx}}{8b} + \frac{1}{4} a x^{3/2} \sqrt{a - bx} + \frac{1}{3} x^{3/2} (a - bx)^{3/2} + \frac{a^3 \tan^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a - bx}}\right)}{8b^{3/2}}
 \end{aligned}$$

Mathematica [A] time = 0.12, size = 87, normalized size = 0.88

$$\frac{\sqrt{a - bx} \left(\frac{3a^{5/2} \sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{1 - \frac{bx}{a}}} + \sqrt{b} \sqrt{x} (-3a^2 + 14abx - 8b^2x^2) \right)}{24b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*(a - b*x)^(3/2), x]

[Out] (Sqrt[a - b*x]*(Sqrt[b]*Sqrt[x]*(-3*a^2 + 14*a*b*x - 8*b^2*x^2) + (3*a^(5/2)*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 - (b*x)/a])/(24*b^(3/2))

fricas [A] time = 0.46, size = 141, normalized size = 1.42

$$\left[\frac{3 a^3 \sqrt{-b} \log(-2 b x + 2 \sqrt{-b x + a} \sqrt{-b} \sqrt{x} + a) + 2 (8 b^3 x^2 - 14 a b^2 x + 3 a^2 b) \sqrt{-b x + a} \sqrt{x}}{48 b^2}, - \frac{3 a^3 \sqrt{b} \arctan}{}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(3/2)*x^(1/2),x, algorithm="fricas")

[Out] [-1/48*(3*a^3*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) + 2*(8*b^3*x^2 - 14*a*b^2*x + 3*a^2*b)*sqrt(-b*x + a)*sqrt(x))/b^2, -1/24*(3*a^3*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) + (8*b^3*x^2 - 14*a*b^2*x + 3*a^2*b)*sqrt(-b*x + a)*sqrt(x))/b^2]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(3/2)*x^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 102, normalized size = 1.03

$$\frac{\sqrt{-b x + a} a^3 x^{\frac{3}{2}}}{4} + \frac{\sqrt{-b x + a} x a^3 \arctan\left(\frac{(x - \frac{a}{2b})\sqrt{b}}{\sqrt{-b x^2 + a x}}\right)}{16\sqrt{-b x + a} b^{\frac{3}{2}} \sqrt{x}} - \frac{\sqrt{-b x + a} a^2 \sqrt{x}}{8b} + \frac{(-b x + a)^{\frac{3}{2}} x^{\frac{3}{2}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+a)^(3/2)*x^(1/2),x)

[Out] 1/3*x^(3/2)*(-b*x+a)^(3/2)+1/4*a*x^(3/2)*(-b*x+a)^(1/2)-1/8*a^2*x^(1/2)*(-b*x+a)^(1/2)/b+1/16*a^3/b^(3/2)*((-b*x+a)*x)^(1/2)/x^(1/2)/(-b*x+a)^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))

maxima [A] time = 2.99, size = 133, normalized size = 1.34

$$-\frac{a^3 \arctan\left(\frac{\sqrt{-b x + a}}{\sqrt{b} \sqrt{x}}\right)}{8 b^{\frac{3}{2}}} + \frac{\frac{3 \sqrt{-b x + a} a^3 b^2}{\sqrt{x}} + \frac{8 (-b x + a)^{\frac{3}{2}} a^3 b}{x^{\frac{3}{2}}} - \frac{3 (-b x + a)^{\frac{5}{2}} a^3}{x^{\frac{5}{2}}}}{24 \left(b^4 - \frac{3 (b x - a) b^3}{x} + \frac{3 (b x - a)^2 b^2}{x^2} - \frac{(b x - a)^3 b}{x^3} \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(3/2)*x^(1/2),x, algorithm="maxima")

[Out] $-1/8*a^3*\arctan(\sqrt{-b*x+a}/(\sqrt{b}*\sqrt{x}))/b^{(3/2)} + 1/24*(3*\sqrt{-b*x+a})*a^3*b^2/\sqrt{x} + 8*(-b*x+a)^{(3/2)}*a^3*b/x^{(3/2)} - 3*(-b*x+a)^{(5/2)}*a^3/x^{(5/2)}/(b^4 - 3*(b*x-a)*b^3/x + 3*(b*x-a)^2*b^2/x^2 - (b*x-a)^3*b/x^3)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{x} (a - bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)*(a - b*x)^(3/2),x)

[Out] int(x^(1/2)*(a - b*x)^(3/2), x)

sympy [A] time = 5.54, size = 264, normalized size = 2.67

$$\begin{cases} \frac{ia^2\sqrt{x}}{8b\sqrt{-1+\frac{bx}{a}}} - \frac{17ia^2x^2}{24\sqrt{-1+\frac{bx}{a}}} + \frac{11i\sqrt{a}bx^2}{12\sqrt{-1+\frac{bx}{a}}} - \frac{ia^3\operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8b^2} - \frac{ib^2x^2}{3\sqrt{a}\sqrt{-1+\frac{bx}{a}}} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{a^2\sqrt{x}}{8b\sqrt{1-\frac{bx}{a}}} + \frac{17a^2x^2}{24\sqrt{1-\frac{bx}{a}}} - \frac{11\sqrt{a}bx^2}{12\sqrt{1-\frac{bx}{a}}} + \frac{a^3\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8b^2} + \frac{b^2x^2}{3\sqrt{a}\sqrt{1-\frac{bx}{a}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)**(3/2)*x**(1/2),x)

[Out] Piecewise((I*a**(5/2)*sqrt(x)/(8*b*sqrt(-1 + b*x/a)) - 17*I*a**(3/2)*x**(3/2)/(24*sqrt(-1 + b*x/a)) + 11*I*sqrt(a)*b*x**(5/2)/(12*sqrt(-1 + b*x/a)) - I*a**3*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(8*b**(3/2)) - I*b**2*x**(7/2)/(3*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (-a**(5/2)*sqrt(x)/(8*b*sqrt(1 - b*x/a)) + 17*a**(3/2)*x**(3/2)/(24*sqrt(1 - b*x/a)) - 11*sqrt(a)*b*x**(5/2)/(12*sqrt(1 - b*x/a)) + a**3*asin(sqrt(b)*sqrt(x)/sqrt(a))/(8*b**(3/2)) + b**2*x**(7/2)/(3*sqrt(a)*sqrt(1 - b*x/a)), True))

$$3.530 \quad \int \frac{(a-bx)^{3/2}}{\sqrt{x}} dx$$

Optimal. Leaf size=74

$$\frac{3a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4\sqrt{b}} + \frac{3}{4}a\sqrt{x}\sqrt{a-bx} + \frac{1}{2}\sqrt{x}(a-bx)^{3/2}$$

[Out] $3/4*a^2*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(1/2)}+1/2*(-b*x+a)^{(3/2)}*x^{(1/2)}+3/4*a*x^{(1/2)}*(-b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$\frac{3a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4\sqrt{b}} + \frac{3}{4}a\sqrt{x}\sqrt{a-bx} + \frac{1}{2}\sqrt{x}(a-bx)^{3/2}$$

Antiderivative was successfully verified.

[In] Int[(a - b*x)^(3/2)/Sqrt[x], x]

[Out] $(3*a*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/4 + (\text{Sqrt}[x]*(a - b*x)^{(3/2)})/2 + (3*a^2*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(4*\text{Sqrt}[b])$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a-bx)^{3/2}}{\sqrt{x}} dx &= \frac{1}{2} \sqrt{x} (a-bx)^{3/2} + \frac{1}{4} (3a) \int \frac{\sqrt{a-bx}}{\sqrt{x}} dx \\
 &= \frac{3}{4} a \sqrt{x} \sqrt{a-bx} + \frac{1}{2} \sqrt{x} (a-bx)^{3/2} + \frac{1}{8} (3a^2) \int \frac{1}{\sqrt{x} \sqrt{a-bx}} dx \\
 &= \frac{3}{4} a \sqrt{x} \sqrt{a-bx} + \frac{1}{2} \sqrt{x} (a-bx)^{3/2} + \frac{1}{4} (3a^2) \text{Subst} \left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x} \right) \\
 &= \frac{3}{4} a \sqrt{x} \sqrt{a-bx} + \frac{1}{2} \sqrt{x} (a-bx)^{3/2} + \frac{1}{4} (3a^2) \text{Subst} \left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}} \right) \\
 &= \frac{3}{4} a \sqrt{x} \sqrt{a-bx} + \frac{1}{2} \sqrt{x} (a-bx)^{3/2} + \frac{3a^2 \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a-bx}} \right)}{4\sqrt{b}}
 \end{aligned}$$

Mathematica [A] time = 0.12, size = 71, normalized size = 0.96

$$\frac{1}{4} \sqrt{a-bx} \left(\frac{3a^{3/2} \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{b} \sqrt{1 - \frac{bx}{a}}} + \sqrt{x} (5a - 2bx) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a - b*x)^(3/2)/Sqrt[x], x]

[Out] (Sqrt[a - b*x]*(Sqrt[x]*(5*a - 2*b*x) + (3*a^(3/2)*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[b]*Sqrt[1 - (b*x)/a]))) / 4

fricas [A] time = 0.45, size = 119, normalized size = 1.61

$$\left[\frac{3a^2 \sqrt{-b} \log(-2bx + 2\sqrt{-bx+a} \sqrt{-b} \sqrt{x} + a) + 2(2b^2x - 5ab) \sqrt{-bx+a} \sqrt{x}}{8b}, -\frac{3a^2 \sqrt{b} \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b} \sqrt{x}}\right)}{4\sqrt{b}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(3/2)/x^(1/2),x, algorithm="fricas")

[Out] [-1/8*(3*a^2*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) + 2*(2*b^2*x - 5*a*b)*sqrt(-b*x + a)*sqrt(x))/b, -1/4*(3*a^2*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) + (2*b^2*x - 5*a*b)*sqrt(-b*x + a)*sqrt(x))/b]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(3/2)/x^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.00, size = 83, normalized size = 1.12

$$\frac{3\sqrt{-bx+a} x a^2 \arctan\left(\frac{(x-\frac{a}{2b})\sqrt{b}}{\sqrt{-bx+a}x}\right)}{8\sqrt{-bx+a} \sqrt{b} \sqrt{x}} + \frac{3\sqrt{-bx+a} a \sqrt{x}}{4} + \frac{(-bx+a)^{\frac{3}{2}} \sqrt{x}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+a)^(3/2)/x^(1/2),x)

[Out] 1/2*(-b*x+a)^(3/2)*x^(1/2)+3/4*a*x^(1/2)*(-b*x+a)^(1/2)+3/8*a^2*((-b*x+a)*x)^(1/2)/(-b*x+a)^(1/2)/x^(1/2)/b^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2))*b^(1/2))

maxima [A] time = 2.90, size = 93, normalized size = 1.26

$$-\frac{3 a^2 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b} \sqrt{x}}\right)}{4 \sqrt{b}} + \frac{\frac{3 \sqrt{-bx+a} a^2 b}{\sqrt{x}} + \frac{5(-bx+a)^{\frac{3}{2}} a^2}{x^2}}{4 \left(b^2 - \frac{2(bx-a)b}{x} + \frac{(bx-a)^2}{x^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(3/2)/x^(1/2),x, algorithm="maxima")

[Out] -3/4*a^2*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/sqrt(b) + 1/4*(3*sqrt(-b*x + a)*a^2*b/sqrt(x) + 5*(-b*x + a)^(3/2)*a^2/x^(3/2))/(b^2 - 2*(b*x - a)*b/x + (b*x - a)^2/x^2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - bx)^{3/2}}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - b*x)^(3/2)/x^(1/2), x)`

[Out] `int((a - b*x)^(3/2)/x^(1/2), x)`

sympy [A] time = 3.21, size = 190, normalized size = 2.57

$$\left\{ \begin{array}{l} -\frac{5ia^2\sqrt{x}}{4\sqrt{-1+\frac{bx}{a}}} + \frac{7i\sqrt{a}bx^{\frac{3}{2}}}{4\sqrt{-1+\frac{bx}{a}}} - \frac{3ia^2\operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{b}} - \frac{ib^2x^{\frac{5}{2}}}{2\sqrt{a}\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ \frac{5a^{\frac{3}{2}}\sqrt{x}\sqrt{1-\frac{bx}{a}}}{4} - \frac{\sqrt{a}bx^{\frac{3}{2}}\sqrt{1-\frac{bx}{a}}}{2} + \frac{3a^2\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4\sqrt{b}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+a)**(3/2)/x**(1/2), x)`

[Out] `Piecewise((-5*I*a**(3/2)*sqrt(x)/(4*sqrt(-1 + b*x/a)) + 7*I*sqrt(a)*b*x**(3/2)/(4*sqrt(-1 + b*x/a)) - 3*I*a**2*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(4*sqrt(b)) - I*b**2*x**(5/2)/(2*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (5*a**(3/2)*sqrt(x)*sqrt(1 - b*x/a)/4 - sqrt(a)*b*x**(3/2)*sqrt(1 - b*x/a)/2 + 3*a**2*asin(sqrt(b)*sqrt(x)/sqrt(a))/(4*sqrt(b)), True)`

$$3.531 \quad \int \frac{(a-bx)^{3/2}}{x^{3/2}} dx$$

Optimal. Leaf size=66

$$-\frac{2(a-bx)^{3/2}}{\sqrt{x}} - 3b\sqrt{x}\sqrt{a-bx} - 3a\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)$$

[Out] $-3*a*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})*b^{(1/2)}-2*(-b*x+a)^{(3/2)/x^{(1/2)}}-3*b*x^{(1/2)}*(-b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.312$, Rules used = {47, 50, 63, 217, 203}

$$-\frac{2(a-bx)^{3/2}}{\sqrt{x}} - 3b\sqrt{x}\sqrt{a-bx} - 3a\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)$$

Antiderivative was successfully verified.

[In] Int[(a - b*x)^(3/2)/x^(3/2), x]

[Out] $-3*b*\text{Sqrt}[x]*\text{Sqrt}[a - b*x] - (2*(a - b*x)^{(3/2)})/\text{Sqrt}[x] - 3*a*\text{Sqrt}[b]*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a - bx)^{3/2}}{x^{3/2}} dx &= -\frac{2(a - bx)^{3/2}}{\sqrt{x}} - (3b) \int \frac{\sqrt{a - bx}}{\sqrt{x}} dx \\
&= -3b\sqrt{x}\sqrt{a - bx} - \frac{2(a - bx)^{3/2}}{\sqrt{x}} - \frac{1}{2}(3ab) \int \frac{1}{\sqrt{x}\sqrt{a - bx}} dx \\
&= -3b\sqrt{x}\sqrt{a - bx} - \frac{2(a - bx)^{3/2}}{\sqrt{x}} - (3ab) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a - bx^2}} dx, x, \sqrt{x}\right) \\
&= -3b\sqrt{x}\sqrt{a - bx} - \frac{2(a - bx)^{3/2}}{\sqrt{x}} - (3ab) \operatorname{Subst}\left(\int \frac{1}{1 + bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a - bx}}\right) \\
&= -3b\sqrt{x}\sqrt{a - bx} - \frac{2(a - bx)^{3/2}}{\sqrt{x}} - 3a\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a - bx}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 47, normalized size = 0.71

$$-\frac{2a\sqrt{a - bx} {}_2F_1\left(-\frac{3}{2}, -\frac{1}{2}; \frac{1}{2}; \frac{bx}{a}\right)}{\sqrt{x}\sqrt{1 - \frac{bx}{a}}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a - b*x)^(3/2)/x^(3/2), x]
```

[Out] $(-2*a*\text{Sqrt}[a - b*x]*\text{Hypergeometric2F1}[-3/2, -1/2, 1/2, (b*x)/a]) / (\text{Sqrt}[x]*\text{Sqrt}[1 - (b*x)/a])$

fricas [A] time = 0.45, size = 109, normalized size = 1.65

$$\left[\frac{3a\sqrt{-b}x \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) - 2(bx + 2a)\sqrt{-bx+a}\sqrt{x}}{2x}, \frac{3a\sqrt{b}x \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right) - (bx + 2a)\sqrt{-bx+a}\sqrt{x}}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+a)^(3/2)/x^(3/2),x, algorithm="fricas")`

[Out] $[1/2*(3*a*\text{sqrt}(-b)*x*\log(-2*b*x + 2*\text{sqrt}(-b*x + a)*\text{sqrt}(-b)*\text{sqrt}(x) + a) - 2*(b*x + 2*a)*\text{sqrt}(-b*x + a)*\text{sqrt}(x))/x, (3*a*\text{sqrt}(b)*x*\arctan(\text{sqrt}(-b*x + a)/(\text{sqrt}(b)*\text{sqrt}(x))) - (b*x + 2*a)*\text{sqrt}(-b*x + a)*\text{sqrt}(x))/x]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+a)^(3/2)/x^(3/2),x, algorithm="giac")`

[Out] Timed out

maple [F] time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{(-bx+a)^{\frac{3}{2}}}{x^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-b*x+a)^(3/2)/x^(3/2),x)`

[Out] `int((-b*x+a)^(3/2)/x^(3/2),x)`

maxima [A] time = 2.85, size = 68, normalized size = 1.03

$$3a\sqrt{b} \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right) - \frac{2\sqrt{-bx+a}a}{\sqrt{x}} - \frac{\sqrt{-bx+a}ab}{\left(b - \frac{bx-a}{x}\right)\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(3/2)/x^(3/2),x, algorithm="maxima")

[Out] $3*a*\sqrt{b}*\arctan(\sqrt{-b*x+a}/(\sqrt{b}*\sqrt{x})) - 2*\sqrt{-b*x+a}*a/\sqrt{x} - \sqrt{-b*x+a}*a*b/((b-(b*x-a)/x)*\sqrt{x})$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a-bx)^{3/2}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - b*x)^(3/2)/x^(3/2), x)

[Out] int((a - b*x)^(3/2)/x^(3/2), x)

sympy [A] time = 2.88, size = 197, normalized size = 2.98

$$\begin{cases} \frac{2ia^{\frac{3}{2}}}{\sqrt{x}\sqrt{-1+\frac{bx}{a}}} - \frac{i\sqrt{a}b\sqrt{x}}{\sqrt{-1+\frac{bx}{a}}} + 3ia\sqrt{b} \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) - \frac{ib^2x^{\frac{3}{2}}}{\sqrt{a}\sqrt{-1+\frac{bx}{a}}} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{2a^{\frac{3}{2}}}{\sqrt{x}\sqrt{1-\frac{bx}{a}}} + \frac{\sqrt{a}b\sqrt{x}}{\sqrt{1-\frac{bx}{a}}} - 3a\sqrt{b} \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) + \frac{b^2x^{\frac{3}{2}}}{\sqrt{a}\sqrt{1-\frac{bx}{a}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)**(3/2)/x**(3/2),x)

[Out] Piecewise((2*I*a**(3/2)/(sqrt(x)*sqrt(-1 + b*x/a)) - I*sqrt(a)*b*sqrt(x)/sqrt(-1 + b*x/a) + 3*I*a*sqrt(b)*acosh(sqrt(b)*sqrt(x)/sqrt(a)) - I*b**2*x**(3/2)/(sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (-2*a**(3/2)/(sqrt(x)*sqrt(1 - b*x/a)) + sqrt(a)*b*sqrt(x)/sqrt(1 - b*x/a) - 3*a*sqrt(b)*asin(sqrt(b)*sqrt(x)/sqrt(a)) + b**2*x**(3/2)/(sqrt(a)*sqrt(1 - b*x/a)), True))

$$3.532 \quad \int \frac{(a-bx)^{3/2}}{x^{5/2}} dx$$

Optimal. Leaf size=67

$$2b^{3/2} \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a-bx}} \right) - \frac{2(a-bx)^{3/2}}{3x^{3/2}} + \frac{2b\sqrt{a-bx}}{\sqrt{x}}$$

[Out] $-2/3*(-b*x+a)^{(3/2)}/x^{(3/2)}+2*b^{(3/2)}*\arctan(b^{(1/2)}*x^{(1/2)}/(-b*x+a)^{(1/2)})+2*b*(-b*x+a)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {47, 63, 217, 203}

$$2b^{3/2} \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a-bx}} \right) - \frac{2(a-bx)^{3/2}}{3x^{3/2}} + \frac{2b\sqrt{a-bx}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[(a - b*x)^(3/2)/x^(5/2), x]

[Out] $(2*b*\text{Sqrt}[a - b*x])/ \text{Sqrt}[x] - (2*(a - b*x)^{(3/2)})/(3*x^{(3/2)}) + 2*b^{(3/2)}* \text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/ \text{Sqrt}[a - b*x]]$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[Rt[b, 2]*x]/Rt
[a, 2])]/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
```


, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a - bx)^{3/2}}{x^{5/2}} dx &= -\frac{2(a - bx)^{3/2}}{3x^{3/2}} - b \int \frac{\sqrt{a - bx}}{x^{3/2}} dx \\
 &= \frac{2b\sqrt{a - bx}}{\sqrt{x}} - \frac{2(a - bx)^{3/2}}{3x^{3/2}} + b^2 \int \frac{1}{\sqrt{x}\sqrt{a - bx}} dx \\
 &= \frac{2b\sqrt{a - bx}}{\sqrt{x}} - \frac{2(a - bx)^{3/2}}{3x^{3/2}} + (2b^2) \text{Subst}\left(\int \frac{1}{\sqrt{a - bx^2}} dx, x, \sqrt{x}\right) \\
 &= \frac{2b\sqrt{a - bx}}{\sqrt{x}} - \frac{2(a - bx)^{3/2}}{3x^{3/2}} + (2b^2) \text{Subst}\left(\int \frac{1}{1 + bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a - bx}}\right) \\
 &= \frac{2b\sqrt{a - bx}}{\sqrt{x}} - \frac{2(a - bx)^{3/2}}{3x^{3/2}} + 2b^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a - bx}}\right)
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 49, normalized size = 0.73

$$\frac{2a\sqrt{a - bx} {}_2F_1\left(-\frac{3}{2}, -\frac{3}{2}; -\frac{1}{2}; \frac{bx}{a}\right)}{3x^{3/2}\sqrt{1 - \frac{bx}{a}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - b*x)^(3/2)/x^(5/2), x]

[Out] (-2*a*Sqrt[a - b*x]*Hypergeometric2F1[-3/2, -3/2, -1/2, (b*x)/a])/(3*x^(3/2)*Sqrt[1 - (b*x)/a])

fricas [A] time = 0.45, size = 115, normalized size = 1.72

$$\left[\frac{3\sqrt{-b}bx^2 \log(-2bx - 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) + 2(4bx - a)\sqrt{-bx+a}\sqrt{x}}{3x^2}, -\frac{2\left(3b^{\frac{3}{2}}x^2 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right) - (4\right)}{3x^2} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(3/2)/x^(5/2),x, algorithm="fricas")

[Out] [1/3*(3*sqrt(-b)*b*x^2*log(-2*b*x - 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) + 2*(4*b*x - a)*sqrt(-b*x + a)*sqrt(x))/x^2, -2/3*(3*b^(3/2)*x^2*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - (4*b*x - a)*sqrt(-b*x + a)*sqrt(x))/x^2]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(3/2)/x^(5/2),x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{(-bx + a)^{\frac{3}{2}}}{x^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+a)^(3/2)/x^(5/2),x)

[Out] int((-b*x+a)^(3/2)/x^(5/2),x)

maxima [A] time = 2.86, size = 49, normalized size = 0.73

$$-2b^{\frac{3}{2}} \arctan\left(\frac{\sqrt{-bx + a}}{\sqrt{b}\sqrt{x}}\right) + \frac{2\sqrt{-bx + a}b}{\sqrt{x}} - \frac{2(-bx + a)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(3/2)/x^(5/2),x, algorithm="maxima")

[Out] -2*b^(3/2)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) + 2*sqrt(-b*x + a)*b/sqrt(x) - 2/3*(-b*x + a)^(3/2)/x^(3/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - bx)^{3/2}}{x^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - b*x)^(3/2)/x^(5/2), x)`

[Out] `int((a - b*x)^(3/2)/x^(5/2), x)`

sympy [C] time = 3.24, size = 187, normalized size = 2.79

$$\left\{ \begin{array}{ll} -\frac{2a\sqrt{b}\sqrt{\frac{a}{bx}-1}}{3x} + \frac{8b^{\frac{3}{2}}\sqrt{\frac{a}{bx}-1}}{3} - 2ib^{\frac{3}{2}}\log\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) + ib^{\frac{3}{2}}\log\left(\frac{a}{bx}\right) + 2b^{\frac{3}{2}}\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) & \text{for } \left|\frac{a}{bx}\right| > 1 \\ -\frac{2ia\sqrt{b}\sqrt{-\frac{a}{bx}+1}}{3x} + \frac{8ib^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}}{3} + ib^{\frac{3}{2}}\log\left(\frac{a}{bx}\right) - 2ib^{\frac{3}{2}}\log\left(\sqrt{-\frac{a}{bx}+1} + 1\right) & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+a)**(3/2)/x**(5/2), x)`

[Out] `Piecewise((-2*a*sqrt(b)*sqrt(a/(b*x) - 1)/(3*x) + 8*b**(3/2)*sqrt(a/(b*x) - 1)/3 - 2*I*b**(3/2)*log(sqrt(a)/(sqrt(b)*sqrt(x))) + I*b**(3/2)*log(a/(b*x)) + 2*b**(3/2)*asin(sqrt(b)*sqrt(x)/sqrt(a)), Abs(a/(b*x)) > 1), (-2*I*a*sqrt(b)*sqrt(-a/(b*x) + 1)/(3*x) + 8*I*b**(3/2)*sqrt(-a/(b*x) + 1)/3 + I*b**(3/2)*log(a/(b*x)) - 2*I*b**(3/2)*log(sqrt(-a/(b*x) + 1) + 1), True))`

3.533 $\int x^{5/2}(2 + bx)^{3/2} dx$

Optimal. Leaf size=126

$$-\frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}} + \frac{3\sqrt{x}\sqrt{bx+2}}{8b^3} - \frac{x^{3/2}\sqrt{bx+2}}{8b^2} + \frac{1}{5}x^{7/2}(bx+2)^{3/2} + \frac{3}{20}x^{7/2}\sqrt{bx+2} + \frac{x^{5/2}\sqrt{bx+2}}{20b}$$

[Out] $1/5*x^{(7/2)}*(b*x+2)^{(3/2)}-3/4*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(7/2)}-1/8*x^{(3/2)}*(b*x+2)^{(1/2)}/b^2+1/20*x^{(5/2)}*(b*x+2)^{(1/2)}/b+3/20*x^{(7/2)}*(b*x+2)^{(1/2)}+3/8*x^{(1/2)}*(b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.03, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{x^{3/2}\sqrt{bx+2}}{8b^2} + \frac{3\sqrt{x}\sqrt{bx+2}}{8b^3} - \frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}} + \frac{1}{5}x^{7/2}(bx+2)^{3/2} + \frac{3}{20}x^{7/2}\sqrt{bx+2} + \frac{x^{5/2}\sqrt{bx+2}}{20b}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(5/2)}*(2 + b*x)^{(3/2)}, x]$

[Out] $(3*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/(8*b^3) - (x^{(3/2)}*\operatorname{Sqrt}[2 + b*x])/(8*b^2) + (x^{(5/2)}*\operatorname{Sqrt}[2 + b*x])/(20*b) + (3*x^{(7/2)}*\operatorname{Sqrt}[2 + b*x])/20 + (x^{(7/2)}*(2 + b*x)^{(3/2)})/5 - (3*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]])/(4*b^{(7/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned}
\int x^{5/2}(2+bx)^{3/2} dx &= \frac{1}{5}x^{7/2}(2+bx)^{3/2} + \frac{3}{5} \int x^{5/2}\sqrt{2+bx} dx \\
&= \frac{3}{20}x^{7/2}\sqrt{2+bx} + \frac{1}{5}x^{7/2}(2+bx)^{3/2} + \frac{3}{20} \int \frac{x^{5/2}}{\sqrt{2+bx}} dx \\
&= \frac{x^{5/2}\sqrt{2+bx}}{20b} + \frac{3}{20}x^{7/2}\sqrt{2+bx} + \frac{1}{5}x^{7/2}(2+bx)^{3/2} - \frac{\int \frac{x^{3/2}}{\sqrt{2+bx}} dx}{4b} \\
&= -\frac{x^{3/2}\sqrt{2+bx}}{8b^2} + \frac{x^{5/2}\sqrt{2+bx}}{20b} + \frac{3}{20}x^{7/2}\sqrt{2+bx} + \frac{1}{5}x^{7/2}(2+bx)^{3/2} + \frac{3 \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx}{8b^2} \\
&= \frac{3\sqrt{x}\sqrt{2+bx}}{8b^3} - \frac{x^{3/2}\sqrt{2+bx}}{8b^2} + \frac{x^{5/2}\sqrt{2+bx}}{20b} + \frac{3}{20}x^{7/2}\sqrt{2+bx} + \frac{1}{5}x^{7/2}(2+bx)^{3/2} - \frac{3 \int \sqrt{x}}{8b^2} \\
&= \frac{3\sqrt{x}\sqrt{2+bx}}{8b^3} - \frac{x^{3/2}\sqrt{2+bx}}{8b^2} + \frac{x^{5/2}\sqrt{2+bx}}{20b} + \frac{3}{20}x^{7/2}\sqrt{2+bx} + \frac{1}{5}x^{7/2}(2+bx)^{3/2} - \frac{3 \int \sqrt{x}}{8b^2} \\
&= \frac{3\sqrt{x}\sqrt{2+bx}}{8b^3} - \frac{x^{3/2}\sqrt{2+bx}}{8b^2} + \frac{x^{5/2}\sqrt{2+bx}}{20b} + \frac{3}{20}x^{7/2}\sqrt{2+bx} + \frac{1}{5}x^{7/2}(2+bx)^{3/2} - \frac{3 \int \sqrt{x}}{8b^2}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 78, normalized size = 0.62

$$\frac{\sqrt{x}\sqrt{bx+2}(8b^4x^4+22b^3x^3+2b^2x^2-5bx+15)}{40b^3} - \frac{3\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*(2+b*x)^(3/2),x]

[Out] (Sqrt[x]*Sqrt[2+b*x]*(15-5*b*x+2*b^2*x^2+22*b^3*x^3+8*b^4*x^4))/(40*b^3)-(3*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(4*b^(7/2))

fricas [A] time = 0.44, size = 156, normalized size = 1.24

$$\left[\frac{(8b^5x^4+22b^4x^3+2b^3x^2-5b^2x+15b)\sqrt{bx+2}\sqrt{x}+15\sqrt{b}\log(bx-\sqrt{bx+2}\sqrt{b}\sqrt{x}+1)}{40b^4}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(5/2)*(b*x+2)^(3/2),x, algorithm="fricas")
```

```
[Out] [1/40*((8*b^5*x^4 + 22*b^4*x^3 + 2*b^3*x^2 - 5*b^2*x + 15*b)*sqrt(b*x + 2)*
sqrt(x) + 15*sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^4, 1/4
0*((8*b^5*x^4 + 22*b^4*x^3 + 2*b^3*x^2 - 5*b^2*x + 15*b)*sqrt(b*x + 2)*sqrt
(x) + 30*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))))/b^4]
```

```
giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00
```

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(5/2)*(b*x+2)^(3/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warni
ng, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}
+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,
[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+
%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,
[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}
+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,
[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,
4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%
{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[
3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}
+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%
{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,
2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [82.7280518
371,8.05231268331]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1
,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}
+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,
2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+
%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[
2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}
+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-3
2,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]
%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%
{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2
,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}
+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-
8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parame
ters values [64.3995612673,28.4266860783]Warning, choosing root of [1,0,%%
{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2
,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%
{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,
```


{-20, [3, 2]%%}+%%{20, [3, 1]%%}+%%{-8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{-4, [1, 4]%%}+%%{20, [1, 3]%%}+%%{-40, [1, 2]%%}+%%{48, [1, 1]%%}+%%{-32, [1, 0]%%}+%%{1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{16, [0, 0]%%}] at parameters values [88.2886286299, 17.6881634681] $1/b*(2*b^2*abs(b)/b^2*(2*((((5040*b^19/100800/b^23*sqrt(b*x+2)*sqrt(b*x+2)-51660*b^19/100800/b^23)*sqrt(b*x+2)*sqrt(b*x+2)+215460*b^19/100800/b^23)*sqrt(b*x+2)*sqrt(b*x+2)-469350*b^19/100800/b^23)*sqrt(b*x+2)*sqrt(b*x+2)+607950*b^19/100800/b^23)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)+63/8/b^3/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))+8*b*abs(b)/b^2*(2*((((90*b^11/1440/b^14*sqrt(b*x+2)*sqrt(b*x+2)-750*b^11/1440/b^14)*sqrt(b*x+2)*sqrt(b*x+2)+2445*b^11/1440/b^14)*sqrt(b*x+2)*sqrt(b*x+2)-4185*b^11/1440/b^14)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)-35/8/b^2/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))+8*abs(b)/b^2*(2*((12*b^5/144/b^7*sqrt(b*x+2)*sqrt(b*x+2)-78*b^5/144/b^7)*sqrt(b*x+2)*sqrt(b*x+2)+198*b^5/144/b^7)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)+5/2/b/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))))$

maple [A] time = 0.01, size = 123, normalized size = 0.98

$$\frac{(bx+2)^{\frac{5}{2}}x^{\frac{5}{2}}}{5b} - \frac{(bx+2)^{\frac{5}{2}}x^{\frac{3}{2}}}{4b^2} + \frac{(bx+2)^{\frac{5}{2}}\sqrt{x}}{4b^3} - \frac{(bx+2)^{\frac{3}{2}}\sqrt{x}}{8b^3} - \frac{3\sqrt{bx+2}\sqrt{x}}{8b^3} - \frac{3\sqrt{(bx+2)x}\ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{8\sqrt{bx+2}b^{\frac{7}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{(5/2)}*(b*x+2)^{(3/2)}, x)$

[Out] $1/5/b*x^{(5/2)}*(b*x+2)^{(5/2)}-1/4/b^2*x^{(3/2)}*(b*x+2)^{(5/2)}+1/4/b^3*x^{(1/2)}*(b*x+2)^{(5/2)}-1/8*(b*x+2)^{(3/2)}/b^3*x^{(1/2)}-3/8*(b*x+2)^{(1/2)}/b^3*x^{(1/2)}-3/8*((b*x+2)*x)^{(1/2)}/(b*x+2)^{(1/2)}/b^{(7/2)}/x^{(1/2)}*\ln((b*x+1)/b^{(1/2)}+(b*x^2+2*x)^{(1/2)})$

maxima [B] time = 2.99, size = 194, normalized size = 1.54

$$\frac{\frac{15\sqrt{bx+2}b^4}{\sqrt{x}} - \frac{70(bx+2)^{\frac{3}{2}}b^3}{x^2} - \frac{128(bx+2)^{\frac{5}{2}}b^2}{x^2} + \frac{70(bx+2)^{\frac{7}{2}}b}{x^2} - \frac{15(bx+2)^{\frac{9}{2}}}{x^2}}{20\left(b^8 - \frac{5(bx+2)b^7}{x} + \frac{10(bx+2)^2b^6}{x^2} - \frac{10(bx+2)^3b^5}{x^3} + \frac{5(bx+2)^4b^4}{x^4} - \frac{(bx+2)^5b^3}{x^5}\right)} + \frac{3\log\left(-\frac{\sqrt{b}-\sqrt{bx+2}}{\sqrt{x}}\right)}{8b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{(5/2)}*(b*x+2)^{(3/2)}, x, \text{algorithm}=\text{"maxima"})$

[Out] $1/20*(15*sqrt(b*x+2)*b^4/sqrt(x) - 70*(b*x+2)^{(3/2)}*b^3/x^{(3/2)} - 128*(b*x+2)^{(5/2)}*b^2/x^{(5/2)} + 70*(b*x+2)^{(7/2)}*b/x^{(7/2)} - 15*(b*x+2)^{(9/2)})$

$/2)/x^{(9/2)})/(b^8 - 5*(b*x + 2)*b^7/x + 10*(b*x + 2)^2*b^6/x^2 - 10*(b*x + 2)^3*b^5/x^3 + 5*(b*x + 2)^4*b^4/x^4 - (b*x + 2)^5*b^3/x^5) + 3/8*\log(-(\sqrt{t(b) - \sqrt{b*x + 2}}/\sqrt{t(x)})/(\sqrt{t(b) + \sqrt{b*x + 2}}/\sqrt{t(x)}))/b^{(7/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} (bx + 2)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(b*x + 2)^(3/2), x)

[Out] int(x^(5/2)*(b*x + 2)^(3/2), x)

sympy [A] time = 15.67, size = 136, normalized size = 1.08

$$\frac{b^2 x^{\frac{11}{2}}}{5\sqrt{bx+2}} + \frac{19bx^{\frac{9}{2}}}{20\sqrt{bx+2}} + \frac{23x^{\frac{7}{2}}}{20\sqrt{bx+2}} - \frac{x^{\frac{5}{2}}}{40b\sqrt{bx+2}} + \frac{x^{\frac{3}{2}}}{8b^2\sqrt{bx+2}} + \frac{3\sqrt{x}}{4b^3\sqrt{bx+2}} - \frac{3 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)*(b*x+2)**(3/2), x)

[Out] $b**2*x**(11/2)/(5*\sqrt{b*x + 2}) + 19*b*x**(9/2)/(20*\sqrt{b*x + 2}) + 23*x** (7/2)/(20*\sqrt{b*x + 2}) - x**(5/2)/(40*b*\sqrt{b*x + 2}) + x**(3/2)/(8*b** 2*\sqrt{b*x + 2}) + 3*\sqrt{x}/(4*b**3*\sqrt{b*x + 2}) - 3*asinh(\sqrt{2}*\sqrt{b}*\sqrt{x}*(b)*\sqrt{x}/2)/(4*b**(7/2))$

3.534 $\int x^{3/2}(2 + bx)^{3/2} dx$

Optimal. Leaf size=105

$$\frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} - \frac{3\sqrt{x}\sqrt{bx+2}}{8b^2} + \frac{1}{4}x^{5/2}(bx+2)^{3/2} + \frac{1}{4}x^{5/2}\sqrt{bx+2} + \frac{x^{3/2}\sqrt{bx+2}}{8b}$$

[Out] $1/4*x^{(5/2)}*(b*x+2)^{(3/2)}+3/4*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(5/2)}+1/8*x^{(3/2)}*(b*x+2)^{(1/2)}/b+1/4*x^{(5/2)}*(b*x+2)^{(1/2)}-3/8*x^{(1/2)}*(b*x+2)^{(1/2)}/b^2$

Rubi [A] time = 0.03, antiderivative size = 105, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{3\sqrt{x}\sqrt{bx+2}}{8b^2} + \frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} + \frac{1}{4}x^{5/2}(bx+2)^{3/2} + \frac{1}{4}x^{5/2}\sqrt{bx+2} + \frac{x^{3/2}\sqrt{bx+2}}{8b}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(3/2)}*(2 + b*x)^{(3/2)}, x]$

[Out] $(-3*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/(8*b^2) + (x^{(3/2)}*\operatorname{Sqrt}[2 + b*x])/(8*b) + (x^{(5/2)}*\operatorname{Sqrt}[2 + b*x])/4 + (x^{(5/2)}*(2 + b*x)^{(3/2)})/4 + (3*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]])/(4*b^{(5/2)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{NeQ}[m + n + 1, 0]$ && $!(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] \mid\mid (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m - n, 0])))$ && $!\operatorname{ILtQ}[m + n + 2, 0]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 54

$\operatorname{Int}[1/(\operatorname{Sqrt}[(a_.) + (b_.)*(x_.)]*\operatorname{Sqrt}[(c_.) + (d_.)*(x_.)]), x_Symbol] \rightarrow \operatorname{Dist}[2/\operatorname{Sqrt}[b], \operatorname{Subst}[\operatorname{Int}[1/\operatorname{Sqrt}[b*c - a*d + d*x^2], x], x, \operatorname{Sqrt}[a + b*x]], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{GtQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[b, 0]$

Rule 215

$\operatorname{Int}[1/\operatorname{Sqrt}[(a_.) + (b_.)*(x_.)^2], x_Symbol] \rightarrow \operatorname{Simp}[\operatorname{ArcSinh}[(\operatorname{Rt}[b, 2]*x)/\operatorname{Sqrt}[a]]/\operatorname{Rt}[b, 2], x] /;$ $\operatorname{FreeQ}\{a, b\}, x$ && $\operatorname{GtQ}[a, 0]$ && $\operatorname{PosQ}[b]$

Rubi steps

$$\begin{aligned}
\int x^{3/2}(2+bx)^{3/2} dx &= \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{3}{4} \int x^{3/2}\sqrt{2+bx} dx \\
&= \frac{1}{4}x^{5/2}\sqrt{2+bx} + \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{1}{4} \int \frac{x^{3/2}}{\sqrt{2+bx}} dx \\
&= \frac{x^{3/2}\sqrt{2+bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2+bx} + \frac{1}{4}x^{5/2}(2+bx)^{3/2} - \frac{3 \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx}{8b} \\
&= -\frac{3\sqrt{x}\sqrt{2+bx}}{8b^2} + \frac{x^{3/2}\sqrt{2+bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2+bx} + \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{3 \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx}{8b^2} \\
&= -\frac{3\sqrt{x}\sqrt{2+bx}}{8b^2} + \frac{x^{3/2}\sqrt{2+bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2+bx} + \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{3 \text{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx\right)}{4b^2} \\
&= -\frac{3\sqrt{x}\sqrt{2+bx}}{8b^2} + \frac{x^{3/2}\sqrt{2+bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2+bx} + \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 70, normalized size = 0.67

$$\frac{\sqrt{b}\sqrt{x}\sqrt{bx+2}(2b^3x^3+6b^2x^2+bx-3)+6\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{8b^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*(2 + b*x)^(3/2), x]

[Out] (Sqrt[b]*Sqrt[x]*Sqrt[2 + b*x]*(-3 + b*x + 6*b^2*x^2 + 2*b^3*x^3) + 6*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(8*b^(5/2))

fricas [A] time = 0.45, size = 137, normalized size = 1.30

$$\left[\frac{(2b^4x^3 + 6b^3x^2 + b^2x - 3b)\sqrt{bx+2}\sqrt{x} + 3\sqrt{b}\log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{8b^3}, \frac{(2b^4x^3 + 6b^3x^2 + b^2x - 3b)}{8b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+2)^(3/2), x, algorithm="fricas")

[Out] [1/8*((2*b^4*x^3 + 6*b^3*x^2 + b^2*x - 3*b)*sqrt(b*x + 2)*sqrt(x) + 3*sqrt(b)*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^3, 1/8*((2*b^4*x^3 + 6*b

$$\frac{\sqrt{3x^2 + b^2x - 3b} \sqrt{bx + 2} \sqrt{x} - 6 \sqrt{-b} \arctan(\sqrt{bx + 2} \sqrt{-b} / (b \sqrt{x}))}{b^3}$$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+2)^(3/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [82.7280518371,8.05231268331]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [64.3995612673,28.4266860783]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6

0]%%}] at parameters values [88.2886286299,17.6881634681]1/b*(2*b^2*abs(b)/b^2*(2*((90*b^11/1440/b^14*sqrt(b*x+2)*sqrt(b*x+2)-750*b^11/1440/b^14)*sqrt(b*x+2)*sqrt(b*x+2)+2445*b^11/1440/b^14)*sqrt(b*x+2)*sqrt(b*x+2)-4185*b^11/1440/b^14)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)-35/8/b^2/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))+8*b*abs(b)/b^2*(2*((12*b^5/144/b^7*sqrt(b*x+2)*sqrt(b*x+2)-78*b^5/144/b^7)*sqrt(b*x+2)*sqrt(b*x+2)+198*b^5/144/b^7)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)+5/2/b/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))+8*abs(b)/b^2/b*(2*(1/8*sqrt(b*x+2)*sqrt(b*x+2)-5/8)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)-6*b/4/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))))

maple [A] time = 0.00, size = 108, normalized size = 1.03

$$\frac{(bx+2)^{\frac{5}{2}}x^{\frac{3}{2}}}{4b} - \frac{(bx+2)^{\frac{5}{2}}\sqrt{x}}{4b^2} + \frac{(bx+2)^{\frac{3}{2}}\sqrt{x}}{8b^2} + \frac{3\sqrt{bx+2}\sqrt{x}}{8b^2} + \frac{3\sqrt{(bx+2)x}\ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{8\sqrt{bx+2}b^{\frac{5}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(b*x+2)^(3/2),x)

[Out] 1/4/b*x^(3/2)*(b*x+2)^(5/2)-1/4/b^2*x^(1/2)*(b*x+2)^(5/2)+1/8*(b*x+2)^(3/2)/b^2*x^(1/2)+3/8*(b*x+2)^(1/2)/b^2*x^(1/2)+3/8*((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)/b^(5/2)/x^(1/2)*ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))

maxima [B] time = 3.04, size = 163, normalized size = 1.55

$$-\frac{\frac{3\sqrt{bx+2}b^3}{\sqrt{x}} - \frac{11(bx+2)^{\frac{3}{2}}b^2}{x^{\frac{3}{2}}} - \frac{11(bx+2)^{\frac{5}{2}}b}{x^{\frac{5}{2}}} + \frac{3(bx+2)^{\frac{7}{2}}}{x^{\frac{7}{2}}}}{4\left(b^6 - \frac{4(bx+2)b^5}{x} + \frac{6(bx+2)^2b^4}{x^2} - \frac{4(bx+2)^3b^3}{x^3} + \frac{(bx+2)^4b^2}{x^4}\right)} - \frac{3\log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{8b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+2)^(3/2),x, algorithm="maxima")

[Out] -1/4*(3*sqrt(b*x + 2)*b^3/sqrt(x) - 11*(b*x + 2)^(3/2)*b^2/x^(3/2) - 11*(b*x + 2)^(5/2)*b/x^(5/2) + 3*(b*x + 2)^(7/2)/x^(7/2))/(b^6 - 4*(b*x + 2)*b^5/x + 6*(b*x + 2)^2*b^4/x^2 - 4*(b*x + 2)^3*b^3/x^3 + (b*x + 2)^4*b^2/x^4) - 3/8*log(-(sqrt(b) - sqrt(b*x + 2)/sqrt(x))/(sqrt(b) + sqrt(b*x + 2)/sqrt(x)))/b^(5/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} (bx + 2)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)*(b*x + 2)^(3/2), x)`

[Out] `int(x^(3/2)*(b*x + 2)^(3/2), x)`

sympy [A] time = 7.86, size = 117, normalized size = 1.11

$$\frac{b^2 x^{\frac{9}{2}}}{4\sqrt{bx+2}} + \frac{5bx^{\frac{7}{2}}}{4\sqrt{bx+2}} + \frac{13x^{\frac{5}{2}}}{8\sqrt{bx+2}} - \frac{x^{\frac{3}{2}}}{8b\sqrt{bx+2}} - \frac{3\sqrt{x}}{4b^2\sqrt{bx+2}} + \frac{3 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)*(b*x+2)**(3/2), x)`

[Out] `b**2*x**(9/2)/(4*sqrt(b*x + 2)) + 5*b*x**(7/2)/(4*sqrt(b*x + 2)) + 13*x**(5/2)/(8*sqrt(b*x + 2)) - x**(3/2)/(8*b*sqrt(b*x + 2)) - 3*sqrt(x)/(4*b**2*sqrt(b*x + 2)) + 3*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(5/2))`

3.535 $\int \sqrt{x} (2 + bx)^{3/2} dx$

Optimal. Leaf size=82

$$-\frac{\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} + \frac{1}{3}x^{3/2}(bx+2)^{3/2} + \frac{1}{2}x^{3/2}\sqrt{bx+2} + \frac{\sqrt{x}\sqrt{bx+2}}{2b}$$

[Out] $1/3*x^{(3/2)}*(b*x+2)^{(3/2)}-\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)*2^{(1/2)}})/b^{(3/2)}+1/2*x^{(3/2)}*(b*x+2)^{(1/2)}+1/2*x^{(1/2)}*(b*x+2)^{(1/2)}/b$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} + \frac{1}{3}x^{3/2}(bx+2)^{3/2} + \frac{1}{2}x^{3/2}\sqrt{bx+2} + \frac{\sqrt{x}\sqrt{bx+2}}{2b}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[x]*(2 + b*x)^(3/2), x]`

[Out] $(\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/(2*b) + (x^{(3/2)}*\operatorname{Sqrt}[2 + b*x])/2 + (x^{(3/2)}*(2 + b*x)^{(3/2)})/3 - \operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]]/b^{(3/2)}$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```


Rubi steps

$$\begin{aligned}
\int \sqrt{x} (2 + bx)^{3/2} dx &= \frac{1}{3} x^{3/2} (2 + bx)^{3/2} + \int \sqrt{x} \sqrt{2 + bx} dx \\
&= \frac{1}{2} x^{3/2} \sqrt{2 + bx} + \frac{1}{3} x^{3/2} (2 + bx)^{3/2} + \frac{1}{2} \int \frac{\sqrt{x}}{\sqrt{2 + bx}} dx \\
&= \frac{\sqrt{x} \sqrt{2 + bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2 + bx} + \frac{1}{3} x^{3/2} (2 + bx)^{3/2} - \frac{\int \frac{1}{\sqrt{x} \sqrt{2 + bx}} dx}{2b} \\
&= \frac{\sqrt{x} \sqrt{2 + bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2 + bx} + \frac{1}{3} x^{3/2} (2 + bx)^{3/2} - \frac{\text{Subst}\left(\int \frac{1}{\sqrt{2 + bx^2}} dx, x, \sqrt{x}\right)}{b} \\
&= \frac{\sqrt{x} \sqrt{2 + bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2 + bx} + \frac{1}{3} x^{3/2} (2 + bx)^{3/2} - \frac{\sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 60, normalized size = 0.73

$$\frac{\sqrt{x} \sqrt{bx + 2} (2b^2x^2 + 7bx + 3)}{6b} - \frac{\sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*(2 + b*x)^(3/2), x]

[Out] (Sqrt[x]*Sqrt[2 + b*x]*(3 + 7*b*x + 2*b^2*x^2))/(6*b) - ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]]/b^(3/2)

fricas [A] time = 0.45, size = 124, normalized size = 1.51

$$\left[\frac{(2b^3x^2 + 7b^2x + 3b)\sqrt{bx + 2}\sqrt{x} + 3\sqrt{b} \log(bx - \sqrt{bx + 2}\sqrt{b}\sqrt{x} + 1)}{6b^2}, \frac{(2b^3x^2 + 7b^2x + 3b)\sqrt{bx + 2}\sqrt{x} + 3\sqrt{b} \log(bx - \sqrt{bx + 2}\sqrt{b}\sqrt{x} + 1)}{6b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(3/2)*x^(1/2), x, algorithm="fricas")

[Out] [1/6*((2*b^3*x^2 + 7*b^2*x + 3*b)*sqrt(b*x + 2)*sqrt(x) + 3*sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^2, 1/6*((2*b^3*x^2 + 7*b^2*x + 3*b)*sqrt(b*x + 2)*sqrt(x) + 6*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))))/b^2]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(3/2)*x^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of $[1, 0, \{-4, [1, 1]\} + \{-4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{4, [1, 2]\} + \{28, [1, 1]\} + \{8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{-4, [3, 3]\} + \{4, [3, 2]\} + \{4, [3, 1]\} + \{-4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{4, [1, 3]\} + \{20, [1, 2]\} + \{-128, [1, 1]\} + \{16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{-4, [3, 4]\} + \{12, [3, 3]\} + \{-20, [3, 2]\} + \{20, [3, 1]\} + \{-8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{-4, [1, 4]\} + \{20, [1, 3]\} + \{-40, [1, 2]\} + \{48, [1, 1]\} + \{-32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values [82.7280518371, 8.05231268331] Warning, choosing root of $[1, 0, \{-4, [1, 1]\} + \{-4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{4, [1, 2]\} + \{28, [1, 1]\} + \{8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{-4, [3, 3]\} + \{4, [3, 2]\} + \{4, [3, 1]\} + \{-4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{4, [1, 3]\} + \{20, [1, 2]\} + \{-128, [1, 1]\} + \{16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{-4, [3, 4]\} + \{12, [3, 3]\} + \{-20, [3, 2]\} + \{20, [3, 1]\} + \{-8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{-4, [1, 4]\} + \{20, [1, 3]\} + \{-40, [1, 2]\} + \{48, [1, 1]\} + \{-32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values [64.3995612673, 28.4266860783] Warning, choosing root of $[1, 0, \{-4, [1, 1]\} + \{-4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{4, [1, 2]\} + \{28, [1, 1]\} + \{8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{-4, [3, 3]\} + \{4, [3, 2]\} + \{4, [3, 1]\} + \{-4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{4, [1, 3]\} + \{20, [1, 2]\} + \{-128, [1, 1]\} + \{16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{-4, [3, 4]\} + \{12, [3, 3]\} + \{-20, [3, 2]\} + \{20, [3, 1]\} + \{-8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{-4, [1, 4]\} + \{20, [1, 3]\} + \{-40, [1, 2]\} + \{48, [1, 1]\} + \{-32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$

$-20, [2, 3] \} + \{46, [2, 2] \} + \{-40, [2, 1] \} + \{24, [2, 0] \} + \{-4, [1, 4] \} + \{20, [1, 3] \} + \{-40, [1, 2] \} + \{48, [1, 1] \} + \{-32, [1, 0] \} + \{1, [0, 4] \} + \{-8, [0, 3] \} + \{24, [0, 2] \} + \{-32, [0, 1] \} + \{16, [0, 0] \}$ at parameters values [39.1803401988, 96.7771189027] Warning, choosing root of $[1, 0, \{-4, [1, 1] \} + \{-4, [1, 0] \} + \{-4, [0, 1] \} + \{-8, [0, 0] \}, 0, \{6, [2, 2] \} + \{4, [2, 1] \} + \{6, [2, 0] \} + \{4, [1, 2] \} + \{28, [1, 1] \} + \{8, [1, 0] \} + \{6, [0, 2] \} + \{8, [0, 1] \} + \{24, [0, 0] \}, 0, \{-4, [3, 3] \} + \{4, [3, 2] \} + \{4, [3, 1] \} + \{-4, [3, 0] \} + \{4, [2, 3] \} + \{-64, [2, 2] \} + \{20, [2, 1] \} + \{8, [2, 0] \} + \{4, [1, 3] \} + \{20, [1, 2] \} + \{-128, [1, 1] \} + \{16, [1, 0] \} + \{-4, [0, 3] \} + \{8, [0, 2] \} + \{16, [0, 1] \} + \{-32, [0, 0] \}, 0, \{1, [4, 4] \} + \{-4, [4, 3] \} + \{6, [4, 2] \} + \{-4, [4, 1] \} + \{1, [4, 0] \} + \{-4, [3, 4] \} + \{12, [3, 3] \} + \{-20, [3, 2] \} + \{20, [3, 1] \} + \{-8, [3, 0] \} + \{6, [2, 4] \} + \{-20, [2, 3] \} + \{46, [2, 2] \} + \{-40, [2, 1] \} + \{24, [2, 0] \} + \{-4, [1, 4] \} + \{20, [1, 3] \} + \{-40, [1, 2] \} + \{48, [1, 1] \} + \{-32, [1, 0] \} + \{1, [0, 4] \} + \{-8, [0, 3] \} + \{24, [0, 2] \} + \{-32, [0, 1] \} + \{16, [0, 0] \}$ at parameters values [95.5969694792, 66.1769613782] Warning, choosing root of $[1, 0, \{-4, [1, 1] \} + \{-4, [1, 0] \} + \{-4, [0, 1] \} + \{-8, [0, 0] \}, 0, \{6, [2, 2] \} + \{4, [2, 1] \} + \{6, [2, 0] \} + \{4, [1, 2] \} + \{28, [1, 1] \} + \{8, [1, 0] \} + \{6, [0, 2] \} + \{8, [0, 1] \} + \{24, [0, 0] \}, 0, \{-4, [3, 3] \} + \{4, [3, 2] \} + \{4, [3, 1] \} + \{-4, [3, 0] \} + \{4, [2, 3] \} + \{-64, [2, 2] \} + \{20, [2, 1] \} + \{8, [2, 0] \} + \{4, [1, 3] \} + \{20, [1, 2] \} + \{-128, [1, 1] \} + \{16, [1, 0] \} + \{-4, [0, 3] \} + \{8, [0, 2] \} + \{16, [0, 1] \} + \{-32, [0, 0] \}, 0, \{1, [4, 4] \} + \{-4, [4, 3] \} + \{6, [4, 2] \} + \{-4, [4, 1] \} + \{1, [4, 0] \} + \{-4, [3, 4] \} + \{12, [3, 3] \} + \{-20, [3, 2] \} + \{20, [3, 1] \} + \{-8, [3, 0] \} + \{6, [2, 4] \} + \{-20, [2, 3] \} + \{46, [2, 2] \} + \{-40, [2, 1] \} + \{24, [2, 0] \} + \{-4, [1, 4] \} + \{20, [1, 3] \} + \{-40, [1, 2] \} + \{48, [1, 1] \} + \{-32, [1, 0] \} + \{1, [0, 4] \} + \{-8, [0, 3] \} + \{24, [0, 2] \} + \{-32, [0, 1] \} + \{16, [0, 0] \}$ at parameters values [39.9828299829, 94.1262030317] Warning, choosing root of $[1, 0, \{-4, [1, 1] \} + \{-4, [1, 0] \} + \{-4, [0, 1] \} + \{-8, [0, 0] \}, 0, \{6, [2, 2] \} + \{4, [2, 1] \} + \{6, [2, 0] \} + \{4, [1, 2] \} + \{28, [1, 1] \} + \{8, [1, 0] \} + \{6, [0, 2] \} + \{8, [0, 1] \} + \{24, [0, 0] \}, 0, \{-4, [3, 3] \} + \{4, [3, 2] \} + \{4, [3, 1] \} + \{-4, [3, 0] \} + \{4, [2, 3] \} + \{-64, [2, 2] \} + \{20, [2, 1] \} + \{8, [2, 0] \} + \{4, [1, 3] \} + \{20, [1, 2] \} + \{-128, [1, 1] \} + \{16, [1, 0] \} + \{-4, [0, 3] \} + \{8, [0, 2] \} + \{16, [0, 1] \} + \{-32, [0, 0] \}, 0, \{1, [4, 4] \} + \{-4, [4, 3] \} + \{6, [4, 2] \} + \{-4, [4, 1] \} + \{1, [4, 0] \} + \{-4, [3, 4] \} + \{12, [3, 3] \} + \{-20, [3, 2] \} + \{20, [3, 1] \} + \{-8, [3, 0] \} + \{6, [2, 4] \} + \{-20, [2, 3] \} + \{46, [2, 2] \} + \{-40, [2, 1] \} + \{24, [2, 0] \} + \{-4, [1, 4] \} + \{20, [1, 3] \} + \{-40, [1, 2] \} + \{48, [1, 1] \} + \{-32, [1, 0] \} + \{1, [0, 4] \} + \{-8, [0, 3] \} + \{24, [0, 2] \} + \{-32, [0, 1] \} + \{16, [0, 0] \}$ at parameters values [88.2886286299, 17.6881634681] $1/b * (2*b^2*abs(b)/b^2 * (2*((12*b^5/144/b^7*sqrt(b*x+2)*sqrt(b*x+2) - 78*b^5/144/b^7)*sqrt(b*x+2$

) $\sqrt{bx+2}$ +198 $b^5/144/b^7$) $\sqrt{bx+2}$) $\sqrt{b(bx+2)-2b}$ +5/2/b/ \sqrt{b}) $\ln(\text{abs}(\sqrt{b(bx+2)-2b}-\sqrt{b})\sqrt{bx+2}))$ +8 $b\text{abs}(b)/b^2/b(2*(1/8\sqrt{bx+2})\sqrt{bx+2}-5/8)\sqrt{bx+2})\sqrt{b(bx+2)-2b}$ -6 $b/4/\sqrt{b}$) $\ln(\text{abs}(\sqrt{b(bx+2)-2b}-\sqrt{b})\sqrt{bx+2}))$ +8 $\text{abs}(b)/b^2*(1/2\sqrt{bx+2})\sqrt{b(bx+2)-2b}+2b/2/\sqrt{b})\ln(\text{abs}(\sqrt{b(bx+2)-2b}-\sqrt{b})\sqrt{bx+2}))$)

maple [A] time = 0.00, size = 87, normalized size = 1.06

$$\frac{(bx+2)^{\frac{3}{2}}x^{\frac{3}{2}}}{3} + \frac{\sqrt{bx+2}x^{\frac{3}{2}}}{2} + \frac{\sqrt{bx+2}\sqrt{x}}{2b} - \frac{\sqrt{bx+2}x \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{2\sqrt{bx+2}b^{\frac{3}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((bx+2)^{(3/2)}x^{(1/2)}, x)$

[Out] $1/3x^{(3/2)}(bx+2)^{(3/2)}+1/2(bx+2)^{(1/2)}x^{(3/2)}+1/2(bx+2)^{(1/2)}/bx^{(1/2)}-1/2((bx+2)x)^{(1/2)}/(bx+2)^{(1/2)}/b^{(3/2)}/x^{(1/2)}*\ln((bx+1)/b^{(1/2)}+(bx^2+2x)^{(1/2)})$

maxima [B] time = 2.99, size = 132, normalized size = 1.61

$$\frac{\frac{3\sqrt{bx+2}b^2}{\sqrt{x}} - \frac{8(bx+2)^{\frac{3}{2}}b}{x^2} - \frac{3(bx+2)^{\frac{5}{2}}}{x^2}}{3\left(b^4 - \frac{3(bx+2)b^3}{x} + \frac{3(bx+2)^2b^2}{x^2} - \frac{(bx+2)^3b}{x^3}\right)} + \frac{\log\left(\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{2b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((bx+2)^{(3/2)}x^{(1/2)}, x, \text{algorithm}="maxima")$

[Out] $1/3*(3*\sqrt{bx+2}*b^2/\sqrt{x} - 8*(bx+2)^{(3/2)}*b/x^{(3/2)} - 3*(bx+2)^{(5/2)}/x^{(5/2)})/(b^4 - 3*(bx+2)*b^3/x + 3*(bx+2)^2*b^2/x^2 - (bx+2)^3*b/x^3) + 1/2*\log(-(\sqrt{b} - \sqrt{bx+2})/\sqrt{x})/(\sqrt{b} + \sqrt{bx+2})/\sqrt{x})/b^{(3/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{x} (bx+2)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{(1/2)}*(bx+2)^{(3/2)}, x)$

[Out] `int(x^(1/2)*(b*x + 2)^(3/2), x)`

sympy [A] time = 4.81, size = 92, normalized size = 1.12

$$\frac{b^2 x^{\frac{7}{2}}}{3\sqrt{bx+2}} + \frac{11bx^{\frac{5}{2}}}{6\sqrt{bx+2}} + \frac{17x^{\frac{3}{2}}}{6\sqrt{bx+2}} + \frac{\sqrt{x}}{b\sqrt{bx+2}} - \frac{\operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)**(3/2)*x**(1/2),x)`

[Out] `b**2*x**(7/2)/(3*sqrt(b*x + 2)) + 11*b*x**(5/2)/(6*sqrt(b*x + 2)) + 17*x**(3/2)/(6*sqrt(b*x + 2)) + sqrt(x)/(b*sqrt(b*x + 2)) - asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2)`

$$3.536 \quad \int \frac{(2+bx)^{3/2}}{\sqrt{x}} dx$$

Optimal. Leaf size=61

$$\frac{1}{2}\sqrt{x}(bx+2)^{3/2} + \frac{3}{2}\sqrt{x}\sqrt{bx+2} + \frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

[Out] 3*arcsinh(1/2*b^(1/2)*x^(1/2)*2^(1/2))/b^(1/2)+1/2*(b*x+2)^(3/2)*x^(1/2)+3/2*x^(1/2)*(b*x+2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$\frac{1}{2}\sqrt{x}(bx+2)^{3/2} + \frac{3}{2}\sqrt{x}\sqrt{bx+2} + \frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[(2 + b*x)^(3/2)/Sqrt[x], x]

[Out] (3*Sqrt[x]*Sqrt[2 + b*x])/2 + (Sqrt[x]*(2 + b*x)^(3/2))/2 + (3*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(2+bx)^{3/2}}{\sqrt{x}} dx &= \frac{1}{2} \sqrt{x} (2+bx)^{3/2} + \frac{3}{2} \int \frac{\sqrt{2+bx}}{\sqrt{x}} dx \\
&= \frac{3}{2} \sqrt{x} \sqrt{2+bx} + \frac{1}{2} \sqrt{x} (2+bx)^{3/2} + \frac{3}{2} \int \frac{1}{\sqrt{x} \sqrt{2+bx}} dx \\
&= \frac{3}{2} \sqrt{x} \sqrt{2+bx} + \frac{1}{2} \sqrt{x} (2+bx)^{3/2} + 3 \operatorname{Subst} \left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x} \right) \\
&= \frac{3}{2} \sqrt{x} \sqrt{2+bx} + \frac{1}{2} \sqrt{x} (2+bx)^{3/2} + \frac{3 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 48, normalized size = 0.79

$$\frac{1}{2} \sqrt{x} \sqrt{bx+2} (bx+5) + \frac{3 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Integrate[(2 + b*x)^(3/2)/Sqrt[x], x]

[Out] (Sqrt[x]*Sqrt[2 + b*x]*(5 + b*x))/2 + (3*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

fricas [A] time = 0.52, size = 105, normalized size = 1.72

$$\left[\frac{(b^2x + 5b)\sqrt{bx+2}\sqrt{x} + 3\sqrt{b} \log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{2b}, \frac{(b^2x + 5b)\sqrt{bx+2}\sqrt{x} - 6\sqrt{-b} \arctan\left(\frac{\sqrt{bx+2}\sqrt{x}}{b}\right)}{2b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(3/2)/x^(1/2), x, algorithm="fricas")

[Out] [1/2*((b^2*x + 5*b)*sqrt(b*x + 2)*sqrt(x) + 3*sqrt(b)*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b, 1/2*((b^2*x + 5*b)*sqrt(b*x + 2)*sqrt(x) - 6*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))))/b]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+2)^(3/2)/x^(1/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [85.3561567818,61.7937478349]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [71.707969239,78.6493344628]1/abs(b)*b^2/b*(2*(1/4/b*sqrt(b*x+2))*sqrt(b*x+2)+3/4/b)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)-3/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2)))
```

maple [A] time = 0.00, size = 72, normalized size = 1.18

$$\frac{(bx+2)^{\frac{3}{2}}\sqrt{x}}{2} + \frac{3\sqrt{bx+2}\sqrt{x}}{2} + \frac{3\sqrt{(bx+2)x}\ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{2\sqrt{bx+2}\sqrt{b}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((b*x+2)^(3/2)/x^(1/2),x)
```

```
[Out] 1/2*(b*x+2)^(3/2)*x^(1/2)+3/2*(b*x+2)^(1/2)*x^(1/2)+3/2*((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)/b^(1/2)/x^(1/2)*ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))
```


maxima [B] time = 2.89, size = 98, normalized size = 1.61

$$\frac{3 \log\left(\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{2\sqrt{b}} - \frac{\frac{3\sqrt{bx+2}b}{\sqrt{x}} - \frac{5(bx+2)^{\frac{3}{2}}}{x^2}}{b^2 - \frac{2(bx+2)b}{x} + \frac{(bx+2)^2}{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(3/2)/x^(1/2),x, algorithm="maxima")

[Out] -3/2*log(-(sqrt(b) - sqrt(b*x + 2)/sqrt(x))/(sqrt(b) + sqrt(b*x + 2)/sqrt(x)))/sqrt(b) - (3*sqrt(b*x + 2)*b/sqrt(x) - 5*(b*x + 2)^(3/2)/x^(3/2))/(b^2 - 2*(b*x + 2)*b/x + (b*x + 2)^2/x^2)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(bx+2)^{3/2}}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x + 2)^(3/2)/x^(1/2),x)

[Out] int((b*x + 2)^(3/2)/x^(1/2), x)

sympy [A] time = 2.82, size = 76, normalized size = 1.25

$$\frac{b^2 x^{\frac{5}{2}}}{2\sqrt{bx+2}} + \frac{7bx^{\frac{3}{2}}}{2\sqrt{bx+2}} + \frac{5\sqrt{x}}{\sqrt{bx+2}} + \frac{3 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)**(3/2)/x**(1/2),x)

[Out] b**2*x**(5/2)/(2*sqrt(b*x + 2)) + 7*b*x**(3/2)/(2*sqrt(b*x + 2)) + 5*sqrt(x)/sqrt(b*x + 2) + 3*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/sqrt(b)

$$3.537 \quad \int \frac{(2+bx)^{3/2}}{x^{3/2}} dx$$

Optimal. Leaf size=58

$$-\frac{2(bx+2)^{3/2}}{\sqrt{x}} + 3b\sqrt{x}\sqrt{bx+2} + 6\sqrt{b} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)$$

[Out] 6*arcsinh(1/2*b^(1/2)*x^(1/2)*2^(1/2))*b^(1/2)-2*(b*x+2)^(3/2)/x^(1/2)+3*b*x^(1/2)*(b*x+2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 54, 215}

$$-\frac{2(bx+2)^{3/2}}{\sqrt{x}} + 3b\sqrt{x}\sqrt{bx+2} + 6\sqrt{b} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Int[(2 + b*x)^(3/2)/x^(3/2), x]

[Out] 3*b*Sqrt[x]*Sqrt[2 + b*x] - (2*(2 + b*x)^(3/2))/Sqrt[x] + 6*Sqrt[b]*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]]

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(2+bx)^{3/2}}{x^{3/2}} dx &= -\frac{2(2+bx)^{3/2}}{\sqrt{x}} + (3b) \int \frac{\sqrt{2+bx}}{\sqrt{x}} dx \\
&= 3b\sqrt{x}\sqrt{2+bx} - \frac{2(2+bx)^{3/2}}{\sqrt{x}} + (3b) \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx \\
&= 3b\sqrt{x}\sqrt{2+bx} - \frac{2(2+bx)^{3/2}}{\sqrt{x}} + (6b) \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right) \\
&= 3b\sqrt{x}\sqrt{2+bx} - \frac{2(2+bx)^{3/2}}{\sqrt{x}} + 6\sqrt{b} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)
\end{aligned}$$

Mathematica [C] time = 0.00, size = 28, normalized size = 0.48

$$-\frac{4\sqrt{2} {}_2F_1\left(-\frac{3}{2}, -\frac{1}{2}; \frac{1}{2}; -\frac{bx}{2}\right)}{\sqrt{x}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(2 + b*x)^(3/2)/x^(3/2), x]
```

```
[Out] (-4*Sqrt[2]*Hypergeometric2F1[-3/2, -1/2, 1/2, -1/2*(b*x)]) / Sqrt[x]
```

fricas [A] time = 0.48, size = 99, normalized size = 1.71

$$\left[\frac{3\sqrt{b}x \log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1) + \sqrt{bx+2}(bx-4)\sqrt{x}}{x}, -\frac{6\sqrt{-b}x \arctan\left(\frac{\sqrt{bx+2}\sqrt{-b}}{b\sqrt{x}}\right) - \sqrt{bx+2}(bx-4)}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+2)^(3/2)/x^(3/2),x, algorithm="fricas")
```

```
[Out] [(3*sqrt(b)*x*log(b*x + sqrt(b*x + 2))*sqrt(b)*sqrt(x) + 1) + sqrt(b*x + 2)*
(b*x - 4)*sqrt(x))/x, -(6*sqrt(-b)*x*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(
x)))) - sqrt(b*x + 2)*(b*x - 4)*sqrt(x))/x]
```

```
giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00
```

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+2)^(3/2)/x^(3/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warni
ng, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}
}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,
[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+
%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,
[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}
}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-
4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,
4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%
{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[
3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}
}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%
{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,
2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [85.3561567
818,61.7937478349]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1
,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}
+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,
2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+
%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[
2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}
}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-3
2,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]
%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%
{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2
,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}
}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-
8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parame
ters values [71.707969239,78.6493344628]b/abs(b)*b^2/b*(2*(1/2*sqrt(b*x+2)*
sqrt(b*x+2)-3)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)/(b*(b*x+2)-2*b)-6/sqrt(b)*ln
(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))
```

maple [A] time = 0.02, size = 72, normalized size = 1.24

$$\frac{3\sqrt{(bx+2)x} \sqrt{b} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{\sqrt{bx+2} \sqrt{x}} + \frac{b^2x^2 - 2bx - 8}{\sqrt{bx+2} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+2)^(3/2)/x^(3/2), x)

[Out] (b^2*x^2-2*b*x-8)/(b*x+2)^(1/2)/x^(1/2)+3*((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)*b^(1/2)/x^(1/2)*ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))

maxima [A] time = 2.91, size = 81, normalized size = 1.40

$$-3\sqrt{b} \log\left(-\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right) - \frac{4\sqrt{bx+2}}{\sqrt{x}} - \frac{2\sqrt{bx+2}b}{\left(b - \frac{bx+2}{x}\right)\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(3/2)/x^(3/2), x, algorithm="maxima")

[Out] -3*sqrt(b)*log(-(sqrt(b) - sqrt(b*x + 2)/sqrt(x))/(sqrt(b) + sqrt(b*x + 2)/sqrt(x))) - 4*sqrt(b*x + 2)/sqrt(x) - 2*sqrt(b*x + 2)*b/((b - (b*x + 2)/x)*sqrt(x))

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(bx+2)^{3/2}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x + 2)^(3/2)/x^(3/2), x)

[Out] int((b*x + 2)^(3/2)/x^(3/2), x)

sympy [A] time = 2.44, size = 73, normalized size = 1.26

$$6\sqrt{b} \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right) + \frac{b^2x^{\frac{3}{2}}}{\sqrt{bx+2}} - \frac{2b\sqrt{x}}{\sqrt{bx+2}} - \frac{8}{\sqrt{x}\sqrt{bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)**(3/2)/x**(3/2), x)

[Out] 6*sqrt(b)*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2) + b**2*x**(3/2)/sqrt(b*x + 2) - 2*b*sqrt(x)/sqrt(b*x + 2) - 8/(sqrt(x)*sqrt(b*x + 2))

$$3.538 \quad \int \frac{(2+bx)^{3/2}}{x^{5/2}} dx$$

Optimal. Leaf size=60

$$2b^{3/2} \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right) - \frac{2(bx+2)^{3/2}}{3x^{3/2}} - \frac{2b\sqrt{bx+2}}{\sqrt{x}}$$

[Out] $-2/3*(b*x+2)^{(3/2)}/x^{(3/2)}+2*b^{(3/2)}*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})-2*b*(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 54, 215}

$$2b^{3/2} \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right) - \frac{2(bx+2)^{3/2}}{3x^{3/2}} - \frac{2b\sqrt{bx+2}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(2 + b*x)^{(3/2)}/x^{(5/2)}, x]$

[Out] $(-2*b*\operatorname{Sqrt}[2 + b*x])/ \operatorname{Sqrt}[x] - (2*(2 + b*x)^{(3/2)})/(3*x^{(3/2)}) + 2*b^{(3/2)}*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/ \operatorname{Sqrt}[2]]$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m+n+2], 0] && (FractionQ[m] || GeQ[2*n+m+1, 0]) && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

$\operatorname{Int}[1/(\operatorname{Sqrt}[(a_.) + (b_.)*(x_.)]*\operatorname{Sqrt}[(c_.) + (d_.)*(x_.)]), x_Symbol] \rightarrow \operatorname{Dist}[2/\operatorname{Sqrt}[b], \operatorname{Subst}[\operatorname{Int}[1/\operatorname{Sqrt}[b*c - a*d + d*x^2], x], x, \operatorname{Sqrt}[a + b*x]], x] /;$ FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 215

$\operatorname{Int}[1/\operatorname{Sqrt}[(a_.) + (b_.)*(x_.)^2], x_Symbol] \rightarrow \operatorname{Simp}[\operatorname{ArcSinh}[\operatorname{Rt}[b, 2]*x]/\operatorname{Sqrt}[a]/\operatorname{Rt}[b, 2], x] /;$ FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(2+bx)^{3/2}}{x^{5/2}} dx &= -\frac{2(2+bx)^{3/2}}{3x^{3/2}} + b \int \frac{\sqrt{2+bx}}{x^{3/2}} dx \\
&= -\frac{2b\sqrt{2+bx}}{\sqrt{x}} - \frac{2(2+bx)^{3/2}}{3x^{3/2}} + b^2 \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx \\
&= -\frac{2b\sqrt{2+bx}}{\sqrt{x}} - \frac{2(2+bx)^{3/2}}{3x^{3/2}} + (2b^2) \text{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right) \\
&= -\frac{2b\sqrt{2+bx}}{\sqrt{x}} - \frac{2(2+bx)^{3/2}}{3x^{3/2}} + 2b^{3/2} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.50

$$-\frac{4\sqrt{2} {}_2F_1\left(-\frac{3}{2}, -\frac{3}{2}; -\frac{1}{2}; -\frac{bx}{2}\right)}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(2 + b*x)^(3/2)/x^(5/2), x]

[Out] (-4*Sqrt[2]*Hypergeometric2F1[-3/2, -3/2, -1/2, -1/2*(b*x)])/(3*x^(3/2))

fricas [A] time = 0.45, size = 108, normalized size = 1.80

$$\left[\frac{3b^{\frac{3}{2}}x^2 \log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1) - 4(2bx+1)\sqrt{bx+2}\sqrt{x}}{3x^2}, -\frac{2\left(3\sqrt{-b}bx^2 \arctan\left(\frac{\sqrt{bx+2}\sqrt{-b}}{b\sqrt{x}}\right) + 2(2bx+1)\sqrt{-b}\sqrt{x}\right)}{3x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(3/2)/x^(5/2), x, algorithm="fricas")

[Out] [1/3*(3*b^(3/2)*x^2*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1) - 4*(2*b*x + 1)*sqrt(b*x + 2)*sqrt(x))/x^2, -2/3*(3*sqrt(-b)*b*x^2*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))) + 2*(2*b*x + 1)*sqrt(b*x + 2)*sqrt(x))/x^2]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(3/2)/x^(5/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [85.3561567818,61.7937478349]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [71.707969239,78.6493344628] 1/abs(b)*b^2/b*(2*(-12*b^3/9*sqrt(b*x+2)*sqrt(b*x+2)+18*b^3/9)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)/(b*(b*x+2)-2*b)^2-2*b^2/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))

maple [A] time = 0.02, size = 73, normalized size = 1.22

$$\frac{\sqrt{(bx+2)x} b^{\frac{3}{2}} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{\sqrt{bx+2} \sqrt{x}} - \frac{4(2b^2x^2+5bx+2)}{3\sqrt{bx+2} x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+2)^(3/2)/x^(5/2),x)

[Out] -4/3*(2*b^2*x^2+5*b*x+2)/x^(3/2)/(b*x+2)^(1/2)+b^(3/2)*ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))*((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)/x^(1/2)

maxima [A] time = 2.97, size = 67, normalized size = 1.12

$$-b^{\frac{3}{2}} \log \left(-\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}} \right) - \frac{2\sqrt{bx+2}b}{\sqrt{x}} - \frac{2(bx+2)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(3/2)/x^(5/2),x, algorithm="maxima")

[Out] $-b^{(3/2)}*\log(-(\text{sqrt}(b) - \text{sqrt}(b*x + 2)/\text{sqrt}(x))/(\text{sqrt}(b) + \text{sqrt}(b*x + 2)/\text{sqrt}(x))) - 2*\text{sqrt}(b*x + 2)*b/\text{sqrt}(x) - 2/3*(b*x + 2)^{(3/2)}/x^{(3/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(bx+2)^{3/2}}{x^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x + 2)^(3/2)/x^(5/2),x)

[Out] int((b*x + 2)^(3/2)/x^(5/2), x)

sympy [A] time = 2.81, size = 70, normalized size = 1.17

$$-\frac{8b^{\frac{3}{2}}\sqrt{1+\frac{2}{bx}}}{3} - b^{\frac{3}{2}} \log\left(\frac{1}{bx}\right) + 2b^{\frac{3}{2}} \log\left(\sqrt{1+\frac{2}{bx}} + 1\right) - \frac{4\sqrt{b}\sqrt{1+\frac{2}{bx}}}{3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)**(3/2)/x**(5/2),x)

[Out] $-8*b^{(3/2)}*\text{sqrt}(1 + 2/(b*x))/3 - b^{(3/2)}*\log(1/(b*x)) + 2*b^{(3/2)}*\log(\text{sqrt}(1 + 2/(b*x)) + 1) - 4*\text{sqrt}(b)*\text{sqrt}(1 + 2/(b*x))/(3*x)$

$$3.539 \quad \int x^{5/2}(2 - bx)^{3/2} dx$$

Optimal. Leaf size=131

$$\frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}} - \frac{3\sqrt{x}\sqrt{2-bx}}{8b^3} - \frac{x^{3/2}\sqrt{2-bx}}{8b^2} + \frac{1}{5}x^{7/2}(2-bx)^{3/2} + \frac{3}{20}x^{7/2}\sqrt{2-bx} - \frac{x^{5/2}\sqrt{2-bx}}{20b}$$

[Out] $1/5*x^{(7/2)}*(-b*x+2)^{(3/2)}+3/4*\arcsin(1/2*b^{(1/2)}*x^{(1/2)*2^{(1/2)}}/b^{(7/2)}-1/8*x^{(3/2)}*(-b*x+2)^{(1/2)}/b^2-1/20*x^{(5/2)}*(-b*x+2)^{(1/2)}/b+3/20*x^{(7/2)}*(-b*x+2)^{(1/2)}-3/8*x^{(1/2)}*(-b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.04, antiderivative size = 131, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$-\frac{x^{3/2}\sqrt{2-bx}}{8b^2} - \frac{3\sqrt{x}\sqrt{2-bx}}{8b^3} + \frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}} + \frac{1}{5}x^{7/2}(2-bx)^{3/2} + \frac{3}{20}x^{7/2}\sqrt{2-bx} - \frac{x^{5/2}\sqrt{2-bx}}{20b}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)*(2 - b*x)^(3/2), x]

[Out] $(-3*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/(8*b^3) - (x^{(3/2)}*\text{Sqrt}[2 - b*x])/(8*b^2) - (x^{(5/2)}*\text{Sqrt}[2 - b*x])/(20*b) + (3*x^{(7/2)}*\text{Sqrt}[2 - b*x])/20 + (x^{(7/2)}*(2 - b*x)^{(3/2)})/5 + (3*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/(4*b^{(7/2)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] :> Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int x^{5/2}(2-bx)^{3/2} dx &= \frac{1}{5}x^{7/2}(2-bx)^{3/2} + \frac{3}{5} \int x^{5/2}\sqrt{2-bx} dx \\
&= \frac{3}{20}x^{7/2}\sqrt{2-bx} + \frac{1}{5}x^{7/2}(2-bx)^{3/2} + \frac{3}{20} \int \frac{x^{5/2}}{\sqrt{2-bx}} dx \\
&= -\frac{x^{5/2}\sqrt{2-bx}}{20b} + \frac{3}{20}x^{7/2}\sqrt{2-bx} + \frac{1}{5}x^{7/2}(2-bx)^{3/2} + \frac{\int \frac{x^{3/2}}{\sqrt{2-bx}} dx}{4b} \\
&= -\frac{x^{3/2}\sqrt{2-bx}}{8b^2} - \frac{x^{5/2}\sqrt{2-bx}}{20b} + \frac{3}{20}x^{7/2}\sqrt{2-bx} + \frac{1}{5}x^{7/2}(2-bx)^{3/2} + \frac{3 \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx}{8b^2} \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{8b^3} - \frac{x^{3/2}\sqrt{2-bx}}{8b^2} - \frac{x^{5/2}\sqrt{2-bx}}{20b} + \frac{3}{20}x^{7/2}\sqrt{2-bx} + \frac{1}{5}x^{7/2}(2-bx)^{3/2} + \frac{3 \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx}{8b^2} \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{8b^3} - \frac{x^{3/2}\sqrt{2-bx}}{8b^2} - \frac{x^{5/2}\sqrt{2-bx}}{20b} + \frac{3}{20}x^{7/2}\sqrt{2-bx} + \frac{1}{5}x^{7/2}(2-bx)^{3/2} + \frac{3 \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx}{8b^2} \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{8b^3} - \frac{x^{3/2}\sqrt{2-bx}}{8b^2} - \frac{x^{5/2}\sqrt{2-bx}}{20b} + \frac{3}{20}x^{7/2}\sqrt{2-bx} + \frac{1}{5}x^{7/2}(2-bx)^{3/2} + \frac{3 \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx}{8b^2}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 79, normalized size = 0.60

$$\frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{7/2}} - \frac{\sqrt{x}\sqrt{2-bx}(8b^4x^4 - 22b^3x^3 + 2b^2x^2 + 5bx + 15)}{40b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*(2 - b*x)^(3/2), x]

[Out] -1/40*(Sqrt[x]*Sqrt[2 - b*x]*(15 + 5*b*x + 2*b^2*x^2 - 22*b^3*x^3 + 8*b^4*x^4))/b^3 + (3*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(4*b^(7/2))

fricas [A] time = 0.47, size = 157, normalized size = 1.20

$$\left[\frac{(8b^5x^4 - 22b^4x^3 + 2b^3x^2 + 5b^2x + 15b)\sqrt{-bx+2}\sqrt{x} + 15\sqrt{-b}\log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1)}{40b^4}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(5/2)*(-b*x+2)^(3/2),x, algorithm="fricas")
```

```
[Out] [-1/40*((8*b^5*x^4 - 22*b^4*x^3 + 2*b^3*x^2 + 5*b^2*x + 15*b)*sqrt(-b*x + 2)
)*sqrt(x) + 15*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^
4, -1/40*((8*b^5*x^4 - 22*b^4*x^3 + 2*b^3*x^2 + 5*b^2*x + 15*b)*sqrt(-b*x +
2)*sqrt(x) + 30*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))))/b^4]
```

```
giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00
```

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(5/2)*(-b*x+2)^(3/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warni
ng, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+
%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[
1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}
+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4
,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%
}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+
%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,
[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}
+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8
,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]
%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+
%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0
,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-18.27194
81629,8.05231268331]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1
,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}
+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,
[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%
}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{2
0,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]
%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+
%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,
[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%
}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{4
6,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]
%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+
%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at par
ameters values [-36.6004387327,28.4266860783]Warning, choosing root of [1,0
,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,
[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}
+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4
```


[3, 3] + [20, [3, 2]] + [-20, [3, 1]] + [8, [3, 0]] + [6, [2, 4]] + [-20, [2, 3]] + [46, [2, 2]] + [-40, [2, 1]] + [24, [2, 0]] + [4, [1, 4]] + [-20, [1, 3]] + [40, [1, 2]] + [-48, [1, 1]] + [32, [1, 0]] + [1, [0, 4]] + [-8, [0, 3]] + [24, [0, 2]] + [-32, [0, 1]] + [16, [0, 0]] at parameters values [-12.7113713701, 17.6881634681] $1/b * (-2*b^2*abs(b)/b^2 * (2 * (((5040*b^19/100800/b^23*sqrt(-b*x+2)*sqrt(-b*x+2) - 51660*b^19/100800/b^23)*sqrt(-b*x+2)*sqrt(-b*x+2) + 215460*b^19/100800/b^23)*sqrt(-b*x+2)*sqrt(-b*x+2) - 469350*b^19/100800/b^23)*sqrt(-b*x+2)*sqrt(-b*x+2) + 607950*b^19/100800/b^23)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b) - 63/8/b^3/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b) - sqrt(-b)*sqrt(-b*x+2)))) + 8*b*abs(b)/b^2 * (2 * (((-90*b^11/1440/b^14*sqrt(-b*x+2)*sqrt(-b*x+2) + 750*b^11/1440/b^14)*sqrt(-b*x+2)*sqrt(-b*x+2) - 2445*b^11/1440/b^14)*sqrt(-b*x+2)*sqrt(-b*x+2) + 4185*b^11/1440/b^14)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b) - 35/8/b^2/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b) - sqrt(-b)*sqrt(-b*x+2)))) - 8*abs(b)/b^2 * (2 * ((12*b^5/144/b^7*sqrt(-b*x+2)*sqrt(-b*x+2) - 78*b^5/144/b^7)*sqrt(-b*x+2)*sqrt(-b*x+2) + 198*b^5/144/b^7)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b) - 5/2/b/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b) - sqrt(-b)*sqrt(-b*x+2))))))$

maple [A] time = 0.01, size = 132, normalized size = 1.01

$$\frac{(-bx+2)^{\frac{5}{2}}x^{\frac{5}{2}}}{5b} - \frac{(-bx+2)^{\frac{5}{2}}x^{\frac{3}{2}}}{4b^2} - \frac{(-bx+2)^{\frac{5}{2}}\sqrt{x}}{4b^3} + \frac{(-bx+2)^{\frac{3}{2}}\sqrt{x}}{8b^3} + \frac{3\sqrt{-bx+2}\sqrt{x}}{8b^3} + \frac{3\sqrt{-bx+2}x \arctan\left(\frac{x-\sqrt{-bx+2}}{\sqrt{-bx+2}}\right)}{8\sqrt{-bx+2}b^{\frac{7}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{(5/2)}*(-b*x+2)^{(3/2)}, x)$

[Out] $-1/5/b*x^{(5/2)}*(-b*x+2)^{(5/2)} - 1/4/b^2*x^{(3/2)}*(-b*x+2)^{(5/2)} - 1/4/b^3*x^{(1/2)}*(-b*x+2)^{(5/2)} + 1/8*(-b*x+2)^{(3/2)}/b^3*x^{(1/2)} + 3/8*(-b*x+2)^{(1/2)}/b^3*x^{(1/2)} + 3/8*((-b*x+2)*x)^{(1/2)}/(-b*x+2)^{(1/2)}/b^{(7/2)}/x^{(1/2)}*\arctan((x-1/b)/(-b*x^2+2*x))^{(1/2)}*b^{(1/2)}$

maxima [A] time = 2.94, size = 179, normalized size = 1.37

$$\frac{15\sqrt{-bx+2}b^4}{\sqrt{x}} + \frac{70(-bx+2)^{\frac{3}{2}}b^3}{x^2} - \frac{128(-bx+2)^{\frac{5}{2}}b^2}{x^2} - \frac{70(-bx+2)^{\frac{7}{2}}b}{x^2} - \frac{15(-bx+2)^{\frac{9}{2}}}{x^2} - \frac{3 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{4b^{\frac{7}{2}}}$$

$$20\left(b^8 - \frac{5(bx-2)b^7}{x} + \frac{10(bx-2)^2b^6}{x^2} - \frac{10(bx-2)^3b^5}{x^3} + \frac{5(bx-2)^4b^4}{x^4} - \frac{(bx-2)^5b^3}{x^5}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{(5/2)}*(-b*x+2)^{(3/2)}, x, \text{algorithm}=\text{"maxima"})$

[Out] $1/20*(15*sqrt(-b*x + 2)*b^4/sqrt(x) + 70*(-b*x + 2)^{(3/2)}*b^3/x^{(3/2)} - 128*(-b*x + 2)^{(5/2)}*b^2/x^{(5/2)} - 70*(-b*x + 2)^{(7/2)}*b/x^{(7/2)} - 15*(-b*x +$

$(2)^{(9/2)}/x^{(9/2)}/(b^8 - 5*(b*x - 2)*b^7/x + 10*(b*x - 2)^2*b^6/x^2 - 10*(b*x - 2)^3*b^5/x^3 + 5*(b*x - 2)^4*b^4/x^4 - (b*x - 2)^5*b^3/x^5) - 3/4*\arctan(\sqrt{-b*x + 2}/(\sqrt{b}*\sqrt{x}))/b^{(7/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} (2 - bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/2)*(2 - b*x)^(3/2), x)`

[Out] `int(x^(5/2)*(2 - b*x)^(3/2), x)`

sympy [A] time = 15.28, size = 291, normalized size = 2.22

$$\left\{ \begin{array}{l} -\frac{ib^2x^{\frac{11}{2}}}{5\sqrt{bx-2}} + \frac{19ibx^{\frac{9}{2}}}{20\sqrt{bx-2}} - \frac{23ix^{\frac{7}{2}}}{20\sqrt{bx-2}} - \frac{ix^{\frac{5}{2}}}{40b\sqrt{bx-2}} - \frac{ix^{\frac{3}{2}}}{8b^2\sqrt{bx-2}} + \frac{3i\sqrt{x}}{4b^3\sqrt{bx-2}} - \frac{3i\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{7}{2}}} \quad \text{for } \frac{|bx|}{2} > 1 \\ \frac{b^2x^{\frac{11}{2}}}{5\sqrt{-bx+2}} - \frac{19bx^{\frac{9}{2}}}{20\sqrt{-bx+2}} + \frac{23x^{\frac{7}{2}}}{20\sqrt{-bx+2}} + \frac{x^{\frac{5}{2}}}{40b\sqrt{-bx+2}} + \frac{x^{\frac{3}{2}}}{8b^2\sqrt{-bx+2}} - \frac{3\sqrt{x}}{4b^3\sqrt{-bx+2}} + \frac{3\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{7}{2}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/2)*(-b*x+2)**(3/2), x)`

[Out] `Piecewise((-I*b**2*x**(11/2)/(5*sqrt(b*x - 2)) + 19*I*b*x**(9/2)/(20*sqrt(b*x - 2)) - 23*I*x**(7/2)/(20*sqrt(b*x - 2)) - I*x**(5/2)/(40*b*sqrt(b*x - 2)) - I*x**(3/2)/(8*b**2*sqrt(b*x - 2)) + 3*I*sqrt(x)/(4*b**3*sqrt(b*x - 2)) - 3*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(7/2)), Abs(b*x)/2 > 1), (b**2*x**(11/2)/(5*sqrt(-b*x + 2)) - 19*b*x**(9/2)/(20*sqrt(-b*x + 2)) + 23*x**(7/2)/(20*sqrt(-b*x + 2)) + x**(5/2)/(40*b*sqrt(-b*x + 2)) + x**(3/2)/(8*b**2*sqrt(-b*x + 2)) - 3*sqrt(x)/(4*b**3*sqrt(-b*x + 2)) + 3*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(7/2)), True))`

3.540 $\int x^{3/2}(2 - bx)^{3/2} dx$

Optimal. Leaf size=109

$$\frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} - \frac{3\sqrt{x}\sqrt{2-bx}}{8b^2} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{4}x^{5/2}\sqrt{2-bx} - \frac{x^{3/2}\sqrt{2-bx}}{8b}$$

[Out] $1/4*x^{(5/2)}*(-b*x+2)^{(3/2)}+3/4*\arcsin(1/2*b^{(1/2)}*x^{(1/2)*2^{(1/2)}}/b^{(5/2)}-1/8*x^{(3/2)}*(-b*x+2)^{(1/2)}/b+1/4*x^{(5/2)}*(-b*x+2)^{(1/2)}-3/8*x^{(1/2)}*(-b*x+2)^{(1/2)}/b^2$

Rubi [A] time = 0.03, antiderivative size = 109, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$-\frac{3\sqrt{x}\sqrt{2-bx}}{8b^2} + \frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{4}x^{5/2}\sqrt{2-bx} - \frac{x^{3/2}\sqrt{2-bx}}{8b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(3/2)}*(2 - b*x)^{(3/2)}, x]$

[Out] $(-3*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/(8*b^2) - (x^{(3/2)}*\text{Sqrt}[2 - b*x])/(8*b) + (x^{(5/2)}*\text{Sqrt}[2 - b*x])/4 + (x^{(5/2)}*(2 - b*x)^{(3/2)})/4 + (3*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/(4*b^{(5/2)})$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\text{FreeQ}\{a, b, c, d\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{NeQ}[m + n + 1, 0] \ \&\& \ !(\text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{GtQ}[m, 0] \ \&\& \ \text{LtQ}[m - n, 0]))) \ \&\& \ !\text{ILtQ}[m + n + 2, 0] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 54

$\text{Int}[1/(\text{Sqrt}[(a_.) + (b_.)*(x_.)]*\text{Sqrt}[(c_.) + (d_.)*(x_.)]), x_Symbol] \rightarrow \text{Dist}[2/\text{Sqrt}[b], \text{Subst}[\text{Int}[1/\text{Sqrt}[b*c - a*d + d*x^2], x], x, \text{Sqrt}[a + b*x]], x] /;$ $\text{FreeQ}\{a, b, c, d\}, x \ \&\& \ \text{GtQ}[b*c - a*d, 0] \ \&\& \ \text{GtQ}[b, 0]$

Rule 216

$\text{Int}[1/\text{Sqrt}[(a_.) + (b_.)*(x_.)^2], x_Symbol] \rightarrow \text{Simp}[\text{ArcSin}[(\text{Rt}[-b, 2]*x)/\text{Sqrt}[a]]/\text{Rt}[-b, 2], x] /;$ $\text{FreeQ}\{a, b\}, x \ \&\& \ \text{GtQ}[a, 0] \ \&\& \ \text{NegQ}[b]$

Rubi steps

$$\begin{aligned}
\int x^{3/2}(2-bx)^{3/2} dx &= \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{3}{4} \int x^{3/2}\sqrt{2-bx} dx \\
&= \frac{1}{4}x^{5/2}\sqrt{2-bx} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{4} \int \frac{x^{3/2}}{\sqrt{2-bx}} dx \\
&= -\frac{x^{3/2}\sqrt{2-bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2-bx} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{3 \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx}{8b} \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{8b^2} - \frac{x^{3/2}\sqrt{2-bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2-bx} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{3 \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx}{8b^2} \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{8b^2} - \frac{x^{3/2}\sqrt{2-bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2-bx} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{3 \text{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx\right)}{4b^2} \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{8b^2} - \frac{x^{3/2}\sqrt{2-bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2-bx} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 70, normalized size = 0.64

$$\frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} - \frac{\sqrt{x}\sqrt{2-bx}(2b^3x^3 - 6b^2x^2 + bx + 3)}{8b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*(2 - b*x)^(3/2),x]

[Out] -1/8*(Sqrt[x]*Sqrt[2 - b*x]*(3 + b*x - 6*b^2*x^2 + 2*b^3*x^3))/b^2 + (3*Arc Sin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(4*b^(5/2))

fricas [A] time = 0.47, size = 139, normalized size = 1.28

$$\left[\frac{(2b^4x^3 - 6b^3x^2 + b^2x + 3b)\sqrt{-bx+2}\sqrt{x} + 3\sqrt{-b}\log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1)}{8b^3}, - \frac{(2b^4x^3 - 6b^3x^2 + b^2x + 3b)\sqrt{-bx+2}\sqrt{x} + 3\sqrt{-b}\log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1)}{8b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+2)^(3/2),x, algorithm="fricas")

[Out] [-1/8*((2*b^4*x^3 - 6*b^3*x^2 + b^2*x + 3*b)*sqrt(-b*x + 2)*sqrt(x) + 3*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^3, -1/8*((2*b^4*x^3 - 6*b^3*x^2 + b^2*x + 3*b)*sqrt(-b*x + 2)*sqrt(x) + 3*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^3]

$$3 - 6*b^3*x^2 + b^2*x + 3*b)*\text{sqrt}(-b*x + 2)*\text{sqrt}(x) + 6*\text{sqrt}(b)*\text{arctan}(\text{sqrt}(-b*x + 2)/(\text{sqrt}(b)*\text{sqrt}(x)))/b^3]$$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+2)^(3/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-18.2719481629,8.05231268331]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-36.6004387327,28.4266860783]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-18.2719481629,8.05231268331]

$\{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values [-61.8196598012, 96.7771189027] Warning, choosing root of $\{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values [-5.403030 52077, 66.1769613782] Warning, choosing root of $\{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values [-61.0171700171, 94.1262030317] Warning, choosing root of $\{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$

++++{16,[0,0]}}] at parameters values [-12.7113713701,17.6881634681]1/b*(-2*b^2*abs(b)/b^2*(2*((-90*b^11/1440/b^14*sqrt(-b*x+2)*sqrt(-b*x+2)+750*b^11/1440/b^14)*sqrt(-b*x+2)*sqrt(-b*x+2)-2445*b^11/1440/b^14)*sqrt(-b*x+2)*sqrt(-b*x+2)+4185*b^11/1440/b^14)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)-35/8/b^2/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b)-sqrt(-b)*sqrt(-b*x+2))))+8*b*abs(b)/b^2*(2*((12*b^5/144/b^7*sqrt(-b*x+2)*sqrt(-b*x+2)-78*b^5/144/b^7)*sqrt(-b*x+2)*sqrt(-b*x+2)+198*b^5/144/b^7)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)-5/2/b/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b)-sqrt(-b)*sqrt(-b*x+2))))+8*abs(b)/b^2/b*(2*(1/8*sqrt(-b*x+2)*sqrt(-b*x+2)-5/8)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)+6*b/4/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b)-sqrt(-b)*sqrt(-b*x+2))))))

maple [A] time = 0.01, size = 116, normalized size = 1.06

$$-\frac{(-bx+2)^{\frac{5}{2}}x^{\frac{3}{2}}}{4b}-\frac{(-bx+2)^{\frac{5}{2}}\sqrt{x}}{4b^2}+\frac{(-bx+2)^{\frac{3}{2}}\sqrt{x}}{8b^2}+\frac{3\sqrt{-bx+2}\sqrt{x}}{8b^2}+\frac{3\sqrt{-bx+2}x\arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{8\sqrt{-bx+2}b^{\frac{5}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(-b*x+2)^(3/2),x)

[Out] -1/4/b*x^(3/2)*(-b*x+2)^(5/2)-1/4/b^2*x^(1/2)*(-b*x+2)^(5/2)+1/8*(-b*x+2)^(3/2)/b^2*x^(1/2)+3/8*(-b*x+2)^(1/2)/b^2*x^(1/2)+3/8*((-b*x+2)*x)^(1/2)/(-b*x+2)^(1/2)/b^(5/2)/x^(1/2)*arctan((x-1/b)/(-b*x^2+2*x)^(1/2)*b^(1/2))

maxima [A] time = 2.92, size = 147, normalized size = 1.35

$$\frac{\frac{3\sqrt{-bx+2}b^3}{\sqrt{x}}+\frac{11(-bx+2)^{\frac{3}{2}}b^2}{x^{\frac{3}{2}}}-\frac{11(-bx+2)^{\frac{5}{2}}b}{x^{\frac{5}{2}}}-\frac{3(-bx+2)^{\frac{7}{2}}}{x^{\frac{7}{2}}}}{4\left(b^6-\frac{4(bx-2)b^5}{x}+\frac{6(bx-2)^2b^4}{x^2}-\frac{4(bx-2)^3b^3}{x^3}+\frac{(bx-2)^4b^2}{x^4}\right)}-\frac{3\arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{4b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+2)^(3/2),x, algorithm="maxima")

[Out] 1/4*(3*sqrt(-b*x+2)*b^3/sqrt(x)+11*(-b*x+2)^(3/2)*b^2/x^(3/2)-11*(-b*x+2)^(5/2)*b/x^(5/2)-3*(-b*x+2)^(7/2)/x^(7/2))/(b^6-4*(b*x-2)*b^5/x+6*(b*x-2)^2*b^4/x^2-4*(b*x-2)^3*b^3/x^3+(b*x-2)^4*b^2/x^4)-3/4*arctan(sqrt(-b*x+2)/(sqrt(b)*sqrt(x)))/b^(5/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} (2 - bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)*(2 - b*x)^(3/2), x)`

[Out] `int(x^(3/2)*(2 - b*x)^(3/2), x)`

sympy [A] time = 7.73, size = 252, normalized size = 2.31

$$\left\{ \begin{array}{l} -\frac{ib^2x^{\frac{9}{2}}}{4\sqrt{bx-2}} + \frac{5ibx^{\frac{7}{2}}}{4\sqrt{bx-2}} - \frac{13ix^{\frac{5}{2}}}{8\sqrt{bx-2}} - \frac{ix^{\frac{3}{2}}}{8b\sqrt{bx-2}} + \frac{3i\sqrt{x}}{4b^2\sqrt{bx-2}} - \frac{3i\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{5}{2}}} \\ \frac{b^2x^{\frac{9}{2}}}{4\sqrt{-bx+2}} - \frac{5bx^{\frac{7}{2}}}{4\sqrt{-bx+2}} + \frac{13x^{\frac{5}{2}}}{8\sqrt{-bx+2}} + \frac{x^{\frac{3}{2}}}{8b\sqrt{-bx+2}} - \frac{3\sqrt{x}}{4b^2\sqrt{-bx+2}} + \frac{3\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{5}{2}}} \end{array} \right. \begin{array}{l} \text{for } \frac{|bx|}{2} > 1 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)*(-b*x+2)**(3/2), x)`

[Out] `Piecewise((-I*b**2*x**(9/2)/(4*sqrt(b*x - 2)) + 5*I*b*x**(7/2)/(4*sqrt(b*x - 2)) - 13*I*x**(5/2)/(8*sqrt(b*x - 2)) - I*x**(3/2)/(8*b*sqrt(b*x - 2)) + 3*I*sqrt(x)/(4*b**2*sqrt(b*x - 2)) - 3*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(5/2)), Abs(b*x)/2 > 1, (b**2*x**(9/2)/(4*sqrt(-b*x + 2)) - 5*b*x**(7/2)/(4*sqrt(-b*x + 2)) + 13*x**(5/2)/(8*sqrt(-b*x + 2)) + x**(3/2)/(8*b*sqrt(-b*x + 2)) - 3*sqrt(x)/(4*b**2*sqrt(-b*x + 2)) + 3*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(5/2)), True))`

3.541 $\int \sqrt{x} (2 - bx)^{3/2} dx$

Optimal. Leaf size=84

$$\frac{\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} + \frac{1}{3}x^{3/2}(2-bx)^{3/2} + \frac{1}{2}x^{3/2}\sqrt{2-bx} - \frac{\sqrt{x}\sqrt{2-bx}}{2b}$$

[Out] $1/3*x^{(3/2)}*(-b*x+2)^{(3/2)}+\arcsin(1/2*b^{(1/2)}*x^{(1/2)*2^{(1/2)}}/b^{(3/2)}+1/2*x^{(3/2)}*(-b*x+2)^{(1/2)}-1/2*x^{(1/2)}*(-b*x+2)^{(1/2)}/b$

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$\frac{\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} + \frac{1}{3}x^{3/2}(2-bx)^{3/2} + \frac{1}{2}x^{3/2}\sqrt{2-bx} - \frac{\sqrt{x}\sqrt{2-bx}}{2b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*(2 - b*x)^(3/2), x]

[Out] $-(\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/(2*b) + (x^{(3/2)}*\text{Sqrt}[2 - b*x])/2 + (x^{(3/2)}*(2 - b*x)^{(3/2)})/3 + \text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/(\text{Sqrt}[2])]/b^{(3/2)}$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int \sqrt{x} (2 - bx)^{3/2} dx &= \frac{1}{3} x^{3/2} (2 - bx)^{3/2} + \int \sqrt{x} \sqrt{2 - bx} dx \\
&= \frac{1}{2} x^{3/2} \sqrt{2 - bx} + \frac{1}{3} x^{3/2} (2 - bx)^{3/2} + \frac{1}{2} \int \frac{\sqrt{x}}{\sqrt{2 - bx}} dx \\
&= -\frac{\sqrt{x} \sqrt{2 - bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2 - bx} + \frac{1}{3} x^{3/2} (2 - bx)^{3/2} + \frac{\int \frac{1}{\sqrt{x} \sqrt{2 - bx}} dx}{2b} \\
&= -\frac{\sqrt{x} \sqrt{2 - bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2 - bx} + \frac{1}{3} x^{3/2} (2 - bx)^{3/2} + \frac{\text{Subst}\left(\int \frac{1}{\sqrt{2 - bx^2}} dx, x, \sqrt{x}\right)}{b} \\
&= -\frac{\sqrt{x} \sqrt{2 - bx}}{2b} + \frac{1}{2} x^{3/2} \sqrt{2 - bx} + \frac{1}{3} x^{3/2} (2 - bx)^{3/2} + \frac{\sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 60, normalized size = 0.71

$$\frac{\sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} - \frac{\sqrt{x} \sqrt{2 - bx} (2b^2 x^2 - 7bx + 3)}{6b}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*(2 - b*x)^(3/2), x]

[Out] -1/6*(Sqrt[x]*Sqrt[2 - b*x]*(3 - 7*b*x + 2*b^2*x^2))/b + ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]]/b^(3/2)

fricas [A] time = 0.46, size = 125, normalized size = 1.49

$$\left[\frac{(2b^3x^2 - 7b^2x + 3b)\sqrt{-bx + 2}\sqrt{x} + 3\sqrt{-b} \log(-bx + \sqrt{-bx + 2}\sqrt{-b}\sqrt{x} + 1)}{6b^2}, -\frac{(2b^3x^2 - 7b^2x + 3b)\sqrt{-bx + 2}\sqrt{x}}{6b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(3/2)*x^(1/2), x, algorithm="fricas")

[Out] [-1/6*((2*b^3*x^2 - 7*b^2*x + 3*b)*sqrt(-b*x + 2)*sqrt(x) + 3*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^2, -1/6*((2*b^3*x^2 - 7*b^2*x + 3*b)*sqrt(-b*x + 2)*sqrt(x) + 6*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))))/b^2]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(3/2)*x^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of $[1,0, \sqrt{4, [1,1]} + \sqrt{4, [1,0]} + \sqrt{-4, [0,1]} + \sqrt{-8, [0,0]}, 0, \sqrt{6, [2,2]} + \sqrt{4, [2,1]} + \sqrt{6, [2,0]} + \sqrt{-4, [1,2]} + \sqrt{-28, [1,1]} + \sqrt{-8, [1,0]} + \sqrt{6, [0,2]} + \sqrt{8, [0,1]} + \sqrt{24, [0,0]}, 0, \sqrt{4, [3,3]} + \sqrt{-4, [3,2]} + \sqrt{-4, [3,1]} + \sqrt{4, [3,0]} + \sqrt{4, [2,3]} + \sqrt{-64, [2,2]} + \sqrt{20, [2,1]} + \sqrt{8, [2,0]} + \sqrt{-4, [1,3]} + \sqrt{-20, [1,2]} + \sqrt{128, [1,1]} + \sqrt{-16, [1,0]} + \sqrt{-4, [0,3]} + \sqrt{8, [0,2]} + \sqrt{16, [0,1]} + \sqrt{-32, [0,0]}, 0, \sqrt{1, [4,4]} + \sqrt{-4, [4,3]} + \sqrt{6, [4,2]} + \sqrt{-4, [4,1]} + \sqrt{1, [4,0]} + \sqrt{4, [3,4]} + \sqrt{-12, [3,3]} + \sqrt{20, [3,2]} + \sqrt{-20, [3,1]} + \sqrt{8, [3,0]} + \sqrt{6, [2,4]} + \sqrt{-20, [2,3]} + \sqrt{46, [2,2]} + \sqrt{-40, [2,1]} + \sqrt{24, [2,0]} + \sqrt{4, [1,4]} + \sqrt{-20, [1,3]} + \sqrt{40, [1,2]} + \sqrt{-48, [1,1]} + \sqrt{32, [1,0]} + \sqrt{1, [0,4]} + \sqrt{-8, [0,3]} + \sqrt{24, [0,2]} + \sqrt{-32, [0,1]} + \sqrt{16, [0,0]}}$ at parameters values $[-18.2719481629, 8.05231268331]$ Warning, choosing root of $[1,0, \sqrt{4, [1,1]} + \sqrt{4, [1,0]} + \sqrt{-4, [0,1]} + \sqrt{-8, [0,0]}, 0, \sqrt{6, [2,2]} + \sqrt{4, [2,1]} + \sqrt{6, [2,0]} + \sqrt{-4, [1,2]} + \sqrt{-28, [1,1]} + \sqrt{-8, [1,0]} + \sqrt{6, [0,2]} + \sqrt{8, [0,1]} + \sqrt{24, [0,0]}, 0, \sqrt{4, [3,3]} + \sqrt{-4, [3,2]} + \sqrt{-4, [3,1]} + \sqrt{4, [3,0]} + \sqrt{4, [2,3]} + \sqrt{-64, [2,2]} + \sqrt{20, [2,1]} + \sqrt{8, [2,0]} + \sqrt{-4, [1,3]} + \sqrt{-20, [1,2]} + \sqrt{128, [1,1]} + \sqrt{-16, [1,0]} + \sqrt{-4, [0,3]} + \sqrt{8, [0,2]} + \sqrt{16, [0,1]} + \sqrt{-32, [0,0]}, 0, \sqrt{1, [4,4]} + \sqrt{-4, [4,3]} + \sqrt{6, [4,2]} + \sqrt{-4, [4,1]} + \sqrt{1, [4,0]} + \sqrt{4, [3,4]} + \sqrt{-12, [3,3]} + \sqrt{20, [3,2]} + \sqrt{-20, [3,1]} + \sqrt{8, [3,0]} + \sqrt{6, [2,4]} + \sqrt{-20, [2,3]} + \sqrt{46, [2,2]} + \sqrt{-40, [2,1]} + \sqrt{24, [2,0]} + \sqrt{4, [1,4]} + \sqrt{-20, [1,3]} + \sqrt{40, [1,2]} + \sqrt{-48, [1,1]} + \sqrt{32, [1,0]} + \sqrt{1, [0,4]} + \sqrt{-8, [0,3]} + \sqrt{24, [0,2]} + \sqrt{-32, [0,1]} + \sqrt{16, [0,0]}}$ at parameters values $[-36.6004387327, 28.4266860783]$ Warning, choosing root of $[1,0, \sqrt{4, [1,1]} + \sqrt{4, [1,0]} + \sqrt{-4, [0,1]} + \sqrt{-8, [0,0]}, 0, \sqrt{6, [2,2]} + \sqrt{4, [2,1]} + \sqrt{6, [2,0]} + \sqrt{-4, [1,2]} + \sqrt{-28, [1,1]} + \sqrt{-8, [1,0]} + \sqrt{6, [0,2]} + \sqrt{8, [0,1]} + \sqrt{24, [0,0]}, 0, \sqrt{4, [3,3]} + \sqrt{-4, [3,2]} + \sqrt{-4, [3,1]} + \sqrt{4, [3,0]} + \sqrt{4, [2,3]} + \sqrt{-64, [2,2]} + \sqrt{20, [2,1]} + \sqrt{8, [2,0]} + \sqrt{-4, [1,3]} + \sqrt{-20, [1,2]} + \sqrt{128, [1,1]} + \sqrt{-16, [1,0]} + \sqrt{-4, [0,3]} + \sqrt{8, [0,2]} + \sqrt{16, [0,1]} + \sqrt{-32, [0,0]}, 0, \sqrt{1, [4,4]} + \sqrt{-4, [4,3]} + \sqrt{6, [4,2]} + \sqrt{-4, [4,1]} + \sqrt{1, [4,0]} + \sqrt{4, [3,4]} + \sqrt{-12, [3,3]} + \sqrt{20, [3,2]} + \sqrt{-20, [3,1]} + \sqrt{8, [3,0]} + \sqrt{6, [2,4]} + \sqrt{-20, [2,3]} + \sqrt{46, [2,2]} + \sqrt{-40, [2,1]} + \sqrt{24, [2,0]} + \sqrt{4, [1,4]} + \sqrt{-20, [1,3]} + \sqrt{40, [1,2]} + \sqrt{-48, [1,1]} + \sqrt{32, [1,0]} + \sqrt{1, [0,4]} + \sqrt{-8, [0,3]} + \sqrt{24, [0,2]} + \sqrt{-32, [0,1]} + \sqrt{16, [0,0]}}$

$\{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values $[-61.8196598012, 96.7771189027]$ Warning, choosing root of $\{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values $[-5.40303052077, 66.1769613782]$ Warning, choosing root of $\{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values $[-61.0171700171, 94.1262030317]$ Warning, choosing root of $\{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values $[-12.7113713701, 17.6881634681]$ $1/b * (-2*b^2*abs(b)/b^2 * (2*((12*b^5/144/b^7*\sqrt{-b*x+2})*\sqrt{-b*x+2}) - 78*b^5/144/$

$b^7 \sqrt{-bx+2} \sqrt{-bx+2} + 198b^5/144/b^7 \sqrt{-bx+2} \sqrt{-b(-bx+2)+2b} - 5/2/b/\sqrt{-b} \ln(\text{abs}(\sqrt{-b(-bx+2)+2b} - \sqrt{-b} \sqrt{-bx+2}))$
 $- 8b \text{abs}(b)/b^2/b * (2 * (1/8 \sqrt{-bx+2} \sqrt{-bx+2} - 5/8) \sqrt{-bx+2} \sqrt{-b(-bx+2)+2b} + 6*b/4/\sqrt{-b} \ln(\text{abs}(\sqrt{-b(-bx+2)+2b} - \sqrt{-b} \sqrt{-bx+2})))$
 $- 8 \text{abs}(b)/b^2 * (1/2 \sqrt{-bx+2} \sqrt{-b(-bx+2)+2b} - 2*b/2/\sqrt{-b} \ln(\text{abs}(\sqrt{-b(-bx+2)+2b} - \sqrt{-b} \sqrt{-bx+2})))$

maple [A] time = 0.00, size = 94, normalized size = 1.12

$$\frac{(-bx+2)^{\frac{3}{2}} x^{\frac{3}{2}}}{3} + \frac{\sqrt{-bx+2} x^{\frac{3}{2}}}{2} - \frac{\sqrt{-bx+2} \sqrt{x}}{2b} + \frac{\sqrt{-bx+2} x \arctan\left(\frac{(x-\frac{1}{b})\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{2\sqrt{-bx+2} b^{\frac{3}{2}} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+2)^(3/2)*x^(1/2), x)

[Out] $1/3 x^{3/2} (-bx+2)^{3/2} + 1/2 (-bx+2)^{1/2} x^{3/2} - 1/2 (-bx+2)^{1/2} / b x^{1/2} + 1/2 ((-bx+2)x)^{1/2} / (-bx+2)^{1/2} / b^{3/2} / x^{1/2} * \arctan((x-1/b) / (-bx^2+2x)^{1/2} * b^{1/2})$

maxima [A] time = 3.04, size = 115, normalized size = 1.37

$$\frac{\frac{3\sqrt{-bx+2}b^2}{\sqrt{x}} + \frac{8(-bx+2)^{\frac{3}{2}}b}{x^{\frac{3}{2}}} - \frac{3(-bx+2)^{\frac{5}{2}}}{x^{\frac{5}{2}}}}{3\left(b^4 - \frac{3(bx-2)b^3}{x} + \frac{3(bx-2)^2b^2}{x^2} - \frac{(bx-2)^3b}{x^3}\right)} - \frac{\arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(3/2)*x^(1/2), x, algorithm="maxima")

[Out] $1/3 * (3 \sqrt{-bx+2} * b^2 / \sqrt{x} + 8 * (-bx+2)^{3/2} * b / x^{3/2} - 3 * (-bx+2)^{5/2} / x^{5/2}) / (b^4 - 3 * (bx-2) * b^3 / x + 3 * (bx-2)^2 * b^2 / x^2 - (bx-2)^3 * b / x^3) - \arctan(\sqrt{-bx+2} / (\sqrt{b} * \sqrt{x})) / b^{3/2}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{x} (2 - bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)*(2 - b*x)^(3/2), x)

[Out] int(x^(1/2)*(2 - b*x)^(3/2), x)

sympy [A] time = 4.78, size = 199, normalized size = 2.37

$$\left\{ \begin{array}{l} -\frac{ib^2x^{\frac{7}{2}}}{3\sqrt{bx-2}} + \frac{11ibx^{\frac{5}{2}}}{6\sqrt{bx-2}} - \frac{17ix^{\frac{3}{2}}}{6\sqrt{bx-2}} + \frac{i\sqrt{x}}{b\sqrt{bx-2}} - \frac{i\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}} \\ \frac{b^2x^{\frac{7}{2}}}{3\sqrt{-bx+2}} - \frac{11bx^{\frac{5}{2}}}{6\sqrt{-bx+2}} + \frac{17x^{\frac{3}{2}}}{6\sqrt{-bx+2}} - \frac{\sqrt{x}}{b\sqrt{-bx+2}} + \frac{\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}} \end{array} \right. \begin{array}{l} \text{for } \frac{|bx|}{2} > 1 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)**(3/2)*x**(1/2),x)

[Out] Piecewise((-I*b**2*x**(7/2)/(3*sqrt(b*x - 2)) + 11*I*b*x**(5/2)/(6*sqrt(b*x - 2)) - 17*I*x**(3/2)/(6*sqrt(b*x - 2)) + I*sqrt(x)/(b*sqrt(b*x - 2)) - I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2), Abs(b*x)/2 > 1), (b**2*x**(7/2)/(3*sqrt(-b*x + 2)) - 11*b*x**(5/2)/(6*sqrt(-b*x + 2)) + 17*x**(3/2)/(6*sqrt(-b*x + 2)) - sqrt(x)/(b*sqrt(-b*x + 2)) + asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2), True))

$$3.542 \quad \int \frac{(2-bx)^{3/2}}{\sqrt{x}} dx$$

Optimal. Leaf size=63

$$\frac{1}{2}\sqrt{x}(2-bx)^{3/2} + \frac{3}{2}\sqrt{x}\sqrt{2-bx} + \frac{3\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

[Out] 3*arcsin(1/2*b^(1/2)*x^(1/2)*2^(1/2))/b^(1/2)+1/2*(-b*x+2)^(3/2)*x^(1/2)+3/2*x^(1/2)*(-b*x+2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$\frac{1}{2}\sqrt{x}(2-bx)^{3/2} + \frac{3}{2}\sqrt{x}\sqrt{2-bx} + \frac{3\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[(2 - b*x)^(3/2)/Sqrt[x], x]

[Out] (3*Sqrt[x]*Sqrt[2 - b*x])/2 + (Sqrt[x]*(2 - b*x)^(3/2))/2 + (3*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(2-bx)^{3/2}}{\sqrt{x}} dx &= \frac{1}{2} \sqrt{x} (2-bx)^{3/2} + \frac{3}{2} \int \frac{\sqrt{2-bx}}{\sqrt{x}} dx \\
&= \frac{3}{2} \sqrt{x} \sqrt{2-bx} + \frac{1}{2} \sqrt{x} (2-bx)^{3/2} + \frac{3}{2} \int \frac{1}{\sqrt{x} \sqrt{2-bx}} dx \\
&= \frac{3}{2} \sqrt{x} \sqrt{2-bx} + \frac{1}{2} \sqrt{x} (2-bx)^{3/2} + 3 \operatorname{Subst} \left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x} \right) \\
&= \frac{3}{2} \sqrt{x} \sqrt{2-bx} + \frac{1}{2} \sqrt{x} (2-bx)^{3/2} + \frac{3 \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 49, normalized size = 0.78

$$\frac{3 \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}} - \frac{1}{2} \sqrt{x} \sqrt{2-bx} (bx-5)$$

Antiderivative was successfully verified.

[In] Integrate[(2 - b*x)^(3/2)/Sqrt[x], x]

[Out] -1/2*(Sqrt[x]*Sqrt[2 - b*x]*(-5 + b*x)) + (3*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

fricas [A] time = 0.46, size = 107, normalized size = 1.70

$$\left[\frac{(b^2x - 5b)\sqrt{-bx + 2}\sqrt{x} + 3\sqrt{-b} \log(-bx + \sqrt{-bx + 2}\sqrt{-b}\sqrt{x} + 1)}{2b}, -\frac{(b^2x - 5b)\sqrt{-bx + 2}\sqrt{x} + 6\sqrt{b} \arctan(\sqrt{-bx + 2}/(\sqrt{b}\sqrt{x}))}{2b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(3/2)/x^(1/2), x, algorithm="fricas")

[Out] [-1/2*((b^2*x - 5*b)*sqrt(-b*x + 2)*sqrt(x) + 3*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b, -1/2*((b^2*x - 5*b)*sqrt(-b*x + 2)*sqrt(x) + 6*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))))/b]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((-b*x+2)^(3/2)/x^(1/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-15.6438432182,61.7937478349]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-29.292030761,78.6493344628]1/abs(b)*b^2/b*(2*(1/4/b*sqrt(-b*x+2)*sqrt(-b*x+2)+3/4/b)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)+3/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b)-sqrt(-b)*sqrt(-b*x+2))))
```

maple [A] time = 0.00, size = 78, normalized size = 1.24

$$\frac{(-bx+2)^{\frac{3}{2}}\sqrt{x}}{2} + \frac{3\sqrt{-bx+2}\sqrt{x}}{2} + \frac{3\sqrt{-bx+2}x \arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{2\sqrt{-bx+2}\sqrt{b}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((-b*x+2)^(3/2)/x^(1/2),x)
```

[Out] $\frac{1}{2}(-bx+2)^{3/2}x^{1/2} + \frac{3}{2}(-bx+2)^{1/2}x^{1/2} + \frac{3}{2}((-bx+2)x)^{1/2} / (-bx+2)^{1/2} / b^{1/2} / x^{1/2} \arctan((x-1/b) / (-bx^2+2x)^{1/2} * b^{1/2})$

maxima [A] time = 2.98, size = 79, normalized size = 1.25

$$-\frac{3 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{b}} + \frac{\frac{3\sqrt{-bx+2}b}{\sqrt{x}} + \frac{5(-bx+2)^{\frac{3}{2}}}{x^2}}{b^2 - \frac{2(bx-2)b}{x} + \frac{(bx-2)^2}{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+2)^(3/2)/x^(1/2),x, algorithm="maxima")`

[Out] $-3\arctan(\sqrt{-bx+2}/(\sqrt{b}\sqrt{x}))/\sqrt{b} + (3\sqrt{-bx+2}b/\sqrt{x} + 5(-bx+2)^{3/2}/x^2)/(b^2 - 2(bx-2)b/x + (bx-2)^2/x^2)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(2-bx)^{3/2}}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((2 - b*x)^(3/2)/x^(1/2), x)`

[Out] `int((2 - b*x)^(3/2)/x^(1/2), x)`

sympy [A] time = 2.86, size = 167, normalized size = 2.65

$$\begin{cases} -\frac{ib^2x^{\frac{5}{2}}}{2\sqrt{bx-2}} + \frac{7ibx^{\frac{3}{2}}}{2\sqrt{bx-2}} - \frac{5i\sqrt{x}}{\sqrt{bx-2}} - \frac{3i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}} & \text{for } \frac{|bx|}{2} > 1 \\ \frac{b^2x^{\frac{5}{2}}}{2\sqrt{-bx+2}} - \frac{7bx^{\frac{3}{2}}}{2\sqrt{-bx+2}} + \frac{5\sqrt{x}}{\sqrt{-bx+2}} + \frac{3 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+2)**(3/2)/x**(1/2),x)`

[Out] `Piecewise((-I*b**2*x**(5/2)/(2*sqrt(b*x - 2)) + 7*I*b*x**(3/2)/(2*sqrt(b*x - 2)) - 5*I*sqrt(x)/sqrt(b*x - 2) - 3*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/sqrt(b), Abs(b*x)/2 > 1), (b**2*x**(5/2)/(2*sqrt(-b*x + 2)) - 7*b*x**(3/2)/(2*sqrt(-b*x + 2)) + 5*sqrt(x)/sqrt(-b*x + 2) + 3*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/sqrt(b), True))`

$$3.543 \quad \int \frac{(2-bx)^{3/2}}{x^{3/2}} dx$$

Optimal. Leaf size=60

$$-\frac{2(2-bx)^{3/2}}{\sqrt{x}} - 3b\sqrt{x}\sqrt{2-bx} - 6\sqrt{b}\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)$$

[Out] $-6*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})*b^{(1/2)}-2*(-b*x+2)^{(3/2)}/x^{(1/2)}-3*b*x^{(1/2)}*(-b*x+2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {47, 50, 54, 216}

$$-\frac{2(2-bx)^{3/2}}{\sqrt{x}} - 3b\sqrt{x}\sqrt{2-bx} - 6\sqrt{b}\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(2 - b*x)^{(3/2)}/x^{(3/2)}, x]$

[Out] $-3*b*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x] - (2*(2 - b*x)^{(3/2)})/\text{Sqrt}[x] - 6*\text{Sqrt}[b]*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]]$

Rule 47

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \text{Dist}[(d*n)/(b*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54


```
Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(2-bx)^{3/2}}{x^{3/2}} dx &= -\frac{2(2-bx)^{3/2}}{\sqrt{x}} - (3b) \int \frac{\sqrt{2-bx}}{\sqrt{x}} dx \\
&= -3b\sqrt{x}\sqrt{2-bx} - \frac{2(2-bx)^{3/2}}{\sqrt{x}} - (3b) \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx \\
&= -3b\sqrt{x}\sqrt{2-bx} - \frac{2(2-bx)^{3/2}}{\sqrt{x}} - (6b) \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right) \\
&= -3b\sqrt{x}\sqrt{2-bx} - \frac{2(2-bx)^{3/2}}{\sqrt{x}} - 6\sqrt{b} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 28, normalized size = 0.47

$$-\frac{4\sqrt{2} {}_2F_1\left(-\frac{3}{2}, -\frac{1}{2}; \frac{1}{2}; \frac{bx}{2}\right)}{\sqrt{x}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(2 - b*x)^(3/2)/x^(3/2), x]
```

```
[Out] (-4*Sqrt[2]*Hypergeometric2F1[-3/2, -1/2, 1/2, (b*x)/2])/Sqrt[x]
```

fricas [A] time = 0.46, size = 101, normalized size = 1.68

$$\left[\frac{3\sqrt{-b}x \log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1) - (bx+4)\sqrt{-bx+2}\sqrt{x}}{x}, \frac{6\sqrt{b}x \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) - (bx+4)\sqrt{-bx}}{x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(3/2)/x^(3/2),x, algorithm="fricas")

[Out] [(3*sqrt(-b)*x*log(-b*x + sqrt(-b*x + 2))*sqrt(-b)*sqrt(x) + 1) - (b*x + 4)*sqrt(-b*x + 2)*sqrt(x))/x, (6*sqrt(b)*x*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) - (b*x + 4)*sqrt(-b*x + 2)*sqrt(x))/x]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(3/2)/x^(3/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-15.6438432182,61.7937478349]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-29.292030761,78.6493344628]-b/abs(b)*b^2/b*(2*(-1/2*sqrt(-b*x+2))*sqrt(-b*x+2)+3)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)/(-b*(-b*x+2)+2*b)+6/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b)-sqrt(-b)*sqrt(-b*x+2))))

maple [B] time = 0.02, size = 97, normalized size = 1.62

$$-\frac{3\sqrt{-bx+2}x\sqrt{b}\arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{\sqrt{-bx+2}\sqrt{x}} + \frac{(b^2x^2+2bx-8)\sqrt{-bx+2}x}{\sqrt{-(bx-2)x}\sqrt{-bx+2}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-b*x+2)^(3/2)/x^(3/2),x)`

[Out] $(b^2x^2+2bx-8)/(-(bx-2)x)^{(1/2)}*((-bx+2)x)^{(1/2)}/(-bx+2)^{(1/2)}/x^{(1/2)}-3*((-bx+2)x)^{(1/2)}/(-bx+2)^{(1/2)}*b^{(1/2)}/x^{(1/2)}*\arctan((x-1/b)/(-bx^2+2x)^{(1/2)}*b^{(1/2)})$

maxima [A] time = 2.99, size = 63, normalized size = 1.05

$$6\sqrt{b}\arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) - \frac{4\sqrt{-bx+2}}{\sqrt{x}} - \frac{2\sqrt{-bx+2}b}{\left(b-\frac{bx-2}{x}\right)\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+2)^(3/2)/x^(3/2),x, algorithm="maxima")`

[Out] $6*\text{sqrt}(b)*\arctan(\text{sqrt}(-b*x+2)/(\text{sqrt}(b)*\text{sqrt}(x))) - 4*\text{sqrt}(-b*x+2)/\text{sqrt}(x) - 2*\text{sqrt}(-b*x+2)*b/((b-(b*x-2)/x)*\text{sqrt}(x))$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(2-bx)^{3/2}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((2-b*x)^(3/2)/x^(3/2),x)`

[Out] `int((2-b*x)^(3/2)/x^(3/2),x)`

sympy [A] time = 2.49, size = 160, normalized size = 2.67

$$\begin{cases} 6i\sqrt{b}\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right) - \frac{ib^2x^{\frac{3}{2}}}{\sqrt{bx-2}} - \frac{2ib\sqrt{x}}{\sqrt{bx-2}} + \frac{8i}{\sqrt{x}\sqrt{bx-2}} & \text{for } \frac{|bx|}{2} > 1 \\ -6\sqrt{b}\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right) + \frac{b^2x^{\frac{3}{2}}}{\sqrt{-bx+2}} + \frac{2b\sqrt{x}}{\sqrt{-bx+2}} - \frac{8}{\sqrt{x}\sqrt{-bx+2}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((-b*x+2)**(3/2)/x**(3/2),x)
```

```
[Out] Piecewise((6*I*sqrt(b)*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2) - I*b**2*x**(3/2)/s  
qrt(b*x - 2) - 2*I*b*sqrt(x)/sqrt(b*x - 2) + 8*I/(sqrt(x)*sqrt(b*x - 2)), A  
bs(b*x)/2 > 1), (-6*sqrt(b)*asin(sqrt(2)*sqrt(b)*sqrt(x)/2) + b**2*x**(3/2)  
/sqrt(-b*x + 2) + 2*b*sqrt(x)/sqrt(-b*x + 2) - 8/(sqrt(x)*sqrt(-b*x + 2)),  
True))
```

$$3.544 \quad \int \frac{(2-bx)^{3/2}}{x^{5/2}} dx$$

Optimal. Leaf size=62

$$2b^{3/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right) - \frac{2(2-bx)^{3/2}}{3x^{3/2}} + \frac{2b\sqrt{2-bx}}{\sqrt{x}}$$

[Out] $-2/3*(-b*x+2)^{(3/2)}/x^{(3/2)}+2*b^{(3/2)}*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})+2*b*(-b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 62, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {47, 54, 216}

$$2b^{3/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right) - \frac{2(2-bx)^{3/2}}{3x^{3/2}} + \frac{2b\sqrt{2-bx}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[(2 - b*x)^(3/2)/x^(5/2), x]

[Out] $(2*b*\text{Sqrt}[2 - b*x])/ \text{Sqrt}[x] - (2*(2 - b*x)^{(3/2)})/(3*x^{(3/2)}) + 2*b^{(3/2)}* \text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/ \text{Sqrt}[2]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(2-bx)^{3/2}}{x^{5/2}} dx &= -\frac{2(2-bx)^{3/2}}{3x^{3/2}} - b \int \frac{\sqrt{2-bx}}{x^{3/2}} dx \\
&= \frac{2b\sqrt{2-bx}}{\sqrt{x}} - \frac{2(2-bx)^{3/2}}{3x^{3/2}} + b^2 \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx \\
&= \frac{2b\sqrt{2-bx}}{\sqrt{x}} - \frac{2(2-bx)^{3/2}}{3x^{3/2}} + (2b^2) \text{Subst} \left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x} \right) \\
&= \frac{2b\sqrt{2-bx}}{\sqrt{x}} - \frac{2(2-bx)^{3/2}}{3x^{3/2}} + 2b^{3/2} \sin^{-1} \left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}} \right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.48

$$-\frac{4\sqrt{2} {}_2F_1\left(-\frac{3}{2}, -\frac{3}{2}; -\frac{1}{2}; \frac{bx}{2}\right)}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(2 - b*x)^(3/2)/x^(5/2), x]

[Out] (-4*Sqrt[2]*Hypergeometric2F1[-3/2, -3/2, -1/2, (b*x)/2])/(3*x^(3/2))

fricas [A] time = 0.48, size = 111, normalized size = 1.79

$$\left[\frac{3\sqrt{-b}bx^2 \log(-bx - \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1) + 4(2bx-1)\sqrt{-bx+2}\sqrt{x}}{3x^2}, -\frac{2\left(3b^{\frac{3}{2}}x^2 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) - 2(2bx-1)\sqrt{-bx+2}\sqrt{x}\right)}{3x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(3/2)/x^(5/2), x, algorithm="fricas")

[Out] [1/3*(3*sqrt(-b)*b*x^2*log(-b*x - sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1) + 4*(2*b*x - 1)*sqrt(-b*x + 2)*sqrt(x))/x^2, -2/3*(3*b^(3/2)*x^2*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) - 2*(2*b*x - 1)*sqrt(-b*x + 2)*sqrt(x))/x^2]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(3/2)/x^(5/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-15.6438432182,61.7937478349]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-29.292030761,78.6493344628] 1/abs(b)*b^2/b*(2*(-12*b^3/9*sqrt(-b*x+2)*sqrt(-b*x+2)+18*b^3/9)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)/(-b*(-b*x+2)+2*b)^2+2*b^2/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b)-sqrt(-b)*sqrt(-b*x+2))))

maple [B] time = 0.02, size = 98, normalized size = 1.58

$$\frac{\sqrt{-bx+2} x b^{\frac{3}{2}} \arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{\sqrt{-bx+2} \sqrt{x}} - \frac{4(2b^2x^2 - 5bx + 2)\sqrt{-bx+2}x}{3\sqrt{-(bx-2)x} \sqrt{-bx+2} x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+2)^(3/2)/x^(5/2),x)

[Out] -4/3*(2*b^2*x^2-5*b*x+2)/x^(3/2)/(-(b*x-2)*x)^(1/2)*((-b*x+2)*x)^(1/2)/(-b*

$$(x+2)^{(1/2)} + b^{(3/2)} \arctan\left(\frac{(x-1/b)/(-b*x^2+2*x)^{(1/2)} * b^{(1/2)}}{((-b*x+2)*x)^{(1/2)}/(-b*x+2)^{(1/2)}/x^{(1/2)}}\right)$$

maxima [A] time = 3.00, size = 49, normalized size = 0.79

$$-2b^{\frac{3}{2}} \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) + \frac{2\sqrt{-bx+2}b}{\sqrt{x}} - \frac{2(-bx+2)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(3/2)/x^(5/2),x, algorithm="maxima")

[Out] -2*b^(3/2)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) + 2*sqrt(-b*x + 2)*b/sqrt(x) - 2/3*(-b*x + 2)^(3/2)/x^(3/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(2-bx)^{3/2}}{x^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((2 - b*x)^(3/2)/x^(5/2), x)

[Out] int((2 - b*x)^(3/2)/x^(5/2), x)

sympy [C] time = 2.92, size = 182, normalized size = 2.94

$$\begin{cases} \frac{8b^{\frac{3}{2}}\sqrt{-1+\frac{2}{bx}}}{3} + ib^{\frac{3}{2}}\log\left(\frac{1}{bx}\right) - 2ib^{\frac{3}{2}}\log\left(\frac{1}{\sqrt{b}\sqrt{x}}\right) + 2b^{\frac{3}{2}}\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right) - \frac{4\sqrt{b}\sqrt{-1+\frac{2}{bx}}}{3x} & \text{for } \frac{2}{|bx|} > 1 \\ \frac{8ib^{\frac{3}{2}}\sqrt{1-\frac{2}{bx}}}{3} + ib^{\frac{3}{2}}\log\left(\frac{1}{bx}\right) - 2ib^{\frac{3}{2}}\log\left(\sqrt{1-\frac{2}{bx}} + 1\right) - \frac{4i\sqrt{b}\sqrt{1-\frac{2}{bx}}}{3x} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)**(3/2)/x**(5/2),x)

[Out] Piecewise((8*b**(3/2)*sqrt(-1 + 2/(b*x)))/3 + I*b**(3/2)*log(1/(b*x)) - 2*I*b**(3/2)*log(1/(sqrt(b)*sqrt(x))) + 2*b**(3/2)*asin(sqrt(2)*sqrt(b)*sqrt(x)/2) - 4*sqrt(b)*sqrt(-1 + 2/(b*x))/(3*x), 2/Abs(b*x) > 1), (8*I*b**(3/2)*sqrt(1 - 2/(b*x))/3 + I*b**(3/2)*log(1/(b*x)) - 2*I*b**(3/2)*log(sqrt(1 - 2/(b*x)) + 1) - 4*I*sqrt(b)*sqrt(1 - 2/(b*x))/(3*x), True))

3.545 $\int x^{5/2}(a + bx)^{5/2} dx$

Optimal. Leaf size=164

$$-\frac{5a^6 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{512b^{7/2}} + \frac{5a^5\sqrt{x}\sqrt{a+bx}}{512b^3} - \frac{5a^4x^{3/2}\sqrt{a+bx}}{768b^2} + \frac{a^3x^{5/2}\sqrt{a+bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a+bx} + \frac{1}{12}ax^{7/2}(a+bx)^{3/2}$$

[Out] $1/12*a*x^{(7/2)}*(b*x+a)^{(3/2)}+1/6*x^{(7/2)}*(b*x+a)^{(5/2)}-5/512*a^6*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(7/2)}-5/768*a^4*x^{(3/2)}*(b*x+a)^{(1/2)}/b^2+1/192*a^3*x^{(5/2)}*(b*x+a)^{(1/2)}/b+1/32*a^2*x^{(7/2)}*(b*x+a)^{(1/2)}+5/512*a^5*x^{(1/2)}*(b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.06, antiderivative size = 164, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$-\frac{5a^4x^{3/2}\sqrt{a+bx}}{768b^2} + \frac{5a^5\sqrt{x}\sqrt{a+bx}}{512b^3} - \frac{5a^6 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{512b^{7/2}} + \frac{a^3x^{5/2}\sqrt{a+bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a+bx} + \frac{1}{12}ax^{7/2}(a+bx)^{3/2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(5/2)}*(a + b*x)^{(5/2)}, x]$

[Out] $(5*a^5*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(512*b^3) - (5*a^4*x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/(768*b^2) + (a^3*x^{(5/2)}*\operatorname{Sqrt}[a + b*x])/(192*b) + (a^2*x^{(7/2)}*\operatorname{Sqrt}[a + b*x])/32 + (a*x^{(7/2)}*(a + b*x)^{(3/2)})/12 + (x^{(7/2)}*(a + b*x)^{(5/2)})/6 - (5*a^6*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(512*b^{(7/2)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

$\text{Int}[(a_ + (b_ \cdot)(x_)^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(1 \cdot \text{ArcTanh}[\text{Rt}[-b, 2] \cdot x] / \text{Rt}[a, 2]) / (\text{Rt}[a, 2] \cdot \text{Rt}[-b, 2]), x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[a/b] \ \&\& \ (\text{GtQ}[a, 0] \ || \ \text{LtQ}[b, 0])$

Rule 217

$\text{Int}[1/\text{Sqrt}[(a_ + (b_ \cdot)(x_)^2)], x_Symbol] \rightarrow \text{Subst}[\text{Int}[1/(1 - b \cdot x^2), x], x, x/\text{Sqrt}[a + b \cdot x^2]] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
 \int x^{5/2}(a+bx)^{5/2} dx &= \frac{1}{6}x^{7/2}(a+bx)^{5/2} + \frac{1}{12}(5a) \int x^{5/2}(a+bx)^{3/2} dx \\
 &= \frac{1}{12}ax^{7/2}(a+bx)^{3/2} + \frac{1}{6}x^{7/2}(a+bx)^{5/2} + \frac{1}{8}a^2 \int x^{5/2}\sqrt{a+bx} dx \\
 &= \frac{1}{32}a^2x^{7/2}\sqrt{a+bx} + \frac{1}{12}ax^{7/2}(a+bx)^{3/2} + \frac{1}{6}x^{7/2}(a+bx)^{5/2} + \frac{1}{64}a^3 \int \frac{x^{5/2}}{\sqrt{a+bx}} dx \\
 &= \frac{a^3x^{5/2}\sqrt{a+bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a+bx} + \frac{1}{12}ax^{7/2}(a+bx)^{3/2} + \frac{1}{6}x^{7/2}(a+bx)^{5/2} - \frac{(5a^4) \int \frac{x^{3/2}}{\sqrt{a+bx}} dx}{384b} \\
 &= -\frac{5a^4x^{3/2}\sqrt{a+bx}}{768b^2} + \frac{a^3x^{5/2}\sqrt{a+bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a+bx} + \frac{1}{12}ax^{7/2}(a+bx)^{3/2} + \frac{1}{6}x^{7/2}(a+bx)^{5/2} \\
 &= \frac{5a^5\sqrt{x}\sqrt{a+bx}}{512b^3} - \frac{5a^4x^{3/2}\sqrt{a+bx}}{768b^2} + \frac{a^3x^{5/2}\sqrt{a+bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a+bx} + \frac{1}{12}ax^{7/2}(a+bx)^{3/2} \\
 &= \frac{5a^5\sqrt{x}\sqrt{a+bx}}{512b^3} - \frac{5a^4x^{3/2}\sqrt{a+bx}}{768b^2} + \frac{a^3x^{5/2}\sqrt{a+bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a+bx} + \frac{1}{12}ax^{7/2}(a+bx)^{3/2} \\
 &= \frac{5a^5\sqrt{x}\sqrt{a+bx}}{512b^3} - \frac{5a^4x^{3/2}\sqrt{a+bx}}{768b^2} + \frac{a^3x^{5/2}\sqrt{a+bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a+bx} + \frac{1}{12}ax^{7/2}(a+bx)^{3/2} \\
 &= \frac{5a^5\sqrt{x}\sqrt{a+bx}}{512b^3} - \frac{5a^4x^{3/2}\sqrt{a+bx}}{768b^2} + \frac{a^3x^{5/2}\sqrt{a+bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a+bx} + \frac{1}{12}ax^{7/2}(a+bx)^{3/2}
 \end{aligned}$$

Mathematica [A] time = 0.24, size = 118, normalized size = 0.72

$$\frac{\sqrt{a+bx} \left(\sqrt{b} \sqrt{x} (15a^5 - 10a^4bx + 8a^3b^2x^2 + 432a^2b^3x^3 + 640ab^4x^4 + 256b^5x^5) - \frac{15a^{11/2} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{\frac{bx}{a}+1}} \right)}{1536b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*(a + b*x)^(5/2), x]

[Out] (Sqrt[a + b*x]*(Sqrt[b]*Sqrt[x]*(15*a^5 - 10*a^4*b*x + 8*a^3*b^2*x^2 + 432*a^2*b^3*x^3 + 640*a*b^4*x^4 + 256*b^5*x^5) - (15*a^(11/2)*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 + (b*x)/a]))/(1536*b^(7/2))

fricas [A] time = 0.49, size = 206, normalized size = 1.26

$$\left[\frac{15a^6\sqrt{b} \log(2bx - 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(256b^6x^5 + 640ab^5x^4 + 432a^2b^4x^3 + 8a^3b^3x^2 - 10a^4b^2x + 15a^5b)}{3072b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^(5/2), x, algorithm="fricas")

[Out] [1/3072*(15*a^6*sqrt(b)*log(2*b*x - 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(256*b^6*x^5 + 640*a*b^5*x^4 + 432*a^2*b^4*x^3 + 8*a^3*b^3*x^2 - 10*a^4*b^2*x + 15*a^5*b)*sqrt(b*x + a)*sqrt(x))/b^4, 1/1536*(15*a^6*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) + (256*b^6*x^5 + 640*a*b^5*x^4 + 432*a^2*b^4*x^3 + 8*a^3*b^3*x^2 - 10*a^4*b^2*x + 15*a^5*b)*sqrt(b*x + a)*sqrt(x))/b^4]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+a)^(5/2), x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.00, size = 156, normalized size = 0.95

$$\frac{5\sqrt{(bx+a)x} a^6 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{1024\sqrt{bx+a} b^{\frac{7}{2}}\sqrt{x}} - \frac{5\sqrt{bx+a} a^5\sqrt{x}}{512b^3} - \frac{5(bx+a)^{\frac{3}{2}} a^4\sqrt{x}}{768b^3} + \frac{(bx+a)^{\frac{7}{2}} x^{\frac{5}{2}}}{6b} - \frac{(bx+a)^{\frac{5}{2}} a^3\sqrt{x}}{192b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{5/2}*(b*x+a)^{5/2}, x)$

[Out] $\frac{1}{6}b*x^{5/2}*(b*x+a)^{7/2} - \frac{1}{12}a/b^2*x^{3/2}*(b*x+a)^{7/2} + \frac{1}{32}a^2/b^3*x^{1/2}*(b*x+a)^{7/2} - \frac{1}{192}a^3/b^3*(b*x+a)^{5/2}*x^{1/2} - \frac{5}{768}a^4/b^3*(b*x+a)^{3/2}*x^{1/2} - \frac{5}{512}a^5*x^{1/2}*(b*x+a)^{1/2}/b^3 - \frac{5}{1024}a^6/b^{7/2}*((b*x+a)*x)^{1/2}/(b*x+a)^{1/2}/x^{1/2}*\ln((b*x+1/2*a)/b^{1/2}+(b*x^2+a*x)^{1/2})$

maxima [B] time = 2.99, size = 244, normalized size = 1.49

$$\frac{5a^6 \log\left(\frac{\sqrt{b}-\sqrt{bx+a}}{\sqrt{b}+\sqrt{bx+a}}\right)}{1024b^{\frac{7}{2}}} + \frac{\frac{15\sqrt{bx+a}a^6b^5}{\sqrt{x}} - \frac{85(bx+a)^{\frac{3}{2}}a^6b^4}{x^2} + \frac{198(bx+a)^{\frac{5}{2}}a^6b^3}{x^2} + \frac{198(bx+a)^{\frac{7}{2}}a^6b^2}{x^2} - \frac{85(bx+a)^{\frac{9}{2}}a^6b}{x^2} + \frac{15(bx+a)^{\frac{11}{2}}a^6}{x^2}}{1536\left(b^9 - \frac{6(bx+a)b^8}{x} + \frac{15(bx+a)^2b^7}{x^2} - \frac{20(bx+a)^3b^6}{x^3} + \frac{15(bx+a)^4b^5}{x^4} - \frac{6(bx+a)^5b^4}{x^5} + \frac{(bx+a)^6b^3}{x^6}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{5/2}*(b*x+a)^{5/2}, x, \text{algorithm}="maxima")$

[Out] $\frac{5}{1024}a^6*\log(-(\text{sqrt}(b) - \text{sqrt}(b*x + a))/\text{sqrt}(x))/(\text{sqrt}(b) + \text{sqrt}(b*x + a)/\text{sqrt}(x)))/b^{7/2} + \frac{1}{1536}*(15*\text{sqrt}(b*x + a)*a^6*b^5/\text{sqrt}(x) - 85*(b*x + a)^{3/2}*a^6*b^4/x^{3/2} + 198*(b*x + a)^{5/2}*a^6*b^3/x^{5/2} + 198*(b*x + a)^{7/2}*a^6*b^2/x^{7/2} - 85*(b*x + a)^{9/2}*a^6*b/x^{9/2} + 15*(b*x + a)^{11/2}*a^6/x^{11/2})/(b^9 - 6*(b*x + a)*b^8/x + 15*(b*x + a)^2*b^7/x^2 - 20*(b*x + a)^3*b^6/x^3 + 15*(b*x + a)^4*b^5/x^4 - 6*(b*x + a)^5*b^4/x^5 + (b*x + a)^6*b^3/x^6)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} (a + bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{5/2}*(a + b*x)^{5/2}, x)$

[Out] $\text{int}(x^{5/2}*(a + b*x)^{5/2}, x)$

sympy [A] time = 25.94, size = 207, normalized size = 1.26

$$\frac{5a^{\frac{11}{2}}\sqrt{x}}{512b^3\sqrt{1+\frac{bx}{a}}} + \frac{5a^{\frac{9}{2}}x^{\frac{3}{2}}}{1536b^2\sqrt{1+\frac{bx}{a}}} - \frac{a^{\frac{7}{2}}x^{\frac{5}{2}}}{768b\sqrt{1+\frac{bx}{a}}} + \frac{55a^{\frac{5}{2}}x^{\frac{7}{2}}}{192\sqrt{1+\frac{bx}{a}}} + \frac{67a^{\frac{3}{2}}bx^{\frac{9}{2}}}{96\sqrt{1+\frac{bx}{a}}} + \frac{7\sqrt{a}b^2x^{\frac{11}{2}}}{12\sqrt{1+\frac{bx}{a}}} - \frac{5a^6 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{512b^{\frac{7}{2}}} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(5/2)*(b*x+a)**(5/2),x)
```

```
[Out] 5*a**(11/2)*sqrt(x)/(512*b**3*sqrt(1 + b*x/a)) + 5*a**(9/2)*x**(3/2)/(1536*  
b**2*sqrt(1 + b*x/a)) - a**(7/2)*x**(5/2)/(768*b*sqrt(1 + b*x/a)) + 55*a**(  
5/2)*x**(7/2)/(192*sqrt(1 + b*x/a)) + 67*a**(3/2)*b*x**(9/2)/(96*sqrt(1 + b  
*x/a)) + 7*sqrt(a)*b**2*x**(11/2)/(12*sqrt(1 + b*x/a)) - 5*a**6*asinh(sqrt(  
b)*sqrt(x)/sqrt(a))/(512*b**(7/2)) + b**3*x**(13/2)/(6*sqrt(a)*sqrt(1 + b*x  
/a))
```

3.546 $\int x^{3/2}(a + bx)^{5/2} dx$

Optimal. Leaf size=140

$$\frac{3a^5 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{128b^{5/2}} - \frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^2} + \frac{a^3x^{3/2}\sqrt{a+bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a+bx} + \frac{1}{8}ax^{5/2}(a+bx)^{3/2} + \frac{1}{5}x^{5/2}(a+bx)^{5/2}$$

[Out] $1/8*a*x^{(5/2)}*(b*x+a)^{(3/2)}+1/5*x^{(5/2)}*(b*x+a)^{(5/2)}+3/128*a^5*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(5/2)}+1/64*a^3*x^{(3/2)}*(b*x+a)^{(1/2)}/b+1/16*a^2*x^{(5/2)}*(b*x+a)^{(1/2)}-3/128*a^4*x^{(1/2)}*(b*x+a)^{(1/2)}/b^2$

Rubi [A] time = 0.05, antiderivative size = 140, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$-\frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^2} + \frac{3a^5 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{128b^{5/2}} + \frac{a^3x^{3/2}\sqrt{a+bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a+bx} + \frac{1}{8}ax^{5/2}(a+bx)^{3/2} + \frac{1}{5}x^{5/2}(a+bx)^{5/2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(3/2)}*(a + b*x)^{(5/2)}, x]$

[Out] $(-3*a^4*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(128*b^2) + (a^3*x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/(64*b) + (a^2*x^{(5/2)}*\operatorname{Sqrt}[a + b*x])/16 + (a*x^{(5/2)}*(a + b*x)^{(3/2)})/8 + (x^{(5/2)}*(a + b*x)^{(5/2)})/5 + (3*a^5*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(128*b^{(5/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int x^{3/2}(a+bx)^{5/2} dx &= \frac{1}{5}x^{5/2}(a+bx)^{5/2} + \frac{1}{2}a \int x^{3/2}(a+bx)^{3/2} dx \\
 &= \frac{1}{8}ax^{5/2}(a+bx)^{3/2} + \frac{1}{5}x^{5/2}(a+bx)^{5/2} + \frac{1}{16}(3a^2) \int x^{3/2}\sqrt{a+bx} dx \\
 &= \frac{1}{16}a^2x^{5/2}\sqrt{a+bx} + \frac{1}{8}ax^{5/2}(a+bx)^{3/2} + \frac{1}{5}x^{5/2}(a+bx)^{5/2} + \frac{1}{32}a^3 \int \frac{x^{3/2}}{\sqrt{a+bx}} dx \\
 &= \frac{a^3x^{3/2}\sqrt{a+bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a+bx} + \frac{1}{8}ax^{5/2}(a+bx)^{3/2} + \frac{1}{5}x^{5/2}(a+bx)^{5/2} - \frac{(3a^4) \int \frac{\sqrt{x}}{\sqrt{a+bx}} dx}{128b} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^2} + \frac{a^3x^{3/2}\sqrt{a+bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a+bx} + \frac{1}{8}ax^{5/2}(a+bx)^{3/2} + \frac{1}{5}x^{5/2}(a+bx)^{5/2} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^2} + \frac{a^3x^{3/2}\sqrt{a+bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a+bx} + \frac{1}{8}ax^{5/2}(a+bx)^{3/2} + \frac{1}{5}x^{5/2}(a+bx)^{5/2} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^2} + \frac{a^3x^{3/2}\sqrt{a+bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a+bx} + \frac{1}{8}ax^{5/2}(a+bx)^{3/2} + \frac{1}{5}x^{5/2}(a+bx)^{5/2} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a+bx}}{128b^2} + \frac{a^3x^{3/2}\sqrt{a+bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a+bx} + \frac{1}{8}ax^{5/2}(a+bx)^{3/2} + \frac{1}{5}x^{5/2}(a+bx)^{5/2}
 \end{aligned}$$

Mathematica [A] time = 0.14, size = 107, normalized size = 0.76

$$\frac{\sqrt{a+bx} \left(\frac{15a^{9/2} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{\frac{bx}{a}+1}} + \sqrt{b}\sqrt{x} (-15a^4 + 10a^3bx + 248a^2b^2x^2 + 336ab^3x^3 + 128b^4x^4) \right)}{640b^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*(a + b*x)^(5/2),x]

[Out] (Sqrt[a + b*x]*(Sqrt[b]*Sqrt[x]*(-15*a^4 + 10*a^3*b*x + 248*a^2*b^2*x^2 + 36*a*b^3*x^3 + 128*b^4*x^4) + (15*a^(9/2)*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 + (b*x)/a]))/(640*b^(5/2))

fricas [A] time = 0.44, size = 185, normalized size = 1.32

$$\left[\frac{15 a^5 \sqrt{b} \log(2 b x + 2 \sqrt{b x + a} \sqrt{b} \sqrt{x} + a) + 2 (128 b^5 x^4 + 336 a b^4 x^3 + 248 a^2 b^3 x^2 + 10 a^3 b^2 x - 15 a^4 b) \sqrt{b x + a}}{1280 b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^(5/2),x, algorithm="fricas")

[Out] [1/1280*(15*a^5*sqrt(b)*log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(128*b^5*x^4 + 336*a*b^4*x^3 + 248*a^2*b^3*x^2 + 10*a^3*b^2*x - 15*a^4*b)*sqrt(b*x + a)*sqrt(x))/b^3, -1/640*(15*a^5*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) - (128*b^5*x^4 + 336*a*b^4*x^3 + 248*a^2*b^3*x^2 + 10*a^3*b^2*x - 15*a^4*b)*sqrt(b*x + a)*sqrt(x))/b^3]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^(5/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 138, normalized size = 0.99

$$\frac{3\sqrt{(bx+a)x} a^5 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{256\sqrt{bx+a} b^{\frac{5}{2}}\sqrt{x}} + \frac{3\sqrt{bx+a} a^4\sqrt{x}}{128b^2} + \frac{(bx+a)^{\frac{3}{2}} a^3\sqrt{x}}{64b^2} + \frac{(bx+a)^{\frac{5}{2}} a^2\sqrt{x}}{80b^2} + \frac{(bx+a)^{\frac{7}{2}} x^{\frac{3}{2}}}{5b} - 3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(b*x+a)^(5/2),x)

[Out] 1/5/b*x^(3/2)*(b*x+a)^(7/2)-3/40*a/b^2*x^(1/2)*(b*x+a)^(7/2)+1/80*a^2/b^2*(b*x+a)^(5/2)*x^(1/2)+1/64*a^3/b^2*(b*x+a)^(3/2)*x^(1/2)+3/128*a^4*x^(1/2)*(b*x+a)^(1/2)/b^2+3/256*a^5/b^(5/2)*((b*x+a)*x)^(1/2)/(b*x+a)^(1/2)/x^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))

maxima [B] time = 2.98, size = 212, normalized size = 1.51

$$\frac{3 a^5 \log\left(-\frac{\sqrt{b}-\sqrt{bx+a}}{\sqrt{x}}\right)}{256 b^{\frac{5}{2}}}-\frac{\frac{15 \sqrt{bx+a} a^5 b^4}{\sqrt{x}}-\frac{70(bx+a)^{\frac{3}{2}} a^5 b^3}{x^{\frac{3}{2}}}+\frac{128(bx+a)^{\frac{5}{2}} a^5 b^2}{x^{\frac{5}{2}}}+\frac{70(bx+a)^{\frac{7}{2}} a^5 b}{x^{\frac{7}{2}}}-\frac{15(bx+a)^{\frac{9}{2}} a^5}{x^{\frac{9}{2}}}}{640\left(b^7-\frac{5(bx+a)b^6}{x}+\frac{10(bx+a)^2 b^5}{x^2}-\frac{10(bx+a)^3 b^4}{x^3}+\frac{5(bx+a)^4 b^3}{x^4}-\frac{(bx+a)^5 b^2}{x^5}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^(5/2),x, algorithm="maxima")

[Out] $-3/256*a^5*\log(-(\text{sqrt}(b) - \text{sqrt}(b*x + a))/\text{sqrt}(x))/(\text{sqrt}(b) + \text{sqrt}(b*x + a)/\text{sqrt}(x)))/b^{(5/2)} - 1/640*(15*\text{sqrt}(b*x + a)*a^5*b^4/\text{sqrt}(x) - 70*(b*x + a)^{(3/2)}*a^5*b^3/x^{(3/2)} + 128*(b*x + a)^{(5/2)}*a^5*b^2/x^{(5/2)} + 70*(b*x + a)^{(7/2)}*a^5*b/x^{(7/2)} - 15*(b*x + a)^{(9/2)}*a^5/x^{(9/2)})/(b^7 - 5*(b*x + a)*b^6/x + 10*(b*x + a)^2*b^5/x^2 - 10*(b*x + a)^3*b^4/x^3 + 5*(b*x + a)^4*b^3/x^4 - (b*x + a)^5*b^2/x^5)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} (a + bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(a + b*x)^(5/2),x)

[Out] int(x^(3/2)*(a + b*x)^(5/2), x)

sympy [A] time = 16.41, size = 180, normalized size = 1.29

$$-\frac{3a^{\frac{9}{2}}\sqrt{x}}{128b^2\sqrt{1+\frac{bx}{a}}}-\frac{a^{\frac{7}{2}}x^{\frac{3}{2}}}{128b\sqrt{1+\frac{bx}{a}}}+\frac{129a^{\frac{5}{2}}x^{\frac{5}{2}}}{320\sqrt{1+\frac{bx}{a}}}+\frac{73a^{\frac{3}{2}}bx^{\frac{7}{2}}}{80\sqrt{1+\frac{bx}{a}}}+\frac{29\sqrt{a}b^2x^{\frac{9}{2}}}{40\sqrt{1+\frac{bx}{a}}}+\frac{3a^5\operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{128b^{\frac{5}{2}}}+\frac{b^3x^{\frac{11}{2}}}{5\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)*(b*x+a)**(5/2),x)

[Out] $-3*a^{(9/2)}*\text{sqrt}(x)/(128*b^{**2}*\text{sqrt}(1 + b*x/a)) - a^{(7/2)}*x^{(3/2)}/(128*b*s\text{qrt}(1 + b*x/a)) + 129*a^{(5/2)}*x^{(5/2)}/(320*\text{sqrt}(1 + b*x/a)) + 73*a^{(3/2)}*b*x^{(7/2)}/(80*\text{sqrt}(1 + b*x/a)) + 29*\text{sqrt}(a)*b^{**2}*x^{(9/2)}/(40*\text{sqrt}(1 + b*x/a)) + 3*a^{**5}*\operatorname{asinh}(\text{sqrt}(b)*\text{sqrt}(x)/\text{sqrt}(a))/(128*b^{**}(5/2)) + b^{**3}*x^{(11/2)}/(5*\text{sqrt}(a)*\text{sqrt}(1 + b*x/a))$

3.547 $\int \sqrt{x} (a + bx)^{5/2} dx$

Optimal. Leaf size=116

$$-\frac{5a^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{64b^{3/2}} + \frac{5a^3 \sqrt{x} \sqrt{a+bx}}{64b} + \frac{5}{32} a^2 x^{3/2} \sqrt{a+bx} + \frac{5}{24} a x^{3/2} (a+bx)^{3/2} + \frac{1}{4} x^{3/2} (a+bx)^{5/2}$$

[Out] $5/24*a*x^{(3/2)}*(b*x+a)^{(3/2)}+1/4*x^{(3/2)}*(b*x+a)^{(5/2)}-5/64*a^4*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(3/2)}+5/32*a^2*x^{(3/2)}*(b*x+a)^{(1/2)}+5/64*a^3*x^{(1/2)}*(b*x+a)^{(1/2)}/b$

Rubi [A] time = 0.04, antiderivative size = 116, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$-\frac{5a^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{64b^{3/2}} + \frac{5}{32} a^2 x^{3/2} \sqrt{a+bx} + \frac{5a^3 \sqrt{x} \sqrt{a+bx}}{64b} + \frac{5}{24} a x^{3/2} (a+bx)^{3/2} + \frac{1}{4} x^{3/2} (a+bx)^{5/2}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[x]*(a + b*x)^(5/2), x]`

[Out] $(5*a^3*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(64*b) + (5*a^2*x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/32 + (5*a*x^{(3/2)}*(a + b*x)^{(3/2)})/24 + (x^{(3/2)}*(a + b*x)^{(5/2)})/4 - (5*a^4*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(64*b^{(3/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \sqrt{x} (a + bx)^{5/2} dx &= \frac{1}{4} x^{3/2} (a + bx)^{5/2} + \frac{1}{8} (5a) \int \sqrt{x} (a + bx)^{3/2} dx \\
 &= \frac{5}{24} ax^{3/2} (a + bx)^{3/2} + \frac{1}{4} x^{3/2} (a + bx)^{5/2} + \frac{1}{16} (5a^2) \int \sqrt{x} \sqrt{a + bx} dx \\
 &= \frac{5}{32} a^2 x^{3/2} \sqrt{a + bx} + \frac{5}{24} ax^{3/2} (a + bx)^{3/2} + \frac{1}{4} x^{3/2} (a + bx)^{5/2} + \frac{1}{64} (5a^3) \int \frac{\sqrt{x}}{\sqrt{a + bx}} dx \\
 &= \frac{5a^3 \sqrt{x} \sqrt{a + bx}}{64b} + \frac{5}{32} a^2 x^{3/2} \sqrt{a + bx} + \frac{5}{24} ax^{3/2} (a + bx)^{3/2} + \frac{1}{4} x^{3/2} (a + bx)^{5/2} - \frac{(5a^4) \int \frac{\sqrt{x}}{\sqrt{a + bx}} dx}{12} \\
 &= \frac{5a^3 \sqrt{x} \sqrt{a + bx}}{64b} + \frac{5}{32} a^2 x^{3/2} \sqrt{a + bx} + \frac{5}{24} ax^{3/2} (a + bx)^{3/2} + \frac{1}{4} x^{3/2} (a + bx)^{5/2} - \frac{(5a^4) \operatorname{Subst}\left[\int \frac{\sqrt{x}}{\sqrt{a + bx}} dx, x, \frac{x}{\sqrt{a + bx}}\right]}{12} \\
 &= \frac{5a^3 \sqrt{x} \sqrt{a + bx}}{64b} + \frac{5}{32} a^2 x^{3/2} \sqrt{a + bx} + \frac{5}{24} ax^{3/2} (a + bx)^{3/2} + \frac{1}{4} x^{3/2} (a + bx)^{5/2} - \frac{(5a^4) \operatorname{Subst}\left[\int \frac{\sqrt{x}}{\sqrt{a + bx}} dx, x, \frac{x}{\sqrt{a + bx}}\right]}{12} \\
 &= \frac{5a^3 \sqrt{x} \sqrt{a + bx}}{64b} + \frac{5}{32} a^2 x^{3/2} \sqrt{a + bx} + \frac{5}{24} ax^{3/2} (a + bx)^{3/2} + \frac{1}{4} x^{3/2} (a + bx)^{5/2} - \frac{5a^4 \operatorname{tanh}^{-1}\left(\frac{\sqrt{bx}}{\sqrt{a}}\right)}{64}
 \end{aligned}$$

Mathematica [A] time = 0.20, size = 96, normalized size = 0.83

$$\frac{\sqrt{a + bx} \left(\sqrt{b} \sqrt{x} (15a^3 + 118a^2bx + 136ab^2x^2 + 48b^3x^3) - \frac{15a^{7/2} \sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{\frac{bx}{a} + 1}} \right)}{192b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*(a + b*x)^(5/2), x]

[Out] (Sqrt[a + b*x]*(Sqrt[b]*Sqrt[x]*(15*a^3 + 118*a^2*b*x + 136*a*b^2*x^2 + 48*b^3*x^3) - (15*a^(7/2)*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 + (b*x)/a]))/(192*b^(3/2))

fricas [A] time = 0.47, size = 162, normalized size = 1.40

$$\left[\frac{15 a^4 \sqrt{b} \log(2 b x - 2 \sqrt{b x + a} \sqrt{b} \sqrt{x} + a) + 2 (48 b^4 x^3 + 136 a b^3 x^2 + 118 a^2 b^2 x + 15 a^3 b) \sqrt{b x + a} \sqrt{x}}{384 b^2}, \frac{15 a^4 \sqrt{b}}{384 b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*x^(1/2),x, algorithm="fricas")

[Out] [1/384*(15*a^4*sqrt(b)*log(2*b*x - 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(48*b^4*x^3 + 136*a*b^3*x^2 + 118*a^2*b^2*x + 15*a^3*b)*sqrt(b*x + a)*sqrt(x))/b^2, 1/192*(15*a^4*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) + (48*b^4*x^3 + 136*a*b^3*x^2 + 118*a^2*b^2*x + 15*a^3*b)*sqrt(b*x + a)*sqrt(x))/b^2]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*x^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 111, normalized size = 0.96

$$\frac{5\sqrt{bx+a} a^2 x^{\frac{3}{2}}}{32} - \frac{5\sqrt{(bx+a)x} a^4 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{128\sqrt{bx+a} b^{\frac{3}{2}}\sqrt{x}} + \frac{5\sqrt{bx+a} a^3 \sqrt{x}}{64b} + \frac{5(bx+a)^{\frac{3}{2}} a x^{\frac{3}{2}}}{24} + \frac{(bx+a)^{\frac{5}{2}} x^{\frac{3}{2}}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)*x^(1/2),x)

[Out] 1/4*x^(3/2)*(b*x+a)^(5/2)+5/24*a*x^(3/2)*(b*x+a)^(3/2)+5/32*a^2*x^(3/2)*(b*x+a)^(1/2)+5/64*a^3*x^(1/2)*(b*x+a)^(1/2)/b-5/128*a^4/b^(3/2)*((b*x+a)*x)^(1/2)/x^(1/2)/(b*x+a)^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))

maxima [B] time = 2.98, size = 176, normalized size = 1.52

$$\frac{5a^4 \log\left(-\frac{\sqrt{b}-\sqrt{bx+a}}{\sqrt{b}+\sqrt{bx+a}}\right)}{128b^{\frac{3}{2}}} + \frac{\frac{15\sqrt{bx+a}a^4b^3}{\sqrt{x}} - \frac{55(bx+a)^{\frac{3}{2}}a^4b^2}{x^{\frac{3}{2}}} + \frac{73(bx+a)^{\frac{5}{2}}a^4b}{x^{\frac{5}{2}}} + \frac{15(bx+a)^{\frac{7}{2}}a^4}{x^{\frac{7}{2}}}}{192\left(b^5 - \frac{4(bx+a)b^4}{x} + \frac{6(bx+a)^2b^3}{x^2} - \frac{4(bx+a)^3b^2}{x^3} + \frac{(bx+a)^4b}{x^4}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*x^(1/2),x, algorithm="maxima")

[Out] $5/128*a^4*\log(-(\text{sqrt}(b) - \text{sqrt}(b*x + a))/\text{sqrt}(x))/(\text{sqrt}(b) + \text{sqrt}(b*x + a)/\text{sqrt}(x)))/b^{3/2} + 1/192*(15*\text{sqrt}(b*x + a)*a^4*b^3/\text{sqrt}(x) - 55*(b*x + a)^{(3/2)}*a^4*b^2/x^{3/2} + 73*(b*x + a)^{(5/2)}*a^4*b/x^{5/2} + 15*(b*x + a)^{(7/2)}*a^4/x^{7/2})/(b^5 - 4*(b*x + a)*b^4/x + 6*(b*x + a)^2*b^3/x^2 - 4*(b*x + a)^3*b^2/x^3 + (b*x + a)^4*b/x^4)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{x} (a + bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)*(a + b*x)^(5/2),x)

[Out] int(x^(1/2)*(a + b*x)^(5/2), x)

sympy [A] time = 9.86, size = 155, normalized size = 1.34

$$\frac{5a^{\frac{7}{2}}\sqrt{x}}{64b\sqrt{1+\frac{bx}{a}}} + \frac{133a^{\frac{5}{2}}x^{\frac{3}{2}}}{192\sqrt{1+\frac{bx}{a}}} + \frac{127a^{\frac{3}{2}}bx^{\frac{5}{2}}}{96\sqrt{1+\frac{bx}{a}}} + \frac{23\sqrt{a}b^2x^{\frac{7}{2}}}{24\sqrt{1+\frac{bx}{a}}} - \frac{5a^4 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{64b^{\frac{3}{2}}} + \frac{b^3x^{\frac{9}{2}}}{4\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)*x**(1/2),x)

[Out] $5*a^{7/2}*\text{sqrt}(x)/(64*b*\text{sqrt}(1 + b*x/a)) + 133*a^{5/2}*x^{3/2}/(192*\text{sqrt}(1 + b*x/a)) + 127*a^{3/2}*b*x^{5/2}/(96*\text{sqrt}(1 + b*x/a)) + 23*\text{sqrt}(a)*b^2*x^{7/2}/(24*\text{sqrt}(1 + b*x/a)) - 5*a^4*\operatorname{asinh}(\text{sqrt}(b)*\text{sqrt}(x)/\text{sqrt}(a))/(64*b^{3/2}) + b^3*x^{9/2}/(4*\text{sqrt}(a)*\text{sqrt}(1 + b*x/a))$

$$3.548 \quad \int \frac{(a+bx)^{5/2}}{\sqrt{x}} dx$$

Optimal. Leaf size=92

$$\frac{5a^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{8\sqrt{b}} + \frac{5}{8}a^2\sqrt{x}\sqrt{a+bx} + \frac{5}{12}a\sqrt{x}(a+bx)^{3/2} + \frac{1}{3}\sqrt{x}(a+bx)^{5/2}$$

[Out] $5/8*a^3*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(1/2)}+5/12*a*(b*x+a)^{(3/2)}*x^{(1/2)}+1/3*(b*x+a)^{(5/2)}*x^{(1/2)}+5/8*a^2*x^{(1/2)}*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$\frac{5}{8}a^2\sqrt{x}\sqrt{a+bx} + \frac{5a^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{8\sqrt{b}} + \frac{5}{12}a\sqrt{x}(a+bx)^{3/2} + \frac{1}{3}\sqrt{x}(a+bx)^{5/2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}/\operatorname{Sqrt}[x], x]$

[Out] $(5*a^2*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/8 + (5*a*\operatorname{Sqrt}[x]*(a + b*x)^{(3/2)})/12 + (\operatorname{Sqrt}[x]*(a + b*x)^{(5/2)})/3 + (5*a^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/(\operatorname{Sqrt}[a + b*x])])/(8*\operatorname{Sqrt}[b])$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{NeQ}[m + n + 1, 0]$ && $!(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] \mid\mid (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m - n, 0])))$ && $!\operatorname{ILtQ}[m + n + 2, 0]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{LtQ}[-1, m, 0]$ && $\operatorname{LeQ}[-1, n, 0]$ && $\operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 206

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{5/2}}{\sqrt{x}} dx &= \frac{1}{3} \sqrt{x} (a+bx)^{5/2} + \frac{1}{6} (5a) \int \frac{(a+bx)^{3/2}}{\sqrt{x}} dx \\
 &= \frac{5}{12} a \sqrt{x} (a+bx)^{3/2} + \frac{1}{3} \sqrt{x} (a+bx)^{5/2} + \frac{1}{8} (5a^2) \int \frac{\sqrt{a+bx}}{\sqrt{x}} dx \\
 &= \frac{5}{8} a^2 \sqrt{x} \sqrt{a+bx} + \frac{5}{12} a \sqrt{x} (a+bx)^{3/2} + \frac{1}{3} \sqrt{x} (a+bx)^{5/2} + \frac{1}{16} (5a^3) \int \frac{1}{\sqrt{x} \sqrt{a+bx}} dx \\
 &= \frac{5}{8} a^2 \sqrt{x} \sqrt{a+bx} + \frac{5}{12} a \sqrt{x} (a+bx)^{3/2} + \frac{1}{3} \sqrt{x} (a+bx)^{5/2} + \frac{1}{8} (5a^3) \text{Subst} \left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \frac{x}{\sqrt{x}} \right) \\
 &= \frac{5}{8} a^2 \sqrt{x} \sqrt{a+bx} + \frac{5}{12} a \sqrt{x} (a+bx)^{3/2} + \frac{1}{3} \sqrt{x} (a+bx)^{5/2} + \frac{1}{8} (5a^3) \text{Subst} \left(\int \frac{1}{1-bx^2} dx, x, \frac{x}{\sqrt{x}} \right) \\
 &= \frac{5}{8} a^2 \sqrt{x} \sqrt{a+bx} + \frac{5}{12} a \sqrt{x} (a+bx)^{3/2} + \frac{1}{3} \sqrt{x} (a+bx)^{5/2} + \frac{5a^3 \tanh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a+bx}} \right)}{8\sqrt{b}}
 \end{aligned}$$

Mathematica [A] time = 0.11, size = 80, normalized size = 0.87

$$\frac{1}{24} \sqrt{a+bx} \left(\frac{15a^{5/2} \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{b} \sqrt{\frac{bx}{a} + 1}} + \sqrt{x} (33a^2 + 26abx + 8b^2x^2) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/Sqrt[x], x]

[Out] (Sqrt[a + b*x]*(Sqrt[x]*(33*a^2 + 26*a*b*x + 8*b^2*x^2) + (15*a^(5/2)*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[b]*Sqrt[1 + (b*x)/a]))) / 24

fricas [A] time = 0.45, size = 141, normalized size = 1.53

$$\left[\frac{15 a^3 \sqrt{b} \log(2 b x + 2 \sqrt{b x + a} \sqrt{b} \sqrt{x} + a) + 2 (8 b^3 x^2 + 26 a b^2 x + 33 a^2 b) \sqrt{b x + a} \sqrt{x}}{48 b}, -\frac{15 a^3 \sqrt{-b} \arctan\left(\frac{\sqrt{b}}{\sqrt{x}}\right)}{48 b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^(1/2),x, algorithm="fricas")

[Out] [1/48*(15*a^3*sqrt(b)*log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(8*b^3*x^2 + 26*a*b^2*x + 33*a^2*b)*sqrt(b*x + a)*sqrt(x))/b, -1/24*(15*a^3*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) - (8*b^3*x^2 + 26*a*b^2*x + 33*a^2*b)*sqrt(b*x + a)*sqrt(x))/b]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 93, normalized size = 1.01

$$\frac{5\sqrt{bx+a} x a^3 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{16\sqrt{bx+a} \sqrt{b} \sqrt{x}} + \frac{5\sqrt{bx+a} a^2 \sqrt{x}}{8} + \frac{5(bx+a)^{\frac{3}{2}} a \sqrt{x}}{12} + \frac{(bx+a)^{\frac{5}{2}} \sqrt{x}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/x^(1/2),x)

[Out] 1/3*(b*x+a)^(5/2)*x^(1/2)+5/12*a*(b*x+a)^(3/2)*x^(1/2)+5/8*a^2*x^(1/2)*(b*x+a)^(1/2)+5/16*a^3*((b*x+a)*x)^(1/2)/(b*x+a)^(1/2)/x^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))/b^(1/2)

maxima [B] time = 2.99, size = 141, normalized size = 1.53

$$\frac{5 a^3 \log\left(\frac{\sqrt{b}-\frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+a}}{\sqrt{x}}}\right)}{16 \sqrt{b}} - \frac{\frac{15 \sqrt{bx+a} a^3 b^2}{\sqrt{x}} - \frac{40 (bx+a)^{\frac{3}{2}} a^3 b}{x^2} + \frac{33 (bx+a)^{\frac{5}{2}} a^3}{x^2}}{24 \left(b^3 - \frac{3 (bx+a) b^2}{x} + \frac{3 (bx+a)^2 b}{x^2} - \frac{(bx+a)^3}{x^3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^(1/2),x, algorithm="maxima")

[Out] $-5/16*a^3*\log(-(\sqrt{b} - \sqrt{b*x + a})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x + a})/\sqrt{x} - 1/24*(15*\sqrt{b*x + a}*a^3*b^2/\sqrt{x} - 40*(b*x + a)^{(3/2)}*a^3*b/x^{(3/2)} + 33*(b*x + a)^{(5/2)}*a^3/x^{(5/2)})/(b^3 - 3*(b*x + a)*b^2/x + 3*(b*x + a)^2*b/x^2 - (b*x + a)^3/x^3)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{5/2}}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)/x^(1/2),x)

[Out] int((a + b*x)^(5/2)/x^(1/2), x)

sympy [A] time = 6.23, size = 102, normalized size = 1.11

$$\frac{11a^{\frac{5}{2}}\sqrt{x}\sqrt{1+\frac{bx}{a}}}{8} + \frac{13a^{\frac{3}{2}}bx^{\frac{3}{2}}\sqrt{1+\frac{bx}{a}}}{12} + \frac{\sqrt{a}b^2x^{\frac{5}{2}}\sqrt{1+\frac{bx}{a}}}{3} + \frac{5a^3 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)/x**(1/2),x)

[Out] $11*a^{(5/2)}*\sqrt{x}*\sqrt{1 + b*x/a}/8 + 13*a^{(3/2)}*b*x^{(3/2)}*\sqrt{1 + b*x/a}/12 + \sqrt{a}*b^{(2)}*x^{(5/2)}*\sqrt{1 + b*x/a}/3 + 5*a^{(3)}*\operatorname{asinh}(\sqrt{b}*\sqrt{x}/\sqrt{a})/(8*\sqrt{b})$

$$3.549 \quad \int \frac{(a+bx)^{5/2}}{x^{3/2}} dx$$

Optimal. Leaf size=89

$$\frac{15}{4}a^2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right) - \frac{2(a+bx)^{5/2}}{\sqrt{x}} + \frac{5}{2}b\sqrt{x}(a+bx)^{3/2} + \frac{15}{4}ab\sqrt{x}\sqrt{a+bx}$$

[Out] $15/4*a^2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)/(b*x+a)^{(1/2)})}*b^{(1/2)}-2*(b*x+a)^{(5/2)}/x^{(1/2)}+5/2*b*(b*x+a)^{(3/2)}*x^{(1/2)}+15/4*a*b*x^{(1/2)}*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 89, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {47, 50, 63, 217, 206}

$$\frac{15}{4}a^2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right) - \frac{2(a+bx)^{5/2}}{\sqrt{x}} + \frac{5}{2}b\sqrt{x}(a+bx)^{3/2} + \frac{15}{4}ab\sqrt{x}\sqrt{a+bx}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}/x^{(3/2)}, x]$

[Out] $(15*a*b*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/4 + (5*b*\operatorname{Sqrt}[x]*(a + b*x)^{(3/2)})/2 - (2*(a + b*x)^{(5/2)})/\operatorname{Sqrt}[x] + (15*a^2*\operatorname{Sqrt}[b]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/4$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{x^{3/2}} dx &= -\frac{2(a+bx)^{5/2}}{\sqrt{x}} + (5b) \int \frac{(a+bx)^{3/2}}{\sqrt{x}} dx \\
&= \frac{5}{2}b\sqrt{x}(a+bx)^{3/2} - \frac{2(a+bx)^{5/2}}{\sqrt{x}} + \frac{1}{4}(15ab) \int \frac{\sqrt{a+bx}}{\sqrt{x}} dx \\
&= \frac{15}{4}ab\sqrt{x}\sqrt{a+bx} + \frac{5}{2}b\sqrt{x}(a+bx)^{3/2} - \frac{2(a+bx)^{5/2}}{\sqrt{x}} + \frac{1}{8}(15a^2b) \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx \\
&= \frac{15}{4}ab\sqrt{x}\sqrt{a+bx} + \frac{5}{2}b\sqrt{x}(a+bx)^{3/2} - \frac{2(a+bx)^{5/2}}{\sqrt{x}} + \frac{1}{4}(15a^2b) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right) \\
&= \frac{15}{4}ab\sqrt{x}\sqrt{a+bx} + \frac{5}{2}b\sqrt{x}(a+bx)^{3/2} - \frac{2(a+bx)^{5/2}}{\sqrt{x}} + \frac{1}{4}(15a^2b) \operatorname{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \sqrt{x}\right) \\
&= \frac{15}{4}ab\sqrt{x}\sqrt{a+bx} + \frac{5}{2}b\sqrt{x}(a+bx)^{3/2} - \frac{2(a+bx)^{5/2}}{\sqrt{x}} + \frac{15}{4}a^2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 48, normalized size = 0.54

$$-\frac{2a^2\sqrt{a+bx} {}_2F_1\left(-\frac{5}{2}, -\frac{1}{2}; \frac{1}{2}; -\frac{bx}{a}\right)}{\sqrt{x}\sqrt{\frac{bx}{a}+1}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/x^(3/2),x]

[Out] $(-2a^2\sqrt{a + bx} \operatorname{Hypergeometric2F1}[-5/2, -1/2, 1/2, -(bx)/a]) / (\sqrt{x} \sqrt{1 + (bx)/a})$

fricas [A] time = 0.46, size = 137, normalized size = 1.54

$$\left[\frac{15a^2\sqrt{b}x \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(2b^2x^2 + 9abx - 8a^2)\sqrt{bx+a}\sqrt{x}}{8x}, -\frac{15a^2\sqrt{-b}x \arctan\left(\frac{\sqrt{bx+a}}{b\sqrt{x}}\right)}{8x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^(3/2),x, algorithm="fricas")

[Out] $[1/8*(15a^2\sqrt{b}x \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(2b^2x^2 + 9abx - 8a^2)\sqrt{bx+a}\sqrt{x})/x, -1/4*(15a^2\sqrt{-b}x \arctan(\sqrt{bx+a}\sqrt{-b}/(b\sqrt{x})) - (2b^2x^2 + 9abx - 8a^2)\sqrt{bx+a}\sqrt{x})/x]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^(3/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.02, size = 84, normalized size = 0.94

$$\frac{15\sqrt{(bx+a)x} a^2\sqrt{b} \ln\left(\frac{bx+a}{\sqrt{b}} + \sqrt{bx+a}\sqrt{x}\right)}{8\sqrt{bx+a}\sqrt{x}} - \frac{\sqrt{bx+a}(-2b^2x^2 - 9abx + 8a^2)}{4\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/x^(3/2),x)

[Out] $-1/4*(b*x+a)^{(1/2)}*(-2*b^2*x^2-9*a*b*x+8*a^2)/x^{(1/2)}+15/8*a^2*b^{(1/2)}*\ln((b*x+1/2*a)/b^{(1/2)}+(b*x^2+a*x)^{(1/2)})*((b*x+a)*x)^{(1/2)}/(b*x+a)^{(1/2)}/x^{(1/2)}$

maxima [A] time = 2.98, size = 125, normalized size = 1.40

$$-\frac{15}{8}a^2\sqrt{b} \log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+a}}{\sqrt{x}}}\right) - \frac{2\sqrt{bx+a}a^2}{\sqrt{x}} - \frac{\frac{7\sqrt{bx+a}a^2b^2}{\sqrt{x}} - \frac{9(bx+a)^{\frac{3}{2}}a^2b}{x^{\frac{3}{2}}}}{4\left(b^2 - \frac{2(bx+a)b}{x} + \frac{(bx+a)^2}{x^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^(3/2),x, algorithm="maxima")

[Out] $-15/8*a^2*\sqrt{b}*\log(-(\sqrt{b} - \sqrt{b*x + a})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x + a})/\sqrt{x}) - 2*\sqrt{b*x + a}*a^2/\sqrt{x} - 1/4*(7*\sqrt{b*x + a}*a^2*b^2/\sqrt{x} - 9*(b*x + a)^{(3/2)}*a^2*b/x^{(3/2)})/(b^2 - 2*(b*x + a)*b/x + (b*x + a)^2/x^2)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{5/2}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)/x^(3/2),x)

[Out] int((a + b*x)^(5/2)/x^(3/2), x)

sympy [A] time = 6.15, size = 126, normalized size = 1.42

$$-\frac{2a^{\frac{5}{2}}}{\sqrt{x}\sqrt{1+\frac{bx}{a}}} + \frac{a^{\frac{3}{2}}b\sqrt{x}}{4\sqrt{1+\frac{bx}{a}}} + \frac{11\sqrt{a}b^2x^{\frac{3}{2}}}{4\sqrt{1+\frac{bx}{a}}} + \frac{15a^2\sqrt{b}\operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4} + \frac{b^3x^{\frac{5}{2}}}{2\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)/x**(3/2),x)

[Out] $-2*a^{(5/2)}/(\sqrt{x}*\sqrt{1 + b*x/a}) + a^{(3/2)}*b*\sqrt{x}/(4*\sqrt{1 + b*x/a}) + 11*\sqrt{a}*b^{**2}*x^{(3/2)}/(4*\sqrt{1 + b*x/a}) + 15*a^{**2}*\sqrt{b}*\operatorname{asinh}(\sqrt{b}*\sqrt{x}/\sqrt{a})/4 + b^{**3}*x^{(5/2)}/(2*\sqrt{a}*\sqrt{1 + b*x/a})$

$$3.550 \quad \int \frac{(a+bx)^{5/2}}{x^{5/2}} dx$$

Optimal. Leaf size=86

$$5ab^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right) + 5b^2\sqrt{x}\sqrt{a+bx} - \frac{2(a+bx)^{5/2}}{3x^{3/2}} - \frac{10b(a+bx)^{3/2}}{3\sqrt{x}}$$

[Out] $-2/3*(b*x+a)^{(5/2)}/x^{(3/2)}+5*a*b^{(3/2)}*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})-10/3*b*(b*x+a)^{(3/2)}/x^{(1/2)}+5*b^2*x^{(1/2)}*(b*x+a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {47, 50, 63, 217, 206}

$$5b^2\sqrt{x}\sqrt{a+bx} + 5ab^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right) - \frac{2(a+bx)^{5/2}}{3x^{3/2}} - \frac{10b(a+bx)^{3/2}}{3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2)/x^(5/2), x]

[Out] $5*b^2*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x] - (10*b*(a + b*x)^{(3/2)})/(3*\operatorname{Sqrt}[x]) - (2*(a + b*x)^{(5/2)})/(3*x^{(3/2)}) + 5*a*b^{(3/2)}*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{x^{5/2}} dx &= -\frac{2(a+bx)^{5/2}}{3x^{3/2}} + \frac{1}{3}(5b) \int \frac{(a+bx)^{3/2}}{x^{3/2}} dx \\
&= -\frac{10b(a+bx)^{3/2}}{3\sqrt{x}} - \frac{2(a+bx)^{5/2}}{3x^{3/2}} + (5b^2) \int \frac{\sqrt{a+bx}}{\sqrt{x}} dx \\
&= 5b^2\sqrt{x}\sqrt{a+bx} - \frac{10b(a+bx)^{3/2}}{3\sqrt{x}} - \frac{2(a+bx)^{5/2}}{3x^{3/2}} + \frac{1}{2}(5ab^2) \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx \\
&= 5b^2\sqrt{x}\sqrt{a+bx} - \frac{10b(a+bx)^{3/2}}{3\sqrt{x}} - \frac{2(a+bx)^{5/2}}{3x^{3/2}} + (5ab^2) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right) \\
&= 5b^2\sqrt{x}\sqrt{a+bx} - \frac{10b(a+bx)^{3/2}}{3\sqrt{x}} - \frac{2(a+bx)^{5/2}}{3x^{3/2}} + (5ab^2) \operatorname{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right) \\
&= 5b^2\sqrt{x}\sqrt{a+bx} - \frac{10b(a+bx)^{3/2}}{3\sqrt{x}} - \frac{2(a+bx)^{5/2}}{3x^{3/2}} + 5ab^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.58

$$\frac{2a^2\sqrt{a+bx} {}_2F_1\left(-\frac{5}{2}, -\frac{3}{2}; -\frac{1}{2}; -\frac{bx}{a}\right)}{3x^{3/2}\sqrt{\frac{bx}{a}+1}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/x^(5/2),x]

[Out] $(-2a^2\sqrt{a + bx} \operatorname{Hypergeometric2F1}[-5/2, -3/2, -1/2, -(bx)/a]) / (3x^{3/2}\sqrt{1 + (bx)/a})$

fricas [A] time = 0.44, size = 138, normalized size = 1.60

$$\left[\frac{15ab^2x^2 \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(3b^2x^2 - 14abx - 2a^2)\sqrt{bx+a}\sqrt{x}}{6x^2}, -\frac{15a\sqrt{-b}bx^2 \arctan\left(\frac{\sqrt{bx+a}}{b}\right)}{6x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^(5/2),x, algorithm="fricas")

[Out] $[1/6*(15*a*b^{3/2}*x^2*\log(2*b*x + 2*\sqrt{b*x + a}*\sqrt{b}*\sqrt{x} + a) + 2*(3*b^2*x^2 - 14*a*b*x - 2*a^2)*\sqrt{b*x + a}*\sqrt{x})/x^2, -1/3*(15*a*\sqrt{-b}*b*x^2*\arctan(\sqrt{b*x + a}*\sqrt{-b}/(b*\sqrt{x})) - (3*b^2*x^2 - 14*a*b*x - 2*a^2)*\sqrt{b*x + a}*\sqrt{x})/x^2]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^(5/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.02, size = 82, normalized size = 0.95

$$\frac{5\sqrt{(bx+a)x} a b^2 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{2\sqrt{bx+a}\sqrt{x}} - \frac{\sqrt{bx+a}(-3b^2x^2+14abx+2a^2)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/x^(5/2),x)

[Out] $-1/3*(b*x+a)^{1/2}*(-3*b^2*x^2+14*a*b*x+2*a^2)/x^{3/2}+5/2*a*b^{3/2}*\ln((b*x+1/2*a)/b^{1/2}+(b*x^2+a*x)^{1/2})*((b*x+a)*x)^{1/2}/(b*x+a)^{1/2}/x^{1/2}$

maxima [A] time = 2.95, size = 100, normalized size = 1.16

$$-\frac{5}{2}ab^2 \log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+a}}{\sqrt{x}}}\right) - \frac{4\sqrt{bx+a}ab}{\sqrt{x}} - \frac{\sqrt{bx+a}ab^2}{\left(b-\frac{bx+a}{x}\right)\sqrt{x}} - \frac{2(bx+a)^{\frac{3}{2}}a}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/x^(5/2),x, algorithm="maxima")

[Out] $-5/2*a*b^{(3/2)}*\log(-(\sqrt{b} - \sqrt{b*x + a})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x + a})/\sqrt{x}) - 4*\sqrt{b*x + a}*a*b/\sqrt{x} - \sqrt{b*x + a}*a*b^2/((b - (b*x + a)/x)*\sqrt{x}) - 2/3*(b*x + a)^{(3/2)}*a/x^{(3/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{5/2}}{x^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)/x^(5/2),x)

[Out] int((a + b*x)^(5/2)/x^(5/2), x)

sympy [A] time = 5.62, size = 99, normalized size = 1.15

$$-\frac{2a^2\sqrt{b}\sqrt{\frac{a}{bx}+1}}{3x} - \frac{14ab^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}}{3} - \frac{5ab^{\frac{3}{2}}\log\left(\frac{a}{bx}\right)}{2} + 5ab^{\frac{3}{2}}\log\left(\sqrt{\frac{a}{bx}+1}+1\right) + b^{\frac{5}{2}}x\sqrt{\frac{a}{bx}+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)/x**(5/2),x)

[Out] $-2*a**2*\sqrt{b}*\sqrt{a/(b*x) + 1}/(3*x) - 14*a*b**(3/2)*\sqrt{a/(b*x) + 1}/3 - 5*a*b**(3/2)*\log(a/(b*x))/2 + 5*a*b**(3/2)*\log(\sqrt{a/(b*x) + 1} + 1) + b**(5/2)*x*\sqrt{a/(b*x) + 1}$

3.551 $\int x^{5/2}(a - bx)^{5/2} dx$

Optimal. Leaf size=171

$$\frac{5a^6 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{512b^{7/2}} - \frac{5a^5\sqrt{x}\sqrt{a-bx}}{512b^3} - \frac{5a^4x^{3/2}\sqrt{a-bx}}{768b^2} - \frac{a^3x^{5/2}\sqrt{a-bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a-bx} + \frac{1}{12}ax^{7/2}(a-bx)^{3/2} + \frac{1}{6}x^{7/2}$$

[Out] $\frac{1}{12}ax^{7/2}(-bx+a)^{3/2} + \frac{1}{6}x^{7/2}(-bx+a)^{5/2} + \frac{5}{512}a^6 \arctan\left(\frac{b^{1/2}x^{1/2}}{(-bx+a)^{1/2}}\right) - \frac{5}{768}a^4x^{3/2}(-bx+a)^{1/2} - \frac{1}{192}a^3x^{5/2}(-bx+a)^{1/2} + \frac{1}{32}a^2x^{7/2}(-bx+a)^{1/2} - \frac{5}{512}a^5x^{1/2}(-bx+a)^{1/2}$

Rubi [A] time = 0.06, antiderivative size = 171, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$-\frac{5a^4x^{3/2}\sqrt{a-bx}}{768b^2} - \frac{5a^5\sqrt{x}\sqrt{a-bx}}{512b^3} + \frac{5a^6 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{512b^{7/2}} - \frac{a^3x^{5/2}\sqrt{a-bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a-bx} + \frac{1}{12}ax^{7/2}(a-bx)^{3/2} + \frac{1}{6}x^{7/2}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)*(a - b*x)^(5/2), x]

[Out] $\frac{(-5a^5\sqrt{x}\sqrt{a-bx})}{(512b^3)} - \frac{(5a^4x^{3/2}\sqrt{a-bx})}{(768b^2)} - \frac{(a^3x^{5/2}\sqrt{a-bx})}{(192b)} + \frac{(a^2x^{7/2}\sqrt{a-bx})}{32} + \frac{(ax^{7/2}(a-bx)^{3/2})}{12} + \frac{(x^{7/2}(a-bx)^{5/2})}{6} + \frac{(5a^6 \text{ArcTan}[\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}])}{(512b^{7/2})}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

$\text{Int}[(a_ + (b_ \cdot)(x_)^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(1 \cdot \text{ArcTan}[\text{Rt}[b, 2] \cdot x] / \text{Rt}[a, 2]]) / (\text{Rt}[a, 2] \cdot \text{Rt}[b, 2]), x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{PosQ}[a/b] \ \&\& \ (\text{GtQ}[a, 0] \ || \ \text{GtQ}[b, 0])$

Rule 217

$\text{Int}[1/\text{Sqrt}[(a_ + (b_ \cdot)(x_)^2)], x_Symbol] \rightarrow \text{Subst}[\text{Int}[1/(1 - b \cdot x^2), x], x, x/\text{Sqrt}[a + b \cdot x^2]] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
 \int x^{5/2}(a - bx)^{5/2} dx &= \frac{1}{6}x^{7/2}(a - bx)^{5/2} + \frac{1}{12}(5a) \int x^{5/2}(a - bx)^{3/2} dx \\
 &= \frac{1}{12}ax^{7/2}(a - bx)^{3/2} + \frac{1}{6}x^{7/2}(a - bx)^{5/2} + \frac{1}{8}a^2 \int x^{5/2}\sqrt{a - bx} dx \\
 &= \frac{1}{32}a^2x^{7/2}\sqrt{a - bx} + \frac{1}{12}ax^{7/2}(a - bx)^{3/2} + \frac{1}{6}x^{7/2}(a - bx)^{5/2} + \frac{1}{64}a^3 \int \frac{x^{5/2}}{\sqrt{a - bx}} dx \\
 &= -\frac{a^3x^{5/2}\sqrt{a - bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a - bx} + \frac{1}{12}ax^{7/2}(a - bx)^{3/2} + \frac{1}{6}x^{7/2}(a - bx)^{5/2} + \frac{(5a^4) \int \frac{x^{5/2}}{\sqrt{a - bx}} dx}{384} \\
 &= -\frac{5a^4x^{3/2}\sqrt{a - bx}}{768b^2} - \frac{a^3x^{5/2}\sqrt{a - bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a - bx} + \frac{1}{12}ax^{7/2}(a - bx)^{3/2} + \frac{1}{6}x^{7/2}(a - bx)^{5/2} \\
 &= -\frac{5a^5\sqrt{x}\sqrt{a - bx}}{512b^3} - \frac{5a^4x^{3/2}\sqrt{a - bx}}{768b^2} - \frac{a^3x^{5/2}\sqrt{a - bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a - bx} + \frac{1}{12}ax^{7/2}(a - bx)^{3/2} \\
 &= -\frac{5a^5\sqrt{x}\sqrt{a - bx}}{512b^3} - \frac{5a^4x^{3/2}\sqrt{a - bx}}{768b^2} - \frac{a^3x^{5/2}\sqrt{a - bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a - bx} + \frac{1}{12}ax^{7/2}(a - bx)^{3/2} \\
 &= -\frac{5a^5\sqrt{x}\sqrt{a - bx}}{512b^3} - \frac{5a^4x^{3/2}\sqrt{a - bx}}{768b^2} - \frac{a^3x^{5/2}\sqrt{a - bx}}{192b} + \frac{1}{32}a^2x^{7/2}\sqrt{a - bx} + \frac{1}{12}ax^{7/2}(a - bx)^{3/2}
 \end{aligned}$$

Mathematica [A] time = 0.19, size = 120, normalized size = 0.70

$$\frac{\sqrt{a-bx} \left(\frac{15a^{11/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{1-\frac{bx}{a}}} + \sqrt{b}\sqrt{x} (-15a^5 - 10a^4bx - 8a^3b^2x^2 + 432a^2b^3x^3 - 640ab^4x^4 + 256b^5x^5) \right)}{1536b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*(a - b*x)^(5/2), x]

[Out] (Sqrt[a - b*x]*(Sqrt[b]*Sqrt[x]*(-15*a^5 - 10*a^4*b*x - 8*a^3*b^2*x^2 + 432*a^2*b^3*x^3 - 640*a*b^4*x^4 + 256*b^5*x^5) + (15*a^(11/2)*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 - (b*x)/a]))/(1536*b^(7/2))

fricas [A] time = 0.44, size = 208, normalized size = 1.22

$$\left[\frac{15a^6\sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) - 2(256b^6x^5 - 640ab^5x^4 + 432a^2b^4x^3 - 8a^3b^3x^2 - 10a^4b^2x - 15a^5b)\sqrt{-bx+a}\sqrt{x}}{3072b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(-b*x+a)^(5/2), x, algorithm="fricas")

[Out] [-1/3072*(15*a^6*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*(256*b^6*x^5 - 640*a*b^5*x^4 + 432*a^2*b^4*x^3 - 8*a^3*b^3*x^2 - 10*a^4*b^2*x - 15*a^5*b)*sqrt(-b*x + a)*sqrt(x))/b^4, -1/1536*(15*a^6*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - (256*b^6*x^5 - 640*a*b^5*x^4 + 432*a^2*b^4*x^3 - 8*a^3*b^3*x^2 - 10*a^4*b^2*x - 15*a^5*b)*sqrt(-b*x + a)*sqrt(x))/b^4]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(-b*x+a)^(5/2), x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 165, normalized size = 0.96

$$\frac{5\sqrt{-bx+a}x a^6 \arctan\left(\frac{(x-\frac{a}{2b})\sqrt{b}}{\sqrt{-bx+a}}\right)}{1024\sqrt{-bx+a} b^{\frac{7}{2}}\sqrt{x}} + \frac{5\sqrt{-bx+a} a^5\sqrt{x}}{512b^3} + \frac{5(-bx+a)^{\frac{3}{2}} a^4\sqrt{x}}{768b^3} - \frac{(-bx+a)^{\frac{7}{2}} x^{\frac{5}{2}}}{6b} + \frac{(-bx+a)^{\frac{5}{2}} a^3\sqrt{x}}{192b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{5/2}*(-b*x+a)^{5/2}, x)$

[Out] $-1/6/b*x^{5/2}*(-b*x+a)^{7/2}-1/12*a/b^2*x^{3/2}*(-b*x+a)^{7/2}-1/32*a^2/b^3*x^{1/2}*(-b*x+a)^{7/2}+1/192*a^3/b^3*(-b*x+a)^{5/2}*x^{1/2}+5/768*a^4/b^3*(-b*x+a)^{3/2}*x^{1/2}+5/512*a^5*x^{1/2}*(-b*x+a)^{1/2}/b^3+5/1024*a^6/b^{7/2}*((-b*x+a)*x)^{1/2}/(-b*x+a)^{1/2}/x^{1/2}*\arctan((x-1/2*a/b)/(-b*x^2+a*x)^{1/2})*b^{1/2}$

maxima [A] time = 2.86, size = 242, normalized size = 1.42

$$\frac{5a^6 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{512b^{\frac{7}{2}}} + \frac{\frac{15\sqrt{-bx+a}a^6b^5}{\sqrt{x}} + \frac{85(-bx+a)^3a^6b^4}{x^2} + \frac{198(-bx+a)^5a^6b^3}{x^2} - \frac{198(-bx+a)^7a^6b^2}{x^2} - \frac{85(-bx+a)^9a^6b}{x^2} - \frac{15(-bx+a)^{11}a^6}{x^2}}{1536\left(b^9 - \frac{6(bx-a)b^8}{x} + \frac{15(bx-a)^2b^7}{x^2} - \frac{20(bx-a)^3b^6}{x^3} + \frac{15(bx-a)^4b^5}{x^4} - \frac{6(bx-a)^5b^4}{x^5} + \frac{(bx-a)^6b^3}{x^6}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{5/2}*(-b*x+a)^{5/2}, x, \text{algorithm}="maxima")$

[Out] $-5/512*a^6*\arctan(\text{sqrt}(-b*x + a)/(\text{sqrt}(b)*\text{sqrt}(x)))/b^{7/2} + 1/1536*(15*\text{sqrt}(-b*x + a)*a^6*b^5/\text{sqrt}(x) + 85*(-b*x + a)^{3/2}*a^6*b^4/x^{3/2} + 198*(-b*x + a)^{5/2}*a^6*b^3/x^{5/2} - 198*(-b*x + a)^{7/2}*a^6*b^2/x^{7/2} - 85*(-b*x + a)^{9/2}*a^6*b/x^{9/2} - 15*(-b*x + a)^{11/2}*a^6/x^{11/2})/(b^9 - 6*(b*x - a)*b^8/x + 15*(b*x - a)^2*b^7/x^2 - 20*(b*x - a)^3*b^6/x^3 + 15*(b*x - a)^4*b^5/x^4 - 6*(b*x - a)^5*b^4/x^5 + (b*x - a)^6*b^3/x^6)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} (a - bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{5/2}*(a - b*x)^{5/2}, x)$

[Out] $\text{int}(x^{5/2}*(a - b*x)^{5/2}, x)$

sympy [A] time = 25.96, size = 435, normalized size = 2.54

$$\left\{ \begin{array}{l} \frac{5ia^{\frac{11}{2}}\sqrt{x}}{512b^3\sqrt{-1+\frac{bx}{a}}} - \frac{5ia^{\frac{9}{2}}x^{\frac{3}{2}}}{1536b^2\sqrt{-1+\frac{bx}{a}}} - \frac{7a^{\frac{7}{2}}x^{\frac{5}{2}}}{768b\sqrt{-1+\frac{bx}{a}}} - \frac{55ia^{\frac{5}{2}}x^{\frac{7}{2}}}{192\sqrt{-1+\frac{bx}{a}}} + \frac{67ia^{\frac{3}{2}}bx^{\frac{9}{2}}}{96\sqrt{-1+\frac{bx}{a}}} - \frac{7i\sqrt{a}b^2x^{\frac{11}{2}}}{12\sqrt{-1+\frac{bx}{a}}} - \frac{5ia^6 \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{512b^{\frac{7}{2}}} + \frac{ib^3x^{\frac{13}{2}}}{6\sqrt{a}\sqrt{-1+\frac{bx}{a}}} \\ - \frac{5a^{\frac{11}{2}}\sqrt{x}}{512b^3\sqrt{1-\frac{bx}{a}}} + \frac{5a^{\frac{9}{2}}x^{\frac{3}{2}}}{1536b^2\sqrt{1-\frac{bx}{a}}} + \frac{7a^{\frac{7}{2}}x^{\frac{5}{2}}}{768b\sqrt{1-\frac{bx}{a}}} + \frac{55a^{\frac{5}{2}}x^{\frac{7}{2}}}{192\sqrt{1-\frac{bx}{a}}} - \frac{67a^{\frac{3}{2}}bx^{\frac{9}{2}}}{96\sqrt{1-\frac{bx}{a}}} + \frac{7\sqrt{a}b^2x^{\frac{11}{2}}}{12\sqrt{1-\frac{bx}{a}}} + \frac{5a^6 \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{512b^{\frac{7}{2}}} - \frac{b^3x^{\frac{13}{2}}}{6\sqrt{a}\sqrt{1-\frac{bx}{a}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(5/2)*(-b*x+a)**(5/2),x)
```

```
[Out] Piecewise((5*I*a**(11/2)*sqrt(x)/(512*b**3*sqrt(-1 + b*x/a)) - 5*I*a**(9/2)*x**(3/2)/(1536*b**2*sqrt(-1 + b*x/a)) - I*a**(7/2)*x**(5/2)/(768*b*sqrt(-1 + b*x/a)) - 55*I*a**(5/2)*x**(7/2)/(192*sqrt(-1 + b*x/a)) + 67*I*a**(3/2)*b*x**(9/2)/(96*sqrt(-1 + b*x/a)) - 7*I*sqrt(a)*b**2*x**(11/2)/(12*sqrt(-1 + b*x/a)) - 5*I*a**6*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(512*b**(7/2)) + I*b**3*x**(13/2)/(6*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (-5*a**(11/2)*sqrt(x)/(512*b**3*sqrt(1 - b*x/a)) + 5*a**(9/2)*x**(3/2)/(1536*b**2*sqrt(1 - b*x/a)) + a**(7/2)*x**(5/2)/(768*b*sqrt(1 - b*x/a)) + 55*a**(5/2)*x**(7/2)/(192*sqrt(1 - b*x/a)) - 67*a**(3/2)*b*x**(9/2)/(96*sqrt(1 - b*x/a)) + 7*sqrt(a)*b**2*x**(11/2)/(12*sqrt(1 - b*x/a)) + 5*a**6*asin(sqrt(b)*sqrt(x)/sqrt(a))/(512*b**(7/2)) - b**3*x**(13/2)/(6*sqrt(a)*sqrt(1 - b*x/a)), True))
```

3.552 $\int x^{3/2}(a - bx)^{5/2} dx$

Optimal. Leaf size=146

$$\frac{3a^5 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{128b^{5/2}} - \frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^2} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a-bx} + \frac{1}{8}ax^{5/2}(a-bx)^{3/2} + \frac{1}{5}x^{5/2}(a-bx)^{5/2}$$

[Out] $1/8*a*x^{(5/2)}*(-b*x+a)^{(3/2)}+1/5*x^{(5/2)}*(-b*x+a)^{(5/2)}+3/128*a^5*\arctan(b^{(1/2)}*x^{(1/2)}/(-b*x+a)^{(1/2)})/b^{(5/2)}-1/64*a^3*x^{(3/2)}*(-b*x+a)^{(1/2)}/b+1/16*a^2*x^{(5/2)}*\sqrt{a-bx}+1/8*a*x^{(5/2)}*(a-bx)^{(3/2)}+1/5*x^{(5/2)}*(a-bx)^{(5/2)}$

Rubi [A] time = 0.05, antiderivative size = 146, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$-\frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^2} + \frac{3a^5 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{128b^{5/2}} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a-bx} + \frac{1}{8}ax^{5/2}(a-bx)^{3/2} + \frac{1}{5}x^{5/2}(a-bx)^{5/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(3/2)}*(a - b*x)^{(5/2)}, x]$

[Out] $(-3*a^4*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(128*b^2) - (a^3*x^{(3/2)}*\text{Sqrt}[a - b*x])/(64*b) + (a^2*x^{(5/2)}*\text{Sqrt}[a - b*x])/16 + (a*x^{(5/2)}*(a - b*x)^{(3/2)})/8 + (x^{(5/2)}*(a - b*x)^{(5/2)})/5 + (3*a^5*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(128*b^{(5/2)})$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int x^{3/2}(a-bx)^{5/2} dx &= \frac{1}{5}x^{5/2}(a-bx)^{5/2} + \frac{1}{2}a \int x^{3/2}(a-bx)^{3/2} dx \\
 &= \frac{1}{8}ax^{5/2}(a-bx)^{3/2} + \frac{1}{5}x^{5/2}(a-bx)^{5/2} + \frac{1}{16}(3a^2) \int x^{3/2}\sqrt{a-bx} dx \\
 &= \frac{1}{16}a^2x^{5/2}\sqrt{a-bx} + \frac{1}{8}ax^{5/2}(a-bx)^{3/2} + \frac{1}{5}x^{5/2}(a-bx)^{5/2} + \frac{1}{32}a^3 \int \frac{x^{3/2}}{\sqrt{a-bx}} dx \\
 &= -\frac{a^3x^{3/2}\sqrt{a-bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a-bx} + \frac{1}{8}ax^{5/2}(a-bx)^{3/2} + \frac{1}{5}x^{5/2}(a-bx)^{5/2} + \frac{(3a^4) \int \frac{\sqrt{x}}{\sqrt{a-bx}} dx}{128b} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^2} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a-bx} + \frac{1}{8}ax^{5/2}(a-bx)^{3/2} + \frac{1}{5}x^{5/2}(a-bx)^{5/2} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^2} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a-bx} + \frac{1}{8}ax^{5/2}(a-bx)^{3/2} + \frac{1}{5}x^{5/2}(a-bx)^{5/2} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^2} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a-bx} + \frac{1}{8}ax^{5/2}(a-bx)^{3/2} + \frac{1}{5}x^{5/2}(a-bx)^{5/2} \\
 &= -\frac{3a^4\sqrt{x}\sqrt{a-bx}}{128b^2} - \frac{a^3x^{3/2}\sqrt{a-bx}}{64b} + \frac{1}{16}a^2x^{5/2}\sqrt{a-bx} + \frac{1}{8}ax^{5/2}(a-bx)^{3/2} + \frac{1}{5}x^{5/2}(a-bx)^{5/2}
 \end{aligned}$$

Mathematica [A] time = 0.15, size = 109, normalized size = 0.75

$$\frac{\sqrt{a-bx} \left(\frac{15a^{9/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{1-\frac{bx}{a}}} + \sqrt{b}\sqrt{x} (-15a^4 - 10a^3bx + 248a^2b^2x^2 - 336ab^3x^3 + 128b^4x^4) \right)}{640b^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*(a - b*x)^(5/2),x]

[Out] (Sqrt[a - b*x]*(Sqrt[b]*Sqrt[x]*(-15*a^4 - 10*a^3*b*x + 248*a^2*b^2*x^2 - 336*a*b^3*x^3 + 128*b^4*x^4) + (15*a^(9/2)*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 - (b*x)/a]))/(640*b^(5/2))

fricas [A] time = 0.46, size = 186, normalized size = 1.27

$$\left[\frac{15 a^5 \sqrt{-b} \log(-2 b x + 2 \sqrt{-b x + a} \sqrt{-b} \sqrt{x} + a) - 2 (128 b^5 x^4 - 336 a b^4 x^3 + 248 a^2 b^3 x^2 - 10 a^3 b^2 x - 15 a^4 b)}{1280 b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+a)^(5/2),x, algorithm="fricas")

[Out] [-1/1280*(15*a^5*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*(128*b^5*x^4 - 336*a*b^4*x^3 + 248*a^2*b^3*x^2 - 10*a^3*b^2*x - 15*a^4*b)*sqrt(-b*x + a)*sqrt(x))/b^3, -1/640*(15*a^5*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - (128*b^5*x^4 - 336*a*b^4*x^3 + 248*a^2*b^3*x^2 - 10*a^3*b^2*x - 15*a^4*b)*sqrt(-b*x + a)*sqrt(x))/b^3]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+a)^(5/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 146, normalized size = 1.00

$$\frac{3\sqrt{-bx+a}x a^5 \arctan\left(\frac{(x-\frac{a}{2b})\sqrt{b}}{\sqrt{-bx^2+ax}}\right)}{256\sqrt{-bx+a} b^{\frac{5}{2}}\sqrt{x}} + \frac{3\sqrt{-bx+a} a^4 \sqrt{x}}{128b^2} + \frac{(-bx+a)^{\frac{3}{2}} a^3 \sqrt{x}}{64b^2} + \frac{(-bx+a)^{\frac{5}{2}} a^2 \sqrt{x}}{80b^2} - \frac{(-bx+a)^{\frac{7}{2}} x^{\frac{3}{2}}}{5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(-b*x+a)^(5/2),x)

[Out] -1/5/b*x^(3/2)*(-b*x+a)^(7/2)-3/40*a/b^2*x^(1/2)*(-b*x+a)^(7/2)+1/80*a^2/b^2*(-b*x+a)^(5/2)*x^(1/2)+1/64*a^3/b^2*(-b*x+a)^(3/2)*x^(1/2)+3/128*a^4*x^(1/2)*(-b*x+a)^(1/2)/b^2+3/256*a^5/b^(5/2)*((-b*x+a)*x)^(1/2)/(-b*x+a)^(1/2)/x^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))

maxima [A] time = 3.01, size = 207, normalized size = 1.42

$$-\frac{3a^5 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{128b^{\frac{5}{2}}} + \frac{15\sqrt{-bx+a}a^5b^4}{\sqrt{x}} + \frac{70(-bx+a)^{\frac{3}{2}}a^5b^3}{x^{\frac{3}{2}}} + \frac{128(-bx+a)^{\frac{5}{2}}a^5b^2}{x^{\frac{5}{2}}} - \frac{70(-bx+a)^{\frac{7}{2}}a^5b}{x^{\frac{7}{2}}} - \frac{15(-bx+a)^{\frac{9}{2}}a^5}{x^{\frac{9}{2}}}$$

$$+ \frac{640\left(b^7 - \frac{5(bx-a)b^6}{x} + \frac{10(bx-a)^2b^5}{x^2} - \frac{10(bx-a)^3b^4}{x^3} + \frac{5(bx-a)^4b^3}{x^4} - \frac{(bx-a)^5b^2}{x^5}\right)}{640\left(b^7 - \frac{5(bx-a)b^6}{x} + \frac{10(bx-a)^2b^5}{x^2} - \frac{10(bx-a)^3b^4}{x^3} + \frac{5(bx-a)^4b^3}{x^4} - \frac{(bx-a)^5b^2}{x^5}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+a)^(5/2),x, algorithm="maxima")

[Out] -3/128*a^5*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/b^(5/2) + 1/640*(15*sqrt(-b*x + a)*a^5*b^4/sqrt(x) + 70*(-b*x + a)^(3/2)*a^5*b^3/x^(3/2) + 128*(-b*x + a)^(5/2)*a^5*b^2/x^(5/2) - 70*(-b*x + a)^(7/2)*a^5*b/x^(7/2) - 15*(-b*x + a)^(9/2)*a^5/x^(9/2))/(b^7 - 5*(b*x - a)*b^6/x + 10*(b*x - a)^2*b^5/x^2 - 10*(b*x - a)^3*b^4/x^3 + 5*(b*x - a)^4*b^3/x^4 - (b*x - a)^5*b^2/x^5)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} (a - bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(a - b*x)^(5/2),x)

[Out] int(x^(3/2)*(a - b*x)^(5/2), x)

sympy [A] time = 16.40, size = 379, normalized size = 2.60

$$\left\{ \begin{array}{l} \frac{3ia^{\frac{9}{2}}\sqrt{x}}{128b^2\sqrt{-1+\frac{bx}{a}}} - \frac{7ia^{\frac{7}{2}}x^{\frac{3}{2}}}{128b\sqrt{-1+\frac{bx}{a}}} - \frac{129ia^{\frac{5}{2}}x^{\frac{5}{2}}}{320\sqrt{-1+\frac{bx}{a}}} + \frac{73ia^{\frac{3}{2}}bx^{\frac{7}{2}}}{80\sqrt{-1+\frac{bx}{a}}} - \frac{29i\sqrt{a}b^2x^{\frac{9}{2}}}{40\sqrt{-1+\frac{bx}{a}}} - \frac{3ia^5 \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{128b^{\frac{5}{2}}} + \frac{ib^3x^{\frac{11}{2}}}{5\sqrt{a}\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{3a^{\frac{9}{2}}\sqrt{x}}{128b^2\sqrt{1-\frac{bx}{a}}} + \frac{7a^{\frac{7}{2}}x^{\frac{3}{2}}}{128b\sqrt{1-\frac{bx}{a}}} + \frac{129a^{\frac{5}{2}}x^{\frac{5}{2}}}{320\sqrt{1-\frac{bx}{a}}} - \frac{73a^{\frac{3}{2}}bx^{\frac{7}{2}}}{80\sqrt{1-\frac{bx}{a}}} + \frac{29\sqrt{a}b^2x^{\frac{9}{2}}}{40\sqrt{1-\frac{bx}{a}}} + \frac{3a^5 \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{128b^{\frac{5}{2}}} - \frac{b^3x^{\frac{11}{2}}}{5\sqrt{a}\sqrt{1-\frac{bx}{a}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)*(-b*x+a)**(5/2),x)

[Out] Piecewise((3*I*a**(9/2)*sqrt(x)/(128*b**2*sqrt(-1 + b*x/a)) - I*a**(7/2)*x**(3/2)/(128*b*sqrt(-1 + b*x/a)) - 129*I*a**(5/2)*x**(5/2)/(320*sqrt(-1 + b*x/a)) + 73*I*a**(3/2)*b*x**(7/2)/(80*sqrt(-1 + b*x/a)) - 29*I*sqrt(a)*b**2*x**(9/2)/(40*sqrt(-1 + b*x/a)) - 3*I*a**5*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(1

```

28*b**(5/2)) + I*b**3*x**(11/2)/(5*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) >
1), (-3*a**(9/2)*sqrt(x)/(128*b**2*sqrt(1 - b*x/a)) + a**(7/2)*x**(3/2)/(12
8*b*sqrt(1 - b*x/a)) + 129*a**(5/2)*x**(5/2)/(320*sqrt(1 - b*x/a)) - 73*a**
(3/2)*b*x**(7/2)/(80*sqrt(1 - b*x/a)) + 29*sqrt(a)*b**2*x**(9/2)/(40*sqrt(1
- b*x/a)) + 3*a**5*asin(sqrt(b)*sqrt(x)/sqrt(a))/(128*b**(5/2)) - b**3*x**
(11/2)/(5*sqrt(a)*sqrt(1 - b*x/a)), True))

```

3.553 $\int \sqrt{x} (a - bx)^{5/2} dx$

Optimal. Leaf size=121

$$\frac{5a^4 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{64b^{3/2}} - \frac{5a^3 \sqrt{x} \sqrt{a-bx}}{64b} + \frac{5}{32} a^2 x^{3/2} \sqrt{a-bx} + \frac{5}{24} a x^{3/2} (a-bx)^{3/2} + \frac{1}{4} x^{3/2} (a-bx)^{5/2}$$

[Out] $5/24*a*x^{(3/2)}*(-b*x+a)^{(3/2)}+1/4*x^{(3/2)}*(-b*x+a)^{(5/2)}+5/64*a^4*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(3/2)}+5/32*a^2*x^{(3/2)}*(-b*x+a)^{(1/2)}-5/64*a^3*x^{(1/2)}*(-b*x+a)^{(1/2)}/b$

Rubi [A] time = 0.04, antiderivative size = 121, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$\frac{5a^4 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{64b^{3/2}} + \frac{5}{32} a^2 x^{3/2} \sqrt{a-bx} - \frac{5a^3 \sqrt{x} \sqrt{a-bx}}{64b} + \frac{5}{24} a x^{3/2} (a-bx)^{3/2} + \frac{1}{4} x^{3/2} (a-bx)^{5/2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*(a - b*x)^(5/2), x]

[Out] $(-5*a^3*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(64*b) + (5*a^2*x^{(3/2)}*\text{Sqrt}[a - b*x])/32 + (5*a*x^{(3/2)}*(a - b*x)^{(3/2)})/24 + (x^{(3/2)}*(a - b*x)^{(5/2)})/4 + (5*a^4*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(64*b^{(3/2)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \sqrt{x} (a - bx)^{5/2} dx &= \frac{1}{4} x^{3/2} (a - bx)^{5/2} + \frac{1}{8} (5a) \int \sqrt{x} (a - bx)^{3/2} dx \\
&= \frac{5}{24} ax^{3/2} (a - bx)^{3/2} + \frac{1}{4} x^{3/2} (a - bx)^{5/2} + \frac{1}{16} (5a^2) \int \sqrt{x} \sqrt{a - bx} dx \\
&= \frac{5}{32} a^2 x^{3/2} \sqrt{a - bx} + \frac{5}{24} ax^{3/2} (a - bx)^{3/2} + \frac{1}{4} x^{3/2} (a - bx)^{5/2} + \frac{1}{64} (5a^3) \int \frac{\sqrt{x}}{\sqrt{a - bx}} dx \\
&= -\frac{5a^3 \sqrt{x} \sqrt{a - bx}}{64b} + \frac{5}{32} a^2 x^{3/2} \sqrt{a - bx} + \frac{5}{24} ax^{3/2} (a - bx)^{3/2} + \frac{1}{4} x^{3/2} (a - bx)^{5/2} + \frac{(5a^4) \int \sqrt{x}}{1} \\
&= -\frac{5a^3 \sqrt{x} \sqrt{a - bx}}{64b} + \frac{5}{32} a^2 x^{3/2} \sqrt{a - bx} + \frac{5}{24} ax^{3/2} (a - bx)^{3/2} + \frac{1}{4} x^{3/2} (a - bx)^{5/2} + \frac{(5a^4) \text{Su}}{1} \\
&= -\frac{5a^3 \sqrt{x} \sqrt{a - bx}}{64b} + \frac{5}{32} a^2 x^{3/2} \sqrt{a - bx} + \frac{5}{24} ax^{3/2} (a - bx)^{3/2} + \frac{1}{4} x^{3/2} (a - bx)^{5/2} + \frac{(5a^4) \text{Su}}{1} \\
&= -\frac{5a^3 \sqrt{x} \sqrt{a - bx}}{64b} + \frac{5}{32} a^2 x^{3/2} \sqrt{a - bx} + \frac{5}{24} ax^{3/2} (a - bx)^{3/2} + \frac{1}{4} x^{3/2} (a - bx)^{5/2} + \frac{5a^4 \tan^{-1}}{64}
\end{aligned}$$

Mathematica [A] time = 0.13, size = 98, normalized size = 0.81

$$\frac{\sqrt{a - bx} \left(\frac{15a^{7/2} \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{1 - \frac{bx}{a}}} + \sqrt{b} \sqrt{x} (-15a^3 + 118a^2 bx - 136ab^2 x^2 + 48b^3 x^3) \right)}{192b^{3/2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[x]*(a - b*x)^(5/2), x]
```

[Out] (Sqrt[a - b*x]*(Sqrt[b]*Sqrt[x]*(-15*a^3 + 118*a^2*b*x - 136*a*b^2*x^2 + 48*b^3*x^3) + (15*a^(7/2)*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/Sqrt[1 - (b*x)/a]))/(192*b^(3/2))

fricas [A] time = 0.45, size = 164, normalized size = 1.36

$$\left[\frac{15 a^4 \sqrt{-b} \log(-2 b x + 2 \sqrt{-b x + a} \sqrt{-b} \sqrt{x} + a) - 2 (48 b^4 x^3 - 136 a b^3 x^2 + 118 a^2 b^2 x - 15 a^3 b) \sqrt{-b x + a} \sqrt{x}}{384 b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)*x^(1/2),x, algorithm="fricas")

[Out] [-1/384*(15*a^4*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*(48*b^4*x^3 - 136*a*b^3*x^2 + 118*a^2*b^2*x - 15*a^3*b)*sqrt(-b*x + a)*sqrt(x))/b^2, -1/192*(15*a^4*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - (48*b^4*x^3 - 136*a*b^3*x^2 + 118*a^2*b^2*x - 15*a^3*b)*sqrt(-b*x + a)*sqrt(x))/b^2]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)*x^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 118, normalized size = 0.98

$$\frac{5\sqrt{-bx+a} a^2 x^{\frac{3}{2}}}{32} + \frac{5\sqrt{-bx+a} x a^4 \arctan\left(\frac{(x-\frac{a}{2b})\sqrt{b}}{\sqrt{-bx+a}x}\right)}{128\sqrt{-bx+a} b^{\frac{3}{2}}\sqrt{x}} - \frac{5\sqrt{-bx+a} a^3 \sqrt{x}}{64b} + \frac{5(-bx+a)^{\frac{3}{2}} a x^{\frac{3}{2}}}{24} + \frac{(-bx+a)^{\frac{5}{2}} x^{\frac{3}{2}}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+a)^(5/2)*x^(1/2),x)

[Out] 1/4*x^(3/2)*(-b*x+a)^(5/2)+5/24*a*x^(3/2)*(-b*x+a)^(3/2)+5/32*a^2*x^(3/2)*(-b*x+a)^(1/2)-5/64*a^3*x^(1/2)*(-b*x+a)^(1/2)/b+5/128*a^4/b^(3/2)*((-b*x+a)*x)^(1/2)/x^(1/2)/(-b*x+a)^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))

maxima [A] time = 3.05, size = 168, normalized size = 1.39

$$-\frac{5a^4 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{64b^{\frac{3}{2}}} + \frac{15\sqrt{-bx+a}a^4b^3}{\sqrt{x}} + \frac{55(-bx+a)^{\frac{3}{2}}a^4b^2}{x^{\frac{3}{2}}} + \frac{73(-bx+a)^{\frac{5}{2}}a^4b}{x^{\frac{5}{2}}} - \frac{15(-bx+a)^{\frac{7}{2}}a^4}{x^{\frac{7}{2}}}$$

$$192\left(b^5 - \frac{4(bx-a)b^4}{x} + \frac{6(bx-a)^2b^3}{x^2} - \frac{4(bx-a)^3b^2}{x^3} + \frac{(bx-a)^4b}{x^4}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)*x^(1/2),x, algorithm="maxima")

[Out] $-5/64*a^4*\arctan(\sqrt{-b*x+a}/(\sqrt{b}*\sqrt{x}))/b^{3/2} + 1/192*(15*\sqrt{-b*x+a}*a^4*b^3/\sqrt{x} + 55*(-b*x+a)^{3/2}*a^4*b^2/x^{3/2} + 73*(-b*x+a)^{5/2}*a^4*b/x^{5/2} - 15*(-b*x+a)^{7/2}*a^4/x^{7/2})/(b^5 - 4*(b*x-a)*b^4/x + 6*(b*x-a)^2*b^3/x^2 - 4*(b*x-a)^3*b^2/x^3 + (b*x-a)^4*b/x^4)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{x} (a - bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)*(a - b*x)^(5/2),x)

[Out] int(x^(1/2)*(a - b*x)^(5/2), x)

sympy [A] time = 9.81, size = 326, normalized size = 2.69

$$\left\{ \begin{array}{l} \frac{5ia^{\frac{7}{2}}\sqrt{x}}{64b\sqrt{-1+\frac{bx}{a}}} - \frac{133ia^{\frac{5}{2}}x^{\frac{3}{2}}}{192\sqrt{-1+\frac{bx}{a}}} + \frac{127ia^{\frac{3}{2}}bx^{\frac{5}{2}}}{96\sqrt{-1+\frac{bx}{a}}} - \frac{23i\sqrt{a}b^2x^{\frac{7}{2}}}{24\sqrt{-1+\frac{bx}{a}}} - \frac{5ia^4 \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{64b^{\frac{3}{2}}} + \frac{ib^3x^{\frac{9}{2}}}{4\sqrt{a}\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{5a^{\frac{7}{2}}\sqrt{x}}{64b\sqrt{1-\frac{bx}{a}}} + \frac{133a^{\frac{5}{2}}x^{\frac{3}{2}}}{192\sqrt{1-\frac{bx}{a}}} - \frac{127a^{\frac{3}{2}}bx^{\frac{5}{2}}}{96\sqrt{1-\frac{bx}{a}}} + \frac{23\sqrt{a}b^2x^{\frac{7}{2}}}{24\sqrt{1-\frac{bx}{a}}} + \frac{5a^4 \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{64b^{\frac{3}{2}}} - \frac{b^3x^{\frac{9}{2}}}{4\sqrt{a}\sqrt{1-\frac{bx}{a}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)**(5/2)*x**(1/2),x)

[Out] Piecewise((5*I*a**(7/2)*sqrt(x)/(64*b*sqrt(-1 + b*x/a)) - 133*I*a**(5/2)*x*(3/2)/(192*sqrt(-1 + b*x/a)) + 127*I*a**(3/2)*b*x**(5/2)/(96*sqrt(-1 + b*x/a)) - 23*I*sqrt(a)*b**2*x**(7/2)/(24*sqrt(-1 + b*x/a)) - 5*I*a**4*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(64*b**(3/2)) + I*b**3*x**(9/2)/(4*sqrt(a)*sqrt(-1 +

```
b*x/a)), Abs(b*x/a) > 1), (-5*a**(7/2)*sqrt(x)/(64*b*sqrt(1 - b*x/a)) + 13  
3*a**(5/2)*x**(3/2)/(192*sqrt(1 - b*x/a)) - 127*a**(3/2)*b*x**(5/2)/(96*sqrt(1 - b*x/a)) + 23*sqrt(a)*b**2*x**(7/2)/(24*sqrt(1 - b*x/a)) + 5*a**4*asin(sqrt(b)*sqrt(x)/sqrt(a))/(64*b**(3/2)) - b**3*x**(9/2)/(4*sqrt(a)*sqrt(1 - b*x/a)), True))
```


$$3.554 \quad \int \frac{(a-bx)^{5/2}}{\sqrt{x}} dx$$

Optimal. Leaf size=96

$$\frac{5a^3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{8\sqrt{b}} + \frac{5}{8}a^2\sqrt{x}\sqrt{a-bx} + \frac{5}{12}a\sqrt{x}(a-bx)^{3/2} + \frac{1}{3}\sqrt{x}(a-bx)^{5/2}$$

[Out] $5/8*a^3*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(1/2)}+5/12*a*(-b*x+a)^{(3/2)}*x^{(1/2)}+1/3*(-b*x+a)^{(5/2)}*x^{(1/2)}+5/8*a^2*x^{(1/2)}*(-b*x+a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$\frac{5}{8}a^2\sqrt{x}\sqrt{a-bx} + \frac{5a^3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{8\sqrt{b}} + \frac{5}{12}a\sqrt{x}(a-bx)^{3/2} + \frac{1}{3}\sqrt{x}(a-bx)^{5/2}$$

Antiderivative was successfully verified.

[In] Int[(a - b*x)^(5/2)/Sqrt[x], x]

[Out] $(5*a^2*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/8 + (5*a*\text{Sqrt}[x]*(a - b*x)^{(3/2)})/12 + (\text{Sqrt}[x]*(a - b*x)^{(5/2)})/3 + (5*a^3*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/ \text{Sqrt}[a - b*x]])/(8*\text{Sqrt}[b])$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

```
Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
 \int \frac{(a - bx)^{5/2}}{\sqrt{x}} dx &= \frac{1}{3} \sqrt{x} (a - bx)^{5/2} + \frac{1}{6} (5a) \int \frac{(a - bx)^{3/2}}{\sqrt{x}} dx \\
 &= \frac{5}{12} a \sqrt{x} (a - bx)^{3/2} + \frac{1}{3} \sqrt{x} (a - bx)^{5/2} + \frac{1}{8} (5a^2) \int \frac{\sqrt{a - bx}}{\sqrt{x}} dx \\
 &= \frac{5}{8} a^2 \sqrt{x} \sqrt{a - bx} + \frac{5}{12} a \sqrt{x} (a - bx)^{3/2} + \frac{1}{3} \sqrt{x} (a - bx)^{5/2} + \frac{1}{16} (5a^3) \int \frac{1}{\sqrt{x} \sqrt{a - bx}} dx \\
 &= \frac{5}{8} a^2 \sqrt{x} \sqrt{a - bx} + \frac{5}{12} a \sqrt{x} (a - bx)^{3/2} + \frac{1}{3} \sqrt{x} (a - bx)^{5/2} + \frac{1}{8} (5a^3) \text{Subst} \left(\int \frac{1}{\sqrt{a - bx^2}} dx, x, \sqrt{a} \right) \\
 &= \frac{5}{8} a^2 \sqrt{x} \sqrt{a - bx} + \frac{5}{12} a \sqrt{x} (a - bx)^{3/2} + \frac{1}{3} \sqrt{x} (a - bx)^{5/2} + \frac{1}{8} (5a^3) \text{Subst} \left(\int \frac{1}{1 + bx^2} dx, x, \frac{\sqrt{a}}{\sqrt{b}} \right) \\
 &= \frac{5}{8} a^2 \sqrt{x} \sqrt{a - bx} + \frac{5}{12} a \sqrt{x} (a - bx)^{3/2} + \frac{1}{3} \sqrt{x} (a - bx)^{5/2} + \frac{5a^3 \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a - bx}} \right)}{8\sqrt{b}}
 \end{aligned}$$

Mathematica [A] time = 0.12, size = 82, normalized size = 0.85

$$\frac{1}{24} \sqrt{a - bx} \left(\frac{15a^{5/2} \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{b} \sqrt{1 - \frac{bx}{a}}} + \sqrt{x} (33a^2 - 26abx + 8b^2x^2) \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(a - b*x)^(5/2)/Sqrt[x], x]
```

```
[Out] (Sqrt[a - b*x]*(Sqrt[x]*(33*a^2 - 26*a*b*x + 8*b^2*x^2) + (15*a^(5/2)*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[b]*Sqrt[1 - (b*x)/a]))) / 24
```

fricas [A] time = 0.45, size = 142, normalized size = 1.48

$$\left[\frac{15 a^3 \sqrt{-b} \log(-2 b x + 2 \sqrt{-b x + a} \sqrt{-b} \sqrt{x} + a) - 2 (8 b^3 x^2 - 26 a b^2 x + 33 a^2 b) \sqrt{-b x + a} \sqrt{x}}{48 b}, - \frac{15 a^3 \sqrt{b} \arctan(\sqrt{-b x + a} / (\sqrt{b} \sqrt{x}))}{48 b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)/x^(1/2),x, algorithm="fricas")

[Out] [-1/48*(15*a^3*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*(8*b^3*x^2 - 26*a*b^2*x + 33*a^2*b)*sqrt(-b*x + a)*sqrt(x))/b, -1/24*(15*a^3*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - (8*b^3*x^2 - 26*a*b^2*x + 33*a^2*b)*sqrt(-b*x + a)*sqrt(x))/b]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)/x^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.00, size = 99, normalized size = 1.03

$$\frac{5 \sqrt{-b x + a} x a^3 \arctan\left(\frac{(x - \frac{a}{2b}) \sqrt{b}}{\sqrt{-b x^2 + a x}}\right)}{16 \sqrt{-b x + a} \sqrt{b} \sqrt{x}} + \frac{5 \sqrt{-b x + a} a^2 \sqrt{x}}{8} + \frac{5 (-b x + a)^{\frac{3}{2}} a \sqrt{x}}{12} + \frac{(-b x + a)^{\frac{5}{2}} \sqrt{x}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+a)^(5/2)/x^(1/2),x)

[Out] 1/3*(-b*x+a)^(5/2)*x^(1/2)+5/12*a*(-b*x+a)^(3/2)*x^(1/2)+5/8*a^2*x^(1/2)*(-b*x+a)^(1/2)+5/16*a^3*((-b*x+a)*x)^(1/2)/(-b*x+a)^(1/2)/x^(1/2)/b^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))

maxima [A] time = 2.93, size = 130, normalized size = 1.35

$$-\frac{5 a^3 \arctan\left(\frac{\sqrt{-b x + a}}{\sqrt{b} \sqrt{x}}\right)}{8 \sqrt{b}} + \frac{\frac{15 \sqrt{-b x + a} a^3 b^2}{\sqrt{x}} + \frac{40 (-b x + a)^{\frac{3}{2}} a^3 b}{x^2} + \frac{33 (-b x + a)^{\frac{5}{2}} a^3}{x^2}}{24 \left(b^3 - \frac{3 (b x - a) b^2}{x} + \frac{3 (b x - a)^2 b}{x^2} - \frac{(b x - a)^3}{x^3} \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)/x^(1/2),x, algorithm="maxima")

[Out] $-5/8*a^3*\arctan(\sqrt{-b*x+a}/(\sqrt{b}*\sqrt{x}))/\sqrt{b} + 1/24*(15*\sqrt{-b*x+a}*a^3*b^2/\sqrt{x} + 40*(-b*x+a)^{(3/2)}*a^3*b/x^{(3/2)} + 33*(-b*x+a)^{(5/2)}*a^3/x^{(5/2)})/(b^3 - 3*(b*x-a)*b^2/x + 3*(b*x-a)^2*b/x^2 - (b*x-a)^3/x^3)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a-bx)^{5/2}}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - b*x)^(5/2)/x^(1/2), x)

[Out] int((a - b*x)^(5/2)/x^(1/2), x)

sympy [A] time = 6.23, size = 246, normalized size = 2.56

$$\left\{ \begin{array}{ll} -\frac{11ia^5\sqrt{x}}{8\sqrt{-1+\frac{bx}{a}}} + \frac{59ia^3bx^2}{24\sqrt{-1+\frac{bx}{a}}} - \frac{17i\sqrt{a}b^2x^2}{12\sqrt{-1+\frac{bx}{a}}} - \frac{5ia^3\operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8\sqrt{b}} + \frac{ib^3x^2}{3\sqrt{a}\sqrt{-1+\frac{bx}{a}}} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ \frac{11a^5\sqrt{x}\sqrt{1-\frac{bx}{a}}}{8} - \frac{13a^3bx^2\sqrt{1-\frac{bx}{a}}}{12} + \frac{\sqrt{a}b^2x^2\sqrt{1-\frac{bx}{a}}}{3} + \frac{5a^3\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8\sqrt{b}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)**(5/2)/x**(1/2),x)

[Out] Piecewise((-11*I*a**(5/2)*sqrt(x)/(8*sqrt(-1 + b*x/a)) + 59*I*a**(3/2)*b*x*(3/2)/(24*sqrt(-1 + b*x/a)) - 17*I*sqrt(a)*b**2*x**(5/2)/(12*sqrt(-1 + b*x/a)) - 5*I*a**3*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(8*sqrt(b)) + I*b**3*x**(7/2)/(3*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (11*a**(5/2)*sqrt(x)*sqrt(1 - b*x/a)/8 - 13*a**(3/2)*b*x**(3/2)*sqrt(1 - b*x/a)/12 + sqrt(a)*b**2*x**(5/2)*sqrt(1 - b*x/a)/3 + 5*a**3*asin(sqrt(b)*sqrt(x)/sqrt(a))/(8*sqrt(b)), True))

$$3.555 \quad \int \frac{(a-bx)^{5/2}}{x^{3/2}} dx$$

Optimal. Leaf size=93

$$-\frac{15}{4}a^2\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right) - \frac{2(a-bx)^{5/2}}{\sqrt{x}} - \frac{5}{2}b\sqrt{x}(a-bx)^{3/2} - \frac{15}{4}ab\sqrt{x}\sqrt{a-bx}$$

[Out] $-15/4*a^2*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})*b^{(1/2)}-2*(-b*x+a)^{(5/2)/x^{(1/2)}-5/2*b*(-b*x+a)^{(3/2)}*x^{(1/2)}-15/4*a*b*x^{(1/2)}*(-b*x+a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.312$, Rules used = {47, 50, 63, 217, 203}

$$-\frac{15}{4}a^2\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right) - \frac{2(a-bx)^{5/2}}{\sqrt{x}} - \frac{5}{2}b\sqrt{x}(a-bx)^{3/2} - \frac{15}{4}ab\sqrt{x}\sqrt{a-bx}$$

Antiderivative was successfully verified.

[In] Int[(a - b*x)^(5/2)/x^(3/2), x]

[Out] $(-15*a*b*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/4 - (5*b*\text{Sqrt}[x]*(a - b*x)^{(3/2)})/2 - (2*(a - b*x)^{(5/2)})/\text{Sqrt}[x] - (15*a^2*\text{Sqrt}[b]*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/4$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a - bx)^{5/2}}{x^{3/2}} dx &= -\frac{2(a - bx)^{5/2}}{\sqrt{x}} - (5b) \int \frac{(a - bx)^{3/2}}{\sqrt{x}} dx \\
&= -\frac{5}{2}b\sqrt{x}(a - bx)^{3/2} - \frac{2(a - bx)^{5/2}}{\sqrt{x}} - \frac{1}{4}(15ab) \int \frac{\sqrt{a - bx}}{\sqrt{x}} dx \\
&= -\frac{15}{4}ab\sqrt{x}\sqrt{a - bx} - \frac{5}{2}b\sqrt{x}(a - bx)^{3/2} - \frac{2(a - bx)^{5/2}}{\sqrt{x}} - \frac{1}{8}(15a^2b) \int \frac{1}{\sqrt{x}\sqrt{a - bx}} dx \\
&= -\frac{15}{4}ab\sqrt{x}\sqrt{a - bx} - \frac{5}{2}b\sqrt{x}(a - bx)^{3/2} - \frac{2(a - bx)^{5/2}}{\sqrt{x}} - \frac{1}{4}(15a^2b) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a - bx^2}} dx, x, \sqrt{a - bx}\right) \\
&= -\frac{15}{4}ab\sqrt{x}\sqrt{a - bx} - \frac{5}{2}b\sqrt{x}(a - bx)^{3/2} - \frac{2(a - bx)^{5/2}}{\sqrt{x}} - \frac{1}{4}(15a^2b) \operatorname{Subst}\left(\int \frac{1}{1 + bx^2} dx, x, \frac{\sqrt{a - bx}}{\sqrt{a}}\right) \\
&= -\frac{15}{4}ab\sqrt{x}\sqrt{a - bx} - \frac{5}{2}b\sqrt{x}(a - bx)^{3/2} - \frac{2(a - bx)^{5/2}}{\sqrt{x}} - \frac{15}{4}a^2\sqrt{b} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a - bx}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 49, normalized size = 0.53

$$\frac{2a^2\sqrt{a - bx} {}_2F_1\left(-\frac{5}{2}, -\frac{1}{2}; \frac{1}{2}; \frac{bx}{a}\right)}{\sqrt{x}\sqrt{1 - \frac{bx}{a}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - b*x)^(5/2)/x^(3/2),x]

[Out] $(-2*a^2*\text{Sqrt}[a - b*x]*\text{Hypergeometric2F1}[-5/2, -1/2, 1/2, (b*x)/a]) / (\text{Sqrt}[x] * \text{Sqrt}[1 - (b*x)/a])$

fricas [A] time = 0.48, size = 137, normalized size = 1.47

$$\left[\frac{15 a^2 \sqrt{-b} x \log(-2 b x + 2 \sqrt{-b x + a} \sqrt{-b} \sqrt{x} + a) + 2 (2 b^2 x^2 - 9 a b x - 8 a^2) \sqrt{-b x + a} \sqrt{x}}{8 x}, \frac{15 a^2 \sqrt{b} x \arctan\left(\frac{\sqrt{-b x + a}}{\sqrt{b} \sqrt{x}}\right)}{4 \left(b^2 - \frac{2(b x - a) b}{x} + \frac{(b x - a)^2}{x^2}\right)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)/x^(3/2),x, algorithm="fricas")

[Out] $[1/8*(15*a^2*\text{sqrt}(-b)*x*\log(-2*b*x + 2*\text{sqrt}(-b*x + a)*\text{sqrt}(-b)*\text{sqrt}(x) + a) + 2*(2*b^2*x^2 - 9*a*b*x - 8*a^2)*\text{sqrt}(-b*x + a)*\text{sqrt}(x))/x, 1/4*(15*a^2*\text{sqrt}(b)*x*\arctan(\text{sqrt}(-b*x + a)/(\text{sqrt}(b)*\text{sqrt}(x))) + (2*b^2*x^2 - 9*a*b*x - 8*a^2)*\text{sqrt}(-b*x + a)*\text{sqrt}(x))/x]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)/x^(3/2),x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{(-bx + a)^{\frac{5}{2}}}{x^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+a)^(5/2)/x^(3/2),x)

[Out] int((-b*x+a)^(5/2)/x^(3/2),x)

maxima [A] time = 2.99, size = 112, normalized size = 1.20

$$\frac{15}{4} a^2 \sqrt{b} \arctan\left(\frac{\sqrt{-bx + a}}{\sqrt{b} \sqrt{x}}\right) - \frac{2 \sqrt{-bx + a} a^2}{\sqrt{x}} - \frac{\frac{7 \sqrt{-bx+a} a^2 b^2}{\sqrt{x}} + \frac{9 (-bx+a)^{\frac{3}{2}} a^2 b}{x^{\frac{3}{2}}}}{4 \left(b^2 - \frac{2(bx-a)b}{x} + \frac{(bx-a)^2}{x^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)/x^(3/2),x, algorithm="maxima")

[Out] $15/4*a^2*\sqrt{b}*\arctan(\sqrt{-b*x+a}/(\sqrt{b}*\sqrt{x})) - 2*\sqrt{-b*x+a} * a^2/\sqrt{x} - 1/4*(7*\sqrt{-b*x+a}*a^2*b^2/\sqrt{x} + 9*(-b*x+a)^{(3/2)} * a^2*b/x^{(3/2)})/(b^2 - 2*(b*x-a)*b/x + (b*x-a)^2/x^2)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - bx)^{5/2}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - b*x)^(5/2)/x^(3/2),x)

[Out] int((a - b*x)^(5/2)/x^(3/2), x)

sympy [A] time = 6.22, size = 267, normalized size = 2.87

$$\left\{ \begin{array}{l} \frac{2ia^{\frac{5}{2}}}{\sqrt{x}\sqrt{-1+\frac{bx}{a}}} + \frac{ia^{\frac{3}{2}}b\sqrt{x}}{4\sqrt{-1+\frac{bx}{a}}} - \frac{11i\sqrt{a}b^2x^{\frac{3}{2}}}{4\sqrt{-1+\frac{bx}{a}}} + \frac{15ia^2\sqrt{b}\operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4} + \frac{ib^3x^{\frac{5}{2}}}{2\sqrt{a}\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{2a^{\frac{5}{2}}}{\sqrt{x}\sqrt{1-\frac{bx}{a}}} - \frac{a^{\frac{3}{2}}b\sqrt{x}}{4\sqrt{1-\frac{bx}{a}}} + \frac{11\sqrt{a}b^2x^{\frac{3}{2}}}{4\sqrt{1-\frac{bx}{a}}} - \frac{15a^2\sqrt{b}\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4} - \frac{b^3x^{\frac{5}{2}}}{2\sqrt{a}\sqrt{1-\frac{bx}{a}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)**(5/2)/x**(3/2),x)

[Out] Piecewise((2*I*a**(5/2)/(sqrt(x)*sqrt(-1 + b*x/a)) + I*a**(3/2)*b*sqrt(x)/(4*sqrt(-1 + b*x/a)) - 11*I*sqrt(a)*b**2*x**(3/2)/(4*sqrt(-1 + b*x/a)) + 15*I*a**2*sqrt(b)*acosh(sqrt(b)*sqrt(x)/sqrt(a))/4 + I*b**3*x**(5/2)/(2*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (-2*a**(5/2)/(sqrt(x)*sqrt(1 - b*x/a)) - a**(3/2)*b*sqrt(x)/(4*sqrt(1 - b*x/a)) + 11*sqrt(a)*b**2*x**(3/2)/(4*sqrt(1 - b*x/a)) - 15*a**2*sqrt(b)*asin(sqrt(b)*sqrt(x)/sqrt(a))/4 - b**3*x**(5/2)/(2*sqrt(a)*sqrt(1 - b*x/a)), True))

$$3.556 \quad \int \frac{(a-bx)^{5/2}}{x^{5/2}} dx$$

Optimal. Leaf size=90

$$5ab^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right) + 5b^2\sqrt{x}\sqrt{a-bx} - \frac{2(a-bx)^{5/2}}{3x^{3/2}} + \frac{10b(a-bx)^{3/2}}{3\sqrt{x}}$$

[Out] $-2/3*(-b*x+a)^{(5/2)}/x^{(3/2)}+5*a*b^{(3/2)}*\arctan(b^{(1/2)}*x^{(1/2)}/(-b*x+a)^{(1/2)})+10/3*b*(-b*x+a)^{(3/2)}/x^{(1/2)}+5*b^2*x^{(1/2)}*(-b*x+a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 90, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.312$, Rules used = {47, 50, 63, 217, 203}

$$5b^2\sqrt{x}\sqrt{a-bx} + 5ab^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right) - \frac{2(a-bx)^{5/2}}{3x^{3/2}} + \frac{10b(a-bx)^{3/2}}{3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[(a - b*x)^(5/2)/x^(5/2), x]

[Out] $5*b^2*\text{Sqrt}[x]*\text{Sqrt}[a - b*x] + (10*b*(a - b*x)^{(3/2)})/(3*\text{Sqrt}[x]) - (2*(a - b*x)^{(5/2)})/(3*x^{(3/2)}) + 5*a*b^{(3/2)}*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/ \text{Sqrt}[a - b*x]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a-bx)^{5/2}}{x^{5/2}} dx &= -\frac{2(a-bx)^{5/2}}{3x^{3/2}} - \frac{1}{3}(5b) \int \frac{(a-bx)^{3/2}}{x^{3/2}} dx \\
&= \frac{10b(a-bx)^{3/2}}{3\sqrt{x}} - \frac{2(a-bx)^{5/2}}{3x^{3/2}} + (5b^2) \int \frac{\sqrt{a-bx}}{\sqrt{x}} dx \\
&= 5b^2\sqrt{x}\sqrt{a-bx} + \frac{10b(a-bx)^{3/2}}{3\sqrt{x}} - \frac{2(a-bx)^{5/2}}{3x^{3/2}} + \frac{1}{2}(5ab^2) \int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx \\
&= 5b^2\sqrt{x}\sqrt{a-bx} + \frac{10b(a-bx)^{3/2}}{3\sqrt{x}} - \frac{2(a-bx)^{5/2}}{3x^{3/2}} + (5ab^2) \text{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x}\right) \\
&= 5b^2\sqrt{x}\sqrt{a-bx} + \frac{10b(a-bx)^{3/2}}{3\sqrt{x}} - \frac{2(a-bx)^{5/2}}{3x^{3/2}} + (5ab^2) \text{Subst}\left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right) \\
&= 5b^2\sqrt{x}\sqrt{a-bx} + \frac{10b(a-bx)^{3/2}}{3\sqrt{x}} - \frac{2(a-bx)^{5/2}}{3x^{3/2}} + 5ab^{3/2} \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 51, normalized size = 0.57

$$-\frac{2a^2\sqrt{a-bx} {}_2F_1\left(-\frac{5}{2}, -\frac{3}{2}; -\frac{1}{2}; \frac{bx}{a}\right)}{3x^{3/2}\sqrt{1-\frac{bx}{a}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - b*x)^(5/2)/x^(5/2),x]

[Out] $(-2a^2\sqrt{a - bx} \operatorname{Hypergeometric2F1}[-5/2, -3/2, -1/2, (bx)/a]) / (3x^{3/2}\sqrt{1 - (bx)/a})$

fricas [A] time = 0.45, size = 139, normalized size = 1.54

$$\left[\frac{15a\sqrt{-b}bx^2 \log(-2bx - 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) + 2(3b^2x^2 + 14abx - 2a^2)\sqrt{-bx+a}\sqrt{x}}{6x^2}, -\frac{15ab^{\frac{3}{2}}x^2 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{6x^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)/x^(5/2),x, algorithm="fricas")

[Out] $[1/6*(15*a*\sqrt{-b}*b*x^2*\log(-2*b*x - 2*\sqrt{-b*x + a}*\sqrt{-b}*\sqrt{x} + a) + 2*(3*b^2*x^2 + 14*a*b*x - 2*a^2)*\sqrt{-b*x + a}*\sqrt{x})/x^2, -1/3*(15*a*b^{3/2}*x^2*\arctan(\sqrt{-b*x + a}/(\sqrt{b}*\sqrt{x}))) - (3*b^2*x^2 + 14*a*b*x - 2*a^2)*\sqrt{-b*x + a}*\sqrt{x})/x^2]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)/x^(5/2),x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{(-bx + a)^{\frac{5}{2}}}{x^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*x+a)^(5/2)/x^(5/2),x)

[Out] int((-b*x+a)^(5/2)/x^(5/2),x)

maxima [A] time = 3.00, size = 84, normalized size = 0.93

$$-5ab^{\frac{3}{2}} \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right) + \frac{4\sqrt{-bx+a}ab}{\sqrt{x}} + \frac{\sqrt{-bx+a}ab^2}{\left(b - \frac{bx-a}{x}\right)\sqrt{x}} - \frac{2(-bx+a)^{\frac{3}{2}}a}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)^(5/2)/x^(5/2),x, algorithm="maxima")

[Out] $-5*a*b^{3/2}*\arctan(\sqrt{-b*x + a}/(\sqrt{b}*\sqrt{x})) + 4*\sqrt{-b*x + a}*a*b/\sqrt{x} + \sqrt{-b*x + a}*a*b^2/((b - (b*x - a)/x)*\sqrt{x}) - 2/3*(-b*x + a)^{3/2}*a/x^{3/2}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - bx)^{5/2}}{x^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - b*x)^(5/2)/x^(5/2),x)

[Out] int((a - b*x)^(5/2)/x^(5/2), x)

sympy [C] time = 5.85, size = 245, normalized size = 2.72

$$\begin{cases} -\frac{2a^2\sqrt{b}\sqrt{\frac{a}{bx}-1}}{3x} + \frac{14ab^{\frac{3}{2}}\sqrt{\frac{a}{bx}-1}}{3} - 5iab^{\frac{3}{2}}\log\left(\frac{\sqrt{a}}{\sqrt{b}\sqrt{x}}\right) + \frac{5iab^{\frac{3}{2}}\log\left(\frac{a}{bx}\right)}{2} + 5ab^{\frac{3}{2}}\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) + b^{\frac{5}{2}}x\sqrt{\frac{a}{bx}-1} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ -\frac{2ia^2\sqrt{b}\sqrt{-\frac{a}{bx}+1}}{3x} + \frac{14iab^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}}{3} + \frac{5iab^{\frac{3}{2}}\log\left(\frac{a}{bx}\right)}{2} - 5iab^{\frac{3}{2}}\log\left(\sqrt{-\frac{a}{bx}+1}+1\right) + ib^{\frac{5}{2}}x\sqrt{-\frac{a}{bx}+1} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+a)**(5/2)/x**(5/2),x)

[Out] Piecewise((-2*a**2*sqrt(b)*sqrt(a/(b*x) - 1)/(3*x) + 14*a*b**(3/2)*sqrt(a/(b*x) - 1)/3 - 5*I*a*b**(3/2)*log(sqrt(a)/(sqrt(b)*sqrt(x))) + 5*I*a*b**(3/2)*log(a/(b*x))/2 + 5*a*b**(3/2)*asin(sqrt(b)*sqrt(x)/sqrt(a)) + b**(5/2)*x*sqrt(a/(b*x) - 1), Abs(a/(b*x)) > 1), (-2*I*a**2*sqrt(b)*sqrt(-a/(b*x) + 1)/(3*x) + 14*I*a*b**(3/2)*sqrt(-a/(b*x) + 1)/3 + 5*I*a*b**(3/2)*log(a/(b*x))/2 - 5*I*a*b**(3/2)*log(sqrt(-a/(b*x) + 1) + 1) + I*b**(5/2)*x*sqrt(-a/(b*x) + 1), True))

3.557 $\int x^{5/2}(2 + bx)^{5/2} dx$

Optimal. Leaf size=144

$$-\frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{8b^{7/2}} + \frac{5\sqrt{x}\sqrt{bx+2}}{16b^3} - \frac{5x^{3/2}\sqrt{bx+2}}{48b^2} + \frac{1}{6}x^{7/2}(bx+2)^{5/2} + \frac{1}{6}x^{7/2}(bx+2)^{3/2} + \frac{1}{8}x^{7/2}\sqrt{bx+2} + \frac{x^{5/2}\sqrt{bx+2}}{24b}$$

[Out] $1/6*x^{(7/2)}*(b*x+2)^{(3/2)}+1/6*x^{(7/2)}*(b*x+2)^{(5/2)}-5/8*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(7/2)}-5/48*x^{(3/2)}*(b*x+2)^{(1/2)}/b^2+1/24*x^{(5/2)}*(b*x+2)^{(1/2)}/b+1/8*x^{(7/2)}*(b*x+2)^{(1/2)}+5/16*x^{(1/2)}*(b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.05, antiderivative size = 144, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{5x^{3/2}\sqrt{bx+2}}{48b^2} + \frac{5\sqrt{x}\sqrt{bx+2}}{16b^3} - \frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{8b^{7/2}} + \frac{1}{6}x^{7/2}(bx+2)^{5/2} + \frac{1}{6}x^{7/2}(bx+2)^{3/2} + \frac{1}{8}x^{7/2}\sqrt{bx+2} + \frac{x^{5/2}\sqrt{bx+2}}{24b}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(5/2)}*(2 + b*x)^{(5/2)}, x]$

[Out] $(5*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/(16*b^3) - (5*x^{(3/2)}*\operatorname{Sqrt}[2 + b*x])/(48*b^2) + (x^{(5/2)}*\operatorname{Sqrt}[2 + b*x])/(24*b) + (x^{(7/2)}*\operatorname{Sqrt}[2 + b*x])/8 + (x^{(7/2)}*(2 + b*x)^{(3/2)})/6 + (x^{(7/2)}*(2 + b*x)^{(5/2)})/6 - (5*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]])/(8*b^{(7/2)})$

Rule 50

$\operatorname{Int}[(a + b*x)^m * (c + d*x)^n, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{m+1} * (c + d*x)^n / (b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d)) / (b*(m+n+1)), \operatorname{Int}[(a + b*x)^m * (c + d*x)^{n-1}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m+n+1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m-n, 0]))) && !ILtQ[m+n+2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

$\operatorname{Int}[1/(\operatorname{Sqrt}[a + b*x] * \operatorname{Sqrt}[c + d*x]), x_Symbol] \rightarrow \operatorname{Dist}[2/\operatorname{Sqrt}[b], \operatorname{Subst}[\operatorname{Int}[1/\operatorname{Sqrt}[b*c - a*d + d*x^2], x], x, \operatorname{Sqrt}[a + b*x]], x] /;$ FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 215

Int[1/Sqrt[(a_) + (b.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned}
 \int x^{5/2}(2+bx)^{5/2} dx &= \frac{1}{6}x^{7/2}(2+bx)^{5/2} + \frac{5}{6} \int x^{5/2}(2+bx)^{3/2} dx \\
 &= \frac{1}{6}x^{7/2}(2+bx)^{3/2} + \frac{1}{6}x^{7/2}(2+bx)^{5/2} + \frac{1}{2} \int x^{5/2}\sqrt{2+bx} dx \\
 &= \frac{1}{8}x^{7/2}\sqrt{2+bx} + \frac{1}{6}x^{7/2}(2+bx)^{3/2} + \frac{1}{6}x^{7/2}(2+bx)^{5/2} + \frac{1}{8} \int \frac{x^{5/2}}{\sqrt{2+bx}} dx \\
 &= \frac{x^{5/2}\sqrt{2+bx}}{24b} + \frac{1}{8}x^{7/2}\sqrt{2+bx} + \frac{1}{6}x^{7/2}(2+bx)^{3/2} + \frac{1}{6}x^{7/2}(2+bx)^{5/2} - \frac{5 \int \frac{x^{3/2}}{\sqrt{2+bx}} dx}{24b} \\
 &= -\frac{5x^{3/2}\sqrt{2+bx}}{48b^2} + \frac{x^{5/2}\sqrt{2+bx}}{24b} + \frac{1}{8}x^{7/2}\sqrt{2+bx} + \frac{1}{6}x^{7/2}(2+bx)^{3/2} + \frac{1}{6}x^{7/2}(2+bx)^{5/2} + \dots \\
 &= \frac{5\sqrt{x}\sqrt{2+bx}}{16b^3} - \frac{5x^{3/2}\sqrt{2+bx}}{48b^2} + \frac{x^{5/2}\sqrt{2+bx}}{24b} + \frac{1}{8}x^{7/2}\sqrt{2+bx} + \frac{1}{6}x^{7/2}(2+bx)^{3/2} + \frac{1}{6}x^{7/2}(2+bx)^{5/2} \\
 &= \frac{5\sqrt{x}\sqrt{2+bx}}{16b^3} - \frac{5x^{3/2}\sqrt{2+bx}}{48b^2} + \frac{x^{5/2}\sqrt{2+bx}}{24b} + \frac{1}{8}x^{7/2}\sqrt{2+bx} + \frac{1}{6}x^{7/2}(2+bx)^{3/2} + \frac{1}{6}x^{7/2}(2+bx)^{5/2} \\
 &= \frac{5\sqrt{x}\sqrt{2+bx}}{16b^3} - \frac{5x^{3/2}\sqrt{2+bx}}{48b^2} + \frac{x^{5/2}\sqrt{2+bx}}{24b} + \frac{1}{8}x^{7/2}\sqrt{2+bx} + \frac{1}{6}x^{7/2}(2+bx)^{3/2} + \frac{1}{6}x^{7/2}(2+bx)^{5/2}
 \end{aligned}$$

Mathematica [A] time = 0.06, size = 86, normalized size = 0.60

$$\frac{\sqrt{x}\sqrt{bx+2}\left(8b^5x^5+40b^4x^4+54b^3x^3+2b^2x^2-5bx+15\right)}{48b^3} - \frac{5\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{8b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)*(2 + b*x)^(5/2), x]

[Out] (Sqrt[x]*Sqrt[2 + b*x]*(15 - 5*b*x + 2*b^2*x^2 + 54*b^3*x^3 + 40*b^4*x^4 + 8*b^5*x^5))/(48*b^3) - (5*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(8*b^(7/2))

fricas [A] time = 0.45, size = 172, normalized size = 1.19

$$\left[\frac{(8b^6x^5 + 40b^5x^4 + 54b^4x^3 + 2b^3x^2 - 5b^2x + 15b)\sqrt{bx+2}\sqrt{x} + 15\sqrt{b}\log(bx - \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{48b^4}, (8b^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+2)^(5/2),x, algorithm="fricas")

[Out] [1/48*((8*b^6*x^5 + 40*b^5*x^4 + 54*b^4*x^3 + 2*b^3*x^2 - 5*b^2*x + 15*b)*sqrt(b*x + 2)*sqrt(x) + 15*sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^4, 1/48*((8*b^6*x^5 + 40*b^5*x^4 + 54*b^4*x^3 + 2*b^3*x^2 - 5*b^2*x + 15*b)*sqrt(b*x + 2)*sqrt(x) + 30*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))))/b^4]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(b*x+2)^(5/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [83.4865739918,53.112478131]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32

, [0, 0]%%}, 0, %%{-1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{1, [4, 0]%%}+%%{-4, [3, 4]%%}+%%{12, [3, 3]%%}+%%{-20, [3, 2]%%}+%%{20, [3, 1]%%}+%%{-8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{-4, [1, 4]%%}+%%{20, [1, 3]%%}+%%{-40, [1, 2]%%}+%%{48, [1, 1]%%}+%%{-32, [1, 0]%%}+%%{1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{16, [0, 0]%%}] at parameters values [38.6973876911, 89.629912049]Warning, choosing root of [1, 0, %%{-4, [1, 1]%%}+%%{-4, [1, 0]%%}+%%{-4, [0, 1]%%}+%%{-8, [0, 0]%%}, 0, %%{6, [2, 2]%%}+%%{4, [2, 1]%%}+%%{6, [2, 0]%%}+%%{4, [1, 2]%%}+%%{28, [1, 1]%%}+%%{8, [1, 0]%%}+%%{6, [0, 2]%%}+%%{8, [0, 1]%%}+%%{24, [0, 0]%%}, 0, %%{-4, [3, 3]%%}+%%{4, [3, 2]%%}+%%{4, [3, 1]%%}+%%{-4, [3, 0]%%}+%%{4, [2, 3]%%}+%%{-64, [2, 2]%%}+%%{20, [2, 1]%%}+%%{8, [2, 0]%%}+%%{4, [1, 3]%%}+%%{20, [1, 2]%%}+%%{-128, [1, 1]%%}+%%{16, [1, 0]%%}+%%{-4, [0, 3]%%}+%%{8, [0, 2]%%}+%%{16, [0, 1]%%}+%%{-32, [0, 0]%%}, 0, %%{1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{1, [4, 0]%%}+%%{-4, [3, 4]%%}+%%{12, [3, 3]%%}+%%{-20, [3, 2]%%}+%%{20, [3, 1]%%}+%%{-8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{-4, [1, 4]%%}+%%{20, [1, 3]%%}+%%{-40, [1, 2]%%}+%%{48, [1, 1]%%}+%%{-32, [1, 0]%%}+%%{1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{16, [0, 0]%%}] at parameters values [6.82230772497, 55.0343274642]Warning, choosing root of [1, 0, %%{-4, [1, 1]%%}+%%{-4, [1, 0]%%}+%%{-4, [0, 1]%%}+%%{-8, [0, 0]%%}, 0, %%{6, [2, 2]%%}+%%{4, [2, 1]%%}+%%{6, [2, 0]%%}+%%{4, [1, 2]%%}+%%{28, [1, 1]%%}+%%{8, [1, 0]%%}+%%{6, [0, 2]%%}+%%{8, [0, 1]%%}+%%{24, [0, 0]%%}, 0, %%{-4, [3, 3]%%}+%%{4, [3, 2]%%}+%%{4, [3, 1]%%}+%%{-4, [3, 0]%%}+%%{4, [2, 3]%%}+%%{-64, [2, 2]%%}+%%{20, [2, 1]%%}+%%{8, [2, 0]%%}+%%{4, [1, 3]%%}+%%{20, [1, 2]%%}+%%{-128, [1, 1]%%}+%%{16, [1, 0]%%}+%%{-4, [0, 3]%%}+%%{8, [0, 2]%%}+%%{16, [0, 1]%%}+%%{-32, [0, 0]%%}, 0, %%{1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{1, [4, 0]%%}+%%{-4, [3, 4]%%}+%%{12, [3, 3]%%}+%%{-20, [3, 2]%%}+%%{20, [3, 1]%%}+%%{-8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{-4, [1, 4]%%}+%%{20, [1, 3]%%}+%%{-40, [1, 2]%%}+%%{48, [1, 1]%%}+%%{-32, [1, 0]%%}+%%{1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{16, [0, 0]%%}] at parameters values [53.4880634798, 16.0204098616]Warning, choosing root of [1, 0, %%{-4, [1, 1]%%}+%%{-4, [1, 0]%%}+%%{-4, [0, 1]%%}+%%{-8, [0, 0]%%}, 0, %%{6, [2, 2]%%}+%%{4, [2, 1]%%}+%%{6, [2, 0]%%}+%%{4, [1, 2]%%}+%%{28, [1, 1]%%}+%%{8, [1, 0]%%}+%%{6, [0, 2]%%}+%%{8, [0, 1]%%}+%%{24, [0, 0]%%}, 0, %%{-4, [3, 3]%%}+%%{4, [3, 2]%%}+%%{4, [3, 1]%%}+%%{-4, [3, 0]%%}+%%{4, [2, 3]%%}+%%{-64, [2, 2]%%}+%%{20, [2, 1]%%}+%%{8, [2, 0]%%}+%%{4, [1, 3]%%}+%%{20, [1, 2]%%}+%%{-128, [1, 1]%%}+%%{16, [1, 0]%%}+%%{-4, [0, 3]%%}+%%{8, [0, 2]%%}+%%{16, [0, 1]%%}+%%{-32, [0, 0]%%}, 0, %%{1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{1, [4, 0]%%}+%%{-4, [3, 4]%%}+%%{12, [3, 3]%%}+%%{-20, [3, 2]%%}+%%{20, [3, 1]%%}+%%{-8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{-4, [1, 4]%%}+%%{20, [1, 3]%%}+%%{-40, [1, 2]%%}+%%{48, [1, 1]%%}+%%{-32, [1, 0]%%}+%%{1, [0, 4]%%}+%%{-8, [0, 3]%%}

$\sqrt{bx+2} - 33722325b^{29}/2721600/b^{34} \sqrt{bx+2} \sqrt{b(bx+2)-2b} - 231/16/b^4/\sqrt{b} \ln(\text{abs}(\sqrt{b(bx+2)-2b} - \sqrt{b} \sqrt{bx+2}))) + 12b^2 \text{abs}(b)/b^2 * (2 * (((5040b^{19}/100800/b^{23} \sqrt{bx+2} \sqrt{bx+2} - 51660b^{19}/100800/b^{23}) \sqrt{bx+2} \sqrt{bx+2} + 215460b^{19}/100800/b^{23}) \sqrt{bx+2} \sqrt{bx+2} - 469350b^{19}/100800/b^{23}) \sqrt{bx+2} \sqrt{bx+2} + 607950b^{19}/100800/b^{23}) \sqrt{bx+2} \sqrt{b(bx+2)-2b} + 63/8/b^3/\sqrt{b} \ln(\text{abs}(\sqrt{b(bx+2)-2b} - \sqrt{b} \sqrt{bx+2}))) + 24b \text{abs}(b)/b^2 * (2 * (((90b^{11}/1440/b^{14} \sqrt{bx+2} \sqrt{bx+2} - 750b^{11}/1440/b^{14}) \sqrt{bx+2} \sqrt{bx+2} + 2445b^{11}/1440/b^{14}) \sqrt{bx+2} \sqrt{bx+2} - 4185b^{11}/1440/b^{14}) \sqrt{bx+2} \sqrt{bx+2} \sqrt{b(bx+2)-2b} - 35/8/b^2/\sqrt{b} \ln(\text{abs}(\sqrt{b(bx+2)-2b} - \sqrt{b} \sqrt{bx+2})))) + 16 \text{abs}(b)/b^2 * (2 * ((12b^5/144/b^7 \sqrt{bx+2} \sqrt{bx+2} - 78b^5/144/b^7) \sqrt{bx+2} \sqrt{bx+2} + 198b^5/144/b^7) \sqrt{bx+2} \sqrt{bx+2} \sqrt{b(bx+2)-2b} + 5/2/b/\sqrt{b} \ln(\text{abs}(\sqrt{b(bx+2)-2b} - \sqrt{b} \sqrt{bx+2}))))$

maple [A] time = 0.00, size = 138, normalized size = 0.96

$$\frac{(bx+2)^{\frac{7}{2}} x^{\frac{5}{2}}}{6b} - \frac{(bx+2)^{\frac{7}{2}} x^{\frac{3}{2}}}{6b^2} + \frac{(bx+2)^{\frac{7}{2}} \sqrt{x}}{8b^3} - \frac{(bx+2)^{\frac{5}{2}} \sqrt{x}}{24b^3} - \frac{5(bx+2)^{\frac{3}{2}} \sqrt{x}}{48b^3} - \frac{5\sqrt{bx+2} \sqrt{x}}{16b^3} - \frac{5\sqrt{(bx+2)x} \ln\left(\frac{bx+2}{\sqrt{bx+2}}\right)}{16\sqrt{bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{(5/2)}*(bx+2)^{(5/2)}, x)$

[Out] $1/6/b*x^{(5/2)}*(bx+2)^{(7/2)} - 1/6/b^2*x^{(3/2)}*(bx+2)^{(7/2)} + 1/8/b^3*x^{(1/2)}*(bx+2)^{(7/2)} - 1/24*(bx+2)^{(5/2)}/b^3*x^{(1/2)} - 5/48*(bx+2)^{(3/2)}/b^3*x^{(1/2)} - 5/16*(bx+2)^{(1/2)}/b^3*x^{(1/2)} - 5/16*((bx+2)*x)^{(1/2)}/(bx+2)^{(1/2)}/b^{(7/2)}/x^{(1/2)} \ln((bx+1)/b^{(1/2)} + (bx^2+2*x)^{(1/2)})$

maxima [B] time = 2.98, size = 223, normalized size = 1.55

$$\frac{15\sqrt{bx+2}b^5}{\sqrt{x}} - \frac{85(bx+2)^{\frac{3}{2}}b^4}{x^{\frac{3}{2}}} + \frac{198(bx+2)^{\frac{5}{2}}b^3}{x^{\frac{5}{2}}} + \frac{198(bx+2)^{\frac{7}{2}}b^2}{x^{\frac{7}{2}}} - \frac{85(bx+2)^{\frac{9}{2}}b}{x^{\frac{9}{2}}} + \frac{15(bx+2)^{\frac{11}{2}}}{x^{\frac{11}{2}}} + 5 \log\left(\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right) + \frac{24\left(b^9 - \frac{6(bx+2)b^8}{x} + \frac{15(bx+2)^2b^7}{x^2} - \frac{20(bx+2)^3b^6}{x^3} + \frac{15(bx+2)^4b^5}{x^4} - \frac{6(bx+2)^5b^4}{x^5} + \frac{(bx+2)^6b^3}{x^6}\right)}{16b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{(5/2)}*(bx+2)^{(5/2)}, x, \text{algorithm}="maxima")$

[Out] $1/24*(15*\sqrt{bx+2}*b^5/\sqrt{x} - 85*(bx+2)^{(3/2)}*b^4/x^{(3/2)} + 198*(bx+2)^{(5/2)}*b^3/x^{(5/2)} + 198*(bx+2)^{(7/2)}*b^2/x^{(7/2)} - 85*(bx+2)^{(9/2)}*b/x^{(9/2)} + 15*(bx+2)^{(11/2)}/x^{(11/2)})/(b^9 - 6*(bx+2)*b^8/x + 15*(bx+2)^2*b^7/x^2 - 20*(bx+2)^3*b^6/x^3 + 15*(bx+2)^4*b^5/x^4 - 6*(bx+2)^5*b^4/x^5 + (bx+2)^6*b^3/x^6) + 5/16*\log(-(\sqrt{b} - \sqrt{bx+2}/\sqrt{x})/(\sqrt{b} + \sqrt{bx+2}/\sqrt{x}))/b^{(7/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} (bx + 2)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(b*x + 2)^(5/2), x)

[Out] int(x^(5/2)*(b*x + 2)^(5/2), x)

sympy [A] time = 22.96, size = 158, normalized size = 1.10

$$\frac{b^3 x^{\frac{13}{2}}}{6\sqrt{bx+2}} + \frac{7b^2 x^{\frac{11}{2}}}{6\sqrt{bx+2}} + \frac{67bx^{\frac{9}{2}}}{24\sqrt{bx+2}} + \frac{55x^{\frac{7}{2}}}{24\sqrt{bx+2}} - \frac{x^{\frac{5}{2}}}{48b\sqrt{bx+2}} + \frac{5x^{\frac{3}{2}}}{48b^2\sqrt{bx+2}} + \frac{5\sqrt{x}}{8b^3\sqrt{bx+2}} - \frac{5 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{8b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)*(b*x+2)**(5/2), x)

[Out] b**3*x**(13/2)/(6*sqrt(b*x + 2)) + 7*b**2*x**(11/2)/(6*sqrt(b*x + 2)) + 67*b*x**(9/2)/(24*sqrt(b*x + 2)) + 55*x**(7/2)/(24*sqrt(b*x + 2)) - x**(5/2)/(48*b*sqrt(b*x + 2)) + 5*x**(3/2)/(48*b**2*sqrt(b*x + 2)) + 5*sqrt(x)/(8*b**3*sqrt(b*x + 2)) - 5*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(8*b**(7/2))

3.558 $\int x^{3/2}(2 + bx)^{5/2} dx$

Optimal. Leaf size=123

$$\frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} - \frac{3\sqrt{x}\sqrt{bx+2}}{8b^2} + \frac{1}{5}x^{5/2}(bx+2)^{5/2} + \frac{1}{4}x^{5/2}(bx+2)^{3/2} + \frac{1}{4}x^{5/2}\sqrt{bx+2} + \frac{x^{3/2}\sqrt{bx+2}}{8b}$$

[Out] $1/4*x^{(5/2)}*(b*x+2)^{(3/2)}+1/5*x^{(5/2)}*(b*x+2)^{(5/2)}+3/4*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(5/2)}+1/8*x^{(3/2)}*(b*x+2)^{(1/2)}/b+1/4*x^{(5/2)}*(b*x+2)^{(1/2)}-3/8*x^{(1/2)}*(b*x+2)^{(1/2)}/b^2$

Rubi [A] time = 0.03, antiderivative size = 123, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{3\sqrt{x}\sqrt{bx+2}}{8b^2} + \frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} + \frac{1}{5}x^{5/2}(bx+2)^{5/2} + \frac{1}{4}x^{5/2}(bx+2)^{3/2} + \frac{1}{4}x^{5/2}\sqrt{bx+2} + \frac{x^{3/2}\sqrt{bx+2}}{8b}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(3/2)}*(2 + b*x)^{(5/2)}, x]$

[Out] $(-3*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/(8*b^2) + (x^{(3/2)}*\operatorname{Sqrt}[2 + b*x])/(8*b) + (x^{(5/2)}*\operatorname{Sqrt}[2 + b*x])/4 + (x^{(5/2)}*(2 + b*x)^{(3/2)})/4 + (x^{(5/2)}*(2 + b*x)^{(5/2)})/5 + (3*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]])/(4*b^{(5/2)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{NeQ}[m + n + 1, 0] \&\& !(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] || (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m - n, 0]))) \&\& !\operatorname{ILtQ}[m + n + 2, 0] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 54

$\operatorname{Int}[1/(\operatorname{Sqrt}[(a_.) + (b_.)*(x_.)]*\operatorname{Sqrt}[(c_.) + (d_.)*(x_.)]), x_Symbol] \rightarrow \operatorname{Dist}[2/\operatorname{Sqrt}[b], \operatorname{Subst}[\operatorname{Int}[1/\operatorname{Sqrt}[b*c - a*d + d*x^2], x], x, \operatorname{Sqrt}[a + b*x]], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{GtQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[b, 0]$

Rule 215

$\operatorname{Int}[1/\operatorname{Sqrt}[(a_.) + (b_.)*(x_.)^2], x_Symbol] \rightarrow \operatorname{Simp}[\operatorname{ArcSinh}[\operatorname{Rt}[b, 2]*x]/\operatorname{Sqrt}[a]/\operatorname{Rt}[b, 2], x] /;$ $\operatorname{FreeQ}\{a, b\}, x \&\& \operatorname{GtQ}[a, 0] \&\& \operatorname{PosQ}[b]$

Rubi steps

$$\begin{aligned}
\int x^{3/2}(2+bx)^{5/2} dx &= \frac{1}{5}x^{5/2}(2+bx)^{5/2} + \int x^{3/2}(2+bx)^{3/2} dx \\
&= \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{1}{5}x^{5/2}(2+bx)^{5/2} + \frac{3}{4} \int x^{3/2}\sqrt{2+bx} dx \\
&= \frac{1}{4}x^{5/2}\sqrt{2+bx} + \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{1}{5}x^{5/2}(2+bx)^{5/2} + \frac{1}{4} \int \frac{x^{3/2}}{\sqrt{2+bx}} dx \\
&= \frac{x^{3/2}\sqrt{2+bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2+bx} + \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{1}{5}x^{5/2}(2+bx)^{5/2} - \frac{3 \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx}{8b} \\
&= -\frac{3\sqrt{x}\sqrt{2+bx}}{8b^2} + \frac{x^{3/2}\sqrt{2+bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2+bx} + \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{1}{5}x^{5/2}(2+bx)^{5/2} + \\
&= -\frac{3\sqrt{x}\sqrt{2+bx}}{8b^2} + \frac{x^{3/2}\sqrt{2+bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2+bx} + \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{1}{5}x^{5/2}(2+bx)^{5/2} + \\
&= -\frac{3\sqrt{x}\sqrt{2+bx}}{8b^2} + \frac{x^{3/2}\sqrt{2+bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2+bx} + \frac{1}{4}x^{5/2}(2+bx)^{3/2} + \frac{1}{5}x^{5/2}(2+bx)^{5/2} +
\end{aligned}$$

Mathematica [A] time = 0.05, size = 78, normalized size = 0.63

$$\frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} + \frac{\sqrt{x}\sqrt{bx+2}(8b^4x^4 + 42b^3x^3 + 62b^2x^2 + 5bx - 15)}{40b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*(2 + b*x)^(5/2),x]

[Out] (Sqrt[x]*Sqrt[2 + b*x]*(-15 + 5*b*x + 62*b^2*x^2 + 42*b^3*x^3 + 8*b^4*x^4)) / (40*b^2) + (3*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]]) / (4*b^(5/2))

fricas [A] time = 0.45, size = 155, normalized size = 1.26

$$\left[\frac{(8b^5x^4 + 42b^4x^3 + 62b^3x^2 + 5b^2x - 15b)\sqrt{bx+2}\sqrt{x} + 15\sqrt{b}\log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{40b^3}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+2)^(5/2),x, algorithm="fricas")

```
[Out] [1/40*((8*b^5*x^4 + 42*b^4*x^3 + 62*b^3*x^2 + 5*b^2*x - 15*b)*sqrt(b*x + 2)
*sqrt(x) + 15*sqrt(b)*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^3, 1/
40*((8*b^5*x^4 + 42*b^4*x^3 + 62*b^3*x^2 + 5*b^2*x - 15*b)*sqrt(b*x + 2)*sq
rt(x) - 30*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x)))/b^3]
```

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(3/2)*(b*x+2)^(5/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warni
ng, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}
+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,
[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+
%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,
[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}
+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-
4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,
4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%
{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[
3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}
+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%
{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,
2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [83.4865739
918,53.112478131]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,
0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+
%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]
%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+
%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,
1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}
+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32
,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}
+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%
{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,
2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}
+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-
8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at paramet
ers values [38.6973876911,89.629912049]Warning, choosing root of [1,0,%%{-
4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]
%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,
[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]
%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-
64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}
```

$\{ -128, [1, 1] \} + \{ 16, [1, 0] \} + \{ -4, [0, 3] \} + \{ 8, [0, 2] \} + \{ 16, [0, 1] \} + \{ -32, [0, 0] \}, 0, \{ 1, [4, 4] \} + \{ -4, [4, 3] \} + \{ 6, [4, 2] \} + \{ -4, [4, 1] \} + \{ 1, [4, 0] \} + \{ -4, [3, 4] \} + \{ 12, [3, 3] \} + \{ -20, [3, 2] \} + \{ 20, [3, 1] \} + \{ -8, [3, 0] \} + \{ 6, [2, 4] \} + \{ -20, [2, 3] \} + \{ 46, [2, 2] \} + \{ -40, [2, 1] \} + \{ 24, [2, 0] \} + \{ -4, [1, 4] \} + \{ 20, [1, 3] \} + \{ -40, [1, 2] \} + \{ 48, [1, 1] \} + \{ -32, [1, 0] \} + \{ 1, [0, 4] \} + \{ -8, [0, 3] \} + \{ 24, [0, 2] \} + \{ -32, [0, 1] \} + \{ 16, [0, 0] \}$ at parameters values [6.82230772497, 55.0343274642] Warning, choosing root of $\{ -4, [1, 1] \} + \{ -4, [1, 0] \} + \{ -4, [0, 1] \} + \{ -8, [0, 0] \}, 0, \{ 6, [2, 2] \} + \{ 4, [2, 1] \} + \{ 6, [2, 0] \} + \{ 4, [1, 2] \} + \{ 28, [1, 1] \} + \{ 8, [1, 0] \} + \{ 6, [0, 2] \} + \{ 8, [0, 1] \} + \{ 24, [0, 0] \}, 0, \{ -4, [3, 3] \} + \{ 4, [3, 2] \} + \{ 4, [3, 1] \} + \{ -4, [3, 0] \} + \{ 4, [2, 3] \} + \{ -64, [2, 2] \} + \{ 20, [2, 1] \} + \{ 8, [2, 0] \} + \{ 4, [1, 3] \} + \{ 20, [1, 2] \} + \{ -128, [1, 1] \} + \{ 16, [1, 0] \} + \{ -4, [0, 3] \} + \{ 8, [0, 2] \} + \{ 16, [0, 1] \} + \{ -32, [0, 0] \}, 0, \{ 1, [4, 4] \} + \{ -4, [4, 3] \} + \{ 6, [4, 2] \} + \{ -4, [4, 1] \} + \{ 1, [4, 0] \} + \{ -4, [3, 4] \} + \{ 12, [3, 3] \} + \{ -20, [3, 2] \} + \{ 20, [3, 1] \} + \{ -8, [3, 0] \} + \{ 6, [2, 4] \} + \{ -20, [2, 3] \} + \{ 46, [2, 2] \} + \{ -40, [2, 1] \} + \{ 24, [2, 0] \} + \{ -4, [1, 4] \} + \{ 20, [1, 3] \} + \{ -40, [1, 2] \} + \{ 48, [1, 1] \} + \{ -32, [1, 0] \} + \{ 1, [0, 4] \} + \{ -8, [0, 3] \} + \{ 24, [0, 2] \} + \{ -32, [0, 1] \} + \{ 16, [0, 0] \}$ at parameters values [53.4880634798, 16.0204098616] Warning, choosing root of $\{ -4, [1, 1] \} + \{ -4, [1, 0] \} + \{ -4, [0, 1] \} + \{ -8, [0, 0] \}, 0, \{ 6, [2, 2] \} + \{ 4, [2, 1] \} + \{ 6, [2, 0] \} + \{ 4, [1, 2] \} + \{ 28, [1, 1] \} + \{ 8, [1, 0] \} + \{ 6, [0, 2] \} + \{ 8, [0, 1] \} + \{ 24, [0, 0] \}, 0, \{ -4, [3, 3] \} + \{ 4, [3, 2] \} + \{ 4, [3, 1] \} + \{ -4, [3, 0] \} + \{ 4, [2, 3] \} + \{ -64, [2, 2] \} + \{ 20, [2, 1] \} + \{ 8, [2, 0] \} + \{ 4, [1, 3] \} + \{ 20, [1, 2] \} + \{ -128, [1, 1] \} + \{ 16, [1, 0] \} + \{ -4, [0, 3] \} + \{ 8, [0, 2] \} + \{ 16, [0, 1] \} + \{ -32, [0, 0] \}, 0, \{ 1, [4, 4] \} + \{ -4, [4, 3] \} + \{ 6, [4, 2] \} + \{ -4, [4, 1] \} + \{ 1, [4, 0] \} + \{ -4, [3, 4] \} + \{ 12, [3, 3] \} + \{ -20, [3, 2] \} + \{ 20, [3, 1] \} + \{ -8, [3, 0] \} + \{ 6, [2, 4] \} + \{ -20, [2, 3] \} + \{ 46, [2, 2] \} + \{ -40, [2, 1] \} + \{ 24, [2, 0] \} + \{ -4, [1, 4] \} + \{ 20, [1, 3] \} + \{ -40, [1, 2] \} + \{ 48, [1, 1] \} + \{ -32, [1, 0] \} + \{ 1, [0, 4] \} + \{ -8, [0, 3] \} + \{ 24, [0, 2] \} + \{ -32, [0, 1] \} + \{ 16, [0, 0] \}$ at parameters values [46.2456374937, 66.0382199469] Warning, choosing root of $\{ -4, [1, 1] \} + \{ -4, [1, 0] \} + \{ -4, [0, 1] \} + \{ -8, [0, 0] \}, 0, \{ 6, [2, 2] \} + \{ 4, [2, 1] \} + \{ 6, [2, 0] \} + \{ 4, [1, 2] \} + \{ 28, [1, 1] \} + \{ 8, [1, 0] \} + \{ 6, [0, 2] \} + \{ 8, [0, 1] \} + \{ 24, [0, 0] \}, 0, \{ -4, [3, 3] \} + \{ 4, [3, 2] \} + \{ 4, [3, 1] \} + \{ -4, [3, 0] \} + \{ 4, [2, 3] \} + \{ -64, [2, 2] \} + \{ 20, [2, 1] \} + \{ 8, [2, 0] \} + \{ 4, [1, 3] \} + \{ 20, [1, 2] \} + \{ -128, [1, 1] \} + \{ 16, [1, 0] \} + \{ -4, [0, 3] \} + \{ 8, [0, 2] \} + \{ 16, [0, 1] \} + \{ -32, [0, 0] \}, 0, \{ 1, [4, 4] \} + \{ -4, [4, 3] \} + \{ 6, [4, 2] \} + \{ -4, [4, 1] \} + \{ 1, [4, 0] \} + \{ -4, [3, 4] \} + \{ 12, [3, 3] \} + \{ -20, [3, 2] \} + \{ 20, [3, 1] \} + \{ -8, [3, 0] \} + \{ 6, [2, 4] \} + \{ -20, [2, 3] \} + \{ 46, [2, 2] \} + \{ -40, [2, 1] \} + \{ 24, [2, 0] \} + \{ -4, [1, 4] \} +$

$\{20, [1, 3]\} + \{-40, [1, 2]\} + \{48, [1, 1]\} + \{-32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$
] at parameters values [94.9264369817, 51.8441526662] Warning, choosing root of $\{1, 0\} + \{-4, [1, 1]\} + \{-4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}$, $\{0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{4, [1, 2]\} + \{28, [1, 1]\} + \{8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}$, $\{0, \{-4, [3, 3]\} + \{4, [3, 2]\} + \{4, [3, 1]\} + \{-4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{4, [1, 3]\} + \{20, [1, 2]\} + \{-128, [1, 1]\} + \{16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}$, $\{0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{-4, [3, 4]\} + \{12, [3, 3]\} + \{-20, [3, 2]\} + \{20, [3, 1]\} + \{-8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{-4, [1, 4]\} + \{20, [1, 3]\} + \{-40, [1, 2]\} + \{48, [1, 1]\} + \{-32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$
] at parameters values [98.7121795234, 4.66774101928] Warning, choosing root of $\{1, 0\} + \{-4, [1, 1]\} + \{-4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}$, $\{0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{4, [1, 2]\} + \{28, [1, 1]\} + \{8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}$, $\{0, \{-4, [3, 3]\} + \{4, [3, 2]\} + \{4, [3, 1]\} + \{-4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{4, [1, 3]\} + \{20, [1, 2]\} + \{-128, [1, 1]\} + \{16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}$, $\{0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{-4, [3, 4]\} + \{12, [3, 3]\} + \{-20, [3, 2]\} + \{20, [3, 1]\} + \{-8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{-4, [1, 4]\} + \{20, [1, 3]\} + \{-40, [1, 2]\} + \{48, [1, 1]\} + \{-32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$
] at parameters values [90.2102860468, 38.2197840363] $1/b * (2*b^3*abs(b)/b^2 * (2 * (((5040*b^19/100800/b^23 * sqrt(b*x+2) * sqrt(b*x+2) - 51660*b^19/100800/b^23) * sqrt(b*x+2) * sqrt(b*x+2) + 215460*b^19/100800/b^23) * sqrt(b*x+2) * sqrt(b*x+2) - 469350*b^19/100800/b^23) * sqrt(b*x+2) * sqrt(b*x+2) + 607950*b^19/100800/b^23) * sqrt(b*x+2) * sqrt(b*(b*x+2) - 2*b) + 63/8/b^3/sqrt(b) * ln(abs(sqrt(b*(b*x+2) - 2*b) - sqrt(b) * sqrt(b*x+2)))) + 12 * b^2 * abs(b) / b^2 * (2 * (((90*b^11/1440/b^14 * sqrt(b*x+2) * sqrt(b*x+2) - 750*b^11/1440/b^14) * sqrt(b*x+2) * sqrt(b*x+2) + 2445*b^11/1440/b^14) * sqrt(b*x+2) * sqrt(b*x+2) - 4185*b^11/1440/b^14) * sqrt(b*x+2) * sqrt(b*(b*x+2) - 2*b) - 35/8/b^2/sqrt(b) * ln(abs(sqrt(b*(b*x+2) - 2*b) - sqrt(b) * sqrt(b*x+2)))) + 24 * b * abs(b) / b^2 * (2 * ((12*b^5/144/b^7 * sqrt(b*x+2) * sqrt(b*x+2) - 78*b^5/144/b^7) * sqrt(b*x+2) * sqrt(b*x+2) + 198 * b^5/144/b^7) * sqrt(b*x+2) * sqrt(b*(b*x+2) - 2*b) + 5/2/b/sqrt(b) * ln(abs(sqrt(b*(b*x+2) - 2*b) - sqrt(b) * sqrt(b*x+2)))) + 16 * abs(b) / b^2 / b * (2 * (1/8 * sqrt(b*x+2) * sqrt(b*x+2) - 5/8) * sqrt(b*x+2) * sqrt(b*(b*x+2) - 2*b) - 6*b/4/sqrt(b) * ln(abs(sqrt(b*(b*x+2) - 2*b) - sqrt(b) * sqrt(b*x+2))))))$

maple [A] time = 0.00, size = 123, normalized size = 1.00

$$\frac{(bx+2)^{\frac{7}{2}}x^{\frac{3}{2}}}{5b} - \frac{3(bx+2)^{\frac{7}{2}}\sqrt{x}}{20b^2} + \frac{(bx+2)^{\frac{5}{2}}\sqrt{x}}{20b^2} + \frac{(bx+2)^{\frac{3}{2}}\sqrt{x}}{8b^2} + \frac{3\sqrt{bx+2}\sqrt{x}}{8b^2} + \frac{3\sqrt{(bx+2)x} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2}\right)}{8\sqrt{bx+2}b^{\frac{5}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)*(b*x+2)^(5/2), x)`

[Out] $\frac{1}{5}b^{\frac{3}{2}}x^{\frac{3}{2}}(bx+2)^{\frac{7}{2}} - \frac{3}{20}b^{\frac{1}{2}}x^{\frac{1}{2}}(bx+2)^{\frac{7}{2}} + \frac{1}{20}b^{\frac{3}{2}}(bx+2)^{\frac{5}{2}}x^{\frac{1}{2}} + \frac{1}{8}b^{\frac{1}{2}}(bx+2)^{\frac{3}{2}}x^{\frac{1}{2}} + \frac{3}{8}b^{\frac{3}{2}}(bx+2)^{\frac{1}{2}}x^{\frac{1}{2}} + \frac{3}{8}b^{\frac{1}{2}}(bx+2)^{\frac{1}{2}}x^{\frac{1}{2}} \ln\left(\frac{bx+1}{b^{\frac{1}{2}}} + \sqrt{bx^2+2}\right)$

maxima [B] time = 2.94, size = 194, normalized size = 1.58

$$\frac{\frac{15\sqrt{bx+2}b^4}{\sqrt{x}} - \frac{70(bx+2)^{\frac{3}{2}}b^3}{x^{\frac{3}{2}}} + \frac{128(bx+2)^{\frac{5}{2}}b^2}{x^{\frac{5}{2}}} + \frac{70(bx+2)^{\frac{7}{2}}b}{x^{\frac{7}{2}}} - \frac{15(bx+2)^{\frac{9}{2}}}{x^{\frac{9}{2}}}}{20\left(b^7 - \frac{5(bx+2)b^6}{x} + \frac{10(bx+2)^2b^5}{x^2} - \frac{10(bx+2)^3b^4}{x^3} + \frac{5(bx+2)^4b^3}{x^4} - \frac{(bx+2)^5b^2}{x^5}\right)} - \frac{3 \log\left(\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{8b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)*(b*x+2)^(5/2), x, algorithm="maxima")`

[Out] $-1/20*(15*\sqrt{bx+2}*b^4/\sqrt{x} - 70*(bx+2)^{(3/2)}*b^3/x^{(3/2)} + 128*(bx+2)^{(5/2)}*b^2/x^{(5/2)} + 70*(bx+2)^{(7/2)}*b/x^{(7/2)} - 15*(bx+2)^{(9/2)}/x^{(9/2)})/(b^7 - 5*(bx+2)*b^6/x + 10*(bx+2)^2*b^5/x^2 - 10*(bx+2)^3*b^4/x^3 + 5*(bx+2)^4*b^3/x^4 - (bx+2)^5*b^2/x^5) - 3/8*\log(-(\sqrt{b} - \sqrt{bx+2}/\sqrt{x})/(\sqrt{b} + \sqrt{bx+2}/\sqrt{x}))/b^{(5/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} (bx+2)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)*(b*x+2)^(5/2), x)`

[Out] `int(x^(3/2)*(b*x+2)^(5/2), x)`

sympy [A] time = 14.42, size = 138, normalized size = 1.12

$$\frac{b^3x^{\frac{11}{2}}}{5\sqrt{bx+2}} + \frac{29b^2x^{\frac{9}{2}}}{20\sqrt{bx+2}} + \frac{73bx^{\frac{7}{2}}}{20\sqrt{bx+2}} + \frac{129x^{\frac{5}{2}}}{40\sqrt{bx+2}} - \frac{x^{\frac{3}{2}}}{8b\sqrt{bx+2}} - \frac{3\sqrt{x}}{4b^2\sqrt{bx+2}} + \frac{3 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(3/2)*(b*x+2)**(5/2),x)
```

```
[Out] b**3*x**(11/2)/(5*sqrt(b*x + 2)) + 29*b**2*x**(9/2)/(20*sqrt(b*x + 2)) + 73  
*b*x**(7/2)/(20*sqrt(b*x + 2)) + 129*x**(5/2)/(40*sqrt(b*x + 2)) - x**(3/2)  
/(8*b*sqrt(b*x + 2)) - 3*sqrt(x)/(4*b**2*sqrt(b*x + 2)) + 3*asinh(sqrt(2)*s  
qrt(b)*sqrt(x)/2)/(4*b**(5/2))
```

3.559 $\int \sqrt{x} (2 + bx)^{5/2} dx$

Optimal. Leaf size=102

$$-\frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{3/2}} + \frac{1}{4}x^{3/2}(bx+2)^{5/2} + \frac{5}{12}x^{3/2}(bx+2)^{3/2} + \frac{5}{8}x^{3/2}\sqrt{bx+2} + \frac{5\sqrt{x}\sqrt{bx+2}}{8b}$$

[Out] $5/12*x^{(3/2)}*(b*x+2)^{(3/2)}+1/4*x^{(3/2)}*(b*x+2)^{(5/2)}-5/4*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(3/2)}+5/8*x^{(3/2)}*(b*x+2)^{(1/2)}+5/8*x^{(1/2)}*(b*x+2)^{(1/2)}/b$

Rubi [A] time = 0.02, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{3/2}} + \frac{1}{4}x^{3/2}(bx+2)^{5/2} + \frac{5}{12}x^{3/2}(bx+2)^{3/2} + \frac{5}{8}x^{3/2}\sqrt{bx+2} + \frac{5\sqrt{x}\sqrt{bx+2}}{8b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]*(2 + b*x)^(5/2), x]

[Out] $(5*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/(8*b) + (5*x^{(3/2)}*\operatorname{Sqrt}[2 + b*x])/8 + (5*x^{(3/2)}*(2 + b*x)^{(3/2)})/12 + (x^{(3/2)}*(2 + b*x)^{(5/2)})/4 - (5*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]])/(4*b^{(3/2)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 215

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned}
\int \sqrt{x}(2+bx)^{5/2} dx &= \frac{1}{4}x^{3/2}(2+bx)^{5/2} + \frac{5}{4} \int \sqrt{x}(2+bx)^{3/2} dx \\
&= \frac{5}{12}x^{3/2}(2+bx)^{3/2} + \frac{1}{4}x^{3/2}(2+bx)^{5/2} + \frac{5}{4} \int \sqrt{x}\sqrt{2+bx} dx \\
&= \frac{5}{8}x^{3/2}\sqrt{2+bx} + \frac{5}{12}x^{3/2}(2+bx)^{3/2} + \frac{1}{4}x^{3/2}(2+bx)^{5/2} + \frac{5}{8} \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx \\
&= \frac{5\sqrt{x}\sqrt{2+bx}}{8b} + \frac{5}{8}x^{3/2}\sqrt{2+bx} + \frac{5}{12}x^{3/2}(2+bx)^{3/2} + \frac{1}{4}x^{3/2}(2+bx)^{5/2} - \frac{5 \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx}{8b} \\
&= \frac{5\sqrt{x}\sqrt{2+bx}}{8b} + \frac{5}{8}x^{3/2}\sqrt{2+bx} + \frac{5}{12}x^{3/2}(2+bx)^{3/2} + \frac{1}{4}x^{3/2}(2+bx)^{5/2} - \frac{5 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}}\right)}{4b} \\
&= \frac{5\sqrt{x}\sqrt{2+bx}}{8b} + \frac{5}{8}x^{3/2}\sqrt{2+bx} + \frac{5}{12}x^{3/2}(2+bx)^{3/2} + \frac{1}{4}x^{3/2}(2+bx)^{5/2} - \frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 70, normalized size = 0.69

$$\frac{\sqrt{x}\sqrt{bx+2}(6b^3x^3+34b^2x^2+59bx+15)}{24b} - \frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*(2 + b*x)^(5/2), x]

[Out] (Sqrt[x]*Sqrt[2 + b*x]*(15 + 59*b*x + 34*b^2*x^2 + 6*b^3*x^3))/(24*b) - (5*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(4*b^(3/2))

fricas [A] time = 0.44, size = 140, normalized size = 1.37

$$\left[\frac{(6b^4x^3 + 34b^3x^2 + 59b^2x + 15b)\sqrt{bx+2}\sqrt{x} + 15\sqrt{b}\log(bx - \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{24b^2}, \frac{(6b^4x^3 + 34b^3x^2 + 59b^2x + 15b)\sqrt{bx+2}\sqrt{x} + 15\sqrt{b}\log(bx - \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{24b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(5/2)*x^(1/2), x, algorithm="fricas")

[Out] [1/24*((6*b^4*x^3 + 34*b^3*x^2 + 59*b^2*x + 15*b)*sqrt(b*x + 2)*sqrt(x) + 15*sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^2, 1/24*((6*b^4*x

$\sqrt[3]{3 + 34b^3x^2 + 59b^2x + 15b} \sqrt{bx + 2} \sqrt{x} + 30 \sqrt{-b} \arctan(\sqrt{bx + 2} \sqrt{-b} / (b \sqrt{x})) / b^2$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(5/2)*x^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{-24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [83.4865739918,53.112478131]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [38.6973876911,89.629912049]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[

$\{4, 2\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{-4, [3, 4]\} + \{12, [3, 3]\} + \{-20, [3, 2]\} + \{20, [3, 1]\} + \{-8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{-4, [1, 4]\} + \{20, [1, 3]\} + \{-40, [1, 2]\} + \{48, [1, 1]\} + \{-32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values [6.82230772497, 55.0343274642] Warning, choosing root of $\{1, 0, \{-4, [1, 1]\} + \{-4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{4, [1, 2]\} + \{28, [1, 1]\} + \{8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{-4, [3, 3]\} + \{4, [3, 2]\} + \{4, [3, 1]\} + \{-4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{4, [1, 3]\} + \{20, [1, 2]\} + \{-128, [1, 1]\} + \{16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{-4, [3, 4]\} + \{12, [3, 3]\} + \{-20, [3, 2]\} + \{20, [3, 1]\} + \{-8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{-4, [1, 4]\} + \{20, [1, 3]\} + \{-40, [1, 2]\} + \{48, [1, 1]\} + \{-32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values [53.4880634798, 16.0204098616] Warning, choosing root of $\{1, 0, \{-4, [1, 1]\} + \{-4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{4, [1, 2]\} + \{28, [1, 1]\} + \{8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{-4, [3, 3]\} + \{4, [3, 2]\} + \{4, [3, 1]\} + \{-4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{4, [1, 3]\} + \{20, [1, 2]\} + \{-128, [1, 1]\} + \{16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{-4, [3, 4]\} + \{12, [3, 3]\} + \{-20, [3, 2]\} + \{20, [3, 1]\} + \{-8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{-4, [1, 4]\} + \{20, [1, 3]\} + \{-40, [1, 2]\} + \{48, [1, 1]\} + \{-32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values [46.2456374937, 66.0382199469] Warning, choosing root of $\{1, 0, \{-4, [1, 1]\} + \{-4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{4, [1, 2]\} + \{28, [1, 1]\} + \{8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{-4, [3, 3]\} + \{4, [3, 2]\} + \{4, [3, 1]\} + \{-4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{4, [1, 3]\} + \{20, [1, 2]\} + \{-128, [1, 1]\} + \{16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{-4, [3, 4]\} + \{12, [3, 3]\} + \{-20, [3, 2]\} + \{20, [3, 1]\} + \{-8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{-4, [1, 4]\} + \{20, [1, 3]\} + \{-40, [1, 2]\} + \{48, [1, 1]\} + \{-32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$

Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{-16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [94.9264369817,51.8441526662]Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{-16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [98.7121795234,4.66774101928]Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{-16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [90.2102860468,38.2197840363] $1/b*(2*b^3*abs(b)/b^2*(2*((90*b^11/1440/b^14*\sqrt{b*x+2})*\sqrt{b*x+2}-750*b^11/1440/b^14)*\sqrt{b*x+2}*\sqrt{b*x+2}+2445*b^11/1440/b^14)*\sqrt{b*x+2}*\sqrt{b*x+2}-4185*b^11/1440/b^14)*\sqrt{b*x+2}*\sqrt{b*(b*x+2)-2*b}-35/8/b^2/\sqrt{b}*\ln(abs(\sqrt{b*(b*x+2)-2*b}-\sqrt{b}*\sqrt{b*x+2})))$ +12*b^2*abs(b)/b^2*(2*((12*b^5/144/b^7*\sqrt{b*x+2})*\sqrt{b*x+2}-78*b^5/144/b^7)*\sqrt{b*x+2}*\sqrt{b*x+2}+198*b^5/144/b^7)*\sqrt{b*x+2}*\sqrt{b*(b*x+2)-2*b}+5/2/b/\sqrt{b}*\ln(abs(\sqrt{b*(b*x+2)-2*b}-\sqrt{b}*\sqrt{b*x+2})))+24*b*abs(b)/b^2/b*(2*(1/8*\sqrt{b*x+2})*\sqrt{b*x+2}-5/8)*\sqrt{b*x+2}*\sqrt{b*(b*x+2)-2*b}-6*b/4/\sqrt{b}*\ln(abs(\sqrt{b*(b*x+2)-2*b}-\sqrt{b}*\sqrt{b*x+2})))+16*abs(b)/b^2*(1/2*\sqrt{b*x+2})*\sqrt{b*(b*x+2)-2*b}+2*b/2/\sqrt{b}*\ln(abs(\sqrt{b*(b*x+2)-2*b}-\sqrt{b}*\sqrt{b*x+2})))

maple [A] time = 0.01, size = 99, normalized size = 0.97

$$\frac{(bx+2)^{\frac{5}{2}}x^{\frac{3}{2}}}{4} + \frac{5(bx+2)^{\frac{3}{2}}x^{\frac{3}{2}}}{12} + \frac{5\sqrt{bx+2}x^{\frac{3}{2}}}{8} + \frac{5\sqrt{bx+2}\sqrt{x}}{8b} - \frac{5\sqrt{(bx+2)x}\ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{8\sqrt{bx+2}b^{\frac{3}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+2)^(5/2)*x^(1/2),x)`

[Out] $\frac{1}{4}x^{3/2}(b*x+2)^{5/2} + \frac{5}{12}(b*x+2)^{3/2}x^{3/2} + \frac{5}{8}(b*x+2)^{1/2}x^{3/2} + \frac{5}{8}(b*x+2)^{1/2}/b*x^{1/2} - \frac{5}{8}((b*x+2)*x)^{1/2}/(b*x+2)^{1/2}/b^{3/2}/x^{1/2} * \ln((b*x+1)/b^{1/2} + (b*x^2+2*x)^{1/2})$

maxima [B] time = 2.99, size = 161, normalized size = 1.58

$$\frac{\frac{15\sqrt{bx+2}b^3}{\sqrt{x}} - \frac{55(bx+2)^{\frac{3}{2}}b^2}{x^{\frac{3}{2}}} + \frac{73(bx+2)^{\frac{5}{2}}b}{x^{\frac{5}{2}}} + \frac{15(bx+2)^{\frac{7}{2}}}{x^{\frac{7}{2}}}}{12\left(b^5 - \frac{4(bx+2)b^4}{x} + \frac{6(bx+2)^2b^3}{x^2} - \frac{4(bx+2)^3b^2}{x^3} + \frac{(bx+2)^4b}{x^4}\right)} + \frac{5 \log\left(-\frac{\sqrt{b}-\sqrt{bx+2}}{\sqrt{x}}\right)}{8b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)^(5/2)*x^(1/2),x, algorithm="maxima")`

[Out] $\frac{1}{12} * (15 * \sqrt{bx+2} * b^3 / \sqrt{x} - 55 * (bx+2)^{3/2} * b^2 / x^{3/2} + 73 * (bx+2)^{5/2} * b / x^{5/2} + 15 * (bx+2)^{7/2} / x^{7/2}) / (b^5 - 4 * (bx+2) * b^4 / x + 6 * (bx+2)^2 * b^3 / x^2 - 4 * (bx+2)^3 * b^2 / x^3 + (bx+2)^4 * b / x^4) + \frac{5}{8} * \log\left(-\frac{\sqrt{b}-\sqrt{bx+2}}{\sqrt{x}}\right) / (b^{3/2})$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{x} (bx+2)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)*(b*x+2)^(5/2),x)`

[Out] `int(x^(1/2)*(b*x+2)^(5/2),x)`

sympy [A] time = 8.61, size = 119, normalized size = 1.17

$$\frac{b^3x^{\frac{9}{2}}}{4\sqrt{bx+2}} + \frac{23b^2x^{\frac{7}{2}}}{12\sqrt{bx+2}} + \frac{127bx^{\frac{5}{2}}}{24\sqrt{bx+2}} + \frac{133x^{\frac{3}{2}}}{24\sqrt{bx+2}} + \frac{5\sqrt{x}}{4b\sqrt{bx+2}} - \frac{5 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)**(5/2)*x**(1/2),x)`

[Out] $b^{3/2}x^{9/2}/(4*\sqrt{bx+2}) + 23*b^{5/2}x^{7/2}/(12*\sqrt{bx+2}) + 127*b^{3/2}x^{5/2}/(24*\sqrt{bx+2}) + 133*x^{3/2}/(24*\sqrt{bx+2}) + 5*\sqrt{x}/(4*b*\sqrt{bx+2}) - 5*\operatorname{asinh}(\sqrt{2}*\sqrt{b}*\sqrt{x}/2)/(4*b^{3/2})$

$$3.560 \quad \int \frac{(2+bx)^{5/2}}{\sqrt{x}} dx$$

Optimal. Leaf size=79

$$\frac{1}{3}\sqrt{x}(bx+2)^{5/2} + \frac{5}{6}\sqrt{x}(bx+2)^{3/2} + \frac{5}{2}\sqrt{x}\sqrt{bx+2} + \frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

[Out] $5*\operatorname{arcsinh}(1/2*b^{(1/2)*x^{(1/2)}*2^{(1/2)})/b^{(1/2)}+5/6*(b*x+2)^{(3/2)*x^{(1/2)}+1/3*(b*x+2)^{(5/2)*x^{(1/2)}+5/2*x^{(1/2)}*(b*x+2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$\frac{1}{3}\sqrt{x}(bx+2)^{5/2} + \frac{5}{6}\sqrt{x}(bx+2)^{3/2} + \frac{5}{2}\sqrt{x}\sqrt{bx+2} + \frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(2 + b*x)^{(5/2)}/\operatorname{Sqrt}[x], x]$

[Out] $(5*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/2 + (5*\operatorname{Sqrt}[x]*(2 + b*x)^{(3/2)})/6 + (\operatorname{Sqrt}[x]*(2 + b*x)^{(5/2)})/3 + (5*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/ \operatorname{Sqrt}[2]])/\operatorname{Sqrt}[b]$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{GtQ}[n, 0] \ \&\& \ \operatorname{NeQ}[m+n+1, 0] \ \&\& \ !(\operatorname{IGtQ}[m, 0] \ \&\& \ (!\operatorname{IntegerQ}[n] \ || \ (\operatorname{GtQ}[m, 0] \ \&\& \ \operatorname{LtQ}[m-n, 0]))) \ \&\& \ !\operatorname{ILtQ}[m+n+2, 0] \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 54

$\operatorname{Int}[1/(\operatorname{Sqrt}[(a_.) + (b_.)*(x_)]*\operatorname{Sqrt}[(c_.) + (d_.)*(x_)]), x_Symbol] \rightarrow \operatorname{Dist}[2/\operatorname{Sqrt}[b], \operatorname{Subst}[\operatorname{Int}[1/\operatorname{Sqrt}[b*c - a*d + d*x^2], x], x, \operatorname{Sqrt}[a + b*x]], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{GtQ}[b*c - a*d, 0] \ \&\& \ \operatorname{GtQ}[b, 0]$

Rule 215

$\operatorname{Int}[1/\operatorname{Sqrt}[(a_.) + (b_.)*(x_)^2], x_Symbol] \rightarrow \operatorname{Simp}[\operatorname{ArcSinh}[(\operatorname{Rt}[b, 2]*x)/\operatorname{Sqrt}[a]]/\operatorname{Rt}[b, 2], x] /;$ $\operatorname{FreeQ}\{a, b, x\} \ \&\& \ \operatorname{GtQ}[a, 0] \ \&\& \ \operatorname{PosQ}[b]$

Rubi steps

$$\begin{aligned}
\int \frac{(2+bx)^{5/2}}{\sqrt{x}} dx &= \frac{1}{3} \sqrt{x} (2+bx)^{5/2} + \frac{5}{3} \int \frac{(2+bx)^{3/2}}{\sqrt{x}} dx \\
&= \frac{5}{6} \sqrt{x} (2+bx)^{3/2} + \frac{1}{3} \sqrt{x} (2+bx)^{5/2} + \frac{5}{2} \int \frac{\sqrt{2+bx}}{\sqrt{x}} dx \\
&= \frac{5}{2} \sqrt{x} \sqrt{2+bx} + \frac{5}{6} \sqrt{x} (2+bx)^{3/2} + \frac{1}{3} \sqrt{x} (2+bx)^{5/2} + \frac{5}{2} \int \frac{1}{\sqrt{x} \sqrt{2+bx}} dx \\
&= \frac{5}{2} \sqrt{x} \sqrt{2+bx} + \frac{5}{6} \sqrt{x} (2+bx)^{3/2} + \frac{1}{3} \sqrt{x} (2+bx)^{5/2} + 5 \operatorname{Subst} \left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x} \right) \\
&= \frac{5}{2} \sqrt{x} \sqrt{2+bx} + \frac{5}{6} \sqrt{x} (2+bx)^{3/2} + \frac{1}{3} \sqrt{x} (2+bx)^{5/2} + \frac{5 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 57, normalized size = 0.72

$$\frac{1}{6} \sqrt{x} \sqrt{bx+2} (2b^2x^2 + 13bx + 33) + \frac{5 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Integrate[(2 + b*x)^(5/2)/Sqrt[x], x]

[Out] (Sqrt[x]*Sqrt[2 + b*x]*(33 + 13*b*x + 2*b^2*x^2))/6 + (5*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

fricas [A] time = 0.45, size = 123, normalized size = 1.56

$$\left[\frac{(2b^3x^2 + 13b^2x + 33b)\sqrt{bx+2}\sqrt{x} + 15\sqrt{b} \log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{6b}, \frac{(2b^3x^2 + 13b^2x + 33b)\sqrt{bx+2}\sqrt{x}}{6b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(5/2)/x^(1/2), x, algorithm="fricas")

[Out] [1/6*((2*b^3*x^2 + 13*b^2*x + 33*b)*sqrt(b*x + 2)*sqrt(x) + 15*sqrt(b)*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b, 1/6*((2*b^3*x^2 + 13*b^2*x + 33*b)*sqrt(b*x + 2)*sqrt(x) - 30*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))))/b]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(5/2)/x^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [85.3561567818,61.7937478349]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [71.707969239,78.6493344628]1/abs(b)*b^2/b*(2*((1/6/b*sqrt(b*x+2))*sqrt(b*x+2)+5/12/b)*sqrt(b*x+2)*sqrt(b*x+2)+5/4/b)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)-5/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))

maple [A] time = 0.00, size = 84, normalized size = 1.06

$$\frac{(bx+2)^{\frac{5}{2}}\sqrt{x}}{3} + \frac{5(bx+2)^{\frac{3}{2}}\sqrt{x}}{6} + \frac{5\sqrt{bx+2}\sqrt{x}}{2} + \frac{5\sqrt{(bx+2)x}\ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{2\sqrt{bx+2}\sqrt{b}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+2)^(5/2)/x^(1/2),x)`

[Out] $\frac{1}{3}(b*x+2)^{5/2}*x^{1/2} + \frac{5}{6}(b*x+2)^{3/2}*x^{1/2} + \frac{5}{2}(b*x+2)^{1/2}*x^{1/2} + \frac{5}{2}((b*x+2)*x)^{1/2}/(b*x+2)^{1/2}/b^{1/2}/x^{1/2} * \ln((b*x+1)/b^{1/2} + (b*x^2+2*x)^{1/2})$

maxima [B] time = 3.03, size = 129, normalized size = 1.63

$$-\frac{5 \log\left(-\frac{\sqrt{b}-\sqrt{bx+2}}{\sqrt{b}+\frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{2\sqrt{b}} - \frac{\frac{15\sqrt{bx+2}b^2}{\sqrt{x}} - \frac{40(bx+2)^3b}{x^2} + \frac{33(bx+2)^5}{x^2}}{3\left(b^3 - \frac{3(bx+2)b^2}{x} + \frac{3(bx+2)^2b}{x^2} - \frac{(bx+2)^3}{x^3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)^(5/2)/x^(1/2),x, algorithm="maxima")`

[Out] $-5/2*\log(-(\sqrt{b} - \sqrt{b*x + 2})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x + 2})/\sqrt{x} - 1/3*(15*\sqrt{b*x + 2}*b^2/\sqrt{x} - 40*(b*x + 2)^{3/2}*b/x^{3/2} + 33*(b*x + 2)^{5/2}/x^{5/2})/(b^3 - 3*(b*x + 2)*b^2/x + 3*(b*x + 2)^2*b/x^2 - (b*x + 2)^3/x^3)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(bx+2)^{5/2}}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x + 2)^(5/2)/x^(1/2),x)`

[Out] `int((b*x + 2)^(5/2)/x^(1/2), x)`

sympy [A] time = 5.46, size = 97, normalized size = 1.23

$$\frac{b^3x^7}{3\sqrt{bx+2}} + \frac{17b^2x^5}{6\sqrt{bx+2}} + \frac{59bx^3}{6\sqrt{bx+2}} + \frac{11\sqrt{x}}{\sqrt{bx+2}} + \frac{5 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)**(5/2)/x**(1/2),x)`

[Out] $b**3*x**(7/2)/(3*\sqrt{b*x + 2}) + 17*b**2*x**(5/2)/(6*\sqrt{b*x + 2}) + 59*b*x**(3/2)/(6*\sqrt{b*x + 2}) + 11*\sqrt{x}/\sqrt{b*x + 2} + 5*asinh(\sqrt{2}*sqrt(b)*sqrt(x)/2)/\sqrt{b}$

$$3.561 \quad \int \frac{(2+bx)^{5/2}}{x^{3/2}} dx$$

Optimal. Leaf size=79

$$-\frac{2(bx+2)^{5/2}}{\sqrt{x}} + \frac{5}{2}b\sqrt{x}(bx+2)^{3/2} + \frac{15}{2}b\sqrt{x}\sqrt{bx+2} + 15\sqrt{b} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)$$

[Out] 15*arcsinh(1/2*b^(1/2)*x^(1/2)*2^(1/2))*b^(1/2)-2*(b*x+2)^(5/2)/x^(1/2)+5/2*b*(b*x+2)^(3/2)*x^(1/2)+15/2*b*x^(1/2)*(b*x+2)^(1/2)

Rubi [A] time = 0.02, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 54, 215}

$$-\frac{2(bx+2)^{5/2}}{\sqrt{x}} + \frac{5}{2}b\sqrt{x}(bx+2)^{3/2} + \frac{15}{2}b\sqrt{x}\sqrt{bx+2} + 15\sqrt{b} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Int[(2 + b*x)^(5/2)/x^(3/2), x]

[Out] (15*b*Sqrt[x]*Sqrt[2 + b*x])/2 + (5*b*Sqrt[x]*(2 + b*x)^(3/2))/2 - (2*(2 + b*x)^(5/2))/Sqrt[x] + 15*Sqrt[b]*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[Rt[b, 2]*x]/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(2+bx)^{5/2}}{x^{3/2}} dx &= -\frac{2(2+bx)^{5/2}}{\sqrt{x}} + (5b) \int \frac{(2+bx)^{3/2}}{\sqrt{x}} dx \\
&= \frac{5}{2}b\sqrt{x}(2+bx)^{3/2} - \frac{2(2+bx)^{5/2}}{\sqrt{x}} + \frac{1}{2}(15b) \int \frac{\sqrt{2+bx}}{\sqrt{x}} dx \\
&= \frac{15}{2}b\sqrt{x}\sqrt{2+bx} + \frac{5}{2}b\sqrt{x}(2+bx)^{3/2} - \frac{2(2+bx)^{5/2}}{\sqrt{x}} + \frac{1}{2}(15b) \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx \\
&= \frac{15}{2}b\sqrt{x}\sqrt{2+bx} + \frac{5}{2}b\sqrt{x}(2+bx)^{3/2} - \frac{2(2+bx)^{5/2}}{\sqrt{x}} + (15b) \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right) \\
&= \frac{15}{2}b\sqrt{x}\sqrt{2+bx} + \frac{5}{2}b\sqrt{x}(2+bx)^{3/2} - \frac{2(2+bx)^{5/2}}{\sqrt{x}} + 15\sqrt{b} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 28, normalized size = 0.35

$$-\frac{8\sqrt{2} {}_2F_1\left(-\frac{5}{2}, -\frac{1}{2}; \frac{1}{2}; -\frac{bx}{2}\right)}{\sqrt{x}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(2 + b*x)^(5/2)/x^(3/2), x]
```

```
[Out] (-8*Sqrt[2]*Hypergeometric2F1[-5/2, -1/2, 1/2, -1/2*(b*x)]) / Sqrt[x]
```

fricas [A] time = 0.47, size = 116, normalized size = 1.47

$$\left[\frac{15\sqrt{b}x \log\left(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1\right) + (b^2x^2 + 9bx - 16)\sqrt{bx+2}\sqrt{x}}{2x}, -\frac{30\sqrt{-b}x \arctan\left(\frac{\sqrt{bx+2}\sqrt{-b}}{b\sqrt{x}}\right) - (b^2x^2)}{2x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+2)^(5/2)/x^(3/2),x, algorithm="fricas")
```

```
[Out] [1/2*(15*sqrt(b)*x*log(b*x + sqrt(b*x + 2))*sqrt(b)*sqrt(x) + 1) + (b^2*x^2
+ 9*b*x - 16)*sqrt(b*x + 2)*sqrt(x))/x, -1/2*(30*sqrt(-b)*x*arctan(sqrt(b*x
+ 2)*sqrt(-b)/(b*sqrt(x))) - (b^2*x^2 + 9*b*x - 16)*sqrt(b*x + 2)*sqrt(x))
/x]
```

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+2)^(5/2)/x^(3/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warni
ng, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%
}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,
[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+
%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,
[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%
}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-
4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,
4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%
{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[
3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%
}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%
{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,
2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [85.3561567
818,61.7937478349]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1
,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}
+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,
2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+
%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[
2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%
}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-3
2,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]
%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%
{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2
,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%
}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-
8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parame
ters values [71.707969239,78.6493344628]b/abs(b)*b^2/b*(2*((1/4*sqrt(b*x+2)
*sqrt(b*x+2)+5/4)*sqrt(b*x+2)*sqrt(b*x+2)-15/2)*sqrt(b*x+2)*sqrt(b*(b*x+2)-
```

$2*b)/(b*(b*x+2)-2*b)-15/\sqrt{b}*\ln(\text{abs}(\sqrt{b*(b*x+2)-2*b}-\sqrt{b})*\sqrt{b*x+2})))$

maple [A] time = 0.02, size = 81, normalized size = 1.03

$$\frac{15\sqrt{(bx+2)x} \sqrt{b} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{2\sqrt{bx+2} \sqrt{x}} + \frac{b^3x^3 + 11b^2x^2 + 2bx - 32}{2\sqrt{bx+2} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+2)^(5/2)/x^(3/2), x)`

[Out] $1/2*(b^3*x^3+11*b^2*x^2+2*b*x-32)/(b*x+2)^(1/2)/x^(1/2)+15/2*((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)*b^(1/2)/x^(1/2)*\ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))$

maxima [B] time = 2.94, size = 113, normalized size = 1.43

$$-\frac{15}{2} \sqrt{b} \log\left(-\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right) - \frac{\frac{7\sqrt{bx+2}b^2}{\sqrt{x}} - \frac{9(bx+2)^{\frac{3}{2}}b}{x^{\frac{3}{2}}}}{b^2 - \frac{2(bx+2)b}{x} + \frac{(bx+2)^2}{x^2}} - \frac{8\sqrt{bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+2)^(5/2)/x^(3/2), x, algorithm="maxima")`

[Out] $-15/2*\sqrt{b}*\log(-(\sqrt{b} - \sqrt{b*x+2}/\sqrt{x})/(\sqrt{b} + \sqrt{b*x+2}/\sqrt{x})) - (7*\sqrt{b*x+2}*b^2/\sqrt{x} - 9*(b*x+2)^(3/2)*b/x^(3/2))/(b^2 - 2*(b*x+2)*b/x + (b*x+2)^2/x^2) - 8*\sqrt{b*x+2}/\sqrt{x}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(bx+2)^{5/2}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+2)^(5/2)/x^(3/2), x)`

[Out] `int((b*x+2)^(5/2)/x^(3/2), x)`

sympy [A] time = 5.60, size = 94, normalized size = 1.19

$$15\sqrt{b} \operatorname{asinh}\left(\frac{\sqrt{2} \sqrt{b} \sqrt{x}}{2}\right) + \frac{b^3x^{\frac{5}{2}}}{2\sqrt{bx+2}} + \frac{11b^2x^{\frac{3}{2}}}{2\sqrt{bx+2}} + \frac{b\sqrt{x}}{\sqrt{bx+2}} - \frac{16}{\sqrt{x}\sqrt{bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+2)**(5/2)/x**(3/2),x)
```

```
[Out] 15*sqrt(b)*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2) + b**3*x**(5/2)/(2*sqrt(b*x + 2)) + 11*b**2*x**(3/2)/(2*sqrt(b*x + 2)) + b*sqrt(x)/sqrt(b*x + 2) - 16/(sqrt(x)*sqrt(b*x + 2))
```

$$3.562 \quad \int \frac{(2+bx)^{5/2}}{x^{5/2}} dx$$

Optimal. Leaf size=81

$$10b^{3/2} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right) + 5b^2\sqrt{x}\sqrt{bx+2} - \frac{2(bx+2)^{5/2}}{3x^{3/2}} - \frac{10b(bx+2)^{3/2}}{3\sqrt{x}}$$

[Out] $-2/3*(b*x+2)^{(5/2)}/x^{(3/2)}+10*b^{(3/2)}*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})-10/3*b*(b*x+2)^{(3/2)}/x^{(1/2)}+5*b^2*x^{(1/2)}*(b*x+2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 54, 215}

$$5b^2\sqrt{x}\sqrt{bx+2} + 10b^{3/2} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right) - \frac{2(bx+2)^{5/2}}{3x^{3/2}} - \frac{10b(bx+2)^{3/2}}{3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[(2 + b*x)^(5/2)/x^(5/2), x]

[Out] $5*b^2*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x] - (10*b*(2 + b*x)^{(3/2)})/(3*\operatorname{Sqrt}[x]) - (2*(2 + b*x)^{(5/2)})/(3*x^{(3/2)}) + 10*b^{(3/2)}*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/ \operatorname{Sqrt}[2]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(2+bx)^{5/2}}{x^{5/2}} dx &= -\frac{2(2+bx)^{5/2}}{3x^{3/2}} + \frac{1}{3}(5b) \int \frac{(2+bx)^{3/2}}{x^{3/2}} dx \\
&= -\frac{10b(2+bx)^{3/2}}{3\sqrt{x}} - \frac{2(2+bx)^{5/2}}{3x^{3/2}} + (5b^2) \int \frac{\sqrt{2+bx}}{\sqrt{x}} dx \\
&= 5b^2\sqrt{x}\sqrt{2+bx} - \frac{10b(2+bx)^{3/2}}{3\sqrt{x}} - \frac{2(2+bx)^{5/2}}{3x^{3/2}} + (5b^2) \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx \\
&= 5b^2\sqrt{x}\sqrt{2+bx} - \frac{10b(2+bx)^{3/2}}{3\sqrt{x}} - \frac{2(2+bx)^{5/2}}{3x^{3/2}} + (10b^2) \text{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right) \\
&= 5b^2\sqrt{x}\sqrt{2+bx} - \frac{10b(2+bx)^{3/2}}{3\sqrt{x}} - \frac{2(2+bx)^{5/2}}{3x^{3/2}} + 10b^{3/2} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.37

$$\frac{8\sqrt{2} {}_2F_1\left(-\frac{5}{2}, -\frac{3}{2}; -\frac{1}{2}; -\frac{bx}{2}\right)}{3x^{3/2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(2 + b*x)^(5/2)/x^(5/2), x]
```

```
[Out] (-8*Sqrt[2]*Hypergeometric2F1[-5/2, -3/2, -1/2, -1/2*(b*x)])/(3*x^(3/2))
```

fricas [A] time = 0.45, size = 123, normalized size = 1.52

$$\left[\frac{15b^{\frac{3}{2}}x^2 \log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1) + (3b^2x^2 - 28bx - 8)\sqrt{bx+2}\sqrt{x}}{3x^2}, -\frac{30\sqrt{-b}bx^2 \arctan\left(\frac{\sqrt{bx+2}\sqrt{-b}}{b\sqrt{x}}\right)}{3x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+2)^(5/2)/x^(5/2),x, algorithm="fricas")
```

```
[Out] [1/3*(15*b^(3/2)*x^2*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1) + (3*b^2*x^2 - 28*b*x - 8)*sqrt(b*x + 2)*sqrt(x))/x^2, -1/3*(30*sqrt(-b)*b*x^2*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))) - (3*b^2*x^2 - 28*b*x - 8)*sqrt(b*x + 2)*sqrt(x))/x^2]
```

```
giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00
```

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+2)^(5/2)/x^(5/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [85.3561567818,61.7937478349]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [71.707969239,78.6493344628]1/abs(b)*b^2/b*(2*((9*b^4/18/b*sqrt(b*x+2)*sqrt(b*x+2)-120*b^4/18/b)*sqrt(b*x+2)*sqrt(b*x+2)+180*b^4/18/b)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)/(b*(b*x+2)-2*b)^2-10*b^2/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))
```

maple [A] time = 0.02, size = 82, normalized size = 1.01

$$\frac{5\sqrt{(bx+2)x} b^{\frac{3}{2}} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{\sqrt{bx+2} \sqrt{x}} + \frac{3b^3x^3 - 22b^2x^2 - 64bx - 16}{3\sqrt{bx+2} x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+2)^(5/2)/x^(5/2), x)

[Out] $\frac{1}{3} * (3 * b^3 * x^3 - 22 * b^2 * x^2 - 64 * b * x - 16) / x^{3/2} / (b * x + 2)^{1/2} + 5 * ((b * x + 2) * x)^{1/2} / (b * x + 2)^{1/2} * b^{3/2} / x^{1/2} * \ln((b * x + 1) / b^{1/2} + (b * x^2 + 2 * x)^{1/2})$

maxima [A] time = 2.94, size = 96, normalized size = 1.19

$$-5b^{\frac{3}{2}} \log\left(\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right) - \frac{8\sqrt{bx+2}b}{\sqrt{x}} - \frac{2\sqrt{bx+2}b^2}{\left(b - \frac{bx+2}{x}\right)\sqrt{x}} - \frac{4(bx+2)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+2)^(5/2)/x^(5/2), x, algorithm="maxima")

[Out] $-5 * b^{3/2} * \log(-(\text{sqrt}(b) - \text{sqrt}(b * x + 2) / \text{sqrt}(x)) / (\text{sqrt}(b) + \text{sqrt}(b * x + 2) / \text{sqrt}(x))) - 8 * \text{sqrt}(b * x + 2) * b / \text{sqrt}(x) - 2 * \text{sqrt}(b * x + 2) * b^2 / ((b - (b * x + 2) / x) * \text{sqrt}(x)) - 4 / 3 * (b * x + 2)^{3/2} / x^{3/2}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(bx+2)^{5/2}}{x^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x + 2)^(5/2)/x^(5/2), x)

[Out] int((b*x + 2)^(5/2)/x^(5/2), x)

sympy [A] time = 5.15, size = 88, normalized size = 1.09

$$b^{\frac{5}{2}} x \sqrt{1 + \frac{2}{bx}} - \frac{28b^{\frac{3}{2}} \sqrt{1 + \frac{2}{bx}}}{3} - 5b^{\frac{3}{2}} \log\left(\frac{1}{bx}\right) + 10b^{\frac{3}{2}} \log\left(\sqrt{1 + \frac{2}{bx}} + 1\right) - \frac{8\sqrt{b} \sqrt{1 + \frac{2}{bx}}}{3x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+2)**(5/2)/x**(5/2),x)
```

```
[Out] b**(5/2)*x*sqrt(1 + 2/(b*x)) - 28*b**(3/2)*sqrt(1 + 2/(b*x))/3 - 5*b**(3/2)
*log(1/(b*x)) + 10*b**(3/2)*log(sqrt(1 + 2/(b*x)) + 1) - 8*sqrt(b)*sqrt(1 +
2/(b*x))/(3*x)
```

3.563 $\int x^{5/2}(2 - bx)^{5/2} dx$

Optimal. Leaf size=150

$$\frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{8b^{7/2}} - \frac{5\sqrt{x}\sqrt{2-bx}}{16b^3} - \frac{5x^{3/2}\sqrt{2-bx}}{48b^2} + \frac{1}{6}x^{7/2}(2-bx)^{5/2} + \frac{1}{6}x^{7/2}(2-bx)^{3/2} + \frac{1}{8}x^{7/2}\sqrt{2-bx} - \frac{x^{5/2}\sqrt{2-bx}}{24b}$$

[Out] $1/6*x^{(7/2)}*(-b*x+2)^{(3/2)}+1/6*x^{(7/2)}*(-b*x+2)^{(5/2)}+5/8*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(7/2)}-5/48*x^{(3/2)}*(-b*x+2)^{(1/2)}/b^2-1/24*x^{(5/2)}*(-b*x+2)^{(1/2)}/b+1/8*x^{(7/2)}*(-b*x+2)^{(1/2)}-5/16*x^{(1/2)}*(-b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.05, antiderivative size = 150, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$-\frac{5x^{3/2}\sqrt{2-bx}}{48b^2} - \frac{5\sqrt{x}\sqrt{2-bx}}{16b^3} + \frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{8b^{7/2}} + \frac{1}{6}x^{7/2}(2-bx)^{5/2} + \frac{1}{6}x^{7/2}(2-bx)^{3/2} + \frac{1}{8}x^{7/2}\sqrt{2-bx} - \frac{x^{5/2}\sqrt{2-bx}}{24b}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)*(2 - b*x)^(5/2), x]

[Out] $(-5*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/(16*b^3) - (5*x^{(3/2)}*\text{Sqrt}[2 - b*x])/(48*b^2) - (x^{(5/2)}*\text{Sqrt}[2 - b*x])/(24*b) + (x^{(7/2)}*\text{Sqrt}[2 - b*x])/8 + (x^{(7/2)}*(2 - b*x)^{(3/2)})/6 + (x^{(7/2)}*(2 - b*x)^{(5/2)})/6 + (5*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/(8*b^{(7/2)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int x^{5/2}(2-bx)^{5/2} dx &= \frac{1}{6}x^{7/2}(2-bx)^{5/2} + \frac{5}{6} \int x^{5/2}(2-bx)^{3/2} dx \\
 &= \frac{1}{6}x^{7/2}(2-bx)^{3/2} + \frac{1}{6}x^{7/2}(2-bx)^{5/2} + \frac{1}{2} \int x^{5/2}\sqrt{2-bx} dx \\
 &= \frac{1}{8}x^{7/2}\sqrt{2-bx} + \frac{1}{6}x^{7/2}(2-bx)^{3/2} + \frac{1}{6}x^{7/2}(2-bx)^{5/2} + \frac{1}{8} \int \frac{x^{5/2}}{\sqrt{2-bx}} dx \\
 &= -\frac{x^{5/2}\sqrt{2-bx}}{24b} + \frac{1}{8}x^{7/2}\sqrt{2-bx} + \frac{1}{6}x^{7/2}(2-bx)^{3/2} + \frac{1}{6}x^{7/2}(2-bx)^{5/2} + \frac{5 \int \frac{x^{3/2}}{\sqrt{2-bx}} dx}{24b} \\
 &= -\frac{5x^{3/2}\sqrt{2-bx}}{48b^2} - \frac{x^{5/2}\sqrt{2-bx}}{24b} + \frac{1}{8}x^{7/2}\sqrt{2-bx} + \frac{1}{6}x^{7/2}(2-bx)^{3/2} + \frac{1}{6}x^{7/2}(2-bx)^{5/2} + \dots \\
 &= -\frac{5\sqrt{x}\sqrt{2-bx}}{16b^3} - \frac{5x^{3/2}\sqrt{2-bx}}{48b^2} - \frac{x^{5/2}\sqrt{2-bx}}{24b} + \frac{1}{8}x^{7/2}\sqrt{2-bx} + \frac{1}{6}x^{7/2}(2-bx)^{3/2} + \frac{1}{6}x^{7/2}(2-bx)^{5/2} \\
 &= -\frac{5\sqrt{x}\sqrt{2-bx}}{16b^3} - \frac{5x^{3/2}\sqrt{2-bx}}{48b^2} - \frac{x^{5/2}\sqrt{2-bx}}{24b} + \frac{1}{8}x^{7/2}\sqrt{2-bx} + \frac{1}{6}x^{7/2}(2-bx)^{3/2} + \frac{1}{6}x^{7/2}(2-bx)^{5/2} \\
 &= -\frac{5\sqrt{x}\sqrt{2-bx}}{16b^3} - \frac{5x^{3/2}\sqrt{2-bx}}{48b^2} - \frac{x^{5/2}\sqrt{2-bx}}{24b} + \frac{1}{8}x^{7/2}\sqrt{2-bx} + \frac{1}{6}x^{7/2}(2-bx)^{3/2} + \frac{1}{6}x^{7/2}(2-bx)^{5/2}
 \end{aligned}$$

Mathematica [A] time = 0.06, size = 87, normalized size = 0.58

$$\frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{8b^{7/2}} + \frac{\sqrt{x}\sqrt{2-bx}(8b^5x^5 - 40b^4x^4 + 54b^3x^3 - 2b^2x^2 - 5bx - 15)}{48b^3}$$

Antiderivative was successfully verified.

[In] `Integrate[x^(5/2)*(2 - b*x)^(5/2), x]`

[Out] `(Sqrt[x]*Sqrt[2 - b*x]*(-15 - 5*b*x - 2*b^2*x^2 + 54*b^3*x^3 - 40*b^4*x^4 + 8*b^5*x^5))/(48*b^3) + (5*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(8*b^(7/2))`

fricas [A] time = 0.45, size = 173, normalized size = 1.15

$$\left[\frac{(8b^6x^5 - 40b^5x^4 + 54b^4x^3 - 2b^3x^2 - 5b^2x - 15b)\sqrt{-bx+2}\sqrt{x} - 15\sqrt{-b}\log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1)}{48b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(-b*x+2)^(5/2),x, algorithm="fricas")

[Out] [1/48*((8*b^6*x^5 - 40*b^5*x^4 + 54*b^4*x^3 - 2*b^3*x^2 - 5*b^2*x - 15*b)*sqrt(-b*x + 2)*sqrt(x) - 15*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^4, 1/48*((8*b^6*x^5 - 40*b^5*x^4 + 54*b^4*x^3 - 2*b^3*x^2 - 5*b^2*x - 15*b)*sqrt(-b*x + 2)*sqrt(x) - 30*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))))/b^4]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(-b*x+2)^(5/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.00, size = 148, normalized size = 0.99

$$\frac{(-bx+2)^{\frac{7}{2}}x^{\frac{5}{2}}}{6b} - \frac{(-bx+2)^{\frac{7}{2}}x^{\frac{3}{2}}}{6b^2} - \frac{(-bx+2)^{\frac{7}{2}}\sqrt{x}}{8b^3} + \frac{(-bx+2)^{\frac{5}{2}}\sqrt{x}}{24b^3} + \frac{5(-bx+2)^{\frac{3}{2}}\sqrt{x}}{48b^3} + \frac{5\sqrt{-bx+2}\sqrt{x}}{16b^3} + \frac{5\sqrt{-bx+2}\sqrt{x}}{16b^3} + \frac{5\sqrt{-bx+2}\sqrt{x}}{16b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(-b*x+2)^(5/2),x)

[Out] -1/6/b*x^(5/2)*(-b*x+2)^(7/2)-1/6/b^2*x^(3/2)*(-b*x+2)^(7/2)-1/8/b^3*x^(1/2)*(-b*x+2)^(7/2)+1/24*(-b*x+2)^(5/2)/b^3*x^(1/2)+5/48*(-b*x+2)^(3/2)/b^3*x^(1/2)+5/16*(-b*x+2)^(1/2)/b^3*x^(1/2)+5/16*((-b*x+2)*x)^(1/2)/(-b*x+2)^(1/2)/b^(7/2)/x^(1/2)*arctan((x-1/b)/(-b*x^2+2*x)^(1/2)*b^(1/2))

maxima [A] time = 2.96, size = 209, normalized size = 1.39

$$\frac{15\sqrt{-bx+2}b^5}{\sqrt{x}} + \frac{85(-bx+2)^{\frac{3}{2}}b^4}{x^{\frac{3}{2}}} + \frac{198(-bx+2)^{\frac{5}{2}}b^3}{x^{\frac{5}{2}}} - \frac{198(-bx+2)^{\frac{7}{2}}b^2}{x^{\frac{7}{2}}} - \frac{85(-bx+2)^{\frac{9}{2}}b}{x^{\frac{9}{2}}} - \frac{15(-bx+2)^{\frac{11}{2}}}{x^{\frac{11}{2}}} - \frac{5\arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{8b^{\frac{7}{2}}}$$

$$24\left(b^9 - \frac{6(bx-2)b^8}{x} + \frac{15(bx-2)^2b^7}{x^2} - \frac{20(bx-2)^3b^6}{x^3} + \frac{15(bx-2)^4b^5}{x^4} - \frac{6(bx-2)^5b^4}{x^5} + \frac{(bx-2)^6b^3}{x^6}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)*(-b*x+2)^(5/2),x, algorithm="maxima")

[Out] 1/24*(15*sqrt(-b*x + 2)*b^5/sqrt(x) + 85*(-b*x + 2)^(3/2)*b^4/x^(3/2) + 198*(-b*x + 2)^(5/2)*b^3/x^(5/2) - 198*(-b*x + 2)^(7/2)*b^2/x^(7/2) - 85*(-b*x + 2)^(9/2)*b/x^(9/2) - 15*(-b*x + 2)^(11/2)/x^(11/2))/(b^9 - 6*(b*x - 2)*b^8/x + 15*(b*x - 2)^2*b^7/x^2 - 20*(b*x - 2)^3*b^6/x^3 + 15*(b*x - 2)^4*b^5/x^4 - 6*(b*x - 2)^5*b^4/x^5 + (b*x - 2)^6*b^3/x^6) - 5/8*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/b^(7/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{5/2} (2 - bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)*(2 - b*x)^(5/2),x)

[Out] int(x^(5/2)*(2 - b*x)^(5/2), x)

sympy [A] time = 22.84, size = 337, normalized size = 2.25

$$\left\{ \begin{array}{l} \frac{ib^3x^{13}}{6\sqrt{bx-2}} - \frac{7ib^2x^{11}}{6\sqrt{bx-2}} + \frac{67ibx^9}{24\sqrt{bx-2}} - \frac{55ix^7}{24\sqrt{bx-2}} - \frac{ix^5}{48b\sqrt{bx-2}} - \frac{5ix^3}{48b^2\sqrt{bx-2}} + \frac{5i\sqrt{x}}{8b^3\sqrt{bx-2}} - \frac{5i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{8b^{\frac{7}{2}}} \quad \text{for } \frac{|bx|}{2} > 1 \\ -\frac{b^3x^{13}}{6\sqrt{-bx+2}} + \frac{7b^2x^{11}}{6\sqrt{-bx+2}} - \frac{67bx^9}{24\sqrt{-bx+2}} + \frac{55x^7}{24\sqrt{-bx+2}} + \frac{x^5}{48b\sqrt{-bx+2}} + \frac{5x^3}{48b^2\sqrt{-bx+2}} - \frac{5\sqrt{x}}{8b^3\sqrt{-bx+2}} + \frac{5 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{8b^{\frac{7}{2}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)*(-b*x+2)**(5/2),x)

[Out] Piecewise((I*b**3*x**(13/2)/(6*sqrt(b*x - 2)) - 7*I*b**2*x**(11/2)/(6*sqrt(b*x - 2)) + 67*I*b*x**(9/2)/(24*sqrt(b*x - 2)) - 55*I*x**(7/2)/(24*sqrt(b*x - 2)) - I*x**(5/2)/(48*b*sqrt(b*x - 2)) - 5*I*x**(3/2)/(48*b**2*sqrt(b*x - 2)) + 5*I*sqrt(x)/(8*b**3*sqrt(b*x - 2)) - 5*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(8*b**(7/2)), Abs(b*x)/2 > 1), (-b**3*x**(13/2)/(6*sqrt(-b*x + 2)) + 7*b**2*x**(11/2)/(6*sqrt(-b*x + 2)) - 67*b*x**(9/2)/(24*sqrt(-b*x + 2)) + 55*x**(7/2)/(24*sqrt(-b*x + 2)) + x**(5/2)/(48*b*sqrt(-b*x + 2)) + 5*x**(3/2)/(48*b**2*sqrt(-b*x + 2)) - 5*sqrt(x)/(8*b**3*sqrt(-b*x + 2)) + 5*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/(8*b**(7/2)), True))

3.564 $\int x^{3/2}(2 - bx)^{5/2} dx$

Optimal. Leaf size=128

$$\frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} - \frac{3\sqrt{x}\sqrt{2-bx}}{8b^2} + \frac{1}{5}x^{5/2}(2-bx)^{5/2} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{4}x^{5/2}\sqrt{2-bx} - \frac{x^{3/2}\sqrt{2-bx}}{8b}$$

[Out] $1/4*x^{(5/2)}*(-b*x+2)^{(3/2)}+1/5*x^{(5/2)}*(-b*x+2)^{(5/2)}+3/4*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(5/2)}-1/8*x^{(3/2)}*(-b*x+2)^{(1/2)}/b+1/4*x^{(5/2)}*(-b*x+2)^{(1/2)}-3/8*x^{(1/2)}*(-b*x+2)^{(1/2)}/b^2$

Rubi [A] time = 0.03, antiderivative size = 128, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$-\frac{3\sqrt{x}\sqrt{2-bx}}{8b^2} + \frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} + \frac{1}{5}x^{5/2}(2-bx)^{5/2} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{4}x^{5/2}\sqrt{2-bx} - \frac{x^{3/2}\sqrt{2-bx}}{8b}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)*(2 - b*x)^(5/2), x]

[Out] $(-3*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/(8*b^2) - (x^{(3/2)}*\text{Sqrt}[2 - b*x])/(8*b) + (x^{(5/2)}*\text{Sqrt}[2 - b*x])/4 + (x^{(5/2)}*(2 - b*x)^{(3/2)})/4 + (x^{(5/2)}*(2 - b*x)^{(5/2)})/5 + (3*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/(4*b^{(5/2)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int x^{3/2}(2-bx)^{5/2} dx &= \frac{1}{5}x^{5/2}(2-bx)^{5/2} + \int x^{3/2}(2-bx)^{3/2} dx \\
&= \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{5}x^{5/2}(2-bx)^{5/2} + \frac{3}{4} \int x^{3/2}\sqrt{2-bx} dx \\
&= \frac{1}{4}x^{5/2}\sqrt{2-bx} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{5}x^{5/2}(2-bx)^{5/2} + \frac{1}{4} \int \frac{x^{3/2}}{\sqrt{2-bx}} dx \\
&= -\frac{x^{3/2}\sqrt{2-bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2-bx} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{5}x^{5/2}(2-bx)^{5/2} + \frac{3}{8b} \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{8b^2} - \frac{x^{3/2}\sqrt{2-bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2-bx} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{5}x^{5/2}(2-bx)^{5/2} + \frac{3}{8b} \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{8b^2} - \frac{x^{3/2}\sqrt{2-bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2-bx} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{5}x^{5/2}(2-bx)^{5/2} + \frac{3}{8b} \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{8b^2} - \frac{x^{3/2}\sqrt{2-bx}}{8b} + \frac{1}{4}x^{5/2}\sqrt{2-bx} + \frac{1}{4}x^{5/2}(2-bx)^{3/2} + \frac{1}{5}x^{5/2}(2-bx)^{5/2} + \frac{3}{8b} \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx
\end{aligned}$$

Mathematica [A] time = 0.05, size = 79, normalized size = 0.62

$$\frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{5/2}} + \frac{\sqrt{x}\sqrt{2-bx}(8b^4x^4 - 42b^3x^3 + 62b^2x^2 - 5bx - 15)}{40b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*(2 - b*x)^(5/2), x]

[Out] (Sqrt[x]*Sqrt[2 - b*x]*(-15 - 5*b*x + 62*b^2*x^2 - 42*b^3*x^3 + 8*b^4*x^4))/(40*b^2) + (3*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(4*b^(5/2))

fricas [A] time = 0.44, size = 157, normalized size = 1.23

$$\left[\frac{(8b^5x^4 - 42b^4x^3 + 62b^3x^2 - 5b^2x - 15b)\sqrt{-bx+2}\sqrt{x} - 15\sqrt{-b}\log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1)}{40b^3}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+2)^(5/2), x, algorithm="fricas")

```
[Out] [1/40*((8*b^5*x^4 - 42*b^4*x^3 + 62*b^3*x^2 - 5*b^2*x - 15*b)*sqrt(-b*x + 2)
)*sqrt(x) - 15*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^
3, 1/40*((8*b^5*x^4 - 42*b^4*x^3 + 62*b^3*x^2 - 5*b^2*x - 15*b)*sqrt(-b*x +
2)*sqrt(x) - 30*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/b^3]
```

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^(3/2)*(-b*x+2)^(5/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warni
ng, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+
%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[
1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}
+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4
,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%
}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+
%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,
[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}
+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8
,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]
%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%
{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0
,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-17.51342
60082,53.112478131]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,
0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+
%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[
0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%
}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20
,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]
%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%
{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[
4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}
+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46
,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]
%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%
{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at para
meters values [-62.3026123089,89.629912049]Warning, choosing root of [1,0,
%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2
,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+
%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[
3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+
%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20
```

, [1, 2]%%}+%%{128, [1, 1]%%}+%%{-16, [1, 0]%%}+%%{-4, [0, 3]%%}+%%{8, [0, 2]%%}+%%{16, [0, 1]%%}+%%{-32, [0, 0]%%}, 0, %%{1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{1, [4, 0]%%}+%%{4, [3, 4]%%}+%%{-12, [3, 3]%%}+%%{20, [3, 2]%%}+%%{-20, [3, 1]%%}+%%{8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{4, [1, 4]%%}+%%{-20, [1, 3]%%}+%%{40, [1, 2]%%}+%%{-48, [1, 1]%%}+%%{32, [1, 0]%%}+%%{1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{16, [0, 0]%%}] at parameters values [-94.177692275, 55.0343274642]Warning, choosing root of [1, 0, %%{4, [1, 1]%%}+%%{4, [1, 0]%%}+%%{-4, [0, 1]%%}+%%{-8, [0, 0]%%}, 0, %%{6, [2, 2]%%}+%%{4, [2, 1]%%}+%%{6, [2, 0]%%}+%%{-4, [1, 2]%%}+%%{-28, [1, 1]%%}+%%{-8, [1, 0]%%}+%%{6, [0, 2]%%}+%%{8, [0, 1]%%}+%%{24, [0, 0]%%}, 0, %%{4, [3, 3]%%}+%%{-4, [3, 2]%%}+%%{-4, [3, 1]%%}+%%{4, [3, 0]%%}+%%{4, [2, 3]%%}+%%{-64, [2, 2]%%}+%%{20, [2, 1]%%}+%%{8, [2, 0]%%}+%%{-4, [1, 3]%%}+%%{-20, [1, 2]%%}+%%{128, [1, 1]%%}+%%{-16, [1, 0]%%}+%%{-4, [0, 3]%%}+%%{8, [0, 2]%%}+%%{16, [0, 1]%%}+%%{-32, [0, 0]%%}, 0, %%{1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{1, [4, 0]%%}+%%{4, [3, 4]%%}+%%{-12, [3, 3]%%}+%%{20, [3, 2]%%}+%%{-20, [3, 1]%%}+%%{8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{4, [1, 4]%%}+%%{-20, [1, 3]%%}+%%{40, [1, 2]%%}+%%{-48, [1, 1]%%}+%%{32, [1, 0]%%}+%%{1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{16, [0, 0]%%}] at parameters values [-47.5119365202, 16.0204098616]Warning, choosing root of [1, 0, %%{4, [1, 1]%%}+%%{4, [1, 0]%%}+%%{-4, [0, 1]%%}+%%{-8, [0, 0]%%}, 0, %%{6, [2, 2]%%}+%%{4, [2, 1]%%}+%%{6, [2, 0]%%}+%%{-4, [1, 2]%%}+%%{-28, [1, 1]%%}+%%{-8, [1, 0]%%}+%%{6, [0, 2]%%}+%%{8, [0, 1]%%}+%%{24, [0, 0]%%}, 0, %%{4, [3, 3]%%}+%%{-4, [3, 2]%%}+%%{-4, [3, 1]%%}+%%{4, [3, 0]%%}+%%{4, [2, 3]%%}+%%{-64, [2, 2]%%}+%%{20, [2, 1]%%}+%%{8, [2, 0]%%}+%%{-4, [1, 3]%%}+%%{-20, [1, 2]%%}+%%{128, [1, 1]%%}+%%{-16, [1, 0]%%}+%%{-4, [0, 3]%%}+%%{8, [0, 2]%%}+%%{16, [0, 1]%%}+%%{-32, [0, 0]%%}, 0, %%{1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{1, [4, 0]%%}+%%{4, [3, 4]%%}+%%{-12, [3, 3]%%}+%%{20, [3, 2]%%}+%%{-20, [3, 1]%%}+%%{8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{4, [1, 4]%%}+%%{-20, [1, 3]%%}+%%{40, [1, 2]%%}+%%{-48, [1, 1]%%}+%%{32, [1, 0]%%}+%%{1, [0, 4]%%}+%%{-8, [0, 3]%%}+%%{24, [0, 2]%%}+%%{-32, [0, 1]%%}+%%{16, [0, 0]%%}] at parameters values [-54.7543625063, 66.0382199469]Warning, choosing root of [1, 0, %%{4, [1, 1]%%}+%%{4, [1, 0]%%}+%%{-4, [0, 1]%%}+%%{-8, [0, 0]%%}, 0, %%{6, [2, 2]%%}+%%{4, [2, 1]%%}+%%{6, [2, 0]%%}+%%{-4, [1, 2]%%}+%%{-28, [1, 1]%%}+%%{-8, [1, 0]%%}+%%{6, [0, 2]%%}+%%{8, [0, 1]%%}+%%{24, [0, 0]%%}, 0, %%{4, [3, 3]%%}+%%{-4, [3, 2]%%}+%%{-4, [3, 1]%%}+%%{4, [3, 0]%%}+%%{4, [2, 3]%%}+%%{-64, [2, 2]%%}+%%{20, [2, 1]%%}+%%{8, [2, 0]%%}+%%{-4, [1, 3]%%}+%%{-20, [1, 2]%%}+%%{128, [1, 1]%%}+%%{-16, [1, 0]%%}+%%{-4, [0, 3]%%}+%%{8, [0, 2]%%}+%%{16, [0, 1]%%}+%%{-32, [0, 0]%%}, 0, %%{1, [4, 4]%%}+%%{-4, [4, 3]%%}+%%{6, [4, 2]%%}+%%{-4, [4, 1]%%}+%%{1, [4, 0]%%}+%%{4, [3, 4]%%}+%%{-12, [3, 3]%%}+%%{20, [3, 2]%%}+%%{-20, [3, 1]%%}+%%{8, [3, 0]%%}+%%{6, [2, 4]%%}+%%{-20, [2, 3]%%}+%%{46, [2, 2]%%}+%%{-40, [2, 1]%%}+%%{24, [2, 0]%%}+%%{4,

$[1, 4] + \{-20, [1, 3] + \{40, [1, 2] + \{-48, [1, 1] + \{32, [1, 0] + \{1, [0, 4] + \{-8, [0, 3] + \{24, [0, 2] + \{-32, [0, 1] + \{16, [0, 0]\}\}\}\}\}$ at parameters values $[-6.07356301835, 51.8441526662]$ Warning, choosing root of $[1, 0, \{4, [1, 1] + \{4, [1, 0] + \{-4, [0, 1] + \{-8, [0, 0] + \{6, [2, 2] + \{4, [2, 1] + \{6, [2, 0] + \{-4, [1, 2] + \{-28, [1, 1] + \{-8, [1, 0] + \{6, [0, 2] + \{8, [0, 1] + \{24, [0, 0] + \{0, \{4, [3, 3] + \{-4, [3, 2] + \{-4, [3, 1] + \{4, [3, 0] + \{4, [2, 3] + \{-64, [2, 2] + \{20, [2, 1] + \{8, [2, 0] + \{-4, [1, 3] + \{-20, [1, 2] + \{128, [1, 1] + \{-16, [1, 0] + \{-4, [0, 3] + \{8, [0, 2] + \{16, [0, 1] + \{-32, [0, 0] + \{1, [4, 4] + \{-4, [4, 3] + \{6, [4, 2] + \{-4, [4, 1] + \{1, [4, 0] + \{4, [3, 4] + \{-12, [3, 3] + \{20, [3, 2] + \{-20, [3, 1] + \{8, [3, 0] + \{6, [2, 4] + \{-20, [2, 3] + \{46, [2, 2] + \{-40, [2, 1] + \{24, [2, 0] + \{4, [1, 4] + \{-20, [1, 3] + \{40, [1, 2] + \{-48, [1, 1] + \{32, [1, 0] + \{1, [0, 4] + \{-8, [0, 3] + \{24, [0, 2] + \{-32, [0, 1] + \{16, [0, 0]\}\}\}\}\}$ at parameters values $[-2.28782047657, 4.66774101928]$ Warning, choosing root of $[1, 0, \{4, [1, 1] + \{4, [1, 0] + \{-4, [0, 1] + \{-8, [0, 0] + \{6, [2, 2] + \{4, [2, 1] + \{6, [2, 0] + \{-4, [1, 2] + \{-28, [1, 1] + \{-8, [1, 0] + \{6, [0, 2] + \{8, [0, 1] + \{24, [0, 0] + \{0, \{4, [3, 3] + \{-4, [3, 2] + \{-4, [3, 1] + \{4, [3, 0] + \{4, [2, 3] + \{-64, [2, 2] + \{20, [2, 1] + \{8, [2, 0] + \{-4, [1, 3] + \{-20, [1, 2] + \{128, [1, 1] + \{-16, [1, 0] + \{-4, [0, 3] + \{8, [0, 2] + \{16, [0, 1] + \{-32, [0, 0] + \{1, [4, 4] + \{-4, [4, 3] + \{6, [4, 2] + \{-4, [4, 1] + \{1, [4, 0] + \{4, [3, 4] + \{-12, [3, 3] + \{20, [3, 2] + \{-20, [3, 1] + \{8, [3, 0] + \{6, [2, 4] + \{-20, [2, 3] + \{46, [2, 2] + \{-40, [2, 1] + \{24, [2, 0] + \{4, [1, 4] + \{-20, [1, 3] + \{40, [1, 2] + \{-48, [1, 1] + \{32, [1, 0] + \{1, [0, 4] + \{-8, [0, 3] + \{24, [0, 2] + \{-32, [0, 1] + \{16, [0, 0]\}\}\}\}\}$ at parameters values $[-10.7897139532, 38.2197840363]$ $1/b * (2*b^3*abs(b)/b^2*(2*((5040*b^19/100800/b^23*\sqrt{-b*x+2})*\sqrt{-b*x+2}-51660*b^19/100800/b^23)*\sqrt{-b*x+2})*\sqrt{-b*x+2}+215460*b^19/100800/b^23)*\sqrt{-b*x+2})*\sqrt{-b*x+2}-469350*b^19/100800/b^23)*\sqrt{-b*x+2})*\sqrt{-b*x+2}+607950*b^19/100800/b^23)*\sqrt{-b*x+2})*\sqrt{-b*(-b*x+2)+2*b}-63/8/b^3/\sqrt{-b}*\ln(abs(\sqrt{-b*(-b*x+2)+2*b}-\sqrt{-b})*\sqrt{-b*x+2}))-12*b^2*abs(b)/b^2*(2*((-90*b^11/1440/b^14*\sqrt{-b*x+2})*\sqrt{-b*x+2}+750*b^11/1440/b^14)*\sqrt{-b*x+2})*\sqrt{-b*x+2}-2445*b^11/1440/b^14)*\sqrt{-b*x+2})*\sqrt{-b*x+2}+4185*b^11/1440/b^14)*\sqrt{-b*x+2})*\sqrt{-b*(-b*x+2)+2*b}-35/8/b^2/\sqrt{-b}*\ln(abs(\sqrt{-b*(-b*x+2)+2*b}-\sqrt{-b})*\sqrt{-b*x+2}))+24*b*abs(b)/b^2*(2*((12*b^5/144/b^7*\sqrt{-b*x+2})*\sqrt{-b*x+2}-78*b^5/144/b^7)*\sqrt{-b*x+2})*\sqrt{-b*x+2}+198*b^5/144/b^7)*\sqrt{-b*x+2})*\sqrt{-b*(-b*x+2)+2*b}-5/2/b/\sqrt{-b}*\ln(abs(\sqrt{-b*(-b*x+2)+2*b}-\sqrt{-b})*\sqrt{-b*x+2}))+16*abs(b)/b^2/b*(2*(1/8*\sqrt{-b*x+2})*\sqrt{-b*x+2}-5/8)*\sqrt{-b*x+2})*\sqrt{-b*(-b*x+2)+2*b}+6*b/4/\sqrt{-b}*\ln(abs(\sqrt{-b*(-b*x+2)+2*b}-\sqrt{-b})*\sqrt{-b*x+2}))))$

maple [A] time = 0.01, size = 132, normalized size = 1.03

$$-\frac{(-bx+2)^{\frac{7}{2}}x^{\frac{3}{2}}}{5b} - \frac{3(-bx+2)^{\frac{7}{2}}\sqrt{x}}{20b^2} + \frac{(-bx+2)^{\frac{5}{2}}\sqrt{x}}{20b^2} + \frac{(-bx+2)^{\frac{3}{2}}\sqrt{x}}{8b^2} + \frac{3\sqrt{-bx+2}\sqrt{x}}{8b^2} + \frac{3\sqrt{-bx+2}x \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{8\sqrt{-bx+2}b^{\frac{5}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(-b*x+2)^(5/2), x)

[Out] $-1/5/b*x^{(3/2)}*(-b*x+2)^{(7/2)}-3/20/b^2*x^{(1/2)}*(-b*x+2)^{(7/2)}+1/20*(-b*x+2)^{(5/2)}/b^2*x^{(1/2)}+1/8*(-b*x+2)^{(3/2)}/b^2*x^{(1/2)}+3/8*(-b*x+2)^{(1/2)}/b^2*x^{(1/2)}+3/8*((-b*x+2)*x)^{(1/2)}/(-b*x+2)^{(1/2)}/b^{(5/2)}/x^{(1/2)}*\arctan((x-1/b)/(-b*x^2+2*x))^{(1/2)}*b^{(1/2)}$

maxima [B] time = 3.01, size = 179, normalized size = 1.40

$$\frac{\frac{15\sqrt{-bx+2}b^4}{\sqrt{x}} + \frac{70(-bx+2)^{\frac{3}{2}}b^3}{x^{\frac{3}{2}}} + \frac{128(-bx+2)^{\frac{5}{2}}b^2}{x^{\frac{5}{2}}} - \frac{70(-bx+2)^{\frac{7}{2}}b}{x^{\frac{7}{2}}} - \frac{15(-bx+2)^{\frac{9}{2}}}{x^{\frac{9}{2}}}}{20\left(b^7 - \frac{5(bx-2)b^6}{x} + \frac{10(bx-2)^2b^5}{x^2} - \frac{10(bx-2)^3b^4}{x^3} + \frac{5(bx-2)^4b^3}{x^4} - \frac{(bx-2)^5b^2}{x^5}\right)} - \frac{3 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{4b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(-b*x+2)^(5/2), x, algorithm="maxima")

[Out] $1/20*(15*\sqrt{-b*x+2}*b^4/\sqrt{x} + 70*(-b*x+2)^{(3/2)}*b^3/x^{(3/2)} + 128*(-b*x+2)^{(5/2)}*b^2/x^{(5/2)} - 70*(-b*x+2)^{(7/2)}*b/x^{(7/2)} - 15*(-b*x+2)^{(9/2)}/x^{(9/2)})/(b^7 - 5*(b*x-2)*b^6/x + 10*(b*x-2)^2*b^5/x^2 - 10*(b*x-2)^3*b^4/x^3 + 5*(b*x-2)^4*b^3/x^4 - (b*x-2)^5*b^2/x^5) - 3/4*\arctan(\sqrt{-b*x+2}/(\sqrt{b}*\sqrt{x}))/b^{(5/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3/2} (2 - bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(2 - b*x)^(5/2), x)

[Out] int(x^(3/2)*(2 - b*x)^(5/2), x)

sympy [A] time = 14.30, size = 294, normalized size = 2.30

$$\left\{ \begin{array}{l} \frac{ib^3x^{\frac{11}{2}}}{5\sqrt{bx-2}} - \frac{29ib^2x^{\frac{9}{2}}}{20\sqrt{bx-2}} + \frac{73ibx^{\frac{7}{2}}}{20\sqrt{bx-2}} - \frac{129ix^{\frac{5}{2}}}{40\sqrt{bx-2}} - \frac{ix^{\frac{3}{2}}}{8b\sqrt{bx-2}} + \frac{3i\sqrt{x}}{4b^2\sqrt{bx-2}} - \frac{3i\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{5}{2}}} \\ -\frac{b^3x^{\frac{11}{2}}}{5\sqrt{-bx+2}} + \frac{29b^2x^{\frac{9}{2}}}{20\sqrt{-bx+2}} - \frac{73bx^{\frac{7}{2}}}{20\sqrt{-bx+2}} + \frac{129x^{\frac{5}{2}}}{40\sqrt{-bx+2}} + \frac{x^{\frac{3}{2}}}{8b\sqrt{-bx+2}} - \frac{3\sqrt{x}}{4b^2\sqrt{-bx+2}} + \frac{3\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{5}{2}}} \end{array} \right. \begin{array}{l} \text{for } \frac{|bx|}{2} > 1 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)*(-b*x+2)**(5/2),x)

[Out] Piecewise((I*b**3*x**(11/2)/(5*sqrt(b*x - 2)) - 29*I*b**2*x**(9/2)/(20*sqrt(b*x - 2)) + 73*I*b*x**(7/2)/(20*sqrt(b*x - 2)) - 129*I*x**(5/2)/(40*sqrt(b*x - 2)) - I*x**(3/2)/(8*b*sqrt(b*x - 2)) + 3*I*sqrt(x)/(4*b**2*sqrt(b*x - 2)) - 3*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(5/2)), Abs(b*x)/2 > 1), (-b**3*x**(11/2)/(5*sqrt(-b*x + 2)) + 29*b**2*x**(9/2)/(20*sqrt(-b*x + 2)) - 73*b*x**(7/2)/(20*sqrt(-b*x + 2)) + 129*x**(5/2)/(40*sqrt(-b*x + 2)) + x**(3/2)/(8*b*sqrt(-b*x + 2)) - 3*sqrt(x)/(4*b**2*sqrt(-b*x + 2)) + 3*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(5/2)), True))

3.565 $\int \sqrt{x} (2 - bx)^{5/2} dx$

Optimal. Leaf size=106

$$\frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{3/2}} + \frac{1}{4}x^{3/2}(2 - bx)^{5/2} + \frac{5}{12}x^{3/2}(2 - bx)^{3/2} + \frac{5}{8}x^{3/2}\sqrt{2 - bx} - \frac{5\sqrt{x}\sqrt{2 - bx}}{8b}$$

[Out] $5/12*x^{(3/2)}*(-b*x+2)^{(3/2)}+1/4*x^{(3/2)}*(-b*x+2)^{(5/2)}+5/4*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(3/2)}+5/8*x^{(3/2)}*(-b*x+2)^{(1/2)}-5/8*x^{(1/2)}*(-b*x+2)^{(1/2)}/b$

Rubi [A] time = 0.02, antiderivative size = 106, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$\frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{4b^{3/2}} + \frac{1}{4}x^{3/2}(2 - bx)^{5/2} + \frac{5}{12}x^{3/2}(2 - bx)^{3/2} + \frac{5}{8}x^{3/2}\sqrt{2 - bx} - \frac{5\sqrt{x}\sqrt{2 - bx}}{8b}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[x]*(2 - b*x)^(5/2), x]`

[Out] $(-5*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/(8*b) + (5*x^{(3/2)}*\text{Sqrt}[2 - b*x])/8 + (5*x^{(3/2)}*(2 - b*x)^{(3/2)})/12 + (x^{(3/2)}*(2 - b*x)^{(5/2)})/4 + (5*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/(4*b^{(3/2)})$

Rule 50

`Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 54

`Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]`

Rule 216

`Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
\int \sqrt{x} (2 - bx)^{5/2} dx &= \frac{1}{4} x^{3/2} (2 - bx)^{5/2} + \frac{5}{4} \int \sqrt{x} (2 - bx)^{3/2} dx \\
&= \frac{5}{12} x^{3/2} (2 - bx)^{3/2} + \frac{1}{4} x^{3/2} (2 - bx)^{5/2} + \frac{5}{4} \int \sqrt{x} \sqrt{2 - bx} dx \\
&= \frac{5}{8} x^{3/2} \sqrt{2 - bx} + \frac{5}{12} x^{3/2} (2 - bx)^{3/2} + \frac{1}{4} x^{3/2} (2 - bx)^{5/2} + \frac{5}{8} \int \frac{\sqrt{x}}{\sqrt{2 - bx}} dx \\
&= -\frac{5\sqrt{x} \sqrt{2 - bx}}{8b} + \frac{5}{8} x^{3/2} \sqrt{2 - bx} + \frac{5}{12} x^{3/2} (2 - bx)^{3/2} + \frac{1}{4} x^{3/2} (2 - bx)^{5/2} + \frac{5 \int \frac{1}{\sqrt{x} \sqrt{2 - bx}} dx}{8b} \\
&= -\frac{5\sqrt{x} \sqrt{2 - bx}}{8b} + \frac{5}{8} x^{3/2} \sqrt{2 - bx} + \frac{5}{12} x^{3/2} (2 - bx)^{3/2} + \frac{1}{4} x^{3/2} (2 - bx)^{5/2} + \frac{5 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2 - bx}} dx\right)}{4b} \\
&= -\frac{5\sqrt{x} \sqrt{2 - bx}}{8b} + \frac{5}{8} x^{3/2} \sqrt{2 - bx} + \frac{5}{12} x^{3/2} (2 - bx)^{3/2} + \frac{1}{4} x^{3/2} (2 - bx)^{5/2} + \frac{5 \sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{4b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 71, normalized size = 0.67

$$\frac{5 \sin^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{4b^{3/2}} + \frac{\sqrt{x} \sqrt{2 - bx} (6b^3 x^3 - 34b^2 x^2 + 59bx - 15)}{24b}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*(2 - b*x)^(5/2), x]

[Out] (Sqrt[x]*Sqrt[2 - b*x]*(-15 + 59*b*x - 34*b^2*x^2 + 6*b^3*x^3))/(24*b) + (5*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(4*b^(3/2))

fricas [A] time = 0.47, size = 141, normalized size = 1.33

$$\left[\frac{(6b^4 x^3 - 34b^3 x^2 + 59b^2 x - 15b) \sqrt{-bx + 2} \sqrt{x} - 15 \sqrt{-b} \log(-bx + \sqrt{-bx + 2} \sqrt{-b} \sqrt{x} + 1)}{24b^2}, \frac{(6b^4 x^3 - 34b^3 x^2 + 59b^2 x - 15b) \sqrt{-bx + 2} \sqrt{x} - 15 \sqrt{-b} \log(-bx + \sqrt{-bx + 2} \sqrt{-b} \sqrt{x} + 1)}{24b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(5/2)*x^(1/2), x, algorithm="fricas")

[Out] [1/24*((6*b^4*x^3 - 34*b^3*x^2 + 59*b^2*x - 15*b)*sqrt(-b*x + 2)*sqrt(x) - 15*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^2, 1/24*((6*

$$b^4 x^3 - 34 b^3 x^2 + 59 b^2 x - 15 b) \sqrt{-b x + 2} \sqrt{x} - 30 \sqrt{b} \arctan(\sqrt{-b x + 2} / (\sqrt{b} \sqrt{x})) / b^2]$$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(5/2)*x^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4, [1,1]%%}+%%{4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0, %%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{-4, [1,2]%%}+%%{-28, [1,1]%%}+%%{-8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0, %%{4, [3,3]%%}+%%{-4, [3,2]%%}+%%{-4, [3,1]%%}+%%{4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{-4, [1,3]%%}+%%{-20, [1,2]%%}+%%{128, [1,1]%%}+%%{-16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0, %%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{4, [3,4]%%}+%%{-12, [3,3]%%}+%%{20, [3,2]%%}+%%{-20, [3,1]%%}+%%{8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{4, [1,4]%%}+%%{-20, [1,3]%%}+%%{40, [1,2]%%}+%%{-48, [1,1]%%}+%%{32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [-17.51342 60082,53.112478131]Warning, choosing root of [1,0,%%{4, [1,1]%%}+%%{4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0, %%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{-4, [1,2]%%}+%%{-28, [1,1]%%}+%%{-8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0, %%{4, [3,3]%%}+%%{-4, [3,2]%%}+%%{-4, [3,1]%%}+%%{4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{-4, [1,3]%%}+%%{-20, [1,2]%%}+%%{128, [1,1]%%}+%%{-16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0, %%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{4, [3,4]%%}+%%{-12, [3,3]%%}+%%{20, [3,2]%%}+%%{-20, [3,1]%%}+%%{8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{4, [1,4]%%}+%%{-20, [1,3]%%}+%%{40, [1,2]%%}+%%{-48, [1,1]%%}+%%{32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [-62.3026123089,89.629912049]Warning, choosing root of [1,0,%%{4, [1,1]%%}+%%{4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0, %%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{-4, [1,2]%%}+%%{-28, [1,1]%%}+%%{-8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0, %%{4, [3,3]%%}+%%{-4, [3,2]%%}+%%{-4, [3,1]%%}+%%{4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{-4, [1,3]%%}+%%{-20, [1,2]%%}+%%{128, [1,1]%%}+%%{-16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0, %%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{4, [3,4]%%}+%%{-12, [3,3]%%}+%%{20, [3,2]%%}+%%{-20, [3,1]%%}+%%{8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{4, [1,4]%%}+%%{-20, [1,3]%%}+%%{40, [1,2]%%}+%%{-48, [1,1]%%}+%%{32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [-17.51342 60082,53.112478131]Warning, choosing root of [1,0,%%{4, [1,1]%%}+%%{4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0, %%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{-4, [1,2]%%}+%%{-28, [1,1]%%}+%%{-8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0, %%{4, [3,3]%%}+%%{-4, [3,2]%%}+%%{-4, [3,1]%%}+%%{4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{-4, [1,3]%%}+%%{-20, [1,2]%%}+%%{128, [1,1]%%}+%%{-16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0, %%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{4, [3,4]%%}+%%{-12, [3,3]%%}+%%{20, [3,2]%%}+%%{-20, [3,1]%%}+%%{8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{4, [1,4]%%}+%%{-20, [1,3]%%}+%%{40, [1,2]%%}+%%{-48, [1,1]%%}+%%{32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [-62.3026123089,89.629912049]

$\{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values $[-94.177692275, 55.0343274642]$ Warning, choosing root of $[1, 0, \{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values $[-47.5119365202, 16.0204098616]$ Warning, choosing root of $[1, 0, \{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$ at parameters values $[-54.7543625063, 66.0382199469]$ Warning, choosing root of $[1, 0, \{4, [1, 1]\} + \{4, [1, 0]\} + \{-4, [0, 1]\} + \{-8, [0, 0]\}, 0, \{6, [2, 2]\} + \{4, [2, 1]\} + \{6, [2, 0]\} + \{-4, [1, 2]\} + \{-28, [1, 1]\} + \{-8, [1, 0]\} + \{6, [0, 2]\} + \{8, [0, 1]\} + \{24, [0, 0]\}, 0, \{4, [3, 3]\} + \{-4, [3, 2]\} + \{-4, [3, 1]\} + \{4, [3, 0]\} + \{4, [2, 3]\} + \{-64, [2, 2]\} + \{20, [2, 1]\} + \{8, [2, 0]\} + \{-4, [1, 3]\} + \{-20, [1, 2]\} + \{128, [1, 1]\} + \{-16, [1, 0]\} + \{-4, [0, 3]\} + \{8, [0, 2]\} + \{16, [0, 1]\} + \{-32, [0, 0]\}, 0, \{1, [4, 4]\} + \{-4, [4, 3]\} + \{6, [4, 2]\} + \{-4, [4, 1]\} + \{1, [4, 0]\} + \{4, [3, 4]\} + \{-12, [3, 3]\} + \{20, [3, 2]\} + \{-20, [3, 1]\} + \{8, [3, 0]\} + \{6, [2, 4]\} + \{-20, [2, 3]\} + \{46, [2, 2]\} + \{-40, [2, 1]\} + \{24, [2, 0]\} + \{4, [1, 4]\} + \{-20, [1, 3]\} + \{40, [1, 2]\} + \{-48, [1, 1]\} + \{32, [1, 0]\} + \{1, [0, 4]\} + \{-8, [0, 3]\} + \{24, [0, 2]\} + \{-32, [0, 1]\} + \{16, [0, 0]\}$

$\% \{16, [0, 0]\}$] at parameters values $[-6.07356301835, 51.8441526662]$ Warning, choosing root of $[1, 0, \% \{4, [1, 1]\} + \% \{4, [1, 0]\} + \% \{-4, [0, 1]\} + \% \{-8, [0, 0]\}, 0, \% \{6, [2, 2]\} + \% \{4, [2, 1]\} + \% \{6, [2, 0]\} + \% \{-4, [1, 2]\} + \% \{-28, [1, 1]\} + \% \{-8, [1, 0]\} + \% \{6, [0, 2]\} + \% \{8, [0, 1]\} + \% \{24, [0, 0]\}, 0, \% \{4, [3, 3]\} + \% \{-4, [3, 2]\} + \% \{-4, [3, 1]\} + \% \{4, [3, 0]\} + \% \{4, [2, 3]\} + \% \{-64, [2, 2]\} + \% \{20, [2, 1]\} + \% \{8, [2, 0]\} + \% \{-4, [1, 3]\} + \% \{-20, [1, 2]\} + \% \{128, [1, 1]\} + \% \{-16, [1, 0]\} + \% \{-4, [0, 3]\} + \% \{8, [0, 2]\} + \% \{16, [0, 1]\} + \% \{-32, [0, 0]\}, 0, \% \{1, [4, 4]\} + \% \{-4, [4, 3]\} + \% \{6, [4, 2]\} + \% \{-4, [4, 1]\} + \% \{1, [4, 0]\} + \% \{4, [3, 4]\} + \% \{-12, [3, 3]\} + \% \{20, [3, 2]\} + \% \{-20, [3, 1]\} + \% \{8, [3, 0]\} + \% \{6, [2, 4]\} + \% \{-20, [2, 3]\} + \% \{46, [2, 2]\} + \% \{-40, [2, 1]\} + \% \{24, [2, 0]\} + \% \{4, [1, 4]\} + \% \{-20, [1, 3]\} + \% \{40, [1, 2]\} + \% \{-48, [1, 1]\} + \% \{32, [1, 0]\} + \% \{1, [0, 4]\} + \% \{-8, [0, 3]\} + \% \{24, [0, 2]\} + \% \{-32, [0, 1]\} + \% \{16, [0, 0]\}$] at parameters values $[-2.28782047657, 4.66774101928]$ Warning, choosing root of $[1, 0, \% \{4, [1, 1]\} + \% \{4, [1, 0]\} + \% \{-4, [0, 1]\} + \% \{-8, [0, 0]\}, 0, \% \{6, [2, 2]\} + \% \{4, [2, 1]\} + \% \{6, [2, 0]\} + \% \{-4, [1, 2]\} + \% \{-28, [1, 1]\} + \% \{-8, [1, 0]\} + \% \{6, [0, 2]\} + \% \{8, [0, 1]\} + \% \{24, [0, 0]\}, 0, \% \{4, [3, 3]\} + \% \{-4, [3, 2]\} + \% \{-4, [3, 1]\} + \% \{4, [3, 0]\} + \% \{4, [2, 3]\} + \% \{-64, [2, 2]\} + \% \{20, [2, 1]\} + \% \{8, [2, 0]\} + \% \{-4, [1, 3]\} + \% \{-20, [1, 2]\} + \% \{128, [1, 1]\} + \% \{-16, [1, 0]\} + \% \{-4, [0, 3]\} + \% \{8, [0, 2]\} + \% \{16, [0, 1]\} + \% \{-32, [0, 0]\}, 0, \% \{1, [4, 4]\} + \% \{-4, [4, 3]\} + \% \{6, [4, 2]\} + \% \{-4, [4, 1]\} + \% \{1, [4, 0]\} + \% \{4, [3, 4]\} + \% \{-12, [3, 3]\} + \% \{20, [3, 2]\} + \% \{-20, [3, 1]\} + \% \{8, [3, 0]\} + \% \{6, [2, 4]\} + \% \{-20, [2, 3]\} + \% \{46, [2, 2]\} + \% \{-40, [2, 1]\} + \% \{24, [2, 0]\} + \% \{4, [1, 4]\} + \% \{-20, [1, 3]\} + \% \{40, [1, 2]\} + \% \{-48, [1, 1]\} + \% \{32, [1, 0]\} + \% \{1, [0, 4]\} + \% \{-8, [0, 3]\} + \% \{24, [0, 2]\} + \% \{-32, [0, 1]\} + \% \{16, [0, 0]\}$] at parameters values $[-10.7897139532, 38.2197840363]$ $1/b * (2*b^3*abs(b)/b^2 * (2*(((-90*b^11/1440/b^14*\sqrt{-b*x+2})*\sqrt{-b*x+2}+750*b^11/1440/b^14)*\sqrt{-b*x+2}*\sqrt{-b*x+2}-2445*b^11/1440/b^14)*\sqrt{-b*x+2}*\sqrt{-b*x+2}+4185*b^11/1440/b^14)*\sqrt{-b*x+2}*\sqrt{-b*(-b*x+2)+2*b}-35/8/b^2/\sqrt{-b}*\ln(abs(\sqrt{-b*(-b*x+2)+2*b}-\sqrt{-b}*\sqrt{-b*x+2}))))-12*b^2*abs(b)/b^2*(2*((12*b^5/144/b^7*\sqrt{-b*x+2})*\sqrt{-b*x+2}-78*b^5/144/b^7)*\sqrt{-b*x+2}*\sqrt{-b*x+2}+198*b^5/144/b^7)*\sqrt{-b*x+2}*\sqrt{-b*(-b*x+2)+2*b}-5/2/b/\sqrt{-b}*\ln(abs(\sqrt{-b*(-b*x+2)+2*b}-\sqrt{-b}*\sqrt{-b*x+2}))))-24*b*abs(b)/b^2/b*(2*(1/8*\sqrt{-b*x+2})*\sqrt{-b*x+2}-5/8)*\sqrt{-b*x+2}*\sqrt{-b*(-b*x+2)+2*b}+6*b/4/\sqrt{-b}*\ln(abs(\sqrt{-b*(-b*x+2)+2*b}-\sqrt{-b}*\sqrt{-b*x+2}))))-16*abs(b)/b^2*(1/2*\sqrt{-b*x+2})*\sqrt{-b*(-b*x+2)+2*b}-2*b/2/\sqrt{-b}*\ln(abs(\sqrt{-b*(-b*x+2)+2*b}-\sqrt{-b}*\sqrt{-b*x+2}))))$

sympy [A] time = 8.59, size = 255, normalized size = 2.41

$$\left\{ \begin{array}{l} \frac{ib^3x^{\frac{9}{2}}}{4\sqrt{bx-2}} - \frac{23ib^2x^{\frac{7}{2}}}{12\sqrt{bx-2}} + \frac{127ibx^{\frac{5}{2}}}{24\sqrt{bx-2}} - \frac{133ix^{\frac{3}{2}}}{24\sqrt{bx-2}} + \frac{5i\sqrt{x}}{4b\sqrt{bx-2}} - \frac{5i\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{3}{2}}} \\ -\frac{b^3x^{\frac{9}{2}}}{4\sqrt{-bx+2}} + \frac{23b^2x^{\frac{7}{2}}}{12\sqrt{-bx+2}} - \frac{127bx^{\frac{5}{2}}}{24\sqrt{-bx+2}} + \frac{133x^{\frac{3}{2}}}{24\sqrt{-bx+2}} - \frac{5\sqrt{x}}{4b\sqrt{-bx+2}} + \frac{5\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{4b^{\frac{3}{2}}} \end{array} \right. \begin{array}{l} \text{for } \frac{|bx|}{2} > 1 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)**(5/2)*x**(1/2), x)

[Out] Piecewise((I*b**3*x**(9/2)/(4*sqrt(b*x - 2)) - 23*I*b**2*x**(7/2)/(12*sqrt(b*x - 2)) + 127*I*b*x**(5/2)/(24*sqrt(b*x - 2)) - 133*I*x**(3/2)/(24*sqrt(b*x - 2)) + 5*I*sqrt(x)/(4*b*sqrt(b*x - 2)) - 5*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(3/2)), Abs(b*x)/2 > 1), (-b**3*x**(9/2)/(4*sqrt(-b*x + 2)) + 23*b**2*x**(7/2)/(12*sqrt(-b*x + 2)) - 127*b*x**(5/2)/(24*sqrt(-b*x + 2)) + 133*x**(3/2)/(24*sqrt(-b*x + 2)) - 5*sqrt(x)/(4*b*sqrt(-b*x + 2)) + 5*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/(4*b**(3/2)), True))

$$3.566 \quad \int \frac{(2-bx)^{5/2}}{\sqrt{x}} dx$$

Optimal. Leaf size=82

$$\frac{1}{3}\sqrt{x}(2-bx)^{5/2} + \frac{5}{6}\sqrt{x}(2-bx)^{3/2} + \frac{5}{2}\sqrt{x}\sqrt{2-bx} + \frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

[Out] $5*\arcsin(1/2*b^{(1/2)*x^{(1/2)}*2^{(1/2)})/b^{(1/2)}+5/6*(-b*x+2)^{(3/2)*x^{(1/2)}+1/3*(-b*x+2)^{(5/2)*x^{(1/2)}+5/2*x^{(1/2)}*(-b*x+2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$\frac{1}{3}\sqrt{x}(2-bx)^{5/2} + \frac{5}{6}\sqrt{x}(2-bx)^{3/2} + \frac{5}{2}\sqrt{x}\sqrt{2-bx} + \frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(2 - b*x)^{(5/2)}/\text{Sqrt}[x], x]$

[Out] $(5*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/2 + (5*\text{Sqrt}[x]*(2 - b*x)^{(3/2)})/6 + (\text{Sqrt}[x]*(2 - b*x)^{(5/2)})/3 + (5*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/\text{Sqrt}[b]$

Rule 50

$\text{Int}[(a + b*x)^m * (c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{m+1} * (c + d*x)^n / (b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d)) / (b*(m+n+1)), \text{Int}[(a + b*x)^m * (c + d*x)^{n-1}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m+n+1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m-n, 0]))) && !ILtQ[m+n+2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

$\text{Int}[1/(\text{Sqrt}[a + b*x] * \text{Sqrt}[c + d*x]), x_Symbol] \rightarrow \text{Dist}[2/\text{Sqrt}[b], \text{Subst}[\text{Int}[1/\text{Sqrt}[b*c - a*d + d*x^2], x], x, \text{Sqrt}[a + b*x]], x] /;$ FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

$\text{Int}[1/\text{Sqrt}[a + b*x^2], x_Symbol] \rightarrow \text{Simp}[\text{ArcSin}[(\text{Rt}[-b, 2]*x)/\text{Sqrt}[a]]/\text{Rt}[-b, 2], x] /;$ FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(2-bx)^{5/2}}{\sqrt{x}} dx &= \frac{1}{3} \sqrt{x} (2-bx)^{5/2} + \frac{5}{3} \int \frac{(2-bx)^{3/2}}{\sqrt{x}} dx \\
&= \frac{5}{6} \sqrt{x} (2-bx)^{3/2} + \frac{1}{3} \sqrt{x} (2-bx)^{5/2} + \frac{5}{2} \int \frac{\sqrt{2-bx}}{\sqrt{x}} dx \\
&= \frac{5}{2} \sqrt{x} \sqrt{2-bx} + \frac{5}{6} \sqrt{x} (2-bx)^{3/2} + \frac{1}{3} \sqrt{x} (2-bx)^{5/2} + \frac{5}{2} \int \frac{1}{\sqrt{x} \sqrt{2-bx}} dx \\
&= \frac{5}{2} \sqrt{x} \sqrt{2-bx} + \frac{5}{6} \sqrt{x} (2-bx)^{3/2} + \frac{1}{3} \sqrt{x} (2-bx)^{5/2} + 5 \operatorname{Subst} \left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x} \right) \\
&= \frac{5}{2} \sqrt{x} \sqrt{2-bx} + \frac{5}{6} \sqrt{x} (2-bx)^{3/2} + \frac{1}{3} \sqrt{x} (2-bx)^{5/2} + \frac{5 \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 58, normalized size = 0.71

$$\frac{1}{6} \sqrt{x} \sqrt{2-bx} (2b^2x^2 - 13bx + 33) + \frac{5 \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Integrate[(2 - b*x)^(5/2)/Sqrt[x], x]

[Out] (Sqrt[x]*Sqrt[2 - b*x]*(33 - 13*b*x + 2*b^2*x^2))/6 + (5*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

fricas [A] time = 0.45, size = 125, normalized size = 1.52

$$\left[\frac{(2b^3x^2 - 13b^2x + 33b)\sqrt{-bx + 2}\sqrt{x} - 15\sqrt{-b} \log(-bx + \sqrt{-bx + 2}\sqrt{-b}\sqrt{x} + 1)}{6b}, \frac{(2b^3x^2 - 13b^2x + 33b)\sqrt{-bx + 2}\sqrt{x} - 15\sqrt{-b} \log(-bx + \sqrt{-bx + 2}\sqrt{-b}\sqrt{x} + 1)}{6b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(5/2)/x^(1/2), x, algorithm="fricas")

[Out] [1/6*((2*b^3*x^2 - 13*b^2*x + 33*b)*sqrt(-b*x + 2)*sqrt(x) - 15*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b, 1/6*((2*b^3*x^2 - 13*b^2*x + 33*b)*sqrt(-b*x + 2)*sqrt(x) - 30*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))))/b]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)^(5/2)/x^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-15.6438432182,61.7937478349]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-29.292030761,78.6493344628]1/abs(b)*b^2/b*(2*((1/6/b*sqrt(-b*x+2)*sqrt(-b*x+2)+5/12/b)*sqrt(-b*x+2)*sqrt(-b*x+2)+5/4/b)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)+5/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b)-sqrt(-b)*sqrt(-b*x+2))))

maple [A] time = 0.00, size = 91, normalized size = 1.11

$$\frac{(-bx+2)^{\frac{5}{2}}\sqrt{x}}{3} + \frac{5(-bx+2)^{\frac{3}{2}}\sqrt{x}}{6} + \frac{5\sqrt{-bx+2}\sqrt{x}}{2} + \frac{5\sqrt{(-bx+2)x}\arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{2\sqrt{-bx+2}\sqrt{b}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-b*x+2)^(5/2)/x^(1/2), x)`

[Out] $\frac{1}{3}(-b*x+2)^{5/2}*x^{1/2}+5/6*(-b*x+2)^{3/2}*x^{1/2}+5/2*(-b*x+2)^{1/2}*x^{1/2}+5/2*((-b*x+2)*x)^{1/2}/(-b*x+2)^{1/2}/b^{1/2}/x^{1/2}*\arctan((x-1/b)/(-b*x^2+2*x))^{1/2}*b^{1/2}$

maxima [A] time = 2.98, size = 112, normalized size = 1.37

$$-\frac{5 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{b}} + \frac{\frac{15\sqrt{-bx+2}b^2}{\sqrt{x}} + \frac{40(-bx+2)^{\frac{3}{2}}b}{x^{\frac{3}{2}}} + \frac{33(-bx+2)^{\frac{5}{2}}}{x^{\frac{5}{2}}}}{3\left(b^3 - \frac{3(bx-2)b^2}{x} + \frac{3(bx-2)^2b}{x^2} - \frac{(bx-2)^3}{x^3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+2)^(5/2)/x^(1/2), x, algorithm="maxima")`

[Out] $-5*\arctan(\sqrt{-b*x + 2}/(\sqrt{b}*\sqrt{x}))/\sqrt{b} + 1/3*(15*\sqrt{-b*x + 2})*b^2/\sqrt{x} + 40*(-b*x + 2)^{3/2}*b/x^{3/2} + 33*(-b*x + 2)^{5/2}/x^{5/2})/(b^3 - 3*(b*x - 2)*b^2/x + 3*(b*x - 2)^2*b/x^2 - (b*x - 2)^3/x^3)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(2 - bx)^{5/2}}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((2 - b*x)^(5/2)/x^(1/2), x)`

[Out] `int((2 - b*x)^(5/2)/x^(1/2), x)`

sympy [A] time = 5.52, size = 209, normalized size = 2.55

$$\begin{cases} \frac{ib^3x^{\frac{7}{2}}}{3\sqrt{bx-2}} - \frac{17ib^2x^{\frac{5}{2}}}{6\sqrt{bx-2}} + \frac{59ibx^{\frac{3}{2}}}{6\sqrt{bx-2}} - \frac{11i\sqrt{x}}{\sqrt{bx-2}} - \frac{5i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}} & \text{for } \frac{|bx|}{2} > 1 \\ -\frac{b^3x^{\frac{7}{2}}}{3\sqrt{-bx+2}} + \frac{17b^2x^{\frac{5}{2}}}{6\sqrt{-bx+2}} - \frac{59bx^{\frac{3}{2}}}{6\sqrt{-bx+2}} + \frac{11\sqrt{x}}{\sqrt{-bx+2}} + \frac{5 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+2)**(5/2)/x**(1/2), x)`

```
[Out] Piecewise((I*b**3*x**(7/2)/(3*sqrt(b*x - 2)) - 17*I*b**2*x**(5/2)/(6*sqrt(b
*x - 2)) + 59*I*b*x**(3/2)/(6*sqrt(b*x - 2)) - 11*I*sqrt(x)/sqrt(b*x - 2) -
5*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/sqrt(b), Abs(b*x)/2 > 1), (-b**3*x**(
7/2)/(3*sqrt(-b*x + 2)) + 17*b**2*x**(5/2)/(6*sqrt(-b*x + 2)) - 59*b*x**(3/
2)/(6*sqrt(-b*x + 2)) + 11*sqrt(x)/sqrt(-b*x + 2) + 5*asin(sqrt(2)*sqrt(b)*
sqrt(x)/2)/sqrt(b), True))
```

$$3.567 \quad \int \frac{(2-bx)^{5/2}}{x^{3/2}} dx$$

Optimal. Leaf size=82

$$-\frac{2(2-bx)^{5/2}}{\sqrt{x}} - \frac{5}{2}b\sqrt{x}(2-bx)^{3/2} - \frac{15}{2}b\sqrt{x}\sqrt{2-bx} - 15\sqrt{b} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)$$

[Out] $-15*\arcsin(1/2*b^{(1/2)*x^{(1/2)}*2^{(1/2)})*b^{(1/2)}-2*(-b*x+2)^{(5/2)}/x^{(1/2)}-5/2*b*(-b*x+2)^{(3/2)*x^{(1/2)}}-15/2*b*x^{(1/2)}*(-b*x+2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {47, 50, 54, 216}

$$-\frac{2(2-bx)^{5/2}}{\sqrt{x}} - \frac{5}{2}b\sqrt{x}(2-bx)^{3/2} - \frac{15}{2}b\sqrt{x}\sqrt{2-bx} - 15\sqrt{b} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Int[(2 - b*x)^(5/2)/x^(3/2), x]

[Out] $(-15*b*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/2 - (5*b*\text{Sqrt}[x]*(2 - b*x)^{(3/2)})/2 - (2*(2 - b*x)^{(5/2)})/\text{Sqrt}[x] - 15*\text{Sqrt}[b]*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(2-bx)^{5/2}}{x^{3/2}} dx &= -\frac{2(2-bx)^{5/2}}{\sqrt{x}} - (5b) \int \frac{(2-bx)^{3/2}}{\sqrt{x}} dx \\
&= -\frac{5}{2}b\sqrt{x}(2-bx)^{3/2} - \frac{2(2-bx)^{5/2}}{\sqrt{x}} - \frac{1}{2}(15b) \int \frac{\sqrt{2-bx}}{\sqrt{x}} dx \\
&= -\frac{15}{2}b\sqrt{x}\sqrt{2-bx} - \frac{5}{2}b\sqrt{x}(2-bx)^{3/2} - \frac{2(2-bx)^{5/2}}{\sqrt{x}} - \frac{1}{2}(15b) \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx \\
&= -\frac{15}{2}b\sqrt{x}\sqrt{2-bx} - \frac{5}{2}b\sqrt{x}(2-bx)^{3/2} - \frac{2(2-bx)^{5/2}}{\sqrt{x}} - (15b) \text{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right) \\
&= -\frac{15}{2}b\sqrt{x}\sqrt{2-bx} - \frac{5}{2}b\sqrt{x}(2-bx)^{3/2} - \frac{2(2-bx)^{5/2}}{\sqrt{x}} - 15\sqrt{b} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 28, normalized size = 0.34

$$\frac{8\sqrt{2} {}_2F_1\left(-\frac{5}{2}, -\frac{1}{2}; \frac{1}{2}; \frac{bx}{2}\right)}{\sqrt{x}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(2 - b*x)^(5/2)/x^(3/2), x]
```

```
[Out] (-8*Sqrt[2]*Hypergeometric2F1[-5/2, -1/2, 1/2, (b*x)/2])/Sqrt[x]
```

fricas [A] time = 0.48, size = 117, normalized size = 1.43

$$\left[\frac{15\sqrt{-b}x \log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1) + (b^2x^2 - 9bx - 16)\sqrt{-bx+2}\sqrt{x}}{2x}, \frac{30\sqrt{b}x \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) + (b^2x^2 - 9bx - 16)\sqrt{-bx+2}\sqrt{x}}{2x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((-b*x+2)^(5/2)/x^(3/2),x, algorithm="fricas")
```

```
[Out] [1/2*(15*sqrt(-b)*x*log(-b*x + sqrt(-b*x + 2))*sqrt(-b)*sqrt(x) + 1) + (b^2*x^2 - 9*b*x - 16)*sqrt(-b*x + 2)*sqrt(x))/x, 1/2*(30*sqrt(b)*x*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) + (b^2*x^2 - 9*b*x - 16)*sqrt(-b*x + 2)*sqrt(x))/x]
```

```
giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00
```

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((-b*x+2)^(5/2)/x^(3/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-15.6438432182,61.7937478349]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-29.292030761,78.6493344628]-b/abs(b)*b^2/b*(2*((-5/4-1/4*sqrt(-b*x+2))*sqrt(-b*x+2))*sqrt(-b*x+2)*sqrt(-b*x+2)+15/2)*sqrt(-b*x+2)*sqrt
```


$(-b*(-b*x+2)+2*b)/(-b*(-b*x+2)+2*b)+15/\text{sqrt}(-b)*\ln(\text{abs}(\text{sqrt}(-b*(-b*x+2)+2*b)-\text{sqrt}(-b)*\text{sqrt}(-b*x+2))))$

maple [A] time = 0.02, size = 106, normalized size = 1.29

$$\frac{15\sqrt{-bx+2}x\sqrt{b}\arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{2\sqrt{-bx+2}\sqrt{x}} - \frac{(b^3x^3 - 11b^2x^2 + 2bx + 32)\sqrt{-bx+2}x}{2\sqrt{-(bx-2)}x\sqrt{-bx+2}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((-b*x+2)^{(5/2)}/x^{(3/2)}, x)$

[Out] $-1/2*(b^3*x^3-11*b^2*x^2+2*b*x+32)/(-(b*x-2)*x)^{(1/2)}*((-b*x+2)*x)^{(1/2)}/(-b*x+2)^{(1/2)}/x^{(1/2)}-15/2*((-b*x+2)*x)^{(1/2)}/(-b*x+2)^{(1/2)}*b^{(1/2)}/x^{(1/2)}$
 $*\arctan((x-1/b)/(-b*x^2+2*x)^{(1/2)}*b^{(1/2)})$

maxima [A] time = 2.92, size = 96, normalized size = 1.17

$$15\sqrt{b}\arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) - \frac{\frac{7\sqrt{-bx+2}b^2}{\sqrt{x}} + \frac{9(-bx+2)^{\frac{3}{2}}b}{x^{\frac{3}{2}}}}{b^2 - \frac{2(bx-2)b}{x} + \frac{(bx-2)^2}{x^2}} - \frac{8\sqrt{-bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((-b*x+2)^{(5/2)}/x^{(3/2)}, x, \text{algorithm}="maxima")$

[Out] $15*\text{sqrt}(b)*\arctan(\text{sqrt}(-b*x + 2)/(\text{sqrt}(b)*\text{sqrt}(x))) - (7*\text{sqrt}(-b*x + 2)*b^2/\text{sqrt}(x) + 9*(-b*x + 2)^{(3/2)}*b/x^{(3/2)})/(b^2 - 2*(b*x - 2)*b/x + (b*x - 2)^2/x^2) - 8*\text{sqrt}(-b*x + 2)/\text{sqrt}(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(2 - bx)^{5/2}}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((2 - b*x)^{(5/2)}/x^{(3/2)}, x)$

[Out] $\text{int}((2 - b*x)^{(5/2)}/x^{(3/2)}, x)$

sympy [A] time = 5.62, size = 202, normalized size = 2.46

$$\begin{cases} 15i\sqrt{b} \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right) + \frac{ib^3x^{\frac{5}{2}}}{2\sqrt{bx-2}} - \frac{11ib^2x^{\frac{3}{2}}}{2\sqrt{bx-2}} + \frac{ib\sqrt{x}}{\sqrt{bx-2}} + \frac{16i}{\sqrt{x}\sqrt{bx-2}} & \text{for } \frac{|bx|}{2} > 1 \\ -15\sqrt{b} \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right) - \frac{b^3x^{\frac{5}{2}}}{2\sqrt{-bx+2}} + \frac{11b^2x^{\frac{3}{2}}}{2\sqrt{-bx+2}} - \frac{b\sqrt{x}}{\sqrt{-bx+2}} - \frac{16}{\sqrt{x}\sqrt{-bx+2}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)**(5/2)/x**(3/2),x)

[Out] Piecewise((15*I*sqrt(b)*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2) + I*b**3*x**(5/2)/(2*sqrt(b*x - 2)) - 11*I*b**2*x**(3/2)/(2*sqrt(b*x - 2)) + I*b*sqrt(x)/sqrt(b*x - 2) + 16*I/(sqrt(x)*sqrt(b*x - 2)), Abs(b*x)/2 > 1), (-15*sqrt(b)*asin(sqrt(2)*sqrt(b)*sqrt(x)/2) - b**3*x**(5/2)/(2*sqrt(-b*x + 2)) + 11*b**2*x**(3/2)/(2*sqrt(-b*x + 2)) - b*sqrt(x)/sqrt(-b*x + 2) - 16/(sqrt(x)*sqrt(-b*x + 2)), True))

$$3.568 \quad \int \frac{(2-bx)^{5/2}}{x^{5/2}} dx$$

Optimal. Leaf size=84

$$10b^{3/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right) + 5b^2\sqrt{x}\sqrt{2-bx} - \frac{2(2-bx)^{5/2}}{3x^{3/2}} + \frac{10b(2-bx)^{3/2}}{3\sqrt{x}}$$

[Out] $-2/3*(-b*x+2)^{(5/2)}/x^{(3/2)}+10*b^{(3/2)}*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})+10/3*b*(-b*x+2)^{(3/2)}/x^{(1/2)}+5*b^2*x^{(1/2)}*(-b*x+2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {47, 50, 54, 216}

$$5b^2\sqrt{x}\sqrt{2-bx} + 10b^{3/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right) - \frac{2(2-bx)^{5/2}}{3x^{3/2}} + \frac{10b(2-bx)^{3/2}}{3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[(2 - b*x)^(5/2)/x^(5/2), x]

[Out] $5*b^2*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x] + (10*b*(2 - b*x)^{(3/2)})/(3*\text{Sqrt}[x]) - (2*(2 - b*x)^{(5/2)})/(3*x^{(3/2)}) + 10*b^{(3/2)}*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]]$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(2-bx)^{5/2}}{x^{5/2}} dx &= -\frac{2(2-bx)^{5/2}}{3x^{3/2}} - \frac{1}{3}(5b) \int \frac{(2-bx)^{3/2}}{x^{3/2}} dx \\
&= \frac{10b(2-bx)^{3/2}}{3\sqrt{x}} - \frac{2(2-bx)^{5/2}}{3x^{3/2}} + (5b^2) \int \frac{\sqrt{2-bx}}{\sqrt{x}} dx \\
&= 5b^2\sqrt{x}\sqrt{2-bx} + \frac{10b(2-bx)^{3/2}}{3\sqrt{x}} - \frac{2(2-bx)^{5/2}}{3x^{3/2}} + (5b^2) \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx \\
&= 5b^2\sqrt{x}\sqrt{2-bx} + \frac{10b(2-bx)^{3/2}}{3\sqrt{x}} - \frac{2(2-bx)^{5/2}}{3x^{3/2}} + (10b^2) \text{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right) \\
&= 5b^2\sqrt{x}\sqrt{2-bx} + \frac{10b(2-bx)^{3/2}}{3\sqrt{x}} - \frac{2(2-bx)^{5/2}}{3x^{3/2}} + 10b^{3/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.36

$$-\frac{8\sqrt{2} {}_2F_1\left(-\frac{5}{2}, -\frac{3}{2}; -\frac{1}{2}; \frac{bx}{2}\right)}{3x^{3/2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(2 - b*x)^(5/2)/x^(5/2), x]
```

```
[Out] (-8*Sqrt[2]*Hypergeometric2F1[-5/2, -3/2, -1/2, (b*x)/2])/(3*x^(3/2))
```

fricas [A] time = 0.44, size = 126, normalized size = 1.50

$$\left[\frac{15\sqrt{-b}bx^2 \log(-bx - \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1) + (3b^2x^2 + 28bx - 8)\sqrt{-bx+2}\sqrt{x}}{3x^2}, -\frac{30b^{\frac{3}{2}}x^2 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{b}\sqrt{x}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((-b*x+2)^(5/2)/x^(5/2),x, algorithm="fricas")
```

```
[Out] [1/3*(15*sqrt(-b)*b*x^2*log(-b*x - sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1) + (
3*b^2*x^2 + 28*b*x - 8)*sqrt(-b*x + 2)*sqrt(x))/x^2, -1/3*(30*b^(3/2)*x^2*a
rctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) - (3*b^2*x^2 + 28*b*x - 8)*sqrt(-b*
x + 2)*sqrt(x))/x^2]
```

```
giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00
```

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((-b*x+2)^(5/2)/x^(5/2),x, algorithm="giac")
```

```
[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warni
ng, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+
%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[
1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}
+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4
,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%
}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%
{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,
[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}
+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8
,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]
%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%
{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0
,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-15.64384
32182,61.7937478349]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1
,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}
+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,
[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%
}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{2
0,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1
]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%
{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,
[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%
}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{4
6,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3
]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%
{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at par
ameters values [-29.292030761,78.6493344628]1/abs(b)*b^2/b*(2*((9*b^4/18/b*
sqrt(-b*x+2)*sqrt(-b*x+2)-120*b^4/18/b)*sqrt(-b*x+2)*sqrt(-b*x+2)+180*b^4/1
```

$8/b) \cdot \sqrt{-bx+2} \cdot \sqrt{-b(-bx+2)+2b} / (-b(-bx+2)+2b)^2 + 10b^2 / \sqrt{-b} \cdot \ln(\text{abs}(\sqrt{-b(-bx+2)+2b} - \sqrt{-b} \cdot \sqrt{-bx+2}))$

maple [A] time = 0.02, size = 107, normalized size = 1.27

$$\frac{5\sqrt{-bx+2} x b^{\frac{3}{2}} \arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{\sqrt{-bx+2} \sqrt{x}} - \frac{(3b^3x^3 + 22b^2x^2 - 64bx + 16) \sqrt{-bx+2} x}{3\sqrt{-(bx-2)x} \sqrt{-bx+2} x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-b*x+2)^(5/2)/x^(5/2), x)`

[Out] $-1/3 \cdot (3b^3x^3 + 22b^2x^2 - 64bx + 16) / x^{3/2} / (-(bx-2)x)^{1/2} \cdot ((-bx+2)x)^{1/2} / (-bx+2)^{1/2} + 5 \cdot ((-bx+2)x)^{1/2} / (-bx+2)^{1/2} \cdot b^{3/2} / x^{1/2} \cdot \arctan((x-1/b) / (-bx^2+2x)^{1/2} \cdot b^{1/2})$

maxima [A] time = 2.89, size = 79, normalized size = 0.94

$$-10b^{\frac{3}{2}} \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) + \frac{8\sqrt{-bx+2}b}{\sqrt{x}} + \frac{2\sqrt{-bx+2}b^2}{\left(b - \frac{bx-2}{x}\right)\sqrt{x}} - \frac{4(-bx+2)^{\frac{3}{2}}}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*x+2)^(5/2)/x^(5/2), x, algorithm="maxima")`

[Out] $-10b^{3/2} \cdot \arctan(\sqrt{-bx+2} / (\sqrt{b} \cdot \sqrt{x})) + 8 \cdot \sqrt{-bx+2} \cdot b / \sqrt{x} + 2 \cdot \sqrt{-bx+2} \cdot b^2 / \left(b - \frac{bx-2}{x}\right) \cdot \sqrt{x} - 4/3 \cdot (-bx+2)^{3/2} / x^{3/2}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(2-bx)^{5/2}}{x^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((2 - b*x)^(5/2)/x^(5/2), x)`

[Out] `int((2 - b*x)^(5/2)/x^(5/2), x)`

sympy [C] time = 5.35, size = 221, normalized size = 2.63

$$\left\{ \begin{array}{l} b^{\frac{5}{2}} x \sqrt{-1 + \frac{2}{bx}} + \frac{28b^{\frac{3}{2}} \sqrt{-1 + \frac{2}{bx}}}{3} + 5ib^{\frac{3}{2}} \log\left(\frac{1}{bx}\right) - 10ib^{\frac{3}{2}} \log\left(\frac{1}{\sqrt{b}\sqrt{x}}\right) + 10b^{\frac{3}{2}} \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right) - \frac{8\sqrt{b}\sqrt{-1 + \frac{2}{bx}}}{3x} \\ ib^{\frac{5}{2}} x \sqrt{1 - \frac{2}{bx}} + \frac{28ib^{\frac{3}{2}} \sqrt{1 - \frac{2}{bx}}}{3} + 5ib^{\frac{3}{2}} \log\left(\frac{1}{bx}\right) - 10ib^{\frac{3}{2}} \log\left(\sqrt{1 - \frac{2}{bx}} + 1\right) - \frac{8i\sqrt{b}\sqrt{1 - \frac{2}{bx}}}{3x} \end{array} \right. \begin{array}{l} \text{for } \frac{2}{|b|} < 1 \\ \text{other} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*x+2)**(5/2)/x**(5/2),x)

[Out] Piecewise((b**(5/2)*x*sqrt(-1 + 2/(b*x)) + 28*b**(3/2)*sqrt(-1 + 2/(b*x))/3 + 5*I*b**(3/2)*log(1/(b*x)) - 10*I*b**(3/2)*log(1/(sqrt(b)*sqrt(x))) + 10*b**(3/2)*asin(sqrt(2)*sqrt(b)*sqrt(x)/2) - 8*sqrt(b)*sqrt(-1 + 2/(b*x))/(3*x), 2/Abs(b*x) > 1), (I*b**(5/2)*x*sqrt(1 - 2/(b*x)) + 28*I*b**(3/2)*sqrt(1 - 2/(b*x))/3 + 5*I*b**(3/2)*log(1/(b*x)) - 10*I*b**(3/2)*log(sqrt(1 - 2/(b*x)) + 1) - 8*I*sqrt(b)*sqrt(1 - 2/(b*x))/(3*x), True))

$$3.569 \quad \int \frac{x^{5/2}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=101

$$-\frac{5a^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{8b^{7/2}} + \frac{5a^2\sqrt{x}\sqrt{a+bx}}{8b^3} - \frac{5ax^{3/2}\sqrt{a+bx}}{12b^2} + \frac{x^{5/2}\sqrt{a+bx}}{3b}$$

[Out] $-5/8*a^3*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(7/2)}-5/12*a*x^{(3/2)}*(b*x+a)^{(1/2)}/b^2+1/3*x^{(5/2)}*(b*x+a)^{(1/2)}/b+5/8*a^2*x^{(1/2)}*(b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.03, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$\frac{5a^2\sqrt{x}\sqrt{a+bx}}{8b^3} - \frac{5a^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{8b^{7/2}} - \frac{5ax^{3/2}\sqrt{a+bx}}{12b^2} + \frac{x^{5/2}\sqrt{a+bx}}{3b}$$

Antiderivative was successfully verified.

[In] `Int[x^(5/2)/Sqrt[a + b*x], x]`

[Out] $(5*a^2*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(8*b^3) - (5*a*x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/(12*b^2) + (x^{(5/2)}*\operatorname{Sqrt}[a + b*x])/(3*b) - (5*a^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(8*b^{(7/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{x^{5/2}}{\sqrt{a+bx}} dx &= \frac{x^{5/2}\sqrt{a+bx}}{3b} - \frac{(5a) \int \frac{x^{3/2}}{\sqrt{a+bx}} dx}{6b} \\
 &= -\frac{5ax^{3/2}\sqrt{a+bx}}{12b^2} + \frac{x^{5/2}\sqrt{a+bx}}{3b} + \frac{(5a^2) \int \frac{\sqrt{x}}{\sqrt{a+bx}} dx}{8b^2} \\
 &= \frac{5a^2\sqrt{x}\sqrt{a+bx}}{8b^3} - \frac{5ax^{3/2}\sqrt{a+bx}}{12b^2} + \frac{x^{5/2}\sqrt{a+bx}}{3b} - \frac{(5a^3) \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx}{16b^3} \\
 &= \frac{5a^2\sqrt{x}\sqrt{a+bx}}{8b^3} - \frac{5ax^{3/2}\sqrt{a+bx}}{12b^2} + \frac{x^{5/2}\sqrt{a+bx}}{3b} - \frac{(5a^3) \text{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right)}{8b^3} \\
 &= \frac{5a^2\sqrt{x}\sqrt{a+bx}}{8b^3} - \frac{5ax^{3/2}\sqrt{a+bx}}{12b^2} + \frac{x^{5/2}\sqrt{a+bx}}{3b} - \frac{(5a^3) \text{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right)}{8b^3} \\
 &= \frac{5a^2\sqrt{x}\sqrt{a+bx}}{8b^3} - \frac{5ax^{3/2}\sqrt{a+bx}}{12b^2} + \frac{x^{5/2}\sqrt{a+bx}}{3b} - \frac{5a^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{8b^{7/2}}
 \end{aligned}$$

Mathematica [A] time = 0.16, size = 85, normalized size = 0.84

$$\frac{\sqrt{a+bx} \left(\sqrt{b}\sqrt{x} (15a^2 - 10abx + 8b^2x^2) - \frac{15a^{5/2} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{\frac{bx}{a}+1}} \right)}{24b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/Sqrt[a + b*x], x]

[Out] (Sqrt[a + b*x]*(Sqrt[b]*Sqrt[x]*(15*a^2 - 10*a*b*x + 8*b^2*x^2) - (15*a^(5/2)*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]]/Sqrt[1 + (b*x)/a]))/(24*b^(7/2))

fricas [A] time = 0.45, size = 140, normalized size = 1.39

$$\left[\frac{15 a^3 \sqrt{b} \log(2 b x - 2 \sqrt{b x + a} \sqrt{b} \sqrt{x} + a) + 2 (8 b^3 x^2 - 10 a b^2 x + 15 a^2 b) \sqrt{b x + a} \sqrt{x}}{48 b^4}, \frac{15 a^3 \sqrt{-b} \arctan\left(\frac{\sqrt{b x + a}}{b \sqrt{x}}\right)}{b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [1/48*(15*a^3*sqrt(b)*log(2*b*x - 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(8*b^3*x^2 - 10*a*b^2*x + 15*a^2*b)*sqrt(b*x + a)*sqrt(x))/b^4, 1/24*(15*a^3*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) + (8*b^3*x^2 - 10*a*b^2*x + 15*a^2*b)*sqrt(b*x + a)*sqrt(x))/b^4]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 102, normalized size = 1.01

$$\frac{\sqrt{b x + a} x^{\frac{5}{2}}}{3 b} - \frac{5 \sqrt{b x + a} a x^{\frac{3}{2}}}{12 b^2} - \frac{5 \sqrt{b x + a} x a^3 \ln\left(\frac{b x + \frac{a}{2}}{\sqrt{b}} + \sqrt{b x^2 + a x}\right)}{16 \sqrt{b x + a} b^{\frac{7}{2}} \sqrt{x}} + \frac{5 \sqrt{b x + a} a^2 \sqrt{x}}{8 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x+a)^(1/2),x)

[Out] 1/3*x^(5/2)*(b*x+a)^(1/2)/b-5/12*a*x^(3/2)*(b*x+a)^(1/2)/b^2+5/8*a^2*x^(1/2)*(b*x+a)^(1/2)/b^3-5/16*a^3/b^(7/2)*((b*x+a)*x)^(1/2)/x^(1/2)/(b*x+a)^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))

maxima [A] time = 3.01, size = 146, normalized size = 1.45

$$\frac{5 a^3 \log\left(-\frac{\sqrt{b}-\sqrt{b x+a}}{\sqrt{x}}\right)}{16 b^{\frac{7}{2}}}-\frac{\frac{33 \sqrt{b x+a} a^3 b^2}{\sqrt{x}}-\frac{40(b x+a)^{\frac{3}{2}} a^3 b}{x^{\frac{3}{2}}}+\frac{15(b x+a)^{\frac{5}{2}} a^3}{x^{\frac{5}{2}}}}{24\left(b^6-\frac{3(b x+a) b^5}{x}+\frac{3(b x+a)^2 b^4}{x^2}-\frac{(b x+a)^3 b^3}{x^3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] $\frac{5}{16}a^3 \log\left(\frac{-\sqrt{b} - \sqrt{bx+a}}{\sqrt{x}}\right) / (\sqrt{b} + \sqrt{bx+a}) / \sqrt{x} - \frac{1}{24} \left(\frac{33\sqrt{bx+a} a^3 b^2}{\sqrt{x}} - 40(bx+a)^{3/2} a^3 b / x^{3/2} + 15(bx+a)^{5/2} a^3 / x^{5/2} \right) / (b^6 - 3(bx+a)b^5/x + 3(bx+a)^2 b^4/x^2 - (bx+a)^3 b^3/x^3)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(a + b*x)^(1/2),x)

[Out] int(x^(5/2)/(a + b*x)^(1/2), x)

sympy [A] time = 8.52, size = 128, normalized size = 1.27

$$\frac{5a^{\frac{5}{2}}\sqrt{x}}{8b^3\sqrt{1+\frac{bx}{a}}} + \frac{5a^{\frac{3}{2}}x^{\frac{3}{2}}}{24b^2\sqrt{1+\frac{bx}{a}}} - \frac{\sqrt{a}x^{\frac{5}{2}}}{12b\sqrt{1+\frac{bx}{a}}} - \frac{5a^3 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8b^{\frac{7}{2}}} + \frac{x^{\frac{7}{2}}}{3\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(b*x+a)**(1/2),x)

[Out] $5a^{5/2}\sqrt{x}/(8b^3\sqrt{1+bx/a}) + 5a^{3/2}x^{3/2}/(24b^2\sqrt{1+bx/a}) - \sqrt{a}x^{5/2}/(12b\sqrt{1+bx/a}) - 5a^3\operatorname{asinh}(\sqrt{b}\sqrt{x}/\sqrt{a})/(8b^{7/2}) + x^{7/2}/(3\sqrt{a}\sqrt{1+bx/a})$

$$3.570 \quad \int \frac{x^{3/2}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=77

$$\frac{3a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^{5/2}} - \frac{3a\sqrt{x}\sqrt{a+bx}}{4b^2} + \frac{x^{3/2}\sqrt{a+bx}}{2b}$$

[Out] $3/4*a^2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(5/2)}+1/2*x^{(3/2)}*(b*x+a)^{(1/2)}/b-3/4*a*x^{(1/2)}*(b*x+a)^{(1/2)}/b^2$

Rubi [A] time = 0.02, antiderivative size = 77, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$\frac{3a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^{5/2}} - \frac{3a\sqrt{x}\sqrt{a+bx}}{4b^2} + \frac{x^{3/2}\sqrt{a+bx}}{2b}$$

Antiderivative was successfully verified.

[In] `Int[x^(3/2)/Sqrt[a + b*x], x]`

[Out] $(-3*a*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(4*b^2) + (x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/(2*b) + (3*a^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(4*b^{(5/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{x^{3/2}}{\sqrt{a+bx}} dx &= \frac{x^{3/2}\sqrt{a+bx}}{2b} - \frac{(3a) \int \frac{\sqrt{x}}{\sqrt{a+bx}} dx}{4b} \\
 &= -\frac{3a\sqrt{x}\sqrt{a+bx}}{4b^2} + \frac{x^{3/2}\sqrt{a+bx}}{2b} + \frac{(3a^2) \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx}{8b^2} \\
 &= -\frac{3a\sqrt{x}\sqrt{a+bx}}{4b^2} + \frac{x^{3/2}\sqrt{a+bx}}{2b} + \frac{(3a^2) \text{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right)}{4b^2} \\
 &= -\frac{3a\sqrt{x}\sqrt{a+bx}}{4b^2} + \frac{x^{3/2}\sqrt{a+bx}}{2b} + \frac{(3a^2) \text{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^2} \\
 &= -\frac{3a\sqrt{x}\sqrt{a+bx}}{4b^2} + \frac{x^{3/2}\sqrt{a+bx}}{2b} + \frac{3a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.05, size = 85, normalized size = 1.10

$$\frac{3a^{5/2}\sqrt{\frac{bx}{a}+1} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) + \sqrt{b}\sqrt{x}(-3a^2 - abx + 2b^2x^2)}{4b^{5/2}\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/Sqrt[a + b*x], x]

[Out] (Sqrt[b]*Sqrt[x]*(-3*a^2 - a*b*x + 2*b^2*x^2) + 3*a^(5/2)*Sqrt[1 + (b*x)/a]*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(4*b^(5/2)*Sqrt[a + b*x])

fricas [A] time = 0.45, size = 119, normalized size = 1.55

$$\left[\frac{3a^2\sqrt{b} \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(2b^2x - 3ab)\sqrt{bx+a}\sqrt{x}}{8b^3}, -\frac{3a^2\sqrt{-b} \arctan\left(\frac{\sqrt{bx+a}\sqrt{-b}}{b\sqrt{x}}\right) - (2b}{4b^3} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [1/8*(3*a^2*sqrt(b)*log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(2*b^2*x - 3*a*b)*sqrt(b*x + a)*sqrt(x))/b^3, -1/4*(3*a^2*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) - (2*b^2*x - 3*a*b)*sqrt(b*x + a)*sqrt(x))/b^3]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 84, normalized size = 1.09

$$\frac{\sqrt{bx+a} x^{\frac{3}{2}}}{2b} + \frac{3\sqrt{(bx+a)x} a^2 \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{8\sqrt{bx+a} b^{\frac{5}{2}} \sqrt{x}} - \frac{3\sqrt{bx+a} a \sqrt{x}}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(b*x+a)^(1/2),x)

[Out] 1/2*x^(3/2)*(b*x+a)^(1/2)/b-3/4*a*x^(1/2)*(b*x+a)^(1/2)/b^2+3/8*a^2/b^(5/2)*((b*x+a)*x)^(1/2)/x^(1/2)/(b*x+a)^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))

maxima [B] time = 2.87, size = 112, normalized size = 1.45

$$-\frac{3a^2 \log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+a}}{\sqrt{x}}}\right)}{8b^{\frac{5}{2}}} + \frac{\frac{5\sqrt{bx+a}a^2b}{\sqrt{x}} - \frac{3(bx+a)^{\frac{3}{2}}a^2}{x^{\frac{3}{2}}}}{4\left(b^4 - \frac{2(bx+a)b^3}{x} + \frac{(bx+a)^2b^2}{x^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] -3/8*a^2*log(-sqrt(b) - sqrt(b*x + a)/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x))/b^(5/2) + 1/4*(5*sqrt(b*x + a)*a^2*b/sqrt(x) - 3*(b*x + a)^(3/2)*a^2/x^(3/2))/(b^4 - 2*(b*x + a)*b^3/x + (b*x + a)^2*b^2/x^2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{3/2}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(a + b*x)^(1/2), x)`

[Out] `int(x^(3/2)/(a + b*x)^(1/2), x)`

sympy [A] time = 4.30, size = 100, normalized size = 1.30

$$-\frac{3a^{\frac{3}{2}}\sqrt{x}}{4b^2\sqrt{1+\frac{bx}{a}}} - \frac{\sqrt{a}x^{\frac{3}{2}}}{4b\sqrt{1+\frac{bx}{a}}} + \frac{3a^2 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{\frac{5}{2}}} + \frac{x^{\frac{5}{2}}}{2\sqrt{a}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(b*x+a)**(1/2), x)`

[Out] `-3*a**(3/2)*sqrt(x)/(4*b**2*sqrt(1 + b*x/a)) - sqrt(a)*x**(3/2)/(4*b*sqrt(1 + b*x/a)) + 3*a**2*asinh(sqrt(b)*sqrt(x)/sqrt(a))/(4*b**(5/2)) + x**(5/2)/(2*sqrt(a)*sqrt(1 + b*x/a))`

$$3.571 \quad \int \frac{\sqrt{x}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=48

$$\frac{\sqrt{x} \sqrt{a+bx}}{b} - \frac{a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{3/2}}$$

[Out] $-a \operatorname{arctanh}(b^{1/2} x^{1/2} / (b x + a)^{1/2}) / b^{3/2} + x^{1/2} (b x + a)^{1/2} / b$

Rubi [A] time = 0.02, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 63, 217, 206}

$$\frac{\sqrt{x} \sqrt{a+bx}}{b} - \frac{a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/Sqrt[a + b*x], x]

[Out] (Sqrt[x]*Sqrt[a + b*x])/b - (a*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a + b*x]])/b^(3/2)

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[Rt[-b, 2]*x]/
Rt[a, 2])]/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && Gt
```


Q[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{x}}{\sqrt{a+bx}} dx &= \frac{\sqrt{x}\sqrt{a+bx}}{b} - \frac{a \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx}{2b} \\ &= \frac{\sqrt{x}\sqrt{a+bx}}{b} - \frac{a \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right)}{b} \\ &= \frac{\sqrt{x}\sqrt{a+bx}}{b} - \frac{a \operatorname{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right)}{b} \\ &= \frac{\sqrt{x}\sqrt{a+bx}}{b} - \frac{a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.04, size = 68, normalized size = 1.42

$$\frac{\sqrt{b}\sqrt{x}(a+bx) - a^{3/2}\sqrt{\frac{bx}{a}+1} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/Sqrt[a + b*x], x]

[Out] (Sqrt[b]*Sqrt[x]*(a + b*x) - a^(3/2)*Sqrt[1 + (b*x)/a]*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(b^(3/2)*Sqrt[a + b*x])

fricas [A] time = 0.46, size = 91, normalized size = 1.90

$$\left[\frac{a\sqrt{b} \log(2bx - 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2\sqrt{bx+a}b\sqrt{x}}{2b^2}, \frac{a\sqrt{-b} \arctan\left(\frac{\sqrt{bx+a}\sqrt{-b}}{b\sqrt{x}}\right) + \sqrt{bx+a}b\sqrt{x}}{b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [1/2*(a*sqrt(b)*log(2*b*x - 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*sqrt(b*x + a)*b*sqrt(x))/b^2, (a*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x)))) + sqrt(b*x + a)*b*sqrt(x))/b^2]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.00, size = 65, normalized size = 1.35

$$-\frac{\sqrt{bx+a} x a \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{2\sqrt{bx+a} b^{\frac{3}{2}}\sqrt{x}} + \frac{\sqrt{bx+a} \sqrt{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x+a)^(1/2),x)

[Out] x^(1/2)*(b*x+a)^(1/2)/b-1/2*a/b^(3/2)*((b*x+a)*x)^(1/2)/x^(1/2)/(b*x+a)^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))

maxima [B] time = 2.91, size = 73, normalized size = 1.52

$$\frac{a \log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+a}}{\sqrt{x}}}\right)}{2b^{\frac{3}{2}}} - \frac{\sqrt{bx+a} a}{\left(b^2 - \frac{(bx+a)b}{x}\right)\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] 1/2*a*log(-(sqrt(b) - sqrt(b*x + a)/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x)))/b^(3/2) - sqrt(b*x + a)*a/((b^2 - (b*x + a)*b/x)*sqrt(x))

mupad [B] time = 0.55, size = 44, normalized size = 0.92

$$\frac{\sqrt{x} \sqrt{a+bx}}{b} - \frac{2a \operatorname{atanh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a+bx}-\sqrt{a}}\right)}{b^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)/(a + b*x)^(1/2),x)`

[Out] $(x^{1/2}*(a + b*x)^{1/2})/b - (2*a*atanh((b^{1/2}*x^{1/2})/((a + b*x)^{1/2} - a^{1/2}))) / b^{3/2}$

sympy [A] time = 2.19, size = 44, normalized size = 0.92

$$\frac{\sqrt{a} \sqrt{x} \sqrt{1 + \frac{bx}{a}}}{b} - \frac{a \operatorname{asinh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)/(b*x+a)**(1/2),x)`

[Out] $\sqrt{a}*\sqrt{x}*\sqrt{1 + b*x/a}/b - a*\operatorname{asinh}(\sqrt{b}*\sqrt{x}/\sqrt{a})/b^{3/2}$

$$3.572 \quad \int \frac{1}{\sqrt{x} \sqrt{a+bx}} dx$$

Optimal. Leaf size=28

$$\frac{2 \tanh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a+bx}} \right)}{\sqrt{b}}$$

[Out] 2*arctanh(b^(1/2)*x^(1/2)/(b*x+a)^(1/2))/b^(1/2)

Rubi [A] time = 0.01, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {63, 217, 206}

$$\frac{2 \tanh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a+bx}} \right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*Sqrt[a + b*x]),x]

[Out] (2*ArcTanh[(Sqrt[b]*Sqrt[x])/Sqrt[a + b*x]])/Sqrt[b]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt{x} \sqrt{a+bx}} dx &= 2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x} \right) \\
&= 2 \operatorname{Subst} \left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}} \right) \\
&= \frac{2 \tanh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a+bx}} \right)}{\sqrt{b}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 50, normalized size = 1.79

$$\frac{2\sqrt{a} \sqrt{\frac{bx}{a} + 1} \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{b} \sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*Sqrt[a + b*x]),x]

[Out] (2*Sqrt[a]*Sqrt[1 + (b*x)/a]*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[b]*Sqrt[a + b*x])

fricas [A] time = 0.46, size = 57, normalized size = 2.04

$$\left[\frac{\log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a)}{\sqrt{b}}, -\frac{2\sqrt{-b} \arctan\left(\frac{\sqrt{bx+a}\sqrt{-b}}{b\sqrt{x}}\right)}{b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a)/sqrt(b), -2*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x)))/b]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [B] time = 0.00, size = 48, normalized size = 1.71

$$\frac{\sqrt{(bx+a)x} \ln\left(\frac{bx+\frac{a}{2}}{\sqrt{b}} + \sqrt{bx^2+ax}\right)}{\sqrt{bx+a} \sqrt{b} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/2)/(b*x+a)^(1/2),x)

[Out] ((b*x+a)*x)^(1/2)/x^(1/2)/(b*x+a)^(1/2)*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))/b^(1/2)

maxima [B] time = 2.95, size = 41, normalized size = 1.46

$$\frac{\log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+a}}{\sqrt{x}}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] -log(-(sqrt(b) - sqrt(b*x + a)/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x)))/sqrt(b)

mupad [B] time = 0.03, size = 30, normalized size = 1.07

$$\frac{4 \operatorname{atan}\left(\frac{\sqrt{a+bx}-\sqrt{a}}{\sqrt{-b} \sqrt{x}}\right)}{\sqrt{-b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/2)*(a + b*x)^(1/2)),x)

[Out] -(4*atan(((a + b*x)^(1/2) - a^(1/2))/((-b)^(1/2)*x^(1/2))))/(-b)^(1/2)

sympy [A] time = 1.10, size = 22, normalized size = 0.79

$$\frac{2 \operatorname{asinh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**(1/2)/(b*x+a)**(1/2),x)
```

```
[Out] 2*asinh(sqrt(b)*sqrt(x)/sqrt(a))/sqrt(b)
```

$$3.573 \quad \int \frac{1}{x^{3/2} \sqrt{a+bx}} dx$$

Optimal. Leaf size=19

$$-\frac{2\sqrt{a+bx}}{a\sqrt{x}}$$

[Out] $-2*(b*x+a)^{(1/2)}/a/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$-\frac{2\sqrt{a+bx}}{a\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*Sqrt[a + b*x]),x]

[Out] (-2*Sqrt[a + b*x])/(a*Sqrt[x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{3/2} \sqrt{a+bx}} dx = -\frac{2\sqrt{a+bx}}{a\sqrt{x}}$$

Mathematica [A] time = 0.00, size = 19, normalized size = 1.00

$$-\frac{2\sqrt{a+bx}}{a\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*Sqrt[a + b*x]),x]

[Out] (-2*Sqrt[a + b*x])/(a*Sqrt[x])

fricas [A] time = 0.46, size = 15, normalized size = 0.79

$$-\frac{2\sqrt{bx+a}}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] -2*sqrt(b*x + a)/(a*sqrt(x))

giac [B] time = 2.05, size = 33, normalized size = 1.74

$$-\frac{2\sqrt{bx+a}b^2}{\sqrt{(bx+a)b-ab}a|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] -2*sqrt(b*x + a)*b^2/(sqrt((b*x + a)*b - a*b)*a*abs(b))

maple [A] time = 0.00, size = 16, normalized size = 0.84

$$-\frac{2\sqrt{bx+a}}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2)/(b*x+a)^(1/2),x)

[Out] -2*(b*x+a)^(1/2)/a/x^(1/2)

maxima [A] time = 1.34, size = 15, normalized size = 0.79

$$-\frac{2\sqrt{bx+a}}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] -2*sqrt(b*x + a)/(a*sqrt(x))

mupad [B] time = 0.35, size = 15, normalized size = 0.79

$$-\frac{2\sqrt{a+bx}}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(a + b*x)^(1/2)),x)`

[Out] `-(2*(a + b*x)^(1/2))/(a*x^(1/2))`

sympy [A] time = 0.91, size = 19, normalized size = 1.00

$$-\frac{2\sqrt{b}\sqrt{\frac{a}{bx}+1}}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(b*x+a)**(1/2),x)`

[Out] `-2*sqrt(b)*sqrt(a/(b*x) + 1)/a`

$$3.574 \quad \int \frac{1}{x^{5/2} \sqrt{a+bx}} dx$$

Optimal. Leaf size=44

$$\frac{4b\sqrt{a+bx}}{3a^2\sqrt{x}} - \frac{2\sqrt{a+bx}}{3ax^{3/2}}$$

[Out] $-2/3*(b*x+a)^{(1/2)}/a/x^{(3/2)}+4/3*b*(b*x+a)^{(1/2)}/a^2/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 44, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{4b\sqrt{a+bx}}{3a^2\sqrt{x}} - \frac{2\sqrt{a+bx}}{3ax^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*Sqrt[a + b*x]),x]

[Out] $(-2*\text{Sqrt}[a + b*x])/(3*a*x^{(3/2)}) + (4*b*\text{Sqrt}[a + b*x])/(3*a^2*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{x^{5/2}\sqrt{a+bx}} dx = -\frac{2\sqrt{a+bx}}{3ax^{3/2}} - \frac{(2b) \int \frac{1}{x^{3/2}\sqrt{a+bx}} dx}{3a}$$

$$= -\frac{2\sqrt{a+bx}}{3ax^{3/2}} + \frac{4b\sqrt{a+bx}}{3a^2\sqrt{x}}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.61

$$-\frac{2(a-2bx)\sqrt{a+bx}}{3a^2x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*Sqrt[a + b*x]),x]

[Out] (-2*(a - 2*b*x)*Sqrt[a + b*x])/(3*a^2*x^(3/2))

fricas [A] time = 0.46, size = 23, normalized size = 0.52

$$\frac{2(2bx-a)\sqrt{bx+a}}{3a^2x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] 2/3*(2*b*x - a)*sqrt(b*x + a)/(a^2*x^(3/2))

giac [A] time = 1.90, size = 50, normalized size = 1.14

$$\frac{2\left(\frac{2(bx+a)b^3}{a^2} - \frac{3b^3}{a}\right)\sqrt{bx+a}b}{3((bx+a)b-ab)^{\frac{3}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] 2/3*(2*(b*x + a)*b^3/a^2 - 3*b^3/a)*sqrt(b*x + a)*b/(((b*x + a)*b - a*b)^(3/2)*abs(b))

maple [A] time = 0.00, size = 22, normalized size = 0.50

$$-\frac{2\sqrt{bx+a}(-2bx+a)}{3a^2x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/2)/(b*x+a)^(1/2),x)`

[Out] $-2/3*(b*x+a)^{(1/2)}*(-2*b*x+a)/x^{(3/2)}/a^2$

maxima [A] time = 1.30, size = 31, normalized size = 0.70

$$\frac{2 \left(\frac{3 \sqrt{bx+ab}}{\sqrt{x}} - \frac{(bx+a)^{\frac{3}{2}}}{x^{\frac{3}{2}}} \right)}{3a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2)/(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] $2/3*(3*\text{sqrt}(b*x + a)*b/\text{sqrt}(x) - (b*x + a)^{(3/2)}/x^{(3/2)})/a^2$

mupad [B] time = 0.34, size = 25, normalized size = 0.57

$$\frac{\left(\frac{2}{3a} - \frac{4bx}{3a^2} \right) \sqrt{a+bx}}{x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/2)*(a + b*x)^(1/2)),x)`

[Out] $-((2/(3*a) - (4*b*x)/(3*a^2))*(a + b*x)^{(1/2)})/x^{(3/2)}$

sympy [A] time = 1.92, size = 42, normalized size = 0.95

$$-\frac{2\sqrt{b}\sqrt{\frac{a}{bx}+1}}{3ax} + \frac{4b^{\frac{3}{2}}\sqrt{\frac{a}{bx}+1}}{3a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(b*x+a)**(1/2),x)`

[Out] $-2*\text{sqrt}(b)*\text{sqrt}(a/(b*x) + 1)/(3*a*x) + 4*b**(3/2)*\text{sqrt}(a/(b*x) + 1)/(3*a**2)$
)

$$3.575 \quad \int \frac{1}{x^{7/2} \sqrt{a+bx}} dx$$

Optimal. Leaf size=68

$$-\frac{16b^2\sqrt{a+bx}}{15a^3\sqrt{x}} + \frac{8b\sqrt{a+bx}}{15a^2x^{3/2}} - \frac{2\sqrt{a+bx}}{5ax^{5/2}}$$

[Out] $-2/5*(b*x+a)^{(1/2)}/a/x^{(5/2)}+8/15*b*(b*x+a)^{(1/2)}/a^2/x^{(3/2)}-16/15*b^2*(b*x+a)^{(1/2)}/a^3/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{16b^2\sqrt{a+bx}}{15a^3\sqrt{x}} + \frac{8b\sqrt{a+bx}}{15a^2x^{3/2}} - \frac{2\sqrt{a+bx}}{5ax^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(7/2)*Sqrt[a + b*x]),x]

[Out] $(-2*\text{Sqrt}[a + b*x])/(5*a*x^{(5/2)}) + (8*b*\text{Sqrt}[a + b*x])/(15*a^2*x^{(3/2)}) - (16*b^2*\text{Sqrt}[a + b*x])/(15*a^3*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{7/2}\sqrt{a+bx}} dx &= -\frac{2\sqrt{a+bx}}{5ax^{5/2}} - \frac{(4b) \int \frac{1}{x^{5/2}\sqrt{a+bx}} dx}{5a} \\
&= -\frac{2\sqrt{a+bx}}{5ax^{5/2}} + \frac{8b\sqrt{a+bx}}{15a^2x^{3/2}} + \frac{(8b^2) \int \frac{1}{x^{3/2}\sqrt{a+bx}} dx}{15a^2} \\
&= -\frac{2\sqrt{a+bx}}{5ax^{5/2}} + \frac{8b\sqrt{a+bx}}{15a^2x^{3/2}} - \frac{16b^2\sqrt{a+bx}}{15a^3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 0.59

$$-\frac{2\sqrt{a+bx}(3a^2-4abx+8b^2x^2)}{15a^3x^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(7/2)*Sqrt[a + b*x]), x]

[Out] (-2*Sqrt[a + b*x]*(3*a^2 - 4*a*b*x + 8*b^2*x^2))/(15*a^3*x^(5/2))

fricas [A] time = 0.48, size = 34, normalized size = 0.50

$$-\frac{2(8b^2x^2-4abx+3a^2)\sqrt{bx+a}}{15a^3x^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] -2/15*(8*b^2*x^2 - 4*a*b*x + 3*a^2)*sqrt(b*x + a)/(a^3*x^(5/2))

giac [A] time = 1.67, size = 66, normalized size = 0.97

$$-\frac{2\left(\frac{15b^5}{a} + 4\left(\frac{2(bx+a)b^5}{a^3} - \frac{5b^5}{a^2}\right)(bx+a)\right)\sqrt{bx+a}b}{15((bx+a)b-ab)^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+a)^(1/2), x, algorithm="giac")

[Out] -2/15*(15*b^5/a + 4*(2*(b*x + a)*b^5/a^3 - 5*b^5/a^2)*(b*x + a))*sqrt(b*x + a)*b/(((b*x + a)*b - a*b)^(5/2)*abs(b))

maple [A] time = 0.00, size = 35, normalized size = 0.51

$$-\frac{2\sqrt{bx+a} (8b^2x^2 - 4abx + 3a^2)}{15a^3x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(7/2)/(b*x+a)^(1/2),x)`

[Out] `-2/15*(b*x+a)^(1/2)*(8*b^2*x^2-4*a*b*x+3*a^2)/x^(5/2)/a^3`

maxima [A] time = 1.34, size = 46, normalized size = 0.68

$$-\frac{2\left(\frac{15\sqrt{bx+ab^2}}{\sqrt{x}} - \frac{10(bx+a)^{\frac{3}{2}}b}{x^{\frac{3}{2}}} + \frac{3(bx+a)^{\frac{5}{2}}}{x^{\frac{5}{2}}}\right)}{15a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(7/2)/(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] `-2/15*(15*sqrt(b*x + a)*b^2/sqrt(x) - 10*(b*x + a)^(3/2)*b/x^(3/2) + 3*(b*x + a)^(5/2)/x^(5/2))/a^3`

mupad [B] time = 0.35, size = 36, normalized size = 0.53

$$-\frac{\sqrt{a+bx} \left(\frac{2}{5a} + \frac{16b^2x^2}{15a^3} - \frac{8bx}{15a^2}\right)}{x^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(7/2)*(a + b*x)^(1/2)),x)`

[Out] `-((a + b*x)^(1/2)*(2/(5*a) + (16*b^2*x^2)/(15*a^3) - (8*b*x)/(15*a^2)))/x^(5/2)`

sympy [B] time = 6.25, size = 287, normalized size = 4.22

$$-\frac{6a^4b^{\frac{9}{2}}\sqrt{\frac{a}{bx}+1}}{15a^5b^4x^2+30a^4b^5x^3+15a^3b^6x^4} - \frac{4a^3b^{\frac{11}{2}}x\sqrt{\frac{a}{bx}+1}}{15a^5b^4x^2+30a^4b^5x^3+15a^3b^6x^4} - \frac{6a^2b^{\frac{13}{2}}x^2\sqrt{\frac{a}{bx}+1}}{15a^5b^4x^2+30a^4b^5x^3+15a^3b^6x^4} - \frac{1}{15a^5b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(7/2)/(b*x+a)**(1/2),x)`


```
[Out] -6*a**4*b**(9/2)*sqrt(a/(b*x) + 1)/(15*a**5*b**4*x**2 + 30*a**4*b**5*x**3 +
15*a**3*b**6*x**4) - 4*a**3*b**(11/2)*x*sqrt(a/(b*x) + 1)/(15*a**5*b**4*x*
**2 + 30*a**4*b**5*x**3 + 15*a**3*b**6*x**4) - 6*a**2*b**(13/2)*x**2*sqrt(a/
(b*x) + 1)/(15*a**5*b**4*x**2 + 30*a**4*b**5*x**3 + 15*a**3*b**6*x**4) - 24
*a*b**(15/2)*x**3*sqrt(a/(b*x) + 1)/(15*a**5*b**4*x**2 + 30*a**4*b**5*x**3
+ 15*a**3*b**6*x**4) - 16*b**(17/2)*x**4*sqrt(a/(b*x) + 1)/(15*a**5*b**4*x*
**2 + 30*a**4*b**5*x**3 + 15*a**3*b**6*x**4)
```

$$3.576 \quad \int \frac{1}{x^{9/2} \sqrt{a+bx}} dx$$

Optimal. Leaf size=92

$$\frac{32b^3\sqrt{a+bx}}{35a^4\sqrt{x}} - \frac{16b^2\sqrt{a+bx}}{35a^3x^{3/2}} + \frac{12b\sqrt{a+bx}}{35a^2x^{5/2}} - \frac{2\sqrt{a+bx}}{7ax^{7/2}}$$

[Out] $-2/7*(b*x+a)^{(1/2)}/a/x^{(7/2)}+12/35*b*(b*x+a)^{(1/2)}/a^2/x^{(5/2)}-16/35*b^2*(b*x+a)^{(1/2)}/a^3/x^{(3/2)}+32/35*b^3*(b*x+a)^{(1/2)}/a^4/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{16b^2\sqrt{a+bx}}{35a^3x^{3/2}} + \frac{32b^3\sqrt{a+bx}}{35a^4\sqrt{x}} + \frac{12b\sqrt{a+bx}}{35a^2x^{5/2}} - \frac{2\sqrt{a+bx}}{7ax^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(9/2)*Sqrt[a + b*x]),x]

[Out] $(-2*\text{Sqrt}[a + b*x])/(7*a*x^{(7/2)}) + (12*b*\text{Sqrt}[a + b*x])/(35*a^2*x^{(5/2)}) - (16*b^2*\text{Sqrt}[a + b*x])/(35*a^3*x^{(3/2)}) + (32*b^3*\text{Sqrt}[a + b*x])/(35*a^4*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{9/2}\sqrt{a+bx}} dx &= -\frac{2\sqrt{a+bx}}{7ax^{7/2}} - \frac{(6b) \int \frac{1}{x^{7/2}\sqrt{a+bx}} dx}{7a} \\
&= -\frac{2\sqrt{a+bx}}{7ax^{7/2}} + \frac{12b\sqrt{a+bx}}{35a^2x^{5/2}} + \frac{(24b^2) \int \frac{1}{x^{5/2}\sqrt{a+bx}} dx}{35a^2} \\
&= -\frac{2\sqrt{a+bx}}{7ax^{7/2}} + \frac{12b\sqrt{a+bx}}{35a^2x^{5/2}} - \frac{16b^2\sqrt{a+bx}}{35a^3x^{3/2}} - \frac{(16b^3) \int \frac{1}{x^{3/2}\sqrt{a+bx}} dx}{35a^3} \\
&= -\frac{2\sqrt{a+bx}}{7ax^{7/2}} + \frac{12b\sqrt{a+bx}}{35a^2x^{5/2}} - \frac{16b^2\sqrt{a+bx}}{35a^3x^{3/2}} + \frac{32b^3\sqrt{a+bx}}{35a^4\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 51, normalized size = 0.55

$$-\frac{2\sqrt{a+bx}(5a^3 - 6a^2bx + 8ab^2x^2 - 16b^3x^3)}{35a^4x^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(9/2)*Sqrt[a + b*x]),x]

[Out] (-2*Sqrt[a + b*x]*(5*a^3 - 6*a^2*b*x + 8*a*b^2*x^2 - 16*b^3*x^3))/(35*a^4*x^(7/2))

fricas [A] time = 0.44, size = 45, normalized size = 0.49

$$\frac{2(16b^3x^3 - 8ab^2x^2 + 6a^2bx - 5a^3)\sqrt{bx+a}}{35a^4x^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(9/2)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] 2/35*(16*b^3*x^3 - 8*a*b^2*x^2 + 6*a^2*b*x - 5*a^3)*sqrt(b*x + a)/(a^4*x^(7/2))

giac [A] time = 1.41, size = 82, normalized size = 0.89

$$-\frac{2\left(\frac{35b^7}{a} - 2\left(\frac{35b^7}{a^2} + 4\left(\frac{2(bx+a)b^7}{a^4} - \frac{7b^7}{a^3}\right)(bx+a)\right)\sqrt{bx+a}b}{35((bx+a)b-ab)^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(9/2)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] $-2/35*(35*b^7/a - 2*(35*b^7/a^2 + 4*(2*(b*x + a)*b^7/a^4 - 7*b^7/a^3)*(b*x + a))*(b*x + a))*sqrt(b*x + a)*b/(((b*x + a)*b - a*b)^(7/2)*abs(b))$

maple [A] time = 0.00, size = 46, normalized size = 0.50

$$\frac{2\sqrt{bx+a} \left(-16b^3x^3 + 8ab^2x^2 - 6a^2bx + 5a^3 \right)}{35a^4x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(9/2)/(b*x+a)^(1/2),x)

[Out] $-2/35*(b*x+a)^(1/2)*(-16*b^3*x^3+8*a*b^2*x^2-6*a^2*b*x+5*a^3)/x^(7/2)/a^4$

maxima [A] time = 1.30, size = 61, normalized size = 0.66

$$\frac{2 \left(\frac{35 \sqrt{bx+a} b^3}{\sqrt{x}} - \frac{35 (bx+a)^{\frac{3}{2}} b^2}{x^{\frac{3}{2}}} + \frac{21 (bx+a)^{\frac{5}{2}} b}{x^{\frac{5}{2}}} - \frac{5 (bx+a)^{\frac{7}{2}}}{x^{\frac{7}{2}}} \right)}{35 a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(9/2)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] $2/35*(35*sqrt(b*x + a)*b^3/sqrt(x) - 35*(b*x + a)^(3/2)*b^2/x^(3/2) + 21*(b*x + a)^(5/2)*b/x^(5/2) - 5*(b*x + a)^(7/2)/x^(7/2))/a^4$

mupad [B] time = 0.38, size = 47, normalized size = 0.51

$$\frac{\sqrt{a+bx} \left(\frac{2}{7a} + \frac{16b^2x^2}{35a^3} - \frac{32b^3x^3}{35a^4} - \frac{12bx}{35a^2} \right)}{x^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(9/2)*(a + b*x)^(1/2)),x)

[Out] $-((a + b*x)^(1/2)*(2/(7*a) + (16*b^2*x^2)/(35*a^3) - (32*b^3*x^3)/(35*a^4) - (12*b*x)/(35*a^2)))/x^(7/2)$

sympy [B] time = 16.14, size = 488, normalized size = 5.30

$$\frac{10a^6b^{\frac{19}{2}}\sqrt{\frac{a}{bx}+1}}{35a^7b^9x^3+105a^6b^{10}x^4+105a^5b^{11}x^5+35a^4b^{12}x^6} - \frac{18a^5b^{\frac{21}{2}}x\sqrt{\frac{a}{bx}+1}}{35a^7b^9x^3+105a^6b^{10}x^4+105a^5b^{11}x^5+35a^4b^{12}x^6} - \frac{1}{35a^7b^9x^3+105a^6b^{10}x^4+105a^5b^{11}x^5+35a^4b^{12}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(9/2)/(b*x+a)**(1/2),x)

[Out]
$$\begin{aligned} & -10a^6b^{19/2}\sqrt{a/(bx) + 1}/(35a^7b^9x^3 + 105a^6b^{10}x^4 \\ & + 105a^5b^{11}x^5 + 35a^4b^{12}x^6) - 18a^5b^{21/2}x\sqrt{a/(bx) + 1}/(35a^7b^9x^3 \\ & + 105a^6b^{10}x^4 + 105a^5b^{11}x^5 + 35a^4b^{12}x^6) - 10a^4b^{23/2}x^2\sqrt{a/(bx) + 1}/(35a^7b^9x^3 \\ & + 105a^6b^{10}x^4 + 105a^5b^{11}x^5 + 35a^4b^{12}x^6) + 10a^3b^{25/2}x^3\sqrt{a/(bx) + 1}/(35a^7b^9x^3 \\ & + 105a^6b^{10}x^4 + 105a^5b^{11}x^5 + 35a^4b^{12}x^6) + 60a^2b^{27/2}x^4\sqrt{a/(bx) + 1}/(35a^7b^9x^3 \\ & + 105a^6b^{10}x^4 + 105a^5b^{11}x^5 + 35a^4b^{12}x^6) + 80ab^{29/2}x^5\sqrt{a/(bx) + 1}/(35a^7b^9x^3 \\ & + 105a^6b^{10}x^4 + 105a^5b^{11}x^5 + 35a^4b^{12}x^6) + 32b^{31/2}x^6\sqrt{a/(bx) + 1}/(35a^7b^9x^3 \\ & + 105a^6b^{10}x^4 + 105a^5b^{11}x^5 + 35a^4b^{12}x^6) \end{aligned}$$

$$3.577 \quad \int \frac{x^{5/2}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=96

$$\frac{15a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^{7/2}} - \frac{15a\sqrt{x}\sqrt{a+bx}}{4b^3} + \frac{5x^{3/2}\sqrt{a+bx}}{2b^2} - \frac{2x^{5/2}}{b\sqrt{a+bx}}$$

[Out] $15/4*a^2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(7/2)}-2*x^{(5/2)}/b/(b*x+a)^{(1/2)}+5/2*x^{(3/2)}*(b*x+a)^{(1/2)}/b^2-15/4*a*x^{(1/2)}*(b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.03, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {47, 50, 63, 217, 206}

$$\frac{15a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^{7/2}} + \frac{5x^{3/2}\sqrt{a+bx}}{2b^2} - \frac{15a\sqrt{x}\sqrt{a+bx}}{4b^3} - \frac{2x^{5/2}}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(5/2)}/(a + b*x)^{(3/2)}, x]$

[Out] $(-2*x^{(5/2)})/(b*\operatorname{Sqrt}[a + b*x]) - (15*a*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/(4*b^3) + (5*x^{(3/2)}*\operatorname{Sqrt}[a + b*x])/(2*b^2) + (15*a^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/(4*b^{(7/2)})$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(a+bx)^{3/2}} dx &= -\frac{2x^{5/2}}{b\sqrt{a+bx}} + \frac{5 \int \frac{x^{3/2}}{\sqrt{a+bx}} dx}{b} \\
&= -\frac{2x^{5/2}}{b\sqrt{a+bx}} + \frac{5x^{3/2}\sqrt{a+bx}}{2b^2} - \frac{(15a) \int \frac{\sqrt{x}}{\sqrt{a+bx}} dx}{4b^2} \\
&= -\frac{2x^{5/2}}{b\sqrt{a+bx}} - \frac{15a\sqrt{x}\sqrt{a+bx}}{4b^3} + \frac{5x^{3/2}\sqrt{a+bx}}{2b^2} + \frac{(15a^2) \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx}{8b^3} \\
&= -\frac{2x^{5/2}}{b\sqrt{a+bx}} - \frac{15a\sqrt{x}\sqrt{a+bx}}{4b^3} + \frac{5x^{3/2}\sqrt{a+bx}}{2b^2} + \frac{(15a^2) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right)}{4b^3} \\
&= -\frac{2x^{5/2}}{b\sqrt{a+bx}} - \frac{15a\sqrt{x}\sqrt{a+bx}}{4b^3} + \frac{5x^{3/2}\sqrt{a+bx}}{2b^2} + \frac{(15a^2) \operatorname{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^3} \\
&= -\frac{2x^{5/2}}{b\sqrt{a+bx}} - \frac{15a\sqrt{x}\sqrt{a+bx}}{4b^3} + \frac{5x^{3/2}\sqrt{a+bx}}{2b^2} + \frac{15a^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{4b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.52

$$\frac{2x^{7/2}\sqrt{\frac{bx}{a}+1} {}_2F_1\left(\frac{3}{2}, \frac{7}{2}; \frac{9}{2}; -\frac{bx}{a}\right)}{7a\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/(a + b*x)^(3/2), x]

[Out] (2*x^(7/2)*Sqrt[1 + (b*x)/a]*Hypergeometric2F1[3/2, 7/2, 9/2, -((b*x)/a)])/(7*a*Sqrt[a + b*x])

fricas [A] time = 0.50, size = 175, normalized size = 1.82

$$\left[\frac{15(a^2bx + a^3)\sqrt{b} \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(2b^3x^2 - 5ab^2x - 15a^2b)\sqrt{bx+a}\sqrt{x}}{8(b^5x + ab^4)}, -\frac{15(a^2bx + a^3)}{8(b^5x + ab^4)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^(3/2), x, algorithm="fricas")

[Out] [1/8*(15*(a^2*b*x + a^3)*sqrt(b)*log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(2*b^3*x^2 - 5*a*b^2*x - 15*a^2*b)*sqrt(b*x + a)*sqrt(x))/(b^5*x + a*b^4), -1/4*(15*(a^2*b*x + a^3)*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) - (2*b^3*x^2 - 5*a*b^2*x - 15*a^2*b)*sqrt(b*x + a)*sqrt(x))/(b^5*x + a*b^4)]

giac [A] time = 92.14, size = 131, normalized size = 1.36

$$\frac{\left(2\sqrt{(bx+a)b-ab}\sqrt{bx+a}\left(\frac{2(bx+a)}{b^3}-\frac{9a}{b^3}\right) - \frac{32a^3}{\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2+ab\right)b^{\frac{3}{2}}} - \frac{15a^2\log\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2\right)}{b^{\frac{5}{2}}} \right) |b|}{8b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^(3/2), x, algorithm="giac")

[Out] 1/8*(2*sqrt((b*x + a)*b - a*b)*sqrt(b*x + a)*(2*(b*x + a)/b^3 - 9*a/b^3) - 32*a^3/(((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2 + a*b)*b^(3/2)) - 15*a^2*log((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2)/b^(5/2))*abs(b)/b^2

maple [A] time = 0.04, size = 119, normalized size = 1.24

$$\frac{\left(\frac{15a^2 \ln\left(\frac{bx+\frac{a}{2}+\sqrt{bx^2+ax}}{\sqrt{b}}\right)}{8b^{\frac{7}{2}}} - \frac{2\sqrt{-(x+\frac{a}{b})a+(x+\frac{a}{b})^2 b a^2}}{(x+\frac{a}{b})b^4} \right) \sqrt{(bx+a)x}}{\sqrt{bx+a} \sqrt{x}} - \frac{(-2bx+7a)\sqrt{bx+a}\sqrt{x}}{4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x+a)^(3/2), x)

[Out] $-1/4*(-2*b*x+7*a)*(b*x+a)^{(1/2)}*x^{(1/2)}/b^3+(15/8/b^{(7/2)}*a^2*\ln((b*x+1/2*a)/b^{(1/2)}+(b*x^2+a*x)^{(1/2)})-2/b^4*a^2/(x+a/b)*(b*(x+a/b)^2-(x+a/b)*a)^{(1/2)})*((b*x+a)*x)^{(1/2)}/(b*x+a)^{(1/2)}/x^{(1/2)}$

maxima [A] time = 2.92, size = 131, normalized size = 1.36

$$-\frac{8a^2b^2 - \frac{25(bx+a)a^2b}{x} + \frac{15(bx+a)^2a^2}{x^2}}{4\left(\frac{\sqrt{bx+a}b^5}{\sqrt{x}} - \frac{2(bx+a)^{\frac{3}{2}}b^4}{x^2} + \frac{(bx+a)^{\frac{5}{2}}b^3}{x^2}\right)} - \frac{15a^2 \log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+a}}{\sqrt{x}}}\right)}{8b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^(3/2), x, algorithm="maxima")

[Out] $-1/4*(8*a^2*b^2 - 25*(b*x + a)*a^2*b/x + 15*(b*x + a)^2*a^2/x^2)/(sqrt(b*x + a)*b^5/sqrt(x) - 2*(b*x + a)^{(3/2)}*b^4/x^{(3/2)} + (b*x + a)^{(5/2)}*b^3/x^{(5/2)}) - 15/8*a^2*log(-sqrt(b) - sqrt(b*x + a)/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x))/b^{(7/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{(a+bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(a + b*x)^(3/2), x)

[Out] int(x^(5/2)/(a + b*x)^(3/2), x)

sympy [A] time = 8.14, size = 105, normalized size = 1.09

$$-\frac{15a^{\frac{3}{2}}\sqrt{x}}{4b^3\sqrt{1+\frac{bx}{a}}}-\frac{5\sqrt{a}x^{\frac{3}{2}}}{4b^2\sqrt{1+\frac{bx}{a}}}+\frac{15a^2\operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{\frac{7}{2}}}+\frac{x^{\frac{5}{2}}}{2\sqrt{a}b\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(b*x+a)**(3/2),x)

[Out] -15*a**(3/2)*sqrt(x)/(4*b**3*sqrt(1 + b*x/a)) - 5*sqrt(a)*x**(3/2)/(4*b**2*sqrt(1 + b*x/a)) + 15*a**2*asinh(sqrt(b)*sqrt(x)/sqrt(a))/(4*b**(7/2)) + x*(5/2)/(2*sqrt(a)*b*sqrt(1 + b*x/a))

$$3.578 \quad \int \frac{x^{3/2}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=68

$$-\frac{3a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{5/2}} + \frac{3\sqrt{x}\sqrt{a+bx}}{b^2} - \frac{2x^{3/2}}{b\sqrt{a+bx}}$$

[Out] $-3*a*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(5/2)}-2*x^{(3/2)}/b/(b*x+a)^{(1/2)}+3*x^{(1/2)}*(b*x+a)^{(1/2)}/b^2$

Rubi [A] time = 0.02, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {47, 50, 63, 217, 206}

$$\frac{3\sqrt{x}\sqrt{a+bx}}{b^2} - \frac{3a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{5/2}} - \frac{2x^{3/2}}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(3/2)}/(a + b*x)^{(3/2)}, x]$

[Out] $(-2*x^{(3/2)})/(b*\operatorname{Sqrt}[a + b*x]) + (3*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/b^2 - (3*a*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/ \operatorname{Sqrt}[a + b*x]])/b^{(5/2)}$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^{(m)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{NeQ}[m + n + 1, 0]$ && $!(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] \mid\mid (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m - n, 0])))$ && $!\operatorname{ILtQ}[m + n + 2, 0]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{3/2}}{(a+bx)^{3/2}} dx &= -\frac{2x^{3/2}}{b\sqrt{a+bx}} + \frac{3 \int \frac{\sqrt{x}}{\sqrt{a+bx}} dx}{b} \\
&= -\frac{2x^{3/2}}{b\sqrt{a+bx}} + \frac{3\sqrt{x}\sqrt{a+bx}}{b^2} - \frac{(3a) \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx}{2b^2} \\
&= -\frac{2x^{3/2}}{b\sqrt{a+bx}} + \frac{3\sqrt{x}\sqrt{a+bx}}{b^2} - \frac{(3a) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\
&= -\frac{2x^{3/2}}{b\sqrt{a+bx}} + \frac{3\sqrt{x}\sqrt{a+bx}}{b^2} - \frac{(3a) \operatorname{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right)}{b^2} \\
&= -\frac{2x^{3/2}}{b\sqrt{a+bx}} + \frac{3\sqrt{x}\sqrt{a+bx}}{b^2} - \frac{3a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.74

$$\frac{2x^{5/2}\sqrt{\frac{bx}{a}+1} {}_2F_1\left(\frac{3}{2}, \frac{5}{2}; \frac{7}{2}; -\frac{bx}{a}\right)}{5a\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/(a + b*x)^(3/2),x]

[Out] (2*x^(5/2)*Sqrt[1 + (b*x)/a]*Hypergeometric2F1[3/2, 5/2, 7/2, -((b*x)/a)]/(5*a*Sqrt[a + b*x])

fricas [A] time = 0.44, size = 145, normalized size = 2.13

$$\left[\frac{3(abx + a^2)\sqrt{b} \log(2bx - 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(b^2x + 3ab)\sqrt{bx+a}\sqrt{x}}{2(b^4x + ab^3)}, \frac{3(abx + a^2)\sqrt{-b} \arctan\left(\frac{\sqrt{bx+a}}{b}\right)}{b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] [1/2*(3*(a*b*x + a^2)*sqrt(b)*log(2*b*x - 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(b^2*x + 3*a*b)*sqrt(b*x + a)*sqrt(x))/(b^4*x + a*b^3), (3*(a*b*x + a^2)*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) + (b^2*x + 3*a*b)*sqrt(b*x + a)*sqrt(x))/(b^4*x + a*b^3)]

giac [B] time = 93.12, size = 115, normalized size = 1.69

$$\frac{\left(\frac{8a^2\sqrt{b}}{(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab})^2+ab} + \frac{3a \log\left(\frac{\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}}{\sqrt{b}}\right)^2}{\sqrt{b}} + \frac{2\sqrt{(bx+a)b-ab}\sqrt{bx+a}}{b} \right) |b|}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^(3/2),x, algorithm="giac")

[Out] 1/2*(8*a^2*sqrt(b)/((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2 + a*b) + 3*a*log((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2)/sqrt(b) + 2*sqrt((b*x + a)*b - a*b)*sqrt(b*x + a)/b)*abs(b)/b^3

maple [B] time = 0.03, size = 106, normalized size = 1.56

$$\frac{\left(-\frac{3a \ln\left(\frac{bx+\frac{a}{2}+\sqrt{bx^2+ax}}{\sqrt{b}}\right)}{2b^{\frac{5}{2}}} + \frac{2\sqrt{-(x+\frac{a}{b})a+(x+\frac{a}{b})^2ba}}{(x+\frac{a}{b})b^3} \right) \sqrt{(bx+a)x}}{\sqrt{bx+a}\sqrt{x}} + \frac{\sqrt{bx+a}\sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(b*x+a)^(3/2),x)

[Out] $x^{(1/2)}*(b*x+a)^{(1/2)}/b^2+(-3/2*a/b^{(5/2)}*\ln((b*x+1/2*a)/b^{(1/2)}+(b*x^2+a*x)^{(1/2)})+2*a/b^3/(x+a/b)*(-(x+a/b)*a+(x+a/b)^2*b)^{(1/2)}*((b*x+a)*x)^{(1/2)}/(b*x+a)^{(1/2)}/x^{(1/2)}$

maxima [A] time = 3.02, size = 92, normalized size = 1.35

$$\frac{2ab - \frac{3(bx+a)a}{x}}{\frac{\sqrt{bx+a}b^3}{\sqrt{x}} - \frac{(bx+a)^3 b^2}{x^2}} + \frac{3a \log\left(-\frac{\sqrt{b} - \frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+a}}{\sqrt{x}}}\right)}{2b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)/(b*x+a)^(3/2),x, algorithm="maxima")`

[Out] $(2*a*b - 3*(b*x + a)*a/x)/(\sqrt{b*x + a}*b^3/\sqrt{x} - (b*x + a)^{(3/2)}*b^2/x^{(3/2)}) + 3/2*a*\log(-(\sqrt{b} - \sqrt{b*x + a})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x + a})/b^{(5/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{3/2}}{(a + bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(a + b*x)^(3/2),x)`

[Out] `int(x^(3/2)/(a + b*x)^(3/2), x)`

sympy [A] time = 3.68, size = 71, normalized size = 1.04

$$\frac{3\sqrt{a}\sqrt{x}}{b^2\sqrt{1 + \frac{bx}{a}}} - \frac{3a \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{\frac{5}{2}}} + \frac{x^{\frac{3}{2}}}{\sqrt{a}b\sqrt{1 + \frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(b*x+a)**(3/2),x)`

[Out] $3*\sqrt{a}*\sqrt{x}/(b**2*\sqrt{1 + b*x/a}) - 3*a*\operatorname{asinh}(\sqrt{b}*\sqrt{x})/\sqrt{a})/b**(5/2) + x**(3/2)/(\sqrt{a}*b*\sqrt{1 + b*x/a})$

$$3.579 \quad \int \frac{\sqrt{x}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=48

$$\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{3/2}} - \frac{2\sqrt{x}}{b\sqrt{a+bx}}$$

[Out] $2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)/(b*x+a)^{(1/2)})/b^{(3/2)}-2*x^{(1/2)}/b/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 63, 217, 206}

$$\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{3/2}} - \frac{2\sqrt{x}}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(a + b*x)^(3/2), x]

[Out] $(-2*\operatorname{Sqrt}[x])/(b*\operatorname{Sqrt}[a + b*x]) + (2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a + b*x]])/b^{(3/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt

Q[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{x}}{(a+bx)^{3/2}} dx &= -\frac{2\sqrt{x}}{b\sqrt{a+bx}} + \frac{\int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx}{b} \\ &= -\frac{2\sqrt{x}}{b\sqrt{a+bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right)}{b} \\ &= -\frac{2\sqrt{x}}{b\sqrt{a+bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right)}{b} \\ &= -\frac{2\sqrt{x}}{b\sqrt{a+bx}} + \frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.07, size = 64, normalized size = 1.33

$$\frac{2\left(\sqrt{a}\sqrt{\frac{bx}{a}+1} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) - \sqrt{b}\sqrt{x}\right)}{b^{3/2}\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(a + b*x)^(3/2), x]

[Out] (2*(-(Sqrt[b]*Sqrt[x]) + Sqrt[a]*Sqrt[1 + (b*x)/a]*ArcSinh[(Sqrt[b]*Sqrt[x])
)/Sqrt[a]])/(b^(3/2)*Sqrt[a + b*x])

fricas [A] time = 0.45, size = 119, normalized size = 2.48

$$\left[\frac{(bx+a)\sqrt{b} \log(2bx+2\sqrt{bx+a}\sqrt{b}\sqrt{x}+a) - 2\sqrt{bx+a}b\sqrt{x}}{b^3x+ab^2}, -\frac{2\left((bx+a)\sqrt{-b} \arctan\left(\frac{\sqrt{bx+a}\sqrt{-b}}{b\sqrt{x}}\right) + \sqrt{bx+a}\right)}{b^3x+ab^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] [((b*x + a)*sqrt(b)*log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) - 2*sqrt(b*x + a)*b*sqrt(x))/(b^3*x + a*b^2), -2*((b*x + a)*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) + sqrt(b*x + a)*b*sqrt(x))/(b^3*x + a*b^2)]

giac [B] time = 94.86, size = 85, normalized size = 1.77

$$\frac{\left(\frac{4a\sqrt{b}}{(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab})^2+ab} + \frac{\log\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2\right)}{\sqrt{b}} \right) |b|}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^(3/2),x, algorithm="giac")

[Out] -(4*a*sqrt(b)/((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2 + a*b) + log((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2/sqrt(b))*abs(b)/b^2

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{x}}{(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x+a)^(3/2),x)

[Out] int(x^(1/2)/(b*x+a)^(3/2),x)

maxima [A] time = 2.98, size = 57, normalized size = 1.19

$$-\frac{\log\left(\frac{\sqrt{b}-\frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+a}}{\sqrt{x}}}\right)}{b^{\frac{3}{2}}} - \frac{2\sqrt{x}}{\sqrt{bx+ab}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] -log(-(sqrt(b) - sqrt(b*x + a)/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x)))/b^(3/2) - 2*sqrt(x)/(sqrt(b*x + a)*b)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{x}}{(a + bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)/(a + b*x)^(3/2), x)`

[Out] `int(x^(1/2)/(a + b*x)^(3/2), x)`

sympy [A] time = 1.78, size = 46, normalized size = 0.96

$$\frac{2 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}} - \frac{2\sqrt{x}}{\sqrt{a}b\sqrt{1 + \frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)/(b*x+a)**(3/2), x)`

[Out] `2*asinh(sqrt(b)*sqrt(x)/sqrt(a))/b**(3/2) - 2*sqrt(x)/(sqrt(a)*b*sqrt(1 + b*x/a))`

$$3.580 \quad \int \frac{1}{\sqrt{x}(a+bx)^{3/2}} dx$$

Optimal. Leaf size=19

$$\frac{2\sqrt{x}}{a\sqrt{a+bx}}$$

[Out] $2*x^{(1/2)}/a/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$\frac{2\sqrt{x}}{a\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(a + b*x)^(3/2)),x]

[Out] (2*Sqrt[x])/(a*Sqrt[a + b*x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt{x}(a+bx)^{3/2}} dx = \frac{2\sqrt{x}}{a\sqrt{a+bx}}$$

Mathematica [A] time = 0.00, size = 19, normalized size = 1.00

$$\frac{2\sqrt{x}}{a\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(a + b*x)^(3/2)),x]

[Out] (2*Sqrt[x])/(a*Sqrt[a + b*x])

fricas [A] time = 0.43, size = 22, normalized size = 1.16

$$\frac{2\sqrt{bx+a}\sqrt{x}}{abx+a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/x^(1/2),x, algorithm="fricas")

[Out] 2*sqrt(b*x + a)*sqrt(x)/(a*b*x + a^2)

giac [B] time = 1.11, size = 45, normalized size = 2.37

$$\frac{4b^{\frac{3}{2}}}{\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2+ab\right)|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/x^(1/2),x, algorithm="giac")

[Out] 4*b^(3/2)/(((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2 + a*b)*abs(b))

maple [A] time = 0.00, size = 16, normalized size = 0.84

$$\frac{2\sqrt{x}}{\sqrt{bx+a}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/x^(1/2),x)

[Out] 2*x^(1/2)/a/(b*x+a)^(1/2)

maxima [A] time = 1.32, size = 15, normalized size = 0.79

$$\frac{2\sqrt{x}}{\sqrt{bx+a}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/x^(1/2),x, algorithm="maxima")

[Out] 2*sqrt(x)/(sqrt(b*x + a)*a)

mupad [B] time = 0.33, size = 22, normalized size = 1.16

$$\frac{2\sqrt{x}\sqrt{a+bx}}{a^2+bx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(a + b*x)^(3/2)),x)`

[Out] `(2*x^(1/2)*(a + b*x)^(1/2))/(a^2 + a*b*x)`

sympy [A] time = 0.88, size = 17, normalized size = 0.89

$$\frac{2}{a\sqrt{b}\sqrt{\frac{a}{bx} + 1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(3/2)/x**(1/2),x)`

[Out] `2/(a*sqrt(b)*sqrt(a/(b*x) + 1))`

$$3.581 \quad \int \frac{1}{x^{3/2}(a+bx)^{3/2}} dx$$

Optimal. Leaf size=39

$$\frac{2}{a\sqrt{x}\sqrt{a+bx}} - \frac{4\sqrt{a+bx}}{a^2\sqrt{x}}$$

[Out] 2/a/x^(1/2)/(b*x+a)^(1/2)-4*(b*x+a)^(1/2)/a^2/x^(1/2)

Rubi [A] time = 0.00, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{2}{a\sqrt{x}\sqrt{a+bx}} - \frac{4\sqrt{a+bx}}{a^2\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(a + b*x)^(3/2)),x]

[Out] 2/(a*Sqrt[x]*Sqrt[a + b*x]) - (4*Sqrt[a + b*x])/(a^2*Sqrt[x])

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{x^{3/2}(a+bx)^{3/2}} dx = \frac{2}{a\sqrt{x}\sqrt{a+bx}} + \frac{2 \int \frac{1}{x^{3/2}\sqrt{a+bx}} dx}{a}$$

$$= \frac{2}{a\sqrt{x}\sqrt{a+bx}} - \frac{4\sqrt{a+bx}}{a^2\sqrt{x}}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 0.64

$$-\frac{2(a+2bx)}{a^2\sqrt{x}\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(a + b*x)^(3/2)), x]

[Out] (-2*(a + 2*b*x))/(a^2*Sqrt[x]*Sqrt[a + b*x])

fricas [A] time = 0.43, size = 34, normalized size = 0.87

$$-\frac{2(2bx+a)\sqrt{bx+a}\sqrt{x}}{a^2bx^2+a^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a)^(3/2), x, algorithm="fricas")

[Out] -2*(2*b*x + a)*sqrt(b*x + a)*sqrt(x)/(a^2*b*x^2 + a^3*x)

giac [B] time = 1.05, size = 82, normalized size = 2.10

$$-\frac{4b^{\frac{5}{2}}}{\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2+ab\right)a|b|} - \frac{2\sqrt{bx+a}b^2}{\sqrt{(bx+a)b-ab}a^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a)^(3/2), x, algorithm="giac")

[Out] -4*b^(5/2)/(((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2 + a*b)*a*a*bs(b)) - 2*sqrt(b*x + a)*b^2/(sqrt((b*x + a)*b - a*b)*a^2*abs(b))

maple [A] time = 0.01, size = 22, normalized size = 0.56

$$-\frac{2(2bx+a)}{\sqrt{bx+a}a^2\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(3/2)/(b*x+a)^(3/2),x)`

[Out] $-2*(2*b*x+a)/(b*x+a)^(1/2)/x^(1/2)/a^2$

maxima [A] time = 1.32, size = 32, normalized size = 0.82

$$-\frac{2b\sqrt{x}}{\sqrt{bx+a}a^2} - \frac{2\sqrt{bx+a}}{a^2\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(b*x+a)^(3/2),x, algorithm="maxima")`

[Out] $-2*b*\text{sqrt}(x)/(\text{sqrt}(b*x + a)*a^2) - 2*\text{sqrt}(b*x + a)/(a^2*\text{sqrt}(x))$

mupad [B] time = 0.39, size = 39, normalized size = 1.00

$$-\frac{2a\sqrt{a+bx} + 4bx\sqrt{a+bx}}{\sqrt{x}(a^3 + bxa^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(a + b*x)^(3/2)),x)`

[Out] $-(2*a*(a + b*x)^(1/2) + 4*b*x*(a + b*x)^(1/2))/(x^(1/2)*(a^3 + a^2*b*x))$

sympy [A] time = 1.60, size = 41, normalized size = 1.05

$$-\frac{2}{a\sqrt{b}x\sqrt{\frac{a}{bx}+1}} - \frac{4\sqrt{b}}{a^2\sqrt{\frac{a}{bx}+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(b*x+a)**(3/2),x)`

[Out] $-2/(a*\text{sqrt}(b)*x*\text{sqrt}(a/(b*x) + 1)) - 4*\text{sqrt}(b)/(a**2*\text{sqrt}(a/(b*x) + 1))$

$$3.582 \quad \int \frac{1}{x^{5/2}(a+bx)^{3/2}} dx$$

Optimal. Leaf size=63

$$\frac{16b\sqrt{a+bx}}{3a^3\sqrt{x}} - \frac{8\sqrt{a+bx}}{3a^2x^{3/2}} + \frac{2}{ax^{3/2}\sqrt{a+bx}}$$

[Out] $2/a/x^{(3/2)}/(b*x+a)^{(1/2)}-8/3*(b*x+a)^{(1/2)}/a^2/x^{(3/2)}+16/3*b*(b*x+a)^{(1/2)}/a^3/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{8\sqrt{a+bx}}{3a^2x^{3/2}} + \frac{16b\sqrt{a+bx}}{3a^3\sqrt{x}} + \frac{2}{ax^{3/2}\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(a + b*x)^(3/2)),x]

[Out] $2/(a*x^{(3/2)}*Sqrt[a + b*x]) - (8*Sqrt[a + b*x])/(3*a^2*x^{(3/2)}) + (16*b*Sqrt[a + b*x])/(3*a^3*Sqrt[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{5/2}(a+bx)^{3/2}} dx &= \frac{2}{ax^{3/2}\sqrt{a+bx}} + \frac{4 \int \frac{1}{x^{5/2}\sqrt{a+bx}} dx}{a} \\
&= \frac{2}{ax^{3/2}\sqrt{a+bx}} - \frac{8\sqrt{a+bx}}{3a^2x^{3/2}} - \frac{(8b) \int \frac{1}{x^{3/2}\sqrt{a+bx}} dx}{3a^2} \\
&= \frac{2}{ax^{3/2}\sqrt{a+bx}} - \frac{8\sqrt{a+bx}}{3a^2x^{3/2}} + \frac{16b\sqrt{a+bx}}{3a^3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 38, normalized size = 0.60

$$-\frac{2(a^2 - 4abx - 8b^2x^2)}{3a^3x^{3/2}\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(a + b*x)^(3/2)),x]

[Out] (-2*(a^2 - 4*a*b*x - 8*b^2*x^2))/(3*a^3*x^(3/2)*Sqrt[a + b*x])

fricas [A] time = 0.43, size = 49, normalized size = 0.78

$$\frac{2(8b^2x^2 + 4abx - a^2)\sqrt{bx+a}\sqrt{x}}{3(a^3bx^3 + a^4x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] 2/3*(8*b^2*x^2 + 4*a*b*x - a^2)*sqrt(b*x + a)*sqrt(x)/(a^3*b*x^3 + a^4*x^2)

giac [B] time = 1.20, size = 98, normalized size = 1.56

$$\frac{2\sqrt{bx+a}\left(\frac{5(bx+a)b^2|b|}{a^3} - \frac{6b^2|b|}{a^2}\right)}{3((bx+a)b-ab)^{\frac{3}{2}}} + \frac{4b^{\frac{7}{2}}}{\left(\left(\sqrt{bx+a}\sqrt{b} - \sqrt{(bx+a)b-ab}\right)^2 + ab\right)a^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^(3/2),x, algorithm="giac")

[Out] $\frac{2}{3}\sqrt{bx+a}(5(bx+a)b^2\text{abs}(b)/a^3 - 6b^2\text{abs}(b)/a^2)/((bx+a)*b - a*b)^{(3/2)} + 4*b^{(7/2)}/(((\sqrt{bx+a})*\sqrt{b} - \sqrt{(bx+a)*b - a*b})^2 + a*b)*a^2*\text{abs}(b))$

maple [A] time = 0.00, size = 33, normalized size = 0.52

$$-\frac{2(-8b^2x^2 - 4abx + a^2)}{3\sqrt{bx+a}a^3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/x^{(5/2)}/(bx+a)^{(3/2)}, x)$

[Out] $-2/3*(-8*b^2*x^2-4*a*b*x+a^2)/(bx+a)^{(1/2)}/x^{(3/2)}/a^3$

maxima [A] time = 1.31, size = 50, normalized size = 0.79

$$\frac{2b^2\sqrt{x}}{\sqrt{bx+a}a^3} + \frac{2\left(\frac{6\sqrt{bx+a}b}{\sqrt{x}} - \frac{(bx+a)^{\frac{3}{2}}}{x^{\frac{3}{2}}}\right)}{3a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^{(5/2)}/(bx+a)^{(3/2)}, x, \text{algorithm}="maxima")$

[Out] $2*b^2*\sqrt{x}/(\sqrt{bx+a})*a^3 + 2/3*(6*\sqrt{bx+a}*b/\sqrt{x} - (bx+a)^{(3/2)}/x^{(3/2)})/a^3$

mupad [B] time = 0.41, size = 46, normalized size = 0.73

$$\frac{\sqrt{a+bx}\left(\frac{8x}{3a^2} - \frac{2}{3ab} + \frac{16bx^2}{3a^3}\right)}{x^{5/2} + \frac{ax^{3/2}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(x^{(5/2)}*(a+bx)^{(3/2)}), x)$

[Out] $((a+bx)^{(1/2)}*((8*x)/(3*a^2) - 2/(3*a*b) + (16*b*x^2)/(3*a^3)))/(x^{(5/2)} + (a*x^{(3/2)})/b)$

sympy [B] time = 3.98, size = 219, normalized size = 3.48

$$-\frac{2a^3b^{\frac{9}{2}}\sqrt{\frac{a}{bx}+1}}{3a^5b^4x+6a^4b^5x^2+3a^3b^6x^3} + \frac{6a^2b^{\frac{11}{2}}x\sqrt{\frac{a}{bx}+1}}{3a^5b^4x+6a^4b^5x^2+3a^3b^6x^3} + \frac{24ab^{\frac{13}{2}}x^2\sqrt{\frac{a}{bx}+1}}{3a^5b^4x+6a^4b^5x^2+3a^3b^6x^3} + \frac{16b^{\frac{15}{2}}x^3\sqrt{\frac{a}{bx}}}{3a^5b^4x+6a^4b^5x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**(5/2)/(b*x+a)**(3/2),x)
```

```
[Out] -2*a**3*b**(9/2)*sqrt(a/(b*x) + 1)/(3*a**5*b**4*x + 6*a**4*b**5*x**2 + 3*a*  
*3*b**6*x**3) + 6*a**2*b**(11/2)*x*sqrt(a/(b*x) + 1)/(3*a**5*b**4*x + 6*a**  
4*b**5*x**2 + 3*a**3*b**6*x**3) + 24*a*b**(13/2)*x**2*sqrt(a/(b*x) + 1)/(3*  
a**5*b**4*x + 6*a**4*b**5*x**2 + 3*a**3*b**6*x**3) + 16*b**(15/2)*x**3*sqrt  
(a/(b*x) + 1)/(3*a**5*b**4*x + 6*a**4*b**5*x**2 + 3*a**3*b**6*x**3)
```

$$3.583 \quad \int \frac{1}{x^{7/2}(a+bx)^{3/2}} dx$$

Optimal. Leaf size=87

$$-\frac{32b^2\sqrt{a+bx}}{5a^4\sqrt{x}} + \frac{16b\sqrt{a+bx}}{5a^3x^{3/2}} - \frac{12\sqrt{a+bx}}{5a^2x^{5/2}} + \frac{2}{ax^{5/2}\sqrt{a+bx}}$$

[Out] $2/a/x^{(5/2)}/(b*x+a)^{(1/2)}-12/5*(b*x+a)^{(1/2)}/a^2/x^{(5/2)}+16/5*b*(b*x+a)^{(1/2)}/a^3/x^{(3/2)}-32/5*b^2*(b*x+a)^{(1/2)}/a^4/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 87, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{32b^2\sqrt{a+bx}}{5a^4\sqrt{x}} + \frac{16b\sqrt{a+bx}}{5a^3x^{3/2}} - \frac{12\sqrt{a+bx}}{5a^2x^{5/2}} + \frac{2}{ax^{5/2}\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(7/2)*(a + b*x)^(3/2)), x]

[Out] $2/(a*x^{(5/2)}*Sqrt[a + b*x]) - (12*Sqrt[a + b*x])/(5*a^2*x^{(5/2)}) + (16*b*Sqrt[a + b*x])/(5*a^3*x^{(3/2)}) - (32*b^2*Sqrt[a + b*x])/(5*a^4*Sqrt[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{7/2}(a+bx)^{3/2}} dx &= \frac{2}{ax^{5/2}\sqrt{a+bx}} + \frac{6 \int \frac{1}{x^{7/2}\sqrt{a+bx}} dx}{a} \\
&= \frac{2}{ax^{5/2}\sqrt{a+bx}} - \frac{12\sqrt{a+bx}}{5a^2x^{5/2}} - \frac{(24b) \int \frac{1}{x^{5/2}\sqrt{a+bx}} dx}{5a^2} \\
&= \frac{2}{ax^{5/2}\sqrt{a+bx}} - \frac{12\sqrt{a+bx}}{5a^2x^{5/2}} + \frac{16b\sqrt{a+bx}}{5a^3x^{3/2}} + \frac{(16b^2) \int \frac{1}{x^{3/2}\sqrt{a+bx}} dx}{5a^3} \\
&= \frac{2}{ax^{5/2}\sqrt{a+bx}} - \frac{12\sqrt{a+bx}}{5a^2x^{5/2}} + \frac{16b\sqrt{a+bx}}{5a^3x^{3/2}} - \frac{32b^2\sqrt{a+bx}}{5a^4\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 49, normalized size = 0.56

$$\frac{2(a^3 - 2a^2bx + 8ab^2x^2 + 16b^3x^3)}{5a^4x^{5/2}\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(7/2)*(a + b*x)^(3/2)),x]

[Out] (-2*(a^3 - 2*a^2*b*x + 8*a*b^2*x^2 + 16*b^3*x^3))/(5*a^4*x^(5/2)*Sqrt[a + b*x])

fricas [A] time = 0.42, size = 58, normalized size = 0.67

$$\frac{2(16b^3x^3 + 8ab^2x^2 - 2a^2bx + a^3)\sqrt{bx+a}\sqrt{x}}{5(a^4bx^4 + a^5x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] -2/5*(16*b^3*x^3 + 8*a*b^2*x^2 - 2*a^2*b*x + a^3)*sqrt(b*x + a)*sqrt(x)/(a^4*b*x^4 + a^5*x^3)

giac [A] time = 1.21, size = 121, normalized size = 1.39

$$\frac{4b^{\frac{9}{2}}}{\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2+ab\right)a^3|b|} - \frac{2\left(\frac{15b^6}{a^2|b|}+(bx+a)\left(\frac{11(bx+a)b^6}{a^4|b|}-\frac{25b^6}{a^3|b|}\right)\right)\sqrt{bx+a}}{5((bx+a)b-ab)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+a)^(3/2),x, algorithm="giac")

[Out] $-4*b^{9/2}/(((\sqrt{b*x+a}*\sqrt{b}-\sqrt{(b*x+a)*b-a*b})^2+a*b)*a^3*abs(b))-2/5*(15*b^6/(a^2*abs(b))+b*x+a)*(11*(b*x+a)*b^6/(a^4*abs(b))-25*b^6/(a^3*abs(b))))*\sqrt{b*x+a}/((b*x+a)*b-a*b)^{5/2}$

maple [A] time = 0.00, size = 44, normalized size = 0.51

$$\frac{2(16b^3x^3 + 8ab^2x^2 - 2a^2bx + a^3)}{5\sqrt{bx+a}a^4x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(7/2)/(b*x+a)^(3/2),x)

[Out] $-2/5*(16*b^3*x^3+8*a*b^2*x^2-2*a^2*b*x+a^3)/(b*x+a)^{1/2}/x^{5/2}/a^4$

maxima [A] time = 1.31, size = 64, normalized size = 0.74

$$\frac{2b^3\sqrt{x}}{\sqrt{bx+a}a^4} - \frac{2\left(\frac{15\sqrt{bx+a}b^2}{\sqrt{x}} - \frac{5(bx+a)^{\frac{3}{2}}b}{x^{\frac{3}{2}}} + \frac{(bx+a)^{\frac{5}{2}}}{x^{\frac{5}{2}}}\right)}{5a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] $-2*b^3*\sqrt{x}/(\sqrt{b*x+a})*a^4 - 2/5*(15*\sqrt{b*x+a}*b^2/\sqrt{x} - 5*(b*x+a)^{3/2}*b/x^{3/2} + (b*x+a)^{5/2}/x^{5/2})/a^4$

mupad [B] time = 0.43, size = 58, normalized size = 0.67

$$\frac{\sqrt{a+bx}\left(\frac{2}{5ab} - \frac{4x}{5a^2} + \frac{16bx^2}{5a^3} + \frac{32b^2x^3}{5a^4}\right)}{x^{7/2} + \frac{ax^{5/2}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(7/2)*(a+b*x)^(3/2)),x)

[Out] $-((a+b*x)^{1/2}*(2/(5*a*b) - (4*x)/(5*a^2) + (16*b*x^2)/(5*a^3) + (32*b^2*x^3)/(5*a^4)))/(x^{7/2} + (a*x^{5/2})/b)$

sympy [B] time = 11.15, size = 348, normalized size = 4.00

$$\frac{2a^5b^{\frac{19}{2}}\sqrt{\frac{a}{bx}+1}}{5a^7b^9x^2+15a^6b^{10}x^3+15a^5b^{11}x^4+5a^4b^{12}x^5} - \frac{10a^3b^{\frac{23}{2}}x^2\sqrt{\frac{a}{bx}+1}}{5a^7b^9x^2+15a^6b^{10}x^3+15a^5b^{11}x^4+5a^4b^{12}x^5} - \frac{60a^2}{5a^7b^9x^2+15a^6b^{10}x^3+15a^5b^{11}x^4+5a^4b^{12}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(7/2)/(b*x+a)**(3/2),x)

[Out]
$$\begin{aligned} & -2a^{5/2}b^{19/2}\sqrt{a/(bx)+1}/(5a^{7/2}b^9x^2+15a^6b^{10}x^3 \\ & +15a^5b^{11}x^4+5a^4b^{12}x^5) - 10a^{3/2}b^{23/2}x^2\sqrt{a/(bx)+1}/(5a^{7/2}b^9x^2 \\ & +15a^6b^{10}x^3+15a^5b^{11}x^4+5a^4b^{12}x^5) - 60a^2b^{25/2}x^3\sqrt{a/(bx)+1}/(5a^{7/2}b^9x^2 \\ & +15a^6b^{10}x^3+15a^5b^{11}x^4+5a^4b^{12}x^5) - 80ab^{27/2}x^4\sqrt{a/(bx)+1}/(5a^{7/2}b^9x^2 \\ & +15a^6b^{10}x^3+15a^5b^{11}x^4+5a^4b^{12}x^5) - 32b^{29/2}x^5\sqrt{a/(bx)+1}/(5a^{7/2}b^9x^2 \\ & +15a^6b^{10}x^3+15a^5b^{11}x^4+5a^4b^{12}x^5) \end{aligned}$$

$$3.584 \quad \int \frac{x^{5/2}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=91

$$-\frac{5a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{7/2}} + \frac{5\sqrt{x}\sqrt{a+bx}}{b^3} - \frac{10x^{3/2}}{3b^2\sqrt{a+bx}} - \frac{2x^{5/2}}{3b(a+bx)^{3/2}}$$

[Out] $-2/3*x^{(5/2)}/b/(b*x+a)^{(3/2)}-5*a*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(7/2)}-10/3*x^{(3/2)}/b^2/(b*x+a)^{(1/2)}+5*x^{(1/2)}*(b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.03, antiderivative size = 91, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {47, 50, 63, 217, 206}

$$-\frac{10x^{3/2}}{3b^2\sqrt{a+bx}} + \frac{5\sqrt{x}\sqrt{a+bx}}{b^3} - \frac{5a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{7/2}} - \frac{2x^{5/2}}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(5/2)}/(a + b*x)^{(5/2)}, x]$

[Out] $(-2*x^{(5/2)})/(3*b*(a + b*x)^{(3/2)}) - (10*x^{(3/2)})/(3*b^2*\operatorname{Sqrt}[a + b*x]) + (5*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[a + b*x])/b^3 - (5*a*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/ \operatorname{Sqrt}[a + b*x]])/b^{(7/2)}$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{NeQ}[m + n + 1, 0]$ && $!(\operatorname{IGtQ}[m, 0] \&\& (\operatorname{IntegerQ}[n] \mid\mid (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m - n, 0])))$ && $!\operatorname{ILtQ}[m + n + 2, 0]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(a+bx)^{5/2}} dx &= -\frac{2x^{5/2}}{3b(a+bx)^{3/2}} + \frac{5 \int \frac{x^{3/2}}{(a+bx)^{3/2}} dx}{3b} \\
&= -\frac{2x^{5/2}}{3b(a+bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{a+bx}} + \frac{5 \int \frac{\sqrt{x}}{\sqrt{a+bx}} dx}{b^2} \\
&= -\frac{2x^{5/2}}{3b(a+bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{a+bx}} + \frac{5\sqrt{x}\sqrt{a+bx}}{b^3} - \frac{(5a) \int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx}{2b^3} \\
&= -\frac{2x^{5/2}}{3b(a+bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{a+bx}} + \frac{5\sqrt{x}\sqrt{a+bx}}{b^3} - \frac{(5a) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right)}{b^3} \\
&= -\frac{2x^{5/2}}{3b(a+bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{a+bx}} + \frac{5\sqrt{x}\sqrt{a+bx}}{b^3} - \frac{(5a) \operatorname{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right)}{b^3} \\
&= -\frac{2x^{5/2}}{3b(a+bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{a+bx}} + \frac{5\sqrt{x}\sqrt{a+bx}}{b^3} - \frac{5a \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.55

$$\frac{2x^{7/2}\sqrt{\frac{bx}{a}+1} {}_2F_1\left(\frac{5}{2}, \frac{7}{2}; \frac{9}{2}; -\frac{bx}{a}\right)}{7a^2\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/(a + b*x)^(5/2), x]

[Out] (2*x^(7/2)*Sqrt[1 + (b*x)/a]*Hypergeometric2F1[5/2, 7/2, 9/2, -(b*x)/a])/ (7*a^2*Sqrt[a + b*x])

fricas [A] time = 0.45, size = 214, normalized size = 2.35

$$\left[\frac{15(ab^2x^2 + 2a^2bx + a^3)\sqrt{b} \log(2bx - 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) + 2(3b^3x^2 + 20ab^2x + 15a^2b)\sqrt{bx+a}\sqrt{x}}{6(b^6x^2 + 2ab^5x + a^2b^4)}, \frac{15}{6} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] [1/6*(15*(a*b^2*x^2 + 2*a^2*b*x + a^3)*sqrt(b)*log(2*b*x - 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) + 2*(3*b^3*x^2 + 20*a*b^2*x + 15*a^2*b)*sqrt(b*x + a)*sqrt(x))/(b^6*x^2 + 2*a*b^5*x + a^2*b^4), 1/3*(15*(a*b^2*x^2 + 2*a^2*b*x + a^3)*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x))) + (3*b^3*x^2 + 20*a*b^2*x + 15*a^2*b)*sqrt(b*x + a)*sqrt(x))/(b^6*x^2 + 2*a*b^5*x + a^2*b^4)]

giac [B] time = 92.46, size = 197, normalized size = 2.16

$$\left(\frac{15a \log\left(\frac{\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}}{b}\right)^2}{b^2} + \frac{6\sqrt{(bx+a)b-ab}\sqrt{bx+a}}{b^3} + \frac{8\left(9a^2(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab})^4\sqrt{b}+12a^3(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab})\right)}{\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2+ab\right)^3} \right) \frac{1}{6b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^(5/2), x, algorithm="giac")

[Out] 1/6*(15*a*log((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2)/b^(5/2) + 6*sqrt((b*x + a)*b - a*b)*sqrt(b*x + a)/b^3 + 8*(9*a^2*(sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^4*sqrt(b) + 12*a^3*(sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2*b^(3/2) + 7*a^4*b^(5/2))/(((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2 + a*b)^3*abs(b)/b^2)

maple [B] time = 0.05, size = 147, normalized size = 1.62

$$\frac{\left(-\frac{5a \ln\left(\frac{bx+\frac{a}{2}+\sqrt{bx^2+ax}}{\sqrt{b}}\right)}{2b^{\frac{7}{2}}} - \frac{2\sqrt{-(x+\frac{a}{b})a+(x+\frac{a}{b})^2b} a^2}{3(x+\frac{a}{b})^2 b^5} + \frac{14\sqrt{-(x+\frac{a}{b})a+(x+\frac{a}{b})^2b} a}{3(x+\frac{a}{b})b^4} \right) \sqrt{(bx+a)x}}{\sqrt{bx+a} \sqrt{x}} + \frac{\sqrt{bx+a} \sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x+a)^(5/2), x)

[Out] x^(1/2)*(b*x+a)^(1/2)/b^3+(-5/2/b^(7/2)*a*ln((b*x+1/2*a)/b^(1/2)+(b*x^2+a*x)^(1/2))+14/3/b^4*a/(x+a/b)*(-(x+a/b)*a+(x+a/b)^2*b)^(1/2)-2/3/b^5*a^2/(x+a/b)^2*(-(x+a/b)*a+(x+a/b)^2*b)^(1/2))*((b*x+a)*x)^(1/2)/(b*x+a)^(1/2)/x^(1/2)

maxima [A] time = 2.94, size = 109, normalized size = 1.20

$$\frac{2ab^2 + \frac{10(bx+a)ab}{x} - \frac{15(bx+a)^2a}{x^2}}{3\left(\frac{(bx+a)^{\frac{3}{2}}b^4}{x^{\frac{3}{2}}} - \frac{(bx+a)^{\frac{5}{2}}b^3}{x^{\frac{5}{2}}}\right)} + \frac{5a \log\left(-\frac{\sqrt{b}-\sqrt{bx+a}}{\sqrt{x}}\right)}{2b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+a)^(5/2), x, algorithm="maxima")

[Out] 1/3*(2*a*b^2 + 10*(b*x + a)*a*b/x - 15*(b*x + a)^2*a/x^2)/((b*x + a)^(3/2)*b^4/x^(3/2) - (b*x + a)^(5/2)*b^3/x^(5/2)) + 5/2*a*log(-(sqrt(b) - sqrt(b*x + a))/sqrt(x))/(sqrt(b) + sqrt(b*x + a)/sqrt(x))/b^(7/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{(a + bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(a + b*x)^(5/2), x)

[Out] int(x^(5/2)/(a + b*x)^(5/2), x)

sympy [B] time = 7.61, size = 396, normalized size = 4.35

$$\frac{15a^{\frac{81}{2}}b^{22}x^{\frac{51}{2}}\sqrt{1+\frac{bx}{a}}\operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{3a^{\frac{79}{2}}b^{\frac{51}{2}}x^{\frac{51}{2}}\sqrt{1+\frac{bx}{a}}+3a^{\frac{77}{2}}b^{\frac{53}{2}}x^{\frac{53}{2}}\sqrt{1+\frac{bx}{a}}}-\frac{15a^{\frac{79}{2}}b^{23}x^{\frac{53}{2}}\sqrt{1+\frac{bx}{a}}\operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{3a^{\frac{79}{2}}b^{\frac{51}{2}}x^{\frac{51}{2}}\sqrt{1+\frac{bx}{a}}+3a^{\frac{77}{2}}b^{\frac{53}{2}}x^{\frac{53}{2}}\sqrt{1+\frac{bx}{a}}}+\frac{15a^{40}}{3a^{\frac{79}{2}}b^{\frac{51}{2}}x^{\frac{51}{2}}\sqrt{1+\frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(b*x+a)**(5/2),x)

[Out] $-15*a^{81/2}*b^{22}*x^{51/2}*sqrt(1 + b*x/a)*asinh(sqrt(b)*sqrt(x)/sqrt(a)) / (3*a^{79/2}*b^{51/2}*x^{51/2}*sqrt(1 + b*x/a) + 3*a^{77/2}*b^{53/2}*x^{53/2}*sqrt(1 + b*x/a)) - 15*a^{79/2}*b^{23}*x^{53/2}*sqrt(1 + b*x/a)*asinh(sqrt(b)*sqrt(x)/sqrt(a)) / (3*a^{79/2}*b^{51/2}*x^{51/2}*sqrt(1 + b*x/a) + 3*a^{77/2}*b^{53/2}*x^{53/2}*sqrt(1 + b*x/a)) + 15*a^{40}*b^{45/2}*x^{26} / (3*a^{79/2}*b^{51/2}*x^{51/2}*sqrt(1 + b*x/a) + 3*a^{77/2}*b^{53/2}*x^{53/2}*sqrt(1 + b*x/a)) + 20*a^{39}*b^{47/2}*x^{27} / (3*a^{79/2}*b^{51/2}*x^{51/2}*sqrt(1 + b*x/a) + 3*a^{77/2}*b^{53/2}*x^{53/2}*sqrt(1 + b*x/a)) + 3*a^{38}*b^{49/2}*x^{28} / (3*a^{79/2}*b^{51/2}*x^{51/2}*sqrt(1 + b*x/a) + 3*a^{77/2}*b^{53/2}*x^{53/2}*sqrt(1 + b*x/a))$

$$3.585 \quad \int \frac{x^{3/2}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=69

$$\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{5/2}} - \frac{2\sqrt{x}}{b^2\sqrt{a+bx}} - \frac{2x^{3/2}}{3b(a+bx)^{3/2}}$$

[Out] $-2/3*x^{(3/2)}/b/(b*x+a)^{(3/2)}+2*\operatorname{arctanh}(b^{(1/2)}*x^{(1/2)}/(b*x+a)^{(1/2)})/b^{(5/2)}-2*x^{(1/2)}/b^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 63, 217, 206}

$$-\frac{2\sqrt{x}}{b^2\sqrt{a+bx}} + \frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{5/2}} - \frac{2x^{3/2}}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(3/2)}/(a+b*x)^{(5/2)}, x]$

[Out] $(-2*x^{(3/2)})/(3*b*(a+b*x)^{(3/2)}) - (2*\operatorname{Sqrt}[x])/(b^2*\operatorname{Sqrt}[a+b*x]) + (2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[a+b*x]])/b^{(5/2)}$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{GtQ}[n, 0] \ \&\& \operatorname{LtQ}[m, -1] \ \&\& \operatorname{IntegerQ}[n] \ \&\& \operatorname{IntegerQ}[m] \ \&\& \operatorname{IntegerQ}[m + n + 2, 0] \ \&\& (\operatorname{FractionQ}[m] \ || \operatorname{GeQ}[2*n + m + 1, 0]) \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{LtQ}[-1, m, 0] \ \&\& \operatorname{LeQ}[-1, n, 0] \ \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{3/2}}{(a+bx)^{5/2}} dx &= -\frac{2x^{3/2}}{3b(a+bx)^{3/2}} + \frac{\int \frac{\sqrt{x}}{(a+bx)^{3/2}} dx}{b} \\
&= -\frac{2x^{3/2}}{3b(a+bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{a+bx}} + \frac{\int \frac{1}{\sqrt{x}\sqrt{a+bx}} dx}{b^2} \\
&= -\frac{2x^{3/2}}{3b(a+bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{a+bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a+bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\
&= -\frac{2x^{3/2}}{3b(a+bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{a+bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{1-bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a+bx}}\right)}{b^2} \\
&= -\frac{2x^{3/2}}{3b(a+bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{a+bx}} + \frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a+bx}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.12, size = 80, normalized size = 1.16

$$\frac{6\sqrt{a}(a+bx)\sqrt{\frac{bx}{a}+1} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) - 2\sqrt{b}\sqrt{x}(3a+4bx)}{3b^{5/2}(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(3/2)/(a + b*x)^(5/2), x]
```

```
[Out] (-2*Sqrt[b]*Sqrt[x]*(3*a + 4*b*x) + 6*Sqrt[a]*(a + b*x)*Sqrt[1 + (b*x)/a]*A
rcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(3*b^(5/2)*(a + b*x)^(3/2))
```

fricas [A] time = 0.48, size = 186, normalized size = 2.70

$$\left[\frac{3(b^2x^2 + 2abx + a^2)\sqrt{b} \log(2bx + 2\sqrt{bx+a}\sqrt{b}\sqrt{x} + a) - 2(4b^2x + 3ab)\sqrt{bx+a}\sqrt{x}}{3(b^5x^2 + 2ab^4x + a^2b^3)}, -\frac{2(3(b^2x^2 + 2abx -$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^(5/2),x, algorithm="fricas")

[Out] [1/3*(3*(b^2*x^2 + 2*a*b*x + a^2)*sqrt(b)*log(2*b*x + 2*sqrt(b*x + a)*sqrt(b)*sqrt(x) + a) - 2*(4*b^2*x + 3*a*b)*sqrt(b*x + a)*sqrt(x))/(b^5*x^2 + 2*a*b^4*x + a^2*b^3), -2/3*(3*(b^2*x^2 + 2*a*b*x + a^2)*sqrt(-b)*arctan(sqrt(b*x + a)*sqrt(-b)/(b*sqrt(x)))) + (4*b^2*x + 3*a*b)*sqrt(b*x + a)*sqrt(x)/(b^5*x^2 + 2*a*b^4*x + a^2*b^3)]

giac [B] time = 105.59, size = 165, normalized size = 2.39

$$\left(\frac{3 \log\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2\right)}{\sqrt{b}} + \frac{8\left(3a\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^4\sqrt{b}+3a^2\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2b^{\frac{3}{2}}+2a^3b^{\frac{5}{2}}\right)}{\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2+ab\right)^3} \right) |b|$$

$$3b^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^(5/2),x, algorithm="giac")

[Out] -1/3*(3*log((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2)/sqrt(b) + 8*(3*a*(sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^4*sqrt(b) + 3*a^2*(sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2*b^(3/2) + 2*a^3*b^(5/2))/((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2 + a*b)^3)*abs(b)/b^3

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{x^{\frac{3}{2}}}{(bx+a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(b*x+a)^(5/2),x)

[Out] int(x^(3/2)/(b*x+a)^(5/2),x)

maxima [A] time = 2.83, size = 69, normalized size = 1.00

$$\frac{2 \left(b + \frac{3(bx+a)}{x} \right) x^{\frac{3}{2}}}{3(bx+a)^{\frac{3}{2}} b^2} - \frac{\log \left(-\frac{\sqrt{b} - \frac{\sqrt{bx+a}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+a}}{\sqrt{x}}} \right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] $-2/3*(b + 3*(b*x + a)/x)*x^{3/2}/((b*x + a)^{3/2}*b^2) - \log(-(\text{sqrt}(b) - \text{sqrt}(b*x + a)/\text{sqrt}(x))/(\text{sqrt}(b) + \text{sqrt}(b*x + a)/\text{sqrt}(x)))/b^{5/2}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{3/2}}{(a + bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(a + b*x)^(5/2),x)

[Out] int(x^(3/2)/(a + b*x)^(5/2), x)

sympy [B] time = 4.03, size = 328, normalized size = 4.75

$$\frac{6a^{\frac{39}{2}} b^{11} x^{\frac{27}{2}} \sqrt{1 + \frac{bx}{a}} \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{3a^{\frac{39}{2}} b^{\frac{27}{2}} x^{\frac{27}{2}} \sqrt{1 + \frac{bx}{a}} + 3a^{\frac{37}{2}} b^{\frac{29}{2}} x^{\frac{29}{2}} \sqrt{1 + \frac{bx}{a}}} + \frac{6a^{\frac{37}{2}} b^{12} x^{\frac{29}{2}} \sqrt{1 + \frac{bx}{a}} \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{3a^{\frac{39}{2}} b^{\frac{27}{2}} x^{\frac{27}{2}} \sqrt{1 + \frac{bx}{a}} + 3a^{\frac{37}{2}} b^{\frac{29}{2}} x^{\frac{29}{2}} \sqrt{1 + \frac{bx}{a}}} - \frac{6a^{19} b^2}{3a^{\frac{39}{2}} b^{\frac{27}{2}} x^{\frac{27}{2}} \sqrt{1 + \frac{bx}{a}} + 3a^{\frac{37}{2}} b^{\frac{29}{2}} x^{\frac{29}{2}} \sqrt{1 + \frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)/(b*x+a)**(5/2),x)

[Out] $6*a^{39/2}*b^{11}*x^{27/2}*\text{sqrt}(1 + b*x/a)*\text{asinh}(\text{sqrt}(b)*\text{sqrt}(x)/\text{sqrt}(a))/ (3*a^{39/2}*b^{27/2}*x^{27/2}*\text{sqrt}(1 + b*x/a) + 3*a^{37/2}*b^{29/2}*x^{29/2}*\text{sqrt}(1 + b*x/a)) + 6*a^{37/2}*b^{12}*x^{29/2}*\text{sqrt}(1 + b*x/a)*\text{asinh}(\text{sqrt}(b)*\text{sqrt}(x)/\text{sqrt}(a))/ (3*a^{39/2}*b^{27/2}*x^{27/2}*\text{sqrt}(1 + b*x/a) + 3*a^{37/2}*b^{29/2}*x^{29/2}*\text{sqrt}(1 + b*x/a)) - 6*a^{19}*b^{23/2}*x^{14}/ (3*a^{39/2}*b^{27/2}*x^{27/2}*\text{sqrt}(1 + b*x/a) + 3*a^{37/2}*b^{29/2}*x^{29/2}*\text{sqrt}(1 + b*x/a)) - 8*a^{18}*b^{25/2}*x^{15}/ (3*a^{39/2}*b^{27/2}*x^{27/2}*\text{sqrt}(1 + b*x/a) + 3*a^{37/2}*b^{29/2}*x^{29/2}*\text{sqrt}(1 + b*x/a))$

$$3.586 \quad \int \frac{\sqrt{x}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=21

$$\frac{2x^{3/2}}{3a(a+bx)^{3/2}}$$

[Out] $2/3*x^{(3/2)}/a/(b*x+a)^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$\frac{2x^{3/2}}{3a(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(a + b*x)^(5/2), x]

[Out] $(2*x^{(3/2)})/(3*a*(a + b*x)^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{x}}{(a+bx)^{5/2}} dx = \frac{2x^{3/2}}{3a(a+bx)^{3/2}}$$

Mathematica [A] time = 0.00, size = 21, normalized size = 1.00

$$\frac{2x^{3/2}}{3a(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(a + b*x)^(5/2), x]

[Out] $(2*x^{(3/2)})/(3*a*(a + b*x)^{(3/2)})$

fricas [B] time = 0.43, size = 33, normalized size = 1.57

$$\frac{2\sqrt{bx+a}x^{\frac{3}{2}}}{3(ab^2x^2+2a^2bx+a^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^(5/2),x, algorithm="fricas")

[Out] 2/3*sqrt(b*x + a)*x^(3/2)/(a*b^2*x^2 + 2*a^2*b*x + a^3)

giac [B] time = 1.63, size = 86, normalized size = 4.10

$$\frac{4\left(3\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^4\sqrt{b}+a^2b^{\frac{5}{2}}\right)|b|}{3\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2+ab\right)^3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^(5/2),x, algorithm="giac")

[Out] 4/3*(3*(sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^4*sqrt(b) + a^2*b^(5/2))*abs(b)/(((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2 + a*b)^3*b^2)

maple [A] time = 0.00, size = 16, normalized size = 0.76

$$\frac{2x^{\frac{3}{2}}}{3(bx+a)^{\frac{3}{2}}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x+a)^(5/2),x)

[Out] 2/3*x^(3/2)/a/(b*x+a)^(3/2)

maxima [A] time = 1.33, size = 15, normalized size = 0.71

$$\frac{2x^{\frac{3}{2}}}{3(bx+a)^{\frac{3}{2}}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] $2/3*x^{3/2}/((b*x + a)^{3/2}*a)$

mupad [B] time = 0.24, size = 36, normalized size = 1.71

$$\frac{2x^{3/2}\sqrt{a+bx}}{3(a^3+2a^2bx+ab^2x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{1/2}/(a + b*x)^{5/2}, x)$

[Out] $(2*x^{3/2}*(a + b*x)^{1/2})/(3*(a^3 + a*b^2*x^2 + 2*a^2*b*x))$

sympy [B] time = 1.43, size = 42, normalized size = 2.00

$$\frac{2x^{\frac{3}{2}}}{3a^{\frac{5}{2}}\sqrt{1 + \frac{bx}{a}} + 3a^{\frac{3}{2}}bx\sqrt{1 + \frac{bx}{a}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{1/2}/(b*x+a)^{5/2}, x)$

[Out] $2*x^{3/2}/(3*a^{5/2}*sqrt(1 + b*x/a) + 3*a^{3/2}*b*x*sqrt(1 + b*x/a))$

$$3.587 \quad \int \frac{1}{\sqrt{x}(a+bx)^{5/2}} dx$$

Optimal. Leaf size=43

$$\frac{4\sqrt{x}}{3a^2\sqrt{a+bx}} + \frac{2\sqrt{x}}{3a(a+bx)^{3/2}}$$

[Out] $2/3*x^{(1/2)}/a/(b*x+a)^{(3/2)}+4/3*x^{(1/2)}/a^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{4\sqrt{x}}{3a^2\sqrt{a+bx}} + \frac{2\sqrt{x}}{3a(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(a + b*x)^(5/2)),x]

[Out] (2*Sqrt[x])/(3*a*(a + b*x)^(3/2)) + (4*Sqrt[x])/(3*a^2*Sqrt[a + b*x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{\sqrt{x}(a+bx)^{5/2}} dx = \frac{2\sqrt{x}}{3a(a+bx)^{3/2}} + \frac{2 \int \frac{1}{\sqrt{x}(a+bx)^{3/2}} dx}{3a}$$

$$= \frac{2\sqrt{x}}{3a(a+bx)^{3/2}} + \frac{4\sqrt{x}}{3a^2\sqrt{a+bx}}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 0.67

$$\frac{2\sqrt{x}(3a+2bx)}{3a^2(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(a + b*x)^(5/2)),x]

[Out] (2*Sqrt[x]*(3*a + 2*b*x))/(3*a^2*(a + b*x)^(3/2))

fricas [A] time = 0.44, size = 43, normalized size = 1.00

$$\frac{2(2bx+3a)\sqrt{bx+a}\sqrt{x}}{3(a^2b^2x^2+2a^3bx+a^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/x^(1/2),x, algorithm="fricas")

[Out] 2/3*(2*b*x + 3*a)*sqrt(b*x + a)*sqrt(x)/(a^2*b^2*x^2 + 2*a^3*b*x + a^4)

giac [B] time = 1.50, size = 81, normalized size = 1.88

$$\frac{8 \left(3 \left(\sqrt{bx+a} \sqrt{b} - \sqrt{(bx+a)b-ab} \right)^2 + ab \right) b^{\frac{5}{2}}}{3 \left(\left(\sqrt{bx+a} \sqrt{b} - \sqrt{(bx+a)b-ab} \right)^2 + ab \right)^3 |b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/x^(1/2),x, algorithm="giac")

[Out] 8/3*(3*(sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2 + a*b)*b^(5/2)/((sqrt(b*x + a)*sqrt(b) - sqrt((b*x + a)*b - a*b))^2 + a*b)^3*abs(b)

maple [A] time = 0.00, size = 24, normalized size = 0.56

$$\frac{2(2bx + 3a)\sqrt{x}}{3(bx + a)^{\frac{3}{2}}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(5/2)/x^(1/2),x)`

[Out] `2/3*x^(1/2)*(2*b*x+3*a)/(b*x+a)^(3/2)/a^2`

maxima [A] time = 1.34, size = 27, normalized size = 0.63

$$\frac{2\left(b - \frac{3(bx+a)}{x}\right)x^{\frac{3}{2}}}{3(bx + a)^{\frac{3}{2}}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/2)/x^(1/2),x, algorithm="maxima")`

[Out] `-2/3*(b - 3*(b*x + a)/x)*x^(3/2)/((b*x + a)^(3/2)*a^2)`

mupad [B] time = 0.40, size = 54, normalized size = 1.26

$$\frac{6a\sqrt{x}\sqrt{a+bx} + 4bx^{3/2}\sqrt{a+bx}}{3a^4 + 6a^3bx + 3a^2b^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(a + b*x)^(5/2)),x)`

[Out] `(6*a*x^(1/2)*(a + b*x)^(1/2) + 4*b*x^(3/2)*(a + b*x)^(1/2))/(3*a^4 + 3*a^2*b^2*x^2 + 6*a^3*b*x)`

sympy [B] time = 1.90, size = 92, normalized size = 2.14

$$\frac{6a}{3a^3\sqrt{b}\sqrt{\frac{a}{bx}+1} + 3a^2b^{\frac{3}{2}}x\sqrt{\frac{a}{bx}+1}} + \frac{4bx}{3a^3\sqrt{b}\sqrt{\frac{a}{bx}+1} + 3a^2b^{\frac{3}{2}}x\sqrt{\frac{a}{bx}+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/2)/x**(1/2),x)`

[Out] `6*a/(3*a**3*sqrt(b)*sqrt(a/(b*x) + 1) + 3*a**2*b**(3/2)*x*sqrt(a/(b*x) + 1)) + 4*b*x/(3*a**3*sqrt(b)*sqrt(a/(b*x) + 1) + 3*a**2*b**(3/2)*x*sqrt(a/(b*x) + 1))`

$$3.588 \quad \int \frac{1}{x^{3/2}(a+bx)^{5/2}} dx$$

Optimal. Leaf size=64

$$-\frac{16\sqrt{a+bx}}{3a^3\sqrt{x}} + \frac{8}{3a^2\sqrt{x}\sqrt{a+bx}} + \frac{2}{3a\sqrt{x}(a+bx)^{3/2}}$$

[Out] $2/3/a/(b*x+a)^{(3/2)}/x^{(1/2)}+8/3/a^2/x^{(1/2)}/(b*x+a)^{(1/2)}-16/3*(b*x+a)^{(1/2)}/a^3/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{16\sqrt{a+bx}}{3a^3\sqrt{x}} + \frac{8}{3a^2\sqrt{x}\sqrt{a+bx}} + \frac{2}{3a\sqrt{x}(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(a + b*x)^(5/2)),x]

[Out] $2/(3*a*\text{Sqrt}[x]*(a + b*x)^{(3/2)}) + 8/(3*a^2*\text{Sqrt}[x]*\text{Sqrt}[a + b*x]) - (16*\text{Sqrt}[a + b*x])/(3*a^3*\text{Sqrt}[x])$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
  implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{3/2}(a+bx)^{5/2}} dx &= \frac{2}{3a\sqrt{x}(a+bx)^{3/2}} + \frac{4 \int \frac{1}{x^{3/2}(a+bx)^{3/2}} dx}{3a} \\
&= \frac{2}{3a\sqrt{x}(a+bx)^{3/2}} + \frac{8}{3a^2\sqrt{x}\sqrt{a+bx}} + \frac{8 \int \frac{1}{x^{3/2}\sqrt{a+bx}} dx}{3a^2} \\
&= \frac{2}{3a\sqrt{x}(a+bx)^{3/2}} + \frac{8}{3a^2\sqrt{x}\sqrt{a+bx}} - \frac{16\sqrt{a+bx}}{3a^3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 0.62

$$\frac{2(3a^2 + 12abx + 8b^2x^2)}{3a^3\sqrt{x}(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(a + b*x)^(5/2)), x]

[Out] (-2*(3*a^2 + 12*a*b*x + 8*b^2*x^2))/(3*a^3*Sqrt[x]*(a + b*x)^(3/2))

fricas [A] time = 0.43, size = 58, normalized size = 0.91

$$-\frac{2(8b^2x^2 + 12abx + 3a^2)\sqrt{bx+a}\sqrt{x}}{3(a^3b^2x^3 + 2a^4bx^2 + a^5x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] -2/3*(8*b^2*x^2 + 12*a*b*x + 3*a^2)*sqrt(b*x + a)*sqrt(x)/(a^3*b^2*x^3 + 2*a^4*b*x^2 + a^5*x)

giac [B] time = 1.63, size = 159, normalized size = 2.48

$$\frac{2\sqrt{bx+a}b^2}{\sqrt{(bx+a)b-ab}a^3|b|} - \frac{4\left(3\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^4b^{\frac{5}{2}}+12a\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2b^{\frac{7}{2}}\right)}{3\left(\left(\sqrt{bx+a}\sqrt{b}-\sqrt{(bx+a)b-ab}\right)^2+ab\right)^3a^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+a)^(5/2), x, algorithm="giac")

[Out] $-2\sqrt{bx+a}b^2/(\sqrt{(bx+a)b-ab})a^3\text{abs}(b) - 4/3(3(\sqrt{bx+a}\sqrt{b} - \sqrt{(bx+a)b-ab})^4b^{5/2} + 12a(\sqrt{bx+a}\sqrt{b} - \sqrt{(bx+a)b-ab})^2b^{7/2} + 5a^2b^{9/2})/((\sqrt{bx+a}\sqrt{b} - \sqrt{(bx+a)b-ab})^2 + a^2\text{abs}(b))$

maple [A] time = 0.01, size = 35, normalized size = 0.55

$$\frac{2(8b^2x^2 + 12abx + 3a^2)}{3(bx+a)^{\frac{3}{2}}a^3\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/x^{3/2}/(bx+a)^{5/2}, x)$

[Out] $-2/3(8b^2x^2+12a*b*x+3a^2)/(bx+a)^{3/2}/x^{1/2}/a^3$

maxima [A] time = 1.34, size = 46, normalized size = 0.72

$$\frac{2\left(b^2 - \frac{6(bx+a)b}{x}\right)x^{\frac{3}{2}}}{3(bx+a)^{\frac{3}{2}}a^3} - \frac{2\sqrt{bx+a}}{a^3\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^{3/2}/(bx+a)^{5/2}, x, \text{algorithm}="maxima")$

[Out] $2/3(b^2 - 6*(bx+a)*b/x)*x^{3/2}/((bx+a)^{3/2}*a^3) - 2*\sqrt{bx+a}/(a^3*\sqrt{x})$

mupad [B] time = 0.42, size = 71, normalized size = 1.11

$$\frac{6a^2\sqrt{a+bx} + 16b^2x^2\sqrt{a+bx} + 24abx\sqrt{a+bx}}{\sqrt{x}(x(6a^4b + 3xa^3b^2) + 3a^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(x^{3/2}*(a+bx)^{5/2}), x)$

[Out] $-(6a^2*(a+bx)^{1/2} + 16b^2*x^2*(a+bx)^{1/2} + 24*a*b*x*(a+bx)^{1/2})/(x^{1/2}*(x*(6a^4*b + 3a^3*b^2*x) + 3a^5))$

sympy [B] time = 3.97, size = 153, normalized size = 2.39

$$\frac{6a^2b^{\frac{9}{2}}\sqrt{\frac{a}{bx}+1}}{3a^5b^4+6a^4b^5x+3a^3b^6x^2} - \frac{24ab^{\frac{11}{2}}x\sqrt{\frac{a}{bx}+1}}{3a^5b^4+6a^4b^5x+3a^3b^6x^2} - \frac{16b^{\frac{13}{2}}x^2\sqrt{\frac{a}{bx}+1}}{3a^5b^4+6a^4b^5x+3a^3b^6x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**(3/2)/(b*x+a)**(5/2),x)
```

```
[Out] -6*a**2*b**(9/2)*sqrt(a/(b*x) + 1)/(3*a**5*b**4 + 6*a**4*b**5*x + 3*a**3*b*  
*6*x**2) - 24*a*b**(11/2)*x*sqrt(a/(b*x) + 1)/(3*a**5*b**4 + 6*a**4*b**5*x  
+ 3*a**3*b**6*x**2) - 16*b**(13/2)*x**2*sqrt(a/(b*x) + 1)/(3*a**5*b**4 + 6*  
a**4*b**5*x + 3*a**3*b**6*x**2)
```

$$3.589 \quad \int \frac{1}{x^{5/2}(a+bx)^{5/2}} dx$$

Optimal. Leaf size=84

$$\frac{32b\sqrt{a+bx}}{3a^4\sqrt{x}} - \frac{16\sqrt{a+bx}}{3a^3x^{3/2}} + \frac{4}{a^2x^{3/2}\sqrt{a+bx}} + \frac{2}{3ax^{3/2}(a+bx)^{3/2}}$$

[Out] $2/3/a/x^{(3/2)}/(b*x+a)^{(3/2)}+4/a^2/x^{(3/2)}/(b*x+a)^{(1/2)}-16/3*(b*x+a)^{(1/2)}/a^3/x^{(3/2)}+32/3*b*(b*x+a)^{(1/2)}/a^4/x^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{16\sqrt{a+bx}}{3a^3x^{3/2}} + \frac{4}{a^2x^{3/2}\sqrt{a+bx}} + \frac{32b\sqrt{a+bx}}{3a^4\sqrt{x}} + \frac{2}{3ax^{3/2}(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(a + b*x)^(5/2)), x]

[Out] $2/(3*a*x^{(3/2)}*(a + b*x)^{(3/2)}) + 4/(a^2*x^{(3/2)}*Sqrt[a + b*x]) - (16*Sqrt[a + b*x])/(3*a^3*x^{(3/2)}) + (32*b*Sqrt[a + b*x])/(3*a^4*Sqrt[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{5/2}(a+bx)^{5/2}} dx &= \frac{2}{3ax^{3/2}(a+bx)^{3/2}} + \frac{2 \int \frac{1}{x^{5/2}(a+bx)^{3/2}} dx}{a} \\
&= \frac{2}{3ax^{3/2}(a+bx)^{3/2}} + \frac{4}{a^2x^{3/2}\sqrt{a+bx}} + \frac{8 \int \frac{1}{x^{5/2}\sqrt{a+bx}} dx}{a^2} \\
&= \frac{2}{3ax^{3/2}(a+bx)^{3/2}} + \frac{4}{a^2x^{3/2}\sqrt{a+bx}} - \frac{16\sqrt{a+bx}}{3a^3x^{3/2}} - \frac{(16b) \int \frac{1}{x^{3/2}\sqrt{a+bx}} dx}{3a^3} \\
&= \frac{2}{3ax^{3/2}(a+bx)^{3/2}} + \frac{4}{a^2x^{3/2}\sqrt{a+bx}} - \frac{16\sqrt{a+bx}}{3a^3x^{3/2}} + \frac{32b\sqrt{a+bx}}{3a^4\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 49, normalized size = 0.58

$$-\frac{2(a^3 - 6a^2bx - 24ab^2x^2 - 16b^3x^3)}{3a^4x^{3/2}(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(a + b*x)^(5/2)),x]

[Out] (-2*(a^3 - 6*a^2*b*x - 24*a*b^2*x^2 - 16*b^3*x^3))/(3*a^4*x^(3/2)*(a + b*x)^(3/2))

fricas [A] time = 0.44, size = 71, normalized size = 0.85

$$\frac{2(16b^3x^3 + 24ab^2x^2 + 6a^2bx - a^3)\sqrt{bx+a}\sqrt{x}}{3(a^4b^2x^4 + 2a^5bx^3 + a^6x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^(5/2),x, algorithm="fricas")

[Out] 2/3*(16*b^3*x^3 + 24*a*b^2*x^2 + 6*a^2*b*x - a^3)*sqrt(b*x + a)*sqrt(x)/(a^4*b^2*x^4 + 2*a^5*b*x^3 + a^6*x^2)

giac [B] time = 2.24, size = 175, normalized size = 2.08

$$\frac{2\sqrt{bx+a}\left(\frac{8(bx+a)b^2|b|}{a^4} - \frac{9b^2|b|}{a^3}\right)}{3((bx+a)b-ab)^{\frac{3}{2}}} + \frac{8\left(3\left(\sqrt{bx+a}\sqrt{b} - \sqrt{(bx+a)b-ab}\right)^4 b^{\frac{7}{2}} + 9a\left(\sqrt{bx+a}\sqrt{b} - \sqrt{(bx+a)b-ab}\right)\right)}{3\left(\left(\sqrt{bx+a}\sqrt{b} - \sqrt{(bx+a)b-ab}\right)^2 + ab\right)^3 a^3|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^(5/2),x, algorithm="giac")

[Out] $\frac{2}{3}\sqrt{b*x+a}*(8*(b*x+a)*b^2*abs(b)/a^4 - 9*b^2*abs(b)/a^3)/((b*x+a)*b - a*b)^(3/2) + 8/3*(3*(sqrt(b*x+a)*sqrt(b) - sqrt((b*x+a)*b - a*b))^4*b^(7/2) + 9*a*(sqrt(b*x+a)*sqrt(b) - sqrt((b*x+a)*b - a*b))^2*b^(9/2) + 4*a^2*b^(11/2))/(((sqrt(b*x+a)*sqrt(b) - sqrt((b*x+a)*b - a*b))^2 + a*b)^3*a^3*abs(b))$

maple [A] time = 0.00, size = 44, normalized size = 0.52

$$-\frac{2(-16b^3x^3 - 24ab^2x^2 - 6a^2bx + a^3)}{3(bx+a)^{\frac{3}{2}}a^4x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(5/2)/(b*x+a)^(5/2),x)

[Out] $-2/3*(-16*b^3*x^3-24*a*b^2*x^2-6*a^2*b*x+a^3)/(b*x+a)^(3/2)/x^(3/2)/a^4$

maxima [A] time = 1.27, size = 64, normalized size = 0.76

$$\frac{2\left(\frac{9\sqrt{bx+a}b}{\sqrt{x}} - \frac{(bx+a)^{\frac{3}{2}}}{x^2}\right)}{3a^4} - \frac{2\left(b^3 - \frac{9(bx+a)b^2}{x}\right)x^{\frac{3}{2}}}{3(bx+a)^{\frac{3}{2}}a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] $\frac{2}{3}*(9*sqrt(b*x+a)*b/sqrt(x) - (b*x+a)^(3/2)/x^(3/2))/a^4 - 2/3*(b^3 - 9*(b*x+a)*b^2/x)*x^(3/2)/((b*x+a)^(3/2)*a^4)$

mupad [B] time = 0.47, size = 88, normalized size = 1.05

$$\frac{32b^3x^3\sqrt{a+bx} - 2a^3\sqrt{a+bx} + 12a^2bx\sqrt{a+bx} + 48ab^2x^2\sqrt{a+bx}}{x^{3/2}(x(6a^5b + 3xa^4b^2) + 3a^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(5/2)*(a+b*x)^(5/2)),x)

[Out] $(32*b^3*x^3*(a+b*x)^(1/2) - 2*a^3*(a+b*x)^(1/2) + 12*a^2*b*x*(a+b*x)^(1/2) + 48*a*b^2*x^2*(a+b*x)^(1/2))/(x^(3/2)*(x*(6*a^5*b + 3*a^4*b^2*x) + 3*a^6))$

sympy [B] time = 7.06, size = 337, normalized size = 4.01

$$\frac{2a^4b^{\frac{19}{2}}\sqrt{\frac{a}{bx}+1}}{3a^7b^9x+9a^6b^{10}x^2+9a^5b^{11}x^3+3a^4b^{12}x^4} + \frac{10a^3b^{\frac{21}{2}}x\sqrt{\frac{a}{bx}+1}}{3a^7b^9x+9a^6b^{10}x^2+9a^5b^{11}x^3+3a^4b^{12}x^4} + \frac{60a^2b^{\frac{23}{2}}x^2}{3a^7b^9x+9a^6b^{10}x^2+9a^5b^{11}x^3+3a^4b^{12}x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(5/2)/(b*x+a)**(5/2),x)

[Out] $-2*a^{**4}*b^{**\frac{19}{2}}*\text{sqrt}(a/(b*x) + 1)/(3*a^{**7}*b^{**9}*x + 9*a^{**6}*b^{**10}*x^{**2} + 9*a^{**5}*b^{**11}*x^{**3} + 3*a^{**4}*b^{**12}*x^{**4}) + 10*a^{**3}*b^{**\frac{21}{2}}*x*\text{sqrt}(a/(b*x) + 1)/(3*a^{**7}*b^{**9}*x + 9*a^{**6}*b^{**10}*x^{**2} + 9*a^{**5}*b^{**11}*x^{**3} + 3*a^{**4}*b^{**12}*x^{**4}) + 60*a^{**2}*b^{**\frac{23}{2}}*x^{**2}*\text{sqrt}(a/(b*x) + 1)/(3*a^{**7}*b^{**9}*x + 9*a^{**6}*b^{**10}*x^{**2} + 9*a^{**5}*b^{**11}*x^{**3} + 3*a^{**4}*b^{**12}*x^{**4}) + 80*a*b^{**\frac{25}{2}}*x^{**3}*\text{sqrt}(a/(b*x) + 1)/(3*a^{**7}*b^{**9}*x + 9*a^{**6}*b^{**10}*x^{**2} + 9*a^{**5}*b^{**11}*x^{**3} + 3*a^{**4}*b^{**12}*x^{**4}) + 32*b^{**\frac{27}{2}}*x^{**4}*\text{sqrt}(a/(b*x) + 1)/(3*a^{**7}*b^{**9}*x + 9*a^{**6}*b^{**10}*x^{**2} + 9*a^{**5}*b^{**11}*x^{**3} + 3*a^{**4}*b^{**12}*x^{**4})$

$$3.590 \quad \int \frac{x^{5/2}}{\sqrt{a-bx}} dx$$

Optimal. Leaf size=105

$$\frac{5a^3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{8b^{7/2}} - \frac{5a^2\sqrt{x}\sqrt{a-bx}}{8b^3} - \frac{5ax^{3/2}\sqrt{a-bx}}{12b^2} - \frac{x^{5/2}\sqrt{a-bx}}{3b}$$

[Out] $5/8*a^3*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(7/2)}-5/12*a*x^{(3/2)}*(-b*x+a)^{(1/2)/b^2-1/3*x^{(5/2)}*(-b*x+a)^{(1/2)/b-5/8*a^2*x^{(1/2)}*(-b*x+a)^{(1/2)/b^3}$

Rubi [A] time = 0.03, antiderivative size = 105, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$-\frac{5a^2\sqrt{x}\sqrt{a-bx}}{8b^3} + \frac{5a^3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{8b^{7/2}} - \frac{5ax^{3/2}\sqrt{a-bx}}{12b^2} - \frac{x^{5/2}\sqrt{a-bx}}{3b}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)/Sqrt[a - b*x], x]

[Out] $(-5*a^2*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(8*b^3) - (5*a*x^{(3/2)}*\text{Sqrt}[a - b*x])/(12*b^2) - (x^{(5/2)}*\text{Sqrt}[a - b*x])/(3*b) + (5*a^3*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(8*b^{(7/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```


Rule 203

$\text{Int}[(a_ + (b_ \cdot)(x_)^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(1 \cdot \text{ArcTan}[\text{Rt}[b, 2] \cdot x] / \text{Rt}[a, 2]]) / (\text{Rt}[a, 2] \cdot \text{Rt}[b, 2]), x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{PosQ}[a/b] \ \&\& \ (\text{GtQ}[a, 0] \ || \ \text{GtQ}[b, 0])$

Rule 217

$\text{Int}[1/\text{Sqrt}[(a_ + (b_ \cdot)(x_)^2)], x_Symbol] \rightarrow \text{Subst}[\text{Int}[1/(1 - b \cdot x^2), x], x, x/\text{Sqrt}[a + b \cdot x^2]] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
 \int \frac{x^{5/2}}{\sqrt{a-bx}} dx &= -\frac{x^{5/2}\sqrt{a-bx}}{3b} + \frac{(5a) \int \frac{x^{3/2}}{\sqrt{a-bx}} dx}{6b} \\
 &= -\frac{5ax^{3/2}\sqrt{a-bx}}{12b^2} - \frac{x^{5/2}\sqrt{a-bx}}{3b} + \frac{(5a^2) \int \frac{\sqrt{x}}{\sqrt{a-bx}} dx}{8b^2} \\
 &= -\frac{5a^2\sqrt{x}\sqrt{a-bx}}{8b^3} - \frac{5ax^{3/2}\sqrt{a-bx}}{12b^2} - \frac{x^{5/2}\sqrt{a-bx}}{3b} + \frac{(5a^3) \int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx}{16b^3} \\
 &= -\frac{5a^2\sqrt{x}\sqrt{a-bx}}{8b^3} - \frac{5ax^{3/2}\sqrt{a-bx}}{12b^2} - \frac{x^{5/2}\sqrt{a-bx}}{3b} + \frac{(5a^3) \text{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x}\right)}{8b^3} \\
 &= -\frac{5a^2\sqrt{x}\sqrt{a-bx}}{8b^3} - \frac{5ax^{3/2}\sqrt{a-bx}}{12b^2} - \frac{x^{5/2}\sqrt{a-bx}}{3b} + \frac{(5a^3) \text{Subst}\left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right)}{8b^3} \\
 &= -\frac{5a^2\sqrt{x}\sqrt{a-bx}}{8b^3} - \frac{5ax^{3/2}\sqrt{a-bx}}{12b^2} - \frac{x^{5/2}\sqrt{a-bx}}{3b} + \frac{5a^3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{8b^{7/2}}
 \end{aligned}$$

Mathematica [A] time = 0.15, size = 88, normalized size = 0.84

$$\frac{\sqrt{a-bx} \left(\frac{15a^{5/2} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{\sqrt{1-\frac{bx}{a}}} - \sqrt{b}\sqrt{x} (15a^2 + 10abx + 8b^2x^2) \right)}{24b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/Sqrt[a - b*x], x]

[Out] $(\sqrt{a - bx}) * (-(\sqrt{b} * \sqrt{x}) * (15a^2 + 10abx + 8b^2x^2)) + (15a^{5/2} * \text{ArcSin}[(\sqrt{b} * \sqrt{x}) / \sqrt{a}]) / \sqrt{1 - (bx/a)}) / (24b^{7/2})$

fricas [A] time = 0.46, size = 141, normalized size = 1.34

$$\left[\frac{15a^3\sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) + 2(8b^3x^2 + 10ab^2x + 15a^2b)\sqrt{-bx+a}\sqrt{x}}{48b^4}, -\frac{15a^3\sqrt{b} \arctan\left(\frac{\sqrt{-bx+a}\sqrt{x}}{\sqrt{b}\sqrt{x}}\right)}{48b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/2)/(-b*x+a)^(1/2),x, algorithm="fricas")`

[Out] $[-1/48 * (15a^3 * \sqrt{-b} * \log(-2bx + 2\sqrt{-bx+a} * \sqrt{-b} * \sqrt{x} + a) + 2 * (8b^3x^2 + 10ab^2x + 15a^2b) * \sqrt{-bx+a} * \sqrt{x}) / b^4, -1/24 * (15a^3 * \sqrt{b} * \arctan(\sqrt{-bx+a} / (\sqrt{b} * \sqrt{x}))) + (8b^3x^2 + 10ab^2x + 15a^2b) * \sqrt{-bx+a} * \sqrt{x}) / b^4]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/2)/(-b*x+a)^(1/2),x, algorithm="giac")`

[Out] Timed out

maple [A] time = 0.01, size = 108, normalized size = 1.03

$$-\frac{\sqrt{-bx+a} x^{\frac{5}{2}}}{3b} - \frac{5\sqrt{-bx+a} a x^{\frac{3}{2}}}{12b^2} + \frac{5\sqrt{-bx+a} x a^3 \arctan\left(\frac{(x-\frac{a}{2b})\sqrt{b}}{\sqrt{-bx+a}}\right)}{16\sqrt{-bx+a} b^{\frac{7}{2}}\sqrt{x}} - \frac{5\sqrt{-bx+a} a^2\sqrt{x}}{8b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/2)/(-b*x+a)^(1/2),x)`

[Out] $-1/3 * x^{5/2} * (-bx+a)^{1/2} / b - 5/12 * a * x^{3/2} * (-bx+a)^{1/2} / b^2 - 5/8 * a^2 * x^{1/2} * (-bx+a)^{1/2} / b^3 + 5/16 * a^3 / b^{7/2} * ((-bx+a) * x)^{1/2} / x^{1/2} / (-bx+a)^{1/2} * \arctan((x - 1/2 * a/b) / (-bx^2 + a * x)^{1/2} * b^{1/2})$

maxima [A] time = 2.96, size = 135, normalized size = 1.29

$$-\frac{5a^3 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{8b^{\frac{7}{2}}} - \frac{\frac{33\sqrt{-bx+a}a^3b^2}{\sqrt{x}} + \frac{40(-bx+a)^{\frac{3}{2}}a^3b}{x^{\frac{3}{2}}} + \frac{15(-bx+a)^{\frac{5}{2}}a^3}{x^{\frac{5}{2}}}}{24\left(b^6 - \frac{3(bx-a)b^5}{x} + \frac{3(bx-a)^2b^4}{x^2} - \frac{(bx-a)^3b^3}{x^3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+a)^(1/2),x, algorithm="maxima")

[Out]
$$-5/8*a^3*\arctan(\sqrt{-b*x+a}/(\sqrt{b}*\sqrt{x}))/b^{7/2} - 1/24*(33*\sqrt{-b*x+a}*a^3*b^2/\sqrt{x} + 40*(-b*x+a)^{3/2}*a^3*b/x^{3/2} + 15*(-b*x+a)^{5/2}*a^3/x^{5/2})/(b^6 - 3*(b*x-a)*b^5/x + 3*(b*x-a)^2*b^4/x^2 - (b*x-a)^3*b^3/x^3)$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{\sqrt{a-bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(a-b*x)^(1/2),x)

[Out] int(x^(5/2)/(a-b*x)^(1/2), x)

sympy [A] time = 8.43, size = 270, normalized size = 2.57

$$\left\{ \begin{array}{l} \frac{5ia^2\sqrt{x}}{8b^3\sqrt{-1+\frac{bx}{a}}} - \frac{5ia^2x^{\frac{3}{2}}}{24b^2\sqrt{-1+\frac{bx}{a}}} - \frac{i\sqrt{a}x^{\frac{5}{2}}}{12b\sqrt{-1+\frac{bx}{a}}} - \frac{5ia^3\operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8b^{\frac{7}{2}}} - \frac{ix^{\frac{7}{2}}}{3\sqrt{a}\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{5a^2\sqrt{x}}{8b^3\sqrt{1-\frac{bx}{a}}} + \frac{5a^2x^{\frac{3}{2}}}{24b^2\sqrt{1-\frac{bx}{a}}} + \frac{\sqrt{a}x^{\frac{5}{2}}}{12b\sqrt{1-\frac{bx}{a}}} + \frac{5a^3\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{8b^{\frac{7}{2}}} + \frac{x^{\frac{7}{2}}}{3\sqrt{a}\sqrt{1-\frac{bx}{a}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(-b*x+a)**(1/2),x)

[Out] Piecewise((5*I*a**(5/2)*sqrt(x)/(8*b**3*sqrt(-1 + b*x/a)) - 5*I*a**(3/2)*x**(3/2)/(24*b**2*sqrt(-1 + b*x/a)) - I*sqrt(a)*x**(5/2)/(12*b*sqrt(-1 + b*x/a)) - 5*I*a**3*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(8*b**(7/2)) - I*x**(7/2)/(3*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (-5*a**(5/2)*sqrt(x)/(8*b**3*sqrt(1 - b*x/a)) + 5*a**(3/2)*x**(3/2)/(24*b**2*sqrt(1 - b*x/a)) + sqrt(a)*x**(5/2)/(12*b*sqrt(1 - b*x/a)) + 5*a**3*asin(sqrt(b)*sqrt(x)/sqrt(a))/(8*b**(7/2)) + x**(7/2)/(3*sqrt(a)*sqrt(1 - b*x/a)), True))

$$3.591 \quad \int \frac{x^{3/2}}{\sqrt{a-bx}} dx$$

Optimal. Leaf size=80

$$\frac{3a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^{5/2}} - \frac{3a\sqrt{x}\sqrt{a-bx}}{4b^2} - \frac{x^{3/2}\sqrt{a-bx}}{2b}$$

[Out] $3/4*a^2*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(5/2)}-1/2*x^{(3/2)}*(-b*x+a)^{(1/2)/b}-3/4*a*x^{(1/2)}*(-b*x+a)^{(1/2)/b^2}$

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$\frac{3a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^{5/2}} - \frac{3a\sqrt{x}\sqrt{a-bx}}{4b^2} - \frac{x^{3/2}\sqrt{a-bx}}{2b}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)/Sqrt[a - b*x], x]

[Out] $(-3*a*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(4*b^2) - (x^{(3/2)}*\text{Sqrt}[a - b*x])/(2*b) + (3*a^2*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(4*b^{(5/2)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{x^{3/2}}{\sqrt{a-bx}} dx &= -\frac{x^{3/2}\sqrt{a-bx}}{2b} + \frac{(3a) \int \frac{\sqrt{x}}{\sqrt{a-bx}} dx}{4b} \\
 &= -\frac{3a\sqrt{x}\sqrt{a-bx}}{4b^2} - \frac{x^{3/2}\sqrt{a-bx}}{2b} + \frac{(3a^2) \int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx}{8b^2} \\
 &= -\frac{3a\sqrt{x}\sqrt{a-bx}}{4b^2} - \frac{x^{3/2}\sqrt{a-bx}}{2b} + \frac{(3a^2) \text{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x}\right)}{4b^2} \\
 &= -\frac{3a\sqrt{x}\sqrt{a-bx}}{4b^2} - \frac{x^{3/2}\sqrt{a-bx}}{2b} + \frac{(3a^2) \text{Subst}\left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^2} \\
 &= -\frac{3a\sqrt{x}\sqrt{a-bx}}{4b^2} - \frac{x^{3/2}\sqrt{a-bx}}{2b} + \frac{3a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.05, size = 86, normalized size = 1.08

$$\frac{3a^{5/2}\sqrt{1-\frac{bx}{a}}\sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) + \sqrt{b}\sqrt{x}(-3a^2 + abx + 2b^2x^2)}{4b^{5/2}\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/Sqrt[a - b*x], x]

[Out] (Sqrt[b]*Sqrt[x]*(-3*a^2 + a*b*x + 2*b^2*x^2) + 3*a^(5/2)*Sqrt[1 - (b*x)/a]*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(4*b^(5/2)*Sqrt[a - b*x])

fricas [A] time = 0.46, size = 119, normalized size = 1.49

$$\left[\frac{3 a^2 \sqrt{-b} \log(-2 b x + 2 \sqrt{-b x + a} \sqrt{-b} \sqrt{x} + a) + 2 (2 b^2 x + 3 a b) \sqrt{-b x + a} \sqrt{x}}{8 b^3}, -\frac{3 a^2 \sqrt{b} \arctan\left(\frac{\sqrt{-b x + a}}{\sqrt{b} \sqrt{x}}\right) +}{4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+a)^(1/2),x, algorithm="fricas")

[Out] [-1/8*(3*a^2*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) + 2*(2*b^2*x + 3*a*b)*sqrt(-b*x + a)*sqrt(x))/b^3, -1/4*(3*a^2*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) + (2*b^2*x + 3*a*b)*sqrt(-b*x + a)*sqrt(x))/b^3]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 89, normalized size = 1.11

$$-\frac{\sqrt{-b x + a} x^{\frac{3}{2}}}{2 b} + \frac{3 \sqrt{(-b x + a) x} a^2 \arctan\left(\frac{(x - \frac{a}{2 b}) \sqrt{b}}{\sqrt{-b x^2 + a x}}\right)}{8 \sqrt{-b x + a} b^{\frac{5}{2}} \sqrt{x}} - \frac{3 \sqrt{-b x + a} a \sqrt{x}}{4 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(-b*x+a)^(1/2),x)

[Out] -1/2*x^(3/2)*(-b*x+a)^(1/2)/b-3/4*a*x^(1/2)*(-b*x+a)^(1/2)/b^2+3/8*a^2/b^(5/2)*((-b*x+a)*x)^(1/2)/x^(1/2)/(-b*x+a)^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))

maxima [A] time = 2.96, size = 98, normalized size = 1.22

$$-\frac{3 a^2 \arctan\left(\frac{\sqrt{-b x + a}}{\sqrt{b} \sqrt{x}}\right)}{4 b^{\frac{5}{2}}} - \frac{\frac{5 \sqrt{-b x + a} a^2 b}{\sqrt{x}} + \frac{3 (-b x + a)^{\frac{3}{2}} a^2}{x^{\frac{3}{2}}}}{4 \left(b^4 - \frac{2 (b x - a) b^3}{x} + \frac{(b x - a)^2 b^2}{x^2} \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)/(-b*x+a)^(1/2),x, algorithm="maxima")`

[Out]
$$-3/4*a^2*\arctan(\sqrt{-b*x+a}/(\sqrt{b}*\sqrt{x}))/b^{5/2} - 1/4*(5*\sqrt{-b*x+a}*a^2*b/\sqrt{x} + 3*(-b*x+a)^{3/2}*a^2/x^{3/2})/(b^4 - 2*(b*x-a)*b^3/x + (b*x-a)^2*b^2/x^2)$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{3/2}}{\sqrt{a-bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(a-b*x)^(1/2),x)`

[Out] `int(x^(3/2)/(a-b*x)^(1/2), x)`

sympy [A] time = 4.30, size = 214, normalized size = 2.68

$$\left\{ \begin{array}{l} \frac{3ia^2\sqrt{x}}{4b^2\sqrt{-1+\frac{bx}{a}}} - \frac{i\sqrt{a}x^{\frac{3}{2}}}{4b\sqrt{-1+\frac{bx}{a}}} - \frac{3ia^2\operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{\frac{5}{2}}} - \frac{ix^{\frac{5}{2}}}{2\sqrt{a}\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{3a^2\sqrt{x}}{4b^2\sqrt{1-\frac{bx}{a}}} + \frac{\sqrt{a}x^{\frac{3}{2}}}{4b\sqrt{1-\frac{bx}{a}}} + \frac{3a^2\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{\frac{5}{2}}} + \frac{x^{\frac{5}{2}}}{2\sqrt{a}\sqrt{1-\frac{bx}{a}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(-b*x+a)**(1/2),x)`

[Out] `Piecewise((3*I*a**(3/2)*sqrt(x)/(4*b**2*sqrt(-1 + b*x/a)) - I*sqrt(a)*x**(3/2)/(4*b*sqrt(-1 + b*x/a)) - 3*I*a**2*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(4*b**(5/2)) - I*x**(5/2)/(2*sqrt(a)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (-3*a**(3/2)*sqrt(x)/(4*b**2*sqrt(1 - b*x/a)) + sqrt(a)*x**(3/2)/(4*b*sqrt(1 - b*x/a)) + 3*a**2*asin(sqrt(b)*sqrt(x)/sqrt(a))/(4*b**(5/2)) + x**(5/2)/(2*sqrt(a)*sqrt(1 - b*x/a)), True))`

$$3.592 \quad \int \frac{\sqrt{x}}{\sqrt{a-bx}} dx$$

Optimal. Leaf size=50

$$\frac{a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{3/2}} - \frac{\sqrt{x}\sqrt{a-bx}}{b}$$

[Out] a*arctan(b^(1/2)*x^(1/2)/(-b*x+a)^(1/2))/b^(3/2)-x^(1/2)*(-b*x+a)^(1/2)/b

Rubi [A] time = 0.02, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {50, 63, 217, 203}

$$\frac{a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{3/2}} - \frac{\sqrt{x}\sqrt{a-bx}}{b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/Sqrt[a - b*x], x]

[Out] -((Sqrt[x]*Sqrt[a - b*x])/b) + (a*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a - b*x]])/b^(3/2)

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
```


, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{x}}{\sqrt{a-bx}} dx &= -\frac{\sqrt{x}\sqrt{a-bx}}{b} + \frac{a \int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx}{2b} \\ &= -\frac{\sqrt{x}\sqrt{a-bx}}{b} + \frac{a \operatorname{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x}\right)}{b} \\ &= -\frac{\sqrt{x}\sqrt{a-bx}}{b} + \frac{a \operatorname{Subst}\left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right)}{b} \\ &= -\frac{\sqrt{x}\sqrt{a-bx}}{b} + \frac{a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.04, size = 71, normalized size = 1.42

$$\frac{a^{3/2} \sqrt{1 - \frac{bx}{a}} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right) + \sqrt{b}\sqrt{x}(bx - a)}{b^{3/2} \sqrt{a - bx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/Sqrt[a - b*x], x]

[Out] (Sqrt[b]*Sqrt[x]*(-a + b*x) + a^(3/2)*Sqrt[1 - (b*x)/a]*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(b^(3/2)*Sqrt[a - b*x])

fricas [A] time = 0.45, size = 93, normalized size = 1.86

$$\left[-\frac{a\sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) + 2\sqrt{-bx+a}b\sqrt{x}}{2b^2}, -\frac{a\sqrt{b} \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right) + \sqrt{-bx+a}b\sqrt{x}}{b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+a)^(1/2),x, algorithm="fricas")

[Out] [-1/2*(a*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) + 2*sqrt(-b*x + a)*b*sqrt(x))/b^2, -(a*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) + sqrt(-b*x + a)*b*sqrt(x))/b^2]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.01, size = 70, normalized size = 1.40

$$\frac{\sqrt{-bx+a} x a \arctan\left(\frac{(x-\frac{a}{2b})\sqrt{b}}{\sqrt{-bx^2+ax}}\right)}{2\sqrt{-bx+a} b^{\frac{3}{2}} \sqrt{x}} - \frac{\sqrt{-bx+a} \sqrt{x}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(-b*x+a)^(1/2),x)

[Out] -x^(1/2)*(-b*x+a)^(1/2)/b+1/2*a/b^(3/2)*((-b*x+a)*x)^(1/2)/x^(1/2)/(-b*x+a)^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))

maxima [A] time = 3.00, size = 56, normalized size = 1.12

$$-\frac{a \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b} \sqrt{x}}\right)}{b^{\frac{3}{2}}} - \frac{\sqrt{-bx+a} a}{\left(b^2 - \frac{(bx-a)b}{x}\right) \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+a)^(1/2),x, algorithm="maxima")

[Out] -a*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/b^(3/2) - sqrt(-b*x + a)*a/((b^2 - (b*x - a)*b/x)*sqrt(x))

mupad [B] time = 0.52, size = 47, normalized size = 0.94

$$\frac{2 a \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a-bx}-\sqrt{a}}\right)}{b^{3/2}} - \frac{\sqrt{x} \sqrt{a-bx}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)/(a - b*x)^(1/2), x)`

[Out] $(2*a*atan((b^{1/2}*x^{1/2})/((a - b*x)^{1/2} - a^{1/2}))/b^{3/2} - (x^{1/2})*(a - b*x)^{1/2})/b$

sympy [A] time = 2.28, size = 121, normalized size = 2.42

$$\left\{ \begin{array}{ll} -\frac{i\sqrt{a}\sqrt{x}\sqrt{-1+\frac{bx}{a}}}{b} - \frac{ia \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{\frac{3}{2}}} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{\sqrt{a}\sqrt{x}}{b\sqrt{1-\frac{bx}{a}}} + \frac{a \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{\frac{3}{2}}} + \frac{x^{\frac{3}{2}}}{\sqrt{a}\sqrt{1-\frac{bx}{a}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)/(-b*x+a)**(1/2), x)`

[Out] `Piecewise((-I*sqrt(a)*sqrt(x)*sqrt(-1 + b*x/a)/b - I*a*acosh(sqrt(b)*sqrt(x)/sqrt(a))/b**(3/2), Abs(b*x/a) > 1), (-sqrt(a)*sqrt(x)/(b*sqrt(1 - b*x/a)) + a*asin(sqrt(b)*sqrt(x)/sqrt(a))/b**(3/2) + x**(3/2)/(sqrt(a)*sqrt(1 - b*x/a)), True)`

$$3.593 \quad \int \frac{1}{\sqrt{x} \sqrt{a-bx}} dx$$

Optimal. Leaf size=29

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a-bx}} \right)}{\sqrt{b}}$$

[Out] 2*arctan(b^(1/2)*x^(1/2)/(-b*x+a)^(1/2))/b^(1/2)

Rubi [A] time = 0.01, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {63, 217, 203}

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a-bx}} \right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*Sqrt[a - b*x]),x]

[Out] (2*ArcTan[(Sqrt[b]*Sqrt[x])/Sqrt[a - b*x]])/Sqrt[b]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt{x} \sqrt{a-bx}} dx &= 2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x} \right) \\
&= 2 \operatorname{Subst} \left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}} \right) \\
&= \frac{2 \tan^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a-bx}} \right)}{\sqrt{b}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 52, normalized size = 1.79

$$\frac{2\sqrt{a} \sqrt{1 - \frac{bx}{a}} \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}} \right)}{\sqrt{b} \sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*Sqrt[a - b*x]),x]

[Out] (2*Sqrt[a]*Sqrt[1 - (b*x)/a]*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(Sqrt[b]*Sqrt[a - b*x])

fricas [A] time = 0.43, size = 57, normalized size = 1.97

$$\left[-\frac{\sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a)}{b}, -\frac{2 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{b}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-b*x+a)^(1/2),x, algorithm="fricas")

[Out] [-sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a)/b, -2*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/sqrt(b)]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-b*x+a)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [B] time = 0.01, size = 51, normalized size = 1.76

$$\frac{\sqrt{(-bx+a)x} \arctan\left(\frac{(x-\frac{a}{2b})\sqrt{b}}{\sqrt{-bx^2+ax}}\right)}{\sqrt{-bx+a} \sqrt{b} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/2)/(-b*x+a)^(1/2),x)

[Out] ((-b*x+a)*x)^(1/2)/x^(1/2)/(-b*x+a)^(1/2)/b^(1/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))

maxima [A] time = 2.88, size = 21, normalized size = 0.72

$$-\frac{2 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b} \sqrt{x}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-b*x+a)^(1/2),x, algorithm="maxima")

[Out] -2*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/sqrt(b)

mupad [B] time = 0.03, size = 27, normalized size = 0.93

$$-\frac{4 \operatorname{atan}\left(\frac{\sqrt{a-bx}-\sqrt{a}}{\sqrt{b} \sqrt{x}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/2)*(a - b*x)^(1/2)),x)

[Out] -(4*atan(((a - b*x)^(1/2) - a^(1/2))/(b^(1/2)*x^(1/2))))/b^(1/2)

sympy [A] time = 1.15, size = 54, normalized size = 1.86

$$\begin{cases} -\frac{2i \operatorname{acosh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{b}} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ \frac{2 \operatorname{asin}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{\sqrt{b}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**(1/2)/(-b*x+a)**(1/2),x)
```

```
[Out] Piecewise((-2*I*acosh(sqrt(b)*sqrt(x)/sqrt(a))/sqrt(b), Abs(b*x/a) > 1), (2  
*asin(sqrt(b)*sqrt(x)/sqrt(a))/sqrt(b), True))
```

$$3.594 \quad \int \frac{1}{x^{3/2} \sqrt{a-bx}} dx$$

Optimal. Leaf size=20

$$-\frac{2\sqrt{a-bx}}{a\sqrt{x}}$$

[Out] $-2*(-b*x+a)^{(1/2)}/a/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {37}

$$-\frac{2\sqrt{a-bx}}{a\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*Sqrt[a - b*x]),x]

[Out] (-2*Sqrt[a - b*x])/(a*Sqrt[x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{3/2} \sqrt{a-bx}} dx = -\frac{2\sqrt{a-bx}}{a\sqrt{x}}$$

Mathematica [A] time = 0.00, size = 20, normalized size = 1.00

$$-\frac{2\sqrt{a-bx}}{a\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*Sqrt[a - b*x]),x]

[Out] (-2*Sqrt[a - b*x])/(a*Sqrt[x])

fricas [A] time = 0.43, size = 16, normalized size = 0.80

$$-\frac{2\sqrt{-bx+a}}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+a)^(1/2),x, algorithm="fricas")

[Out] -2*sqrt(-b*x + a)/(a*sqrt(x))

giac [B] time = 1.28, size = 35, normalized size = 1.75

$$-\frac{2\sqrt{-bx+a}b^2}{\sqrt{(bx-a)b+ab}a|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+a)^(1/2),x, algorithm="giac")

[Out] -2*sqrt(-b*x + a)*b^2/(sqrt((b*x - a)*b + a*b)*a*abs(b))

maple [A] time = 0.00, size = 17, normalized size = 0.85

$$-\frac{2\sqrt{-bx+a}}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2)/(-b*x+a)^(1/2),x)

[Out] -2*(-b*x+a)^(1/2)/a/x^(1/2)

maxima [A] time = 1.34, size = 16, normalized size = 0.80

$$-\frac{2\sqrt{-bx+a}}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+a)^(1/2),x, algorithm="maxima")

[Out] -2*sqrt(-b*x + a)/(a*sqrt(x))

mupad [B] time = 0.40, size = 16, normalized size = 0.80

$$-\frac{2\sqrt{a-bx}}{a\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(a - b*x)^(1/2)),x)`

[Out] `-(2*(a - b*x)^(1/2))/(a*x^(1/2))`

sympy [A] time = 0.97, size = 46, normalized size = 2.30

$$\begin{cases} -\frac{2\sqrt{b}\sqrt{\frac{a}{bx}-1}}{a} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ -\frac{2i\sqrt{b}\sqrt{-\frac{a}{bx}+1}}{a} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(-b*x+a)**(1/2),x)`

[Out] `Piecewise((-2*sqrt(b)*sqrt(a/(b*x) - 1)/a, Abs(a/(b*x)) > 1), (-2*I*sqrt(b)*sqrt(-a/(b*x) + 1)/a, True))`

$$3.595 \quad \int \frac{1}{x^{5/2} \sqrt{a-bx}} dx$$

Optimal. Leaf size=46

$$-\frac{4b\sqrt{a-bx}}{3a^2\sqrt{x}} - \frac{2\sqrt{a-bx}}{3ax^{3/2}}$$

[Out] $-2/3*(-b*x+a)^{(1/2)}/a/x^{(3/2)}-4/3*b*(-b*x+a)^{(1/2)}/a^2/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{4b\sqrt{a-bx}}{3a^2\sqrt{x}} - \frac{2\sqrt{a-bx}}{3ax^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*Sqrt[a - b*x]),x]

[Out] $(-2*\text{Sqrt}[a - b*x])/(3*a*x^{(3/2)}) - (4*b*\text{Sqrt}[a - b*x])/(3*a^2*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 $((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] /;$ FreeQ[{
a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 $((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] - \text{Dist}[(d*\text{S}$
 $\text{implify}[m + n + 2])/((b*c - a*d)*(m + 1)), \text{Int}[(a + b*x)^{\text{Simplify}[m + 1]}*(c$
 $+ d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{x^{5/2}\sqrt{a-bx}} dx = -\frac{2\sqrt{a-bx}}{3ax^{3/2}} + \frac{(2b) \int \frac{1}{x^{3/2}\sqrt{a-bx}} dx}{3a}$$

$$= -\frac{2\sqrt{a-bx}}{3ax^{3/2}} - \frac{4b\sqrt{a-bx}}{3a^2\sqrt{x}}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.61

$$-\frac{2\sqrt{a-bx}(a+2bx)}{3a^2x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*Sqrt[a - b*x]),x]

[Out] (-2*Sqrt[a - b*x]*(a + 2*b*x))/(3*a^2*x^(3/2))

fricas [A] time = 0.44, size = 22, normalized size = 0.48

$$-\frac{2(2bx+a)\sqrt{-bx+a}}{3a^2x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+a)^(1/2),x, algorithm="fricas")

[Out] -2/3*(2*b*x + a)*sqrt(-b*x + a)/(a^2*x^(3/2))

giac [A] time = 1.45, size = 54, normalized size = 1.17

$$-\frac{2\left(\frac{2(bx-a)b^3}{a^2} + \frac{3b^3}{a}\right)\sqrt{-bx+a}b}{3((bx-a)b+ab)^{\frac{3}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+a)^(1/2),x, algorithm="giac")

[Out] -2/3*(2*(b*x - a)*b^3/a^2 + 3*b^3/a)*sqrt(-b*x + a)*b/(((b*x - a)*b + a*b)^(3/2)*abs(b))

maple [A] time = 0.00, size = 23, normalized size = 0.50

$$-\frac{2\sqrt{-bx+a}(2bx+a)}{3a^2x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/2)/(-b*x+a)^(1/2),x)`

[Out] $-2/3*(-b*x+a)^{(1/2)}*(2*b*x+a)/x^{(3/2)}/a^2$

maxima [A] time = 1.30, size = 32, normalized size = 0.70

$$\frac{2 \left(\frac{3 \sqrt{-bx+a} b}{\sqrt{x}} + \frac{(-bx+a)^{\frac{3}{2}}}{x^{\frac{3}{2}}} \right)}{3 a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2)/(-b*x+a)^(1/2),x, algorithm="maxima")`

[Out] $-2/3*(3*\text{sqrt}(-b*x + a)*b/\text{sqrt}(x) + (-b*x + a)^{(3/2)}/x^{(3/2)})/a^2$

mupad [B] time = 0.35, size = 26, normalized size = 0.57

$$\frac{\left(\frac{2}{3a} + \frac{4bx}{3a^2} \right) \sqrt{a-bx}}{x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/2)*(a - b*x)^(1/2)),x)`

[Out] $-((2/(3*a) + (4*b*x)/(3*a^2))*(a - b*x)^{(1/2)})/x^{(3/2)}$

sympy [A] time = 2.06, size = 177, normalized size = 3.85

$$\begin{cases} -\frac{2\sqrt{b}\sqrt{\frac{a}{bx}-1}}{3ax} - \frac{4b^{\frac{3}{2}}\sqrt{\frac{a}{bx}-1}}{3a^2} & \text{for } \left| \frac{a}{bx} \right| > 1 \\ \frac{2ia^2b^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}}{-3a^3bx+3a^2b^2x^2} + \frac{2iab^{\frac{5}{2}}x\sqrt{-\frac{a}{bx}+1}}{-3a^3bx+3a^2b^2x^2} - \frac{4ib^{\frac{7}{2}}x^2\sqrt{-\frac{a}{bx}+1}}{-3a^3bx+3a^2b^2x^2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(-b*x+a)**(1/2),x)`

[Out] `Piecewise((-2*sqrt(b)*sqrt(a/(b*x) - 1)/(3*a*x) - 4*b**(3/2)*sqrt(a/(b*x) - 1)/(3*a**2), Abs(a/(b*x)) > 1), (2*I*a**2*b**(3/2)*sqrt(-a/(b*x) + 1)/(-3*a**3*b*x + 3*a**2*b**2*x**2) + 2*I*a*b**(5/2)*x*sqrt(-a/(b*x) + 1)/(-3*a**3*b*x + 3*a**2*b**2*x**2) - 4*I*b**(7/2)*x**2*sqrt(-a/(b*x) + 1)/(-3*a**3*b*x + 3*a**2*b**2*x**2), True))`

$$3.596 \quad \int \frac{x^{5/2}}{(a-bx)^{3/2}} dx$$

Optimal. Leaf size=100

$$-\frac{15a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^{7/2}} + \frac{15a\sqrt{x}\sqrt{a-bx}}{4b^3} + \frac{5x^{3/2}\sqrt{a-bx}}{2b^2} + \frac{2x^{5/2}}{b\sqrt{a-bx}}$$

[Out] $-15/4*a^2*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(7/2)}+2*x^{(5/2)}/b/(-b*x+a)^{(1/2)}+5/2*x^{(3/2)}*(-b*x+a)^{(1/2)}/b^2+15/4*a*x^{(1/2)}*(-b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.03, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.312$, Rules used = {47, 50, 63, 217, 203}

$$-\frac{15a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^{7/2}} + \frac{5x^{3/2}\sqrt{a-bx}}{2b^2} + \frac{15a\sqrt{x}\sqrt{a-bx}}{4b^3} + \frac{2x^{5/2}}{b\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(5/2)}/(a - b*x)^{(3/2)}, x]$

[Out] $(2*x^{(5/2)})/(b*\text{Sqrt}[a - b*x]) + (15*a*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/(4*b^3) + (5*x^{(3/2)}*\text{Sqrt}[a - b*x])/(2*b^2) - (15*a^2*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/(4*b^{(7/2)})$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(a-bx)^{3/2}} dx &= \frac{2x^{5/2}}{b\sqrt{a-bx}} - \frac{5 \int \frac{x^{3/2}}{\sqrt{a-bx}} dx}{b} \\
&= \frac{2x^{5/2}}{b\sqrt{a-bx}} + \frac{5x^{3/2}\sqrt{a-bx}}{2b^2} - \frac{(15a) \int \frac{\sqrt{x}}{\sqrt{a-bx}} dx}{4b^2} \\
&= \frac{2x^{5/2}}{b\sqrt{a-bx}} + \frac{15a\sqrt{x}\sqrt{a-bx}}{4b^3} + \frac{5x^{3/2}\sqrt{a-bx}}{2b^2} - \frac{(15a^2) \int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx}{8b^3} \\
&= \frac{2x^{5/2}}{b\sqrt{a-bx}} + \frac{15a\sqrt{x}\sqrt{a-bx}}{4b^3} + \frac{5x^{3/2}\sqrt{a-bx}}{2b^2} - \frac{(15a^2) \text{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x}\right)}{4b^3} \\
&= \frac{2x^{5/2}}{b\sqrt{a-bx}} + \frac{15a\sqrt{x}\sqrt{a-bx}}{4b^3} + \frac{5x^{3/2}\sqrt{a-bx}}{2b^2} - \frac{(15a^2) \text{Subst}\left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^3} \\
&= \frac{2x^{5/2}}{b\sqrt{a-bx}} + \frac{15a\sqrt{x}\sqrt{a-bx}}{4b^3} + \frac{5x^{3/2}\sqrt{a-bx}}{2b^2} - \frac{15a^2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{4b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 51, normalized size = 0.51

$$\frac{2x^{7/2} \sqrt{1 - \frac{bx}{a}} {}_2F_1\left(\frac{3}{2}, \frac{7}{2}, \frac{9}{2}, \frac{bx}{a}\right)}{7a\sqrt{a - bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/(a - b*x)^(3/2), x]

[Out] (2*x^(7/2)*Sqrt[1 - (b*x)/a]*Hypergeometric2F1[3/2, 7/2, 9/2, (b*x)/a])/(7*a*Sqrt[a - b*x])

fricas [A] time = 0.45, size = 181, normalized size = 1.81

$$\left[\frac{15(a^2bx - a^3)\sqrt{-b} \log(-2bx - 2\sqrt{-bx + a}\sqrt{-b}\sqrt{x} + a) - 2(2b^3x^2 + 5ab^2x - 15a^2b)\sqrt{-bx + a}\sqrt{x}}{8(b^5x - ab^4)}, \frac{15(a^2bx - a^3)\sqrt{-b} \log(-2bx - 2\sqrt{-bx + a}\sqrt{-b}\sqrt{x} + a) - 2(2b^3x^2 + 5ab^2x - 15a^2b)\sqrt{-bx + a}\sqrt{x}}{8(b^5x - ab^4)}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+a)^(3/2), x, algorithm="fricas")

[Out] [-1/8*(15*(a^2*b*x - a^3)*sqrt(-b)*log(-2*b*x - 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*(2*b^3*x^2 + 5*a*b^2*x - 15*a^2*b)*sqrt(-b*x + a)*sqrt(x))/(b^5*x - a*b^4), 1/4*(15*(a^2*b*x - a^3)*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) + (2*b^3*x^2 + 5*a*b^2*x - 15*a^2*b)*sqrt(-b*x + a)*sqrt(x))/(b^5*x - a*b^4)]

giac [B] time = 98.07, size = 154, normalized size = 1.54

$$\frac{\left(2\sqrt{(bx-a)b+ab}\sqrt{-bx+a}\left(\frac{2(bx-a)}{b^3} + \frac{9a}{b^3}\right) + \frac{32a^3}{\left(\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^2-ab\right)\sqrt{-b}b} - \frac{15a^2\log\left(\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)\sqrt{-b}b\right)}{\sqrt{-b}b^2} \right)}{8b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+a)^(3/2), x, algorithm="giac")

[Out] 1/8*(2*sqrt((b*x - a)*b + a*b)*sqrt(-b*x + a)*(2*(b*x - a)/b^3 + 9*a/b^3) + 32*a^3/(((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2 - a*b)*sqrt(-b)*b) - 15*a^2*log((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2)/(sqrt(-b)*b^2))*abs(b)/b^2

maple [A] time = 0.04, size = 127, normalized size = 1.27

$$\frac{\left(\frac{15a^2 \arctan\left(\frac{\left(x-\frac{a}{2b}\right)\sqrt{b}}{\sqrt{-bx^2+ax}}\right)}{8b^{\frac{7}{2}}} - \frac{2\sqrt{-\left(x-\frac{a}{b}\right)a-\left(x-\frac{a}{b}\right)^2 b a^2}}{\left(x-\frac{a}{b}\right)b^4} \right) \sqrt{(-bx+a)x}}{\sqrt{-bx+a} \sqrt{x}} + \frac{(2bx+7a)\sqrt{-bx+a} \sqrt{x}}{4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(-b*x+a)^(3/2), x)

[Out] 1/4*(2*b*x+7*a)/b^3*(-b*x+a)^(1/2)*x^(1/2)+(-15/8*a^2/b^(7/2)*arctan((x-1/2*a/b)/(-b*x^2+a*x)^(1/2)*b^(1/2))-2*a^2/b^4/(x-a/b)*(-b*(x-a/b)^2-(x-a/b)*a)^(1/2))*((-b*x+a)*x)^(1/2)/(-b*x+a)^(1/2)/x^(1/2)

maxima [A] time = 2.92, size = 118, normalized size = 1.18

$$\frac{8a^2b^2 - \frac{25(bx-a)a^2b}{x} + \frac{15(bx-a)^2a^2}{x^2}}{4\left(\frac{\sqrt{-bx+a}b^5}{\sqrt{x}} + \frac{2(-bx+a)^{\frac{3}{2}}b^4}{x^{\frac{3}{2}}} + \frac{(-bx+a)^{\frac{5}{2}}b^3}{x^{\frac{5}{2}}}\right)} + \frac{15a^2 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{4b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+a)^(3/2), x, algorithm="maxima")

[Out] 1/4*(8*a^2*b^2 - 25*(b*x - a)*a^2*b/x + 15*(b*x - a)^2*a^2/x^2)/(sqrt(-b*x + a)*b^5/sqrt(x) + 2*(-b*x + a)^(3/2)*b^4/x^(3/2) + (-b*x + a)^(5/2)*b^3/x^(5/2)) + 15/4*a^2*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/b^(7/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{(a-bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(a - b*x)^(3/2), x)

[Out] int(x^(5/2)/(a - b*x)^(3/2), x)

sympy [A] time = 8.03, size = 224, normalized size = 2.24

$$\left\{ \begin{array}{l} -\frac{15ia^{\frac{3}{2}}\sqrt{x}}{4b^3\sqrt{-1+\frac{bx}{a}}} + \frac{5i\sqrt{a}x^{\frac{3}{2}}}{4b^2\sqrt{-1+\frac{bx}{a}}} + \frac{15ia^2\operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{\frac{7}{2}}} + \frac{ix^{\frac{5}{2}}}{2\sqrt{a}b\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ \frac{15a^{\frac{3}{2}}\sqrt{x}}{4b^3\sqrt{1-\frac{bx}{a}}} - \frac{5\sqrt{a}x^{\frac{3}{2}}}{4b^2\sqrt{1-\frac{bx}{a}}} - \frac{15a^2\operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{4b^{\frac{7}{2}}} - \frac{x^{\frac{5}{2}}}{2\sqrt{a}b\sqrt{1-\frac{bx}{a}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(-b*x+a)**(3/2), x)

[Out] Piecewise((-15*I*a**(3/2)*sqrt(x)/(4*b**3*sqrt(-1 + b*x/a)) + 5*I*sqrt(a)*x**(3/2)/(4*b**2*sqrt(-1 + b*x/a)) + 15*I*a**2*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(4*b**(7/2)) + I*x**(5/2)/(2*sqrt(a)*b*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1, (15*a**(3/2)*sqrt(x)/(4*b**3*sqrt(1 - b*x/a)) - 5*sqrt(a)*x**(3/2)/(4*b**2*sqrt(1 - b*x/a)) - 15*a**2*asin(sqrt(b)*sqrt(x)/sqrt(a))/(4*b**(7/2)) - x**(5/2)/(2*sqrt(a)*b*sqrt(1 - b*x/a)), True))

$$3.597 \quad \int \frac{x^{3/2}}{(a-bx)^{3/2}} dx$$

Optimal. Leaf size=71

$$-\frac{3a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{5/2}} + \frac{3\sqrt{x}\sqrt{a-bx}}{b^2} + \frac{2x^{3/2}}{b\sqrt{a-bx}}$$

[Out] $-3*a*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(5/2)}+2*x^{(3/2)}/b/(-b*x+a)^{(1/2)}+3*x^{(1/2)}*(-b*x+a)^{(1/2)}/b^2$

Rubi [A] time = 0.02, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.312$, Rules used = {47, 50, 63, 217, 203}

$$\frac{3\sqrt{x}\sqrt{a-bx}}{b^2} - \frac{3a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{5/2}} + \frac{2x^{3/2}}{b\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)/(a - b*x)^(3/2), x]

[Out] $(2*x^{(3/2)})/(b*\text{Sqrt}[a - b*x]) + (3*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/b^2 - (3*a*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/ \text{Sqrt}[a - b*x]])/b^{(5/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{3/2}}{(a-bx)^{3/2}} dx &= \frac{2x^{3/2}}{b\sqrt{a-bx}} - \frac{3 \int \frac{\sqrt{x}}{\sqrt{a-bx}} dx}{b} \\
&= \frac{2x^{3/2}}{b\sqrt{a-bx}} + \frac{3\sqrt{x}\sqrt{a-bx}}{b^2} - \frac{(3a) \int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx}{2b^2} \\
&= \frac{2x^{3/2}}{b\sqrt{a-bx}} + \frac{3\sqrt{x}\sqrt{a-bx}}{b^2} - \frac{(3a) \text{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\
&= \frac{2x^{3/2}}{b\sqrt{a-bx}} + \frac{3\sqrt{x}\sqrt{a-bx}}{b^2} - \frac{(3a) \text{Subst}\left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right)}{b^2} \\
&= \frac{2x^{3/2}}{b\sqrt{a-bx}} + \frac{3\sqrt{x}\sqrt{a-bx}}{b^2} - \frac{3a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 51, normalized size = 0.72

$$\frac{2x^{5/2} \sqrt{1 - \frac{bx}{a}} {}_2F_1\left(\frac{3}{2}, \frac{5}{2}; \frac{7}{2}; \frac{bx}{a}\right)}{5a\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/(a - b*x)^(3/2),x]

[Out] (2*x^(5/2)*Sqrt[1 - (b*x)/a]*Hypergeometric2F1[3/2, 5/2, 7/2, (b*x)/a])/(5*a*Sqrt[a - b*x])

fricas [A] time = 0.45, size = 152, normalized size = 2.14

$$\left[\frac{3(abx - a^2)\sqrt{-b} \log(-2bx - 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) - 2(b^2x - 3ab)\sqrt{-bx+a}\sqrt{x}}{2(b^4x - ab^3)}, \frac{3(abx - a^2)\sqrt{b} \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{2(b^4x - ab^3)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+a)^(3/2),x, algorithm="fricas")

[Out] [-1/2*(3*(a*b*x - a^2)*sqrt(-b)*log(-2*b*x - 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*(b^2*x - 3*a*b)*sqrt(-b*x + a)*sqrt(x))/(b^4*x - a*b^3), (3*(a*b*x - a^2)*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) + (b^2*x - 3*a*b)*sqrt(-b*x + a)*sqrt(x))/(b^4*x - a*b^3)]

giac [B] time = 111.13, size = 130, normalized size = 1.83

$$\left[\frac{8a^2\sqrt{-b}}{(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab})^2-ab} + \frac{3a \log\left(\frac{(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab})^2}{\sqrt{-b}}\right)}{\sqrt{-b}} - \frac{2\sqrt{(bx-a)b+ab}\sqrt{-bx+a}}{b} \right] |b|$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+a)^(3/2),x, algorithm="giac")

[Out] -1/2*(8*a^2*sqrt(-b)/((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2 - a*b) + 3*a*log((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2)/sqrt(-b) - 2*sqrt((b*x - a)*b + a*b)*sqrt(-b*x + a)/b)*abs(b)/b^3

maple [B] time = 0.03, size = 114, normalized size = 1.61

$$\left[\frac{3a \arctan\left(\frac{(x-\frac{a}{b})\sqrt{b}}{\sqrt{-bx^2+ax}}\right)}{2b^{\frac{5}{2}}} - \frac{2\sqrt{-(x-\frac{a}{b})a-(x-\frac{a}{b})^2b}a}{(x-\frac{a}{b})b^3} \right] \frac{\sqrt{(-bx+a)x}}{\sqrt{-bx+a}\sqrt{x}} + \frac{\sqrt{-bx+a}\sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(-b*x+a)^(3/2),x)

[Out] $x^{(1/2)}*(-b*x+a)^{(1/2)}/b^2+(-3/2*a/b^{(5/2)}*\arctan((x-1/2*a/b)/(-b*x^2+a*x)^{(1/2)*b^{(1/2)}})-2*a/b^3/(x-a/b)*(-(x-a/b)*a-(x-a/b)^2*b)^{(1/2)}*((-b*x+a)*x)^{(1/2)}/(-b*x+a)^{(1/2)}/x^{(1/2)}$

maxima [A] time = 2.95, size = 75, normalized size = 1.06

$$\frac{2ab - \frac{3(bx-a)a}{x}}{\frac{\sqrt{-bx+a}b^3}{\sqrt{x}} + \frac{(-bx+a)^2b^2}{x^2}} + \frac{3a \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)/(-b*x+a)^(3/2),x, algorithm="maxima")`

[Out] $(2*a*b - 3*(b*x - a)*a/x)/(\sqrt{-b*x + a})*b^3/\sqrt{x} + (-b*x + a)^{(3/2)}*b^2/x^{(3/2)} + 3*a*\arctan(\sqrt{-b*x + a}/(\sqrt{b}*\sqrt{x}))/b^{(5/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{3/2}}{(a - bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(a - b*x)^(3/2),x)`

[Out] `int(x^(3/2)/(a - b*x)^(3/2), x)`

sympy [A] time = 3.70, size = 155, normalized size = 2.18

$$\begin{cases} -\frac{3i\sqrt{a}\sqrt{x}}{b^2\sqrt{-1+\frac{bx}{a}}} + \frac{3ia \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{\frac{5}{2}}} + \frac{ix^{\frac{3}{2}}}{\sqrt{a}b\sqrt{-1+\frac{bx}{a}}} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ \frac{3\sqrt{a}\sqrt{x}}{b^2\sqrt{1-\frac{bx}{a}}} - \frac{3a \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{\frac{5}{2}}} - \frac{x^{\frac{3}{2}}}{\sqrt{a}b\sqrt{1-\frac{bx}{a}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(-b*x+a)**(3/2),x)`

[Out] `Piecewise((-3*I*sqrt(a)*sqrt(x)/(b**2*sqrt(-1 + b*x/a)) + 3*I*a*acosh(sqrt(b)*sqrt(x)/sqrt(a))/b**(5/2) + I*x**(3/2)/(sqrt(a)*b*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (3*sqrt(a)*sqrt(x)/(b**2*sqrt(1 - b*x/a)) - 3*a*asin(sqrt(b)*sqrt(x)/sqrt(a))/b**(5/2) - x**(3/2)/(sqrt(a)*b*sqrt(1 - b*x/a)), True)`

$$3.598 \quad \int \frac{\sqrt{x}}{(a-bx)^{3/2}} dx$$

Optimal. Leaf size=50

$$\frac{2\sqrt{x}}{b\sqrt{a-bx}} - \frac{2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{3/2}}$$

[Out] $-2*\arctan(b^{(1/2)}*x^{(1/2)/(-b*x+a)^{(1/2)})/b^{(3/2)}+2*x^{(1/2)}/b/(-b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {47, 63, 217, 203}

$$\frac{2\sqrt{x}}{b\sqrt{a-bx}} - \frac{2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(a - b*x)^(3/2), x]

[Out] $(2*\text{Sqrt}[x])/(b*\text{Sqrt}[a - b*x]) - (2*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/b^{(3/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[Rt[b, 2]*x]/Rt[a, 2])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a

, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{x}}{(a-bx)^{3/2}} dx &= \frac{2\sqrt{x}}{b\sqrt{a-bx}} - \frac{\int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx}{b} \\ &= \frac{2\sqrt{x}}{b\sqrt{a-bx}} - \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x}\right)}{b} \\ &= \frac{2\sqrt{x}}{b\sqrt{a-bx}} - \frac{2 \operatorname{Subst}\left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right)}{b} \\ &= \frac{2\sqrt{x}}{b\sqrt{a-bx}} - \frac{2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.08, size = 66, normalized size = 1.32

$$\frac{2\sqrt{b}\sqrt{x} - 2\sqrt{a}\sqrt{1-\frac{bx}{a}} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(a - b*x)^(3/2), x]

[Out] (2*Sqrt[b]*Sqrt[x] - 2*Sqrt[a]*Sqrt[1 - (b*x)/a]*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(b^(3/2)*Sqrt[a - b*x])

fricas [A] time = 0.46, size = 128, normalized size = 2.56

$$\left[\frac{(bx-a)\sqrt{-b} \log(-2bx - 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) + 2\sqrt{-bx+a}b\sqrt{x}}{b^3x - ab^2}, \frac{2\left((bx-a)\sqrt{b} \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right) - \sqrt{-bx+a}\right)}{b^3x - ab^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+a)^(3/2),x, algorithm="fricas")

[Out] [-(b*x - a)*sqrt(-b)*log(-2*b*x - 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) + 2*sqrt(-b*x + a)*b*sqrt(x))/(b^3*x - a*b^2), 2*((b*x - a)*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - sqrt(-b*x + a)*b*sqrt(x))/(b^3*x - a*b^2)]

giac [B] time = 113.04, size = 98, normalized size = 1.96

$$\frac{\left(\frac{4a\sqrt{-b}}{(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab})^2-ab} + \frac{\log\left(\frac{\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}}{\sqrt{-b}}\right)}{\sqrt{-b}} \right) |b|}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+a)^(3/2),x, algorithm="giac")

[Out] -(4*a*sqrt(-b))/((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2 - a*b) + log((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2/sqrt(-b))*abs(b)/b^2

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{x}}{(-bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(-b*x+a)^(3/2),x)

[Out] int(x^(1/2)/(-b*x+a)^(3/2),x)

maxima [A] time = 3.01, size = 38, normalized size = 0.76

$$\frac{2 \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{3}{2}}} + \frac{2\sqrt{x}}{\sqrt{-bx+a}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+a)^(3/2),x, algorithm="maxima")

[Out] 2*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/b^(3/2) + 2*sqrt(x)/(sqrt(-b*x + a)*b)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{x}}{(a - bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)/(a - b*x)^(3/2), x)`

[Out] `int(x^(1/2)/(a - b*x)^(3/2), x)`

sympy [A] time = 1.89, size = 102, normalized size = 2.04

$$\begin{cases} \frac{2i \operatorname{acosh}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}} - \frac{2i\sqrt{x}}{\sqrt{a}b\sqrt{-1+\frac{bx}{a}}} & \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{2 \operatorname{asin}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)}{b^{3/2}} + \frac{2\sqrt{x}}{\sqrt{a}b\sqrt{1-\frac{bx}{a}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)/(-b*x+a)**(3/2), x)`

[Out] `Piecewise((2*I*acosh(sqrt(b)*sqrt(x)/sqrt(a))/b**(3/2) - 2*I*sqrt(x)/(sqrt(a)*b*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (-2*asin(sqrt(b)*sqrt(x)/sqrt(a))/b**(3/2) + 2*sqrt(x)/(sqrt(a)*b*sqrt(1 - b*x/a)), True))`

$$3.599 \quad \int \frac{1}{\sqrt{x}(a-bx)^{3/2}} dx$$

Optimal. Leaf size=20

$$\frac{2\sqrt{x}}{a\sqrt{a-bx}}$$

[Out] $2*x^{(1/2)}/a/(-b*x+a)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {37}

$$\frac{2\sqrt{x}}{a\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(a - b*x)^(3/2)),x]

[Out] (2*Sqrt[x])/(a*Sqrt[a - b*x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt{x}(a-bx)^{3/2}} dx = \frac{2\sqrt{x}}{a\sqrt{a-bx}}$$

Mathematica [A] time = 0.00, size = 20, normalized size = 1.00

$$\frac{2\sqrt{x}}{a\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(a - b*x)^(3/2)),x]

[Out] (2*Sqrt[x])/(a*Sqrt[a - b*x])

fricas [A] time = 0.43, size = 25, normalized size = 1.25

$$-\frac{2\sqrt{-bx+a}\sqrt{x}}{abx-a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+a)^(3/2)/x^(1/2),x, algorithm="fricas")

[Out] -2*sqrt(-b*x + a)*sqrt(x)/(a*b*x - a^2)

giac [B] time = 1.37, size = 53, normalized size = 2.65

$$-\frac{4\sqrt{-b}b}{\left(\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^2-ab\right)|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+a)^(3/2)/x^(1/2),x, algorithm="giac")

[Out] -4*sqrt(-b)*b/(((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2 - a*b)*abs(b))

maple [A] time = 0.00, size = 17, normalized size = 0.85

$$\frac{2\sqrt{x}}{\sqrt{-bx+a}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x+a)^(3/2)/x^(1/2),x)

[Out] 2*x^(1/2)/a/(-b*x+a)^(1/2)

maxima [A] time = 1.30, size = 16, normalized size = 0.80

$$\frac{2\sqrt{x}}{\sqrt{-bx+a}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+a)^(3/2)/x^(1/2),x, algorithm="maxima")

[Out] 2*sqrt(x)/(sqrt(-b*x + a)*a)

mupad [B] time = 0.34, size = 24, normalized size = 1.20

$$\frac{2\sqrt{x}\sqrt{a-bx}}{a^2-abx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(a - b*x)^(3/2)),x)`

[Out] `(2*x^(1/2)*(a - b*x)^(1/2))/(a^2 - a*b*x)`

sympy [A] time = 0.94, size = 44, normalized size = 2.20

$$\begin{cases} \frac{2}{a\sqrt{b}\sqrt{\frac{a}{bx}-1}} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ -\frac{2i}{a\sqrt{b}\sqrt{-\frac{a}{bx}+1}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x+a)**(3/2)/x**(1/2),x)`

[Out] `Piecewise((2/(a*sqrt(b)*sqrt(a/(b*x) - 1)), Abs(a/(b*x)) > 1), (-2*I/(a*sqrt(b)*sqrt(-a/(b*x) + 1)), True))`

$$3.600 \quad \int \frac{1}{x^{3/2}(a-bx)^{3/2}} dx$$

Optimal. Leaf size=41

$$\frac{2}{a\sqrt{x}\sqrt{a-bx}} - \frac{4\sqrt{a-bx}}{a^2\sqrt{x}}$$

[Out] 2/a/x^(1/2)/(-b*x+a)^(1/2)-4*(-b*x+a)^(1/2)/a^2/x^(1/2)

Rubi [A] time = 0.00, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$\frac{2}{a\sqrt{x}\sqrt{a-bx}} - \frac{4\sqrt{a-bx}}{a^2\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(a - b*x)^(3/2)),x]

[Out] 2/(a*Sqrt[x]*Sqrt[a - b*x]) - (4*Sqrt[a - b*x])/(a^2*Sqrt[x])

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{x^{3/2}(a-bx)^{3/2}} dx = \frac{2}{a\sqrt{x}\sqrt{a-bx}} + \frac{2 \int \frac{1}{x^{3/2}\sqrt{a-bx}} dx}{a}$$

$$= \frac{2}{a\sqrt{x}\sqrt{a-bx}} - \frac{4\sqrt{a-bx}}{a^2\sqrt{x}}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 0.63

$$\frac{2(a-2bx)}{a^2\sqrt{x}\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(a - b*x)^(3/2)), x]

[Out] (-2*(a - 2*b*x))/(a^2*Sqrt[x]*Sqrt[a - b*x])

fricas [A] time = 0.44, size = 38, normalized size = 0.93

$$-\frac{2(2bx-a)\sqrt{-bx+a}\sqrt{x}}{a^2bx^2-a^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+a)^(3/2), x, algorithm="fricas")

[Out] -2*(2*b*x - a)*sqrt(-b*x + a)*sqrt(x)/(a^2*b*x^2 - a^3*x)

giac [B] time = 1.44, size = 94, normalized size = 2.29

$$-\frac{4\sqrt{-b}b^2}{\left(\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^2-ab\right)a|b|} - \frac{2\sqrt{-bx+a}b^2}{\sqrt{(bx-a)b+ab}a^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+a)^(3/2), x, algorithm="giac")

[Out] -4*sqrt(-b)*b^2/(((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2 - a*b)*a*abs(b)) - 2*sqrt(-b*x + a)*b^2/(sqrt((b*x - a)*b + a*b)*a^2*abs(b))

maple [A] time = 0.00, size = 23, normalized size = 0.56

$$\frac{2(-2bx+a)}{\sqrt{-bx+a}a^2\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(3/2)/(-b*x+a)^(3/2),x)`

[Out] `-2*(-2*b*x+a)/(-b*x+a)^(1/2)/x^(1/2)/a^2`

maxima [A] time = 1.30, size = 34, normalized size = 0.83

$$\frac{2b\sqrt{x}}{\sqrt{-bx+a}a^2} - \frac{2\sqrt{-bx+a}}{a^2\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(-b*x+a)^(3/2),x, algorithm="maxima")`

[Out] `2*b*sqrt(x)/(sqrt(-b*x + a)*a^2) - 2*sqrt(-b*x + a)/(a^2*sqrt(x))`

mupad [B] time = 0.40, size = 42, normalized size = 1.02

$$-\frac{2a\sqrt{a-bx} - 4bx\sqrt{a-bx}}{\sqrt{x}(a^3 - a^2bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(a - b*x)^(3/2)),x)`

[Out] `-(2*a*(a - b*x)^(1/2) - 4*b*x*(a - b*x)^(1/2))/(x^(1/2)*(a^3 - a^2*b*x))`

sympy [A] time = 1.68, size = 112, normalized size = 2.73

$$\begin{cases} -\frac{2}{a\sqrt{bx}\sqrt{\frac{a}{bx}-1}} + \frac{4\sqrt{b}}{a^2\sqrt{\frac{a}{bx}-1}} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ -\frac{2iab^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}}{a^3b-a^2b^2x} + \frac{4ib^{\frac{5}{2}}x\sqrt{-\frac{a}{bx}+1}}{a^3b-a^2b^2x} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(-b*x+a)**(3/2),x)`

[Out] `Piecewise((-2/(a*sqrt(b)*x*sqrt(a/(b*x) - 1)) + 4*sqrt(b)/(a**2*sqrt(a/(b*x) - 1)), Abs(a/(b*x)) > 1), (-2*I*a*b**(3/2)*sqrt(-a/(b*x) + 1)/(a**3*b - a**2*b**2*x) + 4*I*b**(5/2)*x*sqrt(-a/(b*x) + 1)/(a**3*b - a**2*b**2*x), True))`

$$3.601 \quad \int \frac{1}{x^{5/2}(a-bx)^{3/2}} dx$$

Optimal. Leaf size=66

$$-\frac{16b\sqrt{a-bx}}{3a^3\sqrt{x}} - \frac{8\sqrt{a-bx}}{3a^2x^{3/2}} + \frac{2}{ax^{3/2}\sqrt{a-bx}}$$

[Out] $2/a/x^{(3/2)/(-b*x+a)^{(1/2)}-8/3*(-b*x+a)^{(1/2)/a^2/x^{(3/2)}-16/3*b*(-b*x+a)^{(1/2)/a^3/x^{(1/2)}}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{8\sqrt{a-bx}}{3a^2x^{3/2}} - \frac{16b\sqrt{a-bx}}{3a^3\sqrt{x}} + \frac{2}{ax^{3/2}\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(a - b*x)^(3/2)), x]

[Out] $2/(a*x^{(3/2)*\text{Sqrt}[a - b*x]) - (8*\text{Sqrt}[a - b*x])/(3*a^2*x^{(3/2)}) - (16*b*\text{Sqrt}[a - b*x])/(3*a^3*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{5/2}(a-bx)^{3/2}} dx &= \frac{2}{ax^{3/2}\sqrt{a-bx}} + \frac{4 \int \frac{1}{x^{5/2}\sqrt{a-bx}} dx}{a} \\
&= \frac{2}{ax^{3/2}\sqrt{a-bx}} - \frac{8\sqrt{a-bx}}{3a^2x^{3/2}} + \frac{(8b) \int \frac{1}{x^{3/2}\sqrt{a-bx}} dx}{3a^2} \\
&= \frac{2}{ax^{3/2}\sqrt{a-bx}} - \frac{8\sqrt{a-bx}}{3a^2x^{3/2}} - \frac{16b\sqrt{a-bx}}{3a^3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.59

$$-\frac{2(a^2 + 4abx - 8b^2x^2)}{3a^3x^{3/2}\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(a - b*x)^(3/2)),x]

[Out] (-2*(a^2 + 4*a*b*x - 8*b^2*x^2))/(3*a^3*x^(3/2)*Sqrt[a - b*x])

fricas [A] time = 0.45, size = 51, normalized size = 0.77

$$-\frac{2(8b^2x^2 - 4abx - a^2)\sqrt{-bx + a}\sqrt{x}}{3(a^3bx^3 - a^4x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+a)^(3/2),x, algorithm="fricas")

[Out] -2/3*(8*b^2*x^2 - 4*a*b*x - a^2)*sqrt(-b*x + a)*sqrt(x)/(a^3*b*x^3 - a^4*x^2)

giac [B] time = 1.48, size = 112, normalized size = 1.70

$$-\frac{2\sqrt{-bx+a}\left(\frac{5(bx-a)b^2|b|}{a^3} + \frac{6b^2|b|}{a^2}\right)}{3((bx-a)b+ab)^{\frac{3}{2}}} - \frac{4\sqrt{-b}b^3}{\left(\left(\sqrt{-bx+a}\sqrt{-b} - \sqrt{(bx-a)b+ab}\right)^2 - ab\right)a^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+a)^(3/2),x, algorithm="giac")

[Out] $-2/3*\sqrt{-b*x + a}*(5*(b*x - a)*b^2*abs(b)/a^3 + 6*b^2*abs(b)/a^2)/((b*x - a)*b + a*b)^{(3/2)} - 4*\sqrt{-b}*b^3/(((\sqrt{-b*x + a})*\sqrt{-b}) - \sqrt{(b*x - a)*b + a*b})^2 - a*b)*a^2*abs(b))$

maple [A] time = 0.00, size = 34, normalized size = 0.52

$$-\frac{2(-8b^2x^2 + 4abx + a^2)}{3\sqrt{-bx + a} a^3 x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/x^{(5/2)} / (-b*x+a)^{(3/2)}, x)$

[Out] $-2/3*(-8*b^2*x^2+4*a*b*x+a^2)/(-b*x+a)^{(1/2)}/x^{(3/2)}/a^3$

maxima [A] time = 1.35, size = 52, normalized size = 0.79

$$\frac{2b^2\sqrt{x}}{\sqrt{-bx + a} a^3} - \frac{2\left(\frac{6\sqrt{-bx+ab}}{\sqrt{x}} + \frac{(-bx+a)^{\frac{3}{2}}}{x^2}\right)}{3a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^{(5/2)} / (-b*x+a)^{(3/2)}, x, \text{algorithm}="maxima")$

[Out] $2*b^2*\sqrt{x}/(\sqrt{-b*x + a})*a^3 - 2/3*(6*\sqrt{-b*x + a})*b/\sqrt{x} + (-b*x + a)^{(3/2)}/x^{(3/2)}/a^3$

mupad [B] time = 0.43, size = 48, normalized size = 0.73

$$\frac{\sqrt{a-bx} \left(\frac{8x}{3a^2} + \frac{2}{3ab} - \frac{16bx^2}{3a^3} \right)}{x^{5/2} - \frac{ax^{3/2}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(x^{(5/2)}*(a - b*x)^{(3/2)}), x)$

[Out] $((a - b*x)^{(1/2)}*((8*x)/(3*a^2) + 2/(3*a*b) - (16*b*x^2)/(3*a^3)))/(x^{(5/2)} - (a*x^{(3/2)})/b)$

sympy [B] time = 4.64, size = 452, normalized size = 6.85

$$\begin{cases} \frac{2a^3b^{\frac{9}{2}}\sqrt{\frac{a}{bx}-1}}{-3a^5b^4x+6a^4b^5x^2-3a^3b^6x^3} + \frac{6a^2b^{\frac{11}{2}}x\sqrt{\frac{a}{bx}-1}}{-3a^5b^4x+6a^4b^5x^2-3a^3b^6x^3} - \frac{24ab^{\frac{13}{2}}x^2\sqrt{\frac{a}{bx}-1}}{-3a^5b^4x+6a^4b^5x^2-3a^3b^6x^3} + \frac{16b^{\frac{15}{2}}x^3\sqrt{\frac{a}{bx}-1}}{-3a^5b^4x+6a^4b^5x^2-3a^3b^6x^3} & \text{for } \left| \frac{a}{bx} \right| > 1 \\ \frac{2ia^3b^{\frac{9}{2}}\sqrt{\frac{a}{bx}+1}}{-3a^5b^4x+6a^4b^5x^2-3a^3b^6x^3} + \frac{6ia^2b^{\frac{11}{2}}x\sqrt{\frac{a}{bx}+1}}{-3a^5b^4x+6a^4b^5x^2-3a^3b^6x^3} - \frac{24iab^{\frac{13}{2}}x^2\sqrt{\frac{a}{bx}+1}}{-3a^5b^4x+6a^4b^5x^2-3a^3b^6x^3} + \frac{16ib^{\frac{15}{2}}x^3\sqrt{\frac{a}{bx}+1}}{-3a^5b^4x+6a^4b^5x^2-3a^3b^6x^3} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(5/2)/(-b*x+a)**(3/2),x)

[Out] Piecewise((2*a**3*b**(9/2)*sqrt(a/(b*x) - 1)/(-3*a**5*b**4*x + 6*a**4*b**5*x**2 - 3*a**3*b**6*x**3) + 6*a**2*b**(11/2)*x*sqrt(a/(b*x) - 1)/(-3*a**5*b**4*x + 6*a**4*b**5*x**2 - 3*a**3*b**6*x**3) - 24*a*b**(13/2)*x**2*sqrt(a/(b*x) - 1)/(-3*a**5*b**4*x + 6*a**4*b**5*x**2 - 3*a**3*b**6*x**3) + 16*b**(15/2)*x**3*sqrt(a/(b*x) - 1)/(-3*a**5*b**4*x + 6*a**4*b**5*x**2 - 3*a**3*b**6*x**3), Abs(a/(b*x)) > 1), (2*I*a**3*b**(9/2)*sqrt(-a/(b*x) + 1)/(-3*a**5*b**4*x + 6*a**4*b**5*x**2 - 3*a**3*b**6*x**3) + 6*I*a**2*b**(11/2)*x*sqrt(-a/(b*x) + 1)/(-3*a**5*b**4*x + 6*a**4*b**5*x**2 - 3*a**3*b**6*x**3) - 24*I*a*b**(13/2)*x**2*sqrt(-a/(b*x) + 1)/(-3*a**5*b**4*x + 6*a**4*b**5*x**2 - 3*a**3*b**6*x**3) + 16*I*b**(15/2)*x**3*sqrt(-a/(b*x) + 1)/(-3*a**5*b**4*x + 6*a**4*b**5*x**2 - 3*a**3*b**6*x**3), True))

$$3.602 \quad \int \frac{x^{5/2}}{(a-bx)^{5/2}} dx$$

Optimal. Leaf size=95

$$\frac{5a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{7/2}} - \frac{5\sqrt{x}\sqrt{a-bx}}{b^3} - \frac{10x^{3/2}}{3b^2\sqrt{a-bx}} + \frac{2x^{5/2}}{3b(a-bx)^{3/2}}$$

[Out] $2/3*x^{(5/2)}/b/(-b*x+a)^{(3/2)}+5*a*\arctan(b^{(1/2)}*x^{(1/2)}/(-b*x+a)^{(1/2)})/b^{(7/2)}-10/3*x^{(3/2)}/b^2/(-b*x+a)^{(1/2)}-5*x^{(1/2)}*(-b*x+a)^{(1/2)}/b^3$

Rubi [A] time = 0.03, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.312$, Rules used = {47, 50, 63, 217, 203}

$$-\frac{10x^{3/2}}{3b^2\sqrt{a-bx}} - \frac{5\sqrt{x}\sqrt{a-bx}}{b^3} + \frac{5a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{7/2}} + \frac{2x^{5/2}}{3b(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)/(a - b*x)^(5/2), x]

[Out] $(2*x^{(5/2)})/(3*b*(a - b*x)^{(3/2)}) - (10*x^{(3/2)})/(3*b^2*\text{Sqrt}[a - b*x]) - (5*\text{Sqrt}[x]*\text{Sqrt}[a - b*x])/b^3 + (5*a*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/(\text{Sqrt}[a - b*x])])/b^{(7/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(a-bx)^{5/2}} dx &= \frac{2x^{5/2}}{3b(a-bx)^{3/2}} - \frac{5 \int \frac{x^{3/2}}{(a-bx)^{3/2}} dx}{3b} \\
&= \frac{2x^{5/2}}{3b(a-bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{a-bx}} + \frac{5 \int \frac{\sqrt{x}}{\sqrt{a-bx}} dx}{b^2} \\
&= \frac{2x^{5/2}}{3b(a-bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{a-bx}} - \frac{5\sqrt{x}\sqrt{a-bx}}{b^3} + \frac{(5a) \int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx}{2b^3} \\
&= \frac{2x^{5/2}}{3b(a-bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{a-bx}} - \frac{5\sqrt{x}\sqrt{a-bx}}{b^3} + \frac{(5a) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x}\right)}{b^3} \\
&= \frac{2x^{5/2}}{3b(a-bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{a-bx}} - \frac{5\sqrt{x}\sqrt{a-bx}}{b^3} + \frac{(5a) \operatorname{Subst}\left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right)}{b^3} \\
&= \frac{2x^{5/2}}{3b(a-bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{a-bx}} - \frac{5\sqrt{x}\sqrt{a-bx}}{b^3} + \frac{5a \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 51, normalized size = 0.54

$$\frac{2x^{7/2}\sqrt{1-\frac{bx}{a}}{}_2F_1\left(\frac{5}{2}, \frac{7}{2}; \frac{9}{2}; \frac{bx}{a}\right)}{7a^2\sqrt{a-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/(a - b*x)^(5/2), x]

[Out] (2*x^(7/2)*Sqrt[1 - (b*x)/a]*Hypergeometric2F1[5/2, 7/2, 9/2, (b*x)/a])/(7*a^2*Sqrt[a - b*x])

fricas [A] time = 0.46, size = 215, normalized size = 2.26

$$\left[\frac{15(ab^2x^2 - 2a^2bx + a^3)\sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) + 2(3b^3x^2 - 20ab^2x + 15a^2b)\sqrt{-bx+a}}{6(b^6x^2 - 2ab^5x + a^2b^4)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+a)^(5/2), x, algorithm="fricas")

[Out] [-1/6*(15*(a*b^2*x^2 - 2*a^2*b*x + a^3)*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) + 2*(3*b^3*x^2 - 20*a*b^2*x + 15*a^2*b)*sqrt(-b*x + a)*sqrt(x))/(b^6*x^2 - 2*a*b^5*x + a^2*b^4), -1/3*(15*(a*b^2*x^2 - 2*a^2*b*x + a^3)*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) + (3*b^3*x^2 - 20*a*b^2*x + 15*a^2*b)*sqrt(-b*x + a)*sqrt(x))/(b^6*x^2 - 2*a*b^5*x + a^2*b^4)]

giac [B] time = 112.52, size = 221, normalized size = 2.33

$$\left(\frac{15a \log\left(\frac{\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}}{\sqrt{-b}b^2}\right)}{\sqrt{-b}b^2} - \frac{6\sqrt{(bx-a)b+ab}\sqrt{-bx+a}}{b^3} - \frac{8\left(9a^2(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab})^4 - 12a^3(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)})\right)}{\left(\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^2 - ab\right)^3\sqrt{-b}b} \right) / 6b^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+a)^(5/2), x, algorithm="giac")

[Out] 1/6*(15*a*log((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2)/(sqrt(-b)*b^2) - 6*sqrt((b*x - a)*b + a*b)*sqrt(-b*x + a)/b^3 - 8*(9*a^2*(sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^4 - 12*a^3*(sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2*b + 7*a^4*b^2)/(((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2 - a*b)^3*sqrt(-b)*b))

maple [B] time = 0.04, size = 160, normalized size = 1.68

$$\frac{\left(\frac{5a \arctan\left(\frac{\left(x-\frac{a}{2b}\right)\sqrt{b}}{\sqrt{-bx^2+ax}}\right)}{2b^{\frac{7}{2}}} + \frac{2\sqrt{-\left(x-\frac{a}{b}\right)a-\left(x-\frac{a}{b}\right)^2b}a^2}{3\left(x-\frac{a}{b}\right)^2b^5} + \frac{14\sqrt{-\left(x-\frac{a}{b}\right)a-\left(x-\frac{a}{b}\right)^2b}a}{3\left(x-\frac{a}{b}\right)b^4} \right) \sqrt{(-bx+a)x}}{\sqrt{-bx+a} \sqrt{x}} - \frac{\sqrt{-bx+a} \sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(-b*x+a)^(5/2), x)

[Out] $-x^{(1/2)}*(-b*x+a)^{(1/2)}/b^3+(5/2/b^{(7/2)}*a*\arctan((x-1/2*a/b)/(-b*x^2+a*x)^{(1/2)}*b^{(1/2)}))+2/3/b^5*a^2/(x-a/b)^2*(-(x-a/b)*a-(x-a/b)^2*b)^{(1/2)}+14/3/b^4*a/(x-a/b)*(-(x-a/b)*a-(x-a/b)^2*b)^{(1/2)}*((-b*x+a)*x)^{(1/2)}/(-b*x+a)^{(1/2)}/x^{(1/2)}$

maxima [A] time = 3.02, size = 94, normalized size = 0.99

$$\frac{2ab^2 + \frac{10(bx-a)ab}{x} - \frac{15(bx-a)^2a}{x^2}}{3\left(\frac{(-bx+a)^{\frac{3}{2}}b^4}{x^{\frac{3}{2}}} + \frac{(-bx+a)^{\frac{5}{2}}b^3}{x^{\frac{5}{2}}}\right)} - \frac{5a \arctan\left(\frac{\sqrt{-bx+a}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+a)^(5/2), x, algorithm="maxima")

[Out] $1/3*(2*a*b^2 + 10*(b*x - a)*a*b/x - 15*(b*x - a)^2*a/x^2)/((-b*x + a)^{(3/2)}*b^4/x^{(3/2)} + (-b*x + a)^{(5/2)}*b^3/x^{(5/2)}) - 5*a*\arctan(\text{sqrt}(-b*x + a)/(\text{sqrt}(b)*\text{sqrt}(x)))/b^{(7/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{(a-bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(a - b*x)^(5/2), x)

[Out] int(x^(5/2)/(a - b*x)^(5/2), x)

sympy [B] time = 8.48, size = 971, normalized size = 10.22

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/2)/(-b*x+a)**(5/2),x)`

[Out] `Piecewise((-30*I*a**(81/2)*b**22*x**(51/2)*sqrt(-1 + b*x/a)*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(6*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(-1 + b*x/a) - 6*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(-1 + b*x/a)) + 15*pi*a**(81/2)*b**22*x**(51/2)*sqrt(-1 + b*x/a)/(6*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(-1 + b*x/a) - 6*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(-1 + b*x/a)) + 30*I*a**(79/2)*b**23*x**(53/2)*sqrt(-1 + b*x/a)*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(6*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(-1 + b*x/a) - 6*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(-1 + b*x/a)) - 15*pi*a**(79/2)*b**23*x**(53/2)*sqrt(-1 + b*x/a)/(6*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(-1 + b*x/a) - 6*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(-1 + b*x/a)) + 30*I*a**40*b**(45/2)*x**26/(6*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(-1 + b*x/a) - 6*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(-1 + b*x/a)) - 40*I*a**39*b**(47/2)*x**27/(6*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(-1 + b*x/a) - 6*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(-1 + b*x/a)) + 6*I*a**38*b**(49/2)*x**28/(6*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(-1 + b*x/a) - 6*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (15*a**(81/2)*b**22*x**(51/2)*sqrt(1 - b*x/a)*asin(sqrt(b)*sqrt(x)/sqrt(a))/(3*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(1 - b*x/a) - 3*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(1 - b*x/a)) - 15*a**(79/2)*b**23*x**(53/2)*sqrt(1 - b*x/a)*asin(sqrt(b)*sqrt(x)/sqrt(a))/(3*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(1 - b*x/a) - 3*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(1 - b*x/a)) - 15*a**40*b**(45/2)*x**26/(3*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(1 - b*x/a) - 3*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(1 - b*x/a)) + 20*a**39*b**(47/2)*x**27/(3*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(1 - b*x/a) - 3*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(1 - b*x/a)) - 3*a**38*b**(49/2)*x**28/(3*a**(79/2)*b**(51/2)*x**(51/2)*sqrt(1 - b*x/a) - 3*a**(77/2)*b**(53/2)*x**(53/2)*sqrt(1 - b*x/a)), True))`

$$3.603 \quad \int \frac{x^{3/2}}{(a-bx)^{5/2}} dx$$

Optimal. Leaf size=72

$$\frac{2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{5/2}} - \frac{2\sqrt{x}}{b^2\sqrt{a-bx}} + \frac{2x^{3/2}}{3b(a-bx)^{3/2}}$$

[Out] $2/3*x^{(3/2)}/b/(-b*x+a)^{(3/2)}+2*\arctan(b^{(1/2)}*x^{(1/2)}/(-b*x+a)^{(1/2)})/b^{(5/2)}-2*x^{(1/2)}/b^2/(-b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {47, 63, 217, 203}

$$-\frac{2\sqrt{x}}{b^2\sqrt{a-bx}} + \frac{2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{5/2}} + \frac{2x^{3/2}}{3b(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)/(a - b*x)^(5/2), x]

[Out] $(2*x^{(3/2)})/(3*b*(a - b*x)^{(3/2)}) - (2*\text{Sqrt}[x])/(b^2*\text{Sqrt}[a - b*x]) + (2*\text{ArcTan}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[a - b*x]])/b^{(5/2)}$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)),
Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
 \int \frac{x^{3/2}}{(a-bx)^{5/2}} dx &= \frac{2x^{3/2}}{3b(a-bx)^{3/2}} - \frac{\int \frac{\sqrt{x}}{(a-bx)^{3/2}} dx}{b} \\
 &= \frac{2x^{3/2}}{3b(a-bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{a-bx}} + \frac{\int \frac{1}{\sqrt{x}\sqrt{a-bx}} dx}{b^2} \\
 &= \frac{2x^{3/2}}{3b(a-bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{a-bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a-bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\
 &= \frac{2x^{3/2}}{3b(a-bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{a-bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{1+bx^2} dx, x, \frac{\sqrt{x}}{\sqrt{a-bx}}\right)}{b^2} \\
 &= \frac{2x^{3/2}}{3b(a-bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{a-bx}} + \frac{2 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a-bx}}\right)}{b^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.17, size = 82, normalized size = 1.14

$$\frac{2\left(\sqrt{b}\sqrt{x}(4bx-3a) + 3\sqrt{a}(a-bx)\sqrt{1-\frac{bx}{a}} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{a}}\right)\right)}{3b^{5/2}(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(3/2)/(a - b*x)^(5/2), x]
```

```
[Out] (2*(Sqrt[b]*Sqrt[x]*(-3*a + 4*b*x) + 3*Sqrt[a]*(a - b*x)*Sqrt[1 - (b*x)/a]*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[a]])/(3*b^(5/2)*(a - b*x)^(3/2))
```

fricas [A] time = 0.45, size = 188, normalized size = 2.61

$$\left[\frac{3(b^2x^2 - 2abx + a^2)\sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) - 2(4b^2x - 3ab)\sqrt{-bx+a}\sqrt{x}}{3(b^5x^2 - 2ab^4x + a^2b^3)}, -\frac{2(3(b^2x^2 - 2abx + a^2)\sqrt{-b} \log(-2bx + 2\sqrt{-bx+a}\sqrt{-b}\sqrt{x} + a) - 2(4b^2x - 3ab)\sqrt{-bx+a}\sqrt{x})}{3(b^5x^2 - 2ab^4x + a^2b^3)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+a)^(5/2),x, algorithm="fricas")

[Out] [-1/3*(3*(b^2*x^2 - 2*a*b*x + a^2)*sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + a)*sqrt(-b)*sqrt(x) + a) - 2*(4*b^2*x - 3*a*b)*sqrt(-b*x + a)*sqrt(x))/(b^5*x^2 - 2*a*b^4*x + a^2*b^3), -2/3*(3*(b^2*x^2 - 2*a*b*x + a^2)*sqrt(b)*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x))) - (4*b^2*x - 3*a*b)*sqrt(-b*x + a)*sqrt(x))/(b^5*x^2 - 2*a*b^4*x + a^2*b^3)]

giac [B] time = 110.08, size = 194, normalized size = 2.69

$$\left(\frac{3 \log\left(\frac{\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}}{\sqrt{-b}}\right)^2}{\sqrt{-b}} + \frac{8\left(3a(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab})^4\sqrt{-b}-3a^2(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab})^2\sqrt{-b}+2a^3\sqrt{-b}b^2\right)}{\left(\frac{\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}}{\sqrt{-b}}\right)^2-ab} \right) \frac{1}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+a)^(5/2),x, algorithm="giac")

[Out] 1/3*(3*log((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2)/sqrt(-b) + 8*(3*a*(sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^4*sqrt(-b) - 3*a^2*(sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2*sqrt(-b)*b + 2*a^3*sqrt(-b)*b^2)/((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2 - a*b)^3)*abs(b)/b^3

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{x^{\frac{3}{2}}}{(-bx+a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(-b*x+a)^(5/2),x)

[Out] int(x^(3/2)/(-b*x+a)^(5/2),x)

maxima [A] time = 2.94, size = 52, normalized size = 0.72

$$\frac{2 \left(b + \frac{3(bx-a)}{x} \right) x^{\frac{3}{2}}}{3(-bx+a)^{\frac{3}{2}} b^2} - \frac{2 \arctan \left(\frac{\sqrt{-bx+a}}{\sqrt{b} \sqrt{x}} \right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+a)^(5/2),x, algorithm="maxima")

[Out] 2/3*(b + 3*(b*x - a)/x)*x^(3/2)/((-b*x + a)^(3/2)*b^2) - 2*arctan(sqrt(-b*x + a)/(sqrt(b)*sqrt(x)))/b^(5/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{3/2}}{(a - bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(a - b*x)^(5/2),x)

[Out] int(x^(3/2)/(a - b*x)^(5/2), x)

sympy [B] time = 4.50, size = 833, normalized size = 11.57

$$\left\{ \begin{array}{l} \frac{6ia^{\frac{39}{2}} b^{11} x^{\frac{27}{2}} \sqrt{-1+\frac{bx}{a}} \operatorname{acosh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{3a^{\frac{39}{2}} b^{\frac{27}{2}} x^{\frac{27}{2}} \sqrt{-1+\frac{bx}{a}} - 3a^{\frac{37}{2}} b^{\frac{29}{2}} x^{\frac{29}{2}} \sqrt{-1+\frac{bx}{a}}} + \frac{3\pi a^{\frac{39}{2}} b^{11} x^{\frac{27}{2}} \sqrt{-1+\frac{bx}{a}}}{3a^{\frac{39}{2}} b^{\frac{27}{2}} x^{\frac{27}{2}} \sqrt{-1+\frac{bx}{a}} - 3a^{\frac{37}{2}} b^{\frac{29}{2}} x^{\frac{29}{2}} \sqrt{-1+\frac{bx}{a}}} + \frac{6ia^{\frac{37}{2}} b^{12} x^{\frac{29}{2}} \sqrt{-1+\frac{bx}{a}} \operatorname{acosh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{3a^{\frac{39}{2}} b^{\frac{27}{2}} x^{\frac{27}{2}} \sqrt{-1+\frac{bx}{a}} - 3a^{\frac{37}{2}} b^{\frac{29}{2}} x^{\frac{29}{2}} \sqrt{-1+\frac{bx}{a}}} \\ \frac{6a^{\frac{39}{2}} b^{11} x^{\frac{27}{2}} \sqrt{1-\frac{bx}{a}} \operatorname{asin}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{3a^{\frac{39}{2}} b^{\frac{27}{2}} x^{\frac{27}{2}} \sqrt{1-\frac{bx}{a}} - 3a^{\frac{37}{2}} b^{\frac{29}{2}} x^{\frac{29}{2}} \sqrt{1-\frac{bx}{a}}} - \frac{6a^{\frac{37}{2}} b^{12} x^{\frac{29}{2}} \sqrt{1-\frac{bx}{a}} \operatorname{asin}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{a}}\right)}{3a^{\frac{39}{2}} b^{\frac{27}{2}} x^{\frac{27}{2}} \sqrt{1-\frac{bx}{a}} - 3a^{\frac{37}{2}} b^{\frac{29}{2}} x^{\frac{29}{2}} \sqrt{1-\frac{bx}{a}}} - \frac{6a^{19} b^{\frac{23}{2}} x^{14}}{3a^{\frac{39}{2}} b^{\frac{27}{2}} x^{\frac{27}{2}} \sqrt{1-\frac{bx}{a}} - 3a^{\frac{37}{2}} b^{\frac{29}{2}} x^{\frac{29}{2}} \sqrt{1-\frac{bx}{a}}} + \frac{3}{3a^{\frac{39}{2}} b^{\frac{27}{2}} x^{\frac{27}{2}} \sqrt{1-\frac{bx}{a}} - 3a^{\frac{37}{2}} b^{\frac{29}{2}} x^{\frac{29}{2}} \sqrt{1-\frac{bx}{a}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)/(-b*x+a)**(5/2),x)

[Out] Piecewise((-6*I*a**(39/2)*b**11*x**(27/2)*sqrt(-1 + b*x/a)*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(3*a**(39/2)*b**(27/2)*x**(27/2)*sqrt(-1 + b*x/a) - 3*a**(37/2)*b**(29/2)*x**(29/2)*sqrt(-1 + b*x/a)) + 3*pi*a**(39/2)*b**11*x**(27/2)*sqrt(-1 + b*x/a)/(3*a**(39/2)*b**(27/2)*x**(27/2)*sqrt(-1 + b*x/a) - 3*a**(37/2)*b**(29/2)*x**(29/2)*sqrt(-1 + b*x/a)) + 6*I*a**(37/2)*b**12*x**(29/2)*sqrt(-1 + b*x/a)*acosh(sqrt(b)*sqrt(x)/sqrt(a))/(3*a**(39/2)*b**(27/2)*x**(27/2)*sqrt(-1 + b*x/a) - 3*a**(37/2)*b**(29/2)*x**(29/2)*sqrt(-1 + b*x/a)) + 3/(3*a**(39/2)*b**(27/2)*x**(27/2)*sqrt(-1 + b*x/a) - 3*a**(37/2)*b**(29/2)*x**(29/2)*sqrt(-1 + b*x/a))

```

- 3*pi*a**(37/2)*b**12*x**(29/2)*sqrt(-1 + b*x/a)/(3*a**(39/2)*b**(27/2)*x
**(27/2)*sqrt(-1 + b*x/a) - 3*a**(37/2)*b**(29/2)*x**(29/2)*sqrt(-1 + b*x/a
)) + 6*I*a**19*b**(23/2)*x**14/(3*a**(39/2)*b**(27/2)*x**(27/2)*sqrt(-1 + b
*x/a) - 3*a**(37/2)*b**(29/2)*x**(29/2)*sqrt(-1 + b*x/a)) - 8*I*a**18*b**(2
5/2)*x**15/(3*a**(39/2)*b**(27/2)*x**(27/2)*sqrt(-1 + b*x/a) - 3*a**(37/2)*
b**(29/2)*x**(29/2)*sqrt(-1 + b*x/a)), Abs(b*x/a) > 1), (6*a**(39/2)*b**11*
x**(27/2)*sqrt(1 - b*x/a)*asin(sqrt(b)*sqrt(x)/sqrt(a))/(3*a**(39/2)*b**(27
/2)*x**(27/2)*sqrt(1 - b*x/a) - 3*a**(37/2)*b**(29/2)*x**(29/2)*sqrt(1 - b*
x/a)) - 6*a**(37/2)*b**12*x**(29/2)*sqrt(1 - b*x/a)*asin(sqrt(b)*sqrt(x)/sq
rt(a))/(3*a**(39/2)*b**(27/2)*x**(27/2)*sqrt(1 - b*x/a) - 3*a**(37/2)*b**(2
9/2)*x**(29/2)*sqrt(1 - b*x/a)) - 6*a**19*b**(23/2)*x**14/(3*a**(39/2)*b**(
27/2)*x**(27/2)*sqrt(1 - b*x/a) - 3*a**(37/2)*b**(29/2)*x**(29/2)*sqrt(1 -
b*x/a)) + 8*a**18*b**(25/2)*x**15/(3*a**(39/2)*b**(27/2)*x**(27/2)*sqrt(1 -
b*x/a) - 3*a**(37/2)*b**(29/2)*x**(29/2)*sqrt(1 - b*x/a)), True))

```

$$3.604 \quad \int \frac{\sqrt{x}}{(a-bx)^{5/2}} dx$$

Optimal. Leaf size=22

$$\frac{2x^{3/2}}{3a(a-bx)^{3/2}}$$

[Out] $2/3*x^{(3/2)}/a/(-b*x+a)^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {37}

$$\frac{2x^{3/2}}{3a(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(a - b*x)^(5/2), x]

[Out] $(2*x^{(3/2)})/(3*a*(a - b*x)^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{x}}{(a-bx)^{5/2}} dx = \frac{2x^{3/2}}{3a(a-bx)^{3/2}}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 1.00

$$\frac{2x^{3/2}}{3a(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(a - b*x)^(5/2), x]

[Out] $(2*x^{(3/2)})/(3*a*(a - b*x)^{(3/2)})$

fricas [B] time = 0.42, size = 34, normalized size = 1.55

$$\frac{2\sqrt{-bx+a}x^{\frac{3}{2}}}{3(ab^2x^2-2a^2bx+a^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+a)^(5/2),x, algorithm="fricas")

[Out] 2/3*sqrt(-b*x + a)*x^(3/2)/(a*b^2*x^2 - 2*a^2*b*x + a^3)

giac [B] time = 1.63, size = 102, normalized size = 4.64

$$\frac{4\left(3\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^4\sqrt{-b}+a^2\sqrt{-b}b^2\right)|b|}{3\left(\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^2-ab\right)^3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+a)^(5/2),x, algorithm="giac")

[Out] 4/3*(3*(sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^4*sqrt(-b) + a^2*sqrt(-b)*b^2)*abs(b)/(((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2 - a*b)^3*b^2)

maple [A] time = 0.00, size = 17, normalized size = 0.77

$$\frac{2x^{\frac{3}{2}}}{3(-bx+a)^{\frac{3}{2}}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(-b*x+a)^(5/2),x)

[Out] 2/3*x^(3/2)/a/(-b*x+a)^(3/2)

maxima [A] time = 1.36, size = 16, normalized size = 0.73

$$\frac{2x^{\frac{3}{2}}}{3(-bx+a)^{\frac{3}{2}}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+a)^(5/2),x, algorithm="maxima")

[Out] $2/3*x^{(3/2)/((-b*x + a)^{(3/2)*a)}$

mupad [B] time = 0.25, size = 37, normalized size = 1.68

$$\frac{2x^{3/2}\sqrt{a-bx}}{3(a^3-2a^2bx+ab^2x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{(1/2)/(a-b*x)^{(5/2)}, x)$

[Out] $(2*x^{(3/2)*(a-b*x)^{(1/2)})/(3*(a^3+a*b^2*x^2-2*a^2*b*x))$

sympy [B] time = 1.51, size = 95, normalized size = 4.32

$$\left\{ \begin{array}{l} \frac{2ix^{\frac{3}{2}}}{-3a^{\frac{5}{2}}\sqrt{-1+\frac{bx}{a}}+3a^{\frac{3}{2}}bx\sqrt{-1+\frac{bx}{a}}} \quad \text{for } \left|\frac{bx}{a}\right| > 1 \\ -\frac{2x^{\frac{3}{2}}}{-3a^{\frac{5}{2}}\sqrt{1-\frac{bx}{a}}+3a^{\frac{3}{2}}bx\sqrt{1-\frac{bx}{a}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{(1/2)/(-b*x+a)^{(5/2)}, x)$

[Out] $\text{Piecewise}((2*I*x^{(3/2)/(-3*a^{(5/2)}*\text{sqrt}(-1+b*x/a)+3*a^{(3/2)}*b*x*\text{sqrt}(-1+b*x/a)), \text{Abs}(b*x/a) > 1), (-2*x^{(3/2)/(-3*a^{(5/2)}*\text{sqrt}(1-b*x/a)+3*a^{(3/2)}*b*x*\text{sqrt}(1-b*x/a)), \text{True}))$

$$3.605 \quad \int \frac{1}{\sqrt{x}(a-bx)^{5/2}} dx$$

Optimal. Leaf size=45

$$\frac{4\sqrt{x}}{3a^2\sqrt{a-bx}} + \frac{2\sqrt{x}}{3a(a-bx)^{3/2}}$$

[Out] $2/3*x^{(1/2)}/a/(-b*x+a)^{(3/2)}+4/3*x^{(1/2)}/a^2/(-b*x+a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$\frac{4\sqrt{x}}{3a^2\sqrt{a-bx}} + \frac{2\sqrt{x}}{3a(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(a - b*x)^(5/2)),x]

[Out] (2*Sqrt[x])/(3*a*(a - b*x)^(3/2)) + (4*Sqrt[x])/(3*a^2*Sqrt[a - b*x])

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{\sqrt{x}(a-bx)^{5/2}} dx = \frac{2\sqrt{x}}{3a(a-bx)^{3/2}} + \frac{2 \int \frac{1}{\sqrt{x}(a-bx)^{3/2}} dx}{3a}$$

$$= \frac{2\sqrt{x}}{3a(a-bx)^{3/2}} + \frac{4\sqrt{x}}{3a^2\sqrt{a-bx}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 0.67

$$\frac{2\sqrt{x}(3a-2bx)}{3a^2(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(a - b*x)^(5/2)),x]

[Out] (2*Sqrt[x]*(3*a - 2*b*x))/(3*a^2*(a - b*x)^(3/2))

fricas [A] time = 0.42, size = 44, normalized size = 0.98

$$\frac{2(2bx-3a)\sqrt{-bx+a}\sqrt{x}}{3(a^2b^2x^2-2a^3bx+a^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+a)^(5/2)/x^(1/2),x, algorithm="fricas")

[Out] -2/3*(2*b*x - 3*a)*sqrt(-b*x + a)*sqrt(x)/(a^2*b^2*x^2 - 2*a^3*b*x + a^4)

giac [B] time = 1.43, size = 96, normalized size = 2.13

$$\frac{8\left(3\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^2-ab\right)\sqrt{-b}b^2}{3\left(\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^2-ab\right)^3|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+a)^(5/2)/x^(1/2),x, algorithm="giac")

[Out] 8/3*(3*(sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2 - a*b)*sqrt(-b)*b^2/(((sqrt(-b*x + a)*sqrt(-b) - sqrt((b*x - a)*b + a*b))^2 - a*b)^3*abs(b))

maple [A] time = 0.00, size = 25, normalized size = 0.56

$$\frac{2(-2bx + 3a)\sqrt{x}}{3(-bx + a)^{\frac{3}{2}}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-b*x+a)^(5/2)/x^(1/2),x)`

[Out] `2/3*x^(1/2)*(-2*b*x+3*a)/(-b*x+a)^(3/2)/a^2`

maxima [A] time = 1.34, size = 30, normalized size = 0.67

$$\frac{2\left(b - \frac{3(bx-a)}{x}\right)x^{\frac{3}{2}}}{3(-bx + a)^{\frac{3}{2}}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x+a)^(5/2)/x^(1/2),x, algorithm="maxima")`

[Out] `2/3*(b - 3*(b*x - a)/x)*x^(3/2)/((-b*x + a)^(3/2)*a^2)`

mupad [B] time = 0.41, size = 56, normalized size = 1.24

$$\frac{6a\sqrt{x}\sqrt{a-bx} - 4bx^{3/2}\sqrt{a-bx}}{3a^4 - 6a^3bx + 3a^2b^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(a - b*x)^(5/2)),x)`

[Out] `(6*a*x^(1/2)*(a - b*x)^(1/2) - 4*b*x^(3/2)*(a - b*x)^(1/2))/(3*a^4 + 3*a^2*b^2*x^2 - 6*a^3*b*x)`

sympy [C] time = 2.00, size = 211, normalized size = 4.69

$$\begin{cases} \frac{6ia}{3ia^3\sqrt{b}\sqrt{\frac{a}{bx}-1}-3ia^2b^{\frac{3}{2}}x\sqrt{\frac{a}{bx}-1}} - \frac{4ibx}{3ia^3\sqrt{b}\sqrt{\frac{a}{bx}-1}-3ia^2b^{\frac{3}{2}}x\sqrt{\frac{a}{bx}-1}} & \text{for } \left|\frac{a}{bx}\right| > 1 \\ \frac{6ab}{3ia^3b^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}-3ia^2b^{\frac{5}{2}}x\sqrt{-\frac{a}{bx}+1}} - \frac{4b^2x}{3ia^3b^{\frac{3}{2}}\sqrt{-\frac{a}{bx}+1}-3ia^2b^{\frac{5}{2}}x\sqrt{-\frac{a}{bx}+1}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(-b*x+a)**(5/2)/x**(1/2),x)
```

```
[Out] Piecewise((6*I*a/(3*I*a**3*sqrt(b)*sqrt(a/(b*x) - 1) - 3*I*a**2*b**(3/2)*x*sqrt(a/(b*x) - 1)) - 4*I*b*x/(3*I*a**3*sqrt(b)*sqrt(a/(b*x) - 1) - 3*I*a**2*b**(3/2)*x*sqrt(a/(b*x) - 1)), Abs(a/(b*x)) > 1), (6*a*b/(3*I*a**3*b**(3/2)*sqrt(-a/(b*x) + 1) - 3*I*a**2*b**(5/2)*x*sqrt(-a/(b*x) + 1)) - 4*b**2*x/(3*I*a**3*b**(3/2)*sqrt(-a/(b*x) + 1) - 3*I*a**2*b**(5/2)*x*sqrt(-a/(b*x) + 1)), True))
```

$$3.606 \quad \int \frac{1}{x^{3/2}(a-bx)^{5/2}} dx$$

Optimal. Leaf size=67

$$-\frac{16\sqrt{a-bx}}{3a^3\sqrt{x}} + \frac{8}{3a^2\sqrt{x}\sqrt{a-bx}} + \frac{2}{3a\sqrt{x}(a-bx)^{3/2}}$$

[Out] $2/3/a/(-b*x+a)^{(3/2)}/x^{(1/2)}+8/3/a^2/x^{(1/2)}/(-b*x+a)^{(1/2)}-16/3*(-b*x+a)^{(1/2)}/a^3/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{16\sqrt{a-bx}}{3a^3\sqrt{x}} + \frac{8}{3a^2\sqrt{x}\sqrt{a-bx}} + \frac{2}{3a\sqrt{x}(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(a - b*x)^(5/2)),x]

[Out] $2/(3*a*\text{Sqrt}[x]*(a - b*x)^{(3/2)}) + 8/(3*a^2*\text{Sqrt}[x]*\text{Sqrt}[a - b*x]) - (16*\text{Sqrt}[a - b*x])/(3*a^3*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{3/2}(a-bx)^{5/2}} dx &= \frac{2}{3a\sqrt{x}(a-bx)^{3/2}} + \frac{4 \int \frac{1}{x^{3/2}(a-bx)^{3/2}} dx}{3a} \\
&= \frac{2}{3a\sqrt{x}(a-bx)^{3/2}} + \frac{8}{3a^2\sqrt{x}\sqrt{a-bx}} + \frac{8 \int \frac{1}{x^{3/2}\sqrt{a-bx}} dx}{3a^2} \\
&= \frac{2}{3a\sqrt{x}(a-bx)^{3/2}} + \frac{8}{3a^2\sqrt{x}\sqrt{a-bx}} - \frac{16\sqrt{a-bx}}{3a^3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 41, normalized size = 0.61

$$\frac{2(3a^2 - 12abx + 8b^2x^2)}{3a^3\sqrt{x}(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(a - b*x)^(5/2)), x]

[Out] (-2*(3*a^2 - 12*a*b*x + 8*b^2*x^2))/(3*a^3*Sqrt[x]*(a - b*x)^(3/2))

fricas [A] time = 0.44, size = 59, normalized size = 0.88

$$\frac{2(8b^2x^2 - 12abx + 3a^2)\sqrt{-bx+a}\sqrt{x}}{3(a^3b^2x^3 - 2a^4bx^2 + a^5x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+a)^(5/2), x, algorithm="fricas")

[Out] -2/3*(8*b^2*x^2 - 12*a*b*x + 3*a^2)*sqrt(-b*x + a)*sqrt(x)/(a^3*b^2*x^3 - 2*a^4*b*x^2 + a^5*x)

giac [B] time = 1.61, size = 189, normalized size = 2.82

$$\frac{2\sqrt{-bx+a}b^2}{\sqrt{(bx-a)b+ab}a^3|b|} - \frac{4\left(3\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^4\sqrt{-b}b^2-12a\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)+\sqrt{(bx-a)b+ab}\right)^3}{3\left(\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^2-ab\right)^3a^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+a)^(5/2), x, algorithm="giac")

[Out] $-2\sqrt{-bx+a}b^2/(\sqrt{(bx-a)b+ab})a^3\text{abs}(b) - 4/3(3(\sqrt{-bx+a}\sqrt{-b} - \sqrt{(bx-a)b+ab})^4\sqrt{-b}b^2 - 12a(\sqrt{-bx+a}\sqrt{-b} - \sqrt{(bx-a)b+ab})^2\sqrt{-b}b^3 + 5a^2\sqrt{-b}b^4)/(((\sqrt{-bx+a}\sqrt{-b} - \sqrt{(bx-a)b+ab})^2 - ab)^3a^2\text{abs}(b))$

maple [A] time = 0.00, size = 36, normalized size = 0.54

$$-\frac{2(8b^2x^2 - 12abx + 3a^2)}{3(-bx + a)^{\frac{3}{2}}a^3\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(3/2)/(-b*x+a)^(5/2),x)`

[Out] $-2/3(8b^2x^2-12a*b*x+3a^2)/(-b*x+a)^(3/2)/x^(1/2)/a^3$

maxima [A] time = 1.29, size = 50, normalized size = 0.75

$$\frac{2\left(b^2 - \frac{6(bx-a)b}{x}\right)x^{\frac{3}{2}}}{3(-bx+a)^{\frac{3}{2}}a^3} - \frac{2\sqrt{-bx+a}}{a^3\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(-b*x+a)^(5/2),x, algorithm="maxima")`

[Out] $2/3(b^2 - 6*(bx - a)*b/x)*x^{3/2}/((-bx + a)^{3/2}*a^3) - 2*\sqrt{-bx + a}/(a^3*\sqrt{x})$

mupad [B] time = 0.44, size = 73, normalized size = 1.09

$$\frac{6a^2\sqrt{a-bx} + 16b^2x^2\sqrt{a-bx} - 24abx\sqrt{a-bx}}{\sqrt{x}(x(6a^4b - 3a^3b^2x) - 3a^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(a-b*x)^(5/2)),x)`

[Out] $(6a^2(a-bx)^{1/2} + 16b^2x^2(a-bx)^{1/2} - 24a*b*x*(a-bx)^{1/2})/(x^{1/2}*(x*(6a^4*b - 3a^3*b^2*x) - 3a^5))$

sympy [B] time = 4.27, size = 314, normalized size = 4.69

$$\left\{ \begin{array}{l} -\frac{6a^2b^{\frac{9}{2}}\sqrt{\frac{a}{bx}-1}}{3a^5b^4-6a^4b^5x+3a^3b^6x^2} + \frac{24ab^{\frac{11}{2}}x\sqrt{\frac{a}{bx}-1}}{3a^5b^4-6a^4b^5x+3a^3b^6x^2} - \frac{16b^{\frac{13}{2}}x^2\sqrt{\frac{a}{bx}-1}}{3a^5b^4-6a^4b^5x+3a^3b^6x^2} \\ -\frac{6ia^2b^{\frac{9}{2}}\sqrt{-\frac{a}{bx}+1}}{3a^5b^4-6a^4b^5x+3a^3b^6x^2} + \frac{24iab^{\frac{11}{2}}x\sqrt{-\frac{a}{bx}+1}}{3a^5b^4-6a^4b^5x+3a^3b^6x^2} - \frac{16ib^{\frac{13}{2}}x^2\sqrt{-\frac{a}{bx}+1}}{3a^5b^4-6a^4b^5x+3a^3b^6x^2} \end{array} \right. \begin{array}{l} \text{for } \left| \frac{a}{bx} \right| > 1 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(3/2)/(-b*x+a)**(5/2), x)

[Out] Piecewise((-6*a**2*b**(9/2)*sqrt(a/(b*x) - 1)/(3*a**5*b**4 - 6*a**4*b**5*x + 3*a**3*b**6*x**2) + 24*a*b**(11/2)*x*sqrt(a/(b*x) - 1)/(3*a**5*b**4 - 6*a**4*b**5*x + 3*a**3*b**6*x**2) - 16*b**(13/2)*x**2*sqrt(a/(b*x) - 1)/(3*a**5*b**4 - 6*a**4*b**5*x + 3*a**3*b**6*x**2), Abs(a/(b*x)) > 1), (-6*I*a**2*b**(9/2)*sqrt(-a/(b*x) + 1)/(3*a**5*b**4 - 6*a**4*b**5*x + 3*a**3*b**6*x**2) + 24*I*a*b**(11/2)*x*sqrt(-a/(b*x) + 1)/(3*a**5*b**4 - 6*a**4*b**5*x + 3*a**3*b**6*x**2) - 16*I*b**(13/2)*x**2*sqrt(-a/(b*x) + 1)/(3*a**5*b**4 - 6*a**4*b**5*x + 3*a**3*b**6*x**2), True))

$$3.607 \quad \int \frac{1}{x^{5/2}(a-bx)^{5/2}} dx$$

Optimal. Leaf size=88

$$-\frac{32b\sqrt{a-bx}}{3a^4\sqrt{x}} - \frac{16\sqrt{a-bx}}{3a^3x^{3/2}} + \frac{4}{a^2x^{3/2}\sqrt{a-bx}} + \frac{2}{3ax^{3/2}(a-bx)^{3/2}}$$

[Out] 2/3/a/x^(3/2)/(-b*x+a)^(3/2)+4/a^2/x^(3/2)/(-b*x+a)^(1/2)-16/3*(-b*x+a)^(1/2)/a^3/x^(3/2)-32/3*b*(-b*x+a)^(1/2)/a^4/x^(1/2)

Rubi [A] time = 0.02, antiderivative size = 88, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{16\sqrt{a-bx}}{3a^3x^{3/2}} + \frac{4}{a^2x^{3/2}\sqrt{a-bx}} - \frac{32b\sqrt{a-bx}}{3a^4\sqrt{x}} + \frac{2}{3ax^{3/2}(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(a - b*x)^(5/2)), x]

[Out] 2/(3*a*x^(3/2)*(a - b*x)^(3/2)) + 4/(a^2*x^(3/2)*Sqrt[a - b*x]) - (16*Sqrt[a - b*x])/(3*a^3*x^(3/2)) - (32*b*Sqrt[a - b*x])/(3*a^4*Sqrt[x])

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{5/2}(a-bx)^{5/2}} dx &= \frac{2}{3ax^{3/2}(a-bx)^{3/2}} + \frac{2 \int \frac{1}{x^{5/2}(a-bx)^{3/2}} dx}{a} \\
&= \frac{2}{3ax^{3/2}(a-bx)^{3/2}} + \frac{4}{a^2 x^{3/2} \sqrt{a-bx}} + \frac{8 \int \frac{1}{x^{5/2} \sqrt{a-bx}} dx}{a^2} \\
&= \frac{2}{3ax^{3/2}(a-bx)^{3/2}} + \frac{4}{a^2 x^{3/2} \sqrt{a-bx}} - \frac{16\sqrt{a-bx}}{3a^3 x^{3/2}} + \frac{(16b) \int \frac{1}{x^{3/2} \sqrt{a-bx}} dx}{3a^3} \\
&= \frac{2}{3ax^{3/2}(a-bx)^{3/2}} + \frac{4}{a^2 x^{3/2} \sqrt{a-bx}} - \frac{16\sqrt{a-bx}}{3a^3 x^{3/2}} - \frac{32b\sqrt{a-bx}}{3a^4 \sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 50, normalized size = 0.57

$$-\frac{2(a^3 + 6a^2bx - 24ab^2x^2 + 16b^3x^3)}{3a^4x^{3/2}(a-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(a - b*x)^(5/2)),x]

[Out] (-2*(a^3 + 6*a^2*b*x - 24*a*b^2*x^2 + 16*b^3*x^3))/(3*a^4*x^(3/2)*(a - b*x)^(3/2))

fricas [A] time = 0.44, size = 70, normalized size = 0.80

$$-\frac{2(16b^3x^3 - 24ab^2x^2 + 6a^2bx + a^3)\sqrt{-bx+a}\sqrt{x}}{3(a^4b^2x^4 - 2a^5bx^3 + a^6x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+a)^(5/2),x, algorithm="fricas")

[Out] -2/3*(16*b^3*x^3 - 24*a*b^2*x^2 + 6*a^2*b*x + a^3)*sqrt(-b*x + a)*sqrt(x)/(a^4*b^2*x^4 - 2*a^5*b*x^3 + a^6*x^2)

giac [B] time = 1.70, size = 207, normalized size = 2.35

$$-\frac{2\sqrt{-bx+a}\left(\frac{8(bx-a)b^2|b|}{a^4} + \frac{9b^2|b|}{a^3}\right)}{3((bx-a)b+ab)^{\frac{3}{2}}}-\frac{8\left(3\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^4\sqrt{-b}b^3-9a\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^2-\sqrt{(bx-a)b+ab}\right)}{3\left(\left(\sqrt{-bx+a}\sqrt{-b}-\sqrt{(bx-a)b+ab}\right)^2-ab\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+a)^(5/2),x, algorithm="giac")

[Out]
$$-2/3\sqrt{-bx+a}*(8*(bx-a)*b^2*abs(b)/a^4 + 9*b^2*abs(b)/a^3)/((bx-a)*b + a*b)^(3/2) - 8/3*(3*(sqrt(-bx+a)*sqrt(-b) - sqrt((bx-a)*b + a*b))^4*sqrt(-b)*b^3 - 9*a*(sqrt(-bx+a)*sqrt(-b) - sqrt((bx-a)*b + a*b))^2*sqrt(-b)*b^4 + 4*a^2*sqrt(-b)*b^5)/(((sqrt(-bx+a)*sqrt(-b) - sqrt((bx-a)*b + a*b))^2 - a*b)^3*a^3*abs(b))$$

maple [A] time = 0.00, size = 45, normalized size = 0.51

$$-\frac{2(16b^3x^3 - 24ab^2x^2 + 6a^2bx + a^3)}{3(-bx+a)^{\frac{3}{2}}a^4x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(5/2)/(-b*x+a)^(5/2),x)

[Out]
$$-2/3*(16*b^3*x^3-24*a*b^2*x^2+6*a^2*b*x+a^3)/(-b*x+a)^(3/2)/x^(3/2)/a^4$$

maxima [A] time = 1.33, size = 68, normalized size = 0.77

$$-\frac{2\left(\frac{9\sqrt{-bx+ab}}{\sqrt{x}} + \frac{(-bx+a)^{\frac{3}{2}}}{x^2}\right)}{3a^4} + \frac{2\left(b^3 - \frac{9(bx-a)b^2}{x}\right)x^{\frac{3}{2}}}{3(-bx+a)^{\frac{3}{2}}a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+a)^(5/2),x, algorithm="maxima")

[Out]
$$-2/3*(9*sqrt(-bx+a)*b/sqrt(x) + (-bx+a)^(3/2)/x^(3/2))/a^4 + 2/3*(b^3 - 9*(bx-a)*b^2/x)*x^(3/2)/((-bx+a)^(3/2)*a^4)$$

mupad [B] time = 0.47, size = 92, normalized size = 1.05

$$\frac{2a^3\sqrt{a-bx} + 32b^3x^3\sqrt{a-bx} + 12a^2bx\sqrt{a-bx} - 48ab^2x^2\sqrt{a-bx}}{x^{3/2}(x(6a^5b - 3a^4b^2x) - 3a^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(5/2)*(a-b*x)^(5/2)),x)

[Out]
$$(2*a^3*(a-b*x)^(1/2) + 32*b^3*x^3*(a-b*x)^(1/2) + 12*a^2*b*x*(a-b*x)^(1/2) - 48*a*b^2*x^2*(a-b*x)^(1/2))/(x^(3/2)*(x*(6*a^5*b - 3*a^4*b^2*x) - 3*a^6))$$

sympy [B] time = 13.45, size = 688, normalized size = 7.82

$$\left\{ \begin{array}{l} \frac{2a^4 b^{\frac{19}{2}} \sqrt{\frac{a}{bx}-1}}{-3a^7 b^9 x + 9a^6 b^{10} x^2 - 9a^5 b^{11} x^3 + 3a^4 b^{12} x^4} + \frac{10a^3 b^{\frac{21}{2}} x \sqrt{\frac{a}{bx}-1}}{-3a^7 b^9 x + 9a^6 b^{10} x^2 - 9a^5 b^{11} x^3 + 3a^4 b^{12} x^4} - \frac{60a^2 b^{\frac{23}{2}} x^2 \sqrt{\frac{a}{bx}-1}}{-3a^7 b^9 x + 9a^6 b^{10} x^2 - 9a^5 b^{11} x^3 + 3a^4 b^{12} x^4} + \frac{80a b^{\frac{25}{2}} x^3 \sqrt{\frac{a}{bx}-1}}{-3a^7 b^9 x + 9a^6 b^{10} x^2 - 9a^5 b^{11} x^3 + 3a^4 b^{12} x^4} \\ \frac{2ia^4 b^{\frac{19}{2}} \sqrt{-\frac{a}{bx}+1}}{-3a^7 b^9 x + 9a^6 b^{10} x^2 - 9a^5 b^{11} x^3 + 3a^4 b^{12} x^4} + \frac{10ia^3 b^{\frac{21}{2}} x \sqrt{-\frac{a}{bx}+1}}{-3a^7 b^9 x + 9a^6 b^{10} x^2 - 9a^5 b^{11} x^3 + 3a^4 b^{12} x^4} - \frac{60ia^2 b^{\frac{23}{2}} x^2 \sqrt{-\frac{a}{bx}+1}}{-3a^7 b^9 x + 9a^6 b^{10} x^2 - 9a^5 b^{11} x^3 + 3a^4 b^{12} x^4} + \frac{80iab^{\frac{25}{2}} x^3 \sqrt{-\frac{a}{bx}+1}}{-3a^7 b^9 x + 9a^6 b^{10} x^2 - 9a^5 b^{11} x^3 + 3a^4 b^{12} x^4} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(5/2)/(-b*x+a)**(5/2), x)

[Out] Piecewise((2*a**4*b**(19/2)*sqrt(a/(b*x) - 1)/(-3*a**7*b**9*x + 9*a**6*b**10*x**2 - 9*a**5*b**11*x**3 + 3*a**4*b**12*x**4) + 10*a**3*b**(21/2)*x*sqrt(a/(b*x) - 1)/(-3*a**7*b**9*x + 9*a**6*b**10*x**2 - 9*a**5*b**11*x**3 + 3*a**4*b**12*x**4) - 60*a**2*b**(23/2)*x**2*sqrt(a/(b*x) - 1)/(-3*a**7*b**9*x + 9*a**6*b**10*x**2 - 9*a**5*b**11*x**3 + 3*a**4*b**12*x**4) + 80*a*b**(25/2)*x**3*sqrt(a/(b*x) - 1)/(-3*a**7*b**9*x + 9*a**6*b**10*x**2 - 9*a**5*b**11*x**3 + 3*a**4*b**12*x**4) - 32*b**(27/2)*x**4*sqrt(a/(b*x) - 1)/(-3*a**7*b**9*x + 9*a**6*b**10*x**2 - 9*a**5*b**11*x**3 + 3*a**4*b**12*x**4), Abs(a/(b*x)) > 1), (2*I*a**4*b**(19/2)*sqrt(-a/(b*x) + 1)/(-3*a**7*b**9*x + 9*a**6*b**10*x**2 - 9*a**5*b**11*x**3 + 3*a**4*b**12*x**4) + 10*I*a**3*b**(21/2)*x*sqrt(-a/(b*x) + 1)/(-3*a**7*b**9*x + 9*a**6*b**10*x**2 - 9*a**5*b**11*x**3 + 3*a**4*b**12*x**4) - 60*I*a**2*b**(23/2)*x**2*sqrt(-a/(b*x) + 1)/(-3*a**7*b**9*x + 9*a**6*b**10*x**2 - 9*a**5*b**11*x**3 + 3*a**4*b**12*x**4) + 80*I*a*b**(25/2)*x**3*sqrt(-a/(b*x) + 1)/(-3*a**7*b**9*x + 9*a**6*b**10*x**2 - 9*a**5*b**11*x**3 + 3*a**4*b**12*x**4) - 32*I*b**(27/2)*x**4*sqrt(-a/(b*x) + 1)/(-3*a**7*b**9*x + 9*a**6*b**10*x**2 - 9*a**5*b**11*x**3 + 3*a**4*b**12*x**4), True))

$$3.608 \quad \int \frac{x^{5/2}}{\sqrt{2+bx}} dx$$

Optimal. Leaf size=88

$$-\frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} + \frac{5\sqrt{x}\sqrt{bx+2}}{2b^3} - \frac{5x^{3/2}\sqrt{bx+2}}{6b^2} + \frac{x^{5/2}\sqrt{bx+2}}{3b}$$

[Out] $-5*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(7/2)}-5/6*x^{(3/2)}*(b*x+2)^{(1/2)}/b^{(7/2)}+1/3*x^{(5/2)}*(b*x+2)^{(1/2)}/b+5/2*x^{(1/2)}*(b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.02, antiderivative size = 88, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{5x^{3/2}\sqrt{bx+2}}{6b^2} + \frac{5\sqrt{x}\sqrt{bx+2}}{2b^3} - \frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} + \frac{x^{5/2}\sqrt{bx+2}}{3b}$$

Antiderivative was successfully verified.

[In] `Int[x^(5/2)/Sqrt[2 + b*x], x]`

[Out] $(5*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/(2*b^3) - (5*x^{(3/2)}*\operatorname{Sqrt}[2 + b*x])/(6*b^2) + (x^{(5/2)}*\operatorname{Sqrt}[2 + b*x])/(3*b) - (5*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]])/b^{(7/2)}$

Rule 50

`Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 54

`Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]`

Rule 215

`Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]`

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{\sqrt{2+bx}} dx &= \frac{x^{5/2}\sqrt{2+bx}}{3b} - \frac{5 \int \frac{x^{3/2}}{\sqrt{2+bx}} dx}{3b} \\
&= -\frac{5x^{3/2}\sqrt{2+bx}}{6b^2} + \frac{x^{5/2}\sqrt{2+bx}}{3b} + \frac{5 \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx}{2b^2} \\
&= \frac{5\sqrt{x}\sqrt{2+bx}}{2b^3} - \frac{5x^{3/2}\sqrt{2+bx}}{6b^2} + \frac{x^{5/2}\sqrt{2+bx}}{3b} - \frac{5 \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx}{2b^3} \\
&= \frac{5\sqrt{x}\sqrt{2+bx}}{2b^3} - \frac{5x^{3/2}\sqrt{2+bx}}{6b^2} + \frac{x^{5/2}\sqrt{2+bx}}{3b} - \frac{5 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right)}{b^3} \\
&= \frac{5\sqrt{x}\sqrt{2+bx}}{2b^3} - \frac{5x^{3/2}\sqrt{2+bx}}{6b^2} + \frac{x^{5/2}\sqrt{2+bx}}{3b} - \frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 60, normalized size = 0.68

$$\frac{\sqrt{x}\sqrt{bx+2}(2b^2x^2-5bx+15)}{6b^3} - \frac{5 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/Sqrt[2 + b*x], x]

[Out] (Sqrt[x]*Sqrt[2 + b*x]*(15 - 5*b*x + 2*b^2*x^2))/(6*b^3) - (5*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(7/2)

fricas [A] time = 0.44, size = 124, normalized size = 1.41

$$\left[\frac{(2b^3x^2 - 5b^2x + 15b)\sqrt{bx+2}\sqrt{x} + 15\sqrt{b}\log(bx - \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{6b^4}, \frac{(2b^3x^2 - 5b^2x + 15b)\sqrt{bx+2}\sqrt{x}}{6b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+2)^(1/2), x, algorithm="fricas")

[Out] [1/6*((2*b^3*x^2 - 5*b^2*x + 15*b)*sqrt(b*x + 2)*sqrt(x) + 15*sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^4, 1/6*((2*b^3*x^2 - 5*b^2*x + 15*b)*sqrt(b*x + 2)*sqrt(x) + 15*sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^4]

$5*b)*\sqrt{b*x + 2}*\sqrt{x} + 30*\sqrt{-b}*\arctan(\sqrt{b*x + 2}*\sqrt{-b}/(b*\sqrt{x})))/b^4]$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [85.3561567818,61.7937478349]Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [71.707969239,78.6493344628]2*abs(b)/b^2/b*(2*((12*b^5/144/b^7*sqrt(b*x+2)*sqrt(b*x+2)-78*b^5/144/b^7)*sqrt(b*x+2)*sqrt(b*x+2)+198*b^5/144/b^7)*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)+5/2/b/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))

maple [A] time = 0.00, size = 93, normalized size = 1.06

$$\frac{\sqrt{bx+2} x^{\frac{5}{2}}}{3b} - \frac{5\sqrt{bx+2} x^{\frac{3}{2}}}{6b^2} + \frac{5\sqrt{bx+2} \sqrt{x}}{2b^3} - \frac{5\sqrt{(bx+2)x} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{2\sqrt{bx+2} b^{\frac{7}{2}} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x+2)^(1/2), x)

[Out] 1/3*x^(5/2)*(b*x+2)^(1/2)/b-5/6*x^(3/2)*(b*x+2)^(1/2)/b^2+5/2*(b*x+2)^(1/2)/b^3*x^(1/2)-5/2*((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)/b^(7/2)/x^(1/2)*ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))

maxima [B] time = 2.97, size = 134, normalized size = 1.52

$$-\frac{\frac{33\sqrt{bx+2}b^2}{\sqrt{x}} - \frac{40(bx+2)^2b}{x^2} + \frac{15(bx+2)^2}{x^2}}{3\left(b^6 - \frac{3(bx+2)b^5}{x} + \frac{3(bx+2)^2b^4}{x^2} - \frac{(bx+2)^3b^3}{x^3}\right)} + \frac{5 \log\left(-\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{2b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+2)^(1/2), x, algorithm="maxima")

[Out] -1/3*(33*sqrt(b*x + 2)*b^2/sqrt(x) - 40*(b*x + 2)^(3/2)*b/x^(3/2) + 15*(b*x + 2)^(5/2)/x^(5/2))/(b^6 - 3*(b*x + 2)*b^5/x + 3*(b*x + 2)^2*b^4/x^2 - (b*x + 2)^3*b^3/x^3) + 5/2*log(-(sqrt(b) - sqrt(b*x + 2)/sqrt(x))/(sqrt(b) + sqrt(b*x + 2)/sqrt(x)))/b^(7/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{\sqrt{bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x + 2)^(1/2), x)

[Out] int(x^(5/2)/(b*x + 2)^(1/2), x)

sympy [A] time = 7.40, size = 95, normalized size = 1.08

$$\frac{x^{\frac{7}{2}}}{3\sqrt{bx+2}} - \frac{x^{\frac{5}{2}}}{6b\sqrt{bx+2}} + \frac{5x^{\frac{3}{2}}}{6b^2\sqrt{bx+2}} + \frac{5\sqrt{x}}{b^3\sqrt{bx+2}} - \frac{5 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(5/2)/(b*x+2)**(1/2),x)
```

```
[Out] x**(7/2)/(3*sqrt(b*x + 2)) - x**(5/2)/(6*b*sqrt(b*x + 2)) + 5*x**(3/2)/(6*b  
**2*sqrt(b*x + 2)) + 5*sqrt(x)/(b**3*sqrt(b*x + 2)) - 5*asinh(sqrt(2)*sqrt(  
b)*sqrt(x)/2)/b**(7/2)
```

$$3.609 \quad \int \frac{x^{3/2}}{\sqrt{2+bx}} dx$$

Optimal. Leaf size=67

$$\frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{3\sqrt{x}\sqrt{bx+2}}{2b^2} + \frac{x^{3/2}\sqrt{bx+2}}{2b}$$

[Out] $3*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(5/2)}+1/2*x^{(3/2)}*(b*x+2)^{(1/2)}/b-3/2*x^{(1/2)}*(b*x+2)^{(1/2)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$-\frac{3\sqrt{x}\sqrt{bx+2}}{2b^2} + \frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{x^{3/2}\sqrt{bx+2}}{2b}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(3/2)}/\operatorname{Sqrt}[2 + b*x], x]$

[Out] $(-3*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/(2*b^2) + (x^{(3/2)}*\operatorname{Sqrt}[2 + b*x])/(2*b) + (3*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]])/b^{(5/2)}$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{GtQ}[n, 0] \ \&\& \ \operatorname{NeQ}[m+n+1, 0] \ \&\& \ !(\operatorname{IGtQ}[m, 0] \ \&\& \ (!\operatorname{IntegerQ}[n] \ || \ (\operatorname{GtQ}[m, 0] \ \&\& \ \operatorname{LtQ}[m-n, 0]))) \ \&\& \ !\operatorname{ILtQ}[m+n+2, 0] \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 54

$\operatorname{Int}[1/(\operatorname{Sqrt}[(a_.) + (b_.)*(x_)]*\operatorname{Sqrt}[(c_.) + (d_.)*(x_)]), x_Symbol] \rightarrow \operatorname{Dist}[2/\operatorname{Sqrt}[b], \operatorname{Subst}[\operatorname{Int}[1/\operatorname{Sqrt}[b*c - a*d + d*x^2], x], x, \operatorname{Sqrt}[a + b*x]], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{GtQ}[b*c - a*d, 0] \ \&\& \ \operatorname{GtQ}[b, 0]$

Rule 215

$\operatorname{Int}[1/\operatorname{Sqrt}[(a_.) + (b_.)*(x_)^2], x_Symbol] \rightarrow \operatorname{Simp}[\operatorname{ArcSinh}[(\operatorname{Rt}[b, 2]*x)/\operatorname{Sqrt}[a]]/\operatorname{Rt}[b, 2], x] /;$ $\operatorname{FreeQ}\{a, b, x\} \ \&\& \ \operatorname{GtQ}[a, 0] \ \&\& \ \operatorname{PosQ}[b]$

Rubi steps

$$\begin{aligned}
\int \frac{x^{3/2}}{\sqrt{2+bx}} dx &= \frac{x^{3/2}\sqrt{2+bx}}{2b} - \frac{3 \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx}{2b} \\
&= -\frac{3\sqrt{x}\sqrt{2+bx}}{2b^2} + \frac{x^{3/2}\sqrt{2+bx}}{2b} + \frac{3 \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx}{2b^2} \\
&= -\frac{3\sqrt{x}\sqrt{2+bx}}{2b^2} + \frac{x^{3/2}\sqrt{2+bx}}{2b} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\
&= -\frac{3\sqrt{x}\sqrt{2+bx}}{2b^2} + \frac{x^{3/2}\sqrt{2+bx}}{2b} + \frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 51, normalized size = 0.76

$$\frac{3 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{\sqrt{x}\sqrt{bx+2}(bx-3)}{2b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/Sqrt[2 + b*x], x]

[Out] (Sqrt[x]*(-3 + b*x)*Sqrt[2 + b*x])/(2*b^2) + (3*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(5/2)

fricas [A] time = 0.44, size = 105, normalized size = 1.57

$$\left[\frac{(b^2x - 3b)\sqrt{bx+2}\sqrt{x} + 3\sqrt{b}\log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1)}{2b^3}, \frac{(b^2x - 3b)\sqrt{bx+2}\sqrt{x} - 6\sqrt{-b}\arctan\left(\frac{\sqrt{bx+2}\sqrt{x}}{b\sqrt{x}}\right)}{2b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+2)^(1/2), x, algorithm="fricas")

[Out] [1/2*((b^2*x - 3*b)*sqrt(b*x + 2)*sqrt(x) + 3*sqrt(b)*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^3, 1/2*((b^2*x - 3*b)*sqrt(b*x + 2)*sqrt(x) - 6*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))))/b^3]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)/(b*x+2)^(1/2),x, algorithm="giac")`

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [85.3561567818,61.7937478349]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [71.707969239,78.6493344628] $2*\text{abs}(b)/b^2/b^2*(2*(1/8*\text{sqrt}(b*x+2))*\text{sqrt}(b*x+2)-5/8)*\text{sqrt}(b*x+2)*\text{sqrt}(b*(b*x+2)-2*b)-6*b/4/\text{sqrt}(b)*\ln(\text{abs}(\text{sqrt}(b*(b*x+2)-2*b)-\text{sqrt}(b)*\text{sqrt}(b*x+2))))$

maple [A] time = 0.00, size = 78, normalized size = 1.16

$$\frac{\sqrt{bx+2} x^{\frac{3}{2}}}{2b} - \frac{3\sqrt{bx+2} \sqrt{x}}{2b^2} + \frac{3\sqrt{(bx+2)x} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{2\sqrt{bx+2} b^{\frac{5}{2}} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(b*x+2)^(1/2),x)`

[Out] $\frac{1}{2}x^{3/2}(bx+2)^{1/2}/b - 3/2(bx+2)^{1/2}/b^2x^{1/2} + 3/2((bx+2)x)^{1/2}/(bx+2)^{1/2}/b^{5/2}/x^{1/2} * \ln((bx+1)/b^{1/2} + (bx^2+2x)^{1/2})$

maxima [B] time = 2.86, size = 102, normalized size = 1.52

$$\frac{\frac{5\sqrt{bx+2}b}{\sqrt{x}} - \frac{3(bx+2)^{\frac{3}{2}}}{x^{\frac{3}{2}}}}{b^4 - \frac{2(bx+2)b^3}{x} + \frac{(bx+2)^2b^2}{x^2}} - \frac{3 \log\left(-\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{2b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)/(b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $(5*\sqrt{bx+2}*b/\sqrt{x} - 3*(bx+2)^{(3/2)}/x^{(3/2)})/(b^4 - 2*(bx+2)*b^3/x + (bx+2)^2*b^2/x^2) - 3/2*\log(-(\sqrt{b} - \sqrt{bx+2}/\sqrt{x})/(\sqrt{b} + \sqrt{bx+2}/\sqrt{x}))/b^{(5/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{3/2}}{\sqrt{bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(b*x+2)^(1/2),x)`

[Out] `int(x^(3/2)/(b*x+2)^(1/2),x)`

sympy [A] time = 3.67, size = 75, normalized size = 1.12

$$\frac{x^{\frac{5}{2}}}{2\sqrt{bx+2}} - \frac{x^{\frac{3}{2}}}{2b\sqrt{bx+2}} - \frac{3\sqrt{x}}{b^2\sqrt{bx+2}} + \frac{3 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(b*x+2)**(1/2),x)`

[Out] $x^{(5/2)}/(2*\sqrt{bx+2}) - x^{(3/2)}/(2*b*\sqrt{bx+2}) - 3*\sqrt{x}/(b^{**2}*\sqrt{bx+2}) + 3*\operatorname{asinh}(\sqrt{2}*\sqrt{b}*\sqrt{x})/2/b^{(5/2)}$

$$3.610 \quad \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx$$

Optimal. Leaf size=43

$$\frac{\sqrt{x} \sqrt{bx+2}}{b} - \frac{2 \sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}$$

[Out] $-2*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(3/2)}+x^{(1/2)}*(b*x+2)^{(1/2)}/b$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 54, 215}

$$\frac{\sqrt{x} \sqrt{bx+2}}{b} - \frac{2 \sinh^{-1}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/Sqrt[2 + b*x], x]

[Out] (Sqrt[x]*Sqrt[2 + b*x])/b - (2*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(3/2)

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 215

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{x}}{\sqrt{2+bx}} dx &= \frac{\sqrt{x} \sqrt{2+bx}}{b} - \frac{\int \frac{1}{\sqrt{x} \sqrt{2+bx}} dx}{b} \\
&= \frac{\sqrt{x} \sqrt{2+bx}}{b} - \frac{2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x} \right)}{b} \\
&= \frac{\sqrt{x} \sqrt{2+bx}}{b} - \frac{2 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 43, normalized size = 1.00

$$\frac{\sqrt{x} \sqrt{bx+2}}{b} - \frac{2 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/Sqrt[2 + b*x], x]

[Out] (Sqrt[x]*Sqrt[2 + b*x])/b - (2*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(3/2)

fricas [A] time = 0.43, size = 87, normalized size = 2.02

$$\left[\frac{\sqrt{bx+2} b \sqrt{x} + \sqrt{b} \log(bx - \sqrt{bx+2} \sqrt{b} \sqrt{x} + 1)}{b^2}, \frac{\sqrt{bx+2} b \sqrt{x} + 2 \sqrt{-b} \arctan\left(\frac{\sqrt{bx+2} \sqrt{-b}}{b \sqrt{x}}\right)}{b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+2)^(1/2), x, algorithm="fricas")

[Out] [(sqrt(b*x + 2)*b*sqrt(x) + sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1))/b^2, (sqrt(b*x + 2)*b*sqrt(x) + 2*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))))/b^2]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+2)^(1/2), x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [85.3561567 818,61.7937478349]Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [71.707969239,78.6493344628]2*abs(b)/b^2/b*(1/2*sqrt(b*x+2)*sqrt(b*(b*x+2)-2*b)+2*b/2/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2))))

maple [A] time = 0.00, size = 62, normalized size = 1.44

$$\frac{\sqrt{bx+2} \sqrt{x}}{b} - \frac{\sqrt{(bx+2)x} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{\sqrt{bx+2} b^{\frac{3}{2}} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x+2)^(1/2),x)

[Out] (b*x+2)^(1/2)/b*x^(1/2)-((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)/b^(3/2)/x^(1/2)*ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))

maxima [B] time = 2.92, size = 70, normalized size = 1.63

$$\frac{\log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{b^{\frac{3}{2}}}-\frac{2\sqrt{bx+2}}{\left(b^2-\frac{(bx+2)b}{x}\right)\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")

[Out] log(-(sqrt(b) - sqrt(b*x + 2)/sqrt(x))/(sqrt(b) + sqrt(b*x + 2)/sqrt(x)))/b^(3/2) - 2*sqrt(b*x + 2)/((b^2 - (b*x + 2)*b/x)*sqrt(x))

mupad [B] time = 0.59, size = 43, normalized size = 1.00

$$\frac{4 \operatorname{atanh}\left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}-\sqrt{bx+2}}\right)}{b^{3/2}} + \frac{\sqrt{x} \sqrt{bx+2}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x + 2)^(1/2),x)

[Out] (4*atanh((b^(1/2)*x^(1/2))/(2^(1/2) - (b*x + 2)^(1/2))))/b^(3/2) + (x^(1/2)*(b*x + 2)^(1/2))/b

sympy [A] time = 1.93, size = 54, normalized size = 1.26

$$\frac{x^{\frac{3}{2}}}{\sqrt{bx+2}} + \frac{2\sqrt{x}}{b\sqrt{bx+2}} - \frac{2 \operatorname{asinh}\left(\frac{\sqrt{2} \sqrt{b} \sqrt{x}}{2}\right)}{b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(1/2)/(b*x+2)**(1/2),x)

[Out] x**(3/2)/sqrt(b*x + 2) + 2*sqrt(x)/(b*sqrt(b*x + 2)) - 2*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2)

$$3.611 \quad \int \frac{1}{\sqrt{x} \sqrt{2+bx}} dx$$

Optimal. Leaf size=24

$$\frac{2 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}$$

[Out] 2*arcsinh(1/2*b^(1/2)*x^(1/2)*2^(1/2))/b^(1/2)

Rubi [A] time = 0.01, antiderivative size = 24, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {54, 215}

$$\frac{2 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*Sqrt[2 + b*x]),x]

[Out] (2*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{x} \sqrt{2+bx}} dx &= 2 \text{Subst} \left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x} \right) \\ &= \frac{2 \sinh^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 1.00

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*Sqrt[2 + b*x]),x]

[Out] (2*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

fricas [A] time = 0.46, size = 55, normalized size = 2.29

$$\left[\frac{\log\left(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1\right)}{\sqrt{b}}, -\frac{2\sqrt{-b}\arctan\left(\frac{\sqrt{bx+2}\sqrt{-b}}{b\sqrt{x}}\right)}{b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")

[Out] [log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1)/sqrt(b), -2*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x)))/b]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{-4,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,2]%%}+%%{28,[1,1]%%}+%%{8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{-4,[3,3]%%}+%%{4,[3,2]%%}+%%{4,[3,1]%%}+%%{-4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{4,[1,3]%%}+%%{20,[1,2]%%}+%%{-128,[1,1]%%}+%%{16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{-4,[3,4]%%}+%%{12,[3,3]%%}+%%{-20,[3,2]%%}+%%{20,[3,1]%%}+%%{-8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{-4,[1,4]%%}+%%{20,[1,3]%%}+%%{-40,[1,2]%%}+%%{48,[1,1]%%}+%%{-32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,

2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [85.3561567 818,61.7937478349]Warning, choosing root of [1,0,%%{-4, [1,1]%%}+%%{-4, [1,0]%%}+%%{-4, [0,1]%%}+%%{-8, [0,0]%%}, 0,%%{6, [2,2]%%}+%%{4, [2,1]%%}+%%{6, [2,0]%%}+%%{4, [1,2]%%}+%%{28, [1,1]%%}+%%{8, [1,0]%%}+%%{6, [0,2]%%}+%%{8, [0,1]%%}+%%{24, [0,0]%%}, 0,%%{-4, [3,3]%%}+%%{4, [3,2]%%}+%%{4, [3,1]%%}+%%{-4, [3,0]%%}+%%{4, [2,3]%%}+%%{-64, [2,2]%%}+%%{20, [2,1]%%}+%%{8, [2,0]%%}+%%{4, [1,3]%%}+%%{20, [1,2]%%}+%%{-128, [1,1]%%}+%%{16, [1,0]%%}+%%{-4, [0,3]%%}+%%{8, [0,2]%%}+%%{16, [0,1]%%}+%%{-32, [0,0]%%}, 0,%%{1, [4,4]%%}+%%{-4, [4,3]%%}+%%{6, [4,2]%%}+%%{-4, [4,1]%%}+%%{1, [4,0]%%}+%%{-4, [3,4]%%}+%%{12, [3,3]%%}+%%{-20, [3,2]%%}+%%{20, [3,1]%%}+%%{-8, [3,0]%%}+%%{6, [2,4]%%}+%%{-20, [2,3]%%}+%%{46, [2,2]%%}+%%{-40, [2,1]%%}+%%{24, [2,0]%%}+%%{-4, [1,4]%%}+%%{20, [1,3]%%}+%%{-40, [1,2]%%}+%%{48, [1,1]%%}+%%{-32, [1,0]%%}+%%{1, [0,4]%%}+%%{-8, [0,3]%%}+%%{24, [0,2]%%}+%%{-32, [0,1]%%}+%%{16, [0,0]%%}] at parameters values [71.707969239, 78.6493344628] -2/abs(b)*b^2/b/sqrt(b)*ln(abs(sqrt(b*(b*x+2)-2*b)-sqrt(b)*sqrt(b*x+2)))

maple [B] time = 0.00, size = 46, normalized size = 1.92

$$\frac{\sqrt{(bx+2)x} \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{\sqrt{bx+2} \sqrt{b} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/2)/(b*x+2)^(1/2),x)

[Out] ((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)/b^(1/2)/x^(1/2)*ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))

maxima [B] time = 2.96, size = 41, normalized size = 1.71

$$\frac{\log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")

[Out] -log(-(sqrt(b) - sqrt(b*x + 2)/sqrt(x))/(sqrt(b) + sqrt(b*x + 2)/sqrt(x)))/sqrt(b)

mupad [B] time = 0.04, size = 30, normalized size = 1.25

$$\frac{4 \operatorname{atan}\left(\frac{\sqrt{2}-\sqrt{bx+2}}{\sqrt{-b} \sqrt{x}}\right)}{\sqrt{-b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(b*x + 2)^(1/2)),x)`

[Out] `(4*atan((2^(1/2) - (b*x + 2)^(1/2))/((-b)^(1/2)*x^(1/2))))/(-b)^(1/2)`

sympy [A] time = 1.02, size = 24, normalized size = 1.00

$$\frac{2 \operatorname{asinh}\left(\frac{\sqrt{2} \sqrt{b} \sqrt{x}}{2}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(1/2)/(b*x+2)**(1/2),x)`

[Out] `2*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/sqrt(b)`

$$3.612 \quad \int \frac{1}{x^{3/2} \sqrt{2+bx}} dx$$

Optimal. Leaf size=16

$$-\frac{\sqrt{bx+2}}{\sqrt{x}}$$

[Out] $-(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$-\frac{\sqrt{bx+2}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*Sqrt[2 + b*x]),x]

[Out] -(Sqrt[2 + b*x]/Sqrt[x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{3/2} \sqrt{2+bx}} dx = -\frac{\sqrt{2+bx}}{\sqrt{x}}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$-\frac{\sqrt{bx+2}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*Sqrt[2 + b*x]),x]

[Out] -(Sqrt[2 + b*x]/Sqrt[x])

fricas [A] time = 0.42, size = 12, normalized size = 0.75

$$-\frac{\sqrt{bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+2)^(1/2),x, algorithm="fricas")

[Out] -sqrt(b*x + 2)/sqrt(x)

giac [B] time = 1.11, size = 29, normalized size = 1.81

$$-\frac{\sqrt{bx+2}b^2}{\sqrt{(bx+2)b-2b|b|}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] -sqrt(b*x + 2)*b^2/(sqrt((b*x + 2)*b - 2*b)*abs(b))

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$-\frac{\sqrt{bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2)/(b*x+2)^(1/2),x)

[Out] -(b*x+2)^(1/2)/x^(1/2)

maxima [A] time = 1.35, size = 12, normalized size = 0.75

$$-\frac{\sqrt{bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+2)^(1/2),x, algorithm="maxima")

[Out] -sqrt(b*x + 2)/sqrt(x)

mupad [B] time = 0.33, size = 12, normalized size = 0.75

$$-\frac{\sqrt{bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(x^(3/2)*(b*x + 2)^(1/2)),x)
```

```
[Out] -(b*x + 2)^(1/2)/x^(1/2)
```

```
sympy [A] time = 0.88, size = 15, normalized size = 0.94
```

$$-\sqrt{b} \sqrt{1 + \frac{2}{bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**(3/2)/(b*x+2)**(1/2),x)
```

```
[Out] -sqrt(b)*sqrt(1 + 2/(b*x))
```

$$3.613 \quad \int \frac{1}{x^{5/2} \sqrt{2+bx}} dx$$

Optimal. Leaf size=38

$$\frac{b\sqrt{bx+2}}{3\sqrt{x}} - \frac{\sqrt{bx+2}}{3x^{3/2}}$$

[Out] $-1/3*(b*x+2)^{(1/2)}/x^{(3/2)}+1/3*b*(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{b\sqrt{bx+2}}{3\sqrt{x}} - \frac{\sqrt{bx+2}}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] `Int[1/(x^(5/2)*Sqrt[2 + b*x]),x]`

[Out] $-\text{Sqrt}[2 + b*x]/(3*x^{(3/2)}) + (b*\text{Sqrt}[2 + b*x])/(3*\text{Sqrt}[x])$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
  implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{x^{5/2}\sqrt{2+bx}} dx = -\frac{\sqrt{2+bx}}{3x^{3/2}} - \frac{1}{3}b \int \frac{1}{x^{3/2}\sqrt{2+bx}} dx$$

$$= -\frac{\sqrt{2+bx}}{3x^{3/2}} + \frac{b\sqrt{2+bx}}{3\sqrt{x}}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.61

$$\frac{(bx-1)\sqrt{bx+2}}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*Sqrt[2 + b*x]), x]

[Out] ((-1 + b*x)*Sqrt[2 + b*x])/(3*x^(3/2))

fricas [A] time = 0.42, size = 17, normalized size = 0.45

$$\frac{\sqrt{bx+2}(bx-1)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+2)^(1/2), x, algorithm="fricas")

[Out] 1/3*sqrt(b*x + 2)*(b*x - 1)/x^(3/2)

giac [A] time = 1.09, size = 42, normalized size = 1.11

$$\frac{((bx+2)b^3 - 3b^3)\sqrt{bx+2}b}{3((bx+2)b - 2b)^{\frac{3}{2}}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+2)^(1/2), x, algorithm="giac")

[Out] 1/3*((b*x + 2)*b^3 - 3*b^3)*sqrt(b*x + 2)*b/(((b*x + 2)*b - 2*b)^(3/2)*abs(b))

maple [A] time = 0.00, size = 18, normalized size = 0.47

$$\frac{\sqrt{bx+2}(bx-1)}{3x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/2)/(b*x+2)^(1/2),x)`

[Out] $1/3*(b*x+2)^(1/2)*(b*x-1)/x^(3/2)$

maxima [A] time = 1.32, size = 26, normalized size = 0.68

$$\frac{\sqrt{bx+2}b}{2\sqrt{x}} - \frac{(bx+2)^{\frac{3}{2}}}{6x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2)/(b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $1/2*\text{sqrt}(b*x + 2)*b/\text{sqrt}(x) - 1/6*(b*x + 2)^(3/2)/x^(3/2)$

mupad [B] time = 0.32, size = 17, normalized size = 0.45

$$\frac{\sqrt{bx+2} \left(\frac{bx}{3} - \frac{1}{3} \right)}{x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/2)*(b*x + 2)^(1/2)),x)`

[Out] $((b*x + 2)^(1/2)*((b*x)/3 - 1/3))/x^(3/2)$

sympy [A] time = 1.87, size = 34, normalized size = 0.89

$$\frac{b^{\frac{3}{2}}\sqrt{1+\frac{2}{bx}}}{3} - \frac{\sqrt{b}\sqrt{1+\frac{2}{bx}}}{3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(b*x+2)**(1/2),x)`

[Out] $b**(3/2)*\text{sqrt}(1 + 2/(b*x))/3 - \text{sqrt}(b)*\text{sqrt}(1 + 2/(b*x))/(3*x)$

$$3.614 \quad \int \frac{1}{x^{7/2} \sqrt{2+bx}} dx$$

Optimal. Leaf size=59

$$-\frac{2b^2\sqrt{bx+2}}{15\sqrt{x}} + \frac{2b\sqrt{bx+2}}{15x^{3/2}} - \frac{\sqrt{bx+2}}{5x^{5/2}}$$

[Out] $-1/5*(b*x+2)^{(1/2)}/x^{(5/2)}+2/15*b*(b*x+2)^{(1/2)}/x^{(3/2)}-2/15*b^2*(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{2b^2\sqrt{bx+2}}{15\sqrt{x}} + \frac{2b\sqrt{bx+2}}{15x^{3/2}} - \frac{\sqrt{bx+2}}{5x^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(7/2)*Sqrt[2 + b*x]), x]

[Out] $-\text{Sqrt}[2 + b*x]/(5*x^{(5/2)}) + (2*b*\text{Sqrt}[2 + b*x])/(15*x^{(3/2)}) - (2*b^2*\text{Sqrt}[2 + b*x])/(15*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{7/2}\sqrt{2+bx}} dx &= -\frac{\sqrt{2+bx}}{5x^{5/2}} - \frac{1}{5}(2b) \int \frac{1}{x^{5/2}\sqrt{2+bx}} dx \\
&= -\frac{\sqrt{2+bx}}{5x^{5/2}} + \frac{2b\sqrt{2+bx}}{15x^{3/2}} + \frac{1}{15}(2b^2) \int \frac{1}{x^{3/2}\sqrt{2+bx}} dx \\
&= -\frac{\sqrt{2+bx}}{5x^{5/2}} + \frac{2b\sqrt{2+bx}}{15x^{3/2}} - \frac{2b^2\sqrt{2+bx}}{15\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 0.54

$$-\frac{\sqrt{bx+2}(2b^2x^2-2bx+3)}{15x^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(7/2)*Sqrt[2 + b*x]), x]

[Out] -1/15*(Sqrt[2 + b*x]*(3 - 2*b*x + 2*b^2*x^2))/x^(5/2)

fricas [A] time = 0.42, size = 26, normalized size = 0.44

$$-\frac{(2b^2x^2-2bx+3)\sqrt{bx+2}}{15x^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+2)^(1/2), x, algorithm="fricas")

[Out] -1/15*(2*b^2*x^2 - 2*b*x + 3)*sqrt(b*x + 2)/x^(5/2)

giac [A] time = 1.06, size = 55, normalized size = 0.93

$$-\frac{(15b^5 + 2((bx+2)b^5 - 5b^5)(bx+2))\sqrt{bx+2}b}{15((bx+2)b - 2b)^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+2)^(1/2), x, algorithm="giac")

[Out] -1/15*(15*b^5 + 2*((b*x + 2)*b^5 - 5*b^5)*(b*x + 2))*sqrt(b*x + 2)*b/(((b*x + 2)*b - 2*b)^(5/2)*abs(b))

maple [A] time = 0.01, size = 27, normalized size = 0.46

$$-\frac{\sqrt{bx+2} (2b^2x^2 - 2bx + 3)}{15x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(7/2)/(b*x+2)^(1/2),x)

[Out] -1/15*(b*x+2)^(1/2)*(2*b^2*x^2-2*b*x+3)/x^(5/2)

maxima [A] time = 1.31, size = 41, normalized size = 0.69

$$-\frac{\sqrt{bx+2}b^2}{4\sqrt{x}} + \frac{(bx+2)^{\frac{3}{2}}b}{6x^{\frac{3}{2}}} - \frac{(bx+2)^{\frac{5}{2}}}{20x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+2)^(1/2),x, algorithm="maxima")

[Out] -1/4*sqrt(b*x + 2)*b^2/sqrt(x) + 1/6*(b*x + 2)^(3/2)*b/x^(3/2) - 1/20*(b*x + 2)^(5/2)/x^(5/2)

mupad [B] time = 0.32, size = 26, normalized size = 0.44

$$-\frac{\sqrt{bx+2} \left(\frac{2b^2x^2}{15} - \frac{2bx}{15} + \frac{1}{5} \right)}{x^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(7/2)*(b*x + 2)^(1/2)),x)

[Out] -((b*x + 2)^(1/2)*((2*b^2*x^2)/15 - (2*b*x)/15 + 1/5))/x^(5/2)

sympy [B] time = 6.10, size = 224, normalized size = 3.80

$$\frac{2b^{\frac{17}{2}}x^4\sqrt{1+\frac{2}{bx}}}{15b^6x^4+60b^5x^3+60b^4x^2} - \frac{6b^{\frac{15}{2}}x^3\sqrt{1+\frac{2}{bx}}}{15b^6x^4+60b^5x^3+60b^4x^2} - \frac{3b^{\frac{13}{2}}x^2\sqrt{1+\frac{2}{bx}}}{15b^6x^4+60b^5x^3+60b^4x^2} - \frac{4b^{\frac{11}{2}}x\sqrt{1+\frac{2}{bx}}}{15b^6x^4+60b^5x^3+60b^4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(7/2)/(b*x+2)**(1/2),x)

[Out] -2*b**(17/2)*x**4*sqrt(1 + 2/(b*x))/(15*b**6*x**4 + 60*b**5*x**3 + 60*b**4*x**2) - 6*b**(15/2)*x**3*sqrt(1 + 2/(b*x))/(15*b**6*x**4 + 60*b**5*x**3 + 60*b**4*x**2)

$$\begin{aligned} & 0*b^{**4}*x^{**2}) - 3*b^{**}(13/2)*x^{**2}*sqrt(1 + 2/(b*x))/(15*b^{**6}*x^{**4} + 60*b^{**5}*x \\ & **3 + 60*b^{**4}*x^{**2}) - 4*b^{**}(11/2)*x*sqrt(1 + 2/(b*x))/(15*b^{**6}*x^{**4} + 60*b* \\ & *5*x^{**3} + 60*b^{**4}*x^{**2}) - 12*b^{**}(9/2)*sqrt(1 + 2/(b*x))/(15*b^{**6}*x^{**4} + 60* \\ & b^{**5}*x^{**3} + 60*b^{**4}*x^{**2}) \end{aligned}$$

$$3.615 \quad \int \frac{1}{x^{9/2} \sqrt{2+bx}} dx$$

Optimal. Leaf size=80

$$\frac{2b^3 \sqrt{bx+2}}{35\sqrt{x}} - \frac{2b^2 \sqrt{bx+2}}{35x^{3/2}} + \frac{3b \sqrt{bx+2}}{35x^{5/2}} - \frac{\sqrt{bx+2}}{7x^{7/2}}$$

[Out] $-1/7*(b*x+2)^{(1/2)}/x^{(7/2)}+3/35*b*(b*x+2)^{(1/2)}/x^{(5/2)}-2/35*b^2*(b*x+2)^{(1/2)}/x^{(3/2)}+2/35*b^3*(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{2b^2 \sqrt{bx+2}}{35x^{3/2}} + \frac{2b^3 \sqrt{bx+2}}{35\sqrt{x}} + \frac{3b \sqrt{bx+2}}{35x^{5/2}} - \frac{\sqrt{bx+2}}{7x^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(9/2)*Sqrt[2 + b*x]), x]

[Out] $-\text{Sqrt}[2 + b*x]/(7*x^{(7/2)}) + (3*b*\text{Sqrt}[2 + b*x])/(35*x^{(5/2)}) - (2*b^2*\text{Sqrt}[2 + b*x])/(35*x^{(3/2)}) + (2*b^3*\text{Sqrt}[2 + b*x])/(35*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{9/2}\sqrt{2+bx}} dx &= -\frac{\sqrt{2+bx}}{7x^{7/2}} - \frac{1}{7}(3b) \int \frac{1}{x^{7/2}\sqrt{2+bx}} dx \\
&= -\frac{\sqrt{2+bx}}{7x^{7/2}} + \frac{3b\sqrt{2+bx}}{35x^{5/2}} + \frac{1}{35}(6b^2) \int \frac{1}{x^{5/2}\sqrt{2+bx}} dx \\
&= -\frac{\sqrt{2+bx}}{7x^{7/2}} + \frac{3b\sqrt{2+bx}}{35x^{5/2}} - \frac{2b^2\sqrt{2+bx}}{35x^{3/2}} - \frac{1}{35}(2b^3) \int \frac{1}{x^{3/2}\sqrt{2+bx}} dx \\
&= -\frac{\sqrt{2+bx}}{7x^{7/2}} + \frac{3b\sqrt{2+bx}}{35x^{5/2}} - \frac{2b^2\sqrt{2+bx}}{35x^{3/2}} + \frac{2b^3\sqrt{2+bx}}{35\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 0.50

$$\frac{\sqrt{bx+2} (2b^3x^3 - 2b^2x^2 + 3bx - 5)}{35x^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(9/2)*Sqrt[2 + b*x]), x]

[Out] (Sqrt[2 + b*x]*(-5 + 3*b*x - 2*b^2*x^2 + 2*b^3*x^3))/(35*x^(7/2))

fricas [A] time = 0.41, size = 34, normalized size = 0.42

$$\frac{(2b^3x^3 - 2b^2x^2 + 3bx - 5)\sqrt{bx+2}}{35x^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(9/2)/(b*x+2)^(1/2), x, algorithm="fricas")

[Out] 1/35*(2*b^3*x^3 - 2*b^2*x^2 + 3*b*x - 5)*sqrt(b*x + 2)/x^(7/2)

giac [A] time = 1.03, size = 68, normalized size = 0.85

$$\frac{(35b^7 - (35b^7 + 2((bx+2)b^7 - 7b^7)(bx+2))(bx+2))\sqrt{bx+2}b}{35((bx+2)b - 2b)^2|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(9/2)/(b*x+2)^(1/2), x, algorithm="giac")

[Out] $-1/35*(35*b^7 - (35*b^7 + 2*((b*x + 2)*b^7 - 7*b^7)*(b*x + 2))*(b*x + 2))*\text{sqrt}(b*x + 2)*b/(((b*x + 2)*b - 2*b)^{(7/2)}*abs(b))$

maple [A] time = 0.01, size = 35, normalized size = 0.44

$$\frac{\sqrt{bx+2} (2b^3x^3 - 2b^2x^2 + 3bx - 5)}{35x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/x^{(9/2)}/(b*x+2)^{(1/2)}, x)$

[Out] $1/35*(b*x+2)^{(1/2)}*(2*b^3*x^3-2*b^2*x^2+3*b*x-5)/x^{(7/2)}$

maxima [A] time = 1.29, size = 56, normalized size = 0.70

$$\frac{\sqrt{bx+2} b^3}{8\sqrt{x}} - \frac{(bx+2)^{\frac{3}{2}} b^2}{8x^{\frac{3}{2}}} + \frac{3(bx+2)^{\frac{5}{2}} b}{40x^{\frac{5}{2}}} - \frac{(bx+2)^{\frac{7}{2}}}{56x^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^{(9/2)}/(b*x+2)^{(1/2)}, x, \text{algorithm}="maxima")$

[Out] $1/8*\text{sqrt}(b*x + 2)*b^3/\text{sqrt}(x) - 1/8*(b*x + 2)^{(3/2)}*b^2/x^{(3/2)} + 3/40*(b*x + 2)^{(5/2)}*b/x^{(5/2)} - 1/56*(b*x + 2)^{(7/2)}/x^{(7/2)}$

mupad [B] time = 0.33, size = 33, normalized size = 0.41

$$\frac{\sqrt{bx+2} \left(\frac{2b^3x^3}{35} - \frac{2b^2x^2}{35} + \frac{3bx}{35} - \frac{1}{7} \right)}{x^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(x^{(9/2)}*(b*x + 2)^{(1/2)}), x)$

[Out] $((b*x + 2)^{(1/2)}*((3*b*x)/35 - (2*b^2*x^2)/35 + (2*b^3*x^3)/35 - 1/7))/x^{(7/2)}$

sympy [B] time = 15.99, size = 374, normalized size = 4.68

$$\frac{2b^{\frac{31}{2}}x^6\sqrt{1+\frac{2}{bx}}}{35b^{12}x^6 + 210b^{11}x^5 + 420b^{10}x^4 + 280b^9x^3} + \frac{10b^{\frac{29}{2}}x^5\sqrt{1+\frac{2}{bx}}}{35b^{12}x^6 + 210b^{11}x^5 + 420b^{10}x^4 + 280b^9x^3} + \frac{15b^{\frac{27}{2}}x^4\sqrt{1+\frac{2}{bx}}}{35b^{12}x^6 + 210b^{11}x^5 + 420b^{10}x^4 + 280b^9x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(9/2)/(b*x+2)**(1/2),x)

[Out] $2*b^{31/2}*x^6*\sqrt{1 + 2/(b*x)}/(35*b^{12}*x^6 + 210*b^{11}*x^5 + 420*b^{10}*x^4 + 280*b^9*x^3) + 10*b^{29/2}*x^5*\sqrt{1 + 2/(b*x)}/(35*b^{12}*x^6 + 210*b^{11}*x^5 + 420*b^{10}*x^4 + 280*b^9*x^3) + 15*b^{27/2}*x^4*\sqrt{1 + 2/(b*x)}/(35*b^{12}*x^6 + 210*b^{11}*x^5 + 420*b^{10}*x^4 + 280*b^9*x^3) + 5*b^{25/2}*x^3*\sqrt{1 + 2/(b*x)}/(35*b^{12}*x^6 + 210*b^{11}*x^5 + 420*b^{10}*x^4 + 280*b^9*x^3) - 10*b^{23/2}*x^2*\sqrt{1 + 2/(b*x)}/(35*b^{12}*x^6 + 210*b^{11}*x^5 + 420*b^{10}*x^4 + 280*b^9*x^3) - 36*b^{21/2}*x*\sqrt{1 + 2/(b*x)}/(35*b^{12}*x^6 + 210*b^{11}*x^5 + 420*b^{10}*x^4 + 280*b^9*x^3) - 40*b^{19/2}*sqrt(1 + 2/(b*x))/(35*b^{12}*x^6 + 210*b^{11}*x^5 + 420*b^{10}*x^4 + 280*b^9*x^3)$

$$3.616 \quad \int \frac{x^{5/2}}{(2+bx)^{3/2}} dx$$

Optimal. Leaf size=86

$$\frac{15 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} - \frac{15\sqrt{x}\sqrt{bx+2}}{2b^3} + \frac{5x^{3/2}\sqrt{bx+2}}{2b^2} - \frac{2x^{5/2}}{b\sqrt{bx+2}}$$

[Out] 15*arcsinh(1/2*b^(1/2)*x^(1/2)*2^(1/2))/b^(7/2)-2*x^(5/2)/b/(b*x+2)^(1/2)+5/2*x^(3/2)*(b*x+2)^(1/2)/b^2-15/2*x^(1/2)*(b*x+2)^(1/2)/b^3

Rubi [A] time = 0.02, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 54, 215}

$$\frac{5x^{3/2}\sqrt{bx+2}}{2b^2} - \frac{15\sqrt{x}\sqrt{bx+2}}{2b^3} + \frac{15 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} - \frac{2x^{5/2}}{b\sqrt{bx+2}}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)/(2 + b*x)^(3/2), x]

[Out] (-2*x^(5/2))/(b*Sqrt[2 + b*x]) - (15*Sqrt[x]*Sqrt[2 + b*x])/(2*b^3) + (5*x^(3/2)*Sqrt[2 + b*x])/(2*b^2) + (15*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(7/2)

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(2+bx)^{3/2}} dx &= -\frac{2x^{5/2}}{b\sqrt{2+bx}} + \frac{5 \int \frac{x^{3/2}}{\sqrt{2+bx}} dx}{b} \\
&= -\frac{2x^{5/2}}{b\sqrt{2+bx}} + \frac{5x^{3/2}\sqrt{2+bx}}{2b^2} - \frac{15 \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx}{2b^2} \\
&= -\frac{2x^{5/2}}{b\sqrt{2+bx}} - \frac{15\sqrt{x}\sqrt{2+bx}}{2b^3} + \frac{5x^{3/2}\sqrt{2+bx}}{2b^2} + \frac{15 \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx}{2b^3} \\
&= -\frac{2x^{5/2}}{b\sqrt{2+bx}} - \frac{15\sqrt{x}\sqrt{2+bx}}{2b^3} + \frac{5x^{3/2}\sqrt{2+bx}}{2b^2} + \frac{15 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right)}{b^3} \\
&= -\frac{2x^{5/2}}{b\sqrt{2+bx}} - \frac{15\sqrt{x}\sqrt{2+bx}}{2b^3} + \frac{5x^{3/2}\sqrt{2+bx}}{2b^2} + \frac{15 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.35

$$\frac{x^{7/2} {}_2F_1\left(\frac{3}{2}, \frac{7}{2}; \frac{9}{2}; -\frac{bx}{2}\right)}{7\sqrt{2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(5/2)/(2 + b*x)^(3/2), x]
```

```
[Out] (x^(7/2)*Hypergeometric2F1[3/2, 7/2, 9/2, -1/2*(b*x)])/(7*Sqrt[2])
```

fricas [A] time = 0.46, size = 152, normalized size = 1.77

$$\left[\frac{15 (bx + 2)\sqrt{b} \log (bx + \sqrt{bx + 2} \sqrt{b} \sqrt{x} + 1) + (b^3 x^2 - 5 b^2 x - 30 b)\sqrt{bx + 2} \sqrt{x}}{2 (b^5 x + 2 b^4)}, -\frac{30 (bx + 2)\sqrt{-b} \arctan \left(\frac{\sqrt{bx + 2} \sqrt{b} \sqrt{x}}{\sqrt{-b}} \right)}{2 (b^5 x + 2 b^4)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+2)^(3/2),x, algorithm="fricas")

[Out] [1/2*(15*(b*x + 2)*sqrt(b)*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1) + (b^3*x^2 - 5*b^2*x - 30*b)*sqrt(b*x + 2)*sqrt(x))/(b^5*x + 2*b^4), -1/2*(30*(b*x + 2)*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))) - (b^3*x^2 - 5*b^2*x - 30*b)*sqrt(b*x + 2)*sqrt(x))/(b^5*x + 2*b^4)]

giac [A] time = 11.12, size = 119, normalized size = 1.38

$$\left(\frac{\sqrt{(bx + 2)b - 2b} \sqrt{bx + 2} \left(\frac{bx + 2}{b^3} - \frac{9}{b^3} \right) - \frac{15 \log \left(\left(\sqrt{bx + 2} \sqrt{b} - \sqrt{(bx + 2)b - 2b} \right)^2 \right)}{b^{\frac{5}{2}}} - \frac{64}{\left(\left(\sqrt{bx + 2} \sqrt{b} - \sqrt{(bx + 2)b - 2b} \right)^2 + 2b \right) b^{\frac{3}{2}}}}{2 b^2} \right) |b|$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+2)^(3/2),x, algorithm="giac")

[Out] 1/2*(sqrt((b*x + 2)*b - 2*b)*sqrt(b*x + 2)*((b*x + 2)/b^3 - 9/b^3) - 15*log((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2/b^(5/2) - 64/(((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2 + 2*b)*b^(3/2)))*abs(b)/b^2

maple [A] time = 0.03, size = 106, normalized size = 1.23

$$\frac{\left(\frac{15 \ln \left(\frac{bx + 1}{\sqrt{b}} + \sqrt{bx^2 + 2x} \right)}{2b^{\frac{7}{2}}} - \frac{8 \sqrt{\left(x + \frac{2}{b} \right)^2 b - 2x - \frac{4}{b}}}{\left(x + \frac{2}{b} \right) b^4} \right) \sqrt{(bx + 2)x}}{\sqrt{bx + 2} \sqrt{x}} + \frac{(bx - 7) \sqrt{bx + 2} \sqrt{x}}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x+2)^(3/2),x)

[Out] 1/2*(b*x-7)*(b*x+2)^(1/2)*x^(1/2)/b^3+(15/2/b^(7/2)*ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))-8/b^4/(x+2/b)*(b*(x+2/b)^2-2*x-4/b)^(1/2))*((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)/x^(1/2)

maxima [A] time = 3.06, size = 119, normalized size = 1.38

$$-\frac{8b^2 - \frac{25(bx+2)b}{x} + \frac{15(bx+2)^2}{x^2}}{\frac{\sqrt{bx+2}b^5}{\sqrt{x}} - \frac{2(bx+2)^{\frac{3}{2}}b^4}{x^{\frac{3}{2}}} + \frac{(bx+2)^{\frac{5}{2}}b^3}{x^{\frac{5}{2}}}} - \frac{15 \log\left(-\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{2b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+2)^(3/2),x, algorithm="maxima")

[Out] $-(8*b^2 - 25*(b*x + 2)*b/x + 15*(b*x + 2)^2/x^2)/(\sqrt{b*x + 2})*b^5/\sqrt{x} - 2*(b*x + 2)^{(3/2)}*b^4/x^{(3/2)} + (b*x + 2)^{(5/2)}*b^3/x^{(5/2)} - 15/2*\log(-(\sqrt{b} - \sqrt{b*x + 2})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x + 2})/\sqrt{x})/b^{(7/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{(bx+2)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x + 2)^(3/2),x)

[Out] int(x^(5/2)/(b*x + 2)^(3/2), x)

sympy [A] time = 7.10, size = 80, normalized size = 0.93

$$\frac{x^{\frac{5}{2}}}{2b\sqrt{bx+2}} - \frac{5x^{\frac{3}{2}}}{2b^2\sqrt{bx+2}} - \frac{15\sqrt{x}}{b^3\sqrt{bx+2}} + \frac{15 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(b*x+2)**(3/2),x)

[Out] $x^{(5/2)}/(2*b*\sqrt{b*x + 2}) - 5*x^{(3/2)}/(2*b**2*\sqrt{b*x + 2}) - 15*\sqrt{x}/(b**3*\sqrt{b*x + 2}) + 15*\operatorname{asinh}(\sqrt{2}*\sqrt{b}*\sqrt{x}/2)/b^{(7/2)}$

$$3.617 \quad \int \frac{x^{3/2}}{(2+bx)^{3/2}} dx$$

Optimal. Leaf size=63

$$-\frac{6 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{3\sqrt{x}\sqrt{bx+2}}{b^2} - \frac{2x^{3/2}}{b\sqrt{bx+2}}$$

[Out] $-6*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(5/2)}-2*x^{(3/2)}/b/(b*x+2)^{(1/2)}+3*x^{(1/2)}*(b*x+2)^{(1/2)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {47, 50, 54, 215}

$$\frac{3\sqrt{x}\sqrt{bx+2}}{b^2} - \frac{6 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{2x^{3/2}}{b\sqrt{bx+2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(3/2)}/(2 + b*x)^{(3/2)}, x]$

[Out] $(-2*x^{(3/2)})/(b*\operatorname{Sqrt}[2 + b*x]) + (3*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/b^2 - (6*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/ \operatorname{Sqrt}[2]])/b^{(5/2)}$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^{(m)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{NeQ}[m + n + 1, 0]$ && $!(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] \mid\mid (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m - n, 0])))$ && $!\operatorname{ILtQ}[m + n + 2, 0]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned} \int \frac{x^{3/2}}{(2+bx)^{3/2}} dx &= -\frac{2x^{3/2}}{b\sqrt{2+bx}} + \frac{3 \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx}{b} \\ &= -\frac{2x^{3/2}}{b\sqrt{2+bx}} + \frac{3\sqrt{x}\sqrt{2+bx}}{b^2} - \frac{3 \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx}{b^2} \\ &= -\frac{2x^{3/2}}{b\sqrt{2+bx}} + \frac{3\sqrt{x}\sqrt{2+bx}}{b^2} - \frac{6 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\ &= -\frac{2x^{3/2}}{b\sqrt{2+bx}} + \frac{3\sqrt{x}\sqrt{2+bx}}{b^2} - \frac{6 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.48

$$\frac{x^{5/2} {}_2F_1\left(\frac{3}{2}, \frac{5}{2}; \frac{7}{2}; -\frac{bx}{2}\right)}{5\sqrt{2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(3/2)/(2 + b*x)^(3/2), x]
```

```
[Out] (x^(5/2)*Hypergeometric2F1[3/2, 5/2, 7/2, -1/2*(b*x)])/(5*Sqrt[2])
```

fricas [A] time = 0.46, size = 134, normalized size = 2.13

$$\left[\frac{3(bx+2)\sqrt{b} \log\left(bx - \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1\right) + (b^2x+6b)\sqrt{bx+2}\sqrt{x}}{b^4x+2b^3}, \frac{6(bx+2)\sqrt{-b} \arctan\left(\frac{\sqrt{bx+2}\sqrt{-b}}{b\sqrt{x}}\right) + (b^2x+6b)\sqrt{-b}}{b^4x+2b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+2)^(3/2),x, algorithm="fricas")

[Out] [(3*(b*x + 2)*sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1) + (b^2*x + 6*b)*sqrt(b*x + 2)*sqrt(x))/(b^4*x + 2*b^3), (6*(b*x + 2)*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))) + (b^2*x + 6*b)*sqrt(b*x + 2)*sqrt(x))/(b^4*x + 2*b^3)]

giac [B] time = 10.16, size = 106, normalized size = 1.68

$$\frac{\left(\frac{3 \log\left(\sqrt{bx+2} \sqrt{b} - \sqrt{(bx+2)b-2b}\right)^2}{\sqrt{b}} + \frac{\sqrt{(bx+2)b-2b} \sqrt{bx+2}}{b} + \frac{16 \sqrt{b}}{(\sqrt{bx+2} \sqrt{b} - \sqrt{(bx+2)b-2b})^2 + 2b} \right) |b|}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+2)^(3/2),x, algorithm="giac")

[Out] (3*log((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2)/sqrt(b) + sqrt((b*x + 2)*b - 2*b)*sqrt(b*x + 2)/b + 16*sqrt(b)/((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2 + 2*b))*abs(b)/b^3

maple [B] time = 0.02, size = 100, normalized size = 1.59

$$\frac{\left(-\frac{3 \ln\left(\frac{bx+1}{\sqrt{b}} + \sqrt{bx^2+2x}\right)}{b^{\frac{5}{2}}} + \frac{4 \sqrt{\left(x+\frac{2}{b}\right)^2 b - 2x - \frac{4}{b}}}{\left(x+\frac{2}{b}\right) b^3} \right) \sqrt{(bx+2)x}}{\sqrt{bx+2} \sqrt{x}} + \frac{\sqrt{bx+2} \sqrt{x}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(b*x+2)^(3/2),x)

[Out] (b*x+2)^(1/2)/b^2*x^(1/2)+(-3/b^(5/2)*ln((b*x+1)/b^(1/2)+(b*x^2+2*x)^(1/2))+4/b^3/(x+2/b)*((x+2/b)^2*b-2*x-4/b)^(1/2))*((b*x+2)*x)^(1/2)/(b*x+2)^(1/2)/x^(1/2)

maxima [A] time = 2.99, size = 90, normalized size = 1.43

$$\frac{2 \left(2b - \frac{3(bx+2)}{x} \right)}{\frac{\sqrt{bx+2} b^3}{\sqrt{x}} - \frac{(bx+2)^{\frac{3}{2}} b^2}{x^{\frac{3}{2}}}} + \frac{3 \log \left(-\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}} \right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+2)^(3/2),x, algorithm="maxima")

[Out] $2*(2*b - 3*(b*x + 2)/x)/(\sqrt{b*x + 2})*b^3/\sqrt{x} - (b*x + 2)^{(3/2)}*b^2/x^{(3/2)} + 3*\log(-(\sqrt{b} - \sqrt{b*x + 2})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x + 2}/\sqrt{x}))/b^{(5/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^{3/2}}{(bx+2)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(b*x + 2)^(3/2),x)

[Out] int(x^(3/2)/(b*x + 2)^(3/2), x)

sympy [A] time = 3.06, size = 58, normalized size = 0.92

$$\frac{x^{\frac{3}{2}}}{b\sqrt{bx+2}} + \frac{6\sqrt{x}}{b^2\sqrt{bx+2}} - \frac{6 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)/(b*x+2)**(3/2),x)

[Out] $x^{(3/2)}/(b*\sqrt{b*x + 2}) + 6*\sqrt{x}/(b**2*\sqrt{b*x + 2}) - 6*\operatorname{asinh}(\sqrt{2}*\sqrt{b}*\sqrt{x}/2)/b^{(5/2)}$

$$3.618 \quad \int \frac{\sqrt{x}}{(2+bx)^{3/2}} dx$$

Optimal. Leaf size=44

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} - \frac{2\sqrt{x}}{b\sqrt{bx+2}}$$

[Out] $2*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(3/2)}-2*x^{(1/2)}/b/(b*x+2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 44, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 54, 215}

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} - \frac{2\sqrt{x}}{b\sqrt{bx+2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(2 + b*x)^(3/2), x]

[Out] $(-2*\operatorname{Sqrt}[x])/(b*\operatorname{Sqrt}[2 + b*x]) + (2*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]])/b^{(3/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 215

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[Rt[b, 2]*x]/Sqrt[a]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{x}}{(2+bx)^{3/2}} dx &= -\frac{2\sqrt{x}}{b\sqrt{2+bx}} + \frac{\int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx}{b} \\
&= -\frac{2\sqrt{x}}{b\sqrt{2+bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right)}{b} \\
&= -\frac{2\sqrt{x}}{b\sqrt{2+bx}} + \frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 44, normalized size = 1.00

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} - \frac{2\sqrt{x}}{b\sqrt{bx+2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(2 + b*x)^(3/2), x]

[Out] (-2*Sqrt[x])/(b*Sqrt[2 + b*x]) + (2*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(3/2)

fricas [A] time = 0.49, size = 117, normalized size = 2.66

$$\left[\frac{(bx+2)\sqrt{b} \log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1) - 2\sqrt{bx+2}b\sqrt{x}}{b^3x + 2b^2}, -\frac{2\left((bx+2)\sqrt{-b} \arctan\left(\frac{\sqrt{bx+2}\sqrt{-b}}{b\sqrt{x}}\right) + \sqrt{bx+2}\right)}{b^3x + 2b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+2)^(3/2), x, algorithm="fricas")

[Out] [((b*x + 2)*sqrt(b)*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1) - 2*sqrt(b*x + 2)*b*sqrt(x))/(b^3*x + 2*b^2), -2*((b*x + 2)*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))) + sqrt(b*x + 2)*b*sqrt(x))/(b^3*x + 2*b^2)]

giac [B] time = 10.61, size = 82, normalized size = 1.86

$$-\frac{\left(\frac{\log\left(\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^2\right)}{\sqrt{b}} + \frac{8\sqrt{b}}{\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^2+2b}\right)|b|}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+2)^(3/2),x, algorithm="giac")

[Out] $-\frac{(\log((\sqrt{b*x+2})*\sqrt{b}) - \sqrt{((b*x+2)*b - 2*b)})^2)/\sqrt{b} + 8*\sqrt{b}}{((\sqrt{b*x+2})*\sqrt{b} - \sqrt{((b*x+2)*b - 2*b)})^2 + 2*b)*\text{abs}(b)/b^2}$

maple [A] time = 0.11, size = 48, normalized size = 1.09

$$\frac{-\frac{\sqrt{\pi} \sqrt{2} \sqrt{b} \sqrt{x}}{\sqrt{\frac{bx}{2}+1}} + 2\sqrt{\pi} \operatorname{arcsinh}\left(\frac{\sqrt{2} \sqrt{b} \sqrt{x}}{2}\right)}{\sqrt{\pi} b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x+2)^(3/2),x)

[Out] $\frac{2/b^{3/2}/\pi^{1/2}*(-1/2*\pi^{1/2}*x^{1/2}*2^{1/2}*b^{1/2}/(1/2*b*x+1)^{1/2}) + \pi^{1/2}*\operatorname{arcsinh}(1/2*b^{1/2}*x^{1/2}*2^{1/2})}{b^2}$

maxima [A] time = 2.90, size = 57, normalized size = 1.30

$$-\frac{\log\left(-\frac{\sqrt{b}-\frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b}+\frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{b^{\frac{3}{2}}} - \frac{2\sqrt{x}}{\sqrt{bx+2}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+2)^(3/2),x, algorithm="maxima")

[Out] $-\frac{\log(-(\sqrt{b} - \sqrt{b*x+2})/\sqrt{x})/(\sqrt{b} + \sqrt{b*x+2})/\sqrt{x})}{b^{3/2} - 2*\sqrt{x}/(\sqrt{b*x+2}*b)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{x}}{(bx+2)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x+2)^(3/2),x)

[Out] int(x^(1/2)/(b*x+2)^(3/2), x)

sympy [A] time = 1.56, size = 41, normalized size = 0.93

$$-\frac{2\sqrt{x}}{b\sqrt{bx+2}} + \frac{2 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)/(b*x+2)**(3/2),x)`

[Out] `-2*sqrt(x)/(b*sqrt(b*x + 2)) + 2*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2)`

$$3.619 \quad \int \frac{1}{\sqrt{x}(2+bx)^{3/2}} dx$$

Optimal. Leaf size=15

$$\frac{\sqrt{x}}{\sqrt{bx+2}}$$

[Out] $x^{(1/2)}/(b*x+2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$\frac{\sqrt{x}}{\sqrt{bx+2}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(2 + b*x)^(3/2)),x]

[Out] Sqrt[x]/Sqrt[2 + b*x]

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt{x}(2+bx)^{3/2}} dx = \frac{\sqrt{x}}{\sqrt{2+bx}}$$

Mathematica [A] time = 0.00, size = 15, normalized size = 1.00

$$\frac{\sqrt{x}}{\sqrt{bx+2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(2 + b*x)^(3/2)),x]

[Out] Sqrt[x]/Sqrt[2 + b*x]

fricas [A] time = 0.43, size = 11, normalized size = 0.73

$$\frac{\sqrt{x}}{\sqrt{bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(3/2)/x^(1/2),x, algorithm="fricas")

[Out] sqrt(x)/sqrt(b*x + 2)

giac [B] time = 1.22, size = 44, normalized size = 2.93

$$\frac{4b^{\frac{3}{2}}}{\left(\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^2+2b\right)|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(3/2)/x^(1/2),x, algorithm="giac")

[Out] 4*b^(3/2)/(((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2 + 2*b)*abs(b))

maple [A] time = 0.00, size = 12, normalized size = 0.80

$$\frac{\sqrt{x}}{\sqrt{bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+2)^(3/2)/x^(1/2),x)

[Out] x^(1/2)/(b*x+2)^(1/2)

maxima [A] time = 1.34, size = 11, normalized size = 0.73

$$\frac{\sqrt{x}}{\sqrt{bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(3/2)/x^(1/2),x, algorithm="maxima")

[Out] sqrt(x)/sqrt(b*x + 2)

mupad [B] time = 0.31, size = 11, normalized size = 0.73

$$\frac{\sqrt{x}}{\sqrt{bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(b*x + 2)^(3/2)),x)`

[Out] `x^(1/2)/(b*x + 2)^(1/2)`

sympy [A] time = 0.86, size = 15, normalized size = 1.00

$$\frac{1}{\sqrt{b}\sqrt{1+\frac{2}{bx}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+2)**(3/2)/x**(1/2),x)`

[Out] `1/(sqrt(b)*sqrt(1 + 2/(b*x)))`

$$3.620 \quad \int \frac{1}{x^{3/2}(2+bx)^{3/2}} dx$$

Optimal. Leaf size=32

$$\frac{1}{\sqrt{x}\sqrt{bx+2}} - \frac{\sqrt{bx+2}}{\sqrt{x}}$$

[Out] $1/x^{(1/2)}/(b*x+2)^{(1/2)}-(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{1}{\sqrt{x}\sqrt{bx+2}} - \frac{\sqrt{bx+2}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(2 + b*x)^(3/2)),x]

[Out] 1/(Sqrt[x]*Sqrt[2 + b*x]) - Sqrt[2 + b*x]/Sqrt[x]

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{x^{3/2}(2+bx)^{3/2}} dx = \frac{1}{\sqrt{x}\sqrt{2+bx}} + \int \frac{1}{x^{3/2}\sqrt{2+bx}} dx$$

$$= \frac{1}{\sqrt{x}\sqrt{2+bx}} - \frac{\sqrt{2+bx}}{\sqrt{x}}$$

Mathematica [A] time = 0.01, size = 21, normalized size = 0.66

$$\frac{-bx - 1}{\sqrt{x}\sqrt{bx + 2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(2 + b*x)^(3/2)), x]

[Out] (-1 - b*x)/(Sqrt[x]*Sqrt[2 + b*x])

fricas [A] time = 0.44, size = 28, normalized size = 0.88

$$-\frac{\sqrt{bx + 2}(bx + 1)\sqrt{x}}{bx^2 + 2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+2)^(3/2), x, algorithm="fricas")

[Out] -sqrt(b*x + 2)*(b*x + 1)*sqrt(x)/(b*x^2 + 2*x)

giac [B] time = 1.12, size = 74, normalized size = 2.31

$$-\frac{\sqrt{bx + 2}b^2}{2\sqrt{(bx + 2)b - 2b}|b|} - \frac{2b^{\frac{5}{2}}}{\left(\left(\sqrt{bx + 2}\sqrt{b} - \sqrt{(bx + 2)b - 2b}\right)^2 + 2b\right)|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+2)^(3/2), x, algorithm="giac")

[Out] -1/2*sqrt(b*x + 2)*b^2/(sqrt((b*x + 2)*b - 2*b)*abs(b)) - 2*b^(5/2)/(((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2 + 2*b)*abs(b))

maple [A] time = 0.00, size = 18, normalized size = 0.56

$$-\frac{bx + 1}{\sqrt{bx + 2}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(3/2)/(b*x+2)^(3/2),x)`

[Out] `-(b*x+1)/(b*x+2)^(1/2)/x^(1/2)`

maxima [A] time = 1.34, size = 26, normalized size = 0.81

$$-\frac{b\sqrt{x}}{2\sqrt{bx+2}} - \frac{\sqrt{bx+2}}{2\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(b*x+2)^(3/2),x, algorithm="maxima")`

[Out] `-1/2*b*sqrt(x)/sqrt(b*x + 2) - 1/2*sqrt(b*x + 2)/sqrt(x)`

mupad [B] time = 0.35, size = 17, normalized size = 0.53

$$-\frac{bx+1}{\sqrt{x}\sqrt{bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(b*x + 2)^(3/2)),x)`

[Out] `-(b*x + 1)/(x^(1/2)*(b*x + 2)^(1/2))`

sympy [A] time = 1.54, size = 34, normalized size = 1.06

$$-\frac{\sqrt{b}}{\sqrt{1 + \frac{2}{bx}}} - \frac{1}{\sqrt{b}x\sqrt{1 + \frac{2}{bx}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(b*x+2)**(3/2),x)`

[Out] `-sqrt(b)/sqrt(1 + 2/(b*x)) - 1/(sqrt(b)*x*sqrt(1 + 2/(b*x)))`

$$3.621 \quad \int \frac{1}{x^{5/2}(2+bx)^{3/2}} dx$$

Optimal. Leaf size=53

$$-\frac{2\sqrt{bx+2}}{3x^{3/2}} + \frac{1}{x^{3/2}\sqrt{bx+2}} + \frac{2b\sqrt{bx+2}}{3\sqrt{x}}$$

[Out] $1/x^{(3/2)}/(b*x+2)^{(1/2)}-2/3*(b*x+2)^{(1/2)}/x^{(3/2)}+2/3*b*(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{2\sqrt{bx+2}}{3x^{3/2}} + \frac{1}{x^{3/2}\sqrt{bx+2}} + \frac{2b\sqrt{bx+2}}{3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(2 + b*x)^(3/2)),x]

[Out] $1/(x^{(3/2)}*\text{Sqrt}[2 + b*x]) - (2*\text{Sqrt}[2 + b*x])/(3*x^{(3/2)}) + (2*b*\text{Sqrt}[2 + b*x])/(3*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{5/2}(2+bx)^{3/2}} dx &= \frac{1}{x^{3/2}\sqrt{2+bx}} + 2 \int \frac{1}{x^{5/2}\sqrt{2+bx}} dx \\
&= \frac{1}{x^{3/2}\sqrt{2+bx}} - \frac{2\sqrt{2+bx}}{3x^{3/2}} - \frac{1}{3}(2b) \int \frac{1}{x^{3/2}\sqrt{2+bx}} dx \\
&= \frac{1}{x^{3/2}\sqrt{2+bx}} - \frac{2\sqrt{2+bx}}{3x^{3/2}} + \frac{2b\sqrt{2+bx}}{3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 0.60

$$\frac{2b^2x^2 + 2bx - 1}{3x^{3/2}\sqrt{bx + 2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(2 + b*x)^(3/2)),x]

[Out] (-1 + 2*b*x + 2*b^2*x^2)/(3*x^(3/2)*Sqrt[2 + b*x])

fricas [A] time = 0.43, size = 39, normalized size = 0.74

$$\frac{(2b^2x^2 + 2bx - 1)\sqrt{bx + 2}\sqrt{x}}{3(bx^3 + 2x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+2)^(3/2),x, algorithm="fricas")

[Out] 1/3*(2*b^2*x^2 + 2*b*x - 1)*sqrt(b*x + 2)*sqrt(x)/(b*x^3 + 2*x^2)

giac [B] time = 1.23, size = 86, normalized size = 1.62

$$\frac{b^{7/2}}{\left(\left(\sqrt{bx+2}\sqrt{b} - \sqrt{(bx+2)b-2b}\right)^2 + 2b\right)|b|} + \frac{(5(bx+2)b^2|b| - 12b^2|b|)\sqrt{bx+2}}{12((bx+2)b - 2b)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+2)^(3/2),x, algorithm="giac")

[Out] b^(7/2)/(((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2 + 2*b)*abs(b) + 1/12*(5*(b*x + 2)*b^2*abs(b) - 12*b^2*abs(b))*sqrt(b*x + 2)/((b*x + 2)*b - 2*b)^(3/2)

maple [A] time = 0.00, size = 27, normalized size = 0.51

$$\frac{2b^2x^2 + 2bx - 1}{3\sqrt{bx+2}x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/2)/(b*x+2)^(3/2),x)`

[Out] `1/3*(2*b^2*x^2+2*b*x-1)/(b*x+2)^(1/2)/x^(3/2)`

maxima [A] time = 1.37, size = 41, normalized size = 0.77

$$\frac{b^2\sqrt{x}}{4\sqrt{bx+2}} + \frac{\sqrt{bx+2}b}{2\sqrt{x}} - \frac{(bx+2)^{\frac{3}{2}}}{12x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2)/(b*x+2)^(3/2),x, algorithm="maxima")`

[Out] `1/4*b^2*sqrt(x)/sqrt(b*x + 2) + 1/2*sqrt(b*x + 2)*b/sqrt(x) - 1/12*(b*x + 2)^(3/2)/x^(3/2)`

mupad [B] time = 0.38, size = 37, normalized size = 0.70

$$\frac{\sqrt{bx+2} \left(\frac{2x}{3} + \frac{2bx^2}{3} - \frac{1}{3b} \right)}{x^{5/2} + \frac{2x^{3/2}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/2)*(b*x + 2)^(3/2)),x)`

[Out] `((b*x + 2)^(1/2)*((2*x)/3 + (2*b*x^2)/3 - 1/(3*b)))/(x^(5/2) + (2*x^(3/2))/b)`

sympy [B] time = 3.86, size = 170, normalized size = 3.21

$$\frac{2b^{\frac{15}{2}}x^3\sqrt{1+\frac{2}{bx}}}{3b^6x^3+12b^5x^2+12b^4x} + \frac{6b^{\frac{13}{2}}x^2\sqrt{1+\frac{2}{bx}}}{3b^6x^3+12b^5x^2+12b^4x} + \frac{3b^{\frac{11}{2}}x\sqrt{1+\frac{2}{bx}}}{3b^6x^3+12b^5x^2+12b^4x} - \frac{2b^{\frac{9}{2}}\sqrt{1+\frac{2}{bx}}}{3b^6x^3+12b^5x^2+12b^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(b*x+2)**(3/2),x)`

```
[Out] 2*b**(15/2)*x**3*sqrt(1 + 2/(b*x))/(3*b**6*x**3 + 12*b**5*x**2 + 12*b**4*x)
+ 6*b**(13/2)*x**2*sqrt(1 + 2/(b*x))/(3*b**6*x**3 + 12*b**5*x**2 + 12*b**4
*x) + 3*b**(11/2)*x*sqrt(1 + 2/(b*x))/(3*b**6*x**3 + 12*b**5*x**2 + 12*b**4
*x) - 2*b**(9/2)*sqrt(1 + 2/(b*x))/(3*b**6*x**3 + 12*b**5*x**2 + 12*b**4*x)
```

$$3.622 \quad \int \frac{1}{x^{7/2}(2+bx)^{3/2}} dx$$

Optimal. Leaf size=74

$$-\frac{2b^2\sqrt{bx+2}}{5\sqrt{x}} + \frac{2b\sqrt{bx+2}}{5x^{3/2}} - \frac{3\sqrt{bx+2}}{5x^{5/2}} + \frac{1}{x^{5/2}\sqrt{bx+2}}$$

[Out] $1/x^{(5/2)}/(b*x+2)^{(1/2)}-3/5*(b*x+2)^{(1/2)}/x^{(5/2)}+2/5*b*(b*x+2)^{(1/2)}/x^{(3/2)}-2/5*b^2*(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{2b^2\sqrt{bx+2}}{5\sqrt{x}} + \frac{2b\sqrt{bx+2}}{5x^{3/2}} - \frac{3\sqrt{bx+2}}{5x^{5/2}} + \frac{1}{x^{5/2}\sqrt{bx+2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(7/2)*(2 + b*x)^(3/2)), x]

[Out] $1/(x^{(5/2)}*\text{Sqrt}[2 + b*x]) - (3*\text{Sqrt}[2 + b*x])/(5*x^{(5/2)}) + (2*b*\text{Sqrt}[2 + b*x])/(5*x^{(3/2)}) - (2*b^2*\text{Sqrt}[2 + b*x])/(5*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{7/2}(2+bx)^{3/2}} dx &= \frac{1}{x^{5/2}\sqrt{2+bx}} + 3 \int \frac{1}{x^{7/2}\sqrt{2+bx}} dx \\
&= \frac{1}{x^{5/2}\sqrt{2+bx}} - \frac{3\sqrt{2+bx}}{5x^{5/2}} - \frac{1}{5}(6b) \int \frac{1}{x^{5/2}\sqrt{2+bx}} dx \\
&= \frac{1}{x^{5/2}\sqrt{2+bx}} - \frac{3\sqrt{2+bx}}{5x^{5/2}} + \frac{2b\sqrt{2+bx}}{5x^{3/2}} + \frac{1}{5}(2b^2) \int \frac{1}{x^{3/2}\sqrt{2+bx}} dx \\
&= \frac{1}{x^{5/2}\sqrt{2+bx}} - \frac{3\sqrt{2+bx}}{5x^{5/2}} + \frac{2b\sqrt{2+bx}}{5x^{3/2}} - \frac{2b^2\sqrt{2+bx}}{5\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.53

$$\frac{-2b^3x^3 - 2b^2x^2 + bx - 1}{5x^{5/2}\sqrt{bx + 2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(7/2)*(2 + b*x)^(3/2)),x]

[Out] (-1 + b*x - 2*b^2*x^2 - 2*b^3*x^3)/(5*x^(5/2)*Sqrt[2 + b*x])

fricas [A] time = 0.45, size = 47, normalized size = 0.64

$$\frac{(2b^3x^3 + 2b^2x^2 - bx + 1)\sqrt{bx + 2}\sqrt{x}}{5(bx^4 + 2x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+2)^(3/2),x, algorithm="fricas")

[Out] -1/5*(2*b^3*x^3 + 2*b^2*x^2 - b*x + 1)*sqrt(b*x + 2)*sqrt(x)/(b*x^4 + 2*x^3)

giac [B] time = 1.11, size = 107, normalized size = 1.45

$$\frac{\frac{9}{b^2}}{2\left(\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^2+2b\right)|b|} - \frac{\left(\frac{60b^6}{|b|} + \left(\frac{11(bx+2)b^6}{|b|} - \frac{50b^6}{|b|}\right)(bx+2)\right)\sqrt{bx+2}}{40((bx+2)b-2b)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+2)^(3/2),x, algorithm="giac")

[Out] $-1/2*b^{(9/2)/((\sqrt{b*x+2}*\sqrt{b}-\sqrt{(b*x+2)*b-2*b})^2+2*b)*a$
 $bs(b))-1/40*(60*b^6/abs(b)+(11*(b*x+2)*b^6/abs(b)-50*b^6/abs(b))*(b$
 $*x+2))*\sqrt{b*x+2}/((b*x+2)*b-2*b)^{(5/2)}$

maple [A] time = 0.00, size = 35, normalized size = 0.47

$$-\frac{2b^3x^3+2b^2x^2-bx+1}{5\sqrt{bx+2}x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(7/2)/(b*x+2)^(3/2),x)

[Out] $-1/5*(2*b^3*x^3+2*b^2*x^2-b*x+1)/(b*x+2)^{(1/2)}/x^{(5/2)}$

maxima [A] time = 1.30, size = 56, normalized size = 0.76

$$-\frac{b^3\sqrt{x}}{8\sqrt{bx+2}}-\frac{3\sqrt{bx+2}b^2}{8\sqrt{x}}+\frac{(bx+2)^{\frac{3}{2}}b}{8x^{\frac{3}{2}}}-\frac{(bx+2)^{\frac{5}{2}}}{40x^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(7/2)/(b*x+2)^(3/2),x, algorithm="maxima")

[Out] $-1/8*b^3*\sqrt{x}/\sqrt{b*x+2}-3/8*\sqrt{b*x+2}*b^2/\sqrt{x}+1/8*(b*x+2)^{(3/2)}*b/x^{(3/2)}-1/40*(b*x+2)^{(5/2)}/x^{(5/2)}$

mupad [B] time = 0.43, size = 46, normalized size = 0.62

$$-\frac{\sqrt{bx+2}\left(\frac{2bx^2}{5}-\frac{x}{5}+\frac{1}{5b}+\frac{2b^2x^3}{5}\right)}{x^{7/2}+\frac{2x^{5/2}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(7/2)*(b*x+2)^(3/2)),x)

[Out] $-((b*x+2)^{(1/2)}*((2*b*x^2)/5-x/5+1/(5*b)+(2*b^2*x^3)/5))/(x^{(7/2)}+(2*x^{(5/2)})/b)$

sympy [B] time = 10.97, size = 269, normalized size = 3.64

$$\frac{2b^{\frac{29}{2}}x^5\sqrt{1+\frac{2}{bx}}}{5b^{12}x^5+30b^{11}x^4+60b^{10}x^3+40b^9x^2}-\frac{10b^{\frac{27}{2}}x^4\sqrt{1+\frac{2}{bx}}}{5b^{12}x^5+30b^{11}x^4+60b^{10}x^3+40b^9x^2}-\frac{15b^{\frac{25}{2}}x^3\sqrt{1+\frac{2}{bx}}}{5b^{12}x^5+30b^{11}x^4+60b^{10}x^3+40b^9x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(7/2)/(b*x+2)**(3/2),x)`

[Out]
$$\begin{aligned} & -2*b**(29/2)*x**5*\sqrt{1 + 2/(b*x)}/(5*b**12*x**5 + 30*b**11*x**4 + 60*b**10*x**3 + 40*b**9*x**2) - 10*b**(27/2)*x**4*\sqrt{1 + 2/(b*x)}/(5*b**12*x**5 + 30*b**11*x**4 + 60*b**10*x**3 + 40*b**9*x**2) - 15*b**(25/2)*x**3*\sqrt{1 + 2/(b*x)}/(5*b**12*x**5 + 30*b**11*x**4 + 60*b**10*x**3 + 40*b**9*x**2) - 5*b**(23/2)*x**2*\sqrt{1 + 2/(b*x)}/(5*b**12*x**5 + 30*b**11*x**4 + 60*b**10*x**3 + 40*b**9*x**2) - 4*b**(19/2)*\sqrt{1 + 2/(b*x)}/(5*b**12*x**5 + 30*b**11*x**4 + 60*b**10*x**3 + 40*b**9*x**2) \end{aligned}$$

$$3.623 \quad \int \frac{x^{5/2}}{(2+bx)^{5/2}} dx$$

Optimal. Leaf size=86

$$-\frac{10 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} + \frac{5\sqrt{x}\sqrt{bx+2}}{b^3} - \frac{10x^{3/2}}{3b^2\sqrt{bx+2}} - \frac{2x^{5/2}}{3b(bx+2)^{3/2}}$$

[Out] $-2/3*x^{(5/2)}/b/(b*x+2)^{(3/2)}-10*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(7/2)}$
 $-10/3*x^{(3/2)}/b^2/(b*x+2)^{(1/2)}+5*x^{(1/2)}*(b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.02, antiderivative size = 86, normalized size of antiderivative = 1.00,
 number of steps used = 5, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} =$
 0.267, Rules used = {47, 50, 54, 215}

$$-\frac{10x^{3/2}}{3b^2\sqrt{bx+2}} + \frac{5\sqrt{x}\sqrt{bx+2}}{b^3} - \frac{10 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} - \frac{2x^{5/2}}{3b(bx+2)^{3/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^{(5/2)}/(2 + b*x)^{(5/2)}, x]$

[Out] $(-2*x^{(5/2)})/(3*b*(2 + b*x)^{(3/2)}) - (10*x^{(3/2)})/(3*b^2*\operatorname{Sqrt}[2 + b*x]) + ($
 $5*\operatorname{Sqrt}[x]*\operatorname{Sqrt}[2 + b*x])/b^3 - (10*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/(\operatorname{Sqrt}[2])])/b^{(7$
 $/2)$

Rule 47

$\operatorname{Int}[(a + b*x)^m * (c + d*x)^n, x] := \operatorname{Simp}[(a + b*x)^{m+1} * (c + d*x)^n / (b*(m+1)), x] - \operatorname{Dist}[(d*n) / (b*(m+1)), \operatorname{Int}[(a + b*x)^{m+1} * (c + d*x)^{n-1}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\operatorname{Int}[(a + b*x)^m * (c + d*x)^n, x] := \operatorname{Simp}[(a + b*x)^{m+1} * (c + d*x)^n / (b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d)) / (b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m * (c + d*x)^{n-1}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqr
t[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(2+bx)^{5/2}} dx &= -\frac{2x^{5/2}}{3b(2+bx)^{3/2}} + \frac{5 \int \frac{x^{3/2}}{(2+bx)^{3/2}} dx}{3b} \\
&= -\frac{2x^{5/2}}{3b(2+bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{2+bx}} + \frac{5 \int \frac{\sqrt{x}}{\sqrt{2+bx}} dx}{b^2} \\
&= -\frac{2x^{5/2}}{3b(2+bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{2+bx}} + \frac{5\sqrt{x}\sqrt{2+bx}}{b^3} - \frac{5 \int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx}{b^3} \\
&= -\frac{2x^{5/2}}{3b(2+bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{2+bx}} + \frac{5\sqrt{x}\sqrt{2+bx}}{b^3} - \frac{10 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right)}{b^3} \\
&= -\frac{2x^{5/2}}{3b(2+bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{2+bx}} + \frac{5\sqrt{x}\sqrt{2+bx}}{b^3} - \frac{10 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.35

$$\frac{x^{7/2} {}_2F_1\left(\frac{5}{2}, \frac{7}{2}; \frac{9}{2}; -\frac{bx}{2}\right)}{14\sqrt{2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(5/2)/(2 + b*x)^(5/2), x]
```

```
[Out] (x^(7/2)*Hypergeometric2F1[5/2, 7/2, 9/2, -1/2*(b*x)])/(14*Sqrt[2])
```


fricas [A] time = 0.45, size = 186, normalized size = 2.16

$$\left[\frac{15(b^2x^2 + 4bx + 4)\sqrt{b} \log(bx - \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1) + (3b^3x^2 + 40b^2x + 60b)\sqrt{bx+2}\sqrt{x}}{3(b^6x^2 + 4b^5x + 4b^4)}, \frac{30(b^2x^2 + 4bx + 4)\sqrt{b} \log(bx - \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1) + (3b^3x^2 + 40b^2x + 60b)\sqrt{bx+2}\sqrt{x}}{3(b^6x^2 + 4b^5x + 4b^4)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+2)^(5/2),x, algorithm="fricas")

[Out] [1/3*(15*(b^2*x^2 + 4*b*x + 4)*sqrt(b)*log(b*x - sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1) + (3*b^3*x^2 + 40*b^2*x + 60*b)*sqrt(b*x + 2)*sqrt(x))/(b^6*x^2 + 4*b^5*x + 4*b^4), 1/3*(30*(b^2*x^2 + 4*b*x + 4)*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))) + (3*b^3*x^2 + 40*b^2*x + 60*b)*sqrt(b*x + 2)*sqrt(x))/(b^6*x^2 + 4*b^5*x + 4*b^4)]

giac [B] time = 10.82, size = 182, normalized size = 2.12

$$\left(\frac{15 \log\left(\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^2\right)}{b^{\frac{5}{2}}} + \frac{3\sqrt{(bx+2)b-2b}\sqrt{bx+2}}{b^3} + \frac{16\left(9\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^4\sqrt{b}+24\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^2b\right)}{\left(\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^2+2b\right)^3b^2} \right) \frac{1}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(b*x+2)^(5/2),x, algorithm="giac")

[Out] 1/3*(15*log((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2)/b^(5/2) + 3*sqrt((b*x + 2)*b - 2*b)*sqrt(b*x + 2)/b^3 + 16*(9*(sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^4*sqrt(b) + 24*(sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2*b^(3/2) + 28*b^(5/2))/(((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2 + 2*b)^3*b^2)*abs(b)/b^2

maple [B] time = 0.04, size = 136, normalized size = 1.58

$$\left(-\frac{5\ln\left(\frac{bx+1}{\sqrt{b}}+\sqrt{bx^2+2x}\right)}{b^{\frac{7}{2}}} + \frac{28\sqrt{\left(x+\frac{2}{b}\right)^2b-2x-\frac{4}{b}}}{3\left(x+\frac{2}{b}\right)b^4} - \frac{8\sqrt{\left(x+\frac{2}{b}\right)^2b-2x-\frac{4}{b}}}{3\left(x+\frac{2}{b}\right)b^5} \right) \frac{\sqrt{(bx+2)x}}{\sqrt{bx+2}\sqrt{x}} + \frac{\sqrt{bx+2}\sqrt{x}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(b*x+2)^(5/2),x)

[Out] $(b*x+2)^{(1/2)}/b^3*x^{(1/2)}+(-5/b^{(7/2)}*\ln((b*x+1)/b^{(1/2)}+(b*x^2+2*x)^{(1/2)})+28/3/(x+2/b)*((x+2/b)^2*b-2*x-4/b)^{(1/2)}/b^4-8/3/b^5/(x+2/b)^2*((x+2/b)^2*b-2*x-4/b)^{(1/2)})*((b*x+2)*x)^{(1/2)}/(b*x+2)^{(1/2)}/x^{(1/2)}$

maxima [A] time = 3.00, size = 105, normalized size = 1.22

$$\frac{2\left(2b^2 + \frac{10(bx+2)b}{x} - \frac{15(bx+2)^2}{x^2}\right)}{3\left(\frac{(bx+2)^2 b^4}{x^2} - \frac{(bx+2)^2 b^3}{x^2}\right)} + \frac{5 \log\left(-\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/2)/(b*x+2)^(5/2),x, algorithm="maxima")`

[Out] $2/3*(2*b^2 + 10*(b*x + 2)*b/x - 15*(b*x + 2)^2/x^2)/((b*x + 2)^{(3/2)}*b^4/x^{(3/2)} - (b*x + 2)^{(5/2)}*b^3/x^{(5/2)}) + 5*\log(-(\text{sqrt}(b) - \text{sqrt}(b*x + 2)/\text{sqrt}(x)))/(\text{sqrt}(b) + \text{sqrt}(b*x + 2)/\text{sqrt}(x)))/b^{(7/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{(bx+2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/2)/(b*x + 2)^(5/2),x)`

[Out] `int(x^(5/2)/(b*x + 2)^(5/2), x)`

sympy [B] time = 6.62, size = 308, normalized size = 3.58

$$\frac{3b^{\frac{23}{2}}x^{15}}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{bx+2} + 6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{bx+2}} + \frac{40b^{\frac{21}{2}}x^{14}}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{bx+2} + 6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{bx+2}} + \frac{60b^{\frac{19}{2}}x^{13}}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{bx+2} + 6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/2)/(b*x+2)**(5/2),x)`

[Out] $3*b^{(23/2)}*x^{15}/(3*b^{(27/2)}*x^{(27/2)}*\text{sqrt}(b*x + 2) + 6*b^{(25/2)}*x^{(25/2)}*\text{sqrt}(b*x + 2)) + 40*b^{(21/2)}*x^{14}/(3*b^{(27/2)}*x^{(27/2)}*\text{sqrt}(b*x + 2) + 6*b^{(25/2)}*x^{(25/2)}*\text{sqrt}(b*x + 2)) + 60*b^{(19/2)}*x^{13}/(3*b^{(27/2)}*x^{(27/2)}*\text{sqrt}(b*x + 2) + 6*b^{(25/2)}*x^{(25/2)}*\text{sqrt}(b*x + 2)) - 30*b^{10}*x^{(27/2)}*\text{sqrt}(b*x + 2)*\text{asinh}(\text{sqrt}(2)*\text{sqrt}(b)*\text{sqrt}(x)/2)/(3*b^{(27/2)}*x^{(27/2)}*\text{sqrt}(b*x + 2))$

$$\begin{aligned} & /2) * \sqrt{b*x + 2} + 6*b**(25/2)*x**(25/2)*\sqrt{b*x + 2}) - 60*b**9*x**(25/2) \\ &) * \sqrt{b*x + 2} * \operatorname{asinh}(\sqrt{2}*\sqrt{b}*\sqrt{x})/2) / (3*b**(27/2)*x**(27/2)*\sqrt{b*x + 2} + 6*b**(25/2)*x**(25/2)*\sqrt{b*x + 2}) \end{aligned}$$

$$3.624 \quad \int \frac{x^{3/2}}{(2+bx)^{5/2}} dx$$

Optimal. Leaf size=65

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{2\sqrt{x}}{b^2\sqrt{bx+2}} - \frac{2x^{3/2}}{3b(bx+2)^{3/2}}$$

[Out] $-2/3*x^{(3/2)}/b/(b*x+2)^{(3/2)}+2*\operatorname{arcsinh}(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(5/2)}$
 $-2*x^{(1/2)}/b^2/(b*x+2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 54, 215}

$$-\frac{2\sqrt{x}}{b^2\sqrt{bx+2}} + \frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{2x^{3/2}}{3b(bx+2)^{3/2}}$$

Antiderivative was successfully verified.

[In] `Int[x^(3/2)/(2 + b*x)^(5/2), x]`

[Out] $(-2*x^{(3/2)})/(3*b*(2 + b*x)^{(3/2)}) - (2*\operatorname{Sqrt}[x])/(b^2*\operatorname{Sqrt}[2 + b*x]) + (2*\operatorname{ArcSinh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[x])/\operatorname{Sqrt}[2]])/b^{(5/2)}$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[
(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[
2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /;
FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 215

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /;
FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{3/2}}{(2+bx)^{5/2}} dx &= -\frac{2x^{3/2}}{3b(2+bx)^{3/2}} + \frac{\int \frac{\sqrt{x}}{(2+bx)^{3/2}} dx}{b} \\
&= -\frac{2x^{3/2}}{3b(2+bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{2+bx}} + \frac{\int \frac{1}{\sqrt{x}\sqrt{2+bx}} dx}{b^2} \\
&= -\frac{2x^{3/2}}{3b(2+bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{2+bx}} + \frac{2 \text{Subst}\left(\int \frac{1}{\sqrt{2+bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\
&= -\frac{2x^{3/2}}{3b(2+bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{2+bx}} + \frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.07, size = 52, normalized size = 0.80

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{4\sqrt{x}(2bx+3)}{3b^2(bx+2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/(2 + b*x)^(5/2), x]

[Out] (-4*Sqrt[x]*(3 + 2*b*x))/(3*b^2*(2 + b*x)^(3/2)) + (2*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(5/2)

fricas [A] time = 0.43, size = 171, normalized size = 2.63

$$\left[\frac{3(b^2x^2 + 4bx + 4)\sqrt{b} \log(bx + \sqrt{bx+2}\sqrt{b}\sqrt{x} + 1) - 4(2b^2x + 3b)\sqrt{bx+2}\sqrt{x}}{3(b^5x^2 + 4b^4x + 4b^3)}, -\frac{2(3(b^2x^2 + 4bx + 4)\sqrt{b}}{3(b^5x^2 + 4b^4x + 4b^3)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+2)^(5/2), x, algorithm="fricas")

[Out] [1/3*(3*(b^2*x^2 + 4*b*x + 4)*sqrt(b)*log(b*x + sqrt(b*x + 2)*sqrt(b)*sqrt(x) + 1) - 4*(2*b^2*x + 3*b)*sqrt(b*x + 2)*sqrt(x))/(b^5*x^2 + 4*b^4*x + 4*b^3), -2/3*(3*(b^2*x^2 + 4*b*x + 4)*sqrt(-b)*arctan(sqrt(b*x + 2)*sqrt(-b)/(b*sqrt(x))) + 2*(2*b^2*x + 3*b)*sqrt(b*x + 2)*sqrt(x))/(b^5*x^2 + 4*b^4*x + 4*b^3)]

giac [B] time = 10.77, size = 154, normalized size = 2.37

$$\frac{\left(\frac{3 \log\left(\left(\sqrt{bx+2} \sqrt{b} - \sqrt{(bx+2)b-2b}\right)^2\right)}{\sqrt{b}} + \frac{16 \left(3 \left(\sqrt{bx+2} \sqrt{b} - \sqrt{(bx+2)b-2b}\right)^4 \sqrt{b} + 6 \left(\sqrt{bx+2} \sqrt{b} - \sqrt{(bx+2)b-2b}\right)^2 b^{\frac{3}{2}} + 8 b^{\frac{5}{2}}\right)}{\left(\left(\sqrt{bx+2} \sqrt{b} - \sqrt{(bx+2)b-2b}\right)^2 + 2b\right)^3} \right) |b|}{3 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+2)^(5/2),x, algorithm="giac")

[Out] $-1/3*(3*\log((\text{sqrt}(b*x + 2)*\text{sqrt}(b) - \text{sqrt}((b*x + 2)*b - 2*b))^2)/\text{sqrt}(b) + 16*(3*(\text{sqrt}(b*x + 2)*\text{sqrt}(b) - \text{sqrt}((b*x + 2)*b - 2*b))^4*\text{sqrt}(b) + 6*(\text{sqrt}(b*x + 2)*\text{sqrt}(b) - \text{sqrt}((b*x + 2)*b - 2*b))^2*b^{(3/2)} + 8*b^{(5/2)})/((\text{sqrt}(b*x + 2)*\text{sqrt}(b) - \text{sqrt}((b*x + 2)*b - 2*b))^2 + 2*b)^3)*\text{abs}(b)/b^3$

maple [A] time = 0.04, size = 55, normalized size = 0.85

$$\frac{-\frac{\sqrt{\pi} \sqrt{2} (10bx+15)\sqrt{b} \sqrt{x}}{15\left(\frac{bx}{2}+1\right)^2} + 2\sqrt{\pi} \operatorname{arcsinh}\left(\frac{\sqrt{2} \sqrt{b} \sqrt{x}}{2}\right)}{\sqrt{\pi} b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(b*x+2)^(5/2),x)

[Out] $4/3/b^{(5/2)}/\text{Pi}^{(1/2)}*(-1/20*\text{Pi}^{(1/2)}*x^{(1/2)}*2^{(1/2)}*b^{(1/2)}*(10*b*x+15)/(1/2*b*x+1)^{(3/2)}+3/2*\text{Pi}^{(1/2)}*\operatorname{arcsinh}(1/2*2^{(1/2)}*b^{(1/2)}*x^{(1/2)})$

maxima [A] time = 2.97, size = 69, normalized size = 1.06

$$\frac{2 \left(b + \frac{3(bx+2)}{x}\right) x^{\frac{3}{2}}}{3(bx+2)^2 b^2} - \frac{\log\left(\frac{\sqrt{b} - \frac{\sqrt{bx+2}}{\sqrt{x}}}{\sqrt{b} + \frac{\sqrt{bx+2}}{\sqrt{x}}}\right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(b*x+2)^(5/2),x, algorithm="maxima")

[Out] $-2/3*(b + 3*(b*x + 2)/x)*x^{(3/2)}/((b*x + 2)^{(3/2)}*b^2) - \log(-(\text{sqrt}(b) - \text{sqrt}(b*x + 2)/\text{sqrt}(x))/(\text{sqrt}(b) + \text{sqrt}(b*x + 2)/\text{sqrt}(x)))/b^{(5/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^{3/2}}{(bx+2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(b*x + 2)^(5/2), x)`

[Out] `int(x^(3/2)/(b*x + 2)^(5/2), x)`

sympy [B] time = 3.58, size = 257, normalized size = 3.95

$$-\frac{8b^{\frac{11}{2}}x^8}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{bx+2} + 6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{bx+2}} - \frac{12b^{\frac{9}{2}}x^7}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{bx+2} + 6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{bx+2}} + \frac{6b^5x^{\frac{15}{2}}\sqrt{bx+2} \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{bx+2} + 6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(b*x+2)**(5/2), x)`

[Out] `-8*b**(11/2)*x**8/(3*b**(15/2)*x**(15/2)*sqrt(b*x + 2) + 6*b**(13/2)*x**(13/2)*sqrt(b*x + 2)) - 12*b**(9/2)*x**7/(3*b**(15/2)*x**(15/2)*sqrt(b*x + 2) + 6*b**(13/2)*x**(13/2)*sqrt(b*x + 2)) + 6*b**5*x**(15/2)*sqrt(b*x + 2)*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(3*b**(15/2)*x**(15/2)*sqrt(b*x + 2) + 6*b**(13/2)*x**(13/2)*sqrt(b*x + 2)) + 12*b**4*x**(13/2)*sqrt(b*x + 2)*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(3*b**(15/2)*x**(15/2)*sqrt(b*x + 2) + 6*b**(13/2)*x**(13/2)*sqrt(b*x + 2))`

$$3.625 \quad \int \frac{\sqrt{x}}{(2+bx)^{5/2}} dx$$

Optimal. Leaf size=18

$$\frac{x^{3/2}}{3(bx+2)^{3/2}}$$

[Out] 1/3*x^(3/2)/(b*x+2)^(3/2)

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$\frac{x^{3/2}}{3(bx+2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(2 + b*x)^(5/2), x]

[Out] x^(3/2)/(3*(2 + b*x)^(3/2))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{x}}{(2+bx)^{5/2}} dx = \frac{x^{3/2}}{3(2+bx)^{3/2}}$$

Mathematica [A] time = 0.00, size = 18, normalized size = 1.00

$$\frac{x^{3/2}}{3(bx+2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(2 + b*x)^(5/2), x]

[Out] x^(3/2)/(3*(2 + b*x)^(3/2))

fricas [B] time = 0.41, size = 27, normalized size = 1.50

$$\frac{\sqrt{bx+2}x^{\frac{3}{2}}}{3(b^2x^2+4bx+4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+2)^(5/2),x, algorithm="fricas")

[Out] 1/3*sqrt(b*x + 2)*x^(3/2)/(b^2*x^2 + 4*b*x + 4)

giac [B] time = 1.22, size = 82, normalized size = 4.56

$$\frac{4\left(3\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^4\sqrt{b}+4b^{\frac{5}{2}}\right)|b|}{3\left(\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^2+2b\right)^3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+2)^(5/2),x, algorithm="giac")

[Out] 4/3*(3*(sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^4*sqrt(b) + 4*b^(5/2))*abs(b)/(((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2 + 2*b)^3*b^2)

maple [A] time = 0.00, size = 13, normalized size = 0.72

$$\frac{x^{\frac{3}{2}}}{3(bx+2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(b*x+2)^(5/2),x)

[Out] 1/3*x^(3/2)/(b*x+2)^(3/2)

maxima [A] time = 1.33, size = 12, normalized size = 0.67

$$\frac{x^{\frac{3}{2}}}{3(bx+2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(b*x+2)^(5/2),x, algorithm="maxima")

[Out] $\frac{1}{3}x^{3/2}/(bx + 2)^{3/2}$

mupad [B] time = 0.25, size = 12, normalized size = 0.67

$$\frac{x^{3/2}}{3(bx + 2)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)/(b*x + 2)^(5/2), x)`

[Out] $x^{3/2}/(3*(bx + 2)^{3/2})$

sympy [A] time = 1.40, size = 27, normalized size = 1.50

$$\frac{x^{\frac{3}{2}}}{3bx\sqrt{bx + 2} + 6\sqrt{bx + 2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)/(b*x+2)**(5/2), x)`

[Out] $x^{3/2}/(3*b*x*\sqrt{bx + 2} + 6*\sqrt{bx + 2})$

$$3.626 \quad \int \frac{1}{\sqrt{x}(2+bx)^{5/2}} dx$$

Optimal. Leaf size=37

$$\frac{\sqrt{x}}{3\sqrt{bx+2}} + \frac{\sqrt{x}}{3(bx+2)^{3/2}}$$

[Out] $1/3*x^{(1/2)/(b*x+2)^{(3/2)}+1/3*x^{(1/2)/(b*x+2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{\sqrt{x}}{3\sqrt{bx+2}} + \frac{\sqrt{x}}{3(bx+2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(2 + b*x)^(5/2)),x]

[Out] Sqrt[x]/(3*(2 + b*x)^(3/2)) + Sqrt[x]/(3*Sqrt[2 + b*x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{\sqrt{x}(2+bx)^{5/2}} dx = \frac{\sqrt{x}}{3(2+bx)^{3/2}} + \frac{1}{3} \int \frac{1}{\sqrt{x}(2+bx)^{3/2}} dx$$

$$= \frac{\sqrt{x}}{3(2+bx)^{3/2}} + \frac{\sqrt{x}}{3\sqrt{2+bx}}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.62

$$\frac{\sqrt{x}(bx+3)}{3(bx+2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(2 + b*x)^(5/2)),x]

[Out] (Sqrt[x]*(3 + b*x))/(3*(2 + b*x)^(3/2))

fricas [A] time = 0.43, size = 32, normalized size = 0.86

$$\frac{(bx+3)\sqrt{bx+2}\sqrt{x}}{3(b^2x^2+4bx+4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(5/2)/x^(1/2),x, algorithm="fricas")

[Out] 1/3*(b*x + 3)*sqrt(b*x + 2)*sqrt(x)/(b^2*x^2 + 4*b*x + 4)

giac [B] time = 1.22, size = 79, normalized size = 2.14

$$\frac{8 \left(3 \left(\sqrt{bx+2} \sqrt{b} - \sqrt{(bx+2)b-2b} \right)^2 + 2b \right) b^{\frac{5}{2}}}{3 \left(\left(\sqrt{bx+2} \sqrt{b} - \sqrt{(bx+2)b-2b} \right)^2 + 2b \right)^3 |b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(5/2)/x^(1/2),x, algorithm="giac")

[Out] 8/3*(3*(sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2 + 2*b)*b^(5/2)/((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2 + 2*b)^3*abs(b)

maple [A] time = 0.00, size = 18, normalized size = 0.49

$$\frac{(bx + 3) \sqrt{x}}{3 (bx + 2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+2)^(5/2)/x^(1/2),x)

[Out] 1/3*x^(1/2)*(b*x+3)/(b*x+2)^(3/2)

maxima [A] time = 1.32, size = 24, normalized size = 0.65

$$-\frac{\left(b - \frac{3(bx+2)}{x}\right)x^{\frac{3}{2}}}{6(bx+2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(5/2)/x^(1/2),x, algorithm="maxima")

[Out] -1/6*(b - 3*(b*x + 2)/x)*x^(3/2)/(b*x + 2)^(3/2)

mupad [B] time = 0.36, size = 42, normalized size = 1.14

$$\frac{3\sqrt{x}\sqrt{bx+2} + bx^{3/2}\sqrt{bx+2}}{3b^2x^2 + 12bx + 12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/2)*(b*x + 2)^(5/2)),x)

[Out] (3*x^(1/2)*(b*x + 2)^(1/2) + b*x^(3/2)*(b*x + 2)^(1/2))/(12*b*x + 3*b^2*x^2 + 12)

sympy [B] time = 1.84, size = 75, normalized size = 2.03

$$\frac{bx}{3b^{\frac{3}{2}}x\sqrt{1 + \frac{2}{bx}} + 6\sqrt{b}\sqrt{1 + \frac{2}{bx}}} + \frac{3}{3b^{\frac{3}{2}}x\sqrt{1 + \frac{2}{bx}} + 6\sqrt{b}\sqrt{1 + \frac{2}{bx}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)**(5/2)/x**(1/2),x)

[Out] b*x/(3*b**(3/2)*x*sqrt(1 + 2/(b*x)) + 6*sqrt(b)*sqrt(1 + 2/(b*x))) + 3/(3*b**(3/2)*x*sqrt(1 + 2/(b*x)) + 6*sqrt(b)*sqrt(1 + 2/(b*x)))

$$3.627 \quad \int \frac{1}{x^{3/2}(2+bx)^{5/2}} dx$$

Optimal. Leaf size=55

$$-\frac{2\sqrt{bx+2}}{3\sqrt{x}} + \frac{2}{3\sqrt{x}\sqrt{bx+2}} + \frac{1}{3\sqrt{x}(bx+2)^{3/2}}$$

[Out] $1/3/(b*x+2)^{(3/2)}/x^{(1/2)}+2/3/x^{(1/2)}/(b*x+2)^{(1/2)}-2/3*(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 55, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{2\sqrt{bx+2}}{3\sqrt{x}} + \frac{2}{3\sqrt{x}\sqrt{bx+2}} + \frac{1}{3\sqrt{x}(bx+2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(2 + b*x)^(5/2)),x]

[Out] $1/(3*\text{Sqrt}[x]*(2 + b*x)^{(3/2)}) + 2/(3*\text{Sqrt}[x]*\text{Sqrt}[2 + b*x]) - (2*\text{Sqrt}[2 + b*x])/ (3*\text{Sqrt}[x])$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{3/2}(2+bx)^{5/2}} dx &= \frac{1}{3\sqrt{x}(2+bx)^{3/2}} + \frac{2}{3} \int \frac{1}{x^{3/2}(2+bx)^{3/2}} dx \\
&= \frac{1}{3\sqrt{x}(2+bx)^{3/2}} + \frac{2}{3\sqrt{x}\sqrt{2+bx}} + \frac{2}{3} \int \frac{1}{x^{3/2}\sqrt{2+bx}} dx \\
&= \frac{1}{3\sqrt{x}(2+bx)^{3/2}} + \frac{2}{3\sqrt{x}\sqrt{2+bx}} - \frac{2\sqrt{2+bx}}{3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 0.58

$$\frac{-2b^2x^2 - 6bx - 3}{3\sqrt{x}(bx+2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(2 + b*x)^(5/2)), x]

[Out] (-3 - 6*b*x - 2*b^2*x^2)/(3*Sqrt[x]*(2 + b*x)^(3/2))

fricas [A] time = 0.42, size = 45, normalized size = 0.82

$$\frac{(2b^2x^2 + 6bx + 3)\sqrt{bx+2}\sqrt{x}}{3(b^2x^3 + 4bx^2 + 4x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+2)^(5/2), x, algorithm="fricas")

[Out] -1/3*(2*b^2*x^2 + 6*b*x + 3)*sqrt(b*x + 2)*sqrt(x)/(b^2*x^3 + 4*b*x^2 + 4*x)

giac [B] time = 1.36, size = 145, normalized size = 2.64

$$\frac{\sqrt{bx+2}b^2}{4\sqrt{(bx+2)b-2b}|b|} \frac{3\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^4 b^{\frac{5}{2}} + 24\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^2 b^{\frac{7}{2}} + 20}{3\left(\left(\sqrt{bx+2}\sqrt{b}-\sqrt{(bx+2)b-2b}\right)^2 + 2b\right)^3 |b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(b*x+2)^(5/2), x, algorithm="giac")

[Out] -1/4*sqrt(b*x + 2)*b^2/(sqrt((b*x + 2)*b - 2*b)*abs(b)) - 1/3*(3*(sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^4*b^(5/2) + 24*(sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^2*b^(7/2) + 20*(sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b)))^3*abs(b))

b) - $\text{sqrt}((b*x + 2)*b - 2*b))^2*b^{(7/2)} + 20*b^{(9/2)} / (((\text{sqrt}(b*x + 2)*\text{sqrt}(b) - \text{sqrt}((b*x + 2)*b - 2*b))^2 + 2*b)^3*\text{abs}(b))$

maple [A] time = 0.00, size = 27, normalized size = 0.49

$$\frac{2b^2x^2 + 6bx + 3}{3(bx + 2)^{\frac{3}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/x^{(3/2)}/(b*x+2)^{(5/2)}, x)$

[Out] $-1/3*(2*b^2*x^2+6*b*x+3)/(b*x+2)^{(3/2)}/x^{(1/2)}$

maxima [A] time = 1.40, size = 40, normalized size = 0.73

$$\frac{\left(b^2 - \frac{6(bx+2)b}{x}\right)x^{\frac{3}{2}}}{12(bx + 2)^{\frac{3}{2}}} - \frac{\sqrt{bx + 2}}{4\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^{(3/2)}/(b*x+2)^{(5/2)}, x, \text{algorithm}="maxima")$

[Out] $1/12*(b^2 - 6*(b*x + 2)*b/x)*x^{(3/2)}/(b*x + 2)^{(3/2)} - 1/4*\text{sqrt}(b*x + 2)/\text{sqrt}(x)$

mupad [B] time = 0.38, size = 57, normalized size = 1.04

$$\frac{3\sqrt{bx+2} + 6bx\sqrt{bx+2} + 2b^2x^2\sqrt{bx+2}}{\sqrt{x}(x(3xb^2 + 12b) + 12)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(x^{(3/2)}*(b*x + 2)^{(5/2)}), x)$

[Out] $-(3*(b*x + 2)^{(1/2)} + 6*b*x*(b*x + 2)^{(1/2)} + 2*b^2*x^2*(b*x + 2)^{(1/2)})/(x^{(1/2)}*(x*(12*b + 3*b^2*x) + 12))$

sympy [B] time = 3.89, size = 117, normalized size = 2.13

$$-\frac{2b^{\frac{13}{2}}x^2\sqrt{1+\frac{2}{bx}}}{3b^6x^2+12b^5x+12b^4} - \frac{6b^{\frac{11}{2}}x\sqrt{1+\frac{2}{bx}}}{3b^6x^2+12b^5x+12b^4} - \frac{3b^{\frac{9}{2}}\sqrt{1+\frac{2}{bx}}}{3b^6x^2+12b^5x+12b^4}$$

Verification of antiderivative is not currently implemented for this CAS.


```
[In] integrate(1/x**(3/2)/(b*x+2)**(5/2),x)
```

```
[Out] -2*b**(13/2)*x**2*sqrt(1 + 2/(b*x))/(3*b**6*x**2 + 12*b**5*x + 12*b**4) - 6  
*b**(11/2)*x*sqrt(1 + 2/(b*x))/(3*b**6*x**2 + 12*b**5*x + 12*b**4) - 3*b**(  
9/2)*sqrt(1 + 2/(b*x))/(3*b**6*x**2 + 12*b**5*x + 12*b**4)
```

$$3.628 \quad \int \frac{1}{x^{5/2}(2+bx)^{5/2}} dx$$

Optimal. Leaf size=71

$$-\frac{2\sqrt{bx+2}}{3x^{3/2}} + \frac{1}{x^{3/2}\sqrt{bx+2}} + \frac{1}{3x^{3/2}(bx+2)^{3/2}} + \frac{2b\sqrt{bx+2}}{3\sqrt{x}}$$

[Out] $1/3/x^{(3/2)}/(b*x+2)^{(3/2)}+1/x^{(3/2)}/(b*x+2)^{(1/2)}-2/3*(b*x+2)^{(1/2)}/x^{(3/2)}+2/3*b*(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{2\sqrt{bx+2}}{3x^{3/2}} + \frac{1}{x^{3/2}\sqrt{bx+2}} + \frac{1}{3x^{3/2}(bx+2)^{3/2}} + \frac{2b\sqrt{bx+2}}{3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(2 + b*x)^(5/2)), x]

[Out] $1/(3*x^{(3/2)}*(2 + b*x)^{(3/2)}) + 1/(x^{(3/2)}*Sqrt[2 + b*x]) - (2*Sqrt[2 + b*x])/ (3*x^{(3/2)}) + (2*b*Sqrt[2 + b*x])/(3*Sqrt[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{5/2}(2+bx)^{5/2}} dx &= \frac{1}{3x^{3/2}(2+bx)^{3/2}} + \int \frac{1}{x^{5/2}(2+bx)^{3/2}} dx \\
&= \frac{1}{3x^{3/2}(2+bx)^{3/2}} + \frac{1}{x^{3/2}\sqrt{2+bx}} + 2 \int \frac{1}{x^{5/2}\sqrt{2+bx}} dx \\
&= \frac{1}{3x^{3/2}(2+bx)^{3/2}} + \frac{1}{x^{3/2}\sqrt{2+bx}} - \frac{2\sqrt{2+bx}}{3x^{3/2}} - \frac{1}{3}(2b) \int \frac{1}{x^{3/2}\sqrt{2+bx}} dx \\
&= \frac{1}{3x^{3/2}(2+bx)^{3/2}} + \frac{1}{x^{3/2}\sqrt{2+bx}} - \frac{2\sqrt{2+bx}}{3x^{3/2}} + \frac{2b\sqrt{2+bx}}{3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 0.56

$$\frac{2b^3x^3 + 6b^2x^2 + 3bx - 1}{3x^{3/2}(bx + 2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(2 + b*x)^(5/2)), x]

[Out] (-1 + 3*b*x + 6*b^2*x^2 + 2*b^3*x^3)/(3*x^(3/2)*(2 + b*x)^(3/2))

fricas [A] time = 0.43, size = 55, normalized size = 0.77

$$\frac{(2b^3x^3 + 6b^2x^2 + 3bx - 1)\sqrt{bx + 2}\sqrt{x}}{3(b^2x^4 + 4bx^3 + 4x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+2)^(5/2), x, algorithm="fricas")

[Out] 1/3*(2*b^3*x^3 + 6*b^2*x^2 + 3*b*x - 1)*sqrt(b*x + 2)*sqrt(x)/(b^2*x^4 + 4*b*x^3 + 4*x^2)

giac [B] time = 1.27, size = 158, normalized size = 2.23

$$\frac{(4(bx + 2)b^2|b| - 9b^2|b|)\sqrt{bx + 2}}{12((bx + 2)b - 2b)^{\frac{3}{2}}} + \frac{3(\sqrt{bx + 2}\sqrt{b} - \sqrt{(bx + 2)b - 2b})^4 b^{\frac{7}{2}} + 18(\sqrt{bx + 2}\sqrt{b} - \sqrt{(bx + 2)b - 2b})^3 |b|}{3\left(\left(\sqrt{bx + 2}\sqrt{b} - \sqrt{(bx + 2)b - 2b}\right)^2 + 2b\right)^3 |b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(b*x+2)^(5/2), x, algorithm="giac")

[Out] $\frac{1}{12}*(4*(b*x + 2)*b^2*abs(b) - 9*b^2*abs(b))*sqrt(b*x + 2)/((b*x + 2)*b - 2*b)^{(3/2)} + \frac{1}{3}*(3*(sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^{4*b^{(7/2)} + 18*(sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^{2*b^{(9/2)} + 16*b^{(11/2)}})/(((sqrt(b*x + 2)*sqrt(b) - sqrt((b*x + 2)*b - 2*b))^{2} + 2*b)^{3*abs(b)})$

maple [A] time = 0.00, size = 35, normalized size = 0.49

$$\frac{2b^3x^3 + 6b^2x^2 + 3bx - 1}{3(bx + 2)^{\frac{3}{2}}x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/2)/(b*x+2)^(5/2),x)`

[Out] $\frac{1}{3}*(2*b^3*x^3+6*b^2*x^2+3*b*x-1)/(b*x+2)^{(3/2)}/x^{(3/2)}$

maxima [A] time = 1.28, size = 55, normalized size = 0.77

$$\frac{3\sqrt{bx+2}}{8\sqrt{x}} - \frac{\left(b^3 - \frac{9(bx+2)b^2}{x}\right)x^{\frac{3}{2}}}{24(bx+2)^{\frac{3}{2}}} - \frac{(bx+2)^{\frac{3}{2}}}{24x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2)/(b*x+2)^(5/2),x, algorithm="maxima")`

[Out] $\frac{3}{8}*sqrt(b*x + 2)*b/sqrt(x) - \frac{1}{24}*(b^3 - 9*(b*x + 2)*b^2/x)*x^{(3/2)}/(b*x + 2)^{(3/2)} - \frac{1}{24}*(b*x + 2)^{(3/2)}/x^{(3/2)}$

mupad [B] time = 0.42, size = 71, normalized size = 1.00

$$\frac{3bx\sqrt{bx+2} - \sqrt{bx+2} + 6b^2x^2\sqrt{bx+2} + 2b^3x^3\sqrt{bx+2}}{x^{3/2}(x(3xb^2 + 12b) + 12)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/2)*(b*x + 2)^(5/2)),x)`

[Out] $\frac{(3*b*x*(b*x + 2)^{(1/2)} - (b*x + 2)^{(1/2)} + 6*b^2*x^2*(b*x + 2)^{(1/2)} + 2*b^3*x^3*(b*x + 2)^{(1/2)})/(x^{(3/2)}*(x*(12*b + 3*b^2*x) + 12))$

sympy [B] time = 6.85, size = 257, normalized size = 3.62

$$\frac{2b^{\frac{27}{2}}x^4\sqrt{1+\frac{2}{bx}}}{3b^{12}x^4+18b^{11}x^3+36b^{10}x^2+24b^9x} + \frac{10b^{\frac{25}{2}}x^3\sqrt{1+\frac{2}{bx}}}{3b^{12}x^4+18b^{11}x^3+36b^{10}x^2+24b^9x} + \frac{15b^{\frac{23}{2}}x^2\sqrt{1+\frac{2}{bx}}}{3b^{12}x^4+18b^{11}x^3+36b^{10}x^2+24b^9x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(b*x+2)**(5/2),x)`

[Out] $2*b^{27/2}*x^4*\sqrt{1 + 2/(b*x)} / (3*b^{12}*x^4 + 18*b^{11}*x^3 + 36*b^{10}*x^2 + 24*b^9*x) + 10*b^{25/2}*x^3*\sqrt{1 + 2/(b*x)} / (3*b^{12}*x^4 + 18*b^{11}*x^3 + 36*b^{10}*x^2 + 24*b^9*x) + 15*b^{23/2}*x^2*\sqrt{1 + 2/(b*x)} / (3*b^{12}*x^4 + 18*b^{11}*x^3 + 36*b^{10}*x^2 + 24*b^9*x) + 5*b^{21/2}*x*\sqrt{1 + 2/(b*x)} / (3*b^{12}*x^4 + 18*b^{11}*x^3 + 36*b^{10}*x^2 + 24*b^9*x) - 2*b^{19/2}*\sqrt{1 + 2/(b*x)} / (3*b^{12}*x^4 + 18*b^{11}*x^3 + 36*b^{10}*x^2 + 24*b^9*x)$

$$3.629 \quad \int \frac{x^{5/2}}{\sqrt{2-bx}} dx$$

Optimal. Leaf size=91

$$\frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} - \frac{5\sqrt{x}\sqrt{2-bx}}{2b^3} - \frac{5x^{3/2}\sqrt{2-bx}}{6b^2} - \frac{x^{5/2}\sqrt{2-bx}}{3b}$$

[Out] $5*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(7/2)}-5/6*x^{(3/2)}*(-b*x+2)^{(1/2)}/b^2-1/3*x^{(5/2)}*(-b*x+2)^{(1/2)}/b-5/2*x^{(1/2)}*(-b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.02, antiderivative size = 91, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$-\frac{5x^{3/2}\sqrt{2-bx}}{6b^2} - \frac{5\sqrt{x}\sqrt{2-bx}}{2b^3} + \frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} - \frac{x^{5/2}\sqrt{2-bx}}{3b}$$

Antiderivative was successfully verified.

[In] `Int[x^(5/2)/Sqrt[2 - b*x], x]`

[Out] $(-5*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/(2*b^3) - (5*x^{(3/2)}*\text{Sqrt}[2 - b*x])/(6*b^2) - (x^{(5/2)}*\text{Sqrt}[2 - b*x])/(3*b) + (5*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/b^{(7/2)}$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{\sqrt{2-bx}} dx &= -\frac{x^{5/2}\sqrt{2-bx}}{3b} + \frac{5 \int \frac{x^{3/2}}{\sqrt{2-bx}} dx}{3b} \\
&= -\frac{5x^{3/2}\sqrt{2-bx}}{6b^2} - \frac{x^{5/2}\sqrt{2-bx}}{3b} + \frac{5 \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx}{2b^2} \\
&= -\frac{5\sqrt{x}\sqrt{2-bx}}{2b^3} - \frac{5x^{3/2}\sqrt{2-bx}}{6b^2} - \frac{x^{5/2}\sqrt{2-bx}}{3b} + \frac{5 \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx}{2b^3} \\
&= -\frac{5\sqrt{x}\sqrt{2-bx}}{2b^3} - \frac{5x^{3/2}\sqrt{2-bx}}{6b^2} - \frac{x^{5/2}\sqrt{2-bx}}{3b} + \frac{5 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right)}{b^3} \\
&= -\frac{5\sqrt{x}\sqrt{2-bx}}{2b^3} - \frac{5x^{3/2}\sqrt{2-bx}}{6b^2} - \frac{x^{5/2}\sqrt{2-bx}}{3b} + \frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 61, normalized size = 0.67

$$\frac{5 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} - \frac{\sqrt{x}\sqrt{2-bx}(2b^2x^2 + 5bx + 15)}{6b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/2)/Sqrt[2 - b*x], x]

[Out] -1/6*(Sqrt[x]*Sqrt[2 - b*x]*(15 + 5*b*x + 2*b^2*x^2))/b^3 + (5*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(7/2)

fricas [A] time = 0.44, size = 125, normalized size = 1.37

$$\left[\frac{(2b^3x^2 + 5b^2x + 15b)\sqrt{-bx + 2}\sqrt{x} + 15\sqrt{-b} \log(-bx + \sqrt{-bx + 2}\sqrt{-b}\sqrt{x} + 1)}{6b^4}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+2)^(1/2), x, algorithm="fricas")

[Out] [-1/6*((2*b^3*x^2 + 5*b^2*x + 15*b)*sqrt(-b*x + 2)*sqrt(x) + 15*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^4, -1/6*((2*b^3*x^2 + 5*b^

$2*x + 15*b)*\sqrt{-b*x + 2}*\sqrt{x} + 30*\sqrt{b}*\arctan(\sqrt{-b*x + 2}/(\sqrt{b}*\sqrt{x}))/b^4$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+2)^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-15.6438432182,61.7937478349]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-29.292030761,78.6493344628]-2*abs(b)/b^2/b*(2*((12*b^5/144/b^7)*sqrt(-b*x+2)*sqrt(-b*x+2)-78*b^5/144/b^7)*sqrt(-b*x+2)*sqrt(-b*x+2)+19*8*b^5/144/b^7)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)-5/2/b/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b)-sqrt(-b)*sqrt(-b*x+2))))

maple [A] time = 0.00, size = 100, normalized size = 1.10

$$-\frac{\sqrt{-bx+2} x^{\frac{5}{2}}}{3b} - \frac{5\sqrt{-bx+2} x^{\frac{3}{2}}}{6b^2} - \frac{5\sqrt{-bx+2} \sqrt{x}}{2b^3} + \frac{5\sqrt{-bx+2} x \arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{2\sqrt{-bx+2} b^{\frac{7}{2}} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/2)/(-b*x+2)^(1/2),x)`

[Out] $-1/3*x^{(5/2)}*(-b*x+2)^{(1/2)}/b-5/6*x^{(3/2)}*(-b*x+2)^{(1/2)}/b^2-5/2*(-b*x+2)^{(1/2)}/b^3*x^{(1/2)}+5/2*((-b*x+2)*x)^{(1/2)}/(-b*x+2)^{(1/2)}/b^{(7/2)}/x^{(1/2)}*\arctan((x-1/b)/(-b*x^2+2*x)^{(1/2)}*b^{(1/2)})$

maxima [A] time = 3.03, size = 117, normalized size = 1.29

$$\frac{\frac{33\sqrt{-bx+2}b^2}{\sqrt{x}} + \frac{40(-bx+2)^{\frac{3}{2}}b}{x^{\frac{3}{2}}} + \frac{15(-bx+2)^{\frac{5}{2}}}{x^{\frac{5}{2}}}}{3\left(b^6 - \frac{3(bx-2)b^5}{x} + \frac{3(bx-2)^2b^4}{x^2} - \frac{(bx-2)^3b^3}{x^3}\right)} - \frac{5 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/2)/(-b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $-1/3*(33*\sqrt{-b*x+2})*b^2/\sqrt{x} + 40*(-b*x+2)^{(3/2)}*b/x^{(3/2)} + 15*(-b*x+2)^{(5/2)}/x^{(5/2)})/(b^6 - 3*(b*x-2)*b^5/x + 3*(b*x-2)^2*b^4/x^2 - (b*x-2)^3*b^3/x^3) - 5*\arctan(\sqrt{-b*x+2}/(\sqrt{b}*\sqrt{x}))/b^{(7/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{\sqrt{2-bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/2)/(2-b*x)^(1/2),x)`

[Out] `int(x^(5/2)/(2-b*x)^(1/2),x)`

sympy [A] time = 7.51, size = 206, normalized size = 2.26

$$\left\{ \begin{array}{l} -\frac{x^{\frac{7}{2}}}{3\sqrt{bx-2}} - \frac{x^{\frac{5}{2}}}{6b\sqrt{bx-2}} - \frac{5x^{\frac{3}{2}}}{6b^2\sqrt{bx-2}} + \frac{5i\sqrt{x}}{b^3\sqrt{bx-2}} - \frac{5i\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{7}{2}}} \\ \frac{x^{\frac{7}{2}}}{3\sqrt{-bx+2}} + \frac{x^{\frac{5}{2}}}{6b\sqrt{-bx+2}} + \frac{5x^{\frac{3}{2}}}{6b^2\sqrt{-bx+2}} - \frac{5\sqrt{x}}{b^3\sqrt{-bx+2}} + \frac{5\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{7}{2}}} \end{array} \right. \begin{array}{l} \text{for } \frac{|bx|}{2} > 1 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(-b*x+2)**(1/2), x)

[Out] Piecewise((-I*x**(7/2)/(3*sqrt(b*x - 2)) - I*x**(5/2)/(6*b*sqrt(b*x - 2)) - 5*I*x**(3/2)/(6*b**2*sqrt(b*x - 2)) + 5*I*sqrt(x)/(b**3*sqrt(b*x - 2)) - 5*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(7/2), Abs(b*x)/2 > 1), (x**(7/2)/(3*sqrt(-b*x + 2)) + x**(5/2)/(6*b*sqrt(-b*x + 2)) + 5*x**(3/2)/(6*b**2*sqrt(-b*x + 2)) - 5*sqrt(x)/(b**3*sqrt(-b*x + 2)) + 5*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(7/2), True))

$$3.630 \quad \int \frac{x^{3/2}}{\sqrt{2-bx}} dx$$

Optimal. Leaf size=69

$$\frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{3\sqrt{x}\sqrt{2-bx}}{2b^2} - \frac{x^{3/2}\sqrt{2-bx}}{2b}$$

[Out] $3*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(5/2)}-1/2*x^{(3/2)}*(-b*x+2)^{(1/2)}/b-3/2*x^{(1/2)}*(-b*x+2)^{(1/2)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$-\frac{3\sqrt{x}\sqrt{2-bx}}{2b^2} + \frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{x^{3/2}\sqrt{2-bx}}{2b}$$

Antiderivative was successfully verified.

[In] Int[x^(3/2)/Sqrt[2 - b*x], x]

[Out] $(-3*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/(2*b^2) - (x^{(3/2)}*\text{Sqrt}[2 - b*x])/(2*b) + (3*\text{Arc Sin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/b^{(5/2)}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] :> Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{x^{3/2}}{\sqrt{2-bx}} dx &= -\frac{x^{3/2}\sqrt{2-bx}}{2b} + \frac{3}{2b} \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{2b^2} - \frac{x^{3/2}\sqrt{2-bx}}{2b} + \frac{3}{2b^2} \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{2b^2} - \frac{x^{3/2}\sqrt{2-bx}}{2b} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\
&= -\frac{3\sqrt{x}\sqrt{2-bx}}{2b^2} - \frac{x^{3/2}\sqrt{2-bx}}{2b} + \frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 52, normalized size = 0.75

$$\frac{3 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{\sqrt{x}\sqrt{2-bx}(bx+3)}{2b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/Sqrt[2 - b*x], x]

[Out] -1/2*(Sqrt[x]*Sqrt[2 - b*x]*(3 + b*x))/b^2 + (3*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(5/2)

fricas [A] time = 0.47, size = 107, normalized size = 1.55

$$\left[-\frac{(b^2x+3b)\sqrt{-bx+2}\sqrt{x}+3\sqrt{-b}\log(-bx+\sqrt{-bx+2}\sqrt{-b}\sqrt{x}+1)}{2b^3}, -\frac{(b^2x+3b)\sqrt{-bx+2}\sqrt{x}+6\sqrt{b}\arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{2b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+2)^(1/2), x, algorithm="fricas")

[Out] [-1/2*((b^2*x+3*b)*sqrt(-b*x+2)*sqrt(x)+3*sqrt(-b)*log(-b*x+sqrt(-b*x+2)*sqrt(-b)*sqrt(x)+1))/b^3, -1/2*((b^2*x+3*b)*sqrt(-b*x+2)*sqrt(x)+6*sqrt(b)*arctan(sqrt(-b*x+2)/(sqrt(b)*sqrt(x))))/b^3]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+2)^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-15.6438432182,61.7937478349]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-29.292030761,78.6493344628]2*abs(b)/b^2/b^2*(2*(1/8*sqrt(-b*x+2)*sqrt(-b*x+2)-5/8)*sqrt(-b*x+2)*sqrt(-b*(-b*x+2)+2*b)+6*b/4/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b)-sqrt(-b)*sqrt(-b*x+2))))

maple [A] time = 0.00, size = 84, normalized size = 1.22

$$-\frac{\sqrt{-bx+2} x^{\frac{3}{2}}}{2b} - \frac{3\sqrt{-bx+2} \sqrt{x}}{2b^2} + \frac{3\sqrt{-bx+2} x \arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{2\sqrt{-bx+2} b^{\frac{5}{2}} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(-b*x+2)^(1/2),x)

[Out] $-1/2*x^{(3/2)}*(-b*x+2)^{(1/2)}/b-3/2*(-b*x+2)^{(1/2)}/b^2*x^{(1/2)}+3/2*((-b*x+2)*x)^{(1/2)}/(-b*x+2)^{(1/2)}/b^{(5/2)}/x^{(1/2)}*\arctan((x-1/b)/(-b*x^2+2*x)^{(1/2)}*b^{(1/2)})$

maxima [A] time = 2.93, size = 85, normalized size = 1.23

$$-\frac{\frac{5\sqrt{-bx+2}b}{\sqrt{x}} + \frac{3(-bx+2)^{\frac{3}{2}}}{x^{\frac{3}{2}}}}{b^4 - \frac{2(bx-2)b^3}{x} + \frac{(bx-2)^2b^2}{x^2}} - \frac{3 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(3/2)/(-b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $-(5*\sqrt{-b*x + 2})*b/\sqrt{x} + 3*(-b*x + 2)^{(3/2)}/x^{(3/2)}/(b^4 - 2*(b*x - 2)*b^3/x + (b*x - 2)^2*b^2/x^2) - 3*\arctan(\sqrt{-b*x + 2}/(\sqrt{b}*\sqrt{x}))/b^{(5/2)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{3/2}}{\sqrt{2-bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(2 - b*x)^(1/2),x)`

[Out] `int(x^(3/2)/(2 - b*x)^(1/2), x)`

sympy [A] time = 3.59, size = 163, normalized size = 2.36

$$\begin{cases} -\frac{5}{2\sqrt{bx-2}} - \frac{3}{2b\sqrt{bx-2}} + \frac{3i\sqrt{x}}{b^2\sqrt{bx-2}} - \frac{3i\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{5}{2}}} & \text{for } \frac{|bx|}{2} > 1 \\ \frac{5}{2\sqrt{-bx+2}} + \frac{3}{2b\sqrt{-bx+2}} - \frac{3\sqrt{x}}{b^2\sqrt{-bx+2}} + \frac{3\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{5}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(-b*x+2)**(1/2),x)`

[Out] `Piecewise((-I*x**(5/2)/(2*sqrt(b*x - 2)) - I*x**(3/2)/(2*b*sqrt(b*x - 2)) + 3*I*sqrt(x)/(b**2*sqrt(b*x - 2)) - 3*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(5/2), Abs(b*x)/2 > 1), (x**(5/2)/(2*sqrt(-b*x + 2)) + x**(3/2)/(2*b*sqrt(-b*x + 2)) - 3*sqrt(x)/(b**2*sqrt(-b*x + 2)) + 3*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(5/2), True))`

$$3.631 \quad \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx$$

Optimal. Leaf size=45

$$\frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} - \frac{\sqrt{x}\sqrt{2-bx}}{b}$$

[Out] $2*\arcsin(1/2*b^{(1/2)*x^{(1/2)}*2^{(1/2)})/b^{(3/2)}-x^{(1/2)}*(-b*x+2)^{(1/2)}/b$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {50, 54, 216}

$$\frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} - \frac{\sqrt{x}\sqrt{2-bx}}{b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/Sqrt[2 - b*x], x]

[Out] $-((\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/b) + (2*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/(\text{Sqrt}[2])])/b^{(3/2)}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{x}}{\sqrt{2-bx}} dx &= -\frac{\sqrt{x}\sqrt{2-bx}}{b} + \frac{\int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx}{b} \\
&= -\frac{\sqrt{x}\sqrt{2-bx}}{b} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right)}{b} \\
&= -\frac{\sqrt{x}\sqrt{2-bx}}{b} + \frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 1.00

$$\frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} - \frac{\sqrt{x}\sqrt{2-bx}}{b}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/Sqrt[2 - b*x], x]

[Out] -((Sqrt[x]*Sqrt[2 - b*x])/b) + (2*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(3/2)

fricas [A] time = 0.46, size = 90, normalized size = 2.00

$$\left[-\frac{\sqrt{-bx+2} b\sqrt{x} + \sqrt{-b} \log(-bx + \sqrt{-bx+2} \sqrt{-b} \sqrt{x} + 1)}{b^2}, -\frac{\sqrt{-bx+2} b\sqrt{x} + 2\sqrt{b} \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+2)^(1/2), x, algorithm="fricas")

[Out] [-(sqrt(-b*x + 2)*b*sqrt(x) + sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1))/b^2, -(sqrt(-b*x + 2)*b*sqrt(x) + 2*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))))/b^2]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+2)^(1/2), x, algorithm="giac")

maxima [A] time = 2.93, size = 52, normalized size = 1.16

$$-\frac{2 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{3}{2}}} - \frac{2\sqrt{-bx+2}}{\left(b^2 - \frac{(bx-2)b}{x}\right)\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+2)^(1/2),x, algorithm="maxima")

[Out] -2*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/b^(3/2) - 2*sqrt(-b*x + 2)/((b^2 - (b*x - 2)*b/x)*sqrt(x))

mupad [B] time = 0.52, size = 46, normalized size = 1.02

$$-\frac{4 \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}-\sqrt{2-bx}}\right)}{b^{3/2}} - \frac{\sqrt{x}\sqrt{2-bx}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(2 - b*x)^(1/2),x)

[Out] - (4*atan((b^(1/2)*x^(1/2))/(2^(1/2) - (2 - b*x)^(1/2))))/b^(3/2) - (x^(1/2)*(2 - b*x)^(1/2))/b

sympy [A] time = 1.97, size = 121, normalized size = 2.69

$$\begin{cases} -\frac{x^{\frac{3}{2}}}{\sqrt{bx-2}} + \frac{2i\sqrt{x}}{b\sqrt{bx-2}} - \frac{2i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}} & \text{for } \frac{|bx|}{2} > 1 \\ \frac{x^{\frac{3}{2}}}{\sqrt{-bx+2}} - \frac{2\sqrt{x}}{b\sqrt{-bx+2}} + \frac{2 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(1/2)/(-b*x+2)**(1/2),x)

[Out] Piecewise((-I*x**(3/2)/sqrt(b*x - 2) + 2*I*sqrt(x)/(b*sqrt(b*x - 2)) - 2*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2), Abs(b*x)/2 > 1), (x**(3/2)/sqrt(-b*x + 2) - 2*sqrt(x)/(b*sqrt(-b*x + 2)) + 2*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2), True))

$$3.632 \quad \int \frac{1}{\sqrt{x} \sqrt{2-bx}} dx$$

Optimal. Leaf size=24

$$\frac{2 \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}$$

[Out] 2*arcsin(1/2*b^(1/2)*x^(1/2)*2^(1/2))/b^(1/2)

Rubi [A] time = 0.01, antiderivative size = 24, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {54, 216}

$$\frac{2 \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*Sqrt[2 - b*x]),x]

[Out] (2*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{x} \sqrt{2-bx}} dx &= 2 \text{Subst} \left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x} \right) \\ &= \frac{2 \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 1.00

$$\frac{2 \sin^{-1} \left(\frac{\sqrt{b} \sqrt{x}}{\sqrt{2}} \right)}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*Sqrt[2 - b*x]),x]

[Out] (2*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/Sqrt[b]

fricas [A] time = 0.45, size = 56, normalized size = 2.33

$$\left[-\frac{\sqrt{-b} \log(-bx + \sqrt{-bx+2} \sqrt{-b} \sqrt{x} + 1)}{b}, \frac{2 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b} \sqrt{x}}\right)}{\sqrt{b}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-b*x+2)^(1/2),x, algorithm="fricas")

[Out] [-sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1)/b, -2*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/sqrt(b)]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-b*x+2)^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0

,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-15.64384 32182,61.7937478349]Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-8,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-28,[1,1]%%}+%%{-8,[1,0]%%}+%%{6,[0,2]%%}+%%{8,[0,1]%%}+%%{24,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-64,[2,2]%%}+%%{20,[2,1]%%}+%%{8,[2,0]%%}+%%{-4,[1,3]%%}+%%{-20,[1,2]%%}+%%{128,[1,1]%%}+%%{-16,[1,0]%%}+%%{-4,[0,3]%%}+%%{8,[0,2]%%}+%%{16,[0,1]%%}+%%{-32,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-12,[3,3]%%}+%%{20,[3,2]%%}+%%{-20,[3,1]%%}+%%{8,[3,0]%%}+%%{6,[2,4]%%}+%%{-20,[2,3]%%}+%%{46,[2,2]%%}+%%{-40,[2,1]%%}+%%{24,[2,0]%%}+%%{4,[1,4]%%}+%%{-20,[1,3]%%}+%%{40,[1,2]%%}+%%{-48,[1,1]%%}+%%{32,[1,0]%%}+%%{1,[0,4]%%}+%%{-8,[0,3]%%}+%%{24,[0,2]%%}+%%{-32,[0,1]%%}+%%{16,[0,0]%%}] at parameters values [-29.292030761,78.6493344628]2/abs(b)*b^2/b/sqrt(-b)*ln(abs(sqrt(-b*(-b*x+2)+2*b)-sqrt(-b)*sqrt(-b*x+2)))

maple [B] time = 0.00, size = 50, normalized size = 2.08

$$\frac{\sqrt{-bx+2}x \arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{\sqrt{-bx+2} \sqrt{b} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/2)/(-b*x+2)^(1/2),x)

[Out] ((-b*x+2)*x)^(1/2)/(-b*x+2)^(1/2)/b^(1/2)/x^(1/2)*arctan((x-1/b)/(-b*x^2+2*x)^(1/2)*b^(1/2))

maxima [A] time = 2.96, size = 21, normalized size = 0.88

$$\frac{2 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b} \sqrt{x}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-b*x+2)^(1/2),x, algorithm="maxima")

[Out] -2*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/sqrt(b)

mupad [B] time = 0.03, size = 27, normalized size = 1.12

$$\frac{4 \operatorname{atan}\left(\frac{\sqrt{2}-\sqrt{2-bx}}{\sqrt{b} \sqrt{x}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(2 - b*x)^(1/2)),x)`

[Out] `(4*atan((2^(1/2) - (2 - b*x)^(1/2))/(b^(1/2)*x^(1/2))))/b^(1/2)`

sympy [A] time = 1.08, size = 58, normalized size = 2.42

$$\begin{cases} -\frac{2i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}} & \text{for } \frac{|bx|}{2} > 1 \\ \frac{2 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(1/2)/(-b*x+2)**(1/2),x)`

[Out] `Piecewise((-2*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/sqrt(b), Abs(b*x)/2 > 1), (2*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/sqrt(b), True))`

$$3.633 \quad \int \frac{1}{x^{3/2} \sqrt{2-bx}} dx$$

Optimal. Leaf size=17

$$-\frac{\sqrt{2-bx}}{\sqrt{x}}$$

[Out] $-(b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {37}

$$-\frac{\sqrt{2-bx}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*Sqrt[2 - b*x]),x]

[Out] -(Sqrt[2 - b*x]/Sqrt[x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{x^{3/2} \sqrt{2-bx}} dx = -\frac{\sqrt{2-bx}}{\sqrt{x}}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$-\frac{\sqrt{2-bx}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*Sqrt[2 - b*x]),x]

[Out] -(Sqrt[2 - b*x]/Sqrt[x])

fricas [A] time = 0.42, size = 13, normalized size = 0.76

$$-\frac{\sqrt{-bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+2)^(1/2),x, algorithm="fricas")

[Out] -sqrt(-b*x + 2)/sqrt(x)

giac [B] time = 1.28, size = 30, normalized size = 1.76

$$-\frac{\sqrt{-bx+2}b^2}{\sqrt{(bx-2)b+2b|b|}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+2)^(1/2),x, algorithm="giac")

[Out] -sqrt(-b*x + 2)*b^2/(sqrt((b*x - 2)*b + 2*b)*abs(b))

maple [A] time = 0.00, size = 14, normalized size = 0.82

$$-\frac{\sqrt{-bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2)/(-b*x+2)^(1/2),x)

[Out] -(-b*x+2)^(1/2)/x^(1/2)

maxima [A] time = 1.35, size = 13, normalized size = 0.76

$$-\frac{\sqrt{-bx+2}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+2)^(1/2),x, algorithm="maxima")

[Out] -sqrt(-b*x + 2)/sqrt(x)

mupad [B] time = 0.31, size = 13, normalized size = 0.76

$$-\frac{\sqrt{2-bx}}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(2 - b*x)^(1/2)),x)`

[Out] $-(2 - b*x)^{(1/2)}/x^{(1/2)}$

sympy [A] time = 0.93, size = 39, normalized size = 2.29

$$\begin{cases} -\sqrt{b} \sqrt{-1 + \frac{2}{bx}} & \text{for } \frac{2}{|bx|} > 1 \\ -i\sqrt{b} \sqrt{1 - \frac{2}{bx}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(-b*x+2)**(1/2),x)`

[Out] `Piecewise((-sqrt(b)*sqrt(-1 + 2/(b*x)), 2/Abs(b*x) > 1), (-I*sqrt(b)*sqrt(1 - 2/(b*x)), True))`

$$3.634 \quad \int \frac{1}{x^{5/2} \sqrt{2-bx}} dx$$

Optimal. Leaf size=40

$$-\frac{\sqrt{2-bx}}{3x^{3/2}} - \frac{b\sqrt{2-bx}}{3\sqrt{x}}$$

[Out] $-1/3*(-b*x+2)^{(1/2)}/x^{(3/2)}-1/3*b*(-b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{\sqrt{2-bx}}{3x^{3/2}} - \frac{b\sqrt{2-bx}}{3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] `Int[1/(x^(5/2)*Sqrt[2 - b*x]),x]`

[Out] $-\text{Sqrt}[2 - b*x]/(3*x^{(3/2)}) - (b*\text{Sqrt}[2 - b*x])/(3*\text{Sqrt}[x])$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp
[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
+ d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{x^{5/2}\sqrt{2-bx}} dx = -\frac{\sqrt{2-bx}}{3x^{3/2}} + \frac{1}{3}b \int \frac{1}{x^{3/2}\sqrt{2-bx}} dx$$

$$= -\frac{\sqrt{2-bx}}{3x^{3/2}} - \frac{b\sqrt{2-bx}}{3\sqrt{x}}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.60

$$-\frac{\sqrt{2-bx}(bx+1)}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*Sqrt[2 - b*x]), x]

[Out] -1/3*(Sqrt[2 - b*x]*(1 + b*x))/x^(3/2)

fricas [A] time = 0.45, size = 18, normalized size = 0.45

$$-\frac{(bx+1)\sqrt{-bx+2}}{3x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+2)^(1/2), x, algorithm="fricas")

[Out] -1/3*(b*x + 1)*sqrt(-b*x + 2)/x^(3/2)

giac [A] time = 1.12, size = 43, normalized size = 1.08

$$-\frac{((bx-2)b^3 + 3b^3)\sqrt{-bx+2}b}{3((bx-2)b + 2b)^{3/2}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+2)^(1/2), x, algorithm="giac")

[Out] -1/3*((b*x - 2)*b^3 + 3*b^3)*sqrt(-b*x + 2)*b/(((b*x - 2)*b + 2*b)^(3/2)*abs(b))

maple [A] time = 0.00, size = 19, normalized size = 0.48

$$-\frac{(bx+1)\sqrt{-bx+2}}{3x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/2)/(-b*x+2)^(1/2),x)`

[Out] $-1/3*(b*x+1)/x^(3/2)*(-b*x+2)^(1/2)$

maxima [A] time = 1.35, size = 28, normalized size = 0.70

$$-\frac{\sqrt{-bx+2}b}{2\sqrt{x}} - \frac{(-bx+2)^{\frac{3}{2}}}{6x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/2)/(-b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $-1/2*\text{sqrt}(-b*x + 2)*b/\text{sqrt}(x) - 1/6*(-b*x + 2)^(3/2)/x^(3/2)$

mupad [B] time = 0.29, size = 19, normalized size = 0.48

$$-\frac{\sqrt{2-bx}\left(\frac{bx}{3} + \frac{1}{3}\right)}{x^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/2)*(2 - b*x)^(1/2)),x)`

[Out] $-((2 - b*x)^(1/2)*((b*x)/3 + 1/3))/x^(3/2)$

sympy [A] time = 1.96, size = 139, normalized size = 3.48

$$\begin{cases} -\frac{b^{\frac{3}{2}}\sqrt{-1+\frac{2}{bx}}}{3} - \frac{\sqrt{b}\sqrt{-1+\frac{2}{bx}}}{3x} & \text{for } \frac{2}{|bx|} > 1 \\ \frac{ib^{\frac{7}{2}}x^2\sqrt{1-\frac{2}{bx}}}{-3b^2x^2+6bx} - \frac{ib^{\frac{5}{2}}x\sqrt{1-\frac{2}{bx}}}{-3b^2x^2+6bx} - \frac{2ib^{\frac{3}{2}}\sqrt{1-\frac{2}{bx}}}{-3b^2x^2+6bx} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/2)/(-b*x+2)**(1/2),x)`

[Out] `Piecewise((-b**(3/2)*sqrt(-1 + 2/(b*x))/3 - sqrt(b)*sqrt(-1 + 2/(b*x))/(3*x), 2/Abs(b*x) > 1), (I*b**(7/2)*x**2*sqrt(1 - 2/(b*x))/(-3*b**2*x**2 + 6*b*x) - I*b**(5/2)*x*sqrt(1 - 2/(b*x))/(-3*b**2*x**2 + 6*b*x) - 2*I*b**(3/2)*sqrt(1 - 2/(b*x))/(-3*b**2*x**2 + 6*b*x), True))`

$$3.635 \quad \int \frac{x^{5/2}}{(2-bx)^{3/2}} dx$$

Optimal. Leaf size=89

$$-\frac{15 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} + \frac{15\sqrt{x}\sqrt{2-bx}}{2b^3} + \frac{5x^{3/2}\sqrt{2-bx}}{2b^2} + \frac{2x^{5/2}}{b\sqrt{2-bx}}$$

[Out] $-15*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(7/2)}+2*x^{(5/2)}/b/(-b*x+2)^{(1/2)}+5/2*x^{(3/2)}*(-b*x+2)^{(1/2)}/b^2+15/2*x^{(1/2)}*(-b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.02, antiderivative size = 89, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {47, 50, 54, 216}

$$\frac{5x^{3/2}\sqrt{2-bx}}{2b^2} + \frac{15\sqrt{x}\sqrt{2-bx}}{2b^3} - \frac{15 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} + \frac{2x^{5/2}}{b\sqrt{2-bx}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(5/2)}/(2 - b*x)^{(3/2)}, x]$

[Out] $(2*x^{(5/2)})/(b*\text{Sqrt}[2 - b*x]) + (15*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/(2*b^3) + (5*x^{(3/2)}*\text{Sqrt}[2 - b*x])/(2*b^2) - (15*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/b^{(7/2)}$

Rule 47

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + 1)), x] - \text{Dist}[(d*n)/(b*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned} \int \frac{x^{5/2}}{(2-bx)^{3/2}} dx &= \frac{2x^{5/2}}{b\sqrt{2-bx}} - \frac{5 \int \frac{x^{3/2}}{\sqrt{2-bx}} dx}{b} \\ &= \frac{2x^{5/2}}{b\sqrt{2-bx}} + \frac{5x^{3/2}\sqrt{2-bx}}{2b^2} - \frac{15 \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx}{2b^2} \\ &= \frac{2x^{5/2}}{b\sqrt{2-bx}} + \frac{15\sqrt{x}\sqrt{2-bx}}{2b^3} + \frac{5x^{3/2}\sqrt{2-bx}}{2b^2} - \frac{15 \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx}{2b^3} \\ &= \frac{2x^{5/2}}{b\sqrt{2-bx}} + \frac{15\sqrt{x}\sqrt{2-bx}}{2b^3} + \frac{5x^{3/2}\sqrt{2-bx}}{2b^2} - \frac{15 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right)}{b^3} \\ &= \frac{2x^{5/2}}{b\sqrt{2-bx}} + \frac{15\sqrt{x}\sqrt{2-bx}}{2b^3} + \frac{5x^{3/2}\sqrt{2-bx}}{2b^2} - \frac{15 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.34

$$\frac{x^{7/2} {}_2F_1\left(\frac{3}{2}, \frac{7}{2}, \frac{9}{2}, \frac{bx}{2}\right)}{7\sqrt{2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(5/2)/(2 - b*x)^(3/2), x]
```

```
[Out] (x^(7/2)*Hypergeometric2F1[3/2, 7/2, 9/2, (b*x)/2])/(7*Sqrt[2])
```

fricas [A] time = 0.48, size = 155, normalized size = 1.74

$$\left[\frac{15(bx-2)\sqrt{-b} \log(-bx - \sqrt{-bx+2} \sqrt{-b} \sqrt{x} + 1) - (b^3x^2 + 5b^2x - 30b)\sqrt{-bx+2} \sqrt{x}}{2(b^5x - 2b^4)}, \frac{30(bx-2)\sqrt{b} \arctan\left(\frac{\sqrt{-bx+2} \sqrt{-b} \sqrt{x}}{\sqrt{b} \sqrt{x}}\right)}{2(b^5x - 2b^4)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+2)^(3/2),x, algorithm="fricas")

[Out] [-1/2*(15*(b*x - 2)*sqrt(-b)*log(-b*x - sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1) - (b^3*x^2 + 5*b^2*x - 30*b)*sqrt(-b*x + 2)*sqrt(x))/(b^5*x - 2*b^4), 1/2*(30*(b*x - 2)*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) + (b^3*x^2 + 5*b^2*x - 30*b)*sqrt(-b*x + 2)*sqrt(x))/(b^5*x - 2*b^4)]

giac [B] time = 10.85, size = 136, normalized size = 1.53

$$\frac{\left(\sqrt{(bx-2)b+2b} \sqrt{-bx+2} \left(\frac{bx-2}{b^3} + \frac{9}{b^3} \right) - \frac{15 \log\left(\left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b}\right)^2\right)}{\sqrt{-b} b^2} \right) + \frac{64}{\left(\left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b}\right)^2 - 2b\right) \sqrt{-b} b^2}}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+2)^(3/2),x, algorithm="giac")

[Out] 1/2*(sqrt((b*x - 2)*b + 2*b)*sqrt(-b*x + 2)*((b*x - 2)/b^3 + 9/b^3) - 15*log((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2)/(sqrt(-b)*b^2) + 64/(((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2 - 2*b)*sqrt(-b)*b))*abs(b)/b^2

maple [B] time = 0.03, size = 138, normalized size = 1.55

$$\frac{\left(\frac{15 \arctan\left(\frac{\left(\frac{x-1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{2b^{\frac{7}{2}}} + \frac{8\sqrt{\left(\frac{x-2}{b}\right)^2 b - 2x + \frac{4}{b}}}{\left(\frac{x-2}{b}\right)b^4} \right) \sqrt{(-bx+2)x}}{\sqrt{-bx+2} \sqrt{x}} - \frac{(bx+7)(bx-2)\sqrt{(-bx+2)x} \sqrt{x}}{2\sqrt{-(bx-2)x} \sqrt{-bx+2} b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(-b*x+2)^(3/2),x)

[Out] -1/2*(b*x+7)*(b*x-2)*x^(1/2)/b^3/(-(b*x-2)*x)^(1/2)*((-b*x+2)*x)^(1/2)/(-b*x+2)^(1/2)-(15/2/b^(7/2)*arctan((x-1/b)/(-b*x^2+2*x)^(1/2)*b^(1/2))+8/b^4/(

$x-2/b)*(-b*(x-2/b)^2-2*x+4/b)^{(1/2)}*((-b*x+2)*x)^{(1/2)/(-b*x+2)^{(1/2)/x^{(1/2)}}$

maxima [A] time = 2.99, size = 101, normalized size = 1.13

$$\frac{8b^2 - \frac{25(bx-2)b}{x} + \frac{15(bx-2)^2}{x^2}}{\frac{\sqrt{-bx+2}b^5}{\sqrt{x}} + \frac{2(-bx+2)^{\frac{3}{2}}b^4}{x^{\frac{3}{2}}} + \frac{(-bx+2)^{\frac{5}{2}}b^3}{x^{\frac{5}{2}}}} + \frac{15 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+2)^(3/2),x, algorithm="maxima")

[Out] (8*b^2 - 25*(b*x - 2)*b/x + 15*(b*x - 2)^2/x^2)/(sqrt(-b*x + 2)*b^5/sqrt(x) + 2*(-b*x + 2)^(3/2)*b^4/x^(3/2) + (-b*x + 2)^(5/2)*b^3/x^(5/2)) + 15*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/b^(7/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{(2 - bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(2 - b*x)^(3/2),x)

[Out] int(x^(5/2)/(2 - b*x)^(3/2), x)

sympy [A] time = 7.03, size = 173, normalized size = 1.94

$$\begin{cases} \frac{ix^{\frac{5}{2}}}{2b\sqrt{bx-2}} + \frac{5ix^{\frac{3}{2}}}{2b^2\sqrt{bx-2}} - \frac{15i\sqrt{x}}{b^3\sqrt{bx-2}} + \frac{15i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{7}{2}}} & \text{for } \frac{|bx|}{2} > 1 \\ -\frac{x^{\frac{5}{2}}}{2b\sqrt{-bx+2}} - \frac{5x^{\frac{3}{2}}}{2b^2\sqrt{-bx+2}} + \frac{15\sqrt{x}}{b^3\sqrt{-bx+2}} - \frac{15 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{7}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/2)/(-b*x+2)**(3/2),x)

[Out] Piecewise((I*x**(5/2)/(2*b*sqrt(b*x - 2)) + 5*I*x**(3/2)/(2*b**2*sqrt(b*x - 2)) - 15*I*sqrt(x)/(b**3*sqrt(b*x - 2)) + 15*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(7/2), Abs(b*x)/2 > 1), (-x**(5/2)/(2*b*sqrt(-b*x + 2)) - 5*x**(3/2)/(2*b**2*sqrt(-b*x + 2)) + 15*sqrt(x)/(b**3*sqrt(-b*x + 2)) - 15*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(7/2), True))

$$3.636 \quad \int \frac{x^{3/2}}{(2-bx)^{3/2}} dx$$

Optimal. Leaf size=65

$$-\frac{6 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{3\sqrt{x}\sqrt{2-bx}}{b^2} + \frac{2x^{3/2}}{b\sqrt{2-bx}}$$

[Out] $-6*\arcsin(1/2*b^{(1/2)}*x^{(1/2)*2^{(1/2)}}/b^{(5/2)}+2*x^{(3/2)}/b/(-b*x+2)^{(1/2)}+3*x^{(1/2)}*(-b*x+2)^{(1/2)}/b^2$

Rubi [A] time = 0.01, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {47, 50, 54, 216}

$$\frac{3\sqrt{x}\sqrt{2-bx}}{b^2} - \frac{6 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{2x^{3/2}}{b\sqrt{2-bx}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(3/2)}/(2 - b*x)^{(3/2)}, x]$

[Out] $(2*x^{(3/2)})/(b*\text{Sqrt}[2 - b*x]) + (3*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/b^2 - (6*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/(\text{Sqrt}[2])])/b^{(5/2)}$

Rule 47

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + 1)), x] - \text{Dist}[(d*n)/(b*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\text{FreeQ}\{a, b, c, d\}, x$ && $\text{NeQ}[b*c - a*d, 0]$ && $\text{GtQ}[n, 0]$ && $\text{LtQ}[m, -1]$ && $!(\text{IntegerQ}[n] \&\& \text{IntegerQ}[m])$ && $!(\text{ILeQ}[m + n + 2, 0] \&\& (\text{FractionQ}[m] \mid\mid \text{GeQ}[2*n + m + 1, 0]))$ && $\text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^{(m)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\text{FreeQ}\{a, b, c, d\}, x$ && $\text{NeQ}[b*c - a*d, 0]$ && $\text{GtQ}[n, 0]$ && $\text{NeQ}[m + n + 1, 0]$ && $!(\text{IGtQ}[m, 0] \&\& (\text{IntegerQ}[n] \mid\mid (\text{GtQ}[m, 0] \&\& \text{LtQ}[m - n, 0])))$ && $!\text{ILtQ}[m + n + 2, 0]$ && $\text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned} \int \frac{x^{3/2}}{(2-bx)^{3/2}} dx &= \frac{2x^{3/2}}{b\sqrt{2-bx}} - \frac{3 \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx}{b} \\ &= \frac{2x^{3/2}}{b\sqrt{2-bx}} + \frac{3\sqrt{x}\sqrt{2-bx}}{b^2} - \frac{3 \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx}{b^2} \\ &= \frac{2x^{3/2}}{b\sqrt{2-bx}} + \frac{3\sqrt{x}\sqrt{2-bx}}{b^2} - \frac{6 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\ &= \frac{2x^{3/2}}{b\sqrt{2-bx}} + \frac{3\sqrt{x}\sqrt{2-bx}}{b^2} - \frac{6 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.46

$$\frac{x^{5/2} {}_2F_1\left(\frac{3}{2}, \frac{5}{2}, \frac{7}{2}, \frac{bx}{2}\right)}{5\sqrt{2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(3/2)/(2 - b*x)^(3/2), x]
```

```
[Out] (x^(5/2)*Hypergeometric2F1[3/2, 5/2, 7/2, (b*x)/2])/(5*Sqrt[2])
```

fricas [A] time = 0.46, size = 138, normalized size = 2.12

$$\left[\frac{3(bx-2)\sqrt{-b} \log(-bx - \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1) - (b^2x - 6b)\sqrt{-bx+2}\sqrt{x}}{b^4x - 2b^3}, \frac{6(bx-2)\sqrt{b} \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^4x - 2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+2)^(3/2),x, algorithm="fricas")

[Out] $[-(3*(b*x - 2)*\sqrt{-b}*\log(-b*x - \sqrt{-b*x + 2}*\sqrt{-b}*\sqrt{x} + 1) - (b^2*x - 6*b)*\sqrt{-b*x + 2}*\sqrt{x})/(b^4*x - 2*b^3), (6*(b*x - 2)*\sqrt{b}*\arctan(\sqrt{-b*x + 2}/(\sqrt{b}*\sqrt{x}))) + (b^2*x - 6*b)*\sqrt{-b*x + 2}*\sqrt{x})/(b^4*x - 2*b^3)]$

giac [B] time = 10.41, size = 119, normalized size = 1.83

$$\frac{\left(\frac{3 \log\left(\left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b}\right)^2\right)}{\sqrt{-b}} - \frac{\sqrt{(bx-2)b+2b} \sqrt{-bx+2}}{b} + \frac{16 \sqrt{-b}}{\left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b}\right)^2 - 2b} \right) |b|}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+2)^(3/2),x, algorithm="giac")

[Out] $-(3*\log((\sqrt{-b*x + 2}*\sqrt{-b} - \sqrt{((b*x - 2)*b + 2*b)})^2)/\sqrt{-b} - \sqrt{((b*x - 2)*b + 2*b)*\sqrt{-b*x + 2}}/b + 16*\sqrt{-b}/((\sqrt{-b*x + 2}*\sqrt{-b} - \sqrt{((b*x - 2)*b + 2*b)})^2 - 2*b))*\text{abs}(b)/b^3$

maple [B] time = 0.03, size = 133, normalized size = 2.05

$$\frac{\left(\frac{3 \arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{\frac{5}{b^2}} + \frac{4\sqrt{-\left(x-\frac{2}{b}\right)^2 b-2x+\frac{4}{b}}}{\left(x-\frac{2}{b}\right)b^3} \right) \sqrt{(-bx+2)x}}{\sqrt{-bx+2} \sqrt{x}} - \frac{(bx-2)\sqrt{(-bx+2)x} \sqrt{x}}{\sqrt{-(bx-2)x} \sqrt{-bx+2} b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(-b*x+2)^(3/2),x)

[Out] $-1/b^2*(b*x-2)*x^{(1/2)/(-b*x-2)*x^{(1/2)}*((-b*x+2)*x)^{(1/2)/(-b*x+2)^{(1/2)}} - (3/b^{(5/2)}*\arctan((x-1/b)/(-b*x^2+2*x)^{(1/2)}*b^{(1/2)})+4/b^3/(x-2/b)*(-(x-2)/b)^2*b-2*x+4/b)^{(1/2)}*((-b*x+2)*x)^{(1/2)/(-b*x+2)^{(1/2)}/x^{(1/2)}}$

maxima [A] time = 3.00, size = 71, normalized size = 1.09

$$\frac{2\left(2b - \frac{3(bx-2)}{x}\right)}{\frac{\sqrt{-bx+2} b^3}{\sqrt{x}} + \frac{(-bx+2)^3 b^2}{x^2}} + \frac{6 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b} \sqrt{x}}\right)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+2)^(3/2),x, algorithm="maxima")

[Out] 2*(2*b - 3*(b*x - 2)/x)/(sqrt(-b*x + 2)*b^3/sqrt(x) + (-b*x + 2)^(3/2)*b^2/x^(3/2)) + 6*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/b^(5/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^{3/2}}{(2 - bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(2 - b*x)^(3/2), x)

[Out] int(x^(3/2)/(2 - b*x)^(3/2), x)

sympy [A] time = 3.20, size = 128, normalized size = 1.97

$$\begin{cases} \frac{ix^{\frac{3}{2}}}{b\sqrt{bx-2}} - \frac{6i\sqrt{x}}{b^2\sqrt{bx-2}} + \frac{6i\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{5}{2}}} & \text{for } \frac{|bx|}{2} > 1 \\ -\frac{x^{\frac{3}{2}}}{b\sqrt{-bx+2}} + \frac{6\sqrt{x}}{b^2\sqrt{-bx+2}} - \frac{6\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{5}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)/(-b*x+2)**(3/2),x)

[Out] Piecewise((I*x**(3/2)/(b*sqrt(b*x - 2)) - 6*I*sqrt(x)/(b**2*sqrt(b*x - 2)) + 6*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(5/2), Abs(b*x)/2 > 1), (-x**(3/2)/(b*sqrt(-b*x + 2)) + 6*sqrt(x)/(b**2*sqrt(-b*x + 2)) - 6*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(5/2), True))

$$3.637 \quad \int \frac{\sqrt{x}}{(2-bx)^{3/2}} dx$$

Optimal. Leaf size=45

$$\frac{2\sqrt{x}}{b\sqrt{2-bx}} - \frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}$$

[Out] $-2*\arcsin(1/2*b^{(1/2)*x^{(1/2)}*2^{(1/2)})/b^{(3/2)}+2*x^{(1/2)}/b/(-b*x+2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {47, 54, 216}

$$\frac{2\sqrt{x}}{b\sqrt{2-bx}} - \frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(2 - b*x)^(3/2), x]

[Out] $(2*\text{Sqrt}[x])/(b*\text{Sqrt}[2 - b*x]) - (2*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/b^{(3/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] :> Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{x}}{(2-bx)^{3/2}} dx &= \frac{2\sqrt{x}}{b\sqrt{2-bx}} - \frac{\int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx}{b} \\ &= \frac{2\sqrt{x}}{b\sqrt{2-bx}} - \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right)}{b} \\ &= \frac{2\sqrt{x}}{b\sqrt{2-bx}} - \frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.04, size = 45, normalized size = 1.00

$$\frac{2\sqrt{x}}{b\sqrt{2-bx}} - \frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(2 - b*x)^(3/2), x]

[Out] (2*Sqrt[x])/(b*Sqrt[2 - b*x]) - (2*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(3/2)

fricas [A] time = 0.46, size = 122, normalized size = 2.71

$$\left[\frac{(bx-2)\sqrt{-b} \log(-bx - \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1) + 2\sqrt{-bx+2}b\sqrt{x}}{b^3x - 2b^2}, \frac{2\left((bx-2)\sqrt{b} \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) - \sqrt{-bx}\right)}{b^3x - 2b^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+2)^(3/2), x, algorithm="fricas")

[Out] [-(b*x - 2)*sqrt(-b)*log(-b*x - sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1) + 2*sqrt(-b*x + 2)*b*sqrt(x)]/(b^3*x - 2*b^2), 2*((b*x - 2)*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) - sqrt(-b*x + 2)*b*sqrt(x))/(b^3*x - 2*b^2)]

giac [B] time = 10.06, size = 92, normalized size = 2.04

$$\frac{\left(\frac{\log\left(\left(\sqrt{-bx+2}\sqrt{-b}-\sqrt{(bx-2)b+2b}\right)^2\right)}{\sqrt{-b}} + \frac{8\sqrt{-b}}{\left(\sqrt{-bx+2}\sqrt{-b}-\sqrt{(bx-2)b+2b}\right)^2-2b}\right)|b|}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+2)^(3/2),x, algorithm="giac")

[Out] $-\frac{(\log(\sqrt{-bx+2})\sqrt{-b} - \sqrt{(bx-2)b+2b})^2/\sqrt{-b} + 8\sqrt{-b})/((\sqrt{-bx+2})\sqrt{-b} - \sqrt{(bx-2)b+2b})^2 - 2b)}{b^2}$

maple [A] time = 0.05, size = 67, normalized size = 1.49

$$-\frac{2\left(\frac{\sqrt{\pi}\sqrt{2}(-b)^{\frac{3}{2}}\sqrt{x}}{2\sqrt{-\frac{bx}{2}+1}b} - \frac{\sqrt{\pi}(-b)^{\frac{3}{2}}\arcsin\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}}\right)}{\sqrt{-b}\sqrt{\pi}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(-b*x+2)^(3/2),x)

[Out] $-2/(-b)^{(1/2)}/\text{Pi}^{(1/2)}/b*(1/2*\text{Pi}^{(1/2)}*x^{(1/2)}*2^{(1/2)}*(-b)^{(3/2)}/b/(-1/2*b*x+1)^{(1/2)}-\text{Pi}^{(1/2)}*(-b)^{(3/2)}/b^{(3/2)}*\arcsin(1/2*2^{(1/2)}*b^{(1/2)}*x^{(1/2)})$

maxima [A] time = 2.98, size = 38, normalized size = 0.84

$$\frac{2\arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^{\frac{3}{2}}} + \frac{2\sqrt{x}}{\sqrt{-bx+2}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+2)^(3/2),x, algorithm="maxima")

[Out] $2*\arctan(\sqrt{-bx+2}/(\sqrt{b}*\sqrt{x}))/b^{(3/2)} + 2*\sqrt{x}/(\sqrt{-bx+2})*b$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{x}}{(2-bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(2-b*x)^(3/2),x)

[Out] int(x^(1/2)/(2-b*x)^(3/2), x)

sympy [A] time = 1.69, size = 92, normalized size = 2.04

$$\left\{ \begin{array}{ll} -\frac{2i\sqrt{x}}{b\sqrt{bx-2}} + \frac{2i\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}} & \text{for } \frac{|bx|}{2} > 1 \\ \frac{2\sqrt{x}}{b\sqrt{-bx+2}} - \frac{2\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b^{\frac{3}{2}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(1/2)/(-b*x+2)**(3/2), x)

[Out] Piecewise((-2*I*sqrt(x)/(b*sqrt(b*x - 2)) + 2*I*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2), Abs(b*x)/2 > 1), (2*sqrt(x)/(b*sqrt(-b*x + 2)) - 2*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/b**(3/2), True))

$$3.638 \quad \int \frac{1}{\sqrt{x}(2-bx)^{3/2}} dx$$

Optimal. Leaf size=16

$$\frac{\sqrt{x}}{\sqrt{2-bx}}$$

[Out] $x^{(1/2)/(-b*x+2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {37}

$$\frac{\sqrt{x}}{\sqrt{2-bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(2 - b*x)^(3/2)),x]

[Out] Sqrt[x]/Sqrt[2 - b*x]

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt{x}(2-bx)^{3/2}} dx = \frac{\sqrt{x}}{\sqrt{2-bx}}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$\frac{\sqrt{x}}{\sqrt{2-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(2 - b*x)^(3/2)),x]

[Out] Sqrt[x]/Sqrt[2 - b*x]

fricas [A] time = 0.42, size = 20, normalized size = 1.25

$$-\frac{\sqrt{-bx+2}\sqrt{x}}{bx-2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(3/2)/x^(1/2),x, algorithm="fricas")

[Out] -sqrt(-b*x + 2)*sqrt(x)/(b*x - 2)

giac [B] time = 1.03, size = 50, normalized size = 3.12

$$-\frac{4\sqrt{-b}b}{\left(\left(\sqrt{-bx+2}\sqrt{-b}-\sqrt{(bx-2)b+2b}\right)^2-2b\right)|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(3/2)/x^(1/2),x, algorithm="giac")

[Out] -4*sqrt(-b)*b/(((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2 - 2*b)*abs(b))

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{\sqrt{x}}{\sqrt{-bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x+2)^(3/2)/x^(1/2),x)

[Out] x^(1/2)/(-b*x+2)^(1/2)

maxima [A] time = 1.27, size = 12, normalized size = 0.75

$$\frac{\sqrt{x}}{\sqrt{-bx+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(3/2)/x^(1/2),x, algorithm="maxima")

[Out] sqrt(x)/sqrt(-b*x + 2)

mupad [B] time = 0.30, size = 12, normalized size = 0.75

$$\frac{\sqrt{x}}{\sqrt{2 - bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(2 - b*x)^(3/2)), x)`

[Out] `x^(1/2)/(2 - b*x)^(1/2)`

sympy [A] time = 0.93, size = 39, normalized size = 2.44

$$\begin{cases} \frac{1}{\sqrt{b} \sqrt{-1 + \frac{2}{bx}}} & \text{for } \frac{2}{|bx|} > 1 \\ -\frac{i}{\sqrt{b} \sqrt{1 - \frac{2}{bx}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x+2)**(3/2)/x**(1/2), x)`

[Out] `Piecewise((1/(sqrt(b)*sqrt(-1 + 2/(b*x))), 2/Abs(b*x) > 1), (-I/(sqrt(b)*sqrt(1 - 2/(b*x))), True))`

$$3.639 \quad \int \frac{1}{x^{3/2}(2-bx)^{3/2}} dx$$

Optimal. Leaf size=34

$$\frac{1}{\sqrt{x}\sqrt{2-bx}} - \frac{\sqrt{2-bx}}{\sqrt{x}}$$

[Out] $1/x^{(1/2)/(-b*x+2)^{(1/2)}-(-b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$\frac{1}{\sqrt{x}\sqrt{2-bx}} - \frac{\sqrt{2-bx}}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(2 - b*x)^(3/2)),x]

[Out] 1/(Sqrt[x]*Sqrt[2 - b*x]) - Sqrt[2 - b*x]/Sqrt[x]

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{x^{3/2}(2-bx)^{3/2}} dx = \frac{1}{\sqrt{x}\sqrt{2-bx}} + \int \frac{1}{x^{3/2}\sqrt{2-bx}} dx$$

$$= \frac{1}{\sqrt{x}\sqrt{2-bx}} - \frac{\sqrt{2-bx}}{\sqrt{x}}$$

Mathematica [A] time = 0.01, size = 21, normalized size = 0.62

$$\frac{bx - 1}{\sqrt{x}\sqrt{2 - bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(2 - b*x)^(3/2)), x]

[Out] (-1 + b*x)/(Sqrt[x]*Sqrt[2 - b*x])

fricas [A] time = 0.41, size = 29, normalized size = 0.85

$$\frac{(bx - 1)\sqrt{-bx + 2}\sqrt{x}}{bx^2 - 2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+2)^(3/2), x, algorithm="fricas")

[Out] -(b*x - 1)*sqrt(-b*x + 2)*sqrt(x)/(b*x^2 - 2*x)

giac [B] time = 1.09, size = 83, normalized size = 2.44

$$\frac{\sqrt{-bx + 2} b^2}{2\sqrt{(bx - 2)b + 2b}|b|} - \frac{2\sqrt{-b} b^2}{\left(\left(\sqrt{-bx + 2}\sqrt{-b} - \sqrt{(bx - 2)b + 2b}\right)^2 - 2b\right)|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+2)^(3/2), x, algorithm="giac")

[Out] -1/2*sqrt(-b*x + 2)*b^2/(sqrt((b*x - 2)*b + 2*b)*abs(b)) - 2*sqrt(-b)*b^2/((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2 - 2*b)*abs(b))

maple [A] time = 0.00, size = 18, normalized size = 0.53

$$\frac{bx - 1}{\sqrt{-bx + 2}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(3/2)/(-b*x+2)^(3/2),x)`

[Out] $(b*x-1)/x^{(1/2)/(-b*x+2)^{(1/2)}$

maxima [A] time = 1.26, size = 28, normalized size = 0.82

$$\frac{b\sqrt{x}}{2\sqrt{-bx+2}} - \frac{\sqrt{-bx+2}}{2\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(-b*x+2)^(3/2),x, algorithm="maxima")`

[Out] $1/2*b*\text{sqrt}(x)/\text{sqrt}(-b*x + 2) - 1/2*\text{sqrt}(-b*x + 2)/\text{sqrt}(x)$

mupad [B] time = 0.32, size = 27, normalized size = 0.79

$$\frac{b\sqrt{x}}{\sqrt{2-bx}} - \frac{1}{\sqrt{x}\sqrt{2-bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(2 - b*x)^(3/2)),x)`

[Out] $(b*x^{(1/2)})/(2 - b*x)^{(1/2)} - 1/(x^{(1/2)}*(2 - b*x)^{(1/2)})$

sympy [A] time = 1.61, size = 90, normalized size = 2.65

$$\left\{ \begin{array}{ll} \frac{\sqrt{b}}{\sqrt{-1+\frac{2}{bx}}} - \frac{1}{\sqrt{b}x\sqrt{-1+\frac{2}{bx}}} & \text{for } \frac{2}{|bx|} > 1 \\ \frac{ib^{\frac{5}{2}}x\sqrt{1-\frac{2}{bx}}}{-b^2x+2b} - \frac{ib^{\frac{3}{2}}\sqrt{1-\frac{2}{bx}}}{-b^2x+2b} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(3/2)/(-b*x+2)**(3/2),x)`

[Out] `Piecewise((sqrt(b)/sqrt(-1 + 2/(b*x)) - 1/(sqrt(b)*x*sqrt(-1 + 2/(b*x))), 2/Abs(b*x) > 1), (I*b**(5/2)*x*sqrt(1 - 2/(b*x))/(-b**2*x + 2*b) - I*b**(3/2)*sqrt(1 - 2/(b*x))/(-b**2*x + 2*b), True))`

$$3.640 \quad \int \frac{1}{x^{5/2}(2-bx)^{3/2}} dx$$

Optimal. Leaf size=56

$$-\frac{2\sqrt{2-bx}}{3x^{3/2}} + \frac{1}{x^{3/2}\sqrt{2-bx}} - \frac{2b\sqrt{2-bx}}{3\sqrt{x}}$$

[Out] $1/x^{(3/2)/(-b*x+2)^{(1/2)}-2/3*(-b*x+2)^{(1/2)}/x^{(3/2)}-2/3*b*(-b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{2\sqrt{2-bx}}{3x^{3/2}} + \frac{1}{x^{3/2}\sqrt{2-bx}} - \frac{2b\sqrt{2-bx}}{3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(2 - b*x)^(3/2)),x]

[Out] $1/(x^{(3/2)*\text{Sqrt}[2 - b*x])} - (2*\text{Sqrt}[2 - b*x])/(3*x^{(3/2)}) - (2*b*\text{Sqrt}[2 - b*x])/(3*\text{Sqrt}[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{5/2}(2-bx)^{3/2}} dx &= \frac{1}{x^{3/2}\sqrt{2-bx}} + 2 \int \frac{1}{x^{5/2}\sqrt{2-bx}} dx \\
&= \frac{1}{x^{3/2}\sqrt{2-bx}} - \frac{2\sqrt{2-bx}}{3x^{3/2}} + \frac{1}{3}(2b) \int \frac{1}{x^{3/2}\sqrt{2-bx}} dx \\
&= \frac{1}{x^{3/2}\sqrt{2-bx}} - \frac{2\sqrt{2-bx}}{3x^{3/2}} - \frac{2b\sqrt{2-bx}}{3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.59

$$\frac{2b^2x^2 - 2bx - 1}{3x^{3/2}\sqrt{2-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(2 - b*x)^(3/2)),x]

[Out] (-1 - 2*b*x + 2*b^2*x^2)/(3*x^(3/2)*Sqrt[2 - b*x])

fricas [A] time = 0.41, size = 40, normalized size = 0.71

$$-\frac{(2b^2x^2 - 2bx - 1)\sqrt{-bx + 2}\sqrt{x}}{3(bx^3 - 2x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+2)^(3/2),x, algorithm="fricas")

[Out] -1/3*(2*b^2*x^2 - 2*b*x - 1)*sqrt(-b*x + 2)*sqrt(x)/(b*x^3 - 2*x^2)

giac [B] time = 1.17, size = 96, normalized size = 1.71

$$-\frac{\sqrt{-b}b^3}{\left(\left(\sqrt{-bx+2}\sqrt{-b} - \sqrt{(bx-2)b+2b}\right)^2 - 2b\right)|b|} - \frac{(5(bx-2)b^2|b| + 12b^2|b|)\sqrt{-bx+2}}{12((bx-2)b+2b)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+2)^(3/2),x, algorithm="giac")

[Out] -sqrt(-b)*b^3/(((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2 - 2*b)*abs(b)) - 1/12*(5*(b*x - 2)*b^2*abs(b) + 12*b^2*abs(b))*sqrt(-b*x + 2)/((b*x - 2)*b + 2*b)^(3/2)

maple [A] time = 0.01, size = 28, normalized size = 0.50

$$\frac{2b^2x^2 - 2bx - 1}{3\sqrt{-bx + 2} x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(5/2)/(-b*x+2)^(3/2), x)

[Out] 1/3*(2*b^2*x^2-2*b*x-1)/x^(3/2)/(-b*x+2)^(1/2)

maxima [A] time = 1.28, size = 44, normalized size = 0.79

$$\frac{b^2\sqrt{x}}{4\sqrt{-bx+2}} - \frac{\sqrt{-bx+2}b}{2\sqrt{x}} - \frac{(-bx+2)^{\frac{3}{2}}}{12x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+2)^(3/2), x, algorithm="maxima")

[Out] 1/4*b^2*sqrt(x)/sqrt(-b*x + 2) - 1/2*sqrt(-b*x + 2)*b/sqrt(x) - 1/12*(-b*x + 2)^(3/2)/x^(3/2)

mupad [B] time = 0.36, size = 38, normalized size = 0.68

$$\frac{\sqrt{2-bx} \left(\frac{2x}{3} - \frac{2bx^2}{3} + \frac{1}{3b} \right)}{x^{5/2} - \frac{2x^{3/2}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(5/2)*(2 - b*x)^(3/2)), x)

[Out] ((2 - b*x)^(1/2)*((2*x)/3 - (2*b*x^2)/3 + 1/(3*b)))/(x^(5/2) - (2*x^(3/2))/b)

sympy [B] time = 4.29, size = 354, normalized size = 6.32

$$\left\{ \begin{array}{l} \frac{2b^{\frac{15}{2}}x^3\sqrt{-1+\frac{2}{bx}}}{-3b^6x^3+12b^5x^2-12b^4x} - \frac{6b^{\frac{13}{2}}x^2\sqrt{-1+\frac{2}{bx}}}{-3b^6x^3+12b^5x^2-12b^4x} + \frac{3b^{\frac{11}{2}}x\sqrt{-1+\frac{2}{bx}}}{-3b^6x^3+12b^5x^2-12b^4x} + \frac{2b^{\frac{9}{2}}\sqrt{-1+\frac{2}{bx}}}{-3b^6x^3+12b^5x^2-12b^4x} \quad \text{for } \frac{2}{|bx|} > 1 \\ \frac{2ib^{\frac{15}{2}}x^3\sqrt{1-\frac{2}{bx}}}{-3b^6x^3+12b^5x^2-12b^4x} - \frac{6ib^{\frac{13}{2}}x^2\sqrt{1-\frac{2}{bx}}}{-3b^6x^3+12b^5x^2-12b^4x} + \frac{3ib^{\frac{11}{2}}x\sqrt{1-\frac{2}{bx}}}{-3b^6x^3+12b^5x^2-12b^4x} + \frac{2ib^{\frac{9}{2}}\sqrt{1-\frac{2}{bx}}}{-3b^6x^3+12b^5x^2-12b^4x} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(5/2)/(-b*x+2)**(3/2),x)

[Out] Piecewise((2*b**(15/2)*x**3*sqrt(-1 + 2/(b*x))/(-3*b**6*x**3 + 12*b**5*x**2 - 12*b**4*x) - 6*b**(13/2)*x**2*sqrt(-1 + 2/(b*x))/(-3*b**6*x**3 + 12*b**5*x**2 - 12*b**4*x) + 3*b**(11/2)*x*sqrt(-1 + 2/(b*x))/(-3*b**6*x**3 + 12*b**5*x**2 - 12*b**4*x) + 2*b**(9/2)*sqrt(-1 + 2/(b*x))/(-3*b**6*x**3 + 12*b**5*x**2 - 12*b**4*x), 2/Abs(b*x) > 1), (2*I*b**(15/2)*x**3*sqrt(1 - 2/(b*x))/(-3*b**6*x**3 + 12*b**5*x**2 - 12*b**4*x) - 6*I*b**(13/2)*x**2*sqrt(1 - 2/(b*x))/(-3*b**6*x**3 + 12*b**5*x**2 - 12*b**4*x) + 3*I*b**(11/2)*x*sqrt(1 - 2/(b*x))/(-3*b**6*x**3 + 12*b**5*x**2 - 12*b**4*x) + 2*I*b**(9/2)*sqrt(1 - 2/(b*x))/(-3*b**6*x**3 + 12*b**5*x**2 - 12*b**4*x), True))

$$3.641 \quad \int \frac{x^{5/2}}{(2-bx)^{5/2}} dx$$

Optimal. Leaf size=89

$$\frac{10 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} - \frac{5\sqrt{x}\sqrt{2-bx}}{b^3} - \frac{10x^{3/2}}{3b^2\sqrt{2-bx}} + \frac{2x^{5/2}}{3b(2-bx)^{3/2}}$$

[Out] $2/3*x^{(5/2)}/b/(-b*x+2)^{(3/2)}+10*\arcsin(1/2*b^{(1/2)}*x^{(1/2)}*2^{(1/2)})/b^{(7/2)}$
 $-10/3*x^{(3/2)}/b^2/(-b*x+2)^{(1/2)}-5*x^{(1/2)}*(-b*x+2)^{(1/2)}/b^3$

Rubi [A] time = 0.02, antiderivative size = 89, normalized size of antiderivative = 1.00,
 number of steps used = 5, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} =$
 0.250, Rules used = {47, 50, 54, 216}

$$-\frac{10x^{3/2}}{3b^2\sqrt{2-bx}} - \frac{5\sqrt{x}\sqrt{2-bx}}{b^3} + \frac{10 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}} + \frac{2x^{5/2}}{3b(2-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[x^(5/2)/(2 - b*x)^(5/2), x]

[Out] $(2*x^{(5/2)})/(3*b*(2 - b*x)^{(3/2)}) - (10*x^{(3/2)})/(3*b^2*\text{Sqrt}[2 - b*x]) - (5$
 $*\text{Sqrt}[x]*\text{Sqrt}[2 - b*x])/b^3 + (10*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/b^{(7/2)}$
 $)$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 ((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
 nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
 NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
 rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
 & IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 ((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
 (b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
 c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
 [m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
 + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/2}}{(2-bx)^{5/2}} dx &= \frac{2x^{5/2}}{3b(2-bx)^{3/2}} - \frac{5 \int \frac{x^{3/2}}{(2-bx)^{3/2}} dx}{3b} \\
&= \frac{2x^{5/2}}{3b(2-bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{2-bx}} + \frac{5 \int \frac{\sqrt{x}}{\sqrt{2-bx}} dx}{b^2} \\
&= \frac{2x^{5/2}}{3b(2-bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{2-bx}} - \frac{5\sqrt{x}\sqrt{2-bx}}{b^3} + \frac{5 \int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx}{b^3} \\
&= \frac{2x^{5/2}}{3b(2-bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{2-bx}} - \frac{5\sqrt{x}\sqrt{2-bx}}{b^3} + \frac{10 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right)}{b^3} \\
&= \frac{2x^{5/2}}{3b(2-bx)^{3/2}} - \frac{10x^{3/2}}{3b^2\sqrt{2-bx}} - \frac{5\sqrt{x}\sqrt{2-bx}}{b^3} + \frac{10 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 30, normalized size = 0.34

$$\frac{x^{7/2} {}_2F_1\left(\frac{5}{2}, \frac{7}{2}; \frac{9}{2}; \frac{bx}{2}\right)}{14\sqrt{2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^(5/2)/(2 - b*x)^(5/2), x]
```

```
[Out] (x^(7/2)*Hypergeometric2F1[5/2, 7/2, 9/2, (b*x)/2])/(14*Sqrt[2])
```

fricas [A] time = 0.47, size = 187, normalized size = 2.10

$$\left[\frac{15(b^2x^2 - 4bx + 4)\sqrt{-b} \log(-bx + \sqrt{-bx+2}\sqrt{-b}\sqrt{x} + 1) + (3b^3x^2 - 40b^2x + 60b)\sqrt{-bx+2}\sqrt{x}}{3(b^6x^2 - 4b^5x + 4b^4)}, - \frac{30(b^2x^2 - 4bx + 4)\sqrt{-b}}{3(b^6x^2 - 4b^5x + 4b^4)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+2)^(5/2),x, algorithm="fricas")

[Out] [-1/3*(15*(b^2*x^2 - 4*b*x + 4)*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1) + (3*b^3*x^2 - 40*b^2*x + 60*b)*sqrt(-b*x + 2)*sqrt(x))/(b^6*x^2 - 4*b^5*x + 4*b^4), -1/3*(30*(b^2*x^2 - 4*b*x + 4)*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) + (3*b^3*x^2 - 40*b^2*x + 60*b)*sqrt(-b*x + 2)*sqrt(x))/(b^6*x^2 - 4*b^5*x + 4*b^4)]

giac [B] time = 10.72, size = 200, normalized size = 2.25

$$\frac{\left(\frac{15 \log\left(\left(\sqrt{-bx+2}\sqrt{-b}-\sqrt{(bx-2)b+2b}\right)^2\right)}{\sqrt{-b}b^2} - \frac{3\sqrt{(bx-2)b+2b}\sqrt{-bx+2}}{b^3} - \frac{16\left(9\left(\sqrt{-bx+2}\sqrt{-b}-\sqrt{(bx-2)b+2b}\right)^4 - 24\left(\sqrt{-bx+2}\sqrt{-b}-\sqrt{(bx-2)b+2b}\right)^2 - 2b\right)^3\sqrt{-b}b}{\left(\left(\sqrt{-bx+2}\sqrt{-b}-\sqrt{(bx-2)b+2b}\right)^2 - 2b\right)^3\sqrt{-b}b} \right)}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/2)/(-b*x+2)^(5/2),x, algorithm="giac")

[Out] 1/3*(15*log((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2)/(sqrt(-b)*b^2) - 3*sqrt((b*x - 2)*b + 2*b)*sqrt(-b*x + 2)/b^3 - 16*(9*(sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^4 - 24*(sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2*b + 28*b^2)/(((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2 - 2*b)^3*sqrt(-b)*b)*abs(b)/b^2

maple [B] time = 0.04, size = 168, normalized size = 1.89

$$\frac{\left(\frac{5 \arctan\left(\frac{\left(x-\frac{1}{b}\right)\sqrt{b}}{\sqrt{-bx^2+2x}}\right)}{\frac{7}{b^2}} + \frac{28\sqrt{\left(x-\frac{2}{b}\right)^2 b-2x+\frac{4}{b}}}{3\left(x-\frac{2}{b}\right)b^4} + \frac{8\sqrt{\left(x-\frac{2}{b}\right)^2 b-2x+\frac{4}{b}}}{3\left(x-\frac{2}{b}\right)b^5} \right) \sqrt{(-bx+2)x}}{\sqrt{-bx+2}\sqrt{x}} + \frac{(bx-2)\sqrt{(-bx+2)x}\sqrt{x}}{\sqrt{-(bx-2)x}\sqrt{-bx+2}b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/2)/(-b*x+2)^(5/2),x)

[Out] $\frac{1}{b^3} \frac{(bx-2)x^{1/2}}{(-bx-2)x^{1/2}} \frac{(-bx+2)x^{1/2}}{(-bx+2)^{1/2}} + \frac{5}{b^{7/2}} \arctan\left(\frac{x-1/b}{(-bx^2+2x)^{1/2}b^{1/2}}\right) + \frac{8}{3} \frac{1}{b^5} \frac{(x-2/b)^2}{(-bx+2)^{1/2}} + \frac{28}{3} \frac{1}{b^4} \frac{(x-2/b)^2}{(-bx+2)^{1/2}} \frac{1}{x^{1/2}}$

maxima [A] time = 2.99, size = 86, normalized size = 0.97

$$\frac{2 \left(2b^2 + \frac{10(bx-2)b}{x} - \frac{15(bx-2)^2}{x^2} \right)}{3 \left(\frac{(-bx+2)^3 b^4}{x^3} + \frac{(-bx+2)^5 b^3}{x^5} \right)} - \frac{10 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right)}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/2)/(-b*x+2)^(5/2),x, algorithm="maxima")`

[Out] $\frac{2}{3} \frac{(2b^2 + 10(bx-2)b/x - 15(bx-2)^2/x^2)}{(-bx+2)^{3/2}b^4/x^{3/2}} + \frac{(-bx+2)^{5/2}b^3/x^{5/2}}{(-bx+2)^{3/2}b^4/x^{3/2}} - 10 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b}\sqrt{x}}\right) / b^{7/2}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{5/2}}{(2-bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/2)/(2 - b*x)^(5/2),x)`

[Out] `int(x^(5/2)/(2 - b*x)^(5/2), x)`

sympy [B] time = 6.80, size = 753, normalized size = 8.46

$$\left\{ \begin{array}{l} -\frac{3ib^{\frac{23}{2}}x^{15}}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{bx-2}-6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{bx-2}} + \frac{40ib^{\frac{21}{2}}x^{14}}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{bx-2}-6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{bx-2}} - \frac{60ib^{\frac{19}{2}}x^{13}}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{bx-2}-6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{bx-2}} - \frac{30ib^{10}x^{\frac{27}{2}}\sqrt{bx-2} \operatorname{acosh}\left(\frac{\sqrt{2}x}{\sqrt{bx-2}}\right)}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{bx-2}-6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{bx-2}} \\ \frac{3ib^{\frac{23}{2}}x^{15}}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{-bx+2}-6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{-bx+2}} - \frac{40ib^{\frac{21}{2}}x^{14}}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{-bx+2}-6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{-bx+2}} + \frac{60ib^{\frac{19}{2}}x^{13}}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{-bx+2}-6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{-bx+2}} + \frac{30ib^{10}x^{\frac{27}{2}}\sqrt{-bx+2} \operatorname{acosh}\left(\frac{\sqrt{2}x}{\sqrt{-bx+2}}\right)}{3b^{\frac{27}{2}}x^{\frac{27}{2}}\sqrt{-bx+2}-6b^{\frac{25}{2}}x^{\frac{25}{2}}\sqrt{-bx+2}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/2)/(-b*x+2)**(5/2),x)`

[Out] `Piecewise((-3*I*b**(23/2)*x**15/(3*b**(27/2)*x**(27/2)*sqrt(b*x - 2) - 6*b*(25/2)*x**(25/2)*sqrt(b*x - 2)) + 40*I*b**(21/2)*x**14/(3*b**(27/2)*x**(27/2)*sqrt(b*x - 2) - 6*b*(25/2)*x**(25/2)*sqrt(b*x - 2)) - 60*I*b**(19/2)*x**13/(3*b**(27/2)*x**(27/2)*sqrt(b*x - 2) - 6*b*(25/2)*x**(25/2)*sqrt(b*x - 2)) - 30*I*b**10*x**(27/2)*sqrt(b*x - 2)*acosh(sqrt(2)*x/sqrt(b*x - 2))/(3*b**(27/2)*x**(27/2)*sqrt(b*x - 2) - 6*b*(25/2)*x**(25/2)*sqrt(b*x - 2)), (-3*I*b**(23/2)*x**15/(3*b**(27/2)*x**(27/2)*sqrt(-b*x + 2) - 6*b*(25/2)*x**(25/2)*sqrt(-b*x + 2)) + 40*I*b**(21/2)*x**14/(3*b**(27/2)*x**(27/2)*sqrt(-b*x + 2) - 6*b*(25/2)*x**(25/2)*sqrt(-b*x + 2)) - 60*I*b**(19/2)*x**13/(3*b**(27/2)*x**(27/2)*sqrt(-b*x + 2) - 6*b*(25/2)*x**(25/2)*sqrt(-b*x + 2)) + 30*I*b**10*x**(27/2)*sqrt(-b*x + 2)*acosh(sqrt(2)*x/sqrt(-b*x + 2))/(3*b**(27/2)*x**(27/2)*sqrt(-b*x + 2) - 6*b*(25/2)*x**(25/2)*sqrt(-b*x + 2))`

```

/2)*sqrt(b*x - 2) - 6*b**(25/2)*x**(25/2)*sqrt(b*x - 2)) - 60*I*b**(19/2)*x
**13/(3*b**(27/2)*x**(27/2)*sqrt(b*x - 2) - 6*b**(25/2)*x**(25/2)*sqrt(b*x
- 2)) - 30*I*b**10*x**(27/2)*sqrt(b*x - 2)*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)
/(3*b**(27/2)*x**(27/2)*sqrt(b*x - 2) - 6*b**(25/2)*x**(25/2)*sqrt(b*x - 2)
) + 15*pi*b**10*x**(27/2)*sqrt(b*x - 2)/(3*b**(27/2)*x**(27/2)*sqrt(b*x - 2)
) - 6*b**(25/2)*x**(25/2)*sqrt(b*x - 2)) + 60*I*b**9*x**(25/2)*sqrt(b*x - 2
)*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(3*b**(27/2)*x**(27/2)*sqrt(b*x - 2) - 6
*b**(25/2)*x**(25/2)*sqrt(b*x - 2)) - 30*pi*b**9*x**(25/2)*sqrt(b*x - 2)/(3
*b**(27/2)*x**(27/2)*sqrt(b*x - 2) - 6*b**(25/2)*x**(25/2)*sqrt(b*x - 2)),
Abs(b*x)/2 > 1), (3*b**(23/2)*x**15/(3*b**(27/2)*x**(27/2)*sqrt(-b*x + 2) -
6*b**(25/2)*x**(25/2)*sqrt(-b*x + 2)) - 40*b**(21/2)*x**14/(3*b**(27/2)*x*
*(27/2)*sqrt(-b*x + 2) - 6*b**(25/2)*x**(25/2)*sqrt(-b*x + 2)) + 60*b**(19/
2)*x**13/(3*b**(27/2)*x**(27/2)*sqrt(-b*x + 2) - 6*b**(25/2)*x**(25/2)*sqrt
(-b*x + 2)) + 30*b**10*x**(27/2)*sqrt(-b*x + 2)*asin(sqrt(2)*sqrt(b)*sqrt(x
)/2)/(3*b**(27/2)*x**(27/2)*sqrt(-b*x + 2) - 6*b**(25/2)*x**(25/2)*sqrt(-b*
x + 2)) - 60*b**9*x**(25/2)*sqrt(-b*x + 2)*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/
(3*b**(27/2)*x**(27/2)*sqrt(-b*x + 2) - 6*b**(25/2)*x**(25/2)*sqrt(-b*x + 2
)), True))

```

$$3.642 \quad \int \frac{x^{3/2}}{(2-bx)^{5/2}} dx$$

Optimal. Leaf size=67

$$\frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} - \frac{2\sqrt{x}}{b^2\sqrt{2-bx}} + \frac{2x^{3/2}}{3b(2-bx)^{3/2}}$$

[Out] $2/3*x^{(3/2)}/b/(-b*x+2)^{(3/2)}+2*\arcsin(1/2*b^{(1/2)}*x^{(1/2)*2^{(1/2)}}/b^{(5/2)}-2*x^{(1/2)}/b^2/(-b*x+2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {47, 54, 216}

$$-\frac{2\sqrt{x}}{b^2\sqrt{2-bx}} + \frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{2x^{3/2}}{3b(2-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] `Int[x^(3/2)/(2 - b*x)^(5/2), x]`

[Out] $(2*x^{(3/2)})/(3*b*(2 - b*x)^{(3/2)}) - (2*\text{Sqrt}[x])/(b^2*\text{Sqrt}[2 - b*x]) + (2*\text{ArcSin}[(\text{Sqrt}[b]*\text{Sqrt}[x])/\text{Sqrt}[2]])/b^{(5/2)}$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 54

```
Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dis
t[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x]
/; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]
```

Rule 216

```
Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```


Rubi steps

$$\begin{aligned}
\int \frac{x^{3/2}}{(2-bx)^{5/2}} dx &= \frac{2x^{3/2}}{3b(2-bx)^{3/2}} - \frac{\int \frac{\sqrt{x}}{(2-bx)^{3/2}} dx}{b} \\
&= \frac{2x^{3/2}}{3b(2-bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{2-bx}} + \frac{\int \frac{1}{\sqrt{x}\sqrt{2-bx}} dx}{b^2} \\
&= \frac{2x^{3/2}}{3b(2-bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{2-bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-bx^2}} dx, x, \sqrt{x}\right)}{b^2} \\
&= \frac{2x^{3/2}}{3b(2-bx)^{3/2}} - \frac{2\sqrt{x}}{b^2\sqrt{2-bx}} + \frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.06, size = 53, normalized size = 0.79

$$\frac{2 \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{b^{5/2}} + \frac{4\sqrt{x}(2bx-3)}{3b^2(2-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)/(2 - b*x)^(5/2), x]

[Out] (4*Sqrt[x]*(-3 + 2*b*x))/(3*b^2*(2 - b*x)^(3/2)) + (2*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/b^(5/2)

fricas [A] time = 0.46, size = 173, normalized size = 2.58

$$\left[\frac{3(b^2x^2 - 4bx + 4)\sqrt{-b} \log(-bx + \sqrt{-bx + 2}\sqrt{-b}\sqrt{x} + 1) - 4(2b^2x - 3b)\sqrt{-bx + 2}\sqrt{x}}{3(b^5x^2 - 4b^4x + 4b^3)}, -\frac{2(3(b^2x^2 - 4bx + 4)\sqrt{-b} \log(-bx + \sqrt{-bx + 2}\sqrt{-b}\sqrt{x} + 1) - 4(2b^2x - 3b)\sqrt{-bx + 2}\sqrt{x})}{3(b^5x^2 - 4b^4x + 4b^3)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+2)^(5/2), x, algorithm="fricas")

[Out] [-1/3*(3*(b^2*x^2 - 4*b*x + 4)*sqrt(-b)*log(-b*x + sqrt(-b*x + 2)*sqrt(-b)*sqrt(x) + 1) - 4*(2*b^2*x - 3*b)*sqrt(-b*x + 2)*sqrt(x))/(b^5*x^2 - 4*b^4*x + 4*b^3), -2/3*(3*(b^2*x^2 - 4*b*x + 4)*sqrt(b)*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x))) - 2*(2*b^2*x - 3*b)*sqrt(-b*x + 2)*sqrt(x))/(b^5*x^2 - 4*b^4*x + 4*b^3)]

giac [B] time = 10.63, size = 178, normalized size = 2.66

$$\frac{\left(\frac{3 \log\left(\left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b}\right)^2\right)}{\sqrt{-b}} + \frac{16 \left(3 \left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b}\right)^4 \sqrt{-b} - 6 \left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b}\right)^2 \sqrt{-b} b + 8 \sqrt{-b} b^2\right)}{\left(\left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b}\right)^2 - 2b\right)^3} \right) |b|}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+2)^(5/2),x, algorithm="giac")

[Out] 1/3*(3*log((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2)/sqrt(-b) + 16*(3*(sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^4*sqrt(-b) - 6*(sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2*sqrt(-b)*b + 8*sqrt(-b)*b^2)/((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2 - 2*b)^3)*ab s(b)/b^3

maple [A] time = 0.04, size = 73, normalized size = 1.09

$$\frac{4 \left(-\frac{\sqrt{\pi} \sqrt{2} (-b)^{\frac{5}{2}} (-10bx+15)\sqrt{x}}{20\left(-\frac{bx}{2}+1\right)^{\frac{3}{2}} b^2} + \frac{3\sqrt{\pi} (-b)^{\frac{5}{2}} \arcsin\left(\frac{\sqrt{2} \sqrt{b} \sqrt{x}}{2}\right)}{2b^{\frac{5}{2}}} \right)}{3(-b)^{\frac{3}{2}} \sqrt{\pi} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)/(-b*x+2)^(5/2),x)

[Out] -4/3/(-b)^(3/2)/Pi^(1/2)/b*(-1/20*Pi^(1/2)*x^(1/2)*2^(1/2)*(-b)^(5/2)*(-10*b*x+15)/b^2/(-1/2*b*x+1)^(3/2)+3/2*Pi^(1/2)*(-b)^(5/2)/b^(5/2)*arcsin(1/2*2^(1/2)*b^(1/2)*x^(1/2))

maxima [A] time = 2.92, size = 50, normalized size = 0.75

$$\frac{2 \left(b + \frac{3(bx-2)}{x} \right) x^{\frac{3}{2}}}{3(-bx+2)^{\frac{3}{2}} b^2} - \frac{2 \arctan\left(\frac{\sqrt{-bx+2}}{\sqrt{b} \sqrt{x}}\right)}{b^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)/(-b*x+2)^(5/2),x, algorithm="maxima")

[Out] 2/3*(b + 3*(b*x - 2)/x)*x^(3/2)/((-b*x + 2)^(3/2)*b^2) - 2*arctan(sqrt(-b*x + 2)/(sqrt(b)*sqrt(x)))/b^(5/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^{3/2}}{(2 - bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(3/2)/(2 - b*x)^(5/2), x)`

[Out] `int(x^(3/2)/(2 - b*x)^(5/2), x)`

sympy [B] time = 3.70, size = 649, normalized size = 9.69

$$\left\{ \begin{array}{l} \frac{8ib^{\frac{11}{2}}x^8}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{bx-2}-6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{bx-2}} - \frac{12ib^{\frac{9}{2}}x^7}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{bx-2}-6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{bx-2}} - \frac{6ib^5x^{\frac{15}{2}}\sqrt{bx-2}\operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{bx-2}-6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{bx-2}} + \frac{3\pi b^5x^{\frac{15}{2}}\sqrt{bx-2}}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{bx-2}-6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{bx-2}} \\ - \frac{8b^{\frac{11}{2}}x^8}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{-bx+2}-6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{-bx+2}} + \frac{12b^{\frac{9}{2}}x^7}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{-bx+2}-6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{-bx+2}} + \frac{6b^5x^{\frac{15}{2}}\sqrt{-bx+2}\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{-bx+2}-6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{-bx+2}} - \frac{12b^4x^{\frac{13}{2}}\sqrt{-bx+2}}{3b^{\frac{15}{2}}x^{\frac{15}{2}}\sqrt{-bx+2}-6b^{\frac{13}{2}}x^{\frac{13}{2}}\sqrt{-bx+2}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(3/2)/(-b*x+2)**(5/2), x)`

[Out] `Piecewise((8*I*b**(11/2)*x**8/(3*b**(15/2)*x**(15/2)*sqrt(b*x - 2) - 6*b**(13/2)*x**(13/2)*sqrt(b*x - 2)) - 12*I*b**(9/2)*x**7/(3*b**(15/2)*x**(15/2)*sqrt(b*x - 2) - 6*b**(13/2)*x**(13/2)*sqrt(b*x - 2)) - 6*I*b**5*x**(15/2)*sqrt(b*x - 2)*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(3*b**(15/2)*x**(15/2)*sqrt(b*x - 2) - 6*b**(13/2)*x**(13/2)*sqrt(b*x - 2)) + 3*pi*b**5*x**(15/2)*sqrt(b*x - 2)/(3*b**(15/2)*x**(15/2)*sqrt(b*x - 2) - 6*b**(13/2)*x**(13/2)*sqrt(b*x - 2)) + 12*I*b**4*x**(13/2)*sqrt(b*x - 2)*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/(3*b**(15/2)*x**(15/2)*sqrt(b*x - 2) - 6*b**(13/2)*x**(13/2)*sqrt(b*x - 2)) - 6*pi*b**4*x**(13/2)*sqrt(b*x - 2)/(3*b**(15/2)*x**(15/2)*sqrt(b*x - 2) - 6*b**(13/2)*x**(13/2)*sqrt(b*x - 2)), Abs(b*x)/2 > 1), (-8*b**(11/2)*x**8/(3*b**(15/2)*x**(15/2)*sqrt(-b*x + 2) - 6*b**(13/2)*x**(13/2)*sqrt(-b*x + 2)) + 12*b**(9/2)*x**7/(3*b**(15/2)*x**(15/2)*sqrt(-b*x + 2) - 6*b**(13/2)*x**(13/2)*sqrt(-b*x + 2)) + 6*b**5*x**(15/2)*sqrt(-b*x + 2)*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/(3*b**(15/2)*x**(15/2)*sqrt(-b*x + 2) - 6*b**(13/2)*x**(13/2)*sqrt(-b*x + 2)) - 12*b**4*x**(13/2)*sqrt(-b*x + 2)*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/(3*b**(15/2)*x**(15/2)*sqrt(-b*x + 2) - 6*b**(13/2)*x**(13/2)*sqrt(-b*x + 2)), True))`

$$3.643 \quad \int \frac{\sqrt{x}}{(2-bx)^{5/2}} dx$$

Optimal. Leaf size=19

$$\frac{x^{3/2}}{3(2-bx)^{3/2}}$$

[Out] 1/3*x^(3/2)/(-b*x+2)^(3/2)

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {37}

$$\frac{x^{3/2}}{3(2-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/(2 - b*x)^(5/2), x]

[Out] x^(3/2)/(3*(2 - b*x)^(3/2))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{x}}{(2-bx)^{5/2}} dx = \frac{x^{3/2}}{3(2-bx)^{3/2}}$$

Mathematica [A] time = 0.01, size = 19, normalized size = 1.00

$$\frac{x^{3/2}}{3(2-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/(2 - b*x)^(5/2), x]

[Out] x^(3/2)/(3*(2 - b*x)^(3/2))

fricas [B] time = 0.44, size = 28, normalized size = 1.47

$$\frac{\sqrt{-bx+2} x^{\frac{3}{2}}}{3(b^2x^2 - 4bx + 4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+2)^(5/2),x, algorithm="fricas")

[Out] 1/3*sqrt(-b*x + 2)*x^(3/2)/(b^2*x^2 - 4*b*x + 4)

giac [B] time = 1.25, size = 95, normalized size = 5.00

$$\frac{4 \left(3 \left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b} \right)^4 \sqrt{-b} + 4 \sqrt{-b} b^2 \right) |b|}{3 \left(\left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b} \right)^2 - 2b \right)^3 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+2)^(5/2),x, algorithm="giac")

[Out] 4/3*(3*(sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^4*sqrt(-b) + 4*sqrt(-b)*b^2)*abs(b)/(((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2 - 2*b)^3*b^2)

maple [A] time = 0.00, size = 14, normalized size = 0.74

$$\frac{x^{\frac{3}{2}}}{3(-bx+2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)/(-b*x+2)^(5/2),x)

[Out] 1/3*x^(3/2)/(-b*x+2)^(3/2)

maxima [A] time = 1.38, size = 13, normalized size = 0.68

$$\frac{x^{\frac{3}{2}}}{3(-bx+2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(-b*x+2)^(5/2),x, algorithm="maxima")

[Out] $1/3*x^{(3/2)/(-b*x + 2)^{(3/2)}$

mupad [B] time = 0.23, size = 13, normalized size = 0.68

$$\frac{x^{3/2}}{3(2 - bx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)/(2 - b*x)^(5/2), x)`

[Out] $x^{(3/2)/(3*(2 - b*x)^{(3/2)})}$

sympy [B] time = 1.46, size = 65, normalized size = 3.42

$$\left\{ \begin{array}{ll} \frac{ix^{\frac{3}{2}}}{3bx\sqrt{bx-2}-6\sqrt{bx-2}} & \text{for } \frac{|bx|}{2} > 1 \\ -\frac{x^{\frac{3}{2}}}{3bx\sqrt{-bx+2}-6\sqrt{-bx+2}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)/(-b*x+2)**(5/2), x)`

[Out] `Piecewise((I*x**(3/2)/(3*b*x*sqrt(b*x - 2) - 6*sqrt(b*x - 2)), Abs(b*x)/2 > 1), (-x**(3/2)/(3*b*x*sqrt(-b*x + 2) - 6*sqrt(-b*x + 2)), True))`

$$3.644 \quad \int \frac{1}{\sqrt{x}(2-bx)^{5/2}} dx$$

Optimal. Leaf size=39

$$\frac{\sqrt{x}}{3\sqrt{2-bx}} + \frac{\sqrt{x}}{3(2-bx)^{3/2}}$$

[Out] 1/3*x^(1/2)/(-b*x+2)^(3/2)+1/3*x^(1/2)/(-b*x+2)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$\frac{\sqrt{x}}{3\sqrt{2-bx}} + \frac{\sqrt{x}}{3(2-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*(2 - b*x)^(5/2)),x]

[Out] Sqrt[x]/(3*(2 - b*x)^(3/2)) + Sqrt[x]/(3*Sqrt[2 - b*x])

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{\sqrt{x}(2-bx)^{5/2}} dx = \frac{\sqrt{x}}{3(2-bx)^{3/2}} + \frac{1}{3} \int \frac{1}{\sqrt{x}(2-bx)^{3/2}} dx$$

$$= \frac{\sqrt{x}}{3(2-bx)^{3/2}} + \frac{\sqrt{x}}{3\sqrt{2-bx}}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.62

$$\frac{\sqrt{x}(bx-3)}{3(2-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*(2 - b*x)^(5/2)),x]

[Out] -1/3*(Sqrt[x]*(-3 + b*x))/(2 - b*x)^(3/2)

fricas [A] time = 0.45, size = 33, normalized size = 0.85

$$\frac{(bx-3)\sqrt{-bx+2}\sqrt{x}}{3(b^2x^2-4bx+4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(5/2)/x^(1/2),x, algorithm="fricas")

[Out] -1/3*(b*x - 3)*sqrt(-b*x + 2)*sqrt(x)/(b^2*x^2 - 4*b*x + 4)

giac [B] time = 1.10, size = 90, normalized size = 2.31

$$\frac{8 \left(3 \left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b} \right)^2 - 2b \right) \sqrt{-b} b^2}{3 \left(\left(\sqrt{-bx+2} \sqrt{-b} - \sqrt{(bx-2)b+2b} \right)^2 - 2b \right)^3 |b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(5/2)/x^(1/2),x, algorithm="giac")

[Out] 8/3*(3*(sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2 - 2*b)*sqrt(-b)*b^2/(((sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2 - 2*b)^3*abs(b))

maple [A] time = 0.00, size = 19, normalized size = 0.49

$$-\frac{(bx-3)\sqrt{x}}{3(-bx+2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x+2)^(5/2)/x^(1/2),x)

[Out] -1/3*x^(1/2)*(b*x-3)/(-b*x+2)^(3/2)

maxima [A] time = 1.30, size = 25, normalized size = 0.64

$$\frac{\left(b - \frac{3(bx-2)}{x}\right)x^{\frac{3}{2}}}{6(-bx+2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(5/2)/x^(1/2),x, algorithm="maxima")

[Out] 1/6*(b - 3*(b*x - 2)/x)*x^(3/2)/(-b*x + 2)^(3/2)

mupad [B] time = 0.36, size = 45, normalized size = 1.15

$$\frac{3\sqrt{x}\sqrt{2-bx}-bx^{3/2}\sqrt{2-bx}}{3b^2x^2-12bx+12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/2)*(2-b*x)^(5/2)),x)

[Out] (3*x^(1/2)*(2-b*x)^(1/2)-b*x^(3/2)*(2-b*x)^(1/2))/(3*b^2*x^2-12*b*x+12)

sympy [C] time = 1.91, size = 177, normalized size = 4.54

$$\begin{cases} \frac{ibx}{3ib^{\frac{3}{2}}x\sqrt{-1+\frac{2}{bx}}-6i\sqrt{b}\sqrt{-1+\frac{2}{bx}}} - \frac{3i}{3ib^{\frac{3}{2}}x\sqrt{-1+\frac{2}{bx}}-6i\sqrt{b}\sqrt{-1+\frac{2}{bx}}} & \text{for } \frac{2}{|bx|} > 1 \\ \frac{b^2x}{3ib^{\frac{5}{2}}x\sqrt{1-\frac{2}{bx}}-6ib^{\frac{3}{2}}\sqrt{1-\frac{2}{bx}}} - \frac{3b}{3ib^{\frac{5}{2}}x\sqrt{1-\frac{2}{bx}}-6ib^{\frac{3}{2}}\sqrt{1-\frac{2}{bx}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(-b*x+2)**(5/2)/x**(1/2),x)
```

```
[Out] Piecewise((I*b*x/(3*I*b**(3/2)*x*sqrt(-1 + 2/(b*x)) - 6*I*sqrt(b)*sqrt(-1 + 2/(b*x))) - 3*I/(3*I*b**(3/2)*x*sqrt(-1 + 2/(b*x)) - 6*I*sqrt(b)*sqrt(-1 + 2/(b*x))), 2/Abs(b*x) > 1), (b**2*x/(3*I*b**(5/2)*x*sqrt(1 - 2/(b*x)) - 6*I*b**(3/2)*sqrt(1 - 2/(b*x))) - 3*b/(3*I*b**(5/2)*x*sqrt(1 - 2/(b*x)) - 6*I*b**(3/2)*sqrt(1 - 2/(b*x))), True))
```

$$3.645 \quad \int \frac{1}{x^{3/2}(2-bx)^{5/2}} dx$$

Optimal. Leaf size=58

$$-\frac{2\sqrt{2-bx}}{3\sqrt{x}} + \frac{2}{3\sqrt{x}\sqrt{2-bx}} + \frac{1}{3\sqrt{x}(2-bx)^{3/2}}$$

[Out] 1/3/(-b*x+2)^(3/2)/x^(1/2)+2/3/x^(1/2)/(-b*x+2)^(1/2)-2/3*(-b*x+2)^(1/2)/x^(1/2)

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{2\sqrt{2-bx}}{3\sqrt{x}} + \frac{2}{3\sqrt{x}\sqrt{2-bx}} + \frac{1}{3\sqrt{x}(2-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(3/2)*(2 - b*x)^(5/2)), x]

[Out] 1/(3*Sqrt[x]*(2 - b*x)^(3/2)) + 2/(3*Sqrt[x]*Sqrt[2 - b*x]) - (2*Sqrt[2 - b*x])/ (3*Sqrt[x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{3/2}(2-bx)^{5/2}} dx &= \frac{1}{3\sqrt{x}(2-bx)^{3/2}} + \frac{2}{3} \int \frac{1}{x^{3/2}(2-bx)^{3/2}} dx \\
&= \frac{1}{3\sqrt{x}(2-bx)^{3/2}} + \frac{2}{3\sqrt{x}\sqrt{2-bx}} + \frac{2}{3} \int \frac{1}{x^{3/2}\sqrt{2-bx}} dx \\
&= \frac{1}{3\sqrt{x}(2-bx)^{3/2}} + \frac{2}{3\sqrt{x}\sqrt{2-bx}} - \frac{2\sqrt{2-bx}}{3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.57

$$\frac{2b^2x^2 - 6bx + 3}{3\sqrt{x}(2-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(3/2)*(2 - b*x)^(5/2)), x]

[Out] -1/3*(3 - 6*b*x + 2*b^2*x^2)/(Sqrt[x]*(2 - b*x)^(3/2))

fricas [A] time = 0.44, size = 46, normalized size = 0.79

$$\frac{(2b^2x^2 - 6bx + 3)\sqrt{-bx + 2}\sqrt{x}}{3(b^2x^3 - 4bx^2 + 4x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+2)^(5/2), x, algorithm="fricas")

[Out] -1/3*(2*b^2*x^2 - 6*b*x + 3)*sqrt(-b*x + 2)*sqrt(x)/(b^2*x^3 - 4*b*x^2 + 4*x)

giac [B] time = 1.12, size = 170, normalized size = 2.93

$$\frac{\sqrt{-bx + 2}b^2}{4\sqrt{(bx - 2)b + 2b}|b|} - \frac{3(\sqrt{-bx + 2}\sqrt{-b} - \sqrt{(bx - 2)b + 2b})^4\sqrt{-b}b^2 - 24(\sqrt{-bx + 2}\sqrt{-b} - \sqrt{(bx - 2)b + 2b})^3}{3\left(\left(\sqrt{-bx + 2}\sqrt{-b} - \sqrt{(bx - 2)b + 2b}\right)^2 - 2b\right)^3|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)/(-b*x+2)^(5/2), x, algorithm="giac")

[Out] -1/4*sqrt(-b*x + 2)*b^2/(sqrt((b*x - 2)*b + 2*b)*abs(b)) - 1/3*(3*(sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^4*sqrt(-b)*b^2 - 24*(sqrt(-b*x + 2)*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^3*abs(b))

$2*\sqrt{-b} - \sqrt{((b*x - 2)*b + 2*b))^2*\sqrt{-b}*b^3 + 20*\sqrt{-b}*b^4)/((\sqrt{-b*x + 2}*\sqrt{-b} - \sqrt{((b*x - 2)*b + 2*b))^2 - 2*b})^3*abs(b))$

maple [A] time = 0.00, size = 28, normalized size = 0.48

$$\frac{2b^2x^2 - 6bx + 3}{3(-bx + 2)^{\frac{3}{2}}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(3/2)/(-b*x+2)^(5/2),x)`

[Out] $-1/3*(2*b^2*x^2-6*b*x+3)/x^{(1/2)/(-b*x+2)^{(3/2)}$

maxima [A] time = 1.35, size = 42, normalized size = 0.72

$$\frac{\left(b^2 - \frac{6(bx-2)b}{x}\right)x^{\frac{3}{2}}}{12(-bx+2)^{\frac{3}{2}}} - \frac{\sqrt{-bx+2}}{4\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(3/2)/(-b*x+2)^(5/2),x, algorithm="maxima")`

[Out] $1/12*(b^2 - 6*(b*x - 2)*b/x)*x^{(3/2)/(-b*x + 2)^{(3/2)} - 1/4*\sqrt{-b*x + 2}/\sqrt{x}$

mupad [B] time = 0.37, size = 59, normalized size = 1.02

$$\frac{3\sqrt{2-bx} - 6bx\sqrt{2-bx} + 2b^2x^2\sqrt{2-bx}}{\sqrt{x}(x(12b-3b^2x)-12)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(3/2)*(2 - b*x)^(5/2)),x)`

[Out] $(3*(2 - b*x)^{(1/2)} - 6*b*x*(2 - b*x)^{(1/2)} + 2*b^2*x^2*(2 - b*x)^{(1/2)})/(x^{(1/2)}*(x*(12*b - 3*b^2*x) - 12))$

sympy [B] time = 4.00, size = 243, normalized size = 4.19

$$\begin{cases} -\frac{2b^{\frac{13}{2}}x^2\sqrt{-1+\frac{2}{bx}}}{3b^6x^2-12b^5x+12b^4} + \frac{6b^{\frac{11}{2}}x\sqrt{-1+\frac{2}{bx}}}{3b^6x^2-12b^5x+12b^4} - \frac{3b^{\frac{9}{2}}\sqrt{-1+\frac{2}{bx}}}{3b^6x^2-12b^5x+12b^4} & \text{for } \frac{2}{|bx|} > 1 \\ -\frac{2ib^{\frac{13}{2}}x^2\sqrt{1-\frac{2}{bx}}}{3b^6x^2-12b^5x+12b^4} + \frac{6ib^{\frac{11}{2}}x\sqrt{1-\frac{2}{bx}}}{3b^6x^2-12b^5x+12b^4} - \frac{3ib^{\frac{9}{2}}\sqrt{1-\frac{2}{bx}}}{3b^6x^2-12b^5x+12b^4} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**(3/2)/(-b*x+2)**(5/2),x)
```

```
[Out] Piecewise((-2*b**(13/2)*x**2*sqrt(-1 + 2/(b*x))/(3*b**6*x**2 - 12*b**5*x + 12*b**4) + 6*b**(11/2)*x*sqrt(-1 + 2/(b*x))/(3*b**6*x**2 - 12*b**5*x + 12*b**4) - 3*b**(9/2)*sqrt(-1 + 2/(b*x))/(3*b**6*x**2 - 12*b**5*x + 12*b**4), 2/Abs(b*x) > 1), (-2*I*b**(13/2)*x**2*sqrt(1 - 2/(b*x))/(3*b**6*x**2 - 12*b**5*x + 12*b**4) + 6*I*b**(11/2)*x*sqrt(1 - 2/(b*x))/(3*b**6*x**2 - 12*b**5*x + 12*b**4) - 3*I*b**(9/2)*sqrt(1 - 2/(b*x))/(3*b**6*x**2 - 12*b**5*x + 12*b**4), True))
```

$$3.646 \quad \int \frac{1}{x^{5/2}(2-bx)^{5/2}} dx$$

Optimal. Leaf size=75

$$-\frac{2\sqrt{2-bx}}{3x^{3/2}} + \frac{1}{x^{3/2}\sqrt{2-bx}} + \frac{1}{3x^{3/2}(2-bx)^{3/2}} - \frac{2b\sqrt{2-bx}}{3\sqrt{x}}$$

[Out] $1/3/x^{(3/2)/(-b*x+2)^{(3/2)}+1/x^{(3/2)/(-b*x+2)^{(1/2)}-2/3*(-b*x+2)^{(1/2)}/x^{(3/2)}-2/3*b*(-b*x+2)^{(1/2)}/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 75, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {45, 37}

$$-\frac{2\sqrt{2-bx}}{3x^{3/2}} + \frac{1}{x^{3/2}\sqrt{2-bx}} + \frac{1}{3x^{3/2}(2-bx)^{3/2}} - \frac{2b\sqrt{2-bx}}{3\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/2)*(2 - b*x)^(5/2)),x]

[Out] $1/(3*x^{(3/2)}*(2 - b*x)^{(3/2)}) + 1/(x^{(3/2)}*Sqrt[2 - b*x]) - (2*Sqrt[2 - b*x])/ (3*x^{(3/2)}) - (2*b*Sqrt[2 - b*x])/ (3*Sqrt[x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{5/2}(2-bx)^{5/2}} dx &= \frac{1}{3x^{3/2}(2-bx)^{3/2}} + \int \frac{1}{x^{5/2}(2-bx)^{3/2}} dx \\
&= \frac{1}{3x^{3/2}(2-bx)^{3/2}} + \frac{1}{x^{3/2}\sqrt{2-bx}} + 2 \int \frac{1}{x^{5/2}\sqrt{2-bx}} dx \\
&= \frac{1}{3x^{3/2}(2-bx)^{3/2}} + \frac{1}{x^{3/2}\sqrt{2-bx}} - \frac{2\sqrt{2-bx}}{3x^{3/2}} + \frac{1}{3}(2b) \int \frac{1}{x^{3/2}\sqrt{2-bx}} dx \\
&= \frac{1}{3x^{3/2}(2-bx)^{3/2}} + \frac{1}{x^{3/2}\sqrt{2-bx}} - \frac{2\sqrt{2-bx}}{3x^{3/2}} - \frac{2b\sqrt{2-bx}}{3\sqrt{x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 41, normalized size = 0.55

$$-\frac{2b^3x^3 - 6b^2x^2 + 3bx + 1}{3x^{3/2}(2-bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/2)*(2 - b*x)^(5/2)),x]

[Out] -1/3*(1 + 3*b*x - 6*b^2*x^2 + 2*b^3*x^3)/(x^(3/2)*(2 - b*x)^(3/2))

fricas [A] time = 0.44, size = 56, normalized size = 0.75

$$-\frac{(2b^3x^3 - 6b^2x^2 + 3bx + 1)\sqrt{-bx + 2}\sqrt{x}}{3(b^2x^4 - 4bx^3 + 4x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+2)^(5/2),x, algorithm="fricas")

[Out] -1/3*(2*b^3*x^3 - 6*b^2*x^2 + 3*b*x + 1)*sqrt(-b*x + 2)*sqrt(x)/(b^2*x^4 - 4*b*x^3 + 4*x^2)

giac [B] time = 1.25, size = 183, normalized size = 2.44

$$-\frac{(4(bx-2)b^2|b| + 9b^2|b|)\sqrt{-bx+2}}{12((bx-2)b+2b)^{\frac{3}{2}}} - \frac{3(\sqrt{-bx+2}\sqrt{-b} - \sqrt{(bx-2)b+2b})^4\sqrt{-b}b^3 - 18(\sqrt{-bx+2}\sqrt{-b} - \sqrt{(bx-2)b+2b})^2}{3\left(\left(\sqrt{-bx+2}\sqrt{-b} - \sqrt{(bx-2)b+2b}\right)^2 - 2\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/2)/(-b*x+2)^(5/2),x, algorithm="giac")

[Out]
$$-1/12*(4*(b*x - 2)*b^2*abs(b) + 9*b^2*abs(b))*sqrt(-b*x + 2)/((b*x - 2)*b + 2*b)^{(3/2)} - 1/3*(3*(sqrt(-b*x + 2))*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^4*sqrt(-b)*b^3 - 18*(sqrt(-b*x + 2))*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2*sqrt(-b)*b^4 + 16*sqrt(-b)*b^5)/(((sqrt(-b*x + 2))*sqrt(-b) - sqrt((b*x - 2)*b + 2*b))^2 - 2*b)^3*abs(b))$$

maple [A] time = 0.00, size = 36, normalized size = 0.48

$$\frac{2b^3x^3 - 6b^2x^2 + 3bx + 1}{3(-bx + 2)^{\frac{3}{2}}x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/x^{(5/2)}/(-b*x+2)^{(5/2)}, x)$

[Out] $-1/3*(2*b^3*x^3 - 6*b^2*x^2 + 3*b*x + 1)/x^{(3/2)}/(-b*x+2)^{(3/2)}$

maxima [A] time = 1.35, size = 58, normalized size = 0.77

$$-\frac{3\sqrt{-bx+2}b}{8\sqrt{x}} + \frac{\left(b^3 - \frac{9(bx-2)b^2}{x}\right)x^{\frac{3}{2}}}{24(-bx+2)^{\frac{3}{2}}} - \frac{(-bx+2)^{\frac{3}{2}}}{24x^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^{(5/2)}/(-b*x+2)^{(5/2)}, x, \text{algorithm}="maxima")$

[Out] $-3/8*sqrt(-b*x + 2)*b/sqrt(x) + 1/24*(b^3 - 9*(b*x - 2)*b^2/x)*x^{(3/2)}/(-b*x + 2)^{(3/2)} - 1/24*(-b*x + 2)^{(3/2)}/x^{(3/2)}$

mupad [B] time = 0.44, size = 73, normalized size = 0.97

$$\frac{\sqrt{2-bx} + 3bx\sqrt{2-bx} - 6b^2x^2\sqrt{2-bx} + 2b^3x^3\sqrt{2-bx}}{x^{3/2}(x(12b - 3b^2x) - 12)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(x^{(5/2)}*(2 - b*x)^{(5/2)}), x)$

[Out] $((2 - b*x)^{(1/2)} + 3*b*x*(2 - b*x)^{(1/2)} - 6*b^2*x^2*(2 - b*x)^{(1/2)} + 2*b^3*x^3*(2 - b*x)^{(1/2)})/(x^{(3/2)}*(x*(12*b - 3*b^2*x) - 12))$

sympy [B] time = 12.40, size = 529, normalized size = 7.05

$$\left\{ \begin{array}{l} \frac{2b^{\frac{27}{2}}x^4\sqrt{-1+\frac{2}{bx}}}{-3b^{12}x^4+18b^{11}x^3-36b^{10}x^2+24b^9x} - \frac{10b^{\frac{25}{2}}x^3\sqrt{-1+\frac{2}{bx}}}{-3b^{12}x^4+18b^{11}x^3-36b^{10}x^2+24b^9x} + \frac{15b^{\frac{23}{2}}x^2\sqrt{-1+\frac{2}{bx}}}{-3b^{12}x^4+18b^{11}x^3-36b^{10}x^2+24b^9x} - \frac{5b^{\frac{21}{2}}x\sqrt{-1+\frac{2}{bx}}}{-3b^{12}x^4+18b^{11}x^3-36b^{10}x^2+24b^9x} \\ \frac{2ib^{\frac{27}{2}}x^4\sqrt{1-\frac{2}{bx}}}{-3b^{12}x^4+18b^{11}x^3-36b^{10}x^2+24b^9x} - \frac{10ib^{\frac{25}{2}}x^3\sqrt{1-\frac{2}{bx}}}{-3b^{12}x^4+18b^{11}x^3-36b^{10}x^2+24b^9x} + \frac{15ib^{\frac{23}{2}}x^2\sqrt{1-\frac{2}{bx}}}{-3b^{12}x^4+18b^{11}x^3-36b^{10}x^2+24b^9x} - \frac{5ib^{\frac{21}{2}}x\sqrt{1-\frac{2}{bx}}}{-3b^{12}x^4+18b^{11}x^3-36b^{10}x^2+24b^9x} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(5/2)/(-b*x+2)**(5/2),x)

[Out] Piecewise((2*b**(27/2)*x**4*sqrt(-1 + 2/(b*x)))/(-3*b**12*x**4 + 18*b**11*x**3 - 36*b**10*x**2 + 24*b**9*x) - 10*b**(25/2)*x**3*sqrt(-1 + 2/(b*x)))/(-3*b**12*x**4 + 18*b**11*x**3 - 36*b**10*x**2 + 24*b**9*x) + 15*b**(23/2)*x**2*sqrt(-1 + 2/(b*x)))/(-3*b**12*x**4 + 18*b**11*x**3 - 36*b**10*x**2 + 24*b**9*x) - 5*b**(21/2)*x*sqrt(-1 + 2/(b*x)))/(-3*b**12*x**4 + 18*b**11*x**3 - 36*b**10*x**2 + 24*b**9*x) - 2*b**(19/2)*sqrt(-1 + 2/(b*x)))/(-3*b**12*x**4 + 18*b**11*x**3 - 36*b**10*x**2 + 24*b**9*x), 2/Abs(b*x) > 1), (2*I*b**(27/2)*x**4*sqrt(1 - 2/(b*x)))/(-3*b**12*x**4 + 18*b**11*x**3 - 36*b**10*x**2 + 24*b**9*x) - 10*I*b**(25/2)*x**3*sqrt(1 - 2/(b*x)))/(-3*b**12*x**4 + 18*b**11*x**3 - 36*b**10*x**2 + 24*b**9*x) + 15*I*b**(23/2)*x**2*sqrt(1 - 2/(b*x)))/(-3*b**12*x**4 + 18*b**11*x**3 - 36*b**10*x**2 + 24*b**9*x) - 5*I*b**(21/2)*x*sqrt(1 - 2/(b*x)))/(-3*b**12*x**4 + 18*b**11*x**3 - 36*b**10*x**2 + 24*b**9*x) - 2*I*b**(19/2)*sqrt(1 - 2/(b*x)))/(-3*b**12*x**4 + 18*b**11*x**3 - 36*b**10*x**2 + 24*b**9*x), True))

$$3.647 \quad \int \frac{\sqrt{x}}{\sqrt{1-x}} dx$$

Optimal. Leaf size=27

$$-\sqrt{1-x}\sqrt{x} - \frac{1}{2}\sin^{-1}(1-2x)$$

[Out] 1/2*arcsin(-1+2*x)-(1-x)^(1/2)*x^(1/2)

Rubi [A] time = 0.01, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {50, 53, 619, 216}

$$-\sqrt{1-x}\sqrt{x} - \frac{1}{2}\sin^{-1}(1-2x)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[x]/Sqrt[1-x],x]

[Out] -(Sqrt[1-x]*Sqrt[x]) - ArcSin[1-2*x]/2

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 53

Int[1/(Sqrt[(a_) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Int[1/Sqrt[a*c - b*(a - c)*x - b^2*x^2], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b + d, 0] && GtQ[a + c, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 619

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := Dist[1/(2*c*((-4*c)/(b^2 - 4*a*c))^(p)), Subst[Int[Simp[1 - x^2/(b^2 - 4*a*c), x]^p, x], x, b

+ 2*c*x], x] /; FreeQ[{a, b, c, p}, x] && GtQ[4*a - b^2/c, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt{x}}{\sqrt{1-x}} dx &= -\sqrt{1-x} \sqrt{x} + \frac{1}{2} \int \frac{1}{\sqrt{1-x} \sqrt{x}} dx \\
 &= -\sqrt{1-x} \sqrt{x} + \frac{1}{2} \int \frac{1}{\sqrt{x-x^2}} dx \\
 &= -\sqrt{1-x} \sqrt{x} - \frac{1}{2} \text{Subst} \left(\int \frac{1}{\sqrt{1-x^2}} dx, x, 1-2x \right) \\
 &= -\sqrt{1-x} \sqrt{x} - \frac{1}{2} \sin^{-1}(1-2x)
 \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 0.93

$$-\sqrt{-((x-1)x)} - \sin^{-1}(\sqrt{1-x})$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]/Sqrt[1-x],x]

[Out] -Sqrt[-((-1+x)*x)] - ArcSin[Sqrt[1-x]]

fricas [A] time = 0.42, size = 27, normalized size = 1.00

$$-\sqrt{x} \sqrt{-x+1} - \arctan\left(\frac{\sqrt{-x+1}}{\sqrt{x}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(1-x)^(1/2),x, algorithm="fricas")

[Out] -sqrt(x)*sqrt(-x+1) - arctan(sqrt(-x+1)/sqrt(x))

giac [A] time = 1.17, size = 17, normalized size = 0.63

$$-\sqrt{x} \sqrt{-x+1} + \arcsin(\sqrt{x})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)/(1-x)^(1/2),x, algorithm="giac")

[Out] $-\sqrt{x}\sqrt{-x+1} + \arcsin(\sqrt{x})$

maple [A] time = 0.01, size = 41, normalized size = 1.52

$$-\sqrt{-x+1}\sqrt{x} + \frac{\sqrt{(-x+1)x}\arcsin(2x-1)}{2\sqrt{-x+1}\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{1/2}/(1-x)^{1/2}, x)$

[Out] $-(1-x)^{1/2}*x^{1/2}+1/2*(x*(1-x))^{1/2}/x^{1/2}/(1-x)^{1/2}*\arcsin(-1+2*x)$

maxima [A] time = 3.00, size = 37, normalized size = 1.37

$$\frac{\sqrt{-x+1}}{\sqrt{x}\left(\frac{x-1}{x}-1\right)} - \arctan\left(\frac{\sqrt{-x+1}}{\sqrt{x}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{1/2}/(1-x)^{1/2}, x, \text{algorithm}="maxima")$

[Out] $\sqrt{-x+1}/(\sqrt{x}*((x-1)/x-1)) - \arctan(\sqrt{-x+1}/\sqrt{x})$

mupad [B] time = 0.57, size = 31, normalized size = 1.15

$$2 \operatorname{atan}\left(\frac{\sqrt{x}}{\sqrt{1-x}-1}\right) - \sqrt{x}\sqrt{1-x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{1/2}/(1-x)^{1/2}, x)$

[Out] $2*\operatorname{atan}(x^{1/2}/((1-x)^{1/2}-1)) - x^{1/2}*(1-x)^{1/2}$

sympy [A] time = 1.65, size = 54, normalized size = 2.00

$$\begin{cases} -i\sqrt{x}\sqrt{x-1} - i \operatorname{acosh}(\sqrt{x}) & \text{for } |x| > 1 \\ \frac{x^3}{\sqrt{1-x}} - \frac{\sqrt{x}}{\sqrt{1-x}} + \operatorname{asin}(\sqrt{x}) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{1/2}/(1-x)^{1/2}, x)$

[Out] $\text{Piecewise}((-I*\sqrt{x}*\sqrt{x-1} - I*\operatorname{acosh}(\sqrt{x}), \operatorname{Abs}(x) > 1), (x^{3/2}/\sqrt{1-x} - \sqrt{x}/\sqrt{1-x} + \operatorname{asin}(\sqrt{x}), \operatorname{True}))$

$$3.648 \quad \int \frac{1}{\sqrt{1-x} \sqrt{x}} dx$$

Optimal. Leaf size=8

$$-\sin^{-1}(1-2x)$$

[Out] arcsin(-1+2*x)

Rubi [A] time = 0.00, antiderivative size = 8, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {53, 619, 216}

$$-\sin^{-1}(1-2x)$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[1-x]*Sqrt[x]),x]

[Out] -ArcSin[1-2*x]

Rule 53

Int[1/(Sqrt[(a_) + (b_)*(x_)]*Sqrt[(c_) + (d_)*(x_)]), x_Symbol] := Int[1/Sqrt[a*c - b*(a - c)*x - b^2*x^2], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b + d, 0] && GtQ[a + c, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 619

Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(p_), x_Symbol] := Dist[1/(2*c*((-4*c)/(b^2 - 4*a*c))^p), Subst[Int[Simp[1 - x^2/(b^2 - 4*a*c), x]^p, x], x, b + 2*c*x], x] /; FreeQ[{a, b, c, p}, x] && GtQ[4*a - b^2/c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{1-x}\sqrt{x}} dx &= \int \frac{1}{\sqrt{x-x^2}} dx \\ &= -\text{Subst}\left(\int \frac{1}{\sqrt{1-x^2}} dx, x, 1-2x\right) \\ &= -\sin^{-1}(1-2x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 12, normalized size = 1.50

$$-2 \sin^{-1}\left(\sqrt{1-x}\right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[1 - x]*Sqrt[x]),x]

[Out] -2*ArcSin[Sqrt[1 - x]]

fricas [B] time = 0.46, size = 14, normalized size = 1.75

$$-2 \arctan\left(\frac{\sqrt{-x+1}}{\sqrt{x}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(1/2)/x^(1/2),x, algorithm="fricas")

[Out] -2*arctan(sqrt(-x + 1)/sqrt(x))

giac [A] time = 1.09, size = 6, normalized size = 0.75

$$2 \arcsin\left(\sqrt{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(1/2)/x^(1/2),x, algorithm="giac")

[Out] 2*arcsin(sqrt(x))

maple [B] time = 0.00, size = 27, normalized size = 3.38

$$\frac{\sqrt{(-x+1)x} \arcsin(2x-1)}{\sqrt{-x+1} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-x+1)^(1/2)/x^(1/2),x)`

[Out] `((-x+1)*x)^(1/2)/(-x+1)^(1/2)/x^(1/2)*arcsin(2*x-1)`

maxima [B] time = 2.95, size = 14, normalized size = 1.75

$$-2 \operatorname{arctan}\left(\frac{\sqrt{-x+1}}{\sqrt{x}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(1/2)/x^(1/2),x, algorithm="maxima")`

[Out] `-2*arctan(sqrt(-x + 1)/sqrt(x))`

mupad [B] time = 0.05, size = 16, normalized size = 2.00

$$-4 \operatorname{atan}\left(\frac{\sqrt{1-x}-1}{\sqrt{x}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(1-x)^(1/2)),x)`

[Out] `-4*atan(((1-x)^(1/2)-1)/x^(1/2))`

sympy [A] time = 0.97, size = 20, normalized size = 2.50

$$\begin{cases} -2i \operatorname{acosh}(\sqrt{x}) & \text{for } |x| > 1 \\ 2 \operatorname{asin}(\sqrt{x}) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)**(1/2)/x**(1/2),x)`

[Out] `Piecewise((-2*I*acosh(sqrt(x)), Abs(x) > 1), (2*asin(sqrt(x)), True))`

$$3.649 \quad \int \frac{1}{\sqrt{x} \sqrt{1-bx}} dx$$

Optimal. Leaf size=19

$$\frac{2 \sin^{-1}(\sqrt{b} \sqrt{x})}{\sqrt{b}}$$

[Out] 2*arcsin(b^(1/2)*x^(1/2))/b^(1/2)

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {54, 216}

$$\frac{2 \sin^{-1}(\sqrt{b} \sqrt{x})}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*Sqrt[1 - b*x]),x]

[Out] (2*ArcSin[Sqrt[b]*Sqrt[x]])/Sqrt[b]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_.)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{x} \sqrt{1-bx}} dx &= 2 \text{Subst} \left(\int \frac{1}{\sqrt{1-bx^2}} dx, x, \sqrt{x} \right) \\ &= \frac{2 \sin^{-1}(\sqrt{b} \sqrt{x})}{\sqrt{b}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 19, normalized size = 1.00

$$\frac{2 \sin^{-1}(\sqrt{b} \sqrt{x})}{\sqrt{b}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*Sqrt[1 - b*x]),x]

[Out] (2*ArcSin[Sqrt[b]*Sqrt[x]])/Sqrt[b]

fricas [A] time = 0.43, size = 57, normalized size = 3.00

$$\left[-\frac{\sqrt{-b} \log(-2bx + 2\sqrt{-bx+1}\sqrt{-b}\sqrt{x} + 1)}{b}, -\frac{2 \arctan\left(\frac{\sqrt{-bx+1}}{\sqrt{b}\sqrt{x}}\right)}{\sqrt{b}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-b*x+1)^(1/2),x, algorithm="fricas")

[Out] [-sqrt(-b)*log(-2*b*x + 2*sqrt(-b*x + 1)*sqrt(-b)*sqrt(x) + 1)/b, -2*arctan(sqrt(-b*x + 1)/(sqrt(b)*sqrt(x)))/sqrt(b)]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: NotImplementedError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-b*x+1)^(1/2),x, algorithm="giac")

[Out] Exception raised: NotImplementedError >> Unable to parse Giac output: Warning, choosing root of [1,0,%%{4,[1,1]%%}+%%{4,[1,0]%%}+%%{-4,[0,1]%%}+%%{-4,[0,0]%%},0,%%{6,[2,2]%%}+%%{4,[2,1]%%}+%%{6,[2,0]%%}+%%{-4,[1,2]%%}+%%{-16,[1,1]%%}+%%{-4,[1,0]%%}+%%{6,[0,2]%%}+%%{4,[0,1]%%}+%%{6,[0,0]%%},0,%%{4,[3,3]%%}+%%{-4,[3,2]%%}+%%{-4,[3,1]%%}+%%{4,[3,0]%%}+%%{4,[2,3]%%}+%%{-52,[2,2]%%}+%%{12,[2,1]%%}+%%{4,[2,0]%%}+%%{-4,[1,3]%%}+%%{-12,[1,2]%%}+%%{52,[1,1]%%}+%%{-4,[1,0]%%}+%%{-4,[0,3]%%}+%%{4,[0,2]%%}+%%{4,[0,1]%%}+%%{-4,[0,0]%%},0,%%{1,[4,4]%%}+%%{-4,[4,3]%%}+%%{6,[4,2]%%}+%%{-4,[4,1]%%}+%%{1,[4,0]%%}+%%{4,[3,4]%%}+%%{-8,[3,3]%%}+%%{8,[3,2]%%}+%%{-8,[3,1]%%}+%%{4,[3,0]%%}+%%{6,[2,4]%%}+%%{-8,[2,3]%%}+%%{20,[2,2]%%}+%%{-8,[2,1]%%}+%%{6,[2,0]%%}+%%{4,[1,4]%%}+%%{-8,[1,3]%%}+%%{8,[1,2]%%}+%%{-8,[1,1]%%}+%%{4,[1,0]%%}+%%{1,[0,4]%%}+%%{-4,[0,3]%%}+%%{6,[0,2]%%}+%%{-4,[0,1]%%}+%%{1,[0,0]%%}] at parameters values [-15.6438432182,61.793747834

9]Warning, choosing root of $[1,0,\%{\{4,[1,1]\}}+\%{\{4,[1,0]\}}+\%{\{-4,[0,1]\}}+\%{\{-4,[0,0]\}},0,\%{\{6,[2,2]\}}+\%{\{4,[2,1]\}}+\%{\{6,[2,0]\}}+\%{\{-4,[1,2]\}}+\%{\{-16,[1,1]\}}+\%{\{-4,[1,0]\}}+\%{\{6,[0,2]\}}+\%{\{4,[0,1]\}}+\%{\{6,[0,0]\}},0,\%{\{4,[3,3]\}}+\%{\{-4,[3,2]\}}+\%{\{-4,[3,1]\}}+\%{\{4,[3,0]\}}+\%{\{4,[2,3]\}}+\%{\{-52,[2,2]\}}+\%{\{12,[2,1]\}}+\%{\{4,[2,0]\}}+\%{\{-4,[1,3]\}}+\%{\{-12,[1,2]\}}+\%{\{52,[1,1]\}}+\%{\{-4,[1,0]\}}+\%{\{-4,[0,3]\}}+\%{\{4,[0,2]\}}+\%{\{4,[0,1]\}}+\%{\{-4,[0,0]\}},0,\%{\{1,[4,4]\}}+\%{\{-4,[4,3]\}}+\%{\{6,[4,2]\}}+\%{\{-4,[4,1]\}}+\%{\{1,[4,0]\}}+\%{\{4,[3,4]\}}+\%{\{-8,[3,3]\}}+\%{\{8,[3,2]\}}+\%{\{-8,[3,1]\}}+\%{\{4,[3,0]\}}+\%{\{6,[2,4]\}}+\%{\{-8,[2,3]\}}+\%{\{20,[2,2]\}}+\%{\{-8,[2,1]\}}+\%{\{6,[2,0]\}}+\%{\{4,[1,4]\}}+\%{\{-8,[1,3]\}}+\%{\{8,[1,2]\}}+\%{\{-8,[1,1]\}}+\%{\{4,[1,0]\}}+\%{\{1,[0,4]\}}+\%{\{-4,[0,3]\}}+\%{\{6,[0,2]\}}+\%{\{-4,[0,1]\}}+\%{\{1,[0,0]\}}$ at parameters values $[-29.292030761,78.6493344628]2/\text{abs}(b)*b^2/b/\text{sqrt}(-b)*\ln(\text{abs}(\text{sqrt}(-b*(-b*x+1)+b)-\text{sqrt}(-b)*\text{sqrt}(-b*x+1)))$

maple [B] time = 0.01, size = 48, normalized size = 2.53

$$\frac{\sqrt{-bx+1}x \arctan\left(\frac{\left(x-\frac{1}{2b}\right)\sqrt{b}}{\sqrt{-bx^2+x}}\right)}{\sqrt{-bx+1} \sqrt{b} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/x^{(1/2)}/(-b*x+1)^{(1/2)},x)$

[Out] $(x*(-b*x+1))^{(1/2)}/x^{(1/2)}/(-b*x+1)^{(1/2)}/b^{(1/2)}*\arctan(b^{(1/2)}*(x-1/2/b)/(-b*x^2+x)^{(1/2)})$

maxima [A] time = 2.89, size = 21, normalized size = 1.11

$$\frac{2 \arctan\left(\frac{\sqrt{-bx+1}}{\sqrt{b} \sqrt{x}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^{(1/2)}/(-b*x+1)^{(1/2)},x, \text{algorithm}=\text{"maxima"})$

[Out] $-2*\arctan(\text{sqrt}(-b*x + 1)/(\text{sqrt}(b)*\text{sqrt}(x)))/\text{sqrt}(b)$

mupad [B] time = 0.13, size = 23, normalized size = 1.21

$$\frac{4 \text{atan}\left(\frac{\sqrt{1-bx}-1}{\sqrt{b} \sqrt{x}}\right)}{\sqrt{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/2)*(1 - b*x)^(1/2)),x)`

[Out] `-(4*atan(((1 - b*x)^(1/2) - 1)/(b^(1/2)*x^(1/2))))/b^(1/2)`

sympy [A] time = 1.06, size = 42, normalized size = 2.21

$$\begin{cases} -\frac{2i \operatorname{acosh}(\sqrt{b} \sqrt{x})}{\sqrt{b}} & \text{for } |bx| > 1 \\ \frac{2 \operatorname{asin}(\sqrt{b} \sqrt{x})}{\sqrt{b}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(1/2)/(-b*x+1)**(1/2),x)`

[Out] `Piecewise((-2*I*acosh(sqrt(b)*sqrt(x))/sqrt(b), Abs(b*x) > 1), (2*asin(sqrt(b)*sqrt(x))/sqrt(b), True))`

3.650 $\int x^{5/3}(a + bx) dx$

Optimal. Leaf size=21

$$\frac{3}{8}ax^{8/3} + \frac{3}{11}bx^{11/3}$$

[Out] $3/8*a*x^{(8/3)}+3/11*b*x^{(11/3)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3}{8}ax^{8/3} + \frac{3}{11}bx^{11/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(5/3)}*(a + b*x), x]$

[Out] $(3*a*x^{(8/3)})/8 + (3*b*x^{(11/3)})/11$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^{5/3}(a + bx) dx &= \int (ax^{5/3} + bx^{8/3}) dx \\ &= \frac{3}{8}ax^{8/3} + \frac{3}{11}bx^{11/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 17, normalized size = 0.81

$$\frac{3}{88}x^{8/3}(11a + 8bx)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(5/3)}*(a + b*x), x]$

[Out] $(3*x^{(8/3)}*(11*a + 8*b*x))/88$

fricas [A] time = 0.40, size = 18, normalized size = 0.86

$$\frac{3}{88} (8bx^3 + 11ax^2)x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)*(b*x+a),x, algorithm="fricas")

[Out] 3/88*(8*b*x^3 + 11*a*x^2)*x^(2/3)

giac [A] time = 0.98, size = 13, normalized size = 0.62

$$\frac{3}{11}bx^{\frac{11}{3}} + \frac{3}{8}ax^{\frac{8}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)*(b*x+a),x, algorithm="giac")

[Out] 3/11*b*x^(11/3) + 3/8*a*x^(8/3)

maple [A] time = 0.00, size = 14, normalized size = 0.67

$$\frac{3(8bx + 11a)x^{\frac{8}{3}}}{88}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/3)*(b*x+a),x)

[Out] 3/88*x^(8/3)*(8*b*x+11*a)

maxima [A] time = 1.30, size = 13, normalized size = 0.62

$$\frac{3}{11}bx^{\frac{11}{3}} + \frac{3}{8}ax^{\frac{8}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)*(b*x+a),x, algorithm="maxima")

[Out] 3/11*b*x^(11/3) + 3/8*a*x^(8/3)

mupad [B] time = 0.03, size = 13, normalized size = 0.62

$$\frac{3x^{8/3}(11a + 8bx)}{88}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(5/3)*(a + b*x), x)
```

```
[Out] (3*x^(8/3)*(11*a + 8*b*x))/88
```

```
sympy [A] time = 2.01, size = 19, normalized size = 0.90
```

$$\frac{3ax^{\frac{8}{3}}}{8} + \frac{3bx^{\frac{11}{3}}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(5/3)*(b*x+a), x)
```

```
[Out] 3*a*x**(8/3)/8 + 3*b*x**(11/3)/11
```

3.651 $\int x^{4/3}(a + bx) dx$

Optimal. Leaf size=21

$$\frac{3}{7}ax^{7/3} + \frac{3}{10}bx^{10/3}$$

[Out] $3/7*a*x^{(7/3)}+3/10*b*x^{(10/3)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3}{7}ax^{7/3} + \frac{3}{10}bx^{10/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(4/3)}*(a + b*x), x]$

[Out] $(3*a*x^{(7/3)})/7 + (3*b*x^{(10/3)})/10$

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ $\text{FreeQ}\{a, b, c, d, n\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (\ !\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0]) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x^{4/3}(a + bx) dx &= \int (ax^{4/3} + bx^{7/3}) dx \\ &= \frac{3}{7}ax^{7/3} + \frac{3}{10}bx^{10/3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 0.81

$$\frac{3}{70}x^{7/3}(10a + 7bx)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(4/3)}*(a + b*x), x]$

[Out] $(3*x^{(7/3)}*(10*a + 7*b*x))/70$

fricas [A] time = 0.41, size = 18, normalized size = 0.86

$$\frac{3}{70} (7bx^3 + 10ax^2)x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)*(b*x+a),x, algorithm="fricas")

[Out] 3/70*(7*b*x^3 + 10*a*x^2)*x^(1/3)

giac [A] time = 1.04, size = 13, normalized size = 0.62

$$\frac{3}{10}bx^{\frac{10}{3}} + \frac{3}{7}ax^{\frac{7}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)*(b*x+a),x, algorithm="giac")

[Out] 3/10*b*x^(10/3) + 3/7*a*x^(7/3)

maple [A] time = 0.00, size = 14, normalized size = 0.67

$$\frac{3(7bx + 10a)x^{\frac{7}{3}}}{70}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(4/3)*(b*x+a),x)

[Out] 3/70*x^(7/3)*(7*b*x+10*a)

maxima [A] time = 1.35, size = 13, normalized size = 0.62

$$\frac{3}{10}bx^{\frac{10}{3}} + \frac{3}{7}ax^{\frac{7}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)*(b*x+a),x, algorithm="maxima")

[Out] 3/10*b*x^(10/3) + 3/7*a*x^(7/3)

mupad [B] time = 0.02, size = 13, normalized size = 0.62

$$\frac{3x^{7/3}(10a + 7bx)}{70}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(4/3)*(a + b*x), x)
```

```
[Out] (3*x^(7/3)*(10*a + 7*b*x))/70
```

sympy [A] time = 1.30, size = 19, normalized size = 0.90

$$\frac{3ax^{\frac{7}{3}}}{7} + \frac{3bx^{\frac{10}{3}}}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(4/3)*(b*x+a), x)
```

```
[Out] 3*a*x**(7/3)/7 + 3*b*x**(10/3)/10
```

3.652 $\int x^{2/3}(a + bx) dx$

Optimal. Leaf size=21

$$\frac{3}{5}ax^{5/3} + \frac{3}{8}bx^{8/3}$$

[Out] $3/5*a*x^{(5/3)}+3/8*b*x^{(8/3)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3}{5}ax^{5/3} + \frac{3}{8}bx^{8/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(2/3)}*(a + b*x), x]$

[Out] $(3*a*x^{(5/3)})/5 + (3*b*x^{(8/3)})/8$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^{2/3}(a + bx) dx &= \int (ax^{2/3} + bx^{5/3}) dx \\ &= \frac{3}{5}ax^{5/3} + \frac{3}{8}bx^{8/3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 0.81

$$\frac{3}{40}x^{5/3}(8a + 5bx)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(2/3)}*(a + b*x), x]$

[Out] $(3*x^{(5/3)}*(8*a + 5*b*x))/40$

fricas [A] time = 0.40, size = 16, normalized size = 0.76

$$\frac{3}{40} (5bx^2 + 8ax)x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)*(b*x+a),x, algorithm="fricas")

[Out] 3/40*(5*b*x^2 + 8*a*x)*x^(2/3)

giac [A] time = 0.99, size = 13, normalized size = 0.62

$$\frac{3}{8}bx^{\frac{8}{3}} + \frac{3}{5}ax^{\frac{5}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)*(b*x+a),x, algorithm="giac")

[Out] 3/8*b*x^(8/3) + 3/5*a*x^(5/3)

maple [A] time = 0.00, size = 14, normalized size = 0.67

$$\frac{3(5bx + 8a)x^{\frac{5}{3}}}{40}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(2/3)*(b*x+a),x)

[Out] 3/40*x^(5/3)*(5*b*x+8*a)

maxima [A] time = 1.35, size = 13, normalized size = 0.62

$$\frac{3}{8}bx^{\frac{8}{3}} + \frac{3}{5}ax^{\frac{5}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)*(b*x+a),x, algorithm="maxima")

[Out] 3/8*b*x^(8/3) + 3/5*a*x^(5/3)

mupad [B] time = 0.02, size = 13, normalized size = 0.62

$$\frac{3x^{5/3}(8a + 5bx)}{40}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(2/3)*(a + b*x), x)
```

```
[Out] (3*x^(5/3)*(8*a + 5*b*x))/40
```

```
sympy [A] time = 0.45, size = 19, normalized size = 0.90
```

$$\frac{3ax^{\frac{5}{3}}}{5} + \frac{3bx^{\frac{8}{3}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(2/3)*(b*x+a), x)
```

```
[Out] 3*a*x**(5/3)/5 + 3*b*x**(8/3)/8
```

3.653 $\int \sqrt[3]{x} (a + bx) dx$

Optimal. Leaf size=21

$$\frac{3}{4}ax^{4/3} + \frac{3}{7}bx^{7/3}$$

[Out] $3/4*a*x^{(4/3)}+3/7*b*x^{(7/3)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3}{4}ax^{4/3} + \frac{3}{7}bx^{7/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(1/3)}*(a + b*x), x]$

[Out] $(3*a*x^{(4/3)})/4 + (3*b*x^{(7/3)})/7$

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \sqrt[3]{x} (a + bx) dx &= \int (a\sqrt[3]{x} + bx^{4/3}) dx \\ &= \frac{3}{4}ax^{4/3} + \frac{3}{7}bx^{7/3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 0.81

$$\frac{3}{28}x^{4/3}(7a + 4bx)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(1/3)}*(a + b*x), x]$

[Out] $(3*x^{(4/3)}*(7*a + 4*b*x))/28$

fricas [A] time = 0.46, size = 16, normalized size = 0.76

$$\frac{3}{28} (4bx^2 + 7ax)x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)*(b*x+a),x, algorithm="fricas")

[Out] 3/28*(4*b*x^2 + 7*a*x)*x^(1/3)

giac [A] time = 1.03, size = 13, normalized size = 0.62

$$\frac{3}{7}bx^{\frac{7}{3}} + \frac{3}{4}ax^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)*(b*x+a),x, algorithm="giac")

[Out] 3/7*b*x^(7/3) + 3/4*a*x^(4/3)

maple [A] time = 0.00, size = 14, normalized size = 0.67

$$\frac{3(4bx + 7a)x^{\frac{4}{3}}}{28}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/3)*(b*x+a),x)

[Out] 3/28*x^(4/3)*(4*b*x+7*a)

maxima [A] time = 1.37, size = 13, normalized size = 0.62

$$\frac{3}{7}bx^{\frac{7}{3}} + \frac{3}{4}ax^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)*(b*x+a),x, algorithm="maxima")

[Out] 3/7*b*x^(7/3) + 3/4*a*x^(4/3)

mupad [B] time = 0.02, size = 13, normalized size = 0.62

$$\frac{3x^{4/3}(7a + 4bx)}{28}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(1/3)*(a + b*x), x)
```

```
[Out] (3*x^(4/3)*(7*a + 4*b*x))/28
```

sympy [A] time = 1.52, size = 19, normalized size = 0.90

$$\frac{3ax^{\frac{4}{3}}}{4} + \frac{3bx^{\frac{7}{3}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(1/3)*(b*x+a), x)
```

```
[Out] 3*a*x**(4/3)/4 + 3*b*x**(7/3)/7
```


$$3.654 \quad \int \frac{a+bx}{\sqrt[3]{x}} dx$$

Optimal. Leaf size=21

$$\frac{3}{2}ax^{2/3} + \frac{3}{5}bx^{5/3}$$

[Out] $3/2*a*x^{(2/3)}+3/5*b*x^{(5/3)}$

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3}{2}ax^{2/3} + \frac{3}{5}bx^{5/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x^(1/3), x]

[Out] $(3*a*x^{(2/3)})/2 + (3*b*x^{(5/3)})/5$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{\sqrt[3]{x}} dx &= \int \left(\frac{a}{\sqrt[3]{x}} + bx^{2/3} \right) dx \\ &= \frac{3}{2}ax^{2/3} + \frac{3}{5}bx^{5/3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 0.81

$$\frac{3}{10}x^{2/3}(5a + 2bx)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x^(1/3), x]

[Out] $(3x^{2/3}(5a + 2bx))/10$

fricas [A] time = 0.44, size = 13, normalized size = 0.62

$$\frac{3}{10} (2bx + 5a)x^{2/3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(1/3),x, algorithm="fricas")`

[Out] $3/10*(2bx + 5a)*x^{2/3}$

giac [A] time = 1.12, size = 13, normalized size = 0.62

$$\frac{3}{5}bx^{5/3} + \frac{3}{2}ax^{2/3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(1/3),x, algorithm="giac")`

[Out] $3/5*b*x^{5/3} + 3/2*a*x^{2/3}$

maple [A] time = 0.00, size = 14, normalized size = 0.67

$$\frac{3(2bx + 5a)x^{2/3}}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/x^(1/3),x)`

[Out] $3/10*x^{2/3}*(2bx+5a)$

maxima [A] time = 1.31, size = 13, normalized size = 0.62

$$\frac{3}{5}bx^{5/3} + \frac{3}{2}ax^{2/3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(1/3),x, algorithm="maxima")`

[Out] $3/5*b*x^{5/3} + 3/2*a*x^{2/3}$

mupad [B] time = 0.02, size = 13, normalized size = 0.62

$$\frac{3x^{2/3}(5a + 2bx)}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^(1/3), x)
```

```
[Out] (3*x^(2/3)*(5*a + 2*b*x))/10
```

```
sympy [A] time = 1.66, size = 19, normalized size = 0.90
```

$$\frac{3ax^{\frac{2}{3}}}{2} + \frac{3bx^{\frac{5}{3}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**(1/3), x)
```

```
[Out] 3*a*x**(2/3)/2 + 3*b*x**(5/3)/5
```

$$3.655 \quad \int \frac{a+bx}{x^{2/3}} dx$$

Optimal. Leaf size=19

$$3a\sqrt[3]{x} + \frac{3}{4}bx^{4/3}$$

[Out] $3*a*x^{(1/3)}+3/4*b*x^{(4/3)}$

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$3a\sqrt[3]{x} + \frac{3}{4}bx^{4/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x^(2/3), x]

[Out] $3*a*x^{(1/3)} + (3*b*x^{(4/3)})/4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^{2/3}} dx &= \int \left(\frac{a}{x^{2/3}} + b\sqrt[3]{x} \right) dx \\ &= 3a\sqrt[3]{x} + \frac{3}{4}bx^{4/3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 0.84

$$\frac{3}{4}\sqrt[3]{x}(4a + bx)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x^(2/3), x]

[Out] $(3*x^{(1/3)}*(4*a + b*x))/4$

fricas [A] time = 0.42, size = 12, normalized size = 0.63

$$\frac{3}{4} (bx + 4a)x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^(2/3),x, algorithm="fricas")

[Out] 3/4*(b*x + 4*a)*x^(1/3)

giac [A] time = 1.12, size = 13, normalized size = 0.68

$$\frac{3}{4} bx^{\frac{4}{3}} + 3ax^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^(2/3),x, algorithm="giac")

[Out] 3/4*b*x^(4/3) + 3*a*x^(1/3)

maple [A] time = 0.00, size = 13, normalized size = 0.68

$$\frac{3 (bx + 4a) x^{\frac{1}{3}}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^(2/3),x)

[Out] 3/4*x^(1/3)*(b*x+4*a)

maxima [A] time = 1.28, size = 13, normalized size = 0.68

$$\frac{3}{4} bx^{\frac{4}{3}} + 3ax^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^(2/3),x, algorithm="maxima")

[Out] 3/4*b*x^(4/3) + 3*a*x^(1/3)

mupad [B] time = 0.02, size = 12, normalized size = 0.63

$$\frac{3x^{1/3}(4a+bx)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^(2/3),x)
```

```
[Out] (3*x^(1/3)*(4*a + b*x))/4
```

sympy [A] time = 1.49, size = 17, normalized size = 0.89

$$3a\sqrt[3]{x} + \frac{3bx^{\frac{4}{3}}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**(2/3),x)
```

```
[Out] 3*a*x**(1/3) + 3*b*x**(4/3)/4
```

$$3.656 \quad \int \frac{a+bx}{x^{4/3}} dx$$

Optimal. Leaf size=19

$$\frac{3}{2}bx^{2/3} - \frac{3a}{\sqrt[3]{x}}$$

[Out] $-3*a/x^{(1/3)}+3/2*b*x^{(2/3)}$

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3}{2}bx^{2/3} - \frac{3a}{\sqrt[3]{x}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x^(4/3), x]

[Out] $(-3*a)/x^{(1/3)} + (3*b*x^{(2/3)})/2$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^{4/3}} dx &= \int \left(\frac{a}{x^{4/3}} + \frac{b}{\sqrt[3]{x}} \right) dx \\ &= -\frac{3a}{\sqrt[3]{x}} + \frac{3}{2}bx^{2/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 16, normalized size = 0.84

$$\frac{3(bx - 2a)}{2\sqrt[3]{x}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x^(4/3), x]

[Out] $(3*(-2*a + b*x))/(2*x^{(1/3)})$

fricas [A] time = 0.43, size = 12, normalized size = 0.63

$$\frac{3(bx - 2a)}{2x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(4/3),x, algorithm="fricas")`

[Out] $3/2*(b*x - 2*a)/x^{(1/3)}$

giac [A] time = 1.13, size = 13, normalized size = 0.68

$$\frac{3}{2}bx^{\frac{2}{3}} - \frac{3a}{x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(4/3),x, algorithm="giac")`

[Out] $3/2*b*x^{(2/3)} - 3*a/x^{(1/3)}$

maple [A] time = 0.00, size = 14, normalized size = 0.74

$$-\frac{3(-bx + 2a)}{2x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/x^(4/3),x)`

[Out] $-3/2*(-b*x+2*a)/x^{(1/3)}$

maxima [A] time = 1.34, size = 13, normalized size = 0.68

$$\frac{3}{2}bx^{\frac{2}{3}} - \frac{3a}{x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^(4/3),x, algorithm="maxima")`

[Out] $3/2*b*x^{(2/3)} - 3*a/x^{(1/3)}$

mupad [B] time = 0.03, size = 13, normalized size = 0.68

$$-\frac{6a - 3bx}{2x^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^(4/3), x)
```

```
[Out] -(6*a - 3*b*x)/(2*x^(1/3))
```

sympy [A] time = 0.39, size = 17, normalized size = 0.89

$$-\frac{3a}{\sqrt[3]{x}} + \frac{3bx^{\frac{2}{3}}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**(4/3), x)
```

```
[Out] -3*a/x**(1/3) + 3*b*x**(2/3)/2
```

$$3.657 \quad \int \frac{a+bx}{x^{5/3}} dx$$

Optimal. Leaf size=19

$$3b\sqrt[3]{x} - \frac{3a}{2x^{2/3}}$$

[Out] $-3/2*a/x^{(2/3)}+3*b*x^{(1/3)}$

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$3b\sqrt[3]{x} - \frac{3a}{2x^{2/3}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/x^(5/3), x]

[Out] $(-3*a)/(2*x^{(2/3)}) + 3*b*x^{(1/3)}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^{5/3}} dx &= \int \left(\frac{a}{x^{5/3}} + \frac{b}{x^{2/3}} \right) dx \\ &= -\frac{3a}{2x^{2/3}} + 3b\sqrt[3]{x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 19, normalized size = 1.00

$$3b\sqrt[3]{x} - \frac{3a}{2x^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/x^(5/3), x]

[Out] $(-3*a)/(2*x^{(2/3)}) + 3*b*x^{(1/3)}$

fricas [A] time = 0.46, size = 13, normalized size = 0.68

$$\frac{3(2bx - a)}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^(5/3),x, algorithm="fricas")

[Out] 3/2*(2*b*x - a)/x^(2/3)

giac [A] time = 1.10, size = 13, normalized size = 0.68

$$3bx^{\frac{1}{3}} - \frac{3a}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^(5/3),x, algorithm="giac")

[Out] 3*b*x^(1/3) - 3/2*a/x^(2/3)

maple [A] time = 0.00, size = 12, normalized size = 0.63

$$-\frac{3(-2bx + a)}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^(5/3),x)

[Out] -3/2*(-2*b*x+a)/x^(2/3)

maxima [A] time = 1.30, size = 13, normalized size = 0.68

$$3bx^{\frac{1}{3}} - \frac{3a}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^(5/3),x, algorithm="maxima")

[Out] 3*b*x^(1/3) - 3/2*a/x^(2/3)

mupad [B] time = 0.03, size = 13, normalized size = 0.68

$$-\frac{3a - 6bx}{2x^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/x^(5/3),x)
```

```
[Out] -(3*a - 6*b*x)/(2*x^(2/3))
```

sympy [A] time = 0.45, size = 17, normalized size = 0.89

$$-\frac{3a}{2x^{\frac{2}{3}}} + 3b\sqrt[3]{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/x**(5/3),x)
```

```
[Out] -3*a/(2*x**(2/3)) + 3*b*x**(1/3)
```

3.658 $\int x^{5/3}(a + bx)^2 dx$

Optimal. Leaf size=36

$$\frac{3}{8}a^2x^{8/3} + \frac{6}{11}abx^{11/3} + \frac{3}{14}b^2x^{14/3}$$

[Out] $3/8*a^2*x^{(8/3)}+6/11*a*b*x^{(11/3)}+3/14*b^2*x^{(14/3)}$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3}{8}a^2x^{8/3} + \frac{6}{11}abx^{11/3} + \frac{3}{14}b^2x^{14/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(5/3)}*(a + b*x)^2, x]$

[Out] $(3*a^2*x^{(8/3)})/8 + (6*a*b*x^{(11/3)})/11 + (3*b^2*x^{(14/3)})/14$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{IGtQ}[m, 0] \&\& (!\text{IntegerQ}[n] || (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0]) || \text{LtQ}[9*m + 5*(n + 1), 0]) || \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x^{5/3}(a + bx)^2 dx &= \int (a^2x^{5/3} + 2abx^{8/3} + b^2x^{11/3}) dx \\ &= \frac{3}{8}a^2x^{8/3} + \frac{6}{11}abx^{11/3} + \frac{3}{14}b^2x^{14/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.78

$$\frac{3}{616}x^{8/3}(77a^2 + 112abx + 44b^2x^2)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(5/3)}*(a + b*x)^2, x]$

[Out] $(3*x^{(8/3)}*(77*a^2 + 112*a*b*x + 44*b^2*x^2))/616$

fricas [A] time = 0.45, size = 29, normalized size = 0.81

$$\frac{3}{616} (44b^2x^4 + 112abx^3 + 77a^2x^2)x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)*(b*x+a)^2,x, algorithm="fricas")

[Out] 3/616*(44*b^2*x^4 + 112*a*b*x^3 + 77*a^2*x^2)*x^(2/3)

giac [A] time = 1.04, size = 24, normalized size = 0.67

$$\frac{3}{14} b^2 x^{\frac{14}{3}} + \frac{6}{11} abx^{\frac{11}{3}} + \frac{3}{8} a^2 x^{\frac{8}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)*(b*x+a)^2,x, algorithm="giac")

[Out] 3/14*b^2*x^(14/3) + 6/11*a*b*x^(11/3) + 3/8*a^2*x^(8/3)

maple [A] time = 0.00, size = 25, normalized size = 0.69

$$\frac{3(44b^2x^2 + 112abx + 77a^2)x^{\frac{8}{3}}}{616}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/3)*(b*x+a)^2,x)

[Out] 3/616*x^(8/3)*(44*b^2*x^2+112*a*b*x+77*a^2)

maxima [A] time = 1.31, size = 24, normalized size = 0.67

$$\frac{3}{14} b^2 x^{\frac{14}{3}} + \frac{6}{11} abx^{\frac{11}{3}} + \frac{3}{8} a^2 x^{\frac{8}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)*(b*x+a)^2,x, algorithm="maxima")

[Out] 3/14*b^2*x^(14/3) + 6/11*a*b*x^(11/3) + 3/8*a^2*x^(8/3)

mupad [B] time = 0.04, size = 24, normalized size = 0.67

$$\frac{3x^{8/3}(77a^2 + 112abx + 44b^2x^2)}{616}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/3)*(a + b*x)^2,x)`

[Out] `(3*x^(8/3)*(77*a^2 + 44*b^2*x^2 + 112*a*b*x))/616`

sympy [A] time = 3.75, size = 34, normalized size = 0.94

$$\frac{3a^2x^{\frac{8}{3}}}{8} + \frac{6abx^{\frac{11}{3}}}{11} + \frac{3b^2x^{\frac{14}{3}}}{14}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/3)*(b*x+a)**2,x)`

[Out] `3*a**2*x**(8/3)/8 + 6*a*b*x**(11/3)/11 + 3*b**2*x**(14/3)/14`

3.659 $\int x^{4/3}(a + bx)^2 dx$

Optimal. Leaf size=36

$$\frac{3}{7}a^2x^{7/3} + \frac{3}{5}abx^{10/3} + \frac{3}{13}b^2x^{13/3}$$

[Out] $3/7*a^2*x^{(7/3)}+3/5*a*b*x^{(10/3)}+3/13*b^2*x^{(13/3)}$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3}{7}a^2x^{7/3} + \frac{3}{5}abx^{10/3} + \frac{3}{13}b^2x^{13/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(4/3)}*(a + b*x)^2, x]$

[Out] $(3*a^2*x^{(7/3)})/7 + (3*a*b*x^{(10/3)})/5 + (3*b^2*x^{(13/3)})/13$

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^{4/3}(a + bx)^2 dx &= \int (a^2x^{4/3} + 2abx^{7/3} + b^2x^{10/3}) dx \\ &= \frac{3}{7}a^2x^{7/3} + \frac{3}{5}abx^{10/3} + \frac{3}{13}b^2x^{13/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.78

$$\frac{3}{455}x^{7/3} (65a^2 + 91abx + 35b^2x^2)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(4/3)}*(a + b*x)^2, x]$

[Out] $(3*x^{(7/3)}*(65*a^2 + 91*a*b*x + 35*b^2*x^2))/455$

fricas [A] time = 0.43, size = 29, normalized size = 0.81

$$\frac{3}{455} (35 b^2 x^4 + 91 a b x^3 + 65 a^2 x^2) x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)*(b*x+a)^2,x, algorithm="fricas")

[Out] 3/455*(35*b^2*x^4 + 91*a*b*x^3 + 65*a^2*x^2)*x^(1/3)

giac [A] time = 1.06, size = 24, normalized size = 0.67

$$\frac{3}{13} b^2 x^{\frac{13}{3}} + \frac{3}{5} a b x^{\frac{10}{3}} + \frac{3}{7} a^2 x^{\frac{7}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)*(b*x+a)^2,x, algorithm="giac")

[Out] 3/13*b^2*x^(13/3) + 3/5*a*b*x^(10/3) + 3/7*a^2*x^(7/3)

maple [A] time = 0.00, size = 25, normalized size = 0.69

$$\frac{3(35b^2x^2 + 91abx + 65a^2)x^{\frac{7}{3}}}{455}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(4/3)*(b*x+a)^2,x)

[Out] 3/455*x^(7/3)*(35*b^2*x^2+91*a*b*x+65*a^2)

maxima [A] time = 1.32, size = 24, normalized size = 0.67

$$\frac{3}{13} b^2 x^{\frac{13}{3}} + \frac{3}{5} a b x^{\frac{10}{3}} + \frac{3}{7} a^2 x^{\frac{7}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)*(b*x+a)^2,x, algorithm="maxima")

[Out] 3/13*b^2*x^(13/3) + 3/5*a*b*x^(10/3) + 3/7*a^2*x^(7/3)

mupad [B] time = 0.04, size = 24, normalized size = 0.67

$$\frac{3x^{7/3}(65a^2 + 91abx + 35b^2x^2)}{455}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(4/3)*(a + b*x)^2,x)`

[Out] `(3*x^(7/3)*(65*a^2 + 35*b^2*x^2 + 91*a*b*x))/455`

sympy [A] time = 2.65, size = 34, normalized size = 0.94

$$\frac{3a^2x^{\frac{7}{3}}}{7} + \frac{3abx^{\frac{10}{3}}}{5} + \frac{3b^2x^{\frac{13}{3}}}{13}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(4/3)*(b*x+a)**2,x)`

[Out] `3*a**2*x**(7/3)/7 + 3*a*b*x**(10/3)/5 + 3*b**2*x**(13/3)/13`

3.660 $\int x^{2/3}(a + bx)^2 dx$

Optimal. Leaf size=36

$$\frac{3}{5}a^2x^{5/3} + \frac{3}{4}abx^{8/3} + \frac{3}{11}b^2x^{11/3}$$

[Out] $3/5*a^2*x^{(5/3)}+3/4*a*b*x^{(8/3)}+3/11*b^2*x^{(11/3)}$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3}{5}a^2x^{5/3} + \frac{3}{4}abx^{8/3} + \frac{3}{11}b^2x^{11/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(2/3)}*(a + b*x)^2, x]$

[Out] $(3*a^2*x^{(5/3)})/5 + (3*a*b*x^{(8/3)})/4 + (3*b^2*x^{(11/3)})/11$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0]) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0]) \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x^{2/3}(a + bx)^2 dx &= \int (a^2x^{2/3} + 2abx^{5/3} + b^2x^{8/3}) dx \\ &= \frac{3}{5}a^2x^{5/3} + \frac{3}{4}abx^{8/3} + \frac{3}{11}b^2x^{11/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.78

$$\frac{3}{220}x^{5/3} (44a^2 + 55abx + 20b^2x^2)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(2/3)}*(a + b*x)^2, x]$

[Out] $(3*x^{(5/3)}*(44*a^2 + 55*a*b*x + 20*b^2*x^2))/220$

fricas [A] time = 0.49, size = 27, normalized size = 0.75

$$\frac{3}{220} (20 b^2 x^3 + 55 a b x^2 + 44 a^2 x) x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)*(b*x+a)^2,x, algorithm="fricas")

[Out] 3/220*(20*b^2*x^3 + 55*a*b*x^2 + 44*a^2*x)*x^(2/3)

giac [A] time = 1.05, size = 24, normalized size = 0.67

$$\frac{3}{11} b^2 x^{\frac{11}{3}} + \frac{3}{4} a b x^{\frac{8}{3}} + \frac{3}{5} a^2 x^{\frac{5}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)*(b*x+a)^2,x, algorithm="giac")

[Out] 3/11*b^2*x^(11/3) + 3/4*a*b*x^(8/3) + 3/5*a^2*x^(5/3)

maple [A] time = 0.00, size = 25, normalized size = 0.69

$$\frac{3 (20 b^2 x^2 + 55 a b x + 44 a^2) x^{\frac{5}{3}}}{220}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(2/3)*(b*x+a)^2,x)

[Out] 3/220*x^(5/3)*(20*b^2*x^2+55*a*b*x+44*a^2)

maxima [A] time = 1.32, size = 24, normalized size = 0.67

$$\frac{3}{11} b^2 x^{\frac{11}{3}} + \frac{3}{4} a b x^{\frac{8}{3}} + \frac{3}{5} a^2 x^{\frac{5}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)*(b*x+a)^2,x, algorithm="maxima")

[Out] 3/11*b^2*x^(11/3) + 3/4*a*b*x^(8/3) + 3/5*a^2*x^(5/3)

mupad [B] time = 0.04, size = 24, normalized size = 0.67

$$\frac{3 x^{5/3} (44 a^2 + 55 a b x + 20 b^2 x^2)}{220}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(2/3)*(a + b*x)^2,x)`

[Out] $(3*x^{(5/3)}*(44*a^2 + 20*b^2*x^2 + 55*a*b*x))/220$

sympy [A] time = 1.06, size = 34, normalized size = 0.94

$$\frac{3a^2x^{\frac{5}{3}}}{5} + \frac{3abx^{\frac{8}{3}}}{4} + \frac{3b^2x^{\frac{11}{3}}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(2/3)*(b*x+a)**2,x)`

[Out] $3*a**2*x**(5/3)/5 + 3*a*b*x**(8/3)/4 + 3*b**2*x**(11/3)/11$

3.661 $\int \sqrt[3]{x} (a + bx)^2 dx$

Optimal. Leaf size=36

$$\frac{3}{4}a^2x^{4/3} + \frac{6}{7}abx^{7/3} + \frac{3}{10}b^2x^{10/3}$$

[Out] $3/4*a^2*x^{(4/3)}+6/7*a*b*x^{(7/3)}+3/10*b^2*x^{(10/3)}$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3}{4}a^2x^{4/3} + \frac{6}{7}abx^{7/3} + \frac{3}{10}b^2x^{10/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(1/3)}*(a + b*x)^2, x]$

[Out] $(3*a^2*x^{(4/3)})/4 + (6*a*b*x^{(7/3)})/7 + (3*b^2*x^{(10/3)})/10$

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \sqrt[3]{x} (a + bx)^2 dx &= \int (a^2 \sqrt[3]{x} + 2abx^{4/3} + b^2x^{7/3}) dx \\ &= \frac{3}{4}a^2x^{4/3} + \frac{6}{7}abx^{7/3} + \frac{3}{10}b^2x^{10/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.78

$$\frac{3}{140}x^{4/3} (35a^2 + 40abx + 14b^2x^2)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(1/3)}*(a + b*x)^2, x]$

[Out] $(3*x^{(4/3)}*(35*a^2 + 40*a*b*x + 14*b^2*x^2))/140$

fricas [A] time = 0.44, size = 27, normalized size = 0.75

$$\frac{3}{140} (14b^2x^3 + 40abx^2 + 35a^2x)x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)*(b*x+a)^2,x, algorithm="fricas")

[Out] 3/140*(14*b^2*x^3 + 40*a*b*x^2 + 35*a^2*x)*x^(1/3)

giac [A] time = 1.04, size = 24, normalized size = 0.67

$$\frac{3}{10} b^2 x^{\frac{10}{3}} + \frac{6}{7} abx^{\frac{7}{3}} + \frac{3}{4} a^2 x^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)*(b*x+a)^2,x, algorithm="giac")

[Out] 3/10*b^2*x^(10/3) + 6/7*a*b*x^(7/3) + 3/4*a^2*x^(4/3)

maple [A] time = 0.01, size = 25, normalized size = 0.69

$$\frac{3(14b^2x^2 + 40abx + 35a^2)x^{\frac{4}{3}}}{140}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/3)*(b*x+a)^2,x)

[Out] 3/140*x^(4/3)*(14*b^2*x^2+40*a*b*x+35*a^2)

maxima [A] time = 1.28, size = 24, normalized size = 0.67

$$\frac{3}{10} b^2 x^{\frac{10}{3}} + \frac{6}{7} abx^{\frac{7}{3}} + \frac{3}{4} a^2 x^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)*(b*x+a)^2,x, algorithm="maxima")

[Out] 3/10*b^2*x^(10/3) + 6/7*a*b*x^(7/3) + 3/4*a^2*x^(4/3)

mupad [B] time = 0.04, size = 24, normalized size = 0.67

$$\frac{3x^{4/3}(35a^2 + 40abx + 14b^2x^2)}{140}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(1/3)*(a + b*x)^2,x)
```

```
[Out] (3*x^(4/3)*(35*a^2 + 14*b^2*x^2 + 40*a*b*x))/140
```

```
sympy [C] time = 2.22, size = 2633, normalized size = 73.14
```

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(1/3)*(b*x+a)**2,x)
```

```
[Out] Piecewise((27*a**(34/3)*(-1 + b*(a/b + x)/a)**(1/3)*exp(2*I*pi/3)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) + 27*a**(34/3)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) - 72*a**(31/3)*b*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)*exp(2*I*pi/3)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) - 81*a**(31/3)*b*(a/b + x)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) + 60*a**(28/3)*b**2*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**2*exp(2*I*pi/3)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) + 81*a**(28/3)*b**2*(a/b + x)**2/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) - 60*a**(25/3)*b**3*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**3*exp(2*I*pi/3)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) - 27*a**(25/3)*b**3*(a/b + x)**3/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) + 135*a**(22/3)*b**4*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**4*exp(2*I*pi/3)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) - 132*a**(19/3)*b**5*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**5*exp(2*I*pi/3)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) + 42*a**(16/3)*b**6*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**6*exp(2*I*pi/3)/(-140*a**8*b**(4/3)*exp(2*I*pi
```



```

/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b +
x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)), Abs(
b*(a/b + x)/a) > 1), (-27*a**(34/3)*(1 - b*(a/b + x)/a)**(1/3)/(-140*a**8*b
**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**
6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*ex
p(2*I*pi/3)) + 27*a**(34/3)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b*
*(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi
/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) + 72*a**(31/3)*b*(1 -
b*(a/b + x)/a)**(1/3)*(a/b + x)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**
7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*
I*pi/3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) - 81*a**(31/3)*b*(
a/b + x)/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*ex
p(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(
13/3)*(a/b + x)**3*exp(2*I*pi/3)) - 60*a**(28/3)*b**2*(1 - b*(a/b + x)/a)**
(1/3)*(a/b + x)**2/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a
/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140
*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) + 81*a**(28/3)*b**2*(a/b + x)**
2/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*p
i/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(
a/b + x)**3*exp(2*I*pi/3)) + 60*a**(25/3)*b**3*(1 - b*(a/b + x)/a)**(1/3)*(
a/b + x)**3/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)
*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b
**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) - 27*a**(25/3)*b**3*(a/b + x)**3/(-140
*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2*I*pi/3) -
420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/3)*(a/b + x
)**3*exp(2*I*pi/3)) - 135*a**(22/3)*b**4*(1 - b*(a/b + x)/a)**(1/3)*(a/b +
x)**4/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b + x)*exp(2
*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a**5*b**(13/
3)*(a/b + x)**3*exp(2*I*pi/3)) + 132*a**(19/3)*b**5*(1 - b*(a/b + x)/a)**(1
/3)*(a/b + x)**5/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**(7/3)*(a/b
+ x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/3) + 140*a
**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)) - 42*a**(16/3)*b**6*(1 - b*(a/b +
x)/a)**(1/3)*(a/b + x)**6/(-140*a**8*b**(4/3)*exp(2*I*pi/3) + 420*a**7*b**
(7/3)*(a/b + x)*exp(2*I*pi/3) - 420*a**6*b**(10/3)*(a/b + x)**2*exp(2*I*pi/
3) + 140*a**5*b**(13/3)*(a/b + x)**3*exp(2*I*pi/3)), True))

```

$$3.662 \quad \int \frac{(a+bx)^2}{\sqrt[3]{x}} dx$$

Optimal. Leaf size=36

$$\frac{3}{2}a^2x^{2/3} + \frac{6}{5}abx^{5/3} + \frac{3}{8}b^2x^{8/3}$$

[Out] $3/2*a^2*x^{(2/3)}+6/5*a*b*x^{(5/3)}+3/8*b^2*x^{(8/3)}$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3}{2}a^2x^{2/3} + \frac{6}{5}abx^{5/3} + \frac{3}{8}b^2x^{8/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^(1/3), x]

[Out] $(3*a^2*x^{(2/3)})/2 + (6*a*b*x^{(5/3)})/5 + (3*b^2*x^{(8/3)})/8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{\sqrt[3]{x}} dx &= \int \left(\frac{a^2}{\sqrt[3]{x}} + 2abx^{2/3} + b^2x^{5/3} \right) dx \\ &= \frac{3}{2}a^2x^{2/3} + \frac{6}{5}abx^{5/3} + \frac{3}{8}b^2x^{8/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.78

$$\frac{3}{40}x^{2/3} (20a^2 + 16abx + 5b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^(1/3), x]

[Out] $(3x^{2/3}(20a^2 + 16abx + 5b^2x^2))/40$

fricas [A] time = 0.46, size = 24, normalized size = 0.67

$$\frac{3}{40} (5b^2x^2 + 16abx + 20a^2)x^{2/3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^(1/3),x, algorithm="fricas")`

[Out] $3/40*(5*b^2*x^2 + 16*a*b*x + 20*a^2)*x^{2/3}$

giac [A] time = 1.11, size = 24, normalized size = 0.67

$$\frac{3}{8}b^2x^{8/3} + \frac{6}{5}abx^{5/3} + \frac{3}{2}a^2x^{2/3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^(1/3),x, algorithm="giac")`

[Out] $3/8*b^2*x^{8/3} + 6/5*a*b*x^{5/3} + 3/2*a^2*x^{2/3}$

maple [A] time = 0.00, size = 25, normalized size = 0.69

$$\frac{3(5b^2x^2 + 16abx + 20a^2)x^{2/3}}{40}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^(1/3),x)`

[Out] $3/40*x^{2/3}*(5*b^2*x^2+16*a*b*x+20*a^2)$

maxima [A] time = 1.32, size = 24, normalized size = 0.67

$$\frac{3}{8}b^2x^{8/3} + \frac{6}{5}abx^{5/3} + \frac{3}{2}a^2x^{2/3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^(1/3),x, algorithm="maxima")`

[Out] $3/8*b^2*x^{8/3} + 6/5*a*b*x^{5/3} + 3/2*a^2*x^{2/3}$

mupad [B] time = 0.04, size = 24, normalized size = 0.67

$$\frac{3x^{2/3}(20a^2 + 16abx + 5b^2x^2)}{40}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^2/x^{(1/3)}, x)$

[Out] $(3*x^{(2/3)}*(20*a^2 + 5*b^2*x^2 + 16*a*b*x))/40$

sympy [C] time = 2.05, size = 1765, normalized size = 49.03

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)**2/x**(1/3), x)$

[Out] $\text{Piecewise}((-27*a^{(32/3)}*(-1 + b*(a/b + x)/a)**(2/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) + 27*a^{(32/3)}*\exp(2*I*\pi/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) + 63*a^{(29/3)}*b*(-1 + b*(a/b + x)/a)**(2/3)*(a/b + x)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) - 81*a^{(29/3)}*b*(a/b + x)*\exp(2*I*\pi/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) - 42*a^{(26/3)}*b**2*(-1 + b*(a/b + x)/a)**(2/3)*(a/b + x)**2/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) + 81*a^{(26/3)}*b**2*(a/b + x)**2*\exp(2*I*\pi/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) + 18*a^{(23/3)}*b**3*(-1 + b*(a/b + x)/a)**(2/3)*(a/b + x)**3/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) - 27*a^{(23/3)}*b**3*(a/b + x)**3*\exp(2*I*\pi/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) - 27*a^{(20/3)}*b**4*(-1 + b*(a/b + x)/a)**(2/3)*(a/b + x)**4/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) + 15*a^{(17/3)}*b**5*(-1 + b*(a/b + x)/a)**(2/3)*(a/b + x)**5/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3), $\text{Abs}(b*(a/b + x)/a) > 1$), $(-27*a^{(32/3)}*(1 - b*(a/b + x)/a)**(2/3)*\exp(2*I*\pi/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) + 27*a^{(32/3)}*\exp(2*I*\pi/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) + 63*a^{(29/3)}*b*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)*\exp(2*I*\pi/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) - 81*a^{(29/3)}*b*(a/b + x)*\exp(2*I*\pi/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) - 42*a^{(26/3)}*b**2*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**2/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) + 81*a^{(26/3)}*b**2*(a/b + x)**2*\exp(2*I*\pi/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) + 18*a^{(23/3)}*b**3*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**3/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) - 27*a^{(23/3)}*b**3*(a/b + x)**3*\exp(2*I*\pi/3)/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) - 27*a^{(20/3)}*b**4*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**4/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3) + 15*a^{(17/3)}*b**5*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**5/(-40*a^{(8/3)}*b^{(2/3)} + 120*a^{(7/3)}*b^{(5/3)}*(a/b + x) - 120*a^{(6/3)}*b^{(8/3)}*(a/b + x)**2 + 40*a^{(5/3)}*b^{(11/3)}*(a/b + x)**3)$$

$$\begin{aligned}
&*(2/3)*(a/b + x)**2*\exp(2*I*pi/3)/(-40*a**8*b**(2/3) + 120*a**7*b**(5/3)*(a/b + x) - 120*a**6*b**(8/3)*(a/b + x)**2 + 40*a**5*b**(11/3)*(a/b + x)**3) \\
&+ 81*a**(26/3)*b**2*(a/b + x)**2*\exp(2*I*pi/3)/(-40*a**8*b**(2/3) + 120*a**7*b**(5/3)*(a/b + x) - 120*a**6*b**(8/3)*(a/b + x)**2 + 40*a**5*b**(11/3)*(a/b + x)**3) \\
&+ 18*a**(23/3)*b**3*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**3*\exp(2*I*pi/3)/(-40*a**8*b**(2/3) + 120*a**7*b**(5/3)*(a/b + x) - 120*a**6*b**(8/3)*(a/b + x)**2 + 40*a**5*b**(11/3)*(a/b + x)**3) - 27*a**(23/3)*b**3*(a/b + x)**3*\exp(2*I*pi/3)/(-40*a**8*b**(2/3) + 120*a**7*b**(5/3)*(a/b + x) - 120*a**6*b**(8/3)*(a/b + x)**2 + 40*a**5*b**(11/3)*(a/b + x)**3) - 27*a**(20/3)*b**4*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**4*\exp(2*I*pi/3)/(-40*a**8*b**(2/3) + 120*a**7*b**(5/3)*(a/b + x) - 120*a**6*b**(8/3)*(a/b + x)**2 + 40*a**5*b**(11/3)*(a/b + x)**3) + 15*a**(17/3)*b**5*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**5*\exp(2*I*pi/3)/(-40*a**8*b**(2/3) + 120*a**7*b**(5/3)*(a/b + x) - 120*a**6*b**(8/3)*(a/b + x)**2 + 40*a**5*b**(11/3)*(a/b + x)**3), True)
\end{aligned}$$

$$3.663 \quad \int \frac{(a+bx)^2}{x^{2/3}} dx$$

Optimal. Leaf size=34

$$3a^2\sqrt[3]{x} + \frac{3}{2}abx^{4/3} + \frac{3}{7}b^2x^{7/3}$$

[Out] $3a^2x^{1/3} + 3/2*a*b*x^{4/3} + 3/7*b^2*x^{7/3}$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$3a^2\sqrt[3]{x} + \frac{3}{2}abx^{4/3} + \frac{3}{7}b^2x^{7/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^(2/3), x]

[Out] $3a^2x^{1/3} + (3a*b*x^{4/3})/2 + (3*b^2*x^{7/3})/7$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^{2/3}} dx &= \int \left(\frac{a^2}{x^{2/3}} + 2ab\sqrt[3]{x} + b^2x^{4/3} \right) dx \\ &= 3a^2\sqrt[3]{x} + \frac{3}{2}abx^{4/3} + \frac{3}{7}b^2x^{7/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.82

$$\frac{3}{14}\sqrt[3]{x} (14a^2 + 7abx + 2b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^(2/3), x]

[Out] $(3*x^{1/3}*(14*a^2 + 7*a*b*x + 2*b^2*x^2))/14$

fricas [A] time = 0.44, size = 24, normalized size = 0.71

$$\frac{3}{14} (2b^2x^2 + 7abx + 14a^2)x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(2/3),x, algorithm="fricas")

[Out] 3/14*(2*b^2*x^2 + 7*a*b*x + 14*a^2)*x^(1/3)

giac [A] time = 0.92, size = 24, normalized size = 0.71

$$\frac{3}{7}b^2x^{\frac{7}{3}} + \frac{3}{2}abx^{\frac{4}{3}} + 3a^2x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(2/3),x, algorithm="giac")

[Out] 3/7*b^2*x^(7/3) + 3/2*a*b*x^(4/3) + 3*a^2*x^(1/3)

maple [A] time = 0.01, size = 25, normalized size = 0.74

$$\frac{3(2b^2x^2 + 7abx + 14a^2)x^{\frac{1}{3}}}{14}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/x^(2/3),x)

[Out] 3/14*x^(1/3)*(2*b^2*x^2+7*a*b*x+14*a^2)

maxima [A] time = 1.38, size = 24, normalized size = 0.71

$$\frac{3}{7}b^2x^{\frac{7}{3}} + \frac{3}{2}abx^{\frac{4}{3}} + 3a^2x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(2/3),x, algorithm="maxima")

[Out] 3/7*b^2*x^(7/3) + 3/2*a*b*x^(4/3) + 3*a^2*x^(1/3)

mupad [B] time = 0.03, size = 24, normalized size = 0.71

$$\frac{3x^{1/3}(14a^2 + 7abx + 2b^2x^2)}{14}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^2/x^{(2/3)}, x)$

[Out] $(3*x^{(1/3)}*(14*a^2 + 2*b^2*x^2 + 7*a*b*x))/14$

sympy [C] time = 2.08, size = 1741, normalized size = 51.21

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)**2/x**(2/3), x)$

[Out] $\text{Piecewise}((-27*a**(31/3)*(-1 + b*(a/b + x)/a)**(1/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 27*a**(31/3)*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 72*a**(28/3)*b*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) - 81*a**(28/3)*b*(a/b + x)*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) - 60*a**(25/3)*b**2*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**2/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 81*a**(25/3)*b**2*(a/b + x)**2*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 18*a**(22/3)*b**3*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**3/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) - 27*a**(22/3)*b**3*(a/b + x)**3*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) - 9*a**(19/3)*b**4*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**4/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 6*a**(16/3)*b**5*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**5/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3), $\text{Abs}(b*(a/b + x)/a) > 1$), $(-27*a**(31/3)*(1 - b*(a/b + x)/a)**(1/3)*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 27*a**(31/3)*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 72*a**(28/3)*b*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) - 81*a**(28/3)*b*(a/b + x)*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) - 60*a**(25/3)*b**2*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**2*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 81*a**(25/3)*b**2*(a/b + x)**2*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 18*a**(22/3)*b**3*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**3*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) - 27*a**(22/3)*b**3*(a/b + x)**3*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) - 9*a**(19/3)*b**4*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**4*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 6*a**(16/3)*b**5*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**5*\exp(I*\pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3)$$


```

1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5
*b**(10/3)*(a/b + x)**3) + 81*a**(25/3)*b**2*(a/b + x)**2*exp(I*pi/3)/(-14*
a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2
+ 14*a**5*b**(10/3)*(a/b + x)**3) + 18*a**(22/3)*b**3*(1 - b*(a/b + x)/a)**
(1/3)*(a/b + x)**3*exp(I*pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b +
x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) - 27*
a**(22/3)*b**3*(a/b + x)**3*exp(I*pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/
3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)*
*3) - 9*a**(19/3)*b**4*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**4*exp(I*pi/3)/
(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a/b + x) - 42*a**6*b**(7/3)*(a/b + x
)**2 + 14*a**5*b**(10/3)*(a/b + x)**3) + 6*a**(16/3)*b**5*(1 - b*(a/b + x)/
a)**(1/3)*(a/b + x)**5*exp(I*pi/3)/(-14*a**8*b**(1/3) + 42*a**7*b**(4/3)*(a
/b + x) - 42*a**6*b**(7/3)*(a/b + x)**2 + 14*a**5*b**(10/3)*(a/b + x)**3),
True))

```

$$3.664 \quad \int \frac{(a+bx)^2}{x^{4/3}} dx$$

Optimal. Leaf size=32

$$-\frac{3a^2}{\sqrt[3]{x}} + 3abx^{2/3} + \frac{3}{5}b^2x^{5/3}$$

[Out] $-3*a^2/x^{(1/3)}+3*a*b*x^{(2/3)}+3/5*b^2*x^{(5/3)}$

Rubi [A] time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{3a^2}{\sqrt[3]{x}} + 3abx^{2/3} + \frac{3}{5}b^2x^{5/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^2/x^{(4/3)}, x]$

[Out] $(-3*a^2)/x^{(1/3)} + 3*a*b*x^{(2/3)} + (3*b^2*x^{(5/3)})/5$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)*((c_. + (d_.)*(x_))^{(n_.)}, x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0]) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^{4/3}} dx &= \int \left(\frac{a^2}{x^{4/3}} + \frac{2ab}{\sqrt[3]{x}} + b^2x^{2/3} \right) dx \\ &= -\frac{3a^2}{\sqrt[3]{x}} + 3abx^{2/3} + \frac{3}{5}b^2x^{5/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.84

$$\frac{3(-5a^2 + 5abx + b^2x^2)}{5\sqrt[3]{x}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^(4/3),x]

[Out] (3*(-5*a^2 + 5*a*b*x + b^2*x^2))/(5*x^(1/3))

fricas [A] time = 0.46, size = 23, normalized size = 0.72

$$\frac{3(b^2x^2 + 5abx - 5a^2)}{5x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(4/3),x, algorithm="fricas")

[Out] 3/5*(b^2*x^2 + 5*a*b*x - 5*a^2)/x^(1/3)

giac [A] time = 1.17, size = 24, normalized size = 0.75

$$\frac{3}{5}b^2x^{\frac{5}{3}} + 3abx^{\frac{2}{3}} - \frac{3a^2}{x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(4/3),x, algorithm="giac")

[Out] 3/5*b^2*x^(5/3) + 3*a*b*x^(2/3) - 3*a^2/x^(1/3)

maple [A] time = 0.00, size = 25, normalized size = 0.78

$$-\frac{3(-b^2x^2 - 5abx + 5a^2)}{5x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/x^(4/3),x)

[Out] -3/5*(-b^2*x^2-5*a*b*x+5*a^2)/x^(1/3)

maxima [A] time = 1.36, size = 24, normalized size = 0.75

$$\frac{3}{5}b^2x^{\frac{5}{3}} + 3abx^{\frac{2}{3}} - \frac{3a^2}{x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^(4/3),x, algorithm="maxima")

[Out] 3/5*b^2*x^(5/3) + 3*a*b*x^(2/3) - 3*a^2/x^(1/3)


```

6*b**2*(a/b + x)**2*exp(I*pi/3) + 5*a**5*b**3*(a/b + x)**3*exp(I*pi/3)) - 6
3*a**(26/3)*b**(4/3)*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)/(-5*a**8*exp(I*pi
/3) + 15*a**7*b*(a/b + x)*exp(I*pi/3) - 15*a**6*b**2*(a/b + x)**2*exp(I*pi/
3) + 5*a**5*b**3*(a/b + x)**3*exp(I*pi/3)) + 81*a**(26/3)*b**(4/3)*(a/b + x
)/(-5*a**8*exp(I*pi/3) + 15*a**7*b*(a/b + x)*exp(I*pi/3) - 15*a**6*b**2*(a/
b + x)**2*exp(I*pi/3) + 5*a**5*b**3*(a/b + x)**3*exp(I*pi/3)) + 42*a**(23/3
)*b**(7/3)*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**2/(-5*a**8*exp(I*pi/3) + 1
5*a**7*b*(a/b + x)*exp(I*pi/3) - 15*a**6*b**2*(a/b + x)**2*exp(I*pi/3) + 5*
a**5*b**3*(a/b + x)**3*exp(I*pi/3)) - 81*a**(23/3)*b**(7/3)*(a/b + x)**2/(-
5*a**8*exp(I*pi/3) + 15*a**7*b*(a/b + x)*exp(I*pi/3) - 15*a**6*b**2*(a/b +
x)**2*exp(I*pi/3) + 5*a**5*b**3*(a/b + x)**3*exp(I*pi/3)) - 3*a**(20/3)*b**
(10/3)*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**3/(-5*a**8*exp(I*pi/3) + 15*a*
**7*b*(a/b + x)*exp(I*pi/3) - 15*a**6*b**2*(a/b + x)**2*exp(I*pi/3) + 5*a**5
*b**3*(a/b + x)**3*exp(I*pi/3)) + 27*a**(20/3)*b**(10/3)*(a/b + x)**3/(-5*a
**8*exp(I*pi/3) + 15*a**7*b*(a/b + x)*exp(I*pi/3) - 15*a**6*b**2*(a/b + x)*
**2*exp(I*pi/3) + 5*a**5*b**3*(a/b + x)**3*exp(I*pi/3)) - 3*a**(17/3)*b**(13
/3)*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**4/(-5*a**8*exp(I*pi/3) + 15*a**7*
b*(a/b + x)*exp(I*pi/3) - 15*a**6*b**2*(a/b + x)**2*exp(I*pi/3) + 5*a**5*b*
**3*(a/b + x)**3*exp(I*pi/3)), True))

```

$$3.665 \quad \int \frac{(a+bx)^2}{x^{5/3}} dx$$

Optimal. Leaf size=34

$$-\frac{3a^2}{2x^{2/3}} + 6ab\sqrt[3]{x} + \frac{3}{4}b^2x^{4/3}$$

[Out] $-3/2*a^2/x^{(2/3)}+6*a*b*x^{(1/3)}+3/4*b^2*x^{(4/3)}$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{3a^2}{2x^{2/3}} + 6ab\sqrt[3]{x} + \frac{3}{4}b^2x^{4/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/x^(5/3), x]

[Out] $(-3*a^2)/(2*x^{(2/3)}) + 6*a*b*x^{(1/3)} + (3*b^2*x^{(4/3)})/4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^{5/3}} dx &= \int \left(\frac{a^2}{x^{5/3}} + \frac{2ab}{x^{2/3}} + b^2\sqrt[3]{x} \right) dx \\ &= -\frac{3a^2}{2x^{2/3}} + 6ab\sqrt[3]{x} + \frac{3}{4}b^2x^{4/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.79

$$\frac{3(-2a^2 + 8abx + b^2x^2)}{4x^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/x^(5/3), x]

[Out] $(3*(-2*a^2 + 8*a*b*x + b^2*x^2))/(4*x^{(2/3)})$

fricas [A] time = 0.45, size = 23, normalized size = 0.68

$$\frac{3(b^2x^2 + 8abx - 2a^2)}{4x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^(5/3),x, algorithm="fricas")`

[Out] $3/4*(b^2*x^2 + 8*a*b*x - 2*a^2)/x^{(2/3)}$

giac [A] time = 1.22, size = 24, normalized size = 0.71

$$\frac{3}{4}b^2x^{\frac{4}{3}} + 6abx^{\frac{1}{3}} - \frac{3a^2}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^(5/3),x, algorithm="giac")`

[Out] $3/4*b^2*x^{(4/3)} + 6*a*b*x^{(1/3)} - 3/2*a^2/x^{(2/3)}$

maple [A] time = 0.00, size = 25, normalized size = 0.74

$$-\frac{3(-b^2x^2 - 8abx + 2a^2)}{4x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^(5/3),x)`

[Out] $-3/4*(-b^2*x^2-8*a*b*x+2*a^2)/x^{(2/3)}$

maxima [A] time = 1.35, size = 24, normalized size = 0.71

$$\frac{3}{4}b^2x^{\frac{4}{3}} + 6abx^{\frac{1}{3}} - \frac{3a^2}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^(5/3),x, algorithm="maxima")`

[Out] $3/4*b^2*x^{(4/3)} + 6*a*b*x^{(1/3)} - 3/2*a^2/x^{(2/3)}$

mupad [B] time = 0.04, size = 24, normalized size = 0.71

$$\frac{-6a^2 + 24abx + 3b^2x^2}{4x^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/x^(5/3), x)`

[Out] `(3*b^2*x^2 - 6*a^2 + 24*a*b*x)/(4*x^(2/3))`

sympy [C] time = 2.06, size = 1957, normalized size = 57.56

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**(5/3), x)`

[Out] `Piecewise((-27*a**(28/3)*b**(2/3)*(-1 + b*(a/b + x)/a)**(1/3)*exp(2*I*pi/3)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) - 27*a**(28/3)*b**(2/3)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) + 72*a**(25/3)*b**(5/3)*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)*exp(2*I*pi/3)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) + 81*a**(25/3)*b**(5/3)*(a/b + x)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) - 60*a**(22/3)*b**(8/3)*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**2*exp(2*I*pi/3)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) - 81*a**(22/3)*b**(8/3)*(a/b + x)**2/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) + 12*a**(19/3)*b**(11/3)*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**3*exp(2*I*pi/3)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) + 27*a**(19/3)*b**(11/3)*(a/b + x)**3/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) + 3*a**(16/3)*b**(14/3)*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**4*exp(2*I*pi/3)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)), Abs(b*(a/b + x)/a) > 1), (27*a**(28/3)*b**(2/3)*(1 - b*(a/b + x)/a)**(1/3)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)`


```

3)) - 27*a**(28/3)*b**(2/3)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) - 72*a**(25/3)*b**(5/3)*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) + 81*a**(25/3)*b**(5/3)*(a/b + x)/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) + 60*a**(22/3)*b**(8/3)*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**2/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) - 81*a**(22/3)*b**(8/3)*(a/b + x)**2/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) - 12*a**(19/3)*b**(11/3)*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**3/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) + 27*a**(19/3)*b**(11/3)*(a/b + x)**3/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)) - 3*a**(16/3)*b**(14/3)*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**4/(-4*a**8*exp(2*I*pi/3) + 12*a**7*b*(a/b + x)*exp(2*I*pi/3) - 12*a**6*b**2*(a/b + x)**2*exp(2*I*pi/3) + 4*a**5*b**3*(a/b + x)**3*exp(2*I*pi/3)), True))

```

3.666 $\int x^{5/3}(a + bx)^3 dx$

Optimal. Leaf size=51

$$\frac{3}{8}a^3x^{8/3} + \frac{9}{11}a^2bx^{11/3} + \frac{9}{14}ab^2x^{14/3} + \frac{3}{17}b^3x^{17/3}$$

[Out] $3/8*a^3*x^(8/3)+9/11*a^2*b*x^(11/3)+9/14*a*b^2*x^(14/3)+3/17*b^3*x^(17/3)$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9}{11}a^2bx^{11/3} + \frac{3}{8}a^3x^{8/3} + \frac{9}{14}ab^2x^{14/3} + \frac{3}{17}b^3x^{17/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(5/3)}*(a + b*x)^3, x]$

[Out] $(3*a^3*x^(8/3))/8 + (9*a^2*b*x^(11/3))/11 + (9*a*b^2*x^(14/3))/14 + (3*b^3*x^(17/3))/17$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^(m_.)*((c_.) + (d_.)*(x_.))^(n_.), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ $\text{FreeQ}\{a, b, c, d, n\}, x\} \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (\ !\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0]) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x^{5/3}(a + bx)^3 dx &= \int (a^3x^{5/3} + 3a^2bx^{8/3} + 3ab^2x^{11/3} + b^3x^{14/3}) dx \\ &= \frac{3}{8}a^3x^{8/3} + \frac{9}{11}a^2bx^{11/3} + \frac{9}{14}ab^2x^{14/3} + \frac{3}{17}b^3x^{17/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.76

$$\frac{3x^{8/3} (1309a^3 + 2856a^2bx + 2244ab^2x^2 + 616b^3x^3)}{10472}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/3)*(a + b*x)^3,x]

[Out] (3*x^(8/3)*(1309*a^3 + 2856*a^2*b*x + 2244*a*b^2*x^2 + 616*b^3*x^3))/10472

fricas [A] time = 0.42, size = 40, normalized size = 0.78

$$\frac{3}{10472} (616b^3x^5 + 2244ab^2x^4 + 2856a^2bx^3 + 1309a^3x^2)x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)*(b*x+a)^3,x, algorithm="fricas")

[Out] 3/10472*(616*b^3*x^5 + 2244*a*b^2*x^4 + 2856*a^2*b*x^3 + 1309*a^3*x^2)*x^(2/3)

giac [A] time = 1.06, size = 35, normalized size = 0.69

$$\frac{3}{17}b^3x^{\frac{17}{3}} + \frac{9}{14}ab^2x^{\frac{14}{3}} + \frac{9}{11}a^2bx^{\frac{11}{3}} + \frac{3}{8}a^3x^{\frac{8}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)*(b*x+a)^3,x, algorithm="giac")

[Out] 3/17*b^3*x^(17/3) + 9/14*a*b^2*x^(14/3) + 9/11*a^2*b*x^(11/3) + 3/8*a^3*x^(8/3)

maple [A] time = 0.00, size = 36, normalized size = 0.71

$$\frac{3(616b^3x^3 + 2244ab^2x^2 + 2856a^2bx + 1309a^3)x^{\frac{8}{3}}}{10472}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/3)*(b*x+a)^3,x)

[Out] 3/10472*x^(8/3)*(616*b^3*x^3+2244*a*b^2*x^2+2856*a^2*b*x+1309*a^3)

maxima [A] time = 1.35, size = 35, normalized size = 0.69

$$\frac{3}{17}b^3x^{\frac{17}{3}} + \frac{9}{14}ab^2x^{\frac{14}{3}} + \frac{9}{11}a^2bx^{\frac{11}{3}} + \frac{3}{8}a^3x^{\frac{8}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)*(b*x+a)^3,x, algorithm="maxima")

[Out] $3/17*b^3*x^{(17/3)} + 9/14*a*b^2*x^{(14/3)} + 9/11*a^2*b*x^{(11/3)} + 3/8*a^3*x^{(8/3)}$

mupad [B] time = 0.04, size = 35, normalized size = 0.69

$$\frac{3a^3x^{8/3}}{8} + \frac{3b^3x^{17/3}}{17} + \frac{9a^2bx^{11/3}}{11} + \frac{9ab^2x^{14/3}}{14}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/3)*(a + b*x)^3,x)`

[Out] $(3*a^3*x^{(8/3)})/8 + (3*b^3*x^{(17/3)})/17 + (9*a^2*b*x^{(11/3)})/11 + (9*a*b^2*x^{(14/3)})/14$

sympy [A] time = 6.39, size = 49, normalized size = 0.96

$$\frac{3a^3x^{8/3}}{8} + \frac{9a^2bx^{11/3}}{11} + \frac{9ab^2x^{14/3}}{14} + \frac{3b^3x^{17/3}}{17}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/3)*(b*x+a)**3,x)`

[Out] $3*a**3*x**(8/3)/8 + 9*a**2*b*x**(11/3)/11 + 9*a*b**2*x**(14/3)/14 + 3*b**3*x**(17/3)/17$

$$3.667 \quad \int x^{4/3}(a + bx)^3 dx$$

Optimal. Leaf size=51

$$\frac{3}{7}a^3x^{7/3} + \frac{9}{10}a^2bx^{10/3} + \frac{9}{13}ab^2x^{13/3} + \frac{3}{16}b^3x^{16/3}$$

[Out] $3/7*a^3*x^{(7/3)}+9/10*a^2*b*x^{(10/3)}+9/13*a*b^2*x^{(13/3)}+3/16*b^3*x^{(16/3)}$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9}{10}a^2bx^{10/3} + \frac{3}{7}a^3x^{7/3} + \frac{9}{13}ab^2x^{13/3} + \frac{3}{16}b^3x^{16/3}$$

Antiderivative was successfully verified.

[In] Int[x^(4/3)*(a + b*x)^3,x]

[Out] $(3*a^3*x^{(7/3)})/7 + (9*a^2*b*x^{(10/3)})/10 + (9*a*b^2*x^{(13/3)})/13 + (3*b^3*x^{(16/3)})/16$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^{4/3}(a + bx)^3 dx &= \int (a^3x^{4/3} + 3a^2bx^{7/3} + 3ab^2x^{10/3} + b^3x^{13/3}) dx \\ &= \frac{3}{7}a^3x^{7/3} + \frac{9}{10}a^2bx^{10/3} + \frac{9}{13}ab^2x^{13/3} + \frac{3}{16}b^3x^{16/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.76

$$\frac{3x^{7/3} (1040a^3 + 2184a^2bx + 1680ab^2x^2 + 455b^3x^3)}{7280}$$

Antiderivative was successfully verified.

[In] Integrate[x^(4/3)*(a + b*x)^3,x]

[Out] (3*x^(7/3)*(1040*a^3 + 2184*a^2*b*x + 1680*a*b^2*x^2 + 455*b^3*x^3))/7280

fricas [A] time = 0.42, size = 40, normalized size = 0.78

$$\frac{3}{7280} (455 b^3 x^5 + 1680 a b^2 x^4 + 2184 a^2 b x^3 + 1040 a^3 x^2) x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)*(b*x+a)^3,x, algorithm="fricas")

[Out] 3/7280*(455*b^3*x^5 + 1680*a*b^2*x^4 + 2184*a^2*b*x^3 + 1040*a^3*x^2)*x^(1/3)

giac [A] time = 1.06, size = 35, normalized size = 0.69

$$\frac{3}{16} b^3 x^{\frac{16}{3}} + \frac{9}{13} a b^2 x^{\frac{13}{3}} + \frac{9}{10} a^2 b x^{\frac{10}{3}} + \frac{3}{7} a^3 x^{\frac{7}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)*(b*x+a)^3,x, algorithm="giac")

[Out] 3/16*b^3*x^(16/3) + 9/13*a*b^2*x^(13/3) + 9/10*a^2*b*x^(10/3) + 3/7*a^3*x^(7/3)

maple [A] time = 0.00, size = 36, normalized size = 0.71

$$\frac{3 (455 b^3 x^3 + 1680 a b^2 x^2 + 2184 a^2 b x + 1040 a^3) x^{\frac{7}{3}}}{7280}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(4/3)*(b*x+a)^3,x)

[Out] 3/7280*x^(7/3)*(455*b^3*x^3+1680*a*b^2*x^2+2184*a^2*b*x+1040*a^3)

maxima [A] time = 1.29, size = 35, normalized size = 0.69

$$\frac{3}{16} b^3 x^{\frac{16}{3}} + \frac{9}{13} a b^2 x^{\frac{13}{3}} + \frac{9}{10} a^2 b x^{\frac{10}{3}} + \frac{3}{7} a^3 x^{\frac{7}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)*(b*x+a)^3,x, algorithm="maxima")

[Out] $3/16*b^3*x^{(16/3)} + 9/13*a*b^2*x^{(13/3)} + 9/10*a^2*b*x^{(10/3)} + 3/7*a^3*x^{(7/3)}$

mupad [B] time = 0.04, size = 35, normalized size = 0.69

$$\frac{3a^3x^{7/3}}{7} + \frac{3b^3x^{16/3}}{16} + \frac{9a^2bx^{10/3}}{10} + \frac{9ab^2x^{13/3}}{13}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(4/3)*(a + b*x)^3,x)`

[Out] $(3*a^3*x^{(7/3)})/7 + (3*b^3*x^{(16/3)})/16 + (9*a^2*b*x^{(10/3)})/10 + (9*a*b^2*x^{(13/3)})/13$

sympy [A] time = 4.55, size = 49, normalized size = 0.96

$$\frac{3a^3x^{7/3}}{7} + \frac{9a^2bx^{10/3}}{10} + \frac{9ab^2x^{13/3}}{13} + \frac{3b^3x^{16/3}}{16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(4/3)*(b*x+a)**3,x)`

[Out] $3*a**3*x**(7/3)/7 + 9*a**2*b*x**(10/3)/10 + 9*a*b**2*x**(13/3)/13 + 3*b**3*x**(16/3)/16$

3.668 $\int x^{2/3}(a + bx)^3 dx$

Optimal. Leaf size=51

$$\frac{3}{5}a^3x^{5/3} + \frac{9}{8}a^2bx^{8/3} + \frac{9}{11}ab^2x^{11/3} + \frac{3}{14}b^3x^{14/3}$$

[Out] $3/5*a^3*x^{(5/3)}+9/8*a^2*b*x^{(8/3)}+9/11*a*b^2*x^{(11/3)}+3/14*b^3*x^{(14/3)}$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9}{8}a^2bx^{8/3} + \frac{3}{5}a^3x^{5/3} + \frac{9}{11}ab^2x^{11/3} + \frac{3}{14}b^3x^{14/3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(2/3)}*(a + b*x)^3, x]$

[Out] $(3*a^3*x^{(5/3)})/5 + (9*a^2*b*x^{(8/3)})/8 + (9*a*b^2*x^{(11/3)})/11 + (3*b^3*x^{(14/3)})/14$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ $\text{FreeQ}\{a, b, c, d, n\}, x\} \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (\text{!IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0])) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x^{2/3}(a + bx)^3 dx &= \int (a^3x^{2/3} + 3a^2bx^{5/3} + 3ab^2x^{8/3} + b^3x^{11/3}) dx \\ &= \frac{3}{5}a^3x^{5/3} + \frac{9}{8}a^2bx^{8/3} + \frac{9}{11}ab^2x^{11/3} + \frac{3}{14}b^3x^{14/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.76

$$\frac{3x^{5/3} (616a^3 + 1155a^2bx + 840ab^2x^2 + 220b^3x^3)}{3080}$$

Antiderivative was successfully verified.

[In] Integrate[x^(2/3)*(a + b*x)^3,x]

[Out] (3*x^(5/3)*(616*a^3 + 1155*a^2*b*x + 840*a*b^2*x^2 + 220*b^3*x^3))/3080

fricas [A] time = 0.46, size = 38, normalized size = 0.75

$$\frac{3}{3080} (220b^3x^4 + 840ab^2x^3 + 1155a^2bx^2 + 616a^3x)x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)*(b*x+a)^3,x, algorithm="fricas")

[Out] 3/3080*(220*b^3*x^4 + 840*a*b^2*x^3 + 1155*a^2*b*x^2 + 616*a^3*x)*x^(2/3)

giac [A] time = 1.07, size = 35, normalized size = 0.69

$$\frac{3}{14}b^3x^{\frac{14}{3}} + \frac{9}{11}ab^2x^{\frac{11}{3}} + \frac{9}{8}a^2bx^{\frac{8}{3}} + \frac{3}{5}a^3x^{\frac{5}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)*(b*x+a)^3,x, algorithm="giac")

[Out] 3/14*b^3*x^(14/3) + 9/11*a*b^2*x^(11/3) + 9/8*a^2*b*x^(8/3) + 3/5*a^3*x^(5/3)

maple [A] time = 0.01, size = 36, normalized size = 0.71

$$\frac{3(220b^3x^3 + 840ab^2x^2 + 1155a^2bx + 616a^3)x^{\frac{5}{3}}}{3080}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(2/3)*(b*x+a)^3,x)

[Out] 3/3080*x^(5/3)*(220*b^3*x^3+840*a*b^2*x^2+1155*a^2*b*x+616*a^3)

maxima [A] time = 1.34, size = 35, normalized size = 0.69

$$\frac{3}{14}b^3x^{\frac{14}{3}} + \frac{9}{11}ab^2x^{\frac{11}{3}} + \frac{9}{8}a^2bx^{\frac{8}{3}} + \frac{3}{5}a^3x^{\frac{5}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)*(b*x+a)^3,x, algorithm="maxima")

[Out] 3/14*b^3*x^(14/3) + 9/11*a*b^2*x^(11/3) + 9/8*a^2*b*x^(8/3) + 3/5*a^3*x^(5/3)

mupad [B] time = 0.04, size = 35, normalized size = 0.69

$$\frac{3a^3x^{5/3}}{5} + \frac{3b^3x^{14/3}}{14} + \frac{9a^2bx^{8/3}}{8} + \frac{9ab^2x^{11/3}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(2/3)*(a + b*x)^3,x)`

[Out] `(3*a^3*x^(5/3))/5 + (3*b^3*x^(14/3))/14 + (9*a^2*b*x^(8/3))/8 + (9*a*b^2*x^(11/3))/11`

sympy [A] time = 2.19, size = 49, normalized size = 0.96

$$\frac{3a^3x^{\frac{5}{3}}}{5} + \frac{9a^2bx^{\frac{8}{3}}}{8} + \frac{9ab^2x^{\frac{11}{3}}}{11} + \frac{3b^3x^{\frac{14}{3}}}{14}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(2/3)*(b*x+a)**3,x)`

[Out] `3*a**3*x**(5/3)/5 + 9*a**2*b*x**(8/3)/8 + 9*a*b**2*x**(11/3)/11 + 3*b**3*x***(14/3)/14`

$$3.669 \quad \int \sqrt[3]{x} (a + bx)^3 dx$$

Optimal. Leaf size=51

$$\frac{3}{4}a^3x^{4/3} + \frac{9}{7}a^2bx^{7/3} + \frac{9}{10}ab^2x^{10/3} + \frac{3}{13}b^3x^{13/3}$$

[Out] $3/4*a^3*x^{(4/3)}+9/7*a^2*b*x^{(7/3)}+9/10*a*b^2*x^{(10/3)}+3/13*b^3*x^{(13/3)}$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9}{7}a^2bx^{7/3} + \frac{3}{4}a^3x^{4/3} + \frac{9}{10}ab^2x^{10/3} + \frac{3}{13}b^3x^{13/3}$$

Antiderivative was successfully verified.

[In] Int[x^(1/3)*(a + b*x)^3,x]

[Out] $(3*a^3*x^{(4/3)})/4 + (9*a^2*b*x^{(7/3)})/7 + (9*a*b^2*x^{(10/3)})/10 + (3*b^3*x^{(13/3)})/13$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \sqrt[3]{x} (a + bx)^3 dx &= \int (a^3 \sqrt[3]{x} + 3a^2bx^{4/3} + 3ab^2x^{7/3} + b^3x^{10/3}) dx \\ &= \frac{3}{4}a^3x^{4/3} + \frac{9}{7}a^2bx^{7/3} + \frac{9}{10}ab^2x^{10/3} + \frac{3}{13}b^3x^{13/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.76

$$\frac{3x^{4/3} (455a^3 + 780a^2bx + 546ab^2x^2 + 140b^3x^3)}{1820}$$

Antiderivative was successfully verified.

[In] Integrate[x^(1/3)*(a + b*x)^3,x]

[Out] (3*x^(4/3)*(455*a^3 + 780*a^2*b*x + 546*a*b^2*x^2 + 140*b^3*x^3))/1820

fricas [A] time = 0.44, size = 38, normalized size = 0.75

$$\frac{3}{1820} (140 b^3 x^4 + 546 a b^2 x^3 + 780 a^2 b x^2 + 455 a^3 x) x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)*(b*x+a)^3,x, algorithm="fricas")

[Out] 3/1820*(140*b^3*x^4 + 546*a*b^2*x^3 + 780*a^2*b*x^2 + 455*a^3*x)*x^(1/3)

giac [A] time = 1.16, size = 35, normalized size = 0.69

$$\frac{3}{13} b^3 x^{\frac{13}{3}} + \frac{9}{10} a b^2 x^{\frac{10}{3}} + \frac{9}{7} a^2 b x^{\frac{7}{3}} + \frac{3}{4} a^3 x^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)*(b*x+a)^3,x, algorithm="giac")

[Out] 3/13*b^3*x^(13/3) + 9/10*a*b^2*x^(10/3) + 9/7*a^2*b*x^(7/3) + 3/4*a^3*x^(4/3)

maple [A] time = 0.00, size = 36, normalized size = 0.71

$$\frac{3(140b^3x^3 + 546ab^2x^2 + 780a^2bx + 455a^3)x^{\frac{4}{3}}}{1820}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/3)*(b*x+a)^3,x)

[Out] 3/1820*x^(4/3)*(140*b^3*x^3+546*a*b^2*x^2+780*a^2*b*x+455*a^3)

maxima [A] time = 1.35, size = 35, normalized size = 0.69

$$\frac{3}{13} b^3 x^{\frac{13}{3}} + \frac{9}{10} a b^2 x^{\frac{10}{3}} + \frac{9}{7} a^2 b x^{\frac{7}{3}} + \frac{3}{4} a^3 x^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)*(b*x+a)^3,x, algorithm="maxima")

[Out] 3/13*b^3*x^(13/3) + 9/10*a*b^2*x^(10/3) + 9/7*a^2*b*x^(7/3) + 3/4*a^3*x^(4/3)

mupad [B] time = 0.05, size = 35, normalized size = 0.69

$$\frac{3a^3x^{4/3}}{4} + \frac{3b^3x^{13/3}}{13} + \frac{9a^2bx^{7/3}}{7} + \frac{9ab^2x^{10/3}}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/3)*(a + b*x)^3,x)`

[Out] $(3a^3x^{4/3})/4 + (3b^3x^{13/3})/13 + (9a^2bx^{7/3})/7 + (9ab^2x^{10/3})/10$

sympy [C] time = 3.22, size = 5012, normalized size = 98.27

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/3)*(b*x+a)**3,x)`

[Out] `Piecewise((-243*a**(73/3)*(-1 + b*(a/b + x)/a)**(1/3)/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300*a**18*b**(10/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(16/3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)*(a/b + x)**6) + 243*a**(73/3)*exp(I*pi/3)/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300*a**18*b**(10/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(16/3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)*(a/b + x)**6) + 1377*a**(70/3)*b*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300*a**18*b**(10/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(16/3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)*(a/b + x)**6) - 1458*a**(70/3)*b*(a/b + x)*exp(I*pi/3)/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300*a**18*b**(10/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(16/3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)*(a/b + x)**6) - 3213*a**(67/3)*b**2*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**2/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300*a**18*b**(10/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(16/3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)*(a/b + x)**6) + 3645*a**(67/3)*b**2*(a/b + x)**2*exp(I*pi/3)/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300*a**18*b**(10/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(16/3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)*(a/b + x)**6) + 3927*a**(64/3)*b**3*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**3/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300*a**18*b**(10/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(16/3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)*(a/b + x)**6)`

$$\begin{aligned}
& 4 - 10920*a^{15}*b^{(19/3)}*(a/b + x)^{**5} + 1820*a^{14}*b^{(22/3)}*(a/b + x)^{**6} \\
& - 4860*a^{(64/3)}*b^{**3}*(a/b + x)^{**3}*exp(I*pi/3)/(1820*a^{20}*b^{(4/3)} - 10920 \\
& 0*a^{19}*b^{(7/3)}*(a/b + x) + 27300*a^{18}*b^{(10/3)}*(a/b + x)^{**2} - 36400*a^{17} \\
& *b^{(13/3)}*(a/b + x)^{**3} + 27300*a^{16}*b^{(16/3)}*(a/b + x)^{**4} - 10920*a^{15} \\
& *b^{(19/3)}*(a/b + x)^{**5} + 1820*a^{14}*b^{(22/3)}*(a/b + x)^{**6} - 2163*a^{(61/3)} \\
& *b^{**4}*(-1 + b*(a/b + x)/a)^{**1/3}*(a/b + x)^{**4}/(1820*a^{20}*b^{(4/3)} - 10 \\
& 920*a^{19}*b^{(7/3)}*(a/b + x) + 27300*a^{18}*b^{(10/3)}*(a/b + x)^{**2} - 36400*a \\
& **17*b^{(13/3)}*(a/b + x)^{**3} + 27300*a^{16}*b^{(16/3)}*(a/b + x)^{**4} - 10920*a \\
& *15*b^{(19/3)}*(a/b + x)^{**5} + 1820*a^{14}*b^{(22/3)}*(a/b + x)^{**6} + 3645*a^{(61/3)} \\
& *b^{**4}*(a/b + x)^{**4}*exp(I*pi/3)/(1820*a^{20}*b^{(4/3)} - 10920*a^{19}*b^{(7/3)} \\
& *(a/b + x) + 27300*a^{18}*b^{(10/3)}*(a/b + x)^{**2} - 36400*a^{17}*b^{(13/3)} \\
& *(a/b + x)^{**3} + 27300*a^{16}*b^{(16/3)}*(a/b + x)^{**4} - 10920*a^{15}*b^{(19/3)} \\
& *(a/b + x)^{**5} + 1820*a^{14}*b^{(22/3)}*(a/b + x)^{**6} - 1827*a^{(58/3)}*b^{**5}*(-1 \\
& + b*(a/b + x)/a)^{**1/3}*(a/b + x)^{**5}/(1820*a^{20}*b^{(4/3)} - 10920*a^{19}*b \\
& *(7/3)*(a/b + x) + 27300*a^{18}*b^{(10/3)}*(a/b + x)^{**2} - 36400*a^{17}*b^{(13/3)} \\
& *(a/b + x)^{**3} + 27300*a^{16}*b^{(16/3)}*(a/b + x)^{**4} - 10920*a^{15}*b^{(19/3)} \\
& *(a/b + x)^{**5} + 1820*a^{14}*b^{(22/3)}*(a/b + x)^{**6} - 1458*a^{(58/3)}*b^{**5} \\
& *(a/b + x)^{**5}*exp(I*pi/3)/(1820*a^{20}*b^{(4/3)} - 10920*a^{19}*b^{(7/3)}*(a/b + \\
& x) + 27300*a^{18}*b^{(10/3)}*(a/b + x)^{**2} - 36400*a^{17}*b^{(13/3)}*(a/b + x)^{** \\
& 3} + 27300*a^{16}*b^{(16/3)}*(a/b + x)^{**4} - 10920*a^{15}*b^{(19/3)}*(a/b + x)^{**5} \\
& + 1820*a^{14}*b^{(22/3)}*(a/b + x)^{**6} + 6573*a^{(55/3)}*b^{**6}*(-1 + b*(a/b + \\
& x)/a)^{**1/3}*(a/b + x)^{**6}/(1820*a^{20}*b^{(4/3)} - 10920*a^{19}*b^{(7/3)}*(a/b \\
& + x) + 27300*a^{18}*b^{(10/3)}*(a/b + x)^{**2} - 36400*a^{17}*b^{(13/3)}*(a/b + x)^{** \\
& 3} + 27300*a^{16}*b^{(16/3)}*(a/b + x)^{**4} - 10920*a^{15}*b^{(19/3)}*(a/b + x)^{** \\
& 5} + 1820*a^{14}*b^{(22/3)}*(a/b + x)^{**6} + 243*a^{(55/3)}*b^{**6}*(a/b + x)^{**6}*e \\
& xp(I*pi/3)/(1820*a^{20}*b^{(4/3)} - 10920*a^{19}*b^{(7/3)}*(a/b + x) + 27300*a \\
& *18*b^{(10/3)}*(a/b + x)^{**2} - 36400*a^{17}*b^{(13/3)}*(a/b + x)^{**3} + 27300*a \\
& *16*b^{(16/3)}*(a/b + x)^{**4} - 10920*a^{15}*b^{(19/3)}*(a/b + x)^{**5} + 1820*a^{14} \\
& *b^{(22/3)}*(a/b + x)^{**6} - 8787*a^{(52/3)}*b^{**7}*(-1 + b*(a/b + x)/a)^{**1/3} \\
& *(a/b + x)^{**7}/(1820*a^{20}*b^{(4/3)} - 10920*a^{19}*b^{(7/3)}*(a/b + x) + 27300 \\
& *a^{18}*b^{(10/3)}*(a/b + x)^{**2} - 36400*a^{17}*b^{(13/3)}*(a/b + x)^{**3} + 27300*a \\
& **16*b^{(16/3)}*(a/b + x)^{**4} - 10920*a^{15}*b^{(19/3)}*(a/b + x)^{**5} + 1820*a^{14} \\
& *b^{(22/3)}*(a/b + x)^{**6} + 6498*a^{(49/3)}*b^{**8}*(-1 + b*(a/b + x)/a)^{**1/3} \\
& *(a/b + x)^{**8}/(1820*a^{20}*b^{(4/3)} - 10920*a^{19}*b^{(7/3)}*(a/b + x) + 2730 \\
& 0*a^{18}*b^{(10/3)}*(a/b + x)^{**2} - 36400*a^{17}*b^{(13/3)}*(a/b + x)^{**3} + 27300 \\
& *a^{16}*b^{(16/3)}*(a/b + x)^{**4} - 10920*a^{15}*b^{(19/3)}*(a/b + x)^{**5} + 1820*a \\
& **14*b^{(22/3)}*(a/b + x)^{**6} - 2562*a^{(46/3)}*b^{**9}*(-1 + b*(a/b + x)/a)^{**1 \\
& /3}*(a/b + x)^{**9}/(1820*a^{20}*b^{(4/3)} - 10920*a^{19}*b^{(7/3)}*(a/b + x) + 27 \\
& 300*a^{18}*b^{(10/3)}*(a/b + x)^{**2} - 36400*a^{17}*b^{(13/3)}*(a/b + x)^{**3} + 273 \\
& 00*a^{16}*b^{(16/3)}*(a/b + x)^{**4} - 10920*a^{15}*b^{(19/3)}*(a/b + x)^{**5} + 1820 \\
& *a^{14}*b^{(22/3)}*(a/b + x)^{**6} + 420*a^{(43/3)}*b^{**10}*(-1 + b*(a/b + x)/a)^{** \\
& (1/3)}*(a/b + x)^{**10}/(1820*a^{20}*b^{(4/3)} - 10920*a^{19}*b^{(7/3)}*(a/b + x) + \\
& 27300*a^{18}*b^{(10/3)}*(a/b + x)^{**2} - 36400*a^{17}*b^{(13/3)}*(a/b + x)^{**3} + \\
& 27300*a^{16}*b^{(16/3)}*(a/b + x)^{**4} - 10920*a^{15}*b^{(19/3)}*(a/b + x)^{**5} + 1 \\
& 820*a^{14}*b^{(22/3)}*(a/b + x)^{**6}), Abs(b*(a/b + x)/a) > 1), (-243*a^{(73/3)}
\end{aligned}$$


```

x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(16/3)*(a/b + x)
)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)*(a/b + x)*
*6) + 6573*a**(55/3)*b**6*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**6*exp(I*pi/
3)/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300*a**18*b**(
10/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(1
6/3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/
3)*(a/b + x)**6) + 243*a**(55/3)*b**6*(a/b + x)**6*exp(I*pi/3)/(1820*a**20*
b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300*a**18*b**(10/3)*(a/b + x)
**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(16/3)*(a/b + x)*
**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)*(a/b + x)**6
) - 8787*a**(52/3)*b**7*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**7*exp(I*pi/3)
/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300*a**18*b**(10
/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*a**16*b**(16/
3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)
*(a/b + x)**6) + 6498*a**(49/3)*b**8*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**
8*exp(I*pi/3)/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b + x) + 27300
*a**18*b**(10/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)**3 + 27300*
a**16*b**(16/3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)**5 + 1820*a
**14*b**(22/3)*(a/b + x)**6) - 2562*a**(46/3)*b**9*(1 - b*(a/b + x)/a)**(1/3
)*(a/b + x)**9*exp(I*pi/3)/(1820*a**20*b**(4/3) - 10920*a**19*b**(7/3)*(a/b
+ x) + 27300*a**18*b**(10/3)*(a/b + x)**2 - 36400*a**17*b**(13/3)*(a/b + x)
)**3 + 27300*a**16*b**(16/3)*(a/b + x)**4 - 10920*a**15*b**(19/3)*(a/b + x)
**5 + 1820*a**14*b**(22/3)*(a/b + x)**6) + 420*a**(43/3)*b**10*(1 - b*(a/b
+ x)/a)**(1/3)*(a/b + x)**10*exp(I*pi/3)/(1820*a**20*b**(4/3) - 10920*a**19
*b**(7/3)*(a/b + x) + 27300*a**18*b**(10/3)*(a/b + x)**2 - 36400*a**17*b**(
13/3)*(a/b + x)**3 + 27300*a**16*b**(16/3)*(a/b + x)**4 - 10920*a**15*b**(1
9/3)*(a/b + x)**5 + 1820*a**14*b**(22/3)*(a/b + x)**6), True))

```


$$3.670 \quad \int \frac{(a+bx)^3}{\sqrt[3]{x}} dx$$

Optimal. Leaf size=51

$$\frac{3}{2}a^3x^{2/3} + \frac{9}{5}a^2bx^{5/3} + \frac{9}{8}ab^2x^{8/3} + \frac{3}{11}b^3x^{11/3}$$

[Out] $3/2*a^3*x^{(2/3)}+9/5*a^2*b*x^{(5/3)}+9/8*a*b^2*x^{(8/3)}+3/11*b^3*x^{(11/3)}$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9}{5}a^2bx^{5/3} + \frac{3}{2}a^3x^{2/3} + \frac{9}{8}ab^2x^{8/3} + \frac{3}{11}b^3x^{11/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^(1/3), x]

[Out] $(3*a^3*x^{(2/3)})/2 + (9*a^2*b*x^{(5/3)})/5 + (9*a*b^2*x^{(8/3)})/8 + (3*b^3*x^{(11/3)})/11$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{\sqrt[3]{x}} dx &= \int \left(\frac{a^3}{\sqrt[3]{x}} + 3a^2bx^{2/3} + 3ab^2x^{5/3} + b^3x^{8/3} \right) dx \\ &= \frac{3}{2}a^3x^{2/3} + \frac{9}{5}a^2bx^{5/3} + \frac{9}{8}ab^2x^{8/3} + \frac{3}{11}b^3x^{11/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.76

$$\frac{3}{440}x^{2/3} (220a^3 + 264a^2bx + 165ab^2x^2 + 40b^3x^3)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^(1/3), x]

[Out] (3*x^(2/3)*(220*a^3 + 264*a^2*b*x + 165*a*b^2*x^2 + 40*b^3*x^3))/440

fricas [A] time = 0.43, size = 35, normalized size = 0.69

$$\frac{3}{440} (40b^3x^3 + 165ab^2x^2 + 264a^2bx + 220a^3)x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(1/3), x, algorithm="fricas")

[Out] 3/440*(40*b^3*x^3 + 165*a*b^2*x^2 + 264*a^2*b*x + 220*a^3)*x^(2/3)

giac [A] time = 0.86, size = 35, normalized size = 0.69

$$\frac{3}{11} b^3 x^{\frac{11}{3}} + \frac{9}{8} ab^2 x^{\frac{8}{3}} + \frac{9}{5} a^2 b x^{\frac{5}{3}} + \frac{3}{2} a^3 x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(1/3), x, algorithm="giac")

[Out] 3/11*b^3*x^(11/3) + 9/8*a*b^2*x^(8/3) + 9/5*a^2*b*x^(5/3) + 3/2*a^3*x^(2/3)

maple [A] time = 0.00, size = 36, normalized size = 0.71

$$\frac{3(40b^3x^3 + 165ab^2x^2 + 264a^2bx + 220a^3)x^{\frac{2}{3}}}{440}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/x^(1/3), x)

[Out] 3/440*x^(2/3)*(40*b^3*x^3+165*a*b^2*x^2+264*a^2*b*x+220*a^3)

maxima [A] time = 1.33, size = 35, normalized size = 0.69

$$\frac{3}{11} b^3 x^{\frac{11}{3}} + \frac{9}{8} ab^2 x^{\frac{8}{3}} + \frac{9}{5} a^2 b x^{\frac{5}{3}} + \frac{3}{2} a^3 x^{\frac{2}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(1/3), x, algorithm="maxima")

[Out] 3/11*b^3*x^(11/3) + 9/8*a*b^2*x^(8/3) + 9/5*a^2*b*x^(5/3) + 3/2*a^3*x^(2/3)

$$\begin{aligned}
& a^{16}b^{14/3}(a/b+x)^4 \exp(I\pi/3) - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) + 440a^{14}b^{20/3}(a/b+x)^6 \exp(I\pi/3) - 4860a^{13}b^{23/3}(a/b+x)^3 / (440a^{20}b^{2/3} \exp(I\pi/3) - 2640a^{19}b^{5/3}) \\
& (a/b+x) \exp(I\pi/3) + 6600a^{18}b^{8/3}(a/b+x)^2 \exp(I\pi/3) - 8800a^{17}b^{11/3}(a/b+x)^3 \exp(I\pi/3) + 6600a^{16}b^{14/3}(a/b+x)^4 \exp(I\pi/3) - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) + 440a^{14}b^{20/3} \\
& (a/b+x)^6 \exp(I\pi/3) - 1710a^{59/3}b^4(1-b(a/b+x)/a)^{2/3}(a/b+x)^4 / (440a^{20}b^{2/3} \exp(I\pi/3) - 2640a^{19}b^{5/3}) (a/b+x) \exp(I\pi/3) + 6600a^{18}b^{8/3}(a/b+x)^2 \exp(I\pi/3) - 8800a^{17}b^{11/3}(a/b+x)^3 \exp(I\pi/3) \\
& + 6600a^{16}b^{14/3}(a/b+x)^4 \exp(I\pi/3) - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) + 440a^{14}b^{20/3}(a/b+x)^6 \exp(I\pi/3) + 3645a^{59/3}b^4(a/b+x)^4 / (440a^{20}b^{2/3} \exp(I\pi/3) - 2640a^{19}b^{5/3}) (a/b+x) \exp(I\pi/3) \\
& + 6600a^{18}b^{8/3}(a/b+x)^2 \exp(I\pi/3) - 8800a^{17}b^{11/3}(a/b+x)^3 \exp(I\pi/3) + 6600a^{16}b^{14/3}(a/b+x)^4 \exp(I\pi/3) - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) + 440a^{14}b^{20/3}(a/b+x)^6 \exp(I\pi/3) \\
& - 72a^{56/3}b^5(1-b(a/b+x)/a)^{2/3}(a/b+x)^5 / (440a^{20}b^{2/3} \exp(I\pi/3) - 2640a^{19}b^{5/3}) (a/b+x) \exp(I\pi/3) + 6600a^{18}b^{8/3}(a/b+x)^2 \exp(I\pi/3) - 8800a^{17}b^{11/3}(a/b+x)^3 \exp(I\pi/3) \\
& + 6600a^{16}b^{14/3}(a/b+x)^4 \exp(I\pi/3) - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) + 440a^{14}b^{20/3}(a/b+x)^6 \exp(I\pi/3) - 1458a^{56/3}b^5(a/b+x)^5 / (440a^{20}b^{2/3} \exp(I\pi/3) - 2640a^{19}b^{5/3}) (a/b+x) \exp(I\pi/3) \\
& - 2640a^{19}b^{5/3}(a/b+x) \exp(I\pi/3) + 6600a^{18}b^{8/3}(a/b+x)^2 \exp(I\pi/3) - 8800a^{17}b^{11/3}(a/b+x)^3 \exp(I\pi/3) + 6600a^{16}b^{14/3}(a/b+x)^4 \exp(I\pi/3) - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) \\
& + 440a^{14}b^{20/3}(a/b+x)^6 \exp(I\pi/3) + 1104a^{53/3}b^6(1-b(a/b+x)/a)^{2/3}(a/b+x)^6 / (440a^{20}b^{2/3} \exp(I\pi/3) - 2640a^{19}b^{5/3}) (a/b+x) \exp(I\pi/3) + 6600a^{18}b^{8/3}(a/b+x)^2 \exp(I\pi/3) \\
& - 8800a^{17}b^{11/3}(a/b+x)^3 \exp(I\pi/3) + 6600a^{16}b^{14/3}(a/b+x)^4 \exp(I\pi/3) - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) + 440a^{14}b^{20/3}(a/b+x)^6 \exp(I\pi/3) - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) \\
& + 440a^{14}b^{20/3}(a/b+x)^6 \exp(I\pi/3) - 1152a^{50/3}b^7(1-b(a/b+x)/a)^{2/3}(a/b+x)^7 / (440a^{20}b^{2/3} \exp(I\pi/3) - 2640a^{19}b^{5/3}) (a/b+x) \exp(I\pi/3) + 6600a^{18}b^{8/3}(a/b+x)^2 \exp(I\pi/3) \\
& - 8800a^{17}b^{11/3}(a/b+x)^3 \exp(I\pi/3) + 6600a^{16}b^{14/3}(a/b+x)^4 \exp(I\pi/3) - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) + 440a^{14}b^{20/3}(a/b+x)^6 \exp(I\pi/3) + 585a^{47/3}b^8(1-b(a/b+x)/a)^{2/3} \\
& (a/b+x)^8 / (440a^{20}b^{2/3} \exp(I\pi/3) - 2640a^{19}b^{5/3}) (a/b+x) \exp(I\pi/3) + 6600a^{18}b^{8/3}(a/b+x)^2 \exp(I\pi/3) - 8800a^{17}b^{11/3}(a/b+x)^3 \exp(I\pi/3) + 6600a^{16}b^{14/3}(a/b+x)^4 \exp(I\pi/3) \\
& - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) + 440a^{14}b^{20/3}(a/b+x)^6 \exp(I\pi/3) - 2640a^{15}b^{17/3}(a/b+x)^5 \exp(I\pi/3) + 440a^{14}b^{20/3}(a/b+x)^6 \exp(I\pi/3)
\end{aligned}$$

```
0*a**14*b**(20/3)*(a/b + x)**6*exp(I*pi/3)) - 120*a**(44/3)*b**9*(1 - b*(a/
b + x)/a)**(2/3)*(a/b + x)**9/(440*a**20*b**(2/3)*exp(I*pi/3) - 2640*a**19*
b**(5/3)*(a/b + x)*exp(I*pi/3) + 6600*a**18*b**(8/3)*(a/b + x)**2*exp(I*pi/
3) - 8800*a**17*b**(11/3)*(a/b + x)**3*exp(I*pi/3) + 6600*a**16*b**(14/3)*(
a/b + x)**4*exp(I*pi/3) - 2640*a**15*b**(17/3)*(a/b + x)**5*exp(I*pi/3) + 4
40*a**14*b**(20/3)*(a/b + x)**6*exp(I*pi/3)), True))
```

$$3.671 \quad \int \frac{(a+bx)^3}{x^{2/3}} dx$$

Optimal. Leaf size=49

$$3a^3\sqrt[3]{x} + \frac{9}{4}a^2bx^{4/3} + \frac{9}{7}ab^2x^{7/3} + \frac{3}{10}b^3x^{10/3}$$

[Out] $3a^3x^{(1/3)} + 9/4a^2b*x^{(4/3)} + 9/7*a*b^2*x^{(7/3)} + 3/10*b^3*x^{(10/3)}$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9}{4}a^2bx^{4/3} + 3a^3\sqrt[3]{x} + \frac{9}{7}ab^2x^{7/3} + \frac{3}{10}b^3x^{10/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^(2/3), x]

[Out] $3a^3x^{(1/3)} + (9a^2b*x^{(4/3)})/4 + (9a*b^2*x^{(7/3)})/7 + (3b^3*x^{(10/3)})/10$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^{2/3}} dx &= \int \left(\frac{a^3}{x^{2/3}} + 3a^2b\sqrt[3]{x} + 3ab^2x^{4/3} + b^3x^{7/3} \right) dx \\ &= 3a^3\sqrt[3]{x} + \frac{9}{4}a^2bx^{4/3} + \frac{9}{7}ab^2x^{7/3} + \frac{3}{10}b^3x^{10/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.80

$$\frac{3}{140}\sqrt[3]{x} (140a^3 + 105a^2bx + 60ab^2x^2 + 14b^3x^3)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^(2/3),x]

[Out] (3*x^(1/3)*(140*a^3 + 105*a^2*b*x + 60*a*b^2*x^2 + 14*b^3*x^3))/140

fricas [A] time = 0.45, size = 35, normalized size = 0.71

$$\frac{3}{140} (14b^3x^3 + 60ab^2x^2 + 105a^2bx + 140a^3)x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(2/3),x, algorithm="fricas")

[Out] 3/140*(14*b^3*x^3 + 60*a*b^2*x^2 + 105*a^2*b*x + 140*a^3)*x^(1/3)

giac [A] time = 0.94, size = 35, normalized size = 0.71

$$\frac{3}{10} b^3 x^{\frac{10}{3}} + \frac{9}{7} ab^2 x^{\frac{7}{3}} + \frac{9}{4} a^2 b x^{\frac{4}{3}} + 3 a^3 x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(2/3),x, algorithm="giac")

[Out] 3/10*b^3*x^(10/3) + 9/7*a*b^2*x^(7/3) + 9/4*a^2*b*x^(4/3) + 3*a^3*x^(1/3)

maple [A] time = 0.01, size = 36, normalized size = 0.73

$$\frac{3(14b^3x^3 + 60a b^2x^2 + 105a^2bx + 140a^3)x^{\frac{1}{3}}}{140}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/x^(2/3),x)

[Out] 3/140*x^(1/3)*(14*b^3*x^3+60*a*b^2*x^2+105*a^2*b*x+140*a^3)

maxima [A] time = 1.29, size = 35, normalized size = 0.71

$$\frac{3}{10} b^3 x^{\frac{10}{3}} + \frac{9}{7} ab^2 x^{\frac{7}{3}} + \frac{9}{4} a^2 b x^{\frac{4}{3}} + 3 a^3 x^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(2/3),x, algorithm="maxima")

[Out] 3/10*b^3*x^(10/3) + 9/7*a*b^2*x^(7/3) + 9/4*a^2*b*x^(4/3) + 3*a^3*x^(1/3)

mupad [B] time = 0.04, size = 35, normalized size = 0.71

$$3a^3x^{1/3} + \frac{3b^3x^{10/3}}{10} + \frac{9a^2bx^{4/3}}{4} + \frac{9ab^2x^{7/3}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^(2/3), x)`

[Out] `3*a^3*x^(1/3) + (3*b^3*x^(10/3))/10 + (9*a^2*b*x^(4/3))/4 + (9*a*b^2*x^(7/3))/7`

sympy [C] time = 3.17, size = 6667, normalized size = 136.06

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**(2/3), x)`

[Out] `Piecewise((243*a**(70/3)*(-1 + b*(a/b + x)/a)**(1/3)*exp(2*I*pi/3)/(140*a**20*b**(1/3)*exp(2*I*pi/3) - 840*a**19*b**(4/3)*(a/b + x)*exp(2*I*pi/3) + 2100*a**18*b**(7/3)*(a/b + x)**2*exp(2*I*pi/3) - 2800*a**17*b**(10/3)*(a/b + x)**3*exp(2*I*pi/3) + 2100*a**16*b**(13/3)*(a/b + x)**4*exp(2*I*pi/3) - 840*a**15*b**(16/3)*(a/b + x)**5*exp(2*I*pi/3) + 140*a**14*b**(19/3)*(a/b + x)**6*exp(2*I*pi/3)) + 243*a**(70/3)/(140*a**20*b**(1/3)*exp(2*I*pi/3) - 840*a**19*b**(4/3)*(a/b + x)*exp(2*I*pi/3) + 2100*a**18*b**(7/3)*(a/b + x)**2*exp(2*I*pi/3) - 2800*a**17*b**(10/3)*(a/b + x)**3*exp(2*I*pi/3) + 2100*a**16*b**(13/3)*(a/b + x)**4*exp(2*I*pi/3) - 840*a**15*b**(16/3)*(a/b + x)**5*exp(2*I*pi/3) + 140*a**14*b**(19/3)*(a/b + x)**6*exp(2*I*pi/3)) - 1377*a**(67/3)*b*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)*exp(2*I*pi/3)/(140*a**20*b**(1/3)*exp(2*I*pi/3) - 840*a**19*b**(4/3)*(a/b + x)*exp(2*I*pi/3) + 2100*a**18*b**(7/3)*(a/b + x)**2*exp(2*I*pi/3) - 2800*a**17*b**(10/3)*(a/b + x)**3*exp(2*I*pi/3) + 2100*a**16*b**(13/3)*(a/b + x)**4*exp(2*I*pi/3) - 840*a**15*b**(16/3)*(a/b + x)**5*exp(2*I*pi/3) + 140*a**14*b**(19/3)*(a/b + x)**6*exp(2*I*pi/3)) + 3213*a**(64/3)*b**2*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**2*exp(2*I*pi/3)/(140*a**20*b**(1/3)*exp(2*I*pi/3) - 840*a**19*b**(4/3)*(a/b + x)*exp(2*I*pi/3) + 2100*a**18*b**(7/3)*(a/b + x)**2*exp(2*I*pi/3) - 2800*a**17*b**(10/3)*(a/b + x)**3*exp(2*I*pi/3) + 2100*a**16*b**(13/3)*(a/b + x)**4*exp(2*I*pi/3) - 840*a**15*b**(16/3)*(a/b + x)**5*exp(2*I*pi/3) + 140*a**14*b**(19/3)*(a/b + x)**6*exp(2*I*pi/3)) + 3645*a**(64/3)*b**2*(a/b + x)**2/(140*a**20*b**(1/3)*`

$$\begin{aligned}
& \exp(2I\pi/3) - 840a^{19}b^{4/3}(a/b + x)\exp(2I\pi/3) + 2100a^{18}b^{7/3}(a/b + x)^2\exp(2I\pi/3) - 2800a^{17}b^{10/3}(a/b + x)^3\exp(2I\pi/3) \\
& + 2100a^{16}b^{13/3}(a/b + x)^4\exp(2I\pi/3) - 840a^{15}b^{16/3}(a/b + x)^5\exp(2I\pi/3) + 140a^{14}b^{19/3}(a/b + x)^6\exp(2I\pi/3) \\
& - 3927a^{61/3}b^3(-1 + b(a/b + x)/a)^{1/3}(a/b + x)^3\exp(2I\pi/3) / (140a^{20}b^{1/3}\exp(2I\pi/3) - 840a^{19}b^{4/3}(a/b + x)\exp(2I\pi/3) \\
& + 2100a^{18}b^{7/3}(a/b + x)^2\exp(2I\pi/3) - 2800a^{17}b^{10/3}(a/b + x)^3\exp(2I\pi/3) + 2100a^{16}b^{13/3}(a/b + x)^4\exp(2I\pi/3) \\
& - 840a^{15}b^{16/3}(a/b + x)^5\exp(2I\pi/3) + 140a^{14}b^{19/3}(a/b + x)^6\exp(2I\pi/3) - 4860a^{61/3}b^3(a/b + x)^3 / (140a^{20}b^{1/3}\exp(2I\pi/3) \\
& - 840a^{19}b^{4/3}(a/b + x)\exp(2I\pi/3) + 2100a^{18}b^{7/3}(a/b + x)^2\exp(2I\pi/3) - 2800a^{17}b^{10/3}(a/b + x)^3\exp(2I\pi/3) \\
& + 2100a^{16}b^{13/3}(a/b + x)^4\exp(2I\pi/3) - 840a^{15}b^{16/3}(a/b + x)^5\exp(2I\pi/3) + 140a^{14}b^{19/3}(a/b + x)^6\exp(2I\pi/3) \\
& + 2583a^{58/3}b^4(-1 + b(a/b + x)/a)^{1/3}(a/b + x)^4\exp(2I\pi/3) / (140a^{20}b^{1/3}\exp(2I\pi/3) - 840a^{19}b^{4/3}(a/b + x)\exp(2I\pi/3) \\
& + 2100a^{18}b^{7/3}(a/b + x)^2\exp(2I\pi/3) - 2800a^{17}b^{10/3}(a/b + x)^3\exp(2I\pi/3) + 2100a^{16}b^{13/3}(a/b + x)^4\exp(2I\pi/3) \\
& - 840a^{15}b^{16/3}(a/b + x)^5\exp(2I\pi/3) + 140a^{14}b^{19/3}(a/b + x)^6\exp(2I\pi/3) + 3645a^{58/3}b^4(a/b + x)^4 / (140a^{20}b^{1/3}\exp(2I\pi/3) \\
& - 840a^{19}b^{4/3}(a/b + x)\exp(2I\pi/3) + 2100a^{18}b^{7/3}(a/b + x)^2\exp(2I\pi/3) - 2800a^{17}b^{10/3}(a/b + x)^3\exp(2I\pi/3) \\
& + 2100a^{16}b^{13/3}(a/b + x)^4\exp(2I\pi/3) - 840a^{15}b^{16/3}(a/b + x)^5\exp(2I\pi/3) + 140a^{14}b^{19/3}(a/b + x)^6\exp(2I\pi/3) \\
& - 693a^{55/3}b^5(-1 + b(a/b + x)/a)^{1/3}(a/b + x)^5\exp(2I\pi/3) / (140a^{20}b^{1/3}\exp(2I\pi/3) - 840a^{19}b^{4/3}(a/b + x)\exp(2I\pi/3) \\
& + 2100a^{18}b^{7/3}(a/b + x)^2\exp(2I\pi/3) - 2800a^{17}b^{10/3}(a/b + x)^3\exp(2I\pi/3) + 2100a^{16}b^{13/3}(a/b + x)^4\exp(2I\pi/3) \\
& - 840a^{15}b^{16/3}(a/b + x)^5\exp(2I\pi/3) + 140a^{14}b^{19/3}(a/b + x)^6\exp(2I\pi/3) - 1458a^{55/3}b^5(a/b + x)^5 / (140a^{20}b^{1/3}\exp(2I\pi/3) \\
& - 840a^{19}b^{4/3}(a/b + x)\exp(2I\pi/3) + 2100a^{18}b^{7/3}(a/b + x)^2\exp(2I\pi/3) - 2800a^{17}b^{10/3}(a/b + x)^3\exp(2I\pi/3) \\
& + 2100a^{16}b^{13/3}(a/b + x)^4\exp(2I\pi/3) - 840a^{15}b^{16/3}(a/b + x)^5\exp(2I\pi/3) + 140a^{14}b^{19/3}(a/b + x)^6\exp(2I\pi/3) \\
& - 273a^{52/3}b^6(-1 + b(a/b + x)/a)^{1/3}(a/b + x)^6\exp(2I\pi/3) / (140a^{20}b^{1/3}\exp(2I\pi/3) - 840a^{19}b^{4/3}(a/b + x)\exp(2I\pi/3) \\
& + 2100a^{18}b^{7/3}(a/b + x)^2\exp(2I\pi/3) - 2800a^{17}b^{10/3}(a/b + x)^3\exp(2I\pi/3) + 2100a^{16}b^{13/3}(a/b + x)^4\exp(2I\pi/3) \\
& - 840a^{15}b^{16/3}(a/b + x)^5\exp(2I\pi/3) + 140a^{14}b^{19/3}(a/b + x)^6\exp(2I\pi/3) + 243a^{52/3}b^6(a/b + x)^6 / (140a^{20}b^{1/3}\exp(2I\pi/3) \\
& - 840a^{19}b^{4/3}(a/b + x)\exp(2I\pi/3) + 2100a^{18}b^{7/3}(a/b + x)^2\exp(2I\pi/3) - 2800a^{17}b^{10/3}(a/b + x)^3\exp(2I\pi/3) \\
& + 2100a^{16}b^{13/3}(a/b + x)^4\exp(2I\pi/3) - 840a^{15}b^{16/3}(a/b + x)^5\exp(2I\pi/3) + 140a^{14}b^{19/3}(a/b + x)^6\exp(2I\pi/3) \\
& + 387a
\end{aligned}$$

$$\begin{aligned}
& i/3) + 140*a^{14}*b^{(19/3)}*(a/b + x)^{6}*exp(2*I*pi/3) + 3927*a^{(61/3)}*b^{3} \\
& * (1 - b*(a/b + x)/a)^{(1/3)}*(a/b + x)^{3}/(140*a^{20}*b^{(1/3)}*exp(2*I*pi/3) \\
& - 840*a^{19}*b^{(4/3)}*(a/b + x)*exp(2*I*pi/3) + 2100*a^{18}*b^{(7/3)}*(a/b + \\
& x)^{2}*exp(2*I*pi/3) - 2800*a^{17}*b^{(10/3)}*(a/b + x)^{3}*exp(2*I*pi/3) + 210 \\
& 0*a^{16}*b^{(13/3)}*(a/b + x)^{4}*exp(2*I*pi/3) - 840*a^{15}*b^{(16/3)}*(a/b + x) \\
&)^{5}*exp(2*I*pi/3) + 140*a^{14}*b^{(19/3)}*(a/b + x)^{6}*exp(2*I*pi/3) - 4860 \\
& *a^{(61/3)}*b^{3}*(a/b + x)^{3}/(140*a^{20}*b^{(1/3)}*exp(2*I*pi/3) - 840*a^{19}* \\
& b^{(4/3)}*(a/b + x)*exp(2*I*pi/3) + 2100*a^{18}*b^{(7/3)}*(a/b + x)^{2}*exp(2*I \\
& *pi/3) - 2800*a^{17}*b^{(10/3)}*(a/b + x)^{3}*exp(2*I*pi/3) + 2100*a^{16}*b^{(1 \\
& 3/3)}*(a/b + x)^{4}*exp(2*I*pi/3) - 840*a^{15}*b^{(16/3)}*(a/b + x)^{5}*exp(2*I* \\
& pi/3) + 140*a^{14}*b^{(19/3)}*(a/b + x)^{6}*exp(2*I*pi/3) - 2583*a^{(58/3)}*b \\
& *4*(1 - b*(a/b + x)/a)^{(1/3)}*(a/b + x)^{4}/(140*a^{20}*b^{(1/3)}*exp(2*I*pi/3) \\
&) - 840*a^{19}*b^{(4/3)}*(a/b + x)*exp(2*I*pi/3) + 2100*a^{18}*b^{(7/3)}*(a/b + \\
& x)^{2}*exp(2*I*pi/3) - 2800*a^{17}*b^{(10/3)}*(a/b + x)^{3}*exp(2*I*pi/3) + 21 \\
& 00*a^{16}*b^{(13/3)}*(a/b + x)^{4}*exp(2*I*pi/3) - 840*a^{15}*b^{(16/3)}*(a/b + \\
& x)^{5}*exp(2*I*pi/3) + 140*a^{14}*b^{(19/3)}*(a/b + x)^{6}*exp(2*I*pi/3) + 364 \\
& 5*a^{(58/3)}*b^{4}*(a/b + x)^{4}/(140*a^{20}*b^{(1/3)}*exp(2*I*pi/3) - 840*a^{19} \\
& *b^{(4/3)}*(a/b + x)*exp(2*I*pi/3) + 2100*a^{18}*b^{(7/3)}*(a/b + x)^{2}*exp(2* \\
& I*pi/3) - 2800*a^{17}*b^{(10/3)}*(a/b + x)^{3}*exp(2*I*pi/3) + 2100*a^{16}*b^{(\\
& 13/3)}*(a/b + x)^{4}*exp(2*I*pi/3) - 840*a^{15}*b^{(16/3)}*(a/b + x)^{5}*exp(2*I \\
& *pi/3) + 140*a^{14}*b^{(19/3)}*(a/b + x)^{6}*exp(2*I*pi/3) + 693*a^{(55/3)}*b \\
& *5*(1 - b*(a/b + x)/a)^{(1/3)}*(a/b + x)^{5}/(140*a^{20}*b^{(1/3)}*exp(2*I*pi/3) \\
&) - 840*a^{19}*b^{(4/3)}*(a/b + x)*exp(2*I*pi/3) + 2100*a^{18}*b^{(7/3)}*(a/b + \\
& x)^{2}*exp(2*I*pi/3) - 2800*a^{17}*b^{(10/3)}*(a/b + x)^{3}*exp(2*I*pi/3) + 21 \\
& 00*a^{16}*b^{(13/3)}*(a/b + x)^{4}*exp(2*I*pi/3) - 840*a^{15}*b^{(16/3)}*(a/b + \\
& x)^{5}*exp(2*I*pi/3) + 140*a^{14}*b^{(19/3)}*(a/b + x)^{6}*exp(2*I*pi/3) - 145 \\
& 8*a^{(55/3)}*b^{5}*(a/b + x)^{5}/(140*a^{20}*b^{(1/3)}*exp(2*I*pi/3) - 840*a^{19} \\
& *b^{(4/3)}*(a/b + x)*exp(2*I*pi/3) + 2100*a^{18}*b^{(7/3)}*(a/b + x)^{2}*exp(2* \\
& I*pi/3) - 2800*a^{17}*b^{(10/3)}*(a/b + x)^{3}*exp(2*I*pi/3) + 2100*a^{16}*b^{(\\
& 13/3)}*(a/b + x)^{4}*exp(2*I*pi/3) - 840*a^{15}*b^{(16/3)}*(a/b + x)^{5}*exp(2*I \\
& *pi/3) + 140*a^{14}*b^{(19/3)}*(a/b + x)^{6}*exp(2*I*pi/3) + 273*a^{(52/3)}*b \\
& *6*(1 - b*(a/b + x)/a)^{(1/3)}*(a/b + x)^{6}/(140*a^{20}*b^{(1/3)}*exp(2*I*pi/3) \\
&) - 840*a^{19}*b^{(4/3)}*(a/b + x)*exp(2*I*pi/3) + 2100*a^{18}*b^{(7/3)}*(a/b + \\
& x)^{2}*exp(2*I*pi/3) - 2800*a^{17}*b^{(10/3)}*(a/b + x)^{3}*exp(2*I*pi/3) + 21 \\
& 00*a^{16}*b^{(13/3)}*(a/b + x)^{4}*exp(2*I*pi/3) - 840*a^{15}*b^{(16/3)}*(a/b + \\
& x)^{5}*exp(2*I*pi/3) + 140*a^{14}*b^{(19/3)}*(a/b + x)^{6}*exp(2*I*pi/3) + 243 \\
& *a^{(52/3)}*b^{6}*(a/b + x)^{6}/(140*a^{20}*b^{(1/3)}*exp(2*I*pi/3) - 840*a^{19}* \\
& b^{(4/3)}*(a/b + x)*exp(2*I*pi/3) + 2100*a^{18}*b^{(7/3)}*(a/b + x)^{2}*exp(2*I \\
& *pi/3) - 2800*a^{17}*b^{(10/3)}*(a/b + x)^{3}*exp(2*I*pi/3) + 2100*a^{16}*b^{(1 \\
& 3/3)}*(a/b + x)^{4}*exp(2*I*pi/3) - 840*a^{15}*b^{(16/3)}*(a/b + x)^{5}*exp(2*I* \\
& pi/3) + 140*a^{14}*b^{(19/3)}*(a/b + x)^{6}*exp(2*I*pi/3) - 387*a^{(49/3)}*b \\
& *7*(1 - b*(a/b + x)/a)^{(1/3)}*(a/b + x)^{7}/(140*a^{20}*b^{(1/3)}*exp(2*I*pi/3) \\
& - 840*a^{19}*b^{(4/3)}*(a/b + x)*exp(2*I*pi/3) + 2100*a^{18}*b^{(7/3)}*(a/b + \\
& x)^{2}*exp(2*I*pi/3) - 2800*a^{17}*b^{(10/3)}*(a/b + x)^{3}*exp(2*I*pi/3) + 210 \\
& 0*a^{16}*b^{(13/3)}*(a/b + x)^{4}*exp(2*I*pi/3) - 840*a^{15}*b^{(16/3)}*(a/b + x
\end{aligned}$$

```

)**5*exp(2*I*pi/3) + 140*a**14*b**(19/3)*(a/b + x)**6*exp(2*I*pi/3)) + 198*
a**(46/3)*b**8*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**8/(140*a**20*b**(1/3)*
exp(2*I*pi/3) - 840*a**19*b**(4/3)*(a/b + x)*exp(2*I*pi/3) + 2100*a**18*b**
(7/3)*(a/b + x)**2*exp(2*I*pi/3) - 2800*a**17*b**(10/3)*(a/b + x)**3*exp(2*
I*pi/3) + 2100*a**16*b**(13/3)*(a/b + x)**4*exp(2*I*pi/3) - 840*a**15*b**(1
6/3)*(a/b + x)**5*exp(2*I*pi/3) + 140*a**14*b**(19/3)*(a/b + x)**6*exp(2*I*
pi/3)) - 42*a**(43/3)*b**9*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**9/(140*a**
20*b**(1/3)*exp(2*I*pi/3) - 840*a**19*b**(4/3)*(a/b + x)*exp(2*I*pi/3) + 21
00*a**18*b**(7/3)*(a/b + x)**2*exp(2*I*pi/3) - 2800*a**17*b**(10/3)*(a/b +
x)**3*exp(2*I*pi/3) + 2100*a**16*b**(13/3)*(a/b + x)**4*exp(2*I*pi/3) - 840
*a**15*b**(16/3)*(a/b + x)**5*exp(2*I*pi/3) + 140*a**14*b**(19/3)*(a/b + x)
**6*exp(2*I*pi/3)), True))

```

$$3.672 \quad \int \frac{(a+bx)^3}{x^{4/3}} dx$$

Optimal. Leaf size=49

$$-\frac{3a^3}{\sqrt[3]{x}} + \frac{9}{2}a^2bx^{2/3} + \frac{9}{5}ab^2x^{5/3} + \frac{3}{8}b^3x^{8/3}$$

[Out] $-3*a^3/x^{(1/3)}+9/2*a^2*b*x^{(2/3)}+9/5*a*b^2*x^{(5/3)}+3/8*b^3*x^{(8/3)}$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{9}{2}a^2bx^{2/3} - \frac{3a^3}{\sqrt[3]{x}} + \frac{9}{5}ab^2x^{5/3} + \frac{3}{8}b^3x^{8/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^(4/3), x]

[Out] $(-3*a^3)/x^{(1/3)} + (9*a^2*b*x^{(2/3)})/2 + (9*a*b^2*x^{(5/3)})/5 + (3*b^3*x^{(8/3)})/8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^{4/3}} dx &= \int \left(\frac{a^3}{x^{4/3}} + \frac{3a^2b}{\sqrt[3]{x}} + 3ab^2x^{2/3} + b^3x^{5/3} \right) dx \\ &= -\frac{3a^3}{\sqrt[3]{x}} + \frac{9}{2}a^2bx^{2/3} + \frac{9}{5}ab^2x^{5/3} + \frac{3}{8}b^3x^{8/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.80

$$\frac{3(-40a^3 + 60a^2bx + 24ab^2x^2 + 5b^3x^3)}{40\sqrt[3]{x}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^(4/3), x]

[Out] (3*(-40*a^3 + 60*a^2*b*x + 24*a*b^2*x^2 + 5*b^3*x^3))/(40*x^(1/3))

fricas [A] time = 0.45, size = 35, normalized size = 0.71

$$\frac{3(5b^3x^3 + 24ab^2x^2 + 60a^2bx - 40a^3)}{40x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(4/3), x, algorithm="fricas")

[Out] 3/40*(5*b^3*x^3 + 24*a*b^2*x^2 + 60*a^2*b*x - 40*a^3)/x^(1/3)

giac [A] time = 1.07, size = 35, normalized size = 0.71

$$\frac{3}{8}b^3x^{\frac{8}{3}} + \frac{9}{5}ab^2x^{\frac{5}{3}} + \frac{9}{2}a^2bx^{\frac{2}{3}} - \frac{3a^3}{x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(4/3), x, algorithm="giac")

[Out] 3/8*b^3*x^(8/3) + 9/5*a*b^2*x^(5/3) + 9/2*a^2*b*x^(2/3) - 3*a^3/x^(1/3)

maple [A] time = 0.00, size = 36, normalized size = 0.73

$$\frac{3(-5b^3x^3 - 24ab^2x^2 - 60a^2bx + 40a^3)}{40x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/x^(4/3), x)

[Out] -3/40*(-5*b^3*x^3-24*a*b^2*x^2-60*a^2*b*x+40*a^3)/x^(1/3)

maxima [A] time = 1.32, size = 35, normalized size = 0.71

$$\frac{3}{8}b^3x^{\frac{8}{3}} + \frac{9}{5}ab^2x^{\frac{5}{3}} + \frac{9}{2}a^2bx^{\frac{2}{3}} - \frac{3a^3}{x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(4/3), x, algorithm="maxima")

[Out] $3/8*b^3*x^{(8/3)} + 9/5*a*b^2*x^{(5/3)} + 9/2*a^2*b*x^{(2/3)} - 3*a^3/x^{(1/3)}$

mupad [B] time = 0.04, size = 35, normalized size = 0.71

$$\frac{3b^3x^{8/3}}{8} - \frac{3a^3}{x^{1/3}} + \frac{9a^2bx^{2/3}}{2} + \frac{9ab^2x^{5/3}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^(4/3),x)`

[Out] $(3*b^3*x^{(8/3)})/8 - (3*a^3)/x^{(1/3)} + (9*a^2*b*x^{(2/3)})/2 + (9*a*b^2*x^{(5/3)})/5$

sympy [C] time = 3.26, size = 4004, normalized size = 81.71

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**(4/3),x)`

[Out] `Piecewise((243*a**(68/3)*b**(1/3)*(-1 + b*(a/b + x)/a)**(2/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) - 243*a**(68/3)*b**(1/3)*exp(2*I*pi/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) - 1296*a**(65/3)*b**(4/3)*(-1 + b*(a/b + x)/a)**(2/3)*(a/b + x)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) + 1458*a**(65/3)*b**(4/3)*(a/b + x)*exp(2*I*pi/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) + 2808*a**(62/3)*b**(7/3)*(-1 + b*(a/b + x)/a)**(2/3)*(a/b + x)**2/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) - 3645*a**(62/3)*b**(7/3)*(a/b + x)**2*exp(2*I*pi/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) - 3120*a**(59/3)*b**(10/3)*(-1 + b*(a/b + x)/a)**(2/3)*(a/b + x)**3/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) + 4860*a**(59/3)*b**(10/3)*(a/b + x)**3*exp(2*I*pi/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b`

$$\begin{aligned}
& + x)^{**2} - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a^{**16}*b^{**4}*(a/b + x)^{**4} - 240* \\
& a^{**15}*b^{**5}*(a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x)^{**6}) + 1830*a^{**56/3}*b^{**} \\
& (13/3)*(-1 + b*(a/b + x)/a)^{**2/3}*(a/b + x)^{**4}/(40*a^{**20} - 240*a^{**19}*b*(a/b \\
& + x) + 600*a^{**18}*b^{**2}*(a/b + x)^{**2} - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a^{**} \\
& 16*b^{**4}*(a/b + x)^{**4} - 240*a^{**15}*b^{**5}*(a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x \\
&)^{**6}) - 3645*a^{**56/3}*b^{**}(13/3)*(a/b + x)^{**4}*exp(2*I*pi/3)/(40*a^{**20} - 240 \\
& *a^{**19}*b*(a/b + x) + 600*a^{**18}*b^{**2}*(a/b + x)^{**2} - 800*a^{**17}*b^{**3}*(a/b + x) \\
&)^{**3} + 600*a^{**16}*b^{**4}*(a/b + x)^{**4} - 240*a^{**15}*b^{**5}*(a/b + x)^{**5} + 40*a^{**14} \\
& *b^{**6}*(a/b + x)^{**6}) - 528*a^{**53/3}*b^{**}(16/3)*(-1 + b*(a/b + x)/a)^{**2/3}*(a \\
& /b + x)^{**5}/(40*a^{**20} - 240*a^{**19}*b*(a/b + x) + 600*a^{**18}*b^{**2}*(a/b + x)^{**2} \\
& - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a^{**16}*b^{**4}*(a/b + x)^{**4} - 240*a^{**15}*b^{**} \\
& 5*(a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x)^{**6}) + 1458*a^{**53/3}*b^{**}(16/3)*(a/ \\
& b + x)^{**5}*exp(2*I*pi/3)/(40*a^{**20} - 240*a^{**19}*b*(a/b + x) + 600*a^{**18}*b^{**2} \\
& (a/b + x)^{**2} - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a^{**16}*b^{**4}*(a/b + x)^{**4} - \\
& 240*a^{**15}*b^{**5}*(a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x)^{**6}) + 96*a^{**50/3}*b* \\
& *(19/3)*(-1 + b*(a/b + x)/a)^{**2/3}*(a/b + x)^{**6}/(40*a^{**20} - 240*a^{**19}*b*(a \\
& /b + x) + 600*a^{**18}*b^{**2}*(a/b + x)^{**2} - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a \\
&)^{**4} - 240*a^{**15}*b^{**5}*(a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x)^{**6}) - 243*a^{**50/3} \\
& *b^{**}(19/3)*(a/b + x)^{**6}*exp(2*I*pi/3)/(40*a^{**20} - 24 \\
& 0*a^{**19}*b*(a/b + x) + 600*a^{**18}*b^{**2}*(a/b + x)^{**2} - 800*a^{**17}*b^{**3}*(a/b + x \\
&)^{**3} + 600*a^{**16}*b^{**4}*(a/b + x)^{**4} - 240*a^{**15}*b^{**5}*(a/b + x)^{**5} + 40*a^{**14} \\
& *b^{**6}*(a/b + x)^{**6}) - 48*a^{**47/3}*b^{**}(22/3)*(-1 + b*(a/b + x)/a)^{**2/3}*(a \\
& /b + x)^{**7}/(40*a^{**20} - 240*a^{**19}*b*(a/b + x) + 600*a^{**18}*b^{**2}*(a/b + x)^{**2} \\
& - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a^{**16}*b^{**4}*(a/b + x)^{**4} - 240*a^{**15}*b^{**} \\
& 5*(a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x)^{**6}) + 15*a^{**44/3}*b^{**}(25/3)*(-1 + \\
& b*(a/b + x)/a)^{**2/3}*(a/b + x)^{**8}/(40*a^{**20} - 240*a^{**19}*b*(a/b + x) + 600 \\
& *a^{**18}*b^{**2}*(a/b + x)^{**2} - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a^{**16}*b^{**4}*(a/ \\
& b + x)^{**4} - 240*a^{**15}*b^{**5}*(a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x)^{**6}), Abs(\\
& b*(a/b + x)/a) > 1), (243*a^{**68/3}*b^{**}(1/3)*(1 - b*(a/b + x)/a)^{**2/3}*exp \\
& (2*I*pi/3)/(40*a^{**20} - 240*a^{**19}*b*(a/b + x) + 600*a^{**18}*b^{**2}*(a/b + x)^{**2} \\
& - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a^{**16}*b^{**4}*(a/b + x)^{**4} - 240*a^{**15}*b^{**} \\
& 5*(a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x)^{**6}) - 243*a^{**68/3}*b^{**}(1/3)*exp(2 \\
& *I*pi/3)/(40*a^{**20} - 240*a^{**19}*b*(a/b + x) + 600*a^{**18}*b^{**2}*(a/b + x)^{**2} - \\
& 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a^{**16}*b^{**4}*(a/b + x)^{**4} - 240*a^{**15}*b^{**5} \\
& (a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x)^{**6}) - 1296*a^{**65/3}*b^{**}(4/3)*(1 - b \\
& *(a/b + x)/a)^{**2/3}*(a/b + x)*exp(2*I*pi/3)/(40*a^{**20} - 240*a^{**19}*b*(a/b + \\
& x) + 600*a^{**18}*b^{**2}*(a/b + x)^{**2} - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a^{**16} \\
&)^{**4} - 240*a^{**15}*b^{**5}*(a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x)^{**6}) + 1458*a^{**65/3} \\
& *b^{**}(4/3)*(a/b + x)*exp(2*I*pi/3)/(40*a^{**20} - 240*a^{**19} \\
& *b*(a/b + x) + 600*a^{**18}*b^{**2}*(a/b + x)^{**2} - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + \\
& 600*a^{**16}*b^{**4}*(a/b + x)^{**4} - 240*a^{**15}*b^{**5}*(a/b + x)^{**5} + 40*a^{**14}*b^{**6}*(\\
& a/b + x)^{**6}) + 2808*a^{**62/3}*b^{**}(7/3)*(1 - b*(a/b + x)/a)^{**2/3}*(a/b + x) \\
&)^{**2}*exp(2*I*pi/3)/(40*a^{**20} - 240*a^{**19}*b*(a/b + x) + 600*a^{**18}*b^{**2}*(a/b + \\
& x)^{**2} - 800*a^{**17}*b^{**3}*(a/b + x)^{**3} + 600*a^{**16}*b^{**4}*(a/b + x)^{**4} - 240*a \\
&)^{**5} + 40*a^{**14}*b^{**6}*(a/b + x)^{**6}) - 3645*a^{**62/3}*b^{**}(7/
\end{aligned}$$

```

3)*(a/b + x)**2*exp(2*I*pi/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18
*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)
**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) - 3120*a**
(59/3)*b**(10/3)*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**3*exp(2*I*pi/3)/(40*a
**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3
*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 +
40*a**14*b**6*(a/b + x)**6) + 4860*a**
(59/3)*b**(10/3)*(a/b + x)**3*exp(2*
I*pi/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 8
00*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(
a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) + 1830*a**
(56/3)*b**(13/3)*(1 - b
*(a/b + x)/a)**(2/3)*(a/b + x)**4*exp(2*I*pi/3)/(40*a**20 - 240*a**19*b*(a/
b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a
**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b +
x)**6) - 3645*a**
(56/3)*b**(13/3)*(a/b + x)**4*exp(2*I*pi/3)/(40*a**20 - 24
0*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x
)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14
*b**6*(a/b + x)**6) - 528*a**
(53/3)*b**(16/3)*(1 - b*(a/b + x)/a)**(2/3)*(a
/b + x)**5*exp(2*I*pi/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2
*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 -
240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) + 1458*a**
(53/3)
*b**(16/3)*(a/b + x)**5*exp(2*I*pi/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 6
00*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(
a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) + 9
6*a**
(50/3)*b**(19/3)*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**6*exp(2*I*pi/3)
/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**1
7*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x
)**5 + 40*a**14*b**6*(a/b + x)**6) - 243*a**
(50/3)*b**(19/3)*(a/b + x)**6*e
xp(2*I*pi/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)**
2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*b
**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6) - 48*a**
(47/3)*b**(22/3)*(1
- b*(a/b + x)/a)**(2/3)*(a/b + x)**7*exp(2*I*pi/3)/(40*a**20 - 240*a**19*b*
(a/b + x) + 600*a**18*b**2*(a/b + x)**2 - 800*a**17*b**3*(a/b + x)**3 + 600
*a**16*b**4*(a/b + x)**4 - 240*a**15*b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b
+ x)**6) + 15*a**
(44/3)*b**(25/3)*(1 - b*(a/b + x)/a)**(2/3)*(a/b + x)**8*
exp(2*I*pi/3)/(40*a**20 - 240*a**19*b*(a/b + x) + 600*a**18*b**2*(a/b + x)
**2 - 800*a**17*b**3*(a/b + x)**3 + 600*a**16*b**4*(a/b + x)**4 - 240*a**15*
b**5*(a/b + x)**5 + 40*a**14*b**6*(a/b + x)**6), True))

```

$$3.673 \quad \int \frac{(a+bx)^3}{x^{5/3}} dx$$

Optimal. Leaf size=49

$$-\frac{3a^3}{2x^{2/3}} + 9a^2b\sqrt[3]{x} + \frac{9}{4}ab^2x^{4/3} + \frac{3}{7}b^3x^{7/3}$$

[Out] $-3/2*a^3/x^{(2/3)}+9*a^2*b*x^{(1/3)}+9/4*a*b^2*x^{(4/3)}+3/7*b^3*x^{(7/3)}$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$9a^2b\sqrt[3]{x} - \frac{3a^3}{2x^{2/3}} + \frac{9}{4}ab^2x^{4/3} + \frac{3}{7}b^3x^{7/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/x^(5/3), x]

[Out] $(-3*a^3)/(2*x^{(2/3)}) + 9*a^2*b*x^{(1/3)} + (9*a*b^2*x^{(4/3)})/4 + (3*b^3*x^{(7/3)})/7$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{x^{5/3}} dx &= \int \left(\frac{a^3}{x^{5/3}} + \frac{3a^2b}{x^{2/3}} + 3ab^2\sqrt[3]{x} + b^3x^{4/3} \right) dx \\ &= -\frac{3a^3}{2x^{2/3}} + 9a^2b\sqrt[3]{x} + \frac{9}{4}ab^2x^{4/3} + \frac{3}{7}b^3x^{7/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.80

$$\frac{3(-14a^3 + 84a^2bx + 21ab^2x^2 + 4b^3x^3)}{28x^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/x^(5/3),x]

[Out] (3*(-14*a^3 + 84*a^2*b*x + 21*a*b^2*x^2 + 4*b^3*x^3))/(28*x^(2/3))

fricas [A] time = 0.42, size = 35, normalized size = 0.71

$$\frac{3(4b^3x^3 + 21ab^2x^2 + 84a^2bx - 14a^3)}{28x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(5/3),x, algorithm="fricas")

[Out] 3/28*(4*b^3*x^3 + 21*a*b^2*x^2 + 84*a^2*b*x - 14*a^3)/x^(2/3)

giac [A] time = 1.17, size = 35, normalized size = 0.71

$$\frac{3}{7}b^3x^{\frac{7}{3}} + \frac{9}{4}ab^2x^{\frac{4}{3}} + 9a^2bx^{\frac{1}{3}} - \frac{3a^3}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(5/3),x, algorithm="giac")

[Out] 3/7*b^3*x^(7/3) + 9/4*a*b^2*x^(4/3) + 9*a^2*b*x^(1/3) - 3/2*a^3/x^(2/3)

maple [A] time = 0.00, size = 36, normalized size = 0.73

$$\frac{3(-4b^3x^3 - 21ab^2x^2 - 84a^2bx + 14a^3)}{28x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/x^(5/3),x)

[Out] -3/28*(-4*b^3*x^3-21*a*b^2*x^2-84*a^2*b*x+14*a^3)/x^(2/3)

maxima [A] time = 1.36, size = 35, normalized size = 0.71

$$\frac{3}{7}b^3x^{\frac{7}{3}} + \frac{9}{4}ab^2x^{\frac{4}{3}} + 9a^2bx^{\frac{1}{3}} - \frac{3a^3}{2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/x^(5/3),x, algorithm="maxima")

[Out] 3/7*b^3*x^(7/3) + 9/4*a*b^2*x^(4/3) + 9*a^2*b*x^(1/3) - 3/2*a^3/x^(2/3)

mupad [B] time = 0.04, size = 35, normalized size = 0.71

$$\frac{3b^3x^{7/3}}{7} - \frac{3a^3}{2x^{2/3}} + 9a^2bx^{1/3} + \frac{9ab^2x^{4/3}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3/x^(5/3), x)`

[Out] `(3*b^3*x^(7/3))/7 - (3*a^3)/(2*x^(2/3)) + 9*a^2*b*x^(1/3) + (9*a*b^2*x^(4/3))/4`

sympy [C] time = 3.24, size = 3964, normalized size = 80.90

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3/x**(5/3), x)`

[Out] `Piecewise((243*a**(67/3)*b**(2/3)*(-1 + b*(a/b + x)/a)**(1/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) - 243*a**(67/3)*b**(2/3)*exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) - 1377*a**(64/3)*b**(5/3)*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) + 1458*a**(64/3)*b**(5/3)*(a/b + x)*exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) + 3213*a**(61/3)*b**(8/3)*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**2/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) - 3645*a**(61/3)*b**(8/3)*(a/b + x)**2*exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) - 3927*a**(58/3)*b**(11/3)*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**3/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) + 4860*a**(58/3)*b**(11/3)*(a/b + x)**3*exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) + 2625*a**(55/3)*b**(14/3)*(-`

$$\begin{aligned}
& 1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**4/(28*a**20 - 168*a**19*b*(a/b + x) + \\
& 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4* \\
& (a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) - \\
& 3645*a**(55/3)*b**(14/3)*(a/b + x)**4*\exp(I*pi/3)/(28*a**20 - 168*a**19*b*(\\
& a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420* \\
& a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b \\
& + x)**6) - 903*a**(52/3)*b**(17/3)*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**5 \\
& /(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**1 \\
& 7*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x \\
&)**5 + 28*a**14*b**6*(a/b + x)**6) + 1458*a**(52/3)*b**(17/3)*(a/b + x)**5* \\
& \exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 \\
& - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b* \\
& **5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) + 147*a**(49/3)*b**(20/3)*(-1 \\
& + b*(a/b + x)/a)**(1/3)*(a/b + x)**6/(28*a**20 - 168*a**19*b*(a/b + x) + 4 \\
& 20*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(\\
& a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) - 2 \\
& 43*a**(49/3)*b**(20/3)*(a/b + x)**6*\exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/ \\
& b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a* \\
& *16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + \\
& x)**6) - 33*a**(46/3)*b**(23/3)*(-1 + b*(a/b + x)/a)**(1/3)*(a/b + x)**7/(2 \\
& 8*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b \\
& **3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)** \\
& 5 + 28*a**14*b**6*(a/b + x)**6) + 12*a**(43/3)*b**(26/3)*(-1 + b*(a/b + x)/ \\
& a)**(1/3)*(a/b + x)**8/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(\\
& a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 1 \\
& 68*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6), \text{Abs}(b*(a/b + x)/a \\
&) > 1), (243*a**(67/3)*b**(2/3)*(1 - b*(a/b + x)/a)**(1/3)*\exp(I*pi/3)/(28* \\
& a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b** \\
& 3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 \\
& + 28*a**14*b**6*(a/b + x)**6) - 243*a**(67/3)*b**(2/3)*\exp(I*pi/3)/(28*a**2 \\
& 0 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a \\
& /b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28 \\
& *a**14*b**6*(a/b + x)**6) - 1377*a**(64/3)*b**(5/3)*(1 - b*(a/b + x)/a)**(1 \\
& /3)*(a/b + x)*\exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b** \\
& 2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 \\
& - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) + 1458*a**(64/3 \\
&)*b**(5/3)*(a/b + x)*\exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a* \\
& *18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + \\
& x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) + 3213*a \\
& *(61/3)*b**(8/3)*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**2*\exp(I*pi/3)/(28*a \\
& **20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3 \\
& *(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + \\
& 28*a**14*b**6*(a/b + x)**6) - 3645*a**(61/3)*b**(8/3)*(a/b + x)**2*\exp(I*p \\
& i/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560* \\
& a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b
\end{aligned}$$

```

+ x)**5 + 28*a**14*b**6*(a/b + x)**6) - 3927*a**(58/3)*b**(11/3)*(1 - b*(a
/b + x)/a)**(1/3)*(a/b + x)**3*exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x
) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b
**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6
) + 4860*a**(58/3)*b**(11/3)*(a/b + x)**3*exp(I*pi/3)/(28*a**20 - 168*a**19
*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 +
420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(
a/b + x)**6) + 2625*a**(55/3)*b**(14/3)*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x
)**4*exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b +
x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**
15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) - 3645*a**(55/3)*b**(14/
3)*(a/b + x)**4*exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b
**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**
4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) - 903*a**(52/
3)*b**(17/3)*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**5*exp(I*pi/3)/(28*a**20
- 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b
+ x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a
**14*b**6*(a/b + x)**6) + 1458*a**(52/3)*b**(17/3)*(a/b + x)**5*exp(I*pi/3)
/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**1
7*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x
)**5 + 28*a**14*b**6*(a/b + x)**6) + 147*a**(49/3)*b**(20/3)*(1 - b*(a/b +
x)/a)**(1/3)*(a/b + x)**6*exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 4
20*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(
a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) - 2
43*a**(49/3)*b**(20/3)*(a/b + x)**6*exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/
b + x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a*
**16*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b +
x)**6) - 33*a**(46/3)*b**(23/3)*(1 - b*(a/b + x)/a)**(1/3)*(a/b + x)**7*exp
(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b + x) + 420*a**18*b**2*(a/b + x)**2 -
560*a**17*b**3*(a/b + x)**3 + 420*a**16*b**4*(a/b + x)**4 - 168*a**15*b**5*
(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**6) + 12*a**(43/3)*b**(26/3)*(1 - b*
(a/b + x)/a)**(1/3)*(a/b + x)**8*exp(I*pi/3)/(28*a**20 - 168*a**19*b*(a/b +
x) + 420*a**18*b**2*(a/b + x)**2 - 560*a**17*b**3*(a/b + x)**3 + 420*a**16
*b**4*(a/b + x)**4 - 168*a**15*b**5*(a/b + x)**5 + 28*a**14*b**6*(a/b + x)**
6), True))

```


$$3.674 \quad \int \frac{x^{5/3}}{a+bx} dx$$

Optimal. Leaf size=125

$$-\frac{3a^{5/3} \log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{2b^{8/3}} + \frac{a^{5/3} \log(ax+b)}{2b^{8/3}} - \frac{\sqrt{3} a^{5/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{b^{8/3}} - \frac{3ax^{2/3}}{2b^2} + \frac{3x^{5/3}}{5b}$$

[Out] $-3/2*a*x^{(2/3)}/b^2+3/5*x^{(5/3)}/b-3/2*a^{(5/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/b^{(8/3)}+1/2*a^{(5/3)}*\ln(b*x+a)/b^{(8/3)}-a^{(5/3)}*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/b^{(8/3)}$

Rubi [A] time = 0.07, antiderivative size = 125, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {50, 56, 617, 204, 31}

$$-\frac{3a^{5/3} \log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{2b^{8/3}} + \frac{a^{5/3} \log(ax+b)}{2b^{8/3}} - \frac{\sqrt{3} a^{5/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{b^{8/3}} - \frac{3ax^{2/3}}{2b^2} + \frac{3x^{5/3}}{5b}$$

Antiderivative was successfully verified.

[In] Int[x^(5/3)/(a + b*x), x]

[Out] $(-3*a*x^{(2/3)})/(2*b^2) + (3*x^{(5/3)})/(5*b) - (\text{Sqrt}[3]*a^{(5/3)}*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/b^{(8/3)} - (3*a^{(5/3)}*\text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(2*b^{(8/3)}) + (a^{(5/3)}*\text{Log}[a + b*x])/ (2*b^{(8/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 56

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),

```
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]) / ; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
 \int \frac{x^{5/3}}{a+bx} dx &= \frac{3x^{5/3}}{5b} - \frac{a \int \frac{x^{2/3}}{a+bx} dx}{b} \\
 &= -\frac{3ax^{2/3}}{2b^2} + \frac{3x^{5/3}}{5b} + \frac{a^2 \int \frac{1}{\sqrt[3]{x}(a+bx)} dx}{b^2} \\
 &= -\frac{3ax^{2/3}}{2b^2} + \frac{3x^{5/3}}{5b} + \frac{a^{5/3} \log(a+bx)}{2b^{8/3}} + \frac{(3a^2) \text{Subst} \left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{ax}}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x} \right)}{2b^3} - \frac{(3a^{5/3}) \text{Subst} \left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}} \right)}{2b^{8/3}} \\
 &= -\frac{3ax^{2/3}}{2b^2} + \frac{3x^{5/3}}{5b} - \frac{3a^{5/3} \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{2b^{8/3}} + \frac{a^{5/3} \log(a+bx)}{2b^{8/3}} + \frac{(3a^{5/3}) \text{Subst} \left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}} \right)}{b^{8/3}} \\
 &= -\frac{3ax^{2/3}}{2b^2} + \frac{3x^{5/3}}{5b} - \frac{\sqrt{3} a^{5/3} \tan^{-1} \left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}} \right)}{b^{8/3}} - \frac{3a^{5/3} \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{2b^{8/3}} + \frac{a^{5/3} \log(a+bx)}{2b^{8/3}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 38, normalized size = 0.30

$$\frac{3x^{2/3} \left(5a {}_2F_1 \left(\frac{2}{3}, 1; \frac{5}{3}; -\frac{bx}{a} \right) - 5a + 2bx \right)}{10b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/3)/(a + b*x), x]

[Out] (3*x^(2/3)*(-5*a + 2*b*x + 5*a*Hypergeometric2F1[2/3, 1, 5/3, -(b*x)/a]))/(10*b^2)

fricas [A] time = 0.46, size = 147, normalized size = 1.18

$$\frac{10\sqrt{3}a\left(-\frac{a^2}{b^2}\right)^{\frac{1}{3}}\arctan\left(\frac{2\sqrt{3}bx^{\frac{1}{3}}\left(-\frac{a^2}{b^2}\right)^{\frac{1}{3}}+\sqrt{3}a}{3a}\right)-5a\left(-\frac{a^2}{b^2}\right)^{\frac{1}{3}}\log\left(-bx^{\frac{1}{3}}\left(-\frac{a^2}{b^2}\right)^{\frac{2}{3}}+ax^{\frac{2}{3}}-a\left(-\frac{a^2}{b^2}\right)^{\frac{1}{3}}\right)+10a\left(-\frac{a^2}{b^2}\right)^{\frac{1}{3}}\log\left(-bx^{\frac{1}{3}}\left(-\frac{a^2}{b^2}\right)^{\frac{2}{3}}+ax^{\frac{2}{3}}-a\left(-\frac{a^2}{b^2}\right)^{\frac{1}{3}}\right)}{10b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)/(b*x+a), x, algorithm="fricas")

[Out] 1/10*(10*sqrt(3)*a*(-a^2/b^2)^(1/3)*arctan(1/3*(2*sqrt(3)*b*x^(1/3)*(-a^2/b^2)^(1/3) + sqrt(3)*a)/a) - 5*a*(-a^2/b^2)^(1/3)*log(-b*x^(1/3)*(-a^2/b^2)^(2/3) + a*x^(2/3) - a*(-a^2/b^2)^(1/3)) + 10*a*(-a^2/b^2)^(1/3)*log(b*(-a^2/b^2)^(2/3) + a*x^(1/3)) + 3*(2*b*x - 5*a)*x^(2/3)/b^2

giac [A] time = 1.04, size = 138, normalized size = 1.10

$$\frac{a\left(-\frac{a}{b}\right)^{\frac{2}{3}}\log\left(x^{\frac{1}{3}}-\left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{b^2}-\frac{\sqrt{3}\left(-ab^2\right)^{\frac{2}{3}}a\arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}+\left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{b^4}+\frac{\left(-ab^2\right)^{\frac{2}{3}}a\log\left(x^{\frac{2}{3}}+x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}}+\left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)/(b*x+a), x, algorithm="giac")

[Out] -a*(-a/b)^(2/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/b^2 - sqrt(3)*(-a*b^2)^(2/3)*a*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/b^4 + 1/2*(-a*b^2)^(2/3)*a*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/b^4 + 3/10*(2*b^4*x^(5/3) - 5*a*b^3*x^(2/3))/b^5

maple [A] time = 0.01, size = 122, normalized size = 0.98

$$\frac{3x^{\frac{5}{3}}}{5b} + \frac{\sqrt{3} a^2 \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{\left(\frac{a}{b}\right)^{\frac{1}{3}} b^3} - \frac{a^2 \ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{\left(\frac{a}{b}\right)^{\frac{1}{3}} b^3} + \frac{a^2 \ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2\left(\frac{a}{b}\right)^{\frac{1}{3}} b^3} - \frac{3ax^{\frac{2}{3}}}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/3)/(b*x+a),x)

[Out] 3/5*x^(5/3)/b-3/2*a*x^(2/3)/b^2-a^2/b^3/(a/b)^(1/3)*ln(x^(1/3)+(a/b)^(1/3))+1/2*a^2/b^3/(a/b)^(1/3)*ln(x^(2/3)-(a/b)^(1/3)*x^(1/3)+(a/b)^(2/3))+a^2/b^3*3^(1/2)/(a/b)^(1/3)*arctan(1/3*3^(1/2)*(2/(a/b)^(1/3)*x^(1/3)-1))

maxima [A] time = 3.00, size = 130, normalized size = 1.04

$$\frac{\sqrt{3} a^2 \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{b^3\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{a^2 \log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2b^3\left(\frac{a}{b}\right)^{\frac{1}{3}}} - \frac{a^2 \log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{b^3\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{3\left(2bx^{\frac{5}{3}} - 5ax^{\frac{2}{3}}\right)}{10b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)/(b*x+a),x, algorithm="maxima")

[Out] sqrt(3)*a^2*arctan(1/3*sqrt(3)*(2*x^(1/3) - (a/b)^(1/3))/(a/b)^(1/3))/(b^3*(a/b)^(1/3)) + 1/2*a^2*log(x^(2/3) - x^(1/3)*(a/b)^(1/3) + (a/b)^(2/3))/(b^3*(a/b)^(1/3)) - a^2*log(x^(1/3) + (a/b)^(1/3))/(b^3*(a/b)^(1/3)) + 3/10*(2*b*x^(5/3) - 5*a*x^(2/3))/b^2

mupad [B] time = 0.24, size = 151, normalized size = 1.21

$$\frac{3x^{\frac{5}{3}}}{5b} + \frac{(-a)^{\frac{5}{3}} \ln\left(\frac{9a^4 x^{\frac{1}{3}}}{b^3} - \frac{9(-a)^{\frac{13}{3}}}{b^{10/3}}\right)}{b^{8/3}} - \frac{3ax^{\frac{2}{3}}}{2b^2} + \frac{(-a)^{\frac{5}{3}} \ln\left(\frac{9a^4 x^{\frac{1}{3}}}{b^3} - \frac{9(-a)^{\frac{13}{3}}\left(-\frac{1}{2} + \frac{\sqrt{3}ii}{2}\right)^2}{b^{10/3}}\right)}{b^{8/3}} - \frac{\left(-\frac{1}{2} + \frac{\sqrt{3}ii}{2}\right) (-a)^{\frac{5}{3}} \ln\left(\frac{9a^4 x^{\frac{1}{3}}}{b^3} - \frac{9(-a)^{\frac{13}{3}}\left(-\frac{1}{2} + \frac{\sqrt{3}ii}{2}\right)^2}{b^{10/3}}\right)}{b^{8/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/3)/(a + b*x),x)`

[Out] $(3*x^{5/3})/(5*b) + ((-a)^{5/3}*\log((9*a^4*x^{1/3})/b^3 - (9*(-a)^{13/3})/b^{10/3}))/b^{8/3} - (3*a*x^{2/3})/(2*b^2) + ((-a)^{5/3}*\log((9*a^4*x^{1/3})/b^3 - (9*(-a)^{13/3}*((3^{1/2}*1i)/2 - 1/2)^2)/b^{10/3})*((3^{1/2}*1i)/2 - 1/2))/b^{8/3} - ((-a)^{5/3}*\log((9*a^4*x^{1/3})/b^3 - (9*(-a)^{13/3}*((3^{1/2}*1i)/2 + 1/2)^2)/b^{10/3})*((3^{1/2}*1i)/2 + 1/2))/b^{8/3}$

sympy [A] time = 47.12, size = 241, normalized size = 1.93

$$\left\{ \begin{array}{l} \frac{5}{3}x^{\frac{5}{3}} \\ \frac{3x^{\frac{8}{3}}}{8a} \\ \frac{3x^{\frac{5}{3}}}{5b} \\ \frac{(-1)^{\frac{2}{3}}a^{\frac{5}{3}}\log\left(-\sqrt[3]{-1}\sqrt[3]{a}\sqrt[3]{\frac{1}{b}}+\sqrt[3]{x}\right)}{b^4\left(\frac{1}{b}\right)^{\frac{4}{3}}} + \frac{(-1)^{\frac{2}{3}}a^{\frac{5}{3}}\log\left(4(-1)^{\frac{2}{3}}a^{\frac{2}{3}}\left(\frac{1}{b}\right)^{\frac{2}{3}}+4\sqrt[3]{-1}\sqrt[3]{a}\sqrt[3]{x}\sqrt[3]{\frac{1}{b}}+4x^{\frac{2}{3}}\right)}{2b^4\left(\frac{1}{b}\right)^{\frac{4}{3}}} - \frac{(-1)^{\frac{2}{3}}\sqrt{3}a^{\frac{5}{3}}\operatorname{atan}\left(\frac{\sqrt{3}}{3}-\frac{2(-1)^{\frac{2}{3}}\sqrt{3}\sqrt[3]{x}}{3\sqrt[3]{a}\sqrt[3]{\frac{1}{b}}}\right)}{b^4\left(\frac{1}{b}\right)^{\frac{4}{3}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(5/3)/(b*x+a),x)`

[Out] `Piecewise((zoo*x**(5/3), Eq(a, 0) & Eq(b, 0)), (3*x**(8/3)/(8*a), Eq(b, 0)), (3*x**(5/3)/(5*b), Eq(a, 0)), ((-1)**(2/3)*a**(5/3)*log((-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(b**4*(1/b)**(4/3)) + (-1)**(2/3)*a**(5/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(2*b**4*(1/b)**(4/3)) - (-1)**(2/3)*sqrt(3)*a**(5/3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(b**4*(1/b)**(4/3)) - 3*a*x**(2/3)/(2*b**2) + 3*x**(5/3)/(5*b), True))`

$$3.675 \quad \int \frac{x^{4/3}}{a+bx} dx$$

Optimal. Leaf size=123

$$\frac{3a^{4/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{7/3}} - \frac{a^{4/3} \log(a+bx)}{2b^{7/3}} - \frac{\sqrt{3} a^{4/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{b^{7/3}} - \frac{3a\sqrt[3]{x}}{b^2} + \frac{3x^{4/3}}{4b}$$

[Out] $-3*a*x^{(1/3)}/b^2+3/4*x^{(4/3)}/b+3/2*a^{(4/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/b^{(7/3)}-1/2*a^{(4/3)}*\ln(b*x+a)/b^{(7/3)}-a^{(4/3)}*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})*3^{(1/2)}/b^{(7/3)}$

Rubi [A] time = 0.06, antiderivative size = 123, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {50, 58, 617, 204, 31}

$$\frac{3a^{4/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{7/3}} - \frac{a^{4/3} \log(a+bx)}{2b^{7/3}} - \frac{\sqrt{3} a^{4/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{b^{7/3}} - \frac{3a\sqrt[3]{x}}{b^2} + \frac{3x^{4/3}}{4b}$$

Antiderivative was successfully verified.

[In] Int[x^(4/3)/(a + b*x), x]

[Out] $(-3*a*x^{(1/3)})/b^2 + (3*x^{(4/3)})/(4*b) - (\text{Sqrt}[3]*a^{(4/3)}*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/b^{(7/3)} + (3*a^{(4/3)}*\text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(2*b^{(7/3)}) - (a^{(4/3)}*\text{Log}[a + b*x])/ (2*b^{(7/3)})$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 50

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 58

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^

2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]) /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{x^{4/3}}{a+bx} dx &= \frac{3x^{4/3}}{4b} - \frac{a \int \frac{\sqrt[3]{x}}{a+bx} dx}{b} \\
 &= -\frac{3a\sqrt[3]{x}}{b^2} + \frac{3x^{4/3}}{4b} + \frac{a^2 \int \frac{1}{x^{2/3}(a+bx)} dx}{b^2} \\
 &= -\frac{3a\sqrt[3]{x}}{b^2} + \frac{3x^{4/3}}{4b} - \frac{a^{4/3} \log(a+bx)}{2b^{7/3}} + \frac{(3a^{5/3}) \text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{ax}}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{2b^{8/3}} + \frac{(3a^{4/3}) \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1\right)}{2b^{7/3}} \\
 &= -\frac{3a\sqrt[3]{x}}{b^2} + \frac{3x^{4/3}}{4b} + \frac{3a^{4/3} \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{2b^{7/3}} - \frac{a^{4/3} \log(a+bx)}{2b^{7/3}} + \frac{(3a^{4/3}) \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1\right)}{b^{7/3}} \\
 &= -\frac{3a\sqrt[3]{x}}{b^2} + \frac{3x^{4/3}}{4b} - \frac{\sqrt{3} a^{4/3} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{b^{7/3}} + \frac{3a^{4/3} \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{2b^{7/3}} - \frac{a^{4/3} \log(a+bx)}{2b^{7/3}}
 \end{aligned}$$

Mathematica [A] time = 0.06, size = 140, normalized size = 1.14

$$\frac{-2a^{4/3} \log(a^{2/3} - \sqrt[3]{a} \sqrt[3]{b} \sqrt[3]{x} + b^{2/3} x^{2/3}) + 4a^{4/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}) - 4\sqrt{3} a^{4/3} \tan^{-1}\left(\frac{1 - 2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt[3]{a}}\right) - 12a \sqrt[3]{b} \sqrt[3]{x} + 3}{4b^{7/3}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(4/3)/(a + b*x), x]

[Out] (-12*a*b^(1/3)*x^(1/3) + 3*b^(4/3)*x^(4/3) - 4*Sqrt[3]*a^(4/3)*ArcTan[(1 - (2*b^(1/3)*x^(1/3))/a^(1/3))/Sqrt[3]] + 4*a^(4/3)*Log[a^(1/3) + b^(1/3)*x^(1/3)] - 2*a^(4/3)*Log[a^(2/3) - a^(1/3)*b^(1/3)*x^(1/3) + b^(2/3)*x^(2/3)])/(4*b^(7/3))

fricas [A] time = 0.46, size = 116, normalized size = 0.94

$$\frac{4\sqrt{3}a\left(\frac{a}{b}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}bx^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{2}{3}} - \sqrt{3}a}{3a}\right) - 2a\left(\frac{a}{b}\right)^{\frac{1}{3}} \log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right) + 4a\left(\frac{a}{b}\right)^{\frac{1}{3}} \log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right) + 3(bx - a)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)/(b*x+a), x, algorithm="fricas")

[Out] 1/4*(4*sqrt(3)*a*(a/b)^(1/3)*arctan(1/3*(2*sqrt(3)*b*x^(1/3)*(a/b)^(2/3) - sqrt(3)*a)/a) - 2*a*(a/b)^(1/3)*log(x^(2/3) - x^(1/3)*(a/b)^(1/3) + (a/b)^(2/3)) + 4*a*(a/b)^(1/3)*log(x^(1/3) + (a/b)^(1/3)) + 3*(b*x - 4*a)*x^(1/3)/b^2

giac [A] time = 1.21, size = 136, normalized size = 1.11

$$\frac{a\left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{b^2} + \frac{\sqrt{3}(-ab^2)^{\frac{1}{3}} a \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{b^3} + \frac{(-ab^2)^{\frac{1}{3}} a \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2b^3} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)/(b*x+a), x, algorithm="giac")

[Out] -a*(-a/b)^(1/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/b^2 + sqrt(3)*(-a*b^2)^(1/3)*a*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/b^3 + 1/2*

$$(-a*b^2)^{1/3}*a*\log(x^{2/3} + x^{1/3}*(-a/b)^{1/3} + (-a/b)^{2/3})/b^3 + 3/4*(b^3*x^{4/3} - 4*a*b^2*x^{1/3})/b^4$$

maple [A] time = 0.01, size = 121, normalized size = 0.98

$$\frac{3x^{\frac{4}{3}}}{4b} + \frac{\sqrt{3} a^2 \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{\left(\frac{a}{b}\right)^{\frac{2}{3}} b^3} + \frac{a^2 \ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{\left(\frac{a}{b}\right)^{\frac{2}{3}} b^3} - \frac{a^2 \ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2\left(\frac{a}{b}\right)^{\frac{2}{3}} b^3} - \frac{3a x^{\frac{1}{3}}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(4/3)/(b*x+a),x)

[Out] 3/4*x^(4/3)/b-3*a*x^(1/3)/b^2+a^2/b^3/(a/b)^(2/3)*ln(x^(1/3)+(a/b)^(1/3))-1/2*a^2/b^3/(a/b)^(2/3)*ln(x^(2/3)-(a/b)^(1/3)*x^(1/3)+(a/b)^(2/3))+a^2/b^3/(a/b)^(2/3)*3^(1/2)*arctan(1/3*3^(1/2)*(2/(a/b)^(1/3)*x^(1/3)-1))

maxima [A] time = 3.05, size = 128, normalized size = 1.04

$$\frac{\sqrt{3} a^2 \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{b^3\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{a^2 \log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2b^3\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{a^2 \log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{b^3\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{3\left(bx^{\frac{4}{3}} - 4ax^{\frac{1}{3}}\right)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)/(b*x+a),x, algorithm="maxima")

[Out] sqrt(3)*a^2*arctan(1/3*sqrt(3)*(2*x^(1/3) - (a/b)^(1/3))/(a/b)^(1/3))/(b^3*(a/b)^(2/3)) - 1/2*a^2*log(x^(2/3) - x^(1/3)*(a/b)^(1/3) + (a/b)^(2/3))/(b^3*(a/b)^(2/3)) + a^2*log(x^(1/3) + (a/b)^(1/3))/(b^3*(a/b)^(2/3)) + 3/4*(b*x^(4/3) - 4*a*x^(1/3))/b^2

mupad [B] time = 0.07, size = 126, normalized size = 1.02

$$\frac{3x^{4/3}}{4b} - \frac{3ax^{1/3}}{b^2} + \frac{a^{4/3} \ln\left(\frac{9a^{7/3}}{b^{1/3}} + 9a^2 x^{1/3}\right)}{b^{7/3}} + \frac{a^{4/3} \ln\left(9a^2 x^{1/3} + \frac{9a^{7/3}\left(-\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right)}{b^{1/3}}\right)}{b^{7/3}} \left(-\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right) - \frac{a^{4/3} \ln\left(9a^2 x^{1/3} - \frac{9a^{7/3}\left(-\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right)}{b^{1/3}}\right)}{b^{7/3}} \left(-\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(4/3)/(a + b*x), x)`

[Out] $(3*x^{(4/3)})/(4*b) - (3*a*x^{(1/3)})/b^2 + (a^{(4/3)}*\log((9*a^{(7/3)})/b^{(1/3)} + 9*a^2*x^{(1/3)}))/b^{(7/3)} + (a^{(4/3)}*\log(9*a^2*x^{(1/3)} + (9*a^{(7/3)}*((3^{(1/2)}*1i)/2 - 1/2)))/b^{(1/3)}*((3^{(1/2)}*1i)/2 - 1/2))/b^{(7/3)} - (a^{(4/3)}*\log(9*a^2*x^{(1/3)} - (9*a^{(7/3)}*((3^{(1/2)}*1i)/2 + 1/2)))/b^{(1/3)}*((3^{(1/2)}*1i)/2 + 1/2))/b^{(7/3)}$

sympy [A] time = 25.86, size = 240, normalized size = 1.95

$$\left\{ \begin{array}{l} \infty x^{\frac{4}{3}} \\ \frac{3x^{\frac{7}{3}}}{7a} \\ \frac{3x^{\frac{4}{3}}}{4b} \end{array} \right. - \frac{\sqrt[3]{-1} a^{\frac{4}{3}} \sqrt[3]{\frac{1}{b}} \log\left(-\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{\frac{1}{b}} + \sqrt[3]{x}\right)}{b^2} + \frac{\sqrt[3]{-1} a^{\frac{4}{3}} \sqrt[3]{\frac{1}{b}} \log\left(4(-1)^{\frac{2}{3}} a^{\frac{2}{3}} \left(\frac{1}{b}\right)^{\frac{2}{3}} + 4\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{x} \sqrt[3]{\frac{1}{b}} + 4x^{\frac{2}{3}}\right)}{2b^2} + \frac{\sqrt[3]{-1} \sqrt{3} a^{\frac{4}{3}} \sqrt[3]{\frac{1}{b}} \operatorname{atan}\left(\frac{\sqrt{3}}{3} - \frac{2(-1)^{\frac{2}{3}} \sqrt{3}}{3 \sqrt[3]{a} \sqrt[3]{\frac{1}{b}}}\right)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(4/3)/(b*x+a), x)`

[Out] `Piecewise((zoo*x**(4/3), Eq(a, 0) & Eq(b, 0)), (3*x**(7/3)/(7*a), Eq(b, 0)), (3*x**(4/3)/(4*b), Eq(a, 0)), ((-1)**(1/3)*a**(4/3)*(1/b)**(1/3)*log((-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/b**2 + (-1)**(1/3)*a**(4/3)*(1/b)**(1/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(2*b**2) + (-1)**(1/3)*sqrt(3)*a**(4/3)*(1/b)**(1/3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/b**2 - 3*a*x**(1/3)/b**2 + 3*x**(4/3)/(4*b), True))`

$$3.676 \quad \int \frac{x^{2/3}}{a+bx} dx$$

Optimal. Leaf size=111

$$\frac{3a^{2/3} \log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{2b^{5/3}} - \frac{a^{2/3} \log(a+bx)}{2b^{5/3}} + \frac{\sqrt{3} a^{2/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{b^{5/3}} + \frac{3x^{2/3}}{2b}$$

[Out] $3/2*x^{(2/3)}/b+3/2*a^{(2/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/b^{(5/3)}-1/2*a^{(2/3)}*1$
 $n(b*x+a)/b^{(5/3)}+a^{(2/3)}*arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{($
 $1/2))*3^{(1/2)}/b^{(5/3)}$

Rubi [A] time = 0.04, antiderivative size = 111, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {50, 56, 617, 204, 31}

$$\frac{3a^{2/3} \log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{2b^{5/3}} - \frac{a^{2/3} \log(a+bx)}{2b^{5/3}} + \frac{\sqrt{3} a^{2/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{b^{5/3}} + \frac{3x^{2/3}}{2b}$$

Antiderivative was successfully verified.

[In] Int[x^(2/3)/(a + b*x), x]

[Out] $(3*x^{(2/3)})/(2*b) + (\text{Sqrt}[3]*a^{(2/3)}*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/b^{(5/3)} + (3*a^{(2/3)}*\text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(2*$
 $b^{(5/3)}) - (a^{(2/3)}*\text{Log}[a + b*x])/(2*b^{(5/3)})$

Rule 31

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 50

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 56

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),

```
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]]) /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{x^{2/3}}{a+bx} dx &= \frac{3x^{2/3}}{2b} - \frac{a \int \frac{1}{\sqrt[3]{x}(a+bx)} dx}{b} \\ &= \frac{3x^{2/3}}{2b} - \frac{a^{2/3} \log(a+bx)}{2b^{5/3}} - \frac{(3a) \operatorname{Subst} \left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x} \right)}{2b^2} + \frac{(3a^{2/3}) \operatorname{Subst} \left(\int \frac{1}{\frac{\sqrt[3]{a}}{\sqrt[3]{b}} + x} dx, x, \sqrt[3]{x} \right)}{2b^{5/3}} \\ &= \frac{3x^{2/3}}{2b} + \frac{3a^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{5/3}} - \frac{a^{2/3} \log(a+bx)}{2b^{5/3}} - \frac{(3a^{2/3}) \operatorname{Subst} \left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt[3]{a}} \right)}{b^{5/3}} \\ &= \frac{3x^{2/3}}{2b} + \frac{\sqrt{3} a^{2/3} \tan^{-1} \left(\frac{1 - \frac{2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}} \right)}{b^{5/3}} + \frac{3a^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{5/3}} - \frac{a^{2/3} \log(a+bx)}{2b^{5/3}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 29, normalized size = 0.26

$$\frac{3x^{2/3} \left({}_2F_1 \left(\frac{2}{3}, 1; \frac{5}{3}; -\frac{bx}{a} \right) - 1 \right)}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[x^(2/3)/(a + b*x),x]

[Out] (-3*x^(2/3)*(-1 + Hypergeometric2F1[2/3, 1, 5/3, -((b*x)/a)]))/(2*b)

fricas [A] time = 0.45, size = 128, normalized size = 1.15

$$\frac{2\sqrt{3}\left(\frac{a^2}{b^2}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}bx^{\frac{1}{3}}\left(\frac{a^2}{b^2}\right)^{\frac{1}{3}} - \sqrt{3}a}{3a}\right) + \left(\frac{a^2}{b^2}\right)^{\frac{1}{3}} \log\left(-bx^{\frac{1}{3}}\left(\frac{a^2}{b^2}\right)^{\frac{2}{3}} + ax^{\frac{2}{3}} + a\left(\frac{a^2}{b^2}\right)^{\frac{1}{3}}\right) - 2\left(\frac{a^2}{b^2}\right)^{\frac{1}{3}} \log\left(b\left(\frac{a^2}{b^2}\right)^{\frac{2}{3}} + ax^{\frac{2}{3}}\right)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)/(b*x+a),x, algorithm="fricas")

[Out] -1/2*(2*sqrt(3)*(a^2/b^2)^(1/3)*arctan(1/3*(2*sqrt(3)*b*x^(1/3)*(a^2/b^2)^(1/3) - sqrt(3)*a)/a) + (a^2/b^2)^(1/3)*log(-b*x^(1/3)*(a^2/b^2)^(2/3) + a*x^(2/3) + a*(a^2/b^2)^(1/3)) - 2*(a^2/b^2)^(1/3)*log(b*(a^2/b^2)^(2/3) + a*x^(1/3)) - 3*x^(2/3))/b

giac [A] time = 1.04, size = 118, normalized size = 1.06

$$\frac{\left(-\frac{a}{b}\right)^{\frac{2}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{b} + \frac{3x^{\frac{2}{3}}}{2b} + \frac{\sqrt{3}(-ab^2)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{b^3} - \frac{(-ab^2)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)/(b*x+a),x, algorithm="giac")

[Out] (-a/b)^(2/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/b + 3/2*x^(2/3)/b + sqrt(3)*(-a*b^2)^(2/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/b^3 - 1/2*(-a*b^2)^(2/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/b^3

maple [A] time = 0.01, size = 107, normalized size = 0.96

$$-\frac{\sqrt{3} a \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{\left(\frac{a}{b}\right)^{\frac{1}{3}} b^2} + \frac{a \ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{\left(\frac{a}{b}\right)^{\frac{1}{3}} b^2} - \frac{a \ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2\left(\frac{a}{b}\right)^{\frac{1}{3}} b^2} + \frac{3x^{\frac{2}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(2/3)/(b*x+a),x)`

[Out] $\frac{3}{2}x^{2/3}/b + a/b^2/(a/b)^{1/3} \ln(x^{1/3} + (a/b)^{1/3}) - 1/2*a/b^2/(a/b)^{1/3} \ln(x^{2/3} - (a/b)^{1/3}*x^{1/3} + (a/b)^{2/3}) - a/b^2*3^{1/2}/(a/b)^{1/3} \arctan(1/3*3^{1/2}*(2/(a/b)^{1/3}*x^{1/3} - 1))$

maxima [A] time = 2.90, size = 114, normalized size = 1.03

$$-\frac{\sqrt{3} a \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{b^2\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{3x^{\frac{2}{3}}}{2b} - \frac{a \log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2b^2\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{a \log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{b^2\left(\frac{a}{b}\right)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(2/3)/(b*x+a),x, algorithm="maxima")`

[Out] $-\sqrt{3}*a*\arctan(1/3*\sqrt{3}*(2*x^{1/3} - (a/b)^{1/3})/(a/b)^{1/3})/(b^2*(a/b)^{1/3}) + 3/2*x^{2/3}/b - 1/2*a*\log(x^{2/3} - x^{1/3}*(a/b)^{1/3} + (a/b)^{2/3})/(b^2*(a/b)^{1/3}) + a*\log(x^{1/3} + (a/b)^{1/3})/(b^2*(a/b)^{1/3})$

mupad [B] time = 0.15, size = 130, normalized size = 1.17

$$\frac{3x^{2/3}}{2b} + \frac{a^{2/3} \ln\left(\frac{9a^{7/3}}{b^{4/3}} + \frac{9a^2x^{1/3}}{b}\right)}{b^{5/3}} + \frac{a^{2/3} \ln\left(\frac{9a^{7/3}\left(-\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right)^2}{b^{4/3}} + \frac{9a^2x^{1/3}}{b}\right)}{b^{5/3}} - \frac{a^{2/3} \ln\left(\frac{9a^{7/3}\left(\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right)^2}{b^{4/3}} + \frac{9a^2x^{1/3}}{b}\right)}{b^{5/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(2/3)/(a + b*x),x)`

[Out] $(3*x^{2/3})/(2*b) + (a^{2/3}*\log((9*a^{7/3})/b^{4/3} + (9*a^2*x^{1/3})/b))/b^{5/3} + (a^{2/3}*\log((9*a^{7/3})*((3^{1/2}*1i)/2 - 1/2)^2/b^{4/3} + (9*a^2*x^{1/3})/b)*((3^{1/2}*1i)/2 - 1/2))/b^{5/3} - (a^{2/3}*\log((9*a^{7/3})*((3^{1/2}*1i)/2 + 1/2)^2/b^{4/3} + (9*a^2*x^{1/3})/b)*((3^{1/2}*1i)/2 + 1/2))/b^{5/3}$

sympy [A] time = 9.08, size = 228, normalized size = 2.05

$$\left\{ \begin{array}{l} \infty x^{\frac{2}{3}} \\ \frac{3x^{\frac{5}{3}}}{5a} \\ \frac{3x^{\frac{2}{3}}}{2b} \end{array} \right. \frac{(-1)^{\frac{2}{3}} a^{\frac{2}{3}} \log\left(-\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{\frac{1}{b}} + \sqrt[3]{x}\right)}{b^2 \sqrt[3]{\frac{1}{b}}} - \frac{(-1)^{\frac{2}{3}} a^{\frac{2}{3}} \log\left(4(-1)^{\frac{2}{3}} a^{\frac{2}{3}} \left(\frac{1}{b}\right)^{\frac{2}{3}} + 4\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{x} \sqrt[3]{\frac{1}{b}} + 4x^{\frac{2}{3}}\right)}{2b^2 \sqrt[3]{\frac{1}{b}}} + \frac{(-1)^{\frac{2}{3}} \sqrt{3} a^{\frac{2}{3}} \operatorname{atan}\left(\frac{\sqrt{3}}{3} - \frac{2(-1)^{\frac{2}{3}} \sqrt{3} \sqrt[3]{x}}{3 \sqrt[3]{a} \sqrt[3]{\frac{1}{b}}}\right)}{b^2 \sqrt[3]{\frac{1}{b}}} + \frac{3x^{\frac{2}{3}}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(2/3)/(b*x+a), x)

[Out] Piecewise((zoo*x**(2/3), Eq(a, 0) & Eq(b, 0)), (3*x**(5/3)/(5*a), Eq(b, 0)), (3*x**(2/3)/(2*b), Eq(a, 0)), ((-1)**(2/3)*a**(2/3)*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(b**2*(1/b)**(1/3)) - (-1)**(2/3)*a**(2/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(2*b**2*(1/b)**(1/3)) + (-1)**(2/3)*sqrt(3)*a**(2/3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(b**2*(1/b)**(1/3)) + 3*x**(2/3)/(2*b), True))

$$3.677 \quad \int \frac{\sqrt[3]{x}}{a+bx} dx$$

Optimal. Leaf size=109

$$-\frac{3\sqrt[3]{a} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{4/3}} + \frac{\sqrt[3]{a} \log(a+bx)}{2b^{4/3}} + \frac{\sqrt{3} \sqrt[3]{a} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt{3} \sqrt[3]{a}}\right)}{b^{4/3}} + \frac{3\sqrt[3]{x}}{b}$$

[Out] $3x^{(1/3)}/b-3/2*a^{(1/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/b^{(4/3)}+1/2*a^{(1/3)}*\ln(b*x+a)/b^{(4/3)}+a^{(1/3)}*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})*3^{(1/2)}/b^{(4/3)}$

Rubi [A] time = 0.04, antiderivative size = 109, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {50, 58, 617, 204, 31}

$$-\frac{3\sqrt[3]{a} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{4/3}} + \frac{\sqrt[3]{a} \log(a+bx)}{2b^{4/3}} + \frac{\sqrt{3} \sqrt[3]{a} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt{3} \sqrt[3]{a}}\right)}{b^{4/3}} + \frac{3\sqrt[3]{x}}{b}$$

Antiderivative was successfully verified.

[In] Int[x^(1/3)/(a + b*x), x]

[Out] $(3*x^{(1/3)})/b + (\text{Sqrt}[3]*a^{(1/3)}*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/b^{(4/3)} - (3*a^{(1/3)}*\text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(2*b^{(4/3)}) + (a^{(1/3)}*\text{Log}[a + b*x])/(2*b^{(4/3)})$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 50

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 58

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^

2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]) /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt[3]{x}}{a+bx} dx &= \frac{3\sqrt[3]{x}}{b} - \frac{a \int \frac{1}{x^{2/3}(a+bx)} dx}{b} \\ &= \frac{3\sqrt[3]{x}}{b} + \frac{\sqrt[3]{a} \log(a+bx)}{2b^{4/3}} - \frac{(3a^{2/3}) \text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{2b^{5/3}} - \frac{(3\sqrt[3]{a}) \text{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{a}}{\sqrt[3]{b}} + x} dx, x, \sqrt[3]{x}\right)}{2b^{4/3}} \\ &= \frac{3\sqrt[3]{x}}{b} - \frac{3\sqrt[3]{a} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{4/3}} + \frac{\sqrt[3]{a} \log(a+bx)}{2b^{4/3}} - \frac{(3\sqrt[3]{a}) \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt[3]{a}}\right)}{b^{4/3}} \\ &= \frac{3\sqrt[3]{x}}{b} + \frac{\sqrt{3} \sqrt[3]{a} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{b^{4/3}} - \frac{3\sqrt[3]{a} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{4/3}} + \frac{\sqrt[3]{a} \log(a+bx)}{2b^{4/3}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 126, normalized size = 1.16

$$\frac{\sqrt[3]{a} \log(a^{2/3} - \sqrt[3]{a} \sqrt[3]{b} \sqrt[3]{x} + b^{2/3} x^{2/3}) - 2\sqrt[3]{a} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}) + 2\sqrt{3} \sqrt[3]{a} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right) + 6\sqrt[3]{b} \sqrt[3]{x}}{2b^{4/3}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(1/3)/(a + b*x), x]

[Out] (6*b^(1/3)*x^(1/3) + 2*Sqrt[3]*a^(1/3)*ArcTan[(1 - (2*b^(1/3)*x^(1/3))/a^(1/3))/Sqrt[3]] - 2*a^(1/3)*Log[a^(1/3) + b^(1/3)*x^(1/3)] + a^(1/3)*Log[a^(2/3) - a^(1/3)*b^(1/3)*x^(1/3) + b^(2/3)*x^(2/3)])/(2*b^(4/3))

fricas [A] time = 0.49, size = 114, normalized size = 1.05

$$\frac{2\sqrt{3}\left(-\frac{a}{b}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}bx^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{2}{3}} - \sqrt{3}a}{3a}\right) - \left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right) + 2\left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right) + 6x^{\frac{1}{3}}}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)/(b*x+a), x, algorithm="fricas")

[Out] 1/2*(2*sqrt(3)*(-a/b)^(1/3)*arctan(1/3*(2*sqrt(3)*b*x^(1/3)*(-a/b)^(2/3) - sqrt(3)*a)/a) - (-a/b)^(1/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3)) + 2*(-a/b)^(1/3)*log(x^(1/3) - (-a/b)^(1/3)) + 6*x^(1/3)/b

giac [A] time = 1.15, size = 119, normalized size = 1.09

$$\frac{\left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{b} - \frac{\sqrt{3}\left(-ab^2\right)^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{b^2} + \frac{3x^{\frac{1}{3}}}{b} - \frac{\left(-ab^2\right)^{\frac{1}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)/(b*x+a), x, algorithm="giac")

[Out] (-a/b)^(1/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/b - sqrt(3)*(-a*b^2)^(1/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/b^2 + 3*x^(1/3)/b - 1/2*(-a*b^2)^(1/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/b^2

maple [A] time = 0.01, size = 108, normalized size = 0.99

$$-\frac{\sqrt{3} a \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{\left(\frac{a}{b}\right)^{\frac{2}{3}} b^2} - \frac{a \ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{\left(\frac{a}{b}\right)^{\frac{2}{3}} b^2} + \frac{a \ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2\left(\frac{a}{b}\right)^{\frac{2}{3}} b^2} + \frac{3x^{\frac{1}{3}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/3)/(b*x+a),x)

[Out] 3*x^(1/3)/b-a/b^2/(a/b)^(2/3)*ln(x^(1/3)+(a/b)^(1/3))+1/2*a/b^2/(a/b)^(2/3)*ln(x^(2/3)-(a/b)^(1/3)*x^(1/3)+(a/b)^(2/3))-a/b^2/(a/b)^(2/3)*3^(1/2)*arctan(1/3*3^(1/2)*(2/(a/b)^(1/3)*x^(1/3)-1))

maxima [A] time = 2.93, size = 115, normalized size = 1.06

$$-\frac{\sqrt{3} a \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{b^2\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{3x^{\frac{1}{3}}}{b} + \frac{a \log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2b^2\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{a \log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{b^2\left(\frac{a}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)/(b*x+a),x, algorithm="maxima")

[Out] -sqrt(3)*a*arctan(1/3*sqrt(3)*(2*x^(1/3) - (a/b)^(1/3))/(a/b)^(1/3))/(b^2*(a/b)^(2/3)) + 3*x^(1/3)/b + 1/2*a*log(x^(2/3) - x^(1/3)*(a/b)^(1/3) + (a/b)^(2/3))/(b^2*(a/b)^(2/3)) - a*log(x^(1/3) + (a/b)^(1/3))/(b^2*(a/b)^(2/3))

mupad [B] time = 0.07, size = 126, normalized size = 1.16

$$\frac{3x^{1/3}}{b} + \frac{(-a)^{1/3} \ln\left(9(-a)^{4/3} b^{2/3} + 9abx^{1/3}\right)}{b^{4/3}} + \frac{(-a)^{1/3} \ln\left(9(-a)^{4/3} b^{2/3} \left(-\frac{1}{2} + \frac{\sqrt{3} 1i}{2}\right) + 9abx^{1/3}\right) \left(-\frac{1}{2} + \frac{\sqrt{3} 1i}{2}\right)}{b^{4/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/3)/(a + b*x),x)

```
[Out] (3*x^(1/3))/b + ((-a)^(1/3)*log(9*(-a)^(4/3)*b^(2/3) + 9*a*b*x^(1/3)))/b^(4/3) + ((-a)^(1/3)*log(9*(-a)^(4/3)*b^(2/3)*((3^(1/2)*1i)/2 - 1/2) + 9*a*b*x^(1/3))*((3^(1/2)*1i)/2 - 1/2))/b^(4/3) - ((-a)^(1/3)*log(9*(-a)^(4/3)*b^(2/3)*((3^(1/2)*1i)/2 + 1/2) - 9*a*b*x^(1/3))*((3^(1/2)*1i)/2 + 1/2))/b^(4/3)
```

sympy [A] time = 6.10, size = 219, normalized size = 2.01

$$\left\{ \begin{array}{l} \infty \sqrt[3]{x} \\ \frac{3x^{\frac{4}{3}}}{4a} \\ \frac{3\sqrt[3]{x}}{b} \\ \frac{\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{\frac{1}{b}} \log\left(-\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{\frac{1}{b}} + \sqrt[3]{x}\right)}{b} - \frac{\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{\frac{1}{b}} \log\left(4(-1)^{\frac{2}{3}} a^{\frac{2}{3}} \left(\frac{1}{b}\right)^{\frac{2}{3}} + 4\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{x} \sqrt[3]{\frac{1}{b}} + 4x^{\frac{2}{3}}\right)}{2b} - \frac{\sqrt[3]{-1} \sqrt{3} \sqrt[3]{a} \sqrt[3]{\frac{1}{b}} \operatorname{atan}\left(\frac{\sqrt{3}}{3} - \frac{2(-1)^{\frac{2}{3}} \sqrt{3}}{3 \sqrt[3]{a} \sqrt[3]{\frac{1}{b}}}\right)}{b} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(1/3)/(b*x+a), x)
```

```
[Out] Piecewise((zoo*x**(1/3), Eq(a, 0) & Eq(b, 0)), (3*x**(4/3)/(4*a), Eq(b, 0)), (3*x**(1/3)/b, Eq(a, 0)), ((-1)**(1/3)*a**(1/3)*(1/b)**(1/3)*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/b - (-1)**(1/3)*a**(1/3)*(1/b)**(1/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(2*b) - (-1)**(1/3)*sqrt(3)*a**(1/3)*(1/b)**(1/3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/b + 3*x**(1/3)/b, True))
```

$$3.678 \quad \int \frac{1}{\sqrt[3]{x}(a+bx)} dx$$

Optimal. Leaf size=100

$$-\frac{3 \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2\sqrt[3]{a} b^{2/3}} + \frac{\log(a+bx)}{2\sqrt[3]{a} b^{2/3}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt[3]{a} b^{2/3}}$$

[Out] $-3/2*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(1/3)}/b^{(2/3)}+1/2*\ln(b*x+a)/a^{(1/3)}/b^{(2/3)}-\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})*3^{(1/2)}/a^{(1/3)}/b^{(2/3)}$

Rubi [A] time = 0.03, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {56, 617, 204, 31}

$$-\frac{3 \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2\sqrt[3]{a} b^{2/3}} + \frac{\log(a+bx)}{2\sqrt[3]{a} b^{2/3}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt[3]{a} b^{2/3}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(1/3)*(a + b*x)),x]

[Out] $-((\text{Sqrt}[3]*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/(a^{(1/3)}*b^{(2/3)})) - (3*\text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(2*a^{(1/3)}*b^{(2/3)}) + \text{Log}[a + b*x]/(2*a^{(1/3)}*b^{(2/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 56

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]], x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])] /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_.)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[

a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt[3]{x}(a+bx)} dx &= \frac{\log(a+bx)}{2\sqrt[3]{a}b^{2/3}} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{2b} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{a}}{\sqrt[3]{b}} + x} dx, x, \sqrt[3]{x}\right)}{2\sqrt[3]{a}b^{2/3}} \\ &= -\frac{3 \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2\sqrt[3]{a}b^{2/3}} + \frac{\log(a+bx)}{2\sqrt[3]{a}b^{2/3}} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}\right)}{\sqrt[3]{a}b^{2/3}} \\ &= -\frac{\sqrt{3} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt[3]{a}b^{2/3}} - \frac{3 \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2\sqrt[3]{a}b^{2/3}} + \frac{\log(a+bx)}{2\sqrt[3]{a}b^{2/3}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 27, normalized size = 0.27

$$\frac{3x^{2/3} {}_2F_1\left(\frac{2}{3}, 1; \frac{5}{3}; -\frac{bx}{a}\right)}{2a}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(1/3)*(a + b*x)),x]

[Out] (3*x^(2/3)*Hypergeometric2F1[2/3, 1, 5/3, -(b*x)/a])/(2*a)

fricas [A] time = 0.48, size = 313, normalized size = 3.13

$$\frac{\sqrt{3} ab \sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} \log \left(\frac{2b^2x - ab + \sqrt{3} \left(abx^{\frac{1}{3}} + (-ab^2)^{\frac{1}{3}} a + 2(-ab^2)^{\frac{2}{3}} x^{\frac{2}{3}} \right) \sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} - 3(-ab^2)^{\frac{2}{3}} x^{\frac{1}{3}}}{bx+a} \right) + (-ab^2)^{\frac{2}{3}} \log \left(b^2x^{\frac{2}{3}} + (-ab^2)^{\frac{1}{3}} \right)}{2ab^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3)/(b*x+a),x, algorithm="fricas")

[Out] [1/2*(sqrt(3)*a*b*sqrt((-a*b^2)^(1/3)/a)*log((2*b^2*x - a*b + sqrt(3)*(a*b*x^(1/3) + (-a*b^2)^(1/3)*a + 2*(-a*b^2)^(2/3)*x^(2/3))*sqrt((-a*b^2)^(1/3)/a) - 3*(-a*b^2)^(2/3)*x^(1/3))/(b*x + a)) + (-a*b^2)^(2/3)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) - 2*(-a*b^2)^(2/3)*log(b*x^(1/3) - (-a*b^2)^(1/3)))/(a*b^2), 1/2*(2*sqrt(3)*a*b*sqrt(-(-a*b^2)^(1/3)/a)*arctan(1/3*sqrt(3)*(2*b*x^(1/3) + (-a*b^2)^(1/3))*sqrt(-(-a*b^2)^(1/3)/a)/b) + (-a*b^2)^(2/3)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) - 2*(-a*b^2)^(2/3)*log(b*x^(1/3) - (-a*b^2)^(1/3)))/(a*b^2)]

giac [A] time = 1.17, size = 118, normalized size = 1.18

$$\frac{\left(-\frac{a}{b}\right)^{\frac{2}{3}} \log \left(\left| x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}} \right| \right)}{a} - \frac{\sqrt{3} (-ab^2)^{\frac{2}{3}} \arctan \left(\frac{\sqrt{3} \left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}} \right)}{3 \left(-\frac{a}{b}\right)^{\frac{1}{3}}} \right)}{ab^2} + \frac{(-ab^2)^{\frac{2}{3}} \log \left(x^{\frac{2}{3}} + x^{\frac{1}{3}} \left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}} \right)}{2ab^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3)/(b*x+a),x, algorithm="giac")

[Out] -(-a/b)^(2/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/a - sqrt(3)*(-a*b^2)^(2/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/(a*b^2) + 1/2*(-a*b^2)^(2/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/(a*b^2)

maple [A] time = 0.00, size = 96, normalized size = 0.96

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{\left(\frac{a}{b}\right)^{\frac{1}{3}} b} - \frac{\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{\left(\frac{a}{b}\right)^{\frac{1}{3}} b} + \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2\left(\frac{a}{b}\right)^{\frac{1}{3}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/3)/(b*x+a),x)

[Out] -1/b/(a/b)^(1/3)*ln(x^(1/3)+(a/b)^(1/3))+1/2/b/(a/b)^(1/3)*ln(x^(2/3)-(a/b)^(1/3)*x^(1/3)+(a/b)^(2/3))+3^(1/2)/b/(a/b)^(1/3)*arctan(1/3*3^(1/2)*(2/(a/b)^(1/3)*x^(1/3)-1))

maxima [A] time = 2.83, size = 103, normalized size = 1.03

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{b\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2b\left(\frac{a}{b}\right)^{\frac{1}{3}}} - \frac{\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{b\left(\frac{a}{b}\right)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3)/(b*x+a),x, algorithm="maxima")

[Out] sqrt(3)*arctan(1/3*sqrt(3)*(2*x^(1/3) - (a/b)^(1/3))/(a/b)^(1/3))/(b*(a/b)^(1/3)) + 1/2*log(x^(2/3) - x^(1/3)*(a/b)^(1/3) + (a/b)^(2/3))/(b*(a/b)^(1/3)) - log(x^(1/3) + (a/b)^(1/3))/(b*(a/b)^(1/3))

mupad [B] time = 0.11, size = 120, normalized size = 1.20

$$\frac{\ln\left(9bx^{1/3} - 9(-a)^{1/3}b^{2/3}\right)}{(-a)^{1/3}b^{2/3}} + \frac{\ln\left(9bx^{1/3} - \frac{9(-a)^{1/3}b^{2/3}(-1+\sqrt{3}1i)^2}{4}\right)(-1+\sqrt{3}1i)}{2(-a)^{1/3}b^{2/3}} - \frac{\ln\left(9bx^{1/3} - \frac{9(-a)^{1/3}b^{2/3}(1+\sqrt{3}1i)^2}{4}\right)}{2(-a)^{1/3}b^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/3)*(a + b*x)),x)

[Out] $\log(9*b*x^{(1/3)} - 9*(-a)^{(1/3)}*b^{(2/3)})/((-a)^{(1/3)}*b^{(2/3)}) + (\log(9*b*x^{(1/3)} - 9*(-a)^{(1/3)}*b^{(2/3)}*(3^{(1/2)}*1i - 1)^2/4)*(3^{(1/2)}*1i - 1))/(2*(-a)^{(1/3)}*b^{(2/3)}) - (\log(9*b*x^{(1/3)} - 9*(-a)^{(1/3)}*b^{(2/3)}*(3^{(1/2)}*1i + 1)^2/4)*(3^{(1/2)}*1i + 1))/(2*(-a)^{(1/3)}*b^{(2/3)})$

sympy [A] time = 7.41, size = 212, normalized size = 2.12

$$\left\{ \begin{array}{l} \frac{\infty}{\sqrt[3]{x}} \\ \frac{3x^{\frac{2}{3}}}{2a} \\ \frac{3}{b\sqrt[3]{x}} \end{array} \right. \quad \begin{array}{l} \text{for } a = \\ \text{for } b = \\ \text{for } a = \end{array}$$

$$-\frac{(-1)^{\frac{2}{3}} \log\left(-\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{\frac{1}{b}} + \sqrt[3]{x}\right)}{\sqrt[3]{a} b \sqrt[3]{\frac{1}{b}}} + \frac{(-1)^{\frac{2}{3}} \log\left(4(-1)^{\frac{2}{3}} a^{\frac{2}{3}} \left(\frac{1}{b}\right)^{\frac{2}{3}} + 4\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{x} \sqrt[3]{\frac{1}{b}} + 4x^{\frac{2}{3}}\right)}{2\sqrt[3]{a} b \sqrt[3]{\frac{1}{b}}} - \frac{(-1)^{\frac{2}{3}} \sqrt{3} \operatorname{atan}\left(\frac{\sqrt{3} - 2(-1)^{\frac{2}{3}} \sqrt{3} \sqrt[3]{x}}{3 \sqrt[3]{a} \sqrt[3]{\frac{1}{b}}}\right)}{\sqrt[3]{a} b \sqrt[3]{\frac{1}{b}}} \quad \begin{array}{l} \text{otherw} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(1/3)/(b*x+a), x)`

[Out] `Piecewise((zoo/x**(1/3), Eq(a, 0) & Eq(b, 0)), (3*x**(2/3)/(2*a), Eq(b, 0)), (-3/(b*x**(1/3)), Eq(a, 0)), ((-1)**(2/3)*log((-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(a**(1/3)*b*(1/b)**(1/3)) + (-1)**(2/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(2*a**(1/3)*b*(1/b)**(1/3)) - (-1)**(2/3)*sqrt(3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(a**(1/3)*b*(1/b)**(1/3)), True))`

$$3.679 \quad \int \frac{1}{x^{2/3}(a+bx)} dx$$

Optimal. Leaf size=100

$$\frac{3 \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{2/3} \sqrt[3]{b}} - \frac{\log(a+bx)}{2a^{2/3} \sqrt[3]{b}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{a^{2/3} \sqrt[3]{b}}$$

[Out] $3/2*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(2/3)}/b^{(1/3)}-1/2*\ln(b*x+a)/a^{(2/3)}/b^{(1/3)}-\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})*3^{(1/2)}/a^{(2/3)}/b^{(1/3)}$

Rubi [A] time = 0.03, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {58, 617, 204, 31}

$$\frac{3 \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{2/3} \sqrt[3]{b}} - \frac{\log(a+bx)}{2a^{2/3} \sqrt[3]{b}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{a^{2/3} \sqrt[3]{b}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(2/3)*(a + b*x)), x]

[Out] $-((\text{Sqrt}[3]*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/(a^{(2/3)}*b^{(1/3)})) + (3*\text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(2*a^{(2/3)}*b^{(1/3)}) - \text{Log}[a + b*x]/(2*a^{(2/3)}*b^{(1/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 58

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^(2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]]) /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_.)*(x_)^2)^(n_), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[

a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{x^{2/3}(a+bx)} dx &= -\frac{\log(a+bx)}{2a^{2/3}\sqrt[3]{b}} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{2\sqrt[3]{a}b^{2/3}} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{a}}{\sqrt[3]{b}} + x} dx, x, \sqrt[3]{x}\right)}{2a^{2/3}\sqrt[3]{b}} \\ &= \frac{3 \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{2a^{2/3}\sqrt[3]{b}} - \frac{\log(a+bx)}{2a^{2/3}\sqrt[3]{b}} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}\right)}{a^{2/3}\sqrt[3]{b}} \\ &= -\frac{\sqrt{3} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{a^{2/3}\sqrt[3]{b}} + \frac{3 \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{2a^{2/3}\sqrt[3]{b}} - \frac{\log(a+bx)}{2a^{2/3}\sqrt[3]{b}} \end{aligned}$$

Mathematica [A] time = 0.02, size = 103, normalized size = 1.03

$$\frac{\log(a^{2/3} - \sqrt[3]{a}\sqrt[3]{b}\sqrt[3]{x} + b^{2/3}x^{2/3}) - 2\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x}) + 2\sqrt{3} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{2a^{2/3}\sqrt[3]{b}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(2/3)*(a + b*x)), x]

[Out] -1/2*(2*Sqrt[3]*ArcTan[(1 - (2*b^(1/3)*x^(1/3))/a^(1/3))/Sqrt[3]] - 2*Log[a^(1/3) + b^(1/3)*x^(1/3)] + Log[a^(2/3) - a^(1/3)*b^(1/3)*x^(1/3) + b^(2/3)*x^(2/3)])/(a^(2/3)*b^(1/3))

fricas [A] time = 0.51, size = 307, normalized size = 3.07

$$\frac{\sqrt{3} ab \sqrt{-\frac{(a^2 b)^{\frac{1}{3}}}{b}} \log \left(\frac{2 abx - a^2 + \sqrt{3} \left(2 abx^{\frac{2}{3}} - (a^2 b)^{\frac{1}{3}} a + (a^2 b)^{\frac{2}{3}} x^{\frac{1}{3}} \right) \sqrt{-\frac{(a^2 b)^{\frac{1}{3}}}{b}} - 3 (a^2 b)^{\frac{1}{3}} a x^{\frac{1}{3}}}{bx+a} \right) - (a^2 b)^{\frac{2}{3}} \log \left(abx^{\frac{2}{3}} + (a^2 b)^{\frac{1}{3}} a - (a^2 b)^{\frac{2}{3}} \right)}{2 a^2 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3)/(b*x+a),x, algorithm="fricas")

[Out] [1/2*(sqrt(3)*a*b*sqrt(-(a^2*b)^(1/3)/b)*log((2*a*b*x - a^2 + sqrt(3)*(2*a*b*x^(2/3) - (a^2*b)^(1/3)*a + (a^2*b)^(2/3)*x^(1/3))*sqrt(-(a^2*b)^(1/3)/b - 3*(a^2*b)^(1/3)*a*x^(1/3))/(b*x + a)) - (a^2*b)^(2/3)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) + 2*(a^2*b)^(2/3)*log(a*b*x^(1/3) + (a^2*b)^(2/3)))/(a^2*b), 1/2*(2*sqrt(3)*a*b*sqrt((a^2*b)^(1/3)/b)*arctan(-1/3*sqrt(3)*((a^2*b)^(1/3)*a - 2*(a^2*b)^(2/3)*x^(1/3))*sqrt((a^2*b)^(1/3)/b)/a^2) - (a^2*b)^(2/3)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) + 2*(a^2*b)^(2/3)*log(a*b*x^(1/3) + (a^2*b)^(2/3)))/(a^2*b)]

giac [A] time = 1.18, size = 117, normalized size = 1.17

$$-\frac{\left(-\frac{a}{b}\right)^{\frac{1}{3}} \log \left(\left| x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}} \right| \right)}{a} + \frac{\sqrt{3} \left(-ab^2\right)^{\frac{1}{3}} \arctan \left(\frac{\sqrt{3} \left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}} \right)}{3 \left(-\frac{a}{b}\right)^{\frac{1}{3}}} \right)}{ab} + \frac{\left(-ab^2\right)^{\frac{1}{3}} \log \left(x^{\frac{2}{3}} + x^{\frac{1}{3}} \left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}} \right)}{2 ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3)/(b*x+a),x, algorithm="giac")

[Out] -(-a/b)^(1/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/a + sqrt(3)*(-a*b^2)^(1/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/(a*b) + 1/2*(-a*b^2)^(1/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/(a*b)

maple [A] time = 0.01, size = 95, normalized size = 0.95

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3} \left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{\left(\frac{a}{b}\right)^{\frac{2}{3}} b} + \frac{\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{\left(\frac{a}{b}\right)^{\frac{2}{3}} b} - \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2 \left(\frac{a}{b}\right)^{\frac{2}{3}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(2/3)/(b*x+a),x)

[Out] 1/b/(a/b)^(2/3)*ln(x^(1/3)+(a/b)^(1/3))-1/2/b/(a/b)^(2/3)*ln(x^(2/3)-(a/b)^(1/3)*x^(1/3)+(a/b)^(2/3))+1/b/(a/b)^(2/3)*3^(1/2)*arctan(1/3*3^(1/2)*(2/(a/b)^(1/3)*x^(1/3)-1))

maxima [A] time = 2.96, size = 102, normalized size = 1.02

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3} \left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3 \left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{b \left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}} \left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2 b \left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{b \left(\frac{a}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3)/(b*x+a),x, algorithm="maxima")

[Out] sqrt(3)*arctan(1/3*sqrt(3)*(2*x^(1/3) - (a/b)^(1/3))/(a/b)^(1/3))/(b*(a/b)^(2/3)) - 1/2*log(x^(2/3) - x^(1/3)*(a/b)^(1/3) + (a/b)^(2/3))/(b*(a/b)^(2/3)) + log(x^(1/3) + (a/b)^(1/3))/(b*(a/b)^(2/3))

mupad [B] time = 0.21, size = 110, normalized size = 1.10

$$\frac{\ln\left(9 a^{1/3} b^{5/3} + 9 b^2 x^{1/3}\right)}{a^{2/3} b^{1/3}} + \frac{\ln\left(9 b^2 x^{1/3} + \frac{9 a^{1/3} b^{5/3} (-1 + \sqrt{3} 1i)}{2}\right) (-1 + \sqrt{3} 1i)}{2 a^{2/3} b^{1/3}} - \frac{\ln\left(9 b^2 x^{1/3} - \frac{9 a^{1/3} b^{5/3} (1 + \sqrt{3} 1i)}{2}\right) (1 + \sqrt{3} 1i)}{2 a^{2/3} b^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(2/3)*(a + b*x)),x)

[Out] $\log(9a^{1/3}b^{5/3} + 9b^2x^{1/3})/(a^{2/3}b^{1/3}) + (\log(9b^2x^{1/3} + 9a^{1/3}b^{5/3}*(3^{1/2}*1i - 1))/2*(3^{1/2}*1i - 1))/(2a^{2/3}b^{1/3}) - (\log(9b^2x^{1/3} - 9a^{1/3}b^{5/3}*(3^{1/2}*1i + 1))/2*(3^{1/2}*1i + 1))/(2a^{2/3}b^{1/3})$

sympy [A] time = 11.35, size = 212, normalized size = 2.12

$$\left\{ \begin{array}{ll} \frac{\infty}{x^3} & \text{for } a = 0 \\ \frac{3\sqrt[3]{x}}{a} & \text{for } b = 0 \\ -\frac{3}{2bx^{\frac{2}{3}}} & \text{for } a = 0 \\ \frac{\sqrt[3]{-1} \log\left(-\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{\frac{1}{b}} + \sqrt[3]{x}\right)}{a^{\frac{2}{3}}b\left(\frac{1}{b}\right)^{\frac{2}{3}}} + \frac{\sqrt[3]{-1} \log\left(4(-1)^{\frac{2}{3}}a^{\frac{2}{3}}\left(\frac{1}{b}\right)^{\frac{2}{3}} + 4\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{x} \sqrt[3]{\frac{1}{b}} + 4x^{\frac{2}{3}}\right)}{2a^{\frac{2}{3}}b\left(\frac{1}{b}\right)^{\frac{2}{3}}} + \frac{\sqrt[3]{-1} \sqrt{3} \operatorname{atan}\left(\frac{\sqrt{3}}{3} - \frac{2(-1)^{\frac{2}{3}} \sqrt{3} \sqrt[3]{x}}{3\sqrt[3]{a} \sqrt[3]{\frac{1}{b}}}\right)}{a^{\frac{2}{3}}b\left(\frac{1}{b}\right)^{\frac{2}{3}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(2/3)/(b*x+a), x)`

[Out] `Piecewise((zoo/x**(2/3), Eq(a, 0) & Eq(b, 0)), (3*x**(1/3)/a, Eq(b, 0)), (-3/(2*b*x**(2/3)), Eq(a, 0)), ((-1)**(1/3)*log((-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(a**(2/3)*b*(1/b)**(2/3)) + (-1)**(1/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(2*a**(2/3)*b*(1/b)**(2/3)) + (-1)**(1/3)*sqrt(3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(a**(2/3)*b*(1/b)**(2/3)), True))`

$$3.680 \quad \int \frac{1}{x^{4/3}(a+bx)} dx$$

Optimal. Leaf size=109

$$\frac{3\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{4/3}} - \frac{\sqrt[3]{b} \log(a+bx)}{2a^{4/3}} + \frac{\sqrt{3} \sqrt[3]{b} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt{3} \sqrt[3]{a}}\right)}{a^{4/3}} - \frac{3}{a\sqrt[3]{x}}$$

[Out] $-3/a/x^{(1/3)}+3/2*b^{(1/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(4/3)}-1/2*b^{(1/3)}*\ln(b*x+a)/a^{(4/3)}+b^{(1/3)}*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})*3^{(1/2)}/a^{(4/3)}$

Rubi [A] time = 0.04, antiderivative size = 109, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 56, 617, 204, 31}

$$\frac{3\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{4/3}} - \frac{\sqrt[3]{b} \log(a+bx)}{2a^{4/3}} + \frac{\sqrt{3} \sqrt[3]{b} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt{3} \sqrt[3]{a}}\right)}{a^{4/3}} - \frac{3}{a\sqrt[3]{x}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(4/3)*(a + b*x)), x]

[Out] $-3/(a*x^{(1/3)}) + (\text{Sqrt}[3]*b^{(1/3)}*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/a^{(4/3)} + (3*b^{(1/3)}*\text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(2*a^{(4/3)}) - (b^{(1/3)}*\text{Log}[a + b*x])/(2*a^{(4/3)})$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])] /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{x^{4/3}(a+bx)} dx &= -\frac{3}{a\sqrt[3]{x}} - \frac{b \int \frac{1}{\sqrt[3]{x}(a+bx)} dx}{a} \\ &= -\frac{3}{a\sqrt[3]{x}} - \frac{\sqrt[3]{b} \log(a+bx)}{2a^{4/3}} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{2a} + \frac{(3\sqrt[3]{b}) \operatorname{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{a}}{\sqrt[3]{b}} + x} dx, x, \sqrt[3]{x}\right)}{2a^{4/3}} \\ &= -\frac{3}{a\sqrt[3]{x}} + \frac{3\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{4/3}} - \frac{\sqrt[3]{b} \log(a+bx)}{2a^{4/3}} - \frac{(3\sqrt[3]{b}) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b}}{\sqrt[3]{a}}\right)}{a^{4/3}} \\ &= -\frac{3}{a\sqrt[3]{x}} + \frac{\sqrt{3} \sqrt[3]{b} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{a^{4/3}} + \frac{3\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{4/3}} - \frac{\sqrt[3]{b} \log(a+bx)}{2a^{4/3}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 25, normalized size = 0.23

$$-\frac{{}_3F_1\left(-\frac{1}{3}, 1; \frac{2}{3}; -\frac{bx}{a}\right)}{a\sqrt[3]{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(4/3)*(a + b*x)),x]

[Out] (-3*Hypergeometric2F1[-1/3, 1, 2/3, -((b*x)/a)])/(a*x^(1/3))

fricas [A] time = 0.47, size = 113, normalized size = 1.04

$$\frac{2\sqrt{3}x\left(\frac{b}{a}\right)^{\frac{1}{3}} \arctan\left(\frac{2}{3}\sqrt{3}x^{\frac{1}{3}}\left(\frac{b}{a}\right)^{\frac{1}{3}} - \frac{1}{3}\sqrt{3}\right) + x\left(\frac{b}{a}\right)^{\frac{1}{3}} \log\left(-ax^{\frac{1}{3}}\left(\frac{b}{a}\right)^{\frac{2}{3}} + bx^{\frac{2}{3}} + a\left(\frac{b}{a}\right)^{\frac{1}{3}}\right) - 2x\left(\frac{b}{a}\right)^{\frac{1}{3}} \log\left(a\left(\frac{b}{a}\right)^{\frac{2}{3}} + \dots\right)}{2ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3)/(b*x+a),x, algorithm="fricas")

[Out] -1/2*(2*sqrt(3)*x*(b/a)^(1/3)*arctan(2/3*sqrt(3)*x^(1/3)*(b/a)^(1/3) - 1/3*sqrt(3)) + x*(b/a)^(1/3)*log(-a*x^(1/3)*(b/a)^(2/3) + b*x^(2/3) + a*(b/a)^(1/3)) - 2*x*(b/a)^(1/3)*log(a*(b/a)^(2/3) + b*x^(1/3)) + 6*x^(2/3))/(a*x)

giac [A] time = 1.21, size = 125, normalized size = 1.15

$$\frac{b\left(-\frac{a}{b}\right)^{\frac{2}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{a^2} + \frac{\sqrt{3}\left(-ab^2\right)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{a^2b} - \frac{3}{ax^{\frac{1}{3}}} - \frac{\left(-ab^2\right)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2a^2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3)/(b*x+a),x, algorithm="giac")

[Out] b*(-a/b)^(2/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/a^2 + sqrt(3)*(-a*b^2)^(2/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/(a^2*b) - 3/(a*x^(1/3)) - 1/2*(-a*b^2)^(2/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/(a^2*b)

maple [A] time = 0.01, size = 104, normalized size = 0.95

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{\left(\frac{a}{b}\right)^{\frac{1}{3}} a} + \frac{\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{\left(\frac{a}{b}\right)^{\frac{1}{3}} a} - \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2\left(\frac{a}{b}\right)^{\frac{1}{3}} a} - \frac{3}{ax^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(4/3)/(b*x+a),x)`

[Out] $-3/a/x^{(1/3)}+1/a/(a/b)^{(1/3)}*\ln(x^{(1/3)}+(a/b)^{(1/3)})-1/2/a/(a/b)^{(1/3)}*\ln(x^{(2/3)}-(a/b)^{(1/3)}*x^{(1/3)}+(a/b)^{(2/3)})-1/a*3^{(1/2)}/(a/b)^{(1/3)}*\arctan(1/3*3^{(1/2)}*(2/(a/b)^{(1/3)}*x^{(1/3)}-1))$

maxima [A] time = 2.96, size = 111, normalized size = 1.02

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{a\left(\frac{a}{b}\right)^{\frac{1}{3}}} - \frac{\log\left(x^{\frac{2}{3}}-x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}}+\left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2a\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{\log\left(x^{\frac{1}{3}}+\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{a\left(\frac{a}{b}\right)^{\frac{1}{3}}} - \frac{3}{ax^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(4/3)/(b*x+a),x, algorithm="maxima")`

[Out] $-\sqrt{3}*\arctan(1/3*\sqrt{3}*(2*x^{(1/3)}-(a/b)^{(1/3)})/(a/b)^{(1/3)})/(a*(a/b)^{(1/3)})-1/2*\log(x^{(2/3)}-x^{(1/3)}*(a/b)^{(1/3)}+(a/b)^{(2/3)})/(a*(a/b)^{(1/3)})+\log(x^{(1/3)}+(a/b)^{(1/3)})/(a*(a/b)^{(1/3)})-3/(a*x^{(1/3)})$

mupad [B] time = 0.15, size = 124, normalized size = 1.14

$$\frac{b^{1/3} \ln\left(9a^{4/3}b^{8/3}+9ab^3x^{1/3}\right)}{a^{4/3}} - \frac{3}{ax^{1/3}} + \frac{b^{1/3} \ln\left(9ab^3x^{1/3}+9a^{4/3}b^{8/3}\left(-\frac{1}{2}+\frac{\sqrt{3}1i}{2}\right)^2\right)\left(-\frac{1}{2}+\frac{\sqrt{3}1i}{2}\right)}{a^{4/3}} - \frac{b^{1/3} \ln\left(9ab^3x^{1/3}+9a^{4/3}b^{8/3}\left(-\frac{1}{2}-\frac{\sqrt{3}1i}{2}\right)^2\right)\left(-\frac{1}{2}-\frac{\sqrt{3}1i}{2}\right)}{a^{4/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(4/3)*(a+b*x)),x)`

[Out] $(b^{(1/3)}*\log(9*a^{(4/3)}*b^{(8/3)}+9*a*b^3*x^{(1/3)}))/a^{(4/3)}-3/(a*x^{(1/3)})+(b^{(1/3)}*\log(9*a*b^3*x^{(1/3)}+9*a^{(4/3)}*b^{(8/3)}*((3^{(1/2)}*1i)/2-1/2)^2)*((3^{(1/2)}*1i)/2-1/2))/a^{(4/3)}-(b^{(1/3)}*\log(9*a*b^3*x^{(1/3)}+9*a^{(4/3)}*b^{(8/3)}*((3^{(1/2)}*1i)/2+1/2)^2)*((3^{(1/2)}*1i)/2+1/2))/a^{(4/3)}$

sympy [A] time = 25.29, size = 218, normalized size = 2.00

$$\left\{ \begin{array}{l} \frac{\infty}{x^{\frac{4}{3}}} \\ -\frac{3}{4bx^{\frac{4}{3}}} \\ -\frac{3}{a\sqrt[3]{x}} \\ -\frac{3}{a\sqrt[3]{x}} + \frac{(-1)^{\frac{2}{3}} \log\left(-\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{\frac{1}{b}} + \sqrt[3]{x}\right)}{a^{\frac{4}{3}} \sqrt[3]{\frac{1}{b}}} - \frac{(-1)^{\frac{2}{3}} \log\left(4(-1)^{\frac{2}{3}} a^{\frac{2}{3}} \left(\frac{1}{b}\right)^{\frac{2}{3}} + 4\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{x} \sqrt[3]{\frac{1}{b}} + 4x^{\frac{2}{3}}\right)}{2a^{\frac{4}{3}} \sqrt[3]{\frac{1}{b}}} + \frac{(-1)^{\frac{2}{3}} \sqrt{3} \operatorname{atan}\left(\frac{\sqrt{3}}{3} - \frac{2(-1)^{\frac{2}{3}} \sqrt{3} \sqrt[3]{x}}{3 \sqrt[3]{a} \sqrt[3]{\frac{1}{b}}}\right)}{a^{\frac{4}{3}} \sqrt[3]{\frac{1}{b}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(4/3)/(b*x+a), x)

[Out] Piecewise((zoo/x**(4/3), Eq(a, 0) & Eq(b, 0)), (-3/(4*b*x**(4/3)), Eq(a, 0)), (-3/(a*x**(1/3)), Eq(b, 0)), (-3/(a*x**(1/3)) + (-1)**(2/3)*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(a**(4/3)*(1/b)**(1/3)) - (-1)**(2/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(2*a**(4/3)*(1/b)**(1/3)) + (-1)**(2/3)*sqrt(3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(a**(4/3)*(1/b)**(1/3)), True))

$$3.681 \quad \int \frac{1}{x^{5/3}(a+bx)} dx$$

Optimal. Leaf size=111

$$-\frac{3b^{2/3} \log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{2a^{5/3}} + \frac{b^{2/3} \log(a+bx)}{2a^{5/3}} + \frac{\sqrt{3} b^{2/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{a^{5/3}} - \frac{3}{2ax^{2/3}}$$

[Out] $-3/2/a/x^{(2/3)}-3/2*b^{(2/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(5/3)}+1/2*b^{(2/3)}*\ln(b*x+a)/a^{(5/3)}+b^{(2/3)}*arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})*3^{(1/2)}/a^{(5/3)}$

Rubi [A] time = 0.04, antiderivative size = 111, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 58, 617, 204, 31}

$$-\frac{3b^{2/3} \log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{2a^{5/3}} + \frac{b^{2/3} \log(a+bx)}{2a^{5/3}} + \frac{\sqrt{3} b^{2/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{a^{5/3}} - \frac{3}{2ax^{2/3}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/3)*(a + b*x)),x]

[Out] $-3/(2*a*x^{(2/3)}) + (\text{Sqrt}[3]*b^{(2/3)}*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/a^{(5/3)} - (3*b^{(2/3)}*\text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(2*a^{(5/3)}) + (b^{(2/3)}*\text{Log}[a + b*x])/(2*a^{(5/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 58

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^

2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]) /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{x^{5/3}(a+bx)} dx &= -\frac{3}{2ax^{2/3}} - \frac{b \int \frac{1}{x^{2/3}(a+bx)} dx}{a} \\
 &= -\frac{3}{2ax^{2/3}} + \frac{b^{2/3} \log(a+bx)}{2a^{5/3}} - \frac{(3\sqrt[3]{b}) \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{2a^{4/3}} - \frac{(3b^{2/3}) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{3}{\sqrt[3]{a}x}\right)}{2a^{5/3}} \\
 &= -\frac{3}{2ax^{2/3}} - \frac{3b^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{5/3}} + \frac{b^{2/3} \log(a+bx)}{2a^{5/3}} - \frac{(3b^{2/3}) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{3}{\sqrt[3]{a}x}\right)}{a^{5/3}} \\
 &= -\frac{3}{2ax^{2/3}} + \frac{\sqrt{3} b^{2/3} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{a^{5/3}} - \frac{3b^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{5/3}} + \frac{b^{2/3} \log(a+bx)}{2a^{5/3}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 27, normalized size = 0.24

$$-\frac{{}_3F_1\left(-\frac{2}{3}, 1; \frac{1}{3}; -\frac{bx}{a}\right)}{2ax^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/3)*(a + b*x)),x]

[Out] (-3*Hypergeometric2F1[-2/3, 1, 1/3, -((b*x)/a)])/(2*a*x^(2/3))

fricas [A] time = 0.47, size = 147, normalized size = 1.32

$$\frac{2\sqrt{3}x\left(-\frac{b^2}{a^2}\right)^{\frac{1}{3}}\arctan\left(\frac{2\sqrt{3}ax^{\frac{1}{3}}\left(-\frac{b^2}{a^2}\right)^{\frac{2}{3}}-\sqrt{3}b}{3b}\right)-x\left(-\frac{b^2}{a^2}\right)^{\frac{1}{3}}\log\left(b^2x^{\frac{2}{3}}+abx^{\frac{1}{3}}\left(-\frac{b^2}{a^2}\right)^{\frac{1}{3}}+a^2\left(-\frac{b^2}{a^2}\right)^{\frac{2}{3}}\right)+2x\left(-\frac{b^2}{a^2}\right)^{\frac{1}{3}}\log\left(b^2x^{\frac{2}{3}}+abx^{\frac{1}{3}}\left(-\frac{b^2}{a^2}\right)^{\frac{1}{3}}+a^2\left(-\frac{b^2}{a^2}\right)^{\frac{2}{3}}\right)}{2ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/3)/(b*x+a),x, algorithm="fricas")

[Out] 1/2*(2*sqrt(3)*x*(-b^2/a^2)^(1/3)*arctan(1/3*(2*sqrt(3)*a*x^(1/3)*(-b^2/a^2)^(2/3) - sqrt(3)*b)/b) - x*(-b^2/a^2)^(1/3)*log(b^2*x^(2/3) + a*b*x^(1/3)*(-b^2/a^2)^(1/3) + a^2*(-b^2/a^2)^(2/3)) + 2*x*(-b^2/a^2)^(1/3)*log(b*x^(1/3) - a*(-b^2/a^2)^(1/3)) - 3*x^(1/3))/(a*x)

giac [A] time = 1.14, size = 120, normalized size = 1.08

$$\frac{b\left(-\frac{a}{b}\right)^{\frac{1}{3}}\log\left(x^{\frac{1}{3}}-\left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{a^2}-\frac{\sqrt{3}\left(-ab^2\right)^{\frac{1}{3}}\arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}+\left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{a^2}-\frac{\left(-ab^2\right)^{\frac{1}{3}}\log\left(x^{\frac{2}{3}}+x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}}+\left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2a^2}-\frac{3}{2ax^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/3)/(b*x+a),x, algorithm="giac")

[Out] b*(-a/b)^(1/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/a^2 - sqrt(3)*(-a*b^2)^(1/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/a^2 - 1/2*(-a*b^2)^(1/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/a^2 - 3/2/(a*x^(2/3))

maple [A] time = 0.01, size = 105, normalized size = 0.95

$$-\frac{\sqrt{3}\arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{\left(\frac{a}{b}\right)^{\frac{2}{3}}a}-\frac{\ln\left(x^{\frac{1}{3}}+\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{\left(\frac{a}{b}\right)^{\frac{2}{3}}a}+\frac{\ln\left(x^{\frac{2}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}}+\left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2\left(\frac{a}{b}\right)^{\frac{2}{3}}a}-\frac{3}{2ax^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(5/3)/(b*x+a),x)`

[Out] $-3/2/a/x^{2/3}-1/a/(a/b)^{2/3}*\ln(x^{1/3}+(a/b)^{1/3})+1/2/a/(a/b)^{2/3}*\ln(x^{2/3}-(a/b)^{1/3}*x^{1/3}+(a/b)^{2/3})-1/a/(a/b)^{2/3}*3^{1/2}*\arctan(1/3*3^{1/2}*(2/(a/b)^{1/3}*x^{1/3}-1))$

maxima [A] time = 2.99, size = 112, normalized size = 1.01

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{a\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{\log\left(x^{\frac{2}{3}}-x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}}+\left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{2a\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{\log\left(x^{\frac{1}{3}}+\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{a\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{3}{2ax^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(5/3)/(b*x+a),x, algorithm="maxima")`

[Out] $-\sqrt{3}*\arctan(1/3*\sqrt{3}*(2*x^{1/3}-(a/b)^{1/3})/(a/b)^{1/3})/(a*(a/b)^{2/3})+1/2*\log(x^{2/3}-x^{1/3}*(a/b)^{1/3}+(a/b)^{2/3})/(a*(a/b)^{2/3})-\log(x^{1/3}+(a/b)^{1/3})/(a*(a/b)^{2/3})-3/2/(a*x^{2/3})$

mupad [B] time = 0.07, size = 138, normalized size = 1.24

$$\frac{b^{2/3} \ln\left(9(-a)^{7/3} b^{8/3} - 9 a^2 b^3 x^{1/3}\right)}{(-a)^{5/3}} - \frac{3}{2 a x^{2/3}} + \frac{b^{2/3} \ln\left(9(-a)^{7/3} b^{8/3} \left(-\frac{1}{2} + \frac{\sqrt{3} 1i}{2}\right) - 9 a^2 b^3 x^{1/3}\right) \left(-\frac{1}{2} + \frac{\sqrt{3} 1i}{2}\right)}{(-a)^{5/3}} - \frac{b^{2/3} \ln\left(9(-a)^{7/3} b^{8/3} \left(-\frac{1}{2} + \frac{\sqrt{3} 1i}{2}\right) - 9 a^2 b^3 x^{1/3}\right) \left(-\frac{1}{2} - \frac{\sqrt{3} 1i}{2}\right)}{(-a)^{5/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(5/3)*(a + b*x)),x)`

[Out] $(b^{2/3}*\log(9*(-a)^{7/3}*b^{8/3}-9*a^2*b^3*x^{1/3}))/(-a)^{5/3}-3/(2*a*x^{2/3})+(b^{2/3}*\log(9*(-a)^{7/3}*b^{8/3}*((3^{1/2}*1i)/2-1/2)-9*a^2*b^3*x^{1/3}))*((3^{1/2}*1i)/2-1/2)/(-a)^{5/3}-(b^{2/3}*\log(9*(-a)^{7/3}*b^{8/3}*((3^{1/2}*1i)/2+1/2)+9*a^2*b^3*x^{1/3}))*((3^{1/2}*1i)/2+1/2)/(-a)^{5/3}$

sympy [A] time = 34.96, size = 221, normalized size = 1.99

$$\left\{ \begin{array}{l} \frac{\infty}{5} \\ x^{\frac{5}{3}} \\ -\frac{3}{2ax^{\frac{2}{3}}} \\ -\frac{3}{5bx^{\frac{5}{3}}} \end{array} \right. + \frac{\sqrt[3]{-1} \log\left(-\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{\frac{1}{b}} + \sqrt[3]{x}\right)}{a^{\frac{5}{3}} \left(\frac{1}{b}\right)^{\frac{2}{3}}} - \frac{\sqrt[3]{-1} \log\left(4(-1)^{\frac{2}{3}} a^{\frac{2}{3}} \left(\frac{1}{b}\right)^{\frac{2}{3}} + 4\sqrt[3]{-1} \sqrt[3]{a} \sqrt[3]{x} \sqrt[3]{\frac{1}{b}} + 4x^{\frac{2}{3}}\right)}{2a^{\frac{5}{3}} \left(\frac{1}{b}\right)^{\frac{2}{3}}} - \frac{\sqrt[3]{-1} \sqrt{3} \operatorname{atan}\left(\frac{\sqrt{3}}{3} - \frac{2(-1)^{\frac{2}{3}} \sqrt{3} \sqrt[3]{x}}{3\sqrt[3]{a} \sqrt[3]{\frac{1}{b}}}\right)}{a^{\frac{5}{3}} \left(\frac{1}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(5/3)/(b*x+a),x)`

[Out] `Piecewise((zoo/x**(5/3), Eq(a, 0) & Eq(b, 0)), (-3/(2*a*x**(2/3)), Eq(b, 0)), (-3/(5*b*x**(5/3)), Eq(a, 0)), (-3/(2*a*x**(2/3)) + (-1)**(1/3)*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(a**(5/3)*(1/b)**(2/3)) - (-1)**(1/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(2*a**(5/3)*(1/b)**(2/3)) - (-1)**(1/3)*sqrt(3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(a**(5/3)*(1/b)**(2/3)), True))`

$$3.682 \quad \int \frac{x^{5/3}}{(a+bx)^2} dx$$

Optimal. Leaf size=129

$$\frac{5a^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{8/3}} - \frac{5a^{2/3} \log(a+bx)}{6b^{8/3}} + \frac{5a^{2/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}b^{8/3}} - \frac{x^{5/3}}{b(a+bx)} + \frac{5x^{2/3}}{2b^2}$$

[Out] $5/2*x^{(2/3)}/b^2-x^{(5/3)}/b/(b*x+a)+5/2*a^{(2/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/b^{(8/3)}-5/6*a^{(2/3)}*\ln(b*x+a)/b^{(8/3)}+5/3*a^{(2/3)}*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/b^{(8/3)}*3^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 129, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.462$, Rules used = {47, 50, 56, 617, 204, 31}

$$\frac{5a^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{8/3}} - \frac{5a^{2/3} \log(a+bx)}{6b^{8/3}} + \frac{5a^{2/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}b^{8/3}} - \frac{x^{5/3}}{b(a+bx)} + \frac{5x^{2/3}}{2b^2}$$

Antiderivative was successfully verified.

[In] Int[x^(5/3)/(a + b*x)^2, x]

[Out] $(5*x^{(2/3)})/(2*b^2) - x^{(5/3)}/(b*(a + b*x)) + (5*a^{(2/3)}*ArcTan[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(Sqrt[3]*a^{(1/3)})])/(Sqrt[3]*b^{(8/3)}) + (5*a^{(2/3)}*Log[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(2*b^{(8/3)}) - (5*a^{(2/3)}*Log[a + b*x])/(6*b^{(8/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])] /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/3}}{(a+bx)^2} dx &= -\frac{x^{5/3}}{b(a+bx)} + \frac{5}{3b} \int \frac{x^{2/3}}{a+bx} dx \\
&= \frac{5x^{2/3}}{2b^2} - \frac{x^{5/3}}{b(a+bx)} - \frac{(5a)}{3b^2} \int \frac{1}{\sqrt[3]{x(a+bx)}} dx \\
&= \frac{5x^{2/3}}{2b^2} - \frac{x^{5/3}}{b(a+bx)} - \frac{5a^{2/3} \log(a+bx)}{6b^{8/3}} - \frac{(5a^{2/3}) \text{Subst} \left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x} \right)}{2b^3} + \frac{(5a^{2/3}) \text{Subst} \left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{x} \right)}{b^{8/3}} \\
&= \frac{5x^{2/3}}{2b^2} - \frac{x^{5/3}}{b(a+bx)} + \frac{5a^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{8/3}} - \frac{5a^{2/3} \log(a+bx)}{6b^{8/3}} - \frac{(5a^{2/3}) \text{Subst} \left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{x} \right)}{b^{8/3}} \\
&= \frac{5x^{2/3}}{2b^2} - \frac{x^{5/3}}{b(a+bx)} + \frac{5a^{2/3} \tan^{-1} \left(\frac{1 - 2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt[3]{a}} \right)}{\sqrt{3} b^{8/3}} + \frac{5a^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2b^{8/3}} - \frac{5a^{2/3} \log(a+bx)}{6b^{8/3}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.21

$$\frac{3x^{8/3} {}_2F_1\left(2, \frac{8}{3}; \frac{11}{3}; -\frac{bx}{a}\right)}{8a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/3)/(a + b*x)^2,x]

[Out] (3*x^(8/3)*Hypergeometric2F1[2, 8/3, 11/3, -(b*x)/a])/(8*a^2)

fricas [A] time = 0.47, size = 162, normalized size = 1.26

$$\frac{10 \sqrt{3} (bx+a) \left(\frac{a^2}{b^2}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}bx^{\frac{1}{3}}\left(\frac{a^2}{b^2}\right)^{\frac{1}{3}} - \sqrt{3}a}{3a}\right) + 5(bx+a) \left(\frac{a^2}{b^2}\right)^{\frac{1}{3}} \log\left(-bx^{\frac{1}{3}}\left(\frac{a^2}{b^2}\right)^{\frac{2}{3}} + ax^{\frac{2}{3}} + a\left(\frac{a^2}{b^2}\right)^{\frac{1}{3}}\right) - 10(bx)}{6(b^3x + ab^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)/(b*x+a)^2,x, algorithm="fricas")

[Out] $-1/6*(10*\sqrt{3}*(b*x + a)*(a^2/b^2)^{(1/3)}*\arctan(1/3*(2*\sqrt{3})*b*x^{(1/3)}*(a^2/b^2)^{(1/3)} - \sqrt{3}*a)/a) + 5*(b*x + a)*(a^2/b^2)^{(1/3)}*\log(-b*x^{(1/3)}*(a^2/b^2)^{(2/3)} + a*x^{(2/3)} + a*(a^2/b^2)^{(1/3)}) - 10*(b*x + a)*(a^2/b^2)^{(1/3)}*\log(b*(a^2/b^2)^{(2/3)} + a*x^{(1/3)}) - 3*(3*b*x + 5*a)*x^{(2/3)}/(b^3*x + a*b^2)$

giac [A] time = 1.05, size = 135, normalized size = 1.05

$$\frac{5 \left(-\frac{a}{b}\right)^{\frac{2}{3}} \log\left(x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3b^2} + \frac{ax^{\frac{2}{3}}}{(bx+a)b^2} + \frac{3x^{\frac{2}{3}}}{2b^2} + \frac{5\sqrt{3}(-ab^2)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3b^4} - \frac{5(-ab^2)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\right)}{6b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)/(b*x+a)^2,x, algorithm="giac")

[Out] $5/3*(-a/b)^{(2/3)}*\log(\text{abs}(x^{(1/3)} - (-a/b)^{(1/3)}))/b^2 + a*x^{(2/3)}/((b*x + a)*b^2) + 3/2*x^{(2/3)}/b^2 + 5/3*\sqrt{3}*(-a*b^2)^{(2/3)}*\arctan(1/3*\sqrt{3}*(2*x^{(1/3)} + (-a/b)^{(1/3)})/(-a/b)^{(1/3)})/b^4 - 5/6*(-a*b^2)^{(2/3)}*\log(x^{(2/3)} + x^{(1/3)}*(-a/b)^{(1/3)} + (-a/b)^{(2/3)})/b^4$

maple [A] time = 0.01, size = 123, normalized size = 0.95

$$\frac{ax^{\frac{2}{3}}}{(bx+a)b^2} - \frac{5\sqrt{3}a \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}b^3} + \frac{5a \ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}b^3} - \frac{5a \ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{6\left(\frac{a}{b}\right)^{\frac{1}{3}}b^3} + \frac{3x^{\frac{2}{3}}}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/3)/(b*x+a)^2,x)

[Out] $3/2*x^{(2/3)}/b^2+a/b^2*x^{(2/3)}/(b*x+a)+5/3*a/b^3/(a/b)^{(1/3)}*\ln(x^{(1/3)}+(a/b)^{(1/3)})-5/6*a/b^3/(a/b)^{(1/3)}*\ln(x^{(2/3)}-(a/b)^{(1/3)}*x^{(1/3)}+(a/b)^{(2/3)})-5/3*a/b^3*3^{(1/2)}/(a/b)^{(1/3)}*\arctan(1/3*3^{(1/2)}*(2/(a/b)^{(1/3)}*x^{(1/3)}-1))$

maxima [A] time = 2.96, size = 133, normalized size = 1.03

$$\frac{ax^{\frac{2}{3}}}{b^3x + ab^2} - \frac{5\sqrt{3}a \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3b^3\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{3x^{\frac{2}{3}}}{2b^2} - \frac{5a \log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{6b^3\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{5a \log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3b^3\left(\frac{a}{b}\right)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)/(b*x+a)^2,x, algorithm="maxima")

[Out] a*x^(2/3)/(b^3*x + a*b^2) - 5/3*sqrt(3)*a*arctan(1/3*sqrt(3)*(2*x^(1/3) - (a/b)^(1/3))/(a/b)^(1/3))/(b^3*(a/b)^(1/3)) + 3/2*x^(2/3)/b^2 - 5/6*a*log(x^(2/3) - x^(1/3)*(a/b)^(1/3) + (a/b)^(2/3))/(b^3*(a/b)^(1/3)) + 5/3*a*log(x^(1/3) + (a/b)^(1/3))/(b^3*(a/b)^(1/3))

mupad [B] time = 0.26, size = 150, normalized size = 1.16

$$\frac{3x^{2/3}}{2b^2} + \frac{5a^{2/3} \ln\left(\frac{25a^{7/3}}{b^{10/3}} + \frac{25a^2x^{1/3}}{b^3}\right)}{3b^{8/3}} + \frac{ax^{2/3}}{xb^3 + ab^2} + \frac{5a^{2/3} \ln\left(\frac{25a^{7/3}\left(-\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right)^2}{b^{10/3}} + \frac{25a^2x^{1/3}}{b^3}\right)\left(-\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right)}{3b^{8/3}} - \frac{5a^{2/3} \ln\left(\frac{25a^{7/3}\left(-\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right)^2}{b^{10/3}} + \frac{25a^2x^{1/3}}{b^3}\right)\left(-\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right)}{3b^{8/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/3)/(a + b*x)^2,x)

[Out] (3*x^(2/3))/(2*b^2) + (5*a^(2/3)*log((25*a^(7/3))/b^(10/3) + (25*a^2*x^(1/3))/b^3))/(3*b^(8/3)) + (a*x^(2/3))/(a*b^2 + b^3*x) + (5*a^(2/3)*log((25*a^(7/3)*((3^(1/2)*1i)/2 - 1/2)^2)/b^(10/3) + (25*a^2*x^(1/3))/b^3)*((3^(1/2)*1i)/2 - 1/2))/(3*b^(8/3)) - (5*a^(2/3)*log((25*a^(7/3)*((3^(1/2)*1i)/2 + 1/2)^2)/b^(10/3) + (25*a^2*x^(1/3))/b^3)*((3^(1/2)*1i)/2 + 1/2))/(3*b^(8/3))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/3)/(b*x+a)**2,x)

[Out] Timed out

$$3.683 \quad \int \frac{x^{4/3}}{(a+bx)^2} dx$$

Optimal. Leaf size=125

$$-\frac{2\sqrt[3]{a} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{b^{7/3}} + \frac{2\sqrt[3]{a} \log(a+bx)}{3b^{7/3}} + \frac{4\sqrt[3]{a} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}b^{7/3}} - \frac{x^{4/3}}{b(a+bx)} + \frac{4\sqrt[3]{x}}{b^2}$$

[Out] $4*x^{(1/3)}/b^2-x^{(4/3)}/b/(b*x+a)-2*a^{(1/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/b^{(7/3)}+2/3*a^{(1/3)}*\ln(b*x+a)/b^{(7/3)}+4/3*a^{(1/3)}*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/b^{(7/3)}*3^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 125, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.462$, Rules used = {47, 50, 58, 617, 204, 31}

$$-\frac{2\sqrt[3]{a} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{b^{7/3}} + \frac{2\sqrt[3]{a} \log(a+bx)}{3b^{7/3}} + \frac{4\sqrt[3]{a} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}b^{7/3}} - \frac{x^{4/3}}{b(a+bx)} + \frac{4\sqrt[3]{x}}{b^2}$$

Antiderivative was successfully verified.

[In] Int[x^(4/3)/(a + b*x)^2, x]

[Out] $(4*x^{(1/3)})/b^2 - x^{(4/3)}/(b*(a + b*x)) + (4*a^{(1/3)}*ArcTan[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(Sqrt[3]*a^{(1/3)})])/(Sqrt[3]*b^{(7/3)}) - (2*a^{(1/3)}*Log[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/b^{(7/3)} + (2*a^{(1/3)}*Log[a + b*x])/(3*b^{(7/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 58

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^
2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(
1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)],
x])] /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{4/3}}{(a+bx)^2} dx &= -\frac{x^{4/3}}{b(a+bx)} + \frac{4}{3b} \int \frac{\sqrt[3]{x}}{a+bx} dx \\
&= \frac{4\sqrt[3]{x}}{b^2} - \frac{x^{4/3}}{b(a+bx)} - \frac{(4a)}{3b^2} \int \frac{1}{x^{2/3}(a+bx)} dx \\
&= \frac{4\sqrt[3]{x}}{b^2} - \frac{x^{4/3}}{b(a+bx)} + \frac{2\sqrt[3]{a} \log(a+bx)}{3b^{7/3}} - \frac{(2a^{2/3}) \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{b^{8/3}} - \frac{(2\sqrt[3]{a}) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{x}\right)}{b^{7/3}} \\
&= \frac{4\sqrt[3]{x}}{b^2} - \frac{x^{4/3}}{b(a+bx)} - \frac{2\sqrt[3]{a} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{b^{7/3}} + \frac{2\sqrt[3]{a} \log(a+bx)}{3b^{7/3}} - \frac{(4\sqrt[3]{a}) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{x}\right)}{b^{7/3}} \\
&= \frac{4\sqrt[3]{x}}{b^2} - \frac{x^{4/3}}{b(a+bx)} + \frac{4\sqrt[3]{a} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3} b^{7/3}} - \frac{2\sqrt[3]{a} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{b^{7/3}} + \frac{2\sqrt[3]{a} \log(a+bx)}{3b^{7/3}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.22

$$\frac{3x^{7/3} {}_2F_1\left(2, \frac{7}{3}; \frac{10}{3}; -\frac{bx}{a}\right)}{7a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(4/3)/(a + b*x)^2,x]

[Out] (3*x^(7/3)*Hypergeometric2F1[2, 7/3, 10/3, -(b*x)/a])/(7*a^2)

fricas [A] time = 0.49, size = 147, normalized size = 1.18

$$\frac{4\sqrt{3}(bx+a)\left(-\frac{a}{b}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}bx^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{2}{3}} - \sqrt{3}a}{3a}\right) - 2(bx+a)\left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right) + 4(bx+a)\left(-\frac{a}{b}\right)^{\frac{1}{3}}}{3(b^3x + ab^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)/(b*x+a)^2,x, algorithm="fricas")

[Out] $\frac{1}{3} \cdot (4 \sqrt{3} (bx + a) (-a/b)^{1/3} \arctan(1/3 \cdot (2 \sqrt{3} (bx + a)^{1/3} (-a/b)^{1/3} - \sqrt{3} a/a) - 2 (bx + a) (-a/b)^{1/3} \log(x^{2/3} + x^{1/3} (-a/b)^{1/3} + (-a/b)^{2/3})) + 4 (bx + a) (-a/b)^{1/3} \log(x^{1/3} - (-a/b)^{1/3}) + 3 (3bx + 4a) x^{1/3}) / (b^3 x + a b^2)$

giac [A] time = 1.07, size = 135, normalized size = 1.08

$$\frac{4 \left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{3 b^2} - \frac{4 \sqrt{3} (-ab^2)^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3 b^3} + \frac{ax^{\frac{1}{3}}}{(bx+a)b^2} + \frac{3x^{\frac{1}{3}}}{b^2} - \frac{2(-ab^2)^{\frac{1}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\right)}{3 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(4/3)/(b*x+a)^2,x, algorithm="giac")`

[Out] $\frac{4}{3} (-a/b)^{1/3} \log(\text{abs}(x^{1/3} - (-a/b)^{1/3})) / b^2 - \frac{4}{3} \sqrt{3} (-a b^2)^{1/3} \arctan(1/3 \sqrt{3} (2x^{1/3} + (-a/b)^{1/3}) / (-a/b)^{1/3}) / b^3 + a x^{1/3} / ((bx + a) b^2) + 3x^{1/3} / b^2 - \frac{2}{3} (-a b^2)^{1/3} \log(x^{2/3} + x^{1/3} (-a/b)^{1/3} + (-a/b)^{2/3}) / b^3$

maple [A] time = 0.01, size = 123, normalized size = 0.98

$$\frac{ax^{\frac{1}{3}}}{(bx+a)b^2} - \frac{4\sqrt{3} a \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{3\left(\frac{a}{b}\right)^{\frac{2}{3}} b^3} - \frac{4a \ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{2}{3}} b^3} + \frac{2a \ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{2}{3}} b^3} + \frac{3x^{\frac{1}{3}}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(4/3)/(b*x+a)^2,x)`

[Out] $3x^{1/3}/b^2 + a/b^2 \cdot x^{1/3}/(bx+a) - \frac{4}{3} a/b^3 / (a/b)^{2/3} \cdot \ln(x^{1/3} + (a/b)^{1/3}) + \frac{2}{3} a/b^3 / (a/b)^{2/3} \cdot \ln(x^{2/3} - (a/b)^{1/3} x^{1/3} + (a/b)^{2/3}) - \frac{4}{3} a/b^3 / (a/b)^{2/3} \cdot 3^{1/2} \arctan(1/3 \cdot 3^{1/2} \cdot (2/(a/b)^{1/3} x^{1/3} - 1))$

maxima [A] time = 2.93, size = 133, normalized size = 1.06

$$\frac{ax^{\frac{1}{3}}}{b^3 x + ab^2} - \frac{4 \sqrt{3} a \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3 b^3 \left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{3x^{\frac{1}{3}}}{b^2} + \frac{2 a \log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}} \left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{3 b^3 \left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{4 a \log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3 b^3 \left(\frac{a}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)/(b*x+a)^2,x, algorithm="maxima")

[Out] $a*x^{1/3}/(b^3*x + a*b^2) - 4/3*\sqrt{3}*a*\arctan(1/3*\sqrt{3}*(2*x^{1/3} - (a/b)^{1/3}))/((a/b)^{1/3}*(b^3*(a/b)^{2/3})) + 3*x^{1/3}/b^2 + 2/3*a*\log(x^{2/3} - x^{1/3}*(a/b)^{1/3} + (a/b)^{2/3})/(b^3*(a/b)^{2/3}) - 4/3*a*\log(x^{1/3} + (a/b)^{1/3})/(b^3*(a/b)^{2/3})$

mupad [B] time = 0.15, size = 142, normalized size = 1.14

$$\frac{3x^{1/3}}{b^2} + \frac{ax^{1/3}}{xb^3 + ab^2} + \frac{4(-a)^{1/3} \ln\left(\frac{12(-a)^{4/3}}{b^{1/3}} + 12ax^{1/3}\right)}{3b^{7/3}} - \frac{4(-a)^{1/3} \ln\left(12ax^{1/3} - \frac{12(-a)^{4/3}\left(\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right)}{b^{1/3}}\right)}{3b^{7/3}} \left(\frac{1}{2} + \frac{\sqrt{3}1i}{2}\right) + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(4/3)/(a + b*x)^2,x)

[Out] $(3*x^{1/3})/b^2 + (a*x^{1/3})/(a*b^2 + b^3*x) + (4*(-a)^{1/3}*\log((12*(-a)^{4/3})/b^{1/3} + 12*a*x^{1/3}))/((3*b^{7/3})) - (4*(-a)^{1/3}*\log(12*a*x^{1/3} - (12*(-a)^{4/3}*((3^{1/2}*1i)/2 + 1/2))/b^{1/3}))/((3^{1/2}*1i)/2 + 1/2))/((3*b^{7/3})) + ((-a)^{1/3}*\log(12*a*x^{1/3} + (9*(-a)^{4/3}*((3^{1/2}*2i)/3 - 2/3))/b^{1/3}))/((3^{1/2}*2i)/3 - 2/3))/b^{7/3}$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(4/3)/(b*x+a)**2,x)

[Out] Timed out

$$3.684 \quad \int \frac{x^{2/3}}{(a+bx)^2} dx$$

Optimal. Leaf size=115

$$-\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{\sqrt[3]{a} b^{5/3}} + \frac{\log(a+bx)}{3\sqrt[3]{a} b^{5/3}} - \frac{2 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}\sqrt[3]{a} b^{5/3}} - \frac{x^{2/3}}{b(a+bx)}$$

[Out] $-x^{2/3}/b/(b*x+a)-\ln(a^{1/3}+b^{1/3}*x^{1/3})/a^{1/3}/b^{5/3}+1/3*\ln(b*x+a)/a^{1/3}/b^{5/3}-2/3*\arctan(1/3*(a^{1/3}-2*b^{1/3}*x^{1/3})/a^{1/3})*3^{1/2})/a^{1/3}/b^{5/3}*3^{1/2}$

Rubi [A] time = 0.04, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {47, 56, 617, 204, 31}

$$-\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{\sqrt[3]{a} b^{5/3}} + \frac{\log(a+bx)}{3\sqrt[3]{a} b^{5/3}} - \frac{2 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}\sqrt[3]{a} b^{5/3}} - \frac{x^{2/3}}{b(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[x^(2/3)/(a + b*x)^2, x]

[Out] $-(x^{2/3}/(b*(a + b*x))) - (2*\text{ArcTan}[(a^{1/3} - 2*b^{1/3}*x^{1/3})]/(\text{Sqrt}[3]*a^{1/3}))/(\text{Sqrt}[3]*a^{1/3}*b^{5/3}) - \text{Log}[a^{1/3} + b^{1/3}*x^{1/3}]/(a^{1/3}*b^{5/3}) + \text{Log}[a + b*x]/(3*a^{1/3}*b^{5/3})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m+1)*(c + d*x)^n/(b*(m+1)), x] - Dist[(d*n)/(b*(m+1)), Int[(a + b*x)^(m+1)*(c + d*x)^(n-1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m+n+2, 0] && (FractionQ[m] || GeQ[2*n+m+1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]) /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{2/3}}{(a+bx)^2} dx &= -\frac{x^{2/3}}{b(a+bx)} + \frac{2 \int \frac{1}{\sqrt[3]{x}(a+bx)} dx}{3b} \\
&= -\frac{x^{2/3}}{b(a+bx)} + \frac{\log(a+bx)}{3\sqrt[3]{a}b^{5/3}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{b^2} - \frac{\text{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{a}}{\sqrt[3]{b}} + x} dx, x, \sqrt[3]{x}\right)}{\sqrt[3]{a}b^{5/3}} \\
&= -\frac{x^{2/3}}{b(a+bx)} - \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{\sqrt[3]{a}b^{5/3}} + \frac{\log(a+bx)}{3\sqrt[3]{a}b^{5/3}} + \frac{2 \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}\right)}{\sqrt[3]{a}b^{5/3}} \\
&= -\frac{x^{2/3}}{b(a+bx)} - \frac{2 \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3}\sqrt[3]{a}b^{5/3}} - \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{\sqrt[3]{a}b^{5/3}} + \frac{\log(a+bx)}{3\sqrt[3]{a}b^{5/3}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.23

$$\frac{3x^{5/3} {}_2F_1\left(\frac{5}{3}, 2; \frac{8}{3}; -\frac{bx}{a}\right)}{5a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(2/3)/(a + b*x)^2,x]

[Out] (3*x^(5/3)*Hypergeometric2F1[5/3, 2, 8/3, -((b*x)/a)])/(5*a^2)

fricas [B] time = 0.48, size = 394, normalized size = 3.43

$$\frac{3ab^2x^{\frac{2}{3}} - 3\sqrt{\frac{1}{3}}(ab^2x + a^2b)\sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} \log\left(\frac{2b^2x - ab + 3\sqrt{\frac{1}{3}}\left(abx^{\frac{1}{3}} + (-ab^2)^{\frac{1}{3}}a + 2(-ab^2)^{\frac{2}{3}}x^{\frac{2}{3}}\right)\sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} - 3(-ab^2)^{\frac{2}{3}}x^{\frac{1}{3}}}{bx+a}}{3(ab^4x + a^2b^3)}\right) - (-ab^2)^{\frac{2}{3}}x^{\frac{1}{3}}}{3(ab^4x + a^2b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)/(b*x+a)^2,x, algorithm="fricas")

[Out] [-1/3*(3*a*b^2*x^(2/3) - 3*sqrt(1/3)*(a*b^2*x + a^2*b)*sqrt((-a*b^2)^(1/3)/a)*log((2*b^2*x - a*b + 3*sqrt(1/3)*(a*b*x^(1/3) + (-a*b^2)^(1/3)*a + 2*(-a*b^2)^(2/3)*x^(2/3))*sqrt((-a*b^2)^(1/3)/a) - 3*(-a*b^2)^(2/3)*x^(1/3))/(b*x + a)) - (-a*b^2)^(2/3)*(b*x + a)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) + 2*(-a*b^2)^(2/3)*(b*x + a)*log(b*x^(1/3) - (-a*b^2)^(1/3)))/(a*b^4*x + a^2*b^3), -1/3*(3*a*b^2*x^(2/3) - 6*sqrt(1/3)*(a*b^2*x + a^2*b)*sqrt(-(-a*b^2)^(1/3)/a)*arctan(sqrt(1/3)*(2*b*x^(1/3) + (-a*b^2)^(1/3))*sqrt(-(-a*b^2)^(1/3)/a)/b) - (-a*b^2)^(2/3)*(b*x + a)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) + 2*(-a*b^2)^(2/3)*(b*x + a)*log(b*x^(1/3) - (-a*b^2)^(1/3)))/(a*b^4*x + a^2*b^3)]

giac [A] time = 1.20, size = 136, normalized size = 1.18

$$\frac{2\left(-\frac{a}{b}\right)^{\frac{2}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{3ab} - \frac{x^{\frac{2}{3}}}{(bx+a)b} - \frac{2\sqrt{3}(-ab^2)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3ab^3} + \frac{(-ab^2)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3ab^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)/(b*x+a)^2,x, algorithm="giac")

[Out] -2/3*(-a/b)^(2/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/(a*b) - x^(2/3)/((b*x + a)*b) - 2/3*sqrt(3)*(-a*b^2)^(2/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3)))/3ab^3

$1/3)/(-a/b)^{(1/3)}/(a*b^3) + 1/3*(-a*b^2)^{(2/3)}*\log(x^{(2/3)} + x^{(1/3)}*(-a/b)^{(1/3)} + (-a/b)^{(2/3)})/(a*b^3)$

maple [A] time = 0.01, size = 112, normalized size = 0.97

$$-\frac{x^{\frac{2}{3}}}{(bx+a)b} + \frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}b^2} - \frac{2\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}b^2} + \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(2/3)/(b*x+a)^2,x)`

[Out] $-x^{(2/3)}/b/(b*x+a)^{-2/3}/b^2/(a/b)^{(1/3)}*\ln(x^{(1/3)}+(a/b)^{(1/3)})+1/3/b^2/(a/b)^{(1/3)}*\ln(x^{(2/3)}-(a/b)^{(1/3)}*x^{(1/3)}+(a/b)^{(2/3)})+2/3/b^2*3^{(1/2)}/(a/b)^{(1/3)}*\arctan(1/3*3^{(1/2)}*(2/(a/b)^{(1/3)}*x^{(1/3)}-1))$

maxima [A] time = 2.99, size = 120, normalized size = 1.04

$$-\frac{x^{\frac{2}{3}}}{b^2x+ab} + \frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3b^2\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{3b^2\left(\frac{a}{b}\right)^{\frac{1}{3}}} - \frac{2\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3b^2\left(\frac{a}{b}\right)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(2/3)/(b*x+a)^2,x, algorithm="maxima")`

[Out] $-x^{(2/3)}/(b^2*x+a*b) + 2/3*\sqrt{3}*\arctan(1/3*\sqrt{3}*(2*x^{(1/3)} - (a/b)^{(1/3)})/(a/b)^{(1/3)})/(b^2*(a/b)^{(1/3)}) + 1/3*\log(x^{(2/3)} - x^{(1/3)}*(a/b)^{(1/3)} + (a/b)^{(2/3)})/(b^2*(a/b)^{(1/3)}) - 2/3*\log(x^{(1/3)} + (a/b)^{(1/3)})/(b^2*(a/b)^{(1/3)})$

mupad [B] time = 0.24, size = 142, normalized size = 1.23

$$\frac{2\ln\left(\frac{4x^{1/3}}{b} - \frac{4(-a)^{1/3}}{b^{4/3}}\right)}{3(-a)^{1/3}b^{5/3}} - \frac{x^{2/3}}{b(a+bx)} + \frac{\ln\left(\frac{4x^{1/3}}{b} - \frac{(-a)^{1/3}(-1+\sqrt{3}i)^2}{b^{4/3}}\right)(-1+\sqrt{3}i)}{3(-a)^{1/3}b^{5/3}} - \frac{\ln\left(\frac{4x^{1/3}}{b} - \frac{(-a)^{1/3}(1+\sqrt{3}i)^2}{b^{4/3}}\right)(1+\sqrt{3}i)}{3(-a)^{1/3}b^{5/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(2/3)/(a + b*x)^2,x)`

[Out] $(2*\log((4*x^{(1/3)})/b - (4*(-a)^{(1/3)})/b^{(4/3)}))/(3*(-a)^{(1/3)}*b^{(5/3)}) - x^{(2/3)}/(b*(a + b*x)) + (\log((4*x^{(1/3)})/b - ((-a)^{(1/3)}*(3^{(1/2)}*1i - 1)^2)/b^{(4/3)})*(3^{(1/2)}*1i - 1))/(3*(-a)^{(1/3)}*b^{(5/3)}) - (\log((4*x^{(1/3)})/b - ((-a)^{(1/3)}*(3^{(1/2)}*1i + 1)^2)/b^{(4/3)})*(3^{(1/2)}*1i + 1))/(3*(-a)^{(1/3)}*b^{(5/3)})$

sympy [A] time = 106.98, size = 787, normalized size = 6.84

$$\left\{ \begin{array}{l} \frac{\infty}{\sqrt[3]{x}} \\ \frac{3x^5}{5a^2} \\ \frac{3}{b^2\sqrt[3]{x}} \end{array} \right. - \frac{3\sqrt[3]{-1}\sqrt[3]{a}bx^{\frac{2}{3}}\sqrt[3]{\frac{1}{b}}}{3\sqrt[3]{-1}a^{\frac{4}{3}}b^2\sqrt[3]{\frac{1}{b}}+3\sqrt[3]{-1}\sqrt[3]{a}b^3x\sqrt[3]{\frac{1}{b}}} + \frac{2a\log\left(-\sqrt[3]{-1}\sqrt[3]{a}\sqrt[3]{\frac{1}{b}}+\sqrt[3]{x}\right)}{3\sqrt[3]{-1}a^{\frac{4}{3}}b^2\sqrt[3]{\frac{1}{b}}+3\sqrt[3]{-1}\sqrt[3]{a}b^3x\sqrt[3]{\frac{1}{b}}} - \frac{a\log\left(4(-1)^{\frac{2}{3}}a^{\frac{2}{3}}\left(\frac{1}{b}\right)^{\frac{2}{3}}+4\sqrt[3]{-1}\sqrt[3]{a}\sqrt[3]{x}\sqrt[3]{\frac{1}{b}}+4x^{\frac{2}{3}}\right)}{3\sqrt[3]{-1}a^{\frac{4}{3}}b^2\sqrt[3]{\frac{1}{b}}+3\sqrt[3]{-1}\sqrt[3]{a}b^3x\sqrt[3]{\frac{1}{b}}} + \frac{2\sqrt{3}a}{3\sqrt[3]{-1}a^{\frac{4}{3}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(2/3)/(b*x+a)**2,x)`

[Out] `Piecewise((zoo/x**(1/3), Eq(a, 0) & Eq(b, 0)), (3*x**(5/3)/(5*a**2), Eq(b, 0)), (-3/(b**2*x**(1/3)), Eq(a, 0)), (-3*(-1)**(1/3)*a**(1/3)*b*x**(2/3)*(1/b)**(1/3)/(3*(-1)**(1/3)*a**(4/3)*b**2*(1/b)**(1/3) + 3*(-1)**(1/3)*a**(1/3)*b**3*x*(1/b)**(1/3)) + 2*a*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(3*(-1)**(1/3)*a**(4/3)*b**2*(1/b)**(1/3) + 3*(-1)**(1/3)*a**(1/3)*b**3*x*(1/b)**(1/3)) - a*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(3*(-1)**(1/3)*a**(4/3)*b**2*(1/b)**(1/3) + 3*(-1)**(1/3)*a**(1/3)*b**3*x*(1/b)**(1/3)) + 2*sqrt(3)*a*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(3*(-1)**(1/3)*a**(4/3)*b**2*(1/b)**(1/3) + 3*(-1)**(1/3)*a**(1/3)*b**3*x*(1/b)**(1/3)) + 2*a*log(2)/(3*(-1)**(1/3)*a**(4/3)*b**2*(1/b)**(1/3) + 3*(-1)**(1/3)*a**(1/3)*b**3*x*(1/b)**(1/3)) + 2*b*x*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(3*(-1)**(1/3)*a**(4/3)*b**2*(1/b)**(1/3) + 3*(-1)**(1/3)*a**(1/3)*b**3*x*(1/b)**(1/3)) - b*x*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(3*(-1)**(1/3)*a**(4/3)*b**2*(1/b)**(1/3) + 3*(-1)**(1/3)*a**(1/3)*b**3*x*(1/b)**(1/3)) + 2*sqrt(3)*b*x*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(3*(-1)**(1/3)*a**(4/3)*b**2*(1/b)**(1/3) + 3*(-1)**(1/3)*a**(1/3)*b**3*x*(1/b)**(1/3))`

```
(1/3)*a**(1/3)*b**3*x*(1/b)**(1/3)) + 2*b*x*log(2)/(3*(-1)**(1/3)*a**(4/3)*  
b**2*(1/b)**(1/3) + 3*(-1)**(1/3)*a**(1/3)*b**3*x*(1/b)**(1/3)), True))
```


$$3.685 \quad \int \frac{\sqrt[3]{x}}{(a+bx)^2} dx$$

Optimal. Leaf size=117

$$\frac{\log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{2a^{2/3}b^{4/3}} - \frac{\log(a+bx)}{6a^{2/3}b^{4/3}} - \frac{\tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{2/3}b^{4/3}} - \frac{\sqrt[3]{x}}{b(a+bx)}$$

[Out] $-x^{(1/3)}/b/(b*x+a)+1/2*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(2/3)}/b^{(4/3)}-1/6*\ln(b*x+a)/a^{(2/3)}/b^{(4/3)}-1/3*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/a^{(2/3)}/b^{(4/3)}*3^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 117, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {47, 58, 617, 204, 31}

$$\frac{\log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{2a^{2/3}b^{4/3}} - \frac{\log(a+bx)}{6a^{2/3}b^{4/3}} - \frac{\tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{2/3}b^{4/3}} - \frac{\sqrt[3]{x}}{b(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[x^(1/3)/(a + b*x)^2,x]

[Out] $-(x^{(1/3)}/(b*(a + b*x))) - \text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})]/(\text{Sqrt}[3]*a^{(2/3)}*b^{(4/3)}) + \text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}]/(2*a^{(2/3)}*b^{(4/3)}) - \text{Log}[a + b*x]/(6*a^{(2/3)}*b^{(4/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 58

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^
2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(
1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)],
x])] /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt[3]{x}}{(a+bx)^2} dx &= -\frac{\sqrt[3]{x}}{b(a+bx)} + \frac{\int \frac{1}{x^{2/3}(a+bx)} dx}{3b} \\ &= -\frac{\sqrt[3]{x}}{b(a+bx)} - \frac{\log(a+bx)}{6a^{2/3}b^{4/3}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{ax}}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{2\sqrt[3]{a}b^{5/3}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{a}}{\sqrt[3]{b}} + x} dx, x, \sqrt[3]{x}\right)}{2a^{2/3}b^{4/3}} \\ &= -\frac{\sqrt[3]{x}}{b(a+bx)} + \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{2a^{2/3}b^{4/3}} - \frac{\log(a+bx)}{6a^{2/3}b^{4/3}} + \frac{\text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}\right)}{a^{2/3}b^{4/3}} \\ &= -\frac{\sqrt[3]{x}}{b(a+bx)} - \frac{\tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3}a^{2/3}b^{4/3}} + \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{2a^{2/3}b^{4/3}} - \frac{\log(a+bx)}{6a^{2/3}b^{4/3}} \end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.23

$$\frac{3x^{4/3} {}_2F_1\left(\frac{4}{3}, 2; \frac{7}{3}; -\frac{bx}{a}\right)}{4a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(1/3)/(a + b*x)^2,x]

[Out] (3*x^(4/3)*Hypergeometric2F1[4/3, 2, 7/3, -((b*x)/a)])/(4*a^2)

fricas [B] time = 0.50, size = 389, normalized size = 3.32

$$\frac{6 a^2 b x^{\frac{1}{3}} - 3 \sqrt{\frac{1}{3}} (a b^2 x + a^2 b) \sqrt{-\frac{(a^2 b)^{\frac{1}{3}}}{b}} \log \left(\frac{2 a b x - a^2 + 3 \sqrt{\frac{1}{3}} \left(2 a b x^{\frac{2}{3}} - (a^2 b)^{\frac{1}{3}} a + (a^2 b)^{\frac{2}{3}} x^{\frac{1}{3}} \right) \sqrt{-\frac{(a^2 b)^{\frac{1}{3}}}{b}} - 3 (a^2 b)^{\frac{1}{3}} a x^{\frac{1}{3}}}{b x + a} \right) + (a^2 b)^{\frac{2}{3}}}{6 (a^2 b^3 x + a^3 b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)/(b*x+a)^2,x, algorithm="fricas")

[Out] [-1/6*(6*a^2*b*x^(1/3) - 3*sqrt(1/3)*(a*b^2*x + a^2*b)*sqrt(-(a^2*b)^(1/3)/b)*log((2*a*b*x - a^2 + 3*sqrt(1/3)*(2*a*b*x^(2/3) - (a^2*b)^(1/3)*a + (a^2*b)^(2/3)*x^(1/3))*sqrt(-(a^2*b)^(1/3)/b) - 3*(a^2*b)^(1/3)*a*x^(1/3))/(b*x + a)) + (a^2*b)^(2/3)*(b*x + a)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) - 2*(a^2*b)^(2/3)*(b*x + a)*log(a*b*x^(1/3) + (a^2*b)^(2/3)))/(a^2*b^3*x + a^3*b^2), -1/6*(6*a^2*b*x^(1/3) - 6*sqrt(1/3)*(a*b^2*x + a^2*b)*sqrt((a^2*b)^(1/3)/b)*arctan(-sqrt(1/3)*((a^2*b)^(1/3)*a - 2*(a^2*b)^(2/3)*x^(1/3))*sqrt((a^2*b)^(1/3)/b)/a^2) + (a^2*b)^(2/3)*(b*x + a)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) - 2*(a^2*b)^(2/3)*(b*x + a)*log(a*b*x^(1/3) + (a^2*b)^(2/3)))/(a^2*b^3*x + a^3*b^2)]

giac [A] time = 1.13, size = 136, normalized size = 1.16

$$\frac{\left(-\frac{a}{b}\right)^{\frac{1}{3}} \log \left(\left| x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}} \right| \right)}{3 a b} + \frac{\sqrt{3} (-a b^2)^{\frac{1}{3}} \arctan \left(\frac{\sqrt{3} \left(2 x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}} \right)}{3 \left(-\frac{a}{b}\right)^{\frac{1}{3}}} \right)}{3 a b^2} - \frac{x^{\frac{1}{3}}}{(b x + a) b} + \frac{(-a b^2)^{\frac{1}{3}} \log \left(x^{\frac{2}{3}} + x^{\frac{1}{3}} \left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}} \right)}{6 a b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)/(b*x+a)^2,x, algorithm="giac")

[Out] -1/3*(-a/b)^(1/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/(a*b) + 1/3*sqrt(3)*(-a*b^2)^(1/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/(a*b

$\sqrt{2} - x^{1/3}/((b*x + a)*b) + 1/6*(-a*b^2)^{1/3}*\log(x^{2/3} + x^{1/3}*(-a/b)^{1/3} + (-a/b)^{2/3})/(a*b^2)$

maple [A] time = 0.01, size = 112, normalized size = 0.96

$$-\frac{x^{\frac{1}{3}}}{(bx+a)b} + \frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{3\left(\frac{a}{b}\right)^{\frac{2}{3}}b^2} + \frac{\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{2}{3}}b^2} - \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{6\left(\frac{a}{b}\right)^{\frac{2}{3}}b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/3)/(b*x+a)^2,x)

[Out] $-x^{1/3}/b/(b*x+a)+1/3/b^2/(a/b)^{2/3}*\ln(x^{1/3}+(a/b)^{1/3})-1/6/b^2/(a/b)^{2/3}*\ln(x^{2/3}-(a/b)^{1/3}*x^{1/3}+(a/b)^{2/3})+1/3/b^2/(a/b)^{2/3}*3^{1/2}*\arctan(1/3*3^{1/2}*(2/(a/b)^{1/3}*x^{1/3}-1))$

maxima [A] time = 3.03, size = 120, normalized size = 1.03

$$-\frac{x^{\frac{1}{3}}}{b^2x+ab} + \frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3b^2\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{6b^2\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3b^2\left(\frac{a}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)/(b*x+a)^2,x, algorithm="maxima")

[Out] $-x^{1/3}/(b^2*x+a*b)+1/3*\sqrt{3}*\arctan(1/3*\sqrt{3}*(2*x^{1/3}-(a/b)^{1/3})/(a/b)^{1/3})/(b^2*(a/b)^{2/3})-1/6*\log(x^{2/3}-x^{1/3}*(a/b)^{1/3}+(a/b)^{2/3})/(b^2*(a/b)^{2/3})+1/3*\log(x^{1/3}+(a/b)^{1/3})/(b^2*(a/b)^{2/3})$

mupad [B] time = 0.06, size = 120, normalized size = 1.03

$$\frac{\ln\left(3bx^{1/3}+3a^{1/3}b^{2/3}\right)}{3a^{2/3}b^{4/3}} - \frac{x^{1/3}}{b(a+bx)} + \frac{\ln\left(3bx^{1/3}+\frac{3a^{1/3}b^{2/3}(-1+\sqrt{3}i)}{2}\right)(-1+\sqrt{3}i)}{6a^{2/3}b^{4/3}} - \frac{\ln\left(3bx^{1/3}-\frac{3a^{1/3}b^{2/3}(1+\sqrt{3}i)}{2}\right)}{6a^{2/3}b^{4/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/3)/(a + b*x)^2,x)`

[Out] $\log(3bx^{1/3} + 3a^{1/3}b^{2/3})/(3a^{2/3}b^{4/3}) - x^{1/3}/(b(a + bx)) + (\log(3bx^{1/3} + (3a^{1/3}b^{2/3})(3^{1/2}i - 1))/2)*(3^{1/2}i - 1)/(6a^{2/3}b^{4/3}) - (\log(3bx^{1/3} - (3a^{1/3}b^{2/3})(3^{1/2}i + 1))/2)*(3^{1/2}i + 1)/(6a^{2/3}b^{4/3})$

sympy [A] time = 71.72, size = 607, normalized size = 5.19

$$\left\{ \begin{array}{l} \frac{\infty}{2} \\ x^3 \\ \frac{4}{3x^3} \\ \frac{4a^2}{3} \\ -\frac{3}{2b^2x^{\frac{2}{3}}} \end{array} \right. - \frac{2\sqrt[3]{-1}a^{\frac{4}{3}}\sqrt[3]{\frac{1}{b}}\log\left(-\sqrt[3]{-1}\sqrt[3]{a}\sqrt[3]{\frac{1}{b}}+\sqrt[3]{x}\right)}{6a^2b+6ab^2x} + \frac{\sqrt[3]{-1}a^{\frac{4}{3}}\sqrt[3]{\frac{1}{b}}\log\left(4(-1)^{\frac{2}{3}}a^{\frac{2}{3}}\left(\frac{1}{b}\right)^{\frac{2}{3}}+4\sqrt[3]{-1}\sqrt[3]{a}\sqrt[3]{x}\sqrt[3]{\frac{1}{b}}+4x^{\frac{2}{3}}\right)}{6a^2b+6ab^2x} + \frac{2\sqrt[3]{-1}\sqrt{3}a^{\frac{4}{3}}\sqrt[3]{\frac{1}{b}}\operatorname{atan}\left(\frac{\sqrt{3}}{3}-\frac{2(-1)}{3\sqrt[3]{-1}}\right)}{6a^2b+6ab^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/3)/(b*x+a)**2,x)`

[Out] `Piecewise((zoo/x**(2/3), Eq(a, 0) & Eq(b, 0)), (3*x**(4/3)/(4*a**2), Eq(b, 0)), (-3/(2*b**2*x**(2/3)), Eq(a, 0)), (-2*(-1)**(1/3)*a**(4/3)*(1/b)**(1/3)*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(6*a**2*b + 6*a*b**2*x) + (-1)**(1/3)*a**(4/3)*(1/b)**(1/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(6*a**2*b + 6*a*b**2*x) + 2*(-1)**(1/3)*sqrt(3)*a**(4/3)*(1/b)**(1/3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(6*a**2*b + 6*a*b**2*x) - 2*(-1)**(1/3)*a**(4/3)*(1/b)**(1/3)*log(2)/(6*a**2*b + 6*a*b**2*x) - 2*(-1)**(1/3)*a**(1/3)*b*x*(1/b)**(1/3)*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(6*a**2*b + 6*a*b**2*x) + (-1)**(1/3)*a**(1/3)*b*x*(1/b)**(1/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(6*a**2*b + 6*a*b**2*x) + 2*(-1)**(1/3)*sqrt(3)*a**(1/3)*b*x*(1/b)**(1/3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(6*a**2*b + 6*a*b**2*x) - 2*(-1)**(1/3)*a**(1/3)*b*x*(1/b)**(1/3)*log(2)/(6*a**2*b + 6*a*b**2*x) - 6*a*x**(1/3)/(6*a**2*b + 6*a*b**2*x), True))`

$$3.686 \quad \int \frac{1}{\sqrt[3]{x}(a+bx)^2} dx$$

Optimal. Leaf size=116

$$-\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{4/3}b^{2/3}} + \frac{\log(a+bx)}{6a^{4/3}b^{2/3}} - \frac{\tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{4/3}b^{2/3}} + \frac{x^{2/3}}{a(a+bx)}$$

[Out] $x^{2/3}/a/(b*x+a)-1/2*\ln(a^{1/3}+b^{1/3}*x^{1/3})/a^{4/3}/b^{2/3}+1/6*\ln(b*x+a)/a^{4/3}/b^{2/3}-1/3*\arctan(1/3*(a^{1/3}-2*b^{1/3}*x^{1/3})/a^{1/3}*3^{1/2})/a^{4/3}/b^{2/3}*3^{1/2}$

Rubi [A] time = 0.04, antiderivative size = 116, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 56, 617, 204, 31}

$$-\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{4/3}b^{2/3}} + \frac{\log(a+bx)}{6a^{4/3}b^{2/3}} - \frac{\tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{4/3}b^{2/3}} + \frac{x^{2/3}}{a(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(1/3)*(a + b*x)^2), x]

[Out] $x^{2/3}/(a*(a + b*x)) - \text{ArcTan}[(a^{1/3} - 2*b^{1/3}*x^{1/3})/(\text{Sqrt}[3]*a^{1/3})]/(\text{Sqrt}[3]*a^{4/3}*b^{2/3}) - \text{Log}[a^{1/3} + b^{1/3}*x^{1/3}]/(2*a^{4/3}*b^{2/3}) + \text{Log}[a + b*x]/(6*a^{4/3}*b^{2/3})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])] /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt[3]{x}(a+bx)^2} dx &= \frac{x^{2/3}}{a(a+bx)} + \frac{\int \frac{1}{\sqrt[3]{x}(a+bx)} dx}{3a} \\
&= \frac{x^{2/3}}{a(a+bx)} + \frac{\log(a+bx)}{6a^{4/3}b^{2/3}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{ax}}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{2ab} - \frac{\text{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{a}}{\sqrt[3]{b}} + x} dx, x, \sqrt[3]{x}\right)}{2a^{4/3}b^{2/3}} \\
&= \frac{x^{2/3}}{a(a+bx)} - \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{2a^{4/3}b^{2/3}} + \frac{\log(a+bx)}{6a^{4/3}b^{2/3}} + \frac{\text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}\right)}{a^{4/3}b^{2/3}} \\
&= \frac{x^{2/3}}{a(a+bx)} - \frac{\tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3}a^{4/3}b^{2/3}} - \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{2a^{4/3}b^{2/3}} + \frac{\log(a+bx)}{6a^{4/3}b^{2/3}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.23

$$\frac{3x^{2/3} {}_2F_1\left(\frac{2}{3}, 2; \frac{5}{3}; -\frac{bx}{a}\right)}{2a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(1/3)*(a + b*x)^2),x]

[Out] (3*x^(2/3)*Hypergeometric2F1[2/3, 2, 5/3, -((b*x)/a)])/(2*a^2)

fricas [B] time = 0.51, size = 396, normalized size = 3.41

$$\frac{6ab^2x^{\frac{2}{3}} + 3\sqrt{\frac{1}{3}}(ab^2x + a^2b)\sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} \log\left(\frac{2b^2x - ab + 3\sqrt{\frac{1}{3}}\left(abx^{\frac{1}{3}} + (-ab^2)^{\frac{1}{3}}a + 2(-ab^2)^{\frac{2}{3}}x^{\frac{2}{3}}\right)\sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} - 3(-ab^2)^{\frac{2}{3}}x^{\frac{1}{3}}}{bx+a}}{6(a^2b^3x + a^3b^2)}\right) + (-ab^2)}{6(a^2b^3x + a^3b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3)/(b*x+a)^2,x, algorithm="fricas")

[Out] [1/6*(6*a*b^2*x^(2/3) + 3*sqrt(1/3)*(a*b^2*x + a^2*b)*sqrt((-a*b^2)^(1/3)/a)*log((2*b^2*x - a*b + 3*sqrt(1/3)*(a*b*x^(1/3) + (-a*b^2)^(1/3)*a + 2*(-a*b^2)^(2/3)*x^(2/3))*sqrt((-a*b^2)^(1/3)/a) - 3*(-a*b^2)^(2/3)*x^(1/3))/(b*x + a)) + (-a*b^2)^(2/3)*(b*x + a)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) - 2*(-a*b^2)^(2/3)*(b*x + a)*log(b*x^(1/3) - (-a*b^2)^(1/3)))/(a^2*b^3*x + a^3*b^2), 1/6*(6*a*b^2*x^(2/3) + 6*sqrt(1/3)*(a*b^2*x + a^2*b)*sqrt(-(-a*b^2)^(1/3)/a)*arctan(sqrt(1/3)*(2*b*x^(1/3) + (-a*b^2)^(1/3))*sqrt(-(-a*b^2)^(1/3)/a)/b) + (-a*b^2)^(2/3)*(b*x + a)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) - 2*(-a*b^2)^(2/3)*(b*x + a)*log(b*x^(1/3) - (-a*b^2)^(1/3)))/(a^2*b^3*x + a^3*b^2)]

giac [A] time = 1.11, size = 132, normalized size = 1.14

$$-\frac{\left(-\frac{a}{b}\right)^{\frac{2}{3}} \log\left(x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3a^2} + \frac{x^{\frac{2}{3}}}{(bx+a)a} - \frac{\sqrt{3}(-ab^2)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3a^2b^2} + \frac{(-ab^2)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{6a^2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3)/(b*x+a)^2,x, algorithm="giac")

[Out] -1/3*(-a/b)^(2/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/a^2 + x^(2/3)/((b*x + a)*a) - 1/3*sqrt(3)*(-a*b^2)^(2/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3)))/a^2

3))/(-a/b)^(1/3))/(a^2*b^2) + 1/6*(-a*b^2)^(2/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/(a^2*b^2)

maple [A] time = 0.01, size = 120, normalized size = 1.03

$$\frac{x^{\frac{2}{3}}}{(bx+a)a} + \frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}ab} - \frac{\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}ab} + \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{6\left(\frac{a}{b}\right)^{\frac{1}{3}}ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/3)/(b*x+a)^2,x)

[Out] x^(2/3)/a/(b*x+a)-1/3/a/b/(a/b)^(1/3)*ln(x^(1/3)+(a/b)^(1/3))+1/6/a/b/(a/b)^(1/3)*ln(x^(2/3)-(a/b)^(1/3)*x^(1/3)+(a/b)^(2/3))+1/3/a*3^(1/2)/b/(a/b)^(1/3)*arctan(1/3*3^(1/2)*(2/(a/b)^(1/3)*x^(1/3)-1))

maxima [A] time = 2.96, size = 127, normalized size = 1.09

$$\frac{x^{\frac{2}{3}}}{abx+a^2} + \frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3ab\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{6ab\left(\frac{a}{b}\right)^{\frac{1}{3}}} - \frac{\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3ab\left(\frac{a}{b}\right)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3)/(b*x+a)^2,x, algorithm="maxima")

[Out] x^(2/3)/(a*b*x + a^2) + 1/3*sqrt(3)*arctan(1/3*sqrt(3)*(2*x^(1/3) - (a/b)^(1/3))/(a/b)^(1/3))/(a*b*(a/b)^(1/3)) + 1/6*log(x^(2/3) - x^(1/3)*(a/b)^(1/3) + (a/b)^(2/3))/(a*b*(a/b)^(1/3)) - 1/3*log(x^(1/3) + (a/b)^(1/3))/(a*b*(a/b)^(1/3))

mupad [B] time = 0.36, size = 144, normalized size = 1.24

$$\frac{x^{2/3}}{a(a+bx)} + \frac{(-1)^{1/3} \ln\left(\frac{(-1)^{2/3} b^{2/3}}{a^{5/3}} + \frac{bx^{1/3}}{a^2}\right)}{3a^{4/3}b^{2/3}} - \frac{(-1)^{1/3} \ln\left(\frac{bx^{1/3}}{a^2} + \frac{(-1)^{2/3} b^{2/3} \left(\frac{1}{2} + \frac{\sqrt{3} 1i}{2}\right)^2}{a^{5/3}}\right)}{3a^{4/3}b^{2/3}} \left(\frac{1}{2} + \frac{\sqrt{3} 1i}{2}\right) + \frac{(-1)^{1/3} \ln\left(\frac{bx^{1/3}}{a^2}\right)}{3a^{4/3}b^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(1/3)*(a + b*x)^2), x)`

[Out] $x^{2/3}/(a*(a + b*x)) + ((-1)^{1/3}*\log(((-1)^{2/3}*b^{2/3})/a^{5/3} + (b*x^{1/3})/a^2))/ (3*a^{4/3}*b^{2/3}) - ((-1)^{1/3}*\log((b*x^{1/3})/a^2 + ((-1)^{2/3}*b^{2/3}*((3^{1/2}*1i)/2 + 1/2)^2)/a^{5/3}))*((3^{1/2}*1i)/2 + 1/2))/ (3*a^{4/3}*b^{2/3}) + ((-1)^{1/3}*\log((b*x^{1/3})/a^2 + (9*(-1)^{2/3}*b^{2/3}))*((3^{1/2}*1i)/6 - 1/6)^2)/a^{5/3}))*((3^{1/2}*1i)/6 - 1/6))/(a^{4/3}*b^{2/3})$

sympy [A] time = 79.66, size = 774, normalized size = 6.67

$$\left\{ \begin{array}{l} \frac{\infty}{4} \\ x^3 \\ \frac{3x^2}{2a^2} \\ -\frac{3}{4b^2x^3} \end{array} \right. + \frac{6\sqrt[3]{-1}\sqrt[3]{a}bx^{\frac{2}{3}}\sqrt[3]{\frac{1}{b}}}{6\sqrt[3]{-1}a^{\frac{7}{3}}b^{\frac{3}{3}}\sqrt[3]{\frac{1}{b}} + 6\sqrt[3]{-1}a^{\frac{4}{3}}b^2x^{\frac{3}{3}}\sqrt[3]{\frac{1}{b}}} + \frac{2a \log\left(-\sqrt[3]{-1}\sqrt[3]{a}\sqrt[3]{\frac{1}{b}} + \sqrt[3]{x}\right)}{6\sqrt[3]{-1}a^{\frac{7}{3}}b^{\frac{3}{3}}\sqrt[3]{\frac{1}{b}} + 6\sqrt[3]{-1}a^{\frac{4}{3}}b^2x^{\frac{3}{3}}\sqrt[3]{\frac{1}{b}}} - \frac{a \log\left(4(-1)^{\frac{2}{3}}a^{\frac{2}{3}}\left(\frac{1}{b}\right)^{\frac{2}{3}} + 4\sqrt[3]{-1}\sqrt[3]{a}\sqrt[3]{x}\sqrt[3]{\frac{1}{b}} + 4x^{\frac{2}{3}}\right)}{6\sqrt[3]{-1}a^{\frac{7}{3}}b^{\frac{3}{3}}\sqrt[3]{\frac{1}{b}} + 6\sqrt[3]{-1}a^{\frac{4}{3}}b^2x^{\frac{3}{3}}\sqrt[3]{\frac{1}{b}}} + \frac{2\sqrt{3}a \operatorname{atan}\left(\frac{\sqrt{3}}{3}\right)}{6\sqrt[3]{-1}a^{\frac{7}{3}}b^{\frac{3}{3}}\sqrt[3]{\frac{1}{b}} + 6\sqrt[3]{-1}a^{\frac{4}{3}}b^2x^{\frac{3}{3}}\sqrt[3]{\frac{1}{b}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(1/3)/(b*x+a)**2, x)`

[Out] `Piecewise((zoo/x**(4/3), Eq(a, 0) & Eq(b, 0)), (3*x**(2/3)/(2*a**2), Eq(b, 0)), (-3/(4*b**2*x**(4/3)), Eq(a, 0)), (6*(-1)**(1/3)*a**(1/3)*b*x**(2/3)*(1/b)**(1/3)/(6*(-1)**(1/3)*a**(7/3)*b*(1/b)**(1/3) + 6*(-1)**(1/3)*a**(4/3)*b**2*x*(1/b)**(1/3)) + 2*a*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(6*(-1)**(1/3)*a**(7/3)*b*(1/b)**(1/3) + 6*(-1)**(1/3)*a**(4/3)*b**2*x*(1/b)**(1/3)) - a*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(6*(-1)**(1/3)*a**(7/3)*b*(1/b)**(1/3) + 6*(-1)**(1/3)*a**(4/3)*b**2*x*(1/b)**(1/3)) + 2*sqrt(3)*a*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(6*(-1)**(1/3)*a**(7/3)*b*(1/b)**(1/3) + 6*(-1)**(1/3)*a**(4/3)*b**2*x*(1/b)**(1/3)) + 2*a*log(2)/(6*(-1)**(1/3)*a**(7/3)*b*(1/b)**(1/3) + 6*(-1)**(1/3)*a**(4/3)*b**2*x*(1/b)**(1/3)) + 2*b*x*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(6*(-1)**(1/3)*a**(7/3)*b*(1/b)**(1/3) + 6*(-1)**(1/3)*a**(4/3)*b**2*x*(1/b)**(1/3)) - b*x*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(6*(-1)**(1/3)*a**(7/3)*b*(1/b)**(1/3) + 6*(-1)**(1/3)*a**(4/3)*b**2*x*(1/b)**(1/3))`

```

*b*(1/b)**(1/3) + 6*(-1)**(1/3)*a**(4/3)*b**2*x*(1/b)**(1/3)) + 2*sqrt(3)*b
*x*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)
))/ (6*(-1)**(1/3)*a**(7/3)*b*(1/b)**(1/3) + 6*(-1)**(1/3)*a**(4/3)*b**2*x*(
1/b)**(1/3)) + 2*b*x*log(2)/(6*(-1)**(1/3)*a**(7/3)*b*(1/b)**(1/3) + 6*(-1)
** (1/3)*a**(4/3)*b**2*x*(1/b)**(1/3)), True))

```

$$3.687 \quad \int \frac{1}{x^{2/3}(a+bx)^2} dx$$

Optimal. Leaf size=113

$$\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{a^{5/3} \sqrt[3]{b}} - \frac{\log(a+bx)}{3a^{5/3} \sqrt[3]{b}} - \frac{2 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt{3} \sqrt[3]{a}}\right)}{\sqrt{3} a^{5/3} \sqrt[3]{b}} + \frac{\sqrt[3]{x}}{a(a+bx)}$$

[Out] $x^{(1/3)}/a/(b*x+a)+\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(5/3)}/b^{(1/3)}-1/3*\ln(b*x+a)/a^{(5/3)}/b^{(1/3)}-2/3*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/a^{(5/3)}/b^{(1/3)}*3^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 113, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 58, 617, 204, 31}

$$\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{a^{5/3} \sqrt[3]{b}} - \frac{\log(a+bx)}{3a^{5/3} \sqrt[3]{b}} - \frac{2 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b} \sqrt[3]{x}}{\sqrt{3} \sqrt[3]{a}}\right)}{\sqrt{3} a^{5/3} \sqrt[3]{b}} + \frac{\sqrt[3]{x}}{a(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(2/3)*(a + b*x)^2), x]

[Out] $x^{(1/3)}/(a*(a + b*x)) - (2*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/(\text{Sqrt}[3]*a^{(5/3)}*b^{(1/3)}) + \text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}]/(a^{(5/3)}*b^{(1/3)}) - \text{Log}[a + b*x]/(3*a^{(5/3)}*b^{(1/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 58

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^
2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(
1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)],
x])] /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c]) /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{x^{2/3}(a+bx)^2} dx &= \frac{\sqrt[3]{x}}{a(a+bx)} + \frac{2 \int \frac{1}{x^{2/3}(a+bx)} dx}{3a} \\ &= \frac{\sqrt[3]{x}}{a(a+bx)} - \frac{\log(a+bx)}{3a^{5/3}\sqrt[3]{b}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{ax}}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{a^{4/3}b^{2/3}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{a}}{\sqrt[3]{b}} + x} dx, x, \sqrt[3]{x}\right)}{a^{5/3}\sqrt[3]{b}} \\ &= \frac{\sqrt[3]{x}}{a(a+bx)} + \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{a^{5/3}\sqrt[3]{b}} - \frac{\log(a+bx)}{3a^{5/3}\sqrt[3]{b}} + \frac{2 \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}\right)}{a^{5/3}\sqrt[3]{b}} \\ &= \frac{\sqrt[3]{x}}{a(a+bx)} - \frac{2 \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3}a^{5/3}\sqrt[3]{b}} + \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{a^{5/3}\sqrt[3]{b}} - \frac{\log(a+bx)}{3a^{5/3}\sqrt[3]{b}} \end{aligned}$$

Mathematica [C] time = 0.00, size = 25, normalized size = 0.22

$$\frac{3\sqrt[3]{x} {}_2F_1\left(\frac{1}{3}, 2; \frac{4}{3}; -\frac{bx}{a}\right)}{a^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(2/3)*(a + b*x)^2),x]

[Out] (3*x^(1/3)*Hypergeometric2F1[1/3, 2, 4/3, -((b*x)/a)]/a^2

fricas [B] time = 0.51, size = 387, normalized size = 3.42

$$\frac{3 a^2 b x^{\frac{1}{3}} + 3 \sqrt{\frac{1}{3}} (a b^2 x + a^2 b) \sqrt{-\frac{(a^2 b)^{\frac{1}{3}}}{b}} \log \left(\frac{2 a b x - a^2 + 3 \sqrt{\frac{1}{3}} \left(2 a b x^{\frac{2}{3}} - (a^2 b)^{\frac{1}{3}} a + (a^2 b)^{\frac{2}{3}} x^{\frac{1}{3}} \right) \sqrt{-\frac{(a^2 b)^{\frac{1}{3}}}{b}} - 3 (a^2 b)^{\frac{1}{3}} a x^{\frac{1}{3}}}{b x + a} \right) - (a^2 b)^{\frac{2}{3}} (b x + a)}{3 (a^3 b^2 x + a^4 b)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3)/(b*x+a)^2,x, algorithm="fricas")

[Out] [1/3*(3*a^2*b*x^(1/3) + 3*sqrt(1/3)*(a*b^2*x + a^2*b)*sqrt(-(a^2*b)^(1/3)/b)*log((2*a*b*x - a^2 + 3*sqrt(1/3)*(2*a*b*x^(2/3) - (a^2*b)^(1/3)*a + (a^2*b)^(2/3)*x^(1/3))*sqrt(-(a^2*b)^(1/3)/b) - 3*(a^2*b)^(1/3)*a*x^(1/3))/(b*x + a) - (a^2*b)^(2/3)*(b*x + a)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) + 2*(a^2*b)^(2/3)*(b*x + a)*log(a*b*x^(1/3) + (a^2*b)^(2/3)))/(a^3*b^2*x + a^4*b), 1/3*(3*a^2*b*x^(1/3) + 6*sqrt(1/3)*(a*b^2*x + a^2*b)*sqrt((a^2*b)^(1/3)/b)*arctan(-sqrt(1/3)*((a^2*b)^(1/3)*a - 2*(a^2*b)^(2/3)*x^(1/3))*sqrt((a^2*b)^(1/3)/b)/a^2 - (a^2*b)^(2/3)*(b*x + a)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) + 2*(a^2*b)^(2/3)*(b*x + a)*log(a*b*x^(1/3) + (a^2*b)^(2/3)))/(a^3*b^2*x + a^4*b)]

giac [A] time = 1.04, size = 132, normalized size = 1.17

$$-\frac{2 \left(-\frac{a}{b}\right)^{\frac{1}{3}} \log \left(\left| x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}} \right| \right)}{3 a^2} + \frac{2 \sqrt{3} (-a b^2)^{\frac{1}{3}} \arctan \left(\frac{\sqrt{3} \left(2 x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}} \right)}{3 \left(-\frac{a}{b}\right)^{\frac{1}{3}}} \right)}{3 a^2 b} + \frac{x^{\frac{1}{3}}}{(b x + a) a} + \frac{(-a b^2)^{\frac{1}{3}} \log \left(x^{\frac{2}{3}} + x^{\frac{1}{3}} \left(-\frac{a}{b}\right)^{\frac{1}{3}} \right)}{3 a^2 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3)/(b*x+a)^2,x, algorithm="giac")

[Out] -2/3*(-a/b)^(1/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/a^2 + 2/3*sqrt(3)*(-a*b^2)^(1/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/(a^2*b

) + $x^{1/3}/((b*x + a)*a) + 1/3*(-a*b^2)^{1/3}*\log(x^{2/3} + x^{1/3}*(-a/b)^{1/3} + (-a/b)^{2/3})/(a^2*b)$

maple [A] time = 0.01, size = 120, normalized size = 1.06

$$\frac{x^{\frac{1}{3}}}{(bx+a)a} + \frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{3\left(\frac{a}{b}\right)^{\frac{2}{3}}ab} + \frac{2\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{2}{3}}ab} - \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{2}{3}}ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^(2/3)/(b*x+a)^2,x)`

[Out] $x^{1/3}/a/(b*x+a)+2/3/a/b/(a/b)^{2/3}*\ln(x^{1/3}+(a/b)^{1/3})-1/3/a/b/(a/b)^{2/3}*\ln(x^{2/3}-(a/b)^{1/3}*x^{1/3}+(a/b)^{2/3})+2/3/a/b/(a/b)^{2/3}*3^{1/2}*\arctan(1/3*3^{1/2}*(2/(a/b)^{1/3}*x^{1/3}-1))$

maxima [A] time = 3.01, size = 127, normalized size = 1.12

$$\frac{x^{\frac{1}{3}}}{abx+a^2} + \frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3ab\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{3ab\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{2\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3ab\left(\frac{a}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^(2/3)/(b*x+a)^2,x, algorithm="maxima")`

[Out] $x^{1/3}/(a*b*x + a^2) + 2/3*\sqrt{3}*\arctan(1/3*\sqrt{3}*(2*x^{1/3} - (a/b)^{1/3})/(a/b)^{1/3})/(a*b*(a/b)^{2/3}) - 1/3*\log(x^{2/3} - x^{1/3}*(a/b)^{1/3} + (a/b)^{2/3})/(a*b*(a/b)^{2/3}) + 2/3*\log(x^{1/3} + (a/b)^{1/3})/(a*b*(a/b)^{2/3})$

mupad [B] time = 0.22, size = 134, normalized size = 1.19

$$\frac{2\ln\left(\frac{6b^5/3}{a^{2/3}} + \frac{6b^2x^{1/3}}{a}\right)}{3a^{5/3}b^{1/3}} + \frac{x^{1/3}}{a(a+bx)} + \frac{\ln\left(\frac{6b^2x^{1/3}}{a} + \frac{3b^{5/3}(-1+\sqrt{3}1i)}{a^{2/3}}\right)(-1+\sqrt{3}1i)}{3a^{5/3}b^{1/3}} - \frac{\ln\left(\frac{6b^2x^{1/3}}{a} - \frac{3b^{5/3}(1+\sqrt{3}1i)}{a^{2/3}}\right)(1+\sqrt{3}1i)}{3a^{5/3}b^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^(2/3)*(a + b*x)^2), x)`

[Out] $(2*\log((6*b^(5/3))/a^(2/3) + (6*b^2*x^(1/3))/a))/(3*a^(5/3)*b^(1/3)) + x^(1/3)/(a*(a + b*x)) + (\log((6*b^2*x^(1/3))/a + (3*b^(5/3)*(3^(1/2)*1i - 1))/a^(2/3))*(3^(1/2)*1i - 1))/(3*a^(5/3)*b^(1/3)) - (\log((6*b^2*x^(1/3))/a - (3*b^(5/3)*(3^(1/2)*1i + 1))/a^(2/3))*(3^(1/2)*1i + 1))/(3*a^(5/3)*b^(1/3))$

sympy [A] time = 115.98, size = 590, normalized size = 5.22

$$\left\{ \begin{array}{l} \frac{\infty}{5} \\ x^3 \\ \frac{3\sqrt[3]{x}}{a^2} \\ \frac{3}{5b^2x^3} \end{array} \right. - \frac{2\sqrt[3]{-1}a^{\frac{4}{3}}\sqrt[3]{\frac{1}{b}}\log\left(-\sqrt[3]{-1}\sqrt[3]{a}\sqrt[3]{\frac{1}{b}}+\sqrt[3]{x}\right)}{3a^3+3a^2bx} + \frac{\sqrt[3]{-1}a^{\frac{4}{3}}\sqrt[3]{\frac{1}{b}}\log\left(4(-1)^{\frac{2}{3}}a^{\frac{2}{3}}\left(\frac{1}{b}\right)^{\frac{2}{3}}+4\sqrt[3]{-1}\sqrt[3]{a}\sqrt[3]{x}\sqrt[3]{\frac{1}{b}}+4x^{\frac{2}{3}}\right)}{3a^3+3a^2bx} + \frac{2\sqrt[3]{-1}\sqrt{3}a^{\frac{4}{3}}\sqrt[3]{\frac{1}{b}}\operatorname{atan}\left(\frac{\sqrt{3}}{3}-\frac{2(-1)^{\frac{2}{3}}}{3\sqrt[3]{a}}\right)}{3a^3+3a^2bx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**(2/3)/(b*x+a)**2,x)`

[Out] `Piecewise((zoo/x**(5/3), Eq(a, 0) & Eq(b, 0)), (3*x**(1/3)/a**2, Eq(b, 0)), (-3/(5*b**2*x**(5/3)), Eq(a, 0)), (-2*(-1)**(1/3)*a**(4/3)*(1/b)**(1/3)*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x**(1/3))/(3*a**3 + 3*a**2*b*x) + (-1)**(1/3)*a**(4/3)*(1/b)**(1/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(3*a**3 + 3*a**2*b*x) + 2*(-1)**(1/3)*sqrt(3)*a**(4/3)*(1/b)**(1/3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(3*a**3 + 3*a**2*b*x) - 2*(-1)**(1/3)*a**(4/3)*(1/b)**(1/3)*log(2)/(3*a**3 + 3*a**2*b*x) - 2*(-1)**(1/3)*a**(1/3)*b*x*(1/b)**(1/3)*log(-(-1)**(1/3)*a**(1/3)*(1/b)**(1/3) + x*(1/3))/(3*a**3 + 3*a**2*b*x) + (-1)**(1/3)*a**(1/3)*b*x*(1/b)**(1/3)*log(4*(-1)**(2/3)*a**(2/3)*(1/b)**(2/3) + 4*(-1)**(1/3)*a**(1/3)*x**(1/3)*(1/b)**(1/3) + 4*x**(2/3))/(3*a**3 + 3*a**2*b*x) + 2*(-1)**(1/3)*sqrt(3)*a**(1/3)*b*x*(1/b)**(1/3)*atan(sqrt(3)/3 - 2*(-1)**(2/3)*sqrt(3)*x**(1/3)/(3*a**(1/3)*(1/b)**(1/3)))/(3*a**3 + 3*a**2*b*x) - 2*(-1)**(1/3)*a**(1/3)*b*x*(1/b)**(1/3)*log(2)/(3*a**3 + 3*a**2*b*x) + 3*a*x**(1/3)/(3*a**3 + 3*a**2*b*x), True))`

$$3.688 \quad \int \frac{1}{x^{4/3}(a+bx)^2} dx$$

Optimal. Leaf size=124

$$\frac{2\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{a^{7/3}} - \frac{2\sqrt[3]{b} \log(a+bx)}{3a^{7/3}} + \frac{4\sqrt[3]{b} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{7/3}} - \frac{4}{a^2\sqrt[3]{x}} + \frac{1}{a\sqrt[3]{x}(a+bx)}$$

[Out] $-4/a^2/x^{(1/3)}+1/a/x^{(1/3)}/(b*x+a)+2*b^{(1/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(7/3)}-2/3*b^{(1/3)}*\ln(b*x+a)/a^{(7/3)}+4/3*b^{(1/3)}*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/a^{(7/3)}*3^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 124, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 56, 617, 204, 31}

$$\frac{2\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{a^{7/3}} - \frac{2\sqrt[3]{b} \log(a+bx)}{3a^{7/3}} + \frac{4\sqrt[3]{b} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{7/3}} - \frac{4}{a^2\sqrt[3]{x}} + \frac{1}{a\sqrt[3]{x}(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(4/3)*(a + b*x)^2), x]

[Out] $-4/(a^2*x^{(1/3)}) + 1/(a*x^{(1/3)}*(a + b*x)) + (4*b^{(1/3)}*ArcTan[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(Sqrt[3]*a^{(1/3)})])/(Sqrt[3]*a^{(7/3)}) + (2*b^{(1/3)}*Log[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/a^{(7/3)} - (2*b^{(1/3)}*Log[a + b*x])/(3*a^{(7/3)})$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x]) /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{4/3}(a+bx)^2} dx &= \frac{1}{a\sqrt[3]{x}(a+bx)} + \frac{4 \int \frac{1}{x^{4/3}(a+bx)} dx}{3a} \\
&= -\frac{4}{a^2\sqrt[3]{x}} + \frac{1}{a\sqrt[3]{x}(a+bx)} - \frac{(4b) \int \frac{1}{\sqrt[3]{x}(a+bx)} dx}{3a^2} \\
&= -\frac{4}{a^2\sqrt[3]{x}} + \frac{1}{a\sqrt[3]{x}(a+bx)} - \frac{2\sqrt[3]{b} \log(a+bx)}{3a^{7/3}} - \frac{2 \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{a^2} + \frac{(2\sqrt[3]{b})}{a^2} \\
&= -\frac{4}{a^2\sqrt[3]{x}} + \frac{1}{a\sqrt[3]{x}(a+bx)} + \frac{2\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{a^{7/3}} - \frac{2\sqrt[3]{b} \log(a+bx)}{3a^{7/3}} - \frac{(4\sqrt[3]{b}) \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{a^2} \\
&= -\frac{4}{a^2\sqrt[3]{x}} + \frac{1}{a\sqrt[3]{x}(a+bx)} + \frac{4\sqrt[3]{b} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3}a^{7/3}} + \frac{2\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{a^{7/3}} - \frac{2\sqrt[3]{b} \log(a+bx)}{3a^{7/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 25, normalized size = 0.20

$$\frac{{}_3F_1\left(-\frac{1}{3}, 2, \frac{2}{3}; -\frac{bx}{a}\right)}{a^2 \sqrt[3]{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(4/3)*(a + b*x)^2), x]

[Out] (-3*Hypergeometric2F1[-1/3, 2, 2/3, -((b*x)/a)])/(a^2*x^(1/3))

fricas [A] time = 0.49, size = 156, normalized size = 1.26

$$\frac{4\sqrt{3}(bx^2 + ax)\left(\frac{b}{a}\right)^{\frac{1}{3}} \arctan\left(\frac{2}{3}\sqrt{3}x^{\frac{1}{3}}\left(\frac{b}{a}\right)^{\frac{1}{3}} - \frac{1}{3}\sqrt{3}\right) + 2(bx^2 + ax)\left(\frac{b}{a}\right)^{\frac{1}{3}} \log\left(-ax^{\frac{1}{3}}\left(\frac{b}{a}\right)^{\frac{2}{3}} + bx^{\frac{2}{3}} + a\left(\frac{b}{a}\right)^{\frac{1}{3}}\right) - 4}{3(a^2bx^2 + a^3x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3)/(b*x+a)^2,x, algorithm="fricas")

[Out] -1/3*(4*sqrt(3)*(b*x^2 + a*x)*(b/a)^(1/3)*arctan(2/3*sqrt(3)*x^(1/3)*(b/a)^(1/3) - 1/3*sqrt(3)) + 2*(b*x^2 + a*x)*(b/a)^(1/3)*log(-a*x^(1/3)*(b/a)^(2/3) + b*x^(2/3) + a*(b/a)^(1/3)) - 4*(b*x^2 + a*x)*(b/a)^(1/3)*log(a*(b/a)^(2/3) + b*x^(1/3)) + 3*(4*b*x + 3*a)*x^(2/3))/(a^2*b*x^2 + a^3*x)

giac [A] time = 0.97, size = 145, normalized size = 1.17

$$\frac{4b\left(-\frac{a}{b}\right)^{\frac{2}{3}} \log\left(x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3a^3} + \frac{4\sqrt{3}(-ab^2)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3a^3b} - \frac{4bx + 3a}{\left(bx^{\frac{4}{3}} + ax^{\frac{1}{3}}\right)a^2} - \frac{2(-ab^2)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\right)}{3a^3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3)/(b*x+a)^2,x, algorithm="giac")

[Out] 4/3*b*(-a/b)^(2/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/a^3 + 4/3*sqrt(3)*(-a*b^2)^(2/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/a^3*b - (4*b*x + 3*a)/((b*x^(4/3) + a*x^(1/3))*a^2) - 2/3*(-a*b^2)^(2/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/(a^3*b)

maple [A] time = 0.01, size = 121, normalized size = 0.98

$$\frac{bx^{\frac{2}{3}}}{(bx+a)a^2} - \frac{4\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}a^2} + \frac{4 \ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}a^2} - \frac{2 \ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}a^2} - \frac{3}{a^2x^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(4/3)/(b*x+a)^2,x)

[Out] -3/a^2/x^(1/3)-1/a^2*b*x^(2/3)/(b*x+a)+4/3/a^2/(a/b)^(1/3)*ln(x^(1/3)+(a/b)^(1/3))-2/3/a^2/(a/b)^(1/3)*ln(x^(2/3)-(a/b)^(1/3)*x^(1/3)+(a/b)^(2/3))-4/3/a^2*3^(1/2)/(a/b)^(1/3)*arctan(1/3*3^(1/2)*(2/(a/b)^(1/3)*x^(1/3)-1))

maxima [A] time = 3.04, size = 132, normalized size = 1.06

$$\frac{4bx+3a}{a^2bx^{\frac{4}{3}}+a^3x^{\frac{1}{3}}} - \frac{4\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3a^2\left(\frac{a}{b}\right)^{\frac{1}{3}}} - \frac{2 \log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{3a^2\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{4 \log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3a^2\left(\frac{a}{b}\right)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3)/(b*x+a)^2,x, algorithm="maxima")

[Out] -(4*b*x + 3*a)/(a^2*b*x^(4/3) + a^3*x^(1/3)) - 4/3*sqrt(3)*arctan(1/3*sqrt(3)*(2*x^(1/3) - (a/b)^(1/3))/(a/b)^(1/3))/(a^2*(a/b)^(1/3)) - 2/3*log(x^(2/3) - x^(1/3)*(a/b)^(1/3) + (a/b)^(2/3))/(a^2*(a/b)^(1/3)) + 4/3*log(x^(1/3) + (a/b)^(1/3))/(a^2*(a/b)^(1/3))

mupad [B] time = 0.15, size = 151, normalized size = 1.22

$$\frac{4b^{1/3} \ln\left(16a^{7/3}b^{8/3} + 16a^2b^3x^{1/3}\right)}{3a^{7/3}} - \frac{\frac{3}{a} + \frac{4bx}{a^2}}{ax^{1/3} + bx^{4/3}} - \frac{4b^{1/3} \ln\left(16a^{7/3}b^{8/3}\left(\frac{1}{2} + \frac{\sqrt{3} \operatorname{li}}{2}\right)^2 + 16a^2b^3x^{1/3}\right)}{3a^{7/3}} \left(\frac{1}{2} + \frac{\sqrt{3} \operatorname{li}}{2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(4/3)*(a + b*x)^2),x)

```
[Out] (4*b^(1/3)*log(16*a^(7/3)*b^(8/3) + 16*a^2*b^3*x^(1/3)))/(3*a^(7/3)) - (3/a
+ (4*b*x)/a^2)/(a*x^(1/3) + b*x^(4/3)) - (4*b^(1/3)*log(16*a^(7/3)*b^(8/3)
*((3^(1/2)*1i)/2 + 1/2)^2 + 16*a^2*b^3*x^(1/3))*((3^(1/2)*1i)/2 + 1/2))/(3*
a^(7/3)) + (b^(1/3)*log(9*a^(7/3)*b^(8/3)*((3^(1/2)*2i)/3 - 2/3)^2 + 16*a^2
*b^3*x^(1/3))*((3^(1/2)*2i)/3 - 2/3))/a^(7/3)
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**(4/3)/(b*x+a)**2,x)
```

```
[Out] Timed out
```

$$3.689 \quad \int \frac{1}{x^{5/3}(a+bx)^2} dx$$

Optimal. Leaf size=128

$$-\frac{5b^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{8/3}} + \frac{5b^{2/3} \log(a+bx)}{6a^{8/3}} + \frac{5b^{2/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{8/3}} - \frac{5}{2a^2x^{2/3}} + \frac{1}{ax^{2/3}(a+bx)}$$

[Out] $-5/2/a^{2/x^{(2/3)}+1/a/x^{(2/3)/(b*x+a)-5/2*b^{(2/3)*ln(a^{(1/3)}+b^{(1/3)*x^{(1/3)}})/a^{(8/3)}+5/6*b^{(2/3)*ln(b*x+a)/a^{(8/3)}+5/3*b^{(2/3)*arctan(1/3*(a^{(1/3)}-2*b^{(1/3)*x^{(1/3)}})/a^{(1/3)*3^{(1/2)}}/a^{(8/3)*3^{(1/2)}}$

Rubi [A] time = 0.05, antiderivative size = 128, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 58, 617, 204, 31}

$$-\frac{5b^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{8/3}} + \frac{5b^{2/3} \log(a+bx)}{6a^{8/3}} + \frac{5b^{2/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{\sqrt{3}a^{8/3}} - \frac{5}{2a^2x^{2/3}} + \frac{1}{ax^{2/3}(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/3)*(a + b*x)^2), x]

[Out] $-5/(2*a^2*x^{(2/3)} + 1/(a*x^{(2/3)*(a + b*x)}) + (5*b^{(2/3)*ArcTan[(a^{(1/3)} - 2*b^{(1/3)*x^{(1/3)}})/(Sqrt[3]*a^{(1/3)})])/(Sqrt[3]*a^{(8/3)}) - (5*b^{(2/3)*Log[a^{(1/3)} + b^{(1/3)*x^{(1/3)}}]}/(2*a^{(8/3)}) + (5*b^{(2/3)*Log[a + b*x]}/(6*a^{(8/3)}))$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 58

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^
2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(
1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)],
x])] /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c]) /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{5/3}(a+bx)^2} dx &= \frac{1}{ax^{2/3}(a+bx)} + \frac{5 \int \frac{1}{x^{5/3}(a+bx)} dx}{3a} \\
&= -\frac{5}{2a^2x^{2/3}} + \frac{1}{ax^{2/3}(a+bx)} - \frac{(5b) \int \frac{1}{x^{2/3}(a+bx)} dx}{3a^2} \\
&= -\frac{5}{2a^2x^{2/3}} + \frac{1}{ax^{2/3}(a+bx)} + \frac{5b^{2/3} \log(a+bx)}{6a^{8/3}} - \frac{(5\sqrt[3]{b}) \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{2a^{7/3}} \\
&= -\frac{5}{2a^2x^{2/3}} + \frac{1}{ax^{2/3}(a+bx)} - \frac{5b^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{8/3}} + \frac{5b^{2/3} \log(a+bx)}{6a^{8/3}} - \frac{(5b^{2/3}) \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{2a^{7/3}} \\
&= -\frac{5}{2a^2x^{2/3}} + \frac{1}{ax^{2/3}(a+bx)} + \frac{5b^{2/3} \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{\sqrt{3}a^{8/3}} - \frac{5b^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{2a^{8/3}} + \frac{5b^{2/3} \log(a+bx)}{6a^{8/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 27, normalized size = 0.21

$$\frac{{}_3F_1\left(-\frac{2}{3}, 2; \frac{1}{3}; -\frac{bx}{a}\right)}{2a^2x^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/3)*(a + b*x)^2), x]

[Out] (-3*Hypergeometric2F1[-2/3, 2, 1/3, -(b*x)/a])/(2*a^2*x^(2/3))

fricas [B] time = 0.50, size = 189, normalized size = 1.48

$$\frac{10\sqrt{3}(bx^2 + ax)\left(-\frac{b^2}{a^2}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}ax^{\frac{1}{3}}\left(-\frac{b^2}{a^2}\right)^{\frac{2}{3}} - \sqrt{3}b}{3b}\right) - 5(bx^2 + ax)\left(-\frac{b^2}{a^2}\right)^{\frac{1}{3}} \log\left(b^2x^{\frac{2}{3}} + abx^{\frac{1}{3}}\left(-\frac{b^2}{a^2}\right)^{\frac{1}{3}} + a^2\left(-\frac{b^2}{a^2}\right)^{\frac{2}{3}}\right)}{6(a^2bx^2 + a^3x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/3)/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/6*(10*sqrt(3)*(b*x^2 + a*x)*(-b^2/a^2)^(1/3)*arctan(1/3*(2*sqrt(3)*a*x^(1/3)*(-b^2/a^2)^(2/3) - sqrt(3)*b)/b) - 5*(b*x^2 + a*x)*(-b^2/a^2)^(1/3)*log(b^2*x^(2/3) + a*b*x^(1/3)*(-b^2/a^2)^(1/3) + a^2*(-b^2/a^2)^(2/3)) + 10*(b*x^2 + a*x)*(-b^2/a^2)^(1/3)*log(b*x^(1/3) - a*(-b^2/a^2)^(1/3)) - 3*(5*b*x + 3*a)*x^(1/3))/(a^2*b*x^2 + a^3*x)

giac [A] time = 1.01, size = 137, normalized size = 1.07

$$\frac{5b\left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{3a^3} - \frac{5\sqrt{3}(-ab^2)^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3a^3} - \frac{bx^{\frac{1}{3}}}{(bx+a)a^2} - \frac{5(-ab^2)^{\frac{1}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{6a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/3)/(b*x+a)^2,x, algorithm="giac")

[Out] 5/3*b*(-a/b)^(1/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/a^3 - 5/3*sqrt(3)*(-a*b^2)^(1/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/a^3 - b*x^(1/3)/((b*x + a)*a^2) - 5/6*(-a*b^2)^(1/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/a^3 - 3/2/(a^2*x^(2/3))

maple [A] time = 0.01, size = 121, normalized size = 0.95

$$\frac{bx^{\frac{1}{3}}}{(bx+a)a^2} - \frac{5\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{3\left(\frac{a}{b}\right)^{\frac{2}{3}}a^2} - \frac{5\ln\left(x^{\frac{1}{3}}+\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{2}{3}}a^2} + \frac{5\ln\left(x^{\frac{2}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}}+\left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{6\left(\frac{a}{b}\right)^{\frac{2}{3}}a^2} - \frac{3}{2a^2x^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(5/3)/(b*x+a)^2,x)

[Out] $-3/2/a^2/x^{2/3}-1/a^2*b*x^{1/3}/(b*x+a)-5/3/a^2/(a/b)^{2/3}*\ln(x^{1/3}+(a/b)^{1/3})+5/6/a^2/(a/b)^{2/3}*\ln(x^{2/3}-(a/b)^{1/3}*x^{1/3}+(a/b)^{2/3})-5/3/a^2/(a/b)^{2/3}*3^{1/2}*arctan(1/3*3^{1/2}*(2/(a/b)^{1/3}*x^{1/3}-1))$

maxima [A] time = 2.94, size = 132, normalized size = 1.03

$$\frac{5bx+3a}{2\left(a^2bx^{\frac{5}{3}}+a^3x^{\frac{2}{3}}\right)} - \frac{5\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}}-\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{3a^2\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{5\log\left(x^{\frac{2}{3}}-x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}}+\left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{6a^2\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{5\log\left(x^{\frac{1}{3}}+\left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3a^2\left(\frac{a}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/3)/(b*x+a)^2,x, algorithm="maxima")

[Out] $-1/2*(5*b*x+3*a)/(a^2*b*x^{5/3}+a^3*x^{2/3})-5/3*sqrt(3)*arctan(1/3*sqrt(3)*(2*x^{1/3}-(a/b)^{1/3})/(a/b)^{1/3})/(a^2*(a/b)^{2/3})+5/6*log(x^{2/3}-x^{1/3}*(a/b)^{1/3}+(a/b)^{2/3})/(a^2*(a/b)^{2/3})-5/3*log(x^{1/3}+(a/b)^{1/3})/(a^2*(a/b)^{2/3})$

mupad [B] time = 0.17, size = 166, normalized size = 1.30

$$\frac{5(-1)^{1/3}b^{2/3}\ln\left(15(-1)^{1/3}a^{13/3}b^{8/3}-15a^4b^3x^{1/3}\right)}{3a^{8/3}} - \frac{\frac{3}{2a}+\frac{5bx}{2a^2}}{ax^{2/3}+bx^{5/3}} + \frac{5(-1)^{1/3}b^{2/3}\ln\left(15a^4b^3x^{1/3}-15(-1)^{1/3}a^{13/3}b^{8/3}\right)}{3a^{8/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(5/3)*(a+b*x)^2),x)

```
[Out] (5*(-1)^(1/3)*b^(2/3)*log(15*(-1)^(1/3)*a^(13/3)*b^(8/3) - 15*a^4*b^3*x^(1/3)))/(3*a^(8/3)) - (3/(2*a) + (5*b*x)/(2*a^2))/(a*x^(2/3) + b*x^(5/3)) + (5*(-1)^(1/3)*b^(2/3)*log(15*a^4*b^3*x^(1/3) - 15*(-1)^(1/3)*a^(13/3)*b^(8/3)*((3^(1/2)*1i)/2 - 1/2))*((3^(1/2)*1i)/2 - 1/2))/(3*a^(8/3)) - (5*(-1)^(1/3)*b^(2/3)*log(15*a^4*b^3*x^(1/3) + 15*(-1)^(1/3)*a^(13/3)*b^(8/3)*((3^(1/2)*1i)/2 + 1/2))*((3^(1/2)*1i)/2 + 1/2))/(3*a^(8/3))
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**(5/3)/(b*x+a)**2,x)
```

```
[Out] Timed out
```

$$3.690 \quad \int \frac{x^{5/3}}{(a+bx)^3} dx$$

Optimal. Leaf size=140

$$-\frac{5 \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{6\sqrt[3]{a} b^{8/3}} + \frac{5 \log(a+bx)}{18\sqrt[3]{a} b^{8/3}} - \frac{5 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}\sqrt[3]{a} b^{8/3}} - \frac{5x^{2/3}}{6b^2(a+bx)} - \frac{x^{5/3}}{2b(a+bx)^2}$$

[Out] $-1/2*x^{(5/3)}/b/(b*x+a)^2-5/6*x^{(2/3)}/b^2/(b*x+a)-5/6*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(1/3)}/b^{(8/3)}+5/18*\ln(b*x+a)/a^{(1/3)}/b^{(8/3)}-5/9*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/a^{(1/3)}/b^{(8/3)}*3^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 140, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {47, 56, 617, 204, 31}

$$-\frac{5x^{2/3}}{6b^2(a+bx)} - \frac{5 \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{6\sqrt[3]{a} b^{8/3}} + \frac{5 \log(a+bx)}{18\sqrt[3]{a} b^{8/3}} - \frac{5 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}\sqrt[3]{a} b^{8/3}} - \frac{x^{5/3}}{2b(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[x^(5/3)/(a + b*x)^3, x]

[Out] $-x^{(5/3)}/(2*b*(a + b*x)^2) - (5*x^{(2/3)})/(6*b^2*(a + b*x)) - (5*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/(3*\text{Sqrt}[3]*a^{(1/3)}*b^{(8/3)}) - (5*\text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(6*a^{(1/3)}*b^{(8/3)}) + (5*\text{Log}[a + b*x])/ (18*a^{(1/3)}*b^{(8/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])] /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{5/3}}{(a+bx)^3} dx &= -\frac{x^{5/3}}{2b(a+bx)^2} + \frac{5 \int \frac{x^{2/3}}{(a+bx)^2} dx}{6b} \\
&= -\frac{x^{5/3}}{2b(a+bx)^2} - \frac{5x^{2/3}}{6b^2(a+bx)} + \frac{5 \int \frac{1}{\sqrt[3]{x}(a+bx)} dx}{9b^2} \\
&= -\frac{x^{5/3}}{2b(a+bx)^2} - \frac{5x^{2/3}}{6b^2(a+bx)} + \frac{5 \log(a+bx)}{18\sqrt[3]{a}b^{8/3}} + \frac{5 \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{6b^3} - \frac{5 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{x}\right)}{3\sqrt[3]{a}b^{8/3}} \\
&= -\frac{x^{5/3}}{2b(a+bx)^2} - \frac{5x^{2/3}}{6b^2(a+bx)} - \frac{5 \log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{6\sqrt[3]{a}b^{8/3}} + \frac{5 \log(a+bx)}{18\sqrt[3]{a}b^{8/3}} + \frac{5 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{x}\right)}{3\sqrt[3]{a}b^{8/3}} \\
&= -\frac{x^{5/3}}{2b(a+bx)^2} - \frac{5x^{2/3}}{6b^2(a+bx)} - \frac{5 \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{3\sqrt{3}\sqrt[3]{a}b^{8/3}} - \frac{5 \log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{6\sqrt[3]{a}b^{8/3}} + \frac{5 \log(a+bx)}{18\sqrt[3]{a}b^{8/3}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.19

$$\frac{3x^{8/3} {}_2F_1\left(\frac{8}{3}, 3; \frac{11}{3}; -\frac{bx}{a}\right)}{8a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/3)/(a + b*x)^3,x]

[Out] (3*x^(8/3)*Hypergeometric2F1[8/3, 3, 11/3, -((b*x)/a)])/(8*a^3)

fricas [B] time = 0.50, size = 506, normalized size = 3.61

$$\left[15 \sqrt{\frac{1}{3}} (ab^3x^2 + 2a^2b^2x + a^3b) \sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} \log \left(\frac{2b^2x - ab + 3 \sqrt{\frac{1}{3}} \left(abx^{\frac{1}{3}} + (-ab^2)^{\frac{1}{3}} a + 2(-ab^2)^{\frac{2}{3}} x^{\frac{2}{3}} \right) \sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} - 3(-ab^2)^{\frac{2}{3}} x^{\frac{1}{3}}}{bx+a} \right) + 5(b \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)/(b*x+a)^3,x, algorithm="fricas")

[Out] [1/18*(15*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt((-a*b^2)^(1/3)/a)*log((2*b^2*x - a*b + 3*sqrt(1/3)*(a*b*x^(1/3) + (-a*b^2)^(1/3)*a + 2*(-a*b^2)^(2/3)*x^(2/3))*sqrt((-a*b^2)^(1/3)/a) - 3*(-a*b^2)^(2/3)*x^(1/3))/(b*x + a)) + 5*(b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) - 10*(b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b*x^(1/3) - (-a*b^2)^(1/3)) - 3*(8*a*b^3*x + 5*a^2*b^2)*x^(2/3))/(a*b^6*x^2 + 2*a^2*b^5*x + a^3*b^4), 1/18*(30*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt(-(-a*b^2)^(1/3)/a)*arctan(sqrt(1/3)*(2*b*x^(1/3) + (-a*b^2)^(1/3))*sqrt(-(-a*b^2)^(1/3)/a)/b) + 5*(b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) - 10*(b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b*x^(1/3) - (-a*b^2)^(1/3)) - 3*(8*a*b^3*x + 5*a^2*b^2)*x^(2/3))/(a*b^6*x^2 + 2*a^2*b^5*x + a^3*b^4)]

giac [A] time = 1.06, size = 146, normalized size = 1.04

$$\frac{5 \left(-\frac{a}{b}\right)^{\frac{2}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{9ab^2} - \frac{5\sqrt{3}(-ab^2)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9ab^4} - \frac{8bx^{\frac{5}{3}} + 5ax^{\frac{2}{3}}}{6(bx+a)^2b^2} + \frac{5(-ab^2)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\right)}{18ab^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)/(b*x+a)^3,x, algorithm="giac")

[Out] $-5/9*(-a/b)^{(2/3)}*\log(\text{abs}(x^{(1/3)} - (-a/b)^{(1/3)}))/(a*b^2) - 5/9*\text{sqrt}(3)*(-a*b^2)^{(2/3)}*\arctan(1/3*\text{sqrt}(3)*(2*x^{(1/3)} + (-a/b)^{(1/3)})/(-a/b)^{(1/3)})/(a*b^4) - 1/6*(8*b*x^{(5/3)} + 5*a*x^{(2/3)})/((b*x + a)^2*b^2) + 5/18*(-a*b^2)^{(2/3)}*\log(x^{(2/3)} + x^{(1/3)}*(-a/b)^{(1/3)} + (-a/b)^{(2/3)})/(a*b^4)$

maple [A] time = 0.01, size = 124, normalized size = 0.89

$$\frac{5\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{9\left(\frac{a}{b}\right)^{\frac{1}{3}}b^3} - \frac{5\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9\left(\frac{a}{b}\right)^{\frac{1}{3}}b^3} + \frac{5\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{18\left(\frac{a}{b}\right)^{\frac{1}{3}}b^3} + \frac{-\frac{4x^{\frac{5}{3}}}{3b} - \frac{5ax^{\frac{2}{3}}}{6b^2}}{(bx+a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/3)/(b*x+a)^3,x)

[Out] $3*(-4/9/b*x^{(5/3)}-5/18*a/b^2*x^{(2/3)})/(b*x+a)^2-5/9/b^3/(a/b)^{(1/3)}*\ln(x^{(1/3)}+(a/b)^{(1/3)})+5/18/b^3/(a/b)^{(1/3)}*\ln(x^{(2/3)}-(a/b)^{(1/3)}*x^{(1/3)}+(a/b)^{(2/3)})+5/9/b^3*3^{(1/2)}/(a/b)^{(1/3)}*\arctan(1/3*3^{(1/2)}*(2/(a/b)^{(1/3)}*x^{(1/3)}-1))$

maxima [A] time = 2.95, size = 143, normalized size = 1.02

$$\frac{8bx^{\frac{5}{3}} + 5ax^{\frac{2}{3}}}{6(b^4x^2 + 2ab^3x + a^2b^2)} + \frac{5\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9b^3\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{5\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{18b^3\left(\frac{a}{b}\right)^{\frac{1}{3}}} - \frac{5\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9b^3\left(\frac{a}{b}\right)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/3)/(b*x+a)^3,x, algorithm="maxima")

[Out] $-1/6*(8*b*x^{(5/3)} + 5*a*x^{(2/3)})/(b^4*x^2 + 2*a*b^3*x + a^2*b^2) + 5/9*\text{sqrt}(3)*\arctan(1/3*\text{sqrt}(3)*(2*x^{(1/3)} - (a/b)^{(1/3)})/(a/b)^{(1/3)})/(b^3*(a/b)^{(1/3)}) + 5/18*\log(x^{(2/3)} - x^{(1/3)}*(a/b)^{(1/3)} + (a/b)^{(2/3)})/(b^3*(a/b)^{(1/3)}) - 5/9*\log(x^{(1/3)} + (a/b)^{(1/3)})/(b^3*(a/b)^{(1/3)})$

mupad [B] time = 0.17, size = 165, normalized size = 1.18

$$\frac{5 \ln\left(\frac{25x^{1/3}}{9b^3} - \frac{25(-a)^{1/3}}{9b^{10/3}}\right)}{9(-a)^{1/3}b^{8/3}} - \frac{\frac{4x^{5/3}}{3b} + \frac{5ax^{2/3}}{6b^2}}{a^2 + 2abx + b^2x^2} + \frac{\ln\left(\frac{25x^{1/3}}{9b^3} - \frac{(-a)^{1/3}(-5 + \sqrt{3}5i)^2}{36b^{10/3}}\right)(-5 + \sqrt{3}5i)}{18(-a)^{1/3}b^{8/3}} - \frac{\ln\left(\frac{25x^{1/3}}{9b^3} - \frac{(-a)^{1/3}(5 + \sqrt{3}5i)^2}{36b^{10/3}}\right)(-5 - \sqrt{3}5i)}{18(-a)^{1/3}b^{8/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(5/3)/(a + b*x)^3,x)

[Out] (5*log((25*x^(1/3))/(9*b^3) - (25*(-a)^(1/3))/(9*b^(10/3))))/(9*(-a)^(1/3)*b^(8/3)) - ((4*x^(5/3))/(3*b) + (5*a*x^(2/3))/(6*b^2))/(a^2 + b^2*x^2 + 2*a*b*x) + (log((25*x^(1/3))/(9*b^3) - ((-a)^(1/3)*(3^(1/2)*5i - 5)^2)/(36*b^(10/3))))*(3^(1/2)*5i - 5)/(18*(-a)^(1/3)*b^(8/3)) - (log((25*x^(1/3))/(9*b^3) - ((-a)^(1/3)*(3^(1/2)*5i + 5)^2)/(36*b^(10/3))))*(3^(1/2)*5i + 5)/(18*(-a)^(1/3)*b^(8/3))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(5/3)/(b*x+a)**3,x)

[Out] Timed out

$$3.691 \quad \int \frac{x^{4/3}}{(a+bx)^3} dx$$

Optimal. Leaf size=140

$$\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{3a^{2/3}b^{7/3}} - \frac{\log(a+bx)}{9a^{2/3}b^{7/3}} - \frac{2 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{2/3}b^{7/3}} - \frac{2\sqrt[3]{x}}{3b^2(a+bx)} - \frac{x^{4/3}}{2b(a+bx)^2}$$

[Out] $-1/2*x^{(4/3)}/b/(b*x+a)^2-2/3*x^{(1/3)}/b^2/(b*x+a)+1/3*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(2/3)}/b^{(7/3)}-1/9*\ln(b*x+a)/a^{(2/3)}/b^{(7/3)}-2/9*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/a^{(2/3)}/b^{(7/3)}*3^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 140, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {47, 58, 617, 204, 31}

$$\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{3a^{2/3}b^{7/3}} - \frac{\log(a+bx)}{9a^{2/3}b^{7/3}} - \frac{2 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{2/3}b^{7/3}} - \frac{2\sqrt[3]{x}}{3b^2(a+bx)} - \frac{x^{4/3}}{2b(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[x^(4/3)/(a + b*x)^3, x]

[Out] $-x^{(4/3)}/(2*b*(a + b*x)^2) - (2*x^{(1/3)})/(3*b^2*(a + b*x)) - (2*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/(3*\text{Sqrt}[3]*a^{(2/3)}*b^{(7/3)}) + \text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}]/(3*a^{(2/3)}*b^{(7/3)}) - \text{Log}[a + b*x]/(9*a^{(2/3)}*b^{(7/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 58


```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^
2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(
1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)],
x]])] /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{4/3}}{(a+bx)^3} dx &= -\frac{x^{4/3}}{2b(a+bx)^2} + \frac{2 \int \frac{\sqrt[3]{x}}{(a+bx)^2} dx}{3b} \\
&= -\frac{x^{4/3}}{2b(a+bx)^2} - \frac{2\sqrt[3]{x}}{3b^2(a+bx)} + \frac{2 \int \frac{1}{x^{2/3}(a+bx)} dx}{9b^2} \\
&= -\frac{x^{4/3}}{2b(a+bx)^2} - \frac{2\sqrt[3]{x}}{3b^2(a+bx)} - \frac{\log(a+bx)}{9a^{2/3}b^{7/3}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{3\sqrt[3]{a}b^{8/3}} + \frac{\text{Subst}\left(\int \frac{\sqrt[3]{x}}{\sqrt[3]{a} - \sqrt[3]{b}x} dx, x, \sqrt[3]{x}\right)}{3a^{2/3}b^{7/3}} \\
&= -\frac{x^{4/3}}{2b(a+bx)^2} - \frac{2\sqrt[3]{x}}{3b^2(a+bx)} + \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{3a^{2/3}b^{7/3}} - \frac{\log(a+bx)}{9a^{2/3}b^{7/3}} + \frac{2 \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1\right)}{3a^{2/3}b^{7/3}} \\
&= -\frac{x^{4/3}}{2b(a+bx)^2} - \frac{2\sqrt[3]{x}}{3b^2(a+bx)} - \frac{2 \tan^{-1}\left(\frac{1 - 2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}\right)}{3\sqrt[3]{a}a^{2/3}b^{7/3}} + \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{3a^{2/3}b^{7/3}} - \frac{\log(a+bx)}{9a^{2/3}b^{7/3}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.19

$$\frac{3x^{7/3} {}_2F_1\left(\frac{7}{3}, 3; \frac{10}{3}; -\frac{bx}{a}\right)}{7a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(4/3)/(a + b*x)^3,x]

[Out] (3*x^(7/3)*Hypergeometric2F1[7/3, 3, 10/3, -((b*x)/a)])/(7*a^3)

fricas [B] time = 0.48, size = 503, normalized size = 3.59

$$\left[6\sqrt{\frac{1}{3}}(ab^3x^2 + 2a^2b^2x + a^3b)\sqrt{-\frac{(a^2b)^{\frac{1}{3}}}{b}} \log\left(\frac{2abx - a^2 + 3\sqrt{\frac{1}{3}}\left(2abx^{\frac{2}{3}} - (a^2b)^{\frac{1}{3}}a + (a^2b)^{\frac{2}{3}}x^{\frac{1}{3}}\right)\sqrt{-\frac{(a^2b)^{\frac{1}{3}}}{b}} - 3(a^2b)^{\frac{1}{3}}ax^{\frac{1}{3}}}{bx+a}\right) - 2(b^2x^2 - \dots) \right] \frac{1}{18(a^{\dots})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)/(b*x+a)^3,x, algorithm="fricas")

[Out] [1/18*(6*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt(-(a^2*b)^(1/3)/b) *log((2*a*b*x - a^2 + 3*sqrt(1/3)*(2*a*b*x^(2/3) - (a^2*b)^(1/3)*a + (a^2*b)^(2/3)*x^(1/3))*sqrt(-(a^2*b)^(1/3)/b) - 3*(a^2*b)^(1/3)*a*x^(1/3))/(b*x + a)) - 2*(b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) + 4*(b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3) *log(a*b*x^(1/3) + (a^2*b)^(2/3)) - 3*(7*a^2*b^2*x + 4*a^3*b)*x^(1/3))/(a^2*b^5*x^2 + 2*a^3*b^4*x + a^4*b^3), 1/18*(12*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt((a^2*b)^(1/3)/b)*arctan(-sqrt(1/3)*((a^2*b)^(1/3)*a - 2*(a^2*b)^(2/3)*x^(1/3))*sqrt((a^2*b)^(1/3)/b)/a^2) - 2*(b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) + 4*(b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(1/3) + (a^2*b)^(2/3)) - 3*(7*a^2*b^2*x + 4*a^3*b)*x^(1/3))/(a^2*b^5*x^2 + 2*a^3*b^4*x + a^4*b^3)]

giac [A] time = 1.13, size = 146, normalized size = 1.04

$$\frac{2 \left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{9ab^2} + \frac{2\sqrt{3}(-ab^2)^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9ab^3} + \frac{(-ab^2)^{\frac{1}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{9ab^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)/(b*x+a)^3,x, algorithm="giac")

[Out] $-2/9*(-a/b)^{(1/3)}*\log(\text{abs}(x^{(1/3)} - (-a/b)^{(1/3)}))/(a*b^2) + 2/9*\text{sqrt}(3)*(-a*b^2)^{(1/3)}*\arctan(1/3*\text{sqrt}(3)*(2*x^{(1/3)} + (-a/b)^{(1/3)})/(-a/b)^{(1/3)})/(a*b^3) + 1/9*(-a*b^2)^{(1/3)}*\log(x^{(2/3)} + x^{(1/3)}*(-a/b)^{(1/3)} + (-a/b)^{(2/3)})/(a*b^3) - 1/6*(7*b*x^{(4/3)} + 4*a*x^{(1/3)})/((b*x + a)^2*b^2)$

maple [A] time = 0.01, size = 124, normalized size = 0.89

$$\frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{9\left(\frac{a}{b}\right)^{\frac{2}{3}}b^3} + \frac{2\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9\left(\frac{a}{b}\right)^{\frac{2}{3}}b^3} - \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{9\left(\frac{a}{b}\right)^{\frac{2}{3}}b^3} + \frac{-\frac{7x^{\frac{4}{3}}}{6b} - \frac{2ax^{\frac{1}{3}}}{3b^2}}{(bx+a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(4/3)/(b*x+a)^3,x)

[Out] $3*(-7/18/b*x^{(4/3)}-2/9*a/b^2*x^{(1/3)})/(b*x+a)^2+2/9/b^3/(a/b)^{(2/3)}*\ln(x^{(1/3)}+(a/b)^{(1/3)})-1/9/b^3/(a/b)^{(2/3)}*\ln(x^{(2/3)}-(a/b)^{(1/3)}*x^{(1/3)}+(a/b)^{(2/3)})+2/9/b^3/(a/b)^{(2/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2/(a/b)^{(1/3)}*x^{(1/3)}-1))$

maxima [A] time = 2.88, size = 143, normalized size = 1.02

$$\frac{7bx^{\frac{4}{3}} + 4ax^{\frac{1}{3}}}{6(b^4x^2 + 2ab^3x + a^2b^2)} + \frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9b^3\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{9b^3\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{2\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9b^3\left(\frac{a}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(4/3)/(b*x+a)^3,x, algorithm="maxima")

[Out] $-\frac{1}{6} \cdot (7bx^{4/3} + 4ax^{1/3}) / (b^4x^2 + 2ab^3x + a^2b^2) + \frac{2}{9} \sqrt{3} \arctan\left(\frac{1}{3} \sqrt{3} (2x^{1/3} - (a/b)^{1/3}) / ((a/b)^{1/3})\right) / (b^3(a/b)^{2/3}) - \frac{1}{9} \log(x^{2/3} - x^{1/3}(a/b)^{1/3} + (a/b)^{2/3}) / (b^3(a/b)^{2/3}) + \frac{2}{9} \log(x^{1/3} + (a/b)^{1/3}) / (b^3(a/b)^{2/3})$

mupad [B] time = 0.07, size = 139, normalized size = 0.99

$$\frac{2 \ln\left(2x^{1/3} + \frac{2a^{1/3}}{b^{1/3}}\right)}{9a^{2/3}b^{7/3}} - \frac{\frac{7x^{4/3}}{6b} + \frac{2ax^{1/3}}{3b^2}}{a^2 + 2abx + b^2x^2} + \frac{\ln\left(2x^{1/3} + \frac{a^{1/3}(-1+\sqrt{3}i)}{b^{1/3}}\right) (-1 + \sqrt{3}i)}{9a^{2/3}b^{7/3}} - \frac{\ln\left(2x^{1/3} - \frac{a^{1/3}(1+\sqrt{3}i)}{b^{1/3}}\right) (1 - \sqrt{3}i)}{9a^{2/3}b^{7/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(4/3)/(a + b*x)^3,x)

[Out] $(2 \log(2x^{1/3} + (2a^{1/3})/b^{1/3})) / (9a^{2/3}b^{7/3}) - ((7x^{4/3}) / (6b) + (2ax^{1/3}) / (3b^2)) / (a^2 + b^2x^2 + 2abx) + (\log(2x^{1/3} + (a^{1/3}(3^{1/2}i - 1)) / b^{1/3})) * (3^{1/2}i - 1) / (9a^{2/3}b^{7/3}) - (\log(2x^{1/3} - (a^{1/3}(3^{1/2}i + 1)) / b^{1/3})) * (3^{1/2}i + 1) / (9a^{2/3}b^{7/3})$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(4/3)/(b*x+a)**3,x)

[Out] Timed out

$$3.692 \quad \int \frac{x^{2/3}}{(a+bx)^3} dx$$

Optimal. Leaf size=143

$$-\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{6a^{4/3}b^{5/3}} + \frac{\log(a+bx)}{18a^{4/3}b^{5/3}} - \frac{\tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{4/3}b^{5/3}} + \frac{x^{2/3}}{3ab(a+bx)} - \frac{x^{2/3}}{2b(a+bx)^2}$$

[Out] $-1/2*x^{(2/3)}/b/(b*x+a)^2+1/3*x^{(2/3)}/a/b/(b*x+a)-1/6*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(4/3)}/b^{(5/3)}+1/18*\ln(b*x+a)/a^{(4/3)}/b^{(5/3)}-1/9*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/a^{(4/3)}/b^{(5/3)}*3^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 143, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.462$, Rules used = {47, 51, 56, 617, 204, 31}

$$-\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{6a^{4/3}b^{5/3}} + \frac{\log(a+bx)}{18a^{4/3}b^{5/3}} - \frac{\tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{4/3}b^{5/3}} + \frac{x^{2/3}}{3ab(a+bx)} - \frac{x^{2/3}}{2b(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[x^(2/3)/(a + b*x)^3, x]

[Out] $-x^{(2/3)}/(2*b*(a + b*x)^2) + x^{(2/3)}/(3*a*b*(a + b*x)) - \text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})]/(3*\text{Sqrt}[3]*a^{(4/3)}*b^{(5/3)}) - \text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}]/(6*a^{(4/3)}*b^{(5/3)}) + \text{Log}[a + b*x]/(18*a^{(4/3)}*b^{(5/3)})$

Rule 31

Int[((a_) + (b_)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])] /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^{2/3}}{(a+bx)^3} dx &= -\frac{x^{2/3}}{2b(a+bx)^2} + \frac{\int \frac{1}{\sqrt[3]{x}(a+bx)^2} dx}{3b} \\
&= -\frac{x^{2/3}}{2b(a+bx)^2} + \frac{x^{2/3}}{3ab(a+bx)} + \frac{\int \frac{1}{\sqrt[3]{x}(a+bx)} dx}{9ab} \\
&= -\frac{x^{2/3}}{2b(a+bx)^2} + \frac{x^{2/3}}{3ab(a+bx)} + \frac{\log(a+bx)}{18a^{4/3}b^{5/3}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{6ab^2} - \frac{\text{Subst}\left(\int \frac{\sqrt[3]{x}}{\sqrt[3]{x}} dx, x, \sqrt[3]{x}\right)}{6a^{4/3}b^{5/3}} \\
&= -\frac{x^{2/3}}{2b(a+bx)^2} + \frac{x^{2/3}}{3ab(a+bx)} - \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{6a^{4/3}b^{5/3}} + \frac{\log(a+bx)}{18a^{4/3}b^{5/3}} + \frac{\text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{\sqrt[3]{x}}{\sqrt[3]{a}}\right)}{3a^{4/3}b^{5/3}} \\
&= -\frac{x^{2/3}}{2b(a+bx)^2} + \frac{x^{2/3}}{3ab(a+bx)} - \frac{\tan^{-1}\left(\frac{1 - 2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}\right)}{3\sqrt{3}a^{4/3}b^{5/3}} - \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{6a^{4/3}b^{5/3}} + \frac{\log(a+bx)}{18a^{4/3}b^{5/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 27, normalized size = 0.19

$$\frac{3x^{5/3} {}_2F_1\left(\frac{5}{3}, 3; \frac{8}{3}; -\frac{bx}{a}\right)}{5a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(2/3)/(a + b*x)^3,x]

[Out] (3*x^(5/3)*Hypergeometric2F1[5/3, 3, 8/3, -((b*x)/a)])/(5*a^3)

fricas [B] time = 0.48, size = 508, normalized size = 3.55

$$\left[3\sqrt{\frac{1}{3}}(ab^3x^2 + 2a^2b^2x + a^3b)\sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} \log\left(\frac{2b^2x-ab+3\sqrt{\frac{1}{3}}\left(abx^{\frac{1}{3}}+(-ab^2)^{\frac{1}{3}}a+2(-ab^2)^{\frac{2}{3}}x^{\frac{2}{3}}\right)\sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}}-3(-ab^2)^{\frac{2}{3}}x^{\frac{1}{3}}}{bx+a}}\right) + (b^2x^{\frac{5}{3}}) \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)/(b*x+a)^3,x, algorithm="fricas")

[Out] [1/18*(3*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt((-a*b^2)^(1/3)/a)*log((2*b^2*x - a*b + 3*sqrt(1/3)*(a*b*x^(1/3) + (-a*b^2)^(1/3)*a + 2*(-a*b^2)^(2/3)*x^(2/3))*sqrt((-a*b^2)^(1/3)/a) - 3*(-a*b^2)^(2/3)*x^(1/3))/(b*x + a) + (b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) - 2*(b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b*x^(1/3) - (-a*b^2)^(1/3)) + 3*(2*a*b^3*x - a^2*b^2)*x^(2/3)/(a^2*b^5*x^2 + 2*a^3*b^4*x + a^4*b^3), 1/18*(6*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt(-(-a*b^2)^(1/3)/a)*arctan(sqrt(1/3)*(2*b*x^(1/3) + (-a*b^2)^(1/3))*sqrt(-(-a*b^2)^(1/3)/a)/b) + (b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) - 2*(b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b*x^(1/3) - (-a*b^2)^(1/3)) + 3*(2*a*b^3*x - a^2*b^2)*x^(2/3)/(a^2*b^5*x^2 + 2*a^3*b^4*x + a^4*b^3)]

giac [A] time = 1.06, size = 149, normalized size = 1.04

$$\frac{\left(-\frac{a}{b}\right)^{\frac{2}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{9 a^2 b} - \frac{\sqrt{3} (-ab^2)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9 a^2 b^3} + \frac{2 b x^{\frac{5}{3}} - a x^{\frac{2}{3}}}{6 (b x + a)^2 a b} + \frac{(-ab^2)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}} \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{18 a^2 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2/3)/(b*x+a)^3,x, algorithm="giac")

[Out] -1/9*(-a/b)^(2/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/(a^2*b) - 1/9*sqrt(3)*(-a*b^2)^(2/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/(a^2*b^3) + 1/6*(2*b*x^(5/3) - a*x^(2/3))/((b*x + a)^2*a*b) + 1/18*(-a*b^2)^(2/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/(a^2*b^3)

maple [A] time = 0.01, size = 132, normalized size = 0.92

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{9\left(\frac{a}{b}\right)^{\frac{1}{3}} a b^2} - \frac{\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9\left(\frac{a}{b}\right)^{\frac{1}{3}} a b^2} + \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{18\left(\frac{a}{b}\right)^{\frac{1}{3}} a b^2} + \frac{\frac{5}{3a} - \frac{x^{\frac{2}{3}}}{6b}}{(bx+a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{(2/3)}/(b*x+a)^3,x)$

[Out] $3*(1/9/a*x^{(5/3)}-1/18/b*x^{(2/3)})/(b*x+a)^2-1/9/b^2/a/(a/b)^{(1/3)}*\ln(x^{(1/3)}+(a/b)^{(1/3)})+1/18/b^2/a/(a/b)^{(1/3)}*\ln(x^{(2/3)}-(a/b)^{(1/3)}*x^{(1/3)}+(a/b)^{(2/3)})+1/9/b^2/a*3^{(1/2)}/(a/b)^{(1/3)}*\arctan(1/3*3^{(1/2)}*(2/(a/b)^{(1/3)}*x^{(1/3)}-1))$

maxima [A] time = 2.92, size = 153, normalized size = 1.07

$$\frac{2bx^{\frac{5}{3}} - ax^{\frac{2}{3}}}{6(ab^3x^2 + 2a^2b^2x + a^3b)} + \frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9ab^2\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{18ab^2\left(\frac{a}{b}\right)^{\frac{1}{3}}} - \frac{\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9ab^2\left(\frac{a}{b}\right)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{(2/3)}/(b*x+a)^3,x, \text{algorithm}="maxima")$

[Out] $1/6*(2*b*x^{(5/3)} - a*x^{(2/3)})/(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b) + 1/9*\sqrt{3}*(3)*\arctan(1/3*\sqrt{3}*(2*x^{(1/3)} - (a/b)^{(1/3)})/(a/b)^{(1/3)})/(a*b^2*(a/b)^{(1/3)}) + 1/18*\log(x^{(2/3)} - x^{(1/3)}*(a/b)^{(1/3)} + (a/b)^{(2/3)})/(a*b^2*(a/b)^{(1/3)}) - 1/9*\log(x^{(1/3)} + (a/b)^{(1/3)})/(a*b^2*(a/b)^{(1/3)})$

mupad [B] time = 0.26, size = 172, normalized size = 1.20

$$\frac{\frac{x^{5/3}}{3a} - \frac{x^{2/3}}{6b}}{a^2 + 2abx + b^2x^2} + \frac{\ln\left(\frac{1}{9a^{5/3}(-b)^{4/3}} + \frac{x^{1/3}}{9a^2b}\right)}{9a^{4/3}(-b)^{5/3}} + \frac{\ln\left(\frac{x^{1/3}}{9a^2b} + \frac{(-1+\sqrt{3}1i)^2}{36a^{5/3}(-b)^{4/3}}\right)(-1+\sqrt{3}1i)}{18a^{4/3}(-b)^{5/3}} - \frac{\ln\left(\frac{x^{1/3}}{9a^2b} + \frac{(1+\sqrt{3}1i)^2}{36a^{5/3}(-b)^{4/3}}\right)(1-\sqrt{3}1i)}{18a^{4/3}(-b)^{5/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{(2/3)}/(a + b*x)^3,x)$

[Out] $(x^{(5/3)}/(3*a) - x^{(2/3)}/(6*b))/(a^2 + b^2*x^2 + 2*a*b*x) + \log(1/(9*a^{(5/3)}*(-b)^{(4/3)}) + x^{(1/3)}/(9*a^2*b))/(9*a^{(4/3)}*(-b)^{(5/3)}) + (\log(x^{(1/3)}/(9*a^2*b) + (3^{(1/2)}*1i - 1)^2/(36*a^{(5/3)}*(-b)^{(4/3)}))*(3^{(1/2)}*1i - 1))/(18*a^{(4/3)}*(-b)^{(5/3)}) - (\log(x^{(1/3)}/(9*a^2*b) + (3^{(1/2)}*1i + 1)^2/(36*a^{(5/3)}*(-b)^{(4/3)}))*(3^{(1/2)}*1i + 1))/(18*a^{(4/3)}*(-b)^{(5/3)})$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{(2/3)}/(b*x+a)^3,x)$

[Out] Timed out

$$3.693 \quad \int \frac{\sqrt[3]{x}}{(a+bx)^3} dx$$

Optimal. Leaf size=143

$$\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{6a^{5/3}b^{4/3}} - \frac{\log(a+bx)}{18a^{5/3}b^{4/3}} - \frac{\tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{5/3}b^{4/3}} + \frac{\sqrt[3]{x}}{6ab(a+bx)} - \frac{\sqrt[3]{x}}{2b(a+bx)^2}$$

[Out] $-1/2*x^{(1/3)}/b/(b*x+a)^2+1/6*x^{(1/3)}/a/b/(b*x+a)+1/6*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(5/3)}/b^{(4/3)}-1/18*\ln(b*x+a)/a^{(5/3)}/b^{(4/3)}-1/9*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/a^{(5/3)}/b^{(4/3)}*3^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 143, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.462$, Rules used = {47, 51, 58, 617, 204, 31}

$$\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{6a^{5/3}b^{4/3}} - \frac{\log(a+bx)}{18a^{5/3}b^{4/3}} - \frac{\tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{5/3}b^{4/3}} + \frac{\sqrt[3]{x}}{6ab(a+bx)} - \frac{\sqrt[3]{x}}{2b(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[x^(1/3)/(a + b*x)^3, x]

[Out] $-x^{(1/3)}/(2*b*(a + b*x)^2) + x^{(1/3)}/(6*a*b*(a + b*x)) - \text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})]/(3*\text{Sqrt}[3]*a^{(5/3)}*b^{(4/3)}) + \text{Log}[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}]/(6*a^{(5/3)}*b^{(4/3)}) - \text{Log}[a + b*x]/(18*a^{(5/3)}*b^{(4/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 58

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^
2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(
1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)],
x])]) /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c]) /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[3]{x}}{(a+bx)^3} dx &= -\frac{\sqrt[3]{x}}{2b(a+bx)^2} + \frac{\int \frac{1}{x^{2/3}(a+bx)^2} dx}{6b} \\
&= -\frac{\sqrt[3]{x}}{2b(a+bx)^2} + \frac{\sqrt[3]{x}}{6ab(a+bx)} + \frac{\int \frac{1}{x^{2/3}(a+bx)} dx}{9ab} \\
&= -\frac{\sqrt[3]{x}}{2b(a+bx)^2} + \frac{\sqrt[3]{x}}{6ab(a+bx)} - \frac{\log(a+bx)}{18a^{5/3}b^{4/3}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{6a^{4/3}b^{5/3}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{a}}{\sqrt[3]{b}}} dx, x, \frac{\sqrt[3]{a}}{\sqrt[3]{b}}\right)}{6a^{5/3}} \\
&= -\frac{\sqrt[3]{x}}{2b(a+bx)^2} + \frac{\sqrt[3]{x}}{6ab(a+bx)} + \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{6a^{5/3}b^{4/3}} - \frac{\log(a+bx)}{18a^{5/3}b^{4/3}} + \frac{\text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 - \frac{\sqrt[3]{a}}{\sqrt[3]{b}}\right)}{3a^{5/3}b^{4/3}} \\
&= -\frac{\sqrt[3]{x}}{2b(a+bx)^2} + \frac{\sqrt[3]{x}}{6ab(a+bx)} - \frac{\tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{3\sqrt{3}a^{5/3}b^{4/3}} + \frac{\log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{6a^{5/3}b^{4/3}} - \frac{\log(a+bx)}{18a^{5/3}b^{4/3}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.19

$$\frac{3x^{4/3} {}_2F_1\left(\frac{4}{3}, 3; \frac{7}{3}; -\frac{bx}{a}\right)}{4a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(1/3)/(a + b*x)^3,x]

[Out] (3*x^(4/3)*Hypergeometric2F1[4/3, 3, 7/3, -((b*x)/a)])/(4*a^3)

fricas [B] time = 0.48, size = 501, normalized size = 3.50

$$\left[3\sqrt{\frac{1}{3}}(ab^3x^2 + 2a^2b^2x + a^3b)\sqrt{-\frac{(a^2b)^{1/3}}{b}} \log\left(\frac{2abx - a^2 + 3\sqrt{\frac{1}{3}}\left(2abx^{\frac{2}{3}} - (a^2b)^{\frac{1}{3}}a + (a^2b)^{\frac{2}{3}}x^{\frac{1}{3}}\right)\sqrt{-\frac{(a^2b)^{1/3}}{b}} - 3(a^2b)^{\frac{1}{3}}ax^{\frac{1}{3}}}{bx+a}}\right) - (b^2x^2 + \dots) \right]$$

$$18(a^3b^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)/(b*x+a)^3,x, algorithm="fricas")

[Out] [1/18*(3*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt(-(a^2*b)^(1/3)/b) *log((2*a*b*x - a^2 + 3*sqrt(1/3)*(2*a*b*x^(2/3) - (a^2*b)^(1/3)*a + (a^2*b)^(2/3)*x^(1/3))*sqrt(-(a^2*b)^(1/3)/b) - 3*(a^2*b)^(1/3)*a*x^(1/3))/(b*x + a)) - (b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) + 2*(b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(1/3) + (a^2*b)^(2/3)) + 3*(a^2*b^2*x - 2*a^3*b)*x^(1/3))/(a^3*b^4*x^2 + 2*a^4*b^3*x + a^5*b^2), 1/18*(6*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt((a^2*b)^(1/3)/b)*arctan(-sqrt(1/3)*((a^2*b)^(1/3)*a - 2*(a^2*b)^(2/3)*x^(1/3))*sqrt((a^2*b)^(1/3)/b)/a^2) - (b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) + 2*(b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(1/3) + (a^2*b)^(2/3)) + 3*(a^2*b^2*x - 2*a^3*b)*x^(1/3))/(a^3*b^4*x^2 + 2*a^4*b^3*x + a^5*b^2)]

giac [A] time = 1.11, size = 148, normalized size = 1.03

$$\frac{\left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9 a^2 b} + \frac{\sqrt{3} (-ab^2)^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9 a^2 b^2} + \frac{(-ab^2)^{\frac{1}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}} \left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{18 a^2 b^2} + \frac{bx}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/3)/(b*x+a)^3,x, algorithm="giac")

[Out] -1/9*(-a/b)^(1/3)*log(abs(x^(1/3) - (-a/b)^(1/3)))/(a^2*b) + 1/9*sqrt(3)*(-a*b^2)^(1/3)*arctan(1/3*sqrt(3)*(2*x^(1/3) + (-a/b)^(1/3))/(-a/b)^(1/3))/(a^2*b^2) + 1/18*(-a*b^2)^(1/3)*log(x^(2/3) + x^(1/3)*(-a/b)^(1/3) + (-a/b)^(2/3))/(a^2*b^2) + 1/6*(b*x^(4/3) - 2*a*x^(1/3))/((b*x + a)^2*a*b)

maple [A] time = 0.01, size = 132, normalized size = 0.92

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{9\left(\frac{a}{b}\right)^{\frac{2}{3}} a b^2} + \frac{\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9\left(\frac{a}{b}\right)^{\frac{2}{3}} a b^2} - \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{18\left(\frac{a}{b}\right)^{\frac{2}{3}} a b^2} + \frac{\frac{4}{6a} - \frac{x^{\frac{1}{3}}}{3b}}{(bx + a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{1/3}/(b*x+a)^3, x)$

[Out] $3*(1/18/a*x^{4/3}-1/9/b*x^{1/3})/(b*x+a)^2+1/9/b^2/a/(a/b)^{2/3}*\ln(x^{1/3}+(a/b)^{1/3})-1/18/b^2/a/(a/b)^{2/3}*\ln(x^{2/3}-(a/b)^{1/3}*x^{1/3}+(a/b)^{2/3})+1/9/b^2/a/(a/b)^{2/3}*3^{1/2}*\arctan(1/3*3^{1/2}*(2/(a/b)^{1/3}*x^{1/3}-1))$

maxima [A] time = 2.96, size = 152, normalized size = 1.06

$$\frac{bx^{\frac{4}{3}} - 2ax^{\frac{1}{3}}}{6(ab^3x^2 + 2a^2b^2x + a^3b)} + \frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9ab^2\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{18ab^2\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9ab^2\left(\frac{a}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{1/3}/(b*x+a)^3, x, \text{algorithm}="maxima")$

[Out] $1/6*(b*x^{4/3} - 2*a*x^{1/3})/(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b) + 1/9*\text{sqrt}(3)*\arctan(1/3*\text{sqrt}(3)*(2*x^{1/3} - (a/b)^{1/3})/(a/b)^{1/3})/(a*b^2*(a/b)^{2/3}) - 1/18*\log(x^{2/3} - x^{1/3}*(a/b)^{1/3} + (a/b)^{2/3})/(a*b^2*(a/b)^{2/3}) + 1/9*\log(x^{1/3} + (a/b)^{1/3})/(a*b^2*(a/b)^{2/3})$

mupad [B] time = 0.24, size = 146, normalized size = 1.02

$$\frac{\frac{x^{4/3}}{6a} - \frac{x^{1/3}}{3b}}{a^2 + 2abx + b^2x^2} + \frac{\ln\left(\frac{b^{2/3}}{a^{2/3}} + \frac{bx^{1/3}}{a}\right)}{9a^{5/3}b^{4/3}} + \frac{\ln\left(\frac{bx^{1/3}}{a} + \frac{b^{2/3}(-1+\sqrt{3}i)}{2a^{2/3}}\right)(-1+\sqrt{3}i)}{18a^{5/3}b^{4/3}} - \frac{\ln\left(\frac{bx^{1/3}}{a} - \frac{b^{2/3}(1+\sqrt{3}i)}{2a^{2/3}}\right)(1+\sqrt{3}i)}{18a^{5/3}b^{4/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^{1/3}/(a + b*x)^3, x)$

[Out] $(x^{4/3}/(6*a) - x^{1/3}/(3*b))/(a^2 + b^2*x^2 + 2*a*b*x) + \log(b^{2/3}/a^{2/3} + (b*x^{1/3})/a)/(9*a^{5/3}*b^{4/3}) + (\log((b*x^{1/3})/a + (b^{2/3})*(3^{1/2}*1i - 1))/(2*a^{2/3}))*((3^{1/2}*1i - 1))/(18*a^{5/3}*b^{4/3}) - (\log((b*x^{1/3})/a - (b^{2/3})*(3^{1/2}*1i + 1))/(2*a^{2/3}))*((3^{1/2}*1i + 1))/(18*a^{5/3}*b^{4/3})$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^{1/3}/(b*x+a)^3, x)$

[Out] Timed out

$$3.694 \quad \int \frac{1}{\sqrt[3]{x}(a+bx)^3} dx$$

Optimal. Leaf size=140

$$-\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{3a^{7/3}b^{2/3}} + \frac{\log(a+bx)}{9a^{7/3}b^{2/3}} - \frac{2 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{7/3}b^{2/3}} + \frac{2x^{2/3}}{3a^2(a+bx)} + \frac{x^{2/3}}{2a(a+bx)^2}$$

[Out] 1/2*x^(2/3)/a/(b*x+a)^2+2/3*x^(2/3)/a^2/(b*x+a)-1/3*ln(a^(1/3)+b^(1/3)*x^(1/3))/a^(7/3)/b^(2/3)+1/9*ln(b*x+a)/a^(7/3)/b^(2/3)-2/9*arctan(1/3*(a^(1/3)-2*b^(1/3)*x^(1/3))/a^(1/3)*3^(1/2))/a^(7/3)/b^(2/3)*3^(1/2)

Rubi [A] time = 0.05, antiderivative size = 140, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 56, 617, 204, 31}

$$-\frac{\log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{3a^{7/3}b^{2/3}} + \frac{\log(a+bx)}{9a^{7/3}b^{2/3}} - \frac{2 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{7/3}b^{2/3}} + \frac{2x^{2/3}}{3a^2(a+bx)} + \frac{x^{2/3}}{2a(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(1/3)*(a + b*x)^3), x]

[Out] x^(2/3)/(2*a*(a + b*x)^2) + (2*x^(2/3))/(3*a^2*(a + b*x)) - (2*ArcTan[(a^(1/3) - 2*b^(1/3)*x^(1/3))/(Sqrt[3]*a^(1/3))]/(3*Sqrt[3]*a^(7/3)*b^(2/3)) - Log[a^(1/3) + b^(1/3)*x^(1/3)]/(3*a^(7/3)*b^(2/3)) + Log[a + b*x]/(9*a^(7/3)*b^(2/3))

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])] /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt[3]{x}(a+bx)^3} dx &= \frac{x^{2/3}}{2a(a+bx)^2} + \frac{2 \int \frac{1}{\sqrt[3]{x}(a+bx)^2} dx}{3a} \\
&= \frac{x^{2/3}}{2a(a+bx)^2} + \frac{2x^{2/3}}{3a^2(a+bx)} + \frac{2 \int \frac{1}{\sqrt[3]{x}(a+bx)} dx}{9a^2} \\
&= \frac{x^{2/3}}{2a(a+bx)^2} + \frac{2x^{2/3}}{3a^2(a+bx)} + \frac{\log(a+bx)}{9a^{7/3}b^{2/3}} + \frac{\text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{ax}}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{3a^2b} - \frac{\text{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{ax}}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{3a^2b} \\
&= \frac{x^{2/3}}{2a(a+bx)^2} + \frac{2x^{2/3}}{3a^2(a+bx)} - \frac{\log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{3a^{7/3}b^{2/3}} + \frac{\log(a+bx)}{9a^{7/3}b^{2/3}} + \frac{2 \text{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1\right)}{3a^{7/3}b^{2/3}} \\
&= \frac{x^{2/3}}{2a(a+bx)^2} + \frac{2x^{2/3}}{3a^2(a+bx)} - \frac{2 \tan^{-1}\left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}}\right)}{3\sqrt{3}a^{7/3}b^{2/3}} - \frac{\log\left(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x}\right)}{3a^{7/3}b^{2/3}} + \frac{\log(a+bx)}{9a^{7/3}b^{2/3}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 27, normalized size = 0.19

$$\frac{3x^{2/3} {}_2F_1\left(\frac{2}{3}, 3; \frac{5}{3}; -\frac{bx}{a}\right)}{2a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(1/3)*(a + b*x)^3), x]

[Out] (3*x^(2/3)*Hypergeometric2F1[2/3, 3, 5/3, -((b*x)/a)])/(2*a^3)

fricas [B] time = 0.48, size = 510, normalized size = 3.64

$$\left[6\sqrt{\frac{1}{3}}(ab^3x^2 + 2a^2b^2x + a^3b)\sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} \log\left(\frac{2b^2x-ab+3\sqrt{\frac{1}{3}}\left(abx^{\frac{1}{3}}+(-ab^2)^{\frac{1}{3}}a+2(-ab^2)^{\frac{2}{3}}x^{\frac{2}{3}}\right)\sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}}-3(-ab^2)^{\frac{2}{3}}x^{\frac{1}{3}}}{bx+a}}\right) + 2(b^2x^2 + 2abx + a^2)\sqrt{\frac{(-ab^2)^{\frac{1}{3}}}{a}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3)/(b*x+a)^3,x, algorithm="fricas")

[Out] [1/18*(6*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt((-a*b^2)^(1/3)/a) *log((2*b^2*x - a*b + 3*sqrt(1/3)*(a*b*x^(1/3) + (-a*b^2)^(1/3)*a + 2*(-a*b^2)^(2/3)*x^(2/3))*sqrt((-a*b^2)^(1/3)/a) - 3*(-a*b^2)^(2/3)*x^(1/3))/(b*x + a)) + 2*(b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) - 4*(b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b*x^(1/3) - (-a*b^2)^(1/3)) + 3*(4*a*b^3*x + 7*a^2*b^2)*x^(2/3))/(a^3*b^4*x^2 + 2*a^4*b^3*x + a^5*b^2), 1/18*(12*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt(-(-a*b^2)^(1/3)/a)*arctan(sqrt(1/3)*(2*b*x^(1/3) + (-a*b^2)^(1/3))*sqrt(-(-a*b^2)^(1/3)/a)/b) + 2*(b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b^2*x^(2/3) + (-a*b^2)^(1/3)*b*x^(1/3) + (-a*b^2)^(2/3)) - 4*(b^2*x^2 + 2*a*b*x + a^2)*(-a*b^2)^(2/3)*log(b*x^(1/3) - (-a*b^2)^(1/3)) + 3*(4*a*b^3*x + 7*a^2*b^2)*x^(2/3))/(a^3*b^4*x^2 + 2*a^4*b^3*x + a^5*b^2)]

giac [A] time = 1.06, size = 143, normalized size = 1.02

$$\frac{2\left(-\frac{a}{b}\right)^{\frac{2}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{9a^3} - \frac{2\sqrt{3}(-ab^2)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9a^3b^2} + \frac{4bx^{\frac{5}{3}} + 7ax^{\frac{2}{3}}}{6(bx+a)^2a^2} + \frac{(-ab^2)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\right)}{9a^3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3)/(b*x+a)^3,x, algorithm="giac")

[Out] $-2/9*(-a/b)^{(2/3)}*\log(\text{abs}(x^{(1/3)} - (-a/b)^{(1/3)}))/a^3 - 2/9*\text{sqrt}(3)*(-a*b^2)^{(2/3)}*\arctan(1/3*\text{sqrt}(3)*(2*x^{(1/3)} + (-a/b)^{(1/3)})/(-a/b)^{(1/3)})/(a^3*b^2) + 1/6*(4*b*x^{(5/3)} + 7*a*x^{(2/3)})/((b*x + a)^2*a^2) + 1/9*(-a*b^2)^{(2/3)}*\log(x^{(2/3)} + x^{(1/3)}*(-a/b)^{(1/3)} + (-a/b)^{(2/3)})/(a^3*b^2)$

maple [A] time = 0.01, size = 136, normalized size = 0.97

$$\frac{x^{\frac{2}{3}}}{2(bx+a)^2 a} + \frac{2x^{\frac{2}{3}}}{3(bx+a)a^2} + \frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{9\left(\frac{a}{b}\right)^{\frac{1}{3}}a^2b} - \frac{2\ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9\left(\frac{a}{b}\right)^{\frac{1}{3}}a^2b} + \frac{\ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{9\left(\frac{a}{b}\right)^{\frac{1}{3}}a^2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/3)/(b*x+a)^3,x)

[Out] $1/2*x^{(2/3)}/a/(b*x+a)^2+2/3*x^{(2/3)}/a^2/(b*x+a)-2/9/a^2/b/(a/b)^{(1/3)}*\ln(x^{(1/3)}+(a/b)^{(1/3)})+1/9/a^2/b/(a/b)^{(1/3)}*\ln(x^{(2/3)}-(a/b)^{(1/3)}*x^{(1/3)}+(a/b)^{(2/3)})+2/9/a^2*3^{(1/2)}/b/(a/b)^{(1/3)}*\arctan(1/3*3^{(1/2)}*(2/(a/b)^{(1/3)}*x^{(1/3)}-1))$

maxima [A] time = 2.96, size = 151, normalized size = 1.08

$$\frac{4bx^{\frac{5}{3}} + 7ax^{\frac{2}{3}}}{6(a^2b^2x^2 + 2a^3bx + a^4)} + \frac{2\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9a^2b\left(\frac{a}{b}\right)^{\frac{1}{3}}} + \frac{\log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{9a^2b\left(\frac{a}{b}\right)^{\frac{1}{3}}} - \frac{2\log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9a^2b\left(\frac{a}{b}\right)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/3)/(b*x+a)^3,x, algorithm="maxima")

[Out] $1/6*(4*b*x^{(5/3)} + 7*a*x^{(2/3)})/(a^2*b^2*x^2 + 2*a^3*b*x + a^4) + 2/9*\text{sqrt}(3)*\arctan(1/3*\text{sqrt}(3)*(2*x^{(1/3)} - (a/b)^{(1/3)})/(a/b)^{(1/3)})/(a^2*b*(a/b)^{(1/3)}) + 1/9*\log(x^{(2/3)} - x^{(1/3)}*(a/b)^{(1/3)} + (a/b)^{(2/3)})/(a^2*b*(a/b)^{(1/3)}) - 2/9*\log(x^{(1/3)} + (a/b)^{(1/3)})/(a^2*b*(a/b)^{(1/3)})$

mupad [B] time = 0.19, size = 167, normalized size = 1.19

$$\frac{\frac{7x^{2/3}}{6a} + \frac{2bx^{5/3}}{3a^2}}{a^2 + 2abx + b^2x^2} + \frac{2 \ln\left(\frac{4bx^{1/3}}{9a^4} - \frac{4b^{2/3}}{9(-a)^{11/3}}\right)}{9(-a)^{7/3}b^{2/3}} + \frac{\ln\left(\frac{4bx^{1/3}}{9a^4} - \frac{b^{2/3}(-1+\sqrt{3}i)^2}{9(-a)^{11/3}}\right)(-1+\sqrt{3}i)}{9(-a)^{7/3}b^{2/3}} - \frac{\ln\left(\frac{4bx^{1/3}}{9a^4} - \frac{b^{2/3}(1+\sqrt{3}i)}{9(-a)^{11/3}}\right)}{9(-a)^{7/3}b^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/3)*(a + b*x)^3),x)

[Out] ((7*x^(2/3))/(6*a) + (2*b*x^(5/3))/(3*a^2))/(a^2 + b^2*x^2 + 2*a*b*x) + (2*log((4*b*x^(1/3))/(9*a^4) - (4*b^(2/3))/(9*(-a)^(11/3))))/(9*(-a)^(7/3)*b^(2/3)) + (log((4*b*x^(1/3))/(9*a^4) - (b^(2/3)*(3^(1/2)*1i - 1)^2)/(9*(-a)^(11/3)))*(3^(1/2)*1i - 1))/(9*(-a)^(7/3)*b^(2/3)) - (log((4*b*x^(1/3))/(9*a^4) - (b^(2/3)*(3^(1/2)*1i + 1)^2)/(9*(-a)^(11/3)))*(3^(1/2)*1i + 1))/(9*(-a)^(7/3)*b^(2/3))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(1/3)/(b*x+a)**3,x)

[Out] Timed out

$$3.695 \quad \int \frac{1}{x^{2/3}(a+bx)^3} dx$$

Optimal. Leaf size=140

$$\frac{5 \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{6a^{8/3}\sqrt[3]{b}} - \frac{5 \log(a+bx)}{18a^{8/3}\sqrt[3]{b}} - \frac{5 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{8/3}\sqrt[3]{b}} + \frac{5\sqrt[3]{x}}{6a^2(a+bx)} + \frac{\sqrt[3]{x}}{2a(a+bx)^2}$$

[Out] $1/2*x^{(1/3)}/a/(b*x+a)^2+5/6*x^{(1/3)}/a^2/(b*x+a)+5/6*\ln(a^{(1/3)}+b^{(1/3)*x^{(1/3)})/a^{(8/3)}/b^{(1/3)}-5/18*\ln(b*x+a)/a^{(8/3)}/b^{(1/3)}-5/9*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)*x^{(1/3)})/a^{(1/3)*3^{(1/2)})/a^{(8/3)}/b^{(1/3)*3^{(1/2)}}$

Rubi [A] time = 0.05, antiderivative size = 140, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 58, 617, 204, 31}

$$\frac{5\sqrt[3]{x}}{6a^2(a+bx)} + \frac{5 \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{6a^{8/3}\sqrt[3]{b}} - \frac{5 \log(a+bx)}{18a^{8/3}\sqrt[3]{b}} - \frac{5 \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{8/3}\sqrt[3]{b}} + \frac{\sqrt[3]{x}}{2a(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(2/3)*(a + b*x)^3), x]

[Out] $x^{(1/3)}/(2*a*(a + b*x)^2) + (5*x^{(1/3)})/(6*a^2*(a + b*x)) - (5*\text{ArcTan}[(a^{(1/3)} - 2*b^{(1/3)*x^{(1/3)})/(\text{Sqrt}[3]*a^{(1/3)})])/(3*\text{Sqrt}[3]*a^{(8/3)*b^{(1/3)}}) + (5*\text{Log}[a^{(1/3)} + b^{(1/3)*x^{(1/3)}}])/(6*a^{(8/3)*b^{(1/3)}}) - (5*\text{Log}[a + b*x])/ (18*a^{(8/3)*b^{(1/3)}})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 58

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^
2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(
1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)],
x]])] /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{2/3}(a+bx)^3} dx &= \frac{\sqrt[3]{x}}{2a(a+bx)^2} + \frac{5 \int \frac{1}{x^{2/3}(a+bx)^2} dx}{6a} \\
&= \frac{\sqrt[3]{x}}{2a(a+bx)^2} + \frac{5\sqrt[3]{x}}{6a^2(a+bx)} + \frac{5 \int \frac{1}{x^{2/3}(a+bx)} dx}{9a^2} \\
&= \frac{\sqrt[3]{x}}{2a(a+bx)^2} + \frac{5\sqrt[3]{x}}{6a^2(a+bx)} - \frac{5 \log(a+bx)}{18a^{8/3}\sqrt[3]{b}} + \frac{5 \operatorname{Subst}\left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{a}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{x}\right)}{6a^{7/3}b^{2/3}} + \frac{5 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{x}\right)}{3a^{8/3}\sqrt[3]{b}} \\
&= \frac{\sqrt[3]{x}}{2a(a+bx)^2} + \frac{5\sqrt[3]{x}}{6a^2(a+bx)} + \frac{5 \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{6a^{8/3}\sqrt[3]{b}} - \frac{5 \log(a+bx)}{18a^{8/3}\sqrt[3]{b}} + \frac{5 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, \sqrt[3]{x}\right)}{3a^{8/3}\sqrt[3]{b}} \\
&= \frac{\sqrt[3]{x}}{2a(a+bx)^2} + \frac{5\sqrt[3]{x}}{6a^2(a+bx)} - \frac{5 \tan^{-1}\left(\frac{1 - 2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}\right)}{3\sqrt{3}a^{8/3}\sqrt[3]{b}} + \frac{5 \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{6a^{8/3}\sqrt[3]{b}} - \frac{5 \log(a+bx)}{18a^{8/3}\sqrt[3]{b}}
\end{aligned}$$

Mathematica [C] time = 0.00, size = 25, normalized size = 0.18

$$\frac{3\sqrt[3]{x} {}_2F_1\left(\frac{1}{3}, 3; \frac{4}{3}; -\frac{bx}{a}\right)}{a^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(2/3)*(a + b*x)^3), x]

[Out] (3*x^(1/3)*Hypergeometric2F1[1/3, 3, 4/3, -((b*x)/a)]/a^3

fricas [B] time = 0.81, size = 499, normalized size = 3.56

$$15\sqrt{\frac{1}{3}}(ab^3x^2 + 2a^2b^2x + a^3b)\sqrt{-\frac{(a^2b)^{\frac{1}{3}}}{b}} \log\left(\frac{2abx - a^2 + 3\sqrt{\frac{1}{3}}\left(2abx^{\frac{2}{3}} - (a^2b)^{\frac{1}{3}}a + (a^2b)^{\frac{2}{3}}x^{\frac{1}{3}}\right)\sqrt{-\frac{(a^2b)^{\frac{1}{3}}}{b}} - 3(a^2b)^{\frac{1}{3}}ax^{\frac{1}{3}}}{bx+a}\right) - 5(b^2x^2$$

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Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3)/(b*x+a)^3,x, algorithm="fricas")

[Out] [1/18*(15*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt(-(a^2*b)^(1/3)/b)*log((2*a*b*x - a^2 + 3*sqrt(1/3)*(2*a*b*x^(2/3) - (a^2*b)^(1/3)*a + (a^2*b)^(2/3)*x^(1/3))*sqrt(-(a^2*b)^(1/3)/b) - 3*(a^2*b)^(1/3)*a*x^(1/3))/(b*x + a)) - 5*(b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) + 10*(b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(1/3) + (a^2*b)^(2/3)) + 3*(5*a^2*b^2*x + 8*a^3*b)*x^(1/3))/(a^4*b^3*x^2 + 2*a^5*b^2*x + a^6*b), 1/18*(30*sqrt(1/3)*(a*b^3*x^2 + 2*a^2*b^2*x + a^3*b)*sqrt((a^2*b)^(1/3)/b)*arctan(-sqrt(1/3)*((a^2*b)^(1/3)*a - 2*(a^2*b)^(2/3)*x^(1/3))*sqrt((a^2*b)^(1/3)/b)/a^2) - 5*(b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(2/3) + (a^2*b)^(1/3)*a - (a^2*b)^(2/3)*x^(1/3)) + 10*(b^2*x^2 + 2*a*b*x + a^2)*(a^2*b)^(2/3)*log(a*b*x^(1/3) + (a^2*b)^(2/3)) + 3*(5*a^2*b^2*x + 8*a^3*b)*x^(1/3))/(a^4*b^3*x^2 + 2*a^5*b^2*x + a^6*b)]

giac [A] time = 1.00, size = 143, normalized size = 1.02

$$\frac{5 \left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{9a^3} + \frac{5\sqrt{3}(-ab^2)^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9a^3b} + \frac{5(-ab^2)^{\frac{1}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{18a^3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3)/(b*x+a)^3,x, algorithm="giac")

[Out] $-5/9*(-a/b)^{(1/3)}*\log(\text{abs}(x^{(1/3)} - (-a/b)^{(1/3)}))/a^3 + 5/9*\text{sqrt}(3)*(-a*b^2)^{(1/3)}*\arctan(1/3*\text{sqrt}(3)*(2*x^{(1/3)} + (-a/b)^{(1/3)})/(-a/b)^{(1/3)})/(a^3*b) + 5/18*(-a*b^2)^{(1/3)}*\log(x^{(2/3)} + x^{(1/3)}*(-a/b)^{(1/3)} + (-a/b)^{(2/3)})/(a^3*b) + 1/6*(5*b*x^{(4/3)} + 8*a*x^{(1/3)})/((b*x + a)^2*a^2)$

maple [A] time = 0.01, size = 136, normalized size = 0.97

$$\frac{x^{\frac{1}{3}}}{2(bx+a)^2a} + \frac{5x^{\frac{1}{3}}}{6(bx+a)a^2} + \frac{5\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{9\left(\frac{a}{b}\right)^{\frac{2}{3}}a^2b} + \frac{5 \ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9\left(\frac{a}{b}\right)^{\frac{2}{3}}a^2b} - \frac{5 \ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{18\left(\frac{a}{b}\right)^{\frac{2}{3}}a^2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(2/3)/(b*x+a)^3,x)

[Out] $1/2*x^{(1/3)}/a/(b*x+a)^2+5/6*x^{(1/3)}/a^2/(b*x+a)+5/9/a^2/b/(a/b)^{(2/3)}*\ln(x^{(1/3)}+(a/b)^{(1/3)})-5/18/a^2/b/(a/b)^{(2/3)}*\ln(x^{(2/3)}-(a/b)^{(1/3)}*x^{(1/3)}+(a/b)^{(2/3)})+5/9/a^2/b/(a/b)^{(2/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2/(a/b)^{(1/3)}*x^{(1/3)}-1))$

maxima [A] time = 3.00, size = 151, normalized size = 1.08

$$\frac{5bx^{\frac{4}{3}} + 8ax^{\frac{1}{3}}}{6(a^2b^2x^2 + 2a^3bx + a^4)} + \frac{5\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9a^2b\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{5 \log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{18a^2b\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{5 \log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9a^2b\left(\frac{a}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(2/3)/(b*x+a)^3,x, algorithm="maxima")

[Out] $\frac{1}{6} \cdot (5 \cdot b \cdot x^{4/3} + 8 \cdot a \cdot x^{1/3}) / (a^2 \cdot b^2 \cdot x^2 + 2 \cdot a^3 \cdot b \cdot x + a^4) + \frac{5}{9} \cdot \sqrt{3} \cdot \arctan\left(\frac{1}{3} \cdot \sqrt{3} \cdot (2 \cdot x^{1/3} - (a/b)^{1/3}) / (a/b)^{1/3}\right) / (a^2 \cdot b \cdot (a/b)^{2/3}) - \frac{5}{18} \cdot \log(x^{2/3} - x^{1/3} \cdot (a/b)^{1/3} + (a/b)^{2/3}) / (a^2 \cdot b \cdot (a/b)^{2/3}) + \frac{5}{9} \cdot \log(x^{1/3} + (a/b)^{1/3}) / (a^2 \cdot b \cdot (a/b)^{2/3})$

mupad [B] time = 0.24, size = 157, normalized size = 1.12

$$\frac{\frac{4x^{1/3}}{3a} + \frac{5bx^{4/3}}{6a^2}}{a^2 + 2abx + b^2x^2} + \frac{5 \ln\left(\frac{5b^{5/3}}{a^{5/3}} + \frac{5b^2x^{1/3}}{a^2}\right)}{9a^{8/3}b^{1/3}} + \frac{\ln\left(\frac{5b^2x^{1/3}}{a^2} + \frac{b^{5/3}(-5+\sqrt{3}5i)}{2a^{5/3}}\right) (-5 + \sqrt{3}5i)}{18a^{8/3}b^{1/3}} - \frac{\ln\left(\frac{5b^2x^{1/3}}{a^2} - \frac{b^{5/3}(5+\sqrt{3}5i)}{2a^{5/3}}\right)}{18a^{8/3}b^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(2/3)*(a + b*x)^3),x)

[Out] $\left(\frac{4x^{1/3}}{3a} + \frac{5bx^{4/3}}{6a^2}\right) / (a^2 + b^2x^2 + 2abx) + \frac{5 \log\left(\frac{5b^{5/3}}{a^{5/3}} + \frac{5b^2x^{1/3}}{a^2}\right) / (9a^{8/3}b^{1/3}) + \left(\log\left(\frac{5b^2x^{1/3}}{a^2} + \frac{b^{5/3}(3^{1/2}5i - 5)}{2a^{5/3}}\right) \cdot (3^{1/2}5i - 5)\right) / (18a^{8/3}b^{1/3}) - \left(\log\left(\frac{5b^2x^{1/3}}{a^2} - \frac{b^{5/3}(3^{1/2}5i + 5)}{2a^{5/3}}\right) \cdot (3^{1/2}5i + 5)\right) / (18a^{8/3}b^{1/3})}{9a^{8/3}b^{1/3}}$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(2/3)/(b*x+a)**3,x)

[Out] Timed out

$$3.696 \quad \int \frac{1}{x^{4/3}(a+bx)^3} dx$$

Optimal. Leaf size=152

$$\frac{7\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{3a^{10/3}} - \frac{7\sqrt[3]{b} \log(a+bx)}{9a^{10/3}} + \frac{14\sqrt[3]{b} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{10/3}} - \frac{14}{3a^3\sqrt[3]{x}} + \frac{7}{6a^2\sqrt[3]{x}(a+bx)} + \frac{1}{2a\sqrt[3]{x}(a+bx)}$$

[Out] $-14/3/a^3/x^{(1/3)}+1/2/a/x^{(1/3)}/(b*x+a)^2+7/6/a^2/x^{(1/3)}/(b*x+a)+7/3*b^{(1/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(10/3)}-7/9*b^{(1/3)}*\ln(b*x+a)/a^{(10/3)}+14/9*b^{(1/3)}*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)*3^{(1/2)}})/a^{(10/3)*3^{(1/2)}}$

Rubi [A] time = 0.06, antiderivative size = 152, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 56, 617, 204, 31}

$$\frac{7}{6a^2\sqrt[3]{x}(a+bx)} + \frac{7\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{3a^{10/3}} - \frac{7\sqrt[3]{b} \log(a+bx)}{9a^{10/3}} + \frac{14\sqrt[3]{b} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{10/3}} - \frac{14}{3a^3\sqrt[3]{x}} + \frac{1}{2a\sqrt[3]{x}(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(4/3)*(a + b*x)^3), x]

[Out] $-14/(3*a^3*x^{(1/3)}) + 1/(2*a*x^{(1/3)}*(a + b*x)^2) + 7/(6*a^2*x^{(1/3)}*(a + b*x)) + (14*b^{(1/3)}*ArcTan[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(Sqrt[3]*a^{(1/3)})])/(3*Sqrt[3]*a^{(10/3)}) + (7*b^{(1/3)}*Log[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(3*a^{(10/3)}) - (7*b^{(1/3)}*Log[a + b*x])/(9*a^{(10/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])))] && IntLinearQ[a, b, c, d, m, n, x]

Rule 56

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q),
x] + (Dist[3/(2*b), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(1/3)]
, x] - Dist[3/(2*b*q), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)], x])] /
; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{4/3}(a+bx)^3} dx &= \frac{1}{2a\sqrt[3]{x}(a+bx)^2} + \frac{7 \int \frac{1}{x^{4/3}(a+bx)^2} dx}{6a} \\
&= \frac{1}{2a\sqrt[3]{x}(a+bx)^2} + \frac{7}{6a^2\sqrt[3]{x}(a+bx)} + \frac{14 \int \frac{1}{x^{4/3}(a+bx)} dx}{9a^2} \\
&= -\frac{14}{3a^3\sqrt[3]{x}} + \frac{1}{2a\sqrt[3]{x}(a+bx)^2} + \frac{7}{6a^2\sqrt[3]{x}(a+bx)} - \frac{(14b) \int \frac{1}{\sqrt[3]{x}(a+bx)} dx}{9a^3} \\
&= -\frac{14}{3a^3\sqrt[3]{x}} + \frac{1}{2a\sqrt[3]{x}(a+bx)^2} + \frac{7}{6a^2\sqrt[3]{x}(a+bx)} - \frac{7\sqrt[3]{b} \log(a+bx)}{9a^{10/3}} - \frac{7 \text{Subst} \left(\int \frac{1}{\frac{a^{2/3}}{b^{2/3}} - \frac{\sqrt[3]{ax}}{\sqrt[3]{b}}} + \right)}{3a^3} \\
&= -\frac{14}{3a^3\sqrt[3]{x}} + \frac{1}{2a\sqrt[3]{x}(a+bx)^2} + \frac{7}{6a^2\sqrt[3]{x}(a+bx)} + \frac{7\sqrt[3]{b} \log(\sqrt[3]{a} + \sqrt[3]{b}\sqrt[3]{x})}{3a^{10/3}} - \frac{7\sqrt[3]{b} \log(a+bx)}{9a^{10/3}} \\
&= -\frac{14}{3a^3\sqrt[3]{x}} + \frac{1}{2a\sqrt[3]{x}(a+bx)^2} + \frac{7}{6a^2\sqrt[3]{x}(a+bx)} + \frac{14\sqrt[3]{b} \tan^{-1} \left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}} \right)}{3\sqrt{3}a^{10/3}} + \frac{7\sqrt[3]{b} \log(\sqrt[3]{a})}{3a^{10/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 25, normalized size = 0.16

$$-\frac{{}_3F_1\left(-\frac{1}{3}, 3; \frac{2}{3}; -\frac{bx}{a}\right)}{a^3\sqrt[3]{x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(4/3)*(a + b*x)^3), x]

[Out] (-3*Hypergeometric2F1[-1/3, 3, 2/3, -((b*x)/a)])/(a^3*x^(1/3))

fricas [A] time = 0.51, size = 211, normalized size = 1.39

$$\frac{28\sqrt{3}(b^2x^3 + 2abx^2 + a^2x)\left(\frac{b}{a}\right)^{\frac{1}{3}} \arctan\left(\frac{2}{3}\sqrt{3}x^{\frac{1}{3}}\left(\frac{b}{a}\right)^{\frac{1}{3}} - \frac{1}{3}\sqrt{3}\right) + 14(b^2x^3 + 2abx^2 + a^2x)\left(\frac{b}{a}\right)^{\frac{1}{3}} \log\left(-ax^{\frac{1}{3}}\left(\frac{b}{a}\right)^{\frac{1}{3}}\right)}{18(a^3b^2x^3 + 2a^2bx^2 + a^3x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3)/(b*x+a)^3,x, algorithm="fricas")

[Out]
$$-1/18*(28*\sqrt{3}*(b^2*x^3 + 2*a*b*x^2 + a^2*x)*(b/a)^{1/3}*\arctan(2/3*\sqrt{3}*(3)*x^{1/3}*(b/a)^{1/3} - 1/3*\sqrt{3}) + 14*(b^2*x^3 + 2*a*b*x^2 + a^2*x)*(b/a)^{1/3}*\log(-a*x^{1/3}*(b/a)^{2/3} + b*x^{2/3} + a*(b/a)^{1/3}) - 28*(b^2*x^3 + 2*a*b*x^2 + a^2*x)*(b/a)^{1/3}*\log(a*(b/a)^{2/3} + b*x^{1/3}) + 3*(28*b^2*x^2 + 49*a*b*x + 18*a^2)*x^{2/3})/(a^3*b^2*x^3 + 2*a^4*b*x^2 + a^5*x)$$

giac [A] time = 1.16, size = 155, normalized size = 1.02

$$\frac{14 b \left(-\frac{a}{b}\right)^{\frac{2}{3}} \log\left(x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9 a^4} + \frac{14 \sqrt{3} \left(-ab^2\right)^{\frac{2}{3}} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9 a^4 b} - \frac{7 \left(-ab^2\right)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{a^3 x^{\frac{1}{3}}} - \frac{7 \left(-ab^2\right)^{\frac{2}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9 a^4 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3)/(b*x+a)^3,x, algorithm="giac")

[Out]
$$14/9*b*(-a/b)^{2/3}*\log(\text{abs}(x^{1/3} - (-a/b)^{1/3}))/a^4 + 14/9*\sqrt{3}*(-a*b^2)^{2/3}*\arctan(1/3*\sqrt{3}*(2*x^{1/3} + (-a/b)^{1/3})/(-a/b)^{1/3})/(a^4*b) - 3/(a^3*x^{1/3}) - 7/9*(-a*b^2)^{2/3}*\log(x^{2/3} + x^{1/3}*(-a/b)^{1/3} + (-a/b)^{2/3})/(a^4*b) - 1/6*(10*b^2*x^{5/3} + 13*a*b*x^{2/3})/((b*x + a)^2*a^3)$$

maple [A] time = 0.02, size = 139, normalized size = 0.91

$$\frac{5b^2x^{\frac{5}{3}}}{3(bx+a)^2a^3} - \frac{13bx^{\frac{2}{3}}}{6(bx+a)^2a^2} + \frac{14\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{2x^{\frac{1}{3}}}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}-1\right)}{3}\right)}{9\left(\frac{a}{b}\right)^{\frac{1}{3}}a^3} + \frac{14 \ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9\left(\frac{a}{b}\right)^{\frac{1}{3}}a^3} - \frac{7 \ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{9\left(\frac{a}{b}\right)^{\frac{1}{3}}a^3} - \frac{1}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(4/3)/(b*x+a)^3,x)

[Out]
$$-3/a^3/x^{1/3} - 5/3*b^2/a^3/(b*x+a)^2*x^{5/3} - 13/6*b/a^2/(b*x+a)^2*x^{2/3} + 14/9/a^3/(a/b)^{1/3}*\ln(x^{1/3} + (a/b)^{1/3}) - 7/9/a^3/(a/b)^{1/3}*\ln(x^{2/3} - (a/b)^{1/3}*x^{1/3} + (a/b)^{2/3}) - 14/9/a^3*3^{1/2}/(a/b)^{1/3}*\arctan(1/3*3^{1/2}*(2/(a/b)^{1/3}*x^{1/3} - 1))$$

maxima [A] time = 2.99, size = 154, normalized size = 1.01

$$\frac{28 b^2 x^2 + 49 a b x + 18 a^2}{6 \left(a^3 b^2 x^{\frac{7}{3}} + 2 a^4 b x^{\frac{4}{3}} + a^5 x^{\frac{1}{3}} \right)} - \frac{14 \sqrt{3} \arctan \left(\frac{\sqrt{3} \left(2 x^{\frac{1}{3}} - \left(\frac{a}{b} \right)^{\frac{1}{3}} \right)}{3 \left(\frac{a}{b} \right)^{\frac{1}{3}}} \right)}{9 a^3 \left(\frac{a}{b} \right)^{\frac{1}{3}}} - \frac{7 \log \left(x^{\frac{2}{3}} - x^{\frac{1}{3}} \left(\frac{a}{b} \right)^{\frac{1}{3}} + \left(\frac{a}{b} \right)^{\frac{2}{3}} \right)}{9 a^3 \left(\frac{a}{b} \right)^{\frac{1}{3}}} + \frac{14 \log \left(x^{\frac{1}{3}} + \left(\frac{a}{b} \right)^{\frac{1}{3}} \right)}{9 a^3 \left(\frac{a}{b} \right)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(4/3)/(b*x+a)^3,x, algorithm="maxima")

[Out] $-1/6*(28*b^2*x^2 + 49*a*b*x + 18*a^2)/(a^3*b^2*x^{7/3} + 2*a^4*b*x^{4/3} + a^5*x^{1/3}) - 14/9*\text{sqrt}(3)*\arctan(1/3*\text{sqrt}(3)*(2*x^{1/3} - (a/b)^{1/3})/(a/b)^{1/3})/(a^3*(a/b)^{1/3}) - 7/9*\log(x^{2/3} - x^{1/3}*(a/b)^{1/3} + (a/b)^{2/3})/(a^3*(a/b)^{1/3}) + 14/9*\log(x^{1/3} + (a/b)^{1/3})/(a^3*(a/b)^{1/3})$

mupad [B] time = 0.09, size = 174, normalized size = 1.14

$$\frac{14 b^{1/3} \ln \left(588 a^{10/3} b^{8/3} + 588 a^3 b^3 x^{1/3} \right)}{9 a^{10/3}} - \frac{\frac{3}{a} + \frac{14 b^2 x^2}{3 a^3} + \frac{49 b x}{6 a^2}}{a^2 x^{1/3} + b^2 x^{7/3} + 2 a b x^{4/3}} + \frac{14 b^{1/3} \ln \left(588 a^{10/3} b^{8/3} \left(-\frac{1}{2} + \frac{\sqrt{3} i}{2} \right)^2 \right)}{9 a^{10/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(4/3)*(a + b*x)^3),x)

[Out] $(14*b^{1/3}*\log(588*a^{10/3}*b^{8/3} + 588*a^3*b^3*x^{1/3}))/ (9*a^{10/3}) - (3/a + (14*b^2*x^2)/(3*a^3) + (49*b*x)/(6*a^2))/ (a^2*x^{1/3} + b^2*x^{7/3} + 2*a*b*x^{4/3}) + (14*b^{1/3}*\log(588*a^{10/3}*b^{8/3}*((3^{1/2})*i)/2 - 1/2)^2 + 588*a^3*b^3*x^{1/3})*((3^{1/2})*i)/2 - 1/2)/ (9*a^{10/3}) - (14*b^{1/3}*\log(588*a^{10/3}*b^{8/3}*((3^{1/2})*i)/2 + 1/2)^2 + 588*a^3*b^3*x^{1/3})*((3^{1/2})*i)/2 + 1/2)/ (9*a^{10/3})$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(4/3)/(b*x+a)**3,x)

[Out] Timed out

$$3.697 \quad \int \frac{1}{x^{5/3}(a+bx)^3} dx$$

Optimal. Leaf size=152

$$-\frac{10b^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{3a^{11/3}} + \frac{10b^{2/3} \log(a+bx)}{9a^{11/3}} + \frac{20b^{2/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{11/3}} - \frac{10}{3a^3x^{2/3}} + \frac{4}{3a^2x^{2/3}(a+bx)} + \frac{1}{2ax^{2/3}(a+bx)}$$

[Out] $-10/3/a^3/x^{(2/3)}+1/2/a/x^{(2/3)}/(b*x+a)^2+4/3/a^2/x^{(2/3)}/(b*x+a)-10/3*b^{(2/3)}*\ln(a^{(1/3)}+b^{(1/3)}*x^{(1/3)})/a^{(11/3)}+10/9*b^{(2/3)}*\ln(b*x+a)/a^{(11/3)}+20/9*b^{(2/3)}*\arctan(1/3*(a^{(1/3)}-2*b^{(1/3)}*x^{(1/3)})/a^{(1/3)}*3^{(1/2)})/a^{(11/3)}*3^{(1/2)}$

Rubi [A] time = 0.06, antiderivative size = 152, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {51, 58, 617, 204, 31}

$$-\frac{10b^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{3a^{11/3}} + \frac{10b^{2/3} \log(a+bx)}{9a^{11/3}} + \frac{20b^{2/3} \tan^{-1}\left(\frac{\sqrt[3]{a}-2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt{3}\sqrt[3]{a}}\right)}{3\sqrt{3}a^{11/3}} + \frac{4}{3a^2x^{2/3}(a+bx)} - \frac{10}{3a^3x^{2/3}} + \frac{1}{2ax^{2/3}(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(x^(5/3)*(a + b*x)^3), x]

[Out] $-10/(3*a^3*x^{(2/3)}) + 1/(2*a*x^{(2/3)}*(a + b*x)^2) + 4/(3*a^2*x^{(2/3)}*(a + b*x)) + (20*b^{(2/3)}*ArcTan[(a^{(1/3)} - 2*b^{(1/3)}*x^{(1/3)})/(Sqrt[3]*a^{(1/3)})])/(3*Sqrt[3]*a^{(11/3)}) - (10*b^{(2/3)}*Log[a^{(1/3)} + b^{(1/3)}*x^{(1/3)}])/(3*a^{(11/3)}) + (10*b^{(2/3)}*Log[a + b*x])/(9*a^{(11/3)})$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 58

```
Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[
{q = Rt[-((b*c - a*d)/b), 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^
2), x] + (Dist[3/(2*b*q), Subst[Int[1/(q^2 - q*x + x^2), x], x, (c + d*x)^(
1/3)], x] + Dist[3/(2*b*q^2), Subst[Int[1/(q + x), x], x, (c + d*x)^(1/3)],
x])] /; FreeQ[{a, b, c, d}, x] && NegQ[(b*c - a*d)/b]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^{5/3}(a+bx)^3} dx &= \frac{1}{2ax^{2/3}(a+bx)^2} + \frac{4 \int \frac{1}{x^{5/3}(a+bx)^2} dx}{3a} \\
&= \frac{1}{2ax^{2/3}(a+bx)^2} + \frac{4}{3a^2x^{2/3}(a+bx)} + \frac{20 \int \frac{1}{x^{5/3}(a+bx)} dx}{9a^2} \\
&= -\frac{10}{3a^3x^{2/3}} + \frac{1}{2ax^{2/3}(a+bx)^2} + \frac{4}{3a^2x^{2/3}(a+bx)} - \frac{(20b) \int \frac{1}{x^{2/3}(a+bx)} dx}{9a^3} \\
&= -\frac{10}{3a^3x^{2/3}} + \frac{1}{2ax^{2/3}(a+bx)^2} + \frac{4}{3a^2x^{2/3}(a+bx)} + \frac{10b^{2/3} \log(a+bx)}{9a^{11/3}} - \frac{(10\sqrt[3]{b}) \operatorname{Subst} \left(\int \frac{a^{2/3}}{b^{2/3}} \right)}{3a^{11/3}} \\
&= -\frac{10}{3a^3x^{2/3}} + \frac{1}{2ax^{2/3}(a+bx)^2} + \frac{4}{3a^2x^{2/3}(a+bx)} - \frac{10b^{2/3} \log(\sqrt[3]{a} + \sqrt[3]{b} \sqrt[3]{x})}{3a^{11/3}} + \frac{10b^{2/3} \log(a)}{9a^{11/3}} \\
&= -\frac{10}{3a^3x^{2/3}} + \frac{1}{2ax^{2/3}(a+bx)^2} + \frac{4}{3a^2x^{2/3}(a+bx)} + \frac{20b^{2/3} \tan^{-1} \left(\frac{1 - \frac{2\sqrt[3]{b}\sqrt[3]{x}}{\sqrt[3]{a}}}{\sqrt{3}} \right)}{3\sqrt{3}a^{11/3}} - \frac{10b^{2/3} \log(\sqrt[3]{a})}{3a^{11/3}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 27, normalized size = 0.18

$$-\frac{{}_3F_1\left(-\frac{2}{3}, 3; \frac{1}{3}; -\frac{bx}{a}\right)}{2a^3x^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^(5/3)*(a + b*x)^3), x]

[Out] (-3*Hypergeometric2F1[-2/3, 3, 1/3, -((b*x)/a)])/(2*a^3*x^(2/3))

fricas [B] time = 0.49, size = 244, normalized size = 1.61

$$40\sqrt{3}(b^2x^3 + 2abx^2 + a^2x)\left(-\frac{b^2}{a^2}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}ax^{\frac{1}{3}}\left(-\frac{b^2}{a^2}\right)^{\frac{2}{3}} - \sqrt{3}b}{3b}\right) - 20(b^2x^3 + 2abx^2 + a^2x)\left(-\frac{b^2}{a^2}\right)^{\frac{1}{3}} \log\left(b^2x^{\frac{2}{3}} + a\right)$$

$$18(a^3b^2x^3 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/3)/(b*x+a)^3,x, algorithm="fricas")

[Out] $\frac{1}{18} \cdot (40 \cdot \sqrt{3}) \cdot (b^2 x^3 + 2 a b x^2 + a^2 x) \cdot (-b^2/a^2)^{1/3} \cdot \arctan\left(\frac{1/3 \cdot (2 \cdot \sqrt{3}) \cdot a \cdot x^{1/3} \cdot (-b^2/a^2)^{2/3} - \sqrt{3} \cdot b}{b}\right) - 20 \cdot (b^2 x^3 + 2 a b x^2 + a^2 x) \cdot (-b^2/a^2)^{1/3} \cdot \log(b^2 x^{2/3} + a b x^{1/3} \cdot (-b^2/a^2)^{1/3} + a^2 \cdot (-b^2/a^2)^{2/3}) + 40 \cdot (b^2 x^3 + 2 a b x^2 + a^2 x) \cdot (-b^2/a^2)^{1/3} \cdot \log(b x^{1/3} - a \cdot (-b^2/a^2)^{1/3}) - 3 \cdot (20 b^2 x^2 + 32 a b x + 9 a^2) \cdot x^{1/3} / (a^3 b^2 x^3 + 2 a^4 b x^2 + a^5 x)$

giac [A] time = 1.08, size = 150, normalized size = 0.99

$$\frac{20 b \left(-\frac{a}{b}\right)^{\frac{1}{3}} \log\left(\left|x^{\frac{1}{3}} - \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right|\right)}{9 a^4} - \frac{20 \sqrt{3} \left(-a b^2\right)^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(2 x^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(-\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9 a^4} - \frac{10 \left(-a b^2\right)^{\frac{1}{3}} \log\left(x^{\frac{2}{3}} + x^{\frac{1}{3}}\left(-\frac{a}{b}\right)^{\frac{1}{3}} + \left(-\frac{a}{b}\right)^{\frac{2}{3}}\right)}{9 a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/3)/(b*x+a)^3,x, algorithm="giac")

[Out] $\frac{20}{9} b \cdot (-a/b)^{1/3} \cdot \log(\text{abs}(x^{1/3} - (-a/b)^{1/3}))/a^4 - \frac{20}{9} \sqrt{3} \cdot (-a b^2)^{1/3} \cdot \arctan(1/3 \cdot \sqrt{3} \cdot (2 x^{1/3} + (-a/b)^{1/3})/(-a/b)^{1/3})/a^4 - \frac{10}{9} \cdot (-a b^2)^{1/3} \cdot \log(x^{2/3} + x^{1/3} \cdot (-a/b)^{1/3} + (-a/b)^{2/3})/a^4 - \frac{1}{6} \cdot (20 b^2 x^2 + 32 a b x + 9 a^2) / ((b x^{4/3} + a x^{1/3})^2 a^3)$

maple [A] time = 0.02, size = 139, normalized size = 0.91

$$\frac{\frac{11 b^2 x^{\frac{4}{3}}}{6 (b x + a)^2 a^3} - \frac{7 b x^{\frac{1}{3}}}{3 (b x + a)^2 a^2} + \frac{20 \sqrt{3} \arctan\left(\frac{\sqrt{3}\left(\frac{1}{2 x^{\frac{1}{3}} - 1}\right)}{\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9 \left(\frac{a}{b}\right)^{\frac{2}{3}} a^3} - \frac{20 \ln\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9 \left(\frac{a}{b}\right)^{\frac{2}{3}} a^3} + \frac{10 \ln\left(x^{\frac{2}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}} x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{9 \left(\frac{a}{b}\right)^{\frac{2}{3}} a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(5/3)/(b*x+a)^3,x)

[Out] $-3/2/a^3/x^{2/3} - 11/6/a^3 b^2/(b*x+a)^2 x^{4/3} - 7/3/a^2 b/(b*x+a)^2 x^{1/3} - 20/9/a^3/(a/b)^{2/3} \cdot \ln(x^{1/3} + (a/b)^{1/3}) + 10/9/a^3/(a/b)^{2/3} \cdot \ln(x^{2/3} - (a/b)^{1/3} x^{1/3} + (a/b)^{2/3}) - 20/9/a^3/(a/b)^{2/3} \cdot 3^{1/2} \cdot \arctan(1/3 \cdot 3^{1/2} \cdot (2/(a/b)^{1/3} x^{1/3} - 1))$

maxima [A] time = 2.99, size = 154, normalized size = 1.01

$$\frac{20b^2x^2 + 32abx + 9a^2}{6\left(a^3b^2x^{\frac{8}{3}} + 2a^4bx^{\frac{5}{3}} + a^5x^{\frac{2}{3}}\right)} - \frac{20\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2x^{\frac{1}{3}} - \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{a}{b}\right)^{\frac{1}{3}}}\right)}{9a^3\left(\frac{a}{b}\right)^{\frac{2}{3}}} + \frac{10 \log\left(x^{\frac{2}{3}} - x^{\frac{1}{3}}\left(\frac{a}{b}\right)^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{2}{3}}\right)}{9a^3\left(\frac{a}{b}\right)^{\frac{2}{3}}} - \frac{20 \log\left(x^{\frac{1}{3}} + \left(\frac{a}{b}\right)^{\frac{1}{3}}\right)}{9a^3\left(\frac{a}{b}\right)^{\frac{2}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(5/3)/(b*x+a)^3,x, algorithm="maxima")

[Out] $-1/6*(20*b^2*x^2 + 32*a*b*x + 9*a^2)/(a^3*b^2*x^{8/3} + 2*a^4*b*x^{5/3} + a^5*x^{2/3}) - 20/9*\sqrt{3}*\arctan(1/3*\sqrt{3}*(2*x^{1/3} - (a/b)^{1/3})/(a/b)^{1/3})/(a^3*(a/b)^{2/3}) + 10/9*\log(x^{2/3} - x^{1/3}*(a/b)^{1/3} + (a/b)^{2/3})/(a^3*(a/b)^{2/3}) - 20/9*\log(x^{1/3} + (a/b)^{1/3})/(a^3*(a/b)^{2/3})$

mupad [B] time = 0.17, size = 182, normalized size = 1.20

$$\frac{20b^{2/3} \ln\left(540(-a)^{19/3}b^{8/3} - 540a^6b^3x^{1/3}\right)}{9(-a)^{11/3}} - \frac{\frac{3}{2a} + \frac{10b^2x^2}{3a^3} + \frac{16bx}{3a^2}}{a^2x^{2/3} + b^2x^{8/3} + 2abx^{5/3}} + \frac{20b^{2/3} \ln\left(540(-a)^{19/3}b^{8/3}\left(-\frac{1}{2} + \frac{\sqrt{3}}{2}\right)\right)}{9(-a)^{11/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(5/3)*(a + b*x)^3),x)

[Out] $(20*b^{2/3}*log(540*(-a)^{(19/3)}*b^{8/3} - 540*a^6*b^3*x^{1/3}))/ (9*(-a)^{(11/3)}) - (3/(2*a) + (10*b^2*x^2)/(3*a^3) + (16*b*x)/(3*a^2))/(a^2*x^{2/3} + b^2*x^{8/3} + 2*a*b*x^{5/3}) + (20*b^{2/3}*log(540*(-a)^{(19/3)}*b^{8/3}*((3^{(1/2)}*i)/2 - 1/2) - 540*a^6*b^3*x^{1/3})*((3^{(1/2)}*i)/2 - 1/2))/ (9*(-a)^{(11/3)}) - (20*b^{2/3}*log(540*(-a)^{(19/3)}*b^{8/3}*((3^{(1/2)}*i)/2 + 1/2) + 540*a^6*b^3*x^{1/3})*((3^{(1/2)}*i)/2 + 1/2))/ (9*(-a)^{(11/3)})$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(5/3)/(b*x+a)**3,x)

[Out] Timed out

$$3.698 \quad \int \frac{\sqrt[4]{1-x}}{1+x} dx$$

Optimal. Leaf size=58

$$4\sqrt[4]{1-x} - 2\sqrt[4]{2} \tan^{-1}\left(\frac{\sqrt[4]{1-x}}{\sqrt[4]{2}}\right) - 2\sqrt[4]{2} \tanh^{-1}\left(\frac{\sqrt[4]{1-x}}{\sqrt[4]{2}}\right)$$

[Out] $4*(1-x)^{(1/4)} - 2*2^{(1/4)}*\arctan(1/2*(1-x)^{(1/4)}*2^{(3/4)}) - 2*2^{(1/4)}*\operatorname{arctanh}(1/2*(1-x)^{(1/4)}*2^{(3/4)})$

Rubi [A] time = 0.02, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {50, 63, 212, 206, 203}

$$4\sqrt[4]{1-x} - 2\sqrt[4]{2} \tan^{-1}\left(\frac{\sqrt[4]{1-x}}{\sqrt[4]{2}}\right) - 2\sqrt[4]{2} \tanh^{-1}\left(\frac{\sqrt[4]{1-x}}{\sqrt[4]{2}}\right)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(1-x)^{(1/4)}/(1+x), x]$

[Out] $4*(1-x)^{(1/4)} - 2*2^{(1/4)}*\text{ArcTan}[(1-x)^{(1/4)}/2^{(1/4)}] - 2*2^{(1/4)}*\text{ArcTanh}[(1-x)^{(1/4)}/2^{(1/4)}]$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n)}/(b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m+n+1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m-n, 0]))) && !ILtQ[m+n+2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

$\text{Int}[(a_. + (b_.)*(x_)^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(1*\text{ArcTan}[\text{Rt}[b, 2]*x]/\text{Rt}[a, 2])]/(\text{Rt}[a, 2]*\text{Rt}[b, 2]), x] /;$ FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a

, 0] || GtQ[b, 0])

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[Rt[-b, 2]*x]/Rt[a, 2])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 212

Int[((a_) + (b_.)*(x_)^4)^(-1), x_Symbol] := With[{r = Numerator[Rt[-(a/b), 2]], s = Denominator[Rt[-(a/b), 2]]}, Dist[r/(2*a), Int[1/(r - s*x^2), x], x] + Dist[r/(2*a), Int[1/(r + s*x^2), x], x]] /; FreeQ[{a, b}, x] && !GtQ[a/b, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt[4]{1-x}}{1+x} dx &= 4\sqrt[4]{1-x} + 2 \int \frac{1}{(1-x)^{3/4}(1+x)} dx \\ &= 4\sqrt[4]{1-x} - 8 \operatorname{Subst} \left(\int \frac{1}{2-x^4} dx, x, \sqrt[4]{1-x} \right) \\ &= 4\sqrt[4]{1-x} - (2\sqrt{2}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{2}-x^2} dx, x, \sqrt[4]{1-x} \right) - (2\sqrt{2}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{2}+x^2} dx, x, \sqrt[4]{1-x} \right) \\ &= 4\sqrt[4]{1-x} - 2\sqrt{2} \tan^{-1} \left(\frac{\sqrt[4]{1-x}}{\sqrt{2}} \right) - 2\sqrt{2} \tanh^{-1} \left(\frac{\sqrt[4]{1-x}}{\sqrt{2}} \right) \end{aligned}$$

Mathematica [A] time = 0.02, size = 58, normalized size = 1.00

$$4\sqrt[4]{1-x} - 2\sqrt{2} \tan^{-1} \left(\frac{\sqrt[4]{1-x}}{\sqrt{2}} \right) - 2\sqrt{2} \tanh^{-1} \left(\frac{\sqrt[4]{1-x}}{\sqrt{2}} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(1/4)/(1 + x), x]

[Out] 4*(1 - x)^(1/4) - 2*2^(1/4)*ArcTan[(1 - x)^(1/4)/2^(1/4)] - 2*2^(1/4)*ArcTanh[(1 - x)^(1/4)/2^(1/4)]

fricas [A] time = 0.52, size = 82, normalized size = 1.41

$$4 \cdot 2^{\frac{1}{4}} \arctan \left(\frac{1}{2} \cdot 2^{\frac{3}{4}} \sqrt{\sqrt{2} + \sqrt{-x+1}} - \frac{1}{2} \cdot 2^{\frac{3}{4}} (-x+1)^{\frac{1}{4}} \right) - 2^{\frac{1}{4}} \log \left(2^{\frac{1}{4}} + (-x+1)^{\frac{1}{4}} \right) + 2^{\frac{1}{4}} \log \left(-2^{\frac{1}{4}} + (-x+1)^{\frac{1}{4}} \right) + 4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/4)/(1+x),x, algorithm="fricas")

[Out] $4 \cdot 2^{1/4} \cdot \arctan(1/2 \cdot 2^{3/4} \cdot \sqrt{\sqrt{2} + \sqrt{-x + 1}}) - 1/2 \cdot 2^{3/4} \cdot (-x + 1)^{1/4} - 2^{1/4} \cdot \log(2^{1/4} + (-x + 1)^{1/4}) + 2^{1/4} \cdot \log(-2^{1/4} + (-x + 1)^{1/4}) + 4 \cdot (-x + 1)^{1/4}$

giac [A] time = 1.17, size = 64, normalized size = 1.10

$$-2 \cdot 2^{1/4} \arctan\left(\frac{1}{2} \cdot 2^{3/4} (-x + 1)^{1/4}\right) - 2^{1/4} \log\left(2^{1/4} + (-x + 1)^{1/4}\right) + 2^{1/4} \log\left(-2^{1/4} + (-x + 1)^{1/4}\right) + 4(-x + 1)^{1/4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/4)/(1+x),x, algorithm="giac")

[Out] $-2 \cdot 2^{1/4} \cdot \arctan(1/2 \cdot 2^{3/4} \cdot (-x + 1)^{1/4}) - 2^{1/4} \cdot \log(2^{1/4} + (-x + 1)^{1/4}) + 2^{1/4} \cdot \log(\text{abs}(-2^{1/4} + (-x + 1)^{1/4})) + 4 \cdot (-x + 1)^{1/4}$

maple [A] time = 0.01, size = 62, normalized size = 1.07

$$-2 \cdot 2^{1/4} \arctan\left(\frac{(-x + 1)^{1/4} \cdot 2^{3/4}}{2}\right) - 2^{1/4} \ln\left(\frac{(-x + 1)^{1/4} + 2^{1/4}}{(-x + 1)^{1/4} - 2^{1/4}}\right) + 4(-x + 1)^{1/4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(1/4)/(1+x),x)

[Out] $4 \cdot (-x + 1)^{1/4} - 2 \cdot 2^{1/4} \cdot \arctan(1/2 \cdot (-x + 1)^{1/4} \cdot 2^{3/4}) - 2^{1/4} \cdot \ln\left(\frac{(-x + 1)^{1/4} + 2^{1/4}}{(-x + 1)^{1/4} - 2^{1/4}}\right)$

maxima [A] time = 2.91, size = 61, normalized size = 1.05

$$-2 \cdot 2^{1/4} \arctan\left(\frac{1}{2} \cdot 2^{3/4} (-x + 1)^{1/4}\right) + 2^{1/4} \log\left(-\frac{2^{1/4} - (-x + 1)^{1/4}}{2^{1/4} + (-x + 1)^{1/4}}\right) + 4(-x + 1)^{1/4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/4)/(1+x),x, algorithm="maxima")

[Out] $-2 \cdot 2^{1/4} \cdot \arctan(1/2 \cdot 2^{3/4} \cdot (-x + 1)^{1/4}) + 2^{1/4} \cdot \log\left(\frac{-2^{1/4} - (-x + 1)^{1/4}}{2^{1/4} + (-x + 1)^{1/4}}\right) + 4 \cdot (-x + 1)^{1/4}$

mupad [B] time = 0.07, size = 46, normalized size = 0.79

$$4(1 - x)^{1/4} - 2 \cdot 2^{1/4} \operatorname{atanh}\left(\frac{2^{3/4} (1 - x)^{1/4}}{2}\right) - 2 \cdot 2^{1/4} \operatorname{atan}\left(\frac{2^{3/4} (1 - x)^{1/4}}{2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(1/4)/(x + 1), x)`

[Out] $4*(1 - x)^{1/4} - 2*2^{1/4}*atanh((2^{3/4}*(1 - x)^{1/4})/2) - 2*2^{1/4}*atan((2^{3/4}*(1 - x)^{1/4})/2)$

sympy [C] time = 2.35, size = 243, normalized size = 4.19

$$\frac{5\sqrt[4]{-1}\sqrt[4]{x-1}\Gamma\left(\frac{5}{4}\right)}{\Gamma\left(\frac{9}{4}\right)} + \frac{5\sqrt[4]{-2}e^{-\frac{i\pi}{4}}\log\left(-\frac{2^{\frac{3}{4}}\sqrt[4]{x-1}e^{\frac{i\pi}{4}}}{2} + 1\right)\Gamma\left(\frac{5}{4}\right)}{4\Gamma\left(\frac{9}{4}\right)} - \frac{5(-1)^{\frac{3}{4}}\sqrt[4]{2}e^{-\frac{i\pi}{4}}\log\left(-\frac{2^{\frac{3}{4}}\sqrt[4]{x-1}e^{\frac{3i\pi}{4}}}{2} + 1\right)\Gamma\left(\frac{5}{4}\right)}{4\Gamma\left(\frac{9}{4}\right)} - \frac{5\sqrt[4]{-2}}{\Gamma\left(\frac{9}{4}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(1/4)/(1+x), x)`

[Out] $5*(-1)**(1/4)*(x - 1)**(1/4)*gamma(5/4)/gamma(9/4) + 5*(-2)**(1/4)*exp(-I*pi/4)*log(-2**(3/4)*(x - 1)**(1/4)*exp_polar(I*pi/4)/2 + 1)*gamma(5/4)/(4*gamma(9/4)) - 5*(-1)**(3/4)*2**(1/4)*exp(-I*pi/4)*log(-2**(3/4)*(x - 1)**(1/4)*exp_polar(3*I*pi/4)/2 + 1)*gamma(5/4)/(4*gamma(9/4)) - 5*(-2)**(1/4)*exp(-I*pi/4)*log(-2**(3/4)*(x - 1)**(1/4)*exp_polar(5*I*pi/4)/2 + 1)*gamma(5/4)/(4*gamma(9/4)) + 5*(-1)**(3/4)*2**(1/4)*exp(-I*pi/4)*log(-2**(3/4)*(x - 1)**(1/4)*exp_polar(7*I*pi/4)/2 + 1)*gamma(5/4)/(4*gamma(9/4))$

3.699 $\int x^m(a + bx)^{10} dx$

Optimal. Leaf size=187

$$\frac{a^{10}x^{m+1}}{m+1} + \frac{10a^9bx^{m+2}}{m+2} + \frac{45a^8b^2x^{m+3}}{m+3} + \frac{120a^7b^3x^{m+4}}{m+4} + \frac{210a^6b^4x^{m+5}}{m+5} + \frac{252a^5b^5x^{m+6}}{m+6} + \frac{210a^4b^6x^{m+7}}{m+7} + \frac{120a^3b^7x^{m+8}}{m+8} + \frac{45a^2b^8x^{m+9}}{m+9} + \frac{10a^1b^9x^{m+10}}{m+10} + \frac{b^{10}x^{m+11}}{m+11}$$

[Out] $a^{10}x^{(1+m)/(1+m)} + 10a^9b^1x^{(2+m)/(2+m)} + 45a^8b^2x^{(3+m)/(3+m)} + 120a^7b^3x^{(4+m)/(4+m)} + 210a^6b^4x^{(5+m)/(5+m)} + 252a^5b^5x^{(6+m)/(6+m)} + 210a^4b^6x^{(7+m)/(7+m)} + 120a^3b^7x^{(8+m)/(8+m)} + 45a^2b^8x^{(9+m)/(9+m)} + 10a^1b^9x^{(10+m)/(10+m)} + b^{10}x^{(11+m)/(11+m)}$

Rubi [A] time = 0.08, antiderivative size = 187, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{45a^8b^2x^{m+3}}{m+3} + \frac{120a^7b^3x^{m+4}}{m+4} + \frac{210a^6b^4x^{m+5}}{m+5} + \frac{252a^5b^5x^{m+6}}{m+6} + \frac{210a^4b^6x^{m+7}}{m+7} + \frac{120a^3b^7x^{m+8}}{m+8} + \frac{45a^2b^8x^{m+9}}{m+9} + \frac{10a^1b^9x^{m+10}}{m+10} + \frac{b^{10}x^{m+11}}{m+11}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x)^10, x]

[Out] $(a^{10}x^{(1+m)/(1+m)})/(1+m) + (10a^9b^1x^{(2+m)/(2+m)})/(2+m) + (45a^8b^2x^{(3+m)/(3+m)})/(3+m) + (120a^7b^3x^{(4+m)/(4+m)})/(4+m) + (210a^6b^4x^{(5+m)/(5+m)})/(5+m) + (252a^5b^5x^{(6+m)/(6+m)})/(6+m) + (210a^4b^6x^{(7+m)/(7+m)})/(7+m) + (120a^3b^7x^{(8+m)/(8+m)})/(8+m) + (45a^2b^8x^{(9+m)/(9+m)})/(9+m) + (10a^1b^9x^{(10+m)/(10+m)})/(10+m) + (b^{10}x^{(11+m)/(11+m)})/(11+m)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int x^m(a + bx)^{10} dx = \int (a^{10}x^m + 10a^9bx^{1+m} + 45a^8b^2x^{2+m} + 120a^7b^3x^{3+m} + 210a^6b^4x^{4+m} + 252a^5b^5x^{5+m} + 210a^4b^6x^{6+m} + 120a^3b^7x^{7+m} + 45a^2b^8x^{8+m} + 10a^1b^9x^{9+m} + b^{10}x^{10+m}) dx$$

$$= \frac{a^{10}x^{1+m}}{1+m} + \frac{10a^9bx^{2+m}}{2+m} + \frac{45a^8b^2x^{3+m}}{3+m} + \frac{120a^7b^3x^{4+m}}{4+m} + \frac{210a^6b^4x^{5+m}}{5+m} + \frac{252a^5b^5x^{6+m}}{6+m} + \frac{210a^4b^6x^{7+m}}{7+m} + \frac{120a^3b^7x^{8+m}}{8+m} + \frac{45a^2b^8x^{9+m}}{9+m} + \frac{10a^1b^9x^{10+m}}{10+m} + \frac{b^{10}x^{11+m}}{11+m}$$

Mathematica [A] time = 0.11, size = 166, normalized size = 0.89

$$x^{m+1} \left(\frac{a^{10}}{m+1} + \frac{10a^9bx}{m+2} + \frac{45a^8b^2x^2}{m+3} + \frac{120a^7b^3x^3}{m+4} + \frac{210a^6b^4x^4}{m+5} + \frac{252a^5b^5x^5}{m+6} + \frac{210a^4b^6x^6}{m+7} + \frac{120a^3b^7x^7}{m+8} + \frac{45a^2b^8x^8}{m+9} + \frac{10ab^9x^9}{m+10} + \frac{b^{10}x^{10}}{m+11} \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x)^10,x]

[Out] x^(1 + m)*(a^10/(1 + m) + (10*a^9*b*x)/(2 + m) + (45*a^8*b^2*x^2)/(3 + m) + (120*a^7*b^3*x^3)/(4 + m) + (210*a^6*b^4*x^4)/(5 + m) + (252*a^5*b^5*x^5)/(6 + m) + (210*a^4*b^6*x^6)/(7 + m) + (120*a^3*b^7*x^7)/(8 + m) + (45*a^2*b^8*x^8)/(9 + m) + (10*a*b^9*x^9)/(10 + m) + (b^10*x^10)/(11 + m))

fricas [B] time = 0.51, size = 1277, normalized size = 6.83

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^10,x, algorithm="fricas")

[Out] ((b^10*m^10 + 55*b^10*m^9 + 1320*b^10*m^8 + 18150*b^10*m^7 + 157773*b^10*m^6 + 902055*b^10*m^5 + 3416930*b^10*m^4 + 8409500*b^10*m^3 + 12753576*b^10*m^2 + 10628640*b^10*m + 3628800*b^10)*x^11 + 10*(a*b^9*m^10 + 56*a*b^9*m^9 + 1365*a*b^9*m^8 + 19020*a*b^9*m^7 + 167223*a*b^9*m^6 + 965328*a*b^9*m^5 + 3686255*a*b^9*m^4 + 9133180*a*b^9*m^3 + 13926276*a*b^9*m^2 + 11655216*a*b^9*m + 3991680*a*b^9)*x^10 + 45*(a^2*b^8*m^10 + 57*a^2*b^8*m^9 + 1412*a^2*b^8*m^8 + 19962*a^2*b^8*m^7 + 177765*a^2*b^8*m^6 + 1037673*a^2*b^8*m^5 + 4000478*a^2*b^8*m^4 + 9991428*a^2*b^8*m^3 + 15335224*a^2*b^8*m^2 + 12900960*a^2*b^8*m + 4435200*a^2*b^8)*x^9 + 120*(a^3*b^7*m^10 + 58*a^3*b^7*m^9 + 1461*a^3*b^7*m^8 + 20982*a^3*b^7*m^7 + 189567*a^3*b^7*m^6 + 1121022*a^3*b^7*m^5 + 4371359*a^3*b^7*m^4 + 11024858*a^3*b^7*m^3 + 17059212*a^3*b^7*m^2 + 14444280*a^3*b^7*m + 4989600*a^3*b^7)*x^8 + 210*(a^4*b^6*m^10 + 59*a^4*b^6*m^9 + 1512*a^4*b^6*m^8 + 22086*a^4*b^6*m^7 + 202821*a^4*b^6*m^6 + 1217811*a^4*b^6*m^5 + 4814858*a^4*b^6*m^4 + 12291724*a^4*b^6*m^3 + 19216008*a^4*b^6*m^2 + 16405920*a^4*b^6*m + 5702400*a^4*b^6)*x^7 + 252*(a^5*b^5*m^10 + 60*a^5*b^5*m^9 + 1565*a^5*b^5*m^8 + 23280*a^5*b^5*m^7 + 217743*a^5*b^5*m^6 + 1331100*a^5*b^5*m^5 + 5352935*a^5*b^5*m^4 + 13878120*a^5*b^5*m^3 + 21989356*a^5*b^5*m^2 + 18981840*a^5*b^5*m + 6652800*a^5*b^5)*x^6 + 210*(a^6*b^4*m^10 + 61*a^6*b^4*m^9 + 1620*a^6*b^4*m^8 + 24570*a^6*b^4*m^7 + 234573*a^6*b^4*m^6 + 1464693*a^6*b^4*m^5 + 6016070*a^6*b^4*m^4 + 15915380*a^6*b^4*m^3 + 25681176*a^6*b^4*m^2 + 22512096*a^6*b^4*m + 7983360*a^6*b^4)*x^5 + 120*(a^7*b^3*m^10 + 62*a^7*b^3*m^9 + 1677*a^7*b^3*m^8 + 25962*a^7*b^3*m^7 + 253575*a^7*b^3*m^6 + 1623258*a^7*b^3*m^5 + 6846503*a^7*b^3*m^4 + 18609718*a^7*b^3*m^3 + 30819204*a^7*b^3*m^2 + 27641160*a^7*b^3*m + 9979200*a^7*b^3)*x^4 + 45*(a^8*b^2*m^10 + 55*a^8*b^2*m^9 + 1320*a^8*b^2*m^8 + 18150*a^8*b^2*m^7 + 157773*a^8*b^2*m^6 + 902055*a^8*b^2*m^5 + 3416930*a^8*b^2*m^4 + 8409500*a^8*b^2*m^3 + 12753576*a^8*b^2*m^2 + 10628640*a^8*b^2*m + 3628800*a^8*b^2)*x^3 + 10*(a^9*b*m^10 + 56*a^9*b*m^9 + 1365*a^9*b*m^8 + 19020*a^9*b*m^7 + 167223*a^9*b*m^6 + 965328*a^9*b*m^5 + 3686255*a^9*b*m^4 + 9133180*a^9*b*m^3 + 13926276*a^9*b*m^2 + 11655216*a^9*b*m + 3991680*a^9*b)*x^2 + 45*(a^10*b*m^10 + 55*a^10*b*m^9 + 1320*a^10*b*m^8 + 18150*a^10*b*m^7 + 157773*a^10*b*m^6 + 902055*a^10*b*m^5 + 3416930*a^10*b*m^4 + 8409500*a^10*b*m^3 + 12753576*a^10*b*m^2 + 10628640*a^10*b*m + 3628800*a^10*b)*x + 3628800*b^10*x^2 + 10628640*b^10*x + 3628800*b^10)

$$0 + 63a^8b^2m^9 + 1736a^8b^2m^8 + 27462a^8b^2m^7 + 275037a^8b^2m^6 + 1812447a^8b^2m^5 + 7902194a^8b^2m^4 + 22289148a^8b^2m^3 + 38390632a^8b^2m^2 + 35746080a^8b^2m + 13305600a^8b^2)x^3 + 10(a^9b^3m^{10} + 64a^9b^3m^9 + 1797a^9b^3m^8 + 29076a^9b^3m^7 + 299271a^9b^3m^6 + 2039016a^9b^3m^5 + 9261503a^9b^3m^4 + 27472724a^9b^3m^3 + 50312628a^9b^3m^2 + 50292720a^9b^3m + 19958400a^9b^3)x^2 + (a^{10}m^{10} + 65a^{10}m^9 + 1860a^{10}m^8 + 30810a^{10}m^7 + 326613a^{10}m^6 + 2310945a^{10}m^5 + 11028590a^{10}m^4 + 34967140a^{10}m^3 + 70290936a^{10}m^2 + 80627040a^{10}m + 39916800a^{10})x) \cdot x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800)$$

giac [B] time = 1.20, size = 1925, normalized size = 10.29

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^10,x, algorithm="giac")

[Out] $(b^{10}m^{10}x^{11}x^m + 10a*b^9m^{10}x^{10}x^m + 55b^{10}m^9x^{11}x^m + 45a^2b^8m^{10}x^9x^m + 560a*b^9m^9x^{10}x^m + 1320b^{10}m^8x^{11}x^m + 120a^3b^7m^{10}x^8x^m + 2565a^2b^8m^9x^9x^m + 13650a*b^9m^8x^{10}x^m + 18150b^{10}m^7x^{11}x^m + 210a^4b^6m^{10}x^7x^m + 6960a^3b^7m^9x^8x^m + 63540a^2b^8m^8x^9x^m + 190200a*b^9m^7x^{10}x^m + 157773b^{10}m^6x^{11}x^m + 252a^5b^5m^{10}x^6x^m + 12390a^4b^6m^9x^7x^m + 175320a^3b^7m^8x^8x^m + 898290a^2b^8m^7x^9x^m + 1672230a*b^9m^6x^{10}x^m + 902055b^{10}m^5x^{11}x^m + 210a^6b^4m^{10}x^5x^m + 15120a^5b^5m^9x^6x^m + 317520a^4b^6m^8x^7x^m + 2517840a^3b^7m^7x^8x^m + 7999425a^2b^8m^6x^9x^m + 9653280a*b^9m^5x^{10}x^m + 3416930b^{10}m^4x^{11}x^m + 120a^7b^3m^{10}x^4x^m + 12810a^6b^4m^9x^5x^m + 394380a^5b^5m^8x^6x^m + 4638060a^4b^6m^7x^7x^m + 22748040a^3b^7m^6x^8x^m + 46695285a^2b^8m^5x^9x^m + 36862550a*b^9m^4x^{10}x^m + 8409500b^{10}m^3x^{11}x^m + 45a^8b^2m^{10}x^3x^m + 7440a^7b^3m^9x^4x^m + 340200a^6b^4m^8x^5x^m + 5866560a^5b^5m^7x^6x^m + 42592410a^4b^6m^6x^7x^m + 134522640a^3b^7m^5x^8x^m + 180021510a^2b^8m^4x^9x^m + 91331800a*b^9m^3x^{10}x^m + 12753576b^{10}m^2x^{11}x^m + 10a^9b^3m^{10}x^2x^m + 2835a^8b^2m^9x^3x^m + 201240a^7b^3m^8x^4x^m + 5159700a^6b^4m^7x^5x^m + 54871236a^5b^5m^6x^6x^m + 255740310a^4b^6m^5x^7x^m + 524563080a^3b^7m^4x^8x^m + 449614260a^2b^8m^3x^9x^m + 139262760a*b^9m^2x^{10}x^m + 10628640b^{10}m^1x^{11}x^m + a^{10}m^{10}x^1x^m + 640a^9b^3m^9x^2x^m + 78120a^8b^2m^8x^3x^m + 3115440a^7b^3m^7x^4x^m + 49260330a^6b^4m^6x^5x^m + 335437200a^5b^5m^5x^6x^m + 1011120180a^4b^6m^4x^7x^m + 1322982960a^3b^7m^3x^8x^m + 690085080a^2b^8m^2x^9x^m + 116552160a*b^9m^1x^{10}x^m + 3628800b^{10}m^0x^{11}x^m + 65a^10m^9x^1x^m + 17970a^9b^3m^8x^2x^m + 1235790a^8b^2m^7x^3x^m + 30429$

$$\begin{aligned}
& 000*a^7*b^3*m^6*x^4*x^m + 307585530*a^6*b^4*m^5*x^5*x^m + 1348939620*a^5*b^5*m^4*x^6*x^m + 2581262040*a^4*b^6*m^3*x^7*x^m + 2047105440*a^3*b^7*m^2*x^8*x^m + 580543200*a^2*b^8*m*x^9*x^m + 39916800*a*b^9*x^10*x^m + 1860*a^10*m^8*x*x^m + 290760*a^9*b*m^7*x^2*x^m + 12376665*a^8*b^2*m^6*x^3*x^m + 194790960*a^7*b^3*m^5*x^4*x^m + 1263374700*a^6*b^4*m^4*x^5*x^m + 3497286240*a^5*b^5*m^3*x^6*x^m + 4035361680*a^4*b^6*m^2*x^7*x^m + 1733313600*a^3*b^7*m*x^8*x^m + 199584000*a^2*b^8*x^9*x^m + 30810*a^10*m^7*x*x^m + 2992710*a^9*b*m^6*x^2*x^m + 81560115*a^8*b^2*m^5*x^3*x^m + 821580360*a^7*b^3*m^4*x^4*x^m + 3342229800*a^6*b^4*m^3*x^5*x^m + 5541317712*a^5*b^5*m^2*x^6*x^m + 3445243200*a^4*b^6*m*x^7*x^m + 598752000*a^3*b^7*x^8*x^m + 326613*a^10*m^6*x*x^m + 20390160*a^9*b*m^5*x^2*x^m + 355598730*a^8*b^2*m^4*x^3*x^m + 2233166160*a^7*b^3*m^3*x^4*x^m + 5393046960*a^6*b^4*m^2*x^5*x^m + 4783423680*a^5*b^5*m*x^6*x^m + 1197504000*a^4*b^6*x^7*x^m + 2310945*a^10*m^5*x*x^m + 92615030*a^9*b*m^4*x^2*x^m + 1003011660*a^8*b^2*m^3*x^3*x^m + 3698304480*a^7*b^3*m^2*x^4*x^m + 4727540160*a^6*b^4*m*x^5*x^m + 1676505600*a^5*b^5*x^6*x^m + 11028590*a^10*m^4*x*x^m + 274727240*a^9*b*m^3*x^2*x^m + 1727578440*a^8*b^2*m^2*x^3*x^m + 3316939200*a^7*b^3*m*x^4*x^m + 1676505600*a^6*b^4*x^5*x^m + 34967140*a^10*m^3*x*x^m + 503126280*a^9*b*m^2*x^2*x^m + 1608573600*a^8*b^2*m*x^3*x^m + 1197504000*a^7*b^3*x^4*x^m + 70290936*a^10*m^2*x*x^m + 502927200*a^9*b*m*x^2*x^m + 598752000*a^8*b^2*x^3*x^m + 80627040*a^10*m*x*x^m + 199584000*a^9*b*x^2*x^m + 39916800*a^10*x*x^m)/(m^11 + 66*m^10 + 1925*m^9 + 32670*m^8 + 357423*m^7 + 2637558*m^6 + 13339535*m^5 + 45995730*m^4 + 105258076*m^3 + 150917976*m^2 + 120543840*m + 39916800)
\end{aligned}$$

maple [B] time = 0.01, size = 1535, normalized size = 8.21

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^m*(b*x+a)^{10},x)$

[Out] $x^{(m+1)}*(b^{10}*m^{10}*x^{10}+10*a*b^9*m^{10}*x^9+55*b^{10}*m^9*x^{10}+45*a^2*b^8*m^{10}*x^8+560*a*b^9*m^9*x^9+1320*b^{10}*m^8*x^{10}+120*a^3*b^7*m^{10}*x^7+2565*a^2*b^8*m^9*x^8+13650*a*b^9*m^8*x^9+18150*b^{10}*m^7*x^{10}+210*a^4*b^6*m^{10}*x^6+6960*a^3*b^7*m^9*x^7+63540*a^2*b^8*m^8*x^8+190200*a*b^9*m^7*x^9+157773*b^{10}*m^6*x^{10}+252*a^5*b^5*m^{10}*x^5+12390*a^4*b^6*m^9*x^6+175320*a^3*b^7*m^8*x^7+898290*a^2*b^8*m^7*x^8+1672230*a*b^9*m^6*x^9+902055*b^{10}*m^5*x^{10}+210*a^6*b^4*m^{10}*x^4+15120*a^5*b^5*m^9*x^5+317520*a^4*b^6*m^8*x^6+2517840*a^3*b^7*m^7*x^7+7999425*a^2*b^8*m^6*x^8+9653280*a*b^9*m^5*x^9+3416930*b^{10}*m^4*x^{10}+120*a^7*b^3*m^{10}*x^3+12810*a^6*b^4*m^9*x^4+394380*a^5*b^5*m^8*x^5+4638060*a^4*b^6*m^7*x^6+22748040*a^3*b^7*m^6*x^7+46695285*a^2*b^8*m^5*x^8+36862550*a*b^9*m^4*x^9+8409500*b^{10}*m^3*x^{10}+45*a^8*b^2*m^{10}*x^2+7440*a^7*b^3*m^9*x^3+34020*a^6*b^4*m^8*x^4+5866560*a^5*b^5*m^7*x^5+42592410*a^4*b^6*m^6*x^6+134522640*a^3*b^7*m^5*x^7+180021510*a^2*b^8*m^4*x^8+91331800*a*b^9*m^3*x^9+12753576*b^{10}*m^2*x^{10}+10*a^9*b*m^{10}*x+2835*a^8*b^2*m^9*x^2+201240*a^7*b^3*m^8*x^3+$

5159700*a^6*b^4*m^7*x^4+54871236*a^5*b^5*m^6*x^5+255740310*a^4*b^6*m^5*x^6+524563080*a^3*b^7*m^4*x^7+449614260*a^2*b^8*m^3*x^8+139262760*a*b^9*m^2*x^9+10628640*b^10*m*x^10+a^10*m^10+640*a^9*b*m^9*x+78120*a^8*b^2*m^8*x^2+3115440*a^7*b^3*m^7*x^3+49260330*a^6*b^4*m^6*x^4+335437200*a^5*b^5*m^5*x^5+1011120180*a^4*b^6*m^4*x^6+1322982960*a^3*b^7*m^3*x^7+690085080*a^2*b^8*m^2*x^8+116552160*a*b^9*m*x^9+3628800*b^10*x^10+65*a^10*m^9+17970*a^9*b*m^8*x+1235790*a^8*b^2*m^7*x^2+30429000*a^7*b^3*m^6*x^3+307585530*a^6*b^4*m^5*x^4+1348939620*a^5*b^5*m^4*x^5+2581262040*a^4*b^6*m^3*x^6+2047105440*a^3*b^7*m^2*x^7+580543200*a^2*b^8*m*x^8+39916800*a*b^9*x^9+1860*a^10*m^8+290760*a^9*b*m^7*x+12376665*a^8*b^2*m^6*x^2+194790960*a^7*b^3*m^5*x^3+1263374700*a^6*b^4*m^4*x^4+3497286240*a^5*b^5*m^3*x^5+4035361680*a^4*b^6*m^2*x^6+1733313600*a^3*b^7*m*x^7+199584000*a^2*b^8*x^8+30810*a^10*m^7+2992710*a^9*b*m^6*x+81560115*a^8*b^2*m^5*x^2+821580360*a^7*b^3*m^4*x^3+3342229800*a^6*b^4*m^3*x^4+5541317712*a^5*b^5*m^2*x^5+3445243200*a^4*b^6*m*x^6+598752000*a^3*b^7*x^7+326613*a^10*m^6+20390160*a^9*b*m^5*x+355598730*a^8*b^2*m^4*x^2+2233166160*a^7*b^3*m^3*x^3+5393046960*a^6*b^4*m^2*x^4+4783423680*a^5*b^5*m*x^5+1197504000*a^4*b^6*x^6+2310945*a^10*m^5+92615030*a^9*b*m^4*x+1003011660*a^8*b^2*m^3*x^2+3698304480*a^7*b^3*m^2*x^3+4727540160*a^6*b^4*m*x^4+1676505600*a^5*b^5*x^5+11028590*a^10*m^4+274727240*a^9*b*m^3*x+1727578440*a^8*b^2*m^2*x^2+3316939200*a^7*b^3*m*x^3+1676505600*a^6*b^4*x^4+34967140*a^10*m^3+503126280*a^9*b*m^2*x+1608573600*a^8*b^2*m*x^2+1197504000*a^7*b^3*x^3+70290936*a^10*m^2+502927200*a^9*b*m*x+598752000*a^8*b^2*x^2+80627040*a^10*m+199584000*a^9*b*x+39916800*a^10)/(11+m)/(10+m)/(9+m)/(8+m)/(7+m)/(6+m)/(5+m)/(m+4)/(m+3)/(m+2)/(m+1)

maxima [A] time = 1.39, size = 187, normalized size = 1.00

$$\frac{b^{10}x^{m+11}}{m+11} + \frac{10ab^9x^{m+10}}{m+10} + \frac{45a^2b^8x^{m+9}}{m+9} + \frac{120a^3b^7x^{m+8}}{m+8} + \frac{210a^4b^6x^{m+7}}{m+7} + \frac{252a^5b^5x^{m+6}}{m+6} + \frac{210a^6b^4x^{m+5}}{m+5} + \frac{120a^7b^3x^{m+4}}{m+4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^10,x, algorithm="maxima")

[Out] b^10*x^(m + 11)/(m + 11) + 10*a*b^9*x^(m + 10)/(m + 10) + 45*a^2*b^8*x^(m + 9)/(m + 9) + 120*a^3*b^7*x^(m + 8)/(m + 8) + 210*a^4*b^6*x^(m + 7)/(m + 7) + 252*a^5*b^5*x^(m + 6)/(m + 6) + 210*a^6*b^4*x^(m + 5)/(m + 5) + 120*a^7*b^3*x^(m + 4)/(m + 4) + 45*a^8*b^2*x^(m + 3)/(m + 3) + 10*a^9*b*x^(m + 2)/(m + 2) + a^10*x^(m + 1)/(m + 1)

mupad [B] time = 1.37, size = 1274, normalized size = 6.81

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(a + b*x)^10,x)

```
[Out] (a^10*x*x^m*(80627040*m + 70290936*m^2 + 34967140*m^3 + 11028590*m^4 + 2310
945*m^5 + 326613*m^6 + 30810*m^7 + 1860*m^8 + 65*m^9 + m^10 + 39916800))/(1
20543840*m + 150917976*m^2 + 105258076*m^3 + 45995730*m^4 + 13339535*m^5 +
2637558*m^6 + 357423*m^7 + 32670*m^8 + 1925*m^9 + 66*m^10 + m^11 + 39916800
) + (b^10*x^m*x^11*(10628640*m + 12753576*m^2 + 8409500*m^3 + 3416930*m^4 +
902055*m^5 + 157773*m^6 + 18150*m^7 + 1320*m^8 + 55*m^9 + m^10 + 3628800))
/(120543840*m + 150917976*m^2 + 105258076*m^3 + 45995730*m^4 + 13339535*m^5
+ 2637558*m^6 + 357423*m^7 + 32670*m^8 + 1925*m^9 + 66*m^10 + m^11 + 39916
800) + (45*a^2*b^8*x^m*x^9*(12900960*m + 15335224*m^2 + 9991428*m^3 + 40004
78*m^4 + 1037673*m^5 + 177765*m^6 + 19962*m^7 + 1412*m^8 + 57*m^9 + m^10 +
4435200))/(120543840*m + 150917976*m^2 + 105258076*m^3 + 45995730*m^4 + 133
39535*m^5 + 2637558*m^6 + 357423*m^7 + 32670*m^8 + 1925*m^9 + 66*m^10 + m^1
1 + 39916800) + (120*a^3*b^7*x^m*x^8*(14444280*m + 17059212*m^2 + 11024858*
m^3 + 4371359*m^4 + 1121022*m^5 + 189567*m^6 + 20982*m^7 + 1461*m^8 + 58*m^
9 + m^10 + 4989600))/(120543840*m + 150917976*m^2 + 105258076*m^3 + 4599573
0*m^4 + 13339535*m^5 + 2637558*m^6 + 357423*m^7 + 32670*m^8 + 1925*m^9 + 66
*m^10 + m^11 + 39916800) + (210*a^4*b^6*x^m*x^7*(16405920*m + 19216008*m^2
+ 12291724*m^3 + 4814858*m^4 + 1217811*m^5 + 202821*m^6 + 22086*m^7 + 1512*
m^8 + 59*m^9 + m^10 + 5702400))/(120543840*m + 150917976*m^2 + 105258076*m^
3 + 45995730*m^4 + 13339535*m^5 + 2637558*m^6 + 357423*m^7 + 32670*m^8 + 19
25*m^9 + 66*m^10 + m^11 + 39916800) + (252*a^5*b^5*x^m*x^6*(18981840*m + 21
989356*m^2 + 13878120*m^3 + 5352935*m^4 + 1331100*m^5 + 217743*m^6 + 23280*
m^7 + 1565*m^8 + 60*m^9 + m^10 + 6652800))/(120543840*m + 150917976*m^2 + 1
05258076*m^3 + 45995730*m^4 + 13339535*m^5 + 2637558*m^6 + 357423*m^7 + 326
70*m^8 + 1925*m^9 + 66*m^10 + m^11 + 39916800) + (210*a^6*b^4*x^m*x^5*(2251
2096*m + 25681176*m^2 + 15915380*m^3 + 6016070*m^4 + 1464693*m^5 + 234573*m
^6 + 24570*m^7 + 1620*m^8 + 61*m^9 + m^10 + 7983360))/(120543840*m + 150917
976*m^2 + 105258076*m^3 + 45995730*m^4 + 13339535*m^5 + 2637558*m^6 + 35742
3*m^7 + 32670*m^8 + 1925*m^9 + 66*m^10 + m^11 + 39916800) + (120*a^7*b^3*x^
m*x^4*(27641160*m + 30819204*m^2 + 18609718*m^3 + 6846503*m^4 + 1623258*m^5
+ 253575*m^6 + 25962*m^7 + 1677*m^8 + 62*m^9 + m^10 + 9979200))/(120543840
*m + 150917976*m^2 + 105258076*m^3 + 45995730*m^4 + 13339535*m^5 + 2637558*
m^6 + 357423*m^7 + 32670*m^8 + 1925*m^9 + 66*m^10 + m^11 + 39916800) + (45*
a^8*b^2*x^m*x^3*(35746080*m + 38390632*m^2 + 22289148*m^3 + 7902194*m^4 + 1
812447*m^5 + 275037*m^6 + 27462*m^7 + 1736*m^8 + 63*m^9 + m^10 + 13305600))
/(120543840*m + 150917976*m^2 + 105258076*m^3 + 45995730*m^4 + 13339535*m^5
+ 2637558*m^6 + 357423*m^7 + 32670*m^8 + 1925*m^9 + 66*m^10 + m^11 + 39916
800) + (10*a*b^9*x^m*x^10*(11655216*m + 13926276*m^2 + 9133180*m^3 + 368625
5*m^4 + 965328*m^5 + 167223*m^6 + 19020*m^7 + 1365*m^8 + 56*m^9 + m^10 + 39
91680))/(120543840*m + 150917976*m^2 + 105258076*m^3 + 45995730*m^4 + 13339
535*m^5 + 2637558*m^6 + 357423*m^7 + 32670*m^8 + 1925*m^9 + 66*m^10 + m^11
+ 39916800) + (10*a^9*b*x^m*x^2*(50292720*m + 50312628*m^2 + 27472724*m^3 +
9261503*m^4 + 2039016*m^5 + 299271*m^6 + 29076*m^7 + 1797*m^8 + 64*m^9 + m
^10 + 19958400))/(120543840*m + 150917976*m^2 + 105258076*m^3 + 45995730*m^
4 + 13339535*m^5 + 2637558*m^6 + 357423*m^7 + 32670*m^8 + 1925*m^9 + 66*m^1
```

0 + m¹¹ + 39916800)

sympy [A] time = 6.93, size = 9996, normalized size = 53.45

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*(b*x+a)**10,x)

[Out] Piecewise((-a**10/(10*x**10) - 10*a**9*b/(9*x**9) - 45*a**8*b**2/(8*x**8) - 120*a**7*b**3/(7*x**7) - 35*a**6*b**4/x**6 - 252*a**5*b**5/(5*x**5) - 105*a**4*b**6/(2*x**4) - 40*a**3*b**7/x**3 - 45*a**2*b**8/(2*x**2) - 10*a*b**9/x + b**10*log(x), Eq(m, -11)), (-a**10/(9*x**9) - 5*a**9*b/(4*x**8) - 45*a**8*b**2/(7*x**7) - 20*a**7*b**3/x**6 - 42*a**6*b**4/x**5 - 63*a**5*b**5/x**4 - 70*a**4*b**6/x**3 - 60*a**3*b**7/x**2 - 45*a**2*b**8/x + 10*a*b**9*log(x) + b**10*x, Eq(m, -10)), (-a**10/(8*x**8) - 10*a**9*b/(7*x**7) - 15*a**8*b**2/(2*x**6) - 24*a**7*b**3/x**5 - 105*a**6*b**4/(2*x**4) - 84*a**5*b**5/x**3 - 105*a**4*b**6/x**2 - 120*a**3*b**7/x + 45*a**2*b**8*log(x) + 10*a*b**9*x + b**10*x**2/2, Eq(m, -9)), (-a**10/(7*x**7) - 5*a**9*b/(3*x**6) - 9*a**8*b**2/x**5 - 30*a**7*b**3/x**4 - 70*a**6*b**4/x**3 - 126*a**5*b**5/x**2 - 210*a**4*b**6/x + 120*a**3*b**7*log(x) + 45*a**2*b**8*x + 5*a*b**9*x**2 + b**10*x**3/3, Eq(m, -8)), (-a**10/(6*x**6) - 2*a**9*b/x**5 - 45*a**8*b**2/(4*x**4) - 40*a**7*b**3/x**3 - 105*a**6*b**4/x**2 - 252*a**5*b**5/x + 210*a**4*b**6*log(x) + 120*a**3*b**7*x + 45*a**2*b**8*x**2/2 + 10*a*b**9*x**3/3 + b**10*x**4/4, Eq(m, -7)), (-a**10/(5*x**5) - 5*a**9*b/(2*x**4) - 15*a**8*b**2/x**3 - 60*a**7*b**3/x**2 - 210*a**6*b**4/x + 252*a**5*b**5*log(x) + 210*a**4*b**6*x + 60*a**3*b**7*x**2 + 15*a**2*b**8*x**3 + 5*a*b**9*x**4/2 + b**10*x**5/5, Eq(m, -6)), (-a**10/(4*x**4) - 10*a**9*b/(3*x**3) - 45*a**8*b**2/(2*x**2) - 120*a**7*b**3/x + 210*a**6*b**4*log(x) + 252*a**5*b**5*x + 105*a**4*b**6*x**2 + 40*a**3*b**7*x**3 + 45*a**2*b**8*x**4/4 + 2*a*b**9*x**5 + b**10*x**6/6, Eq(m, -5)), (-a**10/(3*x**3) - 5*a**9*b/x**2 - 45*a**8*b**2/x + 120*a**7*b**3*log(x) + 210*a**6*b**4*x + 126*a**5*b**5*x**2 + 70*a**4*b**6*x**3 + 30*a**3*b**7*x**4 + 9*a**2*b**8*x**5 + 5*a*b**9*x**6/3 + b**10*x**7/7, Eq(m, -4)), (-a**10/(2*x**2) - 10*a**9*b/x + 45*a**8*b**2*log(x) + 120*a**7*b**3*x + 105*a**6*b**4*x**2 + 84*a**5*b**5*x**3 + 105*a**4*b**6*x**4/2 + 24*a**3*b**7*x**5 + 15*a**2*b**8*x**6/2 + 10*a*b**9*x**7/7 + b**10*x**8/8, Eq(m, -3)), (-a**10/x + 10*a**9*b*log(x) + 45*a**8*b**2*x + 60*a**7*b**3*x**2 + 70*a**6*b**4*x**3 + 63*a**5*b**5*x**4 + 42*a**4*b**6*x**5 + 20*a**3*b**7*x**6 + 45*a**2*b**8*x**7/7 + 5*a*b**9*x**8/4 + b**10*x**9/9, Eq(m, -2)), (a**10*log(x) + 10*a**9*b*x + 45*a**8*b**2*x**2/2 + 40*a**7*b**3*x**3 + 105*a**6*b**4*x**4/2 + 252*a**5*b**5*x**5/5 + 35*a**4*b**6*x**6 + 120*a**3*b**7*x**7/7 + 45*a**2*b**8*x**8/8 + 10*a*b**9*x**9/9 + b**10*x**10/10, Eq(m, -1)), (a**10*m**10*x*x**m/(m**11 + 66*m**10 + 1925*m**9 + 32670*m**8 + 357423*m**7 + 2637558*m**6 + 13339535*m**5 + 45995730*m**4 + 105258076*m**3 + 150917976*m**2 + 120543840*m + 39916800) + 65*a**10*m**9*x*x**m/(m**11

$$\begin{aligned}
& *4 + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 503126280* \\
& a^{**9}*b*m^{**2}*x^{**2}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m \\
& **7 + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 15091 \\
& 7976*m^{**2} + 120543840*m + 39916800) + 502927200*a^{**9}*b*m*x^{**2}*x^{**m}/(m^{**11} + \\
& 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535* \\
& m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 3991 \\
& 6800) + 199584000*a^{**9}*b*x^{**2}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m* \\
& *8 + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076 \\
& *m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 45*a^{**8}*b^{**2}*m^{**10}*x^{**3}* \\
& x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{** \\
& 6 + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 12054 \\
& 3840*m + 39916800) + 2835*a^{**8}*b^{**2}*m^{**9}*x^{**3}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925 \\
& *m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730* \\
& m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 78120*a* \\
& *8*b^{**2}*m^{**8}*x^{**3}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423* \\
& m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 1509 \\
& 17976*m^{**2} + 120543840*m + 39916800) + 1235790*a^{**8}*b^{**2}*m^{**7}*x^{**3}*x^{**m}/(m* \\
& *11 + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 1333 \\
& 9535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + \\
& 39916800) + 12376665*a^{**8}*b^{**2}*m^{**6}*x^{**3}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{** \\
& 9 + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} \\
& + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 81560115*a^{** \\
& 8}*b^{**2}*m^{**5}*x^{**3}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m \\
& **7 + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 15091 \\
& 7976*m^{**2} + 120543840*m + 39916800) + 355598730*a^{**8}*b^{**2}*m^{**4}*x^{**3}*x^{**m}/(m \\
& **11 + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 133 \\
& 39535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m \\
& + 39916800) + 1003011660*a^{**8}*b^{**2}*m^{**3}*x^{**3}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925* \\
& m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m \\
& **4 + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 172757844 \\
& 0*a^{**8}*b^{**2}*m^{**2}*x^{**3}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357 \\
& 423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + \\
& 150917976*m^{**2} + 120543840*m + 39916800) + 1608573600*a^{**8}*b^{**2}*m*x^{**3}*x^{**m} \\
& /(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + \\
& 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840 \\
& *m + 39916800) + 598752000*a^{**8}*b^{**2}*x^{**3}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{** \\
& 9 + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} \\
& + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 120*a^{**7}*b^{** \\
& 3}*m^{**10}*x^{**4}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} \\
& + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976 \\
& *m^{**2} + 120543840*m + 39916800) + 7440*a^{**7}*b^{**3}*m^{**9}*x^{**4}*x^{**m}/(m^{**11} + 66 \\
& *m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{** \\
& 5 + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 3991680 \\
& 0) + 201240*a^{**7}*b^{**3}*m^{**8}*x^{**4}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670* \\
& m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 1052580
\end{aligned}$$

$76m^3 + 150917976m^2 + 120543840m + 39916800) + 3115440a^7b^3m^7$
 $x^4x^m/(m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 26375$
 $58m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 +$
 $120543840m + 39916800) + 30429000a^7b^3m^6x^4x^m/(m^{11} + 66m^$
 $^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 +$
 $45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800)$
 $+ 194790960a^7b^3m^5x^4x^m/(m^{11} + 66m^{10} + 1925m^9 + 32670m$
 $^{10} + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 1052580$
 $76m^3 + 150917976m^2 + 120543840m + 39916800) + 821580360a^7b^3m^$
 $^4x^4x^m/(m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 263$
 $7558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2$
 $+ 120543840m + 39916800) + 2233166160a^7b^3m^3x^4x^m/(m^{11} + 6$
 $6m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^$
 $^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 399168$
 $00) + 3698304480a^7b^3m^2x^4x^m/(m^{11} + 66m^{10} + 1925m^9 + 3$
 $2670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 10$
 $5258076m^3 + 150917976m^2 + 120543840m + 39916800) + 3316939200a^7b$
 $^3m^x^4x^m/(m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 +$
 $2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m$
 $^2 + 120543840m + 39916800) + 1197504000a^7b^3x^4x^m/(m^{11} + 66m$
 $^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5$
 $+ 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800$
 $) + 210a^6b^4m^{10}x^5x^m/(m^{11} + 66m^{10} + 1925m^9 + 32670m^$
 $^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m$
 $^3 + 150917976m^2 + 120543840m + 39916800) + 12810a^6b^4m^9x^5$
 $x^m/(m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^$
 $^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 1205$
 $43840m + 39916800) + 340200a^6b^4m^8x^5x^m/(m^{11} + 66m^{10} + 1$
 $925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 459957$
 $30m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 51597$
 $00a^6b^4m^7x^5x^m/(m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 35$
 $7423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 +$
 $150917976m^2 + 120543840m + 39916800) + 49260330a^6b^4m^6x^5x^$
 $m/(m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6$
 $+ 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 1205438$
 $40m + 39916800) + 307585530a^6b^4m^5x^5x^m/(m^{11} + 66m^{10} + 1$
 $925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 459957$
 $30m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 12633$
 $74700a^6b^4m^4x^5x^m/(m^{11} + 66m^{10} + 1925m^9 + 32670m^8 +$
 $357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^$
 $^3 + 150917976m^2 + 120543840m + 39916800) + 3342229800a^6b^4m^3x^$
 $^5x^m/(m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m$
 $^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 12$
 $0543840m + 39916800) + 5393046960a^6b^4m^2x^5x^m/(m^{11} + 66m^$
 $^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 +$

$45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) +$
 $4727540160*a^{**6}*b^{**4}*m*x^{**5}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8}$
 $+ 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*$
 $m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 1676505600*a^{**6}*b^{**4}*x^{**5}$
 $*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6}$
 $+ 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 1205$
 $43840*m + 39916800) + 252*a^{**5}*b^{**5}*m^{**10}*x^{**6}*x^{**m}/(m^{**11} + 66*m^{**10} + 192$
 $5*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730$
 $*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 15120*a$
 $**5*b^{**5}*m^{**9}*x^{**6}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423$
 $*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150$
 $917976*m^{**2} + 120543840*m + 39916800) + 394380*a^{**5}*b^{**5}*m^{**8}*x^{**6}*x^{**m}/(m*$
 $*11 + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 1333$
 $9535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m +$
 $39916800) + 5866560*a^{**5}*b^{**5}*m^{**7}*x^{**6}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9}$
 $+ 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4}$
 $+ 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 54871236*a^{**5}$
 $*b^{**5}*m^{**6}*x^{**6}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m*$
 $*7 + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917$
 $976*m^{**2} + 120543840*m + 39916800) + 335437200*a^{**5}*b^{**5}*m^{**5}*x^{**6}*x^{**m}/(m*$
 $*11 + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 1333$
 $9535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m +$
 $39916800) + 1348939620*a^{**5}*b^{**5}*m^{**4}*x^{**6}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m*$
 $**9 + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m*$
 $*4 + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 3497286240$
 $*a^{**5}*b^{**5}*m^{**3}*x^{**6}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 3574$
 $23*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 1$
 $50917976*m^{**2} + 120543840*m + 39916800) + 5541317712*a^{**5}*b^{**5}*m^{**2}*x^{**6}*x*$
 $*m/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6}$
 $+ 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 1205438$
 $40*m + 39916800) + 4783423680*a^{**5}*b^{**5}*m*x^{**6}*x^{**m}/(m^{**11} + 66*m^{**10} + 192$
 $5*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730$
 $*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 1676505$
 $600*a^{**5}*b^{**5}*x^{**6}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423$
 $*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150$
 $917976*m^{**2} + 120543840*m + 39916800) + 210*a^{**4}*b^{**6}*m^{**10}*x^{**7}*x^{**m}/(m^{**1}$
 $1 + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 133395$
 $35*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 3$
 $9916800) + 12390*a^{**4}*b^{**6}*m^{**9}*x^{**7}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 3$
 $2670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 10$
 $5258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 317520*a^{**4}*b^{**6}*$
 $m^{**8}*x^{**7}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2$
 $637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m*$
 $*2 + 120543840*m + 39916800) + 4638060*a^{**4}*b^{**6}*m^{**7}*x^{**7}*x^{**m}/(m^{**11} + 66$
 $*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m*$

$58m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 598752000a^3b^7x^8x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 45a^2b^8m^{10}x^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 2565a^2b^8m^9x^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 63540a^2b^8m^8x^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 898290a^2b^8m^7x^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 7999425a^2b^8m^6x^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 46695285a^2b^8m^5x^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 180021510a^2b^8m^4x^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 449614260a^2b^8m^3x^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 690085080a^2b^8m^2x^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 580543200a^2b^8mx^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 199584000a^2b^8x^9x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 10ab^9m^{10}x^{10}x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 560ab^9m^9x^{10}x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 13650ab^9m^8x^{10}x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 190200ab^9m^7x^{10}x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5 + 45995730m^4 + 105258076m^3 + 150917976m^2 + 120543840m + 39916800) + 1672230ab^9m^6x^{10}x^m / (m^{11} + 66m^{10} + 1925m^9 + 32670m^8 + 357423m^7 + 2637558m^6 + 13339535m^5$

$$\begin{aligned}
& + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800 \\
&) + 9653280*a*b^{**9}*m^{**5}*x^{**10}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} \\
& + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076 \\
& *m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 36862550*a*b^{**9}*m^{**4}*x^{** \\
& 10}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558* \\
& m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 12 \\
& 0543840*m + 39916800) + 91331800*a*b^{**9}*m^{**3}*x^{**10}*x^{**m}/(m^{**11} + 66*m^{**10} + \\
& 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 4599 \\
& 5730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 139 \\
& 262760*a*b^{**9}*m^{**2}*x^{**10}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + \\
& 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} \\
& + 150917976*m^{**2} + 120543840*m + 39916800) + 116552160*a*b^{**9}*m*x^{**10}*x^{**m} \\
& /(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + \\
& 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840 \\
& *m + 39916800) + 39916800*a*b^{**9}*x^{**10}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + \\
& 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + \\
& 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + b^{**10}*m^{**10}*x^{** \\
& 11}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558* \\
& m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 12 \\
& 0543840*m + 39916800) + 55*b^{**10}*m^{**9}*x^{**11}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m \\
& **9 + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m* \\
& *4 + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 1320*b^{**10} \\
& *m^{**8}*x^{**11}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + \\
& 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976* \\
& m^{**2} + 120543840*m + 39916800) + 18150*b^{**10}*m^{**7}*x^{**11}*x^{**m}/(m^{**11} + 66*m* \\
& *10 + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + \\
& 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) \\
& + 157773*b^{**10}*m^{**6}*x^{**11}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + \\
& 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} \\
& + 150917976*m^{**2} + 120543840*m + 39916800) + 902055*b^{**10}*m^{**5}*x^{**11}*x^{**m} \\
& /(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + \\
& 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840 \\
& *m + 39916800) + 3416930*b^{**10}*m^{**4}*x^{**11}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} \\
& + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} \\
& + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 8409500*b^{**1 \\
& 0}*m^{**3}*x^{**11}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} \\
& + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976 \\
& *m^{**2} + 120543840*m + 39916800) + 12753576*b^{**10}*m^{**2}*x^{**11}*x^{**m}/(m^{**11} + 6 \\
& 6*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m* \\
& *5 + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*m + 399168 \\
& 00) + 10628640*b^{**10}*m*x^{**11}*x^{**m}/(m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} \\
& + 357423*m^{**7} + 2637558*m^{**6} + 13339535*m^{**5} + 45995730*m^{**4} + 105258076* \\
& m^{**3} + 150917976*m^{**2} + 120543840*m + 39916800) + 3628800*b^{**10}*x^{**11}*x^{**m}/ \\
& (m^{**11} + 66*m^{**10} + 1925*m^{**9} + 32670*m^{**8} + 357423*m^{**7} + 2637558*m^{**6} + 1 \\
& 3339535*m^{**5} + 45995730*m^{**4} + 105258076*m^{**3} + 150917976*m^{**2} + 120543840*
\end{aligned}$$

m + 39916800), True))

3.700 $\int x^m (a + bx)^7 dx$

Optimal. Leaf size=133

$$\frac{a^7 x^{m+1}}{m+1} + \frac{7a^6 b x^{m+2}}{m+2} + \frac{21a^5 b^2 x^{m+3}}{m+3} + \frac{35a^4 b^3 x^{m+4}}{m+4} + \frac{35a^3 b^4 x^{m+5}}{m+5} + \frac{21a^2 b^5 x^{m+6}}{m+6} + \frac{7ab^6 x^{m+7}}{m+7} + \frac{b^7 x^{m+8}}{m+8}$$

[Out] $a^7 x^{(1+m)/(1+m)} + 7a^6 b x^{(2+m)/(2+m)} + 21a^5 b^2 x^{(3+m)/(3+m)} + 35a^4 b^3 x^{(4+m)/(4+m)} + 35a^3 b^4 x^{(5+m)/(5+m)} + 21a^2 b^5 x^{(6+m)/(6+m)} + 7a b^6 x^{(7+m)/(7+m)} + b^7 x^{(8+m)/(8+m)}$

Rubi [A] time = 0.05, antiderivative size = 133, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{21a^5 b^2 x^{m+3}}{m+3} + \frac{35a^4 b^3 x^{m+4}}{m+4} + \frac{35a^3 b^4 x^{m+5}}{m+5} + \frac{21a^2 b^5 x^{m+6}}{m+6} + \frac{7a^6 b x^{m+2}}{m+2} + \frac{a^7 x^{m+1}}{m+1} + \frac{7ab^6 x^{m+7}}{m+7} + \frac{b^7 x^{m+8}}{m+8}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x)^7, x]

[Out] $(a^7 x^{(1+m)/(1+m)})/(1+m) + (7a^6 b x^{(2+m)/(2+m)})/(2+m) + (21a^5 b^2 x^{(3+m)/(3+m)})/(3+m) + (35a^4 b^3 x^{(4+m)/(4+m)})/(4+m) + (35a^3 b^4 x^{(5+m)/(5+m)})/(5+m) + (21a^2 b^5 x^{(6+m)/(6+m)})/(6+m) + (7a b^6 x^{(7+m)/(7+m)})/(7+m) + (b^7 x^{(8+m)/(8+m)})/(8+m)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^m (a + bx)^7 dx &= \int (a^7 x^m + 7a^6 b x^{1+m} + 21a^5 b^2 x^{2+m} + 35a^4 b^3 x^{3+m} + 35a^3 b^4 x^{4+m} + 21a^2 b^5 x^{5+m} + 7ab^6 x^{6+m} + b^7 x^{7+m}) dx \\ &= \frac{a^7 x^{1+m}}{1+m} + \frac{7a^6 b x^{2+m}}{2+m} + \frac{21a^5 b^2 x^{3+m}}{3+m} + \frac{35a^4 b^3 x^{4+m}}{4+m} + \frac{35a^3 b^4 x^{5+m}}{5+m} + \frac{21a^2 b^5 x^{6+m}}{6+m} + \frac{7ab^6 x^{7+m}}{7+m} + \frac{b^7 x^{8+m}}{8+m} \end{aligned}$$

Mathematica [A] time = 0.07, size = 118, normalized size = 0.89

$$x^{m+1} \left(\frac{a^7}{m+1} + \frac{7a^6 b x}{m+2} + \frac{21a^5 b^2 x^2}{m+3} + \frac{35a^4 b^3 x^3}{m+4} + \frac{35a^3 b^4 x^4}{m+5} + \frac{21a^2 b^5 x^5}{m+6} + \frac{7ab^6 x^6}{m+7} + \frac{b^7 x^7}{m+8} \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x)^7,x]

[Out] $x^{(1+m)}(a^7/(1+m) + (7*a^6*b*x)/(2+m) + (21*a^5*b^2*x^2)/(3+m) + (35*a^4*b^3*x^3)/(4+m) + (35*a^3*b^4*x^4)/(5+m) + (21*a^2*b^5*x^5)/(6+m) + (7*a*b^6*x^6)/(7+m) + (b^7*x^7)/(8+m))$

fricas [B] time = 0.50, size = 665, normalized size = 5.00

$$\frac{((b^7 m^7 + 28 b^7 m^6 + 322 b^7 m^5 + 1960 b^7 m^4 + 6769 b^7 m^3 + 13132 b^7 m^2 + 13068 b^7 m + 5040 b^7) x^8 + 7 (ab^6 m^7 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^7,x, algorithm="fricas")

[Out] $((b^7 m^7 + 28 b^7 m^6 + 322 b^7 m^5 + 1960 b^7 m^4 + 6769 b^7 m^3 + 13132 b^7 m^2 + 13068 b^7 m + 5040 b^7) x^8 + 7(a b^6 m^7 + 29 a b^6 m^6 + 343 a b^6 m^5 + 2135 a b^6 m^4 + 7504 a b^6 m^3 + 14756 a b^6 m^2 + 14832 a b^6 m + 5760 a b^6) x^7 + 21(a^2 b^5 m^7 + 30 a^2 b^5 m^6 + 366 a^2 b^5 m^5 + 2340 a^2 b^5 m^4 + 8409 a^2 b^5 m^3 + 16830 a^2 b^5 m^2 + 17144 a^2 b^5 m + 6720 a^2 b^5) x^6 + 35(a^3 b^4 m^7 + 31 a^3 b^4 m^6 + 391 a^3 b^4 m^5 + 2581 a^3 b^4 m^4 + 9544 a^3 b^4 m^3 + 19564 a^3 b^4 m^2 + 20304 a^3 b^4 m + 8064 a^3 b^4) x^5 + 35(a^4 b^3 m^7 + 32 a^4 b^3 m^6 + 418 a^4 b^3 m^5 + 2864 a^4 b^3 m^4 + 10993 a^4 b^3 m^3 + 23312 a^4 b^3 m^2 + 24876 a^4 b^3 m + 10080 a^4 b^3) x^4 + 21(a^5 b^2 m^7 + 33 a^5 b^2 m^6 + 447 a^5 b^2 m^5 + 3195 a^5 b^2 m^4 + 12864 a^5 b^2 m^3 + 28692 a^5 b^2 m^2 + 32048 a^5 b^2 m + 13440 a^5 b^2) x^3 + 7(a^6 b m^7 + 34 a^6 b m^6 + 478 a^6 b m^5 + 3580 a^6 b m^4 + 15289 a^6 b m^3 + 36706 a^6 b m^2 + 44712 a^6 b m + 20160 a^6 b) x^2 + (a^7 m^7 + 35 a^7 m^6 + 511 a^7 m^5 + 4025 a^7 m^4 + 18424 a^7 m^3 + 48860 a^7 m^2 + 69264 a^7 m + 40320 a^7) x) x^m / (m^8 + 36 m^7 + 546 m^6 + 4536 m^5 + 22449 m^4 + 67284 m^3 + 118124 m^2 + 109584 m + 40320)$

giac [B] time = 1.40, size = 992, normalized size = 7.46

$$b^7 m^7 x^8 x^m + 7 a b^6 m^7 x^7 x^m + 28 b^7 m^6 x^8 x^m + 21 a^2 b^5 m^7 x^6 x^m + 203 a b^6 m^6 x^7 x^m + 322 b^7 m^5 x^8 x^m + 35 a^3 b^4 m^7 x^5 x^m$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^7,x, algorithm="giac")

[Out] $(b^7 m^7 x^8 x^m + 7 a b^6 m^7 x^7 x^m + 28 b^7 m^6 x^8 x^m + 21 a^2 b^5 m^7 x^6 x^m + 203 a b^6 m^6 x^7 x^m + 322 b^7 m^5 x^8 x^m + 35 a^3 b^4 m^7 x^5 x^m + 630 a^2 b^5 m^6 x^6 x^m + 2401 a b^6 m^5 x^7 x^m + 1960 b^7 m^4 x^8 x^m + 35 a^4 b^3 m^7 x^4 x^m + 1085 a^3 b^4 m^6 x^5 x^m + 7686 a^2 b^5 m^5$

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*x^6*x^m + 14945*a*b^6*m^4*x^7*x^m + 6769*b^7*m^3*x^8*x^m + 21*a^5*b^2*m^7*
x^3*x^m + 1120*a^4*b^3*m^6*x^4*x^m + 13685*a^3*b^4*m^5*x^5*x^m + 49140*a^2*
b^5*m^4*x^6*x^m + 52528*a*b^6*m^3*x^7*x^m + 13132*b^7*m^2*x^8*x^m + 7*a^6*b
*m^7*x^2*x^m + 693*a^5*b^2*m^6*x^3*x^m + 14630*a^4*b^3*m^5*x^4*x^m + 90335*
a^3*b^4*m^4*x^5*x^m + 176589*a^2*b^5*m^3*x^6*x^m + 103292*a*b^6*m^2*x^7*x^m
+ 13068*b^7*m*x^8*x^m + a^7*m^7*x*x^m + 238*a^6*b*m^6*x^2*x^m + 9387*a^5*b
^2*m^5*x^3*x^m + 100240*a^4*b^3*m^4*x^4*x^m + 334040*a^3*b^4*m^3*x^5*x^m +
353430*a^2*b^5*m^2*x^6*x^m + 103824*a*b^6*m*x^7*x^m + 5040*b^7*x^8*x^m + 35
*a^7*m^6*x*x^m + 3346*a^6*b*m^5*x^2*x^m + 67095*a^5*b^2*m^4*x^3*x^m + 38475
5*a^4*b^3*m^3*x^4*x^m + 684740*a^3*b^4*m^2*x^5*x^m + 360024*a^2*b^5*m*x^6*x
^m + 40320*a*b^6*x^7*x^m + 511*a^7*m^5*x*x^m + 25060*a^6*b*m^4*x^2*x^m + 27
0144*a^5*b^2*m^3*x^3*x^m + 815920*a^4*b^3*m^2*x^4*x^m + 710640*a^3*b^4*m*x^
5*x^m + 141120*a^2*b^5*x^6*x^m + 4025*a^7*m^4*x*x^m + 107023*a^6*b*m^3*x^2*
x^m + 602532*a^5*b^2*m^2*x^3*x^m + 870660*a^4*b^3*m*x^4*x^m + 282240*a^3*b^
4*x^5*x^m + 18424*a^7*m^3*x*x^m + 256942*a^6*b*m^2*x^2*x^m + 673008*a^5*b^2
*m*x^3*x^m + 352800*a^4*b^3*x^4*x^m + 48860*a^7*m^2*x*x^m + 312984*a^6*b*m*
x^2*x^m + 282240*a^5*b^2*x^3*x^m + 69264*a^7*m*x*x^m + 141120*a^6*b*x^2*x^m
+ 40320*a^7*x*x^m)/(m^8 + 36*m^7 + 546*m^6 + 4536*m^5 + 22449*m^4 + 67284*
m^3 + 118124*m^2 + 109584*m + 40320)

```

maple [B] time = 0.01, size = 782, normalized size = 5.88

$$(b^7 m^7 x^7 + 7a b^6 m^7 x^6 + 28b^7 m^6 x^7 + 21a^2 b^5 m^7 x^5 + 203a b^6 m^6 x^6 + 322b^7 m^5 x^7 + 35a^3 b^4 m^7 x^4 + 630a^2 b^5 m^6 x^5 + 2401a b^6 m^5 x^6 + 1960b^7 m^4 x^7 + 35a^4 b^3 m^7 x^3 + 1085a^3 b^4 m^6 x^4 + 7686a^2 b^5 m^5 x^5 + 14945a b^6 m^4 x^6 + 6769b^7 m^3 x^7 + 21a^5 b^2 m^7 x^2 + 1120a^4 b^3 m^6 x^3 + 13685a^3 b^4 m^5 x^4 + 49140a^2 b^5 m^4 x^5 + 52528a b^6 m^3 x^6 + 13132b^7 m^2 x^7 + 7a^6 b m^7 x + 693a^5 b^2 m^6 x^2 + 14630a^4 b^3 m^5 x^3 + 90335a^3 b^4 m^4 x^4 + 176589a^2 b^5 m^3 x^5 + 103292a b^6 m^2 x^6 + 13068b^7 m x^7 + a^7 m^7 x + 238a^6 b m^6 x^2 + 9387a^5 b^2 m^5 x^3 + 100240a^4 b^3 m^4 x^4 + 334040a^3 b^4 m^3 x^5 + 353430a^2 b^5 m^2 x^6 + 103824a b^6 m x^7 + 5040b^7 x^8 + 35a^7 m^6 x + 3346a^6 b m^5 x^2 + 67095a^5 b^2 m^4 x^3 + 384755a^4 b^3 m^3 x^4 + 684740a^3 b^4 m^2 x^5 + 360024a^2 b^5 m x^6 + 40320a b^6 x^7 + 511a^7 m^5 x + 25060a^6 b m^4 x^2 + 270144a^5 b^2 m^3 x^3 + 815920a^4 b^3 m^2 x^4 + 710640a^3 b^4 m x^5 + 141120a^2 b^5 x^6 + 4025a^7 m^4 x + 107023a^6 b m^3 x^2 + 602532a^5 b^2 m^2 x^3 + 870660a^4 b^3 m x^4 + 282240a^3 b^4 x^5 + 18424a^7 m^3 x + 256942a^6 b m^2 x^2 + 673008a^5 b^2 m x^3 + 352800a^4 b^3 x^4 + 48860a^7 m^2 x + 312984a^6 b m x^2 + 282240a^5 b^2 x^3 + 69264a^7 m x + 141120a^6 b x^2 + 40320a^7 x) / (m^8 + 36m^7 + 546m^6 + 4536m^5 + 22449m^4 + 67284m^3 + 118124m^2 + 109584m + 40320)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(b*x+a)^7,x)

```

[Out] x^(m+1)*(b^7*m^7*x^7+7*a*b^6*m^7*x^6+28*b^7*m^6*x^7+21*a^2*b^5*m^7*x^5+203*
a*b^6*m^6*x^6+322*b^7*m^5*x^7+35*a^3*b^4*m^7*x^4+630*a^2*b^5*m^6*x^5+2401*a
*b^6*m^5*x^6+1960*b^7*m^4*x^7+35*a^4*b^3*m^7*x^3+1085*a^3*b^4*m^6*x^4+7686*
a^2*b^5*m^5*x^5+14945*a*b^6*m^4*x^6+6769*b^7*m^3*x^7+21*a^5*b^2*m^7*x^2+112
0*a^4*b^3*m^6*x^3+13685*a^3*b^4*m^5*x^4+49140*a^2*b^5*m^4*x^5+52528*a*b^6*m
^3*x^6+13132*b^7*m^2*x^7+7*a^6*b*m^7*x+693*a^5*b^2*m^6*x^2+14630*a^4*b^3*m^
5*x^3+90335*a^3*b^4*m^4*x^4+176589*a^2*b^5*m^3*x^5+103292*a*b^6*m^2*x^6+130
68*b^7*m*x^7+a^7*m^7+238*a^6*b*m^6*x+9387*a^5*b^2*m^5*x^2+100240*a^4*b^3*m^
4*x^3+334040*a^3*b^4*m^3*x^4+353430*a^2*b^5*m^2*x^5+103824*a*b^6*m*x^6+5040
*b^7*x^7+35*a^7*m^6+3346*a^6*b*m^5*x+67095*a^5*b^2*m^4*x^2+384755*a^4*b^3*m
^3*x^3+684740*a^3*b^4*m^2*x^4+360024*a^2*b^5*m*x^5+40320*a*b^6*x^6+511*a^7*
m^5+25060*a^6*b*m^4*x+270144*a^5*b^2*m^3*x^2+815920*a^4*b^3*m^2*x^3+710640*
a^3*b^4*m*x^4+141120*a^2*b^5*x^5+4025*a^7*m^4+107023*a^6*b*m^3*x+602532*a^5
*b^2*m^2*x^2+870660*a^4*b^3*m*x^3+282240*a^3*b^4*x^4+18424*a^7*m^3+256942*a
^6*b*m^2*x+673008*a^5*b^2*m*x^2+352800*a^4*b^3*x^3+48860*a^7*m^2+312984*a^6
*b*m*x+282240*a^5*b^2*x^2+69264*a^7*m+141120*a^6*b*x+40320*a^7)/(m+8)/(m+7)
/(m+6)/(m+5)/(m+4)/(m+3)/(m+2)/(m+1)

```


maxima [A] time = 1.37, size = 133, normalized size = 1.00

$$\frac{b^7 x^{m+8}}{m+8} + \frac{7ab^6 x^{m+7}}{m+7} + \frac{21a^2 b^5 x^{m+6}}{m+6} + \frac{35a^3 b^4 x^{m+5}}{m+5} + \frac{35a^4 b^3 x^{m+4}}{m+4} + \frac{21a^5 b^2 x^{m+3}}{m+3} + \frac{7a^6 b x^{m+2}}{m+2} + \frac{a^7 x^{m+1}}{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^7,x, algorithm="maxima")

[Out] $b^7 x^{m+8}/(m+8) + 7*a*b^6*x^{m+7}/(m+7) + 21*a^2*b^5*x^{m+6}/(m+6) + 35*a^3*b^4*x^{m+5}/(m+5) + 35*a^4*b^3*x^{m+4}/(m+4) + 21*a^5*b^2*x^{m+3}/(m+3) + 7*a^6*b*x^{m+2}/(m+2) + a^7*x^{m+1}/(m+1)$

mupad [B] time = 0.78, size = 683, normalized size = 5.14

$$\frac{a^7 x x^m (m^7 + 35 m^6 + 511 m^5 + 4025 m^4 + 18424 m^3 + 48860 m^2 + 69264 m + 40320)}{m^8 + 36 m^7 + 546 m^6 + 4536 m^5 + 22449 m^4 + 67284 m^3 + 118124 m^2 + 109584 m + 40320} + \frac{b^7 x^m x^8 (m^7 + 36 m^6 + 546 m^5 + 22449 m^4 + 67284 m^3 + 118124 m^2 + 109584 m + 40320)}{m^8 + 36 m^7 + 546 m^6 + 4536 m^5 + 22449 m^4 + 67284 m^3 + 118124 m^2 + 109584 m + 40320}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(a + b*x)^7,x)

[Out] $(a^7*x*x^m*(69264*m + 48860*m^2 + 18424*m^3 + 4025*m^4 + 511*m^5 + 35*m^6 + m^7 + 40320))/(109584*m + 118124*m^2 + 67284*m^3 + 22449*m^4 + 4536*m^5 + 546*m^6 + 36*m^7 + m^8 + 40320) + (b^7*x^m*x^8*(13068*m + 13132*m^2 + 6769*m^3 + 1960*m^4 + 322*m^5 + 28*m^6 + m^7 + 5040))/(109584*m + 118124*m^2 + 67284*m^3 + 22449*m^4 + 4536*m^5 + 546*m^6 + 36*m^7 + m^8 + 40320) + (21*a^2*b^5*x^m*x^6*(17144*m + 16830*m^2 + 8409*m^3 + 2340*m^4 + 366*m^5 + 30*m^6 + m^7 + 6720))/(109584*m + 118124*m^2 + 67284*m^3 + 22449*m^4 + 4536*m^5 + 546*m^6 + 36*m^7 + m^8 + 40320) + (35*a^3*b^4*x^m*x^5*(20304*m + 19564*m^2 + 9544*m^3 + 2581*m^4 + 391*m^5 + 31*m^6 + m^7 + 8064))/(109584*m + 118124*m^2 + 67284*m^3 + 22449*m^4 + 4536*m^5 + 546*m^6 + 36*m^7 + m^8 + 40320) + (35*a^4*b^3*x^m*x^4*(24876*m + 23312*m^2 + 10993*m^3 + 2864*m^4 + 418*m^5 + 32*m^6 + m^7 + 10080))/(109584*m + 118124*m^2 + 67284*m^3 + 22449*m^4 + 4536*m^5 + 546*m^6 + 36*m^7 + m^8 + 40320) + (21*a^5*b^2*x^m*x^3*(32048*m + 28692*m^2 + 12864*m^3 + 3195*m^4 + 447*m^5 + 33*m^6 + m^7 + 13440))/(109584*m + 118124*m^2 + 67284*m^3 + 22449*m^4 + 4536*m^5 + 546*m^6 + 36*m^7 + m^8 + 40320) + (7*a^6*b*x^m*x^2*(44712*m + 36706*m^2 + 15289*m^3 + 3580*m^4 + 478*m^5 + 34*m^6 + m^7 + 20160))/(109584*m + 118124*m^2 + 67284*m^3 + 22449*m^4 + 4536*m^5 + 546*m^6 + 36*m^7 + m^8 + 40320)$

sympy [A] time = 3.34, size = 4257, normalized size = 32.01

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*(b*x+a)**7,x)

[Out] Piecewise((-a**7/(7*x**7) - 7*a**6*b/(6*x**6) - 21*a**5*b**2/(5*x**5) - 35*a**4*b**3/(4*x**4) - 35*a**3*b**4/(3*x**3) - 21*a**2*b**5/(2*x**2) - 7*a*b**6/x + b**7*log(x), Eq(m, -8)), (-a**7/(6*x**6) - 7*a**6*b/(5*x**5) - 21*a**5*b**2/(4*x**4) - 35*a**4*b**3/(3*x**3) - 35*a**3*b**4/(2*x**2) - 21*a**2*b**5/x + 7*a*b**6*log(x) + b**7*x, Eq(m, -7)), (-a**7/(5*x**5) - 7*a**6*b/(4*x**4) - 7*a**5*b**2/x**3 - 35*a**4*b**3/(2*x**2) - 35*a**3*b**4/x + 21*a**2*b**5*log(x) + 7*a*b**6*x + b**7*x**2/2, Eq(m, -6)), (-a**7/(4*x**4) - 7*a**6*b/(3*x**3) - 21*a**5*b**2/(2*x**2) - 35*a**4*b**3/x + 35*a**3*b**4*log(x) + 21*a**2*b**5*x + 7*a*b**6*x**2/2 + b**7*x**3/3, Eq(m, -5)), (-a**7/(3*x**3) - 7*a**6*b/(2*x**2) - 21*a**5*b**2/x + 35*a**4*b**3*log(x) + 35*a**3*b**4*x + 21*a**2*b**5*x**2/2 + 7*a*b**6*x**3/3 + b**7*x**4/4, Eq(m, -4)), (-a**7/(2*x**2) - 7*a**6*b/x + 21*a**5*b**2*log(x) + 35*a**4*b**3*x + 35*a**3*b**4*x**2/2 + 7*a**2*b**5*x**3 + 7*a*b**6*x**4/4 + b**7*x**5/5, Eq(m, -3)), (-a**7/x + 7*a**6*b*log(x) + 21*a**5*b**2*x + 35*a**4*b**3*x**2/2 + 35*a**3*b**4*x**3/3 + 21*a**2*b**5*x**4/4 + 7*a*b**6*x**5/5 + b**7*x**6/6, Eq(m, -2)), (a**7*log(x) + 7*a**6*b*x + 21*a**5*b**2*x**2/2 + 35*a**4*b**3*x**3/3 + 35*a**3*b**4*x**4/4 + 21*a**2*b**5*x**5/5 + 7*a*b**6*x**6/6 + b**7*x**7/7, Eq(m, -1)), (a**7*m**7*x*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 35*a**7*m**6*x*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 511*a**7*m**5*x*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 4025*a**7*m**4*x*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 18424*a**7*m**3*x*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 48860*a**7*m**2*x*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 69264*a**7*m*x*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 40320*a**7*x*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 7*a**6*b*m**7*x**2*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 238*a**6*b*m**6*x**2*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 3346*a**6*b*m**5*x**2*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 25060*a**6*b*m**4*x**2*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 107023*a**6*b*m**3*x**2*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 256942*a**6*b*m**2*x**2*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 312984*a**6*b*m*x**2*x**m/(m**8 + 36*m**


```

*6*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 +
118124*m**2 + 109584*m + 40320) + 630*a**2*b**5*m**6*x**6*x**m/(m**8 + 36*m
**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584
*m + 40320) + 7686*a**2*b**5*m**5*x**6*x**m/(m**8 + 36*m**7 + 546*m**6 + 45
36*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 49140
*a**2*b**5*m**4*x**6*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m*
*4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 176589*a**2*b**5*m**3*x
**6*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 +
118124*m**2 + 109584*m + 40320) + 353430*a**2*b**5*m**2*x**6*x**m/(m**8 +
36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 10
9584*m + 40320) + 360024*a**2*b**5*m*x**6*x**m/(m**8 + 36*m**7 + 546*m**6 +
4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 14
1120*a**2*b**5*x**6*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**
4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 7*a*b**6*m**7*x**7*x**m/
(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m
**2 + 109584*m + 40320) + 203*a*b**6*m**6*x**7*x**m/(m**8 + 36*m**7 + 546*m
**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320)
+ 2401*a*b**6*m**5*x**7*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 2244
9*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 14945*a*b**6*m**4*x
**7*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 +
118124*m**2 + 109584*m + 40320) + 52528*a*b**6*m**3*x**7*x**m/(m**8 + 36*m
**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584
*m + 40320) + 103292*a*b**6*m**2*x**7*x**m/(m**8 + 36*m**7 + 546*m**6 + 453
6*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 103824
*a*b**6*m*x**7*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 6
7284*m**3 + 118124*m**2 + 109584*m + 40320) + 40320*a*b**6*x**7*x**m/(m**8
+ 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 +
109584*m + 40320) + b**7*m**7*x**8*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m
**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 28*b**7*m
**6*x**8*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m
**3 + 118124*m**2 + 109584*m + 40320) + 322*b**7*m**5*x**8*x**m/(m**8 + 36*
m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 10958
4*m + 40320) + 1960*b**7*m**4*x**8*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m
**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 6769*b**7
*m**3*x**8*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284
*m**3 + 118124*m**2 + 109584*m + 40320) + 13132*b**7*m**2*x**8*x**m/(m**8 +
36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 1
09584*m + 40320) + 13068*b**7*m*x**8*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536
*m**5 + 22449*m**4 + 67284*m**3 + 118124*m**2 + 109584*m + 40320) + 5040*b*
**7*x**8*x**m/(m**8 + 36*m**7 + 546*m**6 + 4536*m**5 + 22449*m**4 + 67284*m*
*3 + 118124*m**2 + 109584*m + 40320), True))

```

3.701 $\int x^m(a + bx)^3 dx$

Optimal. Leaf size=61

$$\frac{a^3x^{m+1}}{m+1} + \frac{3a^2bx^{m+2}}{m+2} + \frac{3ab^2x^{m+3}}{m+3} + \frac{b^3x^{m+4}}{m+4}$$

[Out] $a^3x^{(1+m)/(1+m)} + 3a^2bx^{(2+m)/(2+m)} + 3ab^2x^{(3+m)/(3+m)} + b^3x^{(4+m)/(4+m)}$

Rubi [A] time = 0.02, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{3a^2bx^{m+2}}{m+2} + \frac{a^3x^{m+1}}{m+1} + \frac{3ab^2x^{m+3}}{m+3} + \frac{b^3x^{m+4}}{m+4}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x)^3, x]

[Out] $(a^3x^{(1+m)/(1+m)} + (3a^2bx^{(2+m)/(2+m)} + (3ab^2x^{(3+m)/(3+m)} + (b^3x^{(4+m)/(4+m)})))/((1+m) + (2+m) + (3+m) + (4+m))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^m(a + bx)^3 dx &= \int (a^3x^m + 3a^2bx^{1+m} + 3ab^2x^{2+m} + b^3x^{3+m}) dx \\ &= \frac{a^3x^{1+m}}{1+m} + \frac{3a^2bx^{2+m}}{2+m} + \frac{3ab^2x^{3+m}}{3+m} + \frac{b^3x^{4+m}}{4+m} \end{aligned}$$

Mathematica [A] time = 0.03, size = 54, normalized size = 0.89

$$x^{m+1} \left(\frac{a^3}{m+1} + \frac{3a^2bx}{m+2} + \frac{3ab^2x^2}{m+3} + \frac{b^3x^3}{m+4} \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x)^3,x]

[Out] $x^{(1+m)}*(a^3/(1+m) + (3*a^2*b*x)/(2+m) + (3*a*b^2*x^2)/(3+m) + (b^3*x^3)/(4+m))$

fricas [B] time = 0.52, size = 157, normalized size = 2.57

$$\frac{((b^3 m^3 + 6 b^3 m^2 + 11 b^3 m + 6 b^3)x^4 + 3(ab^2 m^3 + 7 ab^2 m^2 + 14 ab^2 m + 8 ab^2)x^3 + 3(a^2 b m^3 + 8 a^2 b m^2 + 19 a^2 b m + 6 a^2 b)x^2 + (a^3 m^3 + 9 a^3 m^2 + 26 a^3 m + 24 a^3)x)x^m}{m^4 + 10 m^3 + 35 m^2 + 50 m + 24}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^3,x, algorithm="fricas")

[Out] $((b^3 m^3 + 6 b^3 m^2 + 11 b^3 m + 6 b^3)x^4 + 3(a b^2 m^3 + 7 a b^2 m^2 + 14 a b^2 m + 8 a b^2)x^3 + 3(a^2 b m^3 + 8 a^2 b m^2 + 19 a^2 b m + 6 a^2 b)x^2 + (a^3 m^3 + 9 a^3 m^2 + 26 a^3 m + 24 a^3)x)x^m/(m^4 + 10 m^3 + 35 m^2 + 50 m + 24)$

giac [B] time = 1.07, size = 224, normalized size = 3.67

$$\frac{b^3 m^3 x^4 x^m + 3 a b^2 m^3 x^3 x^m + 6 b^3 m^2 x^4 x^m + 3 a^2 b m^3 x^2 x^m + 21 a b^2 m^2 x^3 x^m + 11 b^3 m x^4 x^m + a^3 m^3 x x^m + 24 a^2 b m^2 x^2 x^m}{m^4 + 10 m^3 + 35 m^2 + 50 m + 24}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^3,x, algorithm="giac")

[Out] $(b^3 m^3 x^4 x^m + 3 a b^2 m^3 x^3 x^m + 6 b^3 m^2 x^4 x^m + 3 a^2 b m^3 x^2 x^m + 21 a b^2 m^2 x^3 x^m + 11 b^3 m x^4 x^m + a^3 m^3 x x^m + 24 a^2 b m^2 x^2 x^m + 42 a b^2 m^2 x^3 x^m + 6 b^3 m^3 x^4 x^m + 9 a^3 m^2 x^2 x^m + 57 a^2 b m^2 x^3 x^m + 24 a b^2 m^2 x^3 x^m + 26 a^3 m^2 x^2 x^m + 36 a^2 b m^2 x^2 x^m + 24 a^3 m^2 x^2 x^m)/(m^4 + 10 m^3 + 35 m^2 + 50 m + 24)$

maple [B] time = 0.00, size = 170, normalized size = 2.79

$$\frac{(b^3 m^3 x^3 + 3 a b^2 m^3 x^2 + 6 b^3 m^2 x^3 + 3 a^2 b m^3 x + 21 a b^2 m^2 x^2 + 11 b^3 m x^3 + a^3 m^3 + 24 a^2 b m^2 x + 42 a b^2 m x^2 + 6 b^3 x^3)}{(m+4)(m+3)(m+2)(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(b*x+a)^3,x)

[Out] $(b^3 m^3 x^3 + 3 a b^2 m^3 x^2 + 6 b^3 m^2 x^3 + 3 a^2 b m^3 x + 21 a b^2 m^2 x^2 + 11 b^3 m x^3 + a^3 m^3 + 24 a^2 b m^2 x + 42 a b^2 m x^2 + 6 b^3 x^3)/(m+4)/(m+3)/(m+2)/(m+1)*x^{m+1}$

maxima [A] time = 1.30, size = 61, normalized size = 1.00

$$\frac{b^3 x^{m+4}}{m+4} + \frac{3ab^2 x^{m+3}}{m+3} + \frac{3a^2 b x^{m+2}}{m+2} + \frac{a^3 x^{m+1}}{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^3,x, algorithm="maxima")

[Out] b^3*x^(m + 4)/(m + 4) + 3*a*b^2*x^(m + 3)/(m + 3) + 3*a^2*b*x^(m + 2)/(m + 2) + a^3*x^(m + 1)/(m + 1)

mupad [B] time = 0.44, size = 167, normalized size = 2.74

$$x^m \left(\frac{a^3 x (m^3 + 9m^2 + 26m + 24)}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{b^3 x^4 (m^3 + 6m^2 + 11m + 6)}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{3ab^2 x^3 (m^3 + 7m^2 + 14m + 8)}{m^4 + 10m^3 + 35m^2 + 50m + 24} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(a + b*x)^3,x)

[Out] x^m*((a^3*x*(26*m + 9*m^2 + m^3 + 24))/(50*m + 35*m^2 + 10*m^3 + m^4 + 24) + (b^3*x^4*(11*m + 6*m^2 + m^3 + 6))/(50*m + 35*m^2 + 10*m^3 + m^4 + 24) + (3*a*b^2*x^3*(14*m + 7*m^2 + m^3 + 8))/(50*m + 35*m^2 + 10*m^3 + m^4 + 24) + (3*a^2*b*x^2*(19*m + 8*m^2 + m^3 + 12))/(50*m + 35*m^2 + 10*m^3 + m^4 + 24))

sympy [A] time = 0.92, size = 663, normalized size = 10.87

$$\left\{ \begin{array}{l} -\frac{a^3}{3x^3} - \frac{3a^2b}{2x^2} - \frac{3ab^2}{x} + b^3 \log(x) \\ -\frac{a^3}{2x^2} - \frac{3a^2b}{x} + 3ab^2 \log(x) + b^3 x \\ -\frac{a^3}{x} + 3a^2b \log(x) + 3ab^2 x + \frac{b^3 x^2}{2} \\ a^3 \log(x) + 3a^2bx + \frac{3ab^2 x^2}{2} + \frac{b^3 x^3}{3} \\ \frac{a^3 m^3 x x^m}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{9a^3 m^2 x x^m}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{26a^3 m x x^m}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{24a^3 x x^m}{m^4 + 10m^3 + 35m^2 + 50m + 24} + \frac{3a^2 b m^3 x^2 x^m}{m^4 + 10m^3 + 35m^2 + 50m + 24} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*(b*x+a)**3,x)

[Out] Piecewise((-a**3/(3*x**3) - 3*a**2*b/(2*x**2) - 3*a*b**2/x + b**3*log(x), Eq(m, -4)), (-a**3/(2*x**2) - 3*a**2*b/x + 3*a*b**2*log(x) + b**3*x, Eq(m, -

$3))$, $(-a^{**3}/x + 3*a^{**2}*b*\log(x) + 3*a*b^{**2}*x + b^{**3}*x^{**2}/2, \text{Eq}(m, -2))$, $(a^{**3}*\log(x) + 3*a^{**2}*b*x + 3*a*b^{**2}*x^{**2}/2 + b^{**3}*x^{**3}/3, \text{Eq}(m, -1))$, $(a^{**3}*m^{**3}*x^{**3}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 9*a^{**3}*m^{**2}*x^{**2}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 26*a^{**3}*m*x^{**1}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 24*a^{**3}*x^{**0}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 3*a^{**2}*b*m^{**3}*x^{**2}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 24*a^{**2}*b*m^{**2}*x^{**1}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 57*a^{**2}*b*m*x^{**0}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 36*a^{**2}*b*x^{**2}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 3*a*b^{**2}*m^{**3}*x^{**3}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 21*a*b^{**2}*m^{**2}*x^{**3}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 42*a*b^{**2}*m*x^{**3}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 24*a*b^{**2}*x^{**3}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + b^{**3}*m^{**3}*x^{**4}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 6*b^{**3}*m^{**2}*x^{**4}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 11*b^{**3}*m*x^{**4}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24) + 6*b^{**3}*x^{**4}/(m^{**4} + 10*m^{**3} + 35*m^{**2} + 50*m + 24), \text{True}))$

3.702 $\int x^m(a + bx)^2 dx$

Optimal. Leaf size=43

$$\frac{a^2x^{m+1}}{m+1} + \frac{2abx^{m+2}}{m+2} + \frac{b^2x^{m+3}}{m+3}$$

[Out] $a^2x^{(1+m)}/(1+m)+2*a*b*x^{(2+m)}/(2+m)+b^2*x^{(3+m)}/(3+m)$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2x^{m+1}}{m+1} + \frac{2abx^{m+2}}{m+2} + \frac{b^2x^{m+3}}{m+3}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x)^2,x]

[Out] $(a^2*x^{(1+m)})/(1+m) + (2*a*b*x^{(2+m)})/(2+m) + (b^2*x^{(3+m)})/(3+m)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^m(a + bx)^2 dx &= \int (a^2x^m + 2abx^{1+m} + b^2x^{2+m}) dx \\ &= \frac{a^2x^{1+m}}{1+m} + \frac{2abx^{2+m}}{2+m} + \frac{b^2x^{3+m}}{3+m} \end{aligned}$$

Mathematica [A] time = 0.03, size = 38, normalized size = 0.88

$$x^{m+1} \left(\frac{a^2}{m+1} + \frac{2abx}{m+2} + \frac{b^2x^2}{m+3} \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x)^2,x]

[Out] $x^{(1+m)} \cdot (a^2/(1+m) + (2abx)/(2+m) + (b^2x^2)/(3+m))$

fricas [A] time = 0.46, size = 85, normalized size = 1.98

$$\frac{((b^2m^2 + 3b^2m + 2b^2)x^3 + 2(abm^2 + 4abm + 3ab)x^2 + (a^2m^2 + 5a^2m + 6a^2)x)x^m}{m^3 + 6m^2 + 11m + 6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m*(b*x+a)^2,x, algorithm="fricas")`

[Out] $((b^2m^2 + 3b^2m + 2b^2)x^3 + 2(a^2m^2 + 4a^2m + 3a^2)x^2 + (a^2m^2 + 5a^2m + 6a^2)x)x^m/(m^3 + 6m^2 + 11m + 6)$

giac [B] time = 1.04, size = 117, normalized size = 2.72

$$\frac{b^2m^2x^3x^m + 2abm^2x^2x^m + 3b^2mx^3x^m + a^2m^2xx^m + 8abmx^2x^m + 2b^2x^3x^m + 5a^2mxx^m + 6abx^2x^m + 6a^2xx^m}{m^3 + 6m^2 + 11m + 6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m*(b*x+a)^2,x, algorithm="giac")`

[Out] $(b^2m^2x^3x^m + 2a^2b^2m^2x^2x^m + 3b^2m^2x^3x^m + a^2m^2x^2x^m + 8a^2b^2m^2x^2x^m + 2b^2m^2x^3x^m + 5a^2m^2x^2x^m + 6a^2b^2m^2x^2x^m + 6a^2m^2x^2x^m)/(m^3 + 6m^2 + 11m + 6)$

maple [A] time = 0.00, size = 87, normalized size = 2.02

$$\frac{(b^2m^2x^2 + 2abm^2x + 3b^2mx^2 + a^2m^2 + 8abmx + 2b^2x^2 + 5a^2m + 6abx + 6a^2)x^{m+1}}{(m+3)(m+2)(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(b*x+a)^2,x)`

[Out] $(b^2m^2x^2 + 2a^2b^2m^2x + 3b^2m^2x^2 + a^2m^2 + 8a^2b^2m^2x + 2b^2m^2x^2 + 5a^2m^2 + 6a^2b^2m^2x + 6a^2m^2)/(m+3)/(m+2)/(m+1)x^{m+1}$

maxima [A] time = 1.32, size = 43, normalized size = 1.00

$$\frac{b^2x^{m+3}}{m+3} + \frac{2abx^{m+2}}{m+2} + \frac{a^2x^{m+1}}{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m*(b*x+a)^2,x, algorithm="maxima")`

[Out] $b^2 x^{m+3}/(m+3) + 2abx^{m+2}/(m+2) + a^2 x^{m+1}/(m+1)$

mupad [B] time = 0.37, size = 93, normalized size = 2.16

$$x^m \left(\frac{a^2 x (m^2 + 5m + 6)}{m^3 + 6m^2 + 11m + 6} + \frac{b^2 x^3 (m^2 + 3m + 2)}{m^3 + 6m^2 + 11m + 6} + \frac{2abx^2 (m^2 + 4m + 3)}{m^3 + 6m^2 + 11m + 6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(a + b*x)^2,x)`

[Out] $x^m((a^2 x (5m + m^2 + 6))/(11m + 6m^2 + m^3 + 6) + (b^2 x^3 (3m + m^2 + 2))/(11m + 6m^2 + m^3 + 6) + (2abx^2 (4m + m^2 + 3))/(11m + 6m^2 + m^3 + 6))$

sympy [A] time = 0.55, size = 299, normalized size = 6.95

$$\left\{ \begin{array}{l} -\frac{a^2}{2x^2} - \frac{2ab}{x} + b^2 \log(x) \\ -\frac{a^2}{x} + 2ab \log(x) + b^2 x \\ a^2 \log(x) + 2abx + \frac{b^2 x^2}{2} \\ \frac{a^2 m^2 x x^m}{m^3 + 6m^2 + 11m + 6} + \frac{5a^2 m x x^m}{m^3 + 6m^2 + 11m + 6} + \frac{6a^2 x x^m}{m^3 + 6m^2 + 11m + 6} + \frac{2ab m^2 x^2 x^m}{m^3 + 6m^2 + 11m + 6} + \frac{8ab m x^2 x^m}{m^3 + 6m^2 + 11m + 6} + \frac{6ab x^2 x^m}{m^3 + 6m^2 + 11m + 6} + \frac{b^2 m^2 x^3 x^m}{m^3 + 6m^2 + 11m + 6} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m*(b*x+a)**2,x)`

[Out] `Piecewise((-a**2/(2*x**2) - 2*a*b/x + b**2*log(x), Eq(m, -3)), (-a**2/x + 2*a*b*log(x) + b**2*x, Eq(m, -2)), (a**2*log(x) + 2*a*b*x + b**2*x**2/2, Eq(m, -1)), (a**2*m**2*x*x**m/(m**3 + 6*m**2 + 11*m + 6) + 5*a**2*m*x*x**m/(m**3 + 6*m**2 + 11*m + 6) + 6*a**2*x*x**m/(m**3 + 6*m**2 + 11*m + 6) + 2*a*b*m**2*x**2*x**m/(m**3 + 6*m**2 + 11*m + 6) + 8*a*b*m*x**2*x**m/(m**3 + 6*m**2 + 11*m + 6) + 6*a*b*x**2*x**m/(m**3 + 6*m**2 + 11*m + 6) + b**2*m**2*x**3*x**m/(m**3 + 6*m**2 + 11*m + 6) + 3*b**2*m*x**3*x**m/(m**3 + 6*m**2 + 11*m + 6) + 2*b**2*x**3*x**m/(m**3 + 6*m**2 + 11*m + 6), True))`

3.703 $\int x^m(a + bx) dx$

Optimal. Leaf size=25

$$\frac{ax^{m+1}}{m+1} + \frac{bx^{m+2}}{m+2}$$

[Out] $a*x^{(1+m)/(1+m)}+b*x^{(2+m)/(2+m)}$

Rubi [A] time = 0.01, antiderivative size = 25, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{ax^{m+1}}{m+1} + \frac{bx^{m+2}}{m+2}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x), x]

[Out] (a*x^(1 + m))/(1 + m) + (b*x^(2 + m))/(2 + m)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^m(a + bx) dx &= \int (ax^m + bx^{1+m}) dx \\ &= \frac{ax^{1+m}}{1+m} + \frac{bx^{2+m}}{2+m} \end{aligned}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 0.88

$$x^{m+1} \left(\frac{a}{m+1} + \frac{bx}{m+2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x), x]

[Out] x^(1 + m)*(a/(1 + m) + (b*x)/(2 + m))

fricas [A] time = 0.46, size = 33, normalized size = 1.32

$$\frac{((bm + b)x^2 + (am + 2a)x)x^m}{m^2 + 3m + 2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a),x, algorithm="fricas")

[Out] ((b*m + b)*x^2 + (a*m + 2*a)*x)*x^m/(m^2 + 3*m + 2)

giac [A] time = 1.02, size = 43, normalized size = 1.72

$$\frac{bmx^2x^m + amxx^m + bx^2x^m + 2axx^m}{m^2 + 3m + 2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a),x, algorithm="giac")

[Out] (b*m*x^2*x^m + a*m*x*x^m + b*x^2*x^m + 2*a*x*x^m)/(m^2 + 3*m + 2)

maple [A] time = 0.00, size = 31, normalized size = 1.24

$$\frac{(bmx + am + bx + 2a)x^{m+1}}{(m + 2)(m + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(b*x+a),x)

[Out] (b*m*x+a*m+b*x+2*a)/(m+2)/(m+1)*x^(m+1)

maxima [A] time = 1.35, size = 25, normalized size = 1.00

$$\frac{bx^{m+2}}{m+2} + \frac{ax^{m+1}}{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a),x, algorithm="maxima")

[Out] b*x^(m + 2)/(m + 2) + a*x^(m + 1)/(m + 1)

mupad [B] time = 0.30, size = 30, normalized size = 1.20

$$\frac{x^{m+1} (2a + am + bx + bmx)}{m^2 + 3m + 2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(a + b*x), x)`

[Out] $(x^{(m + 1)}*(2*a + a*m + b*x + b*m*x))/(3*m + m^2 + 2)$

sympy [A] time = 0.31, size = 87, normalized size = 3.48

$$\begin{cases} -\frac{a}{x} + b \log(x) & \text{for } m = -2 \\ a \log(x) + bx & \text{for } m = -1 \\ \frac{amx^m}{m^2+3m+2} + \frac{2axx^m}{m^2+3m+2} + \frac{bmx^2x^m}{m^2+3m+2} + \frac{bx^2x^m}{m^2+3m+2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m*(b*x+a), x)`

[Out] `Piecewise((-a/x + b*log(x), Eq(m, -2)), (a*log(x) + b*x, Eq(m, -1)), (a*m*x*x**m/(m**2 + 3*m + 2) + 2*a*x*x**m/(m**2 + 3*m + 2) + b*m*x**2*x**m/(m**2 + 3*m + 2) + b*x**2*x**m/(m**2 + 3*m + 2), True))`

$$3.704 \quad \int \frac{x^m}{a+bx} dx$$

Optimal. Leaf size=29

$$\frac{x^{m+1} {}_2F_1\left(1, m+1; m+2; -\frac{bx}{a}\right)}{a(m+1)}$$

[Out] $x^{(1+m)} \cdot \text{hypergeom}([1, 1+m], [2+m], -b*x/a)/a/(1+m)$

Rubi [A] time = 0.01, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {64}

$$\frac{x^{m+1} {}_2F_1\left(1, m+1; m+2; -\frac{bx}{a}\right)}{a(m+1)}$$

Antiderivative was successfully verified.

[In] Int[x^m/(a + b*x), x]

[Out] $(x^{(1+m)} \cdot \text{Hypergeometric2F1}[1, 1+m, 2+m, -((b*x)/a)]) / (a*(1+m))$

Rule 64

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -((d*x)/c)])/ (b*(m+1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)]) && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rubi steps

$$\int \frac{x^m}{a+bx} dx = \frac{x^{1+m} {}_2F_1\left(1, 1+m; 2+m; -\frac{bx}{a}\right)}{a(1+m)}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 1.00

$$\frac{x^{m+1} {}_2F_1\left(1, m+1; m+2; -\frac{bx}{a}\right)}{a(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[x^m/(a + b*x), x]

[Out] $(x^{(1+m)} \text{Hypergeometric2F1}[1, 1+m, 2+m, -((b*x)/a)]) / (a*(1+m))$
fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^m}{bx+a}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m/(b*x+a),x, algorithm="fricas")`

[Out] `integral(x^m/(b*x + a), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{bx+a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m/(b*x+a),x, algorithm="giac")`

[Out] `integrate(x^m/(b*x + a), x)`

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^m}{bx+a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m/(b*x+a),x)`

[Out] `int(x^m/(b*x+a),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{bx+a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m/(b*x+a),x, algorithm="maxima")`

[Out] `integrate(x^m/(b*x + a), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^m}{a+bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m/(a + b*x), x)`

[Out] `int(x^m/(a + b*x), x)`

sympy [C] time = 0.78, size = 61, normalized size = 2.10

$$\frac{m x x^m \Phi\left(\frac{b x e^{i \pi}}{a}, 1, m+1\right) \Gamma(m+1)}{a \Gamma(m+2)} + \frac{x x^m \Phi\left(\frac{b x e^{i \pi}}{a}, 1, m+1\right) \Gamma(m+1)}{a \Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m/(b*x+a), x)`

[Out] `m*x*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(a*gamma(m + 2)) + x*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(a*gamma(m + 2))`

$$3.705 \quad \int \frac{x^m}{(a+bx)^2} dx$$

Optimal. Leaf size=29

$$\frac{x^{m+1} {}_2F_1\left(2, m+1; m+2; -\frac{bx}{a}\right)}{a^2(m+1)}$$

[Out] $x^{(1+m)} \cdot \text{hypergeom}([2, 1+m], [2+m], -b*x/a) / a^2 / (1+m)$

Rubi [A] time = 0.01, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {64}

$$\frac{x^{m+1} {}_2F_1\left(2, m+1; m+2; -\frac{bx}{a}\right)}{a^2(m+1)}$$

Antiderivative was successfully verified.

[In] Int[x^m/(a + b*x)^2, x]

[Out] $(x^{(1+m)} \cdot \text{Hypergeometric2F1}[2, 1+m, 2+m, -((b*x)/a)]) / (a^2 * (1+m))$

Rule 64

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -((d*x)/c)]/(b*(m+1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rubi steps

$$\int \frac{x^m}{(a+bx)^2} dx = \frac{x^{1+m} {}_2F_1\left(2, 1+m; 2+m; -\frac{bx}{a}\right)}{a^2(1+m)}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 1.00

$$\frac{x^{m+1} {}_2F_1\left(2, m+1; m+2; -\frac{bx}{a}\right)}{a^2(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[x^m/(a + b*x)^2,x]

[Out] (x^(1 + m)*Hypergeometric2F1[2, 1 + m, 2 + m, -((b*x)/a)])/(a^2*(1 + m))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^m}{b^2x^2 + 2abx + a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^2,x, algorithm="fricas")

[Out] integral(x^m/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^2,x, algorithm="giac")

[Out] integrate(x^m/(b*x + a)^2, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(b*x+a)^2,x)

[Out] int(x^m/(b*x+a)^2,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^2,x, algorithm="maxima")

[Out] integrate(x^m/(b*x + a)^2, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^m}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(a + b*x)^2, x)

[Out] int(x^m/(a + b*x)^2, x)

sympy [C] time = 1.04, size = 262, normalized size = 9.03

$$\frac{am^2xx^m\Phi\left(\frac{bx e^{i\pi}}{a}, 1, m+1\right)\Gamma(m+1)}{a^3\Gamma(m+2) + a^2bx\Gamma(m+2)} - \frac{amxx^m\Phi\left(\frac{bx e^{i\pi}}{a}, 1, m+1\right)\Gamma(m+1)}{a^3\Gamma(m+2) + a^2bx\Gamma(m+2)} + \frac{amxx^m\Gamma(m+1)}{a^3\Gamma(m+2) + a^2bx\Gamma(m+2)} + \frac{1}{a^3\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m/(b*x+a)**2, x)

[Out] -a*m**2*x*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(a**3*gamma(m + 2) + a**2*b*x*gamma(m + 2)) - a*m*x*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(a**3*gamma(m + 2) + a**2*b*x*gamma(m + 2)) + a*m*x*x**m*gamma(m + 1)/(a**3*gamma(m + 2) + a**2*b*x*gamma(m + 2)) + a*x*x**m*gamma(m + 1)/(a**3*gamma(m + 2) + a**2*b*x*gamma(m + 2)) - b*m**2*x*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(a**3*gamma(m + 2) + a**2*b*x*gamma(m + 2)) - b*m*x**2*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(a**3*gamma(m + 2) + a**2*b*x*gamma(m + 2))

$$3.706 \quad \int \frac{x^m}{(a+bx)^3} dx$$

Optimal. Leaf size=29

$$\frac{x^{m+1} {}_2F_1\left(3, m+1; m+2; -\frac{bx}{a}\right)}{a^3(m+1)}$$

[Out] $x^{(1+m)} \cdot \text{hypergeom}([3, 1+m], [2+m], -b*x/a)/a^3/(1+m)$

Rubi [A] time = 0.01, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {64}

$$\frac{x^{m+1} {}_2F_1\left(3, m+1; m+2; -\frac{bx}{a}\right)}{a^3(m+1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^m/(a + b*x)^3, x]$

[Out] $(x^{(1+m)} \cdot \text{Hypergeometric2F1}[3, 1+m, 2+m, -(b*x)/a]) / (a^3 * (1+m))$

Rule 64

$\text{Int}[\frac{(b \cdot x)^m \cdot ((c) + (d \cdot x)^n)}{(a + b \cdot x)^3}, x_Symbol] \rightarrow \text{Simp}[\frac{(c^n \cdot (b \cdot x)^{m+1} \cdot \text{Hypergeometric2F1}[-n, m+1, m+2, -(d \cdot x)/c])}{(b \cdot (m+1))}, x]$
 /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rubi steps

$$\int \frac{x^m}{(a+bx)^3} dx = \frac{x^{1+m} {}_2F_1\left(3, 1+m; 2+m; -\frac{bx}{a}\right)}{a^3(1+m)}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 1.00

$$\frac{x^{m+1} {}_2F_1\left(3, m+1; m+2; -\frac{bx}{a}\right)}{a^3(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[x^m/(a + b*x)^3,x]

[Out] (x^(1 + m)*Hypergeometric2F1[3, 1 + m, 2 + m, -((b*x)/a)])/(a^3*(1 + m))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^m}{b^3x^3 + 3ab^2x^2 + 3a^2bx + a^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^3,x, algorithm="fricas")

[Out] integral(x^m/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx + a)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^3,x, algorithm="giac")

[Out] integrate(x^m/(b*x + a)^3, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx + a)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(b*x+a)^3,x)

[Out] int(x^m/(b*x+a)^3,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx + a)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^3,x, algorithm="maxima")

[Out] integrate(x^m/(b*x + a)^3, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^m}{(a + bx)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(a + b*x)^3,x)

[Out] int(x^m/(a + b*x)^3, x)

sympy [C] time = 1.45, size = 717, normalized size = 24.72

$$\frac{a^2 m^3 x x^m \Phi\left(\frac{bx e^{i\pi}}{a}, 1, m + 1\right) \Gamma(m + 1)}{2a^5 \Gamma(m + 2) + 4a^4 b x \Gamma(m + 2) + 2a^3 b^2 x^2 \Gamma(m + 2)} - \frac{a^2 m^2 x x^m \Gamma(m + 1)}{2a^5 \Gamma(m + 2) + 4a^4 b x \Gamma(m + 2) + 2a^3 b^2 x^2 \Gamma(m + 2)} - \frac{2a^5 \Gamma(m + 2)}{2a^5 \Gamma(m + 2) + 4a^4 b x \Gamma(m + 2) + 2a^3 b^2 x^2 \Gamma(m + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m/(b*x+a)**3,x)

[Out] a**2*m**3*x*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2)) - a**2*m**2*x*x**m*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2)) - a**2*m*x*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2)) + a**2*m*x*x**m*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2)) + 2*a**2*x*x**m*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2)) + 2*a*b*m**3*x**2*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2)) - a*b*m**2*x**2*x**m*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2)) - 2*a*b*m*x**2*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2)) + a*b*x**2*x**m*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2)) + b**2*m**3*x**3*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2)) - b**2*m*x**3*x**m*lerchphi(b*x*exp_polar(I*pi)/a, 1, m + 1)*gamma(m + 1)/(2*a**5*gamma(m + 2) + 4*a**4*b*x*gamma(m + 2) + 2*a**3*b**2*x**2*gamma(m + 2))

3.707 $\int x^m (a + bx)^{5/2} dx$

Optimal. Leaf size=48

$$\frac{2x^m (a + bx)^{7/2} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{7}{2}, -m; \frac{9}{2}; \frac{bx}{a} + 1\right)}{7b}$$

[Out] $2/7*x^m*(b*x+a)^{(7/2)}*hypergeom([7/2, -m], [9/2], 1+b*x/a)/b/((-b*x/a)^m)$

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {67, 65}

$$\frac{2x^m (a + bx)^{7/2} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{7}{2}, -m; \frac{9}{2}; \frac{bx}{a} + 1\right)}{7b}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x)^(5/2), x]

[Out] $(2*x^m*(a + b*x)^{(7/2)}*Hypergeometric2F1[7/2, -m, 9/2, 1 + (b*x)/a])/(7*b*(-(b*x)/a)^m)$

Rule 65

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])
```

Rule 67

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(-(b*c)/d)^IntPart[m]*(b*x)^FracPart[m]/(-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)^m*(c + d*x)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]
```

Rubi steps

$$\int x^m (a + bx)^{5/2} dx = \left(x^m \left(-\frac{bx}{a} \right)^{-m} \right) \int \left(-\frac{bx}{a} \right)^m (a + bx)^{5/2} dx$$

$$= \frac{2x^m \left(-\frac{bx}{a} \right)^{-m} (a + bx)^{7/2} {}_2F_1 \left(\frac{7}{2}, -m; \frac{9}{2}; 1 + \frac{bx}{a} \right)}{7b}$$

Mathematica [A] time = 0.06, size = 48, normalized size = 1.00

$$\frac{2x^m (a + bx)^{7/2} \left(-\frac{bx}{a} \right)^{-m} {}_2F_1 \left(\frac{7}{2}, -m; \frac{9}{2}; \frac{bx}{a} + 1 \right)}{7b}$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x)^(5/2),x]

[Out] (2*x^m*(a + b*x)^(7/2)*Hypergeometric2F1[7/2, -m, 9/2, 1 + (b*x)/a])/(7*b*(-((b*x)/a))^m)

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(b^2x^2 + 2abx + a^2\right)\sqrt{bx + a}x^m, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^(5/2),x, algorithm="fricas")

[Out] integral((b^2*x^2 + 2*a*b*x + a^2)*sqrt(b*x + a)*x^m, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{2}} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^(5/2),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/2)*x^m, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{2}} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(b*x+a)^(5/2),x)`

[Out] `int(x^m*(b*x+a)^(5/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{2}} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m*(b*x+a)^(5/2),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(5/2)*x^m, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^m (a + bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(a + b*x)^(5/2),x)`

[Out] `int(x^m*(a + b*x)^(5/2), x)`

sympy [C] time = 10.17, size = 37, normalized size = 0.77

$$\frac{a^{\frac{5}{2}} x x^m \Gamma(m+1) {}_2F_1\left(-\frac{5}{2}, m+1 \left| \frac{bx e^{i\pi}}{a} \right. \right)}{\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m*(b*x+a)**(5/2),x)`

[Out] `a**(5/2)*x*x**m*gamma(m + 1)*hyper((-5/2, m + 1), (m + 2,), b*x*exp_polar(I*pi)/a)/gamma(m + 2)`

3.708 $\int x^m (a + bx)^{3/2} dx$

Optimal. Leaf size=48

$$\frac{2x^m (a + bx)^{5/2} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{5}{2}, -m; \frac{7}{2}; \frac{bx}{a} + 1\right)}{5b}$$

[Out] $2/5*x^m*(b*x+a)^{(5/2)}*hypergeom([5/2, -m], [7/2], 1+b*x/a)/b/((-b*x/a)^m)$

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {67, 65}

$$\frac{2x^m (a + bx)^{5/2} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{5}{2}, -m; \frac{7}{2}; \frac{bx}{a} + 1\right)}{5b}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x)^(3/2), x]

[Out] $(2*x^m*(a + b*x)^{(5/2)}*Hypergeometric2F1[5/2, -m, 7/2, 1 + (b*x)/a])/(5*b*(-((b*x)/a))^m)$

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(-(b*c)/d)^IntPart[m]*(b*x)^FracPart[m]/(-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)^m*(c + d*x)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\int x^m (a + bx)^{3/2} dx = \left(x^m \left(-\frac{bx}{a} \right)^{-m} \right) \int \left(-\frac{bx}{a} \right)^m (a + bx)^{3/2} dx$$

$$= \frac{2x^m \left(-\frac{bx}{a} \right)^{-m} (a + bx)^{5/2} {}_2F_1 \left(\frac{5}{2}, -m; \frac{7}{2}; 1 + \frac{bx}{a} \right)}{5b}$$

Mathematica [A] time = 0.04, size = 48, normalized size = 1.00

$$\frac{2x^m (a + bx)^{5/2} \left(-\frac{bx}{a} \right)^{-m} {}_2F_1 \left(\frac{5}{2}, -m; \frac{7}{2}; \frac{bx}{a} + 1 \right)}{5b}$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x)^(3/2), x]

[Out] (2*x^m*(a + b*x)^(5/2)*Hypergeometric2F1[5/2, -m, 7/2, 1 + (b*x)/a])/(5*b*(-((b*x)/a))^m)

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral} \left((bx + a)^{\frac{3}{2}} x^m, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^(3/2), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)*x^m, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^(3/2), x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)*x^m, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(b*x+a)^(3/2),x)`

[Out] `int(x^m*(b*x+a)^(3/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m*(b*x+a)^(3/2),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(3/2)*x^m, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^m (a + bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(a + b*x)^(3/2),x)`

[Out] `int(x^m*(a + b*x)^(3/2), x)`

sympy [C] time = 3.46, size = 37, normalized size = 0.77

$$\frac{a^{\frac{3}{2}} x x^m \Gamma(m+1) {}_2F_1\left(-\frac{3}{2}, m+1 \left| \frac{bx e^{i\pi}}{a} \right. \right)}{\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m*(b*x+a)**(3/2),x)`

[Out] `a**(3/2)*x*x**m*gamma(m + 1)*hyper((-3/2, m + 1), (m + 2,), b*x*exp_polar(I*pi)/a)/gamma(m + 2)`

3.709 $\int x^m \sqrt{a + bx} dx$

Optimal. Leaf size=48

$$\frac{2x^m(a+bx)^{3/2} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{3}{2}, -m; \frac{5}{2}; \frac{bx}{a} + 1\right)}{3b}$$

[Out] $2/3*x^m*(b*x+a)^{(3/2)*hypergeom([3/2, -m], [5/2], 1+b*x/a)/b/((-b*x/a)^m)$

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {67, 65}

$$\frac{2x^m(a+bx)^{3/2} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{3}{2}, -m; \frac{5}{2}; \frac{bx}{a} + 1\right)}{3b}$$

Antiderivative was successfully verified.

[In] Int[x^m*Sqrt[a + b*x], x]

[Out] $(2*x^m*(a + b*x)^{(3/2)*Hypergeometric2F1[3/2, -m, 5/2, 1 + (b*x)/a]} / (3*b*(-((b*x)/a))^m)$

Rule 65

Int[((b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c]) / (d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Dist[(-(b*c)/d)^(n+1)*IntPart[m]*(b*x)^FracPart[m] / (-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)^(n+1)*IntPart[m]*(c + d*x)^n, x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\int x^m \sqrt{a+bx} dx = \left(x^m \left(-\frac{bx}{a} \right)^{-m} \right) \int \left(-\frac{bx}{a} \right)^m \sqrt{a+bx} dx$$

$$= \frac{2x^m \left(-\frac{bx}{a} \right)^{-m} (a+bx)^{3/2} {}_2F_1 \left(\frac{3}{2}, -m; \frac{5}{2}; 1 + \frac{bx}{a} \right)}{3b}$$

Mathematica [A] time = 0.03, size = 48, normalized size = 1.00

$$\frac{2x^m (a+bx)^{3/2} \left(-\frac{bx}{a} \right)^{-m} {}_2F_1 \left(\frac{3}{2}, -m; \frac{5}{2}; \frac{bx}{a} + 1 \right)}{3b}$$

Antiderivative was successfully verified.

[In] Integrate[x^m*Sqrt[a + b*x], x]

[Out] (2*x^m*(a + b*x)^(3/2)*Hypergeometric2F1[3/2, -m, 5/2, 1 + (b*x)/a])/(3*b*(-((b*x)/a))^m)

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral} \left(\sqrt{bx+a} x^m, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^(1/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*x^m, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^(1/2), x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)*x^m, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(b*x+a)^(1/2),x)`

[Out] `int(x^m*(b*x+a)^(1/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m*(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] `integrate(sqrt(b*x + a)*x^m, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^m \sqrt{a+bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(a + b*x)^(1/2),x)`

[Out] `int(x^m*(a + b*x)^(1/2), x)`

sympy [C] time = 1.68, size = 37, normalized size = 0.77

$$\frac{\sqrt{a} x x^m \Gamma(m+1) {}_2F_1\left(-\frac{1}{2}, m+1 \mid \frac{bx e^{i\pi}}{a}\right)}{\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m*(b*x+a)**(1/2),x)`

[Out] `sqrt(a)*x*x**m*gamma(m + 1)*hyper((-1/2, m + 1), (m + 2,), b*x*exp_polar(I*pi)/a)/gamma(m + 2)`

$$3.710 \quad \int \frac{x^m}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=46

$$\frac{2x^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b}$$

[Out] 2*x^m*hypergeom([1/2, -m], [3/2], 1+b*x/a)*(b*x+a)^(1/2)/b/((-b*x/a)^m)

Rubi [A] time = 0.01, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {67, 65}

$$\frac{2x^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[x^m/Sqrt[a + b*x], x]

[Out] (2*x^m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, -m, 3/2, 1 + (b*x)/a])/(b*(-(b*x)/a))^m)

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(-(b*c)/d)^IntPart[m]*(b*x)^FracPart[m]/(-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)]^m*(c + d*x)^n, x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\int \frac{x^m}{\sqrt{a+bx}} dx = \left(x^m \left(-\frac{bx}{a} \right)^{-m} \right) \int \frac{\left(-\frac{bx}{a} \right)^m}{\sqrt{a+bx}} dx$$

$$= \frac{2x^m \left(-\frac{bx}{a} \right)^{-m} \sqrt{a+bx} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 1 + \frac{bx}{a}\right)}{b}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 1.00

$$\frac{2x^m \sqrt{a+bx} \left(-\frac{bx}{a} \right)^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[x^m/Sqrt[a + b*x], x]

[Out] (2*x^m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, -m, 3/2, 1 + (b*x)/a])/(b*(-((b*x)/a))^m)

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^m}{\sqrt{bx+a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] integral(x^m/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^(1/2), x, algorithm="giac")

[Out] integrate(x^m/sqrt(b*x + a), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(1/2)*x^m,x)`

[Out] `int(1/(b*x+a)^(1/2)*x^m,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m/(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] `integrate(x^m/sqrt(b*x + a), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^m}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m/(a + b*x)^(1/2),x)`

[Out] `int(x^m/(a + b*x)^(1/2), x)`

sympy [C] time = 1.56, size = 36, normalized size = 0.78

$$\frac{xx^m \Gamma(m+1) {}_2F_1\left(\frac{1}{2}, m+1 \mid \frac{bx e^{i\pi}}{a}\right)}{\sqrt{a} \Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m/(b*x+a)**(1/2),x)`

[Out] `x*x**m*gamma(m + 1)*hyper((1/2, m + 1), (m + 2,), b*x*exp_polar(I*pi)/a)/(sqrt(a)*gamma(m + 2))`

$$3.711 \quad \int \frac{x^m}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=46

$$-\frac{2x^m \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(-\frac{1}{2}, -m; \frac{1}{2}; \frac{bx}{a} + 1\right)}{b\sqrt{a+bx}}$$

[Out] $-2*x^m*\text{hypergeom}([-1/2, -m], [1/2], 1+b*x/a)/b/((-b*x/a)^m)/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {67, 65}

$$-\frac{2x^m \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(-\frac{1}{2}, -m; \frac{1}{2}; \frac{bx}{a} + 1\right)}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^m/(a + b*x)^{(3/2)}, x]$

[Out] $(-2*x^m*\text{Hypergeometric2F1}[-1/2, -m, 1/2, 1 + (b*x)/a])/(b*(-((b*x)/a))^m*\text{Sqrt}[a + b*x])$

Rule 65

$\text{Int}[(b_.*(x_))^{(m_)*((c_)+(d_.*(x_))^{(n_)}), x_Symbol] :> \text{Simp}[(c + d*x)^{(n + 1)*\text{Hypergeometric2F1}[-m, n + 1, n + 2, 1 + (d*x)/c]}/(d*(n + 1)*(-(d/(b*c)))^m), x] /;$ $\text{FreeQ}\{b, c, d, m, n\}, x \ \&\& \ !\text{IntegerQ}[n] \ \&\& \ (\text{IntegerQ}[m] \ || \ \text{GtQ}[-(d/(b*c)), 0])$

Rule 67

$\text{Int}[(b_.*(x_))^{(m_)*((c_)+(d_.*(x_))^{(n_)}), x_Symbol] :> \text{Dist}[(-(b*c)/d)^{\text{IntPart}[m]}*(b*x)^{\text{FracPart}[m]}/(-(d*x)/c)^{\text{FracPart}[m]}, \text{Int}[(-(d*x)/c)^m*(c + d*x)^n, x], x] /;$ $\text{FreeQ}\{b, c, d, m, n\}, x \ \&\& \ !\text{IntegerQ}[m] \ \&\& \ !\text{IntegerQ}[n] \ \&\& \ !\text{GtQ}[c, 0] \ \&\& \ !\text{GtQ}[-(d/(b*c)), 0]$

Rubi steps

$$\int \frac{x^m}{(a+bx)^{3/2}} dx = \left(x^m \left(-\frac{bx}{a} \right)^{-m} \right) \int \frac{\left(-\frac{bx}{a} \right)^m}{(a+bx)^{3/2}} dx$$

$$= -\frac{2x^m \left(-\frac{bx}{a} \right)^{-m} {}_2F_1\left(-\frac{1}{2}, -m; \frac{1}{2}; 1 + \frac{bx}{a}\right)}{b\sqrt{a+bx}}$$

Mathematica [A] time = 0.04, size = 46, normalized size = 1.00

$$-\frac{2x^m \left(-\frac{bx}{a} \right)^{-m} {}_2F_1\left(-\frac{1}{2}, -m; \frac{1}{2}; \frac{bx}{a} + 1\right)}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Integrate[x^m/(a + b*x)^(3/2),x]

[Out] (-2*x^m*Hypergeometric2F1[-1/2, -m, 1/2, 1 + (b*x)/a])/(b*(-((b*x)/a))^m*Sqrt[a + b*x])

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a} x^m}{b^2 x^2 + 2 abx + a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*x^m/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^(3/2),x, algorithm="giac")

[Out] integrate(x^m/(b*x + a)^(3/2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(b*x+a)^(3/2), x)

[Out] int(x^m/(b*x+a)^(3/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^(3/2), x, algorithm="maxima")

[Out] integrate(x^m/(b*x + a)^(3/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^m}{(a + bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(a + b*x)^(3/2), x)

[Out] int(x^m/(a + b*x)^(3/2), x)

sympy [C] time = 1.90, size = 36, normalized size = 0.78

$$\frac{xx^m \Gamma(m+1) {}_2F_1\left(\frac{3}{2}, m+1 \mid \frac{bx e^{i\pi}}{a}\right)}{a^{\frac{3}{2}} \Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m/(b*x+a)**(3/2), x)

[Out] x*x**m*gamma(m + 1)*hyper((3/2, m + 1), (m + 2,), b*x*exp_polar(I*pi)/a)/(a** (3/2)*gamma(m + 2))

$$3.712 \quad \int \frac{x^m}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=48

$$-\frac{2x^m \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(-\frac{3}{2}, -m; -\frac{1}{2}; \frac{bx}{a} + 1\right)}{3b(a+bx)^{3/2}}$$

[Out] $-2/3*x^m*\text{hypergeom}([-3/2, -m], [-1/2], 1+b*x/a)/b/((-b*x/a)^m)/(b*x+a)^{(3/2)}$

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {67, 65}

$$-\frac{2x^m \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(-\frac{3}{2}, -m; -\frac{1}{2}; \frac{bx}{a} + 1\right)}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[x^m/(a + b*x)^(5/2), x]

[Out] $(-2*x^m*\text{Hypergeometric2F1}[-3/2, -m, -1/2, 1 + (b*x)/a])/(3*b*(-((b*x)/a))^m*(a + b*x)^{(3/2)})$

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(-(b*c)/d)^(n+1)*IntPart[m]*(b*x)^FracPart[m]/(-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)^(n+1)*m*(c + d*x)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\int \frac{x^m}{(a+bx)^{5/2}} dx = \left(x^m \left(-\frac{bx}{a} \right)^{-m} \right) \int \frac{\left(-\frac{bx}{a} \right)^m}{(a+bx)^{5/2}} dx$$

$$= -\frac{2x^m \left(-\frac{bx}{a} \right)^{-m} {}_2F_1\left(-\frac{3}{2}, -m; -\frac{1}{2}; 1 + \frac{bx}{a}\right)}{3b(a+bx)^{3/2}}$$

Mathematica [A] time = 0.04, size = 48, normalized size = 1.00

$$-\frac{2x^m \left(-\frac{bx}{a} \right)^{-m} {}_2F_1\left(-\frac{3}{2}, -m; -\frac{1}{2}; \frac{bx}{a} + 1\right)}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^m/(a + b*x)^(5/2), x]

[Out] (-2*x^m*Hypergeometric2F1[-3/2, -m, -1/2, 1 + (b*x)/a])/(3*b*(-((b*x)/a))^m*(a + b*x)^(3/2))

fricas [F] time = 0.54, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a} x^m}{b^3 x^3 + 3 a b^2 x^2 + 3 a^2 b x + a^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*x^m/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx+a)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^(5/2), x, algorithm="giac")

[Out] integrate(x^m/(b*x + a)^(5/2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(b*x+a)^(5/2), x)

[Out] int(x^m/(b*x+a)^(5/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^(5/2), x, algorithm="maxima")

[Out] integrate(x^m/(b*x + a)^(5/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^m}{(a + bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(a + b*x)^(5/2), x)

[Out] int(x^m/(a + b*x)^(5/2), x)

sympy [C] time = 3.54, size = 36, normalized size = 0.75

$$\frac{xx^m \Gamma(m + 1) {}_2F_1\left(\frac{5}{2}, m + 1 \mid \frac{bx e^{i\pi}}{a}\right)}{a^{\frac{5}{2}} \Gamma(m + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m/(b*x+a)**(5/2), x)

[Out] x*x**m*gamma(m + 1)*hyper((5/2, m + 1), (m + 2,), b*x*exp_polar(I*pi)/a)/(a** (5/2)*gamma(m + 2))

$$3.713 \quad \int \frac{x^{2+m}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=51

$$\frac{2a^2x^m\sqrt{a+bx}\left(-\frac{bx}{a}\right)^{-m}{}_2F_1\left(\frac{1}{2}, -m-2; \frac{3}{2}; \frac{bx}{a}+1\right)}{b^3}$$

[Out] $2*a^2*x^m*\text{hypergeom}([1/2, -2-m], [3/2], 1+b*x/a)*(b*x+a)^{(1/2)}/b^3/((-b*x/a)^m)$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {67, 65}

$$\frac{2a^2x^m\sqrt{a+bx}\left(-\frac{bx}{a}\right)^{-m}{}_2F_1\left(\frac{1}{2}, -m-2; \frac{3}{2}; \frac{bx}{a}+1\right)}{b^3}$$

Antiderivative was successfully verified.

[In] Int[x^(2 + m)/Sqrt[a + b*x], x]

[Out] $(2*a^2*x^m*\text{Sqrt}[a + b*x]*\text{Hypergeometric2F1}[1/2, -2 - m, 3/2, 1 + (b*x)/a])/ (b^3*(-((b*x)/a))^m)$

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(-(b*c)/d)^IntPart[m]*(b*x)^FracPart[m]/(-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)^m*(c + d*x)^n, x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\int \frac{x^{2+m}}{\sqrt{a+bx}} dx = \frac{\left(a^2 x^m \left(-\frac{bx}{a}\right)^{-m}\right) \int \frac{\left(-\frac{bx}{a}\right)^{2+m}}{\sqrt{a+bx}} dx}{b^2}$$

$$= \frac{2a^2 x^m \left(-\frac{bx}{a}\right)^{-m} \sqrt{a+bx} {}_2F_1\left(\frac{1}{2}, -2-m; \frac{3}{2}; 1 + \frac{bx}{a}\right)}{b^3}$$

Mathematica [A] time = 0.04, size = 51, normalized size = 1.00

$$\frac{2a^2 x^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, -m-2; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^(2 + m)/Sqrt[a + b*x], x]

[Out] (2*a^2*x^m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, -2 - m, 3/2, 1 + (b*x)/a])/ (b^3*(-((b*x)/a))^m)

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^{m+2}}{\sqrt{bx+a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2+m)/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] integral(x^(m + 2)/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{m+2}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2+m)/(b*x+a)^(1/2), x, algorithm="giac")

[Out] integrate(x^(m + 2)/sqrt(b*x + a), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^{m+2}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(m+2)/(b*x+a)^(1/2),x)

[Out] int(x^(m+2)/(b*x+a)^(1/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{m+2}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(2+m)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] integrate(x^(m + 2)/sqrt(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^{m+2}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(m + 2)/(a + b*x)^(1/2),x)

[Out] int(x^(m + 2)/(a + b*x)^(1/2), x)

sympy [C] time = 3.38, size = 37, normalized size = 0.73

$$\frac{x^3 x^m \Gamma(m+3) {}_2F_1\left(\frac{1}{2}, m+3 \left| \frac{bx e^{i\pi}}{a} \right.\right)}{\sqrt{a} \Gamma(m+4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(2+m)/(b*x+a)**(1/2),x)

[Out] x**3*x**m*gamma(m + 3)*hyper((1/2, m + 3), (m + 4,), b*x*exp_polar(I*pi)/a)/(sqrt(a)*gamma(m + 4))

$$3.714 \quad \int \frac{x^{1+m}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=49

$$\frac{2ax^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, -m-1; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b^2}$$

[Out] $-2*a*x^m*\text{hypergeom}([1/2, -1-m], [3/2], 1+b*x/a)*(b*x+a)^{(1/2)}/b^2/((-b*x/a)^m)$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {67, 65}

$$\frac{2ax^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, -m-1; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(1+m)}/\text{Sqrt}[a+b*x], x]$

[Out] $(-2*a*x^m*\text{Sqrt}[a+b*x]*\text{Hypergeometric2F1}[1/2, -1-m, 3/2, 1+(b*x)/a])/b^2*(-((b*x)/a))^m$

Rule 65

$\text{Int}[\left((b_)*(x_)\right)^{(m_)*\left((c_)+(d_)*(x_)\right)^{(n_)}, x_Symbol] :> \text{Simp}[\left((c+d*x)\right)^{(n+1)*\text{Hypergeometric2F1}[-m, n+1, n+2, 1+(d*x)/c]}/(d*(n+1)*(-d/(b*c)))^m, x] /; \text{FreeQ}\{b, c, d, m, n\}, x] \&\& !\text{IntegerQ}[n] \&\& (\text{IntegerQ}[m] \parallel \text{GtQ}[-d/(b*c), 0])$

Rule 67

$\text{Int}[\left((b_)*(x_)\right)^{(m_)*\left((c_)+(d_)*(x_)\right)^{(n_)}, x_Symbol] :> \text{Dist}[\left(-((b*c)/d)\right)^{\text{IntPart}[m]*\text{FracPart}[m]}/\left(-((d*x)/c)\right)^{\text{FracPart}[m]}, \text{Int}[\left(-((d*x)/c)\right)^m*(c+d*x)^n, x], x] /; \text{FreeQ}\{b, c, d, m, n\}, x] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& !\text{GtQ}[c, 0] \&\& !\text{GtQ}[-d/(b*c), 0]$

Rubi steps

$$\int \frac{x^{1+m}}{\sqrt{a+bx}} dx = -\frac{\left(ax^m \left(-\frac{bx}{a}\right)^{-m}\right) \int \frac{\left(-\frac{bx}{a}\right)^{1+m}}{\sqrt{a+bx}} dx}{b}$$

$$= -\frac{2ax^m \left(-\frac{bx}{a}\right)^{-m} \sqrt{a+bx} {}_2F_1\left(\frac{1}{2}, -1-m; \frac{3}{2}; 1 + \frac{bx}{a}\right)}{b^2}$$

Mathematica [A] time = 0.03, size = 49, normalized size = 1.00

$$\frac{2ax^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, -m-1; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(1+m)/Sqrt[a+b*x],x]

[Out] (-2*a*x^m*Sqrt[a+b*x]*Hypergeometric2F1[1/2, -1-m, 3/2, 1+(b*x)/a])/ (b^2*(-((b*x)/a))^m)

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^{m+1}}{\sqrt{bx+a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1+m)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] integral(x^(m+1)/sqrt(b*x+a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{m+1}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1+m)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] integrate(x^(m+1)/sqrt(b*x+a), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^{m+1}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(m+1)/(b*x+a)^(1/2),x)

[Out] int(x^(m+1)/(b*x+a)^(1/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{m+1}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1+m)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] integrate(x^(m + 1)/sqrt(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^{m+1}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(m + 1)/(a + b*x)^(1/2),x)

[Out] int(x^(m + 1)/(a + b*x)^(1/2), x)

sympy [C] time = 2.47, size = 37, normalized size = 0.76

$$\frac{x^2 x^m \Gamma(m+2) {}_2F_1\left(\frac{1}{2}, m+2 \left| \frac{bx e^{i\pi}}{a} \right. \right)}{\sqrt{a} \Gamma(m+3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(1+m)/(b*x+a)**(1/2),x)

[Out] x**2*x**m*gamma(m + 2)*hyper((1/2, m + 2), (m + 3,), b*x*exp_polar(I*pi)/a)/(sqrt(a)*gamma(m + 3))

$$3.715 \quad \int \frac{x^m}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=46

$$\frac{2x^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b}$$

[Out] 2*x^m*hypergeom([1/2, -m], [3/2], 1+b*x/a)*(b*x+a)^(1/2)/b/((-b*x/a)^m)

Rubi [A] time = 0.01, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {67, 65}

$$\frac{2x^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[x^m/Sqrt[a + b*x], x]

[Out] (2*x^m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, -m, 3/2, 1 + (b*x)/a])/(b*(-((b*x)/a))^m)

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(-(b*c)/d)^IntPart[m]*(b*x)^FracPart[m]/(-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)^m*(c + d*x)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\int \frac{x^m}{\sqrt{a+bx}} dx = \left(x^m \left(-\frac{bx}{a} \right)^{-m} \right) \int \frac{\left(-\frac{bx}{a} \right)^m}{\sqrt{a+bx}} dx$$

$$= \frac{2x^m \left(-\frac{bx}{a} \right)^{-m} \sqrt{a+bx} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 1 + \frac{bx}{a}\right)}{b}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 1.00

$$\frac{2x^m \sqrt{a+bx} \left(-\frac{bx}{a} \right)^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[x^m/Sqrt[a + b*x], x]

[Out] (2*x^m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, -m, 3/2, 1 + (b*x)/a])/(b*(-((b*x)/a))^m)

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^m}{\sqrt{bx+a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] integral(x^m/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(b*x+a)^(1/2), x, algorithm="giac")

[Out] integrate(x^m/sqrt(b*x + a), x)

maple [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(1/2)*x^m,x)`

[Out] `int(1/(b*x+a)^(1/2)*x^m,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m/(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] `integrate(x^m/sqrt(b*x+a),x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^m}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m/(a+b*x)^(1/2),x)`

[Out] `int(x^m/(a+b*x)^(1/2),x)`

sympy [C] time = 1.51, size = 36, normalized size = 0.78

$$\frac{xx^m \Gamma(m+1) {}_2F_1\left(\frac{1}{2}, m+1 \mid \frac{bx e^{i\pi}}{a}\right)}{\sqrt{a} \Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m/(b*x+a)**(1/2),x)`

[Out] `x*x**m*gamma(m+1)*hyper((1/2, m+1), (m+2,), b*x*exp_polar(I*pi)/a)/(sqrt(a)*gamma(m+2))`

$$3.716 \quad \int \frac{x^{-1+m}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=48

$$\frac{2x^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, 1-m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{a}$$

[Out] $-2*x^m*\text{hypergeom}([1/2, 1-m], [3/2], 1+b*x/a)*(b*x+a)^{(1/2)}/a/((-b*x/a)^m)$

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {67, 65}

$$\frac{2x^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, 1-m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{a}$$

Antiderivative was successfully verified.

[In] Int[x^(-1 + m)/Sqrt[a + b*x], x]

[Out] $(-2*x^m*\text{Sqrt}[a + b*x]*\text{Hypergeometric2F1}[1/2, 1 - m, 3/2, 1 + (b*x)/a])/(a*(-(b*x)/a))^m)$

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(-(b*c)/d)^m*IntPart[m]*(b*x)^{FracPart[m]}/(-(d*x)/c)^{FracPart[m]}, Int[(-(d*x)/c)^m*(c + d*x)ⁿ, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\int \frac{x^{-1+m}}{\sqrt{a+bx}} dx = -\frac{\left(bx^m \left(-\frac{bx}{a}\right)^{-m}\right) \int \frac{\left(-\frac{bx}{a}\right)^{-1+m}}{\sqrt{a+bx}} dx}{a}$$

$$= -\frac{2x^m \left(-\frac{bx}{a}\right)^{-m} \sqrt{a+bx} {}_2F_1\left(\frac{1}{2}, 1-m; \frac{3}{2}; 1+\frac{bx}{a}\right)}{a}$$

Mathematica [A] time = 0.03, size = 48, normalized size = 1.00

$$\frac{2x^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, 1-m; \frac{3}{2}; \frac{bx}{a}+1\right)}{a}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-1 + m)/Sqrt[a + b*x], x]

[Out] (-2*x^m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, 1 - m, 3/2, 1 + (b*x)/a])/(a*(-((b*x)/a))^m)

fricas [F] time = 0.51, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^{m-1}}{\sqrt{bx+a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-1+m)/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] integral(x^(m - 1)/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{m-1}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-1+m)/(b*x+a)^(1/2), x, algorithm="giac")

[Out] integrate(x^(m - 1)/sqrt(b*x + a), x)

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{x^{m-1}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(m-1)/(b*x+a)^(1/2),x)

[Out] int(x^(m-1)/(b*x+a)^(1/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{m-1}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-1+m)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] integrate(x^(m - 1)/sqrt(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^{m-1}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(m - 1)/(a + b*x)^(1/2),x)

[Out] int(x^(m - 1)/(a + b*x)^(1/2), x)

sympy [C] time = 3.75, size = 31, normalized size = 0.65

$$\frac{x^m \Gamma(m) {}_2F_1\left(\frac{1}{2}, m \left| \frac{bx e^{i\pi}}{a} \right.\right)}{\sqrt{a} \Gamma(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(-1+m)/(b*x+a)**(1/2),x)

[Out] x**m*gamma(m)*hyper((1/2, m), (m + 1,), b*x*exp_polar(I*pi)/a)/(sqrt(a)*gamma(m + 1))

$$3.717 \quad \int \frac{x^{-2+m}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=49

$$\frac{2bx^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, 2-m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{a^2}$$

[Out] 2*b*x^m*hypergeom([1/2, 2-m], [3/2], 1+b*x/a)*(b*x+a)^(1/2)/a^2/((-b*x/a)^m)

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {67, 65}

$$\frac{2bx^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, 2-m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{a^2}$$

Antiderivative was successfully verified.

[In] Int[x^(-2 + m)/Sqrt[a + b*x], x]

[Out] (2*b*x^m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, 2 - m, 3/2, 1 + (b*x)/a])/(a^2*(-((b*x)/a))^m)

Rule 65

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])
```

Rule 67

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(-(b*c)/d)^IntPart[m]*(b*x)^FracPart[m]/(-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)^m*(c + d*x)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]
```

Rubi steps

$$\int \frac{x^{-2+m}}{\sqrt{a+bx}} dx = \frac{\left(b^2 x^m \left(-\frac{bx}{a}\right)^{-m}\right) \int \frac{\left(-\frac{bx}{a}\right)^{-2+m}}{\sqrt{a+bx}} dx}{a^2}$$

$$= \frac{2bx^m \left(-\frac{bx}{a}\right)^{-m} \sqrt{a+bx} {}_2F_1\left(\frac{1}{2}, 2-m; \frac{3}{2}; 1 + \frac{bx}{a}\right)}{a^2}$$

Mathematica [A] time = 0.03, size = 49, normalized size = 1.00

$$\frac{2bx^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, 2-m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-2 + m)/Sqrt[a + b*x], x]

[Out] (2*b*x^m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, 2 - m, 3/2, 1 + (b*x)/a])/(a^2*(-((b*x)/a))^m)

fricas [F] time = 0.54, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^{m-2}}{\sqrt{bx+a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-2+m)/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] integral(x^(m - 2)/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{m-2}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-2+m)/(b*x+a)^(1/2), x, algorithm="giac")

[Out] integrate(x^(m - 2)/sqrt(b*x + a), x)

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{x^{m-2}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x[^](-2+m)/(b*x+a)^{^(1/2)}, x)

[Out] int(x[^](-2+m)/(b*x+a)^{^(1/2)}, x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{m-2}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x[^](-2+m)/(b*x+a)^{^(1/2)}, x, algorithm="maxima")

[Out] integrate(x[^](m - 2)/sqrt(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^{m-2}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x[^](m - 2)/(a + b*x)^{^(1/2)}, x)

[Out] int(x[^](m - 2)/(a + b*x)^{^(1/2)}, x)

sympy [C] time = 9.26, size = 32, normalized size = 0.65

$$\frac{x^m \Gamma(m-1) {}_2F_1\left(\frac{1}{2}, m-1 \mid \frac{bx e^{i\pi}}{a}\right)}{\sqrt{a} x \Gamma(m)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^{**}(-2+m)/(b*x+a)^{**}(1/2), x)

[Out] x^{**}m*gamma(m - 1)*hyper((1/2, m - 1), (m,), b*x*exp_polar(I*pi)/a)/(sqrt(a)*x*gamma(m))

$$3.718 \quad \int \frac{x^{-3+m}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=51

$$\frac{2b^2x^m\sqrt{a+bx}\left(-\frac{bx}{a}\right)^{-m}{}_2F_1\left(\frac{1}{2}, 3-m; \frac{3}{2}; \frac{bx}{a}+1\right)}{a^3}$$

[Out] $-2*b^2*x^m*hypergeom([1/2, 3-m], [3/2], 1+b*x/a)*(b*x+a)^{(1/2)}/a^3/((-b*x/a)^m)$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {67, 65}

$$\frac{2b^2x^m\sqrt{a+bx}\left(-\frac{bx}{a}\right)^{-m}{}_2F_1\left(\frac{1}{2}, 3-m; \frac{3}{2}; \frac{bx}{a}+1\right)}{a^3}$$

Antiderivative was successfully verified.

[In] Int[x^(-3 + m)/Sqrt[a + b*x], x]

[Out] $(-2*b^2*x^m*\text{Sqrt}[a + b*x]*\text{Hypergeometric2F1}[1/2, 3 - m, 3/2, 1 + (b*x)/a])/ (a^3*(-((b*x)/a))^m)$

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(-(b*c)/d)^IntPart[m]*(b*x)^FracPart[m])/(-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)]^m*(c + d*x)^n, x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\int \frac{x^{-3+m}}{\sqrt{a+bx}} dx = -\frac{\left(b^3 x^m \left(-\frac{bx}{a}\right)^{-m}\right) \int \frac{\left(-\frac{bx}{a}\right)^{-3+m}}{\sqrt{a+bx}} dx}{a^3}$$

$$= -\frac{2b^2 x^m \left(-\frac{bx}{a}\right)^{-m} \sqrt{a+bx} {}_2F_1\left(\frac{1}{2}, 3-m; \frac{3}{2}; 1 + \frac{bx}{a}\right)}{a^3}$$

Mathematica [A] time = 0.03, size = 51, normalized size = 1.00

$$\frac{2b^2 x^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, 3-m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x[^](-3 + m)/Sqrt[a + b*x], x]

[Out] (-2*b[^]2*x[^]m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, 3 - m, 3/2, 1 + (b*x)/a])/ (a[^]3*(-((b*x)/a))[^]m)

fricas [F] time = 0.58, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^{m-3}}{\sqrt{bx+a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x[^](-3+m)/(b*x+a)^{^(1/2)}, x, algorithm="fricas")

[Out] integral(x[^](m - 3)/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{m-3}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x[^](-3+m)/(b*x+a)^{^(1/2)}, x, algorithm="giac")

[Out] integrate(x[^](m - 3)/sqrt(b*x + a), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^{m-3}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(-3+m)/(b*x+a)^(1/2), x)

[Out] int(x^(-3+m)/(b*x+a)^(1/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{m-3}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-3+m)/(b*x+a)^(1/2), x, algorithm="maxima")

[Out] integrate(x^(m - 3)/sqrt(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^{m-3}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(m - 3)/(a + b*x)^(1/2), x)

[Out] int(x^(m - 3)/(a + b*x)^(1/2), x)

sympy [C] time = 24.01, size = 37, normalized size = 0.73

$$\frac{x^m \Gamma(m-2) {}_2F_1\left(\frac{1}{2}, m-2 \left| \frac{bx e^{i\pi}}{a} \right. \right)}{\sqrt{a} x^2 \Gamma(m-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^{**(-3+m)}/(b*x+a)^{**1/2}, x)

[Out] x**m*gamma(m - 2)*hyper((1/2, m - 2), (m - 1,), b*x*exp_polar(I*pi)/a)/(sqrt(a)*x**2*gamma(m - 1))

$$3.719 \quad \int \frac{x^m}{\sqrt{2+3x}} dx$$

Optimal. Leaf size=31

$$\frac{x^{m+1} {}_2F_1\left(\frac{1}{2}, m+1; m+2; -\frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

[Out] 1/2*x^(1+m)*hypergeom([1/2, 1+m], [2+m], -3/2*x)/(1+m)*2^(1/2)

Rubi [A] time = 0.01, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {64}

$$\frac{x^{m+1} {}_2F_1\left(\frac{1}{2}, m+1; m+2; -\frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

Antiderivative was successfully verified.

[In] Int[x^m/Sqrt[2 + 3*x], x]

[Out] (x^(1 + m)*Hypergeometric2F1[1/2, 1 + m, 2 + m, (-3*x)/2])/(Sqrt[2]*(1 + m))

Rule 64

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*x)/c)])/(b*(m + 1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rubi steps

$$\int \frac{x^m}{\sqrt{2+3x}} dx = \frac{x^{1+m} {}_2F_1\left(\frac{1}{2}, 1+m; 2+m; -\frac{3x}{2}\right)}{\sqrt{2}(1+m)}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 1.00

$$\frac{x^{m+1} {}_2F_1\left(\frac{1}{2}, m+1; m+2; -\frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[x^m/Sqrt[2 + 3*x],x]

[Out] (x^(1 + m)*Hypergeometric2F1[1/2, 1 + m, 2 + m, (-3*x)/2])/(Sqrt[2]*(1 + m))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^m}{\sqrt{3x+2}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(2+3*x)^(1/2),x, algorithm="fricas")

[Out] integral(x^m/sqrt(3*x + 2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{3x+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(2+3*x)^(1/2),x, algorithm="giac")

[Out] integrate(x^m/sqrt(3*x + 2), x)

maple [A] time = 0.05, size = 29, normalized size = 0.94

$$\frac{\sqrt{2} x^{m+1} \text{hypergeom}\left(\left[\frac{1}{2}, m+1\right], [m+2], -\frac{3x}{2}\right)}{2m+2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(3*x+2)^(1/2),x)

[Out] 1/2*x^(m+1)*hypergeom([1/2,m+1],[m+2],-3/2*x)/(m+1)*2^(1/2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{3x+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(2+3*x)^(1/2),x, algorithm="maxima")

[Out] integrate(x^m/sqrt(3*x + 2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^m}{\sqrt{3x+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m/(3*x + 2)^(1/2), x)`

[Out] `int(x^m/(3*x + 2)^(1/2), x)`

sympy [C] time = 1.20, size = 37, normalized size = 1.19

$$\frac{\sqrt{2} x x^m \Gamma(m+1) {}_2F_1\left(\frac{1}{2}, m+1 \mid \frac{3xe^{i\pi}}{2}\right)}{2\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m/(2+3*x)**(1/2), x)`

[Out] `sqrt(2)*x*x**m*gamma(m + 1)*hyper((1/2, m + 1), (m + 2,), 3*x*exp_polar(I*pi)/2)/(2*gamma(m + 2))`

$$3.720 \quad \int \frac{x^m}{\sqrt{2-3x}} dx$$

Optimal. Leaf size=31

$$\frac{x^{m+1} {}_2F_1\left(\frac{1}{2}, m+1; m+2; \frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

[Out] $1/2*x^{(1+m)}*\text{hypergeom}([1/2, 1+m], [2+m], 3/2*x)/(1+m)*2^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {64}

$$\frac{x^{m+1} {}_2F_1\left(\frac{1}{2}, m+1; m+2; \frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

Antiderivative was successfully verified.

[In] Int[x^m/Sqrt[2 - 3*x], x]

[Out] $(x^{(1+m)}*\text{Hypergeometric2F1}[1/2, 1+m, 2+m, (3*x)/2])/(Sqrt[2]*(1+m))$

Rule 64

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -((d*x)/c)])/ (b*(m+1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)]) && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rubi steps

$$\int \frac{x^m}{\sqrt{2-3x}} dx = \frac{x^{1+m} {}_2F_1\left(\frac{1}{2}, 1+m; 2+m; \frac{3x}{2}\right)}{\sqrt{2}(1+m)}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 1.00

$$\frac{x^{m+1} {}_2F_1\left(\frac{1}{2}, m+1; m+2; \frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[x^m/Sqrt[2 - 3*x],x]

[Out] (x^(1 + m)*Hypergeometric2F1[1/2, 1 + m, 2 + m, (3*x)/2])/(Sqrt[2]*(1 + m))

fricas [F] time = 0.56, size = 0, normalized size = 0.00

$$\text{integral}\left(-\frac{x^m\sqrt{-3x+2}}{3x-2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(2-3*x)^(1/2),x, algorithm="fricas")

[Out] integral(-x^m*sqrt(-3*x + 2)/(3*x - 2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{-3x+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(2-3*x)^(1/2),x, algorithm="giac")

[Out] integrate(x^m/sqrt(-3*x + 2), x)

maple [A] time = 0.05, size = 29, normalized size = 0.94

$$\frac{\sqrt{2} x^{m+1} \text{hypergeom}\left(\left[\frac{1}{2}, m+1\right], [m+2], \frac{3x}{2}\right)}{2m+2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(2-3*x)^(1/2),x)

[Out] 1/2*x^(m+1)*hypergeom([1/2,m+1],[m+2],3/2*x)/(m+1)*2^(1/2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{-3x+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(2-3*x)^(1/2),x, algorithm="maxima")

[Out] integrate(x^m/sqrt(-3*x + 2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^m}{\sqrt{2-3x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(2 - 3*x)^(1/2), x)

[Out] int(x^m/(2 - 3*x)^(1/2), x)

sympy [C] time = 1.22, size = 46, normalized size = 1.48

$$\frac{2 \cdot 2^m \sqrt{3} \cdot 3^{-m} i \sqrt{x - \frac{2}{3}} {}_2F_1\left(\frac{1}{2}, -m \mid \frac{3\left(x - \frac{2}{3}\right) e^{i\pi}}{2}\right)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m/(2-3*x)**(1/2), x)

[Out] -2*2**m*sqrt(3)*3**(-m)*I*sqrt(x - 2/3)*hyper((1/2, -m), (3/2,), 3*(x - 2/3)*exp_polar(I*pi)/2)/3

$$3.721 \quad \int \frac{x^m}{\sqrt{-2+3x}} dx$$

Optimal. Leaf size=36

$$\left(\frac{3}{2}\right)^{-m-1} \sqrt{3x-2} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 1 - \frac{3x}{2}\right)$$

[Out] $(3/2)^{-1-m} \text{hypergeom}([1/2, -m], [3/2], 1-3/2*x) * (-2+3*x)^{1/2}$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {65}

$$\left(\frac{3}{2}\right)^{-m-1} \sqrt{3x-2} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 1 - \frac{3x}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[x^m/Sqrt[-2 + 3*x], x]

[Out] $(3/2)^{-1-m} \text{Sqrt}[-2 + 3*x] \text{Hypergeometric2F1}[1/2, -m, 3/2, 1 - (3*x)/2]$

Rule 65

Int[((b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{x^m}{\sqrt{-2+3x}} dx = \left(\frac{3}{2}\right)^{-1-m} \sqrt{-2+3x} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 1 - \frac{3x}{2}\right)$$

Mathematica [A] time = 0.01, size = 36, normalized size = 1.00

$$\left(\frac{3}{2}\right)^{-m-1} \sqrt{3x-2} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 1 - \frac{3x}{2}\right)$$

Antiderivative was successfully verified.

[In] Integrate[x^m/Sqrt[-2 + 3*x],x]

[Out] (3/2)^(-1 - m)*Sqrt[-2 + 3*x]*Hypergeometric2F1[1/2, -m, 3/2, 1 - (3*x)/2]

fricas [F] time = 0.54, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{x^m}{\sqrt{3x-2}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(-2+3*x)^(1/2),x, algorithm="fricas")

[Out] integral(x^m/sqrt(3*x - 2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{3x-2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(-2+3*x)^(1/2),x, algorithm="giac")

[Out] integrate(x^m/sqrt(3*x - 2), x)

maple [C] time = 0.06, size = 43, normalized size = 1.19

$$\frac{\sqrt{2} \sqrt{-\text{signum}\left(x - \frac{2}{3}\right)} x^{m+1} \text{hypergeom}\left(\left[\frac{1}{2}, m+1\right], [m+2], \frac{3x}{2}\right)}{2(m+1) \sqrt{\text{signum}\left(x - \frac{2}{3}\right)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(-2+3*x)^(1/2),x)

[Out] 1/2*2^(1/2)/signum(x-2/3)^(1/2)*(-signum(x-2/3))^(1/2)/(m+1)*x^(m+1)*hypergeom([1/2,m+1], [m+2], 3/2*x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{3x-2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(-2+3*x)^(1/2),x, algorithm="maxima")

[Out] integrate(x^m/sqrt(3*x - 2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^m}{\sqrt{3x-2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m/(3*x - 2)^(1/2), x)

[Out] int(x^m/(3*x - 2)^(1/2), x)

sympy [C] time = 1.22, size = 36, normalized size = 1.00

$$\frac{\sqrt{2} i x x^m \Gamma(m+1) {}_2F_1\left(\frac{1}{2}, m+1 \left| \frac{3x}{2} \right. \right)}{2\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m/(-2+3*x)**(1/2), x)

[Out] -sqrt(2)*I*x*x**m*gamma(m + 1)*hyper((1/2, m + 1), (m + 2,), 3*x/2)/(2*gamma(m + 2))

$$3.722 \quad \int \frac{x^m}{\sqrt{-2-3x}} dx$$

Optimal. Leaf size=50

$$-2^{m+1}3^{-m-1}\sqrt{-3x-2}(-x)^{-m}x^m {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{3x}{2} + 1\right)$$

[Out] $-2^{(1+m)}*3^{(-1-m)}*x^m*\text{hypergeom}([1/2, -m], [3/2], 1+3/2*x)*(-2-3*x)^{(1/2)}/((-x)^m)$

Rubi [A] time = 0.01, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {67, 12, 65}

$$-2^{m+1}3^{-m-1}\sqrt{-3x-2}(-x)^{-m}x^m {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{3x}{2} + 1\right)$$

Antiderivative was successfully verified.

[In] Int[x^m/Sqrt[-2 - 3*x], x]

[Out] $-((2^{(1+m)}*3^{(-1-m)}*\text{Sqrt}[-2-3*x]*x^m*\text{Hypergeometric2F1}[1/2, -m, 3/2, 1+(3*x)/2])/(-x)^m)$

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 65

Int[((b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Dist[(-((b*c)/d))^m*IntPart[m]*(b*x)^FracPart[m])/(-(d*x)/c)^FracPart[m], Int[(-((d*x)/c))^m*(c + d*x)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\begin{aligned}
\int \frac{x^m}{\sqrt{-2-3x}} dx &= \left(\left(\frac{2}{3} \right)^m (-x)^{-m} x^m \right) \int \frac{\left(\frac{3}{2} \right)^m (-x)^m}{\sqrt{-2-3x}} dx \\
&= ((-x)^{-m} x^m) \int \frac{(-x)^m}{\sqrt{-2-3x}} dx \\
&= -2^{1+m} 3^{-1-m} \sqrt{-2-3x} (-x)^{-m} x^m {}_2F_1 \left(\frac{1}{2}, -m; \frac{3}{2}; 1 + \frac{3x}{2} \right)
\end{aligned}$$

Mathematica [A] time = 0.03, size = 48, normalized size = 0.96

$$-\frac{2}{3} \sqrt{-3x-2} \left(\frac{1}{2}(-3x-2)+1 \right)^{-m} x^m {}_2F_1 \left(\frac{1}{2}, -m; \frac{3}{2}; \frac{3x}{2} + 1 \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^m/Sqrt[-2 - 3*x],x]

[Out] (-2*Sqrt[-2 - 3*x]*x^m*Hypergeometric2F1[1/2, -m, 3/2, 1 + (3*x)/2])/(3*(1 + (-2 - 3*x)/2)^m)

fricas [F] time = 0.59, size = 0, normalized size = 0.00

$$\text{integral} \left(-\frac{x^m \sqrt{-3x-2}}{3x+2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(-2-3*x)^(1/2),x, algorithm="fricas")

[Out] integral(-x^m*sqrt(-3*x - 2)/(3*x + 2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{-3x-2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m/(-2-3*x)^(1/2),x, algorithm="giac")

[Out] integrate(x^m/sqrt(-3*x - 2), x)

maple [C] time = 0.04, size = 30, normalized size = 0.60

$$\frac{i\sqrt{2} x^{m+1} \operatorname{hypergeom}\left(\left[\frac{1}{2}, m+1\right], [m+2], -\frac{3x}{2}\right)}{2(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m/(-2-3*x)^(1/2),x)`

[Out] `-1/2*I*x^(m+1)*hypergeom([1/2,m+1],[m+2],-3/2*x)/(m+1)*2^(1/2)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^m}{\sqrt{-3x-2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m/(-2-3*x)^(1/2),x, algorithm="maxima")`

[Out] `integrate(x^m/sqrt(-3*x - 2), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^m}{\sqrt{-3x-2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m/(-3*x-2)^(1/2),x)`

[Out] `int(x^m/(-3*x-2)^(1/2),x)`

sympy [C] time = 1.19, size = 41, normalized size = 0.82

$$\frac{\sqrt{2} i x x^m \Gamma(m+1) {}_2F_1\left(\frac{1}{2}, m+1 \mid \frac{3x e^{i\pi}}{2}\right)}{2\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m/(-2-3*x)**(1/2),x)`

[Out] `-sqrt(2)*I*x*x**m*gamma(m+1)*hyper((1/2, m+1), (m+2,), 3*x*exp_polar(I*pi)/2)/(2*gamma(m+2))`

$$3.723 \quad \int \frac{(-x)^m}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=48

$$\frac{2(-x)^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b}$$

[Out] 2*(-x)^m*hypergeom([1/2, -m], [3/2], 1+b*x/a)*(b*x+a)^(1/2)/b/((-b*x/a)^m)

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {67, 65}

$$\frac{2(-x)^m \sqrt{a+bx} \left(-\frac{bx}{a}\right)^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[(-x)^m/Sqrt[a + b*x], x]

[Out] (2*(-x)^m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, -m, 3/2, 1 + (b*x)/a])/(b*(-(b*x)/a))^m)

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(-(b*c)/d)^IntPart[m]*(b*x)^FracPart[m]/(-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)^m*(c + d*x)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\int \frac{(-x)^m}{\sqrt{a+bx}} dx = \left((-x)^m \left(-\frac{bx}{a} \right)^{-m} \right) \int \frac{\left(-\frac{bx}{a} \right)^m}{\sqrt{a+bx}} dx$$

$$= \frac{2(-x)^m \left(-\frac{bx}{a} \right)^{-m} \sqrt{a+bx} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 1 + \frac{bx}{a}\right)}{b}$$

Mathematica [A] time = 0.02, size = 48, normalized size = 1.00

$$\frac{2(-x)^m \sqrt{a+bx} \left(-\frac{bx}{a} \right)^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{bx}{a} + 1\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[(-x)^m/Sqrt[a + b*x], x]

[Out] (2*(-x)^m*Sqrt[a + b*x]*Hypergeometric2F1[1/2, -m, 3/2, 1 + (b*x)/a])/(b*(-((b*x)/a))^m)

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(-x)^m}{\sqrt{bx+a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] integral((-x)^m/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(b*x+a)^(1/2), x, algorithm="giac")

[Out] integrate((-x)^m/sqrt(b*x + a), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-x)^m/(b*x+a)^(1/2),x)`

[Out] `int((-x)^m/(b*x+a)^(1/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-x)^m/(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] `integrate((-x)^m/sqrt(b*x + a), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(-x)^m}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-x)^m/(a + b*x)^(1/2),x)`

[Out] `int((-x)^m/(a + b*x)^(1/2), x)`

sympy [C] time = 1.54, size = 42, normalized size = 0.88

$$\frac{xx^m e^{i\pi m} \Gamma(m+1) {}_2F_1\left(\frac{1}{2}, m+1 \left| \frac{bx e^{i\pi}}{a} \right.\right)}{\sqrt{a} \Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-x)**m/(b*x+a)**(1/2),x)`

[Out] `x*x**m*exp(I*pi*m)*gamma(m + 1)*hyper((1/2, m + 1), (m + 2,), b*x*exp_polar(I*pi)/a)/(sqrt(a)*gamma(m + 2))`

$$3.724 \quad \int \frac{(-x)^m}{\sqrt{2+3x}} dx$$

Optimal. Leaf size=34

$$-\frac{(-x)^{m+1} {}_2F_1\left(\frac{1}{2}, m+1; m+2; -\frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

[Out] $-1/2*(-x)^{(1+m)}*\text{hypergeom}([1/2, 1+m], [2+m], -3/2*x)/(1+m)*2^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {64}

$$-\frac{(-x)^{m+1} {}_2F_1\left(\frac{1}{2}, m+1; m+2; -\frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(-x)^m/\text{Sqrt}[2 + 3*x], x]$

[Out] $-(((x)^{(1+m)}*\text{Hypergeometric2F1}[1/2, 1+m, 2+m, (-3*x)/2])/(Sqrt[2]*(1+m)))$

Rule 64

$\text{Int}[(b_*)*(x_*)^{(m_*)}*((c_*) + (d_*)*(x_*)^{(n_*)}), x_Symbol] \rightarrow \text{Simp}[(c^{n+1}*(b*x)^{(m+1)}*\text{Hypergeometric2F1}[-n, m+1, m+2, -(d*x)/c])/(b*(m+1)), x]$
 /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0])))

Rubi steps

$$\int \frac{(-x)^m}{\sqrt{2+3x}} dx = -\frac{(-x)^{1+m} {}_2F_1\left(\frac{1}{2}, 1+m; 2+m; -\frac{3x}{2}\right)}{\sqrt{2}(1+m)}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 0.94

$$\frac{x(-x)^m {}_2F_1\left(\frac{1}{2}, m+1; m+2; -\frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[(-x)^m/Sqrt[2 + 3*x], x]

[Out] ((-x)^m*x*Hypergeometric2F1[1/2, 1 + m, 2 + m, (-3*x)/2])/(Sqrt[2]*(1 + m))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(-x)^m}{\sqrt{3x+2}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(2+3*x)^(1/2), x, algorithm="fricas")

[Out] integral((-x)^m/sqrt(3*x + 2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{3x+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(2+3*x)^(1/2), x, algorithm="giac")

[Out] integrate((-x)^m/sqrt(3*x + 2), x)

maple [A] time = 0.06, size = 30, normalized size = 0.88

$$\frac{\sqrt{2} x (-x)^m \text{hypergeom}\left(\left[\frac{1}{2}, m+1\right], [m+2], -\frac{3x}{2}\right)}{2m+2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x)^m/(3*x+2)^(1/2), x)

[Out] 1/2*2^(1/2)*(-x)^m/(m+1)*x*hypergeom([1/2, m+1], [m+2], -3/2*x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{3x+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(2+3*x)^(1/2), x, algorithm="maxima")

[Out] integrate((-x)^m/sqrt(3*x + 2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(-x)^m}{\sqrt{3x+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x)^m/(3*x + 2)^(1/2), x)

[Out] int((-x)^m/(3*x + 2)^(1/2), x)

sympy [C] time = 1.20, size = 44, normalized size = 1.29

$$\frac{2 \cdot 2^m \sqrt{3} \cdot 3^{-m} \sqrt{x + \frac{2}{3}} {}_2F_1\left(\frac{1}{2}, -m \middle| \frac{3\left(x + \frac{2}{3}\right) e^{2i\pi}}{2}\right)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)**m/(2+3*x)**(1/2), x)

[Out] 2*2**m*sqrt(3)*3**(-m)*sqrt(x + 2/3)*hyper((1/2, -m), (3/2,), 3*(x + 2/3)*exp_polar(2*I*pi)/2)/3

$$3.725 \quad \int \frac{(-x)^m}{\sqrt{2-3x}} dx$$

Optimal. Leaf size=34

$$-\frac{(-x)^{m+1} {}_2F_1\left(\frac{1}{2}, m+1; m+2; \frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

[Out] $-1/2*(-x)^{(1+m)}*\text{hypergeom}([1/2, 1+m], [2+m], 3/2*x)/(1+m)*2^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 34, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {64}

$$-\frac{(-x)^{m+1} {}_2F_1\left(\frac{1}{2}, m+1; m+2; \frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

Antiderivative was successfully verified.

[In] Int[(-x)^m/Sqrt[2 - 3*x], x]

[Out] $-(((x)^{(1+m)}*\text{Hypergeometric2F1}[1/2, 1+m, 2+m, (3*x)/2])/(Sqrt[2]*(1+m)))$

Rule 64

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -(d*x)/c])/(b*(m+1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rubi steps

$$\int \frac{(-x)^m}{\sqrt{2-3x}} dx = -\frac{(-x)^{1+m} {}_2F_1\left(\frac{1}{2}, 1+m; 2+m; \frac{3x}{2}\right)}{\sqrt{2}(1+m)}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 0.94

$$\frac{x(-x)^m {}_2F_1\left(\frac{1}{2}, m+1; m+2; \frac{3x}{2}\right)}{\sqrt{2}(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[(-x)^m/Sqrt[2 - 3*x],x]

[Out] ((-x)^m*x*Hypergeometric2F1[1/2, 1 + m, 2 + m, (3*x)/2])/(Sqrt[2]*(1 + m))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(-\frac{(-x)^m \sqrt{-3x+2}}{3x-2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(2-3*x)^(1/2),x, algorithm="fricas")

[Out] integral(-(-x)^m*sqrt(-3*x + 2)/(3*x - 2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{-3x+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(2-3*x)^(1/2),x, algorithm="giac")

[Out] integrate((-x)^m/sqrt(-3*x + 2), x)

maple [A] time = 0.05, size = 30, normalized size = 0.88

$$\frac{\sqrt{2} x (-x)^m \text{hypergeom}\left(\left[\frac{1}{2}, m+1\right], [m+2], \frac{3x}{2}\right)}{2m+2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x)^m/(2-3*x)^(1/2),x)

[Out] 1/2*2^(1/2)*(-x)^m/(m+1)*x*hypergeom([1/2,m+1], [m+2], 3/2*x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{-3x+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(2-3*x)^(1/2),x, algorithm="maxima")

[Out] integrate((-x)^m/sqrt(-3*x + 2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(-x)^m}{\sqrt{2-3x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x)^m/(2 - 3*x)^(1/2), x)

[Out] int((-x)^m/(2 - 3*x)^(1/2), x)

sympy [C] time = 1.26, size = 53, normalized size = 1.56

$$\frac{2 \cdot 2^m \sqrt{3} \cdot 3^{-m} i \sqrt{x - \frac{2}{3}} e^{i\pi m} {}_2F_1\left(\frac{1}{2}, -m \middle| \frac{3\left(x - \frac{2}{3}\right) e^{i\pi}}{2}\right)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)**m/(2-3*x)**(1/2), x)

[Out] -2*2**m*sqrt(3)*3**(-m)*I*sqrt(x - 2/3)*exp(I*pi*m)*hyper((1/2, -m), (3/2,)
, 3*(x - 2/3)*exp_polar(I*pi)/2)/3

$$3.726 \quad \int \frac{(-x)^m}{\sqrt{-2+3x}} dx$$

Optimal. Leaf size=49

$$2^{m+1}3^{-m-1}\sqrt{3x-2}(-x)^m x^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 1 - \frac{3x}{2}\right)$$

[Out] $2^{(1+m)}*3^{(-1-m)}*(-x)^m*\text{hypergeom}([1/2, -m], [3/2], 1-3/2*x)*(-2+3*x)^{(1/2)}/(x^m)$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {67, 12, 65}

$$2^{m+1}3^{-m-1}\sqrt{3x-2}(-x)^m x^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 1 - \frac{3x}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[(-x)^m/Sqrt[-2 + 3*x], x]

[Out] $(2^{(1+m)}*3^{(-1-m)}*(-x)^m*\text{Sqrt}[-2+3*x]*\text{Hypergeometric2F1}[1/2, -m, 3/2, 1-(3*x)/2])/x^m$

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rule 67

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(-(b*c)/d)^m*IntPart[m]*(b*x)^FracPart[m]/(-(d*x)/c)^FracPart[m], Int[(-(d*x)/c)^m*(c + d*x)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0]

Rubi steps

$$\begin{aligned}
\int \frac{(-x)^m}{\sqrt{-2+3x}} dx &= \left(\left(\frac{2}{3} \right)^m (-x)^m x^{-m} \right) \int \frac{\left(\frac{3}{2} \right)^m x^m}{\sqrt{-2+3x}} dx \\
&= ((-x)^m x^{-m}) \int \frac{x^m}{\sqrt{-2+3x}} dx \\
&= 2^{1+m} 3^{-1-m} (-x)^m x^{-m} \sqrt{-2+3x} {}_2F_1 \left(\frac{1}{2}, -m; \frac{3}{2}; 1 - \frac{3x}{2} \right)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 49, normalized size = 1.00

$$2^{m+1} 3^{-m-1} \sqrt{3x-2} (-x)^m x^{-m} {}_2F_1 \left(\frac{1}{2}, -m; \frac{3}{2}; 1 - \frac{3x}{2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(-x)^m/Sqrt[-2 + 3*x], x]

[Out] (2^(1 + m)*3^(-1 - m)*(-x)^m*Sqrt[-2 + 3*x]*Hypergeometric2F1[1/2, -m, 3/2, 1 - (3*x)/2])/x^m

fricas [F] time = 0.56, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(-x)^m}{\sqrt{3x-2}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(-2+3*x)^(1/2), x, algorithm="fricas")

[Out] integral((-x)^m/sqrt(3*x - 2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{3x-2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(-2+3*x)^(1/2), x, algorithm="giac")

[Out] integrate((-x)^m/sqrt(3*x - 2), x)

maple [C] time = 0.06, size = 44, normalized size = 0.90

$$\frac{\sqrt{2} \sqrt{-\operatorname{signum}\left(x - \frac{2}{3}\right)} x (-x)^m \operatorname{hypergeom}\left(\left[\frac{1}{2}, m + 1\right], [m + 2], \frac{3x}{2}\right)}{2(m + 1) \sqrt{\operatorname{signum}\left(x - \frac{2}{3}\right)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x)^m/(-2+3*x)^(1/2), x)

[Out] 1/2*2^(1/2)*(-x)^m/signum(x-2/3)^(1/2)*(-signum(x-2/3))^(1/2)/(m+1)*x*hypergeom([1/2,m+1],[m+2],3/2*x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{3x - 2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(-2+3*x)^(1/2), x, algorithm="maxima")

[Out] integrate((-x)^m/sqrt(3*x - 2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(-x)^m}{\sqrt{3x - 2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x)^m/(3*x - 2)^(1/2), x)

[Out] int((-x)^m/(3*x - 2)^(1/2), x)

sympy [C] time = 1.28, size = 42, normalized size = 0.86

$$\frac{\sqrt{2} i x^m e^{i\pi m} \Gamma(m + 1) {}_2F_1\left(\frac{1}{2}, m + 1 \middle| \frac{3x}{2}\right)}{2\Gamma(m + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)**m/(-2+3*x)**(1/2), x)

[Out] -sqrt(2)*I*x*x**m*exp(I*pi*m)*gamma(m + 1)*hyper((1/2, m + 1), (m + 2,), 3*x/2)/(2*gamma(m + 2))

$$3.727 \quad \int \frac{(-x)^m}{\sqrt{-2-3x}} dx$$

Optimal. Leaf size=37

$$-\left(\frac{3}{2}\right)^{-m-1} \sqrt{-3x-2} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{3x}{2} + 1\right)$$

[Out] $-(3/2)^{-(-1-m)} * \text{hypergeom}([1/2, -m], [3/2], 1+3/2*x) * (-2-3*x)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {65}

$$-\left(\frac{3}{2}\right)^{-m-1} \sqrt{-3x-2} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{3x}{2} + 1\right)$$

Antiderivative was successfully verified.

[In] Int[(-x)^m/Sqrt[-2 - 3*x], x]

[Out] $-\left(\frac{3}{2}\right)^{-(-1-m)} * \text{Sqrt}[-2 - 3*x] * \text{Hypergeometric2F1}[1/2, -m, 3/2, 1 + (3*x)/2]$

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(-x)^m}{\sqrt{-2-3x}} dx = -\left(\frac{3}{2}\right)^{-1-m} \sqrt{-2-3x} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 1 + \frac{3x}{2}\right)$$

Mathematica [A] time = 0.02, size = 57, normalized size = 1.54

$$-\frac{2}{3} \sqrt{-3x-2} \left(\frac{1}{2}(-3x-2) + 1\right)^{-m} x^{-m} (-x^2)^m {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{3x}{2} + 1\right)$$

Antiderivative was successfully verified.

[In] Integrate[(-x)^m/Sqrt[-2 - 3*x],x]

[Out] $(-2\sqrt{-2 - 3x}*(-x^2)^m\text{Hypergeometric2F1}[1/2, -m, 3/2, 1 + (3x)/2])/ (3*(1 + (-2 - 3x)/2)^m*x^m)$

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(-\frac{(-x)^m\sqrt{-3x-2}}{3x+2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(-2-3*x)^(1/2),x, algorithm="fricas")

[Out] integral(-(-x)^m*sqrt(-3*x - 2)/(3*x + 2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{-3x-2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(-2-3*x)^(1/2),x, algorithm="giac")

[Out] integrate((-x)^m/sqrt(-3*x - 2), x)

maple [C] time = 0.04, size = 31, normalized size = 0.84

$$\frac{i\sqrt{2}x(-x)^m\text{hypergeom}\left(\left[\frac{1}{2}, m+1\right], [m+2], -\frac{3x}{2}\right)}{2(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x)^m/(-2-3*x)^(1/2),x)

[Out] $-1/2*I*2^{(1/2)}*(-x)^m/(m+1)*x*\text{hypergeom}([1/2, m+1], [m+2], -3/2*x)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x)^m}{\sqrt{-3x-2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)^m/(-2-3*x)^(1/2),x, algorithm="maxima")

[Out] integrate((-x)^m/sqrt(-3*x - 2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(-x)^m}{\sqrt{-3x-2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x)^m/(-3*x - 2)^(1/2), x)

[Out] int((-x)^m/(-3*x - 2)^(1/2), x)

sympy [C] time = 1.19, size = 48, normalized size = 1.30

$$\frac{2 \cdot 2^m \sqrt{3} \cdot 3^{-m} i \sqrt{x + \frac{2}{3}} {}_2F_1\left(\frac{1}{2}, -m \middle| \frac{3\left(x + \frac{2}{3}\right) e^{2i\pi}}{2}\right)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-x)**m/(-2-3*x)**(1/2), x)

[Out] -2*2**m*sqrt(3)*3**(-m)*I*sqrt(x + 2/3)*hyper((1/2, -m), (3/2,), 3*(x + 2/3)*exp_polar(2*I*pi)/2)/3

$$3.728 \quad \int \frac{x^n}{\sqrt{1-x}} dx$$

Optimal. Leaf size=26

$$-2\sqrt{1-x} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; 1-x\right)$$

[Out] -2*hypergeom([1/2, -n], [3/2], 1-x)*(1-x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {65}

$$-2\sqrt{1-x} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; 1-x\right)$$

Antiderivative was successfully verified.

[In] Int[x^n/Sqrt[1 - x], x]

[Out] -2*Sqrt[1 - x]*Hypergeometric2F1[1/2, -n, 3/2, 1 - x]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{x^n}{\sqrt{1-x}} dx = -2\sqrt{1-x} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; 1-x\right)$$

Mathematica [A] time = 0.00, size = 26, normalized size = 1.00

$$-2\sqrt{1-x} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; 1-x\right)$$

Antiderivative was successfully verified.

[In] Integrate[x^n/Sqrt[1 - x], x]

[Out] -2*Sqrt[1 - x]*Hypergeometric2F1[1/2, -n, 3/2, 1 - x]

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral}\left(-\frac{x^n\sqrt{-x+1}}{x-1}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^n/(1-x)^(1/2), x, algorithm="fricas")

[Out] integral(-x^n*sqrt(-x + 1)/(x - 1), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^n}{\sqrt{-x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^n/(1-x)^(1/2), x, algorithm="giac")

[Out] integrate(x^n/sqrt(-x + 1), x)

maple [A] time = 0.05, size = 23, normalized size = 0.88

$$\frac{x^{n+1} \text{hypergeom}\left(\left[\frac{1}{2}, n+1\right], [n+2], x\right)}{n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^n/(-x+1)^(1/2), x)

[Out] 1/(n+1)*x^(n+1)*hypergeom([1/2, n+1], [2+n], x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^n}{\sqrt{-x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^n/(1-x)^(1/2), x, algorithm="maxima")

[Out] integrate(x^n/sqrt(-x + 1), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{x^n}{\sqrt{1-x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^n/(1 - x)^(1/2), x)`

[Out] `int(x^n/(1 - x)^(1/2), x)`

sympy [C] time = 1.11, size = 26, normalized size = 1.00

$$-2i\sqrt{x-1} {}_2F_1\left(\frac{1}{2}, -n \middle| \frac{3}{2}, (x-1)e^{i\pi}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**n/(1-x)**(1/2), x)`

[Out] `-2*I*sqrt(x - 1)*hyper((1/2, -n), (3/2,), (x - 1)*exp_polar(I*pi))`

$$3.729 \quad \int \frac{x^n}{\sqrt{a-ax}} dx$$

Optimal. Leaf size=30

$$-\frac{2\sqrt{a-ax} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; 1-x\right)}{a}$$

[Out] -2*hypergeom([1/2, -n], [3/2], 1-x)*(-a*x+a)^(1/2)/a

Rubi [A] time = 0.00, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.071$, Rules used = {65}

$$-\frac{2\sqrt{a-ax} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; 1-x\right)}{a}$$

Antiderivative was successfully verified.

[In] Int[x^n/Sqrt[a - a*x], x]

[Out] (-2*Sqrt[a - a*x]*Hypergeometric2F1[1/2, -n, 3/2, 1 - x])/a

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{x^n}{\sqrt{a-ax}} dx = -\frac{2\sqrt{a-ax} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; 1-x\right)}{a}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$-\frac{2\sqrt{a-ax} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; 1-x\right)}{a}$$

Antiderivative was successfully verified.

[In] Integrate[x^n/Sqrt[a - a*x], x]

[Out] $(-2\sqrt{a - ax} \text{Hypergeometric2F1}[1/2, -n, 3/2, 1 - x])/a$

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left(-\frac{\sqrt{-ax + a}x^n}{ax - a}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^n/(-a*x+a)^(1/2),x, algorithm="fricas")`

[Out] `integral(-sqrt(-a*x + a)*x^n/(a*x - a), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^n}{\sqrt{-ax + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^n/(-a*x+a)^(1/2),x, algorithm="giac")`

[Out] `integrate(x^n/sqrt(-a*x + a), x)`

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^n}{\sqrt{-ax + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^n/(-a*x+a)^(1/2),x)`

[Out] `int(x^n/(-a*x+a)^(1/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^n}{\sqrt{-ax + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^n/(-a*x+a)^(1/2),x, algorithm="maxima")`

[Out] `integrate(x^n/sqrt(-a*x + a), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^n}{\sqrt{a - ax}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^n/(a - a*x)^(1/2), x)`

[Out] `int(x^n/(a - a*x)^(1/2), x)`

sympy [C] time = 1.16, size = 31, normalized size = 1.03

$$\frac{2i\sqrt{x-1} {}_2F_1\left(\frac{1}{2}, -n \mid \frac{3}{2}\right) (x-1) e^{i\pi}}{\sqrt{a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**n/(-a*x+a)**(1/2), x)`

[Out] `-2*I*sqrt(x - 1)*hyper((1/2, -n), (3/2,), (x - 1)*exp_polar(I*pi))/sqrt(a)`

3.730 $\int x^m (a + bx)^n dx$

Optimal. Leaf size=47

$$\frac{x^{m+1} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 1, -n; m + 2; -\frac{bx}{a}\right)}{m + 1}$$

[Out] $x^{(1+m)}*(b*x+a)^n*\text{hypergeom}([-n, 1+m], [2+m], -b*x/a)/(1+m)/((1+b*x/a)^n)$

Rubi [A] time = 0.01, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {66, 64}

$$\frac{x^{m+1} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 1, -n; m + 2; -\frac{bx}{a}\right)}{m + 1}$$

Antiderivative was successfully verified.

[In] Int[x^m*(a + b*x)^n, x]

[Out] $(x^{(1 + m)}*(a + b*x)^n*\text{Hypergeometric2F1}[1 + m, -n, 2 + m, -((b*x)/a)])/((1 + m)*(1 + (b*x)/a)^n)$

Rule 64

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*x)/c)]/(b*(m + 1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0])))

Rule 66

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c^IntPart[n]*(c + d*x)^FracPart[n]/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0])) || !RationalQ[n])

Rubi steps

$$\int x^m (a + bx)^n dx = \left((a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} \right) \int x^m \left(1 + \frac{bx}{a} \right)^n dx$$

$$= \frac{x^{1+m} (a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} {}_2F_1 \left(1 + m, -n; 2 + m; -\frac{bx}{a} \right)}{1 + m}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 1.00

$$\frac{x^{m+1} (a + bx)^n \left(\frac{bx}{a} + 1 \right)^{-n} {}_2F_1 \left(m + 1, -n; m + 2; -\frac{bx}{a} \right)}{m + 1}$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(a + b*x)^n,x]

[Out] (x^(1 + m)*(a + b*x)^n*Hypergeometric2F1[1 + m, -n, 2 + m, -(b*x)/a])/((1 + m)*(1 + (b*x)/a)^n)

fricas [F] time = 0.52, size = 0, normalized size = 0.00

$$\text{integral}((bx + a)^n x^m, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^n,x, algorithm="fricas")

[Out] integral((b*x + a)^n*x^m, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(b*x+a)^n,x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^m, x)

maple [F] time = 0.07, size = 0, normalized size = 0.00

$$\int x^m (bx + a)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(b*x+a)^n,x)`

[Out] `int(x^m*(b*x+a)^n,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^m*(b*x+a)^n,x, algorithm="maxima")`

[Out] `integrate((b*x + a)^n*x^m, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^m (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^m*(a + b*x)^n,x)`

[Out] `int(x^m*(a + b*x)^n, x)`

sympy [C] time = 3.57, size = 34, normalized size = 0.72

$$\frac{a^n x x^m \Gamma(m+1) {}_2F_1\left(-n, m+1 \left| \frac{bx e^{i\pi}}{a} \right. \right)}{\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**m*(b*x+a)**n,x)`

[Out] `a**n*x*x**m*gamma(m + 1)*hyper((-n, m + 1), (m + 2,), b*x*exp_polar(I*pi)/a)/gamma(m + 2)`

3.731 $\int (cx)^m (a + bx)^n dx$

Optimal. Leaf size=52

$$\frac{(cx)^{m+1} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 1, -n; m + 2; -\frac{bx}{a}\right)}{c(m + 1)}$$

[Out] $(c*x)^{(1+m)}*(b*x+a)^n*\text{hypergeom}([-n, 1+m], [2+m], -b*x/a)/c/(1+m)/((1+b*x/a)^n)$

Rubi [A] time = 0.01, antiderivative size = 52, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {66, 64}

$$\frac{(cx)^{m+1} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 1, -n; m + 2; -\frac{bx}{a}\right)}{c(m + 1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x)^m*(a + b*x)^n, x]$

[Out] $((c*x)^{(1 + m)}*(a + b*x)^n*\text{Hypergeometric2F1}[1 + m, -n, 2 + m, -((b*x)/a)])/(c*(1 + m)*(1 + (b*x)/a)^n)$

Rule 64

$\text{Int}[(b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}, x_Symbol] :> \text{Simp}[(c^{n+1}*(b*x)^{(m+1)}*\text{Hypergeometric2F1}[-n, m+1, m+2, -((d*x)/c)]/(b*(m+1)), x] /; \text{FreeQ}[\{b, c, d, m, n\}, x] \&\& \text{!IntegerQ}[m] \&\& (\text{IntegerQ}[n] \mid\mid (\text{GtQ}[c, 0] \&\& \text{!(EqQ}[n, -2^{(-1)}]) \&\& \text{EqQ}[c^2 - d^2, 0] \&\& \text{GtQ}[-(d/(b*c)), 0]))]$

Rule 66

$\text{Int}[(b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}, x_Symbol] :> \text{Dist}[(c^{\text{IntPart}[n]}*(c + d*x)^{\text{FracPart}[n]})/(1 + (d*x)/c)^{\text{FracPart}[n]}, \text{Int}[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; \text{FreeQ}[\{b, c, d, m, n\}, x] \&\& \text{!IntegerQ}[m] \&\& \text{!IntegerQ}[n] \&\& \text{!GtQ}[c, 0] \&\& \text{!GtQ}[-(d/(b*c)), 0] \&\& ((\text{RationalQ}[m] \&\& \text{!(EqQ}[n, -2^{(-1)}]) \&\& \text{EqQ}[c^2 - d^2, 0])) \mid\mid \text{!RationalQ}[n])]$

Rubi steps

$$\int (cx)^m (a + bx)^n dx = \left((a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} \right) \int (cx)^m \left(1 + \frac{bx}{a} \right)^n dx$$

$$= \frac{(cx)^{1+m} (a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} {}_2F_1 \left(1 + m, -n; 2 + m; -\frac{bx}{a} \right)}{c(1 + m)}$$

Mathematica [A] time = 0.01, size = 48, normalized size = 0.92

$$\frac{x(cx)^m (a + bx)^n \left(\frac{bx}{a} + 1 \right)^{-n} {}_2F_1 \left(m + 1, -n; m + 2; -\frac{bx}{a} \right)}{m + 1}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x)^m*(a + b*x)^n,x]

[Out] (x*(c*x)^m*(a + b*x)^n*Hypergeometric2F1[1 + m, -n, 2 + m, -((b*x)/a)])/((1 + m)*(1 + (b*x)/a)^n)

fricas [F] time = 0.51, size = 0, normalized size = 0.00

$$\text{integral}((bx + a)^n (cx)^m, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x)^m*(b*x+a)^n,x, algorithm="fricas")

[Out] integral((b*x + a)^n*(c*x)^m, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n (cx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x)^m*(b*x+a)^n,x, algorithm="giac")

[Out] integrate((b*x + a)^n*(c*x)^m, x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int (cx)^m (bx + a)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x)^m*(b*x+a)^n,x)`

[Out] `int((c*x)^m*(b*x+a)^n,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n (cx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x)^m*(b*x+a)^n,x, algorithm="maxima")`

[Out] `integrate((b*x + a)^n*(c*x)^m, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (cx)^m (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x)^m*(a + b*x)^n,x)`

[Out] `int((c*x)^m*(a + b*x)^n, x)`

sympy [C] time = 3.14, size = 37, normalized size = 0.71

$$\frac{a^n c^m x x^m \Gamma(m+1) {}_2F_1\left(-n, m+1 \left| \frac{bx e^{i\pi}}{a} \right. \right)}{\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x)**m*(b*x+a)**n,x)`

[Out] `a**n*c**m*x*x**m*gamma(m + 1)*hyper((-n, m + 1), (m + 2,), b*x*exp_polar(I*pi)/a)/gamma(m + 2)`

3.732 $\int x^3(a + bx)^n dx$

Optimal. Leaf size=83

$$-\frac{a^3(a+bx)^{n+1}}{b^4(n+1)} + \frac{3a^2(a+bx)^{n+2}}{b^4(n+2)} - \frac{3a(a+bx)^{n+3}}{b^4(n+3)} + \frac{(a+bx)^{n+4}}{b^4(n+4)}$$

[Out] $-a^3*(b*x+a)^{(1+n)}/b^4/(1+n)+3*a^2*(b*x+a)^{(2+n)}/b^4/(2+n)-3*a*(b*x+a)^{(3+n)}/b^4/(3+n)+(b*x+a)^{(4+n)}/b^4/(4+n)$

Rubi [A] time = 0.03, antiderivative size = 83, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$-\frac{a^3(a+bx)^{n+1}}{b^4(n+1)} + \frac{3a^2(a+bx)^{n+2}}{b^4(n+2)} - \frac{3a(a+bx)^{n+3}}{b^4(n+3)} + \frac{(a+bx)^{n+4}}{b^4(n+4)}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*x)^n, x]

[Out] $-((a^3*(a + b*x)^{(1 + n)})/(b^4*(1 + n))) + (3*a^2*(a + b*x)^{(2 + n)})/(b^4*(2 + n)) - (3*a*(a + b*x)^{(3 + n)})/(b^4*(3 + n)) + (a + b*x)^{(4 + n)}/(b^4*(4 + n))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3(a + bx)^n dx &= \int \left(-\frac{a^3(a+bx)^n}{b^3} + \frac{3a^2(a+bx)^{1+n}}{b^3} - \frac{3a(a+bx)^{2+n}}{b^3} + \frac{(a+bx)^{3+n}}{b^3} \right) dx \\ &= -\frac{a^3(a+bx)^{1+n}}{b^4(1+n)} + \frac{3a^2(a+bx)^{2+n}}{b^4(2+n)} - \frac{3a(a+bx)^{3+n}}{b^4(3+n)} + \frac{(a+bx)^{4+n}}{b^4(4+n)} \end{aligned}$$

Mathematica [A] time = 0.05, size = 67, normalized size = 0.81

$$\frac{(a+bx)^{n+1} \left(-\frac{a^3}{n+1} + \frac{3a^2(a+bx)}{n+2} - \frac{3a(a+bx)^2}{n+3} + \frac{(a+bx)^3}{n+4} \right)}{b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*x)^n,x]

[Out] ((a + b*x)^(1 + n)*(-(a^3/(1 + n)) + (3*a^2*(a + b*x))/(2 + n) - (3*a*(a + b*x)^2)/(3 + n) + (a + b*x)^3/(4 + n)))/b^4

fricas [A] time = 0.48, size = 143, normalized size = 1.72

$$\frac{(6a^3bnx + (b^4n^3 + 6b^4n^2 + 11b^4n + 6b^4)x^4 - 6a^4 + (ab^3n^3 + 3ab^3n^2 + 2ab^3n)x^3 - 3(a^2b^2n^2 + a^2b^2n)x^2)(bx + a)^n}{b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n,x, algorithm="fricas")

[Out] (6*a^3*b*n*x + (b^4*n^3 + 6*b^4*n^2 + 11*b^4*n + 6*b^4)*x^4 - 6*a^4 + (a*b^3*n^3 + 3*a*b^3*n^2 + 2*a*b^3*n)*x^3 - 3*(a^2*b^2*n^2 + a^2*b^2*n)*x^2)*(b*x + a)^n/(b^4*n^4 + 10*b^4*n^3 + 35*b^4*n^2 + 50*b^4*n + 24*b^4)

giac [B] time = 1.21, size = 226, normalized size = 2.72

$$\frac{(bx + a)^n b^4 n^3 x^4 + (bx + a)^n ab^3 n^3 x^3 + 6(bx + a)^n b^4 n^2 x^4 + 3(bx + a)^n ab^3 n^2 x^3 + 11(bx + a)^n b^4 n x^4 - 3(bx + a)^n a^4}{b^4 n^4 + 10 b^4 n^3 + 35 b^4 n^2 + 50 b^4 n + 24 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n,x, algorithm="giac")

[Out] ((b*x + a)^n*b^4*n^3*x^4 + (b*x + a)^n*a*b^3*n^3*x^3 + 6*(b*x + a)^n*b^4*n^2*x^4 + 3*(b*x + a)^n*a*b^3*n^2*x^3 + 11*(b*x + a)^n*b^4*n*x^4 - 3*(b*x + a)^n*a^2*b^2*n^2*x^2 + 2*(b*x + a)^n*a*b^3*n*x^3 + 6*(b*x + a)^n*b^4*x^4 - 3*(b*x + a)^n*a^2*b^2*n*x^2 + 6*(b*x + a)^n*a^3*b*n*x - 6*(b*x + a)^n*a^4)/(b^4*n^4 + 10*b^4*n^3 + 35*b^4*n^2 + 50*b^4*n + 24*b^4)

maple [A] time = 0.01, size = 126, normalized size = 1.52

$$\frac{(-b^3n^3x^3 - 6b^3n^2x^3 + 3ab^2n^2x^2 - 11b^3nx^3 + 9ab^2nx^2 - 6b^3x^3 - 6a^2bnx + 6ab^2x^2 - 6a^2bx + 6a^3)(bx + a)^{n+1}}{(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^n,x)

[Out] -(b*x+a)^(n+1)*(-b^3*n^3*x^3-6*b^3*n^2*x^3+3*a*b^2*n^2*x^2-11*b^3*n*x^3+9*a*b^2*n*x^2-6*b^3*x^3-6*a^2*b*n*x+6*a*b^2*x^2-6*a^2*b*x+6*a^3)/b^4/(n^4+10*n^3+35*n^2+50*n+24)

maxima [A] time = 1.36, size = 101, normalized size = 1.22

$$\frac{\left((n^3 + 6n^2 + 11n + 6)b^4x^4 + (n^3 + 3n^2 + 2n)ab^3x^3 - 3(n^2 + n)a^2b^2x^2 + 6a^3bnx - 6a^4\right)(bx + a)^n}{(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n,x, algorithm="maxima")

[Out] ((n^3 + 6*n^2 + 11*n + 6)*b^4*x^4 + (n^3 + 3*n^2 + 2*n)*a*b^3*x^3 - 3*(n^2 + n)*a^2*b^2*x^2 + 6*a^3*b*n*x - 6*a^4)*(b*x + a)^n/((n^4 + 10*n^3 + 35*n^2 + 50*n + 24)*b^4)

mupad [B] time = 0.53, size = 176, normalized size = 2.12

$$(a + bx)^n \left(\frac{x^4 (n^3 + 6n^2 + 11n + 6)}{n^4 + 10n^3 + 35n^2 + 50n + 24} - \frac{6a^4}{b^4 (n^4 + 10n^3 + 35n^2 + 50n + 24)} \right) + \frac{6a^3nx}{b^3 (n^4 + 10n^3 + 35n^2 + 50n + 24)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(a + b*x)^n,x)

[Out] (a + b*x)^n*((x^4*(11*n + 6*n^2 + n^3 + 6))/(50*n + 35*n^2 + 10*n^3 + n^4 + 24) - (6*a^4)/(b^4*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (6*a^3*n*x)/(b^3*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (a*n*x^3*(3*n + n^2 + 2))/(b*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) - (3*a^2*n*x^2*(n + 1))/(b^2*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)))

sympy [A] time = 2.33, size = 1318, normalized size = 15.88

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**n,x)

[Out] Piecewise((a**n*x**4/4, Eq(b, 0)), (6*a**3*log(a/b + x)/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 11*a**3/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 18*a**2*b*x*log(a/b + x)/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 27*a**2*b*x/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 18*a*b**2*x**2*log(a/b + x)/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 18*a*b**2*x**2/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 6*b**3*x**3*log(a/b + x)/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3), Eq(n, -4)), (-6*a**3*log(a/b + x)/(2*a**2*b**4 + 4*a*b**5*x

```

+ 2*b**6*x**2) - 9*a**3/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) - 12*a**2
*b*x*log(a/b + x)/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) - 12*a**2*b*x/(2
*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) - 6*a*b**2*x**2*log(a/b + x)/(2*a**2
*b**4 + 4*a*b**5*x + 2*b**6*x**2) + 2*b**3*x**3/(2*a**2*b**4 + 4*a*b**5*x +
2*b**6*x**2), Eq(n, -3)), (6*a**3*log(a/b + x)/(2*a*b**4 + 2*b**5*x) + 6*a
**3/(2*a*b**4 + 2*b**5*x) + 6*a**2*b*x*log(a/b + x)/(2*a*b**4 + 2*b**5*x) -
3*a*b**2*x**2/(2*a*b**4 + 2*b**5*x) + b**3*x**3/(2*a*b**4 + 2*b**5*x), Eq(
n, -2)), (-a**3*log(a/b + x)/b**4 + a**2*x/b**3 - a*x**2/(2*b**2) + x**3/(3
*b), Eq(n, -1)), (-6*a**4*(a + b*x)**n/(b**4*n**4 + 10*b**4*n**3 + 35*b**4*
n**2 + 50*b**4*n + 24*b**4) + 6*a**3*b*n*x*(a + b*x)**n/(b**4*n**4 + 10*b**
4*n**3 + 35*b**4*n**2 + 50*b**4*n + 24*b**4) - 3*a**2*b**2*n**2*x**2*(a + b
*x)**n/(b**4*n**4 + 10*b**4*n**3 + 35*b**4*n**2 + 50*b**4*n + 24*b**4) - 3*
a**2*b**2*n*x**2*(a + b*x)**n/(b**4*n**4 + 10*b**4*n**3 + 35*b**4*n**2 + 50
*b**4*n + 24*b**4) + a*b**3*n**3*x**3*(a + b*x)**n/(b**4*n**4 + 10*b**4*n**
3 + 35*b**4*n**2 + 50*b**4*n + 24*b**4) + 3*a*b**3*n**2*x**3*(a + b*x)**n/(
b**4*n**4 + 10*b**4*n**3 + 35*b**4*n**2 + 50*b**4*n + 24*b**4) + 2*a*b**3*n
*x**3*(a + b*x)**n/(b**4*n**4 + 10*b**4*n**3 + 35*b**4*n**2 + 50*b**4*n + 2
4*b**4) + b**4*n**3*x**4*(a + b*x)**n/(b**4*n**4 + 10*b**4*n**3 + 35*b**4*n
**2 + 50*b**4*n + 24*b**4) + 6*b**4*n**2*x**4*(a + b*x)**n/(b**4*n**4 + 10*
b**4*n**3 + 35*b**4*n**2 + 50*b**4*n + 24*b**4) + 11*b**4*n*x**4*(a + b*x)*
n/(b**4*n**4 + 10*b**4*n**3 + 35*b**4*n**2 + 50*b**4*n + 24*b**4) + 6*b**4
*x**4*(a + b*x)**n/(b**4*n**4 + 10*b**4*n**3 + 35*b**4*n**2 + 50*b**4*n + 2
4*b**4), True))

```

3.733 $\int x^2(a + bx)^n dx$

Optimal. Leaf size=60

$$\frac{a^2(a + bx)^{n+1}}{b^3(n + 1)} - \frac{2a(a + bx)^{n+2}}{b^3(n + 2)} + \frac{(a + bx)^{n+3}}{b^3(n + 3)}$$

[Out] $a^2(bx+a)^{(1+n)}/b^3/(1+n)-2*a*(bx+a)^{(2+n)}/b^3/(2+n)+(bx+a)^{(3+n)}/b^3/(3+n)$

Rubi [A] time = 0.02, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{a^2(a + bx)^{n+1}}{b^3(n + 1)} - \frac{2a(a + bx)^{n+2}}{b^3(n + 2)} + \frac{(a + bx)^{n+3}}{b^3(n + 3)}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*x)^n,x]

[Out] $(a^2*(a + b*x)^{(1 + n)})/(b^3*(1 + n)) - (2*a*(a + b*x)^{(2 + n)})/(b^3*(2 + n)) + (a + b*x)^{(3 + n)}/(b^3*(3 + n))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2(a + bx)^n dx &= \int \left(\frac{a^2(a + bx)^n}{b^2} - \frac{2a(a + bx)^{1+n}}{b^2} + \frac{(a + bx)^{2+n}}{b^2} \right) dx \\ &= \frac{a^2(a + bx)^{1+n}}{b^3(1 + n)} - \frac{2a(a + bx)^{2+n}}{b^3(2 + n)} + \frac{(a + bx)^{3+n}}{b^3(3 + n)} \end{aligned}$$

Mathematica [A] time = 0.03, size = 57, normalized size = 0.95

$$\frac{(a + bx)^{n+1} (2a^2 - 2ab(n + 1)x + b^2(n^2 + 3n + 2)x^2)}{b^3(n + 1)(n + 2)(n + 3)}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*x)^n,x]

[Out] ((a + b*x)^(1 + n)*(2*a^2 - 2*a*b*(1 + n)*x + b^2*(2 + 3*n + n^2)*x^2))/(b^3*(1 + n)*(2 + n)*(3 + n))

fricas [A] time = 0.48, size = 96, normalized size = 1.60

$$\frac{(2a^2bnx - (b^3n^2 + 3b^3n + 2b^3)x^3 - 2a^3 - (ab^2n^2 + ab^2n)x^2)(bx + a)^n}{b^3n^3 + 6b^3n^2 + 11b^3n + 6b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n,x, algorithm="fricas")

[Out] -(2*a^2*b*n*x - (b^3*n^2 + 3*b^3*n + 2*b^3)*x^3 - 2*a^3 - (a*b^2*n^2 + a*b^2*n)*x^2)*(b*x + a)^n/(b^3*n^3 + 6*b^3*n^2 + 11*b^3*n + 6*b^3)

giac [B] time = 1.07, size = 140, normalized size = 2.33

$$\frac{(bx + a)^n b^3 n^2 x^3 + (bx + a)^n ab^2 n^2 x^2 + 3(bx + a)^n b^3 n x^3 + (bx + a)^n ab^2 n x^2 + 2(bx + a)^n b^3 x^3 - 2(bx + a)^n a^2 b n x}{b^3 n^3 + 6 b^3 n^2 + 11 b^3 n + 6 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n,x, algorithm="giac")

[Out] ((b*x + a)^n*b^3*n^2*x^3 + (b*x + a)^n*a*b^2*n^2*x^2 + 3*(b*x + a)^n*b^3*n*x^3 + (b*x + a)^n*a*b^2*n*x^2 + 2*(b*x + a)^n*b^3*x^3 - 2*(b*x + a)^n*a^2*b*n*x + 2*(b*x + a)^n*a^3)/(b^3*n^3 + 6*b^3*n^2 + 11*b^3*n + 6*b^3)

maple [A] time = 0.01, size = 73, normalized size = 1.22

$$\frac{(b^2n^2x^2 + 3b^2nx^2 - 2abnx + 2b^2x^2 - 2abx + 2a^2)(bx + a)^{n+1}}{(n^3 + 6n^2 + 11n + 6)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^n,x)

[Out] (b*x+a)^(n+1)*(b^2*n^2*x^2+3*b^2*n*x^2-2*a*b*n*x+2*b^2*x^2-2*a*b*x+2*a^2)/b^3/(n^3+6*n^2+11*n+6)

maxima [A] time = 1.37, size = 68, normalized size = 1.13

$$\frac{((n^2 + 3n + 2)b^3x^3 + (n^2 + n)ab^2x^2 - 2a^2bnx + 2a^3)(bx + a)^n}{(n^3 + 6n^2 + 11n + 6)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n,x, algorithm="maxima")

[Out] ((n^2 + 3*n + 2)*b^3*x^3 + (n^2 + n)*a*b^2*x^2 - 2*a^2*b*n*x + 2*a^3)*(b*x + a)^n/((n^3 + 6*n^2 + 11*n + 6)*b^3)

mupad [B] time = 0.56, size = 192, normalized size = 3.20

$$\left\{ \begin{array}{ll} \frac{2a^2 \ln(a+bx) + b^2 x^2 - 2abx}{2b^3} & \text{if } n = -1 \\ \frac{x}{b^2} - \frac{a^2}{b^3(a+bx)} - \frac{2a \ln(a+bx)}{b^3} & \text{if } n = -2 \\ \frac{\ln(a+bx) + \frac{2a}{a+bx} - \frac{a^2}{2(a+bx)^2}}{b^3} & \text{if } n = -3 \\ \frac{2(a+bx)^{n+1} (8a^2 - 8abnx - 8abx + 4b^2 n^2 x^2 + 12b^2 nx^2 + 8b^2 x^2)}{b^3 (8n^3 + 48n^2 + 88n + 48)} & \text{if } n \neq -1 \wedge n \neq -2 \wedge n \neq -3 \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a + b*x)^n,x)

[Out] piecewise(n == -1, (2*a^2*log(a + b*x) + b^2*x^2 - 2*a*b*x)/(2*b^3), n == -2, x/b^2 - a^2/(b^3*(a + b*x)) - (2*a*log(a + b*x))/b^3, n == -3, (log(a + b*x) + (2*a)/(a + b*x) - a^2/(2*(a + b*x)^2))/b^3, n ~ -1 & n ~ -2 & n ~ -3, (2*(a + b*x)^(n + 1)*(8*a^2 + 8*b^2*x^2 + 12*b^2*n*x^2 - 8*a*b*x + 4*b^2*n^2*x^2 - 8*a*b*n*x))/(b^3*(88*n + 48*n^2 + 8*n^3 + 48)))

sympy [A] time = 1.32, size = 597, normalized size = 9.95

$$\left\{ \begin{array}{l} \frac{a^n x^3}{3} \\ \frac{2a^2 \log\left(\frac{a}{b} + x\right)}{2a^2 b^3 + 4ab^4 x + 2b^5 x^2} + \frac{3a^2}{2a^2 b^3 + 4ab^4 x + 2b^5 x^2} + \frac{4abx \log\left(\frac{a}{b} + x\right)}{2a^2 b^3 + 4ab^4 x + 2b^5 x^2} + \frac{4abx}{2a^2 b^3 + 4ab^4 x + 2b^5 x^2} + \frac{2b^2 x^2 \log\left(\frac{a}{b} + x\right)}{2a^2 b^3 + 4ab^4 x + 2b^5 x^2} \\ \frac{2a^2 \log\left(\frac{a}{b} + x\right)}{ab^3 + b^4 x} - \frac{2a^2}{ab^3 + b^4 x} - \frac{2abx \log\left(\frac{a}{b} + x\right)}{ab^3 + b^4 x} + \frac{b^2 x^2}{ab^3 + b^4 x} \\ \frac{a^2 \log\left(\frac{a}{b} + x\right)}{b^3} - \frac{ax}{b^2} + \frac{x^2}{2b} \\ \frac{2a^3(a+bx)^n}{b^3 n^3 + 6b^3 n^2 + 11b^3 n + 6b^3} - \frac{2a^2 b n x (a+bx)^n}{b^3 n^3 + 6b^3 n^2 + 11b^3 n + 6b^3} + \frac{ab^2 n^2 x^2 (a+bx)^n}{b^3 n^3 + 6b^3 n^2 + 11b^3 n + 6b^3} + \frac{ab^2 n x^2 (a+bx)^n}{b^3 n^3 + 6b^3 n^2 + 11b^3 n + 6b^3} + \frac{b^3 n^2 x^3 (a+bx)^n}{b^3 n^3 + 6b^3 n^2 + 11b^3 n + 6b^3} + \dots \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)**n,x)

[Out] Piecewise((a**n*x**3/3, Eq(b, 0)), (2*a**2*log(a/b + x)/(2*a**2*b**3 + 4*a*b**4*x + 2*b**5*x**2) + 3*a**2/(2*a**2*b**3 + 4*a*b**4*x + 2*b**5*x**2) + 4*a*b*x*log(a/b + x)/(2*a**2*b**3 + 4*a*b**4*x + 2*b**5*x**2) + 4*a*b*x/(2*a**2*b**3 + 4*a*b**4*x + 2*b**5*x**2) + 2*b**2*x**2*log(a/b + x)/(2*a**2*b**3 + 4*a*b**4*x + 2*b**5*x**2), Eq(n, -3)), (-2*a**2*log(a/b + x)/(a*b**3 + b**4*x) - 2*a**2/(a*b**3 + b**4*x) - 2*a*b*x*log(a/b + x)/(a*b**3 + b**4*x) + b**2*x**2/(a*b**3 + b**4*x), Eq(n, -2)), (a**2*log(a/b + x)/b**3 - a*x/b**2 + x**2/(2*b), Eq(n, -1)), (2*a**3*(a + b*x)**n/(b**3*n**3 + 6*b**3*n**2 + 11*b**3*n + 6*b**3) - 2*a**2*b*n*x*(a + b*x)**n/(b**3*n**3 + 6*b**3*n**2 + 11*b**3*n + 6*b**3) + a*b**2*n**2*x**2*(a + b*x)**n/(b**3*n**3 + 6*b**3*n**2 + 11*b**3*n + 6*b**3) + a*b**2*n*x**2*(a + b*x)**n/(b**3*n**3 + 6*b**3*n**2 + 11*b**3*n + 6*b**3) + b**3*n**2*x**3*(a + b*x)**n/(b**3*n**3 + 6*b**3*n**2 + 11*b**3*n + 6*b**3) + 3*b**3*n*x**3*(a + b*x)**n/(b**3*n**3 + 6*b**3*n**2 + 11*b**3*n + 6*b**3) + 2*b**3*x**3*(a + b*x)**n/(b**3*n**3 + 6*b**3*n**2 + 11*b**3*n + 6*b**3), True))

3.734 $\int x(a + bx)^n dx$

Optimal. Leaf size=39

$$\frac{(a + bx)^{n+2}}{b^2(n + 2)} - \frac{a(a + bx)^{n+1}}{b^2(n + 1)}$$

[Out] $-a*(b*x+a)^{(1+n)}/b^2/(1+n)+(b*x+a)^{(2+n)}/b^2/(2+n)$

Rubi [A] time = 0.01, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {43}

$$\frac{(a + bx)^{n+2}}{b^2(n + 2)} - \frac{a(a + bx)^{n+1}}{b^2(n + 1)}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*x)^n,x]

[Out] $-((a*(a + b*x)^{(1 + n)})/(b^2*(1 + n))) + (a + b*x)^{(2 + n)}/(b^2*(2 + n))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x(a + bx)^n dx &= \int \left(-\frac{a(a + bx)^n}{b} + \frac{(a + bx)^{1+n}}{b} \right) dx \\ &= -\frac{a(a + bx)^{1+n}}{b^2(1 + n)} + \frac{(a + bx)^{2+n}}{b^2(2 + n)} \end{aligned}$$

Mathematica [A] time = 0.02, size = 33, normalized size = 0.85

$$\frac{(a + bx)^{n+1}(b(n + 1)x - a)}{b^2(n + 1)(n + 2)}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*x)^n,x]

[Out] $((a + b*x)^{(1 + n)}*(-a + b*(1 + n)*x))/(b^2*(1 + n)*(2 + n))$

fricas [A] time = 0.47, size = 53, normalized size = 1.36

$$\frac{(abnx + (b^2n + b^2)x^2 - a^2)(bx + a)^n}{b^2n^2 + 3b^2n + 2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^n,x, algorithm="fricas")`

[Out] $(a*b*n*x + (b^2*n + b^2)*x^2 - a^2)*(b*x + a)^n/(b^2*n^2 + 3*b^2*n + 2*b^2)$

giac [A] time = 1.05, size = 76, normalized size = 1.95

$$\frac{(bx + a)^n b^2 n x^2 + (bx + a)^n abnx + (bx + a)^n b^2 x^2 - (bx + a)^n a^2}{b^2 n^2 + 3 b^2 n + 2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^n,x, algorithm="giac")`

[Out] $((b*x + a)^n*b^2*n*x^2 + (b*x + a)^n*a*b*n*x + (b*x + a)^n*b^2*x^2 - (b*x + a)^n*a^2)/(b^2*n^2 + 3*b^2*n + 2*b^2)$

maple [A] time = 0.00, size = 36, normalized size = 0.92

$$\frac{(-xnb - bx + a)(bx + a)^{n+1}}{(n^2 + 3n + 2)b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)^n,x)`

[Out] $-(b*x+a)^{(n+1)}*(-b*n*x-b*x+a)/b^2/(n^2+3*n+2)$

maxima [A] time = 1.31, size = 42, normalized size = 1.08

$$\frac{(b^2(n + 1)x^2 + abnx - a^2)(bx + a)^n}{(n^2 + 3n + 2)b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^n,x, algorithm="maxima")`

[Out] $(b^2*(n + 1)*x^2 + a*b*n*x - a^2)*(b*x + a)^n/((n^2 + 3*n + 2)*b^2)$

mupad [B] time = 0.38, size = 94, normalized size = 2.41

$$\left\{ \begin{array}{ll} -\frac{a \ln(a+bx)-bx}{b^2} & \text{if } n = -1 \\ \frac{\ln(a+bx)+\frac{a}{a+bx}}{b^2} & \text{if } n = -2 \\ 2\left(\frac{(a+bx)^{n+2}}{2n+4} - \frac{a(a+bx)^{n+1}}{2n+2}\right) & \text{if } n \neq -1 \wedge n \neq -2 \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(a + b*x)^n,x)`

[Out] `piecewise(n == -1, -(a*log(a + b*x) - b*x)/b^2, n == -2, (log(a + b*x) + a/(a + b*x))/b^2, n ~= -1 & n ~= -2, (2*((a + b*x)^(n + 2)/(2*n + 4) - (a*(a + b*x)^(n + 1))/(2*n + 2)))/b^2)`

sympy [A] time = 0.70, size = 201, normalized size = 5.15

$$\left\{ \begin{array}{ll} \frac{a^n x^2}{2} & \text{for } b = 0 \\ \frac{a \log\left(\frac{a}{b}+x\right)}{ab^2+b^3x} + \frac{a}{ab^2+b^3x} + \frac{bx \log\left(\frac{a}{b}+x\right)}{ab^2+b^3x} & \text{for } n = -2 \\ -\frac{a \log\left(\frac{a}{b}+x\right)}{b^2} + \frac{x}{b} & \text{for } n = -1 \\ -\frac{a^2(a+bx)^n}{b^2n^2+3b^2n+2b^2} + \frac{abnx(a+bx)^n}{b^2n^2+3b^2n+2b^2} + \frac{b^2nx^2(a+bx)^n}{b^2n^2+3b^2n+2b^2} + \frac{b^2x^2(a+bx)^n}{b^2n^2+3b^2n+2b^2} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**n,x)`

[Out] `Piecewise((a**n*x**2/2, Eq(b, 0)), (a*log(a/b + x)/(a*b**2 + b**3*x) + a/(a*b**2 + b**3*x) + b*x*log(a/b + x)/(a*b**2 + b**3*x), Eq(n, -2)), (-a*log(a/b + x)/b**2 + x/b, Eq(n, -1)), (-a**2*(a + b*x)**n/(b**2*n**2 + 3*b**2*n + 2*b**2) + a*b*n*x*(a + b*x)**n/(b**2*n**2 + 3*b**2*n + 2*b**2) + b**2*n*x**2*(a + b*x)**n/(b**2*n**2 + 3*b**2*n + 2*b**2) + b**2*x**2*(a + b*x)**n/(b**2*n**2 + 3*b**2*n + 2*b**2), True))`

3.735 $\int (a + bx)^n dx$

Optimal. Leaf size=18

$$\frac{(a + bx)^{n+1}}{b(n + 1)}$$

[Out] (b*x+a)^(1+n)/b/(1+n)

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(a + bx)^{n+1}}{b(n + 1)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n, x]

[Out] (a + b*x)^(1 + n)/(b*(1 + n))

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^n dx = \frac{(a + bx)^{1+n}}{b(1 + n)}$$

Mathematica [A] time = 0.01, size = 17, normalized size = 0.94

$$\frac{(a + bx)^{n+1}}{bn + b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n, x]

[Out] (a + b*x)^(1 + n)/(b + b*n)

fricas [A] time = 0.49, size = 20, normalized size = 1.11

$$\frac{(bx + a)(bx + a)^n}{bn + b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n,x, algorithm="fricas")

[Out] (b*x + a)*(b*x + a)^n/(b*n + b)

giac [A] time = 1.14, size = 18, normalized size = 1.00

$$\frac{(bx + a)^{n+1}}{b(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n,x, algorithm="giac")

[Out] (b*x + a)^(n + 1)/(b*(n + 1))

maple [A] time = 0.00, size = 19, normalized size = 1.06

$$\frac{(bx + a)^{n+1}}{(n + 1)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n,x)

[Out] (b*x+a)^(n+1)/b/(n+1)

maxima [A] time = 1.30, size = 18, normalized size = 1.00

$$\frac{(bx + a)^{n+1}}{b(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n,x, algorithm="maxima")

[Out] (b*x + a)^(n + 1)/(b*(n + 1))

mupad [B] time = 0.20, size = 18, normalized size = 1.00

$$\frac{(a + bx)^{n+1}}{b(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n,x)

[Out] $(a + b*x)^{(n + 1)}/(b*(n + 1))$

sympy [A] time = 0.07, size = 20, normalized size = 1.11

$$\frac{\begin{cases} \frac{(a+bx)^{n+1}}{n+1} & \text{for } n \neq -1 \\ \log(a + bx) & \text{otherwise} \end{cases}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n,x)

[Out] Piecewise(((a + b*x)**(n + 1)/(n + 1), Ne(n, -1)), (log(a + b*x), True))/b

$$3.736 \quad \int \frac{(a+bx)^n}{x} dx$$

Optimal. Leaf size=35

$$-\frac{(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)}$$

[Out] $-(b*x+a)^{(1+n)}*\text{hypergeom}([1, 1+n], [2+n], 1+b*x/a)/a/(1+n)$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {65}

$$-\frac{(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n/x, x]

[Out] $-\left(\left(\left(a + b*x\right)^{(1+n)}*\text{Hypergeometric2F1}\left[1, 1+n, 2+n, 1 + \left(b*x\right)/a\right]\right)/\left(a*\left(1+n\right)\right)\right)$

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/((d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(a+bx)^n}{x} dx = -\frac{(a+bx)^{1+n} {}_2F_1\left(1, 1+n; 2+n; 1 + \frac{bx}{a}\right)}{a(1+n)}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 1.00

$$-\frac{(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/x, x]

[Out] -(((a + b*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, 1 + (b*x)/a])/(a*(1 + n)))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^n}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x, x, algorithm="fricas")

[Out] integral((b*x + a)^n/x, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x, x, algorithm="giac")

[Out] integrate((b*x + a)^n/x, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n/x, x)

[Out] int((b*x+a)^n/x, x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x, x, algorithm="maxima")

[Out] integrate((b*x + a)^n/x, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(a + bx)^n}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/x, x)

[Out] int((a + b*x)^n/x, x)

sympy [B] time = 1.60, size = 83, normalized size = 2.37

$$\frac{bb^n n \left(\frac{a}{b} + x\right) \left(\frac{a}{b} + x\right)^n \Phi\left(\frac{b\left(\frac{a}{b} + x\right)}{a}, 1, n + 1\right) \Gamma(n + 1)}{a \Gamma(n + 2)} - \frac{bb^n \left(\frac{a}{b} + x\right) \left(\frac{a}{b} + x\right)^n \Phi\left(\frac{b\left(\frac{a}{b} + x\right)}{a}, 1, n + 1\right) \Gamma(n + 1)}{a \Gamma(n + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n/x, x)

[Out] -b*b**n*n*(a/b + x)*(a/b + x)**n*lerchphi(b*(a/b + x)/a, 1, n + 1)*gamma(n + 1)/(a*gamma(n + 2)) - b*b**n*(a/b + x)*(a/b + x)**n*lerchphi(b*(a/b + x)/a, 1, n + 1)*gamma(n + 1)/(a*gamma(n + 2))

$$3.737 \quad \int \frac{(a+bx)^n}{x^2} dx$$

Optimal. Leaf size=35

$$\frac{b(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)}$$

[Out] b*(b*x+a)^(1+n)*hypergeom([2, 1+n], [2+n], 1+b*x/a)/a^2/(1+n)

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {65}

$$\frac{b(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n/x^2, x]

[Out] (b*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n))

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(a+bx)^n}{x^2} dx = \frac{b(a+bx)^{1+n} {}_2F_1\left(2, 1+n; 2+n; 1 + \frac{bx}{a}\right)}{a^2(1+n)}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 1.00

$$\frac{b(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/x^2,x]

[Out] (b*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n))

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^n}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^2,x, algorithm="fricas")

[Out] integral((b*x + a)^n/x^2, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^2,x, algorithm="giac")

[Out] integrate((b*x + a)^n/x^2, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n/x^2,x)

[Out] int((b*x+a)^n/x^2,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^2,x, algorithm="maxima")

[Out] integrate((b*x + a)^n/x^2, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(a + bx)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/x^2, x)

[Out] int((a + b*x)^n/x^2, x)

sympy [B] time = 2.09, size = 354, normalized size = 10.11

$$\frac{ab^2b^n n^2 \left(\frac{a}{b} + x\right) \left(\frac{a}{b} + x\right)^n \Phi\left(\frac{b\left(\frac{a}{b} + x\right)}{a}, 1, n + 1\right) \Gamma(n + 1)}{-a^3 \Gamma(n + 2) + a^2 b \left(\frac{a}{b} + x\right) \Gamma(n + 2)} + \frac{ab^2b^n n \left(\frac{a}{b} + x\right) \left(\frac{a}{b} + x\right)^n \Phi\left(\frac{b\left(\frac{a}{b} + x\right)}{a}, 1, n + 1\right) \Gamma(n + 1)}{-a^3 \Gamma(n + 2) + a^2 b \left(\frac{a}{b} + x\right) \Gamma(n + 2)} - \frac{a}{-a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n/x**2, x)

[Out] a*b**2*b**n*n**2*(a/b + x)*(a/b + x)**n*lerchphi(b*(a/b + x)/a, 1, n + 1)*gamma(n + 1)/(-a**3*gamma(n + 2) + a**2*b*(a/b + x)*gamma(n + 2)) + a*b**2*b**n*n*(a/b + x)*(a/b + x)**n*lerchphi(b*(a/b + x)/a, 1, n + 1)*gamma(n + 1)/(-a**3*gamma(n + 2) + a**2*b*(a/b + x)*gamma(n + 2)) - a*b**2*b**n*n*(a/b + x)*(a/b + x)**n*gamma(n + 1)/(-a**3*gamma(n + 2) + a**2*b*(a/b + x)*gamma(n + 2)) - a*b**2*b**n*(a/b + x)*(a/b + x)**n*gamma(n + 1)/(-a**3*gamma(n + 2) + a**2*b*(a/b + x)*gamma(n + 2)) - b**3*b**n*n**2*(a/b + x)**2*(a/b + x)**n*lerchphi(b*(a/b + x)/a, 1, n + 1)*gamma(n + 1)/(-a**3*gamma(n + 2) + a**2*b*(a/b + x)*gamma(n + 2)) - b**3*b**n*n*(a/b + x)**2*(a/b + x)**n*lerchphi(b*(a/b + x)/a, 1, n + 1)*gamma(n + 1)/(-a**3*gamma(n + 2) + a**2*b*(a/b + x)*gamma(n + 2))

$$3.738 \quad \int \frac{(a+bx)^n}{x^3} dx$$

Optimal. Leaf size=38

$$-\frac{b^2(a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3(n+1)}$$

[Out] $-b^2*(b*x+a)^{(1+n)}*\text{hypergeom}([3, 1+n], [2+n], 1+b*x/a)/a^3/(1+n)$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {65}

$$-\frac{b^2(a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3(n+1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^n/x^3, x]$

[Out] $-((b^2*(a + b*x)^{(1 + n)}*\text{Hypergeometric2F1}[3, 1 + n, 2 + n, 1 + (b*x)/a])/(a^3*(1 + n)))$

Rule 65

$\text{Int}[(b_*)*(x_*)^{(m_*)}*((c_*) + (d_*)*(x_*))^{(n_*)}, x_Symbol] :> \text{Simp}[(c + d*x)^{(n + 1)}*\text{Hypergeometric2F1}[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; \text{FreeQ}\{b, c, d, m, n\}, x \ \&\& \ !\text{IntegerQ}[n] \ \&\& \ (\text{IntegerQ}[m] \ || \ \text{GtQ}[-(d/(b*c)), 0])$

Rubi steps

$$\int \frac{(a+bx)^n}{x^3} dx = -\frac{b^2(a+bx)^{1+n} {}_2F_1\left(3, 1+n; 2+n; 1 + \frac{bx}{a}\right)}{a^3(1+n)}$$

Mathematica [A] time = 0.01, size = 38, normalized size = 1.00

$$-\frac{b^2(a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3(n+1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/x^3,x]

[Out] $-\left(\frac{b^2(a + bx)^{(1+n)} \operatorname{Hypergeometric2F1}\left[3, 1+n, 2+n, 1 + \frac{bx}{a}\right]}{a^{3(1+n)}}\right)$

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\operatorname{integral}\left(\frac{(bx + a)^n}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^3,x, algorithm="fricas")

[Out] integral((b*x + a)^n/x^3, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^3,x, algorithm="giac")

[Out] integrate((b*x + a)^n/x^3, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n/x^3,x)

[Out] int((b*x+a)^n/x^3,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^3,x, algorithm="maxima")

[Out] integrate((b*x + a)^n/x^3, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(a + bx)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/x^3,x)

[Out] int((a + b*x)^n/x^3, x)

sympy [B] time = 2.84, size = 918, normalized size = 24.16

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n/x**3,x)

[Out]
$$-a^{**2}b^{**3}b^{**n}n^{**3}(a/b + x)(a/b + x)^{**n}\text{lerchphi}(b(a/b + x)/a, 1, n + 1)\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) + a^{**2}b^{**3}b^{**n}n^{**2}(a/b + x)(a/b + x)^{**n}\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) + a^{**2}b^{**3}b^{**n}n(a/b + x)(a/b + x)^{**n}\text{lerchphi}(b(a/b + x)/a, 1, n + 1)\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) - a^{**2}b^{**3}b^{**n}n(a/b + x)(a/b + x)^{**n}\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) - 2a^{**2}b^{**3}b^{**n}(a/b + x)(a/b + x)^{**n}\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) + 2ab^{**4}b^{**n}n^{**3}(a/b + x)^{**2}(a/b + x)^{**n}\text{lerchphi}(b(a/b + x)/a, 1, n + 1)\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) - ab^{**4}b^{**n}n^{**2}(a/b + x)^{**2}(a/b + x)^{**n}\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) - 2ab^{**4}b^{**n}n(a/b + x)^{**2}(a/b + x)^{**n}\text{lerchphi}(b(a/b + x)/a, 1, n + 1)\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) + ab^{**4}b^{**n}(a/b + x)^{**2}(a/b + x)^{**n}\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2) - b^{**5}b^{**n}n^{**3}(a/b + x)^{**3}(a/b + x)^{**n}\text{lerchphi}(b(a/b + x)/a, 1, n + 1)\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) + b^{**5}b^{**n}n(a/b + x)^{**3}(a/b + x)^{**n}\text{lerchphi}(b(a/b + x)/a, 1, n + 1)\text{gamma}(n + 1)/(2a^{**5}\text{gamma}(n + 2) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)) - 4a^{**4}b(a/b + x)\text{gamma}(n + 2) + 2a^{**3}b^{**2}(a/b + x)^{**2}\text{gamma}(n + 2)$$

$$3.739 \quad \int x^{-4+n}(a+bx)^{-n} dx$$

Optimal. Leaf size=110

$$-\frac{2b^2x^{n-1}(a+bx)^{1-n}}{a^3(1-n)(2-n)(3-n)} + \frac{2bx^{n-2}(a+bx)^{1-n}}{a^2(2-n)(3-n)} - \frac{x^{n-3}(a+bx)^{1-n}}{a(3-n)}$$

[Out] $-x^{(-3+n)}*(b*x+a)^{(1-n)}/a/(3-n)+2*b*x^{(-2+n)}*(b*x+a)^{(1-n)}/a^2/(2-n)/(3-n)-2*b^2*x^{(-1+n)}*(b*x+a)^{(1-n)}/a^3/(3-n)/(n^2-3*n+2)$

Rubi [A] time = 0.04, antiderivative size = 110, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{2b^2x^{n-1}(a+bx)^{1-n}}{a^3(1-n)(2-n)(3-n)} + \frac{2bx^{n-2}(a+bx)^{1-n}}{a^2(2-n)(3-n)} - \frac{x^{n-3}(a+bx)^{1-n}}{a(3-n)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(-4+n)}/(a+b*x)^n, x]$

[Out] $-((x^{(-3+n)}*(a+b*x)^{(1-n)})/(a*(3-n))) + (2*b*x^{(-2+n)}*(a+b*x)^{(1-n)})/(a^2*(2-n)*(3-n)) - (2*b^2*x^{(-1+n)}*(a+b*x)^{(1-n)})/(a^3*(1-n)*(2-n)*(3-n))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{EqQ}[m + n + 2, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rule 45

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] - \text{Dist}[(d*\text{Simplify}[m + n + 2])/((b*c - a*d)*(m+1)), \text{Int}[(a + b*x)^{\text{Simplify}[m + 1]}*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IntegerQ}[m + n + 2] \ \&\& \ \text{LtQ}[\text{Simplify}[m + n + 2], 0] \ \&\& \ \text{NeQ}[m, -1] \ \&\& \ !(\text{LtQ}[m, -1] \ \&\& \ \text{LtQ}[n, -1] \ \&\& \ (\text{EqQ}[a, 0] \ || \ (\text{NeQ}[c, 0] \ \&\& \ \text{LtQ}[m - n, 0] \ \&\& \ \text{IntegerQ}[n]))) \ \&\& \ (\text{SumSimplerQ}[m, 1] \ || \ !\text{SumSimplerQ}[n, 1])$

Rubi steps

$$\begin{aligned}
\int x^{-4+n}(a+bx)^{-n} dx &= -\frac{x^{-3+n}(a+bx)^{1-n}}{a(3-n)} - \frac{(2b) \int x^{-3+n}(a+bx)^{-n} dx}{a(3-n)} \\
&= -\frac{x^{-3+n}(a+bx)^{1-n}}{a(3-n)} + \frac{2bx^{-2+n}(a+bx)^{1-n}}{a^2(2-n)(3-n)} + \frac{(2b^2) \int x^{-2+n}(a+bx)^{-n} dx}{a^2(2-n)(3-n)} \\
&= -\frac{x^{-3+n}(a+bx)^{1-n}}{a(3-n)} + \frac{2bx^{-2+n}(a+bx)^{1-n}}{a^2(2-n)(3-n)} - \frac{2b^2x^{-1+n}(a+bx)^{1-n}}{a^3(1-n)(2-n)(3-n)}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 64, normalized size = 0.58

$$\frac{x^{n-3}(a+bx)^{1-n} \left(a^2(n^2-3n+2) + 2ab(n-1)x + 2b^2x^2 \right)}{a^3(n-3)(n-2)(n-1)}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-4 + n)/(a + b*x)^n,x]

[Out] (x^(-3 + n)*(a + b*x)^(1 - n)*(a^2*(2 - 3*n + n^2) + 2*a*b*(-1 + n)*x + 2*b^2*x^2))/(a^3*(-3 + n)*(-2 + n)*(-1 + n))

fricas [A] time = 0.52, size = 104, normalized size = 0.95

$$\frac{(2ab^2nx^3 + 2b^3x^4 + (a^2bn^2 - a^2bn)x^2 + (a^3n^2 - 3a^3n + 2a^3)x)x^{n-4}}{(a^3n^3 - 6a^3n^2 + 11a^3n - 6a^3)(bx + a)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-4+n)/((b*x+a)^n),x, algorithm="fricas")

[Out] (2*a*b^2*n*x^3 + 2*b^3*x^4 + (a^2*b*n^2 - a^2*b*n)*x^2 + (a^3*n^2 - 3*a^3*n + 2*a^3)*x)*x^(n - 4)/((a^3*n^3 - 6*a^3*n^2 + 11*a^3*n - 6*a^3)*(b*x + a)^n)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{n-4}}{(bx+a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-4+n)/((b*x+a)^n),x, algorithm="giac")

[Out] integrate(x^(n - 4)/(b*x + a)^n, x)

maple [A] time = 0.01, size = 77, normalized size = 0.70

$$\frac{(bx + a) \left(a^2 n^2 + 2abnx + 2b^2 x^2 - 3a^2 n - 2abx + 2a^2 \right) x^{n-3} (bx + a)^{-n}}{(n-3)(n-2)(n-1)a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(-4+n)/((b*x+a)^n), x)

[Out] x^(-3+n)*(b*x+a)*(a^2*n^2+2*a*b*n*x+2*b^2*x^2-3*a^2*n-2*a*b*x+2*a^2)/((b*x+a)^n)/(-3+n)/(-2+n)/(-1+n)/a^3

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{n-4}}{(bx + a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-4+n)/((b*x+a)^n), x, algorithm="maxima")

[Out] integrate(x^(n - 4)/(b*x + a)^n, x)

mupad [B] time = 0.52, size = 136, normalized size = 1.24

$$\frac{\frac{x x^{n-4} (n^2 - 3n + 2)}{n^3 - 6n^2 + 11n - 6} + \frac{2b^3 x^{n-4} x^4}{a^3 (n^3 - 6n^2 + 11n - 6)} + \frac{2b^2 n x^{n-4} x^3}{a^2 (n^3 - 6n^2 + 11n - 6)} + \frac{b n x^{n-4} x^2 (n-1)}{a (n^3 - 6n^2 + 11n - 6)}}{(a + bx)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(n - 4)/(a + b*x)^n, x)

[Out] ((x*x^(n - 4)*(n^2 - 3*n + 2))/(11*n - 6*n^2 + n^3 - 6) + (2*b^3*x^(n - 4)*x^4)/(a^3*(11*n - 6*n^2 + n^3 - 6)) + (2*b^2*n*x^(n - 4)*x^3)/(a^2*(11*n - 6*n^2 + n^3 - 6)) + (b*n*x^(n - 4)*x^2*(n - 1))/(a*(11*n - 6*n^2 + n^3 - 6)))/(a + b*x)^n

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(-4+n)/((b*x+a)**n), x)

[Out] Timed out

3.740 $\int x^{-3+n}(a+bx)^{-n} dx$

Optimal. Leaf size=64

$$\frac{bx^{n-1}(a+bx)^{1-n}}{a^2(1-n)(2-n)} - \frac{x^{n-2}(a+bx)^{1-n}}{a(2-n)}$$

[Out] $-x^{(-2+n)}*(b*x+a)^{(1-n)}/a/(2-n)+b*x^{(-1+n)}*(b*x+a)^{(1-n)}/a^2/(1-n)/(2-n)$

Rubi [A] time = 0.01, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{bx^{n-1}(a+bx)^{1-n}}{a^2(1-n)(2-n)} - \frac{x^{n-2}(a+bx)^{1-n}}{a(2-n)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(-3+n)}/(a+b*x)^n, x]$

[Out] $-((x^{(-2+n)}*(a+b*x)^{(1-n)})/(a*(2-n))) + (b*x^{(-1+n)}*(a+b*x)^{(1-n)})/(a^2*(1-n)*(2-n))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] - \text{Dist}[(d*Simplify[m + n + 2])/((b*c - a*d)*(m+1)), \text{Int}[(a + b*x)^{\text{Simplify}[m+1]}*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int x^{-3+n}(a+bx)^{-n} dx = -\frac{x^{-2+n}(a+bx)^{1-n}}{a(2-n)} - \frac{b \int x^{-2+n}(a+bx)^{-n} dx}{a(2-n)}$$

$$= -\frac{x^{-2+n}(a+bx)^{1-n}}{a(2-n)} + \frac{bx^{-1+n}(a+bx)^{1-n}}{a^2(1-n)(2-n)}$$

Mathematica [A] time = 0.02, size = 39, normalized size = 0.61

$$\frac{x^{n-2}(a+bx)^{1-n}(a(n-1)+bx)}{a^2(n-2)(n-1)}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-3 + n)/(a + b*x)^n, x]

[Out] (x^(-2 + n)*(a + b*x)^(1 - n)*(a*(-1 + n) + b*x))/(a^2*(-2 + n)*(-1 + n))

fricas [A] time = 0.48, size = 64, normalized size = 1.00

$$\frac{(abnx^2 + b^2x^3 + (a^2n - a^2)x)x^{n-3}}{(a^2n^2 - 3a^2n + 2a^2)(bx + a)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-3+n)/((b*x+a)^n), x, algorithm="fricas")

[Out] (a*b*n*x^2 + b^2*x^3 + (a^2*n - a^2)*x)*x^(n - 3)/((a^2*n^2 - 3*a^2*n + 2*a^2)*(b*x + a)^n)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{n-3}}{(bx+a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-3+n)/((b*x+a)^n), x, algorithm="giac")

[Out] integrate(x^(n - 3)/(b*x + a)^n, x)

maple [A] time = 0.00, size = 44, normalized size = 0.69

$$\frac{(an + bx - a)(bx + a)x^{n-2}(bx + a)^{-n}}{(n-2)(n-1)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(n-3)/((b*x+a)^n),x)`

[Out] $x^{(n-2)}*(a*n+b*x-a)*(b*x+a)/((b*x+a)^n)/(n-2)/(n-1)/a^2$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{n-3}}{(bx+a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(-3+n)/((b*x+a)^n),x, algorithm="maxima")`

[Out] `integrate(x^(n - 3)/(b*x + a)^n, x)`

mupad [B] time = 0.45, size = 80, normalized size = 1.25

$$\frac{\frac{xx^{n-3}(n-1)}{n^2-3n+2} + \frac{b^2x^{n-3}x^3}{a^2(n^2-3n+2)} + \frac{bnx^{n-3}x^2}{a(n^2-3n+2)}}{(a+bx)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(n - 3)/(a + b*x)^n,x)`

[Out] $((x*x^{(n-3)}*(n-1))/(n^2-3*n+2) + (b^2*x^{(n-3)}*x^3)/(a^2*(n^2-3*n+2)) + (b*n*x^{(n-3)}*x^2)/(a*(n^2-3*n+2)))/(a+b*x)^n$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(-3+n)/((b*x+a)**n),x)`

[Out] Timed out

$$3.741 \quad \int x^{-2+n}(a+bx)^{-n} dx$$

Optimal. Leaf size=28

$$\frac{x^{n-1}(a+bx)^{1-n}}{a(1-n)}$$

[Out] $-x^{(-1+n)}*(b*x+a)^{(1-n)}/a/(1-n)$

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$\frac{x^{n-1}(a+bx)^{1-n}}{a(1-n)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(-2+n)}/(a+b*x)^n, x]$

[Out] $-((x^{(-1+n)}*(a+b*x)^{(1-n)})/(a*(1-n)))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)}*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \text{ :> Simp} [(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{EqQ}[m + n + 2, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rubi steps

$$\int x^{-2+n}(a+bx)^{-n} dx = -\frac{x^{-1+n}(a+bx)^{1-n}}{a(1-n)}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 0.89

$$\frac{x^{n-1}(a+bx)^{1-n}}{a(n-1)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(-2+n)}/(a+b*x)^n, x]$

[Out] $(x^{(-1+n)}*(a+b*x)^{(1-n)})/(a*(-1+n))$

fricas [A] time = 0.48, size = 33, normalized size = 1.18

$$\frac{(bx^2 + ax)x^{n-2}}{(an - a)(bx + a)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^{(-2+n)/((b*x+a)^n),x, algorithm="fricas")}

[Out] (b*x² + a*x)*x^{(n - 2)/((a*n - a)*(b*x + a)^n)}

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{n-2}}{(bx + a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^{(-2+n)/((b*x+a)^n),x, algorithm="giac")}

[Out] integrate(x^{(n - 2)/(b*x + a)^n, x)}

maple [A] time = 0.00, size = 29, normalized size = 1.04

$$\frac{(bx + a)x^{n-1}(bx + a)^{-n}}{(n - 1)a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^{(n-2)/((b*x+a)^n),x)}

[Out] (b*x+a)*x^{(n-1)/a/(n-1)/((b*x+a)^n)}

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{n-2}}{(bx + a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^{(-2+n)/((b*x+a)^n),x, algorithm="maxima")}

[Out] integrate(x^{(n - 2)/(b*x + a)^n, x)}

mupad [B] time = 0.35, size = 29, normalized size = 1.04

$$\frac{x^n (a + bx)}{ax (n - 1) (a + bx)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(n - 2)/(a + b*x)^n,x)
```

```
[Out] (x^n*(a + b*x))/(a*x*(n - 1)*(a + b*x)^n)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(-2+n)/((b*x+a)**n),x)
```

```
[Out] Timed out
```

3.742 $\int x^{-1+n}(a+bx)^{-n} dx$

Optimal. Leaf size=39

$$\frac{x^n(a+bx)^{-n} \left(\frac{bx}{a} + 1\right)^n {}_2F_1\left(n, n; n+1; -\frac{bx}{a}\right)}{n}$$

[Out] $x^n(1+b*x/a)^n \text{hypergeom}([n, n], [1+n], -b*x/a)/n/((b*x+a)^n)$

Rubi [A] time = 0.01, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {66, 64}

$$\frac{x^n(a+bx)^{-n} \left(\frac{bx}{a} + 1\right)^n {}_2F_1\left(n, n; n+1; -\frac{bx}{a}\right)}{n}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(-1+n)}/(a+bx)^n, x]$

[Out] $(x^n(1+(b*x)/a)^n \text{Hypergeometric2F1}[n, n, 1+n, -(b*x)/a])/(n*(a+bx)^n)$

Rule 64

$\text{Int}[(b_.)(x_)^{(m_)}((c_) + (d_.)(x_)^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(c^n(b*x)^{(m+1)} \text{Hypergeometric2F1}[-n, m+1, m+2, -(d*x)/c])/(b*(m+1)), x]$
 /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0])))

Rule 66

$\text{Int}[(b_.)(x_)^{(m_)}((c_) + (d_.)(x_)^{(n_)}), x_Symbol] \rightarrow \text{Dist}[(c^{\text{IntPart}[n]}(c+d*x)^{\text{FracPart}[n]})/(1+(d*x)/c)^{\text{FracPart}[n]}, \text{Int}[(b*x)^m(1+(d*x)/c)^n, x], x]$
 /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0])) || !RationalQ[n])

Rubi steps

$$\int x^{-1+n}(a+bx)^{-n} dx = \left((a+bx)^{-n} \left(1 + \frac{bx}{a} \right)^n \right) \int x^{-1+n} \left(1 + \frac{bx}{a} \right)^{-n} dx$$

$$= \frac{x^n (a+bx)^{-n} \left(1 + \frac{bx}{a} \right)^n {}_2F_1 \left(n, n; 1+n; -\frac{bx}{a} \right)}{n}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 1.00

$$\frac{x^n (a+bx)^{-n} \left(\frac{bx}{a} + 1 \right)^n {}_2F_1 \left(n, n; n+1; -\frac{bx}{a} \right)}{n}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-1+n)/(a+b*x)^n,x]

[Out] (x^n*(1+(b*x)/a)^n*Hypergeometric2F1[n,n,1+n,-((b*x)/a)])/(n*(a+b*x)^n)

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{x^{n-1}}{(bx+a)^n}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-1+n)/((b*x+a)^n),x, algorithm="fricas")

[Out] integral(x^(n-1)/(b*x+a)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{n-1}}{(bx+a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-1+n)/((b*x+a)^n),x, algorithm="giac")

[Out] integrate(x^(n-1)/(b*x+a)^n, x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int x^{n-1} (bx+a)^{-n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(n-1)/((b*x+a)^n),x)`

[Out] `int(x^(n-1)/((b*x+a)^n),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{n-1}}{(bx+a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(-1+n)/((b*x+a)^n),x, algorithm="maxima")`

[Out] `integrate(x^(n - 1)/(b*x + a)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^{n-1}}{(a+bx)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(n - 1)/(a + b*x)^n,x)`

[Out] `int(x^(n - 1)/(a + b*x)^n, x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(-1+n)/((b*x+a)**n),x)`

[Out] Timed out

3.743 $\int x^n (a + bx)^{-n} dx$

Optimal. Leaf size=45

$$\frac{x^{n+1}(a+bx)^{-n} \left(\frac{bx}{a} + 1\right)^n {}_2F_1\left(n, n+1; n+2; -\frac{bx}{a}\right)}{n+1}$$

[Out] $x^{(1+n)}*(1+b*x/a)^n*\text{hypergeom}([n, 1+n], [2+n], -b*x/a)/(1+n)/((b*x+a)^n)$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {66, 64}

$$\frac{x^{n+1}(a+bx)^{-n} \left(\frac{bx}{a} + 1\right)^n {}_2F_1\left(n, n+1; n+2; -\frac{bx}{a}\right)}{n+1}$$

Antiderivative was successfully verified.

[In] Int[x^n/(a + b*x)^n, x]

[Out] $(x^{(1+n)}*(1+(b*x)/a)^n*\text{Hypergeometric2F1}[n, 1+n, 2+n, -((b*x)/a)])/(1+n)*(a+b*x)^n$

Rule 64

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -((d*x)/c)]/(b*(m+1)), x]
/; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))
```

Rule 66

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c^IntPart[n]*(c+d*x)^FracPart[n])/(1+(d*x)/c)^FracPart[n], Int[(b*x)^m*(1+(d*x)/c)^n, x], x]
/; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0])) || !RationalQ[n])
```

Rubi steps

$$\int x^n (a + bx)^{-n} dx = \left((a + bx)^{-n} \left(1 + \frac{bx}{a} \right)^n \right) \int x^n \left(1 + \frac{bx}{a} \right)^{-n} dx$$

$$= \frac{x^{1+n} (a + bx)^{-n} \left(1 + \frac{bx}{a} \right)^n {}_2F_1 \left(n, 1 + n; 2 + n; -\frac{bx}{a} \right)}{1 + n}$$

Mathematica [A] time = 0.01, size = 45, normalized size = 1.00

$$\frac{x^{n+1} (a + bx)^{-n} \left(\frac{bx}{a} + 1 \right)^n {}_2F_1 \left(n, n + 1; n + 2; -\frac{bx}{a} \right)}{n + 1}$$

Antiderivative was successfully verified.

[In] Integrate[x^n/(a + b*x)^n,x]

[Out] (x^(1 + n)*(1 + (b*x)/a)^n*Hypergeometric2F1[n, 1 + n, 2 + n, -((b*x)/a)])/((1 + n)*(a + b*x)^n)

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{x^n}{(bx + a)^n}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^n/((b*x+a)^n),x, algorithm="fricas")

[Out] integral(x^n/(b*x + a)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^n}{(bx + a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^n/((b*x+a)^n),x, algorithm="giac")

[Out] integrate(x^n/(b*x + a)^n, x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int x^n (bx + a)^{-n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^n/((b*x+a)^n),x)`

[Out] `int(x^n/((b*x+a)^n),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^n}{(bx+a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^n/((b*x+a)^n),x, algorithm="maxima")`

[Out] `integrate(x^n/(b*x + a)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^n}{(a+bx)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^n/(a + b*x)^n,x)`

[Out] `int(x^n/(a + b*x)^n, x)`

sympy [C] time = 28.69, size = 32, normalized size = 0.71

$$\frac{a^{-n} x^n \Gamma(n+1) {}_2F_1\left(n, n+1 \left| \frac{bx e^{i\pi}}{a} \right. \right)}{\Gamma(n+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**n/((b*x+a)**n),x)`

[Out] `a**(-n)*x**n*gamma(n + 1)*hyper((n, n + 1), (n + 2,), b*x*exp_polar(I*pi)/a)/gamma(n + 2)`

3.744 $\int x^{1+n}(a+bx)^{-n} dx$

Optimal. Leaf size=45

$$\frac{x^{n+2}(a+bx)^{-n} \left(\frac{bx}{a} + 1\right)^n {}_2F_1\left(n, n+2; n+3; -\frac{bx}{a}\right)}{n+2}$$

[Out] $x^{(2+n)}*(1+b*x/a)^n*\text{hypergeom}([n, 2+n], [3+n], -b*x/a)/(2+n)/((b*x+a)^n)$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {66, 64}

$$\frac{x^{n+2}(a+bx)^{-n} \left(\frac{bx}{a} + 1\right)^n {}_2F_1\left(n, n+2; n+3; -\frac{bx}{a}\right)}{n+2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(1+n)}/(a+b*x)^n, x]$

[Out] $(x^{(2+n)}*(1+(b*x)/a)^n*\text{Hypergeometric2F1}[n, 2+n, 3+n, -((b*x)/a)])/((2+n)*(a+b*x)^n)$

Rule 64

$\text{Int}[(b_.)*(x_)^{(m_*)}*((c_) + (d_.)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(c^n*(b*x)^{(m+1)}*\text{Hypergeometric2F1}[-n, m+1, m+2, -((d*x)/c)])/(b*(m+1)), x]$
 /; $\text{FreeQ}\{b, c, d, m, n\}, x$ && $!\text{IntegerQ}[m]$ && $(\text{IntegerQ}[n] \mid\mid (\text{GtQ}[c, 0] \&\& !(\text{EqQ}[n, -2^{(-1)}]) \&\& \text{EqQ}[c^2 - d^2, 0]) \&\& \text{GtQ}[-(d/(b*c)), 0])$

Rule 66

$\text{Int}[(b_.)*(x_)^{(m_*)}*((c_) + (d_.)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Dist}[(c^{\text{IntPart}[n]}*(c+d*x)^{\text{FracPart}[n]}/(1+(d*x)/c)^{\text{FracPart}[n]}, \text{Int}[(b*x)^m*(1+(d*x)/c)^n, x], x]$
 /; $\text{FreeQ}\{b, c, d, m, n\}, x$ && $!\text{IntegerQ}[m]$ && $!\text{IntegerQ}[n]$ && $!\text{GtQ}[c, 0]$ && $!\text{GtQ}[-(d/(b*c)), 0]$ && $((\text{RationalQ}[m] \&\& !(\text{EqQ}[n, -2^{(-1)}]) \&\& \text{EqQ}[c^2 - d^2, 0])) \mid\mid !\text{RationalQ}[n]$

Rubi steps

$$\int x^{1+n}(a+bx)^{-n} dx = \left((a+bx)^{-n} \left(1 + \frac{bx}{a} \right)^n \right) \int x^{1+n} \left(1 + \frac{bx}{a} \right)^{-n} dx$$

$$= \frac{x^{2+n}(a+bx)^{-n} \left(1 + \frac{bx}{a} \right)^n {}_2F_1 \left(n, 2+n; 3+n; -\frac{bx}{a} \right)}{2+n}$$

Mathematica [A] time = 0.01, size = 45, normalized size = 1.00

$$\frac{x^{n+2}(a+bx)^{-n} \left(\frac{bx}{a} + 1 \right)^n {}_2F_1 \left(n, n+2; n+3; -\frac{bx}{a} \right)}{n+2}$$

Antiderivative was successfully verified.

[In] Integrate[x^(1+n)/(a+b*x)^n,x]

[Out] (x^(2+n)*(1+(b*x)/a)^n*Hypergeometric2F1[n,2+n,3+n,-((b*x)/a)])/(2+n)*(a+b*x)^n)

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{x^{n+1}}{(bx+a)^n}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1+n)/((b*x+a)^n),x, algorithm="fricas")

[Out] integral(x^(n+1)/(b*x+a)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{n+1}}{(bx+a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1+n)/((b*x+a)^n),x, algorithm="giac")

[Out] integrate(x^(n+1)/(b*x+a)^n, x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int x^{n+1} (bx+a)^{-n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(n+1)/((b*x+a)^n),x)`

[Out] `int(x^(n+1)/((b*x+a)^n),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^{n+1}}{(bx+a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(1+n)/((b*x+a)^n),x, algorithm="maxima")`

[Out] `integrate(x^(n + 1)/(b*x + a)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^{n+1}}{(a+bx)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(n + 1)/(a + b*x)^n,x)`

[Out] `int(x^(n + 1)/(a + b*x)^n, x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1+n)/((b*x+a)**n),x)`

[Out] Timed out

3.745 $\int x^{3/2}(a + bx)^n dx$

Optimal. Leaf size=45

$$\frac{2}{5}x^{5/2}(a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(\frac{5}{2}, -n; \frac{7}{2}; -\frac{bx}{a}\right)$$

[Out] $2/5*x^{(5/2)}*(b*x+a)^n*\text{hypergeom}([5/2, -n], [7/2], -b*x/a)/((1+b*x/a)^n)$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {66, 64}

$$\frac{2}{5}x^{5/2}(a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(\frac{5}{2}, -n; \frac{7}{2}; -\frac{bx}{a}\right)$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(3/2)}*(a + b*x)^n, x]$

[Out] $(2*x^{(5/2)}*(a + b*x)^n*\text{Hypergeometric2F1}[5/2, -n, 7/2, -(b*x)/a])/((5*(1 + (b*x)/a)^n)$

Rule 64

$\text{Int}[(b_*)*(x_*)^{(m_*)}*((c_*) + (d_*)*(x_*)^{(n_*)}), x_Symbol] \rightarrow \text{Simp}[(c^n*(b*x)^{(m+1)}*\text{Hypergeometric2F1}[-n, m+1, m+2, -(d*x)/c])/(b*(m+1)), x] /; \text{FreeQ}\{b, c, d, m, n\}, x] \&\& \text{!IntegerQ}[m] \&\& (\text{IntegerQ}[n] \mid\mid (\text{GtQ}[c, 0] \&\& \text{!(EqQ}[n, -2^{(-1)}] \&\& \text{EqQ}[c^2 - d^2, 0] \&\& \text{GtQ}[-(d/(b*c)), 0])))$

Rule 66

$\text{Int}[(b_*)*(x_*)^{(m_*)}*((c_*) + (d_*)*(x_*)^{(n_*)}), x_Symbol] \rightarrow \text{Dist}[(c^{\text{IntPart}[n]}*(c + d*x)^{\text{FracPart}[n]})/(1 + (d*x)/c)^{\text{FracPart}[n]}, \text{Int}[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; \text{FreeQ}\{b, c, d, m, n\}, x] \&\& \text{!IntegerQ}[m] \&\& \text{!IntegerQ}[n] \&\& \text{!GtQ}[c, 0] \&\& \text{!GtQ}[-(d/(b*c)), 0] \&\& ((\text{RationalQ}[m] \&\& \text{!(EqQ}[n, -2^{(-1)}] \&\& \text{EqQ}[c^2 - d^2, 0])) \mid\mid \text{!RationalQ}[n])$

Rubi steps

$$\begin{aligned} \int x^{3/2}(a + bx)^n dx &= \left((a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n}\right) \int x^{3/2} \left(1 + \frac{bx}{a}\right)^n dx \\ &= \frac{2}{5}x^{5/2}(a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n} {}_2F_1\left(\frac{5}{2}, -n; \frac{7}{2}; -\frac{bx}{a}\right) \end{aligned}$$

Mathematica [A] time = 0.01, size = 45, normalized size = 1.00

$$\frac{2}{5}x^{5/2}(a+bx)^n\left(\frac{bx}{a}+1\right)^{-n} {}_2F_1\left(\frac{5}{2}, -n; \frac{7}{2}; -\frac{bx}{a}\right)$$

Antiderivative was successfully verified.

[In] Integrate[x^(3/2)*(a + b*x)^n,x]

[Out] (2*x^(5/2)*(a + b*x)^n*Hypergeometric2F1[5/2, -n, 7/2, -((b*x)/a)])/(5*(1 + (b*x)/a)^n)

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left((bx+a)^n x^{\frac{3}{2}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^n,x, algorithm="fricas")

[Out] integral((b*x + a)^n*x^(3/2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx+a)^n x^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^n,x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^(3/2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int x^{\frac{3}{2}}(bx+a)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(b*x+a)^n,x)

[Out] int(x^(3/2)*(b*x+a)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx+a)^n x^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(3/2)*(b*x+a)^n,x, algorithm="maxima")

[Out] integrate((b*x + a)^n*x^(3/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^{3/2} (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(3/2)*(a + b*x)^n,x)

[Out] int(x^(3/2)*(a + b*x)^n, x)

sympy [C] time = 87.99, size = 27, normalized size = 0.60

$$\frac{2a^n x^{\frac{5}{2}} {}_2F_1\left(\frac{5}{2}, -n \mid \frac{bx e^{i\pi}}{a}\right)}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**(3/2)*(b*x+a)**n,x)

[Out] 2*a**n*x**(5/2)*hyper((5/2, -n), (7/2,), b*x*exp_polar(I*pi)/a)/5

3.746 $\int \sqrt{x} (a + bx)^n dx$

Optimal. Leaf size=45

$$\frac{2}{3}x^{3/2}(a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(\frac{3}{2}, -n; \frac{5}{2}; -\frac{bx}{a}\right)$$

[Out] $2/3*x^{3/2}*(b*x+a)^n*\text{hypergeom}([3/2, -n], [5/2], -b*x/a)/((1+b*x/a)^n)$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {66, 64}

$$\frac{2}{3}x^{3/2}(a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(\frac{3}{2}, -n; \frac{5}{2}; -\frac{bx}{a}\right)$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{Sqrt}[x]*(a + b*x)^n, x]$

[Out] $(2*x^{3/2}*(a + b*x)^n*\text{Hypergeometric2F1}[3/2, -n, 5/2, -(b*x)/a])/((3*(1 + (b*x)/a)^n)$

Rule 64

$\text{Int}[(b_*.x_*)^{m_*}((c_*) + (d_*.x_*)^{n_*}), x_Symbol] \rightarrow \text{Simp}[(c^{n_*}(b*x)^{m_*+1}*\text{Hypergeometric2F1}[-n, m_*+1, m_*+2, -(d*x)/c])/(b*(m_*+1)), x] /;$ $\text{FreeQ}\{b, c, d, m, n\}, x \ \&\& \ !\text{IntegerQ}[m] \ \&\& \ (\text{IntegerQ}[n] \ || \ (\text{GtQ}[c, 0] \ \&\& \ !(\text{EqQ}[n, -2^{(-1)}] \ \&\& \ \text{EqQ}[c^2 - d^2, 0] \ \&\& \ \text{GtQ}[-(d/(b*c)), 0])))$

Rule 66

$\text{Int}[(b_*.x_*)^{m_*}((c_*) + (d_*.x_*)^{n_*}), x_Symbol] \rightarrow \text{Dist}[(c^{\text{IntPart}[n]}*(c + d*x)^{\text{FracPart}[n]})/(1 + (d*x)/c)^{\text{FracPart}[n]}, \text{Int}[(b*x)^{m_*}(1 + (d*x)/c)^n, x], x] /;$ $\text{FreeQ}\{b, c, d, m, n\}, x \ \&\& \ !\text{IntegerQ}[m] \ \&\& \ !\text{IntegerQ}[n] \ \&\& \ !\text{GtQ}[c, 0] \ \&\& \ !\text{GtQ}[-(d/(b*c)), 0] \ \&\& \ ((\text{RationalQ}[m] \ \&\& \ !(\text{EqQ}[n, -2^{(-1)}] \ \&\& \ \text{EqQ}[c^2 - d^2, 0])) \ || \ !\text{RationalQ}[n])$

Rubi steps

$$\begin{aligned} \int \sqrt{x} (a + bx)^n dx &= \left((a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n} \right) \int \sqrt{x} \left(1 + \frac{bx}{a}\right)^n dx \\ &= \frac{2}{3}x^{3/2}(a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n} {}_2F_1\left(\frac{3}{2}, -n; \frac{5}{2}; -\frac{bx}{a}\right) \end{aligned}$$

Mathematica [A] time = 0.01, size = 45, normalized size = 1.00

$$\frac{2}{3}x^{3/2}(a+bx)^n\left(\frac{bx}{a}+1\right)^{-n} {}_2F_1\left(\frac{3}{2}, -n; \frac{5}{2}; -\frac{bx}{a}\right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[x]*(a + b*x)^n, x]

[Out] (2*x^(3/2)*(a + b*x)^n*Hypergeometric2F1[3/2, -n, 5/2, -(b*x)/a])/(3*(1 + (b*x)/a)^n)

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}((bx + a)^n \sqrt{x}, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(b*x+a)^n, x, algorithm="fricas")

[Out] integral((b*x + a)^n*sqrt(x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n \sqrt{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(1/2)*(b*x+a)^n, x, algorithm="giac")

[Out] integrate((b*x + a)^n*sqrt(x), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \sqrt{x} (bx + a)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^(1/2)*(b*x+a)^n, x)

[Out] int(x^(1/2)*(b*x+a)^n, x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n \sqrt{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(1/2)*(b*x+a)^n,x, algorithm="maxima")`

[Out] `integrate((b*x + a)^n*sqrt(x), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \sqrt{x} (a + b x)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)*(a + b*x)^n,x)`

[Out] `int(x^(1/2)*(a + b*x)^n, x)`

sympy [C] time = 8.38, size = 27, normalized size = 0.60

$$\frac{2a^n x^{\frac{3}{2}} {}_2F_1\left(\frac{3}{2}, -n \mid \frac{bx e^{i\pi}}{a}\right)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(1/2)*(b*x+a)**n,x)`

[Out] `2*a**n*x**(3/2)*hyper((3/2, -n), (5/2,), b*x*exp_polar(I*pi)/a)/3`

$$3.747 \quad \int \frac{(a+bx)^n}{\sqrt{x}} dx$$

Optimal. Leaf size=43

$$2\sqrt{x}(a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; -\frac{bx}{a}\right)$$

[Out] 2*(b*x+a)^n*hypergeom([1/2, -n], [3/2], -b*x/a)*x^(1/2)/((1+b*x/a)^n)

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {66, 64}

$$2\sqrt{x}(a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; -\frac{bx}{a}\right)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n/Sqrt[x], x]

[Out] (2*Sqrt[x]*(a + b*x)^n*Hypergeometric2F1[1/2, -n, 3/2, -(b*x)/a])/((1 + (b*x)/a)^n)

Rule 64

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -(d*x)/c])/(b*(m + 1)), x]
/; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0])))
```

Rule 66

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c^IntPart[n]*(c + d*x)^FracPart[n])/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x], x]
/; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0])) || !RationalQ[n])
```

Rubi steps

$$\int \frac{(a+bx)^n}{\sqrt{x}} dx = \left((a+bx)^n \left(1 + \frac{bx}{a} \right)^{-n} \right) \int \frac{\left(1 + \frac{bx}{a} \right)^n}{\sqrt{x}} dx$$

$$= 2\sqrt{x} (a+bx)^n \left(1 + \frac{bx}{a} \right)^{-n} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; -\frac{bx}{a}\right)$$

Mathematica [A] time = 0.01, size = 43, normalized size = 1.00

$$2\sqrt{x} (a+bx)^n \left(\frac{bx}{a} + 1 \right)^{-n} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; -\frac{bx}{a}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/Sqrt[x], x]

[Out] (2*Sqrt[x]*(a + b*x)^n*Hypergeometric2F1[1/2, -n, 3/2, -((b*x)/a)])/(1 + (b*x)/a)^n

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^n}{\sqrt{x}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^(1/2), x, algorithm="fricas")

[Out] integral((b*x + a)^n/sqrt(x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^(1/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n/sqrt(x), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^n/x^(1/2),x)`

[Out] `int((b*x+a)^n/x^(1/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^n/x^(1/2),x, algorithm="maxima")`

[Out] `integrate((b*x+a)^n/sqrt(x),x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a+bx)^n}{\sqrt{x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*x)^n/x^(1/2),x)`

[Out] `int((a+b*x)^n/x^(1/2),x)`

sympy [C] time = 5.69, size = 26, normalized size = 0.60

$$2a^n \sqrt{x} {}_2F_1 \left(\begin{matrix} \frac{1}{2}, -n \\ \frac{3}{2} \end{matrix} \middle| \frac{bx e^{i\pi}}{a} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**n/x**(1/2),x)`

[Out] `2*a**n*sqrt(x)*hyper((1/2, -n), (3/2,), b*x*exp_polar(I*pi)/a)`

$$3.748 \quad \int \frac{(a+bx)^n}{x^{3/2}} dx$$

Optimal. Leaf size=43

$$\frac{2(a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(-\frac{1}{2}, -n; \frac{1}{2}; -\frac{bx}{a}\right)}{\sqrt{x}}$$

[Out] $-2*(b*x+a)^n*\text{hypergeom}([-1/2, -n], [1/2], -b*x/a)/((1+b*x/a)^n)/x^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {66, 64}

$$\frac{2(a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(-\frac{1}{2}, -n; \frac{1}{2}; -\frac{bx}{a}\right)}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n/x^(3/2), x]

[Out] $(-2*(a + b*x)^n*\text{Hypergeometric2F1}[-1/2, -n, 1/2, -(b*x)/a])/(\text{Sqrt}[x]*(1 + (b*x)/a)^n)$

Rule 64

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -(d*x)/c])/(b*(m+1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rule 66

Int[(b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c^IntPart[n]*(c + d*x)^FracPart[n])/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0])) || !RationalQ[n])

Rubi steps

$$\int \frac{(a+bx)^n}{x^{3/2}} dx = \left((a+bx)^n \left(1 + \frac{bx}{a} \right)^{-n} \right) \int \frac{\left(1 + \frac{bx}{a} \right)^n}{x^{3/2}} dx$$

$$= -\frac{2(a+bx)^n \left(1 + \frac{bx}{a} \right)^{-n} {}_2F_1\left(-\frac{1}{2}, -n; \frac{1}{2}; -\frac{bx}{a}\right)}{\sqrt{x}}$$

Mathematica [A] time = 0.01, size = 43, normalized size = 1.00

$$-\frac{2(a+bx)^n \left(\frac{bx}{a} + 1 \right)^{-n} {}_2F_1\left(-\frac{1}{2}, -n; \frac{1}{2}; -\frac{bx}{a}\right)}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/x^(3/2), x]

[Out] (-2*(a + b*x)^n*Hypergeometric2F1[-1/2, -n, 1/2, -((b*x)/a)])/(Sqrt[x]*(1 + (b*x)/a)^n)

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^n}{x^{\frac{3}{2}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^(3/2), x, algorithm="fricas")

[Out] integral((b*x + a)^n/x^(3/2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n}{x^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^(3/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n/x^(3/2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n/x^(3/2),x)

[Out] int((b*x+a)^n/x^(3/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^(3/2),x, algorithm="maxima")

[Out] integrate((b*x + a)^n/x^(3/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^n}{x^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/x^(3/2),x)

[Out] int((a + b*x)^n/x^(3/2), x)

sympy [C] time = 31.96, size = 29, normalized size = 0.67

$$\frac{2a^n {}_2F_1\left(-\frac{1}{2}, -n \mid \frac{bx e^{i\pi}}{a}\right)}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n/x**(3/2),x)

[Out] -2*a**n*hyper((-1/2, -n), (1/2,), b*x*exp_polar(I*pi)/a)/sqrt(x)

$$3.749 \quad \int \frac{(a+bx)^n}{x^{5/2}} dx$$

Optimal. Leaf size=45

$$\frac{2(a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(-\frac{3}{2}, -n; -\frac{1}{2}; -\frac{bx}{a}\right)}{3x^{3/2}}$$

[Out] $-2/3*(b*x+a)^n*\text{hypergeom}([-3/2, -n], [-1/2], -b*x/a)/x^{(3/2)/((1+b*x/a)^n)}$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {66, 64}

$$\frac{2(a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(-\frac{3}{2}, -n; -\frac{1}{2}; -\frac{bx}{a}\right)}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n/x^(5/2), x]

[Out] $(-2*(a + b*x)^n*\text{Hypergeometric2F1}[-3/2, -n, -1/2, -((b*x)/a)])/(3*x^{(3/2)}*(1 + (b*x)/a)^n)$

Rule 64

Int[((b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -((d*x)/c)]/(b*(m+1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rule 66

Int[((b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Dist[(c^IntPart[n]*(c + d*x)^FracPart[n]]/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0])) || !RationalQ[n])

Rubi steps

$$\int \frac{(a + bx)^n}{x^{5/2}} dx = \left((a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} \right) \int \frac{\left(1 + \frac{bx}{a} \right)^n}{x^{5/2}} dx$$

$$= -\frac{2(a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} {}_2F_1\left(-\frac{3}{2}, -n; -\frac{1}{2}; -\frac{bx}{a}\right)}{3x^{3/2}}$$

Mathematica [A] time = 0.01, size = 45, normalized size = 1.00

$$-\frac{2(a + bx)^n \left(\frac{bx}{a} + 1 \right)^{-n} {}_2F_1\left(-\frac{3}{2}, -n; -\frac{1}{2}; -\frac{bx}{a}\right)}{3x^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/x^(5/2), x]

[Out] (-2*(a + b*x)^n*Hypergeometric2F1[-3/2, -n, -1/2, -(b*x)/a])/(3*x^(3/2)*(1 + (b*x)/a)^n)

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^n}{x^{\frac{5}{2}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^(5/2), x, algorithm="fricas")

[Out] integral((b*x + a)^n/x^(5/2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^(5/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n/x^(5/2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n/x^(5/2),x)

[Out] int((b*x+a)^n/x^(5/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{x^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^(5/2),x, algorithm="maxima")

[Out] integrate((b*x + a)^n/x^(5/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^n}{x^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/x^(5/2),x)

[Out] int((a + b*x)^n/x^(5/2), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n/x**(5/2),x)

[Out] Timed out

3.750 $\int (bx)^m (2 + dx)^n dx$

Optimal. Leaf size=35

$$\frac{2^n (bx)^{m+1} {}_2F_1\left(m+1, -n; m+2; -\frac{dx}{2}\right)}{b(m+1)}$$

[Out] $2^n (bx)^{1+m} \text{hypergeom}([-n, 1+m], [2+m], -1/2*d*x)/b/(1+m)$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {64}

$$\frac{2^n (bx)^{m+1} {}_2F_1\left(m+1, -n; m+2; -\frac{dx}{2}\right)}{b(m+1)}$$

Antiderivative was successfully verified.

[In] Int[(b*x)^m*(2 + d*x)^n,x]

[Out] $(2^n (bx)^{1+m} \text{Hypergeometric2F1}[1+m, -n, 2+m, -(d*x)/2])/(b*(1+m))$

Rule 64

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -((d*x)/c)])/(b*(m+1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rubi steps

$$\int (bx)^m (2 + dx)^n dx = \frac{2^n (bx)^{1+m} {}_2F_1\left(1+m, -n; 2+m; -\frac{dx}{2}\right)}{b(1+m)}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 0.89

$$\frac{2^n x (bx)^m {}_2F_1\left(m+1, -n; m+2; -\frac{dx}{2}\right)}{m+1}$$

Antiderivative was successfully verified.

[In] Integrate[(b*x)^m*(2 + d*x)^n,x]

[Out] $(2^n*x*(b*x)^m*\text{Hypergeometric2F1}[1 + m, -n, 2 + m, -1/2*(d*x)])/(1 + m)$

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\int (bx)^m (dx + 2)^n, x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*(d*x+2)^n,x, algorithm="fricas")

[Out] integral((b*x)^m*(d*x + 2)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx)^m (dx + 2)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*(d*x+2)^n,x, algorithm="giac")

[Out] integrate((b*x)^m*(d*x + 2)^n, x)

maple [A] time = 0.09, size = 32, normalized size = 0.91

$$\frac{x2^n (bx)^m \text{hypergeom}\left([-n, m + 1], [m + 2], -\frac{dx}{2}\right)}{m + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m*(d*x+2)^n,x)

[Out] $2^n*(b*x)^m/(m+1)*x*\text{hypergeom}([-n, m+1], [m+2], -1/2*d*x)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx)^m (dx + 2)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*(d*x+2)^n,x, algorithm="maxima")

[Out] integrate((b*x)^m*(d*x + 2)^n, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int (bx)^m (dx + 2)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m*(d*x + 2)^n,x)

[Out] int((b*x)^m*(d*x + 2)^n, x)

sympy [C] time = 2.53, size = 37, normalized size = 1.06

$$\frac{2^n b^m x x^m \Gamma(m+1) {}_2F_1\left(-n, m+1 \middle| \frac{dx e^{i\pi}}{2}\right)}{\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)**m*(d*x+2)**n,x)

[Out] 2**n*b**m*x**m*gamma(m + 1)*hyper((-n, m + 1), (m + 2,), d*x*exp_polar(I*pi)/2)/gamma(m + 2)

3.751 $\int (bx)^m (c - bcx)^n dx$

Optimal. Leaf size=40

$$\frac{(c - bcx)^{n+1} {}_2F_1(-m, n + 1; n + 2; 1 - bx)}{bc(n + 1)}$$

[Out] $-(-b*c*x+c)^{(1+n)}*\text{hypergeom}([-m, 1+n], [2+n], -b*x+1)/b/c/(1+n)$

Rubi [A] time = 0.01, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {65}

$$\frac{(c - bcx)^{n+1} {}_2F_1(-m, n + 1; n + 2; 1 - bx)}{bc(n + 1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(b*x)^m*(c - b*c*x)^n, x]$

[Out] $-(((c - b*c*x)^{(1 + n)}*\text{Hypergeometric2F1}[-m, 1 + n, 2 + n, 1 - b*x])/(b*c*(1 + n)))$

Rule 65

$\text{Int}[(b_*)*(x_)^{(m_*)}*((c_) + (d_*)*(x_)^{(n_*)}, x_Symbol] \rightarrow \text{Simp}[(c + d*x)^{(n + 1)}*\text{Hypergeometric2F1}[-m, n + 1, n + 2, 1 + (d*x)/c]/(d*(n + 1)*(-(d/(b*c)))^m), x] /; \text{FreeQ}\{b, c, d, m, n\}, x \ \&\& \ !\text{IntegerQ}[n] \ \&\& \ (\text{IntegerQ}[m] \ || \ \text{GtQ}[-(d/(b*c)), 0])$

Rubi steps

$$\int (bx)^m (c - bcx)^n dx = -\frac{(c - bcx)^{1+n} {}_2F_1(-m, 1 + n; 2 + n; 1 - bx)}{bc(1 + n)}$$

Mathematica [A] time = 0.01, size = 44, normalized size = 1.10

$$\frac{x(bx)^m(1 - bx)^{-n}(c - bcx)^n {}_2F_1(m + 1, -n; m + 2; bx)}{m + 1}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(b*x)^m*(c - b*c*x)^n, x]$

[Out] $(x*(b*x)^m*(c - b*c*x)^n*Hypergeometric2F1[1 + m, -n, 2 + m, b*x])/((1 + m)*(1 - b*x)^n)$

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}((-bcx + c)^n (bx)^m, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x)^m*(-b*c*x+c)^n,x, algorithm="fricas")`

[Out] `integral((-b*c*x + c)^n*(b*x)^m, x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (-bcx + c)^n (bx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x)^m*(-b*c*x+c)^n,x, algorithm="giac")`

[Out] `integrate((-b*c*x + c)^n*(b*x)^m, x)`

maple [F] time = 0.12, size = 0, normalized size = 0.00

$$\int (bx)^m (-bcx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x)^m*(-b*c*x+c)^n,x)`

[Out] `int((b*x)^m*(-b*c*x+c)^n,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (-bcx + c)^n (bx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x)^m*(-b*c*x+c)^n,x, algorithm="maxima")`

[Out] `integrate((-b*c*x + c)^n*(b*x)^m, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (bx)^m (c - bcx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x)^m*(c - b*c*x)^n, x)`

[Out] `int((b*x)^m*(c - b*c*x)^n, x)`

sympy [C] time = 2.50, size = 37, normalized size = 0.92

$$\frac{b^m c^n x x^m \Gamma(m+1) {}_2F_1\left(\begin{matrix} -n, m+1 \\ m+2 \end{matrix} \middle| bxe^{2i\pi}\right)}{\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x)**m*(-b*c*x+c)**n, x)`

[Out] `b**m*c**n*x*x**m*gamma(m + 1)*hyper((-n, m + 1), (m + 2,), b*x*exp_polar(2*I*pi))/gamma(m + 2)`

3.752 $\int (bx)^m (c + dx)^n dx$

Optimal. Leaf size=52

$$\frac{(bx)^{m+1}(c+dx)^n \left(\frac{dx}{c} + 1\right)^{-n} {}_2F_1\left(m+1, -n; m+2; -\frac{dx}{c}\right)}{b(m+1)}$$

[Out] $(b*x)^{(1+m)}*(d*x+c)^n*\text{hypergeom}([-n, 1+m], [2+m], -d*x/c)/b/(1+m)/((1+d*x/c)^n)$

Rubi [A] time = 0.01, antiderivative size = 52, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {66, 64}

$$\frac{(bx)^{m+1}(c+dx)^n \left(\frac{dx}{c} + 1\right)^{-n} {}_2F_1\left(m+1, -n; m+2; -\frac{dx}{c}\right)}{b(m+1)}$$

Antiderivative was successfully verified.

[In] Int[(b*x)^m*(c + d*x)^n,x]

[Out] $((b*x)^{(1+m)}*(c+d*x)^n*\text{Hypergeometric2F1}[1+m, -n, 2+m, -((d*x)/c)])/(b*(1+m)*(1+(d*x)/c)^n)$

Rule 64

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -((d*x)/c)])/(b*(m+1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0])))

Rule 66

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c^IntPart[n]*(c+d*x)^FracPart[n])/(1+(d*x)/c)^FracPart[n], Int[(b*x)^m*(1+(d*x)/c)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0])) || !RationalQ[n])

Rubi steps

$$\int (bx)^m (c + dx)^n dx = \left((c + dx)^n \left(1 + \frac{dx}{c} \right)^{-n} \right) \int (bx)^m \left(1 + \frac{dx}{c} \right)^n dx$$

$$= \frac{(bx)^{1+m} (c + dx)^n \left(1 + \frac{dx}{c} \right)^{-n} {}_2F_1 \left(1 + m, -n; 2 + m; -\frac{dx}{c} \right)}{b(1 + m)}$$

Mathematica [A] time = 0.01, size = 48, normalized size = 0.92

$$\frac{x(bx)^m (c + dx)^n \left(\frac{dx}{c} + 1 \right)^{-n} {}_2F_1 \left(m + 1, -n; m + 2; -\frac{dx}{c} \right)}{m + 1}$$

Antiderivative was successfully verified.

[In] Integrate[(b*x)^m*(c + d*x)^n,x]

[Out] (x*(b*x)^m*(c + d*x)^n*Hypergeometric2F1[1 + m, -n, 2 + m, -((d*x)/c)])/((1 + m)*(1 + (d*x)/c)^n)

fricas [F] time = 0.70, size = 0, normalized size = 0.00

$$\text{integral} \left((bx)^m (dx + c)^n, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*(d*x+c)^n,x, algorithm="fricas")

[Out] integral((b*x)^m*(d*x + c)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx)^m (dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*(d*x+c)^n,x, algorithm="giac")

[Out] integrate((b*x)^m*(d*x + c)^n, x)

maple [F] time = 0.07, size = 0, normalized size = 0.00

$$\int (bx)^m (dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x)^m*(d*x+c)^n,x)`

[Out] `int((b*x)^m*(d*x+c)^n,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx)^m (dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x)^m*(d*x+c)^n,x, algorithm="maxima")`

[Out] `integrate((b*x)^m*(d*x + c)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (bx)^m (c + dx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x)^m*(c + d*x)^n,x)`

[Out] `int((b*x)^m*(c + d*x)^n, x)`

sympy [C] time = 3.17, size = 37, normalized size = 0.71

$$\frac{b^m c^n x x^m \Gamma(m+1) {}_2F_1\left(-n, m+1 \middle| \frac{dx e^{i\pi}}{c}\right)}{\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x)**m*(d*x+c)**n,x)`

[Out] `b**m*c**n*x*x**m*gamma(m + 1)*hyper((-n, m + 1), (m + 2,), d*x*exp_polar(I*pi)/c)/gamma(m + 2)`

$$3.753 \quad \int x^{-1+n}(a+bx)^{-1-n} dx$$

Optimal. Leaf size=19

$$\frac{x^n(a+bx)^{-n}}{an}$$

[Out] $x^n/a/n/((b*x+a)^n)$

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {37}

$$\frac{x^n(a+bx)^{-n}}{an}$$

Antiderivative was successfully verified.

[In] Int[x^(-1 + n)*(a + b*x)^(-1 - n), x]

[Out] $x^n/(a*n*(a + b*x)^n)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int x^{-1+n}(a+bx)^{-1-n} dx = \frac{x^n(a+bx)^{-n}}{an}$$

Mathematica [A] time = 0.00, size = 19, normalized size = 1.00

$$\frac{x^n(a+bx)^{-n}}{an}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-1 + n)*(a + b*x)^(-1 - n), x]

[Out] $x^n/(a*n*(a + b*x)^n)$

fricas [A] time = 0.51, size = 32, normalized size = 1.68

$$\frac{(bx^2 + ax)(bx + a)^{-n-1}x^{n-1}}{an}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x⁽⁻¹⁺ⁿ⁾*(b*x+a)⁽⁻¹⁻ⁿ⁾,x, algorithm="fricas")

[Out] (b*x² + a*x)*(b*x + a)^(-n - 1)*x^(n - 1)/(a*n)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n-1}x^{n-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x⁽⁻¹⁺ⁿ⁾*(b*x+a)⁽⁻¹⁻ⁿ⁾,x, algorithm="giac")

[Out] integrate((b*x + a)^(-n - 1)*x^(n - 1), x)

maple [A] time = 0.00, size = 20, normalized size = 1.05

$$\frac{x^n (bx + a)^{-n}}{an}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x⁽ⁿ⁻¹⁾*(b*x+a)⁽⁻¹⁻ⁿ⁾,x)

[Out] (b*x+a)⁽⁻ⁿ⁾*xⁿ/a/n

maxima [A] time = 1.30, size = 22, normalized size = 1.16

$$\frac{e^{(-n \log(bx+a)+n \log(x))}}{an}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x⁽⁻¹⁺ⁿ⁾*(b*x+a)⁽⁻¹⁻ⁿ⁾,x, algorithm="maxima")

[Out] e^{(-n*log(b*x + a) + n*log(x))}/(a*n)

mupad [B] time = 0.50, size = 19, normalized size = 1.00

$$\frac{x^n}{an(a + bx)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^(n - 1)/(a + b*x)^(n + 1),x)
```

```
[Out] x^n/(a*n*(a + b*x)^n)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(-1+n)*(b*x+a)**(-1-n),x)
```

```
[Out] Timed out
```

3.754 $\int x^{-3-n}(a+bx)^n dx$

Optimal. Leaf size=58

$$\frac{bx^{-n-1}(a+bx)^{n+1}}{a^2(n+1)(n+2)} - \frac{x^{-n-2}(a+bx)^{n+1}}{a(n+2)}$$

[Out] $-x^{(-2-n)}*(b*x+a)^{(1+n)}/a/(2+n)+b*x^{(-1-n)}*(b*x+a)^{(1+n)}/a^2/(1+n)/(2+n)$

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{bx^{-n-1}(a+bx)^{n+1}}{a^2(n+1)(n+2)} - \frac{x^{-n-2}(a+bx)^{n+1}}{a(n+2)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(-3-n)}*(a+bx)^n, x]$

[Out] $-((x^{(-2-n)}*(a+bx)^{(1+n)})/(a*(2+n))) + (b*x^{(-1-n)}*(a+bx)^{(1+n)})/(a^2*(1+n)*(2+n))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x\} \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rule 45

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] - \text{Dist}[(d*Simplify[m + n + 2])/((b*c - a*d)*(m+1)), \text{Int}[(a + b*x)^{\text{Simplify}[m+1]}*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x\} \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[\text{Simplify}[m + n + 2], 0] \&\& \text{NeQ}[m, -1] \&\& !(\text{LtQ}[m, -1] \&\& \text{LtQ}[n, -1] \&\& (\text{EqQ}[a, 0] \|\| (\text{NeQ}[c, 0] \&\& \text{LtQ}[m - n, 0] \&\& \text{IntegerQ}[n]))) \&\& (\text{SumSimplerQ}[m, 1] \|\| !\text{SumSimplerQ}[n, 1])$

Rubi steps

$$\begin{aligned}\int x^{-3-n}(a+bx)^n dx &= -\frac{x^{-2-n}(a+bx)^{1+n}}{a(2+n)} - \frac{b \int x^{-2-n}(a+bx)^n dx}{a(2+n)} \\ &= -\frac{x^{-2-n}(a+bx)^{1+n}}{a(2+n)} + \frac{bx^{-1-n}(a+bx)^{1+n}}{a^2(1+n)(2+n)}\end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 0.69

$$-\frac{x^{-n-2}(an+a-bx)(a+bx)^{n+1}}{a^2(n+1)(n+2)}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-3 - n)*(a + b*x)^n,x]

[Out] -((x^(-2 - n)*(a + a*n - b*x)*(a + b*x)^(1 + n))/(a^2*(1 + n)*(2 + n)))

fricas [A] time = 0.49, size = 64, normalized size = 1.10

$$\frac{(abnx^2 - b^2x^3 + (a^2n + a^2)x)(bx + a)^n x^{-n-3}}{a^2n^2 + 3a^2n + 2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-3-n)*(b*x+a)^n,x, algorithm="fricas")

[Out] -(a*b*n*x^2 - b^2*x^3 + (a^2*n + a^2)*x)*(b*x + a)^n*x^(-n - 3)/(a^2*n^2 + 3*a^2*n + 2*a^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n x^{-n-3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-3-n)*(b*x+a)^n,x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^(-n - 3), x)

maple [A] time = 0.00, size = 41, normalized size = 0.71

$$\frac{(an - bx + a)x^{-n-2}(bx + a)^{n+1}}{(n+2)(n+1)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(-3-n)*(b*x+a)^n,x)`

[Out] $-(b*x+a)^{(n+1)}*x^{(-2-n)}*(a*n-b*x+a)/(n+2)/(n+1)/a^2$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n x^{-n-3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(-3-n)*(b*x+a)^n,x, algorithm="maxima")`

[Out] `integrate((b*x + a)^n*x^(-n - 3), x)`

mupad [B] time = 0.50, size = 86, normalized size = 1.48

$$-(a + bx)^n \left(\frac{x(n+1)}{x^{n+3}(n^2+3n+2)} - \frac{b^2 x^3}{a^2 x^{n+3}(n^2+3n+2)} + \frac{bnx^2}{a x^{n+3}(n^2+3n+2)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^n/x^(n + 3),x)`

[Out] $-(a + b*x)^n*((x*(n + 1))/(x^(n + 3)*(3*n + n^2 + 2)) - (b^2*x^3)/(a^2*x^(n + 3)*(3*n + n^2 + 2))) + (b*n*x^2)/(a*x^(n + 3)*(3*n + n^2 + 2))$

sympy [A] time = 94.82, size = 323, normalized size = 5.57

$$\left\{ \begin{array}{l} -\frac{b^n}{2x^2} \\ \frac{a \log(x)}{a^3+a^2bx} - \frac{a \log\left(\frac{a}{b}+x\right)}{a^3+a^2bx} + \frac{a}{a^3+a^2bx} + \frac{bx \log(x)}{a^3+a^2bx} - \frac{bx \log\left(\frac{a}{b}+x\right)}{a^3+a^2bx} \\ -\frac{1}{ax} - \frac{b \log(x)}{a^2} + \frac{b \log\left(\frac{a}{b}+x\right)}{a^2} \\ -\frac{a^2n(a+bx)^n}{a^2n^2x^2x^n+3a^2nx^2x^n+2a^2x^2x^n} - \frac{a^2(a+bx)^n}{a^2n^2x^2x^n+3a^2nx^2x^n+2a^2x^2x^n} - \frac{abnx(a+bx)^n}{a^2n^2x^2x^n+3a^2nx^2x^n+2a^2x^2x^n} + \frac{b^2x^2(a+bx)^n}{a^2n^2x^2x^n+3a^2nx^2x^n+2a^2x^2x^n} \end{array} \right.$$

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Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(-3-n)*(b*x+a)**n,x)`

[Out] `Piecewise((-b**n/(2*x**2), Eq(a, 0)), (a*log(x)/(a**3 + a**2*b*x) - a*log(a/b + x)/(a**3 + a**2*b*x) + a/(a**3 + a**2*b*x) + b*x*log(x)/(a**3 + a**2*b`

```

*x) - b*x*log(a/b + x)/(a**3 + a**2*b*x), Eq(n, -2)), (-1/(a*x) - b*log(x)/
a**2 + b*log(a/b + x)/a**2, Eq(n, -1)), (-a**2*n*(a + b*x)**n/(a**2*n**2*x*
*2*x**n + 3*a**2*n*x**2*x**n + 2*a**2*x**2*x**n) - a**2*(a + b*x)**n/(a**2*
n**2*x**2*x**n + 3*a**2*n*x**2*x**n + 2*a**2*x**2*x**n) - a*b*n*x*(a + b*x)
**n/(a**2*n**2*x**2*x**n + 3*a**2*n*x**2*x**n + 2*a**2*x**2*x**n) + b**2*x*
*2*(a + b*x)**n/(a**2*n**2*x**2*x**n + 3*a**2*n*x**2*x**n + 2*a**2*x**2*x**
n), True))

```

3.755 $\int x^{2n-3(1+n)}(a+bx)^n dx$

Optimal. Leaf size=58

$$\frac{bx^{-n-1}(a+bx)^{n+1}}{a^2(n+1)(n+2)} - \frac{x^{-n-2}(a+bx)^{n+1}}{a(n+2)}$$

[Out] $-x^{(-2-n)}*(b*x+a)^{(1+n)}/a/(2+n)+b*x^{(-1-n)}*(b*x+a)^{(1+n)}/a^2/(n^2+3*n+2)$

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{bx^{-n-1}(a+bx)^{n+1}}{a^2(n+1)(n+2)} - \frac{x^{-n-2}(a+bx)^{n+1}}{a(n+2)}$$

Antiderivative was successfully verified.

[In] Int[x^(2*n - 3*(1 + n))*(a + b*x)^n, x]

[Out] $-((x^{(-2 - n)}*(a + b*x)^{(1 + n)})/(a*(2 + n))) + (b*x^{(-1 - n)}*(a + b*x)^{(1 + n)})/(a^2*(1 + n)*(2 + n))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int x^{2n-3(1+n)}(a+bx)^n dx = -\frac{x^{-2-n}(a+bx)^{1+n}}{a(2+n)} - \frac{b \int x^{-2-n}(a+bx)^n dx}{a(2+n)}$$

$$= -\frac{x^{-2-n}(a+bx)^{1+n}}{a(2+n)} + \frac{bx^{-1-n}(a+bx)^{1+n}}{a^2(1+n)(2+n)}$$

Mathematica [A] time = 0.00, size = 40, normalized size = 0.69

$$-\frac{x^{-n-2}(an+a-bx)(a+bx)^{n+1}}{a^2(n+1)(n+2)}$$

Antiderivative was successfully verified.

[In] Integrate[x^(2*n - 3*(1 + n))*(a + b*x)^n,x]

[Out] -((x^(-2 - n)*(a + a*n - b*x)*(a + b*x)^(1 + n))/(a^2*(1 + n)*(2 + n)))

fricas [A] time = 0.47, size = 64, normalized size = 1.10

$$\frac{(abnx^2 - b^2x^3 + (a^2n + a^2)x)(bx + a)^n x^{-n-3}}{a^2n^2 + 3a^2n + 2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-3-n)*(b*x+a)^n,x, algorithm="fricas")

[Out] -(a*b*n*x^2 - b^2*x^3 + (a^2*n + a^2)*x)*(b*x + a)^n*x^(-n - 3)/(a^2*n^2 + 3*a^2*n + 2*a^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n x^{-n-3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(-3-n)*(b*x+a)^n,x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^(-n - 3), x)

maple [A] time = 0.00, size = 41, normalized size = 0.71

$$\frac{(an - bx + a)x^{-n-2}(bx + a)^{n+1}}{(n+2)(n+1)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(-3-n)*(b*x+a)^n,x)`

[Out] $-(a*n-b*x+a)/(n+2)/(n+1)/a^2*x^{(-n-2)}*(b*x+a)^{(n+1)}$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n x^{-n-3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(-3-n)*(b*x+a)^n,x, algorithm="maxima")`

[Out] `integrate((b*x + a)^n*x^(-n - 3), x)`

mupad [B] time = 0.00, size = 86, normalized size = 1.48

$$-(a + bx)^n \left(\frac{x(n+1)}{x^{n+3}(n^2+3n+2)} - \frac{b^2 x^3}{a^2 x^{n+3}(n^2+3n+2)} + \frac{bnx^2}{ax^{n+3}(n^2+3n+2)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^n/x^(n + 3),x)`

[Out] $-(a + b*x)^n*((x*(n + 1))/(x^(n + 3)*(3*n + n^2 + 2)) - (b^2*x^3)/(a^2*x^(n + 3)*(3*n + n^2 + 2))) + (b*n*x^2)/(a*x^(n + 3)*(3*n + n^2 + 2))$

sympy [A] time = 94.49, size = 323, normalized size = 5.57

$$\left\{ \begin{array}{l} -\frac{b^n}{2x^2} \\ \frac{a \log(x)}{a^3+a^2bx} - \frac{a \log\left(\frac{a}{b}+x\right)}{a^3+a^2bx} + \frac{a}{a^3+a^2bx} + \frac{bx \log(x)}{a^3+a^2bx} - \frac{bx \log\left(\frac{a}{b}+x\right)}{a^3+a^2bx} \\ -\frac{1}{ax} - \frac{b \log(x)}{a^2} + \frac{b \log\left(\frac{a}{b}+x\right)}{a^2} \\ -\frac{a^2n(a+bx)^n}{a^2n^2x^2x^n+3a^2nx^2x^n+2a^2x^2x^n} - \frac{a^2(a+bx)^n}{a^2n^2x^2x^n+3a^2nx^2x^n+2a^2x^2x^n} - \frac{abnx(a+bx)^n}{a^2n^2x^2x^n+3a^2nx^2x^n+2a^2x^2x^n} + \frac{b^2x^2(a+bx)^n}{a^2n^2x^2x^n+3a^2nx^2x^n+2a^2x^2x^n} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**(-3-n)*(b*x+a)**n,x)`

[Out] `Piecewise((-b**n/(2*x**2), Eq(a, 0)), (a*log(x)/(a**3 + a**2*b*x) - a*log(a/b + x)/(a**3 + a**2*b*x) + a/(a**3 + a**2*b*x) + b*x*log(x)/(a**3 + a**2*b`

```

*x) - b*x*log(a/b + x)/(a**3 + a**2*b*x), Eq(n, -2)), (-1/(a*x) - b*log(x)/
a**2 + b*log(a/b + x)/a**2, Eq(n, -1)), (-a**2*n*(a + b*x)**n/(a**2*n**2*x*
**2*x**n + 3*a**2*n*x**2*x**n + 2*a**2*x**2*x**n) - a**2*(a + b*x)**n/(a**2*
n**2*x**2*x**n + 3*a**2*n*x**2*x**n + 2*a**2*x**2*x**n) - a*b*n*x*(a + b*x)
**n/(a**2*n**2*x**2*x**n + 3*a**2*n*x**2*x**n + 2*a**2*x**2*x**n) + b**2*x*
**2*(a + b*x)**n/(a**2*n**2*x**2*x**n + 3*a**2*n*x**2*x**n + 2*a**2*x**2*x**
n), True))

```

3.756 $\int x^3 \sqrt{cx^2} (a + bx) dx$

Optimal. Leaf size=35

$$\frac{1}{5}ax^4\sqrt{cx^2} + \frac{1}{6}bx^5\sqrt{cx^2}$$

[Out] $1/5*a*x^4*(c*x^2)^(1/2)+1/6*b*x^5*(c*x^2)^(1/2)$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{5}ax^4\sqrt{cx^2} + \frac{1}{6}bx^5\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*\text{Sqrt}[c*x^2]*(a + b*x), x]$

[Out] $(a*x^4*\text{Sqrt}[c*x^2])/5 + (b*x^5*\text{Sqrt}[c*x^2])/6$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3 \sqrt{cx^2} (a + bx) dx &= \frac{\sqrt{cx^2} \int x^4 (a + bx) dx}{x} \\ &= \frac{\sqrt{cx^2} \int (ax^4 + bx^5) dx}{x} \\ &= \frac{1}{5}ax^4\sqrt{cx^2} + \frac{1}{6}bx^5\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 0.69

$$\frac{1}{30}x^4\sqrt{cx^2}(6a + 5bx)$$

Antiderivative was successfully verified.

[In] Integrate[x^3*Sqrt[c*x^2]*(a + b*x), x]

[Out] (x^4*Sqrt[c*x^2]*(6*a + 5*b*x))/30

fricas [A] time = 0.42, size = 22, normalized size = 0.63

$$\frac{1}{30}(5bx^5 + 6ax^4)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)*(c*x^2)^(1/2), x, algorithm="fricas")

[Out] 1/30*(5*b*x^5 + 6*a*x^4)*sqrt(c*x^2)

giac [A] time = 0.89, size = 22, normalized size = 0.63

$$\frac{1}{30}(5bx^6\text{sgn}(x) + 6ax^5\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)*(c*x^2)^(1/2), x, algorithm="giac")

[Out] 1/30*(5*b*x^6*sgn(x) + 6*a*x^5*sgn(x))*sqrt(c)

maple [A] time = 0.01, size = 21, normalized size = 0.60

$$\frac{(5bx + 6a)\sqrt{cx^2}x^4}{30}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)*(c*x^2)^(1/2), x)

[Out] 1/30*x^4*(5*b*x+6*a)*(c*x^2)^(1/2)

maxima [A] time = 1.33, size = 33, normalized size = 0.94

$$\frac{(cx^2)^{\frac{3}{2}}bx^3}{6c} + \frac{(cx^2)^{\frac{3}{2}}ax^2}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(b*x+a)*(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $1/6*(c*x^2)^(3/2)*b*x^3/c + 1/5*(c*x^2)^(3/2)*a*x^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int x^3 \sqrt{cx^2} (a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(c*x^2)^(1/2)*(a + b*x),x)`

[Out] `int(x^3*(c*x^2)^(1/2)*(a + b*x), x)`

sympy [A] time = 0.43, size = 36, normalized size = 1.03

$$\frac{a\sqrt{c}x^4\sqrt{x^2}}{5} + \frac{b\sqrt{c}x^5\sqrt{x^2}}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(b*x+a)*(c*x**2)**(1/2),x)`

[Out] `a*sqrt(c)*x**4*sqrt(x**2)/5 + b*sqrt(c)*x**5*sqrt(x**2)/6`

3.757 $\int x^2 \sqrt{cx^2} (a + bx) dx$

Optimal. Leaf size=35

$$\frac{1}{4}ax^3\sqrt{cx^2} + \frac{1}{5}bx^4\sqrt{cx^2}$$

[Out] $1/4*a*x^3*(c*x^2)^{(1/2)}+1/5*b*x^4*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{4}ax^3\sqrt{cx^2} + \frac{1}{5}bx^4\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*\text{Sqrt}[c*x^2]*(a + b*x), x]$

[Out] $(a*x^3*\text{Sqrt}[c*x^2])/4 + (b*x^4*\text{Sqrt}[c*x^2])/5$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2 \sqrt{cx^2} (a + bx) dx &= \frac{\sqrt{cx^2} \int x^3 (a + bx) dx}{x} \\ &= \frac{\sqrt{cx^2} \int (ax^3 + bx^4) dx}{x} \\ &= \frac{1}{4}ax^3\sqrt{cx^2} + \frac{1}{5}bx^4\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 0.69

$$\frac{1}{20}x^3\sqrt{cx^2}(5a + 4bx)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*Sqrt[c*x^2]*(a + b*x), x]

[Out] (x^3*Sqrt[c*x^2]*(5*a + 4*b*x))/20

fricas [A] time = 0.43, size = 22, normalized size = 0.63

$$\frac{1}{20}(4bx^4 + 5ax^3)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)*(c*x^2)^(1/2), x, algorithm="fricas")

[Out] 1/20*(4*b*x^4 + 5*a*x^3)*sqrt(c*x^2)

giac [A] time = 1.03, size = 22, normalized size = 0.63

$$\frac{1}{20}(4bx^5\text{sgn}(x) + 5ax^4\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)*(c*x^2)^(1/2), x, algorithm="giac")

[Out] 1/20*(4*b*x^5*sgn(x) + 5*a*x^4*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 21, normalized size = 0.60

$$\frac{(4bx + 5a)\sqrt{cx^2}x^3}{20}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)*(c*x^2)^(1/2), x)

[Out] 1/20*x^3*(4*b*x+5*a)*(c*x^2)^(1/2)

maxima [A] time = 1.37, size = 31, normalized size = 0.89

$$\frac{(cx^2)^{\frac{3}{2}}bx^2}{5c} + \frac{(cx^2)^{\frac{3}{2}}ax}{4c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)*(c*x^2)^(1/2),x, algorithm="maxima")

[Out] 1/5*(c*x^2)^(3/2)*b*x^2/c + 1/4*(c*x^2)^(3/2)*a*x/c

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int x^2 \sqrt{c x^2} (a + b x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(c*x^2)^(1/2)*(a + b*x),x)

[Out] int(x^2*(c*x^2)^(1/2)*(a + b*x), x)

sympy [A] time = 0.34, size = 36, normalized size = 1.03

$$\frac{a\sqrt{c}x^3\sqrt{x^2}}{4} + \frac{b\sqrt{c}x^4\sqrt{x^2}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)*(c*x**2)**(1/2),x)

[Out] a*sqrt(c)*x**3*sqrt(x**2)/4 + b*sqrt(c)*x**4*sqrt(x**2)/5

3.758 $\int x\sqrt{cx^2} (a + bx) dx$

Optimal. Leaf size=35

$$\frac{1}{3}ax^2\sqrt{cx^2} + \frac{1}{4}bx^3\sqrt{cx^2}$$

[Out] $1/3*a*x^2*(c*x^2)^(1/2)+1/4*b*x^3*(c*x^2)^(1/2)$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {15, 43}

$$\frac{1}{3}ax^2\sqrt{cx^2} + \frac{1}{4}bx^3\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*\text{Sqrt}[c*x^2]*(a + b*x), x]$

[Out] $(a*x^2*\text{Sqrt}[c*x^2])/3 + (b*x^3*\text{Sqrt}[c*x^2])/4$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x\sqrt{cx^2} (a + bx) dx &= \frac{\sqrt{cx^2} \int x^2(a + bx) dx}{x} \\ &= \frac{\sqrt{cx^2} \int (ax^2 + bx^3) dx}{x} \\ &= \frac{1}{3}ax^2\sqrt{cx^2} + \frac{1}{4}bx^3\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 0.69

$$\frac{1}{12}x^2\sqrt{cx^2}(4a + 3bx)$$

Antiderivative was successfully verified.

[In] Integrate[x*Sqrt[c*x^2]*(a + b*x), x]

[Out] (x^2*Sqrt[c*x^2]*(4*a + 3*b*x))/12

fricas [A] time = 0.46, size = 22, normalized size = 0.63

$$\frac{1}{12}(3bx^3 + 4ax^2)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)*(c*x^2)^(1/2), x, algorithm="fricas")

[Out] 1/12*(3*b*x^3 + 4*a*x^2)*sqrt(c*x^2)

giac [A] time = 0.85, size = 22, normalized size = 0.63

$$\frac{1}{12}(3bx^4\text{sgn}(x) + 4ax^3\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)*(c*x^2)^(1/2), x, algorithm="giac")

[Out] 1/12*(3*b*x^4*sgn(x) + 4*a*x^3*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 21, normalized size = 0.60

$$\frac{(3bx + 4a)\sqrt{cx^2}x^2}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)*(c*x^2)^(1/2), x)

[Out] 1/12*x^2*(3*b*x+4*a)*(c*x^2)^(1/2)

maxima [A] time = 1.35, size = 28, normalized size = 0.80

$$\frac{(cx^2)^{\frac{3}{2}}bx}{4c} + \frac{(cx^2)^{\frac{3}{2}}a}{3c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)*(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $1/4*(c*x^2)^{(3/2)}*b*x/c + 1/3*(c*x^2)^{(3/2)}*a/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int x \sqrt{c x^2} (a + b x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(1/2)*(a + b*x),x)`

[Out] `int(x*(c*x^2)^(1/2)*(a + b*x), x)`

sympy [A] time = 0.27, size = 36, normalized size = 1.03

$$\frac{a\sqrt{c}x^2\sqrt{x^2}}{3} + \frac{b\sqrt{c}x^3\sqrt{x^2}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)*(c*x**2)**(1/2),x)`

[Out] `a*sqrt(c)*x**2*sqrt(x**2)/3 + b*sqrt(c)*x**3*sqrt(x**2)/4`

3.759 $\int \sqrt{cx^2} (a + bx) dx$

Optimal. Leaf size=33

$$\frac{1}{2}ax\sqrt{cx^2} + \frac{1}{3}bx^2\sqrt{cx^2}$$

[Out] $1/2*a*x*(c*x^2)^{(1/2)}+1/3*b*x^2*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {15, 43}

$$\frac{1}{2}ax\sqrt{cx^2} + \frac{1}{3}bx^2\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[c*x^2]*(a + b*x), x]`

[Out] $(a*x*\text{Sqrt}[c*x^2])/2 + (b*x^2*\text{Sqrt}[c*x^2])/3$

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rule 43

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])`

Rubi steps

$$\begin{aligned} \int \sqrt{cx^2} (a + bx) dx &= \frac{\sqrt{cx^2} \int x(a + bx) dx}{x} \\ &= \frac{\sqrt{cx^2} \int (ax + bx^2) dx}{x} \\ &= \frac{1}{2}ax\sqrt{cx^2} + \frac{1}{3}bx^2\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 0.67

$$\frac{1}{6}x\sqrt{cx^2}(3a + 2bx)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]*(a + b*x), x]

[Out] (x*Sqrt[c*x^2]*(3*a + 2*b*x))/6

fricas [A] time = 0.43, size = 20, normalized size = 0.61

$$\frac{1}{6}(2bx^2 + 3ax)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2), x, algorithm="fricas")

[Out] 1/6*(2*b*x^2 + 3*a*x)*sqrt(c*x^2)

giac [A] time = 1.05, size = 22, normalized size = 0.67

$$\frac{1}{6}(2bx^3\text{sgn}(x) + 3ax^2\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2), x, algorithm="giac")

[Out] 1/6*(2*b*x^3*sgn(x) + 3*a*x^2*sgn(x))*sqrt(c)

maple [A] time = 0.01, size = 19, normalized size = 0.58

$$\frac{(2bx + 3a)\sqrt{cx^2}x}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(c*x^2)^(1/2), x)

[Out] 1/6*x*(2*b*x+3*a)*(c*x^2)^(1/2)

maxima [A] time = 1.32, size = 25, normalized size = 0.76

$$\frac{1}{2}\sqrt{cx^2}ax + \frac{(cx^2)^{\frac{3}{2}}b}{3c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2),x, algorithm="maxima")

[Out] 1/2*sqrt(c*x^2)*a*x + 1/3*(c*x^2)^(3/2)*b/c

mupad [B] time = 0.54, size = 20, normalized size = 0.61

$$\frac{\sqrt{c} \left(2b \sqrt{x^6} + 3ax|x| \right)}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)*(a + b*x),x)

[Out] (c^(1/2)*(2*b*(x^6)^(1/2) + 3*a*x*abs(x)))/6

sympy [A] time = 0.22, size = 34, normalized size = 1.03

$$\frac{a\sqrt{c}x\sqrt{x^2}}{2} + \frac{b\sqrt{c}x^2\sqrt{x^2}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x**2)**(1/2),x)

[Out] a*sqrt(c)*x*sqrt(x**2)/2 + b*sqrt(c)*x**2*sqrt(x**2)/3

$$3.760 \quad \int \frac{\sqrt{cx^2}(a+bx)}{x} dx$$

Optimal. Leaf size=27

$$a\sqrt{cx^2} + \frac{1}{2}bx\sqrt{cx^2}$$

[Out] $a*(c*x^2)^{(1/2)}+1/2*b*x*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.056$, Rules used = {15}

$$a\sqrt{cx^2} + \frac{1}{2}bx\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x))/x,x]

[Out] a*Sqrt[c*x^2] + (b*x*Sqrt[c*x^2])/2

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2}(a+bx)}{x} dx &= \frac{\sqrt{cx^2} \int (a+bx) dx}{x} \\ &= a\sqrt{cx^2} + \frac{1}{2}bx\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 0.89

$$\frac{cx^2(2a+bx)}{2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x))/x,x]

[Out] (c*x^2*(2*a + b*x))/(2*Sqrt[c*x^2])

fricas [A] time = 0.47, size = 16, normalized size = 0.59

$$\frac{1}{2} \sqrt{cx^2} (bx + 2a)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x,x, algorithm="fricas")

[Out] 1/2*sqrt(c*x^2)*(b*x + 2*a)

giac [A] time = 1.09, size = 17, normalized size = 0.63

$$\frac{1}{2} (bx^2 + 2ax) \sqrt{c} \operatorname{sgn}(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x,x, algorithm="giac")

[Out] 1/2*(b*x^2 + 2*a*x)*sqrt(c)*sgn(x)

maple [A] time = 0.00, size = 17, normalized size = 0.63

$$\frac{(bx + 2a) \sqrt{cx^2}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(c*x^2)^(1/2)/x,x)

[Out] 1/2*(b*x+2*a)*(c*x^2)^(1/2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [B] time = 0.19, size = 14, normalized size = 0.52

$$\frac{\sqrt{c} |x| (2a + bx)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(1/2)*(a + b*x))/x,x)`

[Out] `(c^(1/2)*abs(x)*(2*a + b*x))/2`

sympy [A] time = 0.23, size = 29, normalized size = 1.07

$$a\sqrt{c}\sqrt{x^2} + \frac{b\sqrt{c}x\sqrt{x^2}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(c*x**2)**(1/2)/x,x)`

[Out] `a*sqrt(c)*sqrt(x**2) + b*sqrt(c)*x*sqrt(x**2)/2`

$$3.761 \quad \int \frac{\sqrt{cx^2}(a+bx)}{x^2} dx$$

Optimal. Leaf size=28

$$\frac{a\sqrt{cx^2} \log(x)}{x} + b\sqrt{cx^2}$$

[Out] b*(c*x^2)^(1/2)+a*ln(x)*(c*x^2)^(1/2)/x

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{a\sqrt{cx^2} \log(x)}{x} + b\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x))/x^2,x]

[Out] b*Sqrt[c*x^2] + (a*Sqrt[c*x^2]*Log[x])/x

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_)^(m_))*((c_.) + (d_.)*(x_)^(n_)), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2}(a+bx)}{x^2} dx &= \frac{\sqrt{cx^2} \int \frac{a+bx}{x} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(b + \frac{a}{x}\right) dx}{x} \\ &= b\sqrt{cx^2} + \frac{a\sqrt{cx^2} \log(x)}{x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 0.71

$$\frac{cx(a \log(x) + bx)}{\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x))/x^2,x]

[Out] (c*x*(b*x + a*Log[x]))/Sqrt[c*x^2]

fricas [A] time = 0.47, size = 19, normalized size = 0.68

$$\frac{\sqrt{cx^2} (bx + a \log(x))}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x^2,x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x + a*log(x))/x

giac [A] time = 0.92, size = 17, normalized size = 0.61

$$(bx \operatorname{sgn}(x) + a \log(|x|) \operatorname{sgn}(x)) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x^2,x, algorithm="giac")

[Out] (b*x*sgn(x) + a*log(abs(x))*sgn(x))*sqrt(c)

maple [A] time = 0.02, size = 20, normalized size = 0.71

$$\frac{\sqrt{cx^2} (a \ln(x) + bx)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(c*x^2)^(1/2)/x^2,x)

[Out] (c*x^2)^(1/2)/x*(a*ln(x)+b*x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x^2,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{\sqrt{cx^2} (a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(1/2)*(a + b*x))/x^2,x)

[Out] int(((c*x^2)^(1/2)*(a + b*x))/x^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x**2)**(1/2)/x**2,x)

[Out] Integral(sqrt(c*x**2)*(a + b*x)/x**2, x)

$$3.762 \quad \int \frac{\sqrt{cx^2}(a+bx)}{x^3} dx$$

Optimal. Leaf size=32

$$\frac{b\sqrt{cx^2} \log(x)}{x} - \frac{a\sqrt{cx^2}}{x^2}$$

[Out] $-a*(c*x^2)^{(1/2)}/x^2+b*\ln(x)*(c*x^2)^{(1/2)}/x$

Rubi [A] time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{b\sqrt{cx^2} \log(x)}{x} - \frac{a\sqrt{cx^2}}{x^2}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x))/x^3,x]

[Out] $-((a*\text{Sqrt}[c*x^2])/x^2) + (b*\text{Sqrt}[c*x^2]*\text{Log}[x])/x$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2}(a+bx)}{x^3} dx &= \frac{\sqrt{cx^2} \int \frac{a+bx}{x^2} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(\frac{a}{x^2} + \frac{b}{x}\right) dx}{x} \\ &= -\frac{a\sqrt{cx^2}}{x^2} + \frac{b\sqrt{cx^2} \log(x)}{x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 0.62

$$\frac{c(bx \log(x) - a)}{\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x))/x^3,x]

[Out] (c*(-a + b*x*Log[x]))/Sqrt[c*x^2]

fricas [A] time = 0.44, size = 20, normalized size = 0.62

$$\frac{\sqrt{cx^2}(bx \log(x) - a)}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x^3,x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x*log(x) - a)/x^2

giac [A] time = 1.10, size = 20, normalized size = 0.62

$$\left(b \log(|x|) \operatorname{sgn}(x) - \frac{a \operatorname{sgn}(x)}{x}\right) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x^3,x, algorithm="giac")

[Out] (b*log(abs(x))*sgn(x) - a*sgn(x)/x)*sqrt(c)

maple [A] time = 0.01, size = 21, normalized size = 0.66

$$\frac{\sqrt{cx^2}(bx \ln(x) - a)}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(c*x^2)^(1/2)/x^3,x)

[Out] (c*x^2)^(1/2)*(b*ln(x)*x-a)/x^2

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(c*x^2)^(1/2)/x^3,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{\sqrt{cx^2} (a + bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(1/2)*(a + b*x))/x^3,x)`

[Out] `int(((c*x^2)^(1/2)*(a + b*x))/x^3, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (a + bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(c*x**2)**(1/2)/x**3,x)`

[Out] `Integral(sqrt(c*x**2)*(a + b*x)/x**3, x)`

$$3.763 \quad \int \frac{\sqrt{cx^2}(a+bx)}{x^4} dx$$

Optimal. Leaf size=26

$$-\frac{\sqrt{cx^2}(a+bx)^2}{2ax^3}$$

[Out] $-1/2*(b*x+a)^2*(c*x^2)^{(1/2)}/x^3/a$

Rubi [A] time = 0.00, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 37}

$$-\frac{\sqrt{cx^2}(a+bx)^2}{2ax^3}$$

Antiderivative was successfully verified.

[In] `Int[(Sqrt[c*x^2]*(a + b*x))/x^4,x]`

[Out] $-(\text{Sqrt}[c*x^2]*(a + b*x)^2)/(2*a*x^3)$

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rule 37

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]`

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2}(a+bx)}{x^4} dx &= \frac{\sqrt{cx^2} \int \frac{a+bx}{x^3} dx}{x} \\ &= -\frac{\sqrt{cx^2}(a+bx)^2}{2ax^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 0.85

$$-\frac{\sqrt{cx^2}(a+2bx)}{2x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x))/x^4,x]

[Out] -1/2*(Sqrt[c*x^2]*(a + 2*b*x))/x^3

fricas [A] time = 0.43, size = 18, normalized size = 0.69

$$-\frac{\sqrt{cx^2}(2bx+a)}{2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x^4,x, algorithm="fricas")

[Out] -1/2*sqrt(c*x^2)*(2*b*x + a)/x^3

giac [A] time = 0.97, size = 19, normalized size = 0.73

$$-\frac{(2bx\operatorname{sgn}(x) + a\operatorname{sgn}(x))\sqrt{c}}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x^4,x, algorithm="giac")

[Out] -1/2*(2*b*x*sgn(x) + a*sgn(x))*sqrt(c)/x^2

maple [A] time = 0.00, size = 19, normalized size = 0.73

$$-\frac{(2bx+a)\sqrt{cx^2}}{2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(c*x^2)^(1/2)/x^4,x)

[Out] -1/2*(2*b*x+a)*(c*x^2)^(1/2)/x^3

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x^2)^(1/2)/x^4,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [B] time = 0.14, size = 28, normalized size = 1.08

$$-\frac{a\sqrt{c}x^2 + 2b\sqrt{c}x^3}{2x(x^2)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(1/2)*(a + b*x))/x^4,x)

[Out] -(a*c^(1/2)*x^2 + 2*b*c^(1/2)*x^3)/(2*x*(x^2)^(3/2))

sympy [A] time = 0.51, size = 36, normalized size = 1.38

$$-\frac{a\sqrt{c}\sqrt{x^2}}{2x^3} - \frac{b\sqrt{c}\sqrt{x^2}}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(c*x**2)**(1/2)/x**4,x)

[Out] -a*sqrt(c)*sqrt(x**2)/(2*x**3) - b*sqrt(c)*sqrt(x**2)/x**2

$$3.764 \quad \int x^3 (cx^2)^{3/2} (a + bx) dx$$

Optimal. Leaf size=37

$$\frac{1}{7}acx^6\sqrt{cx^2} + \frac{1}{8}bcx^7\sqrt{cx^2}$$

[Out] $1/7*a*c*x^6*(c*x^2)^{(1/2)}+1/8*b*c*x^7*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{7}acx^6\sqrt{cx^2} + \frac{1}{8}bcx^7\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*(c*x^2)^{(3/2)}*(a + b*x), x]$

[Out] $(a*c*x^6*\text{Sqrt}[c*x^2])/7 + (b*c*x^7*\text{Sqrt}[c*x^2])/8$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)]^{(m_.)}*((c_.) + (d_.)*(x_)]^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3 (cx^2)^{3/2} (a + bx) dx &= \frac{(c\sqrt{cx^2}) \int x^6 (a + bx) dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (ax^6 + bx^7) dx}{x} \\ &= \frac{1}{7}acx^6\sqrt{cx^2} + \frac{1}{8}bcx^7\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.65

$$\frac{1}{56}x^4 (cx^2)^{3/2} (8a + 7bx)$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(c*x^2)^(3/2)*(a + b*x), x]

[Out] (x^4*(c*x^2)^(3/2)*(8*a + 7*b*x))/56

fricas [A] time = 0.45, size = 24, normalized size = 0.65

$$\frac{1}{56} (7bcx^7 + 8acx^6) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^(3/2)*(b*x+a), x, algorithm="fricas")

[Out] 1/56*(7*b*c*x^7 + 8*a*c*x^6)*sqrt(c*x^2)

giac [A] time = 1.17, size = 22, normalized size = 0.59

$$\frac{1}{56} (7bx^8 \operatorname{sgn}(x) + 8ax^7 \operatorname{sgn}(x)) c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^(3/2)*(b*x+a), x, algorithm="giac")

[Out] 1/56*(7*b*x^8*sgn(x) + 8*a*x^7*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 21, normalized size = 0.57

$$\frac{(7bx + 8a)(cx^2)^{\frac{3}{2}} x^4}{56}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(c*x^2)^(3/2)*(b*x+a), x)

[Out] 1/56*x^4*(7*b*x+8*a)*(c*x^2)^(3/2)

maxima [A] time = 1.33, size = 33, normalized size = 0.89

$$\frac{(cx^2)^{\frac{5}{2}} bx^3}{8c} + \frac{(cx^2)^{\frac{5}{2}} ax^2}{7c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(c*x^2)^(3/2)*(b*x+a), x, algorithm="maxima")`

[Out] $1/8*(c*x^2)^{(5/2)}*b*x^3/c + 1/7*(c*x^2)^{(5/2)}*a*x^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int x^3 (c x^2)^{3/2} (a + b x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(c*x^2)^(3/2)*(a + b*x), x)`

[Out] `int(x^3*(c*x^2)^(3/2)*(a + b*x), x)`

sympy [A] time = 1.16, size = 36, normalized size = 0.97

$$\frac{ac^{\frac{3}{2}}x^4(x^2)^{\frac{3}{2}}}{7} + \frac{bc^{\frac{3}{2}}x^5(x^2)^{\frac{3}{2}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(c*x**2)**(3/2)*(b*x+a), x)`

[Out] `a*c**(3/2)*x**4*(x**2)**(3/2)/7 + b*c**(3/2)*x**5*(x**2)**(3/2)/8`

$$3.765 \quad \int x^2 (cx^2)^{3/2} (a + bx) dx$$

Optimal. Leaf size=37

$$\frac{1}{6}acx^5\sqrt{cx^2} + \frac{1}{7}bcx^6\sqrt{cx^2}$$

[Out] 1/6*a*c*x^5*(c*x^2)^(1/2)+1/7*b*c*x^6*(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{6}acx^5\sqrt{cx^2} + \frac{1}{7}bcx^6\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[x^2*(c*x^2)^(3/2)*(a + b*x), x]

[Out] (a*c*x^5*Sqrt[c*x^2])/6 + (b*c*x^6*Sqrt[c*x^2])/7

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2 (cx^2)^{3/2} (a + bx) dx &= \frac{(c\sqrt{cx^2}) \int x^5 (a + bx) dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (ax^5 + bx^6) dx}{x} \\ &= \frac{1}{6}acx^5\sqrt{cx^2} + \frac{1}{7}bcx^6\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.65

$$\frac{1}{42}x^3 (cx^2)^{3/2} (7a + 6bx)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(c*x^2)^(3/2)*(a + b*x), x]

[Out] (x^3*(c*x^2)^(3/2)*(7*a + 6*b*x))/42

fricas [A] time = 0.43, size = 24, normalized size = 0.65

$$\frac{1}{42} (6bcx^6 + 7acx^5) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(3/2)*(b*x+a), x, algorithm="fricas")

[Out] 1/42*(6*b*c*x^6 + 7*a*c*x^5)*sqrt(c*x^2)

giac [A] time = 0.93, size = 22, normalized size = 0.59

$$\frac{1}{42} (6bx^7 \operatorname{sgn}(x) + 7ax^6 \operatorname{sgn}(x)) c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(3/2)*(b*x+a), x, algorithm="giac")

[Out] 1/42*(6*b*x^7*sgn(x) + 7*a*x^6*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 21, normalized size = 0.57

$$\frac{(6bx + 7a)(cx^2)^{\frac{3}{2}} x^3}{42}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(c*x^2)^(3/2)*(b*x+a), x)

[Out] 1/42*x^3*(6*b*x+7*a)*(c*x^2)^(3/2)

maxima [A] time = 1.34, size = 31, normalized size = 0.84

$$\frac{(cx^2)^{\frac{5}{2}} bx^2}{7c} + \frac{(cx^2)^{\frac{5}{2}} ax}{6c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(3/2)*(b*x+a),x, algorithm="maxima")

[Out] 1/7*(c*x^2)^(5/2)*b*x^2/c + 1/6*(c*x^2)^(5/2)*a*x/c

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int x^2 (c x^2)^{3/2} (a + b x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(c*x^2)^(3/2)*(a + b*x),x)

[Out] int(x^2*(c*x^2)^(3/2)*(a + b*x), x)

sympy [A] time = 0.91, size = 36, normalized size = 0.97

$$\frac{a c^{\frac{3}{2}} x^3 (x^2)^{\frac{3}{2}}}{6} + \frac{b c^{\frac{3}{2}} x^4 (x^2)^{\frac{3}{2}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(c*x**2)**(3/2)*(b*x+a),x)

[Out] a*c**(3/2)*x**3*(x**2)**(3/2)/6 + b*c**(3/2)*x**4*(x**2)**(3/2)/7

$$3.766 \quad \int x (cx^2)^{3/2} (a + bx) dx$$

Optimal. Leaf size=37

$$\frac{1}{5}acx^4\sqrt{cx^2} + \frac{1}{6}bcx^5\sqrt{cx^2}$$

[Out] $1/5*a*c*x^4*(c*x^2)^{(1/2)}+1/6*b*c*x^5*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {15, 43}

$$\frac{1}{5}acx^4\sqrt{cx^2} + \frac{1}{6}bcx^5\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*(c*x^2)^{(3/2)}*(a + b*x), x]$

[Out] $(a*c*x^4*\text{Sqrt}[c*x^2])/5 + (b*c*x^5*\text{Sqrt}[c*x^2])/6$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[((a_*) + (b_*)*(x_))^{(m_*)}*((c_*) + (d_*)*(x_))^{(n_*)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x (cx^2)^{3/2} (a + bx) dx &= \frac{(c\sqrt{cx^2}) \int x^4 (a + bx) dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (ax^4 + bx^5) dx}{x} \\ &= \frac{1}{5}acx^4\sqrt{cx^2} + \frac{1}{6}bcx^5\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.65

$$\frac{1}{30}x^2 (cx^2)^{3/2} (6a + 5bx)$$

Antiderivative was successfully verified.

[In] Integrate[x*(c*x^2)^(3/2)*(a + b*x),x]

[Out] (x^2*(c*x^2)^(3/2)*(6*a + 5*b*x))/30

fricas [A] time = 0.42, size = 24, normalized size = 0.65

$$\frac{1}{30} (5bcx^5 + 6acx^4) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)*(b*x+a),x, algorithm="fricas")

[Out] 1/30*(5*b*c*x^5 + 6*a*c*x^4)*sqrt(c*x^2)

giac [A] time = 0.99, size = 22, normalized size = 0.59

$$\frac{1}{30} (5bx^6 \operatorname{sgn}(x) + 6ax^5 \operatorname{sgn}(x)) c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)*(b*x+a),x, algorithm="giac")

[Out] 1/30*(5*b*x^6*sgn(x) + 6*a*x^5*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 21, normalized size = 0.57

$$\frac{(5bx + 6a)(cx^2)^{\frac{3}{2}} x^2}{30}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(c*x^2)^(3/2)*(b*x+a),x)

[Out] 1/30*x^2*(5*b*x+6*a)*(c*x^2)^(3/2)

maxima [A] time = 1.35, size = 28, normalized size = 0.76

$$\frac{(cx^2)^{\frac{5}{2}} bx}{6c} + \frac{(cx^2)^{\frac{5}{2}} a}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x^2)^(3/2)*(b*x+a),x, algorithm="maxima")`

[Out] `1/6*(c*x^2)^(5/2)*b*x/c + 1/5*(c*x^2)^(5/2)*a/c`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int x (c x^2)^{3/2} (a + b x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(3/2)*(a + b*x),x)`

[Out] `int(x*(c*x^2)^(3/2)*(a + b*x), x)`

sympy [A] time = 0.73, size = 36, normalized size = 0.97

$$\frac{ac^{\frac{3}{2}}x^2(x^2)^{\frac{3}{2}}}{5} + \frac{bc^{\frac{3}{2}}x^3(x^2)^{\frac{3}{2}}}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x**2)**(3/2)*(b*x+a),x)`

[Out] `a*c**(3/2)*x**2*(x**2)**(3/2)/5 + b*c**(3/2)*x**3*(x**2)**(3/2)/6`

3.767 $\int (cx^2)^{3/2} (a + bx) dx$

Optimal. Leaf size=37

$$\frac{1}{4}acx^3\sqrt{cx^2} + \frac{1}{5}bcx^4\sqrt{cx^2}$$

[Out] $1/4*a*c*x^3*(c*x^2)^{(1/2)}+1/5*b*c*x^4*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {15, 43}

$$\frac{1}{4}acx^3\sqrt{cx^2} + \frac{1}{5}bcx^4\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}*(a + b*x), x]$

[Out] $(a*c*x^3*\text{Sqrt}[c*x^2])/4 + (b*c*x^4*\text{Sqrt}[c*x^2])/5$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_. + (b_.)*(x_)^{(m_.)})*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (cx^2)^{3/2} (a + bx) dx &= \frac{(c\sqrt{cx^2}) \int x^3(a + bx) dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (ax^3 + bx^4) dx}{x} \\ &= \frac{1}{4}acx^3\sqrt{cx^2} + \frac{1}{5}bcx^4\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 0.59

$$\frac{1}{20}x (cx^2)^{3/2} (5a + 4bx)$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)*(a + b*x),x]

[Out] (x*(c*x^2)^(3/2)*(5*a + 4*b*x))/20

fricas [A] time = 0.43, size = 24, normalized size = 0.65

$$\frac{1}{20} (4bcx^4 + 5acx^3) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a),x, algorithm="fricas")

[Out] 1/20*(4*b*c*x^4 + 5*a*c*x^3)*sqrt(c*x^2)

giac [A] time = 0.88, size = 22, normalized size = 0.59

$$\frac{1}{20} (4bx^5 \operatorname{sgn}(x) + 5ax^4 \operatorname{sgn}(x)) c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a),x, algorithm="giac")

[Out] 1/20*(4*b*x^5*sgn(x) + 5*a*x^4*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 19, normalized size = 0.51

$$\frac{(4bx + 5a)(cx^2)^{\frac{3}{2}} x}{20}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(b*x+a),x)

[Out] 1/20*x*(4*b*x+5*a)*(c*x^2)^(3/2)

maxima [A] time = 1.30, size = 25, normalized size = 0.68

$$\frac{1}{4} (cx^2)^{\frac{3}{2}} ax + \frac{(cx^2)^{\frac{5}{2}} b}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a),x, algorithm="maxima")

[Out] 1/4*(c*x^2)^(3/2)*a*x + 1/5*(c*x^2)^(5/2)*b/c

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int (cx^2)^{3/2} (a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(a + b*x),x)

[Out] int((c*x^2)^(3/2)*(a + b*x), x)

sympy [A] time = 0.56, size = 34, normalized size = 0.92

$$\frac{ac^{\frac{3}{2}}x(x^2)^{\frac{3}{2}}}{4} + \frac{bc^{\frac{3}{2}}x^2(x^2)^{\frac{3}{2}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)*(b*x+a),x)

[Out] a*c**(3/2)*x*(x**2)**(3/2)/4 + b*c**(3/2)*x**2*(x**2)**(3/2)/5

$$3.768 \quad \int \frac{(cx^2)^{3/2}(a+bx)}{x} dx$$

Optimal. Leaf size=37

$$\frac{1}{3}acx^2\sqrt{cx^2} + \frac{1}{4}bcx^3\sqrt{cx^2}$$

[Out] $1/3*a*c*x^2*(c*x^2)^{(1/2)}+1/4*b*c*x^3*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{3}acx^2\sqrt{cx^2} + \frac{1}{4}bcx^3\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}*(a + b*x))/x, x]$

[Out] $(a*c*x^2*\text{Sqrt}[c*x^2])/3 + (b*c*x^3*\text{Sqrt}[c*x^2])/4$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] :> \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)}*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] :> \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2}(a+bx)}{x} dx &= \frac{(c\sqrt{cx^2}) \int x^2(a+bx) dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (ax^2 + bx^3) dx}{x} \\ &= \frac{1}{3}acx^2\sqrt{cx^2} + \frac{1}{4}bcx^3\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 25, normalized size = 0.68

$$\frac{1}{12}cx^2\sqrt{cx^2}(4a + 3bx)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x))/x,x]

[Out] (c*x^2*Sqrt[c*x^2]*(4*a + 3*b*x))/12

fricas [A] time = 0.44, size = 24, normalized size = 0.65

$$\frac{1}{12}(3bcx^3 + 4acx^2)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)/x,x, algorithm="fricas")

[Out] 1/12*(3*b*c*x^3 + 4*a*c*x^2)*sqrt(c*x^2)

giac [A] time = 1.09, size = 22, normalized size = 0.59

$$\frac{1}{12}(3bx^4\text{sgn}(x) + 4ax^3\text{sgn}(x))c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)/x,x, algorithm="giac")

[Out] 1/12*(3*b*x^4*sgn(x) + 4*a*x^3*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 18, normalized size = 0.49

$$\frac{(3bx + 4a)(cx^2)^{\frac{3}{2}}}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(b*x+a)/x,x)

[Out] 1/12*(3*b*x+4*a)*(c*x^2)^(3/2)

maxima [A] time = 1.34, size = 22, normalized size = 0.59

$$\frac{1}{4}(cx^2)^{\frac{3}{2}}bx + \frac{1}{3}(cx^2)^{\frac{3}{2}}a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)/x,x, algorithm="maxima")

[Out] 1/4*(c*x^2)^(3/2)*b*x + 1/3*(c*x^2)^(3/2)*a

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(cx^2)^{3/2} (a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(3/2)*(a + b*x))/x,x)

[Out] int(((c*x^2)^(3/2)*(a + b*x))/x, x)

sympy [A] time = 0.58, size = 31, normalized size = 0.84

$$\frac{ac^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}{3} + \frac{bc^{\frac{3}{2}}x(x^2)^{\frac{3}{2}}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)*(b*x+a)/x,x)

[Out] a*c**(3/2)*(x**2)**(3/2)/3 + b*c**(3/2)*x*(x**2)**(3/2)/4

$$3.769 \quad \int \frac{(cx^2)^{3/2} (a+bx)}{x^2} dx$$

Optimal. Leaf size=35

$$\frac{1}{2}acx\sqrt{cx^2} + \frac{1}{3}bcx^2\sqrt{cx^2}$$

[Out] 1/2*a*c*x*(c*x^2)^(1/2)+1/3*b*c*x^2*(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{2}acx\sqrt{cx^2} + \frac{1}{3}bcx^2\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x))/x^2,x]

[Out] (a*c*x*Sqrt[c*x^2])/2 + (b*c*x^2*Sqrt[c*x^2])/3

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2} (a+bx)}{x^2} dx &= \frac{(c\sqrt{cx^2}) \int x(a+bx) dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (ax+bx^2) dx}{x} \\ &= \frac{1}{2}acx\sqrt{cx^2} + \frac{1}{3}bcx^2\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 23, normalized size = 0.66

$$\frac{1}{6}cx\sqrt{cx^2}(3a + 2bx)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x))/x^2,x]

[Out] (c*x*Sqrt[c*x^2]*(3*a + 2*b*x))/6

fricas [A] time = 0.45, size = 22, normalized size = 0.63

$$\frac{1}{6}(2bcx^2 + 3acx)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)/x^2,x, algorithm="fricas")

[Out] 1/6*(2*b*c*x^2 + 3*a*c*x)*sqrt(c*x^2)

giac [A] time = 1.08, size = 22, normalized size = 0.63

$$\frac{1}{6}(2bx^3\text{sgn}(x) + 3ax^2\text{sgn}(x))c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)/x^2,x, algorithm="giac")

[Out] 1/6*(2*b*x^3*sgn(x) + 3*a*x^2*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 21, normalized size = 0.60

$$\frac{(2bx + 3a)(cx^2)^{\frac{3}{2}}}{6x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(b*x+a)/x^2,x)

[Out] 1/6/x*(2*b*x+3*a)*(c*x^2)^(3/2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)/x^2,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [B] time = 0.27, size = 20, normalized size = 0.57

$$\frac{c^{3/2} \left(2b \sqrt{x^6} + 3ax|x| \right)}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(3/2)*(a + b*x))/x^2,x)

[Out] (c^(3/2)*(2*b*(x^6)^(1/2) + 3*a*x*abs(x)))/6

sympy [A] time = 0.57, size = 31, normalized size = 0.89

$$\frac{ac^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}{2x} + \frac{bc^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)*(b*x+a)/x**2,x)

[Out] a*c**(3/2)*(x**2)**(3/2)/(2*x) + b*c**(3/2)*(x**2)**(3/2)/3

$$3.770 \quad \int \frac{(cx^2)^{3/2} (a+bx)}{x^3} dx$$

Optimal. Leaf size=29

$$ac\sqrt{cx^2} + \frac{1}{2}bcx\sqrt{cx^2}$$

[Out] a*c*(c*x^2)^(1/2)+1/2*b*c*x*(c*x^2)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.056$, Rules used = {15}

$$ac\sqrt{cx^2} + \frac{1}{2}bcx\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x))/x^3,x]

[Out] a*c*Sqrt[c*x^2] + (b*c*x*Sqrt[c*x^2])/2

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2} (a+bx)}{x^3} dx &= \frac{(c\sqrt{cx^2}) \int (a+bx) dx}{x} \\ &= ac\sqrt{cx^2} + \frac{1}{2}bcx\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 21, normalized size = 0.72

$$\frac{1}{2}c\sqrt{cx^2} (2a + bx)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x))/x^3,x]

[Out] $(c\sqrt{c x^2} (2a + b x))/2$

fricas [A] time = 0.43, size = 18, normalized size = 0.62

$$\frac{1}{2} (bcx + 2ac)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)*(b*x+a)/x^3,x, algorithm="fricas")`

[Out] $1/2*(b*c*x + 2*a*c)*\text{sqrt}(c*x^2)$

giac [A] time = 0.99, size = 17, normalized size = 0.59

$$\frac{1}{2} (bx^2 + 2ax)c^{\frac{3}{2}}\text{sgn}(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)*(b*x+a)/x^3,x, algorithm="giac")`

[Out] $1/2*(b*x^2 + 2*a*x)*c^{(3/2)}*\text{sgn}(x)$

maple [A] time = 0.00, size = 20, normalized size = 0.69

$$\frac{(bx + 2a)(cx^2)^{\frac{3}{2}}}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)*(b*x+a)/x^3,x)`

[Out] $1/2/x^2*(b*x+2*a)*(c*x^2)^{(3/2)}$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)*(b*x+a)/x^3,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [B] time = 0.22, size = 14, normalized size = 0.48

$$\frac{c^{3/2} |x| (2a + bx)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(3/2)*(a + b*x))/x^3,x)`

[Out] `(c^(3/2)*abs(x)*(2*a + b*x))/2`

sympy [A] time = 0.74, size = 32, normalized size = 1.10

$$\frac{ac^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}{x^2} + \frac{bc^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}{2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(3/2)*(b*x+a)/x**3,x)`

[Out] `a*c**(3/2)*(x**2)**(3/2)/x**2 + b*c**(3/2)*(x**2)**(3/2)/(2*x)`

$$3.771 \quad \int \frac{(cx^2)^{3/2} (a+bx)}{x^4} dx$$

Optimal. Leaf size=30

$$\frac{ac\sqrt{cx^2} \log(x)}{x} + bc\sqrt{cx^2}$$

[Out] b*c*(c*x^2)^(1/2)+a*c*ln(x)*(c*x^2)^(1/2)/x

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{ac\sqrt{cx^2} \log(x)}{x} + bc\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x))/x^4,x]

[Out] b*c*Sqrt[c*x^2] + (a*c*Sqrt[c*x^2]*Log[x])/x

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_)^(m_.))*((c_.) + (d_.)*(x_)^(n_.)), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2} (a + bx)}{x^4} dx &= \frac{(c\sqrt{cx^2}) \int \frac{a+bx}{x} dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (b + \frac{a}{x}) dx}{x} \\ &= bc\sqrt{cx^2} + \frac{ac\sqrt{cx^2} \log(x)}{x} \end{aligned}$$

Mathematica [A] time = 0.00, size = 21, normalized size = 0.70

$$\frac{(cx^2)^{3/2} (a \log(x) + bx)}{x^3}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x))/x^4,x]

[Out] ((c*x^2)^(3/2)*(b*x + a*Log[x]))/x^3

fricas [A] time = 0.46, size = 21, normalized size = 0.70

$$\frac{(bcx + ac \log(x))\sqrt{cx^2}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)/x^4,x, algorithm="fricas")

[Out] (b*c*x + a*c*log(x))*sqrt(c*x^2)/x

giac [A] time = 0.96, size = 17, normalized size = 0.57

$$(bx\operatorname{sgn}(x) + a \log(|x|) \operatorname{sgn}(x))c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)/x^4,x, algorithm="giac")

[Out] (b*x*sgn(x) + a*log(abs(x))*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 20, normalized size = 0.67

$$\frac{(cx^2)^{\frac{3}{2}} (a \ln(x) + bx)}{x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)*(b*x+a)/x^4,x)`

[Out] `(c*x^2)^(3/2)/x^3*(a*ln(x)+b*x)`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)*(b*x+a)/x^4,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(cx^2)^{3/2} (a + bx)}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(3/2)*(a + b*x))/x^4,x)`

[Out] `int(((c*x^2)^(3/2)*(a + b*x))/x^4, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (a + bx)}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(3/2)*(b*x+a)/x**4,x)`

[Out] `Integral((c*x**2)**(3/2)*(a + b*x)/x**4, x)`

$$3.772 \quad \int x^3 (cx^2)^{5/2} (a + bx) dx$$

Optimal. Leaf size=41

$$\frac{1}{9}ac^2x^8\sqrt{cx^2} + \frac{1}{10}bc^2x^9\sqrt{cx^2}$$

[Out] $1/9*a*c^2*x^8*(c*x^2)^{(1/2)}+1/10*b*c^2*x^9*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{9}ac^2x^8\sqrt{cx^2} + \frac{1}{10}bc^2x^9\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*(c*x^2)^{(5/2)}*(a + b*x), x]$

[Out] $(a*c^2*x^8*\text{Sqrt}[c*x^2])/9 + (b*c^2*x^9*\text{Sqrt}[c*x^2])/10$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_*) + (b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3 (cx^2)^{5/2} (a + bx) dx &= \frac{(c^2\sqrt{cx^2}) \int x^8 (a + bx) dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (ax^8 + bx^9) dx}{x} \\ &= \frac{1}{9}ac^2x^8\sqrt{cx^2} + \frac{1}{10}bc^2x^9\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.59

$$\frac{1}{90}x^4 (cx^2)^{5/2} (10a + 9bx)$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(c*x^2)^(5/2)*(a + b*x), x]

[Out] (x^4*(c*x^2)^(5/2)*(10*a + 9*b*x))/90

fricas [A] time = 0.43, size = 28, normalized size = 0.68

$$\frac{1}{90} (9bc^2x^9 + 10ac^2x^8)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^(5/2)*(b*x+a), x, algorithm="fricas")

[Out] 1/90*(9*b*c^2*x^9 + 10*a*c^2*x^8)*sqrt(c*x^2)

giac [A] time = 0.97, size = 28, normalized size = 0.68

$$\frac{1}{90} (9bc^2x^{10}\text{sgn}(x) + 10ac^2x^9\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^(5/2)*(b*x+a), x, algorithm="giac")

[Out] 1/90*(9*b*c^2*x^10*sgn(x) + 10*a*c^2*x^9*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$\frac{(9bx + 10a)(cx^2)^{\frac{5}{2}}x^4}{90}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(c*x^2)^(5/2)*(b*x+a), x)

[Out] 1/90*x^4*(9*b*x+10*a)*(c*x^2)^(5/2)

maxima [A] time = 1.24, size = 33, normalized size = 0.80

$$\frac{(cx^2)^{\frac{7}{2}}bx^3}{10c} + \frac{(cx^2)^{\frac{7}{2}}ax^2}{9c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(c*x^2)^(5/2)*(b*x+a),x, algorithm="maxima")`

[Out] `1/10*(c*x^2)^(7/2)*b*x^3/c + 1/9*(c*x^2)^(7/2)*a*x^2/c`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^3 (c x^2)^{5/2} (a + b x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(c*x^2)^(5/2)*(a + b*x),x)`

[Out] `int(x^3*(c*x^2)^(5/2)*(a + b*x), x)`

sympy [A] time = 2.54, size = 36, normalized size = 0.88

$$\frac{ac^{\frac{5}{2}}x^4(x^2)^{\frac{5}{2}}}{9} + \frac{bc^{\frac{5}{2}}x^5(x^2)^{\frac{5}{2}}}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(c*x**2)**(5/2)*(b*x+a),x)`

[Out] `a*c**(5/2)*x**4*(x**2)**(5/2)/9 + b*c**(5/2)*x**5*(x**2)**(5/2)/10`

$$3.773 \quad \int x^2 (cx^2)^{5/2} (a + bx) dx$$

Optimal. Leaf size=41

$$\frac{1}{8}ac^2x^7\sqrt{cx^2} + \frac{1}{9}bc^2x^8\sqrt{cx^2}$$

[Out] $1/8*a*c^2*x^7*(c*x^2)^{(1/2)}+1/9*b*c^2*x^8*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{8}ac^2x^7\sqrt{cx^2} + \frac{1}{9}bc^2x^8\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*(c*x^2)^{(5/2)}*(a + b*x), x]$

[Out] $(a*c^2*x^7*\text{Sqrt}[c*x^2])/8 + (b*c^2*x^8*\text{Sqrt}[c*x^2])/9$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_*) + (b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2 (cx^2)^{5/2} (a + bx) dx &= \frac{(c^2\sqrt{cx^2}) \int x^7(a + bx) dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (ax^7 + bx^8) dx}{x} \\ &= \frac{1}{8}ac^2x^7\sqrt{cx^2} + \frac{1}{9}bc^2x^8\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.59

$$\frac{1}{72}x^3 (cx^2)^{5/2} (9a + 8bx)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(c*x^2)^(5/2)*(a + b*x), x]

[Out] (x^3*(c*x^2)^(5/2)*(9*a + 8*b*x))/72

fricas [A] time = 0.45, size = 28, normalized size = 0.68

$$\frac{1}{72} (8bc^2x^8 + 9ac^2x^7)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(5/2)*(b*x+a), x, algorithm="fricas")

[Out] 1/72*(8*b*c^2*x^8 + 9*a*c^2*x^7)*sqrt(c*x^2)

giac [A] time = 0.80, size = 28, normalized size = 0.68

$$\frac{1}{72} (8bc^2x^9\text{sgn}(x) + 9ac^2x^8\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(5/2)*(b*x+a), x, algorithm="giac")

[Out] 1/72*(8*b*c^2*x^9*sgn(x) + 9*a*c^2*x^8*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$\frac{(8bx + 9a)(cx^2)^{\frac{5}{2}}x^3}{72}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(c*x^2)^(5/2)*(b*x+a), x)

[Out] 1/72*x^3*(8*b*x+9*a)*(c*x^2)^(5/2)

maxima [A] time = 1.30, size = 31, normalized size = 0.76

$$\frac{(cx^2)^{\frac{7}{2}}bx^2}{9c} + \frac{(cx^2)^{\frac{7}{2}}ax}{8c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(5/2)*(b*x+a),x, algorithm="maxima")

[Out] 1/9*(c*x^2)^(7/2)*b*x^2/c + 1/8*(c*x^2)^(7/2)*a*x/c

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^2 (c x^2)^{5/2} (a + b x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(c*x^2)^(5/2)*(a + b*x),x)

[Out] int(x^2*(c*x^2)^(5/2)*(a + b*x), x)

sympy [A] time = 2.10, size = 36, normalized size = 0.88

$$\frac{ac^{\frac{5}{2}}x^3(x^2)^{\frac{5}{2}}}{8} + \frac{bc^{\frac{5}{2}}x^4(x^2)^{\frac{5}{2}}}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(c*x**2)**(5/2)*(b*x+a),x)

[Out] a*c**(5/2)*x**3*(x**2)**(5/2)/8 + b*c**(5/2)*x**4*(x**2)**(5/2)/9

$$3.774 \quad \int x (cx^2)^{5/2} (a + bx) dx$$

Optimal. Leaf size=41

$$\frac{1}{7}ac^2x^6\sqrt{cx^2} + \frac{1}{8}bc^2x^7\sqrt{cx^2}$$

[Out] $1/7*a*c^2*x^6*(c*x^2)^{(1/2)}+1/8*b*c^2*x^7*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {15, 43}

$$\frac{1}{7}ac^2x^6\sqrt{cx^2} + \frac{1}{8}bc^2x^7\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*(c*x^2)^{(5/2)}*(a + b*x), x]$

[Out] $(a*c^2*x^6*\text{Sqrt}[c*x^2])/7 + (b*c^2*x^7*\text{Sqrt}[c*x^2])/8$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_*) + (b_*)*(x_)]^{(m_)*((c_*) + (d_*)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x (cx^2)^{5/2} (a + bx) dx &= \frac{(c^2\sqrt{cx^2}) \int x^6(a + bx) dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (ax^6 + bx^7) dx}{x} \\ &= \frac{1}{7}ac^2x^6\sqrt{cx^2} + \frac{1}{8}bc^2x^7\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.59

$$\frac{1}{56}x^2 (cx^2)^{5/2} (8a + 7bx)$$

Antiderivative was successfully verified.

[In] Integrate[x*(c*x^2)^(5/2)*(a + b*x), x]

[Out] (x^2*(c*x^2)^(5/2)*(8*a + 7*b*x))/56

fricas [A] time = 0.42, size = 28, normalized size = 0.68

$$\frac{1}{56} (7bc^2x^7 + 8ac^2x^6) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(5/2)*(b*x+a), x, algorithm="fricas")

[Out] 1/56*(7*b*c^2*x^7 + 8*a*c^2*x^6)*sqrt(c*x^2)

giac [A] time = 1.03, size = 28, normalized size = 0.68

$$\frac{1}{56} (7bc^2x^8 \operatorname{sgn}(x) + 8ac^2x^7 \operatorname{sgn}(x)) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(5/2)*(b*x+a), x, algorithm="giac")

[Out] 1/56*(7*b*c^2*x^8*sgn(x) + 8*a*c^2*x^7*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$\frac{(7bx + 8a)(cx^2)^{\frac{5}{2}}x^2}{56}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(c*x^2)^(5/2)*(b*x+a), x)

[Out] 1/56*x^2*(7*b*x+8*a)*(c*x^2)^(5/2)

maxima [A] time = 1.35, size = 28, normalized size = 0.68

$$\frac{(cx^2)^{\frac{7}{2}}bx}{8c} + \frac{(cx^2)^{\frac{7}{2}}a}{7c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x^2)^(5/2)*(b*x+a),x, algorithm="maxima")`

[Out] $1/8*(c*x^2)^{(7/2)}*b*x/c + 1/7*(c*x^2)^{(7/2)}*a/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x (c x^2)^{5/2} (a + b x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(5/2)*(a + b*x),x)`

[Out] `int(x*(c*x^2)^(5/2)*(a + b*x), x)`

sympy [A] time = 1.74, size = 36, normalized size = 0.88

$$\frac{ac^{\frac{5}{2}}x^2(x^2)^{\frac{5}{2}}}{7} + \frac{bc^{\frac{5}{2}}x^3(x^2)^{\frac{5}{2}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x**2)**(5/2)*(b*x+a),x)`

[Out] `a*c**(5/2)*x**2*(x**2)**(5/2)/7 + b*c**(5/2)*x**3*(x**2)**(5/2)/8`

3.775 $\int (cx^2)^{5/2} (a + bx) dx$

Optimal. Leaf size=41

$$\frac{1}{6}ac^2x^5\sqrt{cx^2} + \frac{1}{7}bc^2x^6\sqrt{cx^2}$$

[Out] $1/6*a*c^2*x^5*(c*x^2)^{(1/2)}+1/7*b*c^2*x^6*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {15, 43}

$$\frac{1}{6}ac^2x^5\sqrt{cx^2} + \frac{1}{7}bc^2x^6\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(5/2)}*(a + b*x), x]$

[Out] $(a*c^2*x^5*\text{Sqrt}[c*x^2])/6 + (b*c^2*x^6*\text{Sqrt}[c*x^2])/7$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (cx^2)^{5/2} (a + bx) dx &= \frac{(c^2\sqrt{cx^2}) \int x^5(a + bx) dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (ax^5 + bx^6) dx}{x} \\ &= \frac{1}{6}ac^2x^5\sqrt{cx^2} + \frac{1}{7}bc^2x^6\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 0.54

$$\frac{1}{42}x(cx^2)^{5/2}(7a+6bx)$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)*(a + b*x),x]

[Out] (x*(c*x^2)^(5/2)*(7*a + 6*b*x))/42

fricas [A] time = 0.43, size = 28, normalized size = 0.68

$$\frac{1}{42}(6bc^2x^6 + 7ac^2x^5)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a),x, algorithm="fricas")

[Out] 1/42*(6*b*c^2*x^6 + 7*a*c^2*x^5)*sqrt(c*x^2)

giac [A] time = 0.95, size = 28, normalized size = 0.68

$$\frac{1}{42}(6bc^2x^7\text{sgn}(x) + 7ac^2x^6\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a),x, algorithm="giac")

[Out] 1/42*(6*b*c^2*x^7*sgn(x) + 7*a*c^2*x^6*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 19, normalized size = 0.46

$$\frac{(6bx + 7a)(cx^2)^{\frac{5}{2}}x}{42}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a),x)

[Out] 1/42*x*(6*b*x+7*a)*(c*x^2)^(5/2)

maxima [A] time = 1.34, size = 25, normalized size = 0.61

$$\frac{1}{6}(cx^2)^{\frac{5}{2}}ax + \frac{(cx^2)^{\frac{7}{2}}b}{7c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a),x, algorithm="maxima")

[Out] 1/6*(c*x^2)^(5/2)*a*x + 1/7*(c*x^2)^(7/2)*b/c

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (cx^2)^{5/2} (a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(a + b*x),x)

[Out] int((c*x^2)^(5/2)*(a + b*x), x)

sympy [A] time = 1.41, size = 34, normalized size = 0.83

$$\frac{ac^{\frac{5}{2}}x(x^2)^{\frac{5}{2}}}{6} + \frac{bc^{\frac{5}{2}}x^2(x^2)^{\frac{5}{2}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a),x)

[Out] a*c**(5/2)*x*(x**2)**(5/2)/6 + b*c**(5/2)*x**2*(x**2)**(5/2)/7

$$3.776 \quad \int \frac{(cx^2)^{5/2} (a+bx)}{x} dx$$

Optimal. Leaf size=41

$$\frac{1}{5}ac^2x^4\sqrt{cx^2} + \frac{1}{6}bc^2x^5\sqrt{cx^2}$$

[Out] $1/5*a*c^2*x^4*(c*x^2)^{(1/2)}+1/6*b*c^2*x^5*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{5}ac^2x^4\sqrt{cx^2} + \frac{1}{6}bc^2x^5\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(5/2)}*(a + b*x))/x, x]$

[Out] $(a*c^2*x^4*\text{Sqrt}[c*x^2])/5 + (b*c^2*x^5*\text{Sqrt}[c*x^2])/6$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] :> \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\amp; \text{!IntegerQ}[m]$

Rule 43

$\text{Int}[(a_*) + (b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}), x_Symbol] :> \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\amp; \text{NeQ}[b*c - a*d, 0] \&\amp; \text{IGtQ}[m, 0] \&\amp; (\text{!IntegerQ}[n] \mid\mid (\text{EqQ}[c, 0] \&\amp; \text{LeQ}[7*m + 4*n + 4, 0]) \mid\mid \text{LtQ}[9*m + 5*(n + 1), 0] \mid\mid \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)}{x} dx &= \frac{(c^2\sqrt{cx^2}) \int x^4(a+bx) dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (ax^4 + bx^5) dx}{x} \\ &= \frac{1}{5}ac^2x^4\sqrt{cx^2} + \frac{1}{6}bc^2x^5\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 25, normalized size = 0.61

$$\frac{1}{30}cx^2 (cx^2)^{3/2} (6a + 5bx)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x))/x,x]

[Out] (c*x^2*(c*x^2)^(3/2)*(6*a + 5*b*x))/30

fricas [A] time = 0.47, size = 28, normalized size = 0.68

$$\frac{1}{30} (5bc^2x^5 + 6ac^2x^4)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)/x,x, algorithm="fricas")

[Out] 1/30*(5*b*c^2*x^5 + 6*a*c^2*x^4)*sqrt(c*x^2)

giac [A] time = 1.07, size = 28, normalized size = 0.68

$$\frac{1}{30} (5bc^2x^6\text{sgn}(x) + 6ac^2x^5\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)/x,x, algorithm="giac")

[Out] 1/30*(5*b*c^2*x^6*sgn(x) + 6*a*c^2*x^5*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 18, normalized size = 0.44

$$\frac{(5bx + 6a)(cx^2)^{\frac{5}{2}}}{30}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)/x,x)

[Out] 1/30*(5*b*x+6*a)*(c*x^2)^(5/2)

maxima [A] time = 1.40, size = 22, normalized size = 0.54

$$\frac{1}{6} (cx^2)^{\frac{5}{2}} bx + \frac{1}{5} (cx^2)^{\frac{5}{2}} a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(5/2)*(b*x+a)/x,x, algorithm="maxima")`

[Out] $1/6*(c*x^2)^{(5/2)}*b*x + 1/5*(c*x^2)^{(5/2)}*a$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(c x^2)^{5/2} (a + b x)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(5/2)*(a + b*x))/x,x)`

[Out] `int(((c*x^2)^(5/2)*(a + b*x))/x, x)`

sympy [A] time = 1.43, size = 31, normalized size = 0.76

$$\frac{ac^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}{5} + \frac{bc^{\frac{5}{2}}x(x^2)^{\frac{5}{2}}}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(5/2)*(b*x+a)/x,x)`

[Out] `a*c**(5/2)*(x**2)**(5/2)/5 + b*c**(5/2)*x*(x**2)**(5/2)/6`

$$3.777 \quad \int \frac{(cx^2)^{5/2} (a+bx)}{x^2} dx$$

Optimal. Leaf size=41

$$\frac{1}{4}ac^2x^3\sqrt{cx^2} + \frac{1}{5}bc^2x^4\sqrt{cx^2}$$

[Out] 1/4*a*c^2*x^3*(c*x^2)^(1/2)+1/5*b*c^2*x^4*(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{4}ac^2x^3\sqrt{cx^2} + \frac{1}{5}bc^2x^4\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x))/x^2,x]

[Out] (a*c^2*x^3*Sqrt[c*x^2])/4 + (b*c^2*x^4*Sqrt[c*x^2])/5

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)}{x^2} dx &= \frac{(c^2\sqrt{cx^2}) \int x^3(a+bx) dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (ax^3 + bx^4) dx}{x} \\ &= \frac{1}{4}ac^2x^3\sqrt{cx^2} + \frac{1}{5}bc^2x^4\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 23, normalized size = 0.56

$$\frac{1}{20}cx(cx^2)^{3/2}(5a+4bx)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x))/x^2,x]

[Out] (c*x*(c*x^2)^(3/2)*(5*a + 4*b*x))/20

fricas [A] time = 0.40, size = 28, normalized size = 0.68

$$\frac{1}{20}(4bc^2x^4 + 5ac^2x^3)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)/x^2,x, algorithm="fricas")

[Out] 1/20*(4*b*c^2*x^4 + 5*a*c^2*x^3)*sqrt(c*x^2)

giac [A] time = 1.10, size = 28, normalized size = 0.68

$$\frac{1}{20}(4bc^2x^5\text{sgn}(x) + 5ac^2x^4\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)/x^2,x, algorithm="giac")

[Out] 1/20*(4*b*c^2*x^5*sgn(x) + 5*a*c^2*x^4*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$\frac{(4bx + 5a)(cx^2)^{\frac{5}{2}}}{20x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)/x^2,x)

[Out] 1/20/x*(4*b*x+5*a)*(c*x^2)^(5/2)

maxima [A] time = 1.28, size = 24, normalized size = 0.59

$$\frac{1}{5}(cx^2)^{\frac{5}{2}}b + \frac{(cx^2)^{\frac{5}{2}}a}{4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)/x^2,x, algorithm="maxima")

[Out] 1/5*(c*x^2)^(5/2)*b + 1/4*(c*x^2)^(5/2)*a/x

mupad [B] time = 0.28, size = 25, normalized size = 0.61

$$\frac{c^{5/2} \left(4b \sqrt{x^{10}} + 5a x^3 \sqrt{x^2} \right)}{20}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(5/2)*(a + b*x))/x^2,x)

[Out] (c^(5/2)*(4*b*(x^10)^(1/2) + 5*a*x^3*(x^2)^(1/2)))/20

sympy [A] time = 1.53, size = 31, normalized size = 0.76

$$\frac{ac^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{4x} + \frac{bc^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a)/x**2,x)

[Out] a*c**(5/2)*(x**2)**(5/2)/(4*x) + b*c**(5/2)*(x**2)**(5/2)/5

$$3.778 \quad \int \frac{(cx^2)^{5/2} (a+bx)}{x^3} dx$$

Optimal. Leaf size=41

$$\frac{1}{3}ac^2x^2\sqrt{cx^2} + \frac{1}{4}bc^2x^3\sqrt{cx^2}$$

[Out] $1/3*a*c^2*x^2*(c*x^2)^{(1/2)}+1/4*b*c^2*x^3*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{3}ac^2x^2\sqrt{cx^2} + \frac{1}{4}bc^2x^3\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(5/2)}*(a + b*x))/x^3, x]$

[Out] $(a*c^2*x^2*\text{Sqrt}[c*x^2])/3 + (b*c^2*x^3*\text{Sqrt}[c*x^2])/4$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] :> \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_*) + (b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}), x_Symbol] :> \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)}{x^3} dx &= \frac{(c^2\sqrt{cx^2}) \int x^2(a+bx) dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (ax^2 + bx^3) dx}{x} \\ &= \frac{1}{3}ac^2x^2\sqrt{cx^2} + \frac{1}{4}bc^2x^3\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 27, normalized size = 0.66

$$\frac{1}{12}c^2x^2\sqrt{cx^2}(4a + 3bx)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x))/x^3,x]

[Out] (c^2*x^2*Sqrt[c*x^2]*(4*a + 3*b*x))/12

fricas [A] time = 0.45, size = 28, normalized size = 0.68

$$\frac{1}{12}(3bc^2x^3 + 4ac^2x^2)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)/x^3,x, algorithm="fricas")

[Out] 1/12*(3*b*c^2*x^3 + 4*a*c^2*x^2)*sqrt(c*x^2)

giac [A] time = 0.99, size = 28, normalized size = 0.68

$$\frac{1}{12}(3bc^2x^4\text{sgn}(x) + 4ac^2x^3\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)/x^3,x, algorithm="giac")

[Out] 1/12*(3*b*c^2*x^4*sgn(x) + 4*a*c^2*x^3*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$\frac{(3bx + 4a)(cx^2)^{\frac{5}{2}}}{12x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)/x^3,x)

[Out] 1/12/x^2*(3*b*x+4*a)*(c*x^2)^(5/2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(5/2)*(b*x+a)/x^3,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [B] time = 0.27, size = 25, normalized size = 0.61

$$\frac{c^{5/2} \left(4a \sqrt{x^6} + 3bx^3 \sqrt{x^2} \right)}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(5/2)*(a + b*x))/x^3,x)`

[Out] `(c^(5/2)*(4*a*(x^6)^(1/2) + 3*b*x^3*(x^2)^(1/2)))/12`

sympy [A] time = 1.58, size = 34, normalized size = 0.83

$$\frac{ac^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}{3x^2} + \frac{bc^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}{4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(5/2)*(b*x+a)/x**3,x)`

[Out] `a*c**(5/2)*(x**2)**(5/2)/(3*x**2) + b*c**(5/2)*(x**2)**(5/2)/(4*x)`

$$3.779 \quad \int \frac{(cx^2)^{5/2} (a+bx)}{x^4} dx$$

Optimal. Leaf size=39

$$\frac{1}{2}ac^2x\sqrt{cx^2} + \frac{1}{3}bc^2x^2\sqrt{cx^2}$$

[Out] $1/2*a*c^2*x*(c*x^2)^{(1/2)}+1/3*b*c^2*x^2*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{2}ac^2x\sqrt{cx^2} + \frac{1}{3}bc^2x^2\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x))/x^4,x]

[Out] (a*c^2*x*Sqrt[c*x^2])/2 + (b*c^2*x^2*Sqrt[c*x^2])/3

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)}{x^4} dx &= \frac{(c^2\sqrt{cx^2}) \int x(a+bx) dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (ax+bx^2) dx}{x} \\ &= \frac{1}{2}ac^2x\sqrt{cx^2} + \frac{1}{3}bc^2x^2\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 25, normalized size = 0.64

$$\frac{1}{6}c^2x\sqrt{cx^2}(3a + 2bx)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x))/x^4,x]

[Out] (c^2*x*Sqrt[c*x^2]*(3*a + 2*b*x))/6

fricas [A] time = 0.46, size = 26, normalized size = 0.67

$$\frac{1}{6}(2bc^2x^2 + 3ac^2x)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)/x^4,x, algorithm="fricas")

[Out] 1/6*(2*b*c^2*x^2 + 3*a*c^2*x)*sqrt(c*x^2)

giac [A] time = 1.14, size = 28, normalized size = 0.72

$$\frac{1}{6}(2bc^2x^3\operatorname{sgn}(x) + 3ac^2x^2\operatorname{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)/x^4,x, algorithm="giac")

[Out] 1/6*(2*b*c^2*x^3*sgn(x) + 3*a*c^2*x^2*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 21, normalized size = 0.54

$$\frac{(2bx + 3a)(cx^2)^{\frac{5}{2}}}{6x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)/x^4,x)

[Out] 1/6/x^3*(2*b*x+3*a)*(c*x^2)^(5/2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)/x^4,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [B] time = 0.26, size = 20, normalized size = 0.51

$$\frac{c^{5/2} \left(2b \sqrt{x^6} + 3ax|x| \right)}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(5/2)*(a + b*x))/x^4,x)

[Out] (c^(5/2)*(2*b*(x^6)^(1/2) + 3*a*x*abs(x)))/6

sympy [A] time = 1.62, size = 36, normalized size = 0.92

$$\frac{ac^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}{2x^3} + \frac{bc^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}{3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a)/x**4,x)

[Out] a*c**(5/2)*(x**2)**(5/2)/(2*x**3) + b*c**(5/2)*(x**2)**(5/2)/(3*x**2)

$$3.780 \quad \int \frac{x^3(a+bx)}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=35

$$\frac{ax^4}{3\sqrt{cx^2}} + \frac{bx^5}{4\sqrt{cx^2}}$$

[Out] $1/3*a*x^4/(c*x^2)^{(1/2)}+1/4*b*x^5/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{ax^4}{3\sqrt{cx^2}} + \frac{bx^5}{4\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x^3*(a + b*x))/\text{Sqrt}[c*x^2], x]$

[Out] $(a*x^4)/(3*\text{Sqrt}[c*x^2]) + (b*x^5)/(4*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)})*((c_.) + (d_.)*(x_)^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3(a+bx)}{\sqrt{cx^2}} dx &= \frac{x \int x^2(a+bx) dx}{\sqrt{cx^2}} \\ &= \frac{x \int (ax^2 + bx^3) dx}{\sqrt{cx^2}} \\ &= \frac{ax^4}{3\sqrt{cx^2}} + \frac{bx^5}{4\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 0.69

$$\frac{x^4(4a + 3bx)}{12\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*(a + b*x))/Sqrt[c*x^2],x]

[Out] (x^4*(4*a + 3*b*x))/(12*Sqrt[c*x^2])

fricas [A] time = 0.43, size = 25, normalized size = 0.71

$$\frac{(3bx^3 + 4ax^2)\sqrt{cx^2}}{12c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/12*(3*b*x^3 + 4*a*x^2)*sqrt(c*x^2)/c

giac [A] time = 1.30, size = 26, normalized size = 0.74

$$\frac{1}{12} \sqrt{cx^2} \left(\frac{3bx}{c} + \frac{4a}{c} \right) x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)/(c*x^2)^(1/2),x, algorithm="giac")

[Out] 1/12*sqrt(c*x^2)*(3*b*x/c + 4*a/c)*x^2

maple [A] time = 0.00, size = 21, normalized size = 0.60

$$\frac{(3bx + 4a)x^4}{12\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)/(c*x^2)^(1/2),x)

[Out] 1/12*x^4*(3*b*x+4*a)/(c*x^2)^(1/2)

maxima [A] time = 1.40, size = 33, normalized size = 0.94

$$\frac{\sqrt{cx^2}bx^3}{4c} + \frac{\sqrt{cx^2}ax^2}{3c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(b*x+a)/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $1/4*\sqrt{c*x^2}*b*x^3/c + 1/3*\sqrt{c*x^2}*a*x^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^3 (a + b x)}{\sqrt{c x^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x^3*(a + b*x))/(c*x^2)^(1/2),x)`

[Out] `int((x^3*(a + b*x))/(c*x^2)^(1/2), x)`

sympy [A] time = 0.61, size = 36, normalized size = 1.03

$$\frac{ax^4}{3\sqrt{c}\sqrt{x^2}} + \frac{bx^5}{4\sqrt{c}\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(b*x+a)/(c*x**2)**(1/2),x)`

[Out] $a*x**4/(3*\sqrt{c}*\sqrt{x**2}) + b*x**5/(4*\sqrt{c}*\sqrt{x**2})$

$$3.781 \quad \int \frac{x^2(a+bx)}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=35

$$\frac{ax^3}{2\sqrt{cx^2}} + \frac{bx^4}{3\sqrt{cx^2}}$$

[Out] 1/2*a*x^3/(c*x^2)^(1/2)+1/3*b*x^4/(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{ax^3}{2\sqrt{cx^2}} + \frac{bx^4}{3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^2*(a + b*x))/Sqrt[c*x^2],x]

[Out] (a*x^3)/(2*Sqrt[c*x^2]) + (b*x^4)/(3*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_)^(m_.))*((c_.) + (d_.)*(x_)^(n_.)), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2(a+bx)}{\sqrt{cx^2}} dx &= \frac{x \int x(a+bx) dx}{\sqrt{cx^2}} \\ &= \frac{x \int (ax + bx^2) dx}{\sqrt{cx^2}} \\ &= \frac{ax^3}{2\sqrt{cx^2}} + \frac{bx^4}{3\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 0.69

$$\frac{x^3(3a + 2bx)}{6\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*(a + b*x))/Sqrt[c*x^2], x]

[Out] (x^3*(3*a + 2*b*x))/(6*Sqrt[c*x^2])

fricas [A] time = 0.48, size = 23, normalized size = 0.66

$$\frac{(2bx^2 + 3ax)\sqrt{cx^2}}{6c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] 1/6*(2*b*x^2 + 3*a*x)*sqrt(c*x^2)/c

giac [A] time = 1.16, size = 24, normalized size = 0.69

$$\frac{1}{6} \sqrt{cx^2} \left(\frac{2bx}{c} + \frac{3a}{c} \right) x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)/(c*x^2)^(1/2), x, algorithm="giac")

[Out] 1/6*sqrt(c*x^2)*(2*b*x/c + 3*a/c)*x

maple [A] time = 0.00, size = 21, normalized size = 0.60

$$\frac{(2bx + 3a)x^3}{6\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)/(c*x^2)^(1/2), x)

[Out] 1/6*x^3*(2*b*x+3*a)/(c*x^2)^(1/2)

maxima [A] time = 1.30, size = 26, normalized size = 0.74

$$\frac{\sqrt{cx^2} bx^2}{3c} + \frac{ax^2}{2\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] 1/3*sqrt(c*x^2)*b*x^2/c + 1/2*a*x^2/sqrt(c)

mupad [B] time = 0.25, size = 23, normalized size = 0.66

$$\frac{2b\sqrt{x^6} + 3ax\sqrt{x^2}}{6\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^2*(a + b*x))/(c*x^2)^(1/2),x)

[Out] (2*b*(x^6)^(1/2) + 3*a*x*(x^2)^(1/2))/(6*c^(1/2))

sympy [A] time = 0.52, size = 36, normalized size = 1.03

$$\frac{ax^3}{2\sqrt{c}\sqrt{x^2}} + \frac{bx^4}{3\sqrt{c}\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)/(c*x**2)**(1/2),x)

[Out] a*x**3/(2*sqrt(c)*sqrt(x**2)) + b*x**4/(3*sqrt(c)*sqrt(x**2))

$$3.782 \quad \int \frac{x(a+bx)}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=32

$$\frac{ax^2}{\sqrt{cx^2}} + \frac{bx^3}{2\sqrt{cx^2}}$$

[Out] $a*x^2/(c*x^2)^{(1/2)}+1/2*b*x^3/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {15}

$$\frac{ax^2}{\sqrt{cx^2}} + \frac{bx^3}{2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] `Int[(x*(a + b*x))/Sqrt[c*x^2], x]`

[Out] $(a*x^2)/\text{Sqrt}[c*x^2] + (b*x^3)/(2*\text{Sqrt}[c*x^2])$

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rubi steps

$$\begin{aligned} \int \frac{x(a+bx)}{\sqrt{cx^2}} dx &= \frac{x \int (a+bx) dx}{\sqrt{cx^2}} \\ &= \frac{ax^2}{\sqrt{cx^2}} + \frac{bx^3}{2\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 23, normalized size = 0.72

$$\frac{x^2(2a+bx)}{2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] `Integrate[(x*(a + b*x))/Sqrt[c*x^2], x]`

[Out] $(x^2(2a + bx))/(2\sqrt{cx^2})$

fricas [A] time = 0.46, size = 19, normalized size = 0.59

$$\frac{\sqrt{cx^2}(bx + 2a)}{2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)/(c*x^2)^(1/2),x, algorithm="fricas")`

[Out] $1/2*\sqrt{c*x^2}*(b*x + 2*a)/c$

giac [A] time = 1.11, size = 22, normalized size = 0.69

$$\frac{1}{2} \sqrt{cx^2} \left(\frac{bx}{c} + \frac{2a}{c} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)/(c*x^2)^(1/2),x, algorithm="giac")`

[Out] $1/2*\sqrt{c*x^2}*(b*x/c + 2*a/c)$

maple [A] time = 0.00, size = 20, normalized size = 0.62

$$\frac{(bx + 2a)x^2}{2\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)/(c*x^2)^(1/2),x)`

[Out] $1/2*x^2*(b*x+2*a)/(c*x^2)^(1/2)$

maxima [A] time = 1.30, size = 22, normalized size = 0.69

$$\frac{bx^2}{2\sqrt{c}} + \frac{\sqrt{cx^2}a}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $1/2*b*x^2/\sqrt{c} + \sqrt{c*x^2}*a/c$

mupad [B] time = 0.22, size = 19, normalized size = 0.59

$$\frac{2 a |x| + b x \sqrt{x^2}}{2 \sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x*(a + b*x))/(c*x^2)^(1/2), x)`

[Out] `(2*a*abs(x) + b*x*(x^2)^(1/2))/(2*c^(1/2))`

sympy [A] time = 0.46, size = 34, normalized size = 1.06

$$\frac{ax^2}{\sqrt{c}\sqrt{x^2}} + \frac{bx^3}{2\sqrt{c}\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)/(c*x**2)**(1/2), x)`

[Out] `a*x**2/(sqrt(c)*sqrt(x**2)) + b*x**3/(2*sqrt(c)*sqrt(x**2))`

$$3.783 \quad \int \frac{a+bx}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=29

$$\frac{ax \log(x)}{\sqrt{cx^2}} + \frac{bx^2}{\sqrt{cx^2}}$$

[Out] $b*x^2/(c*x^2)^{(1/2)}+a*x*\ln(x)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {15, 43}

$$\frac{ax \log(x)}{\sqrt{cx^2}} + \frac{bx^2}{\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/Sqrt[c*x^2], x]

[Out] (b*x^2)/Sqrt[c*x^2] + (a*x*Log[x])/Sqrt[c*x^2]

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{\sqrt{cx^2}} dx &= \frac{x \int \frac{a+bx}{x} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(b + \frac{a}{x}\right) dx}{\sqrt{cx^2}} \\ &= \frac{bx^2}{\sqrt{cx^2}} + \frac{ax \log(x)}{\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 19, normalized size = 0.66

$$\frac{x(a \log(x) + bx)}{\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/Sqrt[c*x^2], x]

[Out] (x*(b*x + a*Log[x]))/Sqrt[c*x^2]

fricas [A] time = 0.43, size = 22, normalized size = 0.76

$$\frac{\sqrt{cx^2} (bx + a \log(x))}{cx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x + a*log(x))/(c*x)

giac [A] time = 1.32, size = 35, normalized size = 1.21

$$-\frac{a \log\left(\left|-\sqrt{c}x + \sqrt{cx^2}\right|\right)}{\sqrt{c}} + \frac{\sqrt{cx^2} b}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(c*x^2)^(1/2), x, algorithm="giac")

[Out] -a*log(abs(-sqrt(c)*x + sqrt(c*x^2)))/sqrt(c) + sqrt(c*x^2)*b/c

maple [A] time = 0.00, size = 18, normalized size = 0.62

$$\frac{(a \ln(x) + bx)x}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/(c*x^2)^(1/2), x)

[Out] 1/(c*x^2)^(1/2)*x*(a*ln(x)+b*x)

maxima [A] time = 1.32, size = 20, normalized size = 0.69

$$\frac{a \log(x)}{\sqrt{c}} + \frac{\sqrt{cx^2} b}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] a*log(x)/sqrt(c) + sqrt(c*x^2)*b/c

mupad [B] time = 0.51, size = 17, normalized size = 0.59

$$\frac{b|x| + a \ln(cx) \operatorname{sign}(x)}{\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(c*x^2)^(1/2),x)

[Out] (b*abs(x) + a*log(c*x)*sign(x))/c^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{a + bx}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(c*x**2)**(1/2),x)

[Out] Integral((a + b*x)/sqrt(c*x**2), x)

$$3.784 \quad \int \frac{a+bx}{x\sqrt{cx^2}} dx$$

Optimal. Leaf size=27

$$\frac{bx \log(x)}{\sqrt{cx^2}} - \frac{a}{\sqrt{cx^2}}$$

[Out] $-a/(c*x^2)^{(1/2)}+b*x*\ln(x)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{bx \log(x)}{\sqrt{cx^2}} - \frac{a}{\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x*sqrt[c*x^2]),x]

[Out] $-(a/\text{sqrt}[c*x^2]) + (b*x*\text{Log}[x])/\text{sqrt}[c*x^2]$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x\sqrt{cx^2}} dx &= \frac{x \int \frac{a+bx}{x^2} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^2} + \frac{b}{x} \right) dx}{\sqrt{cx^2}} \\ &= -\frac{a}{\sqrt{cx^2}} + \frac{bx \log(x)}{\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.85

$$\frac{cx^2(bx \log(x) - a)}{(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x*Sqrt[c*x^2]),x]

[Out] (c*x^2*(-a + b*x*Log[x]))/(c*x^2)^(3/2)

fricas [A] time = 0.46, size = 23, normalized size = 0.85

$$\frac{\sqrt{cx^2}(bx \log(x) - a)}{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x*log(x) - a)/(c*x^2)

giac [B] time = 0.98, size = 47, normalized size = 1.74

$$-\frac{b \log\left(\left|-\sqrt{c}x + \sqrt{cx^2}\right|\right) - \frac{2a\sqrt{c}}{\sqrt{c}x - \sqrt{cx^2}}}{\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x/(c*x^2)^(1/2),x, algorithm="giac")

[Out] -(b*log(abs(-sqrt(c)*x + sqrt(c*x^2))) - 2*a*sqrt(c)/(sqrt(c)*x - sqrt(c*x^2)))/sqrt(c)

maple [A] time = 0.00, size = 18, normalized size = 0.67

$$\frac{bx \ln(x) - a}{\sqrt{c}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x/(c*x^2)^(1/2),x)

[Out] (b*x*ln(x)-a)/(c*x^2)^(1/2)

maxima [A] time = 1.33, size = 17, normalized size = 0.63

$$\frac{b \log(x)}{\sqrt{c}} - \frac{a}{\sqrt{c} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] b*log(x)/sqrt(c) - a/(sqrt(c)*x)

mupad [B] time = 1.22, size = 22, normalized size = 0.81

$$-\frac{\frac{a}{\sqrt{x^2}} - b \ln(cx) \operatorname{sign}(x)}{\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(x*(c*x^2)^(1/2)),x)

[Out] -(a/(x^2)^(1/2) - b*log(c*x)*sign(x))/c^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{a + bx}{x\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x/(c*x**2)**(1/2),x)

[Out] Integral((a + b*x)/(x*sqrt(c*x**2)), x)

$$3.785 \quad \int \frac{a+bx}{x^2 \sqrt{cx^2}} dx$$

Optimal. Leaf size=26

$$-\frac{(a+bx)^2}{2ax\sqrt{cx^2}}$$

[Out] $-1/2*(b*x+a)^2/a/x/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 37}

$$-\frac{(a+bx)^2}{2ax\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] `Int[(a + b*x)/(x^2*sqrt[c*x^2]), x]`

[Out] $-(a + b*x)^2/(2*a*x*sqrt[c*x^2])$

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rule 37

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]`

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^2 \sqrt{cx^2}} dx &= \frac{x \int \frac{a+bx}{x^3} dx}{\sqrt{cx^2}} \\ &= -\frac{(a+bx)^2}{2ax\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.88

$$\frac{cx(-a - 2bx)}{2(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x^2*Sqrt[c*x^2]), x]

[Out] (c*x*(-a - 2*b*x))/(2*(c*x^2)^(3/2))

fricas [A] time = 0.47, size = 21, normalized size = 0.81

$$-\frac{\sqrt{cx^2}(2bx + a)}{2cx^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^2/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] -1/2*sqrt(c*x^2)*(2*b*x + a)/(c*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^2/(c*x^2)^(1/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 19, normalized size = 0.73

$$-\frac{2bx + a}{2\sqrt{cx^2}x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^2/(c*x^2)^(1/2), x)

[Out] -1/2*(2*b*x+a)/x/(c*x^2)^(1/2)

maxima [A] time = 1.25, size = 19, normalized size = 0.73

$$-\frac{b}{\sqrt{c}x} - \frac{a}{2\sqrt{c}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^2/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] -b/(sqrt(c)*x) - 1/2*a/(sqrt(c)*x^2)

mupad [B] time = 0.16, size = 25, normalized size = 0.96

$$-\frac{2bx^3 + ax^2}{2\sqrt{c}x(x^2)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(x^2*(c*x^2)^(1/2)),x)

[Out] -(a*x^2 + 2*b*x^3)/(2*c^(1/2)*x*(x^2)^(3/2))

sympy [A] time = 0.54, size = 31, normalized size = 1.19

$$-\frac{a}{2\sqrt{c}x\sqrt{x^2}} - \frac{b}{\sqrt{c}\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x**2/(c*x**2)**(1/2),x)

[Out] -a/(2*sqrt(c)*x*sqrt(x**2)) - b/(sqrt(c)*sqrt(x**2))

$$3.786 \quad \int \frac{a+bx}{x^3 \sqrt{cx^2}} dx$$

Optimal. Leaf size=35

$$-\frac{a}{3x^2\sqrt{cx^2}} - \frac{b}{2x\sqrt{cx^2}}$$

[Out] $-1/3*a/x^2/(c*x^2)^{(1/2)}-1/2*b/x/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a}{3x^2\sqrt{cx^2}} - \frac{b}{2x\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x^3*sqrt[c*x^2]), x]

[Out] $-a/(3*x^2*\text{sqrt}[c*x^2]) - b/(2*x*\text{sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^3 \sqrt{cx^2}} dx &= \frac{x \int \frac{a+bx}{x^4} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^4} + \frac{b}{x^3} \right) dx}{\sqrt{cx^2}} \\ &= -\frac{a}{3x^2\sqrt{cx^2}} - \frac{b}{2x\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 0.63

$$\frac{c(-2a - 3bx)}{6(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x^3*Sqrt[c*x^2]), x]

[Out] (c*(-2*a - 3*b*x))/(6*(c*x^2)^(3/2))

fricas [A] time = 0.42, size = 23, normalized size = 0.66

$$-\frac{\sqrt{cx^2}(3bx + 2a)}{6cx^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] -1/6*sqrt(c*x^2)*(3*b*x + 2*a)/(c*x^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{bx + a}{\sqrt{cx^2} x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3/(c*x^2)^(1/2), x, algorithm="giac")

[Out] integrate((b*x + a)/(sqrt(c*x^2)*x^3), x)

maple [A] time = 0.00, size = 21, normalized size = 0.60

$$-\frac{3bx + 2a}{6\sqrt{cx^2} x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^3/(c*x^2)^(1/2), x)

[Out] -1/6*(3*b*x+2*a)/x^2/(c*x^2)^(1/2)

maxima [A] time = 1.28, size = 19, normalized size = 0.54

$$-\frac{b}{2\sqrt{c}x^2} - \frac{a}{3\sqrt{c}x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^3/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $-1/2*b/(sqrt(c)*x^2) - 1/3*a/(sqrt(c)*x^3)$

mupad [B] time = 0.15, size = 26, normalized size = 0.74

$$-\frac{2a\sqrt{x^2} + 3bx\sqrt{x^2}}{6\sqrt{c}x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(x^3*(c*x^2)^(1/2)),x)`

[Out] $-(2*a*(x^2)^(1/2) + 3*b*x*(x^2)^(1/2))/(6*c^(1/2)*x^4)$

sympy [A] time = 0.64, size = 36, normalized size = 1.03

$$-\frac{a}{3\sqrt{c}x^2\sqrt{x^2}} - \frac{b}{2\sqrt{c}x\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x**3/(c*x**2)**(1/2),x)`

[Out] $-a/(3*sqrt(c)*x**2*sqrt(x**2)) - b/(2*sqrt(c)*x*sqrt(x**2))$

$$3.787 \quad \int \frac{a+bx}{x^4 \sqrt{cx^2}} dx$$

Optimal. Leaf size=35

$$-\frac{a}{4x^3 \sqrt{cx^2}} - \frac{b}{3x^2 \sqrt{cx^2}}$$

[Out] $-1/4*a/x^3/(c*x^2)^{(1/2)}-1/3*b/x^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a}{4x^3 \sqrt{cx^2}} - \frac{b}{3x^2 \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x^4*Sqrt[c*x^2]), x]

[Out] $-a/(4*x^3*\text{Sqrt}[c*x^2]) - b/(3*x^2*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^4 \sqrt{cx^2}} dx &= \frac{x \int \frac{a+bx}{x^5} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^5} + \frac{b}{x^4} \right) dx}{\sqrt{cx^2}} \\ &= -\frac{a}{4x^3 \sqrt{cx^2}} - \frac{b}{3x^2 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.69

$$\frac{-3a - 4bx}{12x^3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x^4*Sqrt[c*x^2]), x]

[Out] (-3*a - 4*b*x)/(12*x^3*Sqrt[c*x^2])

fricas [A] time = 0.44, size = 23, normalized size = 0.66

$$-\frac{\sqrt{cx^2}(4bx + 3a)}{12cx^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^4/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] -1/12*sqrt(c*x^2)*(4*b*x + 3*a)/(c*x^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^4/(c*x^2)^(1/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 21, normalized size = 0.60

$$-\frac{4bx + 3a}{12\sqrt{c}x^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^4/(c*x^2)^(1/2), x)

[Out] -1/12*(4*b*x+3*a)/x^3/(c*x^2)^(1/2)

maxima [A] time = 1.30, size = 19, normalized size = 0.54

$$-\frac{b}{3\sqrt{c}x^3} - \frac{a}{4\sqrt{c}x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^4/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] -1/3*b/(sqrt(c)*x^3) - 1/4*a/(sqrt(c)*x^4)

mupad [B] time = 0.15, size = 26, normalized size = 0.74

$$-\frac{3a\sqrt{x^2} + 4bx\sqrt{x^2}}{12\sqrt{c}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(x^4*(c*x^2)^(1/2)),x)

[Out] -(3*a*(x^2)^(1/2) + 4*b*x*(x^2)^(1/2))/(12*c^(1/2)*x^5)

sympy [A] time = 0.81, size = 37, normalized size = 1.06

$$-\frac{a}{4\sqrt{c}x^3\sqrt{x^2}} - \frac{b}{3\sqrt{c}x^2\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x**4/(c*x**2)**(1/2),x)

[Out] -a/(4*sqrt(c)*x**3*sqrt(x**2)) - b/(3*sqrt(c)*x**2*sqrt(x**2))

$$3.788 \quad \int \frac{x^3(a+bx)}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=38

$$\frac{ax^2}{c\sqrt{cx^2}} + \frac{bx^3}{2c\sqrt{cx^2}}$$

[Out] $a*x^2/c/(c*x^2)^{(1/2)}+1/2*b*x^3/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.056$, Rules used = {15}

$$\frac{ax^2}{c\sqrt{cx^2}} + \frac{bx^3}{2c\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x^3*(a + b*x))/(c*x^2)^{(3/2)}, x]$

[Out] $(a*x^2)/(c*\text{Sqrt}[c*x^2]) + (b*x^3)/(2*c*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int \frac{x^3(a+bx)}{(cx^2)^{3/2}} dx &= \frac{x \int (a+bx) dx}{c\sqrt{cx^2}} \\ &= \frac{ax^2}{c\sqrt{cx^2}} + \frac{bx^3}{2c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 23, normalized size = 0.61

$$\frac{x^4(2a+bx)}{2(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*(a + b*x))/(c*x^2)^(3/2),x]

[Out] (x^4*(2*a + b*x))/(2*(c*x^2)^(3/2))

fricas [A] time = 0.44, size = 19, normalized size = 0.50

$$\frac{\sqrt{cx^2}(bx + 2a)}{2c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)/(c*x^2)^(3/2),x, algorithm="fricas")

[Out] 1/2*sqrt(c*x^2)*(b*x + 2*a)/c^2

giac [A] time = 1.01, size = 25, normalized size = 0.66

$$\frac{\sqrt{cx^2}\left(\frac{bx}{c} + \frac{2a}{c}\right)}{2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)/(c*x^2)^(3/2),x, algorithm="giac")

[Out] 1/2*sqrt(c*x^2)*(b*x/c + 2*a/c)/c

maple [A] time = 0.00, size = 20, normalized size = 0.53

$$\frac{(bx + 2a)x^4}{2(c x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)/(c*x^2)^(3/2),x)

[Out] 1/2*x^4*(b*x+2*a)/(c*x^2)^(3/2)

maxima [A] time = 1.31, size = 32, normalized size = 0.84

$$\frac{bx^3}{2\sqrt{cx^2}c} + \frac{ax^2}{\sqrt{cx^2}c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)/(c*x^2)^(3/2),x, algorithm="maxima")

[Out] 1/2*b*x^3/(sqrt(c*x^2)*c) + a*x^2/(sqrt(c*x^2)*c)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^3 (a + b x)}{(c x^2)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^3*(a + b*x))/(c*x^2)^(3/2), x)

[Out] int((x^3*(a + b*x))/(c*x^2)^(3/2), x)

sympy [A] time = 0.64, size = 34, normalized size = 0.89

$$\frac{ax^4}{c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} + \frac{bx^5}{2c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)/(c*x**2)**(3/2), x)

[Out] a*x**4/(c**(3/2)*(x**2)**(3/2)) + b*x**5/(2*c**(3/2)*(x**2)**(3/2))

$$3.789 \quad \int \frac{x^2(a+bx)}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=35

$$\frac{ax \log(x)}{c\sqrt{cx^2}} + \frac{bx^2}{c\sqrt{cx^2}}$$

[Out] $b*x^2/c/(c*x^2)^{(1/2)}+a*x*\ln(x)/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{ax \log(x)}{c\sqrt{cx^2}} + \frac{bx^2}{c\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x^2*(a + b*x))/(c*x^2)^{(3/2)}, x]$

[Out] $(b*x^2)/(c*\text{Sqrt}[c*x^2]) + (a*x*\text{Log}[x])/(c*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] :> \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[((a_.) + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] :> \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2(a+bx)}{(cx^2)^{3/2}} dx &= \frac{x \int \frac{a+bx}{x} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(b + \frac{a}{x}\right) dx}{c\sqrt{cx^2}} \\ &= \frac{bx^2}{c\sqrt{cx^2}} + \frac{ax \log(x)}{c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 21, normalized size = 0.60

$$\frac{x^3(a \log(x) + bx)}{(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*(a + b*x))/(c*x^2)^(3/2), x]

[Out] (x^3*(b*x + a*Log[x]))/(c*x^2)^(3/2)

fricas [A] time = 0.50, size = 22, normalized size = 0.63

$$\frac{\sqrt{cx^2} (bx + a \log(x))}{c^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x + a*log(x))/(c^2*x)

giac [A] time = 0.99, size = 40, normalized size = 1.14

$$-\frac{\frac{a \log\left(|-\sqrt{c}x + \sqrt{cx^2}\right)}{\sqrt{c}} - \frac{\sqrt{cx^2}b}{c}}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)/(c*x^2)^(3/2), x, algorithm="giac")

[Out] -(a*log(abs(-sqrt(c)*x + sqrt(c*x^2)))/sqrt(c) - sqrt(c*x^2)*b/c)/c

maple [A] time = 0.00, size = 20, normalized size = 0.57

$$\frac{(a \ln(x) + bx)x^3}{(cx^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(b*x+a)/(c*x^2)^(3/2),x)`

[Out] `1/(c*x^2)^(3/2)*x^3*(a*ln(x)+b*x)`

maxima [A] time = 1.35, size = 23, normalized size = 0.66

$$\frac{bx^2}{\sqrt{cx^2}c} + \frac{a \log(x)}{c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(b*x+a)/(c*x^2)^(3/2),x, algorithm="maxima")`

[Out] `b*x^2/(sqrt(c*x^2)*c) + a*log(x)/c^(3/2)`

mupad [B] time = 0.32, size = 30, normalized size = 0.86

$$\frac{b|x|}{c^{3/2}} + \frac{a \ln(x + |x|)}{c^{3/2}} - \frac{ax}{c^{3/2} \sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x^2*(a + b*x))/(c*x^2)^(3/2),x)`

[Out] `(b*abs(x))/c^(3/2) + (a*log(x + abs(x)))/c^(3/2) - (a*x)/(c^(3/2)*(x^2)^(1/2))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2(a + bx)}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(b*x+a)/(c*x**2)**(3/2),x)`

[Out] `Integral(x**2*(a + b*x)/(c*x**2)**(3/2), x)`

$$3.790 \quad \int \frac{x(a+bx)}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=33

$$\frac{bx \log(x)}{c\sqrt{cx^2}} - \frac{a}{c\sqrt{cx^2}}$$

[Out] $-a/c/(c*x^2)^{(1/2)}+b*x*\ln(x)/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {15, 43}

$$\frac{bx \log(x)}{c\sqrt{cx^2}} - \frac{a}{c\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x*(a + b*x))/(c*x^2)^{(3/2)}, x]$

[Out] $-(a/(c*\text{Sqrt}[c*x^2])) + (b*x*\text{Log}[x])/(c*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[((a_.) + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x(a+bx)}{(cx^2)^{3/2}} dx &= \frac{x \int \frac{a+bx}{x^2} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^2} + \frac{b}{x} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{a}{c\sqrt{cx^2}} + \frac{bx \log(x)}{c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 0.67

$$\frac{x^2(bx \log(x) - a)}{(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x*(a + b*x))/(c*x^2)^(3/2), x]

[Out] (x^2*(-a + b*x*Log[x]))/(c*x^2)^(3/2)

fricas [A] time = 0.43, size = 23, normalized size = 0.70

$$\frac{\sqrt{cx^2}(bx \log(x) - a)}{c^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x*log(x) - a)/(c^2*x^2)

giac [A] time = 1.22, size = 47, normalized size = 1.42

$$-\frac{b \log\left(\left|-\sqrt{c}x + \sqrt{cx^2}\right|\right) - \frac{2a\sqrt{c}}{\sqrt{c}x - \sqrt{cx^2}}}{c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)/(c*x^2)^(3/2), x, algorithm="giac")

[Out] -(b*log(abs(-sqrt(c)*x + sqrt(c*x^2))) - 2*a*sqrt(c)/(sqrt(c)*x - sqrt(c*x^2)))/c^(3/2)

maple [A] time = 0.00, size = 21, normalized size = 0.64

$$\frac{(bx \ln(x) - a) x^2}{(c x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)/(c*x^2)^(3/2),x)`

[Out] `x^2*(b*x*ln(x)-a)/(c*x^2)^(3/2)`

maxima [A] time = 1.31, size = 21, normalized size = 0.64

$$\frac{b \log(x)}{c^{\frac{3}{2}}} - \frac{a}{\sqrt{c x^2} c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)/(c*x^2)^(3/2),x, algorithm="maxima")`

[Out] `b*log(x)/c^(3/2) - a/(sqrt(c*x^2)*c)`

mupad [B] time = 0.25, size = 28, normalized size = 0.85

$$-\frac{a + b x - b \ln(x + |x|) \sqrt{x^2}}{c^{3/2} \sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x*(a + b*x))/(c*x^2)^(3/2),x)`

[Out] `-(a + b*x - b*log(x + abs(x))*(x^2)^(1/2))/(c^(3/2)*(x^2)^(1/2))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x(a + bx)}{(c x^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)/(c*x**2)**(3/2),x)`

[Out] `Integral(x*(a + b*x)/(c*x**2)**(3/2), x)`

$$3.791 \quad \int \frac{a+bx}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=29

$$-\frac{(a+bx)^2}{2acx\sqrt{cx^2}}$$

[Out] $-1/2*(b*x+a)^2/a/c/x/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {15, 37}

$$-\frac{(a+bx)^2}{2acx\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)/(c*x^2)^{(3/2)}, x]$

[Out] $-(a + b*x)^2/(2*a*c*x*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{!IntegerQ}[m]$

Rule 37

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{(cx^2)^{3/2}} dx &= \frac{x \int \frac{a+bx}{x^3} dx}{c\sqrt{cx^2}} \\ &= -\frac{(a+bx)^2}{2acx\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 0.76

$$\frac{x(-a - 2bx)}{2(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(c*x^2)^(3/2), x]

[Out] (x*(-a - 2*b*x))/(2*(c*x^2)^(3/2))

fricas [A] time = 0.46, size = 21, normalized size = 0.72

$$-\frac{\sqrt{cx^2}(2bx + a)}{2c^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] -1/2*sqrt(c*x^2)*(2*b*x + a)/(c^2*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(c*x^2)^(3/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 17, normalized size = 0.59

$$-\frac{(2bx + a)x}{2(cx^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/(c*x^2)^(3/2), x)

[Out] -1/2*x*(2*b*x+a)/(c*x^2)^(3/2)

maxima [A] time = 1.35, size = 23, normalized size = 0.79

$$-\frac{b}{\sqrt{cx^2}c} - \frac{a}{2c^{\frac{3}{2}}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(c*x^2)^(3/2),x, algorithm="maxima")

[Out] -b/(sqrt(c*x^2)*c) - 1/2*a/(c^(3/2)*x^2)

mupad [B] time = 0.15, size = 25, normalized size = 0.86

$$-\frac{2bx^3 + ax^2}{2c^{3/2}x(x^2)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(c*x^2)^(3/2),x)

[Out] -(a*x^2 + 2*b*x^3)/(2*c^(3/2)*x*(x^2)^(3/2))

sympy [A] time = 0.54, size = 34, normalized size = 1.17

$$-\frac{ax}{2c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} - \frac{bx^2}{c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(c*x**2)**(3/2),x)

[Out] -a*x/(2*c**(3/2)*(x**2)**(3/2)) - b*x**2/(c**(3/2)*(x**2)**(3/2))

$$3.792 \quad \int \frac{a+bx}{x(cx^2)^{3/2}} dx$$

Optimal. Leaf size=41

$$-\frac{a}{3cx^2\sqrt{cx^2}} - \frac{b}{2cx\sqrt{cx^2}}$$

[Out] $-1/3*a/c/x^2/(c*x^2)^{(1/2)}-1/2*b/c/x/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a}{3cx^2\sqrt{cx^2}} - \frac{b}{2cx\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x*(c*x^2)^(3/2)), x]

[Out] $-a/(3*c*x^2*\text{Sqrt}[c*x^2]) - b/(2*c*x*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a + bx}{x (cx^2)^{3/2}} dx &= \frac{x \int \frac{a+bx}{x^4} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^4} + \frac{b}{x^3} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{a}{3cx^2\sqrt{cx^2}} - \frac{b}{2cx\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 0.61

$$\frac{cx^2(-2a - 3bx)}{6 (cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x*(c*x^2)^(3/2)), x]

[Out] (c*x^2*(-2*a - 3*b*x))/(6*(c*x^2)^(5/2))

fricas [A] time = 0.45, size = 23, normalized size = 0.56

$$-\frac{\sqrt{cx^2} (3bx + 2a)}{6c^2x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] -1/6*sqrt(c*x^2)*(3*b*x + 2*a)/(c^2*x^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{bx + a}{(cx^2)^{\frac{3}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x/(c*x^2)^(3/2), x, algorithm="giac")

[Out] integrate((b*x + a)/((c*x^2)^(3/2)*x), x)

maple [A] time = 0.00, size = 18, normalized size = 0.44

$$-\frac{3bx + 2a}{6(c^2x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x/(c*x^2)^(3/2), x)

[Out] -1/6*(3*b*x+2*a)/(c*x^2)^(3/2)

maxima [A] time = 1.32, size = 19, normalized size = 0.46

$$-\frac{b}{2c^{\frac{3}{2}}x^2} - \frac{a}{3c^{\frac{3}{2}}x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x/(c*x^2)^(3/2), x, algorithm="maxima")

[Out] -1/2*b/(c^(3/2)*x^2) - 1/3*a/(c^(3/2)*x^3)

mupad [B] time = 0.16, size = 26, normalized size = 0.63

$$-\frac{2a\sqrt{x^2} + 3bx\sqrt{x^2}}{6c^{3/2}x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(x*(c*x^2)^(3/2)), x)

[Out] -(2*a*(x^2)^(1/2) + 3*b*x*(x^2)^(1/2))/(6*c^(3/2)*x^4)

sympy [A] time = 0.63, size = 32, normalized size = 0.78

$$-\frac{a}{3c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} - \frac{bx}{2c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x/(c*x**2)**(3/2), x)

[Out] -a/(3*c**(3/2)*(x**2)**(3/2)) - b*x/(2*c**(3/2)*(x**2)**(3/2))

$$3.793 \quad \int \frac{a+bx}{x^2(cx^2)^{3/2}} dx$$

Optimal. Leaf size=41

$$-\frac{a}{4cx^3\sqrt{cx^2}} - \frac{b}{3cx^2\sqrt{cx^2}}$$

[Out] $-1/4*a/c/x^3/(c*x^2)^{(1/2)}-1/3*b/c/x^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a}{4cx^3\sqrt{cx^2}} - \frac{b}{3cx^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x^2*(c*x^2)^(3/2)),x]

[Out] $-a/(4*c*x^3*\text{Sqrt}[c*x^2]) - b/(3*c*x^2*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a + bx}{x^2 (cx^2)^{3/2}} dx &= \frac{x \int \frac{a+bx}{x^5} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^5} + \frac{b}{x^4} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{a}{4cx^3\sqrt{cx^2}} - \frac{b}{3cx^2\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.66

$$-\frac{\sqrt{cx^2} (3a + 4bx)}{12c^2x^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x^2*(c*x^2)^(3/2)), x]

[Out] -1/12*(Sqrt[c*x^2]*(3*a + 4*b*x))/(c^2*x^5)

fricas [A] time = 0.45, size = 23, normalized size = 0.56

$$-\frac{\sqrt{cx^2} (4bx + 3a)}{12c^2x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^2/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] -1/12*sqrt(c*x^2)*(4*b*x + 3*a)/(c^2*x^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^2/(c*x^2)^(3/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$-\frac{4bx + 3a}{12(c x^2)^{\frac{3}{2}} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/x^2/(c*x^2)^(3/2),x)`

[Out] $-1/12*(4*b*x+3*a)/x/(c*x^2)^(3/2)$

maxima [A] time = 1.34, size = 19, normalized size = 0.46

$$-\frac{b}{3c^{\frac{3}{2}}x^3} - \frac{a}{4c^{\frac{3}{2}}x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^2/(c*x^2)^(3/2),x, algorithm="maxima")`

[Out] $-1/3*b/(c^(3/2)*x^3) - 1/4*a/(c^(3/2)*x^4)$

mupad [B] time = 0.15, size = 26, normalized size = 0.63

$$-\frac{3a\sqrt{x^2} + 4bx\sqrt{x^2}}{12c^{3/2}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(x^2*(c*x^2)^(3/2)),x)`

[Out] $-(3*a*(x^2)^(1/2) + 4*b*x*(x^2)^(1/2))/(12*c^(3/2)*x^5)$

sympy [A] time = 0.77, size = 32, normalized size = 0.78

$$-\frac{a}{4c^{\frac{3}{2}}x(x^2)^{\frac{3}{2}}} - \frac{b}{3c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x**2/(c*x**2)**(3/2),x)`

[Out] $-a/(4*c**(3/2)*x*(x**2)**(3/2)) - b/(3*c**(3/2)*(x**2)**(3/2))$

$$3.794 \quad \int \frac{a+bx}{x^3(cx^2)^{3/2}} dx$$

Optimal. Leaf size=41

$$-\frac{a}{5cx^4\sqrt{cx^2}} - \frac{b}{4cx^3\sqrt{cx^2}}$$

[Out] $-1/5*a/c/x^4/(c*x^2)^{(1/2)}-1/4*b/c/x^3/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a}{5cx^4\sqrt{cx^2}} - \frac{b}{4cx^3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x^3*(c*x^2)^(3/2)),x]

[Out] $-a/(5*c*x^4*\text{Sqrt}[c*x^2]) - b/(4*c*x^3*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a + bx}{x^3 (cx^2)^{3/2}} dx &= \frac{x \int \frac{a+bx}{x^6} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^6} + \frac{b}{x^5} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{a}{5cx^4\sqrt{cx^2}} - \frac{b}{4cx^3\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 0.54

$$\frac{c(-4a - 5bx)}{20 (cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x^3*(c*x^2)^(3/2)),x]

[Out] (c*(-4*a - 5*b*x))/(20*(c*x^2)^(5/2))

fricas [A] time = 0.46, size = 23, normalized size = 0.56

$$-\frac{\sqrt{cx^2} (5bx + 4a)}{20 c^2 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3/(c*x^2)^(3/2),x, algorithm="fricas")

[Out] -1/20*sqrt(c*x^2)*(5*b*x + 4*a)/(c^2*x^6)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{bx + a}{(cx^2)^{\frac{3}{2}} x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3/(c*x^2)^(3/2),x, algorithm="giac")

[Out] integrate((b*x + a)/((c*x^2)^(3/2)*x^3), x)

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$-\frac{5bx + 4a}{20(c x^2)^{\frac{3}{2}} x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^3/(c*x^2)^(3/2), x)

[Out] -1/20*(5*b*x+4*a)/x^2/(c*x^2)^(3/2)

maxima [A] time = 1.28, size = 19, normalized size = 0.46

$$-\frac{b}{4c^{\frac{3}{2}}x^4} - \frac{a}{5c^{\frac{3}{2}}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3/(c*x^2)^(3/2), x, algorithm="maxima")

[Out] -1/4*b/(c^(3/2)*x^4) - 1/5*a/(c^(3/2)*x^5)

mupad [B] time = 0.15, size = 26, normalized size = 0.63

$$-\frac{4a\sqrt{x^2} + 5bx\sqrt{x^2}}{20c^{3/2}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(x^3*(c*x^2)^(3/2)), x)

[Out] -(4*a*(x^2)^(1/2) + 5*b*x*(x^2)^(1/2))/(20*c^(3/2)*x^6)

sympy [A] time = 0.93, size = 36, normalized size = 0.88

$$-\frac{a}{5c^{\frac{3}{2}}x^2(x^2)^{\frac{3}{2}}} - \frac{b}{4c^{\frac{3}{2}}x(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x**3/(c*x**2)**(3/2), x)

[Out] -a/(5*c**(3/2)*x**2*(x**2)**(3/2)) - b/(4*c**(3/2)*x*(x**2)**(3/2))

$$3.795 \quad \int \frac{a+bx}{x^4(cx^2)^{3/2}} dx$$

Optimal. Leaf size=41

$$-\frac{a}{6cx^5\sqrt{cx^2}} - \frac{b}{5cx^4\sqrt{cx^2}}$$

[Out] $-1/6*a/c/x^5/(c*x^2)^{(1/2)}-1/5*b/c/x^4/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a}{6cx^5\sqrt{cx^2}} - \frac{b}{5cx^4\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x^4*(c*x^2)^(3/2)), x]

[Out] $-a/(6*c*x^5*\text{Sqrt}[c*x^2]) - b/(5*c*x^4*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a + bx}{x^4 (cx^2)^{3/2}} dx &= \frac{x \int \frac{a+bx}{x^7} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^7} + \frac{b}{x^6} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{a}{6cx^5\sqrt{cx^2}} - \frac{b}{5cx^4\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.59

$$\frac{-5a - 6bx}{30x^3 (cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x^4*(c*x^2)^(3/2)), x]

[Out] (-5*a - 6*b*x)/(30*x^3*(c*x^2)^(3/2))

fricas [A] time = 0.51, size = 23, normalized size = 0.56

$$-\frac{\sqrt{cx^2} (6bx + 5a)}{30 c^2 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^4/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] -1/30*sqrt(c*x^2)*(6*b*x + 5*a)/(c^2*x^7)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^4/(c*x^2)^(3/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$-\frac{6bx + 5a}{30 (cx^2)^{\frac{3}{2}} x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/x^4/(c*x^2)^(3/2),x)`

[Out] $-1/30*(6*b*x+5*a)/x^3/(c*x^2)^(3/2)$

maxima [A] time = 1.35, size = 19, normalized size = 0.46

$$-\frac{b}{5c^{\frac{3}{2}}x^5} - \frac{a}{6c^{\frac{3}{2}}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^4/(c*x^2)^(3/2),x, algorithm="maxima")`

[Out] $-1/5*b/(c^(3/2)*x^5) - 1/6*a/(c^(3/2)*x^6)$

mupad [B] time = 0.15, size = 26, normalized size = 0.63

$$-\frac{5a\sqrt{x^2} + 6bx\sqrt{x^2}}{30c^{3/2}x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(x^4*(c*x^2)^(3/2)),x)`

[Out] $-(5*a*(x^2)^(1/2) + 6*b*x*(x^2)^(1/2))/(30*c^(3/2)*x^7)$

sympy [A] time = 1.16, size = 37, normalized size = 0.90

$$-\frac{a}{6c^{\frac{3}{2}}x^3(x^2)^{\frac{3}{2}}} - \frac{b}{5c^{\frac{3}{2}}x^2(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x**4/(c*x**2)**(3/2),x)`

[Out] $-a/(6*c**(3/2)*x**3*(x**2)**(3/2)) - b/(5*c**(3/2)*x**2*(x**2)**(3/2))$

$$3.796 \quad \int \frac{x^3(a+bx)}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=33

$$\frac{bx \log(x)}{c^2 \sqrt{cx^2}} - \frac{a}{c^2 \sqrt{cx^2}}$$

[Out] $-a/c^2/(c*x^2)^{(1/2)}+b*x*\ln(x)/c^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{bx \log(x)}{c^2 \sqrt{cx^2}} - \frac{a}{c^2 \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x^3*(a + b*x))/(c*x^2)^{(5/2)}, x]$

[Out] $-(a/(c^2*\text{Sqrt}[c*x^2])) + (b*x*\text{Log}[x])/(c^2*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[((a_*) + (b_*)*(x_))^{(m_*)}*((c_*) + (d_*)*(x_))^{(n_*)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3(a+bx)}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{a+bx}{x^2} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^2} + \frac{b}{x} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a}{c^2 \sqrt{cx^2}} + \frac{bx \log(x)}{c^2 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 0.67

$$\frac{bx \log(x) - a}{c^2 \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*(a + b*x))/(c*x^2)^(5/2),x]

[Out] (-a + b*x*Log[x])/(c^2*Sqrt[c*x^2])

fricas [A] time = 0.48, size = 23, normalized size = 0.70

$$\frac{\sqrt{cx^2} (bx \log(x) - a)}{c^3 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)/(c*x^2)^(5/2),x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x*log(x) - a)/(c^3*x^2)

giac [A] time = 1.02, size = 47, normalized size = 1.42

$$-\frac{b \log\left(\left|-\sqrt{c}x + \sqrt{cx^2}\right|\right) - \frac{2a\sqrt{c}}{\sqrt{c}x - \sqrt{cx^2}}}{c^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)/(c*x^2)^(5/2),x, algorithm="giac")

[Out] -(b*log(abs(-sqrt(c)*x + sqrt(c*x^2))) - 2*a*sqrt(c)/(sqrt(c)*x - sqrt(c*x^2)))/c^(5/2)

maple [A] time = 0.00, size = 21, normalized size = 0.64

$$\frac{(bx \ln(x) - a) x^4}{(c x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(b*x+a)/(c*x^2)^(5/2),x)`

[Out] `x^4*(b*x*ln(x)-a)/(c*x^2)^(5/2)`

maxima [A] time = 1.43, size = 24, normalized size = 0.73

$$-\frac{ax^2}{(cx^2)^{\frac{3}{2}}c} + \frac{b \log(x)}{c^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(b*x+a)/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] `-a*x^2/((c*x^2)^(3/2)*c) + b*log(x)/c^(5/2)`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^3 (a + bx)}{(c x^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x^3*(a + b*x))/(c*x^2)^(5/2),x)`

[Out] `int((x^3*(a + b*x))/(c*x^2)^(5/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^3 (a + bx)}{(c x^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(b*x+a)/(c*x**2)**(5/2),x)`

[Out] `Integral(x**3*(a + b*x)/(c*x**2)**(5/2), x)`

$$3.797 \quad \int \frac{x^2(a+bx)}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=29

$$-\frac{(a+bx)^2}{2ac^2x\sqrt{cx^2}}$$

[Out] $-1/2*(b*x+a)^2/a/c^2/x/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 37}

$$-\frac{(a+bx)^2}{2ac^2x\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x^2*(a + b*x))/(c*x^2)^{(5/2)}, x]$

[Out] $-(a + b*x)^2/(2*a*c^2*x*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] :> \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ $\text{FreeQ}\{a, m, n, x\}$ && $!\text{IntegerQ}[m]$

Rule 37

$\text{Int}[((a_.) + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] :> \text{Simp} [((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] /;$ $\text{FreeQ}\{a, b, c, d, m, n\}, x]$ && $\text{NeQ}[b*c - a*d, 0]$ && $\text{EqQ}[m + n + 2, 0]$ && $\text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int \frac{x^2(a+bx)}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{a+bx}{x^3} dx}{c^2\sqrt{cx^2}} \\ &= -\frac{(a+bx)^2}{2ac^2x\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.83

$$\frac{x^3(-a - 2bx)}{2(cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*(a + b*x))/(c*x^2)^(5/2), x]

[Out] (x^3*(-a - 2*b*x))/(2*(c*x^2)^(5/2))

fricas [A] time = 0.44, size = 21, normalized size = 0.72

$$-\frac{\sqrt{cx^2}(2bx + a)}{2c^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/2*sqrt(c*x^2)*(2*b*x + a)/(c^3*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)/(c*x^2)^(5/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 19, normalized size = 0.66

$$-\frac{(2bx + a)x^3}{2(cx^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)/(c*x^2)^(5/2), x)

[Out] -1/2*x^3*(2*b*x+a)/(c*x^2)^(5/2)

maxima [A] time = 1.34, size = 26, normalized size = 0.90

$$-\frac{bx^2}{(cx^2)^{\frac{3}{2}}c} - \frac{a}{2c^{\frac{5}{2}}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)/(c*x^2)^(5/2),x, algorithm="maxima")

[Out] -b*x^2/((c*x^2)^(3/2)*c) - 1/2*a/(c^(5/2)*x^2)

mupad [B] time = 0.15, size = 25, normalized size = 0.86

$$-\frac{2bx^3 + ax^2}{2c^{5/2}x(x^2)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^2*(a + b*x))/(c*x^2)^(5/2),x)

[Out] -(a*x^2 + 2*b*x^3)/(2*c^(5/2)*x*(x^2)^(3/2))

sympy [A] time = 0.93, size = 36, normalized size = 1.24

$$-\frac{ax^3}{2c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} - \frac{bx^4}{c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)/(c*x**2)**(5/2),x)

[Out] -a*x**3/(2*c**(5/2)*(x**2)**(5/2)) - b*x**4/(c**(5/2)*(x**2)**(5/2))

$$3.798 \quad \int \frac{x(a+bx)}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=41

$$-\frac{a}{3c^2x^2\sqrt{cx^2}} - \frac{b}{2c^2x\sqrt{cx^2}}$$

[Out] $-1/3*a/c^2/x^2/(c*x^2)^{(1/2)}-1/2*b/c^2/x/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {15, 43}

$$-\frac{a}{3c^2x^2\sqrt{cx^2}} - \frac{b}{2c^2x\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x*(a + b*x))/(c*x^2)^(5/2), x]

[Out] $-a/(3*c^2*x^2*\text{Sqrt}[c*x^2]) - b/(2*c^2*x*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x(a+bx)}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{a+bx}{x^4} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^4} + \frac{b}{x^3} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a}{3c^2 x^2 \sqrt{cx^2}} - \frac{b}{2c^2 x \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 0.59

$$\frac{x^2(-2a - 3bx)}{6(cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x*(a + b*x))/(c*x^2)^(5/2), x]

[Out] (x^2*(-2*a - 3*b*x))/(6*(c*x^2)^(5/2))

fricas [A] time = 0.44, size = 23, normalized size = 0.56

$$-\frac{\sqrt{cx^2}(3bx + 2a)}{6c^3x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/6*sqrt(c*x^2)*(3*b*x + 2*a)/(c^3*x^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)x}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)/(c*x^2)^(5/2), x, algorithm="giac")

[Out] integrate((b*x + a)*x/(c*x^2)^(5/2), x)

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$-\frac{(3bx + 2a)x^2}{6(c x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)/(c*x^2)^(5/2),x)`

[Out] `-1/6*x^2*(3*b*x+2*a)/(c*x^2)^(5/2)`

maxima [A] time = 1.39, size = 23, normalized size = 0.56

$$-\frac{a}{3(c x^2)^{\frac{3}{2}}c} - \frac{b}{2c^{\frac{5}{2}}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] `-1/3*a/((c*x^2)^(3/2)*c) - 1/2*b/(c^(5/2)*x^2)`

mupad [B] time = 0.15, size = 26, normalized size = 0.63

$$-\frac{2a\sqrt{x^2} + 3bx\sqrt{x^2}}{6c^{5/2}x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x*(a + b*x))/(c*x^2)^(5/2),x)`

[Out] `-(2*a*(x^2)^(1/2) + 3*b*x*(x^2)^(1/2))/(6*c^(5/2)*x^4)`

sympy [A] time = 0.92, size = 37, normalized size = 0.90

$$-\frac{ax^2}{3c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} - \frac{bx^3}{2c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)/(c*x**2)**(5/2),x)`

[Out] `-a*x**2/(3*c**(5/2)*(x**2)**(5/2)) - b*x**3/(2*c**(5/2)*(x**2)**(5/2))`

$$3.799 \quad \int \frac{a+bx}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=41

$$-\frac{a}{4c^2x^3\sqrt{cx^2}} - \frac{b}{3c^2x^2\sqrt{cx^2}}$$

[Out] $-1/4*a/c^2/x^3/(c*x^2)^{(1/2)}-1/3*b/c^2/x^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {15, 43}

$$-\frac{a}{4c^2x^3\sqrt{cx^2}} - \frac{b}{3c^2x^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(c*x^2)^(5/2), x]

[Out] $-a/(4*c^2*x^3*\text{Sqrt}[c*x^2]) - b/(3*c^2*x^2*\text{Sqrt}[c*x^2])$

Rule 15

```
Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]
```

Rule 43

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])
```

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{a+bx}{x^5} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^5} + \frac{b}{x^4} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a}{4c^2 x^3 \sqrt{cx^2}} - \frac{b}{3c^2 x^2 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 27, normalized size = 0.66

$$-\frac{\sqrt{cx^2} (3a + 4bx)}{12c^3 x^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(c*x^2)^(5/2), x]

[Out] -1/12*(Sqrt[c*x^2]*(3*a + 4*b*x))/(c^3*x^5)

fricas [A] time = 0.43, size = 23, normalized size = 0.56

$$-\frac{\sqrt{cx^2} (4bx + 3a)}{12c^3 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/12*sqrt(c*x^2)*(4*b*x + 3*a)/(c^3*x^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(c*x^2)^(5/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 19, normalized size = 0.46

$$-\frac{(4bx + 3a)x}{12(c x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/(c*x^2)^(5/2),x)`

[Out] `-1/12*x*(4*b*x+3*a)/(c*x^2)^(5/2)`

maxima [A] time = 1.37, size = 23, normalized size = 0.56

$$-\frac{b}{3(c^2)^{\frac{3}{2}}c} - \frac{a}{4c^{\frac{5}{2}}x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] `-1/3*b/((c*x^2)^(3/2)*c) - 1/4*a/(c^(5/2)*x^4)`

mupad [B] time = 0.16, size = 26, normalized size = 0.63

$$-\frac{3a\sqrt{x^2} + 4bx\sqrt{x^2}}{12c^{5/2}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(c*x^2)^(5/2),x)`

[Out] `-(3*a*(x^2)^(1/2) + 4*b*x*(x^2)^(1/2))/(12*c^(5/2)*x^5)`

sympy [A] time = 0.92, size = 36, normalized size = 0.88

$$-\frac{ax}{4c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} - \frac{bx^2}{3c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(c*x**2)**(5/2),x)`

[Out] `-a*x/(4*c**(5/2)*(x**2)**(5/2)) - b*x**2/(3*c**(5/2)*(x**2)**(5/2))`

$$3.800 \quad \int \frac{a+bx}{x(cx^2)^{5/2}} dx$$

Optimal. Leaf size=41

$$-\frac{a}{5c^2x^4\sqrt{cx^2}} - \frac{b}{4c^2x^3\sqrt{cx^2}}$$

[Out] $-1/5*a/c^2/x^4/(c*x^2)^{(1/2)}-1/4*b/c^2/x^3/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a}{5c^2x^4\sqrt{cx^2}} - \frac{b}{4c^2x^3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x*(c*x^2)^(5/2)), x]

[Out] $-a/(5*c^2*x^4*\text{Sqrt}[c*x^2]) - b/(4*c^2*x^3*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x(cx^2)^{5/2}} dx &= \frac{x \int \frac{a+bx}{x^6} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^6} + \frac{b}{x^5} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a}{5c^2 x^4 \sqrt{cx^2}} - \frac{b}{4c^2 x^3 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.66

$$-\frac{\sqrt{cx^2}(4a+5bx)}{20c^3x^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x*(c*x^2)^(5/2)), x]

[Out] -1/20*(Sqrt[c*x^2]*(4*a + 5*b*x))/(c^3*x^6)

fricas [A] time = 0.44, size = 23, normalized size = 0.56

$$-\frac{\sqrt{cx^2}(5bx+4a)}{20c^3x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/20*sqrt(c*x^2)*(5*b*x + 4*a)/(c^3*x^6)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{bx+a}{(cx^2)^{\frac{5}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x/(c*x^2)^(5/2), x, algorithm="giac")

[Out] integrate((b*x + a)/((c*x^2)^(5/2)*x), x)

maple [A] time = 0.00, size = 18, normalized size = 0.44

$$-\frac{5bx + 4a}{20(c x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/x/(c*x^2)^(5/2),x)`

[Out] `-1/20*(5*b*x+4*a)/(c*x^2)^(5/2)`

maxima [A] time = 1.33, size = 19, normalized size = 0.46

$$-\frac{b}{4c^{\frac{5}{2}}x^4} - \frac{a}{5c^{\frac{5}{2}}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] `-1/4*b/(c^(5/2)*x^4) - 1/5*a/(c^(5/2)*x^5)`

mupad [B] time = 0.16, size = 26, normalized size = 0.63

$$-\frac{4a\sqrt{x^2} + 5bx\sqrt{x^2}}{20c^{5/2}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(x*(c*x^2)^(5/2)),x)`

[Out] `-(4*a*(x^2)^(1/2) + 5*b*x*(x^2)^(1/2))/(20*c^(5/2)*x^6)`

sympy [A] time = 1.12, size = 32, normalized size = 0.78

$$-\frac{a}{5c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} - \frac{bx}{4c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x/(c*x**2)**(5/2),x)`

[Out] `-a/(5*c**(5/2)*(x**2)**(5/2)) - b*x/(4*c**(5/2)*(x**2)**(5/2))`

$$3.801 \quad \int \frac{a+bx}{x^2(cx^2)^{5/2}} dx$$

Optimal. Leaf size=41

$$-\frac{a}{6c^2x^5\sqrt{cx^2}} - \frac{b}{5c^2x^4\sqrt{cx^2}}$$

[Out] $-1/6*a/c^2/x^5/(c*x^2)^{(1/2)}-1/5*b/c^2/x^4/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a}{6c^2x^5\sqrt{cx^2}} - \frac{b}{5c^2x^4\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x^2*(c*x^2)^(5/2)), x]

[Out] $-a/(6*c^2*x^5*\text{Sqrt}[c*x^2]) - b/(5*c^2*x^4*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a + bx}{x^2 (cx^2)^{5/2}} dx &= \frac{x \int \frac{a+bx}{x^7} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^7} + \frac{b}{x^6} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a}{6c^2 x^5 \sqrt{cx^2}} - \frac{b}{5c^2 x^4 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.66

$$-\frac{\sqrt{cx^2} (5a + 6bx)}{30c^3 x^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x^2*(c*x^2)^(5/2)), x]

[Out] -1/30*(Sqrt[c*x^2]*(5*a + 6*b*x))/(c^3*x^7)

fricas [A] time = 0.44, size = 23, normalized size = 0.56

$$-\frac{\sqrt{cx^2} (6bx + 5a)}{30c^3 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^2/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/30*sqrt(c*x^2)*(6*b*x + 5*a)/(c^3*x^7)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^2/(c*x^2)^(5/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$-\frac{6bx + 5a}{30(c x^2)^{\frac{5}{2}} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/x^2/(c*x^2)^(5/2),x)`

[Out] $-1/30*(6*b*x+5*a)/x/(c*x^2)^{(5/2)}$

maxima [A] time = 1.32, size = 19, normalized size = 0.46

$$-\frac{b}{5c^{\frac{5}{2}}x^5} - \frac{a}{6c^{\frac{5}{2}}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^2/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] $-1/5*b/(c^{(5/2)}*x^5) - 1/6*a/(c^{(5/2)}*x^6)$

mupad [B] time = 0.16, size = 26, normalized size = 0.63

$$-\frac{5a\sqrt{x^2} + 6bx\sqrt{x^2}}{30c^{5/2}x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(x^2*(c*x^2)^(5/2)),x)`

[Out] $-(5*a*(x^2)^{(1/2)} + 6*b*x*(x^2)^{(1/2)})/(30*c^{(5/2)}*x^7)$

sympy [A] time = 1.34, size = 32, normalized size = 0.78

$$-\frac{a}{6c^{\frac{5}{2}}x(x^2)^{\frac{5}{2}}} - \frac{b}{5c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x**2/(c*x**2)**(5/2),x)`

[Out] $-a/(6*c^{(5/2)}*x*(x**2)^{(5/2)}) - b/(5*c^{(5/2)}*(x**2)^{(5/2)})$

$$3.802 \quad \int \frac{a+bx}{x^3(cx^2)^{5/2}} dx$$

Optimal. Leaf size=41

$$-\frac{a}{7c^2x^6\sqrt{cx^2}} - \frac{b}{6c^2x^5\sqrt{cx^2}}$$

[Out] $-1/7*a/c^2/x^6/(c*x^2)^{(1/2)}-1/6*b/c^2/x^5/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a}{7c^2x^6\sqrt{cx^2}} - \frac{b}{6c^2x^5\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x^3*(c*x^2)^(5/2)), x]

[Out] $-a/(7*c^2*x^6*\text{Sqrt}[c*x^2]) - b/(6*c^2*x^5*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{x^3(cx^2)^{5/2}} dx &= \frac{x \int \frac{a+bx}{x^8} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^8} + \frac{b}{x^7} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a}{7c^2 x^6 \sqrt{cx^2}} - \frac{b}{6c^2 x^5 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 0.54

$$\frac{c(-6a - 7bx)}{42 (cx^2)^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x^3*(c*x^2)^(5/2)), x]

[Out] (c*(-6*a - 7*b*x))/(42*(c*x^2)^(7/2))

fricas [A] time = 0.42, size = 23, normalized size = 0.56

$$-\frac{\sqrt{cx^2} (7bx + 6a)}{42 c^3 x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/42*sqrt(c*x^2)*(7*b*x + 6*a)/(c^3*x^8)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{bx+a}{(cx^2)^{\frac{5}{2}} x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3/(c*x^2)^(5/2), x, algorithm="giac")

[Out] integrate((b*x + a)/((c*x^2)^(5/2)*x^3), x)

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$-\frac{7bx + 6a}{42 \left(cx^2 \right)^{\frac{5}{2}} x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/x^3/(c*x^2)^(5/2),x)

[Out] -1/42*(7*b*x+6*a)/x^2/(c*x^2)^(5/2)

maxima [A] time = 1.37, size = 19, normalized size = 0.46

$$-\frac{b}{6c^{\frac{5}{2}}x^6} - \frac{a}{7c^{\frac{5}{2}}x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^3/(c*x^2)^(5/2),x, algorithm="maxima")

[Out] -1/6*b/(c^(5/2)*x^6) - 1/7*a/(c^(5/2)*x^7)

mupad [B] time = 0.16, size = 26, normalized size = 0.63

$$-\frac{6a\sqrt{x^2} + 7bx\sqrt{x^2}}{42c^{5/2}x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(x^3*(c*x^2)^(5/2)),x)

[Out] -(6*a*(x^2)^(1/2) + 7*b*x*(x^2)^(1/2))/(42*c^(5/2)*x^8)

sympy [A] time = 1.64, size = 36, normalized size = 0.88

$$-\frac{a}{7c^{\frac{5}{2}}x^2 \left(x^2 \right)^{\frac{5}{2}}} - \frac{b}{6c^{\frac{5}{2}}x \left(x^2 \right)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x**3/(c*x**2)**(5/2),x)

[Out] -a/(7*c**(5/2)*x**2*(x**2)**(5/2)) - b/(6*c**(5/2)*x*(x**2)**(5/2))

$$3.803 \quad \int \frac{a+bx}{x^4(cx^2)^{5/2}} dx$$

Optimal. Leaf size=41

$$-\frac{a}{8c^2x^7\sqrt{cx^2}} - \frac{b}{7c^2x^6\sqrt{cx^2}}$$

[Out] $-1/8*a/c^2/x^7/(c*x^2)^{(1/2)}-1/7*b/c^2/x^6/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a}{8c^2x^7\sqrt{cx^2}} - \frac{b}{7c^2x^6\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(x^4*(c*x^2)^(5/2)), x]

[Out] $-a/(8*c^2*x^7*\text{Sqrt}[c*x^2]) - b/(7*c^2*x^6*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a + bx}{x^4 (cx^2)^{5/2}} dx &= \frac{x \int \frac{a+bx}{x^9} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a}{x^9} + \frac{b}{x^8} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a}{8c^2 x^7 \sqrt{cx^2}} - \frac{b}{7c^2 x^6 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.59

$$\frac{-7a - 8bx}{56x^3 (cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(x^4*(c*x^2)^(5/2)), x]

[Out] (-7*a - 8*b*x)/(56*x^3*(c*x^2)^(5/2))

fricas [A] time = 0.50, size = 23, normalized size = 0.56

$$-\frac{\sqrt{cx^2} (8bx + 7a)}{56c^3x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^4/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/56*sqrt(c*x^2)*(8*b*x + 7*a)/(c^3*x^9)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/x^4/(c*x^2)^(5/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 21, normalized size = 0.51

$$-\frac{8bx + 7a}{56 (cx^2)^{\frac{5}{2}} x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/x^4/(c*x^2)^(5/2),x)`

[Out] $-1/56*(8*b*x+7*a)/x^3/(c*x^2)^(5/2)$

maxima [A] time = 1.34, size = 19, normalized size = 0.46

$$-\frac{b}{7c^{\frac{5}{2}}x^7} - \frac{a}{8c^{\frac{5}{2}}x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x^4/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] $-1/7*b/(c^(5/2)*x^7) - 1/8*a/(c^(5/2)*x^8)$

mupad [B] time = 0.16, size = 26, normalized size = 0.63

$$-\frac{7a\sqrt{x^2} + 8bx\sqrt{x^2}}{56c^{5/2}x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(x^4*(c*x^2)^(5/2)),x)`

[Out] $-(7*a*(x^2)^(1/2) + 8*b*x*(x^2)^(1/2))/(56*c^(5/2)*x^9)$

sympy [A] time = 1.97, size = 37, normalized size = 0.90

$$-\frac{a}{8c^{\frac{5}{2}}x^3(x^2)^{\frac{5}{2}}} - \frac{b}{7c^{\frac{5}{2}}x^2(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/x**4/(c*x**2)**(5/2),x)`

[Out] $-a/(8*c**(5/2)*x**3*(x**2)**(5/2)) - b/(7*c**(5/2)*x**2*(x**2)**(5/2))$

3.804 $\int x^3 \sqrt{cx^2} (a + bx)^2 dx$

Optimal. Leaf size=57

$$\frac{1}{5}a^2x^4\sqrt{cx^2} + \frac{1}{3}abx^5\sqrt{cx^2} + \frac{1}{7}b^2x^6\sqrt{cx^2}$$

[Out] $1/5*a^2*x^4*(c*x^2)^(1/2)+1/3*a*b*x^5*(c*x^2)^(1/2)+1/7*b^2*x^6*(c*x^2)^(1/2)$

Rubi [A] time = 0.02, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{1}{5}a^2x^4\sqrt{cx^2} + \frac{1}{3}abx^5\sqrt{cx^2} + \frac{1}{7}b^2x^6\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*\text{Sqrt}[c*x^2]*(a + b*x)^2,x]$

[Out] $(a^2*x^4*\text{Sqrt}[c*x^2])/5 + (a*b*x^5*\text{Sqrt}[c*x^2])/3 + (b^2*x^6*\text{Sqrt}[c*x^2])/7$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^(n_))^(m_), x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_*) + (b_*)*(x_)^(m_)*((c_*) + (d_*)*(x_)^(n_)), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^3 \sqrt{cx^2} (a + bx)^2 dx &= \frac{\sqrt{cx^2} \int x^4 (a + bx)^2 dx}{x} \\ &= \frac{\sqrt{cx^2} \int (a^2x^4 + 2abx^5 + b^2x^6) dx}{x} \\ &= \frac{1}{5}a^2x^4\sqrt{cx^2} + \frac{1}{3}abx^5\sqrt{cx^2} + \frac{1}{7}b^2x^6\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.61

$$\frac{1}{105}x^4\sqrt{cx^2} (21a^2 + 35abx + 15b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[x^3*Sqrt[c*x^2]*(a + b*x)^2,x]

[Out] (x^4*Sqrt[c*x^2]*(21*a^2 + 35*a*b*x + 15*b^2*x^2))/105

fricas [A] time = 0.41, size = 33, normalized size = 0.58

$$\frac{1}{105} (15b^2x^6 + 35abx^5 + 21a^2x^4)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2*(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/105*(15*b^2*x^6 + 35*a*b*x^5 + 21*a^2*x^4)*sqrt(c*x^2)

giac [A] time = 1.08, size = 35, normalized size = 0.61

$$\frac{1}{105} (15b^2x^7\operatorname{sgn}(x) + 35abx^6\operatorname{sgn}(x) + 21a^2x^5\operatorname{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2*(c*x^2)^(1/2),x, algorithm="giac")

[Out] 1/105*(15*b^2*x^7*sgn(x) + 35*a*b*x^6*sgn(x) + 21*a^2*x^5*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 32, normalized size = 0.56

$$\frac{(15b^2x^2 + 35abx + 21a^2)\sqrt{cx^2}x^4}{105}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^2*(c*x^2)^(1/2),x)

[Out] 1/105*x^4*(15*b^2*x^2+35*a*b*x+21*a^2)*(c*x^2)^(1/2)

maxima [A] time = 1.39, size = 54, normalized size = 0.95

$$\frac{(cx^2)^{\frac{3}{2}}b^2x^4}{7c} + \frac{(cx^2)^{\frac{3}{2}}abx^3}{3c} + \frac{(cx^2)^{\frac{3}{2}}a^2x^2}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(b*x+a)^2*(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $1/7*(c*x^2)^{(3/2)}*b^2*x^4/c + 1/3*(c*x^2)^{(3/2)}*a*b*x^3/c + 1/5*(c*x^2)^{(3/2)}*a^2*x^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^3 \sqrt{c x^2} (a + b x)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(c*x^2)^(1/2)*(a + b*x)^2,x)`

[Out] `int(x^3*(c*x^2)^(1/2)*(a + b*x)^2, x)`

sympy [A] time = 0.59, size = 60, normalized size = 1.05

$$\frac{a^2 \sqrt{c} x^4 \sqrt{x^2}}{5} + \frac{ab \sqrt{c} x^5 \sqrt{x^2}}{3} + \frac{b^2 \sqrt{c} x^6 \sqrt{x^2}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(b*x+a)**2*(c*x**2)**(1/2),x)`

[Out] $a**2*\text{sqrt}(c)*x**4*\text{sqrt}(x**2)/5 + a*b*\text{sqrt}(c)*x**5*\text{sqrt}(x**2)/3 + b**2*\text{sqrt}(c)*x**6*\text{sqrt}(x**2)/7$

3.805 $\int x^2 \sqrt{cx^2} (a + bx)^2 dx$

Optimal. Leaf size=57

$$\frac{1}{4}a^2x^3\sqrt{cx^2} + \frac{2}{5}abx^4\sqrt{cx^2} + \frac{1}{6}b^2x^5\sqrt{cx^2}$$

[Out] $1/4*a^2*x^3*(c*x^2)^(1/2)+2/5*a*b*x^4*(c*x^2)^(1/2)+1/6*b^2*x^5*(c*x^2)^(1/2)$

Rubi [A] time = 0.01, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{1}{4}a^2x^3\sqrt{cx^2} + \frac{2}{5}abx^4\sqrt{cx^2} + \frac{1}{6}b^2x^5\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[x^2*Sqrt[c*x^2]*(a + b*x)^2,x]

[Out] $(a^2*x^3*\text{Sqrt}[c*x^2])/4 + (2*a*b*x^4*\text{Sqrt}[c*x^2])/5 + (b^2*x^5*\text{Sqrt}[c*x^2])/6$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2 \sqrt{cx^2} (a + bx)^2 dx &= \frac{\sqrt{cx^2} \int x^3 (a + bx)^2 dx}{x} \\ &= \frac{\sqrt{cx^2} \int (a^2 x^3 + 2abx^4 + b^2 x^5) dx}{x} \\ &= \frac{1}{4} a^2 x^3 \sqrt{cx^2} + \frac{2}{5} abx^4 \sqrt{cx^2} + \frac{1}{6} b^2 x^5 \sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.61

$$\frac{1}{60} x^3 \sqrt{cx^2} (15a^2 + 24abx + 10b^2 x^2)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*Sqrt[c*x^2]*(a + b*x)^2,x]

[Out] (x^3*Sqrt[c*x^2]*(15*a^2 + 24*a*b*x + 10*b^2*x^2))/60

fricas [A] time = 0.45, size = 33, normalized size = 0.58

$$\frac{1}{60} (10 b^2 x^5 + 24 abx^4 + 15 a^2 x^3) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2*(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/60*(10*b^2*x^5 + 24*a*b*x^4 + 15*a^2*x^3)*sqrt(c*x^2)

giac [A] time = 1.04, size = 35, normalized size = 0.61

$$\frac{1}{60} (10 b^2 x^6 \operatorname{sgn}(x) + 24 abx^5 \operatorname{sgn}(x) + 15 a^2 x^4 \operatorname{sgn}(x)) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2*(c*x^2)^(1/2),x, algorithm="giac")

[Out] 1/60*(10*b^2*x^6*sgn(x) + 24*a*b*x^5*sgn(x) + 15*a^2*x^4*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 32, normalized size = 0.56

$$\frac{(10b^2x^2 + 24abx + 15a^2) \sqrt{cx^2} x^3}{60}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(b*x+a)^2*(c*x^2)^(1/2),x)`

[Out] `1/60*x^3*(10*b^2*x^2+24*a*b*x+15*a^2)*(c*x^2)^(1/2)`

maxima [A] time = 1.35, size = 52, normalized size = 0.91

$$\frac{(cx^2)^{\frac{3}{2}} b^2 x^3}{6c} + \frac{2 (cx^2)^{\frac{3}{2}} abx^2}{5c} + \frac{(cx^2)^{\frac{3}{2}} a^2 x}{4c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(b*x+a)^2*(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] `1/6*(c*x^2)^(3/2)*b^2*x^3/c + 2/5*(c*x^2)^(3/2)*a*b*x^2/c + 1/4*(c*x^2)^(3/2)*a^2*x/c`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^2 \sqrt{cx^2} (a + bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(c*x^2)^(1/2)*(a + b*x)^2,x)`

[Out] `int(x^2*(c*x^2)^(1/2)*(a + b*x)^2, x)`

sympy [A] time = 0.46, size = 61, normalized size = 1.07

$$\frac{a^2 \sqrt{c} x^3 \sqrt{x^2}}{4} + \frac{2ab \sqrt{c} x^4 \sqrt{x^2}}{5} + \frac{b^2 \sqrt{c} x^5 \sqrt{x^2}}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(b*x+a)**2*(c*x**2)**(1/2),x)`

[Out] `a**2*sqrt(c)*x**3*sqrt(x**2)/4 + 2*a*b*sqrt(c)*x**4*sqrt(x**2)/5 + b**2*sqrt(c)*x**5*sqrt(x**2)/6`

3.806 $\int x\sqrt{cx^2} (a + bx)^2 dx$

Optimal. Leaf size=57

$$\frac{1}{3}a^2x^2\sqrt{cx^2} + \frac{1}{2}abx^3\sqrt{cx^2} + \frac{1}{5}b^2x^4\sqrt{cx^2}$$

[Out] $1/3*a^2*x^2*(c*x^2)^{(1/2)}+1/2*a*b*x^3*(c*x^2)^{(1/2)}+1/5*b^2*x^4*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{3}a^2x^2\sqrt{cx^2} + \frac{1}{2}abx^3\sqrt{cx^2} + \frac{1}{5}b^2x^4\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] `Int[x*Sqrt[c*x^2]*(a + b*x)^2,x]`

[Out] $(a^2*x^2*\text{Sqrt}[c*x^2])/3 + (a*b*x^3*\text{Sqrt}[c*x^2])/2 + (b^2*x^4*\text{Sqrt}[c*x^2])/5$

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rule 43

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])`

Rubi steps

$$\begin{aligned} \int x\sqrt{cx^2} (a + bx)^2 dx &= \frac{\sqrt{cx^2} \int x^2(a + bx)^2 dx}{x} \\ &= \frac{\sqrt{cx^2} \int (a^2x^2 + 2abx^3 + b^2x^4) dx}{x} \\ &= \frac{1}{3}a^2x^2\sqrt{cx^2} + \frac{1}{2}abx^3\sqrt{cx^2} + \frac{1}{5}b^2x^4\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.61

$$\frac{1}{30}x^2\sqrt{cx^2} (10a^2 + 15abx + 6b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[x*Sqrt[c*x^2]*(a + b*x)^2,x]

[Out] (x^2*Sqrt[c*x^2]*(10*a^2 + 15*a*b*x + 6*b^2*x^2))/30

fricas [A] time = 0.42, size = 33, normalized size = 0.58

$$\frac{1}{30} (6b^2x^4 + 15abx^3 + 10a^2x^2)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2*(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/30*(6*b^2*x^4 + 15*a*b*x^3 + 10*a^2*x^2)*sqrt(c*x^2)

giac [A] time = 1.11, size = 35, normalized size = 0.61

$$\frac{1}{30} (6b^2x^5\text{sgn}(x) + 15abx^4\text{sgn}(x) + 10a^2x^3\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2*(c*x^2)^(1/2),x, algorithm="giac")

[Out] 1/30*(6*b^2*x^5*sgn(x) + 15*a*b*x^4*sgn(x) + 10*a^2*x^3*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 32, normalized size = 0.56

$$\frac{(6b^2x^2 + 15abx + 10a^2)\sqrt{cx^2}x^2}{30}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^2*(c*x^2)^(1/2),x)

[Out] 1/30*x^2*(6*b^2*x^2+15*a*b*x+10*a^2)*(c*x^2)^(1/2)

maxima [A] time = 1.31, size = 49, normalized size = 0.86

$$\frac{(cx^2)^{\frac{3}{2}}b^2x^2}{5c} + \frac{(cx^2)^{\frac{3}{2}}abx}{2c} + \frac{(cx^2)^{\frac{3}{2}}a^2}{3c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^2*(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $1/5*(c*x^2)^{(3/2)}*b^2*x^2/c + 1/2*(c*x^2)^{(3/2)}*a*b*x/c + 1/3*(c*x^2)^{(3/2)}*a^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x \sqrt{c x^2} (a + b x)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(1/2)*(a + b*x)^2,x)`

[Out] `int(x*(c*x^2)^(1/2)*(a + b*x)^2, x)`

sympy [A] time = 0.37, size = 60, normalized size = 1.05

$$\frac{a^2 \sqrt{c} x^2 \sqrt{x^2}}{3} + \frac{ab \sqrt{c} x^3 \sqrt{x^2}}{2} + \frac{b^2 \sqrt{c} x^4 \sqrt{x^2}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**2*(c*x**2)**(1/2),x)`

[Out] `a**2*sqrt(c)*x**2*sqrt(x**2)/3 + a*b*sqrt(c)*x**3*sqrt(x**2)/2 + b**2*sqrt(c)*x**4*sqrt(x**2)/5`

3.807 $\int \sqrt{cx^2} (a + bx)^2 dx$

Optimal. Leaf size=55

$$\frac{1}{2}a^2x\sqrt{cx^2} + \frac{2}{3}abx^2\sqrt{cx^2} + \frac{1}{4}b^2x^3\sqrt{cx^2}$$

[Out] $1/2*a^2*x*(c*x^2)^(1/2)+2/3*a*b*x^2*(c*x^2)^(1/2)+1/4*b^2*x^3*(c*x^2)^(1/2)$

Rubi [A] time = 0.01, antiderivative size = 55, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$\frac{1}{2}a^2x\sqrt{cx^2} + \frac{2}{3}abx^2\sqrt{cx^2} + \frac{1}{4}b^2x^3\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c*x^2]*(a + b*x)^2,x]

[Out] $(a^2*x*\text{Sqrt}[c*x^2])/2 + (2*a*b*x^2*\text{Sqrt}[c*x^2])/3 + (b^2*x^3*\text{Sqrt}[c*x^2])/4$

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \sqrt{cx^2} (a + bx)^2 dx &= \frac{\sqrt{cx^2} \int x(a + bx)^2 dx}{x} \\ &= \frac{\sqrt{cx^2} \int (a^2x + 2abx^2 + b^2x^3) dx}{x} \\ &= \frac{1}{2}a^2x\sqrt{cx^2} + \frac{2}{3}abx^2\sqrt{cx^2} + \frac{1}{4}b^2x^3\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.60

$$\frac{1}{12}x\sqrt{cx^2} (6a^2 + 8abx + 3b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]*(a + b*x)^2,x]

[Out] (x*Sqrt[c*x^2]*(6*a^2 + 8*a*b*x + 3*b^2*x^2))/12

fricas [A] time = 0.44, size = 31, normalized size = 0.56

$$\frac{1}{12} (3b^2x^3 + 8abx^2 + 6a^2x)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/12*(3*b^2*x^3 + 8*a*b*x^2 + 6*a^2*x)*sqrt(c*x^2)

giac [A] time = 0.95, size = 35, normalized size = 0.64

$$\frac{1}{12} (3b^2x^4\text{sgn}(x) + 8abx^3\text{sgn}(x) + 6a^2x^2\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2),x, algorithm="giac")

[Out] 1/12*(3*b^2*x^4*sgn(x) + 8*a*b*x^3*sgn(x) + 6*a^2*x^2*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 30, normalized size = 0.55

$$\frac{(3b^2x^2 + 8abx + 6a^2)\sqrt{cx^2}x}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(c*x^2)^(1/2),x)

[Out] 1/12*x*(3*b^2*x^2+8*a*b*x+6*a^2)*(c*x^2)^(1/2)

maxima [A] time = 1.35, size = 44, normalized size = 0.80

$$\frac{1}{2}\sqrt{cx^2}a^2x + \frac{(cx^2)^{\frac{3}{2}}b^2x}{4c} + \frac{2(cx^2)^{\frac{3}{2}}ab}{3c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2),x, algorithm="maxima")

[Out] 1/2*sqrt(c*x^2)*a^2*x + 1/4*(c*x^2)^(3/2)*b^2*x/c + 2/3*(c*x^2)^(3/2)*a*b/c

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \sqrt{cx^2} (a + bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)*(a + b*x)^2,x)

[Out] int((c*x^2)^(1/2)*(a + b*x)^2, x)

sympy [A] time = 0.30, size = 60, normalized size = 1.09

$$\frac{a^2\sqrt{c}x\sqrt{x^2}}{2} + \frac{2ab\sqrt{c}x^2\sqrt{x^2}}{3} + \frac{b^2\sqrt{c}x^3\sqrt{x^2}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2*(c*x**2)**(1/2),x)

[Out] a**2*sqrt(c)*x*sqrt(x**2)/2 + 2*a*b*sqrt(c)*x**2*sqrt(x**2)/3 + b**2*sqrt(c)*x**3*sqrt(x**2)/4

$$3.808 \quad \int \frac{\sqrt{cx^2} (a+bx)^2}{x} dx$$

Optimal. Leaf size=26

$$\frac{\sqrt{cx^2} (a + bx)^3}{3bx}$$

[Out] 1/3*(b*x+a)^3*(c*x^2)^(1/2)/b/x

Rubi [A] time = 0.00, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$\frac{\sqrt{cx^2} (a + bx)^3}{3bx}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x)^2)/x,x]

[Out] (Sqrt[c*x^2]*(a + b*x)^3)/(3*b*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2} (a + bx)^2}{x} dx &= \frac{\sqrt{cx^2} \int (a + bx)^2 dx}{x} \\ &= \frac{\sqrt{cx^2} (a + bx)^3}{3bx} \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 0.96

$$\frac{cx(a + bx)^3}{3b\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x)^2)/x,x]

[Out] (c*x*(a + b*x)^3)/(3*b*Sqrt[c*x^2])

fricas [A] time = 0.44, size = 27, normalized size = 1.04

$$\frac{1}{3} (b^2 x^2 + 3 a b x + 3 a^2) \sqrt{c x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2)/x,x, algorithm="fricas")

[Out] 1/3*(b^2*x^2 + 3*a*b*x + 3*a^2)*sqrt(c*x^2)

giac [A] time = 0.97, size = 29, normalized size = 1.12

$$\frac{1}{3} \left(\frac{(b x + a)^3 \operatorname{sgn}(x)}{b} - \frac{a^3 \operatorname{sgn}(x)}{b} \right) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2)/x,x, algorithm="giac")

[Out] 1/3*((b*x + a)^3*sgn(x)/b - a^3*sgn(x)/b)*sqrt(c)

maple [A] time = 0.00, size = 28, normalized size = 1.08

$$\frac{(b^2 x^2 + 3 a b x + 3 a^2) \sqrt{c x^2}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(c*x^2)^(1/2)/x,x)

[Out] 1/3*(b^2*x^2+3*a*b*x+3*a^2)*(c*x^2)^(1/2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2)/x,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{\sqrt{cx^2} (a + bx)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(1/2)*(a + b*x)^2)/x, x)

[Out] int(((c*x^2)^(1/2)*(a + b*x)^2)/x, x)

sympy [B] time = 0.30, size = 51, normalized size = 1.96

$$a^2\sqrt{c}\sqrt{x^2} + ab\sqrt{c}x\sqrt{x^2} + \frac{b^2\sqrt{c}x^2\sqrt{x^2}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2*(c*x**2)**(1/2)/x, x)

[Out] a**2*sqrt(c)*sqrt(x**2) + a*b*sqrt(c)*x*sqrt(x**2) + b**2*sqrt(c)*x**2*sqrt(x**2)/3

$$3.809 \quad \int \frac{\sqrt{cx^2} (a+bx)^2}{x^2} dx$$

Optimal. Leaf size=49

$$\frac{a^2\sqrt{cx^2} \log(x)}{x} + 2ab\sqrt{cx^2} + \frac{1}{2}b^2x\sqrt{cx^2}$$

[Out] 2*a*b*(c*x^2)^(1/2)+1/2*b^2*x*(c*x^2)^(1/2)+a^2*ln(x)*(c*x^2)^(1/2)/x

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2\sqrt{cx^2} \log(x)}{x} + 2ab\sqrt{cx^2} + \frac{1}{2}b^2x\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x)^2)/x^2,x]

[Out] 2*a*b*Sqrt[c*x^2] + (b^2*x*Sqrt[c*x^2])/2 + (a^2*Sqrt[c*x^2]*Log[x])/x

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_)^(m_.))*((c_.) + (d_.)*(x_)^(n_.)), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2} (a + bx)^2}{x^2} dx &= \frac{\sqrt{cx^2} \int \frac{(a+bx)^2}{x} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(2ab + \frac{a^2}{x} + b^2x\right) dx}{x} \\ &= 2ab\sqrt{cx^2} + \frac{1}{2}b^2x\sqrt{cx^2} + \frac{a^2\sqrt{cx^2} \log(x)}{x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.67

$$\frac{cx(2a^2 \log(x) + bx(4a + bx))}{2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x)^2)/x^2,x]

[Out] (c*x*(b*x*(4*a + b*x) + 2*a^2*Log[x]))/(2*Sqrt[c*x^2])

fricas [A] time = 0.45, size = 32, normalized size = 0.65

$$\frac{(b^2x^2 + 4abx + 2a^2 \log(x))\sqrt{cx^2}}{2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2)/x^2,x, algorithm="fricas")

[Out] 1/2*(b^2*x^2 + 4*a*b*x + 2*a^2*log(x))*sqrt(c*x^2)/x

giac [A] time = 1.08, size = 32, normalized size = 0.65

$$\frac{1}{2} (b^2x^2 \operatorname{sgn}(x) + 4abx \operatorname{sgn}(x) + 2a^2 \log(|x|) \operatorname{sgn}(x)) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2)/x^2,x, algorithm="giac")

[Out] 1/2*(b^2*x^2*sgn(x) + 4*a*b*x*sgn(x) + 2*a^2*log(abs(x))*sgn(x))*sqrt(c)

maple [A] time = 0.01, size = 33, normalized size = 0.67

$$\frac{\sqrt{cx^2} (b^2x^2 + 2a^2 \ln(x) + 4abx)}{2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2*(c*x^2)^(1/2)/x^2,x)`

[Out] `1/2*(c*x^2)^(1/2)*(b^2*x^2+2*a^2*ln(x)+4*a*b*x)/x`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2*(c*x^2)^(1/2)/x^2,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{cx^2} (a + bx)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(1/2)*(a + b*x)^2)/x^2,x)`

[Out] `int(((c*x^2)^(1/2)*(a + b*x)^2)/x^2, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (a + bx)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(c*x**2)**(1/2)/x**2,x)`

[Out] `Integral(sqrt(c*x**2)*(a + b*x)**2/x**2, x)`

$$3.810 \quad \int \frac{\sqrt{cx^2} (a+bx)^2}{x^3} dx$$

Optimal. Leaf size=49

$$-\frac{a^2\sqrt{cx^2}}{x^2} + \frac{2ab\sqrt{cx^2} \log(x)}{x} + b^2\sqrt{cx^2}$$

[Out] $b^2*(c*x^2)^{(1/2)} - a^2*(c*x^2)^{(1/2)}/x^2 + 2*a*b*\ln(x)*(c*x^2)^{(1/2)}/x$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2\sqrt{cx^2}}{x^2} + \frac{2ab\sqrt{cx^2} \log(x)}{x} + b^2\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x)^2)/x^3,x]

[Out] $b^2*\text{Sqrt}[c*x^2] - (a^2*\text{Sqrt}[c*x^2])/x^2 + (2*a*b*\text{Sqrt}[c*x^2]*\text{Log}[x])/x$

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2} (a + bx)^2}{x^3} dx &= \frac{\sqrt{cx^2} \int \frac{(a+bx)^2}{x^2} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(b^2 + \frac{a^2}{x^2} + \frac{2ab}{x} \right) dx}{x} \\ &= b^2 \sqrt{cx^2} - \frac{a^2 \sqrt{cx^2}}{x^2} + \frac{2ab \sqrt{cx^2} \log(x)}{x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 0.63

$$\frac{c(-a^2 + 2abx \log(x) + b^2x^2)}{\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x)^2)/x^3,x]

[Out] (c*(-a^2 + b^2*x^2 + 2*a*b*x*Log[x]))/Sqrt[c*x^2]

fricas [A] time = 0.44, size = 31, normalized size = 0.63

$$\frac{(b^2x^2 + 2abx \log(x) - a^2)\sqrt{cx^2}}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2)/x^3,x, algorithm="fricas")

[Out] (b^2*x^2 + 2*a*b*x*log(x) - a^2)*sqrt(c*x^2)/x^2

giac [A] time = 1.02, size = 31, normalized size = 0.63

$$\left(b^2x \operatorname{sgn}(x) + 2ab \log(|x|) \operatorname{sgn}(x) - \frac{a^2 \operatorname{sgn}(x)}{x} \right) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2)/x^3,x, algorithm="giac")

[Out] (b^2*x*sgn(x) + 2*a*b*log(abs(x))*sgn(x) - a^2*sgn(x)/x)*sqrt(c)

maple [A] time = 0.01, size = 32, normalized size = 0.65

$$\frac{\sqrt{cx^2} (2abx \ln(x) + b^2x^2 - a^2)}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2*(c*x^2)^(1/2)/x^3,x)`

[Out] `(c*x^2)^(1/2)*(2*a*b*ln(x)*x+b^2*x^2-a^2)/x^2`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2*(c*x^2)^(1/2)/x^3,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{cx^2} (a + bx)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(1/2)*(a + b*x)^2)/x^3,x)`

[Out] `int(((c*x^2)^(1/2)*(a + b*x)^2)/x^3, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (a + bx)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(c*x**2)**(1/2)/x**3,x)`

[Out] `Integral(sqrt(c*x**2)*(a + b*x)**2/x**3, x)`

$$3.811 \quad \int \frac{\sqrt{cx^2} (a+bx)^2}{x^4} dx$$

Optimal. Leaf size=54

$$-\frac{a^2\sqrt{cx^2}}{2x^3} - \frac{2ab\sqrt{cx^2}}{x^2} + \frac{b^2\sqrt{cx^2} \log(x)}{x}$$

[Out] $-1/2*a^2*(c*x^2)^{(1/2)}/x^3-2*a*b*(c*x^2)^{(1/2)}/x^2+b^2*\ln(x)*(c*x^2)^{(1/2)}/x$

Rubi [A] time = 0.01, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2\sqrt{cx^2}}{2x^3} - \frac{2ab\sqrt{cx^2}}{x^2} + \frac{b^2\sqrt{cx^2} \log(x)}{x}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x)^2)/x^4, x]

[Out] $-(a^2*\text{Sqrt}[c*x^2])/(2*x^3) - (2*a*b*\text{Sqrt}[c*x^2])/x^2 + (b^2*\text{Sqrt}[c*x^2]*\text{Log}[x])/x$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2} (a + bx)^2}{x^4} dx &= \frac{\sqrt{cx^2} \int \frac{(a+bx)^2}{x^3} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(\frac{a^2}{x^3} + \frac{2ab}{x^2} + \frac{b^2}{x} \right) dx}{x} \\ &= -\frac{a^2 \sqrt{cx^2}}{2x^3} - \frac{2ab \sqrt{cx^2}}{x^2} + \frac{b^2 \sqrt{cx^2} \log(x)}{x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 36, normalized size = 0.67

$$\frac{\sqrt{cx^2} (2b^2x^2 \log(x) - a(a + 4bx))}{2x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x)^2)/x^4,x]

[Out] (Sqrt[c*x^2]*(-(a*(a + 4*b*x)) + 2*b^2*x^2*Log[x]))/(2*x^3)

fricas [A] time = 0.45, size = 33, normalized size = 0.61

$$\frac{(2b^2x^2 \log(x) - 4abx - a^2)\sqrt{cx^2}}{2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2)/x^4,x, algorithm="fricas")

[Out] 1/2*(2*b^2*x^2*log(x) - 4*a*b*x - a^2)*sqrt(c*x^2)/x^3

giac [A] time = 0.99, size = 35, normalized size = 0.65

$$\frac{1}{2} \left(2b^2 \log(|x|) \operatorname{sgn}(x) - \frac{4abx \operatorname{sgn}(x) + a^2 \operatorname{sgn}(x)}{x^2} \right) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(c*x^2)^(1/2)/x^4,x, algorithm="giac")

[Out] 1/2*(2*b^2*log(abs(x))*sgn(x) - (4*a*b*x*sgn(x) + a^2*sgn(x))/x^2)*sqrt(c)

maple [A] time = 0.01, size = 34, normalized size = 0.63

$$\frac{\sqrt{cx^2} (2b^2x^2 \ln(x) - 4abx - a^2)}{2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2*(c*x^2)^(1/2)/x^4,x)`

[Out] `1/2*(c*x^2)^(1/2)*(2*b^2*ln(x)*x^2-4*a*b*x-a^2)/x^3`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2*(c*x^2)^(1/2)/x^4,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{cx^2} (a + bx)^2}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(1/2)*(a + b*x)^2)/x^4,x)`

[Out] `int(((c*x^2)^(1/2)*(a + b*x)^2)/x^4, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (a + bx)^2}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(c*x**2)**(1/2)/x**4,x)`

[Out] `Integral(sqrt(c*x**2)*(a + b*x)**2/x**4, x)`

$$3.812 \quad \int x^3 (cx^2)^{3/2} (a + bx)^2 dx$$

Optimal. Leaf size=60

$$\frac{1}{7}a^2cx^6\sqrt{cx^2} + \frac{1}{4}abcx^7\sqrt{cx^2} + \frac{1}{9}b^2cx^8\sqrt{cx^2}$$

[Out] $1/7*a^2*c*x^6*(c*x^2)^{(1/2)}+1/4*a*b*c*x^7*(c*x^2)^{(1/2)}+1/9*b^2*c*x^8*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{1}{7}a^2cx^6\sqrt{cx^2} + \frac{1}{4}abcx^7\sqrt{cx^2} + \frac{1}{9}b^2cx^8\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*(c*x^2)^{(3/2)}*(a + b*x)^2, x]$

[Out] $(a^2*c*x^6*\text{Sqrt}[c*x^2])/7 + (a*b*c*x^7*\text{Sqrt}[c*x^2])/4 + (b^2*c*x^8*\text{Sqrt}[c*x^2])/9$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}\int x^3 (cx^2)^{3/2} (a + bx)^2 dx &= \frac{(c\sqrt{cx^2}) \int x^6 (a + bx)^2 dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (a^2x^6 + 2abx^7 + b^2x^8) dx}{x} \\ &= \frac{1}{7}a^2cx^6\sqrt{cx^2} + \frac{1}{4}abcx^7\sqrt{cx^2} + \frac{1}{9}b^2cx^8\sqrt{cx^2}\end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.58

$$\frac{1}{252}x^4 (cx^2)^{3/2} (36a^2 + 63abx + 28b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(c*x^2)^(3/2)*(a + b*x)^2,x]

[Out] (x^4*(c*x^2)^(3/2)*(36*a^2 + 63*a*b*x + 28*b^2*x^2))/252

fricas [A] time = 0.41, size = 36, normalized size = 0.60

$$\frac{1}{252} (28b^2cx^8 + 63abcx^7 + 36a^2cx^6)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] 1/252*(28*b^2*c*x^8 + 63*a*b*c*x^7 + 36*a^2*c*x^6)*sqrt(c*x^2)

giac [A] time = 1.09, size = 35, normalized size = 0.58

$$\frac{1}{252} (28b^2x^9\operatorname{sgn}(x) + 63abx^8\operatorname{sgn}(x) + 36a^2x^7\operatorname{sgn}(x))c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="giac")

[Out] 1/252*(28*b^2*x^9*sgn(x) + 63*a*b*x^8*sgn(x) + 36*a^2*x^7*sgn(x))*c^(3/2)

maple [A] time = 0.01, size = 32, normalized size = 0.53

$$\frac{(28b^2x^2 + 63abx + 36a^2)(cx^2)^{\frac{3}{2}}x^4}{252}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(c*x^2)^(3/2)*(b*x+a)^2,x)`

[Out] $1/252*x^4*(28*b^2*x^2+63*a*b*x+36*a^2)*(c*x^2)^(3/2)$

maxima [A] time = 1.35, size = 54, normalized size = 0.90

$$\frac{(cx^2)^{\frac{5}{2}} b^2 x^4}{9c} + \frac{(cx^2)^{\frac{5}{2}} abx^3}{4c} + \frac{(cx^2)^{\frac{5}{2}} a^2 x^2}{7c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="maxima")`

[Out] $1/9*(c*x^2)^(5/2)*b^2*x^4/c + 1/4*(c*x^2)^(5/2)*a*b*x^3/c + 1/7*(c*x^2)^(5/2)*a^2*x^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^3 (cx^2)^{3/2} (a+bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(c*x^2)^(3/2)*(a+b*x)^2,x)`

[Out] `int(x^3*(c*x^2)^(3/2)*(a+b*x)^2, x)`

sympy [A] time = 1.50, size = 60, normalized size = 1.00

$$\frac{a^2 c^{\frac{3}{2}} x^4 (x^2)^{\frac{3}{2}}}{7} + \frac{abc^{\frac{3}{2}} x^5 (x^2)^{\frac{3}{2}}}{4} + \frac{b^2 c^{\frac{3}{2}} x^6 (x^2)^{\frac{3}{2}}}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(c*x**2)**(3/2)*(b*x+a)**2,x)`

[Out] $a**2*c**(3/2)*x**4*(x**2)**(3/2)/7 + a*b*c**(3/2)*x**5*(x**2)**(3/2)/4 + b**2*c**(3/2)*x**6*(x**2)**(3/2)/9$

$$3.813 \quad \int x^2 (cx^2)^{3/2} (a + bx)^2 dx$$

Optimal. Leaf size=60

$$\frac{1}{6}a^2cx^5\sqrt{cx^2} + \frac{2}{7}abcx^6\sqrt{cx^2} + \frac{1}{8}b^2cx^7\sqrt{cx^2}$$

[Out] $\frac{1}{6}a^2c^2x^5(c^2x^2)^{(1/2)} + \frac{2}{7}a^2bcx^6(c^2x^2)^{(1/2)} + \frac{1}{8}b^2c^2x^7(c^2x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{1}{6}a^2cx^5\sqrt{cx^2} + \frac{2}{7}abcx^6\sqrt{cx^2} + \frac{1}{8}b^2cx^7\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[x^2*(c*x^2)^(3/2)*(a + b*x)^2,x]

[Out] $(a^2c^2x^5\sqrt{c^2x^2})/6 + (2a^2bcx^6\sqrt{c^2x^2})/7 + (b^2c^2x^7\sqrt{c^2x^2})/8$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2 (cx^2)^{3/2} (a + bx)^2 dx &= \frac{(c\sqrt{cx^2}) \int x^5 (a + bx)^2 dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (a^2x^5 + 2abx^6 + b^2x^7) dx}{x} \\ &= \frac{1}{6}a^2cx^5\sqrt{cx^2} + \frac{2}{7}abcx^6\sqrt{cx^2} + \frac{1}{8}b^2cx^7\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.58

$$\frac{1}{168}x^3 (cx^2)^{3/2} (28a^2 + 48abx + 21b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(c*x^2)^(3/2)*(a + b*x)^2,x]

[Out] (x^3*(c*x^2)^(3/2)*(28*a^2 + 48*a*b*x + 21*b^2*x^2))/168

fricas [A] time = 0.47, size = 36, normalized size = 0.60

$$\frac{1}{168} (21 b^2 cx^7 + 48 abcx^6 + 28 a^2 cx^5) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] 1/168*(21*b^2*c*x^7 + 48*a*b*c*x^6 + 28*a^2*c*x^5)*sqrt(c*x^2)

giac [A] time = 1.08, size = 35, normalized size = 0.58

$$\frac{1}{168} (21 b^2 x^8 \operatorname{sgn}(x) + 48 abx^7 \operatorname{sgn}(x) + 28 a^2 x^6 \operatorname{sgn}(x)) c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="giac")

[Out] 1/168*(21*b^2*x^8*sgn(x) + 48*a*b*x^7*sgn(x) + 28*a^2*x^6*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 32, normalized size = 0.53

$$\frac{(21b^2x^2 + 48abx + 28a^2)(cx^2)^{\frac{3}{2}}x^3}{168}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(c*x^2)^(3/2)*(b*x+a)^2,x)`

[Out] `1/168*x^3*(21*b^2*x^2+48*a*b*x+28*a^2)*(c*x^2)^(3/2)`

maxima [A] time = 1.33, size = 52, normalized size = 0.87

$$\frac{(cx^2)^{\frac{5}{2}} b^2 x^3}{8c} + \frac{2 (cx^2)^{\frac{5}{2}} abx^2}{7c} + \frac{(cx^2)^{\frac{5}{2}} a^2 x}{6c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="maxima")`

[Out] `1/8*(c*x^2)^(5/2)*b^2*x^3/c + 2/7*(c*x^2)^(5/2)*a*b*x^2/c + 1/6*(c*x^2)^(5/2)*a^2*x/c`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^2 (cx^2)^{3/2} (a+bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(c*x^2)^(3/2)*(a+b*x)^2,x)`

[Out] `int(x^2*(c*x^2)^(3/2)*(a+b*x)^2, x)`

sympy [A] time = 1.22, size = 61, normalized size = 1.02

$$\frac{a^2 c^{\frac{3}{2}} x^3 (x^2)^{\frac{3}{2}}}{6} + \frac{2abc^{\frac{3}{2}} x^4 (x^2)^{\frac{3}{2}}}{7} + \frac{b^2 c^{\frac{3}{2}} x^5 (x^2)^{\frac{3}{2}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(c*x**2)**(3/2)*(b*x+a)**2,x)`

[Out] `a**2*c**(3/2)*x**3*(x**2)**(3/2)/6 + 2*a*b*c**(3/2)*x**4*(x**2)**(3/2)/7 + b**2*c**(3/2)*x**5*(x**2)**(3/2)/8`

$$3.814 \quad \int x (cx^2)^{3/2} (a + bx)^2 dx$$

Optimal. Leaf size=60

$$\frac{1}{5}a^2cx^4\sqrt{cx^2} + \frac{1}{3}abcx^5\sqrt{cx^2} + \frac{1}{7}b^2cx^6\sqrt{cx^2}$$

[Out] $1/5*a^2*c*x^4*(c*x^2)^{(1/2)}+1/3*a*b*c*x^5*(c*x^2)^{(1/2)}+1/7*b^2*c*x^6*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{5}a^2cx^4\sqrt{cx^2} + \frac{1}{3}abcx^5\sqrt{cx^2} + \frac{1}{7}b^2cx^6\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[x*(c*x^2)^(3/2)*(a + b*x)^2,x]

[Out] $(a^2*c*x^4*\text{Sqrt}[c*x^2])/5 + (a*b*c*x^5*\text{Sqrt}[c*x^2])/3 + (b^2*c*x^6*\text{Sqrt}[c*x^2])/7$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x (cx^2)^{3/2} (a + bx)^2 dx &= \frac{(c\sqrt{cx^2}) \int x^4 (a + bx)^2 dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (a^2x^4 + 2abx^5 + b^2x^6) dx}{x} \\ &= \frac{1}{5}a^2cx^4\sqrt{cx^2} + \frac{1}{3}abcx^5\sqrt{cx^2} + \frac{1}{7}b^2cx^6\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.58

$$\frac{1}{105}x^2 (cx^2)^{3/2} (21a^2 + 35abx + 15b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[x*(c*x^2)^(3/2)*(a + b*x)^2,x]

[Out] (x^2*(c*x^2)^(3/2)*(21*a^2 + 35*a*b*x + 15*b^2*x^2))/105

fricas [A] time = 0.41, size = 36, normalized size = 0.60

$$\frac{1}{105} (15b^2cx^6 + 35abcx^5 + 21a^2cx^4)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] 1/105*(15*b^2*c*x^6 + 35*a*b*c*x^5 + 21*a^2*c*x^4)*sqrt(c*x^2)

giac [A] time = 1.18, size = 35, normalized size = 0.58

$$\frac{1}{105} (15b^2x^7\text{sgn}(x) + 35abx^6\text{sgn}(x) + 21a^2x^5\text{sgn}(x))c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="giac")

[Out] 1/105*(15*b^2*x^7*sgn(x) + 35*a*b*x^6*sgn(x) + 21*a^2*x^5*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 32, normalized size = 0.53

$$\frac{(15b^2x^2 + 35abx + 21a^2)(cx^2)^{\frac{3}{2}}x^2}{105}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(3/2)*(b*x+a)^2,x)`

[Out] $1/105*x^2*(15*b^2*x^2+35*a*b*x+21*a^2)*(c*x^2)^(3/2)$

maxima [A] time = 1.31, size = 49, normalized size = 0.82

$$\frac{(cx^2)^{\frac{5}{2}} b^2 x^2}{7c} + \frac{(cx^2)^{\frac{5}{2}} abx}{3c} + \frac{(cx^2)^{\frac{5}{2}} a^2}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="maxima")`

[Out] $1/7*(c*x^2)^(5/2)*b^2*x^2/c + 1/3*(c*x^2)^(5/2)*a*b*x/c + 1/5*(c*x^2)^(5/2)*a^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x (cx^2)^{3/2} (a + bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(3/2)*(a + b*x)^2,x)`

[Out] `int(x*(c*x^2)^(3/2)*(a + b*x)^2, x)`

sympy [A] time = 0.97, size = 60, normalized size = 1.00

$$\frac{a^2 c^{\frac{3}{2}} x^2 (x^2)^{\frac{3}{2}}}{5} + \frac{abc^{\frac{3}{2}} x^3 (x^2)^{\frac{3}{2}}}{3} + \frac{b^2 c^{\frac{3}{2}} x^4 (x^2)^{\frac{3}{2}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x**2)**(3/2)*(b*x+a)**2,x)`

[Out] $a**2*c**(3/2)*x**2*(x**2)**(3/2)/5 + a*b*c**(3/2)*x**3*(x**2)**(3/2)/3 + b**2*c**(3/2)*x**4*(x**2)**(3/2)/7$

$$3.815 \quad \int (cx^2)^{3/2} (a + bx)^2 dx$$

Optimal. Leaf size=60

$$\frac{1}{4}a^2cx^3\sqrt{cx^2} + \frac{2}{5}abcx^4\sqrt{cx^2} + \frac{1}{6}b^2cx^5\sqrt{cx^2}$$

[Out] $\frac{1}{4}a^2cx^3(c*x^2)^{(1/2)} + \frac{2}{5}a*b*c*x^4*(c*x^2)^{(1/2)} + \frac{1}{6}b^2*c*x^5*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$\frac{1}{4}a^2cx^3\sqrt{cx^2} + \frac{2}{5}abcx^4\sqrt{cx^2} + \frac{1}{6}b^2cx^5\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}*(a + b*x)^2, x]$

[Out] $(a^2*c*x^3*\text{Sqrt}[c*x^2])/4 + (2*a*b*c*x^4*\text{Sqrt}[c*x^2])/5 + (b^2*c*x^5*\text{Sqrt}[c*x^2])/6$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ $\text{FreeQ}\{a, m, n, x\}$ && $!\text{IntegerQ}[m]$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ $\text{FreeQ}\{a, b, c, d, n, x\}$ && $\text{NeQ}[b*c - a*d, 0]$ && $\text{IGtQ}[m, 0]$ && $(!\text{IntegerQ}[n] \parallel (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0]) \parallel \text{LtQ}[9*m + 5*(n + 1), 0] \parallel \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int (cx^2)^{3/2} (a + bx)^2 dx &= \frac{(c\sqrt{cx^2}) \int x^3 (a + bx)^2 dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (a^2x^3 + 2abx^4 + b^2x^5) dx}{x} \\ &= \frac{1}{4}a^2cx^3\sqrt{cx^2} + \frac{2}{5}abcx^4\sqrt{cx^2} + \frac{1}{6}b^2cx^5\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.55

$$\frac{1}{60}x (cx^2)^{3/2} (15a^2 + 24abx + 10b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)*(a + b*x)^2,x]

[Out] (x*(c*x^2)^(3/2)*(15*a^2 + 24*a*b*x + 10*b^2*x^2))/60

fricas [A] time = 0.41, size = 36, normalized size = 0.60

$$\frac{1}{60} (10b^2cx^5 + 24abcx^4 + 15a^2cx^3)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] 1/60*(10*b^2*c*x^5 + 24*a*b*c*x^4 + 15*a^2*c*x^3)*sqrt(c*x^2)

giac [A] time = 1.13, size = 35, normalized size = 0.58

$$\frac{1}{60} (10b^2x^6\operatorname{sgn}(x) + 24abx^5\operatorname{sgn}(x) + 15a^2x^4\operatorname{sgn}(x))c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="giac")

[Out] 1/60*(10*b^2*x^6*sgn(x) + 24*a*b*x^5*sgn(x) + 15*a^2*x^4*sgn(x))*c^(3/2)

maple [A] time = 0.01, size = 30, normalized size = 0.50

$$\frac{(10b^2x^2 + 24abx + 15a^2)(cx^2)^{\frac{3}{2}}x}{60}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)*(b*x+a)^2,x)`

[Out] `1/60*x*(10*b^2*x^2+24*a*b*x+15*a^2)*(c*x^2)^(3/2)`

maxima [A] time = 1.36, size = 44, normalized size = 0.73

$$\frac{1}{4} (cx^2)^{\frac{3}{2}} a^2 x + \frac{(cx^2)^{\frac{5}{2}} b^2 x}{6c} + \frac{2 (cx^2)^{\frac{5}{2}} ab}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="maxima")`

[Out] `1/4*(c*x^2)^(3/2)*a^2*x + 1/6*(c*x^2)^(5/2)*b^2*x/c + 2/5*(c*x^2)^(5/2)*a*b/c`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (cx^2)^{3/2} (a+bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)*(a+b*x)^2,x)`

[Out] `int((c*x^2)^(3/2)*(a+b*x)^2, x)`

sympy [A] time = 0.77, size = 60, normalized size = 1.00

$$\frac{a^2 c^{\frac{3}{2}} x (x^2)^{\frac{3}{2}}}{4} + \frac{2abc^{\frac{3}{2}} x^2 (x^2)^{\frac{3}{2}}}{5} + \frac{b^2 c^{\frac{3}{2}} x^3 (x^2)^{\frac{3}{2}}}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(3/2)*(b*x+a)**2,x)`

[Out] `a**2*c**(3/2)*x*(x**2)**(3/2)/4 + 2*a*b*c**(3/2)*x**2*(x**2)**(3/2)/5 + b**2*c**(3/2)*x**3*(x**2)**(3/2)/6`

$$3.816 \quad \int \frac{(cx^2)^{3/2} (a+bx)^2}{x} dx$$

Optimal. Leaf size=60

$$\frac{1}{3}a^2cx^2\sqrt{cx^2} + \frac{1}{2}abcx^3\sqrt{cx^2} + \frac{1}{5}b^2cx^4\sqrt{cx^2}$$

[Out] $\frac{1}{3}a^2c^2x^2(c^2x^2)^{1/2} + \frac{1}{2}a^2bc^2x^3(c^2x^2)^{1/2} + \frac{1}{5}b^2c^2x^4(c^2x^2)^{1/2}$

Rubi [A] time = 0.01, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{1}{3}a^2cx^2\sqrt{cx^2} + \frac{1}{2}abcx^3\sqrt{cx^2} + \frac{1}{5}b^2cx^4\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x)^2)/x,x]

[Out] (a^2*c*x^2*Sqrt[c*x^2])/3 + (a*b*c*x^3*Sqrt[c*x^2])/2 + (b^2*c*x^4*Sqrt[c*x^2])/5

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2} (a + bx)^2}{x} dx &= \frac{(c\sqrt{cx^2})}{x} \int x^2 (a + bx)^2 dx \\ &= \frac{(c\sqrt{cx^2})}{x} \int (a^2x^2 + 2abx^3 + b^2x^4) dx \\ &= \frac{1}{3}a^2cx^2\sqrt{cx^2} + \frac{1}{2}abcx^3\sqrt{cx^2} + \frac{1}{5}b^2cx^4\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 36, normalized size = 0.60

$$\frac{1}{30}cx^2\sqrt{cx^2} (10a^2 + 15abx + 6b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x)^2)/x,x]

[Out] (c*x^2*Sqrt[c*x^2]*(10*a^2 + 15*a*b*x + 6*b^2*x^2))/30

fricas [A] time = 0.41, size = 36, normalized size = 0.60

$$\frac{1}{30} (6b^2cx^4 + 15abcx^3 + 10a^2cx^2)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2/x,x, algorithm="fricas")

[Out] 1/30*(6*b^2*c*x^4 + 15*a*b*c*x^3 + 10*a^2*c*x^2)*sqrt(c*x^2)

giac [A] time = 0.95, size = 35, normalized size = 0.58

$$\frac{1}{30} (6b^2x^5\text{sgn}(x) + 15abx^4\text{sgn}(x) + 10a^2x^3\text{sgn}(x))c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2/x,x, algorithm="giac")

[Out] 1/30*(6*b^2*x^5*sgn(x) + 15*a*b*x^4*sgn(x) + 10*a^2*x^3*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 29, normalized size = 0.48

$$\frac{(6b^2x^2 + 15abx + 10a^2)(cx^2)^{\frac{3}{2}}}{30}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)*(b*x+a)^2/x,x)`

[Out] $1/30*(6*b^2*x^2+15*a*b*x+10*a^2)*(c*x^2)^(3/2)$

maxima [A] time = 1.30, size = 40, normalized size = 0.67

$$\frac{1}{2} (cx^2)^{\frac{3}{2}} abx + \frac{1}{3} (cx^2)^{\frac{3}{2}} a^2 + \frac{(cx^2)^{\frac{5}{2}} b^2}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)*(b*x+a)^2/x,x, algorithm="maxima")`

[Out] $1/2*(c*x^2)^(3/2)*a*b*x + 1/3*(c*x^2)^(3/2)*a^2 + 1/5*(c*x^2)^(5/2)*b^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{3/2} (a+bx)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(3/2)*(a + b*x)^2)/x,x)`

[Out] `int(((c*x^2)^(3/2)*(a + b*x)^2)/x, x)`

sympy [A] time = 0.79, size = 54, normalized size = 0.90

$$\frac{a^2 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}}{3} + \frac{abc^{\frac{3}{2}} x (x^2)^{\frac{3}{2}}}{2} + \frac{b^2 c^{\frac{3}{2}} x^2 (x^2)^{\frac{3}{2}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(3/2)*(b*x+a)**2/x,x)`

[Out] $a**2*c**(3/2)*(x**2)**(3/2)/3 + a*b*c**(3/2)*x*(x**2)**(3/2)/2 + b**2*c**(3/2)*x**2*(x**2)**(3/2)/5$

$$3.817 \quad \int \frac{(cx^2)^{3/2} (a+bx)^2}{x^2} dx$$

Optimal. Leaf size=58

$$\frac{1}{2}a^2cx\sqrt{cx^2} + \frac{2}{3}abcx^2\sqrt{cx^2} + \frac{1}{4}b^2cx^3\sqrt{cx^2}$$

[Out] $1/2*a^2*c*x*(c*x^2)^{(1/2)}+2/3*a*b*c*x^2*(c*x^2)^{(1/2)}+1/4*b^2*c*x^3*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{1}{2}a^2cx\sqrt{cx^2} + \frac{2}{3}abcx^2\sqrt{cx^2} + \frac{1}{4}b^2cx^3\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x)^2)/x^2,x]

[Out] (a^2*c*x*Sqrt[c*x^2])/2 + (2*a*b*c*x^2*Sqrt[c*x^2])/3 + (b^2*c*x^3*Sqrt[c*x^2])/4

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2} (a+bx)^2}{x^2} dx &= \frac{(c\sqrt{cx^2}) \int x(a+bx)^2 dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (a^2x + 2abx^2 + b^2x^3) dx}{x} \\ &= \frac{1}{2}a^2cx\sqrt{cx^2} + \frac{2}{3}abcx^2\sqrt{cx^2} + \frac{1}{4}b^2cx^3\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 34, normalized size = 0.59

$$\frac{1}{12}cx\sqrt{cx^2} (6a^2 + 8abx + 3b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x)^2)/x^2,x]

[Out] (c*x*Sqrt[c*x^2]*(6*a^2 + 8*a*b*x + 3*b^2*x^2))/12

fricas [A] time = 0.42, size = 34, normalized size = 0.59

$$\frac{1}{12} (3b^2cx^3 + 8abcx^2 + 6a^2cx)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2/x^2,x, algorithm="fricas")

[Out] 1/12*(3*b^2*c*x^3 + 8*a*b*c*x^2 + 6*a^2*c*x)*sqrt(c*x^2)

giac [A] time = 1.03, size = 35, normalized size = 0.60

$$\frac{1}{12} (3b^2x^4\text{sgn}(x) + 8abx^3\text{sgn}(x) + 6a^2x^2\text{sgn}(x))c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2/x^2,x, algorithm="giac")

[Out] 1/12*(3*b^2*x^4*sgn(x) + 8*a*b*x^3*sgn(x) + 6*a^2*x^2*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 32, normalized size = 0.55

$$\frac{(3b^2x^2 + 8abx + 6a^2)(cx^2)^{\frac{3}{2}}}{12x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)*(b*x+a)^2/x^2,x)`

[Out] `1/12/x*(3*b^2*x^2+8*a*b*x+6*a^2)*(c*x^2)^(3/2)`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)*(b*x+a)^2/x^2,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{3/2} (a+bx)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(3/2)*(a + b*x)^2)/x^2,x)`

[Out] `int(((c*x^2)^(3/2)*(a + b*x)^2)/x^2, x)`

sympy [A] time = 0.80, size = 54, normalized size = 0.93

$$\frac{a^2 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}}{2x} + \frac{2abc^{\frac{3}{2}} (x^2)^{\frac{3}{2}}}{3} + \frac{b^2 c^{\frac{3}{2}} x (x^2)^{\frac{3}{2}}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(3/2)*(b*x+a)**2/x**2,x)`

[Out] `a**2*c**(3/2)*(x**2)**(3/2)/(2*x) + 2*a*b*c**(3/2)*(x**2)**(3/2)/3 + b**2*c**
(3/2)*x*(x2)**(3/2)/4`

$$3.818 \quad \int \frac{(cx^2)^{3/2} (a+bx)^2}{x^3} dx$$

Optimal. Leaf size=27

$$\frac{c\sqrt{cx^2} (a + bx)^3}{3bx}$$

[Out] 1/3*c*(b*x+a)^3*(c*x^2)^(1/2)/b/x

Rubi [A] time = 0.00, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$\frac{c\sqrt{cx^2} (a + bx)^3}{3bx}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x)^2)/x^3,x]

[Out] (c*Sqrt[c*x^2]*(a + b*x)^3)/(3*b*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2} (a + bx)^2}{x^3} dx &= \frac{(c\sqrt{cx^2}) \int (a + bx)^2 dx}{x} \\ &= \frac{c\sqrt{cx^2} (a + bx)^3}{3bx} \end{aligned}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 0.96

$$\frac{(cx^2)^{3/2} (a + bx)^3}{3bx^3}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x)^2)/x^3,x]

[Out] ((c*x^2)^(3/2)*(a + b*x)^3)/(3*b*x^3)

fricas [A] time = 0.40, size = 30, normalized size = 1.11

$$\frac{1}{3} (b^2cx^2 + 3abcx + 3a^2c)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2/x^3,x, algorithm="fricas")

[Out] 1/3*(b^2*c*x^2 + 3*a*b*c*x + 3*a^2*c)*sqrt(c*x^2)

giac [A] time = 1.22, size = 29, normalized size = 1.07

$$\frac{1}{3} \left(\frac{(bx + a)^3 \operatorname{sgn}(x)}{b} - \frac{a^3 \operatorname{sgn}(x)}{b} \right) c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2/x^3,x, algorithm="giac")

[Out] 1/3*((b*x + a)^3*sgn(x)/b - a^3*sgn(x)/b)*c^(3/2)

maple [A] time = 0.00, size = 31, normalized size = 1.15

$$\frac{(b^2x^2 + 3abx + 3a^2)(cx^2)^{\frac{3}{2}}}{3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(b*x+a)^2/x^3,x)

[Out] 1/3/x^2*(b^2*x^2+3*a*b*x+3*a^2)*(c*x^2)^(3/2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2/x^3,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
 expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{(cx^2)^{3/2} (a+bx)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(3/2)*(a + b*x)^2)/x^3, x)

[Out] int(((c*x^2)^(3/2)*(a + b*x)^2)/x^3, x)

sympy [B] time = 0.94, size = 51, normalized size = 1.89

$$\frac{a^2 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}}{x^2} + \frac{abc^{\frac{3}{2}} (x^2)^{\frac{3}{2}}}{x} + \frac{b^2 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)*(b*x+a)**2/x**3, x)

[Out] a**2*c**(3/2)*(x**2)**(3/2)/x**2 + a*b*c**(3/2)*(x**2)**(3/2)/x + b**2*c**
 (3/2)*(x**2)**(3/2)/3

$$3.819 \quad \int \frac{(cx^2)^{3/2} (a+bx)^2}{x^4} dx$$

Optimal. Leaf size=52

$$\frac{a^2c\sqrt{cx^2} \log(x)}{x} + 2abc\sqrt{cx^2} + \frac{1}{2}b^2cx\sqrt{cx^2}$$

[Out] $2*a*b*c*(c*x^2)^{(1/2)}+1/2*b^2*c*x*(c*x^2)^{(1/2)}+a^2*c*\ln(x)*(c*x^2)^{(1/2)}/x$

Rubi [A] time = 0.01, antiderivative size = 52, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2c\sqrt{cx^2} \log(x)}{x} + 2abc\sqrt{cx^2} + \frac{1}{2}b^2cx\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x)^2)/x^4,x]

[Out] $2*a*b*c*\text{Sqrt}[c*x^2] + (b^2*c*x*\text{Sqrt}[c*x^2])/2 + (a^2*c*\text{Sqrt}[c*x^2]*\text{Log}[x])/x$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2} (a + bx)^2}{x^4} dx &= \frac{(c\sqrt{cx^2})}{x} \int \frac{(a+bx)^2}{x} dx \\ &= \frac{(c\sqrt{cx^2})}{x} \int \left(2ab + \frac{a^2}{x} + b^2x\right) dx \\ &= 2abc\sqrt{cx^2} + \frac{1}{2}b^2cx\sqrt{cx^2} + \frac{a^2c\sqrt{cx^2} \log(x)}{x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 34, normalized size = 0.65

$$\frac{(cx^2)^{3/2} (2a^2 \log(x) + bx(4a + bx))}{2x^3}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x)^2)/x^4,x]

[Out] ((c*x^2)^(3/2)*(b*x*(4*a + b*x) + 2*a^2*Log[x]))/(2*x^3)

fricas [A] time = 0.41, size = 35, normalized size = 0.67

$$\frac{(b^2cx^2 + 4abcx + 2a^2c \log(x))\sqrt{cx^2}}{2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2/x^4,x, algorithm="fricas")

[Out] 1/2*(b^2*c*x^2 + 4*a*b*c*x + 2*a^2*c*log(x))*sqrt(c*x^2)/x

giac [A] time = 1.20, size = 32, normalized size = 0.62

$$\frac{1}{2} \left(b^2x^2 \operatorname{sgn}(x) + 4abx \operatorname{sgn}(x) + 2a^2 \log(|x|) \operatorname{sgn}(x) \right) c^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^2/x^4,x, algorithm="giac")

[Out] 1/2*(b^2*x^2*sgn(x) + 4*a*b*x*sgn(x) + 2*a^2*log(abs(x))*sgn(x))*c^(3/2)

maple [A] time = 0.00, size = 33, normalized size = 0.63

$$\frac{(cx^2)^{\frac{3}{2}} (b^2x^2 + 2a^2 \ln(x) + 4abx)}{2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)*(b*x+a)^2/x^4,x)`

[Out] `1/2*(c*x^2)^(3/2)*(b^2*x^2+2*a^2*ln(x)+4*a*b*x)/x^3`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)*(b*x+a)^2/x^4,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{3/2} (a+bx)^2}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(3/2)*(a + b*x)^2)/x^4,x)`

[Out] `int(((c*x^2)^(3/2)*(a + b*x)^2)/x^4, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (a+bx)^2}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(3/2)*(b*x+a)**2/x**4,x)`

[Out] `Integral((c*x**2)**(3/2)*(a + b*x)**2/x**4, x)`

$$3.820 \quad \int x (cx^2)^{5/2} (a + bx)^2 dx$$

Optimal. Leaf size=66

$$\frac{1}{7}a^2c^2x^6\sqrt{cx^2} + \frac{1}{4}abc^2x^7\sqrt{cx^2} + \frac{1}{9}b^2c^2x^8\sqrt{cx^2}$$

[Out] $1/7*a^2*c^2*x^6*(c*x^2)^{(1/2)}+1/4*a*b*c^2*x^7*(c*x^2)^{(1/2)}+1/9*b^2*c^2*x^8*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{1}{7}a^2c^2x^6\sqrt{cx^2} + \frac{1}{4}abc^2x^7\sqrt{cx^2} + \frac{1}{9}b^2c^2x^8\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[x*(c*x^2)^(5/2)*(a + b*x)^2,x]

[Out] $(a^2*c^2*x^6*\text{Sqrt}[c*x^2])/7 + (a*b*c^2*x^7*\text{Sqrt}[c*x^2])/4 + (b^2*c^2*x^8*\text{Sqrt}[c*x^2])/9$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x (cx^2)^{5/2} (a + bx)^2 dx &= \frac{(c^2 \sqrt{cx^2}) \int x^6 (a + bx)^2 dx}{x} \\ &= \frac{(c^2 \sqrt{cx^2}) \int (a^2 x^6 + 2abx^7 + b^2 x^8) dx}{x} \\ &= \frac{1}{7} a^2 c^2 x^6 \sqrt{cx^2} + \frac{1}{4} abc^2 x^7 \sqrt{cx^2} + \frac{1}{9} b^2 c^2 x^8 \sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.53

$$\frac{1}{252} x^2 (cx^2)^{5/2} (36a^2 + 63abx + 28b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[x*(c*x^2)^(5/2)*(a + b*x)^2,x]

[Out] (x^2*(c*x^2)^(5/2)*(36*a^2 + 63*a*b*x + 28*b^2*x^2))/252

fricas [A] time = 0.45, size = 42, normalized size = 0.64

$$\frac{1}{252} (28 b^2 c^2 x^8 + 63 abc^2 x^7 + 36 a^2 c^2 x^6) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(5/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] 1/252*(28*b^2*c^2*x^8 + 63*a*b*c^2*x^7 + 36*a^2*c^2*x^6)*sqrt(c*x^2)

giac [A] time = 1.22, size = 44, normalized size = 0.67

$$\frac{1}{252} (28 b^2 c^2 x^9 \operatorname{sgn}(x) + 63 abc^2 x^8 \operatorname{sgn}(x) + 36 a^2 c^2 x^7 \operatorname{sgn}(x)) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(5/2)*(b*x+a)^2,x, algorithm="giac")

[Out] 1/252*(28*b^2*c^2*x^9*sgn(x) + 63*a*b*c^2*x^8*sgn(x) + 36*a^2*c^2*x^7*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 32, normalized size = 0.48

$$\frac{(28b^2x^2 + 63abx + 36a^2)(cx^2)^{\frac{5}{2}}x^2}{252}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(5/2)*(b*x+a)^2,x)`

[Out] $1/252*x^2*(28*b^2*x^2+63*a*b*x+36*a^2)*(c*x^2)^(5/2)$

maxima [A] time = 1.34, size = 49, normalized size = 0.74

$$\frac{(cx^2)^{\frac{7}{2}} b^2 x^2}{9c} + \frac{(cx^2)^{\frac{7}{2}} abx}{4c} + \frac{(cx^2)^{\frac{7}{2}} a^2}{7c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x^2)^(5/2)*(b*x+a)^2,x, algorithm="maxima")`

[Out] $1/9*(c*x^2)^(7/2)*b^2*x^2/c + 1/4*(c*x^2)^(7/2)*a*b*x/c + 1/7*(c*x^2)^(7/2)*a^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x (cx^2)^{5/2} (a + bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(5/2)*(a + b*x)^2,x)`

[Out] `int(x*(c*x^2)^(5/2)*(a + b*x)^2, x)`

sympy [A] time = 2.19, size = 60, normalized size = 0.91

$$\frac{a^2 c^{\frac{5}{2}} x^2 (x^2)^{\frac{5}{2}}}{7} + \frac{abc^{\frac{5}{2}} x^3 (x^2)^{\frac{5}{2}}}{4} + \frac{b^2 c^{\frac{5}{2}} x^4 (x^2)^{\frac{5}{2}}}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x**2)**(5/2)*(b*x+a)**2,x)`

[Out] $a**2*c**(5/2)*x**2*(x**2)**(5/2)/7 + a*b*c**(5/2)*x**3*(x**2)**(5/2)/4 + b**2*c**(5/2)*x**4*(x**2)**(5/2)/9$

$$3.821 \quad \int (cx^2)^{5/2} (a + bx)^2 dx$$

Optimal. Leaf size=66

$$\frac{1}{6}a^2c^2x^5\sqrt{cx^2} + \frac{2}{7}abc^2x^6\sqrt{cx^2} + \frac{1}{8}b^2c^2x^7\sqrt{cx^2}$$

[Out] $1/6*a^2*c^2*x^5*(c*x^2)^{(1/2)}+2/7*a*b*c^2*x^6*(c*x^2)^{(1/2)}+1/8*b^2*c^2*x^7*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$\frac{1}{6}a^2c^2x^5\sqrt{cx^2} + \frac{2}{7}abc^2x^6\sqrt{cx^2} + \frac{1}{8}b^2c^2x^7\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(5/2)}*(a + b*x)^2, x]$

[Out] $(a^2*c^2*x^5*\text{Sqrt}[c*x^2])/6 + (2*a*b*c^2*x^6*\text{Sqrt}[c*x^2])/7 + (b^2*c^2*x^7*\text{Sqrt}[c*x^2])/8$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ $\text{FreeQ}\{a, m, n, x\}$ && $!\text{IntegerQ}[m]$

Rule 43

$\text{Int}[((a_.) + (b_.)*(x_))^{(m_.)}*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ $\text{FreeQ}\{a, b, c, d, n, x\}$ && $\text{NeQ}[b*c - a*d, 0]$ && $\text{IGtQ}[m, 0]$ && $(!\text{IntegerQ}[n] \parallel (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0]) \parallel \text{LtQ}[9*m + 5*(n + 1), 0] \parallel \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int (cx^2)^{5/2} (a + bx)^2 dx &= \frac{(c^2 \sqrt{cx^2}) \int x^5 (a + bx)^2 dx}{x} \\ &= \frac{(c^2 \sqrt{cx^2}) \int (a^2 x^5 + 2abx^6 + b^2 x^7) dx}{x} \\ &= \frac{1}{6} a^2 c^2 x^5 \sqrt{cx^2} + \frac{2}{7} abc^2 x^6 \sqrt{cx^2} + \frac{1}{8} b^2 c^2 x^7 \sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.50

$$\frac{1}{168} x (cx^2)^{5/2} (28a^2 + 48abx + 21b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)*(a + b*x)^2,x]

[Out] (x*(c*x^2)^(5/2)*(28*a^2 + 48*a*b*x + 21*b^2*x^2))/168

fricas [A] time = 0.44, size = 42, normalized size = 0.64

$$\frac{1}{168} (21 b^2 c^2 x^7 + 48 abc^2 x^6 + 28 a^2 c^2 x^5) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] 1/168*(21*b^2*c^2*x^7 + 48*a*b*c^2*x^6 + 28*a^2*c^2*x^5)*sqrt(c*x^2)

giac [A] time = 1.05, size = 44, normalized size = 0.67

$$\frac{1}{168} (21 b^2 c^2 x^8 \operatorname{sgn}(x) + 48 abc^2 x^7 \operatorname{sgn}(x) + 28 a^2 c^2 x^6 \operatorname{sgn}(x)) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2,x, algorithm="giac")

[Out] 1/168*(21*b^2*c^2*x^8*sgn(x) + 48*a*b*c^2*x^7*sgn(x) + 28*a^2*c^2*x^6*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 30, normalized size = 0.45

$$\frac{(21b^2x^2 + 48abx + 28a^2)(cx^2)^{\frac{5}{2}}x}{168}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)*(b*x+a)^2,x)`

[Out] `1/168*x*(21*b^2*x^2+48*a*b*x+28*a^2)*(c*x^2)^(5/2)`

maxima [A] time = 1.32, size = 44, normalized size = 0.67

$$\frac{1}{6} (cx^2)^{\frac{5}{2}} a^2 x + \frac{(cx^2)^{\frac{7}{2}} b^2 x}{8c} + \frac{2 (cx^2)^{\frac{7}{2}} ab}{7c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(5/2)*(b*x+a)^2,x, algorithm="maxima")`

[Out] `1/6*(c*x^2)^(5/2)*a^2*x + 1/8*(c*x^2)^(7/2)*b^2*x/c + 2/7*(c*x^2)^(7/2)*a*b/c`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (cx^2)^{5/2} (a+bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)*(a+b*x)^2,x)`

[Out] `int((c*x^2)^(5/2)*(a+b*x)^2, x)`

sympy [A] time = 1.80, size = 60, normalized size = 0.91

$$\frac{a^2 c^{\frac{5}{2}} x (x^2)^{\frac{5}{2}}}{6} + \frac{2abc^{\frac{5}{2}} x^2 (x^2)^{\frac{5}{2}}}{7} + \frac{b^2 c^{\frac{5}{2}} x^3 (x^2)^{\frac{5}{2}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(5/2)*(b*x+a)**2,x)`

[Out] `a**2*c**(5/2)*x*(x**2)**(5/2)/6 + 2*a*b*c**(5/2)*x**2*(x**2)**(5/2)/7 + b**2*c**(5/2)*x**3*(x**2)**(5/2)/8`

$$3.822 \quad \int \frac{(cx^2)^{5/2} (a+bx)^2}{x} dx$$

Optimal. Leaf size=66

$$\frac{1}{5}a^2c^2x^4\sqrt{cx^2} + \frac{1}{3}abc^2x^5\sqrt{cx^2} + \frac{1}{7}b^2c^2x^6\sqrt{cx^2}$$

[Out] $1/5*a^2*c^2*x^4*(c*x^2)^{(1/2)}+1/3*a*b*c^2*x^5*(c*x^2)^{(1/2)}+1/7*b^2*c^2*x^6*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{1}{5}a^2c^2x^4\sqrt{cx^2} + \frac{1}{3}abc^2x^5\sqrt{cx^2} + \frac{1}{7}b^2c^2x^6\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^2)/x,x]

[Out] $(a^2*c^2*x^4*\text{Sqrt}[c*x^2])/5 + (a*b*c^2*x^5*\text{Sqrt}[c*x^2])/3 + (b^2*c^2*x^6*\text{Sqrt}[c*x^2])/7$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)^2}{x} dx &= \frac{(c^2\sqrt{cx^2}) \int x^4(a+bx)^2 dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (a^2x^4 + 2abx^5 + b^2x^6) dx}{x} \\ &= \frac{1}{5}a^2c^2x^4\sqrt{cx^2} + \frac{1}{3}abc^2x^5\sqrt{cx^2} + \frac{1}{7}b^2c^2x^6\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 36, normalized size = 0.55

$$\frac{1}{105}cx^2 (cx^2)^{3/2} (21a^2 + 35abx + 15b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^2)/x,x]

[Out] (c*x^2*(c*x^2)^(3/2)*(21*a^2 + 35*a*b*x + 15*b^2*x^2))/105

fricas [A] time = 0.41, size = 42, normalized size = 0.64

$$\frac{1}{105} (15b^2c^2x^6 + 35abc^2x^5 + 21a^2c^2x^4)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x,x, algorithm="fricas")

[Out] 1/105*(15*b^2*c^2*x^6 + 35*a*b*c^2*x^5 + 21*a^2*c^2*x^4)*sqrt(c*x^2)

giac [A] time = 0.96, size = 44, normalized size = 0.67

$$\frac{1}{105} (15b^2c^2x^7\operatorname{sgn}(x) + 35abc^2x^6\operatorname{sgn}(x) + 21a^2c^2x^5\operatorname{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x,x, algorithm="giac")

[Out] 1/105*(15*b^2*c^2*x^7*sgn(x) + 35*a*b*c^2*x^6*sgn(x) + 21*a^2*c^2*x^5*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 29, normalized size = 0.44

$$\frac{(15b^2x^2 + 35abx + 21a^2)(cx^2)^{5/2}}{105}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)*(b*x+a)^2/x,x)`

[Out] $1/105*(15*b^2*x^2+35*a*b*x+21*a^2)*(c*x^2)^(5/2)$

maxima [A] time = 1.28, size = 40, normalized size = 0.61

$$\frac{1}{3} (cx^2)^{\frac{5}{2}} abx + \frac{1}{5} (cx^2)^{\frac{5}{2}} a^2 + \frac{(cx^2)^{\frac{7}{2}} b^2}{7c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(5/2)*(b*x+a)^2/x,x, algorithm="maxima")`

[Out] $1/3*(c*x^2)^(5/2)*a*b*x + 1/5*(c*x^2)^(5/2)*a^2 + 1/7*(c*x^2)^(7/2)*b^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{5/2} (a+bx)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(5/2)*(a + b*x)^2)/x,x)`

[Out] `int(((c*x^2)^(5/2)*(a + b*x)^2)/x, x)`

sympy [A] time = 1.82, size = 54, normalized size = 0.82

$$\frac{a^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{5} + \frac{abc^{\frac{5}{2}} x (x^2)^{\frac{5}{2}}}{3} + \frac{b^2 c^{\frac{5}{2}} x^2 (x^2)^{\frac{5}{2}}}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(5/2)*(b*x+a)**2/x,x)`

[Out] $a**2*c**(5/2)*(x**2)**(5/2)/5 + a*b*c**(5/2)*x*(x**2)**(5/2)/3 + b**2*c**(5/2)*x**2*(x**2)**(5/2)/7$

$$3.823 \quad \int \frac{(cx^2)^{5/2} (a+bx)^2}{x^2} dx$$

Optimal. Leaf size=66

$$\frac{1}{4}a^2c^2x^3\sqrt{cx^2} + \frac{2}{5}abc^2x^4\sqrt{cx^2} + \frac{1}{6}b^2c^2x^5\sqrt{cx^2}$$

[Out] $\frac{1}{4}a^2c^2x^3(c*x^2)^{(1/2)} + \frac{2}{5}a*b*c^2*x^4*(c*x^2)^{(1/2)} + \frac{1}{6}b^2*c^2*x^5*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{1}{4}a^2c^2x^3\sqrt{cx^2} + \frac{2}{5}abc^2x^4\sqrt{cx^2} + \frac{1}{6}b^2c^2x^5\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^2)/x^2,x]

[Out] $(a^2*c^2*x^3*\text{Sqrt}[c*x^2])/4 + (2*a*b*c^2*x^4*\text{Sqrt}[c*x^2])/5 + (b^2*c^2*x^5*\text{Sqrt}[c*x^2])/6$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)^2}{x^2} dx &= \frac{(c^2\sqrt{cx^2}) \int x^3(a+bx)^2 dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (a^2x^3 + 2abx^4 + b^2x^5) dx}{x} \\ &= \frac{1}{4}a^2c^2x^3\sqrt{cx^2} + \frac{2}{5}abc^2x^4\sqrt{cx^2} + \frac{1}{6}b^2c^2x^5\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 34, normalized size = 0.52

$$\frac{1}{60}cx (cx^2)^{3/2} (15a^2 + 24abx + 10b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^2)/x^2,x]

[Out] (c*x*(c*x^2)^(3/2)*(15*a^2 + 24*a*b*x + 10*b^2*x^2))/60

fricas [A] time = 0.40, size = 42, normalized size = 0.64

$$\frac{1}{60} (10b^2c^2x^5 + 24abc^2x^4 + 15a^2c^2x^3) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^2,x, algorithm="fricas")

[Out] 1/60*(10*b^2*c^2*x^5 + 24*a*b*c^2*x^4 + 15*a^2*c^2*x^3)*sqrt(c*x^2)

giac [A] time = 0.99, size = 44, normalized size = 0.67

$$\frac{1}{60} (10b^2c^2x^6\text{sgn}(x) + 24abc^2x^5\text{sgn}(x) + 15a^2c^2x^4\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^2,x, algorithm="giac")

[Out] 1/60*(10*b^2*c^2*x^6*sgn(x) + 24*a*b*c^2*x^5*sgn(x) + 15*a^2*c^2*x^4*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 32, normalized size = 0.48

$$\frac{(10b^2x^2 + 24abx + 15a^2)(cx^2)^{5/2}}{60x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)*(b*x+a)^2/x^2,x)`

[Out] `1/60/x*(10*b^2*x^2+24*a*b*x+15*a^2)*(c*x^2)^(5/2)`

maxima [A] time = 1.37, size = 40, normalized size = 0.61

$$\frac{1}{6} (cx^2)^{\frac{5}{2}} b^2 x + \frac{2}{5} (cx^2)^{\frac{5}{2}} ab + \frac{(cx^2)^{\frac{5}{2}} a^2}{4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(5/2)*(b*x+a)^2/x^2,x, algorithm="maxima")`

[Out] `1/6*(c*x^2)^(5/2)*b^2*x + 2/5*(c*x^2)^(5/2)*a*b + 1/4*(c*x^2)^(5/2)*a^2/x`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{5/2} (a+bx)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(5/2)*(a+b*x)^2)/x^2,x)`

[Out] `int(((c*x^2)^(5/2)*(a+b*x)^2)/x^2, x)`

sympy [A] time = 1.84, size = 54, normalized size = 0.82

$$\frac{a^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{4x} + \frac{2abc^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{5} + \frac{b^2 c^{\frac{5}{2}} x (x^2)^{\frac{5}{2}}}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(5/2)*(b*x+a)**2/x**2,x)`

[Out] `a**2*c**(5/2)*(x**2)**(5/2)/(4*x) + 2*a*b*c**(5/2)*(x**2)**(5/2)/5 + b**2*c**
 (5/2)*x*(x**2)**(5/2)/6`

$$3.824 \quad \int \frac{(cx^2)^{5/2} (a+bx)^2}{x^3} dx$$

Optimal. Leaf size=66

$$\frac{1}{3}a^2c^2x^2\sqrt{cx^2} + \frac{1}{2}abc^2x^3\sqrt{cx^2} + \frac{1}{5}b^2c^2x^4\sqrt{cx^2}$$

[Out] $\frac{1}{3}a^2c^2x^2(c*x^2)^{(1/2)} + \frac{1}{2}a*b*c^2*x^3*(c*x^2)^{(1/2)} + \frac{1}{5}b^2*c^2*x^4*(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{1}{3}a^2c^2x^2\sqrt{cx^2} + \frac{1}{2}abc^2x^3\sqrt{cx^2} + \frac{1}{5}b^2c^2x^4\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^2)/x^3, x]

[Out] $(a^2*c^2*x^2*\text{Sqrt}[c*x^2])/3 + (a*b*c^2*x^3*\text{Sqrt}[c*x^2])/2 + (b^2*c^2*x^4*\text{Sqrt}[c*x^2])/5$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)^2}{x^3} dx &= \frac{(c^2\sqrt{cx^2}) \int x^2(a+bx)^2 dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (a^2x^2 + 2abx^3 + b^2x^4) dx}{x} \\ &= \frac{1}{3}a^2c^2x^2\sqrt{cx^2} + \frac{1}{2}abc^2x^3\sqrt{cx^2} + \frac{1}{5}b^2c^2x^4\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 38, normalized size = 0.58

$$\frac{1}{30}c^2x^2\sqrt{cx^2} (10a^2 + 15abx + 6b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^2)/x^3,x]

[Out] (c^2*x^2*sqrt[c*x^2]*(10*a^2 + 15*a*b*x + 6*b^2*x^2))/30

fricas [A] time = 0.46, size = 42, normalized size = 0.64

$$\frac{1}{30} (6b^2c^2x^4 + 15abc^2x^3 + 10a^2c^2x^2)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^3,x, algorithm="fricas")

[Out] 1/30*(6*b^2*c^2*x^4 + 15*a*b*c^2*x^3 + 10*a^2*c^2*x^2)*sqrt(c*x^2)

giac [A] time = 0.94, size = 44, normalized size = 0.67

$$\frac{1}{30} (6b^2c^2x^5\text{sgn}(x) + 15abc^2x^4\text{sgn}(x) + 10a^2c^2x^3\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^3,x, algorithm="giac")

[Out] 1/30*(6*b^2*c^2*x^5*sgn(x) + 15*a*b*c^2*x^4*sgn(x) + 10*a^2*c^2*x^3*sgn(x)) *sqrt(c)

maple [A] time = 0.00, size = 32, normalized size = 0.48

$$\frac{(6b^2x^2 + 15abx + 10a^2)(cx^2)^{\frac{5}{2}}}{30x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)*(b*x+a)^2/x^3,x)`

[Out] `1/30/x^2*(6*b^2*x^2+15*a*b*x+10*a^2)*(c*x^2)^(5/2)`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(5/2)*(b*x+a)^2/x^3,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{5/2} (a+bx)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(5/2)*(a + b*x)^2)/x^3,x)`

[Out] `int(((c*x^2)^(5/2)*(a + b*x)^2)/x^3, x)`

sympy [A] time = 1.95, size = 54, normalized size = 0.82

$$\frac{a^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{3x^2} + \frac{abc^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{2x} + \frac{b^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(5/2)*(b*x+a)**2/x**3,x)`

[Out] `a**2*c**(5/2)*(x**2)**(5/2)/(3*x**2) + a*b*c**(5/2)*(x**2)**(5/2)/(2*x) + b**2*c**(5/2)*(x**2)**(5/2)/5`

$$3.825 \quad \int \frac{(cx^2)^{5/2} (a+bx)^2}{x^4} dx$$

Optimal. Leaf size=64

$$\frac{1}{2}a^2c^2x\sqrt{cx^2} + \frac{2}{3}abc^2x^2\sqrt{cx^2} + \frac{1}{4}b^2c^2x^3\sqrt{cx^2}$$

[Out] $\frac{1}{2}a^2c^2x\sqrt{cx^2} + \frac{2}{3}abc^2x^2\sqrt{cx^2} + \frac{1}{4}b^2c^2x^3\sqrt{cx^2}$

Rubi [A] time = 0.01, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{1}{2}a^2c^2x\sqrt{cx^2} + \frac{2}{3}abc^2x^2\sqrt{cx^2} + \frac{1}{4}b^2c^2x^3\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^2)/x^4,x]

[Out] $(a^2c^2x\sqrt{cx^2})/2 + (2ab^2c^2x^2\sqrt{cx^2})/3 + (b^2c^2x^3\sqrt{cx^2})/4$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)^2}{x^4} dx &= \frac{(c^2\sqrt{cx^2}) \int x(a+bx)^2 dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int (a^2x + 2abx^2 + b^2x^3) dx}{x} \\ &= \frac{1}{2}a^2c^2x\sqrt{cx^2} + \frac{2}{3}abc^2x^2\sqrt{cx^2} + \frac{1}{4}b^2c^2x^3\sqrt{cx^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 36, normalized size = 0.56

$$\frac{1}{12}c^2x\sqrt{cx^2} (6a^2 + 8abx + 3b^2x^2)$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^2)/x^4,x]

[Out] (c^2*x*Sqrt[c*x^2]*(6*a^2 + 8*a*b*x + 3*b^2*x^2))/12

fricas [A] time = 0.42, size = 40, normalized size = 0.62

$$\frac{1}{12} (3b^2c^2x^3 + 8abc^2x^2 + 6a^2c^2x)\sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^4,x, algorithm="fricas")

[Out] 1/12*(3*b^2*c^2*x^3 + 8*a*b*c^2*x^2 + 6*a^2*c^2*x)*sqrt(c*x^2)

giac [A] time = 1.05, size = 44, normalized size = 0.69

$$\frac{1}{12} (3b^2c^2x^4\text{sgn}(x) + 8abc^2x^3\text{sgn}(x) + 6a^2c^2x^2\text{sgn}(x))\sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^4,x, algorithm="giac")

[Out] 1/12*(3*b^2*c^2*x^4*sgn(x) + 8*a*b*c^2*x^3*sgn(x) + 6*a^2*c^2*x^2*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 32, normalized size = 0.50

$$\frac{(3b^2x^2 + 8abx + 6a^2)(cx^2)^{\frac{5}{2}}}{12x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)*(b*x+a)^2/x^4,x)`

[Out] `1/12/x^3*(3*b^2*x^2+8*a*b*x+6*a^2)*(c*x^2)^(5/2)`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(5/2)*(b*x+a)^2/x^4,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{5/2} (a+bx)^2}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(5/2)*(a + b*x)^2)/x^4,x)`

[Out] `int(((c*x^2)^(5/2)*(a + b*x)^2)/x^4, x)`

sympy [A] time = 2.01, size = 60, normalized size = 0.94

$$\frac{a^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{2x^3} + \frac{2abc^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{3x^2} + \frac{b^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(5/2)*(b*x+a)**2/x**4,x)`

[Out] `a**2*c**(5/2)*(x**2)**(5/2)/(2*x**3) + 2*a*b*c**(5/2)*(x**2)**(5/2)/(3*x**2) + b**2*c**(5/2)*(x**2)**(5/2)/(4*x)`

$$3.826 \quad \int \frac{(cx^2)^{5/2} (a+bx)^2}{x^5} dx$$

Optimal. Leaf size=29

$$\frac{c^2 \sqrt{cx^2} (a+bx)^3}{3bx}$$

[Out] 1/3*c^2*(b*x+a)^3*(c*x^2)^(1/2)/b/x

Rubi [A] time = 0.00, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$\frac{c^2 \sqrt{cx^2} (a+bx)^3}{3bx}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^2)/x^5,x]

[Out] (c^2*Sqrt[c*x^2]*(a + b*x)^3)/(3*b*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)^2}{x^5} dx &= \frac{\left(c^2 \sqrt{cx^2}\right) \int (a+bx)^2 dx}{x} \\ &= \frac{c^2 \sqrt{cx^2} (a+bx)^3}{3bx} \end{aligned}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 0.90

$$\frac{(cx^2)^{5/2} (a+bx)^3}{3bx^5}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^2)/x^5,x]

[Out] ((c*x^2)^(5/2)*(a + b*x)^3)/(3*b*x^5)

fricas [A] time = 0.42, size = 36, normalized size = 1.24

$$\frac{1}{3} (b^2 c^2 x^2 + 3 abc^2 x + 3 a^2 c^2) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^5,x, algorithm="fricas")

[Out] 1/3*(b^2*c^2*x^2 + 3*a*b*c^2*x + 3*a^2*c^2)*sqrt(c*x^2)

giac [A] time = 1.12, size = 41, normalized size = 1.41

$$\frac{1}{3} (b^2 c^2 x^3 \operatorname{sgn}(x) + 3 abc^2 x^2 \operatorname{sgn}(x) + 3 a^2 c^2 x \operatorname{sgn}(x)) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^5,x, algorithm="giac")

[Out] 1/3*(b^2*c^2*x^3*sgn(x) + 3*a*b*c^2*x^2*sgn(x) + 3*a^2*c^2*x*sgn(x))*sqrt(c)

maple [A] time = 0.00, size = 31, normalized size = 1.07

$$\frac{(b^2 x^2 + 3 abx + 3 a^2) (c x^2)^{\frac{5}{2}}}{3 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)^2/x^5,x)

[Out] 1/3/x^4*(b^2*x^2+3*a*b*x+3*a^2)*(c*x^2)^(5/2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^5,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
 expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(cx^2)^{5/2} (a+bx)^2}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(5/2)*(a + b*x)^2)/x^5, x)

[Out] int(((c*x^2)^(5/2)*(a + b*x)^2)/x^5, x)

sympy [B] time = 2.03, size = 56, normalized size = 1.93

$$\frac{a^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{x^4} + \frac{abc^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{x^3} + \frac{b^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a)**2/x**5, x)

[Out] a**2*c**(5/2)*(x**2)**(5/2)/x**4 + a*b*c**(5/2)*(x**2)**(5/2)/x**3 + b**2*c
 (5/2)(x**2)**(5/2)/(3*x**2)

$$3.827 \quad \int \frac{(cx^2)^{5/2} (a+bx)^2}{x^6} dx$$

Optimal. Leaf size=58

$$\frac{a^2c^2\sqrt{cx^2} \log(x)}{x} + 2abc^2\sqrt{cx^2} + \frac{1}{2}b^2c^2x\sqrt{cx^2}$$

[Out] $2*a*b*c^2*(c*x^2)^{(1/2)}+1/2*b^2*c^2*x*(c*x^2)^{(1/2)}+a^2*c^2*\ln(x)*(c*x^2)^{(1/2)}/x$

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2c^2\sqrt{cx^2} \log(x)}{x} + 2abc^2\sqrt{cx^2} + \frac{1}{2}b^2c^2x\sqrt{cx^2}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^2)/x^6,x]

[Out] $2*a*b*c^2*\text{Sqrt}[c*x^2] + (b^2*c^2*x*\text{Sqrt}[c*x^2])/2 + (a^2*c^2*\text{Sqrt}[c*x^2]*\text{Log}[x])/x$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{5/2} (a+bx)^2}{x^6} dx &= \frac{(c^2\sqrt{cx^2})}{x} \int \frac{(a+bx)^2}{x} dx \\
&= \frac{(c^2\sqrt{cx^2})}{x} \int \left(2ab + \frac{a^2}{x} + b^2x\right) dx \\
&= 2abc^2\sqrt{cx^2} + \frac{1}{2}b^2c^2x\sqrt{cx^2} + \frac{a^2c^2\sqrt{cx^2} \log(x)}{x}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.60

$$\frac{c^3x(2a^2\log(x) + bx(4a + bx))}{2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^2)/x^6,x]

[Out] (c^3*x*(b*x*(4*a + b*x) + 2*a^2*Log[x]))/(2*Sqrt[c*x^2])

fricas [A] time = 0.43, size = 41, normalized size = 0.71

$$\frac{(b^2c^2x^2 + 4abc^2x + 2a^2c^2\log(x))\sqrt{cx^2}}{2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^6,x, algorithm="fricas")

[Out] 1/2*(b^2*c^2*x^2 + 4*a*b*c^2*x + 2*a^2*c^2*log(x))*sqrt(c*x^2)/x

giac [A] time = 1.08, size = 41, normalized size = 0.71

$$\frac{1}{2} \left(b^2c^2x^2\operatorname{sgn}(x) + 4abc^2x\operatorname{sgn}(x) + 2a^2c^2\log(|x|)\operatorname{sgn}(x) \right) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^2/x^6,x, algorithm="giac")

[Out] 1/2*(b^2*c^2*x^2*sgn(x) + 4*a*b*c^2*x*sgn(x) + 2*a^2*c^2*log(abs(x))*sgn(x))*sqrt(c)

maple [A] time = 0.01, size = 33, normalized size = 0.57

$$\frac{(cx^2)^{\frac{5}{2}}(b^2x^2 + 2a^2 \ln(x) + 4abx)}{2x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)*(b*x+a)^2/x^6,x)`

[Out] `1/2*(c*x^2)^(5/2)*(b^2*x^2+2*a^2*ln(x)+4*a*b*x)/x^5`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(5/2)*(b*x+a)^2/x^6,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{5/2}(a+bx)^2}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(5/2)*(a + b*x)^2)/x^6,x)`

[Out] `int(((c*x^2)^(5/2)*(a + b*x)^2)/x^6, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}}(a+bx)^2}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(5/2)*(b*x+a)**2/x**6,x)`

[Out] `Integral((c*x**2)**(5/2)*(a + b*x)**2/x**6, x)`

$$3.828 \quad \int \frac{x^3(a+bx)^2}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=57

$$\frac{a^2x^4}{3\sqrt{cx^2}} + \frac{abx^5}{2\sqrt{cx^2}} + \frac{b^2x^6}{5\sqrt{cx^2}}$$

[Out] $1/3*a^2*x^4/(c*x^2)^{(1/2)}+1/2*a*b*x^5/(c*x^2)^{(1/2)}+1/5*b^2*x^6/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2x^4}{3\sqrt{cx^2}} + \frac{abx^5}{2\sqrt{cx^2}} + \frac{b^2x^6}{5\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^3*(a + b*x)^2)/Sqrt[c*x^2], x]

[Out] $(a^2*x^4)/(3*\text{Sqrt}[c*x^2]) + (a*b*x^5)/(2*\text{Sqrt}[c*x^2]) + (b^2*x^6)/(5*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_.))^(m_.), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3(a+bx)^2}{\sqrt{cx^2}} dx &= \frac{x \int x^2(a+bx)^2 dx}{\sqrt{cx^2}} \\ &= \frac{x \int (a^2x^2 + 2abx^3 + b^2x^4) dx}{\sqrt{cx^2}} \\ &= \frac{a^2x^4}{3\sqrt{cx^2}} + \frac{abx^5}{2\sqrt{cx^2}} + \frac{b^2x^6}{5\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.61

$$\frac{x^4(10a^2 + 15abx + 6b^2x^2)}{30\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*(a + b*x)^2)/Sqrt[c*x^2], x]

[Out] (x^4*(10*a^2 + 15*a*b*x + 6*b^2*x^2))/(30*Sqrt[c*x^2])

fricas [A] time = 0.41, size = 36, normalized size = 0.63

$$\frac{(6b^2x^4 + 15abx^3 + 10a^2x^2)\sqrt{cx^2}}{30c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] 1/30*(6*b^2*x^4 + 15*a*b*x^3 + 10*a^2*x^2)*sqrt(c*x^2)/c

giac [A] time = 0.94, size = 41, normalized size = 0.72

$$\frac{1}{30} \sqrt{cx^2} \left(3 \left(\frac{2b^2x}{c} + \frac{5ab}{c} \right) x + \frac{10a^2}{c} \right) x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2/(c*x^2)^(1/2), x, algorithm="giac")

[Out] 1/30*sqrt(c*x^2)*(3*(2*b^2*x/c + 5*a*b/c)*x + 10*a^2/c)*x^2

maple [A] time = 0.00, size = 32, normalized size = 0.56

$$\frac{(6b^2x^2 + 15abx + 10a^2)x^4}{30\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3*(b*x+a)^2/(c*x^2)^(1/2),x)`

[Out] $1/30*x^4*(6*b^2*x^2+15*a*b*x+10*a^2)/(c*x^2)^(1/2)$

maxima [A] time = 1.34, size = 54, normalized size = 0.95

$$\frac{\sqrt{cx^2} b^2 x^4}{5c} + \frac{\sqrt{cx^2} abx^3}{2c} + \frac{\sqrt{cx^2} a^2 x^2}{3c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3*(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $1/5*\sqrt{c*x^2}*b^2*x^4/c + 1/2*\sqrt{c*x^2}*a*b*x^3/c + 1/3*\sqrt{c*x^2}*a^2*x^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^3 (a + bx)^2}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x^3*(a + b*x)^2)/(c*x^2)^(1/2),x)`

[Out] `int((x^3*(a + b*x)^2)/(c*x^2)^(1/2), x)`

sympy [A] time = 0.79, size = 60, normalized size = 1.05

$$\frac{a^2 x^4}{3\sqrt{c} \sqrt{x^2}} + \frac{abx^5}{2\sqrt{c} \sqrt{x^2}} + \frac{b^2 x^6}{5\sqrt{c} \sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3*(b*x+a)**2/(c*x**2)**(1/2),x)`

[Out] $a**2*x**4/(3*\sqrt{c}*\sqrt{x**2}) + a*b*x**5/(2*\sqrt{c}*\sqrt{x**2}) + b**2*x**6/(5*\sqrt{c}*\sqrt{x**2})$

$$3.829 \quad \int \frac{x^2(a+bx)^2}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=57

$$\frac{a^2x^3}{2\sqrt{cx^2}} + \frac{2abx^4}{3\sqrt{cx^2}} + \frac{b^2x^5}{4\sqrt{cx^2}}$$

[Out] $1/2*a^2*x^3/(c*x^2)^{(1/2)}+2/3*a*b*x^4/(c*x^2)^{(1/2)}+1/4*b^2*x^5/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2x^3}{2\sqrt{cx^2}} + \frac{2abx^4}{3\sqrt{cx^2}} + \frac{b^2x^5}{4\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^2*(a + b*x)^2)/Sqrt[c*x^2], x]

[Out] (a^2*x^3)/(2*Sqrt[c*x^2]) + (2*a*b*x^4)/(3*Sqrt[c*x^2]) + (b^2*x^5)/(4*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2(a+bx)^2}{\sqrt{cx^2}} dx &= \frac{x \int x(a+bx)^2 dx}{\sqrt{cx^2}} \\ &= \frac{x \int (a^2x + 2abx^2 + b^2x^3) dx}{\sqrt{cx^2}} \\ &= \frac{a^2x^3}{2\sqrt{cx^2}} + \frac{2abx^4}{3\sqrt{cx^2}} + \frac{b^2x^5}{4\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.61

$$\frac{x^3(6a^2 + 8abx + 3b^2x^2)}{12\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*(a + b*x)^2)/Sqrt[c*x^2], x]

[Out] (x^3*(6*a^2 + 8*a*b*x + 3*b^2*x^2))/(12*Sqrt[c*x^2])

fricas [A] time = 0.41, size = 34, normalized size = 0.60

$$\frac{(3b^2x^3 + 8abx^2 + 6a^2x)\sqrt{cx^2}}{12c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] 1/12*(3*b^2*x^3 + 8*a*b*x^2 + 6*a^2*x)*sqrt(c*x^2)/c

giac [A] time = 1.25, size = 38, normalized size = 0.67

$$\frac{1}{12} \sqrt{cx^2} \left(\left(\frac{3b^2x}{c} + \frac{8ab}{c} \right) x + \frac{6a^2}{c} \right) x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2/(c*x^2)^(1/2), x, algorithm="giac")

[Out] 1/12*sqrt(c*x^2)*((3*b^2*x/c + 8*a*b/c)*x + 6*a^2/c)*x

maple [A] time = 0.00, size = 32, normalized size = 0.56

$$\frac{(3b^2x^2 + 8abx + 6a^2)x^3}{12\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(b*x+a)^2/(c*x^2)^(1/2),x)`

[Out] $1/12*x^3*(3*b^2*x^2+8*a*b*x+6*a^2)/(c*x^2)^(1/2)$

maxima [A] time = 1.32, size = 47, normalized size = 0.82

$$\frac{\sqrt{cx^2} b^2 x^3}{4c} + \frac{2\sqrt{cx^2} abx^2}{3c} + \frac{a^2 x^2}{2\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $1/4*\text{sqrt}(c*x^2)*b^2*x^3/c + 2/3*\text{sqrt}(c*x^2)*a*b*x^2/c + 1/2*a^2*x^2/\text{sqrt}(c)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^2 (a + bx)^2}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x^2*(a + b*x)^2)/(c*x^2)^(1/2),x)`

[Out] `int((x^2*(a + b*x)^2)/(c*x^2)^(1/2), x)`

sympy [A] time = 0.65, size = 61, normalized size = 1.07

$$\frac{a^2 x^3}{2\sqrt{c} \sqrt{x^2}} + \frac{2abx^4}{3\sqrt{c} \sqrt{x^2}} + \frac{b^2 x^5}{4\sqrt{c} \sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(b*x+a)**2/(c*x**2)**(1/2),x)`

[Out] `a**2*x**3/(2*sqrt(c)*sqrt(x**2)) + 2*a*b*x**4/(3*sqrt(c)*sqrt(x**2)) + b**2*x**5/(4*sqrt(c)*sqrt(x**2))`

$$3.830 \quad \int \frac{x(a+bx)^2}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=24

$$\frac{x(a+bx)^3}{3b\sqrt{cx^2}}$$

[Out] 1/3*x*(b*x+a)^3/b/(c*x^2)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 24, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 32}

$$\frac{x(a+bx)^3}{3b\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x*(a + b*x)^2)/Sqrt[c*x^2], x]

[Out] (x*(a + b*x)^3)/(3*b*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{x(a+bx)^2}{\sqrt{cx^2}} dx &= \frac{x \int (a+bx)^2 dx}{\sqrt{cx^2}} \\ &= \frac{x(a+bx)^3}{3b\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 1.00

$$\frac{x(a+bx)^3}{3b\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x*(a + b*x)^2)/Sqrt[c*x^2],x]

[Out] (x*(a + b*x)^3)/(3*b*Sqrt[c*x^2])

fricas [A] time = 0.43, size = 30, normalized size = 1.25

$$\frac{(b^2x^2 + 3abx + 3a^2)\sqrt{cx^2}}{3c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/3*(b^2*x^2 + 3*a*b*x + 3*a^2)*sqrt(c*x^2)/c

giac [A] time = 1.15, size = 36, normalized size = 1.50

$$\frac{1}{3} \sqrt{cx^2} \left(\left(\frac{b^2x}{c} + \frac{3ab}{c} \right) x + \frac{3a^2}{c} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out] 1/3*sqrt(c*x^2)*((b^2*x/c + 3*a*b/c)*x + 3*a^2/c)

maple [A] time = 0.00, size = 31, normalized size = 1.29

$$\frac{(b^2x^2 + 3abx + 3a^2)x^2}{3\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^2/(c*x^2)^(1/2),x)

[Out] 1/3*x^2*(b^2*x^2+3*a*b*x+3*a^2)/(c*x^2)^(1/2)

maxima [B] time = 1.37, size = 42, normalized size = 1.75

$$\frac{\sqrt{cx^2} b^2x^2}{3c} + \frac{abx^2}{\sqrt{c}} + \frac{\sqrt{cx^2} a^2}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] $1/3*\sqrt{c*x^2}*b^2*x^2/c + a*b*x^2/\sqrt{c} + \sqrt{c*x^2}*a^2/c$

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{x(a+bx)^2}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x*(a + b*x)^2)/(c*x^2)^(1/2), x)`

[Out] `int((x*(a + b*x)^2)/(c*x^2)^(1/2), x)`

sympy [B] time = 0.54, size = 56, normalized size = 2.33

$$\frac{a^2x^2}{\sqrt{c}\sqrt{x^2}} + \frac{abx^3}{\sqrt{c}\sqrt{x^2}} + \frac{b^2x^4}{3\sqrt{c}\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**2/(c*x**2)**(1/2), x)`

[Out] `a**2*x**2/(sqrt(c)*sqrt(x**2)) + a*b*x**3/(sqrt(c)*sqrt(x**2)) + b**2*x**4/(3*sqrt(c)*sqrt(x**2))`

$$3.831 \quad \int \frac{(a+bx)^2}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=52

$$\frac{a^2 x \log(x)}{\sqrt{cx^2}} + \frac{2abx^2}{\sqrt{cx^2}} + \frac{b^2 x^3}{2\sqrt{cx^2}}$$

[Out] $2*a*b*x^2/(c*x^2)^{(1/2)}+1/2*b^2*x^3/(c*x^2)^{(1/2)}+a^2*x*\ln(x)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 52, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$\frac{a^2 x \log(x)}{\sqrt{cx^2}} + \frac{2abx^2}{\sqrt{cx^2}} + \frac{b^2 x^3}{2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/Sqrt[c*x^2], x]

[Out] $(2*a*b*x^2)/\text{Sqrt}[c*x^2] + (b^2*x^3)/(2*\text{Sqrt}[c*x^2]) + (a^2*x*\text{Log}[x])/ \text{Sqrt}[c*x^2]$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_)^(m_.))*((c_.) + (d_.)*(x_)^(n_.)), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{\sqrt{cx^2}} dx &= \frac{x \int \frac{(a+bx)^2}{x} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(2ab + \frac{a^2}{x} + b^2x\right) dx}{\sqrt{cx^2}} \\ &= \frac{2abx^2}{\sqrt{cx^2}} + \frac{b^2x^3}{2\sqrt{cx^2}} + \frac{a^2x \log(x)}{\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 32, normalized size = 0.62

$$\frac{x(2a^2 \log(x) + bx(4a + bx))}{2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/Sqrt[c*x^2], x]

[Out] (x*(b*x*(4*a + b*x) + 2*a^2*Log[x]))/(2*Sqrt[c*x^2])

fricas [A] time = 0.41, size = 35, normalized size = 0.67

$$\frac{(b^2x^2 + 4abx + 2a^2 \log(x))\sqrt{cx^2}}{2cx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] 1/2*(b^2*x^2 + 4*a*b*x + 2*a^2*log(x))*sqrt(c*x^2)/(c*x)

giac [A] time = 1.12, size = 50, normalized size = 0.96

$$-\frac{a^2 \log\left(\left|-\sqrt{c}x + \sqrt{cx^2}\right|\right)}{\sqrt{c}} + \frac{1}{2} \sqrt{cx^2} \left(\frac{b^2x}{c} + \frac{4ab}{c}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(c*x^2)^(1/2), x, algorithm="giac")

[Out] -a^2*log(abs(-sqrt(c)*x + sqrt(c*x^2)))/sqrt(c) + 1/2*sqrt(c*x^2)*(b^2*x/c + 4*a*b/c)

maple [A] time = 0.00, size = 31, normalized size = 0.60

$$\frac{(b^2x^2 + 2a^2 \ln(x) + 4abx)x}{2\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/(c*x^2)^(1/2),x)`

[Out] `1/2*x*(b^2*x^2+2*a^2*ln(x)+4*a*b*x)/(c*x^2)^(1/2)`

maxima [A] time = 1.35, size = 35, normalized size = 0.67

$$\frac{b^2x^2}{2\sqrt{c}} + \frac{a^2 \log(x)}{\sqrt{c}} + \frac{2\sqrt{cx^2}ab}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] `1/2*b^2*x^2/sqrt(c) + a^2*log(x)/sqrt(c) + 2*sqrt(c*x^2)*a*b/c`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^2}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(c*x^2)^(1/2),x)`

[Out] `int((a + b*x)^2/(c*x^2)^(1/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^2}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/(c*x**2)**(1/2),x)`

[Out] `Integral((a + b*x)**2/sqrt(c*x**2), x)`

$$3.832 \quad \int \frac{(a+bx)^2}{x\sqrt{cx^2}} dx$$

Optimal. Leaf size=47

$$-\frac{a^2}{\sqrt{cx^2}} + \frac{2abx \log(x)}{\sqrt{cx^2}} + \frac{b^2x^2}{\sqrt{cx^2}}$$

[Out] $-a^2/(c*x^2)^{(1/2)}+b^2*x^2/(c*x^2)^{(1/2)}+2*a*b*x*\ln(x)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{\sqrt{cx^2}} + \frac{2abx \log(x)}{\sqrt{cx^2}} + \frac{b^2x^2}{\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x*Sqrt[c*x^2]),x]

[Out] $-(a^2/\text{Sqrt}[c*x^2]) + (b^2*x^2)/\text{Sqrt}[c*x^2] + (2*a*b*x*\text{Log}[x])/ \text{Sqrt}[c*x^2]$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x\sqrt{cx^2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^2} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(b^2 + \frac{a^2}{x^2} + \frac{2ab}{x} \right) dx}{\sqrt{cx^2}} \\ &= -\frac{a^2}{\sqrt{cx^2}} + \frac{b^2x^2}{\sqrt{cx^2}} + \frac{2abx \log(x)}{\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 34, normalized size = 0.72

$$\frac{cx^2(-a^2 + 2abx \log(x) + b^2x^2)}{(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x*Sqrt[c*x^2]),x]

[Out] (c*x^2*(-a^2 + b^2*x^2 + 2*a*b*x*Log[x]))/(c*x^2)^(3/2)

fricas [A] time = 0.42, size = 34, normalized size = 0.72

$$\frac{(b^2x^2 + 2abx \log(x) - a^2)\sqrt{cx^2}}{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] (b^2*x^2 + 2*a*b*x*log(x) - a^2)*sqrt(c*x^2)/(c*x^2)

giac [A] time = 0.94, size = 65, normalized size = 1.38

$$\frac{\sqrt{cx^2} b^2}{c} - \frac{2 \left(ab \log \left(\left| -\sqrt{c} x + \sqrt{cx^2} \right| \right) - \frac{a^2 \sqrt{c}}{\sqrt{c} x - \sqrt{cx^2}} \right)}{\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x/(c*x^2)^(1/2),x, algorithm="giac")

[Out] sqrt(c*x^2)*b^2/c - 2*(a*b*log(abs(-sqrt(c)*x + sqrt(c*x^2))) - a^2*sqrt(c)/(sqrt(c)*x - sqrt(c*x^2)))/sqrt(c)

maple [A] time = 0.00, size = 29, normalized size = 0.62

$$\frac{2abx \ln(x) + b^2x^2 - a^2}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/x/(c*x^2)^(1/2), x)

[Out] (2*a*b*x*ln(x)+b^2*x^2-a^2)/(c*x^2)^(1/2)

maxima [A] time = 1.36, size = 35, normalized size = 0.74

$$\frac{2ab \log(x)}{\sqrt{c}} + \frac{\sqrt{cx^2} b^2}{c} - \frac{a^2}{\sqrt{c} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x/(c*x^2)^(1/2), x, algorithm="maxima")

[Out] 2*a*b*log(x)/sqrt(c) + sqrt(c*x^2)*b^2/c - a^2/(sqrt(c)*x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^2}{x \sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(x*(c*x^2)^(1/2)), x)

[Out] int((a + b*x)^2/(x*(c*x^2)^(1/2)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^2}{x \sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/x/(c*x**2)**(1/2), x)

[Out] Integral((a + b*x)**2/(x*sqrt(c*x**2)), x)

$$3.833 \quad \int \frac{(a+bx)^2}{x^2 \sqrt{cx^2}} dx$$

Optimal. Leaf size=49

$$-\frac{a^2}{2x\sqrt{cx^2}} - \frac{2ab}{\sqrt{cx^2}} + \frac{b^2x \log(x)}{\sqrt{cx^2}}$$

[Out] $-2*a*b/(c*x^2)^{(1/2)} - 1/2*a^2/x/(c*x^2)^{(1/2)} + b^2*x*\ln(x)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{2x\sqrt{cx^2}} - \frac{2ab}{\sqrt{cx^2}} + \frac{b^2x \log(x)}{\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x^2*Sqrt[c*x^2]),x]

[Out] $(-2*a*b)/\text{Sqrt}[c*x^2] - a^2/(2*x*\text{Sqrt}[c*x^2]) + (b^2*x*\text{Log}[x])/ \text{Sqrt}[c*x^2]$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_)^(m_.))*((c_.) + (d_.)*(x_)^(n_.)), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^2\sqrt{cx^2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^3} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^3} + \frac{2ab}{x^2} + \frac{b^2}{x} \right) dx}{\sqrt{cx^2}} \\ &= -\frac{2ab}{\sqrt{cx^2}} - \frac{a^2}{2x\sqrt{cx^2}} + \frac{b^2x \log(x)}{\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.71

$$\frac{cx(2b^2x^2 \log(x) - a(a + 4bx))}{2(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x^2*Sqrt[c*x^2]), x]

[Out] (c*x*(-(a*(a + 4*b*x)) + 2*b^2*x^2*Log[x]))/(2*(c*x^2)^(3/2))

fricas [A] time = 0.43, size = 36, normalized size = 0.73

$$\frac{(2b^2x^2 \log(x) - 4abx - a^2)\sqrt{cx^2}}{2cx^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^2/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] 1/2*(2*b^2*x^2*log(x) - 4*a*b*x - a^2)*sqrt(c*x^2)/(c*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^2/(c*x^2)^(1/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.01, size = 34, normalized size = 0.69

$$\frac{2b^2x^2 \ln(x) - 4abx - a^2}{2\sqrt{cx^2} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^2/(c*x^2)^(1/2),x)`

[Out] `1/2/x*(2*b^2*x^2*ln(x)-4*a*b*x-a^2)/(c*x^2)^(1/2)`

maxima [A] time = 1.29, size = 31, normalized size = 0.63

$$\frac{b^2 \log(x)}{\sqrt{c}} - \frac{2ab}{\sqrt{c}x} - \frac{a^2}{2\sqrt{c}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^2/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] `b^2*log(x)/sqrt(c) - 2*a*b/(sqrt(c)*x) - 1/2*a^2/(sqrt(c)*x^2)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a+bx)^2}{x^2 \sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(x^2*(c*x^2)^(1/2)),x)`

[Out] `int((a + b*x)^2/(x^2*(c*x^2)^(1/2)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a+bx)^2}{x^2 \sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**2/(c*x**2)**(1/2),x)`

[Out] `Integral((a + b*x)**2/(x**2*sqrt(c*x**2)), x)`

$$3.834 \quad \int \frac{(a+bx)^2}{x^3 \sqrt{cx^2}} dx$$

Optimal. Leaf size=26

$$-\frac{(a+bx)^3}{3ax^2\sqrt{cx^2}}$$

[Out] $-1/3*(b*x+a)^3/a/x^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 37}

$$-\frac{(a+bx)^3}{3ax^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^2/(x^3*\text{Sqrt}[c*x^2]), x]$

[Out] $-(a + b*x)^3/(3*a*x^2*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 37

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)})*((c_.) + (d_.)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^3 \sqrt{cx^2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^4} dx}{\sqrt{cx^2}} \\ &= -\frac{(a+bx)^3}{3ax^2 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 1.27

$$\frac{c(-a^2 - 3abx - 3b^2x^2)}{3(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x^3*Sqrt[c*x^2]), x]

[Out] (c*(-a^2 - 3*a*b*x - 3*b^2*x^2))/(3*(c*x^2)^(3/2))

fricas [A] time = 0.45, size = 32, normalized size = 1.23

$$-\frac{(3b^2x^2 + 3abx + a^2)\sqrt{cx^2}}{3cx^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^3/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] -1/3*(3*b^2*x^2 + 3*a*b*x + a^2)*sqrt(c*x^2)/(c*x^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^2}{\sqrt{cx^2} x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^3/(c*x^2)^(1/2), x, algorithm="giac")

[Out] integrate((b*x + a)^2/(sqrt(c*x^2)*x^3), x)

maple [A] time = 0.00, size = 30, normalized size = 1.15

$$\frac{3b^2x^2 + 3abx + a^2}{3\sqrt{cx^2} x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/x^3/(c*x^2)^(1/2), x)

[Out] -1/3*(3*b^2*x^2+3*a*b*x+a^2)/x^2/(c*x^2)^(1/2)

maxima [A] time = 1.33, size = 33, normalized size = 1.27

$$-\frac{b^2}{\sqrt{c}x} - \frac{ab}{\sqrt{c}x^2} - \frac{a^2}{3\sqrt{c}x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^3/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] $-b^2/(\sqrt{c}*x) - a*b/(\sqrt{c}*x^2) - 1/3*a^2/(\sqrt{c}*x^3)$

mupad [B] time = 0.18, size = 33, normalized size = 1.27

$$-\frac{a^2 x^2 + 3 a b x^3 + 3 b^2 x^4}{3 \sqrt{c} (x^2)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(x^3*(c*x^2)^(1/2)),x)

[Out] $-(a^2*x^2 + 3*b^2*x^4 + 3*a*b*x^3)/(3*c^(1/2)*(x^2)^(5/2))$

sympy [B] time = 0.66, size = 53, normalized size = 2.04

$$-\frac{a^2}{3\sqrt{c}x^2\sqrt{x^2}} - \frac{ab}{\sqrt{c}x\sqrt{x^2}} - \frac{b^2}{\sqrt{c}\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/x**3/(c*x**2)**(1/2),x)

[Out] $-a**2/(3*\sqrt{c}*x**2*\sqrt{x**2}) - a*b/(\sqrt{c}*x*\sqrt{x**2}) - b**2/(\sqrt{c}*\sqrt{x**2})$

$$3.835 \quad \int \frac{(a+bx)^2}{x^4 \sqrt{cx^2}} dx$$

Optimal. Leaf size=57

$$-\frac{a^2}{4x^3 \sqrt{cx^2}} - \frac{2ab}{3x^2 \sqrt{cx^2}} - \frac{b^2}{2x \sqrt{cx^2}}$$

[Out] $-1/4*a^2/x^3/(c*x^2)^{(1/2)}-2/3*a*b/x^2/(c*x^2)^{(1/2)}-1/2*b^2/x/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{4x^3 \sqrt{cx^2}} - \frac{2ab}{3x^2 \sqrt{cx^2}} - \frac{b^2}{2x \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x^4*sqrt[c*x^2]),x]

[Out] $-a^2/(4*x^3*sqrt[c*x^2]) - (2*a*b)/(3*x^2*sqrt[c*x^2]) - b^2/(2*x*sqrt[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^4\sqrt{cx^2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^5} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^5} + \frac{2ab}{x^4} + \frac{b^2}{x^3} \right) dx}{\sqrt{cx^2}} \\ &= -\frac{a^2}{4x^3\sqrt{cx^2}} - \frac{2ab}{3x^2\sqrt{cx^2}} - \frac{b^2}{2x\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.61

$$\frac{-3a^2 - 8abx - 6b^2x^2}{12x^3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x^4*sqrt[c*x^2]), x]

[Out] (-3*a^2 - 8*a*b*x - 6*b^2*x^2)/(12*x^3*sqrt[c*x^2])

fricas [A] time = 0.42, size = 34, normalized size = 0.60

$$-\frac{(6b^2x^2 + 8abx + 3a^2)\sqrt{cx^2}}{12cx^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^4/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] -1/12*(6*b^2*x^2 + 8*a*b*x + 3*a^2)*sqrt(c*x^2)/(c*x^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^4/(c*x^2)^(1/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.01, size = 32, normalized size = 0.56

$$\frac{6b^2x^2 + 8abx + 3a^2}{12\sqrt{c}x^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^4/(c*x^2)^(1/2),x)`

[Out] $-1/12*(6*b^2*x^2+8*a*b*x+3*a^2)/x^3/(c*x^2)^(1/2)$

maxima [A] time = 1.33, size = 33, normalized size = 0.58

$$-\frac{b^2}{2\sqrt{c}x^2} - \frac{2ab}{3\sqrt{c}x^3} - \frac{a^2}{4\sqrt{c}x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^4/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $-1/2*b^2/(\text{sqrt}(c)*x^2) - 2/3*a*b/(\text{sqrt}(c)*x^3) - 1/4*a^2/(\text{sqrt}(c)*x^4)$

mupad [B] time = 0.19, size = 42, normalized size = 0.74

$$-\frac{3a^2\sqrt{x^2} + 6b^2x^2\sqrt{x^2} + 8abx\sqrt{x^2}}{12\sqrt{c}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(x^4*(c*x^2)^(1/2)),x)`

[Out] $-(3*a^2*(x^2)^(1/2) + 6*b^2*x^2*(x^2)^(1/2) + 8*a*b*x*(x^2)^(1/2))/(12*c^(1/2)*x^5)$

sympy [A] time = 0.82, size = 61, normalized size = 1.07

$$-\frac{a^2}{4\sqrt{c}x^3\sqrt{x^2}} - \frac{2ab}{3\sqrt{c}x^2\sqrt{x^2}} - \frac{b^2}{2\sqrt{c}x\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**4/(c*x**2)**(1/2),x)`

[Out] $-a**2/(4*\text{sqrt}(c)*x**3*\text{sqrt}(x**2)) - 2*a*b/(3*\text{sqrt}(c)*x**2*\text{sqrt}(x**2)) - b**2/(2*\text{sqrt}(c)*x*\text{sqrt}(x**2))$

$$3.836 \quad \int \frac{x^3(a+bx)^2}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=27

$$\frac{x(a+bx)^3}{3bc\sqrt{cx^2}}$$

[Out] $1/3*x*(b*x+a)^3/b/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$\frac{x(a+bx)^3}{3bc\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x^3*(a + b*x)^2)/(c*x^2)^{(3/2)}, x]$

[Out] $(x*(a + b*x)^3)/(3*b*c*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ $\text{FreeQ}\{a, m, n, x\}$ && $! \text{IntegerQ}[m]$

Rule 32

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}/(b*(m + 1)), x] /;$ $\text{FreeQ}\{a, b, m, x\}$ && $\text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{x^3(a+bx)^2}{(cx^2)^{3/2}} dx = \frac{x \int (a+bx)^2 dx}{c\sqrt{cx^2}} = \frac{x(a+bx)^3}{3bc\sqrt{cx^2}}$$

Mathematica [A] time = 0.00, size = 26, normalized size = 0.96

$$\frac{x^3(a + bx)^3}{3b(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*(a + b*x)^2)/(c*x^2)^(3/2),x]

[Out] (x^3*(a + b*x)^3)/(3*b*(c*x^2)^(3/2))

fricas [A] time = 0.41, size = 30, normalized size = 1.11

$$\frac{(b^2x^2 + 3abx + 3a^2)\sqrt{cx^2}}{3c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2/(c*x^2)^(3/2),x, algorithm="fricas")

[Out] 1/3*(b^2*x^2 + 3*a*b*x + 3*a^2)*sqrt(c*x^2)/c^2

giac [A] time = 1.05, size = 39, normalized size = 1.44

$$\frac{\sqrt{cx^2} \left(\left(\frac{b^2x}{c} + \frac{3ab}{c} \right) x + \frac{3a^2}{c} \right)}{3c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2/(c*x^2)^(3/2),x, algorithm="giac")

[Out] 1/3*sqrt(c*x^2)*((b^2*x/c + 3*a*b/c)*x + 3*a^2/c)/c

maple [A] time = 0.00, size = 31, normalized size = 1.15

$$\frac{(b^2x^2 + 3abx + 3a^2)x^4}{3(cx^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^2/(c*x^2)^(3/2),x)

[Out] 1/3*x^4*(b^2*x^2+3*a*b*x+3*a^2)/(c*x^2)^(3/2)

maxima [B] time = 1.36, size = 52, normalized size = 1.93

$$\frac{b^2x^4}{3\sqrt{cx^2c}} + \frac{abx^3}{\sqrt{cx^2c}} + \frac{a^2x^2}{\sqrt{cx^2c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2/(c*x^2)^(3/2), x, algorithm="maxima")

[Out] 1/3*b^2*x^4/(sqrt(c*x^2)*c) + a*b*x^3/(sqrt(c*x^2)*c) + a^2*x^2/(sqrt(c*x^2)*c)

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{x^3 (a + bx)^2}{(cx^2)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^3*(a + b*x)^2)/(c*x^2)^(3/2), x)

[Out] int((x^3*(a + b*x)^2)/(c*x^2)^(3/2), x)

sympy [B] time = 0.80, size = 56, normalized size = 2.07

$$\frac{a^2x^4}{c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} + \frac{abx^5}{c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} + \frac{b^2x^6}{3c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**2/(c*x**2)**(3/2), x)

[Out] a**2*x**4/(c**(3/2)*(x**2)**(3/2)) + a*b*x**5/(c**(3/2)*(x**2)**(3/2)) + b**2*x**6/(3*c**(3/2)*(x**2)**(3/2))

$$3.837 \quad \int \frac{x^2(a+bx)^2}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=61

$$\frac{a^2x \log(x)}{c\sqrt{cx^2}} + \frac{2abx^2}{c\sqrt{cx^2}} + \frac{b^2x^3}{2c\sqrt{cx^2}}$$

[Out] $2*a*b*x^2/c/(c*x^2)^{(1/2)}+1/2*b^2*x^3/c/(c*x^2)^{(1/2)}+a^2*x*\ln(x)/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2x \log(x)}{c\sqrt{cx^2}} + \frac{2abx^2}{c\sqrt{cx^2}} + \frac{b^2x^3}{2c\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x^2*(a + b*x)^2)/(c*x^2)^{(3/2)}, x]$

[Out] $(2*a*b*x^2)/(c*\text{Sqrt}[c*x^2]) + (b^2*x^3)/(2*c*\text{Sqrt}[c*x^2]) + (a^2*x*\text{Log}[x])/(c*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2(a+bx)^2}{(cx^2)^{3/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(2ab + \frac{a^2}{x} + b^2x\right) dx}{c\sqrt{cx^2}} \\ &= \frac{2abx^2}{c\sqrt{cx^2}} + \frac{b^2x^3}{2c\sqrt{cx^2}} + \frac{a^2x \log(x)}{c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 34, normalized size = 0.56

$$\frac{x^3(2a^2 \log(x) + bx(4a + bx))}{2(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*(a + b*x)^2)/(c*x^2)^(3/2), x]

[Out] (x^3*(b*x*(4*a + b*x) + 2*a^2*Log[x]))/(2*(c*x^2)^(3/2))

fricas [A] time = 0.43, size = 35, normalized size = 0.57

$$\frac{(b^2x^2 + 4abx + 2a^2 \log(x))\sqrt{cx^2}}{2c^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] 1/2*(b^2*x^2 + 4*a*b*x + 2*a^2*log(x))*sqrt(c*x^2)/(c^2*x)

giac [A] time = 1.10, size = 55, normalized size = 0.90

$$-\frac{\frac{2a^2 \log\left(|-\sqrt{c}x + \sqrt{cx^2}\right|)}{\sqrt{c}} - \sqrt{cx^2} \left(\frac{b^2x}{c} + \frac{4ab}{c}\right)}{2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2/(c*x^2)^(3/2), x, algorithm="giac")

[Out] $-1/2*(2*a^2*\log(\text{abs}(-\text{sqrt}(c)*x + \text{sqrt}(c*x^2)))/\text{sqrt}(c) - \text{sqrt}(c*x^2)*(b^2*x/c + 4*a*b/c))/c$

maple [A] time = 0.00, size = 33, normalized size = 0.54

$$\frac{(b^2x^2 + 2a^2 \ln(x) + 4abx)x^3}{2(c x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(b*x+a)^2/(c*x^2)^(3/2),x)`

[Out] $1/2*x^3*(b^2*x^2+2*a^2*\ln(x)+4*a*b*x)/(c*x^2)^(3/2)$

maxima [A] time = 1.33, size = 45, normalized size = 0.74

$$\frac{b^2x^3}{2\sqrt{cx^2}c} + \frac{2abx^2}{\sqrt{cx^2}c} + \frac{a^2\log(x)}{c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(b*x+a)^2/(c*x^2)^(3/2),x, algorithm="maxima")`

[Out] $1/2*b^2*x^3/(\text{sqrt}(c*x^2)*c) + 2*a*b*x^2/(\text{sqrt}(c*x^2)*c) + a^2*\log(x)/c^(3/2)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^2 (a + bx)^2}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x^2*(a + b*x)^2)/(c*x^2)^(3/2),x)`

[Out] `int((x^2*(a + b*x)^2)/(c*x^2)^(3/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2 (a + bx)^2}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(b*x+a)**2/(c*x**2)**(3/2),x)`

[Out] `Integral(x**2*(a + b*x)**2/(c*x**2)**(3/2), x)`

$$3.838 \quad \int \frac{x(a+bx)^2}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=56

$$-\frac{a^2}{c\sqrt{cx^2}} + \frac{2abx \log(x)}{c\sqrt{cx^2}} + \frac{b^2x^2}{c\sqrt{cx^2}}$$

[Out] $-a^2/c/(c*x^2)^{(1/2)}+b^2*x^2/c/(c*x^2)^{(1/2)}+2*a*b*x*\ln(x)/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a^2}{c\sqrt{cx^2}} + \frac{2abx \log(x)}{c\sqrt{cx^2}} + \frac{b^2x^2}{c\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x*(a + b*x)^2)/(c*x^2)^(3/2), x]

[Out] $-(a^2/(c*\text{Sqrt}[c*x^2])) + (b^2*x^2)/(c*\text{Sqrt}[c*x^2]) + (2*a*b*x*\text{Log}[x])/(c*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x(a+bx)^2}{(cx^2)^{3/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^2} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(b^2 + \frac{a^2}{x^2} + \frac{2ab}{x}\right) dx}{c\sqrt{cx^2}} \\ &= -\frac{a^2}{c\sqrt{cx^2}} + \frac{b^2x^2}{c\sqrt{cx^2}} + \frac{2abx \log(x)}{c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.59

$$\frac{x^2(-a^2 + 2abx \log(x) + b^2x^2)}{(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x*(a + b*x)^2)/(c*x^2)^(3/2),x]

[Out] (x^2*(-a^2 + b^2*x^2 + 2*a*b*x*Log[x]))/(c*x^2)^(3/2)

fricas [A] time = 0.43, size = 34, normalized size = 0.61

$$\frac{(b^2x^2 + 2abx \log(x) - a^2)\sqrt{cx^2}}{c^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2/(c*x^2)^(3/2),x, algorithm="fricas")

[Out] (b^2*x^2 + 2*a*b*x*log(x) - a^2)*sqrt(c*x^2)/(c^2*x^2)

giac [A] time = 1.08, size = 69, normalized size = 1.23

$$\frac{\frac{\sqrt{cx^2} b^2}{c} - \frac{2 \left(ab \log \left(\left| -\sqrt{c} x + \sqrt{cx^2} \right| \right) - \frac{a^2 \sqrt{c}}{\sqrt{c} x - \sqrt{cx^2}} \right)}{\sqrt{c}}}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2/(c*x^2)^(3/2),x, algorithm="giac")

[Out] $(\sqrt{c*x^2}*b^2/c - 2*(a*b*\log(\text{abs}(-\sqrt{c}*x + \sqrt{c*x^2}))) - a^2*\sqrt{c})/(\sqrt{c}*x - \sqrt{c*x^2}))/\sqrt{c})/c$

maple [A] time = 0.00, size = 32, normalized size = 0.57

$$\frac{(2abx \ln(x) + b^2x^2 - a^2)x^2}{(cx^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(b*x+a)^2/(c*x^2)^(3/2),x)`

[Out] $x^2*(2*a*b*x*\ln(x)+b^2*x^2-a^2)/(c*x^2)^(3/2)$

maxima [A] time = 1.38, size = 42, normalized size = 0.75

$$\frac{b^2x^2}{\sqrt{cx^2}c} + \frac{2ab \log(x)}{c^{\frac{3}{2}}} - \frac{a^2}{\sqrt{cx^2}c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)^2/(c*x^2)^(3/2),x, algorithm="maxima")`

[Out] $b^2*x^2/(\sqrt{c*x^2}*c) + 2*a*b*\log(x)/c^(3/2) - a^2/(\sqrt{c*x^2}*c)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x(a+bx)^2}{(cx^2)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x*(a+b*x)^2)/(c*x^2)^(3/2),x)`

[Out] `int((x*(a+b*x)^2)/(c*x^2)^(3/2),x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x(a+bx)^2}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**2/(c*x**2)**(3/2),x)`

[Out] `Integral(x*(a+b*x)**2/(c*x**2)**(3/2),x)`

$$3.839 \quad \int \frac{(a+bx)^2}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=58

$$-\frac{a^2}{2cx\sqrt{cx^2}} - \frac{2ab}{c\sqrt{cx^2}} + \frac{b^2x \log(x)}{c\sqrt{cx^2}}$$

[Out] $-2*a*b/c/(c*x^2)^{(1/2)}-1/2*a^2/c/x/(c*x^2)^{(1/2)}+b^2*x*\ln(x)/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$-\frac{a^2}{2cx\sqrt{cx^2}} - \frac{2ab}{c\sqrt{cx^2}} + \frac{b^2x \log(x)}{c\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(c*x^2)^(3/2), x]

[Out] $(-2*a*b)/(c*\text{Sqrt}[c*x^2]) - a^2/(2*c*x*\text{Sqrt}[c*x^2]) + (b^2*x*\text{Log}[x])/(c*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_)^(m_.))*((c_.) + (d_.)*(x_)^(n_.)), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(cx^2)^{3/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^3} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^3} + \frac{2ab}{x^2} + \frac{b^2}{x} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{2ab}{c\sqrt{cx^2}} - \frac{a^2}{2cx\sqrt{cx^2}} + \frac{b^2x \log(x)}{c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 34, normalized size = 0.59

$$\frac{x(2b^2x^2 \log(x) - a(a + 4bx))}{2(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(c*x^2)^(3/2), x]

[Out] (x*(-(a*(a + 4*b*x)) + 2*b^2*x^2*Log[x]))/(2*(c*x^2)^(3/2))

fricas [A] time = 0.44, size = 36, normalized size = 0.62

$$\frac{(2b^2x^2 \log(x) - 4abx - a^2)\sqrt{cx^2}}{2c^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] 1/2*(2*b^2*x^2*log(x) - 4*a*b*x - a^2)*sqrt(c*x^2)/(c^2*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0*x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(c*x^2)^(3/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 32, normalized size = 0.55

$$\frac{(2b^2x^2 \ln(x) - 4abx - a^2)x}{2(cx^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/(c*x^2)^(3/2), x)`

[Out] `1/2*x*(2*b^2*x^2*ln(x)-4*a*b*x-a^2)/(c*x^2)^(3/2)`

maxima [A] time = 1.33, size = 35, normalized size = 0.60

$$\frac{b^2 \log(x)}{c^{\frac{3}{2}}} - \frac{2ab}{\sqrt{cx^2}c} - \frac{a^2}{2c^{\frac{3}{2}}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/(c*x^2)^(3/2), x, algorithm="maxima")`

[Out] `b^2*log(x)/c^(3/2) - 2*a*b/(sqrt(c*x^2)*c) - 1/2*a^2/(c^(3/2)*x^2)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^2}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(c*x^2)^(3/2), x)`

[Out] `int((a + b*x)^2/(c*x^2)^(3/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^2}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/(c*x**2)**(3/2), x)`

[Out] `Integral((a + b*x)**2/(c*x**2)**(3/2), x)`

$$3.840 \quad \int \frac{(a+bx)^2}{x(cx^2)^{3/2}} dx$$

Optimal. Leaf size=29

$$-\frac{(a+bx)^3}{3acx^2\sqrt{cx^2}}$$

[Out] $-1/3*(b*x+a)^3/a/c/x^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 37}

$$-\frac{(a+bx)^3}{3acx^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x*(c*x^2)^(3/2)), x]

[Out] $-(a + b*x)^3/(3*a*c*x^2*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x(cx^2)^{3/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^4} dx}{c\sqrt{cx^2}} \\ &= -\frac{(a+bx)^3}{3acx^2\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 36, normalized size = 1.24

$$\frac{cx^2(-a^2 - 3abx - 3b^2x^2)}{3(cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x*(c*x^2)^(3/2)), x]

[Out] (c*x^2*(-a^2 - 3*a*b*x - 3*b^2*x^2))/(3*(c*x^2)^(5/2))

fricas [A] time = 0.42, size = 32, normalized size = 1.10

$$\frac{(3b^2x^2 + 3abx + a^2)\sqrt{cx^2}}{3c^2x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] -1/3*(3*b^2*x^2 + 3*a*b*x + a^2)*sqrt(c*x^2)/(c^2*x^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^2}{(cx^2)^{\frac{3}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x/(c*x^2)^(3/2), x, algorithm="giac")

[Out] integrate((b*x + a)^2/((c*x^2)^(3/2)*x), x)

maple [A] time = 0.00, size = 27, normalized size = 0.93

$$\frac{3b^2x^2 + 3abx + a^2}{3(cx^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/x/(c*x^2)^(3/2), x)

[Out] -1/3*(3*b^2*x^2+3*a*b*x+a^2)/(c*x^2)^(3/2)

maxima [A] time = 1.36, size = 37, normalized size = 1.28

$$-\frac{b^2}{\sqrt{cx^2}c} - \frac{ab}{c^{\frac{3}{2}}x^2} - \frac{a^2}{3c^{\frac{3}{2}}x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x/(c*x^2)^(3/2),x, algorithm="maxima")

[Out] -b^2/(sqrt(c*x^2)*c) - a*b/(c^(3/2)*x^2) - 1/3*a^2/(c^(3/2)*x^3)

mupad [B] time = 0.19, size = 33, normalized size = 1.14

$$\frac{a^2 x^2 + 3 a b x^3 + 3 b^2 x^4}{3 c^{3/2} (x^2)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(x*(c*x^2)^(3/2)),x)

[Out] -(a^2*x^2 + 3*b^2*x^4 + 3*a*b*x^3)/(3*c^(3/2)*(x^2)^(5/2))

sympy [B] time = 0.67, size = 53, normalized size = 1.83

$$-\frac{a^2}{3c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} - \frac{abx}{c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} - \frac{b^2x^2}{c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/x/(c*x**2)**(3/2),x)

[Out] -a**2/(3*c**(3/2)*(x**2)**(3/2)) - a*b*x/(c**(3/2)*(x**2)**(3/2)) - b**2*x**2/(c**(3/2)*(x**2)**(3/2))

$$3.841 \quad \int \frac{(a+bx)^2}{x^2(cx^2)^{3/2}} dx$$

Optimal. Leaf size=66

$$-\frac{a^2}{4cx^3\sqrt{cx^2}} - \frac{2ab}{3cx^2\sqrt{cx^2}} - \frac{b^2}{2cx\sqrt{cx^2}}$$

[Out] $-1/4*a^2/c/x^3/(c*x^2)^{(1/2)}-2/3*a*b/c/x^2/(c*x^2)^{(1/2)}-1/2*b^2/c/x/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{4cx^3\sqrt{cx^2}} - \frac{2ab}{3cx^2\sqrt{cx^2}} - \frac{b^2}{2cx\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x^2*(c*x^2)^(3/2)), x]

[Out] $-a^2/(4*c*x^3*\text{Sqrt}[c*x^2]) - (2*a*b)/(3*c*x^2*\text{Sqrt}[c*x^2]) - b^2/(2*c*x*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^2 (cx^2)^{3/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^5} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^5} + \frac{2ab}{x^4} + \frac{b^2}{x^3} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{a^2}{4cx^3\sqrt{cx^2}} - \frac{2ab}{3cx^2\sqrt{cx^2}} - \frac{b^2}{2cx\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 38, normalized size = 0.58

$$-\frac{\sqrt{cx^2} (3a^2 + 8abx + 6b^2x^2)}{12c^2x^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x^2*(c*x^2)^(3/2)), x]

[Out] -1/12*(Sqrt[c*x^2]*(3*a^2 + 8*a*b*x + 6*b^2*x^2))/(c^2*x^5)

fricas [A] time = 0.42, size = 34, normalized size = 0.52

$$-\frac{(6b^2x^2 + 8abx + 3a^2)\sqrt{cx^2}}{12c^2x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^2/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] -1/12*(6*b^2*x^2 + 8*a*b*x + 3*a^2)*sqrt(c*x^2)/(c^2*x^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^2/(c*x^2)^(3/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.01, size = 32, normalized size = 0.48

$$-\frac{6b^2x^2 + 8abx + 3a^2}{12(c x^2)^{\frac{3}{2}} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^2/(c*x^2)^(3/2),x)`

[Out] $-1/12*(6*b^2*x^2+8*a*b*x+3*a^2)/x/(c*x^2)^(3/2)$

maxima [A] time = 1.31, size = 33, normalized size = 0.50

$$-\frac{b^2}{2c^{\frac{3}{2}}x^2} - \frac{2ab}{3c^{\frac{3}{2}}x^3} - \frac{a^2}{4c^{\frac{3}{2}}x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^2/(c*x^2)^(3/2),x, algorithm="maxima")`

[Out] $-1/2*b^2/(c^(3/2)*x^2) - 2/3*a*b/(c^(3/2)*x^3) - 1/4*a^2/(c^(3/2)*x^4)$

mupad [B] time = 0.19, size = 42, normalized size = 0.64

$$-\frac{3a^2\sqrt{x^2} + 6b^2x^2\sqrt{x^2} + 8abx\sqrt{x^2}}{12c^{3/2}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(x^2*(c*x^2)^(3/2)),x)`

[Out] $-(3*a^2*(x^2)^(1/2) + 6*b^2*x^2*(x^2)^(1/2) + 8*a*b*x*(x^2)^(1/2))/(12*c^(3/2)*x^5)$

sympy [A] time = 0.81, size = 56, normalized size = 0.85

$$-\frac{a^2}{4c^{\frac{3}{2}}x(x^2)^{\frac{3}{2}}} - \frac{2ab}{3c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} - \frac{b^2x}{2c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**2/(c*x**2)**(3/2),x)`

[Out] $-a**2/(4*c**(3/2)*x*(x**2)**(3/2)) - 2*a*b/(3*c**(3/2)*(x**2)**(3/2)) - b**2*x/(2*c**(3/2)*(x**2)**(3/2))$

$$3.842 \quad \int \frac{(a+bx)^2}{x^3(cx^2)^{3/2}} dx$$

Optimal. Leaf size=66

$$-\frac{a^2}{5cx^4\sqrt{cx^2}} - \frac{ab}{2cx^3\sqrt{cx^2}} - \frac{b^2}{3cx^2\sqrt{cx^2}}$$

[Out] $-1/5*a^2/c/x^4/(c*x^2)^{(1/2)}-1/2*a*b/c/x^3/(c*x^2)^{(1/2)}-1/3*b^2/c/x^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{5cx^4\sqrt{cx^2}} - \frac{ab}{2cx^3\sqrt{cx^2}} - \frac{b^2}{3cx^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x^3*(c*x^2)^(3/2)), x]

[Out] $-a^2/(5*c*x^4*\text{Sqrt}[c*x^2]) - (a*b)/(2*c*x^3*\text{Sqrt}[c*x^2]) - b^2/(3*c*x^2*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^3 (cx^2)^{3/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^6} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^6} + \frac{2ab}{x^5} + \frac{b^2}{x^4} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{a^2}{5cx^4\sqrt{cx^2}} - \frac{ab}{2cx^3\sqrt{cx^2}} - \frac{b^2}{3cx^2\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.50

$$\frac{c(-6a^2 - 15abx - 10b^2x^2)}{30(cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x^3*(c*x^2)^(3/2)),x]

[Out] (c*(-6*a^2 - 15*a*b*x - 10*b^2*x^2))/(30*(c*x^2)^(5/2))

fricas [A] time = 0.46, size = 34, normalized size = 0.52

$$-\frac{(10b^2x^2 + 15abx + 6a^2)\sqrt{cx^2}}{30c^2x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^3/(c*x^2)^(3/2),x, algorithm="fricas")

[Out] -1/30*(10*b^2*x^2 + 15*a*b*x + 6*a^2)*sqrt(c*x^2)/(c^2*x^6)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^2}{(cx^2)^{\frac{3}{2}} x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^3/(c*x^2)^(3/2),x, algorithm="giac")

[Out] integrate((b*x + a)^2/((c*x^2)^(3/2)*x^3), x)

maple [A] time = 0.00, size = 32, normalized size = 0.48

$$-\frac{10b^2x^2 + 15abx + 6a^2}{30(c^2x^2)^{\frac{3}{2}}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^3/(c*x^2)^(3/2), x)`

[Out] `-1/30*(10*b^2*x^2+15*a*b*x+6*a^2)/x^2/(c*x^2)^(3/2)`

maxima [A] time = 1.36, size = 33, normalized size = 0.50

$$-\frac{b^2}{3c^{\frac{3}{2}}x^3} - \frac{ab}{2c^{\frac{3}{2}}x^4} - \frac{a^2}{5c^{\frac{3}{2}}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^3/(c*x^2)^(3/2), x, algorithm="maxima")`

[Out] `-1/3*b^2/(c^(3/2)*x^3) - 1/2*a*b/(c^(3/2)*x^4) - 1/5*a^2/(c^(3/2)*x^5)`

mupad [B] time = 0.20, size = 42, normalized size = 0.64

$$-\frac{6a^2\sqrt{x^2} + 10b^2x^2\sqrt{x^2} + 15abx\sqrt{x^2}}{30c^{3/2}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(x^3*(c*x^2)^(3/2)), x)`

[Out] `-(6*a^2*(x^2)^(1/2) + 10*b^2*x^2*(x^2)^(1/2) + 15*a*b*x*(x^2)^(1/2))/(30*c^(3/2)*x^6)`

sympy [A] time = 0.98, size = 56, normalized size = 0.85

$$-\frac{a^2}{5c^{\frac{3}{2}}x^2(x^2)^{\frac{3}{2}}} - \frac{ab}{2c^{\frac{3}{2}}x(x^2)^{\frac{3}{2}}} - \frac{b^2}{3c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**3/(c*x**2)**(3/2), x)`

[Out] `-a**2/(5*c**(3/2)*x**2*(x**2)**(3/2)) - a*b/(2*c**(3/2)*x*(x**2)**(3/2)) - b**2/(3*c**(3/2)*(x**2)**(3/2))`

$$3.843 \quad \int \frac{(a+bx)^2}{x^4(cx^2)^{3/2}} dx$$

Optimal. Leaf size=66

$$-\frac{a^2}{6cx^5\sqrt{cx^2}} - \frac{2ab}{5cx^4\sqrt{cx^2}} - \frac{b^2}{4cx^3\sqrt{cx^2}}$$

[Out] $-1/6*a^2/c/x^5/(c*x^2)^{(1/2)}-2/5*a*b/c/x^4/(c*x^2)^{(1/2)}-1/4*b^2/c/x^3/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{6cx^5\sqrt{cx^2}} - \frac{2ab}{5cx^4\sqrt{cx^2}} - \frac{b^2}{4cx^3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x^4*(c*x^2)^(3/2)), x]

[Out] $-a^2/(6*c*x^5*\text{Sqrt}[c*x^2]) - (2*a*b)/(5*c*x^4*\text{Sqrt}[c*x^2]) - b^2/(4*c*x^3*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^4 (cx^2)^{3/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^7} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^7} + \frac{2ab}{x^6} + \frac{b^2}{x^5} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{a^2}{6cx^5\sqrt{cx^2}} - \frac{2ab}{5cx^4\sqrt{cx^2}} - \frac{b^2}{4cx^3\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.53

$$\frac{-10a^2 - 24abx - 15b^2x^2}{60x^3 (cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x^4*(c*x^2)^(3/2)), x]

[Out] (-10*a^2 - 24*a*b*x - 15*b^2*x^2)/(60*x^3*(c*x^2)^(3/2))

fricas [A] time = 0.43, size = 34, normalized size = 0.52

$$-\frac{(15b^2x^2 + 24abx + 10a^2)\sqrt{cx^2}}{60c^2x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^4/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] -1/60*(15*b^2*x^2 + 24*a*b*x + 10*a^2)*sqrt(c*x^2)/(c^2*x^7)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^4/(c*x^2)^(3/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 32, normalized size = 0.48

$$\frac{15b^2x^2 + 24abx + 10a^2}{60(c^2x^2)^{\frac{3}{2}}x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^4/(c*x^2)^(3/2),x)`

[Out] `-1/60*(15*b^2*x^2+24*a*b*x+10*a^2)/x^3/(c*x^2)^(3/2)`

maxima [A] time = 1.29, size = 33, normalized size = 0.50

$$-\frac{b^2}{4c^{\frac{3}{2}}x^4} - \frac{2ab}{5c^{\frac{3}{2}}x^5} - \frac{a^2}{6c^{\frac{3}{2}}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^4/(c*x^2)^(3/2),x, algorithm="maxima")`

[Out] `-1/4*b^2/(c^(3/2)*x^4) - 2/5*a*b/(c^(3/2)*x^5) - 1/6*a^2/(c^(3/2)*x^6)`

mupad [B] time = 0.18, size = 42, normalized size = 0.64

$$\frac{10a^2\sqrt{x^2} + 15b^2x^2\sqrt{x^2} + 24abx\sqrt{x^2}}{60c^{3/2}x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(x^4*(c*x^2)^(3/2)),x)`

[Out] `-(10*a^2*(x^2)^(1/2) + 15*b^2*x^2*(x^2)^(1/2) + 24*a*b*x*(x^2)^(1/2))/(60*c^(3/2)*x^7)`

sympy [A] time = 1.18, size = 61, normalized size = 0.92

$$-\frac{a^2}{6c^{\frac{3}{2}}x^3(x^2)^{\frac{3}{2}}} - \frac{2ab}{5c^{\frac{3}{2}}x^2(x^2)^{\frac{3}{2}}} - \frac{b^2}{4c^{\frac{3}{2}}x(x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**4/(c*x**2)**(3/2),x)`

[Out] `-a**2/(6*c**(3/2)*x**3*(x**2)**(3/2)) - 2*a*b/(5*c**(3/2)*x**2*(x**2)**(3/2)) - b**2/(4*c**(3/2)*x*(x**2)**(3/2))`

$$3.844 \quad \int \frac{x^3(a+bx)^2}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=56

$$-\frac{a^2}{c^2\sqrt{cx^2}} + \frac{2abx \log(x)}{c^2\sqrt{cx^2}} + \frac{b^2x^2}{c^2\sqrt{cx^2}}$$

[Out] $-a^2/c^2/(c*x^2)^{(1/2)}+b^2*x^2/c^2/(c*x^2)^{(1/2)}+2*a*b*x*\ln(x)/c^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{c^2\sqrt{cx^2}} + \frac{2abx \log(x)}{c^2\sqrt{cx^2}} + \frac{b^2x^2}{c^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^3*(a + b*x)^2)/(c*x^2)^(5/2), x]

[Out] $-(a^2/(c^2*\text{Sqrt}[c*x^2])) + (b^2*x^2)/(c^2*\text{Sqrt}[c*x^2]) + (2*a*b*x*\text{Log}[x])/(c^2*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3(a+bx)^2}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^2} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(b^2 + \frac{a^2}{x^2} + \frac{2ab}{x} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a^2}{c^2 \sqrt{cx^2}} + \frac{b^2 x^2}{c^2 \sqrt{cx^2}} + \frac{2abx \log(x)}{c^2 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.59

$$\frac{-a^2 + 2abx \log(x) + b^2 x^2}{c^2 \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*(a + b*x)^2)/(c*x^2)^(5/2), x]

[Out] (-a^2 + b^2*x^2 + 2*a*b*x*Log[x])/(c^2*sqrt[c*x^2])

fricas [A] time = 0.52, size = 34, normalized size = 0.61

$$\frac{(b^2 x^2 + 2 abx \log(x) - a^2) \sqrt{cx^2}}{c^3 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] (b^2*x^2 + 2*a*b*x*log(x) - a^2)*sqrt(c*x^2)/(c^3*x^2)

giac [A] time = 1.07, size = 65, normalized size = 1.16

$$\frac{\sqrt{cx^2} b^2}{c^3} - \frac{2 \left(ab \log \left(\left| -\sqrt{c} x + \sqrt{cx^2} \right| \right) - \frac{a^2 \sqrt{c}}{\sqrt{c} x - \sqrt{cx^2}} \right)}{c^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2/(c*x^2)^(5/2), x, algorithm="giac")

[Out] sqrt(c*x^2)*b^2/c^3 - 2*(a*b*log(abs(-sqrt(c)*x + sqrt(c*x^2))) - a^2*sqrt(c)/(sqrt(c)*x - sqrt(c*x^2)))/c^(5/2)

maple [A] time = 0.00, size = 32, normalized size = 0.57

$$\frac{(2abx \ln(x) + b^2x^2 - a^2)x^4}{(cx^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^2/(c*x^2)^(5/2), x)

[Out] x^4*(2*a*b*x*ln(x)+b^2*x^2-a^2)/(c*x^2)^(5/2)

maxima [A] time = 1.45, size = 45, normalized size = 0.80

$$\frac{b^2x^4}{(cx^2)^{\frac{3}{2}}c} - \frac{a^2x^2}{(cx^2)^{\frac{3}{2}}c} + \frac{2ab \log(x)}{c^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^2/(c*x^2)^(5/2), x, algorithm="maxima")

[Out] b^2*x^4/((c*x^2)^(3/2)*c) - a^2*x^2/((c*x^2)^(3/2)*c) + 2*a*b*log(x)/c^(5/2)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^3 (a + bx)^2}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^3*(a + b*x)^2)/(c*x^2)^(5/2), x)

[Out] int((x^3*(a + b*x)^2)/(c*x^2)^(5/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^3 (a + bx)^2}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**2/(c*x**2)**(5/2), x)

[Out] Integral(x**3*(a + b*x)**2/(c*x**2)**(5/2), x)

$$3.845 \quad \int \frac{x^2(a+bx)^2}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=58

$$-\frac{a^2}{2c^2x\sqrt{cx^2}} - \frac{2ab}{c^2\sqrt{cx^2}} + \frac{b^2x \log(x)}{c^2\sqrt{cx^2}}$$

[Out] $-2*a*b/c^2/(c*x^2)^{(1/2)} - 1/2*a^2/c^2/x/(c*x^2)^{(1/2)} + b^2*x*\ln(x)/c^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{2c^2x\sqrt{cx^2}} - \frac{2ab}{c^2\sqrt{cx^2}} + \frac{b^2x \log(x)}{c^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^2*(a + b*x)^2)/(c*x^2)^(5/2), x]

[Out] $(-2*a*b)/(c^2*\text{Sqrt}[c*x^2]) - a^2/(2*c^2*x*\text{Sqrt}[c*x^2]) + (b^2*x*\text{Log}[x])/(c^2*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2(a+bx)^2}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^3} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^3} + \frac{2ab}{x^2} + \frac{b^2}{x} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{2ab}{c^2 \sqrt{cx^2}} - \frac{a^2}{2c^2 x \sqrt{cx^2}} + \frac{b^2 x \log(x)}{c^2 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 36, normalized size = 0.62

$$\frac{x^3 (2b^2 x^2 \log(x) - a(a + 4bx))}{2 (cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*(a + b*x)^2)/(c*x^2)^(5/2), x]

[Out] (x^3*(-(a*(a + 4*b*x)) + 2*b^2*x^2*Log[x]))/(2*(c*x^2)^(5/2))

fricas [A] time = 0.48, size = 36, normalized size = 0.62

$$\frac{(2b^2x^2 \log(x) - 4abx - a^2)\sqrt{cx^2}}{2c^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] 1/2*(2*b^2*x^2*log(x) - 4*a*b*x - a^2)*sqrt(c*x^2)/(c^3*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^2/(c*x^2)^(5/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.01, size = 34, normalized size = 0.59

$$\frac{(2b^2x^2 \ln(x) - 4abx - a^2)x^3}{2(cx^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(b*x+a)^2/(c*x^2)^(5/2),x)`

[Out] `1/2*x^3*(2*b^2*x^2*ln(x)-4*a*b*x-a^2)/(c*x^2)^(5/2)`

maxima [A] time = 1.40, size = 38, normalized size = 0.66

$$-\frac{2abx^2}{(cx^2)^{\frac{3}{2}}c} + \frac{b^2 \log(x)}{c^{\frac{5}{2}}} - \frac{a^2}{2c^{\frac{5}{2}}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(b*x+a)^2/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] `-2*a*b*x^2/((c*x^2)^(3/2)*c) + b^2*log(x)/c^(5/2) - 1/2*a^2/(c^(5/2)*x^2)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^2 (a + bx)^2}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x^2*(a + b*x)^2)/(c*x^2)^(5/2),x)`

[Out] `int((x^2*(a + b*x)^2)/(c*x^2)^(5/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2 (a + bx)^2}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(b*x+a)**2/(c*x**2)**(5/2),x)`

[Out] `Integral(x**2*(a + b*x)**2/(c*x**2)**(5/2), x)`

$$3.846 \quad \int \frac{x(a+bx)^2}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=29

$$-\frac{(a+bx)^3}{3ac^2x^2\sqrt{cx^2}}$$

[Out] $-1/3*(b*x+a)^3/a/c^2/x^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 37}

$$-\frac{(a+bx)^3}{3ac^2x^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x*(a + b*x)^2)/(c*x^2)^{(5/2)}, x]$

[Out] $-(a + b*x)^3/(3*a*c^2*x^2*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 37

$\text{Int}[((a_.) + (b_.)*(x_))^{(m_.)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Simp} [((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{x(a+bx)^2}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^4} dx}{c^2\sqrt{cx^2}} \\ &= -\frac{(a+bx)^3}{3ac^2x^2\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 1.21

$$\frac{x^2(-a^2 - 3abx - 3b^2x^2)}{3(cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x*(a + b*x)^2)/(c*x^2)^(5/2), x]

[Out] (x^2*(-a^2 - 3*a*b*x - 3*b^2*x^2))/(3*(c*x^2)^(5/2))

fricas [A] time = 0.42, size = 32, normalized size = 1.10

$$\frac{(3b^2x^2 + 3abx + a^2)\sqrt{cx^2}}{3c^3x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/3*(3*b^2*x^2 + 3*a*b*x + a^2)*sqrt(c*x^2)/(c^3*x^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^2 x}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2/(c*x^2)^(5/2), x, algorithm="giac")

[Out] integrate((b*x + a)^2*x/(c*x^2)^(5/2), x)

maple [A] time = 0.00, size = 30, normalized size = 1.03

$$\frac{(3b^2x^2 + 3abx + a^2)x^2}{3(c x^2)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^2/(c*x^2)^(5/2), x)

[Out] -1/3*x^2*(3*b^2*x^2+3*a*b*x+a^2)/(c*x^2)^(5/2)

maxima [A] time = 1.38, size = 44, normalized size = 1.52

$$-\frac{b^2 x^2}{(cx^2)^{\frac{3}{2}} c} - \frac{a^2}{3 (cx^2)^{\frac{3}{2}} c} - \frac{ab}{c^{\frac{5}{2}} x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^2/(c*x^2)^(5/2),x, algorithm="maxima")

[Out] -b^2*x^2/((c*x^2)^(3/2)*c) - 1/3*a^2/((c*x^2)^(3/2)*c) - a*b/(c^(5/2)*x^2)

mupad [B] time = 0.18, size = 33, normalized size = 1.14

$$-\frac{a^2 x^2 + 3 a b x^3 + 3 b^2 x^4}{3 c^{5/2} (x^2)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x*(a + b*x)^2)/(c*x^2)^(5/2),x)

[Out] -(a^2*x^2 + 3*b^2*x^4 + 3*a*b*x^3)/(3*c^(5/2)*(x^2)^(5/2))

sympy [B] time = 0.96, size = 58, normalized size = 2.00

$$-\frac{a^2 x^2}{3 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}} - \frac{a b x^3}{c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}} - \frac{b^2 x^4}{c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)**2/(c*x**2)**(5/2),x)

[Out] -a**2*x**2/(3*c**(5/2)*(x**2)**(5/2)) - a*b*x**3/(c**(5/2)*(x**2)**(5/2)) - b**2*x**4/(c**(5/2)*(x**2)**(5/2))

$$3.847 \quad \int \frac{(a+bx)^2}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=66

$$-\frac{a^2}{4c^2x^3\sqrt{cx^2}} - \frac{2ab}{3c^2x^2\sqrt{cx^2}} - \frac{b^2}{2c^2x\sqrt{cx^2}}$$

[Out] $-1/4*a^2/c^2/x^3/(c*x^2)^{(1/2)}-2/3*a*b/c^2/x^2/(c*x^2)^{(1/2)}-1/2*b^2/c^2/x/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$-\frac{a^2}{4c^2x^3\sqrt{cx^2}} - \frac{2ab}{3c^2x^2\sqrt{cx^2}} - \frac{b^2}{2c^2x\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(c*x^2)^(5/2), x]

[Out] $-a^2/(4*c^2*x^3*\text{Sqrt}[c*x^2]) - (2*a*b)/(3*c^2*x^2*\text{Sqrt}[c*x^2]) - b^2/(2*c^2*x*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^5} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^5} + \frac{2ab}{x^4} + \frac{b^2}{x^3} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a^2}{4c^2 x^3 \sqrt{cx^2}} - \frac{2ab}{3c^2 x^2 \sqrt{cx^2}} - \frac{b^2}{2c^2 x \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 38, normalized size = 0.58

$$-\frac{\sqrt{cx^2} (3a^2 + 8abx + 6b^2x^2)}{12c^3x^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(c*x^2)^(5/2), x]

[Out] -1/12*(Sqrt[c*x^2]*(3*a^2 + 8*a*b*x + 6*b^2*x^2))/(c^3*x^5)

fricas [A] time = 0.41, size = 34, normalized size = 0.52

$$-\frac{(6b^2x^2 + 8abx + 3a^2)\sqrt{cx^2}}{12c^3x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/12*(6*b^2*x^2 + 8*a*b*x + 3*a^2)*sqrt(c*x^2)/(c^3*x^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(c*x^2)^(5/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 30, normalized size = 0.45

$$-\frac{(6b^2x^2 + 8abx + 3a^2)x}{12(c x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/(c*x^2)^(5/2),x)`

[Out] $-1/12*x*(6*b^2*x^2+8*a*b*x+3*a^2)/(c*x^2)^(5/2)$

maxima [A] time = 1.36, size = 37, normalized size = 0.56

$$-\frac{2ab}{3(c^2x^2)^{\frac{3}{2}}c} - \frac{b^2}{2c^{\frac{5}{2}}x^2} - \frac{a^2}{4c^{\frac{5}{2}}x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] $-2/3*a*b/((c*x^2)^(3/2)*c) - 1/2*b^2/(c^(5/2)*x^2) - 1/4*a^2/(c^(5/2)*x^4)$

mupad [B] time = 0.17, size = 42, normalized size = 0.64

$$-\frac{3a^2\sqrt{x^2} + 6b^2x^2\sqrt{x^2} + 8abx\sqrt{x^2}}{12c^{5/2}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(c*x^2)^(5/2),x)`

[Out] $-(3*a^2*(x^2)^(1/2) + 6*b^2*x^2*(x^2)^(1/2) + 8*a*b*x*(x^2)^(1/2))/(12*c^(5/2)*x^5)$

sympy [A] time = 0.96, size = 61, normalized size = 0.92

$$-\frac{a^2x}{4c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} - \frac{2abx^2}{3c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} - \frac{b^2x^3}{2c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/(c*x**2)**(5/2),x)`

[Out] $-a**2*x/(4*c**(5/2)*(x**2)**(5/2)) - 2*a*b*x**2/(3*c**(5/2)*(x**2)**(5/2)) - b**2*x**3/(2*c**(5/2)*(x**2)**(5/2))$

$$3.848 \quad \int \frac{(a+bx)^2}{x(cx^2)^{5/2}} dx$$

Optimal. Leaf size=66

$$-\frac{a^2}{5c^2x^4\sqrt{cx^2}} - \frac{ab}{2c^2x^3\sqrt{cx^2}} - \frac{b^2}{3c^2x^2\sqrt{cx^2}}$$

[Out] $-1/5*a^2/c^2/x^4/(c*x^2)^{(1/2)} - 1/2*a*b/c^2/x^3/(c*x^2)^{(1/2)} - 1/3*b^2/c^2/x^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{5c^2x^4\sqrt{cx^2}} - \frac{ab}{2c^2x^3\sqrt{cx^2}} - \frac{b^2}{3c^2x^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x*(c*x^2)^(5/2)), x]

[Out] $-a^2/(5*c^2*x^4*\text{Sqrt}[c*x^2]) - (a*b)/(2*c^2*x^3*\text{Sqrt}[c*x^2]) - b^2/(3*c^2*x^2*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x(cx^2)^{5/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^6} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^6} + \frac{2ab}{x^5} + \frac{b^2}{x^4} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a^2}{5c^2 x^4 \sqrt{cx^2}} - \frac{ab}{2c^2 x^3 \sqrt{cx^2}} - \frac{b^2}{3c^2 x^2 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 38, normalized size = 0.58

$$-\frac{\sqrt{cx^2} (6a^2 + 15abx + 10b^2x^2)}{30c^3x^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x*(c*x^2)^(5/2)),x]

[Out] -1/30*(Sqrt[c*x^2]*(6*a^2 + 15*a*b*x + 10*b^2*x^2))/(c^3*x^6)

fricas [A] time = 0.44, size = 34, normalized size = 0.52

$$-\frac{(10b^2x^2 + 15abx + 6a^2)\sqrt{cx^2}}{30c^3x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x/(c*x^2)^(5/2),x, algorithm="fricas")

[Out] -1/30*(10*b^2*x^2 + 15*a*b*x + 6*a^2)*sqrt(c*x^2)/(c^3*x^6)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^2}{(cx^2)^{\frac{5}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x/(c*x^2)^(5/2),x, algorithm="giac")

[Out] integrate((b*x + a)^2/((c*x^2)^(5/2)*x), x)

maple [A] time = 0.01, size = 29, normalized size = 0.44

$$\frac{10b^2x^2 + 15abx + 6a^2}{30(c x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/x/(c*x^2)^(5/2), x)

[Out] -1/30*(10*b^2*x^2+15*a*b*x+6*a^2)/(c*x^2)^(5/2)

maxima [A] time = 1.31, size = 37, normalized size = 0.56

$$-\frac{b^2}{3(c x^2)^{\frac{3}{2}}c} - \frac{ab}{2c^{\frac{5}{2}}x^4} - \frac{a^2}{5c^{\frac{5}{2}}x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x/(c*x^2)^(5/2), x, algorithm="maxima")

[Out] -1/3*b^2/((c*x^2)^(3/2)*c) - 1/2*a*b/(c^(5/2)*x^4) - 1/5*a^2/(c^(5/2)*x^5)

mupad [B] time = 0.18, size = 42, normalized size = 0.64

$$\frac{6a^2\sqrt{x^2} + 10b^2x^2\sqrt{x^2} + 15abx\sqrt{x^2}}{30c^{5/2}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(x*(c*x^2)^(5/2)), x)

[Out] -(6*a^2*(x^2)^(1/2) + 10*b^2*x^2*(x^2)^(1/2) + 15*a*b*x*(x^2)^(1/2))/(30*c^(5/2)*x^6)

sympy [A] time = 1.15, size = 56, normalized size = 0.85

$$-\frac{a^2}{5c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} - \frac{abx}{2c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} - \frac{b^2x^2}{3c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/x/(c*x**2)**(5/2), x)

[Out] -a**2/(5*c**(5/2)*(x**2)**(5/2)) - a*b*x/(2*c**(5/2)*(x**2)**(5/2)) - b**2*x**2/(3*c**(5/2)*(x**2)**(5/2))

$$3.849 \quad \int \frac{(a+bx)^2}{x^2(cx^2)^{5/2}} dx$$

Optimal. Leaf size=66

$$-\frac{a^2}{6c^2x^5\sqrt{cx^2}} - \frac{2ab}{5c^2x^4\sqrt{cx^2}} - \frac{b^2}{4c^2x^3\sqrt{cx^2}}$$

[Out] $-1/6*a^2/c^2/x^5/(c*x^2)^{(1/2)}-2/5*a*b/c^2/x^4/(c*x^2)^{(1/2)}-1/4*b^2/c^2/x^3/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{6c^2x^5\sqrt{cx^2}} - \frac{2ab}{5c^2x^4\sqrt{cx^2}} - \frac{b^2}{4c^2x^3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x^2*(c*x^2)^(5/2)), x]

[Out] $-a^2/(6*c^2*x^5*\text{Sqrt}[c*x^2]) - (2*a*b)/(5*c^2*x^4*\text{Sqrt}[c*x^2]) - b^2/(4*c^2*x^3*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^2 (cx^2)^{5/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^7} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^7} + \frac{2ab}{x^6} + \frac{b^2}{x^5} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a^2}{6c^2 x^5 \sqrt{cx^2}} - \frac{2ab}{5c^2 x^4 \sqrt{cx^2}} - \frac{b^2}{4c^2 x^3 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 38, normalized size = 0.58

$$-\frac{\sqrt{cx^2} (10a^2 + 24abx + 15b^2x^2)}{60c^3x^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x^2*(c*x^2)^(5/2)), x]

[Out] -1/60*(Sqrt[c*x^2]*(10*a^2 + 24*a*b*x + 15*b^2*x^2))/(c^3*x^7)

fricas [A] time = 0.43, size = 34, normalized size = 0.52

$$-\frac{(15b^2x^2 + 24abx + 10a^2)\sqrt{cx^2}}{60c^3x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^2/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/60*(15*b^2*x^2 + 24*a*b*x + 10*a^2)*sqrt(c*x^2)/(c^3*x^7)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^2/(c*x^2)^(5/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 32, normalized size = 0.48

$$-\frac{15b^2x^2 + 24abx + 10a^2}{60(c x^2)^{\frac{5}{2}} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^2/(c*x^2)^(5/2),x)`

[Out] $-1/60*(15*b^2*x^2+24*a*b*x+10*a^2)/x/(c*x^2)^(5/2)$

maxima [A] time = 1.34, size = 33, normalized size = 0.50

$$-\frac{b^2}{4c^{\frac{5}{2}}x^4} - \frac{2ab}{5c^{\frac{5}{2}}x^5} - \frac{a^2}{6c^{\frac{5}{2}}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^2/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] $-1/4*b^2/(c^(5/2)*x^4) - 2/5*a*b/(c^(5/2)*x^5) - 1/6*a^2/(c^(5/2)*x^6)$

mupad [B] time = 0.18, size = 42, normalized size = 0.64

$$\frac{10a^2\sqrt{x^2} + 15b^2x^2\sqrt{x^2} + 24abx\sqrt{x^2}}{60c^{5/2}x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(x^2*(c*x^2)^(5/2)),x)`

[Out] $-(10*a^2*(x^2)^(1/2) + 15*b^2*x^2*(x^2)^(1/2) + 24*a*b*x*(x^2)^(1/2))/(60*c^(5/2)*x^7)$

sympy [A] time = 1.40, size = 56, normalized size = 0.85

$$-\frac{a^2}{6c^{\frac{5}{2}}x(x^2)^{\frac{5}{2}}} - \frac{2ab}{5c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} - \frac{b^2x}{4c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**2/(c*x**2)**(5/2),x)`

[Out] $-a**2/(6*c**(5/2)*x*(x**2)**(5/2)) - 2*a*b/(5*c**(5/2)*(x**2)**(5/2)) - b**2*x/(4*c**(5/2)*(x**2)**(5/2))$

$$3.850 \quad \int \frac{(a+bx)^2}{x^3(cx^2)^{5/2}} dx$$

Optimal. Leaf size=66

$$-\frac{a^2}{7c^2x^6\sqrt{cx^2}} - \frac{ab}{3c^2x^5\sqrt{cx^2}} - \frac{b^2}{5c^2x^4\sqrt{cx^2}}$$

[Out] $-1/7*a^2/c^2/x^6/(c*x^2)^{(1/2)}-1/3*a*b/c^2/x^5/(c*x^2)^{(1/2)}-1/5*b^2/c^2/x^4/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{7c^2x^6\sqrt{cx^2}} - \frac{ab}{3c^2x^5\sqrt{cx^2}} - \frac{b^2}{5c^2x^4\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x^3*(c*x^2)^(5/2)), x]

[Out] $-a^2/(7*c^2*x^6*\text{Sqrt}[c*x^2]) - (a*b)/(3*c^2*x^5*\text{Sqrt}[c*x^2]) - b^2/(5*c^2*x^4*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^3 (cx^2)^{5/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^8} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^8} + \frac{2ab}{x^7} + \frac{b^2}{x^6} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a^2}{7c^2 x^6 \sqrt{cx^2}} - \frac{ab}{3c^2 x^5 \sqrt{cx^2}} - \frac{b^2}{5c^2 x^4 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.50

$$\frac{c(-15a^2 - 35abx - 21b^2x^2)}{105(cx^2)^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x^3*(c*x^2)^(5/2)),x]

[Out] (c*(-15*a^2 - 35*a*b*x - 21*b^2*x^2))/(105*(c*x^2)^(7/2))

fricas [A] time = 0.43, size = 34, normalized size = 0.52

$$-\frac{(21b^2x^2 + 35abx + 15a^2)\sqrt{cx^2}}{105c^3x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^3/(c*x^2)^(5/2),x, algorithm="fricas")

[Out] -1/105*(21*b^2*x^2 + 35*a*b*x + 15*a^2)*sqrt(c*x^2)/(c^3*x^8)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^2}{(cx^2)^{5/2} x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^3/(c*x^2)^(5/2),x, algorithm="giac")

[Out] integrate((b*x + a)^2/((c*x^2)^(5/2)*x^3), x)

maple [A] time = 0.00, size = 32, normalized size = 0.48

$$-\frac{21b^2x^2 + 35abx + 15a^2}{105(c^2x^2)^{\frac{5}{2}}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^3/(c*x^2)^(5/2),x)`

[Out] `-1/105*(21*b^2*x^2+35*a*b*x+15*a^2)/x^2/(c*x^2)^(5/2)`

maxima [A] time = 1.37, size = 33, normalized size = 0.50

$$-\frac{b^2}{5c^{\frac{5}{2}}x^5} - \frac{ab}{3c^{\frac{5}{2}}x^6} - \frac{a^2}{7c^{\frac{5}{2}}x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^3/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] `-1/5*b^2/(c^(5/2)*x^5) - 1/3*a*b/(c^(5/2)*x^6) - 1/7*a^2/(c^(5/2)*x^7)`

mupad [B] time = 0.18, size = 42, normalized size = 0.64

$$-\frac{15a^2\sqrt{x^2} + 21b^2x^2\sqrt{x^2} + 35abx\sqrt{x^2}}{105c^{5/2}x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(x^3*(c*x^2)^(5/2)),x)`

[Out] `-(15*a^2*(x^2)^(1/2) + 21*b^2*x^2*(x^2)^(1/2) + 35*a*b*x*(x^2)^(1/2))/(105*c^(5/2)*x^8)`

sympy [A] time = 1.70, size = 56, normalized size = 0.85

$$-\frac{a^2}{7c^{\frac{5}{2}}x^2(x^2)^{\frac{5}{2}}} - \frac{ab}{3c^{\frac{5}{2}}x(x^2)^{\frac{5}{2}}} - \frac{b^2}{5c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**3/(c*x**2)**(5/2),x)`

[Out] `-a**2/(7*c**(5/2)*x**2*(x**2)**(5/2)) - a*b/(3*c**(5/2)*x*(x**2)**(5/2)) - b**2/(5*c**(5/2)*(x**2)**(5/2))`

$$3.851 \quad \int \frac{(a+bx)^2}{x^4(cx^2)^{5/2}} dx$$

Optimal. Leaf size=66

$$-\frac{a^2}{8c^2x^7\sqrt{cx^2}} - \frac{2ab}{7c^2x^6\sqrt{cx^2}} - \frac{b^2}{6c^2x^5\sqrt{cx^2}}$$

[Out] $-1/8*a^2/c^2/x^7/(c*x^2)^{(1/2)} - 2/7*a*b/c^2/x^6/(c*x^2)^{(1/2)} - 1/6*b^2/c^2/x^5/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2}{8c^2x^7\sqrt{cx^2}} - \frac{2ab}{7c^2x^6\sqrt{cx^2}} - \frac{b^2}{6c^2x^5\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(x^4*(c*x^2)^(5/2)), x]

[Out] $-a^2/(8*c^2*x^7*\text{Sqrt}[c*x^2]) - (2*a*b)/(7*c^2*x^6*\text{Sqrt}[c*x^2]) - b^2/(6*c^2*x^5*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{x^4 (cx^2)^{5/2}} dx &= \frac{x \int \frac{(a+bx)^2}{x^9} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{x^9} + \frac{2ab}{x^8} + \frac{b^2}{x^7} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{a^2}{8c^2 x^7 \sqrt{cx^2}} - \frac{2ab}{7c^2 x^6 \sqrt{cx^2}} - \frac{b^2}{6c^2 x^5 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.53

$$\frac{-21a^2 - 48abx - 28b^2x^2}{168x^3 (cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(x^4*(c*x^2)^(5/2)), x]

[Out] (-21*a^2 - 48*a*b*x - 28*b^2*x^2)/(168*x^3*(c*x^2)^(5/2))

fricas [A] time = 0.43, size = 34, normalized size = 0.52

$$-\frac{(28b^2x^2 + 48abx + 21a^2)\sqrt{cx^2}}{168c^3x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^4/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] -1/168*(28*b^2*x^2 + 48*a*b*x + 21*a^2)*sqrt(c*x^2)/(c^3*x^9)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/x^4/(c*x^2)^(5/2), x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.01, size = 32, normalized size = 0.48

$$\frac{28b^2x^2 + 48abx + 21a^2}{168(c^2x^2)^{\frac{5}{2}}x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/x^4/(c*x^2)^(5/2),x)`

[Out] `-1/168*(28*b^2*x^2+48*a*b*x+21*a^2)/x^3/(c*x^2)^(5/2)`

maxima [A] time = 1.35, size = 33, normalized size = 0.50

$$-\frac{b^2}{6c^{\frac{5}{2}}x^6} - \frac{2ab}{7c^{\frac{5}{2}}x^7} - \frac{a^2}{8c^{\frac{5}{2}}x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/x^4/(c*x^2)^(5/2),x, algorithm="maxima")`

[Out] `-1/6*b^2/(c^(5/2)*x^6) - 2/7*a*b/(c^(5/2)*x^7) - 1/8*a^2/(c^(5/2)*x^8)`

mupad [B] time = 0.18, size = 42, normalized size = 0.64

$$\frac{21a^2\sqrt{x^2} + 28b^2x^2\sqrt{x^2} + 48abx\sqrt{x^2}}{168c^{5/2}x^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(x^4*(c*x^2)^(5/2)),x)`

[Out] `-(21*a^2*(x^2)^(1/2) + 28*b^2*x^2*(x^2)^(1/2) + 48*a*b*x*(x^2)^(1/2))/(168*c^(5/2)*x^9)`

sympy [A] time = 2.03, size = 61, normalized size = 0.92

$$-\frac{a^2}{8c^{\frac{5}{2}}x^3(x^2)^{\frac{5}{2}}} - \frac{2ab}{7c^{\frac{5}{2}}x^2(x^2)^{\frac{5}{2}}} - \frac{b^2}{6c^{\frac{5}{2}}x(x^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/x**4/(c*x**2)**(5/2),x)`

[Out] `-a**2/(8*c**(5/2)*x**3*(x**2)**(5/2)) - 2*a*b/(7*c**(5/2)*x**2*(x**2)**(5/2)) - b**2/(6*c**(5/2)*x*(x**2)**(5/2))`

$$3.852 \quad \int \frac{x^3 \sqrt{cx^2}}{a+bx} dx$$

Optimal. Leaf size=102

$$\frac{a^4 \sqrt{cx^2} \log(a+bx)}{b^5 x} - \frac{a^3 \sqrt{cx^2}}{b^4} + \frac{a^2 x \sqrt{cx^2}}{2b^3} - \frac{ax^2 \sqrt{cx^2}}{3b^2} + \frac{x^3 \sqrt{cx^2}}{4b}$$

[Out] $-a^3*(c*x^2)^{(1/2)}/b^4+1/2*a^2*x*(c*x^2)^{(1/2)}/b^3-1/3*a*x^2*(c*x^2)^{(1/2)}/b^2+1/4*x^3*(c*x^2)^{(1/2)}/b+a^4*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^5/x$

Rubi [A] time = 0.04, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^3 \sqrt{cx^2}}{b^4} + \frac{a^2 x \sqrt{cx^2}}{2b^3} + \frac{a^4 \sqrt{cx^2} \log(a+bx)}{b^5 x} - \frac{ax^2 \sqrt{cx^2}}{3b^2} + \frac{x^3 \sqrt{cx^2}}{4b}$$

Antiderivative was successfully verified.

[In] Int[(x^3*Sqrt[c*x^2])/(a + b*x), x]

[Out] $-((a^3*\text{Sqrt}[c*x^2])/b^4) + (a^2*x*\text{Sqrt}[c*x^2])/(2*b^3) - (a*x^2*\text{Sqrt}[c*x^2])/(3*b^2) + (x^3*\text{Sqrt}[c*x^2])/(4*b) + (a^4*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^5*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3 \sqrt{cx^2}}{a+bx} dx &= \frac{\sqrt{cx^2} \int \frac{x^4}{a+bx} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(-\frac{a^3}{b^4} + \frac{a^2x}{b^3} - \frac{ax^2}{b^2} + \frac{x^3}{b} + \frac{a^4}{b^4(a+bx)} \right) dx}{x} \\ &= -\frac{a^3 \sqrt{cx^2}}{b^4} + \frac{a^2 x \sqrt{cx^2}}{2b^3} - \frac{ax^2 \sqrt{cx^2}}{3b^2} + \frac{x^3 \sqrt{cx^2}}{4b} + \frac{a^4 \sqrt{cx^2} \log(a+bx)}{b^5 x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 63, normalized size = 0.62

$$\frac{cx \left(12a^4 \log(a+bx) + bx \left(-12a^3 + 6a^2bx - 4ab^2x^2 + 3b^3x^3 \right) \right)}{12b^5 \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*Sqrt[c*x^2])/(a + b*x),x]

[Out] (c*x*(b*x*(-12*a^3 + 6*a^2*b*x - 4*a*b^2*x^2 + 3*b^3*x^3) + 12*a^4*Log[a + b*x]))/(12*b^5*Sqrt[c*x^2])

fricas [A] time = 0.43, size = 62, normalized size = 0.61

$$\frac{(3b^4x^4 - 4ab^3x^3 + 6a^2b^2x^2 - 12a^3bx + 12a^4 \log(bx+a)) \sqrt{cx^2}}{12b^5x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^(1/2)/(b*x+a),x, algorithm="fricas")

[Out] 1/12*(3*b^4*x^4 - 4*a*b^3*x^3 + 6*a^2*b^2*x^2 - 12*a^3*b*x + 12*a^4*log(b*x + a))*sqrt(c*x^2)/(b^5*x)

giac [A] time = 1.11, size = 81, normalized size = 0.79

$$\frac{1}{12} \sqrt{c} \left(\frac{12a^4 \log(|bx+a|) \operatorname{sgn}(x)}{b^5} - \frac{12a^4 \log(|a|) \operatorname{sgn}(x)}{b^5} + \frac{3b^3x^4 \operatorname{sgn}(x) - 4ab^2x^3 \operatorname{sgn}(x) + 6a^2bx^2 \operatorname{sgn}(x) - 12a^3x \operatorname{sgn}(x)}{b^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^(1/2)/(b*x+a),x, algorithm="giac")

[Out] $1/12*\sqrt{c}*(12*a^4*\log(\text{abs}(b*x + a))*\text{sgn}(x)/b^5 - 12*a^4*\log(\text{abs}(a))*\text{sgn}(x)/b^5 + (3*b^3*x^4*\text{sgn}(x) - 4*a*b^2*x^3*\text{sgn}(x) + 6*a^2*b*x^2*\text{sgn}(x) - 12*a^3*x*\text{sgn}(x))/b^4)$

maple [A] time = 0.01, size = 63, normalized size = 0.62

$$\frac{\sqrt{cx^2} (3b^4x^4 - 4ab^3x^3 + 6a^2b^2x^2 + 12a^4 \ln(bx + a) - 12a^3bx)}{12b^5x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^3*(c*x^2)^{(1/2)}/(b*x+a), x)$

[Out] $1/12*(c*x^2)^{(1/2)}*(3*b^4*x^4-4*x^3*a*b^3+6*x^2*a^2*b^2+12*a^4*\ln(b*x+a)-12*b*x*a^3)/x/b^5$

maxima [A] time = 1.57, size = 128, normalized size = 1.25

$$\frac{(-1)^{\frac{2cx}{b}} a^4 \sqrt{c} \log\left(\frac{2cx}{b}\right)}{b^5} + \frac{(-1)^{\frac{2acx}{b}} a^4 \sqrt{c} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^5} + \frac{\sqrt{cx^2} a^2 x}{2b^3} + \frac{(cx^2)^{\frac{3}{2}} x}{4bc} - \frac{\sqrt{cx^2} a^3}{b^4} - \frac{(cx^2)^{\frac{3}{2}} a}{3b^2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^3*(c*x^2)^{(1/2)}/(b*x+a), x, \text{algorithm}=\text{"maxima"})$

[Out] $(-1)^{(2*c*x/b)}*a^4*\sqrt{c}*\log(2*c*x/b)/b^5 + (-1)^{(2*a*c*x/b)}*a^4*\sqrt{c}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/b^5 + 1/2*\sqrt{c*x^2}*a^2*x/b^3 + 1/4*(c*x^2)^{(3/2)}*x/(b*c) - \sqrt{c*x^2}*a^3/b^4 - 1/3*(c*x^2)^{(3/2)}*a/(b^2*c)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^3 \sqrt{cx^2}}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((x^3*(c*x^2)^{(1/2)})/(a + b*x), x)$

[Out] $\text{int}((x^3*(c*x^2)^{(1/2)})/(a + b*x), x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^3 \sqrt{cx^2}}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x**3*(c*x**2)**(1/2)/(b*x+a), x)$

[Out] $\text{Integral}(x**3*\sqrt{c*x**2}/(a + b*x), x)$

$$3.853 \quad \int \frac{x^2 \sqrt{cx^2}}{a+bx} dx$$

Optimal. Leaf size=80

$$-\frac{a^3 \sqrt{cx^2} \log(a+bx)}{b^4 x} + \frac{a^2 \sqrt{cx^2}}{b^3} - \frac{ax \sqrt{cx^2}}{2b^2} + \frac{x^2 \sqrt{cx^2}}{3b}$$

[Out] $a^2*(c*x^2)^{(1/2)}/b^3-1/2*a*x*(c*x^2)^{(1/2)}/b^2+1/3*x^2*(c*x^2)^{(1/2)}/b-a^3*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^4/x$

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2 \sqrt{cx^2}}{b^3} - \frac{a^3 \sqrt{cx^2} \log(a+bx)}{b^4 x} - \frac{ax \sqrt{cx^2}}{2b^2} + \frac{x^2 \sqrt{cx^2}}{3b}$$

Antiderivative was successfully verified.

[In] Int[(x^2*Sqrt[c*x^2])/(a + b*x), x]

[Out] $(a^2*\text{Sqrt}[c*x^2])/b^3 - (a*x*\text{Sqrt}[c*x^2])/(2*b^2) + (x^2*\text{Sqrt}[c*x^2])/(3*b) - (a^3*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^4*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{x^2 \sqrt{cx^2}}{a+bx} dx &= \frac{\sqrt{cx^2} \int \frac{x^3}{a+bx} dx}{x} \\
&= \frac{\sqrt{cx^2} \int \left(\frac{a^2}{b^3} - \frac{ax}{b^2} + \frac{x^2}{b} - \frac{a^3}{b^3(a+bx)} \right) dx}{x} \\
&= \frac{a^2 \sqrt{cx^2}}{b^3} - \frac{ax \sqrt{cx^2}}{2b^2} + \frac{x^2 \sqrt{cx^2}}{3b} - \frac{a^3 \sqrt{cx^2} \log(a+bx)}{b^4 x}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 52, normalized size = 0.65

$$\frac{cx \left(bx \left(6a^2 - 3abx + 2b^2x^2 \right) - 6a^3 \log(a+bx) \right)}{6b^4 \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*Sqrt[c*x^2])/(a + b*x),x]

[Out] (c*x*(b*x*(6*a^2 - 3*a*b*x + 2*b^2*x^2) - 6*a^3*Log[a + b*x]))/(6*b^4*Sqrt[c*x^2])

fricas [A] time = 0.42, size = 51, normalized size = 0.64

$$\frac{(2b^3x^3 - 3ab^2x^2 + 6a^2bx - 6a^3 \log(bx+a))\sqrt{cx^2}}{6b^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(1/2)/(b*x+a),x, algorithm="fricas")

[Out] 1/6*(2*b^3*x^3 - 3*a*b^2*x^2 + 6*a^2*b*x - 6*a^3*log(b*x + a))*sqrt(c*x^2)/(b^4*x)

giac [A] time = 0.94, size = 69, normalized size = 0.86

$$-\frac{1}{6} \sqrt{c} \left(\frac{6a^3 \log(|bx+a|) \operatorname{sgn}(x)}{b^4} - \frac{6a^3 \log(|a|) \operatorname{sgn}(x)}{b^4} - \frac{2b^2x^3 \operatorname{sgn}(x) - 3abx^2 \operatorname{sgn}(x) + 6a^2x \operatorname{sgn}(x)}{b^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(1/2)/(b*x+a),x, algorithm="giac")

[Out] -1/6*sqrt(c)*(6*a^3*log(abs(b*x + a))*sgn(x)/b^4 - 6*a^3*log(abs(a))*sgn(x)/b^4 - (2*b^2*x^3*sgn(x) - 3*a*b*x^2*sgn(x) + 6*a^2*x*sgn(x))/b^3)

maple [A] time = 0.01, size = 52, normalized size = 0.65

$$\frac{\sqrt{cx^2} (-2b^3x^3 + 3ab^2x^2 + 6a^3 \ln(bx + a) - 6a^2bx)}{6b^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(c*x^2)^(1/2)/(b*x+a), x)`

[Out] `-1/6*(c*x^2)^(1/2)*(-2*b^3*x^3+3*a*b^2*x^2+6*a^3*ln(b*x+a)-6*a^2*b*x)/x/b^4`

maxima [A] time = 1.56, size = 110, normalized size = 1.38

$$-\frac{(-1)^{\frac{2cx}{b}} a^3 \sqrt{c} \log\left(\frac{2cx}{b}\right)}{b^4} - \frac{(-1)^{\frac{2acx}{b}} a^3 \sqrt{c} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^4} - \frac{\sqrt{cx^2} ax}{2b^2} + \frac{\sqrt{cx^2} a^2}{b^3} + \frac{(cx^2)^{\frac{3}{2}}}{3bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(c*x^2)^(1/2)/(b*x+a), x, algorithm="maxima")`

[Out] `-(-1)^(2*c*x/b)*a^3*sqrt(c)*log(2*c*x/b)/b^4 - (-1)^(2*a*c*x/b)*a^3*sqrt(c)*log(-2*a*c*x/(b*abs(b*x + a)))/b^4 - 1/2*sqrt(c*x^2)*a*x/b^2 + sqrt(c*x^2)*a^2/b^3 + 1/3*(c*x^2)^(3/2)/(b*c)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^2 \sqrt{cx^2}}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x^2*(c*x^2)^(1/2))/(a + b*x), x)`

[Out] `int((x^2*(c*x^2)^(1/2))/(a + b*x), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2 \sqrt{cx^2}}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(c*x**2)**(1/2)/(b*x+a), x)`

[Out] `Integral(x**2*sqrt(c*x**2)/(a + b*x), x)`

$$3.854 \quad \int \frac{x\sqrt{cx^2}}{a+bx} dx$$

Optimal. Leaf size=58

$$\frac{a^2\sqrt{cx^2} \log(a+bx)}{b^3x} - \frac{a\sqrt{cx^2}}{b^2} + \frac{x\sqrt{cx^2}}{2b}$$

[Out] $-a*(c*x^2)^{(1/2)}/b^2+1/2*x*(c*x^2)^{(1/2)}/b+a^2*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^3/x$

Rubi [A] time = 0.02, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{a^2\sqrt{cx^2} \log(a+bx)}{b^3x} - \frac{a\sqrt{cx^2}}{b^2} + \frac{x\sqrt{cx^2}}{2b}$$

Antiderivative was successfully verified.

[In] Int[(x*Sqrt[c*x^2])/(a + b*x), x]

[Out] $-((a*\text{Sqrt}[c*x^2])/b^2) + (x*\text{Sqrt}[c*x^2])/(2*b) + (a^2*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^3*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x\sqrt{cx^2}}{a+bx} dx &= \frac{\sqrt{cx^2} \int \frac{x^2}{a+bx} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(-\frac{a}{b^2} + \frac{x}{b} + \frac{a^2}{b^2(a+bx)}\right) dx}{x} \\ &= -\frac{a\sqrt{cx^2}}{b^2} + \frac{x\sqrt{cx^2}}{2b} + \frac{a^2\sqrt{cx^2} \log(a+bx)}{b^3x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 0.69

$$\frac{cx(2a^2 \log(a+bx) + bx(bx-2a))}{2b^3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x*Sqrt[c*x^2])/(a + b*x),x]

[Out] (c*x*(b*x*(-2*a + b*x) + 2*a^2*Log[a + b*x]))/(2*b^3*Sqrt[c*x^2])

fricas [A] time = 0.42, size = 39, normalized size = 0.67

$$\frac{(b^2x^2 - 2abx + 2a^2 \log(bx+a))\sqrt{cx^2}}{2b^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(1/2)/(b*x+a),x, algorithm="fricas")

[Out] 1/2*(b^2*x^2 - 2*a*b*x + 2*a^2*log(b*x + a))*sqrt(c*x^2)/(b^3*x)

giac [A] time = 1.02, size = 54, normalized size = 0.93

$$\frac{1}{2} \sqrt{c} \left(\frac{2a^2 \log(|bx+a|) \operatorname{sgn}(x)}{b^3} - \frac{2a^2 \log(|a|) \operatorname{sgn}(x)}{b^3} + \frac{bx^2 \operatorname{sgn}(x) - 2ax \operatorname{sgn}(x)}{b^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(1/2)/(b*x+a),x, algorithm="giac")

[Out] 1/2*sqrt(c)*(2*a^2*log(abs(b*x + a))*sgn(x)/b^3 - 2*a^2*log(abs(a))*sgn(x)/b^3 + (b*x^2*sgn(x) - 2*a*x*sgn(x))/b^2)

maple [A] time = 0.01, size = 40, normalized size = 0.69

$$\frac{\sqrt{cx^2} (b^2x^2 + 2a^2 \ln(bx + a) - 2abx)}{2b^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(1/2)/(b*x+a), x)`

[Out] `1/2*(c*x^2)^(1/2)*(b^2*x^2+2*a^2*ln(b*x+a)-2*a*b*x)/x/b^3`

maxima [A] time = 1.49, size = 91, normalized size = 1.57

$$\frac{(-1)^{\frac{2cx}{b}} a^2 \sqrt{c} \log\left(\frac{2cx}{b}\right)}{b^3} + \frac{(-1)^{\frac{2acx}{b}} a^2 \sqrt{c} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^3} + \frac{\sqrt{cx^2} x}{2b} - \frac{\sqrt{cx^2} a}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x^2)^(1/2)/(b*x+a), x, algorithm="maxima")`

[Out] `(-1)^(2*c*x/b)*a^2*sqrt(c)*log(2*c*x/b)/b^3 + (-1)^(2*a*c*x/b)*a^2*sqrt(c)*log(-2*a*c*x/(b*abs(b*x + a)))/b^3 + 1/2*sqrt(c*x^2)*x/b - sqrt(c*x^2)*a/b^2`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x \sqrt{cx^2}}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x*(c*x^2)^(1/2))/(a + b*x), x)`

[Out] `int((x*(c*x^2)^(1/2))/(a + b*x), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x \sqrt{cx^2}}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x**2)**(1/2)/(b*x+a), x)`

[Out] `Integral(x*sqrt(c*x**2)/(a + b*x), x)`

$$3.855 \quad \int \frac{\sqrt{cx^2}}{a+bx} dx$$

Optimal. Leaf size=38

$$\frac{\sqrt{cx^2}}{b} - \frac{a\sqrt{cx^2} \log(a+bx)}{b^2x}$$

[Out] (c*x^2)^(1/2)/b-a*ln(b*x+a)*(c*x^2)^(1/2)/b^2/x

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$\frac{\sqrt{cx^2}}{b} - \frac{a\sqrt{cx^2} \log(a+bx)}{b^2x}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c*x^2]/(a + b*x), x]

[Out] Sqrt[c*x^2]/b - (a*Sqrt[c*x^2]*Log[a + b*x])/(b^2*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2}}{a+bx} dx &= \frac{\sqrt{cx^2} \int \frac{x}{a+bx} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(\frac{1}{b} - \frac{a}{b(a+bx)} \right) dx}{x} \\ &= \frac{\sqrt{cx^2}}{b} - \frac{a\sqrt{cx^2} \log(a+bx)}{b^2x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.74

$$\frac{cx(bx - a \log(a + bx))}{b^2 \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]/(a + b*x), x]

[Out] (c*x*(b*x - a*Log[a + b*x]))/(b^2*Sqrt[c*x^2])

fricas [A] time = 0.41, size = 27, normalized size = 0.71

$$\frac{\sqrt{cx^2} (bx - a \log(bx + a))}{b^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/(b*x+a), x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x - a*log(b*x + a))/(b^2*x)

giac [A] time = 0.96, size = 37, normalized size = 0.97

$$\sqrt{c} \left(\frac{x \operatorname{sgn}(x)}{b} - \frac{a \log(|bx + a|) \operatorname{sgn}(x)}{b^2} + \frac{a \log(|a|) \operatorname{sgn}(x)}{b^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/(b*x+a), x, algorithm="giac")

[Out] sqrt(c)*(x*sgn(x)/b - a*log(abs(b*x + a))*sgn(x)/b^2 + a*log(abs(a))*sgn(x)/b^2)

maple [A] time = 0.00, size = 29, normalized size = 0.76

$$-\frac{\sqrt{cx^2} (a \ln(bx + a) - bx)}{b^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/(b*x+a), x)

[Out] -(c*x^2)^(1/2)*(a*ln(b*x+a)-b*x)/b^2/x

maxima [B] time = 1.45, size = 74, normalized size = 1.95

$$-\frac{(-1)^{\frac{2cx}{b}} a \sqrt{c} \log\left(\frac{2cx}{b}\right)}{b^2} - \frac{(-1)^{\frac{2acx}{b}} a \sqrt{c} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^2} + \frac{\sqrt{cx^2}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/(b*x+a),x, algorithm="maxima")

[Out] $-(-1)^{(2*c*x/b)*a*\sqrt{c}}*\log(2*c*x/b)/b^2 - (-1)^{(2*a*c*x/b)*a*\sqrt{c}}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/b^2 + \sqrt{c}*x^2/b$

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{\sqrt{cx^2}}{a+bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/(a + b*x), x)

[Out] int((c*x^2)^(1/2)/(a + b*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2}}{a+bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(1/2)/(b*x+a), x)

[Out] Integral(sqrt(c*x**2)/(a + b*x), x)

$$3.856 \quad \int \frac{\sqrt{cx^2}}{x(a+bx)} dx$$

Optimal. Leaf size=22

$$\frac{\sqrt{cx^2} \log(a+bx)}{bx}$$

[Out] $\ln(b*x+a)*(c*x^2)^{(1/2)}/b/x$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 31}

$$\frac{\sqrt{cx^2} \log(a+bx)}{bx}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{Sqrt}[c*x^2]/(x*(a + b*x)), x]$

[Out] $(\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b*x)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 31

$\text{Int}[(a_ + (b_)*(x_))^{(-1)}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] /; \text{FreeQ}\{a, b\}, x]$

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2}}{x(a+bx)} dx &= \frac{\sqrt{cx^2} \int \frac{1}{a+bx} dx}{x} \\ &= \frac{\sqrt{cx^2} \log(a+bx)}{bx} \end{aligned}$$

Mathematica [A] time = 0.00, size = 21, normalized size = 0.95

$$\frac{cx \log(a+bx)}{b\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]/(x*(a + b*x)),x]

[Out] (c*x*Log[a + b*x])/(b*Sqrt[c*x^2])

fricas [A] time = 0.41, size = 20, normalized size = 0.91

$$\frac{\sqrt{cx^2} \log(bx + a)}{bx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x/(b*x+a),x, algorithm="fricas")

[Out] sqrt(c*x^2)*log(b*x + a)/(b*x)

giac [A] time = 0.95, size = 28, normalized size = 1.27

$$\sqrt{c} \left(\frac{\log(|bx + a|) \operatorname{sgn}(x)}{b} - \frac{\log(|a|) \operatorname{sgn}(x)}{b} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x/(b*x+a),x, algorithm="giac")

[Out] sqrt(c)*(log(abs(b*x + a))*sgn(x)/b - log(abs(a))*sgn(x)/b)

maple [A] time = 0.00, size = 21, normalized size = 0.95

$$\frac{\sqrt{cx^2} \ln(bx + a)}{bx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/x/(b*x+a),x)

[Out] ln(b*x+a)*(c*x^2)^(1/2)/b/x

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x/(b*x+a),x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [F] time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{\sqrt{cx^2}}{x(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(1/2)/(x*(a + b*x)), x)`

[Out] `int((c*x^2)^(1/2)/(x*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2}}{x(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(1/2)/x/(b*x+a), x)`

[Out] `Integral(sqrt(c*x**2)/(x*(a + b*x)), x)`

$$3.857 \quad \int \frac{\sqrt{cx^2}}{x^2(a+bx)} dx$$

Optimal. Leaf size=42

$$\frac{\sqrt{cx^2} \log(x)}{ax} - \frac{\sqrt{cx^2} \log(a+bx)}{ax}$$

[Out] $\ln(x) \cdot (c \cdot x^2)^{(1/2)} / a / x - \ln(b \cdot x + a) \cdot (c \cdot x^2)^{(1/2)} / a / x$

Rubi [A] time = 0.01, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {15, 36, 29, 31}

$$\frac{\sqrt{cx^2} \log(x)}{ax} - \frac{\sqrt{cx^2} \log(a+bx)}{ax}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[c*x^2]/(x^2*(a + b*x)),x]`

[Out] `(Sqrt[c*x^2]*Log[x])/(a*x) - (Sqrt[c*x^2]*Log[a + b*x])/(a*x)`

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rule 29

`Int[(x_)^(-1), x_Symbol] := Simp[Log[x], x]`

Rule 31

`Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]`

Rule 36

`Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))), x_Symbol] := Dist[b/(b*c - a*d), Int[1/(a + b*x), x], x] - Dist[d/(b*c - a*d), Int[1/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0]`

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{cx^2}}{x^2(a+bx)} dx &= \frac{\sqrt{cx^2} \int \frac{1}{x(a+bx)} dx}{x} \\
&= \frac{\sqrt{cx^2} \int \frac{1}{x} dx}{ax} - \frac{(b\sqrt{cx^2}) \int \frac{1}{a+bx} dx}{ax} \\
&= \frac{\sqrt{cx^2} \log(x)}{ax} - \frac{\sqrt{cx^2} \log(a+bx)}{ax}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 0.62

$$\frac{cx(\log(x) - \log(a + bx))}{a\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]/(x^2*(a + b*x)),x]

[Out] (c*x*(Log[x] - Log[a + b*x]))/(a*Sqrt[c*x^2])

fricas [A] time = 0.45, size = 64, normalized size = 1.52

$$\left[\frac{\sqrt{cx^2} \log\left(\frac{x}{bx+a}\right)}{ax}, \frac{2\sqrt{-c} \arctan\left(\frac{\sqrt{cx^2}(2bx+a)\sqrt{-c}}{acx}\right)}{a} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^2/(b*x+a),x, algorithm="fricas")

[Out] [sqrt(c*x^2)*log(x/(b*x + a))/(a*x), 2*sqrt(-c)*arctan(sqrt(c*x^2)*(2*b*x + a)*sqrt(-c)/(a*c*x))/a]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^2/(b*x+a),x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
UT:sage2:=int(sage0,x);;OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 26, normalized size = 0.62

$$\frac{\sqrt{cx^2} (\ln(x) - \ln(bx + a))}{ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/x^2/(b*x+a),x)

[Out] (c*x^2)^(1/2)*(ln(x)-ln(b*x+a))/x/a

maxima [A] time = 1.38, size = 24, normalized size = 0.57

$$-\frac{\sqrt{c} \log(bx + a)}{a} + \frac{\sqrt{c} \log(x)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^2/(b*x+a),x, algorithm="maxima")

[Out] -sqrt(c)*log(b*x + a)/a + sqrt(c)*log(x)/a

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{cx^2}}{x^2 (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/(x^2*(a + b*x)),x)

[Out] int((c*x^2)^(1/2)/(x^2*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2}}{x^2 (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(1/2)/x**2/(b*x+a),x)

[Out] Integral(sqrt(c*x**2)/(x**2*(a + b*x)), x)

$$3.858 \quad \int \frac{\sqrt{cx^2}}{x^3(a+bx)} dx$$

Optimal. Leaf size=61

$$-\frac{b\sqrt{cx^2} \log(x)}{a^2x} + \frac{b\sqrt{cx^2} \log(a+bx)}{a^2x} - \frac{\sqrt{cx^2}}{ax^2}$$

[Out] $-(c*x^2)^{(1/2)}/a/x^2-b*\ln(x)*(c*x^2)^{(1/2)}/a^2/x+b*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^2/x$

Rubi [A] time = 0.02, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{b\sqrt{cx^2} \log(x)}{a^2x} + \frac{b\sqrt{cx^2} \log(a+bx)}{a^2x} - \frac{\sqrt{cx^2}}{ax^2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c*x^2]/(x^3*(a + b*x)), x]

[Out] $-(\text{Sqrt}[c*x^2]/(a*x^2)) - (b*\text{Sqrt}[c*x^2]*\text{Log}[x])/(a^2*x) + (b*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(a^2*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{cx^2}}{x^3(a+bx)} dx &= \frac{\sqrt{cx^2} \int \frac{1}{x^2(a+bx)} dx}{x} \\
&= \frac{\sqrt{cx^2} \int \left(\frac{1}{ax^2} - \frac{b}{a^2x} + \frac{b^2}{a^2(a+bx)} \right) dx}{x} \\
&= -\frac{\sqrt{cx^2}}{ax^2} - \frac{b\sqrt{cx^2} \log(x)}{a^2x} + \frac{b\sqrt{cx^2} \log(a+bx)}{a^2x}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 0.52

$$-\frac{c(-bx \log(a+bx) + a + bx \log(x))}{a^2 \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]/(x^3*(a + b*x)),x]

[Out] -((c*(a + b*x*Log[x] - b*x*Log[a + b*x]))/(a^2*Sqrt[c*x^2]))

fricas [A] time = 0.44, size = 31, normalized size = 0.51

$$\frac{\sqrt{cx^2} \left(bx \log\left(\frac{bx+a}{x}\right) - a \right)}{a^2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^3/(b*x+a),x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x*log((b*x + a)/x) - a)/(a^2*x^2)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^3/(b*x+a),x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
 UT:sage2:=int(sage0,x);OUTPUT:Warning, integration of abs or sign assumes
 constant sign by intervals (correct if the argument is real):Check [abs(x)]
 Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 33, normalized size = 0.54

$$\frac{\sqrt{c} x^2 (bx \ln(x) - bx \ln(bx + a) + a)}{a^2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/x^3/(b*x+a), x)

[Out] -(c*x^2)^(1/2)*(b*x*ln(x)-b*ln(b*x+a)*x+a)/x^2/a^2

maxima [A] time = 1.38, size = 37, normalized size = 0.61

$$\frac{b\sqrt{c} \log(bx + a)}{a^2} - \frac{b\sqrt{c} \log(x)}{a^2} - \frac{\sqrt{c}}{ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^3/(b*x+a), x, algorithm="maxima")

[Out] b*sqrt(c)*log(b*x + a)/a^2 - b*sqrt(c)*log(x)/a^2 - sqrt(c)/(a*x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{c} x^2}{x^3 (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/(x^3*(a + b*x)), x)

[Out] int((c*x^2)^(1/2)/(x^3*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{c} x^2}{x^3 (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(1/2)/x**3/(b*x+a), x)

[Out] Integral(sqrt(c*x**2)/(x**3*(a + b*x)), x)

$$3.859 \quad \int \frac{\sqrt{cx^2}}{x^4(a+bx)} dx$$

Optimal. Leaf size=84

$$\frac{b^2\sqrt{cx^2} \log(x)}{a^3x} - \frac{b^2\sqrt{cx^2} \log(a+bx)}{a^3x} + \frac{b\sqrt{cx^2}}{a^2x^2} - \frac{\sqrt{cx^2}}{2ax^3}$$

[Out] $-1/2*(c*x^2)^{(1/2)}/x^3/a+b*(c*x^2)^{(1/2)}/a^2/x^2+b^2*\ln(x)*(c*x^2)^{(1/2)}/a^3/x-b^2*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^3/x$

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$\frac{b^2\sqrt{cx^2} \log(x)}{a^3x} - \frac{b^2\sqrt{cx^2} \log(a+bx)}{a^3x} + \frac{b\sqrt{cx^2}}{a^2x^2} - \frac{\sqrt{cx^2}}{2ax^3}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c*x^2]/(x^4*(a + b*x)),x]

[Out] $-\text{Sqrt}[c*x^2]/(2*a*x^3) + (b*\text{Sqrt}[c*x^2])/(a^2*x^2) + (b^2*\text{Sqrt}[c*x^2]*\text{Log}[x])/ (a^3*x) - (b^2*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/ (a^3*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2}}{x^4(a+bx)} dx &= \frac{\sqrt{cx^2} \int \frac{1}{x^3(a+bx)} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(\frac{1}{ax^3} - \frac{b}{a^2x^2} + \frac{b^2}{a^3x} - \frac{b^3}{a^3(a+bx)} \right) dx}{x} \\ &= -\frac{\sqrt{cx^2}}{2ax^3} + \frac{b\sqrt{cx^2}}{a^2x^2} + \frac{b^2\sqrt{cx^2} \log(x)}{a^3x} - \frac{b^2\sqrt{cx^2} \log(a+bx)}{a^3x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 53, normalized size = 0.63

$$\frac{\sqrt{cx^2} \left(-2b^2x^2 \log(a+bx) - a(a-2bx) + 2b^2x^2 \log(x) \right)}{2a^3x^3}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]/(x^4*(a + b*x)),x]

[Out] (Sqrt[c*x^2]*(-(a*(a - 2*b*x)) + 2*b^2*x^2*Log[x] - 2*b^2*x^2*Log[a + b*x]))/(2*a^3*x^3)

fricas [A] time = 0.42, size = 44, normalized size = 0.52

$$\frac{\left(2b^2x^2 \log\left(\frac{x}{bx+a}\right) + 2abx - a^2 \right) \sqrt{cx^2}}{2a^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^4/(b*x+a),x, algorithm="fricas")

[Out] 1/2*(2*b^2*x^2*log(x/(b*x + a)) + 2*a*b*x - a^2)*sqrt(c*x^2)/(a^3*x^3)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^4/(b*x+a),x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x);;OUTPUT:Warning, integration of abs or sign assumes constant sign by intervals (correct if the argument is real):Check [abs(x)] Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 51, normalized size = 0.61

$$\frac{\sqrt{cx^2} (2b^2x^2 \ln(x) - 2b^2x^2 \ln(bx + a) + 2abx - a^2)}{2a^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(1/2)/x^4/(b*x+a), x)`

[Out] `1/2*(c*x^2)^(1/2)*(2*b^2*x^2*ln(x)-2*b^2*ln(b*x+a)*x^2+2*a*b*x-a^2)/a^3/x^3`

maxima [A] time = 1.36, size = 52, normalized size = 0.62

$$-\frac{b^2\sqrt{c} \log(bx + a)}{a^3} + \frac{b^2\sqrt{c} \log(x)}{a^3} + \frac{2b\sqrt{c}x - a\sqrt{c}}{2a^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(1/2)/x^4/(b*x+a), x, algorithm="maxima")`

[Out] `-b^2*sqrt(c)*log(b*x + a)/a^3 + b^2*sqrt(c)*log(x)/a^3 + 1/2*(2*b*sqrt(c)*x - a*sqrt(c))/(a^2*x^2)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\sqrt{cx^2}}{x^4 (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(1/2)/(x^4*(a + b*x)), x)`

[Out] `int((c*x^2)^(1/2)/(x^4*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2}}{x^4 (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(1/2)/x**4/(b*x+a), x)`

[Out] `Integral(sqrt(c*x**2)/(x**4*(a + b*x)), x)`

$$3.860 \quad \int \frac{x(cx^2)^{3/2}}{a+bx} dx$$

Optimal. Leaf size=107

$$\frac{a^4c\sqrt{cx^2} \log(a+bx)}{b^5x} - \frac{a^3c\sqrt{cx^2}}{b^4} + \frac{a^2cx\sqrt{cx^2}}{2b^3} - \frac{acx^2\sqrt{cx^2}}{3b^2} + \frac{cx^3\sqrt{cx^2}}{4b}$$

[Out] $-a^3c*(c*x^2)^{(1/2)}/b^4+1/2*a^2*c*x*(c*x^2)^{(1/2)}/b^3-1/3*a*c*x^2*(c*x^2)^{(1/2)}/b^2+1/4*c*x^3*(c*x^2)^{(1/2)}/b+a^4*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^5/x$

Rubi [A] time = 0.03, antiderivative size = 107, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a^3c\sqrt{cx^2}}{b^4} + \frac{a^2cx\sqrt{cx^2}}{2b^3} + \frac{a^4c\sqrt{cx^2} \log(a+bx)}{b^5x} - \frac{acx^2\sqrt{cx^2}}{3b^2} + \frac{cx^3\sqrt{cx^2}}{4b}$$

Antiderivative was successfully verified.

[In] Int[(x*(c*x^2)^(3/2))/(a + b*x), x]

[Out] $-((a^3*c*\text{Sqrt}[c*x^2])/b^4) + (a^2*c*x*\text{Sqrt}[c*x^2])/(2*b^3) - (a*c*x^2*\text{Sqrt}[c*x^2])/(3*b^2) + (c*x^3*\text{Sqrt}[c*x^2])/(4*b) + (a^4*c*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^5*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x (cx^2)^{3/2}}{a+bx} dx &= \frac{(c\sqrt{cx^2}) \int \frac{x^4}{a+bx} dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int \left(-\frac{a^3}{b^4} + \frac{a^2x}{b^3} - \frac{ax^2}{b^2} + \frac{x^3}{b} + \frac{a^4}{b^4(a+bx)}\right) dx}{x} \\ &= -\frac{a^3c\sqrt{cx^2}}{b^4} + \frac{a^2cx\sqrt{cx^2}}{2b^3} - \frac{acx^2\sqrt{cx^2}}{3b^2} + \frac{cx^3\sqrt{cx^2}}{4b} + \frac{a^4c\sqrt{cx^2} \log(a+bx)}{b^5x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 64, normalized size = 0.60

$$\frac{(cx^2)^{3/2} (12a^4 \log(a+bx) + bx(-12a^3 + 6a^2bx - 4ab^2x^2 + 3b^3x^3))}{12b^5x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(x*(c*x^2)^(3/2))/(a + b*x), x]

[Out] ((c*x^2)^(3/2)*(b*x*(-12*a^3 + 6*a^2*b*x - 4*a*b^2*x^2 + 3*b^3*x^3) + 12*a^4*Log[a + b*x]))/(12*b^5*x^3)

fricas [A] time = 0.43, size = 67, normalized size = 0.63

$$\frac{(3b^4cx^4 - 4ab^3cx^3 + 6a^2b^2cx^2 - 12a^3bcx + 12a^4c \log(bx+a))\sqrt{cx^2}}{12b^5x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)/(b*x+a), x, algorithm="fricas")

[Out] 1/12*(3*b^4*c*x^4 - 4*a*b^3*c*x^3 + 6*a^2*b^2*c*x^2 - 12*a^3*b*c*x + 12*a^4*c*log(b*x + a))*sqrt(c*x^2)/(b^5*x)

giac [A] time = 1.00, size = 81, normalized size = 0.76

$$\frac{1}{12} c^{\frac{3}{2}} \left(\frac{12 a^4 \log(|bx+a|) \operatorname{sgn}(x)}{b^5} - \frac{12 a^4 \log(|a|) \operatorname{sgn}(x)}{b^5} + \frac{3 b^3 x^4 \operatorname{sgn}(x) - 4 a b^2 x^3 \operatorname{sgn}(x) + 6 a^2 b x^2 \operatorname{sgn}(x) - 12 a^3 \operatorname{sgn}(x)}{b^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)/(b*x+a), x, algorithm="giac")

[Out] $1/12*c^{(3/2)}*(12*a^4*\log(\text{abs}(b*x + a))*\text{sgn}(x)/b^5 - 12*a^4*\log(\text{abs}(a))*\text{sgn}(x)/b^5 + (3*b^3*x^4*\text{sgn}(x) - 4*a*b^2*x^3*\text{sgn}(x) + 6*a^2*b*x^2*\text{sgn}(x) - 12*a^3*x*\text{sgn}(x))/b^4)$

maple [A] time = 0.01, size = 63, normalized size = 0.59

$$\frac{(cx^2)^{\frac{3}{2}} (3b^4x^4 - 4ab^3x^3 + 6a^2b^2x^2 + 12a^4 \ln(bx + a) - 12a^3bx)}{12b^5x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(3/2)/(b*x+a),x)`

[Out] $1/12*(c*x^2)^{(3/2)}*(3*b^4*x^4-4*a*b^3*x^3+6*a^2*b^2*x^2+12*a^4*\ln(b*x+a)-12*a^3*b*x)/x^3/b^5$

maxima [A] time = 1.62, size = 124, normalized size = 1.16

$$\frac{(-1)^{\frac{2cx}{b}} a^4 c^{\frac{3}{2}} \log\left(\frac{2cx}{b}\right)}{b^5} + \frac{(-1)^{\frac{2acx}{b}} a^4 c^{\frac{3}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^5} + \frac{(cx^2)^{\frac{3}{2}} x}{4b} + \frac{\sqrt{cx^2} a^2 cx}{2b^3} - \frac{(cx^2)^{\frac{3}{2}} a}{3b^2} - \frac{\sqrt{cx^2} a^3 c}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x^2)^(3/2)/(b*x+a),x, algorithm="maxima")`

[Out] $(-1)^{(2*c*x/b)}*a^4*c^{(3/2)}*\log(2*c*x/b)/b^5 + (-1)^{(2*a*c*x/b)}*a^4*c^{(3/2)}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/b^5 + 1/4*(c*x^2)^{(3/2)}*x/b + 1/2*\text{sqrt}(c*x^2)*a^2*c*x/b^3 - 1/3*(c*x^2)^{(3/2)}*a/b^2 - \text{sqrt}(c*x^2)*a^3*c/b^4$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x (cx^2)^{3/2}}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x*(c*x^2)^(3/2))/(a + b*x),x)`

[Out] `int((x*(c*x^2)^(3/2))/(a + b*x), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x (cx^2)^{\frac{3}{2}}}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*(c*x**2)**(3/2)/(b*x+a),x)
```

```
[Out] Integral(x*(c*x**2)**(3/2)/(a + b*x), x)
```

$$3.861 \quad \int \frac{(cx^2)^{3/2}}{a+bx} dx$$

Optimal. Leaf size=84

$$-\frac{a^3c\sqrt{cx^2} \log(a+bx)}{b^4x} + \frac{a^2c\sqrt{cx^2}}{b^3} - \frac{acx\sqrt{cx^2}}{2b^2} + \frac{cx^2\sqrt{cx^2}}{3b}$$

[Out] $a^2c*(c*x^2)^{(1/2)}/b^3-1/2*a*c*x*(c*x^2)^{(1/2)}/b^2+1/3*c*x^2*(c*x^2)^{(1/2)}/b-a^3*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^4/x$

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$\frac{a^2c\sqrt{cx^2}}{b^3} - \frac{a^3c\sqrt{cx^2} \log(a+bx)}{b^4x} - \frac{acx\sqrt{cx^2}}{2b^2} + \frac{cx^2\sqrt{cx^2}}{3b}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(3/2)/(a + b*x), x]

[Out] $(a^2*c*\text{Sqrt}[c*x^2])/b^3 - (a*c*x*\text{Sqrt}[c*x^2])/(2*b^2) + (c*x^2*\text{Sqrt}[c*x^2])/(3*b) - (a^3*c*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^4*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2}}{a+bx} dx &= \frac{(c\sqrt{cx^2}) \int \frac{x^3}{a+bx} dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int \left(\frac{a^2}{b^3} - \frac{ax}{b^2} + \frac{x^2}{b} - \frac{a^3}{b^3(a+bx)} \right) dx}{x} \\ &= \frac{a^2c\sqrt{cx^2}}{b^3} - \frac{acx\sqrt{cx^2}}{2b^2} + \frac{cx^2\sqrt{cx^2}}{3b} - \frac{a^3c\sqrt{cx^2} \log(a+bx)}{b^4x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 53, normalized size = 0.63

$$\frac{(cx^2)^{3/2} (bx(6a^2 - 3abx + 2b^2x^2) - 6a^3 \log(a+bx))}{6b^4x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(a + b*x), x]

[Out] ((c*x^2)^(3/2)*(b*x*(6*a^2 - 3*a*b*x + 2*b^2*x^2) - 6*a^3*Log[a + b*x]))/(6*b^4*x^3)

fricas [A] time = 0.41, size = 55, normalized size = 0.65

$$\frac{(2b^3cx^3 - 3ab^2cx^2 + 6a^2bcx - 6a^3c \log(bx+a))\sqrt{cx^2}}{6b^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/(b*x+a), x, algorithm="fricas")

[Out] 1/6*(2*b^3*c*x^3 - 3*a*b^2*c*x^2 + 6*a^2*b*c*x - 6*a^3*c*log(b*x + a))*sqrt(c*x^2)/(b^4*x)

giac [A] time = 1.15, size = 69, normalized size = 0.82

$$-\frac{1}{6}c^{\frac{3}{2}} \left(\frac{6a^3 \log(|bx+a|) \operatorname{sgn}(x)}{b^4} - \frac{6a^3 \log(|a|) \operatorname{sgn}(x)}{b^4} - \frac{2b^2x^3 \operatorname{sgn}(x) - 3abx^2 \operatorname{sgn}(x) + 6a^2x \operatorname{sgn}(x)}{b^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/(b*x+a), x, algorithm="giac")

[Out] -1/6*c^(3/2)*(6*a^3*log(abs(b*x + a))*sgn(x)/b^4 - 6*a^3*log(abs(a))*sgn(x)/b^4 - (2*b^2*x^3*sgn(x) - 3*a*b*x^2*sgn(x) + 6*a^2*x*sgn(x))/b^3)

maple [A] time = 0.00, size = 52, normalized size = 0.62

$$\frac{(cx^2)^{\frac{3}{2}}(-2b^3x^3 + 3ab^2x^2 + 6a^3 \ln(bx + a) - 6a^2bx)}{6b^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(b*x+a), x)

[Out] $-1/6*(c*x^2)^{(3/2)}*(-2*b^3*x^3+3*a*b^2*x^2+6*a^3*\ln(b*x+a)-6*a^2*b*x)/x^3/b^4$

maxima [A] time = 1.54, size = 109, normalized size = 1.30

$$-\frac{(-1)^{\frac{2cx}{b}} a^3 c^{\frac{3}{2}} \log\left(\frac{2cx}{b}\right)}{b^4} - \frac{(-1)^{\frac{2acx}{b}} a^3 c^{\frac{3}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^4} - \frac{\sqrt{cx^2} acx}{2b^2} + \frac{(cx^2)^{\frac{3}{2}}}{3b} + \frac{\sqrt{cx^2} a^2 c}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/(b*x+a), x, algorithm="maxima")

[Out] $-(-1)^{(2*c*x/b)}*a^3*c^{(3/2)}*\log(2*c*x/b)/b^4 - (-1)^{(2*a*c*x/b)}*a^3*c^{(3/2)}*\log(-2*a*c*x/(b*abs(b*x + a)))/b^4 - 1/2*sqrt(c*x^2)*a*c*x/b^2 + 1/3*(c*x^2)^{(3/2)}/b + sqrt(c*x^2)*a^2*c/b^3$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{3/2}}{a+bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(a + b*x), x)

[Out] int((c*x^2)^(3/2)/(a + b*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{a+bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)/(b*x+a), x)

[Out] Integral((c*x**2)**(3/2)/(a + b*x), x)

$$3.862 \quad \int \frac{(cx^2)^{3/2}}{x(a+bx)} dx$$

Optimal. Leaf size=61

$$\frac{a^2c\sqrt{cx^2} \log(a+bx)}{b^3x} - \frac{ac\sqrt{cx^2}}{b^2} + \frac{cx\sqrt{cx^2}}{2b}$$

[Out] $-a*c*(c*x^2)^{(1/2)}/b^2+1/2*c*x*(c*x^2)^{(1/2)}/b+a^2*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^3/x$

Rubi [A] time = 0.02, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2c\sqrt{cx^2} \log(a+bx)}{b^3x} - \frac{ac\sqrt{cx^2}}{b^2} + \frac{cx\sqrt{cx^2}}{2b}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(3/2)/(x*(a + b*x)),x]

[Out] $-((a*c*\text{Sqrt}[c*x^2])/b^2) + (c*x*\text{Sqrt}[c*x^2])/(2*b) + (a^2*c*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^3*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{3/2}}{x(a+bx)} dx &= \frac{(c\sqrt{cx^2}) \int \frac{x^2}{a+bx} dx}{x} \\
&= \frac{(c\sqrt{cx^2}) \int \left(-\frac{a}{b^2} + \frac{x}{b} + \frac{a^2}{b^2(a+bx)}\right) dx}{x} \\
&= -\frac{ac\sqrt{cx^2}}{b^2} + \frac{cx\sqrt{cx^2}}{2b} + \frac{a^2c\sqrt{cx^2} \log(a+bx)}{b^3x}
\end{aligned}$$

Mathematica [A] time = 0.00, size = 42, normalized size = 0.69

$$\frac{c^2x(2a^2 \log(a+bx) + bx(bx-2a))}{2b^3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x*(a + b*x)), x]

[Out] (c^2*x*(b*x*(-2*a + b*x) + 2*a^2*Log[a + b*x]))/(2*b^3*sqrt[c*x^2])

fricas [A] time = 0.41, size = 42, normalized size = 0.69

$$\frac{(b^2cx^2 - 2abcx + 2a^2c \log(bx + a))\sqrt{cx^2}}{2b^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x/(b*x+a), x, algorithm="fricas")

[Out] 1/2*(b^2*c*x^2 - 2*a*b*c*x + 2*a^2*c*log(b*x + a))*sqrt(c*x^2)/(b^3*x)

giac [A] time = 1.12, size = 54, normalized size = 0.89

$$\frac{1}{2}c^{\frac{3}{2}}\left(\frac{2a^2 \log(|bx+a|) \operatorname{sgn}(x)}{b^3} - \frac{2a^2 \log(|a|) \operatorname{sgn}(x)}{b^3} + \frac{bx^2 \operatorname{sgn}(x) - 2ax \operatorname{sgn}(x)}{b^2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x/(b*x+a), x, algorithm="giac")

[Out] 1/2*c^(3/2)*(2*a^2*log(abs(b*x + a))*sgn(x)/b^3 - 2*a^2*log(abs(a))*sgn(x)/b^3 + (b*x^2*sgn(x) - 2*a*x*sgn(x))/b^2)

maple [A] time = 0.00, size = 40, normalized size = 0.66

$$\frac{(cx^2)^{\frac{3}{2}}(b^2x^2 + 2a^2 \ln(bx + a) - 2abx)}{2b^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x/(b*x+a), x)

[Out] 1/2*(c*x^2)^(3/2)*(b^2*x^2+2*a^2*ln(b*x+a)-2*a*b*x)/b^3/x^3

maxima [A] time = 1.48, size = 93, normalized size = 1.52

$$\frac{(-1)^{\frac{2cx}{b}} a^2 c^{\frac{3}{2}} \log\left(\frac{2cx}{b}\right)}{b^3} + \frac{(-1)^{\frac{2acx}{b}} a^2 c^{\frac{3}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^3} + \frac{\sqrt{cx^2} cx}{2b} - \frac{\sqrt{cx^2} ac}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x/(b*x+a), x, algorithm="maxima")

[Out] (-1)^(2*c*x/b)*a^2*c^(3/2)*log(2*c*x/b)/b^3 + (-1)^(2*a*c*x/b)*a^2*c^(3/2)*log(-2*a*c*x/(b*abs(b*x + a)))/b^3 + 1/2*sqrt(c*x^2)*c*x/b - sqrt(c*x^2)*a*c/b^2

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(x*(a + b*x)), x)

[Out] int((c*x^2)^(3/2)/(x*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)/x/(b*x+a), x)

[Out] Integral((c*x**2)**(3/2)/(x*(a + b*x)), x)

$$3.863 \quad \int \frac{(cx^2)^{3/2}}{x^2(a+bx)} dx$$

Optimal. Leaf size=40

$$\frac{c\sqrt{cx^2}}{b} - \frac{ac\sqrt{cx^2} \log(a+bx)}{b^2x}$$

[Out] $c*(c*x^2)^{(1/2)}/b-a*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^2/x$

Rubi [A] time = 0.01, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{c\sqrt{cx^2}}{b} - \frac{ac\sqrt{cx^2} \log(a+bx)}{b^2x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}/(x^2*(a+b*x)), x]$

[Out] $(c*\text{Sqrt}[c*x^2])/b - (a*c*\text{Sqrt}[c*x^2]*\text{Log}[a+b*x])/(b^2*x)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_.)})^{(m_.)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[((a_.) + (b_.)*(x_))^{(m_.)}*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a+b*x)^m*(c+d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2}}{x^2(a+bx)} dx &= \frac{(c\sqrt{cx^2}) \int \frac{x}{a+bx} dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int \left(\frac{1}{b} - \frac{a}{b(a+bx)}\right) dx}{x} \\ &= \frac{c\sqrt{cx^2}}{b} - \frac{ac\sqrt{cx^2} \log(a+bx)}{b^2x} \end{aligned}$$

Mathematica [A] time = 0.00, size = 30, normalized size = 0.75

$$\frac{c^2x(bx - a \log(a + bx))}{b^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^2*(a + b*x)),x]

[Out] (c^2*x*(b*x - a*Log[a + b*x]))/(b^2*Sqrt[c*x^2])

fricas [A] time = 0.44, size = 29, normalized size = 0.72

$$\frac{(bcx - ac \log(bx + a))\sqrt{cx^2}}{b^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^2/(b*x+a),x, algorithm="fricas")

[Out] (b*c*x - a*c*log(b*x + a))*sqrt(c*x^2)/(b^2*x)

giac [A] time = 1.00, size = 37, normalized size = 0.92

$$c^{\frac{3}{2}} \left(\frac{x \operatorname{sgn}(x)}{b} - \frac{a \log(|bx + a|) \operatorname{sgn}(x)}{b^2} + \frac{a \log(|a|) \operatorname{sgn}(x)}{b^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^2/(b*x+a),x, algorithm="giac")

[Out] c^(3/2)*(x*sgn(x)/b - a*log(abs(b*x + a))*sgn(x)/b^2 + a*log(abs(a))*sgn(x)/b^2)

maple [A] time = 0.00, size = 29, normalized size = 0.72

$$\frac{(cx^2)^{\frac{3}{2}}(a \ln(bx+a) - bx)}{b^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x^2/(b*x+a), x)

[Out] -(c*x^2)^(3/2)*(a*ln(b*x+a)-b*x)/b^2/x^3

maxima [B] time = 1.48, size = 75, normalized size = 1.88

$$-\frac{(-1)^{\frac{2cx}{b}} ac^{\frac{3}{2}} \log\left(\frac{2cx}{b}\right)}{b^2} - \frac{(-1)^{\frac{2acx}{b}} ac^{\frac{3}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^2} + \frac{\sqrt{cx^2}c}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^2/(b*x+a), x, algorithm="maxima")

[Out] -(-1)^(2*c*x/b)*a*c^(3/2)*log(2*c*x/b)/b^2 - (-1)^(2*a*c*x/b)*a*c^(3/2)*log(-2*a*c*x/(b*abs(b*x + a)))/b^2 + sqrt(c*x^2)*c/b

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{3/2}}{x^2(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(x^2*(a + b*x)), x)

[Out] int((c*x^2)^(3/2)/(x^2*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^2(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)/x**2/(b*x+a), x)

[Out] Integral((c*x**2)**(3/2)/(x**2*(a + b*x)), x)

$$3.864 \quad \int \frac{(cx^2)^{3/2}}{x^3(a+bx)} dx$$

Optimal. Leaf size=23

$$\frac{c\sqrt{cx^2} \log(a+bx)}{bx}$$

[Out] $c \ln(b*x+a) * (c*x^2)^{(1/2)} / b/x$

Rubi [A] time = 0.00, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 31}

$$\frac{c\sqrt{cx^2} \log(a+bx)}{bx}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)} / (x^3*(a + b*x)), x]$

[Out] $(c*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x]) / (b*x)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ $\text{FreeQ}\{a, m, n\}, x$
&& !IntegerQ[m]

Rule 31

$\text{Int}[(a_) + (b_.)*(x_)^{(-1)}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] /;$ $\text{FreeQ}\{a, b\}, x$

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2}}{x^3(a+bx)} dx &= \frac{(c\sqrt{cx^2}) \int \frac{1}{a+bx} dx}{x} \\ &= \frac{c\sqrt{cx^2} \log(a+bx)}{bx} \end{aligned}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 0.96

$$\frac{(cx^2)^{3/2} \log(a+bx)}{bx^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^3*(a + b*x)),x]

[Out] ((c*x^2)^(3/2)*Log[a + b*x])/(b*x^3)

fricas [A] time = 0.46, size = 21, normalized size = 0.91

$$\frac{\sqrt{cx^2} c \log (bx + a)}{bx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^3/(b*x+a),x, algorithm="fricas")

[Out] sqrt(c*x^2)*c*log(b*x + a)/(b*x)

giac [A] time = 1.14, size = 28, normalized size = 1.22

$$c^{\frac{3}{2}} \left(\frac{\log(|bx + a|) \operatorname{sgn}(x)}{b} - \frac{\log(|a|) \operatorname{sgn}(x)}{b} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^3/(b*x+a),x, algorithm="giac")

[Out] c^(3/2)*(log(abs(b*x + a))*sgn(x)/b - log(abs(a))*sgn(x)/b)

maple [A] time = 0.00, size = 21, normalized size = 0.91

$$\frac{(cx^2)^{\frac{3}{2}} \ln(bx + a)}{bx^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x^3/(b*x+a),x)

[Out] (c*x^2)^(3/2)/x^3*ln(b*x+a)/b

maxima [A] time = 1.36, size = 13, normalized size = 0.57

$$\frac{c^{\frac{3}{2}} \log (bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^3/(b*x+a),x, algorithm="maxima")

[Out] $c^{3/2} \log(bx + a)/b$

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{(cx^2)^{3/2}}{x^3(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)/(x^3*(a + b*x)),x)`

[Out] `int((c*x^2)^(3/2)/(x^3*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{3/2}}{x^3(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(3/2)/x**3/(b*x+a),x)`

[Out] `Integral((c*x**2)**(3/2)/(x**3*(a + b*x)), x)`

$$3.865 \quad \int \frac{(cx^2)^{3/2}}{x^4(a+bx)} dx$$

Optimal. Leaf size=44

$$\frac{c\sqrt{cx^2} \log(x)}{ax} - \frac{c\sqrt{cx^2} \log(a+bx)}{ax}$$

[Out] $c*\ln(x)*(c*x^2)^{(1/2)}/a/x - c*\ln(b*x+a)*(c*x^2)^{(1/2)}/a/x$

Rubi [A] time = 0.01, antiderivative size = 44, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {15, 36, 29, 31}

$$\frac{c\sqrt{cx^2} \log(x)}{ax} - \frac{c\sqrt{cx^2} \log(a+bx)}{ax}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(3/2)/(x^4*(a + b*x)), x]

[Out] (c*Sqrt[c*x^2]*Log[x])/(a*x) - (c*Sqrt[c*x^2]*Log[a + b*x])/(a*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 29

Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] :> Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 36

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))), x_Symbol] :> Dist[b/(b*c - a*d), Int[1/(a + b*x), x], x] - Dist[d/(b*c - a*d), Int[1/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2}}{x^4(a+bx)} dx &= \frac{(c\sqrt{cx^2}) \int \frac{1}{x(a+bx)} dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int \frac{1}{x} dx}{ax} - \frac{(bc\sqrt{cx^2}) \int \frac{1}{a+bx} dx}{ax} \\ &= \frac{c\sqrt{cx^2} \log(x)}{ax} - \frac{c\sqrt{cx^2} \log(a+bx)}{ax} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.61

$$\frac{(cx^2)^{3/2} (\log(x) - \log(a+bx))}{ax^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^4*(a + b*x)),x]

[Out] ((c*x^2)^(3/2)*(Log[x] - Log[a + b*x]))/(a*x^3)

fricas [A] time = 0.44, size = 66, normalized size = 1.50

$$\left[\frac{\sqrt{cx^2} c \log\left(\frac{x}{bx+a}\right)}{ax}, \frac{2\sqrt{-c} c \arctan\left(\frac{\sqrt{cx^2}(2bx+a)\sqrt{-c}}{acx}\right)}{a} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^4/(b*x+a),x, algorithm="fricas")

[Out] [sqrt(c*x^2)*c*log(x/(b*x + a))/(a*x), 2*sqrt(-c)*c*arctan(sqrt(c*x^2)*(2*b*x + a)*sqrt(-c)/(a*c*x))/a]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^4/(b*x+a),x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x)::OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.00, size = 26, normalized size = 0.59

$$\frac{(cx^2)^{\frac{3}{2}} (\ln(x) - \ln(bx + a))}{ax^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x^4/(b*x+a),x)

[Out] (c*x^2)^(3/2)*(ln(x)-ln(b*x+a))/a/x^3

maxima [A] time = 1.38, size = 24, normalized size = 0.55

$$-\frac{c^{\frac{3}{2}} \log(bx + a)}{a} + \frac{c^{\frac{3}{2}} \log(x)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^4/(b*x+a),x, algorithm="maxima")

[Out] -c^(3/2)*log(b*x + a)/a + c^(3/2)*log(x)/a

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{3/2}}{x^4 (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(x^4*(a + b*x)),x)

[Out] int((c*x^2)^(3/2)/(x^4*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^4 (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)/x**4/(b*x+a),x)

[Out] Integral((c*x**2)**(3/2)/(x**4*(a + b*x)), x)

$$3.866 \quad \int \frac{(cx^2)^{3/2}}{x^5(a+bx)} dx$$

Optimal. Leaf size=64

$$-\frac{bc\sqrt{cx^2} \log(x)}{a^2x} + \frac{bc\sqrt{cx^2} \log(a+bx)}{a^2x} - \frac{c\sqrt{cx^2}}{ax^2}$$

[Out] $-c*(c*x^2)^{(1/2)}/a/x^2-b*c*\ln(x)*(c*x^2)^{(1/2)}/a^2/x+b*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^2/x$

Rubi [A] time = 0.02, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{bc\sqrt{cx^2} \log(x)}{a^2x} + \frac{bc\sqrt{cx^2} \log(a+bx)}{a^2x} - \frac{c\sqrt{cx^2}}{ax^2}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(3/2)/(x^5*(a + b*x)),x]

[Out] $-((c*\text{Sqrt}[c*x^2])/(a*x^2)) - (b*c*\text{Sqrt}[c*x^2]*\text{Log}[x])/(a^2*x) + (b*c*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(a^2*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{3/2}}{x^5(a+bx)} dx &= \frac{(c\sqrt{cx^2}) \int \frac{1}{x^2(a+bx)} dx}{x} \\
&= \frac{(c\sqrt{cx^2}) \int \left(\frac{1}{ax^2} - \frac{b}{a^2x} + \frac{b^2}{a^2(a+bx)} \right) dx}{x} \\
&= -\frac{c\sqrt{cx^2}}{ax^2} - \frac{bc\sqrt{cx^2} \log(x)}{a^2x} + \frac{bc\sqrt{cx^2} \log(a+bx)}{a^2x}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 34, normalized size = 0.53

$$-\frac{c^2(-bx \log(a+bx) + a + bx \log(x))}{a^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^5*(a + b*x)), x]

[Out] -((c^2*(a + b*x*Log[x] - b*x*Log[a + b*x]))/(a^2*sqrt[c*x^2]))

fricas [A] time = 0.43, size = 33, normalized size = 0.52

$$\frac{\left(bcx \log\left(\frac{bx+a}{x}\right) - ac \right) \sqrt{cx^2}}{a^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^5/(b*x+a), x, algorithm="fricas")

[Out] (b*c*x*log((b*x + a)/x) - a*c)*sqrt(c*x^2)/(a^2*x^2)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^5/(b*x+a), x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
UT:sage2:=int(sage0,x);OUTPUT:Warning, integration of abs or sign assumes
constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 33, normalized size = 0.52

$$\frac{(cx^2)^{\frac{3}{2}}(bx \ln(x) - bx \ln(bx + a) + a)}{a^2x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)/x^5/(b*x+a), x)`

[Out] `-(c*x^2)^(3/2)*(b*x*ln(x)-b*x*ln(b*x+a)+a)/x^4/a^2`

maxima [A] time = 1.36, size = 37, normalized size = 0.58

$$\frac{bc^{\frac{3}{2}} \log(bx + a)}{a^2} - \frac{bc^{\frac{3}{2}} \log(x)}{a^2} - \frac{c^{\frac{3}{2}}}{ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)/x^5/(b*x+a), x, algorithm="maxima")`

[Out] `b*c^(3/2)*log(b*x + a)/a^2 - b*c^(3/2)*log(x)/a^2 - c^(3/2)/(a*x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^5(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)/(x^5*(a + b*x)), x)`

[Out] `int((c*x^2)^(3/2)/(x^5*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^5(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(3/2)/x**5/(b*x+a), x)`

[Out] `Integral((c*x**2)**(3/2)/(x**5*(a + b*x)), x)`

$$3.867 \quad \int \frac{(cx^2)^{3/2}}{x^6(a+bx)} dx$$

Optimal. Leaf size=88

$$\frac{b^2c\sqrt{cx^2} \log(x)}{a^3x} - \frac{b^2c\sqrt{cx^2} \log(a+bx)}{a^3x} + \frac{bc\sqrt{cx^2}}{a^2x^2} - \frac{c\sqrt{cx^2}}{2ax^3}$$

[Out] $-1/2*c*(c*x^2)^{(1/2)}/x^3/a+b*c*(c*x^2)^{(1/2)}/a^2/x^2+b^2*c*\ln(x)*(c*x^2)^{(1/2)}/a^3/x-b^2*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^3/x$

Rubi [A] time = 0.02, antiderivative size = 88, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$\frac{b^2c\sqrt{cx^2} \log(x)}{a^3x} - \frac{b^2c\sqrt{cx^2} \log(a+bx)}{a^3x} + \frac{bc\sqrt{cx^2}}{a^2x^2} - \frac{c\sqrt{cx^2}}{2ax^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}/(x^6*(a + b*x)), x]$

[Out] $-(c*\text{Sqrt}[c*x^2])/(2*a*x^3) + (b*c*\text{Sqrt}[c*x^2])/(a^2*x^2) + (b^2*c*\text{Sqrt}[c*x^2]*\text{Log}[x])/(a^3*x) - (b^2*c*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(a^3*x)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_.)})^{(m_.)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 44

$\text{Int}[((a_) + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{ILtQ}[m, 0] \&\& \text{IntegerQ}[n] \&\& !(\text{IGtQ}[n, 0] \&\& \text{LtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2}}{x^6(a+bx)} dx &= \frac{(c\sqrt{cx^2}) \int \frac{1}{x^3(a+bx)} dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int \left(\frac{1}{ax^3} - \frac{b}{a^2x^2} + \frac{b^2}{a^3x} - \frac{b^3}{a^3(a+bx)} \right) dx}{x} \\ &= -\frac{c\sqrt{cx^2}}{2ax^3} + \frac{bc\sqrt{cx^2}}{a^2x^2} + \frac{b^2c\sqrt{cx^2} \log(x)}{a^3x} - \frac{b^2c\sqrt{cx^2} \log(a+bx)}{a^3x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 53, normalized size = 0.60

$$\frac{(cx^2)^{3/2} (-2b^2x^2 \log(a+bx) - a(a-2bx) + 2b^2x^2 \log(x))}{2a^3x^5}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^6*(a + b*x)),x]

[Out] ((c*x^2)^(3/2)*(-(a*(a - 2*b*x)) + 2*b^2*x^2*Log[x] - 2*b^2*x^2*Log[a + b*x]))/(2*a^3*x^5)

fricas [A] time = 0.44, size = 47, normalized size = 0.53

$$\frac{(2b^2cx^2 \log\left(\frac{x}{bx+a}\right) + 2abcx - a^2c)\sqrt{cx^2}}{2a^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^6/(b*x+a),x, algorithm="fricas")

[Out] 1/2*(2*b^2*c*x^2*log(x/(b*x + a)) + 2*a*b*c*x - a^2*c)*sqrt(c*x^2)/(a^3*x^3)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^6/(b*x+a),x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x)::OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.00, size = 51, normalized size = 0.58

$$\frac{(cx^2)^{\frac{3}{2}}(2b^2x^2 \ln(x) - 2b^2x^2 \ln(bx + a) + 2abx - a^2)}{2a^3x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x^6/(b*x+a), x)

[Out] 1/2*(c*x^2)^(3/2)*(2*b^2*x^2*ln(x)-2*b^2*x^2*ln(b*x+a)+2*a*b*x-a^2)/x^5/a^3

maxima [A] time = 1.45, size = 52, normalized size = 0.59

$$-\frac{b^2c^{\frac{3}{2}} \log(bx + a)}{a^3} + \frac{b^2c^{\frac{3}{2}} \log(x)}{a^3} + \frac{2bc^{\frac{3}{2}}x - ac^{\frac{3}{2}}}{2a^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^6/(b*x+a), x, algorithm="maxima")

[Out] -b^2*c^(3/2)*log(b*x + a)/a^3 + b^2*c^(3/2)*log(x)/a^3 + 1/2*(2*b*c^(3/2)*x - a*c^(3/2))/(a^2*x^2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^6(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(x^6*(a + b*x)), x)

[Out] int((c*x^2)^(3/2)/(x^6*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^6(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)/x**6/(b*x+a), x)

[Out] Integral((c*x**2)**(3/2)/(x**6*(a + b*x)), x)

$$3.868 \quad \int \frac{(cx^2)^{3/2}}{x^7(a+bx)} dx$$

Optimal. Leaf size=112

$$-\frac{b^3c\sqrt{cx^2} \log(x)}{a^4x} + \frac{b^3c\sqrt{cx^2} \log(a+bx)}{a^4x} - \frac{b^2c\sqrt{cx^2}}{a^3x^2} + \frac{bc\sqrt{cx^2}}{2a^2x^3} - \frac{c\sqrt{cx^2}}{3ax^4}$$

[Out] $-1/3*c*(c*x^2)^{(1/2)}/a/x^4+1/2*b*c*(c*x^2)^{(1/2)}/a^2/x^3-b^2*c*(c*x^2)^{(1/2)}/a^3/x^2-b^3*c*\ln(x)*(c*x^2)^{(1/2)}/a^4/x+b^3*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^4/x$

Rubi [A] time = 0.03, antiderivative size = 112, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{b^2c\sqrt{cx^2}}{a^3x^2} - \frac{b^3c\sqrt{cx^2} \log(x)}{a^4x} + \frac{b^3c\sqrt{cx^2} \log(a+bx)}{a^4x} + \frac{bc\sqrt{cx^2}}{2a^2x^3} - \frac{c\sqrt{cx^2}}{3ax^4}$$

Antiderivative was successfully verified.

[In] `Int[(c*x^2)^(3/2)/(x^7*(a + b*x)),x]`

[Out] $-(c*\text{Sqrt}[c*x^2])/(3*a*x^4) + (b*c*\text{Sqrt}[c*x^2])/(2*a^2*x^3) - (b^2*c*\text{Sqrt}[c*x^2])/(a^3*x^2) - (b^3*c*\text{Sqrt}[c*x^2]*\text{Log}[x])/(a^4*x) + (b^3*c*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(a^4*x)$

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rule 44

`Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])`

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{3/2}}{x^7(a+bx)} dx &= \frac{(c\sqrt{cx^2})}{x} \int \frac{1}{x^4(a+bx)} dx \\
&= \frac{(c\sqrt{cx^2})}{x} \int \left(\frac{1}{ax^4} - \frac{b}{a^2x^3} + \frac{b^2}{a^3x^2} - \frac{b^3}{a^4x} + \frac{b^4}{a^4(a+bx)} \right) dx \\
&= -\frac{c\sqrt{cx^2}}{3ax^4} + \frac{bc\sqrt{cx^2}}{2a^2x^3} - \frac{b^2c\sqrt{cx^2}}{a^3x^2} - \frac{b^3c\sqrt{cx^2} \log(x)}{a^4x} + \frac{b^3c\sqrt{cx^2} \log(a+bx)}{a^4x}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 65, normalized size = 0.58

$$-\frac{(cx^2)^{3/2} \left(a(2a^2 - 3abx + 6b^2x^2) - 6b^3x^3 \log(a+bx) + 6b^3x^3 \log(x) \right)}{6a^4x^6}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^7*(a + b*x)), x]

[Out] -1/6*((c*x^2)^(3/2)*(a*(2*a^2 - 3*a*b*x + 6*b^2*x^2) + 6*b^3*x^3*Log[x] - 6*b^3*x^3*Log[a + b*x]))/(a^4*x^6)

fricas [A] time = 0.42, size = 59, normalized size = 0.53

$$\frac{\left(6b^3cx^3 \log\left(\frac{bx+a}{x}\right) - 6ab^2cx^2 + 3a^2bcx - 2a^3c \right) \sqrt{cx^2}}{6a^4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^7/(b*x+a), x, algorithm="fricas")

[Out] 1/6*(6*b^3*c*x^3*log((b*x + a)/x) - 6*a*b^2*c*x^2 + 3*a^2*b*c*x - 2*a^3*c)*sqrt(c*x^2)/(a^4*x^4)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^7/(b*x+a), x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INPUT:sage2:=int(sage0,x);;OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 62, normalized size = 0.55

$$-\frac{(cx^2)^{\frac{3}{2}}(6b^3x^3\ln(x) - 6b^3x^3\ln(bx+a) + 6ab^2x^2 - 3a^2bx + 2a^3)}{6a^4x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x^7/(b*x+a), x)

[Out] -1/6*(c*x^2)^(3/2)*(6*b^3*ln(x)*x^3-6*b^3*ln(b*x+a)*x^3+6*a*b^2*x^2-3*a^2*b*x+2*a^3)/x^6/a^4

maxima [A] time = 1.45, size = 66, normalized size = 0.59

$$\frac{b^3c^{\frac{3}{2}}\log(bx+a)}{a^4} - \frac{b^3c^{\frac{3}{2}}\log(x)}{a^4} - \frac{6b^2c^{\frac{3}{2}}x^2 - 3abc^{\frac{3}{2}}x + 2a^2c^{\frac{3}{2}}}{6a^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^7/(b*x+a), x, algorithm="maxima")

[Out] b^3*c^(3/2)*log(b*x + a)/a^4 - b^3*c^(3/2)*log(x)/a^4 - 1/6*(6*b^2*c^(3/2)*x^2 - 3*a*b*c^(3/2)*x + 2*a^2*c^(3/2))/(a^3*x^3)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^7(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(x^7*(a + b*x)), x)

[Out] int((c*x^2)^(3/2)/(x^7*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^7(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)/x**7/(b*x+a), x)

[Out] Integral((c*x**2)**(3/2)/(x**7*(a + b*x)), x)

$$3.869 \quad \int \frac{(cx^2)^{5/2}}{a+bx} dx$$

Optimal. Leaf size=142

$$-\frac{a^5 c^2 \sqrt{cx^2} \log(a+bx)}{b^6 x} + \frac{a^4 c^2 \sqrt{cx^2}}{b^5} - \frac{a^3 c^2 x \sqrt{cx^2}}{2b^4} + \frac{a^2 c^2 x^2 \sqrt{cx^2}}{3b^3} - \frac{a c^2 x^3 \sqrt{cx^2}}{4b^2} + \frac{c^2 x^4 \sqrt{cx^2}}{5b}$$

[Out] $a^4 c^2 (c x^2)^{(1/2)} / b^5 - 1/2 a^3 c^2 x (c x^2)^{(1/2)} / b^4 + 1/3 a^2 c^2 x^2 (c x^2)^{(1/2)} / b^3 - 1/4 a c^2 x^3 (c x^2)^{(1/2)} / b^2 + 1/5 c^2 x^4 (c x^2)^{(1/2)} / b - a^5 c^2 \ln(b x + a) (c x^2)^{(1/2)} / b^6 / x$

Rubi [A] time = 0.04, antiderivative size = 142, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$\frac{a^4 c^2 \sqrt{cx^2}}{b^5} - \frac{a^3 c^2 x \sqrt{cx^2}}{2b^4} + \frac{a^2 c^2 x^2 \sqrt{cx^2}}{3b^3} - \frac{a^5 c^2 \sqrt{cx^2} \log(a+bx)}{b^6 x} - \frac{a c^2 x^3 \sqrt{cx^2}}{4b^2} + \frac{c^2 x^4 \sqrt{cx^2}}{5b}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(5/2)/(a + b*x), x]

[Out] $(a^4 c^2 \sqrt{c x^2}) / b^5 - (a^3 c^2 x \sqrt{c x^2}) / (2 b^4) + (a^2 c^2 x^2 \sqrt{c x^2}) / (3 b^3) - (a c^2 x^3 \sqrt{c x^2}) / (4 b^2) + (c^2 x^4 \sqrt{c x^2}) / (5 b) - (a^5 c^2 \sqrt{c x^2} \text{Log}[a + b x]) / (b^6 x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2}}{a+bx} dx &= \frac{(c^2\sqrt{cx^2}) \int \frac{x^5}{a+bx} dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int \left(\frac{a^4}{b^5} - \frac{a^3x}{b^4} + \frac{a^2x^2}{b^3} - \frac{ax^3}{b^2} + \frac{x^4}{b} - \frac{a^5}{b^5(a+bx)} \right) dx}{x} \\ &= \frac{a^4c^2\sqrt{cx^2}}{b^5} - \frac{a^3c^2x\sqrt{cx^2}}{2b^4} + \frac{a^2c^2x^2\sqrt{cx^2}}{3b^3} - \frac{ac^2x^3\sqrt{cx^2}}{4b^2} + \frac{c^2x^4\sqrt{cx^2}}{5b} - \frac{a^5c^2\sqrt{cx^2} \log(a+bx)}{b^6x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 76, normalized size = 0.54

$$\frac{c^3x \left(bx(60a^4 - 30a^3bx + 20a^2b^2x^2 - 15ab^3x^3 + 12b^4x^4) - 60a^5 \log(a+bx) \right)}{60b^6\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)/(a + b*x), x]

[Out] (c^3*x*(b*x*(60*a^4 - 30*a^3*b*x + 20*a^2*b^2*x^2 - 15*a*b^3*x^3 + 12*b^4*x^4) - 60*a^5*Log[a + b*x]))/(60*b^6*Sqrt[c*x^2])

fricas [A] time = 0.41, size = 91, normalized size = 0.64

$$\frac{(12b^5c^2x^5 - 15ab^4c^2x^4 + 20a^2b^3c^2x^3 - 30a^3b^2c^2x^2 + 60a^4bc^2x - 60a^5c^2 \log(bx+a))\sqrt{cx^2}}{60b^6x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/(b*x+a), x, algorithm="fricas")

[Out] 1/60*(12*b^5*c^2*x^5 - 15*a*b^4*c^2*x^4 + 20*a^2*b^3*c^2*x^3 - 30*a^3*b^2*c^2*x^2 + 60*a^4*b*c^2*x - 60*a^5*c^2*log(b*x + a))*sqrt(c*x^2)/(b^6*x)

giac [A] time = 1.18, size = 116, normalized size = 0.82

$$-\frac{1}{60} \left(\frac{60a^5c^2 \log(|bx+a|) \operatorname{sgn}(x)}{b^6} - \frac{60a^5c^2 \log(|a|) \operatorname{sgn}(x)}{b^6} - \frac{12b^4c^2x^5 \operatorname{sgn}(x) - 15ab^3c^2x^4 \operatorname{sgn}(x) + 20a^2b^2c^2x^3}{b^5} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/(b*x+a), x, algorithm="giac")

[Out] $-1/60*(60*a^5*c^2*\log(\text{abs}(b*x + a))*\text{sgn}(x)/b^6 - 60*a^5*c^2*\log(\text{abs}(a))*\text{sgn}(x)/b^6 - (12*b^4*c^2*x^5*\text{sgn}(x) - 15*a*b^3*c^2*x^4*\text{sgn}(x) + 20*a^2*b^2*c^2*x^3*\text{sgn}(x) - 30*a^3*b*c^2*x^2*\text{sgn}(x) + 60*a^4*c^2*x*\text{sgn}(x))/b^5)*\text{sqrt}(c)$

maple [A] time = 0.01, size = 74, normalized size = 0.52

$$\frac{(cx^2)^{\frac{5}{2}}(-12b^5x^5 + 15ab^4x^4 - 20a^2b^3x^3 + 30a^3b^2x^2 + 60a^5 \ln(bx + a) - 60a^4bx)}{60b^6x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)/(b*x+a), x)`

[Out] $-1/60*(c*x^2)^{(5/2)}*(-12*b^5*x^5+15*a*b^4*x^4-20*a^2*b^3*x^3+30*a^3*b^2*x^2+60*a^5*\ln(b*x+a)-60*a^4*b*x)/x^5/b^6$

maxima [A] time = 1.58, size = 146, normalized size = 1.03

$$\frac{(-1)^{\frac{2cx}{b}} a^5 c^{\frac{5}{2}} \log\left(\frac{2cx}{b}\right) - (-1)^{\frac{2acx}{b}} a^5 c^{\frac{5}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right) - \frac{(cx^2)^{\frac{3}{2}} acx}{4b^2} - \frac{\sqrt{cx^2} a^3 c^2 x}{2b^4} + \frac{(cx^2)^{\frac{5}{2}}}{5b} + \frac{(cx^2)^{\frac{3}{2}} a^2 c}{3b^3} + \frac{\sqrt{cx^2} a^4 c^2}{b^5}}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(5/2)/(b*x+a), x, algorithm="maxima")`

[Out] $-(-1)^{(2*c*x/b)}*a^5*c^{(5/2)}*\log(2*c*x/b)/b^6 - (-1)^{(2*a*c*x/b)}*a^5*c^{(5/2)}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/b^6 - 1/4*(c*x^2)^{(3/2)}*a*c*x/b^2 - 1/2*\text{sqrt}(c*x^2)*a^3*c^2*x/b^4 + 1/5*(c*x^2)^{(5/2)}/b + 1/3*(c*x^2)^{(3/2)}*a^2*c/b^3 + \text{sqrt}(c*x^2)*a^4*c^2/b^5$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{5/2}}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)/(a + b*x), x)`

[Out] `int((c*x^2)^(5/2)/(a + b*x), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}}}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((c*x**2)**(5/2)/(b*x+a),x)
```

```
[Out] Integral((c*x**2)**(5/2)/(a + b*x), x)
```

$$3.870 \quad \int \frac{(cx^2)^{5/2}}{x(a+bx)} dx$$

Optimal. Leaf size=117

$$\frac{a^4 c^2 \sqrt{cx^2} \log(a+bx)}{b^5 x} - \frac{a^3 c^2 \sqrt{cx^2}}{b^4} + \frac{a^2 c^2 x \sqrt{cx^2}}{2b^3} - \frac{ac^2 x^2 \sqrt{cx^2}}{3b^2} + \frac{c^2 x^3 \sqrt{cx^2}}{4b}$$

[Out] $-a^3 c^2 (cx^2)^{(1/2)} / b^4 + 1/2 a^2 c^2 x (cx^2)^{(1/2)} / b^3 - 1/3 a c^2 x^2 (cx^2)^{(1/2)} / b^2 + 1/4 c^2 x^3 (cx^2)^{(1/2)} / b + a^4 c^2 \ln(bx+a) (cx^2)^{(1/2)} / b^5 / x$

Rubi [A] time = 0.05, antiderivative size = 117, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^3 c^2 \sqrt{cx^2}}{b^4} + \frac{a^2 c^2 x \sqrt{cx^2}}{2b^3} + \frac{a^4 c^2 \sqrt{cx^2} \log(a+bx)}{b^5 x} - \frac{ac^2 x^2 \sqrt{cx^2}}{3b^2} + \frac{c^2 x^3 \sqrt{cx^2}}{4b}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(5/2)/(x*(a + b*x)), x]

[Out] $-((a^3 c^2 \sqrt{cx^2}) / b^4) + (a^2 c^2 x \sqrt{cx^2}) / (2 b^3) - (a c^2 x^2 \sqrt{cx^2}) / (3 b^2) + (c^2 x^3 \sqrt{cx^2}) / (4 b) + (a^4 c^2 \sqrt{cx^2} \text{Log}[a + b x]) / (b^5 x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{5/2}}{x(a+bx)} dx &= \frac{(c^2\sqrt{cx^2}) \int \frac{x^4}{a+bx} dx}{x} \\
&= \frac{(c^2\sqrt{cx^2}) \int \left(-\frac{a^3}{b^4} + \frac{a^2x}{b^3} - \frac{ax^2}{b^2} + \frac{x^3}{b} + \frac{a^4}{b^4(a+bx)}\right) dx}{x} \\
&= -\frac{a^3c^2\sqrt{cx^2}}{b^4} + \frac{a^2c^2x\sqrt{cx^2}}{2b^3} - \frac{ac^2x^2\sqrt{cx^2}}{3b^2} + \frac{c^2x^3\sqrt{cx^2}}{4b} + \frac{a^4c^2\sqrt{cx^2} \log(a+bx)}{b^5x}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 65, normalized size = 0.56

$$\frac{c (cx^2)^{3/2} (12a^4 \log(a+bx) + bx(-12a^3 + 6a^2bx - 4ab^2x^2 + 3b^3x^3))}{12b^5x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)/(x*(a + b*x)),x]

[Out] (c*(c*x^2)^(3/2)*(b*x*(-12*a^3 + 6*a^2*b*x - 4*a*b^2*x^2 + 3*b^3*x^3) + 12*a^4*Log[a + b*x]))/(12*b^5*x^3)

fricas [A] time = 0.42, size = 77, normalized size = 0.66

$$\frac{(3b^4c^2x^4 - 4ab^3c^2x^3 + 6a^2b^2c^2x^2 - 12a^3bc^2x + 12a^4c^2 \log(bx+a))\sqrt{cx^2}}{12b^5x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x/(b*x+a),x, algorithm="fricas")

[Out] 1/12*(3*b^4*c^2*x^4 - 4*a*b^3*c^2*x^3 + 6*a^2*b^2*c^2*x^2 - 12*a^3*b*c^2*x + 12*a^4*c^2*log(b*x + a))*sqrt(c*x^2)/(b^5*x)

giac [A] time = 1.01, size = 99, normalized size = 0.85

$$\frac{1}{12} \left(\frac{12a^4c^2 \log(|bx+a|) \operatorname{sgn}(x)}{b^5} - \frac{12a^4c^2 \log(|a|) \operatorname{sgn}(x)}{b^5} + \frac{3b^3c^2x^4 \operatorname{sgn}(x) - 4ab^2c^2x^3 \operatorname{sgn}(x) + 6a^2bc^2x^2 \operatorname{sgn}(x)}{b^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x/(b*x+a),x, algorithm="giac")

[Out] $1/12*(12*a^4*c^2*\log(\text{abs}(b*x + a))*\text{sgn}(x)/b^5 - 12*a^4*c^2*\log(\text{abs}(a))*\text{sgn}(x)/b^5 + (3*b^3*c^2*x^4*\text{sgn}(x) - 4*a*b^2*c^2*x^3*\text{sgn}(x) + 6*a^2*b*c^2*x^2*\text{sgn}(x) - 12*a^3*c^2*x*\text{sgn}(x))/b^4)*\text{sqrt}(c)$

maple [A] time = 0.01, size = 63, normalized size = 0.54

$$\frac{(cx^2)^{\frac{5}{2}} (3b^4x^4 - 4ab^3x^3 + 6a^2b^2x^2 + 12a^4 \ln(bx + a) - 12a^3bx)}{12b^5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)/x/(b*x+a), x)`

[Out] $1/12*(c*x^2)^{(5/2)}*(3*b^4*x^4-4*a*b^3*x^3+6*a^2*b^2*x^2+12*a^4*\ln(b*x+a)-12*a^3*b*x)/b^5/x^5$

maxima [A] time = 1.60, size = 130, normalized size = 1.11

$$\frac{(-1)^{\frac{2cx}{b}} a^4 c^{\frac{5}{2}} \log\left(\frac{2cx}{b}\right)}{b^5} + \frac{(-1)^{\frac{2acx}{b}} a^4 c^{\frac{5}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^5} + \frac{(cx^2)^{\frac{3}{2}} cx}{4b} + \frac{\sqrt{cx^2} a^2 c^2 x}{2b^3} - \frac{(cx^2)^{\frac{3}{2}} ac}{3b^2} - \frac{\sqrt{cx^2} a^3 c^2}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(5/2)/x/(b*x+a), x, algorithm="maxima")`

[Out] $(-1)^{(2*c*x/b)}*a^4*c^{(5/2)}*\log(2*c*x/b)/b^5 + (-1)^{(2*a*c*x/b)}*a^4*c^{(5/2)}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/b^5 + 1/4*(c*x^2)^{(3/2)}*c*x/b + 1/2*\text{sqrt}(c*x^2)*a^2*c^2*x/b^3 - 1/3*(c*x^2)^{(3/2)}*a*c/b^2 - \text{sqrt}(c*x^2)*a^3*c^2/b^4$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{5/2}}{x(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)/(x*(a + b*x)), x)`

[Out] `int((c*x^2)^(5/2)/(x*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}}}{x(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((c*x**2)**(5/2)/x/(b*x+a),x)
```

```
[Out] Integral((c*x**2)**(5/2)/(x*(a + b*x)), x)
```

$$3.871 \quad \int \frac{(cx^2)^{5/2}}{x^2(a+bx)} dx$$

Optimal. Leaf size=92

$$-\frac{a^3c^2\sqrt{cx^2} \log(a+bx)}{b^4x} + \frac{a^2c^2\sqrt{cx^2}}{b^3} - \frac{ac^2x\sqrt{cx^2}}{2b^2} + \frac{c^2x^2\sqrt{cx^2}}{3b}$$

[Out] $a^2c^2(c*x^2)^{(1/2)}/b^3-1/2*a*c^2*x*(c*x^2)^{(1/2)}/b^2+1/3*c^2*x^2*(c*x^2)^{(1/2)}/b-a^3*c^2*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^4/x$

Rubi [A] time = 0.03, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2c^2\sqrt{cx^2}}{b^3} - \frac{a^3c^2\sqrt{cx^2} \log(a+bx)}{b^4x} - \frac{ac^2x\sqrt{cx^2}}{2b^2} + \frac{c^2x^2\sqrt{cx^2}}{3b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(5/2)}/(x^2*(a + b*x)), x]$

[Out] $(a^2*c^2*\text{Sqrt}[c*x^2])/b^3 - (a*c^2*x*\text{Sqrt}[c*x^2])/(2*b^2) + (c^2*x^2*\text{Sqrt}[c*x^2])/(3*b) - (a^3*c^2*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^4*x)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[((a_.) + (b_.)*(x_))^{(m_.)}*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{5/2}}{x^2(a+bx)} dx &= \frac{(c^2\sqrt{cx^2}) \int \frac{x^3}{a+bx} dx}{x} \\
&= \frac{(c^2\sqrt{cx^2}) \int \left(\frac{a^2}{b^3} - \frac{ax}{b^2} + \frac{x^2}{b} - \frac{a^3}{b^3(a+bx)}\right) dx}{x} \\
&= \frac{a^2c^2\sqrt{cx^2}}{b^3} - \frac{ac^2x\sqrt{cx^2}}{2b^2} + \frac{c^2x^2\sqrt{cx^2}}{3b} - \frac{a^3c^2\sqrt{cx^2} \log(a+bx)}{b^4x}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 54, normalized size = 0.59

$$\frac{c(cx^2)^{3/2} (bx(6a^2 - 3abx + 2b^2x^2) - 6a^3 \log(a+bx))}{6b^4x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)/(x^2*(a + b*x)), x]

[Out] (c*(c*x^2)^(3/2)*(b*x*(6*a^2 - 3*a*b*x + 2*b^2*x^2) - 6*a^3*Log[a + b*x]))/(6*b^4*x^3)

fricas [A] time = 0.43, size = 63, normalized size = 0.68

$$\frac{(2b^3c^2x^3 - 3ab^2c^2x^2 + 6a^2bc^2x - 6a^3c^2 \log(bx+a))\sqrt{cx^2}}{6b^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^2/(b*x+a), x, algorithm="fricas")

[Out] 1/6*(2*b^3*c^2*x^3 - 3*a*b^2*c^2*x^2 + 6*a^2*b*c^2*x - 6*a^3*c^2*log(b*x + a))*sqrt(c*x^2)/(b^4*x)

giac [A] time = 0.96, size = 84, normalized size = 0.91

$$-\frac{1}{6} \left(\frac{6a^3c^2 \log(|bx+a|) \operatorname{sgn}(x)}{b^4} - \frac{6a^3c^2 \log(|a|) \operatorname{sgn}(x)}{b^4} - \frac{2b^2c^2x^3 \operatorname{sgn}(x) - 3abc^2x^2 \operatorname{sgn}(x) + 6a^2c^2x \operatorname{sgn}(x)}{b^3} \right) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^2/(b*x+a), x, algorithm="giac")

[Out] $-1/6*(6*a^3*c^2*\log(\text{abs}(b*x + a))*\text{sgn}(x)/b^4 - 6*a^3*c^2*\log(\text{abs}(a))*\text{sgn}(x)/b^4 - (2*b^2*c^2*x^3*\text{sgn}(x) - 3*a*b*c^2*x^2*\text{sgn}(x) + 6*a^2*c^2*x*\text{sgn}(x))/b^3)*\text{sqrt}(c)$

maple [A] time = 0.00, size = 52, normalized size = 0.57

$$-\frac{(cx^2)^{\frac{5}{2}}(-2b^3x^3 + 3ab^2x^2 + 6a^3\ln(bx + a) - 6a^2bx)}{6b^4x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((c*x^2)^{(5/2)}/x^2/(b*x+a), x)$

[Out] $-1/6*(c*x^2)^{(5/2)}*(-2*b^3*x^3+3*a*b^2*x^2+6*a^3*\ln(b*x+a)-6*a^2*b*x)/x^5/b^4$

maxima [A] time = 1.56, size = 114, normalized size = 1.24

$$-\frac{(-1)^{\frac{2cx}{b}} a^3 c^{\frac{5}{2}} \log\left(\frac{2cx}{b}\right)}{b^4} - \frac{(-1)^{\frac{2acx}{b}} a^3 c^{\frac{5}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^4} - \frac{\sqrt{cx^2} ac^2 x}{2b^2} + \frac{(cx^2)^{\frac{3}{2}} c}{3b} + \frac{\sqrt{cx^2} a^2 c^2}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((c*x^2)^{(5/2)}/x^2/(b*x+a), x, \text{algorithm}="maxima")$

[Out] $-(-1)^{(2*c*x/b)}*a^3*c^{(5/2)}*\log(2*c*x/b)/b^4 - (-1)^{(2*a*c*x/b)}*a^3*c^{(5/2)}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/b^4 - 1/2*\text{sqrt}(c*x^2)*a*c^2*x/b^2 + 1/3*(c*x^2)^{(3/2)}*c/b + \text{sqrt}(c*x^2)*a^2*c^2/b^3$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{5/2}}{x^2(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((c*x^2)^{(5/2)}/(x^2*(a + b*x)), x)$

[Out] $\text{int}((c*x^2)^{(5/2)}/(x^2*(a + b*x)), x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}}}{x^2(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((c*x**2)**(5/2)/x**2/(b*x+a),x)
```

```
[Out] Integral((c*x**2)**(5/2)/(x**2*(a + b*x)), x)
```

$$3.872 \quad \int \frac{(cx^2)^{5/2}}{x^3(a+bx)} dx$$

Optimal. Leaf size=67

$$\frac{a^2c^2\sqrt{cx^2} \log(a+bx)}{b^3x} - \frac{ac^2\sqrt{cx^2}}{b^2} + \frac{c^2x\sqrt{cx^2}}{2b}$$

[Out] $-a*c^2*(c*x^2)^{(1/2)}/b^2+1/2*c^2*x*(c*x^2)^{(1/2)}/b+a^2*c^2*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^3/x$

Rubi [A] time = 0.02, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2c^2\sqrt{cx^2} \log(a+bx)}{b^3x} - \frac{ac^2\sqrt{cx^2}}{b^2} + \frac{c^2x\sqrt{cx^2}}{2b}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(5/2)/(x^3*(a + b*x)), x]

[Out] $-((a*c^2*\text{Sqrt}[c*x^2])/b^2) + (c^2*x*\text{Sqrt}[c*x^2])/(2*b) + (a^2*c^2*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^3*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2}}{x^3(a+bx)} dx &= \frac{(c^2\sqrt{cx^2})}{x} \int \frac{x^2}{a+bx} dx \\ &= \frac{(c^2\sqrt{cx^2})}{x} \int \left(-\frac{a}{b^2} + \frac{x}{b} + \frac{a^2}{b^2(a+bx)}\right) dx \\ &= -\frac{ac^2\sqrt{cx^2}}{b^2} + \frac{c^2x\sqrt{cx^2}}{2b} + \frac{a^2c^2\sqrt{cx^2} \log(a+bx)}{b^3x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 42, normalized size = 0.63

$$\frac{c^3x(2a^2 \log(a+bx) + bx(bx-2a))}{2b^3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)/(x^3*(a + b*x)), x]

[Out] (c^3*x*(b*x*(-2*a + b*x) + 2*a^2*Log[a + b*x]))/(2*b^3*Sqrt[c*x^2])

fricas [A] time = 0.43, size = 48, normalized size = 0.72

$$\frac{(b^2c^2x^2 - 2abc^2x + 2a^2c^2 \log(bx+a))\sqrt{cx^2}}{2b^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^3/(b*x+a), x, algorithm="fricas")

[Out] 1/2*(b^2*c^2*x^2 - 2*a*b*c^2*x + 2*a^2*c^2*log(b*x + a))*sqrt(c*x^2)/(b^3*x)

giac [A] time = 1.13, size = 66, normalized size = 0.99

$$\frac{1}{2} \left(\frac{2a^2c^2 \log(|bx+a|) \operatorname{sgn}(x)}{b^3} - \frac{2a^2c^2 \log(|a|) \operatorname{sgn}(x)}{b^3} + \frac{bc^2x^2 \operatorname{sgn}(x) - 2ac^2x \operatorname{sgn}(x)}{b^2} \right) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^3/(b*x+a), x, algorithm="giac")

[Out] 1/2*(2*a^2*c^2*log(abs(b*x + a))*sgn(x)/b^3 - 2*a^2*c^2*log(abs(a))*sgn(x)/b^3 + (b*c^2*x^2*sgn(x) - 2*a*c^2*x*sgn(x))/b^2)*sqrt(c)

maple [A] time = 0.01, size = 40, normalized size = 0.60

$$\frac{(cx^2)^{\frac{5}{2}}(b^2x^2 + 2a^2 \ln(bx + a) - 2abx)}{2b^3x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)/x^3/(b*x+a), x)

[Out] 1/2*(c*x^2)^(5/2)*(b^2*x^2+2*a^2*ln(b*x+a)-2*a*b*x)/x^5/b^3

maxima [A] time = 1.50, size = 97, normalized size = 1.45

$$\frac{(-1)^{\frac{2cx}{b}} a^2 c^{\frac{5}{2}} \log\left(\frac{2cx}{b}\right)}{b^3} + \frac{(-1)^{\frac{2acx}{b}} a^2 c^{\frac{5}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^3} + \frac{\sqrt{cx^2} c^2 x}{2b} - \frac{\sqrt{cx^2} ac^2}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^3/(b*x+a), x, algorithm="maxima")

[Out] (-1)^(2*c*x/b)*a^2*c^(5/2)*log(2*c*x/b)/b^3 + (-1)^(2*a*c*x/b)*a^2*c^(5/2)*log(-2*a*c*x/(b*abs(b*x + a)))/b^3 + 1/2*sqrt(c*x^2)*c^2*x/b - sqrt(c*x^2)*a*c^2/b^2

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{5/2}}{x^3 (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)/(x^3*(a + b*x)), x)

[Out] int((c*x^2)^(5/2)/(x^3*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}}}{x^3 (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)/x**3/(b*x+a), x)

[Out] Integral((c*x**2)**(5/2)/(x**3*(a + b*x)), x)

$$3.873 \quad \int \frac{(cx^2)^{5/2}}{x^4(a+bx)} dx$$

Optimal. Leaf size=44

$$\frac{c^2\sqrt{cx^2}}{b} - \frac{ac^2\sqrt{cx^2} \log(a+bx)}{b^2x}$$

[Out] $c^2*(c*x^2)^{(1/2)}/b-a*c^2*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^2/x$

Rubi [A] time = 0.01, antiderivative size = 44, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{c^2\sqrt{cx^2}}{b} - \frac{ac^2\sqrt{cx^2} \log(a+bx)}{b^2x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(5/2)}/(x^4*(a+b*x)),x]$

[Out] $(c^2*\text{Sqrt}[c*x^2])/b - (a*c^2*\text{Sqrt}[c*x^2]*\text{Log}[a+b*x])/(b^2*x)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ $\text{FreeQ}\{a, m, n, x\}$ && $!\text{IntegerQ}[m]$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a+b*x)^m*(c+d*x)^n, x], x] /;$ $\text{FreeQ}\{a, b, c, d, n, x\}$ && $\text{NeQ}[b*c - a*d, 0]$ && $\text{IGtQ}[m, 0]$ && $(!\text{IntegerQ}[n] \parallel (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0]) \parallel \text{LtQ}[9*m + 5*(n + 1), 0] \parallel \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2}}{x^4(a+bx)} dx &= \frac{(c^2\sqrt{cx^2}) \int \frac{x}{a+bx} dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int \left(\frac{1}{b} - \frac{a}{b(a+bx)}\right) dx}{x} \\ &= \frac{c^2\sqrt{cx^2}}{b} - \frac{ac^2\sqrt{cx^2} \log(a+bx)}{b^2x} \end{aligned}$$

Mathematica [A] time = 0.00, size = 30, normalized size = 0.68

$$\frac{c^3x(bx - a \log(a + bx))}{b^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)/(x^4*(a + b*x)), x]

[Out] (c^3*x*(b*x - a*Log[a + b*x]))/(b^2*Sqrt[c*x^2])

fricas [A] time = 0.41, size = 33, normalized size = 0.75

$$\frac{(bc^2x - ac^2 \log(bx + a))\sqrt{cx^2}}{b^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^4/(b*x+a), x, algorithm="fricas")

[Out] (b*c^2*x - a*c^2*log(b*x + a))*sqrt(c*x^2)/(b^2*x)

giac [A] time = 1.04, size = 46, normalized size = 1.05

$$\left(\frac{c^2x\operatorname{sgn}(x)}{b} - \frac{ac^2 \log(|bx + a|) \operatorname{sgn}(x)}{b^2} + \frac{ac^2 \log(|a|) \operatorname{sgn}(x)}{b^2} \right) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^4/(b*x+a), x, algorithm="giac")

[Out] (c^2*x*sgn(x)/b - a*c^2*log(abs(b*x + a))*sgn(x)/b^2 + a*c^2*log(abs(a))*sgn(x)/b^2)*sqrt(c)

maple [A] time = 0.00, size = 29, normalized size = 0.66

$$-\frac{(cx^2)^{\frac{5}{2}}(a \ln(bx+a) - bx)}{b^2x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)/x^4/(b*x+a), x)

[Out] -(c*x^2)^(5/2)*(a*ln(b*x+a)-b*x)/x^5/b^2

maxima [A] time = 1.51, size = 77, normalized size = 1.75

$$-\frac{(-1)^{\frac{2cx}{b}} ac^{\frac{5}{2}} \log\left(\frac{2cx}{b}\right)}{b^2} - \frac{(-1)^{\frac{2acx}{b}} ac^{\frac{5}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^2} + \frac{\sqrt{cx^2} c^2}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^4/(b*x+a), x, algorithm="maxima")

[Out] -(-1)^(2*c*x/b)*a*c^(5/2)*log(2*c*x/b)/b^2 - (-1)^(2*a*c*x/b)*a*c^(5/2)*log(-2*a*c*x/(b*abs(b*x + a)))/b^2 + sqrt(c*x^2)*c^2/b

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{\frac{5}{2}}}{x^4(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)/(x^4*(a + b*x)), x)

[Out] int((c*x^2)^(5/2)/(x^4*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}}}{x^4(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)/x**4/(b*x+a), x)

[Out] Integral((c*x**2)**(5/2)/(x**4*(a + b*x)), x)

$$3.874 \quad \int \frac{(cx^2)^{5/2}}{x^5(a+bx)} dx$$

Optimal. Leaf size=25

$$\frac{c^2\sqrt{cx^2} \log(a+bx)}{bx}$$

[Out] $c^2 \ln(b*x+a) * (c*x^2)^{(1/2)} / b/x$

Rubi [A] time = 0.00, antiderivative size = 25, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 31}

$$\frac{c^2\sqrt{cx^2} \log(a+bx)}{bx}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(5/2)} / (x^5*(a + b*x)), x]$

[Out] $(c^2*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x]) / (b*x)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 31

$\text{Int}[(a_. + (b_.)*(x_)^{(-1)}), x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] /;$ FreeQ[{a, b}, x]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2}}{x^5(a+bx)} dx &= \frac{(c^2\sqrt{cx^2}) \int \frac{1}{a+bx} dx}{x} \\ &= \frac{c^2\sqrt{cx^2} \log(a+bx)}{bx} \end{aligned}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 0.88

$$\frac{(cx^2)^{5/2} \log(a+bx)}{bx^5}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)/(x^5*(a + b*x)),x]

[Out] ((c*x^2)^(5/2)*Log[a + b*x])/(b*x^5)

fricas [A] time = 0.42, size = 23, normalized size = 0.92

$$\frac{\sqrt{cx^2} c^2 \log(bx + a)}{bx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^5/(b*x+a),x, algorithm="fricas")

[Out] sqrt(c*x^2)*c^2*log(b*x + a)/(b*x)

giac [A] time = 1.10, size = 34, normalized size = 1.36

$$\left(\frac{c^2 \log(|bx + a|) \operatorname{sgn}(x)}{b} - \frac{c^2 \log(|a|) \operatorname{sgn}(x)}{b} \right) \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^5/(b*x+a),x, algorithm="giac")

[Out] (c^2*log(abs(b*x + a))*sgn(x)/b - c^2*log(abs(a))*sgn(x)/b)*sqrt(c)

maple [A] time = 0.00, size = 21, normalized size = 0.84

$$\frac{(cx^2)^{\frac{5}{2}} \ln(bx + a)}{bx^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)/x^5/(b*x+a),x)

[Out] (c*x^2)^(5/2)/x^5*ln(b*x+a)/b

maxima [A] time = 1.36, size = 13, normalized size = 0.52

$$\frac{c^{\frac{5}{2}} \log(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^5/(b*x+a),x, algorithm="maxima")

[Out] $c^{(5/2)} \cdot \log(b \cdot x + a) / b$

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{(c x^2)^{5/2}}{x^5 (a + b x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(5/2)/(x^5*(a + b*x)), x)`

[Out] `int((c*x^2)^(5/2)/(x^5*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c x^2)^{\frac{5}{2}}}{x^5 (a + b x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(5/2)/x**5/(b*x+a), x)`

[Out] `Integral((c*x**2)**(5/2)/(x**5*(a + b*x)), x)`

$$3.875 \quad \int \frac{(cx^2)^{5/2}}{x^6(a+bx)} dx$$

Optimal. Leaf size=48

$$\frac{c^2\sqrt{cx^2} \log(x)}{ax} - \frac{c^2\sqrt{cx^2} \log(a+bx)}{ax}$$

[Out] $c^2*\ln(x)*(c*x^2)^{(1/2)}/a/x - c^2*\ln(b*x+a)*(c*x^2)^{(1/2)}/a/x$

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {15, 36, 29, 31}

$$\frac{c^2\sqrt{cx^2} \log(x)}{ax} - \frac{c^2\sqrt{cx^2} \log(a+bx)}{ax}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(5/2)/(x^6*(a + b*x)),x]

[Out] (c^2*Sqrt[c*x^2]*Log[x])/(a*x) - (c^2*Sqrt[c*x^2]*Log[a + b*x])/(a*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 29

Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] :> Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 36

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))), x_Symbol] :> Dist[b/(b*c - a*d), Int[1/(a + b*x), x], x] - Dist[d/(b*c - a*d), Int[1/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2}}{x^6(a+bx)} dx &= \frac{(c^2\sqrt{cx^2}) \int \frac{1}{x(a+bx)} dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int \frac{1}{x} dx}{ax} - \frac{(bc^2\sqrt{cx^2}) \int \frac{1}{a+bx} dx}{ax} \\ &= \frac{c^2\sqrt{cx^2} \log(x)}{ax} - \frac{c^2\sqrt{cx^2} \log(a+bx)}{ax} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.58

$$\frac{c^3x(\log(x) - \log(a+bx))}{a\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)/(x^6*(a + b*x)), x]

[Out] (c^3*x*(Log[x] - Log[a + b*x]))/(a*Sqrt[c*x^2])

fricas [A] time = 0.45, size = 70, normalized size = 1.46

$$\left[\frac{\sqrt{cx^2} c^2 \log\left(\frac{x}{bx+a}\right)}{ax}, \frac{2\sqrt{-c} c^2 \arctan\left(\frac{\sqrt{cx^2}(2bx+a)\sqrt{-c}}{acx}\right)}{a} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^6/(b*x+a), x, algorithm="fricas")

[Out] [sqrt(c*x^2)*c^2*log(x/(b*x + a))/(a*x), 2*sqrt(-c)*c^2*arctan(sqrt(c*x^2)*(2*b*x + a)*sqrt(-c)/(a*c*x))/a]

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^6/(b*x+a), x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
UT:sage2:=int(sage0,x);;OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 27, normalized size = 0.56

$$-\frac{(cx^2)^{\frac{5}{2}}(-\ln(x) + \ln(bx + a))}{ax^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)/x^6/(b*x+a),x)

[Out] -(c*x^2)^(5/2)*(-ln(x)+ln(b*x+a))/x^5/a

maxima [A] time = 1.35, size = 24, normalized size = 0.50

$$-\frac{c^{\frac{5}{2}} \log(bx + a)}{a} + \frac{c^{\frac{5}{2}} \log(x)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^6/(b*x+a),x, algorithm="maxima")

[Out] -c^(5/2)*log(b*x + a)/a + c^(5/2)*log(x)/a

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{\frac{5}{2}}}{x^6(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)/(x^6*(a + b*x)),x)

[Out] int((c*x^2)^(5/2)/(x^6*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}}}{x^6(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)/x**6/(b*x+a),x)

[Out] Integral((c*x**2)**(5/2)/(x**6*(a + b*x)), x)

$$3.876 \quad \int \frac{(cx^2)^{5/2}}{x^7(a+bx)} dx$$

Optimal. Leaf size=70

$$-\frac{bc^2\sqrt{cx^2} \log(x)}{a^2x} + \frac{bc^2\sqrt{cx^2} \log(a+bx)}{a^2x} - \frac{c^2\sqrt{cx^2}}{ax^2}$$

[Out] $-c^2*(c*x^2)^{(1/2)}/a/x^2-b*c^2*\ln(x)*(c*x^2)^{(1/2)}/a^2/x+b*c^2*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^2/x$

Rubi [A] time = 0.02, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{bc^2\sqrt{cx^2} \log(x)}{a^2x} + \frac{bc^2\sqrt{cx^2} \log(a+bx)}{a^2x} - \frac{c^2\sqrt{cx^2}}{ax^2}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(5/2)/(x^7*(a + b*x)), x]

[Out] $-((c^2*\text{Sqrt}[c*x^2])/(a*x^2)) - (b*c^2*\text{Sqrt}[c*x^2]*\text{Log}[x])/(a^2*x) + (b*c^2*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(a^2*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{5/2}}{x^7(a+bx)} dx &= \frac{(c^2\sqrt{cx^2}) \int \frac{1}{x^2(a+bx)} dx}{x} \\
&= \frac{(c^2\sqrt{cx^2}) \int \left(\frac{1}{ax^2} - \frac{b}{a^2x} + \frac{b^2}{a^2(a+bx)} \right) dx}{x} \\
&= -\frac{c^2\sqrt{cx^2}}{ax^2} - \frac{bc^2\sqrt{cx^2} \log(x)}{a^2x} + \frac{bc^2\sqrt{cx^2} \log(a+bx)}{a^2x}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 34, normalized size = 0.49

$$-\frac{c^3(-bx \log(a+bx) + a + bx \log(x))}{a^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)/(x^7*(a + b*x)),x]

[Out] -((c^3*(a + b*x*Log[x] - b*x*Log[a + b*x]))/(a^2*sqrt[c*x^2]))

fricas [A] time = 0.43, size = 37, normalized size = 0.53

$$\frac{\left(bc^2x \log\left(\frac{bx+a}{x}\right) - ac^2\right)\sqrt{cx^2}}{a^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^7/(b*x+a),x, algorithm="fricas")

[Out] (b*c^2*x*log((b*x + a)/x) - a*c^2)*sqrt(c*x^2)/(a^2*x^2)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^7/(b*x+a),x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
UT:sage2:=int(sage0,x)::OUTPUT:Warning, integration of abs or sign assumes
constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 33, normalized size = 0.47

$$-\frac{(cx^2)^{\frac{5}{2}}(bx \ln(x) - bx \ln(bx + a) + a)}{a^2x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)/x^7/(b*x+a), x)

[Out] -(c*x^2)^(5/2)*(b*x*ln(x)-b*x*ln(b*x+a)+a)/x^6/a^2

maxima [A] time = 1.39, size = 37, normalized size = 0.53

$$\frac{bc^{\frac{5}{2}} \log(bx + a)}{a^2} - \frac{bc^{\frac{5}{2}} \log(x)}{a^2} - \frac{c^{\frac{5}{2}}}{ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)/x^7/(b*x+a), x, algorithm="maxima")

[Out] b*c^(5/2)*log(b*x + a)/a^2 - b*c^(5/2)*log(x)/a^2 - c^(5/2)/(a*x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{5/2}}{x^7(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)/(x^7*(a + b*x)), x)

[Out] int((c*x^2)^(5/2)/(x^7*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}}}{x^7(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)/x**7/(b*x+a), x)

[Out] Integral((c*x**2)**(5/2)/(x**7*(a + b*x)), x)

$$3.877 \quad \int \frac{x^4}{\sqrt{cx^2}(a+bx)} dx$$

Optimal. Leaf size=83

$$-\frac{a^3 x \log(a+bx)}{b^4 \sqrt{cx^2}} + \frac{a^2 x^2}{b^3 \sqrt{cx^2}} - \frac{ax^3}{2b^2 \sqrt{cx^2}} + \frac{x^4}{3b \sqrt{cx^2}}$$

[Out] $a^2 x^2 / b^3 / (c x^2)^{(1/2)} - 1/2 a x^3 / b^2 / (c x^2)^{(1/2)} + 1/3 x^4 / b / (c x^2)^{(1/2)} - a^3 x \ln(b x + a) / b^4 / (c x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 83, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2 x^2}{b^3 \sqrt{cx^2}} - \frac{a^3 x \log(a+bx)}{b^4 \sqrt{cx^2}} - \frac{ax^3}{2b^2 \sqrt{cx^2}} + \frac{x^4}{3b \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^4/(Sqrt[c*x^2]*(a + b*x)),x]

[Out] $(a^2 x^2) / (b^3 \sqrt{c x^2}) - (a x^3) / (2 b^2 \sqrt{c x^2}) + x^4 / (3 b \sqrt{c x^2}) - (a^3 x \text{Log}[a + b x]) / (b^4 \sqrt{c x^2})$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{\sqrt{cx^2}(a+bx)} dx &= \frac{x \int \frac{x^3}{a+bx} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2}{b^3} - \frac{ax}{b^2} + \frac{x^2}{b} - \frac{a^3}{b^3(a+bx)} \right) dx}{\sqrt{cx^2}} \\ &= \frac{a^2 x^2}{b^3 \sqrt{cx^2}} - \frac{ax^3}{2b^2 \sqrt{cx^2}} + \frac{x^4}{3b \sqrt{cx^2}} - \frac{a^3 x \log(a+bx)}{b^4 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 51, normalized size = 0.61

$$\frac{x \left(bx \left(6a^2 - 3abx + 2b^2x^2 \right) - 6a^3 \log(a + bx) \right)}{6b^4 \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/(Sqrt[c*x^2]*(a + b*x)),x]

[Out] (x*(b*x*(6*a^2 - 3*a*b*x + 2*b^2*x^2) - 6*a^3*Log[a + b*x]))/(6*b^4*Sqrt[c*x^2])

fricas [A] time = 0.42, size = 54, normalized size = 0.65

$$\frac{(2b^3x^3 - 3ab^2x^2 + 6a^2bx - 6a^3 \log(bx + a))\sqrt{cx^2}}{6b^4cx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/6*(2*b^3*x^3 - 3*a*b^2*x^2 + 6*a^2*b*x - 6*a^3*log(b*x + a))*sqrt(c*x^2)/(b^4*c*x)

giac [A] time = 1.15, size = 81, normalized size = 0.98

$$\frac{1}{6} \sqrt{cx^2} \left(x \left(\frac{2x}{bc} - \frac{3a}{b^2c} \right) + \frac{6a^2}{b^3c} \right) + \frac{a^3 \log \left(\left| -(\sqrt{c}x - \sqrt{cx^2})b\sqrt{c} - 2ac \right| \right)}{b^4 \sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)/(c*x^2)^(1/2),x, algorithm="giac")

[Out] $\frac{1}{6}\sqrt{c*x^2}*(x*(2*x/(b*c) - 3*a/(b^2*c)) + 6*a^2/(b^3*c)) + a^3*\log(\text{abs}(-(\sqrt{c}*x - \sqrt{c*x^2})*b*\sqrt{c} - 2*a*c))/(b^4*\sqrt{c})$

maple [A] time = 0.01, size = 50, normalized size = 0.60

$$-\frac{(-2b^3x^3 + 3ab^2x^2 + 6a^3 \ln(bx + a) - 6a^2bx)x}{6\sqrt{cx^2} b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^4/(b*x+a)/(c*x^2)^(1/2),x)`

[Out] $-1/6*x*(-2*b^3*x^3+3*a*b^2*x^2+6*a^3*\ln(b*x+a)-6*a^2*b*x)/(c*x^2)^(1/2)/b^4$

maxima [A] time = 1.52, size = 142, normalized size = 1.71

$$\frac{\sqrt{cx^2} x^2}{3bc} - \frac{7ax^2}{6b^2\sqrt{c}} - \frac{(-1)^{\frac{2acx}{b}} a^3 \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^4\sqrt{c}} + \frac{2\sqrt{cx^2} ax}{3b^2c} - \frac{14a^2x}{3b^3\sqrt{c}} - \frac{a^3 \log(bx)}{b^4\sqrt{c}} + \frac{17\sqrt{cx^2} a^2}{3b^3c} - \frac{7a^3}{2b^4\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4/(b*x+a)/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $\frac{1}{3}\sqrt{c*x^2}*x^2/(b*c) - \frac{7}{6}*a*x^2/(b^2*\sqrt{c}) - (-1)^(2*a*c*x/b)*a^3*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(b^4*\sqrt{c}) + \frac{2}{3}\sqrt{c*x^2}*a*x/(b^2*c) - \frac{14}{3}*a^2*x/(b^3*\sqrt{c}) - a^3*\log(b*x)/(b^4*\sqrt{c}) + \frac{17}{3}\sqrt{c*x^2}*a^2/(b^3*c) - \frac{7}{2}*a^3/(b^4*\sqrt{c})$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^4}{\sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^4/((c*x^2)^(1/2)*(a + b*x)),x)`

[Out] `int(x^4/((c*x^2)^(1/2)*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^4}{\sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**4/(b*x+a)/(c*x**2)**(1/2),x)`

[Out] `Integral(x**4/(sqrt(c*x**2)*(a + b*x)), x)`

$$3.878 \quad \int \frac{x^3}{\sqrt{cx^2}(a+bx)} dx$$

Optimal. Leaf size=61

$$\frac{a^2 x \log(a+bx)}{b^3 \sqrt{cx^2}} - \frac{ax^2}{b^2 \sqrt{cx^2}} + \frac{x^3}{2b \sqrt{cx^2}}$$

[Out] $-a*x^2/b^2/(c*x^2)^{(1/2)}+1/2*x^3/b/(c*x^2)^{(1/2)}+a^2*x*\ln(b*x+a)/b^3/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2 x \log(a+bx)}{b^3 \sqrt{cx^2}} - \frac{ax^2}{b^2 \sqrt{cx^2}} + \frac{x^3}{2b \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^3/(Sqrt[c*x^2]*(a + b*x)), x]

[Out] $-((a*x^2)/(b^2*\text{Sqrt}[c*x^2])) + x^3/(2*b*\text{Sqrt}[c*x^2]) + (a^2*x*\text{Log}[a + b*x])/(b^3*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{x^3}{\sqrt{cx^2}(a+bx)} dx &= \frac{x \int \frac{x^2}{a+bx} dx}{\sqrt{cx^2}} \\
&= \frac{x \int \left(-\frac{a}{b^2} + \frac{x}{b} + \frac{a^2}{b^2(a+bx)}\right) dx}{\sqrt{cx^2}} \\
&= -\frac{ax^2}{b^2\sqrt{cx^2}} + \frac{x^3}{2b\sqrt{cx^2}} + \frac{a^2x \log(a+bx)}{b^3\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 39, normalized size = 0.64

$$\frac{x(2a^2 \log(a+bx) + bx(bx-2a))}{2b^3\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(Sqrt[c*x^2]*(a + b*x)),x]

[Out] (x*(b*x*(-2*a + b*x) + 2*a^2*Log[a + b*x]))/(2*b^3*Sqrt[c*x^2])

fricas [A] time = 0.42, size = 42, normalized size = 0.69

$$\frac{(b^2x^2 - 2abx + 2a^2 \log(bx+a))\sqrt{cx^2}}{2b^3cx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/2*(b^2*x^2 - 2*a*b*x + 2*a^2*log(b*x + a))*sqrt(c*x^2)/(b^3*c*x)

giac [A] time = 1.09, size = 67, normalized size = 1.10

$$\frac{1}{2} \sqrt{cx^2} \left(\frac{x}{bc} - \frac{2a}{b^2c} \right) - \frac{a^2 \log \left(\left| -(\sqrt{c}x - \sqrt{cx^2})b\sqrt{c} - 2ac \right| \right)}{b^3\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)/(c*x^2)^(1/2),x, algorithm="giac")

[Out] 1/2*sqrt(c*x^2)*(x/(b*c) - 2*a/(b^2*c)) - a^2*log(abs(-(sqrt(c)*x - sqrt(c*x^2))*b*sqrt(c) - 2*a*c))/(b^3*sqrt(c))

maple [A] time = 0.00, size = 38, normalized size = 0.62

$$\frac{(b^2x^2 + 2a^2 \ln(bx + a) - 2abx)x}{2\sqrt{cx^2} b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3/(b*x+a)/(c*x^2)^(1/2),x)`

[Out] `1/2*x*(b^2*x^2+2*a^2*ln(b*x+a)-2*a*b*x)/(c*x^2)^(1/2)/b^3`

maxima [A] time = 1.49, size = 100, normalized size = 1.64

$$\frac{x^2}{2b\sqrt{c}} + \frac{(-1)^{\frac{2acx}{b}} a^2 \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^3\sqrt{c}} + \frac{2ax}{b^2\sqrt{c}} + \frac{a^2 \log(bx)}{b^3\sqrt{c}} - \frac{3\sqrt{cx^2} a}{b^2c} + \frac{3a^2}{2b^3\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3/(b*x+a)/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] `1/2*x^2/(b*sqrt(c)) + (-1)^(2*a*c*x/b)*a^2*log(-2*a*c*x/(b*abs(b*x + a)))/(b^3*sqrt(c)) + 2*a*x/(b^2*sqrt(c)) + a^2*log(b*x)/(b^3*sqrt(c)) - 3*sqrt(c*x^2)*a/(b^2*c) + 3/2*a^2/(b^3*sqrt(c))`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^3}{\sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3/((c*x^2)^(1/2)*(a + b*x)),x)`

[Out] `int(x^3/((c*x^2)^(1/2)*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^3}{\sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**3/(b*x+a)/(c*x**2)**(1/2),x)`

[Out] `Integral(x**3/(sqrt(c*x**2)*(a + b*x)), x)`

$$3.879 \quad \int \frac{x^2}{\sqrt{cx^2}(a+bx)} dx$$

Optimal. Leaf size=39

$$\frac{x^2}{b\sqrt{cx^2}} - \frac{ax \log(a+bx)}{b^2\sqrt{cx^2}}$$

[Out] $x^2/b/(c*x^2)^{(1/2)} - a*x*\ln(b*x+a)/b^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{x^2}{b\sqrt{cx^2}} - \frac{ax \log(a+bx)}{b^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^2/(Sqrt[c*x^2]*(a + b*x)),x]

[Out] $x^2/(b*\text{Sqrt}[c*x^2]) - (a*x*\text{Log}[a + b*x])/(b^2*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sqrt{cx^2}(a+bx)} dx &= \frac{x \int \frac{x}{a+bx} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{1}{b} - \frac{a}{b(a+bx)} \right) dx}{\sqrt{cx^2}} \\ &= \frac{x^2}{b\sqrt{cx^2}} - \frac{ax \log(a+bx)}{b^2\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.69

$$\frac{x(bx - a \log(a + bx))}{b^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(Sqrt[c*x^2]*(a + b*x)),x]

[Out] (x*(b*x - a*Log[a + b*x]))/(b^2*Sqrt[c*x^2])

fricas [A] time = 0.48, size = 30, normalized size = 0.77

$$\frac{\sqrt{cx^2}(bx - a \log(bx + a))}{b^2cx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x - a*log(b*x + a))/(b^2*c*x)

giac [A] time = 1.19, size = 51, normalized size = 1.31

$$\frac{a \log \left(\left| -(\sqrt{c}x - \sqrt{cx^2})b\sqrt{c} - 2ac \right| \right)}{b^2\sqrt{c}} + \frac{\sqrt{cx^2}}{bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)/(c*x^2)^(1/2),x, algorithm="giac")

[Out] a*log(abs(-(sqrt(c)*x - sqrt(c*x^2))*b*sqrt(c) - 2*a*c))/(b^2*sqrt(c)) + sqrt(c*x^2)/(b*c)

maple [A] time = 0.00, size = 27, normalized size = 0.69

$$\frac{(a \ln(bx + a) - bx)x}{\sqrt{cx^2} b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/(b*x+a)/(c*x^2)^(1/2),x)`

[Out] `-x*(a*ln(b*x+a)-b*x)/(c*x^2)^(1/2)/b^2`

maxima [A] time = 1.47, size = 64, normalized size = 1.64

$$-\frac{(-1)^{\frac{2acx}{b}} a \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^2\sqrt{c}} - \frac{a \log(bx)}{b^2\sqrt{c}} + \frac{\sqrt{cx^2}}{bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2/(b*x+a)/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] `-(-1)^(2*a*c*x/b)*a*log(-2*a*c*x/(b*abs(b*x + a)))/(b^2*sqrt(c)) - a*log(b*x)/(b^2*sqrt(c)) + sqrt(c*x^2)/(b*c)`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{x^2}{\sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/((c*x^2)^(1/2)*(a + b*x)),x)`

[Out] `int(x^2/((c*x^2)^(1/2)*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2}{\sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2/(b*x+a)/(c*x**2)**(1/2),x)`

[Out] `Integral(x**2/(sqrt(c*x**2)*(a + b*x)), x)`

$$3.880 \quad \int \frac{x}{\sqrt{cx^2}(a+bx)} dx$$

Optimal. Leaf size=20

$$\frac{x \log(a + bx)}{b\sqrt{cx^2}}$$

[Out] $x \ln(b*x+a)/b/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 31}

$$\frac{x \log(a + bx)}{b\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x/(Sqrt[c*x^2]*(a + b*x)),x]

[Out] (x*Log[a + b*x])/(b*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\begin{aligned} \int \frac{x}{\sqrt{cx^2}(a+bx)} dx &= \frac{x \int \frac{1}{a+bx} dx}{\sqrt{cx^2}} \\ &= \frac{x \log(a + bx)}{b\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 20, normalized size = 1.00

$$\frac{x \log(a + bx)}{b\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[x/(Sqrt[c*x^2]*(a + b*x)),x]

[Out] (x*Log[a + b*x])/(b*Sqrt[c*x^2])

fricas [A] time = 0.43, size = 23, normalized size = 1.15

$$\frac{\sqrt{cx^2} \log(bx + a)}{bcx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] sqrt(c*x^2)*log(b*x + a)/(b*c*x)

giac [A] time = 0.90, size = 36, normalized size = 1.80

$$-\frac{\log\left(\left|-\left(\sqrt{c}x - \sqrt{cx^2}\right)b\sqrt{c} - 2ac\right|\right)}{b\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)/(c*x^2)^(1/2),x, algorithm="giac")

[Out] -log(abs(-(sqrt(c)*x - sqrt(c*x^2))*b*sqrt(c) - 2*a*c))/(b*sqrt(c))

maple [A] time = 0.00, size = 19, normalized size = 0.95

$$\frac{x \ln(bx + a)}{\sqrt{cx^2} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(b*x+a)/(c*x^2)^(1/2),x)

[Out] x*ln(b*x+a)/b/(c*x^2)^(1/2)

maxima [B] time = 1.46, size = 46, normalized size = 2.30

$$\frac{(-1)^{\frac{2acx}{b}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b\sqrt{c}} + \frac{\log(bx)}{b\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] $(-1)^{(2*a*c*x/b)} * \log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(b*\text{sqrt}(c)) + \log(b*x)/(b*\text{sqrt}(c))$

mupad [F] time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{x}{\sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/((c*x^2)^(1/2)*(a + b*x)),x)

[Out] int(x/((c*x^2)^(1/2)*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x}{\sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)/(c*x**2)**(1/2),x)

[Out] Integral(x/(sqrt(c*x**2)*(a + b*x)), x)

$$3.881 \quad \int \frac{1}{\sqrt{cx^2}(a+bx)} dx$$

Optimal. Leaf size=38

$$\frac{x \log(x)}{a\sqrt{cx^2}} - \frac{x \log(a+bx)}{a\sqrt{cx^2}}$$

[Out] x*ln(x)/a/(c*x^2)^(1/2)-x*ln(b*x+a)/a/(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {15, 36, 29, 31}

$$\frac{x \log(x)}{a\sqrt{cx^2}} - \frac{x \log(a+bx)}{a\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[c*x^2]*(a + b*x)),x]

[Out] (x*Log[x])/(a*Sqrt[c*x^2]) - (x*Log[a + b*x])/(a*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 29

Int[(x_)^(-1), x_Symbol] := Simp[Log[x], x]

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 36

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))), x_Symbol] := Dist[b/(b*c - a*d), Int[1/(a + b*x), x], x] - Dist[d/(b*c - a*d), Int[1/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{cx^2}(a+bx)} dx &= \frac{x \int \frac{1}{x(a+bx)} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \frac{1}{x} dx}{a\sqrt{cx^2}} - \frac{(bx) \int \frac{1}{a+bx} dx}{a\sqrt{cx^2}} \\ &= \frac{x \log(x)}{a\sqrt{cx^2}} - \frac{x \log(a+bx)}{a\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 25, normalized size = 0.66

$$\frac{x(\log(x) - \log(a + bx))}{a\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[c*x^2]*(a + b*x)),x]

[Out] (x*(Log[x] - Log[a + b*x]))/(a*Sqrt[c*x^2])

fricas [A] time = 0.44, size = 70, normalized size = 1.84

$$\left[\frac{\sqrt{cx^2} \log\left(\frac{x}{bx+a}\right)}{acx}, \frac{2\sqrt{-c} \arctan\left(\frac{\sqrt{cx^2}(2bx+a)\sqrt{-c}}{acx}\right)}{ac} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] [sqrt(c*x^2)*log(x/(b*x + a))/(a*c*x), 2*sqrt(-c)*arctan(sqrt(c*x^2)*(2*b*x + a)*sqrt(-c)/(a*c*x))/(a*c)]

giac [A] time = 0.97, size = 59, normalized size = 1.55

$$\frac{\log\left(\left|-\left(\sqrt{c}x - \sqrt{cx^2}\right)b - 2a\sqrt{c}\right|\right)}{a\sqrt{c}} - \frac{\log\left(\left|-\sqrt{c}x + \sqrt{cx^2}\right|\right)}{a\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(c*x^2)^(1/2),x, algorithm="giac")

[Out] $\log(\text{abs}(-(\text{sqrt}(c)*x - \text{sqrt}(c*x^2))*b - 2*a*\text{sqrt}(c)))/(a*\text{sqrt}(c)) - \log(\text{abs}(-\text{sqrt}(c)*x + \text{sqrt}(c*x^2)))/(a*\text{sqrt}(c))$

maple [A] time = 0.00, size = 24, normalized size = 0.63

$$\frac{(\ln(x) - \ln(bx + a))x}{\sqrt{cx^2} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)/(c*x^2)^(1/2),x)`

[Out] $x*(\ln(x) - \ln(b*x+a))/(c*x^2)^{(1/2)}/a$

maxima [A] time = 1.46, size = 35, normalized size = 0.92

$$-\frac{(-1)^{\frac{2acx}{b}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{a\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $-(-1)^{(2*a*c*x/b)}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(a*\text{sqrt}(c))$

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{1}{\sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((c*x^2)^(1/2)*(a + b*x)),x)`

[Out] `int(1/((c*x^2)^(1/2)*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/(c*x**2)**(1/2),x)`

[Out] `Integral(1/(sqrt(c*x**2)*(a + b*x)), x)`

$$3.882 \quad \int \frac{1}{x \sqrt{cx^2} (a+bx)} dx$$

Optimal. Leaf size=54

$$-\frac{bx \log(x)}{a^2 \sqrt{cx^2}} + \frac{bx \log(a+bx)}{a^2 \sqrt{cx^2}} - \frac{1}{a \sqrt{cx^2}}$$

[Out] $-1/a/(c*x^2)^{(1/2)}-b*x*\ln(x)/a^2/(c*x^2)^{(1/2)}+b*x*\ln(b*x+a)/a^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{bx \log(x)}{a^2 \sqrt{cx^2}} + \frac{bx \log(a+bx)}{a^2 \sqrt{cx^2}} - \frac{1}{a \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*Sqrt[c*x^2]*(a + b*x)), x]

[Out] $-(1/(a*\text{Sqrt}[c*x^2])) - (b*x*\text{Log}[x])/(a^2*\text{Sqrt}[c*x^2]) + (b*x*\text{Log}[a + b*x])/(a^2*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x\sqrt{cx^2}(a+bx)} dx &= \frac{x \int \frac{1}{x^2(a+bx)} dx}{\sqrt{cx^2}} \\
&= \frac{x \int \left(\frac{1}{ax^2} - \frac{b}{a^2x} + \frac{b^2}{a^2(a+bx)} \right) dx}{\sqrt{cx^2}} \\
&= -\frac{1}{a\sqrt{cx^2}} - \frac{bx \log(x)}{a^2\sqrt{cx^2}} + \frac{bx \log(a+bx)}{a^2\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 36, normalized size = 0.67

$$\frac{cx^2(bx \log(a+bx) - a - bx \log(x))}{a^2(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*Sqrt[c*x^2]*(a + b*x)),x]

[Out] (c*x^2*(-a - b*x*Log[x] + b*x*Log[a + b*x]))/(a^2*(c*x^2)^(3/2))

fricas [A] time = 0.43, size = 34, normalized size = 0.63

$$\frac{\sqrt{cx^2} \left(bx \log\left(\frac{bx+a}{x}\right) - a \right)}{a^2 cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x*log((b*x + a)/x) - a)/(a^2*c*x^2)

giac [A] time = 1.19, size = 91, normalized size = 1.69

$$-\sqrt{c} \left(\frac{b \log\left(\left| -(\sqrt{c}x - \sqrt{cx^2})b - 2a\sqrt{c} \right|\right)}{a^2c} - \frac{b \log\left(\left| -\sqrt{c}x + \sqrt{cx^2} \right|\right)}{a^2c} - \frac{2}{(\sqrt{c}x - \sqrt{cx^2})a\sqrt{c}} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)/(c*x^2)^(1/2),x, algorithm="giac")

[Out] $-\sqrt{c}*(b*\log(\text{abs}(-(\sqrt{c}*x - \sqrt{c*x^2}))*b - 2*a*\sqrt{c}))/(\text{a}^2*c) - b*\log(\text{abs}(-\sqrt{c}*x + \sqrt{c*x^2}))/(\text{a}^2*c) - 2/((\sqrt{c}*x - \sqrt{c*x^2})*a*\sqrt{c}))$

maple [A] time = 0.01, size = 30, normalized size = 0.56

$$-\frac{bx \ln(x) - bx \ln(bx + a) + a}{\sqrt{c} x^2 a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x/(b*x+a)/(c*x^2)^(1/2), x)`

[Out] $-(b*x*\ln(x)-b*x*\ln(b*x+a)+a)/(c*x^2)^(1/2)/a^2$

maxima [A] time = 1.37, size = 37, normalized size = 0.69

$$\frac{b \log(bx + a)}{a^2 \sqrt{c}} - \frac{b \log(x)}{a^2 \sqrt{c}} - \frac{1}{a \sqrt{c} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b*x+a)/(c*x^2)^(1/2), x, algorithm="maxima")`

[Out] $b*\log(b*x + a)/(\text{a}^2*\sqrt{c}) - b*\log(x)/(\text{a}^2*\sqrt{c}) - 1/(\text{a}*\sqrt{c})*x$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{1}{x \sqrt{c x^2} (a + b x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x*(c*x^2)^(1/2)*(a + b*x)), x)`

[Out] `int(1/(x*(c*x^2)^(1/2)*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{x \sqrt{c x^2} (a + b x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(b*x+a)/(c*x**2)**(1/2), x)`

[Out] `Integral(1/(x*sqrt(c*x**2)*(a + b*x)), x)`

$$3.883 \quad \int \frac{1}{x^2 \sqrt{cx^2} (a+bx)} dx$$

Optimal. Leaf size=77

$$\frac{b^2 x \log(x)}{a^3 \sqrt{cx^2}} - \frac{b^2 x \log(a+bx)}{a^3 \sqrt{cx^2}} + \frac{b}{a^2 \sqrt{cx^2}} - \frac{1}{2ax \sqrt{cx^2}}$$

[Out] $b/a^2/(c*x^2)^{(1/2)} - 1/2/a/x/(c*x^2)^{(1/2)} + b^2*x*\ln(x)/a^3/(c*x^2)^{(1/2)} - b^2*x*\ln(b*x+a)/a^3/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 77, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$\frac{b^2 x \log(x)}{a^3 \sqrt{cx^2}} - \frac{b^2 x \log(a+bx)}{a^3 \sqrt{cx^2}} + \frac{b}{a^2 \sqrt{cx^2}} - \frac{1}{2ax \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*sqrt[c*x^2]*(a + b*x)),x]

[Out] $b/(a^2*\sqrt{c*x^2}) - 1/(2*a*x*\sqrt{c*x^2}) + (b^2*x*\text{Log}[x])/(a^3*\sqrt{c*x^2}) - (b^2*x*\text{Log}[a + b*x])/(a^3*\sqrt{c*x^2})$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x^2 \sqrt{cx^2} (a + bx)} dx &= \frac{x \int \frac{1}{x^3(a+bx)} dx}{\sqrt{cx^2}} \\
&= \frac{x \int \left(\frac{1}{ax^3} - \frac{b}{a^2x^2} + \frac{b^2}{a^3x} - \frac{b^3}{a^3(a+bx)} \right) dx}{\sqrt{cx^2}} \\
&= \frac{b}{a^2 \sqrt{cx^2}} - \frac{1}{2ax \sqrt{cx^2}} + \frac{b^2 x \log(x)}{a^3 \sqrt{cx^2}} - \frac{b^2 x \log(a + bx)}{a^3 \sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 52, normalized size = 0.68

$$\frac{cx \left(-2b^2x^2 \log(a + bx) - a(a - 2bx) + 2b^2x^2 \log(x) \right)}{2a^3 (cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*sqrt[c*x^2]*(a + b*x)),x]

[Out] (c*x*(-(a*(a - 2*b*x)) + 2*b^2*x^2*Log[x] - 2*b^2*x^2*Log[a + b*x]))/(2*a^3*(c*x^2)^(3/2))

fricas [A] time = 0.45, size = 47, normalized size = 0.61

$$\frac{\left(2b^2x^2 \log\left(\frac{x}{bx+a}\right) + 2abx - a^2 \right) \sqrt{cx^2}}{2a^3cx^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/2*(2*b^2*x^2*log(x/(b*x + a)) + 2*a*b*x - a^2)*sqrt(c*x^2)/(a^3*c*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0*x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)/(c*x^2)^(1/2),x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.00, size = 51, normalized size = 0.66

$$\frac{2b^2x^2 \ln(x) - 2b^2x^2 \ln(bx + a) + 2abx - a^2}{2\sqrt{cx^2} a^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^2/(b*x+a)/(c*x^2)^(1/2),x)`

[Out] `1/2/x*(2*b^2*x^2*ln(x)-2*b^2*x^2*ln(b*x+a)+2*a*b*x-a^2)/(c*x^2)^(1/2)/a^3`

maxima [A] time = 1.38, size = 55, normalized size = 0.71

$$-\frac{b^2 \log(bx + a)}{a^3 \sqrt{c}} + \frac{b^2 \log(x)}{a^3 \sqrt{c}} + \frac{2b\sqrt{c}x - a\sqrt{c}}{2a^2cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(b*x+a)/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] `-b^2*log(b*x + a)/(a^3*sqrt(c)) + b^2*log(x)/(a^3*sqrt(c)) + 1/2*(2*b*sqrt(c)*x - a*sqrt(c))/(a^2*c*x^2)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{x^2 \sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(x^2*(c*x^2)^(1/2)*(a + b*x)),x)`

[Out] `int(1/(x^2*(c*x^2)^(1/2)*(a + b*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{x^2 \sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(b*x+a)/(c*x**2)**(1/2),x)`

[Out] `Integral(1/(x**2*sqrt(c*x**2)*(a + b*x)), x)`

$$3.884 \quad \int \frac{1}{x^3 \sqrt{cx^2} (a+bx)} dx$$

Optimal. Leaf size=100

$$-\frac{b^3 x \log(x)}{a^4 \sqrt{cx^2}} + \frac{b^3 x \log(a+bx)}{a^4 \sqrt{cx^2}} - \frac{b^2}{a^3 \sqrt{cx^2}} + \frac{b}{2a^2 x \sqrt{cx^2}} - \frac{1}{3ax^2 \sqrt{cx^2}}$$

[Out] $-b^2/a^3/(c*x^2)^{(1/2)}-1/3/a/x^2/(c*x^2)^{(1/2)}+1/2*b/a^2/x/(c*x^2)^{(1/2)}-b^3*x*\ln(x)/a^4/(c*x^2)^{(1/2)}+b^3*x*\ln(b*x+a)/a^4/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{b^2}{a^3 \sqrt{cx^2}} - \frac{b^3 x \log(x)}{a^4 \sqrt{cx^2}} + \frac{b^3 x \log(a+bx)}{a^4 \sqrt{cx^2}} + \frac{b}{2a^2 x \sqrt{cx^2}} - \frac{1}{3ax^2 \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^3*sqrt[c*x^2]*(a + b*x)), x]

[Out] $-(b^2/(a^3*\text{sqrt}[c*x^2])) - 1/(3*a*x^2*\text{sqrt}[c*x^2]) + b/(2*a^2*x*\text{sqrt}[c*x^2]) - (b^3*x*\text{Log}[x])/(a^4*\text{sqrt}[c*x^2]) + (b^3*x*\text{Log}[a + b*x])/(a^4*\text{sqrt}[c*x^2])$

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x^3 \sqrt{cx^2} (a + bx)} dx &= \frac{x \int \frac{1}{x^4(a+bx)} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{1}{ax^4} - \frac{b}{a^2x^3} + \frac{b^2}{a^3x^2} - \frac{b^3}{a^4x} + \frac{b^4}{a^4(a+bx)} \right) dx}{\sqrt{cx^2}} \\ &= -\frac{b^2}{a^3 \sqrt{cx^2}} - \frac{1}{3ax^2 \sqrt{cx^2}} + \frac{b}{2a^2x \sqrt{cx^2}} - \frac{b^3x \log(x)}{a^4 \sqrt{cx^2}} + \frac{b^3x \log(a+bx)}{a^4 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 63, normalized size = 0.63

$$\frac{c \left(a \left(-2a^2 + 3abx - 6b^2x^2 \right) + 6b^3x^3 \log(a + bx) - 6b^3x^3 \log(x) \right)}{6a^4 (cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^3*Sqrt[c*x^2]*(a + b*x)),x]

[Out] (c*(a*(-2*a^2 + 3*a*b*x - 6*b^2*x^2) - 6*b^3*x^3*Log[x] + 6*b^3*x^3*Log[a + b*x]))/(6*a^4*(c*x^2)^(3/2))

fricas [A] time = 0.43, size = 58, normalized size = 0.58

$$\frac{\left(6b^3x^3 \log\left(\frac{bx+a}{x}\right) - 6ab^2x^2 + 3a^2bx - 2a^3 \right) \sqrt{cx^2}}{6a^4cx^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/6*(6*b^3*x^3*log((b*x + a)/x) - 6*a*b^2*x^2 + 3*a^2*b*x - 2*a^3)*sqrt(c*x^2)/(a^4*c*x^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{cx^2} (bx + a)x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)/(c*x^2)^(1/2),x, algorithm="giac")

[Out] integrate(1/(sqrt(c*x^2)*(b*x + a)*x^3), x)

maple [A] time = 0.00, size = 62, normalized size = 0.62

$$-\frac{6b^3x^3 \ln(x) - 6b^3x^3 \ln(bx + a) + 6ab^2x^2 - 3a^2bx + 2a^3}{6\sqrt{cx^2} a^4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^3/(b*x+a)/(c*x^2)^(1/2), x)

[Out] $-1/6/x^2*(6*b^3*x^3*\ln(x)-6*b^3*x^3*\ln(b*x+a)+6*a*b^2*x^2-3*a^2*b*x+2*a^3)/(c*x^2)^(1/2)/a^4$

maxima [A] time = 1.40, size = 69, normalized size = 0.69

$$\frac{b^3 \log(bx + a)}{a^4 \sqrt{c}} - \frac{b^3 \log(x)}{a^4 \sqrt{c}} - \frac{6b^2 \sqrt{c} x^2 - 3ab \sqrt{c} x + 2a^2 \sqrt{c}}{6a^3 c x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3/(b*x+a)/(c*x^2)^(1/2), x, algorithm="maxima")

[Out] $b^3*\log(b*x + a)/(a^4*\sqrt{c}) - b^3*\log(x)/(a^4*\sqrt{c}) - 1/6*(6*b^2*\sqrt{c}*x^2 - 3*a*b*\sqrt{c}*x + 2*a^2*\sqrt{c})/(a^3*c*x^3)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{x^3 \sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^3*(c*x^2)^(1/2)*(a + b*x)), x)

[Out] int(1/(x^3*(c*x^2)^(1/2)*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{x^3 \sqrt{cx^2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**3/(b*x+a)/(c*x**2)**(1/2), x)

[Out] Integral(1/(x**3*sqrt(c*x**2)*(a + b*x)), x)

$$3.885 \quad \int \frac{x^6}{(cx^2)^{3/2}(a+bx)} dx$$

Optimal. Leaf size=95

$$-\frac{a^3x \log(a+bx)}{b^4c\sqrt{cx^2}} + \frac{a^2x^2}{b^3c\sqrt{cx^2}} - \frac{ax^3}{2b^2c\sqrt{cx^2}} + \frac{x^4}{3bc\sqrt{cx^2}}$$

[Out] $a^2*x^2/b^3/c/(c*x^2)^{(1/2)} - 1/2*a*x^3/b^2/c/(c*x^2)^{(1/2)} + 1/3*x^4/b/c/(c*x^2)^{(1/2)} - a^3*x*\ln(b*x+a)/b^4/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2x^2}{b^3c\sqrt{cx^2}} - \frac{a^3x \log(a+bx)}{b^4c\sqrt{cx^2}} - \frac{ax^3}{2b^2c\sqrt{cx^2}} + \frac{x^4}{3bc\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^6/((c*x^2)^{(3/2)}*(a + b*x)), x]$

[Out] $(a^2*x^2)/(b^3*c*\text{Sqrt}[c*x^2]) - (a*x^3)/(2*b^2*c*\text{Sqrt}[c*x^2]) + x^4/(3*b*c*\text{Sqrt}[c*x^2]) - (a^3*x*\text{Log}[a + b*x])/(b^4*c*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{x^6}{(cx^2)^{3/2} (a+bx)} dx &= \frac{x \int \frac{x^3}{a+bx} dx}{c\sqrt{cx^2}} \\
&= \frac{x \int \left(\frac{a^2}{b^3} - \frac{ax}{b^2} + \frac{x^2}{b} - \frac{a^3}{b^3(a+bx)} \right) dx}{c\sqrt{cx^2}} \\
&= \frac{a^2 x^2}{b^3 c \sqrt{cx^2}} - \frac{ax^3}{2b^2 c \sqrt{cx^2}} + \frac{x^4}{3bc \sqrt{cx^2}} - \frac{a^3 x \log(a+bx)}{b^4 c \sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 53, normalized size = 0.56

$$\frac{x^3 (bx (6a^2 - 3abx + 2b^2x^2) - 6a^3 \log(a+bx))}{6b^4 (cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^6/((c*x^2)^(3/2)*(a + b*x)),x]

[Out] (x^3*(b*x*(6*a^2 - 3*a*b*x + 2*b^2*x^2) - 6*a^3*Log[a + b*x]))/(6*b^4*(c*x^2)^(3/2))

fricas [A] time = 0.42, size = 54, normalized size = 0.57

$$\frac{(2b^3x^3 - 3ab^2x^2 + 6a^2bx - 6a^3 \log(bx+a))\sqrt{cx^2}}{6b^4c^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(c*x^2)^(3/2)/(b*x+a),x, algorithm="fricas")

[Out] 1/6*(2*b^3*x^3 - 3*a*b^2*x^2 + 6*a^2*b*x - 6*a^3*log(b*x + a))*sqrt(c*x^2)/(b^4*c^2*x)

giac [A] time = 1.18, size = 86, normalized size = 0.91

$$\frac{\sqrt{cx^2} \left(x \left(\frac{2x}{bc} - \frac{3a}{b^2c} \right) + \frac{6a^2}{b^3c} \right) + \frac{6a^3 \log\left(\left| -(\sqrt{cx} - \sqrt{cx^2})b\sqrt{c} - 2ac \right| \right)}{b^4\sqrt{c}}}{6c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/(c*x^2)^(3/2)/(b*x+a),x, algorithm="giac")

[Out] $\frac{1}{6} \cdot (\sqrt{c \cdot x^2}) \cdot (x \cdot (2 \cdot x / (b \cdot c) - 3 \cdot a / (b^2 \cdot c)) + 6 \cdot a^2 / (b^3 \cdot c)) + 6 \cdot a^3 \cdot \log(\text{abs}(-(\sqrt{c} \cdot x - \sqrt{c \cdot x^2}) \cdot b \cdot \sqrt{c} - 2 \cdot a \cdot c)) / (b^4 \cdot \sqrt{c})) / c$

maple [A] time = 0.01, size = 52, normalized size = 0.55

$$\frac{(-2b^3x^3 + 3ab^2x^2 + 6a^3 \ln(bx + a) - 6a^2bx)x^3}{6(c x^2)^{\frac{3}{2}} b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^6 / (c \cdot x^2)^{(3/2)} / (b \cdot x + a), x)$

[Out] $-1/6 \cdot x^3 \cdot (-2 \cdot b^3 \cdot x^3 + 3 \cdot a \cdot b^2 \cdot x^2 + 6 \cdot a^3 \cdot \ln(b \cdot x + a) - 6 \cdot a^2 \cdot b \cdot x) / (c \cdot x^2)^{(3/2)} / b^4$

maxima [A] time = 1.79, size = 162, normalized size = 1.71

$$\frac{x^4}{3 \sqrt{c x^2} b c} - \frac{a x^3}{2 \sqrt{c x^2} b^2 c} + \frac{a^2 x^2}{\sqrt{c x^2} b^3 c} - \frac{(-1)^{\frac{2 a c x}{b}} a^3 \log\left(-\frac{2 a c x}{b |b x + a|}\right)}{b^4 c^{\frac{3}{2}}} + \frac{29 a^3 x}{6 \sqrt{c x^2} b^4 c} - \frac{a^3 \log(b x)}{b^4 c^{\frac{3}{2}}} - \frac{2 a^4}{\sqrt{c x^2} b^5 c} + \frac{2 a^4}{b^5 c^{\frac{3}{2}} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^6 / (c \cdot x^2)^{(3/2)} / (b \cdot x + a), x, \text{algorithm}="maxima")$

[Out] $\frac{1}{3} \cdot x^4 / (\sqrt{c \cdot x^2} \cdot b \cdot c) - \frac{1}{2} \cdot a \cdot x^3 / (\sqrt{c \cdot x^2} \cdot b^2 \cdot c) + \frac{a^2 \cdot x^2}{\sqrt{c \cdot x^2} \cdot b^3 \cdot c} - \frac{(-1)^{(2 \cdot a \cdot c \cdot x / b)} \cdot a^3 \cdot \log(-2 \cdot a \cdot c \cdot x / (b \cdot \text{abs}(b \cdot x + a)))}{b^4 \cdot c^{(3/2)}} + \frac{29}{6} \cdot a^3 \cdot x / (\sqrt{c \cdot x^2} \cdot b^4 \cdot c) - \frac{a^3 \cdot \log(b \cdot x)}{b^4 \cdot c^{(3/2)}} - \frac{2 \cdot a^4}{\sqrt{c \cdot x^2} \cdot b^5 \cdot c} + \frac{2 \cdot a^4}{b^5 \cdot c^{(3/2)} \cdot x}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^6}{(c x^2)^{\frac{3}{2}} (a + b x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^6 / ((c \cdot x^2)^{(3/2)} \cdot (a + b \cdot x)), x)$

[Out] $\text{int}(x^6 / ((c \cdot x^2)^{(3/2)} \cdot (a + b \cdot x)), x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^6}{(c x^2)^{\frac{3}{2}} (a + b x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**6/(c*x**2)**(3/2)/(b*x+a), x)
```

```
[Out] Integral(x**6/((c*x**2)**(3/2)*(a + b*x)), x)
```

$$3.886 \quad \int \frac{x^5}{(cx^2)^{3/2}(a+bx)} dx$$

Optimal. Leaf size=70

$$\frac{a^2x \log(a+bx)}{b^3c\sqrt{cx^2}} - \frac{ax^2}{b^2c\sqrt{cx^2}} + \frac{x^3}{2bc\sqrt{cx^2}}$$

[Out] $-a*x^2/b^2/c/(c*x^2)^{(1/2)}+1/2*x^3/b/c/(c*x^2)^{(1/2)}+a^2*x*\ln(b*x+a)/b^3/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2x \log(a+bx)}{b^3c\sqrt{cx^2}} - \frac{ax^2}{b^2c\sqrt{cx^2}} + \frac{x^3}{2bc\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^5/((c*x^2)^(3/2)*(a + b*x)),x]

[Out] $-((a*x^2)/(b^2*c*\text{Sqrt}[c*x^2])) + x^3/(2*b*c*\text{Sqrt}[c*x^2]) + (a^2*x*\text{Log}[a + b*x])/(b^3*c*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^5}{(cx^2)^{3/2} (a+bx)} dx &= \frac{x \int \frac{x^2}{a+bx} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(-\frac{a}{b^2} + \frac{x}{b} + \frac{a^2}{b^2(a+bx)} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{ax^2}{b^2c\sqrt{cx^2}} + \frac{x^3}{2bc\sqrt{cx^2}} + \frac{a^2x \log(a+bx)}{b^3c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 41, normalized size = 0.59

$$\frac{x^3 (2a^2 \log(a+bx) + bx(bx-2a))}{2b^3 (cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/((c*x^2)^(3/2)*(a + b*x)), x]

[Out] (x^3*(b*x*(-2*a + b*x) + 2*a^2*Log[a + b*x]))/(2*b^3*(c*x^2)^(3/2))

fricas [A] time = 0.42, size = 42, normalized size = 0.60

$$\frac{(b^2x^2 - 2abx + 2a^2 \log(bx+a))\sqrt{cx^2}}{2b^3c^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(c*x^2)^(3/2)/(b*x+a), x, algorithm="fricas")

[Out] 1/2*(b^2*x^2 - 2*a*b*x + 2*a^2*log(b*x + a))*sqrt(c*x^2)/(b^3*c^2*x)

giac [A] time = 0.96, size = 71, normalized size = 1.01

$$\frac{\sqrt{cx^2} \left(\frac{x}{bc} - \frac{2a}{b^2c} \right) - \frac{2a^2 \log\left(\left| -\left(\sqrt{c}x - \sqrt{cx^2} \right) b\sqrt{c} - 2ac \right| \right)}{b^3\sqrt{c}}}{2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(c*x^2)^(3/2)/(b*x+a), x, algorithm="giac")

[Out] $\frac{1}{2} * (\sqrt{c*x^2}) * (x/(b*c) - 2*a/(b^2*c)) - 2*a^2 * \log(\text{abs}(-(\sqrt{c}) * x - \sqrt{c*x^2})) * b * \sqrt{c} - 2*a*c) / (b^3 * \sqrt{c}) / c$

maple [A] time = 0.00, size = 40, normalized size = 0.57

$$\frac{(b^2 x^2 + 2a^2 \ln(bx + a) - 2abx) x^3}{2 (cx^2)^{\frac{3}{2}} b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^5 / (c*x^2)^{(3/2)} / (b*x+a), x)$

[Out] $\frac{1}{2} * x^3 * (b^2 * x^2 + 2 * a^2 * \ln(b*x+a) - 2 * a * b * x) / (c*x^2)^{(3/2)} / b^3$

maxima [B] time = 1.66, size = 140, normalized size = 2.00

$$\frac{x^3}{2 \sqrt{cx^2} bc} - \frac{ax^2}{\sqrt{cx^2} b^2 c} + \frac{(-1)^{\frac{2acx}{b}} a^2 \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^3 c^{\frac{3}{2}}} - \frac{7a^2 x}{2 \sqrt{cx^2} b^3 c} + \frac{a^2 \log(bx)}{b^3 c^{\frac{3}{2}}} + \frac{2a^3}{\sqrt{cx^2} b^4 c} - \frac{2a^3}{b^4 c^{\frac{3}{2}} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^5 / (c*x^2)^{(3/2)} / (b*x+a), x, \text{algorithm}="maxima")$

[Out] $\frac{1}{2} * x^3 / (\sqrt{c*x^2} * b * c) - a * x^2 / (\sqrt{c*x^2} * b^2 * c) + (-1)^{(2*a*c*x/b)} * a^2 * \log(-2*a*c*x / (b * \text{abs}(b*x + a))) / (b^3 * c^{(3/2)}) - 7/2 * a^2 * x / (\sqrt{c*x^2} * b^3 * c) + a^2 * \log(b*x) / (b^3 * c^{(3/2)}) + 2*a^3 / (\sqrt{c*x^2} * b^4 * c) - 2*a^3 / (b^4 * c^{(3/2)} * x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^5}{(cx^2)^{3/2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^5 / ((c*x^2)^{(3/2)} * (a + b*x)), x)$

[Out] $\text{int}(x^5 / ((c*x^2)^{(3/2)} * (a + b*x)), x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^5}{(cx^2)^{\frac{3}{2}} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5/(c*x**2)**(3/2)/(b*x+a), x)
```

```
[Out] Integral(x**5/((c*x**2)**(3/2)*(a + b*x)), x)
```

$$3.887 \quad \int \frac{x^4}{(cx^2)^{3/2} (a+bx)} dx$$

Optimal. Leaf size=45

$$\frac{x^2}{bc\sqrt{cx^2}} - \frac{ax \log(a+bx)}{b^2c\sqrt{cx^2}}$$

[Out] $x^2/b/c/(c*x^2)^{(1/2)} - a*x*\ln(b*x+a)/b^2/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{x^2}{bc\sqrt{cx^2}} - \frac{ax \log(a+bx)}{b^2c\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^4/((c*x^2)^{(3/2)}*(a + b*x)),x]$

[Out] $x^2/(b*c*\text{Sqrt}[c*x^2]) - (a*x*\text{Log}[a + b*x])/(b^2*c*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] := \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ $\text{FreeQ}\{a, m, n\}, x$
&& $!\text{IntegerQ}[m]$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ $\text{FreeQ}\{a, b, c, d, n\}, x$
&& $\text{NeQ}[b*c - a*d, 0]$ && $\text{IGtQ}[m, 0]$ && $(!\text{IntegerQ}[n] || (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0]) || \text{LtQ}[9*m + 5*(n + 1), 0] || \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int \frac{x^4}{(cx^2)^{3/2}(a+bx)} dx &= \frac{x \int \frac{x}{a+bx} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{1}{b} - \frac{a}{b(a+bx)}\right) dx}{c\sqrt{cx^2}} \\ &= \frac{x^2}{bc\sqrt{cx^2}} - \frac{ax \log(a+bx)}{b^2c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 0.64

$$\frac{x^3(bx - a \log(a + bx))}{b^2 (cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/((c*x^2)^(3/2)*(a + b*x)),x]

[Out] (x^3*(b*x - a*Log[a + b*x]))/(b^2*(c*x^2)^(3/2))

fricas [A] time = 0.41, size = 30, normalized size = 0.67

$$\frac{\sqrt{cx^2} (bx - a \log(bx + a))}{b^2 c^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(c*x^2)^(3/2)/(b*x+a),x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x - a*log(b*x + a))/(b^2*c^2*x)

giac [A] time = 1.09, size = 55, normalized size = 1.22

$$\frac{\frac{a \log\left(\left|-\left(\sqrt{c}x - \sqrt{cx^2}\right)b\sqrt{c} - 2ac\right|\right)}{b^2\sqrt{c}} + \frac{\sqrt{cx^2}}{bc}}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(c*x^2)^(3/2)/(b*x+a),x, algorithm="giac")

[Out] (a*log(abs(-(sqrt(c)*x - sqrt(c*x^2))*b*sqrt(c) - 2*a*c))/(b^2*sqrt(c)) + sqrt(c*x^2)/(b*c))/c

maple [A] time = 0.00, size = 29, normalized size = 0.64

$$\frac{(a \ln(bx + a) - bx) x^3}{(cx^2)^{\frac{3}{2}} b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(c*x^2)^(3/2)/(b*x+a), x)

[Out] -x^3*(a*ln(b*x+a)-b*x)/(c*x^2)^(3/2)/b^2

maxima [B] time = 1.60, size = 116, normalized size = 2.58

$$\frac{x^2}{\sqrt{cx^2} bc} - \frac{(-1)^{\frac{2acx}{b}} a \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^2 c^{\frac{3}{2}}} + \frac{2ax}{\sqrt{cx^2} b^2 c} - \frac{a \log(bx)}{b^2 c^{\frac{3}{2}}} - \frac{2a^2}{\sqrt{cx^2} b^3 c} + \frac{2a^2}{b^3 c^{\frac{3}{2}} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(c*x^2)^(3/2)/(b*x+a), x, algorithm="maxima")

[Out] x^2/(sqrt(c*x^2)*b*c) - (-1)^(2*a*c*x/b)*a*log(-2*a*c*x/(b*abs(b*x + a)))/(b^2*c^(3/2)) + 2*a*x/(sqrt(c*x^2)*b^2*c) - a*log(b*x)/(b^2*c^(3/2)) - 2*a^2/(sqrt(c*x^2)*b^3*c) + 2*a^2/(b^3*c^(3/2)*x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^4}{(cx^2)^{\frac{3}{2}} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/((c*x^2)^(3/2)*(a + b*x)), x)

[Out] int(x^4/((c*x^2)^(3/2)*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^4}{(cx^2)^{\frac{3}{2}} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/(c*x**2)**(3/2)/(b*x+a), x)

[Out] Integral(x**4/((c*x**2)**(3/2)*(a + b*x)), x)

$$3.888 \quad \int \frac{x^3}{(cx^2)^{3/2} (a+bx)} dx$$

Optimal. Leaf size=23

$$\frac{x \log(a + bx)}{bc\sqrt{cx^2}}$$

[Out] x*ln(b*x+a)/b/c/(c*x^2)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 31}

$$\frac{x \log(a + bx)}{bc\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^3/((c*x^2)^(3/2)*(a + b*x)),x]

[Out] (x*Log[a + b*x])/(b*c*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(cx^2)^{3/2} (a+bx)} dx &= \frac{x \int \frac{1}{a+bx} dx}{c\sqrt{cx^2}} \\ &= \frac{x \log(a + bx)}{bc\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 0.96

$$\frac{x^3 \log(ax + bx)}{b(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/((c*x^2)^(3/2)*(a + b*x)),x]

[Out] (x^3*Log[a + b*x])/(b*(c*x^2)^(3/2))

fricas [A] time = 0.43, size = 23, normalized size = 1.00

$$\frac{\sqrt{cx^2} \log(bx + a)}{bc^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(c*x^2)^(3/2)/(b*x+a),x, algorithm="fricas")

[Out] sqrt(c*x^2)*log(b*x + a)/(b*c^2*x)

giac [A] time = 0.97, size = 36, normalized size = 1.57

$$-\frac{\log\left(\left|-\left(\sqrt{c}x - \sqrt{cx^2}\right)b\sqrt{c} - 2ac\right|\right)}{bc^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(c*x^2)^(3/2)/(b*x+a),x, algorithm="giac")

[Out] -log(abs(-(sqrt(c)*x - sqrt(c*x^2))*b*sqrt(c) - 2*a*c))/(b*c^(3/2))

maple [A] time = 0.00, size = 21, normalized size = 0.91

$$\frac{x^3 \ln(bx + a)}{(cx^2)^{\frac{3}{2}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(c*x^2)^(3/2)/(b*x+a),x)

[Out] 1/(c*x^2)^(3/2)*x^3*ln(b*x+a)/b

maxima [B] time = 1.60, size = 74, normalized size = 3.22

$$\frac{(-1)^{\frac{2acx}{b}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{bc^{\frac{3}{2}}} + \frac{\log(bx)}{bc^{\frac{3}{2}}} + \frac{2a}{\sqrt{cx^2} b^2 c} - \frac{2a}{b^2 c^{\frac{3}{2}} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(c*x^2)^(3/2)/(b*x+a), x, algorithm="maxima")

[Out] $(-1)^{(2*a*c*x/b)} * \log(-2*a*c*x/(b*abs(b*x + a)))/(b*c^{(3/2)}) + \log(b*x)/(b*c^{(3/2)}) + 2*a/(sqrt(c*x^2)*b^2*c) - 2*a/(b^2*c^{(3/2)}*x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{x^3}{(cx^2)^{3/2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/((c*x^2)^(3/2)*(a + b*x)), x)

[Out] int(x^3/((c*x^2)^(3/2)*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^3}{(cx^2)^{\frac{3}{2}} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(c*x**2)**(3/2)/(b*x+a), x)

[Out] Integral(x**3/((c*x**2)**(3/2)*(a + b*x)), x)

$$3.889 \quad \int \frac{x^2}{(cx^2)^{3/2}(a+bx)} dx$$

Optimal. Leaf size=44

$$\frac{x \log(x)}{ac\sqrt{cx^2}} - \frac{x \log(a+bx)}{ac\sqrt{cx^2}}$$

[Out] $x*\ln(x)/a/c/(c*x^2)^{(1/2)}-x*\ln(b*x+a)/a/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 44, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {15, 36, 29, 31}

$$\frac{x \log(x)}{ac\sqrt{cx^2}} - \frac{x \log(a+bx)}{ac\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2/((c*x^2)^{(3/2)}*(a + b*x)), x]$

[Out] $(x*\text{Log}[x])/(a*c*\text{Sqrt}[c*x^2]) - (x*\text{Log}[a + b*x])/(a*c*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 29

$\text{Int}[(x_)^{(-1)}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[x], x]$

Rule 31

$\text{Int}[((a_) + (b_.)*(x_))^{(-1)}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] /;$ FreeQ[{a, b}, x]

Rule 36

$\text{Int}[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))), x_Symbol] \rightarrow \text{Dist}[b/(b*c - a*d), \text{Int}[1/(a + b*x), x], x] - \text{Dist}[d/(b*c - a*d), \text{Int}[1/(c + d*x), x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0]

Rubi steps

$$\int \frac{x^2}{(cx^2)^{3/2} (a + bx)} dx = \frac{x \int \frac{1}{x(a+bx)} dx}{c\sqrt{cx^2}}$$

$$= \frac{x \int \frac{1}{x} dx}{ac\sqrt{cx^2}} - \frac{(bx) \int \frac{1}{a+bx} dx}{ac\sqrt{cx^2}}$$

$$= \frac{x \log(x)}{ac\sqrt{cx^2}} - \frac{x \log(a + bx)}{ac\sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.61

$$\frac{x^3(\log(x) - \log(a + bx))}{a(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/((c*x^2)^(3/2)*(a + b*x)), x]

[Out] (x^3*(Log[x] - Log[a + b*x]))/(a*(c*x^2)^(3/2))

fricas [A] time = 0.43, size = 70, normalized size = 1.59

$$\left[\frac{\sqrt{cx^2} \log\left(\frac{x}{bx+a}\right)}{ac^2x}, \frac{2\sqrt{-c} \arctan\left(\frac{\sqrt{cx^2}(2bx+a)\sqrt{-c}}{acx}\right)}{ac^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(c*x^2)^(3/2)/(b*x+a), x, algorithm="fricas")

[Out] [sqrt(c*x^2)*log(x/(b*x + a))/(a*c^2*x), 2*sqrt(-c)*arctan(sqrt(c*x^2)*(2*b*x + a)*sqrt(-c)/(a*c*x))/(a*c^2)]

giac [A] time = 1.05, size = 63, normalized size = 1.43

$$\frac{\log\left(\left|-\left(\sqrt{c}x - \sqrt{cx^2}\right)b - 2a\sqrt{c}\right|\right)}{a\sqrt{c}} - \frac{\log\left(\left|-\sqrt{c}x + \sqrt{cx^2}\right|\right)}{a\sqrt{c}}$$

c

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(c*x^2)^(3/2)/(b*x+a),x, algorithm="giac")

[Out] (log(abs(-(sqrt(c)*x - sqrt(c*x^2))*b - 2*a*sqrt(c)))/(a*sqrt(c)) - log(abs(-sqrt(c)*x + sqrt(c*x^2)))/(a*sqrt(c)))/c

maple [A] time = 0.00, size = 26, normalized size = 0.59

$$\frac{(\ln(x) - \ln(bx + a)) x^3}{(c x^2)^{\frac{3}{2}} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(c*x^2)^(3/2)/(b*x+a),x)

[Out] x^3*(ln(x)-ln(b*x+a))/(c*x^2)^(3/2)/a

maxima [A] time = 1.43, size = 35, normalized size = 0.80

$$-\frac{(-1)^{\frac{2acx}{b}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{ac^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(c*x^2)^(3/2)/(b*x+a),x, algorithm="maxima")

[Out] -(-1)^(2*a*c*x/b)*log(-2*a*c*x/(b*abs(b*x + a)))/(a*c^(3/2))

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^2}{(c x^2)^{3/2} (a + b x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/((c*x^2)^(3/2)*(a + b*x)),x)

[Out] int(x^2/((c*x^2)^(3/2)*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2}{(c x^2)^{\frac{3}{2}} (a + b x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(c*x**2)**(3/2)/(b*x+a),x)

[Out] Integral(x**2/((c*x**2)**(3/2)*(a + b*x)), x)

$$3.890 \quad \int \frac{x}{(cx^2)^{3/2} (a+bx)} dx$$

Optimal. Leaf size=63

$$-\frac{bx \log(x)}{a^2 c \sqrt{cx^2}} + \frac{bx \log(a+bx)}{a^2 c \sqrt{cx^2}} - \frac{1}{ac \sqrt{cx^2}}$$

[Out] $-1/a/c/(c*x^2)^{(1/2)} - b*x*\ln(x)/a^2/c/(c*x^2)^{(1/2)} + b*x*\ln(b*x+a)/a^2/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 44}

$$-\frac{bx \log(x)}{a^2 c \sqrt{cx^2}} + \frac{bx \log(a+bx)}{a^2 c \sqrt{cx^2}} - \frac{1}{ac \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x/((c*x^2)^(3/2)*(a + b*x)), x]

[Out] $-(1/(a*c*\text{Sqrt}[c*x^2])) - (b*x*\text{Log}[x])/(a^2*c*\text{Sqrt}[c*x^2]) + (b*x*\text{Log}[a + b*x])/(a^2*c*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x}{(cx^2)^{3/2}(a+bx)} dx &= \frac{x \int \frac{1}{x^2(a+bx)} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{1}{ax^2} - \frac{b}{a^2x} + \frac{b^2}{a^2(a+bx)} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{1}{ac\sqrt{cx^2}} - \frac{bx \log(x)}{a^2c\sqrt{cx^2}} + \frac{bx \log(a+bx)}{a^2c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.56

$$\frac{x^2(bx \log(a+bx) - a - bx \log(x))}{a^2 (cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[x/((c*x^2)^(3/2)*(a + b*x)),x]

[Out] (x^2*(-a - b*x*Log[x] + b*x*Log[a + b*x]))/(a^2*(c*x^2)^(3/2))

fricas [A] time = 0.43, size = 34, normalized size = 0.54

$$\frac{\sqrt{cx^2} \left(bx \log\left(\frac{bx+a}{x}\right) - a \right)}{a^2 c^2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(c*x^2)^(3/2)/(b*x+a),x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x*log((b*x + a)/x) - a)/(a^2*c^2*x^2)

giac [A] time = 1.08, size = 91, normalized size = 1.44

$$\frac{\frac{b \log\left(\left|-\left(\sqrt{c}x-\sqrt{cx^2}\right)b-2a\sqrt{c}\right|\right)}{a^2c} - \frac{b \log\left(\left|-\sqrt{c}x+\sqrt{cx^2}\right|\right)}{a^2c}}{\sqrt{c}} - \frac{2}{\left(\sqrt{c}x-\sqrt{cx^2}\right)a\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(c*x^2)^(3/2)/(b*x+a),x, algorithm="giac")

[Out] $-(b \cdot \log(\text{abs}(-(\text{sqrt}(c) \cdot x - \text{sqrt}(c \cdot x^2))) \cdot b - 2 \cdot a \cdot \text{sqrt}(c)))/(a^2 \cdot c) - b \cdot \log(\text{abs}(-\text{sqrt}(c) \cdot x + \text{sqrt}(c \cdot x^2)))/(a^2 \cdot c) - 2/((\text{sqrt}(c) \cdot x - \text{sqrt}(c \cdot x^2)) \cdot a \cdot \text{sqrt}(c)))/\text{sqrt}(c)$

maple [A] time = 0.01, size = 33, normalized size = 0.52

$$-\frac{(bx \ln(x) - bx \ln(bx + a) + a)x^2}{(cx^2)^{\frac{3}{2}} a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x/(c \cdot x^2)^{(3/2)}/(b \cdot x + a), x)$

[Out] $-x^2 \cdot (b \cdot x \cdot \ln(x) - b \cdot x \cdot \ln(b \cdot x + a) + a)/(c \cdot x^2)^{(3/2)}/a^2$

maxima [A] time = 1.48, size = 51, normalized size = 0.81

$$\frac{(-1)^{\frac{2acx}{b}} b \log\left(-\frac{2acx}{b|bx+a|}\right)}{a^2 c^{\frac{3}{2}}} - \frac{1}{\sqrt{cx^2} ac}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x/(c \cdot x^2)^{(3/2)}/(b \cdot x + a), x, \text{algorithm}="maxima")$

[Out] $(-1)^{(2 \cdot a \cdot c \cdot x / b)} \cdot b \cdot \log(-2 \cdot a \cdot c \cdot x / (b \cdot \text{abs}(b \cdot x + a)))/(a^2 \cdot c^{(3/2)}) - 1/(\text{sqrt}(c \cdot x^2) \cdot a \cdot c)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x}{(cx^2)^{3/2} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x/((c \cdot x^2)^{(3/2)} \cdot (a + b \cdot x)), x)$

[Out] $\text{int}(x/((c \cdot x^2)^{(3/2)} \cdot (a + b \cdot x)), x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x}{(cx^2)^{\frac{3}{2}} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x/(c \cdot x^{**2})^{**}(3/2)/(b \cdot x + a), x)$

[Out] $\text{Integral}(x/((c \cdot x^{**2})^{**}(3/2) \cdot (a + b \cdot x)), x)$

$$3.891 \quad \int \frac{1}{(cx^2)^{3/2}(a+bx)} dx$$

Optimal. Leaf size=89

$$\frac{b^2x \log(x)}{a^3c\sqrt{cx^2}} - \frac{b^2x \log(a+bx)}{a^3c\sqrt{cx^2}} + \frac{b}{a^2c\sqrt{cx^2}} - \frac{1}{2acx\sqrt{cx^2}}$$

[Out] $b/a^2/c/(c*x^2)^{(1/2)}-1/2/a/c/x/(c*x^2)^{(1/2)}+b^2*x*\ln(x)/a^3/c/(c*x^2)^{(1/2)}-b^2*x*\ln(b*x+a)/a^3/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 89, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 44}

$$\frac{b^2x \log(x)}{a^3c\sqrt{cx^2}} - \frac{b^2x \log(a+bx)}{a^3c\sqrt{cx^2}} + \frac{b}{a^2c\sqrt{cx^2}} - \frac{1}{2acx\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[1/((c*x^2)^(3/2)*(a + b*x)),x]

[Out] $b/(a^2*c*\text{Sqrt}[c*x^2]) - 1/(2*a*c*x*\text{Sqrt}[c*x^2]) + (b^2*x*\text{Log}[x])/(a^3*c*\text{Sqrt}[c*x^2]) - (b^2*x*\text{Log}[a + b*x])/(a^3*c*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(cx^2)^{3/2} (a + bx)} dx &= \frac{x \int \frac{1}{x^3(a+bx)} dx}{c\sqrt{cx^2}} \\
&= \frac{x \int \left(\frac{1}{ax^3} - \frac{b}{a^2x^2} + \frac{b^2}{a^3x} - \frac{b^3}{a^3(a+bx)} \right) dx}{c\sqrt{cx^2}} \\
&= \frac{b}{a^2c\sqrt{cx^2}} - \frac{1}{2acx\sqrt{cx^2}} + \frac{b^2x \log(x)}{a^3c\sqrt{cx^2}} - \frac{b^2x \log(a + bx)}{a^3c\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 51, normalized size = 0.57

$$\frac{x(-2b^2x^2 \log(a + bx) - a(a - 2bx) + 2b^2x^2 \log(x))}{2a^3 (cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((c*x^2)^(3/2)*(a + b*x)),x]

[Out] (x*(-(a*(a - 2*b*x)) + 2*b^2*x^2*Log[x] - 2*b^2*x^2*Log[a + b*x]))/(2*a^3*(c*x^2)^(3/2))

fricas [A] time = 0.44, size = 47, normalized size = 0.53

$$\frac{(2b^2x^2 \log\left(\frac{x}{bx+a}\right) + 2abx - a^2)\sqrt{cx^2}}{2a^3c^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c*x^2)^(3/2)/(b*x+a),x, algorithm="fricas")

[Out] 1/2*(2*b^2*x^2*log(x/(b*x + a)) + 2*a*b*x - a^2)*sqrt(c*x^2)/(a^3*c^2*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

sage0*x

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c*x^2)^(3/2)/(b*x+a),x, algorithm="giac")

[Out] sage0*x

maple [A] time = 0.01, size = 49, normalized size = 0.55

$$\frac{(2b^2x^2 \ln(x) - 2b^2x^2 \ln(bx + a) + 2abx - a^2)x}{2(c x^2)^{\frac{3}{2}} a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c*x^2)^(3/2)/(b*x+a), x)

[Out] 1/2*x*(2*b^2*x^2*ln(x)-2*b^2*x^2*ln(b*x+a)+2*a*b*x-a^2)/(c*x^2)^(3/2)/a^3

maxima [A] time = 1.54, size = 65, normalized size = 0.73

$$-\frac{(-1)^{\frac{2acx}{b}} b^2 \log\left(-\frac{2acx}{b|bx+a|}\right)}{a^3 c^{\frac{3}{2}}} + \frac{b}{\sqrt{cx^2} a^2 c} - \frac{1}{2 ac^{\frac{3}{2}} x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c*x^2)^(3/2)/(b*x+a), x, algorithm="maxima")

[Out] -(-1)^(2*a*c*x/b)*b^2*log(-2*a*c*x/(b*abs(b*x + a)))/(a^3*c^(3/2)) + b/(sqrt(c*x^2)*a^2*c) - 1/2/(a*c^(3/2)*x^2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(cx^2)^{\frac{3}{2}} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((c*x^2)^(3/2)*(a + b*x)), x)

[Out] int(1/((c*x^2)^(3/2)*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(cx^2)^{\frac{3}{2}} (a + bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c*x**2)**(3/2)/(b*x+a), x)

[Out] Integral(1/((c*x**2)**(3/2)*(a + b*x)), x)

$$3.892 \quad \int \frac{1}{x(cx^2)^{3/2}(a+bx)} dx$$

Optimal. Leaf size=115

$$-\frac{b^3x \log(x)}{a^4c\sqrt{cx^2}} + \frac{b^3x \log(a+bx)}{a^4c\sqrt{cx^2}} - \frac{b^2}{a^3c\sqrt{cx^2}} + \frac{b}{2a^2cx\sqrt{cx^2}} - \frac{1}{3acx^2\sqrt{cx^2}}$$

[Out] $-b^2/a^3/c/(c*x^2)^{(1/2)}-1/3/a/c/x^2/(c*x^2)^{(1/2)}+1/2*b/a^2/c/x/(c*x^2)^{(1/2)}-b^3*x*\ln(x)/a^4/c/(c*x^2)^{(1/2)}+b^3*x*\ln(b*x+a)/a^4/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{b^2}{a^3c\sqrt{cx^2}} - \frac{b^3x \log(x)}{a^4c\sqrt{cx^2}} + \frac{b^3x \log(a+bx)}{a^4c\sqrt{cx^2}} + \frac{b}{2a^2cx\sqrt{cx^2}} - \frac{1}{3acx^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*(c*x^2)^(3/2)*(a + b*x)), x]

[Out] $-(b^2/(a^3*c*\text{Sqrt}[c*x^2])) - 1/(3*a*c*x^2*\text{Sqrt}[c*x^2]) + b/(2*a^2*c*x*\text{Sqrt}[c*x^2]) - (b^3*x*\text{Log}[x])/(a^4*c*\text{Sqrt}[c*x^2]) + (b^3*x*\text{Log}[a + b*x])/(a^4*c*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{1}{x (cx^2)^{3/2} (a + bx)} dx &= \frac{x \int \frac{1}{x^4(a+bx)} dx}{c\sqrt{cx^2}} \\
&= \frac{x \int \left(\frac{1}{ax^4} - \frac{b}{a^2x^3} + \frac{b^2}{a^3x^2} - \frac{b^3}{a^4x} + \frac{b^4}{a^4(a+bx)} \right) dx}{c\sqrt{cx^2}} \\
&= -\frac{b^2}{a^3c\sqrt{cx^2}} - \frac{1}{3acx^2\sqrt{cx^2}} + \frac{b}{2a^2cx\sqrt{cx^2}} - \frac{b^3x \log(x)}{a^4c\sqrt{cx^2}} + \frac{b^3x \log(a + bx)}{a^4c\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 66, normalized size = 0.57

$$\frac{cx^2 \left(a(-2a^2 + 3abx - 6b^2x^2) + 6b^3x^3 \log(a + bx) - 6b^3x^3 \log(x) \right)}{6a^4 (cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*(c*x^2)^(3/2)*(a + b*x)),x]

[Out] (c*x^2*(a*(-2*a^2 + 3*a*b*x - 6*b^2*x^2) - 6*b^3*x^3*Log[x] + 6*b^3*x^3*Log[a + b*x]))/(6*a^4*(c*x^2)^(5/2))

fricas [A] time = 0.42, size = 58, normalized size = 0.50

$$\frac{\left(6b^3x^3 \log\left(\frac{bx+a}{x}\right) - 6ab^2x^2 + 3a^2bx - 2a^3 \right) \sqrt{cx^2}}{6a^4c^2x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(c*x^2)^(3/2)/(b*x+a),x, algorithm="fricas")

[Out] 1/6*(6*b^3*x^3*log((b*x + a)/x) - 6*a*b^2*x^2 + 3*a^2*b*x - 2*a^3)*sqrt(c*x^2)/(a^4*c^2*x^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(cx^2)^{\frac{3}{2}} (bx + a)x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(c*x^2)^(3/2)/(b*x+a),x, algorithm="giac")

[Out] integrate(1/((c*x^2)^(3/2)*(b*x + a)*x), x)

maple [A] time = 0.01, size = 59, normalized size = 0.51

$$-\frac{6b^3x^3 \ln(x) - 6b^3x^3 \ln(bx + a) + 6ab^2x^2 - 3a^2bx + 2a^3}{6(c x^2)^{\frac{3}{2}} a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(c*x^2)^(3/2)/(b*x+a), x)

[Out] -1/6*(6*b^3*x^3*ln(x)-6*b^3*x^3*ln(b*x+a)+6*a*b^2*x^2-3*a^2*b*x+2*a^3)/(c*x^2)^(3/2)/a^4

maxima [A] time = 1.36, size = 69, normalized size = 0.60

$$\frac{b^3 \log(bx + a)}{a^4 c^{\frac{3}{2}}} - \frac{b^3 \log(x)}{a^4 c^{\frac{3}{2}}} - \frac{6b^2 \sqrt{c} x^2 - 3ab \sqrt{c} x + 2a^2 \sqrt{c}}{6a^3 c^2 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(c*x^2)^(3/2)/(b*x+a), x, algorithm="maxima")

[Out] b^3*log(b*x + a)/(a^4*c^(3/2)) - b^3*log(x)/(a^4*c^(3/2)) - 1/6*(6*b^2*sqrt(c)*x^2 - 3*a*b*sqrt(c)*x + 2*a^2*sqrt(c))/(a^3*c^2*x^3)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{x (c x^2)^{\frac{3}{2}} (a + b x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(c*x^2)^(3/2)*(a + b*x)), x)

[Out] int(1/(x*(c*x^2)^(3/2)*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{x (c x^2)^{\frac{3}{2}} (a + b x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(c*x**2)**(3/2)/(b*x+a), x)

[Out] Integral(1/(x*(c*x**2)**(3/2)*(a + b*x)), x)

$$3.893 \quad \int \frac{x^3 \sqrt{cx^2}}{(a+bx)^2} dx$$

Optimal. Leaf size=106

$$-\frac{a^4 \sqrt{cx^2}}{b^5 x(a+bx)} - \frac{4a^3 \sqrt{cx^2} \log(a+bx)}{b^5 x} + \frac{3a^2 \sqrt{cx^2}}{b^4} - \frac{ax \sqrt{cx^2}}{b^3} + \frac{x^2 \sqrt{cx^2}}{3b^2}$$

[Out] $3a^2*(c*x^2)^{(1/2)}/b^4 - a*x*(c*x^2)^{(1/2)}/b^3 + 1/3*x^2*(c*x^2)^{(1/2)}/b^2 - a^4*(c*x^2)^{(1/2)}/b^5/x/(b*x+a) - 4*a^3*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^5/x$

Rubi [A] time = 0.04, antiderivative size = 106, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^4 \sqrt{cx^2}}{b^5 x(a+bx)} + \frac{3a^2 \sqrt{cx^2}}{b^4} - \frac{4a^3 \sqrt{cx^2} \log(a+bx)}{b^5 x} - \frac{ax \sqrt{cx^2}}{b^3} + \frac{x^2 \sqrt{cx^2}}{3b^2}$$

Antiderivative was successfully verified.

[In] Int[(x^3*Sqrt[c*x^2])/(a + b*x)^2,x]

[Out] $(3*a^2*\text{Sqrt}[c*x^2])/b^4 - (a*x*\text{Sqrt}[c*x^2])/b^3 + (x^2*\text{Sqrt}[c*x^2])/(3*b^2) - (a^4*\text{Sqrt}[c*x^2])/(b^5*x*(a + b*x)) - (4*a^3*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^5*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3 \sqrt{cx^2}}{(a+bx)^2} dx &= \frac{\sqrt{cx^2} \int \frac{x^4}{(a+bx)^2} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(\frac{3a^2}{b^4} - \frac{2ax}{b^3} + \frac{x^2}{b^2} + \frac{a^4}{b^4(a+bx)^2} - \frac{4a^3}{b^4(a+bx)} \right) dx}{x} \\ &= \frac{3a^2 \sqrt{cx^2}}{b^4} - \frac{ax \sqrt{cx^2}}{b^3} + \frac{x^2 \sqrt{cx^2}}{3b^2} - \frac{a^4 \sqrt{cx^2}}{b^5 x (a+bx)} - \frac{4a^3 \sqrt{cx^2} \log(a+bx)}{b^5 x} \end{aligned}$$

Mathematica [A] time = 0.03, size = 81, normalized size = 0.76

$$\frac{cx \left(-3a^4 + 9a^3bx - 12a^3(a+bx) \log(a+bx) + 6a^2b^2x^2 - 2ab^3x^3 + b^4x^4 \right)}{3b^5 \sqrt{cx^2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*Sqrt[c*x^2])/(a + b*x)^2,x]

[Out] (c*x*(-3*a^4 + 9*a^3*b*x + 6*a^2*b^2*x^2 - 2*a*b^3*x^3 + b^4*x^4 - 12*a^3*(a + b*x)*Log[a + b*x]))/(3*b^5*Sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.42, size = 83, normalized size = 0.78

$$\frac{(b^4x^4 - 2ab^3x^3 + 6a^2b^2x^2 + 9a^3bx - 3a^4 - 12(a^3bx + a^4) \log(bx + a)) \sqrt{cx^2}}{3(b^6x^2 + ab^5x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^(1/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/3*(b^4*x^4 - 2*a*b^3*x^3 + 6*a^2*b^2*x^2 + 9*a^3*b*x - 3*a^4 - 12*(a^3*b*x + a^4)*log(b*x + a))*sqrt(c*x^2)/(b^6*x^2 + a*b^5*x)

giac [A] time = 1.00, size = 96, normalized size = 0.91

$$-\frac{1}{3} \sqrt{c} \left(\frac{12a^3 \log(|bx+a|) \operatorname{sgn}(x)}{b^5} + \frac{3a^4 \operatorname{sgn}(x)}{(bx+a)b^5} - \frac{3(4a^3 \log(|a|) + a^3) \operatorname{sgn}(x)}{b^5} - \frac{b^4x^3 \operatorname{sgn}(x) - 3ab^3x^2 \operatorname{sgn}(x)}{b^6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^(1/2)/(b*x+a)^2,x, algorithm="giac")

[Out] $-1/3*\sqrt{c}*(12*a^3*\log(\text{abs}(b*x + a))*\text{sgn}(x)/b^5 + 3*a^4*\text{sgn}(x)/((b*x + a)*b^5) - 3*(4*a^3*\log(\text{abs}(a)) + a^3)*\text{sgn}(x)/b^5 - (b^4*x^3*\text{sgn}(x) - 3*a*b^3*x^2*\text{sgn}(x) + 9*a^2*b^2*x*\text{sgn}(x))/b^6)$

maple [A] time = 0.01, size = 88, normalized size = 0.83

$$\frac{\sqrt{cx^2} \left(-b^4x^4 + 2ab^3x^3 + 12a^3bx \ln(bx + a) - 6a^2b^2x^2 + 12a^4 \ln(bx + a) - 9a^3bx + 3a^4 \right)}{3(bx + a)b^5x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^3*(c*x^2)^{(1/2)}/(b*x+a)^2, x)$

[Out] $-1/3*(c*x^2)^{(1/2)}*(-b^4*x^4+2*a*b^3*x^3+12*\ln(b*x+a)*x*a^3*b-6*a^2*b^2*x^2+12*a^4*\ln(b*x+a)-9*a^3*b*x+3*a^4)/x/b^5/(b*x+a)$

maxima [A] time = 1.52, size = 135, normalized size = 1.27

$$\frac{\sqrt{cx^2} a^3}{b^5x + ab^4} - \frac{4(-1)^{\frac{2cx}{b}} a^3 \sqrt{c} \log\left(\frac{2cx}{b}\right)}{b^5} - \frac{4(-1)^{\frac{2acx}{b}} a^3 \sqrt{c} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^5} - \frac{\sqrt{cx^2} ax}{b^3} + \frac{3\sqrt{cx^2} a^2}{b^4} + \frac{(cx^2)^{\frac{3}{2}}}{3b^2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^3*(c*x^2)^{(1/2)}/(b*x+a)^2, x, \text{algorithm}=\text{"maxima"})$

[Out] $\sqrt{c*x^2}*a^3/(b^5*x + a*b^4) - 4*(-1)^{(2*c*x/b)}*a^3*\sqrt{c}*\log(2*c*x/b)/b^5 - 4*(-1)^{(2*a*c*x/b)}*a^3*\sqrt{c}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/b^5 - \sqrt{c*x^2}*a*x/b^3 + 3*\sqrt{c*x^2}*a^2/b^4 + 1/3*(c*x^2)^{(3/2)}/(b^2*c)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^3 \sqrt{cx^2}}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((x^3*(c*x^2)^{(1/2)})/(a + b*x)^2, x)$

[Out] $\text{int}((x^3*(c*x^2)^{(1/2)})/(a + b*x)^2, x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^3 \sqrt{cx^2}}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*(c*x**2)**(1/2)/(b*x+a)**2,x)
```

```
[Out] Integral(x**3*sqrt(c*x**2)/(a + b*x)**2, x)
```

$$3.894 \quad \int \frac{x^2 \sqrt{cx^2}}{(a+bx)^2} dx$$

Optimal. Leaf size=85

$$\frac{a^3 \sqrt{cx^2}}{b^4 x(a+bx)} + \frac{3a^2 \sqrt{cx^2} \log(a+bx)}{b^4 x} - \frac{2a \sqrt{cx^2}}{b^3} + \frac{x \sqrt{cx^2}}{2b^2}$$

[Out] $-2*a*(c*x^2)^{(1/2)}/b^3+1/2*x*(c*x^2)^{(1/2)}/b^2+a^3*(c*x^2)^{(1/2)}/b^4/x/(b*x+a)+3*a^2*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^4/x$

Rubi [A] time = 0.03, antiderivative size = 85, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^3 \sqrt{cx^2}}{b^4 x(a+bx)} + \frac{3a^2 \sqrt{cx^2} \log(a+bx)}{b^4 x} - \frac{2a \sqrt{cx^2}}{b^3} + \frac{x \sqrt{cx^2}}{2b^2}$$

Antiderivative was successfully verified.

[In] `Int[(x^2*Sqrt[c*x^2])/(a + b*x)^2,x]`

[Out] $(-2*a*\text{Sqrt}[c*x^2])/b^3 + (x*\text{Sqrt}[c*x^2])/(2*b^2) + (a^3*\text{Sqrt}[c*x^2])/(b^4*x*(a + b*x)) + (3*a^2*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^4*x)$

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rule 43

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])`

Rubi steps

$$\begin{aligned} \int \frac{x^2 \sqrt{cx^2}}{(a+bx)^2} dx &= \frac{\sqrt{cx^2} \int \frac{x^3}{(a+bx)^2} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(-\frac{2a}{b^3} + \frac{x}{b^2} - \frac{a^3}{b^3(a+bx)^2} + \frac{3a^2}{b^3(a+bx)} \right) dx}{x} \\ &= -\frac{2a\sqrt{cx^2}}{b^3} + \frac{x\sqrt{cx^2}}{2b^2} + \frac{a^3\sqrt{cx^2}}{b^4x(a+bx)} + \frac{3a^2\sqrt{cx^2} \log(a+bx)}{b^4x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 70, normalized size = 0.82

$$\frac{cx(2a^3 - 4a^2bx + 6a^2(a+bx)\log(a+bx) - 3ab^2x^2 + b^3x^3)}{2b^4\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*sqrt[c*x^2])/(a + b*x)^2,x]

[Out] (c*x*(2*a^3 - 4*a^2*b*x - 3*a*b^2*x^2 + b^3*x^3 + 6*a^2*(a + b*x)*Log[a + b*x]))/(2*b^4*sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.42, size = 72, normalized size = 0.85

$$\frac{(b^3x^3 - 3ab^2x^2 - 4a^2bx + 2a^3 + 6(a^2bx + a^3)\log(bx + a))\sqrt{cx^2}}{2(b^5x^2 + ab^4x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(1/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/2*(b^3*x^3 - 3*a*b^2*x^2 - 4*a^2*b*x + 2*a^3 + 6*(a^2*b*x + a^3)*log(b*x + a))*sqrt(c*x^2)/(b^5*x^2 + a*b^4*x)

giac [A] time = 1.06, size = 80, normalized size = 0.94

$$\frac{1}{2} \sqrt{c} \left(\frac{6a^2 \log(|bx+a|) \operatorname{sgn}(x)}{b^4} + \frac{2a^3 \operatorname{sgn}(x)}{(bx+a)b^4} - \frac{2(3a^2 \log(|a|) + a^2) \operatorname{sgn}(x)}{b^4} + \frac{b^2x^2 \operatorname{sgn}(x) - 4abx \operatorname{sgn}(x)}{b^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^(1/2)/(b*x+a)^2,x, algorithm="giac")

[Out] $\frac{1}{2}\sqrt{c}(6a^2\log(\text{abs}(bx+a))\text{sgn}(x)/b^4 + 2a^3\text{sgn}(x)/((bx+a)b^4) - 2(3a^2\log(\text{abs}(a)) + a^2)\text{sgn}(x)/b^4 + (b^2x^2\text{sgn}(x) - 4abx\text{sgn}(x))/b^4)$

maple [A] time = 0.01, size = 76, normalized size = 0.89

$$\frac{\sqrt{cx^2} (b^3x^3 + 6a^2bx \ln(bx+a) - 3ab^2x^2 + 6a^3 \ln(bx+a) - 4a^2bx + 2a^3)}{2(bx+a)b^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^2(c*x^2)^{(1/2)}/(b*x+a)^2, x)$

[Out] $\frac{1}{2}(c*x^2)^{(1/2)}(b^3*x^3+6*\ln(b*x+a)*x*a^2*b-3*a*b^2*x^2+6*a^3*\ln(b*x+a)-4*a^2*b*x+2*a^3)/x/b^4/(b*x+a)$

maxima [A] time = 1.55, size = 118, normalized size = 1.39

$$-\frac{\sqrt{cx^2} a^2}{b^4x + ab^3} + \frac{3(-1)^{\frac{2cx}{b}} a^2 \sqrt{c} \log\left(\frac{2cx}{b}\right)}{b^4} + \frac{3(-1)^{\frac{2acx}{b}} a^2 \sqrt{c} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^4} + \frac{\sqrt{cx^2} x}{2b^2} - \frac{2\sqrt{cx^2} a}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^2(c*x^2)^{(1/2)}/(b*x+a)^2, x, \text{algorithm}="maxima")$

[Out] $-\sqrt{c}x^2*a^2/(b^4*x + a*b^3) + 3*(-1)^{(2*c*x/b)}*a^2*\sqrt{c}*\log(2*c*x/b)/b^4 + 3*(-1)^{(2*a*c*x/b)}*a^2*\sqrt{c}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/b^4 + 1/2*\sqrt{c}x^2*x/b^2 - 2*\sqrt{c}x^2*a/b^3$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^2 \sqrt{cx^2}}{(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((x^2(c*x^2)^{(1/2)})/(a + b*x)^2, x)$

[Out] $\text{int}((x^2(c*x^2)^{(1/2)})/(a + b*x)^2, x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2 \sqrt{cx^2}}{(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*(c*x**2)**(1/2)/(b*x+a)**2,x)
```

```
[Out] Integral(x**2*sqrt(c*x**2)/(a + b*x)**2, x)
```

$$3.895 \quad \int \frac{x\sqrt{cx^2}}{(a+bx)^2} dx$$

Optimal. Leaf size=65

$$-\frac{a^2\sqrt{cx^2}}{b^3x(a+bx)} - \frac{2a\sqrt{cx^2} \log(a+bx)}{b^3x} + \frac{\sqrt{cx^2}}{b^2}$$

[Out] $(c*x^2)^{(1/2)}/b^2 - a^2*(c*x^2)^{(1/2)}/b^3/x/(b*x+a) - 2*a*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^3/x$

Rubi [A] time = 0.02, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a^2\sqrt{cx^2}}{b^3x(a+bx)} - \frac{2a\sqrt{cx^2} \log(a+bx)}{b^3x} + \frac{\sqrt{cx^2}}{b^2}$$

Antiderivative was successfully verified.

[In] Int[(x*Sqrt[c*x^2])/(a + b*x)^2,x]

[Out] Sqrt[c*x^2]/b^2 - (a^2*Sqrt[c*x^2])/(b^3*x*(a + b*x)) - (2*a*Sqrt[c*x^2]*Log[a + b*x])/(b^3*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x\sqrt{cx^2}}{(a+bx)^2} dx &= \frac{\sqrt{cx^2} \int \frac{x^2}{(a+bx)^2} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(\frac{1}{b^2} + \frac{a^2}{b^2(a+bx)^2} - \frac{2a}{b^2(a+bx)} \right) dx}{x} \\ &= \frac{\sqrt{cx^2}}{b^2} - \frac{a^2\sqrt{cx^2}}{b^3x(a+bx)} - \frac{2a\sqrt{cx^2} \log(a+bx)}{b^3x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 53, normalized size = 0.82

$$\frac{cx(-a^2 + abx - 2a(a+bx)\log(a+bx) + b^2x^2)}{b^3\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(x*Sqrt[c*x^2])/(a + b*x)^2,x]

[Out] (c*x*(-a^2 + a*b*x + b^2*x^2 - 2*a*(a + b*x)*Log[a + b*x]))/(b^3*Sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.44, size = 57, normalized size = 0.88

$$\frac{(b^2x^2 + abx - a^2 - 2(abx + a^2)\log(bx + a))\sqrt{cx^2}}{b^4x^2 + ab^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(1/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] (b^2*x^2 + a*b*x - a^2 - 2*(a*b*x + a^2)*log(b*x + a))*sqrt(c*x^2)/(b^4*x^2 + a*b^3*x)

giac [A] time = 0.92, size = 58, normalized size = 0.89

$$\sqrt{c} \left(\frac{x\operatorname{sgn}(x)}{b^2} - \frac{2a \log(|bx+a|)\operatorname{sgn}(x)}{b^3} + \frac{(2a \log(|a|) + a)\operatorname{sgn}(x)}{b^3} - \frac{a^2\operatorname{sgn}(x)}{(bx+a)b^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(1/2)/(b*x+a)^2,x, algorithm="giac")

[Out] $\sqrt{c} \cdot (x \cdot \operatorname{sgn}(x) / b^2 - 2 \cdot a \cdot \log(\operatorname{abs}(b \cdot x + a)) \cdot \operatorname{sgn}(x) / b^3 + (2 \cdot a \cdot \log(\operatorname{abs}(a) + a) \cdot \operatorname{sgn}(x) / b^3 - a^2 \cdot \operatorname{sgn}(x) / ((b \cdot x + a) \cdot b^3))$

maple [A] time = 0.01, size = 62, normalized size = 0.95

$$-\frac{\sqrt{cx^2} (2abx \ln(bx + a) - b^2x^2 + 2a^2 \ln(bx + a) - abx + a^2)}{(bx + a)b^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{int}(x \cdot (c \cdot x^2)^{(1/2)} / (b \cdot x + a)^2, x)$

[Out] $-(c \cdot x^2)^{(1/2)} \cdot (2 \cdot \ln(b \cdot x + a) \cdot x \cdot a \cdot b - b^2 \cdot x^2 + 2 \cdot a^2 \cdot \ln(b \cdot x + a) - a \cdot b \cdot x + a^2) / x / b^3 / (b \cdot x + a)$

maxima [A] time = 1.51, size = 96, normalized size = 1.48

$$\frac{\sqrt{cx^2} a}{b^3x + ab^2} - \frac{2(-1)^{\frac{2cx}{b}} a \sqrt{c} \log\left(\frac{2cx}{b}\right)}{b^3} - \frac{2(-1)^{\frac{2acx}{b}} a \sqrt{c} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^3} + \frac{\sqrt{cx^2}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{integrate}(x \cdot (c \cdot x^2)^{(1/2)} / (b \cdot x + a)^2, x, \operatorname{algorithm}="maxima")$

[Out] $\sqrt{c \cdot x^2} \cdot a / (b^3 \cdot x + a \cdot b^2) - 2 \cdot (-1)^{(2 \cdot c \cdot x / b)} \cdot a \cdot \sqrt{c} \cdot \log(2 \cdot c \cdot x / b) / b^3 - 2 \cdot (-1)^{(2 \cdot a \cdot c \cdot x / b)} \cdot a \cdot \sqrt{c} \cdot \log(-2 \cdot a \cdot c \cdot x / (b \cdot \operatorname{abs}(b \cdot x + a))) / b^3 + \sqrt{c \cdot x^2} / b^2$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x \sqrt{cx^2}}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{int}((x \cdot (c \cdot x^2)^{(1/2)}) / (a + b \cdot x)^2, x)$

[Out] $\operatorname{int}((x \cdot (c \cdot x^2)^{(1/2)}) / (a + b \cdot x)^2, x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x \sqrt{cx^2}}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{integrate}(x \cdot (c \cdot x^2)^{(1/2)} / (b \cdot x + a)^2, x)$

[Out] $\operatorname{Integral}(x \cdot \sqrt{c \cdot x^2} / (a + b \cdot x)^2, x)$

$$3.896 \quad \int \frac{\sqrt{cx^2}}{(a+bx)^2} dx$$

Optimal. Leaf size=47

$$\frac{a\sqrt{cx^2}}{b^2x(a+bx)} + \frac{\sqrt{cx^2} \log(a+bx)}{b^2x}$$

[Out] $a*(c*x^2)^{(1/2)}/b^2/x/(b*x+a)+\ln(b*x+a)*(c*x^2)^{(1/2)}/b^2/x$

Rubi [A] time = 0.02, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$\frac{a\sqrt{cx^2}}{b^2x(a+bx)} + \frac{\sqrt{cx^2} \log(a+bx)}{b^2x}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c*x^2]/(a + b*x)^2, x]

[Out] $(a*\text{Sqrt}[c*x^2])/(b^2*x*(a + b*x)) + (\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^2*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt{cx^2}}{(a+bx)^2} dx &= \frac{\sqrt{cx^2} \int \frac{x}{(a+bx)^2} dx}{x} \\
 &= \frac{\sqrt{cx^2} \int \left(-\frac{a}{b(a+bx)^2} + \frac{1}{b(a+bx)} \right) dx}{x} \\
 &= \frac{a\sqrt{cx^2}}{b^2x(a+bx)} + \frac{\sqrt{cx^2} \log(a+bx)}{b^2x}
 \end{aligned}$$

Mathematica [A] time = 0.01, size = 36, normalized size = 0.77

$$\frac{cx((a+bx)\log(a+bx)+a)}{b^2\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]/(a + b*x)^2,x]

[Out] (c*x*(a + (a + b*x)*Log[a + b*x]))/(b^2*Sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.46, size = 38, normalized size = 0.81

$$\frac{\sqrt{cx^2}((bx+a)\log(bx+a)+a)}{b^3x^2+ab^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] sqrt(c*x^2)*((b*x + a)*log(b*x + a) + a)/(b^3*x^2 + a*b^2*x)

giac [A] time = 1.06, size = 46, normalized size = 0.98

$$-\sqrt{c} \left(\frac{(\log(|a|)+1)\operatorname{sgn}(x)}{b^2} - \frac{\log(|bx+a|)\operatorname{sgn}(x)}{b^2} - \frac{a\operatorname{sgn}(x)}{(bx+a)b^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/(b*x+a)^2,x, algorithm="giac")

[Out] -sqrt(c)*((log(abs(a)) + 1)*sgn(x)/b^2 - log(abs(b*x + a))*sgn(x)/b^2 - a*sgn(x)/((b*x + a)*b^2))

maple [A] time = 0.01, size = 41, normalized size = 0.87

$$\frac{\sqrt{cx^2} (bx \ln (bx + a) + a \ln (bx + a) + a)}{(bx + a) b^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/(b*x+a)^2,x)

[Out] (c*x^2)^(1/2)*(b*x*ln(b*x+a)+a*ln(b*x+a)+a)/x/b^2/(b*x+a)

maxima [A] time = 1.47, size = 79, normalized size = 1.68

$$\frac{(-1)^{\frac{2cx}{b}} \sqrt{c} \log\left(\frac{2cx}{b}\right)}{b^2} + \frac{(-1)^{\frac{2acx}{b}} \sqrt{c} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^2} - \frac{\sqrt{cx^2}}{b^2x + ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/(b*x+a)^2,x, algorithm="maxima")

[Out] (-1)^(2*c*x/b)*sqrt(c)*log(2*c*x/b)/b^2 + (-1)^(2*a*c*x/b)*sqrt(c)*log(-2*a*c*x/(b*abs(b*x + a)))/b^2 - sqrt(c*x^2)/(b^2*x + a*b)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{cx^2}}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/(a + b*x)^2,x)

[Out] int((c*x^2)^(1/2)/(a + b*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2}}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(1/2)/(b*x+a)**2,x)

[Out] Integral(sqrt(c*x**2)/(a + b*x)**2, x)

$$3.897 \quad \int \frac{\sqrt{cx^2}}{x(a+bx)^2} dx$$

Optimal. Leaf size=24

$$-\frac{\sqrt{cx^2}}{bx(a+bx)}$$

[Out] $-(c*x^2)^{(1/2)}/b/x/(b*x+a)$

Rubi [A] time = 0.00, antiderivative size = 24, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$-\frac{\sqrt{cx^2}}{bx(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c*x^2]/(x*(a + b*x)^2), x]

[Out] $-(\text{Sqrt}[c*x^2]/(b*x*(a + b*x)))$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2}}{x(a+bx)^2} dx &= \frac{\sqrt{cx^2} \int \frac{1}{(a+bx)^2} dx}{x} \\ &= -\frac{\sqrt{cx^2}}{bx(a+bx)} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.96

$$-\frac{cx}{b\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]/(x*(a + b*x)^2), x]

[Out] -((c*x)/(b*Sqrt[c*x^2]*(a + b*x)))

fricas [A] time = 0.49, size = 23, normalized size = 0.96

$$-\frac{\sqrt{cx^2}}{b^2x^2 + abx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x/(b*x+a)^2,x, algorithm="fricas")

[Out] -sqrt(c*x^2)/(b^2*x^2 + a*b*x)

giac [A] time = 1.02, size = 29, normalized size = 1.21

$$-\sqrt{c} \left(\frac{\operatorname{sgn}(x)}{(bx+a)b} - \frac{\operatorname{sgn}(x)}{ab} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x/(b*x+a)^2,x, algorithm="giac")

[Out] -sqrt(c)*(sgn(x)/((b*x + a)*b) - sgn(x)/(a*b))

maple [A] time = 0.00, size = 23, normalized size = 0.96

$$-\frac{\sqrt{cx^2}}{(bx+a)bx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/x/(b*x+a)^2,x)

[Out] -(c*x^2)^(1/2)/b/x/(b*x+a)

maxima [A] time = 1.36, size = 16, normalized size = 0.67

$$-\frac{\sqrt{c}}{b^2x + ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x/(b*x+a)^2,x, algorithm="maxima")

[Out] $-\sqrt{c}/(b^2x + a*b)$

mupad [B] time = 0.16, size = 22, normalized size = 0.92

$$-\frac{\sqrt{cx^2}}{bx(a+bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(1/2)/(x*(a + b*x)^2), x)`

[Out] $-(c*x^2)^{(1/2)}/(b*x*(a + b*x))$

sympy [A] time = 0.82, size = 39, normalized size = 1.62

$$\begin{cases} -\frac{\sqrt{c}\sqrt{x^2}}{abx+b^2x^2} & \text{for } b \neq 0 \\ \frac{\sqrt{c}\sqrt{x^2}}{a^2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(1/2)/x/(b*x+a)**2,x)`

[Out] `Piecewise((-sqrt(c)*sqrt(x**2)/(a*b*x + b**2*x**2), Ne(b, 0)), (sqrt(c)*sqrt(x**2)/a**2, True))`

$$3.898 \quad \int \frac{\sqrt{cx^2}}{x^2(a+bx)^2} dx$$

Optimal. Leaf size=65

$$-\frac{\sqrt{cx^2} \log(a+bx)}{a^2x} + \frac{\sqrt{cx^2} \log(x)}{a^2x} + \frac{\sqrt{cx^2}}{ax(a+bx)}$$

[Out] (c*x^2)^(1/2)/a/x/(b*x+a)+ln(x)*(c*x^2)^(1/2)/a^2/x-ln(b*x+a)*(c*x^2)^(1/2)/a^2/x

Rubi [A] time = 0.02, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{\sqrt{cx^2} \log(a+bx)}{a^2x} + \frac{\sqrt{cx^2} \log(x)}{a^2x} + \frac{\sqrt{cx^2}}{ax(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c*x^2]/(x^2*(a + b*x)^2), x]

[Out] Sqrt[c*x^2]/(a*x*(a + b*x)) + (Sqrt[c*x^2]*Log[x])/(a^2*x) - (Sqrt[c*x^2]*Log[a + b*x])/(a^2*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{cx^2}}{x^2(a+bx)^2} dx &= \frac{\sqrt{cx^2} \int \frac{1}{x(a+bx)^2} dx}{x} \\
&= \frac{\sqrt{cx^2} \int \left(\frac{1}{a^2x} - \frac{b}{a(a+bx)^2} - \frac{b}{a^2(a+bx)} \right) dx}{x} \\
&= \frac{\sqrt{cx^2}}{ax(a+bx)} + \frac{\sqrt{cx^2} \log(x)}{a^2x} - \frac{\sqrt{cx^2} \log(a+bx)}{a^2x}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 0.69

$$\frac{cx(\log(x)(a+bx) - (a+bx)\log(a+bx) + a)}{a^2\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]/(x^2*(a + b*x)^2), x]

[Out] (c*x*(a + (a + b*x)*Log[x] - (a + b*x)*Log[a + b*x]))/(a^2*Sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.43, size = 42, normalized size = 0.65

$$\frac{\sqrt{cx^2} \left((bx+a) \log\left(\frac{x}{bx+a}\right) + a \right)}{a^2bx^2 + a^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^2/(b*x+a)^2,x, algorithm="fricas")

[Out] sqrt(c*x^2)*((b*x + a)*log(x/(b*x + a)) + a)/(a^2*b*x^2 + a^3*x)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^2/(b*x+a)^2,x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
UT:sage2:=int(sage0,x);;OUTPUT:Warning, integration of abs or sign assumes
constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 52, normalized size = 0.80

$$\frac{\sqrt{cx^2} (bx \ln(x) - bx \ln(bx + a) + a \ln(x) - a \ln(bx + a) + a)}{(bx + a) a^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/x^2/(b*x+a)^2,x)

[Out] (c*x^2)^(1/2)*(b*x*ln(x)-b*x*ln(b*x+a)+a*ln(x)-a*ln(b*x+a)+a)/x/a^2/(b*x+a)

maxima [A] time = 1.32, size = 38, normalized size = 0.58

$$\frac{\sqrt{c}}{abx + a^2} - \frac{\sqrt{c} \log(bx + a)}{a^2} + \frac{\sqrt{c} \log(x)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^2/(b*x+a)^2,x, algorithm="maxima")

[Out] sqrt(c)/(a*b*x + a^2) - sqrt(c)*log(b*x + a)/a^2 + sqrt(c)*log(x)/a^2

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{cx^2}}{x^2 (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/(x^2*(a + b*x)^2),x)

[Out] int((c*x^2)^(1/2)/(x^2*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2}}{x^2 (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(1/2)/x**2/(b*x+a)**2,x)

[Out] Integral(sqrt(c*x**2)/(x**2*(a + b*x)**2), x)

$$3.899 \quad \int \frac{\sqrt{cx^2}}{x^3(a+bx)^2} dx$$

Optimal. Leaf size=87

$$-\frac{2b\sqrt{cx^2} \log(x)}{a^3x} + \frac{2b\sqrt{cx^2} \log(a+bx)}{a^3x} - \frac{b\sqrt{cx^2}}{a^2x(a+bx)} - \frac{\sqrt{cx^2}}{a^2x^2}$$

[Out] $-(c*x^2)^{(1/2)}/a^2/x^2-b*(c*x^2)^{(1/2)}/a^2/x/(b*x+a)-2*b*\ln(x)*(c*x^2)^{(1/2)}/a^3/x+2*b*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^3/x$

Rubi [A] time = 0.03, antiderivative size = 87, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{b\sqrt{cx^2}}{a^2x(a+bx)} - \frac{2b\sqrt{cx^2} \log(x)}{a^3x} + \frac{2b\sqrt{cx^2} \log(a+bx)}{a^3x} - \frac{\sqrt{cx^2}}{a^2x^2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c*x^2]/(x^3*(a + b*x)^2), x]

[Out] $-(\text{Sqrt}[c*x^2]/(a^2*x^2)) - (b*\text{Sqrt}[c*x^2])/(a^2*x*(a + b*x)) - (2*b*\text{Sqrt}[c*x^2]*\text{Log}[x])/(a^3*x) + (2*b*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(a^3*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{cx^2}}{x^3(a+bx)^2} dx &= \frac{\sqrt{cx^2} \int \frac{1}{x^2(a+bx)^2} dx}{x} \\
&= \frac{\sqrt{cx^2} \int \left(\frac{1}{a^2x^2} - \frac{2b}{a^3x} + \frac{b^2}{a^2(a+bx)^2} + \frac{2b^2}{a^3(a+bx)} \right) dx}{x} \\
&= -\frac{\sqrt{cx^2}}{a^2x^2} - \frac{b\sqrt{cx^2}}{a^2x(a+bx)} - \frac{2b\sqrt{cx^2} \log(x)}{a^3x} + \frac{2b\sqrt{cx^2} \log(a+bx)}{a^3x}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 57, normalized size = 0.66

$$-\frac{c(a(a+2bx) + 2bx \log(x)(a+bx) - 2bx(a+bx) \log(a+bx))}{a^3\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]/(x^3*(a + b*x)^2), x]

[Out] -((c*(a*(a + 2*b*x) + 2*b*x*(a + b*x)*Log[x] - 2*b*x*(a + b*x)*Log[a + b*x]))/(a^3*Sqrt[c*x^2]*(a + b*x)))

fricas [A] time = 0.44, size = 60, normalized size = 0.69

$$-\frac{\left(2abx + a^2 - 2(b^2x^2 + abx) \log\left(\frac{bx+a}{x}\right)\right)\sqrt{cx^2}}{a^3bx^3 + a^4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^3/(b*x+a)^2,x, algorithm="fricas")

[Out] -(2*a*b*x + a^2 - 2*(b^2*x^2 + a*b*x)*log((b*x + a)/x))*sqrt(c*x^2)/(a^3*b*x^3 + a^4*x^2)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^3/(b*x+a)^2,x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x);;OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 74, normalized size = 0.85

$$\frac{\sqrt{cx^2} (2b^2x^2 \ln(x) - 2b^2x^2 \ln(bx + a) + 2abx \ln(x) - 2abx \ln(bx + a) + 2abx + a^2)}{(bx + a)a^3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/x^3/(b*x+a)^2,x)

[Out] -(c*x^2)^(1/2)*(2*b^2*x^2*ln(x)-2*b^2*x^2*ln(b*x+a)+2*a*b*x*ln(x)-2*a*b*x*ln(b*x+a)+2*a*b*x+a^2)/x^2/a^3/(b*x+a)

maxima [A] time = 1.40, size = 58, normalized size = 0.67

$$-\frac{2b\sqrt{c}x + a\sqrt{c}}{a^2bx^2 + a^3x} + \frac{2b\sqrt{c} \log(bx + a)}{a^3} - \frac{2b\sqrt{c} \log(x)}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^3/(b*x+a)^2,x, algorithm="maxima")

[Out] -(2*b*sqrt(c)*x + a*sqrt(c))/(a^2*b*x^2 + a^3*x) + 2*b*sqrt(c)*log(b*x + a)/a^3 - 2*b*sqrt(c)*log(x)/a^3

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\sqrt{cx^2}}{x^3(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/(x^3*(a + b*x)^2),x)

[Out] int((c*x^2)^(1/2)/(x^3*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2}}{x^3(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(1/2)/x**3/(b*x+a)**2,x)

[Out] Integral(sqrt(c*x**2)/(x**3*(a + b*x)**2), x)

$$3.900 \quad \int \frac{\sqrt{cx^2}}{x^4(a+bx)^2} dx$$

Optimal. Leaf size=112

$$\frac{3b^2\sqrt{cx^2} \log(x)}{a^4x} - \frac{3b^2\sqrt{cx^2} \log(a+bx)}{a^4x} + \frac{b^2\sqrt{cx^2}}{a^3x(a+bx)} + \frac{2b\sqrt{cx^2}}{a^3x^2} - \frac{\sqrt{cx^2}}{2a^2x^3}$$

[Out] $-1/2*(c*x^2)^{(1/2)}/a^2/x^3+2*b*(c*x^2)^{(1/2)}/a^3/x^2+b^2*(c*x^2)^{(1/2)}/a^3/x/(b*x+a)+3*b^2*\ln(x)*(c*x^2)^{(1/2)}/a^4/x-3*b^2*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^4/x$

Rubi [A] time = 0.04, antiderivative size = 112, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$\frac{b^2\sqrt{cx^2}}{a^3x(a+bx)} + \frac{3b^2\sqrt{cx^2} \log(x)}{a^4x} - \frac{3b^2\sqrt{cx^2} \log(a+bx)}{a^4x} + \frac{2b\sqrt{cx^2}}{a^3x^2} - \frac{\sqrt{cx^2}}{2a^2x^3}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c*x^2]/(x^4*(a + b*x)^2), x]

[Out] $-\text{Sqrt}[c*x^2]/(2*a^2*x^3) + (2*b*\text{Sqrt}[c*x^2])/(a^3*x^2) + (b^2*\text{Sqrt}[c*x^2])/(a^3*x*(a + b*x)) + (3*b^2*\text{Sqrt}[c*x^2]*\text{Log}[x])/(a^4*x) - (3*b^2*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(a^4*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2}}{x^4(a+bx)^2} dx &= \frac{\sqrt{cx^2} \int \frac{1}{x^3(a+bx)^2} dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(\frac{1}{a^2x^3} - \frac{2b}{a^3x^2} + \frac{3b^2}{a^4x} - \frac{b^3}{a^3(a+bx)^2} - \frac{3b^3}{a^4(a+bx)} \right) dx}{x} \\ &= -\frac{\sqrt{cx^2}}{2a^2x^3} + \frac{2b\sqrt{cx^2}}{a^3x^2} + \frac{b^2\sqrt{cx^2}}{a^3x(a+bx)} + \frac{3b^2\sqrt{cx^2} \log(x)}{a^4x} - \frac{3b^2\sqrt{cx^2} \log(a+bx)}{a^4x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 82, normalized size = 0.73

$$\frac{\sqrt{cx^2} \left(a(-a^2 + 3abx + 6b^2x^2) + 6b^2x^2 \log(x)(a+bx) - 6b^2x^2(a+bx) \log(a+bx) \right)}{2a^4x^3(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]/(x^4*(a + b*x)^2),x]

[Out] (Sqrt[c*x^2]*(a*(-a^2 + 3*a*b*x + 6*b^2*x^2) + 6*b^2*x^2*(a + b*x)*Log[x] - 6*b^2*x^2*(a + b*x)*Log[a + b*x]))/(2*a^4*x^3*(a + b*x))

fricas [A] time = 0.50, size = 77, normalized size = 0.69

$$\frac{\left(6ab^2x^2 + 3a^2bx - a^3 + 6(b^3x^3 + ab^2x^2) \log\left(\frac{x}{bx+a}\right) \right) \sqrt{cx^2}}{2(a^4bx^4 + a^5x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^4/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/2*(6*a*b^2*x^2 + 3*a^2*b*x - a^3 + 6*(b^3*x^3 + a*b^2*x^2)*log(x/(b*x + a)))*sqrt(c*x^2)/(a^4*b*x^4 + a^5*x^3)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^4/(b*x+a)^2,x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x)::OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.02, size = 95, normalized size = 0.85

$$\frac{\sqrt{cx^2} (6b^3x^3 \ln(x) - 6b^3x^3 \ln(bx + a) + 6ab^2x^2 \ln(x) - 6ab^2x^2 \ln(bx + a) + 6ab^2x^2 + 3a^2bx - a^3)}{2(bx + a)a^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/x^4/(b*x+a)^2,x)

[Out] 1/2*(c*x^2)^(1/2)*(6*b^3*x^3*ln(x)-6*b^3*x^3*ln(b*x+a)+6*ln(x)*x^2*a*b^2-6*ln(b*x+a)*x^2*a*b^2+6*a*b^2*x^2+3*a^2*b*x-a^3)/x^3/a^4/(b*x+a)

maxima [A] time = 1.42, size = 79, normalized size = 0.71

$$\frac{6b^2\sqrt{c}x^2 + 3ab\sqrt{c}x - a^2\sqrt{c}}{2(a^3bx^3 + a^4x^2)} - \frac{3b^2\sqrt{c} \log(bx + a)}{a^4} + \frac{3b^2\sqrt{c} \log(x)}{a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(1/2)/x^4/(b*x+a)^2,x, algorithm="maxima")

[Out] 1/2*(6*b^2*sqrt(c)*x^2 + 3*a*b*sqrt(c)*x - a^2*sqrt(c))/(a^3*b*x^3 + a^4*x^2) - 3*b^2*sqrt(c)*log(b*x + a)/a^4 + 3*b^2*sqrt(c)*log(x)/a^4

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\sqrt{cx^2}}{x^4(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(1/2)/(x^4*(a + b*x)^2),x)

[Out] int((c*x^2)^(1/2)/(x^4*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2}}{x^4(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(1/2)/x**4/(b*x+a)**2,x)

[Out] Integral(sqrt(c*x**2)/(x**4*(a + b*x)**2), x)

$$3.901 \quad \int \frac{x(cx^2)^{3/2}}{(a+bx)^2} dx$$

Optimal. Leaf size=111

$$-\frac{a^4c\sqrt{cx^2}}{b^5x(a+bx)} - \frac{4a^3c\sqrt{cx^2} \log(a+bx)}{b^5x} + \frac{3a^2c\sqrt{cx^2}}{b^4} - \frac{acx\sqrt{cx^2}}{b^3} + \frac{cx^2\sqrt{cx^2}}{3b^2}$$

[Out] $3a^2c*(cx^2)^{(1/2)}/b^4 - a*c*x*(cx^2)^{(1/2)}/b^3 + 1/3*c*x^2*(cx^2)^{(1/2)}/b^2 - a^4*c*(cx^2)^{(1/2)}/b^5/x - (b*x+a)^{-4}*a^3*c*\ln(b*x+a)*(cx^2)^{(1/2)}/b^5/x$

Rubi [A] time = 0.04, antiderivative size = 111, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$-\frac{a^4c\sqrt{cx^2}}{b^5x(a+bx)} + \frac{3a^2c\sqrt{cx^2}}{b^4} - \frac{4a^3c\sqrt{cx^2} \log(a+bx)}{b^5x} - \frac{acx\sqrt{cx^2}}{b^3} + \frac{cx^2\sqrt{cx^2}}{3b^2}$$

Antiderivative was successfully verified.

[In] `Int[(x*(c*x^2)^(3/2))/(a + b*x)^2, x]`

[Out] $(3a^2c*\text{Sqrt}[cx^2])/b^4 - (a*c*x*\text{Sqrt}[cx^2])/b^3 + (cx^2*\text{Sqrt}[cx^2])/(3b^2) - (a^4*c*\text{Sqrt}[cx^2])/(b^5*x*(a + b*x)) - (4a^3*c*\text{Sqrt}[cx^2]*\text{Log}[a + b*x])/(b^5*x)$

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rule 43

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])`

Rubi steps

$$\begin{aligned} \int \frac{x (cx^2)^{3/2}}{(a+bx)^2} dx &= \frac{(c\sqrt{cx^2}) \int \frac{x^4}{(a+bx)^2} dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int \left(\frac{3a^2}{b^4} - \frac{2ax}{b^3} + \frac{x^2}{b^2} + \frac{a^4}{b^4(a+bx)^2} - \frac{4a^3}{b^4(a+bx)} \right) dx}{x} \\ &= \frac{3a^2c\sqrt{cx^2}}{b^4} - \frac{acx\sqrt{cx^2}}{b^3} + \frac{cx^2\sqrt{cx^2}}{3b^2} - \frac{a^4c\sqrt{cx^2}}{b^5x(a+bx)} - \frac{4a^3c\sqrt{cx^2} \log(a+bx)}{b^5x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 82, normalized size = 0.74

$$\frac{(cx^2)^{3/2} (-3a^4 + 9a^3bx - 12a^3(a+bx) \log(a+bx) + 6a^2b^2x^2 - 2ab^3x^3 + b^4x^4)}{3b^5x^3(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(x*(c*x^2)^(3/2))/(a + b*x)^2,x]

[Out] ((c*x^2)^(3/2)*(-3*a^4 + 9*a^3*b*x + 6*a^2*b^2*x^2 - 2*a*b^3*x^3 + b^4*x^4 - 12*a^3*(a + b*x)*Log[a + b*x]))/(3*b^5*x^3*(a + b*x))

fricas [A] time = 0.42, size = 91, normalized size = 0.82

$$\frac{(b^4cx^4 - 2ab^3cx^3 + 6a^2b^2cx^2 + 9a^3bcx - 3a^4c - 12(a^3bcx + a^4c) \log(bx + a))\sqrt{cx^2}}{3(b^6x^2 + ab^5x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/3*(b^4*c*x^4 - 2*a*b^3*c*x^3 + 6*a^2*b^2*c*x^2 + 9*a^3*b*c*x - 3*a^4*c - 12*(a^3*b*c*x + a^4*c)*log(b*x + a))*sqrt(c*x^2)/(b^6*x^2 + a*b^5*x)

giac [A] time = 1.17, size = 96, normalized size = 0.86

$$-\frac{1}{3}c^{\frac{3}{2}} \left(\frac{12a^3 \log(|bx+a|) \operatorname{sgn}(x)}{b^5} + \frac{3a^4 \operatorname{sgn}(x)}{(bx+a)b^5} - \frac{3(4a^3 \log(|a|) + a^3) \operatorname{sgn}(x)}{b^5} - \frac{b^4x^3 \operatorname{sgn}(x) - 3ab^3x^2 \operatorname{sgn}(x) + \dots}{b^6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="giac")

[Out] $-1/3*c^{(3/2)}*(12*a^3*\log(\text{abs}(b*x + a))*\text{sgn}(x)/b^5 + 3*a^4*\text{sgn}(x)/((b*x + a)*b^5) - 3*(4*a^3*\log(\text{abs}(a)) + a^3)*\text{sgn}(x)/b^5 - (b^4*x^3*\text{sgn}(x) - 3*a*b^3*x^2*\text{sgn}(x) + 9*a^2*b^2*x*\text{sgn}(x))/b^6)$

maple [A] time = 0.01, size = 88, normalized size = 0.79

$$\frac{(cx^2)^{\frac{3}{2}}(-b^4x^4 + 2ab^3x^3 + 12a^3bx \ln(bx + a) - 6a^2b^2x^2 + 12a^4 \ln(bx + a) - 9a^3bx + 3a^4)}{3(bx + a)b^5x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x*(c*x^2)^{(3/2)}/(b*x+a)^2, x)$

[Out] $-1/3*(c*x^2)^{(3/2)}*(-b^4*x^4+2*a*b^3*x^3+12*a^3*b*x*\ln(b*x+a)-6*a^2*b^2*x^2+12*a^4*\ln(b*x+a)-9*a^3*b*x+3*a^4)/x^3/b^5/(b*x+a)$

maxima [A] time = 1.62, size = 132, normalized size = 1.19

$$\frac{(cx^2)^{\frac{3}{2}}a}{b^3x + ab^2} - \frac{4(-1)^{\frac{2cx}{b}}a^3c^{\frac{3}{2}}\log\left(\frac{2cx}{b}\right)}{b^5} - \frac{4(-1)^{\frac{2acx}{b}}a^3c^{\frac{3}{2}}\log\left(-\frac{2acx}{b|bx+a|}\right)}{b^5} - \frac{2\sqrt{cx^2}acx}{b^3} + \frac{(cx^2)^{\frac{3}{2}}}{3b^2} + \frac{4\sqrt{cx^2}a^2c}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x*(c*x^2)^{(3/2)}/(b*x+a)^2, x, \text{algorithm}=\text{"maxima"})$

[Out] $(c*x^2)^{(3/2)}*a/(b^3*x + a*b^2) - 4*(-1)^{(2*c*x/b)}*a^3*c^{(3/2)}*\log(2*c*x/b)/b^5 - 4*(-1)^{(2*a*c*x/b)}*a^3*c^{(3/2)}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/b^5 - 2*\text{sqrt}(c*x^2)*a*c*x/b^3 + 1/3*(c*x^2)^{(3/2)}/b^2 + 4*\text{sqrt}(c*x^2)*a^2*c/b^4$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x (cx^2)^{3/2}}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((x*(c*x^2)^{(3/2)})/(a + b*x)^2, x)$

[Out] $\text{int}((x*(c*x^2)^{(3/2)})/(a + b*x)^2, x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x (cx^2)^{\frac{3}{2}}}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*(c*x**2)**(3/2)/(b*x+a)**2,x)
```

```
[Out] Integral(x*(c*x**2)**(3/2)/(a + b*x)**2, x)
```

$$3.902 \quad \int \frac{(cx^2)^{3/2}}{(a+bx)^2} dx$$

Optimal. Leaf size=89

$$\frac{a^3c\sqrt{cx^2}}{b^4x(a+bx)} + \frac{3a^2c\sqrt{cx^2} \log(a+bx)}{b^4x} - \frac{2ac\sqrt{cx^2}}{b^3} + \frac{cx\sqrt{cx^2}}{2b^2}$$

[Out] $-2*a*c*(c*x^2)^{(1/2)}/b^3+1/2*c*x*(c*x^2)^{(1/2)}/b^2+a^3*c*(c*x^2)^{(1/2)}/b^4/x/(b*x+a)+3*a^2*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^4/x$

Rubi [A] time = 0.03, antiderivative size = 89, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$\frac{a^3c\sqrt{cx^2}}{b^4x(a+bx)} + \frac{3a^2c\sqrt{cx^2} \log(a+bx)}{b^4x} - \frac{2ac\sqrt{cx^2}}{b^3} + \frac{cx\sqrt{cx^2}}{2b^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}/(a+b*x)^2, x]$

[Out] $(-2*a*c*\text{Sqrt}[c*x^2])/b^3 + (c*x*\text{Sqrt}[c*x^2])/(2*b^2) + (a^3*c*\text{Sqrt}[c*x^2])/(b^4*x*(a+b*x)) + (3*a^2*c*\text{Sqrt}[c*x^2]*\text{Log}[a+b*x])/(b^4*x)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a+b*x)^m*(c+d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{3/2}}{(a+bx)^2} dx &= \frac{(c\sqrt{cx^2}) \int \frac{x^3}{(a+bx)^2} dx}{x} \\
&= \frac{(c\sqrt{cx^2}) \int \left(-\frac{2a}{b^3} + \frac{x}{b^2} - \frac{a^3}{b^3(a+bx)^2} + \frac{3a^2}{b^3(a+bx)} \right) dx}{x} \\
&= -\frac{2ac\sqrt{cx^2}}{b^3} + \frac{cx\sqrt{cx^2}}{2b^2} + \frac{a^3c\sqrt{cx^2}}{b^4x(a+bx)} + \frac{3a^2c\sqrt{cx^2} \log(a+bx)}{b^4x}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 71, normalized size = 0.80

$$\frac{(cx^2)^{3/2} (2a^3 - 4a^2bx + 6a^2(a+bx) \log(a+bx) - 3ab^2x^2 + b^3x^3)}{2b^4x^3(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(a + b*x)^2,x]

[Out] ((c*x^2)^(3/2)*(2*a^3 - 4*a^2*b*x - 3*a*b^2*x^2 + b^3*x^3 + 6*a^2*(a + b*x)*Log[a + b*x]))/(2*b^4*x^3*(a + b*x))

fricas [A] time = 0.45, size = 79, normalized size = 0.89

$$\frac{(b^3cx^3 - 3ab^2cx^2 - 4a^2bcx + 2a^3c + 6(a^2bcx + a^3c) \log(bx + a))\sqrt{cx^2}}{2(b^5x^2 + ab^4x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/2*(b^3*c*x^3 - 3*a*b^2*c*x^2 - 4*a^2*b*c*x + 2*a^3*c + 6*(a^2*b*c*x + a^3*c)*log(b*x + a))*sqrt(c*x^2)/(b^5*x^2 + a*b^4*x)

giac [A] time = 0.95, size = 80, normalized size = 0.90

$$\frac{1}{2} c^{\frac{3}{2}} \left(\frac{6a^2 \log(|bx+a|) \operatorname{sgn}(x)}{b^4} + \frac{2a^3 \operatorname{sgn}(x)}{(bx+a)b^4} - \frac{2(3a^2 \log(|a|) + a^2) \operatorname{sgn}(x)}{b^4} + \frac{b^2x^2 \operatorname{sgn}(x) - 4abx \operatorname{sgn}(x)}{b^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="giac")

[Out] $\frac{1}{2}c^{3/2}(6a^2\log(\text{abs}(bx+a))\text{sgn}(x)/b^4 + 2a^3\text{sgn}(x)/((bx+a)b^4) - 2(3a^2\log(\text{abs}(a)) + a^2)\text{sgn}(x)/b^4 + (b^2x^2\text{sgn}(x) - 4abx\text{sgn}(x))/b^4)$

maple [A] time = 0.00, size = 76, normalized size = 0.85

$$\frac{(cx^2)^{\frac{3}{2}}(b^3x^3 + 6a^2bx \ln(bx+a) - 3ab^2x^2 + 6a^3 \ln(bx+a) - 4a^2bx + 2a^3)}{2(bx+a)b^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)/(b*x+a)^2,x)`

[Out] $\frac{1}{2}(c*x^2)^{3/2}(b^3*x^3+6*a^2*b*x*\ln(b*x+a)-3*a*b^2*x^2+6*a^3*\ln(b*x+a)-4*a^2*b*x+2*a^3)/x^3/b^4/(b*x+a)$

maxima [A] time = 1.55, size = 115, normalized size = 1.29

$$\frac{3(-1)^{\frac{2cx}{b}}a^2c^{\frac{3}{2}}\log\left(\frac{2cx}{b}\right)}{b^4} + \frac{3(-1)^{\frac{2acx}{b}}a^2c^{\frac{3}{2}}\log\left(-\frac{2acx}{b|bx+a|}\right)}{b^4} - \frac{(cx^2)^{\frac{3}{2}}}{b^2x+ab} + \frac{3\sqrt{cx^2}cx}{2b^2} - \frac{3\sqrt{cx^2}ac}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="maxima")`

[Out] $3*(-1)^{(2*c*x/b)}*a^2*c^{3/2}*\log(2*c*x/b)/b^4 + 3*(-1)^{(2*a*c*x/b)}*a^2*c^{3/2}*\log(-2*a*c*x/(b*\text{abs}(b*x+a)))/b^4 - (c*x^2)^{3/2}/(b^2*x+a*b) + 3/2*\text{sqrt}(c*x^2)*c*x/b^2 - 3*\text{sqrt}(c*x^2)*a*c/b^3$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{3/2}}{(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)/(a+b*x)^2,x)`

[Out] `int((c*x^2)^(3/2)/(a+b*x)^2,x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((c*x**2)**(3/2)/(b*x+a)**2,x)
```

```
[Out] Integral((c*x**2)**(3/2)/(a + b*x)**2, x)
```

$$3.903 \quad \int \frac{(cx^2)^{3/2}}{x(a+bx)^2} dx$$

Optimal. Leaf size=68

$$-\frac{a^2c\sqrt{cx^2}}{b^3x(a+bx)} - \frac{2ac\sqrt{cx^2} \log(a+bx)}{b^3x} + \frac{c\sqrt{cx^2}}{b^2}$$

[Out] $c*(c*x^2)^{(1/2)}/b^2-a^2*c*(c*x^2)^{(1/2)}/b^3/x/(b*x+a)-2*a*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/b^3/x$

Rubi [A] time = 0.02, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2c\sqrt{cx^2}}{b^3x(a+bx)} - \frac{2ac\sqrt{cx^2} \log(a+bx)}{b^3x} + \frac{c\sqrt{cx^2}}{b^2}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(3/2)/(x*(a + b*x)^2), x]

[Out] $(c*\text{Sqrt}[c*x^2])/b^2 - (a^2*c*\text{Sqrt}[c*x^2])/(b^3*x*(a + b*x)) - (2*a*c*\text{Sqrt}[c*x^2]*\text{Log}[a + b*x])/(b^3*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2}}{x(a+bx)^2} dx &= \frac{(c\sqrt{cx^2}) \int \frac{x^2}{(a+bx)^2} dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int \left(\frac{1}{b^2} + \frac{a^2}{b^2(a+bx)^2} - \frac{2a}{b^2(a+bx)} \right) dx}{x} \\ &= \frac{c\sqrt{cx^2}}{b^2} - \frac{a^2c\sqrt{cx^2}}{b^3x(a+bx)} - \frac{2ac\sqrt{cx^2} \log(a+bx)}{b^3x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 55, normalized size = 0.81

$$\frac{c^2x(-a^2 + abx - 2a(a+bx)\log(a+bx) + b^2x^2)}{b^3\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x*(a + b*x)^2), x]

[Out] (c^2*x*(-a^2 + a*b*x + b^2*x^2 - 2*a*(a + b*x)*Log[a + b*x]))/(b^3*Sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.44, size = 63, normalized size = 0.93

$$\frac{(b^2cx^2 + abcx - a^2c - 2(abcx + a^2c)\log(bx + a))\sqrt{cx^2}}{b^4x^2 + ab^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x/(b*x+a)^2,x, algorithm="fricas")

[Out] (b^2*c*x^2 + a*b*c*x - a^2*c - 2*(a*b*c*x + a^2*c)*log(b*x + a))*sqrt(c*x^2)/(b^4*x^2 + a*b^3*x)

giac [A] time = 0.96, size = 58, normalized size = 0.85

$$c^{\frac{3}{2}} \left(\frac{x \operatorname{sgn}(x)}{b^2} - \frac{2a \log(|bx+a|) \operatorname{sgn}(x)}{b^3} + \frac{(2a \log(|a|) + a) \operatorname{sgn}(x)}{b^3} - \frac{a^2 \operatorname{sgn}(x)}{(bx+a)b^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x/(b*x+a)^2,x, algorithm="giac")

[Out] $c^{(3/2)}*(x*\text{sgn}(x)/b^2 - 2*a*\log(\text{abs}(b*x + a))*\text{sgn}(x)/b^3 + (2*a*\log(\text{abs}(a)) + a)*\text{sgn}(x)/b^3 - a^2*\text{sgn}(x)/((b*x + a)*b^3))$

maple [A] time = 0.01, size = 62, normalized size = 0.91

$$\frac{(cx^2)^{\frac{3}{2}} (2abx \ln(bx + a) - b^2x^2 + 2a^2 \ln(bx + a) - abx + a^2)}{(bx + a)b^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((c*x^2)^{(3/2)}/x/(b*x+a)^2,x)$

[Out] $-(c*x^2)^{(3/2)}*(2*a*b*x*\ln(b*x+a)-b^2*x^2+2*a^2*\ln(b*x+a)-a*b*x+a^2)/x^3/b^3/(b*x+a)$

maxima [A] time = 1.42, size = 98, normalized size = 1.44

$$\frac{\sqrt{cx^2} ac}{b^3x + ab^2} - \frac{2(-1)^{\frac{2cx}{b}} ac^{\frac{3}{2}} \log\left(\frac{2cx}{b}\right)}{b^3} - \frac{2(-1)^{\frac{2acx}{b}} ac^{\frac{3}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^3} + \frac{\sqrt{cx^2} c}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((c*x^2)^{(3/2)}/x/(b*x+a)^2,x, \text{algorithm}="maxima")$

[Out] $\text{sqrt}(c*x^2)*a*c/(b^3*x + a*b^2) - 2*(-1)^{(2*c*x/b)}*a*c^{(3/2)}*\log(2*c*x/b)/b^3 - 2*(-1)^{(2*a*c*x/b)}*a*c^{(3/2)}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/b^3 + \text{sqrt}(c*x^2)*c/b^2$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{3/2}}{x(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((c*x^2)^{(3/2)}/(x*(a + b*x)^2),x)$

[Out] $\text{int}((c*x^2)^{(3/2)}/(x*(a + b*x)^2), x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((c*x**2)**(3/2)/x/(b*x+a)**2,x)
```

```
[Out] Integral((c*x**2)**(3/2)/(x*(a + b*x)**2), x)
```

$$3.904 \quad \int \frac{(cx^2)^{3/2}}{x^2(a+bx)^2} dx$$

Optimal. Leaf size=49

$$\frac{ac\sqrt{cx^2}}{b^2x(a+bx)} + \frac{c\sqrt{cx^2} \log(a+bx)}{b^2x}$$

[Out] a*c*(c*x^2)^(1/2)/b^2/x/(b*x+a)+c*ln(b*x+a)*(c*x^2)^(1/2)/b^2/x

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{ac\sqrt{cx^2}}{b^2x(a+bx)} + \frac{c\sqrt{cx^2} \log(a+bx)}{b^2x}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^(3/2)/(x^2*(a + b*x)^2), x]

[Out] (a*c*Sqrt[c*x^2])/(b^2*x*(a + b*x)) + (c*Sqrt[c*x^2]*Log[a + b*x])/(b^2*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2}}{x^2(a+bx)^2} dx &= \frac{(c\sqrt{cx^2})}{x} \int \frac{x}{(a+bx)^2} dx \\ &= \frac{(c\sqrt{cx^2})}{x} \int \left(-\frac{a}{b(a+bx)^2} + \frac{1}{b(a+bx)} \right) dx \\ &= \frac{ac\sqrt{cx^2}}{b^2x(a+bx)} + \frac{c\sqrt{cx^2} \log(a+bx)}{b^2x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 38, normalized size = 0.78

$$\frac{c^2x((a+bx)\log(a+bx)+a)}{b^2\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^2*(a+b*x)^2),x]

[Out] (c^2*x*(a+(a+b*x)*Log[a+b*x]))/(b^2*Sqrt[c*x^2]*(a+b*x))

fricas [A] time = 0.42, size = 43, normalized size = 0.88

$$\frac{\sqrt{cx^2}(ac+(bcx+ac)\log(bx+a))}{b^3x^2+ab^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^2/(b*x+a)^2,x, algorithm="fricas")

[Out] sqrt(c*x^2)*(a*c+(b*c*x+a*c)*log(b*x+a))/(b^3*x^2+a*b^2*x)

giac [A] time = 0.96, size = 46, normalized size = 0.94

$$-c^{\frac{3}{2}} \left(\frac{(\log(|a|)+1)\operatorname{sgn}(x)}{b^2} - \frac{\log(|bx+a|)\operatorname{sgn}(x)}{b^2} - \frac{a\operatorname{sgn}(x)}{(bx+a)b^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^2/(b*x+a)^2,x, algorithm="giac")

[Out] -c^(3/2)*((log(abs(a))+1)*sgn(x)/b^2 - log(abs(b*x+a))*sgn(x)/b^2 - a*sgn(x)/((b*x+a)*b^2))

maple [A] time = 0.00, size = 41, normalized size = 0.84

$$\frac{(cx^2)^{\frac{3}{2}}(bx \ln(bx+a) + a \ln(bx+a) + a)}{(bx+a)b^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x^2/(b*x+a)^2,x)

[Out] (c*x^2)^(3/2)*(b*x*ln(b*x+a)+a*ln(b*x+a)+a)/x^3/b^2/(b*x+a)

maxima [A] time = 1.48, size = 80, normalized size = 1.63

$$\frac{(-1)^{\frac{2cx}{b}} c^{\frac{3}{2}} \log\left(\frac{2cx}{b}\right)}{b^2} + \frac{(-1)^{\frac{2acx}{b}} c^{\frac{3}{2}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^2} - \frac{\sqrt{cx^2} c}{b^2x + ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^2/(b*x+a)^2,x, algorithm="maxima")

[Out] (-1)^(2*c*x/b)*c^(3/2)*log(2*c*x/b)/b^2 + (-1)^(2*a*c*x/b)*c^(3/2)*log(-2*a*c*x/(b*abs(b*x + a)))/b^2 - sqrt(c*x^2)*c/(b^2*x + a*b)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{3/2}}{x^2(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(x^2*(a + b*x)^2),x)

[Out] int((c*x^2)^(3/2)/(x^2*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^2(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)/x**2/(b*x+a)**2,x)

[Out] Integral((c*x**2)**(3/2)/(x**2*(a + b*x)**2), x)

$$3.905 \quad \int \frac{(cx^2)^{3/2}}{x^3(a+bx)^2} dx$$

Optimal. Leaf size=25

$$-\frac{c\sqrt{cx^2}}{bx(a+bx)}$$

[Out] $-c*(c*x^2)^{(1/2)}/b/x/(b*x+a)$

Rubi [A] time = 0.00, antiderivative size = 25, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$-\frac{c\sqrt{cx^2}}{bx(a+bx)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}/(x^3*(a + b*x)^2), x]$

[Out] $-((c*\text{Sqrt}[c*x^2])/(b*x*(a + b*x)))$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

$\text{Int}[((a_.) + (b_.)*(x_))^{(m_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}/(b*(m + 1)), x] /;$ FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2}}{x^3(a+bx)^2} dx &= \frac{(c\sqrt{cx^2}) \int \frac{1}{(a+bx)^2} dx}{x} \\ &= -\frac{c\sqrt{cx^2}}{bx(a+bx)} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.96

$$\frac{(cx^2)^{3/2}}{bx^3(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^3*(a + b*x)^2), x]

[Out] -((c*x^2)^(3/2)/(b*x^3*(a + b*x)))

fricas [A] time = 0.45, size = 24, normalized size = 0.96

$$\frac{\sqrt{cx^2} c}{b^2x^2 + abx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^3/(b*x+a)^2,x, algorithm="fricas")

[Out] -sqrt(c*x^2)*c/(b^2*x^2 + a*b*x)

giac [A] time = 1.14, size = 29, normalized size = 1.16

$$-c^{\frac{3}{2}} \left(\frac{\operatorname{sgn}(x)}{(bx+a)b} - \frac{\operatorname{sgn}(x)}{ab} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^3/(b*x+a)^2,x, algorithm="giac")

[Out] -c^(3/2)*(sgn(x)/((b*x + a)*b) - sgn(x)/(a*b))

maple [A] time = 0.00, size = 23, normalized size = 0.92

$$\frac{(cx^2)^{\frac{3}{2}}}{(bx+a)bx^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x^3/(b*x+a)^2,x)

[Out] -1/(b*x+a)/b*(c*x^2)^(3/2)/x^3

maxima [A] time = 1.33, size = 16, normalized size = 0.64

$$\frac{c^{\frac{3}{2}}}{b^2x + ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)/x^3/(b*x+a)^2,x, algorithm="maxima")`

[Out] $-c^{3/2}/(b^2*x + a*b)$

mupad [B] time = 0.15, size = 24, normalized size = 0.96

$$-\frac{c^{3/2} \sqrt{x^2}}{b^2 x^2 + a b x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)/(x^3*(a + b*x)^2),x)`

[Out] $-(c^{3/2}*(x^2)^{(1/2)})/(b^2*x^2 + a*b*x)$

sympy [A] time = 2.23, size = 44, normalized size = 1.76

$$\begin{cases} -\frac{c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}{abx^3+b^2x^4} & \text{for } b \neq 0 \\ \frac{c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}{a^2x^2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x**2)**(3/2)/x**3/(b*x+a)**2,x)`

[Out] `Piecewise((-c**(3/2)*(x**2)**(3/2)/(a*b*x**3 + b**2*x**4), Ne(b, 0)), (c**(3/2)*(x**2)**(3/2)/(a**2*x**2), True))`

$$3.906 \quad \int \frac{(cx^2)^{3/2}}{x^4(a+bx)^2} dx$$

Optimal. Leaf size=68

$$-\frac{c\sqrt{cx^2} \log(a+bx)}{a^2x} + \frac{c\sqrt{cx^2} \log(x)}{a^2x} + \frac{c\sqrt{cx^2}}{ax(a+bx)}$$

[Out] $c*(c*x^2)^{(1/2)}/a/x/(b*x+a)+c*\ln(x)*(c*x^2)^{(1/2)}/a^2/x-c*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^2/x$

Rubi [A] time = 0.02, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{c\sqrt{cx^2} \log(a+bx)}{a^2x} + \frac{c\sqrt{cx^2} \log(x)}{a^2x} + \frac{c\sqrt{cx^2}}{ax(a+bx)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}/(x^4*(a+b*x)^2), x]$

[Out] $(c*\text{Sqrt}[c*x^2])/(a*x*(a+b*x)) + (c*\text{Sqrt}[c*x^2]*\text{Log}[x])/(a^2*x) - (c*\text{Sqrt}[c*x^2]*\text{Log}[a+b*x])/(a^2*x)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

$\text{Int}[(a_. + (b_.)*(x_))^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a+b*x)^m*(c+d*x)^n, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{3/2}}{x^4(a+bx)^2} dx &= \frac{(c\sqrt{cx^2}) \int \frac{1}{x(a+bx)^2} dx}{x} \\
&= \frac{(c\sqrt{cx^2}) \int \left(\frac{1}{a^2x} - \frac{b}{a(a+bx)^2} - \frac{b}{a^2(a+bx)} \right) dx}{x} \\
&= \frac{c\sqrt{cx^2}}{ax(a+bx)} + \frac{c\sqrt{cx^2} \log(x)}{a^2x} - \frac{c\sqrt{cx^2} \log(a+bx)}{a^2x}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.68

$$\frac{(cx^2)^{3/2} (\log(x)(a+bx) - (a+bx)\log(a+bx) + a)}{a^2x^3(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^4*(a + b*x)^2), x]

[Out] ((c*x^2)^(3/2)*(a + (a + b*x)*Log[x] - (a + b*x)*Log[a + b*x]))/(a^2*x^3*(a + b*x))

fricas [A] time = 0.43, size = 47, normalized size = 0.69

$$\frac{\sqrt{cx^2} (ac + (bcx + ac) \log\left(\frac{x}{bx+a}\right))}{a^2bx^2 + a^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^4/(b*x+a)^2,x, algorithm="fricas")

[Out] sqrt(c*x^2)*(a*c + (b*c*x + a*c)*log(x/(b*x + a)))/(a^2*b*x^2 + a^3*x)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^4/(b*x+a)^2,x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x)::OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 52, normalized size = 0.76

$$\frac{(cx^2)^{\frac{3}{2}}(bx \ln(x) - bx \ln(bx + a) + a \ln(x) - a \ln(bx + a) + a)}{(bx + a)a^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x^4/(b*x+a)^2,x)

[Out] (c*x^2)^(3/2)*(b*x*ln(x)-b*x*ln(b*x+a)+a*ln(x)-a*ln(b*x+a)+a)/x^3/a^2/(b*x+a)

maxima [A] time = 1.40, size = 38, normalized size = 0.56

$$\frac{c^{\frac{3}{2}}}{abx + a^2} - \frac{c^{\frac{3}{2}} \log(bx + a)}{a^2} + \frac{c^{\frac{3}{2}} \log(x)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^4/(b*x+a)^2,x, algorithm="maxima")

[Out] c^(3/2)/(a*b*x + a^2) - c^(3/2)*log(b*x + a)/a^2 + c^(3/2)*log(x)/a^2

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^4(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(x^4*(a + b*x)^2),x)

[Out] int((c*x^2)^(3/2)/(x^4*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^4(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)/x**4/(b*x+a)**2,x)

[Out] Integral((c*x**2)**(3/2)/(x**4*(a + b*x)**2), x)

$$3.907 \quad \int \frac{(cx^2)^{3/2}}{x^5(a+bx)^2} dx$$

Optimal. Leaf size=91

$$-\frac{2bc\sqrt{cx^2} \log(x)}{a^3x} + \frac{2bc\sqrt{cx^2} \log(a+bx)}{a^3x} - \frac{bc\sqrt{cx^2}}{a^2x(a+bx)} - \frac{c\sqrt{cx^2}}{a^2x^2}$$

[Out] $-c*(c*x^2)^{(1/2)}/a^2/x^2-b*c*(c*x^2)^{(1/2)}/a^2/x/(b*x+a)-2*b*c*\ln(x)*(c*x^2)^{(1/2)}/a^3/x+2*b*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^3/x$

Rubi [A] time = 0.02, antiderivative size = 91, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{bc\sqrt{cx^2}}{a^2x(a+bx)} - \frac{2bc\sqrt{cx^2} \log(x)}{a^3x} + \frac{2bc\sqrt{cx^2} \log(a+bx)}{a^3x} - \frac{c\sqrt{cx^2}}{a^2x^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}/(x^5*(a+b*x)^2), x]$

[Out] $-((c*\text{Sqrt}[c*x^2])/(a^2*x^2)) - (b*c*\text{Sqrt}[c*x^2])/(a^2*x*(a+b*x)) - (2*b*c*\text{Sqrt}[c*x^2]*\text{Log}[x])/(a^3*x) + (2*b*c*\text{Sqrt}[c*x^2]*\text{Log}[a+b*x])/(a^3*x)$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

$\text{Int}[(a_*) + (b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_))^{(n_*)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a+b*x)^m*(c+d*x)^n, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{3/2}}{x^5(a+bx)^2} dx &= \frac{(c\sqrt{cx^2}) \int \frac{1}{x^2(a+bx)^2} dx}{x} \\
&= \frac{(c\sqrt{cx^2}) \int \left(\frac{1}{a^2x^2} - \frac{2b}{a^3x} + \frac{b^2}{a^2(a+bx)^2} + \frac{2b^2}{a^3(a+bx)} \right) dx}{x} \\
&= -\frac{c\sqrt{cx^2}}{a^2x^2} - \frac{bc\sqrt{cx^2}}{a^2x(a+bx)} - \frac{2bc\sqrt{cx^2} \log(x)}{a^3x} + \frac{2bc\sqrt{cx^2} \log(a+bx)}{a^3x}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 59, normalized size = 0.65

$$-\frac{c^2(a(a+2bx) + 2bx \log(x)(a+bx) - 2bx(a+bx) \log(a+bx))}{a^3\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^5*(a + b*x)^2), x]

[Out] -((c^2*(a*(a + 2*b*x) + 2*b*x*(a + b*x))*Log[x] - 2*b*x*(a + b*x)*Log[a + b*x]))/(a^3*sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.45, size = 65, normalized size = 0.71

$$-\frac{\left(2abcx + a^2c - 2(b^2cx^2 + abcx) \log\left(\frac{bx+a}{x}\right)\right)\sqrt{cx^2}}{a^3bx^3 + a^4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^5/(b*x+a)^2,x, algorithm="fricas")

[Out] -(2*a*b*c*x + a^2*c - 2*(b^2*c*x^2 + a*b*c*x)*log((b*x + a)/x))*sqrt(c*x^2)/(a^3*b*x^3 + a^4*x^2)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^5/(b*x+a)^2,x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x):;OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 74, normalized size = 0.81

$$\frac{(cx^2)^{\frac{3}{2}} (2b^2x^2 \ln(x) - 2b^2x^2 \ln(bx + a) + 2abx \ln(x) - 2abx \ln(bx + a) + 2abx + a^2)}{(bx + a)a^3x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x^5/(b*x+a)^2,x)

[Out] -(c*x^2)^(3/2)*(2*b^2*x^2*ln(x)-2*b^2*x^2*ln(b*x+a)+2*a*b*x*ln(x)-2*a*b*x*ln(b*x+a)+2*a*b*x+a^2)/x^4/a^3/(b*x+a)

maxima [A] time = 1.43, size = 58, normalized size = 0.64

$$\frac{2bc^{\frac{3}{2}} \log(bx + a)}{a^3} - \frac{2bc^{\frac{3}{2}} \log(x)}{a^3} - \frac{2bc^{\frac{3}{2}}x + ac^{\frac{3}{2}}}{a^2bx^2 + a^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^5/(b*x+a)^2,x, algorithm="maxima")

[Out] 2*b*c^(3/2)*log(b*x + a)/a^3 - 2*b*c^(3/2)*log(x)/a^3 - (2*b*c^(3/2)*x + a*c^(3/2))/(a^2*b*x^2 + a^3*x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^5(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(x^5*(a + b*x)^2),x)

[Out] int((c*x^2)^(3/2)/(x^5*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^5(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)/x**5/(b*x+a)**2,x)

[Out] Integral((c*x**2)**(3/2)/(x**5*(a + b*x)**2), x)

$$3.908 \quad \int \frac{(cx^2)^{3/2}}{x^6(a+bx)^2} dx$$

Optimal. Leaf size=117

$$\frac{3b^2c\sqrt{cx^2} \log(x)}{a^4x} - \frac{3b^2c\sqrt{cx^2} \log(a+bx)}{a^4x} + \frac{b^2c\sqrt{cx^2}}{a^3x(a+bx)} + \frac{2bc\sqrt{cx^2}}{a^3x^2} - \frac{c\sqrt{cx^2}}{2a^2x^3}$$

[Out] $-1/2*c*(c*x^2)^{(1/2)}/a^2/x^3+2*b*c*(c*x^2)^{(1/2)}/a^3/x^2+b^2*c*(c*x^2)^{(1/2)}/a^3/x/(b*x+a)+3*b^2*c*\ln(x)*(c*x^2)^{(1/2)}/a^4/x-3*b^2*c*\ln(b*x+a)*(c*x^2)^{(1/2)}/a^4/x$

Rubi [A] time = 0.03, antiderivative size = 117, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$\frac{b^2c\sqrt{cx^2}}{a^3x(a+bx)} + \frac{3b^2c\sqrt{cx^2} \log(x)}{a^4x} - \frac{3b^2c\sqrt{cx^2} \log(a+bx)}{a^4x} + \frac{2bc\sqrt{cx^2}}{a^3x^2} - \frac{c\sqrt{cx^2}}{2a^2x^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}/(x^6*(a+b*x)^2), x]$

[Out] $-(c*\text{Sqrt}[c*x^2])/(2*a^2*x^3) + (2*b*c*\text{Sqrt}[c*x^2])/(a^3*x^2) + (b^2*c*\text{Sqrt}[c*x^2])/(a^3*x*(a+b*x)) + (3*b^2*c*\text{Sqrt}[c*x^2]*\text{Log}[x])/(a^4*x) - (3*b^2*c*\text{Sqrt}[c*x^2]*\text{Log}[a+b*x])/(a^4*x)$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] := \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{!IntegerQ}[m]$

Rule 44

$\text{Int}[(a_*) + (b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}), x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a+b*x)^m*(c+d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{ILtQ}[m, 0] \&\& \text{IntegerQ}[n] \&\& \text{!(IGtQ}[n, 0] \&\& \text{LtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{3/2}}{x^6(a+bx)^2} dx &= \frac{(c\sqrt{cx^2})}{x} \int \frac{1}{x^3(a+bx)^2} dx \\
&= \frac{(c\sqrt{cx^2})}{x} \int \left(\frac{1}{a^2x^3} - \frac{2b}{a^3x^2} + \frac{3b^2}{a^4x} - \frac{b^3}{a^3(a+bx)^2} - \frac{3b^3}{a^4(a+bx)} \right) dx \\
&= -\frac{c\sqrt{cx^2}}{2a^2x^3} + \frac{2bc\sqrt{cx^2}}{a^3x^2} + \frac{b^2c\sqrt{cx^2}}{a^3x(a+bx)} + \frac{3b^2c\sqrt{cx^2} \log(x)}{a^4x} - \frac{3b^2c\sqrt{cx^2} \log(a+bx)}{a^4x}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 82, normalized size = 0.70

$$\frac{(cx^2)^{3/2} \left(a(-a^2 + 3abx + 6b^2x^2) + 6b^2x^2 \log(x)(a+bx) - 6b^2x^2(a+bx) \log(a+bx) \right)}{2a^4x^5(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)/(x^6*(a + b*x)^2), x]

[Out] ((c*x^2)^(3/2)*(a*(-a^2 + 3*a*b*x + 6*b^2*x^2) + 6*b^2*x^2*(a + b*x)*Log[x] - 6*b^2*x^2*(a + b*x)*Log[a + b*x]))/(2*a^4*x^5*(a + b*x))

fricas [A] time = 0.44, size = 82, normalized size = 0.70

$$\frac{(6ab^2cx^2 + 3a^2bcx - a^3c + 6(b^3cx^3 + ab^2cx^2) \log\left(\frac{x}{bx+a}\right))\sqrt{cx^2}}{2(a^4bx^4 + a^5x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^6/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/2*(6*a*b^2*c*x^2 + 3*a^2*b*c*x - a^3*c + 6*(b^3*c*x^3 + a*b^2*c*x^2)*log(x/(b*x + a)))*sqrt(c*x^2)/(a^4*b*x^4 + a^5*x^3)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^6/(b*x+a)^2,x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INPUT:sage2:=int(sage0,x);;OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
Sign error (%%{a,0%%}+%%{b,1%%})

maple [A] time = 0.01, size = 95, normalized size = 0.81

$$\frac{(cx^2)^{\frac{3}{2}} (6b^3x^3 \ln(x) - 6b^3x^3 \ln(bx+a) + 6ab^2x^2 \ln(x) - 6ab^2x^2 \ln(bx+a) + 6ab^2x^2 + 3a^2bx - a^3)}{2(bx+a)a^4x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/x^6/(b*x+a)^2,x)

[Out] 1/2*(c*x^2)^(3/2)*(6*b^3*x^3*ln(x)-6*b^3*x^3*ln(b*x+a)+6*a*b^2*x^2*ln(x)-6*a*b^2*x^2*ln(b*x+a)+6*a*b^2*x^2+3*a^2*b*x-a^3)/x^5/a^4/(b*x+a)

maxima [A] time = 1.33, size = 79, normalized size = 0.68

$$-\frac{3b^2c^{\frac{3}{2}} \log(bx+a)}{a^4} + \frac{3b^2c^{\frac{3}{2}} \log(x)}{a^4} + \frac{6b^2c^{\frac{3}{2}}x^2 + 3abc^{\frac{3}{2}}x - a^2c^{\frac{3}{2}}}{2(a^3bx^3 + a^4x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)/x^6/(b*x+a)^2,x, algorithm="maxima")

[Out] -3*b^2*c^(3/2)*log(b*x + a)/a^4 + 3*b^2*c^(3/2)*log(x)/a^4 + 1/2*(6*b^2*c^(3/2)*x^2 + 3*a*b*c^(3/2)*x - a^2*c^(3/2))/(a^3*b*x^3 + a^4*x^2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^6(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)/(x^6*(a + b*x)^2),x)

[Out] int((c*x^2)^(3/2)/(x^6*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}}{x^6(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)/x**6/(b*x+a)**2,x)

[Out] Integral((c*x**2)**(3/2)/(x**6*(a + b*x)**2), x)

$$3.909 \quad \int \frac{x^5}{\sqrt{cx^2}(a+bx)^2} dx$$

Optimal. Leaf size=107

$$-\frac{a^4x}{b^5\sqrt{cx^2}(a+bx)} - \frac{4a^3x \log(a+bx)}{b^5\sqrt{cx^2}} + \frac{3a^2x^2}{b^4\sqrt{cx^2}} - \frac{ax^3}{b^3\sqrt{cx^2}} + \frac{x^4}{3b^2\sqrt{cx^2}}$$

[Out] $3a^2x^2/b^4/(cx^2)^{(1/2)} - ax^3/b^3/(cx^2)^{(1/2)} + 1/3x^4/b^2/(cx^2)^{(1/2)} - a^4x/b^5/(b*x+a)/(cx^2)^{(1/2)} - 4a^3x \ln(b*x+a)/b^5/(cx^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 107, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^4x}{b^5\sqrt{cx^2}(a+bx)} + \frac{3a^2x^2}{b^4\sqrt{cx^2}} - \frac{4a^3x \log(a+bx)}{b^5\sqrt{cx^2}} - \frac{ax^3}{b^3\sqrt{cx^2}} + \frac{x^4}{3b^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^5/(Sqrt[c*x^2]*(a + b*x)^2), x]

[Out] $(3a^2x^2)/(b^4\sqrt{cx^2}) - (ax^3)/(b^3\sqrt{cx^2}) + x^4/(3b^2\sqrt{cx^2}) - (a^4x)/(b^5\sqrt{cx^2}(a+bx)) - (4a^3x \log[a+bx])/(b^5\sqrt{cx^2})$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{x^5}{\sqrt{cx^2} (a+bx)^2} dx &= \frac{x \int \frac{x^4}{(a+bx)^2} dx}{\sqrt{cx^2}} \\
&= \frac{x \int \left(\frac{3a^2}{b^4} - \frac{2ax}{b^3} + \frac{x^2}{b^2} + \frac{a^4}{b^4(a+bx)^2} - \frac{4a^3}{b^4(a+bx)} \right) dx}{\sqrt{cx^2}} \\
&= \frac{3a^2x^2}{b^4\sqrt{cx^2}} - \frac{ax^3}{b^3\sqrt{cx^2}} + \frac{x^4}{3b^2\sqrt{cx^2}} - \frac{a^4x}{b^5\sqrt{cx^2}(a+bx)} - \frac{4a^3x \log(a+bx)}{b^5\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 80, normalized size = 0.75

$$\frac{x(-3a^4 + 9a^3bx - 12a^3(a+bx)\log(a+bx) + 6a^2b^2x^2 - 2ab^3x^3 + b^4x^4)}{3b^5\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/(Sqrt[c*x^2]*(a + b*x)^2), x]

[Out] (x*(-3*a^4 + 9*a^3*b*x + 6*a^2*b^2*x^2 - 2*a*b^3*x^3 + b^4*x^4 - 12*a^3*(a + b*x)*Log[a + b*x]))/(3*b^5*Sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.42, size = 85, normalized size = 0.79

$$\frac{(b^4x^4 - 2ab^3x^3 + 6a^2b^2x^2 + 9a^3bx - 3a^4 - 12(a^3bx + a^4)\log(bx + a))\sqrt{cx^2}}{3(b^6cx^2 + ab^5cx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^2/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] 1/3*(b^4*x^4 - 2*a*b^3*x^3 + 6*a^2*b^2*x^2 + 9*a^3*b*x - 3*a^4 - 12*(a^3*b*x + a^4)*log(b*x + a))*sqrt(c*x^2)/(b^6*c*x^2 + a*b^5*c*x)

giac [A] time = 1.13, size = 155, normalized size = 1.45

$$\frac{(bx+a)^3 \left(\frac{6a}{bx+a} - \frac{18a^2}{(bx+a)^2} - 1 \right) - 12a^3 \log\left(\frac{|bx+a|}{(bx+a)^2|b|} \right) + \frac{3a^4}{(bx+a)b^5 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2} \right)}}{b^5 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2} \right)} \cdot \frac{1}{3\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out] $\frac{1}{3} \left((b*x + a)^3 \left(\frac{6*a}{b*x + a} - 18*a^2/(b*x + a)^2 - 1 \right) / (b^5 * \text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) - 12*a^3 * \log(\text{abs}(b*x + a)/((b*x + a)^2 * \text{abs}(b))) / (b^5 * \text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) + 3*a^4 / ((b*x + a) * b^5 * \text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) \right) / \text{sqrt}(c)$

maple [A] time = 0.01, size = 86, normalized size = 0.80

$$\frac{(-b^4 x^4 + 2a b^3 x^3 + 12a^3 b x \ln(bx + a) - 6a^2 b^2 x^2 + 12a^4 \ln(bx + a) - 9a^3 b x + 3a^4) x}{3\sqrt{c x^2} (bx + a) b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(b*x+a)^2/(c*x^2)^(1/2),x)

[Out] $-1/3 * x * (-b^4 * x^4 + 2 * a * b^3 * x^3 + 12 * a^3 * b * x * \ln(b * x + a) - 6 * a^2 * b^2 * x^2 + 12 * a^4 * \ln(b * x + a) - 9 * a^3 * b * x + 3 * a^4) / (c * x^2)^{(1/2)} / b^5 / (b * x + a)$

maxima [A] time = 1.56, size = 168, normalized size = 1.57

$$\frac{\sqrt{cx^2} a^3}{b^5 cx + ab^4 c} + \frac{\sqrt{cx^2} x^2}{3 b^2 c} - \frac{5 a x^2}{3 b^3 \sqrt{c}} - \frac{4 (-1)^{\frac{2acx}{b}} a^3 \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^5 \sqrt{c}} + \frac{2 \sqrt{cx^2} a x}{3 b^3 c} - \frac{20 a^2 x}{3 b^4 \sqrt{c}} - \frac{4 a^3 \log(bx)}{b^5 \sqrt{c}} + \frac{29 \sqrt{cx^2} a^2}{3 b^4 c} - \frac{5}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] $\text{sqrt}(c*x^2)*a^3/(b^5*c*x + a*b^4*c) + 1/3*\text{sqrt}(c*x^2)*x^2/(b^2*c) - 5/3*a*x^2/(b^3*\text{sqrt}(c)) - 4*(-1)^{(2*a*c*x/b)}*a^3*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(b^5*\text{sqrt}(c)) + 2/3*\text{sqrt}(c*x^2)*a*x/(b^3*c) - 20/3*a^2*x/(b^4*\text{sqrt}(c)) - 4*a^3*\log(b*x)/(b^5*\text{sqrt}(c)) + 29/3*\text{sqrt}(c*x^2)*a^2/(b^4*c) - 5*a^3/(b^5*\text{sqrt}(c))$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^5}{\sqrt{c x^2} (a + b x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/((c*x^2)^(1/2)*(a + b*x)^2),x)

[Out] int(x^5/((c*x^2)^(1/2)*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^5}{\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5/(b*x+a)**2/(c*x**2)**(1/2),x)

[Out] Integral(x**5/(sqrt(c*x**2)*(a + b*x)**2), x)

$$3.910 \quad \int \frac{x^4}{\sqrt{cx^2} (a+bx)^2} dx$$

Optimal. Leaf size=86

$$\frac{a^3x}{b^4\sqrt{cx^2}(a+bx)} + \frac{3a^2x \log(a+bx)}{b^4\sqrt{cx^2}} - \frac{2ax^2}{b^3\sqrt{cx^2}} + \frac{x^3}{2b^2\sqrt{cx^2}}$$

[Out] $-2*a*x^2/b^3/(c*x^2)^{(1/2)}+1/2*x^3/b^2/(c*x^2)^{(1/2)}+a^3*x/b^4/(b*x+a)/(c*x^2)^{(1/2)}+3*a^2*x*\ln(b*x+a)/b^4/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^3x}{b^4\sqrt{cx^2}(a+bx)} + \frac{3a^2x \log(a+bx)}{b^4\sqrt{cx^2}} - \frac{2ax^2}{b^3\sqrt{cx^2}} + \frac{x^3}{2b^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^4/(Sqrt[c*x^2]*(a + b*x)^2), x]

[Out] $(-2*a*x^2)/(b^3*\text{Sqrt}[c*x^2]) + x^3/(2*b^2*\text{Sqrt}[c*x^2]) + (a^3*x)/(b^4*\text{Sqrt}[c*x^2]*(a + b*x)) + (3*a^2*x*\text{Log}[a + b*x])/(b^4*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{\sqrt{cx^2}(a+bx)^2} dx &= \frac{x \int \frac{x^3}{(a+bx)^2} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(-\frac{2a}{b^3} + \frac{x}{b^2} - \frac{a^3}{b^3(a+bx)^2} + \frac{3a^2}{b^3(a+bx)} \right) dx}{\sqrt{cx^2}} \\ &= -\frac{2ax^2}{b^3\sqrt{cx^2}} + \frac{x^3}{2b^2\sqrt{cx^2}} + \frac{a^3x}{b^4\sqrt{cx^2}(a+bx)} + \frac{3a^2x \log(a+bx)}{b^4\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 69, normalized size = 0.80

$$\frac{x(2a^3 - 4a^2bx + 6a^2(a+bx)\log(a+bx) - 3ab^2x^2 + b^3x^3)}{2b^4\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/(Sqrt[c*x^2]*(a + b*x)^2),x]

[Out] (x*(2*a^3 - 4*a^2*b*x - 3*a*b^2*x^2 + b^3*x^3 + 6*a^2*(a + b*x)*Log[a + b*x]))/(2*b^4*Sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.43, size = 74, normalized size = 0.86

$$\frac{(b^3x^3 - 3ab^2x^2 - 4a^2bx + 2a^3 + 6(a^2bx + a^3)\log(bx+a))\sqrt{cx^2}}{2(b^5cx^2 + ab^4cx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/2*(b^3*x^3 - 3*a*b^2*x^2 - 4*a^2*b*x + 2*a^3 + 6*(a^2*b*x + a^3)*log(b*x + a))*sqrt(c*x^2)/(b^5*c*x^2 + a*b^4*c*x)

giac [A] time = 1.04, size = 143, normalized size = 1.66

$$\frac{\frac{(bx+a)^2\left(\frac{6a}{bx+a}-1\right)}{b^4\operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} + \frac{6a^2\log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b^4\operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} - \frac{2a^3}{(bx+a)b^4\operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)}}{2\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out] $\frac{1}{2} * ((b*x + a)^2 * (6*a/(b*x + a) - 1) / (b^4 * \text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) + 6*a^2 * \log(\text{abs}(b*x + a) / ((b*x + a)^2 * \text{abs}(b))) / (b^4 * \text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) - 2*a^3 / ((b*x + a) * b^4 * \text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2))) / \text{sqrt}(c)$

maple [A] time = 0.00, size = 74, normalized size = 0.86

$$\frac{(b^3 x^3 + 6a^2 b x \ln(bx + a) - 3a b^2 x^2 + 6a^3 \ln(bx + a) - 4a^2 b x + 2a^3) x}{2\sqrt{c x^2} (bx + a) b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/(b*x+a)^2/(c*x^2)^(1/2),x)

[Out] $\frac{1}{2} * x * (b^3 * x^3 + 6 * a^2 * b * x * \ln(b * x + a) - 3 * a * b^2 * x^2 + 6 * a^3 * \ln(b * x + a) - 4 * a^2 * b * x + 2 * a^3) / (c * x^2)^{(1/2)} / b^4 / (b * x + a)$

maxima [A] time = 1.55, size = 129, normalized size = 1.50

$$-\frac{\sqrt{cx^2} a^2}{b^4 cx + ab^3 c} + \frac{x^2}{2 b^2 \sqrt{c}} + \frac{3 (-1)^{\frac{2acx}{b}} a^2 \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^4 \sqrt{c}} + \frac{2ax}{b^3 \sqrt{c}} + \frac{3a^2 \log(bx)}{b^4 \sqrt{c}} - \frac{4\sqrt{cx^2} a}{b^3 c} + \frac{3a^2}{2b^4 \sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] $-\text{sqrt}(c*x^2)*a^2/(b^4*c*x + a*b^3*c) + 1/2*x^2/(b^2*\text{sqrt}(c)) + 3*(-1)^{(2*a*c*x/b)}*a^2*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(b^4*\text{sqrt}(c)) + 2*a*x/(b^3*\text{sqrt}(c)) + 3*a^2*\log(b*x)/(b^4*\text{sqrt}(c)) - 4*\text{sqrt}(c*x^2)*a/(b^3*c) + 3/2*a^2/(b^4*\text{sqrt}(c))$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^4}{\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/((c*x^2)^(1/2)*(a + b*x)^2),x)

[Out] int(x^4/((c*x^2)^(1/2)*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^4}{\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4/(b*x+a)**2/(c*x**2)**(1/2),x)
```

```
[Out] Integral(x**4/(sqrt(c*x**2)*(a + b*x)**2), x)
```

$$3.911 \quad \int \frac{x^3}{\sqrt{cx^2} (a+bx)^2} dx$$

Optimal. Leaf size=64

$$-\frac{a^2x}{b^3\sqrt{cx^2}(a+bx)} - \frac{2ax \log(a+bx)}{b^3\sqrt{cx^2}} + \frac{x^2}{b^2\sqrt{cx^2}}$$

[Out] $x^2/b^2/(c*x^2)^{(1/2)} - a^2*x/b^3/(b*x+a)/(c*x^2)^{(1/2)} - 2*a*x*\ln(b*x+a)/b^3/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2x}{b^3\sqrt{cx^2}(a+bx)} - \frac{2ax \log(a+bx)}{b^3\sqrt{cx^2}} + \frac{x^2}{b^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^3/(Sqrt[c*x^2]*(a + b*x)^2), x]

[Out] $x^2/(b^2*\text{Sqrt}[c*x^2]) - (a^2*x)/(b^3*\text{Sqrt}[c*x^2]*(a + b*x)) - (2*a*x*\text{Log}[a + b*x])/(b^3*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3}{\sqrt{cx^2}(a+bx)^2} dx &= \frac{x \int \frac{x^2}{(a+bx)^2} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{1}{b^2} + \frac{a^2}{b^2(a+bx)^2} - \frac{2a}{b^2(a+bx)} \right) dx}{\sqrt{cx^2}} \\ &= \frac{x^2}{b^2\sqrt{cx^2}} - \frac{a^2x}{b^3\sqrt{cx^2}(a+bx)} - \frac{2ax \log(a+bx)}{b^3\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 52, normalized size = 0.81

$$\frac{x(-a^2 + abx - 2a(a+bx)\log(a+bx) + b^2x^2)}{b^3\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/(Sqrt[c*x^2]*(a + b*x)^2),x]

[Out] (x*(-a^2 + a*b*x + b^2*x^2 - 2*a*(a + b*x)*Log[a + b*x]))/(b^3*Sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.41, size = 59, normalized size = 0.92

$$\frac{(b^2x^2 + abx - a^2 - 2(abx + a^2)\log(bx + a))\sqrt{cx^2}}{b^4cx^2 + ab^3cx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] (b^2*x^2 + a*b*x - a^2 - 2*(a*b*x + a^2)*log(b*x + a))*sqrt(c*x^2)/(b^4*c*x^2 + a*b^3*c*x)

giac [B] time = 1.13, size = 127, normalized size = 1.98

$$\frac{2a \log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b^3 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} + \frac{bx+a}{b^3 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} - \frac{a^2}{(bx+a)b^3 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} \sqrt{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out] $-(2*a*\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b))))/(b^3*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) + (b*x + a)/(b^3*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) - a^2/((b*x + a)*b^3*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2))/\text{sqrt}(c)$

maple [A] time = 0.01, size = 60, normalized size = 0.94

$$-\frac{(2abx \ln(bx + a) - b^2x^2 + 2a^2 \ln(bx + a) - abx + a^2)x}{\sqrt{cx^2} (bx + a)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(b*x+a)^2/(c*x^2)^(1/2),x)

[Out] $-x*(2*a*b*x*\ln(b*x+a)-b^2*x^2+2*a^2*\ln(b*x+a)-a*b*x+a^2)/(c*x^2)^(1/2)/b^3/(b*x+a)$

maxima [A] time = 1.45, size = 88, normalized size = 1.38

$$\frac{\sqrt{cx^2} a}{b^3cx + ab^2c} - \frac{2(-1)^{\frac{2acx}{b}} a \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^3\sqrt{c}} - \frac{2a \log(bx)}{b^3\sqrt{c}} + \frac{\sqrt{cx^2}}{b^2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] $\text{sqrt}(c*x^2)*a/(b^3*c*x + a*b^2*c) - 2*(-1)^(2*a*c*x/b)*a*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(b^3*\text{sqrt}(c)) - 2*a*\log(b*x)/(b^3*\text{sqrt}(c)) + \text{sqrt}(c*x^2)/(b^2*c)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^3}{\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/((c*x^2)^(1/2)*(a + b*x)^2),x)

[Out] int(x^3/((c*x^2)^(1/2)*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^3}{\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3/(b*x+a)**2/(c*x**2)**(1/2),x)
```

```
[Out] Integral(x**3/(sqrt(c*x**2)*(a + b*x)**2), x)
```


$$3.912 \quad \int \frac{x^2}{\sqrt{cx^2} (a+bx)^2} dx$$

Optimal. Leaf size=43

$$\frac{ax}{b^2\sqrt{cx^2} (a+bx)} + \frac{x \log(a+bx)}{b^2\sqrt{cx^2}}$$

[Out] $a*x/b^2/(b*x+a)/(c*x^2)^{(1/2)}+x*\ln(b*x+a)/b^2/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{ax}{b^2\sqrt{cx^2} (a+bx)} + \frac{x \log(a+bx)}{b^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^2/(Sqrt[c*x^2]*(a + b*x)^2), x]

[Out] (a*x)/(b^2*Sqrt[c*x^2]*(a + b*x)) + (x*Log[a + b*x])/(b^2*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sqrt{cx^2} (a + bx)^2} dx &= \frac{x \int \frac{x}{(a+bx)^2} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(-\frac{a}{b(a+bx)^2} + \frac{1}{b(a+bx)} \right) dx}{\sqrt{cx^2}} \\ &= \frac{ax}{b^2 \sqrt{cx^2} (a + bx)} + \frac{x \log(a + bx)}{b^2 \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.81

$$\frac{x((a + bx) \log(a + bx) + a)}{b^2 \sqrt{cx^2} (a + bx)}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(Sqrt[c*x^2]*(a + b*x)^2),x]

[Out] (x*(a + (a + b*x)*Log[a + b*x]))/(b^2*Sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.41, size = 40, normalized size = 0.93

$$\frac{\sqrt{cx^2} ((bx + a) \log(bx + a) + a)}{b^3 cx^2 + ab^2 cx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] sqrt(c*x^2)*((b*x + a)*log(b*x + a) + a)/(b^3*c*x^2 + a*b^2*c*x)

giac [B] time = 1.15, size = 89, normalized size = 2.07

$$\frac{\log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b^2 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} - \frac{a}{(bx+a)b^2 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} \frac{1}{\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out] $(\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b))))/(b^2*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) - a/((b*x + a)*b^2*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2))/\text{sqrt}(c)$

maple [A] time = 0.00, size = 39, normalized size = 0.91

$$\frac{(bx \ln(bx + a) + a \ln(bx + a) + a)x}{\sqrt{cx^2} (bx + a)b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/(b*x+a)^2/(c*x^2)^(1/2), x)`

[Out] `x*(b*x*ln(b*x+a)+a*ln(b*x+a)+a)/(c*x^2)^(1/2)/b^2/(b*x+a)`

maxima [A] time = 1.41, size = 68, normalized size = 1.58

$$-\frac{\sqrt{cx^2}}{b^2cx + abc} + \frac{(-1)^{\frac{2acx}{b}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^2\sqrt{c}} + \frac{\log(bx)}{b^2\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2/(b*x+a)^2/(c*x^2)^(1/2), x, algorithm="maxima")`

[Out] `-sqrt(c*x^2)/(b^2*c*x + a*b*c) + (-1)^(2*a*c*x/b)*log(-2*a*c*x/(b*abs(b*x + a)))/(b^2*sqrt(c)) + log(b*x)/(b^2*sqrt(c))`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^2}{\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/((c*x^2)^(1/2)*(a + b*x)^2), x)`

[Out] `int(x^2/((c*x^2)^(1/2)*(a + b*x)^2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2}{\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2/(b*x+a)**2/(c*x**2)**(1/2), x)`

[Out] `Integral(x**2/(sqrt(c*x**2)*(a + b*x)**2), x)`

$$3.913 \quad \int \frac{x}{\sqrt{cx^2} (a+bx)^2} dx$$

Optimal. Leaf size=22

$$-\frac{x}{b\sqrt{cx^2} (a+bx)}$$

[Out] $-x/b/(b*x+a)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 32}

$$-\frac{x}{b\sqrt{cx^2} (a+bx)}$$

Antiderivative was successfully verified.

[In] `Int[x/(Sqrt[c*x^2]*(a + b*x)^2), x]`

[Out] `-(x/(b*Sqrt[c*x^2]*(a + b*x)))`

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rule 32

`Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]`

Rubi steps

$$\begin{aligned} \int \frac{x}{\sqrt{cx^2} (a+bx)^2} dx &= \frac{x \int \frac{1}{(a+bx)^2} dx}{\sqrt{cx^2}} \\ &= -\frac{x}{b\sqrt{cx^2} (a+bx)} \end{aligned}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 1.00

$$-\frac{x}{b\sqrt{cx^2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[x/(Sqrt[c*x^2]*(a + b*x)^2),x]

[Out] -(x/(b*Sqrt[c*x^2]*(a + b*x)))

fricas [A] time = 0.44, size = 25, normalized size = 1.14

$$-\frac{\sqrt{cx^2}}{b^2cx^2 + abcx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] -sqrt(c*x^2)/(b^2*c*x^2 + a*b*c*x)

giac [A] time = 1.16, size = 38, normalized size = 1.73

$$\frac{1}{(bx + a)b\sqrt{c} \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out] 1/((b*x + a)*b*sqrt(c)*sgn(-b/(b*x + a) + a*b/(b*x + a)^2))

maple [A] time = 0.00, size = 21, normalized size = 0.95

$$-\frac{x}{(bx + a)\sqrt{cx^2} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(b*x+a)^2/(c*x^2)^(1/2),x)

[Out] -x/b/(b*x+a)/(c*x^2)^(1/2)

maxima [A] time = 1.45, size = 21, normalized size = 0.95

$$\frac{\sqrt{cx^2}}{abcx + a^2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] $\sqrt{c*x^2}/(a*b*c*x + a^2*c)$

mupad [B] time = 0.16, size = 25, normalized size = 1.14

$$\frac{\sqrt{c x^2}}{b c x (a + b x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x/((c*x^2)^{(1/2)}*(a + b*x)^2), x)$

[Out] $-(c*x^2)^{(1/2)}/(b*c*x*(a + b*x))$

sympy [A] time = 1.17, size = 85, normalized size = 3.86

$$\left\{ \begin{array}{ll} \frac{\infty}{\sqrt{c} \sqrt{x^2}} & \text{for } a = 0 \wedge b = 0 \\ \frac{\infty x^2}{\sqrt{c} \sqrt{x^2}} & \text{for } a = -bx \\ \frac{x^2}{a^2 \sqrt{c} \sqrt{x^2}} & \text{for } b = 0 \\ -\frac{x}{ab \sqrt{c} \sqrt{x^2} + b^2 \sqrt{c} x \sqrt{x^2}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x/(b*x+a)**2/(c*x**2)**(1/2), x)$

[Out] $\text{Piecewise}((zoo/(\sqrt{c}*\sqrt{x**2})), \text{Eq}(a, 0) \ \& \ \text{Eq}(b, 0)), (zoo*x**2/(\sqrt{c}*\sqrt{x**2})), \text{Eq}(a, -b*x)), (x**2/(a**2*\sqrt{c}*\sqrt{x**2})), \text{Eq}(b, 0)), (-x/(a*b*\sqrt{c}*\sqrt{x**2} + b**2*\sqrt{c}*x*\sqrt{x**2})), \text{True}))$

$$3.914 \quad \int \frac{1}{\sqrt{cx^2} (a+bx)^2} dx$$

Optimal. Leaf size=59

$$-\frac{x \log(a+bx)}{a^2 \sqrt{cx^2}} + \frac{x \log(x)}{a^2 \sqrt{cx^2}} + \frac{x}{a \sqrt{cx^2} (a+bx)}$$

[Out] x/a/(b*x+a)/(c*x^2)^(1/2)+x*ln(x)/a^2/(c*x^2)^(1/2)-x*ln(b*x+a)/a^2/(c*x^2)^(1/2)

Rubi [A] time = 0.02, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 44}

$$-\frac{x \log(a+bx)}{a^2 \sqrt{cx^2}} + \frac{x \log(x)}{a^2 \sqrt{cx^2}} + \frac{x}{a \sqrt{cx^2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[c*x^2]*(a + b*x)^2), x]

[Out] x/(a*Sqrt[c*x^2]*(a + b*x)) + (x*Log[x])/(a^2*Sqrt[c*x^2]) - (x*Log[a + b*x])/(a^2*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt{cx^2}(a+bx)^2} dx &= \frac{x \int \frac{1}{x(a+bx)^2} dx}{\sqrt{cx^2}} \\
&= \frac{x \int \left(\frac{1}{a^2x} - \frac{b}{a(a+bx)^2} - \frac{b}{a^2(a+bx)} \right) dx}{\sqrt{cx^2}} \\
&= \frac{x}{a\sqrt{cx^2}(a+bx)} + \frac{x \log(x)}{a^2\sqrt{cx^2}} - \frac{x \log(a+bx)}{a^2\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 44, normalized size = 0.75

$$\frac{x(\log(x)(a+bx) - (a+bx)\log(a+bx) + a)}{a^2\sqrt{cx^2}(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[c*x^2]*(a + b*x)^2),x]

[Out] (x*(a + (a + b*x)*Log[x] - (a + b*x)*Log[a + b*x]))/(a^2*Sqrt[c*x^2]*(a + b*x))

fricas [A] time = 0.44, size = 44, normalized size = 0.75

$$\frac{\sqrt{cx^2} \left((bx+a) \log\left(\frac{x}{bx+a}\right) + a \right)}{a^2bcx^2 + a^3cx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] sqrt(c*x^2)*((b*x + a)*log(x/(b*x + a)) + a)/(a^2*b*c*x^2 + a^3*c*x)

giac [A] time = 1.08, size = 86, normalized size = 1.46

$$-\frac{\log\left(\left|-\frac{a}{bx+a} + 1\right|\right)}{a^2\sqrt{c} \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} - \frac{1}{(bx+a)a\sqrt{c} \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out] $-\log(\text{abs}(-a/(b*x + a) + 1))/(a^2*\text{sqrt}(c)*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) - 1/((b*x + a)*a*\text{sqrt}(c)*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2))$

maple [A] time = 0.01, size = 50, normalized size = 0.85

$$\frac{(bx \ln(x) - bx \ln(bx + a) + a \ln(x) - a \ln(bx + a) + a) x}{\sqrt{cx^2} (bx + a) a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(b*x+a)^2/(c*x^2)^{(1/2)}, x)$

[Out] $x*(b*x*\ln(x)-b*x*\ln(b*x+a)+a*\ln(x)-a*\ln(b*x+a)+a)/(c*x^2)^{(1/2)}/a^2/(b*x+a)$

maxima [A] time = 1.46, size = 61, normalized size = 1.03

$$-\frac{\sqrt{cx^2} b}{a^2 bcx + a^3 c} - \frac{(-1)^{\frac{2acx}{b}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{a^2 \sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(b*x+a)^2/(c*x^2)^{(1/2)}, x, \text{algorithm}="maxima")$

[Out] $-\text{sqrt}(c*x^2)*b/(a^2*b*c*x + a^3*c) - (-1)^{(2*a*c*x/b)}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(a^2*\text{sqrt}(c))$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{1}{\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/((c*x^2)^{(1/2)}*(a + b*x)^2), x)$

[Out] $\text{int}(1/((c*x^2)^{(1/2)}*(a + b*x)^2), x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(b*x+a)**2/(c*x**2)**(1/2), x)$

[Out] $\text{Integral}(1/(\text{sqrt}(c*x**2)*(a + b*x)**2), x)$

$$3.915 \quad \int \frac{1}{x\sqrt{cx^2}(a+bx)^2} dx$$

Optimal. Leaf size=78

$$-\frac{2bx \log(x)}{a^3\sqrt{cx^2}} + \frac{2bx \log(a+bx)}{a^3\sqrt{cx^2}} - \frac{bx}{a^2\sqrt{cx^2}(a+bx)} - \frac{1}{a^2\sqrt{cx^2}}$$

[Out] $-1/a^2/(c*x^2)^{(1/2)}-b*x/a^2/(b*x+a)/(c*x^2)^{(1/2)}-2*b*x*\ln(x)/a^3/(c*x^2)^{(1/2)}+2*b*x*\ln(b*x+a)/a^3/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{bx}{a^2\sqrt{cx^2}(a+bx)} - \frac{2bx \log(x)}{a^3\sqrt{cx^2}} + \frac{2bx \log(a+bx)}{a^3\sqrt{cx^2}} - \frac{1}{a^2\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x*sqrt[c*x^2]*(a + b*x)^2), x]

[Out] $-(1/(a^2*\sqrt{c*x^2})) - (b*x)/(a^2*\sqrt{c*x^2}*(a + b*x)) - (2*b*x*\text{Log}[x])/(a^3*\sqrt{c*x^2}) + (2*b*x*\text{Log}[a + b*x])/(a^3*\sqrt{c*x^2})$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{x\sqrt{cx^2}(a+bx)^2} dx &= \frac{x \int \frac{1}{x^2(a+bx)^2} dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{1}{a^2x^2} - \frac{2b}{a^3x} + \frac{b^2}{a^2(a+bx)^2} + \frac{2b^2}{a^3(a+bx)} \right) dx}{\sqrt{cx^2}} \\ &= -\frac{1}{a^2\sqrt{cx^2}} - \frac{bx}{a^2\sqrt{cx^2}(a+bx)} - \frac{2bx \log(x)}{a^3\sqrt{cx^2}} + \frac{2bx \log(a+bx)}{a^3\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 60, normalized size = 0.77

$$\frac{cx^2(-a(a+2bx) - 2bx \log(x)(a+bx) + 2bx(a+bx) \log(a+bx))}{a^3 (cx^2)^{3/2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x*sqrt[c*x^2]*(a + b*x)^2), x]

[Out] (c*x^2*(-(a*(a + 2*b*x)) - 2*b*x*(a + b*x)*Log[x] + 2*b*x*(a + b*x)*Log[a + b*x]))/(a^3*(c*x^2)^(3/2)*(a + b*x))

fricas [A] time = 0.43, size = 62, normalized size = 0.79

$$-\frac{\left(2abx + a^2 - 2(b^2x^2 + abx) \log\left(\frac{bx+a}{x}\right)\right)\sqrt{cx^2}}{a^3bcx^3 + a^4cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^2/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] -(2*a*b*x + a^2 - 2*(b^2*x^2 + a*b*x)*log((b*x + a)/x))*sqrt(c*x^2)/(a^3*b*c*x^3 + a^4*c*x^2)

giac [A] time = 1.14, size = 126, normalized size = 1.62

$$b \left(\frac{2 \log\left(\left|-\frac{a}{bx+a}+1\right|\right)}{a^3 \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} + \frac{1}{(bx+a)a^2 \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} - \frac{1}{a^3\left(\frac{a}{bx+a}-1\right) \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} \right) \frac{1}{\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out] $b*(2*\log(\text{abs}(-a/(b*x + a) + 1)))/(a^3*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) + 1/((b*x + a)*a^2*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) - 1/(a^3*(a/(b*x + a) - 1)*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)))/\text{sqrt}(c)$

maple [A] time = 0.01, size = 71, normalized size = 0.91

$$-\frac{2b^2x^2 \ln(x) - 2b^2x^2 \ln(bx + a) + 2abx \ln(x) - 2abx \ln(bx + a) + 2abx + a^2}{\sqrt{cx^2} (bx + a)a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(b*x+a)^2/(c*x^2)^(1/2),x)

[Out] $-(2*b^2*x^2*\ln(x)-2*b^2*x^2*\ln(b*x+a)+2*a*b*x*\ln(x)-2*a*b*x*\ln(b*x+a)+2*a*b*x+a^2)/(c*x^2)^(1/2)/a^3/(b*x+a)$

maxima [A] time = 1.43, size = 57, normalized size = 0.73

$$-\frac{2bx + a}{a^2b\sqrt{c}x^2 + a^3\sqrt{c}x} + \frac{2b \log(bx + a)}{a^3\sqrt{c}} - \frac{2b \log(x)}{a^3\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] $-(2*b*x + a)/(a^2*b*\text{sqrt}(c)*x^2 + a^3*\text{sqrt}(c)*x) + 2*b*\log(b*x + a)/(a^3*\text{sqrt}(c)) - 2*b*\log(x)/(a^3*\text{sqrt}(c))$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{x\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x*(c*x^2)^(1/2)*(a + b*x)^2),x)

[Out] int(1/(x*(c*x^2)^(1/2)*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{x\sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(b*x+a)**2/(c*x**2)**(1/2),x)

[Out] Integral(1/(x*sqrt(c*x**2)*(a + b*x)**2), x)

$$3.916 \quad \int \frac{1}{x^2 \sqrt{cx^2} (a+bx)^2} dx$$

Optimal. Leaf size=103

$$\frac{3b^2x \log(x)}{a^4\sqrt{cx^2}} - \frac{3b^2x \log(a+bx)}{a^4\sqrt{cx^2}} + \frac{b^2x}{a^3\sqrt{cx^2}(a+bx)} + \frac{2b}{a^3\sqrt{cx^2}} - \frac{1}{2a^2x\sqrt{cx^2}}$$

[Out] $2*b/a^3/(c*x^2)^(1/2)-1/2/a^2/x/(c*x^2)^(1/2)+b^2*x/a^3/(b*x+a)/(c*x^2)^(1/2)+3*b^2*x*\ln(x)/a^4/(c*x^2)^(1/2)-3*b^2*x*\ln(b*x+a)/a^4/(c*x^2)^(1/2)$

Rubi [A] time = 0.03, antiderivative size = 103, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$\frac{b^2x}{a^3\sqrt{cx^2}(a+bx)} + \frac{3b^2x \log(x)}{a^4\sqrt{cx^2}} - \frac{3b^2x \log(a+bx)}{a^4\sqrt{cx^2}} + \frac{2b}{a^3\sqrt{cx^2}} - \frac{1}{2a^2x\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[1/(x^2*sqrt[c*x^2]*(a + b*x)^2), x]

[Out] $(2*b)/(a^3*\text{sqrt}[c*x^2]) - 1/(2*a^2*x*\text{sqrt}[c*x^2]) + (b^2*x)/(a^3*\text{sqrt}[c*x^2]*(a + b*x)) + (3*b^2*x*\text{Log}[x])/(a^4*\text{sqrt}[c*x^2]) - (3*b^2*x*\text{Log}[a + b*x])/(a^4*\text{sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{x^2 \sqrt{cx^2} (a+bx)^2} dx = \frac{x \int \frac{1}{x^3(a+bx)^2} dx}{\sqrt{cx^2}}$$

$$= \frac{x \int \left(\frac{1}{a^2 x^3} - \frac{2b}{a^3 x^2} + \frac{3b^2}{a^4 x} - \frac{b^3}{a^3(a+bx)^2} - \frac{3b^3}{a^4(a+bx)} \right) dx}{\sqrt{cx^2}}$$

$$= \frac{2b}{a^3 \sqrt{cx^2}} - \frac{1}{2a^2 x \sqrt{cx^2}} + \frac{b^2 x}{a^3 \sqrt{cx^2} (a+bx)} + \frac{3b^2 x \log(x)}{a^4 \sqrt{cx^2}} - \frac{3b^2 x \log(a+bx)}{a^4 \sqrt{cx^2}}$$

Mathematica [A] time = 0.02, size = 81, normalized size = 0.79

$$\frac{cx \left(a(-a^2 + 3abx + 6b^2x^2) + 6b^2x^2 \log(x)(a+bx) - 6b^2x^2(a+bx) \log(a+bx) \right)}{2a^4 (cx^2)^{3/2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[1/(x^2*Sqrt[c*x^2]*(a+b*x)^2),x]

[Out] (c*x*(a*(-a^2 + 3*a*b*x + 6*b^2*x^2) + 6*b^2*x^2*(a+b*x)*Log[x] - 6*b^2*x^2*(a+b*x)*Log[a+b*x]))/(2*a^4*(c*x^2)^(3/2)*(a+b*x))

fricas [A] time = 0.42, size = 79, normalized size = 0.77

$$\frac{(6ab^2x^2 + 3a^2bx - a^3 + 6(b^3x^3 + ab^2x^2) \log\left(\frac{x}{bx+a}\right)) \sqrt{cx^2}}{2(a^4bcx^4 + a^5cx^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] 1/2*(6*a*b^2*x^2 + 3*a^2*b*x - a^3 + 6*(b^3*x^3 + a*b^2*x^2)*log(x/(b*x + a)))*sqrt(c*x^2)/(a^4*b*c*x^4 + a^5*c*x^3)

giac [A] time = 1.22, size = 152, normalized size = 1.48

$$\frac{\frac{6b^2 \log\left(\left|-\frac{a}{bx+a}+1\right|\right)}{a^4 \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} + \frac{2b^2}{(bx+a)a^3 \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} - \frac{\frac{6ab^2}{bx+a}-5b^2}{a^4\left(\frac{a}{bx+a}-1\right)^2 \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)}}{2\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out]
$$-1/2*(6*b^2*\log(\text{abs}(-a/(b*x + a) + 1)))/(a^4*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) + 2*b^2/((b*x + a)*a^3*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) - (6*a*b^2/(b*x + a) - 5*b^2)/(a^4*(a/(b*x + a) - 1)^2*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)))/\text{sqrt}(c)$$

maple [A] time = 0.01, size = 95, normalized size = 0.92

$$\frac{6b^3x^3 \ln(x) - 6b^3x^3 \ln(bx + a) + 6ab^2x^2 \ln(x) - 6ab^2x^2 \ln(bx + a) + 6ab^2x^2 + 3a^2bx - a^3}{2\sqrt{cx^2} (bx + a) a^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(b*x+a)^2/(c*x^2)^(1/2),x)

[Out]
$$1/2/x*(6*b^3*x^3*\ln(x) - 6*b^3*x^3*\ln(b*x+a) + 6*a*b^2*x^2*\ln(x) - 6*a*b^2*x^2*\ln(b*x+a) + 6*a*b^2*x^2 + 3*a^2*b*x - a^3)/(c*x^2)^(1/2)/a^4/(b*x+a)$$

maxima [A] time = 1.41, size = 76, normalized size = 0.74

$$\frac{6b^2x^2 + 3abx - a^2}{2(a^3b\sqrt{c}x^3 + a^4\sqrt{c}x^2)} - \frac{3b^2 \log(bx + a)}{a^4\sqrt{c}} + \frac{3b^2 \log(x)}{a^4\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")

[Out]
$$1/2*(6*b^2*x^2 + 3*a*b*x - a^2)/(a^3*b*\text{sqrt}(c)*x^3 + a^4*\text{sqrt}(c)*x^2) - 3*b^2*\log(b*x + a)/(a^4*\text{sqrt}(c)) + 3*b^2*\log(x)/(a^4*\text{sqrt}(c))$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{x^2 \sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^2*(c*x^2)^(1/2)*(a + b*x)^2),x)

[Out] int(1/(x^2*(c*x^2)^(1/2)*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{x^2 \sqrt{cx^2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**2/(b*x+a)**2/(c*x**2)**(1/2),x)
```

```
[Out] Integral(1/(x**2*sqrt(c*x**2)*(a + b*x)**2), x)
```


$$3.917 \quad \int \frac{x^5}{(cx^2)^{3/2} (a+bx)^2} dx$$

Optimal. Leaf size=73

$$-\frac{a^2x}{b^3c\sqrt{cx^2}(a+bx)} - \frac{2ax \log(a+bx)}{b^3c\sqrt{cx^2}} + \frac{x^2}{b^2c\sqrt{cx^2}}$$

[Out] $x^2/b^2/c/(c*x^2)^{(1/2)} - a^2*x/b^3/c/(b*x+a)/(c*x^2)^{(1/2)} - 2*a*x*\ln(b*x+a)/b^3/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 73, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^2x}{b^3c\sqrt{cx^2}(a+bx)} - \frac{2ax \log(a+bx)}{b^3c\sqrt{cx^2}} + \frac{x^2}{b^2c\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^5/((c*x^2)^(3/2)*(a + b*x)^2), x]

[Out] $x^2/(b^2*c*\text{Sqrt}[c*x^2]) - (a^2*x)/(b^3*c*\text{Sqrt}[c*x^2]*(a + b*x)) - (2*a*x*\text{Log}[a + b*x])/(b^3*c*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^5}{(cx^2)^{3/2} (a+bx)^2} dx &= \frac{x \int \frac{x^2}{(a+bx)^2} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{1}{b^2} + \frac{a^2}{b^2(a+bx)^2} - \frac{2a}{b^2(a+bx)} \right) dx}{c\sqrt{cx^2}} \\ &= \frac{x^2}{b^2c\sqrt{cx^2}} - \frac{a^2x}{b^3c\sqrt{cx^2}(a+bx)} - \frac{2ax \log(a+bx)}{b^3c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 54, normalized size = 0.74

$$\frac{x^3 \left(-a^2 + abx - 2a(a+bx) \log(a+bx) + b^2x^2 \right)}{b^3 (cx^2)^{3/2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/((c*x^2)^(3/2)*(a + b*x)^2),x]

[Out] (x^3*(-a^2 + a*b*x + b^2*x^2 - 2*a*(a + b*x)*Log[a + b*x]))/(b^3*(c*x^2)^(3/2)*(a + b*x))

fricas [A] time = 0.43, size = 63, normalized size = 0.86

$$\frac{(b^2x^2 + abx - a^2 - 2(abx + a^2) \log(bx + a))\sqrt{cx^2}}{b^4c^2x^2 + ab^3c^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] (b^2*x^2 + a*b*x - a^2 - 2*(a*b*x + a^2)*log(b*x + a))*sqrt(c*x^2)/(b^4*c^2*x^2 + a*b^3*c^2*x)

giac [A] time = 1.26, size = 127, normalized size = 1.74

$$\frac{2a \log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b^3 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} + \frac{bx+a}{b^3 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} - \frac{a^2}{(bx+a)b^3 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} \cdot \frac{1}{c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="giac")

[Out] $-(2*a*\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b))))/(b^3*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) + (b*x + a)/(b^3*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) - a^2/((b*x + a)*b^3*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2))/c^{3/2}$

maple [A] time = 0.00, size = 62, normalized size = 0.85

$$\frac{(2abx \ln(bx + a) - b^2x^2 + 2a^2 \ln(bx + a) - abx + a^2)x^3}{(cx^2)^{\frac{3}{2}}(bx + a)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/(c*x^2)^(3/2)/(b*x+a)^2,x)

[Out] $-x^3*(2*a*b*x*\ln(b*x+a)-b^2*x^2+2*a^2*\ln(b*x+a)-a*b*x+a^2)/(c*x^2)^{3/2}/b^3/(b*x+a)$

maxima [B] time = 1.61, size = 149, normalized size = 2.04

$$\frac{a^3}{\sqrt{cx^2}b^5cx + \sqrt{cx^2}ab^4c} + \frac{x^2}{\sqrt{cx^2}b^2c} - \frac{2(-1)^{\frac{2acx}{b}}a \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^3c^{\frac{3}{2}}} + \frac{2ax}{\sqrt{cx^2}b^3c} - \frac{2a \log(bx)}{b^3c^{\frac{3}{2}}} - \frac{5a^2}{\sqrt{cx^2}b^4c} + \frac{4a^2}{b^4c^{\frac{3}{2}}x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="maxima")

[Out] $a^3/(\text{sqrt}(c*x^2)*b^5*c*x + \text{sqrt}(c*x^2)*a*b^4*c) + x^2/(\text{sqrt}(c*x^2)*b^2*c) - 2*(-1)^{(2*a*c*x/b)}*a*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(b^3*c^{3/2}) + 2*a*x/(\text{sqrt}(c*x^2)*b^3*c) - 2*a*\log(b*x)/(b^3*c^{3/2}) - 5*a^2/(\text{sqrt}(c*x^2)*b^4*c) + 4*a^2/(b^4*c^{3/2}*x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^5}{(cx^2)^{3/2}(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/((c*x^2)^(3/2)*(a + b*x)^2),x)

[Out] int(x^5/((c*x^2)^(3/2)*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^5}{(cx^2)^{\frac{3}{2}}(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5/(c*x**2)**(3/2)/(b*x+a)**2,x)
```

```
[Out] Integral(x**5/((c*x**2)**(3/2)*(a + b*x)**2), x)
```

$$3.918 \quad \int \frac{x^4}{(cx^2)^{3/2} (a+bx)^2} dx$$

Optimal. Leaf size=49

$$\frac{ax}{b^2c\sqrt{cx^2}(a+bx)} + \frac{x \log(a+bx)}{b^2c\sqrt{cx^2}}$$

[Out] a*x/b^2/c/(b*x+a)/(c*x^2)^(1/2)+x*ln(b*x+a)/b^2/c/(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{ax}{b^2c\sqrt{cx^2}(a+bx)} + \frac{x \log(a+bx)}{b^2c\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x^4/((c*x^2)^(3/2)*(a + b*x)^2), x]

[Out] (a*x)/(b^2*c*Sqrt[c*x^2]*(a + b*x)) + (x*Log[a + b*x])/(b^2*c*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4}{(cx^2)^{3/2} (a+bx)^2} dx &= \frac{x \int \frac{x}{(a+bx)^2} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(-\frac{a}{b(a+bx)^2} + \frac{1}{b(a+bx)} \right) dx}{c\sqrt{cx^2}} \\ &= \frac{ax}{b^2 c \sqrt{cx^2} (a+bx)} + \frac{x \log(a+bx)}{b^2 c \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 37, normalized size = 0.76

$$\frac{x^3((a+bx)\log(a+bx)+a)}{b^2 (cx^2)^{3/2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/((c*x^2)^(3/2)*(a + b*x)^2),x]

[Out] (x^3*(a + (a + b*x)*Log[a + b*x]))/(b^2*(c*x^2)^(3/2)*(a + b*x))

fricas [A] time = 0.42, size = 44, normalized size = 0.90

$$\frac{\sqrt{cx^2} \left((bx+a) \log(bx+a) + a \right)}{b^3 c^2 x^2 + ab^2 c^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] sqrt(c*x^2)*((b*x + a)*log(b*x + a) + a)/(b^3*c^2*x^2 + a*b^2*c^2*x)

giac [A] time = 1.03, size = 89, normalized size = 1.82

$$\frac{\log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b^2 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} - \frac{a}{(bx+a)b^2 \operatorname{sgn}\left(-\frac{b}{bx+a} + \frac{ab}{(bx+a)^2}\right)} \frac{3}{c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="giac")

[Out] $(\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b)))/(b^2*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) - a/((b*x + a)*b^2*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)))/c^{(3/2)}$

maple [A] time = 0.00, size = 41, normalized size = 0.84

$$\frac{(bx \ln (bx + a) + a \ln (bx + a) + a) x^3}{(c x^2)^{\frac{3}{2}} (bx + a) b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^4/(c*x^2)^{(3/2)}/(b*x+a)^2, x)$

[Out] $x^3*(b*x*\ln(b*x+a)+a*\ln(b*x+a)+a)/(c*x^2)^{(3/2)}/b^2/(b*x+a)$

maxima [B] time = 1.56, size = 108, normalized size = 2.20

$$-\frac{a^2}{\sqrt{cx^2} b^4 cx + \sqrt{cx^2} ab^3 c} + \frac{(-1)^{\frac{2acx}{b}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{b^2 c^{\frac{3}{2}}} + \frac{\log(bx)}{b^2 c^{\frac{3}{2}}} + \frac{3a}{\sqrt{cx^2} b^3 c} - \frac{2a}{b^3 c^{\frac{3}{2}} x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x^4/(c*x^2)^{(3/2)}/(b*x+a)^2, x, \text{algorithm}="maxima")$

[Out] $-a^2/(\text{sqrt}(c*x^2)*b^4*c*x + \text{sqrt}(c*x^2)*a*b^3*c) + (-1)^{(2*a*c*x/b)}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(b^2*c^{(3/2)}) + \log(b*x)/(b^2*c^{(3/2)}) + 3*a/(\text{sqrt}(c*x^2)*b^3*c) - 2*a/(b^3*c^{(3/2)}*x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^4}{(c x^2)^{3/2} (a + b x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x^4/((c*x^2)^{(3/2)}*(a + b*x)^2), x)$

[Out] $\text{int}(x^4/((c*x^2)^{(3/2)}*(a + b*x)^2), x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^4}{(c x^2)^{\frac{3}{2}} (a + b x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4/(c*x**2)**(3/2)/(b*x+a)**2,x)
```

```
[Out] Integral(x**4/((c*x**2)**(3/2)*(a + b*x)**2), x)
```


$$3.919 \quad \int \frac{x^3}{(cx^2)^{3/2} (a+bx)^2} dx$$

Optimal. Leaf size=25

$$-\frac{x}{bc\sqrt{cx^2} (a+bx)}$$

[Out] $-x/b/c/(b*x+a)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 25, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$-\frac{x}{bc\sqrt{cx^2} (a+bx)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3/((c*x^2)^{(3/2)}*(a + b*x)^2), x]$

[Out] $-(x/(b*c*\text{Sqrt}[c*x^2]*(a + b*x)))$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}/(b*(m+1)), x] /;$ FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{x^3}{(cx^2)^{3/2} (a+bx)^2} dx &= \frac{x \int \frac{1}{(a+bx)^2} dx}{c\sqrt{cx^2}} \\ &= -\frac{x}{bc\sqrt{cx^2} (a+bx)} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.96

$$-\frac{x^3}{b(c x^2)^{3/2}(a + b x)}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/((c*x^2)^(3/2)*(a + b*x)^2),x]

[Out] -(x^3/(b*(c*x^2)^(3/2)*(a + b*x)))

fricas [A] time = 0.42, size = 29, normalized size = 1.16

$$-\frac{\sqrt{c x^2}}{b^2 c^2 x^2 + a b c^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] -sqrt(c*x^2)/(b^2*c^2*x^2 + a*b*c^2*x)

giac [A] time = 1.16, size = 38, normalized size = 1.52

$$\frac{1}{(b x + a) b c^{\frac{3}{2}} \operatorname{sgn}\left(-\frac{b}{b x + a} + \frac{a b}{(b x + a)^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="giac")

[Out] 1/((b*x + a)*b*c^(3/2)*sgn(-b/(b*x + a) + a*b/(b*x + a)^2))

maple [A] time = 0.00, size = 23, normalized size = 0.92

$$-\frac{x^3}{(b x + a) (c x^2)^{\frac{3}{2}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/(c*x^2)^(3/2)/(b*x+a)^2,x)

[Out] -1/(b*x+a)/b*x^3/(c*x^2)^(3/2)

maxima [B] time = 1.48, size = 47, normalized size = 1.88

$$\frac{a}{\sqrt{cx^2} b^3 cx + \sqrt{cx^2} ab^2 c} - \frac{1}{\sqrt{cx^2} b^2 c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="maxima")

[Out] a/(sqrt(c*x^2)*b^3*c*x + sqrt(c*x^2)*a*b^2*c) - 1/(sqrt(c*x^2)*b^2*c)

mupad [B] time = 0.17, size = 25, normalized size = 1.00

$$-\frac{\sqrt{cx^2}}{bc^2x(a+bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/((c*x^2)^(3/2)*(a + b*x)^2), x)

[Out] -(c*x^2)^(1/2)/(b*c^2*x*(a + b*x))

sympy [A] time = 1.94, size = 90, normalized size = 3.60

$$\left\{ \begin{array}{ll} \frac{\infty x^2}{c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} & \text{for } a = 0 \wedge b = 0 \\ \frac{\infty x^4}{c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} & \text{for } a = -bx \\ \frac{x^4}{a^2 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} & \text{for } b = 0 \\ -\frac{x^3}{abc^{\frac{3}{2}} (x^2)^{\frac{3}{2}} + b^2 c^{\frac{3}{2}} x (x^2)^{\frac{3}{2}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/(c*x**2)**(3/2)/(b*x+a)**2,x)

[Out] Piecewise((zoo*x**2/(c**(3/2)*(x**2)**(3/2)), Eq(a, 0) & Eq(b, 0)), (zoo*x**4/(c**(3/2)*(x**2)**(3/2)), Eq(a, -b*x)), (x**4/(a**2*c**(3/2)*(x**2)**(3/2)), Eq(b, 0)), (-x**3/(a*b*c**(3/2)*(x**2)**(3/2) + b**2*c**(3/2)*x*(x**2)**(3/2)), True))

$$3.920 \quad \int \frac{x^2}{(cx^2)^{3/2} (a+bx)^2} dx$$

Optimal. Leaf size=68

$$-\frac{x \log(a+bx)}{a^2 c \sqrt{cx^2}} + \frac{x \log(x)}{a^2 c \sqrt{cx^2}} + \frac{x}{ac \sqrt{cx^2} (a+bx)}$$

[Out] x/a/c/(b*x+a)/(c*x^2)^(1/2)+x*ln(x)/a^2/c/(c*x^2)^(1/2)-x*ln(b*x+a)/a^2/c/(c*x^2)^(1/2)

Rubi [A] time = 0.02, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 44}

$$-\frac{x \log(a+bx)}{a^2 c \sqrt{cx^2}} + \frac{x \log(x)}{a^2 c \sqrt{cx^2}} + \frac{x}{ac \sqrt{cx^2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Int[x^2/((c*x^2)^(3/2)*(a + b*x)^2), x]

[Out] x/(a*c*Sqrt[c*x^2]*(a + b*x)) + (x*Log[x])/(a^2*c*Sqrt[c*x^2]) - (x*Log[a + b*x])/(a^2*c*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(cx^2)^{3/2} (a+bx)^2} dx &= \frac{x \int \frac{1}{x(a+bx)^2} dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{1}{a^2x} - \frac{b}{a(a+bx)^2} - \frac{b}{a^2(a+bx)} \right) dx}{c\sqrt{cx^2}} \\ &= \frac{x}{ac\sqrt{cx^2} (a+bx)} + \frac{x \log(x)}{a^2c\sqrt{cx^2}} - \frac{x \log(a+bx)}{a^2c\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 46, normalized size = 0.68

$$\frac{x^3(\log(x)(a+bx) - (a+bx)\log(a+bx) + a)}{a^2 (cx^2)^{3/2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/((c*x^2)^(3/2)*(a+b*x)^2),x]

[Out] (x^3*(a+(a+b*x)*Log[x]-(a+b*x)*Log[a+b*x]))/(a^2*(c*x^2)^(3/2)*(a+b*x))

fricas [A] time = 0.43, size = 48, normalized size = 0.71

$$\frac{\sqrt{cx^2} \left((bx+a) \log\left(\frac{x}{bx+a}\right) + a \right)}{a^2bc^2x^2 + a^3c^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] sqrt(c*x^2)*((b*x+a)*log(x/(b*x+a))+a)/(a^2*b*c^2*x^2+a^3*c^2*x)

giac [A] time = 1.06, size = 83, normalized size = 1.22

$$\frac{\log\left(\left|-\frac{a}{bx+a}+1\right|\right)}{a^2\operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} + \frac{1}{(bx+a)a\operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} - \frac{3}{c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="giac")

[Out] $-(\log(\text{abs}(-a/(b*x + a) + 1)))/(a^2*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) + 1/((b*x + a)*a*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2))/c^{(3/2)}$

maple [A] time = 0.01, size = 52, normalized size = 0.76

$$\frac{(bx \ln(x) - bx \ln(bx + a) + a \ln(x) - a \ln(bx + a) + a)x^3}{(cx^2)^{\frac{3}{2}}(bx + a)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/(c*x^2)^(3/2)/(b*x+a)^2,x)`

[Out] $x^3*(b*x*\ln(x)-b*x*\ln(b*x+a)+a*\ln(x)-a*\ln(b*x+a)+a)/(c*x^2)^{(3/2)}/a^2/(b*x+a)$

maxima [A] time = 1.52, size = 82, normalized size = 1.21

$$-\frac{1}{\sqrt{cx^2} b^2 cx + \sqrt{cx^2} abc} - \frac{(-1)^{\frac{2acx}{b}} \log\left(-\frac{2acx}{b|bx+a|}\right)}{a^2 c^{\frac{3}{2}}} + \frac{1}{\sqrt{cx^2} abc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="maxima")`

[Out] $-1/(\text{sqrt}(c*x^2)*b^2*c*x + \text{sqrt}(c*x^2)*a*b*c) - (-1)^{(2*a*c*x/b)}*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(a^2*c^{(3/2)}) + 1/(\text{sqrt}(c*x^2)*a*b*c)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x^2}{(cx^2)^{3/2} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/((c*x^2)^(3/2)*(a + b*x)^2),x)`

[Out] `int(x^2/((c*x^2)^(3/2)*(a + b*x)^2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2}{(cx^2)^{\frac{3}{2}} (a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2/(c*x**2)**(3/2)/(b*x+a)**2,x)
```

```
[Out] Integral(x**2/((c*x**2)**(3/2)*(a + b*x)**2), x)
```

$$3.921 \quad \int \frac{x}{(cx^2)^{3/2} (a+bx)^2} dx$$

Optimal. Leaf size=90

$$-\frac{2bx \log(x)}{a^3 c \sqrt{cx^2}} + \frac{2bx \log(a+bx)}{a^3 c \sqrt{cx^2}} - \frac{bx}{a^2 c \sqrt{cx^2} (a+bx)} - \frac{1}{a^2 c \sqrt{cx^2}}$$

[Out] $-1/a^2/c/(c*x^2)^{(1/2)}-b*x/a^2/c/(b*x+a)/(c*x^2)^{(1/2)}-2*b*x*\ln(x)/a^3/c/(c*x^2)^{(1/2)}+2*b*x*\ln(b*x+a)/a^3/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 90, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 44}

$$-\frac{bx}{a^2 c \sqrt{cx^2} (a+bx)} - \frac{2bx \log(x)}{a^3 c \sqrt{cx^2}} + \frac{2bx \log(a+bx)}{a^3 c \sqrt{cx^2}} - \frac{1}{a^2 c \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[x/((c*x^2)^(3/2)*(a + b*x)^2),x]

[Out] $-(1/(a^2*c*\text{Sqrt}[c*x^2])) - (b*x)/(a^2*c*\text{Sqrt}[c*x^2]*(a + b*x)) - (2*b*x*\text{Log}[x])/(a^3*c*\text{Sqrt}[c*x^2]) + (2*b*x*\text{Log}[a + b*x])/(a^3*c*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{x}{(cx^2)^{3/2} (a+bx)^2} dx &= \frac{x \int \frac{1}{x^2(a+bx)^2} dx}{c\sqrt{cx^2}} \\
&= \frac{x \int \left(\frac{1}{a^2x^2} - \frac{2b}{a^3x} + \frac{b^2}{a^2(a+bx)^2} + \frac{2b^2}{a^3(a+bx)} \right) dx}{c\sqrt{cx^2}} \\
&= -\frac{1}{a^2c\sqrt{cx^2}} - \frac{bx}{a^2c\sqrt{cx^2}(a+bx)} - \frac{2bx \log(x)}{a^3c\sqrt{cx^2}} + \frac{2bx \log(a+bx)}{a^3c\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 59, normalized size = 0.66

$$\frac{x^2(-a(a+2bx) - 2bx \log(x)(a+bx) + 2bx(a+bx) \log(a+bx))}{a^3 (cx^2)^{3/2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[x/((c*x^2)^(3/2)*(a + b*x)^2), x]

[Out] (x^2*(-(a*(a + 2*b*x)) - 2*b*x*(a + b*x)*Log[x] + 2*b*x*(a + b*x)*Log[a + b*x]))/(a^3*(c*x^2)^(3/2)*(a + b*x))

fricas [A] time = 0.44, size = 66, normalized size = 0.73

$$-\frac{\left(2abx + a^2 - 2(b^2x^2 + abx) \log\left(\frac{bx+a}{x}\right)\right)\sqrt{cx^2}}{a^3bc^2x^3 + a^4c^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] -(2*a*b*x + a^2 - 2*(b^2*x^2 + a*b*x)*log((b*x + a)/x))*sqrt(c*x^2)/(a^3*b*c^2*x^3 + a^4*c^2*x^2)

giac [A] time = 1.11, size = 137, normalized size = 1.52

$$\frac{2b^2 \log\left(\left|-\frac{a}{bx+a}+1\right|\right)}{a^3 \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} + \frac{b^2}{(bx+a)a^2 \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} - \frac{b^2}{a^3\left(\frac{a}{bx+a}-1\right) \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)}$$

$$bc^{\frac{3}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="giac")

[Out] (2*b^2*log(abs(-a/(b*x + a) + 1))/(a^3*sgn(-b/(b*x + a) + a*b/(b*x + a)^2)) + b^2/((b*x + a)*a^2*sgn(-b/(b*x + a) + a*b/(b*x + a)^2)) - b^2/(a^3*(a/(b*x + a) - 1)*sgn(-b/(b*x + a) + a*b/(b*x + a)^2)))/(b*c^(3/2))

maple [A] time = 0.00, size = 74, normalized size = 0.82

$$\frac{(2b^2x^2 \ln(x) - 2b^2x^2 \ln(bx + a) + 2abx \ln(x) - 2abx \ln(bx + a) + 2abx + a^2)x^2}{(cx^2)^{\frac{3}{2}}(bx + a)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(c*x^2)^(3/2)/(b*x+a)^2,x)

[Out] -x^2*(2*b^2*x^2*ln(x)-2*b^2*x^2*ln(b*x+a)+2*a*b*x*ln(x)-2*a*b*x*ln(b*x+a)+2*a*b*x+a^2)/(c*x^2)^(3/2)/a^3/(b*x+a)

maxima [A] time = 1.41, size = 79, normalized size = 0.88

$$\frac{1}{\sqrt{cx^2} abcx + \sqrt{cx^2} a^2c} + \frac{2 (-1)^{\frac{2acx}{b}} b \log\left(-\frac{2acx}{b|bx+a|}\right)}{a^3 c^{\frac{3}{2}}} - \frac{2}{\sqrt{cx^2} a^2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="maxima")

[Out] 1/(sqrt(c*x^2)*a*b*c*x + sqrt(c*x^2)*a^2*c) + 2*(-1)^(2*a*c*x/b)*b*log(-2*a*c*x/(b*abs(b*x + a)))/(a^3*c^(3/2)) - 2/(sqrt(c*x^2)*a^2*c)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{x}{(cx^2)^{\frac{3}{2}}(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/((c*x^2)^(3/2)*(a + b*x)^2),x)

[Out] int(x/((c*x^2)^(3/2)*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x}{(cx^2)^{\frac{3}{2}}(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x/(c*x**2)**(3/2)/(b*x+a)**2,x)
```

```
[Out] Integral(x/((c*x**2)**(3/2)*(a + b*x)**2), x)
```

$$3.922 \quad \int \frac{1}{(cx^2)^{3/2} (a+bx)^2} dx$$

Optimal. Leaf size=118

$$\frac{3b^2x \log(x)}{a^4c\sqrt{cx^2}} - \frac{3b^2x \log(a+bx)}{a^4c\sqrt{cx^2}} + \frac{b^2x}{a^3c\sqrt{cx^2} (a+bx)} + \frac{2b}{a^3c\sqrt{cx^2}} - \frac{1}{2a^2cx\sqrt{cx^2}}$$

[Out] $2*b/a^3/c/(c*x^2)^{(1/2)}-1/2/a^2/c/x/(c*x^2)^{(1/2)}+b^2*x/a^3/c/(b*x+a)/(c*x^2)^{(1/2)}+3*b^2*x*\ln(x)/a^4/c/(c*x^2)^{(1/2)}-3*b^2*x*\ln(b*x+a)/a^4/c/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 118, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 44}

$$\frac{b^2x}{a^3c\sqrt{cx^2} (a+bx)} + \frac{3b^2x \log(x)}{a^4c\sqrt{cx^2}} - \frac{3b^2x \log(a+bx)}{a^4c\sqrt{cx^2}} + \frac{2b}{a^3c\sqrt{cx^2}} - \frac{1}{2a^2cx\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[1/((c*x^2)^(3/2)*(a + b*x)^2), x]

[Out] $(2*b)/(a^3*c*\text{Sqrt}[c*x^2]) - 1/(2*a^2*c*x*\text{Sqrt}[c*x^2]) + (b^2*x)/(a^3*c*\text{Sqrt}[c*x^2]*(a + b*x)) + (3*b^2*x*\text{Log}[x])/(a^4*c*\text{Sqrt}[c*x^2]) - (3*b^2*x*\text{Log}[a + b*x])/(a^4*c*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(cx^2)^{3/2} (a+bx)^2} dx &= \frac{x \int \frac{1}{x^3(a+bx)^2} dx}{c\sqrt{cx^2}} \\
&= \frac{x \int \left(\frac{1}{a^2x^3} - \frac{2b}{a^3x^2} + \frac{3b^2}{a^4x} - \frac{b^3}{a^3(a+bx)^2} - \frac{3b^3}{a^4(a+bx)} \right) dx}{c\sqrt{cx^2}} \\
&= \frac{2b}{a^3c\sqrt{cx^2}} - \frac{1}{2a^2cx\sqrt{cx^2}} + \frac{b^2x}{a^3c\sqrt{cx^2}(a+bx)} + \frac{3b^2x \log(x)}{a^4c\sqrt{cx^2}} - \frac{3b^2x \log(a+bx)}{a^4c\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 80, normalized size = 0.68

$$\frac{x \left(a \left(-a^2 + 3abx + 6b^2x^2 \right) + 6b^2x^2 \log(x)(a+bx) - 6b^2x^2(a+bx) \log(a+bx) \right)}{2a^4 (cx^2)^{3/2} (a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[1/((c*x^2)^(3/2)*(a + b*x)^2), x]

[Out] (x*(a*(-a^2 + 3*a*b*x + 6*b^2*x^2) + 6*b^2*x^2*(a + b*x)*Log[x] - 6*b^2*x^2*(a + b*x)*Log[a + b*x]))/(2*a^4*(c*x^2)^(3/2)*(a + b*x))

fricas [A] time = 0.44, size = 83, normalized size = 0.70

$$\frac{(6ab^2x^2 + 3a^2bx - a^3 + 6(b^3x^3 + ab^2x^2) \log\left(\frac{x}{bx+a}\right))\sqrt{cx^2}}{2(a^4bc^2x^4 + a^5c^2x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c*x^2)^(3/2)/(b*x+a)^2, x, algorithm="fricas")

[Out] 1/2*(6*a*b^2*x^2 + 3*a^2*b*x - a^3 + 6*(b^3*x^3 + a*b^2*x^2)*log(x/(b*x + a)))*sqrt(c*x^2)/(a^4*b*c^2*x^4 + a^5*c^2*x^3)

giac [A] time = 1.03, size = 152, normalized size = 1.29

$$\frac{\frac{6b^2 \log\left(\left|-\frac{a}{bx+a}+1\right|\right)}{a^4 \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} + \frac{2b^2}{(bx+a)a^3 \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)} - \frac{\frac{6ab^2}{bx+a}-5b^2}{a^4\left(\frac{a}{bx+a}-1\right)^2 \operatorname{sgn}\left(-\frac{b}{bx+a}+\frac{ab}{(bx+a)^2}\right)}}{2c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="giac")

[Out]
$$-1/2*(6*b^2*\log(\text{abs}(-a/(b*x + a) + 1))/(a^4*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) + 2*b^2/((b*x + a)*a^3*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)) - (6*a*b^2/(b*x + a) - 5*b^2)/(a^4*(a/(b*x + a) - 1)^2*\text{sgn}(-b/(b*x + a) + a*b/(b*x + a)^2)))/c^{3/2}$$

maple [A] time = 0.01, size = 93, normalized size = 0.79

$$\frac{(6b^3x^3 \ln(x) - 6b^3x^3 \ln(bx + a) + 6ab^2x^2 \ln(x) - 6ab^2x^2 \ln(bx + a) + 6ab^2x^2 + 3a^2bx - a^3)x}{2(c x^2)^{\frac{3}{2}}(bx + a)a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c*x^2)^(3/2)/(b*x+a)^2,x)

[Out]
$$1/2*x*(6*b^3*x^3*\ln(x) - 6*b^3*x^3*\ln(b*x+a) + 6*a*b^2*x^2*\ln(x) - 6*a*b^2*x^2*\ln(b*x+a) + 6*a*b^2*x^2 + 3*a^2*b*x - a^3)/(c*x^2)^{3/2}/a^4/(b*x+a)$$

maxima [A] time = 1.46, size = 98, normalized size = 0.83

$$-\frac{b}{\sqrt{cx^2}a^2bcx + \sqrt{cx^2}a^3c} - \frac{3(-1)^{\frac{2acx}{b}}b^2\log\left(-\frac{2acx}{b|bx+a|}\right)}{a^4c^{\frac{3}{2}}} + \frac{3b}{\sqrt{cx^2}a^3c} - \frac{1}{2a^2c^{\frac{3}{2}}x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(c*x^2)^(3/2)/(b*x+a)^2,x, algorithm="maxima")

[Out]
$$-b/(\text{sqrt}(c*x^2)*a^2*b*c*x + \text{sqrt}(c*x^2)*a^3*c) - 3*(-1)^{(2*a*c*x/b)}*b^2*\log(-2*a*c*x/(b*\text{abs}(b*x + a)))/(a^4*c^{3/2}) + 3*b/(\text{sqrt}(c*x^2)*a^3*c) - 1/2/(a^2*c^{3/2}*x^2)$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(cx^2)^{3/2}(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((c*x^2)^(3/2)*(a + b*x)^2),x)

[Out] int(1/((c*x^2)^(3/2)*(a + b*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(cx^2)^{\frac{3}{2}}(a+bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(c*x**2)**(3/2)/(b*x+a)**2,x)
```

```
[Out] Integral(1/((c*x**2)**(3/2)*(a + b*x)**2), x)
```

3.923 $\int x^2 \sqrt{cx^2} (a + bx)^n dx$

Optimal. Leaf size=131

$$-\frac{a^3 \sqrt{cx^2} (a + bx)^{n+1}}{b^4(n+1)x} + \frac{3a^2 \sqrt{cx^2} (a + bx)^{n+2}}{b^4(n+2)x} - \frac{3a \sqrt{cx^2} (a + bx)^{n+3}}{b^4(n+3)x} + \frac{\sqrt{cx^2} (a + bx)^{n+4}}{b^4(n+4)x}$$

[Out] $-a^3(b*x+a)^{(1+n)}*(c*x^2)^{(1/2)}/b^4/(1+n)/x+3*a^2*(b*x+a)^{(2+n)}*(c*x^2)^{(1/2)}/b^4/(2+n)/x-3*a*(b*x+a)^{(3+n)}*(c*x^2)^{(1/2)}/b^4/(3+n)/x+(b*x+a)^{(4+n)}*(c*x^2)^{(1/2)}/b^4/(4+n)/x$

Rubi [A] time = 0.04, antiderivative size = 131, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^3 \sqrt{cx^2} (a + bx)^{n+1}}{b^4(n+1)x} + \frac{3a^2 \sqrt{cx^2} (a + bx)^{n+2}}{b^4(n+2)x} - \frac{3a \sqrt{cx^2} (a + bx)^{n+3}}{b^4(n+3)x} + \frac{\sqrt{cx^2} (a + bx)^{n+4}}{b^4(n+4)x}$$

Antiderivative was successfully verified.

[In] Int[x^2*Sqrt[c*x^2]*(a + b*x)^n,x]

[Out] $-((a^3*\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)})/(b^4*(1 + n)*x)) + (3*a^2*\text{Sqrt}[c*x^2]*(a + b*x)^{(2 + n)})/(b^4*(2 + n)*x) - (3*a*\text{Sqrt}[c*x^2]*(a + b*x)^{(3 + n)})/(b^4*(3 + n)*x) + (\text{Sqrt}[c*x^2]*(a + b*x)^{(4 + n)})/(b^4*(4 + n)*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int x^2 \sqrt{cx^2} (a+bx)^n dx &= \frac{\sqrt{cx^2} \int x^3 (a+bx)^n dx}{x} \\
&= \frac{\sqrt{cx^2} \int \left(-\frac{a^3(a+bx)^n}{b^3} + \frac{3a^2(a+bx)^{1+n}}{b^3} - \frac{3a(a+bx)^{2+n}}{b^3} + \frac{(a+bx)^{3+n}}{b^3} \right) dx}{x} \\
&= -\frac{a^3 \sqrt{cx^2} (a+bx)^{1+n}}{b^4(1+n)x} + \frac{3a^2 \sqrt{cx^2} (a+bx)^{2+n}}{b^4(2+n)x} - \frac{3a \sqrt{cx^2} (a+bx)^{3+n}}{b^4(3+n)x} + \frac{\sqrt{cx^2} (a+bx)^{4+n}}{b^4(4+n)x}
\end{aligned}$$

Mathematica [A] time = 0.07, size = 97, normalized size = 0.74

$$\frac{cx(a+bx)^{n+1} \left(-6a^3 + 6a^2b(n+1)x - 3ab^2(n^2+3n+2)x^2 + b^3(n^3+6n^2+11n+6)x^3 \right)}{b^4(n+1)(n+2)(n+3)(n+4)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*Sqrt[c*x^2]*(a + b*x)^n,x]

[Out] (c*x*(a + b*x)^(1 + n)*(-6*a^3 + 6*a^2*b*(1 + n)*x - 3*a*b^2*(2 + 3*n + n^2)*x^2 + b^3*(6 + 11*n + 6*n^2 + n^3)*x^3))/(b^4*(1 + n)*(2 + n)*(3 + n)*(4 + n)*Sqrt[c*x^2])

fricas [A] time = 0.46, size = 153, normalized size = 1.17

$$\frac{(6a^3bnx + (b^4n^3 + 6b^4n^2 + 11b^4n + 6b^4)x^4 - 6a^4 + (ab^3n^3 + 3ab^3n^2 + 2ab^3n)x^3 - 3(a^2b^2n^2 + a^2b^2n)x^2)\sqrt{cx^2}}{(b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n*(c*x^2)^(1/2),x, algorithm="fricas")

[Out] (6*a^3*b*n*x + (b^4*n^3 + 6*b^4*n^2 + 11*b^4*n + 6*b^4)*x^4 - 6*a^4 + (a*b^3*n^3 + 3*a*b^3*n^2 + 2*a*b^3*n)*x^3 - 3*(a^2*b^2*n^2 + a^2*b^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^4*n^4 + 10*b^4*n^3 + 35*b^4*n^2 + 50*b^4*n + 24*b^4)*x)

giac [B] time = 1.11, size = 300, normalized size = 2.29

$$\left(\frac{6a^4a^n \operatorname{sgn}(x)}{b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4} + \frac{(bx+a)^n b^4 n^3 x^4 \operatorname{sgn}(x) + (bx+a)^n ab^3 n^3 x^3 \operatorname{sgn}(x) + 6(bx+a)^n b^4}{b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n*(c*x^2)^(1/2),x, algorithm="giac")

[Out]
$$\frac{(6a^4a^n\operatorname{sgn}(x)/(b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4) + ((b*x + a)^nb^4n^3x^4\operatorname{sgn}(x) + (b*x + a)^na^3n^3x^3\operatorname{sgn}(x) + 6*(b*x + a)^nb^4n^2x^4\operatorname{sgn}(x) + 3*(b*x + a)^na^2b^3n^2x^3\operatorname{sgn}(x) + 11*(b*x + a)^nb^4n^2x^4\operatorname{sgn}(x) - 3*(b*x + a)^na^2b^2n^2x^2\operatorname{sgn}(x) + 2*(b*x + a)^na^3n^2x^3\operatorname{sgn}(x) + 6*(b*x + a)^nb^4x^4\operatorname{sgn}(x) - 3*(b*x + a)^na^2b^2n^2x^2\operatorname{sgn}(x) + 6*(b*x + a)^na^3b^2n^2x^2\operatorname{sgn}(x) - 6*(b*x + a)^na^4\operatorname{sgn}(x)))/(b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4))\sqrt{c}}$$

maple [A] time = 0.01, size = 136, normalized size = 1.04

$$\frac{\sqrt{cx^2} (-b^3n^3x^3 - 6b^3n^2x^3 + 3ab^2n^2x^2 - 11b^3nx^3 + 9ab^2nx^2 - 6b^3x^3 - 6a^2bnx + 6ab^2x^2 - 6a^2bx + 6a^3)(bx - (n^4 + 10n^3 + 35n^2 + 50n + 24)b^4x)}{(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^n*(c*x^2)^(1/2),x)

[Out]
$$-(c*x^2)^{(1/2)}*(b*x+a)^{(n+1)}*(-b^3n^3x^3-6b^3n^2x^3+3a*b^2n^2x^2-11*b^3n^2x^3+9a*b^2n^2x^2-6b^3x^3-6a^2*b^2n^2x^2-6a^2*b*x+6a^3)/x/b^4/(n^4+10n^3+35n^2+50n+24)$$

maxima [A] time = 1.46, size = 116, normalized size = 0.89

$$\frac{((n^3 + 6n^2 + 11n + 6)b^4\sqrt{c}x^4 + (n^3 + 3n^2 + 2n)ab^3\sqrt{c}x^3 - 3(n^2 + n)a^2b^2\sqrt{c}x^2 + 6a^3b\sqrt{c}nx - 6a^4\sqrt{c})(bx - (n^4 + 10n^3 + 35n^2 + 50n + 24)b^4)}{(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n*(c*x^2)^(1/2),x, algorithm="maxima")

[Out]
$$((n^3 + 6n^2 + 11n + 6)*b^4*\sqrt{c}*x^4 + (n^3 + 3n^2 + 2n)*a*b^3*\sqrt{c}*x^3 - 3*(n^2 + n)*a^2*b^2*\sqrt{c}*x^2 + 6*a^3*b*\sqrt{c}*n*x - 6*a^4*\sqrt{c}(c))*(b*x + a)^n/((n^4 + 10n^3 + 35n^2 + 50n + 24)*b^4)$$

mupad [B] time = 0.35, size = 214, normalized size = 1.63

$$\frac{(a + bx)^n \left(\frac{x^4 \sqrt{cx^2} (n^3 + 6n^2 + 11n + 6)}{n^4 + 10n^3 + 35n^2 + 50n + 24} - \frac{6a^4 \sqrt{cx^2}}{b^4 (n^4 + 10n^3 + 35n^2 + 50n + 24)} + \frac{6a^3 nx \sqrt{cx^2}}{b^3 (n^4 + 10n^3 + 35n^2 + 50n + 24)} + \frac{anx^3 \sqrt{cx^2} (n^2 + 3n + 2)}{b (n^4 + 10n^3 + 35n^2 + 50n + 24)} \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(c*x^2)^(1/2)*(a + b*x)^n,x)


```
+ 6*b**4*sqrt(c)*n**2*x**4*(a + b*x)**n*sqrt(x**2)/(b**4*n**4*x + 10*b**4*n
**3*x + 35*b**4*n**2*x + 50*b**4*n*x + 24*b**4*x) + 11*b**4*sqrt(c)*n*x**4*
(a + b*x)**n*sqrt(x**2)/(b**4*n**4*x + 10*b**4*n**3*x + 35*b**4*n**2*x + 50
*b**4*n*x + 24*b**4*x) + 6*b**4*sqrt(c)*x**4*(a + b*x)**n*sqrt(x**2)/(b**4*
n**4*x + 10*b**4*n**3*x + 35*b**4*n**2*x + 50*b**4*n*x + 24*b**4*x), True))
```

3.924 $\int x\sqrt{cx^2} (a + bx)^n dx$

Optimal. Leaf size=96

$$\frac{a^2\sqrt{cx^2}(a+bx)^{n+1}}{b^3(n+1)x} - \frac{2a\sqrt{cx^2}(a+bx)^{n+2}}{b^3(n+2)x} + \frac{\sqrt{cx^2}(a+bx)^{n+3}}{b^3(n+3)x}$$

[Out] $a^2(bx+a)^{(1+n)}(cx^2)^{(1/2)}/b^3/(1+n)/x - 2a(bx+a)^{(2+n)}(cx^2)^{(1/2)}/b^3/(2+n)/x + (bx+a)^{(3+n)}(cx^2)^{(1/2)}/b^3/(3+n)/x$

Rubi [A] time = 0.03, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{a^2\sqrt{cx^2}(a+bx)^{n+1}}{b^3(n+1)x} - \frac{2a\sqrt{cx^2}(a+bx)^{n+2}}{b^3(n+2)x} + \frac{\sqrt{cx^2}(a+bx)^{n+3}}{b^3(n+3)x}$$

Antiderivative was successfully verified.

[In] Int[x*Sqrt[c*x^2]*(a + b*x)^n,x]

[Out] $(a^2\sqrt{cx^2}(a+bx)^{(1+n)})/(b^3(1+n)x) - (2a\sqrt{cx^2}(a+bx)^{(2+n)})/(b^3(2+n)x) + (\sqrt{cx^2}(a+bx)^{(3+n)})/(b^3(3+n)x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_.))^(m_.), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x\sqrt{cx^2} (a+bx)^n dx &= \frac{\sqrt{cx^2} \int x^2(a+bx)^n dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(\frac{a^2(a+bx)^n}{b^2} - \frac{2a(a+bx)^{1+n}}{b^2} + \frac{(a+bx)^{2+n}}{b^2} \right) dx}{x} \\ &= \frac{a^2\sqrt{cx^2} (a+bx)^{1+n}}{b^3(1+n)x} - \frac{2a\sqrt{cx^2} (a+bx)^{2+n}}{b^3(2+n)x} + \frac{\sqrt{cx^2} (a+bx)^{3+n}}{b^3(3+n)x} \end{aligned}$$

Mathematica [A] time = 0.05, size = 68, normalized size = 0.71

$$\frac{cx(a+bx)^{n+1} \left(2a^2 - 2ab(n+1)x + b^2(n^2 + 3n + 2)x^2 \right)}{b^3(n+1)(n+2)(n+3)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[x*Sqrt[c*x^2]*(a + b*x)^n,x]

[Out] (c*x*(a + b*x)^(1 + n)*(2*a^2 - 2*a*b*(1 + n)*x + b^2*(2 + 3*n + n^2)*x^2)) / (b^3*(1 + n)*(2 + n)*(3 + n)*Sqrt[c*x^2])

fricas [A] time = 0.46, size = 106, normalized size = 1.10

$$\frac{(2a^2bnx - (b^3n^2 + 3b^3n + 2b^3)x^3 - 2a^3 - (ab^2n^2 + ab^2n)x^2)\sqrt{cx^2}(bx+a)^n}{(b^3n^3 + 6b^3n^2 + 11b^3n + 6b^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n*(c*x^2)^(1/2),x, algorithm="fricas")

[Out] -(2*a^2*b*n*x - (b^3*n^2 + 3*b^3*n + 2*b^3)*x^3 - 2*a^3 - (a*b^2*n^2 + a*b^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^3*n^3 + 6*b^3*n^2 + 11*b^3*n + 6*b^3)*x)

giac [B] time = 0.96, size = 200, normalized size = 2.08

$$\left(\frac{2a^3a^n \operatorname{sgn}(x)}{b^3n^3 + 6b^3n^2 + 11b^3n + 6b^3} - \frac{(bx+a)^n b^3n^2x^3 \operatorname{sgn}(x) + (bx+a)^n ab^2n^2x^2 \operatorname{sgn}(x) + 3(bx+a)^n b^3nx^3 \operatorname{sgn}(x) + b^3n^3}{b^3n^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n*(c*x^2)^(1/2),x, algorithm="giac")

[Out] $-(2a^3a^n \operatorname{sgn}(x)/(b^3n^3 + 6b^3n^2 + 11b^3n + 6b^3) - ((bx + a)^n b^3n^2x^3 \operatorname{sgn}(x) + (bx + a)^n a b^2n^2x^2 \operatorname{sgn}(x) + 3(bx + a)^n b^3n x^3 \operatorname{sgn}(x) + (bx + a)^n a b^2n x^2 \operatorname{sgn}(x) + 2(bx + a)^n b^3x^3 \operatorname{sgn}(x) - 2(bx + a)^n a^2 b n x \operatorname{sgn}(x) + 2(bx + a)^n a^3 \operatorname{sgn}(x))/(b^3n^3 + 6b^3n^2 + 11b^3n + 6b^3)) \sqrt{c} (bx + a)^{n+1}$

maple [A] time = 0.01, size = 83, normalized size = 0.86

$$\frac{(b^2n^2x^2 + 3b^2nx^2 - 2abnx + 2b^2x^2 - 2abx + 2a^2) \sqrt{cx^2} (bx + a)^{n+1}}{(n^3 + 6n^2 + 11n + 6) b^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{int}(x*(bx+a)^n*(cx^2)^{(1/2)}, x)$

[Out] $(bx+a)^{(n+1)}*(b^2n^2x^2+3b^2nx^2-2a*b*n*x+2*b^2*x^2-2*a*b*x+2*a^2)*(cx^2)^{(1/2)}/x/b^3/(n^3+6n^2+11n+6)$

maxima [A] time = 1.41, size = 80, normalized size = 0.83

$$\frac{((n^2 + 3n + 2)b^3\sqrt{c}x^3 + (n^2 + n)ab^2\sqrt{c}x^2 - 2a^2b\sqrt{c}nx + 2a^3\sqrt{c})(bx + a)^n}{(n^3 + 6n^2 + 11n + 6)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{integrate}(x*(bx+a)^n*(cx^2)^{(1/2)}, x, \operatorname{algorithm}="maxima")$

[Out] $((n^2 + 3n + 2)*b^3*\sqrt{c}*x^3 + (n^2 + n)*a*b^2*\sqrt{c}*x^2 - 2*a^2*b*\sqrt{c}*n*x + 2*a^3*\sqrt{c})*(bx + a)^n/((n^3 + 6n^2 + 11n + 6)*b^3)$

mupad [B] time = 0.25, size = 142, normalized size = 1.48

$$\frac{(a + bx)^n \left(\frac{2a^3 \sqrt{cx^2}}{b^3(n^3 + 6n^2 + 11n + 6)} + \frac{x^3 \sqrt{cx^2} (n^2 + 3n + 2)}{n^3 + 6n^2 + 11n + 6} - \frac{2a^2 n x \sqrt{cx^2}}{b^2(n^3 + 6n^2 + 11n + 6)} + \frac{a n x^2 \sqrt{cx^2} (n + 1)}{b(n^3 + 6n^2 + 11n + 6)} \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\operatorname{int}(x*(cx^2)^{(1/2)}*(a + bx)^n, x)$

[Out] $((a + bx)^n*((2a^3*(cx^2)^{(1/2)})/(b^3*(11n + 6n^2 + n^3 + 6)) + (x^3*(cx^2)^{(1/2)}*(3n + n^2 + 2))/(11n + 6n^2 + n^3 + 6) - (2a^2*n*x*(cx^2)^{(1/2)})/(b^2*(11n + 6n^2 + n^3 + 6)) + (a*n*x^2*(cx^2)^{(1/2)}*(n + 1))/(b*(11n + 6n^2 + n^3 + 6)))/x$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{a^n \sqrt{c} x^2 \sqrt{x^2}}{3} \\ \int \frac{x \sqrt{c x^2}}{(a+b x)^3} dx \\ \int \frac{x \sqrt{c x^2}}{(a+b x)^2} dx \\ \int \frac{x \sqrt{c x^2}}{a+b x} dx \\ \frac{2 a^3 \sqrt{c} (a+b x)^n \sqrt{x^2}}{b^3 n^3 x+6 b^3 n^2 x+11 b^3 n x+6 b^3 x} - \frac{2 a^2 b \sqrt{c} n x (a+b x)^n \sqrt{x^2}}{b^3 n^3 x+6 b^3 n^2 x+11 b^3 n x+6 b^3 x} + \frac{a b^2 \sqrt{c} n^2 x^2 (a+b x)^n \sqrt{x^2}}{b^3 n^3 x+6 b^3 n^2 x+11 b^3 n x+6 b^3 x} + \frac{a b^2 \sqrt{c} n x^2 (a+b x)^n \sqrt{x^2}}{b^3 n^3 x+6 b^3 n^2 x+11 b^3 n x+6 b^3 x} + \frac{b^3 \sqrt{c} n^2 x^2}{b^3 n^3 x+6 b^3 n^2 x+11 b^3 n x+6 b^3 x} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)**n*(c*x**2)**(1/2),x)

[Out] Piecewise((a**n*sqrt(c)*x**2*sqrt(x**2)/3, Eq(b, 0)), (Integral(x*sqrt(c*x**2)/(a + b*x)**3, x), Eq(n, -3)), (Integral(x*sqrt(c*x**2)/(a + b*x)**2, x), Eq(n, -2)), (Integral(x*sqrt(c*x**2)/(a + b*x), x), Eq(n, -1)), (2*a**3*sqrt(c)*(a + b*x)**n*sqrt(x**2)/(b**3*n**3*x + 6*b**3*n**2*x + 11*b**3*n*x + 6*b**3*x) - 2*a**2*b*sqrt(c)*n*x*(a + b*x)**n*sqrt(x**2)/(b**3*n**3*x + 6*b**3*n**2*x + 11*b**3*n*x + 6*b**3*x) + a*b**2*sqrt(c)*n**2*x**2*(a + b*x)*n*sqrt(x**2)/(b**3*n**3*x + 6*b**3*n**2*x + 11*b**3*n*x + 6*b**3*x) + a*b**2*sqrt(c)*n*x**2*(a + b*x)**n*sqrt(x**2)/(b**3*n**3*x + 6*b**3*n**2*x + 11*b**3*n*x + 6*b**3*x) + b**3*sqrt(c)*n**2*x**3*(a + b*x)**n*sqrt(x**2)/(b**3*n**3*x + 6*b**3*n**2*x + 11*b**3*n*x + 6*b**3*x) + 3*b**3*sqrt(c)*n*x**3*(a + b*x)**n*sqrt(x**2)/(b**3*n**3*x + 6*b**3*n**2*x + 11*b**3*n*x + 6*b**3*x) + 2*b**3*sqrt(c)*x**3*(a + b*x)**n*sqrt(x**2)/(b**3*n**3*x + 6*b**3*n**2*x + 11*b**3*n*x + 6*b**3*x), True))

3.925 $\int \sqrt{cx^2} (a + bx)^n dx$

Optimal. Leaf size=63

$$\frac{\sqrt{cx^2} (a + bx)^{n+2}}{b^2(n+2)x} - \frac{a\sqrt{cx^2} (a + bx)^{n+1}}{b^2(n+1)x}$$

[Out] $-a*(b*x+a)^{(1+n)}*(c*x^2)^{(1/2)}/b^2/(1+n)/x+(b*x+a)^{(2+n)}*(c*x^2)^{(1/2)}/b^2/(2+n)/x$

Rubi [A] time = 0.02, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$\frac{\sqrt{cx^2} (a + bx)^{n+2}}{b^2(n+2)x} - \frac{a\sqrt{cx^2} (a + bx)^{n+1}}{b^2(n+1)x}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c*x^2]*(a + b*x)^n, x]

[Out] $-((a*\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)})/(b^2*(1 + n)*x)) + (\text{Sqrt}[c*x^2]*(a + b*x)^{(2 + n)})/(b^2*(2 + n)*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \sqrt{cx^2} (a + bx)^n dx &= \frac{\sqrt{cx^2} \int x(a + bx)^n dx}{x} \\ &= \frac{\sqrt{cx^2} \int \left(-\frac{a(a+bx)^n}{b} + \frac{(a+bx)^{1+n}}{b} \right) dx}{x} \\ &= -\frac{a\sqrt{cx^2} (a + bx)^{1+n}}{b^2(1+n)x} + \frac{\sqrt{cx^2} (a + bx)^{2+n}}{b^2(2+n)x} \end{aligned}$$

Mathematica [A] time = 0.03, size = 44, normalized size = 0.70

$$\frac{cx(a + bx)^{n+1}(b(n + 1)x - a)}{b^2(n + 1)(n + 2)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c*x^2]*(a + b*x)^n,x]

[Out] (c*x*(a + b*x)^(1 + n)*(-a + b*(1 + n)*x))/(b^2*(1 + n)*(2 + n)*Sqrt[c*x^2])

fricas [A] time = 0.45, size = 63, normalized size = 1.00

$$\frac{(abnx + (b^2n + b^2)x^2 - a^2)\sqrt{cx^2} (bx + a)^n}{(b^2n^2 + 3b^2n + 2b^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2),x, algorithm="fricas")

[Out] (a*b*n*x + (b^2*n + b^2)*x^2 - a^2)*sqrt(c*x^2)*(b*x + a)^n/((b^2*n^2 + 3*b^2*n + 2*b^2)*x)

giac [B] time = 1.14, size = 119, normalized size = 1.89

$$\left(\frac{a^2 a^n \operatorname{sgn}(x)}{b^2 n^2 + 3 b^2 n + 2 b^2} + \frac{(bx + a)^n b^2 n x^2 \operatorname{sgn}(x) + (bx + a)^n abnx \operatorname{sgn}(x) + (bx + a)^n b^2 x^2 \operatorname{sgn}(x) - (bx + a)^n a^2 \operatorname{sgn}(x)}{b^2 n^2 + 3 b^2 n + 2 b^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2),x, algorithm="giac")

[Out] $(a^2 a^n \operatorname{sgn}(x) / (b^2 n^2 + 3b^2 n + 2b^2) + ((b x + a)^n b^2 n x^2 \operatorname{sgn}(x) + (b x + a)^n a b n x \operatorname{sgn}(x) + (b x + a)^n b^2 x^2 \operatorname{sgn}(x) - (b x + a)^n a^2 \operatorname{sgn}(x)) / (b^2 n^2 + 3b^2 n + 2b^2)) \operatorname{sqrt}(c)$

maple [A] time = 0.00, size = 46, normalized size = 0.73

$$\frac{\sqrt{c x^2} (-x n b - b x + a) (b x + a)^{n+1}}{(n^2 + 3 n + 2) b^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^n*(c*x^2)^(1/2),x)`

[Out] $-(c x^2)^{1/2} (b x + a)^{n+1} (-b n x - b x + a) / x / b^2 / (n^2 + 3 n + 2)$

maxima [A] time = 1.45, size = 51, normalized size = 0.81

$$\frac{(b^2 \sqrt{c} (n+1) x^2 + a b \sqrt{c} n x - a^2 \sqrt{c}) (b x + a)^n}{(n^2 + 3 n + 2) b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^n*(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] $(b^2 \operatorname{sqrt}(c) (n+1) x^2 + a b \operatorname{sqrt}(c) n x - a^2 \operatorname{sqrt}(c)) (b x + a)^n / ((n^2 + 3 n + 2) b^2)$

mupad [B] time = 0.22, size = 85, normalized size = 1.35

$$\frac{(a + b x)^n \left(\frac{x^2 \sqrt{c x^2} (n+1)}{n^2 + 3 n + 2} - \frac{a^2 \sqrt{c x^2}}{b^2 (n^2 + 3 n + 2)} + \frac{a n x \sqrt{c x^2}}{b (n^2 + 3 n + 2)} \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(1/2)*(a+b*x)^n,x)`

[Out] $((a + b x)^n ((x^2 (c x^2)^{1/2} (n+1)) / (3 n + n^2 + 2) - (a^2 (c x^2)^{1/2}) / (b^2 (3 n + n^2 + 2))) + (a n x (c x^2)^{1/2}) / (b (3 n + n^2 + 2))) / x$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{a^n \sqrt{c} x \sqrt{x^2}}{2} & \text{for } b = 0 \\ \int \frac{\sqrt{cx^2}}{(a+bx)^2} dx & \text{for } n = -2 \\ \int \frac{\sqrt{cx^2}}{a+bx} dx & \text{for } n = -1 \\ -\frac{a^2 \sqrt{c} (a+bx)^n \sqrt{x^2}}{b^2 n^2 x + 3b^2 n x + 2b^2 x} + \frac{ab \sqrt{c} n x (a+bx)^n \sqrt{x^2}}{b^2 n^2 x + 3b^2 n x + 2b^2 x} + \frac{b^2 \sqrt{c} n x^2 (a+bx)^n \sqrt{x^2}}{b^2 n^2 x + 3b^2 n x + 2b^2 x} + \frac{b^2 \sqrt{c} x^2 (a+bx)^n \sqrt{x^2}}{b^2 n^2 x + 3b^2 n x + 2b^2 x} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n*(c*x**2)**(1/2),x)

[Out] Piecewise((a**n*sqrt(c)*x*sqrt(x**2)/2, Eq(b, 0)), (Integral(sqrt(c*x**2)/(a + b*x)**2, x), Eq(n, -2)), (Integral(sqrt(c*x**2)/(a + b*x), x), Eq(n, -1)), (-a**2*sqrt(c)*(a + b*x)**n*sqrt(x**2)/(b**2*n**2*x + 3*b**2*n*x + 2*b**2*x) + a*b*sqrt(c)*n*x*(a + b*x)**n*sqrt(x**2)/(b**2*n**2*x + 3*b**2*n*x + 2*b**2*x) + b**2*sqrt(c)*n*x**2*(a + b*x)**n*sqrt(x**2)/(b**2*n**2*x + 3*b**2*n*x + 2*b**2*x) + b**2*sqrt(c)*x**2*(a + b*x)**n*sqrt(x**2)/(b**2*n**2*x + 3*b**2*n*x + 2*b**2*x), True))

$$3.926 \quad \int \frac{\sqrt{cx^2} (a+bx)^n}{x} dx$$

Optimal. Leaf size=30

$$\frac{\sqrt{cx^2} (a+bx)^{n+1}}{b(n+1)x}$$

[Out] (b*x+a)^(1+n)*(c*x^2)^(1/2)/b/(1+n)/x

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$\frac{\sqrt{cx^2} (a+bx)^{n+1}}{b(n+1)x}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x)^n)/x, x]

[Out] (Sqrt[c*x^2]*(a + b*x)^(1 + n))/(b*(1 + n)*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{cx^2} (a+bx)^n}{x} dx &= \frac{\sqrt{cx^2} \int (a+bx)^n dx}{x} \\ &= \frac{\sqrt{cx^2} (a+bx)^{1+n}}{b(1+n)x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 0.97

$$\frac{cx(a+bx)^{n+1}}{b(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x)^n)/x,x]

[Out] (c*x*(a + b*x)^(1 + n))/(b*(1 + n)*Sqrt[c*x^2])

fricas [A] time = 0.45, size = 30, normalized size = 1.00

$$\frac{\sqrt{cx^2} (bx + a)(bx + a)^n}{(bn + b)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2)/x,x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x + a)*(b*x + a)^n/((b*n + b)*x)

giac [A] time = 1.01, size = 42, normalized size = 1.40

$$-\sqrt{c} \left(\frac{a^{n+1} \operatorname{sgn}(x)}{bn + b} - \frac{(bx + a)^{n+1} \operatorname{sgn}(x)}{b(n + 1)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2)/x,x, algorithm="giac")

[Out] -sqrt(c)*(a^(n + 1)*sgn(x)/(b*n + b) - (b*x + a)^(n + 1)*sgn(x)/(b*(n + 1)))

maple [A] time = 0.00, size = 29, normalized size = 0.97

$$\frac{\sqrt{cx^2} (bx + a)^{n+1}}{(n + 1)bx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n*(c*x^2)^(1/2)/x,x)

[Out] (b*x+a)^(n+1)*(c*x^2)^(1/2)/b/(n+1)/x

maxima [A] time = 1.40, size = 28, normalized size = 0.93

$$\frac{(b\sqrt{c}x + a\sqrt{c})(bx + a)^n}{b(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2)/x,x, algorithm="maxima")

[Out] (b*sqrt(c)*x + a*sqrt(c))*(b*x + a)^n/(b*(n + 1))

mupad [B] time = 0.23, size = 31, normalized size = 1.03

$$\frac{\sqrt{cx^2} (a + bx)^n (a + bx)}{bx (n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(1/2)*(a + b*x)^n)/x,x)

[Out] ((c*x^2)^(1/2)*(a + b*x)^n*(a + b*x))/(b*x*(n + 1))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\begin{cases} \frac{\sqrt{c} \sqrt{x^2}}{a} & \text{for } b = 0 \wedge n = -1 \\ a^n \sqrt{c} \sqrt{x^2} & \text{for } b = 0 \\ \int \frac{\sqrt{cx^2}}{x(a+bx)} dx & \text{for } n = -1 \\ \frac{a\sqrt{c}(a+bx)^n \sqrt{x^2}}{bnx+bx} + \frac{b\sqrt{c}x(a+bx)^n \sqrt{x^2}}{bnx+bx} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n*(c*x**2)**(1/2)/x,x)

[Out] Piecewise((sqrt(c)*sqrt(x**2)/a, Eq(b, 0) & Eq(n, -1)), (a**n*sqrt(c)*sqrt(x**2), Eq(b, 0)), (Integral(sqrt(c*x**2)/(x*(a + b*x)), x), Eq(n, -1)), (a*sqrt(c)*(a + b*x)**n*sqrt(x**2)/(b*n*x + b*x) + b*sqrt(c)*x*(a + b*x)**n*sqrt(x**2)/(b*n*x + b*x), True))

$$3.927 \quad \int \frac{\sqrt{cx^2} (a+bx)^n}{x^2} dx$$

Optimal. Leaf size=47

$$\frac{\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)x}$$

[Out] $-(b*x+a)^{(1+n)}*\text{hypergeom}([1, 1+n], [2+n], 1+b*x/a)*(c*x^2)^{(1/2)}/a/(1+n)/x$

Rubi [A] time = 0.01, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$\frac{\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)x}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x)^n)/x^2,x]

[Out] $-\left(\left(\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)}*\text{Hypergeometric2F1}[1, 1 + n, 2 + n, 1 + (b*x)/a]\right)/(a*(1 + n)*x)\right)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{\sqrt{cx^2} (a + bx)^n}{x^2} dx = \frac{\sqrt{cx^2} \int \frac{(a+bx)^n}{x} dx}{x}$$

$$= -\frac{\sqrt{cx^2} (a + bx)^{1+n} {}_2F_1\left(1, 1 + n; 2 + n; 1 + \frac{bx}{a}\right)}{a(1 + n)x}$$

Mathematica [A] time = 0.01, size = 46, normalized size = 0.98

$$-\frac{cx(a + bx)^{n+1} {}_2F_1\left(1, n + 1; n + 2; \frac{bx}{a} + 1\right)}{a(n + 1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x)^n)/x^2,x]

[Out] -((c*x*(a + b*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, 1 + (b*x)/a])/(a*(1 + n)*Sqrt[c*x^2]))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx + a)^n}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2)/x^2,x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/x^2, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (bx + a)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2)/x^2,x, algorithm="giac")

[Out] integrate(sqrt(c*x^2)*(b*x + a)^n/x^2, x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{c x^2} (bx + a)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^n*(c*x^2)^(1/2)/x^2,x)`

[Out] `int((b*x+a)^n*(c*x^2)^(1/2)/x^2,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (bx + a)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^n*(c*x^2)^(1/2)/x^2,x, algorithm="maxima")`

[Out] `integrate(sqrt(c*x^2)*(b*x + a)^n/x^2, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{cx^2} (a + bx)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(1/2)*(a + b*x)^n)/x^2,x)`

[Out] `int(((c*x^2)^(1/2)*(a + b*x)^n)/x^2, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (a + bx)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**n*(c*x**2)**(1/2)/x**2,x)`

[Out] `Integral(sqrt(c*x**2)*(a + b*x)**n/x**2, x)`

$$3.928 \quad \int \frac{\sqrt{cx^2} (a+bx)^n}{x^3} dx$$

Optimal. Leaf size=47

$$\frac{b\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)x}$$

[Out] b*(b*x+a)^(1+n)*hypergeom([2, 1+n], [2+n], 1+b*x/a)*(c*x^2)^(1/2)/a^2/(1+n)/x

Rubi [A] time = 0.01, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$\frac{b\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)x}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x)^n)/x^3, x]

[Out] (b*Sqrt[c*x^2]*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n)*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_)^(m_))*((c_) + (d_.)*(x_)^(n_)), x_Symbol] := Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{\sqrt{cx^2} (a + bx)^n}{x^3} dx = \frac{\sqrt{cx^2} \int \frac{(a+bx)^n}{x^2} dx}{x}$$

$$= \frac{b\sqrt{cx^2} (a + bx)^{1+n} {}_2F_1\left(2, 1 + n; 2 + n; 1 + \frac{bx}{a}\right)}{a^2(1 + n)x}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 1.00

$$\frac{b\sqrt{cx^2} (a + bx)^{n+1} {}_2F_1\left(2, n + 1; n + 2; \frac{bx}{a} + 1\right)}{a^2(n + 1)x}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x)^n)/x^3,x]

[Out] (b*Sqrt[c*x^2]*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n)*x)

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx + a)^n}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2)/x^3,x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/x^3, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (bx + a)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2)/x^3,x, algorithm="giac")

[Out] integrate(sqrt(c*x^2)*(b*x + a)^n/x^3, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (bx + a)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^n*(c*x^2)^(1/2)/x^3,x)`

[Out] `int((b*x+a)^n*(c*x^2)^(1/2)/x^3,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (bx + a)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^n*(c*x^2)^(1/2)/x^3,x, algorithm="maxima")`

[Out] `integrate(sqrt(c*x^2)*(b*x + a)^n/x^3, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{cx^2} (a + bx)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(1/2)*(a + b*x)^n)/x^3,x)`

[Out] `int(((c*x^2)^(1/2)*(a + b*x)^n)/x^3, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (a + bx)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**n*(c*x**2)**(1/2)/x**3,x)`

[Out] `Integral(sqrt(c*x**2)*(a + b*x)**n/x**3, x)`

$$3.929 \quad \int \frac{\sqrt{cx^2} (a+bx)^n}{x^4} dx$$

Optimal. Leaf size=50

$$-\frac{b^2\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3(n+1)x}$$

[Out] $-b^2*(b*x+a)^{(1+n)}*\text{hypergeom}([3, 1+n], [2+n], 1+b*x/a)*(c*x^2)^{(1/2)}/a^3/(1+n)/x$

Rubi [A] time = 0.01, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$-\frac{b^2\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3(n+1)x}$$

Antiderivative was successfully verified.

[In] Int[(Sqrt[c*x^2]*(a + b*x)^n)/x^4,x]

[Out] $-((b^2*\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)}*\text{Hypergeometric2F1}[3, 1 + n, 2 + n, 1 + (b*x)/a])/(a^3*(1 + n)*x))$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_)^(m_))*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{\sqrt{cx^2} (a + bx)^n}{x^4} dx = \frac{\sqrt{cx^2} \int \frac{(a+bx)^n}{x^3} dx}{x}$$

$$= -\frac{b^2 \sqrt{cx^2} (a + bx)^{1+n} {}_2F_1\left(3, 1 + n; 2 + n; 1 + \frac{bx}{a}\right)}{a^3(1 + n)x}$$

Mathematica [A] time = 0.02, size = 50, normalized size = 1.00

$$-\frac{b^2 \sqrt{cx^2} (a + bx)^{n+1} {}_2F_1\left(3, n + 1; n + 2; \frac{bx}{a} + 1\right)}{a^3(n + 1)x}$$

Antiderivative was successfully verified.

[In] Integrate[(Sqrt[c*x^2]*(a + b*x)^n)/x^4,x]

[Out] -((b^2*Sqrt[c*x^2]*(a + b*x)^(1 + n)*Hypergeometric2F1[3, 1 + n, 2 + n, 1 + (b*x)/a])/(a^3*(1 + n)*x))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx + a)^n}{x^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2)/x^4,x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/x^4, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (bx + a)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(c*x^2)^(1/2)/x^4,x, algorithm="giac")

[Out] integrate(sqrt(c*x^2)*(b*x + a)^n/x^4, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{c x^2} (bx + a)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^n*(c*x^2)^(1/2)/x^4,x)`

[Out] `int((b*x+a)^n*(c*x^2)^(1/2)/x^4,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (bx + a)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^n*(c*x^2)^(1/2)/x^4,x, algorithm="maxima")`

[Out] `integrate(sqrt(c*x^2)*(b*x + a)^n/x^4, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{cx^2} (a + bx)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(1/2)*(a + b*x)^n)/x^4,x)`

[Out] `int(((c*x^2)^(1/2)*(a + b*x)^n)/x^4, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{cx^2} (a + bx)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**n*(c*x**2)**(1/2)/x**4,x)`

[Out] `Integral(sqrt(c*x**2)*(a + b*x)**n/x**4, x)`

3.930 $\int x (cx^2)^{3/2} (a + bx)^n dx$

Optimal. Leaf size=169

$$\frac{a^4 c \sqrt{cx^2} (a + bx)^{n+1}}{b^5 (n+1)x} - \frac{4a^3 c \sqrt{cx^2} (a + bx)^{n+2}}{b^5 (n+2)x} + \frac{6a^2 c \sqrt{cx^2} (a + bx)^{n+3}}{b^5 (n+3)x} - \frac{4ac \sqrt{cx^2} (a + bx)^{n+4}}{b^5 (n+4)x} + \frac{c \sqrt{cx^2} (a + bx)^{n+5}}{b^5 (n+5)x}$$

[Out] $a^4 c (b^5 x^5 + 5 a b^4 x^4 + 10 a^2 b^3 x^3 + 10 a^3 b^2 x^2 + 5 a^4 b x + a^5) (c x^2)^{3/2} (a + b x)^n / (b^5 (n+1) x^5 + 5 a b^4 (n+2) x^4 + 10 a^2 b^3 (n+3) x^3 + 10 a^3 b^2 (n+4) x^2 + 5 a^4 b (n+5) x + a^5 (n+6))$

Rubi [A] time = 0.06, antiderivative size = 169, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 43}

$$\frac{a^4 c \sqrt{cx^2} (a + bx)^{n+1}}{b^5 (n+1)x} - \frac{4a^3 c \sqrt{cx^2} (a + bx)^{n+2}}{b^5 (n+2)x} + \frac{6a^2 c \sqrt{cx^2} (a + bx)^{n+3}}{b^5 (n+3)x} - \frac{4ac \sqrt{cx^2} (a + bx)^{n+4}}{b^5 (n+4)x} + \frac{c \sqrt{cx^2} (a + bx)^{n+5}}{b^5 (n+5)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x (c x^2)^{3/2} (a + b x)^n, x]$

[Out] $(a^4 c \sqrt{c x^2} (a + b x)^{n+1}) / (b^5 (n+1) x) - (4 a^3 c \sqrt{c x^2} (a + b x)^{n+2}) / (b^5 (n+2) x) + (6 a^2 c \sqrt{c x^2} (a + b x)^{n+3}) / (b^5 (n+3) x) - (4 a c \sqrt{c x^2} (a + b x)^{n+4}) / (b^5 (n+4) x) + (c \sqrt{c x^2} (a + b x)^{n+5}) / (b^5 (n+5) x)$

Rule 15

$\text{Int}[(u_.) * ((a_.) * (x_.)^{(n_.)})^{(m_.)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]} * (a x^n)^{\text{FracPart}[m]}) / x^{(n * \text{FracPart}[m])}, \text{Int}[u x^{(m n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_.) + (b_.) * (x_.)^{(m_.)}] * ((c_.) + (d_.) * (x_.)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b x)^m (c + d x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x (cx^2)^{3/2} (a+bx)^n dx &= \frac{(c\sqrt{cx^2}) \int x^4 (a+bx)^n dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int \left(\frac{a^4(a+bx)^n}{b^4} - \frac{4a^3(a+bx)^{1+n}}{b^4} + \frac{6a^2(a+bx)^{2+n}}{b^4} - \frac{4a(a+bx)^{3+n}}{b^4} + \frac{(a+bx)^{4+n}}{b^4} \right) dx}{x} \\ &= \frac{a^4 c \sqrt{cx^2} (a+bx)^{1+n}}{b^5(1+n)x} - \frac{4a^3 c \sqrt{cx^2} (a+bx)^{2+n}}{b^5(2+n)x} + \frac{6a^2 c \sqrt{cx^2} (a+bx)^{3+n}}{b^5(3+n)x} - \frac{4ac \sqrt{cx^2} (a+bx)^{4+n}}{b^5(4+n)x} + \frac{c \sqrt{cx^2} (a+bx)^{5+n}}{b^5(5+n)x} \end{aligned}$$

Mathematica [A] time = 0.08, size = 132, normalized size = 0.78

$$\frac{(cx^2)^{3/2} (a+bx)^{n+1} (24a^4 - 24a^3b(n+1)x + 12a^2b^2(n^2 + 3n + 2)x^2 - 4ab^3(n^3 + 6n^2 + 11n + 6)x^3 + b^4(n^4 + 10n^3 + 35n^2 + 10n^3 + n^4)x^4)}{b^5(n+1)(n+2)(n+3)(n+4)(n+5)x^3}$$

Antiderivative was successfully verified.

[In] Integrate[x*(c*x^2)^(3/2)*(a + b*x)^n,x]

[Out] ((c*x^2)^(3/2)*(a + b*x)^(1 + n)*(24*a^4 - 24*a^3*b*(1 + n)*x + 12*a^2*b^2*(2 + 3*n + n^2)*x^2 - 4*a*b^3*(6 + 11*n + 6*n^2 + n^3)*x^3 + b^4*(24 + 50*n + 35*n^2 + 10*n^3 + n^4)*x^4))/(b^5*(1 + n)*(2 + n)*(3 + n)*(4 + n)*(5 + n)*x^3)

fricas [A] time = 0.55, size = 233, normalized size = 1.38

$$\frac{(24 a^4 b c n x - 24 a^5 c - (b^5 c n^4 + 10 b^5 c n^3 + 35 b^5 c n^2 + 50 b^5 c n + 24 b^5 c) x^5 - (a b^4 c n^4 + 6 a b^4 c n^3 + 11 a b^4 c n^2 + 6 a b^4 c n) x^4 + 4 (a^2 b^3 c n^3 + 3 a^2 b^3 c n^2 + 2 a^2 b^3 c n) x^3 - 12 (a^3 b^2 c n^2 + a^3 b^2 c n) x^2) \sqrt{c x^2} (b x + a)^n}{(b^5 n^5 + 15 b^5 n^4 + 85 b^5 n^3 + 225 b^5 n^2 + 274 b^5 n + 120 b^5) x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)*(b*x+a)^n,x, algorithm="fricas")

[Out] -(24*a^4*b*c*n*x - 24*a^5*c - (b^5*c*n^4 + 10*b^5*c*n^3 + 35*b^5*c*n^2 + 50*b^5*c*n + 24*b^5*c)*x^5 - (a*b^4*c*n^4 + 6*a*b^4*c*n^3 + 11*a*b^4*c*n^2 + 6*a*b^4*c*n)*x^4 + 4*(a^2*b^3*c*n^3 + 3*a^2*b^3*c*n^2 + 2*a^2*b^3*c*n)*x^3 - 12*(a^3*b^2*c*n^2 + a^3*b^2*c*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^5*n^5 + 15*b^5*n^4 + 85*b^5*n^3 + 225*b^5*n^2 + 274*b^5*n + 120*b^5)*x)

giac [B] time = 1.20, size = 426, normalized size = 2.52

$$-\left(\frac{24 a^5 a^n \operatorname{sgn}(x)}{b^5 n^5 + 15 b^5 n^4 + 85 b^5 n^3 + 225 b^5 n^2 + 274 b^5 n + 120 b^5} - \frac{(b x + a)^n b^5 n^4 x^5 \operatorname{sgn}(x) + (b x + a)^n a b^4 n^4 x^4 \operatorname{sgn}(x) + \dots}{b^5 n^5 + 15 b^5 n^4 + 85 b^5 n^3 + 225 b^5 n^2 + 274 b^5 n + 120 b^5} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)*(b*x+a)^n,x, algorithm="giac")

[Out]
$$-(24*a^5*a^n*\text{sgn}(x)/(b^5*n^5 + 15*b^5*n^4 + 85*b^5*n^3 + 225*b^5*n^2 + 274*b^5*n + 120*b^5) - ((b*x + a)^n*b^5*n^4*x^5*\text{sgn}(x) + (b*x + a)^n*a*b^4*n^4*x^4*\text{sgn}(x) + 10*(b*x + a)^n*b^5*n^3*x^5*\text{sgn}(x) + 6*(b*x + a)^n*a*b^4*n^3*x^4*\text{sgn}(x) + 35*(b*x + a)^n*b^5*n^2*x^5*\text{sgn}(x) - 4*(b*x + a)^n*a^2*b^3*n^3*x^3*\text{sgn}(x) + 11*(b*x + a)^n*a*b^4*n^2*x^4*\text{sgn}(x) + 50*(b*x + a)^n*b^5*n*x^5*\text{sgn}(x) - 12*(b*x + a)^n*a^2*b^3*n^2*x^3*\text{sgn}(x) + 6*(b*x + a)^n*a*b^4*n*x^4*\text{sgn}(x) + 24*(b*x + a)^n*b^5*x^5*\text{sgn}(x) + 12*(b*x + a)^n*a^3*b^2*n^2*x^2*\text{sgn}(x) - 8*(b*x + a)^n*a^2*b^3*n*x^3*\text{sgn}(x) + 12*(b*x + a)^n*a^3*b^2*n*x^2*\text{sgn}(x) - 24*(b*x + a)^n*a^4*b*n*x*\text{sgn}(x) + 24*(b*x + a)^n*a^5*\text{sgn}(x))/(b^5*n^5 + 15*b^5*n^4 + 85*b^5*n^3 + 225*b^5*n^2 + 274*b^5*n + 120*b^5))*c^(3/2)$$

maple [A] time = 0.01, size = 199, normalized size = 1.18

$$\frac{(b^4 n^4 x^4 + 10 b^4 n^3 x^4 - 4 a b^3 n^3 x^3 + 35 b^4 n^2 x^4 - 24 a b^3 n^2 x^3 + 50 b^4 n x^4 + 12 a^2 b^2 n^2 x^2 - 44 a b^3 n x^3 + 24 b^4 x^4 + 36 a^2 b^2 n^2 x^2 - 24 a^3 b n^2 x^2 + 24 a^4 b n x + 24 a^5) c^{3/2}}{(n^5 + 15 n^4 + 85 n^3 + 225 n^2 + 274 n + 120) b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(c*x^2)^(3/2)*(b*x+a)^n,x)

[Out]
$$(b*x+a)^{(n+1)}*(b^4*n^4*x^4+10*b^4*n^3*x^4-4*a*b^3*n^3*x^3+35*b^4*n^2*x^4-24*a*b^3*n^2*x^3+50*b^4*n*x^4+12*a^2*b^2*n^2*x^2-44*a*b^3*n*x^3+24*b^4*x^4+36*a^2*b^2*n*x^2-24*a*b^3*x^3-24*a^3*b*n*x+24*a^2*b^2*x^2-24*a^3*b*x+24*a^4)*(c*x^2)^(3/2)/x^3/b^5/(n^5+15*n^4+85*n^3+225*n^2+274*n+120)$$

maxima [A] time = 1.44, size = 157, normalized size = 0.93

$$\frac{\left(\left(n^4 + 10 n^3 + 35 n^2 + 50 n + 24\right) b^5 c^{\frac{3}{2}} x^5 + \left(n^4 + 6 n^3 + 11 n^2 + 6 n\right) a b^4 c^{\frac{3}{2}} x^4 - 4 \left(n^3 + 3 n^2 + 2 n\right) a^2 b^3 c^{\frac{3}{2}} x^3 + 12 \left(n^2 + n\right) a^3 b^2 c^{\frac{3}{2}} x^2 - 24 a^4 b c^{\frac{3}{2}} n x + 24 a^5 c^{\frac{3}{2}}\right) (b*x+a)^n}{\left(n^5 + 15 n^4 + 85 n^3 + 225 n^2 + 274 n + 120\right) b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^(3/2)*(b*x+a)^n,x, algorithm="maxima")

[Out]
$$\left(\left(n^4 + 10 n^3 + 35 n^2 + 50 n + 24\right) b^5 c^{\frac{3}{2}} x^5 + \left(n^4 + 6 n^3 + 11 n^2 + 6 n\right) a b^4 c^{\frac{3}{2}} x^4 - 4 \left(n^3 + 3 n^2 + 2 n\right) a^2 b^3 c^{\frac{3}{2}} x^3 + 12 \left(n^2 + n\right) a^3 b^2 c^{\frac{3}{2}} x^2 - 24 a^4 b c^{\frac{3}{2}} n x + 24 a^5 c^{\frac{3}{2}}\right) (b*x+a)^n / \left(\left(n^5 + 15 n^4 + 85 n^3 + 225 n^2 + 274 n + 120\right) b^5\right)$$

mupad [B] time = 0.41, size = 307, normalized size = 1.82

$$(a + bx)^n \left(\frac{24a^5c\sqrt{cx^2}}{b^5(n^5+15n^4+85n^3+225n^2+274n+120)} + \frac{cx^5\sqrt{cx^2}(n^4+10n^3+35n^2+50n+24)}{n^5+15n^4+85n^3+225n^2+274n+120} - \frac{24a^4cnx\sqrt{cx^2}}{b^4(n^5+15n^4+85n^3+225n^2+274n+120)} + \dots \right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*(c*x^2)^(3/2)*(a + b*x)^n,x)`

[Out] $((a + bx)^n * ((24*a^5*c*(c*x^2)^(1/2))/(b^5*(274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120)) + (c*x^5*(c*x^2)^(1/2)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24))/(274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120) - (24*a^4*c*n*x*(c*x^2)^(1/2))/(b^4*(274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120)) + (a*c*n*x^4*(c*x^2)^(1/2)*(11*n + 6*n^2 + n^3 + 6))/(b*(274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120)) + (12*a^3*c*n*x^2*(c*x^2)^(1/2)*(n + 1))/(b^3*(274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120)) - (4*a^2*c*n*x^3*(c*x^2)^(1/2)*(3*n + n^2 + 2))/(b^2*(274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120))))/x$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x (cx^2)^{\frac{3}{2}} (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(c*x**2)**(3/2)*(b*x+a)**n,x)`

[Out] `Integral(x*(c*x**2)**(3/2)*(a + b*x)**n, x)`

3.931 $\int (cx^2)^{3/2} (a + bx)^n dx$

Optimal. Leaf size=135

$$-\frac{a^3 c \sqrt{cx^2} (a + bx)^{n+1}}{b^4 (n+1)x} + \frac{3a^2 c \sqrt{cx^2} (a + bx)^{n+2}}{b^4 (n+2)x} - \frac{3ac \sqrt{cx^2} (a + bx)^{n+3}}{b^4 (n+3)x} + \frac{c \sqrt{cx^2} (a + bx)^{n+4}}{b^4 (n+4)x}$$

[Out] $-a^3 c (b^4 x^4)^{1/2} (a + bx)^{n+1} / (b^4 (n+1)x) + 3a^2 c (b^4 x^4)^{1/2} (a + bx)^{n+2} / (b^4 (n+2)x) - 3ac (b^4 x^4)^{1/2} (a + bx)^{n+3} / (b^4 (n+3)x) + c (b^4 x^4)^{1/2} (a + bx)^{n+4} / (b^4 (n+4)x)$

Rubi [A] time = 0.04, antiderivative size = 135, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$-\frac{a^3 c \sqrt{cx^2} (a + bx)^{n+1}}{b^4 (n+1)x} + \frac{3a^2 c \sqrt{cx^2} (a + bx)^{n+2}}{b^4 (n+2)x} - \frac{3ac \sqrt{cx^2} (a + bx)^{n+3}}{b^4 (n+3)x} + \frac{c \sqrt{cx^2} (a + bx)^{n+4}}{b^4 (n+4)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}*(a + b*x)^n, x]$

[Out] $-(a^3 c \sqrt{cx^2} (a + bx)^{n+1} / (b^4 (n+1)x) + 3a^2 c \sqrt{cx^2} (a + bx)^{n+2} / (b^4 (n+2)x) - 3ac \sqrt{cx^2} (a + bx)^{n+3} / (b^4 (n+3)x) + c \sqrt{cx^2} (a + bx)^{n+4} / (b^4 (n+4)x))$

Rule 15

$\text{Int}[(u_.) * ((a_.) * (x_.)^n)^m, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]} * (a*x^n)^{\text{FracPart}[m]}) / x^{n*\text{FracPart}[m]}, \text{Int}[u*x^{m*n}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_.) + (b_.) * (x_.)^n]^m * ((c_.) + (d_.) * (x_.)^n)^n, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m * (c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (cx^2)^{3/2} (a+bx)^n dx &= \frac{(c\sqrt{cx^2}) \int x^3 (a+bx)^n dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int \left(-\frac{a^3(a+bx)^n}{b^3} + \frac{3a^2(a+bx)^{1+n}}{b^3} - \frac{3a(a+bx)^{2+n}}{b^3} + \frac{(a+bx)^{3+n}}{b^3} \right) dx}{x} \\ &= -\frac{a^3 c \sqrt{cx^2} (a+bx)^{1+n}}{b^4(1+n)x} + \frac{3a^2 c \sqrt{cx^2} (a+bx)^{2+n}}{b^4(2+n)x} - \frac{3ac \sqrt{cx^2} (a+bx)^{3+n}}{b^4(3+n)x} + \frac{c \sqrt{cx^2} (a+bx)^{4+n}}{b^4(4+n)x} \end{aligned}$$

Mathematica [A] time = 0.05, size = 98, normalized size = 0.73

$$\frac{(cx^2)^{3/2} (a+bx)^{n+1} (-6a^3 + 6a^2b(n+1)x - 3ab^2(n^2 + 3n + 2)x^2 + b^3(n^3 + 6n^2 + 11n + 6)x^3)}{b^4(n+1)(n+2)(n+3)(n+4)x^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(3/2)*(a + b*x)^n,x]

[Out] ((c*x^2)^(3/2)*(a + b*x)^(1 + n)*(-6*a^3 + 6*a^2*b*(1 + n)*x - 3*a*b^2*(2 + 3*n + n^2)*x^2 + b^3*(6 + 11*n + 6*n^2 + n^3)*x^3))/(b^4*(1 + n)*(2 + n)*(3 + n)*(4 + n)*x^3)

fricas [A] time = 0.44, size = 164, normalized size = 1.21

$$\frac{(6a^3bcnx - 6a^4c + (b^4cn^3 + 6b^4cn^2 + 11b^4cn + 6b^4c)x^4 + (ab^3cn^3 + 3ab^3cn^2 + 2ab^3cn)x^3 - 3(a^2b^2cn^2 + a^2b^2cn)x^2 + (b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4)x)x}{(b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n,x, algorithm="fricas")

[Out] (6*a^3*b*c*n*x - 6*a^4*c + (b^4*c*n^3 + 6*b^4*c*n^2 + 11*b^4*c*n + 6*b^4*c)*x^4 + (a*b^3*c*n^3 + 3*a*b^3*c*n^2 + 2*a*b^3*c*n)*x^3 - 3*(a^2*b^2*c*n^2 + a^2*b^2*c*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^4*n^4 + 10*b^4*n^3 + 35*b^4*n^2 + 50*b^4*n + 24*b^4)*x)

giac [B] time = 1.14, size = 300, normalized size = 2.22

$$\left(\frac{6a^4a^n \operatorname{sgn}(x)}{b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4} + \frac{(bx+a)^n b^4 n^3 x^4 \operatorname{sgn}(x) + (bx+a)^n ab^3 n^3 x^3 \operatorname{sgn}(x) + 6(bx+a)^n b^4 n^2 x^2 \operatorname{sgn}(x) - 3(a^2 b^2 c n^2 + a^2 b^2 c n) x^2 + (ab^3 c n^3 + 3ab^3 c n^2 + 2ab^3 c n) x^3 - 3(a^2 b^2 c n^2 + a^2 b^2 c n) x^2 + (b^4 c n^3 + 6b^4 c n^2 + 11b^4 c n + 6b^4 c) x^4 + (a^3 b c n x - 6a^4 c) x^4}{(b^4 n^4 + 10b^4 n^3 + 35b^4 n^2 + 50b^4 n + 24b^4) x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n,x, algorithm="giac")

[Out]
$$\frac{(6a^4a^n\operatorname{sgn}(x)/(b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4) + ((b*x + a)^n*b^4*n^3*x^4*\operatorname{sgn}(x) + (b*x + a)^n*a*b^3*n^3*x^3*\operatorname{sgn}(x) + 6*(b*x + a)^n*b^4*n^2*x^4*\operatorname{sgn}(x) + 3*(b*x + a)^n*a*b^3*n^2*x^3*\operatorname{sgn}(x) + 11*(b*x + a)^n*b^4*n*x^4*\operatorname{sgn}(x) - 3*(b*x + a)^n*a^2*b^2*n^2*x^2*\operatorname{sgn}(x) + 2*(b*x + a)^n*a*b^3*n*x^3*\operatorname{sgn}(x) + 6*(b*x + a)^n*b^4*x^4*\operatorname{sgn}(x) - 3*(b*x + a)^n*a^2*b^2*n*x^2*\operatorname{sgn}(x) + 6*(b*x + a)^n*a^3*b*n*x*\operatorname{sgn}(x) - 6*(b*x + a)^n*a^4*\operatorname{sgn}(x))/(b^4*n^4 + 10*b^4*n^3 + 35*b^4*n^2 + 50*b^4*n + 24*b^4))*c^(3/2)}$$

maple [A] time = 0.01, size = 136, normalized size = 1.01

$$\frac{(cx^2)^{\frac{3}{2}}(-b^3n^3x^3 - 6b^3n^2x^3 + 3ab^2n^2x^2 - 11b^3nx^3 + 9ab^2nx^2 - 6b^3x^3 - 6a^2bnx + 6ab^2x^2 - 6a^2bx + 6a^3)(b)}{(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(b*x+a)^n,x)

[Out]
$$-(b*x+a)^{(n+1)}*(c*x^2)^{(3/2)}*(-b^3n^3*x^3-6*b^3n^2*x^3+3*a*b^2*n^2*x^2-11*b^3n*x^3+9*a*b^2*n*x^2-6*b^3*x^3-6*a^2*b*n*x+6*a*b^2*x^2-6*a^2*b*x+6*a^3)/x^3/b^4/(n^4+10*n^3+35*n^2+50*n+24)$$

maxima [A] time = 1.44, size = 116, normalized size = 0.86

$$\frac{\left(\left(n^3 + 6n^2 + 11n + 6\right)b^4c^{\frac{3}{2}}x^4 + \left(n^3 + 3n^2 + 2n\right)ab^3c^{\frac{3}{2}}x^3 - 3\left(n^2 + n\right)a^2b^2c^{\frac{3}{2}}x^2 + 6a^3bc^{\frac{3}{2}}nx - 6a^4c^{\frac{3}{2}}\right)(bx + a)^n}{\left(n^4 + 10n^3 + 35n^2 + 50n + 24\right)b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n,x, algorithm="maxima")

[Out]
$$\left(\left(n^3 + 6n^2 + 11n + 6\right)b^4c^{\frac{3}{2}}x^4 + \left(n^3 + 3n^2 + 2n\right)a*b^3*c^{\frac{3}{2}}x^3 - 3*(n^2 + n)*a^2*b^2*c^{\frac{3}{2}}x^2 + 6*a^3*b*c^{\frac{3}{2}}*n*x - 6*a^4*c^{\frac{3}{2}}/2\right)*(b*x + a)^n/\left(\left(n^4 + 10n^3 + 35n^2 + 50n + 24\right)*b^4\right)$$

mupad [B] time = 0.32, size = 219, normalized size = 1.62

$$\frac{(a + bx)^n \left(\frac{cx^4 \sqrt{cx^2} (n^3 + 6n^2 + 11n + 6)}{n^4 + 10n^3 + 35n^2 + 50n + 24} - \frac{6a^4c \sqrt{cx^2}}{b^4(n^4 + 10n^3 + 35n^2 + 50n + 24)} + \frac{6a^3cnx \sqrt{cx^2}}{b^3(n^4 + 10n^3 + 35n^2 + 50n + 24)} - \frac{3a^2cnx^2 \sqrt{cx^2} (n+1)}{b^2(n^4 + 10n^3 + 35n^2 + 50n + 24)} \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(a + b*x)^n,x)

```
[Out] ((a + b*x)^n*((c*x^4*(c*x^2)^(1/2)*(11*n + 6*n^2 + n^3 + 6))/(50*n + 35*n^2 + 10*n^3 + n^4 + 24) - (6*a^4*c*(c*x^2)^(1/2))/(b^4*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (6*a^3*c*n*x*(c*x^2)^(1/2))/(b^3*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) - (3*a^2*c*n*x^2*(c*x^2)^(1/2)*(n + 1))/(b^2*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (a*c*n*x^3*(c*x^2)^(1/2)*(3*n + n^2 + 2))/(b*(50*n + 35*n^2 + 10*n^3 + n^4 + 24))))/x
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^{\frac{3}{2}} (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((c*x**2)**(3/2)*(b*x+a)**n,x)
```

```
[Out] Integral((c*x**2)**(3/2)*(a + b*x)**n, x)
```


$$3.932 \quad \int \frac{(cx^2)^{3/2} (a+bx)^n}{x} dx$$

Optimal. Leaf size=99

$$\frac{a^2 c \sqrt{cx^2} (a+bx)^{n+1}}{b^3 (n+1)x} - \frac{2ac \sqrt{cx^2} (a+bx)^{n+2}}{b^3 (n+2)x} + \frac{c \sqrt{cx^2} (a+bx)^{n+3}}{b^3 (n+3)x}$$

[Out] $a^2 c (b^3 x^3 + a^3) (a+bx)^{n+1} (cx^2)^{1/2} / b^3 (n+1) x - 2 a c (b^3 x^3 + a^3) (a+bx)^{n+2} (cx^2)^{1/2} / b^3 (n+2) x + c (b^3 x^3 + a^3) (a+bx)^{n+3} (cx^2)^{1/2} / b^3 (n+3) x$

Rubi [A] time = 0.03, antiderivative size = 99, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2 c \sqrt{cx^2} (a+bx)^{n+1}}{b^3 (n+1)x} - \frac{2ac \sqrt{cx^2} (a+bx)^{n+2}}{b^3 (n+2)x} + \frac{c \sqrt{cx^2} (a+bx)^{n+3}}{b^3 (n+3)x}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x)^n)/x,x]

[Out] $(a^2 c \sqrt{cx^2} (a+bx)^{n+1}) / (b^3 (n+1) x) - (2 a c \sqrt{cx^2} (a+bx)^{n+2}) / (b^3 (n+2) x) + (c \sqrt{cx^2} (a+bx)^{n+3}) / (b^3 (n+3) x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2} (a+bx)^n}{x} dx &= \frac{(c\sqrt{cx^2}) \int x^2 (a+bx)^n dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int \left(\frac{a^2(a+bx)^n}{b^2} - \frac{2a(a+bx)^{1+n}}{b^2} + \frac{(a+bx)^{2+n}}{b^2} \right) dx}{x} \\ &= \frac{a^2 c \sqrt{cx^2} (a+bx)^{1+n}}{b^3(1+n)x} - \frac{2ac \sqrt{cx^2} (a+bx)^{2+n}}{b^3(2+n)x} + \frac{c \sqrt{cx^2} (a+bx)^{3+n}}{b^3(3+n)x} \end{aligned}$$

Mathematica [A] time = 0.03, size = 70, normalized size = 0.71

$$\frac{c^2 x (a+bx)^{n+1} (2a^2 - 2ab(n+1)x + b^2(n^2 + 3n + 2)x^2)}{b^3(n+1)(n+2)(n+3)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x)^n)/x,x]

[Out] (c^2*x*(a + b*x)^(1 + n)*(2*a^2 - 2*a*b*(1 + n)*x + b^2*(2 + 3*n + n^2)*x^2))/(b^3*(1 + n)*(2 + n)*(3 + n)*Sqrt[c*x^2])

fricas [A] time = 0.47, size = 113, normalized size = 1.14

$$\frac{(2a^2bcnx - 2a^3c - (b^3cn^2 + 3b^3cn + 2b^3c)x^3 - (ab^2cn^2 + ab^2cn)x^2)\sqrt{cx^2}(bx+a)^n}{(b^3n^3 + 6b^3n^2 + 11b^3n + 6b^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x,x, algorithm="fricas")

[Out] -(2*a^2*b*c*n*x - 2*a^3*c - (b^3*c*n^2 + 3*b^3*c*n + 2*b^3*c)*x^3 - (a*b^2*c*n^2 + a*b^2*c*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^3*n^3 + 6*b^3*n^2 + 11*b^3*n + 6*b^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (bx+a)^n}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x,x, algorithm="giac")

[Out] integrate((c*x^2)^(3/2)*(b*x + a)^n/x, x)

maple [A] time = 0.01, size = 83, normalized size = 0.84

$$\frac{(b^2 n^2 x^2 + 3b^2 n x^2 - 2abnx + 2b^2 x^2 - 2abx + 2a^2)(cx^2)^{\frac{3}{2}}(bx + a)^{n+1}}{(n^3 + 6n^2 + 11n + 6)b^3 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(b*x+a)^n/x,x)

[Out] (b*x+a)^(n+1)*(b^2*n^2*x^2+3*b^2*n*x^2-2*a*b*n*x+2*b^2*x^2-2*a*b*x+2*a^2)*(c*x^2)^(3/2)/x^3/b^3/(n^3+6*n^2+11*n+6)

maxima [A] time = 1.43, size = 80, normalized size = 0.81

$$\frac{\left((n^2 + 3n + 2)b^3 c^{\frac{3}{2}} x^3 + (n^2 + n)ab^2 c^{\frac{3}{2}} x^2 - 2a^2 b c^{\frac{3}{2}} n x + 2a^3 c^{\frac{3}{2}}\right)(bx + a)^n}{(n^3 + 6n^2 + 11n + 6)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x,x, algorithm="maxima")

[Out] ((n^2 + 3*n + 2)*b^3*c^(3/2)*x^3 + (n^2 + n)*a*b^2*c^(3/2)*x^2 - 2*a^2*b*c^(3/2)*n*x + 2*a^3*c^(3/2))*(b*x + a)^n/((n^3 + 6*n^2 + 11*n + 6)*b^3)

mupad [B] time = 0.26, size = 146, normalized size = 1.47

$$\frac{(a + bx)^n \left(\frac{cx^3 \sqrt{cx^2} (n^2 + 3n + 2)}{n^3 + 6n^2 + 11n + 6} + \frac{2a^3 c \sqrt{cx^2}}{b^3 (n^3 + 6n^2 + 11n + 6)} - \frac{2a^2 c n x \sqrt{cx^2}}{b^2 (n^3 + 6n^2 + 11n + 6)} + \frac{ac n x^2 \sqrt{cx^2} (n + 1)}{b (n^3 + 6n^2 + 11n + 6)} \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(3/2)*(a + b*x)^n)/x,x)

[Out] ((a + b*x)^n*((c*x^3*(c*x^2)^(1/2)*(3*n + n^2 + 2))/(11*n + 6*n^2 + n^3 + 6) + (2*a^3*c*(c*x^2)^(1/2))/(b^3*(11*n + 6*n^2 + n^3 + 6)) - (2*a^2*c*n*x*(c*x^2)^(1/2))/(b^2*(11*n + 6*n^2 + n^3 + 6)) + (a*c*n*x^2*(c*x^2)^(1/2)*(n + 1))/(b*(11*n + 6*n^2 + n^3 + 6))))/x

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}}(a + bx)^n}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((c*x**2)**(3/2)*(b*x+a)**n/x, x)
```

```
[Out] Integral((c*x**2)**(3/2)*(a + b*x)**n/x, x)
```

$$3.933 \quad \int \frac{(cx^2)^{3/2} (a+bx)^n}{x^2} dx$$

Optimal. Leaf size=65

$$\frac{c\sqrt{cx^2} (a+bx)^{n+2}}{b^2(n+2)x} - \frac{ac\sqrt{cx^2} (a+bx)^{n+1}}{b^2(n+1)x}$$

[Out] $-a*c*(b*x+a)^{(1+n)}*(c*x^2)^{(1/2)}/b^2/(1+n)/x+c*(b*x+a)^{(2+n)}*(c*x^2)^{(1/2)}/b^2/(2+n)/x$

Rubi [A] time = 0.02, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{c\sqrt{cx^2} (a+bx)^{n+2}}{b^2(n+2)x} - \frac{ac\sqrt{cx^2} (a+bx)^{n+1}}{b^2(n+1)x}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x)^n)/x^2,x]

[Out] $-((a*c*\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)})/(b^2*(1 + n)*x)) + (c*\text{Sqrt}[c*x^2]*(a + b*x)^{(2 + n)})/(b^2*(2 + n)*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(cx^2)^{3/2} (a+bx)^n}{x^2} dx &= \frac{(c\sqrt{cx^2}) \int x(a+bx)^n dx}{x} \\
&= \frac{(c\sqrt{cx^2}) \int \left(-\frac{a(a+bx)^n}{b} + \frac{(a+bx)^{1+n}}{b}\right) dx}{x} \\
&= -\frac{ac\sqrt{cx^2} (a+bx)^{1+n}}{b^2(1+n)x} + \frac{c\sqrt{cx^2} (a+bx)^{2+n}}{b^2(2+n)x}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 46, normalized size = 0.71

$$\frac{c^2x(a+bx)^{n+1}(b(n+1)x-a)}{b^2(n+1)(n+2)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x)^n)/x^2,x]

[Out] (c^2*x*(a + b*x)^(1 + n)*(-a + b*(1 + n)*x))/(b^2*(1 + n)*(2 + n)*Sqrt[c*x^2])

fricas [A] time = 0.44, size = 68, normalized size = 1.05

$$\frac{(abcnx - a^2c + (b^2cn + b^2c)x^2)\sqrt{cx^2}(bx + a)^n}{(b^2n^2 + 3b^2n + 2b^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^2,x, algorithm="fricas")

[Out] (a*b*c*n*x - a^2*c + (b^2*c*n + b^2*c)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^2*n^2 + 3*b^2*n + 2*b^2)*x)

giac [A] time = 0.91, size = 119, normalized size = 1.83

$$\left(\frac{a^2a^n\text{sgn}(x)}{b^2n^2 + 3b^2n + 2b^2} + \frac{(bx + a)^n b^2 n x^2 \text{sgn}(x) + (bx + a)^n a b n x \text{sgn}(x) + (bx + a)^n b^2 x^2 \text{sgn}(x) - (bx + a)^n a^2 \text{sgn}(x)}{b^2 n^2 + 3 b^2 n + 2 b^2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^2,x, algorithm="giac")

[Out] $(a^2 a^n \operatorname{sgn}(x) / (b^2 n^2 + 3b^2 n + 2b^2) + ((b x + a)^n b^2 n x^2 \operatorname{sgn}(x) + (b x + a)^n a b n x \operatorname{sgn}(x) + (b x + a)^n b^2 x^2 \operatorname{sgn}(x) - (b x + a)^n a^2 \operatorname{sgn}(x)) / (b^2 n^2 + 3b^2 n + 2b^2)) c^{3/2}$

maple [A] time = 0.00, size = 46, normalized size = 0.71

$$\frac{(c x^2)^{\frac{3}{2}} (-x n b - b x + a) (b x + a)^{n+1}}{(n^2 + 3n + 2) b^2 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c*x^2)^(3/2)*(b*x+a)^n/x^2,x)`

[Out] $-(b x + a)^{n+1} (c x^2)^{3/2} (-b n x - b x + a) / x^3 / b^2 / (n^2 + 3n + 2)$

maxima [A] time = 1.43, size = 51, normalized size = 0.78

$$\frac{\left(b^2 c^{\frac{3}{2}} (n+1) x^2 + a b c^{\frac{3}{2}} n x - a^2 c^{\frac{3}{2}}\right) (b x + a)^n}{(n^2 + 3n + 2) b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((c*x^2)^(3/2)*(b*x+a)^n/x^2,x, algorithm="maxima")`

[Out] $(b^2 c^{3/2} (n+1) x^2 + a b c^{3/2} n x - a^2 c^{3/2}) (b x + a)^n / ((n^2 + 3n + 2) b^2)$

mupad [B] time = 0.23, size = 88, normalized size = 1.35

$$\frac{(a + b x)^n \left(\frac{c x^2 \sqrt{c x^2} (n+1)}{n^2 + 3n + 2} - \frac{a^2 c \sqrt{c x^2}}{b^2 (n^2 + 3n + 2)} + \frac{a c n x \sqrt{c x^2}}{b (n^2 + 3n + 2)} \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((c*x^2)^(3/2)*(a + b*x)^n)/x^2,x)`

[Out] $((a + b x)^n ((c x^2 (c x^2)^{1/2} (n+1)) / (3n + n^2 + 2) - (a^2 c (c x^2)^{1/2}) / (b^2 (3n + n^2 + 2))) + (a c n x (c x^2)^{1/2}) / (b (3n + n^2 + 2))) / x$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{a^n c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}}{2x} & \text{for } b = 0 \\ \int \frac{(cx^2)^{\frac{3}{2}}}{x^2(a+bx)^2} dx & \text{for } n = -2 \\ \int \frac{(cx^2)^{\frac{3}{2}}}{x^2(a+bx)} dx & \text{for } n = -1 \\ -\frac{a^2 c^{\frac{3}{2}} (a+bx)^n (x^2)^{\frac{3}{2}}}{b^2 n^2 x^3 + 3b^2 n x^3 + 2b^2 x^3} + \frac{abc^{\frac{3}{2}} n x (a+bx)^n (x^2)^{\frac{3}{2}}}{b^2 n^2 x^3 + 3b^2 n x^3 + 2b^2 x^3} + \frac{b^2 c^{\frac{3}{2}} n x^2 (a+bx)^n (x^2)^{\frac{3}{2}}}{b^2 n^2 x^3 + 3b^2 n x^3 + 2b^2 x^3} + \frac{b^2 c^{\frac{3}{2}} x^2 (a+bx)^n (x^2)^{\frac{3}{2}}}{b^2 n^2 x^3 + 3b^2 n x^3 + 2b^2 x^3} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)*(b*x+a)**n/x**2,x)

[Out] Piecewise((a**n*c**(3/2)*(x**2)**(3/2)/(2*x), Eq(b, 0)), (Integral((c*x**2)**(3/2)/(x**2*(a + b*x)**2), x), Eq(n, -2)), (Integral((c*x**2)**(3/2)/(x**2*(a + b*x)), x), Eq(n, -1)), (-a**2*c**(3/2)*(a + b*x)**n*(x**2)**(3/2)/(b**2*n**2*x**3 + 3*b**2*n*x**3 + 2*b**2*x**3) + a*b*c**(3/2)*n*x*(a + b*x)**n*(x**2)**(3/2)/(b**2*n**2*x**3 + 3*b**2*n*x**3 + 2*b**2*x**3) + b**2*c**(3/2)*n*x**2*(a + b*x)**n*(x**2)**(3/2)/(b**2*n**2*x**3 + 3*b**2*n*x**3 + 2*b**2*x**3) + b**2*c**(3/2)*x**2*(a + b*x)**n*(x**2)**(3/2)/(b**2*n**2*x**3 + 3*b**2*n*x**3 + 2*b**2*x**3), True))

$$3.934 \quad \int \frac{(cx^2)^{3/2} (a+bx)^n}{x^3} dx$$

Optimal. Leaf size=31

$$\frac{c\sqrt{cx^2} (a+bx)^{n+1}}{b(n+1)x}$$

[Out] c*(b*x+a)^(1+n)*(c*x^2)^(1/2)/b/(1+n)/x

Rubi [A] time = 0.01, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$\frac{c\sqrt{cx^2} (a+bx)^{n+1}}{b(n+1)x}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x)^n)/x^3,x]

[Out] (c*Sqrt[c*x^2]*(a + b*x)^(1 + n))/(b*(1 + n)*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{3/2} (a+bx)^n}{x^3} dx &= \frac{(c\sqrt{cx^2}) \int (a+bx)^n dx}{x} \\ &= \frac{c\sqrt{cx^2} (a+bx)^{1+n}}{b(1+n)x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 0.97

$$\frac{(cx^2)^{3/2} (a + bx)^{n+1}}{b(n+1)x^3}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x)^n)/x^3,x]

[Out] ((c*x^2)^(3/2)*(a + b*x)^(1 + n))/(b*(1 + n)*x^3)

fricas [A] time = 0.45, size = 33, normalized size = 1.06

$$\frac{(bcx + ac)\sqrt{cx^2} (bx + a)^n}{(bn + b)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^3,x, algorithm="fricas")

[Out] (b*c*x + a*c)*sqrt(c*x^2)*(b*x + a)^n/((b*n + b)*x)

giac [A] time = 1.09, size = 42, normalized size = 1.35

$$-c^{\frac{3}{2}} \left(\frac{a^{n+1} \operatorname{sgn}(x)}{bn + b} - \frac{(bx + a)^{n+1} \operatorname{sgn}(x)}{b(n+1)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^3,x, algorithm="giac")

[Out] -c^(3/2)*(a^(n + 1)*sgn(x)/(b*n + b) - (b*x + a)^(n + 1)*sgn(x)/(b*(n + 1)))

maple [A] time = 0.00, size = 29, normalized size = 0.94

$$\frac{(cx^2)^{\frac{3}{2}} (bx + a)^{n+1}}{(n+1)bx^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(b*x+a)^n/x^3,x)

[Out] (b*x+a)^(n+1)/b/(n+1)*(c*x^2)^(3/2)/x^3

maxima [A] time = 1.42, size = 28, normalized size = 0.90

$$\frac{\left(bc^{\frac{3}{2}}x + ac^{\frac{3}{2}}\right)(bx + a)^n}{b(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^3,x, algorithm="maxima")

[Out] (b*c^(3/2)*x + a*c^(3/2))*(b*x + a)^n/(b*(n + 1))

mupad [B] time = 0.23, size = 45, normalized size = 1.45

$$\frac{\left(\frac{cx\sqrt{cx^2}}{n+1} + \frac{ac\sqrt{cx^2}}{b(n+1)}\right)(a + bx)^n}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(3/2)*(a + b*x)^n)/x^3,x)

[Out] (((c*x*(c*x^2)^(1/2))/(n + 1) + (a*c*(c*x^2)^(1/2))/(b*(n + 1)))*(a + b*x)^n)/x

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}{ax^2} & \text{for } b = 0 \wedge n = -1 \\ \frac{a^n c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}}{x^2} & \text{for } b = 0 \\ \int \frac{(cx^2)^{\frac{3}{2}}}{x^3(a+bx)} dx & \text{for } n = -1 \\ \frac{ac^{\frac{3}{2}}(a+bx)^n(x^2)^{\frac{3}{2}}}{bnx^3+bx^3} + \frac{bc^{\frac{3}{2}}x(a+bx)^n(x^2)^{\frac{3}{2}}}{bnx^3+bx^3} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)*(b*x+a)**n/x**3,x)

[Out] Piecewise((c**(3/2)*(x**2)**(3/2)/(a*x**2), Eq(b, 0) & Eq(n, -1)), (a**n*c**(3/2)*(x**2)**(3/2)/x**2, Eq(b, 0)), (Integral((c*x**2)**(3/2)/(x**3*(a + b*x)), x), Eq(n, -1)), (a*c**(3/2)*(a + b*x)**n*(x**2)**(3/2)/(b*n*x**3 + b*x**3) + b*c**(3/2)*x*(a + b*x)**n*(x**2)**(3/2)/(b*n*x**3 + b*x**3), True))

$$3.935 \quad \int \frac{(cx^2)^{3/2} (a+bx)^n}{x^4} dx$$

Optimal. Leaf size=48

$$-\frac{c\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)x}$$

[Out] $-c*(b*x+a)^{(1+n)}*\text{hypergeom}([1, 1+n], [2+n], 1+b*x/a)*(c*x^2)^{(1/2)}/a/(1+n)/x$

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$-\frac{c\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}*(a + b*x)^n/x^4, x]$

[Out] $-((c*\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)}*\text{Hypergeometric2F1}[1, 1 + n, 2 + n, 1 + (b*x)/a])/(a*(1 + n)*x))$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n, x\} \&\& \text{IntegerQ}[m]$

Rule 65

$\text{Int}[(b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}), x_Symbol] \rightarrow \text{Simp}[(c + d*x)^{(n + 1)}*\text{Hypergeometric2F1}[-m, n + 1, n + 2, 1 + (d*x)/c]/(d*(n + 1)*(-(d/(b*c)))^m), x] /; \text{FreeQ}\{b, c, d, m, n\}, x \&\& \text{IntegerQ}[n] \&\& (\text{IntegerQ}[m] \mid\mid \text{GtQ}[-(d/(b*c)), 0])$

Rubi steps

$$\int \frac{(cx^2)^{3/2} (a+bx)^n}{x^4} dx = \frac{(c\sqrt{cx^2}) \int \frac{(a+bx)^n}{x} dx}{x}$$

$$= -\frac{c\sqrt{cx^2} (a+bx)^{1+n} {}_2F_1\left(1, 1+n; 2+n; 1+\frac{bx}{a}\right)}{a(1+n)x}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 0.98

$$\frac{(cx^2)^{3/2} (a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a}+1\right)}{a(n+1)x^3}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x)^n)/x^4,x]

[Out] -(((c*x^2)^(3/2)*(a + b*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, 1 + (b*x)/a]))/(a*(1 + n)*x^3)

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2}(bx+a)^n c}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^4,x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n*c/x^2, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (bx+a)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^4,x, algorithm="giac")

[Out] integrate((c*x^2)^(3/2)*(b*x + a)^n/x^4, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (bx+a)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(b*x+a)^n/x^4,x)

[Out] int((c*x^2)^(3/2)*(b*x+a)^n/x^4,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (bx+a)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^4,x, algorithm="maxima")

[Out] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^4,x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{\frac{3}{2}} (a+bx)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(3/2)*(a+b*x)^n)/x^4,x)

[Out] int(((c*x^2)^(3/2)*(a+b*x)^n)/x^4,x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (a+bx)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)*(b*x+a)**n/x**4,x)

[Out] Integral((c*x**2)**(3/2)*(a+b*x)**n/x**4,x)

$$3.936 \quad \int \frac{(cx^2)^{3/2} (a+bx)^n}{x^5} dx$$

Optimal. Leaf size=48

$$\frac{bc\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)x}$$

[Out] b*c*(b*x+a)^(1+n)*hypergeom([2, 1+n], [2+n], 1+b*x/a)*(c*x^2)^(1/2)/a^2/(1+n)/x

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$\frac{bc\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)x}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(3/2)*(a + b*x)^n)/x^5, x]

[Out] (b*c*Sqrt[c*x^2]*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n)*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(cx^2)^{3/2} (a + bx)^n}{x^5} dx = \frac{(c\sqrt{cx^2}) \int \frac{(a+bx)^n}{x^2} dx}{x}$$

$$= \frac{bc\sqrt{cx^2} (a + bx)^{1+n} {}_2F_1\left(2, 1 + n; 2 + n; 1 + \frac{bx}{a}\right)}{a^2(1 + n)x}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 0.98

$$\frac{b (cx^2)^{3/2} (a + bx)^{n+1} {}_2F_1\left(2, n + 1; n + 2; \frac{bx}{a} + 1\right)}{a^2(n + 1)x^3}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x)^n)/x^5,x]

[Out] (b*(c*x^2)^(3/2)*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n)*x^3)

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx + a)^n c}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^5,x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n*c/x^3, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (bx + a)^n}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^5,x, algorithm="giac")

[Out] integrate((c*x^2)^(3/2)*(b*x + a)^n/x^5, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (bx+a)^n}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(b*x+a)^n/x^5,x)

[Out] int((c*x^2)^(3/2)*(b*x+a)^n/x^5,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (bx+a)^n}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^5,x, algorithm="maxima")

[Out] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^5, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{\frac{3}{2}} (a+bx)^n}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(3/2)*(a+b*x)^n)/x^5,x)

[Out] int(((c*x^2)^(3/2)*(a+b*x)^n)/x^5, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (a+bx)^n}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)*(b*x+a)**n/x**5,x)

[Out] Integral((c*x**2)**(3/2)*(a+b*x)**n/x**5, x)

$$3.937 \quad \int \frac{(cx^2)^{3/2} (a+bx)^n}{x^6} dx$$

Optimal. Leaf size=51

$$-\frac{b^2 c \sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3 (n+1)x}$$

[Out] $-b^2*c*(b*x+a)^{(1+n)}*\text{hypergeom}([3, 1+n], [2+n], 1+b*x/a)*(c*x^2)^{(1/2)}/a^3/(1+n)/x$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$-\frac{b^2 c \sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3 (n+1)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(3/2)}*(a + b*x)^n/x^6, x]$

[Out] $-\left(\frac{b^2*c*\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)}*\text{Hypergeometric2F1}[3, 1 + n, 2 + n, 1 + (b*x)/a]}{a^3*(1 + n)*x}\right)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

$\text{Int}[(b_.)*(x_)^{(m_)}*((c_) + (d_.)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(c + d*x)^{(n + 1)}*\text{Hypergeometric2F1}[-m, n + 1, n + 2, 1 + (d*x)/c]/(d*(n + 1)*(-(d/(b*c)))^m), x] /;$ FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(cx^2)^{3/2} (a + bx)^n}{x^6} dx = \frac{(c\sqrt{cx^2}) \int \frac{(a+bx)^n}{x^3} dx}{x}$$

$$= -\frac{b^2 c \sqrt{cx^2} (a + bx)^{1+n} {}_2F_1\left(3, 1 + n; 2 + n; 1 + \frac{bx}{a}\right)}{a^3 (1 + n)x}$$

Mathematica [A] time = 0.01, size = 50, normalized size = 0.98

$$\frac{b^2 (cx^2)^{3/2} (a + bx)^{n+1} {}_2F_1\left(3, n + 1; n + 2; \frac{bx}{a} + 1\right)}{a^3 (n + 1)x^3}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(3/2)*(a + b*x)^n)/x^6,x]

[Out] -((b^2*(c*x^2)^(3/2)*(a + b*x)^(1 + n)*Hypergeometric2F1[3, 1 + n, 2 + n, 1 + (b*x)/a])/(a^3*(1 + n)*x^3))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx + a)^n c}{x^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^6,x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n*c/x^4, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (bx + a)^n}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^6,x, algorithm="giac")

[Out] integrate((c*x^2)^(3/2)*(b*x + a)^n/x^6, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (bx+a)^n}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(3/2)*(b*x+a)^n/x^6,x)

[Out] int((c*x^2)^(3/2)*(b*x+a)^n/x^6,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (bx+a)^n}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^6,x, algorithm="maxima")

[Out] integrate((c*x^2)^(3/2)*(b*x+a)^n/x^6, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{3/2} (a+bx)^n}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(3/2)*(a+b*x)^n)/x^6,x)

[Out] int(((c*x^2)^(3/2)*(a+b*x)^n)/x^6, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{3}{2}} (a+bx)^n}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(3/2)*(b*x+a)**n/x**6,x)

[Out] Integral((c*x**2)**(3/2)*(a+b*x)**n/x**6, x)

3.938 $\int (cx^2)^{5/2} (a + bx)^n dx$

Optimal. Leaf size=217

$$-\frac{a^5 c^2 \sqrt{cx^2} (a + bx)^{n+1}}{b^6 (n+1)x} + \frac{5a^4 c^2 \sqrt{cx^2} (a + bx)^{n+2}}{b^6 (n+2)x} - \frac{10a^3 c^2 \sqrt{cx^2} (a + bx)^{n+3}}{b^6 (n+3)x} + \frac{10a^2 c^2 \sqrt{cx^2} (a + bx)^{n+4}}{b^6 (n+4)x} - \frac{5ac^2 \sqrt{cx^2} (a + bx)^{n+5}}{b^6 (n+5)x} + \frac{c^2 (a + bx)^{n+6}}{b^6 (n+6)x}$$

[Out] $-a^5 c^2 (b^6 x^6 + 6 a b^5 x^5 + 15 a^2 b^4 x^4 + 20 a^3 b^3 x^3 + 15 a^4 b^2 x^2 + 6 a^5 b x + a^6) (c x^2)^{5/2} (a + b x)^{n+6} / (b^6 (n+6) x^7 + 6 a b^5 (n+5) x^6 + 15 a^2 b^4 (n+4) x^5 + 20 a^3 b^3 (n+3) x^4 + 15 a^4 b^2 (n+2) x^3 + 6 a^5 b (n+1) x^2 + a^6 (n))$

Rubi [A] time = 0.07, antiderivative size = 217, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 43}

$$-\frac{a^5 c^2 \sqrt{cx^2} (a + bx)^{n+1}}{b^6 (n+1)x} + \frac{5a^4 c^2 \sqrt{cx^2} (a + bx)^{n+2}}{b^6 (n+2)x} - \frac{10a^3 c^2 \sqrt{cx^2} (a + bx)^{n+3}}{b^6 (n+3)x} + \frac{10a^2 c^2 \sqrt{cx^2} (a + bx)^{n+4}}{b^6 (n+4)x} - \frac{5ac^2 \sqrt{cx^2} (a + bx)^{n+5}}{b^6 (n+5)x} + \frac{c^2 (a + bx)^{n+6}}{b^6 (n+6)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(5/2)}*(a + b*x)^n, x]$

[Out] $-(a^5 c^2 \sqrt{cx^2} (a + bx)^{n+1} / (b^6 (n+1)x) + 5a^4 c^2 \sqrt{cx^2} (a + bx)^{n+2} / (b^6 (n+2)x) - 10a^3 c^2 \sqrt{cx^2} (a + bx)^{n+3} / (b^6 (n+3)x) + 10a^2 c^2 \sqrt{cx^2} (a + bx)^{n+4} / (b^6 (n+4)x) - 5ac^2 \sqrt{cx^2} (a + bx)^{n+5} / (b^6 (n+5)x) + c^2 (a + bx)^{n+6} / (b^6 (n+6)x))$

Rule 15

$\text{Int}[(u_.) * ((a_.) * (x_.)^{(n_.)})^{(m_.)}, x_Symbol] := \text{Dist}[(a^{\text{IntPart}[m]} * (a*x^n)^{\text{FracPart}[m]}) / x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

$\text{Int}[(a_.) + (b_.) * (x_.)^{(m_.)}] * ((c_.) + (d_.) * (x_.)^{(n_.)}), x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m * (c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int (cx^2)^{5/2} (a+bx)^n dx = \frac{(c^2\sqrt{cx^2}) \int x^5 (a+bx)^n dx}{x}$$

$$= \frac{(c^2\sqrt{cx^2}) \int \left(-\frac{a^5(a+bx)^n}{b^5} + \frac{5a^4(a+bx)^{1+n}}{b^5} - \frac{10a^3(a+bx)^{2+n}}{b^5} + \frac{10a^2(a+bx)^{3+n}}{b^5} - \frac{5a(a+bx)^{4+n}}{b^5} + \frac{(a+bx)^{5+n}}{b^5} \right) dx}{x}$$

$$= -\frac{a^5 c^2 \sqrt{cx^2} (a+bx)^{1+n}}{b^6(1+n)x} + \frac{5a^4 c^2 \sqrt{cx^2} (a+bx)^{2+n}}{b^6(2+n)x} - \frac{10a^3 c^2 \sqrt{cx^2} (a+bx)^{3+n}}{b^6(3+n)x} + \frac{10a^2 c^2 \sqrt{cx^2} (a+bx)^{4+n}}{b^6(4+n)x} - \frac{5a c^2 \sqrt{cx^2} (a+bx)^{5+n}}{b^6(5+n)x} + \frac{c^2 \sqrt{cx^2} (a+bx)^{6+n}}{b^6(6+n)x}$$

Mathematica [A] time = 0.11, size = 172, normalized size = 0.79

$$\frac{c^3 x (a+bx)^{n+1} (-120a^5 + 120a^4 b(n+1)x - 60a^3 b^2 (n^2 + 3n + 2)x^2 + 20a^2 b^3 (n^3 + 6n^2 + 11n + 6)x^3 - 5ab^4 (n^4 + 6n^3 + 15n^2 + 10n + 5)x^4 + b^5 (n^5 + 5n^4 + 10n^3 + 10n^2 + 5n + 5)x^5)}{b^6(n+1)(n+2)(n+3)(n+4)(n+5)(n+6)}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^(5/2)*(a + b*x)^n,x]

[Out] (c^3*x*(a + b*x)^(1 + n)*(-120*a^5 + 120*a^4*b*(1 + n)*x - 60*a^3*b^2*(2 + 3*n + n^2)*x^2 + 20*a^2*b^3*(6 + 11*n + 6*n^2 + n^3)*x^3 - 5*a*b^4*(24 + 50*n + 35*n^2 + 10*n^3 + n^4)*x^4 + b^5*(120 + 274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5)*x^5)/(b^6*(1 + n)*(2 + n)*(3 + n)*(4 + n)*(5 + n)*(6 + n)*Sqrt[c*x^2])

fricas [A] time = 0.47, size = 352, normalized size = 1.62

$$\frac{(120 a^5 b c^2 n x - 120 a^6 c^2 + (b^6 c^2 n^5 + 15 b^6 c^2 n^4 + 85 b^6 c^2 n^3 + 225 b^6 c^2 n^2 + 274 b^6 c^2 n + 120 b^6 c^2) x^6 + (a b^5 c^2 n^5 + 10 a b^5 c^2 n^4 + 35 a b^5 c^2 n^3 + 50 a b^5 c^2 n^2 + 24 a b^5 c^2 n) x^5 - 5 (a^2 b^4 c^2 n^4 + 6 a^2 b^4 c^2 n^3 + 11 a^2 b^4 c^2 n^2 + 6 a^2 b^4 c^2 n) x^4 + 20 (a^3 b^3 c^2 n^3 + 3 a^3 b^3 c^2 n^2 + 2 a^3 b^3 c^2 n) x^3 - 60 (a^4 b^2 c^2 n^2 + a^4 b^2 c^2 n) x^2) \sqrt{c x^2} (b x + a)^n}{(b^6 n^6 + 21 b^6 n^5 + 175 b^6 n^4 + 735 b^6 n^3 + 1624 b^6 n^2 + 1764 b^6 n + 720 b^6) x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n,x, algorithm="fricas")

[Out] (120*a^5*b*c^2*n*x - 120*a^6*c^2 + (b^6*c^2*n^5 + 15*b^6*c^2*n^4 + 85*b^6*c^2*n^3 + 225*b^6*c^2*n^2 + 274*b^6*c^2*n + 120*b^6*c^2)*x^6 + (a*b^5*c^2*n^5 + 10*a*b^5*c^2*n^4 + 35*a*b^5*c^2*n^3 + 50*a*b^5*c^2*n^2 + 24*a*b^5*c^2*n)*x^5 - 5*(a^2*b^4*c^2*n^4 + 6*a^2*b^4*c^2*n^3 + 11*a^2*b^4*c^2*n^2 + 6*a^2*b^4*c^2*n)*x^4 + 20*(a^3*b^3*c^2*n^3 + 3*a^3*b^3*c^2*n^2 + 2*a^3*b^3*c^2*n)*x^3 - 60*(a^4*b^2*c^2*n^2 + a^4*b^2*c^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^6*n^6 + 21*b^6*n^5 + 175*b^6*n^4 + 735*b^6*n^3 + 1624*b^6*n^2 + 1764*b^6*n + 720*b^6)*x)

giac [B] time = 1.06, size = 640, normalized size = 2.95

$$\left(\frac{120 a^6 a^n c^2 \operatorname{sgn}(x)}{b^6 n^6 + 21 b^6 n^5 + 175 b^6 n^4 + 735 b^6 n^3 + 1624 b^6 n^2 + 1764 b^6 n + 720 b^6} + \frac{(bx+a)^n b^6 c^2 n^5 x^6 \operatorname{sgn}(x) + (bx+a)^n}{b^6 n^6 + 21 b^6 n^5 + 175 b^6 n^4 + 735 b^6 n^3 + 1624 b^6 n^2 + 1764 b^6 n + 720 b^6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n,x, algorithm="giac")

[Out] (120*a^6*a^n*c^2*sgn(x)/(b^6*n^6 + 21*b^6*n^5 + 175*b^6*n^4 + 735*b^6*n^3 + 1624*b^6*n^2 + 1764*b^6*n + 720*b^6) + ((b*x + a)^n*b^6*c^2*n^5*x^6*sgn(x) + (b*x + a)^n*a*b^5*c^2*n^5*x^5*sgn(x) + 15*(b*x + a)^n*b^6*c^2*n^4*x^6*sgn(x) + 10*(b*x + a)^n*a*b^5*c^2*n^4*x^5*sgn(x) + 85*(b*x + a)^n*b^6*c^2*n^3*x^6*sgn(x) - 5*(b*x + a)^n*a^2*b^4*c^2*n^4*x^4*sgn(x) + 35*(b*x + a)^n*a*b^5*c^2*n^3*x^5*sgn(x) + 225*(b*x + a)^n*b^6*c^2*n^2*x^6*sgn(x) - 30*(b*x + a)^n*a^2*b^4*c^2*n^3*x^4*sgn(x) + 50*(b*x + a)^n*a*b^5*c^2*n^2*x^5*sgn(x) + 274*(b*x + a)^n*b^6*c^2*n*x^6*sgn(x) + 20*(b*x + a)^n*a^3*b^3*c^2*n^3*x^3*sgn(x) - 55*(b*x + a)^n*a^2*b^4*c^2*n^2*x^4*sgn(x) + 24*(b*x + a)^n*a*b^5*c^2*n*x^5*sgn(x) + 120*(b*x + a)^n*b^6*c^2*x^6*sgn(x) + 60*(b*x + a)^n*a^3*b^3*c^2*n^2*x^3*sgn(x) - 30*(b*x + a)^n*a^2*b^4*c^2*n*x^4*sgn(x) - 60*(b*x + a)^n*a^4*b^2*c^2*n^2*x^2*sgn(x) + 40*(b*x + a)^n*a^3*b^3*c^2*n*x^3*sgn(x) - 60*(b*x + a)^n*a^4*b^2*c^2*n*x^2*sgn(x) + 120*(b*x + a)^n*a^5*b*c^2*n*x*sgn(x) - 120*(b*x + a)^n*a^6*c^2*sgn(x))/(b^6*n^6 + 21*b^6*n^5 + 175*b^6*n^4 + 735*b^6*n^3 + 1624*b^6*n^2 + 1764*b^6*n + 720*b^6))*sqrt(c)

maple [A] time = 0.01, size = 280, normalized size = 1.29

$$\frac{(cx^2)^{\frac{5}{2}} \left(-b^5 n^5 x^5 - 15b^5 n^4 x^5 + 5a b^4 n^4 x^4 - 85b^5 n^3 x^5 + 50a b^4 n^3 x^4 - 225b^5 n^2 x^5 - 20a^2 b^3 n^3 x^3 + 175a b^4 n^2 x^4 \right)}{b^6 n^6 + 21 b^6 n^5 + 175 b^6 n^4 + 735 b^6 n^3 + 1624 b^6 n^2 + 1764 b^6 n + 720 b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)^n,x)

[Out] -(b*x+a)^(n+1)*(c*x^2)^(5/2)*(-b^5*n^5*x^5-15*b^5*n^4*x^5+5*a*b^4*n^4*x^4-85*b^5*n^3*x^5+50*a*b^4*n^3*x^4-225*b^5*n^2*x^5-20*a^2*b^3*n^3*x^3+175*a*b^4*n^2*x^4-274*b^5*n*x^5-120*a^2*b^3*n^2*x^3+250*a*b^4*n*x^4-120*b^5*x^5+60*a^3*b^2*n^2*x^2-220*a^2*b^3*n*x^3+120*a*b^4*x^4+180*a^3*b^2*n*x^2-120*a^2*b^3*x^3-120*a^4*b*n*x+120*a^3*b^2*x^2-120*a^4*b*x+120*a^5)/x^5/b^6/(n^6+21*n^5+175*n^4+735*n^3+1624*n^2+1764*n+720)

maxima [A] time = 1.53, size = 203, normalized size = 0.94

$$\frac{\left((n^5 + 15n^4 + 85n^3 + 225n^2 + 274n + 120)b^6 c^{\frac{5}{2}} x^6 + (n^5 + 10n^4 + 35n^3 + 50n^2 + 24n)ab^5 c^{\frac{5}{2}} x^5 - 5(n^4 + 6n^3 + 15n^2 + 10n + 5)a^2 b^4 c^{\frac{5}{2}} x^4 - 5(n^3 + 3n^2 + 3n + 1)a^3 b^3 c^{\frac{5}{2}} x^3 - 5(n^2 + 2n + 1)a^4 b^2 c^{\frac{5}{2}} x^2 - 5na^5 b c^{\frac{5}{2}} x + 5a^6 c^{\frac{5}{2}} \right)}{(n^6 + 21n^5 + 175n^4 + 735n^3 + 1624n^2 + 1764n + 720)b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n,x, algorithm="maxima")

[Out] ((n^5 + 15*n^4 + 85*n^3 + 225*n^2 + 274*n + 120)*b^6*c^(5/2)*x^6 + (n^5 + 10*n^4 + 35*n^3 + 50*n^2 + 24*n)*a*b^5*c^(5/2)*x^5 - 5*(n^4 + 6*n^3 + 11*n^2 + 6*n)*a^2*b^4*c^(5/2)*x^4 + 20*(n^3 + 3*n^2 + 2*n)*a^3*b^3*c^(5/2)*x^3 - 60*(n^2 + n)*a^4*b^2*c^(5/2)*x^2 + 120*a^5*b*c^(5/2)*n*x - 120*a^6*c^(5/2))* (b*x + a)^n/((n^6 + 21*n^5 + 175*n^4 + 735*n^3 + 1624*n^2 + 1764*n + 720)* b^6)

mupad [B] time = 0.50, size = 424, normalized size = 1.95

$$(a + bx)^n \left(\frac{c^2 x^6 \sqrt{cx^2} (n^5 + 15n^4 + 85n^3 + 225n^2 + 274n + 120)}{n^6 + 21n^5 + 175n^4 + 735n^3 + 1624n^2 + 1764n + 720} - \frac{120 a^6 c^2 \sqrt{cx^2}}{b^6 (n^6 + 21n^5 + 175n^4 + 735n^3 + 1624n^2 + 1764n + 720)} + \frac{120 a^5 b c \sqrt{cx^2}}{b^5 (n^6 + 21n^5 + 175n^4 + 735n^3 + 1624n^2 + 1764n + 720)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(a + b*x)^n,x)

[Out] ((a + b*x)^n*((c^2*x^6*(c*x^2)^(1/2)*(274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120))/(1764*n + 1624*n^2 + 735*n^3 + 175*n^4 + 21*n^5 + n^6 + 720) - (120*a^6*c^2*(c*x^2)^(1/2))/(b^6*(1764*n + 1624*n^2 + 735*n^3 + 175*n^4 + 21*n^5 + n^6 + 720)) + (120*a^5*c^2*n*x*(c*x^2)^(1/2))/(b^5*(1764*n + 1624*n^2 + 735*n^3 + 175*n^4 + 21*n^5 + n^6 + 720)) - (5*a^2*c^2*n*x^4*(c*x^2)^(1/2)*(11*n + 6*n^2 + n^3 + 6))/(b^2*(1764*n + 1624*n^2 + 735*n^3 + 175*n^4 + 21*n^5 + n^6 + 720)) - (60*a^4*c^2*n*x^2*(c*x^2)^(1/2)*(n + 1))/(b^4*(1764*n + 1624*n^2 + 735*n^3 + 175*n^4 + 21*n^5 + n^6 + 720)) + (a*c^2*n*x^5*(c*x^2)^(1/2)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24))/(b*(1764*n + 1624*n^2 + 735*n^3 + 175*n^4 + 21*n^5 + n^6 + 720)) + (20*a^3*c^2*n*x^3*(c*x^2)^(1/2)*(3*n + n^2 + 2))/(b^3*(1764*n + 1624*n^2 + 735*n^3 + 175*n^4 + 21*n^5 + n^6 + 720))))/x

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^{\frac{5}{2}} (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a)**n,x)

[Out] Integral((c*x**2)**(5/2)*(a + b*x)**n, x)

$$3.939 \quad \int \frac{(cx^2)^{5/2} (a+bx)^n}{x} dx$$

Optimal. Leaf size=179

$$\frac{a^4 c^2 \sqrt{cx^2} (a+bx)^{n+1}}{b^5 (n+1)x} - \frac{4a^3 c^2 \sqrt{cx^2} (a+bx)^{n+2}}{b^5 (n+2)x} + \frac{6a^2 c^2 \sqrt{cx^2} (a+bx)^{n+3}}{b^5 (n+3)x} - \frac{4ac^2 \sqrt{cx^2} (a+bx)^{n+4}}{b^5 (n+4)x} + \frac{c^2 \sqrt{cx^2} (a+bx)}{b^5 (n+5)x}$$

[Out] $a^4 c^2 (b^5 x^5 + a^5) (cx^2)^{5/2} (a+bx)^{n+1} / (b^5 (n+1)x) - 4a^3 c^2 (b^5 x^5 + a^5) (cx^2)^{5/2} (a+bx)^{n+2} / (b^5 (n+2)x) + 6a^2 c^2 (b^5 x^5 + a^5) (cx^2)^{5/2} (a+bx)^{n+3} / (b^5 (n+3)x) - 4ac^2 (b^5 x^5 + a^5) (cx^2)^{5/2} (a+bx)^{n+4} / (b^5 (n+4)x) + c^2 (b^5 x^5 + a^5) (cx^2)^{5/2} (a+bx)^{n+5} / (b^5 (n+5)x)$

Rubi [A] time = 0.05, antiderivative size = 179, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^4 c^2 \sqrt{cx^2} (a+bx)^{n+1}}{b^5 (n+1)x} - \frac{4a^3 c^2 \sqrt{cx^2} (a+bx)^{n+2}}{b^5 (n+2)x} + \frac{6a^2 c^2 \sqrt{cx^2} (a+bx)^{n+3}}{b^5 (n+3)x} - \frac{4ac^2 \sqrt{cx^2} (a+bx)^{n+4}}{b^5 (n+4)x} + \frac{c^2 \sqrt{cx^2} (a+bx)}{b^5 (n+5)x}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^n)/x,x]

[Out] $(a^4 c^2 \sqrt{cx^2} (a+bx)^{n+1}) / (b^5 (n+1)x) - (4a^3 c^2 \sqrt{cx^2} (a+bx)^{n+2}) / (b^5 (n+2)x) + (6a^2 c^2 \sqrt{cx^2} (a+bx)^{n+3}) / (b^5 (n+3)x) - (4ac^2 \sqrt{cx^2} (a+bx)^{n+4}) / (b^5 (n+4)x) + (c^2 \sqrt{cx^2} (a+bx)) / (b^5 (n+5)x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)^n}{x} dx &= \frac{(c^2 \sqrt{cx^2}) \int x^4 (a+bx)^n dx}{x} \\ &= \frac{(c^2 \sqrt{cx^2}) \int \left(\frac{a^4 (a+bx)^n}{b^4} - \frac{4a^3 (a+bx)^{1+n}}{b^4} + \frac{6a^2 (a+bx)^{2+n}}{b^4} - \frac{4a (a+bx)^{3+n}}{b^4} + \frac{(a+bx)^{4+n}}{b^4} \right) dx}{x} \\ &= \frac{a^4 c^2 \sqrt{cx^2} (a+bx)^{1+n}}{b^5 (1+n)x} - \frac{4a^3 c^2 \sqrt{cx^2} (a+bx)^{2+n}}{b^5 (2+n)x} + \frac{6a^2 c^2 \sqrt{cx^2} (a+bx)^{3+n}}{b^5 (3+n)x} - \frac{4ac^2 \sqrt{cx^2} (a+bx)^{4+n}}{b^5 (4+n)x} + \frac{c^2 \sqrt{cx^2} (a+bx)^{5+n}}{b^5 (5+n)x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 133, normalized size = 0.74

$$\frac{c (cx^2)^{3/2} (a+bx)^{n+1} (24a^4 - 24a^3 b(n+1)x + 12a^2 b^2 (n^2 + 3n + 2)x^2 - 4ab^3 (n^3 + 6n^2 + 11n + 6)x^3 + b^4 (n^4 + 5n^3 + 10n^2 + 10n + 5)x^4)}{b^5 (n+1)(n+2)(n+3)(n+4)(n+5)x^3}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^n)/x,x]

[Out] (c*(c*x^2)^(3/2)*(a + b*x)^(1 + n)*(24*a^4 - 24*a^3*b*(1 + n)*x + 12*a^2*b^2*(2 + 3*n + n^2)*x^2 - 4*a*b^3*(6 + 11*n + 6*n^2 + n^3)*x^3 + b^4*(24 + 50*n + 35*n^2 + 10*n^3 + n^4)*x^4))/(b^5*(1 + n)*(2 + n)*(3 + n)*(4 + n)*(5 + n)*x^3)

fricas [A] time = 0.47, size = 265, normalized size = 1.48

$$\frac{(24 a^4 b c^2 n x - 24 a^5 c^2 - (b^5 c^2 n^4 + 10 b^5 c^2 n^3 + 35 b^5 c^2 n^2 + 50 b^5 c^2 n + 24 b^5 c^2) x^5 - (a b^4 c^2 n^4 + 6 a b^4 c^2 n^3 + 11 a b^4 c^2 n^2 + 5 a b^4 c^2 n + 4 a b^4 c^2) x^4 - (a^2 b^3 c^2 n^4 + 3 a^2 b^3 c^2 n^3 + 3 a^2 b^3 c^2 n^2 + 2 a^2 b^3 c^2 n + a^2 b^3 c^2) x^3 - 12 (a^3 b^2 c^2 n^2 + a^3 b^2 c^2 n) x^2) \sqrt{c x^2} (b x + a)^n}{(b^5 n^5 + 15 b^5 n^4 + 85 b^5 n^3 + 225 b^5 n^2 + 274 b^5 n + 120 b^5) x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x,x, algorithm="fricas")

[Out] -(24*a^4*b*c^2*n*x - 24*a^5*c^2 - (b^5*c^2*n^4 + 10*b^5*c^2*n^3 + 35*b^5*c^2*n^2 + 50*b^5*c^2*n + 24*b^5*c^2)*x^5 - (a*b^4*c^2*n^4 + 6*a*b^4*c^2*n^3 + 11*a*b^4*c^2*n^2 + 6*a*b^4*c^2*n)*x^4 + 4*(a^2*b^3*c^2*n^3 + 3*a^2*b^3*c^2*n^2 + 2*a^2*b^3*c^2*n)*x^3 - 12*(a^3*b^2*c^2*n^2 + a^3*b^2*c^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^5*n^5 + 15*b^5*n^4 + 85*b^5*n^3 + 225*b^5*n^2 + 274*b^5*n + 120*b^5)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{5/2} (bx+a)^n}{x} dx$$


```
/(b^5*(274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120)) - (24*a^4*c^2*n*x*(c
*x^2)^(1/2))/(b^4*(274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120)) + (a*c^2
*n*x^4*(c*x^2)^(1/2)*(11*n + 6*n^2 + n^3 + 6))/(b*(274*n + 225*n^2 + 85*n^3
+ 15*n^4 + n^5 + 120)) + (12*a^3*c^2*n*x^2*(c*x^2)^(1/2)*(n + 1))/(b^3*(27
4*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120)) - (4*a^2*c^2*n*x^3*(c*x^2)^(1
/2)*(3*n + n^2 + 2))/(b^2*(274*n + 225*n^2 + 85*n^3 + 15*n^4 + n^5 + 120))
)/x
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (a + bx)^n}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a)**n/x, x)

[Out] Integral((c*x**2)**(5/2)*(a + b*x)**n/x, x)

$$3.940 \quad \int \frac{(cx^2)^{5/2} (a+bx)^n}{x^2} dx$$

Optimal. Leaf size=143

$$-\frac{a^3 c^2 \sqrt{cx^2} (a+bx)^{n+1}}{b^4 (n+1)x} + \frac{3a^2 c^2 \sqrt{cx^2} (a+bx)^{n+2}}{b^4 (n+2)x} - \frac{3ac^2 \sqrt{cx^2} (a+bx)^{n+3}}{b^4 (n+3)x} + \frac{c^2 \sqrt{cx^2} (a+bx)^{n+4}}{b^4 (n+4)x}$$

[Out] $-a^3 c^2 (b^4 (n+1) x)^{-1} (a+bx)^{n+1} (cx^2)^{5/2} / b^4 (n+1) x + 3a^2 c^2 (b^4 (n+2) x)^{-1} (a+bx)^{n+2} (cx^2)^{5/2} / b^4 (n+2) x - 3ac^2 (b^4 (n+3) x)^{-1} (a+bx)^{n+3} (cx^2)^{5/2} / b^4 (n+3) x + c^2 (b^4 (n+4) x)^{-1} (a+bx)^{n+4} (cx^2)^{5/2} / b^4 (n+4) x$

Rubi [A] time = 0.04, antiderivative size = 143, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^3 c^2 \sqrt{cx^2} (a+bx)^{n+1}}{b^4 (n+1)x} + \frac{3a^2 c^2 \sqrt{cx^2} (a+bx)^{n+2}}{b^4 (n+2)x} - \frac{3ac^2 \sqrt{cx^2} (a+bx)^{n+3}}{b^4 (n+3)x} + \frac{c^2 \sqrt{cx^2} (a+bx)^{n+4}}{b^4 (n+4)x}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^n)/x^2, x]

[Out] $-\frac{(a^3 c^2 \sqrt{cx^2} (a+bx)^{n+1}) / (b^4 (n+1) x)}{b^4 (n+1) x} + \frac{(3a^2 c^2 \sqrt{cx^2} (a+bx)^{n+2}) / (b^4 (n+2) x)}{b^4 (n+2) x} - \frac{(3ac^2 \sqrt{cx^2} (a+bx)^{n+3}) / (b^4 (n+3) x)}{b^4 (n+3) x} + \frac{(c^2 \sqrt{cx^2} (a+bx)^{n+4}) / (b^4 (n+4) x)}{b^4 (n+4) x}$

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)^n}{x^2} dx &= \frac{(c^2 \sqrt{cx^2}) \int x^3 (a+bx)^n dx}{x} \\ &= \frac{(c^2 \sqrt{cx^2}) \int \left(-\frac{a^3(a+bx)^n}{b^3} + \frac{3a^2(a+bx)^{1+n}}{b^3} - \frac{3a(a+bx)^{2+n}}{b^3} + \frac{(a+bx)^{3+n}}{b^3} \right) dx}{x} \\ &= -\frac{a^3 c^2 \sqrt{cx^2} (a+bx)^{1+n}}{b^4(1+n)x} + \frac{3a^2 c^2 \sqrt{cx^2} (a+bx)^{2+n}}{b^4(2+n)x} - \frac{3ac^2 \sqrt{cx^2} (a+bx)^{3+n}}{b^4(3+n)x} + \frac{c^2 \sqrt{cx^2} (a+bx)^{4+n}}{b^4(4+n)x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 99, normalized size = 0.69

$$\frac{c (cx^2)^{3/2} (a+bx)^{n+1} (-6a^3 + 6a^2b(n+1)x - 3ab^2(n^2 + 3n + 2)x^2 + b^3(n^3 + 6n^2 + 11n + 6)x^3)}{b^4(n+1)(n+2)(n+3)(n+4)x^3}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^n)/x^2,x]

[Out] (c*(c*x^2)^(3/2)*(a + b*x)^(1 + n)*(-6*a^3 + 6*a^2*b*(1 + n)*x - 3*a*b^2*(2 + 3*n + n^2)*x^2 + b^3*(6 + 11*n + 6*n^2 + n^3)*x^3))/(b^4*(1 + n)*(2 + n)*(3 + n)*(4 + n)*x^3)

fricas [A] time = 0.45, size = 186, normalized size = 1.30

$$\frac{(6a^3bc^2nx - 6a^4c^2 + (b^4c^2n^3 + 6b^4c^2n^2 + 11b^4c^2n + 6b^4c^2)x^4 + (ab^3c^2n^3 + 3ab^3c^2n^2 + 2ab^3c^2n)x^3 - 3(a^2b^2c^2n^2 + 3ab^2c^2n)x^2 + (a^2b^2c^2n^2 + 3ab^2c^2n)x - a^2b^2c^2n)x^3 - 3(a^2b^2c^2n^2 + 3ab^2c^2n)x^2 + (a^2b^2c^2n^2 + 3ab^2c^2n)x - a^2b^2c^2n)x}{(b^4n^4 + 10b^4n^3 + 35b^4n^2 + 50b^4n + 24b^4)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^2,x, algorithm="fricas")

[Out] (6*a^3*b*c^2*n*x - 6*a^4*c^2 + (b^4*c^2*n^3 + 6*b^4*c^2*n^2 + 11*b^4*c^2*n + 6*b^4*c^2)*x^4 + (a*b^3*c^2*n^3 + 3*a*b^3*c^2*n^2 + 2*a*b^3*c^2*n)*x^3 - 3*(a^2*b^2*c^2*n^2 + a^2*b^2*c^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^4*n^4 + 10*b^4*n^3 + 35*b^4*n^2 + 50*b^4*n + 24*b^4)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{5/2} (bx+a)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^2,x, algorithm="giac")

[Out] integrate((c*x^2)^(5/2)*(b*x + a)^n/x^2, x)

maple [A] time = 0.01, size = 136, normalized size = 0.95

$$\frac{(cx^2)^{\frac{5}{2}}(-b^3n^3x^3 - 6b^3n^2x^3 + 3ab^2n^2x^2 - 11b^3nx^3 + 9ab^2nx^2 - 6b^3x^3 - 6a^2bnx + 6ab^2x^2 - 6a^2bx + 6a^3)(b)}{(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)^n/x^2,x)

[Out] $-(b*x+a)^{(n+1)}*(c*x^2)^{(5/2)}*(-b^3*n^3*x^3-6*b^3*n^2*x^3+3*a*b^2*n^2*x^2-11*b^3*n*x^3+9*a*b^2*n*x^2-6*b^3*x^3-6*a^2*b*n*x+6*a*b^2*x^2-6*a^2*b*x+6*a^3)/x^5/b^4/(n^4+10*n^3+35*n^2+50*n+24)$

maxima [A] time = 1.45, size = 116, normalized size = 0.81

$$\frac{\left(\left(n^3 + 6n^2 + 11n + 6\right)b^4c^{\frac{5}{2}}x^4 + \left(n^3 + 3n^2 + 2n\right)ab^3c^{\frac{5}{2}}x^3 - 3\left(n^2 + n\right)a^2b^2c^{\frac{5}{2}}x^2 + 6a^3bc^{\frac{5}{2}}nx - 6a^4c^{\frac{5}{2}}\right)(bx + a)^n}{\left(n^4 + 10n^3 + 35n^2 + 50n + 24\right)b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^2,x, algorithm="maxima")

[Out] $\left(\left(n^3 + 6n^2 + 11n + 6\right)*b^4*c^{\left(5/2\right)}*x^4 + \left(n^3 + 3n^2 + 2n\right)*a*b^3*c^{\left(5/2\right)}*x^3 - 3*\left(n^2 + n\right)*a^2*b^2*c^{\left(5/2\right)}*x^2 + 6*a^3*b*c^{\left(5/2\right)}*n*x - 6*a^4*c^{\left(5/2\right)}\right)*(b*x + a)^n/\left(\left(n^4 + 10n^3 + 35n^2 + 50n + 24\right)*b^4\right)$

mupad [B] time = 0.32, size = 229, normalized size = 1.60

$$\frac{(a + bx)^n \left(\frac{c^2 x^4 \sqrt{cx^2} (n^3 + 6n^2 + 11n + 6)}{n^4 + 10n^3 + 35n^2 + 50n + 24} - \frac{6a^4 c^2 \sqrt{cx^2}}{b^4 (n^4 + 10n^3 + 35n^2 + 50n + 24)} + \frac{6a^3 c^2 n x \sqrt{cx^2}}{b^3 (n^4 + 10n^3 + 35n^2 + 50n + 24)} + \frac{a c^2 n x^3 \sqrt{cx^2} (n^2 + 3n + 2)}{b (n^4 + 10n^3 + 35n^2 + 50n + 24)} \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(5/2)*(a + b*x)^n)/x^2,x)

[Out] $\left(\left(a + b*x\right)^n*\left(\frac{c^2*x^4*(c*x^2)^{\left(1/2\right)}*\left(11*n + 6*n^2 + n^3 + 6\right)}{\left(50*n + 35*n^2 + 10*n^3 + n^4 + 24\right)} - \frac{6*a^4*c^2*(c*x^2)^{\left(1/2\right)}}{b^4*\left(50*n + 35*n^2 + 10*n^3 + n^4 + 24\right)} + \frac{6*a^3*c^2*n*x*(c*x^2)^{\left(1/2\right)}}{b^3*\left(50*n + 35*n^2 + 10*n^3 + n^4 + 24\right)} + \frac{a*c^2*n*x^3*(c*x^2)^{\left(1/2\right)}*\left(3*n + n^2 + 2\right)}{b*\left(50*n + 35*n^2 + 10*n^3 + n^4 + 24\right)} - \frac{3*a^2*c^2*n*x^2*(c*x^2)^{\left(1/2\right)}*\left(n + 1\right)}{b^2*\left(50*n + 35*n^2 + 10*n^3 + n^4 + 24\right)}\right)/x$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (a + bx)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a)**n/x**2,x)

[Out] Integral((c*x**2)**(5/2)*(a + b*x)**n/x**2, x)

$$3.941 \quad \int \frac{(cx^2)^{5/2} (a+bx)^n}{x^3} dx$$

Optimal. Leaf size=105

$$\frac{a^2 c^2 \sqrt{cx^2} (a+bx)^{n+1}}{b^3 (n+1)x} - \frac{2ac^2 \sqrt{cx^2} (a+bx)^{n+2}}{b^3 (n+2)x} + \frac{c^2 \sqrt{cx^2} (a+bx)^{n+3}}{b^3 (n+3)x}$$

[Out] $a^2 c^2 (b^3 x^3 + a^3) (a+bx)^{n+1} (cx^2)^{5/2} / (b^3 (n+1)x^3) - 2ac^2 (b^3 x^3 + a^3) (a+bx)^{n+2} (cx^2)^{5/2} / (b^3 (n+2)x^3) + c^2 (b^3 x^3 + a^3) (a+bx)^{n+3} (cx^2)^{5/2} / (b^3 (n+3)x^3)$

Rubi [A] time = 0.03, antiderivative size = 105, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2 c^2 \sqrt{cx^2} (a+bx)^{n+1}}{b^3 (n+1)x} - \frac{2ac^2 \sqrt{cx^2} (a+bx)^{n+2}}{b^3 (n+2)x} + \frac{c^2 \sqrt{cx^2} (a+bx)^{n+3}}{b^3 (n+3)x}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^n)/x^3, x]

[Out] $(a^2 c^2 \sqrt{cx^2} (a+bx)^{n+1}) / (b^3 (n+1)x) - (2ac^2 \sqrt{cx^2} (a+bx)^{n+2}) / (b^3 (n+2)x) + (c^2 \sqrt{cx^2} (a+bx)^{n+3}) / (b^3 (n+3)x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)^n}{x^3} dx &= \frac{(c^2\sqrt{cx^2}) \int x^2(a+bx)^n dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int \left(\frac{a^2(a+bx)^n}{b^2} - \frac{2a(a+bx)^{1+n}}{b^2} + \frac{(a+bx)^{2+n}}{b^2} \right) dx}{x} \\ &= \frac{a^2c^2\sqrt{cx^2} (a+bx)^{1+n}}{b^3(1+n)x} - \frac{2ac^2\sqrt{cx^2} (a+bx)^{2+n}}{b^3(2+n)x} + \frac{c^2\sqrt{cx^2} (a+bx)^{3+n}}{b^3(3+n)x} \end{aligned}$$

Mathematica [A] time = 0.05, size = 70, normalized size = 0.67

$$\frac{c^3x(a+bx)^{n+1} (2a^2 - 2ab(n+1)x + b^2(n^2 + 3n + 2)x^2)}{b^3(n+1)(n+2)(n+3)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^n)/x^3,x]

[Out] (c^3*x*(a + b*x)^(1 + n)*(2*a^2 - 2*a*b*(1 + n)*x + b^2*(2 + 3*n + n^2)*x^2))/(b^3*(1 + n)*(2 + n)*(3 + n)*Sqrt[c*x^2])

fricas [A] time = 0.46, size = 127, normalized size = 1.21

$$\frac{(2a^2bc^2nx - 2a^3c^2 - (b^3c^2n^2 + 3b^3c^2n + 2b^3c^2)x^3 - (ab^2c^2n^2 + ab^2c^2n)x^2)\sqrt{cx^2}(bx+a)^n}{(b^3n^3 + 6b^3n^2 + 11b^3n + 6b^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^3,x, algorithm="fricas")

[Out] -(2*a^2*b*c^2*n*x - 2*a^3*c^2 - (b^3*c^2*n^2 + 3*b^3*c^2*n + 2*b^3*c^2)*x^3 - (a*b^2*c^2*n^2 + a*b^2*c^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^3*n^3 + 6*b^3*n^2 + 11*b^3*n + 6*b^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (bx+a)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^3,x, algorithm="giac")

[Out] integrate((c*x^2)^(5/2)*(b*x + a)^n/x^3, x)

maple [A] time = 0.01, size = 83, normalized size = 0.79

$$\frac{(b^2 n^2 x^2 + 3b^2 n x^2 - 2abnx + 2b^2 x^2 - 2abx + 2a^2)(cx^2)^{\frac{5}{2}}(bx + a)^{n+1}}{(n^3 + 6n^2 + 11n + 6)b^3 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)^n/x^3,x)

[Out] (b*x+a)^(n+1)*(b^2*n^2*x^2+3*b^2*n*x^2-2*a*b*n*x+2*b^2*x^2-2*a*b*x+2*a^2)*(c*x^2)^(5/2)/x^5/b^3/(n^3+6*n^2+11*n+6)

maxima [A] time = 1.36, size = 80, normalized size = 0.76

$$\frac{\left((n^2 + 3n + 2)b^3 c^{\frac{5}{2}} x^3 + (n^2 + n)ab^2 c^{\frac{5}{2}} x^2 - 2a^2 b c^{\frac{5}{2}} n x + 2a^3 c^{\frac{5}{2}}\right)(bx + a)^n}{(n^3 + 6n^2 + 11n + 6)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^3,x, algorithm="maxima")

[Out] ((n^2 + 3*n + 2)*b^3*c^(5/2)*x^3 + (n^2 + n)*a*b^2*c^(5/2)*x^2 - 2*a^2*b*c^(5/2)*n*x + 2*a^3*c^(5/2))*(b*x + a)^n/((n^3 + 6*n^2 + 11*n + 6)*b^3)

mupad [B] time = 0.27, size = 154, normalized size = 1.47

$$\frac{(a + bx)^n \left(\frac{2a^3 c^2 \sqrt{cx^2}}{b^3 (n^3 + 6n^2 + 11n + 6)} + \frac{c^2 x^3 \sqrt{cx^2} (n^2 + 3n + 2)}{n^3 + 6n^2 + 11n + 6} - \frac{2a^2 c^2 n x \sqrt{cx^2}}{b^2 (n^3 + 6n^2 + 11n + 6)} + \frac{a c^2 n x^2 \sqrt{cx^2} (n + 1)}{b (n^3 + 6n^2 + 11n + 6)} \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(5/2)*(a + b*x)^n)/x^3,x)

[Out] ((a + b*x)^n*((2*a^3*c^2*(c*x^2)^(1/2))/(b^3*(11*n + 6*n^2 + n^3 + 6)) + (c^2*x^3*(c*x^2)^(1/2)*(3*n + n^2 + 2))/(11*n + 6*n^2 + n^3 + 6) - (2*a^2*c^2*n*x*(c*x^2)^(1/2))/(b^2*(11*n + 6*n^2 + n^3 + 6)) + (a*c^2*n*x^2*(c*x^2)^(1/2)*(n + 1))/(b*(11*n + 6*n^2 + n^3 + 6))))/x

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}}(a + bx)^n}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((c*x**2)**(5/2)*(b*x+a)**n/x**3,x)
```

```
[Out] Integral((c*x**2)**(5/2)*(a + b*x)**n/x**3, x)
```

$$3.942 \quad \int \frac{(cx^2)^{5/2} (a+bx)^n}{x^4} dx$$

Optimal. Leaf size=69

$$\frac{c^2 \sqrt{cx^2} (a+bx)^{n+2}}{b^2(n+2)x} - \frac{ac^2 \sqrt{cx^2} (a+bx)^{n+1}}{b^2(n+1)x}$$

[Out] $-a*c^2*(b*x+a)^{(1+n)}*(c*x^2)^{(1/2)}/b^2/(1+n)/x+c^2*(b*x+a)^{(2+n)}*(c*x^2)^{(1/2)}/b^2/(2+n)/x$

Rubi [A] time = 0.02, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{c^2 \sqrt{cx^2} (a+bx)^{n+2}}{b^2(n+2)x} - \frac{ac^2 \sqrt{cx^2} (a+bx)^{n+1}}{b^2(n+1)x}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^n)/x^4, x]

[Out] $-((a*c^2*\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)})/(b^2*(1 + n)*x)) + (c^2*\text{Sqrt}[c*x^2]*(a + b*x)^{(2 + n)})/(b^2*(2 + n)*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)^n}{x^4} dx &= \frac{(c^2\sqrt{cx^2}) \int x(a+bx)^n dx}{x} \\ &= \frac{(c^2\sqrt{cx^2}) \int \left(-\frac{a+bx)^n}{b} + \frac{(a+bx)^{1+n}}{b}\right) dx}{x} \\ &= -\frac{ac^2\sqrt{cx^2} (a+bx)^{1+n}}{b^2(1+n)x} + \frac{c^2\sqrt{cx^2} (a+bx)^{2+n}}{b^2(2+n)x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 46, normalized size = 0.67

$$\frac{c^3x(a+bx)^{n+1}(b(n+1)x-a)}{b^2(n+1)(n+2)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^n)/x^4,x]

[Out] (c^3*x*(a + b*x)^(1 + n)*(-a + b*(1 + n)*x))/(b^2*(1 + n)*(2 + n)*Sqrt[c*x^2])

fricas [A] time = 0.47, size = 76, normalized size = 1.10

$$\frac{(abc^2nx - a^2c^2 + (b^2c^2n + b^2c^2)x^2)\sqrt{cx^2}(bx + a)^n}{(b^2n^2 + 3b^2n + 2b^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^4,x, algorithm="fricas")

[Out] (a*b*c^2*n*x - a^2*c^2 + (b^2*c^2*n + b^2*c^2)*x^2)*sqrt(c*x^2)*(b*x + a)^n / ((b^2*n^2 + 3*b^2*n + 2*b^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (bx+a)^n}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^4,x, algorithm="giac")

[Out] integrate((c*x^2)^(5/2)*(b*x + a)^n/x^4, x)

maple [A] time = 0.00, size = 46, normalized size = 0.67

$$\frac{(cx^2)^{\frac{5}{2}}(-xnb - bx + a)(bx + a)^{n+1}}{(n^2 + 3n + 2)b^2x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)^n/x^4,x)

[Out] -(b*x+a)^(n+1)*(c*x^2)^(5/2)*(-b*n*x-b*x+a)/x^5/b^2/(n^2+3*n+2)

maxima [A] time = 1.45, size = 51, normalized size = 0.74

$$\frac{(b^2c^{\frac{5}{2}}(n+1)x^2 + abc^{\frac{5}{2}}nx - a^2c^{\frac{5}{2}})(bx + a)^n}{(n^2 + 3n + 2)b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^4,x, algorithm="maxima")

[Out] (b^2*c^(5/2)*(n + 1)*x^2 + a*b*c^(5/2)*n*x - a^2*c^(5/2))*(b*x + a)^n/((n^2 + 3*n + 2)*b^2)

mupad [B] time = 0.24, size = 94, normalized size = 1.36

$$\frac{(a + bx)^n \left(\frac{c^2 x^2 \sqrt{cx^2} (n+1)}{n^2+3n+2} - \frac{a^2 c^2 \sqrt{cx^2}}{b^2 (n^2+3n+2)} + \frac{a c^2 n x \sqrt{cx^2}}{b (n^2+3n+2)} \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(5/2)*(a + b*x)^n)/x^4,x)

[Out] ((a + b*x)^n*((c^2*x^2*(c*x^2)^(1/2)*(n + 1))/(3*n + n^2 + 2) - (a^2*c^2*(c*x^2)^(1/2))/(b^2*(3*n + n^2 + 2)) + (a*c^2*n*x*(c*x^2)^(1/2))/(b*(3*n + n^2 + 2)))/x

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{a^n c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}}{2x^3} & \text{for } b = 0 \\ \int \frac{(cx^2)^{\frac{5}{2}}}{x^4(a+bx)^2} dx & \text{for } n = -2 \\ \int \frac{(cx^2)^{\frac{5}{2}}}{x^4(a+bx)} dx & \text{for } n = -1 \\ -\frac{a^2 c^{\frac{5}{2}} (a+bx)^n (x^2)^{\frac{5}{2}}}{b^2 n^2 x^5 + 3b^2 n x^5 + 2b^2 x^5} + \frac{abc^{\frac{5}{2}} n x (a+bx)^n (x^2)^{\frac{5}{2}}}{b^2 n^2 x^5 + 3b^2 n x^5 + 2b^2 x^5} + \frac{b^2 c^{\frac{5}{2}} n x^2 (a+bx)^n (x^2)^{\frac{5}{2}}}{b^2 n^2 x^5 + 3b^2 n x^5 + 2b^2 x^5} + \frac{b^2 c^{\frac{5}{2}} x^2 (a+bx)^n (x^2)^{\frac{5}{2}}}{b^2 n^2 x^5 + 3b^2 n x^5 + 2b^2 x^5} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a)**n/x**4,x)

[Out] Piecewise((a**n*c**(5/2)*(x**2)**(5/2)/(2*x**3), Eq(b, 0)), (Integral((c*x**2)**(5/2)/(x**4*(a + b*x)**2), x), Eq(n, -2)), (Integral((c*x**2)**(5/2)/(x**4*(a + b*x)), x), Eq(n, -1)), (-a**2*c**(5/2)*(a + b*x)**n*(x**2)**(5/2)/(b**2*n**2*x**5 + 3*b**2*n*x**5 + 2*b**2*x**5) + a*b*c**(5/2)*n*x*(a + b*x)**n*(x**2)**(5/2)/(b**2*n**2*x**5 + 3*b**2*n*x**5 + 2*b**2*x**5) + b**2*c*(5/2)*n*x**2*(a + b*x)**n*(x**2)**(5/2)/(b**2*n**2*x**5 + 3*b**2*n*x**5 + 2*b**2*x**5) + b**2*c**(5/2)*x**2*(a + b*x)**n*(x**2)**(5/2)/(b**2*n**2*x**5 + 3*b**2*n*x**5 + 2*b**2*x**5), True))

$$3.943 \quad \int \frac{(cx^2)^{5/2} (a+bx)^n}{x^5} dx$$

Optimal. Leaf size=33

$$\frac{c^2 \sqrt{cx^2} (a+bx)^{n+1}}{b(n+1)x}$$

[Out] $c^2*(b*x+a)^{(1+n)}*(c*x^2)^{(1/2)}/b/(1+n)/x$

Rubi [A] time = 0.01, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$\frac{c^2 \sqrt{cx^2} (a+bx)^{n+1}}{b(n+1)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(5/2)}*(a + b*x)^n/x^5, x]$

[Out] $(c^2*\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)})/(b*(1 + n)*x)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}/(b*(m + 1)), x] /;$ FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^{5/2} (a+bx)^n}{x^5} dx &= \frac{(c^2 \sqrt{cx^2}) \int (a+bx)^n dx}{x} \\ &= \frac{c^2 \sqrt{cx^2} (a+bx)^{1+n}}{b(1+n)x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 31, normalized size = 0.94

$$\frac{c^3 x (a+bx)^{n+1}}{b(n+1) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^n)/x^5,x]

[Out] (c^3*x*(a + b*x)^(1 + n))/(b*(1 + n)*Sqrt[c*x^2])

fricas [A] time = 0.48, size = 37, normalized size = 1.12

$$\frac{(bc^2x + ac^2)\sqrt{cx^2}(bx + a)^n}{(bn + b)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^5,x, algorithm="fricas")

[Out] (b*c^2*x + a*c^2)*sqrt(c*x^2)*(b*x + a)^n/((b*n + b)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}}(bx + a)^n}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^5,x, algorithm="giac")

[Out] integrate((c*x^2)^(5/2)*(b*x + a)^n/x^5, x)

maple [A] time = 0.00, size = 29, normalized size = 0.88

$$\frac{(cx^2)^{\frac{5}{2}}(bx + a)^{n+1}}{(n + 1)bx^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)^n/x^5,x)

[Out] (b*x+a)^(n+1)/b/(n+1)*(c*x^2)^(5/2)/x^5

maxima [A] time = 1.39, size = 28, normalized size = 0.85

$$\frac{\left(bc^{\frac{5}{2}}x + ac^{\frac{5}{2}}\right)(bx + a)^n}{b(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^5,x, algorithm="maxima")

[Out] (b*c^(5/2)*x + a*c^(5/2))*(b*x + a)^n/(b*(n + 1))

mupad [B] time = 0.23, size = 49, normalized size = 1.48

$$\frac{\left(\frac{c^2 x \sqrt{cx^2}}{n+1} + \frac{ac^2 \sqrt{cx^2}}{b(n+1)}\right) (a + bx)^n}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(5/2)*(a + b*x)^n)/x^5,x)

[Out] (((c^2*x*(c*x^2)^(1/2))/(n + 1) + (a*c^2*(c*x^2)^(1/2))/(b*(n + 1)))*(a + b*x)^n)/x

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}{ax^4} & \text{for } b = 0 \wedge n = -1 \\ \frac{a^n c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}}{x^4} & \text{for } b = 0 \\ \int \frac{(cx^2)^{\frac{5}{2}}}{x^5(a+bx)} dx & \text{for } n = -1 \\ \frac{ac^{\frac{5}{2}}(a+bx)^n(x^2)^{\frac{5}{2}}}{bnx^5+bx^5} + \frac{bc^{\frac{5}{2}}x(a+bx)^n(x^2)^{\frac{5}{2}}}{bnx^5+bx^5} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a)**n/x**5,x)

[Out] Piecewise((c**(5/2)*(x**2)**(5/2)/(a*x**4), Eq(b, 0) & Eq(n, -1)), (a**n*c**
(5/2)(x**2)**(5/2)/x**4, Eq(b, 0)), (Integral((c*x**2)**(5/2)/(x**5*(a +
b*x)), x), Eq(n, -1)), (a*c**(5/2)*(a + b*x)**n*(x**2)**(5/2)/(b*n*x**5 + b
*x**5) + b*c**(5/2)*x*(a + b*x)**n*(x**2)**(5/2)/(b*n*x**5 + b*x**5), True)
)

$$3.944 \quad \int \frac{(cx^2)^{5/2} (a+bx)^n}{x^6} dx$$

Optimal. Leaf size=50

$$\frac{c^2 \sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)x}$$

[Out] $-c^2(b*x+a)^{(1+n)}*\text{hypergeom}([1, 1+n], [2+n], 1+b*x/a)*(c*x^2)^{(1/2)}/a/(1+n)/x$

Rubi [A] time = 0.01, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$\frac{c^2 \sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^{(5/2)}*(a + b*x)^n/x^6, x]$

[Out] $-((c^2*\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)}*\text{Hypergeometric2F1}[1, 1 + n, 2 + n, 1 + (b*x)/a])/(a*(1 + n)*x))$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{!IntegerQ}[m]$

Rule 65

$\text{Int}[(b_.)*(x_)^{(m_)}*((c_) + (d_.)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(c + d*x)^{(n+1)}*\text{Hypergeometric2F1}[-m, n+1, n+2, 1 + (d*x)/c]/(d*(n+1)*(-(d/(b*c)))^m), x] /; \text{FreeQ}\{b, c, d, m, n\}, x] \&\& \text{!IntegerQ}[n] \&\& (\text{IntegerQ}[m] \mid\mid \text{GtQ}[-(d/(b*c)), 0])$

Rubi steps

$$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x^6} dx = \frac{(c^2 \sqrt{cx^2}) \int \frac{(a+bx)^n}{x} dx}{x}$$

$$= -\frac{c^2 \sqrt{cx^2} (a+bx)^{1+n} {}_2F_1\left(1, 1+n; 2+n; 1+\frac{bx}{a}\right)}{a(1+n)x}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 0.94

$$\frac{(cx^2)^{5/2} (a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a}+1\right)}{a(n+1)x^5}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^n)/x^6,x]

[Out] -(((c*x^2)^(5/2)*(a + b*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, 1 + (b*x)/a]))/(a*(1 + n)*x^5)

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx+a)^n c^2}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^6,x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n*c^2/x^2, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{5/2} (bx+a)^n}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^6,x, algorithm="giac")

[Out] integrate((c*x^2)^(5/2)*(b*x + a)^n/x^6, x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (bx+a)^n}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)^n/x^6,x)

[Out] int((c*x^2)^(5/2)*(b*x+a)^n/x^6,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (bx+a)^n}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^6,x, algorithm="maxima")

[Out] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^6, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(5/2)*(a+b*x)^n)/x^6,x)

[Out] int(((c*x^2)^(5/2)*(a+b*x)^n)/x^6, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (a+bx)^n}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a)**n/x**6,x)

[Out] Integral((c*x**2)**(5/2)*(a+b*x)**n/x**6, x)

$$3.945 \quad \int \frac{(cx^2)^{5/2} (a+bx)^n}{x^7} dx$$

Optimal. Leaf size=50

$$\frac{bc^2\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)x}$$

[Out] $b*c^2*(b*x+a)^{(1+n)}*hypergeom([2, 1+n], [2+n], 1+b*x/a)*(c*x^2)^{(1/2)}/a^2/(1+n)/x$

Rubi [A] time = 0.01, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$\frac{bc^2\sqrt{cx^2} (a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)x}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^(5/2)*(a + b*x)^n)/x^7, x]

[Out] $(b*c^2*\text{Sqrt}[c*x^2]*(a + b*x)^{(1 + n)}*\text{Hypergeometric2F1}[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n)*x)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x^7} dx = \frac{(c^2 \sqrt{cx^2}) \int \frac{(a+bx)^n}{x^2} dx}{x}$$

$$= \frac{bc^2 \sqrt{cx^2} (a+bx)^{1+n} {}_2F_1\left(2, 1+n; 2+n; 1 + \frac{bx}{a}\right)}{a^2(1+n)x}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 0.94

$$\frac{b (cx^2)^{5/2} (a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)x^5}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^(5/2)*(a + b*x)^n)/x^7,x]

[Out] (b*(c*x^2)^(5/2)*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n)*x^5)

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx+a)^n c^2}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^7,x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n*c^2/x^3, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (bx+a)^n}{x^7} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^7,x, algorithm="giac")

[Out] integrate((c*x^2)^(5/2)*(b*x + a)^n/x^7, x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (bx+a)^n}{x^7} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^(5/2)*(b*x+a)^n/x^7,x)

[Out] int((c*x^2)^(5/2)*(b*x+a)^n/x^7,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (bx+a)^n}{x^7} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^7,x, algorithm="maxima")

[Out] integrate((c*x^2)^(5/2)*(b*x+a)^n/x^7, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(cx^2)^{5/2} (a+bx)^n}{x^7} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^(5/2)*(a+b*x)^n)/x^7,x)

[Out] int(((c*x^2)^(5/2)*(a+b*x)^n)/x^7, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^{\frac{5}{2}} (a+bx)^n}{x^7} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**(5/2)*(b*x+a)**n/x**7,x)

[Out] Integral((c*x**2)**(5/2)*(a+b*x)**n/x**7, x)

$$3.946 \quad \int \frac{x^4(a+bx)^n}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=123

$$-\frac{a^3x(a+bx)^{n+1}}{b^4(n+1)\sqrt{cx^2}} + \frac{3a^2x(a+bx)^{n+2}}{b^4(n+2)\sqrt{cx^2}} - \frac{3ax(a+bx)^{n+3}}{b^4(n+3)\sqrt{cx^2}} + \frac{x(a+bx)^{n+4}}{b^4(n+4)\sqrt{cx^2}}$$

[Out] $-a^3x*(b*x+a)^{(1+n)}/b^4/(1+n)/(c*x^2)^{(1/2)}+3*a^2*x*(b*x+a)^{(2+n)}/b^4/(2+n)/(c*x^2)^{(1/2)}-3*a*x*(b*x+a)^{(3+n)}/b^4/(3+n)/(c*x^2)^{(1/2)}+x*(b*x+a)^{(4+n)}/b^4/(4+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 123, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^3x(a+bx)^{n+1}}{b^4(n+1)\sqrt{cx^2}} + \frac{3a^2x(a+bx)^{n+2}}{b^4(n+2)\sqrt{cx^2}} - \frac{3ax(a+bx)^{n+3}}{b^4(n+3)\sqrt{cx^2}} + \frac{x(a+bx)^{n+4}}{b^4(n+4)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^4*(a + b*x)^n)/Sqrt[c*x^2], x]

[Out] $-((a^3*x*(a + b*x)^{(1 + n)})/(b^4*(1 + n)*Sqrt[c*x^2])) + (3*a^2*x*(a + b*x)^{(2 + n)})/(b^4*(2 + n)*Sqrt[c*x^2]) - (3*a*x*(a + b*x)^{(3 + n)})/(b^4*(3 + n)*Sqrt[c*x^2]) + (x*(a + b*x)^{(4 + n)})/(b^4*(4 + n)*Sqrt[c*x^2])$

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_)*(x_))^(m_)*((c_.) + (d_)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{x^4(a+bx)^n}{\sqrt{cx^2}} dx = \frac{x \int x^3(a+bx)^n dx}{\sqrt{cx^2}}$$

$$= \frac{x \int \left(-\frac{a^3(a+bx)^n}{b^3} + \frac{3a^2(a+bx)^{1+n}}{b^3} - \frac{3a(a+bx)^{2+n}}{b^3} + \frac{(a+bx)^{3+n}}{b^3} \right) dx}{\sqrt{cx^2}}$$

$$= -\frac{a^3 x(a+bx)^{1+n}}{b^4(1+n)\sqrt{cx^2}} + \frac{3a^2 x(a+bx)^{2+n}}{b^4(2+n)\sqrt{cx^2}} - \frac{3ax(a+bx)^{3+n}}{b^4(3+n)\sqrt{cx^2}} + \frac{x(a+bx)^{4+n}}{b^4(4+n)\sqrt{cx^2}}$$

Mathematica [A] time = 0.04, size = 96, normalized size = 0.78

$$\frac{x(a+bx)^{n+1} \left(-6a^3 + 6a^2b(n+1)x - 3ab^2(n^2+3n+2)x^2 + b^3(n^3+6n^2+11n+6)x^3 \right)}{b^4(n+1)(n+2)(n+3)(n+4)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^4*(a + b*x)^n)/Sqrt[c*x^2], x]

[Out] (x*(a + b*x)^(1 + n)*(-6*a^3 + 6*a^2*b*(1 + n)*x - 3*a*b^2*(2 + 3*n + n^2)*x^2 + b^3*(6 + 11*n + 6*n^2 + n^3)*x^3))/(b^4*(1 + n)*(2 + n)*(3 + n)*(4 + n)*Sqrt[c*x^2])

fricas [A] time = 0.47, size = 158, normalized size = 1.28

$$\frac{(6a^3bnx + (b^4n^3 + 6b^4n^2 + 11b^4n + 6b^4)x^4 - 6a^4 + (ab^3n^3 + 3ab^3n^2 + 2ab^3n)x^3 - 3(a^2b^2n^2 + a^2b^2n)x^2)\sqrt{cx^2}}{(b^4cn^4 + 10b^4cn^3 + 35b^4cn^2 + 50b^4cn + 24b^4c)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^n/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] (6*a^3*b*n*x + (b^4*n^3 + 6*b^4*n^2 + 11*b^4*n + 6*b^4)*x^4 - 6*a^4 + (a*b^3*n^3 + 3*a*b^3*n^2 + 2*a*b^3*n)*x^3 - 3*(a^2*b^2*n^2 + a^2*b^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^4*c*n^4 + 10*b^4*c*n^3 + 35*b^4*c*n^2 + 50*b^4*c*n + 24*b^4*c)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^4}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^n/(c*x^2)^(1/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^4/sqrt(c*x^2), x)

maple [A] time = 0.01, size = 134, normalized size = 1.09

$$\frac{(-b^3n^3x^3 - 6b^3n^2x^3 + 3ab^2n^2x^2 - 11b^3nx^3 + 9ab^2nx^2 - 6b^3x^3 - 6a^2bnx + 6ab^2x^2 - 6a^2bx + 6a^3)x(bx + a)^{n-1}}{\sqrt{cx^2} (n^4 + 10n^3 + 35n^2 + 50n + 24)b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*(b*x+a)^n/(c*x^2)^(1/2),x)

[Out] $-(b*x+a)^{(n+1)}*x*(-b^3*n^3*x^3-6*b^3*n^2*x^3+3*a*b^2*n^2*x^2-11*b^3*n*x^3+9*a*b^2*n*x^2-6*b^3*x^3-6*a^2*b*n*x+6*a*b^2*x^2-6*a^2*b*x+6*a^3)/(c*x^2)^{(1/2)}/b^4/(n^4+10*n^3+35*n^2+50*n+24)$

maxima [A] time = 1.45, size = 104, normalized size = 0.85

$$\frac{((n^3 + 6n^2 + 11n + 6)b^4x^4 + (n^3 + 3n^2 + 2n)ab^3x^3 - 3(n^2 + n)a^2b^2x^2 + 6a^3bnx - 6a^4)(bx + a)^n}{(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^n/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] $((n^3 + 6n^2 + 11n + 6)*b^4*x^4 + (n^3 + 3n^2 + 2n)*a*b^3*x^3 - 3*(n^2 + n)*a^2*b^2*x^2 + 6*a^3*b*n*x - 6*a^4)*(b*x + a)^n/((n^4 + 10n^3 + 35n^2 + 50n + 24)*b^4*\sqrt{c})$

mupad [B] time = 0.37, size = 186, normalized size = 1.51

$$\frac{(a + bx)^n \left(\frac{x^5(n^3+6n^2+11n+6)}{n^4+10n^3+35n^2+50n+24} - \frac{6a^4x}{b^4(n^4+10n^3+35n^2+50n+24)} + \frac{6a^3nx^2}{b^3(n^4+10n^3+35n^2+50n+24)} + \frac{anx^4(n^2+3n+2)}{b(n^4+10n^3+35n^2+50n+24)} - \frac{6a^2n^2x^3}{b^2(n^4+10n^3+35n^2+50n+24)} + \frac{6a^2nx^2}{b^2(n^4+10n^3+35n^2+50n+24)} - \frac{6a^2bx}{b^2(n^4+10n^3+35n^2+50n+24)} + \frac{6a^3}{b^2(n^4+10n^3+35n^2+50n+24)} \right)}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^4*(a + b*x)^n)/(c*x^2)^(1/2),x)

[Out] $((a + b*x)^n*((x^5*(11*n + 6*n^2 + n^3 + 6))/(50*n + 35*n^2 + 10*n^3 + n^4 + 24) - (6*a^4*x)/(b^4*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (6*a^3*n*x^2)/(b^3*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (a*n*x^4*(3*n + n^2 + 2))/(b*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) - (3*a^2*n*x^3*(n + 1))/(b^2*(50*n + 35*n^2 + 10*n^3 + n^4 + 24))))/(c*x^2)^{(1/2)}$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4*(b*x+a)**n/(c*x**2)**(1/2),x)

[Out] Piecewise((a**n*x**5/(4*sqrt(c)*sqrt(x**2)), Eq(b, 0)), (Integral(x**4/(sqrt(c*x**2)*(a + b*x)**4), x), Eq(n, -4)), (Integral(x**4/(sqrt(c*x**2)*(a + b*x)**3), x), Eq(n, -3)), (Integral(x**4/(sqrt(c*x**2)*(a + b*x)**2), x), Eq(n, -2)), (Integral(x**4/(sqrt(c*x**2)*(a + b*x)), x), Eq(n, -1)), (-6*a**4*x*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)) + 6*a**3*b*n*x**2*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)) - 3*a**2*b**2*n**2*x**3*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)) - 3*a**2*b**2*n*x**3*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)) + a*b**3*n**3*x**4*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)) + 3*a*b**3*n**2*x**4*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)) + 2*a*b**3*n*x**4*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)) + b**4*n**3*x**5*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)) + 6*b**4*n**2*x**5*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)) + 11*b**4*n*x**5*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)) + 6*b**4*x**5*(a + b*x)**n/(b**4*sqrt(c)*n**4*sqrt(x**2) + 10*b**4*sqrt(c)*n**3*sqrt(x**2) + 35*b**4*sqrt(c)*n**2*sqrt(x**2) + 50*b**4*sqrt(c)*n*sqrt(x**2) + 24*b**4*sqrt(c)*sqrt(x**2)), True))

$$3.947 \quad \int \frac{x^3(a+bx)^n}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=90

$$\frac{a^2x(a+bx)^{n+1}}{b^3(n+1)\sqrt{cx^2}} - \frac{2ax(a+bx)^{n+2}}{b^3(n+2)\sqrt{cx^2}} + \frac{x(a+bx)^{n+3}}{b^3(n+3)\sqrt{cx^2}}$$

[Out] $a^2*x*(b*x+a)^{(1+n)}/b^3/(1+n)/(c*x^2)^{(1/2)}-2*a*x*(b*x+a)^{(2+n)}/b^3/(2+n)/(c*x^2)^{(1/2)}+x*(b*x+a)^{(3+n)}/b^3/(3+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 90, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2x(a+bx)^{n+1}}{b^3(n+1)\sqrt{cx^2}} - \frac{2ax(a+bx)^{n+2}}{b^3(n+2)\sqrt{cx^2}} + \frac{x(a+bx)^{n+3}}{b^3(n+3)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^3*(a + b*x)^n)/Sqrt[c*x^2], x]

[Out] $(a^2*x*(a + b*x)^{(1 + n)})/(b^3*(1 + n)*\text{Sqrt}[c*x^2]) - (2*a*x*(a + b*x)^{(2 + n)})/(b^3*(2 + n)*\text{Sqrt}[c*x^2]) + (x*(a + b*x)^{(3 + n)})/(b^3*(3 + n)*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^3(a+bx)^n}{\sqrt{cx^2}} dx &= \frac{x \int x^2(a+bx)^n dx}{\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2(a+bx)^n}{b^2} - \frac{2a(a+bx)^{1+n}}{b^2} + \frac{(a+bx)^{2+n}}{b^2} \right) dx}{\sqrt{cx^2}} \\ &= \frac{a^2 x(a+bx)^{1+n}}{b^3(1+n)\sqrt{cx^2}} - \frac{2ax(a+bx)^{2+n}}{b^3(2+n)\sqrt{cx^2}} + \frac{x(a+bx)^{3+n}}{b^3(3+n)\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 67, normalized size = 0.74

$$\frac{x(a+bx)^{n+1} \left(2a^2 - 2ab(n+1)x + b^2(n^2 + 3n + 2)x^2 \right)}{b^3(n+1)(n+2)(n+3)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*(a + b*x)^n)/Sqrt[c*x^2], x]

[Out] (x*(a + b*x)^(1 + n)*(2*a^2 - 2*a*b*(1 + n)*x + b^2*(2 + 3*n + n^2)*x^2))/(b^3*(1 + n)*(2 + n)*(3 + n)*Sqrt[c*x^2])

fricas [A] time = 0.43, size = 110, normalized size = 1.22

$$\frac{(2a^2bnx - (b^3n^2 + 3b^3n + 2b^3)x^3 - 2a^3 - (ab^2n^2 + ab^2n)x^2)\sqrt{cx^2}(bx+a)^n}{(b^3cn^3 + 6b^3cn^2 + 11b^3cn + 6b^3c)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] -(2*a^2*b*n*x - (b^3*n^2 + 3*b^3*n + 2*b^3)*x^3 - 2*a^3 - (a*b^2*n^2 + a*b^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^3*c*n^3 + 6*b^3*c*n^2 + 11*b^3*c*n + 6*b^3*c)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^3}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n/(c*x^2)^(1/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^3/sqrt(c*x^2), x)

maple [A] time = 0.00, size = 81, normalized size = 0.90

$$\frac{(b^2n^2x^2 + 3b^2nx^2 - 2abnx + 2b^2x^2 - 2abx + 2a^2)x(bx + a)^{n+1}}{\sqrt{cx^2}(n^3 + 6n^2 + 11n + 6)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^n/(c*x^2)^(1/2), x)

[Out] (b*x+a)^(n+1)*(b^2*n^2*x^2+3*b^2*n*x^2-2*a*b*n*x+2*b^2*x^2-2*a*b*x+2*a^2)*x/(c*x^2)^(1/2)/b^3/(n^3+6*n^2+11*n+6)

maxima [A] time = 1.46, size = 83, normalized size = 0.92

$$\frac{((n^2 + 3n + 2)b^3\sqrt{c}x^3 + (n^2 + n)ab^2\sqrt{c}x^2 - 2a^2b\sqrt{c}nx + 2a^3\sqrt{c})(bx + a)^n}{(n^3 + 6n^2 + 11n + 6)b^3c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n/(c*x^2)^(1/2), x, algorithm="maxima")

[Out] ((n^2 + 3*n + 2)*b^3*sqrt(c)*x^3 + (n^2 + n)*a*b^2*sqrt(c)*x^2 - 2*a^2*b*sqrt(c)*n*x + 2*a^3*sqrt(c))*(b*x + a)^n/((n^3 + 6*n^2 + 11*n + 6)*b^3*c)

mupad [B] time = 0.29, size = 121, normalized size = 1.34

$$\frac{(a + bx)^n \left(\frac{x^4(n^2+3n+2)}{n^3+6n^2+11n+6} + \frac{2a^3x}{b^3(n^3+6n^2+11n+6)} - \frac{2a^2nx^2}{b^2(n^3+6n^2+11n+6)} + \frac{anx^3(n+1)}{b(n^3+6n^2+11n+6)} \right)}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^3*(a + b*x)^n)/(c*x^2)^(1/2), x)

[Out] ((a + b*x)^n*((x^4*(3*n + n^2 + 2))/(11*n + 6*n^2 + n^3 + 6) + (2*a^3*x)/(b^3*(11*n + 6*n^2 + n^3 + 6)) - (2*a^2*n*x^2)/(b^2*(11*n + 6*n^2 + n^3 + 6)) + (a*n*x^3*(n + 1))/(b*(11*n + 6*n^2 + n^3 + 6))))/(c*x^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{a^n x^4}{3\sqrt{c}\sqrt{x^2}} \\ \int \frac{x^3}{\sqrt{cx^2}(a+bx)^3} dx \\ \int \frac{x^3}{\sqrt{cx^2}(a+bx)^2} dx \\ \int \frac{x^3}{\sqrt{cx^2}(a+bx)} dx \end{array} \right. \frac{2a^3x(a+bx)^n}{b^3\sqrt{c}n^3\sqrt{x^2}+6b^3\sqrt{c}n^2\sqrt{x^2}+11b^3\sqrt{c}n\sqrt{x^2}+6b^3\sqrt{c}\sqrt{x^2}} - \frac{2a^2bnx^2(a+bx)^n}{b^3\sqrt{c}n^3\sqrt{x^2}+6b^3\sqrt{c}n^2\sqrt{x^2}+11b^3\sqrt{c}n\sqrt{x^2}+6b^3\sqrt{c}\sqrt{x^2}} + \frac{ab}{b^3\sqrt{c}n^3\sqrt{x^2}+6b^3\sqrt{c}n^2\sqrt{x^2}+11b^3\sqrt{c}n\sqrt{x^2}+6b^3\sqrt{c}\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**n/(c*x**2)**(1/2), x)

[Out] Piecewise((a**n*x**4/(3*sqrt(c)*sqrt(x**2)), Eq(b, 0)), (Integral(x**3/(sqrt(c*x**2)*(a + b*x)**3), x), Eq(n, -3)), (Integral(x**3/(sqrt(c*x**2)*(a + b*x)**2), x), Eq(n, -2)), (Integral(x**3/(sqrt(c*x**2)*(a + b*x)), x), Eq(n, -1)), (2*a**3*x*(a + b*x)**n/(b**3*sqrt(c)*n**3*sqrt(x**2) + 6*b**3*sqrt(c)*n**2*sqrt(x**2) + 11*b**3*sqrt(c)*n*sqrt(x**2) + 6*b**3*sqrt(c)*sqrt(x**2)) - 2*a**2*b*n*x**2*(a + b*x)**n/(b**3*sqrt(c)*n**3*sqrt(x**2) + 6*b**3*sqrt(c)*n**2*sqrt(x**2) + 11*b**3*sqrt(c)*n*sqrt(x**2) + 6*b**3*sqrt(c)*sqrt(x**2)) + a*b**2*n**2*x**3*(a + b*x)**n/(b**3*sqrt(c)*n**3*sqrt(x**2) + 6*b**3*sqrt(c)*n**2*sqrt(x**2) + 11*b**3*sqrt(c)*n*sqrt(x**2) + 6*b**3*sqrt(c)*sqrt(x**2)) + a*b**2*n*x**3*(a + b*x)**n/(b**3*sqrt(c)*n**3*sqrt(x**2) + 6*b**3*sqrt(c)*n**2*sqrt(x**2) + 11*b**3*sqrt(c)*n*sqrt(x**2) + 6*b**3*sqrt(c)*sqrt(x**2)) + b**3*n**2*x**4*(a + b*x)**n/(b**3*sqrt(c)*n**3*sqrt(x**2) + 6*b**3*sqrt(c)*n**2*sqrt(x**2) + 11*b**3*sqrt(c)*n*sqrt(x**2) + 6*b**3*sqrt(c)*sqrt(x**2)) + 3*b**3*n*x**4*(a + b*x)**n/(b**3*sqrt(c)*n**3*sqrt(x**2) + 6*b**3*sqrt(c)*n**2*sqrt(x**2) + 11*b**3*sqrt(c)*n*sqrt(x**2) + 6*b**3*sqrt(c)*sqrt(x**2)) + 2*b**3*x**4*(a + b*x)**n/(b**3*sqrt(c)*n**3*sqrt(x**2) + 6*b**3*sqrt(c)*n**2*sqrt(x**2) + 11*b**3*sqrt(c)*n*sqrt(x**2) + 6*b**3*sqrt(c)*sqrt(x**2)), True))

$$3.948 \quad \int \frac{x^2(a+bx)^n}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=59

$$\frac{x(a+bx)^{n+2}}{b^2(n+2)\sqrt{cx^2}} - \frac{ax(a+bx)^{n+1}}{b^2(n+1)\sqrt{cx^2}}$$

[Out] $-a*x*(b*x+a)^{(1+n)}/b^2/(1+n)/(c*x^2)^{(1/2)}+x*(b*x+a)^{(2+n)}/b^2/(2+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{x(a+bx)^{n+2}}{b^2(n+2)\sqrt{cx^2}} - \frac{ax(a+bx)^{n+1}}{b^2(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^2*(a + b*x)^n)/Sqrt[c*x^2], x]

[Out] $-((a*x*(a + b*x)^{(1 + n)})/(b^2*(1 + n)*Sqrt[c*x^2])) + (x*(a + b*x)^{(2 + n)})/(b^2*(2 + n)*Sqrt[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{x^2(a+bx)^n}{\sqrt{cx^2}} dx &= \frac{x \int x(a+bx)^n dx}{\sqrt{cx^2}} \\
&= \frac{x \int \left(-\frac{a(a+bx)^n}{b} + \frac{(a+bx)^{1+n}}{b} \right) dx}{\sqrt{cx^2}} \\
&= -\frac{ax(a+bx)^{1+n}}{b^2(1+n)\sqrt{cx^2}} + \frac{x(a+bx)^{2+n}}{b^2(2+n)\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 43, normalized size = 0.73

$$\frac{x(a+bx)^{n+1}(b(n+1)x-a)}{b^2(n+1)(n+2)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*(a + b*x)^n)/Sqrt[c*x^2], x]

[Out] (x*(a + b*x)^(1 + n)*(-a + b*(1 + n)*x))/(b^2*(1 + n)*(2 + n)*Sqrt[c*x^2])

fricas [A] time = 0.43, size = 66, normalized size = 1.12

$$\frac{(abnx + (b^2n + b^2)x^2 - a^2)\sqrt{cx^2}(bx + a)^n}{(b^2cn^2 + 3b^2cn + 2b^2c)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] (a*b*n*x + (b^2*n + b^2)*x^2 - a^2)*sqrt(c*x^2)*(b*x + a)^n/((b^2*c*n^2 + 3*b^2*c*n + 2*b^2*c)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^2}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n/(c*x^2)^(1/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^2/sqrt(c*x^2), x)

maple [A] time = 0.00, size = 44, normalized size = 0.75

$$\frac{(-xnb - bx + a)x(bx + a)^{n+1}}{\sqrt{cx^2}(n^2 + 3n + 2)b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(b*x+a)^n/(c*x^2)^(1/2),x)`

[Out] `-(b*x+a)^(n+1)*x*(-b*n*x-b*x+a)/(c*x^2)^(1/2)/b^2/(n^2+3*n+2)`

maxima [A] time = 1.49, size = 45, normalized size = 0.76

$$\frac{(b^2(n+1)x^2 + abnx - a^2)(bx + a)^n}{(n^2 + 3n + 2)b^2\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(b*x+a)^n/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] `(b^2*(n+1)*x^2 + a*b*n*x - a^2)*(b*x+a)^n/((n^2+3*n+2)*b^2*sqrt(c))`

mupad [B] time = 0.28, size = 71, normalized size = 1.20

$$\frac{(a + bx)^n \left(\frac{x^3(n+1)}{n^2+3n+2} - \frac{a^2x}{b^2(n^2+3n+2)} + \frac{anx^2}{b(n^2+3n+2)} \right)}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x^2*(a+b*x)^n)/(c*x^2)^(1/2),x)`

[Out] `((a+b*x)^n*((x^3*(n+1))/(3*n+n^2+2) - (a^2*x)/(b^2*(3*n+n^2+2)) + (a*n*x^2)/(b*(3*n+n^2+2)))/(c*x^2)^(1/2)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{a^n x^3}{2\sqrt{c}\sqrt{x^2}} \\ \int \frac{x^2}{\sqrt{cx^2}(a+bx)^2} dx \\ \int \frac{x^2}{\sqrt{cx^2}(a+bx)} dx \end{array} \right. - \frac{a^2x(a+bx)^n}{b^2\sqrt{c}n^2\sqrt{x^2}+3b^2\sqrt{c}n\sqrt{x^2}+2b^2\sqrt{c}\sqrt{x^2}} + \frac{abnx^2(a+bx)^n}{b^2\sqrt{c}n^2\sqrt{x^2}+3b^2\sqrt{c}n\sqrt{x^2}+2b^2\sqrt{c}\sqrt{x^2}} + \frac{b^2nx^3(a+bx)^n}{b^2\sqrt{c}n^2\sqrt{x^2}+3b^2\sqrt{c}n\sqrt{x^2}+2b^2\sqrt{c}\sqrt{x^2}} + \frac{a^2x(a+bx)^n}{b^2\sqrt{c}n^2\sqrt{x^2}+3b^2\sqrt{c}n\sqrt{x^2}+2b^2\sqrt{c}\sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*(b*x+a)**n/(c*x**2)**(1/2),x)
```

```
[Out] Piecewise((a**n*x**3/(2*sqrt(c)*sqrt(x**2)), Eq(b, 0)), (Integral(x**2/(sqrt(c*x**2)*(a + b*x)**2), x), Eq(n, -2)), (Integral(x**2/(sqrt(c*x**2)*(a + b*x)), x), Eq(n, -1)), (-a**2*x*(a + b*x)**n/(b**2*sqrt(c)*n**2*sqrt(x**2) + 3*b**2*sqrt(c)*n*sqrt(x**2) + 2*b**2*sqrt(c)*sqrt(x**2)) + a*b*n*x**2*(a + b*x)**n/(b**2*sqrt(c)*n**2*sqrt(x**2) + 3*b**2*sqrt(c)*n*sqrt(x**2) + 2*b**2*sqrt(c)*sqrt(x**2)) + b**2*n*x**3*(a + b*x)**n/(b**2*sqrt(c)*n**2*sqrt(x**2) + 3*b**2*sqrt(c)*n*sqrt(x**2) + 2*b**2*sqrt(c)*sqrt(x**2)) + b**2*x**3*(a + b*x)**n/(b**2*sqrt(c)*n**2*sqrt(x**2) + 3*b**2*sqrt(c)*n*sqrt(x**2) + 2*b**2*sqrt(c)*sqrt(x**2)), True))
```

$$3.949 \quad \int \frac{x(a+bx)^n}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=28

$$\frac{x(a+bx)^{n+1}}{b(n+1)\sqrt{cx^2}}$$

[Out] $x*(b*x+a)^{(1+n)}/b/(1+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 32}

$$\frac{x(a+bx)^{n+1}}{b(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x*(a + b*x)^n)/\text{Sqrt}[c*x^2], x]$

[Out] $(x*(a + b*x)^{(1 + n)})/(b*(1 + n)*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] :> \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{!IntegerQ}[m]$

Rule 32

$\text{Int}[(a_. + (b_.)*(x_)^{(m_)})^{(m_)}, x_Symbol] :> \text{Simp}[(a + b*x)^{(m + 1)}/(b*(m + 1)), x] /; \text{FreeQ}\{a, b, m\}, x] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int \frac{x(a+bx)^n}{\sqrt{cx^2}} dx &= \frac{x \int (a+bx)^n dx}{\sqrt{cx^2}} \\ &= \frac{x(a+bx)^{1+n}}{b(1+n)\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 1.00

$$\frac{x(a+bx)^{n+1}}{b(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x*(a + b*x)^n)/Sqrt[c*x^2], x]

[Out] (x*(a + b*x)^(1 + n))/(b*(1 + n)*Sqrt[c*x^2])

fricas [A] time = 0.44, size = 33, normalized size = 1.18

$$\frac{\sqrt{cx^2}(bx+a)(bx+a)^n}{(bcn+bc)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x + a)*(b*x + a)^n/((b*c*n + b*c)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n/(c*x^2)^(1/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x/sqrt(c*x^2), x)

maple [A] time = 0.00, size = 27, normalized size = 0.96

$$\frac{x(bx+a)^{n+1}}{(n+1)\sqrt{cx^2}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^n/(c*x^2)^(1/2), x)

[Out] x*(b*x+a)^(n+1)/b/(n+1)/(c*x^2)^(1/2)

maxima [A] time = 1.44, size = 31, normalized size = 1.11

$$\frac{(b\sqrt{c}x + a\sqrt{c})(bx+a)^n}{bc(n+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n/(c*x^2)^(1/2), x, algorithm="maxima")

[Out] $(b\sqrt{c}x + a\sqrt{c})(bx + a)^n / (bc(n + 1))$

mupad [B] time = 0.22, size = 36, normalized size = 1.29

$$\frac{\left(\frac{x^2}{n+1} + \frac{ax}{b(n+1)}\right) (a + bx)^n}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x*(a + b*x)^n)/(c*x^2)^(1/2), x)`

[Out] $((x^2/(n + 1) + (a*x)/(b*(n + 1)))*(a + b*x)^n)/(c*x^2)^{(1/2)}$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{x^2}{a\sqrt{c}\sqrt{x^2}} & \text{for } b = 0 \wedge n = -1 \\ \frac{a^n x^2}{\sqrt{c}\sqrt{x^2}} & \text{for } b = 0 \\ \int \frac{x}{\sqrt{cx^2}(a+bx)} dx & \text{for } n = -1 \\ \frac{ax(a+bx)^n}{b\sqrt{cn}\sqrt{x^2} + b\sqrt{c}\sqrt{x^2}} + \frac{bx^2(a+bx)^n}{b\sqrt{cn}\sqrt{x^2} + b\sqrt{c}\sqrt{x^2}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*(b*x+a)**n/(c*x**2)**(1/2), x)`

[Out] `Piecewise((x**2/(a*sqrt(c)*sqrt(x**2)), Eq(b, 0) & Eq(n, -1)), (a**n*x**2/(sqrt(c)*sqrt(x**2)), Eq(b, 0)), (Integral(x/(sqrt(c*x**2)*(a + b*x)), x), Eq(n, -1)), (a*x*(a + b*x)**n/(b*sqrt(c)*n*sqrt(x**2) + b*sqrt(c)*sqrt(x**2)) + b*x**2*(a + b*x)**n/(b*sqrt(c)*n*sqrt(x**2) + b*sqrt(c)*sqrt(x**2)), True))`

$$3.950 \quad \int \frac{(a+bx)^n}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=45

$$-\frac{x(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)\sqrt{cx^2}}$$

[Out] $-x*(b*x+a)^{(1+n)}*\text{hypergeom}([1, 1+n], [2+n], 1+b*x/a)/a/(1+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 65}

$$-\frac{x(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{a(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n/Sqrt[c*x^2], x]

[Out] $-((x*(a + b*x)^{(1 + n)}*\text{Hypergeometric2F1}[1, 1 + n, 2 + n, 1 + (b*x)/a])/(a*(1 + n)*\text{Sqrt}[c*x^2]))$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(a+bx)^n}{\sqrt{cx^2}} dx = \frac{x \int \frac{(a+bx)^n}{x} dx}{\sqrt{cx^2}}$$

$$= -\frac{x(a+bx)^{1+n} {}_2F_1\left(1, 1+n; 2+n; 1+\frac{bx}{a}\right)}{a(1+n)\sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 45, normalized size = 1.00

$$-\frac{x(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a}+1\right)}{a(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/Sqrt[c*x^2], x]

[Out] -((x*(a + b*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, 1 + (b*x)/a])/(a*(1 + n)*Sqrt[c*x^2]))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2}(bx+a)^n}{cx^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c*x^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/(c*x^2)^(1/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n/sqrt(c*x^2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n/(c*x^2)^(1/2), x)

[Out] int((b*x+a)^n/(c*x^2)^(1/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/(c*x^2)^(1/2), x, algorithm="maxima")

[Out] integrate((b*x + a)^n/sqrt(c*x^2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^n}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/(c*x^2)^(1/2), x)

[Out] int((a + b*x)^n/(c*x^2)^(1/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^n}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n/(c*x**2)**(1/2), x)

[Out] Integral((a + b*x)**n/sqrt(c*x**2), x)

$$3.951 \quad \int \frac{(a+bx)^n}{x\sqrt{cx^2}} dx$$

Optimal. Leaf size=45

$$\frac{bx(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)\sqrt{cx^2}}$$

[Out] b*x*(b*x+a)^(1+n)*hypergeom([2, 1+n], [2+n], 1+b*x/a)/a^2/(1+n)/(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$\frac{bx(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n/(x*Sqrt[c*x^2]), x]

[Out] (b*x*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n)*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_)^(m_))*((c_) + (d_.)*(x_)^(n_)), x_Symbol] := Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(a+bx)^n}{x\sqrt{cx^2}} dx = \frac{x \int \frac{(a+bx)^n}{x^2} dx}{\sqrt{cx^2}}$$

$$= \frac{bx(a+bx)^{1+n} {}_2F_1\left(2, 1+n; 2+n; 1+\frac{bx}{a}\right)}{a^2(1+n)\sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 48, normalized size = 1.07

$$\frac{bcx^3(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a}+1\right)}{a^2(n+1)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/(x*sqrt[c*x^2]), x]

[Out] (b*c*x^3*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a]) / (a^2*(1 + n)*(c*x^2)^(3/2))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2}(bx+a)^n}{cx^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c*x^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n}{\sqrt{cx^2}x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x/(c*x^2)^(1/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n/(sqrt(c*x^2)*x), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{\sqrt{cx^2} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n/x/(c*x^2)^(1/2), x)

[Out] int((b*x+a)^n/x/(c*x^2)^(1/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{\sqrt{cx^2} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x/(c*x^2)^(1/2), x, algorithm="maxima")

[Out] integrate((b*x + a)^n/(sqrt(c*x^2)*x), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^n}{x \sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/(x*(c*x^2)^(1/2)), x)

[Out] int((a + b*x)^n/(x*(c*x^2)^(1/2)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^n}{x \sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n/x/(c*x**2)**(1/2), x)

[Out] Integral((a + b*x)**n/(x*sqrt(c*x**2)), x)

$$3.952 \quad \int \frac{(a+bx)^n}{x^2 \sqrt{cx^2}} dx$$

Optimal. Leaf size=48

$$-\frac{b^2 x (a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3 (n+1) \sqrt{cx^2}}$$

[Out] $-b^2 x (a+bx)^{n+1} \text{hypergeom}([3, 1+n], [2+n], 1+b*x/a) / a^3 / (1+n) / (c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$-\frac{b^2 x (a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3 (n+1) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^n / (x^2 * \text{Sqrt}[c*x^2]), x]$

[Out] $-((b^2*x*(a + b*x)^{(1 + n)} * \text{Hypergeometric2F1}[3, 1 + n, 2 + n, 1 + (b*x)/a]) / (a^3*(1 + n)*\text{Sqrt}[c*x^2]))$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

$\text{Int}[(b_.)*(x_)^{(m_)}*((c_) + (d_.)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(c + d*x)^{(n + 1)} * \text{Hypergeometric2F1}[-m, n + 1, n + 2, 1 + (d*x)/c] / (d*(n + 1)*(-(d/(b*c)))^m), x] /;$ FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(a+bx)^n}{x^2\sqrt{cx^2}} dx = \frac{x \int \frac{(a+bx)^n}{x^3} dx}{\sqrt{cx^2}}$$

$$= -\frac{b^2x(a+bx)^{1+n} {}_2F_1\left(3, 1+n; 2+n; 1+\frac{bx}{a}\right)}{a^3(1+n)\sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 51, normalized size = 1.06

$$-\frac{b^2cx^3(a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a}+1\right)}{a^3(n+1)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/(x^2*Sqrt[c*x^2]),x]

[Out] -((b^2*c*x^3*(a + b*x)^(1 + n)*Hypergeometric2F1[3, 1 + n, 2 + n, 1 + (b*x)/a])/(a^3*(1 + n)*(c*x^2)^(3/2)))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2}(bx+a)^n}{cx^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^2/(c*x^2)^(1/2),x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c*x^4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n}{\sqrt{cx^2}x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n/(sqrt(c*x^2)*x^2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{\sqrt{cx^2} x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n/x^2/(c*x^2)^(1/2), x)

[Out] int((b*x+a)^n/x^2/(c*x^2)^(1/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{\sqrt{cx^2} x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x^2/(c*x^2)^(1/2), x, algorithm="maxima")

[Out] integrate((b*x + a)^n/(sqrt(c*x^2)*x^2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^n}{x^2 \sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/(x^2*(c*x^2)^(1/2)), x)

[Out] int((a + b*x)^n/(x^2*(c*x^2)^(1/2)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^n}{x^2 \sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n/x**2/(c*x**2)**(1/2), x)

[Out] Integral((a + b*x)**n/(x**2*sqrt(c*x**2)), x)

$$3.953 \quad \int \frac{x^6(a+bx)^n}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=135

$$-\frac{a^3x(a+bx)^{n+1}}{b^4c(n+1)\sqrt{cx^2}} + \frac{3a^2x(a+bx)^{n+2}}{b^4c(n+2)\sqrt{cx^2}} - \frac{3ax(a+bx)^{n+3}}{b^4c(n+3)\sqrt{cx^2}} + \frac{x(a+bx)^{n+4}}{b^4c(n+4)\sqrt{cx^2}}$$

[Out] $-a^3x(bx+a)^{(1+n)}/b^4/c/(1+n)/(cx^2)^{(1/2)}+3a^2x(bx+a)^{(2+n)}/b^4/c/(2+n)/(cx^2)^{(1/2)}-3ax(bx+a)^{(3+n)}/b^4/c/(3+n)/(cx^2)^{(1/2)}+x(bx+a)^{(4+n)}/b^4/c/(4+n)/(cx^2)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 135, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^3x(a+bx)^{n+1}}{b^4c(n+1)\sqrt{cx^2}} + \frac{3a^2x(a+bx)^{n+2}}{b^4c(n+2)\sqrt{cx^2}} - \frac{3ax(a+bx)^{n+3}}{b^4c(n+3)\sqrt{cx^2}} + \frac{x(a+bx)^{n+4}}{b^4c(n+4)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^6*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] $-((a^3x*(a + b*x)^{(1 + n)})/(b^4*c*(1 + n)*\text{Sqrt}[c*x^2])) + (3*a^2*x*(a + b*x)^{(2 + n)})/(b^4*c*(2 + n)*\text{Sqrt}[c*x^2]) - (3*a*x*(a + b*x)^{(3 + n)})/(b^4*c*(3 + n)*\text{Sqrt}[c*x^2]) + (x*(a + b*x)^{(4 + n)})/(b^4*c*(4 + n)*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{x^6(a+bx)^n}{(cx^2)^{3/2}} dx = \frac{x \int x^3(a+bx)^n dx}{c\sqrt{cx^2}}$$

$$= \frac{x \int \left(-\frac{a^3(a+bx)^n}{b^3} + \frac{3a^2(a+bx)^{1+n}}{b^3} - \frac{3a(a+bx)^{2+n}}{b^3} + \frac{(a+bx)^{3+n}}{b^3} \right) dx}{c\sqrt{cx^2}}$$

$$= -\frac{a^3x(a+bx)^{1+n}}{b^4c(1+n)\sqrt{cx^2}} + \frac{3a^2x(a+bx)^{2+n}}{b^4c(2+n)\sqrt{cx^2}} - \frac{3ax(a+bx)^{3+n}}{b^4c(3+n)\sqrt{cx^2}} + \frac{x(a+bx)^{4+n}}{b^4c(4+n)\sqrt{cx^2}}$$

Mathematica [A] time = 0.04, size = 98, normalized size = 0.73

$$\frac{x^3(a+bx)^{n+1} \left(-6a^3 + 6a^2b(n+1)x - 3ab^2(n^2+3n+2)x^2 + b^3(n^3+6n^2+11n+6)x^3 \right)}{b^4(n+1)(n+2)(n+3)(n+4)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^6*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] (x^3*(a + b*x)^(1 + n)*(-6*a^3 + 6*a^2*b*(1 + n)*x - 3*a*b^2*(2 + 3*n + n^2)*x^2 + b^3*(6 + 11*n + 6*n^2 + n^3)*x^3))/(b^4*(1 + n)*(2 + n)*(3 + n)*(4 + n)*(c*x^2)^(3/2))

fricas [A] time = 0.42, size = 168, normalized size = 1.24

$$\frac{(6a^3bnx + (b^4n^3 + 6b^4n^2 + 11b^4n + 6b^4)x^4 - 6a^4 + (ab^3n^3 + 3ab^3n^2 + 2ab^3n)x^3 - 3(a^2b^2n^2 + a^2b^2n)x^2)\sqrt{c}}{(b^4c^2n^4 + 10b^4c^2n^3 + 35b^4c^2n^2 + 50b^4c^2n + 24b^4c^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] (6*a^3*b*n*x + (b^4*n^3 + 6*b^4*n^2 + 11*b^4*n + 6*b^4)*x^4 - 6*a^4 + (a*b^3*n^3 + 3*a*b^3*n^2 + 2*a*b^3*n)*x^3 - 3*(a^2*b^2*n^2 + a^2*b^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^4*c^2*n^4 + 10*b^4*c^2*n^3 + 35*b^4*c^2*n^2 + 50*b^4*c^2*n + 24*b^4*c^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^6}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^n/(c*x^2)^(3/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^6/(c*x^2)^(3/2), x)

maple [A] time = 0.01, size = 136, normalized size = 1.01

$$\frac{(-b^3n^3x^3 - 6b^3n^2x^3 + 3ab^2n^2x^2 - 11b^3nx^3 + 9ab^2nx^2 - 6b^3x^3 - 6a^2bnx + 6ab^2x^2 - 6a^2bx + 6a^3)x^3(bx + a)^n}{(cx^2)^{\frac{3}{2}}(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6*(b*x+a)^n/(c*x^2)^(3/2),x)

[Out] -(b*x+a)^(n+1)*x^3*(-b^3*n^3*x^3-6*b^3*n^2*x^3+3*a*b^2*n^2*x^2-11*b^3*n*x^3+9*a*b^2*n*x^2-6*b^3*x^3-6*a^2*b*n*x+6*a*b^2*x^2-6*a^2*b*x+6*a^3)/(c*x^2)^(3/2)/b^4/(n^4+10*n^3+35*n^2+50*n+24)

maxima [A] time = 1.46, size = 104, normalized size = 0.77

$$\frac{((n^3 + 6n^2 + 11n + 6)b^4x^4 + (n^3 + 3n^2 + 2n)ab^3x^3 - 3(n^2 + n)a^2b^2x^2 + 6a^3bnx - 6a^4)(bx + a)^n}{(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^n/(c*x^2)^(3/2),x, algorithm="maxima")

[Out] ((n^3 + 6*n^2 + 11*n + 6)*b^4*x^4 + (n^3 + 3*n^2 + 2*n)*a*b^3*x^3 - 3*(n^2 + n)*a^2*b^2*x^2 + 6*a^3*b*n*x - 6*a^4)*(b*x + a)^n/((n^4 + 10*n^3 + 35*n^2 + 50*n + 24)*b^4*c^(3/2))

mupad [B] time = 0.40, size = 201, normalized size = 1.49

$$(a + bx)^n \left(\frac{x^5(n^3+6n^2+11n+6)}{c(n^4+10n^3+35n^2+50n+24)} - \frac{6a^4x}{b^4c(n^4+10n^3+35n^2+50n+24)} + \frac{6a^3nx^2}{b^3c(n^4+10n^3+35n^2+50n+24)} + \frac{anx^4(n^2+3n+2)}{bc(n^4+10n^3+35n^2+50n+24)} \right) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^6*(a + b*x)^n)/(c*x^2)^(3/2),x)

[Out] ((a + b*x)^n*((x^5*(11*n + 6*n^2 + n^3 + 6))/(c*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) - (6*a^4*x)/(b^4*c*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (6*a^3*n*x^2)/(b^3*c*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (a*n*x^4*(3*n + n^2 +

/2) + 50*b**4*c**(3/2)*n*(x**2)**(3/2) + 24*b**4*c**(3/2)*(x**2)**(3/2)), True))

$$3.954 \quad \int \frac{x^5(a+bx)^n}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=99

$$\frac{a^2x(a+bx)^{n+1}}{b^3c(n+1)\sqrt{cx^2}} - \frac{2ax(a+bx)^{n+2}}{b^3c(n+2)\sqrt{cx^2}} + \frac{x(a+bx)^{n+3}}{b^3c(n+3)\sqrt{cx^2}}$$

[Out] $a^2x*(b*x+a)^{(1+n)}/b^3/c/(1+n)/(c*x^2)^{(1/2)}-2*a*x*(b*x+a)^{(2+n)}/b^3/c/(2+n)/(c*x^2)^{(1/2)}+x*(b*x+a)^{(3+n)}/b^3/c/(3+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 99, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2x(a+bx)^{n+1}}{b^3c(n+1)\sqrt{cx^2}} - \frac{2ax(a+bx)^{n+2}}{b^3c(n+2)\sqrt{cx^2}} + \frac{x(a+bx)^{n+3}}{b^3c(n+3)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^5*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] $(a^2*x*(a + b*x)^{(1 + n)})/(b^3*c*(1 + n)*\text{Sqrt}[c*x^2]) - (2*a*x*(a + b*x)^{(2 + n)})/(b^3*c*(2 + n)*\text{Sqrt}[c*x^2]) + (x*(a + b*x)^{(3 + n)})/(b^3*c*(3 + n)*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^5(a+bx)^n}{(cx^2)^{3/2}} dx &= \frac{x \int x^2(a+bx)^n dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2(a+bx)^n}{b^2} - \frac{2a(a+bx)^{1+n}}{b^2} + \frac{(a+bx)^{2+n}}{b^2} \right) dx}{c\sqrt{cx^2}} \\ &= \frac{a^2x(a+bx)^{1+n}}{b^3c(1+n)\sqrt{cx^2}} - \frac{2ax(a+bx)^{2+n}}{b^3c(2+n)\sqrt{cx^2}} + \frac{x(a+bx)^{3+n}}{b^3c(3+n)\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 69, normalized size = 0.70

$$\frac{x^3(a+bx)^{n+1} \left(2a^2 - 2ab(n+1)x + b^2(n^2 + 3n + 2)x^2 \right)}{b^3(n+1)(n+2)(n+3)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^5*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] (x^3*(a + b*x)^(1 + n)*(2*a^2 - 2*a*b*(1 + n)*x + b^2*(2 + 3*n + n^2)*x^2)) / (b^3*(1 + n)*(2 + n)*(3 + n)*(c*x^2)^(3/2))

fricas [A] time = 0.44, size = 118, normalized size = 1.19

$$\frac{(2a^2bnx - (b^3n^2 + 3b^3n + 2b^3)x^3 - 2a^3 - (ab^2n^2 + ab^2n)x^2)\sqrt{cx^2}(bx+a)^n}{(b^3c^2n^3 + 6b^3c^2n^2 + 11b^3c^2n + 6b^3c^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] -(2*a^2*b*n*x - (b^3*n^2 + 3*b^3*n + 2*b^3)*x^3 - 2*a^3 - (a*b^2*n^2 + a*b^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^3*c^2*n^3 + 6*b^3*c^2*n^2 + 11*b^3*c^2*n + 6*b^3*c^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^5}{(cx^2)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^n/(c*x^2)^(3/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^5/(c*x^2)^(3/2), x)

maple [A] time = 0.00, size = 83, normalized size = 0.84

$$\frac{(b^2 n^2 x^2 + 3 b^2 n x^2 - 2 a b n x + 2 b^2 x^2 - 2 a b x + 2 a^2) x^3 (b x + a)^{n+1}}{(c x^2)^{\frac{3}{2}} (n^3 + 6 n^2 + 11 n + 6) b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5*(b*x+a)^n/(c*x^2)^(3/2),x)

[Out] (b*x+a)^(n+1)*(b^2*n^2*x^2+3*b^2*n*x^2-2*a*b*n*x+2*b^2*x^2-2*a*b*x+2*a^2)*x^3/(c*x^2)^(3/2)/b^3/(n^3+6*n^2+11*n+6)

maxima [A] time = 1.46, size = 83, normalized size = 0.84

$$\frac{\left((n^2 + 3n + 2)b^3\sqrt{c}x^3 + (n^2 + n)ab^2\sqrt{c}x^2 - 2a^2b\sqrt{c}nx + 2a^3\sqrt{c}\right)(bx + a)^n}{(n^3 + 6n^2 + 11n + 6)b^3c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^n/(c*x^2)^(3/2),x, algorithm="maxima")

[Out] ((n^2 + 3*n + 2)*b^3*sqrt(c)*x^3 + (n^2 + n)*a*b^2*sqrt(c)*x^2 - 2*a^2*b*sqrt(c)*n*x + 2*a^3*sqrt(c))*(b*x + a)^n/((n^3 + 6*n^2 + 11*n + 6)*b^3*c^2)

mupad [B] time = 0.31, size = 133, normalized size = 1.34

$$\frac{(a + bx)^n \left(\frac{x^4(n^2+3n+2)}{c(n^3+6n^2+11n+6)} + \frac{2a^3x}{b^3c(n^3+6n^2+11n+6)} - \frac{2a^2nx^2}{b^2c(n^3+6n^2+11n+6)} + \frac{anx^3(n+1)}{bc(n^3+6n^2+11n+6)} \right)}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^5*(a + b*x)^n)/(c*x^2)^(3/2),x)

[Out] ((a + b*x)^n*((x^4*(3*n + n^2 + 2))/(c*(11*n + 6*n^2 + n^3 + 6)) + (2*a^3*x)/(b^3*c*(11*n + 6*n^2 + n^3 + 6)) - (2*a^2*n*x^2)/(b^2*c*(11*n + 6*n^2 + n^3 + 6)) + (a*n*x^3*(n + 1))/(b*c*(11*n + 6*n^2 + n^3 + 6)))/(c*x^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{a^n x^6}{3c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} \\ \int \frac{x^5}{(cx^2)^{\frac{3}{2}}(a+bx)^3} dx \\ \int \frac{x^5}{(cx^2)^{\frac{3}{2}}(a+bx)^2} dx \\ \int \frac{x^5}{(cx^2)^{\frac{3}{2}}(a+bx)} dx \end{array} \right.$$

$$\frac{2a^3 x^3 (a+bx)^n}{b^3 c^{\frac{3}{2}} n^3 (x^2)^{\frac{3}{2}} + 6b^3 c^{\frac{3}{2}} n^2 (x^2)^{\frac{3}{2}} + 11b^3 c^{\frac{3}{2}} n (x^2)^{\frac{3}{2}} + 6b^3 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} - \frac{2a^2 b n x^4 (a+bx)^n}{b^3 c^{\frac{3}{2}} n^3 (x^2)^{\frac{3}{2}} + 6b^3 c^{\frac{3}{2}} n^2 (x^2)^{\frac{3}{2}} + 11b^3 c^{\frac{3}{2}} n (x^2)^{\frac{3}{2}} + 6b^3 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} + \frac{a^n x^6}{b^3 c^{\frac{3}{2}} n^3 (x^2)^{\frac{3}{2}} + 6b^3 c^{\frac{3}{2}} n^2 (x^2)^{\frac{3}{2}} + 11b^3 c^{\frac{3}{2}} n (x^2)^{\frac{3}{2}} + 6b^3 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5*(b*x+a)**n/(c*x**2)**(3/2),x)

[Out] Piecewise((a**n*x**6/(3*c**(3/2)*(x**2)**(3/2)), Eq(b, 0)), (Integral(x**5/((c*x**2)**(3/2)*(a + b*x)**3), x), Eq(n, -3)), (Integral(x**5/((c*x**2)**(3/2)*(a + b*x)**2), x), Eq(n, -2)), (Integral(x**5/((c*x**2)**(3/2)*(a + b*x)), x), Eq(n, -1)), (2*a**3*x**3*(a + b*x)**n/(b**3*c**(3/2)*n**3*(x**2)**(3/2) + 6*b**3*c**(3/2)*n**2*(x**2)**(3/2) + 11*b**3*c**(3/2)*n*(x**2)**(3/2) + 6*b**3*c**(3/2)*(x**2)**(3/2)) - 2*a**2*b*n*x**4*(a + b*x)**n/(b**3*c**(3/2)*n**3*(x**2)**(3/2) + 6*b**3*c**(3/2)*n**2*(x**2)**(3/2) + 11*b**3*c**(3/2)*n*(x**2)**(3/2) + 6*b**3*c**(3/2)*(x**2)**(3/2)) + a*b**2*n**2*x**5*(a + b*x)**n/(b**3*c**(3/2)*n**3*(x**2)**(3/2) + 6*b**3*c**(3/2)*n**2*(x**2)**(3/2) + 11*b**3*c**(3/2)*n*(x**2)**(3/2) + 6*b**3*c**(3/2)*(x**2)**(3/2)) + a*b**2*n*x**5*(a + b*x)**n/(b**3*c**(3/2)*n**3*(x**2)**(3/2) + 6*b**3*c**(3/2)*n**2*(x**2)**(3/2) + 11*b**3*c**(3/2)*n*(x**2)**(3/2) + 6*b**3*c**(3/2)*(x**2)**(3/2)) + a*b**2*n*x**5*(a + b*x)**n/(b**3*c**(3/2)*n**3*(x**2)**(3/2) + 6*b**3*c**(3/2)*n**2*(x**2)**(3/2) + 11*b**3*c**(3/2)*n*(x**2)**(3/2) + 6*b**3*c**(3/2)*(x**2)**(3/2)) + b**3*n**2*x**6*(a + b*x)**n/(b**3*c**(3/2)*n**3*(x**2)**(3/2) + 6*b**3*c**(3/2)*n**2*(x**2)**(3/2) + 11*b**3*c**(3/2)*n*(x**2)**(3/2) + 6*b**3*c**(3/2)*(x**2)**(3/2)) + 3*b**3*n*x**6*(a + b*x)**n/(b**3*c**(3/2)*n**3*(x**2)**(3/2) + 6*b**3*c**(3/2)*n**2*(x**2)**(3/2) + 11*b**3*c**(3/2)*n*(x**2)**(3/2) + 6*b**3*c**(3/2)*(x**2)**(3/2)) + 2*b**3*x**6*(a + b*x)**n/(b**3*c**(3/2)*n**3*(x**2)**(3/2) + 6*b**3*c**(3/2)*n**2*(x**2)**(3/2) + 11*b**3*c**(3/2)*n*(x**2)**(3/2) + 6*b**3*c**(3/2)*(x**2)**(3/2)), True))

$$3.955 \quad \int \frac{x^4(a+bx)^n}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=65

$$\frac{x(a+bx)^{n+2}}{b^2c(n+2)\sqrt{cx^2}} - \frac{ax(a+bx)^{n+1}}{b^2c(n+1)\sqrt{cx^2}}$$

[Out] $-a*x*(b*x+a)^{(1+n)}/b^2/c/(1+n)/(c*x^2)^{(1/2)}+x*(b*x+a)^{(2+n)}/b^2/c/(2+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{x(a+bx)^{n+2}}{b^2c(n+2)\sqrt{cx^2}} - \frac{ax(a+bx)^{n+1}}{b^2c(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^4*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] $-((a*x*(a + b*x)^{(1 + n)})/(b^2*c*(1 + n)*\text{Sqrt}[c*x^2])) + (x*(a + b*x)^{(2 + n)})/(b^2*c*(2 + n)*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^4(a+bx)^n}{(cx^2)^{3/2}} dx &= \frac{x \int x(a+bx)^n dx}{c\sqrt{cx^2}} \\ &= \frac{x \int \left(-\frac{a(a+bx)^n}{b} + \frac{(a+bx)^{1+n}}{b} \right) dx}{c\sqrt{cx^2}} \\ &= -\frac{ax(a+bx)^{1+n}}{b^2c(1+n)\sqrt{cx^2}} + \frac{x(a+bx)^{2+n}}{b^2c(2+n)\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 0.69

$$\frac{x^3(a+bx)^{n+1}(b(n+1)x-a)}{b^2(n+1)(n+2)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^4*(a+b*x)^n)/(c*x^2)^(3/2),x]

[Out] (x^3*(a+b*x)^(1+n)*(-a+b*(1+n)*x))/(b^2*(1+n)*(2+n)*(c*x^2)^(3/2))

fricas [A] time = 0.43, size = 72, normalized size = 1.11

$$\frac{(abnx + (b^2n + b^2)x^2 - a^2)\sqrt{cx^2}(bx+a)^n}{(b^2c^2n^2 + 3b^2c^2n + 2b^2c^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^n/(c*x^2)^(3/2),x, algorithm="fricas")

[Out] (a*b*n*x + (b^2*n + b^2)*x^2 - a^2)*sqrt(c*x^2)*(b*x + a)^n/((b^2*c^2*n^2 + 3*b^2*c^2*n + 2*b^2*c^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^4}{(cx^2)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^n/(c*x^2)^(3/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^4/(c*x^2)^(3/2), x)

maple [A] time = 0.00, size = 46, normalized size = 0.71

$$\frac{(-xnb - bx + a)x^3(bx + a)^{n+1}}{(cx^2)^{\frac{3}{2}}(n^2 + 3n + 2)b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*(b*x+a)^n/(c*x^2)^(3/2), x)

[Out] -(b*x+a)^(n+1)*x^3*(-b*n*x-b*x+a)/(c*x^2)^(3/2)/b^2/(n^2+3*n+2)

maxima [A] time = 1.47, size = 45, normalized size = 0.69

$$\frac{(b^2(n+1)x^2 + abnx - a^2)(bx + a)^n}{(n^2 + 3n + 2)b^2c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="maxima")

[Out] (b^2*(n+1)*x^2 + a*b*n*x - a^2)*(b*x + a)^n/((n^2 + 3*n + 2)*b^2*c^(3/2))

mupad [B] time = 0.29, size = 80, normalized size = 1.23

$$\frac{(a + bx)^n \left(\frac{x^3(n+1)}{c(n^2+3n+2)} - \frac{a^2x}{b^2c(n^2+3n+2)} + \frac{anx^2}{bc(n^2+3n+2)} \right)}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^4*(a + b*x)^n)/(c*x^2)^(3/2), x)

[Out] ((a + b*x)^n*((x^3*(n+1))/(c*(3*n + n^2 + 2)) - (a^2*x)/(b^2*c*(3*n + n^2 + 2)) + (a*n*x^2)/(b*c*(3*n + n^2 + 2)))/(c*x^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{a^n x^5}{2c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} \\ \int \frac{x^4}{(cx^2)^{\frac{3}{2}}(a+bx)^2} dx \\ \int \frac{x^4}{(cx^2)^{\frac{3}{2}}(a+bx)} dx \end{array} \right. - \frac{a^2 x^3 (a+bx)^n}{b^2 c^{\frac{3}{2}} n^2 (x^2)^{\frac{3}{2}} + 3b^2 c^{\frac{3}{2}} n (x^2)^{\frac{3}{2}} + 2b^2 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} + \frac{abnx^4 (a+bx)^n}{b^2 c^{\frac{3}{2}} n^2 (x^2)^{\frac{3}{2}} + 3b^2 c^{\frac{3}{2}} n (x^2)^{\frac{3}{2}} + 2b^2 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} + \frac{b^2 nx^5 (a+bx)^n}{b^2 c^{\frac{3}{2}} n^2 (x^2)^{\frac{3}{2}} + 3b^2 c^{\frac{3}{2}} n (x^2)^{\frac{3}{2}} + 2b^2 c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} + \frac{1}{b^2 c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4*(b*x+a)**n/(c*x**2)**(3/2),x)

[Out] Piecewise((a**n*x**5/(2*c**(3/2)*(x**2)**(3/2)), Eq(b, 0)), (Integral(x**4/((c*x**2)**(3/2)*(a + b*x)**2), x), Eq(n, -2)), (Integral(x**4/((c*x**2)**(3/2)*(a + b*x)), x), Eq(n, -1)), (-a**2*x**3*(a + b*x)**n/(b**2*c**(3/2)*n**2*(x**2)**(3/2) + 3*b**2*c**(3/2)*n*(x**2)**(3/2) + 2*b**2*c**(3/2)*(x**2)**(3/2)) + a*b*n*x**4*(a + b*x)**n/(b**2*c**(3/2)*n**2*(x**2)**(3/2) + 3*b**2*c**(3/2)*n*(x**2)**(3/2) + 2*b**2*c**(3/2)*(x**2)**(3/2)) + b**2*n*x**5*(a + b*x)**n/(b**2*c**(3/2)*n**2*(x**2)**(3/2) + 3*b**2*c**(3/2)*n*(x**2)**(3/2) + 2*b**2*c**(3/2)*(x**2)**(3/2)) + b**2*x**5*(a + b*x)**n/(b**2*c**(3/2)*n**2*(x**2)**(3/2) + 3*b**2*c**(3/2)*n*(x**2)**(3/2) + 2*b**2*c**(3/2)*(x**2)**(3/2)), True))

$$3.956 \quad \int \frac{x^3(a+bx)^n}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=31

$$\frac{x(a+bx)^{n+1}}{bc(n+1)\sqrt{cx^2}}$$

[Out] x*(b*x+a)^(1+n)/b/c/(1+n)/(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$\frac{x(a+bx)^{n+1}}{bc(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^3*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] (x*(a + b*x)^(1 + n))/(b*c*(1 + n)*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{x^3(a+bx)^n}{(cx^2)^{3/2}} dx &= \frac{x \int (a+bx)^n dx}{c\sqrt{cx^2}} \\ &= \frac{x(a+bx)^{1+n}}{bc(1+n)\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 0.97

$$\frac{x^3(a+bx)^{n+1}}{b(n+1)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] (x^3*(a + b*x)^(1 + n))/(b*(1 + n)*(c*x^2)^(3/2))

fricas [A] time = 0.46, size = 37, normalized size = 1.19

$$\frac{\sqrt{cx^2}(bx+a)(bx+a)^n}{(bc^2n+bc^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x + a)*(b*x + a)^n/((b*c^2*n + b*c^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^3}{(cx^2)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^3/(c*x^2)^(3/2), x)

maple [A] time = 0.00, size = 29, normalized size = 0.94

$$\frac{x^3(bx+a)^{n+1}}{(n+1)(cx^2)^{3/2}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^n/(c*x^2)^(3/2), x)

[Out] (b*x+a)^(n+1)/b/(n+1)*x^3/(c*x^2)^(3/2)

maxima [A] time = 1.44, size = 31, normalized size = 1.00

$$\frac{(b\sqrt{c}x + a\sqrt{c})(bx + a)^n}{bc^2(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="maxima")

[Out] (b*sqrt(c)*x + a*sqrt(c))*(b*x + a)^n/(b*c^2*(n + 1))

mupad [B] time = 0.23, size = 42, normalized size = 1.35

$$\frac{\left(\frac{x^2}{c(n+1)} + \frac{ax}{bc(n+1)}\right)(a + bx)^n}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^3*(a + b*x)^n)/(c*x^2)^(3/2), x)

[Out] ((x^2/(c*(n + 1)) + (a*x)/(b*c*(n + 1)))*(a + b*x)^n)/(c*x^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{x^4}{ac^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} & \text{for } b = 0 \wedge n = -1 \\ \frac{a^n x^4}{c^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} & \text{for } b = 0 \\ \int \frac{x^3}{(cx^2)^{\frac{3}{2}}(a+bx)} dx & \text{for } n = -1 \\ \frac{ax^3(a+bx)^n}{bc^{\frac{3}{2}}n(x^2)^{\frac{3}{2}}+bc^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} + \frac{bx^4(a+bx)^n}{bc^{\frac{3}{2}}n(x^2)^{\frac{3}{2}}+bc^{\frac{3}{2}}(x^2)^{\frac{3}{2}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**n/(c*x**2)**(3/2), x)

[Out] Piecewise((x**4/(a*c**(3/2)*(x**2)**(3/2)), Eq(b, 0) & Eq(n, -1)), (a**n*x**4/(c**(3/2)*(x**2)**(3/2)), Eq(b, 0)), (Integral(x**3/((c*x**2)**(3/2)*(a + b*x)), x), Eq(n, -1)), (a*x**3*(a + b*x)**n/(b*c**(3/2)*n*(x**2)**(3/2) + b*c**(3/2)*(x**2)**(3/2)) + b*x**4*(a + b*x)**n/(b*c**(3/2)*n*(x**2)**(3/2) + b*c**(3/2)*(x**2)**(3/2)), True))

$$3.957 \quad \int \frac{x^2(a+bx)^n}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=48

$$-\frac{x(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{ac(n+1)\sqrt{cx^2}}$$

[Out] -x*(b*x+a)^(1+n)*hypergeom([1, 1+n], [2+n], 1+b*x/a)/a/c/(1+n)/(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$-\frac{x(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{ac(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^2*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] -((x*(a + b*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, 1 + (b*x)/a])/(a*c*(1 + n)*Sqrt[c*x^2]))

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_)^(m_))*((c_) + (d_.)*(x_)^(n_)), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{x^2(a+bx)^n}{(cx^2)^{3/2}} dx = \frac{x \int \frac{(a+bx)^n}{x} dx}{c\sqrt{cx^2}}$$

$$= -\frac{x(a+bx)^{1+n} {}_2F_1\left(1, 1+n; 2+n; 1+\frac{bx}{a}\right)}{ac(1+n)\sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 0.98

$$-\frac{x^3(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a}+1\right)}{a(n+1)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] -((x^3*(a + b*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, 1 + (b*x)/a])/(a*(1 + n)*(c*x^2)^(3/2)))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2}(bx+a)^n}{c^2x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c^2*x^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^2}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^2/(c*x^2)^(3/2), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{x^2 (bx + a)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^n/(c*x^2)^(3/2), x)

[Out] int(x^2*(b*x+a)^n/(c*x^2)^(3/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n x^2}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="maxima")

[Out] integrate((b*x + a)^n*x^2/(c*x^2)^(3/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^2 (a + bx)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^2*(a + b*x)^n)/(c*x^2)^(3/2), x)

[Out] int((x^2*(a + b*x)^n)/(c*x^2)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2 (a + bx)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)**n/(c*x**2)**(3/2), x)

[Out] Integral(x**2*(a + b*x)**n/(c*x**2)**(3/2), x)

$$3.958 \quad \int \frac{x(a+bx)^n}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=48

$$\frac{bx(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2c(n+1)\sqrt{cx^2}}$$

[Out] b*x*(b*x+a)^(1+n)*hypergeom([2, 1+n], [2+n], 1+b*x/a)/a^2/c/(1+n)/(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 65}

$$\frac{bx(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2c(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] (b*x*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*c*(1 + n)*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{x(a+bx)^n}{(cx^2)^{3/2}} dx = \frac{x \int \frac{(a+bx)^n}{x^2} dx}{c\sqrt{cx^2}}$$

$$= \frac{bx(a+bx)^{1+n} {}_2F_1\left(2, 1+n; 2+n; 1+\frac{bx}{a}\right)}{a^2c(1+n)\sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 0.98

$$\frac{bx^3(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a}+1\right)}{a^2(n+1)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x*(a + b*x)^n)/(c*x^2)^(3/2), x]

[Out] (b*x^3*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n)*(c*x^2)^(3/2))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2}(bx+a)^n}{c^2x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c^2*x^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n/(c*x^2)^(3/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x/(c*x^2)^(3/2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x (bx + a)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^n/(c*x^2)^(3/2),x)

[Out] int(x*(b*x+a)^n/(c*x^2)^(3/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n x}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n/(c*x^2)^(3/2),x, algorithm="maxima")

[Out] integrate((b*x + a)^n*x/(c*x^2)^(3/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x (a + bx)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x*(a + b*x)^n)/(c*x^2)^(3/2),x)

[Out] int((x*(a + b*x)^n)/(c*x^2)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x (a + bx)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)**n/(c*x**2)**(3/2),x)

[Out] Integral(x*(a + b*x)**n/(c*x**2)**(3/2), x)

$$3.959 \quad \int \frac{(a+bx)^n}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=51

$$\frac{b^2 x (a + bx)^{n+1} {}_2F_1\left(3, n + 1; n + 2; \frac{bx}{a} + 1\right)}{a^3 c (n + 1) \sqrt{cx^2}}$$

[Out] $-b^2 x (b x + a)^{(1+n)} \text{hypergeom}([3, 1+n], [2+n], 1+b x/a) / a^3 / c / (1+n) / (c x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {15, 65}

$$\frac{b^2 x (a + bx)^{n+1} {}_2F_1\left(3, n + 1; n + 2; \frac{bx}{a} + 1\right)}{a^3 c (n + 1) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^n / (c*x^2)^{(3/2)}, x]$

[Out] $-(b^2 x (a + b x)^{(1 + n)} \text{Hypergeometric2F1}[3, 1 + n, 2 + n, 1 + (b x)/a]) / (a^3 c (1 + n) \text{Sqrt}[c x^2])$

Rule 15

$\text{Int}[(u_.) * ((a_.) * (x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]} * (a * x^n)^{\text{FracPart}[m]}) / x^{(n * \text{FracPart}[m])}, \text{Int}[u * x^{(m * n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

$\text{Int}(((b_.) * (x_)^{(m_)}) * ((c_) + (d_.) * (x_)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(c + d * x)^{(n + 1)} \text{Hypergeometric2F1}[-m, n + 1, n + 2, 1 + (d * x)/c] / (d * (n + 1) * (-d / (b * c))^{(m)}), x] /;$ FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(a+bx)^n}{(cx^2)^{3/2}} dx = \frac{x \int \frac{(a+bx)^n}{x^3} dx}{c\sqrt{cx^2}}$$

$$= -\frac{b^2x(a+bx)^{1+n} {}_2F_1\left(3, 1+n; 2+n; 1+\frac{bx}{a}\right)}{a^3c(1+n)\sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 50, normalized size = 0.98

$$-\frac{b^2x^3(a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a}+1\right)}{a^3(n+1)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/(c*x^2)^(3/2), x]

[Out] -((b^2*x^3*(a + b*x)^(1 + n)*Hypergeometric2F1[3, 1 + n, 2 + n, 1 + (b*x)/a])/((a^3*(1 + n)*(c*x^2)^(3/2)))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2}(bx+a)^n}{c^2x^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c^2*x^4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/(c*x^2)^(3/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n/(c*x^2)^(3/2), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n/(c*x^2)^(3/2), x)

[Out] int((b*x+a)^n/(c*x^2)^(3/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/(c*x^2)^(3/2), x, algorithm="maxima")

[Out] integrate((b*x + a)^n/(c*x^2)^(3/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/(c*x^2)^(3/2), x)

[Out] int((a + b*x)^n/(c*x^2)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n/(c*x**2)**(3/2), x)

[Out] Integral((a + b*x)**n/(c*x**2)**(3/2), x)

$$3.960 \quad \int \frac{(a+bx)^n}{x(cx^2)^{3/2}} dx$$

Optimal. Leaf size=50

$$\frac{b^3 x (a + bx)^{n+1} {}_2F_1\left(4, n + 1; n + 2; \frac{bx}{a} + 1\right)}{a^4 c (n + 1) \sqrt{cx^2}}$$

[Out] $b^3 x (b x + a)^{(1+n)} \text{hypergeom}([4, 1+n], [2+n], 1+b x/a) / a^4 / c / (1+n) / (c x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$\frac{b^3 x (a + bx)^{n+1} {}_2F_1\left(4, n + 1; n + 2; \frac{bx}{a} + 1\right)}{a^4 c (n + 1) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n/(x*(c*x^2)^(3/2)),x]

[Out] $(b^3 x (a + b x)^{(1 + n)} \text{Hypergeometric2F1}[4, 1 + n, 2 + n, 1 + (b x)/a]) / (a^4 c (1 + n) \text{Sqrt}[c x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c]) / (d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{(a+bx)^n}{x(cx^2)^{3/2}} dx = \frac{x \int \frac{(a+bx)^n}{x^4} dx}{c\sqrt{cx^2}}$$

$$= \frac{b^3 x(a+bx)^{1+n} {}_2F_1\left(4, 1+n; 2+n; 1+\frac{bx}{a}\right)}{a^4 c(1+n)\sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 50, normalized size = 1.00

$$\frac{b^3 c x^5 (a+bx)^{n+1} {}_2F_1\left(4, n+1; n+2; \frac{bx}{a}+1\right)}{a^4 (n+1) (cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/(x*(c*x^2)^(3/2)),x]

[Out] (b^3*c*x^5*(a + b*x)^(1 + n)*Hypergeometric2F1[4, 1 + n, 2 + n, 1 + (b*x)/a])/ (a^4*(1 + n)*(c*x^2)^(5/2))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2}(bx+a)^n}{c^2x^5}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x/(c*x^2)^(3/2),x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c^2*x^5), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n}{(cx^2)^{\frac{3}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x/(c*x^2)^(3/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n/((c*x^2)^(3/2)*x), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{(cx^2)^{\frac{3}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n/x/(c*x^2)^(3/2),x)

[Out] int((b*x+a)^n/x/(c*x^2)^(3/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{(cx^2)^{\frac{3}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/x/(c*x^2)^(3/2),x, algorithm="maxima")

[Out] integrate((b*x + a)^n/((c*x^2)^(3/2)*x), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^n}{x (cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/(x*(c*x^2)^(3/2)),x)

[Out] int((a + b*x)^n/(x*(c*x^2)^(3/2)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^n}{x (cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n/x/(c*x**2)**(3/2),x)

[Out] Integral((a + b*x)**n/(x*(c*x**2)**(3/2)), x)

$$3.961 \quad \int \frac{x^8(a+bx)^n}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=135

$$-\frac{a^3x(a+bx)^{n+1}}{b^4c^2(n+1)\sqrt{cx^2}} + \frac{3a^2x(a+bx)^{n+2}}{b^4c^2(n+2)\sqrt{cx^2}} - \frac{3ax(a+bx)^{n+3}}{b^4c^2(n+3)\sqrt{cx^2}} + \frac{x(a+bx)^{n+4}}{b^4c^2(n+4)\sqrt{cx^2}}$$

[Out] $-a^3*x*(b*x+a)^{(1+n)}/b^4/c^2/(1+n)/(c*x^2)^{(1/2)}+3*a^2*x*(b*x+a)^{(2+n)}/b^4/c^2/(2+n)/(c*x^2)^{(1/2)}-3*a*x*(b*x+a)^{(3+n)}/b^4/c^2/(3+n)/(c*x^2)^{(1/2)}+x*(b*x+a)^{(4+n)}/b^4/c^2/(4+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 135, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$-\frac{a^3x(a+bx)^{n+1}}{b^4c^2(n+1)\sqrt{cx^2}} + \frac{3a^2x(a+bx)^{n+2}}{b^4c^2(n+2)\sqrt{cx^2}} - \frac{3ax(a+bx)^{n+3}}{b^4c^2(n+3)\sqrt{cx^2}} + \frac{x(a+bx)^{n+4}}{b^4c^2(n+4)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^8*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] $-((a^3*x*(a + b*x)^{(1 + n)})/(b^4*c^2*(1 + n)*\text{Sqrt}[c*x^2])) + (3*a^2*x*(a + b*x)^{(2 + n)})/(b^4*c^2*(2 + n)*\text{Sqrt}[c*x^2]) - (3*a*x*(a + b*x)^{(3 + n)})/(b^4*c^2*(3 + n)*\text{Sqrt}[c*x^2]) + (x*(a + b*x)^{(4 + n)})/(b^4*c^2*(4 + n)*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{x^8(a+bx)^n}{(cx^2)^{5/2}} dx = \frac{x \int x^3(a+bx)^n dx}{c^2 \sqrt{cx^2}}$$

$$= \frac{x \int \left(-\frac{a^3(a+bx)^n}{b^3} + \frac{3a^2(a+bx)^{1+n}}{b^3} - \frac{3a(a+bx)^{2+n}}{b^3} + \frac{(a+bx)^{3+n}}{b^3} \right) dx}{c^2 \sqrt{cx^2}}$$

$$= -\frac{a^3 x(a+bx)^{1+n}}{b^4 c^2 (1+n) \sqrt{cx^2}} + \frac{3a^2 x(a+bx)^{2+n}}{b^4 c^2 (2+n) \sqrt{cx^2}} - \frac{3ax(a+bx)^{3+n}}{b^4 c^2 (3+n) \sqrt{cx^2}} + \frac{x(a+bx)^{4+n}}{b^4 c^2 (4+n) \sqrt{cx^2}}$$

Mathematica [A] time = 0.04, size = 99, normalized size = 0.73

$$\frac{x(a+bx)^{n+1} \left(-6a^3 + 6a^2 b(n+1)x - 3ab^2(n^2 + 3n + 2)x^2 + b^3(n^3 + 6n^2 + 11n + 6)x^3 \right)}{b^4 c^2 (n+1)(n+2)(n+3)(n+4) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^8*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] (x*(a + b*x)^(1 + n)*(-6*a^3 + 6*a^2*b*(1 + n)*x - 3*a*b^2*(2 + 3*n + n^2)*x^2 + b^3*(6 + 11*n + 6*n^2 + n^3)*x^3))/(b^4*c^2*(1 + n)*(2 + n)*(3 + n)*(4 + n)*Sqrt[c*x^2])

fricas [A] time = 0.44, size = 168, normalized size = 1.24

$$\frac{(6a^3bnx + (b^4n^3 + 6b^4n^2 + 11b^4n + 6b^4)x^4 - 6a^4 + (ab^3n^3 + 3ab^3n^2 + 2ab^3n)x^3 - 3(a^2b^2n^2 + a^2b^2n)x^2) \sqrt{c}}{(b^4c^3n^4 + 10b^4c^3n^3 + 35b^4c^3n^2 + 50b^4c^3n + 24b^4c^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] (6*a^3*b*n*x + (b^4*n^3 + 6*b^4*n^2 + 11*b^4*n + 6*b^4)*x^4 - 6*a^4 + (a*b^3*n^3 + 3*a*b^3*n^2 + 2*a*b^3*n)*x^3 - 3*(a^2*b^2*n^2 + a^2*b^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^4*c^3*n^4 + 10*b^4*c^3*n^3 + 35*b^4*c^3*n^2 + 50*b^4*c^3*n + 24*b^4*c^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^8}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^8/(c*x^2)^(5/2), x)

maple [A] time = 0.01, size = 136, normalized size = 1.01

$$\frac{(-b^3n^3x^3 - 6b^3n^2x^3 + 3ab^2n^2x^2 - 11b^3nx^3 + 9ab^2nx^2 - 6b^3x^3 - 6a^2bnx + 6ab^2x^2 - 6a^2bx + 6a^3)x^5 (bx + a)^n}{(cx^2)^{\frac{5}{2}}(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^8*(b*x+a)^n/(c*x^2)^(5/2),x)

[Out] $-(b*x+a)^{(n+1)}*x^5*(-b^3*n^3*x^3-6*b^3*n^2*x^3+3*a*b^2*n^2*x^2-11*b^3*n*x^3+9*a*b^2*n*x^2-6*b^3*x^3-6*a^2*b*n*x+6*a*b^2*x^2-6*a^2*b*x+6*a^3)/(c*x^2)^{(5/2)}/b^4/(n^4+10*n^3+35*n^2+50*n+24)$

maxima [A] time = 1.47, size = 104, normalized size = 0.77

$$\frac{((n^3 + 6n^2 + 11n + 6)b^4x^4 + (n^3 + 3n^2 + 2n)ab^3x^3 - 3(n^2 + n)a^2b^2x^2 + 6a^3bnx - 6a^4)(bx + a)^n}{(n^4 + 10n^3 + 35n^2 + 50n + 24)b^4c^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^8*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="maxima")

[Out] $((n^3 + 6n^2 + 11n + 6)*b^4*x^4 + (n^3 + 3n^2 + 2n)*a*b^3*x^3 - 3*(n^2 + n)*a^2*b^2*x^2 + 6*a^3*b*n*x - 6*a^4)*(b*x + a)^n/((n^4 + 10*n^3 + 35*n^2 + 50*n + 24)*b^4*c^{(5/2)})$

mupad [B] time = 0.41, size = 201, normalized size = 1.49

$$(a + bx)^n \left(\frac{x^5(n^3+6n^2+11n+6)}{c^2(n^4+10n^3+35n^2+50n+24)} - \frac{6a^4x}{b^4c^2(n^4+10n^3+35n^2+50n+24)} + \frac{6a^3nx^2}{b^3c^2(n^4+10n^3+35n^2+50n+24)} + \frac{anx^4(n^2+3n+2)}{bc^2(n^4+10n^3+35n^2+50n+24)} \right) \sqrt{cx^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^8*(a + b*x)^n)/(c*x^2)^(5/2),x)

[Out] $((a + b*x)^n*((x^5*(11*n + 6*n^2 + n^3 + 6))/(c^2*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) - (6*a^4*x)/(b^4*c^2*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (6*a^3*n*x^2)/(b^3*c^2*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (a*n*x^4*(3*n +$

$/2) + 50*b^{**4}*c^{**}(5/2)*n*(x^{**2})^{**}(5/2) + 24*b^{**4}*c^{**}(5/2)*(x^{**2})^{**}(5/2))$, True))

$$3.962 \quad \int \frac{x^7(a+bx)^n}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=99

$$\frac{a^2x(a+bx)^{n+1}}{b^3c^2(n+1)\sqrt{cx^2}} - \frac{2ax(a+bx)^{n+2}}{b^3c^2(n+2)\sqrt{cx^2}} + \frac{x(a+bx)^{n+3}}{b^3c^2(n+3)\sqrt{cx^2}}$$

[Out] $a^2x*(b*x+a)^{(1+n)}/b^3/c^2/(1+n)/(c*x^2)^{(1/2)} - 2*a*x*(b*x+a)^{(2+n)}/b^3/c^2/(2+n)/(c*x^2)^{(1/2)} + x*(b*x+a)^{(3+n)}/b^3/c^2/(3+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 99, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{a^2x(a+bx)^{n+1}}{b^3c^2(n+1)\sqrt{cx^2}} - \frac{2ax(a+bx)^{n+2}}{b^3c^2(n+2)\sqrt{cx^2}} + \frac{x(a+bx)^{n+3}}{b^3c^2(n+3)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^7*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] $(a^2*x*(a + b*x)^{(1 + n)})/(b^3*c^2*(1 + n)*\text{Sqrt}[c*x^2]) - (2*a*x*(a + b*x)^{(2 + n)})/(b^3*c^2*(2 + n)*\text{Sqrt}[c*x^2]) + (x*(a + b*x)^{(3 + n)})/(b^3*c^2*(3 + n)*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_)*((a_)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^7(a+bx)^n}{(cx^2)^{5/2}} dx &= \frac{x \int x^2(a+bx)^n dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(\frac{a^2(a+bx)^n}{b^2} - \frac{2a(a+bx)^{1+n}}{b^2} + \frac{(a+bx)^{2+n}}{b^2} \right) dx}{c^2 \sqrt{cx^2}} \\ &= \frac{a^2 x(a+bx)^{1+n}}{b^3 c^2 (1+n) \sqrt{cx^2}} - \frac{2ax(a+bx)^{2+n}}{b^3 c^2 (2+n) \sqrt{cx^2}} + \frac{x(a+bx)^{3+n}}{b^3 c^2 (3+n) \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 70, normalized size = 0.71

$$\frac{x(a+bx)^{n+1} (2a^2 - 2ab(n+1)x + b^2(n^2 + 3n + 2)x^2)}{b^3 c^2 (n+1)(n+2)(n+3) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^7*(a + b*x)^n)/(c*x^2)^(5/2),x]

[Out] (x*(a + b*x)^(1 + n)*(2*a^2 - 2*a*b*(1 + n)*x + b^2*(2 + 3*n + n^2)*x^2))/(b^3*c^2*(1 + n)*(2 + n)*(3 + n)*Sqrt[c*x^2])

fricas [A] time = 0.45, size = 118, normalized size = 1.19

$$\frac{(2a^2bnx - (b^3n^2 + 3b^3n + 2b^3)x^3 - 2a^3 - (ab^2n^2 + ab^2n)x^2)\sqrt{cx^2}(bx+a)^n}{(b^3c^3n^3 + 6b^3c^3n^2 + 11b^3c^3n + 6b^3c^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="fricas")

[Out] -(2*a^2*b*n*x - (b^3*n^2 + 3*b^3*n + 2*b^3)*x^3 - 2*a^3 - (a*b^2*n^2 + a*b^2*n)*x^2)*sqrt(c*x^2)*(b*x + a)^n/((b^3*c^3*n^3 + 6*b^3*c^3*n^2 + 11*b^3*c^3*n + 6*b^3*c^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^7}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^7/(c*x^2)^(5/2), x)

maple [A] time = 0.01, size = 83, normalized size = 0.84

$$\frac{(b^2n^2x^2 + 3b^2nx^2 - 2abnx + 2b^2x^2 - 2abx + 2a^2)x^5(bx + a)^{n+1}}{(cx^2)^{\frac{5}{2}}(n^3 + 6n^2 + 11n + 6)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^7*(b*x+a)^n/(c*x^2)^(5/2),x)

[Out] (b*x+a)^(n+1)*(b^2*n^2*x^2+3*b^2*n*x^2-2*a*b*n*x+2*b^2*x^2-2*a*b*x+2*a^2)*x^5/(c*x^2)^(5/2)/b^3/(n^3+6*n^2+11*n+6)

maxima [A] time = 1.45, size = 83, normalized size = 0.84

$$\frac{\left((n^2 + 3n + 2)b^3\sqrt{c}x^3 + (n^2 + n)ab^2\sqrt{c}x^2 - 2a^2b\sqrt{c}nx + 2a^3\sqrt{c}\right)(bx + a)^n}{(n^3 + 6n^2 + 11n + 6)b^3c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^7*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="maxima")

[Out] ((n^2 + 3*n + 2)*b^3*sqrt(c)*x^3 + (n^2 + n)*a*b^2*sqrt(c)*x^2 - 2*a^2*b*sqrt(c)*n*x + 2*a^3*sqrt(c))*(b*x + a)^n/((n^3 + 6*n^2 + 11*n + 6)*b^3*c^3)

mupad [B] time = 0.35, size = 133, normalized size = 1.34

$$\frac{(a + bx)^n \left(\frac{x^4(n^2+3n+2)}{c^2(n^3+6n^2+11n+6)} + \frac{2a^3x}{b^3c^2(n^3+6n^2+11n+6)} - \frac{2a^2nx^2}{b^2c^2(n^3+6n^2+11n+6)} + \frac{anx^3(n+1)}{bc^2(n^3+6n^2+11n+6)} \right)}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^7*(a + b*x)^n)/(c*x^2)^(5/2),x)

[Out] ((a + b*x)^n*((x^4*(3*n + n^2 + 2))/(c^2*(11*n + 6*n^2 + n^3 + 6)) + (2*a^3*x)/(b^3*c^2*(11*n + 6*n^2 + n^3 + 6)) - (2*a^2*n*x^2)/(b^2*c^2*(11*n + 6*n^2 + n^3 + 6)) + (a*n*x^3*(n + 1))/(b*c^2*(11*n + 6*n^2 + n^3 + 6)))/(c*x^2)^(1/2)

$$3.963 \quad \int \frac{x^6(a+bx)^n}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=65

$$\frac{x(a+bx)^{n+2}}{b^2c^2(n+2)\sqrt{cx^2}} - \frac{ax(a+bx)^{n+1}}{b^2c^2(n+1)\sqrt{cx^2}}$$

[Out] $-a*x*(b*x+a)^{(1+n)}/b^2/c^2/(1+n)/(c*x^2)^{(1/2)}+x*(b*x+a)^{(2+n)}/b^2/c^2/(2+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 43}

$$\frac{x(a+bx)^{n+2}}{b^2c^2(n+2)\sqrt{cx^2}} - \frac{ax(a+bx)^{n+1}}{b^2c^2(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^6*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] $-((a*x*(a + b*x)^{(1 + n)})/(b^2*c^2*(1 + n)*\text{Sqrt}[c*x^2])) + (x*(a + b*x)^{(2 + n)})/(b^2*c^2*(2 + n)*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^6(a+bx)^n}{(cx^2)^{5/2}} dx &= \frac{x \int x(a+bx)^n dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x \int \left(-\frac{a(a+bx)^n}{b} + \frac{(a+bx)^{1+n}}{b} \right) dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{ax(a+bx)^{1+n}}{b^2 c^2 (1+n) \sqrt{cx^2}} + \frac{x(a+bx)^{2+n}}{b^2 c^2 (2+n) \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.71

$$\frac{x(a+bx)^{n+1}(b(n+1)x-a)}{b^2 c^2 (n+1)(n+2) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^6*(a+b*x)^n)/(c*x^2)^(5/2),x]

[Out] (x*(a+b*x)^(1+n)*(-a+b*(1+n)*x))/(b^2*c^2*(1+n)*(2+n)*Sqrt[c*x^2])

fricas [A] time = 0.45, size = 72, normalized size = 1.11

$$\frac{(abnx + (b^2n + b^2)x^2 - a^2)\sqrt{cx^2}(bx+a)^n}{(b^2c^3n^2 + 3b^2c^3n + 2b^2c^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="fricas")

[Out] (a*b*n*x + (b^2*n + b^2)*x^2 - a^2)*sqrt(c*x^2)*(b*x + a)^n/((b^2*c^3*n^2 + 3*b^2*c^3*n + 2*b^2*c^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^6}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^6/(c*x^2)^(5/2), x)

maple [A] time = 0.00, size = 46, normalized size = 0.71

$$\frac{(-xnb - bx + a)x^5(bx + a)^{n+1}}{(cx^2)^{\frac{5}{2}}(n^2 + 3n + 2)b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6*(b*x+a)^n/(c*x^2)^(5/2),x)

[Out] -(b*x+a)^(n+1)*x^5*(-b*n*x-b*x+a)/(c*x^2)^(5/2)/b^2/(n^2+3*n+2)

maxima [A] time = 1.41, size = 45, normalized size = 0.69

$$\frac{(b^2(n+1)x^2 + abnx - a^2)(bx + a)^n}{(n^2 + 3n + 2)b^2c^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="maxima")

[Out] (b^2*(n + 1)*x^2 + a*b*n*x - a^2)*(b*x + a)^n/((n^2 + 3*n + 2)*b^2*c^(5/2))

mupad [B] time = 0.29, size = 80, normalized size = 1.23

$$\frac{(a + bx)^n \left(\frac{x^3(n+1)}{c^2(n^2+3n+2)} - \frac{a^2x}{b^2c^2(n^2+3n+2)} + \frac{anx^2}{bc^2(n^2+3n+2)} \right)}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^6*(a + b*x)^n)/(c*x^2)^(5/2),x)

[Out] ((a + b*x)^n*((x^3*(n + 1))/(c^2*(3*n + n^2 + 2)) - (a^2*x)/(b^2*c^2*(3*n + n^2 + 2)) + (a*n*x^2)/(b*c^2*(3*n + n^2 + 2)))/(c*x^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{a^n x^7}{2c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} \\ \int \frac{x^6}{(cx^2)^{\frac{5}{2}}(a+bx)^2} dx \\ \int \frac{x^6}{(cx^2)^{\frac{5}{2}}(a+bx)} dx \end{array} \right. - \frac{a^2 x^5 (a+bx)^n}{b^2 c^{\frac{5}{2}} n^2 (x^2)^{\frac{5}{2}} + 3b^2 c^{\frac{5}{2}} n (x^2)^{\frac{5}{2}} + 2b^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}} + \frac{abnx^6 (a+bx)^n}{b^2 c^{\frac{5}{2}} n^2 (x^2)^{\frac{5}{2}} + 3b^2 c^{\frac{5}{2}} n (x^2)^{\frac{5}{2}} + 2b^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}} + \frac{b^2 nx^7 (a+bx)^n}{b^2 c^{\frac{5}{2}} n^2 (x^2)^{\frac{5}{2}} + 3b^2 c^{\frac{5}{2}} n (x^2)^{\frac{5}{2}} + 2b^2 c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}} + \frac{5}{b^2 c^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6*(b*x+a)**n/(c*x**2)**(5/2),x)

[Out] Piecewise((a**n*x**7/(2*c**(5/2)*(x**2)**(5/2)), Eq(b, 0)), (Integral(x**6/((c*x**2)**(5/2)*(a + b*x)**2), x), Eq(n, -2)), (Integral(x**6/((c*x**2)**(5/2)*(a + b*x)), x), Eq(n, -1)), (-a**2*x**5*(a + b*x)**n/(b**2*c**(5/2)*n**2*(x**2)**(5/2) + 3*b**2*c**(5/2)*n*(x**2)**(5/2) + 2*b**2*c**(5/2)*(x**2)**(5/2)) + a*b*n*x**6*(a + b*x)**n/(b**2*c**(5/2)*n**2*(x**2)**(5/2) + 3*b**2*c**(5/2)*n*(x**2)**(5/2) + 2*b**2*c**(5/2)*(x**2)**(5/2)) + b**2*n*x**7*(a + b*x)**n/(b**2*c**(5/2)*n**2*(x**2)**(5/2) + 3*b**2*c**(5/2)*n*(x**2)**(5/2) + 2*b**2*c**(5/2)*(x**2)**(5/2)) + b**2*x**7*(a + b*x)**n/(b**2*c**(5/2)*n**2*(x**2)**(5/2) + 3*b**2*c**(5/2)*n*(x**2)**(5/2) + 2*b**2*c**(5/2)*(x**2)**(5/2)), True))

$$3.964 \quad \int \frac{x^5(a+bx)^n}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=31

$$\frac{x(a+bx)^{n+1}}{bc^2(n+1)\sqrt{cx^2}}$$

[Out] $x*(b*x+a)^{(1+n)}/b/c^2/(1+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 32}

$$\frac{x(a+bx)^{n+1}}{bc^2(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x^5*(a + b*x)^n)/(c*x^2)^{(5/2)}, x]$

[Out] $(x*(a + b*x)^{(1 + n)})/(b*c^2*(1 + n)*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 32

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}/(b*(m + 1)), x] /;$ FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{x^5(a+bx)^n}{(cx^2)^{5/2}} dx &= \frac{x \int (a+bx)^n dx}{c^2 \sqrt{cx^2}} \\ &= \frac{x(a+bx)^{1+n}}{bc^2(1+n)\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 1.00

$$\frac{x(a + bx)^{n+1}}{bc^2(n + 1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^5*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] (x*(a + b*x)^(1 + n))/(b*c^2*(1 + n)*Sqrt[c*x^2])

fricas [A] time = 0.44, size = 37, normalized size = 1.19

$$\frac{\sqrt{cx^2} (bx + a)(bx + a)^n}{(bc^3n + bc^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] sqrt(c*x^2)*(b*x + a)*(b*x + a)^n/((b*c^3*n + b*c^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n x^5}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^5/(c*x^2)^(5/2), x)

maple [A] time = 0.00, size = 29, normalized size = 0.94

$$\frac{x^5 (bx + a)^{n+1}}{(n + 1) (cx^2)^{\frac{5}{2}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5*(b*x+a)^n/(c*x^2)^(5/2), x)

[Out] (b*x+a)^(n+1)/b/(n+1)*x^5/(c*x^2)^(5/2)

maxima [A] time = 1.45, size = 31, normalized size = 1.00

$$\frac{(b\sqrt{c}x + a\sqrt{c})(bx + a)^n}{bc^3(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="maxima")

[Out] (b*sqrt(c)*x + a*sqrt(c))*(b*x + a)^n/(b*c^3*(n + 1))

mupad [B] time = 0.23, size = 42, normalized size = 1.35

$$\frac{\left(\frac{x^2}{c^{2(n+1)}} + \frac{ax}{bc^{2(n+1)}}\right)(a + bx)^n}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^5*(a + b*x)^n)/(c*x^2)^(5/2), x)

[Out] ((x^2/(c^2*(n + 1)) + (a*x)/(b*c^2*(n + 1)))*(a + b*x)^n)/(c*x^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{x^6}{ac^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} & \text{for } b = 0 \wedge n = -1 \\ \frac{a^n x^6}{c^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} & \text{for } b = 0 \\ \int \frac{x^5}{(cx^2)^{\frac{5}{2}}(a+bx)} dx & \text{for } n = -1 \\ \frac{ax^5(a+bx)^n}{bc^{\frac{5}{2}}n(x^2)^{\frac{5}{2}}+bc^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} + \frac{bx^6(a+bx)^n}{bc^{\frac{5}{2}}n(x^2)^{\frac{5}{2}}+bc^{\frac{5}{2}}(x^2)^{\frac{5}{2}}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5*(b*x+a)**n/(c*x**2)**(5/2), x)

[Out] Piecewise((x**6/(a*c**(5/2)*(x**2)**(5/2)), Eq(b, 0) & Eq(n, -1)), (a**n*x**6/(c**(5/2)*(x**2)**(5/2)), Eq(b, 0)), (Integral(x**5/((c*x**2)**(5/2)*(a + b*x)), x), Eq(n, -1)), (a*x**5*(a + b*x)**n/(b*c**(5/2)*n*(x**2)**(5/2) + b*c**(5/2)*(x**2)**(5/2)) + b*x**6*(a + b*x)**n/(b*c**(5/2)*n*(x**2)**(5/2) + b*c**(5/2)*(x**2)**(5/2)), True))

$$3.965 \quad \int \frac{x^4(a+bx)^n}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=48

$$-\frac{x(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{ac^2(n+1)\sqrt{cx^2}}$$

[Out] -x*(b*x+a)^(1+n)*hypergeom([1, 1+n], [2+n], 1+b*x/a)/a/c^2/(1+n)/(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$-\frac{x(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a} + 1\right)}{ac^2(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^4*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] -((x*(a + b*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, 1 + (b*x)/a])/(a*c^2*(1 + n)*Sqrt[c*x^2]))

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{x^4(a+bx)^n}{(cx^2)^{5/2}} dx = \frac{x \int \frac{(a+bx)^n}{x} dx}{c^2 \sqrt{cx^2}}$$

$$= -\frac{x(a+bx)^{1+n} {}_2F_1\left(1, 1+n; 2+n; 1+\frac{bx}{a}\right)}{ac^2(1+n)\sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 0.98

$$-\frac{x^5(a+bx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{bx}{a}+1\right)}{a(n+1)(cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^4*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] -((x^5*(a + b*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, 1 + (b*x)/a])/(a*(1 + n)*(c*x^2)^(5/2)))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2}(bx+a)^n}{c^3x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c^3*x^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^4}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^4/(c*x^2)^(5/2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^4 (bx + a)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^4*(b*x+a)^n/(c*x^2)^(5/2), x)`

[Out] `int(x^4*(b*x+a)^n/(c*x^2)^(5/2), x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n x^4}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="maxima")`

[Out] `integrate((b*x + a)^n*x^4/(c*x^2)^(5/2), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^4 (a + bx)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x^4*(a + b*x)^n)/(c*x^2)^(5/2), x)`

[Out] `int((x^4*(a + b*x)^n)/(c*x^2)^(5/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^4 (a + bx)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**4*(b*x+a)**n/(c*x**2)**(5/2), x)`

[Out] `Integral(x**4*(a + b*x)**n/(c*x**2)**(5/2), x)`

$$3.966 \quad \int \frac{x^3(a+bx)^n}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=48

$$\frac{bx(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2 c^2 (n+1) \sqrt{cx^2}}$$

[Out] b*x*(b*x+a)^(1+n)*hypergeom([2, 1+n], [2+n], 1+b*x/a)/a^2/c^2/(1+n)/(c*x^2)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$\frac{bx(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a} + 1\right)}{a^2 c^2 (n+1) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x^3*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] (b*x*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*c^2*(1 + n)*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n + 1)*Hypergeometric2F1[-m, n + 1, n + 2, 1 + (d*x)/c])/(d*(n + 1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{x^3(a+bx)^n}{(cx^2)^{5/2}} dx = \frac{x \int \frac{(a+bx)^n}{x^2} dx}{c^2 \sqrt{cx^2}}$$

$$= \frac{bx(a+bx)^{1+n} {}_2F_1\left(2, 1+n; 2+n; 1+\frac{bx}{a}\right)}{a^2 c^2 (1+n) \sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 0.98

$$\frac{bx^5(a+bx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{bx}{a}+1\right)}{a^2(n+1)(cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^3*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] (b*x^5*(a + b*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, 1 + (b*x)/a])/(a^2*(1 + n)*(c*x^2)^(5/2))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2}(bx+a)^n}{c^3x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c^3*x^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^3}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^3/(c*x^2)^(5/2), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{x^3 (bx + a)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(b*x+a)^n/(c*x^2)^(5/2), x)

[Out] int(x^3*(b*x+a)^n/(c*x^2)^(5/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n x^3}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="maxima")

[Out] integrate((b*x + a)^n*x^3/(c*x^2)^(5/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^3 (a + bx)^n}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^3*(a + b*x)^n)/(c*x^2)^(5/2), x)

[Out] int((x^3*(a + b*x)^n)/(c*x^2)^(5/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^3 (a + bx)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(b*x+a)**n/(c*x**2)**(5/2), x)

[Out] Integral(x**3*(a + b*x)**n/(c*x**2)**(5/2), x)

$$3.967 \quad \int \frac{x^2(a+bx)^n}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=51

$$-\frac{b^2x(a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3c^2(n+1)\sqrt{cx^2}}$$

[Out] $-b^2x*(b*x+a)^{(1+n)}*\text{hypergeom}([3, 1+n], [2+n], 1+b*x/a)/a^3/c^2/(1+n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 65}

$$-\frac{b^2x(a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a} + 1\right)}{a^3c^2(n+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(x^2*(a + b*x)^n)/(c*x^2)^{(5/2)}, x]$

[Out] $-((b^2*x*(a + b*x)^{(1 + n)}*\text{Hypergeometric2F1}[3, 1 + n, 2 + n, 1 + (b*x)/a])/(a^3*c^2*(1 + n)*\text{Sqrt}[c*x^2]))$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 65

$\text{Int}[(b_.)*(x_)^{(m_)}*((c_.) + (d_.)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(c + d*x)^{(n + 1)}*\text{Hypergeometric2F1}[-m, n + 1, n + 2, 1 + (d*x)/c]/(d*(n + 1)*(-(d/(b*c)))^m), x] /; \text{FreeQ}\{b, c, d, m, n\}, x] \&\& \text{IntegerQ}[n] \&\& (\text{IntegerQ}[m] \mid\mid \text{GtQ}[-(d/(b*c)), 0])$

Rubi steps

$$\int \frac{x^2(a+bx)^n}{(cx^2)^{5/2}} dx = \frac{x \int \frac{(a+bx)^n}{x^3} dx}{c^2 \sqrt{cx^2}}$$

$$= -\frac{b^2 x(a+bx)^{1+n} {}_2F_1\left(3, 1+n; 2+n; 1+\frac{bx}{a}\right)}{a^3 c^2 (1+n) \sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 50, normalized size = 0.98

$$-\frac{b^2 x^5 (a+bx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{bx}{a}+1\right)}{a^3 (n+1) (cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x^2*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] -((b^2*x^5*(a + b*x)^(1 + n)*Hypergeometric2F1[3, 1 + n, 2 + n, 1 + (b*x)/a])/ (a^3*(1 + n)*(c*x^2)^(5/2))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx+a)^n}{c^3 x^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c^3*x^4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x^2}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x^2/(c*x^2)^(5/2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x^2 (bx + a)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(b*x+a)^n/(c*x^2)^(5/2), x)

[Out] int(x^2*(b*x+a)^n/(c*x^2)^(5/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n x^2}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="maxima")

[Out] integrate((b*x + a)^n*x^2/(c*x^2)^(5/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x^2 (a + bx)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^2*(a + b*x)^n)/(c*x^2)^(5/2), x)

[Out] int((x^2*(a + b*x)^n)/(c*x^2)^(5/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x^2 (a + bx)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(b*x+a)**n/(c*x**2)**(5/2), x)

[Out] Integral(x**2*(a + b*x)**n/(c*x**2)**(5/2), x)

$$3.968 \quad \int \frac{x(a+bx)^n}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=50

$$\frac{b^3 x(a+bx)^{n+1} {}_2F_1\left(4, n+1; n+2; \frac{bx}{a} + 1\right)}{a^4 c^2 (n+1) \sqrt{cx^2}}$$

[Out] $b^3 x (b x + a)^{(1+n)} \text{hypergeom}([4, 1+n], [2+n], 1+b x/a) / a^4 / c^2 / (1+n) / (c x^2)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 65}

$$\frac{b^3 x(a+bx)^{n+1} {}_2F_1\left(4, n+1; n+2; \frac{bx}{a} + 1\right)}{a^4 c^2 (n+1) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[(x*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] $(b^3 x (a + b x)^{(1+n)} \text{Hypergeometric2F1}[4, 1+n, 2+n, 1+(b x)/a]) / (a^4 c^2 (1+n) \text{Sqrt}[c x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 65

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((c + d*x)^(n+1)*Hypergeometric2F1[-m, n+1, n+2, 1+(d*x)/c])/(d*(n+1)*(-(d/(b*c)))^m), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[n] && (IntegerQ[m] || GtQ[-(d/(b*c)), 0])

Rubi steps

$$\int \frac{x(a+bx)^n}{(cx^2)^{5/2}} dx = \frac{x \int \frac{(a+bx)^n}{x^4} dx}{c^2 \sqrt{cx^2}}$$

$$= \frac{b^3 x(a+bx)^{1+n} {}_2F_1\left(4, 1+n; 2+n; 1 + \frac{bx}{a}\right)}{a^4 c^2 (1+n) \sqrt{cx^2}}$$

Mathematica [A] time = 0.01, size = 49, normalized size = 0.98

$$\frac{b^3 x^5 (a+bx)^{n+1} {}_2F_1\left(4, n+1; n+2; \frac{bx}{a} + 1\right)}{a^4 (n+1) (cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(x*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] (b^3*x^5*(a + b*x)^(1 + n)*Hypergeometric2F1[4, 1 + n, 2 + n, 1 + (b*x)/a]) / (a^4*(1 + n)*(c*x^2)^(5/2))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx+a)^n}{c^3 x^5}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n/(c^3*x^5), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^n x}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n/(c*x^2)^(5/2), x, algorithm="giac")

[Out] integrate((b*x + a)^n*x/(c*x^2)^(5/2), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{x (bx + a)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(b*x+a)^n/(c*x^2)^(5/2),x)

[Out] int(x*(b*x+a)^n/(c*x^2)^(5/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n x}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="maxima")

[Out] integrate((b*x + a)^n*x/(c*x^2)^(5/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{x (a + bx)^n}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x*(a + b*x)^n)/(c*x^2)^(5/2),x)

[Out] int((x*(a + b*x)^n)/(c*x^2)^(5/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{x (a + bx)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(b*x+a)**n/(c*x**2)**(5/2),x)

[Out] Integral(x*(a + b*x)**n/(c*x**2)**(5/2), x)

$$3.969 \quad \int (dx)^m (cx^2)^{5/2} (a + bx) dx$$

Optimal. Leaf size=65

$$\frac{ac^2\sqrt{cx^2}(dx)^{m+6}}{d^6(m+6)x} + \frac{bc^2\sqrt{cx^2}(dx)^{m+7}}{d^7(m+7)x}$$

[Out] $a*c^2*(d*x)^{(6+m)}*(c*x^2)^{(1/2)}/d^6/(6+m)/x+b*c^2*(d*x)^{(7+m)}*(c*x^2)^{(1/2)}/d^7/(7+m)/x$

Rubi [A] time = 0.03, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {15, 16, 43}

$$\frac{ac^2\sqrt{cx^2}(dx)^{m+6}}{d^6(m+6)x} + \frac{bc^2\sqrt{cx^2}(dx)^{m+7}}{d^7(m+7)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(d*x)^m*(c*x^2)^{(5/2)}*(a + b*x), x]$

[Out] $(a*c^2*(d*x)^{(6 + m)}*\text{Sqrt}[c*x^2])/d^6*(6 + m)*x + (b*c^2*(d*x)^{(7 + m)}*\text{Sqrt}[c*x^2])/d^7*(7 + m)*x$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ $\text{FreeQ}\{a, m, n\}, x\}$
&& $\text{IntegerQ}[m]$

Rule 16

$\text{Int}[(u_.)*(v_)^{(m_.)}*((b_.)*(v_)^{(n_.)}), x_Symbol] \rightarrow \text{Dist}[1/b^m, \text{Int}[u*(b*v)^{(m+n)}, x], x] /;$ $\text{FreeQ}\{b, n\}, x\}$ && $\text{IntegerQ}[m]$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_)^{(m_.)})*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /;$ $\text{FreeQ}\{a, b, c, d, n\}, x\}$ && $\text{NeQ}[b*c - a*d, 0]$ && $\text{IGtQ}[m, 0]$ && $(\text{IntegerQ}[n] \text{ || } (\text{EqQ}[c, 0] \text{ \&\& } \text{LeQ}[7*m + 4*n + 4, 0])) \text{ || } \text{LtQ}[9*m + 5*(n + 1), 0] \text{ || } \text{GtQ}[m + n + 2, 0]$

Rubi steps

$$\begin{aligned}
\int (dx)^m (cx^2)^{5/2} (a + bx) dx &= \frac{(c^2 \sqrt{cx^2}) \int x^5 (dx)^m (a + bx) dx}{x} \\
&= \frac{(c^2 \sqrt{cx^2}) \int (dx)^{5+m} (a + bx) dx}{d^5 x} \\
&= \frac{(c^2 \sqrt{cx^2}) \int \left(a(dx)^{5+m} + \frac{b(dx)^{6+m}}{d} \right) dx}{d^5 x} \\
&= \frac{ac^2(dx)^{6+m} \sqrt{cx^2}}{d^6(6+m)x} + \frac{bc^2(dx)^{7+m} \sqrt{cx^2}}{d^7(7+m)x}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 38, normalized size = 0.58

$$\frac{x (cx^2)^{5/2} (dx)^m (a(m+7) + b(m+6)x)}{(m+6)(m+7)}$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^m*(c*x^2)^(5/2)*(a + b*x), x]

[Out] (x*(d*x)^m*(c*x^2)^(5/2)*(a*(7 + m) + b*(6 + m)*x))/((6 + m)*(7 + m))

fricas [A] time = 0.49, size = 58, normalized size = 0.89

$$\frac{((bc^2m + 6bc^2)x^6 + (ac^2m + 7ac^2)x^5)\sqrt{cx^2} (dx)^m}{m^2 + 13m + 42}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(5/2)*(b*x+a), x, algorithm="fricas")

[Out] ((b*c^2*m + 6*b*c^2)*x^6 + (a*c^2*m + 7*a*c^2)*x^5)*sqrt(c*x^2)*(d*x)^m/(m^2 + 13*m + 42)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(5/2)*(b*x+a), x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
 UT:sage2:=int(sage0,x);OUTPUT:Warning, integration of abs or sign assumes
 constant sign by intervals (correct if the argument is real):Check [abs(x)]
 Undef/Unsigned Inf encountered in limit

maple [A] time = 0.00, size = 40, normalized size = 0.62

$$\frac{(bmx + am + 6bx + 7a)(cx^2)^{\frac{5}{2}}x(dx)^m}{(m+7)(m+6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(5/2)*(b*x+a),x)

[Out] x*(b*m*x+a*m+6*b*x+7*a)*(d*x)^m*(c*x^2)^(5/2)/(m+7)/(m+6)

maxima [A] time = 1.52, size = 39, normalized size = 0.60

$$\frac{bc^{\frac{5}{2}}d^m x^7 x^m}{m+7} + \frac{ac^{\frac{5}{2}}d^m x^6 x^m}{m+6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(5/2)*(b*x+a),x, algorithm="maxima")

[Out] b*c^(5/2)*d^m*x^7*x^m/(m+7) + a*c^(5/2)*d^m*x^6*x^m/(m+6)

mupad [B] time = 0.27, size = 44, normalized size = 0.68

$$\frac{c^2 x^5 (dx)^m \sqrt{cx^2} (7a + am + 6bx + bmx)}{m^2 + 13m + 42}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(5/2)*(a + b*x),x)

[Out] (c^2*x^5*(d*x)^m*(c*x^2)^(1/2)*(7*a + a*m + 6*b*x + b*m*x))/(13*m + m^2 + 42)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{\int \frac{a(cx^2)^{\frac{5}{2}}}{x^7} dx + \int \frac{b(cx^2)^{\frac{5}{2}}}{x^6} dx}{d^7} & \text{for } m = -7 \\ \frac{\int \frac{a(cx^2)^{\frac{5}{2}}}{x^6} dx + \int \frac{b(cx^2)^{\frac{5}{2}}}{x^5} dx}{d^6} & \text{for } m = -6 \\ \frac{ac^{\frac{5}{2}}d^m mx^m (x^2)^{\frac{5}{2}}}{m^2+13m+42} + \frac{7ac^{\frac{5}{2}}d^m xx^m (x^2)^{\frac{5}{2}}}{m^2+13m+42} + \frac{bc^{\frac{5}{2}}d^m mx^2 x^m (x^2)^{\frac{5}{2}}}{m^2+13m+42} + \frac{6bc^{\frac{5}{2}}d^m x^2 x^m (x^2)^{\frac{5}{2}}}{m^2+13m+42} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(c*x**2)**(5/2)*(b*x+a), x)

[Out] Piecewise(((Integral(a*(c*x**2)**(5/2)/x**7, x) + Integral(b*(c*x**2)**(5/2)/x**6, x))/d**7, Eq(m, -7)), ((Integral(a*(c*x**2)**(5/2)/x**6, x) + Integral(b*(c*x**2)**(5/2)/x**5, x))/d**6, Eq(m, -6)), (a*c**(5/2)*d**m*m*x**m*(x**2)**(5/2)/(m**2 + 13*m + 42) + 7*a*c**(5/2)*d**m*x*x**m*(x**2)**(5/2)/(m**2 + 13*m + 42) + b*c**(5/2)*d**m*m*x**2*x**m*(x**2)**(5/2)/(m**2 + 13*m + 42) + 6*b*c**(5/2)*d**m*x**2*x**m*(x**2)**(5/2)/(m**2 + 13*m + 42), True))

$$3.970 \quad \int (dx)^m (cx^2)^{3/2} (a + bx) dx$$

Optimal. Leaf size=61

$$\frac{ac\sqrt{cx^2} (dx)^{m+4}}{d^4(m+4)x} + \frac{bc\sqrt{cx^2} (dx)^{m+5}}{d^5(m+5)x}$$

[Out] a*c*(d*x)^(4+m)*(c*x^2)^(1/2)/d^4/(4+m)/x+b*c*(d*x)^(5+m)*(c*x^2)^(1/2)/d^5/(5+m)/x

Rubi [A] time = 0.03, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {15, 16, 43}

$$\frac{ac\sqrt{cx^2} (dx)^{m+4}}{d^4(m+4)x} + \frac{bc\sqrt{cx^2} (dx)^{m+5}}{d^5(m+5)x}$$

Antiderivative was successfully verified.

[In] Int[(d*x)^m*(c*x^2)^(3/2)*(a + b*x), x]

[Out] (a*c*(d*x)^(4 + m)*Sqrt[c*x^2])/(d^4*(4 + m)*x) + (b*c*(d*x)^(5 + m)*Sqrt[c*x^2])/(d^5*(5 + m)*x)

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_)^(n_)), x_Symbol] := Dist[1/b^m, Int[u*(b*v)^(m + n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int (dx)^m (cx^2)^{3/2} (a + bx) dx &= \frac{(c\sqrt{cx^2}) \int x^3 (dx)^m (a + bx) dx}{x} \\
&= \frac{(c\sqrt{cx^2}) \int (dx)^{3+m} (a + bx) dx}{d^3 x} \\
&= \frac{(c\sqrt{cx^2}) \int \left(a(dx)^{3+m} + \frac{b(dx)^{4+m}}{d} \right) dx}{d^3 x} \\
&= \frac{ac(dx)^{4+m} \sqrt{cx^2}}{d^4(4+m)x} + \frac{bc(dx)^{5+m} \sqrt{cx^2}}{d^5(5+m)x}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 38, normalized size = 0.62

$$\frac{x (cx^2)^{3/2} (dx)^m (a(m+5) + b(m+4)x)}{(m+4)(m+5)}$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^m*(c*x^2)^(3/2)*(a + b*x), x]

[Out] (x*(d*x)^m*(c*x^2)^(3/2)*(a*(5 + m) + b*(4 + m)*x))/((4 + m)*(5 + m))

fricas [A] time = 0.43, size = 50, normalized size = 0.82

$$\frac{((bcm + 4bc)x^4 + (acm + 5ac)x^3)\sqrt{cx^2} (dx)^m}{m^2 + 9m + 20}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(3/2)*(b*x+a), x, algorithm="fricas")

[Out] ((b*c*m + 4*b*c)*x^4 + (a*c*m + 5*a*c)*x^3)*sqrt(c*x^2)*(d*x)^m/(m^2 + 9*m + 20)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(3/2)*(b*x+a), x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
 UT:sage2:=int(sage0,x)::OUTPUT:Warning, integration of abs or sign assumes
 constant sign by intervals (correct if the argument is real):Check [abs(x)]
 Undef/Unsigned Inf encountered in limit

maple [A] time = 0.00, size = 40, normalized size = 0.66

$$\frac{(bmx + am + 4bx + 5a)(cx^2)^{\frac{3}{2}}x(dx)^m}{(m+5)(m+4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(3/2)*(b*x+a),x)

[Out] x*(b*m*x+a*m+4*b*x+5*a)*(d*x)^m*(c*x^2)^(3/2)/(m+5)/(m+4)

maxima [A] time = 1.55, size = 39, normalized size = 0.64

$$\frac{bc^{\frac{3}{2}}d^m x^5 x^m}{m+5} + \frac{ac^{\frac{3}{2}}d^m x^4 x^m}{m+4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(3/2)*(b*x+a),x, algorithm="maxima")

[Out] b*c^(3/2)*d^m*x^5*x^m/(m+5) + a*c^(3/2)*d^m*x^4*x^m/(m+4)

mupad [B] time = 0.24, size = 42, normalized size = 0.69

$$\frac{cx^3(dx)^m \sqrt{cx^2} (5a + am + 4bx + bmx)}{m^2 + 9m + 20}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(3/2)*(a+b*x),x)

[Out] (c*x^3*(d*x)^m*(c*x^2)^(1/2)*(5*a + a*m + 4*b*x + b*m*x))/(9*m + m^2 + 20)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{\int \frac{a(cx^2)^{\frac{3}{2}}}{x^5} dx + \int \frac{b(cx^2)^{\frac{3}{2}}}{x^4} dx}{d^5} & \text{for } m = -5 \\ \frac{\int \frac{a(cx^2)^{\frac{3}{2}}}{x^4} dx + \int \frac{b(cx^2)^{\frac{3}{2}}}{x^3} dx}{d^4} & \text{for } m = -4 \\ \frac{ac^{\frac{3}{2}}d^m m x x^m (x^2)^{\frac{3}{2}}}{m^2 + 9m + 20} + \frac{5ac^{\frac{3}{2}}d^m x x^m (x^2)^{\frac{3}{2}}}{m^2 + 9m + 20} + \frac{bc^{\frac{3}{2}}d^m m x^2 x^m (x^2)^{\frac{3}{2}}}{m^2 + 9m + 20} + \frac{4bc^{\frac{3}{2}}d^m x^2 x^m (x^2)^{\frac{3}{2}}}{m^2 + 9m + 20} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)**m*(c*x**2)**(3/2)*(b*x+a),x)
```

```
[Out] Piecewise(((Integral(a*(c*x**2)**(3/2)/x**5, x) + Integral(b*(c*x**2)**(3/2)/x**4, x))/d**5, Eq(m, -5)), ((Integral(a*(c*x**2)**(3/2)/x**4, x) + Integral(b*(c*x**2)**(3/2)/x**3, x))/d**4, Eq(m, -4)), (a*c**(3/2)*d**m*m*x*x**m*(x**2)**(3/2)/(m**2 + 9*m + 20) + 5*a*c**(3/2)*d**m*x*x**m*(x**2)**(3/2)/(m**2 + 9*m + 20) + b*c**(3/2)*d**m*m*x**2*x**m*(x**2)**(3/2)/(m**2 + 9*m + 20) + 4*b*c**(3/2)*d**m*x**2*x**m*(x**2)**(3/2)/(m**2 + 9*m + 20), True))
```

3.971 $\int (dx)^m \sqrt{cx^2} (a + bx) dx$

Optimal. Leaf size=59

$$\frac{a\sqrt{cx^2} (dx)^{m+2}}{d^2(m+2)x} + \frac{b\sqrt{cx^2} (dx)^{m+3}}{d^3(m+3)x}$$

[Out] $a*(d*x)^{(2+m)}*(c*x^2)^{(1/2)}/d^2/(2+m)/x+b*(d*x)^{(3+m)}*(c*x^2)^{(1/2)}/d^3/(3+m)/x$

Rubi [A] time = 0.03, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {15, 16, 43}

$$\frac{a\sqrt{cx^2} (dx)^{m+2}}{d^2(m+2)x} + \frac{b\sqrt{cx^2} (dx)^{m+3}}{d^3(m+3)x}$$

Antiderivative was successfully verified.

[In] `Int[(d*x)^m*Sqrt[c*x^2]*(a + b*x), x]`

[Out] $(a*(d*x)^{(2 + m)*Sqrt[c*x^2]})/(d^2*(2 + m)*x) + (b*(d*x)^{(3 + m)*Sqrt[c*x^2]})/(d^3*(3 + m)*x)$

Rule 15

`Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]`

Rule 16

`Int[(u_.)*(v_)^(m_.)*((b_.)*(v_))^(n_), x_Symbol] := Dist[1/b^m, Int[u*(b*v)^(m + n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]`

Rule 43

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])`

Rubi steps

$$\begin{aligned}
\int (dx)^m \sqrt{cx^2} (a + bx) dx &= \frac{\sqrt{cx^2} \int x(dx)^m (a + bx) dx}{x} \\
&= \frac{\sqrt{cx^2} \int (dx)^{1+m} (a + bx) dx}{dx} \\
&= \frac{\sqrt{cx^2} \int \left(a(dx)^{1+m} + \frac{b(dx)^{2+m}}{d} \right) dx}{dx} \\
&= \frac{a(dx)^{2+m} \sqrt{cx^2}}{d^2(2+m)x} + \frac{b(dx)^{3+m} \sqrt{cx^2}}{d^3(3+m)x}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 38, normalized size = 0.64

$$\frac{x\sqrt{cx^2} (dx)^m (a(m+3) + b(m+2)x)}{(m+2)(m+3)}$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^m*Sqrt[c*x^2]*(a + b*x), x]

[Out] (x*(d*x)^m*Sqrt[c*x^2]*(a*(3 + m) + b*(2 + m)*x))/((2 + m)*(3 + m))

fricas [A] time = 0.44, size = 44, normalized size = 0.75

$$\frac{((bm + 2b)x^2 + (am + 3a)x)\sqrt{cx^2} (dx)^m}{m^2 + 5m + 6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(1/2)*(b*x+a), x, algorithm="fricas")

[Out] ((b*m + 2*b)*x^2 + (a*m + 3*a)*x)*sqrt(c*x^2)*(d*x)^m/(m^2 + 5*m + 6)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(1/2)*(b*x+a), x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
UT:sage2:=int(sage0,x)::OUTPUT:Warning, integration of abs or sign assumes

constant sign by intervals (correct if the argument is real):Check [abs(x)]
 Undef/Unsigned Inf encountered in limit

maple [A] time = 0.00, size = 40, normalized size = 0.68

$$\frac{(bmx + am + 2bx + 3a) \sqrt{cx^2} x (dx)^m}{(m + 3)(m + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x)^m*(c*x^2)^(1/2)*(b*x+a), x)`

[Out] `x*(b*m*x+a*m+2*b*x+3*a)*(d*x)^m*(c*x^2)^(1/2)/(m+3)/(m+2)`

maxima [A] time = 1.52, size = 39, normalized size = 0.66

$$\frac{b\sqrt{c}d^m x^3 x^m}{m+3} + \frac{a\sqrt{c}d^m x^2 x^m}{m+2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x)^m*(c*x^2)^(1/2)*(b*x+a), x, algorithm="maxima")`

[Out] `b*sqrt(c)*d^m*x^3*x^m/(m+3) + a*sqrt(c)*d^m*x^2*x^m/(m+2)`

mupad [B] time = 0.21, size = 39, normalized size = 0.66

$$\frac{x(dx)^m \sqrt{cx^2} (3a + am + 2bx + bmx)}{m^2 + 5m + 6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x)^m*(c*x^2)^(1/2)*(a + b*x), x)`

[Out] `(x*(d*x)^m*(c*x^2)^(1/2)*(3*a + a*m + 2*b*x + b*m*x))/(5*m + m^2 + 6)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{\int \frac{a\sqrt{cx^2}}{x^3} dx + \int \frac{b\sqrt{cx^2}}{x^2} dx}{d^3} & \text{for } m = -3 \\ \frac{\int \frac{a\sqrt{cx^2}}{x^2} dx + \int \frac{b\sqrt{cx^2}}{x} dx}{d^2} & \text{for } m = -2 \\ \frac{a\sqrt{c}d^m m x^m \sqrt{x^2}}{m^2+5m+6} + \frac{3a\sqrt{c}d^m x^m \sqrt{x^2}}{m^2+5m+6} + \frac{b\sqrt{c}d^m m x^2 x^m \sqrt{x^2}}{m^2+5m+6} + \frac{2b\sqrt{c}d^m x^2 x^m \sqrt{x^2}}{m^2+5m+6} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)**m*(c*x**2)**(1/2)*(b*x+a),x)
```

```
[Out] Piecewise(((Integral(a*sqrt(c*x**2)/x**3, x) + Integral(b*sqrt(c*x**2)/x**2, x))/d**3, Eq(m, -3)), ((Integral(a*sqrt(c*x**2)/x**2, x) + Integral(b*sqrt(c*x**2)/x, x))/d**2, Eq(m, -2)), (a*sqrt(c)*d**m*m*x**m*sqrt(x**2)/(m**2 + 5*m + 6) + 3*a*sqrt(c)*d**m*x**m*sqrt(x**2)/(m**2 + 5*m + 6) + b*sqrt(c)*d**m*m*x**2*x**m*sqrt(x**2)/(m**2 + 5*m + 6) + 2*b*sqrt(c)*d**m*x**2*x**m*sqrt(x**2)/(m**2 + 5*m + 6), True))
```

$$3.972 \quad \int \frac{(dx)^m (a+bx)}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=48

$$\frac{ax(dx)^m}{m\sqrt{cx^2}} + \frac{bx(dx)^{m+1}}{d(m+1)\sqrt{cx^2}}$$

[Out] a*x*(d*x)^m/m/(c*x^2)^(1/2)+b*x*(d*x)^(1+m)/d/(1+m)/(c*x^2)^(1/2)

Rubi [A] time = 0.02, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {15, 16, 43}

$$\frac{ax(dx)^m}{m\sqrt{cx^2}} + \frac{bx(dx)^{m+1}}{d(m+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[((d*x)^m*(a + b*x))/Sqrt[c*x^2],x]

[Out] (a*x*(d*x)^m)/(m*Sqrt[c*x^2]) + (b*x*(d*x)^(1 + m))/(d*(1 + m)*Sqrt[c*x^2])

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_)^(n_)), x_Symbol] := Dist[1/b^m, Int[u*(b*v)^(m + n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_)^(m_.))*((c_.) + (d_.)*(x_)^(n_.)), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(dx)^m(a+bx)}{\sqrt{cx^2}} dx &= \frac{x \int \frac{(dx)^m(a+bx)}{x} dx}{\sqrt{cx^2}} \\
&= \frac{(dx) \int (dx)^{-1+m}(a+bx) dx}{\sqrt{cx^2}} \\
&= \frac{(dx) \int \left(a(dx)^{-1+m} + \frac{b(dx)^m}{d} \right) dx}{\sqrt{cx^2}} \\
&= \frac{ax(dx)^m}{m\sqrt{cx^2}} + \frac{bx(dx)^{1+m}}{d(1+m)\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 33, normalized size = 0.69

$$\frac{x(dx)^m(am + a + bmx)}{m(m+1)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[((d*x)^m*(a + b*x))/Sqrt[c*x^2], x]

[Out] (x*(d*x)^m*(a + a*m + b*m*x))/(m*(1 + m)*Sqrt[c*x^2])

fricas [A] time = 0.44, size = 36, normalized size = 0.75

$$\frac{(bmx + am + a)\sqrt{cx^2} (dx)^m}{(cm^2 + cm)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] (b*m*x + a*m + a)*sqrt(c*x^2)*(d*x)^m/((c*m^2 + c*m)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)(dx)^m}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)/(c*x^2)^(1/2), x, algorithm="giac")

[Out] integrate((b*x + a)*(d*x)^m/sqrt(c*x^2), x)

maple [A] time = 0.00, size = 32, normalized size = 0.67

$$\frac{(bmx + am + a)x(dx)^m}{(m + 1)\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(b*x+a)/(c*x^2)^(1/2), x)

[Out] x*(b*m*x+a*m+a)*(d*x)^m/(m+1)/m/(c*x^2)^(1/2)

maxima [A] time = 1.48, size = 32, normalized size = 0.67

$$\frac{bd^mxx^m}{\sqrt{c}(m+1)} + \frac{ad^mxx^m}{\sqrt{c}m}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)/(c*x^2)^(1/2), x, algorithm="maxima")

[Out] b*d^m*x*x^m/(sqrt(c)*(m + 1)) + a*d^m*x^m/(sqrt(c)*m)

mupad [B] time = 0.21, size = 30, normalized size = 0.62

$$\frac{\left(\frac{ax}{m} + \frac{bx^2}{m+1}\right)(dx)^m}{\sqrt{cx^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((d*x)^m*(a + b*x))/(c*x^2)^(1/2), x)

[Out] (((a*x)/m + (b*x^2)/(m + 1))*(d*x)^m)/(c*x^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} \frac{\int \frac{b}{\sqrt{cx^2}} dx + \int \frac{a}{x\sqrt{cx^2}} dx}{d} & \text{for } m = -1 \\ \int \frac{a+bx}{\sqrt{cx^2}} dx & \text{for } m = 0 \\ \frac{ad^m m x x^m}{\sqrt{c} m^2 \sqrt{x^2} + \sqrt{c} m \sqrt{x^2}} + \frac{ad^m x x^m}{\sqrt{c} m^2 \sqrt{x^2} + \sqrt{c} m \sqrt{x^2}} + \frac{bd^m m x^2 x^m}{\sqrt{c} m^2 \sqrt{x^2} + \sqrt{c} m \sqrt{x^2}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(b*x+a)/(c*x**2)**(1/2),x)

[Out] Piecewise(((Integral(b/sqrt(c*x**2), x) + Integral(a/(x*sqrt(c*x**2)), x))/d, Eq(m, -1)), (Integral((a + b*x)/sqrt(c*x**2), x), Eq(m, 0)), (a*d**m*m*x*x**m/(sqrt(c)*m**2*sqrt(x**2) + sqrt(c)*m*sqrt(x**2)) + a*d**m*x*x**m/(sqrt(c)*m**2*sqrt(x**2) + sqrt(c)*m*sqrt(x**2)) + b*d**m*m*x**2*x**m/(sqrt(c)*m**2*sqrt(x**2) + sqrt(c)*m*sqrt(x**2)), True))

$$3.973 \quad \int \frac{(dx)^m (a+bx)}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=65

$$-\frac{ad^2x(dx)^{m-2}}{c(2-m)\sqrt{cx^2}} - \frac{bdx(dx)^{m-1}}{c(1-m)\sqrt{cx^2}}$$

[Out] $-a*d^2*x*(d*x)^{-2+m}/c/(2-m)/(c*x^2)^{(1/2)}-b*d*x*(d*x)^{-1+m}/c/(1-m)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {15, 16, 43}

$$-\frac{ad^2x(dx)^{m-2}}{c(2-m)\sqrt{cx^2}} - \frac{bdx(dx)^{m-1}}{c(1-m)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(d*x)^m*(a + b*x)/(c*x^2)^{(3/2)}, x]$

[Out] $-((a*d^2*x*(d*x)^{-2 + m})/(c*(2 - m)*\text{Sqrt}[c*x^2])) - (b*d*x*(d*x)^{-1 + m})/(c*(1 - m)*\text{Sqrt}[c*x^2])$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 16

$\text{Int}[(u_.)*(v_)^{(m_.)*((b_.)*(v_))^{(n_.)}, x_Symbol] \rightarrow \text{Dist}[1/b^m, \text{Int}[u*(b*v)^{(m+n)}, x], x] /; \text{FreeQ}\{b, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{IGtQ}[m, 0] \&\& (!\text{IntegerQ}[n] || (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0])) || \text{LtQ}[9*m + 5*(n + 1), 0] || \text{GtQ}[m + n + 2, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(dx)^m(a+bx)}{(cx^2)^{3/2}} dx &= \frac{x \int \frac{(dx)^m(a+bx)}{x^3} dx}{c\sqrt{cx^2}} \\
&= \frac{(d^3x) \int (dx)^{-3+m}(a+bx) dx}{c\sqrt{cx^2}} \\
&= \frac{(d^3x) \int \left(a(dx)^{-3+m} + \frac{b(dx)^{-2+m}}{d} \right) dx}{c\sqrt{cx^2}} \\
&= -\frac{ad^2x(dx)^{-2+m}}{c(2-m)\sqrt{cx^2}} - \frac{bdx(dx)^{-1+m}}{c(1-m)\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 38, normalized size = 0.58

$$\frac{x(dx)^m(a(m-1) + b(m-2)x)}{(m-2)(m-1)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[((d*x)^m*(a + b*x))/(c*x^2)^(3/2), x]

[Out] (x*(d*x)^m*(a*(-1 + m) + b*(-2 + m)*x))/((-2 + m)*(-1 + m)*(c*x^2)^(3/2))

fricas [A] time = 0.46, size = 53, normalized size = 0.82

$$\frac{\sqrt{cx^2}(am + (bm - 2b)x - a)(dx)^m}{(c^2m^2 - 3c^2m + 2c^2)x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] sqrt(c*x^2)*(a*m + (b*m - 2*b)*x - a)*(d*x)^m/((c^2*m^2 - 3*c^2*m + 2*c^2)*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)(dx)^m}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)/(c*x^2)^(3/2),x, algorithm="giac")

[Out] integrate((b*x + a)*(d*x)^m/(c*x^2)^(3/2), x)

maple [A] time = 0.00, size = 40, normalized size = 0.62

$$\frac{(bmx + am - 2bx - a)x(dx)^m}{(m-1)(m-2)(cx^2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(b*x+a)/(c*x^2)^(3/2),x)

[Out] x*(b*m*x+a*m-2*b*x-a)*(d*x)^m/(m-1)/(m-2)/(c*x^2)^(3/2)

maxima [A] time = 1.51, size = 39, normalized size = 0.60

$$\frac{bd^m x^m}{c^{\frac{3}{2}}(m-1)x} + \frac{ad^m x^m}{c^{\frac{3}{2}}(m-2)x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)/(c*x^2)^(3/2),x, algorithm="maxima")

[Out] b*d^m*x^m/(c^(3/2)*(m-1)*x) + a*d^m*x^m/(c^(3/2)*(m-2)*x^2)

mupad [B] time = 0.26, size = 48, normalized size = 0.74

$$\frac{b(dx)^m}{c\sqrt{cx^2}(m-1)} + \frac{a(dx)^m}{cx\sqrt{cx^2}(m-2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((d*x)^m*(a + b*x))/(c*x^2)^(3/2),x)

[Out] (b*(d*x)^m)/(c*(c*x^2)^(1/2)*(m-1)) + (a*(d*x)^m)/(c*x*(c*x^2)^(1/2)*(m-2))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} d \left(\int \frac{ax}{(cx^2)^{\frac{3}{2}}} dx + \int \frac{bx^2}{(cx^2)^{\frac{3}{2}}} dx \right) \\ d^2 \left(\int \frac{ax^2}{(cx^2)^{\frac{3}{2}}} dx + \int \frac{bx^3}{(cx^2)^{\frac{3}{2}}} dx \right) \\ \frac{ad^m m x^m}{c^{\frac{3}{2}} m^2 (x^2)^{\frac{3}{2}} - 3c^{\frac{3}{2}} m (x^2)^{\frac{3}{2}} + 2c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} - \frac{ad^m x^m}{c^{\frac{3}{2}} m^2 (x^2)^{\frac{3}{2}} - 3c^{\frac{3}{2}} m (x^2)^{\frac{3}{2}} + 2c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} + \frac{bd^m m x^2 x^m}{c^{\frac{3}{2}} m^2 (x^2)^{\frac{3}{2}} - 3c^{\frac{3}{2}} m (x^2)^{\frac{3}{2}} + 2c^{\frac{3}{2}} (x^2)^{\frac{3}{2}}} - \frac{2bd^m x^2 x^m}{c^{\frac{3}{2}} m^2 (x^2)^{\frac{3}{2}} - 3c^{\frac{3}{2}} m (x^2)^{\frac{3}{2}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(b*x+a)/(c*x**2)**(3/2), x)

[Out] Piecewise((d*(Integral(a*x/(c*x**2)**(3/2), x) + Integral(b*x**2/(c*x**2)**(3/2), x)), Eq(m, 1)), (d**2*(Integral(a*x**2/(c*x**2)**(3/2), x) + Integral(b*x**3/(c*x**2)**(3/2), x)), Eq(m, 2)), (a*d**m*m*x*x**m/(c**(3/2)*m**2*(x**2)**(3/2) - 3*c**(3/2)*m*(x**2)**(3/2) + 2*c**(3/2)*(x**2)**(3/2)) - a*d**m*x*x**m/(c**(3/2)*m**2*(x**2)**(3/2) - 3*c**(3/2)*m*(x**2)**(3/2) + 2*c**(3/2)*(x**2)**(3/2)) + b*d**m*m*x**2*x**m/(c**(3/2)*m**2*(x**2)**(3/2) - 3*c**(3/2)*m*(x**2)**(3/2) + 2*c**(3/2)*(x**2)**(3/2)) - 2*b*d**m*x**2*x**m/(c**(3/2)*m**2*(x**2)**(3/2) - 3*c**(3/2)*m*(x**2)**(3/2) + 2*c**(3/2)*(x**2)**(3/2)), True))

$$3.974 \quad \int \frac{(dx)^m (a+bx)}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=67

$$-\frac{ad^4x(dx)^{m-4}}{c^2(4-m)\sqrt{cx^2}} - \frac{bd^3x(dx)^{m-3}}{c^2(3-m)\sqrt{cx^2}}$$

[Out] $-a*d^4*x*(d*x)^{-4+m}/c^2/(4-m)/(c*x^2)^{(1/2)} - b*d^3*x*(d*x)^{-3+m}/c^2/(3-m)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {15, 16, 43}

$$-\frac{ad^4x(dx)^{m-4}}{c^2(4-m)\sqrt{cx^2}} - \frac{bd^3x(dx)^{m-3}}{c^2(3-m)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[((d*x)^m*(a + b*x))/(c*x^2)^(5/2), x]

[Out] $-((a*d^4*x*(d*x)^{-4 + m})/(c^2*(4 - m)*\text{Sqrt}[c*x^2])) - (b*d^3*x*(d*x)^{-3 + m})/(c^2*(3 - m)*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_)^(n_)), x_Symbol] := Dist[1/b^m, Int[u*(b*v)^(m + n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(dx)^m(a+bx)}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{(dx)^m(a+bx)}{x^5} dx}{c^2 \sqrt{cx^2}} \\
&= \frac{(d^5 x) \int (dx)^{-5+m}(a+bx) dx}{c^2 \sqrt{cx^2}} \\
&= \frac{(d^5 x) \int \left(a(dx)^{-5+m} + \frac{b(dx)^{-4+m}}{d} \right) dx}{c^2 \sqrt{cx^2}} \\
&= -\frac{ad^4 x(dx)^{-4+m}}{c^2(4-m)\sqrt{cx^2}} - \frac{bd^3 x(dx)^{-3+m}}{c^2(3-m)\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 38, normalized size = 0.57

$$\frac{x(dx)^m(a(m-3) + b(m-4)x)}{(m-4)(m-3)(cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[((d*x)^m*(a + b*x))/(c*x^2)^(5/2), x]

[Out] (x*(d*x)^m*(a*(-3 + m) + b*(-4 + m)*x))/((-4 + m)*(-3 + m)*(c*x^2)^(5/2))

fricas [A] time = 0.64, size = 53, normalized size = 0.79

$$\frac{\sqrt{cx^2}(am + (bm - 4b)x - 3a)(dx)^m}{(c^3m^2 - 7c^3m + 12c^3)x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] sqrt(c*x^2)*(a*m + (b*m - 4*b)*x - 3*a)*(d*x)^m/((c^3*m^2 - 7*c^3*m + 12*c^3)*x^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)(dx)^m}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)/(c*x^2)^(5/2),x, algorithm="giac")

[Out] integrate((b*x + a)*(d*x)^m/(c*x^2)^(5/2), x)

maple [A] time = 0.00, size = 40, normalized size = 0.60

$$\frac{(bmx + am - 4bx - 3a)x(dx)^m}{(m-3)(m-4)(cx^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(b*x+a)/(c*x^2)^(5/2),x)

[Out] x*(b*m*x+a*m-4*b*x-3*a)*(d*x)^m/(m-3)/(-4+m)/(c*x^2)^(5/2)

maxima [A] time = 1.52, size = 39, normalized size = 0.58

$$\frac{bd^m x^m}{c^{\frac{5}{2}}(m-3)x^3} + \frac{ad^m x^m}{c^{\frac{5}{2}}(m-4)x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)/(c*x^2)^(5/2),x, algorithm="maxima")

[Out] b*d^m*x^m/(c^(5/2)*(m-3)*x^3) + a*d^m*x^m/(c^(5/2)*(m-4)*x^4)

mupad [B] time = 0.28, size = 47, normalized size = 0.70

$$\frac{(dx)^m(3a - am + 4bx - bmx)}{c^2 x^3 \sqrt{cx^2} (m^2 - 7m + 12)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((d*x)^m*(a + b*x))/(c*x^2)^(5/2),x)

[Out] -((d*x)^m*(3*a - a*m + 4*b*x - b*m*x))/(c^2*x^3*(c*x^2)^(1/2)*(m^2 - 7*m + 12))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} d^3 \left(\int \frac{ax^3}{(cx^2)^{\frac{5}{2}}} dx + \int \frac{bx^4}{(cx^2)^{\frac{5}{2}}} dx \right) \\ d^4 \left(\int \frac{ax^4}{(cx^2)^{\frac{5}{2}}} dx + \int \frac{bx^5}{(cx^2)^{\frac{5}{2}}} dx \right) \\ \frac{ad^m m x x^m}{c^{\frac{5}{2}} m^2 (x^2)^{\frac{5}{2}} - 7c^{\frac{5}{2}} m (x^2)^{\frac{5}{2}} + 12c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}} - \frac{3ad^m x x^m}{c^{\frac{5}{2}} m^2 (x^2)^{\frac{5}{2}} - 7c^{\frac{5}{2}} m (x^2)^{\frac{5}{2}} + 12c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}} + \frac{bd^m m x^2 x^m}{c^{\frac{5}{2}} m^2 (x^2)^{\frac{5}{2}} - 7c^{\frac{5}{2}} m (x^2)^{\frac{5}{2}} + 12c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}} - \frac{4bd^m x}{c^{\frac{5}{2}} m^2 (x^2)^{\frac{5}{2}} - 7c^{\frac{5}{2}} m (x^2)^{\frac{5}{2}} + 12c^{\frac{5}{2}} (x^2)^{\frac{5}{2}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(b*x+a)/(c*x**2)**(5/2), x)

[Out] Piecewise((d**3*(Integral(a*x**3/(c*x**2)**(5/2), x) + Integral(b*x**4/(c*x**2)**(5/2), x)), Eq(m, 3)), (d**4*(Integral(a*x**4/(c*x**2)**(5/2), x) + Integral(b*x**5/(c*x**2)**(5/2), x)), Eq(m, 4)), (a*d**m*m*x*x**m/(c**(5/2)*m**2*(x**2)**(5/2) - 7*c**(5/2)*m*(x**2)**(5/2) + 12*c**(5/2)*(x**2)**(5/2)) - 3*a*d**m*x*x**m/(c**(5/2)*m**2*(x**2)**(5/2) - 7*c**(5/2)*m*(x**2)**(5/2) + 12*c**(5/2)*(x**2)**(5/2)) + b*d**m*m*x**2*x**m/(c**(5/2)*m**2*(x**2)**(5/2) - 7*c**(5/2)*m*(x**2)**(5/2) + 12*c**(5/2)*(x**2)**(5/2)) - 4*b*d**m*x**2*x**m/(c**(5/2)*m**2*(x**2)**(5/2) - 7*c**(5/2)*m*(x**2)**(5/2) + 12*c**(5/2)*(x**2)**(5/2)), True))

$$3.975 \quad \int (dx)^m (cx^2)^{5/2} (a + bx)^2 dx$$

Optimal. Leaf size=103

$$\frac{a^2 c^2 \sqrt{cx^2} (dx)^{m+6}}{d^6 (m+6)x} + \frac{2abc^2 \sqrt{cx^2} (dx)^{m+7}}{d^7 (m+7)x} + \frac{b^2 c^2 \sqrt{cx^2} (dx)^{m+8}}{d^8 (m+8)x}$$

[Out] $a^2 c^2 (d*x)^{(6+m)} (c*x^2)^{(1/2)} / d^6 / (6+m) / x + 2*a*b*c^2 (d*x)^{(7+m)} (c*x^2)^{(1/2)} / d^7 / (7+m) / x + b^2 c^2 (d*x)^{(8+m)} (c*x^2)^{(1/2)} / d^8 / (8+m) / x$

Rubi [A] time = 0.05, antiderivative size = 103, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$, Rules used = {15, 16, 43}

$$\frac{a^2 c^2 \sqrt{cx^2} (dx)^{m+6}}{d^6 (m+6)x} + \frac{2abc^2 \sqrt{cx^2} (dx)^{m+7}}{d^7 (m+7)x} + \frac{b^2 c^2 \sqrt{cx^2} (dx)^{m+8}}{d^8 (m+8)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(d*x)^m (c*x^2)^{(5/2)} (a + b*x)^2, x]$

[Out] $(a^2 c^2 (d*x)^{(6+m)} \text{Sqrt}[c*x^2]) / (d^6 (6+m)x) + (2*a*b*c^2 (d*x)^{(7+m)} \text{Sqrt}[c*x^2]) / (d^7 (7+m)x) + (b^2 c^2 (d*x)^{(8+m)} \text{Sqrt}[c*x^2]) / (d^8 (8+m)x)$

Rule 15

$\text{Int}[(u_*) * ((a_*) * (x_*)^{(n_*)})^{(m_*)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]} * (a*x^n)^{\text{FracPart}[m]}) / x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

$\text{Int}[(u_*) * (v_*)^{(m_*)} * ((b_*) * (v_*)^{(n_*)}), x_Symbol] \rightarrow \text{Dist}[1/b^m, \text{Int}[u*(b*v)^{(m+n)}, x], x] /;$ FreeQ[{b, n}, x] && IntegerQ[m]

Rule 43

$\text{Int}[(a_*) + (b_*) * (x_*)^{(m_*)} * ((c_*) + (d_*) * (x_*)^{(n_*)}), x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m (c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int (dx)^m (cx^2)^{5/2} (a+bx)^2 dx &= \frac{(c^2\sqrt{cx^2}) \int x^5 (dx)^m (a+bx)^2 dx}{x} \\
&= \frac{(c^2\sqrt{cx^2}) \int (dx)^{5+m} (a+bx)^2 dx}{d^5 x} \\
&= \frac{(c^2\sqrt{cx^2}) \int \left(a^2 (dx)^{5+m} + \frac{2ab(dx)^{6+m}}{d} + \frac{b^2(dx)^{7+m}}{d^2} \right) dx}{d^5 x} \\
&= \frac{a^2 c^2 (dx)^{6+m} \sqrt{cx^2}}{d^6 (6+m)x} + \frac{2abc^2 (dx)^{7+m} \sqrt{cx^2}}{d^7 (7+m)x} + \frac{b^2 c^2 (dx)^{8+m} \sqrt{cx^2}}{d^8 (8+m)x}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 48, normalized size = 0.47

$$x (cx^2)^{5/2} (dx)^m \left(\frac{a^2}{m+6} + \frac{2abx}{m+7} + \frac{b^2 x^2}{m+8} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^m*(c*x^2)^(5/2)*(a + b*x)^2,x]

[Out] x*(d*x)^m*(c*x^2)^(5/2)*(a^2/(6 + m) + (2*a*b*x)/(7 + m) + (b^2*x^2)/(8 + m))

fricas [A] time = 0.75, size = 123, normalized size = 1.19

$$\frac{\left((b^2 c^2 m^2 + 13 b^2 c^2 m + 42 b^2 c^2) x^7 + 2 (abc^2 m^2 + 14 abc^2 m + 48 abc^2) x^6 + (a^2 c^2 m^2 + 15 a^2 c^2 m + 56 a^2 c^2) x^5 \right) \sqrt{c x^2}}{m^3 + 21 m^2 + 146 m + 336}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(5/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] ((b^2*c^2*m^2 + 13*b^2*c^2*m + 42*b^2*c^2)*x^7 + 2*(a*b*c^2*m^2 + 14*a*b*c^2*m + 48*a*b*c^2)*x^6 + (a^2*c^2*m^2 + 15*a^2*c^2*m + 56*a^2*c^2)*x^5)*sqrt(c*x^2)*(d*x)^m/(m^3 + 21*m^2 + 146*m + 336)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(5/2)*(b*x+a)^2,x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
 UT:sage2:=int(sage0,x):;OUTPUT:Warning, integration of abs or sign assumes
 constant sign by intervals (correct if the argument is real):Check [abs(x)]
 Undef/Unsigned Inf encountered in limit

maple [A] time = 0.00, size = 95, normalized size = 0.92

$$\frac{(b^2 m^2 x^2 + 2ab m^2 x + 13b^2 m x^2 + a^2 m^2 + 28abmx + 42b^2 x^2 + 15a^2 m + 96abx + 56a^2) (c x^2)^{\frac{5}{2}} x (dx)^m}{(m+8)(m+7)(m+6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(5/2)*(b*x+a)^2,x)

[Out] x*(b^2*m^2*x^2+2*a*b*m^2*x+13*b^2*m*x^2+a^2*m^2+28*a*b*m*x+42*b^2*x^2+15*a^2*m+96*a*b*x+56*a^2)*(d*x)^m*(c*x^2)^(5/2)/(m+8)/(m+7)/(m+6)

maxima [A] time = 1.60, size = 64, normalized size = 0.62

$$\frac{b^2 c^{\frac{5}{2}} d^m x^8 x^m}{m+8} + \frac{2abc^{\frac{5}{2}} d^m x^7 x^m}{m+7} + \frac{a^2 c^{\frac{5}{2}} d^m x^6 x^m}{m+6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(5/2)*(b*x+a)^2,x, algorithm="maxima")

[Out] b^2*c^(5/2)*d^m*x^8*x^m/(m+8) + 2*a*b*c^(5/2)*d^m*x^7*x^m/(m+7) + a^2*c^(5/2)*d^m*x^6*x^m/(m+6)

mupad [B] time = 0.31, size = 127, normalized size = 1.23

$$(dx)^m \left(\frac{a^2 c^2 x^5 \sqrt{c x^2} (m^2 + 15 m + 56)}{m^3 + 21 m^2 + 146 m + 336} + \frac{b^2 c^2 x^7 \sqrt{c x^2} (m^2 + 13 m + 42)}{m^3 + 21 m^2 + 146 m + 336} + \frac{2 a b c^2 x^6 \sqrt{c x^2} (m^2 + 14 m + 48)}{m^3 + 21 m^2 + 146 m + 336} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(5/2)*(a+b*x)^2,x)

[Out] (d*x)^m*((a^2*c^2*x^5*(c*x^2)^(1/2)*(15*m+m^2+56))/(146*m+21*m^2+m^3+336) + (b^2*c^2*x^7*(c*x^2)^(1/2)*(13*m+m^2+42))/(146*m+21*m^2+m^3+336) + (2*a*b*c^2*x^6*(c*x^2)^(1/2)*(14*m+m^2+48))/(146*m+21*m^2+m^3+336))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{\int \frac{a^2(cx^2)^{\frac{5}{2}}}{x^8} dx + \int \frac{b^2(cx^2)^{\frac{5}{2}}}{x^6} dx + \int \frac{2ab(cx^2)^{\frac{5}{2}}}{x^7} dx}{d^8} \\ \frac{\int \frac{a^2(cx^2)^{\frac{5}{2}}}{x^7} dx + \int \frac{b^2(cx^2)^{\frac{5}{2}}}{x^5} dx + \int \frac{2ab(cx^2)^{\frac{5}{2}}}{x^6} dx}{d^7} \\ \frac{\int \frac{a^2(cx^2)^{\frac{5}{2}}}{x^6} dx + \int \frac{b^2(cx^2)^{\frac{5}{2}}}{x^4} dx + \int \frac{2ab(cx^2)^{\frac{5}{2}}}{x^5} dx}{d^6} \\ \frac{a^2c^{\frac{5}{2}}d^m m^2 x x^m (x^2)^{\frac{5}{2}}}{m^3+21m^2+146m+336} + \frac{15a^2c^{\frac{5}{2}}d^m m x x^m (x^2)^{\frac{5}{2}}}{m^3+21m^2+146m+336} + \frac{56a^2c^{\frac{5}{2}}d^m x x^m (x^2)^{\frac{5}{2}}}{m^3+21m^2+146m+336} + \frac{2abc^{\frac{5}{2}}d^m m^2 x^2 x^m (x^2)^{\frac{5}{2}}}{m^3+21m^2+146m+336} + \frac{28abc^{\frac{5}{2}}d^m m x^2 x^m (x^2)^{\frac{5}{2}}}{m^3+21m^2+146m+336} + \frac{96abc^{\frac{5}{2}}d^m}{m^3+21m^2} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(c*x**2)**(5/2)*(b*x+a)**2,x)

[Out] Piecewise(((Integral(a**2*(c*x**2)**(5/2)/x**8, x) + Integral(b**2*(c*x**2)**(5/2)/x**6, x) + Integral(2*a*b*(c*x**2)**(5/2)/x**7, x))/d**8, Eq(m, -8)), ((Integral(a**2*(c*x**2)**(5/2)/x**7, x) + Integral(b**2*(c*x**2)**(5/2)/x**5, x) + Integral(2*a*b*(c*x**2)**(5/2)/x**6, x))/d**7, Eq(m, -7)), ((Integral(a**2*(c*x**2)**(5/2)/x**6, x) + Integral(b**2*(c*x**2)**(5/2)/x**4, x) + Integral(2*a*b*(c*x**2)**(5/2)/x**5, x))/d**6, Eq(m, -6)), (a**2*c**(5/2)*d**m*m**2*x*x**m*(x**2)**(5/2)/(m**3 + 21*m**2 + 146*m + 336) + 15*a**2*c**(5/2)*d**m*m*x*x**m*(x**2)**(5/2)/(m**3 + 21*m**2 + 146*m + 336) + 56*a**2*c**(5/2)*d**m*x*x**m*(x**2)**(5/2)/(m**3 + 21*m**2 + 146*m + 336) + 2*a*b*c**(5/2)*d**m*m**2*x**2*x**m*(x**2)**(5/2)/(m**3 + 21*m**2 + 146*m + 336) + 28*a*b*c**(5/2)*d**m*m*x**2*x**m*(x**2)**(5/2)/(m**3 + 21*m**2 + 146*m + 336) + 96*a*b*c**(5/2)*d**m*x**2*x**m*(x**2)**(5/2)/(m**3 + 21*m**2 + 146*m + 336) + b**2*c**(5/2)*d**m*m**2*x**3*x**m*(x**2)**(5/2)/(m**3 + 21*m**2 + 146*m + 336) + 13*b**2*c**(5/2)*d**m*m*x**3*x**m*(x**2)**(5/2)/(m**3 + 21*m**2 + 146*m + 336) + 42*b**2*c**(5/2)*d**m*x**3*x**m*(x**2)**(5/2)/(m**3 + 21*m**2 + 146*m + 336), True))

$$3.976 \quad \int (dx)^m (cx^2)^{3/2} (a + bx)^2 dx$$

Optimal. Leaf size=97

$$\frac{a^2c\sqrt{cx^2}(dx)^{m+4}}{d^4(m+4)x} + \frac{2abc\sqrt{cx^2}(dx)^{m+5}}{d^5(m+5)x} + \frac{b^2c\sqrt{cx^2}(dx)^{m+6}}{d^6(m+6)x}$$

[Out] $a^2*c*(d*x)^{(4+m)}*(c*x^2)^{(1/2)}/d^4/(4+m)/x+2*a*b*c*(d*x)^{(5+m)}*(c*x^2)^{(1/2)}/d^5/(5+m)/x+b^2*c*(d*x)^{(6+m)}*(c*x^2)^{(1/2)}/d^6/(6+m)/x$

Rubi [A] time = 0.04, antiderivative size = 97, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$, Rules used = {15, 16, 43}

$$\frac{a^2c\sqrt{cx^2}(dx)^{m+4}}{d^4(m+4)x} + \frac{2abc\sqrt{cx^2}(dx)^{m+5}}{d^5(m+5)x} + \frac{b^2c\sqrt{cx^2}(dx)^{m+6}}{d^6(m+6)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(d*x)^m*(c*x^2)^{(3/2)}*(a + b*x)^2, x]$

[Out] $(a^2*c*(d*x)^{(4 + m)}*\text{Sqrt}[c*x^2])/d^4*(4 + m)*x + (2*a*b*c*(d*x)^{(5 + m)}*\text{Sqrt}[c*x^2])/d^5*(5 + m)*x + (b^2*c*(d*x)^{(6 + m)}*\text{Sqrt}[c*x^2])/d^6*(6 + m)*x$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] := \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}[\{a, m, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 16

$\text{Int}[(u_.)*(v_)^{(m_.)}*((b_.)*(v_))^{(n_)}, x_Symbol] := \text{Dist}[1/b^m, \text{Int}[u*(b*v)^{(m+n)}, x], x] /; \text{FreeQ}[\{b, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}[\{a, b, c, d, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{IGtQ}[m, 0] \&\& (!\text{IntegerQ}[n] || (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0]) || \text{LtQ}[9*m + 5*(n + 1), 0] || \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned}
\int (dx)^m (cx^2)^{3/2} (a + bx)^2 dx &= \frac{(c\sqrt{cx^2}) \int x^3 (dx)^m (a + bx)^2 dx}{x} \\
&= \frac{(c\sqrt{cx^2}) \int (dx)^{3+m} (a + bx)^2 dx}{d^3 x} \\
&= \frac{(c\sqrt{cx^2}) \int \left(a^2 (dx)^{3+m} + \frac{2ab(dx)^{4+m}}{d} + \frac{b^2(dx)^{5+m}}{d^2} \right) dx}{d^3 x} \\
&= \frac{a^2 c (dx)^{4+m} \sqrt{cx^2}}{d^4 (4+m)x} + \frac{2abc(dx)^{5+m} \sqrt{cx^2}}{d^5 (5+m)x} + \frac{b^2 c (dx)^{6+m} \sqrt{cx^2}}{d^6 (6+m)x}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 48, normalized size = 0.49

$$x (cx^2)^{3/2} (dx)^m \left(\frac{a^2}{m+4} + \frac{2abx}{m+5} + \frac{b^2 x^2}{m+6} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^m*(c*x^2)^(3/2)*(a + b*x)^2,x]

[Out] x*(d*x)^m*(c*x^2)^(3/2)*(a^2/(4 + m) + (2*a*b*x)/(5 + m) + (b^2*x^2)/(6 + m))

fricas [A] time = 0.43, size = 105, normalized size = 1.08

$$\frac{((b^2 cm^2 + 9 b^2 cm + 20 b^2 c)x^5 + 2(abc m^2 + 10 abcm + 24 abc)x^4 + (a^2 cm^2 + 11 a^2 cm + 30 a^2 c)x^3)\sqrt{cx^2} (dx)^m}{m^3 + 15 m^2 + 74 m + 120}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] ((b^2*c*m^2 + 9*b^2*c*m + 20*b^2*c)*x^5 + 2*(a*b*c*m^2 + 10*a*b*c*m + 24*a*b*c)*x^4 + (a^2*c*m^2 + 11*a^2*c*m + 30*a^2*c)*x^3)*sqrt(c*x^2)*(d*x)^m/(m^3 + 15*m^2 + 74*m + 120)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
UT:sage2:=int(sage0,x):;OUTPUT:Warning, integration of abs or sign assumes
constant sign by intervals (correct if the argument is real):Check [abs(x)]
Undef/Unsigned Inf encountered in limit

maple [A] time = 0.00, size = 95, normalized size = 0.98

$$\frac{(b^2 m^2 x^2 + 2ab m^2 x + 9b^2 m x^2 + a^2 m^2 + 20abmx + 20b^2 x^2 + 11a^2 m + 48abx + 30a^2) (c x^2)^{\frac{3}{2}} x (dx)^m}{(m+6)(m+5)(m+4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(3/2)*(b*x+a)^2,x)

[Out] x*(b^2*m^2*x^2+2*a*b*m^2*x+9*b^2*m*x^2+a^2*m^2+20*a*b*m*x+20*b^2*x^2+11*a^2
*m+48*a*b*x+30*a^2)*(d*x)^m*(c*x^2)^(3/2)/(m+6)/(m+5)/(m+4)

maxima [A] time = 1.55, size = 64, normalized size = 0.66

$$\frac{b^2 c^{\frac{3}{2}} d^m x^6 x^m}{m+6} + \frac{2abc^{\frac{3}{2}} d^m x^5 x^m}{m+5} + \frac{a^2 c^{\frac{3}{2}} d^m x^4 x^m}{m+4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(3/2)*(b*x+a)^2,x, algorithm="maxima")

[Out] b^2*c^(3/2)*d^m*x^6*x^m/(m+6) + 2*a*b*c^(3/2)*d^m*x^5*x^m/(m+5) + a^2*c
^(3/2)*d^m*x^4*x^m/(m+4)

mupad [B] time = 0.28, size = 121, normalized size = 1.25

$$(dx)^m \left(\frac{a^2 c x^3 \sqrt{c x^2} (m^2 + 11 m + 30)}{m^3 + 15 m^2 + 74 m + 120} + \frac{b^2 c x^5 \sqrt{c x^2} (m^2 + 9 m + 20)}{m^3 + 15 m^2 + 74 m + 120} + \frac{2 a b c x^4 \sqrt{c x^2} (m^2 + 10 m + 24)}{m^3 + 15 m^2 + 74 m + 120} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(3/2)*(a+b*x)^2,x)

[Out] (d*x)^m*((a^2*c*x^3*(c*x^2)^(1/2)*(11*m+m^2+30))/(74*m+15*m^2+m^3+
120) + (b^2*c*x^5*(c*x^2)^(1/2)*(9*m+m^2+20))/(74*m+15*m^2+m^3+
20) + (2*a*b*c*x^4*(c*x^2)^(1/2)*(10*m+m^2+24))/(74*m+15*m^2+m^3+
120))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{\int \frac{a^2(cx^2)^{\frac{3}{2}}}{x^6} dx + \int \frac{b^2(cx^2)^{\frac{3}{2}}}{x^4} dx + \int \frac{2ab(cx^2)^{\frac{3}{2}}}{x^5} dx}{d^6} \\ \frac{\int \frac{a^2(cx^2)^{\frac{3}{2}}}{x^5} dx + \int \frac{b^2(cx^2)^{\frac{3}{2}}}{x^3} dx + \int \frac{2ab(cx^2)^{\frac{3}{2}}}{x^4} dx}{d^5} \\ \frac{\int \frac{a^2(cx^2)^{\frac{3}{2}}}{x^4} dx + \int \frac{b^2(cx^2)^{\frac{3}{2}}}{x^2} dx + \int \frac{2ab(cx^2)^{\frac{3}{2}}}{x^3} dx}{d^4} \\ \frac{a^2c^{\frac{3}{2}}d^m m^2 x x^m (x^2)^{\frac{3}{2}}}{m^3+15m^2+74m+120} + \frac{11a^2c^{\frac{3}{2}}d^m m x x^m (x^2)^{\frac{3}{2}}}{m^3+15m^2+74m+120} + \frac{30a^2c^{\frac{3}{2}}d^m x x^m (x^2)^{\frac{3}{2}}}{m^3+15m^2+74m+120} + \frac{2abc^{\frac{3}{2}}d^m m^2 x^2 x^m (x^2)^{\frac{3}{2}}}{m^3+15m^2+74m+120} + \frac{20abc^{\frac{3}{2}}d^m m x^2 x^m (x^2)^{\frac{3}{2}}}{m^3+15m^2+74m+120} + \frac{48abc^{\frac{3}{2}}d^m x^2 x^m (x^2)^{\frac{3}{2}}}{m^3+15m^2+74m+120} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(c*x**2)**(3/2)*(b*x+a)**2,x)

[Out] Piecewise(((Integral(a**2*(c*x**2)**(3/2)/x**6, x) + Integral(b**2*(c*x**2)**(3/2)/x**4, x) + Integral(2*a*b*(c*x**2)**(3/2)/x**5, x))/d**6, Eq(m, -6)), ((Integral(a**2*(c*x**2)**(3/2)/x**5, x) + Integral(b**2*(c*x**2)**(3/2)/x**3, x) + Integral(2*a*b*(c*x**2)**(3/2)/x**4, x))/d**5, Eq(m, -5)), ((Integral(a**2*(c*x**2)**(3/2)/x**4, x) + Integral(b**2*(c*x**2)**(3/2)/x**2, x) + Integral(2*a*b*(c*x**2)**(3/2)/x**3, x))/d**4, Eq(m, -4)), (a**2*c**(3/2)*d**m*m**2*x*x**m*(x**2)**(3/2)/(m**3 + 15*m**2 + 74*m + 120) + 11*a**2*c**(3/2)*d**m*m*x*x**m*(x**2)**(3/2)/(m**3 + 15*m**2 + 74*m + 120) + 30*a**2*c**(3/2)*d**m*x*x**m*(x**2)**(3/2)/(m**3 + 15*m**2 + 74*m + 120) + 2*a*b*c**(3/2)*d**m*m**2*x**2*x**m*(x**2)**(3/2)/(m**3 + 15*m**2 + 74*m + 120) + 20*a*b*c**(3/2)*d**m*m*x**2*x**m*(x**2)**(3/2)/(m**3 + 15*m**2 + 74*m + 120) + 48*a*b*c**(3/2)*d**m*x**2*x**m*(x**2)**(3/2)/(m**3 + 15*m**2 + 74*m + 120) + b**2*c**(3/2)*d**m*m**2*x**3*x**m*(x**2)**(3/2)/(m**3 + 15*m**2 + 74*m + 120) + 9*b**2*c**(3/2)*d**m*m*x**3*x**m*(x**2)**(3/2)/(m**3 + 15*m**2 + 74*m + 120) + 20*b**2*c**(3/2)*d**m*x**3*x**m*(x**2)**(3/2)/(m**3 + 15*m**2 + 74*m + 120), True))

3.977 $\int (dx)^m \sqrt{cx^2} (a + bx)^2 dx$

Optimal. Leaf size=94

$$\frac{a^2 \sqrt{cx^2} (dx)^{m+2}}{d^2(m+2)x} + \frac{2ab \sqrt{cx^2} (dx)^{m+3}}{d^3(m+3)x} + \frac{b^2 \sqrt{cx^2} (dx)^{m+4}}{d^4(m+4)x}$$

[Out] $a^2(d*x)^{(2+m)}*(c*x^2)^{(1/2)}/d^2/(2+m)/x+2*a*b*(d*x)^{(3+m)}*(c*x^2)^{(1/2)}/d^3/(3+m)/x+b^2*(d*x)^{(4+m)}*(c*x^2)^{(1/2)}/d^4/(4+m)/x$

Rubi [A] time = 0.04, antiderivative size = 94, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$, Rules used = {15, 16, 43}

$$\frac{a^2 \sqrt{cx^2} (dx)^{m+2}}{d^2(m+2)x} + \frac{2ab \sqrt{cx^2} (dx)^{m+3}}{d^3(m+3)x} + \frac{b^2 \sqrt{cx^2} (dx)^{m+4}}{d^4(m+4)x}$$

Antiderivative was successfully verified.

[In] Int[(d*x)^m*Sqrt[c*x^2]*(a + b*x)^2,x]

[Out] $(a^2*(d*x)^{(2+m)}*Sqrt[c*x^2])/d^2*(2+m)*x + (2*a*b*(d*x)^{(3+m)}*Sqrt[c*x^2])/d^3*(3+m)*x + (b^2*(d*x)^{(4+m)}*Sqrt[c*x^2])/d^4*(4+m)*x$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_))^(n_), x_Symbol] := Dist[1/b^m, Int[u*(b*v)^(m+n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int (dx)^m \sqrt{cx^2} (a + bx)^2 dx &= \frac{\sqrt{cx^2} \int x(dx)^m (a + bx)^2 dx}{x} \\
&= \frac{\sqrt{cx^2} \int (dx)^{1+m} (a + bx)^2 dx}{dx} \\
&= \frac{\sqrt{cx^2} \int \left(a^2(dx)^{1+m} + \frac{2ab(dx)^{2+m}}{d} + \frac{b^2(dx)^{3+m}}{d^2} \right) dx}{dx} \\
&= \frac{a^2(dx)^{2+m} \sqrt{cx^2}}{d^2(2+m)x} + \frac{2ab(dx)^{3+m} \sqrt{cx^2}}{d^3(3+m)x} + \frac{b^2(dx)^{4+m} \sqrt{cx^2}}{d^4(4+m)x}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 72, normalized size = 0.77

$$\frac{x\sqrt{cx^2} (dx)^m \left(a^2 (m^2 + 7m + 12) + 2ab (m^2 + 6m + 8)x + b^2 (m^2 + 5m + 6)x^2 \right)}{(m+2)(m+3)(m+4)}$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^m*Sqrt[c*x^2]*(a + b*x)^2,x]

[Out] (x*(d*x)^m*Sqrt[c*x^2]*(a^2*(12 + 7*m + m^2) + 2*a*b*(8 + 6*m + m^2)*x + b^2*(6 + 5*m + m^2)*x^2))/((2 + m)*(3 + m)*(4 + m))

fricas [A] time = 0.47, size = 94, normalized size = 1.00

$$\frac{\left((b^2 m^2 + 5 b^2 m + 6 b^2) x^3 + 2 (ab m^2 + 6 ab m + 8 ab) x^2 + (a^2 m^2 + 7 a^2 m + 12 a^2) x \right) \sqrt{cx^2} (dx)^m}{m^3 + 9 m^2 + 26 m + 24}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(1/2)*(b*x+a)^2,x, algorithm="fricas")

[Out] ((b^2*m^2 + 5*b^2*m + 6*b^2)*x^3 + 2*(a*b*m^2 + 6*a*b*m + 8*a*b)*x^2 + (a^2*m^2 + 7*a^2*m + 12*a^2)*x)*sqrt(c*x^2)*(d*x)^m/(m^3 + 9*m^2 + 26*m + 24)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(1/2)*(b*x+a)^2,x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
 UT:sage2:=int(sage0,x);;OUTPUT:Warning, integration of abs or sign assumes
 constant sign by intervals (correct if the argument is real):Check [abs(x)]
 Undef/Unsigned Inf encountered in limit

maple [A] time = 0.00, size = 95, normalized size = 1.01

$$\frac{(b^2 m^2 x^2 + 2ab m^2 x + 5b^2 m x^2 + a^2 m^2 + 12abmx + 6b^2 x^2 + 7a^2 m + 16abx + 12a^2) \sqrt{c x^2} x (dx)^m}{(m+4)(m+3)(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(1/2)*(b*x+a)^2,x)

[Out] x*(b^2*m^2*x^2+2*a*b*m^2*x+5*b^2*m*x^2+a^2*m^2+12*a*b*m*x+6*b^2*x^2+7*a^2*m+16*a*b*x+12*a^2)*(d*x)^m*(c*x^2)^(1/2)/(m+4)/(m+3)/(m+2)

maxima [A] time = 1.52, size = 64, normalized size = 0.68

$$\frac{b^2 \sqrt{c} d^m x^4 x^m}{m+4} + \frac{2ab \sqrt{c} d^m x^3 x^m}{m+3} + \frac{a^2 \sqrt{c} d^m x^2 x^m}{m+2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(1/2)*(b*x+a)^2,x, algorithm="maxima")

[Out] b^2*sqrt(c)*d^m*x^4*x^m/(m+4) + 2*a*b*sqrt(c)*d^m*x^3*x^m/(m+3) + a^2*sqrt(c)*d^m*x^2*x^m/(m+2)

mupad [B] time = 0.26, size = 116, normalized size = 1.23

$$(dx)^m \left(\frac{a^2 x \sqrt{c x^2} (m^2 + 7m + 12)}{m^3 + 9m^2 + 26m + 24} + \frac{b^2 x^3 \sqrt{c x^2} (m^2 + 5m + 6)}{m^3 + 9m^2 + 26m + 24} + \frac{2abx^2 \sqrt{c x^2} (m^2 + 6m + 8)}{m^3 + 9m^2 + 26m + 24} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(1/2)*(a + b*x)^2,x)

[Out] (d*x)^m*((a^2*x*(c*x^2)^(1/2)*(7*m + m^2 + 12))/(26*m + 9*m^2 + m^3 + 24) + (b^2*x^3*(c*x^2)^(1/2)*(5*m + m^2 + 6))/(26*m + 9*m^2 + m^3 + 24) + (2*a*b*x^2*(c*x^2)^(1/2)*(6*m + m^2 + 8))/(26*m + 9*m^2 + m^3 + 24))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{\int \frac{a^2 \sqrt{cx^2}}{x^4} dx + \int \frac{b^2 \sqrt{cx^2}}{x^2} dx + \int \frac{2ab \sqrt{cx^2}}{x^3} dx}{d^4} \\ \frac{\int \frac{a^2 \sqrt{cx^2}}{x^3} dx + \int \frac{b^2 \sqrt{cx^2}}{x} dx + \int \frac{2ab \sqrt{cx^2}}{x^2} dx}{d^3} \\ \frac{\int b^2 \sqrt{cx^2} dx + \int \frac{a^2 \sqrt{cx^2}}{x^2} dx + \int \frac{2ab \sqrt{cx^2}}{x} dx}{d^2} \\ \frac{a^2 \sqrt{c} d^m m^2 x x^m \sqrt{x^2}}{m^3 + 9m^2 + 26m + 24} + \frac{7a^2 \sqrt{c} d^m m x x^m \sqrt{x^2}}{m^3 + 9m^2 + 26m + 24} + \frac{12a^2 \sqrt{c} d^m x x^m \sqrt{x^2}}{m^3 + 9m^2 + 26m + 24} + \frac{2ab \sqrt{c} d^m m^2 x^2 x^m \sqrt{x^2}}{m^3 + 9m^2 + 26m + 24} + \frac{12ab \sqrt{c} d^m m x^2 x^m \sqrt{x^2}}{m^3 + 9m^2 + 26m + 24} + \frac{16ab \sqrt{c} d^m x^2 x^m \sqrt{x^2}}{m^3 + 9m^2 + 26m + 24} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(c*x**2)**(1/2)*(b*x+a)**2,x)

[Out] Piecewise(((Integral(a**2*sqrt(c*x**2)/x**4, x) + Integral(b**2*sqrt(c*x**2)/x**2, x) + Integral(2*a*b*sqrt(c*x**2)/x**3, x))/d**4, Eq(m, -4)), ((Integral(a**2*sqrt(c*x**2)/x**3, x) + Integral(b**2*sqrt(c*x**2)/x, x) + Integral(2*a*b*sqrt(c*x**2)/x**2, x))/d**3, Eq(m, -3)), ((Integral(b**2*sqrt(c*x**2), x) + Integral(a**2*sqrt(c*x**2)/x**2, x) + Integral(2*a*b*sqrt(c*x**2)/x, x))/d**2, Eq(m, -2)), (a**2*sqrt(c)*d**m*m**2*x*x**m*sqrt(x**2)/(m**3 + 9*m**2 + 26*m + 24) + 7*a**2*sqrt(c)*d**m*m*x*x**m*sqrt(x**2)/(m**3 + 9*m**2 + 26*m + 24) + 12*a**2*sqrt(c)*d**m*x*x**m*sqrt(x**2)/(m**3 + 9*m**2 + 26*m + 24) + 2*a*b*sqrt(c)*d**m*m**2*x**2*x**m*sqrt(x**2)/(m**3 + 9*m**2 + 26*m + 24) + 12*a*b*sqrt(c)*d**m*m*x**2*x**m*sqrt(x**2)/(m**3 + 9*m**2 + 26*m + 24) + 16*a*b*sqrt(c)*d**m*x**2*x**m*sqrt(x**2)/(m**3 + 9*m**2 + 26*m + 24) + b**2*sqrt(c)*d**m*m**2*x**3*x**m*sqrt(x**2)/(m**3 + 9*m**2 + 26*m + 24) + 5*b**2*sqrt(c)*d**m*m*x**3*x**m*sqrt(x**2)/(m**3 + 9*m**2 + 26*m + 24) + 6*b**2*sqrt(c)*d**m*x**3*x**m*sqrt(x**2)/(m**3 + 9*m**2 + 26*m + 24), True))

$$3.978 \quad \int \frac{(dx)^m (a+bx)^2}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=81

$$\frac{a^2 x (dx)^m}{m \sqrt{cx^2}} + \frac{2abx (dx)^{m+1}}{d(m+1) \sqrt{cx^2}} + \frac{b^2 x (dx)^{m+2}}{d^2(m+2) \sqrt{cx^2}}$$

[Out] $a^2 x (d x)^m / m / (c x^2)^{(1/2)} + 2 a b x (d x)^{(1+m)} / d / (1+m) / (c x^2)^{(1/2)} + b^2 x (d x)^{(2+m)} / d^2 / (2+m) / (c x^2)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$, Rules used = {15, 16, 43}

$$\frac{a^2 x (dx)^m}{m \sqrt{cx^2}} + \frac{2abx (dx)^{m+1}}{d(m+1) \sqrt{cx^2}} + \frac{b^2 x (dx)^{m+2}}{d^2(m+2) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[((d*x)^m*(a + b*x)^2)/Sqrt[c*x^2], x]

[Out] $(a^2 x (d x)^m) / (m \sqrt{c x^2}) + (2 a b x (d x)^{(1+m)}) / (d (1+m) \sqrt{c x^2}) + (b^2 x (d x)^{(2+m)}) / (d^2 (2+m) \sqrt{c x^2})$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_)^(n_)), x_Symbol] := Dist[1/b^m, Int[u*(b*v)^(m+n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(dx)^m (a + bx)^2}{\sqrt{cx^2}} dx &= \frac{x \int \frac{(dx)^m (a+bx)^2}{x} dx}{\sqrt{cx^2}} \\
&= \frac{(dx) \int (dx)^{-1+m} (a + bx)^2 dx}{\sqrt{cx^2}} \\
&= \frac{(dx) \int \left(a^2 (dx)^{-1+m} + \frac{2ab(dx)^m}{d} + \frac{b^2(dx)^{1+m}}{d^2} \right) dx}{\sqrt{cx^2}} \\
&= \frac{a^2 x (dx)^m}{m \sqrt{cx^2}} + \frac{2abx(dx)^{1+m}}{d(1+m)\sqrt{cx^2}} + \frac{b^2 x (dx)^{2+m}}{d^2(2+m)\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 62, normalized size = 0.77

$$\frac{x(dx)^m \left(a^2 (m^2 + 3m + 2) + 2abm(m + 2)x + b^2 m(m + 1)x^2 \right)}{m(m + 1)(m + 2)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Integrate[((d*x)^m*(a + b*x)^2)/Sqrt[c*x^2], x]

[Out] (x*(d*x)^m*(a^2*(2 + 3*m + m^2) + 2*a*b*m*(2 + m)*x + b^2*m*(1 + m)*x^2))/(m*(1 + m)*(2 + m)*Sqrt[c*x^2])

fricas [A] time = 0.45, size = 85, normalized size = 1.05

$$\frac{(a^2 m^2 + 3 a^2 m + (b^2 m^2 + b^2 m)x^2 + 2 a^2 + 2 (abm^2 + 2 abm)x)\sqrt{cx^2} (dx)^m}{(cm^3 + 3 cm^2 + 2 cm)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^2/(c*x^2)^(1/2), x, algorithm="fricas")

[Out] (a^2*m^2 + 3*a^2*m + (b^2*m^2 + b^2*m)*x^2 + 2*a^2 + 2*(a*b*m^2 + 2*a*b*m)*x)*sqrt(c*x^2)*(d*x)^m/((c*m^3 + 3*c*m^2 + 2*c*m)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^2 (dx)^m}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="giac")

[Out] integrate((b*x + a)^2*(d*x)^m/sqrt(c*x^2), x)

maple [A] time = 0.00, size = 79, normalized size = 0.98

$$\frac{(b^2 m^2 x^2 + 2ab m^2 x + b^2 m x^2 + a^2 m^2 + 4abmx + 3a^2 m + 2a^2) x (dx)^m}{(m+2)(m+1) \sqrt{c x^2} m}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(b*x+a)^2/(c*x^2)^(1/2),x)

[Out] x*(b^2*m^2*x^2+2*a*b*m^2*x+b^2*m*x^2+a^2*m^2+4*a*b*m*x+3*a^2*m+2*a^2)*(d*x)^m/(m+2)/(m+1)/m/(c*x^2)^(1/2)

maxima [A] time = 1.64, size = 57, normalized size = 0.70

$$\frac{b^2 d^m x^2 x^m}{\sqrt{c} (m+2)} + \frac{2 ab d^m x x^m}{\sqrt{c} (m+1)} + \frac{a^2 d^m x^m}{\sqrt{c} m}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^2/(c*x^2)^(1/2),x, algorithm="maxima")

[Out] b^2*d^m*x^2*x^m/(sqrt(c)*(m+2)) + 2*a*b*d^m*x*x^m/(sqrt(c)*(m+1)) + a^2*d^m*x^m/(sqrt(c)*m)

mupad [B] time = 0.26, size = 62, normalized size = 0.77

$$\frac{(dx)^m \left(\frac{a^2 x}{m} + \frac{b^2 x^3 (m+1)}{m^2+3m+2} + \frac{2abx^2(m+2)}{m^2+3m+2} \right)}{\sqrt{c x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((d*x)^m*(a + b*x)^2)/(c*x^2)^(1/2),x)

[Out] ((d*x)^m*((a^2*x)/m + (b^2*x^3*(m+1))/(3*m + m^2 + 2) + (2*a*b*x^2*(m+2))/(3*m + m^2 + 2)))/(c*x^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{\int \frac{b^2}{\sqrt{cx^2}} dx + \int \frac{a^2}{x^2 \sqrt{cx^2}} dx + \int \frac{2ab}{x \sqrt{cx^2}} dx}{d^2} \\ \frac{\int \frac{2ab}{\sqrt{cx^2}} dx + \int \frac{a^2}{x \sqrt{cx^2}} dx + \int \frac{b^2 x}{\sqrt{cx^2}} dx}{d} \\ \int \frac{(a+bx)^2}{\sqrt{cx^2}} dx \end{array} \right.$$

$$\frac{a^2 d^m m^2 x^m}{\sqrt{c} m^3 \sqrt{x^2} + 3\sqrt{c} m^2 \sqrt{x^2} + 2\sqrt{c} m \sqrt{x^2}} + \frac{3a^2 d^m m x^m}{\sqrt{c} m^3 \sqrt{x^2} + 3\sqrt{c} m^2 \sqrt{x^2} + 2\sqrt{c} m \sqrt{x^2}} + \frac{2a^2 d^m x^m}{\sqrt{c} m^3 \sqrt{x^2} + 3\sqrt{c} m^2 \sqrt{x^2} + 2\sqrt{c} m \sqrt{x^2}} + \frac{2abd^m m}{\sqrt{c} m^3 \sqrt{x^2} + 3\sqrt{c} m^2 \sqrt{x^2} + 2\sqrt{c} m \sqrt{x^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(b*x+a)**2/(c*x**2)**(1/2),x)

[Out] Piecewise(((Integral(b**2/sqrt(c*x**2), x) + Integral(a**2/(x**2*sqrt(c*x**2)), x) + Integral(2*a*b/(x*sqrt(c*x**2)), x))/d**2, Eq(m, -2)), ((Integral(2*a*b/sqrt(c*x**2), x) + Integral(a**2/(x*sqrt(c*x**2)), x) + Integral(b**2*x/sqrt(c*x**2), x))/d, Eq(m, -1)), (Integral((a + b*x)**2/sqrt(c*x**2), x), Eq(m, 0)), (a**2*d**m*m**2*x*x**m/(sqrt(c)*m**3*sqrt(x**2) + 3*sqrt(c)*m**2*sqrt(x**2) + 2*sqrt(c)*m*sqrt(x**2)) + 3*a**2*d**m*m*x*x**m/(sqrt(c)*m**3*sqrt(x**2) + 3*sqrt(c)*m**2*sqrt(x**2) + 2*sqrt(c)*m*sqrt(x**2)) + 2*a**2*d**m*x*x**m/(sqrt(c)*m**3*sqrt(x**2) + 3*sqrt(c)*m**2*sqrt(x**2) + 2*sqrt(c)*m*sqrt(x**2)) + 2*a*b*d**m*m**2*x**2*x**m/(sqrt(c)*m**3*sqrt(x**2) + 3*sqrt(c)*m**2*sqrt(x**2) + 2*sqrt(c)*m*sqrt(x**2)) + 4*a*b*d**m*m*x**2*x**m/(sqrt(c)*m**3*sqrt(x**2) + 3*sqrt(c)*m**2*sqrt(x**2) + 2*sqrt(c)*m*sqrt(x**2)) + b**2*d**m*m**2*x**3*x**m/(sqrt(c)*m**3*sqrt(x**2) + 3*sqrt(c)*m**2*sqrt(x**2) + 2*sqrt(c)*m*sqrt(x**2)) + b**2*d**m*m*x**3*x**m/(sqrt(c)*m**3*sqrt(x**2) + 3*sqrt(c)*m**2*sqrt(x**2) + 2*sqrt(c)*m*sqrt(x**2))), True))

$$3.979 \quad \int \frac{(dx)^m (a+bx)^2}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=93

$$-\frac{a^2 d^2 x (dx)^{m-2}}{c(2-m)\sqrt{cx^2}} - \frac{2abd x (dx)^{m-1}}{c(1-m)\sqrt{cx^2}} + \frac{b^2 x (dx)^m}{cm\sqrt{cx^2}}$$

[Out] $-a^2 d^2 x^m (d*x)^{-2+m} / c / (2-m) / (c*x^2)^{(1/2)} - 2*a*b*d*x^m (d*x)^{-1+m} / c / (1-m) / (c*x^2)^{(1/2)} + b^2*x^m (d*x)^m / c / m / (c*x^2)^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$, Rules used = {15, 16, 43}

$$-\frac{a^2 d^2 x (dx)^{m-2}}{c(2-m)\sqrt{cx^2}} - \frac{2abd x (dx)^{m-1}}{c(1-m)\sqrt{cx^2}} + \frac{b^2 x (dx)^m}{cm\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[((d*x)^m*(a + b*x)^2)/(c*x^2)^(3/2), x]

[Out] $-((a^2*d^2*x^m*(d*x)^{-2+m})/(c*(2-m)*\text{Sqrt}[c*x^2])) - (2*a*b*d*x^m*(d*x)^{-1+m})/(c*(1-m)*\text{Sqrt}[c*x^2]) + (b^2*x^m*(d*x)^m)/(c*m*\text{Sqrt}[c*x^2])$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_))^(n_), x_Symbol] := Dist[1/b^m, Int[u*(b*v)^(m+n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(dx)^m (a + bx)^2}{(cx^2)^{3/2}} dx &= \frac{x \int \frac{(dx)^m (a+bx)^2}{x^3} dx}{c\sqrt{cx^2}} \\
&= \frac{(d^3 x) \int (dx)^{-3+m} (a + bx)^2 dx}{c\sqrt{cx^2}} \\
&= \frac{(d^3 x) \int \left(a^2 (dx)^{-3+m} + \frac{2ab(dx)^{-2+m}}{d} + \frac{b^2(dx)^{-1+m}}{d^2} \right) dx}{c\sqrt{cx^2}} \\
&= -\frac{a^2 d^2 x (dx)^{-2+m}}{c(2-m)\sqrt{cx^2}} - \frac{2abd x (dx)^{-1+m}}{c(1-m)\sqrt{cx^2}} + \frac{b^2 x (dx)^m}{cm\sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 62, normalized size = 0.67

$$\frac{x(dx)^m \left(a^2(m-1)m + 2ab(m-2)mx + b^2(m^2 - 3m + 2)x^2 \right)}{(m-2)(m-1)m (cx^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[((d*x)^m*(a + b*x)^2)/(c*x^2)^(3/2), x]

[Out] (x*(d*x)^m*(a^2*(-1 + m)*m + 2*a*b*(-2 + m)*m*x + b^2*(2 - 3*m + m^2)*x^2))/((-2 + m)*(-1 + m)*m*(c*x^2)^(3/2))

fricas [A] time = 0.51, size = 92, normalized size = 0.99

$$\frac{(a^2 m^2 - a^2 m + (b^2 m^2 - 3 b^2 m + 2 b^2) x^2 + 2 (ab m^2 - 2 ab m) x) \sqrt{cx^2} (dx)^m}{(c^2 m^3 - 3 c^2 m^2 + 2 c^2 m) x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^2/(c*x^2)^(3/2), x, algorithm="fricas")

[Out] (a^2*m^2 - a^2*m + (b^2*m^2 - 3*b^2*m + 2*b^2)*x^2 + 2*(a*b*m^2 - 2*a*b*m)*x)*sqrt(c*x^2)*(d*x)^m/((c^2*m^3 - 3*c^2*m^2 + 2*c^2*m)*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^2 (dx)^m}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^2/(c*x^2)^(3/2),x, algorithm="giac")

[Out] integrate((b*x + a)^2*(d*x)^m/(c*x^2)^(3/2), x)

maple [A] time = 0.01, size = 83, normalized size = 0.89

$$\frac{(b^2 m^2 x^2 + 2ab m^2 x - 3b^2 m x^2 + a^2 m^2 - 4abmx + 2b^2 x^2 - a^2 m) x (dx)^m}{(m-1)(m-2)(c x^2)^{\frac{3}{2}} m}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(b*x+a)^2/(c*x^2)^(3/2),x)

[Out] x*(b^2*m^2*x^2+2*a*b*m^2*x-3*b^2*m*x^2+a^2*m^2-4*a*b*m*x+2*b^2*x^2-a^2*m)*(d*x)^m/m/(m-1)/(m-2)/(c*x^2)^(3/2)

maxima [A] time = 1.58, size = 59, normalized size = 0.63

$$\frac{b^2 d^m x^m}{c^{\frac{3}{2}} m} + \frac{2abd^m x^m}{c^{\frac{3}{2}}(m-1)x} + \frac{a^2 d^m x^m}{c^{\frac{3}{2}}(m-2)x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^2/(c*x^2)^(3/2),x, algorithm="maxima")

[Out] b^2*d^m*x^m/(c^(3/2)*m) + 2*a*b*d^m*x^m/(c^(3/2)*(m-1)*x) + a^2*d^m*x^m/(c^(3/2)*(m-2)*x^2)

mupad [B] time = 0.32, size = 66, normalized size = 0.71

$$\frac{a^2 (dx)^m}{c x \sqrt{c x^2} (m-2)} + \frac{b (dx)^m (2 a m - b x + b m x)}{c m \sqrt{c x^2} (m-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((d*x)^m*(a + b*x)^2)/(c*x^2)^(3/2),x)

[Out] (a^2*(d*x)^m)/(c*x*(c*x^2)^(1/2)*(m-2)) + (b*(d*x)^m*(2*a*m - b*x + b*m*x))/(c*m*(c*x^2)^(1/2)*(m-1))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \int \frac{(a+bx)^2}{(cx^2)^{\frac{3}{2}}} dx \\ d \left(\int \frac{a^2x}{(cx^2)^{\frac{3}{2}}} dx + \int \frac{b^2x^3}{(cx^2)^{\frac{3}{2}}} dx + \int \frac{2abx^2}{(cx^2)^{\frac{3}{2}}} dx \right) \\ d^2 \left(\int \frac{a^2x^2}{(cx^2)^{\frac{3}{2}}} dx + \int \frac{b^2x^4}{(cx^2)^{\frac{3}{2}}} dx + \int \frac{2abx^3}{(cx^2)^{\frac{3}{2}}} dx \right) \\ \frac{a^2d^m m^2 x x^m}{c^{\frac{3}{2}} m^3 (x^2)^{\frac{3}{2}} - 3c^{\frac{3}{2}} m^2 (x^2)^{\frac{3}{2}} + 2c^{\frac{3}{2}} m (x^2)^{\frac{3}{2}}} - \frac{a^2 d^m m x x^m}{c^{\frac{3}{2}} m^3 (x^2)^{\frac{3}{2}} - 3c^{\frac{3}{2}} m^2 (x^2)^{\frac{3}{2}} + 2c^{\frac{3}{2}} m (x^2)^{\frac{3}{2}}} + \frac{2abd^m m^2 x^2 x^m}{c^{\frac{3}{2}} m^3 (x^2)^{\frac{3}{2}} - 3c^{\frac{3}{2}} m^2 (x^2)^{\frac{3}{2}} + 2c^{\frac{3}{2}} m (x^2)^{\frac{3}{2}}} - \frac{4}{c^{\frac{3}{2}} m^3 (x^2)^{\frac{3}{2}} - 3c^{\frac{3}{2}} m^2 (x^2)^{\frac{3}{2}} + 2c^{\frac{3}{2}} m (x^2)^{\frac{3}{2}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(b*x+a)**2/(c*x**2)**(3/2), x)

[Out] Piecewise((Integral((a + b*x)**2/(c*x**2)**(3/2), x), Eq(m, 0)), (d*(Integral(a**2*x/(c*x**2)**(3/2), x) + Integral(b**2*x**3/(c*x**2)**(3/2), x) + Integral(2*a*b*x**2/(c*x**2)**(3/2), x)), Eq(m, 1)), (d**2*(Integral(a**2*x**2/(c*x**2)**(3/2), x) + Integral(b**2*x**4/(c*x**2)**(3/2), x) + Integral(2*a*b*x**3/(c*x**2)**(3/2), x)), Eq(m, 2)), (a**2*d**m*m**2*x*x**m/(c**(3/2)*m**3*(x**2)**(3/2) - 3*c**(3/2)*m**2*(x**2)**(3/2) + 2*c**(3/2)*m*(x**2)**(3/2)) - a**2*d**m*m*x*x**m/(c**(3/2)*m**3*(x**2)**(3/2) - 3*c**(3/2)*m**2*(x**2)**(3/2) + 2*c**(3/2)*m*(x**2)**(3/2)) + 2*a*b*d**m*m**2*x**2*x**m/(c*(3/2)*m**3*(x**2)**(3/2) - 3*c**(3/2)*m**2*(x**2)**(3/2) + 2*c**(3/2)*m*(x**2)**(3/2)) - 4*a*b*d**m*m*x**2*x**m/(c**(3/2)*m**3*(x**2)**(3/2) - 3*c**(3/2)*m**2*(x**2)**(3/2) + 2*c**(3/2)*m*(x**2)**(3/2)) + b**2*d**m*m**2*x**3*x**m/(c**(3/2)*m**3*(x**2)**(3/2) - 3*c**(3/2)*m**2*(x**2)**(3/2) + 2*c**(3/2)*m*(x**2)**(3/2)) - 3*b**2*d**m*m*x**3*x**m/(c**(3/2)*m**3*(x**2)**(3/2) - 3*c**(3/2)*m**2*(x**2)**(3/2) + 2*c**(3/2)*m*(x**2)**(3/2)) + 2*b**2*d**m*x**3*x**m/(c**(3/2)*m**3*(x**2)**(3/2) - 3*c**(3/2)*m**2*(x**2)**(3/2) + 2*c**(3/2)*m*(x**2)**(3/2)), True))

$$3.980 \quad \int \frac{(dx)^m (a+bx)^2}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=105

$$\frac{a^2 d^4 x (dx)^{m-4}}{c^2 (4-m) \sqrt{cx^2}} - \frac{2abd^3 x (dx)^{m-3}}{c^2 (3-m) \sqrt{cx^2}} - \frac{b^2 d^2 x (dx)^{m-2}}{c^2 (2-m) \sqrt{cx^2}}$$

[Out] $-a^2 d^4 x (dx)^{m-4} / c^2 / (4-m) / (c x^2)^{(1/2)} - 2 a b d^3 x (dx)^{m-3} / c^2 / (3-m) / (c x^2)^{(1/2)} - b^2 d^2 x (dx)^{m-2} / c^2 / (2-m) / (c x^2)^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 105, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$, Rules used = {15, 16, 43}

$$\frac{a^2 d^4 x (dx)^{m-4}}{c^2 (4-m) \sqrt{cx^2}} - \frac{2abd^3 x (dx)^{m-3}}{c^2 (3-m) \sqrt{cx^2}} - \frac{b^2 d^2 x (dx)^{m-2}}{c^2 (2-m) \sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[((d*x)^m*(a + b*x)^2)/(c*x^2)^(5/2), x]

[Out] $-((a^2 d^4 x (dx)^{m-4} / (c^2 (4-m) \sqrt{cx^2})) - (2 a b d^3 x (dx)^{m-3} / (c^2 (3-m) \sqrt{cx^2})) - (b^2 d^2 x (dx)^{m-2} / (c^2 (2-m) \sqrt{cx^2})))$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_)^(n_)), x_Symbol] := Dist[1/b^m, Int[u*(b*v)^(m+n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int \frac{(dx)^m (a + bx)^2}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{(dx)^m (a+bx)^2}{x^5} dx}{c^2 \sqrt{cx^2}} \\
&= \frac{(d^5 x) \int (dx)^{-5+m} (a + bx)^2 dx}{c^2 \sqrt{cx^2}} \\
&= \frac{(d^5 x) \int \left(a^2 (dx)^{-5+m} + \frac{2ab(dx)^{-4+m}}{d} + \frac{b^2(dx)^{-3+m}}{d^2} \right) dx}{c^2 \sqrt{cx^2}} \\
&= -\frac{a^2 d^4 x (dx)^{-4+m}}{c^2 (4-m) \sqrt{cx^2}} - \frac{2abd^3 x (dx)^{-3+m}}{c^2 (3-m) \sqrt{cx^2}} - \frac{b^2 d^2 x (dx)^{-2+m}}{c^2 (2-m) \sqrt{cx^2}}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 72, normalized size = 0.69

$$\frac{x(dx)^m \left(a^2 (m^2 - 5m + 6) + 2ab (m^2 - 6m + 8)x + b^2 (m^2 - 7m + 12)x^2 \right)}{(m-4)(m-3)(m-2)(cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[((d*x)^m*(a + b*x)^2)/(c*x^2)^(5/2), x]

[Out] (x*(d*x)^m*(a^2*(6 - 5*m + m^2) + 2*a*b*(8 - 6*m + m^2)*x + b^2*(12 - 7*m + m^2)*x^2))/((-4 + m)*(-3 + m)*(-2 + m)*(c*x^2)^(5/2))

fricas [A] time = 0.48, size = 106, normalized size = 1.01

$$\frac{(a^2 m^2 - 5 a^2 m + (b^2 m^2 - 7 b^2 m + 12 b^2) x^2 + 6 a^2 + 2 (ab m^2 - 6 ab m + 8 ab) x) \sqrt{cx^2} (dx)^m}{(c^3 m^3 - 9 c^3 m^2 + 26 c^3 m - 24 c^3) x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^2/(c*x^2)^(5/2), x, algorithm="fricas")

[Out] (a^2*m^2 - 5*a^2*m + (b^2*m^2 - 7*b^2*m + 12*b^2)*x^2 + 6*a^2 + 2*(a*b*m^2 - 6*a*b*m + 8*a*b)*x)*sqrt(c*x^2)*(d*x)^m/((c^3*m^3 - 9*c^3*m^2 + 26*c^3*m - 24*c^3)*x^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^2 (dx)^m}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^2/(c*x^2)^(5/2),x, algorithm="giac")

[Out] integrate((b*x + a)^2*(d*x)^m/(c*x^2)^(5/2), x)

maple [A] time = 0.01, size = 95, normalized size = 0.90

$$\frac{(b^2 m^2 x^2 + 2ab m^2 x - 7b^2 m x^2 + a^2 m^2 - 12abmx + 12b^2 x^2 - 5a^2 m + 16abx + 6a^2) x (dx)^m}{(m-2)(m-3)(m-4)(cx^2)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(b*x+a)^2/(c*x^2)^(5/2),x)

[Out] x*(b^2*m^2*x^2+2*a*b*m^2*x-7*b^2*m*x^2+a^2*m^2-12*a*b*m*x+12*b^2*x^2-5*a^2*m+16*a*b*x+6*a^2)*(d*x)^m/(m-2)/(m-3)/(m-4)/(c*x^2)^(5/2)

maxima [A] time = 1.57, size = 64, normalized size = 0.61

$$\frac{b^2 d^m x^m}{c^{\frac{5}{2}} (m-2) x^2} + \frac{2abd^m x^m}{c^{\frac{5}{2}} (m-3) x^3} + \frac{a^2 d^m x^m}{c^{\frac{5}{2}} (m-4) x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^2/(c*x^2)^(5/2),x, algorithm="maxima")

[Out] b^2*d^m*x^m/(c^(5/2)*(m-2)*x^2) + 2*a*b*d^m*x^m/(c^(5/2)*(m-3)*x^3) + a^2*d^m*x^m/(c^(5/2)*(m-4)*x^4)

mupad [B] time = 0.34, size = 82, normalized size = 0.78

$$\frac{a^2 (dx)^m}{c^2 x^3 \sqrt{cx^2} (m-4)} + \frac{b^2 (dx)^m}{c^2 x \sqrt{cx^2} (m-2)} + \frac{2ab (dx)^m}{c^2 x^2 \sqrt{cx^2} (m-3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((d*x)^m*(a + b*x)^2)/(c*x^2)^(5/2),x)

[Out] (a^2*(d*x)^m)/(c^2*x^3*(c*x^2)^(1/2)*(m-4)) + (b^2*(d*x)^m)/(c^2*x*(c*x^2)^(1/2)*(m-2)) + (2*a*b*(d*x)^m)/(c^2*x^2*(c*x^2)^(1/2)*(m-3))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(b*x+a)**2/(c*x**2)**(5/2),x)

[Out] Piecewise((d**2*(Integral(a**2*x**2/(c*x**2)**(5/2), x) + Integral(b**2*x**4/(c*x**2)**(5/2), x) + Integral(2*a*b*x**3/(c*x**2)**(5/2), x)), Eq(m, 2)), (d**3*(Integral(a**2*x**3/(c*x**2)**(5/2), x) + Integral(b**2*x**5/(c*x**2)**(5/2), x) + Integral(2*a*b*x**4/(c*x**2)**(5/2), x)), Eq(m, 3)), (d**4*(Integral(a**2*x**4/(c*x**2)**(5/2), x) + Integral(b**2*x**6/(c*x**2)**(5/2), x) + Integral(2*a*b*x**5/(c*x**2)**(5/2), x)), Eq(m, 4)), (a**2*d**m*m**2*x*x**m/(c**(5/2)*m**3*(x**2)**(5/2) - 9*c**(5/2)*m**2*(x**2)**(5/2) + 26*c**(5/2)*m*(x**2)**(5/2) - 24*c**(5/2)*(x**2)**(5/2)) - 5*a**2*d**m*m*x*x**m/(c**(5/2)*m**3*(x**2)**(5/2) - 9*c**(5/2)*m**2*(x**2)**(5/2) + 26*c**(5/2)*m*(x**2)**(5/2) - 24*c**(5/2)*(x**2)**(5/2)) + 6*a**2*d**m*x*x**m/(c**(5/2)*m**3*(x**2)**(5/2) - 9*c**(5/2)*m**2*(x**2)**(5/2) + 26*c**(5/2)*m*(x**2)**(5/2) - 24*c**(5/2)*(x**2)**(5/2)) + 2*a*b*d**m*m**2*x**2*x**m/(c**(5/2)*m**3*(x**2)**(5/2) - 9*c**(5/2)*m**2*(x**2)**(5/2) + 26*c**(5/2)*m*(x**2)**(5/2) - 24*c**(5/2)*(x**2)**(5/2)) - 12*a*b*d**m*m*x**2*x**m/(c**(5/2)*m**3*(x**2)**(5/2) - 9*c**(5/2)*m**2*(x**2)**(5/2) + 26*c**(5/2)*m*(x**2)**(5/2) - 24*c**(5/2)*(x**2)**(5/2)) + 16*a*b*d**m*x**2*x**m/(c**(5/2)*m**3*(x**2)**(5/2) - 9*c**(5/2)*m**2*(x**2)**(5/2) + 26*c**(5/2)*m*(x**2)**(5/2) - 24*c**(5/2)*(x**2)**(5/2)) + b**2*d**m*m**2*x**3*x**m/(c**(5/2)*m**3*(x**2)**(5/2) - 9*c**(5/2)*m**2*(x**2)**(5/2) + 26*c**(5/2)*m*(x**2)**(5/2) - 24*c**(5/2)*(x**2)**(5/2)) - 7*b**2*d**m*m*x**3*x**m/(c**(5/2)*m**3*(x**2)**(5/2) - 9*c**(5/2)*m**2*(x**2)**(5/2) + 26*c**(5/2)*m*(x**2)**(5/2) - 24*c**(5/2)*(x**2)**(5/2)) + 12*b**2*d**m*x**3*x**m/(c**(5/2)*m**3*(x**2)**(5/2) - 9*c**(5/2)*m**2*(x**2)**(5/2) + 26*c**(5/2)*m*(x**2)**(5/2) - 24*c**(5/2)*(x**2)**(5/2)), True))

$$3.981 \quad \int (dx)^m (cx^2)^{5/2} (a + bx)^n dx$$

Optimal. Leaf size=67

$$\frac{c^2 \sqrt{cx^2} (dx)^{m+6} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 6, -n; m + 7; -\frac{bx}{a}\right)}{d^6(m + 6)x}$$

[Out] $c^2(d*x)^{(6+m)}*(b*x+a)^n*\text{hypergeom}([-n, 6+m], [7+m], -b*x/a)*(c*x^2)^{(1/2)}/d^{6/(6+m)}/x/((1+b*x/a)^n)$

Rubi [A] time = 0.03, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {15, 16, 66, 64}

$$\frac{c^2 \sqrt{cx^2} (dx)^{m+6} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 6, -n; m + 7; -\frac{bx}{a}\right)}{d^6(m + 6)x}$$

Antiderivative was successfully verified.

[In] Int[(d*x)^m*(c*x^2)^(5/2)*(a + b*x)^n,x]

[Out] $(c^2*(d*x)^{(6 + m)}*\text{Sqrt}[c*x^2]*(a + b*x)^n*\text{Hypergeometric2F1}[6 + m, -n, 7 + m, -((b*x)/a)])/(d^6*(6 + m)*x*(1 + (b*x)/a)^n)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_)^(n_)), x_Symbol] := Dist[1/b^m, Int[u*(b*v)^(m + n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 64

Int[((b_.)*(x_)^(m_))*((c_) + (d_.)*(x_)^(n_)), x_Symbol] := Simp[(c^n*(b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*x)/c)]/(b*(m + 1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rule 66

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c^IntPart[n]*(c + d*x)^FracPart[n])/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)]) && EqQ[c^2 - d^2, 0])) || !RationalQ[n]
```

Rubi steps

$$\begin{aligned} \int (dx)^m (cx^2)^{5/2} (a + bx)^n dx &= \frac{(c^2 \sqrt{cx^2}) \int x^5 (dx)^m (a + bx)^n dx}{x} \\ &= \frac{(c^2 \sqrt{cx^2}) \int (dx)^{5+m} (a + bx)^n dx}{d^5 x} \\ &= \frac{(c^2 \sqrt{cx^2} (a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n}) \int (dx)^{5+m} \left(1 + \frac{bx}{a}\right)^n dx}{d^5 x} \\ &= \frac{c^2 (dx)^{6+m} \sqrt{cx^2} (a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n} {}_2F_1\left(6 + m, -n; 7 + m; -\frac{bx}{a}\right)}{d^6 (6 + m)x} \end{aligned}$$

Mathematica [A] time = 0.02, size = 57, normalized size = 0.85

$$\frac{x (cx^2)^{5/2} (dx)^m (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 6, -n; m + 7; -\frac{bx}{a}\right)}{m + 6}$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^m*(c*x^2)^(5/2)*(a + b*x)^n,x]

[Out] (x*(d*x)^m*(c*x^2)^(5/2)*(a + b*x)^n*Hypergeometric2F1[6 + m, -n, 7 + m, -(b*x)/a])/((6 + m)*(1 + (b*x)/a)^n)

fricas [F] time = 0.51, size = 0, normalized size = 0.00

$$\text{integral}\left(\sqrt{cx^2} (bx + a)^n (dx)^m c^2 x^4, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(5/2)*(b*x+a)^n,x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n*(d*x)^m*c^2*x^4, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^{\frac{5}{2}} (bx + a)^n (dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(5/2)*(b*x+a)^n,x, algorithm="giac")

[Out] integrate((c*x^2)^(5/2)*(b*x + a)^n*(d*x)^m, x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int (cx^2)^{\frac{5}{2}} (dx)^m (bx + a)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(5/2)*(b*x+a)^n,x)

[Out] int((d*x)^m*(c*x^2)^(5/2)*(b*x+a)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^{\frac{5}{2}} (bx + a)^n (dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(5/2)*(b*x+a)^n,x, algorithm="maxima")

[Out] integrate((c*x^2)^(5/2)*(b*x + a)^n*(d*x)^m, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (dx)^m (cx^2)^{5/2} (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(5/2)*(a + b*x)^n,x)

[Out] int((d*x)^m*(c*x^2)^(5/2)*(a + b*x)^n, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(c*x**2)**(5/2)*(b*x+a)**n,x)

[Out] Timed out

$$3.982 \quad \int (dx)^m (cx^2)^{3/2} (a + bx)^n dx$$

Optimal. Leaf size=65

$$\frac{c\sqrt{cx^2} (dx)^{m+4} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 4, -n; m + 5; -\frac{bx}{a}\right)}{d^4(m + 4)x}$$

[Out] $c*(d*x)^{(4+m)}*(b*x+a)^n*\text{hypergeom}([-n, 4+m], [5+m], -b*x/a)*(c*x^2)^{(1/2)}/d^{4/(4+m)}/x/((1+b*x/a)^n)$

Rubi [A] time = 0.03, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {15, 16, 66, 64}

$$\frac{c\sqrt{cx^2} (dx)^{m+4} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 4, -n; m + 5; -\frac{bx}{a}\right)}{d^4(m + 4)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(d*x)^m*(c*x^2)^{(3/2)}*(a + b*x)^n, x]$

[Out] $(c*(d*x)^{(4 + m)}*\text{Sqrt}[c*x^2]*(a + b*x)^n*\text{Hypergeometric2F1}[4 + m, -n, 5 + m, -(b*x)/a])/d^{4*(4 + m)}*x*(1 + (b*x)/a)^n$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 16

$\text{Int}[(u_.)*(v_)^{(m_.)}*((b_.)*(v_))^{(n_)}, x_Symbol] \rightarrow \text{Dist}[1/b^m, \text{Int}[u*(b*v)^{(m + n)}, x], x] /; \text{FreeQ}\{b, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 64

$\text{Int}[(b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(c^n*(b*x)^{(m + 1)}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -(d*x)/c])/(b*(m + 1)), x] /; \text{FreeQ}\{b, c, d, m, n\}, x] \&\& \text{IntegerQ}[m] \&\& (\text{IntegerQ}[n] \mid\mid (\text{GtQ}[c, 0] \&\& \text{IntegerQ}[n, -2^{(-1)}] \&\& \text{EqQ}[c^2 - d^2, 0] \&\& \text{GtQ}[-(d/(b*c)), 0]))$

Rule 66

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c^IntPart[n]*(c + d*x)^FracPart[n])/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0])) || !RationalQ[n])
```

Rubi steps

$$\begin{aligned} \int (dx)^m (cx^2)^{3/2} (a + bx)^n dx &= \frac{(c\sqrt{cx^2}) \int x^3 (dx)^m (a + bx)^n dx}{x} \\ &= \frac{(c\sqrt{cx^2}) \int (dx)^{3+m} (a + bx)^n dx}{d^3 x} \\ &= \frac{(c\sqrt{cx^2} (a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n}) \int (dx)^{3+m} \left(1 + \frac{bx}{a}\right)^n dx}{d^3 x} \\ &= \frac{c(dx)^{4+m} \sqrt{cx^2} (a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n} {}_2F_1\left(4 + m, -n; 5 + m; -\frac{bx}{a}\right)}{d^4(4 + m)x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 57, normalized size = 0.88

$$\frac{x (cx^2)^{3/2} (dx)^m (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 4, -n; m + 5; -\frac{bx}{a}\right)}{m + 4}$$

Antiderivative was successfully verified.

```
[In] Integrate[(d*x)^m*(c*x^2)^(3/2)*(a + b*x)^n,x]
```

```
[Out] (x*(d*x)^m*(c*x^2)^(3/2)*(a + b*x)^n*Hypergeometric2F1[4 + m, -n, 5 + m, -(b*x)/a])/((4 + m)*(1 + (b*x)/a)^n)
```

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\sqrt{cx^2} (bx + a)^n (dx)^m cx^2, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^m*(c*x^2)^(3/2)*(b*x+a)^n,x, algorithm="fricas")
```

```
[Out] integral(sqrt(c*x^2)*(b*x + a)^n*(d*x)^m*c*x^2, x)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^{\frac{3}{2}} (bx + a)^n (dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(3/2)*(b*x+a)^n,x, algorithm="giac")

[Out] integrate((c*x^2)^(3/2)*(b*x + a)^n*(d*x)^m, x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int (cx^2)^{\frac{3}{2}} (dx)^m (bx + a)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(3/2)*(b*x+a)^n,x)

[Out] int((d*x)^m*(c*x^2)^(3/2)*(b*x+a)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^{\frac{3}{2}} (bx + a)^n (dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(3/2)*(b*x+a)^n,x, algorithm="maxima")

[Out] integrate((c*x^2)^(3/2)*(b*x + a)^n*(d*x)^m, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (dx)^m (cx^2)^{3/2} (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(3/2)*(a + b*x)^n,x)

[Out] int((d*x)^m*(c*x^2)^(3/2)*(a + b*x)^n, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(c*x**2)**(3/2)*(b*x+a)**n,x)

[Out] Timed out

3.983 $\int (dx)^m \sqrt{cx^2} (a + bx)^n dx$

Optimal. Leaf size=64

$$\frac{\sqrt{cx^2} (dx)^{m+2} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 2, -n; m + 3; -\frac{bx}{a}\right)}{d^2(m + 2)x}$$

[Out] (d*x)^(2+m)*(b*x+a)^n*hypergeom([-n, 2+m], [3+m], -b*x/a)*(c*x^2)^(1/2)/d^2/(2+m)/x/((1+b*x/a)^n)

Rubi [A] time = 0.03, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {15, 16, 66, 64}

$$\frac{\sqrt{cx^2} (dx)^{m+2} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 2, -n; m + 3; -\frac{bx}{a}\right)}{d^2(m + 2)x}$$

Antiderivative was successfully verified.

[In] Int[(d*x)^m*Sqrt[c*x^2]*(a + b*x)^n,x]

[Out] ((d*x)^(2 + m)*Sqrt[c*x^2]*(a + b*x)^n*Hypergeometric2F1[2 + m, -n, 3 + m, -(b*x)/a])/d^2*(2 + m)*x*(1 + (b*x)/a)^n

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_))^(n_), x_Symbol] :> Dist[1/b^m, Int[u*(b*v)^(m + n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 64

Int[((b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -(d*x)/c])/b*(m + 1), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rule 66


```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c^IntPart[n]*(c + d*x)^FracPart[n])/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)]) && EqQ[c^2 - d^2, 0])) || !RationalQ[n]
```

Rubi steps

$$\begin{aligned} \int (dx)^m \sqrt{cx^2} (a + bx)^n dx &= \frac{\sqrt{cx^2} \int x(dx)^m (a + bx)^n dx}{x} \\ &= \frac{\sqrt{cx^2} \int (dx)^{1+m} (a + bx)^n dx}{dx} \\ &= \frac{\left(\sqrt{cx^2} (a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n}\right) \int (dx)^{1+m} \left(1 + \frac{bx}{a}\right)^n dx}{dx} \\ &= \frac{(dx)^{2+m} \sqrt{cx^2} (a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n} {}_2F_1\left(2 + m, -n; 3 + m; -\frac{bx}{a}\right)}{d^2(2 + m)x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 57, normalized size = 0.89

$$\frac{x\sqrt{cx^2} (dx)^m (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m + 2, -n; m + 3; -\frac{bx}{a}\right)}{m + 2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(d*x)^m*Sqrt[c*x^2]*(a + b*x)^n,x]
```

```
[Out] (x*(d*x)^m*Sqrt[c*x^2]*(a + b*x)^n*Hypergeometric2F1[2 + m, -n, 3 + m, -(b*x)/a])/((2 + m)*(1 + (b*x)/a)^n)
```

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral}\left(\sqrt{cx^2} (bx + a)^n (dx)^m, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^m*(c*x^2)^(1/2)*(b*x+a)^n,x, algorithm="fricas")
```

```
[Out] integral(sqrt(c*x^2)*(b*x + a)^n*(d*x)^m, x)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{cx^2} (bx + a)^n (dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(1/2)*(b*x+a)^n,x, algorithm="giac")

[Out] integrate(sqrt(c*x^2)*(b*x + a)^n*(d*x)^m, x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \sqrt{cx^2} (dx)^m (bx + a)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(1/2)*(b*x+a)^n,x)

[Out] int((d*x)^m*(c*x^2)^(1/2)*(b*x+a)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{cx^2} (bx + a)^n (dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^(1/2)*(b*x+a)^n,x, algorithm="maxima")

[Out] integrate(sqrt(c*x^2)*(b*x + a)^n*(d*x)^m, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (dx)^m \sqrt{cx^2} (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^(1/2)*(a + b*x)^n,x)

[Out] int((d*x)^m*(c*x^2)^(1/2)*(a + b*x)^n, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{cx^2} (dx)^m (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(c*x**2)**(1/2)*(b*x+a)**n,x)

[Out] Integral(sqrt(c*x**2)*(d*x)**m*(a + b*x)**n, x)

$$3.984 \quad \int \frac{(dx)^m (a+bx)^n}{\sqrt{cx^2}} dx$$

Optimal. Leaf size=53

$$\frac{x(dx)^m (a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m, -n; m+1; -\frac{bx}{a}\right)}{m\sqrt{cx^2}}$$

[Out] $x*(d*x)^m*(b*x+a)^n*\text{hypergeom}([m, -n], [1+m], -b*x/a)/m/((1+b*x/a)^n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {15, 16, 66, 64}

$$\frac{x(dx)^m (a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m, -n; m+1; -\frac{bx}{a}\right)}{m\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[((d*x)^m*(a + b*x)^n)/Sqrt[c*x^2], x]

[Out] $(x*(d*x)^m*(a + b*x)^n*\text{Hypergeometric2F1}[m, -n, 1 + m, -((b*x)/a)])/(m*\text{Sqrt}[c*x^2]*(1 + (b*x)/a)^n)$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_))^(n_), x_Symbol] :> Dist[1/b^m, Int[u*(b*v)^(m+n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 64

Int[((b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -((d*x)/c)])/(b*(m+1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0])))

Rule 66

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c^IntPart[n]*(c + d*x)^FracPart[n])/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0]))) || !RationalQ[n])
```

Rubi steps

$$\begin{aligned} \int \frac{(dx)^m (a + bx)^n}{\sqrt{cx^2}} dx &= \frac{x \int \frac{(dx)^m (a + bx)^n}{x} dx}{\sqrt{cx^2}} \\ &= \frac{(dx) \int (dx)^{-1+m} (a + bx)^n dx}{\sqrt{cx^2}} \\ &= \frac{\left(dx (a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} \right) \int (dx)^{-1+m} \left(1 + \frac{bx}{a} \right)^n dx}{\sqrt{cx^2}} \\ &= \frac{x (dx)^m (a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} {}_2F_1 \left(m, -n; 1 + m; -\frac{bx}{a} \right)}{m \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 53, normalized size = 1.00

$$\frac{x(dx)^m (a + bx)^n \left(\frac{bx}{a} + 1 \right)^{-n} {}_2F_1 \left(m, -n; m + 1; -\frac{bx}{a} \right)}{m \sqrt{cx^2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[((d*x)^m*(a + b*x)^n)/Sqrt[c*x^2], x]
```

```
[Out] (x*(d*x)^m*(a + b*x)^n*Hypergeometric2F1[m, -n, 1 + m, -(b*x)/a])/(m*Sqrt[c*x^2]*(1 + (b*x)/a)^n)
```

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{cx^2} (bx + a)^n (dx)^m}{cx^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^m*(b*x+a)^n/(c*x^2)^(1/2), x, algorithm="fricas")
```

[Out] `integral(sqrt(c*x^2)*(b*x + a)^n*(d*x)^m/(c*x^2), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n (dx)^m}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x)^m*(b*x+a)^n/(c*x^2)^(1/2),x, algorithm="giac")`

[Out] `integrate((b*x + a)^n*(d*x)^m/sqrt(c*x^2), x)`

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(dx)^m (bx + a)^n}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x)^m*(b*x+a)^n/(c*x^2)^(1/2),x)`

[Out] `int((d*x)^m*(b*x+a)^n/(c*x^2)^(1/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n (dx)^m}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x)^m*(b*x+a)^n/(c*x^2)^(1/2),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^n*(d*x)^m/sqrt(c*x^2), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(dx)^m (a + bx)^n}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((d*x)^m*(a + b*x)^n)/(c*x^2)^(1/2),x)`

[Out] `int(((d*x)^m*(a + b*x)^n)/(c*x^2)^(1/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx)^m (a + bx)^n}{\sqrt{cx^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(b*x+a)**n/(c*x**2)**(1/2), x)

[Out] Integral((d*x)**m*(a + b*x)**n/sqrt(c*x**2), x)

$$3.985 \quad \int \frac{(dx)^m (a+bx)^n}{(cx^2)^{3/2}} dx$$

Optimal. Leaf size=68

$$\frac{d^2x(dx)^{m-2}(a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m-2, -n; m-1; -\frac{bx}{a}\right)}{c(2-m)\sqrt{cx^2}}$$

[Out] $-d^2*x*(d*x)^{-2+m}*(b*x+a)^n*\text{hypergeom}([-n, -2+m], [-1+m], -b*x/a)/c/(2-m)/((1+b*x/a)^n)/(c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {15, 16, 66, 64}

$$\frac{d^2x(dx)^{m-2}(a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m-2, -n; m-1; -\frac{bx}{a}\right)}{c(2-m)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(d*x)^m*(a+b*x)^n/(c*x^2)^{(3/2)}, x]$

[Out] $-((d^2*x*(d*x)^{-2+m}*(a+b*x)^n*\text{Hypergeometric2F1}[-2+m, -n, -1+m, -(b*x)/a])/(c*(2-m)*\text{Sqrt}[c*x^2]*(1+(b*x)/a)^n))$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 16

$\text{Int}[(u_*)*(v_)^{(m_*)}*((b_*)*(v_))^{(n_)}, x_Symbol] \rightarrow \text{Dist}[1/b^m, \text{Int}[u*(b*v)^{(m+n)}, x], x] /; \text{FreeQ}\{b, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 64

$\text{Int}[(b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(c^n*(b*x)^{(m+1)}*\text{Hypergeometric2F1}[-n, m+1, m+2, -(d*x)/c])/(b*(m+1)), x] /; \text{FreeQ}\{b, c, d, m, n\}, x] \&\& \text{IntegerQ}[m] \&\& (\text{IntegerQ}[n] \mid\mid (\text{GtQ}[c, 0] \&\& \text{!(EqQ}[n, -2^{(-1)}]) \&\& \text{EqQ}[c^2 - d^2, 0] \&\& \text{GtQ}[-(d/(b*c)), 0])))$

Rule 66

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c^IntPart[n]*(c + d*x)^FracPart[n])/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)]) && EqQ[c^2 - d^2, 0])) || !RationalQ[n])
```

Rubi steps

$$\begin{aligned} \int \frac{(dx)^m (a + bx)^n}{(cx^2)^{3/2}} dx &= \frac{x \int \frac{(dx)^m (a + bx)^n}{x^3} dx}{c\sqrt{cx^2}} \\ &= \frac{(d^3 x) \int (dx)^{-3+m} (a + bx)^n dx}{c\sqrt{cx^2}} \\ &= \frac{\left(d^3 x (a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n}\right) \int (dx)^{-3+m} \left(1 + \frac{bx}{a}\right)^n dx}{c\sqrt{cx^2}} \\ &= -\frac{d^2 x (dx)^{-2+m} (a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n} {}_2F_1\left(-2 + m, -n; -1 + m; -\frac{bx}{a}\right)}{c(2 - m)\sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 57, normalized size = 0.84

$$\frac{x(dx)^m (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m - 2, -n; m - 1; -\frac{bx}{a}\right)}{(m - 2)(cx^2)^{3/2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[((d*x)^m*(a + b*x)^n)/(c*x^2)^(3/2), x]
```

```
[Out] (x*(d*x)^m*(a + b*x)^n*Hypergeometric2F1[-2 + m, -n, -1 + m, -((b*x)/a)])/(
(-2 + m)*(c*x^2)^(3/2)*(1 + (b*x)/a)^n)
```

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx + a)^n (dx)^m}{c^2 x^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^n/(c*x^2)^(3/2),x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n*(d*x)^m/(c^2*x^4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n (dx)^m}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^n/(c*x^2)^(3/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n*(d*x)^m/(c*x^2)^(3/2), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(dx)^m (bx + a)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(b*x+a)^n/(c*x^2)^(3/2),x)

[Out] int((d*x)^m*(b*x+a)^n/(c*x^2)^(3/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n (dx)^m}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^n/(c*x^2)^(3/2),x, algorithm="maxima")

[Out] integrate((b*x + a)^n*(d*x)^m/(c*x^2)^(3/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(dx)^m (a + bx)^n}{(cx^2)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((d*x)^m*(a + b*x)^n)/(c*x^2)^(3/2),x)

[Out] `int(((d*x)^m*(a + b*x)^n)/(c*x^2)^(3/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx)^m (a + bx)^n}{(cx^2)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x)**m*(b*x+a)**n/(c*x**2)**(3/2), x)`

[Out] `Integral((d*x)**m*(a + b*x)**n/(c*x**2)**(3/2), x)`

$$3.986 \quad \int \frac{(dx)^m (a+bx)^n}{(cx^2)^{5/2}} dx$$

Optimal. Leaf size=68

$$\frac{d^4 x (dx)^{m-4} (a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m-4, -n; m-3; -\frac{bx}{a}\right)}{c^2(4-m)\sqrt{cx^2}}$$

[Out] $-d^4 x (dx)^{-4+m} (b*x+a)^n \text{hypergeom}([-n, -4+m], [-3+m], -b*x/a) / c^2 / (4-m) / ((1+b*x/a)^n) / (c*x^2)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.182$, Rules used = {15, 16, 66, 64}

$$\frac{d^4 x (dx)^{m-4} (a+bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m-4, -n; m-3; -\frac{bx}{a}\right)}{c^2(4-m)\sqrt{cx^2}}$$

Antiderivative was successfully verified.

[In] Int[((d*x)^m*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] $-((d^4*x*(d*x)^{-4+m}*(a+b*x)^n*\text{Hypergeometric2F1}[-4+m, -n, -3+m, -(b*x)/a])/(c^2*(4-m)*\text{Sqrt}[c*x^2]*(1+(b*x)/a)^n))$

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] := Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 16

Int[(u_.)*(v_)^(m_.)*((b_.)*(v_))^(n_), x_Symbol] := Dist[1/b^m, Int[u*(b*v)^(m+n), x], x] /; FreeQ[{b, n}, x] && IntegerQ[m]

Rule 64

Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(c^n*(b*x)^(m+1)*Hypergeometric2F1[-n, m+1, m+2, -(d*x)/c])/(b*(m+1)), x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0])))

Rule 66

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c^IntPart[n]*(c + d*x)^FracPart[n])/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)]) && EqQ[c^2 - d^2, 0])) || !RationalQ[n])
```

Rubi steps

$$\begin{aligned} \int \frac{(dx)^m (a + bx)^n}{(cx^2)^{5/2}} dx &= \frac{x \int \frac{(dx)^m (a + bx)^n}{x^5} dx}{c^2 \sqrt{cx^2}} \\ &= \frac{(d^5 x) \int (dx)^{-5+m} (a + bx)^n dx}{c^2 \sqrt{cx^2}} \\ &= \frac{\left(d^5 x (a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n}\right) \int (dx)^{-5+m} \left(1 + \frac{bx}{a}\right)^n dx}{c^2 \sqrt{cx^2}} \\ &= -\frac{d^4 x (dx)^{-4+m} (a + bx)^n \left(1 + \frac{bx}{a}\right)^{-n} {}_2F_1\left(-4 + m, -n; -3 + m; -\frac{bx}{a}\right)}{c^2 (4 - m) \sqrt{cx^2}} \end{aligned}$$

Mathematica [A] time = 0.02, size = 57, normalized size = 0.84

$$\frac{x(dx)^m (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(m - 4, -n; m - 3; -\frac{bx}{a}\right)}{(m - 4)(cx^2)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[((d*x)^m*(a + b*x)^n)/(c*x^2)^(5/2), x]

[Out] (x*(d*x)^m*(a + b*x)^n*Hypergeometric2F1[-4 + m, -n, -3 + m, -((b*x)/a)])/((-4 + m)*(c*x^2)^(5/2)*(1 + (b*x)/a)^n)

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{cx^2} (bx + a)^n (dx)^m}{c^3 x^6}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="fricas")

[Out] integral(sqrt(c*x^2)*(b*x + a)^n*(d*x)^m/(c^3*x^6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n (dx)^m}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="giac")

[Out] integrate((b*x + a)^n*(d*x)^m/(c*x^2)^(5/2), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(dx)^m (bx + a)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(b*x+a)^n/(c*x^2)^(5/2),x)

[Out] int((d*x)^m*(b*x+a)^n/(c*x^2)^(5/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n (dx)^m}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(b*x+a)^n/(c*x^2)^(5/2),x, algorithm="maxima")

[Out] integrate((b*x + a)^n*(d*x)^m/(c*x^2)^(5/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(dx)^m (a + bx)^n}{(cx^2)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((d*x)^m*(a + b*x)^n)/(c*x^2)^(5/2),x)

[Out] `int(((d*x)^m*(a + b*x)^n)/(c*x^2)^(5/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx)^m (a + bx)^n}{(cx^2)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x)**m*(b*x+a)**n/(c*x**2)**(5/2), x)`

[Out] `Integral((d*x)**m*(a + b*x)**n/(c*x**2)**(5/2), x)`

$$3.987 \quad \int x^3 (cx^2)^p (a + bx)^{-5-2p} dx$$

Optimal. Leaf size=33

$$\frac{x^4 (cx^2)^p (a + bx)^{-2(p+2)}}{2a(p+2)}$$

[Out] 1/2*x^4*(c*x^2)^p/a/(2+p)/((b*x+a)^(4+2*p))

Rubi [A] time = 0.01, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {15, 37}

$$\frac{x^4 (cx^2)^p (a + bx)^{-2(p+2)}}{2a(p+2)}$$

Antiderivative was successfully verified.

[In] Int[x^3*(c*x^2)^p*(a + b*x)^(-5 - 2*p), x]

[Out] (x^4*(c*x^2)^p)/(2*a*(2 + p)*(a + b*x)^(2*(2 + p)))

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int x^3 (cx^2)^p (a + bx)^{-5-2p} dx &= \left(x^{-2p} (cx^2)^p \right) \int x^{3+2p} (a + bx)^{-5-2p} dx \\ &= \frac{x^4 (cx^2)^p (a + bx)^{-2(2+p)}}{2a(2+p)} \end{aligned}$$

Mathematica [A] time = 0.02, size = 32, normalized size = 0.97

$$\frac{x^4 (cx^2)^p (a + bx)^{-2p-4}}{a(2p + 4)}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(c*x^2)^p*(a + b*x)^(-5 - 2*p), x]

[Out] (x^4*(c*x^2)^p*(a + b*x)^(-4 - 2*p))/(a*(4 + 2*p))

fricas [A] time = 0.45, size = 40, normalized size = 1.21

$$\frac{(bx^5 + ax^4)(cx^2)^p (bx + a)^{-2p-5}}{2(ap + 2a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^p*(b*x+a)^(-5-2*p), x, algorithm="fricas")

[Out] 1/2*(b*x^5 + a*x^4)*(c*x^2)^p*(b*x + a)^(-2*p - 5)/(a*p + 2*a)

giac [B] time = 1.26, size = 74, normalized size = 2.24

$$\frac{(cx^2)^p bx^5 e^{(-2p \log(bx+a) - 5 \log(bx+a))} + (cx^2)^p ax^4 e^{(-2p \log(bx+a) - 5 \log(bx+a))}}{2(ap + 2a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^p*(b*x+a)^(-5-2*p), x, algorithm="giac")

[Out] 1/2*((c*x^2)^p*b*x^5*e^(-2*p*log(b*x + a) - 5*log(b*x + a)) + (c*x^2)^p*a*x^4*e^(-2*p*log(b*x + a) - 5*log(b*x + a)))/(a*p + 2*a)

maple [A] time = 0.00, size = 32, normalized size = 0.97

$$\frac{x^4 (cx^2)^p (bx + a)^{-2p-4}}{2(p + 2)a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(c*x^2)^p*(b*x+a)^(-5-2*p), x)

[Out] 1/2*(b*x+a)^(-4-2*p)*x^4/a/(2+p)*(c*x^2)^p

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^{-2p-5} x^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(c*x^2)^p*(b*x+a)^(-5-2*p),x, algorithm="maxima")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p - 5)*x^3, x)

mupad [B] time = 0.27, size = 33, normalized size = 1.00

$$\frac{x^4 (cx^2)^p}{2a(p+2)(a+bx)^{2p+4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^3*(c*x^2)^p)/(a + b*x)^(2*p + 5),x)

[Out] (x^4*(c*x^2)^p)/(2*a*(p + 2)*(a + b*x)^(2*p + 4))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(c*x**2)**p*(b*x+a)**(-5-2*p),x)

[Out] Timed out

$$3.988 \quad \int x^2 (cx^2)^p (a + bx)^{-4-2p} dx$$

Optimal. Leaf size=32

$$\frac{x^3 (cx^2)^p (a + bx)^{-2p-3}}{a(2p + 3)}$$

[Out] $x^3(c*x^2)^p*(b*x+a)^{-3-2*p}/a/(3+2*p)$

Rubi [A] time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {15, 37}

$$\frac{x^3 (cx^2)^p (a + bx)^{-2p-3}}{a(2p + 3)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*(c*x^2)^p*(a + b*x)^{-4 - 2*p}, x]$

[Out] $(x^3*(c*x^2)^p*(a + b*x)^{-3 - 2*p})/(a*(3 + 2*p))$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 37

$\text{Int}[(a_*) + (b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_*)}), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)} / ((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int x^2 (cx^2)^p (a + bx)^{-4-2p} dx &= \left(x^{-2p} (cx^2)^p \right) \int x^{2+2p} (a + bx)^{-4-2p} dx \\ &= \frac{x^3 (cx^2)^p (a + bx)^{-3-2p}}{a(3 + 2p)} \end{aligned}$$

Mathematica [A] time = 0.02, size = 34, normalized size = 1.06

$$\frac{x^3 (cx^2)^p (a + bx)^{1-2(p+2)}}{a(2p + 3)}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(c*x^2)^p*(a + b*x)^(-4 - 2*p), x]

[Out] (x^3*(c*x^2)^p*(a + b*x)^(1 - 2*(2 + p)))/(a*(3 + 2*p))

fricas [A] time = 0.47, size = 40, normalized size = 1.25

$$\frac{(bx^4 + ax^3)(cx^2)^p (bx + a)^{-2p-4}}{2ap + 3a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^p*(b*x+a)^(-4-2*p), x, algorithm="fricas")

[Out] (b*x^4 + a*x^3)*(c*x^2)^p*(b*x + a)^(-2*p - 4)/(2*a*p + 3*a)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^{-2p-4} x^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^p*(b*x+a)^(-4-2*p), x, algorithm="giac")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p - 4)*x^2, x)

maple [A] time = 0.00, size = 33, normalized size = 1.03

$$\frac{x^3 (cx^2)^p (bx + a)^{-2p-3}}{(2p + 3)a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(c*x^2)^p*(b*x+a)^(-2*p-4), x)

[Out] x^3*(c*x^2)^p*(b*x+a)^(-3-2*p)/a/(3+2*p)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^{-2p-4} x^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(c*x^2)^p*(b*x+a)^(-4-2*p),x, algorithm="maxima")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p - 4)*x^2, x)

mupad [B] time = 0.24, size = 34, normalized size = 1.06

$$\frac{x^3 (c x^2)^p}{a (2p + 3) (a + b x)^{2p+3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^2*(c*x^2)^p)/(a + b*x)^(2*p + 4),x)

[Out] (x^3*(c*x^2)^p)/(a*(2*p + 3)*(a + b*x)^(2*p + 3))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(c*x**2)**p*(b*x+a)**(-4-2*p),x)

[Out] Timed out

$$3.989 \quad \int x (cx^2)^p (a + bx)^{-3-2p} dx$$

Optimal. Leaf size=33

$$\frac{x^2 (cx^2)^p (a + bx)^{-2(p+1)}}{2a(p+1)}$$

[Out] 1/2*x^2*(c*x^2)^p/a/(1+p)/((b*x+a)^(2+2*p))

Rubi [A] time = 0.01, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 37}

$$\frac{x^2 (cx^2)^p (a + bx)^{-2(p+1)}}{2a(p+1)}$$

Antiderivative was successfully verified.

[In] Int[x*(c*x^2)^p*(a + b*x)^(-3 - 2*p), x]

[Out] (x^2*(c*x^2)^p)/(2*a*(1 + p)*(a + b*x)^(2*(1 + p)))

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int x (cx^2)^p (a + bx)^{-3-2p} dx &= \left(x^{-2p} (cx^2)^p \right) \int x^{1+2p} (a + bx)^{-3-2p} dx \\ &= \frac{x^2 (cx^2)^p (a + bx)^{-2(1+p)}}{2a(1+p)} \end{aligned}$$

Mathematica [A] time = 0.02, size = 32, normalized size = 0.97

$$\frac{x^2 (cx^2)^p (a + bx)^{-2p-2}}{a(2p + 2)}$$

Antiderivative was successfully verified.

[In] Integrate[x*(c*x^2)^p*(a + b*x)^(-3 - 2*p), x]

[Out] (x^2*(c*x^2)^p*(a + b*x)^(-2 - 2*p))/(a*(2 + 2*p))

fricas [A] time = 0.46, size = 38, normalized size = 1.15

$$\frac{(bx^3 + ax^2)(cx^2)^p (bx + a)^{-2p-3}}{2(ap + a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^p*(b*x+a)^(-3-2*p), x, algorithm="fricas")

[Out] 1/2*(b*x^3 + a*x^2)*(c*x^2)^p*(b*x + a)^(-2*p - 3)/(a*p + a)

giac [B] time = 1.07, size = 72, normalized size = 2.18

$$\frac{(cx^2)^p bx^3 e^{(-2p \log(bx+a) - 3 \log(bx+a))} + (cx^2)^p ax^2 e^{(-2p \log(bx+a) - 3 \log(bx+a))}}{2(ap + a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^p*(b*x+a)^(-3-2*p), x, algorithm="giac")

[Out] 1/2*((c*x^2)^p*b*x^3*e^(-2*p*log(b*x + a) - 3*log(b*x + a)) + (c*x^2)^p*a*x^2*e^(-2*p*log(b*x + a) - 3*log(b*x + a)))/(a*p + a)

maple [A] time = 0.00, size = 32, normalized size = 0.97

$$\frac{x^2 (cx^2)^p (bx + a)^{-2p-2}}{2(p + 1)a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(c*x^2)^p*(b*x+a)^(-2*p-3), x)

[Out] 1/2*(b*x+a)^(-2-2*p)*x^2/a/(1+p)*(c*x^2)^p

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^{-2p-3} x dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x^2)^p*(b*x+a)^(-3-2*p),x, algorithm="maxima")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p - 3)*x, x)

mupad [B] time = 0.22, size = 33, normalized size = 1.00

$$\frac{x^2 (cx^2)^p}{2a(p+1)(a+bx)^{2p+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x*(c*x^2)^p)/(a + b*x)^(2*p + 3),x)

[Out] (x^2*(c*x^2)^p)/(2*a*(p + 1)*(a + b*x)^(2*p + 2))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(c*x**2)**p*(b*x+a)**(-3-2*p),x)

[Out] Timed out

$$3.990 \quad \int (cx^2)^p (a + bx)^{-2-2p} dx$$

Optimal. Leaf size=30

$$\frac{x (cx^2)^p (a + bx)^{-2p-1}}{a(2p + 1)}$$

[Out] x*(c*x^2)^p*(b*x+a)^(-1-2*p)/a/(1+2*p)

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {15, 37}

$$\frac{x (cx^2)^p (a + bx)^{-2p-1}}{a(2p + 1)}$$

Antiderivative was successfully verified.

[In] Int[(c*x^2)^p*(a + b*x)^(-2 - 2*p), x]

[Out] (x*(c*x^2)^p*(a + b*x)^(-1 - 2*p))/(a*(1 + 2*p))

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int (cx^2)^p (a + bx)^{-2-2p} dx &= \left(x^{-2p} (cx^2)^p \right) \int x^{2p} (a + bx)^{-2-2p} dx \\ &= \frac{x (cx^2)^p (a + bx)^{-1-2p}}{a(1 + 2p)} \end{aligned}$$

Mathematica [A] time = 0.02, size = 28, normalized size = 0.93

$$\frac{x (cx^2)^p (a + bx)^{-2p-1}}{2ap + a}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^p*(a + b*x)^(-2 - 2*p), x]

[Out] (x*(c*x^2)^p*(a + b*x)^(-1 - 2*p))/(a + 2*a*p)

fricas [A] time = 0.46, size = 36, normalized size = 1.20

$$\frac{(bx^2 + ax) (cx^2)^p (bx + a)^{-2p-2}}{2ap + a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(-2-2*p), x, algorithm="fricas")

[Out] (b*x^2 + a*x)*(c*x^2)^p*(b*x + a)^(-2*p - 2)/(2*a*p + a)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^{-2p-2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(-2-2*p), x, algorithm="giac")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p - 2), x)

maple [A] time = 0.00, size = 31, normalized size = 1.03

$$\frac{x (cx^2)^p (bx + a)^{-2p-1}}{(2p + 1)a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^p*(b*x+a)^(-2*p-2), x)

[Out] x*(c*x^2)^p*(b*x+a)^(-1-2*p)/a/(1+2*p)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^{-2p-2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(-2-2*p),x, algorithm="maxima")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p - 2), x)

mupad [B] time = 0.20, size = 32, normalized size = 1.07

$$\frac{x(c x^2)^p}{a(2p+1)(a+bx)^{2p+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^p/(a + b*x)^(2*p + 2),x)

[Out] (x*(c*x^2)^p)/(a*(2*p + 1)*(a + b*x)^(2*p + 1))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{l} \frac{b^{-2p}c^p x^{-2p}(x^2)^p}{b^2 x} \\ \frac{0^{-2p-2}c^p x(x^2)^p}{2p+1} \\ \frac{c^p x \left(0^{\frac{1}{p}}\right)^{-2p-2} (x^2)^p}{2p+1} \\ \int \frac{1}{\sqrt{cx^2(a+bx)}} dx \end{array} \right. \frac{a^3 c^p x (x^2)^p}{2a^5 p(a+bx)^{2p} + a^5(a+bx)^{2p} + 8a^4 b p x(a+bx)^{2p} + 4a^4 b x(a+bx)^{2p} + 12a^3 b^2 p x^2(a+bx)^{2p} + 6a^3 b^2 x^2(a+bx)^{2p} + 8a^2 b^3 p x^3(a+bx)^{2p} + 4a^2 b^3 x^3(a+bx)^{2p} + 2ab^4 p x^4(a+bx)^{2p}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**p*(b*x+a)**(-2-2*p),x)

[Out] Piecewise((-b**(-2*p)*c**p*x**(-2*p)*(x**2)**p/(b**2*x), Eq(a, 0)), (0**(-2*p - 2)*c**p*x*(x**2)**p/(2*p + 1), Eq(a, -b*x)), (c**p*x*(0**(1/p))**(-2*p - 2)*(x**2)**p/(2*p + 1), Eq(a, 0**(1/p) - b*x)), (Integral(1/(sqrt(c*x**2)*(a + b*x)), x), Eq(p, -1/2)), (a**3*c**p*x*(x**2)**p/(2*a**5*p*(a + b*x)**(2*p) + a**5*(a + b*x)**(2*p) + 8*a**4*b*p*x*(a + b*x)**(2*p) + 4*a**4*b*x*(a + b*x)**(2*p) + 12*a**3*b**2*p*x**2*(a + b*x)**(2*p) + 6*a**3*b**2*x**2*(a + b*x)**(2*p) + 8*a**2*b**3*p*x**3*(a + b*x)**(2*p) + 4*a**2*b**3*x**3*(a + b*x)**(2*p) + 2*a*b**4*p*x**4*(a + b*x)**(2*p) + a*b**4*x**4*(a + b*x)

```

**(2*p)) + 2*a**2*b*c**p*x**2*(x**2)**p/(2*a**5*p*(a + b*x)**(2*p) + a**5*(
a + b*x)**(2*p) + 8*a**4*b*p*x*(a + b*x)**(2*p) + 4*a**4*b*x*(a + b*x)**(2*
p) + 12*a**3*b**2*p*x**2*(a + b*x)**(2*p) + 6*a**3*b**2*x**2*(a + b*x)**(2*
p) + 8*a**2*b**3*p*x**3*(a + b*x)**(2*p) + 4*a**2*b**3*x**3*(a + b*x)**(2*p
) + 2*a*b**4*p*x**4*(a + b*x)**(2*p) + a*b**4*x**4*(a + b*x)**(2*p)) + a*b*
*2*c**p*x**3*(x**2)**p/(2*a**5*p*(a + b*x)**(2*p) + a**5*(a + b*x)**(2*p) +
8*a**4*b*p*x*(a + b*x)**(2*p) + 4*a**4*b*x*(a + b*x)**(2*p) + 12*a**3*b**2
*p*x**2*(a + b*x)**(2*p) + 6*a**3*b**2*x**2*(a + b*x)**(2*p) + 8*a**2*b**3*
p*x**3*(a + b*x)**(2*p) + 4*a**2*b**3*x**3*(a + b*x)**(2*p) + 2*a*b**4*p*x*
*4*(a + b*x)**(2*p) + a*b**4*x**4*(a + b*x)**(2*p)) + b*c**p*x**2*(x**2)**p
/(2*a**3*p*(a + b*x)**(2*p) + a**3*(a + b*x)**(2*p) + 4*a**2*b*p*x*(a + b*x
)**(2*p) + 2*a**2*b*x*(a + b*x)**(2*p) + 2*a*b**2*p*x**2*(a + b*x)**(2*p) +
a*b**2*x**2*(a + b*x)**(2*p)), True))

```

$$3.991 \quad \int \frac{(cx^2)^p (a+bx)^{-1-2p}}{x} dx$$

Optimal. Leaf size=26

$$\frac{(cx^2)^p (a+bx)^{-2p}}{2ap}$$

[Out] 1/2*(c*x^2)^p/a/p/((b*x+a)^(2*p))

Rubi [A] time = 0.01, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {15, 37}

$$\frac{(cx^2)^p (a+bx)^{-2p}}{2ap}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^p*(a + b*x)^(-1 - 2*p))/x,x]

[Out] (c*x^2)^p/(2*a*p*(a + b*x)^(2*p))

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^p (a+bx)^{-1-2p}}{x} dx &= \left(x^{-2p} (cx^2)^p \right) \int x^{-1+2p} (a+bx)^{-1-2p} dx \\ &= \frac{(cx^2)^p (a+bx)^{-2p}}{2ap} \end{aligned}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 1.00

$$\frac{(cx^2)^p (a + bx)^{-2p}}{2ap}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^p*(a + b*x)^(-1 - 2*p))/x,x]

[Out] (c*x^2)^p/(2*a*p*(a + b*x)^(2*p))

fricas [A] time = 0.47, size = 31, normalized size = 1.19

$$\frac{(bx + a)(cx^2)^p (bx + a)^{-2p-1}}{2ap}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(-1-2*p)/x,x, algorithm="fricas")

[Out] 1/2*(b*x + a)*(c*x^2)^p*(b*x + a)^(-2*p - 1)/(a*p)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^p (bx + a)^{-2p-1}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(-1-2*p)/x,x, algorithm="giac")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p - 1)/x, x)

maple [A] time = 0.00, size = 25, normalized size = 0.96

$$\frac{(cx^2)^p (bx + a)^{-2p}}{2ap}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^p*(b*x+a)^(-2*p-1)/x,x)

[Out] 1/2*(b*x+a)^(-2*p)/a/p*(c*x^2)^p

maxima [A] time = 1.45, size = 27, normalized size = 1.04

$$\frac{c^p e^{(-2p \log(bx+a)+2p \log(x))}}{2ap}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(-1-2*p)/x,x, algorithm="maxima")

[Out] 1/2*c^p*e^(-2*p*log(b*x + a) + 2*p*log(x))/(a*p)

mupad [B] time = 0.26, size = 26, normalized size = 1.00

$$\frac{(cx^2)^p}{2ap(a+bx)^{2p}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^p/(x*(a + b*x)^(2*p + 1)),x)

[Out] (c*x^2)^p/(2*a*p*(a + b*x)^(2*p))

sympy [A] time = 59.69, size = 264, normalized size = 10.15

$$\left\{ \begin{array}{l} \frac{b^{-2p}c^p x^{-2p}(x^2)^p}{bx} \\ \frac{0^{-2p-1}c^p(x^2)^p}{2p} \\ \frac{c^p\left(0^{\frac{1}{p}}\right)^{-2p-1}(x^2)^p}{2p} \\ \frac{\log(x)}{a} - \frac{\log\left(\frac{a}{b}+x\right)}{a} \end{array} \right. + \frac{a^2c^p(x^2)^p}{2a^3p(a+bx)^{2p}+4a^2bpx(a+bx)^{2p}+2ab^2px^2(a+bx)^{2p}} + \frac{abc^p x(x^2)^p}{2a^3p(a+bx)^{2p}+4a^2bpx(a+bx)^{2p}+2ab^2px^2(a+bx)^{2p}} + \frac{bc^p x(x^2)^p}{2a^2p(a+bx)^{2p}+2abpx(a+bx)^{2p}}$$

for a
for a
for a
for p
other

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**p*(b*x+a)**(-1-2*p)/x,x)

[Out] Piecewise((-b**(-2*p)*c**p*x**(-2*p)*(x**2)**p/(b*x), Eq(a, 0)), (0**(-2*p - 1)*c**p*(x**2)**p/(2*p), Eq(a, -b*x)), (c**p*(0**(1/p))**(-2*p - 1)*(x**2)**p/(2*p), Eq(a, 0**(1/p) - b*x)), (log(x)/a - log(a/b + x)/a, Eq(p, 0)), (a**2*c**p*(x**2)**p/(2*a**3*p*(a + b*x)**(2*p) + 4*a**2*b*p*x*(a + b*x)**(2*p) + 2*a*b**2*p*x**2*(a + b*x)**(2*p)) + a*b*c**p*x*(x**2)**p/(2*a**3*p*(a + b*x)**(2*p) + 4*a**2*b*p*x*(a + b*x)**(2*p) + 2*a*b**2*p*x**2*(a + b*x)**(2*p)) + b*c**p*x*(x**2)**p/(2*a**2*p*(a + b*x)**(2*p) + 2*a*b*p*x*(a + b*x)**(2*p)), True))

$$3.992 \quad \int \frac{(cx^2)^p (a+bx)^{-2p}}{x^2} dx$$

Optimal. Leaf size=33

$$-\frac{(cx^2)^p (a+bx)^{1-2p}}{a(1-2p)x}$$

[Out] $-(c*x^2)^p*(b*x+a)^{(1-2*p)}/a/(1-2*p)/x$

Rubi [A] time = 0.01, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {15, 37}

$$-\frac{(cx^2)^p (a+bx)^{1-2p}}{a(1-2p)x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^p/(x^2*(a+b*x)^{(2*p)}), x]$

[Out] $-\frac{((c*x^2)^p*(a+b*x)^{(1-2*p)})}{(a*(1-2*p)*x)}$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 37

$\text{Int}[((a_*) + (b_*)*(x_))^{(m_*)}*((c_*) + (d_*)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Simp}[\frac{((a+b*x)^{(m+1})*(c+d*x)^{(n+1))}{((b*c-a*d)*(m+1))}, x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c-a*d, 0] && EqQ[m+n+2, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^p (a+bx)^{-2p}}{x^2} dx &= \left(x^{-2p} (cx^2)^p \right) \int x^{-2+2p} (a+bx)^{-2p} dx \\ &= -\frac{(cx^2)^p (a+bx)^{1-2p}}{a(1-2p)x} \end{aligned}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 0.97

$$\frac{(cx^2)^p (a + bx)^{1-2p}}{a(2p - 1)x}$$

Antiderivative was successfully verified.

[In] Integrate[(c*x^2)^p/(x^2*(a + b*x)^(2*p)),x]

[Out] ((c*x^2)^p*(a + b*x)^(1 - 2*p))/(a*(-1 + 2*p)*x)

fricas [A] time = 0.46, size = 37, normalized size = 1.12

$$\frac{(bx + a)(cx^2)^p}{(2ap - a)(bx + a)^{2p}x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p/x^2/((b*x+a)^(2*p)),x, algorithm="fricas")

[Out] (b*x + a)*(c*x^2)^p/((2*a*p - a)*(b*x + a)^(2*p)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^p}{(bx + a)^{2p}x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p/x^2/((b*x+a)^(2*p)),x, algorithm="giac")

[Out] integrate((c*x^2)^p/((b*x + a)^(2*p)*x^2), x)

maple [A] time = 0.00, size = 38, normalized size = 1.15

$$\frac{(bx + a)(cx^2)^p (bx + a)^{-2p}}{(2p - 1)ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^p/x^2/((b*x+a)^(2*p)),x)

[Out] (b*x+a)/x/a/(2*p-1)*(c*x^2)^p/((b*x+a)^(2*p))

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^p}{(bx+a)^{2p}x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p/x^2/((b*x+a)^(2*p)),x, algorithm="maxima")

[Out] integrate((c*x^2)^p/((b*x + a)^(2*p)*x^2), x)

mupad [B] time = 0.24, size = 32, normalized size = 0.97

$$\frac{(cx^2)^p (a+bx)^{1-2p}}{ax(2p-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^p/(x^2*(a+b*x)^(2*p)),x)

[Out] ((c*x^2)^p*(a+b*x)^(1-2*p))/(a*x*(2*p-1))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\left\{ \begin{array}{ll} -\frac{\sqrt{c}\sqrt{x^2}}{bx^2} & \text{for } a = 0 \wedge p = \frac{1}{2} \\ -\frac{b^{-2p}c^p x^{-2p}(x^2)^p}{x} & \text{for } a = 0 \\ \int \frac{\sqrt{cx^2}}{x^2(a+bx)} dx & \text{for } p = \frac{1}{2} \\ \frac{ac^p(x^2)^p}{2apx(a+bx)^{2p}-ax(a+bx)^{2p}} + \frac{bc^p x(x^2)^p}{2apx(a+bx)^{2p}-ax(a+bx)^{2p}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**p/x**2/((b*x+a)**(2*p)),x)

[Out] Piecewise((-sqrt(c)*sqrt(x**2)/(b*x**2), Eq(a, 0) & Eq(p, 1/2)), (-b**(-2*p)*c**p*x**(-2*p)*(x**2)**p/x, Eq(a, 0)), (Integral(sqrt(c*x**2)/(x**2*(a+b*x)), x), Eq(p, 1/2)), (a*c**p*(x**2)**p/(2*a*p*x*(a+b*x)**(2*p)-a*x*(a+b*x)**(2*p))+b*c**p*x*(x**2)**p/(2*a*p*x*(a+b*x)**(2*p)-a*x*(a+b*x)**(2*p)), True))

$$3.993 \quad \int \frac{(cx^2)^p (a+bx)^{1-2p}}{x^3} dx$$

Optimal. Leaf size=35

$$\frac{(cx^2)^p (a+bx)^{2-2p}}{2a(1-p)x^2}$$

[Out] $-1/2*(c*x^2)^p*(b*x+a)^{(2-2*p)}/a/(1-p)/x^2$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {15, 37}

$$\frac{(cx^2)^p (a+bx)^{2-2p}}{2a(1-p)x^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c*x^2)^p*(a+b*x)^{(1-2*p)}/x^3, x]$

[Out] $-((c*x^2)^p*(a+b*x)^{(2-2*p)})/(2*a*(1-p)*x^2)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ $\text{FreeQ}\{a, m, n, x\}$ && $!\text{IntegerQ}[m]$

Rule 37

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}]*((c_.) + (d_.)*(x_)^{(n_.)}), x_Symbol] \rightarrow \text{Simp}[(a+b*x)^{(m+1)}*(c+d*x)^{(n+1)}/((b*c-a*d)*(m+1)), x] /;$ $\text{FreeQ}\{a, b, c, d, m, n, x\}$ && $\text{NeQ}[b*c-a*d, 0]$ && $\text{EqQ}[m+n+2, 0]$ && $\text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^p (a+bx)^{1-2p}}{x^3} dx &= \left(x^{-2p} (cx^2)^p\right) \int x^{-3+2p} (a+bx)^{1-2p} dx \\ &= -\frac{(cx^2)^p (a+bx)^{2-2p}}{2a(1-p)x^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 0.91

$$\frac{(cx^2)^p (a + bx)^{2-2p}}{a(2p-2)x^2}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^p*(a + b*x)^(1 - 2*p))/x^3,x]

[Out] ((c*x^2)^p*(a + b*x)^(2 - 2*p))/(a*(-2 + 2*p)*x^2)

fricas [A] time = 0.45, size = 37, normalized size = 1.06

$$\frac{(bx + a)(cx^2)^p (bx + a)^{-2p+1}}{2(ap - a)x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(1-2*p)/x^3,x, algorithm="fricas")

[Out] 1/2*(b*x + a)*(c*x^2)^p*(b*x + a)^(-2*p + 1)/((a*p - a)*x^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^p (bx + a)^{-2p+1}}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(1-2*p)/x^3,x, algorithm="giac")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p + 1)/x^3, x)

maple [A] time = 0.00, size = 32, normalized size = 0.91

$$\frac{(cx^2)^p (bx + a)^{-2p+2}}{2(p-1)ax^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^p*(b*x+a)^(1-2*p)/x^3,x)

[Out] 1/2*(b*x+a)^(2-2*p)/x^2/a/(p-1)*(c*x^2)^p

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^p (bx + a)^{-2p+1}}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(1-2*p)/x^3,x, algorithm="maxima")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p + 1)/x^3, x)

mupad [B] time = 0.25, size = 50, normalized size = 1.43

$$\frac{\left(\frac{(cx^2)^p}{2(p-1)} + \frac{bx(cx^2)^p}{2a(p-1)}\right)(a+bx)^{1-2p}}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^p*(a + b*x)^(1 - 2*p))/x^3,x)

[Out] (((c*x^2)^p/(2*(p - 1)) + (b*x*(c*x^2)^p)/(2*a*(p - 1)))*(a + b*x)^(1 - 2*p))/x^2

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^p (a+bx)^{1-2p}}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**p*(b*x+a)**(1-2*p)/x**3,x)

[Out] Integral((c*x**2)**p*(a + b*x)**(1 - 2*p)/x**3, x)

$$3.994 \quad \int \frac{(cx^2)^p (a+bx)^{2-2p}}{x^4} dx$$

Optimal. Leaf size=33

$$\frac{(cx^2)^p (a+bx)^{3-2p}}{a(3-2p)x^3}$$

[Out] $-(c*x^2)^p*(b*x+a)^{(3-2*p)}/a/(3-2*p)/x^3$

Rubi [A] time = 0.01, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {15, 37}

$$\frac{(cx^2)^p (a+bx)^{3-2p}}{a(3-2p)x^3}$$

Antiderivative was successfully verified.

[In] Int[((c*x^2)^p*(a + b*x)^(2 - 2*p))/x^4,x]

[Out] -(((c*x^2)^p*(a + b*x)^(3 - 2*p))/(a*(3 - 2*p)*x^3))

Rule 15

Int[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] :> Dist[(a^IntPart[m]*(a*x^n)^FracPart[m])/x^(n*FracPart[m]), Int[u*x^(m*n), x], x] /; FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(cx^2)^p (a+bx)^{2-2p}}{x^4} dx &= \left(x^{-2p} (cx^2)^p \right) \int x^{-4+2p} (a+bx)^{2-2p} dx \\ &= -\frac{(cx^2)^p (a+bx)^{3-2p}}{a(3-2p)x^3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 0.97

$$\frac{(cx^2)^p (a + bx)^{3-2p}}{a(2p-3)x^3}$$

Antiderivative was successfully verified.

[In] Integrate[((c*x^2)^p*(a + b*x)^(2 - 2*p))/x^4,x]

[Out] ((c*x^2)^p*(a + b*x)^(3 - 2*p))/(a*(-3 + 2*p)*x^3)

fricas [A] time = 0.46, size = 37, normalized size = 1.12

$$\frac{(bx + a)(cx^2)^p (bx + a)^{-2p+2}}{(2ap - 3a)x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(2-2*p)/x^4,x, algorithm="fricas")

[Out] (b*x + a)*(c*x^2)^p*(b*x + a)^(-2*p + 2)/((2*a*p - 3*a)*x^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^p (bx + a)^{-2p+2}}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(2-2*p)/x^4,x, algorithm="giac")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p + 2)/x^4, x)

maple [A] time = 0.00, size = 33, normalized size = 1.00

$$\frac{(cx^2)^p (bx + a)^{-2p+3}}{(2p-3)ax^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c*x^2)^p*(b*x+a)^(-2*p+2)/x^4,x)

[Out] (b*x+a)^(3-2*p)/x^3/a/(2*p-3)*(c*x^2)^p

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(cx^2)^p (bx + a)^{-2p+2}}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x^2)^p*(b*x+a)^(2-2*p)/x^4,x, algorithm="maxima")

[Out] integrate((c*x^2)^p*(b*x + a)^(-2*p + 2)/x^4, x)

mupad [B] time = 0.25, size = 51, normalized size = 1.55

$$\frac{\left(\frac{(cx^2)^p}{2p-3} + \frac{bx(cx^2)^p}{a(2p-3)}\right)(a+bx)^{2-2p}}{x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((c*x^2)^p*(a + b*x)^(2 - 2*p))/x^4,x)

[Out] (((c*x^2)^p/(2*p - 3) + (b*x*(c*x^2)^p)/(a*(2*p - 3)))*(a + b*x)^(2 - 2*p))/x^3

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((c*x**2)**p*(b*x+a)**(2-2*p)/x**4,x)

[Out] Timed out

$$3.995 \quad \int x^m (cx^2)^p (a + bx)^{-2-m-2p} dx$$

Optimal. Leaf size=38

$$\frac{x^{m+1} (cx^2)^p (a + bx)^{-m-2p-1}}{a(m + 2p + 1)}$$

[Out] $x^{(1+m)}*(c*x^2)^p*(b*x+a)^{-1-m-2*p}/a/(1+m+2*p)$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {15, 37}

$$\frac{x^{m+1} (cx^2)^p (a + bx)^{-m-2p-1}}{a(m + 2p + 1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^m*(c*x^2)^p*(a + b*x)^{-2 - m - 2*p}, x]$

[Out] $(x^{(1 + m)}*(c*x^2)^p*(a + b*x)^{-1 - m - 2*p})/(a*(1 + m + 2*p))$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 37

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_.)}*((c_.) + (d_.)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}]/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int x^m (cx^2)^p (a + bx)^{-2-m-2p} dx &= \left(x^{-2p} (cx^2)^p\right) \int x^{m+2p} (a + bx)^{-2-m-2p} dx \\ &= \frac{x^{1+m} (cx^2)^p (a + bx)^{-1-m-2p}}{a(1 + m + 2p)} \end{aligned}$$

Mathematica [A] time = 0.03, size = 38, normalized size = 1.00

$$\frac{x^{m+1} (cx^2)^p (a + bx)^{-m-2p-1}}{a(m + 2p + 1)}$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(c*x^2)^p*(a + b*x)^(-2 - m - 2*p), x]

[Out] (x^(1 + m)*(c*x^2)^p*(a + b*x)^(-1 - m - 2*p))/(a*(1 + m + 2*p))

fricas [A] time = 0.49, size = 49, normalized size = 1.29

$$\frac{(bx^2 + ax)(bx + a)^{-m-2p-2} x^m e^{(p \log(c) + 2p \log(x))}}{am + 2ap + a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(c*x^2)^p*(b*x+a)^(-2-m-2*p), x, algorithm="fricas")

[Out] (b*x^2 + a*x)*(b*x + a)^(-m - 2*p - 2)*x^m*e^(p*log(c) + 2*p*log(x))/(a*m + 2*a*p + a)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^{-m-2p-2} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(c*x^2)^p*(b*x+a)^(-2-m-2*p), x, algorithm="giac")

[Out] integrate((c*x^2)^p*(b*x + a)^(-m - 2*p - 2)*x^m, x)

maple [A] time = 0.00, size = 39, normalized size = 1.03

$$\frac{x^{m+1} (cx^2)^p (bx + a)^{-m-2p-1}}{(m + 2p + 1) a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(c*x^2)^p*(b*x+a)^(-2-m-2*p), x)

[Out] x^(m+1)*(c*x^2)^p*(b*x+a)^(-1-m-2*p)/a/(1+m+2*p)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^{-m-2p-2} x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(c*x²)^p*(b*x+a)^(-2-m-2*p),x, algorithm="maxima")

[Out] integrate((c*x²)^p*(b*x + a)^(-m - 2*p - 2)*x^m, x)

mupad [B] time = 0.34, size = 50, normalized size = 1.32

$$\frac{x x^m (c x^2)^p}{a (a + b x)^m (a + b x)^{2p} (a + b x) (m + 2p + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x^m*(c*x²)^p)/(a + b*x)^(m + 2*p + 2),x)

[Out] (x*x^m*(c*x²)^p)/(a*(a + b*x)^m*(a + b*x)^(2*p)*(a + b*x)*(m + 2*p + 1))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*(c*x**2)**p*(b*x+a)**(-2-m-2*p),x)

[Out] Timed out

$$3.996 \quad \int (dx)^m (cx^2)^p (a + bx)^{-2-m-2p} dx$$

Optimal. Leaf size=39

$$\frac{x (cx^2)^p (dx)^m (a + bx)^{-m-2p-1}}{a(m + 2p + 1)}$$

[Out] $x*(d*x)^m*(c*x^2)^p*(b*x+a)^{-1-m-2*p}/a/(1+m+2*p)$

Rubi [A] time = 0.01, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 27, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {15, 20, 37}

$$\frac{x (cx^2)^p (dx)^m (a + bx)^{-m-2p-1}}{a(m + 2p + 1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(d*x)^m*(c*x^2)^p*(a + b*x)^{-2 - m - 2*p}, x]$

[Out] $(x*(d*x)^m*(c*x^2)^p*(a + b*x)^{-1 - m - 2*p})/(a*(1 + m + 2*p))$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^n)^m, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{n*\text{FracPart}[m]}, \text{Int}[u*x^{m*n}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 20

$\text{Int}[(u_.)*((a_.)*(v_))^{m_*}((b_.)*(v_))^{n_}, x_Symbol] \rightarrow \text{Dist}[(b^{\text{IntPart}[n]}*(b*v)^{\text{FracPart}[n]})/(a^{\text{IntPart}[n]}*(a*v)^{\text{FracPart}[n]}), \text{Int}[u*(a*v)^{m+n}, x], x] /;$ FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

Rule 37

$\text{Int}[(a_. + (b_.)*(x_))^{m_*}((c_.) + (d_.)*(x_))^{n_}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{m+1}*(c + d*x)^{n+1}/((b*c - a*d)*(m+1)), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned}
\int (dx)^m (cx^2)^p (a+bx)^{-2-m-2p} dx &= \left(x^{-2p} (cx^2)^p\right) \int x^{2p} (dx)^m (a+bx)^{-2-m-2p} dx \\
&= \left(x^{-m-2p} (dx)^m (cx^2)^p\right) \int x^{m+2p} (a+bx)^{-2-m-2p} dx \\
&= \frac{x(dx)^m (cx^2)^p (a+bx)^{-1-m-2p}}{a(1+m+2p)}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 39, normalized size = 1.00

$$\frac{x (cx^2)^p (dx)^m (a+bx)^{-m-2p-1}}{a(m+2p+1)}$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^m*(c*x^2)^p*(a+b*x)^(-2-m-2*p),x]

[Out] (x*(d*x)^m*(c*x^2)^p*(a+b*x)^(-1-m-2*p))/(a*(1+m+2*p))

fricas [A] time = 0.47, size = 57, normalized size = 1.46

$$\frac{(bx^2+ax)(bx+a)^{-m-2p-2} (dx)^m e^{(2p \log(dx) + p \log(\frac{c}{a^2}))}}{am+2ap+a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^p*(b*x+a)^(-2-m-2*p),x, algorithm="fricas")

[Out] (b*x^2+a*x)*(b*x+a)^(-m-2*p-2)*(d*x)^m*e^(2*p*log(d*x)+p*log(c/d^2))/(a*m+2*a*p+a)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx+a)^{-m-2p-2} (dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^p*(b*x+a)^(-2-m-2*p),x, algorithm="giac")

[Out] integrate((c*x^2)^p*(b*x+a)^(-m-2*p-2)*(d*x)^m, x)

maple [A] time = 0.00, size = 40, normalized size = 1.03

$$\frac{x (c x^2)^p (dx)^m (bx + a)^{-m-2p-1}}{(m + 2p + 1) a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^p*(b*x+a)^(-2-m-2*p), x)

[Out] x*(d*x)^m*(c*x^2)^p*(b*x+a)^(-m-2*p-1)/a/(m+2*p+1)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^{-m-2p-2} (dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^p*(b*x+a)^(-2-m-2*p), x, algorithm="maxima")

[Out] integrate((c*x^2)^p*(b*x + a)^(-m - 2*p - 2)*(d*x)^m, x)

mupad [B] time = 0.26, size = 39, normalized size = 1.00

$$\frac{x (dx)^m (cx^2)^p}{a (a + bx)^{m+2p+1} (m + 2p + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((d*x)^m*(c*x^2)^p)/(a + b*x)^(m + 2*p + 2), x)

[Out] (x*(d*x)^m*(c*x^2)^p)/(a*(a + b*x)^(m + 2*p + 1)*(m + 2*p + 1))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(c*x**2)**p*(b*x+a)**(-2-m-2*p), x)

[Out] Timed out

$$3.997 \quad \int x^m (cx^2)^p (a + bx)^n dx$$

Optimal. Leaf size=63

$$\frac{x^{m+1} (cx^2)^p (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(-n, m + 2p + 1; m + 2p + 2; -\frac{bx}{a}\right)}{m + 2p + 1}$$

[Out] $x^{(1+m)}*(c*x^2)^p*(b*x+a)^n*\text{hypergeom}([-n, 1+m+2*p], [2+m+2*p], -b*x/a)/(1+m+2*p)/((1+b*x/a)^n)$

Rubi [A] time = 0.02, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {15, 66, 64}

$$\frac{x^{m+1} (cx^2)^p (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(-n, m + 2p + 1; m + 2p + 2; -\frac{bx}{a}\right)}{m + 2p + 1}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^m*(c*x^2)^p*(a + b*x)^n, x]$

[Out] $(x^{(1 + m)}*(c*x^2)^p*(a + b*x)^n*\text{Hypergeometric2F1}[-n, 1 + m + 2*p, 2 + m + 2*p, -((b*x)/a)])/((1 + m + 2*p)*(1 + (b*x)/a)^n)$

Rule 15

$\text{Int}[(u_*)*((a_*)*(x_)^{(n_)})^{(m_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{IntegerQ}[m]$

Rule 64

$\text{Int}[(b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(c^n*(b*x)^{(m+1)}*\text{Hypergeometric2F1}[-n, m+1, m+2, -((d*x)/c)])/(b*(m+1)), x] /; \text{FreeQ}\{b, c, d, m, n\}, x] \&\& \text{IntegerQ}[m] \&\& (\text{IntegerQ}[n] \parallel (\text{GtQ}[c, 0] \&\& \text{!(EqQ}[n, -2^{(-1)}] \&\& \text{EqQ}[c^2 - d^2, 0] \&\& \text{GtQ}[-(d/(b*c)), 0])))$

Rule 66

$\text{Int}[(b_*)*(x_)^{(m_*)}*((c_*) + (d_*)*(x_)^{(n_)}, x_Symbol] \rightarrow \text{Dist}[(c^{\text{IntPart}[n]}*(c + d*x)^{\text{FracPart}[n]})/(1 + (d*x)/c)^{\text{FracPart}[n]}, \text{Int}[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; \text{FreeQ}\{b, c, d, m, n\}, x] \&\& \text{IntegerQ}[m] \&\& \text{IntegerQ}[n] \&\& \text{!(GtQ}[c, 0] \&\& \text{!(GtQ}[-(d/(b*c)), 0] \&\& (\text{RationalQ}[m] \&\& \text{!(EqQ}[n, -$

$2^{(-1)} \&\& \text{EqQ}[c^2 - d^2, 0]) \mid \mid \text{!RationalQ}[n])$

Rubi steps

$$\begin{aligned} \int x^m (cx^2)^p (a + bx)^n dx &= \left(x^{-2p} (cx^2)^p \right) \int x^{m+2p} (a + bx)^n dx \\ &= \left(x^{-2p} (cx^2)^p (a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} \right) \int x^{m+2p} \left(1 + \frac{bx}{a} \right)^n dx \\ &= \frac{x^{1+m} (cx^2)^p (a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} {}_2F_1 \left(-n, 1 + m + 2p; 2 + m + 2p; -\frac{bx}{a} \right)}{1 + m + 2p} \end{aligned}$$

Mathematica [A] time = 0.01, size = 63, normalized size = 1.00

$$\frac{x^{m+1} (cx^2)^p (a + bx)^n \left(\frac{bx}{a} + 1 \right)^{-n} {}_2F_1 \left(-n, m + 2p + 1; m + 2p + 2; -\frac{bx}{a} \right)}{m + 2p + 1}$$

Antiderivative was successfully verified.

[In] Integrate[x^m*(c*x^2)^p*(a + b*x)^n,x]

[Out] (x^(1 + m)*(c*x^2)^p*(a + b*x)^n*Hypergeometric2F1[-n, 1 + m + 2*p, 2 + m + 2*p, -(b*x)/a])/((1 + m + 2*p)*(1 + (b*x)/a)^n)

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral} \left((cx^2)^p (bx + a)^n x^m, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(c*x^2)^p*(b*x+a)^n,x, algorithm="fricas")

[Out] integral((c*x^2)^p*(b*x + a)^n*x^m, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^n x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(c*x^2)^p*(b*x+a)^n,x, algorithm="giac")

[Out] integrate((c*x^2)^p*(b*x + a)^n*x^m, x)

maple [F] time = 0.12, size = 0, normalized size = 0.00

$$\int x^m (c x^2)^p (b x + a)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(c*x^2)^p*(b*x+a)^n,x)

[Out] int(x^m*(c*x^2)^p*(b*x+a)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (c x^2)^p (b x + a)^n x^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*(c*x^2)^p*(b*x+a)^n,x, algorithm="maxima")

[Out] integrate((c*x^2)^p*(b*x + a)^n*x^m, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int x^m (c x^2)^p (a + b x)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*(c*x^2)^p*(a + b*x)^n,x)

[Out] int(x^m*(c*x^2)^p*(a + b*x)^n, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^m (c x^2)^p (a + b x)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*(c*x**2)**p*(b*x+a)**n,x)

[Out] Integral(x**m*(c*x**2)**p*(a + b*x)**n, x)

3.998 $\int (dx)^m (cx^2)^p (a + bx)^n dx$

Optimal. Leaf size=68

$$\frac{(cx^2)^p (dx)^{m+1} (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(-n, m + 2p + 1; m + 2p + 2; -\frac{bx}{a}\right)}{d(m + 2p + 1)}$$

[Out] $(d*x)^{(1+m)}*(c*x^2)^p*(b*x+a)^n*\text{hypergeom}([-n, 1+m+2*p], [2+m+2*p], -b*x/a)/d$
 $/((1+m+2*p)/((1+b*x/a)^n))$

Rubi [A] time = 0.02, antiderivative size = 64, normalized size of antiderivative = 0.94,
 number of steps used = 4, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} =$
 0.200, Rules used = {15, 20, 66, 64}

$$\frac{x (cx^2)^p (dx)^m (a + bx)^n \left(\frac{bx}{a} + 1\right)^{-n} {}_2F_1\left(-n, m + 2p + 1; m + 2p + 2; -\frac{bx}{a}\right)}{m + 2p + 1}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(d*x)^m*(c*x^2)^p*(a + b*x)^n, x]$

[Out] $(x*(d*x)^m*(c*x^2)^p*(a + b*x)^n*\text{Hypergeometric2F1}[-n, 1 + m + 2*p, 2 + m +$
 $2*p, -((b*x)/a)]/((1 + m + 2*p)*(1 + (b*x)/a)^n)$

Rule 15

$\text{Int}[(u_.)*((a_.)*(x_)^(n_))^(m_), x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[m]}*(a*x^n)^{\text{FracPart}[m]})/x^{(n*\text{FracPart}[m])}, \text{Int}[u*x^{(m*n)}, x], x] /;$ FreeQ[{a, m, n}, x] && !IntegerQ[m]

Rule 20

$\text{Int}[(u_.)*((a_.)*(v_))^(m_)*((b_.)*(v_))^(n_), x_Symbol] \rightarrow \text{Dist}[(b^{\text{IntPart}[n]}*(b*v)^{\text{FracPart}[n]})/(a^{\text{IntPart}[n]}*(a*v)^{\text{FracPart}[n]}), \text{Int}[u*(a*v)^{(m+n)}, x], x] /;$ FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

Rule 64

$\text{Int}[(b_.)*(x_)^(m_)*((c_) + (d_.)*(x_)^(n_)), x_Symbol] \rightarrow \text{Simp}[(c^n*(b*x)^{(m+1)}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -((d*x)/c)]/(b*(m + 1)), x] /;$ FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && (IntegerQ[n] || (GtQ[c, 0] && !(EqQ[n, -2^(-1)] && EqQ[c^2 - d^2, 0] && GtQ[-(d/(b*c)), 0]))

Rule 66

```
Int[((b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c^IntPart[n]*(c + d*x)^FracPart[n])/(1 + (d*x)/c)^FracPart[n], Int[(b*x)^m*(1 + (d*x)/c)^n, x], x] /; FreeQ[{b, c, d, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !GtQ[c, 0] && !GtQ[-(d/(b*c)), 0] && ((RationalQ[m] && !(EqQ[n, -2^(-1)]) && EqQ[c^2 - d^2, 0])) || !RationalQ[n])
```

Rubi steps

$$\begin{aligned} \int (dx)^m (cx^2)^p (a + bx)^n dx &= \left(x^{-2p} (cx^2)^p \right) \int x^{2p} (dx)^m (a + bx)^n dx \\ &= \left(x^{-m-2p} (dx)^m (cx^2)^p \right) \int x^{m+2p} (a + bx)^n dx \\ &= \left(x^{-m-2p} (dx)^m (cx^2)^p (a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} \right) \int x^{m+2p} \left(1 + \frac{bx}{a} \right)^n dx \\ &= \frac{x (dx)^m (cx^2)^p (a + bx)^n \left(1 + \frac{bx}{a} \right)^{-n} {}_2F_1 \left(-n, 1 + m + 2p; 2 + m + 2p; -\frac{bx}{a} \right)}{1 + m + 2p} \end{aligned}$$

Mathematica [A] time = 0.01, size = 64, normalized size = 0.94

$$\frac{x (cx^2)^p (dx)^m (a + bx)^n \left(\frac{bx}{a} + 1 \right)^{-n} {}_2F_1 \left(-n, m + 2p + 1; m + 2p + 2; -\frac{bx}{a} \right)}{m + 2p + 1}$$

Antiderivative was successfully verified.

```
[In] Integrate[(d*x)^m*(c*x^2)^p*(a + b*x)^n,x]
```

```
[Out] (x*(d*x)^m*(c*x^2)^p*(a + b*x)^n*Hypergeometric2F1[-n, 1 + m + 2*p, 2 + m + 2*p, -((b*x)/a)])/((1 + m + 2*p)*(1 + (b*x)/a)^n)
```

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(cx^2\right)^p (bx + a)^n (dx)^m, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^m*(c*x^2)^p*(b*x+a)^n,x, algorithm="fricas")
```

```
[Out] integral((c*x^2)^p*(b*x + a)^n*(d*x)^m, x)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^n (dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^p*(b*x+a)^n,x, algorithm="giac")

[Out] integrate((c*x^2)^p*(b*x + a)^n*(d*x)^m, x)

maple [F] time = 0.18, size = 0, normalized size = 0.00

$$\int (cx^2)^p (dx)^m (bx + a)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^p*(b*x+a)^n,x)

[Out] int((d*x)^m*(c*x^2)^p*(b*x+a)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (bx + a)^n (dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^m*(c*x^2)^p*(b*x+a)^n,x, algorithm="maxima")

[Out] integrate((c*x^2)^p*(b*x + a)^n*(d*x)^m, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (dx)^m (cx^2)^p (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^m*(c*x^2)^p*(a + b*x)^n,x)

[Out] int((d*x)^m*(c*x^2)^p*(a + b*x)^n, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (cx^2)^p (dx)^m (a + bx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**m*(c*x**2)**p*(b*x+a)**n,x)

[Out] Integral((c*x**2)**p*(d*x)**m*(a + b*x)**n, x)

$$3.999 \quad \int \frac{(a+bx)^5}{\left(\frac{ad}{b}+dx\right)^3} dx$$

Optimal. Leaf size=17

$$\frac{b^2(a+bx)^3}{3d^3}$$

[Out] 1/3*b^2*(b*x+a)^3/d^3

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$\frac{b^2(a+bx)^3}{3d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/((a*d)/b + d*x)^3,x]

[Out] (b^2*(a + b*x)^3)/(3*d^3)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{\left(\frac{ad}{b}+dx\right)^3} dx &= \frac{b^3 \int (a+bx)^2 dx}{d^3} \\ &= \frac{b^2(a+bx)^3}{3d^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{b^2(a + bx)^3}{3d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/((a*d)/b + d*x)^3,x]

[Out] (b^2*(a + b*x)^3)/(3*d^3)

fricas [B] time = 0.40, size = 31, normalized size = 1.82

$$\frac{b^5x^3 + 3ab^4x^2 + 3a^2b^3x}{3d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(a*d/b+d*x)^3,x, algorithm="fricas")

[Out] 1/3*(b^5*x^3 + 3*a*b^4*x^2 + 3*a^2*b^3*x)/d^3

giac [B] time = 1.09, size = 31, normalized size = 1.82

$$\frac{b^5x^3 + 3ab^4x^2 + 3a^2b^3x}{3d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(a*d/b+d*x)^3,x, algorithm="giac")

[Out] 1/3*(b^5*x^3 + 3*a*b^4*x^2 + 3*a^2*b^3*x)/d^3

maple [A] time = 0.00, size = 16, normalized size = 0.94

$$\frac{(bx + a)^3 b^2}{3d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(a*d/b+d*x)^3,x)

[Out] 1/3*b^2*(b*x+a)^3/d^3

maxima [B] time = 1.37, size = 31, normalized size = 1.82

$$\frac{b^5x^3 + 3ab^4x^2 + 3a^2b^3x}{3d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(a*d/b+d*x)^3,x, algorithm="maxima")

[Out] 1/3*(b^5*x^3 + 3*a*b^4*x^2 + 3*a^2*b^3*x)/d^3

mupad [B] time = 0.05, size = 27, normalized size = 1.59

$$\frac{b^3 x (3 a^2 + 3 a b x + b^2 x^2)}{3 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/(d*x + (a*d)/b)^3,x)

[Out] (b^3*x*(3*a^2 + b^2*x^2 + 3*a*b*x))/(3*d^3)

sympy [B] time = 0.12, size = 34, normalized size = 2.00

$$\frac{a^2 b^3 x}{d^3} + \frac{a b^4 x^2}{d^3} + \frac{b^5 x^3}{3 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/(a*d/b+d*x)**3,x)

[Out] a**2*b**3*x/d**3 + a*b**4*x**2/d**3 + b**5*x**3/(3*d**3)

$$3.1000 \quad \int \frac{(a+bx)^4}{\left(\frac{ad}{b}+dx\right)^3} dx$$

Optimal. Leaf size=23

$$\frac{ab^3x}{d^3} + \frac{b^4x^2}{2d^3}$$

[Out] $a*b^3*x/d^3+1/2*b^4*x^2/d^3$

Rubi [A] time = 0.01, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.050$, Rules used = {21}

$$\frac{ab^3x}{d^3} + \frac{b^4x^2}{2d^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^4/((a*d)/b + d*x)^3, x]$

[Out] $(a*b^3*x)/d^3 + (b^4*x^2)/(2*d^3)$

Rule 21

$\text{Int}[(u_.)*((a_.) + (b_.)*(v_))^(m_.)*((c_.) + (d_.)*(v_))^(n_.), x_Symbol] \rightarrow$
 $\text{Dist}[(b/d)^m, \text{Int}[u*(c + d*v)^(m + n), x], x] /;$ FreeQ[{a, b, c, d, n}, x]
 && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
 a + b*x])

Rubi steps

$$\int \frac{(a+bx)^4}{\left(\frac{ad}{b}+dx\right)^3} dx = \frac{b^3 \int (a+bx) dx}{d^3}$$

$$= \frac{ab^3x}{d^3} + \frac{b^4x^2}{2d^3}$$

Mathematica [A] time = 0.00, size = 19, normalized size = 0.83

$$\frac{b^3 \left(ax + \frac{bx^2}{2} \right)}{d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4/((a*d)/b + d*x)^3,x]

[Out] (b^3*(a*x + (b*x^2)/2))/d^3

fricas [A] time = 0.47, size = 20, normalized size = 0.87

$$\frac{b^4x^2 + 2ab^3x}{2d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(a*d/b+d*x)^3,x, algorithm="fricas")

[Out] 1/2*(b^4*x^2 + 2*a*b^3*x)/d^3

giac [A] time = 1.19, size = 20, normalized size = 0.87

$$\frac{b^4x^2 + 2ab^3x}{2d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(a*d/b+d*x)^3,x, algorithm="giac")

[Out] 1/2*(b^4*x^2 + 2*a*b^3*x)/d^3

maple [A] time = 0.00, size = 18, normalized size = 0.78

$$\frac{\left(\frac{1}{2}bx^2 + ax\right)b^3}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4/(a*d/b+d*x)^3,x)

[Out] b^3/d^3*(1/2*b*x^2+a*x)

maxima [A] time = 1.24, size = 20, normalized size = 0.87

$$\frac{b^4x^2 + 2ab^3x}{2d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(a*d/b+d*x)^3,x, algorithm="maxima")

[Out] 1/2*(b^4*x^2 + 2*a*b^3*x)/d^3

mupad [B] time = 0.03, size = 16, normalized size = 0.70

$$\frac{b^3 x (2a + b x)}{2d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^4/(d*x + (a*d)/b)^3,x)`

[Out] `(b^3*x*(2*a + b*x))/(2*d^3)`

sympy [A] time = 0.12, size = 20, normalized size = 0.87

$$\frac{ab^3x}{d^3} + \frac{b^4x^2}{2d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**4/(a*d/b+d*x)**3,x)`

[Out] `a*b**3*x/d**3 + b**4*x**2/(2*d**3)`

$$3.1001 \quad \int \frac{(a+bx)^3}{\left(\frac{ad}{b}+dx\right)^3} dx$$

Optimal. Leaf size=8

$$\frac{b^3x}{d^3}$$

[Out] b³*x/d³

Rubi [A] time = 0.00, antiderivative size = 8, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 8}

$$\frac{b^3x}{d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/((a*d)/b + d*x)^3,x]

[Out] (b³*x)/d³

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
&& EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
a + b*x])

Rubi steps

$$\int \frac{(a+bx)^3}{\left(\frac{ad}{b}+dx\right)^3} dx = \frac{b^3 \int 1 dx}{d^3}$$

$$= \frac{b^3x}{d^3}$$

Mathematica [A] time = 0.00, size = 8, normalized size = 1.00

$$\frac{b^3x}{d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/((a*d)/b + d*x)^3,x]

[Out] (b^3*x)/d^3

fricas [A] time = 0.45, size = 8, normalized size = 1.00

$$\frac{b^3x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(a*d/b+d*x)^3,x, algorithm="fricas")

[Out] b^3*x/d^3

giac [A] time = 1.00, size = 8, normalized size = 1.00

$$\frac{b^3x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(a*d/b+d*x)^3,x, algorithm="giac")

[Out] b^3*x/d^3

maple [A] time = 0.00, size = 9, normalized size = 1.12

$$\frac{b^3x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/(a*d/b+d*x)^3,x)

[Out] b^3*x/d^3

maxima [A] time = 1.27, size = 8, normalized size = 1.00

$$\frac{b^3x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(a*d/b+d*x)^3,x, algorithm="maxima")

[Out] b^3*x/d^3

mupad [B] time = 0.01, size = 8, normalized size = 1.00

$$\frac{b^3 x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3/(d*x + (a*d)/b)^3,x)

[Out] (b^3*x)/d^3

sympy [A] time = 0.11, size = 7, normalized size = 0.88

$$\frac{b^3 x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3/(a*d/b+d*x)**3,x)

[Out] b**3*x/d**3

$$3.1002 \quad \int \frac{(a+bx)^2}{\left(\frac{ad}{b}+dx\right)^3} dx$$

Optimal. Leaf size=13

$$\frac{b^2 \log(a+bx)}{d^3}$$

[Out] $b^2 \ln(b*x+a)/d^3$

Rubi [A] time = 0.00, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 31}

$$\frac{b^2 \log(a+bx)}{d^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^2/((a*d)/b + d*x)^3, x]$

[Out] $(b^2*\text{Log}[a + b*x])/d^3$

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 31

```
Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x,
x]]/b, x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{\left(\frac{ad}{b}+dx\right)^3} dx &= \frac{b^3 \int \frac{1}{a+bx} dx}{d^3} \\ &= \frac{b^2 \log(a+bx)}{d^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 13, normalized size = 1.00

$$\frac{b^2 \log(a + bx)}{d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/((a*d)/b + d*x)^3,x]

[Out] (b^2*Log[a + b*x])/d^3

fricas [A] time = 0.42, size = 13, normalized size = 1.00

$$\frac{b^2 \log(bx + a)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(a*d/b+d*x)^3,x, algorithm="fricas")

[Out] b^2*log(b*x + a)/d^3

giac [A] time = 1.07, size = 14, normalized size = 1.08

$$\frac{b^2 \log(|bx + a|)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(a*d/b+d*x)^3,x, algorithm="giac")

[Out] b^2*log(abs(b*x + a))/d^3

maple [A] time = 0.00, size = 14, normalized size = 1.08

$$\frac{b^2 \ln(bx + a)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(a*d/b+d*x)^3,x)

[Out] b^2*ln(b*x+a)/d^3

maxima [A] time = 1.31, size = 13, normalized size = 1.00

$$\frac{b^2 \log(bx + a)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(a*d/b+d*x)^3,x, algorithm="maxima")

[Out] b^2*log(b*x + a)/d^3

mupad [B] time = 0.05, size = 13, normalized size = 1.00

$$\frac{b^2 \ln(a + b x)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(d*x + (a*d)/b)^3,x)

[Out] (b^2*log(a + b*x))/d^3

sympy [A] time = 0.11, size = 19, normalized size = 1.46

$$\frac{b^2 \log(ad^3 + bd^3x)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(a*d/b+d*x)**3,x)

[Out] b**2*log(a*d**3 + b*d**3*x)/d**3

$$3.1003 \quad \int \frac{a+bx}{\left(\frac{ad}{b}+dx\right)^3} dx$$

Optimal. Leaf size=15

$$-\frac{b^2}{d^3(a+bx)}$$

[Out] $-b^2/d^3/(b*x+a)$

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 32}

$$-\frac{b^2}{d^3(a+bx)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)/((a*d)/b + d*x)^3, x]$

[Out] $-(b^2/(d^3*(a + b*x)))$

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{\left(\frac{ad}{b}+dx\right)^3} dx &= \frac{b^3 \int \frac{1}{(a+bx)^2} dx}{d^3} \\ &= -\frac{b^2}{d^3(a+bx)} \end{aligned}$$

Mathematica [A] time = 0.00, size = 15, normalized size = 1.00

$$-\frac{b^2}{d^3(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/((a*d)/b + d*x)^3,x]

[Out] -(b^2/(d^3*(a + b*x)))

fricas [A] time = 0.44, size = 19, normalized size = 1.27

$$-\frac{b^2}{bd^3x + ad^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(a*d/b+d*x)^3,x, algorithm="fricas")

[Out] -b^2/(b*d^3*x + a*d^3)

giac [A] time = 0.99, size = 15, normalized size = 1.00

$$-\frac{b^2}{(bx+a)d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(a*d/b+d*x)^3,x, algorithm="giac")

[Out] -b^2/((b*x + a)*d^3)

maple [A] time = 0.00, size = 16, normalized size = 1.07

$$-\frac{b^2}{(bx+a)d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/(a*d/b+d*x)^3,x)

[Out] -b^2/d^3/(b*x+a)

maxima [A] time = 1.34, size = 19, normalized size = 1.27

$$-\frac{b^2}{bd^3x + ad^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(a*d/b+d*x)^3,x, algorithm="maxima")

[Out] -b^2/(b*d^3*x + a*d^3)

mupad [B] time = 0.04, size = 15, normalized size = 1.00

$$-\frac{b^2}{d^3 (a + b x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(d*x + (a*d)/b)^3,x)

[Out] -b^2/(d^3*(a + b*x))

sympy [A] time = 0.18, size = 19, normalized size = 1.27

$$-\frac{b^3}{abd^3 + b^2d^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(a*d/b+d*x)**3,x)

[Out] -b**3/(a*b*d**3 + b**2*d**3*x)

$$3.1004 \quad \int \frac{1}{(a+bx)\left(\frac{ad}{b}+dx\right)^3} dx$$

Optimal. Leaf size=17

$$-\frac{b^2}{3d^3(a+bx)^3}$$

[Out] $-1/3*b^2/d^3/(b*x+a)^3$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$-\frac{b^2}{3d^3(a+bx)^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)*((a*d)/b + d*x)^3), x]$

[Out] $-b^2/(3*d^3*(a + b*x)^3)$

Rule 21

$\text{Int}[(u_.)*((a_.) + (b_.)*(v_))^{(m_.)}*((c_.) + (d_.)*(v_))^{(n_.)}, x_Symbol] \rightarrow \text{Dist}[(b/d)^m, \text{Int}[u*(c + d*v)^{(m+n)}, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\& \text{EqQ}[b*c - a*d, 0] \&\& \text{IntegerQ}[m] \&\& (!\text{IntegerQ}[n] \mid\mid \text{SimplerQ}[c + d*x, a + b*x])$

Rule 32

$\text{Int}[(a_.) + (b_.)*(x_))^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}/(b*(m+1)), x] /; \text{FreeQ}\{a, b, m\}, x] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)\left(\frac{ad}{b}+dx\right)^3} dx &= \frac{b^3 \int \frac{1}{(a+bx)^4} dx}{d^3} \\ &= -\frac{b^2}{3d^3(a+bx)^3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 17, normalized size = 1.00

$$-\frac{b^2}{3d^3(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*((a*d)/b + d*x)^3),x]

[Out] -1/3*b^2/(d^3*(a + b*x)^3)

fricas [B] time = 0.41, size = 47, normalized size = 2.76

$$-\frac{b^2}{3(b^3d^3x^3 + 3ab^2d^3x^2 + 3a^2bd^3x + a^3d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(a*d/b+d*x)^3,x, algorithm="fricas")

[Out] -1/3*b^2/(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)

giac [A] time = 1.19, size = 15, normalized size = 0.88

$$-\frac{b^2}{3(bx+a)^3d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(a*d/b+d*x)^3,x, algorithm="giac")

[Out] -1/3*b^2/((b*x + a)^3*d^3)

maple [A] time = 0.00, size = 16, normalized size = 0.94

$$-\frac{b^2}{3(bx+a)^3d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)/(a*d/b+d*x)^3,x)

[Out] -1/3*b^2/d^3/(b*x+a)^3

maxima [B] time = 1.31, size = 47, normalized size = 2.76

$$-\frac{b^2}{3(b^3d^3x^3 + 3ab^2d^3x^2 + 3a^2bd^3x + a^3d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(a*d/b+d*x)^3,x, algorithm="maxima")

[Out] $-1/3*b^2/(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)$

mupad [B] time = 0.15, size = 49, normalized size = 2.88

$$-\frac{b^2}{3(a^3 d^3 + 3 a^2 b d^3 x + 3 a b^2 d^3 x^2 + b^3 d^3 x^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((d*x + (a*d)/b)^3*(a + b*x)),x)

[Out] $-b^2/(3*(a^3*d^3 + b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x))$

sympy [B] time = 0.29, size = 53, normalized size = 3.12

$$-\frac{b^3}{3a^3bd^3 + 9a^2b^2d^3x + 9ab^3d^3x^2 + 3b^4d^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(a*d/b+d*x)**3,x)

[Out] $-b**3/(3*a**3*b*d**3 + 9*a**2*b**2*d**3*x + 9*a*b**3*d**3*x**2 + 3*b**4*d**3*x**3)$

$$3.1005 \quad \int \frac{1}{(a+bx)^2 \left(\frac{ad}{b} + dx\right)^3} dx$$

Optimal. Leaf size=17

$$-\frac{b^2}{4d^3(a+bx)^4}$$

[Out] $-1/4*b^2/d^3/(b*x+a)^4$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$-\frac{b^2}{4d^3(a+bx)^4}$$

Antiderivative was successfully verified.

[In] `Int[1/((a + b*x)^2*((a*d)/b + d*x)^3),x]`

[Out] $-b^2/(4*d^3*(a + b*x)^4)$

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\int \frac{1}{(a+bx)^2 \left(\frac{ad}{b} + dx\right)^3} dx = \frac{b^3 \int \frac{1}{(a+bx)^5} dx}{d^3}$$

$$= -\frac{b^2}{4d^3(a+bx)^4}$$

Mathematica [A] time = 0.01, size = 17, normalized size = 1.00

$$-\frac{b^2}{4d^3(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*((a*d)/b + d*x)^3), x]

[Out] -1/4*b^2/(d^3*(a + b*x)^4)

fricas [B] time = 0.43, size = 61, normalized size = 3.59

$$-\frac{b^2}{4(b^4d^3x^4 + 4ab^3d^3x^3 + 6a^2b^2d^3x^2 + 4a^3bd^3x + a^4d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(a*d/b+d*x)^3,x, algorithm="fricas")

[Out] -1/4*b^2/(b^4*d^3*x^4 + 4*a*b^3*d^3*x^3 + 6*a^2*b^2*d^3*x^2 + 4*a^3*b*d^3*x + a^4*d^3)

giac [A] time = 0.91, size = 15, normalized size = 0.88

$$-\frac{b^2}{4(bx+a)^4d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(a*d/b+d*x)^3,x, algorithm="giac")

[Out] -1/4*b^2/((b*x + a)^4*d^3)

maple [A] time = 0.00, size = 16, normalized size = 0.94

$$-\frac{b^2}{4(bx+a)^4d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/(a*d/b+d*x)^3,x)

[Out] -1/4*b^2/d^3/(b*x+a)^4

maxima [B] time = 1.35, size = 61, normalized size = 3.59

$$-\frac{b^2}{4(b^4d^3x^4 + 4ab^3d^3x^3 + 6a^2b^2d^3x^2 + 4a^3bd^3x + a^4d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(a*d/b+d*x)^3,x, algorithm="maxima")

[Out] $-1/4*b^2/(b^4*d^3*x^4 + 4*a*b^3*d^3*x^3 + 6*a^2*b^2*d^3*x^2 + 4*a^3*b*d^3*x + a^4*d^3)$

mupad [B] time = 0.06, size = 63, normalized size = 3.71

$$-\frac{b^2}{4(a^4 d^3 + 4 a^3 b d^3 x + 6 a^2 b^2 d^3 x^2 + 4 a b^3 d^3 x^3 + b^4 d^3 x^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((d*x + (a*d)/b)^3*(a + b*x)^2),x)

[Out] $-b^2/(4*(a^4*d^3 + b^4*d^3*x^4 + 4*a*b^3*d^3*x^3 + 6*a^2*b^2*d^3*x^2 + 4*a^3*b*d^3*x))$

sympy [B] time = 0.36, size = 68, normalized size = 4.00

$$-\frac{b^3}{4a^4bd^3 + 16a^3b^2d^3x + 24a^2b^3d^3x^2 + 16ab^4d^3x^3 + 4b^5d^3x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2/(a*d/b+d*x)**3,x)

[Out] $-b**3/(4*a**4*b*d**3 + 16*a**3*b**2*d**3*x + 24*a**2*b**3*d**3*x**2 + 16*a*b**4*d**3*x**3 + 4*b**5*d**3*x**4)$

$$3.1006 \quad \int \frac{1}{(a+bx)^3 \left(\frac{ad}{b} + dx\right)^3} dx$$

Optimal. Leaf size=17

$$-\frac{b^2}{5d^3(a+bx)^5}$$

[Out] -1/5*b^2/d^3/(b*x+a)^5

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$-\frac{b^2}{5d^3(a+bx)^5}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^3*((a*d)/b + d*x)^3), x]

[Out] -b^2/(5*d^3*(a + b*x)^5)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^3 \left(\frac{ad}{b} + dx\right)^3} dx &= \frac{b^3 \int \frac{1}{(a+bx)^6} dx}{d^3} \\ &= -\frac{b^2}{5d^3(a+bx)^5} \end{aligned}$$

Mathematica [A] time = 0.01, size = 17, normalized size = 1.00

$$-\frac{b^2}{5d^3(a+bx)^5}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^3*((a*d)/b + d*x)^3), x]

[Out] -1/5*b^2/(d^3*(a + b*x)^5)

fricas [B] time = 0.43, size = 75, normalized size = 4.41

$$-\frac{b^2}{5(b^5d^3x^5 + 5ab^4d^3x^4 + 10a^2b^3d^3x^3 + 10a^3b^2d^3x^2 + 5a^4bd^3x + a^5d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(a*d/b+d*x)^3,x, algorithm="fricas")

[Out] -1/5*b^2/(b^5*d^3*x^5 + 5*a*b^4*d^3*x^4 + 10*a^2*b^3*d^3*x^3 + 10*a^3*b^2*d^3*x^2 + 5*a^4*b*d^3*x + a^5*d^3)

giac [A] time = 0.96, size = 15, normalized size = 0.88

$$-\frac{b^2}{5(bx+a)^5d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(a*d/b+d*x)^3,x, algorithm="giac")

[Out] -1/5*b^2/((b*x + a)^5*d^3)

maple [A] time = 0.00, size = 16, normalized size = 0.94

$$-\frac{b^2}{5(bx+a)^5d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^3/(a*d/b+d*x)^3,x)

[Out] -1/5*b^2/d^3/(b*x+a)^5

maxima [B] time = 1.33, size = 75, normalized size = 4.41

$$-\frac{b^2}{5(b^5d^3x^5 + 5ab^4d^3x^4 + 10a^2b^3d^3x^3 + 10a^3b^2d^3x^2 + 5a^4bd^3x + a^5d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(a*d/b+d*x)^3,x, algorithm="maxima")

[Out] $-1/5*b^2/(b^5*d^3*x^5 + 5*a*b^4*d^3*x^4 + 10*a^2*b^3*d^3*x^3 + 10*a^3*b^2*d^3*x^2 + 5*a^4*b*d^3*x + a^5*d^3)$

mupad [B] time = 0.05, size = 77, normalized size = 4.53

$$\frac{b^2}{5 \left(a^5 d^3 + 5 a^4 b d^3 x + 10 a^3 b^2 d^3 x^2 + 10 a^2 b^3 d^3 x^3 + 5 a b^4 d^3 x^4 + b^5 d^3 x^5 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((d*x + (a*d)/b)^3*(a + b*x)^3),x)

[Out] $-b^2/(5*(a^5*d^3 + b^5*d^3*x^5 + 5*a*b^4*d^3*x^4 + 10*a^3*b^2*d^3*x^2 + 10*a^2*b^3*d^3*x^3 + 5*a^4*b*d^3*x))$

sympy [B] time = 0.42, size = 83, normalized size = 4.88

$$\frac{b^3}{5a^5bd^3 + 25a^4b^2d^3x + 50a^3b^3d^3x^2 + 50a^2b^4d^3x^3 + 25ab^5d^3x^4 + 5b^6d^3x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**3/(a*d/b+d*x)**3,x)

[Out] $-b**3/(5*a**5*b*d**3 + 25*a**4*b**2*d**3*x + 50*a**3*b**3*d**3*x**2 + 50*a**2*b**4*d**3*x**3 + 25*a*b**5*d**3*x**4 + 5*b**6*d**3*x**5)$

$$3.1007 \quad \int \frac{\left(\frac{bc}{d} + bx\right)^5}{(c+dx)^3} dx$$

Optimal. Leaf size=17

$$\frac{b^5(c+dx)^3}{3d^6}$$

[Out] 1/3*b^5*(d*x+c)^3/d^6

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$\frac{b^5(c+dx)^3}{3d^6}$$

Antiderivative was successfully verified.

[In] Int[((b*c)/d + b*x)^5/(c + d*x)^3,x]

[Out] (b^5*(c + d*x)^3)/(3*d^6)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int \frac{\left(\frac{bc}{d} + bx\right)^5}{(c+dx)^3} dx &= \frac{b^5 \int (c+dx)^2 dx}{d^5} \\ &= \frac{b^5(c+dx)^3}{3d^6} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{b^5(c + dx)^3}{3d^6}$$

Antiderivative was successfully verified.

[In] Integrate[((b*c)/d + b*x)^5/(c + d*x)^3,x]

[Out] (b^5*(c + d*x)^3)/(3*d^6)

fricas [B] time = 0.43, size = 35, normalized size = 2.06

$$\frac{b^5 d^2 x^3 + 3 b^5 c d x^2 + 3 b^5 c^2 x}{3 d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^5/(d*x+c)^3,x, algorithm="fricas")

[Out] 1/3*(b^5*d^2*x^3 + 3*b^5*c*d*x^2 + 3*b^5*c^2*x)/d^5

giac [B] time = 1.01, size = 35, normalized size = 2.06

$$\frac{b^5 d^2 x^3 + 3 b^5 c d x^2 + 3 b^5 c^2 x}{3 d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^5/(d*x+c)^3,x, algorithm="giac")

[Out] 1/3*(b^5*d^2*x^3 + 3*b^5*c*d*x^2 + 3*b^5*c^2*x)/d^5

maple [A] time = 0.00, size = 16, normalized size = 0.94

$$\frac{(dx + c)^3 b^5}{3d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*c/d+b*x)^5/(d*x+c)^3,x)

[Out] 1/3*b^5*(d*x+c)^3/d^6

maxima [B] time = 1.37, size = 35, normalized size = 2.06

$$\frac{b^5 d^2 x^3 + 3 b^5 c d x^2 + 3 b^5 c^2 x}{3 d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^5/(d*x+c)^3,x, algorithm="maxima")

[Out] 1/3*(b^5*d^2*x^3 + 3*b^5*c*d*x^2 + 3*b^5*c^2*x)/d^5

mupad [B] time = 0.16, size = 27, normalized size = 1.59

$$\frac{b^5 x (3c^2 + 3cdx + d^2 x^2)}{3d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x + (b*c)/d)^5/(c + d*x)^3,x)

[Out] (b^5*x*(3*c^2 + d^2*x^2 + 3*c*d*x))/(3*d^5)

sympy [B] time = 0.13, size = 34, normalized size = 2.00

$$\frac{b^5 c^2 x}{d^5} + \frac{b^5 c x^2}{d^4} + \frac{b^5 x^3}{3d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)**5/(d*x+c)**3,x)

[Out] b**5*c**2*x/d**5 + b**5*c*x**2/d**4 + b**5*x**3/(3*d**3)

$$3.1008 \quad \int \frac{\left(\frac{bc}{d} + bx\right)^4}{(c+dx)^3} dx$$

Optimal. Leaf size=23

$$\frac{b^4 cx}{d^4} + \frac{b^4 x^2}{2d^3}$$

[Out] $b^4 c x / d^4 + 1/2 b^4 x^2 / d^3$

Rubi [A] time = 0.00, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.050$, Rules used = {21}

$$\frac{b^4 cx}{d^4} + \frac{b^4 x^2}{2d^3}$$

Antiderivative was successfully verified.

[In] `Int[((b*c)/d + b*x)^4/(c + d*x)^3,x]`

[Out] $(b^4 c x) / d^4 + (b^4 x^2) / (2 d^3)$

Rule 21

```
Int[(u_)*((a_) + (b_)*(v_))^(m_)*((c_) + (d_)*(v_))^(n_), x_Symbol] :=
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rubi steps

$$\begin{aligned} \int \frac{\left(\frac{bc}{d} + bx\right)^4}{(c+dx)^3} dx &= \frac{b^4 \int (c+dx) dx}{d^4} \\ &= \frac{b^4 cx}{d^4} + \frac{b^4 x^2}{2d^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 19, normalized size = 0.83

$$\frac{b^4 \left(cx + \frac{dx^2}{2} \right)}{d^4}$$

Antiderivative was successfully verified.

[In] Integrate[((b*c)/d + b*x)^4/(c + d*x)^3,x]

[Out] (b^4*(c*x + (d*x^2)/2))/d^4

fricas [A] time = 0.41, size = 21, normalized size = 0.91

$$\frac{b^4 dx^2 + 2 b^4 cx}{2 d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^4/(d*x+c)^3,x, algorithm="fricas")

[Out] 1/2*(b^4*d*x^2 + 2*b^4*c*x)/d^4

giac [A] time = 1.04, size = 21, normalized size = 0.91

$$\frac{b^4 dx^2 + 2 b^4 cx}{2 d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^4/(d*x+c)^3,x, algorithm="giac")

[Out] 1/2*(b^4*d*x^2 + 2*b^4*c*x)/d^4

maple [A] time = 0.00, size = 18, normalized size = 0.78

$$\frac{\left(\frac{1}{2} d x^2 + c x\right) b^4}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*c/d+b*x)^4/(d*x+c)^3,x)

[Out] b^4/d^4*(c*x+1/2*d*x^2)

maxima [A] time = 1.32, size = 21, normalized size = 0.91

$$\frac{b^4 dx^2 + 2 b^4 cx}{2 d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^4/(d*x+c)^3,x, algorithm="maxima")

[Out] 1/2*(b^4*d*x^2 + 2*b^4*c*x)/d^4

mupad [B] time = 0.03, size = 16, normalized size = 0.70

$$\frac{b^4 x (2c + dx)}{2d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x + (b*c)/d)^4/(c + d*x)^3, x)`

[Out] `(b^4*x*(2*c + d*x))/(2*d^4)`

sympy [A] time = 0.12, size = 20, normalized size = 0.87

$$\frac{b^4 cx}{d^4} + \frac{b^4 x^2}{2d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*c/d+b*x)**4/(d*x+c)**3, x)`

[Out] `b**4*c*x/d**4 + b**4*x**2/(2*d**3)`

$$3.1009 \quad \int \frac{\left(\frac{bc}{d} + bx\right)^3}{(c+dx)^3} dx$$

Optimal. Leaf size=8

$$\frac{b^3x}{d^3}$$

[Out] b^3x/d^3

Rubi [A] time = 0.00, antiderivative size = 8, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 8}

$$\frac{b^3x}{d^3}$$

Antiderivative was successfully verified.

[In] Int[((b*c)/d + b*x)^3/(c + d*x)^3,x]

[Out] (b^3*x)/d^3

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] := Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x] && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x, a + b*x])

Rubi steps

$$\int \frac{\left(\frac{bc}{d} + bx\right)^3}{(c + dx)^3} dx = \frac{b^3 \int 1 dx}{d^3} = \frac{b^3x}{d^3}$$

Mathematica [A] time = 0.00, size = 8, normalized size = 1.00

$$\frac{b^3x}{d^3}$$

Antiderivative was successfully verified.

[In] Integrate[((b*c)/d + b*x)^3/(c + d*x)^3,x]

[Out] (b^3*x)/d^3

fricas [A] time = 0.40, size = 8, normalized size = 1.00

$$\frac{b^3x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^3/(d*x+c)^3,x, algorithm="fricas")

[Out] b^3*x/d^3

giac [A] time = 1.05, size = 8, normalized size = 1.00

$$\frac{b^3x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^3/(d*x+c)^3,x, algorithm="giac")

[Out] b^3*x/d^3

maple [A] time = 0.00, size = 9, normalized size = 1.12

$$\frac{b^3x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*c/d+b*x)^3/(d*x+c)^3,x)

[Out] b^3/d^3*x

maxima [A] time = 1.33, size = 8, normalized size = 1.00

$$\frac{b^3x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^3/(d*x+c)^3,x, algorithm="maxima")

[Out] b^3*x/d^3

mupad [B] time = 0.01, size = 8, normalized size = 1.00

$$\frac{b^3 x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x + (b*c)/d)^3/(c + d*x)^3,x)`

[Out] `(b^3*x)/d^3`

sympy [A] time = 0.10, size = 7, normalized size = 0.88

$$\frac{b^3 x}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*c/d+b*x)**3/(d*x+c)**3,x)`

[Out] `b**3*x/d**3`

$$3.1010 \quad \int \frac{\left(\frac{bc}{d} + bx\right)^2}{(c+dx)^3} dx$$

Optimal. Leaf size=13

$$\frac{b^2 \log(c + dx)}{d^3}$$

[Out] $b^2 \ln(d*x+c)/d^3$

Rubi [A] time = 0.00, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 31}

$$\frac{b^2 \log(c + dx)}{d^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\left(\frac{b*c}{d} + b*x\right)^2/(c + d*x)^3, x]$

[Out] $(b^2 * \text{Log}[c + d*x])/d^3$

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplifyQ[c + d*x,
  a + b*x])
```

Rule 31

```
Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] :> Simp[Log[RemoveContent[a + b*x,
x]]/b, x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\begin{aligned} \int \frac{\left(\frac{bc}{d} + bx\right)^2}{(c + dx)^3} dx &= \frac{b^2 \int \frac{1}{c+dx} dx}{d^2} \\ &= \frac{b^2 \log(c + dx)}{d^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 13, normalized size = 1.00

$$\frac{b^2 \log(c + dx)}{d^3}$$

Antiderivative was successfully verified.

[In] Integrate[((b*c)/d + b*x)^2/(c + d*x)^3,x]

[Out] (b^2*Log[c + d*x])/d^3

fricas [A] time = 0.41, size = 13, normalized size = 1.00

$$\frac{b^2 \log(dx + c)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^2/(d*x+c)^3,x, algorithm="fricas")

[Out] b^2*log(d*x + c)/d^3

giac [A] time = 0.89, size = 14, normalized size = 1.08

$$\frac{b^2 \log(|dx + c|)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^2/(d*x+c)^3,x, algorithm="giac")

[Out] b^2*log(abs(d*x + c))/d^3

maple [A] time = 0.00, size = 14, normalized size = 1.08

$$\frac{b^2 \ln(dx + c)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*c/d+b*x)^2/(d*x+c)^3,x)

[Out] b^2*ln(d*x+c)/d^3

maxima [A] time = 1.37, size = 13, normalized size = 1.00

$$\frac{b^2 \log(dx + c)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)^2/(d*x+c)^3,x, algorithm="maxima")

[Out] b^2*log(d*x + c)/d^3

mupad [B] time = 0.14, size = 13, normalized size = 1.00

$$\frac{b^2 \ln(c + dx)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x + (b*c)/d)^2/(c + d*x)^3,x)

[Out] (b^2*log(c + d*x))/d^3

sympy [A] time = 0.10, size = 17, normalized size = 1.31

$$\frac{b^2 \log(cd^2 + d^3x)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)**2/(d*x+c)**3,x)

[Out] b**2*log(c*d**2 + d**3*x)/d**3

$$3.1011 \quad \int \frac{\frac{bc}{d} + bx}{(c+dx)^3} dx$$

Optimal. Leaf size=13

$$-\frac{b}{d^2(c+dx)}$$

[Out] $-b/d^2/(d*x+c)$

Rubi [A] time = 0.00, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 32}

$$-\frac{b}{d^2(c+dx)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(b*c)/d + b*x)/(c + d*x)^3, x]$

[Out] $-(b/(d^2*(c + d*x)))$

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int \frac{\frac{bc}{d} + bx}{(c+dx)^3} dx &= \frac{b \int \frac{1}{(c+dx)^2} dx}{d} \\ &= -\frac{b}{d^2(c+dx)} \end{aligned}$$

Mathematica [A] time = 0.00, size = 13, normalized size = 1.00

$$-\frac{b}{d^2(c+dx)}$$

Antiderivative was successfully verified.

[In] Integrate[((b*c)/d + b*x)/(c + d*x)^3,x]

[Out] -(b/(d^2*(c + d*x)))

fricas [A] time = 0.42, size = 16, normalized size = 1.23

$$-\frac{b}{d^3x + cd^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)/(d*x+c)^3,x, algorithm="fricas")

[Out] -b/(d^3*x + c*d^2)

giac [A] time = 1.00, size = 13, normalized size = 1.00

$$-\frac{b}{(dx + c)d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)/(d*x+c)^3,x, algorithm="giac")

[Out] -b/((d*x + c)*d^2)

maple [A] time = 0.00, size = 14, normalized size = 1.08

$$-\frac{b}{(dx + c)d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*c/d+b*x)/(d*x+c)^3,x)

[Out] -b/d^2/(d*x+c)

maxima [A] time = 1.38, size = 16, normalized size = 1.23

$$-\frac{b}{d^3x + cd^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*c/d+b*x)/(d*x+c)^3,x, algorithm="maxima")

[Out] -b/(d^3*x + c*d^2)

mupad [B] time = 0.04, size = 13, normalized size = 1.00

$$-\frac{b}{d^2 (c + d x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x + (b*c)/d)/(c + d*x)^3,x)`

[Out] `-b/(d^2*(c + d*x))`

sympy [A] time = 0.15, size = 12, normalized size = 0.92

$$-\frac{b}{cd^2 + d^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*c/d+b*x)/(d*x+c)**3,x)`

[Out] `-b/(c*d**2 + d**3*x)`

$$3.1012 \quad \int \frac{1}{\left(\frac{bc}{d} + bx\right)(c+dx)^3} dx$$

Optimal. Leaf size=14

$$-\frac{1}{3b(c+dx)^3}$$

[Out] -1/3/b/(d*x+c)^3

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$-\frac{1}{3b(c+dx)^3}$$

Antiderivative was successfully verified.

[In] Int[1/(((b*c)/d + b*x)*(c + d*x)^3), x]

[Out] -1/(3*b*(c + d*x)^3)

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
 Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
 && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
 a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\left(\frac{bc}{d} + bx\right)(c+dx)^3} dx = \frac{d \int \frac{1}{(c+dx)^4} dx}{b}$$

$$= -\frac{1}{3b(c+dx)^3}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\frac{1}{3b(c+dx)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/(((b*c)/d + b*x)*(c + d*x)^3), x]

[Out] -1/3*1/(b*(c + d*x)^3)

fricas [B] time = 0.41, size = 36, normalized size = 2.57

$$-\frac{1}{3\left(bd^3x^3 + 3bcd^2x^2 + 3bc^2dx + bc^3\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)/(d*x+c)^3,x, algorithm="fricas")

[Out] -1/3/(b*d^3*x^3 + 3*b*c*d^2*x^2 + 3*b*c^2*d*x + b*c^3)

giac [A] time = 1.14, size = 12, normalized size = 0.86

$$-\frac{1}{3(dx+c)^3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)/(d*x+c)^3,x, algorithm="giac")

[Out] -1/3/((d*x + c)^3*b)

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$-\frac{1}{3(dx+c)^3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*c/d+b*x)/(d*x+c)^3,x)

[Out] -1/3/b/(d*x+c)^3

maxima [B] time = 1.34, size = 36, normalized size = 2.57

$$-\frac{1}{3\left(bd^3x^3 + 3bcd^2x^2 + 3bc^2dx + bc^3\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)/(d*x+c)^3,x, algorithm="maxima")

[Out] -1/3/(b*d^3*x^3 + 3*b*c*d^2*x^2 + 3*b*c^2*d*x + b*c^3)

mupad [B] time = 0.05, size = 38, normalized size = 2.71

$$-\frac{1}{3bc^3 + 9bc^2dx + 9bcd^2x^2 + 3bd^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x + (b*c)/d)*(c + d*x)^3),x)

[Out] -1/(3*b*c^3 + 3*b*d^3*x^3 + 9*b*c^2*d*x + 9*b*c*d^2*x^2)

sympy [B] time = 0.28, size = 44, normalized size = 3.14

$$-\frac{d}{3bc^3d + 9bc^2d^2x + 9bcd^3x^2 + 3bd^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)/(d*x+c)**3,x)

[Out] -d/(3*b*c**3*d + 9*b*c**2*d**2*x + 9*b*c*d**3*x**2 + 3*b*d**4*x**3)

$$3.1013 \quad \int \frac{1}{\left(\frac{bc}{d} + bx\right)^2 (c+dx)^3} dx$$

Optimal. Leaf size=15

$$-\frac{d}{4b^2(c+dx)^4}$$

[Out] -1/4*d/b^2/(d*x+c)^4

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$-\frac{d}{4b^2(c+dx)^4}$$

Antiderivative was successfully verified.

[In] Int[1/(((b*c)/d + b*x)^2*(c + d*x)^3),x]

[Out] -d/(4*b^2*(c + d*x)^4)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\int \frac{1}{\left(\frac{bc}{d} + bx\right)^2 (c+dx)^3} dx = \frac{d^2 \int \frac{1}{(c+dx)^5} dx}{b^2}$$

$$= -\frac{d}{4b^2(c+dx)^4}$$

Mathematica [A] time = 0.01, size = 15, normalized size = 1.00

$$-\frac{d}{4b^2(c+dx)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/(((b*c)/d + b*x)^2*(c + d*x)^3), x]

[Out] -1/4*d/(b^2*(c + d*x)^4)

fricas [B] time = 0.41, size = 59, normalized size = 3.93

$$-\frac{d}{4(b^2d^4x^4 + 4b^2cd^3x^3 + 6b^2c^2d^2x^2 + 4b^2c^3dx + b^2c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)^2/(d*x+c)^3,x, algorithm="fricas")

[Out] -1/4*d/(b^2*d^4*x^4 + 4*b^2*c*d^3*x^3 + 6*b^2*c^2*d^2*x^2 + 4*b^2*c^3*d*x + b^2*c^4)

giac [A] time = 0.98, size = 20, normalized size = 1.33

$$-\frac{b^2}{4\left(bx + \frac{bc}{d}\right)^4 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)^2/(d*x+c)^3,x, algorithm="giac")

[Out] -1/4*b^2/((b*x + b*c/d)^4*d^3)

maple [A] time = 0.00, size = 14, normalized size = 0.93

$$-\frac{d}{4(dx+c)^4 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*c/d+b*x)^2/(d*x+c)^3,x)

[Out] -1/4*d/b^2/(d*x+c)^4

maxima [B] time = 1.35, size = 59, normalized size = 3.93

$$\frac{d}{4(b^2 d^4 x^4 + 4 b^2 c d^3 x^3 + 6 b^2 c^2 d^2 x^2 + 4 b^2 c^3 d x + b^2 c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)^2/(d*x+c)^3,x, algorithm="maxima")

[Out] -1/4*d/(b^2*d^4*x^4 + 4*b^2*c*d^3*x^3 + 6*b^2*c^2*d^2*x^2 + 4*b^2*c^3*d*x + b^2*c^4)

mupad [B] time = 0.05, size = 61, normalized size = 4.07

$$\frac{d}{4(b^2 c^4 + 4 b^2 c^3 d x + 6 b^2 c^2 d^2 x^2 + 4 b^2 c d^3 x^3 + b^2 d^4 x^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x + (b*c)/d)^2*(c + d*x)^3),x)

[Out] -d/(4*(b^2*c^4 + b^2*d^4*x^4 + 4*b^2*c*d^3*x^3 + 6*b^2*c^2*d^2*x^2 + 4*b^2*c^3*d*x))

sympy [B] time = 0.36, size = 68, normalized size = 4.53

$$\frac{d^2}{4b^2c^4d + 16b^2c^3d^2x + 24b^2c^2d^3x^2 + 16b^2cd^4x^3 + 4b^2d^5x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)**2/(d*x+c)**3,x)

[Out] -d**2/(4*b**2*c**4*d + 16*b**2*c**3*d**2*x + 24*b**2*c**2*d**3*x**2 + 16*b**2*c*d**4*x**3 + 4*b**2*d**5*x**4)

$$3.1014 \quad \int \frac{1}{\left(\frac{bc}{d} + bx\right)^3 (c+dx)^3} dx$$

Optimal. Leaf size=17

$$-\frac{d^2}{5b^3(c+dx)^5}$$

[Out] $-1/5*d^2/b^3/(d*x+c)^5$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$-\frac{d^2}{5b^3(c+dx)^5}$$

Antiderivative was successfully verified.

[In] Int[1/(((b*c)/d + b*x)^3*(c + d*x)^3), x]

[Out] $-d^2/(5*b^3*(c + d*x)^5)$

Rule 21

Int[(u_.)*((a_.) + (b_.)*(v_.))^(m_.)*((c_.) + (d_.)*(v_.))^(n_.), x_Symbol] :=
Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
&& EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_.))^(m_.), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{1}{\left(\frac{bc}{d} + bx\right)^3 (c+dx)^3} dx &= \frac{d^3 \int \frac{1}{(c+dx)^6} dx}{b^3} \\ &= -\frac{d^2}{5b^3(c+dx)^5} \end{aligned}$$

Mathematica [A] time = 0.01, size = 17, normalized size = 1.00

$$-\frac{d^2}{5b^3(c+dx)^5}$$

Antiderivative was successfully verified.

[In] Integrate[1/(((b*c)/d + b*x)^3*(c + d*x)^3), x]

[Out] -1/5*d^2/(b^3*(c + d*x)^5)

fricas [B] time = 0.45, size = 75, normalized size = 4.41

$$\frac{d^2}{5(b^3d^5x^5 + 5b^3cd^4x^4 + 10b^3c^2d^3x^3 + 10b^3c^3d^2x^2 + 5b^3c^4dx + b^3c^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)^3/(d*x+c)^3,x, algorithm="fricas")

[Out] -1/5*d^2/(b^3*d^5*x^5 + 5*b^3*c*d^4*x^4 + 10*b^3*c^2*d^3*x^3 + 10*b^3*c^3*d^2*x^2 + 5*b^3*c^4*d*x + b^3*c^5)

giac [A] time = 0.92, size = 15, normalized size = 0.88

$$-\frac{d^2}{5(dx+c)^5b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)^3/(d*x+c)^3,x, algorithm="giac")

[Out] -1/5*d^2/((d*x + c)^5*b^3)

maple [A] time = 0.00, size = 16, normalized size = 0.94

$$-\frac{d^2}{5(dx+c)^5b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*c/d+b*x)^3/(d*x+c)^3,x)

[Out] -1/5*d^2/b^3/(d*x+c)^5

maxima [B] time = 1.36, size = 75, normalized size = 4.41

$$\frac{d^2}{5(b^3d^5x^5 + 5b^3cd^4x^4 + 10b^3c^2d^3x^3 + 10b^3c^3d^2x^2 + 5b^3c^4dx + b^3c^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)^3/(d*x+c)^3,x, algorithm="maxima")

[Out] $-1/5*d^2/(b^3*d^5*x^5 + 5*b^3*c*d^4*x^4 + 10*b^3*c^2*d^3*x^3 + 10*b^3*c^3*d^2*x^2 + 5*b^3*c^4*d*x + b^3*c^5)$

mupad [B] time = 0.17, size = 77, normalized size = 4.53

$$\frac{d^2}{5 \left(b^3 c^5 + 5 b^3 c^4 d x + 10 b^3 c^3 d^2 x^2 + 10 b^3 c^2 d^3 x^3 + 5 b^3 c d^4 x^4 + b^3 d^5 x^5 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x + (b*c)/d)^3*(c + d*x)^3),x)

[Out] $-d^2/(5*(b^3*c^5 + b^3*d^5*x^5 + 5*b^3*c*d^4*x^4 + 10*b^3*c^3*d^2*x^2 + 10*b^3*c^2*d^3*x^3 + 5*b^3*c^4*d*x))$

sympy [B] time = 0.42, size = 83, normalized size = 4.88

$$\frac{d^3}{5b^3c^5d + 25b^3c^4d^2x + 50b^3c^3d^3x^2 + 50b^3c^2d^4x^3 + 25b^3cd^5x^4 + 5b^3d^6x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*c/d+b*x)**3/(d*x+c)**3,x)

[Out] $-d**3/(5*b**3*c**5*d + 25*b**3*c**4*d**2*x + 50*b**3*c**3*d**3*x**2 + 50*b**3*c**2*d**4*x**3 + 25*b**3*c*d**5*x**4 + 5*b**3*d**6*x**5)$

3.1015 $\int (a + bx)^5 (ac + bcx)^n dx$

Optimal. Leaf size=24

$$\frac{(ac + bcx)^{n+6}}{bc^6(n + 6)}$$

[Out] $(b*c*x+a*c)^{(6+n)}/b/c^6/(6+n)$

Rubi [A] time = 0.01, antiderivative size = 24, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 32}

$$\frac{(ac + bcx)^{n+6}}{bc^6(n + 6)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^5*(a*c + b*c*x)^n, x]$

[Out] $(a*c + b*c*x)^{(6 + n)}/(b*c^6*(6 + n))$

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int (a + bx)^5 (ac + bcx)^n dx &= \frac{\int (ac + bcx)^{5+n} dx}{c^5} \\ &= \frac{(ac + bcx)^{6+n}}{bc^6(6 + n)} \end{aligned}$$

Mathematica [A] time = 0.02, size = 25, normalized size = 1.04

$$\frac{(a + bx)^6 (c(a + bx))^n}{b(n + 6)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*(a*c + b*c*x)^n,x]

[Out] ((a + b*x)^6*(c*(a + b*x))^n)/(b*(6 + n))

fricas [B] time = 0.45, size = 80, normalized size = 3.33

$$\frac{(b^6x^6 + 6ab^5x^5 + 15a^2b^4x^4 + 20a^3b^3x^3 + 15a^4b^2x^2 + 6a^5bx + a^6)(bcx + ac)^n}{bn + 6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^n,x, algorithm="fricas")

[Out] (b^6*x^6 + 6*a*b^5*x^5 + 15*a^2*b^4*x^4 + 20*a^3*b^3*x^3 + 15*a^4*b^2*x^2 + 6*a^5*b*x + a^6)*(b*c*x + a*c)^n/(b*n + 6*b)

giac [B] time = 1.13, size = 141, normalized size = 5.88

$$\frac{(bcx + ac)^n b^6 x^6 + 6 (bcx + ac)^n ab^5 x^5 + 15 (bcx + ac)^n a^2 b^4 x^4 + 20 (bcx + ac)^n a^3 b^3 x^3 + 15 (bcx + ac)^n a^4 b^2 x^2 + 6 (bcx + ac)^n a^5 b x + a^6 (bcx + ac)^n}{bn + 6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^n,x, algorithm="giac")

[Out] ((b*c*x + a*c)^n*b^6*x^6 + 6*(b*c*x + a*c)^n*a*b^5*x^5 + 15*(b*c*x + a*c)^n*a^2*b^4*x^4 + 20*(b*c*x + a*c)^n*a^3*b^3*x^3 + 15*(b*c*x + a*c)^n*a^4*b^2*x^2 + 6*(b*c*x + a*c)^n*a^5*b*x + (b*c*x + a*c)^n*a^6)/(b*n + 6*b)

maple [A] time = 0.00, size = 27, normalized size = 1.12

$$\frac{(bx + a)^6 (bcx + ac)^n}{(n + 6)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5*(b*c*x+a*c)^n,x)

[Out] (b*x+a)^6/b/(6+n)*(b*c*x+a*c)^n

maxima [B] time = 1.81, size = 649, normalized size = 27.04

$$\frac{5(b^2c^n(n+1)x^2 + abc^n nx - a^2c^n)(bx + a)^n a^4}{(n^2 + 3n + 2)b} + \frac{10((n^2 + 3n + 2)b^3c^n x^3 + (n^2 + n)ab^2c^n x^2 - 2a^2bc^n nx + 2a^3c^n)}{(n^3 + 6n^2 + 11n + 6)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^n,x, algorithm="maxima")

[Out] $5*(b^2*c^n*(n+1)*x^2 + a*b*c^n*n*x - a^2*c^n)*(b*x+a)^n*a^4/((n^2+3*n+2)*b) + 10*((n^2+3*n+2)*b^3*c^n*x^3 + (n^2+n)*a*b^2*c^n*x^2 - 2*a^2*b*c^n*n*x + 2*a^3*c^n)*(b*x+a)^n*a^3/((n^3+6*n^2+11*n+6)*b) + (b*c*x+a*c)^{(n+1)}*a^5/(b*c*(n+1)) + 10*((n^3+6*n^2+11*n+6)*b^4*c^n*x^4 + (n^3+3*n^2+2*n)*a*b^3*c^n*x^3 - 3*(n^2+n)*a^2*b^2*c^n*x^2 + 6*a^3*b*c^n*n*x - 6*a^4*c^n)*(b*x+a)^n*a^2/((n^4+10*n^3+35*n^2+50*n+24)*b) + 5*((n^4+10*n^3+35*n^2+50*n+24)*b^5*c^n*x^5 + (n^4+6*n^3+11*n^2+6*n)*a*b^4*c^n*x^4 - 4*(n^3+3*n^2+2*n)*a^2*b^3*c^n*x^3 + 12*(n^2+n)*a^3*b^2*c^n*x^2 - 24*a^4*b*c^n*n*x + 24*a^5*c^n)*(b*x+a)^n*a/((n^5+15*n^4+85*n^3+225*n^2+274*n+120)*b) + ((n^5+15*n^4+85*n^3+225*n^2+274*n+120)*b^6*c^n*x^6 + (n^5+10*n^4+35*n^3+50*n^2+24*n)*a*b^5*c^n*x^5 - 5*(n^4+6*n^3+11*n^2+6*n)*a^2*b^4*c^n*x^4 + 20*(n^3+3*n^2+2*n)*a^3*b^3*c^n*x^3 - 60*(n^2+n)*a^4*b^2*c^n*x^2 + 120*a^5*b*c^n*n*x - 120*a^6*c^n)*(b*x+a)^n/((n^6+21*n^5+175*n^4+735*n^3+1624*n^2+1764*n+720)*b)$

mupad [B] time = 0.33, size = 107, normalized size = 4.46

$$(ac + bcx)^n \left(\frac{a^6}{b(n+6)} + \frac{b^5 x^6}{n+6} + \frac{6a^5 x}{n+6} + \frac{15a^4 b x^2}{n+6} + \frac{6a b^4 x^5}{n+6} + \frac{20a^3 b^2 x^3}{n+6} + \frac{15a^2 b^3 x^4}{n+6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c + b*c*x)^n*(a + b*x)^5,x)

[Out] $(a*c + b*c*x)^n*(a^6/(b*(n+6)) + (b^5*x^6)/(n+6) + (6*a^5*x)/(n+6) + (15*a^4*b*x^2)/(n+6) + (6*a*b^4*x^5)/(n+6) + (20*a^3*b^2*x^3)/(n+6) + (15*a^2*b^3*x^4)/(n+6))$

sympy [A] time = 2.29, size = 212, normalized size = 8.83

$$\left\{ \begin{array}{l} \frac{x}{ac^6} \\ a^5 x (ac)^n \\ \frac{\log\left(\frac{a}{b}+x\right)}{bc^6} \\ \frac{a^6(ac+bcx)^n}{bn+6b} + \frac{6a^5bx(ac+bcx)^n}{bn+6b} + \frac{15a^4b^2x^2(ac+bcx)^n}{bn+6b} + \frac{20a^3b^3x^3(ac+bcx)^n}{bn+6b} + \frac{15a^2b^4x^4(ac+bcx)^n}{bn+6b} + \frac{6ab^5x^5(ac+bcx)^n}{bn+6b} + \frac{b^6x^6(ac+bcx)^n}{bn+6b} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5*(b*c*x+a*c)**n,x)

```
[Out] Piecewise((x/(a*c**6), Eq(b, 0) & Eq(n, -6)), (a**5*x*(a*c)**n, Eq(b, 0)),
(log(a/b + x)/(b*c**6), Eq(n, -6)), (a**6*(a*c + b*c*x)**n/(b*n + 6*b) + 6*
a**5*b*x*(a*c + b*c*x)**n/(b*n + 6*b) + 15*a**4*b**2*x**2*(a*c + b*c*x)**n/
(b*n + 6*b) + 20*a**3*b**3*x**3*(a*c + b*c*x)**n/(b*n + 6*b) + 15*a**2*b**4
*x**4*(a*c + b*c*x)**n/(b*n + 6*b) + 6*a*b**5*x**5*(a*c + b*c*x)**n/(b*n +
6*b) + b**6*x**6*(a*c + b*c*x)**n/(b*n + 6*b), True))
```

3.1016 $\int (a + bx)^5 (ac + bcx)^3 dx$

Optimal. Leaf size=17

$$\frac{c^3(a + bx)^9}{9b}$$

[Out] 1/9*c^3*(b*x+a)^9/b

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 32}

$$\frac{c^3(a + bx)^9}{9b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*(a*c + b*c*x)^3,x]

[Out] (c^3*(a + b*x)^9)/(9*b)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int (a + bx)^5 (ac + bcx)^3 dx &= c^3 \int (a + bx)^8 dx \\ &= \frac{c^3(a + bx)^9}{9b} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{c^3(a + bx)^9}{9b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*(a*c + b*c*x)^3,x]

[Out] (c^3*(a + b*x)^9)/(9*b)

fricas [B] time = 0.37, size = 113, normalized size = 6.65

$$\frac{1}{9}x^9c^3b^8+x^8c^3b^7a+4x^7c^3b^6a^2+\frac{28}{3}x^6c^3b^5a^3+14x^5c^3b^4a^4+14x^4c^3b^3a^5+\frac{28}{3}x^3c^3b^2a^6+4x^2c^3ba^7+xc^3a^8$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^3,x, algorithm="fricas")

[Out] 1/9*x^9*c^3*b^8 + x^8*c^3*b^7*a + 4*x^7*c^3*b^6*a^2 + 28/3*x^6*c^3*b^5*a^3 + 14*x^5*c^3*b^4*a^4 + 14*x^4*c^3*b^3*a^5 + 28/3*x^3*c^3*b^2*a^6 + 4*x^2*c^3*b*a^7 + x*c^3*a^8

giac [B] time = 0.96, size = 113, normalized size = 6.65

$$\frac{1}{9}b^8c^3x^9+ab^7c^3x^8+4a^2b^6c^3x^7+\frac{28}{3}a^3b^5c^3x^6+14a^4b^4c^3x^5+14a^5b^3c^3x^4+\frac{28}{3}a^6b^2c^3x^3+4a^7bc^3x^2+a^8c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^3,x, algorithm="giac")

[Out] 1/9*b^8*c^3*x^9 + a*b^7*c^3*x^8 + 4*a^2*b^6*c^3*x^7 + 28/3*a^3*b^5*c^3*x^6 + 14*a^4*b^4*c^3*x^5 + 14*a^5*b^3*c^3*x^4 + 28/3*a^6*b^2*c^3*x^3 + 4*a^7*b*c^3*x^2 + a^8*c^3*x

maple [B] time = 0.00, size = 114, normalized size = 6.71

$$\frac{1}{9}b^8c^3x^9+ab^7c^3x^8+4a^2b^6c^3x^7+\frac{28}{3}a^3b^5c^3x^6+14a^4b^4c^3x^5+14a^5b^3c^3x^4+\frac{28}{3}a^6b^2c^3x^3+4a^7bc^3x^2+a^8c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5*(b*c*x+a*c)^3,x)

[Out] 1/9*b^8*c^3*x^9+a*b^7*c^3*x^8+4*a^2*b^6*c^3*x^7+28/3*a^3*b^5*c^3*x^6+14*a^4*b^4*c^3*x^5+14*a^5*b^3*c^3*x^4+28/3*a^6*c^3*b^2*x^3+4*a^7*c^3*b*x^2+a^8*c^3*x

maxima [B] time = 1.31, size = 113, normalized size = 6.65

$$\frac{1}{9}b^8c^3x^9+ab^7c^3x^8+4a^2b^6c^3x^7+\frac{28}{3}a^3b^5c^3x^6+14a^4b^4c^3x^5+14a^5b^3c^3x^4+\frac{28}{3}a^6b^2c^3x^3+4a^7bc^3x^2+a^8c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^3,x, algorithm="maxima")

[Out] $\frac{1}{9}b^8c^3x^9 + ab^7c^3x^8 + 4a^2b^6c^3x^7 + \frac{28}{3}a^3b^5c^3x^6 + 14a^4b^4c^3x^5 + 14a^5b^3c^3x^4 + \frac{28}{3}a^6b^2c^3x^3 + 4a^7b^1c^3x^2 + a^8c^3x$

mupad [B] time = 0.05, size = 113, normalized size = 6.65

$$a^8c^3x + 4a^7bc^3x^2 + \frac{28a^6b^2c^3x^3}{3} + 14a^5b^3c^3x^4 + 14a^4b^4c^3x^5 + \frac{28a^3b^5c^3x^6}{3} + 4a^2b^6c^3x^7 + ab^7c^3x^8 + \frac{b^8c^3x^9}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c + b*c*x)^3*(a + b*x)^5,x)

[Out] $a^8c^3x + (b^8c^3x^9)/9 + 4a^7b^1c^3x^2 + ab^7c^3x^8 + (28a^6b^2c^3x^3)/3 + 14a^5b^3c^3x^4 + 14a^4b^4c^3x^5 + (28a^3b^5c^3x^6)/3 + 4a^2b^6c^3x^7$

sympy [B] time = 0.10, size = 124, normalized size = 7.29

$$a^8c^3x + 4a^7bc^3x^2 + \frac{28a^6b^2c^3x^3}{3} + 14a^5b^3c^3x^4 + 14a^4b^4c^3x^5 + \frac{28a^3b^5c^3x^6}{3} + 4a^2b^6c^3x^7 + ab^7c^3x^8 + \frac{b^8c^3x^9}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5*(b*c*x+a*c)**3,x)

[Out] $a**8*c**3*x + 4*a**7*b*c**3*x**2 + 28*a**6*b**2*c**3*x**3/3 + 14*a**5*b**3*c**3*x**4 + 14*a**4*b**4*c**3*x**5 + 28*a**3*b**5*c**3*x**6/3 + 4*a**2*b**6*c**3*x**7 + a*b**7*c**3*x**8 + b**8*c**3*x**9/9$

$$3.1017 \quad \int (a + bx)^5 (ac + bcx)^2 dx$$

Optimal. Leaf size=17

$$\frac{c^2(a + bx)^8}{8b}$$

[Out] 1/8*c^2*(b*x+a)^8/b

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 32}

$$\frac{c^2(a + bx)^8}{8b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*(a*c + b*c*x)^2,x]

[Out] (c^2*(a + b*x)^8)/(8*b)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int (a + bx)^5 (ac + bcx)^2 dx &= c^2 \int (a + bx)^7 dx \\ &= \frac{c^2(a + bx)^8}{8b} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{c^2(a + bx)^8}{8b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*(a*c + b*c*x)^2,x]

[Out] (c^2*(a + b*x)^8)/(8*b)

fricas [B] time = 0.37, size = 99, normalized size = 5.82

$$\frac{1}{8}x^8c^2b^7 + x^7c^2b^6a + \frac{7}{2}x^6c^2b^5a^2 + 7x^5c^2b^4a^3 + \frac{35}{4}x^4c^2b^3a^4 + 7x^3c^2b^2a^5 + \frac{7}{2}x^2c^2ba^6 + xc^2a^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^2,x, algorithm="fricas")

[Out] 1/8*x^8*c^2*b^7 + x^7*c^2*b^6*a + 7/2*x^6*c^2*b^5*a^2 + 7*x^5*c^2*b^4*a^3 + 35/4*x^4*c^2*b^3*a^4 + 7*x^3*c^2*b^2*a^5 + 7/2*x^2*c^2*b*a^6 + x*c^2*a^7

giac [B] time = 0.99, size = 99, normalized size = 5.82

$$\frac{1}{8}b^7c^2x^8 + ab^6c^2x^7 + \frac{7}{2}a^2b^5c^2x^6 + 7a^3b^4c^2x^5 + \frac{35}{4}a^4b^3c^2x^4 + 7a^5b^2c^2x^3 + \frac{7}{2}a^6bc^2x^2 + a^7c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^2,x, algorithm="giac")

[Out] 1/8*b^7*c^2*x^8 + a*b^6*c^2*x^7 + 7/2*a^2*b^5*c^2*x^6 + 7*a^3*b^4*c^2*x^5 + 35/4*a^4*b^3*c^2*x^4 + 7*a^5*b^2*c^2*x^3 + 7/2*a^6*b*c^2*x^2 + a^7*c^2*x

maple [B] time = 0.00, size = 100, normalized size = 5.88

$$\frac{1}{8}b^7c^2x^8 + ab^6c^2x^7 + \frac{7}{2}a^2b^5c^2x^6 + 7a^3b^4c^2x^5 + \frac{35}{4}a^4b^3c^2x^4 + 7a^5b^2c^2x^3 + \frac{7}{2}a^6bc^2x^2 + a^7c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5*(b*c*x+a*c)^2,x)

[Out] 1/8*b^7*c^2*x^8+a*b^6*c^2*x^7+7/2*a^2*b^5*c^2*x^6+7*a^3*b^4*c^2*x^5+35/4*a^4*b^3*c^2*x^4+7*a^5*b^2*c^2*x^3+7/2*a^6*c^2*b*x^2+a^7*c^2*x

maxima [B] time = 1.36, size = 99, normalized size = 5.82

$$\frac{1}{8}b^7c^2x^8 + ab^6c^2x^7 + \frac{7}{2}a^2b^5c^2x^6 + 7a^3b^4c^2x^5 + \frac{35}{4}a^4b^3c^2x^4 + 7a^5b^2c^2x^3 + \frac{7}{2}a^6bc^2x^2 + a^7c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^2,x, algorithm="maxima")

[Out] $1/8*b^7*c^2*x^8 + a*b^6*c^2*x^7 + 7/2*a^2*b^5*c^2*x^6 + 7*a^3*b^4*c^2*x^5 + 35/4*a^4*b^3*c^2*x^4 + 7*a^5*b^2*c^2*x^3 + 7/2*a^6*b*c^2*x^2 + a^7*c^2*x$

mupad [B] time = 0.04, size = 99, normalized size = 5.82

$$a^7 c^2 x + \frac{7 a^6 b c^2 x^2}{2} + 7 a^5 b^2 c^2 x^3 + \frac{35 a^4 b^3 c^2 x^4}{4} + 7 a^3 b^4 c^2 x^5 + \frac{7 a^2 b^5 c^2 x^6}{2} + a b^6 c^2 x^7 + \frac{b^7 c^2 x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c + b*c*x)^2*(a + b*x)^5,x)

[Out] $a^7*c^2*x + (b^7*c^2*x^8)/8 + (7*a^6*b*c^2*x^2)/2 + a*b^6*c^2*x^7 + 7*a^5*b^2*c^2*x^3 + (35*a^4*b^3*c^2*x^4)/4 + 7*a^3*b^4*c^2*x^5 + (7*a^2*b^5*c^2*x^6)/2$

sympy [B] time = 0.10, size = 110, normalized size = 6.47

$$a^7 c^2 x + \frac{7 a^6 b c^2 x^2}{2} + 7 a^5 b^2 c^2 x^3 + \frac{35 a^4 b^3 c^2 x^4}{4} + 7 a^3 b^4 c^2 x^5 + \frac{7 a^2 b^5 c^2 x^6}{2} + a b^6 c^2 x^7 + \frac{b^7 c^2 x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5*(b*c*x+a*c)**2,x)

[Out] $a**7*c**2*x + 7*a**6*b*c**2*x**2/2 + 7*a**5*b**2*c**2*x**3 + 35*a**4*b**3*c**2*x**4/4 + 7*a**3*b**4*c**2*x**5 + 7*a**2*b**5*c**2*x**6/2 + a*b**6*c**2*x**7 + b**7*c**2*x**8/8$

3.1018 $\int (a + bx)^5 (ac + bcx) dx$

Optimal. Leaf size=15

$$\frac{c(a + bx)^7}{7b}$$

[Out] 1/7*c*(b*x+a)^7/b

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {21, 32}

$$\frac{c(a + bx)^7}{7b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*(a*c + b*c*x), x]

[Out] (c*(a + b*x)^7)/(7*b)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int (a + bx)^5 (ac + bcx) dx &= c \int (a + bx)^6 dx \\ &= \frac{c(a + bx)^7}{7b} \end{aligned}$$

Mathematica [A] time = 0.00, size = 15, normalized size = 1.00

$$\frac{c(a + bx)^7}{7b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*(a*c + b*c*x), x]

[Out] (c*(a + b*x)^7)/(7*b)

fricas [B] time = 0.40, size = 71, normalized size = 4.73

$$\frac{1}{7}x^7cb^6 + x^6cb^5a + 3x^5cb^4a^2 + 5x^4cb^3a^3 + 5x^3cb^2a^4 + 3x^2cba^5 + xca^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c), x, algorithm="fricas")

[Out] 1/7*x^7*c*b^6 + x^6*c*b^5*a + 3*x^5*c*b^4*a^2 + 5*x^4*c*b^3*a^3 + 5*x^3*c*b^2*a^4 + 3*x^2*c*b*a^5 + x*c*a^6

giac [B] time = 1.09, size = 71, normalized size = 4.73

$$\frac{1}{7}b^6cx^7 + ab^5cx^6 + 3a^2b^4cx^5 + 5a^3b^3cx^4 + 5a^4b^2cx^3 + 3a^5bcx^2 + a^6cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c), x, algorithm="giac")

[Out] 1/7*b^6*c*x^7 + a*b^5*c*x^6 + 3*a^2*b^4*c*x^5 + 5*a^3*b^3*c*x^4 + 5*a^4*b^2*c*x^3 + 3*a^5*b*c*x^2 + a^6*c*x

maple [B] time = 0.00, size = 72, normalized size = 4.80

$$\frac{1}{7}b^6cx^7 + ab^5cx^6 + 3a^2b^4cx^5 + 5a^3b^3cx^4 + 5a^4b^2cx^3 + 3a^5bcx^2 + a^6cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5*(b*c*x+a*c), x)

[Out] 1/7*b^6*c*x^7+a*b^5*c*x^6+3*a^2*b^4*c*x^5+5*a^3*b^3*c*x^4+5*a^4*b^2*c*x^3+3*a^5*b*c*x^2+a^6*c*x

maxima [B] time = 1.35, size = 71, normalized size = 4.73

$$\frac{1}{7}b^6cx^7 + ab^5cx^6 + 3a^2b^4cx^5 + 5a^3b^3cx^4 + 5a^4b^2cx^3 + 3a^5bcx^2 + a^6cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c),x, algorithm="maxima")

[Out] $\frac{1}{7}b^6c*x^7 + a*b^5*c*x^6 + 3*a^2*b^4*c*x^5 + 5*a^3*b^3*c*x^4 + 5*a^4*b^2*c*x^3 + 3*a^5*b*c*x^2 + a^6*c*x$

mupad [B] time = 0.03, size = 71, normalized size = 4.73

$$c a^6 x + 3 c a^5 b x^2 + 5 c a^4 b^2 x^3 + 5 c a^3 b^3 x^4 + 3 c a^2 b^4 x^5 + c a b^5 x^6 + \frac{c b^6 x^7}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c + b*c*x)*(a + b*x)^5,x)

[Out] $(b^6*c*x^7)/7 + a^6*c*x + 5*a^4*b^2*c*x^3 + 5*a^3*b^3*c*x^4 + 3*a^2*b^4*c*x^5 + 3*a^5*b*c*x^2 + a*b^5*c*x^6$

sympy [B] time = 0.08, size = 78, normalized size = 5.20

$$a^6cx + 3a^5bcx^2 + 5a^4b^2cx^3 + 5a^3b^3cx^4 + 3a^2b^4cx^5 + ab^5cx^6 + \frac{b^6cx^7}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5*(b*c*x+a*c),x)

[Out] $a**6*c*x + 3*a**5*b*c*x**2 + 5*a**4*b**2*c*x**3 + 5*a**3*b**3*c*x**4 + 3*a**2*b**4*c*x**5 + a*b**5*c*x**6 + b**6*c*x**7/7$

$$3.1019 \quad \int \frac{(a+bx)^5}{ac+bcx} dx$$

Optimal. Leaf size=17

$$\frac{(a+bx)^5}{5bc}$$

[Out] 1/5*(b*x+a)^5/b/c

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 32}

$$\frac{(a+bx)^5}{5bc}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x), x]

[Out] (a + b*x)^5/(5*b*c)

Rule 21

Int[(u_.)*((a_.) + (b_.)*(v_.))^(m_.)*((c_.) + (d_.)*(v_.))^(n_.), x_Symbol] :> Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x] && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x, a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_.))^(m_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{ac+bcx} dx &= \frac{\int (a+bx)^4 dx}{c} \\ &= \frac{(a+bx)^5}{5bc} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{(a+bx)^5}{5bc}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x),x]

[Out] (a + b*x)^5/(5*b*c)

fricas [B] time = 0.41, size = 48, normalized size = 2.82

$$\frac{b^4x^5 + 5ab^3x^4 + 10a^2b^2x^3 + 10a^3bx^2 + 5a^4x}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c),x, algorithm="fricas")

[Out] 1/5*(b^4*x^5 + 5*a*b^3*x^4 + 10*a^2*b^2*x^3 + 10*a^3*b*x^2 + 5*a^4*x)/c

giac [B] time = 0.89, size = 48, normalized size = 2.82

$$\frac{b^4x^5 + 5ab^3x^4 + 10a^2b^2x^3 + 10a^3bx^2 + 5a^4x}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c),x, algorithm="giac")

[Out] 1/5*(b^4*x^5 + 5*a*b^3*x^4 + 10*a^2*b^2*x^3 + 10*a^3*b*x^2 + 5*a^4*x)/c

maple [A] time = 0.00, size = 16, normalized size = 0.94

$$\frac{(bx + a)^5}{5bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c),x)

[Out] 1/5*(b*x+a)^5/b/c

maxima [B] time = 1.35, size = 48, normalized size = 2.82

$$\frac{b^4x^5 + 5ab^3x^4 + 10a^2b^2x^3 + 10a^3bx^2 + 5a^4x}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c),x, algorithm="maxima")

[Out] 1/5*(b^4*x^5 + 5*a*b^3*x^4 + 10*a^2*b^2*x^3 + 10*a^3*b*x^2 + 5*a^4*x)/c

mupad [B] time = 0.03, size = 57, normalized size = 3.35

$$\frac{a^4 x}{c} + \frac{b^4 x^5}{5c} + \frac{2a^3 b x^2}{c} + \frac{a b^3 x^4}{c} + \frac{2a^2 b^2 x^3}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(a*c + b*c*x), x)`

[Out] $(a^4*x)/c + (b^4*x^5)/(5*c) + (2*a^3*b*x^2)/c + (a*b^3*x^4)/c + (2*a^2*b^2*x^3)/c$

sympy [B] time = 0.10, size = 51, normalized size = 3.00

$$\frac{a^4 x}{c} + \frac{2a^3 b x^2}{c} + \frac{2a^2 b^2 x^3}{c} + \frac{a b^3 x^4}{c} + \frac{b^4 x^5}{5c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(b*c*x+a*c), x)`

[Out] $a**4*x/c + 2*a**3*b*x**2/c + 2*a**2*b**2*x**3/c + a*b**3*x**4/c + b**4*x**5/(5*c)$

$$3.1020 \quad \int \frac{(a+bx)^5}{(ac+bcx)^2} dx$$

Optimal. Leaf size=17

$$\frac{(a+bx)^4}{4bc^2}$$

[Out] 1/4*(b*x+a)^4/b/c^2

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 32}

$$\frac{(a+bx)^4}{4bc^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^2,x]

[Out] (a + b*x)^4/(4*b*c^2)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^2} dx &= \frac{\int (a+bx)^3 dx}{c^2} \\ &= \frac{(a+bx)^4}{4bc^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{(a+bx)^4}{4bc^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^2,x]

[Out] (a + b*x)^4/(4*b*c^2)

fricas [B] time = 0.41, size = 37, normalized size = 2.18

$$\frac{b^3x^4 + 4ab^2x^3 + 6a^2bx^2 + 4a^3x}{4c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^2,x, algorithm="fricas")

[Out] 1/4*(b^3*x^4 + 4*a*b^2*x^3 + 6*a^2*b*x^2 + 4*a^3*x)/c^2

giac [A] time = 0.98, size = 18, normalized size = 1.06

$$\frac{(bcx + ac)^4}{4bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^2,x, algorithm="giac")

[Out] 1/4*(b*c*x + a*c)^4/(b*c^6)

maple [A] time = 0.00, size = 16, normalized size = 0.94

$$\frac{(bx + a)^4}{4bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^2,x)

[Out] 1/4*(b*x+a)^4/b/c^2

maxima [B] time = 1.31, size = 37, normalized size = 2.18

$$\frac{b^3x^4 + 4ab^2x^3 + 6a^2bx^2 + 4a^3x}{4c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^2,x, algorithm="maxima")

[Out] 1/4*(b^3*x^4 + 4*a*b^2*x^3 + 6*a^2*b*x^2 + 4*a^3*x)/c^2

mupad [B] time = 0.05, size = 43, normalized size = 2.53

$$\frac{a^3 x}{c^2} + \frac{b^3 x^4}{4c^2} + \frac{3a^2 b x^2}{2c^2} + \frac{a b^2 x^3}{c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(a*c + b*c*x)^2,x)`

[Out] `(a^3*x)/c^2 + (b^3*x^4)/(4*c^2) + (3*a^2*b*x^2)/(2*c^2) + (a*b^2*x^3)/c^2`

sympy [B] time = 0.11, size = 46, normalized size = 2.71

$$\frac{a^3 x}{c^2} + \frac{3a^2 b x^2}{2c^2} + \frac{a b^2 x^3}{c^2} + \frac{b^3 x^4}{4c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(b*c*x+a*c)**2,x)`

[Out] `a**3*x/c**2 + 3*a**2*b*x**2/(2*c**2) + a*b**2*x**3/c**2 + b**3*x**4/(4*c**2)`
)

$$3.1021 \quad \int \frac{(a+bx)^5}{(ac+bcx)^3} dx$$

Optimal. Leaf size=17

$$\frac{(a+bx)^3}{3bc^3}$$

[Out] 1/3*(b*x+a)^3/b/c^3

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 32}

$$\frac{(a+bx)^3}{3bc^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^3, x]

[Out] (a + b*x)^3/(3*b*c^3)

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
 Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
 && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
 a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^3} dx &= \frac{\int (a+bx)^2 dx}{c^3} \\ &= \frac{(a+bx)^3}{3bc^3} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{(a+bx)^3}{3bc^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^3,x]

[Out] (a + b*x)^3/(3*b*c^3)

fricas [A] time = 0.41, size = 26, normalized size = 1.53

$$\frac{b^2x^3 + 3abx^2 + 3a^2x}{3c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^3,x, algorithm="fricas")

[Out] 1/3*(b^2*x^3 + 3*a*b*x^2 + 3*a^2*x)/c^3

giac [A] time = 1.00, size = 26, normalized size = 1.53

$$\frac{b^2x^3 + 3abx^2 + 3a^2x}{3c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^3,x, algorithm="giac")

[Out] 1/3*(b^2*x^3 + 3*a*b*x^2 + 3*a^2*x)/c^3

maple [A] time = 0.00, size = 16, normalized size = 0.94

$$\frac{(bx + a)^3}{3bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^3,x)

[Out] 1/3*(b*x+a)^3/b/c^3

maxima [A] time = 1.31, size = 26, normalized size = 1.53

$$\frac{b^2x^3 + 3abx^2 + 3a^2x}{3c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^3,x, algorithm="maxima")

[Out] 1/3*(b^2*x^3 + 3*a*b*x^2 + 3*a^2*x)/c^3

mupad [B] time = 0.04, size = 24, normalized size = 1.41

$$\frac{x (3 a^2 + 3 a b x + b^2 x^2)}{3 c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(a*c + b*c*x)^3,x)`

[Out] `(x*(3*a^2 + b^2*x^2 + 3*a*b*x))/(3*c^3)`

sympy [B] time = 0.11, size = 29, normalized size = 1.71

$$\frac{a^2 x}{c^3} + \frac{a b x^2}{c^3} + \frac{b^2 x^3}{3 c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(b*c*x+a*c)**3,x)`

[Out] `a**2*x/c**3 + a*b*x**2/c**3 + b**2*x**3/(3*c**3)`

$$3.1022 \quad \int \frac{(a+bx)^5}{(ac+bcx)^4} dx$$

Optimal. Leaf size=18

$$\frac{ax}{c^4} + \frac{bx^2}{2c^4}$$

[Out] $a*x/c^4 + 1/2*b*x^2/c^4$

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.056$, Rules used = {21}

$$\frac{ax}{c^4} + \frac{bx^2}{2c^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^4, x]

[Out] (a*x)/c^4 + (b*x^2)/(2*c^4)

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
 Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
 && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
 a + b*x])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^4} dx &= \frac{\int (a+bx) dx}{c^4} \\ &= \frac{ax}{c^4} + \frac{bx^2}{2c^4} \end{aligned}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 0.89

$$\frac{ax + \frac{bx^2}{2}}{c^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^4, x]

[Out] $(a*x + (b*x^2)/2)/c^4$

fricas [A] time = 0.41, size = 15, normalized size = 0.83

$$\frac{bx^2 + 2ax}{2c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5/(b*c*x+a*c)^4,x, algorithm="fricas")`

[Out] $1/2*(b*x^2 + 2*a*x)/c^4$

giac [A] time = 1.21, size = 15, normalized size = 0.83

$$\frac{bx^2 + 2ax}{2c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5/(b*c*x+a*c)^4,x, algorithm="giac")`

[Out] $1/2*(b*x^2 + 2*a*x)/c^4$

maple [A] time = 0.00, size = 15, normalized size = 0.83

$$\frac{\frac{1}{2}bx^2 + ax}{c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^5/(b*c*x+a*c)^4,x)`

[Out] $1/c^4*(1/2*b*x^2+a*x)$

maxima [A] time = 1.38, size = 15, normalized size = 0.83

$$\frac{bx^2 + 2ax}{2c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5/(b*c*x+a*c)^4,x, algorithm="maxima")`

[Out] $1/2*(b*x^2 + 2*a*x)/c^4$

mupad [B] time = 0.02, size = 13, normalized size = 0.72

$$\frac{x(2a + bx)}{2c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^5/(a*c + b*c*x)^4,x)
```

```
[Out] (x*(2*a + b*x))/(2*c^4)
```

sympy [A] time = 0.11, size = 15, normalized size = 0.83

$$\frac{ax}{c^4} + \frac{bx^2}{2c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**5/(b*c*x+a*c)**4,x)
```

```
[Out] a*x/c**4 + b*x**2/(2*c**4)
```

$$3.1023 \quad \int \frac{(a+bx)^5}{(ac+bcx)^5} dx$$

Optimal. Leaf size=5

$$\frac{x}{c^5}$$

[Out] x/c^5

Rubi [A] time = 0.00, antiderivative size = 5, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 8}

$$\frac{x}{c^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^5, x]

[Out] x/c^5

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] := Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x] && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x, a + b*x])

Rubi steps

$$\int \frac{(a+bx)^5}{(ac+bcx)^5} dx = \frac{\int 1 dx}{c^5} = \frac{x}{c^5}$$

Mathematica [A] time = 0.00, size = 5, normalized size = 1.00

$$\frac{x}{c^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^5,x]

[Out] x/c^5

fricas [A] time = 0.41, size = 5, normalized size = 1.00

$$\frac{x}{c^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^5,x, algorithm="fricas")

[Out] x/c^5

giac [B] time = 1.11, size = 15, normalized size = 3.00

$$\frac{bcx + ac}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^5,x, algorithm="giac")

[Out] (b*c*x + a*c)/(b*c^6)

maple [A] time = 0.00, size = 6, normalized size = 1.20

$$\frac{x}{c^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^5,x)

[Out] x/c^5

maxima [A] time = 1.40, size = 5, normalized size = 1.00

$$\frac{x}{c^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^5,x, algorithm="maxima")

[Out] x/c^5

mupad [B] time = 0.01, size = 5, normalized size = 1.00

$$\frac{x}{c^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^5/(a*c + b*c*x)^5,x)
```

```
[Out] x/c^5
```

sympy [A] time = 0.11, size = 3, normalized size = 0.60

$$\frac{x}{c^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**5/(b*c*x+a*c)**5,x)
```

```
[Out] x/c**5
```

$$3.1024 \quad \int \frac{(a+bx)^5}{(ac+bcx)^6} dx$$

Optimal. Leaf size=13

$$\frac{\log(a+bx)}{bc^6}$$

[Out] ln(b*x+a)/b/c^6

Rubi [A] time = 0.00, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 31}

$$\frac{\log(a+bx)}{bc^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^6, x]

[Out] Log[a + b*x]/(b*c^6)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 31

```
Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x,
x]]/b, x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^6} dx &= \int \frac{1}{a+bx} dx \\ &= \frac{\log(a+bx)}{bc^6} \end{aligned}$$

Mathematica [A] time = 0.00, size = 13, normalized size = 1.00

$$\frac{\log(a+bx)}{bc^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^6,x]

[Out] Log[a + b*x]/(b*c^6)

fricas [A] time = 0.42, size = 13, normalized size = 1.00

$$\frac{\log(bx + a)}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^6,x, algorithm="fricas")

[Out] log(b*x + a)/(b*c^6)

giac [A] time = 0.95, size = 14, normalized size = 1.08

$$\frac{\log(|bx + a|)}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^6,x, algorithm="giac")

[Out] log(abs(b*x + a))/(b*c^6)

maple [A] time = 0.00, size = 14, normalized size = 1.08

$$\frac{\ln(bx + a)}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^6,x)

[Out] ln(b*x+a)/b/c^6

maxima [A] time = 1.31, size = 13, normalized size = 1.00

$$\frac{\log(bx + a)}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^6,x, algorithm="maxima")

[Out] log(b*x + a)/(b*c^6)

mupad [B] time = 0.04, size = 13, normalized size = 1.00

$$\frac{\ln(a + bx)}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(a*c + b*c*x)^6,x)`

[Out] `log(a + b*x)/(b*c^6)`

sympy [A] time = 0.12, size = 17, normalized size = 1.31

$$\frac{\log(ac^6 + bc^6x)}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(b*c*x+a*c)**6,x)`

[Out] `log(a*c**6 + b*c**6*x)/(b*c**6)`

$$3.1025 \quad \int \frac{(a+bx)^5}{(ac+bcx)^7} dx$$

Optimal. Leaf size=15

$$-\frac{1}{bc^7(a+bx)}$$

[Out] -1/b/c^7/(b*x+a)

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 32}

$$-\frac{1}{bc^7(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^7, x]

[Out] -(1/(b*c^7*(a + b*x)))

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :> Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x] && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x, a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^7} dx &= \int \frac{1}{(a+bx)^2} \frac{dx}{c^7} \\ &= -\frac{1}{bc^7(a+bx)} \end{aligned}$$

Mathematica [A] time = 0.00, size = 15, normalized size = 1.00

$$-\frac{1}{bc^7(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^7,x]

[Out] -(1/(b*c^7*(a + b*x)))

fricas [A] time = 0.44, size = 19, normalized size = 1.27

$$-\frac{1}{b^2c^7x + abc^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^7,x, algorithm="fricas")

[Out] -1/(b^2*c^7*x + a*b*c^7)

giac [A] time = 1.09, size = 15, normalized size = 1.00

$$-\frac{1}{(bx + a)bc^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^7,x, algorithm="giac")

[Out] -1/((b*x + a)*b*c^7)

maple [A] time = 0.00, size = 16, normalized size = 1.07

$$-\frac{1}{(bx + a)bc^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^7,x)

[Out] -1/b/c^7/(b*x+a)

maxima [A] time = 1.33, size = 19, normalized size = 1.27

$$-\frac{1}{b^2c^7x + abc^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^7,x, algorithm="maxima")

[Out] -1/(b^2*c^7*x + a*b*c^7)

mupad [B] time = 0.05, size = 19, normalized size = 1.27

$$-\frac{1}{x b^2 c^7 + a b c^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(a*c + b*c*x)^7,x)`

[Out] `-1/(b^2*c^7*x + a*b*c^7)`

sympy [A] time = 0.20, size = 17, normalized size = 1.13

$$-\frac{1}{a b c^7 + b^2 c^7 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(b*c*x+a*c)**7,x)`

[Out] `-1/(a*b*c**7 + b**2*c**7*x)`

$$3.1026 \quad \int \frac{(a+bx)^5}{(ac+bcx)^8} dx$$

Optimal. Leaf size=17

$$-\frac{1}{2bc^8(a+bx)^2}$$

[Out] -1/2/b/c^8/(b*x+a)^2

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {21, 32}

$$-\frac{1}{2bc^8(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^8,x]

[Out] -1/(2*b*c^8*(a + b*x)^2)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^8} dx &= \int \frac{1}{(a+bx)^3} \frac{dx}{c^8} \\ &= -\frac{1}{2bc^8(a+bx)^2} \end{aligned}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$-\frac{1}{2bc^8(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^8,x]

[Out] -1/2*1/(b*c^8*(a + b*x)^2)

fricas [B] time = 0.42, size = 33, normalized size = 1.94

$$-\frac{1}{2(b^3c^8x^2 + 2ab^2c^8x + a^2bc^8)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^8,x, algorithm="fricas")

[Out] -1/2/(b^3*c^8*x^2 + 2*a*b^2*c^8*x + a^2*b*c^8)

giac [A] time = 1.05, size = 15, normalized size = 0.88

$$-\frac{1}{2(bx + a)^2bc^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^8,x, algorithm="giac")

[Out] -1/2/((b*x + a)^2*b*c^8)

maple [A] time = 0.00, size = 16, normalized size = 0.94

$$-\frac{1}{2(bx + a)^2bc^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^8,x)

[Out] -1/2/b/c^8/(b*x+a)^2

maxima [B] time = 1.33, size = 33, normalized size = 1.94

$$-\frac{1}{2(b^3c^8x^2 + 2ab^2c^8x + a^2bc^8)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^8,x, algorithm="maxima")

[Out] $-1/2/(b^3c^8x^2 + 2ab^2c^8x + a^2bc^8)$

mupad [B] time = 0.15, size = 35, normalized size = 2.06

$$-\frac{1}{2a^2bc^8 + 4ab^2c^8x + 2b^3c^8x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(a*c + b*c*x)^8, x)`

[Out] $-1/(2a^2bc^8 + 2b^3c^8x^2 + 4ab^2c^8x)$

sympy [B] time = 0.26, size = 36, normalized size = 2.12

$$-\frac{1}{2a^2bc^8 + 4ab^2c^8x + 2b^3c^8x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(b*c*x+a*c)**8, x)`

[Out] $-1/(2a**2*b*c**8 + 4*a*b**2*c**8*x + 2*b**3*c**8*x**2)$

$$3.1027 \quad \int \frac{1}{\sqrt{-2-3x} \sqrt{2+3x}} dx$$

Optimal. Leaf size=28

$$\frac{\sqrt{3x+2} \log(3x+2)}{3\sqrt{-3x-2}}$$

[Out] 1/3*ln(2+3*x)*(2+3*x)^(1/2)/(-2-3*x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {23, 31}

$$\frac{\sqrt{3x+2} \log(3x+2)}{3\sqrt{-3x-2}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-2 - 3*x]*Sqrt[2 + 3*x]),x]

[Out] (Sqrt[2 + 3*x]*Log[2 + 3*x])/(3*Sqrt[-2 - 3*x])

Rule 23

Int[(u_.)*((a_) + (b_.)*(v_))^(m_)*((c_) + (d_.)*(v_))^(n_), x_Symbol] := Dist[(a + b*v)^m/(c + d*v)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, m, n}, x] && EqQ[b*c - a*d, 0] && !(IntegerQ[m] || IntegerQ[n] || GtQ[b/d, 0])

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-2-3x} \sqrt{2+3x}} dx &= \frac{\sqrt{2+3x} \int \frac{1}{2+3x} dx}{\sqrt{-2-3x}} \\ &= \frac{\sqrt{2+3x} \log(2+3x)}{3\sqrt{-2-3x}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 1.00

$$\frac{(3x + 2) \log(3x + 2)}{3\sqrt{-(3x + 2)^2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-2 - 3*x]*Sqrt[2 + 3*x]),x]

[Out] ((2 + 3*x)*Log[2 + 3*x])/(3*Sqrt[-(2 + 3*x)^2])

fricas [A] time = 0.45, size = 1, normalized size = 0.04

0

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-2-3*x)^(1/2)/(2+3*x)^(1/2),x, algorithm="fricas")

[Out] 0

giac [C] time = 1.01, size = 11, normalized size = 0.39

$$-\frac{1}{3}i \log(|3x + 2|) \operatorname{sgn}(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-2-3*x)^(1/2)/(2+3*x)^(1/2),x, algorithm="giac")

[Out] -1/3*I*log(abs(3*x + 2))*sgn(x)

maple [A] time = 0.00, size = 23, normalized size = 0.82

$$\frac{\sqrt{3x + 2} \ln(3x + 2)}{3\sqrt{-3x - 2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-2-3*x)^(1/2)/(3*x+2)^(1/2),x)

[Out] 1/3*ln(3*x+2)*(3*x+2)^(1/2)/(-2-3*x)^(1/2)

maxima [C] time = 2.99, size = 6, normalized size = 0.21

$$\frac{1}{3}i \log\left(x + \frac{2}{3}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-2-3*x)^(1/2)/(2+3*x)^(1/2),x, algorithm="maxima")`

[Out] $1/3*I*\log(x + 2/3)$

mupad [B] time = 0.22, size = 35, normalized size = 1.25

$$-\frac{4 \operatorname{atan}\left(\frac{-\sqrt{-3x-2}+\sqrt{2} \operatorname{I}i}{\sqrt{2}-\sqrt{3x+2}}\right)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((- 3*x - 2)^(1/2)*(3*x + 2)^(1/2)),x)`

[Out] $-(4*\operatorname{atan}((2^{(1/2)}*1i - (- 3*x - 2)^{(1/2)})/(2^{(1/2)} - (3*x + 2)^{(1/2)})))/3$

sympy [C] time = 1.46, size = 53, normalized size = 1.89

$$\begin{cases} \frac{i \log\left(x + \frac{2}{3}\right)}{3} & \text{for } \left|x + \frac{2}{3}\right| < 1 \\ \frac{i \log\left(\frac{1}{x + \frac{2}{3}}\right)}{3} & \text{for } \frac{1}{\left|x + \frac{2}{3}\right|} < 1 \\ \frac{i G_{2,2}^{2,0}\left(0, 0 \left| x + \frac{2}{3} \right.\right)}{3} - \frac{i G_{2,2}^{0,2}\left(1, 1 \left| x + \frac{2}{3} \right.\right)}{3} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-2-3*x)**(1/2)/(2+3*x)**(1/2),x)`

[Out] `Piecewise((-I*log(x + 2/3)/3, Abs(x + 2/3) < 1), (I*log(1/(x + 2/3))/3, 1/Abs(x + 2/3) < 1), (I*meijerg(((), (1, 1)), ((0, 0), ()), x + 2/3)/3 - I*meijerg(((1, 1), ()), (((), (0, 0))), x + 2/3)/3, True))`

3.1028 $\int (a + bx)(ac - bcx)^3 dx$

Optimal. Leaf size=38

$$\frac{c^3(a - bx)^5}{5b} - \frac{ac^3(a - bx)^4}{2b}$$

[Out] $-1/2*a*c^3*(-b*x+a)^4/b+1/5*c^3*(-b*x+a)^5/b$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{c^3(a - bx)^5}{5b} - \frac{ac^3(a - bx)^4}{2b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(a*c - b*c*x)^3,x]

[Out] $-(a*c^3*(a - b*x)^4)/(2*b) + (c^3*(a - b*x)^5)/(5*b)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)(ac - bcx)^3 dx &= \int \left(2a(ac - bcx)^3 - \frac{(ac - bcx)^4}{c} \right) dx \\ &= -\frac{ac^3(a - bx)^4}{2b} + \frac{c^3(a - bx)^5}{5b} \end{aligned}$$

Mathematica [A] time = 0.00, size = 40, normalized size = 1.05

$$c^3 \left(a^4 x - a^3 b x^2 + \frac{1}{2} a b^3 x^4 - \frac{1}{5} b^4 x^5 \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(a*c - b*c*x)^3,x]

[Out] $c^3(a^4x - a^3bx^2 + (ab^3x^4)/2 - (b^4x^5)/5)$

fricas [A] time = 0.40, size = 44, normalized size = 1.16

$$-\frac{1}{5}x^5c^3b^4 + \frac{1}{2}x^4c^3b^3a - x^2c^3ba^3 + xc^3a^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)^3,x, algorithm="fricas")`

[Out] $-1/5*x^5*c^3*b^4 + 1/2*x^4*c^3*b^3*a - x^2*c^3*b*a^3 + x*c^3*a^4$

giac [A] time = 1.00, size = 44, normalized size = 1.16

$$-\frac{1}{5}b^4c^3x^5 + \frac{1}{2}ab^3c^3x^4 - a^3bc^3x^2 + a^4c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)^3,x, algorithm="giac")`

[Out] $-1/5*b^4*c^3*x^5 + 1/2*a*b^3*c^3*x^4 - a^3*b*c^3*x^2 + a^4*c^3*x$

maple [A] time = 0.00, size = 45, normalized size = 1.18

$$-\frac{1}{5}b^4c^3x^5 + \frac{1}{2}ab^3c^3x^4 - a^3bc^3x^2 + a^4c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)*(-b*c*x+a*c)^3,x)`

[Out] $-1/5*b^4*c^3*x^5+1/2*a*b^3*c^3*x^4-a^3*c^3*b*x^2+a^4*c^3*x$

maxima [A] time = 1.23, size = 44, normalized size = 1.16

$$-\frac{1}{5}b^4c^3x^5 + \frac{1}{2}ab^3c^3x^4 - a^3bc^3x^2 + a^4c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)^3,x, algorithm="maxima")`

[Out] $-1/5*b^4*c^3*x^5 + 1/2*a*b^3*c^3*x^4 - a^3*b*c^3*x^2 + a^4*c^3*x$

mupad [B] time = 0.16, size = 44, normalized size = 1.16

$$a^4c^3x - a^3bc^3x^2 + \frac{ab^3c^3x^4}{2} - \frac{b^4c^3x^5}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c - b*c*x)^3*(a + b*x),x)`

[Out] $a^4*c^3*x - (b^4*c^3*x^5)/5 - a^3*b*c^3*x^2 + (a*b^3*c^3*x^4)/2$

sympy [A] time = 0.08, size = 44, normalized size = 1.16

$$a^4c^3x - a^3bc^3x^2 + \frac{ab^3c^3x^4}{2} - \frac{b^4c^3x^5}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)**3,x)`

[Out] $a**4*c**3*x - a**3*b*c**3*x**2 + a*b**3*c**3*x**4/2 - b**4*c**3*x**5/5$

3.1029 $\int (a + bx)(ac - bcx)^2 dx$

Optimal. Leaf size=38

$$\frac{c^2(a - bx)^4}{4b} - \frac{2ac^2(a - bx)^3}{3b}$$

[Out] $-2/3*a*c^2*(-b*x+a)^3/b+1/4*c^2*(-b*x+a)^4/b$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{c^2(a - bx)^4}{4b} - \frac{2ac^2(a - bx)^3}{3b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(a*c - b*c*x)^2,x]

[Out] $(-2*a*c^2*(a - b*x)^3)/(3*b) + (c^2*(a - b*x)^4)/(4*b)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)(ac - bcx)^2 dx &= \int \left(2a(ac - bcx)^2 - \frac{(ac - bcx)^3}{c} \right) dx \\ &= -\frac{2ac^2(a - bx)^3}{3b} + \frac{c^2(a - bx)^4}{4b} \end{aligned}$$

Mathematica [A] time = 0.00, size = 42, normalized size = 1.11

$$c^2 \left(a^3 x - \frac{1}{2} a^2 b x^2 - \frac{1}{3} a b^2 x^3 + \frac{b^3 x^4}{4} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(a*c - b*c*x)^2,x]

[Out] $c^2*(a^3*x - (a^2*b*x^2)/2 - (a*b^2*x^3)/3 + (b^3*x^4)/4)$

fricas [A] time = 0.38, size = 44, normalized size = 1.16

$$\frac{1}{4}x^4c^2b^3 - \frac{1}{3}x^3c^2b^2a - \frac{1}{2}x^2c^2ba^2 + xc^2a^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)^2,x, algorithm="fricas")`

[Out] $1/4*x^4*c^2*b^3 - 1/3*x^3*c^2*b^2*a - 1/2*x^2*c^2*b*a^2 + x*c^2*a^3$

giac [A] time = 1.04, size = 44, normalized size = 1.16

$$\frac{1}{4}b^3c^2x^4 - \frac{1}{3}ab^2c^2x^3 - \frac{1}{2}a^2bc^2x^2 + a^3c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)^2,x, algorithm="giac")`

[Out] $1/4*b^3*c^2*x^4 - 1/3*a*b^2*c^2*x^3 - 1/2*a^2*b*c^2*x^2 + a^3*c^2*x$

maple [A] time = 0.00, size = 45, normalized size = 1.18

$$\frac{1}{4}b^3c^2x^4 - \frac{1}{3}ab^2c^2x^3 - \frac{1}{2}a^2bc^2x^2 + a^3c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)*(-b*c*x+a*c)^2,x)`

[Out] $1/4*b^3*c^2*x^4 - 1/3*a*b^2*c^2*x^3 - 1/2*a^2*c^2*b*x^2 + a^3*c^2*x$

maxima [A] time = 1.31, size = 44, normalized size = 1.16

$$\frac{1}{4}b^3c^2x^4 - \frac{1}{3}ab^2c^2x^3 - \frac{1}{2}a^2bc^2x^2 + a^3c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)^2,x, algorithm="maxima")`

[Out] $1/4*b^3*c^2*x^4 - 1/3*a*b^2*c^2*x^3 - 1/2*a^2*b*c^2*x^2 + a^3*c^2*x$

mupad [B] time = 0.05, size = 44, normalized size = 1.16

$$a^3c^2x - \frac{a^2bc^2x^2}{2} - \frac{ab^2c^2x^3}{3} + \frac{b^3c^2x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c - b*c*x)^2*(a + b*x),x)`

[Out] $a^3c^2x + (b^3c^2x^4)/4 - (a^2b^2c^2x^2)/2 - (ab^2c^2x^3)/3$

sympy [A] time = 0.07, size = 46, normalized size = 1.21

$$a^3c^2x - \frac{a^2bc^2x^2}{2} - \frac{ab^2c^2x^3}{3} + \frac{b^3c^2x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)**2,x)`

[Out] $a**3*c**2*x - a**2*b*c**2*x**2/2 - a*b**2*c**2*x**3/3 + b**3*c**2*x**4/4$

3.1030 $\int (a + bx)(ac - bcx) dx$

Optimal. Leaf size=18

$$a^2cx - \frac{1}{3}b^2cx^3$$

[Out] $a^2*c*x - 1/3*b^2*c*x^3$

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {41}

$$a^2cx - \frac{1}{3}b^2cx^3$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(a*c - b*c*x), x]

[Out] $a^2*c*x - (b^2*c*x^3)/3$

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rubi steps

$$\begin{aligned} \int (a + bx)(ac - bcx) dx &= \int (a^2c - b^2cx^2) dx \\ &= a^2cx - \frac{1}{3}b^2cx^3 \end{aligned}$$

Mathematica [A] time = 0.00, size = 18, normalized size = 1.00

$$c \left(a^2x - \frac{b^2x^3}{3} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(a*c - b*c*x), x]

[Out] $c*(a^2*x - (b^2*x^3)/3)$

fricas [A] time = 0.38, size = 16, normalized size = 0.89

$$-\frac{1}{3}x^3cb^2 + xca^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(-b*c*x+a*c),x, algorithm="fricas")

[Out] -1/3*x^3*c*b^2 + x*c*a^2

giac [A] time = 1.01, size = 16, normalized size = 0.89

$$-\frac{1}{3}b^2cx^3 + a^2cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(-b*c*x+a*c),x, algorithm="giac")

[Out] -1/3*b^2*c*x^3 + a^2*c*x

maple [A] time = 0.00, size = 17, normalized size = 0.94

$$-\frac{1}{3}b^2cx^3 + a^2cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(-b*c*x+a*c),x)

[Out] a^2*c*x-1/3*b^2*c*x^3

maxima [A] time = 1.35, size = 16, normalized size = 0.89

$$-\frac{1}{3}b^2cx^3 + a^2cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(-b*c*x+a*c),x, algorithm="maxima")

[Out] -1/3*b^2*c*x^3 + a^2*c*x

mupad [B] time = 0.02, size = 18, normalized size = 1.00

$$\frac{cx(3a^2 - b^2x^2)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a*c - b*c*x)*(a + b*x),x)
```

```
[Out] (c*x*(3*a^2 - b^2*x^2))/3
```

sympy [A] time = 0.06, size = 15, normalized size = 0.83

$$a^2cx - \frac{b^2cx^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)*(-b*c*x+a*c),x)
```

```
[Out] a**2*c*x - b**2*c*x**3/3
```

3.1031 $\int(a + bx) dx$

Optimal. Leaf size=12

$$ax + \frac{bx^2}{2}$$

[Out] a*x+1/2*b*x^2

Rubi [A] time = 0.00, antiderivative size = 12, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$ax + \frac{bx^2}{2}$$

Antiderivative was successfully verified.

[In] Int[a + b*x,x]

[Out] a*x + (b*x^2)/2

Rubi steps

$$\int(a + bx) dx = ax + \frac{bx^2}{2}$$

Mathematica [A] time = 0.00, size = 12, normalized size = 1.00

$$ax + \frac{bx^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[a + b*x,x]

[Out] a*x + (b*x^2)/2

fricas [A] time = 0.38, size = 10, normalized size = 0.83

$$\frac{1}{2}x^2b + xa$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(b*x+a,x, algorithm="fricas")

[Out] $\frac{1}{2}x^2b + xa$

giac [A] time = 0.86, size = 10, normalized size = 0.83

$$\frac{1}{2}bx^2 + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(b*x+a,x, algorithm="giac")`

[Out] $\frac{1}{2}b*x^2 + a*x$

maple [A] time = 0.00, size = 11, normalized size = 0.92

$$\frac{1}{2}bx^2 + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(b*x+a,x)`

[Out] $\frac{1}{2}b*x^2+a*x$

maxima [A] time = 1.34, size = 10, normalized size = 0.83

$$\frac{1}{2}bx^2 + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(b*x+a,x, algorithm="maxima")`

[Out] $\frac{1}{2}b*x^2 + a*x$

mupad [B] time = 0.02, size = 10, normalized size = 0.83

$$\frac{bx^2}{2} + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(a + b*x,x)`

[Out] $a*x + (b*x^2)/2$

sympy [A] time = 0.06, size = 8, normalized size = 0.67

$$ax + \frac{bx^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(b*x+a,x)
```

```
[Out] a*x + b*x**2/2
```

$$3.1032 \quad \int \frac{a+bx}{ac-bcx} dx$$

Optimal. Leaf size=23

$$-\frac{2a \log(a - bx)}{bc} - \frac{x}{c}$$

[Out] $-x/c - 2*a*\ln(-b*x+a)/b/c$

Rubi [A] time = 0.01, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{2a \log(a - bx)}{bc} - \frac{x}{c}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(a*c - b*c*x), x]

[Out] $-(x/c) - (2*a*\text{Log}[a - b*x])/(b*c)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{ac-bcx} dx &= \int \left(-\frac{1}{c} + \frac{2a}{c(a-bx)} \right) dx \\ &= -\frac{x}{c} - \frac{2a \log(a-bx)}{bc} \end{aligned}$$

Mathematica [A] time = 0.00, size = 23, normalized size = 1.00

$$-\frac{2a \log(a - bx)}{bc} - \frac{x}{c}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(a*c - b*c*x), x]

[Out] $-(x/c) - (2*a*\text{Log}[a - b*x])/(b*c)$

fricas [A] time = 0.41, size = 23, normalized size = 1.00

$$-\frac{bx + 2a \log (bx - a)}{bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(-b*c*x+a*c),x, algorithm="fricas")

[Out] -(b*x + 2*a*log(b*x - a))/(b*c)

giac [A] time = 0.92, size = 25, normalized size = 1.09

$$-\frac{x}{c} - \frac{2a \log (|bx - a|)}{bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(-b*c*x+a*c),x, algorithm="giac")

[Out] -x/c - 2*a*log(abs(b*x - a))/(b*c)

maple [A] time = 0.00, size = 25, normalized size = 1.09

$$-\frac{2a \ln (bx - a)}{bc} - \frac{x}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/(-b*c*x+a*c),x)

[Out] -x/c-2/c*a/b*ln(b*x-a)

maxima [A] time = 1.31, size = 24, normalized size = 1.04

$$-\frac{x}{c} - \frac{2a \log (bx - a)}{bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(-b*c*x+a*c),x, algorithm="maxima")

[Out] -x/c - 2*a*log(b*x - a)/(b*c)

mupad [B] time = 0.05, size = 23, normalized size = 1.00

$$-\frac{bx + 2a \ln (bx - a)}{bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(a*c - b*c*x), x)`

[Out] $-(b*x + 2*a*\log(b*x - a))/(b*c)$

sympy [A] time = 0.14, size = 17, normalized size = 0.74

$$-\frac{2a \log(-a + bx)}{bc} - \frac{x}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c), x)`

[Out] $-2*a*\log(-a + b*x)/(b*c) - x/c$

$$3.1033 \quad \int \frac{a+bx}{(ac-bcx)^2} dx$$

Optimal. Leaf size=32

$$\frac{2a}{bc^2(a-bx)} + \frac{\log(a-bx)}{bc^2}$$

[Out] $2*a/b/c^2/(-b*x+a)+\ln(-b*x+a)/b/c^2$

Rubi [A] time = 0.02, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{2a}{bc^2(a-bx)} + \frac{\log(a-bx)}{bc^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(a*c - b*c*x)^2, x]

[Out] (2*a)/(b*c^2*(a - b*x)) + Log[a - b*x]/(b*c^2)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{(ac-bcx)^2} dx &= \int \left(\frac{2a}{c^2(a-bx)^2} - \frac{1}{c^2(a-bx)} \right) dx \\ &= \frac{2a}{bc^2(a-bx)} + \frac{\log(a-bx)}{bc^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 28, normalized size = 0.88

$$\frac{\log(c(a-bx)) + \frac{2a}{a-bx}}{bc^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(a*c - b*c*x)^2, x]

[Out] $((2*a)/(a - b*x) + \text{Log}[c*(a - b*x)])/(b*c^2)$

fricas [A] time = 0.41, size = 39, normalized size = 1.22

$$\frac{(bx - a) \log(bx - a) - 2a}{b^2c^2x - abc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^2,x, algorithm="fricas")`

[Out] $((b*x - a)*\log(b*x - a) - 2*a)/(b^2*c^2*x - a*b*c^2)$

giac [B] time = 1.11, size = 81, normalized size = 2.53

$$-\frac{\frac{a}{(bcx-ac)b} + \frac{\log\left(\frac{|bcx-ac|}{(bcx-ac)^2|b||c|}\right)}{bc}}{c} - \frac{a}{(bcx-ac)bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^2,x, algorithm="giac")`

[Out] $-(a/((b*c*x - a*c)*b) + \log(\text{abs}(b*c*x - a*c)/((b*c*x - a*c)^2*\text{abs}(b)*\text{abs}(c))))/(b*c))/c - a/((b*c*x - a*c)*b*c)$

maple [A] time = 0.01, size = 35, normalized size = 1.09

$$-\frac{2a}{(bx - a)bc^2} + \frac{\ln(bx - a)}{bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/(-b*c*x+a*c)^2,x)`

[Out] $-2/c^2*a/b/(b*x-a)+1/c^2/b*\ln(b*x-a)$

maxima [A] time = 1.31, size = 37, normalized size = 1.16

$$-\frac{2a}{b^2c^2x - abc^2} + \frac{\log(bx - a)}{bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^2,x, algorithm="maxima")`

[Out] $-2*a/(b^2*c^2*x - a*b*c^2) + \log(b*x - a)/(b*c^2)$

mupad [B] time = 0.05, size = 37, normalized size = 1.16

$$\frac{\ln(bx - a)}{bc^2} + \frac{2a}{b(ac^2 - bc^2x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(a*c - b*c*x)^2, x)`

[Out] `log(b*x - a)/(b*c^2) + (2*a)/(b*(a*c^2 - b*c^2*x))`

sympy [A] time = 0.19, size = 29, normalized size = 0.91

$$-\frac{2a}{-abc^2 + b^2c^2x} + \frac{\log(-a + bx)}{bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)**2, x)`

[Out] `-2*a/(-a*b*c**2 + b**2*c**2*x) + log(-a + b*x)/(b*c**2)`

$$3.1034 \quad \int \frac{a+bx}{(ac-bcx)^3} dx$$

Optimal. Leaf size=13

$$\frac{x}{c^3(a-bx)^2}$$

[Out] x/c^3/(-b*x+a)^2

Rubi [A] time = 0.00, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {34}

$$\frac{x}{c^3(a-bx)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(a*c - b*c*x)^3, x]

[Out] x/(c^3*(a - b*x)^2)

Rule 34

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_)), x_Symbol] :> Simp[(d*x*(a + b*x)^(m + 1))/(b*(m + 2)), x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[a*d - b*c*(m + 2), 0]

Rubi steps

$$\int \frac{a+bx}{(ac-bcx)^3} dx = \frac{x}{c^3(a-bx)^2}$$

Mathematica [A] time = 0.01, size = 13, normalized size = 1.00

$$\frac{x}{c^3(a-bx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(a*c - b*c*x)^3, x]

[Out] x/(c^3*(a - b*x)^2)

fricas [B] time = 0.41, size = 30, normalized size = 2.31

$$\frac{x}{b^2c^3x^2 - 2abc^3x + a^2c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(-b*c*x+a*c)^3,x, algorithm="fricas")

[Out] x/(b^2*c^3*x^2 - 2*a*b*c^3*x + a^2*c^3)

giac [A] time = 0.89, size = 14, normalized size = 1.08

$$\frac{x}{(bx - a)^2 c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(-b*c*x+a*c)^3,x, algorithm="giac")

[Out] x/((b*x - a)^2*c^3)

maple [B] time = 0.00, size = 33, normalized size = 2.54

$$\frac{\frac{a}{(bx-a)^2 b} + \frac{1}{(bx-a)b}}{c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/(-b*c*x+a*c)^3,x)

[Out] 1/c^3*(a/b/(b*x-a)^2+1/b/(b*x-a))

maxima [B] time = 1.31, size = 30, normalized size = 2.31

$$\frac{x}{b^2 c^3 x^2 - 2 a b c^3 x + a^2 c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(-b*c*x+a*c)^3,x, algorithm="maxima")

[Out] x/(b^2*c^3*x^2 - 2*a*b*c^3*x + a^2*c^3)

mupad [B] time = 0.15, size = 13, normalized size = 1.00

$$\frac{x}{c^3 (a - bx)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(a*c - b*c*x)^3,x)

[Out] x/(c^3*(a - b*x)^2)

sympy [B] time = 0.24, size = 27, normalized size = 2.08

$$\frac{x}{a^2c^3 - 2abc^3x + b^2c^3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(-b*c*x+a*c)**3,x)

[Out] x/(a**2*c**3 - 2*a*b*c**3*x + b**2*c**3*x**2)

$$3.1035 \quad \int \frac{a+bx}{(ac-bcx)^4} dx$$

Optimal. Leaf size=38

$$\frac{2a}{3bc^4(a-bx)^3} - \frac{1}{2bc^4(a-bx)^2}$$

[Out] $2/3*a/b/c^4/(-b*x+a)^3-1/2/b/c^4/(-b*x+a)^2$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{2a}{3bc^4(a-bx)^3} - \frac{1}{2bc^4(a-bx)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(a*c - b*c*x)^4, x]

[Out] (2*a)/(3*b*c^4*(a - b*x)^3) - 1/(2*b*c^4*(a - b*x)^2)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{(ac-bcx)^4} dx &= \int \left(\frac{2a}{c^4(a-bx)^4} - \frac{1}{c^4(a-bx)^3} \right) dx \\ &= \frac{2a}{3bc^4(a-bx)^3} - \frac{1}{2bc^4(a-bx)^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 0.66

$$-\frac{a+3bx}{6bc^4(bx-a)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(a*c - b*c*x)^4, x]

[Out] $-1/6*(a + 3*b*x)/(b*c^4*(-a + b*x)^3)$

fricas [A] time = 0.47, size = 54, normalized size = 1.42

$$-\frac{3bx + a}{6(b^4c^4x^3 - 3ab^3c^4x^2 + 3a^2b^2c^4x - a^3bc^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^4,x, algorithm="fricas")`

[Out] $-1/6*(3*b*x + a)/(b^4*c^4*x^3 - 3*a*b^3*c^4*x^2 + 3*a^2*b^2*c^4*x - a^3*b*c^4)$

giac [A] time = 0.98, size = 23, normalized size = 0.61

$$-\frac{3bx + a}{6(bx - a)^3bc^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^4,x, algorithm="giac")`

[Out] $-1/6*(3*b*x + a)/((b*x - a)^3*b*c^4)$

maple [A] time = 0.01, size = 35, normalized size = 0.92

$$\frac{\frac{2a}{3(bx-a)^3b} - \frac{1}{2(bx-a)^2b}}{c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/(-b*c*x+a*c)^4,x)`

[Out] $1/c^4*(-1/2/b/(b*x-a)^2-2/3*a/b/(b*x-a)^3)$

maxima [A] time = 1.34, size = 54, normalized size = 1.42

$$-\frac{3bx + a}{6(b^4c^4x^3 - 3ab^3c^4x^2 + 3a^2b^2c^4x - a^3bc^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^4,x, algorithm="maxima")`

[Out] $-1/6*(3*b*x + a)/(b^4*c^4*x^3 - 3*a*b^3*c^4*x^2 + 3*a^2*b^2*c^4*x - a^3*b*c^4)$

mupad [B] time = 0.05, size = 54, normalized size = 1.42

$$\frac{\frac{x}{2} + \frac{a}{6b}}{a^3 c^4 - 3 a^2 b c^4 x + 3 a b^2 c^4 x^2 - b^3 c^4 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(a*c - b*c*x)^4, x)`

[Out] `(x/2 + a/(6*b))/(a^3*c^4 - b^3*c^4*x^3 + 3*a*b^2*c^4*x^2 - 3*a^2*b*c^4*x)`

sympy [A] time = 0.31, size = 56, normalized size = 1.47

$$\frac{-a - 3bx}{-6a^3bc^4 + 18a^2b^2c^4x - 18ab^3c^4x^2 + 6b^4c^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)**4, x)`

[Out] `(-a - 3*b*x)/(-6*a**3*b*c**4 + 18*a**2*b**2*c**4*x - 18*a*b**3*c**4*x**2 + 6*b**4*c**4*x**3)`

$$3.1036 \quad \int \frac{a+bx}{(ac-bcx)^5} dx$$

Optimal. Leaf size=38

$$\frac{a}{2bc^5(a-bx)^4} - \frac{1}{3bc^5(a-bx)^3}$$

[Out] $1/2*a/b/c^5/(-b*x+a)^4 - 1/3/b/c^5/(-b*x+a)^3$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{a}{2bc^5(a-bx)^4} - \frac{1}{3bc^5(a-bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(a*c - b*c*x)^5, x]

[Out] $a/(2*b*c^5*(a - b*x)^4) - 1/(3*b*c^5*(a - b*x)^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{(ac-bcx)^5} dx &= \int \left(\frac{2a}{c^5(a-bx)^5} - \frac{1}{c^5(a-bx)^4} \right) dx \\ &= \frac{a}{2bc^5(a-bx)^4} - \frac{1}{3bc^5(a-bx)^3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 0.63

$$\frac{a+2bx}{6bc^5(a-bx)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(a*c - b*c*x)^5, x]

[Out] $(a + 2bx)/(6b^5c^5(a - bx)^4)$

fricas [A] time = 0.42, size = 67, normalized size = 1.76

$$\frac{2bx + a}{6(b^5c^5x^4 - 4ab^4c^5x^3 + 6a^2b^3c^5x^2 - 4a^3b^2c^5x + a^4bc^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^5,x, algorithm="fricas")`

[Out] $1/6*(2bx + a)/(b^5c^5x^4 - 4a^3b^2c^5x^3 + 6a^2b^3c^5x^2 - 4a^4b^3c^5x + a^4bc^5)$

giac [A] time = 0.95, size = 40, normalized size = 1.05

$$\frac{a}{2(bc x - ac)^4 bc} + \frac{1}{3(bc x - ac)^3 bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^5,x, algorithm="giac")`

[Out] $1/2*a/((b*c*x - a*c)^4*b*c) + 1/3/((b*c*x - a*c)^3*b*c^2)$

maple [A] time = 0.00, size = 35, normalized size = 0.92

$$\frac{\frac{a}{2(bx-a)^4b} + \frac{1}{3(bx-a)^3b}}{c^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/(-b*c*x+a*c)^5,x)`

[Out] $1/c^5*(1/2*a/b/(b*x-a)^4+1/3/b/(b*x-a)^3)$

maxima [A] time = 1.35, size = 67, normalized size = 1.76

$$\frac{2bx + a}{6(b^5c^5x^4 - 4ab^4c^5x^3 + 6a^2b^3c^5x^2 - 4a^3b^2c^5x + a^4bc^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^5,x, algorithm="maxima")`

[Out] $1/6*(2bx + a)/(b^5c^5x^4 - 4a^3b^2c^5x^3 + 6a^2b^3c^5x^2 - 4a^4b^3c^5x + a^4bc^5)$

mupad [B] time = 0.17, size = 67, normalized size = 1.76

$$\frac{\frac{x}{3} + \frac{a}{6b}}{a^4 c^5 - 4 a^3 b c^5 x + 6 a^2 b^2 c^5 x^2 - 4 a b^3 c^5 x^3 + b^4 c^5 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(a*c - b*c*x)^5,x)

[Out] (x/3 + a/(6*b))/(a^4*c^5 + b^4*c^5*x^4 - 4*a*b^3*c^5*x^3 + 6*a^2*b^2*c^5*x^2 - 4*a^3*b*c^5*x)

sympy [B] time = 0.39, size = 73, normalized size = 1.92

$$\frac{-a - 2bx}{6a^4bc^5 - 24a^3b^2c^5x + 36a^2b^3c^5x^2 - 24ab^4c^5x^3 + 6b^5c^5x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(-b*c*x+a*c)**5,x)

[Out] -(-a - 2*b*x)/(6*a**4*b*c**5 - 24*a**3*b**2*c**5*x + 36*a**2*b**3*c**5*x**2 - 24*a*b**4*c**5*x**3 + 6*b**5*c**5*x**4)

$$3.1037 \quad \int \frac{a+bx}{(ac-bcx)^6} dx$$

Optimal. Leaf size=38

$$\frac{2a}{5bc^6(a-bx)^5} - \frac{1}{4bc^6(a-bx)^4}$$

[Out] $2/5*a/b/c^6/(-b*x+a)^5-1/4/b/c^6/(-b*x+a)^4$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{2a}{5bc^6(a-bx)^5} - \frac{1}{4bc^6(a-bx)^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(a*c - b*c*x)^6, x]

[Out] (2*a)/(5*b*c^6*(a - b*x)^5) - 1/(4*b*c^6*(a - b*x)^4)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{(ac-bcx)^6} dx &= \int \left(\frac{2a}{c^6(a-bx)^6} - \frac{1}{c^6(a-bx)^5} \right) dx \\ &= \frac{2a}{5bc^6(a-bx)^5} - \frac{1}{4bc^6(a-bx)^4} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.71

$$-\frac{3a+5bx}{20bc^6(bx-a)^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(a*c - b*c*x)^6, x]

[Out] $-1/20*(3*a + 5*b*x)/(b*c^6*(-a + b*x)^5)$

fricas [B] time = 0.45, size = 84, normalized size = 2.21

$$\frac{5bx + 3a}{20(b^6c^6x^5 - 5ab^5c^6x^4 + 10a^2b^4c^6x^3 - 10a^3b^3c^6x^2 + 5a^4b^2c^6x - a^5bc^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^6,x, algorithm="fricas")`

[Out] $-1/20*(5*b*x + 3*a)/(b^6*c^6*x^5 - 5*a*b^5*c^6*x^4 + 10*a^2*b^4*c^6*x^3 - 10*a^3*b^3*c^6*x^2 + 5*a^4*b^2*c^6*x - a^5*b*c^6)$

giac [A] time = 1.04, size = 25, normalized size = 0.66

$$-\frac{5bx + 3a}{20(bx - a)^5bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^6,x, algorithm="giac")`

[Out] $-1/20*(5*b*x + 3*a)/((b*x - a)^5*b*c^6)$

maple [A] time = 0.00, size = 35, normalized size = 0.92

$$\frac{-\frac{2a}{5(bx-a)^5b} - \frac{1}{4(bx-a)^4b}}{c^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/(-b*c*x+a*c)^6,x)`

[Out] $1/c^6*(-1/4/b/(b*x-a)^4-2/5*a/b/(b*x-a)^5)$

maxima [B] time = 1.31, size = 84, normalized size = 2.21

$$\frac{5bx + 3a}{20(b^6c^6x^5 - 5ab^5c^6x^4 + 10a^2b^4c^6x^3 - 10a^3b^3c^6x^2 + 5a^4b^2c^6x - a^5bc^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(-b*c*x+a*c)^6,x, algorithm="maxima")`

[Out] $-1/20*(5*b*x + 3*a)/(b^6*c^6*x^5 - 5*a*b^5*c^6*x^4 + 10*a^2*b^4*c^6*x^3 - 10*a^3*b^3*c^6*x^2 + 5*a^4*b^2*c^6*x - a^5*b*c^6)$

mupad [B] time = 0.08, size = 82, normalized size = 2.16

$$\frac{\frac{x}{4} + \frac{3a}{20b}}{a^5 c^6 - 5 a^4 b c^6 x + 10 a^3 b^2 c^6 x^2 - 10 a^2 b^3 c^6 x^3 + 5 a b^4 c^6 x^4 - b^5 c^6 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(a*c - b*c*x)^6,x)

[Out] (x/4 + (3*a)/(20*b))/(a^5*c^6 - b^5*c^6*x^5 + 5*a*b^4*c^6*x^4 + 10*a^3*b^2*c^6*x^2 - 10*a^2*b^3*c^6*x^3 - 5*a^4*b*c^6*x)

sympy [B] time = 0.46, size = 88, normalized size = 2.32

$$\frac{-3a - 5bx}{-20a^5bc^6 + 100a^4b^2c^6x - 200a^3b^3c^6x^2 + 200a^2b^4c^6x^3 - 100ab^5c^6x^4 + 20b^6c^6x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(-b*c*x+a*c)**6,x)

[Out] (-3*a - 5*b*x)/(-20*a**5*b*c**6 + 100*a**4*b**2*c**6*x - 200*a**3*b**3*c**6*x**2 + 200*a**2*b**4*c**6*x**3 - 100*a*b**5*c**6*x**4 + 20*b**6*c**6*x**5)

3.1038 $\int (a + bx)^2 (ac - bcx)^3 dx$

Optimal. Leaf size=57

$$-\frac{a^2 c^3 (a - bx)^4}{b} - \frac{c^3 (a - bx)^6}{6b} + \frac{4ac^3 (a - bx)^5}{5b}$$

[Out] $-a^2 c^3 (-b*x+a)^4/b + 4/5 * a * c^3 * (-b*x+a)^5/b - 1/6 * c^3 * (-b*x+a)^6/b$

Rubi [A] time = 0.03, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$-\frac{a^2 c^3 (a - bx)^4}{b} - \frac{c^3 (a - bx)^6}{6b} + \frac{4ac^3 (a - bx)^5}{5b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(a*c - b*c*x)^3,x]

[Out] $-((a^2*c^3*(a - b*x)^4)/b) + (4*a*c^3*(a - b*x)^5)/(5*b) - (c^3*(a - b*x)^6)/(6*b)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2 (ac - bcx)^3 dx &= \int \left(4a^2 (ac - bcx)^3 - \frac{4a(ac - bcx)^4}{c} + \frac{(ac - bcx)^5}{c^2} \right) dx \\ &= -\frac{a^2 c^3 (a - bx)^4}{b} + \frac{4ac^3 (a - bx)^5}{5b} - \frac{c^3 (a - bx)^6}{6b} \end{aligned}$$

Mathematica [A] time = 0.00, size = 68, normalized size = 1.19

$$c^3 \left(a^5 x - \frac{1}{2} a^4 b x^2 - \frac{2}{3} a^3 b^2 x^3 + \frac{1}{2} a^2 b^3 x^4 + \frac{1}{5} a b^4 x^5 - \frac{1}{6} b^5 x^6 \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(a*c - b*c*x)^3,x]

[Out] $c^3*(a^5*x - (a^4*b*x^2)/2 - (2*a^3*b^2*x^3)/3 + (a^2*b^3*x^4)/2 + (a*b^4*x^5)/5 - (b^5*x^6)/6)$

fricas [A] time = 0.38, size = 72, normalized size = 1.26

$$-\frac{1}{6}x^6c^3b^5 + \frac{1}{5}x^5c^3b^4a + \frac{1}{2}x^4c^3b^3a^2 - \frac{2}{3}x^3c^3b^2a^3 - \frac{1}{2}x^2c^3ba^4 + xc^3a^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c)^3,x, algorithm="fricas")

[Out] $-1/6*x^6*c^3*b^5 + 1/5*x^5*c^3*b^4*a + 1/2*x^4*c^3*b^3*a^2 - 2/3*x^3*c^3*b^2*a^3 - 1/2*x^2*c^3*b*a^4 + x*c^3*a^5$

giac [A] time = 1.04, size = 72, normalized size = 1.26

$$-\frac{1}{6}b^5c^3x^6 + \frac{1}{5}ab^4c^3x^5 + \frac{1}{2}a^2b^3c^3x^4 - \frac{2}{3}a^3b^2c^3x^3 - \frac{1}{2}a^4bc^3x^2 + a^5c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c)^3,x, algorithm="giac")

[Out] $-1/6*b^5*c^3*x^6 + 1/5*a*b^4*c^3*x^5 + 1/2*a^2*b^3*c^3*x^4 - 2/3*a^3*b^2*c^3*x^3 - 1/2*a^4*b*c^3*x^2 + a^5*c^3*x$

maple [A] time = 0.00, size = 73, normalized size = 1.28

$$-\frac{1}{6}b^5c^3x^6 + \frac{1}{5}ab^4c^3x^5 + \frac{1}{2}a^2b^3c^3x^4 - \frac{2}{3}a^3b^2c^3x^3 - \frac{1}{2}a^4bc^3x^2 + a^5c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(-b*c*x+a*c)^3,x)

[Out] $-1/6*b^5*c^3*x^6+1/5*a*b^4*c^3*x^5+1/2*a^2*b^3*c^3*x^4-2/3*a^3*c^3*b^2*x^3-1/2*a^4*c^3*b*x^2+a^5*c^3*x$

maxima [A] time = 1.29, size = 72, normalized size = 1.26

$$-\frac{1}{6}b^5c^3x^6 + \frac{1}{5}ab^4c^3x^5 + \frac{1}{2}a^2b^3c^3x^4 - \frac{2}{3}a^3b^2c^3x^3 - \frac{1}{2}a^4bc^3x^2 + a^5c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c)^3,x, algorithm="maxima")

[Out] $-1/6*b^5*c^3*x^6 + 1/5*a*b^4*c^3*x^5 + 1/2*a^2*b^3*c^3*x^4 - 2/3*a^3*b^2*c^3*x^3 - 1/2*a^4*b*c^3*x^2 + a^5*c^3*x$

mupad [B] time = 0.03, size = 72, normalized size = 1.26

$$a^5 c^3 x - \frac{a^4 b c^3 x^2}{2} - \frac{2 a^3 b^2 c^3 x^3}{3} + \frac{a^2 b^3 c^3 x^4}{2} + \frac{a b^4 c^3 x^5}{5} - \frac{b^5 c^3 x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c - b*c*x)^3*(a + b*x)^2,x)`

[Out] $a^5*c^3*x - (b^5*c^3*x^6)/6 - (a^4*b*c^3*x^2)/2 + (a*b^4*c^3*x^5)/5 - (2*a^3*b^2*c^3*x^3)/3 + (a^2*b^3*c^3*x^4)/2$

sympy [A] time = 0.09, size = 78, normalized size = 1.37

$$a^5 c^3 x - \frac{a^4 b c^3 x^2}{2} - \frac{2 a^3 b^2 c^3 x^3}{3} + \frac{a^2 b^3 c^3 x^4}{2} + \frac{a b^4 c^3 x^5}{5} - \frac{b^5 c^3 x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(-b*c*x+a*c)**3,x)`

[Out] $a**5*c**3*x - a**4*b*c**3*x**2/2 - 2*a**3*b**2*c**3*x**3/3 + a**2*b**3*c**3*x**4/2 + a*b**4*c**3*x**5/5 - b**5*c**3*x**6/6$

3.1039 $\int (a + bx)^2 (ac - bcx)^2 dx$

Optimal. Leaf size=38

$$a^4 c^2 x - \frac{2}{3} a^2 b^2 c^2 x^3 + \frac{1}{5} b^4 c^2 x^5$$

[Out] $a^4 c^2 x - 2/3 a^2 b^2 c^2 x^3 + 1/5 b^4 c^2 x^5$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {41, 194}

$$-\frac{2}{3} a^2 b^2 c^2 x^3 + a^4 c^2 x + \frac{1}{5} b^4 c^2 x^5$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^2*(a*c - b*c*x)^2, x]$

[Out] $a^4*c^2*x - (2*a^2*b^2*c^2*x^3)/3 + (b^4*c^2*x^5)/5$

Rule 41

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Int}[(a*c + b*d*x^2)^m, x] /; \text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{EqQ}[b*c + a*d, 0] \ \&\& \ (\text{IntegerQ}[m] \ || \ (\text{GtQ}[a, 0] \ \&\& \ \text{GtQ}[c, 0]))$

Rule 194

$\text{Int}[(a + b*x)^n*(c + d*x)^p, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(a + b*x)^n*(c + d*x)^p, x], x] /; \text{FreeQ}\{a, b\}, x \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{IGtQ}[p, 0]$

Rubi steps

$$\begin{aligned} \int (a + bx)^2 (ac - bcx)^2 dx &= \int (a^2 c - b^2 c x^2)^2 dx \\ &= \int (a^4 c^2 - 2 a^2 b^2 c^2 x^2 + b^4 c^2 x^4) dx \\ &= a^4 c^2 x - \frac{2}{3} a^2 b^2 c^2 x^3 + \frac{1}{5} b^4 c^2 x^5 \end{aligned}$$

Mathematica [A] time = 0.00, size = 38, normalized size = 1.00

$$a^4 c^2 x - \frac{2}{3} a^2 b^2 c^2 x^3 + \frac{1}{5} b^4 c^2 x^5$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(a*c - b*c*x)^2,x]

[Out] a^4*c^2*x - (2*a^2*b^2*c^2*x^3)/3 + (b^4*c^2*x^5)/5

fricas [A] time = 0.38, size = 34, normalized size = 0.89

$$\frac{1}{5}x^5c^2b^4 - \frac{2}{3}x^3c^2b^2a^2 + xc^2a^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c)^2,x, algorithm="fricas")

[Out] 1/5*x^5*c^2*b^4 - 2/3*x^3*c^2*b^2*a^2 + x*c^2*a^4

giac [A] time = 1.10, size = 34, normalized size = 0.89

$$\frac{1}{5}b^4c^2x^5 - \frac{2}{3}a^2b^2c^2x^3 + a^4c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c)^2,x, algorithm="giac")

[Out] 1/5*b^4*c^2*x^5 - 2/3*a^2*b^2*c^2*x^3 + a^4*c^2*x

maple [A] time = 0.00, size = 35, normalized size = 0.92

$$\frac{1}{5}b^4c^2x^5 - \frac{2}{3}a^2b^2c^2x^3 + a^4c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(-b*c*x+a*c)^2,x)

[Out] a^4*c^2*x-2/3*a^2*b^2*c^2*x^3+1/5*b^4*c^2*x^5

maxima [A] time = 1.34, size = 34, normalized size = 0.89

$$\frac{1}{5}b^4c^2x^5 - \frac{2}{3}a^2b^2c^2x^3 + a^4c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c)^2,x, algorithm="maxima")

[Out] 1/5*b^4*c^2*x^5 - 2/3*a^2*b^2*c^2*x^3 + a^4*c^2*x

mupad [B] time = 0.04, size = 31, normalized size = 0.82

$$\frac{c^2 x (15 a^4 - 10 a^2 b^2 x^2 + 3 b^4 x^4)}{15}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c - b*c*x)^2*(a + b*x)^2,x)`

[Out] `(c^2*x*(15*a^4 + 3*b^4*x^4 - 10*a^2*b^2*x^2))/15`

sympy [A] time = 0.08, size = 36, normalized size = 0.95

$$a^4 c^2 x - \frac{2 a^2 b^2 c^2 x^3}{3} + \frac{b^4 c^2 x^5}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(-b*c*x+a*c)**2,x)`

[Out] `a**4*c**2*x - 2*a**2*b**2*c**2*x**3/3 + b**4*c**2*x**5/5`

3.1040 $\int (a + bx)^2(ac - bcx) dx$

Optimal. Leaf size=32

$$\frac{2ac(a + bx)^3}{3b} - \frac{c(a + bx)^4}{4b}$$

[Out] $2/3*a*c*(b*x+a)^3/b-1/4*c*(b*x+a)^4/b$

Rubi [A] time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{2ac(a + bx)^3}{3b} - \frac{c(a + bx)^4}{4b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(a*c - b*c*x), x]

[Out] (2*a*c*(a + b*x)^3)/(3*b) - (c*(a + b*x)^4)/(4*b)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2(ac - bcx) dx &= \int (2ac(a + bx)^2 - c(a + bx)^3) dx \\ &= \frac{2ac(a + bx)^3}{3b} - \frac{c(a + bx)^4}{4b} \end{aligned}$$

Mathematica [A] time = 0.00, size = 40, normalized size = 1.25

$$c \left(a^3x + \frac{1}{2}a^2bx^2 - \frac{1}{3}ab^2x^3 - \frac{1}{4}b^3x^4 \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(a*c - b*c*x), x]

[Out] c*(a^3*x + (a^2*b*x^2)/2 - (a*b^2*x^3)/3 - (b^3*x^4)/4)

fricas [A] time = 0.39, size = 36, normalized size = 1.12

$$-\frac{1}{4}x^4cb^3 - \frac{1}{3}x^3cb^2a + \frac{1}{2}x^2cba^2 + xca^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c),x, algorithm="fricas")

[Out] -1/4*x^4*c*b^3 - 1/3*x^3*c*b^2*a + 1/2*x^2*c*b*a^2 + x*c*a^3

giac [A] time = 1.02, size = 36, normalized size = 1.12

$$-\frac{1}{4}b^3cx^4 - \frac{1}{3}ab^2cx^3 + \frac{1}{2}a^2bcx^2 + a^3cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c),x, algorithm="giac")

[Out] -1/4*b^3*c*x^4 - 1/3*a*b^2*c*x^3 + 1/2*a^2*b*c*x^2 + a^3*c*x

maple [A] time = 0.00, size = 37, normalized size = 1.16

$$-\frac{1}{4}b^3cx^4 - \frac{1}{3}ab^2cx^3 + \frac{1}{2}a^2bcx^2 + a^3cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(-b*c*x+a*c),x)

[Out] -1/4*b^3*c*x^4-1/3*a*b^2*c*x^3+1/2*a^2*b*c*x^2+a^3*c*x

maxima [A] time = 1.32, size = 36, normalized size = 1.12

$$-\frac{1}{4}b^3cx^4 - \frac{1}{3}ab^2cx^3 + \frac{1}{2}a^2bcx^2 + a^3cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c),x, algorithm="maxima")

[Out] -1/4*b^3*c*x^4 - 1/3*a*b^2*c*x^3 + 1/2*a^2*b*c*x^2 + a^3*c*x

mupad [B] time = 0.05, size = 36, normalized size = 1.12

$$ca^3x + \frac{ca^2bx^2}{2} - \frac{cab^2x^3}{3} - \frac{cb^3x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c - b*c*x)*(a + b*x)^2,x)`

[Out] `a^3*c*x - (b^3*c*x^4)/4 + (a^2*b*c*x^2)/2 - (a*b^2*c*x^3)/3`

sympy [A] time = 0.07, size = 39, normalized size = 1.22

$$a^3cx + \frac{a^2bcx^2}{2} - \frac{ab^2cx^3}{3} - \frac{b^3cx^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(-b*c*x+a*c),x)`

[Out] `a**3*c*x + a**2*b*c*x**2/2 - a*b**2*c*x**3/3 - b**3*c*x**4/4`

3.1041 $\int (a + bx)^2 dx$

Optimal. Leaf size=14

$$\frac{(a + bx)^3}{3b}$$

[Out] 1/3*(b*x+a)^3/b

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(a + bx)^3}{3b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2,x]

[Out] (a + b*x)^3/(3*b)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^2 dx = \frac{(a + bx)^3}{3b}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{(a + bx)^3}{3b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2,x]

[Out] (a + b*x)^3/(3*b)

fricas [A] time = 0.37, size = 20, normalized size = 1.43

$$\frac{1}{3}x^3b^2 + x^2ba + xa^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2,x, algorithm="fricas")

[Out] 1/3*x^3*b^2 + x^2*b*a + x*a^2

giac [A] time = 0.97, size = 12, normalized size = 0.86

$$\frac{(bx + a)^3}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2,x, algorithm="giac")

[Out] 1/3*(b*x + a)^3/b

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{(bx + a)^3}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2,x)

[Out] 1/3*(b*x+a)^3/b

maxima [A] time = 1.27, size = 20, normalized size = 1.43

$$\frac{1}{3}b^2x^3 + abx^2 + a^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2,x, algorithm="maxima")

[Out] 1/3*b^2*x^3 + a*b*x^2 + a^2*x

mupad [B] time = 0.03, size = 20, normalized size = 1.43

$$a^2x + abx^2 + \frac{b^2x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2,x)

[Out] a^2*x + (b^2*x^3)/3 + a*b*x^2

sympy [B] time = 0.06, size = 19, normalized size = 1.36

$$a^2x + abx^2 + \frac{b^2x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**2,x)
```

```
[Out] a**2*x + a*b*x**2 + b**2*x**3/3
```

$$3.1042 \quad \int \frac{(a+bx)^2}{ac-bcx} dx$$

Optimal. Leaf size=43

$$-\frac{4a^2 \log(a-bx)}{bc} - \frac{(a+bx)^2}{2bc} - \frac{2ax}{c}$$

[Out] $-2*a*x/c - 1/2*(b*x+a)^2/b/c - 4*a^2*\ln(-b*x+a)/b/c$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$-\frac{4a^2 \log(a-bx)}{bc} - \frac{(a+bx)^2}{2bc} - \frac{2ax}{c}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(a*c - b*c*x), x]

[Out] $(-2*a*x)/c - (a + b*x)^2/(2*b*c) - (4*a^2*\text{Log}[a - b*x])/(b*c)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{ac-bcx} dx &= \int \left(-\frac{2a}{c} - \frac{a+bx}{c} + \frac{4a^2}{ac-bcx} \right) dx \\ &= -\frac{2ax}{c} - \frac{(a+bx)^2}{2bc} - \frac{4a^2 \log(a-bx)}{bc} \end{aligned}$$

Mathematica [A] time = 0.01, size = 37, normalized size = 0.86

$$-\frac{4a^2 \log(a-bx)}{bc} - \frac{3ax}{c} - \frac{bx^2}{2c}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(a*c - b*c*x), x]

[Out] $(-3ax)/c - (bx^2)/(2c) - (4a^2 \text{Log}[a - bx])/(bc)$

fricas [A] time = 0.44, size = 34, normalized size = 0.79

$$\frac{b^2x^2 + 6abx + 8a^2 \log(bx - a)}{2bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/(-b*c*x+a*c),x, algorithm="fricas")`

[Out] $-1/2*(b^2x^2 + 6a*bx + 8a^2*\log(bx - a))/(bc)$

giac [A] time = 0.87, size = 46, normalized size = 1.07

$$-\frac{4a^2 \log(|bx - a|)}{bc} - \frac{b^3cx^2 + 6ab^2cx}{2b^2c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/(-b*c*x+a*c),x, algorithm="giac")`

[Out] $-4a^2*\log(\text{abs}(bx - a))/(bc) - 1/2*(b^3c*x^2 + 6a*b^2*c*x)/(b^2*c^2)$

maple [A] time = 0.00, size = 37, normalized size = 0.86

$$\frac{bx^2}{2c} - \frac{4a^2 \ln(bx - a)}{bc} - \frac{3ax}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2/(-b*c*x+a*c),x)`

[Out] $-1/2/c*x^2*b-3*a*x/c-4/c*a^2/b*\ln(b*x-a)$

maxima [A] time = 1.29, size = 35, normalized size = 0.81

$$-\frac{4a^2 \log(bx - a)}{bc} - \frac{bx^2 + 6ax}{2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2/(-b*c*x+a*c),x, algorithm="maxima")`

[Out] $-4a^2*\log(bx - a)/(bc) - 1/2*(bx^2 + 6a*x)/c$

mupad [B] time = 0.05, size = 34, normalized size = 0.79

$$\frac{8a^2 \ln(bx - a) + b^2x^2 + 6abx}{2bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(a*c - b*c*x),x)`

[Out] $-(8*a^2*\log(b*x - a) + b^2*x^2 + 6*a*b*x)/(2*b*c)$

sympy [A] time = 0.17, size = 31, normalized size = 0.72

$$-\frac{4a^2 \log(-a + bx)}{bc} - \frac{3ax}{c} - \frac{bx^2}{2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/(-b*c*x+a*c),x)`

[Out] $-4*a**2*\log(-a + b*x)/(b*c) - 3*a*x/c - b*x**2/(2*c)$

$$3.1043 \quad \int \frac{(a+bx)^2}{(ac-bcx)^2} dx$$

Optimal. Leaf size=41

$$\frac{4a^2}{bc^2(a-bx)} + \frac{4a \log(a-bx)}{bc^2} + \frac{x}{c^2}$$

[Out] $x/c^2 + 4*a^2/b/c^2/(-b*x+a) + 4*a*\ln(-b*x+a)/b/c^2$

Rubi [A] time = 0.02, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$\frac{4a^2}{bc^2(a-bx)} + \frac{4a \log(a-bx)}{bc^2} + \frac{x}{c^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(a*c - b*c*x)^2, x]

[Out] $x/c^2 + (4*a^2)/(b*c^2*(a - b*x)) + (4*a*\text{Log}[a - b*x])/(b*c^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(ac-bcx)^2} dx &= \int \left(\frac{1}{c^2} + \frac{4a^2}{c^2(a-bx)^2} - \frac{4a}{c^2(a-bx)} \right) dx \\ &= \frac{x}{c^2} + \frac{4a^2}{bc^2(a-bx)} + \frac{4a \log(a-bx)}{bc^2} \end{aligned}$$

Mathematica [A] time = 0.03, size = 35, normalized size = 0.85

$$\frac{\frac{4a^2}{b(a-bx)} + \frac{4a \log(a-bx)}{b} + x}{c^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(a*c - b*c*x)^2,x]

[Out] (x + (4*a^2)/(b*(a - b*x))) + (4*a*Log[a - b*x])/b)/c^2

fricas [A] time = 0.41, size = 57, normalized size = 1.39

$$\frac{b^2x^2 - abx - 4a^2 + 4(abx - a^2)\log(bx - a)}{b^2c^2x - abc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^2,x, algorithm="fricas")

[Out] (b^2*x^2 - a*b*x - 4*a^2 + 4*(a*b*x - a^2)*log(b*x - a))/(b^2*c^2*x - a*b*c^2)

giac [A] time = 1.08, size = 79, normalized size = 1.93

$$-\frac{4a^2}{(bcx - ac)bc} - \frac{4a \log\left(\frac{|bcx-ac|}{(bcx-ac)^2|b||c|}\right)}{bc^2} + \frac{bcx - ac}{bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^2,x, algorithm="giac")

[Out] -4*a^2/((b*c*x - a*c)*b*c) - 4*a*log(abs(b*c*x - a*c)/((b*c*x - a*c)^2*abs(b)*abs(c)))/(b*c^2) + (b*c*x - a*c)/(b*c^3)

maple [A] time = 0.01, size = 44, normalized size = 1.07

$$-\frac{4a^2}{(bx - a)bc^2} + \frac{4a \ln(bx - a)}{bc^2} + \frac{x}{c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(-b*c*x+a*c)^2,x)

[Out] x/c^2-4/c^2*a^2/b/(b*x-a)+4/c^2*a/b*ln(b*x-a)

maxima [A] time = 1.38, size = 46, normalized size = 1.12

$$-\frac{4a^2}{b^2c^2x - abc^2} + \frac{x}{c^2} + \frac{4a \log(bx - a)}{bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^2,x, algorithm="maxima")

[Out] $-4a^2/(b^2c^2x - abc^2) + x/c^2 + 4a \log(bx - a)/(bc^2)$

mupad [B] time = 0.15, size = 46, normalized size = 1.12

$$\frac{x}{c^2} + \frac{4a^2}{b(ac^2 - bc^2x)} + \frac{4a \ln(bx - a)}{bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(a*c - b*c*x)^2,x)`

[Out] $x/c^2 + (4a^2)/(b(ac^2 - bc^2x)) + (4a \log(bx - a))/(bc^2)$

sympy [A] time = 0.20, size = 39, normalized size = 0.95

$$-\frac{4a^2}{-abc^2 + b^2c^2x} + \frac{4a \log(-a + bx)}{bc^2} + \frac{x}{c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/(-b*c*x+a*c)**2,x)`

[Out] $-4a^2/(-abc^2 + b^2c^2x) + 4a \log(-a + bx)/(bc^2) + x/c^2$

$$3.1044 \quad \int \frac{(a+bx)^2}{(ac-bcx)^3} dx$$

Optimal. Leaf size=52

$$\frac{2a^2}{bc^3(a-bx)^2} - \frac{4a}{bc^3(a-bx)} - \frac{\log(a-bx)}{bc^3}$$

[Out] $2*a^2/b/c^3/(-b*x+a)^2-4*a/b/c^3/(-b*x+a)-\ln(-b*x+a)/b/c^3$

Rubi [A] time = 0.03, antiderivative size = 52, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$\frac{2a^2}{bc^3(a-bx)^2} - \frac{4a}{bc^3(a-bx)} - \frac{\log(a-bx)}{bc^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(a*c - b*c*x)^3,x]

[Out] $(2*a^2)/(b*c^3*(a - b*x)^2) - (4*a)/(b*c^3*(a - b*x)) - \text{Log}[a - b*x]/(b*c^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(ac-bcx)^3} dx &= \int \left(\frac{4a^2}{c^3(a-bx)^3} - \frac{4a}{c^3(a-bx)^2} + \frac{1}{c^3(a-bx)} \right) dx \\ &= \frac{2a^2}{bc^3(a-bx)^2} - \frac{4a}{bc^3(a-bx)} - \frac{\log(a-bx)}{bc^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 33, normalized size = 0.63

$$-\frac{\frac{2a(a-2bx)}{(a-bx)^2} + \log(a-bx)}{bc^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(a*c - b*c*x)^3,x]

[Out] -(((2*a*(a - 2*b*x))/(a - b*x)^2 + Log[a - b*x])/(b*c^3))

fricas [A] time = 0.41, size = 69, normalized size = 1.33

$$\frac{4 abx - 2 a^2 - (b^2 x^2 - 2 abx + a^2) \log (bx - a)}{b^3 c^3 x^2 - 2 ab^2 c^3 x + a^2 bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^3,x, algorithm="fricas")

[Out] (4*a*b*x - 2*a^2 - (b^2*x^2 - 2*a*b*x + a^2)*log(b*x - a))/(b^3*c^3*x^2 - 2*a*b^2*c^3*x + a^2*b*c^3)

giac [A] time = 1.07, size = 46, normalized size = 0.88

$$-\frac{\log(|bx - a|)}{bc^3} + \frac{2(2 abx - a^2)}{(bx - a)^2 bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^3,x, algorithm="giac")

[Out] -log(abs(b*x - a))/(b*c^3) + 2*(2*a*b*x - a^2)/((b*x - a)^2*b*c^3)

maple [A] time = 0.01, size = 56, normalized size = 1.08

$$\frac{2a^2}{(bx - a)^2 bc^3} + \frac{4a}{(bx - a) bc^3} - \frac{\ln(bx - a)}{bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(-b*c*x+a*c)^3,x)

[Out] 2/c^3*a^2/b/(b*x-a)^2+4/c^3*a/b/(b*x-a)-1/c^3/b*ln(b*x-a)

maxima [A] time = 1.33, size = 61, normalized size = 1.17

$$\frac{2(2 abx - a^2)}{b^3 c^3 x^2 - 2 ab^2 c^3 x + a^2 bc^3} - \frac{\log (bx - a)}{bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^3,x, algorithm="maxima")

[Out] $2*(2*a*b*x - a^2)/(b^3*c^3*x^2 - 2*a*b^2*c^3*x + a^2*b*c^3) - \log(b*x - a)/(b*c^3)$

mupad [B] time = 0.17, size = 59, normalized size = 1.13

$$\frac{4ax - \frac{2a^2}{b}}{a^2c^3 - 2abc^3x + b^2c^3x^2} - \frac{\ln(bx - a)}{bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(a*c - b*c*x)^3,x)

[Out] $(4*a*x - (2*a^2)/b)/(a^2*c^3 + b^2*c^3*x^2 - 2*a*b*c^3*x) - \log(b*x - a)/(b*c^3)$

sympy [A] time = 0.31, size = 54, normalized size = 1.04

$$-\frac{2a^2 - 4abx}{a^2bc^3 - 2ab^2c^3x + b^3c^3x^2} - \frac{\log(-a + bx)}{bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(-b*c*x+a*c)**3,x)

[Out] $-(2*a**2 - 4*a*b*x)/(a**2*b*c**3 - 2*a*b**2*c**3*x + b**3*c**3*x**2) - \log(-a + b*x)/(b*c**3)$

$$3.1045 \quad \int \frac{(a+bx)^2}{(ac-bcx)^4} dx$$

Optimal. Leaf size=28

$$\frac{(a+bx)^3}{6abc^4(a-bx)^3}$$

[Out] 1/6*(b*x+a)^3/a/b/c^4/(-b*x+a)^3

Rubi [A] time = 0.01, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{(a+bx)^3}{6abc^4(a-bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(a*c - b*c*x)^4, x]

[Out] (a + b*x)^3/(6*a*b*c^4*(a - b*x)^3)

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(a+bx)^2}{(ac-bcx)^4} dx = \frac{(a+bx)^3}{6abc^4(a-bx)^3}$$

Mathematica [A] time = 0.02, size = 31, normalized size = 1.11

$$-\frac{a^2 + 3b^2x^2}{3bc^4(bx - a)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(a*c - b*c*x)^4, x]

[Out] -1/3*(a^2 + 3*b^2*x^2)/(b*c^4*(-a + b*x)^3)

fricas [B] time = 0.40, size = 60, normalized size = 2.14

$$\frac{3b^2x^2 + a^2}{3(b^4c^4x^3 - 3ab^3c^4x^2 + 3a^2b^2c^4x - a^3bc^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^4,x, algorithm="fricas")

[Out] -1/3*(3*b^2*x^2 + a^2)/(b^4*c^4*x^3 - 3*a*b^3*c^4*x^2 + 3*a^2*b^2*c^4*x - a^3*b*c^4)

giac [A] time = 0.98, size = 29, normalized size = 1.04

$$\frac{3b^2x^2 + a^2}{3(bx - a)^3bc^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^4,x, algorithm="giac")

[Out] -1/3*(3*b^2*x^2 + a^2)/((b*x - a)^3*b*c^4)

maple [A] time = 0.00, size = 52, normalized size = 1.86

$$\frac{\frac{4a^2}{3(bx-a)^3b} - \frac{2a}{(bx-a)^2b} - \frac{1}{(bx-a)b}}{c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(-b*c*x+a*c)^4,x)

[Out] 1/c^4*(-2/(b*x-a)^2*a/b-4/3*a^2/b/(b*x-a)^3-1/(b*x-a)/b)

maxima [B] time = 1.33, size = 60, normalized size = 2.14

$$\frac{3b^2x^2 + a^2}{3(b^4c^4x^3 - 3ab^3c^4x^2 + 3a^2b^2c^4x - a^3bc^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^4,x, algorithm="maxima")

[Out] -1/3*(3*b^2*x^2 + a^2)/(b^4*c^4*x^3 - 3*a*b^3*c^4*x^2 + 3*a^2*b^2*c^4*x - a^3*b*c^4)

mupad [B] time = 0.05, size = 58, normalized size = 2.07

$$\frac{bx^2 + \frac{a^2}{3b}}{a^3c^4 - 3a^2bc^4x + 3ab^2c^4x^2 - b^3c^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(a*c - b*c*x)^4, x)

[Out] (b*x^2 + a^2/(3*b))/(a^3*c^4 - b^3*c^4*x^3 + 3*a*b^2*c^4*x^2 - 3*a^2*b*c^4*x)

sympy [B] time = 0.35, size = 61, normalized size = 2.18

$$\frac{-a^2 - 3b^2x^2}{-3a^3bc^4 + 9a^2b^2c^4x - 9ab^3c^4x^2 + 3b^4c^4x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(-b*c*x+a*c)**4, x)

[Out] (-a**2 - 3*b**2*x**2)/(-3*a**3*b*c**4 + 9*a**2*b**2*c**4*x - 9*a*b**3*c**4*x**2 + 3*b**4*c**4*x**3)

$$3.1046 \quad \int \frac{(a+bx)^2}{(ac-bcx)^5} dx$$

Optimal. Leaf size=56

$$\frac{a^2}{bc^5(a-bx)^4} - \frac{4a}{3bc^5(a-bx)^3} + \frac{1}{2bc^5(a-bx)^2}$$

[Out] $a^2/b/c^5/(-b*x+a)^4-4/3*a/b/c^5/(-b*x+a)^3+1/2/b/c^5/(-b*x+a)^2$

Rubi [A] time = 0.02, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$\frac{a^2}{bc^5(a-bx)^4} - \frac{4a}{3bc^5(a-bx)^3} + \frac{1}{2bc^5(a-bx)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(a*c - b*c*x)^5,x]

[Out] $a^2/(b*c^5*(a - b*x)^4) - (4*a)/(3*b*c^5*(a - b*x)^3) + 1/(2*b*c^5*(a - b*x)^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(ac-bcx)^5} dx &= \int \left(\frac{4a^2}{c^5(a-bx)^5} - \frac{4a}{c^5(a-bx)^4} + \frac{1}{c^5(a-bx)^3} \right) dx \\ &= \frac{a^2}{bc^5(a-bx)^4} - \frac{4a}{3bc^5(a-bx)^3} + \frac{1}{2bc^5(a-bx)^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.62

$$\frac{a^2 + 2abx + 3b^2x^2}{6bc^5(a-bx)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(a*c - b*c*x)^5,x]

[Out] (a^2 + 2*a*b*x + 3*b^2*x^2)/(6*b*c^5*(a - b*x)^4)

fricas [A] time = 0.41, size = 78, normalized size = 1.39

$$\frac{3b^2x^2 + 2abx + a^2}{6(b^5c^5x^4 - 4ab^4c^5x^3 + 6a^2b^3c^5x^2 - 4a^3b^2c^5x + a^4bc^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^5,x, algorithm="fricas")

[Out] 1/6*(3*b^2*x^2 + 2*a*b*x + a^2)/(b^5*c^5*x^4 - 4*a*b^4*c^5*x^3 + 6*a^2*b^3*c^5*x^2 - 4*a^3*b^2*c^5*x + a^4*b*c^5)

giac [A] time = 1.07, size = 64, normalized size = 1.14

$$\frac{\frac{6a^2}{(bcx-ac)^4b} + \frac{8a}{(bcx-ac)^3bc} + \frac{3}{(bcx-ac)^2bc^2}}{6c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^5,x, algorithm="giac")

[Out] 1/6*(6*a^2/((b*c*x - a*c)^4*b) + 8*a/((b*c*x - a*c)^3*b*c) + 3/((b*c*x - a*c)^2*b*c^2))/c

maple [A] time = 0.00, size = 51, normalized size = 0.91

$$\frac{\frac{a^2}{(bx-a)^4b} + \frac{4a}{3(bx-a)^3b} + \frac{1}{2(bx-a)^2b}}{c^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(-b*c*x+a*c)^5,x)

[Out] 1/c^5*(a^2/b/(b*x-a)^4+1/2/(b*x-a)^2/b+4/3/(b*x-a)^3*a/b)

maxima [A] time = 1.38, size = 78, normalized size = 1.39

$$\frac{3b^2x^2 + 2abx + a^2}{6(b^5c^5x^4 - 4ab^4c^5x^3 + 6a^2b^3c^5x^2 - 4a^3b^2c^5x + a^4bc^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^5,x, algorithm="maxima")

[Out] 1/6*(3*b^2*x^2 + 2*a*b*x + a^2)/(b^5*c^5*x^4 - 4*a*b^4*c^5*x^3 + 6*a^2*b^3*c^5*x^2 - 4*a^3*b^2*c^5*x + a^4*b*c^5)

mupad [B] time = 0.05, size = 76, normalized size = 1.36

$$\frac{\frac{ax}{3} + \frac{bx^2}{2} + \frac{a^2}{6b}}{a^4c^5 - 4a^3bc^5x + 6a^2b^2c^5x^2 - 4ab^3c^5x^3 + b^4c^5x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(a*c - b*c*x)^5,x)

[Out] ((a*x)/3 + (b*x^2)/2 + a^2/(6*b))/(a^4*c^5 + b^4*c^5*x^4 - 4*a*b^3*c^5*x^3 + 6*a^2*b^2*c^5*x^2 - 4*a^3*b*c^5*x)

sympy [A] time = 0.44, size = 85, normalized size = 1.52

$$\frac{-a^2 - 2abx - 3b^2x^2}{6a^4bc^5 - 24a^3b^2c^5x + 36a^2b^3c^5x^2 - 24ab^4c^5x^3 + 6b^5c^5x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(-b*c*x+a*c)**5,x)

[Out] -(-a**2 - 2*a*b*x - 3*b**2*x**2)/(6*a**4*b*c**5 - 24*a**3*b**2*c**5*x + 36*a**2*b**3*c**5*x**2 - 24*a*b**4*c**5*x**3 + 6*b**5*c**5*x**4)

$$3.1047 \quad \int \frac{(a+bx)^2}{(ac-bcx)^6} dx$$

Optimal. Leaf size=57

$$\frac{4a^2}{5bc^6(a-bx)^5} - \frac{a}{bc^6(a-bx)^4} + \frac{1}{3bc^6(a-bx)^3}$$

[Out] $4/5*a^2/b/c^6/(-b*x+a)^5 - a/b/c^6/(-b*x+a)^4 + 1/3/b/c^6/(-b*x+a)^3$

Rubi [A] time = 0.02, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$\frac{4a^2}{5bc^6(a-bx)^5} - \frac{a}{bc^6(a-bx)^4} + \frac{1}{3bc^6(a-bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(a*c - b*c*x)^6,x]

[Out] $(4*a^2)/(5*b*c^6*(a - b*x)^5) - a/(b*c^6*(a - b*x)^4) + 1/(3*b*c^6*(a - b*x)^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(ac-bcx)^6} dx &= \int \left(\frac{4a^2}{c^6(a-bx)^6} - \frac{4a}{c^6(a-bx)^5} + \frac{1}{c^6(a-bx)^4} \right) dx \\ &= \frac{4a^2}{5bc^6(a-bx)^5} - \frac{a}{bc^6(a-bx)^4} + \frac{1}{3bc^6(a-bx)^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 38, normalized size = 0.67

$$-\frac{2a^2 + 5abx + 5b^2x^2}{15bc^6(bx - a)^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(a*c - b*c*x)^6,x]

[Out] -1/15*(2*a^2 + 5*a*b*x + 5*b^2*x^2)/(b*c^6*(-a + b*x)^5)

fricas [A] time = 0.44, size = 95, normalized size = 1.67

$$\frac{5b^2x^2 + 5abx + 2a^2}{15(b^6c^6x^5 - 5ab^5c^6x^4 + 10a^2b^4c^6x^3 - 10a^3b^3c^6x^2 + 5a^4b^2c^6x - a^5bc^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^6,x, algorithm="fricas")

[Out] -1/15*(5*b^2*x^2 + 5*a*b*x + 2*a^2)/(b^6*c^6*x^5 - 5*a*b^5*c^6*x^4 + 10*a^2*b^4*c^6*x^3 - 10*a^3*b^3*c^6*x^2 + 5*a^4*b^2*c^6*x - a^5*b*c^6)

giac [A] time = 0.85, size = 36, normalized size = 0.63

$$\frac{5b^2x^2 + 5abx + 2a^2}{15(bx - a)^5bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^6,x, algorithm="giac")

[Out] -1/15*(5*b^2*x^2 + 5*a*b*x + 2*a^2)/((b*x - a)^5*b*c^6)

maple [A] time = 0.00, size = 52, normalized size = 0.91

$$\frac{\frac{4a^2}{5(bx-a)^5b} - \frac{a}{(bx-a)^4b} - \frac{1}{3(bx-a)^3b}}{c^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(-b*c*x+a*c)^6,x)

[Out] 1/c^6*(-1/(b*x-a)^4*a/b-1/3/(b*x-a)^3/b-4/5*a^2/b/(b*x-a)^5)

maxima [A] time = 1.39, size = 95, normalized size = 1.67

$$\frac{5b^2x^2 + 5abx + 2a^2}{15(b^6c^6x^5 - 5ab^5c^6x^4 + 10a^2b^4c^6x^3 - 10a^3b^3c^6x^2 + 5a^4b^2c^6x - a^5bc^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^6,x, algorithm="maxima")

[Out] $-1/15*(5*b^2*x^2 + 5*a*b*x + 2*a^2)/(b^6*c^6*x^5 - 5*a*b^5*c^6*x^4 + 10*a^2*b^4*c^6*x^3 - 10*a^3*b^3*c^6*x^2 + 5*a^4*b^2*c^6*x - a^5*b*c^6)$

mupad [B] time = 0.19, size = 91, normalized size = 1.60

$$\frac{\frac{ax}{3} + \frac{bx^2}{3} + \frac{2a^2}{15b}}{a^5c^6 - 5a^4bc^6x + 10a^3b^2c^6x^2 - 10a^2b^3c^6x^3 + 5ab^4c^6x^4 - b^5c^6x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(a*c - b*c*x)^6,x)

[Out] $((a*x)/3 + (b*x^2)/3 + (2*a^2)/(15*b))/(a^5*c^6 - b^5*c^6*x^5 + 5*a*b^4*c^6*x^4 + 10*a^3*b^2*c^6*x^2 - 10*a^2*b^3*c^6*x^3 - 5*a^4*b*c^6*x)$

sympy [B] time = 0.51, size = 100, normalized size = 1.75

$$\frac{-2a^2 - 5abx - 5b^2x^2}{-15a^5bc^6 + 75a^4b^2c^6x - 150a^3b^3c^6x^2 + 150a^2b^4c^6x^3 - 75ab^5c^6x^4 + 15b^6c^6x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(-b*c*x+a*c)**6,x)

[Out] $(-2*a**2 - 5*a*b*x - 5*b**2*x**2)/(-15*a**5*b*c**6 + 75*a**4*b**2*c**6*x - 150*a**3*b**3*c**6*x**2 + 150*a**2*b**4*c**6*x**3 - 75*a*b**5*c**6*x**4 + 15*b**6*c**6*x**5)$

$$3.1048 \quad \int \frac{(a+bx)^2}{(ac-bcx)^7} dx$$

Optimal. Leaf size=59

$$\frac{2a^2}{3bc^7(a-bx)^6} - \frac{4a}{5bc^7(a-bx)^5} + \frac{1}{4bc^7(a-bx)^4}$$

[Out] $2/3*a^2/b/c^7/(-b*x+a)^6-4/5*a/b/c^7/(-b*x+a)^5+1/4/b/c^7/(-b*x+a)^4$

Rubi [A] time = 0.03, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$\frac{2a^2}{3bc^7(a-bx)^6} - \frac{4a}{5bc^7(a-bx)^5} + \frac{1}{4bc^7(a-bx)^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(a*c - b*c*x)^7,x]

[Out] $(2*a^2)/(3*b*c^7*(a - b*x)^6) - (4*a)/(5*b*c^7*(a - b*x)^5) + 1/(4*b*c^7*(a - b*x)^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(ac-bcx)^7} dx &= \int \left(\frac{4a^2}{c^7(a-bx)^7} - \frac{4a}{c^7(a-bx)^6} + \frac{1}{c^7(a-bx)^5} \right) dx \\ &= \frac{2a^2}{3bc^7(a-bx)^6} - \frac{4a}{5bc^7(a-bx)^5} + \frac{1}{4bc^7(a-bx)^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 37, normalized size = 0.63

$$\frac{7a^2 + 18abx + 15b^2x^2}{60bc^7(a-bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(a*c - b*c*x)^7,x]

[Out] (7*a^2 + 18*a*b*x + 15*b^2*x^2)/(60*b*c^7*(a - b*x)^6)

fricas [A] time = 0.44, size = 108, normalized size = 1.83

$$\frac{15 b^2 x^2 + 18 a b x + 7 a^2}{60 (b^7 c^7 x^6 - 6 a b^6 c^7 x^5 + 15 a^2 b^5 c^7 x^4 - 20 a^3 b^4 c^7 x^3 + 15 a^4 b^3 c^7 x^2 - 6 a^5 b^2 c^7 x + a^6 b c^7)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^7,x, algorithm="fricas")

[Out] 1/60*(15*b^2*x^2 + 18*a*b*x + 7*a^2)/(b^7*c^7*x^6 - 6*a*b^6*c^7*x^5 + 15*a^2*b^5*c^7*x^4 - 20*a^3*b^4*c^7*x^3 + 15*a^4*b^3*c^7*x^2 - 6*a^5*b^2*c^7*x + a^6*b*c^7)

giac [A] time = 0.93, size = 36, normalized size = 0.61

$$\frac{15 b^2 x^2 + 18 a b x + 7 a^2}{60 (b x - a)^6 b c^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^7,x, algorithm="giac")

[Out] 1/60*(15*b^2*x^2 + 18*a*b*x + 7*a^2)/((b*x - a)^6*b*c^7)

maple [A] time = 0.01, size = 52, normalized size = 0.88

$$\frac{\frac{2a^2}{3(bx-a)^6b} + \frac{4a}{5(bx-a)^5b} + \frac{1}{4(bx-a)^4b}}{c^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(-b*c*x+a*c)^7,x)

[Out] 1/c^7*(1/4/(b*x-a)^4/b+2/3*a^2/b/(b*x-a)^6+4/5/(b*x-a)^5*a/b)

maxima [A] time = 1.42, size = 108, normalized size = 1.83

$$\frac{15 b^2 x^2 + 18 a b x + 7 a^2}{60 (b^7 c^7 x^6 - 6 a b^6 c^7 x^5 + 15 a^2 b^5 c^7 x^4 - 20 a^3 b^4 c^7 x^3 + 15 a^4 b^3 c^7 x^2 - 6 a^5 b^2 c^7 x + a^6 b c^7)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(-b*c*x+a*c)^7,x, algorithm="maxima")

[Out] 1/60*(15*b^2*x^2 + 18*a*b*x + 7*a^2)/(b^7*c^7*x^6 - 6*a*b^6*c^7*x^5 + 15*a^2*b^5*c^7*x^4 - 20*a^3*b^4*c^7*x^3 + 15*a^4*b^3*c^7*x^2 - 6*a^5*b^2*c^7*x + a^6*b*c^7)

mupad [B] time = 0.11, size = 104, normalized size = 1.76

$$\frac{\frac{3ax}{10} + \frac{bx^2}{4} + \frac{7a^2}{60b}}{a^6c^7 - 6a^5bc^7x + 15a^4b^2c^7x^2 - 20a^3b^3c^7x^3 + 15a^2b^4c^7x^4 - 6ab^5c^7x^5 + b^6c^7x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(a*c - b*c*x)^7,x)

[Out] ((3*a*x)/10 + (b*x^2)/4 + (7*a^2)/(60*b))/(a^6*c^7 + b^6*c^7*x^6 - 6*a*b^5*c^7*x^5 + 15*a^4*b^2*c^7*x^2 - 20*a^3*b^3*c^7*x^3 + 15*a^2*b^4*c^7*x^4 - 6*a^5*b*c^7*x)

sympy [B] time = 0.60, size = 117, normalized size = 1.98

$$\frac{-7a^2 - 18abx - 15b^2x^2}{60a^6bc^7 - 360a^5b^2c^7x + 900a^4b^3c^7x^2 - 1200a^3b^4c^7x^3 + 900a^2b^5c^7x^4 - 360ab^6c^7x^5 + 60b^7c^7x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(-b*c*x+a*c)**7,x)

[Out] -(-7*a**2 - 18*a*b*x - 15*b**2*x**2)/(60*a**6*b*c**7 - 360*a**5*b**2*c**7*x + 900*a**4*b**3*c**7*x**2 - 1200*a**3*b**4*c**7*x**3 + 900*a**2*b**5*c**7*x**4 - 360*a*b**6*c**7*x**5 + 60*b**7*c**7*x**6)

$$3.1049 \quad \int \frac{(ac-bcx)^3}{a+bx} dx$$

Optimal. Leaf size=61

$$\frac{8a^3c^3 \log(a+bx)}{b} - 4a^2c^3x + \frac{c^3(a-bx)^3}{3b} + \frac{ac^3(a-bx)^2}{b}$$

[Out] $-4*a^2*c^3*x+a*c^3*(-b*x+a)^2/b+1/3*c^3*(-b*x+a)^3/b+8*a^3*c^3*\ln(b*x+a)/b$

Rubi [A] time = 0.02, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$\frac{8a^3c^3 \log(a+bx)}{b} - 4a^2c^3x + \frac{c^3(a-bx)^3}{3b} + \frac{ac^3(a-bx)^2}{b}$$

Antiderivative was successfully verified.

[In] Int[(a*c - b*c*x)^3/(a + b*x), x]

[Out] $-4*a^2*c^3*x + (a*c^3*(a - b*x)^2)/b + (c^3*(a - b*x)^3)/(3*b) + (8*a^3*c^3*\text{Log}[a + b*x])/b$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(ac-bcx)^3}{a+bx} dx &= \int \left(-4a^2c^3 + \frac{8a^3c^3}{a+bx} - 2ac^2(ac-bcx) - c(ac-bcx)^2 \right) dx \\ &= -4a^2c^3x + \frac{ac^3(a-bx)^2}{b} + \frac{c^3(a-bx)^3}{3b} + \frac{8a^3c^3 \log(a+bx)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 42, normalized size = 0.69

$$c^3 \left(\frac{8a^3 \log(a+bx)}{b} - 7a^2x + 2abx^2 - \frac{b^2x^3}{3} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a*c - b*c*x)^3/(a + b*x),x]

[Out] $c^3*(-7*a^2*x + 2*a*b*x^2 - (b^2*x^3)/3 + (8*a^3*\text{Log}[a + b*x])/b)$

fricas [A] time = 0.45, size = 52, normalized size = 0.85

$$-\frac{b^3c^3x^3 - 6ab^2c^3x^2 + 21a^2bc^3x - 24a^3c^3 \log(bx + a)}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^3/(b*x+a),x, algorithm="fricas")

[Out] $-1/3*(b^3*c^3*x^3 - 6*a*b^2*c^3*x^2 + 21*a^2*b*c^3*x - 24*a^3*c^3*\log(b*x + a))/b$

giac [A] time = 1.15, size = 59, normalized size = 0.97

$$\frac{8a^3c^3 \log(|bx + a|)}{b} - \frac{b^5c^3x^3 - 6ab^4c^3x^2 + 21a^2b^3c^3x}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^3/(b*x+a),x, algorithm="giac")

[Out] $8*a^3*c^3*\log(\text{abs}(b*x + a))/b - 1/3*(b^5*c^3*x^3 - 6*a*b^4*c^3*x^2 + 21*a^2*b^3*c^3*x)/b^3$

maple [A] time = 0.00, size = 49, normalized size = 0.80

$$-\frac{b^2c^3x^3}{3} + 2abc^3x^2 + \frac{8a^3c^3 \ln(bx + a)}{b} - 7a^2c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*c*x+a*c)^3/(b*x+a),x)

[Out] $-1/3*c^3*b^2*x^3+2*c^3*b*x^2*a-7*a^2*c^3*x+8*a^3*c^3*\ln(b*x+a)/b$

maxima [A] time = 1.34, size = 48, normalized size = 0.79

$$-\frac{1}{3}b^2c^3x^3 + 2abc^3x^2 - 7a^2c^3x + \frac{8a^3c^3 \log(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^3/(b*x+a),x, algorithm="maxima")

[Out] $-1/3*b^2*c^3*x^3 + 2*a*b*c^3*x^2 - 7*a^2*c^3*x + 8*a^3*c^3*\log(b*x + a)/b$

mupad [B] time = 0.05, size = 48, normalized size = 0.79

$$\frac{8a^3c^3 \ln(ax+b)}{b} - \frac{b^2c^3x^3}{3} - 7a^2c^3x + 2abc^3x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c - b*c*x)^3/(a + b*x),x)

[Out] (8*a^3*c^3*log(a + b*x))/b - (b^2*c^3*x^3)/3 - 7*a^2*c^3*x + 2*a*b*c^3*x^2

sympy [A] time = 0.18, size = 49, normalized size = 0.80

$$\frac{8a^3c^3 \log(ax+b)}{b} - 7a^2c^3x + 2abc^3x^2 - \frac{b^2c^3x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)**3/(b*x+a),x)

[Out] 8*a**3*c**3*log(a + b*x)/b - 7*a**2*c**3*x + 2*a*b*c**3*x**2 - b**2*c**3*x**3/3

$$3.1050 \quad \int \frac{(ac-bcx)^2}{a+bx} dx$$

Optimal. Leaf size=43

$$\frac{4a^2c^2 \log(a+bx)}{b} + \frac{c^2(a-bx)^2}{2b} - 2ac^2x$$

[Out] $-2*a*c^2*x + 1/2*c^2*(-b*x+a)^2/b + 4*a^2*c^2*\ln(b*x+a)/b$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$\frac{4a^2c^2 \log(a+bx)}{b} + \frac{c^2(a-bx)^2}{2b} - 2ac^2x$$

Antiderivative was successfully verified.

[In] Int[(a*c - b*c*x)^2/(a + b*x), x]

[Out] $-2*a*c^2*x + (c^2*(a - b*x)^2)/(2*b) + (4*a^2*c^2*\text{Log}[a + b*x])/b$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{(ac-bcx)^2}{a+bx} dx &= \int \left(-2ac^2 + \frac{4a^2c^2}{a+bx} - c(ac-bcx) \right) dx \\ &= -2ac^2x + \frac{c^2(a-bx)^2}{2b} + \frac{4a^2c^2 \log(a+bx)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 0.72

$$c^2 \left(\frac{4a^2 \log(a+bx)}{b} - 3ax + \frac{bx^2}{2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a*c - b*c*x)^2/(a + b*x),x]

[Out] $c^2*(-3*a*x + (b*x^2)/2 + (4*a^2*\text{Log}[a + b*x])/b)$

fricas [A] time = 0.42, size = 38, normalized size = 0.88

$$\frac{b^2 c^2 x^2 - 6 a b c^2 x + 8 a^2 c^2 \log(bx + a)}{2 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^2/(b*x+a),x, algorithm="fricas")

[Out] $1/2*(b^2*c^2*x^2 - 6*a*b*c^2*x + 8*a^2*c^2*\log(b*x + a))/b$

giac [A] time = 0.87, size = 45, normalized size = 1.05

$$\frac{4 a^2 c^2 \log(|bx + a|)}{b} + \frac{b^3 c^2 x^2 - 6 a b^2 c^2 x}{2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^2/(b*x+a),x, algorithm="giac")

[Out] $4*a^2*c^2*\log(\text{abs}(b*x + a))/b + 1/2*(b^3*c^2*x^2 - 6*a*b^2*c^2*x)/b^2$

maple [A] time = 0.00, size = 35, normalized size = 0.81

$$\frac{b c^2 x^2}{2} + \frac{4 a^2 c^2 \ln(bx + a)}{b} - 3 a c^2 x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*c*x+a*c)^2/(b*x+a),x)

[Out] $1/2*c^2*x^2*b-3*a*c^2*x+4*a^2*c^2*\ln(b*x+a)/b$

maxima [A] time = 1.34, size = 34, normalized size = 0.79

$$\frac{1}{2} b c^2 x^2 - 3 a c^2 x + \frac{4 a^2 c^2 \log(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^2/(b*x+a),x, algorithm="maxima")

[Out] $1/2*b*c^2*x^2 - 3*a*c^2*x + 4*a^2*c^2*\log(b*x + a)/b$

mupad [B] time = 0.15, size = 32, normalized size = 0.74

$$\frac{c^2 (8a^2 \ln(a + bx) + b^2 x^2 - 6abx)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c - b*c*x)^2/(a + b*x),x)`

[Out] `(c^2*(8*a^2*log(a + b*x) + b^2*x^2 - 6*a*b*x))/(2*b)`

sympy [A] time = 0.15, size = 34, normalized size = 0.79

$$\frac{4a^2c^2 \log(a + bx)}{b} - 3ac^2x + \frac{bc^2x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*c*x+a*c)**2/(b*x+a),x)`

[Out] `4*a**2*c**2*log(a + b*x)/b - 3*a*c**2*x + b*c**2*x**2/2`

$$3.1051 \quad \int \frac{ac-bcx}{a+bx} dx$$

Optimal. Leaf size=18

$$\frac{2ac \log(a+bx)}{b} - cx$$

[Out] $-c*x+2*a*c*\ln(b*x+a)/b$

Rubi [A] time = 0.01, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{2ac \log(a+bx)}{b} - cx$$

Antiderivative was successfully verified.

[In] Int[(a*c - b*c*x)/(a + b*x), x]

[Out] $-(c*x) + (2*a*c*\text{Log}[a + b*x])/b$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int \frac{ac-bcx}{a+bx} dx &= \int \left(-c + \frac{2ac}{a+bx} \right) dx \\ &= -cx + \frac{2ac \log(a+bx)}{b} \end{aligned}$$

Mathematica [A] time = 0.00, size = 18, normalized size = 1.00

$$c \left(\frac{2a \log(a+bx)}{b} - x \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a*c - b*c*x)/(a + b*x), x]

[Out] $c*(-x + (2*a*\text{Log}[a + b*x]))/b$

fricas [A] time = 0.42, size = 20, normalized size = 1.11

$$-\frac{bcx - 2ac \log(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*c*x+a*c)/(b*x+a),x, algorithm="fricas")`

[Out] $-(b*c*x - 2*a*c*\log(b*x + a))/b$

giac [A] time = 1.01, size = 19, normalized size = 1.06

$$-cx + \frac{2ac \log(|bx + a|)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*c*x+a*c)/(b*x+a),x, algorithm="giac")`

[Out] $-c*x + 2*a*c*\log(\text{abs}(b*x + a))/b$

maple [A] time = 0.00, size = 19, normalized size = 1.06

$$\frac{2ac \ln(bx + a)}{b} - cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-b*c*x+a*c)/(b*x+a),x)`

[Out] $-c*x+2*a*c*\ln(b*x+a)/b$

maxima [A] time = 1.34, size = 18, normalized size = 1.00

$$-cx + \frac{2ac \log(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*c*x+a*c)/(b*x+a),x, algorithm="maxima")`

[Out] $-c*x + 2*a*c*\log(b*x + a)/b$

mupad [B] time = 0.04, size = 18, normalized size = 1.00

$$\frac{2ac \ln(a + bx)}{b} - cx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a*c - b*c*x)/(a + b*x),x)
```

```
[Out] (2*a*c*log(a + b*x))/b - c*x
```

```
sympy [A] time = 0.12, size = 15, normalized size = 0.83
```

$$\frac{2ac \log(a + bx)}{b} - cx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((-b*c*x+a*c)/(b*x+a),x)
```

```
[Out] 2*a*c*log(a + b*x)/b - c*x
```

$$3.1052 \quad \int \frac{1}{a+bx} dx$$

Optimal. Leaf size=10

$$\frac{\log(a+bx)}{b}$$

[Out] ln(b*x+a)/b

Rubi [A] time = 0.00, antiderivative size = 10, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {31}

$$\frac{\log(a+bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-1), x]

[Out] Log[a + b*x]/b

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \frac{1}{a+bx} dx = \frac{\log(a+bx)}{b}$$

Mathematica [A] time = 0.00, size = 10, normalized size = 1.00

$$\frac{\log(a+bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-1), x]

[Out] Log[a + b*x]/b

fricas [A] time = 0.44, size = 10, normalized size = 1.00

$$\frac{\log(bx+a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a),x, algorithm="fricas")

[Out] log(b*x + a)/b

giac [A] time = 1.06, size = 11, normalized size = 1.10

$$\frac{\log(|bx + a|)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a),x, algorithm="giac")

[Out] log(abs(b*x + a))/b

maple [A] time = 0.00, size = 11, normalized size = 1.10

$$\frac{\ln(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a),x)

[Out] 1/b*ln(b*x+a)

maxima [A] time = 1.33, size = 10, normalized size = 1.00

$$\frac{\log(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a),x, algorithm="maxima")

[Out] log(b*x + a)/b

mupad [B] time = 0.02, size = 10, normalized size = 1.00

$$\frac{\ln(a + bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x),x)

[Out] log(a + b*x)/b

sympy [A] time = 0.07, size = 7, normalized size = 0.70

$$\frac{\log(a + bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a),x)

[Out] log(a + b*x)/b

$$3.1053 \quad \int \frac{1}{(a+bx)(ac-bcx)} dx$$

Optimal. Leaf size=17

$$\frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{abc}$$

[Out] arctanh(b*x/a)/a/b/c

Rubi [A] time = 0.01, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {35, 208}

$$\frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{abc}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)*(a*c - b*c*x)),x]

[Out] ArcTanh[(b*x)/a]/(a*b*c)

Rule 35

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))), x_Symbol] := Int[1/(a*c + b*d*x^2), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)(ac-bcx)} dx &= \int \frac{1}{a^2c - b^2cx^2} dx \\ &= \frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{abc} \end{aligned}$$

Mathematica [A] time = 0.01, size = 17, normalized size = 1.00

$$\frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{abc}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*(a*c - b*c*x)),x]

[Out] ArcTanh[(b*x)/a]/(a*b*c)

fricas [A] time = 0.43, size = 28, normalized size = 1.65

$$\frac{\log(bx + a) - \log(bx - a)}{2abc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(-b*c*x+a*c),x, algorithm="fricas")

[Out] 1/2*(log(b*x + a) - log(b*x - a))/(a*b*c)

giac [B] time = 1.20, size = 39, normalized size = 2.29

$$\frac{\log(|bx + a|)}{2abc} - \frac{\log(|bx - a|)}{2abc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(-b*c*x+a*c),x, algorithm="giac")

[Out] 1/2*log(abs(b*x + a))/(a*b*c) - 1/2*log(abs(b*x - a))/(a*b*c)

maple [B] time = 0.01, size = 38, normalized size = 2.24

$$-\frac{\ln(bx - a)}{2abc} + \frac{\ln(bx + a)}{2abc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)/(-b*c*x+a*c),x)

[Out] 1/2/c/b/a*ln(b*x+a)-1/2/c/b/a*ln(b*x-a)

maxima [B] time = 1.40, size = 37, normalized size = 2.18

$$\frac{\log(bx + a)}{2abc} - \frac{\log(bx - a)}{2abc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(-b*c*x+a*c),x, algorithm="maxima")

[Out] 1/2*log(b*x + a)/(a*b*c) - 1/2*log(b*x - a)/(a*b*c)

mupad [B] time = 0.17, size = 17, normalized size = 1.00

$$\frac{\operatorname{atanh}\left(\frac{bx}{a}\right)}{abc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a*c - b*c*x)*(a + b*x)),x)`

[Out] `atanh((b*x)/a)/(a*b*c)`

sympy [B] time = 0.17, size = 22, normalized size = 1.29

$$-\frac{\frac{\log\left(-\frac{a}{b}+x\right)}{2} - \frac{\log\left(\frac{a}{b}+x\right)}{2}}{abc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/(-b*c*x+a*c),x)`

[Out] `-(log(-a/b + x)/2 - log(a/b + x)/2)/(a*b*c)`

$$3.1054 \quad \int \frac{1}{(a+bx)(ac-bcx)^2} dx$$

Optimal. Leaf size=42

$$\frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{2a^2bc^2} + \frac{1}{2abc^2(a-bx)}$$

[Out] 1/2/a/b/c^2/(-b*x+a)+1/2*arctanh(b*x/a)/a^2/b/c^2

Rubi [A] time = 0.03, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {44, 208}

$$\frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{2a^2bc^2} + \frac{1}{2abc^2(a-bx)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)*(a*c - b*c*x)^2),x]

[Out] 1/(2*a*b*c^2*(a - b*x)) + ArcTanh[(b*x)/a]/(2*a^2*b*c^2)

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)(ac-bcx)^2} dx &= \int \left(\frac{1}{2ac^2(a-bx)^2} + \frac{1}{2ac^2(a^2-b^2x^2)} \right) dx \\ &= \frac{1}{2abc^2(a-bx)} + \frac{\int \frac{1}{a^2-b^2x^2} dx}{2ac^2} \\ &= \frac{1}{2abc^2(a-bx)} + \frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{2a^2bc^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 53, normalized size = 1.26

$$\frac{(bx-a)\log(a-bx) + (a-bx)\log(a+bx) + 2a}{4a^2bc^2(a-bx)}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*(a*c - b*c*x)^2), x]

[Out] (2*a + (-a + b*x)*Log[a - b*x] + (a - b*x)*Log[a + b*x])/(4*a^2*b*c^2*(a - b*x))

fricas [A] time = 0.41, size = 60, normalized size = 1.43

$$\frac{(bx-a)\log(bx+a) - (bx-a)\log(bx-a) - 2a}{4(a^2b^2c^2x - a^3bc^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(-b*c*x+a*c)^2,x, algorithm="fricas")

[Out] 1/4*((b*x - a)*log(b*x + a) - (b*x - a)*log(b*x - a) - 2*a)/(a^2*b^2*c^2*x - a^3*b*c^2)

giac [A] time = 1.03, size = 53, normalized size = 1.26

$$-\frac{1}{2(bcx-ac)abc} + \frac{\log\left(\left|-\frac{2ac}{bcx-ac} - 1\right|\right)}{4a^2bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(-b*c*x+a*c)^2,x, algorithm="giac")

[Out] $-1/2/((b*c*x - a*c)*a*b*c) + 1/4*\log(\text{abs}(-2*a*c/(b*c*x - a*c) - 1))/(a^2*b*c^2)$

maple [A] time = 0.01, size = 58, normalized size = 1.38

$$-\frac{1}{2(bx-a)abc^2} - \frac{\ln(bx-a)}{4a^2bc^2} + \frac{\ln(bx+a)}{4a^2bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)/(-b*c*x+a*c)^2,x)`

[Out] $1/4/c^2/a^2/b*\ln(b*x+a)-1/4/c^2/a^2/b*\ln(b*x-a)-1/2/c^2/b/a/(b*x-a)$

maxima [A] time = 1.26, size = 60, normalized size = 1.43

$$-\frac{1}{2(ab^2c^2x - a^2bc^2)} + \frac{\log(bx+a)}{4a^2bc^2} - \frac{\log(bx-a)}{4a^2bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/(-b*c*x+a*c)^2,x, algorithm="maxima")`

[Out] $-1/2/(a*b^2*c^2*x - a^2*b*c^2) + 1/4*\log(b*x + a)/(a^2*b*c^2) - 1/4*\log(b*x - a)/(a^2*b*c^2)$

mupad [B] time = 0.07, size = 42, normalized size = 1.00

$$\frac{1}{2ab(ac^2 - bc^2x)} + \frac{\operatorname{atanh}\left(\frac{bx}{a}\right)}{2a^2bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a*c - b*c*x)^2*(a + b*x)),x)`

[Out] $1/(2*a*b*(a*c^2 - b*c^2*x)) + \operatorname{atanh}((b*x)/a)/(2*a^2*b*c^2)$

sympy [A] time = 0.28, size = 48, normalized size = 1.14

$$-\frac{1}{-2a^2bc^2 + 2ab^2c^2x} + \frac{-\frac{\log(-\frac{a}{b}+x)}{4} + \frac{\log(\frac{a}{b}+x)}{4}}{a^2bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/(-b*c*x+a*c)**2,x)`

[Out] $-1/(-2*a**2*b*c**2 + 2*a*b**2*c**2*x) + (-\log(-a/b + x)/4 + \log(a/b + x)/4)/(a**2*b*c**2)$

$$3.1055 \quad \int \frac{1}{(a+bx)(ac-bcx)^3} dx$$

Optimal. Leaf size=63

$$\frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{4a^3bc^3} + \frac{1}{4a^2bc^3(a-bx)} + \frac{1}{4abc^3(a-bx)^2}$$

[Out] $1/4/a/b/c^3/(-b*x+a)^2+1/4/a^2/b/c^3/(-b*x+a)+1/4*\operatorname{arctanh}(b*x/a)/a^3/b/c^3$

Rubi [A] time = 0.04, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {44, 208}

$$\frac{1}{4a^2bc^3(a-bx)} + \frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{4a^3bc^3} + \frac{1}{4abc^3(a-bx)^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)*(a*c - b*c*x)^3), x]

[Out] $1/(4*a*b*c^3*(a - b*x)^2) + 1/(4*a^2*b*c^3*(a - b*x)) + \operatorname{ArcTanh}[(b*x)/a]/(4*a^3*b*c^3)$

Rule 44

Int[((a_) + (b_)*(x_)^(m_))*((c_) + (d_)*(x_)^(n_)), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] :> Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)(ac-bcx)^3} dx &= \int \left(\frac{1}{2ac^3(a-bx)^3} + \frac{1}{4a^2c^3(a-bx)^2} + \frac{1}{4a^2c^3(a^2-b^2x^2)} \right) dx \\ &= \frac{1}{4abc^3(a-bx)^2} + \frac{1}{4a^2bc^3(a-bx)} + \frac{\int \frac{1}{a^2-b^2x^2} dx}{4a^2c^3} \\ &= \frac{1}{4abc^3(a-bx)^2} + \frac{1}{4a^2bc^3(a-bx)} + \frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{4a^3bc^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 65, normalized size = 1.03

$$\frac{2a(2a-bx) + (a-bx)^2(-\log(a-bx)) + (a-bx)^2 \log(a+bx)}{8a^3bc^3(a-bx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a+b*x)*(a*c-b*c*x)^3),x]

[Out] (2*a*(2*a-b*x) - (a-b*x)^2*Log[a-b*x] + (a-b*x)^2*Log[a+b*x])/(8*a^3*b*c^3*(a-b*x)^2)

fricas [A] time = 0.43, size = 98, normalized size = 1.56

$$\frac{2abx - 4a^2 - (b^2x^2 - 2abx + a^2) \log(bx+a) + (b^2x^2 - 2abx + a^2) \log(bx-a)}{8(a^3b^3c^3x^2 - 2a^4b^2c^3x + a^5bc^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(-b*c*x+a*c)^3,x, algorithm="fricas")

[Out] -1/8*(2*a*b*x - 4*a^2 - (b^2*x^2 - 2*a*b*x + a^2)*log(b*x + a) + (b^2*x^2 - 2*a*b*x + a^2)*log(b*x - a))/(a^3*b^3*c^3*x^2 - 2*a^4*b^2*c^3*x + a^5*b*c^3)

giac [A] time = 0.87, size = 69, normalized size = 1.10

$$\frac{\log(|bx+a|)}{8a^3bc^3} - \frac{\log(|bx-a|)}{8a^3bc^3} - \frac{abx - 2a^2}{4(bx-a)^2a^3bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(-b*c*x+a*c)^3,x, algorithm="giac")

[Out] $\frac{1}{8} \log(\text{abs}(b*x + a))/(a^3*b*c^3) - \frac{1}{8} \log(\text{abs}(b*x - a))/(a^3*b*c^3) - \frac{1}{4} * (a*b*x - 2*a^2)/(b*x - a)^2*a^3*b*c^3$

maple [A] time = 0.01, size = 78, normalized size = 1.24

$$\frac{1}{4(bx - a)^2 ab c^3} - \frac{1}{4(bx - a) a^2 b c^3} - \frac{\ln(bx - a)}{8a^3 b c^3} + \frac{\ln(bx + a)}{8a^3 b c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)/(-b*c*x+a*c)^3,x)`

[Out] $\frac{1}{8/c^3/a^3/b*\ln(b*x+a)} - \frac{1}{8/c^3/a^3/b*\ln(b*x-a)} - \frac{1}{4/c^3/a^2/b/(b*x-a)} + \frac{1}{4/c^3/b/a/(b*x-a)^2}$

maxima [A] time = 1.35, size = 82, normalized size = 1.30

$$-\frac{bx - 2a}{4(a^2 b^3 c^3 x^2 - 2 a^3 b^2 c^3 x + a^4 b c^3)} + \frac{\log(bx + a)}{8 a^3 b c^3} - \frac{\log(bx - a)}{8 a^3 b c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/(-b*c*x+a*c)^3,x, algorithm="maxima")`

[Out] $-\frac{1}{4} * (b*x - 2*a)/(a^2*b^3*c^3*x^2 - 2*a^3*b^2*c^3*x + a^4*b*c^3) + \frac{1}{8} * \log(b*x + a)/(a^3*b*c^3) - \frac{1}{8} * \log(b*x - a)/(a^3*b*c^3)$

mupad [B] time = 0.08, size = 64, normalized size = 1.02

$$\frac{\operatorname{atanh}\left(\frac{bx}{a}\right)}{4 a^3 b c^3} - \frac{\frac{x}{4 a^2} - \frac{1}{2 a b}}{a^2 c^3 - 2 a b c^3 x + b^2 c^3 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a*c - b*c*x)^3*(a + b*x)),x)`

[Out] $\operatorname{atanh}((b*x)/a)/(4*a^3*b*c^3) - (x/(4*a^2) - 1/(2*a*b))/(a^2*c^3 + b^2*c^3*x^2 - 2*a*b*c^3*x)$

sympy [A] time = 0.38, size = 71, normalized size = 1.13

$$-\frac{-2a + bx}{4a^4bc^3 - 8a^3b^2c^3x + 4a^2b^3c^3x^2} - \frac{\log\left(-\frac{a}{b}+x\right)}{8} - \frac{\log\left(\frac{a}{b}+x\right)}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)/(-b*c*x+a*c)**3,x)
```

```
[Out] -(-2*a + b*x)/(4*a**4*b*c**3 - 8*a**3*b**2*c**3*x + 4*a**2*b**3*c**3*x**2)  
- (log(-a/b + x)/8 - log(a/b + x)/8)/(a**3*b*c**3)
```


$$3.1056 \quad \int \frac{(ac-bcx)^3}{(a+bx)^2} dx$$

Optimal. Leaf size=54

$$-\frac{8a^3c^3}{b(a+bx)} - \frac{12a^2c^3 \log(a+bx)}{b} + 5ac^3x - \frac{1}{2}bc^3x^2$$

[Out] $5*a*c^3*x - 1/2*b*c^3*x^2 - 8*a^3*c^3/b/(b*x+a) - 12*a^2*c^3*\ln(b*x+a)/b$

Rubi [A] time = 0.03, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$-\frac{8a^3c^3}{b(a+bx)} - \frac{12a^2c^3 \log(a+bx)}{b} + 5ac^3x - \frac{1}{2}bc^3x^2$$

Antiderivative was successfully verified.

[In] Int[(a*c - b*c*x)^3/(a + b*x)^2,x]

[Out] $5*a*c^3*x - (b*c^3*x^2)/2 - (8*a^3*c^3)/(b*(a + b*x)) - (12*a^2*c^3*\text{Log}[a + b*x])/b$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(ac-bcx)^3}{(a+bx)^2} dx &= \int \left(5ac^3 - bc^3x + \frac{8a^3c^3}{(a+bx)^2} - \frac{12a^2c^3}{a+bx} \right) dx \\ &= 5ac^3x - \frac{1}{2}bc^3x^2 - \frac{8a^3c^3}{b(a+bx)} - \frac{12a^2c^3 \log(a+bx)}{b} \end{aligned}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.85

$$c^3 \left(-\frac{8a^3}{b(a+bx)} - \frac{12a^2 \log(a+bx)}{b} + 5ax - \frac{bx^2}{2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a*c - b*c*x)^3/(a + b*x)^2,x]

[Out] $c^3*(5*a*x - (b*x^2)/2 - (8*a^3)/(b*(a + b*x)) - (12*a^2*\text{Log}[a + b*x])/b)$

fricas [A] time = 0.43, size = 79, normalized size = 1.46

$$\frac{b^3 c^3 x^3 - 9 a b^2 c^3 x^2 - 10 a^2 b c^3 x + 16 a^3 c^3 + 24 (a^2 b c^3 x + a^3 c^3) \log (b x + a)}{2 (b^2 x + a b)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^3/(b*x+a)^2,x, algorithm="fricas")

[Out] $-1/2*(b^3*c^3*x^3 - 9*a*b^2*c^3*x^2 - 10*a^2*b*c^3*x + 16*a^3*c^3 + 24*(a^2*b*c^3*x + a^3*c^3)*\log(b*x + a))/(b^2*x + a*b)$

giac [A] time = 1.12, size = 80, normalized size = 1.48

$$\frac{12 a^2 c^3 \log \left(\frac{|b x+a|}{(b x+a)^2|b|} \right)}{b} - \frac{8 a^3 c^3}{(b x+a) b} + \frac{\left(\frac{12 a c^3}{b x+a} - c^3 \right) (b x+a)^2}{2 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^3/(b*x+a)^2,x, algorithm="giac")

[Out] $12*a^2*c^3*\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b)))/b - 8*a^3*c^3/((b*x + a)*b) + 1/2*(12*a*c^3/(b*x + a) - c^3)*(b*x + a)^2/b$

maple [A] time = 0.01, size = 53, normalized size = 0.98

$$-\frac{b c^3 x^2}{2} - \frac{8 a^3 c^3}{(b x+a) b} - \frac{12 a^2 c^3 \ln (b x+a)}{b} + 5 a c^3 x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*c*x+a*c)^3/(b*x+a)^2,x)

[Out] $5*a*c^3*x - 1/2*b*c^3*x^2 - 8*a^3*c^3/b/(b*x+a) - 12*a^2*c^3*\ln(b*x+a)/b$

maxima [A] time = 1.29, size = 53, normalized size = 0.98

$$-\frac{1}{2} b c^3 x^2 - \frac{8 a^3 c^3}{b^2 x + a b} + 5 a c^3 x - \frac{12 a^2 c^3 \log (b x + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^3/(b*x+a)^2,x, algorithm="maxima")

[Out] $-1/2*b*c^3*x^2 - 8*a^3*c^3/(b^2*x + a*b) + 5*a*c^3*x - 12*a^2*c^3*\log(b*x + a)/b$

mupad [B] time = 0.05, size = 52, normalized size = 0.96

$$5ac^3x - \frac{bc^3x^2}{2} - \frac{12a^2c^3 \ln(ax+b)}{b} - \frac{8a^3c^3}{b(ax+b)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c - b*c*x)^3/(a + b*x)^2,x)

[Out] $5*a*c^3*x - (b*c^3*x^2)/2 - (12*a^2*c^3*\log(a + b*x))/b - (8*a^3*c^3)/(b*(a + b*x))$

sympy [A] time = 0.25, size = 51, normalized size = 0.94

$$-\frac{8a^3c^3}{ab+b^2x} - \frac{12a^2c^3 \log(ax+b)}{b} + 5ac^3x - \frac{bc^3x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)**3/(b*x+a)**2,x)

[Out] $-8*a**3*c**3/(a*b + b**2*x) - 12*a**2*c**3*\log(a + b*x)/b + 5*a*c**3*x - b*c**3*x**2/2$

$$3.1057 \quad \int \frac{(ac-bcx)^2}{(a+bx)^2} dx$$

Optimal. Leaf size=39

$$-\frac{4a^2c^2}{b(a+bx)} - \frac{4ac^2 \log(a+bx)}{b} + c^2x$$

[Out] $c^2x - 4a^2c^2/b/(b*x+a) - 4a*c^2*\ln(b*x+a)/b$

Rubi [A] time = 0.02, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$-\frac{4a^2c^2}{b(a+bx)} - \frac{4ac^2 \log(a+bx)}{b} + c^2x$$

Antiderivative was successfully verified.

[In] Int[(a*c - b*c*x)^2/(a + b*x)^2, x]

[Out] $c^2x - (4a^2c^2)/(b*(a + b*x)) - (4a*c^2*\text{Log}[a + b*x])/b$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(ac-bcx)^2}{(a+bx)^2} dx &= \int \left(c^2 + \frac{4a^2c^2}{(a+bx)^2} - \frac{4ac^2}{a+bx} \right) dx \\ &= c^2x - \frac{4a^2c^2}{b(a+bx)} - \frac{4ac^2 \log(a+bx)}{b} \end{aligned}$$

Mathematica [A] time = 0.02, size = 33, normalized size = 0.85

$$c^2 \left(-\frac{4a^2}{b(a+bx)} - \frac{4a \log(a+bx)}{b} + x \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a*c - b*c*x)^2/(a + b*x)^2,x]

[Out] $c^2*(x - (4*a^2)/(b*(a + b*x)) - (4*a*\text{Log}[a + b*x])/b)$

fricas [A] time = 0.46, size = 61, normalized size = 1.56

$$\frac{b^2c^2x^2 + abc^2x - 4a^2c^2 - 4(abc^2x + a^2c^2)\log(bx + a)}{b^2x + ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^2/(b*x+a)^2,x, algorithm="fricas")

[Out] $(b^2*c^2*x^2 + a*b*c^2*x - 4*a^2*c^2 - 4*(a*b*c^2*x + a^2*c^2)*\log(b*x + a))/(b^2*x + a*b)$

giac [A] time = 1.18, size = 59, normalized size = 1.51

$$\frac{4ac^2 \log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b} + \frac{(bx+a)c^2}{b} - \frac{4a^2c^2}{(bx+a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^2/(b*x+a)^2,x, algorithm="giac")

[Out] $4*a*c^2*\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b)))/b + (b*x + a)*c^2/b - 4*a^2*c^2/((b*x + a)*b)$

maple [A] time = 0.01, size = 40, normalized size = 1.03

$$-\frac{4a^2c^2}{(bx+a)b} - \frac{4ac^2 \ln(bx+a)}{b} + c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*c*x+a*c)^2/(b*x+a)^2,x)

[Out] $c^2*x - 4*a^2*c^2/b/(b*x+a) - 4*a*c^2*\ln(b*x+a)/b$

maxima [A] time = 1.36, size = 40, normalized size = 1.03

$$-\frac{4a^2c^2}{b^2x + ab} + c^2x - \frac{4ac^2 \log(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^2/(b*x+a)^2,x, algorithm="maxima")

[Out] $-4a^2c^2/(b^2x + a*b) + c^2x - 4ac^2\log(bx + a)/b$

mupad [B] time = 0.17, size = 39, normalized size = 1.00

$$c^2x - \frac{4ac^2 \ln(a + bx)}{b} - \frac{4a^2c^2}{b(a + bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c - b*c*x)^2/(a + b*x)^2,x)`

[Out] $c^2x - (4ac^2\log(a + bx))/b - (4a^2c^2)/(b(a + b*x))$

sympy [A] time = 0.19, size = 36, normalized size = 0.92

$$-\frac{4a^2c^2}{ab + b^2x} - \frac{4ac^2 \log(a + bx)}{b} + c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*c*x+a*c)**2/(b*x+a)**2,x)`

[Out] $-4a^2c^2/(a*b + b^2*x) - 4ac^2\log(a + b*x)/b + c^2*x$

$$3.1058 \quad \int \frac{ac-bcx}{(a+bx)^2} dx$$

Optimal. Leaf size=27

$$-\frac{2ac}{b(a+bx)} - \frac{c \log(a+bx)}{b}$$

[Out] $-2*a*c/b/(b*x+a)-c*\ln(b*x+a)/b$

Rubi [A] time = 0.01, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{2ac}{b(a+bx)} - \frac{c \log(a+bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[(a*c - b*c*x)/(a + b*x)^2,x]

[Out] $(-2*a*c)/(b*(a + b*x)) - (c*\text{Log}[a + b*x])/b$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{ac-bcx}{(a+bx)^2} dx &= \int \left(\frac{2ac}{(a+bx)^2} - \frac{c}{a+bx} \right) dx \\ &= -\frac{2ac}{b(a+bx)} - \frac{c \log(a+bx)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.85

$$-\frac{c \left(\frac{2a}{a+bx} + \log(a+bx) \right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[(a*c - b*c*x)/(a + b*x)^2,x]

[Out] $-\left(\frac{c \cdot (2a)}{a + bx} + \text{Log}[a + bx]\right)/b$

fricas [A] time = 0.41, size = 33, normalized size = 1.22

$$-\frac{2ac + (bcx + ac) \log(bx + a)}{b^2x + ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*c*x+a*c)/(b*x+a)^2,x, algorithm="fricas")`

[Out] $-(2a*c + (b*c*x + a*c)*\log(b*x + a))/(b^2*x + a*b)$

giac [A] time = 1.02, size = 54, normalized size = 2.00

$$c \left(\frac{\log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b} - \frac{a}{(bx+a)b} \right) - \frac{ac}{(bx+a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*c*x+a*c)/(b*x+a)^2,x, algorithm="giac")`

[Out] $c * (\log(\text{abs}(bx + a) / ((bx + a)^2 * \text{abs}(b)))) / b - a / ((bx + a) * b) - a * c / ((bx + a) * b)$

maple [A] time = 0.00, size = 28, normalized size = 1.04

$$-\frac{2ac}{(bx+a)b} - \frac{c \ln(bx+a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-b*c*x+a*c)/(b*x+a)^2,x)`

[Out] $-2*a*c/b/(b*x+a) - c*\ln(b*x+a)/b$

maxima [A] time = 1.34, size = 28, normalized size = 1.04

$$-\frac{2ac}{b^2x + ab} - \frac{c \log(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-b*c*x+a*c)/(b*x+a)^2,x, algorithm="maxima")`

[Out] $-2*a*c/(b^2*x + a*b) - c*\log(b*x + a)/b$

mupad [B] time = 0.04, size = 27, normalized size = 1.00

$$-\frac{c \ln(a + bx)}{b} - \frac{2ac}{b(a + bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c - b*c*x)/(a + b*x)^2,x)

[Out] - (c*log(a + b*x))/b - (2*a*c)/(b*(a + b*x))

sympy [A] time = 0.17, size = 24, normalized size = 0.89

$$-\frac{2ac}{ab + b^2x} - \frac{c \log(a + bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)/(b*x+a)**2,x)

[Out] -2*a*c/(a*b + b**2*x) - c*log(a + b*x)/b

$$3.1059 \quad \int \frac{1}{(a+bx)^2} dx$$

Optimal. Leaf size=12

$$-\frac{1}{b(a+bx)}$$

[Out] -1/b/(b*x+a)

Rubi [A] time = 0.00, antiderivative size = 12, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$-\frac{1}{b(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-2), x]

[Out] -(1/(b*(a + b*x)))

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^2} dx = -\frac{1}{b(a+bx)}$$

Mathematica [A] time = 0.00, size = 12, normalized size = 1.00

$$-\frac{1}{b(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-2), x]

[Out] -(1/(b*(a + b*x)))

fricas [A] time = 0.41, size = 13, normalized size = 1.08

$$-\frac{1}{b^2x+ab}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2,x, algorithm="fricas")

[Out] -1/(b^2*x + a*b)

giac [A] time = 1.11, size = 12, normalized size = 1.00

$$-\frac{1}{(bx + a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2,x, algorithm="giac")

[Out] -1/((b*x + a)*b)

maple [A] time = 0.00, size = 13, normalized size = 1.08

$$-\frac{1}{(bx + a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2,x)

[Out] -1/(b*x+a)/b

maxima [A] time = 1.37, size = 12, normalized size = 1.00

$$-\frac{1}{(bx + a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2,x, algorithm="maxima")

[Out] -1/((b*x + a)*b)

mupad [B] time = 0.02, size = 12, normalized size = 1.00

$$-\frac{1}{b(a + bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a + b*x)^2,x)

[Out] -1/(b*(a + b*x))

sympy [A] time = 0.14, size = 10, normalized size = 0.83

$$-\frac{1}{ab + b^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2,x)

[Out] -1/(a*b + b**2*x)

$$3.1060 \quad \int \frac{1}{(a+bx)^2(ac-bcx)} dx$$

Optimal. Leaf size=41

$$\frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{2a^2bc} - \frac{1}{2abc(a+bx)}$$

[Out] -1/2/a/b/c/(b*x+a)+1/2*arctanh(b*x/a)/a^2/b/c

Rubi [A] time = 0.03, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {44, 208}

$$\frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{2a^2bc} - \frac{1}{2abc(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^2*(a*c - b*c*x)),x]

[Out] -1/(2*a*b*c*(a + b*x)) + ArcTanh[(b*x)/a]/(2*a^2*b*c)

Rule 44

Int[((a_) + (b_)*(x_)^(m_))*((c_) + (d_)*(x_)^(n_)), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] & & ILtQ[m, 0] & & IntegerQ[n] & & !(IGtQ[n, 0] & & LtQ[m + n + 2, 0])

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] & & NegQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^2(ac-bcx)} dx &= \int \left(\frac{1}{2ac(a+bx)^2} + \frac{1}{2ac(a^2-b^2x^2)} \right) dx \\ &= -\frac{1}{2abc(a+bx)} + \frac{\int \frac{1}{a^2-b^2x^2} dx}{2ac} \\ &= -\frac{1}{2abc(a+bx)} + \frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{2a^2bc} \end{aligned}$$

Mathematica [A] time = 0.02, size = 50, normalized size = 1.22

$$\frac{-(a+bx)\log(a-bx) + (a+bx)\log(a+bx) - 2a}{4a^2bc(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*(a*c - b*c*x)), x]

[Out] (-2*a - (a + b*x)*Log[a - b*x] + (a + b*x)*Log[a + b*x])/(4*a^2*b*c*(a + b*x))

fricas [A] time = 0.44, size = 51, normalized size = 1.24

$$\frac{(bx+a)\log(bx+a) - (bx+a)\log(bx-a) - 2a}{4(a^2b^2cx + a^3bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(-b*c*x+a*c), x, algorithm="fricas")

[Out] 1/4*((b*x + a)*log(b*x + a) - (b*x + a)*log(b*x - a) - 2*a)/(a^2*b^2*c*x + a^3*b*c)

giac [A] time = 0.95, size = 44, normalized size = 1.07

$$-\frac{\log\left(\left|-\frac{2a}{bx+a} + 1\right|\right)}{4a^2bc} - \frac{1}{2(bx+a)abc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(-b*c*x+a*c), x, algorithm="giac")

[Out] -1/4*log(abs(-2*a/(b*x + a) + 1))/(a^2*b*c) - 1/2/((b*x + a)*a*b*c)

maple [A] time = 0.01, size = 56, normalized size = 1.37

$$-\frac{1}{2(bx+a)abc} - \frac{\ln(bx-a)}{4a^2bc} + \frac{\ln(bx+a)}{4a^2bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/(-b*c*x+a*c),x)

[Out] 1/4/c/a^2/b*ln(b*x+a)-1/2/a/b/c/(b*x+a)-1/4/c/a^2/b*ln(b*x-a)

maxima [A] time = 1.38, size = 55, normalized size = 1.34

$$-\frac{1}{2(ab^2cx+a^2bc)} + \frac{\log(bx+a)}{4a^2bc} - \frac{\log(bx-a)}{4a^2bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(-b*c*x+a*c),x, algorithm="maxima")

[Out] -1/2/(a*b^2*c*x + a^2*b*c) + 1/4*log(b*x + a)/(a^2*b*c) - 1/4*log(b*x - a)/(a^2*b*c)

mupad [B] time = 0.18, size = 37, normalized size = 0.90

$$\frac{\operatorname{atanh}\left(\frac{bx}{a}\right)}{2a^2bc} - \frac{1}{2ab(ac+bcx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a*c - b*c*x)*(a + b*x)^2),x)

[Out] atanh((b*x)/a)/(2*a^2*b*c) - 1/(2*a*b*(a*c + b*c*x))

sympy [A] time = 0.28, size = 44, normalized size = 1.07

$$-\frac{1}{2a^2bc + 2ab^2cx} - \frac{\frac{\log(-\frac{a}{b}+x)}{4}}{a^2bc} - \frac{\log(\frac{a}{b}+x)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2/(-b*c*x+a*c),x)

[Out] -1/(2*a**2*b*c + 2*a*b**2*c*x) - (log(-a/b + x)/4 - log(a/b + x)/4)/(a**2*b*c)

$$3.1061 \quad \int \frac{1}{(a+bx)^2(ac-bcx)^2} dx$$

Optimal. Leaf size=46

$$\frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{2a^3bc^2} + \frac{x}{2a^2c^2(a^2 - b^2x^2)}$$

[Out] 1/2*x/a^2/c^2/(-b^2*x^2+a^2)+1/2*arctanh(b*x/a)/a^3/b/c^2

Rubi [A] time = 0.02, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {41, 199, 208}

$$\frac{x}{2a^2c^2(a^2 - b^2x^2)} + \frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{2a^3bc^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^2*(a*c - b*c*x)^2), x]

[Out] x/(2*a^2*c^2*(a^2 - b^2*x^2)) + ArcTanh[(b*x)/a]/(2*a^3*b*c^2)

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 199

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := -Simp[(x*(a + b*x^n)^(p + 1))/(a*n*(p + 1)), x] + Dist[(n*(p + 1) + 1)/(a*n*(p + 1)), Int[(a + b*x^n)^(p + 1), x], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[p, -1] && (IntegerQ[2*p] || (n == 2 && IntegerQ[4*p]) || (n == 2 && IntegerQ[3*p]) || Denominator[p + 1/n] < Denominator[p])

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^2(ac-bcx)^2} dx &= \int \frac{1}{(a^2c-b^2cx^2)^2} dx \\ &= \frac{x}{2a^2c^2(a^2-b^2x^2)} + \frac{\int \frac{1}{a^2c-b^2cx^2} dx}{2a^2c} \\ &= \frac{x}{2a^2c^2(a^2-b^2x^2)} + \frac{\tanh^{-1}\left(\frac{bx}{a}\right)}{2a^3bc^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 74, normalized size = 1.61

$$\frac{(b^2x^2 - a^2) \log(a - bx) + (a^2 - b^2x^2) \log(a + bx) + 2abx}{4a^3bc^2(a - bx)(a + bx)}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*(a*c - b*c*x)^2), x]

[Out] (2*a*b*x + (-a^2 + b^2*x^2)*Log[a - b*x] + (a^2 - b^2*x^2)*Log[a + b*x])/(4*a^3*b*c^2*(a - b*x)*(a + b*x))

fricas [A] time = 0.44, size = 76, normalized size = 1.65

$$-\frac{2abx - (b^2x^2 - a^2) \log(bx + a) + (b^2x^2 - a^2) \log(bx - a)}{4(a^3b^3c^2x^2 - a^5bc^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(-b*c*x+a*c)^2,x, algorithm="fricas")

[Out] -1/4*(2*a*b*x - (b^2*x^2 - a^2)*log(b*x + a) + (b^2*x^2 - a^2)*log(b*x - a))/(a^3*b^3*c^2*x^2 - a^5*b*c^2)

giac [A] time = 1.07, size = 83, normalized size = 1.80

$$-\frac{1}{4(bc x - ac)a^2bc} + \frac{\log\left(\left|-\frac{2ac}{bcx-ac} - 1\right|\right)}{4a^3bc^2} + \frac{1}{8a^3b\left(\frac{2ac}{bcx-ac} + 1\right)c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(-b*c*x+a*c)^2,x, algorithm="giac")

[Out] $-1/4/((b*c*x - a*c)*a^2*b*c) + 1/4*\log(\text{abs}(-2*a*c/(b*c*x - a*c) - 1))/(a^3*b*c^2) + 1/8/(a^3*b*(2*a*c/(b*c*x - a*c) + 1)*c^2)$

maple [A] time = 0.01, size = 76, normalized size = 1.65

$$-\frac{1}{4(bx+a)a^2bc^2} - \frac{1}{4(bx-a)a^2bc^2} - \frac{\ln(bx-a)}{4a^3bc^2} + \frac{\ln(bx+a)}{4a^3bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/(-b*c*x+a*c)^2,x)

[Out] $1/4/c^2/a^3/b*\ln(b*x+a)-1/4/c^2/a^2/b/(b*x+a)-1/4/c^2/a^3/b*\ln(b*x-a)-1/4/c^2/a^2/b/(b*x-a)$

maxima [A] time = 1.32, size = 64, normalized size = 1.39

$$-\frac{x}{2(a^2b^2c^2x^2 - a^4c^2)} + \frac{\log(bx+a)}{4a^3bc^2} - \frac{\log(bx-a)}{4a^3bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(-b*c*x+a*c)^2,x, algorithm="maxima")

[Out] $-1/2*x/(a^2*b^2*c^2*x^2 - a^4*c^2) + 1/4*\log(b*x + a)/(a^3*b*c^2) - 1/4*\log(b*x - a)/(a^3*b*c^2)$

mupad [B] time = 0.18, size = 46, normalized size = 1.00

$$\frac{x}{2a^2(a^2c^2 - b^2c^2x^2)} + \frac{\operatorname{atanh}\left(\frac{bx}{a}\right)}{2a^3bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a*c - b*c*x)^2*(a + b*x)^2),x)

[Out] $x/(2*a^2*(a^2*c^2 - b^2*c^2*x^2)) + \operatorname{atanh}((b*x)/a)/(2*a^3*b*c^2)$

sympy [A] time = 0.27, size = 49, normalized size = 1.07

$$-\frac{x}{-2a^4c^2 + 2a^2b^2c^2x^2} + \frac{-\frac{\log(-\frac{a}{b}+x)}{4} + \frac{\log(\frac{a}{b}+x)}{4}}{a^3bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**2/(-b*c*x+a*c)**2,x)
```

```
[Out] -x/(-2*a**4*c**2 + 2*a**2*b**2*c**2*x**2) + (-log(-a/b + x)/4 + log(a/b + x)/4)/(a**3*b*c**2)
```

$$3.1062 \quad \int \frac{1}{(a+bx)^2(ac-bcx)^3} dx$$

Optimal. Leaf size=83

$$\frac{3 \tanh^{-1}\left(\frac{bx}{a}\right)}{8a^4bc^3} + \frac{1}{4a^3bc^3(a-bx)} - \frac{1}{8a^3bc^3(a+bx)} + \frac{1}{8a^2bc^3(a-bx)^2}$$

[Out] 1/8/a^2/b/c^3/(-b*x+a)^2+1/4/a^3/b/c^3/(-b*x+a)-1/8/a^3/b/c^3/(b*x+a)+3/8*a
rctanh(b*x/a)/a^4/b/c^3

Rubi [A] time = 0.05, antiderivative size = 83, normalized size of antiderivative = 1.00,
number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} =$
0.105, Rules used = {44, 208}

$$\frac{1}{4a^3bc^3(a-bx)} - \frac{1}{8a^3bc^3(a+bx)} + \frac{1}{8a^2bc^3(a-bx)^2} + \frac{3 \tanh^{-1}\left(\frac{bx}{a}\right)}{8a^4bc^3}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^2*(a*c - b*c*x)^3), x]

[Out] 1/(8*a^2*b*c^3*(a - b*x)^2) + 1/(4*a^3*b*c^3*(a - b*x)) - 1/(8*a^3*b*c^3*(a
+ b*x)) + (3*ArcTanh[(b*x)/a])/(8*a^4*b*c^3)

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[
ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] &
& NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m
+ n + 2, 0])

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^2(ac-bcx)^3} dx &= \int \left(\frac{1}{4a^2c^3(a-bx)^3} + \frac{1}{4a^3c^3(a-bx)^2} + \frac{1}{8a^3c^3(a+bx)^2} + \frac{3}{8a^3c^3(a^2-b^2x^2)} \right) dx \\ &= \frac{1}{8a^2bc^3(a-bx)^2} + \frac{1}{4a^3bc^3(a-bx)} - \frac{1}{8a^3bc^3(a+bx)} + \frac{3 \int \frac{1}{a^2-b^2x^2} dx}{8a^3c^3} \\ &= \frac{1}{8a^2bc^3(a-bx)^2} + \frac{1}{4a^3bc^3(a-bx)} - \frac{1}{8a^3bc^3(a+bx)} + \frac{3 \tanh^{-1}\left(\frac{bx}{a}\right)}{8a^4bc^3} \end{aligned}$$

Mathematica [A] time = 0.04, size = 68, normalized size = 0.82

$$\frac{\frac{2a(2a^2+3abx-3b^2x^2)}{(a-bx)^2(a+bx)} - 3 \log(a-bx) + 3 \log(a+bx)}{16a^4bc^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*(a*c - b*c*x)^3), x]

[Out] ((2*a*(2*a^2 + 3*a*b*x - 3*b^2*x^2))/((a - b*x)^2*(a + b*x)) - 3*Log[a - b*x] + 3*Log[a + b*x])/(16*a^4*b*c^3)

fricas [A] time = 0.45, size = 146, normalized size = 1.76

$$\frac{6ab^2x^2 - 6a^2bx - 4a^3 - 3(b^3x^3 - ab^2x^2 - a^2bx + a^3) \log(bx + a) + 3(b^3x^3 - ab^2x^2 - a^2bx + a^3) \log(bx - a)}{16(a^4b^4c^3x^3 - a^5b^3c^3x^2 - a^6b^2c^3x + a^7bc^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(-b*c*x+a*c)^3, x, algorithm="fricas")

[Out] -1/16*(6*a*b^2*x^2 - 6*a^2*b*x - 4*a^3 - 3*(b^3*x^3 - a*b^2*x^2 - a^2*b*x + a^3)*log(b*x + a) + 3*(b^3*x^3 - a*b^2*x^2 - a^2*b*x + a^3)*log(b*x - a))/ (a^4*b^4*c^3*x^3 - a^5*b^3*c^3*x^2 - a^6*b^2*c^3*x + a^7*b*c^3)

giac [A] time = 0.96, size = 81, normalized size = 0.98

$$-\frac{3 \log\left(\left|-\frac{2a}{bx+a} + 1\right|\right)}{16a^4bc^3} - \frac{1}{8(bx+a)a^3bc^3} + \frac{\frac{12a}{bx+a} - 5}{32a^4bc^3\left(\frac{2a}{bx+a} - 1\right)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(-b*c*x+a*c)^3,x, algorithm="giac")

[Out] $-\frac{3}{16} \log(\text{abs}(-2*a/(b*x + a) + 1))/(a^4*b*c^3) - \frac{1}{8} / ((b*x + a)*a^3*b*c^3) + \frac{1}{32} * (12*a/(b*x + a) - 5) / (a^4*b*c^3*(2*a/(b*x + a) - 1)^2)$

maple [A] time = 0.01, size = 96, normalized size = 1.16

$$\frac{1}{8(bx-a)^2 a^2 b c^3} - \frac{1}{8(bx+a) a^3 b c^3} - \frac{1}{4(bx-a) a^3 b c^3} - \frac{3 \ln(bx-a)}{16 a^4 b c^3} + \frac{3 \ln(bx+a)}{16 a^4 b c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/(-b*c*x+a*c)^3,x)

[Out] $\frac{3}{16} / c^3 / a^4 / b * \ln(b*x+a) - \frac{1}{8} / a^3 / b / c^3 / (b*x+a) - \frac{3}{16} / c^3 / a^4 / b * \ln(b*x-a) - \frac{1}{4} / c^3 / a^3 / b / (b*x-a) + \frac{1}{8} / c^3 / a^2 / b / (b*x-a)^2$

maxima [A] time = 1.35, size = 108, normalized size = 1.30

$$-\frac{3 b^2 x^2 - 3 a b x - 2 a^2}{8 (a^3 b^4 c^3 x^3 - a^4 b^3 c^3 x^2 - a^5 b^2 c^3 x + a^6 b c^3)} + \frac{3 \log(bx+a)}{16 a^4 b c^3} - \frac{3 \log(bx-a)}{16 a^4 b c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(-b*c*x+a*c)^3,x, algorithm="maxima")

[Out] $-\frac{1}{8} * (3*b^2*x^2 - 3*a*b*x - 2*a^2) / (a^3*b^4*c^3*x^3 - a^4*b^3*c^3*x^2 - a^5*b^2*c^3*x + a^6*b*c^3) + \frac{3}{16} * \log(b*x + a) / (a^4*b*c^3) - \frac{3}{16} * \log(b*x - a) / (a^4*b*c^3)$

mupad [B] time = 0.10, size = 86, normalized size = 1.04

$$\frac{\frac{3x}{8a^2} + \frac{1}{4ab} - \frac{3bx^2}{8a^3}}{a^3 c^3 - a^2 b c^3 x - a b^2 c^3 x^2 + b^3 c^3 x^3} + \frac{3 \operatorname{atanh}\left(\frac{bx}{a}\right)}{8 a^4 b c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a*c - b*c*x)^3*(a + b*x)^2),x)

[Out] $((3*x)/(8*a^2) + 1/(4*a*b) - (3*b*x^2)/(8*a^3)) / (a^3*c^3 + b^3*c^3*x^3 - a*b^2*c^3*x^2 - a^2*b*c^3*x) + (3*atanh((b*x)/a)) / (8*a^4*b*c^3)$

sympy [A] time = 0.51, size = 104, normalized size = 1.25

$$\frac{-2a^2 - 3abx + 3b^2x^2}{8a^6bc^3 - 8a^5b^2c^3x - 8a^4b^3c^3x^2 + 8a^3b^4c^3x^3} - \frac{\frac{3 \log(-\frac{a}{b}+x)}{16} - \frac{3 \log(\frac{a}{b}+x)}{16}}{a^4bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**2/(-b*c*x+a*c)**3,x)
```

```
[Out] -(-2*a**2 - 3*a*b*x + 3*b**2*x**2)/(8*a**6*b*c**3 - 8*a**5*b**2*c**3*x - 8*  
a**4*b**3*c**3*x**2 + 8*a**3*b**4*c**3*x**3) - (3*log(-a/b + x)/16 - 3*log(  
a/b + x)/16)/(a**4*b*c**3)
```

3.1063 $\int (1-x)^{9/2} \sqrt{1+x} dx$

Optimal. Leaf size=108

$$\frac{1}{6}(x+1)^{3/2}(1-x)^{9/2} + \frac{3}{10}(x+1)^{3/2}(1-x)^{7/2} + \frac{21}{40}(x+1)^{3/2}(1-x)^{5/2} + \frac{7}{8}(x+1)^{3/2}(1-x)^{3/2} + \frac{21}{16}x\sqrt{x+1}\sqrt{1-x} + \frac{21}{16}\sin^{-1}(x)$$

[Out] $7/8*(1-x)^{(3/2)}*(1+x)^{(3/2)}+21/40*(1-x)^{(5/2)}*(1+x)^{(3/2)}+3/10*(1-x)^{(7/2)}*(1+x)^{(3/2)}+1/6*(1-x)^{(9/2)}*(1+x)^{(3/2)}+21/16*\arcsin(x)+21/16*x*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 108, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$\frac{1}{6}(x+1)^{3/2}(1-x)^{9/2} + \frac{3}{10}(x+1)^{3/2}(1-x)^{7/2} + \frac{21}{40}(x+1)^{3/2}(1-x)^{5/2} + \frac{7}{8}(x+1)^{3/2}(1-x)^{3/2} + \frac{21}{16}x\sqrt{x+1}\sqrt{1-x} + \frac{21}{16}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(9/2)*Sqrt[1 + x], x]

[Out] $(21*\text{Sqrt}[1 - x]*x*\text{Sqrt}[1 + x])/16 + (7*(1 - x)^{(3/2)}*(1 + x)^{(3/2)})/8 + (21*(1 - x)^{(5/2)}*(1 + x)^{(3/2)})/40 + (3*(1 - x)^{(7/2)}*(1 + x)^{(3/2)})/10 + ((1 - x)^{(9/2)}*(1 + x)^{(3/2)})/6 + (21*\text{ArcSin}[x])/16$

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(x*(a + b*x)^(m+1)*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m-1)*(c + d*x)^n], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^(m), x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m+1)*(c + d*x)^n/(b*(m+n+1)), x] + Dist[(2*c*n)/(m+n+1), Int[(a + b*x)^(m)*(c + d*x)^(n-1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int (1-x)^{9/2} \sqrt{1+x} \, dx &= \frac{1}{6} (1-x)^{9/2} (1+x)^{3/2} + \frac{3}{2} \int (1-x)^{7/2} \sqrt{1+x} \, dx \\
 &= \frac{3}{10} (1-x)^{7/2} (1+x)^{3/2} + \frac{1}{6} (1-x)^{9/2} (1+x)^{3/2} + \frac{21}{10} \int (1-x)^{5/2} \sqrt{1+x} \, dx \\
 &= \frac{21}{40} (1-x)^{5/2} (1+x)^{3/2} + \frac{3}{10} (1-x)^{7/2} (1+x)^{3/2} + \frac{1}{6} (1-x)^{9/2} (1+x)^{3/2} + \frac{21}{8} \int (1-x)^{3/2} \sqrt{1+x} \, dx \\
 &= \frac{7}{8} (1-x)^{3/2} (1+x)^{3/2} + \frac{21}{40} (1-x)^{5/2} (1+x)^{3/2} + \frac{3}{10} (1-x)^{7/2} (1+x)^{3/2} + \frac{1}{6} (1-x)^{9/2} (1+x)^{3/2} \\
 &= \frac{21}{16} \sqrt{1-x} x \sqrt{1+x} + \frac{7}{8} (1-x)^{3/2} (1+x)^{3/2} + \frac{21}{40} (1-x)^{5/2} (1+x)^{3/2} + \frac{3}{10} (1-x)^{7/2} (1+x)^{3/2} \\
 &= \frac{21}{16} \sqrt{1-x} x \sqrt{1+x} + \frac{7}{8} (1-x)^{3/2} (1+x)^{3/2} + \frac{21}{40} (1-x)^{5/2} (1+x)^{3/2} + \frac{3}{10} (1-x)^{7/2} (1+x)^{3/2} \\
 &= \frac{21}{16} \sqrt{1-x} x \sqrt{1+x} + \frac{7}{8} (1-x)^{3/2} (1+x)^{3/2} + \frac{21}{40} (1-x)^{5/2} (1+x)^{3/2} + \frac{3}{10} (1-x)^{7/2} (1+x)^{3/2}
 \end{aligned}$$

Mathematica [A] time = 0.05, size = 60, normalized size = 0.56

$$\frac{1}{240} \left(\sqrt{1-x^2} (40x^5 - 192x^4 + 350x^3 - 256x^2 - 75x + 448) - 630 \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right) \right)$$

Antiderivative was successfully verified.

[In] `Integrate[(1-x)^(9/2)*Sqrt[1+x],x]`

[Out] `(Sqrt[1-x^2]*(448-75*x-256*x^2+350*x^3-192*x^4+40*x^5)-630*ArcSin[Sqrt[1-x]/Sqrt[2]])/240`

fricas [A] time = 0.44, size = 62, normalized size = 0.57

$$\frac{1}{240} (40x^5 - 192x^4 + 350x^3 - 256x^2 - 75x + 448) \sqrt{x+1} \sqrt{-x+1} - \frac{21}{8} \arctan \left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(9/2)*(1+x)^(1/2),x, algorithm="fricas")`

[Out] $\frac{1}{240}*(40*x^5 - 192*x^4 + 350*x^3 - 256*x^2 - 75*x + 448)*\sqrt{x + 1}*\sqrt{-x + 1} - \frac{21}{8}*\arctan((\sqrt{x + 1})*\sqrt{-x + 1} - 1)/x$

giac [B] time = 1.27, size = 185, normalized size = 1.71

$$\frac{1}{240} ((2((4(5x - 26)(x + 1) + 321)(x + 1) - 451)(x + 1) + 745)(x + 1) - 405)\sqrt{x + 1}\sqrt{-x + 1} - \frac{1}{40} ((2(3(4x - 17$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(9/2)*(1+x)^(1/2),x, algorithm="giac")`

[Out] $\frac{1}{240}*((2*((4*(5*x - 26)*(x + 1) + 321)*(x + 1) - 451)*(x + 1) + 745)*(x + 1) - 405)*\sqrt{x + 1}*\sqrt{-x + 1} - \frac{1}{40}*((2*(3*(4*x - 17)*(x + 1) + 133)*(x + 1) - 295)*(x + 1) + 195)*\sqrt{x + 1}*\sqrt{-x + 1} + \frac{1}{12}*((2*(3*x - 10)*(x + 1) + 43)*(x + 1) - 39)*\sqrt{x + 1}*\sqrt{-x + 1} + \frac{1}{3}*((2*x - 5)*(x + 1) + 9)*\sqrt{x + 1}*\sqrt{-x + 1} - \frac{3}{2}*\sqrt{x + 1}*(x - 2)*\sqrt{-x + 1} + \sqrt{x + 1}*\sqrt{-x + 1} + \frac{21}{8}*\arcsin(\frac{1}{2}*\sqrt{2}*\sqrt{x + 1}))$

maple [A] time = 0.01, size = 113, normalized size = 1.05

$$\frac{21\sqrt{(x+1)(-x+1)} \arcsin(x)}{16\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{9}{2}}(x+1)^{\frac{3}{2}}}{6} + \frac{3(-x+1)^{\frac{7}{2}}(x+1)^{\frac{3}{2}}}{10} + \frac{21(-x+1)^{\frac{5}{2}}(x+1)^{\frac{3}{2}}}{40} + \frac{7(-x+1)^{\frac{3}{2}}(x+1)^{\frac{3}{2}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-x+1)^(9/2)*(1+x)^(1/2),x)`

[Out] $\frac{1}{6}*(-x+1)^{(9/2)}*(1+x)^{(3/2)} + \frac{3}{10}*(-x+1)^{(7/2)}*(1+x)^{(3/2)} + \frac{21}{40}*(-x+1)^{(5/2)}*(1+x)^{(3/2)} + \frac{7}{8}*(-x+1)^{(3/2)}*(1+x)^{(3/2)} + \frac{21}{16}*(-x+1)^{(1/2)}*(1+x)^{(3/2)} - \frac{21}{16}*(-x+1)^{(1/2)}*(1+x)^{(1/2)} + \frac{21}{16}*((1+x)*(-x+1))^{(1/2)}/((1+x)^{(1/2)}*(-x+1)^{(1/2)})*\arcsin(x)$

maxima [A] time = 3.00, size = 68, normalized size = 0.63

$$-\frac{1}{6}(-x^2 + 1)^{\frac{3}{2}}x^3 + \frac{4}{5}(-x^2 + 1)^{\frac{3}{2}}x^2 - \frac{13}{8}(-x^2 + 1)^{\frac{3}{2}}x + \frac{28}{15}(-x^2 + 1)^{\frac{3}{2}} + \frac{21}{16}\sqrt{-x^2 + 1}x + \frac{21}{16}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(9/2)*(1+x)^(1/2),x, algorithm="maxima")`

[Out] $-1/6*(-x^2 + 1)^{(3/2)}*x^3 + 4/5*(-x^2 + 1)^{(3/2)}*x^2 - 13/8*(-x^2 + 1)^{(3/2)}*x + 28/15*(-x^2 + 1)^{(3/2)} + 21/16*\sqrt{-x^2 + 1}*x + 21/16*\arcsin(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{9/2} \sqrt{x+1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(9/2)*(x + 1)^(1/2), x)`

[Out] `int((1 - x)^(9/2)*(x + 1)^(1/2), x)`

sympy [A] time = 48.59, size = 289, normalized size = 2.68

$$\left\{ \begin{array}{l} -\frac{21i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{8} + \frac{i(x+1)^{\frac{13}{2}}}{6\sqrt{x-1}} - \frac{59i(x+1)^{\frac{11}{2}}}{30\sqrt{x-1}} + \frac{1151i(x+1)^{\frac{9}{2}}}{120\sqrt{x-1}} - \frac{2947i(x+1)^{\frac{7}{2}}}{120\sqrt{x-1}} + \frac{8171i(x+1)^{\frac{5}{2}}}{240\sqrt{x-1}} - \frac{1045i(x+1)^{\frac{3}{2}}}{48\sqrt{x-1}} + \frac{21i\sqrt{x+1}}{8\sqrt{x-1}} \\ \frac{21 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{8} - \frac{(x+1)^{\frac{13}{2}}}{6\sqrt{1-x}} + \frac{59(x+1)^{\frac{11}{2}}}{30\sqrt{1-x}} - \frac{1151(x+1)^{\frac{9}{2}}}{120\sqrt{1-x}} + \frac{2947(x+1)^{\frac{7}{2}}}{120\sqrt{1-x}} - \frac{8171(x+1)^{\frac{5}{2}}}{240\sqrt{1-x}} + \frac{1045(x+1)^{\frac{3}{2}}}{48\sqrt{1-x}} - \frac{21\sqrt{x+1}}{8\sqrt{1-x}} \end{array} \right. \begin{array}{l} \text{for } |x| > 1 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(9/2)*(1+x)**(1/2), x)`

[Out] `Piecewise((-21*I*acosh(sqrt(2)*sqrt(x + 1)/2)/8 + I*(x + 1)**(13/2)/(6*sqrt(x - 1)) - 59*I*(x + 1)**(11/2)/(30*sqrt(x - 1)) + 1151*I*(x + 1)**(9/2)/(120*sqrt(x - 1)) - 2947*I*(x + 1)**(7/2)/(120*sqrt(x - 1)) + 8171*I*(x + 1)**(5/2)/(240*sqrt(x - 1)) - 1045*I*(x + 1)**(3/2)/(48*sqrt(x - 1)) + 21*I*sqrt(x + 1)/(8*sqrt(x - 1)), Abs(x + 1)/2 > 1, (21*asin(sqrt(2)*sqrt(x + 1)/2)/8 - (x + 1)**(13/2)/(6*sqrt(1 - x)) + 59*(x + 1)**(11/2)/(30*sqrt(1 - x)) - 1151*(x + 1)**(9/2)/(120*sqrt(1 - x)) + 2947*(x + 1)**(7/2)/(120*sqrt(1 - x)) - 8171*(x + 1)**(5/2)/(240*sqrt(1 - x)) + 1045*(x + 1)**(3/2)/(48*sqrt(1 - x)) - 21*sqrt(x + 1)/(8*sqrt(1 - x)), True))`

3.1064 $\int (1-x)^{7/2} \sqrt{1+x} dx$

Optimal. Leaf size=88

$$\frac{1}{5}(x+1)^{3/2}(1-x)^{7/2} + \frac{7}{20}(x+1)^{3/2}(1-x)^{5/2} + \frac{7}{12}(x+1)^{3/2}(1-x)^{3/2} + \frac{7}{8}x\sqrt{x+1}\sqrt{1-x} + \frac{7}{8}\sin^{-1}(x)$$

[Out] $7/12*(1-x)^{(3/2)}*(1+x)^{(3/2)}+7/20*(1-x)^{(5/2)}*(1+x)^{(3/2)}+1/5*(1-x)^{(7/2)}*(1+x)^{(3/2)}+7/8*\arcsin(x)+7/8*x*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 88, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$\frac{1}{5}(x+1)^{3/2}(1-x)^{7/2} + \frac{7}{20}(x+1)^{3/2}(1-x)^{5/2} + \frac{7}{12}(x+1)^{3/2}(1-x)^{3/2} + \frac{7}{8}x\sqrt{x+1}\sqrt{1-x} + \frac{7}{8}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(7/2)*Sqrt[1 + x], x]

[Out] $(7*\text{Sqrt}[1 - x]*x*\text{Sqrt}[1 + x])/8 + (7*(1 - x)^{(3/2)}*(1 + x)^{(3/2)})/12 + (7*(1 - x)^{(5/2)}*(1 + x)^{(3/2)})/20 + ((1 - x)^{(7/2)}*(1 + x)^{(3/2)})/5 + (7*\text{ArcSin}[x])/8$

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(x*(a + b*x)^m*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(2*c*n)/(m + n + 1), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int (1-x)^{7/2} \sqrt{1+x} \, dx &= \frac{1}{5} (1-x)^{7/2} (1+x)^{3/2} + \frac{7}{5} \int (1-x)^{5/2} \sqrt{1+x} \, dx \\
 &= \frac{7}{20} (1-x)^{5/2} (1+x)^{3/2} + \frac{1}{5} (1-x)^{7/2} (1+x)^{3/2} + \frac{7}{4} \int (1-x)^{3/2} \sqrt{1+x} \, dx \\
 &= \frac{7}{12} (1-x)^{3/2} (1+x)^{3/2} + \frac{7}{20} (1-x)^{5/2} (1+x)^{3/2} + \frac{1}{5} (1-x)^{7/2} (1+x)^{3/2} + \frac{7}{4} \int \sqrt{1-x} \sqrt{1+x} \, dx \\
 &= \frac{7}{8} \sqrt{1-x} x \sqrt{1+x} + \frac{7}{12} (1-x)^{3/2} (1+x)^{3/2} + \frac{7}{20} (1-x)^{5/2} (1+x)^{3/2} + \frac{1}{5} (1-x)^{7/2} (1+x)^{3/2} \\
 &= \frac{7}{8} \sqrt{1-x} x \sqrt{1+x} + \frac{7}{12} (1-x)^{3/2} (1+x)^{3/2} + \frac{7}{20} (1-x)^{5/2} (1+x)^{3/2} + \frac{1}{5} (1-x)^{7/2} (1+x)^{3/2} \\
 &= \frac{7}{8} \sqrt{1-x} x \sqrt{1+x} + \frac{7}{12} (1-x)^{3/2} (1+x)^{3/2} + \frac{7}{20} (1-x)^{5/2} (1+x)^{3/2} + \frac{1}{5} (1-x)^{7/2} (1+x)^{3/2}
 \end{aligned}$$

Mathematica [A] time = 0.05, size = 56, normalized size = 0.64

$$\frac{1}{120} \sqrt{1-x^2} (-24x^4 + 90x^3 - 112x^2 + 15x + 136) - \frac{7}{4} \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right)$$

Antiderivative was successfully verified.

[In] `Integrate[(1-x)^(7/2)*Sqrt[1+x],x]`

[Out] `(Sqrt[1-x^2]*(136+15*x-112*x^2+90*x^3-24*x^4))/120-(7*ArcSin[Sqrt[1-x]/Sqrt[2]])/4`

fricas [A] time = 0.44, size = 57, normalized size = 0.65

$$-\frac{1}{120} (24x^4 - 90x^3 + 112x^2 - 15x - 136) \sqrt{x+1} \sqrt{-x+1} - \frac{7}{4} \arctan \left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(7/2)*(1+x)^(1/2),x, algorithm="fricas")`

[Out] `-1/120*(24*x^4-90*x^3+112*x^2-15*x-136)*sqrt(x+1)*sqrt(-x+1)-7/4*arctan((sqrt(x+1)*sqrt(-x+1)-1)/x)`

giac [A] time = 1.06, size = 115, normalized size = 1.31

$$-\frac{1}{120} ((2(3(4x-17)(x+1)+133)(x+1)-295)(x+1)+195)\sqrt{x+1}\sqrt{-x+1} + \frac{1}{12} ((2(3x-10)(x+1)+43)(x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)*(1+x)^(1/2),x, algorithm="giac")

[Out] -1/120*((2*(3*(4*x - 17)*(x + 1) + 133)*(x + 1) - 295)*(x + 1) + 195)*sqrt(x + 1)*sqrt(-x + 1) + 1/12*((2*(3*x - 10)*(x + 1) + 43)*(x + 1) - 39)*sqrt(x + 1)*sqrt(-x + 1) - sqrt(x + 1)*(x - 2)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + 7/4*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.00, size = 99, normalized size = 1.12

$$\frac{7\sqrt{(x+1)(-x+1)} \arcsin(x)}{8\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{7}{2}}(x+1)^{\frac{3}{2}}}{5} + \frac{7(-x+1)^{\frac{5}{2}}(x+1)^{\frac{3}{2}}}{20} + \frac{7(-x+1)^{\frac{3}{2}}(x+1)^{\frac{3}{2}}}{12} + \frac{7\sqrt{-x+1}(x+1)}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(7/2)*(x+1)^(1/2),x)

[Out] 1/5*(-x+1)^(7/2)*(x+1)^(3/2)+7/20*(-x+1)^(5/2)*(x+1)^(3/2)+7/12*(-x+1)^(3/2)*(x+1)^(3/2)+7/8*(-x+1)^(1/2)*(x+1)^(3/2)-7/8*(-x+1)^(1/2)*(x+1)^(1/2)+7/8*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.97, size = 54, normalized size = 0.61

$$\frac{1}{5}(-x^2+1)^{\frac{3}{2}}x^2 - \frac{3}{4}(-x^2+1)^{\frac{3}{2}}x + \frac{17}{15}(-x^2+1)^{\frac{3}{2}} + \frac{7}{8}\sqrt{-x^2+1}x + \frac{7}{8}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)*(1+x)^(1/2),x, algorithm="maxima")

[Out] 1/5*(-x^2 + 1)^(3/2)*x^2 - 3/4*(-x^2 + 1)^(3/2)*x + 17/15*(-x^2 + 1)^(3/2) + 7/8*sqrt(-x^2 + 1)*x + 7/8*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{7/2} \sqrt{x+1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(7/2)*(x + 1)^(1/2),x)

[Out] $\text{int}((1 - x)^{7/2} * (x + 1)^{1/2}, x)$

sympy [A] time = 21.07, size = 253, normalized size = 2.88

$$\left\{ \begin{array}{l} -\frac{7i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} - \frac{i(x+1)^{\frac{11}{2}}}{5\sqrt{x-1}} + \frac{39i(x+1)^{\frac{9}{2}}}{20\sqrt{x-1}} - \frac{449i(x+1)^{\frac{7}{2}}}{60\sqrt{x-1}} + \frac{1657i(x+1)^{\frac{5}{2}}}{120\sqrt{x-1}} - \frac{263i(x+1)^{\frac{3}{2}}}{24\sqrt{x-1}} + \frac{7i\sqrt{x+1}}{4\sqrt{x-1}} \\ \frac{7 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} + \frac{(x+1)^{\frac{11}{2}}}{5\sqrt{1-x}} - \frac{39(x+1)^{\frac{9}{2}}}{20\sqrt{1-x}} + \frac{449(x+1)^{\frac{7}{2}}}{60\sqrt{1-x}} - \frac{1657(x+1)^{\frac{5}{2}}}{120\sqrt{1-x}} + \frac{263(x+1)^{\frac{3}{2}}}{24\sqrt{1-x}} - \frac{7\sqrt{x+1}}{4\sqrt{1-x}} \end{array} \right. \begin{array}{l} \text{for } \frac{|x+1|}{2} > 1 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((1-x)^{7/2} * (1+x)^{1/2}, x)$

[Out] $\text{Piecewise}\left(\left(-7*I*\operatorname{acosh}\left(\sqrt{2}\sqrt{x+1}/2\right)/4 - I*(x+1)^{11/2}/(5*\sqrt{x-1}) + 39*I*(x+1)^{9/2}/(20*\sqrt{x-1}) - 449*I*(x+1)^{7/2}/(60*\sqrt{x-1}) + 1657*I*(x+1)^{5/2}/(120*\sqrt{x-1}) - 263*I*(x+1)^{3/2}/(24*\sqrt{x-1}) + 7*I*\sqrt{x+1}/(4*\sqrt{x-1}), \operatorname{Abs}(x+1)/2 > 1\right), \left(7*\operatorname{asin}\left(\sqrt{2}\sqrt{x+1}/2\right)/4 + (x+1)^{11/2}/(5*\sqrt{1-x}) - 39*(x+1)^{9/2}/(20*\sqrt{1-x}) + 449*(x+1)^{7/2}/(60*\sqrt{1-x}) - 1657*(x+1)^{5/2}/(120*\sqrt{1-x}) + 263*(x+1)^{3/2}/(24*\sqrt{1-x}) - 7*\sqrt{x+1}/(4*\sqrt{1-x}), \operatorname{True}\right)\right)$

3.1065 $\int (1-x)^{5/2} \sqrt{1+x} dx$

Optimal. Leaf size=68

$$\frac{1}{4}(x+1)^{3/2}(1-x)^{5/2} + \frac{5}{12}(x+1)^{3/2}(1-x)^{3/2} + \frac{5}{8}x\sqrt{x+1}\sqrt{1-x} + \frac{5}{8}\sin^{-1}(x)$$

[Out] 5/12*(1-x)^(3/2)*(1+x)^(3/2)+1/4*(1-x)^(5/2)*(1+x)^(3/2)+5/8*arcsin(x)+5/8*x*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$\frac{1}{4}(x+1)^{3/2}(1-x)^{5/2} + \frac{5}{12}(x+1)^{3/2}(1-x)^{3/2} + \frac{5}{8}x\sqrt{x+1}\sqrt{1-x} + \frac{5}{8}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(5/2)*Sqrt[1 + x], x]

[Out] (5*Sqrt[1 - x]*x*Sqrt[1 + x])/8 + (5*(1 - x)^(3/2)*(1 + x)^(3/2))/12 + ((1 - x)^(5/2)*(1 + x)^(3/2))/4 + (5*ArcSin[x])/8

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(x*(a + b*x)^m*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(2*c*n)/(m + n + 1), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int (1-x)^{5/2} \sqrt{1+x} \, dx &= \frac{1}{4}(1-x)^{5/2}(1+x)^{3/2} + \frac{5}{4} \int (1-x)^{3/2} \sqrt{1+x} \, dx \\
 &= \frac{5}{12}(1-x)^{3/2}(1+x)^{3/2} + \frac{1}{4}(1-x)^{5/2}(1+x)^{3/2} + \frac{5}{4} \int \sqrt{1-x} \sqrt{1+x} \, dx \\
 &= \frac{5}{8} \sqrt{1-x} x \sqrt{1+x} + \frac{5}{12}(1-x)^{3/2}(1+x)^{3/2} + \frac{1}{4}(1-x)^{5/2}(1+x)^{3/2} + \frac{5}{8} \int \frac{1}{\sqrt{1-x} \sqrt{1+x}} \, dx \\
 &= \frac{5}{8} \sqrt{1-x} x \sqrt{1+x} + \frac{5}{12}(1-x)^{3/2}(1+x)^{3/2} + \frac{1}{4}(1-x)^{5/2}(1+x)^{3/2} + \frac{5}{8} \int \frac{1}{\sqrt{1-x^2}} \, dx \\
 &= \frac{5}{8} \sqrt{1-x} x \sqrt{1+x} + \frac{5}{12}(1-x)^{3/2}(1+x)^{3/2} + \frac{1}{4}(1-x)^{5/2}(1+x)^{3/2} + \frac{5}{8} \sin^{-1}(x)
 \end{aligned}$$

Mathematica [A] time = 0.04, size = 50, normalized size = 0.74

$$\frac{1}{24} \left(\sqrt{1-x^2} (6x^3 - 16x^2 + 9x + 16) - 30 \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right) \right)$$

Antiderivative was successfully verified.

[In] `Integrate[(1-x)^(5/2)*Sqrt[1+x],x]`

[Out] `(Sqrt[1-x^2]*(16+9*x-16*x^2+6*x^3)-30*ArcSin[Sqrt[1-x]/Sqrt[2]])/24`

fricas [A] time = 0.45, size = 52, normalized size = 0.76

$$\frac{1}{24} (6x^3 - 16x^2 + 9x + 16) \sqrt{x+1} \sqrt{-x+1} - \frac{5}{4} \arctan \left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(5/2)*(1+x)^(1/2),x, algorithm="fricas")`

[Out] `1/24*(6*x^3-16*x^2+9*x+16)*sqrt(x+1)*sqrt(-x+1)-5/4*arctan((sqrt(x+1)*sqrt(-x+1)-1)/x)`

giac [B] time = 1.29, size = 101, normalized size = 1.49

$$\frac{1}{24} ((2(3x-10)(x+1)+43)(x+1)-39) \sqrt{x+1} \sqrt{-x+1} - \frac{1}{6} ((2x-5)(x+1)+9) \sqrt{x+1} \sqrt{-x+1} - \frac{1}{2} \sqrt{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)*(1+x)^(1/2),x, algorithm="giac")

[Out] 1/24*((2*(3*x - 10)*(x + 1) + 43)*(x + 1) - 39)*sqrt(x + 1)*sqrt(-x + 1) - 1/6*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) - 1/2*sqrt(x + 1)*(x - 2)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + 5/4*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.01, size = 85, normalized size = 1.25

$$\frac{5\sqrt{(x+1)(-x+1)} \arcsin(x)}{8\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{5}{2}}(x+1)^{\frac{3}{2}}}{4} + \frac{5(-x+1)^{\frac{3}{2}}(x+1)^{\frac{3}{2}}}{12} + \frac{5\sqrt{-x+1}(x+1)^{\frac{3}{2}}}{8} - \frac{5\sqrt{-x+1}\sqrt{x+1}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(5/2)*(x+1)^(1/2),x)

[Out] 1/4*(-x+1)^(5/2)*(x+1)^(3/2)+5/12*(-x+1)^(3/2)*(x+1)^(3/2)+5/8*(-x+1)^(1/2)*(x+1)^(3/2)-5/8*(-x+1)^(1/2)*(x+1)^(1/2)+5/8*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.95, size = 40, normalized size = 0.59

$$-\frac{1}{4}(-x^2+1)^{\frac{3}{2}}x + \frac{2}{3}(-x^2+1)^{\frac{3}{2}} + \frac{5}{8}\sqrt{-x^2+1}x + \frac{5}{8}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)*(1+x)^(1/2),x, algorithm="maxima")

[Out] -1/4*(-x^2 + 1)^(3/2)*x + 2/3*(-x^2 + 1)^(3/2) + 5/8*sqrt(-x^2 + 1)*x + 5/8*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{5/2} \sqrt{x+1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(5/2)*(x + 1)^(1/2),x)

[Out] int((1 - x)^(5/2)*(x + 1)^(1/2), x)

sympy [A] time = 9.03, size = 218, normalized size = 3.21

$$\begin{cases} -\frac{5i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} + \frac{i(x+1)^{\frac{9}{2}}}{4\sqrt{x-1}} - \frac{23i(x+1)^{\frac{7}{2}}}{12\sqrt{x-1}} + \frac{127i(x+1)^{\frac{5}{2}}}{24\sqrt{x-1}} - \frac{133i(x+1)^{\frac{3}{2}}}{24\sqrt{x-1}} + \frac{5i\sqrt{x+1}}{4\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ \frac{5 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} - \frac{(x+1)^{\frac{9}{2}}}{4\sqrt{1-x}} + \frac{23(x+1)^{\frac{7}{2}}}{12\sqrt{1-x}} - \frac{127(x+1)^{\frac{5}{2}}}{24\sqrt{1-x}} + \frac{133(x+1)^{\frac{3}{2}}}{24\sqrt{1-x}} - \frac{5\sqrt{x+1}}{4\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(5/2)*(1+x)**(1/2), x)

[Out] Piecewise((-5*I*acosh(sqrt(2)*sqrt(x + 1)/2)/4 + I*(x + 1)**(9/2)/(4*sqrt(x - 1)) - 23*I*(x + 1)**(7/2)/(12*sqrt(x - 1)) + 127*I*(x + 1)**(5/2)/(24*sqrt(x - 1)) - 133*I*(x + 1)**(3/2)/(24*sqrt(x - 1)) + 5*I*sqrt(x + 1)/(4*sqrt(x - 1)), Abs(x + 1)/2 > 1), (5*asin(sqrt(2)*sqrt(x + 1)/2)/4 - (x + 1)**(9/2)/(4*sqrt(1 - x)) + 23*(x + 1)**(7/2)/(12*sqrt(1 - x)) - 127*(x + 1)**(5/2)/(24*sqrt(1 - x)) + 133*(x + 1)**(3/2)/(24*sqrt(1 - x)) - 5*sqrt(x + 1)/(4*sqrt(1 - x)), True))

3.1066 $\int (1-x)^{3/2} \sqrt{1+x} dx$

Optimal. Leaf size=48

$$\frac{1}{3}(1-x)^{3/2}(x+1)^{3/2} + \frac{1}{2}\sqrt{1-x}x\sqrt{x+1} + \frac{1}{2}\sin^{-1}(x)$$

[Out] $1/3*(1-x)^{(3/2)}*(1+x)^{(3/2)}+1/2*\arcsin(x)+1/2*x*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$\frac{1}{3}(1-x)^{3/2}(x+1)^{3/2} + \frac{1}{2}\sqrt{1-x}x\sqrt{x+1} + \frac{1}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(3/2)*Sqrt[1 + x],x]

[Out] (Sqrt[1 - x]*x*Sqrt[1 + x])/2 + ((1 - x)^(3/2)*(1 + x)^(3/2))/3 + ArcSin[x]/2

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(x*(a + b*x)^m*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(2*c*n)/(m + n + 1), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int (1-x)^{3/2} \sqrt{1+x} \, dx &= \frac{1}{3} (1-x)^{3/2} (1+x)^{3/2} + \int \sqrt{1-x} \sqrt{1+x} \, dx \\
 &= \frac{1}{2} \sqrt{1-x} x \sqrt{1+x} + \frac{1}{3} (1-x)^{3/2} (1+x)^{3/2} + \frac{1}{2} \int \frac{1}{\sqrt{1-x} \sqrt{1+x}} \, dx \\
 &= \frac{1}{2} \sqrt{1-x} x \sqrt{1+x} + \frac{1}{3} (1-x)^{3/2} (1+x)^{3/2} + \frac{1}{2} \int \frac{1}{\sqrt{1-x^2}} \, dx \\
 &= \frac{1}{2} \sqrt{1-x} x \sqrt{1+x} + \frac{1}{3} (1-x)^{3/2} (1+x)^{3/2} + \frac{1}{2} \sin^{-1}(x)
 \end{aligned}$$

Mathematica [A] time = 0.04, size = 44, normalized size = 0.92

$$\frac{1}{6} (-2x^2 + 3x + 2) \sqrt{1-x^2} - \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right)$$

Antiderivative was successfully verified.

[In] `Integrate[(1-x)^(3/2)*Sqrt[1+x],x]`

[Out] `((2+3*x-2*x^2)*Sqrt[1-x^2])/6 - ArcSin[Sqrt[1-x]/Sqrt[2]]`

fricas [A] time = 0.43, size = 47, normalized size = 0.98

$$-\frac{1}{6} (2x^2 - 3x - 2) \sqrt{x+1} \sqrt{-x+1} - \arctan \left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(3/2)*(1+x)^(1/2),x, algorithm="fricas")`

[Out] `-1/6*(2*x^2 - 3*x - 2)*sqrt(x+1)*sqrt(-x+1) - arctan((sqrt(x+1)*sqrt(-x+1) - 1)/x)`

giac [A] time = 1.02, size = 50, normalized size = 1.04

$$-\frac{1}{6} ((2x-5)(x+1)+9) \sqrt{x+1} \sqrt{-x+1} + \sqrt{x+1} \sqrt{-x+1} + \arcsin \left(\frac{1}{2} \sqrt{2} \sqrt{x+1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)*(1+x)^(1/2),x, algorithm="giac")

[Out] -1/6*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.00, size = 71, normalized size = 1.48

$$\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{2\sqrt{x+1} \sqrt{-x+1}} + \frac{(-x+1)^{\frac{3}{2}} (x+1)^{\frac{3}{2}}}{3} + \frac{\sqrt{-x+1} (x+1)^{\frac{3}{2}}}{2} - \frac{\sqrt{-x+1} \sqrt{x+1}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(3/2)*(x+1)^(1/2),x)

[Out] 1/3*(-x+1)^(3/2)*(x+1)^(3/2)+1/2*(-x+1)^(1/2)*(x+1)^(3/2)-1/2*(-x+1)^(1/2)*(x+1)^(1/2)+1/2*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.90, size = 28, normalized size = 0.58

$$\frac{1}{3}(-x^2+1)^{\frac{3}{2}} + \frac{1}{2}\sqrt{-x^2+1}x + \frac{1}{2}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)*(1+x)^(1/2),x, algorithm="maxima")

[Out] 1/3*(-x^2 + 1)^(3/2) + 1/2*sqrt(-x^2 + 1)*x + 1/2*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (1-x)^{3/2} \sqrt{x+1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(3/2)*(x + 1)^(1/2),x)

[Out] int((1 - x)^(3/2)*(x + 1)^(1/2), x)

sympy [B] time = 4.49, size = 168, normalized size = 3.50

$$\begin{cases} -i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{i(x+1)^{\frac{7}{2}}}{3\sqrt{x-1}} + \frac{11i(x+1)^{\frac{5}{2}}}{6\sqrt{x-1}} - \frac{17i(x+1)^{\frac{3}{2}}}{6\sqrt{x-1}} + \frac{i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{(x+1)^{\frac{7}{2}}}{3\sqrt{1-x}} - \frac{11(x+1)^{\frac{5}{2}}}{6\sqrt{1-x}} + \frac{17(x+1)^{\frac{3}{2}}}{6\sqrt{1-x}} - \frac{\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((1-x)**(3/2)*(1+x)**(1/2),x)
```

```
[Out] Piecewise((-I*acosh(sqrt(2)*sqrt(x + 1)/2) - I*(x + 1)**(7/2)/(3*sqrt(x - 1)) + 11*I*(x + 1)**(5/2)/(6*sqrt(x - 1)) - 17*I*(x + 1)**(3/2)/(6*sqrt(x - 1)) + I*sqrt(x + 1)/sqrt(x - 1), Abs(x + 1)/2 > 1), (asin(sqrt(2)*sqrt(x + 1)/2) + (x + 1)**(7/2)/(3*sqrt(1 - x)) - 11*(x + 1)**(5/2)/(6*sqrt(1 - x)) + 17*(x + 1)**(3/2)/(6*sqrt(1 - x)) - sqrt(x + 1)/sqrt(1 - x), True))
```

3.1067 $\int \sqrt{1-x} \sqrt{1+x} dx$

Optimal. Leaf size=28

$$\frac{1}{2} \sqrt{1-x} \sqrt{x+1} x + \frac{1}{2} \sin^{-1}(x)$$

[Out] 1/2*arcsin(x)+1/2*x*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {38, 41, 216}

$$\frac{1}{2} \sqrt{1-x} \sqrt{x+1} x + \frac{1}{2} \sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 - x]*Sqrt[1 + x],x]

[Out] (Sqrt[1 - x]*x*Sqrt[1 + x])/2 + ArcSin[x]/2

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> Simp[(x*(a + b*x)^m*(c + d*x)^m)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(m - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \sqrt{1-x} \sqrt{1+x} dx &= \frac{1}{2} \sqrt{1-x} x \sqrt{1+x} + \frac{1}{2} \int \frac{1}{\sqrt{1-x} \sqrt{1+x}} dx \\
&= \frac{1}{2} \sqrt{1-x} x \sqrt{1+x} + \frac{1}{2} \int \frac{1}{\sqrt{1-x^2}} dx \\
&= \frac{1}{2} \sqrt{1-x} x \sqrt{1+x} + \frac{1}{2} \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 0.71

$$\frac{1}{2} \left(\sqrt{1-x^2} x + \sin^{-1}(x) \right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 - x]*Sqrt[1 + x],x]

[Out] (x*Sqrt[1 - x^2] + ArcSin[x])/2

fricas [A] time = 0.45, size = 38, normalized size = 1.36

$$\frac{1}{2} \sqrt{x+1} x \sqrt{-x+1} - \arctan\left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)*(1+x)^(1/2),x, algorithm="fricas")

[Out] 1/2*sqrt(x + 1)*x*sqrt(-x + 1) - arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [B] time = 1.04, size = 42, normalized size = 1.50

$$\frac{1}{2} \sqrt{x+1} (x-2) \sqrt{-x+1} + \sqrt{x+1} \sqrt{-x+1} + \arcsin\left(\frac{1}{2} \sqrt{2} \sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)*(1+x)^(1/2),x, algorithm="giac")

[Out] 1/2*sqrt(x + 1)*(x - 2)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.00, size = 57, normalized size = 2.04

$$\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{2\sqrt{x+1} \sqrt{-x+1}} - \frac{(-x+1)^{\frac{3}{2}} \sqrt{x+1}}{2} + \frac{\sqrt{-x+1} \sqrt{x+1}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-x+1)^(1/2)*(x+1)^(1/2),x)`

[Out] $-1/2*(-x+1)^{(3/2)}*(x+1)^{(1/2)}+1/2*(-x+1)^{(1/2)}*(x+1)^{(1/2)}+1/2*((x+1)*(-x+1))^{\wedge}(1/2)/(x+1)^{(1/2)/(-x+1)^{(1/2)}*\arcsin(x)}$

maxima [A] time = 2.98, size = 17, normalized size = 0.61

$$\frac{1}{2}\sqrt{-x^2+1}x + \frac{1}{2}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(1/2)*(1+x)^(1/2),x, algorithm="maxima")`

[Out] $1/2*\sqrt{-x^2+1}*x + 1/2*\arcsin(x)$

mupad [B] time = 0.20, size = 37, normalized size = 1.32

$$\frac{x\sqrt{1-x}\sqrt{x+1}}{2} - \frac{\ln(x - \sqrt{1-x}\sqrt{x+1})}{2} + \frac{i}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1-x)^(1/2)*(x+1)^(1/2),x)`

[Out] $(x*(1-x)^{(1/2)}*(x+1)^{(1/2)})/2 - (\log(x - (1-x)^{(1/2)}*(x+1)^{(1/2)}*1i)*1i)/2$

sympy [B] time = 2.73, size = 133, normalized size = 4.75

$$\begin{cases} -i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{i(x+1)^{\frac{5}{2}}}{2\sqrt{x-1}} - \frac{3i(x+1)^{\frac{3}{2}}}{2\sqrt{x-1}} + \frac{i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{(x+1)^{\frac{5}{2}}}{2\sqrt{1-x}} + \frac{3(x+1)^{\frac{3}{2}}}{2\sqrt{1-x}} - \frac{\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(1/2)*(1+x)**(1/2),x)`

[Out] $\text{Piecewise}((-I*\operatorname{acosh}(\sqrt{2}*\sqrt{x+1}/2) + I*(x+1)**(5/2)/(2*\sqrt{x-1})) - 3*I*(x+1)**(3/2)/(2*\sqrt{x-1}) + I*\sqrt{x+1}/\sqrt{x-1}, \operatorname{Abs}(x+1)/2 > 1), (\operatorname{asin}(\sqrt{2}*\sqrt{x+1}/2) - (x+1)**(5/2)/(2*\sqrt{1-x}) + 3*(x+1)**(3/2)/(2*\sqrt{1-x}) - \sqrt{x+1}/\sqrt{1-x}, \text{True}))$

$$3.1068 \quad \int \frac{\sqrt{1+x}}{\sqrt{1-x}} dx$$

Optimal. Leaf size=21

$$\sin^{-1}(x) - \sqrt{1-x} \sqrt{x+1}$$

[Out] arcsin(x)-(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {50, 41, 216}

$$\sin^{-1}(x) - \sqrt{1-x} \sqrt{x+1}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 + x]/Sqrt[1 - x], x]

[Out] -(Sqrt[1 - x]*Sqrt[1 + x]) + ArcSin[x]

Rule 41

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 50

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{1+x}}{\sqrt{1-x}} dx &= -\sqrt{1-x}\sqrt{1+x} + \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
&= -\sqrt{1-x}\sqrt{1+x} + \int \frac{1}{\sqrt{1-x^2}} dx \\
&= -\sqrt{1-x}\sqrt{1+x} + \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 1.52

$$-\sqrt{1-x^2} - 2 \sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 + x]/Sqrt[1 - x], x]

[Out] -Sqrt[1 - x^2] - 2*ArcSin[Sqrt[1 - x]/Sqrt[2]]

fricas [B] time = 0.44, size = 37, normalized size = 1.76

$$-\sqrt{x+1}\sqrt{-x+1} - 2 \arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(1/2), x, algorithm="fricas")

[Out] -sqrt(x + 1)*sqrt(-x + 1) - 2*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [A] time = 1.01, size = 28, normalized size = 1.33

$$-\sqrt{x+1}\sqrt{-x+1} + 2 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(1/2), x, algorithm="giac")

[Out] -sqrt(x + 1)*sqrt(-x + 1) + 2*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.01, size = 42, normalized size = 2.00

$$\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1}\sqrt{-x+1}} - \sqrt{-x+1}\sqrt{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x+1)^(1/2)/(-x+1)^(1/2),x)`

[Out] $-(-x+1)^{(1/2)}*(x+1)^{(1/2)}+((x+1)*(-x+1))^{(1/2)}/(x+1)^{(1/2)}/(-x+1)^{(1/2)}*\arcsin(x)$

maxima [A] time = 2.90, size = 14, normalized size = 0.67

$$-\sqrt{-x^2 + 1} + \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)^(1/2)/(1-x)^(1/2),x, algorithm="maxima")`

[Out] $-\sqrt{-x^2 + 1} + \arcsin(x)$

mupad [B] time = 0.14, size = 14, normalized size = 0.67

$$\arcsin(x) - \sqrt{1 - x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x + 1)^(1/2)/(1 - x)^(1/2),x)`

[Out] $\arcsin(x) - (1 - x^2)^{(1/2)}$

sympy [B] time = 1.84, size = 100, normalized size = 4.76

$$\begin{cases} -2i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{i(x+1)^{\frac{3}{2}}}{\sqrt{x-1}} + \frac{2i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ 2 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{(x+1)^{\frac{3}{2}}}{\sqrt{1-x}} - \frac{2\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)**(1/2)/(1-x)**(1/2),x)`

[Out] $\operatorname{Piecewise}\left(\left(-2*I*\operatorname{acosh}\left(\sqrt{2}\sqrt{x+1}/2\right) - I*(x+1)^{(3/2)}/\sqrt{x-1}\right) + 2*I*\sqrt{x+1}/\sqrt{x-1}, \operatorname{Abs}(x+1)/2 > 1\right), \left(2*\operatorname{asin}\left(\sqrt{2}\sqrt{x+1}/2\right) + (x+1)^{(3/2)}/\sqrt{1-x} - 2*\sqrt{x+1}/\sqrt{1-x}\right), \operatorname{True}\right)$

$$3.1069 \quad \int \frac{\sqrt{1+x}}{(1-x)^{3/2}} dx$$

Optimal. Leaf size=23

$$\frac{2\sqrt{x+1}}{\sqrt{1-x}} - \sin^{-1}(x)$$

[Out] -arcsin(x)+2*(1+x)^(1/2)/(1-x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {47, 41, 216}

$$\frac{2\sqrt{x+1}}{\sqrt{1-x}} - \sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 + x]/(1 - x)^(3/2), x]

[Out] (2*Sqrt[1 + x])/Sqrt[1 - x] - ArcSin[x]

Rule 41

```
Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))
```

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 216

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{1+x}}{(1-x)^{3/2}} dx &= \frac{2\sqrt{1+x}}{\sqrt{1-x}} - \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
&= \frac{2\sqrt{1+x}}{\sqrt{1-x}} - \int \frac{1}{\sqrt{1-x^2}} dx \\
&= \frac{2\sqrt{1+x}}{\sqrt{1-x}} - \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 36, normalized size = 1.57

$$2 \left(\frac{\sqrt{x+1}}{\sqrt{1-x}} + \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 + x]/(1 - x)^(3/2), x]

[Out] 2*(Sqrt[1 + x]/Sqrt[1 - x] + ArcSin[Sqrt[1 - x]/Sqrt[2]])

fricas [B] time = 0.47, size = 48, normalized size = 2.09

$$\frac{2 \left((x-1) \arctan \left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x} \right) + x - \sqrt{x+1} \sqrt{-x+1} - 1 \right)}{x-1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(3/2), x, algorithm="fricas")

[Out] 2*((x - 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) + x - sqrt(x + 1)*sqrt(-x + 1) - 1)/(x - 1)

giac [A] time = 1.06, size = 33, normalized size = 1.43

$$-\frac{2\sqrt{x+1}\sqrt{-x+1}}{x-1} - 2 \arcsin \left(\frac{1}{2} \sqrt{2} \sqrt{x+1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(3/2), x, algorithm="giac")

[Out] -2*sqrt(x + 1)*sqrt(-x + 1)/(x - 1) - 2*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.03, size = 64, normalized size = 2.78

$$-\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1} \sqrt{-x+1}} + \frac{2\sqrt{x+1} \sqrt{(x+1)(-x+1)}}{\sqrt{-(x+1)(x-1)} \sqrt{-x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(1/2)/(-x+1)^(3/2),x)

[Out] 2*(x+1)^(1/2)/(-(x+1)*(-1+x))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)-((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.95, size = 21, normalized size = 0.91

$$-\frac{2\sqrt{-x^2+1}}{x-1} - \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(3/2),x, algorithm="maxima")

[Out] -2*sqrt(-x^2 + 1)/(x - 1) - arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{\sqrt{x+1}}{(1-x)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(1/2)/(1 - x)^(3/2),x)

[Out] int((x + 1)^(1/2)/(1 - x)^(3/2), x)

sympy [A] time = 1.62, size = 71, normalized size = 3.09

$$\begin{cases} 2i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{2i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ -2 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{2\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(1/2)/(1-x)**(3/2),x)

[Out] Piecewise((2*I*acosh(sqrt(2)*sqrt(x + 1)/2) - 2*I*sqrt(x + 1)/sqrt(x - 1), Abs(x + 1)/2 > 1), (-2*asin(sqrt(2)*sqrt(x + 1)/2) + 2*sqrt(x + 1)/sqrt(1 - x), True))

$$3.1070 \quad \int \frac{\sqrt{1+x}}{(1-x)^{5/2}} dx$$

Optimal. Leaf size=20

$$\frac{(x+1)^{3/2}}{3(1-x)^{3/2}}$$

[Out] 1/3*(1+x)^(3/2)/(1-x)^(3/2)

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {37}

$$\frac{(x+1)^{3/2}}{3(1-x)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 + x]/(1 - x)^(5/2), x]

[Out] (1 + x)^(3/2)/(3*(1 - x)^(3/2))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{1+x}}{(1-x)^{5/2}} dx = \frac{(1+x)^{3/2}}{3(1-x)^{3/2}}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 1.00

$$\frac{(x+1)^{3/2}}{3(1-x)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 + x]/(1 - x)^(5/2), x]

[Out] (1 + x)^(3/2)/(3*(1 - x)^(3/2))

fricas [B] time = 0.43, size = 33, normalized size = 1.65

$$\frac{x^2 + (x+1)^{\frac{3}{2}}\sqrt{-x+1} - 2x + 1}{3(x^2 - 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(5/2),x, algorithm="fricas")

[Out] 1/3*(x^2 + (x + 1)^(3/2)*sqrt(-x + 1) - 2*x + 1)/(x^2 - 2*x + 1)

giac [A] time = 0.94, size = 19, normalized size = 0.95

$$\frac{(x+1)^{\frac{3}{2}}\sqrt{-x+1}}{3(x-1)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(5/2),x, algorithm="giac")

[Out] 1/3*(x + 1)^(3/2)*sqrt(-x + 1)/(x - 1)^2

maple [A] time = 0.00, size = 15, normalized size = 0.75

$$\frac{(x+1)^{\frac{3}{2}}}{3(-x+1)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(1/2)/(-x+1)^(5/2),x)

[Out] 1/3*(x+1)^(3/2)/(-x+1)^(3/2)

maxima [B] time = 1.26, size = 38, normalized size = 1.90

$$\frac{2\sqrt{-x^2+1}}{3(x^2-2x+1)} + \frac{\sqrt{-x^2+1}}{3(x-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(5/2),x, algorithm="maxima")

[Out] 2/3*sqrt(-x^2 + 1)/(x^2 - 2*x + 1) + 1/3*sqrt(-x^2 + 1)/(x - 1)

mupad [B] time = 0.27, size = 34, normalized size = 1.70

$$\frac{\left(\frac{x\sqrt{x+1}}{3} + \frac{\sqrt{x+1}}{3}\right)\sqrt{1-x}}{x^2 - 2x + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x + 1)^(1/2)/(1 - x)^(5/2), x)`

[Out] `((x*(x + 1)^(1/2))/3 + (x + 1)^(1/2)/3)*(1 - x)^(1/2)/(x^2 - 2*x + 1)`

sympy [A] time = 1.67, size = 61, normalized size = 3.05

$$\begin{cases} \frac{i(x+1)^{\frac{3}{2}}}{3\sqrt{x-1}(x+1)-6\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ -\frac{(x+1)^{\frac{3}{2}}}{3\sqrt{1-x}(x+1)-6\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)**(1/2)/(1-x)**(5/2), x)`

[Out] `Piecewise((I*(x + 1)**(3/2)/(3*sqrt(x - 1)*(x + 1) - 6*sqrt(x - 1)), Abs(x + 1)/2 > 1), (- (x + 1)**(3/2)/(3*sqrt(1 - x)*(x + 1) - 6*sqrt(1 - x)), True))`

$$3.1071 \quad \int \frac{\sqrt{1+x}}{(1-x)^{7/2}} dx$$

Optimal. Leaf size=41

$$\frac{(x+1)^{3/2}}{15(1-x)^{3/2}} + \frac{(x+1)^{3/2}}{5(1-x)^{5/2}}$$

[Out] $1/5*(1+x)^{(3/2)/(1-x)^{(5/2)}+1/15*(1+x)^{(3/2)/(1-x)^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{(x+1)^{3/2}}{15(1-x)^{3/2}} + \frac{(x+1)^{3/2}}{5(1-x)^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 + x]/(1 - x)^(7/2), x]

[Out] $(1 + x)^{(3/2)/(5*(1 - x)^{(5/2)}) + (1 + x)^{(3/2)/(15*(1 - x)^{(3/2)})}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{\sqrt{1+x}}{(1-x)^{7/2}} dx = \frac{(1+x)^{3/2}}{5(1-x)^{5/2}} + \frac{1}{5} \int \frac{\sqrt{1+x}}{(1-x)^{5/2}} dx$$

$$= \frac{(1+x)^{3/2}}{5(1-x)^{5/2}} + \frac{(1+x)^{3/2}}{15(1-x)^{3/2}}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.56

$$\frac{(x-4)(x+1)^{3/2}}{15(1-x)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 + x]/(1 - x)^(7/2), x]

[Out] -1/15*((-4 + x)*(1 + x)^(3/2))/(1 - x)^(5/2)

fricas [A] time = 0.42, size = 53, normalized size = 1.29

$$\frac{4x^3 - 12x^2 + (x^2 - 3x - 4)\sqrt{x+1}\sqrt{-x+1} + 12x - 4}{15(x^3 - 3x^2 + 3x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(7/2), x, algorithm="fricas")

[Out] 1/15*(4*x^3 - 12*x^2 + (x^2 - 3*x - 4)*sqrt(x + 1)*sqrt(-x + 1) + 12*x - 4)/(x^3 - 3*x^2 + 3*x - 1)

giac [A] time = 1.05, size = 22, normalized size = 0.54

$$\frac{(x+1)^{3/2}(x-4)\sqrt{-x+1}}{15(x-1)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(7/2), x, algorithm="giac")

[Out] 1/15*(x + 1)^(3/2)*(x - 4)*sqrt(-x + 1)/(x - 1)^3

maple [A] time = 0.00, size = 18, normalized size = 0.44

$$\frac{(x+1)^{3/2}(x-4)}{15(-x+1)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x+1)^(1/2)/(-x+1)^(7/2),x)`

[Out] $-1/15*(x+1)^{(3/2)}*(x-4)/(-x+1)^{(5/2)}$

maxima [B] time = 1.40, size = 64, normalized size = 1.56

$$-\frac{2\sqrt{-x^2+1}}{5(x^3-3x^2+3x-1)} - \frac{\sqrt{-x^2+1}}{15(x^2-2x+1)} + \frac{\sqrt{-x^2+1}}{15(x-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)^(1/2)/(1-x)^(7/2),x, algorithm="maxima")`

[Out] $-2/5*\sqrt{-x^2+1}/(x^3-3*x^2+3*x-1) - 1/15*\sqrt{-x^2+1}/(x^2-2*x+1) + 1/15*\sqrt{-x^2+1}/(x-1)$

mupad [B] time = 0.24, size = 50, normalized size = 1.22

$$\frac{\sqrt{1-x} \left(\frac{x\sqrt{x+1}}{5} + \frac{4\sqrt{x+1}}{15} - \frac{x^2\sqrt{x+1}}{15} \right)}{x^3-3x^2+3x-1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x+1)^(1/2)/(1-x)^(7/2),x)`

[Out] $-((1-x)^{(1/2)}*((x*(x+1)^(1/2))/5 + (4*(x+1)^(1/2))/15 - (x^2*(x+1)^(1/2))/15))/(3*x-3*x^2+x^3-1)$

sympy [B] time = 6.55, size = 173, normalized size = 4.22

$$\begin{cases} \frac{i(x+1)^{\frac{5}{2}}}{15\sqrt{x-1}(x+1)^2-60\sqrt{x-1}(x+1)+60\sqrt{x-1}} - \frac{5i(x+1)^{\frac{3}{2}}}{15\sqrt{x-1}(x+1)^2-60\sqrt{x-1}(x+1)+60\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ -\frac{(x+1)^{\frac{5}{2}}}{15\sqrt{1-x}(x+1)^2-60\sqrt{1-x}(x+1)+60\sqrt{1-x}} + \frac{5(x+1)^{\frac{3}{2}}}{15\sqrt{1-x}(x+1)^2-60\sqrt{1-x}(x+1)+60\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)**(1/2)/(1-x)**(7/2),x)`

[Out] `Piecewise((I*(x+1)**(5/2)/(15*sqrt(x-1)*(x+1)**2-60*sqrt(x-1)*(x+1)+60*sqrt(x-1))-5*I*(x+1)**(3/2)/(15*sqrt(x-1)*(x+1)**2-60*sqrt(x-1)*(x+1)+60*sqrt(x-1)), Abs(x+1)/2 > 1), (- (x+1)**(5/2)/(15*sqrt(1-x)*(x+1)**2-60*sqrt(1-x)*(x+1)+60*sqrt(1-x))+5*(x+1)**(3/2)/(15*sqrt(1-x)*(x+1)**2-60*sqrt(1-x)*(x+1)+60*sqrt(1-x)), True))`

$$3.1072 \quad \int \frac{\sqrt{1+x}}{(1-x)^{9/2}} dx$$

Optimal. Leaf size=61

$$\frac{2(x+1)^{3/2}}{105(1-x)^{3/2}} + \frac{2(x+1)^{3/2}}{35(1-x)^{5/2}} + \frac{(x+1)^{3/2}}{7(1-x)^{7/2}}$$

[Out] $1/7*(1+x)^{(3/2)}/(1-x)^{(7/2)}+2/35*(1+x)^{(3/2)}/(1-x)^{(5/2)}+2/105*(1+x)^{(3/2)}/(1-x)^{(3/2)}$

Rubi [A] time = 0.01, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{2(x+1)^{3/2}}{105(1-x)^{3/2}} + \frac{2(x+1)^{3/2}}{35(1-x)^{5/2}} + \frac{(x+1)^{3/2}}{7(1-x)^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 + x]/(1 - x)^(9/2), x]

[Out] $(1+x)^{(3/2)}/(7*(1-x)^{(7/2)}) + (2*(1+x)^{(3/2)})/(35*(1-x)^{(5/2)}) + (2*(1+x)^{(3/2)})/(105*(1-x)^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{1+x}}{(1-x)^{9/2}} dx &= \frac{(1+x)^{3/2}}{7(1-x)^{7/2}} + \frac{2}{7} \int \frac{\sqrt{1+x}}{(1-x)^{7/2}} dx \\
&= \frac{(1+x)^{3/2}}{7(1-x)^{7/2}} + \frac{2(1+x)^{3/2}}{35(1-x)^{5/2}} + \frac{2}{35} \int \frac{\sqrt{1+x}}{(1-x)^{5/2}} dx \\
&= \frac{(1+x)^{3/2}}{7(1-x)^{7/2}} + \frac{2(1+x)^{3/2}}{35(1-x)^{5/2}} + \frac{2(1+x)^{3/2}}{105(1-x)^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 0.49

$$\frac{(x+1)^{3/2}(2x^2-10x+23)}{105(1-x)^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 + x]/(1 - x)^(9/2), x]

[Out] ((1 + x)^(3/2)*(23 - 10*x + 2*x^2))/(105*(1 - x)^(7/2))

fricas [A] time = 0.45, size = 70, normalized size = 1.15

$$\frac{23x^4 - 92x^3 + 138x^2 + (2x^3 - 8x^2 + 13x + 23)\sqrt{x+1}\sqrt{-x+1} - 92x + 23}{105(x^4 - 4x^3 + 6x^2 - 4x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(9/2), x, algorithm="fricas")

[Out] 1/105*(23*x^4 - 92*x^3 + 138*x^2 + (2*x^3 - 8*x^2 + 13*x + 23)*sqrt(x + 1)*sqrt(-x + 1) - 92*x + 23)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1)

giac [A] time = 1.22, size = 29, normalized size = 0.48

$$\frac{(2(x+1)(x-6) + 35)(x+1)^{3/2}\sqrt{-x+1}}{105(x-1)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(9/2), x, algorithm="giac")

[Out] 1/105*(2*(x + 1)*(x - 6) + 35)*(x + 1)^(3/2)*sqrt(-x + 1)/(x - 1)^4

maple [A] time = 0.00, size = 25, normalized size = 0.41

$$\frac{(x+1)^{\frac{3}{2}}(2x^2-10x+23)}{105(-x+1)^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(1/2)/(-x+1)^(9/2), x)

[Out] 1/105*(x+1)^(3/2)*(2*x^2-10*x+23)/(-x+1)^(7/2)

maxima [B] time = 1.27, size = 95, normalized size = 1.56

$$\frac{2\sqrt{-x^2+1}}{7(x^4-4x^3+6x^2-4x+1)} + \frac{\sqrt{-x^2+1}}{35(x^3-3x^2+3x-1)} - \frac{2\sqrt{-x^2+1}}{105(x^2-2x+1)} + \frac{2\sqrt{-x^2+1}}{105(x-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(9/2), x, algorithm="maxima")

[Out] 2/7*sqrt(-x^2+1)/(x^4-4*x^3+6*x^2-4*x+1) + 1/35*sqrt(-x^2+1)/(x^3-3*x^2+3*x-1) - 2/105*sqrt(-x^2+1)/(x^2-2*x+1) + 2/105*sqrt(-x^2+1)/(x-1)

mupad [B] time = 0.27, size = 64, normalized size = 1.05

$$\frac{\sqrt{1-x} \left(\frac{13x\sqrt{x+1}}{105} + \frac{23\sqrt{x+1}}{105} - \frac{8x^2\sqrt{x+1}}{105} + \frac{2x^3\sqrt{x+1}}{105} \right)}{x^4-4x^3+6x^2-4x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(1/2)/(1-x)^(9/2), x)

[Out] ((1-x)^(1/2)*((13*x*(x+1)^(1/2))/105 + (23*(x+1)^(1/2))/105 - (8*x^2*(x+1)^(1/2))/105 + (2*x^3*(x+1)^(1/2))/105))/(6*x^2-4*x-4*x^3+x^4+1)

sympy [B] time = 19.92, size = 568, normalized size = 9.31

$$\left\{ \begin{array}{l} \frac{2i(x+1)^{\frac{9}{2}}}{105\sqrt{x-1}(x+1)^4-840\sqrt{x-1}(x+1)^3+2520\sqrt{x-1}(x+1)^2-3360\sqrt{x-1}(x+1)+1680\sqrt{x-1}} - \frac{18i(x+1)^{\frac{7}{2}}}{105\sqrt{x-1}(x+1)^4-840\sqrt{x-1}(x+1)^3+2520\sqrt{x-1}(x+1)^2-3360\sqrt{x-1}(x+1)+1680\sqrt{x-1}} \\ - \frac{2(x+1)^{\frac{9}{2}}}{105\sqrt{1-x}(x+1)^4-840\sqrt{1-x}(x+1)^3+2520\sqrt{1-x}(x+1)^2-3360\sqrt{1-x}(x+1)+1680\sqrt{1-x}} + \frac{18(x+1)^{\frac{7}{2}}}{105\sqrt{1-x}(x+1)^4-840\sqrt{1-x}(x+1)^3+2520\sqrt{1-x}(x+1)^2-3360\sqrt{1-x}(x+1)+1680\sqrt{1-x}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(1/2)/(1-x)**(9/2),x)

[Out] Piecewise((2*I*(x + 1)**(9/2)/(105*sqrt(x - 1)*(x + 1)**4 - 840*sqrt(x - 1)*(x + 1)**3 + 2520*sqrt(x - 1)*(x + 1)**2 - 3360*sqrt(x - 1)*(x + 1) + 1680*sqrt(x - 1)) - 18*I*(x + 1)**(7/2)/(105*sqrt(x - 1)*(x + 1)**4 - 840*sqrt(x - 1)*(x + 1)**3 + 2520*sqrt(x - 1)*(x + 1)**2 - 3360*sqrt(x - 1)*(x + 1) + 1680*sqrt(x - 1)) + 63*I*(x + 1)**(5/2)/(105*sqrt(x - 1)*(x + 1)**4 - 840*sqrt(x - 1)*(x + 1)**3 + 2520*sqrt(x - 1)*(x + 1)**2 - 3360*sqrt(x - 1)*(x + 1) + 1680*sqrt(x - 1)) - 70*I*(x + 1)**(3/2)/(105*sqrt(x - 1)*(x + 1)**4 - 840*sqrt(x - 1)*(x + 1)**3 + 2520*sqrt(x - 1)*(x + 1)**2 - 3360*sqrt(x - 1)*(x + 1) + 1680*sqrt(x - 1)), Abs(x + 1)/2 > 1), (-2*(x + 1)**(9/2)/(105*sqrt(1 - x)*(x + 1)**4 - 840*sqrt(1 - x)*(x + 1)**3 + 2520*sqrt(1 - x)*(x + 1)**2 - 3360*sqrt(1 - x)*(x + 1) + 1680*sqrt(1 - x)) + 18*(x + 1)**(7/2)/(105*sqrt(1 - x)*(x + 1)**4 - 840*sqrt(1 - x)*(x + 1)**3 + 2520*sqrt(1 - x)*(x + 1)**2 - 3360*sqrt(1 - x)*(x + 1) + 1680*sqrt(1 - x)) - 63*(x + 1)**(5/2)/(105*sqrt(1 - x)*(x + 1)**4 - 840*sqrt(1 - x)*(x + 1)**3 + 2520*sqrt(1 - x)*(x + 1)**2 - 3360*sqrt(1 - x)*(x + 1) + 1680*sqrt(1 - x)) + 70*(x + 1)**(3/2)/(105*sqrt(1 - x)*(x + 1)**4 - 840*sqrt(1 - x)*(x + 1)**3 + 2520*sqrt(1 - x)*(x + 1)**2 - 3360*sqrt(1 - x)*(x + 1) + 1680*sqrt(1 - x)), True))

$$3.1073 \quad \int \frac{\sqrt{1+x}}{(1-x)^{11/2}} dx$$

Optimal. Leaf size=81

$$\frac{2(x+1)^{3/2}}{315(1-x)^{3/2}} + \frac{2(x+1)^{3/2}}{105(1-x)^{5/2}} + \frac{(x+1)^{3/2}}{21(1-x)^{7/2}} + \frac{(x+1)^{3/2}}{9(1-x)^{9/2}}$$

[Out] $1/9*(1+x)^{(3/2)}/(1-x)^{(9/2)}+1/21*(1+x)^{(3/2)}/(1-x)^{(7/2)}+2/105*(1+x)^{(3/2)}/(1-x)^{(5/2)}+2/315*(1+x)^{(3/2)}/(1-x)^{(3/2)}$

Rubi [A] time = 0.01, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{2(x+1)^{3/2}}{315(1-x)^{3/2}} + \frac{2(x+1)^{3/2}}{105(1-x)^{5/2}} + \frac{(x+1)^{3/2}}{21(1-x)^{7/2}} + \frac{(x+1)^{3/2}}{9(1-x)^{9/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 + x]/(1 - x)^(11/2), x]

[Out] $(1+x)^{(3/2)}/(9*(1-x)^{(9/2)}) + (1+x)^{(3/2)}/(21*(1-x)^{(7/2)}) + (2*(1+x)^{(3/2)})/(105*(1-x)^{(5/2)}) + (2*(1+x)^{(3/2)})/(315*(1-x)^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{1+x}}{(1-x)^{11/2}} dx &= \frac{(1+x)^{3/2}}{9(1-x)^{9/2}} + \frac{1}{3} \int \frac{\sqrt{1+x}}{(1-x)^{9/2}} dx \\
&= \frac{(1+x)^{3/2}}{9(1-x)^{9/2}} + \frac{(1+x)^{3/2}}{21(1-x)^{7/2}} + \frac{2}{21} \int \frac{\sqrt{1+x}}{(1-x)^{7/2}} dx \\
&= \frac{(1+x)^{3/2}}{9(1-x)^{9/2}} + \frac{(1+x)^{3/2}}{21(1-x)^{7/2}} + \frac{2(1+x)^{3/2}}{105(1-x)^{5/2}} + \frac{2}{105} \int \frac{\sqrt{1+x}}{(1-x)^{5/2}} dx \\
&= \frac{(1+x)^{3/2}}{9(1-x)^{9/2}} + \frac{(1+x)^{3/2}}{21(1-x)^{7/2}} + \frac{2(1+x)^{3/2}}{105(1-x)^{5/2}} + \frac{2(1+x)^{3/2}}{315(1-x)^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.43

$$\frac{(x+1)^{3/2}(-2x^3+12x^2-33x+58)}{315(1-x)^{9/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1+x]/(1-x)^(11/2),x]

[Out] ((1+x)^(3/2)*(58-33*x+12*x^2-2*x^3))/(315*(1-x)^(9/2))

fricas [A] time = 0.44, size = 85, normalized size = 1.05

$$\frac{58x^5 - 290x^4 + 580x^3 - 580x^2 + (2x^4 - 10x^3 + 21x^2 - 25x - 58)\sqrt{x+1}\sqrt{-x+1} + 290x - 58}{315(x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(11/2),x, algorithm="fricas")

[Out] 1/315*(58*x^5 - 290*x^4 + 580*x^3 - 580*x^2 + (2*x^4 - 10*x^3 + 21*x^2 - 25*x - 58)*sqrt(x+1)*sqrt(-x+1) + 290*x - 58)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1)

giac [A] time = 1.12, size = 35, normalized size = 0.43

$$\frac{((2(x+1)(x-8)+63)(x+1)-105)(x+1)^{\frac{3}{2}}\sqrt{-x+1}}{315(x-1)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(11/2),x, algorithm="giac")

[Out] 1/315*((2*(x + 1)*(x - 8) + 63)*(x + 1) - 105)*(x + 1)^(3/2)*sqrt(-x + 1)/(x - 1)^5

maple [A] time = 0.00, size = 30, normalized size = 0.37

$$-\frac{(x+1)^{\frac{3}{2}}(2x^3-12x^2+33x-58)}{315(-x+1)^{\frac{9}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(1/2)/(-x+1)^(11/2),x)

[Out] -1/315*(x+1)^(3/2)*(2*x^3-12*x^2+33*x-58)/(-x+1)^(9/2)

maxima [B] time = 1.35, size = 131, normalized size = 1.62

$$\frac{2\sqrt{-x^2+1}}{9(x^5-5x^4+10x^3-10x^2+5x-1)} - \frac{\sqrt{-x^2+1}}{63(x^4-4x^3+6x^2-4x+1)} + \frac{\sqrt{-x^2+1}}{105(x^3-3x^2+3x-1)} - \frac{2\sqrt{-x^2+1}}{315(x^2-2x+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(11/2),x, algorithm="maxima")

[Out] -2/9*sqrt(-x^2 + 1)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) - 1/63*sqrt(-x^2 + 1)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1) + 1/105*sqrt(-x^2 + 1)/(x^3 - 3*x^2 + 3*x - 1) - 2/315*sqrt(-x^2 + 1)/(x^2 - 2*x + 1) + 2/315*sqrt(-x^2 + 1)/(x - 1)

mupad [B] time = 0.28, size = 80, normalized size = 0.99

$$-\frac{\sqrt{1-x} \left(\frac{5x\sqrt{x+1}}{63} + \frac{58\sqrt{x+1}}{315} - \frac{x^2\sqrt{x+1}}{15} + \frac{2x^3\sqrt{x+1}}{63} - \frac{2x^4\sqrt{x+1}}{315} \right)}{x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(1/2)/(1 - x)^(11/2),x)

[Out] -(((1 - x)^(1/2)*((5*x*(x + 1)^(1/2))/63 + (58*(x + 1)^(1/2))/315 - (x^2*(x + 1)^(1/2))/15 + (2*x^3*(x + 1)^(1/2))/63 - (2*x^4*(x + 1)^(1/2))/315))/(5*x - 10*x^2 + 10*x^3 - 5*x^4 + x^5 - 1)

sympy [B] time = 53.78, size = 1562, normalized size = 19.28

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(1/2)/(1-x)**(11/2),x)

[Out] Piecewise((2*I*(x + 1)**(15/2)/(315*sqrt(x - 1)*(x + 1)**7 - 4410*sqrt(x - 1)*(x + 1)**6 + 26460*sqrt(x - 1)*(x + 1)**5 - 88200*sqrt(x - 1)*(x + 1)**4 + 176400*sqrt(x - 1)*(x + 1)**3 - 211680*sqrt(x - 1)*(x + 1)**2 + 141120*sqrt(x - 1)*(x + 1) - 40320*sqrt(x - 1)) - 30*I*(x + 1)**(13/2)/(315*sqrt(x - 1)*(x + 1)**7 - 4410*sqrt(x - 1)*(x + 1)**6 + 26460*sqrt(x - 1)*(x + 1)**5 - 88200*sqrt(x - 1)*(x + 1)**4 + 176400*sqrt(x - 1)*(x + 1)**3 - 211680*sqrt(x - 1)*(x + 1)**2 + 141120*sqrt(x - 1)*(x + 1) - 40320*sqrt(x - 1)) + 195*I*(x + 1)**(11/2)/(315*sqrt(x - 1)*(x + 1)**7 - 4410*sqrt(x - 1)*(x + 1)**6 + 26460*sqrt(x - 1)*(x + 1)**5 - 88200*sqrt(x - 1)*(x + 1)**4 + 176400*sqrt(x - 1)*(x + 1)**3 - 211680*sqrt(x - 1)*(x + 1)**2 + 141120*sqrt(x - 1)*(x + 1) - 40320*sqrt(x - 1)) - 715*I*(x + 1)**(9/2)/(315*sqrt(x - 1)*(x + 1)**7 - 4410*sqrt(x - 1)*(x + 1)**6 + 26460*sqrt(x - 1)*(x + 1)**5 - 88200*sqrt(x - 1)*(x + 1)**4 + 176400*sqrt(x - 1)*(x + 1)**3 - 211680*sqrt(x - 1)*(x + 1)**2 + 141120*sqrt(x - 1)*(x + 1) - 40320*sqrt(x - 1)) + 1530*I*(x + 1)**(7/2)/(315*sqrt(x - 1)*(x + 1)**7 - 4410*sqrt(x - 1)*(x + 1)**6 + 26460*sqrt(x - 1)*(x + 1)**5 - 88200*sqrt(x - 1)*(x + 1)**4 + 176400*sqrt(x - 1)*(x + 1)**3 - 211680*sqrt(x - 1)*(x + 1)**2 + 141120*sqrt(x - 1)*(x + 1) - 40320*sqrt(x - 1)) - 1764*I*(x + 1)**(5/2)/(315*sqrt(x - 1)*(x + 1)**7 - 4410*sqrt(x - 1)*(x + 1)**6 + 26460*sqrt(x - 1)*(x + 1)**5 - 88200*sqrt(x - 1)*(x + 1)**4 + 176400*sqrt(x - 1)*(x + 1)**3 - 211680*sqrt(x - 1)*(x + 1)**2 + 141120*sqrt(x - 1)*(x + 1) - 40320*sqrt(x - 1)) + 840*I*(x + 1)**(3/2)/(315*sqrt(x - 1)*(x + 1)**7 - 4410*sqrt(x - 1)*(x + 1)**6 + 26460*sqrt(x - 1)*(x + 1)**5 - 88200*sqrt(x - 1)*(x + 1)**4 + 176400*sqrt(x - 1)*(x + 1)**3 - 211680*sqrt(x - 1)*(x + 1)**2 + 141120*sqrt(x - 1)*(x + 1) - 40320*sqrt(x - 1))), Abs(x + 1)/2 > 1), (-2*(x + 1)**(15/2)/(315*sqrt(1 - x)*(x + 1)**7 - 4410*sqrt(1 - x)*(x + 1)**6 + 26460*sqrt(1 - x)*(x + 1)**5 - 88200*sqrt(1 - x)*(x + 1)**4 + 176400*sqrt(1 - x)*(x + 1)**3 - 211680*sqrt(1 - x)*(x + 1)**2 + 141120*sqrt(1 - x)*(x + 1) - 40320*sqrt(1 - x)) + 30*(x + 1)**(13/2)/(315*sqrt(1 - x)*(x + 1)**7 - 4410*sqrt(1 - x)*(x + 1)**6 + 26460*sqrt(1 - x)*(x + 1)**5 - 88200*sqrt(1 - x)*(x + 1)**4 + 176400*sqrt(1 - x)*(x + 1)**3 - 211680*sqrt(1 - x)*(x + 1)**2 + 141120*sqrt(1 - x)*(x + 1) - 40320*sqrt(1 - x)) - 195*(x + 1)**(11/2)/(315*sqrt(1 - x)*(x + 1)**7 - 4410*sqrt(1 - x)*(x + 1)**6 + 26460*sqrt(1 - x)*(x + 1)**5 - 88200*sqrt(1 - x)*(x + 1)**4 + 176400*sqrt(1 - x)*(x + 1)**3 - 211680*sqrt(1 - x)*(x + 1)**2 + 141120*sqrt(1 - x)*(x + 1) - 40320*sqrt(1 - x)) + 715*(x + 1)**(9/2)/(315*sqrt(1 - x)*(x + 1)**7 - 4410*sqrt(1 - x)*(x + 1)**6 + 26460*sqrt(1 - x)*(x + 1)**5 - 88200*sqrt(1 - x)*(x + 1)**4 + 176400*sqrt(1 - x)*(x + 1)**3 - 211680*sqrt(1 - x)*(x + 1)**2 + 141120*sqrt(1 - x)*(x + 1) - 40320*sqrt(1 - x)) - 1530*(x + 1)**(7/2)/(315*sqrt(1 - x)*(x + 1)**7 - 4410*sqrt(1 - x)*(x + 1)**6 + 26460*sqrt(1 - x)*(x + 1)**5 - 88200*sqrt(1 - x)*(x + 1)**4 + 176400*sqrt(1 - x)*(x + 1)**3 - 211680*sqrt(1 - x)*(x + 1)**2 + 141120*sqrt(1 - x)

```

)*(x + 1) - 40320*sqrt(1 - x)) + 1764*(x + 1)**(5/2)/(315*sqrt(1 - x)*(x +
1)**7 - 4410*sqrt(1 - x)*(x + 1)**6 + 26460*sqrt(1 - x)*(x + 1)**5 - 88200*
sqrt(1 - x)*(x + 1)**4 + 176400*sqrt(1 - x)*(x + 1)**3 - 211680*sqrt(1 - x)
*(x + 1)**2 + 141120*sqrt(1 - x)*(x + 1) - 40320*sqrt(1 - x)) - 840*(x + 1)
**(3/2)/(315*sqrt(1 - x)*(x + 1)**7 - 4410*sqrt(1 - x)*(x + 1)**6 + 26460*s
qrt(1 - x)*(x + 1)**5 - 88200*sqrt(1 - x)*(x + 1)**4 + 176400*sqrt(1 - x)*(
x + 1)**3 - 211680*sqrt(1 - x)*(x + 1)**2 + 141120*sqrt(1 - x)*(x + 1) - 40
320*sqrt(1 - x)), True))

```

$$3.1074 \quad \int \frac{\sqrt{1+x}}{(1-x)^{13/2}} dx$$

Optimal. Leaf size=101

$$\frac{8(x+1)^{3/2}}{3465(1-x)^{3/2}} + \frac{8(x+1)^{3/2}}{1155(1-x)^{5/2}} + \frac{4(x+1)^{3/2}}{231(1-x)^{7/2}} + \frac{4(x+1)^{3/2}}{99(1-x)^{9/2}} + \frac{(x+1)^{3/2}}{11(1-x)^{11/2}}$$

[Out] 1/11*(1+x)^(3/2)/(1-x)^(11/2)+4/99*(1+x)^(3/2)/(1-x)^(9/2)+4/231*(1+x)^(3/2)/(1-x)^(7/2)+8/1155*(1+x)^(3/2)/(1-x)^(5/2)+8/3465*(1+x)^(3/2)/(1-x)^(3/2)

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{8(x+1)^{3/2}}{3465(1-x)^{3/2}} + \frac{8(x+1)^{3/2}}{1155(1-x)^{5/2}} + \frac{4(x+1)^{3/2}}{231(1-x)^{7/2}} + \frac{4(x+1)^{3/2}}{99(1-x)^{9/2}} + \frac{(x+1)^{3/2}}{11(1-x)^{11/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 + x]/(1 - x)^(13/2), x]

[Out] (1 + x)^(3/2)/(11*(1 - x)^(11/2)) + (4*(1 + x)^(3/2))/(99*(1 - x)^(9/2)) + (4*(1 + x)^(3/2))/(231*(1 - x)^(7/2)) + (8*(1 + x)^(3/2))/(1155*(1 - x)^(5/2)) + (8*(1 + x)^(3/2))/(3465*(1 - x)^(3/2))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{1+x}}{(1-x)^{13/2}} dx &= \frac{(1+x)^{3/2}}{11(1-x)^{11/2}} + \frac{4}{11} \int \frac{\sqrt{1+x}}{(1-x)^{11/2}} dx \\
&= \frac{(1+x)^{3/2}}{11(1-x)^{11/2}} + \frac{4(1+x)^{3/2}}{99(1-x)^{9/2}} + \frac{4}{33} \int \frac{\sqrt{1+x}}{(1-x)^{9/2}} dx \\
&= \frac{(1+x)^{3/2}}{11(1-x)^{11/2}} + \frac{4(1+x)^{3/2}}{99(1-x)^{9/2}} + \frac{4(1+x)^{3/2}}{231(1-x)^{7/2}} + \frac{8}{231} \int \frac{\sqrt{1+x}}{(1-x)^{7/2}} dx \\
&= \frac{(1+x)^{3/2}}{11(1-x)^{11/2}} + \frac{4(1+x)^{3/2}}{99(1-x)^{9/2}} + \frac{4(1+x)^{3/2}}{231(1-x)^{7/2}} + \frac{8(1+x)^{3/2}}{1155(1-x)^{5/2}} + \frac{8 \int \frac{\sqrt{1+x}}{(1-x)^{5/2}} dx}{1155} \\
&= \frac{(1+x)^{3/2}}{11(1-x)^{11/2}} + \frac{4(1+x)^{3/2}}{99(1-x)^{9/2}} + \frac{4(1+x)^{3/2}}{231(1-x)^{7/2}} + \frac{8(1+x)^{3/2}}{1155(1-x)^{5/2}} + \frac{8(1+x)^{3/2}}{3465(1-x)^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 40, normalized size = 0.40

$$\frac{(x+1)^{3/2} (8x^4 - 56x^3 + 180x^2 - 364x + 547)}{3465(1-x)^{11/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 + x]/(1 - x)^(13/2), x]

[Out] ((1 + x)^(3/2)*(547 - 364*x + 180*x^2 - 56*x^3 + 8*x^4))/(3465*(1 - x)^(11/2))

fricas [A] time = 0.45, size = 100, normalized size = 0.99

$$\frac{547x^6 - 3282x^5 + 8205x^4 - 10940x^3 + 8205x^2 + (8x^5 - 48x^4 + 124x^3 - 184x^2 + 183x + 547)\sqrt{x+1}\sqrt{-x-1}}{3465(x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(13/2), x, algorithm="fricas")

[Out] 1/3465*(547*x^6 - 3282*x^5 + 8205*x^4 - 10940*x^3 + 8205*x^2 + (8*x^5 - 48*x^4 + 124*x^3 - 184*x^2 + 183*x + 547)*sqrt(x + 1)*sqrt(-x + 1) - 3282*x + 547)/(x^6 - 6*x^5 + 15*x^4 - 20*x^3 + 15*x^2 - 6*x + 1)

giac [A] time = 1.36, size = 42, normalized size = 0.42

$$\frac{4((2(x+1)(x-10)+99)(x+1)-231)(x+1)+1155)(x+1)^2\sqrt{-x+1}}{3465(x-1)^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(13/2),x, algorithm="giac")

[Out] 1/3465*(4*((2*(x + 1)*(x - 10) + 99)*(x + 1) - 231)*(x + 1) + 1155)*(x + 1)^(3/2)*sqrt(-x + 1)/(x - 1)^6

maple [A] time = 0.00, size = 35, normalized size = 0.35

$$\frac{(x+1)^{\frac{3}{2}}(8x^4 - 56x^3 + 180x^2 - 364x + 547)}{3465(-x+1)^{\frac{11}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(1/2)/(-x+1)^(13/2),x)

[Out] 1/3465*(x+1)^(3/2)*(8*x^4-56*x^3+180*x^2-364*x+547)/(-x+1)^(11/2)

maxima [B] time = 1.32, size = 172, normalized size = 1.70

$$\frac{2\sqrt{-x^2+1}}{11(x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1)} + \frac{\sqrt{-x^2+1}}{99(x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1)} - \frac{4\sqrt{-x^2+1}}{693(x^4 - 4x^3 + 6x^2 - 4x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(1/2)/(1-x)^(13/2),x, algorithm="maxima")

[Out] 2/11*sqrt(-x^2 + 1)/(x^6 - 6*x^5 + 15*x^4 - 20*x^3 + 15*x^2 - 6*x + 1) + 1/99*sqrt(-x^2 + 1)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) - 4/693*sqrt(-x^2 + 1)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1) + 4/1155*sqrt(-x^2 + 1)/(x^3 - 3*x^2 + 3*x - 1) - 8/3465*sqrt(-x^2 + 1)/(x^2 - 2*x + 1) + 8/3465*sqrt(-x^2 + 1)/(x - 1)

mupad [B] time = 0.29, size = 94, normalized size = 0.93

$$\frac{\sqrt{1-x} \left(\frac{61x\sqrt{x+1}}{1155} + \frac{547\sqrt{x+1}}{3465} - \frac{184x^2\sqrt{x+1}}{3465} + \frac{124x^3\sqrt{x+1}}{3465} - \frac{16x^4\sqrt{x+1}}{1155} + \frac{8x^5\sqrt{x+1}}{3465} \right)}{x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(1/2)/(1 - x)^(13/2),x)

[Out] ((1 - x)^(1/2)*((61*x*(x + 1)^(1/2))/1155 + (547*(x + 1)^(1/2))/3465 - (184*x^2*(x + 1)^(1/2))/3465 + (124*x^3*(x + 1)^(1/2))/3465 - (16*x^4*(x + 1)^(1/2))/1155 + (8*x^5*(x + 1)^(1/2))/3465))/(15*x^2 - 6*x - 20*x^3 + 15*x^4 - 6*x^5 + x^6 + 1)


```

**4 + 146361600*sqrt(x - 1)*(x + 1)**3 - 97574400*sqrt(x - 1)*(x + 1)**2 +
39029760*sqrt(x - 1)*(x + 1) - 7096320*sqrt(x - 1)) - 488224*I*(x + 1)**(9/
2)/(3465*sqrt(x - 1)*(x + 1)**11 - 76230*sqrt(x - 1)*(x + 1)**10 + 762300*s
qrt(x - 1)*(x + 1)**9 - 4573800*sqrt(x - 1)*(x + 1)**8 + 18295200*sqrt(x -
1)*(x + 1)**7 - 51226560*sqrt(x - 1)*(x + 1)**6 + 102453120*sqrt(x - 1)*(x
+ 1)**5 - 146361600*sqrt(x - 1)*(x + 1)**4 + 146361600*sqrt(x - 1)*(x + 1)*
*3 - 97574400*sqrt(x - 1)*(x + 1)**2 + 39029760*sqrt(x - 1)*(x + 1) - 70963
20*sqrt(x - 1)) + 479952*I*(x + 1)**(7/2)/(3465*sqrt(x - 1)*(x + 1)**11 - 7
6230*sqrt(x - 1)*(x + 1)**10 + 762300*sqrt(x - 1)*(x + 1)**9 - 4573800*sqrt
(x - 1)*(x + 1)**8 + 18295200*sqrt(x - 1)*(x + 1)**7 - 51226560*sqrt(x - 1)
*(x + 1)**6 + 102453120*sqrt(x - 1)*(x + 1)**5 - 146361600*sqrt(x - 1)*(x +
1)**4 + 146361600*sqrt(x - 1)*(x + 1)**3 - 97574400*sqrt(x - 1)*(x + 1)**2
+ 39029760*sqrt(x - 1)*(x + 1) - 7096320*sqrt(x - 1)) - 280896*I*(x + 1)**
(5/2)/(3465*sqrt(x - 1)*(x + 1)**11 - 76230*sqrt(x - 1)*(x + 1)**10 + 76230
0*sqrt(x - 1)*(x + 1)**9 - 4573800*sqrt(x - 1)*(x + 1)**8 + 18295200*sqrt(x
- 1)*(x + 1)**7 - 51226560*sqrt(x - 1)*(x + 1)**6 + 102453120*sqrt(x - 1)*
(x + 1)**5 - 146361600*sqrt(x - 1)*(x + 1)**4 + 146361600*sqrt(x - 1)*(x +
1)**3 - 97574400*sqrt(x - 1)*(x + 1)**2 + 39029760*sqrt(x - 1)*(x + 1) - 70
96320*sqrt(x - 1)) + 73920*I*(x + 1)**(3/2)/(3465*sqrt(x - 1)*(x + 1)**11 -
76230*sqrt(x - 1)*(x + 1)**10 + 762300*sqrt(x - 1)*(x + 1)**9 - 4573800*sq
rt(x - 1)*(x + 1)**8 + 18295200*sqrt(x - 1)*(x + 1)**7 - 51226560*sqrt(x -
1)*(x + 1)**6 + 102453120*sqrt(x - 1)*(x + 1)**5 - 146361600*sqrt(x - 1)*(x
+ 1)**4 + 146361600*sqrt(x - 1)*(x + 1)**3 - 97574400*sqrt(x - 1)*(x + 1)*
*2 + 39029760*sqrt(x - 1)*(x + 1) - 7096320*sqrt(x - 1)), Abs(x + 1)/2 > 1)
, (-8*(x + 1)**(23/2)/(3465*sqrt(1 - x)*(x + 1)**11 - 76230*sqrt(1 - x)*(x
+ 1)**10 + 762300*sqrt(1 - x)*(x + 1)**9 - 4573800*sqrt(1 - x)*(x + 1)**8 +
18295200*sqrt(1 - x)*(x + 1)**7 - 51226560*sqrt(1 - x)*(x + 1)**6 + 102453
120*sqrt(1 - x)*(x + 1)**5 - 146361600*sqrt(1 - x)*(x + 1)**4 + 146361600*s
qrt(1 - x)*(x + 1)**3 - 97574400*sqrt(1 - x)*(x + 1)**2 + 39029760*sqrt(1 -
x)*(x + 1) - 7096320*sqrt(1 - x)) + 184*(x + 1)**(21/2)/(3465*sqrt(1 - x)*
(x + 1)**11 - 76230*sqrt(1 - x)*(x + 1)**10 + 762300*sqrt(1 - x)*(x + 1)**9
- 4573800*sqrt(1 - x)*(x + 1)**8 + 18295200*sqrt(1 - x)*(x + 1)**7 - 51226
560*sqrt(1 - x)*(x + 1)**6 + 102453120*sqrt(1 - x)*(x + 1)**5 - 146361600*s
qrt(1 - x)*(x + 1)**4 + 146361600*sqrt(1 - x)*(x + 1)**3 - 97574400*sqrt(1
- x)*(x + 1)**2 + 39029760*sqrt(1 - x)*(x + 1) - 7096320*sqrt(1 - x)) - 193
2*(x + 1)**(19/2)/(3465*sqrt(1 - x)*(x + 1)**11 - 76230*sqrt(1 - x)*(x + 1)
**10 + 762300*sqrt(1 - x)*(x + 1)**9 - 4573800*sqrt(1 - x)*(x + 1)**8 + 182
95200*sqrt(1 - x)*(x + 1)**7 - 51226560*sqrt(1 - x)*(x + 1)**6 + 102453120*
sqrt(1 - x)*(x + 1)**5 - 146361600*sqrt(1 - x)*(x + 1)**4 + 146361600*sqrt(
1 - x)*(x + 1)**3 - 97574400*sqrt(1 - x)*(x + 1)**2 + 39029760*sqrt(1 - x)*
(x + 1) - 7096320*sqrt(1 - x)) + 12236*(x + 1)**(17/2)/(3465*sqrt(1 - x)*(x
+ 1)**11 - 76230*sqrt(1 - x)*(x + 1)**10 + 762300*sqrt(1 - x)*(x + 1)**9 -
4573800*sqrt(1 - x)*(x + 1)**8 + 18295200*sqrt(1 - x)*(x + 1)**7 - 5122656
0*sqrt(1 - x)*(x + 1)**6 + 102453120*sqrt(1 - x)*(x + 1)**5 - 146361600*sqr
t(1 - x)*(x + 1)**4 + 146361600*sqrt(1 - x)*(x + 1)**3 - 97574400*sqrt(1 -

```

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x)*(x + 1)**2 + 39029760*sqrt(1 - x)*(x + 1) - 7096320*sqrt(1 - x)) - 52003
*(x + 1)**(15/2)/(3465*sqrt(1 - x)*(x + 1)**11 - 76230*sqrt(1 - x)*(x + 1)*
*10 + 762300*sqrt(1 - x)*(x + 1)**9 - 4573800*sqrt(1 - x)*(x + 1)**8 + 1829
5200*sqrt(1 - x)*(x + 1)**7 - 51226560*sqrt(1 - x)*(x + 1)**6 + 102453120*s
qrt(1 - x)*(x + 1)**5 - 146361600*sqrt(1 - x)*(x + 1)**4 + 146361600*sqrt(1
- x)*(x + 1)**3 - 97574400*sqrt(1 - x)*(x + 1)**2 + 39029760*sqrt(1 - x)*(
x + 1) - 7096320*sqrt(1 - x)) + 155316*(x + 1)**(13/2)/(3465*sqrt(1 - x)*(x
+ 1)**11 - 76230*sqrt(1 - x)*(x + 1)**10 + 762300*sqrt(1 - x)*(x + 1)**9 -
4573800*sqrt(1 - x)*(x + 1)**8 + 18295200*sqrt(1 - x)*(x + 1)**7 - 5122656
0*sqrt(1 - x)*(x + 1)**6 + 102453120*sqrt(1 - x)*(x + 1)**5 - 146361600*sqr
t(1 - x)*(x + 1)**4 + 146361600*sqrt(1 - x)*(x + 1)**3 - 97574400*sqrt(1 -
x)*(x + 1)**2 + 39029760*sqrt(1 - x)*(x + 1) - 7096320*sqrt(1 - x)) - 32958
8*(x + 1)**(11/2)/(3465*sqrt(1 - x)*(x + 1)**11 - 76230*sqrt(1 - x)*(x + 1)
**10 + 762300*sqrt(1 - x)*(x + 1)**9 - 4573800*sqrt(1 - x)*(x + 1)**8 + 182
95200*sqrt(1 - x)*(x + 1)**7 - 51226560*sqrt(1 - x)*(x + 1)**6 + 102453120*
sqrt(1 - x)*(x + 1)**5 - 146361600*sqrt(1 - x)*(x + 1)**4 + 146361600*sqrt(
1 - x)*(x + 1)**3 - 97574400*sqrt(1 - x)*(x + 1)**2 + 39029760*sqrt(1 - x)*
(x + 1) - 7096320*sqrt(1 - x)) + 488224*(x + 1)**(9/2)/(3465*sqrt(1 - x)*(x
+ 1)**11 - 76230*sqrt(1 - x)*(x + 1)**10 + 762300*sqrt(1 - x)*(x + 1)**9 -
4573800*sqrt(1 - x)*(x + 1)**8 + 18295200*sqrt(1 - x)*(x + 1)**7 - 5122656
0*sqrt(1 - x)*(x + 1)**6 + 102453120*sqrt(1 - x)*(x + 1)**5 - 146361600*sqr
t(1 - x)*(x + 1)**4 + 146361600*sqrt(1 - x)*(x + 1)**3 - 97574400*sqrt(1 -
x)*(x + 1)**2 + 39029760*sqrt(1 - x)*(x + 1) - 7096320*sqrt(1 - x)) - 47995
2*(x + 1)**(7/2)/(3465*sqrt(1 - x)*(x + 1)**11 - 76230*sqrt(1 - x)*(x + 1)*
*10 + 762300*sqrt(1 - x)*(x + 1)**9 - 4573800*sqrt(1 - x)*(x + 1)**8 + 1829
5200*sqrt(1 - x)*(x + 1)**7 - 51226560*sqrt(1 - x)*(x + 1)**6 + 102453120*s
qrt(1 - x)*(x + 1)**5 - 146361600*sqrt(1 - x)*(x + 1)**4 + 146361600*sqrt(1
- x)*(x + 1)**3 - 97574400*sqrt(1 - x)*(x + 1)**2 + 39029760*sqrt(1 - x)*(
x + 1) - 7096320*sqrt(1 - x)) + 280896*(x + 1)**(5/2)/(3465*sqrt(1 - x)*(x
+ 1)**11 - 76230*sqrt(1 - x)*(x + 1)**10 + 762300*sqrt(1 - x)*(x + 1)**9 -
4573800*sqrt(1 - x)*(x + 1)**8 + 18295200*sqrt(1 - x)*(x + 1)**7 - 51226560
*sqrt(1 - x)*(x + 1)**6 + 102453120*sqrt(1 - x)*(x + 1)**5 - 146361600*sqrt
(1 - x)*(x + 1)**4 + 146361600*sqrt(1 - x)*(x + 1)**3 - 97574400*sqrt(1 - x
)*(x + 1)**2 + 39029760*sqrt(1 - x)*(x + 1) - 7096320*sqrt(1 - x)) - 73920*
(x + 1)**(3/2)/(3465*sqrt(1 - x)*(x + 1)**11 - 76230*sqrt(1 - x)*(x + 1)**1
0 + 762300*sqrt(1 - x)*(x + 1)**9 - 4573800*sqrt(1 - x)*(x + 1)**8 + 182952
00*sqrt(1 - x)*(x + 1)**7 - 51226560*sqrt(1 - x)*(x + 1)**6 + 102453120*sqr
t(1 - x)*(x + 1)**5 - 146361600*sqrt(1 - x)*(x + 1)**4 + 146361600*sqrt(1 -
x)*(x + 1)**3 - 97574400*sqrt(1 - x)*(x + 1)**2 + 39029760*sqrt(1 - x)*(x
+ 1) - 7096320*sqrt(1 - x)), True))

```

3.1075 $\int (1-x)^{9/2}(1+x)^{3/2} dx$

Optimal. Leaf size=109

$$\frac{1}{7}(x+1)^{5/2}(1-x)^{9/2} + \frac{3}{14}(x+1)^{5/2}(1-x)^{7/2} + \frac{3}{10}(x+1)^{5/2}(1-x)^{5/2} + \frac{3}{8}x(x+1)^{3/2}(1-x)^{3/2} + \frac{9}{16}x\sqrt{x+1}\sqrt{1-x} + \frac{9}{16}\sin^{-1}(x)$$

[Out] $3/8*(1-x)^{(3/2)}*x*(1+x)^{(3/2)}+3/10*(1-x)^{(5/2)}*(1+x)^{(5/2)}+3/14*(1-x)^{(7/2)}*(1+x)^{(5/2)}+1/7*(1-x)^{(9/2)}*(1+x)^{(5/2)}+9/16*\arcsin(x)+9/16*x*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 109, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$\frac{1}{7}(x+1)^{5/2}(1-x)^{9/2} + \frac{3}{14}(x+1)^{5/2}(1-x)^{7/2} + \frac{3}{10}(x+1)^{5/2}(1-x)^{5/2} + \frac{3}{8}x(x+1)^{3/2}(1-x)^{3/2} + \frac{9}{16}x\sqrt{x+1}\sqrt{1-x} + \frac{9}{16}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(1-x)^{(9/2)}*(1+x)^{(3/2)}, x]$

[Out] $(9*\text{Sqrt}[1-x]*x*\text{Sqrt}[1+x])/16 + (3*(1-x)^{(3/2)}*x*(1+x)^{(3/2)})/8 + (3*(1-x)^{(5/2)}*(1+x)^{(5/2)})/10 + (3*(1-x)^{(7/2)}*(1+x)^{(5/2)})/14 + ((1-x)^{(9/2)}*(1+x)^{(5/2)})/7 + (9*\text{ArcSin}[x])/16$

Rule 38

$\text{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(m_+)}, x_Symbol] :> \text{Simp}[(x_+*(a_+ + b_+*x_+)^{(m_+)}*(c_+ + d_+*x_+)^{(m_+)}/(2*m_+ + 1), x] + \text{Dist}[(2*a_+*c_+*m_+)/(2*m_+ + 1), \text{Int}[(a_+ + b_+*x_+)^{(m_+ - 1)}*(c_+ + d_+*x_+)^{(m_+ - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

$\text{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(m_+)}, x_Symbol] :> \text{Int}[(a_+*c_+ + b_+*d_+*x_+^2)^{(m_+)}, x] /;$ FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

$\text{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] :> \text{Simp}[(a_+ + b_+*x_+)^{(m_+ + 1)}*(c_+ + d_+*x_+)^{(n_+)}/(b_+(m_+ + n_+ + 1)), x] + \text{Dist}[(2*c_+*n_+)/(m_+ + n_+ + 1), \text{Int}[(a_+ + b_+*x_+)^{(m_+)}*(c_+ + d_+*x_+)^{(n_+ - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int (1-x)^{9/2}(1+x)^{3/2} dx &= \frac{1}{7}(1-x)^{9/2}(1+x)^{5/2} + \frac{9}{7} \int (1-x)^{7/2}(1+x)^{3/2} dx \\
 &= \frac{3}{14}(1-x)^{7/2}(1+x)^{5/2} + \frac{1}{7}(1-x)^{9/2}(1+x)^{5/2} + \frac{3}{2} \int (1-x)^{5/2}(1+x)^{3/2} dx \\
 &= \frac{3}{10}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{14}(1-x)^{7/2}(1+x)^{5/2} + \frac{1}{7}(1-x)^{9/2}(1+x)^{5/2} + \frac{3}{2} \int (1-x)^{3/2}(1+x)^{3/2} dx \\
 &= \frac{3}{8}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{10}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{14}(1-x)^{7/2}(1+x)^{5/2} + \frac{1}{7}(1-x)^{9/2}(1+x)^{5/2} \\
 &= \frac{9}{16}\sqrt{1-x}x\sqrt{1+x} + \frac{3}{8}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{10}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{14}(1-x)^{7/2}(1+x)^{5/2} \\
 &= \frac{9}{16}\sqrt{1-x}x\sqrt{1+x} + \frac{3}{8}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{10}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{14}(1-x)^{7/2}(1+x)^{5/2} \\
 &= \frac{9}{16}\sqrt{1-x}x\sqrt{1+x} + \frac{3}{8}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{10}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{14}(1-x)^{7/2}(1+x)^{5/2}
 \end{aligned}$$

Mathematica [A] time = 0.06, size = 66, normalized size = 0.61

$$\frac{1}{560}\sqrt{1-x^2} (80x^6 - 280x^5 + 208x^4 + 350x^3 - 656x^2 + 245x + 368) - \frac{9}{8} \sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(9/2)*(1 + x)^(3/2), x]

[Out] (Sqrt[1 - x^2]*(368 + 245*x - 656*x^2 + 350*x^3 + 208*x^4 - 280*x^5 + 80*x^6))/560 - (9*ArcSin[Sqrt[1 - x]/Sqrt[2]])/8

fricas [A] time = 0.43, size = 67, normalized size = 0.61

$$\frac{1}{560} (80x^6 - 280x^5 + 208x^4 + 350x^3 - 656x^2 + 245x + 368) \sqrt{x+1} \sqrt{-x+1} - \frac{9}{8} \arctan\left(\frac{\sqrt{x+1} \sqrt{-x+1}}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(9/2)*(1+x)^(3/2), x, algorithm="fricas")

[Out] $\frac{1}{560}(80x^6 - 280x^5 + 208x^4 + 350x^3 - 656x^2 + 245x + 368)\sqrt{x+1}\sqrt{-x+1} - \frac{9}{8}\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1} - 1}{x}\right)$

giac [B] time = 1.26, size = 237, normalized size = 2.17

$$\frac{1}{1680} \left((2((4(5(6x - 37)(x + 1) + 661)(x + 1) - 4551)(x + 1) + 4781)(x + 1) - 6335)(x + 1) + 2835)\sqrt{x+1}\sqrt{-x+1} - \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(9/2)*(1+x)^(3/2),x, algorithm="giac")`

[Out] $\frac{1}{1680} \left((2((4(5(6x - 37)(x + 1) + 661)(x + 1) - 4551)(x + 1) + 4781)(x + 1) - 6335)(x + 1) + 2835)\sqrt{x+1}\sqrt{-x+1} - \frac{1}{120} \left((2((4(5x - 26)(x + 1) + 321)(x + 1) - 451)(x + 1) + 745)(x + 1) - 405)\sqrt{x+1}\sqrt{-x+1} - \frac{1}{120} \left((2(3(4x - 17)(x + 1) + 133)(x + 1) - 295)(x + 1) + 195)\sqrt{x+1}\sqrt{-x+1} + \frac{1}{6} \left((2(3x - 10)(x + 1) + 43)(x + 1) - 39)\sqrt{x+1}\sqrt{-x+1} - \frac{1}{6} \left((2x - 5)(x + 1) + 9)\sqrt{x+1}\sqrt{-x+1} - \sqrt{x+1}(x - 2)\sqrt{-x+1} + \sqrt{x+1}\sqrt{-x+1} + \frac{9}{8}\arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right) \right) \right) \right)$

maple [A] time = 0.00, size = 127, normalized size = 1.17

$$\frac{9\sqrt{(x+1)(-x+1)} \arcsin(x)}{16\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{9}{2}}(x+1)^{\frac{5}{2}}}{7} + \frac{3(-x+1)^{\frac{7}{2}}(x+1)^{\frac{5}{2}}}{14} + \frac{3(-x+1)^{\frac{5}{2}}(x+1)^{\frac{5}{2}}}{10} + \frac{3(-x+1)^{\frac{3}{2}}(x+1)^{\frac{5}{2}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-x+1)^(9/2)*(x+1)^(3/2),x)`

[Out] $\frac{1}{7}(-x+1)^{\frac{9}{2}}(x+1)^{\frac{5}{2}} + \frac{3}{14}(-x+1)^{\frac{7}{2}}(x+1)^{\frac{5}{2}} + \frac{3}{10}(-x+1)^{\frac{5}{2}}(x+1)^{\frac{5}{2}} + \frac{3}{8}(-x+1)^{\frac{3}{2}}(x+1)^{\frac{5}{2}} - \frac{3}{16}(-x+1)^{\frac{1}{2}}(x+1)^{\frac{5}{2}} - \frac{3}{16}(-x+1)^{\frac{1}{2}}(x+1)^{\frac{3}{2}} - \frac{9}{16}(-x+1)^{\frac{1}{2}}(x+1)^{\frac{1}{2}} + \frac{9}{16}((x+1)(-x+1))^{\frac{1}{2}} / ((x+1)^{\frac{1}{2}}(-x+1)^{\frac{1}{2}}) \arcsin(x)$

maxima [A] time = 3.03, size = 66, normalized size = 0.61

$$\frac{1}{7}(-x^2+1)^{\frac{5}{2}}x^2 - \frac{1}{2}(-x^2+1)^{\frac{5}{2}}x + \frac{23}{35}(-x^2+1)^{\frac{5}{2}} + \frac{3}{8}(-x^2+1)^{\frac{3}{2}}x + \frac{9}{16}\sqrt{-x^2+1}x + \frac{9}{16}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(9/2)*(1+x)^(3/2),x, algorithm="maxima")`

[Out] $\frac{1}{7}(-x^2+1)^{\frac{5}{2}}x^2 - \frac{1}{2}(-x^2+1)^{\frac{5}{2}}x + \frac{23}{35}(-x^2+1)^{\frac{5}{2}} + \frac{3}{8}(-x^2+1)^{\frac{3}{2}}x + \frac{9}{16}\sqrt{-x^2+1}x + \frac{9}{16}\arcsin(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{9/2} (x+1)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(9/2)*(x + 1)^(3/2), x)`

[Out] `int((1 - x)^(9/2)*(x + 1)^(3/2), x)`

sympy [A] time = 75.20, size = 325, normalized size = 2.98

$$\left\{ \begin{array}{l} -\frac{9i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{8} + \frac{i(x+1)^{15/2}}{7\sqrt{x-1}} - \frac{23i(x+1)^{13/2}}{14\sqrt{x-1}} + \frac{541i(x+1)^{11/2}}{70\sqrt{x-1}} - \frac{5249i(x+1)^9}{280\sqrt{x-1}} + \frac{6653i(x+1)^7}{280\sqrt{x-1}} - \frac{1027i(x+1)^5}{80\sqrt{x-1}} - \frac{3i(x+1)^3}{16\sqrt{x-1}} + \frac{9i\sqrt{x+1}}{8\sqrt{x-1}} \\ \frac{9 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{8} - \frac{(x+1)^{15/2}}{7\sqrt{1-x}} + \frac{23(x+1)^{13/2}}{14\sqrt{1-x}} - \frac{541(x+1)^{11/2}}{70\sqrt{1-x}} + \frac{5249(x+1)^9}{280\sqrt{1-x}} - \frac{6653(x+1)^7}{280\sqrt{1-x}} + \frac{1027(x+1)^5}{80\sqrt{1-x}} + \frac{3(x+1)^3}{16\sqrt{1-x}} - \frac{9\sqrt{x+1}}{8\sqrt{1-x}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(9/2)*(1+x)**(3/2), x)`

[Out] `Piecewise((-9*I*acosh(sqrt(2)*sqrt(x + 1)/2)/8 + I*(x + 1)**(15/2)/(7*sqrt(x - 1)) - 23*I*(x + 1)**(13/2)/(14*sqrt(x - 1)) + 541*I*(x + 1)**(11/2)/(70*sqrt(x - 1)) - 5249*I*(x + 1)**(9/2)/(280*sqrt(x - 1)) + 6653*I*(x + 1)**(7/2)/(280*sqrt(x - 1)) - 1027*I*(x + 1)**(5/2)/(80*sqrt(x - 1)) - 3*I*(x + 1)**(3/2)/(16*sqrt(x - 1)) + 9*I*sqrt(x + 1)/(8*sqrt(x - 1)), Abs(x + 1)/2 > 1), (9*asin(sqrt(2)*sqrt(x + 1)/2)/8 - (x + 1)**(15/2)/(7*sqrt(1 - x)) + 23*(x + 1)**(13/2)/(14*sqrt(1 - x)) - 541*(x + 1)**(11/2)/(70*sqrt(1 - x)) + 5249*(x + 1)**(9/2)/(280*sqrt(1 - x)) - 6653*(x + 1)**(7/2)/(280*sqrt(1 - x)) + 1027*(x + 1)**(5/2)/(80*sqrt(1 - x)) + 3*(x + 1)**(3/2)/(16*sqrt(1 - x)) - 9*sqrt(x + 1)/(8*sqrt(1 - x)), True))`

3.1076 $\int (1-x)^{7/2}(1+x)^{3/2} dx$

Optimal. Leaf size=89

$$\frac{1}{6}(x+1)^{5/2}(1-x)^{7/2} + \frac{7}{30}(x+1)^{5/2}(1-x)^{5/2} + \frac{7}{24}x(x+1)^{3/2}(1-x)^{3/2} + \frac{7}{16}x\sqrt{x+1}\sqrt{1-x} + \frac{7}{16}\sin^{-1}(x)$$

[Out] 7/24*(1-x)^(3/2)*x*(1+x)^(3/2)+7/30*(1-x)^(5/2)*(1+x)^(5/2)+1/6*(1-x)^(7/2)*
*(1+x)^(5/2)+7/16*arcsin(x)+7/16*x*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 89, normalized size of antiderivative = 1.00,
number of steps used = 6, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} =$
0.235, Rules used = {49, 38, 41, 216}

$$\frac{1}{6}(x+1)^{5/2}(1-x)^{7/2} + \frac{7}{30}(x+1)^{5/2}(1-x)^{5/2} + \frac{7}{24}x(x+1)^{3/2}(1-x)^{3/2} + \frac{7}{16}x\sqrt{x+1}\sqrt{1-x} + \frac{7}{16}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(7/2)*(1 + x)^(3/2), x]

[Out] (7*Sqrt[1 - x]*x*Sqrt[1 + x])/16 + (7*(1 - x)^(3/2)*x*(1 + x)^(3/2))/24 + (7*(1 - x)^(5/2)*(1 + x)^(5/2))/30 + ((1 - x)^(7/2)*(1 + x)^(5/2))/6 + (7*ArcSin[x])/16

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> Simp[(x*(a + b*x)^m*(c + d*x)^m)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(m - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(2*c*n)/(m + n + 1), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
 \int (1-x)^{7/2}(1+x)^{3/2} dx &= \frac{1}{6}(1-x)^{7/2}(1+x)^{5/2} + \frac{7}{6} \int (1-x)^{5/2}(1+x)^{3/2} dx \\
 &= \frac{7}{30}(1-x)^{5/2}(1+x)^{5/2} + \frac{1}{6}(1-x)^{7/2}(1+x)^{5/2} + \frac{7}{6} \int (1-x)^{3/2}(1+x)^{3/2} dx \\
 &= \frac{7}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{7}{30}(1-x)^{5/2}(1+x)^{5/2} + \frac{1}{6}(1-x)^{7/2}(1+x)^{5/2} + \frac{7}{8} \int \sqrt{1-x} \\
 &= \frac{7}{16}\sqrt{1-x}x\sqrt{1+x} + \frac{7}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{7}{30}(1-x)^{5/2}(1+x)^{5/2} + \frac{1}{6}(1-x)^{7/2}(1+x)^{5/2} \\
 &= \frac{7}{16}\sqrt{1-x}x\sqrt{1+x} + \frac{7}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{7}{30}(1-x)^{5/2}(1+x)^{5/2} + \frac{1}{6}(1-x)^{7/2}(1+x)^{5/2} \\
 &= \frac{7}{16}\sqrt{1-x}x\sqrt{1+x} + \frac{7}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{7}{30}(1-x)^{5/2}(1+x)^{5/2} + \frac{1}{6}(1-x)^{7/2}(1+x)^{5/2}
 \end{aligned}$$

Mathematica [A] time = 0.06, size = 61, normalized size = 0.69

$$\frac{1}{240}\sqrt{1-x^2}(-40x^5 + 96x^4 + 10x^3 - 192x^2 + 135x + 96) - \frac{7}{8}\sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(7/2)*(1 + x)^(3/2), x]

[Out] (Sqrt[1 - x^2]*(96 + 135*x - 192*x^2 + 10*x^3 + 96*x^4 - 40*x^5))/240 - (7*ArcSin[Sqrt[1 - x]/Sqrt[2]])/8

fricas [A] time = 0.46, size = 62, normalized size = 0.70

$$-\frac{1}{240}(40x^5 - 96x^4 - 10x^3 + 192x^2 - 135x - 96)\sqrt{x+1}\sqrt{-x+1} - \frac{7}{8}\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1} - 1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)*(1+x)^(3/2), x, algorithm="fricas")

[Out] -1/240*(40*x^5 - 96*x^4 - 10*x^3 + 192*x^2 - 135*x - 96)*sqrt(x + 1)*sqrt(-x + 1) - 7/8*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [B] time = 1.33, size = 185, normalized size = 2.08

$$-\frac{1}{240} \left((2 \left((4(5x - 26)(x + 1) + 321)(x + 1) - 451)(x + 1) + 745)(x + 1) - 405 \right) \sqrt{x + 1} \sqrt{-x + 1} + \frac{1}{120} \left((2(3(4x - 1) - 405) \sqrt{x + 1} \sqrt{-x + 1} + 1/120 * ((2 * (3 * (4 * x - 17) * (x + 1) + 133) * (x + 1) - 295) * (x + 1) + 195) * \sqrt{x + 1} * \sqrt{-x + 1} + 1/12 * ((2 * (3 * x - 10) * (x + 1) + 43) * (x + 1) - 39) * \sqrt{x + 1} * \sqrt{-x + 1} - 1/3 * ((2 * x - 5) * (x + 1) + 9) * \sqrt{x + 1} * \sqrt{-x + 1} - 1/2 * \sqrt{x + 1} * (x - 2) * \sqrt{-x + 1} + \sqrt{x + 1} * \sqrt{-x + 1} + 7/8 * \arcsin(1/2 * \sqrt{2}) * \sqrt{x + 1}) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)*(1+x)^(3/2),x, algorithm="giac")

[Out] -1/240*((2*((4*(5*x - 26)*(x + 1) + 321)*(x + 1) - 451)*(x + 1) + 745)*(x + 1) - 405)*sqrt(x + 1)*sqrt(-x + 1) + 1/120*((2*(3*(4*x - 17)*(x + 1) + 133)*(x + 1) - 295)*(x + 1) + 195)*sqrt(x + 1)*sqrt(-x + 1) + 1/12*((2*(3*x - 10)*(x + 1) + 43)*(x + 1) - 39)*sqrt(x + 1)*sqrt(-x + 1) - 1/3*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) - 1/2*sqrt(x + 1)*(x - 2)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + 7/8*arcsin(1/2*sqrt(2))*sqrt(x + 1))

maple [A] time = 0.00, size = 113, normalized size = 1.27

$$\frac{7\sqrt{(x+1)(-x+1)} \arcsin(x)}{16\sqrt{x+1} \sqrt{-x+1}} + \frac{(-x+1)^{\frac{7}{2}}(x+1)^{\frac{5}{2}}}{6} + \frac{7(-x+1)^{\frac{5}{2}}(x+1)^{\frac{5}{2}}}{30} + \frac{7(-x+1)^{\frac{3}{2}}(x+1)^{\frac{5}{2}}}{24} + \frac{7\sqrt{-x+1}(x+1)^{\frac{5}{2}}}{24}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(7/2)*(x+1)^(3/2),x)

[Out] 1/6*(-x+1)^(7/2)*(x+1)^(5/2)+7/30*(-x+1)^(5/2)*(x+1)^(5/2)+7/24*(-x+1)^(3/2)*(x+1)^(5/2)+7/24*(-x+1)^(1/2)*(x+1)^(5/2)-7/48*(-x+1)^(1/2)*(x+1)^(3/2)-7/16*(-x+1)^(1/2)*(x+1)^(1/2)+7/16*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.90, size = 52, normalized size = 0.58

$$-\frac{1}{6}(-x^2+1)^{\frac{5}{2}}x + \frac{2}{5}(-x^2+1)^{\frac{5}{2}} + \frac{7}{24}(-x^2+1)^{\frac{3}{2}}x + \frac{7}{16}\sqrt{-x^2+1}x + \frac{7}{16}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)*(1+x)^(3/2),x, algorithm="maxima")

[Out] -1/6*(-x^2 + 1)^(5/2)*x + 2/5*(-x^2 + 1)^(5/2) + 7/24*(-x^2 + 1)^(3/2)*x + 7/16*sqrt(-x^2 + 1)*x + 7/16*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{7/2} (x+1)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(7/2)*(x + 1)^(3/2), x)`

[Out] `int((1 - x)^(7/2)*(x + 1)^(3/2), x)`

sympy [A] time = 32.99, size = 289, normalized size = 3.25

$$\left\{ \begin{array}{l} \frac{7i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{8} - \frac{i(x+1)^{\frac{13}{2}}}{6\sqrt{x-1}} + \frac{47i(x+1)^{\frac{11}{2}}}{30\sqrt{x-1}} - \frac{683i(x+1)^{\frac{9}{2}}}{120\sqrt{x-1}} + \frac{1151i(x+1)^{\frac{7}{2}}}{120\sqrt{x-1}} - \frac{1543i(x+1)^{\frac{5}{2}}}{240\sqrt{x-1}} - \frac{7i(x+1)^{\frac{3}{2}}}{48\sqrt{x-1}} + \frac{7i\sqrt{x+1}}{8\sqrt{x-1}} \\ \frac{7 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{8} + \frac{(x+1)^{\frac{13}{2}}}{6\sqrt{1-x}} - \frac{47(x+1)^{\frac{11}{2}}}{30\sqrt{1-x}} + \frac{683(x+1)^{\frac{9}{2}}}{120\sqrt{1-x}} - \frac{1151(x+1)^{\frac{7}{2}}}{120\sqrt{1-x}} + \frac{1543(x+1)^{\frac{5}{2}}}{240\sqrt{1-x}} + \frac{7(x+1)^{\frac{3}{2}}}{48\sqrt{1-x}} - \frac{7\sqrt{x+1}}{8\sqrt{1-x}} \end{array} \right. \begin{array}{l} \text{for } \frac{|x+1|}{2} > 1 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(7/2)*(1+x)**(3/2), x)`

[Out] `Piecewise((-7*I*acosh(sqrt(2)*sqrt(x + 1)/2)/8 - I*(x + 1)**(13/2)/(6*sqrt(x - 1)) + 47*I*(x + 1)**(11/2)/(30*sqrt(x - 1)) - 683*I*(x + 1)**(9/2)/(120*sqrt(x - 1)) + 1151*I*(x + 1)**(7/2)/(120*sqrt(x - 1)) - 1543*I*(x + 1)**(5/2)/(240*sqrt(x - 1)) - 7*I*(x + 1)**(3/2)/(48*sqrt(x - 1)) + 7*I*sqrt(x + 1)/(8*sqrt(x - 1)), Abs(x + 1)/2 > 1), (7*asin(sqrt(2)*sqrt(x + 1)/2)/8 + (x + 1)**(13/2)/(6*sqrt(1 - x)) - 47*(x + 1)**(11/2)/(30*sqrt(1 - x)) + 683*(x + 1)**(9/2)/(120*sqrt(1 - x)) - 1151*(x + 1)**(7/2)/(120*sqrt(1 - x)) + 1543*(x + 1)**(5/2)/(240*sqrt(1 - x)) + 7*(x + 1)**(3/2)/(48*sqrt(1 - x)) - 7*sqrt(x + 1)/(8*sqrt(1 - x)), True))`

3.1077 $\int (1-x)^{5/2}(1+x)^{3/2} dx$

Optimal. Leaf size=69

$$\frac{1}{5}(1-x)^{5/2}(x+1)^{5/2} + \frac{1}{4}(1-x)^{3/2}x(x+1)^{3/2} + \frac{3}{8}\sqrt{1-x}x\sqrt{x+1} + \frac{3}{8}\sin^{-1}(x)$$

[Out] 1/4*(1-x)^(3/2)*x*(1+x)^(3/2)+1/5*(1-x)^(5/2)*(1+x)^(5/2)+3/8*arcsin(x)+3/8*x*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$\frac{1}{5}(1-x)^{5/2}(x+1)^{5/2} + \frac{1}{4}(1-x)^{3/2}x(x+1)^{3/2} + \frac{3}{8}\sqrt{1-x}x\sqrt{x+1} + \frac{3}{8}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(5/2)*(1 + x)^(3/2), x]

[Out] (3*Sqrt[1 - x]*x*Sqrt[1 + x])/8 + ((1 - x)^(3/2)*x*(1 + x)^(3/2))/4 + ((1 - x)^(5/2)*(1 + x)^(5/2))/5 + (3*ArcSin[x])/8

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> Simp[(x*(a + b*x)^m*(c + d*x)^m)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(m - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(2*c*n)/(m + n + 1), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int (1-x)^{5/2}(1+x)^{3/2} dx &= \frac{1}{5}(1-x)^{5/2}(1+x)^{5/2} + \int (1-x)^{3/2}(1+x)^{3/2} dx \\
 &= \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{5}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{4} \int \sqrt{1-x} \sqrt{1+x} dx \\
 &= \frac{3}{8}\sqrt{1-x}x\sqrt{1+x} + \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{5}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{8} \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
 &= \frac{3}{8}\sqrt{1-x}x\sqrt{1+x} + \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{5}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{8} \int \frac{1}{\sqrt{1-x^2}} dx \\
 &= \frac{3}{8}\sqrt{1-x}x\sqrt{1+x} + \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{5}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{8} \sin^{-1}(x)
 \end{aligned}$$

Mathematica [A] time = 0.04, size = 55, normalized size = 0.80

$$\frac{1}{40} \left(\sqrt{1-x^2} (8x^4 - 10x^3 - 16x^2 + 25x + 8) - 30 \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(1-x)^(5/2)*(1+x)^(3/2),x]

[Out] (Sqrt[1-x^2]*(8+25*x-16*x^2-10*x^3+8*x^4)-30*ArcSin[Sqrt[1-x]/Sqrt[2]])/40

fricas [A] time = 0.44, size = 57, normalized size = 0.83

$$\frac{1}{40} (8x^4 - 10x^3 - 16x^2 + 25x + 8) \sqrt{x+1} \sqrt{-x+1} - \frac{3}{4} \arctan \left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)*(1+x)^(3/2),x, algorithm="fricas")

[Out] 1/40*(8*x^4 - 10*x^3 - 16*x^2 + 25*x + 8)*sqrt(x + 1)*sqrt(-x + 1) - 3/4*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [A] time = 1.16, size = 91, normalized size = 1.32

$$\frac{1}{120} ((2(3(4x-17)(x+1)+133)(x+1)-295)(x+1)+195)\sqrt{x+1}\sqrt{-x+1} - \frac{1}{3} ((2x-5)(x+1)+9)\sqrt{x+1}\sqrt{-x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)*(1+x)^(3/2),x, algorithm="giac")

[Out] 1/120*((2*(3*(4*x - 17)*(x + 1) + 133)*(x + 1) - 295)*(x + 1) + 195)*sqrt(x + 1)*sqrt(-x + 1) - 1/3*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + 3/4*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.00, size = 99, normalized size = 1.43

$$\frac{3\sqrt{(x+1)(-x+1)} \arcsin(x)}{8\sqrt{x+1} \sqrt{-x+1}} + \frac{(-x+1)^{\frac{5}{2}}(x+1)^{\frac{5}{2}}}{5} + \frac{(-x+1)^{\frac{3}{2}}(x+1)^{\frac{5}{2}}}{4} + \frac{\sqrt{-x+1}(x+1)^{\frac{5}{2}}}{4} - \frac{\sqrt{-x+1}(x+1)^{\frac{3}{2}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(5/2)*(x+1)^(3/2),x)

[Out] 1/5*(-x+1)^(5/2)*(x+1)^(5/2)+1/4*(-x+1)^(3/2)*(x+1)^(5/2)+1/4*(-x+1)^(1/2)*(x+1)^(5/2)-1/8*(-x+1)^(1/2)*(x+1)^(3/2)-3/8*(-x+1)^(1/2)*(x+1)^(1/2)+3/8*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.98, size = 40, normalized size = 0.58

$$\frac{1}{5}(-x^2+1)^{\frac{5}{2}} + \frac{1}{4}(-x^2+1)^{\frac{3}{2}}x + \frac{3}{8}\sqrt{-x^2+1}x + \frac{3}{8}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)*(1+x)^(3/2),x, algorithm="maxima")

[Out] 1/5*(-x^2 + 1)^(5/2) + 1/4*(-x^2 + 1)^(3/2)*x + 3/8*sqrt(-x^2 + 1)*x + 3/8*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{5/2} (x+1)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(5/2)*(x + 1)^(3/2),x)

[Out] int((1 - x)^(5/2)*(x + 1)^(3/2), x)

sympy [B] time = 15.25, size = 250, normalized size = 3.62

$$\left\{ \begin{array}{ll} -\frac{3i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} + \frac{i(x+1)^{\frac{11}{2}}}{5\sqrt{x-1}} - \frac{29i(x+1)^{\frac{9}{2}}}{20\sqrt{x-1}} + \frac{73i(x+1)^{\frac{7}{2}}}{20\sqrt{x-1}} - \frac{129i(x+1)^{\frac{5}{2}}}{40\sqrt{x-1}} - \frac{i(x+1)^{\frac{3}{2}}}{8\sqrt{x-1}} + \frac{3i\sqrt{x+1}}{4\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ \frac{3 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} - \frac{(x+1)^{\frac{11}{2}}}{5\sqrt{1-x}} + \frac{29(x+1)^{\frac{9}{2}}}{20\sqrt{1-x}} - \frac{73(x+1)^{\frac{7}{2}}}{20\sqrt{1-x}} + \frac{129(x+1)^{\frac{5}{2}}}{40\sqrt{1-x}} + \frac{(x+1)^{\frac{3}{2}}}{8\sqrt{1-x}} - \frac{3\sqrt{x+1}}{4\sqrt{1-x}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(5/2)*(1+x)**(3/2), x)

[Out] Piecewise((-3*I*acosh(sqrt(2)*sqrt(x + 1)/2)/4 + I*(x + 1)**(11/2)/(5*sqrt(x - 1)) - 29*I*(x + 1)**(9/2)/(20*sqrt(x - 1)) + 73*I*(x + 1)**(7/2)/(20*sqrt(x - 1)) - 129*I*(x + 1)**(5/2)/(40*sqrt(x - 1)) - I*(x + 1)**(3/2)/(8*sqrt(x - 1)) + 3*I*sqrt(x + 1)/(4*sqrt(x - 1)), Abs(x + 1)/2 > 1), (3*asin(sqrt(2)*sqrt(x + 1)/2)/4 - (x + 1)**(11/2)/(5*sqrt(1 - x)) + 29*(x + 1)**(9/2)/(20*sqrt(1 - x)) - 73*(x + 1)**(7/2)/(20*sqrt(1 - x)) + 129*(x + 1)**(5/2)/(40*sqrt(1 - x)) + (x + 1)**(3/2)/(8*sqrt(1 - x)) - 3*sqrt(x + 1)/(4*sqrt(1 - x)), True))

3.1078 $\int (1-x)^{3/2}(1+x)^{3/2} dx$

Optimal. Leaf size=49

$$\frac{1}{4}(1-x)^{3/2}x(x+1)^{3/2} + \frac{3}{8}\sqrt{1-x}x\sqrt{x+1} + \frac{3}{8}\sin^{-1}(x)$$

[Out] $1/4*(1-x)^{(3/2)}*x*(1+x)^{(3/2)}+3/8*\arcsin(x)+3/8*x*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {38, 41, 216}

$$\frac{1}{4}(1-x)^{3/2}x(x+1)^{3/2} + \frac{3}{8}\sqrt{1-x}x\sqrt{x+1} + \frac{3}{8}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(1-x)^{(3/2)}*(1+x)^{(3/2)}, x]$

[Out] $(3*\text{Sqrt}[1-x]*x*\text{Sqrt}[1+x])/8 + ((1-x)^{(3/2)}*x*(1+x)^{(3/2}))/4 + (3*\text{ArcSin}[x])/8$

Rule 38

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(m_)}), x_Symbol] \rightarrow \text{Simp}[(x*(a + b*x)^m*(c + d*x)^m)/(2*m + 1), x] + \text{Dist}[(2*a*c*m)/(2*m + 1), \text{Int}[(a + b*x)^{(m-1)}*(c + d*x)^{(m-1)}, x], x] /;$ $\text{FreeQ}\{a, b, c, d\}, x \ \&\& \ \text{EqQ}[b*c + a*d, 0] \ \&\& \ \text{IGtQ}[m + 1/2, 0]$

Rule 41

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(m_)}), x_Symbol] \rightarrow \text{Int}[(a*c + b*d*x^2)^m, x] /;$ $\text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{EqQ}[b*c + a*d, 0] \ \&\& \ (\text{IntegerQ}[m] \ || \ (\text{GtQ}[a, 0] \ \&\& \ \text{GtQ}[c, 0]))$

Rule 216

$\text{Int}[1/\text{Sqrt}[(a_ + (b_)*(x_)^2), x_Symbol] \rightarrow \text{Simp}[\text{ArcSin}[(\text{Rt}[-b, 2]*x)/\text{Sqrt}[a]]/\text{Rt}[-b, 2], x] /;$ $\text{FreeQ}\{a, b\}, x \ \&\& \ \text{GtQ}[a, 0] \ \&\& \ \text{NegQ}[b]$

Rubi steps

$$\begin{aligned}
\int (1-x)^{3/2}(1+x)^{3/2} dx &= \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{4} \int \sqrt{1-x} \sqrt{1+x} dx \\
&= \frac{3}{8} \sqrt{1-x} x \sqrt{1+x} + \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{8} \int \frac{1}{\sqrt{1-x} \sqrt{1+x}} dx \\
&= \frac{3}{8} \sqrt{1-x} x \sqrt{1+x} + \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{8} \int \frac{1}{\sqrt{1-x^2}} dx \\
&= \frac{3}{8} \sqrt{1-x} x \sqrt{1+x} + \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{8} \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 0.59

$$\frac{1}{8} \left(x \sqrt{1-x^2} (5-2x^2) + 3 \sin^{-1}(x) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(1-x)^(3/2)*(1+x)^(3/2),x]

[Out] (x*(5-2*x^2)*Sqrt[1-x^2]+3*ArcSin[x])/8

fricas [A] time = 0.44, size = 46, normalized size = 0.94

$$-\frac{1}{8} (2x^3 - 5x) \sqrt{x+1} \sqrt{-x+1} - \frac{3}{4} \arctan\left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)*(1+x)^(3/2),x, algorithm="fricas")

[Out] -1/8*(2*x^3 - 5*x)*sqrt(x + 1)*sqrt(-x + 1) - 3/4*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [B] time = 1.12, size = 101, normalized size = 2.06

$$-\frac{1}{24} ((2(3x-10)(x+1)+43)(x+1)-39)\sqrt{x+1}\sqrt{-x+1} - \frac{1}{6} ((2x-5)(x+1)+9)\sqrt{x+1}\sqrt{-x+1} + \frac{1}{2}\sqrt{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)*(1+x)^(3/2),x, algorithm="giac")

[Out] -1/24*((2*(3*x - 10)*(x + 1) + 43)*(x + 1) - 39)*sqrt(x + 1)*sqrt(-x + 1) - 1/6*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) + 1/2*sqrt(x + 1)*(x

$- 2) \cdot \sqrt{-x + 1} + \sqrt{x + 1} \cdot \sqrt{-x + 1} + 3/4 \cdot \arcsin(1/2 \cdot \sqrt{2} \cdot \sqrt{x + 1})$

maple [B] time = 0.00, size = 85, normalized size = 1.73

$$\frac{3\sqrt{(x+1)(-x+1)} \arcsin(x)}{8\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{3}{2}}(x+1)^{\frac{5}{2}}}{4} + \frac{\sqrt{-x+1}(x+1)^{\frac{5}{2}}}{4} - \frac{\sqrt{-x+1}(x+1)^{\frac{3}{2}}}{8} - \frac{3\sqrt{-x+1}\sqrt{x+1}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-x+1)^(3/2)*(x+1)^(3/2),x)`

[Out] $1/4 \cdot (-x+1)^{3/2} \cdot (x+1)^{5/2} + 1/4 \cdot (-x+1)^{1/2} \cdot (x+1)^{5/2} - 1/8 \cdot (-x+1)^{1/2} \cdot (x+1)^{3/2} - 3/8 \cdot (-x+1)^{1/2} \cdot (x+1)^{1/2} + 3/8 \cdot ((x+1) \cdot (-x+1))^{1/2} / (x+1)^{1/2} / (-x+1)^{1/2} \cdot \arcsin(x)$

maxima [A] time = 2.91, size = 29, normalized size = 0.59

$$\frac{1}{4} (-x^2 + 1)^{\frac{3}{2}} x + \frac{3}{8} \sqrt{-x^2 + 1} x + \frac{3}{8} \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(3/2)*(1+x)^(3/2),x, algorithm="maxima")`

[Out] $1/4 \cdot (-x^2 + 1)^{3/2} \cdot x + 3/8 \cdot \sqrt{-x^2 + 1} \cdot x + 3/8 \cdot \arcsin(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (1-x)^{3/2} (x+1)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1-x)^(3/2)*(x+1)^(3/2),x)`

[Out] `int((1-x)^(3/2)*(x+1)^(3/2),x)`

sympy [B] time = 7.46, size = 214, normalized size = 4.37

$$\begin{cases} -\frac{3i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} - \frac{i(x+1)^{\frac{9}{2}}}{4\sqrt{x-1}} + \frac{5i(x+1)^{\frac{7}{2}}}{4\sqrt{x-1}} - \frac{13i(x+1)^{\frac{5}{2}}}{8\sqrt{x-1}} - \frac{i(x+1)^{\frac{3}{2}}}{8\sqrt{x-1}} + \frac{3i\sqrt{x+1}}{4\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ \frac{3 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} + \frac{(x+1)^{\frac{9}{2}}}{4\sqrt{1-x}} - \frac{5(x+1)^{\frac{7}{2}}}{4\sqrt{1-x}} + \frac{13(x+1)^{\frac{5}{2}}}{8\sqrt{1-x}} + \frac{(x+1)^{\frac{3}{2}}}{8\sqrt{1-x}} - \frac{3\sqrt{x+1}}{4\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((1-x)**(3/2)*(1+x)**(3/2),x)
```

```
[Out] Piecewise((-3*I*acosh(sqrt(2)*sqrt(x + 1)/2)/4 - I*(x + 1)**(9/2)/(4*sqrt(x
- 1)) + 5*I*(x + 1)**(7/2)/(4*sqrt(x - 1)) - 13*I*(x + 1)**(5/2)/(8*sqrt(x
- 1)) - I*(x + 1)**(3/2)/(8*sqrt(x - 1)) + 3*I*sqrt(x + 1)/(4*sqrt(x - 1))
, Abs(x + 1)/2 > 1), (3*asin(sqrt(2)*sqrt(x + 1)/2)/4 + (x + 1)**(9/2)/(4*s
qrt(1 - x)) - 5*(x + 1)**(7/2)/(4*sqrt(1 - x)) + 13*(x + 1)**(5/2)/(8*sqrt(
1 - x)) + (x + 1)**(3/2)/(8*sqrt(1 - x)) - 3*sqrt(x + 1)/(4*sqrt(1 - x)), T
rue))
```

3.1079 $\int \sqrt{1-x} (1+x)^{3/2} dx$

Optimal. Leaf size=48

$$-\frac{1}{3}(1-x)^{3/2}(x+1)^{3/2} + \frac{1}{2}\sqrt{1-x}x\sqrt{x+1} + \frac{1}{2}\sin^{-1}(x)$$

[Out] $-1/3*(1-x)^{(3/2)}*(1+x)^{(3/2)}+1/2*\arcsin(x)+1/2*x*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$-\frac{1}{3}(1-x)^{3/2}(x+1)^{3/2} + \frac{1}{2}\sqrt{1-x}x\sqrt{x+1} + \frac{1}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 - x]*(1 + x)^(3/2), x]

[Out] (Sqrt[1 - x]*x*Sqrt[1 + x])/2 - ((1 - x)^(3/2)*(1 + x)^(3/2))/3 + ArcSin[x]/2

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(x*(a + b*x)^m*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(2*c*n)/(m + n + 1), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int \sqrt{1-x}(1+x)^{3/2} dx &= -\frac{1}{3}(1-x)^{3/2}(1+x)^{3/2} + \int \sqrt{1-x}\sqrt{1+x} dx \\
 &= \frac{1}{2}\sqrt{1-x}x\sqrt{1+x} - \frac{1}{3}(1-x)^{3/2}(1+x)^{3/2} + \frac{1}{2} \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
 &= \frac{1}{2}\sqrt{1-x}x\sqrt{1+x} - \frac{1}{3}(1-x)^{3/2}(1+x)^{3/2} + \frac{1}{2} \int \frac{1}{\sqrt{1-x^2}} dx \\
 &= \frac{1}{2}\sqrt{1-x}x\sqrt{1+x} - \frac{1}{3}(1-x)^{3/2}(1+x)^{3/2} + \frac{1}{2} \sin^{-1}(x)
 \end{aligned}$$

Mathematica [A] time = 0.03, size = 44, normalized size = 0.92

$$\frac{1}{6}\sqrt{1-x^2}(2x^2+3x-2) - \sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 - x]*(1 + x)^(3/2), x]

[Out] (Sqrt[1 - x^2]*(-2 + 3*x + 2*x^2))/6 - ArcSin[Sqrt[1 - x]/Sqrt[2]]

fricas [A] time = 0.45, size = 47, normalized size = 0.98

$$\frac{1}{6}(2x^2+3x-2)\sqrt{x+1}\sqrt{-x+1} - \arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)*(1+x)^(3/2), x, algorithm="fricas")

[Out] 1/6*(2*x^2 + 3*x - 2)*sqrt(x + 1)*sqrt(-x + 1) - arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [A] time = 0.92, size = 66, normalized size = 1.38

$$\frac{1}{6}((2x-5)(x+1)+9)\sqrt{x+1}\sqrt{-x+1} + \sqrt{x+1}(x-2)\sqrt{-x+1} + \sqrt{x+1}\sqrt{-x+1} + \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)*(1+x)^(3/2),x, algorithm="giac")

[Out] 1/6*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) + sqrt(x + 1)*(x - 2)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.01, size = 71, normalized size = 1.48

$$\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{2\sqrt{x+1}\sqrt{-x+1}} + \frac{\sqrt{-x+1}(x+1)^{\frac{5}{2}}}{3} - \frac{\sqrt{-x+1}(x+1)^{\frac{3}{2}}}{6} - \frac{\sqrt{-x+1}\sqrt{x+1}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(1/2)*(x+1)^(3/2),x)

[Out] 1/3*(-x+1)^(1/2)*(x+1)^(5/2)-1/6*(-x+1)^(1/2)*(x+1)^(3/2)-1/2*(-x+1)^(1/2)*(x+1)^(1/2)+1/2*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.97, size = 28, normalized size = 0.58

$$-\frac{1}{3}(-x^2+1)^{\frac{3}{2}} + \frac{1}{2}\sqrt{-x^2+1}x + \frac{1}{2}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)*(1+x)^(3/2),x, algorithm="maxima")

[Out] -1/3*(-x^2 + 1)^(3/2) + 1/2*sqrt(-x^2 + 1)*x + 1/2*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \sqrt{1-x}(x+1)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(1/2)*(x + 1)^(3/2),x)

[Out] int((1 - x)^(1/2)*(x + 1)^(3/2), x)

sympy [B] time = 4.82, size = 165, normalized size = 3.44

$$\begin{cases} -i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{i(x+1)^{\frac{7}{2}}}{3\sqrt{x-1}} - \frac{5i(x+1)^{\frac{5}{2}}}{6\sqrt{x-1}} - \frac{i(x+1)^{\frac{3}{2}}}{6\sqrt{x-1}} + \frac{i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{(x+1)^{\frac{7}{2}}}{3\sqrt{1-x}} + \frac{5(x+1)^{\frac{5}{2}}}{6\sqrt{1-x}} + \frac{(x+1)^{\frac{3}{2}}}{6\sqrt{1-x}} - \frac{\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((1-x)**(1/2)*(1+x)**(3/2),x)
```

```
[Out] Piecewise((-I*acosh(sqrt(2)*sqrt(x + 1)/2) + I*(x + 1)**(7/2)/(3*sqrt(x - 1)) - 5*I*(x + 1)**(5/2)/(6*sqrt(x - 1)) - I*(x + 1)**(3/2)/(6*sqrt(x - 1)) + I*sqrt(x + 1)/sqrt(x - 1), Abs(x + 1)/2 > 1), (asin(sqrt(2)*sqrt(x + 1)/2) - (x + 1)**(7/2)/(3*sqrt(1 - x)) + 5*(x + 1)**(5/2)/(6*sqrt(1 - x)) + (x + 1)**(3/2)/(6*sqrt(1 - x)) - sqrt(x + 1)/sqrt(1 - x), True))
```

3.1080

$$\int \frac{(1+x)^{3/2}}{\sqrt{1-x}} dx$$

Optimal. Leaf size=47

$$-\frac{1}{2}\sqrt{1-x}(x+1)^{3/2} - \frac{3}{2}\sqrt{1-x}\sqrt{x+1} + \frac{3}{2}\sin^{-1}(x)$$

[Out] 3/2*arcsin(x)-1/2*(1-x)^(1/2)*(1+x)^(3/2)-3/2*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {50, 41, 216}

$$-\frac{1}{2}\sqrt{1-x}(x+1)^{3/2} - \frac{3}{2}\sqrt{1-x}\sqrt{x+1} + \frac{3}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(3/2)/Sqrt[1 - x], x]

[Out] (-3*Sqrt[1 - x]*Sqrt[1 + x])/2 - (Sqrt[1 - x]*(1 + x)^(3/2))/2 + (3*ArcSin[x])/2

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(1+x)^{3/2}}{\sqrt{1-x}} dx &= -\frac{1}{2}\sqrt{1-x}(1+x)^{3/2} + \frac{3}{2} \int \frac{\sqrt{1+x}}{\sqrt{1-x}} dx \\
&= -\frac{3}{2}\sqrt{1-x}\sqrt{1+x} - \frac{1}{2}\sqrt{1-x}(1+x)^{3/2} + \frac{3}{2} \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
&= -\frac{3}{2}\sqrt{1-x}\sqrt{1+x} - \frac{1}{2}\sqrt{1-x}(1+x)^{3/2} + \frac{3}{2} \int \frac{1}{\sqrt{1-x^2}} dx \\
&= -\frac{3}{2}\sqrt{1-x}\sqrt{1+x} - \frac{1}{2}\sqrt{1-x}(1+x)^{3/2} + \frac{3}{2} \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 37, normalized size = 0.79

$$-\frac{1}{2}\sqrt{1-x^2}(x+4) - 3\sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(3/2)/Sqrt[1 - x], x]

[Out] -1/2*((4 + x)*Sqrt[1 - x^2]) - 3*ArcSin[Sqrt[1 - x]/Sqrt[2]]

fricas [A] time = 0.47, size = 40, normalized size = 0.85

$$-\frac{1}{2}(x+4)\sqrt{x+1}\sqrt{-x+1} - 3\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(1/2), x, algorithm="fricas")

[Out] -1/2*(x + 4)*sqrt(x + 1)*sqrt(-x + 1) - 3*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [A] time = 1.17, size = 31, normalized size = 0.66

$$-\frac{1}{2}(x+4)\sqrt{x+1}\sqrt{-x+1} + 3\arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(1/2), x, algorithm="giac")

[Out] -1/2*(x + 4)*sqrt(x + 1)*sqrt(-x + 1) + 3*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.00, size = 57, normalized size = 1.21

$$\frac{3\sqrt{(x+1)(-x+1)} \arcsin(x)}{2\sqrt{x+1} \sqrt{-x+1}} - \frac{\sqrt{-x+1} (x+1)^{\frac{3}{2}}}{2} - \frac{3\sqrt{-x+1} \sqrt{x+1}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(3/2)/(-x+1)^(1/2),x)

[Out] -1/2*(-x+1)^(1/2)*(x+1)^(3/2)-3/2*(-x+1)^(1/2)*(x+1)^(1/2)+3/2*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 3.09, size = 28, normalized size = 0.60

$$-\frac{1}{2} \sqrt{-x^2 + 1} x - 2 \sqrt{-x^2 + 1} + \frac{3}{2} \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(1/2),x, algorithm="maxima")

[Out] -1/2*sqrt(-x^2 + 1)*x - 2*sqrt(-x^2 + 1) + 3/2*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(x+1)^{3/2}}{\sqrt{1-x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(3/2)/(1 - x)^(1/2),x)

[Out] int((x + 1)^(3/2)/(1 - x)^(1/2), x)

sympy [A] time = 3.28, size = 136, normalized size = 2.89

$$\begin{cases} -3i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{i(x+1)^{\frac{5}{2}}}{2\sqrt{x-1}} - \frac{i(x+1)^{\frac{3}{2}}}{2\sqrt{x-1}} + \frac{3i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ 3 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{(x+1)^{\frac{5}{2}}}{2\sqrt{1-x}} + \frac{(x+1)^{\frac{3}{2}}}{2\sqrt{1-x}} - \frac{3\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(3/2)/(1-x)**(1/2),x)

```
[Out] Piecewise((-3*I*acosh(sqrt(2)*sqrt(x + 1)/2) - I*(x + 1)**(5/2)/(2*sqrt(x - 1)) - I*(x + 1)**(3/2)/(2*sqrt(x - 1)) + 3*I*sqrt(x + 1)/sqrt(x - 1), Abs(x + 1)/2 > 1), (3*asin(sqrt(2)*sqrt(x + 1)/2) + (x + 1)**(5/2)/(2*sqrt(1 - x)) + (x + 1)**(3/2)/(2*sqrt(1 - x)) - 3*sqrt(x + 1)/sqrt(1 - x), True))
```

$$3.1081 \quad \int \frac{(1+x)^{3/2}}{(1-x)^{3/2}} dx$$

Optimal. Leaf size=41

$$\frac{2(x+1)^{3/2}}{\sqrt{1-x}} + 3\sqrt{1-x}\sqrt{x+1} - 3\sin^{-1}(x)$$

[Out] -3*arcsin(x)+2*(1+x)^(3/2)/(1-x)^(1/2)+3*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 41, 216}

$$\frac{2(x+1)^{3/2}}{\sqrt{1-x}} + 3\sqrt{1-x}\sqrt{x+1} - 3\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(3/2)/(1 - x)^(3/2), x]

[Out] 3*Sqrt[1 - x]*Sqrt[1 + x] + (2*(1 + x)^(3/2))/Sqrt[1 - x] - 3*ArcSin[x]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n

+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int \frac{(1+x)^{3/2}}{(1-x)^{3/2}} dx &= \frac{2(1+x)^{3/2}}{\sqrt{1-x}} - 3 \int \frac{\sqrt{1+x}}{\sqrt{1-x}} dx \\ &= 3\sqrt{1-x}\sqrt{1+x} + \frac{2(1+x)^{3/2}}{\sqrt{1-x}} - 3 \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\ &= 3\sqrt{1-x}\sqrt{1+x} + \frac{2(1+x)^{3/2}}{\sqrt{1-x}} - 3 \int \frac{1}{\sqrt{1-x^2}} dx \\ &= 3\sqrt{1-x}\sqrt{1+x} + \frac{2(1+x)^{3/2}}{\sqrt{1-x}} - 3 \sin^{-1}(x) \end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.85

$$\frac{4\sqrt{2} {}_2F_1\left(-\frac{3}{2}, -\frac{1}{2}; \frac{1}{2}; \frac{1-x}{2}\right)}{\sqrt{1-x}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(3/2)/(1 - x)^(3/2), x]

[Out] (4*Sqrt[2]*Hypergeometric2F1[-3/2, -1/2, 1/2, (1 - x)/2])/Sqrt[1 - x]

fricas [A] time = 0.44, size = 52, normalized size = 1.27

$$\frac{\sqrt{x+1}(x-5)\sqrt{-x+1} + 6(x-1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) + 5x-5}{x-1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(3/2),x, algorithm="fricas")

[Out] (sqrt(x + 1)*(x - 5)*sqrt(-x + 1) + 6*(x - 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) + 5*x - 5)/(x - 1)

giac [A] time = 1.19, size = 35, normalized size = 0.85

$$\frac{\sqrt{x+1}(x-5)\sqrt{-x+1}}{x-1} - 6 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(3/2),x, algorithm="giac")

[Out] sqrt(x + 1)*(x - 5)*sqrt(-x + 1)/(x - 1) - 6*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.02, size = 72, normalized size = 1.76

$$-\frac{3\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1} \sqrt{-x+1}} - \frac{(x^2 - 4x - 5) \sqrt{(x+1)(-x+1)}}{\sqrt{-(x+1)(x-1)} \sqrt{-x+1} \sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(3/2)/(-x+1)^(3/2),x)

[Out] -(x^2-4*x-5)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)/(x+1)^(1/2)-3*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.99, size = 42, normalized size = 1.02

$$-\frac{(-x^2+1)^{\frac{3}{2}}}{x^2-2x+1} - \frac{6\sqrt{-x^2+1}}{x-1} - 3 \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(3/2),x, algorithm="maxima")

[Out] -(-x^2 + 1)^(3/2)/(x^2 - 2*x + 1) - 6*sqrt(-x^2 + 1)/(x - 1) - 3*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(x+1)^{3/2}}{(1-x)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(3/2)/(1 - x)^(3/2),x)

[Out] int((x + 1)^(3/2)/(1 - x)^(3/2), x)

sympy [A] time = 2.92, size = 100, normalized size = 2.44

$$\begin{cases} 6i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{i(x+1)^{\frac{3}{2}}}{\sqrt{x-1}} - \frac{6i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ -6 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{(x+1)^{\frac{3}{2}}}{\sqrt{1-x}} + \frac{6\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(3/2)/(1-x)**(3/2),x)

[Out] Piecewise((6*I*acosh(sqrt(2)*sqrt(x + 1)/2) + I*(x + 1)**(3/2)/sqrt(x - 1) - 6*I*sqrt(x + 1)/sqrt(x - 1), Abs(x + 1)/2 > 1), (-6*asin(sqrt(2)*sqrt(x + 1)/2) - (x + 1)**(3/2)/sqrt(1 - x) + 6*sqrt(x + 1)/sqrt(1 - x), True))

3.1082

$$\int \frac{(1+x)^{3/2}}{(1-x)^{5/2}} dx$$

Optimal. Leaf size=41

$$\frac{2(x+1)^{3/2}}{3(1-x)^{3/2}} - \frac{2\sqrt{x+1}}{\sqrt{1-x}} + \sin^{-1}(x)$$

[Out] $2/3*(1+x)^{(3/2)/(1-x)^{(3/2)}+\arcsin(x)-2*(1+x)^{(1/2)/(1-x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {47, 41, 216}

$$\frac{2(x+1)^{3/2}}{3(1-x)^{3/2}} - \frac{2\sqrt{x+1}}{\sqrt{1-x}} + \sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(3/2)/(1 - x)^(5/2), x]

[Out] (-2*Sqrt[1 + x])/Sqrt[1 - x] + (2*(1 + x)^(3/2))/(3*(1 - x)^(3/2)) + ArcSin[x]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IleQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(1+x)^{3/2}}{(1-x)^{5/2}} dx &= \frac{2(1+x)^{3/2}}{3(1-x)^{3/2}} - \int \frac{\sqrt{1+x}}{(1-x)^{3/2}} dx \\
&= -\frac{2\sqrt{1+x}}{\sqrt{1-x}} + \frac{2(1+x)^{3/2}}{3(1-x)^{3/2}} + \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
&= -\frac{2\sqrt{1+x}}{\sqrt{1-x}} + \frac{2(1+x)^{3/2}}{3(1-x)^{3/2}} + \int \frac{1}{\sqrt{1-x^2}} dx \\
&= -\frac{2\sqrt{1+x}}{\sqrt{1-x}} + \frac{2(1+x)^{3/2}}{3(1-x)^{3/2}} + \sin^{-1}(x)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 37, normalized size = 0.90

$$\frac{4\sqrt{2} {}_2F_1\left(-\frac{3}{2}, -\frac{3}{2}; -\frac{1}{2}; \frac{1-x}{2}\right)}{3(1-x)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(3/2)/(1 - x)^(5/2), x]

[Out] (4*Sqrt[2]*Hypergeometric2F1[-3/2, -3/2, -1/2, (1 - x)/2])/(3*(1 - x)^(3/2))

fricas [B] time = 0.44, size = 71, normalized size = 1.73

$$\frac{2\left(2x^2 - 2(2x-1)\sqrt{x+1}\sqrt{-x+1} + 3(x^2 - 2x + 1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) - 4x + 2\right)}{3(x^2 - 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(5/2), x, algorithm="fricas")

[Out] -2/3*(2*x^2 - 2*(2*x - 1)*sqrt(x + 1)*sqrt(-x + 1) + 3*(x^2 - 2*x + 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) - 4*x + 2)/(x^2 - 2*x + 1)

giac [A] time = 1.02, size = 38, normalized size = 0.93

$$\frac{4(2x-1)\sqrt{x+1}\sqrt{-x+1}}{3(x-1)^2} + 2\arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(5/2),x, algorithm="giac")

[Out] 4/3*(2*x - 1)*sqrt(x + 1)*sqrt(-x + 1)/(x - 1)^2 + 2*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.02, size = 76, normalized size = 1.85

$$\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1} \sqrt{-x+1}} - \frac{4(2x^2+x-1)\sqrt{(x+1)(-x+1)}}{3(x-1)\sqrt{-(x+1)(x-1)}\sqrt{-x+1}\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(3/2)/(-x+1)^(5/2),x)

[Out] -4/3*(2*x^2+x-1)/(x-1)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)/(x+1)^(1/2)+((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [B] time = 2.97, size = 66, normalized size = 1.61

$$-\frac{(-x^2+1)^{\frac{3}{2}}}{3(x^3-3x^2+3x-1)} + \frac{2\sqrt{-x^2+1}}{3(x^2-2x+1)} + \frac{7\sqrt{-x^2+1}}{3(x-1)} + \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(5/2),x, algorithm="maxima")

[Out] -1/3*(-x^2 + 1)^(3/2)/(x^3 - 3*x^2 + 3*x - 1) + 2/3*sqrt(-x^2 + 1)/(x^2 - 2*x + 1) + 7/3*sqrt(-x^2 + 1)/(x - 1) + arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(x+1)^{3/2}}{(1-x)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(3/2)/(1 - x)^(5/2),x)

[Out] int((x + 1)^(3/2)/(1 - x)^(5/2), x)

sympy [B] time = 3.70, size = 500, normalized size = 12.20

$$\left\{ \begin{array}{l} \frac{6i\sqrt{x-1}(x+1)^{\frac{15}{2}} \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{-3\sqrt{x-1}(x+1)^{\frac{15}{2}} + 6\sqrt{x-1}(x+1)^{\frac{13}{2}}} - \frac{3\pi\sqrt{x-1}(x+1)^{\frac{15}{2}}}{-3\sqrt{x-1}(x+1)^{\frac{15}{2}} + 6\sqrt{x-1}(x+1)^{\frac{13}{2}}} - \frac{12i\sqrt{x-1}(x+1)^{\frac{13}{2}} \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{-3\sqrt{x-1}(x+1)^{\frac{15}{2}} + 6\sqrt{x-1}(x+1)^{\frac{13}{2}}} + \frac{6\pi\sqrt{x-1}(x+1)^{\frac{13}{2}}}{-3\sqrt{x-1}(x+1)^{\frac{15}{2}} + 6\sqrt{x-1}(x+1)^{\frac{13}{2}}} \\ \frac{6\sqrt{1-x}(x+1)^{\frac{15}{2}} \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{3\sqrt{1-x}(x+1)^{\frac{15}{2}} - 6\sqrt{1-x}(x+1)^{\frac{13}{2}}} - \frac{12\sqrt{1-x}(x+1)^{\frac{13}{2}} \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{3\sqrt{1-x}(x+1)^{\frac{15}{2}} - 6\sqrt{1-x}(x+1)^{\frac{13}{2}}} - \frac{8(x+1)^8}{3\sqrt{1-x}(x+1)^{\frac{15}{2}} - 6\sqrt{1-x}(x+1)^{\frac{13}{2}}} + \frac{12(x+1)^7}{3\sqrt{1-x}(x+1)^{\frac{15}{2}} - 6\sqrt{1-x}(x+1)^{\frac{13}{2}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(3/2)/(1-x)**(5/2), x)

[Out] Piecewise((6*I*sqrt(x - 1)*(x + 1)**(15/2)*acosh(sqrt(2)*sqrt(x + 1)/2)/(-3*sqrt(x - 1)*(x + 1)**(15/2) + 6*sqrt(x - 1)*(x + 1)**(13/2)) - 3*pi*sqrt(x - 1)*(x + 1)**(15/2)/(-3*sqrt(x - 1)*(x + 1)**(15/2) + 6*sqrt(x - 1)*(x + 1)**(13/2)) - 12*I*sqrt(x - 1)*(x + 1)**(13/2)*acosh(sqrt(2)*sqrt(x + 1)/2)/(-3*sqrt(x - 1)*(x + 1)**(15/2) + 6*sqrt(x - 1)*(x + 1)**(13/2)) + 6*pi*sqrt(x - 1)*(x + 1)**(13/2)/(-3*sqrt(x - 1)*(x + 1)**(15/2) + 6*sqrt(x - 1)*(x + 1)**(13/2)) - 8*I*(x + 1)**8/(-3*sqrt(x - 1)*(x + 1)**(15/2) + 6*sqrt(x - 1)*(x + 1)**(13/2)) + 12*I*(x + 1)**7/(-3*sqrt(x - 1)*(x + 1)**(15/2) + 6*sqrt(x - 1)*(x + 1)**(13/2)), Abs(x + 1)/2 > 1), (6*sqrt(1 - x)*(x + 1)**(15/2)*asin(sqrt(2)*sqrt(x + 1)/2)/(3*sqrt(1 - x)*(x + 1)**(15/2) - 6*sqrt(1 - x)*(x + 1)**(13/2)) - 12*sqrt(1 - x)*(x + 1)**(13/2)*asin(sqrt(2)*sqrt(x + 1)/2)/(3*sqrt(1 - x)*(x + 1)**(15/2) - 6*sqrt(1 - x)*(x + 1)**(13/2)) - 8*(x + 1)**8/(3*sqrt(1 - x)*(x + 1)**(15/2) - 6*sqrt(1 - x)*(x + 1)**(13/2)) + 12*(x + 1)**7/(3*sqrt(1 - x)*(x + 1)**(15/2) - 6*sqrt(1 - x)*(x + 1)**(13/2)), True))

$$3.1083 \quad \int \frac{(1+x)^{3/2}}{(1-x)^{7/2}} dx$$

Optimal. Leaf size=20

$$\frac{(x+1)^{5/2}}{5(1-x)^{5/2}}$$

[Out] 1/5*(1+x)^(5/2)/(1-x)^(5/2)

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {37}

$$\frac{(x+1)^{5/2}}{5(1-x)^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(3/2)/(1 - x)^(7/2), x]

[Out] (1 + x)^(5/2)/(5*(1 - x)^(5/2))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(1+x)^{3/2}}{(1-x)^{7/2}} dx = \frac{(1+x)^{5/2}}{5(1-x)^{5/2}}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 1.00

$$\frac{(x+1)^{5/2}}{5(1-x)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(3/2)/(1 - x)^(7/2), x]

[Out] (1 + x)^(5/2)/(5*(1 - x)^(5/2))

fricas [B] time = 0.44, size = 52, normalized size = 2.60

$$\frac{x^3 - 3x^2 - (x^2 + 2x + 1)\sqrt{x+1}\sqrt{-x+1} + 3x - 1}{5(x^3 - 3x^2 + 3x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(7/2),x, algorithm="fricas")

[Out] 1/5*(x^3 - 3*x^2 - (x^2 + 2*x + 1)*sqrt(x + 1)*sqrt(-x + 1) + 3*x - 1)/(x^3 - 3*x^2 + 3*x - 1)

giac [A] time = 1.06, size = 19, normalized size = 0.95

$$-\frac{(x+1)^{\frac{5}{2}}\sqrt{-x+1}}{5(x-1)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(7/2),x, algorithm="giac")

[Out] -1/5*(x + 1)^(5/2)*sqrt(-x + 1)/(x - 1)^3

maple [A] time = 0.00, size = 15, normalized size = 0.75

$$\frac{(x+1)^{\frac{5}{2}}}{5(-x+1)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(3/2)/(-x+1)^(7/2),x)

[Out] 1/5*(x+1)^(5/2)/(-x+1)^(5/2)

maxima [B] time = 1.28, size = 94, normalized size = 4.70

$$\frac{(-x^2 + 1)^{\frac{3}{2}}}{x^4 - 4x^3 + 6x^2 - 4x + 1} + \frac{6\sqrt{-x^2 + 1}}{5(x^3 - 3x^2 + 3x - 1)} + \frac{\sqrt{-x^2 + 1}}{5(x^2 - 2x + 1)} - \frac{\sqrt{-x^2 + 1}}{5(x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(7/2),x, algorithm="maxima")

[Out] $(-x^2 + 1)^{3/2}/(x^4 - 4x^3 + 6x^2 - 4x + 1) + 6/5\sqrt{-x^2 + 1}/(x^3 - 3x^2 + 3x - 1) + 1/5\sqrt{-x^2 + 1}/(x^2 - 2x + 1) - 1/5\sqrt{-x^2 + 1}/(x - 1)$

mupad [B] time = 0.25, size = 50, normalized size = 2.50

$$\frac{\sqrt{1-x} \left(\frac{2x\sqrt{x+1}}{5} + \frac{\sqrt{x+1}}{5} + \frac{x^2\sqrt{x+1}}{5} \right)}{x^3 - 3x^2 + 3x - 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x + 1)^(3/2)/(1 - x)^(7/2), x)`

[Out] $-((1 - x)^{1/2} * ((2*x*(x + 1)^{1/2})/5 + (x + 1)^{1/2}/5 + (x^2*(x + 1)^{1/2})/5)) / (3*x - 3*x^2 + x^3 - 1)$

sympy [B] time = 6.26, size = 88, normalized size = 4.40

$$\begin{cases} -\frac{i(x+1)^{\frac{5}{2}}}{5\sqrt{x-1}(x+1)^2 - 20\sqrt{x-1}(x+1) + 20\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ \frac{(x+1)^{\frac{5}{2}}}{5\sqrt{1-x}(x+1)^2 - 20\sqrt{1-x}(x+1) + 20\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)**(3/2)/(1-x)**(7/2), x)`

[Out] `Piecewise((-I*(x + 1)**(5/2)/(5*sqrt(x - 1)*(x + 1)**2 - 20*sqrt(x - 1)*(x + 1) + 20*sqrt(x - 1)), Abs(x + 1)/2 > 1), ((x + 1)**(5/2)/(5*sqrt(1 - x)*(x + 1)**2 - 20*sqrt(1 - x)*(x + 1) + 20*sqrt(1 - x)), True))`

3.1084

$$\int \frac{(1+x)^{3/2}}{(1-x)^{9/2}} dx$$

Optimal. Leaf size=41

$$\frac{(x+1)^{5/2}}{35(1-x)^{5/2}} + \frac{(x+1)^{5/2}}{7(1-x)^{7/2}}$$

[Out] $1/7*(1+x)^{(5/2)/(1-x)^{(7/2)}+1/35*(1+x)^{(5/2)/(1-x)^{(5/2)}$

Rubi [A] time = 0.00, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{(x+1)^{5/2}}{35(1-x)^{5/2}} + \frac{(x+1)^{5/2}}{7(1-x)^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(3/2)/(1 - x)^(9/2), x]

[Out] (1 + x)^(5/2)/(7*(1 - x)^(7/2)) + (1 + x)^(5/2)/(35*(1 - x)^(5/2))

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp
[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
+ d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{(1+x)^{3/2}}{(1-x)^{9/2}} dx = \frac{(1+x)^{5/2}}{7(1-x)^{7/2}} + \frac{1}{7} \int \frac{(1+x)^{3/2}}{(1-x)^{7/2}} dx$$

$$= \frac{(1+x)^{5/2}}{7(1-x)^{7/2}} + \frac{(1+x)^{5/2}}{35(1-x)^{5/2}}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.56

$$\frac{(x-6)(x+1)^{5/2}}{35(1-x)^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(3/2)/(1 - x)^(9/2), x]

[Out] -1/35*((-6 + x)*(1 + x)^(5/2))/(1 - x)^(7/2)

fricas [B] time = 0.45, size = 69, normalized size = 1.68

$$\frac{6x^4 - 24x^3 + 36x^2 - (x^3 - 4x^2 - 11x - 6)\sqrt{x+1}\sqrt{-x+1} - 24x + 6}{35(x^4 - 4x^3 + 6x^2 - 4x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(9/2), x, algorithm="fricas")

[Out] 1/35*(6*x^4 - 24*x^3 + 36*x^2 - (x^3 - 4*x^2 - 11*x - 6)*sqrt(x + 1)*sqrt(-x + 1) - 24*x + 6)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1)

giac [A] time = 1.13, size = 22, normalized size = 0.54

$$\frac{(x+1)^{5/2}(x-6)\sqrt{-x+1}}{35(x-1)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(9/2), x, algorithm="giac")

[Out] -1/35*(x + 1)^(5/2)*(x - 6)*sqrt(-x + 1)/(x - 1)^4

maple [A] time = 0.00, size = 18, normalized size = 0.44

$$\frac{(x+1)^{5/2}(x-6)}{35(-x+1)^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x+1)^(3/2)/(-x+1)^(9/2),x)`

[Out] $-1/35*(x+1)^(5/2)*(x-6)/(-x+1)^(7/2)$

maxima [B] time = 1.38, size = 131, normalized size = 3.20

$$\frac{(-x^2 + 1)^{\frac{3}{2}}}{2(x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1)} - \frac{3\sqrt{-x^2 + 1}}{7(x^4 - 4x^3 + 6x^2 - 4x + 1)} - \frac{3\sqrt{-x^2 + 1}}{70(x^3 - 3x^2 + 3x - 1)} + \frac{\sqrt{-x^2 + 1}}{35(x^2 - 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)^(3/2)/(1-x)^(9/2),x, algorithm="maxima")`

[Out] $-1/2*(-x^2 + 1)^(3/2)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) - 3/7*\text{sqrt}(-x^2 + 1)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1) - 3/70*\text{sqrt}(-x^2 + 1)/(x^3 - 3*x^2 + 3*x - 1) + 1/35*\text{sqrt}(-x^2 + 1)/(x^2 - 2*x + 1) - 1/35*\text{sqrt}(-x^2 + 1)/(x - 1)$

mupad [B] time = 0.27, size = 64, normalized size = 1.56

$$\frac{\sqrt{1-x} \left(\frac{11x\sqrt{x+1}}{35} + \frac{6\sqrt{x+1}}{35} + \frac{4x^2\sqrt{x+1}}{35} - \frac{x^3\sqrt{x+1}}{35} \right)}{x^4 - 4x^3 + 6x^2 - 4x + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x + 1)^(3/2)/(1 - x)^(9/2),x)`

[Out] $((1 - x)^(1/2)*((11*x*(x + 1)^(1/2))/35 + (6*(x + 1)^(1/2))/35 + (4*x^2*(x + 1)^(1/2))/35 - (x^3*(x + 1)^(1/2))/35))/(6*x^2 - 4*x - 4*x^3 + x^4 + 1)$

sympy [B] time = 19.08, size = 228, normalized size = 5.56

$$\begin{cases} \frac{i(x+1)^{\frac{7}{2}}}{35\sqrt{x-1}(x+1)^3 - 210\sqrt{x-1}(x+1)^2 + 420\sqrt{x-1}(x+1) - 280\sqrt{x-1}} + \frac{7i(x+1)^{\frac{5}{2}}}{35\sqrt{x-1}(x+1)^3 - 210\sqrt{x-1}(x+1)^2 + 420\sqrt{x-1}(x+1) - 280\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} \\ \frac{(x+1)^{\frac{7}{2}}}{35\sqrt{1-x}(x+1)^3 - 210\sqrt{1-x}(x+1)^2 + 420\sqrt{1-x}(x+1) - 280\sqrt{1-x}} - \frac{7(x+1)^{\frac{5}{2}}}{35\sqrt{1-x}(x+1)^3 - 210\sqrt{1-x}(x+1)^2 + 420\sqrt{1-x}(x+1) - 280\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)**(3/2)/(1-x)**(9/2),x)`

[Out] $\text{Piecewise}((-I*(x + 1)**(7/2)/(35*\text{sqrt}(x - 1)*(x + 1)**3 - 210*\text{sqrt}(x - 1)*(x + 1)**2 + 420*\text{sqrt}(x - 1)*(x + 1) - 280*\text{sqrt}(x - 1)) + 7*I*(x + 1)**(5/2))$

```
/(35*sqrt(x - 1)*(x + 1)**3 - 210*sqrt(x - 1)*(x + 1)**2 + 420*sqrt(x - 1)*  
(x + 1) - 280*sqrt(x - 1)), Abs(x + 1)/2 > 1), ((x + 1)**(7/2)/(35*sqrt(1 -  
x)*(x + 1)**3 - 210*sqrt(1 - x)*(x + 1)**2 + 420*sqrt(1 - x)*(x + 1) - 280  
*sqrt(1 - x)) - 7*(x + 1)**(5/2)/(35*sqrt(1 - x)*(x + 1)**3 - 210*sqrt(1 -  
x)*(x + 1)**2 + 420*sqrt(1 - x)*(x + 1) - 280*sqrt(1 - x)), True))
```

$$3.1085 \quad \int \frac{(1+x)^{3/2}}{(1-x)^{11/2}} dx$$

Optimal. Leaf size=61

$$\frac{2(x+1)^{5/2}}{315(1-x)^{5/2}} + \frac{2(x+1)^{5/2}}{63(1-x)^{7/2}} + \frac{(x+1)^{5/2}}{9(1-x)^{9/2}}$$

[Out] $1/9*(1+x)^{(5/2)}/(1-x)^{(9/2)}+2/63*(1+x)^{(5/2)}/(1-x)^{(7/2)}+2/315*(1+x)^{(5/2)}/(1-x)^{(5/2)}$

Rubi [A] time = 0.01, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{2(x+1)^{5/2}}{315(1-x)^{5/2}} + \frac{2(x+1)^{5/2}}{63(1-x)^{7/2}} + \frac{(x+1)^{5/2}}{9(1-x)^{9/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(3/2)/(1 - x)^(11/2), x]

[Out] $(1+x)^{(5/2)}/(9*(1-x)^{(9/2)}) + (2*(1+x)^{(5/2)})/(63*(1-x)^{(7/2)}) + (2*(1+x)^{(5/2)})/(315*(1-x)^{(5/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[m] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{(1+x)^{3/2}}{(1-x)^{11/2}} dx &= \frac{(1+x)^{5/2}}{9(1-x)^{9/2}} + \frac{2}{9} \int \frac{(1+x)^{3/2}}{(1-x)^{9/2}} dx \\ &= \frac{(1+x)^{5/2}}{9(1-x)^{9/2}} + \frac{2(1+x)^{5/2}}{63(1-x)^{7/2}} + \frac{2}{63} \int \frac{(1+x)^{3/2}}{(1-x)^{7/2}} dx \\ &= \frac{(1+x)^{5/2}}{9(1-x)^{9/2}} + \frac{2(1+x)^{5/2}}{63(1-x)^{7/2}} + \frac{2(1+x)^{5/2}}{315(1-x)^{5/2}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 0.49

$$\frac{(x+1)^{5/2}(2x^2-14x+47)}{315(1-x)^{9/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(3/2)/(1 - x)^(11/2), x]

[Out] ((1 + x)^(5/2)*(47 - 14*x + 2*x^2))/(315*(1 - x)^(9/2))

fricas [A] time = 0.43, size = 86, normalized size = 1.41

$$\frac{47x^5 - 235x^4 + 470x^3 - 470x^2 - (2x^4 - 10x^3 + 21x^2 + 80x + 47)\sqrt{x+1}\sqrt{-x+1} + 235x - 47}{315(x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(11/2), x, algorithm="fricas")

[Out] 1/315*(47*x^5 - 235*x^4 + 470*x^3 - 470*x^2 - (2*x^4 - 10*x^3 + 21*x^2 + 80*x + 47)*sqrt(x + 1)*sqrt(-x + 1) + 235*x - 47)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1)

giac [A] time = 1.11, size = 29, normalized size = 0.48

$$\frac{(2(x+1)(x-8)+63)(x+1)^{5/2}\sqrt{-x+1}}{315(x-1)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(11/2), x, algorithm="giac")

[Out] -1/315*(2*(x + 1)*(x - 8) + 63)*(x + 1)^(5/2)*sqrt(-x + 1)/(x - 1)^5

maple [A] time = 0.00, size = 25, normalized size = 0.41

$$\frac{(x+1)^{\frac{5}{2}}(2x^2-14x+47)}{315(-x+1)^{\frac{9}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(3/2)/(-x+1)^(11/2), x)

[Out] 1/315*(x+1)^(5/2)*(2*x^2-14*x+47)/(-x+1)^(9/2)

maxima [B] time = 1.37, size = 172, normalized size = 2.82

$$\frac{(-x^2+1)^{\frac{3}{2}}}{3(x^6-6x^5+15x^4-20x^3+15x^2-6x+1)} + \frac{2\sqrt{-x^2+1}}{9(x^5-5x^4+10x^3-10x^2+5x-1)} + \frac{\sqrt{-x^2+1}}{63(x^4-4x^3+6x^2-4x+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(11/2), x, algorithm="maxima")

[Out] 1/3*(-x^2+1)^(3/2)/(x^6-6*x^5+15*x^4-20*x^3+15*x^2-6*x+1)+2/9*sqrt(-x^2+1)/(x^5-5*x^4+10*x^3-10*x^2+5*x-1)+1/63*sqrt(-x^2+1)/(x^4-4*x^3+6*x^2-4*x+1)-1/105*sqrt(-x^2+1)/(x^3-3*x^2+3*x-1)+2/315*sqrt(-x^2+1)/(x^2-2*x+1)-2/315*sqrt(-x^2+1)/(x-1)

mupad [B] time = 0.32, size = 80, normalized size = 1.31

$$\frac{\sqrt{1-x} \left(\frac{16x\sqrt{x+1}}{63} + \frac{47\sqrt{x+1}}{315} + \frac{x^2\sqrt{x+1}}{15} - \frac{2x^3\sqrt{x+1}}{63} + \frac{2x^4\sqrt{x+1}}{315} \right)}{x^5-5x^4+10x^3-10x^2+5x-1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(3/2)/(1-x)^(11/2), x)

[Out] -((1-x)^(1/2)*((16*x*(x+1)^(1/2))/63+(47*(x+1)^(1/2))/315+(x^2*(x+1)^(1/2))/15-(2*x^3*(x+1)^(1/2))/63+(2*x^4*(x+1)^(1/2))/315))/(5*x-10*x^2+10*x^3-5*x^4+x^5-1)

sympy [B] time = 51.65, size = 677, normalized size = 11.10

$$\left\{ \begin{array}{l} \frac{2i(x+1)^{\frac{11}{2}}}{315\sqrt{x-1}(x+1)^5-3150\sqrt{x-1}(x+1)^4+12600\sqrt{x-1}(x+1)^3-25200\sqrt{x-1}(x+1)^2+25200\sqrt{x-1}(x+1)-10080\sqrt{x-1}} + \frac{2i(x+1)^{\frac{11}{2}}}{315\sqrt{x-1}(x+1)^5-3150\sqrt{x-1}(x+1)^4+12600\sqrt{x-1}(x+1)^3-25200\sqrt{x-1}(x+1)^2+25200\sqrt{x-1}(x+1)-10080\sqrt{x-1}} \\ \frac{2(x+1)^{\frac{11}{2}}}{315\sqrt{1-x}(x+1)^5-3150\sqrt{1-x}(x+1)^4+12600\sqrt{1-x}(x+1)^3-25200\sqrt{1-x}(x+1)^2+25200\sqrt{1-x}(x+1)-10080\sqrt{1-x}} - \frac{2(x+1)^{\frac{11}{2}}}{315\sqrt{1-x}(x+1)^5-3150\sqrt{1-x}(x+1)^4+12600\sqrt{1-x}(x+1)^3-25200\sqrt{1-x}(x+1)^2+25200\sqrt{1-x}(x+1)-10080\sqrt{1-x}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((1+x)**(3/2)/(1-x)**(11/2),x)
```

```
[Out] Piecewise((-2*I*(x + 1)**(11/2)/(315*sqrt(x - 1)*(x + 1)**5 - 3150*sqrt(x - 1)*(x + 1)**4 + 12600*sqrt(x - 1)*(x + 1)**3 - 25200*sqrt(x - 1)*(x + 1)**2 + 25200*sqrt(x - 1)*(x + 1) - 10080*sqrt(x - 1)) + 22*I*(x + 1)**(9/2)/(315*sqrt(x - 1)*(x + 1)**5 - 3150*sqrt(x - 1)*(x + 1)**4 + 12600*sqrt(x - 1)*(x + 1)**3 - 25200*sqrt(x - 1)*(x + 1)**2 + 25200*sqrt(x - 1)*(x + 1) - 10080*sqrt(x - 1)) - 99*I*(x + 1)**(7/2)/(315*sqrt(x - 1)*(x + 1)**5 - 3150*sqrt(x - 1)*(x + 1)**4 + 12600*sqrt(x - 1)*(x + 1)**3 - 25200*sqrt(x - 1)*(x + 1)**2 + 25200*sqrt(x - 1)*(x + 1) - 10080*sqrt(x - 1)) + 126*I*(x + 1)**(5/2)/(315*sqrt(x - 1)*(x + 1)**5 - 3150*sqrt(x - 1)*(x + 1)**4 + 12600*sqrt(x - 1)*(x + 1)**3 - 25200*sqrt(x - 1)*(x + 1)**2 + 25200*sqrt(x - 1)*(x + 1) - 10080*sqrt(x - 1)), Abs(x + 1)/2 > 1), (2*(x + 1)**(11/2)/(315*sqrt(1 - x)*(x + 1)**5 - 3150*sqrt(1 - x)*(x + 1)**4 + 12600*sqrt(1 - x)*(x + 1)**3 - 25200*sqrt(1 - x)*(x + 1)**2 + 25200*sqrt(1 - x)*(x + 1) - 10080*sqrt(1 - x)) - 22*(x + 1)**(9/2)/(315*sqrt(1 - x)*(x + 1)**5 - 3150*sqrt(1 - x)*(x + 1)**4 + 12600*sqrt(1 - x)*(x + 1)**3 - 25200*sqrt(1 - x)*(x + 1)**2 + 25200*sqrt(1 - x)*(x + 1) - 10080*sqrt(1 - x)) + 99*(x + 1)**(7/2)/(315*sqrt(1 - x)*(x + 1)**5 - 3150*sqrt(1 - x)*(x + 1)**4 + 12600*sqrt(1 - x)*(x + 1)**3 - 25200*sqrt(1 - x)*(x + 1)**2 + 25200*sqrt(1 - x)*(x + 1) - 10080*sqrt(1 - x)) - 126*(x + 1)**(5/2)/(315*sqrt(1 - x)*(x + 1)**5 - 3150*sqrt(1 - x)*(x + 1)**4 + 12600*sqrt(1 - x)*(x + 1)**3 - 25200*sqrt(1 - x)*(x + 1)**2 + 25200*sqrt(1 - x)*(x + 1) - 10080*sqrt(1 - x)), True))
```


$$3.1086 \quad \int \frac{(1+x)^{3/2}}{(1-x)^{13/2}} dx$$

Optimal. Leaf size=81

$$\frac{2(x+1)^{5/2}}{1155(1-x)^{5/2}} + \frac{2(x+1)^{5/2}}{231(1-x)^{7/2}} + \frac{(x+1)^{5/2}}{33(1-x)^{9/2}} + \frac{(x+1)^{5/2}}{11(1-x)^{11/2}}$$

[Out] 1/11*(1+x)^(5/2)/(1-x)^(11/2)+1/33*(1+x)^(5/2)/(1-x)^(9/2)+2/231*(1+x)^(5/2)/(1-x)^(7/2)+2/1155*(1+x)^(5/2)/(1-x)^(5/2)

Rubi [A] time = 0.01, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{2(x+1)^{5/2}}{1155(1-x)^{5/2}} + \frac{2(x+1)^{5/2}}{231(1-x)^{7/2}} + \frac{(x+1)^{5/2}}{33(1-x)^{9/2}} + \frac{(x+1)^{5/2}}{11(1-x)^{11/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(3/2)/(1 - x)^(13/2), x]

[Out] (1 + x)^(5/2)/(11*(1 - x)^(11/2)) + (1 + x)^(5/2)/(33*(1 - x)^(9/2)) + (2*(1 + x)^(5/2))/(231*(1 - x)^(7/2)) + (2*(1 + x)^(5/2))/(1155*(1 - x)^(5/2))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[m] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(1+x)^{3/2}}{(1-x)^{13/2}} dx &= \frac{(1+x)^{5/2}}{11(1-x)^{11/2}} + \frac{3}{11} \int \frac{(1+x)^{3/2}}{(1-x)^{11/2}} dx \\
&= \frac{(1+x)^{5/2}}{11(1-x)^{11/2}} + \frac{(1+x)^{5/2}}{33(1-x)^{9/2}} + \frac{2}{33} \int \frac{(1+x)^{3/2}}{(1-x)^{9/2}} dx \\
&= \frac{(1+x)^{5/2}}{11(1-x)^{11/2}} + \frac{(1+x)^{5/2}}{33(1-x)^{9/2}} + \frac{2(1+x)^{5/2}}{231(1-x)^{7/2}} + \frac{2}{231} \int \frac{(1+x)^{3/2}}{(1-x)^{7/2}} dx \\
&= \frac{(1+x)^{5/2}}{11(1-x)^{11/2}} + \frac{(1+x)^{5/2}}{33(1-x)^{9/2}} + \frac{2(1+x)^{5/2}}{231(1-x)^{7/2}} + \frac{2(1+x)^{5/2}}{1155(1-x)^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.43

$$\frac{(x+1)^{5/2}(-2x^3+16x^2-61x+152)}{1155(1-x)^{11/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1+x)^(3/2)/(1-x)^(13/2),x]

[Out] ((1+x)^(5/2)*(152-61*x+16*x^2-2*x^3))/(1155*(1-x)^(11/2))

fricas [A] time = 0.42, size = 101, normalized size = 1.25

$$\frac{152x^6 - 912x^5 + 2280x^4 - 3040x^3 + 2280x^2 - (2x^5 - 12x^4 + 31x^3 - 46x^2 - 243x - 152)\sqrt{x+1}\sqrt{-x+1} - 912x + 152}{1155(x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(13/2),x, algorithm="fricas")

[Out] 1/1155*(152*x^6 - 912*x^5 + 2280*x^4 - 3040*x^3 + 2280*x^2 - (2*x^5 - 12*x^4 + 31*x^3 - 46*x^2 - 243*x - 152)*sqrt(x+1)*sqrt(-x+1) - 912*x + 152)/(x^6 - 6*x^5 + 15*x^4 - 20*x^3 + 15*x^2 - 6*x + 1)

giac [A] time = 1.17, size = 35, normalized size = 0.43

$$\frac{((2(x+1)(x-10)+99)(x+1)-231)(x+1)^{5/2}\sqrt{-x+1}}{1155(x-1)^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(13/2),x, algorithm="giac")

[Out] $-1/1155*((2*(x + 1)*(x - 10) + 99)*(x + 1) - 231)*(x + 1)^{(5/2)}*\sqrt{-x + 1} / (x - 1)^6$

maple [A] time = 0.00, size = 30, normalized size = 0.37

$$\frac{(x + 1)^{\frac{5}{2}} (2x^3 - 16x^2 + 61x - 152)}{1155(-x + 1)^{\frac{11}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((x+1)^{(3/2)} / (-x+1)^{(13/2)}, x)$

[Out] $-1/1155*(x+1)^{(5/2)}*(2*x^3-16*x^2+61*x-152)/(-x+1)^{(11/2)}$

maxima [B] time = 1.39, size = 218, normalized size = 2.69

$$\frac{(-x^2 + 1)^{\frac{3}{2}}}{4(x^7 - 7x^6 + 21x^5 - 35x^4 + 35x^3 - 21x^2 + 7x - 1)} - \frac{3\sqrt{-x^2 + 1}}{22(x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1)} - \frac{1}{132(x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1)} + \frac{1}{2} \frac{31\sqrt{-x^2 + 1}}{(x^4 - 4x^3 + 6x^2 - 4x + 1)} - \frac{1}{385} \frac{\sqrt{-x^2 + 1}}{(x^3 - 3x^2 + 3x - 1)} + \frac{2}{1155} \frac{\sqrt{-x^2 + 1}}{(x^2 - 2x + 1)} - \frac{2}{1155} \frac{\sqrt{-x^2 + 1}}{(x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((1+x)^{(3/2)} / (1-x)^{(13/2)}, x, \text{algorithm}="maxima")$

[Out] $-1/4*(-x^2 + 1)^{(3/2)} / (x^7 - 7*x^6 + 21*x^5 - 35*x^4 + 35*x^3 - 21*x^2 + 7*x - 1) - 3/22*\sqrt{-x^2 + 1} / (x^6 - 6*x^5 + 15*x^4 - 20*x^3 + 15*x^2 - 6*x + 1) - 1/132*\sqrt{-x^2 + 1} / (x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) + 1/2 * 31*\sqrt{-x^2 + 1} / (x^4 - 4*x^3 + 6*x^2 - 4*x + 1) - 1/385*\sqrt{-x^2 + 1} / (x^3 - 3*x^2 + 3*x - 1) + 2/1155*\sqrt{-x^2 + 1} / (x^2 - 2*x + 1) - 2/1155*\sqrt{-x^2 + 1} / (x - 1)$

mupad [B] time = 0.31, size = 94, normalized size = 1.16

$$\frac{\sqrt{1-x} \left(\frac{81x\sqrt{x+1}}{385} + \frac{152\sqrt{x+1}}{1155} + \frac{46x^2\sqrt{x+1}}{1155} - \frac{31x^3\sqrt{x+1}}{1155} + \frac{4x^4\sqrt{x+1}}{385} - \frac{2x^5\sqrt{x+1}}{1155} \right)}{x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((x + 1)^{(3/2)} / (1 - x)^{(13/2)}, x)$

[Out] $((1 - x)^{(1/2)}*((81*x*(x + 1)^{(1/2)})/385 + (152*(x + 1)^{(1/2)})/1155 + (46*x^2*(x + 1)^{(1/2)})/1155 - (31*x^3*(x + 1)^{(1/2)})/1155 + (4*x^4*(x + 1)^{(1/2)})/385 - (2*x^5*(x + 1)^{(1/2)})/1155)) / (15*x^2 - 6*x - 20*x^3 + 15*x^4 - 6*x^5 + x^6 + 1)$

sympy [B] time = 132.96, size = 1753, normalized size = 21.64

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(3/2)/(1-x)**(13/2),x)

[Out] Piecewise((-2*I*(x + 1)**(17/2)/(1155*sqrt(x - 1)*(x + 1)**8 - 18480*sqrt(x - 1)*(x + 1)**7 + 129360*sqrt(x - 1)*(x + 1)**6 - 517440*sqrt(x - 1)*(x + 1)**5 + 1293600*sqrt(x - 1)*(x + 1)**4 - 2069760*sqrt(x - 1)*(x + 1)**3 + 2069760*sqrt(x - 1)*(x + 1)**2 - 1182720*sqrt(x - 1)*(x + 1) + 295680*sqrt(x - 1)) + 34*I*(x + 1)**(15/2)/(1155*sqrt(x - 1)*(x + 1)**8 - 18480*sqrt(x - 1)*(x + 1)**7 + 129360*sqrt(x - 1)*(x + 1)**6 - 517440*sqrt(x - 1)*(x + 1)**5 + 1293600*sqrt(x - 1)*(x + 1)**4 - 2069760*sqrt(x - 1)*(x + 1)**3 + 2069760*sqrt(x - 1)*(x + 1)**2 - 1182720*sqrt(x - 1)*(x + 1) + 295680*sqrt(x - 1)) - 255*I*(x + 1)**(13/2)/(1155*sqrt(x - 1)*(x + 1)**8 - 18480*sqrt(x - 1)*(x + 1)**7 + 129360*sqrt(x - 1)*(x + 1)**6 - 517440*sqrt(x - 1)*(x + 1)**5 + 1293600*sqrt(x - 1)*(x + 1)**4 - 2069760*sqrt(x - 1)*(x + 1)**3 + 2069760*sqrt(x - 1)*(x + 1)**2 - 1182720*sqrt(x - 1)*(x + 1) + 295680*sqrt(x - 1)) + 1105*I*(x + 1)**(11/2)/(1155*sqrt(x - 1)*(x + 1)**8 - 18480*sqrt(x - 1)*(x + 1)**7 + 129360*sqrt(x - 1)*(x + 1)**6 - 517440*sqrt(x - 1)*(x + 1)**5 + 1293600*sqrt(x - 1)*(x + 1)**4 - 2069760*sqrt(x - 1)*(x + 1)**3 + 2069760*sqrt(x - 1)*(x + 1)**2 - 1182720*sqrt(x - 1)*(x + 1) + 295680*sqrt(x - 1)) - 2750*I*(x + 1)**(9/2)/(1155*sqrt(x - 1)*(x + 1)**8 - 18480*sqrt(x - 1)*(x + 1)**7 + 129360*sqrt(x - 1)*(x + 1)**6 - 517440*sqrt(x - 1)*(x + 1)**5 + 1293600*sqrt(x - 1)*(x + 1)**4 - 2069760*sqrt(x - 1)*(x + 1)**3 + 2069760*sqrt(x - 1)*(x + 1)**2 - 1182720*sqrt(x - 1)*(x + 1) + 295680*sqrt(x - 1)) + 3564*I*(x + 1)**(7/2)/(1155*sqrt(x - 1)*(x + 1)**8 - 18480*sqrt(x - 1)*(x + 1)**7 + 129360*sqrt(x - 1)*(x + 1)**6 - 517440*sqrt(x - 1)*(x + 1)**5 + 1293600*sqrt(x - 1)*(x + 1)**4 - 2069760*sqrt(x - 1)*(x + 1)**3 + 2069760*sqrt(x - 1)*(x + 1)**2 - 1182720*sqrt(x - 1)*(x + 1) + 295680*sqrt(x - 1)) - 1848*I*(x + 1)**(5/2)/(1155*sqrt(x - 1)*(x + 1)**8 - 18480*sqrt(x - 1)*(x + 1)**7 + 129360*sqrt(x - 1)*(x + 1)**6 - 517440*sqrt(x - 1)*(x + 1)**5 + 1293600*sqrt(x - 1)*(x + 1)**4 - 2069760*sqrt(x - 1)*(x + 1)**3 + 2069760*sqrt(x - 1)*(x + 1)**2 - 1182720*sqrt(x - 1)*(x + 1) + 295680*sqrt(x - 1)) , Abs(x + 1)/2 > 1), (2*(x + 1)**(17/2)/(1155*sqrt(1 - x)*(x + 1)**8 - 18480*sqrt(1 - x)*(x + 1)**7 + 129360*sqrt(1 - x)*(x + 1)**6 - 517440*sqrt(1 - x)*(x + 1)**5 + 1293600*sqrt(1 - x)*(x + 1)**4 - 2069760*sqrt(1 - x)*(x + 1)**3 + 2069760*sqrt(1 - x)*(x + 1)**2 - 1182720*sqrt(1 - x)*(x + 1) + 295680*sqrt(1 - x)) - 34*(x + 1)**(15/2)/(1155*sqrt(1 - x)*(x + 1)**8 - 18480*sqrt(1 - x)*(x + 1)**7 + 129360*sqrt(1 - x)*(x + 1)**6 - 517440*sqrt(1 - x)*(x + 1)**5 + 1293600*sqrt(1 - x)*(x + 1)**4 - 2069760*sqrt(1 - x)*(x + 1)**3 + 2069760*sqrt(1 - x)*(x + 1)**2 - 1182720*sqrt(1 - x)*(x + 1) + 295680*sqrt(1 - x)) + 255*(x + 1)**(13/2)/(1155*sqrt(1 - x)*(x + 1)**8 - 18480*sqrt(1 - x)*(x + 1)**7 + 129360*sqrt(1 - x)*(x + 1)**6 - 517440*sqrt(1 - x)*(x + 1)**5 + 1293600*sqrt(1 - x)*(x + 1)**4 - 2069760*sqrt(1 - x)*(x + 1)**3 + 2069760*sqrt(1 - x)*(x + 1)**2 - 1182720*sqrt(1 - x)*(x + 1) + 295680*sqrt(1 - x))

$$\begin{aligned}
& (1-x)(x+1)^7 + 129360\sqrt{1-x}(x+1)^6 - 517440\sqrt{1-x}(x+1)^5 \\
& + 1293600\sqrt{1-x}(x+1)^4 - 2069760\sqrt{1-x}(x+1)^3 + 2069760\sqrt{1-x}(x+1)^2 \\
& - 1182720\sqrt{1-x}(x+1) + 295680\sqrt{1-x}) - 1105(x+1)^{11/2} / (1155\sqrt{1-x}(x+1)^8 - 18480\sqrt{1-x}(x+1)^7 \\
& + 129360\sqrt{1-x}(x+1)^6 - 517440\sqrt{1-x}(x+1)^5 + 1293600\sqrt{1-x}(x+1)^4 \\
& - 2069760\sqrt{1-x}(x+1)^3 + 2069760\sqrt{1-x}(x+1)^2 - 1182720\sqrt{1-x}(x+1) + 295680\sqrt{1-x}) \\
& + 2750(x+1)^{9/2} / (1155\sqrt{1-x}(x+1)^8 - 18480\sqrt{1-x}(x+1)^7 + 129360\sqrt{1-x}(x+1)^6 \\
& - 517440\sqrt{1-x}(x+1)^5 + 1293600\sqrt{1-x}(x+1)^4 - 2069760\sqrt{1-x}(x+1)^3 + 2069760\sqrt{1-x}(x+1)^2 \\
& - 1182720\sqrt{1-x}(x+1) + 295680\sqrt{1-x}) - 3564(x+1)^{7/2} / (1155\sqrt{1-x}(x+1)^8 - 18480\sqrt{1-x}(x+1)^7 \\
& + 129360\sqrt{1-x}(x+1)^6 - 517440\sqrt{1-x}(x+1)^5 + 1293600\sqrt{1-x}(x+1)^4 - 2069760\sqrt{1-x}(x+1)^3 \\
& + 2069760\sqrt{1-x}(x+1)^2 - 1182720\sqrt{1-x}(x+1) + 295680\sqrt{1-x}) \\
& + 1848(x+1)^{5/2} / (1155\sqrt{1-x}(x+1)^8 - 18480\sqrt{1-x}(x+1)^7 + 129360\sqrt{1-x}(x+1)^6 \\
& - 517440\sqrt{1-x}(x+1)^5 + 1293600\sqrt{1-x}(x+1)^4 - 2069760\sqrt{1-x}(x+1)^3 + 2069760\sqrt{1-x}(x+1)^2 \\
& - 1182720\sqrt{1-x}(x+1) + 295680\sqrt{1-x}), \text{ True}
\end{aligned}$$

$$3.1087 \quad \int \frac{(1+x)^{3/2}}{(1-x)^{15/2}} dx$$

Optimal. Leaf size=101

$$\frac{8(x+1)^{5/2}}{15015(1-x)^{5/2}} + \frac{8(x+1)^{5/2}}{3003(1-x)^{7/2}} + \frac{4(x+1)^{5/2}}{429(1-x)^{9/2}} + \frac{4(x+1)^{5/2}}{143(1-x)^{11/2}} + \frac{(x+1)^{5/2}}{13(1-x)^{13/2}}$$

[Out] 1/13*(1+x)^(5/2)/(1-x)^(13/2)+4/143*(1+x)^(5/2)/(1-x)^(11/2)+4/429*(1+x)^(5/2)/(1-x)^(9/2)+8/3003*(1+x)^(5/2)/(1-x)^(7/2)+8/15015*(1+x)^(5/2)/(1-x)^(5/2)

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{8(x+1)^{5/2}}{15015(1-x)^{5/2}} + \frac{8(x+1)^{5/2}}{3003(1-x)^{7/2}} + \frac{4(x+1)^{5/2}}{429(1-x)^{9/2}} + \frac{4(x+1)^{5/2}}{143(1-x)^{11/2}} + \frac{(x+1)^{5/2}}{13(1-x)^{13/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(3/2)/(1 - x)^(15/2), x]

[Out] (1 + x)^(5/2)/(13*(1 - x)^(13/2)) + (4*(1 + x)^(5/2))/(143*(1 - x)^(11/2)) + (4*(1 + x)^(5/2))/(429*(1 - x)^(9/2)) + (8*(1 + x)^(5/2))/(3003*(1 - x)^(7/2)) + (8*(1 + x)^(5/2))/(15015*(1 - x)^(5/2))

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned}
\int \frac{(1+x)^{3/2}}{(1-x)^{15/2}} dx &= \frac{(1+x)^{5/2}}{13(1-x)^{13/2}} + \frac{4}{13} \int \frac{(1+x)^{3/2}}{(1-x)^{13/2}} dx \\
&= \frac{(1+x)^{5/2}}{13(1-x)^{13/2}} + \frac{4(1+x)^{5/2}}{143(1-x)^{11/2}} + \frac{12}{143} \int \frac{(1+x)^{3/2}}{(1-x)^{11/2}} dx \\
&= \frac{(1+x)^{5/2}}{13(1-x)^{13/2}} + \frac{4(1+x)^{5/2}}{143(1-x)^{11/2}} + \frac{4(1+x)^{5/2}}{429(1-x)^{9/2}} + \frac{8}{429} \int \frac{(1+x)^{3/2}}{(1-x)^{9/2}} dx \\
&= \frac{(1+x)^{5/2}}{13(1-x)^{13/2}} + \frac{4(1+x)^{5/2}}{143(1-x)^{11/2}} + \frac{4(1+x)^{5/2}}{429(1-x)^{9/2}} + \frac{8(1+x)^{5/2}}{3003(1-x)^{7/2}} + \frac{8 \int \frac{(1+x)^{3/2}}{(1-x)^{7/2}} dx}{3003} \\
&= \frac{(1+x)^{5/2}}{13(1-x)^{13/2}} + \frac{4(1+x)^{5/2}}{143(1-x)^{11/2}} + \frac{4(1+x)^{5/2}}{429(1-x)^{9/2}} + \frac{8(1+x)^{5/2}}{3003(1-x)^{7/2}} + \frac{8(1+x)^{5/2}}{15015(1-x)^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 40, normalized size = 0.40

$$\frac{(x+1)^{5/2} (8x^4 - 72x^3 + 308x^2 - 852x + 1763)}{15015(1-x)^{13/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1+x)^(3/2)/(1-x)^(15/2),x]

[Out] ((1+x)^(5/2)*(1763-852*x+308*x^2-72*x^3+8*x^4))/(15015*(1-x)^(13/2))

fricas [A] time = 0.43, size = 116, normalized size = 1.15

$$\frac{1763x^7 - 12341x^6 + 37023x^5 - 61705x^4 + 61705x^3 - 37023x^2 - (8x^6 - 56x^5 + 172x^4 - 308x^3 + 367x^2 + 2674x + 1763)\sqrt{x+1}}{15015(x^7 - 7x^6 + 21x^5 - 35x^4 + 35x^3 - 21x^2 + 7x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(15/2),x, algorithm="fricas")

[Out] 1/15015*(1763*x^7 - 12341*x^6 + 37023*x^5 - 61705*x^4 + 61705*x^3 - 37023*x^2 - (8*x^6 - 56*x^5 + 172*x^4 - 308*x^3 + 367*x^2 + 2674*x + 1763)*sqrt(x+1)*sqrt(-x+1) + 12341*x - 1763)/(x^7 - 7*x^6 + 21*x^5 - 35*x^4 + 35*x^3 - 21*x^2 + 7*x - 1)

giac [A] time = 1.23, size = 42, normalized size = 0.42

$$\frac{(4((2(x+1)(x-12)+143)(x+1)-429)(x+1)+3003)(x+1)^{5/2}\sqrt{-x+1}}{15015(x-1)^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(15/2),x, algorithm="giac")

[Out] -1/15015*(4*((2*(x + 1)*(x - 12) + 143)*(x + 1) - 429)*(x + 1) + 3003)*(x + 1)^(5/2)*sqrt(-x + 1)/(x - 1)^7

maple [A] time = 0.00, size = 35, normalized size = 0.35

$$\frac{(x+1)^{\frac{5}{2}}(8x^4 - 72x^3 + 308x^2 - 852x + 1763)}{15015(-x+1)^{\frac{13}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(3/2)/(-x+1)^(15/2),x)

[Out] 1/15015*(x+1)^(5/2)*(8*x^4-72*x^3+308*x^2-852*x+1763)/(-x+1)^(13/2)

maxima [B] time = 1.38, size = 269, normalized size = 2.66

$$\frac{(-x^2+1)^{\frac{3}{2}}}{5(x^8-8x^7+28x^6-56x^5+70x^4-56x^3+28x^2-8x+1)} + \frac{6\sqrt{-x^2+1}}{65(x^7-7x^6+21x^5-35x^4+35x^3-21x^2+7x-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(3/2)/(1-x)^(15/2),x, algorithm="maxima")

[Out] 1/5*(-x^2 + 1)^(3/2)/(x^8 - 8*x^7 + 28*x^6 - 56*x^5 + 70*x^4 - 56*x^3 + 28*x^2 - 8*x + 1) + 6/65*sqrt(-x^2 + 1)/(x^7 - 7*x^6 + 21*x^5 - 35*x^4 + 35*x^3 - 21*x^2 + 7*x - 1) + 3/715*sqrt(-x^2 + 1)/(x^6 - 6*x^5 + 15*x^4 - 20*x^3 + 15*x^2 - 6*x + 1) - 1/429*sqrt(-x^2 + 1)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) + 4/3003*sqrt(-x^2 + 1)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1) - 4/5005*sqrt(-x^2 + 1)/(x^3 - 3*x^2 + 3*x - 1) + 8/15015*sqrt(-x^2 + 1)/(x^2 - 2*x + 1) - 8/15015*sqrt(-x^2 + 1)/(x - 1)

mupad [B] time = 0.33, size = 110, normalized size = 1.09

$$\frac{\sqrt{1-x} \left(\frac{382x\sqrt{x+1}}{2145} + \frac{1763\sqrt{x+1}}{15015} + \frac{367x^2\sqrt{x+1}}{15015} - \frac{4x^3\sqrt{x+1}}{195} + \frac{172x^4\sqrt{x+1}}{15015} - \frac{8x^5\sqrt{x+1}}{2145} + \frac{8x^6\sqrt{x+1}}{15015} \right)}{x^7 - 7x^6 + 21x^5 - 35x^4 + 35x^3 - 21x^2 + 7x - 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(3/2)/(1 - x)^(15/2),x)


```
[Out] -((1 - x)^(1/2)*((382*x*(x + 1)^(1/2))/2145 + (1763*(x + 1)^(1/2))/15015 +  
(367*x^2*(x + 1)^(1/2))/15015 - (4*x^3*(x + 1)^(1/2))/195 + (172*x^4*(x + 1)  
)^(1/2))/15015 - (8*x^5*(x + 1)^(1/2))/2145 + (8*x^6*(x + 1)^(1/2))/15015))  
/(7*x - 21*x^2 + 35*x^3 - 35*x^4 + 21*x^5 - 7*x^6 + x^7 - 1)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((1+x)**(3/2)/(1-x)**(15/2),x)
```

```
[Out] Timed out
```

3.1088 $\int (1-x)^{11/2} (1+x)^{5/2} dx$

Optimal. Leaf size=130

$$\frac{1}{9}(x+1)^{7/2}(1-x)^{11/2} + \frac{11}{72}(x+1)^{7/2}(1-x)^{9/2} + \frac{11}{56}(x+1)^{7/2}(1-x)^{7/2} + \frac{11}{48}x(x+1)^{5/2}(1-x)^{5/2} + \frac{55}{192}x(x+1)^{3/2}(1-x)^{3/2} + \frac{55}{128}x$$

[Out] 55/192*(1-x)^(3/2)*x*(1+x)^(3/2)+11/48*(1-x)^(5/2)*x*(1+x)^(5/2)+11/56*(1-x)^(7/2)*(1+x)^(7/2)+11/72*(1-x)^(9/2)*(1+x)^(7/2)+1/9*(1-x)^(11/2)*(1+x)^(7/2)+55/128*arcsin(x)+55/128*x*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.03, antiderivative size = 130, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$\frac{1}{9}(x+1)^{7/2}(1-x)^{11/2} + \frac{11}{72}(x+1)^{7/2}(1-x)^{9/2} + \frac{11}{56}(x+1)^{7/2}(1-x)^{7/2} + \frac{11}{48}x(x+1)^{5/2}(1-x)^{5/2} + \frac{55}{192}x(x+1)^{3/2}(1-x)^{3/2} + \frac{55}{128}x$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(11/2)*(1 + x)^(5/2), x]

[Out] (55*sqrt[1 - x]*x*sqrt[1 + x])/128 + (55*(1 - x)^(3/2)*x*(1 + x)^(3/2))/192 + (11*(1 - x)^(5/2)*x*(1 + x)^(5/2))/48 + (11*(1 - x)^(7/2)*(1 + x)^(7/2))/56 + (11*(1 - x)^(9/2)*(1 + x)^(7/2))/72 + ((1 - x)^(11/2)*(1 + x)^(7/2))/9 + (55*ArcSin[x])/128

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(x*(a + b*x)^(m+1)*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m-1)*(c + d*x)^(n-1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m+1)*(c + d*x)^n/(b*(m+n+1)), x] + Dist[(2*c*n)/(m+n+1), Int[(a + b*x)^(m-1)*(c + d*x)^(n-1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
 \int (1-x)^{11/2}(1+x)^{5/2} dx &= \frac{1}{9}(1-x)^{11/2}(1+x)^{7/2} + \frac{11}{9} \int (1-x)^{9/2}(1+x)^{5/2} dx \\
 &= \frac{11}{72}(1-x)^{9/2}(1+x)^{7/2} + \frac{1}{9}(1-x)^{11/2}(1+x)^{7/2} + \frac{11}{8} \int (1-x)^{7/2}(1+x)^{5/2} dx \\
 &= \frac{11}{56}(1-x)^{7/2}(1+x)^{7/2} + \frac{11}{72}(1-x)^{9/2}(1+x)^{7/2} + \frac{1}{9}(1-x)^{11/2}(1+x)^{7/2} + \frac{11}{8} \int (1-x)^{5/2}(1+x)^{5/2} dx \\
 &= \frac{11}{48}(1-x)^{5/2}x(1+x)^{5/2} + \frac{11}{56}(1-x)^{7/2}(1+x)^{7/2} + \frac{11}{72}(1-x)^{9/2}(1+x)^{7/2} + \frac{1}{9}(1-x)^{11/2}(1+x)^{7/2} \\
 &= \frac{55}{192}(1-x)^{3/2}x(1+x)^{3/2} + \frac{11}{48}(1-x)^{5/2}x(1+x)^{5/2} + \frac{11}{56}(1-x)^{7/2}(1+x)^{7/2} + \frac{11}{72}(1-x)^{9/2}(1+x)^{7/2} \\
 &= \frac{55}{128}\sqrt{1-x}x\sqrt{1+x} + \frac{55}{192}(1-x)^{3/2}x(1+x)^{3/2} + \frac{11}{48}(1-x)^{5/2}x(1+x)^{5/2} + \frac{11}{56}(1-x)^{7/2}(1+x)^{7/2} \\
 &= \frac{55}{128}\sqrt{1-x}x\sqrt{1+x} + \frac{55}{192}(1-x)^{3/2}x(1+x)^{3/2} + \frac{11}{48}(1-x)^{5/2}x(1+x)^{5/2} + \frac{11}{56}(1-x)^{7/2}(1+x)^{7/2} \\
 &= \frac{55}{128}\sqrt{1-x}x\sqrt{1+x} + \frac{55}{192}(1-x)^{3/2}x(1+x)^{3/2} + \frac{11}{48}(1-x)^{5/2}x(1+x)^{5/2} + \frac{11}{56}(1-x)^{7/2}(1+x)^{7/2}
 \end{aligned}$$

Mathematica [A] time = 0.07, size = 75, normalized size = 0.58

$$\frac{\sqrt{1-x^2} (-896x^8 + 3024x^7 - 1024x^6 - 7224x^5 + 8448x^4 + 3066x^3 - 10240x^2 + 4599x + 3712) - 6930 \sin^{-1}\left(\frac{x}{\sqrt{2}}\right)}{8064}$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(11/2)*(1 + x)^(5/2), x]

[Out] (Sqrt[1 - x^2]*(3712 + 4599*x - 10240*x^2 + 3066*x^3 + 8448*x^4 - 7224*x^5 - 1024*x^6 + 3024*x^7 - 896*x^8) - 6930*ArcSin[Sqrt[1 - x]/Sqrt[2]])/8064

fricas [A] time = 0.45, size = 77, normalized size = 0.59

$$-\frac{1}{8064} (896x^8 - 3024x^7 + 1024x^6 + 7224x^5 - 8448x^4 - 3066x^3 + 10240x^2 - 4599x - 3712)\sqrt{x+1}\sqrt{-x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(11/2)*(1+x)^(5/2),x, algorithm="fricas")

[Out] -1/8064*(896*x^8 - 3024*x^7 + 1024*x^6 + 7224*x^5 - 8448*x^4 - 3066*x^3 + 10240*x^2 - 4599*x - 3712)*sqrt(x + 1)*sqrt(-x + 1) - 55/64*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [B] time = 1.40, size = 323, normalized size = 2.48

$$-\frac{1}{40320} ((2((4(5(2(7(8x-65)(x+1)+2073)(x+1)-9833)(x+1)+75293)(x+1)-310203)(x+1)+21699$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(11/2)*(1+x)^(5/2),x, algorithm="giac")

[Out] -1/40320*((2*((4*(5*(2*(7*(8*x - 65)*(x + 1) + 2073)*(x + 1) - 9833)*(x + 1) + 75293)*(x + 1) - 310203)*(x + 1) + 216993)*(x + 1) - 205275)*(x + 1) + 69615)*sqrt(x + 1)*sqrt(-x + 1) + 1/6720*((2*((4*(5*(6*(7*x - 50)*(x + 1) + 1219)*(x + 1) - 12463)*(x + 1) + 64233)*(x + 1) - 53963)*(x + 1) + 59465)*(x + 1) - 23205)*sqrt(x + 1)*sqrt(-x + 1) + 1/840*((2*((4*(5*(6*x - 37)*(x + 1) + 661)*(x + 1) - 4551)*(x + 1) + 4781)*(x + 1) - 6335)*(x + 1) + 2835)*sqrt(x + 1)*sqrt(-x + 1) - 1/40*((2*((4*(5*x - 26)*(x + 1) + 321)*(x + 1) - 451)*(x + 1) + 745)*(x + 1) - 405)*sqrt(x + 1)*sqrt(-x + 1) + 1/4*((2*(3*x - 10)*(x + 1) + 43)*(x + 1) - 39)*sqrt(x + 1)*sqrt(-x + 1) - 1/3*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) - sqrt(x + 1)*(x - 2)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + 55/64*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.01, size = 155, normalized size = 1.19

$$\frac{55\sqrt{(x+1)(-x+1)} \arcsin(x)}{128\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{11}{2}}(x+1)^{\frac{7}{2}}}{9} + \frac{11(-x+1)^{\frac{9}{2}}(x+1)^{\frac{7}{2}}}{72} + \frac{11(-x+1)^{\frac{7}{2}}(x+1)^{\frac{7}{2}}}{56} + \frac{11(-x+1)^{\frac{5}{2}}}{48}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(11/2)*(x+1)^(5/2),x)

[Out] 1/9*(-x+1)^(11/2)*(x+1)^(7/2)+11/72*(-x+1)^(9/2)*(x+1)^(7/2)+11/56*(-x+1)^(7/2)*(x+1)^(7/2)+11/48*(-x+1)^(5/2)*(x+1)^(7/2)+11/48*(-x+1)^(3/2)*(x+1)^(7/2)+11/64*(-x+1)^(1/2)*(x+1)^(7/2)-11/192*(-x+1)^(1/2)*(x+1)^(5/2)-55/384*(-x+1)^(1/2)*(x+1)^(3/2)-55/128*(-x+1)^(1/2)*(x+1)^(1/2)+55/128*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 3.01, size = 78, normalized size = 0.60

$$\frac{1}{9}(-x^2+1)^{\frac{7}{2}}x^2 - \frac{3}{8}(-x^2+1)^{\frac{7}{2}}x + \frac{29}{63}(-x^2+1)^{\frac{7}{2}} + \frac{11}{48}(-x^2+1)^{\frac{5}{2}}x + \frac{55}{192}(-x^2+1)^{\frac{3}{2}}x + \frac{55}{128}\sqrt{-x^2+1}x + \frac{55}{128}\arcsin$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(11/2)*(1+x)^(5/2),x, algorithm="maxima")

[Out] $\frac{1}{9}*(-x^2 + 1)^{(7/2)}*x^2 - \frac{3}{8}*(-x^2 + 1)^{(7/2)}*x + \frac{29}{63}*(-x^2 + 1)^{(7/2)} + \frac{11}{48}*(-x^2 + 1)^{(5/2)}*x + \frac{55}{192}*(-x^2 + 1)^{(3/2)}*x + \frac{55}{128}*\text{sqrt}(-x^2 + 1)*x + \frac{55}{128}*\text{arcsin}(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{11/2} (x+1)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(11/2)*(x + 1)^(5/2),x)

[Out] int((1 - x)^(11/2)*(x + 1)^(5/2), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(11/2)*(1+x)**(5/2),x)

[Out] Timed out

3.1089 $\int (1-x)^{9/2}(1+x)^{5/2} dx$

Optimal. Leaf size=110

$$\frac{1}{8}(x+1)^{7/2}(1-x)^{9/2} + \frac{9}{56}(x+1)^{7/2}(1-x)^{7/2} + \frac{3}{16}x(x+1)^{5/2}(1-x)^{5/2} + \frac{15}{64}x(x+1)^{3/2}(1-x)^{3/2} + \frac{45}{128}x\sqrt{x+1}\sqrt{1-x} + \frac{45}{128}\arcsin(x)$$

[Out] $15/64*(1-x)^{(3/2)}*x*(1+x)^{(3/2)}+3/16*(1-x)^{(5/2)}*x*(1+x)^{(5/2)}+9/56*(1-x)^{(7/2)}*(1+x)^{(7/2)}+1/8*(1-x)^{(9/2)}*(1+x)^{(7/2)}+45/128*\arcsin(x)+45/128*x*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 110, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$\frac{1}{8}(x+1)^{7/2}(1-x)^{9/2} + \frac{9}{56}(x+1)^{7/2}(1-x)^{7/2} + \frac{3}{16}x(x+1)^{5/2}(1-x)^{5/2} + \frac{15}{64}x(x+1)^{3/2}(1-x)^{3/2} + \frac{45}{128}x\sqrt{x+1}\sqrt{1-x} + \frac{45}{128}\arcsin(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(9/2)*(1 + x)^(5/2), x]

[Out] $(45*\text{Sqrt}[1 - x]*x*\text{Sqrt}[1 + x])/128 + (15*(1 - x)^{(3/2)}*x*(1 + x)^{(3/2)})/64 + (3*(1 - x)^{(5/2)}*x*(1 + x)^{(5/2)})/16 + (9*(1 - x)^{(7/2)}*(1 + x)^{(7/2)})/56 + ((1 - x)^{(9/2)}*(1 + x)^{(7/2)})/8 + (45*\text{ArcSin}[x])/128$

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(x*(a + b*x)^(m+1)*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m-1)*(c + d*x)^(n-1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^(m), x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m+1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(2*c*n)/(m + n + 1), Int[(a + b*x)^(m)*(c + d*x)^(n-1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int (1-x)^{9/2}(1+x)^{5/2} dx &= \frac{1}{8}(1-x)^{9/2}(1+x)^{7/2} + \frac{9}{8} \int (1-x)^{7/2}(1+x)^{5/2} dx \\
 &= \frac{9}{56}(1-x)^{7/2}(1+x)^{7/2} + \frac{1}{8}(1-x)^{9/2}(1+x)^{7/2} + \frac{9}{8} \int (1-x)^{5/2}(1+x)^{5/2} dx \\
 &= \frac{3}{16}(1-x)^{5/2}x(1+x)^{5/2} + \frac{9}{56}(1-x)^{7/2}(1+x)^{7/2} + \frac{1}{8}(1-x)^{9/2}(1+x)^{7/2} + \frac{15}{16} \int (1-x)^{3/2}x(1+x)^{5/2} dx \\
 &= \frac{15}{64}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{16}(1-x)^{5/2}x(1+x)^{5/2} + \frac{9}{56}(1-x)^{7/2}(1+x)^{7/2} + \frac{1}{8}(1-x)^{9/2}(1+x)^{7/2} \\
 &= \frac{45}{128}\sqrt{1-x}x\sqrt{1+x} + \frac{15}{64}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{16}(1-x)^{5/2}x(1+x)^{5/2} + \frac{9}{56}(1-x)^{7/2}(1+x)^{7/2} \\
 &= \frac{45}{128}\sqrt{1-x}x\sqrt{1+x} + \frac{15}{64}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{16}(1-x)^{5/2}x(1+x)^{5/2} + \frac{9}{56}(1-x)^{7/2}(1+x)^{7/2} \\
 &= \frac{45}{128}\sqrt{1-x}x\sqrt{1+x} + \frac{15}{64}(1-x)^{3/2}x(1+x)^{3/2} + \frac{3}{16}(1-x)^{5/2}x(1+x)^{5/2} + \frac{9}{56}(1-x)^{7/2}(1+x)^{7/2}
 \end{aligned}$$

Mathematica [A] time = 0.06, size = 70, normalized size = 0.64

$$\frac{1}{896} \left(\sqrt{1-x^2} (112x^7 - 256x^6 - 168x^5 + 768x^4 - 210x^3 - 768x^2 + 581x + 256) - 630 \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(1-x)^(9/2)*(1+x)^(5/2),x]

[Out] (Sqrt[1-x^2]*(256+581*x-768*x^2-210*x^3+768*x^4-168*x^5-256*x^6+112*x^7)-630*ArcSin[Sqrt[1-x]/Sqrt[2]])/896

fricas [A] time = 0.44, size = 72, normalized size = 0.65

$$\frac{1}{896} (112x^7 - 256x^6 - 168x^5 + 768x^4 - 210x^3 - 768x^2 + 581x + 256) \sqrt{x+1} \sqrt{-x+1} - \frac{45}{64} \arctan \left(\frac{\sqrt{x+1}}{\sqrt{-x+1}} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(9/2)*(1+x)^(5/2),x, algorithm="fricas")

[Out] $\frac{1}{896}*(112*x^7 - 256*x^6 - 168*x^5 + 768*x^4 - 210*x^3 - 768*x^2 + 581*x + 256)*\sqrt{x+1}*\sqrt{-x+1} - \frac{45}{64}*\arctan\left(\frac{\sqrt{x+1}*\sqrt{-x+1} - 1}{x}\right)$

giac [B] time = 1.49, size = 296, normalized size = 2.69

$$\frac{1}{13440} \left((2 \left((4 \left(5 \left(6 \left(7x - 50 \right) (x + 1) + 1219 \right) (x + 1) - 12463 \right) (x + 1) + 64233 \right) (x + 1) - 53963 \right) (x + 1) + 59465 \right) (x + 1) - 23205 \right) \sqrt{x + 1} \sqrt{-x + 1} - \frac{1}{1680} \left((2 \left((4 \left(5 \left(6x - 37 \right) (x + 1) + 661 \right) (x + 1) - 4551 \right) (x + 1) + 4781 \right) (x + 1) - 6335 \right) (x + 1) + 2835 \right) \sqrt{x + 1} \sqrt{-x + 1} - \frac{1}{80} \left((2 \left((4 \left(5x - 26 \right) (x + 1) + 321 \right) (x + 1) - 451 \right) (x + 1) + 745 \right) (x + 1) - 405 \right) \sqrt{x + 1} \sqrt{-x + 1} + \frac{1}{40} \left((2 \left(3 \left(4x - 17 \right) (x + 1) + 133 \right) (x + 1) - 295 \right) (x + 1) + 195 \right) \sqrt{x + 1} \sqrt{-x + 1} + \frac{1}{8} \left((2 \left(3x - 10 \right) (x + 1) + 43 \right) (x + 1) - 39 \right) \sqrt{x + 1} \sqrt{-x + 1} - \frac{1}{2} \left((2x - 5) (x + 1) + 9 \right) \sqrt{x + 1} \sqrt{-x + 1} - \frac{1}{2} \sqrt{x + 1} (x - 2) \sqrt{-x + 1} + \sqrt{x + 1} \sqrt{-x + 1} + \frac{45}{64} \arcsin\left(\frac{1}{2} \sqrt{2} \sqrt{x + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(9/2)*(1+x)^(5/2),x, algorithm="giac")`

[Out] $\frac{1}{13440} \left((2 \left((4 \left(5 \left(6 \left(7x - 50 \right) (x + 1) + 1219 \right) (x + 1) - 12463 \right) (x + 1) + 64233 \right) (x + 1) - 53963 \right) (x + 1) + 59465 \right) (x + 1) - 23205 \right) \sqrt{x + 1} \sqrt{-x + 1} - \frac{1}{1680} \left((2 \left((4 \left(5 \left(6x - 37 \right) (x + 1) + 661 \right) (x + 1) - 4551 \right) (x + 1) + 4781 \right) (x + 1) - 6335 \right) (x + 1) + 2835 \right) \sqrt{x + 1} \sqrt{-x + 1} - \frac{1}{80} \left((2 \left((4 \left(5x - 26 \right) (x + 1) + 321 \right) (x + 1) - 451 \right) (x + 1) + 745 \right) (x + 1) - 405 \right) \sqrt{x + 1} \sqrt{-x + 1} + \frac{1}{40} \left((2 \left(3 \left(4x - 17 \right) (x + 1) + 133 \right) (x + 1) - 295 \right) (x + 1) + 195 \right) \sqrt{x + 1} \sqrt{-x + 1} + \frac{1}{8} \left((2 \left(3x - 10 \right) (x + 1) + 43 \right) (x + 1) - 39 \right) \sqrt{x + 1} \sqrt{-x + 1} - \frac{1}{2} \left((2x - 5) (x + 1) + 9 \right) \sqrt{x + 1} \sqrt{-x + 1} - \frac{1}{2} \sqrt{x + 1} (x - 2) \sqrt{-x + 1} + \sqrt{x + 1} \sqrt{-x + 1} + \frac{45}{64} \arcsin\left(\frac{1}{2} \sqrt{2} \sqrt{x + 1}\right)$

maple [A] time = 0.00, size = 141, normalized size = 1.28

$$\frac{45\sqrt{x+1}(-x+1)\arcsin(x)}{128\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{9}{2}}(x+1)^{\frac{7}{2}}}{8} + \frac{9(-x+1)^{\frac{7}{2}}(x+1)^{\frac{7}{2}}}{56} + \frac{3(-x+1)^{\frac{5}{2}}(x+1)^{\frac{7}{2}}}{16} + \frac{3(-x+1)^{\frac{3}{2}}(x+1)^{\frac{7}{2}}}{16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-x+1)^(9/2)*(x+1)^(5/2),x)`

[Out] $\frac{1}{8}*(-x+1)^{(9/2)}*(x+1)^{(7/2)} + \frac{9}{56}*(-x+1)^{(7/2)}*(x+1)^{(7/2)} + \frac{3}{16}*(-x+1)^{(5/2)}*(x+1)^{(7/2)} + \frac{3}{16}*(-x+1)^{(3/2)}*(x+1)^{(7/2)} + \frac{9}{64}*(-x+1)^{(1/2)}*(x+1)^{(7/2)} - \frac{3}{64}*(-x+1)^{(1/2)}*(x+1)^{(5/2)} - \frac{15}{128}*(-x+1)^{(1/2)}*(x+1)^{(3/2)} - \frac{45}{128}*(-x+1)^{(1/2)}*(x+1)^{(1/2)} + \frac{45}{128}*((x+1)*(-x+1))^{(1/2)}/(x+1)^{(1/2)}/(-x+1)^{(1/2)}*\arcsin(x)$

maxima [A] time = 2.97, size = 64, normalized size = 0.58

$$-\frac{1}{8}(-x^2+1)^{\frac{7}{2}}x + \frac{2}{7}(-x^2+1)^{\frac{7}{2}} + \frac{3}{16}(-x^2+1)^{\frac{5}{2}}x + \frac{15}{64}(-x^2+1)^{\frac{3}{2}}x + \frac{45}{128}\sqrt{-x^2+1}x + \frac{45}{128}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(9/2)*(1+x)^(5/2),x, algorithm="maxima")

[Out] $-1/8*(-x^2 + 1)^{(7/2)}*x + 2/7*(-x^2 + 1)^{(7/2)} + 3/16*(-x^2 + 1)^{(5/2)}*x + 15/64*(-x^2 + 1)^{(3/2)}*x + 45/128*\text{sqrt}(-x^2 + 1)*x + 45/128*\text{arcsin}(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{9/2} (x+1)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(9/2)*(x + 1)^(5/2),x)

[Out] int((1 - x)^(9/2)*(x + 1)^(5/2), x)

sympy [A] time = 117.57, size = 360, normalized size = 3.27

$$\left\{ \begin{array}{l} -\frac{45i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{64} + \frac{i(x+1)^{17/2}}{8\sqrt{x-1}} - \frac{79i(x+1)^{15/2}}{56\sqrt{x-1}} + \frac{725i(x+1)^{13/2}}{112\sqrt{x-1}} - \frac{1699i(x+1)^{11/2}}{112\sqrt{x-1}} + \frac{8191i(x+1)^9}{448\sqrt{x-1}} - \frac{4099i(x+1)^7}{448\sqrt{x-1}} - \frac{3i(x+1)^5}{128\sqrt{x-1}} - \frac{15i(x+1)^3}{128\sqrt{x-1}} \\ \frac{45 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{64} - \frac{(x+1)^{17/2}}{8\sqrt{1-x}} + \frac{79(x+1)^{15/2}}{56\sqrt{1-x}} - \frac{725(x+1)^{13/2}}{112\sqrt{1-x}} + \frac{1699(x+1)^{11/2}}{112\sqrt{1-x}} - \frac{8191(x+1)^9}{448\sqrt{1-x}} + \frac{4099(x+1)^7}{448\sqrt{1-x}} + \frac{3(x+1)^5}{128\sqrt{1-x}} + \frac{15(x+1)^3}{128\sqrt{1-x}} - \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(9/2)*(1+x)**(5/2),x)

[Out] Piecewise((-45*I*acosh(sqrt(2)*sqrt(x + 1)/2)/64 + I*(x + 1)**(17/2)/(8*sqrt(x - 1)) - 79*I*(x + 1)**(15/2)/(56*sqrt(x - 1)) + 725*I*(x + 1)**(13/2)/(112*sqrt(x - 1)) - 1699*I*(x + 1)**(11/2)/(112*sqrt(x - 1)) + 8191*I*(x + 1)**(9/2)/(448*sqrt(x - 1)) - 4099*I*(x + 1)**(7/2)/(448*sqrt(x - 1)) - 3*I*(x + 1)**(5/2)/(128*sqrt(x - 1)) - 15*I*(x + 1)**(3/2)/(128*sqrt(x - 1)) + 45*I*sqrt(x + 1)/(64*sqrt(x - 1)), Abs(x + 1)/2 > 1), (45*asin(sqrt(2)*sqrt(x + 1)/2)/64 - (x + 1)**(17/2)/(8*sqrt(1 - x)) + 79*(x + 1)**(15/2)/(56*sqrt(1 - x)) - 725*(x + 1)**(13/2)/(112*sqrt(1 - x)) + 1699*(x + 1)**(11/2)/(112*sqrt(1 - x)) - 8191*(x + 1)**(9/2)/(448*sqrt(1 - x)) + 4099*(x + 1)**(7/2)/(448*sqrt(1 - x)) + 3*(x + 1)**(5/2)/(128*sqrt(1 - x)) + 15*(x + 1)**(3/2)/(128*sqrt(1 - x)) - 45*sqrt(x + 1)/(64*sqrt(1 - x)), True))

3.1090 $\int (1-x)^{7/2}(1+x)^{5/2} dx$

Optimal. Leaf size=90

$$\frac{1}{7}(1-x)^{7/2}(x+1)^{7/2} + \frac{1}{6}(1-x)^{5/2}x(x+1)^{5/2} + \frac{5}{24}(1-x)^{3/2}x(x+1)^{3/2} + \frac{5}{16}\sqrt{1-x}x\sqrt{x+1} + \frac{5}{16}\sin^{-1}(x)$$

[Out] $5/24*(1-x)^{(3/2)}*x*(1+x)^{(3/2)}+1/6*(1-x)^{(5/2)}*x*(1+x)^{(5/2)}+1/7*(1-x)^{(7/2)}*(1+x)^{(7/2)}+5/16*\arcsin(x)+5/16*x*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 90, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$\frac{1}{7}(1-x)^{7/2}(x+1)^{7/2} + \frac{1}{6}(1-x)^{5/2}x(x+1)^{5/2} + \frac{5}{24}(1-x)^{3/2}x(x+1)^{3/2} + \frac{5}{16}\sqrt{1-x}x\sqrt{x+1} + \frac{5}{16}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(1-x)^{(7/2)}*(1+x)^{(5/2)}, x]$

[Out] $(5*\text{Sqrt}[1-x]*x*\text{Sqrt}[1+x])/16 + (5*(1-x)^{(3/2)}*x*(1+x)^{(3/2)})/24 + ((1-x)^{(5/2)}*x*(1+x)^{(5/2)})/6 + ((1-x)^{(7/2)}*(1+x)^{(7/2)})/7 + (5*\text{ArcSin}[x])/16$

Rule 38

$\text{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(m_+)}, x_Symbol] :> \text{Simp}[(x_+*(a_+ + b_+*x_+)^{m_+}*(c_+ + d_+*x_+)^{m_+}/(2*m_+ + 1), x] + \text{Dist}[(2*a_+*c_+*m_+)/(2*m_+ + 1), \text{Int}[(a_+ + b_+*x_+)^{(m_+ - 1)}*(c_+ + d_+*x_+)^{(m_+ - 1)}, x], x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{EqQ}[b*c + a*d, 0] \&\& \text{IGtQ}[m + 1/2, 0]$

Rule 41

$\text{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(m_+)}, x_Symbol] :> \text{Int}[(a_+*c_+ + b_+*d_+*x_+^2)^{m_+}, x] /; \text{FreeQ}\{a, b, c, d, m\}, x] \&\& \text{EqQ}[b*c + a*d, 0] \&\& (\text{IntegerQ}[m] \|\| (\text{GtQ}[a, 0] \&\& \text{GtQ}[c, 0]))$

Rule 49

$\text{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] :> \text{Simp}[(a_+ + b_+*x_+)^{(m_+ + 1)}*(c_+ + d_+*x_+)^{n_+}/(b_+(m_+ + n_+ + 1)), x] + \text{Dist}[(2*c_+*n_+)/(m_+ + n_+ + 1), \text{Int}[(a_+ + b_+*x_+)^{m_+}*(c_+ + d_+*x_+)^{(n_+ - 1)}, x], x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{EqQ}[b*c + a*d, 0] \&\& \text{IGtQ}[m + 1/2, 0] \&\& \text{IGtQ}[n + 1/2, 0] \&\& \text{LtQ}[m, n]$

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int (1-x)^{7/2}(1+x)^{5/2} dx &= \frac{1}{7}(1-x)^{7/2}(1+x)^{7/2} + \int (1-x)^{5/2}(1+x)^{5/2} dx \\
 &= \frac{1}{6}(1-x)^{5/2}x(1+x)^{5/2} + \frac{1}{7}(1-x)^{7/2}(1+x)^{7/2} + \frac{5}{6} \int (1-x)^{3/2}(1+x)^{3/2} dx \\
 &= \frac{5}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{6}(1-x)^{5/2}x(1+x)^{5/2} + \frac{1}{7}(1-x)^{7/2}(1+x)^{7/2} + \frac{5}{8} \int \sqrt{1-x} \\
 &= \frac{5}{16}\sqrt{1-x}x\sqrt{1+x} + \frac{5}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{6}(1-x)^{5/2}x(1+x)^{5/2} + \frac{1}{7}(1-x)^{7/2}(1+x)^{7/2} \\
 &= \frac{5}{16}\sqrt{1-x}x\sqrt{1+x} + \frac{5}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{6}(1-x)^{5/2}x(1+x)^{5/2} + \frac{1}{7}(1-x)^{7/2}(1+x)^{7/2} \\
 &= \frac{5}{16}\sqrt{1-x}x\sqrt{1+x} + \frac{5}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{6}(1-x)^{5/2}x(1+x)^{5/2} + \frac{1}{7}(1-x)^{7/2}(1+x)^{7/2}
 \end{aligned}$$

Mathematica [A] time = 0.06, size = 66, normalized size = 0.73

$$\frac{1}{336}\sqrt{1-x^2}(-48x^6 + 56x^5 + 144x^4 - 182x^3 - 144x^2 + 231x + 48) - \frac{5}{8}\sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1-x)^(7/2)*(1+x)^(5/2),x]

[Out] (Sqrt[1-x^2]*(48+231*x-144*x^2-182*x^3+144*x^4+56*x^5-48*x^6))/336 - (5*ArcSin[Sqrt[1-x]/Sqrt[2]])/8

fricas [A] time = 0.44, size = 67, normalized size = 0.74

$$-\frac{1}{336}(48x^6 - 56x^5 - 144x^4 + 182x^3 + 144x^2 - 231x - 48)\sqrt{x+1}\sqrt{-x+1} - \frac{5}{8}\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)*(1+x)^(5/2),x, algorithm="fricas")

[Out] -1/336*(48*x^6 - 56*x^5 - 144*x^4 + 182*x^3 + 144*x^2 - 231*x - 48)*sqrt(x+1)*sqrt(-x+1) - 5/8*arctan((sqrt(x+1)*sqrt(-x+1)-1)/x)

giac [B] time = 1.14, size = 143, normalized size = 1.59

$$-\frac{1}{1680} ((2 ((4 (5 (6x - 37)(x + 1) + 661)(x + 1) - 4551)(x + 1) + 4781)(x + 1) - 6335)(x + 1) + 2835)\sqrt{x + 1} \sqrt{-x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)*(1+x)^(5/2),x, algorithm="giac")

[Out] -1/1680*((2*((4*(5*(6*x - 37)*(x + 1) + 661)*(x + 1) - 4551)*(x + 1) + 4781)*(x + 1) - 6335)*(x + 1) + 2835)*sqrt(x + 1)*sqrt(-x + 1) + 1/40*((2*(3*(4*x - 17)*(x + 1) + 133)*(x + 1) - 295)*(x + 1) + 195)*sqrt(x + 1)*sqrt(-x + 1) - 1/2*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + 5/8*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.00, size = 127, normalized size = 1.41

$$\frac{5\sqrt{(x+1)(-x+1)} \arcsin(x)}{16\sqrt{x+1} \sqrt{-x+1}} + \frac{(-x+1)^{\frac{7}{2}}(x+1)^{\frac{7}{2}}}{7} + \frac{(-x+1)^{\frac{5}{2}}(x+1)^{\frac{7}{2}}}{6} + \frac{(-x+1)^{\frac{3}{2}}(x+1)^{\frac{7}{2}}}{6} + \frac{\sqrt{-x+1}(x+1)^{\frac{7}{2}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(7/2)*(x+1)^(5/2),x)

[Out] 1/7*(-x+1)^(7/2)*(x+1)^(7/2)+1/6*(-x+1)^(5/2)*(x+1)^(7/2)+1/6*(-x+1)^(3/2)*(x+1)^(7/2)+1/8*(-x+1)^(1/2)*(x+1)^(7/2)-1/24*(-x+1)^(1/2)*(x+1)^(5/2)-5/48*(-x+1)^(1/2)*(x+1)^(3/2)-5/16*(-x+1)^(1/2)*(x+1)^(1/2)+5/16*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 3.01, size = 52, normalized size = 0.58

$$\frac{1}{7}(-x^2 + 1)^{\frac{7}{2}} + \frac{1}{6}(-x^2 + 1)^{\frac{5}{2}}x + \frac{5}{24}(-x^2 + 1)^{\frac{3}{2}}x + \frac{5}{16}\sqrt{-x^2 + 1}x + \frac{5}{16}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)*(1+x)^(5/2),x, algorithm="maxima")

[Out] 1/7*(-x^2 + 1)^(7/2) + 1/6*(-x^2 + 1)^(5/2)*x + 5/24*(-x^2 + 1)^(3/2)*x + 5/16*sqrt(-x^2 + 1)*x + 5/16*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{7/2} (x+1)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(7/2)*(x + 1)^(5/2), x)`

[Out] `int((1 - x)^(7/2)*(x + 1)^(5/2), x)`

sympy [A] time = 53.58, size = 321, normalized size = 3.57

$$\left\{ \begin{array}{l} -\frac{5i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{8} - \frac{i(x+1)^{\frac{15}{2}}}{7\sqrt{x-1}} + \frac{55i(x+1)^{\frac{13}{2}}}{42\sqrt{x-1}} - \frac{193i(x+1)^{\frac{11}{2}}}{42\sqrt{x-1}} + \frac{1237i(x+1)^{\frac{9}{2}}}{168\sqrt{x-1}} - \frac{769i(x+1)^{\frac{7}{2}}}{168\sqrt{x-1}} - \frac{i(x+1)^{\frac{5}{2}}}{48\sqrt{x-1}} - \frac{5i(x+1)^{\frac{3}{2}}}{48\sqrt{x-1}} + \frac{5i\sqrt{x+1}}{8\sqrt{x-1}} \\ \frac{5 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{8} + \frac{(x+1)^{\frac{15}{2}}}{7\sqrt{1-x}} - \frac{55(x+1)^{\frac{13}{2}}}{42\sqrt{1-x}} + \frac{193(x+1)^{\frac{11}{2}}}{42\sqrt{1-x}} - \frac{1237(x+1)^{\frac{9}{2}}}{168\sqrt{1-x}} + \frac{769(x+1)^{\frac{7}{2}}}{168\sqrt{1-x}} + \frac{(x+1)^{\frac{5}{2}}}{48\sqrt{1-x}} + \frac{5(x+1)^{\frac{3}{2}}}{48\sqrt{1-x}} - \frac{5\sqrt{x+1}}{8\sqrt{1-x}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(7/2)*(1+x)**(5/2), x)`

[Out] `Piecewise((-5*I*acosh(sqrt(2)*sqrt(x + 1)/2)/8 - I*(x + 1)**(15/2)/(7*sqrt(x - 1)) + 55*I*(x + 1)**(13/2)/(42*sqrt(x - 1)) - 193*I*(x + 1)**(11/2)/(42*sqrt(x - 1)) + 1237*I*(x + 1)**(9/2)/(168*sqrt(x - 1)) - 769*I*(x + 1)**(7/2)/(168*sqrt(x - 1)) - I*(x + 1)**(5/2)/(48*sqrt(x - 1)) - 5*I*(x + 1)**(3/2)/(48*sqrt(x - 1)) + 5*I*sqrt(x + 1)/(8*sqrt(x - 1)), Abs(x + 1)/2 > 1), (5*asin(sqrt(2)*sqrt(x + 1)/2)/8 + (x + 1)**(15/2)/(7*sqrt(1 - x)) - 55*(x + 1)**(13/2)/(42*sqrt(1 - x)) + 193*(x + 1)**(11/2)/(42*sqrt(1 - x)) - 1237*(x + 1)**(9/2)/(168*sqrt(1 - x)) + 769*(x + 1)**(7/2)/(168*sqrt(1 - x)) + (x + 1)**(5/2)/(48*sqrt(1 - x)) + 5*(x + 1)**(3/2)/(48*sqrt(1 - x)) - 5*sqrt(x + 1)/(8*sqrt(1 - x)), True))`

3.1091 $\int (1-x)^{5/2}(1+x)^{5/2} dx$

Optimal. Leaf size=70

$$\frac{1}{6}(1-x)^{5/2}x(x+1)^{5/2} + \frac{5}{24}(1-x)^{3/2}x(x+1)^{3/2} + \frac{5}{16}\sqrt{1-x}x\sqrt{x+1} + \frac{5}{16}\sin^{-1}(x)$$

[Out] $5/24*(1-x)^{(3/2)}*x*(1+x)^{(3/2)}+1/6*(1-x)^{(5/2)}*x*(1+x)^{(5/2)}+5/16*\arcsin(x)$
 $+5/16*x*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 70, normalized size of antiderivative = 1.00,
 number of steps used = 5, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} =$
 0.176, Rules used = {38, 41, 216}

$$\frac{1}{6}(1-x)^{5/2}x(x+1)^{5/2} + \frac{5}{24}(1-x)^{3/2}x(x+1)^{3/2} + \frac{5}{16}\sqrt{1-x}x\sqrt{x+1} + \frac{5}{16}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(5/2)*(1 + x)^(5/2), x]

[Out] $(5*\text{Sqrt}[1 - x]*x*\text{Sqrt}[1 + x])/16 + (5*(1 - x)^{(3/2)}*x*(1 + x)^{(3/2)})/24 + ($
 $(1 - x)^{(5/2)}*x*(1 + x)^{(5/2)})/6 + (5*\text{ArcSin}[x])/16$

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> Simp[(x
 *(a + b*x)^m*(c + d*x)^m)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a
 + b*x)^(m - 1)*(c + d*x)^(m - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b
 *c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] :> Int[(
 a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (
 IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqr
 t[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int (1-x)^{5/2}(1+x)^{5/2} dx &= \frac{1}{6}(1-x)^{5/2}x(1+x)^{5/2} + \frac{5}{6} \int (1-x)^{3/2}(1+x)^{3/2} dx \\
&= \frac{5}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{6}(1-x)^{5/2}x(1+x)^{5/2} + \frac{5}{8} \int \sqrt{1-x} \sqrt{1+x} dx \\
&= \frac{5}{16} \sqrt{1-x} x \sqrt{1+x} + \frac{5}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{6}(1-x)^{5/2}x(1+x)^{5/2} + \frac{5}{16} \int \frac{1}{\sqrt{1-x}} dx \\
&= \frac{5}{16} \sqrt{1-x} x \sqrt{1+x} + \frac{5}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{6}(1-x)^{5/2}x(1+x)^{5/2} + \frac{5}{16} \int \frac{1}{\sqrt{1-x}} dx \\
&= \frac{5}{16} \sqrt{1-x} x \sqrt{1+x} + \frac{5}{24}(1-x)^{3/2}x(1+x)^{3/2} + \frac{1}{6}(1-x)^{5/2}x(1+x)^{5/2} + \frac{5}{16} \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 34, normalized size = 0.49

$$\frac{1}{48} \left(x \sqrt{1-x^2} (8x^4 - 26x^2 + 33) + 15 \sin^{-1}(x) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(5/2)*(1 + x)^(5/2), x]

[Out] (x*sqrt[1 - x^2]*(33 - 26*x^2 + 8*x^4) + 15*ArcSin[x])/48

fricas [A] time = 0.44, size = 51, normalized size = 0.73

$$\frac{1}{48} (8x^5 - 26x^3 + 33x) \sqrt{x+1} \sqrt{-x+1} - \frac{5}{8} \arctan\left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)*(1+x)^(5/2), x, algorithm="fricas")

[Out] 1/48*(8*x^5 - 26*x^3 + 33*x)*sqrt(x + 1)*sqrt(-x + 1) - 5/8*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [B] time = 1.31, size = 185, normalized size = 2.64

$$\frac{1}{240} ((2((4(5x-26)(x+1)+321)(x+1)-451)(x+1)+745)(x+1)-405)\sqrt{x+1}\sqrt{-x+1} + \frac{1}{120} ((2(3(4x-$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)*(1+x)^(5/2), x, algorithm="giac")

[Out] $\frac{1}{240} * ((2 * ((4 * (5 * x - 26) * (x + 1) + 321) * (x + 1) - 451) * (x + 1) + 745) * (x + 1) - 405) * \sqrt{x + 1} * \sqrt{-x + 1} + \frac{1}{120} * ((2 * (3 * (4 * x - 17) * (x + 1) + 133) * (x + 1) - 295) * (x + 1) + 195) * \sqrt{x + 1} * \sqrt{-x + 1} - \frac{1}{12} * ((2 * (3 * x - 10) * (x + 1) + 43) * (x + 1) - 39) * \sqrt{x + 1} * \sqrt{-x + 1} - \frac{1}{3} * ((2 * x - 5) * (x + 1) + 9) * \sqrt{x + 1} * \sqrt{-x + 1} + \frac{1}{2} * \sqrt{x + 1} * (x - 2) * \sqrt{-x + 1} + \sqrt{x + 1} * \sqrt{-x + 1} + \frac{5}{8} * \arcsin(\frac{1}{2} * \sqrt{2} * \sqrt{x + 1})$

maple [B] time = 0.00, size = 113, normalized size = 1.61

$$\frac{5\sqrt{(x+1)(-x+1)} \arcsin(x)}{16\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{5}{2}}(x+1)^{\frac{7}{2}}}{6} + \frac{(-x+1)^{\frac{3}{2}}(x+1)^{\frac{7}{2}}}{6} + \frac{\sqrt{-x+1}(x+1)^{\frac{7}{2}}}{8} - \frac{\sqrt{-x+1}(x+1)^{\frac{5}{2}}}{24}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((-x+1)^{(5/2)} * (x+1)^{(5/2)}, x)$

[Out] $\frac{1}{6} * (-x+1)^{(5/2)} * (x+1)^{(7/2)} + \frac{1}{6} * (-x+1)^{(3/2)} * (x+1)^{(7/2)} + \frac{1}{8} * (-x+1)^{(1/2)} * (x+1)^{(7/2)} - \frac{1}{24} * (-x+1)^{(1/2)} * (x+1)^{(5/2)} - \frac{5}{48} * (-x+1)^{(1/2)} * (x+1)^{(3/2)} - \frac{5}{16} * (-x+1)^{(1/2)} * (x+1)^{(1/2)} + \frac{5}{16} * ((x+1) * (-x+1))^{(1/2)} / (x+1)^{(1/2)} / (-x+1)^{(1/2)} * \arcsin(x)$

maxima [A] time = 3.10, size = 41, normalized size = 0.59

$$\frac{1}{6} (-x^2 + 1)^{\frac{5}{2}} x + \frac{5}{24} (-x^2 + 1)^{\frac{3}{2}} x + \frac{5}{16} \sqrt{-x^2 + 1} x + \frac{5}{16} \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((1-x)^{(5/2)} * (1+x)^{(5/2)}, x, \text{algorithm}="maxima")$

[Out] $\frac{1}{6} * (-x^2 + 1)^{(5/2)} * x + \frac{5}{24} * (-x^2 + 1)^{(3/2)} * x + \frac{5}{16} * \sqrt{-x^2 + 1} * x + \frac{5}{16} * \arcsin(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{5/2} (x+1)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((1-x)^{(5/2)} * (x+1)^{(5/2)}, x)$

[Out] $\text{int}((1-x)^{(5/2)} * (x+1)^{(5/2)}, x)$

sympy [B] time = 25.76, size = 286, normalized size = 4.09

$$\left\{ \begin{array}{l} -\frac{5i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{8} + \frac{i(x+1)^{\frac{13}{2}}}{6\sqrt{x-1}} - \frac{7i(x+1)^{\frac{11}{2}}}{6\sqrt{x-1}} + \frac{67i(x+1)^{\frac{9}{2}}}{24\sqrt{x-1}} - \frac{55i(x+1)^{\frac{7}{2}}}{24\sqrt{x-1}} - \frac{i(x+1)^{\frac{5}{2}}}{48\sqrt{x-1}} - \frac{5i(x+1)^{\frac{3}{2}}}{48\sqrt{x-1}} + \frac{5i\sqrt{x+1}}{8\sqrt{x-1}} \\ \frac{5 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{8} - \frac{(x+1)^{\frac{13}{2}}}{6\sqrt{1-x}} + \frac{7(x+1)^{\frac{11}{2}}}{6\sqrt{1-x}} - \frac{67(x+1)^{\frac{9}{2}}}{24\sqrt{1-x}} + \frac{55(x+1)^{\frac{7}{2}}}{24\sqrt{1-x}} + \frac{(x+1)^{\frac{5}{2}}}{48\sqrt{1-x}} + \frac{5(x+1)^{\frac{3}{2}}}{48\sqrt{1-x}} - \frac{5\sqrt{x+1}}{8\sqrt{1-x}} \end{array} \right. \begin{array}{l} \text{for } \frac{|x+1|}{2} > 1 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(5/2)*(1+x)**(5/2), x)

[Out] Piecewise((-5*I*acosh(sqrt(2)*sqrt(x + 1)/2)/8 + I*(x + 1)**(13/2)/(6*sqrt(x - 1)) - 7*I*(x + 1)**(11/2)/(6*sqrt(x - 1)) + 67*I*(x + 1)**(9/2)/(24*sqrt(x - 1)) - 55*I*(x + 1)**(7/2)/(24*sqrt(x - 1)) - I*(x + 1)**(5/2)/(48*sqrt(x - 1)) - 5*I*(x + 1)**(3/2)/(48*sqrt(x - 1)) + 5*I*sqrt(x + 1)/(8*sqrt(x - 1)), Abs(x + 1)/2 > 1), (5*asin(sqrt(2)*sqrt(x + 1)/2)/8 - (x + 1)**(13/2)/(6*sqrt(1 - x)) + 7*(x + 1)**(11/2)/(6*sqrt(1 - x)) - 67*(x + 1)**(9/2)/(24*sqrt(1 - x)) + 55*(x + 1)**(7/2)/(24*sqrt(1 - x)) + (x + 1)**(5/2)/(48*sqrt(1 - x)) + 5*(x + 1)**(3/2)/(48*sqrt(1 - x)) - 5*sqrt(x + 1)/(8*sqrt(1 - x)), True))

3.1092 $\int (1-x)^{3/2}(1+x)^{5/2} dx$

Optimal. Leaf size=69

$$-\frac{1}{5}(1-x)^{5/2}(x+1)^{5/2} + \frac{1}{4}(1-x)^{3/2}x(x+1)^{3/2} + \frac{3}{8}\sqrt{1-x}x\sqrt{x+1} + \frac{3}{8}\sin^{-1}(x)$$

[Out] 1/4*(1-x)^(3/2)*x*(1+x)^(3/2)-1/5*(1-x)^(5/2)*(1+x)^(5/2)+3/8*arcsin(x)+3/8*x*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$-\frac{1}{5}(1-x)^{5/2}(x+1)^{5/2} + \frac{1}{4}(1-x)^{3/2}x(x+1)^{3/2} + \frac{3}{8}\sqrt{1-x}x\sqrt{x+1} + \frac{3}{8}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(3/2)*(1 + x)^(5/2), x]

[Out] (3*Sqrt[1 - x]*x*Sqrt[1 + x])/8 + ((1 - x)^(3/2)*x*(1 + x)^(3/2))/4 - ((1 - x)^(5/2)*(1 + x)^(5/2))/5 + (3*ArcSin[x])/8

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> Simp[(x*(a + b*x)^m*(c + d*x)^m)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(m - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(2*c*n)/(m + n + 1), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :-> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
 \int (1-x)^{3/2}(1+x)^{5/2} dx &= -\frac{1}{5}(1-x)^{5/2}(1+x)^{5/2} + \int (1-x)^{3/2}(1+x)^{3/2} dx \\
 &= \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} - \frac{1}{5}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{4} \int \sqrt{1-x} \sqrt{1+x} dx \\
 &= \frac{3}{8}\sqrt{1-x}x\sqrt{1+x} + \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} - \frac{1}{5}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{8} \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
 &= \frac{3}{8}\sqrt{1-x}x\sqrt{1+x} + \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} - \frac{1}{5}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{8} \int \frac{1}{\sqrt{1-x^2}} dx \\
 &= \frac{3}{8}\sqrt{1-x}x\sqrt{1+x} + \frac{1}{4}(1-x)^{3/2}x(1+x)^{3/2} - \frac{1}{5}(1-x)^{5/2}(1+x)^{5/2} + \frac{3}{8} \sin^{-1}(x)
 \end{aligned}$$

Mathematica [A] time = 0.04, size = 55, normalized size = 0.80

$$\frac{1}{40} \left(\sqrt{1-x^2} (-8x^4 - 10x^3 + 16x^2 + 25x - 8) - 30 \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(3/2)*(1 + x)^(5/2), x]

[Out] (Sqrt[1 - x^2]*(-8 + 25*x + 16*x^2 - 10*x^3 - 8*x^4) - 30*ArcSin[Sqrt[1 - x]/Sqrt[2]])/40

fricas [A] time = 0.44, size = 57, normalized size = 0.83

$$-\frac{1}{40} (8x^4 + 10x^3 - 16x^2 - 25x + 8) \sqrt{x+1} \sqrt{-x+1} - \frac{3}{4} \arctan \left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)*(1+x)^(5/2), x, algorithm="fricas")

[Out] -1/40*(8*x^4 + 10*x^3 - 16*x^2 - 25*x + 8)*sqrt(x + 1)*sqrt(-x + 1) - 3/4*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [B] time = 1.18, size = 114, normalized size = 1.65

$$-\frac{1}{120} ((2(3(4x-17)(x+1)+133)(x+1)-295)(x+1)+195)\sqrt{x+1}\sqrt{-x+1} - \frac{1}{12} ((2(3x-10)(x+1)+43)(x+1)+195)\sqrt{x+1}\sqrt{-x+1} - \frac{3}{8} \arctan \left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)*(1+x)^(5/2),x, algorithm="giac")

[Out] -1/120*((2*(3*(4*x - 17)*(x + 1) + 133)*(x + 1) - 295)*(x + 1) + 195)*sqrt(x + 1)*sqrt(-x + 1) - 1/12*((2*(3*x - 10)*(x + 1) + 43)*(x + 1) - 39)*sqrt(x + 1)*sqrt(-x + 1) + sqrt(x + 1)*(x - 2)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + 3/4*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.00, size = 99, normalized size = 1.43

$$\frac{3\sqrt{(x+1)(-x+1)} \arcsin(x)}{8\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{3}{2}}(x+1)^{\frac{7}{2}}}{5} + \frac{3\sqrt{-x+1}(x+1)^{\frac{7}{2}}}{20} - \frac{\sqrt{-x+1}(x+1)^{\frac{5}{2}}}{20} - \frac{\sqrt{-x+1}(x+1)^{\frac{3}{2}}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(3/2)*(x+1)^(5/2),x)

[Out] 1/5*(-x+1)^(3/2)*(x+1)^(7/2)+3/20*(-x+1)^(1/2)*(x+1)^(7/2)-1/20*(-x+1)^(1/2)*(x+1)^(5/2)-1/8*(-x+1)^(1/2)*(x+1)^(3/2)-3/8*(-x+1)^(1/2)*(x+1)^(1/2)+3/8*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 3.05, size = 40, normalized size = 0.58

$$-\frac{1}{5}(-x^2+1)^{\frac{5}{2}} + \frac{1}{4}(-x^2+1)^{\frac{3}{2}}x + \frac{3}{8}\sqrt{-x^2+1}x + \frac{3}{8}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)*(1+x)^(5/2),x, algorithm="maxima")

[Out] -1/5*(-x^2 + 1)^(5/2) + 1/4*(-x^2 + 1)^(3/2)*x + 3/8*sqrt(-x^2 + 1)*x + 3/8*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (1-x)^{3/2}(x+1)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(3/2)*(x + 1)^(5/2),x)

[Out] int((1 - x)^(3/2)*(x + 1)^(5/2), x)

sympy [B] time = 16.53, size = 246, normalized size = 3.57

$$\left\{ \begin{array}{ll} \frac{3i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} - \frac{i(x+1)^{\frac{11}{2}}}{5\sqrt{x-1}} + \frac{19i(x+1)^{\frac{9}{2}}}{20\sqrt{x-1}} - \frac{23i(x+1)^{\frac{7}{2}}}{20\sqrt{x-1}} - \frac{i(x+1)^{\frac{5}{2}}}{40\sqrt{x-1}} - \frac{i(x+1)^{\frac{3}{2}}}{8\sqrt{x-1}} + \frac{3i\sqrt{x+1}}{4\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ \frac{3 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} + \frac{(x+1)^{\frac{11}{2}}}{5\sqrt{1-x}} - \frac{19(x+1)^{\frac{9}{2}}}{20\sqrt{1-x}} + \frac{23(x+1)^{\frac{7}{2}}}{20\sqrt{1-x}} + \frac{(x+1)^{\frac{5}{2}}}{40\sqrt{1-x}} + \frac{(x+1)^{\frac{3}{2}}}{8\sqrt{1-x}} - \frac{3\sqrt{x+1}}{4\sqrt{1-x}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(3/2)*(1+x)**(5/2), x)

[Out] Piecewise((-3*I*acosh(sqrt(2)*sqrt(x + 1)/2)/4 - I*(x + 1)**(11/2)/(5*sqrt(x - 1)) + 19*I*(x + 1)**(9/2)/(20*sqrt(x - 1)) - 23*I*(x + 1)**(7/2)/(20*sqrt(x - 1)) - I*(x + 1)**(5/2)/(40*sqrt(x - 1)) - I*(x + 1)**(3/2)/(8*sqrt(x - 1)) + 3*I*sqrt(x + 1)/(4*sqrt(x - 1)), Abs(x + 1)/2 > 1), (3*asin(sqrt(2)*sqrt(x + 1)/2)/4 + (x + 1)**(11/2)/(5*sqrt(1 - x)) - 19*(x + 1)**(9/2)/(20*sqrt(1 - x)) + 23*(x + 1)**(7/2)/(20*sqrt(1 - x)) + (x + 1)**(5/2)/(40*sqrt(1 - x)) + (x + 1)**(3/2)/(8*sqrt(1 - x)) - 3*sqrt(x + 1)/(4*sqrt(1 - x)), True))

3.1093 $\int \sqrt{1-x} (1+x)^{5/2} dx$

Optimal. Leaf size=68

$$-\frac{1}{4}(1-x)^{3/2}(x+1)^{5/2} - \frac{5}{12}(1-x)^{3/2}(x+1)^{3/2} + \frac{5}{8}\sqrt{1-x}x\sqrt{x+1} + \frac{5}{8}\sin^{-1}(x)$$

[Out] -5/12*(1-x)^(3/2)*(1+x)^(3/2)-1/4*(1-x)^(3/2)*(1+x)^(5/2)+5/8*arcsin(x)+5/8*x*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {49, 38, 41, 216}

$$-\frac{1}{4}(1-x)^{3/2}(x+1)^{5/2} - \frac{5}{12}(1-x)^{3/2}(x+1)^{3/2} + \frac{5}{8}\sqrt{1-x}x\sqrt{x+1} + \frac{5}{8}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 - x]*(1 + x)^(5/2), x]

[Out] (5*Sqrt[1 - x]*x*Sqrt[1 + x])/8 - (5*(1 - x)^(3/2)*(1 + x)^(3/2))/12 - ((1 - x)^(3/2)*(1 + x)^(5/2))/4 + (5*ArcSin[x])/8

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(x*(a + b*x)^(m+1)*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m-1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] := Int[(a*c + b*d*x^2)^(m), x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 49

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m+1)*(c + d*x)^n/(b*(m+n+1)), x] + Dist[(2*c*n)/(m+n+1), Int[(a + b*x)^(m+1)*(c + d*x)^(n-1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0] && IGtQ[n + 1/2, 0] && LtQ[m, n]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
 \int \sqrt{1-x}(1+x)^{5/2} dx &= -\frac{1}{4}(1-x)^{3/2}(1+x)^{5/2} + \frac{5}{4} \int \sqrt{1-x}(1+x)^{3/2} dx \\
 &= -\frac{5}{12}(1-x)^{3/2}(1+x)^{3/2} - \frac{1}{4}(1-x)^{3/2}(1+x)^{5/2} + \frac{5}{4} \int \sqrt{1-x}\sqrt{1+x} dx \\
 &= \frac{5}{8}\sqrt{1-x}x\sqrt{1+x} - \frac{5}{12}(1-x)^{3/2}(1+x)^{3/2} - \frac{1}{4}(1-x)^{3/2}(1+x)^{5/2} + \frac{5}{8} \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
 &= \frac{5}{8}\sqrt{1-x}x\sqrt{1+x} - \frac{5}{12}(1-x)^{3/2}(1+x)^{3/2} - \frac{1}{4}(1-x)^{3/2}(1+x)^{5/2} + \frac{5}{8} \int \frac{1}{\sqrt{1-x^2}} dx \\
 &= \frac{5}{8}\sqrt{1-x}x\sqrt{1+x} - \frac{5}{12}(1-x)^{3/2}(1+x)^{3/2} - \frac{1}{4}(1-x)^{3/2}(1+x)^{5/2} + \frac{5}{8} \sin^{-1}(x)
 \end{aligned}$$

Mathematica [A] time = 0.04, size = 50, normalized size = 0.74

$$\frac{1}{24} \left(\sqrt{1-x^2} (6x^3 + 16x^2 + 9x - 16) - 30 \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 - x]*(1 + x)^(5/2), x]

[Out] (Sqrt[1 - x^2]*(-16 + 9*x + 16*x^2 + 6*x^3) - 30*ArcSin[Sqrt[1 - x]/Sqrt[2]])/24

fricas [A] time = 0.42, size = 52, normalized size = 0.76

$$\frac{1}{24} (6x^3 + 16x^2 + 9x - 16) \sqrt{x+1} \sqrt{-x+1} - \frac{5}{4} \arctan \left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)*(1+x)^(5/2), x, algorithm="fricas")

[Out] 1/24*(6*x^3 + 16*x^2 + 9*x - 16)*sqrt(x + 1)*sqrt(-x + 1) - 5/4*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [B] time = 1.05, size = 101, normalized size = 1.49

$$\frac{1}{24} ((2(3x - 10)(x + 1) + 43)(x + 1) - 39) \sqrt{x+1} \sqrt{-x+1} + \frac{1}{2} ((2x - 5)(x + 1) + 9) \sqrt{x+1} \sqrt{-x+1} + \frac{3}{2} \sqrt{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)*(1+x)^(5/2),x, algorithm="giac")

[Out] 1/24*((2*(3*x - 10)*(x + 1) + 43)*(x + 1) - 39)*sqrt(x + 1)*sqrt(-x + 1) + 1/2*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) + 3/2*sqrt(x + 1)*(x - 2)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + 5/4*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.00, size = 85, normalized size = 1.25

$$\frac{5\sqrt{(x+1)(-x+1)} \arcsin(x)}{8\sqrt{x+1}\sqrt{-x+1}} + \frac{\sqrt{-x+1}(x+1)^{\frac{7}{2}}}{4} - \frac{\sqrt{-x+1}(x+1)^{\frac{5}{2}}}{12} - \frac{5\sqrt{-x+1}(x+1)^{\frac{3}{2}}}{24} - \frac{5\sqrt{-x+1}\sqrt{x+1}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(1/2)*(x+1)^(5/2),x)

[Out] 1/4*(-x+1)^(1/2)*(x+1)^(7/2)-1/12*(-x+1)^(1/2)*(x+1)^(5/2)-5/24*(-x+1)^(1/2)*(x+1)^(3/2)-5/8*(-x+1)^(1/2)*(x+1)^(1/2)+5/8*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 3.06, size = 40, normalized size = 0.59

$$-\frac{1}{4}(-x^2+1)^{\frac{3}{2}}x - \frac{2}{3}(-x^2+1)^{\frac{3}{2}} + \frac{5}{8}\sqrt{-x^2+1}x + \frac{5}{8}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)*(1+x)^(5/2),x, algorithm="maxima")

[Out] -1/4*(-x^2 + 1)^(3/2)*x - 2/3*(-x^2 + 1)^(3/2) + 5/8*sqrt(-x^2 + 1)*x + 5/8*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{1-x}(x+1)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(1/2)*(x + 1)^(5/2),x)

[Out] int((1 - x)^(1/2)*(x + 1)^(5/2), x)

sympy [A] time = 9.89, size = 214, normalized size = 3.15

$$\left\{ \begin{array}{ll} -\frac{5i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} + \frac{i(x+1)^{\frac{9}{2}}}{4\sqrt{x-1}} - \frac{7i(x+1)^{\frac{7}{2}}}{12\sqrt{x-1}} - \frac{i(x+1)^{\frac{5}{2}}}{24\sqrt{x-1}} - \frac{5i(x+1)^{\frac{3}{2}}}{24\sqrt{x-1}} + \frac{5i\sqrt{x+1}}{4\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ \frac{5 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} - \frac{(x+1)^{\frac{9}{2}}}{4\sqrt{1-x}} + \frac{7(x+1)^{\frac{7}{2}}}{12\sqrt{1-x}} + \frac{(x+1)^{\frac{5}{2}}}{24\sqrt{1-x}} + \frac{5(x+1)^{\frac{3}{2}}}{24\sqrt{1-x}} - \frac{5\sqrt{x+1}}{4\sqrt{1-x}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(1/2)*(1+x)**(5/2), x)

[Out] Piecewise((-5*I*acosh(sqrt(2)*sqrt(x + 1)/2)/4 + I*(x + 1)**(9/2)/(4*sqrt(x - 1)) - 7*I*(x + 1)**(7/2)/(12*sqrt(x - 1)) - I*(x + 1)**(5/2)/(24*sqrt(x - 1)) - 5*I*(x + 1)**(3/2)/(24*sqrt(x - 1)) + 5*I*sqrt(x + 1)/(4*sqrt(x - 1)), Abs(x + 1)/2 > 1), (5*asin(sqrt(2)*sqrt(x + 1)/2)/4 - (x + 1)**(9/2)/(4*sqrt(1 - x)) + 7*(x + 1)**(7/2)/(12*sqrt(1 - x)) + (x + 1)**(5/2)/(24*sqrt(1 - x)) + 5*(x + 1)**(3/2)/(24*sqrt(1 - x)) - 5*sqrt(x + 1)/(4*sqrt(1 - x)), True))

3.1094

$$\int \frac{(1+x)^{5/2}}{\sqrt{1-x}} dx$$

Optimal. Leaf size=67

$$-\frac{1}{3}\sqrt{1-x}(x+1)^{5/2} - \frac{5}{6}\sqrt{1-x}(x+1)^{3/2} - \frac{5}{2}\sqrt{1-x}\sqrt{x+1} + \frac{5}{2}\sin^{-1}(x)$$

[Out] 5/2*arcsin(x)-5/6*(1-x)^(1/2)*(1+x)^(3/2)-1/3*(1-x)^(1/2)*(1+x)^(5/2)-5/2*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {50, 41, 216}

$$-\frac{1}{3}\sqrt{1-x}(x+1)^{5/2} - \frac{5}{6}\sqrt{1-x}(x+1)^{3/2} - \frac{5}{2}\sqrt{1-x}\sqrt{x+1} + \frac{5}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(5/2)/Sqrt[1 - x], x]

[Out] (-5*Sqrt[1 - x]*Sqrt[1 + x])/2 - (5*Sqrt[1 - x]*(1 + x)^(3/2))/6 - (Sqrt[1 - x]*(1 + x)^(5/2))/3 + (5*ArcSin[x])/2

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(1+x)^{5/2}}{\sqrt{1-x}} dx &= -\frac{1}{3}\sqrt{1-x}(1+x)^{5/2} + \frac{5}{3} \int \frac{(1+x)^{3/2}}{\sqrt{1-x}} dx \\
&= -\frac{5}{6}\sqrt{1-x}(1+x)^{3/2} - \frac{1}{3}\sqrt{1-x}(1+x)^{5/2} + \frac{5}{2} \int \frac{\sqrt{1+x}}{\sqrt{1-x}} dx \\
&= -\frac{5}{2}\sqrt{1-x}\sqrt{1+x} - \frac{5}{6}\sqrt{1-x}(1+x)^{3/2} - \frac{1}{3}\sqrt{1-x}(1+x)^{5/2} + \frac{5}{2} \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
&= -\frac{5}{2}\sqrt{1-x}\sqrt{1+x} - \frac{5}{6}\sqrt{1-x}(1+x)^{3/2} - \frac{1}{3}\sqrt{1-x}(1+x)^{5/2} + \frac{5}{2} \int \frac{1}{\sqrt{1-x^2}} dx \\
&= -\frac{5}{2}\sqrt{1-x}\sqrt{1+x} - \frac{5}{6}\sqrt{1-x}(1+x)^{3/2} - \frac{1}{3}\sqrt{1-x}(1+x)^{5/2} + \frac{5}{2} \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.02, size = 44, normalized size = 0.66

$$-\frac{1}{6}\sqrt{1-x^2}(2x^2+9x+22) - 5\sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1+x)^(5/2)/Sqrt[1-x],x]

[Out] -1/6*(Sqrt[1-x^2]*(22+9*x+2*x^2))-5*ArcSin[Sqrt[1-x]/Sqrt[2]]

fricas [A] time = 0.42, size = 47, normalized size = 0.70

$$-\frac{1}{6}(2x^2+9x+22)\sqrt{x+1}\sqrt{-x+1} - 5 \arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(1/2),x, algorithm="fricas")

[Out] -1/6*(2*x^2+9*x+22)*sqrt(x+1)*sqrt(-x+1)-5*arctan((sqrt(x+1)*sqrt(-x+1)-1)/x)

giac [A] time = 1.05, size = 39, normalized size = 0.58

$$-\frac{1}{6}((2x+7)(x+1)+15)\sqrt{x+1}\sqrt{-x+1} + 5 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(1/2),x, algorithm="giac")

[Out] $-1/6*((2*x + 7)*(x + 1) + 15)*\sqrt{x + 1}*\sqrt{-x + 1} + 5*\arcsin(1/2*\sqrt{(2)*\sqrt{x + 1}})$

maple [A] time = 0.00, size = 71, normalized size = 1.06

$$\frac{5\sqrt{(x+1)(-x+1)} \arcsin(x)}{2\sqrt{x+1}\sqrt{-x+1}} - \frac{\sqrt{-x+1}(x+1)^{\frac{5}{2}}}{3} - \frac{5\sqrt{-x+1}(x+1)^{\frac{3}{2}}}{6} - \frac{5\sqrt{-x+1}\sqrt{x+1}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(5/2)/(-x+1)^(1/2),x)

[Out] $-1/3*(-x+1)^{(1/2)}*(x+1)^{(5/2)}-5/6*(-x+1)^{(1/2)}*(x+1)^{(3/2)}-5/2*(-x+1)^{(1/2)}*(x+1)^{(1/2)}+5/2*((x+1)*(-x+1))^{(1/2)}/(x+1)^{(1/2)}/(-x+1)^{(1/2)}*\arcsin(x)$

maxima [A] time = 2.93, size = 42, normalized size = 0.63

$$-\frac{1}{3}\sqrt{-x^2+1}x^2 - \frac{3}{2}\sqrt{-x^2+1}x - \frac{11}{3}\sqrt{-x^2+1} + \frac{5}{2}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(1/2),x, algorithm="maxima")

[Out] $-1/3*\sqrt{-x^2+1}*x^2 - 3/2*\sqrt{-x^2+1}*x - 11/3*\sqrt{-x^2+1} + 5/2*\arcsin(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(x+1)^{5/2}}{\sqrt{1-x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(5/2)/(1 - x)^(1/2),x)

[Out] int((x + 1)^(5/2)/(1 - x)^(1/2), x)

sympy [A] time = 7.50, size = 172, normalized size = 2.57

$$\begin{cases} -5i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{i(x+1)^{\frac{7}{2}}}{3\sqrt{x-1}} - \frac{i(x+1)^{\frac{5}{2}}}{6\sqrt{x-1}} - \frac{5i(x+1)^{\frac{3}{2}}}{6\sqrt{x-1}} + \frac{5i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ 5 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{(x+1)^{\frac{7}{2}}}{3\sqrt{1-x}} + \frac{(x+1)^{\frac{5}{2}}}{6\sqrt{1-x}} + \frac{5(x+1)^{\frac{3}{2}}}{6\sqrt{1-x}} - \frac{5\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((1+x)**(5/2)/(1-x)**(1/2),x)
```

```
[Out] Piecewise((-5*I*acosh(sqrt(2)*sqrt(x + 1)/2) - I*(x + 1)**(7/2)/(3*sqrt(x - 1)) - I*(x + 1)**(5/2)/(6*sqrt(x - 1)) - 5*I*(x + 1)**(3/2)/(6*sqrt(x - 1)) + 5*I*sqrt(x + 1)/sqrt(x - 1), Abs(x + 1)/2 > 1), (5*asin(sqrt(2)*sqrt(x + 1)/2) + (x + 1)**(7/2)/(3*sqrt(1 - x)) + (x + 1)**(5/2)/(6*sqrt(1 - x)) + 5*(x + 1)**(3/2)/(6*sqrt(1 - x)) - 5*sqrt(x + 1)/sqrt(1 - x), True))
```

3.1095

$$\int \frac{(1+x)^{5/2}}{(1-x)^{3/2}} dx$$

Optimal. Leaf size=65

$$\frac{2(x+1)^{5/2}}{\sqrt{1-x}} + \frac{5}{2}\sqrt{1-x}(x+1)^{3/2} + \frac{15}{2}\sqrt{1-x}\sqrt{x+1} - \frac{15}{2}\sin^{-1}(x)$$

[Out] $-15/2*\arcsin(x)+2*(1+x)^{(5/2)/(1-x)^{(1/2)}+5/2*(1-x)^{(1/2)}*(1+x)^{(3/2)}+15/2*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 41, 216}

$$\frac{2(x+1)^{5/2}}{\sqrt{1-x}} + \frac{5}{2}\sqrt{1-x}(x+1)^{3/2} + \frac{15}{2}\sqrt{1-x}\sqrt{x+1} - \frac{15}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(5/2)/(1 - x)^(3/2), x]

[Out] $(15*\text{Sqrt}[1 - x]*\text{Sqrt}[1 + x])/2 + (5*\text{Sqrt}[1 - x]*(1 + x)^{(3/2)})/2 + (2*(1 + x)^{(5/2)})/\text{Sqrt}[1 - x] - (15*\text{ArcSin}[x])/2$

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ

`[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0])) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int \frac{(1+x)^{5/2}}{(1-x)^{3/2}} dx &= \frac{2(1+x)^{5/2}}{\sqrt{1-x}} - 5 \int \frac{(1+x)^{3/2}}{\sqrt{1-x}} dx \\
 &= \frac{5}{2} \sqrt{1-x} (1+x)^{3/2} + \frac{2(1+x)^{5/2}}{\sqrt{1-x}} - \frac{15}{2} \int \frac{\sqrt{1+x}}{\sqrt{1-x}} dx \\
 &= \frac{15}{2} \sqrt{1-x} \sqrt{1+x} + \frac{5}{2} \sqrt{1-x} (1+x)^{3/2} + \frac{2(1+x)^{5/2}}{\sqrt{1-x}} - \frac{15}{2} \int \frac{1}{\sqrt{1-x} \sqrt{1+x}} dx \\
 &= \frac{15}{2} \sqrt{1-x} \sqrt{1+x} + \frac{5}{2} \sqrt{1-x} (1+x)^{3/2} + \frac{2(1+x)^{5/2}}{\sqrt{1-x}} - \frac{15}{2} \int \frac{1}{\sqrt{1-x^2}} dx \\
 &= \frac{15}{2} \sqrt{1-x} \sqrt{1+x} + \frac{5}{2} \sqrt{1-x} (1+x)^{3/2} + \frac{2(1+x)^{5/2}}{\sqrt{1-x}} - \frac{15}{2} \sin^{-1}(x)
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 35, normalized size = 0.54

$$\frac{8\sqrt{2} {}_2F_1\left(-\frac{5}{2}, -\frac{1}{2}; \frac{1}{2}; \frac{1-x}{2}\right)}{\sqrt{1-x}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(5/2)/(1 - x)^(3/2), x]

[Out] (8*Sqrt[2]*Hypergeometric2F1[-5/2, -1/2, 1/2, (1 - x)/2])/Sqrt[1 - x]

fricas [A] time = 0.45, size = 58, normalized size = 0.89

$$\frac{(x^2 + 7x - 24)\sqrt{x+1}\sqrt{-x+1} + 30(x-1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) + 24x - 24}{2(x-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(3/2),x, algorithm="fricas")

[Out] 1/2*((x^2 + 7*x - 24)*sqrt(x + 1)*sqrt(-x + 1) + 30*(x - 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) + 24*x - 24)/(x - 1)

giac [A] time = 1.01, size = 42, normalized size = 0.65

$$\frac{((x + 6)(x + 1) - 30)\sqrt{x + 1}\sqrt{-x + 1}}{2(x - 1)} - 15 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(3/2),x, algorithm="giac")

[Out] 1/2*((x + 6)*(x + 1) - 30)*sqrt(x + 1)*sqrt(-x + 1)/(x - 1) - 15*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.02, size = 77, normalized size = 1.18

$$\frac{15\sqrt{(x + 1)(-x + 1)} \arcsin(x)}{2\sqrt{x + 1}\sqrt{-x + 1}} - \frac{(x^3 + 8x^2 - 17x - 24)\sqrt{(x + 1)(-x + 1)}}{2\sqrt{-(x + 1)(x - 1)}\sqrt{-x + 1}\sqrt{x + 1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(5/2)/(-x+1)^(3/2),x)

[Out] -1/2*(x^3+8*x^2-17*x-24)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)/(x+1)^(1/2)-15/2*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.97, size = 56, normalized size = 0.86

$$-\frac{x^3}{2\sqrt{-x^2 + 1}} - \frac{4x^2}{\sqrt{-x^2 + 1}} + \frac{17x}{2\sqrt{-x^2 + 1}} + \frac{12}{\sqrt{-x^2 + 1}} - \frac{15}{2} \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(3/2),x, algorithm="maxima")

[Out] -1/2*x^3/sqrt(-x^2 + 1) - 4*x^2/sqrt(-x^2 + 1) + 17/2*x/sqrt(-x^2 + 1) + 12/sqrt(-x^2 + 1) - 15/2*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(x + 1)^{5/2}}{(1 - x)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x + 1)^(5/2)/(1 - x)^(3/2), x)`

[Out] `int((x + 1)^(5/2)/(1 - x)^(3/2), x)`

sympy [A] time = 7.76, size = 139, normalized size = 2.14

$$\begin{cases} 15i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{i(x+1)^{\frac{5}{2}}}{2\sqrt{x-1}} + \frac{5i(x+1)^{\frac{3}{2}}}{2\sqrt{x-1}} - \frac{15i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ -15 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{(x+1)^{\frac{5}{2}}}{2\sqrt{1-x}} - \frac{5(x+1)^{\frac{3}{2}}}{2\sqrt{1-x}} + \frac{15\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)**(5/2)/(1-x)**(3/2), x)`

[Out] `Piecewise((15*I*acosh(sqrt(2)*sqrt(x + 1)/2) + I*(x + 1)**(5/2)/(2*sqrt(x - 1)) + 5*I*(x + 1)**(3/2)/(2*sqrt(x - 1)) - 15*I*sqrt(x + 1)/sqrt(x - 1), Abs(x + 1)/2 > 1), (-15*asin(sqrt(2)*sqrt(x + 1)/2) - (x + 1)**(5/2)/(2*sqrt(1 - x)) - 5*(x + 1)**(3/2)/(2*sqrt(1 - x)) + 15*sqrt(x + 1)/sqrt(1 - x), True))`

$$3.1096 \quad \int \frac{(1+x)^{5/2}}{(1-x)^{5/2}} dx$$

Optimal. Leaf size=63

$$\frac{2(x+1)^{5/2}}{3(1-x)^{3/2}} - \frac{10(x+1)^{3/2}}{3\sqrt{1-x}} - 5\sqrt{1-x}\sqrt{x+1} + 5\sin^{-1}(x)$$

[Out] $2/3*(1+x)^{(5/2)/(1-x)^{(3/2)}+5*\arcsin(x)-10/3*(1+x)^{(3/2)/(1-x)^{(1/2)}-5*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 41, 216}

$$\frac{2(x+1)^{5/2}}{3(1-x)^{3/2}} - \frac{10(x+1)^{3/2}}{3\sqrt{1-x}} - 5\sqrt{1-x}\sqrt{x+1} + 5\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(5/2)/(1 - x)^(5/2), x]

[Out] $-5*\text{Sqrt}[1 - x]*\text{Sqrt}[1 + x] - (10*(1 + x)^{(3/2)})/(3*\text{Sqrt}[1 - x]) + (2*(1 + x)^{(5/2)})/(3*(1 - x)^{(3/2)}) + 5*\text{ArcSin}[x]$

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ

`[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0])) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
 \int \frac{(1+x)^{5/2}}{(1-x)^{5/2}} dx &= \frac{2(1+x)^{5/2}}{3(1-x)^{3/2}} - \frac{5}{3} \int \frac{(1+x)^{3/2}}{(1-x)^{3/2}} dx \\
 &= -\frac{10(1+x)^{3/2}}{3\sqrt{1-x}} + \frac{2(1+x)^{5/2}}{3(1-x)^{3/2}} + 5 \int \frac{\sqrt{1+x}}{\sqrt{1-x}} dx \\
 &= -5\sqrt{1-x}\sqrt{1+x} - \frac{10(1+x)^{3/2}}{3\sqrt{1-x}} + \frac{2(1+x)^{5/2}}{3(1-x)^{3/2}} + 5 \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
 &= -5\sqrt{1-x}\sqrt{1+x} - \frac{10(1+x)^{3/2}}{3\sqrt{1-x}} + \frac{2(1+x)^{5/2}}{3(1-x)^{3/2}} + 5 \int \frac{1}{\sqrt{1-x^2}} dx \\
 &= -5\sqrt{1-x}\sqrt{1+x} - \frac{10(1+x)^{3/2}}{3\sqrt{1-x}} + \frac{2(1+x)^{5/2}}{3(1-x)^{3/2}} + 5 \sin^{-1}(x)
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 37, normalized size = 0.59

$$\frac{8\sqrt{2} {}_2F_1\left(-\frac{5}{2}, -\frac{3}{2}; -\frac{1}{2}; \frac{1-x}{2}\right)}{3(1-x)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(5/2)/(1 - x)^(5/2), x]

[Out] (8*Sqrt[2]*Hypergeometric2F1[-5/2, -3/2, -1/2, (1 - x)/2])/(3*(1 - x)^(3/2))

fricas [A] time = 0.43, size = 75, normalized size = 1.19

$$\frac{23x^2 + (3x^2 - 34x + 23)\sqrt{x+1}\sqrt{-x+1} + 30(x^2 - 2x + 1) \arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) - 46x + 23}{3(x^2 - 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(5/2),x, algorithm="fricas")

[Out] $-1/3*(23*x^2 + (3*x^2 - 34*x + 23)*\sqrt{x + 1}*\sqrt{-x + 1} + 30*(x^2 - 2*x + 1)*\arctan((\sqrt{x + 1}*\sqrt{-x + 1} - 1)/x) - 46*x + 23)/(x^2 - 2*x + 1)$

giac [A] time = 0.98, size = 44, normalized size = 0.70

$$-\frac{((3x - 37)(x + 1) + 60)\sqrt{x + 1}\sqrt{-x + 1}}{3(x - 1)^2} + 10 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(5/2),x, algorithm="giac")

[Out] $-1/3*((3*x - 37)*(x + 1) + 60)*\sqrt{x + 1}*\sqrt{-x + 1}/(x - 1)^2 + 10*\arcsin(1/2*\sqrt{2}*\sqrt{x + 1})$

maple [A] time = 0.02, size = 84, normalized size = 1.33

$$\frac{5\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1} \sqrt{-x+1}} + \frac{(3x^3 - 31x^2 - 11x + 23) \sqrt{(x+1)(-x+1)}}{3(x-1) \sqrt{-(x+1)(x-1)} \sqrt{-x+1} \sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(5/2)/(-x+1)^(5/2),x)

[Out] $1/3*(3*x^3-31*x^2-11*x+23)/(x-1)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)/(x+1)^(1/2)+5*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*\arcsin(x)$

maxima [B] time = 2.97, size = 99, normalized size = 1.57

$$-\frac{(-x^2 + 1)^{\frac{5}{2}}}{x^4 - 4x^3 + 6x^2 - 4x + 1} - \frac{5(-x^2 + 1)^{\frac{3}{2}}}{3(x^3 - 3x^2 + 3x - 1)} + \frac{10\sqrt{-x^2 + 1}}{3(x^2 - 2x + 1)} + \frac{35\sqrt{-x^2 + 1}}{3(x - 1)} + 5 \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(5/2),x, algorithm="maxima")

[Out] $-(-x^2 + 1)^(5/2)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1) - 5/3*(-x^2 + 1)^(3/2)/(x^3 - 3*x^2 + 3*x - 1) + 10/3*\sqrt{-x^2 + 1}/(x^2 - 2*x + 1) + 35/3*\sqrt{-x^2 + 1}/(x - 1) + 5*\arcsin(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(x+1)^{5/2}}{(1-x)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x + 1)^(5/2)/(1 - x)^(5/2), x)`

[Out] `int((x + 1)^(5/2)/(1 - x)^(5/2), x)`

sympy [B] time = 7.47, size = 576, normalized size = 9.14

$$\left\{ \begin{array}{l} \frac{30i\sqrt{x-1}(x+1)^{\frac{27}{2}} \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{-3\sqrt{x-1}(x+1)^{\frac{27}{2}} + 6\sqrt{x-1}(x+1)^{\frac{25}{2}}} - \frac{15\pi\sqrt{x-1}(x+1)^{\frac{27}{2}}}{-3\sqrt{x-1}(x+1)^{\frac{27}{2}} + 6\sqrt{x-1}(x+1)^{\frac{25}{2}}} - \frac{60i\sqrt{x-1}(x+1)^{\frac{25}{2}} \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{-3\sqrt{x-1}(x+1)^{\frac{27}{2}} + 6\sqrt{x-1}(x+1)^{\frac{25}{2}}} + \frac{30\pi\sqrt{x-1}(x+1)^{\frac{25}{2}}}{-3\sqrt{x-1}(x+1)^{\frac{27}{2}} + 6\sqrt{x-1}(x+1)^{\frac{25}{2}}} \\ \frac{30\sqrt{1-x}(x+1)^{\frac{27}{2}} \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{3\sqrt{1-x}(x+1)^{\frac{27}{2}} - 6\sqrt{1-x}(x+1)^{\frac{25}{2}}} - \frac{60\sqrt{1-x}(x+1)^{\frac{25}{2}} \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{3\sqrt{1-x}(x+1)^{\frac{27}{2}} - 6\sqrt{1-x}(x+1)^{\frac{25}{2}}} + \frac{3(x+1)^{15}}{3\sqrt{1-x}(x+1)^{\frac{27}{2}} - 6\sqrt{1-x}(x+1)^{\frac{25}{2}}} - \frac{40(x+1)^{14}}{3\sqrt{1-x}(x+1)^{\frac{27}{2}} - 6\sqrt{1-x}(x+1)^{\frac{25}{2}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)**(5/2)/(1-x)**(5/2), x)`

[Out] `Piecewise((30*I*sqrt(x - 1)*(x + 1)**(27/2)*acosh(sqrt(2)*sqrt(x + 1)/2)/(-3*sqrt(x - 1)*(x + 1)**(27/2) + 6*sqrt(x - 1)*(x + 1)**(25/2)) - 15*pi*sqrt(x - 1)*(x + 1)**(27/2)/(-3*sqrt(x - 1)*(x + 1)**(27/2) + 6*sqrt(x - 1)*(x + 1)**(25/2)) - 60*I*sqrt(x - 1)*(x + 1)**(25/2)*acosh(sqrt(2)*sqrt(x + 1)/2)/(-3*sqrt(x - 1)*(x + 1)**(27/2) + 6*sqrt(x - 1)*(x + 1)**(25/2)) + 30*pi*sqrt(x - 1)*(x + 1)**(25/2)/(-3*sqrt(x - 1)*(x + 1)**(27/2) + 6*sqrt(x - 1)*(x + 1)**(25/2)) + 3*I*(x + 1)**15/(-3*sqrt(x - 1)*(x + 1)**(27/2) + 6*sqrt(x - 1)*(x + 1)**(25/2)) - 40*I*(x + 1)**14/(-3*sqrt(x - 1)*(x + 1)**(27/2) + 6*sqrt(x - 1)*(x + 1)**(25/2)) + 60*I*(x + 1)**13/(-3*sqrt(x - 1)*(x + 1)**(27/2) + 6*sqrt(x - 1)*(x + 1)**(25/2)), Abs(x + 1)/2 > 1), (30*sqrt(1 - x)*(x + 1)**(27/2)*asin(sqrt(2)*sqrt(x + 1)/2)/(3*sqrt(1 - x)*(x + 1)**(27/2) - 6*sqrt(1 - x)*(x + 1)**(25/2)) - 60*sqrt(1 - x)*(x + 1)**(25/2)*asin(sqrt(2)*sqrt(x + 1)/2)/(3*sqrt(1 - x)*(x + 1)**(27/2) - 6*sqrt(1 - x)*(x + 1)**(25/2)) + 3*(x + 1)**15/(3*sqrt(1 - x)*(x + 1)**(27/2) - 6*sqrt(1 - x)*(x + 1)**(25/2)) - 40*(x + 1)**14/(3*sqrt(1 - x)*(x + 1)**(27/2) - 6*sqrt(1 - x)*(x + 1)**(25/2)) + 60*(x + 1)**13/(3*sqrt(1 - x)*(x + 1)**(27/2) - 6*sqrt(1 - x)*(x + 1)**(25/2)), True))`

$$3.1097 \quad \int \frac{(1+x)^{5/2}}{(1-x)^{7/2}} dx$$

Optimal. Leaf size=63

$$\frac{2(x+1)^{5/2}}{5(1-x)^{5/2}} - \frac{2(x+1)^{3/2}}{3(1-x)^{3/2}} + \frac{2\sqrt{x+1}}{\sqrt{1-x}} - \sin^{-1}(x)$$

[Out] $-2/3*(1+x)^{(3/2)}/(1-x)^{(3/2)}+2/5*(1+x)^{(5/2)}/(1-x)^{(5/2)}-\arcsin(x)+2*(1+x)^{(1/2)}/(1-x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {47, 41, 216}

$$\frac{2(x+1)^{5/2}}{5(1-x)^{5/2}} - \frac{2(x+1)^{3/2}}{3(1-x)^{3/2}} + \frac{2\sqrt{x+1}}{\sqrt{1-x}} - \sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(5/2)/(1 - x)^(7/2), x]

[Out] (2*Sqrt[1 + x])/Sqrt[1 - x] - (2*(1 + x)^(3/2))/(3*(1 - x)^(3/2)) + (2*(1 + x)^(5/2))/(5*(1 - x)^(5/2)) - ArcSin[x]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(1+x)^{5/2}}{(1-x)^{7/2}} dx &= \frac{2(1+x)^{5/2}}{5(1-x)^{5/2}} - \int \frac{(1+x)^{3/2}}{(1-x)^{5/2}} dx \\
&= -\frac{2(1+x)^{3/2}}{3(1-x)^{3/2}} + \frac{2(1+x)^{5/2}}{5(1-x)^{5/2}} + \int \frac{\sqrt{1+x}}{(1-x)^{3/2}} dx \\
&= \frac{2\sqrt{1+x}}{\sqrt{1-x}} - \frac{2(1+x)^{3/2}}{3(1-x)^{3/2}} + \frac{2(1+x)^{5/2}}{5(1-x)^{5/2}} - \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
&= \frac{2\sqrt{1+x}}{\sqrt{1-x}} - \frac{2(1+x)^{3/2}}{3(1-x)^{3/2}} + \frac{2(1+x)^{5/2}}{5(1-x)^{5/2}} - \int \frac{1}{\sqrt{1-x^2}} dx \\
&= \frac{2\sqrt{1+x}}{\sqrt{1-x}} - \frac{2(1+x)^{3/2}}{3(1-x)^{3/2}} + \frac{2(1+x)^{5/2}}{5(1-x)^{5/2}} - \sin^{-1}(x)
\end{aligned}$$

Mathematica [C] time = 0.01, size = 37, normalized size = 0.59

$$\frac{8\sqrt{2} {}_2F_1\left(-\frac{5}{2}, -\frac{5}{2}; -\frac{3}{2}; \frac{1-x}{2}\right)}{5(1-x)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(5/2)/(1 - x)^(7/2), x]

[Out] (8*Sqrt[2]*Hypergeometric2F1[-5/2, -5/2, -3/2, (1 - x)/2])/(5*(1 - x)^(5/2))

fricas [A] time = 0.46, size = 91, normalized size = 1.44

$$\frac{2\left(13x^3 - 39x^2 - (23x^2 - 24x + 13)\sqrt{x+1}\sqrt{-x+1} + 15(x^3 - 3x^2 + 3x - 1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) + 39x - 3\right)}{15(x^3 - 3x^2 + 3x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(7/2), x, algorithm="fricas")

[Out] 2/15*(13*x^3 - 39*x^2 - (23*x^2 - 24*x + 13)*sqrt(x + 1)*sqrt(-x + 1) + 15*(x^3 - 3*x^2 + 3*x - 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) + 39*x - 3)/(x^3 - 3*x^2 + 3*x - 1)

giac [A] time = 0.98, size = 44, normalized size = 0.70

$$-\frac{2((23x-47)(x+1)+60)\sqrt{x+1}\sqrt{-x+1}}{15(x-1)^3} - 2 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(7/2),x, algorithm="giac")

[Out] -2/15*((23*x - 47)*(x + 1) + 60)*sqrt(x + 1)*sqrt(-x + 1)/(x - 1)^3 - 2*arc sin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.02, size = 84, normalized size = 1.33

$$-\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1} \sqrt{-x+1}} + \frac{2(23x^3 - x^2 - 11x + 13) \sqrt{(x+1)(-x+1)}}{15(x-1)^2 \sqrt{-(x+1)(x-1)} \sqrt{-x+1} \sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(5/2)/(-x+1)^(7/2),x)

[Out] 2/15*(23*x^3-x^2-11*x+13)/(x-1)^2/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)/(x+1)^(1/2)-((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arc sin(x)

maxima [B] time = 3.07, size = 160, normalized size = 2.54

$$-\frac{(-x^2+1)^{\frac{5}{2}}}{5(x^5-5x^4+10x^3-10x^2+5x-1)} + \frac{(-x^2+1)^{\frac{3}{2}}}{x^4-4x^3+6x^2-4x+1} + \frac{(-x^2+1)^{\frac{3}{2}}}{3(x^3-3x^2+3x-1)} + \frac{6\sqrt{-x^2+1}}{5(x^3-3x^2+3x-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(7/2),x, algorithm="maxima")

[Out] -1/5*(-x^2 + 1)^(5/2)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) + (-x^2 + 1)^(3/2)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1) + 1/3*(-x^2 + 1)^(3/2)/(x^3 - 3*x^2 + 3*x - 1) + 6/5*sqrt(-x^2 + 1)/(x^3 - 3*x^2 + 3*x - 1) - 7/15*sqrt(-x^2 + 1)/(x^2 - 2*x + 1) - 38/15*sqrt(-x^2 + 1)/(x - 1) - arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(x+1)^{5/2}}{(1-x)^{7/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.


```
[In] int((x + 1)^(5/2)/(1 - x)^(7/2),x)
```

```
[Out] int((x + 1)^(5/2)/(1 - x)^(7/2), x)
```

sympy [B] time = 11.21, size = 1608, normalized size = 25.52

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((1+x)**(5/2)/(1-x)**(7/2),x)
```

```
[Out] Piecewise((30*I*sqrt(x - 1)*(x + 1)**(35/2)*acosh(sqrt(2)*sqrt(x + 1)/2)/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) - 15*pi*sqrt(x - 1)*(x + 1)**(35/2)/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) - 180*I*sqrt(x - 1)*(x + 1)**(33/2)*acosh(sqrt(2)*sqrt(x + 1)/2)/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) + 90*pi*sqrt(x - 1)*(x + 1)**(33/2)/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) + 360*I*sqrt(x - 1)*(x + 1)**(31/2)*acosh(sqrt(2)*sqrt(x + 1)/2)/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) - 180*pi*sqrt(x - 1)*(x + 1)**(31/2)/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) - 240*I*sqrt(x - 1)*(x + 1)**(29/2)*acosh(sqrt(2)*sqrt(x + 1)/2)/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) + 120*pi*sqrt(x - 1)*(x + 1)**(29/2)/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) - 46*I*(x + 1)**18/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) + 232*I*(x + 1)**17/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) - 400*I*(x + 1)**16/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) + 240*I*(x + 1)**15/(15*sqrt(x - 1)*(x + 1)**(35/2) - 90*sqrt(x - 1)*(x + 1)**(33/2) + 180*sqrt(x - 1)*(x + 1)**(31/2) - 120*sqrt(x - 1)*(x + 1)**(29/2)) , Abs(x + 1)/2 > 1), (-30*sqrt(1 - x)*(x + 1)**(35/2)*asin(sqrt(2)*sqrt(x + 1)/2)/(15*sqrt(1 - x)*(x + 1)**(35/2) - 90*sqrt(1 - x)*(x + 1)**(33/2) + 180*sqrt(1 - x)*(x + 1)**(31/2) - 120*sqrt(1 - x)*(x + 1)**(29/2)) + 180*sqrt(1 - x)*(x + 1)**(33/2)*asin(sqrt(2)*sqrt(x + 1)/2)/(15*sqrt(1 - x)*(x + 1)**(35/2) - 90*sqrt(1 - x)*(x + 1)**(33/2) + 180*sqrt(1 - x)*(x + 1)**(31/2) - 120*sqrt(1 - x)*(x + 1)**(29/2)) - 360*sqrt(1 - x)*(x + 1)**(31/2)*asin
```

```

(sqrt(2)*sqrt(x + 1)/2)/(15*sqrt(1 - x)*(x + 1)**(35/2) - 90*sqrt(1 - x)*(x
+ 1)**(33/2) + 180*sqrt(1 - x)*(x + 1)**(31/2) - 120*sqrt(1 - x)*(x + 1)**
(29/2)) + 240*sqrt(1 - x)*(x + 1)**(29/2)*asin(sqrt(2)*sqrt(x + 1)/2)/(15*s
qrt(1 - x)*(x + 1)**(35/2) - 90*sqrt(1 - x)*(x + 1)**(33/2) + 180*sqrt(1 -
x)*(x + 1)**(31/2) - 120*sqrt(1 - x)*(x + 1)**(29/2)) + 46*(x + 1)**18/(15*
sqrt(1 - x)*(x + 1)**(35/2) - 90*sqrt(1 - x)*(x + 1)**(33/2) + 180*sqrt(1 -
x)*(x + 1)**(31/2) - 120*sqrt(1 - x)*(x + 1)**(29/2)) - 232*(x + 1)**17/(1
5*sqrt(1 - x)*(x + 1)**(35/2) - 90*sqrt(1 - x)*(x + 1)**(33/2) + 180*sqrt(1
- x)*(x + 1)**(31/2) - 120*sqrt(1 - x)*(x + 1)**(29/2)) + 400*(x + 1)**16/
(15*sqrt(1 - x)*(x + 1)**(35/2) - 90*sqrt(1 - x)*(x + 1)**(33/2) + 180*sqrt
(1 - x)*(x + 1)**(31/2) - 120*sqrt(1 - x)*(x + 1)**(29/2)) - 240*(x + 1)**1
5/(15*sqrt(1 - x)*(x + 1)**(35/2) - 90*sqrt(1 - x)*(x + 1)**(33/2) + 180*sq
rt(1 - x)*(x + 1)**(31/2) - 120*sqrt(1 - x)*(x + 1)**(29/2)), True))

```

$$3.1098 \quad \int \frac{(1+x)^{5/2}}{(1-x)^{9/2}} dx$$

Optimal. Leaf size=20

$$\frac{(x+1)^{7/2}}{7(1-x)^{7/2}}$$

[Out] 1/7*(1+x)^(7/2)/(1-x)^(7/2)

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {37}

$$\frac{(x+1)^{7/2}}{7(1-x)^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(5/2)/(1 - x)^(9/2), x]

[Out] (1 + x)^(7/2)/(7*(1 - x)^(7/2))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp [((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(1+x)^{5/2}}{(1-x)^{9/2}} dx = \frac{(1+x)^{7/2}}{7(1-x)^{7/2}}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 1.00

$$\frac{(x+1)^{7/2}}{7(1-x)^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(5/2)/(1 - x)^(9/2), x]

[Out] (1 + x)^(7/2)/(7*(1 - x)^(7/2))

fricas [B] time = 0.44, size = 66, normalized size = 3.30

$$\frac{x^4 - 4x^3 + 6x^2 + (x^3 + 3x^2 + 3x + 1)\sqrt{x+1}\sqrt{-x+1} - 4x + 1}{7(x^4 - 4x^3 + 6x^2 - 4x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(9/2),x, algorithm="fricas")

[Out] 1/7*(x^4 - 4*x^3 + 6*x^2 + (x^3 + 3*x^2 + 3*x + 1)*sqrt(x + 1)*sqrt(-x + 1) - 4*x + 1)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1)

giac [A] time = 1.11, size = 19, normalized size = 0.95

$$\frac{(x+1)^{\frac{7}{2}}\sqrt{-x+1}}{7(x-1)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(9/2),x, algorithm="giac")

[Out] 1/7*(x + 1)^(7/2)*sqrt(-x + 1)/(x - 1)^4

maple [A] time = 0.00, size = 15, normalized size = 0.75

$$\frac{(x+1)^{\frac{7}{2}}}{7(-x+1)^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(5/2)/(-x+1)^(9/2),x)

[Out] 1/7*(x+1)^(7/2)/(-x+1)^(7/2)

maxima [B] time = 1.36, size = 171, normalized size = 8.55

$$\frac{(-x^2 + 1)^{\frac{5}{2}}}{x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1} + \frac{5(-x^2 + 1)^{\frac{3}{2}}}{2(x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1)} + \frac{15\sqrt{-x^2 + 1}}{7(x^4 - 4x^3 + 6x^2 - 4x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(9/2),x, algorithm="maxima")

[Out] (-x^2 + 1)^(5/2)/(x^6 - 6*x^5 + 15*x^4 - 20*x^3 + 15*x^2 - 6*x + 1) + 5/2*(-x^2 + 1)^(3/2)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) + 15/7*sqrt(-x^2

+ 1)/(x⁴ - 4*x³ + 6*x² - 4*x + 1) + 3/14*sqrt(-x² + 1)/(x³ - 3*x² + 3*x - 1) - 1/7*sqrt(-x² + 1)/(x² - 2*x + 1) + 1/7*sqrt(-x² + 1)/(x - 1)

mupad [B] time = 0.28, size = 64, normalized size = 3.20

$$\frac{\sqrt{1-x} \left(\frac{3x\sqrt{x+1}}{7} + \frac{\sqrt{x+1}}{7} + \frac{3x^2\sqrt{x+1}}{7} + \frac{x^3\sqrt{x+1}}{7} \right)}{x^4 - 4x^3 + 6x^2 - 4x + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(5/2)/(1 - x)^(9/2), x)

[Out] ((1 - x)^(1/2)*((3*x*(x + 1)^(1/2))/7 + (x + 1)^(1/2)/7 + (3*x²*(x + 1)^(1/2))/7 + (x³*(x + 1)^(1/2))/7)/(6*x² - 4*x - 4*x³ + x⁴ + 1)

sympy [B] time = 19.49, size = 116, normalized size = 5.80

$$\begin{cases} \frac{i(x+1)^{\frac{7}{2}}}{7\sqrt{x-1}(x+1)^3 - 42\sqrt{x-1}(x+1)^2 + 84\sqrt{x-1}(x+1) - 56\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ \frac{(x+1)^{\frac{7}{2}}}{7\sqrt{1-x}(x+1)^3 - 42\sqrt{1-x}(x+1)^2 + 84\sqrt{1-x}(x+1) - 56\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(5/2)/(1-x)**(9/2), x)

[Out] Piecewise((I*(x + 1)**(7/2)/(7*sqrt(x - 1)*(x + 1)**3 - 42*sqrt(x - 1)*(x + 1)**2 + 84*sqrt(x - 1)*(x + 1) - 56*sqrt(x - 1)), Abs(x + 1)/2 > 1), (- (x + 1)**(7/2)/(7*sqrt(1 - x)*(x + 1)**3 - 42*sqrt(1 - x)*(x + 1)**2 + 84*sqrt(1 - x)*(x + 1) - 56*sqrt(1 - x)), True))

3.1099

$$\int \frac{(1+x)^{5/2}}{(1-x)^{11/2}} dx$$

Optimal. Leaf size=41

$$\frac{(x+1)^{7/2}}{63(1-x)^{7/2}} + \frac{(x+1)^{7/2}}{9(1-x)^{9/2}}$$

[Out] $1/9*(1+x)^{(7/2)/(1-x)^{(9/2)}+1/63*(1+x)^{(7/2)/(1-x)^{(7/2)}$

Rubi [A] time = 0.00, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{(x+1)^{7/2}}{63(1-x)^{7/2}} + \frac{(x+1)^{7/2}}{9(1-x)^{9/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(5/2)/(1 - x)^(11/2), x]

[Out] (1 + x)^(7/2)/(9*(1 - x)^(9/2)) + (1 + x)^(7/2)/(63*(1 - x)^(7/2))

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp
[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
+ d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned}\int \frac{(1+x)^{5/2}}{(1-x)^{11/2}} dx &= \frac{(1+x)^{7/2}}{9(1-x)^{9/2}} + \frac{1}{9} \int \frac{(1+x)^{5/2}}{(1-x)^{9/2}} dx \\ &= \frac{(1+x)^{7/2}}{9(1-x)^{9/2}} + \frac{(1+x)^{7/2}}{63(1-x)^{7/2}}\end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.56

$$\frac{(x-8)(x+1)^{7/2}}{63(1-x)^{9/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^(5/2)/(1 - x)^(11/2), x]

[Out] -1/63*((-8 + x)*(1 + x)^(7/2))/(1 - x)^(9/2)

fricas [B] time = 0.42, size = 83, normalized size = 2.02

$$\frac{8x^5 - 40x^4 + 80x^3 - 80x^2 + (x^4 - 5x^3 - 21x^2 - 23x - 8)\sqrt{x+1}\sqrt{-x+1} + 40x - 8}{63(x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(11/2), x, algorithm="fricas")

[Out] 1/63*(8*x^5 - 40*x^4 + 80*x^3 - 80*x^2 + (x^4 - 5*x^3 - 21*x^2 - 23*x - 8)*sqrt(x + 1)*sqrt(-x + 1) + 40*x - 8)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1)

giac [A] time = 1.23, size = 22, normalized size = 0.54

$$\frac{(x+1)^{7/2}(x-8)\sqrt{-x+1}}{63(x-1)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(11/2), x, algorithm="giac")

[Out] 1/63*(x + 1)^(7/2)*(x - 8)*sqrt(-x + 1)/(x - 1)^5

maple [A] time = 0.00, size = 18, normalized size = 0.44

$$\frac{(x+1)^{7/2}(x-8)}{63(-x+1)^{9/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x+1)^(5/2)/(-x+1)^(11/2),x)`

[Out] $-1/63*(x+1)^{(7/2)}*(x-8)/(-x+1)^{(9/2)}$

maxima [B] time = 1.40, size = 218, normalized size = 5.32

$$\frac{(-x^2 + 1)^{\frac{5}{2}}}{2(x^7 - 7x^6 + 21x^5 - 35x^4 + 35x^3 - 21x^2 + 7x - 1)} - \frac{5(-x^2 + 1)^{\frac{3}{2}}}{6(x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1) - 9(x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)^(5/2)/(1-x)^(11/2),x, algorithm="maxima")`

[Out] $-1/2*(-x^2 + 1)^{(5/2)}/(x^7 - 7*x^6 + 21*x^5 - 35*x^4 + 35*x^3 - 21*x^2 + 7*x - 1) - 5/6*(-x^2 + 1)^{(3/2)}/(x^6 - 6*x^5 + 15*x^4 - 20*x^3 + 15*x^2 - 6*x + 1) - 5/9*\sqrt{-x^2 + 1}/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) - 5/12*6*\sqrt{-x^2 + 1}/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1) + 1/42*\sqrt{-x^2 + 1}/(x^3 - 3*x^2 + 3*x - 1) - 1/63*\sqrt{-x^2 + 1}/(x^2 - 2*x + 1) + 1/63*\sqrt{-x^2 + 1}/(x - 1)$

mupad [B] time = 0.30, size = 80, normalized size = 1.95

$$\frac{\sqrt{1-x} \left(\frac{23x\sqrt{x+1}}{63} + \frac{8\sqrt{x+1}}{63} + \frac{x^2\sqrt{x+1}}{3} + \frac{5x^3\sqrt{x+1}}{63} - \frac{x^4\sqrt{x+1}}{63} \right)}{x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x + 1)^(5/2)/(1 - x)^(11/2),x)`

[Out] $-((1 - x)^{(1/2)}*((23*x*(x + 1)^{(1/2)})/63 + (8*(x + 1)^{(1/2)})/63 + (x^2*(x + 1)^{(1/2)})/3 + (5*x^3*(x + 1)^{(1/2)})/63 - (x^4*(x + 1)^{(1/2)})/63))/(5*x - 10*x^2 + 10*x^3 - 5*x^4 + x^5 - 1)$

sympy [B] time = 53.14, size = 282, normalized size = 6.88

$$\left\{ \begin{array}{l} \frac{i(x+1)^{\frac{9}{2}}}{63\sqrt{x-1}(x+1)^4-504\sqrt{x-1}(x+1)^3+1512\sqrt{x-1}(x+1)^2-2016\sqrt{x-1}(x+1)+1008\sqrt{x-1}} - \frac{9i(x+1)^{\frac{7}{2}}}{63\sqrt{x-1}(x+1)^4-504\sqrt{x-1}(x+1)^3+1512\sqrt{x-1}(x+1)^2-2016\sqrt{x-1}(x+1)+1008\sqrt{x-1}} \\ - \frac{(x+1)^{\frac{9}{2}}}{63\sqrt{1-x}(x+1)^4-504\sqrt{1-x}(x+1)^3+1512\sqrt{1-x}(x+1)^2-2016\sqrt{1-x}(x+1)+1008\sqrt{1-x}} + \frac{9(x+1)^{\frac{7}{2}}}{63\sqrt{1-x}(x+1)^4-504\sqrt{1-x}(x+1)^3+1512\sqrt{1-x}(x+1)^2-2016\sqrt{1-x}(x+1)+1008\sqrt{1-x}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.


```
[In] integrate((1+x)**(5/2)/(1-x)**(11/2),x)
```

```
[Out] Piecewise((I*(x + 1)**(9/2)/(63*sqrt(x - 1)*(x + 1)**4 - 504*sqrt(x - 1)*(x + 1)**3 + 1512*sqrt(x - 1)*(x + 1)**2 - 2016*sqrt(x - 1)*(x + 1) + 1008*sqrt(x - 1)) - 9*I*(x + 1)**(7/2)/(63*sqrt(x - 1)*(x + 1)**4 - 504*sqrt(x - 1)*(x + 1)**3 + 1512*sqrt(x - 1)*(x + 1)**2 - 2016*sqrt(x - 1)*(x + 1) + 1008*sqrt(x - 1)), Abs(x + 1)/2 > 1), (-(x + 1)**(9/2)/(63*sqrt(1 - x)*(x + 1)**4 - 504*sqrt(1 - x)*(x + 1)**3 + 1512*sqrt(1 - x)*(x + 1)**2 - 2016*sqrt(1 - x)*(x + 1) + 1008*sqrt(1 - x)) + 9*(x + 1)**(7/2)/(63*sqrt(1 - x)*(x + 1)**4 - 504*sqrt(1 - x)*(x + 1)**3 + 1512*sqrt(1 - x)*(x + 1)**2 - 2016*sqrt(1 - x)*(x + 1) + 1008*sqrt(1 - x)), True))
```

$$3.1100 \quad \int \frac{(1+x)^{5/2}}{(1-x)^{13/2}} dx$$

Optimal. Leaf size=61

$$\frac{2(x+1)^{7/2}}{693(1-x)^{7/2}} + \frac{2(x+1)^{7/2}}{99(1-x)^{9/2}} + \frac{(x+1)^{7/2}}{11(1-x)^{11/2}}$$

[Out] $1/11*(1+x)^{(7/2)/(1-x)^{(11/2)}+2/99*(1+x)^{(7/2)/(1-x)^{(9/2)}+2/693*(1+x)^{(7/2)/(1-x)^{(7/2)}}$

Rubi [A] time = 0.01, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{2(x+1)^{7/2}}{693(1-x)^{7/2}} + \frac{2(x+1)^{7/2}}{99(1-x)^{9/2}} + \frac{(x+1)^{7/2}}{11(1-x)^{11/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(5/2)/(1 - x)^(13/2), x]

[Out] (1 + x)^(7/2)/(11*(1 - x)^(11/2)) + (2*(1 + x)^(7/2))/(99*(1 - x)^(9/2)) + (2*(1 + x)^(7/2))/(693*(1 - x)^(7/2))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{(1+x)^{5/2}}{(1-x)^{13/2}} dx &= \frac{(1+x)^{7/2}}{11(1-x)^{11/2}} + \frac{2}{11} \int \frac{(1+x)^{5/2}}{(1-x)^{11/2}} dx \\ &= \frac{(1+x)^{7/2}}{11(1-x)^{11/2}} + \frac{2(1+x)^{7/2}}{99(1-x)^{9/2}} + \frac{2}{99} \int \frac{(1+x)^{5/2}}{(1-x)^{9/2}} dx \\ &= \frac{(1+x)^{7/2}}{11(1-x)^{11/2}} + \frac{2(1+x)^{7/2}}{99(1-x)^{9/2}} + \frac{2(1+x)^{7/2}}{693(1-x)^{7/2}} \end{aligned}$$

Mathematica [A] time = 0.02, size = 30, normalized size = 0.49

$$\frac{(x+1)^{7/2}(2x^2-18x+79)}{693(1-x)^{11/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1+x)^(5/2)/(1-x)^(13/2),x]

[Out] ((1+x)^(7/2)*(79-18*x+2*x^2))/(693*(1-x)^(11/2))

fricas [B] time = 0.46, size = 100, normalized size = 1.64

$$\frac{79x^6 - 474x^5 + 1185x^4 - 1580x^3 + 1185x^2 + (2x^5 - 12x^4 + 31x^3 + 185x^2 + 219x + 79)\sqrt{x+1}\sqrt{-x+1} - 474x + 79}{693(x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(13/2),x, algorithm="fricas")

[Out] 1/693*(79*x^6 - 474*x^5 + 1185*x^4 - 1580*x^3 + 1185*x^2 + (2*x^5 - 12*x^4 + 31*x^3 + 185*x^2 + 219*x + 79)*sqrt(x+1)*sqrt(-x+1) - 474*x + 79)/(x^6 - 6*x^5 + 15*x^4 - 20*x^3 + 15*x^2 - 6*x + 1)

giac [A] time = 1.27, size = 29, normalized size = 0.48

$$\frac{(2(x+1)(x-10)+99)(x+1)^{7/2}\sqrt{-x+1}}{693(x-1)^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(13/2),x, algorithm="giac")

[Out] 1/693*(2*(x+1)*(x-10)+99)*(x+1)^(7/2)*sqrt(-x+1)/(x-1)^6

maple [A] time = 0.00, size = 25, normalized size = 0.41

$$\frac{(x+1)^{\frac{7}{2}}(2x^2-18x+79)}{693(-x+1)^{\frac{11}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(5/2)/(-x+1)^(13/2), x)

[Out] 1/693*(x+1)^(7/2)*(2*x^2-18*x+79)/(-x+1)^(11/2)

maxima [B] time = 1.42, size = 269, normalized size = 4.41

$$\frac{(-x^2+1)^{\frac{5}{2}}}{3(x^8-8x^7+28x^6-56x^5+70x^4-56x^3+28x^2-8x+1)} + \frac{5(-x^2+1)^{\frac{3}{2}}}{12(x^7-7x^6+21x^5-35x^4+35x^3-21x^2+7x-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(13/2), x, algorithm="maxima")

[Out] 1/3*(-x^2+1)^(5/2)/(x^8-8*x^7+28*x^6-56*x^5+70*x^4-56*x^3+28*x^2-8*x+1) + 5/12*(-x^2+1)^(3/2)/(x^7-7*x^6+21*x^5-35*x^4+35*x^3-21*x^2+7*x-1) + 5/22*sqrt(-x^2+1)/(x^6-6*x^5+15*x^4-20*x^3+15*x^2-6*x+1) + 5/396*sqrt(-x^2+1)/(x^5-5*x^4+10*x^3-10*x^2+5*x-1) - 5/693*sqrt(-x^2+1)/(x^4-4*x^3+6*x^2-4*x+1) + 1/231*sqrt(-x^2+1)/(x^3-3*x^2+3*x-1) - 2/693*sqrt(-x^2+1)/(x^2-2*x+1) + 2/693*sqrt(-x^2+1)/(x-1)

mupad [B] time = 0.31, size = 94, normalized size = 1.54

$$\frac{\sqrt{1-x} \left(\frac{73x\sqrt{x+1}}{231} + \frac{79\sqrt{x+1}}{693} + \frac{185x^2\sqrt{x+1}}{693} + \frac{31x^3\sqrt{x+1}}{693} - \frac{4x^4\sqrt{x+1}}{231} + \frac{2x^5\sqrt{x+1}}{693} \right)}{x^6-6x^5+15x^4-20x^3+15x^2-6x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(5/2)/(1-x)^(13/2), x)

[Out] ((1-x)^(1/2)*((73*x*(x+1)^(1/2))/231 + (79*(x+1)^(1/2))/693 + (185*x^2*(x+1)^(1/2))/693 + (31*x^3*(x+1)^(1/2))/693 - (4*x^4*(x+1)^(1/2))/231 + (2*x^5*(x+1)^(1/2))/693)/(15*x^2-6*x-20*x^3+15*x^4-6*x^5+x^6+1)

sympy [B] time = 133.94, size = 785, normalized size = 12.87

$$\left\{ \begin{array}{l} \frac{2i(x+1)^{\frac{13}{2}}}{693\sqrt{x-1}(x+1)^6 - 8316\sqrt{x-1}(x+1)^5 + 41580\sqrt{x-1}(x+1)^4 - 110880\sqrt{x-1}(x+1)^3 + 166320\sqrt{x-1}(x+1)^2 - 133056\sqrt{x-1}(x+1) + 44352\sqrt{x-1}} - \frac{693\sqrt{x}}{693\sqrt{x-1}(x+1)^6 - 8316\sqrt{x-1}(x+1)^5 + 41580\sqrt{x-1}(x+1)^4 - 110880\sqrt{x-1}(x+1)^3 + 166320\sqrt{x-1}(x+1)^2 - 133056\sqrt{x-1}(x+1) + 44352\sqrt{x-1}} \\ \frac{2(x+1)^{\frac{13}{2}}}{693\sqrt{1-x}(x+1)^6 - 8316\sqrt{1-x}(x+1)^5 + 41580\sqrt{1-x}(x+1)^4 - 110880\sqrt{1-x}(x+1)^3 + 166320\sqrt{1-x}(x+1)^2 - 133056\sqrt{1-x}(x+1) + 44352\sqrt{1-x}} + \frac{693\sqrt{x}}{693\sqrt{1-x}(x+1)^6 - 8316\sqrt{1-x}(x+1)^5 + 41580\sqrt{1-x}(x+1)^4 - 110880\sqrt{1-x}(x+1)^3 + 166320\sqrt{1-x}(x+1)^2 - 133056\sqrt{1-x}(x+1) + 44352\sqrt{1-x}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(5/2)/(1-x)**(13/2), x)

[Out] Piecewise((2*I*(x + 1)**(13/2)/(693*sqrt(x - 1)*(x + 1)**6 - 8316*sqrt(x - 1)*(x + 1)**5 + 41580*sqrt(x - 1)*(x + 1)**4 - 110880*sqrt(x - 1)*(x + 1)**3 + 166320*sqrt(x - 1)*(x + 1)**2 - 133056*sqrt(x - 1)*(x + 1) + 44352*sqrt(x - 1)) - 26*I*(x + 1)**(11/2)/(693*sqrt(x - 1)*(x + 1)**6 - 8316*sqrt(x - 1)*(x + 1)**5 + 41580*sqrt(x - 1)*(x + 1)**4 - 110880*sqrt(x - 1)*(x + 1)**3 + 166320*sqrt(x - 1)*(x + 1)**2 - 133056*sqrt(x - 1)*(x + 1) + 44352*sqrt(x - 1)) + 143*I*(x + 1)**(9/2)/(693*sqrt(x - 1)*(x + 1)**6 - 8316*sqrt(x - 1)*(x + 1)**5 + 41580*sqrt(x - 1)*(x + 1)**4 - 110880*sqrt(x - 1)*(x + 1)**3 + 166320*sqrt(x - 1)*(x + 1)**2 - 133056*sqrt(x - 1)*(x + 1) + 44352*sqrt(x - 1)) - 198*I*(x + 1)**(7/2)/(693*sqrt(x - 1)*(x + 1)**6 - 8316*sqrt(x - 1)*(x + 1)**5 + 41580*sqrt(x - 1)*(x + 1)**4 - 110880*sqrt(x - 1)*(x + 1)**3 + 166320*sqrt(x - 1)*(x + 1)**2 - 133056*sqrt(x - 1)*(x + 1) + 44352*sqrt(x - 1)), Abs(x + 1)/2 > 1), (-2*(x + 1)**(13/2)/(693*sqrt(1 - x)*(x + 1)**6 - 8316*sqrt(1 - x)*(x + 1)**5 + 41580*sqrt(1 - x)*(x + 1)**4 - 110880*sqrt(1 - x)*(x + 1)**3 + 166320*sqrt(1 - x)*(x + 1)**2 - 133056*sqrt(1 - x)*(x + 1) + 44352*sqrt(1 - x)) + 26*(x + 1)**(11/2)/(693*sqrt(1 - x)*(x + 1)**6 - 8316*sqrt(1 - x)*(x + 1)**5 + 41580*sqrt(1 - x)*(x + 1)**4 - 110880*sqrt(1 - x)*(x + 1)**3 + 166320*sqrt(1 - x)*(x + 1)**2 - 133056*sqrt(1 - x)*(x + 1) + 44352*sqrt(1 - x)) - 143*(x + 1)**(9/2)/(693*sqrt(1 - x)*(x + 1)**6 - 8316*sqrt(1 - x)*(x + 1)**5 + 41580*sqrt(1 - x)*(x + 1)**4 - 110880*sqrt(1 - x)*(x + 1)**3 + 166320*sqrt(1 - x)*(x + 1)**2 - 133056*sqrt(1 - x)*(x + 1) + 44352*sqrt(1 - x)) + 198*(x + 1)**(7/2)/(693*sqrt(1 - x)*(x + 1)**6 - 8316*sqrt(1 - x)*(x + 1)**5 + 41580*sqrt(1 - x)*(x + 1)**4 - 110880*sqrt(1 - x)*(x + 1)**3 + 166320*sqrt(1 - x)*(x + 1)**2 - 133056*sqrt(1 - x)*(x + 1) + 44352*sqrt(1 - x)), True))

$$3.1101 \quad \int \frac{(1+x)^{5/2}}{(1-x)^{15/2}} dx$$

Optimal. Leaf size=81

$$\frac{2(x+1)^{7/2}}{3003(1-x)^{7/2}} + \frac{2(x+1)^{7/2}}{429(1-x)^{9/2}} + \frac{3(x+1)^{7/2}}{143(1-x)^{11/2}} + \frac{(x+1)^{7/2}}{13(1-x)^{13/2}}$$

[Out] $1/13*(1+x)^{(7/2)}/(1-x)^{(13/2)}+3/143*(1+x)^{(7/2)}/(1-x)^{(11/2)}+2/429*(1+x)^{(7/2)}/(1-x)^{(9/2)}+2/3003*(1+x)^{(7/2)}/(1-x)^{(7/2)}$

Rubi [A] time = 0.01, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{2(x+1)^{7/2}}{3003(1-x)^{7/2}} + \frac{2(x+1)^{7/2}}{429(1-x)^{9/2}} + \frac{3(x+1)^{7/2}}{143(1-x)^{11/2}} + \frac{(x+1)^{7/2}}{13(1-x)^{13/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(5/2)/(1 - x)^(15/2), x]

[Out] $(1+x)^{(7/2)}/(13*(1-x)^{(13/2)}) + (3*(1+x)^{(7/2)})/(143*(1-x)^{(11/2)}) + (2*(1+x)^{(7/2)})/(429*(1-x)^{(9/2)}) + (2*(1+x)^{(7/2)})/(3003*(1-x)^{(7/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(1+x)^{5/2}}{(1-x)^{15/2}} dx &= \frac{(1+x)^{7/2}}{13(1-x)^{13/2}} + \frac{3}{13} \int \frac{(1+x)^{5/2}}{(1-x)^{13/2}} dx \\
&= \frac{(1+x)^{7/2}}{13(1-x)^{13/2}} + \frac{3(1+x)^{7/2}}{143(1-x)^{11/2}} + \frac{6}{143} \int \frac{(1+x)^{5/2}}{(1-x)^{11/2}} dx \\
&= \frac{(1+x)^{7/2}}{13(1-x)^{13/2}} + \frac{3(1+x)^{7/2}}{143(1-x)^{11/2}} + \frac{2(1+x)^{7/2}}{429(1-x)^{9/2}} + \frac{2}{429} \int \frac{(1+x)^{5/2}}{(1-x)^{9/2}} dx \\
&= \frac{(1+x)^{7/2}}{13(1-x)^{13/2}} + \frac{3(1+x)^{7/2}}{143(1-x)^{11/2}} + \frac{2(1+x)^{7/2}}{429(1-x)^{9/2}} + \frac{2(1+x)^{7/2}}{3003(1-x)^{7/2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 35, normalized size = 0.43

$$\frac{(x+1)^{7/2}(-2x^3+20x^2-97x+310)}{3003(1-x)^{13/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1+x)^(5/2)/(1-x)^(15/2),x]

[Out] ((1+x)^(7/2)*(310-97*x+20*x^2-2*x^3))/(3003*(1-x)^(13/2))

fricas [B] time = 0.43, size = 115, normalized size = 1.42

$$\frac{310x^7 - 2170x^6 + 6510x^5 - 10850x^4 + 10850x^3 - 6510x^2 + (2x^6 - 14x^5 + 43x^4 - 77x^3 - 659x^2 - 833x - 310)\sqrt{x+1}\sqrt{-x+1}}{3003(x^7 - 7x^6 + 21x^5 - 35x^4 + 35x^3 - 21x^2 + 7x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(15/2),x, algorithm="fricas")

[Out] 1/3003*(310*x^7 - 2170*x^6 + 6510*x^5 - 10850*x^4 + 10850*x^3 - 6510*x^2 + (2*x^6 - 14*x^5 + 43*x^4 - 77*x^3 - 659*x^2 - 833*x - 310)*sqrt(x+1)*sqrt(-x+1) + 2170*x - 310)/(x^7 - 7*x^6 + 21*x^5 - 35*x^4 + 35*x^3 - 21*x^2 + 7*x - 1)

giac [A] time = 0.99, size = 35, normalized size = 0.43

$$\frac{((2(x+1)(x-12)+143)(x+1)-429)(x+1)^{7/2}\sqrt{-x+1}}{3003(x-1)^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(15/2),x, algorithm="giac")

[Out] 1/3003*((2*(x + 1)*(x - 12) + 143)*(x + 1) - 429)*(x + 1)^(7/2)*sqrt(-x + 1)/(x - 1)^7

maple [A] time = 0.00, size = 30, normalized size = 0.37

$$\frac{(x+1)^{\frac{7}{2}}(2x^3-20x^2+97x-310)}{3003(-x+1)^{\frac{13}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(5/2)/(-x+1)^(15/2),x)

[Out] -1/3003*(x+1)^(7/2)*(2*x^3-20*x^2+97*x-310)/(-x+1)^(13/2)

maxima [B] time = 1.46, size = 325, normalized size = 4.01

$$\frac{(-x^2+1)^{\frac{5}{2}}}{4(x^9-9x^8+36x^7-84x^6+126x^5-126x^4+84x^3-36x^2+9x-1)} - \frac{(-x^2+1)^{\frac{3}{2}}}{4(x^8-8x^7+28x^6-56x^5+70x^4-42x^3+28x^2-8x+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(15/2),x, algorithm="maxima")

[Out] -1/4*(-x^2 + 1)^(5/2)/(x^9 - 9*x^8 + 36*x^7 - 84*x^6 + 126*x^5 - 126*x^4 + 84*x^3 - 36*x^2 + 9*x - 1) - 1/4*(-x^2 + 1)^(3/2)/(x^8 - 8*x^7 + 28*x^6 - 56*x^5 + 70*x^4 - 56*x^3 + 28*x^2 - 8*x + 1) - 3/26*sqrt(-x^2 + 1)/(x^7 - 7*x^6 + 21*x^5 - 35*x^4 + 35*x^3 - 21*x^2 + 7*x - 1) - 3/572*sqrt(-x^2 + 1)/(x^6 - 6*x^5 + 15*x^4 - 20*x^3 + 15*x^2 - 6*x + 1) + 5/1716*sqrt(-x^2 + 1)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) - 5/3003*sqrt(-x^2 + 1)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1) + 1/1001*sqrt(-x^2 + 1)/(x^3 - 3*x^2 + 3*x - 1) - 2/3003*sqrt(-x^2 + 1)/(x^2 - 2*x + 1) + 2/3003*sqrt(-x^2 + 1)/(x - 1)

mupad [B] time = 0.31, size = 110, normalized size = 1.36

$$\frac{\sqrt{1-x} \left(\frac{119x\sqrt{x+1}}{429} + \frac{310\sqrt{x+1}}{3003} + \frac{659x^2\sqrt{x+1}}{3003} + \frac{x^3\sqrt{x+1}}{39} - \frac{43x^4\sqrt{x+1}}{3003} + \frac{2x^5\sqrt{x+1}}{429} - \frac{2x^6\sqrt{x+1}}{3003} \right)}{x^7 - 7x^6 + 21x^5 - 35x^4 + 35x^3 - 21x^2 + 7x - 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(5/2)/(1 - x)^(15/2),x)

[Out] -((1 - x)^(1/2)*((119*x*(x + 1)^(1/2))/429 + (310*(x + 1)^(1/2))/3003 + (659*x^2*(x + 1)^(1/2))/3003 + (x^3*(x + 1)^(1/2))/39 - (43*x^4*(x + 1)^(1/2))

$$\frac{1}{3003} + \frac{2x^5(x+1)^{1/2}}{429} - \frac{2x^6(x+1)^{1/2}}{3003} \Big/ (7x - 21x^2 + 35x^3 - 35x^4 + 21x^5 - 7x^6 + x^7 - 1)$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(5/2)/(1-x)**(15/2),x)

[Out] Timed out

3.1102

$$\int \frac{(1+x)^{5/2}}{(1-x)^{17/2}} dx$$

Optimal. Leaf size=101

$$\frac{8(x+1)^{7/2}}{45045(1-x)^{7/2}} + \frac{8(x+1)^{7/2}}{6435(1-x)^{9/2}} + \frac{4(x+1)^{7/2}}{715(1-x)^{11/2}} + \frac{4(x+1)^{7/2}}{195(1-x)^{13/2}} + \frac{(x+1)^{7/2}}{15(1-x)^{15/2}}$$

[Out] 1/15*(1+x)^(7/2)/(1-x)^(15/2)+4/195*(1+x)^(7/2)/(1-x)^(13/2)+4/715*(1+x)^(7/2)/(1-x)^(11/2)+8/6435*(1+x)^(7/2)/(1-x)^(9/2)+8/45045*(1+x)^(7/2)/(1-x)^(7/2)

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{8(x+1)^{7/2}}{45045(1-x)^{7/2}} + \frac{8(x+1)^{7/2}}{6435(1-x)^{9/2}} + \frac{4(x+1)^{7/2}}{715(1-x)^{11/2}} + \frac{4(x+1)^{7/2}}{195(1-x)^{13/2}} + \frac{(x+1)^{7/2}}{15(1-x)^{15/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(5/2)/(1 - x)^(17/2), x]

[Out] (1 + x)^(7/2)/(15*(1 - x)^(15/2)) + (4*(1 + x)^(7/2))/(195*(1 - x)^(13/2)) + (4*(1 + x)^(7/2))/(715*(1 - x)^(11/2)) + (8*(1 + x)^(7/2))/(6435*(1 - x)^(9/2)) + (8*(1 + x)^(7/2))/(45045*(1 - x)^(7/2))

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned}
\int \frac{(1+x)^{5/2}}{(1-x)^{17/2}} dx &= \frac{(1+x)^{7/2}}{15(1-x)^{15/2}} + \frac{4}{15} \int \frac{(1+x)^{5/2}}{(1-x)^{15/2}} dx \\
&= \frac{(1+x)^{7/2}}{15(1-x)^{15/2}} + \frac{4(1+x)^{7/2}}{195(1-x)^{13/2}} + \frac{4}{65} \int \frac{(1+x)^{5/2}}{(1-x)^{13/2}} dx \\
&= \frac{(1+x)^{7/2}}{15(1-x)^{15/2}} + \frac{4(1+x)^{7/2}}{195(1-x)^{13/2}} + \frac{4(1+x)^{7/2}}{715(1-x)^{11/2}} + \frac{8}{715} \int \frac{(1+x)^{5/2}}{(1-x)^{11/2}} dx \\
&= \frac{(1+x)^{7/2}}{15(1-x)^{15/2}} + \frac{4(1+x)^{7/2}}{195(1-x)^{13/2}} + \frac{4(1+x)^{7/2}}{715(1-x)^{11/2}} + \frac{8(1+x)^{7/2}}{6435(1-x)^{9/2}} + \frac{8 \int \frac{(1+x)^{5/2}}{(1-x)^{9/2}} dx}{6435} \\
&= \frac{(1+x)^{7/2}}{15(1-x)^{15/2}} + \frac{4(1+x)^{7/2}}{195(1-x)^{13/2}} + \frac{4(1+x)^{7/2}}{715(1-x)^{11/2}} + \frac{8(1+x)^{7/2}}{6435(1-x)^{9/2}} + \frac{8(1+x)^{7/2}}{45045(1-x)^{7/2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 40, normalized size = 0.40

$$\frac{(x+1)^{7/2} (8x^4 - 88x^3 + 468x^2 - 1628x + 4243)}{45045(1-x)^{15/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1+x)^(5/2)/(1-x)^(17/2),x]

[Out] ((1+x)^(7/2)*(4243 - 1628*x + 468*x^2 - 88*x^3 + 8*x^4))/(45045*(1-x)^(15/2))

fricas [A] time = 0.46, size = 130, normalized size = 1.29

$$\frac{4243x^8 - 33944x^7 + 118804x^6 - 237608x^5 + 297010x^4 - 237608x^3 + 118804x^2 + (8x^7 - 64x^6 + 228x^5 - 480x^4 + 675x^3 + 8313x^2 + 11101x + 4243)\sqrt{x+1}\sqrt{-x+1} - 33944x + 4243}{45045(x^8 - 8x^7 + 28x^6 - 56x^5 + 70x^4 - 56x^3 + 28x^2 - 8x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(17/2),x, algorithm="fricas")

[Out] 1/45045*(4243*x^8 - 33944*x^7 + 118804*x^6 - 237608*x^5 + 297010*x^4 - 237608*x^3 + 118804*x^2 + (8*x^7 - 64*x^6 + 228*x^5 - 480*x^4 + 675*x^3 + 8313*x^2 + 11101*x + 4243)*sqrt(x+1)*sqrt(-x+1) - 33944*x + 4243)/(x^8 - 8*x^7 + 28*x^6 - 56*x^5 + 70*x^4 - 56*x^3 + 28*x^2 - 8*x + 1)

giac [A] time = 0.88, size = 42, normalized size = 0.42

$$\frac{(4((2(x+1)(x-14)+195)(x+1)-715)(x+1)+6435)(x+1)^{7/2}\sqrt{-x+1}}{45045(x-1)^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(17/2),x, algorithm="giac")

[Out] 1/45045*(4*((2*(x + 1)*(x - 14) + 195)*(x + 1) - 715)*(x + 1) + 6435)*(x + 1)^(7/2)*sqrt(-x + 1)/(x - 1)^8

maple [A] time = 0.00, size = 35, normalized size = 0.35

$$\frac{(x+1)^{\frac{7}{2}}(8x^4 - 88x^3 + 468x^2 - 1628x + 4243)}{45045(-x+1)^{\frac{15}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(5/2)/(-x+1)^(17/2),x)

[Out] 1/45045*(x+1)^(7/2)*(8*x^4-88*x^3+468*x^2-1628*x+4243)/(-x+1)^(15/2)

maxima [B] time = 1.39, size = 386, normalized size = 3.82

$$\frac{(-x^2 + 1)^{\frac{5}{2}}}{5(x^{10} - 10x^9 + 45x^8 - 120x^7 + 210x^6 - 252x^5 + 210x^4 - 120x^3 + 45x^2 - 10x + 1)} + \frac{1}{6(x^9 - 9x^8 + 36x^7 - 84x^6 + 126x^5 - 126x^4 + 84x^3 - 36x^2 + 9x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(17/2),x, algorithm="maxima")

[Out] 1/5*(-x^2 + 1)^(5/2)/(x^10 - 10*x^9 + 45*x^8 - 120*x^7 + 210*x^6 - 252*x^5 + 210*x^4 - 120*x^3 + 45*x^2 - 10*x + 1) + 1/6*(-x^2 + 1)^(3/2)/(x^9 - 9*x^8 + 36*x^7 - 84*x^6 + 126*x^5 - 126*x^4 + 84*x^3 - 36*x^2 + 9*x - 1) + 1/15*sqrt(-x^2 + 1)/(x^8 - 8*x^7 + 28*x^6 - 56*x^5 + 70*x^4 - 56*x^3 + 28*x^2 - 8*x + 1) + 1/390*sqrt(-x^2 + 1)/(x^7 - 7*x^6 + 21*x^5 - 35*x^4 + 35*x^3 - 21*x^2 + 7*x - 1) - 1/715*sqrt(-x^2 + 1)/(x^6 - 6*x^5 + 15*x^4 - 20*x^3 + 15*x^2 - 6*x + 1) + 1/1287*sqrt(-x^2 + 1)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) - 4/9009*sqrt(-x^2 + 1)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1) + 4/15015*sqrt(-x^2 + 1)/(x^3 - 3*x^2 + 3*x - 1) - 8/45045*sqrt(-x^2 + 1)/(x^2 - 2*x + 1) + 8/45045*sqrt(-x^2 + 1)/(x - 1)

mupad [B] time = 0.35, size = 124, normalized size = 1.23

$$\frac{\sqrt{1-x} \left(\frac{11101x\sqrt{x+1}}{45045} + \frac{4243\sqrt{x+1}}{45045} + \frac{2771x^2\sqrt{x+1}}{15015} + \frac{15x^3\sqrt{x+1}}{1001} - \frac{32x^4\sqrt{x+1}}{3003} + \frac{76x^5\sqrt{x+1}}{15015} - \frac{64x^6\sqrt{x+1}}{45045} + \frac{8x^7\sqrt{x+1}}{45045} \right)}{x^8 - 8x^7 + 28x^6 - 56x^5 + 70x^4 - 56x^3 + 28x^2 - 8x + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((x + 1)^(5/2)/(1 - x)^(17/2),x)
```

```
[Out] ((1 - x)^(1/2)*((11101*x*(x + 1)^(1/2))/45045 + (4243*(x + 1)^(1/2))/45045
+ (2771*x^2*(x + 1)^(1/2))/15015 + (15*x^3*(x + 1)^(1/2))/1001 - (32*x^4*(x
+ 1)^(1/2))/3003 + (76*x^5*(x + 1)^(1/2))/15015 - (64*x^6*(x + 1)^(1/2))/4
5045 + (8*x^7*(x + 1)^(1/2))/45045))/(28*x^2 - 8*x - 56*x^3 + 70*x^4 - 56*x
^5 + 28*x^6 - 8*x^7 + x^8 + 1)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((1+x)**(5/2)/(1-x)**(17/2),x)
```

```
[Out] Timed out
```

3.1103

$$\int \frac{(1+x)^{5/2}}{(1-x)^{19/2}} dx$$

Optimal. Leaf size=121

$$\frac{8(x+1)^{7/2}}{153153(1-x)^{7/2}} + \frac{8(x+1)^{7/2}}{21879(1-x)^{9/2}} + \frac{4(x+1)^{7/2}}{2431(1-x)^{11/2}} + \frac{4(x+1)^{7/2}}{663(1-x)^{13/2}} + \frac{(x+1)^{7/2}}{51(1-x)^{15/2}} + \frac{(x+1)^{7/2}}{17(1-x)^{17/2}}$$

[Out] $1/17*(1+x)^{(7/2)}/(1-x)^{(17/2)}+1/51*(1+x)^{(7/2)}/(1-x)^{(15/2)}+4/663*(1+x)^{(7/2)}/(1-x)^{(13/2)}+4/2431*(1+x)^{(7/2)}/(1-x)^{(11/2)}+8/21879*(1+x)^{(7/2)}/(1-x)^{(9/2)}+8/153153*(1+x)^{(7/2)}/(1-x)^{(7/2)}$

Rubi [A] time = 0.02, antiderivative size = 121, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{8(x+1)^{7/2}}{153153(1-x)^{7/2}} + \frac{8(x+1)^{7/2}}{21879(1-x)^{9/2}} + \frac{4(x+1)^{7/2}}{2431(1-x)^{11/2}} + \frac{4(x+1)^{7/2}}{663(1-x)^{13/2}} + \frac{(x+1)^{7/2}}{51(1-x)^{15/2}} + \frac{(x+1)^{7/2}}{17(1-x)^{17/2}}$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^(5/2)/(1 - x)^(19/2), x]

[Out] $(1+x)^{(7/2)}/(17*(1-x)^{(17/2)}) + (1+x)^{(7/2)}/(51*(1-x)^{(15/2)}) + (4*(1+x)^{(7/2)})/(663*(1-x)^{(13/2)}) + (4*(1+x)^{(7/2)})/(2431*(1-x)^{(11/2)}) + (8*(1+x)^{(7/2)})/(21879*(1-x)^{(9/2)}) + (8*(1+x)^{(7/2)})/(153153*(1-x)^{(7/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(1+x)^{5/2}}{(1-x)^{19/2}} dx &= \frac{(1+x)^{7/2}}{17(1-x)^{17/2}} + \frac{5}{17} \int \frac{(1+x)^{5/2}}{(1-x)^{17/2}} dx \\
&= \frac{(1+x)^{7/2}}{17(1-x)^{17/2}} + \frac{(1+x)^{7/2}}{51(1-x)^{15/2}} + \frac{4}{51} \int \frac{(1+x)^{5/2}}{(1-x)^{15/2}} dx \\
&= \frac{(1+x)^{7/2}}{17(1-x)^{17/2}} + \frac{(1+x)^{7/2}}{51(1-x)^{15/2}} + \frac{4(1+x)^{7/2}}{663(1-x)^{13/2}} + \frac{4}{221} \int \frac{(1+x)^{5/2}}{(1-x)^{13/2}} dx \\
&= \frac{(1+x)^{7/2}}{17(1-x)^{17/2}} + \frac{(1+x)^{7/2}}{51(1-x)^{15/2}} + \frac{4(1+x)^{7/2}}{663(1-x)^{13/2}} + \frac{4(1+x)^{7/2}}{2431(1-x)^{11/2}} + \frac{8}{2431} \int \frac{(1+x)^{5/2}}{(1-x)^{11/2}} dx \\
&= \frac{(1+x)^{7/2}}{17(1-x)^{17/2}} + \frac{(1+x)^{7/2}}{51(1-x)^{15/2}} + \frac{4(1+x)^{7/2}}{663(1-x)^{13/2}} + \frac{4(1+x)^{7/2}}{2431(1-x)^{11/2}} + \frac{8(1+x)^{7/2}}{21879(1-x)^{9/2}} + \frac{8}{21879} \int \frac{(1+x)^{5/2}}{(1-x)^{9/2}} dx \\
&= \frac{(1+x)^{7/2}}{17(1-x)^{17/2}} + \frac{(1+x)^{7/2}}{51(1-x)^{15/2}} + \frac{4(1+x)^{7/2}}{663(1-x)^{13/2}} + \frac{4(1+x)^{7/2}}{2431(1-x)^{11/2}} + \frac{8(1+x)^{7/2}}{21879(1-x)^{9/2}} + \frac{8(1+x)^{7/2}}{153153(1-x)^{7/2}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 0.37

$$\frac{(x+1)^{7/2}(-8x^5+96x^4-556x^3+2096x^2-5871x+13252)}{153153(1-x)^{17/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1+x)^(5/2)/(1-x)^(19/2),x]

[Out] ((1+x)^(7/2)*(13252-5871*x+2096*x^2-556*x^3+96*x^4-8*x^5))/(153153*(1-x)^(17/2))

fricas [A] time = 0.43, size = 145, normalized size = 1.20

$$\frac{13252x^9 - 119268x^8 + 477072x^7 - 1113168x^6 + 1669752x^5 - 1669752x^4 + 1113168x^3 - 477072x^2 + (8x^8 - 119268x^7 + 1113168x^6 - 477072x^5 + 1669752x^4 - 1113168x^3 - 477072x^2 + 13252)\sqrt{x+1}\sqrt{-x+1} + 119268x - 13252}{153153(x^9 - 9x^8 + 36x^7 - 84x^6 + 126x^5 - 126x^4 + 84x^3 - 36x^2 + 9x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(19/2),x, algorithm="fricas")

[Out] 1/153153*(13252*x^9 - 119268*x^8 + 477072*x^7 - 1113168*x^6 + 1669752*x^5 - 1669752*x^4 + 1113168*x^3 - 477072*x^2 + (8*x^8 - 72*x^7 + 292*x^6 - 708*x^5 + 1155*x^4 - 1371*x^3 - 24239*x^2 - 33885*x - 13252)*sqrt(x+1)*sqrt(-x+1) + 119268*x - 13252)/(x^9 - 9*x^8 + 36*x^7 - 84*x^6 + 126*x^5 - 126*x^4 + 84*x^3 - 36*x^2 + 9*x - 1)

giac [A] time = 0.86, size = 48, normalized size = 0.40

$$\frac{((4((2(x+1)(x-16)+255)(x+1)-1105)(x+1)+12155)(x+1)-21879)(x+1)^{\frac{7}{2}}\sqrt{-x+1}}{153153(x-1)^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(19/2),x, algorithm="giac")

[Out] 1/153153*((4*((2*(x+1)*(x-16)+255)*(x+1)-1105)*(x+1)+12155)*(x+1)-21879)*(x+1)^(7/2)*sqrt(-x+1)/(x-1)^9

maple [A] time = 0.00, size = 40, normalized size = 0.33

$$\frac{(x+1)^{\frac{7}{2}}(8x^5-96x^4+556x^3-2096x^2+5871x-13252)}{153153(-x+1)^{\frac{17}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x+1)^(5/2)/(-x+1)^(19/2),x)

[Out] -1/153153*(x+1)^(7/2)*(8*x^5-96*x^4+556*x^3-2096*x^2+5871*x-13252)/(-x+1)^(17/2)

maxima [B] time = 1.38, size = 452, normalized size = 3.74

$$\frac{(-x^2+1)^{\frac{5}{2}}}{6(x^{11}-11x^{10}+55x^9-165x^8+330x^7-462x^6+462x^5-330x^4+165x^3-55x^2+11x-1)-42(x^{10}-10x^9+45x^8-120x^7+210x^6-252x^5+210x^4-120x^3+45x^2-10x+1)-5/119*\sqrt{-x^2+1}/(x^9-9x^8+36x^7-84x^6+126x^5-126x^4+84x^3-36x^2+9x-1)-1/714*\sqrt{-x^2+1}/(x^8-8x^7+28x^6-56x^5+70x^4-56x^3+28x^2-8x+1)+1/1326*\sqrt{-x^2+1}/(x^7-7x^6+21x^5-35x^4+35x^3-21x^2+7x-1)-1/2431*\sqrt{-x^2+1}/(x^6-6x^5+15x^4-20x^3+15x^2-6x+1)+5/21879*\sqrt{-x^2+1}/(x^5-5x^4+10x^3-10x^2+5x-1)-20/153153*\sqrt{-x^2+1}/(x^4-4x^3+6x^2-4x+1)+4/51051*\sqrt{-x^2+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)^(5/2)/(1-x)^(19/2),x, algorithm="maxima")

[Out] -1/6*(-x^2+1)^(5/2)/(x^11-11*x^10+55*x^9-165*x^8+330*x^7-462*x^6+462*x^5-330*x^4+165*x^3-55*x^2+11*x-1)-5/42*(-x^2+1)^(3/2)/(x^10-10*x^9+45*x^8-120*x^7+210*x^6-252*x^5+210*x^4-120*x^3+45*x^2-10*x+1)-5/119*sqrt(-x^2+1)/(x^9-9*x^8+36*x^7-84*x^6+126*x^5-126*x^4+84*x^3-36*x^2+9*x-1)-1/714*sqrt(-x^2+1)/(x^8-8*x^7+28*x^6-56*x^5+70*x^4-56*x^3+28*x^2-8*x+1)+1/1326*sqrt(-x^2+1)/(x^7-7*x^6+21*x^5-35*x^4+35*x^3-21*x^2+7*x-1)-1/2431*sqrt(-x^2+1)/(x^6-6*x^5+15*x^4-20*x^3+15*x^2-6*x+1)+5/21879*sqrt(-x^2+1)/(x^5-5*x^4+10*x^3-10*x^2+5*x-1)-20/153153*sqrt(-x^2+1)/(x^4-4*x^3+6*x^2-4*x+1)+4/51051*sqrt(-x^2+1)

)/(x³ - 3*x² + 3*x - 1) - 8/153153*sqrt(-x² + 1)/(x² - 2*x + 1) + 8/153153*sqrt(-x² + 1)/(x - 1)

mupad [B] time = 0.37, size = 140, normalized size = 1.16

$$\frac{\sqrt{1-x} \left(\frac{3765x\sqrt{x+1}}{17017} + \frac{13252\sqrt{x+1}}{153153} + \frac{24239x^2\sqrt{x+1}}{153153} + \frac{457x^3\sqrt{x+1}}{51051} - \frac{5x^4\sqrt{x+1}}{663} + \frac{236x^5\sqrt{x+1}}{51051} - \frac{292x^6\sqrt{x+1}}{153153} + \frac{8x^7\sqrt{x+1}}{17017} \right)}{x^9 - 9x^8 + 36x^7 - 84x^6 + 126x^5 - 126x^4 + 84x^3 - 36x^2 + 9x - 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^(5/2)/(1 - x)^(19/2), x)

[Out] -((1 - x)^(1/2)*((3765*x*(x + 1)^(1/2))/17017 + (13252*(x + 1)^(1/2))/153153 + (24239*x^2*(x + 1)^(1/2))/153153 + (457*x^3*(x + 1)^(1/2))/51051 - (5*x^4*(x + 1)^(1/2))/663 + (236*x^5*(x + 1)^(1/2))/51051 - (292*x^6*(x + 1)^(1/2))/153153 + (8*x^7*(x + 1)^(1/2))/17017 - (8*x^8*(x + 1)^(1/2))/153153))/ (9*x - 36*x^2 + 84*x^3 - 126*x^4 + 126*x^5 - 84*x^6 + 36*x^7 - 9*x^8 + x^9 - 1)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**(5/2)/(1-x)**(19/2), x)

[Out] Timed out

$$3.1104 \quad \int \frac{(1+ax)^{3/2}}{\sqrt{1-ax}} dx$$

Optimal. Leaf size=64

$$-\frac{\sqrt{1-ax}(ax+1)^{3/2}}{2a} - \frac{3\sqrt{1-ax}\sqrt{ax+1}}{2a} + \frac{3\sin^{-1}(ax)}{2a}$$

[Out] 3/2*arcsin(a*x)/a-1/2*(a*x+1)^(3/2)*(-a*x+1)^(1/2)/a-3/2*(-a*x+1)^(1/2)*(a*x+1)^(1/2)/a

Rubi [A] time = 0.01, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {50, 41, 216}

$$-\frac{\sqrt{1-ax}(ax+1)^{3/2}}{2a} - \frac{3\sqrt{1-ax}\sqrt{ax+1}}{2a} + \frac{3\sin^{-1}(ax)}{2a}$$

Antiderivative was successfully verified.

[In] Int[(1 + a*x)^(3/2)/Sqrt[1 - a*x],x]

[Out] (-3*Sqrt[1 - a*x]*Sqrt[1 + a*x])/(2*a) - (Sqrt[1 - a*x]*(1 + a*x)^(3/2))/(2*a) + (3*ArcSin[a*x])/(2*a)

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(1+ax)^{3/2}}{\sqrt{1-ax}} dx &= -\frac{\sqrt{1-ax}(1+ax)^{3/2}}{2a} + \frac{3}{2} \int \frac{\sqrt{1+ax}}{\sqrt{1-ax}} dx \\
&= -\frac{3\sqrt{1-ax}\sqrt{1+ax}}{2a} - \frac{\sqrt{1-ax}(1+ax)^{3/2}}{2a} + \frac{3}{2} \int \frac{1}{\sqrt{1-ax}\sqrt{1+ax}} dx \\
&= -\frac{3\sqrt{1-ax}\sqrt{1+ax}}{2a} - \frac{\sqrt{1-ax}(1+ax)^{3/2}}{2a} + \frac{3}{2} \int \frac{1}{\sqrt{1-a^2x^2}} dx \\
&= -\frac{3\sqrt{1-ax}\sqrt{1+ax}}{2a} - \frac{\sqrt{1-ax}(1+ax)^{3/2}}{2a} + \frac{3\sin^{-1}(ax)}{2a}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 47, normalized size = 0.73

$$-\frac{\sqrt{1-a^2x^2}(ax+4)+6\sin^{-1}\left(\frac{\sqrt{1-ax}}{\sqrt{2}}\right)}{2a}$$

Antiderivative was successfully verified.

[In] Integrate[(1 + a*x)^(3/2)/Sqrt[1 - a*x], x]

[Out] -1/2*((4 + a*x)*Sqrt[1 - a^2*x^2] + 6*ArcSin[Sqrt[1 - a*x]/Sqrt[2]])/a

fricas [A] time = 0.45, size = 55, normalized size = 0.86

$$-\frac{(ax+4)\sqrt{ax+1}\sqrt{-ax+1}+6\arctan\left(\frac{\sqrt{ax+1}\sqrt{-ax+1}-1}{ax}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+1)^(3/2)/(-a*x+1)^(1/2), x, algorithm="fricas")

[Out] -1/2*((a*x + 4)*sqrt(a*x + 1)*sqrt(-a*x + 1) + 6*arctan((sqrt(a*x + 1)*sqrt(-a*x + 1) - 1)/(a*x)))/a

giac [A] time = 0.70, size = 42, normalized size = 0.66

$$-\frac{(ax+4)\sqrt{ax+1}\sqrt{-ax+1}-6\arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{ax+1}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+1)^(3/2)/(-a*x+1)^(1/2), x, algorithm="giac")

[Out] $-1/2*((a*x + 4)*\sqrt{a*x + 1}*\sqrt{-a*x + 1} - 6*\arcsin(1/2*\sqrt{2}*\sqrt{a*x + 1}))/a$

maple [A] time = 0.01, size = 98, normalized size = 1.53

$$\frac{3\sqrt{(ax+1)(-ax+1)} \arctan\left(\frac{\sqrt{a^2}x}{\sqrt{-a^2x^2+1}}\right)}{2\sqrt{ax+1}\sqrt{-ax+1}\sqrt{a^2}} - \frac{(ax+1)^{3/2}\sqrt{-ax+1}}{2a} - \frac{3\sqrt{-ax+1}\sqrt{ax+1}}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a*x+1)^{(3/2)} / (-a*x+1)^{(1/2)}, x)$

[Out] $-1/2*(a*x+1)^{(3/2)}*(-a*x+1)^{(1/2)}/a - 3/2*(-a*x+1)^{(1/2)}*(a*x+1)^{(1/2)}/a + 3/2*((a*x+1)*(-a*x+1))^{(1/2)}/(a*x+1)^{(1/2)}/(-a*x+1)^{(1/2)}/(a^2)^{(1/2)}*\arctan((a^2)^{(1/2)}*x/(-a^2*x^2+1)^{(1/2)})$

maxima [A] time = 2.99, size = 42, normalized size = 0.66

$$-\frac{1}{2}\sqrt{-a^2x^2+1}x + \frac{3\arcsin(ax)}{2a} - \frac{2\sqrt{-a^2x^2+1}}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((a*x+1)^{(3/2)} / (-a*x+1)^{(1/2)}, x, \text{algorithm}="maxima")$

[Out] $-1/2*\sqrt{-a^2*x^2 + 1}*x + 3/2*\arcsin(a*x)/a - 2*\sqrt{-a^2*x^2 + 1}/a$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(ax+1)^{3/2}}{\sqrt{1-ax}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a*x + 1)^{(3/2)} / (1 - a*x)^{(1/2)}, x)$

[Out] $\text{int}((a*x + 1)^{(3/2)} / (1 - a*x)^{(1/2)}, x)$

sympy [A] time = 33.75, size = 75, normalized size = 1.17

$$\left\{ \begin{array}{l} 2 \left\{ \left(-\frac{ax\sqrt{-ax+1}\sqrt{ax+1}}{4} - \sqrt{-ax+1}\sqrt{ax+1} + \frac{3\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{ax+1}}{2}\right)}{2} \right) \right. \\ \left. \right\} \\ \hline a \end{array} \right. \begin{array}{l} \text{for } ax - 1 \geq -2 \wedge ax - 1 < 0 \\ \text{otherwise} \end{array}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a*x+1)**(3/2)/(-a*x+1)**(1/2),x)
```

```
[Out] Piecewise((2*Piecewise((-a*x*sqrt(-a*x + 1)*sqrt(a*x + 1)/4 - sqrt(-a*x + 1)
)*sqrt(a*x + 1) + 3*asin(sqrt(2)*sqrt(a*x + 1)/2)/2, (a*x - 1 >= -2) & (a*x
- 1 < 0)))/a, Ne(a, 0)), (x, True))
```

$$3.1105 \quad \int \frac{(1+ax)\sqrt{1-a^2x^2}}{1-ax} dx$$

Optimal. Leaf size=62

$$-\frac{(1-a^2x^2)^{3/2}}{2a(1-ax)} - \frac{3\sqrt{1-a^2x^2}}{2a} + \frac{3\sin^{-1}(ax)}{2a}$$

[Out] $-1/2*(-a^2*x^2+1)^{(3/2)}/a/(-a*x+1)+3/2*\arcsin(a*x)/a-3/2*(-a^2*x^2+1)^{(1/2)}/a$

Rubi [A] time = 0.03, antiderivative size = 62, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 28, $\frac{\text{number of rules}}{\text{integrand size}} = 0.107$, Rules used = {795, 665, 216}

$$-\frac{(1-a^2x^2)^{3/2}}{2a(1-ax)} - \frac{3\sqrt{1-a^2x^2}}{2a} + \frac{3\sin^{-1}(ax)}{2a}$$

Antiderivative was successfully verified.

[In] Int[((1 + a*x)*Sqrt[1 - a^2*x^2])/(1 - a*x), x]

[Out] $(-3*\text{Sqrt}[1 - a^2*x^2])/(2*a) - (1 - a^2*x^2)^{(3/2)}/(2*a*(1 - a*x)) + (3*\text{Arc Sin}[a*x])/(2*a)$

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 665

Int[((d_) + (e_.)*(x_))^(m_)*((a_) + (c_.)*(x_)^2)^(p_), x_Symbol] := Simp[((d + e*x)^(m + 1)*(a + c*x^2)^p)/(e*(m + 2*p + 1)), x] - Dist[(2*c*d*p)/(e^2*(m + 2*p + 1)), Int[(d + e*x)^(m + 1)*(a + c*x^2)^(p - 1), x], x] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 + a*e^2, 0] && GtQ[p, 0] && (LeQ[-2, m, 0] || EqQ[m + p + 1, 0]) && NeQ[m + 2*p + 1, 0] && IntegerQ[2*p]

Rule 795

Int[((d_) + (e_.)*(x_))^(m_)*((f_.) + (g_.)*(x_))*((a_) + (c_.)*(x_)^2)^(p_), x_Symbol] := Simp[(g*(d + e*x)^m*(a + c*x^2)^(p + 1))/(c*(m + 2*p + 2)), x] + Dist[(m*(d*g + e*f) + 2*e*f*(p + 1))/(e*(m + 2*p + 2)), Int[(d + e*x)^(m*(a + c*x^2)^p, x], x] /; FreeQ[{a, c, d, e, f, g, m, p}, x] && EqQ[c*d^2

+ a*e^2, 0] && NeQ[m + 2*p + 2, 0] && NeQ[m, 2]

Rubi steps

$$\begin{aligned} \int \frac{(1+ax)\sqrt{1-a^2x^2}}{1-ax} dx &= -\frac{(1-a^2x^2)^{3/2}}{2a(1-ax)} + \frac{3}{2} \int \frac{\sqrt{1-a^2x^2}}{1-ax} dx \\ &= -\frac{3\sqrt{1-a^2x^2}}{2a} - \frac{(1-a^2x^2)^{3/2}}{2a(1-ax)} + \frac{3}{2} \int \frac{1}{\sqrt{1-a^2x^2}} dx \\ &= -\frac{3\sqrt{1-a^2x^2}}{2a} - \frac{(1-a^2x^2)^{3/2}}{2a(1-ax)} + \frac{3 \sin^{-1}(ax)}{2a} \end{aligned}$$

Mathematica [A] time = 0.10, size = 91, normalized size = 1.47

$$\frac{\sqrt{1-a^2x^2} \left(6\sqrt{ax+1} \sin^{-1}\left(\frac{\sqrt{ax+1}}{\sqrt{2}}\right) - \sqrt{1-ax} (a^2x^2 + 5ax + 4) \right)}{2a\sqrt{1-ax}(ax+1)}$$

Antiderivative was successfully verified.

[In] Integrate[((1 + a*x)*Sqrt[1 - a^2*x^2])/(1 - a*x), x]

[Out] (Sqrt[1 - a^2*x^2]*(-(Sqrt[1 - a*x]*(4 + 5*a*x + a^2*x^2)) + 6*Sqrt[1 + a*x]*ArcSin[Sqrt[1 + a*x]/Sqrt[2]]))/(2*a*Sqrt[1 - a*x]*(1 + a*x))

fricas [A] time = 0.45, size = 48, normalized size = 0.77

$$-\frac{\sqrt{-a^2x^2+1}(ax+4) + 6 \arctan\left(\frac{\sqrt{-a^2x^2+1}-1}{ax}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+1)*(-a^2*x^2+1)^(1/2)/(-a*x+1), x, algorithm="fricas")

[Out] -1/2*(sqrt(-a^2*x^2 + 1)*(a*x + 4) + 6*arctan((sqrt(-a^2*x^2 + 1) - 1)/(a*x)))/a

giac [A] time = 0.70, size = 34, normalized size = 0.55

$$-\frac{1}{2} \sqrt{-a^2x^2+1} \left(x + \frac{4}{a} \right) + \frac{3 \arcsin(ax) \operatorname{sgn}(a)}{2|a|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+1)*(-a^2*x^2+1)^(1/2)/(-a*x+1),x, algorithm="giac")

[Out] -1/2*sqrt(-a^2*x^2 + 1)*(x + 4/a) + 3/2*arcsin(a*x)*sgn(a)/abs(a)

maple [B] time = 0.01, size = 118, normalized size = 1.90

$$-\frac{\sqrt{-a^2x^2+1}x}{2} + \frac{2 \arctan\left(\frac{\sqrt{a^2}x}{\sqrt{-(x-\frac{1}{a})^2a^2-2(x-\frac{1}{a})a}}\right)}{\sqrt{a^2}} - \frac{\arctan\left(\frac{\sqrt{a^2}x}{\sqrt{-a^2x^2+1}}\right)}{2\sqrt{a^2}} - \frac{2\sqrt{-(x-\frac{1}{a})^2a^2-2(x-\frac{1}{a})a}}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*x+1)*(-a^2*x^2+1)^(1/2)/(-a*x+1),x)

[Out] -1/2*x*(-a^2*x^2+1)^(1/2)-1/2/(a^2)^(1/2)*arctan((a^2)^(1/2)/(-a^2*x^2+1)^(1/2)*x)-2/a*(-(x-1/a)^2*a^2-2*(x-1/a)*a)^(1/2)+2/(a^2)^(1/2)*arctan((a^2)^(1/2)*x/(-(x-1/a)^2*a^2-2*(x-1/a)*a)^(1/2))

maxima [A] time = 3.03, size = 42, normalized size = 0.68

$$-\frac{1}{2}\sqrt{-a^2x^2+1}x + \frac{3 \arcsin(ax)}{2a} - \frac{2\sqrt{-a^2x^2+1}}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+1)*(-a^2*x^2+1)^(1/2)/(-a*x+1),x, algorithm="maxima")

[Out] -1/2*sqrt(-a^2*x^2 + 1)*x + 3/2*arcsin(a*x)/a - 2*sqrt(-a^2*x^2 + 1)/a

mupad [B] time = 0.15, size = 55, normalized size = 0.89

$$\frac{\frac{3 \operatorname{asinh}\left(x\sqrt{-a^2}\right)}{2} + \sqrt{1-a^2x^2} \left(\frac{2a}{\sqrt{-a^2}} - \frac{x\sqrt{-a^2}}{2}\right)}{\sqrt{-a^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-((1 - a^2*x^2)^(1/2)*(a*x + 1))/(a*x - 1),x)

[Out] ((3*asinh(x*(-a^2)^(1/2)))/2 + (1 - a^2*x^2)^(1/2)*((2*a)/(-a^2)^(1/2) - (x*(-a^2)^(1/2))/2))/(-a^2)^(1/2)

sympy [A] time = 7.08, size = 76, normalized size = 1.23

$$-\left\{ \frac{-\sqrt{-a^2x^2+1} + \operatorname{asin}(ax)}{a} \quad \text{for } ax > -1 \wedge ax < 1 \right\} - \left\{ \frac{-\frac{ax\sqrt{-a^2x^2+1}}{2} - \sqrt{-a^2x^2+1} + \frac{\operatorname{asin}(ax)}{2}}{a} \quad \text{for } ax > -1 \wedge ax < 1 \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+1)*(-a**2*x**2+1)**(1/2)/(-a*x+1), x)

[Out] -Piecewise((-(-sqrt(-a**2*x**2 + 1) + asin(a*x))/a, (a*x > -1) & (a*x < 1))
) - Piecewise((-(-a*x*sqrt(-a**2*x**2 + 1)/2 - sqrt(-a**2*x**2 + 1) + asin(a*x)/2)/a, (a*x > -1) & (a*x < 1)))

$$3.1106 \quad \int \frac{(1-x)^{7/2}}{\sqrt{1+x}} dx$$

Optimal. Leaf size=87

$$\frac{1}{4}\sqrt{x+1}(1-x)^{7/2} + \frac{7}{12}\sqrt{x+1}(1-x)^{5/2} + \frac{35}{24}\sqrt{x+1}(1-x)^{3/2} + \frac{35}{8}\sqrt{x+1}\sqrt{1-x} + \frac{35}{8}\sin^{-1}(x)$$

[Out] 35/8*arcsin(x)+35/24*(1-x)^(3/2)*(1+x)^(1/2)+7/12*(1-x)^(5/2)*(1+x)^(1/2)+1/4*(1-x)^(7/2)*(1+x)^(1/2)+35/8*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.02, antiderivative size = 87, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {50, 41, 216}

$$\frac{1}{4}\sqrt{x+1}(1-x)^{7/2} + \frac{7}{12}\sqrt{x+1}(1-x)^{5/2} + \frac{35}{24}\sqrt{x+1}(1-x)^{3/2} + \frac{35}{8}\sqrt{x+1}\sqrt{1-x} + \frac{35}{8}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(7/2)/Sqrt[1 + x], x]

[Out] (35*Sqrt[1 - x]*Sqrt[1 + x])/8 + (35*(1 - x)^(3/2)*Sqrt[1 + x])/24 + (7*(1 - x)^(5/2)*Sqrt[1 + x])/12 + ((1 - x)^(7/2)*Sqrt[1 + x])/4 + (35*ArcSin[x])/8

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(1-x)^{7/2}}{\sqrt{1+x}} dx &= \frac{1}{4}(1-x)^{7/2}\sqrt{1+x} + \frac{7}{4} \int \frac{(1-x)^{5/2}}{\sqrt{1+x}} dx \\
&= \frac{7}{12}(1-x)^{5/2}\sqrt{1+x} + \frac{1}{4}(1-x)^{7/2}\sqrt{1+x} + \frac{35}{12} \int \frac{(1-x)^{3/2}}{\sqrt{1+x}} dx \\
&= \frac{35}{24}(1-x)^{3/2}\sqrt{1+x} + \frac{7}{12}(1-x)^{5/2}\sqrt{1+x} + \frac{1}{4}(1-x)^{7/2}\sqrt{1+x} + \frac{35}{8} \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx \\
&= \frac{35}{8}\sqrt{1-x}\sqrt{1+x} + \frac{35}{24}(1-x)^{3/2}\sqrt{1+x} + \frac{7}{12}(1-x)^{5/2}\sqrt{1+x} + \frac{1}{4}(1-x)^{7/2}\sqrt{1+x} + \frac{35}{8} \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx \\
&= \frac{35}{8}\sqrt{1-x}\sqrt{1+x} + \frac{35}{24}(1-x)^{3/2}\sqrt{1+x} + \frac{7}{12}(1-x)^{5/2}\sqrt{1+x} + \frac{1}{4}(1-x)^{7/2}\sqrt{1+x} + \frac{35}{8} \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right)
\end{aligned}$$

Mathematica [A] time = 0.02, size = 61, normalized size = 0.70

$$\frac{\sqrt{x+1} (6x^4 - 38x^3 + 113x^2 - 241x + 160)}{24\sqrt{1-x}} - \frac{35}{4} \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(7/2)/Sqrt[1 + x], x]

[Out] (Sqrt[1 + x]*(160 - 241*x + 113*x^2 - 38*x^3 + 6*x^4))/(24*Sqrt[1 - x]) - (35*ArcSin[Sqrt[1 - x]/Sqrt[2]])/4

fricas [A] time = 0.45, size = 52, normalized size = 0.60

$$-\frac{1}{24} (6x^3 - 32x^2 + 81x - 160)\sqrt{x+1}\sqrt{-x+1} - \frac{35}{4} \arctan \left(\frac{\sqrt{x+1}\sqrt{-x+1} - 1}{x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)/(1+x)^(1/2), x, algorithm="fricas")

[Out] -1/24*(6*x^3 - 32*x^2 + 81*x - 160)*sqrt(x + 1)*sqrt(-x + 1) - 35/4*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [A] time = 0.76, size = 101, normalized size = 1.16

$$-\frac{1}{24} ((2(3x - 10)(x + 1) + 43)(x + 1) - 39)\sqrt{x+1}\sqrt{-x+1} + \frac{1}{2} ((2x - 5)(x + 1) + 9)\sqrt{x+1}\sqrt{-x+1} - \frac{3}{2} \sqrt{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)/(1+x)^(1/2),x, algorithm="giac")

[Out] -1/24*((2*(3*x - 10)*(x + 1) + 43)*(x + 1) - 39)*sqrt(x + 1)*sqrt(-x + 1) + 1/2*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) - 3/2*sqrt(x + 1)*(x - 2)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + 35/4*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.01, size = 85, normalized size = 0.98

$$\frac{35\sqrt{(x+1)(-x+1)} \arcsin(x)}{8\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{7}{2}}\sqrt{x+1}}{4} + \frac{7(-x+1)^{\frac{5}{2}}\sqrt{x+1}}{12} + \frac{35(-x+1)^{\frac{3}{2}}\sqrt{x+1}}{24} + \frac{35\sqrt{-x+1}\sqrt{x+1}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(7/2)/(x+1)^(1/2),x)

[Out] 1/4*(-x+1)^(7/2)*(x+1)^(1/2)+7/12*(-x+1)^(5/2)*(x+1)^(1/2)+35/24*(-x+1)^(3/2)*(x+1)^(1/2)+35/8*(-x+1)^(1/2)*(x+1)^(1/2)+35/8*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.99, size = 56, normalized size = 0.64

$$-\frac{1}{4}\sqrt{-x^2+1}x^3 + \frac{4}{3}\sqrt{-x^2+1}x^2 - \frac{27}{8}\sqrt{-x^2+1}x + \frac{20}{3}\sqrt{-x^2+1} + \frac{35}{8}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)/(1+x)^(1/2),x, algorithm="maxima")

[Out] -1/4*sqrt(-x^2 + 1)*x^3 + 4/3*sqrt(-x^2 + 1)*x^2 - 27/8*sqrt(-x^2 + 1)*x + 20/3*sqrt(-x^2 + 1) + 35/8*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(1-x)^{7/2}}{\sqrt{x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(7/2)/(x + 1)^(1/2),x)

[Out] int((1 - x)^(7/2)/(x + 1)^(1/2), x)

sympy [A] time = 14.68, size = 201, normalized size = 2.31

$$\left\{ \begin{array}{ll} -\frac{35i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} - \frac{i(x+1)^{\frac{9}{2}}}{4\sqrt{x-1}} + \frac{31i(x+1)^{\frac{7}{2}}}{12\sqrt{x-1}} - \frac{263i(x+1)^{\frac{5}{2}}}{24\sqrt{x-1}} + \frac{605i(x+1)^{\frac{3}{2}}}{24\sqrt{x-1}} - \frac{93i\sqrt{x+1}}{4\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ -\frac{\sqrt{1-x}(x+1)^{\frac{7}{2}}}{4} + \frac{25\sqrt{1-x}(x+1)^{\frac{5}{2}}}{12} - \frac{163\sqrt{1-x}(x+1)^{\frac{3}{2}}}{24} + \frac{93\sqrt{1-x}\sqrt{x+1}}{8} + \frac{35 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right)}{4} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(7/2)/(1+x)**(1/2), x)

[Out] Piecewise((-35*I*acosh(sqrt(2)*sqrt(x + 1)/2)/4 - I*(x + 1)**(9/2)/(4*sqrt(x - 1)) + 31*I*(x + 1)**(7/2)/(12*sqrt(x - 1)) - 263*I*(x + 1)**(5/2)/(24*sqrt(x - 1)) + 605*I*(x + 1)**(3/2)/(24*sqrt(x - 1)) - 93*I*sqrt(x + 1)/(4*sqrt(x - 1)), Abs(x + 1)/2 > 1), (-sqrt(1 - x)*(x + 1)**(7/2)/4 + 25*sqrt(1 - x)*(x + 1)**(5/2)/12 - 163*sqrt(1 - x)*(x + 1)**(3/2)/24 + 93*sqrt(1 - x)*sqrt(x + 1)/8 + 35*asin(sqrt(2)*sqrt(x + 1)/2)/4, True))

$$3.1107 \quad \int \frac{(1-x)^{5/2}}{\sqrt{1+x}} dx$$

Optimal. Leaf size=67

$$\frac{1}{3}\sqrt{x+1}(1-x)^{5/2} + \frac{5}{6}\sqrt{x+1}(1-x)^{3/2} + \frac{5}{2}\sqrt{x+1}\sqrt{1-x} + \frac{5}{2}\sin^{-1}(x)$$

[Out] 5/2*arcsin(x)+5/6*(1-x)^(3/2)*(1+x)^(1/2)+1/3*(1-x)^(5/2)*(1+x)^(1/2)+5/2*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {50, 41, 216}

$$\frac{1}{3}\sqrt{x+1}(1-x)^{5/2} + \frac{5}{6}\sqrt{x+1}(1-x)^{3/2} + \frac{5}{2}\sqrt{x+1}\sqrt{1-x} + \frac{5}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(5/2)/Sqrt[1 + x], x]

[Out] (5*Sqrt[1 - x]*Sqrt[1 + x])/2 + (5*(1 - x)^(3/2)*Sqrt[1 + x])/6 + ((1 - x)^(5/2)*Sqrt[1 + x])/3 + (5*ArcSin[x])/2

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(1-x)^{5/2}}{\sqrt{1+x}} dx &= \frac{1}{3}(1-x)^{5/2}\sqrt{1+x} + \frac{5}{3} \int \frac{(1-x)^{3/2}}{\sqrt{1+x}} dx \\
&= \frac{5}{6}(1-x)^{3/2}\sqrt{1+x} + \frac{1}{3}(1-x)^{5/2}\sqrt{1+x} + \frac{5}{2} \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx \\
&= \frac{5}{2}\sqrt{1-x}\sqrt{1+x} + \frac{5}{6}(1-x)^{3/2}\sqrt{1+x} + \frac{1}{3}(1-x)^{5/2}\sqrt{1+x} + \frac{5}{2} \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
&= \frac{5}{2}\sqrt{1-x}\sqrt{1+x} + \frac{5}{6}(1-x)^{3/2}\sqrt{1+x} + \frac{1}{3}(1-x)^{5/2}\sqrt{1+x} + \frac{5}{2} \int \frac{1}{\sqrt{1-x^2}} dx \\
&= \frac{5}{2}\sqrt{1-x}\sqrt{1+x} + \frac{5}{6}(1-x)^{3/2}\sqrt{1+x} + \frac{1}{3}(1-x)^{5/2}\sqrt{1+x} + \frac{5}{2} \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.03, size = 54, normalized size = 0.81

$$\frac{\sqrt{x+1}(-2x^3 + 11x^2 - 31x + 22)}{6\sqrt{1-x}} - 5 \sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(5/2)/Sqrt[1 + x], x]

[Out] (Sqrt[1 + x]*(22 - 31*x + 11*x^2 - 2*x^3))/(6*Sqrt[1 - x]) - 5*ArcSin[Sqrt[1 - x]/Sqrt[2]]

fricas [A] time = 0.44, size = 47, normalized size = 0.70

$$\frac{1}{6}(2x^2 - 9x + 22)\sqrt{x+1}\sqrt{-x+1} - 5 \arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1} - 1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)/(1+x)^(1/2), x, algorithm="fricas")

[Out] 1/6*(2*x^2 - 9*x + 22)*sqrt(x + 1)*sqrt(-x + 1) - 5*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [A] time = 0.70, size = 69, normalized size = 1.03

$$\frac{1}{6}((2x - 5)(x + 1) + 9)\sqrt{x+1}\sqrt{-x+1} - \sqrt{x+1}(x - 2)\sqrt{-x+1} + \sqrt{x+1}\sqrt{-x+1} + 5 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)/(1+x)^(1/2),x, algorithm="giac")

[Out] 1/6*((2*x - 5)*(x + 1) + 9)*sqrt(x + 1)*sqrt(-x + 1) - sqrt(x + 1)*(x - 2)*sqrt(-x + 1) + sqrt(x + 1)*sqrt(-x + 1) + 5*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.00, size = 71, normalized size = 1.06

$$\frac{5\sqrt{(x+1)(-x+1)} \arcsin(x)}{2\sqrt{x+1}\sqrt{-x+1}} + \frac{(-x+1)^{\frac{5}{2}}\sqrt{x+1}}{3} + \frac{5(-x+1)^{\frac{3}{2}}\sqrt{x+1}}{6} + \frac{5\sqrt{-x+1}\sqrt{x+1}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(5/2)/(x+1)^(1/2),x)

[Out] 1/3*(-x+1)^(5/2)*(x+1)^(1/2)+5/6*(-x+1)^(3/2)*(x+1)^(1/2)+5/2*(-x+1)^(1/2)*(x+1)^(1/2)+5/2*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.90, size = 42, normalized size = 0.63

$$\frac{1}{3}\sqrt{-x^2+1}x^2 - \frac{3}{2}\sqrt{-x^2+1}x + \frac{11}{3}\sqrt{-x^2+1} + \frac{5}{2}\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)/(1+x)^(1/2),x, algorithm="maxima")

[Out] 1/3*sqrt(-x^2 + 1)*x^2 - 3/2*sqrt(-x^2 + 1)*x + 11/3*sqrt(-x^2 + 1) + 5/2*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(1-x)^{5/2}}{\sqrt{x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(5/2)/(x + 1)^(1/2),x)

[Out] int((1 - x)^(5/2)/(x + 1)^(1/2), x)

sympy [A] time = 5.64, size = 175, normalized size = 2.61

$$\begin{cases} -5i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{i(x+1)^{\frac{7}{2}}}{3\sqrt{x-1}} - \frac{17i(x+1)^{\frac{5}{2}}}{6\sqrt{x-1}} + \frac{59i(x+1)^{\frac{3}{2}}}{6\sqrt{x-1}} - \frac{11i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ 5 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{(x+1)^{\frac{7}{2}}}{3\sqrt{1-x}} + \frac{17(x+1)^{\frac{5}{2}}}{6\sqrt{1-x}} - \frac{59(x+1)^{\frac{3}{2}}}{6\sqrt{1-x}} + \frac{11\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((1-x)**(5/2)/(1+x)**(1/2),x)
```

```
[Out] Piecewise((-5*I*acosh(sqrt(2)*sqrt(x + 1)/2) + I*(x + 1)**(7/2)/(3*sqrt(x - 1)) - 17*I*(x + 1)**(5/2)/(6*sqrt(x - 1)) + 59*I*(x + 1)**(3/2)/(6*sqrt(x - 1)) - 11*I*sqrt(x + 1)/sqrt(x - 1), Abs(x + 1)/2 > 1), (5*asin(sqrt(2)*sqrt(x + 1)/2) - (x + 1)**(7/2)/(3*sqrt(1 - x)) + 17*(x + 1)**(5/2)/(6*sqrt(1 - x)) - 59*(x + 1)**(3/2)/(6*sqrt(1 - x)) + 11*sqrt(x + 1)/sqrt(1 - x), True))
```

3.1108

$$\int \frac{(1-x)^{3/2}}{\sqrt{1+x}} dx$$

Optimal. Leaf size=47

$$\frac{1}{2}\sqrt{x+1}(1-x)^{3/2} + \frac{3}{2}\sqrt{x+1}\sqrt{1-x} + \frac{3}{2}\sin^{-1}(x)$$

[Out] 3/2*arcsin(x)+1/2*(1-x)^(3/2)*(1+x)^(1/2)+3/2*(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {50, 41, 216}

$$\frac{1}{2}\sqrt{x+1}(1-x)^{3/2} + \frac{3}{2}\sqrt{x+1}\sqrt{1-x} + \frac{3}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(3/2)/Sqrt[1 + x], x]

[Out] (3*Sqrt[1 - x]*Sqrt[1 + x])/2 + ((1 - x)^(3/2)*Sqrt[1 + x])/2 + (3*ArcSin[x])/2

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(1-x)^{3/2}}{\sqrt{1+x}} dx &= \frac{1}{2}(1-x)^{3/2}\sqrt{1+x} + \frac{3}{2} \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx \\
&= \frac{3}{2}\sqrt{1-x}\sqrt{1+x} + \frac{1}{2}(1-x)^{3/2}\sqrt{1+x} + \frac{3}{2} \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
&= \frac{3}{2}\sqrt{1-x}\sqrt{1+x} + \frac{1}{2}(1-x)^{3/2}\sqrt{1+x} + \frac{3}{2} \int \frac{1}{\sqrt{1-x^2}} dx \\
&= \frac{3}{2}\sqrt{1-x}\sqrt{1+x} + \frac{1}{2}(1-x)^{3/2}\sqrt{1+x} + \frac{3}{2} \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.02, size = 47, normalized size = 1.00

$$\frac{\sqrt{x+1}(x^2-5x+4)}{2\sqrt{1-x}} - 3 \sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(3/2)/Sqrt[1 + x], x]

[Out] (Sqrt[1 + x]*(4 - 5*x + x^2))/(2*Sqrt[1 - x]) - 3*ArcSin[Sqrt[1 - x]/Sqrt[2]]

fricas [A] time = 0.45, size = 40, normalized size = 0.85

$$-\frac{1}{2}\sqrt{x+1}(x-4)\sqrt{-x+1} - 3 \arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)/(1+x)^(1/2), x, algorithm="fricas")

[Out] -1/2*sqrt(x + 1)*(x - 4)*sqrt(-x + 1) - 3*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [A] time = 0.70, size = 44, normalized size = 0.94

$$-\frac{1}{2}\sqrt{x+1}(x-2)\sqrt{-x+1} + \sqrt{x+1}\sqrt{-x+1} + 3 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)/(1+x)^(1/2), x, algorithm="giac")

[Out] $-1/2*\sqrt{x+1}*(x-2)*\sqrt{-x+1} + \sqrt{x+1}*\sqrt{-x+1} + 3*\arcsin(1/2*\sqrt{2}*\sqrt{x+1})$

maple [A] time = 0.00, size = 57, normalized size = 1.21

$$\frac{3\sqrt{(x+1)(-x+1)} \arcsin(x)}{2\sqrt{x+1} \sqrt{-x+1}} + \frac{(-x+1)^{\frac{3}{2}} \sqrt{x+1}}{2} + \frac{3\sqrt{-x+1} \sqrt{x+1}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((-x+1)^{(3/2)}/(x+1)^{(1/2)}, x)$

[Out] $1/2*(-x+1)^{(3/2)}*(x+1)^{(1/2)}+3/2*(-x+1)^{(1/2)}*(x+1)^{(1/2)}+3/2*((x+1)*(-x+1))^{(1/2)}/(x+1)^{(1/2)}/(-x+1)^{(1/2)}*\arcsin(x)$

maxima [A] time = 3.02, size = 28, normalized size = 0.60

$$-\frac{1}{2} \sqrt{-x^2+1} x + 2 \sqrt{-x^2+1} + \frac{3}{2} \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((1-x)^{(3/2)}/(1+x)^{(1/2)}, x, \text{algorithm}="maxima")$

[Out] $-1/2*\sqrt{-x^2+1}*x + 2*\sqrt{-x^2+1} + 3/2*\arcsin(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(1-x)^{3/2}}{\sqrt{x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((1-x)^{(3/2)}/(x+1)^{(1/2)}, x)$

[Out] $\text{int}((1-x)^{(3/2)}/(x+1)^{(1/2)}, x)$

sympy [A] time = 2.59, size = 139, normalized size = 2.96

$$\begin{cases} -3i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{i(x+1)^{\frac{5}{2}}}{2\sqrt{x-1}} + \frac{7i(x+1)^{\frac{3}{2}}}{2\sqrt{x-1}} - \frac{5i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ 3 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{(x+1)^{\frac{5}{2}}}{2\sqrt{1-x}} - \frac{7(x+1)^{\frac{3}{2}}}{2\sqrt{1-x}} + \frac{5\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((1-x)**(3/2)/(1+x)**(1/2),x)
```

```
[Out] Piecewise((-3*I*acosh(sqrt(2)*sqrt(x + 1)/2) - I*(x + 1)**(5/2)/(2*sqrt(x - 1)) + 7*I*(x + 1)**(3/2)/(2*sqrt(x - 1)) - 5*I*sqrt(x + 1)/sqrt(x - 1), Abs(x + 1)/2 > 1), (3*asin(sqrt(2)*sqrt(x + 1)/2) + (x + 1)**(5/2)/(2*sqrt(1 - x)) - 7*(x + 1)**(3/2)/(2*sqrt(1 - x)) + 5*sqrt(x + 1)/sqrt(1 - x), True)
```

$$3.1109 \quad \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx$$

Optimal. Leaf size=20

$$\sqrt{1-x} \sqrt{x+1} + \sin^{-1}(x)$$

[Out] arcsin(x)+(1-x)^(1/2)*(1+x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {50, 41, 216}

$$\sqrt{1-x} \sqrt{x+1} + \sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[1 - x]/Sqrt[1 + x],x]

[Out] Sqrt[1 - x]*Sqrt[1 + x] + ArcSin[x]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}\int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx &= \sqrt{1-x} \sqrt{1+x} + \int \frac{1}{\sqrt{1-x} \sqrt{1+x}} dx \\ &= \sqrt{1-x} \sqrt{1+x} + \int \frac{1}{\sqrt{1-x^2}} dx \\ &= \sqrt{1-x} \sqrt{1+x} + \sin^{-1}(x)\end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.50

$$\sqrt{1-x^2} - 2 \sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 - x]/Sqrt[1 + x], x]

[Out] Sqrt[1 - x^2] - 2*ArcSin[Sqrt[1 - x]/Sqrt[2]]

fricas [B] time = 0.43, size = 36, normalized size = 1.80

$$\sqrt{x+1} \sqrt{-x+1} - 2 \arctan\left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)/(1+x)^(1/2), x, algorithm="fricas")

[Out] sqrt(x + 1)*sqrt(-x + 1) - 2*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [A] time = 0.65, size = 27, normalized size = 1.35

$$\sqrt{x+1} \sqrt{-x+1} + 2 \arcsin\left(\frac{1}{2} \sqrt{2} \sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)/(1+x)^(1/2), x, algorithm="giac")

[Out] sqrt(x + 1)*sqrt(-x + 1) + 2*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.00, size = 41, normalized size = 2.05

$$\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1} \sqrt{-x+1}} + \sqrt{-x+1} \sqrt{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-x+1)^(1/2)/(x+1)^(1/2),x)`

[Out] `(-x+1)^(1/2)*(x+1)^(1/2)+((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)`

maxima [A] time = 3.10, size = 12, normalized size = 0.60

$$\sqrt{-x^2 + 1} + \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(1/2)/(1+x)^(1/2),x, algorithm="maxima")`

[Out] `sqrt(-x^2 + 1) + arcsin(x)`

mupad [B] time = 0.12, size = 12, normalized size = 0.60

$$\operatorname{asin}(x) + \sqrt{1 - x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(1/2)/(x + 1)^(1/2),x)`

[Out] `asin(x) + (1 - x^2)^(1/2)`

sympy [B] time = 1.55, size = 100, normalized size = 5.00

$$\begin{cases} -2i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{i(x+1)^{\frac{3}{2}}}{\sqrt{x-1}} - \frac{2i\sqrt{x+1}}{\sqrt{x-1}} & \text{for } \frac{|x+1|}{2} > 1 \\ 2 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{(x+1)^{\frac{3}{2}}}{\sqrt{1-x}} + \frac{2\sqrt{x+1}}{\sqrt{1-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(1/2)/(1+x)**(1/2),x)`

[Out] `Piecewise((-2*I*acosh(sqrt(2)*sqrt(x + 1)/2) + I*(x + 1)**(3/2)/sqrt(x - 1) - 2*I*sqrt(x + 1)/sqrt(x - 1), Abs(x + 1)/2 > 1), (2*asin(sqrt(2)*sqrt(x + 1)/2) - (x + 1)**(3/2)/sqrt(1 - x) + 2*sqrt(x + 1)/sqrt(1 - x), True))`

$$3.1110 \quad \int \frac{1}{\sqrt{1-x} \sqrt{1+x}} dx$$

Optimal. Leaf size=2

$$\sin^{-1}(x)$$

[Out] arcsin(x)

Rubi [A] time = 0.00, antiderivative size = 2, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {41, 216}

$$\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[1 - x]*Sqrt[1 + x]),x]

[Out] ArcSin[x]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\int \frac{1}{\sqrt{1-x} \sqrt{1+x}} dx = \int \frac{1}{\sqrt{1-x^2}} dx = \sin^{-1}(x)$$

Mathematica [A] time = 0.00, size = 2, normalized size = 1.00

$$\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[1 - x]*Sqrt[1 + x]),x]

[Out] ArcSin[x]

fricas [B] time = 0.45, size = 22, normalized size = 11.00

$$-2 \arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(1/2)/(1+x)^(1/2),x, algorithm="fricas")

[Out] -2*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x)

giac [B] time = 0.65, size = 13, normalized size = 6.50

$$2 \arcsin\left(\frac{1}{2} \sqrt{2} \sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(1/2)/(1+x)^(1/2),x, algorithm="giac")

[Out] 2*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.00, size = 27, normalized size = 13.50

$$\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1} \sqrt{-x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+1)^(1/2)/(x+1)^(1/2),x)

[Out] ((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.95, size = 2, normalized size = 1.00

$$\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(1/2)/(1+x)^(1/2),x, algorithm="maxima")

[Out] arcsin(x)

mupad [B] time = 0.08, size = 22, normalized size = 11.00

$$-4 \operatorname{atan}\left(\frac{\sqrt{1-x}-1}{\sqrt{x+1}-1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((1 - x)^(1/2)*(x + 1)^(1/2)), x)`

[Out] `-4*atan(((1 - x)^(1/2) - 1)/((x + 1)^(1/2) - 1))`

sympy [B] time = 1.04, size = 41, normalized size = 20.50

$$\begin{cases} -2i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) & \text{for } \frac{|x+1|}{2} > 1 \\ 2 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)**(1/2)/(1+x)**(1/2), x)`

[Out] `Piecewise((-2*I*acosh(sqrt(2)*sqrt(x + 1)/2), Abs(x + 1)/2 > 1), (2*asin(sqrt(2)*sqrt(x + 1)/2), True))`

$$3.1111 \quad \int \frac{1}{(1-x)^{3/2} \sqrt{1+x}} dx$$

Optimal. Leaf size=17

$$\frac{\sqrt{x+1}}{\sqrt{1-x}}$$

[Out] $(1+x)^{(1/2)}/(1-x)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {37}

$$\frac{\sqrt{x+1}}{\sqrt{1-x}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - x)^(3/2)*Sqrt[1 + x]),x]

[Out] Sqrt[1 + x]/Sqrt[1 - x]

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(1-x)^{3/2} \sqrt{1+x}} dx = \frac{\sqrt{1+x}}{\sqrt{1-x}}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{\sqrt{x+1}}{\sqrt{1-x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1 - x)^(3/2)*Sqrt[1 + x]),x]

[Out] Sqrt[1 + x]/Sqrt[1 - x]

fricas [A] time = 0.44, size = 23, normalized size = 1.35

$$\frac{x - \sqrt{x+1}\sqrt{-x+1} - 1}{x-1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(3/2)/(1+x)^(1/2),x, algorithm="fricas")

[Out] (x - sqrt(x + 1)*sqrt(-x + 1) - 1)/(x - 1)

giac [A] time = 0.68, size = 19, normalized size = 1.12

$$-\frac{\sqrt{x+1}\sqrt{-x+1}}{x-1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(3/2)/(1+x)^(1/2),x, algorithm="giac")

[Out] -sqrt(x + 1)*sqrt(-x + 1)/(x - 1)

maple [A] time = 0.00, size = 14, normalized size = 0.82

$$\frac{\sqrt{x+1}}{\sqrt{-x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+1)^(3/2)/(x+1)^(1/2),x)

[Out] (x+1)^(1/2)/(-x+1)^(1/2)

maxima [A] time = 2.98, size = 16, normalized size = 0.94

$$-\frac{\sqrt{-x^2+1}}{x-1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(3/2)/(1+x)^(1/2),x, algorithm="maxima")

[Out] -sqrt(-x^2 + 1)/(x - 1)

mupad [B] time = 0.28, size = 13, normalized size = 0.76

$$\frac{\sqrt{x+1}}{\sqrt{1-x}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((1 - x)^(3/2)*(x + 1)^(1/2)),x)
```

```
[Out] (x + 1)^(1/2)/(1 - x)^(1/2)
```

sympy [A] time = 0.94, size = 29, normalized size = 1.71

$$\begin{cases} \frac{1}{\sqrt{-1+\frac{2}{x+1}}} & \text{for } \frac{2}{|x+1|} > 1 \\ -\frac{i}{\sqrt{1-\frac{2}{x+1}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(1-x)**(3/2)/(1+x)**(1/2),x)
```

```
[Out] Piecewise((1/sqrt(-1 + 2/(x + 1))), 2/Abs(x + 1) > 1), (-I/sqrt(1 - 2/(x + 1))), True))
```

$$3.1112 \quad \int \frac{1}{(1-x)^{5/2} \sqrt{1+x}} dx$$

Optimal. Leaf size=41

$$\frac{\sqrt{x+1}}{3\sqrt{1-x}} + \frac{\sqrt{x+1}}{3(1-x)^{3/2}}$$

[Out] 1/3*(1+x)^(1/2)/(1-x)^(3/2)+1/3*(1+x)^(1/2)/(1-x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{\sqrt{x+1}}{3\sqrt{1-x}} + \frac{\sqrt{x+1}}{3(1-x)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((1-x)^(5/2)*Sqrt[1+x]),x]

[Out] Sqrt[1+x]/(3*(1-x)^(3/2)) + Sqrt[1+x]/(3*Sqrt[1-x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(1-x)^{5/2}\sqrt{1+x}} dx = \frac{\sqrt{1+x}}{3(1-x)^{3/2}} + \frac{1}{3} \int \frac{1}{(1-x)^{3/2}\sqrt{1+x}} dx$$

$$= \frac{\sqrt{1+x}}{3(1-x)^{3/2}} + \frac{\sqrt{1+x}}{3\sqrt{1-x}}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.56

$$-\frac{(x-2)\sqrt{x+1}}{3(1-x)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(5/2)*Sqrt[1+x]),x]

[Out] -1/3*((-2+x)*Sqrt[1+x])/(1-x)^(3/2)

fricas [A] time = 0.46, size = 39, normalized size = 0.95

$$\frac{2x^2 - \sqrt{x+1}(x-2)\sqrt{-x+1} - 4x + 2}{3(x^2 - 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(5/2)/(1+x)^(1/2),x, algorithm="fricas")

[Out] 1/3*(2*x^2 - sqrt(x+1)*(x-2)*sqrt(-x+1) - 4*x + 2)/(x^2 - 2*x + 1)

giac [A] time = 0.64, size = 22, normalized size = 0.54

$$-\frac{\sqrt{x+1}(x-2)\sqrt{-x+1}}{3(x-1)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(5/2)/(1+x)^(1/2),x, algorithm="giac")

[Out] -1/3*sqrt(x+1)*(x-2)*sqrt(-x+1)/(x-1)^2

maple [A] time = 0.00, size = 18, normalized size = 0.44

$$-\frac{\sqrt{x+1}(x-2)}{3(-x+1)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-x+1)^(5/2)/(x+1)^(1/2),x)`

[Out] $-1/3*(x+1)^{(1/2)*(-2+x)/(-x+1)^{(3/2)}$

maxima [A] time = 3.12, size = 38, normalized size = 0.93

$$\frac{\sqrt{-x^2+1}}{3(x^2-2x+1)} - \frac{\sqrt{-x^2+1}}{3(x-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(5/2)/(1+x)^(1/2),x, algorithm="maxima")`

[Out] $1/3*\text{sqrt}(-x^2+1)/(x^2-2*x+1) - 1/3*\text{sqrt}(-x^2+1)/(x-1)$

mupad [B] time = 0.31, size = 43, normalized size = 1.05

$$\frac{x\sqrt{1-x} + 2\sqrt{1-x} - x^2\sqrt{1-x}}{3(x-1)^2\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((1-x)^(5/2)*(x+1)^(1/2)),x)`

[Out] $(x*(1-x)^{(1/2)} + 2*(1-x)^{(1/2)} - x^2*(1-x)^{(1/2)})/(3*(x-1)^2*(x+1)^{(1/2)})$

sympy [C] time = 2.25, size = 139, normalized size = 3.39

$$\begin{cases} \frac{i(x+1)}{3i\sqrt{-1+\frac{2}{x+1}}(x+1)-6i\sqrt{-1+\frac{2}{x+1}}} - \frac{3i}{3i\sqrt{-1+\frac{2}{x+1}}(x+1)-6i\sqrt{-1+\frac{2}{x+1}}} & \text{for } \frac{2}{|x+1|} > 1 \\ -\frac{x+1}{-3i\sqrt{1-\frac{2}{x+1}}(x+1)+6i\sqrt{1-\frac{2}{x+1}}} + \frac{3}{-3i\sqrt{1-\frac{2}{x+1}}(x+1)+6i\sqrt{1-\frac{2}{x+1}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)**(5/2)/(1+x)**(1/2),x)`

[Out] `Piecewise((I*(x+1)/(3*I*sqrt(-1+2/(x+1))*(x+1)-6*I*sqrt(-1+2/(x+1))) - 3*I/(3*I*sqrt(-1+2/(x+1))*(x+1)-6*I*sqrt(-1+2/(x+1))), 2/Abs(x+1) > 1), (-x+1)/(-3*I*sqrt(1-2/(x+1))*(x+1)+6*I*sqrt(1-2/(x+1))) + 3/(-3*I*sqrt(1-2/(x+1))*(x+1)+6*I*sqrt(1-2/(x+1))), True))`

$$3.1113 \quad \int \frac{1}{(1-x)^{7/2} \sqrt{1+x}} dx$$

Optimal. Leaf size=61

$$\frac{2\sqrt{x+1}}{15\sqrt{1-x}} + \frac{2\sqrt{x+1}}{15(1-x)^{3/2}} + \frac{\sqrt{x+1}}{5(1-x)^{5/2}}$$

[Out] $1/5*(1+x)^{(1/2)/(1-x)^{(5/2)}+2/15*(1+x)^{(1/2)/(1-x)^{(3/2)}+2/15*(1+x)^{(1/2)/(1-x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{2\sqrt{x+1}}{15\sqrt{1-x}} + \frac{2\sqrt{x+1}}{15(1-x)^{3/2}} + \frac{\sqrt{x+1}}{5(1-x)^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - x)^(7/2)*Sqrt[1 + x]),x]

[Out] Sqrt[1 + x]/(5*(1 - x)^(5/2)) + (2*Sqrt[1 + x])/(15*(1 - x)^(3/2)) + (2*Sqrt[1 + x])/(15*Sqrt[1 - x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(1-x)^{7/2}\sqrt{1+x}} dx &= \frac{\sqrt{1+x}}{5(1-x)^{5/2}} + \frac{2}{5} \int \frac{1}{(1-x)^{5/2}\sqrt{1+x}} dx \\
&= \frac{\sqrt{1+x}}{5(1-x)^{5/2}} + \frac{2\sqrt{1+x}}{15(1-x)^{3/2}} + \frac{2}{15} \int \frac{1}{(1-x)^{3/2}\sqrt{1+x}} dx \\
&= \frac{\sqrt{1+x}}{5(1-x)^{5/2}} + \frac{2\sqrt{1+x}}{15(1-x)^{3/2}} + \frac{2\sqrt{1+x}}{15\sqrt{1-x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 0.49

$$\frac{\sqrt{x+1} (2x^2 - 6x + 7)}{15(1-x)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(7/2)*Sqrt[1+x]),x]

[Out] (Sqrt[1+x]*(7-6*x+2*x^2))/(15*(1-x)^(5/2))

fricas [A] time = 0.44, size = 56, normalized size = 0.92

$$\frac{7x^3 - 21x^2 - (2x^2 - 6x + 7)\sqrt{x+1}\sqrt{-x+1} + 21x - 7}{15(x^3 - 3x^2 + 3x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(7/2)/(1+x)^(1/2),x, algorithm="fricas")

[Out] 1/15*(7*x^3 - 21*x^2 - (2*x^2 - 6*x + 7)*sqrt(x + 1)*sqrt(-x + 1) + 21*x - 7)/(x^3 - 3*x^2 + 3*x - 1)

giac [A] time = 0.69, size = 29, normalized size = 0.48

$$\frac{(2(x+1)(x-4) + 15)\sqrt{x+1}\sqrt{-x+1}}{15(x-1)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(7/2)/(1+x)^(1/2),x, algorithm="giac")

[Out] -1/15*(2*(x+1)*(x-4) + 15)*sqrt(x+1)*sqrt(-x+1)/(x-1)^3

maple [A] time = 0.00, size = 25, normalized size = 0.41

$$\frac{\sqrt{x+1} (2x^2 - 6x + 7)}{15(-x+1)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-x+1)^(7/2)/(x+1)^(1/2),x)`

[Out] `1/15*(x+1)^(1/2)*(2*x^2-6*x+7)/(-x+1)^(5/2)`

maxima [A] time = 3.03, size = 64, normalized size = 1.05

$$-\frac{\sqrt{-x^2+1}}{5(x^3-3x^2+3x-1)} + \frac{2\sqrt{-x^2+1}}{15(x^2-2x+1)} - \frac{2\sqrt{-x^2+1}}{15(x-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(7/2)/(1+x)^(1/2),x, algorithm="maxima")`

[Out] `-1/5*sqrt(-x^2+1)/(x^3-3*x^2+3*x-1)+2/15*sqrt(-x^2+1)/(x^2-2*x+1)-2/15*sqrt(-x^2+1)/(x-1)`

mupad [B] time = 0.32, size = 55, normalized size = 0.90

$$-\frac{x\sqrt{1-x}+7\sqrt{1-x}-4x^2\sqrt{1-x}+2x^3\sqrt{1-x}}{15(x-1)^3\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((1-x)^(7/2)*(x+1)^(1/2)),x)`

[Out] `-(x*(1-x)^(1/2)+7*(1-x)^(1/2)-4*x^2*(1-x)^(1/2)+2*x^3*(1-x)^(1/2))/(15*(x-1)^3*(x+1)^(1/2))`

sympy [C] time = 7.89, size = 332, normalized size = 5.44

$$\left\{ \begin{array}{l} -\frac{2i(x+1)^2}{-15i\sqrt{-1+\frac{2}{x+1}}(x+1)^2+60i\sqrt{-1+\frac{2}{x+1}}(x+1)-60i\sqrt{-1+\frac{2}{x+1}}} + \frac{10i(x+1)}{-15i\sqrt{-1+\frac{2}{x+1}}(x+1)^2+60i\sqrt{-1+\frac{2}{x+1}}(x+1)-60i\sqrt{-1+\frac{2}{x+1}}} - \frac{15}{-15i\sqrt{-1+\frac{2}{x+1}}(x+1)^2+60i\sqrt{-1+\frac{2}{x+1}}(x+1)-60i\sqrt{-1+\frac{2}{x+1}}} \\ \frac{2(x+1)^2}{15i\sqrt{1-\frac{2}{x+1}}(x+1)^2-60i\sqrt{1-\frac{2}{x+1}}(x+1)+60i\sqrt{1-\frac{2}{x+1}}} - \frac{10(x+1)}{15i\sqrt{1-\frac{2}{x+1}}(x+1)^2-60i\sqrt{1-\frac{2}{x+1}}(x+1)+60i\sqrt{1-\frac{2}{x+1}}} + \frac{15}{15i\sqrt{1-\frac{2}{x+1}}(x+1)^2-60i\sqrt{1-\frac{2}{x+1}}(x+1)+60i\sqrt{1-\frac{2}{x+1}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)**(7/2)/(1+x)**(1/2),x)

[Out] Piecewise((-2*I*(x + 1)**2/(-15*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 60*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 60*I*sqrt(-1 + 2/(x + 1)))) + 10*I*(x + 1)/(-15*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 60*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 60*I*sqrt(-1 + 2/(x + 1))) - 15*I/(-15*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 60*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 60*I*sqrt(-1 + 2/(x + 1))), 2/Abs(x + 1) > 1), (2*(x + 1)**2/(15*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 60*I*sqrt(1 - 2/(x + 1))*(x + 1) + 60*I*sqrt(1 - 2/(x + 1))) - 10*(x + 1)/(15*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 60*I*sqrt(1 - 2/(x + 1))*(x + 1) + 60*I*sqrt(1 - 2/(x + 1))) + 15/(15*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 60*I*sqrt(1 - 2/(x + 1))*(x + 1) + 60*I*sqrt(1 - 2/(x + 1))), True))

$$3.1114 \quad \int \frac{1}{(1-x)^{9/2} \sqrt{1+x}} dx$$

Optimal. Leaf size=81

$$\frac{2\sqrt{x+1}}{35\sqrt{1-x}} + \frac{2\sqrt{x+1}}{35(1-x)^{3/2}} + \frac{3\sqrt{x+1}}{35(1-x)^{5/2}} + \frac{\sqrt{x+1}}{7(1-x)^{7/2}}$$

[Out] $1/7*(1+x)^{(1/2)/(1-x)^{(7/2)}+3/35*(1+x)^{(1/2)/(1-x)^{(5/2)}+2/35*(1+x)^{(1/2)/(1-x)^{(3/2)}+2/35*(1+x)^{(1/2)/(1-x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{2\sqrt{x+1}}{35\sqrt{1-x}} + \frac{2\sqrt{x+1}}{35(1-x)^{3/2}} + \frac{3\sqrt{x+1}}{35(1-x)^{5/2}} + \frac{\sqrt{x+1}}{7(1-x)^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - x)^(9/2)*Sqrt[1 + x]),x]

[Out] Sqrt[1 + x]/(7*(1 - x)^(7/2)) + (3*Sqrt[1 + x])/(35*(1 - x)^(5/2)) + (2*Sqrt[1 + x])/(35*(1 - x)^(3/2)) + (2*Sqrt[1 + x])/(35*Sqrt[1 - x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(1-x)^{9/2}\sqrt{1+x}} dx &= \frac{\sqrt{1+x}}{7(1-x)^{7/2}} + \frac{3}{7} \int \frac{1}{(1-x)^{7/2}\sqrt{1+x}} dx \\
&= \frac{\sqrt{1+x}}{7(1-x)^{7/2}} + \frac{3\sqrt{1+x}}{35(1-x)^{5/2}} + \frac{6}{35} \int \frac{1}{(1-x)^{5/2}\sqrt{1+x}} dx \\
&= \frac{\sqrt{1+x}}{7(1-x)^{7/2}} + \frac{3\sqrt{1+x}}{35(1-x)^{5/2}} + \frac{2\sqrt{1+x}}{35(1-x)^{3/2}} + \frac{2}{35} \int \frac{1}{(1-x)^{3/2}\sqrt{1+x}} dx \\
&= \frac{\sqrt{1+x}}{7(1-x)^{7/2}} + \frac{3\sqrt{1+x}}{35(1-x)^{5/2}} + \frac{2\sqrt{1+x}}{35(1-x)^{3/2}} + \frac{2\sqrt{1+x}}{35\sqrt{1-x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 35, normalized size = 0.43

$$\frac{\sqrt{x+1}(-2x^3 + 8x^2 - 13x + 12)}{35(1-x)^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(9/2)*Sqrt[1+x]),x]

[Out] (Sqrt[1+x]*(12-13*x+8*x^2-2*x^3))/(35*(1-x)^(7/2))

fricas [A] time = 0.47, size = 71, normalized size = 0.88

$$\frac{12x^4 - 48x^3 + 72x^2 - (2x^3 - 8x^2 + 13x - 12)\sqrt{x+1}\sqrt{-x+1} - 48x + 12}{35(x^4 - 4x^3 + 6x^2 - 4x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(9/2)/(1+x)^(1/2),x, algorithm="fricas")

[Out] 1/35*(12*x^4 - 48*x^3 + 72*x^2 - (2*x^3 - 8*x^2 + 13*x - 12)*sqrt(x + 1)*sqrt(-x + 1) - 48*x + 12)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1)

giac [A] time = 0.66, size = 35, normalized size = 0.43

$$\frac{((2(x+1)(x-6) + 35)(x+1) - 35)\sqrt{x+1}\sqrt{-x+1}}{35(x-1)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(9/2)/(1+x)^(1/2),x, algorithm="giac")

[Out] $-1/35*((2*(x + 1)*(x - 6) + 35)*(x + 1) - 35)*\sqrt{x + 1}*\sqrt{-x + 1}/(x - 1)^4$

maple [A] time = 0.00, size = 30, normalized size = 0.37

$$\frac{\sqrt{x+1} (2x^3 - 8x^2 + 13x - 12)}{35(-x+1)^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(-x+1)^{(9/2)}/(x+1)^{(1/2)}, x)$

[Out] $-1/35*(x+1)^{(1/2)}*(2*x^3-8*x^2+13*x-12)/(-x+1)^{(7/2)}$

maxima [A] time = 3.03, size = 95, normalized size = 1.17

$$\frac{\sqrt{-x^2+1}}{7(x^4-4x^3+6x^2-4x+1)} - \frac{3\sqrt{-x^2+1}}{35(x^3-3x^2+3x-1)} + \frac{2\sqrt{-x^2+1}}{35(x^2-2x+1)} - \frac{2\sqrt{-x^2+1}}{35(x-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(1-x)^{(9/2)}/(1+x)^{(1/2)}, x, \text{algorithm}="maxima")$

[Out] $1/7*\sqrt{-x^2+1}/(x^4-4*x^3+6*x^2-4*x+1) - 3/35*\sqrt{-x^2+1}/(x^3-3*x^2+3*x-1) + 2/35*\sqrt{-x^2+1}/(x^2-2*x+1) - 2/35*\sqrt{-x^2+1}/(x-1)$

mupad [B] time = 0.34, size = 67, normalized size = 0.83

$$\frac{x\sqrt{1-x} - 12\sqrt{1-x} + 5x^2\sqrt{1-x} - 6x^3\sqrt{1-x} + 2x^4\sqrt{1-x}}{35(x-1)^4\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/((1-x)^{(9/2)}*(x+1)^{(1/2)}), x)$

[Out] $-(x*(1-x)^{(1/2)} - 12*(1-x)^{(1/2)} + 5*x^2*(1-x)^{(1/2)} - 6*x^3*(1-x)^{(1/2)} + 2*x^4*(1-x)^{(1/2)})/(35*(x-1)^4*(x+1)^{(1/2)})$

sympy [C] time = 22.13, size = 595, normalized size = 7.35

$$\left\{ \begin{array}{l} \frac{2i(x+1)^3}{35i\sqrt{-1+\frac{2}{x+1}}(x+1)^3-210i\sqrt{-1+\frac{2}{x+1}}(x+1)^2+420i\sqrt{-1+\frac{2}{x+1}}(x+1)-280i\sqrt{-1+\frac{2}{x+1}}} - \frac{14i(x+1)^2}{35i\sqrt{-1+\frac{2}{x+1}}(x+1)^3-210i\sqrt{-1+\frac{2}{x+1}}(x+1)^2+420i\sqrt{-1+\frac{2}{x+1}}} \\ - \frac{2(x+1)^3}{-35i\sqrt{1-\frac{2}{x+1}}(x+1)^3+210i\sqrt{1-\frac{2}{x+1}}(x+1)^2-420i\sqrt{1-\frac{2}{x+1}}(x+1)+280i\sqrt{1-\frac{2}{x+1}}} + \frac{14(x+1)^2}{-35i\sqrt{1-\frac{2}{x+1}}(x+1)^3+210i\sqrt{1-\frac{2}{x+1}}(x+1)^2-420i\sqrt{1-\frac{2}{x+1}}(x+1)} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)**(9/2)/(1+x)**(1/2),x)

[Out] Piecewise((2*I*(x + 1)**3/(35*I*sqrt(-1 + 2/(x + 1)))*(x + 1)**3 - 210*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 420*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 280*I*sqrt(-1 + 2/(x + 1))) - 14*I*(x + 1)**2/(35*I*sqrt(-1 + 2/(x + 1)))*(x + 1)**3 - 210*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 420*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 280*I*sqrt(-1 + 2/(x + 1))) + 35*I*(x + 1)/(35*I*sqrt(-1 + 2/(x + 1)))*(x + 1)**3 - 210*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 420*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 280*I*sqrt(-1 + 2/(x + 1))) - 35*I/(35*I*sqrt(-1 + 2/(x + 1)))*(x + 1)**3 - 210*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 420*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 280*I*sqrt(-1 + 2/(x + 1))), 2/Abs(x + 1) > 1), (-2*(x + 1)**3/(-35*I*sqrt(1 - 2/(x + 1)))*(x + 1)**3 + 210*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 420*I*sqrt(1 - 2/(x + 1))*(x + 1) + 280*I*sqrt(1 - 2/(x + 1))) + 14*(x + 1)**2/(-35*I*sqrt(1 - 2/(x + 1)))*(x + 1)**3 + 210*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 420*I*sqrt(1 - 2/(x + 1))*(x + 1) + 280*I*sqrt(1 - 2/(x + 1))) - 35*(x + 1)/(-35*I*sqrt(1 - 2/(x + 1)))*(x + 1)**3 + 210*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 420*I*sqrt(1 - 2/(x + 1))*(x + 1) + 280*I*sqrt(1 - 2/(x + 1))) + 35/(-35*I*sqrt(1 - 2/(x + 1)))*(x + 1)**3 + 210*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 420*I*sqrt(1 - 2/(x + 1))*(x + 1) + 280*I*sqrt(1 - 2/(x + 1))), True))

$$3.1115 \quad \int \frac{1}{(1-x)^{11/2} \sqrt{1+x}} dx$$

Optimal. Leaf size=101

$$\frac{8\sqrt{x+1}}{315\sqrt{1-x}} + \frac{8\sqrt{x+1}}{315(1-x)^{3/2}} + \frac{4\sqrt{x+1}}{105(1-x)^{5/2}} + \frac{4\sqrt{x+1}}{63(1-x)^{7/2}} + \frac{\sqrt{x+1}}{9(1-x)^{9/2}}$$

[Out] $1/9*(1+x)^{(1/2)/(1-x)^{(9/2)}+4/63*(1+x)^{(1/2)/(1-x)^{(7/2)}+4/105*(1+x)^{(1/2)/(1-x)^{(5/2)}+8/315*(1+x)^{(1/2)/(1-x)^{(3/2)}+8/315*(1+x)^{(1/2)/(1-x)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{8\sqrt{x+1}}{315\sqrt{1-x}} + \frac{8\sqrt{x+1}}{315(1-x)^{3/2}} + \frac{4\sqrt{x+1}}{105(1-x)^{5/2}} + \frac{4\sqrt{x+1}}{63(1-x)^{7/2}} + \frac{\sqrt{x+1}}{9(1-x)^{9/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - x)^(11/2)*Sqrt[1 + x]),x]

[Out] Sqrt[1 + x]/(9*(1 - x)^(9/2)) + (4*Sqrt[1 + x])/(63*(1 - x)^(7/2)) + (4*Sqrt[1 + x])/(105*(1 - x)^(5/2)) + (8*Sqrt[1 + x])/(315*(1 - x)^(3/2)) + (8*Sqrt[1 + x])/(315*Sqrt[1 - x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(1-x)^{11/2}\sqrt{1+x}} dx &= \frac{\sqrt{1+x}}{9(1-x)^{9/2}} + \frac{4}{9} \int \frac{1}{(1-x)^{9/2}\sqrt{1+x}} dx \\
&= \frac{\sqrt{1+x}}{9(1-x)^{9/2}} + \frac{4\sqrt{1+x}}{63(1-x)^{7/2}} + \frac{4}{21} \int \frac{1}{(1-x)^{7/2}\sqrt{1+x}} dx \\
&= \frac{\sqrt{1+x}}{9(1-x)^{9/2}} + \frac{4\sqrt{1+x}}{63(1-x)^{7/2}} + \frac{4\sqrt{1+x}}{105(1-x)^{5/2}} + \frac{8}{105} \int \frac{1}{(1-x)^{5/2}\sqrt{1+x}} dx \\
&= \frac{\sqrt{1+x}}{9(1-x)^{9/2}} + \frac{4\sqrt{1+x}}{63(1-x)^{7/2}} + \frac{4\sqrt{1+x}}{105(1-x)^{5/2}} + \frac{8\sqrt{1+x}}{315(1-x)^{3/2}} + \frac{8}{315} \int \frac{1}{(1-x)^{3/2}\sqrt{1+x}} dx \\
&= \frac{\sqrt{1+x}}{9(1-x)^{9/2}} + \frac{4\sqrt{1+x}}{63(1-x)^{7/2}} + \frac{4\sqrt{1+x}}{105(1-x)^{5/2}} + \frac{8\sqrt{1+x}}{315(1-x)^{3/2}} + \frac{8\sqrt{1+x}}{315\sqrt{1-x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 0.40

$$\frac{\sqrt{x+1} (8x^4 - 40x^3 + 84x^2 - 100x + 83)}{315(1-x)^{9/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(11/2)*Sqrt[1+x]),x]

[Out] (Sqrt[1+x]*(83-100*x+84*x^2-40*x^3+8*x^4))/(315*(1-x)^(9/2))

fricas [A] time = 0.46, size = 86, normalized size = 0.85

$$\frac{83x^5 - 415x^4 + 830x^3 - 830x^2 - (8x^4 - 40x^3 + 84x^2 - 100x + 83)\sqrt{x+1}\sqrt{-x+1} + 415x - 83}{315(x^5 - 5x^4 + 10x^3 - 10x^2 + 5x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(11/2)/(1+x)^(1/2),x, algorithm="fricas")

[Out] 1/315*(83*x^5 - 415*x^4 + 830*x^3 - 830*x^2 - (8*x^4 - 40*x^3 + 84*x^2 - 100*x + 83)*sqrt(x+1)*sqrt(-x+1) + 415*x - 83)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1)

giac [A] time = 0.67, size = 42, normalized size = 0.42

$$\frac{(4((2(x+1)(x-8)+63)(x+1)-105)(x+1)+315)\sqrt{x+1}\sqrt{-x+1}}{315(x-1)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(11/2)/(1+x)^(1/2),x, algorithm="giac")

[Out] -1/315*(4*((2*(x + 1)*(x - 8) + 63)*(x + 1) - 105)*(x + 1) + 315)*sqrt(x + 1)*sqrt(-x + 1)/(x - 1)^5

maple [A] time = 0.00, size = 35, normalized size = 0.35

$$\frac{\sqrt{x+1} (8x^4 - 40x^3 + 84x^2 - 100x + 83)}{315(-x+1)^{\frac{9}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+1)^(11/2)/(x+1)^(1/2),x)

[Out] 1/315*(x+1)^(1/2)*(8*x^4-40*x^3+84*x^2-100*x+83)/(-x+1)^(9/2)

maxima [A] time = 3.08, size = 131, normalized size = 1.30

$$-\frac{\sqrt{-x^2+1}}{9(x^5-5x^4+10x^3-10x^2+5x-1)} + \frac{4\sqrt{-x^2+1}}{63(x^4-4x^3+6x^2-4x+1)} - \frac{4\sqrt{-x^2+1}}{105(x^3-3x^2+3x-1)} + \frac{8\sqrt{-x^2+1}}{315(x^2-2x+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(11/2)/(1+x)^(1/2),x, algorithm="maxima")

[Out] -1/9*sqrt(-x^2 + 1)/(x^5 - 5*x^4 + 10*x^3 - 10*x^2 + 5*x - 1) + 4/63*sqrt(-x^2 + 1)/(x^4 - 4*x^3 + 6*x^2 - 4*x + 1) - 4/105*sqrt(-x^2 + 1)/(x^3 - 3*x^2 + 3*x - 1) + 8/315*sqrt(-x^2 + 1)/(x^2 - 2*x + 1) - 8/315*sqrt(-x^2 + 1)/(x - 1)

mupad [B] time = 0.36, size = 80, normalized size = 0.79

$$\frac{17x\sqrt{1-x} - 83\sqrt{1-x} + 16x^2\sqrt{1-x} - 44x^3\sqrt{1-x} + 32x^4\sqrt{1-x} - 8x^5\sqrt{1-x}}{315(x-1)^5\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((1-x)^(11/2)*(x+1)^(1/2)),x)

[Out] (17*x*(1-x)^(1/2) - 83*(1-x)^(1/2) + 16*x^2*(1-x)^(1/2) - 44*x^3*(1-x)^(1/2) + 32*x^4*(1-x)^(1/2) - 8*x^5*(1-x)^(1/2))/(315*(x-1)^5*(x+1)^(1/2))

sympy [C] time = 58.39, size = 933, normalized size = 9.24

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)**(11/2)/(1+x)**(1/2),x)`

[Out] `Piecewise((-8*I*(x + 1)**4/(-315*I*sqrt(-1 + 2/(x + 1)))*(x + 1)**4 + 2520*I*sqrt(-1 + 2/(x + 1))*(x + 1)**3 - 7560*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 10080*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 5040*I*sqrt(-1 + 2/(x + 1))) + 72*I*(x + 1)**3/(-315*I*sqrt(-1 + 2/(x + 1))*(x + 1)**4 + 2520*I*sqrt(-1 + 2/(x + 1))*(x + 1)**3 - 7560*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 10080*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 5040*I*sqrt(-1 + 2/(x + 1))) - 252*I*(x + 1)**2/(-315*I*sqrt(-1 + 2/(x + 1))*(x + 1)**4 + 2520*I*sqrt(-1 + 2/(x + 1))*(x + 1)**3 - 7560*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 10080*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 5040*I*sqrt(-1 + 2/(x + 1))) + 420*I*(x + 1)/(-315*I*sqrt(-1 + 2/(x + 1))*(x + 1)**4 + 2520*I*sqrt(-1 + 2/(x + 1))*(x + 1)**3 - 7560*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 10080*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 5040*I*sqrt(-1 + 2/(x + 1))) - 315*I/(-315*I*sqrt(-1 + 2/(x + 1))*(x + 1)**4 + 2520*I*sqrt(-1 + 2/(x + 1))*(x + 1)**3 - 7560*I*sqrt(-1 + 2/(x + 1))*(x + 1)**2 + 10080*I*sqrt(-1 + 2/(x + 1))*(x + 1) - 5040*I*sqrt(-1 + 2/(x + 1))), 2/Abs(x + 1) > 1), (8*(x + 1)**4/(315*I*sqrt(1 - 2/(x + 1))*(x + 1)**4 - 2520*I*sqrt(1 - 2/(x + 1))*(x + 1)**3 + 7560*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 10080*I*sqrt(1 - 2/(x + 1))*(x + 1) + 5040*I*sqrt(1 - 2/(x + 1))) - 72*(x + 1)**3/(315*I*sqrt(1 - 2/(x + 1))*(x + 1)**4 - 2520*I*sqrt(1 - 2/(x + 1))*(x + 1)**3 + 7560*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 10080*I*sqrt(1 - 2/(x + 1))*(x + 1) + 5040*I*sqrt(1 - 2/(x + 1))) + 252*(x + 1)**2/(315*I*sqrt(1 - 2/(x + 1))*(x + 1)**4 - 2520*I*sqrt(1 - 2/(x + 1))*(x + 1)**3 + 7560*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 10080*I*sqrt(1 - 2/(x + 1))*(x + 1) + 5040*I*sqrt(1 - 2/(x + 1))) - 420*(x + 1)/(315*I*sqrt(1 - 2/(x + 1))*(x + 1)**4 - 2520*I*sqrt(1 - 2/(x + 1))*(x + 1)**3 + 7560*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 10080*I*sqrt(1 - 2/(x + 1))*(x + 1) + 5040*I*sqrt(1 - 2/(x + 1))) + 315/(315*I*sqrt(1 - 2/(x + 1))*(x + 1)**4 - 2520*I*sqrt(1 - 2/(x + 1))*(x + 1)**3 + 7560*I*sqrt(1 - 2/(x + 1))*(x + 1)**2 - 10080*I*sqrt(1 - 2/(x + 1))*(x + 1) + 5040*I*sqrt(1 - 2/(x + 1))), True))`

$$3.1116 \quad \int \frac{(1-x)^{7/2}}{(1+x)^{3/2}} dx$$

Optimal. Leaf size=85

$$-\frac{2(1-x)^{7/2}}{\sqrt{x+1}} - \frac{7}{3}\sqrt{x+1}(1-x)^{5/2} - \frac{35}{6}\sqrt{x+1}(1-x)^{3/2} - \frac{35}{2}\sqrt{x+1}\sqrt{1-x} - \frac{35}{2}\sin^{-1}(x)$$

[Out] $-35/2*\arcsin(x)-2*(1-x)^{(7/2)/(1+x)^{(1/2)}-35/6*(1-x)^{(3/2)*(1+x)^{(1/2)}-7/3*(1-x)^{(5/2)*(1+x)^{(1/2)}-35/2*(1-x)^{(1/2)*(1+x)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 85, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 41, 216}

$$-\frac{2(1-x)^{7/2}}{\sqrt{x+1}} - \frac{7}{3}\sqrt{x+1}(1-x)^{5/2} - \frac{35}{6}\sqrt{x+1}(1-x)^{3/2} - \frac{35}{2}\sqrt{x+1}\sqrt{1-x} - \frac{35}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(7/2)/(1 + x)^(3/2), x]

[Out] $(-2*(1-x)^{(7/2)}/\text{Sqrt}[1+x] - (35*\text{Sqrt}[1-x]*\text{Sqrt}[1+x])/2 - (35*(1-x)^{(3/2)*\text{Sqrt}[1+x])/6 - (7*(1-x)^{(5/2)*\text{Sqrt}[1+x])/3 - (35*\text{ArcSin}[x])/2$

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,

c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
 \int \frac{(1-x)^{7/2}}{(1+x)^{3/2}} dx &= -\frac{2(1-x)^{7/2}}{\sqrt{1+x}} - 7 \int \frac{(1-x)^{5/2}}{\sqrt{1+x}} dx \\
 &= -\frac{2(1-x)^{7/2}}{\sqrt{1+x}} - \frac{7}{3}(1-x)^{5/2}\sqrt{1+x} - \frac{35}{3} \int \frac{(1-x)^{3/2}}{\sqrt{1+x}} dx \\
 &= -\frac{2(1-x)^{7/2}}{\sqrt{1+x}} - \frac{35}{6}(1-x)^{3/2}\sqrt{1+x} - \frac{7}{3}(1-x)^{5/2}\sqrt{1+x} - \frac{35}{2} \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx \\
 &= -\frac{2(1-x)^{7/2}}{\sqrt{1+x}} - \frac{35}{2}\sqrt{1-x}\sqrt{1+x} - \frac{35}{6}(1-x)^{3/2}\sqrt{1+x} - \frac{7}{3}(1-x)^{5/2}\sqrt{1+x} - \frac{35}{2} \int \frac{1}{\sqrt{1-x}} dx \\
 &= -\frac{2(1-x)^{7/2}}{\sqrt{1+x}} - \frac{35}{2}\sqrt{1-x}\sqrt{1+x} - \frac{35}{6}(1-x)^{3/2}\sqrt{1+x} - \frac{7}{3}(1-x)^{5/2}\sqrt{1+x} - \frac{35}{2} \int \frac{1}{\sqrt{1-x}} dx \\
 &= -\frac{2(1-x)^{7/2}}{\sqrt{1+x}} - \frac{35}{2}\sqrt{1-x}\sqrt{1+x} - \frac{35}{6}(1-x)^{3/2}\sqrt{1+x} - \frac{7}{3}(1-x)^{5/2}\sqrt{1+x} - \frac{35}{2} \sin^{-1}(x)
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 37, normalized size = 0.44

$$\frac{(1-x)^{9/2} {}_2F_1\left(\frac{3}{2}, \frac{9}{2}; \frac{11}{2}; \frac{1-x}{2}\right)}{9\sqrt{2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(7/2)/(1 + x)^(3/2), x]

[Out] -1/9*((1 - x)^(9/2)*Hypergeometric2F1[3/2, 9/2, 11/2, (1 - x)/2])/Sqrt[2]

fricas [A] time = 0.45, size = 65, normalized size = 0.76

$$\frac{(2x^3 - 13x^2 + 55x + 166)\sqrt{x+1}\sqrt{-x+1} - 210(x+1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) + 166x + 166}{6(x+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)/(1+x)^(3/2),x, algorithm="fricas")

[Out] -1/6*((2*x^3 - 13*x^2 + 55*x + 166)*sqrt(x + 1)*sqrt(-x + 1) - 210*(x + 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) + 166*x + 166)/(x + 1)

giac [A] time = 0.75, size = 81, normalized size = 0.95

$$-\frac{1}{6}((2x - 17)(x + 1) + 87)\sqrt{x + 1}\sqrt{-x + 1} + \frac{8(\sqrt{2} - \sqrt{-x + 1})}{\sqrt{x + 1}} - \frac{8\sqrt{x + 1}}{\sqrt{2} - \sqrt{-x + 1}} - 35 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)/(1+x)^(3/2),x, algorithm="giac")

[Out] -1/6*((2*x - 17)*(x + 1) + 87)*sqrt(x + 1)*sqrt(-x + 1) + 8*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) - 8*sqrt(x + 1)/(sqrt(2) - sqrt(-x + 1)) - 35*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.02, size = 84, normalized size = 0.99

$$-\frac{35\sqrt{(x+1)(-x+1)} \arcsin(x)}{2\sqrt{x+1}\sqrt{-x+1}} + \frac{(2x^4 - 15x^3 + 68x^2 + 111x - 166)\sqrt{(x+1)(-x+1)}}{6\sqrt{-(x+1)(x-1)}\sqrt{-x+1}\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(7/2)/(x+1)^(3/2),x)

[Out] 1/6*(2*x^4-15*x^3+68*x^2+111*x-166)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)/(x+1)^(1/2)-35/2*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.84, size = 70, normalized size = 0.82

$$\frac{x^4}{3\sqrt{-x^2+1}} - \frac{5x^3}{2\sqrt{-x^2+1}} + \frac{34x^2}{3\sqrt{-x^2+1}} + \frac{37x}{2\sqrt{-x^2+1}} - \frac{83}{3\sqrt{-x^2+1}} - \frac{35}{2} \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)/(1+x)^(3/2),x, algorithm="maxima")

[Out] 1/3*x^4/sqrt(-x^2 + 1) - 5/2*x^3/sqrt(-x^2 + 1) + 34/3*x^2/sqrt(-x^2 + 1) + 37/2*x/sqrt(-x^2 + 1) - 83/3/sqrt(-x^2 + 1) - 35/2*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(1-x)^{7/2}}{(x+1)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(7/2)/(x + 1)^(3/2), x)`

[Out] `int((1 - x)^(7/2)/(x + 1)^(3/2), x)`

sympy [A] time = 17.48, size = 207, normalized size = 2.44

$$\begin{cases} 35i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{i(x+1)^{\frac{7}{2}}}{3\sqrt{x-1}} + \frac{23i(x+1)^{\frac{5}{2}}}{6\sqrt{x-1}} - \frac{125i(x+1)^{\frac{3}{2}}}{6\sqrt{x-1}} + \frac{13i\sqrt{x+1}}{\sqrt{x-1}} + \frac{32i}{\sqrt{x-1}\sqrt{x+1}} & \text{for } \frac{|x+1|}{2} > 1 \\ -35 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{(x+1)^{\frac{7}{2}}}{3\sqrt{1-x}} - \frac{23(x+1)^{\frac{5}{2}}}{6\sqrt{1-x}} + \frac{125(x+1)^{\frac{3}{2}}}{6\sqrt{1-x}} - \frac{13\sqrt{x+1}}{\sqrt{1-x}} - \frac{32}{\sqrt{1-x}\sqrt{x+1}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(7/2)/(1+x)**(3/2), x)`

[Out] `Piecewise((35*I*acosh(sqrt(2)*sqrt(x + 1)/2) - I*(x + 1)**(7/2)/(3*sqrt(x - 1)) + 23*I*(x + 1)**(5/2)/(6*sqrt(x - 1)) - 125*I*(x + 1)**(3/2)/(6*sqrt(x - 1)) + 13*I*sqrt(x + 1)/sqrt(x - 1) + 32*I/(sqrt(x - 1)*sqrt(x + 1)), Abs(x + 1)/2 > 1), (-35*asin(sqrt(2)*sqrt(x + 1)/2) + (x + 1)**(7/2)/(3*sqrt(1 - x)) - 23*(x + 1)**(5/2)/(6*sqrt(1 - x)) + 125*(x + 1)**(3/2)/(6*sqrt(1 - x)) - 13*sqrt(x + 1)/sqrt(1 - x) - 32/(sqrt(1 - x)*sqrt(x + 1)), True))`

$$3.1117 \quad \int \frac{(1-x)^{5/2}}{(1+x)^{3/2}} dx$$

Optimal. Leaf size=65

$$-\frac{2(1-x)^{5/2}}{\sqrt{x+1}} - \frac{5}{2}\sqrt{x+1}(1-x)^{3/2} - \frac{15}{2}\sqrt{x+1}\sqrt{1-x} - \frac{15}{2}\sin^{-1}(x)$$

[Out] $-15/2*\arcsin(x)-2*(1-x)^{(5/2)/(1+x)^{(1/2)}-5/2*(1-x)^{(3/2)*(1+x)^{(1/2)}-15/2*(1-x)^{(1/2)*(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 41, 216}

$$-\frac{2(1-x)^{5/2}}{\sqrt{x+1}} - \frac{5}{2}\sqrt{x+1}(1-x)^{3/2} - \frac{15}{2}\sqrt{x+1}\sqrt{1-x} - \frac{15}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(5/2)/(1 + x)^(3/2), x]

[Out] $(-2*(1-x)^{(5/2))/\text{Sqrt}[1+x] - (15*\text{Sqrt}[1-x]*\text{Sqrt}[1+x])/2 - (5*(1-x)^{(3/2)*\text{Sqrt}[1+x])/2 - (15*\text{ArcSin}[x])/2$

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ

$[m, 0] \ \&\& \ (\ !\text{IntegerQ}[n] \ || \ (\text{GtQ}[m, 0] \ \&\& \ \text{LtQ}[m - n, 0])) \ \&\& \ !\text{ILtQ}[m + n + 2, 0] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 216

$\text{Int}[1/\text{Sqrt}[(a_) + (b_.)*(x_)^2], x_Symbol] \ :> \ \text{Simp}[\text{ArcSin}[(\text{Rt}[-b, 2]*x)/\text{Sqrt}[a]]/\text{Rt}[-b, 2], x] \ /; \ \text{FreeQ}\{\{a, b\}, x\} \ \&\& \ \text{GtQ}[a, 0] \ \&\& \ \text{NegQ}[b]$

Rubi steps

$$\begin{aligned} \int \frac{(1-x)^{5/2}}{(1+x)^{3/2}} dx &= -\frac{2(1-x)^{5/2}}{\sqrt{1+x}} - 5 \int \frac{(1-x)^{3/2}}{\sqrt{1+x}} dx \\ &= -\frac{2(1-x)^{5/2}}{\sqrt{1+x}} - \frac{5}{2}(1-x)^{3/2}\sqrt{1+x} - \frac{15}{2} \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx \\ &= -\frac{2(1-x)^{5/2}}{\sqrt{1+x}} - \frac{15}{2}\sqrt{1-x}\sqrt{1+x} - \frac{5}{2}(1-x)^{3/2}\sqrt{1+x} - \frac{15}{2} \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\ &= -\frac{2(1-x)^{5/2}}{\sqrt{1+x}} - \frac{15}{2}\sqrt{1-x}\sqrt{1+x} - \frac{5}{2}(1-x)^{3/2}\sqrt{1+x} - \frac{15}{2} \int \frac{1}{\sqrt{1-x^2}} dx \\ &= -\frac{2(1-x)^{5/2}}{\sqrt{1+x}} - \frac{15}{2}\sqrt{1-x}\sqrt{1+x} - \frac{5}{2}(1-x)^{3/2}\sqrt{1+x} - \frac{15}{2} \sin^{-1}(x) \end{aligned}$$

Mathematica [C] time = 0.01, size = 37, normalized size = 0.57

$$\frac{(1-x)^{7/2} {}_2F_1\left(\frac{3}{2}, \frac{7}{2}; \frac{9}{2}; \frac{1-x}{2}\right)}{7\sqrt{2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(5/2)/(1 + x)^(3/2), x]

[Out] -1/7*((1 - x)^(7/2)*Hypergeometric2F1[3/2, 7/2, 9/2, (1 - x)/2])/Sqrt[2]

fricas [A] time = 0.44, size = 58, normalized size = 0.89

$$\frac{(x^2 - 7x - 24)\sqrt{x+1}\sqrt{-x+1} + 30(x+1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) - 24x - 24}{2(x+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)/(1+x)^(3/2),x, algorithm="fricas")

[Out] 1/2*((x^2 - 7*x - 24)*sqrt(x + 1)*sqrt(-x + 1) + 30*(x + 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) - 24*x - 24)/(x + 1)

giac [A] time = 0.79, size = 73, normalized size = 1.12

$$\frac{1}{2} \sqrt{x+1} (x-8) \sqrt{-x+1} + \frac{4(\sqrt{2} - \sqrt{-x+1})}{\sqrt{x+1}} - \frac{4\sqrt{x+1}}{\sqrt{2} - \sqrt{-x+1}} - 15 \arcsin\left(\frac{1}{2} \sqrt{2} \sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)/(1+x)^(3/2),x, algorithm="giac")

[Out] 1/2*sqrt(x + 1)*(x - 8)*sqrt(-x + 1) + 4*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) - 4*sqrt(x + 1)/(sqrt(2) - sqrt(-x + 1)) - 15*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.02, size = 77, normalized size = 1.18

$$-\frac{15\sqrt{(x+1)(-x+1)} \arcsin(x)}{2\sqrt{x+1} \sqrt{-x+1}} - \frac{(x^3 - 8x^2 - 17x + 24) \sqrt{(x+1)(-x+1)}}{2\sqrt{-(x+1)(x-1)} \sqrt{-x+1} \sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(5/2)/(x+1)^(3/2),x)

[Out] -1/2*(x^3-8*x^2-17*x+24)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)/(x+1)^(1/2)-15/2*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.99, size = 56, normalized size = 0.86

$$-\frac{x^3}{2\sqrt{-x^2+1}} + \frac{4x^2}{\sqrt{-x^2+1}} + \frac{17x}{2\sqrt{-x^2+1}} - \frac{12}{\sqrt{-x^2+1}} - \frac{15}{2} \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)/(1+x)^(3/2),x, algorithm="maxima")

[Out] -1/2*x^3/sqrt(-x^2 + 1) + 4*x^2/sqrt(-x^2 + 1) + 17/2*x/sqrt(-x^2 + 1) - 12/sqrt(-x^2 + 1) - 15/2*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(1-x)^{5/2}}{(x+1)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(5/2)/(x + 1)^(3/2), x)`

[Out] `int((1 - x)^(5/2)/(x + 1)^(3/2), x)`

sympy [A] time = 6.99, size = 168, normalized size = 2.58

$$\begin{cases} 15i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{i(x+1)^{\frac{5}{2}}}{2\sqrt{x-1}} - \frac{11i(x+1)^{\frac{3}{2}}}{2\sqrt{x-1}} + \frac{i\sqrt{x+1}}{\sqrt{x-1}} + \frac{16i}{\sqrt{x-1}\sqrt{x+1}} & \text{for } \frac{|x+1|}{2} > 1 \\ -15 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{(x+1)^{\frac{5}{2}}}{2\sqrt{1-x}} + \frac{11(x+1)^{\frac{3}{2}}}{2\sqrt{1-x}} - \frac{\sqrt{x+1}}{\sqrt{1-x}} - \frac{16}{\sqrt{1-x}\sqrt{x+1}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(5/2)/(1+x)**(3/2), x)`

[Out] `Piecewise((15*I*acosh(sqrt(2)*sqrt(x + 1)/2) + I*(x + 1)**(5/2)/(2*sqrt(x - 1)) - 11*I*(x + 1)**(3/2)/(2*sqrt(x - 1)) + I*sqrt(x + 1)/sqrt(x - 1) + 16*I/(sqrt(x - 1)*sqrt(x + 1)), Abs(x + 1)/2 > 1), (-15*asin(sqrt(2)*sqrt(x + 1)/2) - (x + 1)**(5/2)/(2*sqrt(1 - x)) + 11*(x + 1)**(3/2)/(2*sqrt(1 - x)) - sqrt(x + 1)/sqrt(1 - x) - 16/(sqrt(1 - x)*sqrt(x + 1)), True))`

$$3.1118 \quad \int \frac{(1-x)^{3/2}}{(1+x)^{3/2}} dx$$

Optimal. Leaf size=41

$$-\frac{2(1-x)^{3/2}}{\sqrt{x+1}} - 3\sqrt{x+1}\sqrt{1-x} - 3\sin^{-1}(x)$$

[Out] $-3*\arcsin(x)-2*(1-x)^{(3/2)}/(1+x)^{(1/2)}-3*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 41, 216}

$$-\frac{2(1-x)^{3/2}}{\sqrt{x+1}} - 3\sqrt{x+1}\sqrt{1-x} - 3\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(1-x)^{(3/2)}/(1+x)^{(3/2)}, x]$

[Out] $(-2*(1-x)^{(3/2)})/\text{Sqrt}[1+x] - 3*\text{Sqrt}[1-x]*\text{Sqrt}[1+x] - 3*\text{ArcSin}[x]$

Rule 41

$\text{Int}[(a_.) + (b_.)*(x_.)^{(m_.)}*((c_.) + (d_.)*(x_.)^{(m_.)}), x_Symbol] \rightarrow \text{Int}[(a*c + b*d*x^2)^m, x] /;$ FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

$\text{Int}[(a_.) + (b_.)*(x_.)^{(m_.)}*((c_.) + (d_.)*(x_.)^{(n_.)}), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \text{Dist}[(d*n)/(b*(m+1)), \text{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\text{Int}[(a_.) + (b_.)*(x_.)^{(m_.)}*((c_.) + (d_.)*(x_.)^{(n_.)}), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n

+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
 \int \frac{(1-x)^{3/2}}{(1+x)^{3/2}} dx &= -\frac{2(1-x)^{3/2}}{\sqrt{1+x}} - 3 \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx \\
 &= -\frac{2(1-x)^{3/2}}{\sqrt{1+x}} - 3\sqrt{1-x}\sqrt{1+x} - 3 \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
 &= -\frac{2(1-x)^{3/2}}{\sqrt{1+x}} - 3\sqrt{1-x}\sqrt{1+x} - 3 \int \frac{1}{\sqrt{1-x^2}} dx \\
 &= -\frac{2(1-x)^{3/2}}{\sqrt{1+x}} - 3\sqrt{1-x}\sqrt{1+x} - 3 \sin^{-1}(x)
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 37, normalized size = 0.90

$$\frac{(1-x)^{5/2} {}_2F_1\left(\frac{3}{2}, \frac{5}{2}; \frac{7}{2}; \frac{1-x}{2}\right)}{5\sqrt{2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(3/2)/(1 + x)^(3/2), x]

[Out] -1/5*((1 - x)^(5/2)*Hypergeometric2F1[3/2, 5/2, 7/2, (1 - x)/2])/Sqrt[2]

fricas [A] time = 0.43, size = 53, normalized size = 1.29

$$\frac{(x+5)\sqrt{x+1}\sqrt{-x+1} - 6(x+1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) + 5x+5}{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)/(1+x)^(3/2), x, algorithm="fricas")

[Out] -((x + 5)*sqrt(x + 1)*sqrt(-x + 1) - 6*(x + 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) + 5*x + 5)/(x + 1)

giac [B] time = 0.73, size = 70, normalized size = 1.71

$$-\sqrt{x+1}\sqrt{-x+1} + \frac{2(\sqrt{2}-\sqrt{-x+1})}{\sqrt{x+1}} - \frac{2\sqrt{x+1}}{\sqrt{2}-\sqrt{-x+1}} - 6\arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)/(1+x)^(3/2),x, algorithm="giac")

[Out] -sqrt(x + 1)*sqrt(-x + 1) + 2*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) - 2*sqrt(x + 1)/(sqrt(2) - sqrt(-x + 1)) - 6*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.02, size = 71, normalized size = 1.73

$$-\frac{3\sqrt{(x+1)(-x+1)}\arcsin(x)}{\sqrt{x+1}\sqrt{-x+1}} + \frac{(x^2+4x-5)\sqrt{(x+1)(-x+1)}}{\sqrt{-(x+1)(x-1)}\sqrt{-x+1}\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(3/2)/(x+1)^(3/2),x)

[Out] (x^2+4*x-5)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)/(x+1)^(1/2)-3*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.86, size = 41, normalized size = 1.00

$$\frac{(-x^2+1)^{\frac{3}{2}}}{x^2+2x+1} - \frac{6\sqrt{-x^2+1}}{x+1} - 3\arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)/(1+x)^(3/2),x, algorithm="maxima")

[Out] (-x^2 + 1)^(3/2)/(x^2 + 2*x + 1) - 6*sqrt(-x^2 + 1)/(x + 1) - 3*arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(1-x)^{3/2}}{(x+1)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(3/2)/(x + 1)^(3/2),x)

[Out] int((1 - x)^(3/2)/(x + 1)^(3/2), x)

sympy [A] time = 2.48, size = 133, normalized size = 3.24

$$\begin{cases} 6i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{i(x+1)^{\frac{3}{2}}}{\sqrt{x-1}} - \frac{2i\sqrt{x+1}}{\sqrt{x-1}} + \frac{8i}{\sqrt{x-1}\sqrt{x+1}} & \text{for } \frac{|x+1|}{2} > 1 \\ -6 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{(x+1)^{\frac{3}{2}}}{\sqrt{1-x}} + \frac{2\sqrt{x+1}}{\sqrt{1-x}} - \frac{8}{\sqrt{1-x}\sqrt{x+1}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(3/2)/(1+x)**(3/2),x)`

[Out] `Piecewise((6*I*acosh(sqrt(2)*sqrt(x + 1)/2) - I*(x + 1)**(3/2)/sqrt(x - 1) - 2*I*sqrt(x + 1)/sqrt(x - 1) + 8*I/(sqrt(x - 1)*sqrt(x + 1)), Abs(x + 1)/2 > 1), (-6*asin(sqrt(2)*sqrt(x + 1)/2) + (x + 1)**(3/2)/sqrt(1 - x) + 2*sqrt(x + 1)/sqrt(1 - x) - 8/(sqrt(1 - x)*sqrt(x + 1)), True))`

$$3.1119 \quad \int \frac{\sqrt{1-x}}{(1+x)^{3/2}} dx$$

Optimal. Leaf size=23

$$-\frac{2\sqrt{1-x}}{\sqrt{x+1}} - \sin^{-1}(x)$$

[Out] $-\arcsin(x) - 2*(1-x)^{(1/2)}/(1+x)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {47, 41, 216}

$$-\frac{2\sqrt{1-x}}{\sqrt{x+1}} - \sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[1 - x]/(1 + x)^(3/2), x]`

[Out] `(-2*Sqrt[1 - x])/Sqrt[1 + x] - ArcSin[x]`

Rule 41

`Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))`

Rule 47

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]`

Rule 216

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]`

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{1-x}}{(1+x)^{3/2}} dx &= -\frac{2\sqrt{1-x}}{\sqrt{1+x}} - \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
&= -\frac{2\sqrt{1-x}}{\sqrt{1+x}} - \int \frac{1}{\sqrt{1-x^2}} dx \\
&= -\frac{2\sqrt{1-x}}{\sqrt{1+x}} - \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.04, size = 34, normalized size = 1.48

$$2 \left(\frac{x-1}{\sqrt{1-x^2}} + \sin^{-1} \left(\frac{\sqrt{1-x}}{\sqrt{2}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[1 - x]/(1 + x)^(3/2), x]

[Out] 2*((-1 + x)/Sqrt[1 - x^2] + ArcSin[Sqrt[1 - x]/Sqrt[2]])

fricas [B] time = 0.47, size = 50, normalized size = 2.17

$$\frac{2 \left((x+1) \arctan \left(\frac{\sqrt{x+1} \sqrt{-x+1} - 1}{x} \right) - x - \sqrt{x+1} \sqrt{-x+1} - 1 \right)}{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)/(1+x)^(3/2), x, algorithm="fricas")

[Out] 2*((x + 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) - x - sqrt(x + 1)*sqrt(-x + 1) - 1)/(x + 1)

giac [B] time = 0.69, size = 55, normalized size = 2.39

$$\frac{\sqrt{2} - \sqrt{-x+1}}{\sqrt{x+1}} - \frac{\sqrt{x+1}}{\sqrt{2} - \sqrt{-x+1}} - 2 \arcsin \left(\frac{1}{2} \sqrt{2} \sqrt{x+1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)/(1+x)^(3/2), x, algorithm="giac")

[Out] (sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) - sqrt(x + 1)/(sqrt(2) - sqrt(-x + 1)) - 2*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.02, size = 67, normalized size = 2.91

$$-\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1} \sqrt{-x+1}} + \frac{2(x-1) \sqrt{(x+1)(-x+1)}}{\sqrt{-(x+1)(x-1)} \sqrt{-x+1} \sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(1/2)/(x+1)^(3/2),x)

[Out] 2*(x-1)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)/(x+1)^(1/2)-((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 2.86, size = 21, normalized size = 0.91

$$-\frac{2\sqrt{-x^2+1}}{x+1} - \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)/(1+x)^(3/2),x, algorithm="maxima")

[Out] -2*sqrt(-x^2 + 1)/(x + 1) - arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{\sqrt{1-x}}{(x+1)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(1/2)/(x + 1)^(3/2),x)

[Out] int((1 - x)^(1/2)/(x + 1)^(3/2), x)

sympy [B] time = 1.54, size = 104, normalized size = 4.52

$$\begin{cases} 2i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{2i\sqrt{x+1}}{\sqrt{x-1}} + \frac{4i}{\sqrt{x-1}\sqrt{x+1}} & \text{for } \frac{|x+1|}{2} > 1 \\ -2 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{2\sqrt{x+1}}{\sqrt{1-x}} - \frac{4}{\sqrt{1-x}\sqrt{x+1}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(1/2)/(1+x)**(3/2),x)

[Out] Piecewise((2*I*acosh(sqrt(2)*sqrt(x + 1)/2) - 2*I*sqrt(x + 1)/sqrt(x - 1) + 4*I/(sqrt(x - 1)*sqrt(x + 1)), Abs(x + 1)/2 > 1), (-2*asin(sqrt(2)*sqrt(x + 1)/2) + 2*sqrt(x + 1)/sqrt(1 - x) - 4/(sqrt(1 - x)*sqrt(x + 1)), True))

$$3.1120 \quad \int \frac{1}{\sqrt{1-x}(1+x)^{3/2}} dx$$

Optimal. Leaf size=18

$$-\frac{\sqrt{1-x}}{\sqrt{x+1}}$$

[Out] $-(1-x)^{(1/2)}/(1+x)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {37}

$$-\frac{\sqrt{1-x}}{\sqrt{x+1}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[1 - x]*(1 + x)^(3/2)), x]

[Out] -(Sqrt[1 - x]/Sqrt[1 + x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt{1-x}(1+x)^{3/2}} dx = -\frac{\sqrt{1-x}}{\sqrt{1+x}}$$

Mathematica [A] time = 0.00, size = 18, normalized size = 1.00

$$-\frac{\sqrt{1-x}}{\sqrt{x+1}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[1 - x]*(1 + x)^(3/2)), x]

[Out] $-(\text{Sqrt}[1 - x]/\text{Sqrt}[1 + x])$

fricas [A] time = 0.45, size = 23, normalized size = 1.28

$$-\frac{x + \sqrt{x+1}\sqrt{-x+1} + 1}{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(1/2)/(1+x)^(3/2),x, algorithm="fricas")`

[Out] $-(x + \text{sqrt}(x + 1)*\text{sqrt}(-x + 1) + 1)/(x + 1)$

giac [B] time = 0.65, size = 43, normalized size = 2.39

$$\frac{\sqrt{2} - \sqrt{-x+1}}{2\sqrt{x+1}} - \frac{\sqrt{x+1}}{2(\sqrt{2} - \sqrt{-x+1})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(1/2)/(1+x)^(3/2),x, algorithm="giac")`

[Out] $1/2*(\text{sqrt}(2) - \text{sqrt}(-x + 1))/\text{sqrt}(x + 1) - 1/2*\text{sqrt}(x + 1)/(\text{sqrt}(2) - \text{sqrt}(-x + 1))$

maple [A] time = 0.00, size = 15, normalized size = 0.83

$$-\frac{\sqrt{-x+1}}{\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-x+1)^(1/2)/(x+1)^(3/2),x)`

[Out] $-(-x+1)^(1/2)/(x+1)^(1/2)$

maxima [A] time = 2.94, size = 16, normalized size = 0.89

$$-\frac{\sqrt{-x^2+1}}{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(1/2)/(1+x)^(3/2),x, algorithm="maxima")`

[Out] $-\text{sqrt}(-x^2 + 1)/(x + 1)$

mupad [B] time = 0.36, size = 14, normalized size = 0.78

$$-\frac{\sqrt{1-x}}{\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((1-x)^(1/2)*(x+1)^(3/2)),x)`

[Out] `-(1-x)^(1/2)/(x+1)^(1/2)`

sympy [A] time = 1.20, size = 29, normalized size = 1.61

$$\begin{cases} -\sqrt{-1 + \frac{2}{x+1}} & \text{for } \frac{2}{|x+1|} > 1 \\ -i\sqrt{1 - \frac{2}{x+1}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)**(1/2)/(1+x)**(3/2),x)`

[Out] `Piecewise((-sqrt(-1 + 2/(x + 1)), 2/Abs(x + 1) > 1), (-I*sqrt(1 - 2/(x + 1)), True))`

$$3.1121 \quad \int \frac{1}{(1-x)^{3/2}(1+x)^{3/2}} dx$$

Optimal. Leaf size=18

$$\frac{x}{\sqrt{1-x}\sqrt{x+1}}$$

[Out] $x/(1-x)^{(1/2)}/(1+x)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {39}

$$\frac{x}{\sqrt{1-x}\sqrt{x+1}}$$

Antiderivative was successfully verified.

[In] `Int[1/((1 - x)^(3/2)*(1 + x)^(3/2)),x]`

[Out] `x/(Sqrt[1 - x]*Sqrt[1 + x])`

Rule 39

`Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] :> Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]`

Rubi steps

$$\int \frac{1}{(1-x)^{3/2}(1+x)^{3/2}} dx = \frac{x}{\sqrt{1-x}\sqrt{1+x}}$$

Mathematica [A] time = 0.00, size = 13, normalized size = 0.72

$$\frac{x}{\sqrt{1-x^2}}$$

Antiderivative was successfully verified.

[In] `Integrate[1/((1 - x)^(3/2)*(1 + x)^(3/2)),x]`

[Out] `x/Sqrt[1 - x^2]`

fricas [A] time = 0.43, size = 22, normalized size = 1.22

$$-\frac{\sqrt{x+1}x\sqrt{-x+1}}{x^2-1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(3/2)/(1+x)^(3/2),x, algorithm="fricas")

[Out] -sqrt(x + 1)*x*sqrt(-x + 1)/(x^2 - 1)

giac [B] time = 0.72, size = 62, normalized size = 3.44

$$\frac{\sqrt{2}-\sqrt{-x+1}}{4\sqrt{x+1}}-\frac{\sqrt{x+1}\sqrt{-x+1}}{2(x-1)}-\frac{\sqrt{x+1}}{4(\sqrt{2}-\sqrt{-x+1})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(3/2)/(1+x)^(3/2),x, algorithm="giac")

[Out] 1/4*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) - 1/2*sqrt(x + 1)*sqrt(-x + 1)/(x - 1) - 1/4*sqrt(x + 1)/(sqrt(2) - sqrt(-x + 1))

maple [A] time = 0.00, size = 15, normalized size = 0.83

$$\frac{x}{\sqrt{-x+1}\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+1)^(3/2)/(x+1)^(3/2),x)

[Out] x/(-x+1)^(1/2)/(x+1)^(1/2)

maxima [A] time = 1.34, size = 11, normalized size = 0.61

$$\frac{x}{\sqrt{-x^2+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(3/2)/(1+x)^(3/2),x, algorithm="maxima")

[Out] x/sqrt(-x^2 + 1)

mupad [B] time = 0.31, size = 14, normalized size = 0.78

$$\frac{x}{\sqrt{1-x}\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((1 - x)^(3/2)*(x + 1)^(3/2)),x)
```

```
[Out] x/((1 - x)^(1/2)*(x + 1)^(1/2))
```

sympy [A] time = 1.86, size = 65, normalized size = 3.61

$$\begin{cases} \frac{1}{\sqrt{-1+\frac{2}{x+1}}} - \frac{1}{\sqrt{-1+\frac{2}{x+1}}(x+1)} & \text{for } \frac{2}{|x+1|} > 1 \\ -\frac{i\sqrt{1-\frac{2}{x+1}}(x+1)}{x-1} + \frac{i\sqrt{1-\frac{2}{x+1}}}{x-1} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(1-x)**(3/2)/(1+x)**(3/2),x)
```

```
[Out] Piecewise((1/sqrt(-1 + 2/(x + 1)) - 1/(sqrt(-1 + 2/(x + 1))*(x + 1)), 2/Abs
(x + 1) > 1), (-I*sqrt(1 - 2/(x + 1))*(x + 1)/(x - 1) + I*sqrt(1 - 2/(x + 1
)))/(x - 1), True))
```

$$3.1122 \quad \int \frac{1}{(1-x)^{5/2}(1+x)^{3/2}} dx$$

Optimal. Leaf size=42

$$\frac{2x}{3\sqrt{1-x}\sqrt{x+1}} + \frac{1}{3(1-x)^{3/2}\sqrt{x+1}}$$

[Out] 1/3/(1-x)^(3/2)/(1+x)^(1/2)+2/3*x/(1-x)^(1/2)/(1+x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 39}

$$\frac{2x}{3\sqrt{1-x}\sqrt{x+1}} + \frac{1}{3(1-x)^{3/2}\sqrt{x+1}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - x)^(5/2)*(1 + x)^(3/2)), x]

[Out] 1/(3*(1 - x)^(3/2)*Sqrt[1 + x]) + (2*x)/(3*Sqrt[1 - x]*Sqrt[1 + x])

Rule 39

Int[1/(((a_) + (b_)*(x_))^(3/2)*((c_) + (d_)*(x_))^(3/2)), x_Symbol] := Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 45

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[n] && (LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(1-x)^{5/2}(1+x)^{3/2}} dx = \frac{1}{3(1-x)^{3/2}\sqrt{1+x}} + \frac{2}{3} \int \frac{1}{(1-x)^{3/2}(1+x)^{3/2}} dx$$

$$= \frac{1}{3(1-x)^{3/2}\sqrt{1+x}} + \frac{2x}{3\sqrt{1-x}\sqrt{1+x}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 0.71

$$\frac{2x^2 - 2x - 1}{3(x-1)\sqrt{1-x^2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(5/2)*(1+x)^(3/2)),x]

[Out] (-1 - 2*x + 2*x^2)/(3*(-1 + x)*Sqrt[1 - x^2])

fricas [A] time = 0.44, size = 54, normalized size = 1.29

$$\frac{x^3 - x^2 - (2x^2 - 2x - 1)\sqrt{x+1}\sqrt{-x+1} - x + 1}{3(x^3 - x^2 - x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(5/2)/(1+x)^(3/2),x, algorithm="fricas")

[Out] 1/3*(x^3 - x^2 - (2*x^2 - 2*x - 1)*sqrt(x + 1)*sqrt(-x + 1) - x + 1)/(x^3 - x^2 - x + 1)

giac [B] time = 0.70, size = 67, normalized size = 1.60

$$\frac{\sqrt{2} - \sqrt{-x+1}}{8\sqrt{x+1}} - \frac{(5x-7)\sqrt{x+1}\sqrt{-x+1}}{12(x-1)^2} - \frac{\sqrt{x+1}}{8(\sqrt{2} - \sqrt{-x+1})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(5/2)/(1+x)^(3/2),x, algorithm="giac")

[Out] 1/8*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) - 1/12*(5*x - 7)*sqrt(x + 1)*sqrt(-x + 1)/(x - 1)^2 - 1/8*sqrt(x + 1)/(sqrt(2) - sqrt(-x + 1))

maple [A] time = 0.00, size = 25, normalized size = 0.60

$$-\frac{2x^2 - 2x - 1}{3\sqrt{x+1}(-x+1)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-x+1)^(5/2)/(x+1)^(3/2),x)`

[Out] `-1/3*(2*x^2-2*x-1)/(x+1)^(1/2)/(-x+1)^(3/2)`

maxima [A] time = 1.42, size = 40, normalized size = 0.95

$$\frac{2x}{3\sqrt{-x^2+1}} - \frac{1}{3\left(\sqrt{-x^2+1}x - \sqrt{-x^2+1}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(5/2)/(1+x)^(3/2),x, algorithm="maxima")`

[Out] `2/3*x/sqrt(-x^2+1) - 1/3/(sqrt(-x^2+1)*x - sqrt(-x^2+1))`

mupad [B] time = 0.32, size = 42, normalized size = 1.00

$$\frac{2x\sqrt{1-x} + \sqrt{1-x} - 2x^2\sqrt{1-x}}{3(x-1)^2\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((1-x)^(5/2)*(x+1)^(3/2)),x)`

[Out] `(2*x*(1-x)^(1/2) + (1-x)^(1/2) - 2*x^2*(1-x)^(1/2))/(3*(x-1)^2*(x+1)^(1/2))`

sympy [B] time = 5.28, size = 158, normalized size = 3.76

$$\begin{cases} -\frac{2\sqrt{-1+\frac{2}{x+1}}(x+1)^2}{-12x+3(x+1)^2} + \frac{6\sqrt{-1+\frac{2}{x+1}}(x+1)}{-12x+3(x+1)^2} - \frac{3\sqrt{-1+\frac{2}{x+1}}}{-12x+3(x+1)^2} & \text{for } \frac{2}{|x+1|} > 1 \\ -\frac{2i\sqrt{1-\frac{2}{x+1}}(x+1)^2}{-12x+3(x+1)^2} + \frac{6i\sqrt{1-\frac{2}{x+1}}(x+1)}{-12x+3(x+1)^2} - \frac{3i\sqrt{1-\frac{2}{x+1}}}{-12x+3(x+1)^2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)**(5/2)/(1+x)**(3/2),x)`

[Out] `Piecewise((-2*sqrt(-1+2/(x+1))*(x+1)**2/(-12*x+3*(x+1)**2) + 6*sqrt(-1+2/(x+1))*(x+1)/(-12*x+3*(x+1)**2) - 3*sqrt(-1+2/(x+1))/(-12*x+3*(x+1)**2), 2/Abs(x+1) > 1), (-2*I*sqrt(1-2/(x+1))*(x+1)**2/(-12*x+3*(x+1)**2) + 6*I*sqrt(1-2/(x+1))*(x+1)/(-12*x+3*(x+1)**2) - 3*I*sqrt(1-2/(x+1))/(-12*x+3*(x+1)**2), True))`

$$3.1123 \quad \int \frac{1}{(1-x)^{7/2}(1+x)^{3/2}} dx$$

Optimal. Leaf size=62

$$\frac{2x}{5\sqrt{1-x}\sqrt{x+1}} + \frac{1}{5(1-x)^{3/2}\sqrt{x+1}} + \frac{1}{5(1-x)^{5/2}\sqrt{x+1}}$$

[Out] 1/5/(1-x)^(5/2)/(1+x)^(1/2)+1/5/(1-x)^(3/2)/(1+x)^(1/2)+2/5*x/(1-x)^(1/2)/(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 62, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 39}

$$\frac{2x}{5\sqrt{1-x}\sqrt{x+1}} + \frac{1}{5(1-x)^{3/2}\sqrt{x+1}} + \frac{1}{5(1-x)^{5/2}\sqrt{x+1}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - x)^(7/2)*(1 + x)^(3/2)),x]

[Out] 1/(5*(1 - x)^(5/2)*Sqrt[1 + x]) + 1/(5*(1 - x)^(3/2)*Sqrt[1 + x]) + (2*x)/(5*Sqrt[1 - x]*Sqrt[1 + x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] :> Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(1-x)^{7/2}(1+x)^{3/2}} dx &= \frac{1}{5(1-x)^{5/2}\sqrt{1+x}} + \frac{3}{5} \int \frac{1}{(1-x)^{5/2}(1+x)^{3/2}} dx \\
&= \frac{1}{5(1-x)^{5/2}\sqrt{1+x}} + \frac{1}{5(1-x)^{3/2}\sqrt{1+x}} + \frac{2}{5} \int \frac{1}{(1-x)^{3/2}(1+x)^{3/2}} dx \\
&= \frac{1}{5(1-x)^{5/2}\sqrt{1+x}} + \frac{1}{5(1-x)^{3/2}\sqrt{1+x}} + \frac{2x}{5\sqrt{1-x}\sqrt{1+x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.53

$$\frac{2x^3 - 4x^2 + x + 2}{5(x-1)^2\sqrt{1-x^2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(7/2)*(1+x)^(3/2)),x]

[Out] (2 + x - 4*x^2 + 2*x^3)/(5*(-1 + x)^2*Sqrt[1 - x^2])

fricas [A] time = 0.43, size = 59, normalized size = 0.95

$$\frac{2x^4 - 4x^3 - (2x^3 - 4x^2 + x + 2)\sqrt{x+1}\sqrt{-x+1} + 4x - 2}{5(x^4 - 2x^3 + 2x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(7/2)/(1+x)^(3/2),x, algorithm="fricas")

[Out] 1/5*(2*x^4 - 4*x^3 - (2*x^3 - 4*x^2 + x + 2)*sqrt(x + 1)*sqrt(-x + 1) + 4*x - 2)/(x^4 - 2*x^3 + 2*x - 1)

giac [A] time = 0.66, size = 73, normalized size = 1.18

$$\frac{\sqrt{2} - \sqrt{-x+1}}{16\sqrt{x+1}} - \frac{\sqrt{x+1}}{16(\sqrt{2} - \sqrt{-x+1})} - \frac{((11x-39)(x+1)+60)\sqrt{x+1}\sqrt{-x+1}}{40(x-1)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(7/2)/(1+x)^(3/2),x, algorithm="giac")

[Out] 1/16*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) - 1/16*sqrt(x + 1)/(sqrt(2) - sqrt(-x + 1)) - 1/40*((11*x - 39)*(x + 1) + 60)*sqrt(x + 1)*sqrt(-x + 1)/(x - 1)^3

maple [A] time = 0.00, size = 28, normalized size = 0.45

$$\frac{2x^3 - 4x^2 + x + 2}{5\sqrt{x+1}(-x+1)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-x+1)^(7/2)/(x+1)^(3/2),x)`

[Out] `1/5*(2*x^3-4*x^2+x+2)/(x+1)^(1/2)/(-x+1)^(5/2)`

maxima [A] time = 1.35, size = 79, normalized size = 1.27

$$\frac{2x}{5\sqrt{-x^2+1}} + \frac{1}{5\left(\sqrt{-x^2+1}x^2 - 2\sqrt{-x^2+1}x + \sqrt{-x^2+1}\right)} - \frac{1}{5\left(\sqrt{-x^2+1}x - \sqrt{-x^2+1}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(7/2)/(1+x)^(3/2),x, algorithm="maxima")`

[Out] `2/5*x/sqrt(-x^2+1) + 1/5/(sqrt(-x^2+1)*x^2 - 2*sqrt(-x^2+1)*x + sqrt(-x^2+1)) - 1/5/(sqrt(-x^2+1)*x - sqrt(-x^2+1))`

mupad [B] time = 0.34, size = 55, normalized size = 0.89

$$\frac{x\sqrt{1-x} + 2\sqrt{1-x} - 4x^2\sqrt{1-x} + 2x^3\sqrt{1-x}}{5(x-1)^3\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((1-x)^(7/2)*(x+1)^(3/2)),x)`

[Out] `-(x*(1-x)^(1/2) + 2*(1-x)^(1/2) - 4*x^2*(1-x)^(1/2) + 2*x^3*(1-x)^(1/2))/(5*(x-1)^3*(x+1)^(1/2))`

sympy [B] time = 16.83, size = 282, normalized size = 4.55

$$\left\{ \begin{array}{l} \frac{2\sqrt{-1+\frac{2}{x+1}}(x+1)^3}{-60x-5(x+1)^3+30(x+1)^2-20} - \frac{10\sqrt{-1+\frac{2}{x+1}}(x+1)^2}{-60x-5(x+1)^3+30(x+1)^2-20} + \frac{15\sqrt{-1+\frac{2}{x+1}}(x+1)}{-60x-5(x+1)^3+30(x+1)^2-20} - \frac{5\sqrt{-1+\frac{2}{x+1}}}{-60x-5(x+1)^3+30(x+1)^2-20} \quad \text{for } \frac{2}{|x+1|} > \\ \frac{2i\sqrt{1-\frac{2}{x+1}}(x+1)^3}{-60x-5(x+1)^3+30(x+1)^2-20} - \frac{10i\sqrt{1-\frac{2}{x+1}}(x+1)^2}{-60x-5(x+1)^3+30(x+1)^2-20} + \frac{15i\sqrt{1-\frac{2}{x+1}}(x+1)}{-60x-5(x+1)^3+30(x+1)^2-20} - \frac{5i\sqrt{1-\frac{2}{x+1}}}{-60x-5(x+1)^3+30(x+1)^2-20} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)**(7/2)/(1+x)**(3/2),x)

[Out] Piecewise((2*sqrt(-1 + 2/(x + 1))*(x + 1)**3/(-60*x - 5*(x + 1)**3 + 30*(x + 1)**2 - 20) - 10*sqrt(-1 + 2/(x + 1))*(x + 1)**2/(-60*x - 5*(x + 1)**3 + 30*(x + 1)**2 - 20) + 15*sqrt(-1 + 2/(x + 1))*(x + 1)/(-60*x - 5*(x + 1)**3 + 30*(x + 1)**2 - 20) - 5*sqrt(-1 + 2/(x + 1))/(-60*x - 5*(x + 1)**3 + 30*(x + 1)**2 - 20), 2/Abs(x + 1) > 1), (2*I*sqrt(1 - 2/(x + 1))*(x + 1)**3/(-60*x - 5*(x + 1)**3 + 30*(x + 1)**2 - 20) - 10*I*sqrt(1 - 2/(x + 1))*(x + 1)**2/(-60*x - 5*(x + 1)**3 + 30*(x + 1)**2 - 20) + 15*I*sqrt(1 - 2/(x + 1))*(x + 1)/(-60*x - 5*(x + 1)**3 + 30*(x + 1)**2 - 20) - 5*I*sqrt(1 - 2/(x + 1))/(-60*x - 5*(x + 1)**3 + 30*(x + 1)**2 - 20), True))

$$3.1124 \quad \int \frac{1}{(1-x)^{9/2}(1+x)^{3/2}} dx$$

Optimal. Leaf size=82

$$\frac{8x}{35\sqrt{1-x}\sqrt{x+1}} + \frac{4}{35(1-x)^{3/2}\sqrt{x+1}} + \frac{4}{35(1-x)^{5/2}\sqrt{x+1}} + \frac{1}{7(1-x)^{7/2}\sqrt{x+1}}$$

[Out] $1/7/(1-x)^{(7/2)}/(1+x)^{(1/2)}+4/35/(1-x)^{(5/2)}/(1+x)^{(1/2)}+4/35/(1-x)^{(3/2)}/(1+x)^{(1/2)}+8/35*x/(1-x)^{(1/2)}/(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 39}

$$\frac{8x}{35\sqrt{1-x}\sqrt{x+1}} + \frac{4}{35(1-x)^{3/2}\sqrt{x+1}} + \frac{4}{35(1-x)^{5/2}\sqrt{x+1}} + \frac{1}{7(1-x)^{7/2}\sqrt{x+1}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - x)^(9/2)*(1 + x)^(3/2)),x]

[Out] $1/(7*(1-x)^{(7/2)}*\text{Sqrt}[1+x]) + 4/(35*(1-x)^{(5/2)}*\text{Sqrt}[1+x]) + 4/(35*(1-x)^{(3/2)}*\text{Sqrt}[1+x]) + (8*x)/(35*\text{Sqrt}[1-x]*\text{Sqrt}[1+x])$

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] :> Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(1-x)^{9/2}(1+x)^{3/2}} dx &= \frac{1}{7(1-x)^{7/2}\sqrt{1+x}} + \frac{4}{7} \int \frac{1}{(1-x)^{7/2}(1+x)^{3/2}} dx \\
&= \frac{1}{7(1-x)^{7/2}\sqrt{1+x}} + \frac{4}{35(1-x)^{5/2}\sqrt{1+x}} + \frac{12}{35} \int \frac{1}{(1-x)^{5/2}(1+x)^{3/2}} dx \\
&= \frac{1}{7(1-x)^{7/2}\sqrt{1+x}} + \frac{4}{35(1-x)^{5/2}\sqrt{1+x}} + \frac{4}{35(1-x)^{3/2}\sqrt{1+x}} + \frac{8}{35} \int \frac{1}{(1-x)^{3/2}(1+x)} dx \\
&= \frac{1}{7(1-x)^{7/2}\sqrt{1+x}} + \frac{4}{35(1-x)^{5/2}\sqrt{1+x}} + \frac{4}{35(1-x)^{3/2}\sqrt{1+x}} + \frac{8x}{35\sqrt{1-x}\sqrt{1+x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 0.49

$$\frac{8x^4 - 24x^3 + 20x^2 + 4x - 13}{35(x-1)^3\sqrt{1-x^2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(9/2)*(1+x)^(3/2)),x]

[Out] (-13 + 4*x + 20*x^2 - 24*x^3 + 8*x^4)/(35*(-1 + x)^3*Sqrt[1 - x^2])

fricas [A] time = 0.43, size = 86, normalized size = 1.05

$$\frac{13x^5 - 39x^4 + 26x^3 + 26x^2 - (8x^4 - 24x^3 + 20x^2 + 4x - 13)\sqrt{x+1}\sqrt{-x+1} - 39x + 13}{35(x^5 - 3x^4 + 2x^3 + 2x^2 - 3x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(9/2)/(1+x)^(3/2),x, algorithm="fricas")

[Out] 1/35*(13*x^5 - 39*x^4 + 26*x^3 + 26*x^2 - (8*x^4 - 24*x^3 + 20*x^2 + 4*x - 13)*sqrt(x + 1)*sqrt(-x + 1) - 39*x + 13)/(x^5 - 3*x^4 + 2*x^3 + 2*x^2 - 3*x + 1)

giac [A] time = 0.70, size = 79, normalized size = 0.96

$$\frac{\sqrt{2} - \sqrt{-x+1}}{32\sqrt{x+1}} - \frac{\sqrt{x+1}}{32(\sqrt{2} - \sqrt{-x+1})} - \frac{(((93x - 523)(x + 1) + 1400)(x + 1) - 1120)\sqrt{x+1}\sqrt{-x+1}}{560(x-1)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(9/2)/(1+x)^(3/2),x, algorithm="giac")

[Out] $1/32*(\sqrt{2} - \sqrt{-x + 1})/\sqrt{x + 1} - 1/32*\sqrt{x + 1}/(\sqrt{2} - \sqrt{-x + 1}) - 1/560*((93*x - 523)*(x + 1) + 1400)*(x + 1) - 1120)*\sqrt{x + 1}*\sqrt{-x + 1}/(x - 1)^4$

maple [A] time = 0.00, size = 35, normalized size = 0.43

$$\frac{8x^4 - 24x^3 + 20x^2 + 4x - 13}{35\sqrt{x+1}(-x+1)^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-x+1)^(9/2)/(x+1)^(3/2),x)`

[Out] $-1/35*(8*x^4-24*x^3+20*x^2+4*x-13)/(x+1)^(1/2)/(-x+1)^(7/2)$

maxima [B] time = 1.38, size = 134, normalized size = 1.63

$$\frac{8x}{35\sqrt{-x^2+1}} - \frac{1}{7\left(\sqrt{-x^2+1}x^3 - 3\sqrt{-x^2+1}x^2 + 3\sqrt{-x^2+1}x - \sqrt{-x^2+1}\right)} + \frac{4}{35\left(\sqrt{-x^2+1}x^2 - 2\sqrt{-x^2+1}x + \sqrt{-x^2+1}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(9/2)/(1+x)^(3/2),x, algorithm="maxima")`

[Out] $8/35*x/\sqrt{-x^2 + 1} - 1/7/(\sqrt{-x^2 + 1}*x^3 - 3*\sqrt{-x^2 + 1}*x^2 + 3*\sqrt{-x^2 + 1}*x - \sqrt{-x^2 + 1}) + 4/35/(\sqrt{-x^2 + 1}*x^2 - 2*\sqrt{-x^2 + 1}*x + \sqrt{-x^2 + 1}) - 4/35/(\sqrt{-x^2 + 1}*x - \sqrt{-x^2 + 1})$

mupad [B] time = 0.36, size = 68, normalized size = 0.83

$$\frac{4x\sqrt{1-x} - 13\sqrt{1-x} + 20x^2\sqrt{1-x} - 24x^3\sqrt{1-x} + 8x^4\sqrt{1-x}}{35(x-1)^4\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((1-x)^(9/2)*(x+1)^(3/2)),x)`

[Out] $-(4*x*(1-x)^(1/2) - 13*(1-x)^(1/2) + 20*x^2*(1-x)^(1/2) - 24*x^3*(1-x)^(1/2) + 8*x^4*(1-x)^(1/2))/(35*(x-1)^4*(x+1)^(1/2))$

sympy [B] time = 44.94, size = 423, normalized size = 5.16

$$\left\{ \begin{array}{l} \frac{8\sqrt{-1+\frac{2}{x+1}}(x+1)^4}{-1120x+35(x+1)^4-280(x+1)^3+840(x+1)^2-560} + \frac{56\sqrt{-1+\frac{2}{x+1}}(x+1)^3}{-1120x+35(x+1)^4-280(x+1)^3+840(x+1)^2-560} - \frac{140\sqrt{-1+\frac{2}{x+1}}(x+1)^2}{-1120x+35(x+1)^4-280(x+1)^3+840(x+1)^2-560} \\ \frac{8i\sqrt{1-\frac{2}{x+1}}(x+1)^4}{-1120x+35(x+1)^4-280(x+1)^3+840(x+1)^2-560} + \frac{56i\sqrt{1-\frac{2}{x+1}}(x+1)^3}{-1120x+35(x+1)^4-280(x+1)^3+840(x+1)^2-560} - \frac{140i\sqrt{1-\frac{2}{x+1}}(x+1)^2}{-1120x+35(x+1)^4-280(x+1)^3+840(x+1)^2-560} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)**(9/2)/(1+x)**(3/2),x)`

[Out] `Piecewise((-8*sqrt(-1 + 2/(x + 1))*(x + 1)**4/(-1120*x + 35*(x + 1)**4 - 280*(x + 1)**3 + 840*(x + 1)**2 - 560) + 56*sqrt(-1 + 2/(x + 1))*(x + 1)**3/(-1120*x + 35*(x + 1)**4 - 280*(x + 1)**3 + 840*(x + 1)**2 - 560) - 140*sqrt(-1 + 2/(x + 1))*(x + 1)**2/(-1120*x + 35*(x + 1)**4 - 280*(x + 1)**3 + 840*(x + 1)**2 - 560) + 140*sqrt(-1 + 2/(x + 1))*(x + 1)/(-1120*x + 35*(x + 1)**4 - 280*(x + 1)**3 + 840*(x + 1)**2 - 560) - 35*sqrt(-1 + 2/(x + 1))/(-1120*x + 35*(x + 1)**4 - 280*(x + 1)**3 + 840*(x + 1)**2 - 560), 2/Abs(x + 1) > 1), (-8*I*sqrt(1 - 2/(x + 1))*(x + 1)**4/(-1120*x + 35*(x + 1)**4 - 280*(x + 1)**3 + 840*(x + 1)**2 - 560) + 56*I*sqrt(1 - 2/(x + 1))*(x + 1)**3/(-1120*x + 35*(x + 1)**4 - 280*(x + 1)**3 + 840*(x + 1)**2 - 560) - 140*I*sqrt(1 - 2/(x + 1))*(x + 1)**2/(-1120*x + 35*(x + 1)**4 - 280*(x + 1)**3 + 840*(x + 1)**2 - 560) + 140*I*sqrt(1 - 2/(x + 1))*(x + 1)/(-1120*x + 35*(x + 1)**4 - 280*(x + 1)**3 + 840*(x + 1)**2 - 560) - 35*I*sqrt(1 - 2/(x + 1))/(-1120*x + 35*(x + 1)**4 - 280*(x + 1)**3 + 840*(x + 1)**2 - 560), True))`

$$3.1125 \quad \int \frac{1}{(1-x)^{11/2}(1+x)^{3/2}} dx$$

Optimal. Leaf size=102

$$\frac{8x}{63\sqrt{1-x}\sqrt{x+1}} + \frac{4}{63(1-x)^{3/2}\sqrt{x+1}} + \frac{4}{63(1-x)^{5/2}\sqrt{x+1}} + \frac{5}{63(1-x)^{7/2}\sqrt{x+1}} + \frac{1}{9(1-x)^{9/2}\sqrt{x+1}}$$

[Out] $1/9/(1-x)^{(9/2)}/(1+x)^{(1/2)}+5/63/(1-x)^{(7/2)}/(1+x)^{(1/2)}+4/63/(1-x)^{(5/2)}/(1+x)^{(1/2)}+4/63/(1-x)^{(3/2)}/(1+x)^{(1/2)}+8/63*x/(1-x)^{(1/2)}/(1+x)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 39}

$$\frac{8x}{63\sqrt{1-x}\sqrt{x+1}} + \frac{4}{63(1-x)^{3/2}\sqrt{x+1}} + \frac{4}{63(1-x)^{5/2}\sqrt{x+1}} + \frac{5}{63(1-x)^{7/2}\sqrt{x+1}} + \frac{1}{9(1-x)^{9/2}\sqrt{x+1}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - x)^(11/2)*(1 + x)^(3/2)),x]

[Out] $1/(9*(1-x)^{(9/2)}*\text{Sqrt}[1+x]) + 5/(63*(1-x)^{(7/2)}*\text{Sqrt}[1+x]) + 4/(63*(1-x)^{(5/2)}*\text{Sqrt}[1+x]) + 4/(63*(1-x)^{(3/2)}*\text{Sqrt}[1+x]) + (8*x)/(63*\text{Sqrt}[1-x]*\text{Sqrt}[1+x])$

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] :> Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(1-x)^{11/2}(1+x)^{3/2}} dx &= \frac{1}{9(1-x)^{9/2}\sqrt{1+x}} + \frac{5}{9} \int \frac{1}{(1-x)^{9/2}(1+x)^{3/2}} dx \\
&= \frac{1}{9(1-x)^{9/2}\sqrt{1+x}} + \frac{5}{63(1-x)^{7/2}\sqrt{1+x}} + \frac{20}{63} \int \frac{1}{(1-x)^{7/2}(1+x)^{3/2}} dx \\
&= \frac{1}{9(1-x)^{9/2}\sqrt{1+x}} + \frac{5}{63(1-x)^{7/2}\sqrt{1+x}} + \frac{4}{63(1-x)^{5/2}\sqrt{1+x}} + \frac{4}{21} \int \frac{1}{(1-x)^{5/2}(1+x)^{3/2}} dx \\
&= \frac{1}{9(1-x)^{9/2}\sqrt{1+x}} + \frac{5}{63(1-x)^{7/2}\sqrt{1+x}} + \frac{4}{63(1-x)^{5/2}\sqrt{1+x}} + \frac{4}{63(1-x)^{3/2}\sqrt{1+x}} \\
&= \frac{1}{9(1-x)^{9/2}\sqrt{1+x}} + \frac{5}{63(1-x)^{7/2}\sqrt{1+x}} + \frac{4}{63(1-x)^{5/2}\sqrt{1+x}} + \frac{4}{63(1-x)^{3/2}\sqrt{1+x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 45, normalized size = 0.44

$$\frac{8x^5 - 32x^4 + 44x^3 - 16x^2 - 17x + 20}{63(x-1)^4\sqrt{1-x^2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(11/2)*(1+x)^(3/2)),x]

[Out] (20 - 17*x - 16*x^2 + 44*x^3 - 32*x^4 + 8*x^5)/(63*(-1 + x)^4*Sqrt[1 - x^2])

fricas [A] time = 0.48, size = 91, normalized size = 0.89

$$\frac{20x^6 - 80x^5 + 100x^4 - 100x^2 - (8x^5 - 32x^4 + 44x^3 - 16x^2 - 17x + 20)\sqrt{x+1}\sqrt{-x+1} + 80x - 20}{63(x^6 - 4x^5 + 5x^4 - 5x^2 + 4x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(11/2)/(1+x)^(3/2),x, algorithm="fricas")

[Out] 1/63*(20*x^6 - 80*x^5 + 100*x^4 - 100*x^2 - (8*x^5 - 32*x^4 + 44*x^3 - 16*x^2 - 17*x + 20)*sqrt(x + 1)*sqrt(-x + 1) + 80*x - 20)/(x^6 - 4*x^5 + 5*x^4 - 5*x^2 + 4*x - 1)

giac [A] time = 0.68, size = 85, normalized size = 0.83

$$\frac{\sqrt{2} - \sqrt{-x+1}}{64\sqrt{x+1}} - \frac{\sqrt{x+1}}{64(\sqrt{2} - \sqrt{-x+1})} - \frac{(((193x - 1481)(x+1) + 5544)(x+1) - 8400)(x+1) + 5040\sqrt{x+1}\sqrt{-x+1}}{2016(x-1)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(11/2)/(1+x)^(3/2),x, algorithm="giac")

[Out] $\frac{1}{64}(\sqrt{2} - \sqrt{-x + 1})/\sqrt{x + 1} - \frac{1}{64}\sqrt{x + 1}/(\sqrt{2} - \sqrt{-x + 1}) - \frac{1}{2016}(\frac{1}{3}((193x - 1481)(x + 1) + 5544)(x + 1) - 8400)(x + 1) + 5040)\sqrt{x + 1}\sqrt{-x + 1}/(x - 1)^5$

maple [A] time = 0.00, size = 40, normalized size = 0.39

$$\frac{8x^5 - 32x^4 + 44x^3 - 16x^2 - 17x + 20}{63\sqrt{x+1}(-x+1)^{\frac{9}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+1)^(11/2)/(x+1)^(3/2),x)

[Out] $\frac{1}{63}(8x^5 - 32x^4 + 44x^3 - 16x^2 - 17x + 20)/(x+1)^{(1/2)/(-x+1)^{(9/2)}$

maxima [B] time = 1.37, size = 201, normalized size = 1.97

$$\frac{8x}{63\sqrt{-x^2+1}} + \frac{1}{9\left(\sqrt{-x^2+1}x^4 - 4\sqrt{-x^2+1}x^3 + 6\sqrt{-x^2+1}x^2 - 4\sqrt{-x^2+1}x + \sqrt{-x^2+1}\right)} - \frac{1}{63\left(\sqrt{-x^2+1}x^3 - \dots\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(11/2)/(1+x)^(3/2),x, algorithm="maxima")

[Out] $\frac{8}{63}x/\sqrt{-x^2 + 1} + \frac{1}{9}(\sqrt{-x^2 + 1})x^4 - 4\sqrt{-x^2 + 1})x^3 + 6\sqrt{-x^2 + 1})x^2 - 4\sqrt{-x^2 + 1})x + \sqrt{-x^2 + 1}) - \frac{5}{63}(\sqrt{-x^2 + 1})x^3 - 3\sqrt{-x^2 + 1})x^2 + 3\sqrt{-x^2 + 1})x - \sqrt{-x^2 + 1}) + \frac{4}{63}(\sqrt{-x^2 + 1})x^2 - 2\sqrt{-x^2 + 1})x + \sqrt{-x^2 + 1}) - \frac{4}{63}(\sqrt{-x^2 + 1})x - \sqrt{-x^2 + 1})$

mupad [B] time = 0.36, size = 80, normalized size = 0.78

$$\frac{17x\sqrt{1-x} - 20\sqrt{1-x} + 16x^2\sqrt{1-x} - 44x^3\sqrt{1-x} + 32x^4\sqrt{1-x} - 8x^5\sqrt{1-x}}{63(x-1)^5\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((1-x)^(11/2)*(x+1)^(3/2)),x)

[Out] $\frac{(17x*(1-x)^{(1/2)} - 20*(1-x)^{(1/2)} + 16*x^2*(1-x)^{(1/2)} - 44*x^3*(1-x)^{(1/2)} + 32*x^4*(1-x)^{(1/2)} - 8*x^5*(1-x)^{(1/2)})}{(63*(x-1)^5*(x+1)^{(1/2)}}$

sympy [B] time = 113.61, size = 592, normalized size = 5.80

$$\left\{ \begin{array}{l} \frac{8\sqrt{-1+\frac{2}{x+1}}(x+1)^5}{-5040x-63(x+1)^5+630(x+1)^4-2520(x+1)^3+5040(x+1)^2-3024} - \frac{72\sqrt{-1+\frac{2}{x+1}}(x+1)^4}{-5040x-63(x+1)^5+630(x+1)^4-2520(x+1)^3+5040(x+1)^2-3024} + \frac{\dots}{-5040x-63(x+1)^5+630(x+1)^4-2520(x+1)^3+5040(x+1)^2-3024} \\ \frac{8i\sqrt{1-\frac{2}{x+1}}(x+1)^5}{-5040x-63(x+1)^5+630(x+1)^4-2520(x+1)^3+5040(x+1)^2-3024} - \frac{72i\sqrt{1-\frac{2}{x+1}}(x+1)^4}{-5040x-63(x+1)^5+630(x+1)^4-2520(x+1)^3+5040(x+1)^2-3024} + \frac{\dots}{-5040x-63(x+1)^5+630(x+1)^4-2520(x+1)^3+5040(x+1)^2-3024} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)**(11/2)/(1+x)**(3/2), x)

[Out] Piecewise((8*sqrt(-1 + 2/(x + 1))*(x + 1)**5/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024) - 72*sqrt(-1 + 2/(x + 1))*(x + 1)**4/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024) + 252*sqrt(-1 + 2/(x + 1))*(x + 1)**3/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024) - 420*sqrt(-1 + 2/(x + 1))*(x + 1)**2/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024) + 315*sqrt(-1 + 2/(x + 1))*(x + 1)/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024) - 63*sqrt(-1 + 2/(x + 1))/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024), 2/Abs(x + 1) > 1), (8*I*sqrt(1 - 2/(x + 1))*(x + 1)**5/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024) - 72*I*sqrt(1 - 2/(x + 1))*(x + 1)**4/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024) + 252*I*sqrt(1 - 2/(x + 1))*(x + 1)**3/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024) - 420*I*sqrt(1 - 2/(x + 1))*(x + 1)**2/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024) + 315*I*sqrt(1 - 2/(x + 1))*(x + 1)/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024) - 63*I*sqrt(1 - 2/(x + 1))/(-5040*x - 63*(x + 1)**5 + 630*(x + 1)**4 - 2520*(x + 1)**3 + 5040*(x + 1)**2 - 3024), True))

$$3.1126 \quad \int \frac{(1-x)^{9/2}}{(1+x)^{5/2}} dx$$

Optimal. Leaf size=103

$$-\frac{2(1-x)^{9/2}}{3(x+1)^{3/2}} + \frac{6(1-x)^{7/2}}{\sqrt{x+1}} + 7\sqrt{x+1}(1-x)^{5/2} + \frac{35}{2}\sqrt{x+1}(1-x)^{3/2} + \frac{105}{2}\sqrt{x+1}\sqrt{1-x} + \frac{105}{2}\sin^{-1}(x)$$

[Out] $-2/3*(1-x)^{(9/2)}/(1+x)^{(3/2)}+105/2*\arcsin(x)+6*(1-x)^{(7/2)}/(1+x)^{(1/2)}+35/2*(1-x)^{(3/2)}*(1+x)^{(1/2)}+7*(1-x)^{(5/2)}*(1+x)^{(1/2)}+105/2*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 103, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 41, 216}

$$-\frac{2(1-x)^{9/2}}{3(x+1)^{3/2}} + \frac{6(1-x)^{7/2}}{\sqrt{x+1}} + 7\sqrt{x+1}(1-x)^{5/2} + \frac{35}{2}\sqrt{x+1}(1-x)^{3/2} + \frac{105}{2}\sqrt{x+1}\sqrt{1-x} + \frac{105}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(1-x)^{(9/2)}/(1+x)^{(5/2)}, x]$

[Out] $(-2*(1-x)^{(9/2)})/(3*(1+x)^{(3/2)}) + (6*(1-x)^{(7/2)})/\text{Sqrt}[1+x] + (105*\text{Sqrt}[1-x]*\text{Sqrt}[1+x])/2 + (35*(1-x)^{(3/2)}*\text{Sqrt}[1+x])/2 + 7*(1-x)^{(5/2)}*\text{Sqrt}[1+x] + (105*\text{ArcSin}[x])/2$

Rule 41

$\text{Int}[(a + b*x)^m * (c + d*x)^n, x_Symbol] \rightarrow \text{Int}[(a*c + b*d*x^2)^m, x] /;$ FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

$\text{Int}[(a + b*x)^m * (c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{m+1} * (c + d*x)^n / (b*(m+1)), x] - \text{Dist}[(d*n) / (b*(m+1)), \text{Int}[(a + b*x)^{m+1} * (c + d*x)^{n-1}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m+n+2], 0] && (FractionQ[m] || GeQ[2*n+m+1, 0]) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\text{Int}[(a + b*x)^m * (c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{m+1} * (c + d*x)^n / (b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d)) /$

$(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^2], x_Symbol] :> \text{Simp}[\text{ArcSin}[(\text{Rt}[-b, 2]*x)/\text{Sqrt}[a]]/\text{Rt}[-b, 2], x] /;$ FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int \frac{(1-x)^{9/2}}{(1+x)^{5/2}} dx &= -\frac{2(1-x)^{9/2}}{3(1+x)^{3/2}} - 3 \int \frac{(1-x)^{7/2}}{(1+x)^{3/2}} dx \\ &= -\frac{2(1-x)^{9/2}}{3(1+x)^{3/2}} + \frac{6(1-x)^{7/2}}{\sqrt{1+x}} + 21 \int \frac{(1-x)^{5/2}}{\sqrt{1+x}} dx \\ &= -\frac{2(1-x)^{9/2}}{3(1+x)^{3/2}} + \frac{6(1-x)^{7/2}}{\sqrt{1+x}} + 7(1-x)^{5/2}\sqrt{1+x} + 35 \int \frac{(1-x)^{3/2}}{\sqrt{1+x}} dx \\ &= -\frac{2(1-x)^{9/2}}{3(1+x)^{3/2}} + \frac{6(1-x)^{7/2}}{\sqrt{1+x}} + \frac{35}{2}(1-x)^{3/2}\sqrt{1+x} + 7(1-x)^{5/2}\sqrt{1+x} + \frac{105}{2} \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx \\ &= -\frac{2(1-x)^{9/2}}{3(1+x)^{3/2}} + \frac{6(1-x)^{7/2}}{\sqrt{1+x}} + \frac{105}{2}\sqrt{1-x}\sqrt{1+x} + \frac{35}{2}(1-x)^{3/2}\sqrt{1+x} + 7(1-x)^{5/2}\sqrt{1+x} + \\ &= -\frac{2(1-x)^{9/2}}{3(1+x)^{3/2}} + \frac{6(1-x)^{7/2}}{\sqrt{1+x}} + \frac{105}{2}\sqrt{1-x}\sqrt{1+x} + \frac{35}{2}(1-x)^{3/2}\sqrt{1+x} + 7(1-x)^{5/2}\sqrt{1+x} + \\ &= -\frac{2(1-x)^{9/2}}{3(1+x)^{3/2}} + \frac{6(1-x)^{7/2}}{\sqrt{1+x}} + \frac{105}{2}\sqrt{1-x}\sqrt{1+x} + \frac{35}{2}(1-x)^{3/2}\sqrt{1+x} + 7(1-x)^{5/2}\sqrt{1+x} + \end{aligned}$$

Mathematica [C] time = 0.01, size = 37, normalized size = 0.36

$$-\frac{(1-x)^{11/2} {}_2F_1\left(\frac{5}{2}, \frac{11}{2}; \frac{13}{2}; \frac{1-x}{2}\right)}{22\sqrt{2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(9/2)/(1 + x)^(5/2), x]

[Out] -1/22*((1 - x)^(11/2)*Hypergeometric2F1[5/2, 11/2, 13/2, (1 - x)/2])/Sqrt[2]

fricas [A] time = 0.44, size = 85, normalized size = 0.83

$$\frac{494x^2 + (2x^4 - 17x^3 + 102x^2 + 679x + 494)\sqrt{x+1}\sqrt{-x+1} - 630(x^2 + 2x + 1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) + 988x + 494}{6(x^2 + 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(9/2)/(1+x)^(5/2),x, algorithm="fricas")

[Out] 1/6*(494*x^2 + (2*x^4 - 17*x^3 + 102*x^2 + 679*x + 494)*sqrt(x + 1)*sqrt(-x + 1) - 630*(x^2 + 2*x + 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) + 988*x + 494)/(x^2 + 2*x + 1)

giac [A] time = 0.89, size = 127, normalized size = 1.23

$$\frac{1}{6}((2x - 23)(x + 1) + 165)\sqrt{x+1}\sqrt{-x+1} + \frac{2(\sqrt{2} - \sqrt{-x+1})^3}{3(x+1)^{\frac{3}{2}}} - \frac{34(\sqrt{2} - \sqrt{-x+1})}{\sqrt{x+1}} + \frac{2(x+1)^{\frac{3}{2}}\left(\frac{51(\sqrt{2}-\sqrt{-x+1})}{x+1}\right)}{3(\sqrt{2} - \sqrt{-x+1})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(9/2)/(1+x)^(5/2),x, algorithm="giac")

[Out] 1/6*((2*x - 23)*(x + 1) + 165)*sqrt(x + 1)*sqrt(-x + 1) + 2/3*(sqrt(2) - sqrt(-x + 1))^3/(x + 1)^(3/2) - 34*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) + 2/3*(x + 1)^(3/2)*(51*(sqrt(2) - sqrt(-x + 1))^2/(x + 1) - 1)/(sqrt(2) - sqrt(-x + 1))^3 + 105*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.02, size = 89, normalized size = 0.86

$$\frac{105\sqrt{(x+1)(-x+1)}\arcsin(x)}{2\sqrt{x+1}\sqrt{-x+1}} - \frac{(2x^5 - 19x^4 + 119x^3 + 577x^2 - 185x - 494)\sqrt{(x+1)(-x+1)}}{6(x+1)^{\frac{3}{2}}\sqrt{-(x+1)(x-1)}\sqrt{-x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(9/2)/(x+1)^(5/2),x)

[Out] -1/6*(2*x^5-19*x^4+119*x^3+577*x^2-185*x-494)/(x+1)^(3/2)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)+105/2*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 3.01, size = 125, normalized size = 1.21

$$\frac{x^6}{3(-x^2+1)^{\frac{3}{2}}} - \frac{7x^5}{2(-x^2+1)^{\frac{3}{2}}} + \frac{23x^4}{(-x^2+1)^{\frac{3}{2}}} + \frac{35}{2}x\left(\frac{3x^2}{(-x^2+1)^{\frac{3}{2}}} - \frac{2}{(-x^2+1)^{\frac{3}{2}}}\right) - \frac{143x}{6\sqrt{-x^2+1}} - \frac{127x^2}{(-x^2+1)^{\frac{3}{2}}} + \frac{22x}{3(-x^2+1)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(9/2)/(1+x)^(5/2),x, algorithm="maxima")

[Out] $\frac{1}{3}x^6/(-x^2 + 1)^{(3/2)} - \frac{7}{2}x^5/(-x^2 + 1)^{(3/2)} + \frac{23x^4}{(-x^2 + 1)^{(3/2)} + \frac{35}{2}x(3x^2/(-x^2 + 1)^{(3/2)} - 2/(-x^2 + 1)^{(3/2)}) - \frac{143}{6}x/\sqrt{-x^2 + 1} - \frac{127x^2}{(-x^2 + 1)^{(3/2)} + \frac{22}{3}x/(-x^2 + 1)^{(3/2)} + \frac{247}{3}/(-x^2 + 1)^{(3/2)} + \frac{105}{2}\arcsin(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(1-x)^{9/2}}{(x+1)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(9/2)/(x + 1)^(5/2),x)

[Out] int((1 - x)^(9/2)/(x + 1)^(5/2), x)

sympy [A] time = 45.20, size = 250, normalized size = 2.43

$$\begin{cases} -105i \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) + \frac{i(x+1)^{7/2}}{3\sqrt{x-1}} - \frac{29i(x+1)^{5/2}}{6\sqrt{x-1}} + \frac{215i(x+1)^{3/2}}{6\sqrt{x-1}} + \frac{43i\sqrt{x+1}}{3\sqrt{x-1}} - \frac{448i}{3\sqrt{x-1}\sqrt{x+1}} + \frac{64i}{3\sqrt{x-1}(x+1)^{3/2}} & \text{for } \frac{|x+1|}{2} > 1 \\ 105 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) - \frac{(x+1)^{7/2}}{3\sqrt{1-x}} + \frac{29(x+1)^{5/2}}{6\sqrt{1-x}} - \frac{215(x+1)^{3/2}}{6\sqrt{1-x}} - \frac{43\sqrt{x+1}}{3\sqrt{1-x}} + \frac{448}{3\sqrt{1-x}\sqrt{x+1}} - \frac{64}{3\sqrt{1-x}(x+1)^{3/2}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(9/2)/(1+x)**(5/2),x)

[Out] Piecewise((-105*I*acosh(sqrt(2)*sqrt(x + 1)/2) + I*(x + 1)**(7/2)/(3*sqrt(x - 1)) - 29*I*(x + 1)**(5/2)/(6*sqrt(x - 1)) + 215*I*(x + 1)**(3/2)/(6*sqrt(x - 1)) + 43*I*sqrt(x + 1)/(3*sqrt(x - 1)) - 448*I/(3*sqrt(x - 1)*sqrt(x + 1)) + 64*I/(3*sqrt(x - 1)*(x + 1)**(3/2)), Abs(x + 1)/2 > 1), (105*asin(sqrt(2)*sqrt(x + 1)/2) - (x + 1)**(7/2)/(3*sqrt(1 - x)) + 29*(x + 1)**(5/2)/(6*sqrt(1 - x)) - 215*(x + 1)**(3/2)/(6*sqrt(1 - x)) - 43*sqrt(x + 1)/(3*sqrt(1 - x)) + 448/(3*sqrt(1 - x)*sqrt(x + 1)) - 64/(3*sqrt(1 - x)*(x + 1)**(3/2)), True))

$$3.1127 \quad \int \frac{(1-x)^{7/2}}{(1+x)^{5/2}} dx$$

Optimal. Leaf size=87

$$-\frac{2(1-x)^{7/2}}{3(x+1)^{3/2}} + \frac{14(1-x)^{5/2}}{3\sqrt{x+1}} + \frac{35}{6}\sqrt{x+1}(1-x)^{3/2} + \frac{35}{2}\sqrt{x+1}\sqrt{1-x} + \frac{35}{2}\sin^{-1}(x)$$

[Out] $-2/3*(1-x)^{(7/2)}/(1+x)^{(3/2)}+35/2*\arcsin(x)+14/3*(1-x)^{(5/2)}/(1+x)^{(1/2)}+35/6*(1-x)^{(3/2)}*(1+x)^{(1/2)}+35/2*(1-x)^{(1/2)}*(1+x)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 87, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 41, 216}

$$-\frac{2(1-x)^{7/2}}{3(x+1)^{3/2}} + \frac{14(1-x)^{5/2}}{3\sqrt{x+1}} + \frac{35}{6}\sqrt{x+1}(1-x)^{3/2} + \frac{35}{2}\sqrt{x+1}\sqrt{1-x} + \frac{35}{2}\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(7/2)/(1 + x)^(5/2), x]

[Out] $(-2*(1-x)^{(7/2)})/(3*(1+x)^{(3/2)}) + (14*(1-x)^{(5/2)})/(3*\text{Sqrt}[1+x]) + (35*\text{Sqrt}[1-x]*\text{Sqrt}[1+x])/2 + (35*(1-x)^{(3/2)}*\text{Sqrt}[1+x])/6 + (35*\text{ArcSin}[x])/2$

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,

c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
 \int \frac{(1-x)^{7/2}}{(1+x)^{5/2}} dx &= -\frac{2(1-x)^{7/2}}{3(1+x)^{3/2}} - \frac{7}{3} \int \frac{(1-x)^{5/2}}{(1+x)^{3/2}} dx \\
 &= -\frac{2(1-x)^{7/2}}{3(1+x)^{3/2}} + \frac{14(1-x)^{5/2}}{3\sqrt{1+x}} + \frac{35}{3} \int \frac{(1-x)^{3/2}}{\sqrt{1+x}} dx \\
 &= -\frac{2(1-x)^{7/2}}{3(1+x)^{3/2}} + \frac{14(1-x)^{5/2}}{3\sqrt{1+x}} + \frac{35}{6}(1-x)^{3/2}\sqrt{1+x} + \frac{35}{2} \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx \\
 &= -\frac{2(1-x)^{7/2}}{3(1+x)^{3/2}} + \frac{14(1-x)^{5/2}}{3\sqrt{1+x}} + \frac{35}{2}\sqrt{1-x}\sqrt{1+x} + \frac{35}{6}(1-x)^{3/2}\sqrt{1+x} + \frac{35}{2} \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
 &= -\frac{2(1-x)^{7/2}}{3(1+x)^{3/2}} + \frac{14(1-x)^{5/2}}{3\sqrt{1+x}} + \frac{35}{2}\sqrt{1-x}\sqrt{1+x} + \frac{35}{6}(1-x)^{3/2}\sqrt{1+x} + \frac{35}{2} \int \frac{1}{\sqrt{1-x^2}} dx \\
 &= -\frac{2(1-x)^{7/2}}{3(1+x)^{3/2}} + \frac{14(1-x)^{5/2}}{3\sqrt{1+x}} + \frac{35}{2}\sqrt{1-x}\sqrt{1+x} + \frac{35}{6}(1-x)^{3/2}\sqrt{1+x} + \frac{35}{2} \sin^{-1}(x)
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 37, normalized size = 0.43

$$\frac{(1-x)^{9/2} {}_2F_1\left(\frac{5}{2}, \frac{9}{2}; \frac{11}{2}; \frac{1-x}{2}\right)}{18\sqrt{2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(7/2)/(1 + x)^(5/2), x]

[Out] -1/18*((1 - x)^(9/2)*Hypergeometric2F1[5/2, 9/2, 11/2, (1 - x)/2])/Sqrt[2]

fricas [A] time = 0.43, size = 81, normalized size = 0.93

$$\frac{164x^2 - (3x^3 - 30x^2 - 229x - 164)\sqrt{x+1}\sqrt{-x+1} - 210(x^2 + 2x + 1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) + 328x + 164}{6(x^2 + 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)/(1+x)^(5/2),x, algorithm="fricas")

[Out] 1/6*(164*x^2 - (3*x^3 - 30*x^2 - 229*x - 164)*sqrt(x + 1)*sqrt(-x + 1) - 210*(x^2 + 2*x + 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) + 328*x + 164)/(x^2 + 2*x + 1)

giac [A] time = 0.80, size = 119, normalized size = 1.37

$$-\frac{1}{2}\sqrt{x+1}(x-12)\sqrt{-x+1} + \frac{(\sqrt{2}-\sqrt{-x+1})^3}{3(x+1)^{\frac{3}{2}}} - \frac{13(\sqrt{2}-\sqrt{-x+1})}{\sqrt{x+1}} + \frac{(x+1)^{\frac{3}{2}}\left(\frac{39(\sqrt{2}-\sqrt{-x+1})^2}{x+1} - 1\right)}{3(\sqrt{2}-\sqrt{-x+1})^3} + 35 \arcsin$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)/(1+x)^(5/2),x, algorithm="giac")

[Out] -1/2*sqrt(x + 1)*(x - 12)*sqrt(-x + 1) + 1/3*(sqrt(2) - sqrt(-x + 1))^3/(x + 1)^(3/2) - 13*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) + 1/3*(x + 1)^(3/2)*(39*(sqrt(2) - sqrt(-x + 1))^2/(x + 1) - 1)/(sqrt(2) - sqrt(-x + 1))^3 + 35*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [A] time = 0.02, size = 84, normalized size = 0.97

$$\frac{35\sqrt{(x+1)(-x+1)} \arcsin(x)}{2\sqrt{x+1} \sqrt{-x+1}} + \frac{(3x^4 - 33x^3 - 199x^2 + 65x + 164) \sqrt{(x+1)(-x+1)}}{6(x+1)^{\frac{3}{2}} \sqrt{-(x+1)(x-1)} \sqrt{-x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(7/2)/(x+1)^(5/2),x)

[Out] 1/6*(3*x^4-33*x^3-199*x^2+65*x+164)/(x+1)^(3/2)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)+35/2*((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [A] time = 3.00, size = 111, normalized size = 1.28

$$-\frac{x^5}{2(-x^2+1)^{\frac{3}{2}}} + \frac{6x^4}{(-x^2+1)^{\frac{3}{2}}} + \frac{35}{6}x \left(\frac{3x^2}{(-x^2+1)^{\frac{3}{2}}} - \frac{2}{(-x^2+1)^{\frac{3}{2}}} \right) - \frac{61x}{6\sqrt{-x^2+1}} - \frac{44x^2}{(-x^2+1)^{\frac{3}{2}}} + \frac{16x}{3(-x^2+1)^{\frac{3}{2}}} + \frac{82}{3(-x^2+1)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/2)/(1+x)^(5/2),x, algorithm="maxima")

[Out] $-1/2*x^5/(-x^2 + 1)^{(3/2)} + 6*x^4/(-x^2 + 1)^{(3/2)} + 35/6*x*(3*x^2/(-x^2 + 1)^{(3/2)} - 2/(-x^2 + 1)^{(3/2)}) - 61/6*x/\sqrt{-x^2 + 1} - 44*x^2/(-x^2 + 1)^{(3/2)} + 16/3*x/(-x^2 + 1)^{(3/2)} + 82/3/(-x^2 + 1)^{(3/2)} + 35/2*\arcsin(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(1-x)^{7/2}}{(x+1)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(7/2)/(x + 1)^(5/2), x)`

[Out] `int((1 - x)^(7/2)/(x + 1)^(5/2), x)`

sympy [C] time = 17.50, size = 207, normalized size = 2.38

$$\left\{ \begin{array}{l} -\frac{\sqrt{-1+\frac{2}{x+1}}(x+1)^2}{2} + \frac{13\sqrt{-1+\frac{2}{x+1}}(x+1)}{2} + \frac{80\sqrt{-1+\frac{2}{x+1}}}{3} - \frac{16\sqrt{-1+\frac{2}{x+1}}}{3(x+1)} + \frac{35i\log\left(\frac{1}{x+1}\right)}{2} + \frac{35i\log(x+1)}{2} + 35\operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) \\ -\frac{i\sqrt{1-\frac{2}{x+1}}(x+1)^2}{2} + \frac{13i\sqrt{1-\frac{2}{x+1}}(x+1)}{2} + \frac{80i\sqrt{1-\frac{2}{x+1}}}{3} - \frac{16i\sqrt{1-\frac{2}{x+1}}}{3(x+1)} + \frac{35i\log\left(\frac{1}{x+1}\right)}{2} - 35i\log\left(\sqrt{1-\frac{2}{x+1}}+1\right) \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(7/2)/(1+x)**(5/2), x)`

[Out] `Piecewise((-sqrt(-1 + 2/(x + 1))*(x + 1)**2/2 + 13*sqrt(-1 + 2/(x + 1))*(x + 1)/2 + 80*sqrt(-1 + 2/(x + 1))/3 - 16*sqrt(-1 + 2/(x + 1))/(3*(x + 1)) + 35*I*log(1/(x + 1))/2 + 35*I*log(x + 1)/2 + 35*asin(sqrt(2)*sqrt(x + 1)/2), 2/Abs(x + 1) > 1), (-I*sqrt(1 - 2/(x + 1))*(x + 1)**2/2 + 13*I*sqrt(1 - 2/(x + 1))*(x + 1)/2 + 80*I*sqrt(1 - 2/(x + 1))/3 - 16*I*sqrt(1 - 2/(x + 1))/(3*(x + 1)) + 35*I*log(1/(x + 1))/2 - 35*I*log(sqrt(1 - 2/(x + 1)) + 1), True))`

$$3.1128 \quad \int \frac{(1-x)^{5/2}}{(1+x)^{5/2}} dx$$

Optimal. Leaf size=63

$$-\frac{2(1-x)^{5/2}}{3(x+1)^{3/2}} + \frac{10(1-x)^{3/2}}{3\sqrt{x+1}} + 5\sqrt{x+1}\sqrt{1-x} + 5\sin^{-1}(x)$$

[Out] $-2/3*(1-x)^{(5/2)/(1+x)^{(3/2)}+5*\arcsin(x)+10/3*(1-x)^{(3/2)/(1+x)^{(1/2)}+5*(1-x)^{(1/2)*(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 41, 216}

$$-\frac{2(1-x)^{5/2}}{3(x+1)^{3/2}} + \frac{10(1-x)^{3/2}}{3\sqrt{x+1}} + 5\sqrt{x+1}\sqrt{1-x} + 5\sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(1-x)^{(5/2)/(1+x)^{(5/2)}, x]$

[Out] $(-2*(1-x)^{(5/2))/(3*(1+x)^{(3/2)}) + (10*(1-x)^{(3/2))/(3*\text{Sqrt}[1+x]) + 5*\text{Sqrt}[1-x]*\text{Sqrt}[1+x] + 5*\text{ArcSin}[x]$

Rule 41

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(m_)}), x_Symbol] \rightarrow \text{Int}[(a*c + b*d*x^2)^m, x] /;$ FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \text{Dist}[(d*n)/(b*(m+1)), \text{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ

[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0])) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
 \int \frac{(1-x)^{5/2}}{(1+x)^{5/2}} dx &= -\frac{2(1-x)^{5/2}}{3(1+x)^{3/2}} - \frac{5}{3} \int \frac{(1-x)^{3/2}}{(1+x)^{3/2}} dx \\
 &= -\frac{2(1-x)^{5/2}}{3(1+x)^{3/2}} + \frac{10(1-x)^{3/2}}{3\sqrt{1+x}} + 5 \int \frac{\sqrt{1-x}}{\sqrt{1+x}} dx \\
 &= -\frac{2(1-x)^{5/2}}{3(1+x)^{3/2}} + \frac{10(1-x)^{3/2}}{3\sqrt{1+x}} + 5\sqrt{1-x}\sqrt{1+x} + 5 \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
 &= -\frac{2(1-x)^{5/2}}{3(1+x)^{3/2}} + \frac{10(1-x)^{3/2}}{3\sqrt{1+x}} + 5\sqrt{1-x}\sqrt{1+x} + 5 \int \frac{1}{\sqrt{1-x^2}} dx \\
 &= -\frac{2(1-x)^{5/2}}{3(1+x)^{3/2}} + \frac{10(1-x)^{3/2}}{3\sqrt{1+x}} + 5\sqrt{1-x}\sqrt{1+x} + 5 \sin^{-1}(x)
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 37, normalized size = 0.59

$$\frac{(1-x)^{7/2} {}_2F_1\left(\frac{5}{2}, \frac{7}{2}; \frac{9}{2}; \frac{1-x}{2}\right)}{14\sqrt{2}}$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(5/2)/(1 + x)^(5/2), x]

[Out] -1/14*((1 - x)^(7/2)*Hypergeometric2F1[5/2, 7/2, 9/2, (1 - x)/2])/Sqrt[2]

fricas [A] time = 0.45, size = 75, normalized size = 1.19

$$\frac{23x^2 + (3x^2 + 34x + 23)\sqrt{x+1}\sqrt{-x+1} - 30(x^2 + 2x + 1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) + 46x + 23}{3(x^2 + 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)/(1+x)^(5/2),x, algorithm="fricas")

[Out] $\frac{1}{3}*(23*x^2 + (3*x^2 + 34*x + 23)*\sqrt{x + 1}*\sqrt{-x + 1} - 30*(x^2 + 2*x + 1)*\arctan((\sqrt{x + 1}*\sqrt{-x + 1} - 1)/x) + 46*x + 23)/(x^2 + 2*x + 1)$

giac [B] time = 0.75, size = 115, normalized size = 1.83

$$\frac{(\sqrt{2} - \sqrt{-x+1})^3}{6(x+1)^{\frac{3}{2}}} + \sqrt{x+1}\sqrt{-x+1} - \frac{9(\sqrt{2} - \sqrt{-x+1})}{2\sqrt{x+1}} + \frac{(x+1)^{\frac{3}{2}}\left(\frac{27(\sqrt{2}-\sqrt{-x+1})^2}{x+1} - 1\right)}{6(\sqrt{2} - \sqrt{-x+1})^3} + 10 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)/(1+x)^(5/2),x, algorithm="giac")

[Out] $\frac{1}{6}*(\sqrt{2} - \sqrt{-x + 1})^3/(x + 1)^{3/2} + \sqrt{x + 1}*\sqrt{-x + 1} - 9/2*(\sqrt{2} - \sqrt{-x + 1})/\sqrt{x + 1} + 1/6*(x + 1)^{3/2}*(27*(\sqrt{2} - \sqrt{-x + 1})^2/(x + 1) - 1)/(\sqrt{2} - \sqrt{-x + 1})^3 + 10*\arcsin(1/2*\sqrt{2}*\sqrt{x + 1})$

maple [A] time = 0.02, size = 79, normalized size = 1.25

$$\frac{5\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1}\sqrt{-x+1}} - \frac{(3x^3 + 31x^2 - 11x - 23)\sqrt{(x+1)(-x+1)}}{3(x+1)^{\frac{3}{2}}\sqrt{-(x+1)(x-1)}\sqrt{-x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(5/2)/(x+1)^(5/2),x)

[Out] $-1/3*(3*x^3+31*x^2-11*x-23)/(x+1)^{3/2}/(-(x+1)*(x-1))^{1/2}*((x+1)*(-x+1))^{1/2}/(-x+1)^{1/2}+5*((x+1)*(-x+1))^{1/2}/(x+1)^{1/2}/(-x+1)^{1/2}*\arcsin(x)$

maxima [B] time = 2.97, size = 98, normalized size = 1.56

$$\frac{(-x^2 + 1)^{\frac{5}{2}}}{x^4 + 4x^3 + 6x^2 + 4x + 1} - \frac{5(-x^2 + 1)^{\frac{3}{2}}}{3(x^3 + 3x^2 + 3x + 1)} - \frac{10\sqrt{-x^2 + 1}}{3(x^2 + 2x + 1)} + \frac{35\sqrt{-x^2 + 1}}{3(x + 1)} + 5 \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(5/2)/(1+x)^(5/2),x, algorithm="maxima")

[Out] $(-x^2 + 1)^{5/2}/(x^4 + 4*x^3 + 6*x^2 + 4*x + 1) - 5/3*(-x^2 + 1)^{3/2}/(x^3 + 3*x^2 + 3*x + 1) - 10/3*\sqrt{-x^2 + 1}/(x^2 + 2*x + 1) + 35/3*\sqrt{-x^2 + 1}/(x + 1) + 5*\arcsin(x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(1-x)^{5/2}}{(x+1)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(5/2)/(x + 1)^(5/2), x)`

[Out] `int((1 - x)^(5/2)/(x + 1)^(5/2), x)`

sympy [C] time = 6.46, size = 160, normalized size = 2.54

$$\begin{cases} \sqrt{-1 + \frac{2}{x+1}} (x+1) + \frac{28\sqrt{-1 + \frac{2}{x+1}}}{3} - \frac{8\sqrt{-1 + \frac{2}{x+1}}}{3(x+1)} + 5i \log\left(\frac{1}{x+1}\right) + 5i \log(x+1) + 10 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) & \text{for } \frac{2}{|x+1|} > 1 \\ i\sqrt{1 - \frac{2}{x+1}} (x+1) + \frac{28i\sqrt{1 - \frac{2}{x+1}}}{3} - \frac{8i\sqrt{1 - \frac{2}{x+1}}}{3(x+1)} + 5i \log\left(\frac{1}{x+1}\right) - 10i \log\left(\sqrt{1 - \frac{2}{x+1}} + 1\right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(5/2)/(1+x)**(5/2), x)`

[Out] `Piecewise((sqrt(-1 + 2/(x + 1))*(x + 1) + 28*sqrt(-1 + 2/(x + 1)))/3 - 8*sqrt(-1 + 2/(x + 1))/(3*(x + 1)) + 5*I*log(1/(x + 1)) + 5*I*log(x + 1) + 10*asin(sqrt(2)*sqrt(x + 1)/2), 2/Abs(x + 1) > 1), (I*sqrt(1 - 2/(x + 1))*(x + 1) + 28*I*sqrt(1 - 2/(x + 1)))/3 - 8*I*sqrt(1 - 2/(x + 1))/(3*(x + 1)) + 5*I*log(1/(x + 1)) - 10*I*log(sqrt(1 - 2/(x + 1)) + 1), True))`

$$3.1129 \quad \int \frac{(1-x)^{3/2}}{(1+x)^{5/2}} dx$$

Optimal. Leaf size=41

$$-\frac{2(1-x)^{3/2}}{3(x+1)^{3/2}} + \frac{2\sqrt{1-x}}{\sqrt{x+1}} + \sin^{-1}(x)$$

[Out] $-2/3*(1-x)^{(3/2)}/(1+x)^{(3/2)}+\arcsin(x)+2*(1-x)^{(1/2)}/(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {47, 41, 216}

$$-\frac{2(1-x)^{3/2}}{3(x+1)^{3/2}} + \frac{2\sqrt{1-x}}{\sqrt{x+1}} + \sin^{-1}(x)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(3/2)/(1 + x)^(5/2), x]

[Out] $(-2*(1-x)^{(3/2)})/(3*(1+x)^{(3/2)}) + (2*\text{Sqrt}[1-x])/ \text{Sqrt}[1+x] + \text{ArcSin}[x]$

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IleQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \frac{(1-x)^{3/2}}{(1+x)^{5/2}} dx &= -\frac{2(1-x)^{3/2}}{3(1+x)^{3/2}} - \int \frac{\sqrt{1-x}}{(1+x)^{3/2}} dx \\
&= -\frac{2(1-x)^{3/2}}{3(1+x)^{3/2}} + \frac{2\sqrt{1-x}}{\sqrt{1+x}} + \int \frac{1}{\sqrt{1-x}\sqrt{1+x}} dx \\
&= -\frac{2(1-x)^{3/2}}{3(1+x)^{3/2}} + \frac{2\sqrt{1-x}}{\sqrt{1+x}} + \int \frac{1}{\sqrt{1-x^2}} dx \\
&= -\frac{2(1-x)^{3/2}}{3(1+x)^{3/2}} + \frac{2\sqrt{1-x}}{\sqrt{1+x}} + \sin^{-1}(x)
\end{aligned}$$

Mathematica [A] time = 0.06, size = 49, normalized size = 1.20

$$\frac{-8x^2 + 4x + 4}{3\sqrt{1-x}(x+1)^{3/2}} - 2 \sin^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(3/2)/(1 + x)^(5/2), x]

[Out] (4 + 4*x - 8*x^2)/(3*Sqrt[1 - x]*(1 + x)^(3/2)) - 2*ArcSin[Sqrt[1 - x]/Sqrt[2]]

fricas [B] time = 0.45, size = 71, normalized size = 1.73

$$\frac{2\left(2x^2 + 2(2x+1)\sqrt{x+1}\sqrt{-x+1} - 3(x^2 + 2x+1)\arctan\left(\frac{\sqrt{x+1}\sqrt{-x+1}-1}{x}\right) + 4x + 2\right)}{3(x^2 + 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)/(1+x)^(5/2), x, algorithm="fricas")

[Out] 2/3*(2*x^2 + 2*(2*x + 1)*sqrt(x + 1)*sqrt(-x + 1) - 3*(x^2 + 2*x + 1)*arctan((sqrt(x + 1)*sqrt(-x + 1) - 1)/x) + 4*x + 2)/(x^2 + 2*x + 1)

giac [B] time = 0.70, size = 102, normalized size = 2.49

$$\frac{(\sqrt{2} - \sqrt{-x+1})^3}{12(x+1)^{\frac{3}{2}}} - \frac{5(\sqrt{2} - \sqrt{-x+1})}{4\sqrt{x+1}} + \frac{(x+1)^{\frac{3}{2}}\left(\frac{15(\sqrt{2}-\sqrt{-x+1})^2}{x+1} - 1\right)}{12(\sqrt{2} - \sqrt{-x+1})^3} + 2 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)/(1+x)^(5/2),x, algorithm="giac")

[Out] 1/12*(sqrt(2) - sqrt(-x + 1))^3/(x + 1)^(3/2) - 5/4*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) + 1/12*(x + 1)^(3/2)*(15*(sqrt(2) - sqrt(-x + 1))^2/(x + 1) - 1)/(sqrt(2) - sqrt(-x + 1))^3 + 2*arcsin(1/2*sqrt(2)*sqrt(x + 1))

maple [B] time = 0.02, size = 73, normalized size = 1.78

$$\frac{\sqrt{(x+1)(-x+1)} \arcsin(x)}{\sqrt{x+1} \sqrt{-x+1}} - \frac{4(2x^2 - x - 1) \sqrt{(x+1)(-x+1)}}{3(x+1)^{\frac{3}{2}} \sqrt{-(x+1)(x-1)} \sqrt{-x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(3/2)/(x+1)^(5/2),x)

[Out] -4/3*(2*x^2-x-1)/(x+1)^(3/2)/(-(x+1)*(x-1))^(1/2)*((x+1)*(-x+1))^(1/2)/(-x+1)^(1/2)+((x+1)*(-x+1))^(1/2)/(x+1)^(1/2)/(-x+1)^(1/2)*arcsin(x)

maxima [B] time = 3.01, size = 66, normalized size = 1.61

$$-\frac{(-x^2 + 1)^{\frac{3}{2}}}{3(x^3 + 3x^2 + 3x + 1)} - \frac{2\sqrt{-x^2 + 1}}{3(x^2 + 2x + 1)} + \frac{7\sqrt{-x^2 + 1}}{3(x + 1)} + \arcsin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(3/2)/(1+x)^(5/2),x, algorithm="maxima")

[Out] -1/3*(-x^2 + 1)^(3/2)/(x^3 + 3*x^2 + 3*x + 1) - 2/3*sqrt(-x^2 + 1)/(x^2 + 2*x + 1) + 7/3*sqrt(-x^2 + 1)/(x + 1) + arcsin(x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(1-x)^{3/2}}{(x+1)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(3/2)/(x + 1)^(5/2),x)

[Out] int((1 - x)^(3/2)/(x + 1)^(5/2), x)

sympy [C] time = 3.28, size = 126, normalized size = 3.07

$$\begin{cases} \frac{8\sqrt{-1+\frac{2}{x+1}}}{3} - \frac{4\sqrt{-1+\frac{2}{x+1}}}{3(x+1)} + i \log\left(\frac{1}{x+1}\right) + i \log(x+1) + 2 \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{x+1}}{2}\right) & \text{for } \frac{2}{|x+1|} > 1 \\ \frac{8i\sqrt{1-\frac{2}{x+1}}}{3} - \frac{4i\sqrt{1-\frac{2}{x+1}}}{3(x+1)} + i \log\left(\frac{1}{x+1}\right) - 2i \log\left(\sqrt{1-\frac{2}{x+1}} + 1\right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(3/2)/(1+x)**(5/2),x)

[Out] Piecewise((8*sqrt(-1 + 2/(x + 1)))/3 - 4*sqrt(-1 + 2/(x + 1))/(3*(x + 1)) + I*log(1/(x + 1)) + I*log(x + 1) + 2*asin(sqrt(2)*sqrt(x + 1)/2), 2/Abs(x + 1) > 1), (8*I*sqrt(1 - 2/(x + 1)))/3 - 4*I*sqrt(1 - 2/(x + 1))/(3*(x + 1)) + I*log(1/(x + 1)) - 2*I*log(sqrt(1 - 2/(x + 1)) + 1), True))

$$3.1130 \quad \int \frac{\sqrt{1-x}}{(1+x)^{5/2}} dx$$

Optimal. Leaf size=20

$$-\frac{(1-x)^{3/2}}{3(x+1)^{3/2}}$$

[Out] $-1/3*(1-x)^{(3/2)/(1+x)^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {37}

$$-\frac{(1-x)^{3/2}}{3(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[1 - x]/(1 + x)^(5/2), x]`

[Out] $-(1-x)^{(3/2)/(3*(1+x)^{(3/2)})}$

Rule 37

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp`
`[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /;`
`FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -`
`1]`

Rubi steps

$$\int \frac{\sqrt{1-x}}{(1+x)^{5/2}} dx = -\frac{(1-x)^{3/2}}{3(1+x)^{3/2}}$$

Mathematica [A] time = 0.00, size = 20, normalized size = 1.00

$$-\frac{(1-x)^{3/2}}{3(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] `Integrate[Sqrt[1 - x]/(1 + x)^(5/2), x]`

[Out] $-1/3*(1-x)^{(3/2)/(1+x)^{(3/2)}$

fricas [B] time = 0.45, size = 37, normalized size = 1.85

$$-\frac{x^2 - \sqrt{x+1}(x-1)\sqrt{-x+1} + 2x+1}{3(x^2 + 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)/(1+x)^(5/2),x, algorithm="fricas")

[Out] -1/3*(x^2 - sqrt(x + 1)*(x - 1)*sqrt(-x + 1) + 2*x + 1)/(x^2 + 2*x + 1)

giac [B] time = 0.71, size = 89, normalized size = 4.45

$$\frac{(\sqrt{2} - \sqrt{-x+1})^3}{24(x+1)^{\frac{3}{2}}} - \frac{\sqrt{2} - \sqrt{-x+1}}{8\sqrt{x+1}} + \frac{(x+1)^{\frac{3}{2}} \left(\frac{3(\sqrt{2} - \sqrt{-x+1})^2}{x+1} - 1 \right)}{24(\sqrt{2} - \sqrt{-x+1})^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)/(1+x)^(5/2),x, algorithm="giac")

[Out] 1/24*(sqrt(2) - sqrt(-x + 1))^3/(x + 1)^(3/2) - 1/8*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) + 1/24*(x + 1)^(3/2)*(3*(sqrt(2) - sqrt(-x + 1))^2/(x + 1) - 1)/(sqrt(2) - sqrt(-x + 1))^3

maple [A] time = 0.00, size = 15, normalized size = 0.75

$$-\frac{(-x+1)^{\frac{3}{2}}}{3(x+1)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(1/2)/(x+1)^(5/2),x)

[Out] -1/3*(-x+1)^(3/2)/(x+1)^(3/2)

maxima [B] time = 1.32, size = 38, normalized size = 1.90

$$-\frac{2\sqrt{-x^2+1}}{3(x^2+2x+1)} + \frac{\sqrt{-x^2+1}}{3(x+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/2)/(1+x)^(5/2),x, algorithm="maxima")

[Out] $-2/3*\sqrt{-x^2 + 1}/(x^2 + 2*x + 1) + 1/3*\sqrt{-x^2 + 1}/(x + 1)$

mupad [B] time = 0.26, size = 32, normalized size = 1.60

$$\frac{x\sqrt{1-x} - \sqrt{1-x}}{(3x+3)\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1 - x)^(1/2)/(x + 1)^(5/2), x)`

[Out] $(x*(1 - x)^{(1/2)} - (1 - x)^{(1/2)})/((3*x + 3)*(x + 1)^{(1/2)})$

sympy [A] time = 1.69, size = 65, normalized size = 3.25

$$\left\{ \begin{array}{ll} \frac{\sqrt{-1+\frac{2}{x+1}}}{3} - \frac{2\sqrt{-1+\frac{2}{x+1}}}{3(x+1)} & \text{for } \frac{2}{|x+1|} > 1 \\ \frac{i\sqrt{1-\frac{2}{x+1}}}{3} - \frac{2i\sqrt{1-\frac{2}{x+1}}}{3(x+1)} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(1/2)/(1+x)**(5/2), x)`

[Out] `Piecewise((sqrt(-1 + 2/(x + 1))/3 - 2*sqrt(-1 + 2/(x + 1))/(3*(x + 1)), 2/abs(x + 1) > 1), (I*sqrt(1 - 2/(x + 1))/3 - 2*I*sqrt(1 - 2/(x + 1))/(3*(x + 1)), True))`

$$3.1131 \quad \int \frac{1}{\sqrt{1-x}(1+x)^{5/2}} dx$$

Optimal. Leaf size=41

$$-\frac{\sqrt{1-x}}{3\sqrt{x+1}} - \frac{\sqrt{1-x}}{3(x+1)^{3/2}}$$

[Out] $-1/3*(1-x)^{(1/2)/(1+x)^{(3/2)}-1/3*(1-x)^{(1/2)/(1+x)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$-\frac{\sqrt{1-x}}{3\sqrt{x+1}} - \frac{\sqrt{1-x}}{3(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[1 - x]*(1 + x)^(5/2)), x]

[Out] $-\text{Sqrt}[1 - x]/(3*(1 + x)^{(3/2)}) - \text{Sqrt}[1 - x]/(3*\text{Sqrt}[1 + x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{\sqrt{1-x}(1+x)^{5/2}} dx = -\frac{\sqrt{1-x}}{3(1+x)^{3/2}} + \frac{1}{3} \int \frac{1}{\sqrt{1-x}(1+x)^{3/2}} dx$$

$$= -\frac{\sqrt{1-x}}{3(1+x)^{3/2}} - \frac{\sqrt{1-x}}{3\sqrt{1+x}}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.56

$$-\frac{\sqrt{1-x}(x+2)}{3(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[1 - x]*(1 + x)^(5/2)), x]

[Out] -1/3*(Sqrt[1 - x]*(2 + x))/(1 + x)^(3/2)

fricas [A] time = 0.44, size = 38, normalized size = 0.93

$$-\frac{2x^2 + (x+2)\sqrt{x+1}\sqrt{-x+1} + 4x + 2}{3(x^2 + 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(1/2)/(1+x)^(5/2), x, algorithm="fricas")

[Out] -1/3*(2*x^2 + (x + 2)*sqrt(x + 1)*sqrt(-x + 1) + 4*x + 2)/(x^2 + 2*x + 1)

giac [B] time = 0.67, size = 89, normalized size = 2.17

$$\frac{(\sqrt{2} - \sqrt{-x+1})^3}{48(x+1)^{3/2}} + \frac{3(\sqrt{2} - \sqrt{-x+1})}{16\sqrt{x+1}} - \frac{(x+1)^{3/2} \left(\frac{9(\sqrt{2} - \sqrt{-x+1})^2}{x+1} + 1 \right)}{48(\sqrt{2} - \sqrt{-x+1})^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(1/2)/(1+x)^(5/2), x, algorithm="giac")

[Out] 1/48*(sqrt(2) - sqrt(-x + 1))^3/(x + 1)^(3/2) + 3/16*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) - 1/48*(x + 1)^(3/2)*(9*(sqrt(2) - sqrt(-x + 1))^2/(x + 1) + 1)/(sqrt(2) - sqrt(-x + 1))^3

maple [A] time = 0.00, size = 18, normalized size = 0.44

$$\frac{(x+2)\sqrt{-x+1}}{3(x+1)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+1)^(1/2)/(x+1)^(5/2), x)

[Out] -1/3*(2+x)/(x+1)^(3/2)*(-x+1)^(1/2)

maxima [A] time = 2.93, size = 38, normalized size = 0.93

$$-\frac{\sqrt{-x^2+1}}{3(x^2+2x+1)} - \frac{\sqrt{-x^2+1}}{3(x+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(1/2)/(1+x)^(5/2), x, algorithm="maxima")

[Out] -1/3*sqrt(-x^2 + 1)/(x^2 + 2*x + 1) - 1/3*sqrt(-x^2 + 1)/(x + 1)

mupad [B] time = 0.31, size = 33, normalized size = 0.80

$$\frac{x\sqrt{1-x} + 2\sqrt{1-x}}{(3x+3)\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((1-x)^(1/2)*(x+1)^(5/2)), x)

[Out] -(x*(1-x)^(1/2) + 2*(1-x)^(1/2))/((3*x + 3)*(x + 1)^(1/2))

sympy [A] time = 2.35, size = 65, normalized size = 1.59

$$\begin{cases} -\frac{\sqrt{-1+\frac{2}{x+1}}}{3} - \frac{\sqrt{-1+\frac{2}{x+1}}}{3(x+1)} & \text{for } \frac{2}{|x+1|} > 1 \\ -\frac{i\sqrt{1-\frac{2}{x+1}}}{3} - \frac{i\sqrt{1-\frac{2}{x+1}}}{3(x+1)} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)**(1/2)/(1+x)**(5/2), x)

[Out] Piecewise((-sqrt(-1 + 2/(x + 1)))/3 - sqrt(-1 + 2/(x + 1))/(3*(x + 1)), 2/Abs(x + 1) > 1), (-I*sqrt(1 - 2/(x + 1)))/3 - I*sqrt(1 - 2/(x + 1))/(3*(x + 1)), True))

$$3.1132 \quad \int \frac{1}{(1-x)^{3/2}(1+x)^{5/2}} dx$$

Optimal. Leaf size=58

$$-\frac{2\sqrt{1-x}}{3\sqrt{x+1}} - \frac{2\sqrt{1-x}}{3(x+1)^{3/2}} + \frac{1}{(x+1)^{3/2}\sqrt{1-x}}$$

[Out] $1/(1-x)^{(1/2)/(1+x)^{(3/2)}-2/3*(1-x)^{(1/2)/(1+x)^{(3/2)}-2/3*(1-x)^{(1/2)/(1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$-\frac{2\sqrt{1-x}}{3\sqrt{x+1}} - \frac{2\sqrt{1-x}}{3(x+1)^{3/2}} + \frac{1}{(x+1)^{3/2}\sqrt{1-x}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - x)^(3/2)*(1 + x)^(5/2)),x]

[Out] $1/(\text{Sqrt}[1 - x]*(1 + x)^{(3/2)}) - (2*\text{Sqrt}[1 - x])/(3*(1 + x)^{(3/2)}) - (2*\text{Sqrt}[1 - x])/(3*\text{Sqrt}[1 + x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(1-x)^{3/2}(1+x)^{5/2}} dx &= \frac{1}{\sqrt{1-x}(1+x)^{3/2}} + 2 \int \frac{1}{\sqrt{1-x}(1+x)^{5/2}} dx \\
&= \frac{1}{\sqrt{1-x}(1+x)^{3/2}} - \frac{2\sqrt{1-x}}{3(1+x)^{3/2}} + \frac{2}{3} \int \frac{1}{\sqrt{1-x}(1+x)^{3/2}} dx \\
&= \frac{1}{\sqrt{1-x}(1+x)^{3/2}} - \frac{2\sqrt{1-x}}{3(1+x)^{3/2}} - \frac{2\sqrt{1-x}}{3\sqrt{1+x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 0.52

$$\frac{2x^2 + 2x - 1}{3\sqrt{1-x}(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(3/2)*(1+x)^(5/2)),x]

[Out] (-1 + 2*x + 2*x^2)/(3*sqrt[1-x]*(1+x)^(3/2))

fricas [A] time = 0.44, size = 49, normalized size = 0.84

$$\frac{x^3 + x^2 + (2x^2 + 2x - 1)\sqrt{x+1}\sqrt{-x+1} - x - 1}{3(x^3 + x^2 - x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(3/2)/(1+x)^(5/2),x, algorithm="fricas")

[Out] -1/3*(x^3 + x^2 + (2*x^2 + 2*x - 1)*sqrt(x + 1)*sqrt(-x + 1) - x - 1)/(x^3 + x^2 - x - 1)

giac [B] time = 0.68, size = 108, normalized size = 1.86

$$\frac{(\sqrt{2} - \sqrt{-x+1})^3}{96(x+1)^{\frac{3}{2}}} + \frac{7(\sqrt{2} - \sqrt{-x+1})}{32\sqrt{x+1}} - \frac{\sqrt{x+1}\sqrt{-x+1}}{4(x-1)} - \frac{(x+1)^{\frac{3}{2}} \left(\frac{21(\sqrt{2} - \sqrt{-x+1})^2}{x+1} + 1 \right)}{96(\sqrt{2} - \sqrt{-x+1})^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(3/2)/(1+x)^(5/2),x, algorithm="giac")

[Out] $\frac{1}{96}(\sqrt{2} - \sqrt{-x + 1})^3/(x + 1)^{3/2} + \frac{7}{32}(\sqrt{2} - \sqrt{-x + 1})/\sqrt{x + 1} - \frac{1}{4}\sqrt{x + 1}\sqrt{-x + 1}/(x - 1) - \frac{1}{96}(x + 1)^{3/2} * (21(\sqrt{2} - \sqrt{-x + 1})^2/(x + 1) + 1)/(\sqrt{2} - \sqrt{-x + 1})^3$

maple [A] time = 0.00, size = 25, normalized size = 0.43

$$\frac{2x^2 + 2x - 1}{3(x + 1)^{\frac{3}{2}} \sqrt{-x + 1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-x+1)^(3/2)/(x+1)^(5/2),x)`

[Out] $\frac{1}{3} * (2x^2 + 2x - 1) / (x + 1)^{3/2} / (-x + 1)^{1/2}$

maxima [A] time = 1.35, size = 38, normalized size = 0.66

$$\frac{2x}{3\sqrt{-x^2 + 1}} - \frac{1}{3\left(\sqrt{-x^2 + 1}x + \sqrt{-x^2 + 1}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(3/2)/(1+x)^(5/2),x, algorithm="maxima")`

[Out] $\frac{2}{3} * x / \sqrt{-x^2 + 1} - \frac{1}{3} / (\sqrt{-x^2 + 1} * x + \sqrt{-x^2 + 1})$

mupad [B] time = 0.34, size = 48, normalized size = 0.83

$$-\frac{2x\sqrt{1-x} - \sqrt{1-x} + 2x^2\sqrt{1-x}}{(3x^2 - 3)\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((1 - x)^(3/2)*(x + 1)^(5/2)),x)`

[Out] $-(2x*(1 - x)^{1/2} - (1 - x)^{1/2} + 2x^2*(1 - x)^{1/2}) / ((3x^2 - 3)*(x + 1)^{1/2})$

sympy [A] time = 5.40, size = 165, normalized size = 2.84

$$\begin{cases} -\frac{2\sqrt{-1+\frac{2}{x+1}}(x+1)^2}{-6x+3(x+1)^2-6} + \frac{2\sqrt{-1+\frac{2}{x+1}}(x+1)}{-6x+3(x+1)^2-6} + \frac{\sqrt{-1+\frac{2}{x+1}}}{-6x+3(x+1)^2-6} & \text{for } \frac{2}{|x+1}| > 1 \\ -\frac{2i\sqrt{1-\frac{2}{x+1}}(x+1)^2}{-6x+3(x+1)^2-6} + \frac{2i\sqrt{1-\frac{2}{x+1}}(x+1)}{-6x+3(x+1)^2-6} + \frac{i\sqrt{1-\frac{2}{x+1}}}{-6x+3(x+1)^2-6} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(1-x)**(3/2)/(1+x)**(5/2),x)
```

```
[Out] Piecewise((-2*sqrt(-1 + 2/(x + 1))*(x + 1)**2/(-6*x + 3*(x + 1)**2 - 6) + 2*sqrt(-1 + 2/(x + 1))*(x + 1)/(-6*x + 3*(x + 1)**2 - 6) + sqrt(-1 + 2/(x + 1)))/(-6*x + 3*(x + 1)**2 - 6), 2/Abs(x + 1) > 1), (-2*I*sqrt(1 - 2/(x + 1))*(x + 1)**2/(-6*x + 3*(x + 1)**2 - 6) + 2*I*sqrt(1 - 2/(x + 1))*(x + 1)/(-6*x + 3*(x + 1)**2 - 6) + I*sqrt(1 - 2/(x + 1)))/(-6*x + 3*(x + 1)**2 - 6), True))
```

$$3.1133 \quad \int \frac{1}{(1-x)^{5/2}(1+x)^{5/2}} dx$$

Optimal. Leaf size=43

$$\frac{2x}{3\sqrt{1-x}\sqrt{x+1}} + \frac{x}{3(1-x)^{3/2}(x+1)^{3/2}}$$

[Out] $1/3*x/(1-x)^{(3/2)/(1+x)^{(3/2)}+2/3*x/(1-x)^{(1/2)/(1+x)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {40, 39}

$$\frac{2x}{3\sqrt{1-x}\sqrt{x+1}} + \frac{x}{3(1-x)^{3/2}(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - x)^(5/2)*(1 + x)^(5/2)),x]

[Out] x/(3*(1 - x)^(3/2)*(1 + x)^(3/2)) + (2*x)/(3*Sqrt[1 - x]*Sqrt[1 + x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] :> Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> -Simp[(x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{(1-x)^{5/2}(1+x)^{5/2}} dx &= \frac{x}{3(1-x)^{3/2}(1+x)^{3/2}} + \frac{2}{3} \int \frac{1}{(1-x)^{3/2}(1+x)^{3/2}} dx \\ &= \frac{x}{3(1-x)^{3/2}(1+x)^{3/2}} + \frac{2x}{3\sqrt{1-x}\sqrt{1+x}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.53

$$-\frac{x(2x^2 - 3)}{3(1 - x^2)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1 - x)^(5/2)*(1 + x)^(5/2)), x]

[Out] -1/3*(x*(-3 + 2*x^2))/(1 - x^2)^(3/2)

fricas [A] time = 0.47, size = 35, normalized size = 0.81

$$-\frac{(2x^3 - 3x)\sqrt{x+1}\sqrt{-x+1}}{3(x^4 - 2x^2 + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(5/2)/(1+x)^(5/2), x, algorithm="fricas")

[Out] -1/3*(2*x^3 - 3*x)*sqrt(x + 1)*sqrt(-x + 1)/(x^4 - 2*x^2 + 1)

giac [B] time = 0.68, size = 113, normalized size = 2.63

$$\frac{(\sqrt{2} - \sqrt{-x+1})^3}{192(x+1)^{\frac{3}{2}}} + \frac{11(\sqrt{2} - \sqrt{-x+1})}{64\sqrt{x+1}} - \frac{(4x-5)\sqrt{x+1}\sqrt{-x+1}}{12(x-1)^2} - \frac{(x+1)^{\frac{3}{2}}\left(\frac{33(\sqrt{2}-\sqrt{-x+1})^2}{x+1} + 1\right)}{192(\sqrt{2} - \sqrt{-x+1})^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(5/2)/(1+x)^(5/2), x, algorithm="giac")

[Out] 1/192*(sqrt(2) - sqrt(-x + 1))^3/(x + 1)^(3/2) + 11/64*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) - 1/12*(4*x - 5)*sqrt(x + 1)*sqrt(-x + 1)/(x - 1)^2 - 1/192*(x + 1)^(3/2)*(33*(sqrt(2) - sqrt(-x + 1))^2/(x + 1) + 1)/(sqrt(2) - sqrt(-x + 1))^3

maple [A] time = 0.00, size = 23, normalized size = 0.53

$$-\frac{(2x^2 - 3)x}{3(x+1)^{\frac{3}{2}}(-x+1)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-x+1)^(5/2)/(x+1)^(5/2),x)`

[Out] `-1/3*x*(2*x^2-3)/(x+1)^(3/2)/(-x+1)^(3/2)`

maxima [A] time = 1.39, size = 25, normalized size = 0.58

$$\frac{2x}{3\sqrt{-x^2+1}} + \frac{x}{3(-x^2+1)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)^(5/2)/(1+x)^(5/2),x, algorithm="maxima")`

[Out] `2/3*x/sqrt(-x^2 + 1) + 1/3*x/(-x^2 + 1)^(3/2)`

mupad [B] time = 0.37, size = 41, normalized size = 0.95

$$\frac{3x\sqrt{1-x} - 2x^3\sqrt{1-x}}{(3x+3)(x-1)^2\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((1-x)^(5/2)*(x+1)^(5/2)),x)`

[Out] `(3*x*(1-x)^(1/2) - 2*x^3*(1-x)^(1/2))/((3*x+3)*(x-1)^2*(x+1)^(1/2))`

sympy [B] time = 9.61, size = 279, normalized size = 6.49

$$\left\{ \begin{array}{ll} \frac{2\sqrt{-1+\frac{2}{x+1}}(x+1)^3}{12x+3(x+1)^3-12(x+1)^2+12} + \frac{6\sqrt{-1+\frac{2}{x+1}}(x+1)^2}{12x+3(x+1)^3-12(x+1)^2+12} - \frac{3\sqrt{-1+\frac{2}{x+1}}(x+1)}{12x+3(x+1)^3-12(x+1)^2+12} - \frac{\sqrt{-1+\frac{2}{x+1}}}{12x+3(x+1)^3-12(x+1)^2+12} & \text{for } \frac{2}{|x+1|} > 1 \\ \frac{2i\sqrt{1-\frac{2}{x+1}}(x+1)^3}{12x+3(x+1)^3-12(x+1)^2+12} + \frac{6i\sqrt{1-\frac{2}{x+1}}(x+1)^2}{12x+3(x+1)^3-12(x+1)^2+12} - \frac{3i\sqrt{1-\frac{2}{x+1}}(x+1)}{12x+3(x+1)^3-12(x+1)^2+12} - \frac{i\sqrt{1-\frac{2}{x+1}}}{12x+3(x+1)^3-12(x+1)^2+12} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(1-x)**(5/2)/(1+x)**(5/2),x)`

[Out] `Piecewise((-2*sqrt(-1 + 2/(x + 1))*(x + 1)**3/(12*x + 3*(x + 1)**3 - 12*(x + 1)**2 + 12) + 6*sqrt(-1 + 2/(x + 1))*(x + 1)**2/(12*x + 3*(x + 1)**3 - 12*(x + 1)**2 + 12) - 3*sqrt(-1 + 2/(x + 1))*(x + 1)/(12*x + 3*(x + 1)**3 - 12*(x + 1)**2 + 12) - sqrt(-1 + 2/(x + 1))/(12*x + 3*(x + 1)**3 - 12*(x + 1)**2 + 12), 2/Abs(x + 1) > 1, (-2*I*sqrt(1 - 2/(x + 1))*(x + 1)**3/(12*x + 3*(x + 1)**3 - 12*(x + 1)**2 + 12) + 6*I*sqrt(1 - 2/(x + 1))*(x + 1)**2/(12*x + 3*(x + 1)**3 - 12*(x + 1)**2 + 12) - 3*I*sqrt(1 - 2/(x + 1))*(x + 1)/(12*x + 3*(x + 1)**3 - 12*(x + 1)**2 + 12) - I*sqrt(1 - 2/(x + 1))/(12*x + 3*(x + 1)**3 - 12*(x + 1)**2 + 12), True))`

$$3.1134 \quad \int \frac{1}{(1-x)^{7/2}(1+x)^{5/2}} dx$$

Optimal. Leaf size=63

$$\frac{8x}{15\sqrt{1-x}\sqrt{x+1}} + \frac{4x}{15(1-x)^{3/2}(x+1)^{3/2}} + \frac{1}{5(1-x)^{5/2}(x+1)^{3/2}}$$

[Out] 1/5/(1-x)^(5/2)/(1+x)^(3/2)+4/15*x/(1-x)^(3/2)/(1+x)^(3/2)+8/15*x/(1-x)^(1/2)/(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {45, 40, 39}

$$\frac{8x}{15\sqrt{1-x}\sqrt{x+1}} + \frac{4x}{15(1-x)^{3/2}(x+1)^{3/2}} + \frac{1}{5(1-x)^{5/2}(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((1-x)^(7/2)*(1+x)^(5/2)),x]

[Out] 1/(5*(1-x)^(5/2)*(1+x)^(3/2)) + (4*x)/(15*(1-x)^(3/2)*(1+x)^(3/2)) + (8*x)/(15*Sqrt[1-x]*Sqrt[1+x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := S
imp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && Eq
Q[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := -Simp[(
x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)
/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[
{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
+ d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler

Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{1}{(1-x)^{7/2}(1+x)^{5/2}} dx &= \frac{1}{5(1-x)^{5/2}(1+x)^{3/2}} + \frac{4}{5} \int \frac{1}{(1-x)^{5/2}(1+x)^{5/2}} dx \\ &= \frac{1}{5(1-x)^{5/2}(1+x)^{3/2}} + \frac{4x}{15(1-x)^{3/2}(1+x)^{3/2}} + \frac{8}{15} \int \frac{1}{(1-x)^{3/2}(1+x)^{3/2}} dx \\ &= \frac{1}{5(1-x)^{5/2}(1+x)^{3/2}} + \frac{4x}{15(1-x)^{3/2}(1+x)^{3/2}} + \frac{8x}{15\sqrt{1-x}\sqrt{1+x}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 0.63

$$\frac{8x^4 - 8x^3 - 12x^2 + 12x + 3}{15(1-x)^{5/2}(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1 - x)^(7/2)*(1 + x)^(5/2)), x]

[Out] (3 + 12*x - 12*x^2 - 8*x^3 + 8*x^4)/(15*(1 - x)^(5/2)*(1 + x)^(3/2))

fricas [A] time = 0.44, size = 84, normalized size = 1.33

$$\frac{3x^5 - 3x^4 - 6x^3 + 6x^2 - (8x^4 - 8x^3 - 12x^2 + 12x + 3)\sqrt{x+1}\sqrt{-x+1} + 3x - 3}{15(x^5 - x^4 - 2x^3 + 2x^2 + x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(7/2)/(1+x)^(5/2), x, algorithm="fricas")

[Out] 1/15*(3*x^5 - 3*x^4 - 6*x^3 + 6*x^2 - (8*x^4 - 8*x^3 - 12*x^2 + 12*x + 3)*sqrt(x + 1)*sqrt(-x + 1) + 3*x - 3)/(x^5 - x^4 - 2*x^3 + 2*x^2 + x - 1)

giac [B] time = 0.71, size = 119, normalized size = 1.89

$$\frac{(\sqrt{2} - \sqrt{-x+1})^3}{384(x+1)^{\frac{3}{2}}} + \frac{15(\sqrt{2} - \sqrt{-x+1})}{128\sqrt{x+1}} - \frac{(x+1)^{\frac{3}{2}} \left(\frac{45(\sqrt{2} - \sqrt{-x+1})^2}{x+1} + 1 \right)}{384(\sqrt{2} - \sqrt{-x+1})^3} - \frac{((73x - 247)(x+1) + 360)\sqrt{x+1}\sqrt{-x}}{240(x-1)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(7/2)/(1+x)^(5/2),x, algorithm="giac")

[Out] $\frac{1}{384}(\sqrt{2} - \sqrt{-x + 1})^3/(x + 1)^{3/2} + \frac{15}{128}(\sqrt{2} - \sqrt{-x + 1})/\sqrt{x + 1} - \frac{1}{384}(x + 1)^{3/2}*(45*(\sqrt{2} - \sqrt{-x + 1})^2/(x + 1) + 1)/(\sqrt{2} - \sqrt{-x + 1})^3 - \frac{1}{240}((73*x - 247)*(x + 1) + 360)*\sqrt{x + 1}*\sqrt{-x + 1}/(x - 1)^3$

maple [A] time = 0.00, size = 35, normalized size = 0.56

$$\frac{8x^4 - 8x^3 - 12x^2 + 12x + 3}{15(x+1)^{\frac{3}{2}}(-x+1)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+1)^(7/2)/(x+1)^(5/2),x)

[Out] $\frac{1}{15}(8*x^4-8*x^3-12*x^2+12*x+3)/(x+1)^{3/2}/(-x+1)^{5/2}$

maxima [A] time = 1.39, size = 52, normalized size = 0.83

$$\frac{8x}{15\sqrt{-x^2+1}} + \frac{4x}{15(-x^2+1)^{\frac{3}{2}}} - \frac{1}{5\left(\left(-x^2+1\right)^{\frac{3}{2}}x - \left(-x^2+1\right)^{\frac{3}{2}}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(7/2)/(1+x)^(5/2),x, algorithm="maxima")

[Out] $\frac{8}{15}x/\sqrt{-x^2+1} + \frac{4}{15}x/(-x^2+1)^{3/2} - \frac{1}{5}/((-x^2+1)^{3/2}*x - (-x^2+1)^{3/2})$

mupad [B] time = 0.38, size = 75, normalized size = 1.19

$$\frac{12x\sqrt{1-x} + 3\sqrt{1-x} - 12x^2\sqrt{1-x} - 8x^3\sqrt{1-x} + 8x^4\sqrt{1-x}}{(15x+15)(x-1)^3\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((1-x)^(7/2)*(x+1)^(5/2)),x)

[Out] $-(12*x*(1-x)^{1/2} + 3*(1-x)^{1/2} - 12*x^2*(1-x)^{1/2} - 8*x^3*(1-x)^{1/2} + 8*x^4*(1-x)^{1/2})/((15*x+15)*(x-1)^3*(x+1)^{1/2})$

sympy [B] time = 27.61, size = 423, normalized size = 6.71

$$\left\{ \begin{array}{l} -\frac{8\sqrt{-1+\frac{2}{x+1}}(x+1)^4}{-120x+15(x+1)^4-90(x+1)^3+180(x+1)^2-120} + \frac{40\sqrt{-1+\frac{2}{x+1}}(x+1)^3}{-120x+15(x+1)^4-90(x+1)^3+180(x+1)^2-120} - \frac{60\sqrt{-1+\frac{2}{x+1}}(x+1)^2}{-120x+15(x+1)^4-90(x+1)^3+180(x+1)^2-120} + \\ -\frac{8i\sqrt{1-\frac{2}{x+1}}(x+1)^4}{-120x+15(x+1)^4-90(x+1)^3+180(x+1)^2-120} + \frac{40i\sqrt{1-\frac{2}{x+1}}(x+1)^3}{-120x+15(x+1)^4-90(x+1)^3+180(x+1)^2-120} - \frac{60i\sqrt{1-\frac{2}{x+1}}(x+1)^2}{-120x+15(x+1)^4-90(x+1)^3+180(x+1)^2-120} + \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)**(7/2)/(1+x)**(5/2),x)

[Out] Piecewise((-8*sqrt(-1 + 2/(x + 1))*(x + 1)**4/(-120*x + 15*(x + 1)**4 - 90*(x + 1)**3 + 180*(x + 1)**2 - 120) + 40*sqrt(-1 + 2/(x + 1))*(x + 1)**3/(-120*x + 15*(x + 1)**4 - 90*(x + 1)**3 + 180*(x + 1)**2 - 120) - 60*sqrt(-1 + 2/(x + 1))*(x + 1)**2/(-120*x + 15*(x + 1)**4 - 90*(x + 1)**3 + 180*(x + 1)**2 - 120) + 20*sqrt(-1 + 2/(x + 1))*(x + 1)/(-120*x + 15*(x + 1)**4 - 90*(x + 1)**3 + 180*(x + 1)**2 - 120) + 5*sqrt(-1 + 2/(x + 1))/(-120*x + 15*(x + 1)**4 - 90*(x + 1)**3 + 180*(x + 1)**2 - 120), 2/Abs(x + 1) > 1), (-8*I*sqrt(1 - 2/(x + 1))*(x + 1)**4/(-120*x + 15*(x + 1)**4 - 90*(x + 1)**3 + 180*(x + 1)**2 - 120) + 40*I*sqrt(1 - 2/(x + 1))*(x + 1)**3/(-120*x + 15*(x + 1)**4 - 90*(x + 1)**3 + 180*(x + 1)**2 - 120) - 60*I*sqrt(1 - 2/(x + 1))*(x + 1)**2/(-120*x + 15*(x + 1)**4 - 90*(x + 1)**3 + 180*(x + 1)**2 - 120) + 20*I*sqrt(1 - 2/(x + 1))*(x + 1)/(-120*x + 15*(x + 1)**4 - 90*(x + 1)**3 + 180*(x + 1)**2 - 120) + 5*I*sqrt(1 - 2/(x + 1))/(-120*x + 15*(x + 1)**4 - 90*(x + 1)**3 + 180*(x + 1)**2 - 120), True))

$$3.1135 \quad \int \frac{1}{(1-x)^{9/2}(1+x)^{5/2}} dx$$

Optimal. Leaf size=83

$$\frac{8x}{21\sqrt{1-x}\sqrt{x+1}} + \frac{4x}{21(1-x)^{3/2}(x+1)^{3/2}} + \frac{1}{7(1-x)^{5/2}(x+1)^{3/2}} + \frac{1}{7(1-x)^{7/2}(x+1)^{3/2}}$$

[Out] 1/7/(1-x)^(7/2)/(1+x)^(3/2)+1/7/(1-x)^(5/2)/(1+x)^(3/2)+4/21*x/(1-x)^(3/2)/(1+x)^(3/2)+8/21*x/(1-x)^(1/2)/(1+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 83, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {45, 40, 39}

$$\frac{8x}{21\sqrt{1-x}\sqrt{x+1}} + \frac{4x}{21(1-x)^{3/2}(x+1)^{3/2}} + \frac{1}{7(1-x)^{5/2}(x+1)^{3/2}} + \frac{1}{7(1-x)^{7/2}(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((1-x)^(9/2)*(1+x)^(5/2)),x]

[Out] 1/(7*(1-x)^(7/2)*(1+x)^(3/2)) + 1/(7*(1-x)^(5/2)*(1+x)^(3/2)) + (4*x)/(21*(1-x)^(3/2)*(1+x)^(3/2)) + (8*x)/(21*Sqrt[1-x]*Sqrt[1+x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := S
imp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && Eq
Q[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := -Simp[(
x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)
/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[
{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
+ d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler

Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{1}{(1-x)^{9/2}(1+x)^{5/2}} dx &= \frac{1}{7(1-x)^{7/2}(1+x)^{3/2}} + \frac{5}{7} \int \frac{1}{(1-x)^{7/2}(1+x)^{5/2}} dx \\ &= \frac{1}{7(1-x)^{7/2}(1+x)^{3/2}} + \frac{1}{7(1-x)^{5/2}(1+x)^{3/2}} + \frac{4}{7} \int \frac{1}{(1-x)^{5/2}(1+x)^{5/2}} dx \\ &= \frac{1}{7(1-x)^{7/2}(1+x)^{3/2}} + \frac{1}{7(1-x)^{5/2}(1+x)^{3/2}} + \frac{4x}{21(1-x)^{3/2}(1+x)^{3/2}} + \frac{8}{21} \int \frac{1}{(1-x)^{3/2}} dx \\ &= \frac{1}{7(1-x)^{7/2}(1+x)^{3/2}} + \frac{1}{7(1-x)^{5/2}(1+x)^{3/2}} + \frac{4x}{21(1-x)^{3/2}(1+x)^{3/2}} + \frac{8x}{21\sqrt{1-x}\sqrt{1+x}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 45, normalized size = 0.54

$$\frac{-8x^5 + 16x^4 + 4x^3 - 24x^2 + 9x + 6}{21(1-x)^{7/2}(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(9/2)*(1+x)^(5/2)),x]

[Out] (6 + 9*x - 24*x^2 + 4*x^3 + 16*x^4 - 8*x^5)/(21*(1-x)^(7/2)*(1+x)^(3/2))

fricas [A] time = 0.44, size = 101, normalized size = 1.22

$$\frac{6x^6 - 12x^5 - 6x^4 + 24x^3 - 6x^2 - (8x^5 - 16x^4 - 4x^3 + 24x^2 - 9x - 6)\sqrt{x+1}\sqrt{-x+1} - 12x + 6}{21(x^6 - 2x^5 - x^4 + 4x^3 - x^2 - 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(9/2)/(1+x)^(5/2),x, algorithm="fricas")

[Out] 1/21*(6*x^6 - 12*x^5 - 6*x^4 + 24*x^3 - 6*x^2 - (8*x^5 - 16*x^4 - 4*x^3 + 24*x^2 - 9*x - 6)*sqrt(x + 1)*sqrt(-x + 1) - 12*x + 6)/(x^6 - 2*x^5 - x^4 + 4*x^3 - x^2 - 2*x + 1)

giac [B] time = 0.69, size = 125, normalized size = 1.51

$$\frac{(\sqrt{2} - \sqrt{-x+1})^3}{768(x+1)^{\frac{3}{2}}} + \frac{19(\sqrt{2} - \sqrt{-x+1})}{256\sqrt{x+1}} - \frac{(x+1)^{\frac{3}{2}} \left(\frac{57(\sqrt{2} - \sqrt{-x+1})^2}{x+1} + 1 \right)}{768(\sqrt{2} - \sqrt{-x+1})^3} - \frac{(((79x - 432)(x+1) + 1120)(x+1) - 8)}{336(x-1)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(9/2)/(1+x)^(5/2),x, algorithm="giac")

[Out] $\frac{1}{768}(\sqrt{2} - \sqrt{-x + 1})^3/(x + 1)^{3/2} + \frac{19}{256}(\sqrt{2} - \sqrt{-x + 1})/\sqrt{x + 1} - \frac{1}{768}(x + 1)^{3/2} * (57(\sqrt{2} - \sqrt{-x + 1})^2/(x + 1) + 1)/(\sqrt{2} - \sqrt{-x + 1})^3 - \frac{1}{336}(((79x - 432)(x + 1) + 1120)(x + 1) - 840)\sqrt{x + 1}\sqrt{-x + 1}/(x - 1)^4$

maple [A] time = 0.00, size = 40, normalized size = 0.48

$$\frac{8x^5 - 16x^4 - 4x^3 + 24x^2 - 9x - 6}{21(x+1)^{\frac{3}{2}}(-x+1)^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+1)^(9/2)/(x+1)^(5/2),x)

[Out] $-1/21*(8*x^5-16*x^4-4*x^3+24*x^2-9*x-6)/(x+1)^{(3/2)/(-x+1)^{(7/2)}$

maxima [A] time = 1.34, size = 91, normalized size = 1.10

$$\frac{8x}{21\sqrt{-x^2+1}} + \frac{4x}{21(-x^2+1)^{\frac{3}{2}}} + \frac{1}{7\left(\left(-x^2+1\right)^{\frac{3}{2}}x^2 - 2\left(-x^2+1\right)^{\frac{3}{2}}x + \left(-x^2+1\right)^{\frac{3}{2}}\right)} - \frac{1}{7\left(\left(-x^2+1\right)^{\frac{3}{2}}x - \left(-x^2+1\right)^{\frac{3}{2}}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(9/2)/(1+x)^(5/2),x, algorithm="maxima")

[Out] $\frac{8}{21}x/\sqrt{-x^2 + 1} + \frac{4}{21}x/(-x^2 + 1)^{3/2} + \frac{1}{7}/((-x^2 + 1)^{3/2}*x^2 - 2*(-x^2 + 1)^{3/2}*x + (-x^2 + 1)^{3/2}) - \frac{1}{7}/((-x^2 + 1)^{3/2}*x - (-x^2 + 1)^{3/2})$

mupad [B] time = 0.41, size = 86, normalized size = 1.04

$$\frac{9x\sqrt{1-x} + 6\sqrt{1-x} - 24x^2\sqrt{1-x} + 4x^3\sqrt{1-x} + 16x^4\sqrt{1-x} - 8x^5\sqrt{1-x}}{(21x+21)(x-1)^4\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(((1-x)^(9/2)*(x+1)^(5/2))),x)

[Out] $(9*x*(1-x)^{(1/2)} + 6*(1-x)^{(1/2)} - 24*x^2*(1-x)^{(1/2)} + 4*x^3*(1-x)^{(1/2)} + 16*x^4*(1-x)^{(1/2)} - 8*x^5*(1-x)^{(1/2)})/((21*x+21)*(x-1)^4*(x+1)^{(1/2)})$

sympy [B] time = 71.01, size = 592, normalized size = 7.13

$$\left\{ \begin{array}{l} \frac{8\sqrt{-1+\frac{2}{x+1}}(x+1)^5}{-336x-21(x+1)^5+168(x+1)^4-504(x+1)^3+672(x+1)^2-336} - \frac{56\sqrt{-1+\frac{2}{x+1}}(x+1)^4}{-336x-21(x+1)^5+168(x+1)^4-504(x+1)^3+672(x+1)^2-336} + \frac{140\sqrt{-1+\frac{2}{x+1}}(x+1)^3}{-336x-21(x+1)^5+168(x+1)^4-504(x+1)^3+672(x+1)^2-336} \\ \frac{8i\sqrt{1-\frac{2}{x+1}}(x+1)^5}{-336x-21(x+1)^5+168(x+1)^4-504(x+1)^3+672(x+1)^2-336} - \frac{56i\sqrt{1-\frac{2}{x+1}}(x+1)^4}{-336x-21(x+1)^5+168(x+1)^4-504(x+1)^3+672(x+1)^2-336} + \frac{140i\sqrt{1-\frac{2}{x+1}}(x+1)^3}{-336x-21(x+1)^5+168(x+1)^4-504(x+1)^3+672(x+1)^2-336} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)**(9/2)/(1+x)**(5/2),x)

[Out] Piecewise((8*sqrt(-1 + 2/(x + 1))*(x + 1)**5/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336) - 56*sqrt(-1 + 2/(x + 1))*(x + 1)**4/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336) + 140*sqrt(-1 + 2/(x + 1))*(x + 1)**3/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336) - 140*sqrt(-1 + 2/(x + 1))*(x + 1)**2/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336) + 35*sqrt(-1 + 2/(x + 1))*(x + 1)/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336) + 7*sqrt(-1 + 2/(x + 1))/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336), 2/Abs(x + 1) > 1), (8*I*sqrt(1 - 2/(x + 1))*(x + 1)**5/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336) - 56*I*sqrt(1 - 2/(x + 1))*(x + 1)**4/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336) + 140*I*sqrt(1 - 2/(x + 1))*(x + 1)**3/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336) - 140*I*sqrt(1 - 2/(x + 1))*(x + 1)**2/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336) + 35*I*sqrt(1 - 2/(x + 1))*(x + 1)/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336) + 7*I*sqrt(1 - 2/(x + 1))/(-336*x - 21*(x + 1)**5 + 168*(x + 1)**4 - 504*(x + 1)**3 + 672*(x + 1)**2 - 336), True))

$$3.1136 \quad \int \frac{1}{(1-x)^{11/2}(1+x)^{5/2}} dx$$

Optimal. Leaf size=103

$$\frac{16x}{63\sqrt{1-x}\sqrt{x+1}} + \frac{8x}{63(1-x)^{3/2}(x+1)^{3/2}} + \frac{2}{21(1-x)^{5/2}(x+1)^{3/2}} + \frac{2}{21(1-x)^{7/2}(x+1)^{3/2}} + \frac{1}{9(1-x)^{9/2}(x+1)^{3/2}}$$

[Out] 1/9/(1-x)^(9/2)/(1+x)^(3/2)+2/21/(1-x)^(7/2)/(1+x)^(3/2)+2/21/(1-x)^(5/2)/(1+x)^(3/2)+8/63*x/(1-x)^(3/2)/(1+x)^(3/2)+16/63*x/(1-x)^(1/2)/(1+x)^(1/2)

Rubi [A] time = 0.02, antiderivative size = 103, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {45, 40, 39}

$$\frac{16x}{63\sqrt{1-x}\sqrt{x+1}} + \frac{8x}{63(1-x)^{3/2}(x+1)^{3/2}} + \frac{2}{21(1-x)^{5/2}(x+1)^{3/2}} + \frac{2}{21(1-x)^{7/2}(x+1)^{3/2}} + \frac{1}{9(1-x)^{9/2}(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((1-x)^(11/2)*(1+x)^(5/2)),x]

[Out] 1/(9*(1-x)^(9/2)*(1+x)^(3/2)) + 2/(21*(1-x)^(7/2)*(1+x)^(3/2)) + 2/(21*(1-x)^(5/2)*(1+x)^(3/2)) + (8*x)/(63*(1-x)^(3/2)*(1+x)^(3/2)) + (16*x)/(63*Sqrt[1-x]*Sqrt[1+x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := S
imp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && Eq
Q[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := -Simp[(
x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)
/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[
{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
+ d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&

(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(1-x)^{11/2}(1+x)^{5/2}} dx &= \frac{1}{9(1-x)^{9/2}(1+x)^{3/2}} + \frac{2}{3} \int \frac{1}{(1-x)^{9/2}(1+x)^{5/2}} dx \\
 &= \frac{1}{9(1-x)^{9/2}(1+x)^{3/2}} + \frac{2}{21(1-x)^{7/2}(1+x)^{3/2}} + \frac{10}{21} \int \frac{1}{(1-x)^{7/2}(1+x)^{5/2}} dx \\
 &= \frac{1}{9(1-x)^{9/2}(1+x)^{3/2}} + \frac{2}{21(1-x)^{7/2}(1+x)^{3/2}} + \frac{2}{21(1-x)^{5/2}(1+x)^{3/2}} + \frac{8}{21} \int \frac{1}{(1-x)^{5/2}(1+x)^{3/2}} dx \\
 &= \frac{1}{9(1-x)^{9/2}(1+x)^{3/2}} + \frac{2}{21(1-x)^{7/2}(1+x)^{3/2}} + \frac{2}{21(1-x)^{5/2}(1+x)^{3/2}} + \frac{8x}{63(1-x)^{3/2}(1+x)^{3/2}} \\
 &= \frac{1}{9(1-x)^{9/2}(1+x)^{3/2}} + \frac{2}{21(1-x)^{7/2}(1+x)^{3/2}} + \frac{2}{21(1-x)^{5/2}(1+x)^{3/2}} + \frac{8x}{63(1-x)^{3/2}(1+x)^{3/2}}
 \end{aligned}$$

Mathematica [A] time = 0.01, size = 50, normalized size = 0.49

$$\frac{16x^6 - 48x^5 + 24x^4 + 56x^3 - 66x^2 + 6x + 19}{63(1-x)^{9/2}(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1-x)^(11/2)*(1+x)^(5/2)),x]

[Out] (19 + 6*x - 66*x^2 + 56*x^3 + 24*x^4 - 48*x^5 + 16*x^6)/(63*(1-x)^(9/2)*(1+x)^(3/2))

fricas [A] time = 0.43, size = 114, normalized size = 1.11

$$\frac{19x^7 - 57x^6 + 19x^5 + 95x^4 - 95x^3 - 19x^2 - (16x^6 - 48x^5 + 24x^4 + 56x^3 - 66x^2 + 6x + 19)\sqrt{x+1}\sqrt{-x+1}}{63(x^7 - 3x^6 + x^5 + 5x^4 - 5x^3 - x^2 + 3x - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(11/2)/(1+x)^(5/2),x, algorithm="fricas")

[Out] 1/63*(19*x^7 - 57*x^6 + 19*x^5 + 95*x^4 - 95*x^3 - 19*x^2 - (16*x^6 - 48*x^5 + 24*x^4 + 56*x^3 - 66*x^2 + 6*x + 19)*sqrt(x+1)*sqrt(-x+1) + 57*x - 19)/(x^7 - 3*x^6 + x^5 + 5*x^4 - 5*x^3 - x^2 + 3*x - 1)

giac [A] time = 0.74, size = 131, normalized size = 1.27

$$\frac{(\sqrt{2} - \sqrt{-x+1})^3}{1536(x+1)^{\frac{3}{2}}} + \frac{23(\sqrt{2} - \sqrt{-x+1})}{512\sqrt{x+1}} - \frac{(x+1)^{\frac{3}{2}} \left(\frac{69(\sqrt{2} - \sqrt{-x+1})^2}{x+1} + 1 \right)}{1536(\sqrt{2} - \sqrt{-x+1})^3} \frac{((((667x - 5021)(x+1) + 18396)(x+1) + 18396)(x+1) - 26880)(x+1) + 15120)\sqrt{x+1}\sqrt{-x+1}}{40320(x-1)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(11/2)/(1+x)^(5/2), x, algorithm="giac")

[Out] 1/1536*(sqrt(2) - sqrt(-x + 1))^3/(x + 1)^(3/2) + 23/512*(sqrt(2) - sqrt(-x + 1))/sqrt(x + 1) - 1/1536*(x + 1)^(3/2)*(69*(sqrt(2) - sqrt(-x + 1))^2/(x + 1) + 1)/(sqrt(2) - sqrt(-x + 1))^3 - 1/4032*(((667*x - 5021)*(x + 1) + 18396)*(x + 1) - 26880)*(x + 1) + 15120)*sqrt(x + 1)*sqrt(-x + 1)/(x - 1)^5

maple [A] time = 0.00, size = 45, normalized size = 0.44

$$\frac{16x^6 - 48x^5 + 24x^4 + 56x^3 - 66x^2 + 6x + 19}{63(x+1)^{\frac{3}{2}}(-x+1)^{\frac{9}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+1)^(11/2)/(x+1)^(5/2), x)

[Out] 1/63*(16*x^6-48*x^5+24*x^4+56*x^3-66*x^2+6*x+19)/(x+1)^(3/2)/(-x+1)^(9/2)

maxima [A] time = 1.42, size = 146, normalized size = 1.42

$$\frac{16x}{63\sqrt{-x^2+1}} + \frac{8x}{63(-x^2+1)^{\frac{3}{2}}} - \frac{1}{9\left(\left(-x^2+1\right)^{\frac{3}{2}}x^3 - 3\left(-x^2+1\right)^{\frac{3}{2}}x^2 + 3\left(-x^2+1\right)^{\frac{3}{2}}x - \left(-x^2+1\right)^{\frac{3}{2}}\right)} + \frac{1}{21\left(\left(-x^2+1\right)^{\frac{3}{2}}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(1-x)^(11/2)/(1+x)^(5/2), x, algorithm="maxima")

[Out] 16/63*x/sqrt(-x^2 + 1) + 8/63*x/(-x^2 + 1)^(3/2) - 1/9/((-x^2 + 1)^(3/2)*x^3 - 3*(-x^2 + 1)^(3/2)*x^2 + 3*(-x^2 + 1)^(3/2)*x - (-x^2 + 1)^(3/2)) + 2/21/((-x^2 + 1)^(3/2)*x - (-x^2 + 1)^(3/2))

mupad [B] time = 0.42, size = 99, normalized size = 0.96

$$\frac{6x\sqrt{1-x} + 19\sqrt{1-x} - 66x^2\sqrt{1-x} + 56x^3\sqrt{1-x} + 24x^4\sqrt{1-x} - 48x^5\sqrt{1-x} + 16x^6\sqrt{1-x}}{(63x + 63)(x-1)^5\sqrt{x+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((1 - x)^(11/2)*(x + 1)^(5/2)),x)
```

```
[Out] -(6*x*(1 - x)^(1/2) + 19*(1 - x)^(1/2) - 66*x^2*(1 - x)^(1/2) + 56*x^3*(1 -
x)^(1/2) + 24*x^4*(1 - x)^(1/2) - 48*x^5*(1 - x)^(1/2) + 16*x^6*(1 - x)^(1
/2))/((63*x + 63)*(x - 1)^5*(x + 1)^(1/2))
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(1-x)**(11/2)/(1+x)**(5/2),x)
```

```
[Out] Timed out
```

3.1137 $\int (a + ax)^{5/2}(c - cx)^{5/2} dx$

Optimal. Leaf size=126

$$\frac{5}{8}a^{5/2}c^{5/2} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{ax+a}}{\sqrt{a}\sqrt{c-cx}}\right) + \frac{5}{16}a^2c^2x\sqrt{ax+a}\sqrt{c-cx} + \frac{5}{24}acx(ax+a)^{3/2}(c-cx)^{3/2} + \frac{1}{6}x(ax+a)^{5/2}(c-cx)^{5/2}$$

[Out] $5/24*a*c*x*(a*x+a)^{(3/2)}*(-c*x+c)^{(3/2)}+1/6*x*(a*x+a)^{(5/2)}*(-c*x+c)^{(5/2)}+5/8*a^{(5/2)}*c^{(5/2)}*\arctan(c^{(1/2)}*(a*x+a)^{(1/2)}/a^{(1/2)}/(-c*x+c)^{(1/2)})+5/16*a^2*c^2*x*(a*x+a)^{(1/2)}*(-c*x+c)^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {38, 63, 217, 203}

$$\frac{5}{16}a^2c^2x\sqrt{ax+a}\sqrt{c-cx} + \frac{5}{8}a^{5/2}c^{5/2} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{ax+a}}{\sqrt{a}\sqrt{c-cx}}\right) + \frac{5}{24}acx(ax+a)^{3/2}(c-cx)^{3/2} + \frac{1}{6}x(ax+a)^{5/2}(c-cx)^{5/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + a*x)^{(5/2)}*(c - c*x)^{(5/2)}, x]$

[Out] $(5*a^2*c^2*x*\text{Sqrt}[a + a*x]*\text{Sqrt}[c - c*x])/16 + (5*a*c*x*(a + a*x)^{(3/2)}*(c - c*x)^{(3/2)})/24 + (x*(a + a*x)^{(5/2)}*(c - c*x)^{(5/2)})/6 + (5*a^{(5/2)}*c^{(5/2)}*\text{ArcTan}[(\text{Sqrt}[c]*\text{Sqrt}[a + a*x])/(\text{Sqrt}[a]*\text{Sqrt}[c - c*x])])/8$

Rule 38

$\text{Int}[(a + b*x)^m*(c + d*x)^m, x_Symbol] \rightarrow \text{Simp}[(x*(a + b*x)^m*(c + d*x)^m)/(2*m + 1), x] + \text{Dist}[(2*a*c*m)/(2*m + 1), \text{Int}[(a + b*x)^{m-1}*(c + d*x)^{m-1}, x], x] /;$ FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 63

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{p*(m+1)-1}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

$\text{Int}[(a + b*x^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(1*\text{ArcTan}[\text{Rt}[b, 2]*x]/\text{Rt}[a, 2])]/(\text{Rt}[a, 2]*\text{Rt}[b, 2]), x] /;$ FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a

, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int (a + ax)^{5/2} (c - cx)^{5/2} dx &= \frac{1}{6} x (a + ax)^{5/2} (c - cx)^{5/2} + \frac{1}{6} (5ac) \int (a + ax)^{3/2} (c - cx)^{3/2} dx \\
 &= \frac{5}{24} acx (a + ax)^{3/2} (c - cx)^{3/2} + \frac{1}{6} x (a + ax)^{5/2} (c - cx)^{5/2} + \frac{1}{8} (5a^2c^2) \int \sqrt{a + ax} \sqrt{c - cx} dx \\
 &= \frac{5}{16} a^2c^2x \sqrt{a + ax} \sqrt{c - cx} + \frac{5}{24} acx (a + ax)^{3/2} (c - cx)^{3/2} + \frac{1}{6} x (a + ax)^{5/2} (c - cx)^{5/2} + \\
 &= \frac{5}{16} a^2c^2x \sqrt{a + ax} \sqrt{c - cx} + \frac{5}{24} acx (a + ax)^{3/2} (c - cx)^{3/2} + \frac{1}{6} x (a + ax)^{5/2} (c - cx)^{5/2} + \\
 &= \frac{5}{16} a^2c^2x \sqrt{a + ax} \sqrt{c - cx} + \frac{5}{24} acx (a + ax)^{3/2} (c - cx)^{3/2} + \frac{1}{6} x (a + ax)^{5/2} (c - cx)^{5/2} + \\
 &= \frac{5}{16} a^2c^2x \sqrt{a + ax} \sqrt{c - cx} + \frac{5}{24} acx (a + ax)^{3/2} (c - cx)^{3/2} + \frac{1}{6} x (a + ax)^{5/2} (c - cx)^{5/2} +
 \end{aligned}$$

Mathematica [A] time = 0.10, size = 114, normalized size = 0.90

$$\frac{c^{3/2} (a(x+1))^{5/2} \sqrt{c-cx} \left(\sqrt{c} x \sqrt{x+1} (8x^5 - 8x^4 - 26x^3 + 26x^2 + 33x - 33) + 30\sqrt{c-cx} \sin^{-1} \left(\frac{\sqrt{c-cx}}{\sqrt{2}\sqrt{c}} \right) \right)}{48(x-1)(x+1)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + a*x)^(5/2)*(c - c*x)^(5/2), x]

[Out] (c^(3/2)*(a*(1 + x))^(5/2)*Sqrt[c - c*x]*(Sqrt[c]*x*Sqrt[1 + x]*(-33 + 33*x + 26*x^2 - 26*x^3 - 8*x^4 + 8*x^5) + 30*Sqrt[c - c*x]*ArcSin[Sqrt[c - c*x]/(Sqrt[2]*Sqrt[c])])/(48*(-1 + x)*(1 + x)^(5/2))

fricas [A] time = 0.47, size = 201, normalized size = 1.60

$$\left[\frac{5}{32} \sqrt{-ac} a^2c^2 \log(2acx^2 + 2\sqrt{-ac}\sqrt{ax+a}\sqrt{-cx+cx-ac}) + \frac{1}{48} (8a^2c^2x^5 - 26a^2c^2x^3 + 33a^2c^2x) \sqrt{ax+a} \sqrt{-cx+cx-ac} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+a)^(5/2)*(-c*x+c)^(5/2),x, algorithm="fricas")

[Out] [5/32*sqrt(-a*c)*a^2*c^2*log(2*a*c*x^2 + 2*sqrt(-a*c)*sqrt(a*x + a)*sqrt(-c*x + c)*x - a*c) + 1/48*(8*a^2*c^2*x^5 - 26*a^2*c^2*x^3 + 33*a^2*c^2*x)*sqrt(a*x + a)*sqrt(-c*x + c), -5/16*sqrt(a*c)*a^2*c^2*arctan(sqrt(a*c)*sqrt(a*x + a)*sqrt(-c*x + c)*x/(a*c*x^2 - a*c)) + 1/48*(8*a^2*c^2*x^5 - 26*a^2*c^2*x^3 + 33*a^2*c^2*x)*sqrt(a*x + a)*sqrt(-c*x + c)]

giac [B] time = 1.57, size = 679, normalized size = 5.39

$$\frac{1}{240} \left(\frac{150 a^2 c \log \left(\left| -\sqrt{-ac} \sqrt{ax+a} + \sqrt{-(ax+a)ac + 2a^2c} \right| \right)}{\sqrt{-ac}} + \sqrt{-(ax+a)ac + 2a^2c} \left(2 \left((ax+a) \left(4(ax+a) \left(\right) \right) \right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+a)^(5/2)*(-c*x+c)^(5/2),x, algorithm="giac")

[Out] 1/240*(150*a^2*c*log(abs(-sqrt(-a*c)*sqrt(a*x + a) + sqrt(-(a*x + a)*a*c + 2*a^2*c)))/sqrt(-a*c) + sqrt(-(a*x + a)*a*c + 2*a^2*c)*((2*((a*x + a)*(4*(a*x + a)*(5*(a*x + a)/a^5 - 31/a^4) + 321/a^3) - 451/a^2)*(a*x + a) + 745/a)*(a*x + a) - 405)*sqrt(a*x + a))*c^2*abs(a) - 1/120*(90*a^2*c*log(abs(-sqrt(-a*c)*sqrt(a*x + a) + sqrt(-(a*x + a)*a*c + 2*a^2*c)))/sqrt(-a*c) - sqrt(-(a*x + a)*a*c + 2*a^2*c)*((2*(a*x + a)*(3*(a*x + a)*(4*(a*x + a)/a^4 - 21/a^3) + 133/a^2) - 295/a)*(a*x + a) + 195)*sqrt(a*x + a))*c^2*abs(a) - 1/12*(18*a^2*c*log(abs(-sqrt(-a*c)*sqrt(a*x + a) + sqrt(-(a*x + a)*a*c + 2*a^2*c)))/sqrt(-a*c) + sqrt(-(a*x + a)*a*c + 2*a^2*c)*((a*x + a)*(2*(a*x + a)*(3*(a*x + a)/a^3 - 13/a^2) + 43/a) - 39)*sqrt(a*x + a))*c^2*abs(a) + 1/3*(6*a^2*c*log(abs(-sqrt(-a*c)*sqrt(a*x + a) + sqrt(-(a*x + a)*a*c + 2*a^2*c)))/sqrt(-a*c) - sqrt(-(a*x + a)*a*c + 2*a^2*c)*sqrt(a*x + a)*((a*x + a)*(2*(a*x + a)/a^2 - 7/a) + 9))*c^2*abs(a) - (2*a^2*c*log(abs(-sqrt(-a*c)*sqrt(a*x + a) + sqrt(-(a*x + a)*a*c + 2*a^2*c)))/sqrt(-a*c) - sqrt(-(a*x + a)*a*c + 2*a^2*c)*sqrt(a*x + a))*c^2*abs(a) + 1/2*(2*a^3*c*log(abs(-sqrt(-a*c)*sqrt(a*x + a) + sqrt(-(a*x + a)*a*c + 2*a^2*c)))/sqrt(-a*c) + sqrt(-(a*x + a)*a*c + 2*a^2*c)*sqrt(a*x + a)*(a*x - 2*a))*c^2*abs(a)/a

maple [B] time = 0.01, size = 193, normalized size = 1.53

$$\frac{5\sqrt{(-cx+c)(ax+a)} a^3 c^3 \arctan\left(\frac{\sqrt{ac} x}{\sqrt{-acx^2+ac}}\right)}{16\sqrt{-cx+c} \sqrt{ax+a} \sqrt{ac}} + \frac{5\sqrt{-cx+c} \sqrt{ax+a} a^2 c^2}{16} + \frac{5(-cx+c)^{\frac{3}{2}} \sqrt{ax+a} a^2 c}{48} + \frac{(-cx+c)}{16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*x+a)^(5/2)*(-c*x+c)^(5/2),x)`

[Out]
$$-1/6/c*(a*x+a)^(5/2)*(-c*x+c)^(7/2)-1/6*a/c*(a*x+a)^(3/2)*(-c*x+c)^(7/2)-1/8*a^2/c*(a*x+a)^(1/2)*(-c*x+c)^(7/2)+1/24*a^2*(-c*x+c)^(5/2)*(a*x+a)^(1/2)+5/48*a^2*c*(-c*x+c)^(3/2)*(a*x+a)^(1/2)+5/16*a^2*c^2*(-c*x+c)^(1/2)*(a*x+a)^(1/2)+5/16*a^3*c^3*((-c*x+c)*(a*x+a))^(1/2)/(-c*x+c)^(1/2)/(a*x+a)^(1/2)/(a*c)^(1/2)*\arctan((a*c)^(1/2)*x/(-a*c*x^2+a*c)^(1/2))$$

maxima [A] time = 3.02, size = 72, normalized size = 0.57

$$\frac{5a^3c^3 \arcsin(x)}{16\sqrt{ac}} + \frac{5}{16}\sqrt{-acx^2 + ac} a^2c^2x + \frac{5}{24}(-acx^2 + ac)^{\frac{3}{2}}acx + \frac{1}{6}(-acx^2 + ac)^{\frac{5}{2}}x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a*x+a)^(5/2)*(-c*x+c)^(5/2),x, algorithm="maxima")`

[Out]
$$5/16*a^3*c^3*\arcsin(x)/\sqrt{a*c} + 5/16*\sqrt{-a*c*x^2 + a*c}*a^2*c^2*x + 5/24*(-a*c*x^2 + a*c)^(3/2)*a*c*x + 1/6*(-a*c*x^2 + a*c)^(5/2)*x$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + ax)^{5/2} (c - cx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + a*x)^(5/2)*(c - c*x)^(5/2),x)`

[Out] `int((a + a*x)^(5/2)*(c - c*x)^(5/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a(x+1))^{\frac{5}{2}} (-c(x-1))^{\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a*x+a)**(5/2)*(-c*x+c)**(5/2),x)`

[Out] `Integral((a*(x + 1))**(5/2)*(-c*(x - 1))**(5/2), x)`

3.1138 $\int (a + ax)^{3/2}(c - cx)^{3/2} dx$

Optimal. Leaf size=96

$$\frac{3}{4}a^{3/2}c^{3/2} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{ax+a}}{\sqrt{a}\sqrt{c-cx}}\right) + \frac{3}{8}acx\sqrt{ax+a}\sqrt{c-cx} + \frac{1}{4}x(ax+a)^{3/2}(c-cx)^{3/2}$$

[Out] $1/4*x*(a*x+a)^{(3/2)}*(-c*x+c)^{(3/2)}+3/4*a^{(3/2)}*c^{(3/2)}*\arctan(c^{(1/2)}*(a*x+a)^{(1/2)}/a^{(1/2)}/(-c*x+c)^{(1/2)})+3/8*a*c*x*(a*x+a)^{(1/2)}*(-c*x+c)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {38, 63, 217, 203}

$$\frac{3}{4}a^{3/2}c^{3/2} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{ax+a}}{\sqrt{a}\sqrt{c-cx}}\right) + \frac{3}{8}acx\sqrt{ax+a}\sqrt{c-cx} + \frac{1}{4}x(ax+a)^{3/2}(c-cx)^{3/2}$$

Antiderivative was successfully verified.

[In] Int[(a + a*x)^(3/2)*(c - c*x)^(3/2), x]

[Out] $(3*a*c*x*\text{Sqrt}[a + a*x]*\text{Sqrt}[c - c*x])/8 + (x*(a + a*x)^{(3/2)}*(c - c*x)^{(3/2)})/4 + (3*a^{(3/2)}*c^{(3/2)}*\text{ArcTan}[(\text{Sqrt}[c]*\text{Sqrt}[a + a*x])/(\text{Sqrt}[a]*\text{Sqrt}[c - c*x])])/4$

Rule 38

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[(x*(a + b*x)^m*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 63

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])

Rule 217

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]`

Rubi steps

$$\begin{aligned}
 \int (a + ax)^{3/2}(c - cx)^{3/2} dx &= \frac{1}{4}x(a + ax)^{3/2}(c - cx)^{3/2} + \frac{1}{4}(3ac) \int \sqrt{a + ax} \sqrt{c - cx} dx \\
 &= \frac{3}{8}acx\sqrt{a + ax} \sqrt{c - cx} + \frac{1}{4}x(a + ax)^{3/2}(c - cx)^{3/2} + \frac{1}{8}(3a^2c^2) \int \frac{1}{\sqrt{a + ax} \sqrt{c - cx}} dx \\
 &= \frac{3}{8}acx\sqrt{a + ax} \sqrt{c - cx} + \frac{1}{4}x(a + ax)^{3/2}(c - cx)^{3/2} + \frac{1}{4}(3ac^2) \text{Subst} \left(\int \frac{1}{\sqrt{2c - \frac{cx^2}{a}}} dx, x, \right. \\
 &= \frac{3}{8}acx\sqrt{a + ax} \sqrt{c - cx} + \frac{1}{4}x(a + ax)^{3/2}(c - cx)^{3/2} + \frac{1}{4}(3ac^2) \text{Subst} \left(\int \frac{1}{1 + \frac{cx^2}{a}} dx, x, \right. \\
 &= \frac{3}{8}acx\sqrt{a + ax} \sqrt{c - cx} + \frac{1}{4}x(a + ax)^{3/2}(c - cx)^{3/2} + \frac{3}{4}a^{3/2}c^{3/2} \tan^{-1} \left(\frac{\sqrt{c} \sqrt{a + ax}}{\sqrt{a} \sqrt{c - cx}} \right)
 \end{aligned}$$

Mathematica [A] time = 0.08, size = 104, normalized size = 1.08

$$\frac{\sqrt{c}(a(x+1))^{3/2}\sqrt{c-cx} \left(\sqrt{c}x\sqrt{x+1}(-2x^3+2x^2+5x-5) + 6\sqrt{c-cx} \sin^{-1} \left(\frac{\sqrt{c-cx}}{\sqrt{2}\sqrt{c}} \right) \right)}{8(x-1)(x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + a*x)^(3/2)*(c - c*x)^(3/2), x]

[Out] (Sqrt[c]*(a*(1 + x))^(3/2)*Sqrt[c - c*x]*(Sqrt[c]*x*Sqrt[1 + x]*(-5 + 5*x + 2*x^2 - 2*x^3) + 6*Sqrt[c - c*x]*ArcSin[Sqrt[c - c*x]/(Sqrt[2]*Sqrt[c])]) / (8*(-1 + x)*(1 + x)^(3/2))

fricas [A] time = 0.47, size = 155, normalized size = 1.61

$$\left[\frac{3}{16} \sqrt{-ac} ac \log(2acx^2 + 2\sqrt{-ac}\sqrt{ax+a}\sqrt{-cx+cx-ac}) - \frac{1}{8}(2acx^3 - 5acx)\sqrt{ax+a}\sqrt{-cx+c}, -\frac{3}{8}\sqrt{ac} ac \arcsin\left(\frac{\sqrt{c-cx}}{\sqrt{2}\sqrt{c}}\right) \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+a)^(3/2)*(-c*x+c)^(3/2), x, algorithm="fricas")

[Out] $[3/16*\sqrt{-a*c}*a*c*\log(2*a*c*x^2 + 2*\sqrt{-a*c}*\sqrt{a*x + a}*\sqrt{-c*x + c})*x - a*c) - 1/8*(2*a*c*x^3 - 5*a*c*x)*\sqrt{a*x + a}*\sqrt{-c*x + c}, -3/8*\sqrt{a*c}*a*c*\arctan(\sqrt{a*c}*\sqrt{a*x + a}*\sqrt{-c*x + c})*x/(a*c*x^2 - a*c)) - 1/8*(2*a*c*x^3 - 5*a*c*x)*\sqrt{a*x + a}*\sqrt{-c*x + c}]$

giac [B] time = 1.25, size = 403, normalized size = 4.20

$$\frac{\left(\frac{18 a^2 c \log\left(\left|-\sqrt{-ac} \sqrt{ax+a} + \sqrt{-(ax+a)ac+2a^2c}\right|\right)}{\sqrt{-ac}} + \sqrt{-(ax+a)ac+2a^2c} \left((ax+a) \left(2(ax+a) \left(\frac{3(ax+a)}{a^3} - \frac{13}{a^2}\right) + \frac{43}{a}\right) - 39\right)\right)}{24 a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a*x+a)^(3/2)*(-c*x+c)^(3/2),x, algorithm="giac")`

[Out] $-1/24*(18*a^2*c*\log(\text{abs}(-\sqrt{-a*c})*\sqrt{a*x + a} + \sqrt{-(a*x + a)*a*c + 2*a^2*c}))/\sqrt{-a*c} + \sqrt{-(a*x + a)*a*c + 2*a^2*c}*((a*x + a)*(2*(a*x + a)*(3*(a*x + a)/a^3 - 13/a^2) + 43/a) - 39)*\sqrt{a*x + a})*c*\text{abs}(a)/a + 1/6*(6*a^2*c*\log(\text{abs}(-\sqrt{-a*c})*\sqrt{a*x + a} + \sqrt{-(a*x + a)*a*c + 2*a^2*c}))/\sqrt{-a*c} - \sqrt{-(a*x + a)*a*c + 2*a^2*c}*\sqrt{a*x + a}*((a*x + a)*(2*(a*x + a)/a^2 - 7/a) + 9))*c*\text{abs}(a)/a - (2*a^2*c*\log(\text{abs}(-\sqrt{-a*c})*\sqrt{a*x + a} + \sqrt{-(a*x + a)*a*c + 2*a^2*c}))/\sqrt{-a*c} - \sqrt{-(a*x + a)*a*c + 2*a^2*c}*\sqrt{a*x + a})*c*\text{abs}(a)/a + 1/2*(2*a^3*c*\log(\text{abs}(-\sqrt{-a*c})*\sqrt{a*x + a} + \sqrt{-(a*x + a)*a*c + 2*a^2*c}))/\sqrt{-a*c} + \sqrt{-(a*x + a)*a*c + 2*a^2*c}*\sqrt{a*x + a}*(a*x - 2*a))*c*\text{abs}(a)/a^2$

maple [B] time = 0.00, size = 143, normalized size = 1.49

$$\frac{3\sqrt{-cx+c} \sqrt{ax+a} a^2 c^2 \arctan\left(\frac{\sqrt{ac} x}{\sqrt{-acx^2+ac}}\right)}{8\sqrt{-cx+c} \sqrt{ax+a} \sqrt{ac}} + \frac{3\sqrt{-cx+c} \sqrt{ax+a} ac}{8} + \frac{\sqrt{ax+a} (-cx+c)^{\frac{3}{2}} a}{8} - \frac{\sqrt{ax+a} (-cx+c)}{4c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*x+a)^(3/2)*(-c*x+c)^(3/2),x)`

[Out] $-1/4/c*(a*x+a)^(3/2)*(-c*x+c)^(5/2) - 1/4*a/c*(a*x+a)^(1/2)*(-c*x+c)^(5/2) + 1/8*(a*x+a)^(1/2)*(-c*x+c)^(3/2)*a + 3/8*a*c*(-c*x+c)^(1/2)*(a*x+a)^(1/2) + 3/8*a^2*c^2*((-c*x+c)*(a*x+a)^(1/2)/(-c*x+c)^(1/2)/(a*x+a)^(1/2)/(a*c)^(1/2)*\arctan((a*c)^(1/2)/(-a*c*x^2+a*c)^(1/2)*x)$

maxima [A] time = 3.09, size = 50, normalized size = 0.52

$$\frac{3 a^2 c^2 \arcsin(x)}{8 \sqrt{ac}} + \frac{3}{8} \sqrt{-acx^2 + ac} acx + \frac{1}{4} (-acx^2 + ac)^{\frac{3}{2}} x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+a)^(3/2)*(-c*x+c)^(3/2),x, algorithm="maxima")

[Out] $\frac{3}{8}a^2c^2\arcsin(x)/\sqrt{ac} + \frac{3}{8}\sqrt{-acx^2 + ac}acx + \frac{1}{4}(-acx^2 + ac)^{3/2}x$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + ax)^{3/2} (c - cx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + a*x)^(3/2)*(c - c*x)^(3/2),x)

[Out] int((a + a*x)^(3/2)*(c - c*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a(x+1))^{3/2} (-c(x-1))^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+a)**(3/2)*(-c*x+c)**(3/2),x)

[Out] Integral((a*(x + 1))**(3/2)*(-c*(x - 1))**(3/2), x)

3.1139 $\int \sqrt{a+ax} \sqrt{c-cx} dx$

Optimal. Leaf size=67

$$\frac{1}{2}x\sqrt{ax+a}\sqrt{c-cx} + \sqrt{a}\sqrt{c} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{ax+a}}{\sqrt{a}\sqrt{c-cx}}\right)$$

[Out] arctan(c^(1/2)*(a*x+a)^(1/2)/a^(1/2)/(-c*x+c)^(1/2))*a^(1/2)*c^(1/2)+1/2*x*(a*x+a)^(1/2)*(-c*x+c)^(1/2)

Rubi [A] time = 0.03, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {38, 63, 217, 203}

$$\frac{1}{2}x\sqrt{ax+a}\sqrt{c-cx} + \sqrt{a}\sqrt{c} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{ax+a}}{\sqrt{a}\sqrt{c-cx}}\right)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + a*x]*Sqrt[c - c*x], x]

[Out] (x*Sqrt[a + a*x]*Sqrt[c - c*x])/2 + Sqrt[a]*Sqrt[c]*ArcTan[(Sqrt[c]*Sqrt[a + a*x])/(Sqrt[a]*Sqrt[c - c*x])]

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(x*(a + b*x)^m*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])

Rule 217

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]`

Rubi steps

$$\begin{aligned}
 \int \sqrt{a+ax} \sqrt{c-cx} \, dx &= \frac{1}{2}x\sqrt{a+ax} \sqrt{c-cx} + \frac{1}{2}(ac) \int \frac{1}{\sqrt{a+ax} \sqrt{c-cx}} \, dx \\
 &= \frac{1}{2}x\sqrt{a+ax} \sqrt{c-cx} + c \operatorname{Subst} \left(\int \frac{1}{\sqrt{2c - \frac{cx^2}{a}}} \, dx, x, \sqrt{a+ax} \right) \\
 &= \frac{1}{2}x\sqrt{a+ax} \sqrt{c-cx} + c \operatorname{Subst} \left(\int \frac{1}{1 + \frac{cx^2}{a}} \, dx, x, \frac{\sqrt{a+ax}}{\sqrt{c-cx}} \right) \\
 &= \frac{1}{2}x\sqrt{a+ax} \sqrt{c-cx} + \sqrt{a} \sqrt{c} \tan^{-1} \left(\frac{\sqrt{c} \sqrt{a+ax}}{\sqrt{a} \sqrt{c-cx}} \right)
 \end{aligned}$$

Mathematica [A] time = 0.06, size = 69, normalized size = 1.03

$$\frac{\sqrt{a(x+1)} \left(x\sqrt{x+1} \sqrt{c-cx} - 2\sqrt{c} \sin^{-1} \left(\frac{\sqrt{c-cx}}{\sqrt{2}\sqrt{c}} \right) \right)}{2\sqrt{x+1}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + a*x]*Sqrt[c - c*x],x]

[Out] (Sqrt[a*(1 + x)]*(x*Sqrt[1 + x]*Sqrt[c - c*x] - 2*Sqrt[c]*ArcSin[Sqrt[c - c*x]/(Sqrt[2]*Sqrt[c])]))/(2*Sqrt[1 + x])

fricas [A] time = 0.47, size = 127, normalized size = 1.90

$$\left[\frac{1}{2} \sqrt{ax+a} \sqrt{-cx+cx} + \frac{1}{4} \sqrt{-ac} \log(2acx^2 + 2\sqrt{-ac} \sqrt{ax+a} \sqrt{-cx+cx} - ac), \frac{1}{2} \sqrt{ax+a} \sqrt{-cx+cx} - \frac{1}{2} \sqrt{a} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+a)^(1/2)*(-c*x+c)^(1/2),x, algorithm="fricas")

[Out] [1/2*sqrt(a*x + a)*sqrt(-c*x + c)*x + 1/4*sqrt(-a*c)*log(2*a*c*x^2 + 2*sqrt(-a*c)*sqrt(a*x + a)*sqrt(-c*x + c)*x - a*c), 1/2*sqrt(a*x + a)*sqrt(-c*x +

$c) * x - 1/2 * \sqrt{a * c} * \arctan(\sqrt{a * c} * \sqrt{a * x + a} * \sqrt{-c * x + c} * x / (a * c * x^2 - a * c))]$

giac [B] time = 0.90, size = 173, normalized size = 2.58

$$\frac{\left(\frac{2 a^2 c \log\left(\left| -\sqrt{-ac} \sqrt{ax+a} + \sqrt{-(ax+a)ac+2a^2c} \right|\right)}{\sqrt{-ac}} - \sqrt{-(ax+a)ac+2a^2c} \sqrt{ax+a} \right) |a|}{a^2} + \frac{\left(\frac{2 a^3 c \log\left(\left| -\sqrt{-ac} \sqrt{ax+a} + \sqrt{-(ax+a)ac+2a^2c} \right|\right)}{\sqrt{-ac}} \right)}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+a)^(1/2)*(-c*x+c)^(1/2),x, algorithm="giac")

[Out] $-(2 * a^2 * c * \log(\text{abs}(-\sqrt{-a * c}) * \sqrt{a * x + a} + \sqrt{-(a * x + a) * a * c + 2 * a^2 * c})) / \sqrt{-a * c} - \sqrt{-(a * x + a) * a * c + 2 * a^2 * c} * \sqrt{a * x + a} * \text{abs}(a) / a^2 + 1/2 * (2 * a^3 * c * \log(\text{abs}(-\sqrt{-a * c}) * \sqrt{a * x + a} + \sqrt{-(a * x + a) * a * c + 2 * a^2 * c})) / \sqrt{-a * c} + \sqrt{-(a * x + a) * a * c + 2 * a^2 * c} * \sqrt{a * x + a} * (a * x - 2 * a) * \text{abs}(a) / a^3$

maple [A] time = 0.01, size = 98, normalized size = 1.46

$$\frac{\sqrt{-cx+c} (ax+a) ac \arctan\left(\frac{\sqrt{ac} x}{\sqrt{-acx^2+ac}}\right)}{2\sqrt{-cx+c} \sqrt{ax+a} \sqrt{ac}} - \frac{\sqrt{ax+a} (-cx+c)^{\frac{3}{2}}}{2c} + \frac{\sqrt{ax+a} \sqrt{-cx+c}}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*x+a)^(1/2)*(-c*x+c)^(1/2),x)

[Out] $-1/2/c * (a * x + a)^{1/2} * (-c * x + c)^{3/2} + 1/2 * (a * x + a)^{1/2} * (-c * x + c)^{1/2} + 1/2 * a * c * ((-c * x + c) * (a * x + a))^{1/2} / (-c * x + c)^{1/2} / (a * x + a)^{1/2} / (a * c)^{1/2} * \arctan((a * c)^{1/2} / (-a * c * x^2 + a * c)^{1/2} * x)$

maxima [A] time = 3.08, size = 28, normalized size = 0.42

$$\frac{ac \arcsin(x)}{2 \sqrt{ac}} + \frac{1}{2} \sqrt{-acx^2 + ac} x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+a)^(1/2)*(-c*x+c)^(1/2),x, algorithm="maxima")

[Out] $1/2 * a * c * \arcsin(x) / \sqrt{a * c} + 1/2 * \sqrt{-a * c * x^2 + a * c} * x$

mupad [B] time = 0.30, size = 59, normalized size = 0.88

$$\frac{x \sqrt{a + ax} \sqrt{c - cx}}{2} - \frac{\sqrt{a} \sqrt{-c} \ln\left(\sqrt{-c} \sqrt{a} (x + 1) \sqrt{-c} (x - 1) - \sqrt{a} c x\right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + a*x)^(1/2)*(c - c*x)^(1/2),x)`

[Out] $(x*(a + a*x)^{(1/2)}*(c - c*x)^{(1/2)})/2 - (a^{(1/2)}*(-c)^{(1/2)}*\log((-c)^{(1/2)}*(a*(x + 1))^{(1/2)}*(-c*(x - 1))^{(1/2)} - a^{(1/2)*c*x})/2$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{a(x+1)} \sqrt{-c(x-1)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a*x+a)**(1/2)*(-c*x+c)**(1/2),x)`

[Out] `Integral(sqrt(a*(x + 1))*sqrt(-c*(x - 1)), x)`

$$3.1140 \quad \int \frac{1}{\sqrt{a+ax} \sqrt{c-cx}} dx$$

Optimal. Leaf size=43

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{c} \sqrt{ax+a}}{\sqrt{a} \sqrt{c-cx}} \right)}{\sqrt{a} \sqrt{c}}$$

[Out] $2 \arctan(c^{(1/2)}(a*x+a)^{(1/2)}/a^{(1/2)}/(-c*x+c)^{(1/2)})/a^{(1/2)}/c^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {63, 217, 203}

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{c} \sqrt{ax+a}}{\sqrt{a} \sqrt{c-cx}} \right)}{\sqrt{a} \sqrt{c}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + a*x]*Sqrt[c - c*x]),x]

[Out] (2*ArcTan[(Sqrt[c]*Sqrt[a + a*x])/(Sqrt[a]*Sqrt[c - c*x])])/(Sqrt[a]*Sqrt[c])

Rule 63

Int[((a_.) + (b_.)*(x_)^(m_))*((c_.) + (d_.)*(x_)^(n_)), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(1*ArcTan[Rt[b, 2]*x]/Rt[a, 2])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\int \frac{1}{\sqrt{a+ax}\sqrt{c-cx}} dx = \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2c-\frac{cx^2}{a}}} dx, x, \sqrt{a+ax}\right)}{a}$$

$$= \frac{2 \operatorname{Subst}\left(\int \frac{1}{1+\frac{cx^2}{a}} dx, x, \frac{\sqrt{a+ax}}{\sqrt{c-cx}}\right)}{a}$$

$$= \frac{2 \tan^{-1}\left(\frac{\sqrt{c}\sqrt{a+ax}}{\sqrt{a}\sqrt{c-cx}}\right)}{\sqrt{a}\sqrt{c}}$$

Mathematica [A] time = 0.02, size = 47, normalized size = 1.09

$$\frac{2\sqrt{x+1} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{x+1}}{\sqrt{c-cx}}\right)}{\sqrt{c}\sqrt{a(x+1)}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + a*x]*Sqrt[c - c*x]),x]

[Out] (2*Sqrt[1 + x]*ArcTan[(Sqrt[c]*Sqrt[1 + x])/Sqrt[c - c*x]])/(Sqrt[c]*Sqrt[a*(1 + x)])

fricas [A] time = 0.45, size = 101, normalized size = 2.35

$$\left[-\frac{\sqrt{-ac} \log\left(2acx^2 - 2\sqrt{-ac}\sqrt{ax+a}\sqrt{-cx+cx} - ac\right)}{2ac}, -\frac{\sqrt{ac} \arctan\left(\frac{\sqrt{ac}\sqrt{ax+a}\sqrt{-cx+cx}}{acx^2-ac}\right)}{ac} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(1/2)/(-c*x+c)^(1/2),x, algorithm="fricas")

[Out] [-1/2*sqrt(-a*c)*log(2*a*c*x^2 - 2*sqrt(-a*c)*sqrt(a*x + a)*sqrt(-c*x + c)*x - a*c)/(a*c), -sqrt(a*c)*arctan(sqrt(a*c)*sqrt(a*x + a)*sqrt(-c*x + c)*x/(a*c*x^2 - a*c))/(a*c)]

giac [A] time = 0.76, size = 49, normalized size = 1.14

$$\frac{2a \log\left(\left|-\sqrt{-ac}\sqrt{ax+a} + \sqrt{-(ax+a)ac + 2a^2c}\right|\right)}{\sqrt{-ac}|a|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(1/2)/(-c*x+c)^(1/2),x, algorithm="giac")

[Out] $-2*a*\log(\text{abs}(-\sqrt{-a*c})*\sqrt{a*x+a} + \sqrt{-(a*x+a)*a*c + 2*a^2*c}))/(\sqrt{-a*c}*\text{abs}(a))$

maple [A] time = 0.00, size = 57, normalized size = 1.33

$$\frac{\sqrt{-cx+c}(ax+a) \arctan\left(\frac{\sqrt{ac}x}{\sqrt{-acx^2+ac}}\right)}{\sqrt{ax+a} \sqrt{-cx+c} \sqrt{ac}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a*x+a)^(1/2)/(-c*x+c)^(1/2),x)

[Out] $((-c*x+c)*(a*x+a))^(1/2)/(a*x+a)^(1/2)/(-c*x+c)^(1/2)/(a*c)^(1/2)*\arctan((a*c)^(1/2)/(-a*c*x^2+a*c)^(1/2)*x)$

maxima [A] time = 2.99, size = 8, normalized size = 0.19

$$\frac{\arcsin(x)}{\sqrt{ac}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(1/2)/(-c*x+c)^(1/2),x, algorithm="maxima")

[Out] arcsin(x)/sqrt(a*c)

mupad [B] time = 0.18, size = 44, normalized size = 1.02

$$-\frac{4 \operatorname{atan}\left(\frac{a(\sqrt{c-cx}-\sqrt{c})}{\sqrt{ac}(\sqrt{a+ax}-\sqrt{a})}\right)}{\sqrt{ac}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a+a*x)^(1/2)*(c-c*x)^(1/2)),x)

[Out] $-(4*\operatorname{atan}((a*((c-c*x)^(1/2)-c^(1/2)))/((a*c)^(1/2)*((a+a*x)^(1/2)-a^(1/2)))))/(a*c)^(1/2)$

sympy [C] time = 3.95, size = 85, normalized size = 1.98

$$\frac{iG_{6,6}^{6,2} \left(\begin{matrix} \frac{1}{4}, \frac{3}{4} & \frac{1}{2}, \frac{1}{2}, 1, 1 \\ 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1, 0 \end{matrix} \middle| \frac{1}{x^2} \right)}{4\pi^{\frac{3}{2}} \sqrt{a} \sqrt{c}} + \frac{G_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, -\frac{1}{4}, 0, \frac{1}{4}, \frac{1}{2}, 1 \\ -\frac{1}{4}, \frac{1}{4} & -\frac{1}{2}, 0, 0, 0 \end{matrix} \middle| \frac{e^{-2i\pi}}{x^2} \right)}{4\pi^{\frac{3}{2}} \sqrt{a} \sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)**(1/2)/(-c*x+c)**(1/2),x)

[Out] -I*meijerg(((1/4, 3/4), (1/2, 1/2, 1, 1)), ((0, 1/4, 1/2, 3/4, 1, 0), ()), x**(-2))/(4*pi**(3/2)*sqrt(a)*sqrt(c)) + meijerg(((1/2, -1/4, 0, 1/4, 1/2, 1), ()), ((-1/4, 1/4), (-1/2, 0, 0, 0)), exp_polar(-2*I*pi)/x**2)/(4*pi**(3/2)*sqrt(a)*sqrt(c))

$$3.1141 \quad \int \frac{1}{(a+ax)^{3/2}(c-cx)^{3/2}} dx$$

Optimal. Leaf size=27

$$\frac{x}{ac\sqrt{ax+a}\sqrt{c-cx}}$$

[Out] x/a/c/(a*x+a)^(1/2)/(-c*x+c)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.050$, Rules used = {39}

$$\frac{x}{ac\sqrt{ax+a}\sqrt{c-cx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + a*x)^(3/2)*(c - c*x)^(3/2)), x]

[Out] x/(a*c*Sqrt[a + a*x]*Sqrt[c - c*x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := S imp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && Eq Q[b*c + a*d, 0]

Rubi steps

$$\int \frac{1}{(a+ax)^{3/2}(c-cx)^{3/2}} dx = \frac{x}{ac\sqrt{a+ax}\sqrt{c-cx}}$$

Mathematica [A] time = 0.02, size = 27, normalized size = 1.00

$$\frac{x(x+1)}{c(a(x+1))^{3/2}\sqrt{c-cx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + a*x)^(3/2)*(c - c*x)^(3/2)), x]

[Out] (x*(1 + x))/(c*(a*(1 + x))^(3/2)*Sqrt[c - c*x])

fricas [A] time = 0.42, size = 39, normalized size = 1.44

$$-\frac{\sqrt{ax+a}\sqrt{-cx+c}x}{a^2c^2x^2 - a^2c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(3/2)/(-c*x+c)^(3/2),x, algorithm="fricas")

[Out] -sqrt(a*x + a)*sqrt(-c*x + c)*x/(a^2*c^2*x^2 - a^2*c^2)

giac [B] time = 0.70, size = 116, normalized size = 4.30

$$-\frac{2\sqrt{-ac}a}{\left(2a^2c - \left(\sqrt{-ac}\sqrt{ax+a} - \sqrt{-(ax+a)ac + 2a^2c}\right)^2\right)c|a|} - \frac{\sqrt{-(ax+a)ac + 2a^2c}\sqrt{ax+a}}{2\left((ax+a)ac - 2a^2c\right)c|a|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(3/2)/(-c*x+c)^(3/2),x, algorithm="giac")

[Out] -2*sqrt(-a*c)*a/((2*a^2*c - (sqrt(-a*c)*sqrt(a*x + a) - sqrt(-(a*x + a)*a*c + 2*a^2*c))^2)*c*abs(a)) - 1/2*sqrt(-(a*x + a)*a*c + 2*a^2*c)*sqrt(a*x + a)/(((a*x + a)*a*c - 2*a^2*c)*c*abs(a))

maple [A] time = 0.00, size = 25, normalized size = 0.93

$$-\frac{(x+1)(x-1)x}{(ax+a)^2(-cx+c)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a*x+a)^(3/2)/(-c*x+c)^(3/2),x)

[Out] -(x+1)*(x-1)*x/(a*x+a)^(3/2)/(-c*x+c)^(3/2)

maxima [A] time = 1.31, size = 21, normalized size = 0.78

$$\frac{x}{\sqrt{-acx^2 + ac}ac}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(3/2)/(-c*x+c)^(3/2),x, algorithm="maxima")

[Out] x/(sqrt(-a*c*x^2 + a*c)*a*c)

mupad [B] time = 0.39, size = 23, normalized size = 0.85

$$\frac{x}{ac\sqrt{a+ax}\sqrt{c-cx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + a*x)^(3/2)*(c - c*x)^(3/2)),x)

[Out] x/(a*c*(a + a*x)^(1/2)*(c - c*x)^(1/2))

sympy [C] time = 4.44, size = 82, normalized size = 3.04

$$-\frac{iG_{6,6}^{5,3}\left(\begin{matrix} \frac{3}{4}, \frac{5}{4}, 1 & \frac{1}{2}, \frac{3}{2}, 2 \\ \frac{3}{4}, 1, \frac{5}{4}, \frac{3}{2}, 2 & 0 \end{matrix} \middle| \frac{1}{x^2}\right)}{2\pi^{\frac{3}{2}}a^{\frac{3}{2}}c^{\frac{3}{2}}} + \frac{G_{6,6}^{2,6}\left(\begin{matrix} -\frac{1}{2}, 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1 \\ \frac{1}{4}, \frac{3}{4} & -\frac{1}{2}, 0, 1, 0 \end{matrix} \middle| \frac{e^{-2i\pi}}{x^2}\right)}{2\pi^{\frac{3}{2}}a^{\frac{3}{2}}c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)**(3/2)/(-c*x+c)**(3/2),x)

[Out] -I*meijerg(((3/4, 5/4, 1), (1/2, 3/2, 2)), ((3/4, 1, 5/4, 3/2, 2), (0,)), x**(-2))/(2*pi**(3/2)*a**(3/2)*c**(3/2)) + meijerg((-1/2, 0, 1/4, 1/2, 3/4, 1), ()), ((1/4, 3/4), (-1/2, 0, 1, 0)), exp_polar(-2*I*pi)/x**2)/(2*pi**(3/2)*a**(3/2)*c**(3/2))

$$3.1142 \quad \int \frac{1}{(a+ax)^{5/2}(c-cx)^{5/2}} dx$$

Optimal. Leaf size=61

$$\frac{2x}{3a^2c^2\sqrt{ax+a}\sqrt{c-cx}} + \frac{x}{3ac(ax+a)^{3/2}(c-cx)^{3/2}}$$

[Out] $1/3*x/a/c/(a*x+a)^{(3/2)}/(-c*x+c)^{(3/2)}+2/3*x/a^2/c^2/(a*x+a)^{(1/2)}/(-c*x+c)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 61, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {40, 39}

$$\frac{2x}{3a^2c^2\sqrt{ax+a}\sqrt{c-cx}} + \frac{x}{3ac(ax+a)^{3/2}(c-cx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + a*x)^(5/2)*(c - c*x)^(5/2)),x]

[Out] $x/(3*a*c*(a + a*x)^{(3/2)*(c - c*x)^{(3/2)}) + (2*x)/(3*a^2*c^2*sqrt[a + a*x]*sqrt[c - c*x])$

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] :> Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> -Simp[(x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+ax)^{5/2}(c-cx)^{5/2}} dx &= \frac{x}{3ac(a+ax)^{3/2}(c-cx)^{3/2}} + \frac{2 \int \frac{1}{(a+ax)^{3/2}(c-cx)^{3/2}} dx}{3ac} \\ &= \frac{x}{3ac(a+ax)^{3/2}(c-cx)^{3/2}} + \frac{2x}{3a^2c^2\sqrt{a+ax}\sqrt{c-cx}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 42, normalized size = 0.69

$$\frac{x(x+1)(2x^2-3)}{3c^2(x-1)(a(x+1))^{5/2}\sqrt{c-cx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + a*x)^(5/2)*(c - c*x)^(5/2)),x]

[Out] (x*(1 + x)*(-3 + 2*x^2))/(3*c^2*(-1 + x)*(a*(1 + x))^(5/2)*Sqrt[c - c*x])

fricas [A] time = 0.45, size = 57, normalized size = 0.93

$$-\frac{(2x^3 - 3x)\sqrt{ax + a}\sqrt{-cx + c}}{3(a^3c^3x^4 - 2a^3c^3x^2 + a^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(5/2)/(-c*x+c)^(5/2),x, algorithm="fricas")

[Out] -1/3*(2*x^3 - 3*x)*sqrt(a*x + a)*sqrt(-c*x + c)/(a^3*c^3*x^4 - 2*a^3*c^3*x^2 + a^3*c^3)

giac [B] time = 0.81, size = 237, normalized size = 3.89

$$\frac{\sqrt{-(ax+a)ac+2a^2c}\sqrt{ax+a}\left(\frac{4(ax+a)|a|}{a^2c}-\frac{9|a|}{ac}\right)}{12((ax+a)ac-2a^2c)^2} - \frac{16\sqrt{-ac}a^4c^2-18\sqrt{-ac}(\sqrt{-ac}\sqrt{ax+a}-\sqrt{-(ax+a)ac+2a^2c})}{3(2a^2c-(\sqrt{-ac}\sqrt{ax+a}-\sqrt{-(ax+a)ac+2a^2c}))^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(5/2)/(-c*x+c)^(5/2),x, algorithm="giac")

[Out] -1/12*sqrt(-(a*x + a)*a*c + 2*a^2*c)*sqrt(a*x + a)*(4*(a*x + a)*abs(a)/(a^2*c) - 9*abs(a)/(a*c))/((a*x + a)*a*c - 2*a^2*c)^2 - 1/3*(16*sqrt(-a*c)*a^4*c^2 - 18*sqrt(-a*c)*(sqrt(-a*c)*sqrt(a*x + a) - sqrt(-(a*x + a)*a*c + 2*a^2*c))^2*a^2*c + 3*sqrt(-a*c)*(sqrt(-a*c)*sqrt(a*x + a) - sqrt(-(a*x + a)*a*c + 2*a^2*c))^4)/((2*a^2*c - (sqrt(-a*c)*sqrt(a*x + a) - sqrt(-(a*x + a)*a*c + 2*a^2*c))^2)^3*c^2*abs(a))

maple [A] time = 0.00, size = 32, normalized size = 0.52

$$\frac{(x+1)(x-1)(2x^2-3)x}{3(ax+a)^{\frac{5}{2}}(-cx+c)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(a*x+a)^(5/2)/(-c*x+c)^(5/2),x)`

[Out] $1/3*(x+1)*(x-1)*x*(2*x^2-3)/(a*x+a)^(5/2)/(-c*x+c)^(5/2)$

maxima [A] time = 1.35, size = 45, normalized size = 0.74

$$\frac{x}{3(-acx^2 + ac)^{\frac{3}{2}}ac} + \frac{2x}{3\sqrt{-acx^2 + ac}a^2c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a*x+a)^(5/2)/(-c*x+c)^(5/2),x, algorithm="maxima")`

[Out] $1/3*x/((-a*c*x^2 + a*c)^(3/2)*a*c) + 2/3*x/(sqrt(-a*c*x^2 + a*c)*a^2*c^2)$

mupad [B] time = 0.41, size = 62, normalized size = 1.02

$$-\frac{3x\sqrt{c-cx} - 2x^3\sqrt{c-cx}}{\sqrt{a+ax}(c-cx)^2(3a^2(c-cx) - 6a^2c)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + a*x)^(5/2)*(c - c*x)^(5/2)),x)`

[Out] $-(3*x*(c - c*x)^(1/2) - 2*x^3*(c - c*x)^(1/2))/((a + a*x)^(1/2)*(c - c*x)^2*(3*a^2*(c - c*x) - 6*a^2*c))$

sympy [C] time = 13.69, size = 82, normalized size = 1.34

$$\frac{iG_{6,6}^{5,3}\left(\begin{matrix} \frac{5}{4}, \frac{7}{4}, 1 \\ \frac{1}{2}, \frac{5}{2}, 3 \end{matrix} \middle| \frac{1}{x^2}\right)}{3\pi^{\frac{3}{2}}a^{\frac{5}{2}}c^{\frac{5}{2}}} + \frac{G_{6,6}^{2,6}\left(\begin{matrix} -\frac{1}{2}, 0, \frac{1}{2}, \frac{3}{4}, \frac{5}{4}, 1 \\ \frac{3}{4}, \frac{5}{4} \end{matrix} \middle| \frac{e^{-2i\pi}}{x^2}\right)}{3\pi^{\frac{3}{2}}a^{\frac{5}{2}}c^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a*x+a)**(5/2)/(-c*x+c)**(5/2),x)`

[Out] $I*meijerg(((5/4, 7/4, 1), (1/2, 5/2, 3)), ((5/4, 7/4, 2, 5/2, 3), (0,)), x*(-2))/(3*pi**(3/2)*a**(5/2)*c**(5/2)) + meijerg(((-1/2, 0, 1/2, 3/4, 5/4, 1), ()), ((3/4, 5/4), (-1/2, 0, 2, 0)), exp_polar(-2*I*pi)/x**2)/(3*pi**(3/2)*a**(5/2)*c**(5/2))$

$$3.1143 \quad \int \frac{1}{(a+ax)^{7/2}(c-cx)^{7/2}} dx$$

Optimal. Leaf size=91

$$\frac{8x}{15a^3c^3\sqrt{ax+a}\sqrt{c-cx}} + \frac{4x}{15a^2c^2(ax+a)^{3/2}(c-cx)^{3/2}} + \frac{x}{5ac(ax+a)^{5/2}(c-cx)^{5/2}}$$

[Out] $1/5*x/a/c/(a*x+a)^{(5/2)/(-c*x+c)^{(5/2)}+4/15*x/a^2/c^2/(a*x+a)^{(3/2)/(-c*x+c)^{(3/2)}+8/15*x/a^3/c^3/(a*x+a)^{(1/2)/(-c*x+c)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 91, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {40, 39}

$$\frac{8x}{15a^3c^3\sqrt{ax+a}\sqrt{c-cx}} + \frac{4x}{15a^2c^2(ax+a)^{3/2}(c-cx)^{3/2}} + \frac{x}{5ac(ax+a)^{5/2}(c-cx)^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + a*x)^(7/2)*(c - c*x)^(7/2)), x]

[Out] $x/(5*a*c*(a + a*x)^{(5/2)*(c - c*x)^{(5/2)} + (4*x)/(15*a^2*c^2*(a + a*x)^{(3/2)*(c - c*x)^{(3/2)} + (8*x)/(15*a^3*c^3*\text{Sqrt}[a + a*x]*\text{Sqrt}[c - c*x])$

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := -Simp[(x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+ax)^{7/2}(c-cx)^{7/2}} dx &= \frac{x}{5ac(a+ax)^{5/2}(c-cx)^{5/2}} + \frac{4 \int \frac{1}{(a+ax)^{5/2}(c-cx)^{5/2}} dx}{5ac} \\
&= \frac{x}{5ac(a+ax)^{5/2}(c-cx)^{5/2}} + \frac{4x}{15a^2c^2(a+ax)^{3/2}(c-cx)^{3/2}} + \frac{8 \int \frac{1}{(a+ax)^{3/2}(c-cx)^{3/2}} dx}{15a^2c^2} \\
&= \frac{x}{5ac(a+ax)^{5/2}(c-cx)^{5/2}} + \frac{4x}{15a^2c^2(a+ax)^{3/2}(c-cx)^{3/2}} + \frac{8x}{15a^3c^3\sqrt{a+ax}\sqrt{c-cx}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 49, normalized size = 0.54

$$\frac{x(8x^4 - 20x^2 + 15)}{15a^3c^3(x^2 - 1)^2\sqrt{a(x+1)}\sqrt{c-cx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + a*x)^(7/2)*(c - c*x)^(7/2)), x]

[Out] (x*(15 - 20*x^2 + 8*x^4))/(15*a^3*c^3*Sqrt[a*(1 + x)]*Sqrt[c - c*x]*(-1 + x^2)^2)

fricas [A] time = 0.44, size = 74, normalized size = 0.81

$$\frac{(8x^5 - 20x^3 + 15x)\sqrt{ax+a}\sqrt{-cx+c}}{15(a^4c^4x^6 - 3a^4c^4x^4 + 3a^4c^4x^2 - a^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(7/2)/(-c*x+c)^(7/2), x, algorithm="fricas")

[Out] -1/15*(8*x^5 - 20*x^3 + 15*x)*sqrt(a*x + a)*sqrt(-c*x + c)/(a^4*c^4*x^6 - 3*a^4*c^4*x^4 + 3*a^4*c^4*x^2 - a^4*c^4)

giac [B] time = 1.06, size = 333, normalized size = 3.66

$$\frac{\sqrt{-(ax+a)ac+2a^2c}\sqrt{ax+a}\left((ax+a)\left(\frac{64(ax+a)}{c|a|}-\frac{275a}{c|a|}\right)+\frac{300a^2}{c|a|}\right)}{240((ax+a)ac-2a^2c)^3} + \frac{1024a^8c^4-2200(\sqrt{-ac}\sqrt{ax+a}-\sqrt{-(ax+a)c})}{15a^3c^3\sqrt{a+ax}\sqrt{c-cx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(7/2)/(-c*x+c)^(7/2),x, algorithm="giac")

[Out]
$$-1/240*\sqrt{-(a*x + a)*a*c + 2*a^2*c}*\sqrt{a*x + a}*((a*x + a)*(64*(a*x + a)/(c*\text{abs}(a)) - 275*a/(c*\text{abs}(a))) + 300*a^2/(c*\text{abs}(a)))/((a*x + a)*a*c - 2*a^2*c)^3 + 1/60*(1024*a^8*c^4 - 2200*(\sqrt{-a*c}*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c}))^2*a^6*c^3 + 1660*(\sqrt{-a*c}*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c})^4*a^4*c^2 - 450*(\sqrt{-a*c}*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c})^6*a^2*c + 45*(\sqrt{-a*c}*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c})^8)/((2*a^2*c - (\sqrt{-a*c}*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c}))^2)^5*\sqrt{-a*c}*c^2*\text{abs}(a)$$

maple [A] time = 0.00, size = 37, normalized size = 0.41

$$\frac{(x+1)(x-1)(8x^4-20x^2+15)x}{15(ax+a)^{\frac{7}{2}}(-cx+c)^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a*x+a)^(7/2)/(-c*x+c)^(7/2),x)

[Out]
$$-1/15*(x+1)*(x-1)*x*(8*x^4-20*x^2+15)/(a*x+a)^{7/2}/(-c*x+c)^{7/2}$$

maxima [A] time = 1.36, size = 67, normalized size = 0.74

$$\frac{x}{5(-acx^2+ac)^{\frac{5}{2}}ac} + \frac{4x}{15(-acx^2+ac)^{\frac{3}{2}}a^2c^2} + \frac{8x}{15\sqrt{-acx^2+ac}a^3c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(7/2)/(-c*x+c)^(7/2),x, algorithm="maxima")

[Out]
$$1/5*x/((-a*c*x^2 + a*c)^{5/2}*a*c) + 4/15*x/((-a*c*x^2 + a*c)^{3/2}*a^2*c^2) + 8/15*x/(\sqrt{-a*c*x^2 + a*c}*a^3*c^3)$$

mupad [B] time = 0.44, size = 50, normalized size = 0.55

$$\frac{x(8x^4-20x^2+15)}{15a^3\sqrt{a+ax}(c-cx)^{5/2}(c+3cx-x(c-cx))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + a*x)^(7/2)*(c - c*x)^(7/2)),x)

[Out]
$$(x*(8*x^4 - 20*x^2 + 15))/(15*a^3*(a + a*x)^{1/2}*(c - c*x)^{5/2}*(c + 3*c*x - x*(c - c*x)))$$

sympy [C] time = 55.15, size = 85, normalized size = 0.93

$$\frac{2iG_{6,6}^{5,3} \left(\begin{matrix} \frac{7}{4}, \frac{9}{4}, 1 & \frac{1}{2}, \frac{7}{2}, 4 \\ \frac{7}{4}, \frac{9}{4}, 3, \frac{7}{2}, 4 & 0 \end{matrix} \middle| \frac{1}{x^2} \right)}{15\pi^{\frac{3}{2}} a^{\frac{7}{2}} c^{\frac{7}{2}}} + \frac{2G_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, 0, \frac{1}{2}, \frac{5}{4}, \frac{7}{4}, 1 \\ \frac{5}{4}, \frac{7}{4} & -\frac{1}{2}, 0, 3, 0 \end{matrix} \middle| \frac{e^{-2i\pi}}{x^2} \right)}{15\pi^{\frac{3}{2}} a^{\frac{7}{2}} c^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)**(7/2)/(-c*x+c)**(7/2),x)

[Out] -2*I*meijerg(((7/4, 9/4, 1), (1/2, 7/2, 4)), ((7/4, 9/4, 3, 7/2, 4), (0,)), x**(-2))/(15*pi**(3/2)*a**(7/2)*c**(7/2)) + 2*meijerg(((-1/2, 0, 1/2, 5/4, 7/4, 1), ()), ((5/4, 7/4), (-1/2, 0, 3, 0)), exp_polar(-2*I*pi)/x**2)/(15*pi**(3/2)*a**(7/2)*c**(7/2))

$$3.1144 \quad \int \frac{1}{(a+ax)^{9/2}(c-cx)^{9/2}} dx$$

Optimal. Leaf size=121

$$\frac{16x}{35a^4c^4\sqrt{ax+a}\sqrt{c-cx}} + \frac{8x}{35a^3c^3(ax+a)^{3/2}(c-cx)^{3/2}} + \frac{6x}{35a^2c^2(ax+a)^{5/2}(c-cx)^{5/2}} + \frac{x}{7ac(ax+a)^{7/2}(c-cx)^{7/2}}$$

[Out] $1/7*x/a/c/(a*x+a)^{(7/2)/(-c*x+c)^{(7/2)}+6/35*x/a^2/c^2/(a*x+a)^{(5/2)/(-c*x+c)^{(5/2)}+8/35*x/a^3/c^3/(a*x+a)^{(3/2)/(-c*x+c)^{(3/2)}+16/35*x/a^4/c^4/(a*x+a)^{(1/2)/(-c*x+c)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 121, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {40, 39}

$$\frac{16x}{35a^4c^4\sqrt{ax+a}\sqrt{c-cx}} + \frac{8x}{35a^3c^3(ax+a)^{3/2}(c-cx)^{3/2}} + \frac{6x}{35a^2c^2(ax+a)^{5/2}(c-cx)^{5/2}} + \frac{x}{7ac(ax+a)^{7/2}(c-cx)^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + a*x)^(9/2)*(c - c*x)^(9/2)), x]

[Out] $x/(7*a*c*(a + a*x)^{(7/2)*(c - c*x)^{(7/2)} + (6*x)/(35*a^2*c^2*(a + a*x)^{(5/2)*(c - c*x)^{(5/2)} + (8*x)/(35*a^3*c^3*(a + a*x)^{(3/2)*(c - c*x)^{(3/2)} + (16*x)/(35*a^4*c^4*sqrt[a + a*x]*sqrt[c - c*x])$

Rule 39

Int[1/(((a_) + (b_)*(x_))^(3/2)*((c_) + (d_)*(x_))^(3/2)), x_Symbol] := Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(m_), x_Symbol] := -Simp[(x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+ax)^{9/2}(c-cx)^{9/2}} dx &= \frac{x}{7ac(a+ax)^{7/2}(c-cx)^{7/2}} + \frac{6 \int \frac{1}{(a+ax)^{7/2}(c-cx)^{7/2}} dx}{7ac} \\
&= \frac{x}{7ac(a+ax)^{7/2}(c-cx)^{7/2}} + \frac{6x}{35a^2c^2(a+ax)^{5/2}(c-cx)^{5/2}} + \frac{24 \int \frac{1}{(a+ax)^{5/2}(c-cx)^{5/2}} dx}{35a^2c^2} \\
&= \frac{x}{7ac(a+ax)^{7/2}(c-cx)^{7/2}} + \frac{6x}{35a^2c^2(a+ax)^{5/2}(c-cx)^{5/2}} + \frac{8x}{35a^3c^3(a+ax)^{3/2}(c-cx)^{3/2}} \\
&= \frac{x}{7ac(a+ax)^{7/2}(c-cx)^{7/2}} + \frac{6x}{35a^2c^2(a+ax)^{5/2}(c-cx)^{5/2}} + \frac{8x}{35a^3c^3(a+ax)^{3/2}(c-cx)^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 54, normalized size = 0.45

$$\frac{x(16x^6 - 56x^4 + 70x^2 - 35)}{35a^4c^4(x^2 - 1)^3 \sqrt{a(x+1)} \sqrt{c-cx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + a*x)^(9/2)*(c - c*x)^(9/2)), x]

[Out] (x*(-35 + 70*x^2 - 56*x^4 + 16*x^6))/(35*a^4*c^4*Sqrt[a*(1 + x)]*Sqrt[c - c*x]*(-1 + x^2)^3)

fricas [A] time = 0.43, size = 89, normalized size = 0.74

$$\frac{(16x^7 - 56x^5 + 70x^3 - 35x)\sqrt{ax+a}\sqrt{-cx+c}}{35(a^5c^5x^8 - 4a^5c^5x^6 + 6a^5c^5x^4 - 4a^5c^5x^2 + a^5c^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a*x+a)^(9/2)/(-c*x+c)^(9/2), x, algorithm="fricas")

[Out] -1/35*(16*x^7 - 56*x^5 + 70*x^3 - 35*x)*sqrt(a*x + a)*sqrt(-c*x + c)/(a^5*c^5*x^8 - 4*a^5*c^5*x^6 + 6*a^5*c^5*x^4 - 4*a^5*c^5*x^2 + a^5*c^5)

giac [B] time = 1.56, size = 437, normalized size = 3.61

$$\frac{\sqrt{-(ax+a)ac+2a^2c} \left((ax+a) \left((ax+a) \left(\frac{256(ax+a)|a|}{a^2c} - \frac{1617|a|}{ac} \right) + \frac{3430|a|}{c} \right) - \frac{2450a|a|}{c} \right) \sqrt{ax+a}}{1120((ax+a)ac-2a^2c)^4} + \frac{16384a^{12}c^6 - 51744a^{11}c^5 + 103488a^{10}c^4 - 103488a^9c^3 + 51744a^8c^2 - 16384a^7c}{1120((ax+a)ac-2a^2c)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a*x+a)^(9/2)/(-c*x+c)^(9/2),x, algorithm="giac")`

[Out]
$$\begin{aligned} & -1/1120*\sqrt{-(a*x + a)*a*c + 2*a^2*c}*((a*x + a)*((a*x + a)*(256*(a*x + a) \\ & *abs(a)/(a^2*c) - 1617*abs(a)/(a*c)) + 3430*abs(a)/c) - 2450*a*abs(a)/c)*\sqrt{ \\ & a*x + a}/((a*x + a)*a*c - 2*a^2*c)^4 + 1/280*(16384*a^12*c^6 - 51744*(\sqrt{ \\ & -a*c})*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c})^2*a^10*c^5 + 66416 \\ & *(\sqrt{-a*c})*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c})^4*a^8*c^4 - 43 \\ & 120*(\sqrt{-a*c})*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c})^6*a^6*c^3 + \\ & 14280*(\sqrt{-a*c})*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c})^8*a^4*c^2 \\ & - 2450*(\sqrt{-a*c})*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c})^10*a^2 \\ & *c + 175*(\sqrt{-a*c})*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c})^12)/((\\ & 2*a^2*c - (\sqrt{-a*c})*\sqrt{a*x + a} - \sqrt{-(a*x + a)*a*c + 2*a^2*c})^2)^7* \\ & \sqrt{-a*c}*a*c^3*abs(a) \end{aligned}$$

maple [A] time = 0.00, size = 42, normalized size = 0.35

$$\frac{(x+1)(x-1)(16x^6 - 56x^4 + 70x^2 - 35)x}{35(ax+a)^{\frac{9}{2}}(-cx+c)^{\frac{9}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(a*x+a)^(9/2)/(-c*x+c)^(9/2),x)`

[Out] $1/35*(x+1)*(x-1)*x*(16*x^6-56*x^4+70*x^2-35)/(a*x+a)^(9/2)/(-c*x+c)^(9/2)$

maxima [A] time = 1.40, size = 89, normalized size = 0.74

$$\frac{x}{7(-acx^2 + ac)^{\frac{7}{2}}ac} + \frac{6x}{35(-acx^2 + ac)^{\frac{5}{2}}a^2c^2} + \frac{8x}{35(-acx^2 + ac)^{\frac{3}{2}}a^3c^3} + \frac{16x}{35\sqrt{-acx^2 + ac}a^4c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a*x+a)^(9/2)/(-c*x+c)^(9/2),x, algorithm="maxima")`

[Out]
$$\begin{aligned} & 1/7*x/((-a*c*x^2 + a*c)^(7/2)*a*c) + 6/35*x/((-a*c*x^2 + a*c)^(5/2)*a^2*c^2 \\ &) + 8/35*x/((-a*c*x^2 + a*c)^(3/2)*a^3*c^3) + 16/35*x/(\sqrt{-a*c*x^2 + a*c} \\ & *a^4*c^4) \end{aligned}$$

mupad [B] time = 0.48, size = 66, normalized size = 0.55

$$\frac{x(16x^6 - 56x^4 + 70x^2 - 35)}{35a^4\sqrt{a+ax}(c-cx)^{7/2}(c-x^2(c-cx)+7cx-4x(c-cx))}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a + a*x)^(9/2)*(c - c*x)^(9/2)),x)
```

```
[Out] -(x*(70*x^2 - 56*x^4 + 16*x^6 - 35))/(35*a^4*(a + a*x)^(1/2)*(c - c*x)^(7/2)
)*(c - x^2*(c - c*x) + 7*c*x - 4*x*(c - c*x))
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a*x+a)**(9/2)/(-c*x+c)**(9/2),x)
```

```
[Out] Timed out
```


3.1145 $\int (a + bx)^{5/2} (ac - bcx)^{5/2} dx$

Optimal. Leaf size=135

$$\frac{5a^6c^{5/2} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{a+bx}}{\sqrt{c(a-bx)}}\right)}{8b} + \frac{5}{16}a^4c^2x\sqrt{a+bx}\sqrt{ac-bcx} + \frac{5}{24}a^2cx(a+bx)^{3/2}(ac-bcx)^{3/2} + \frac{1}{6}x(a+bx)^{5/2}(ac-bcx)^{5/2}$$

[Out] $5/24*a^2*c*x*(b*x+a)^{(3/2)}*(-b*c*x+a*c)^{(3/2)}+1/6*x*(b*x+a)^{(5/2)}*(-b*c*x+a*c)^{(5/2)}+5/8*a^6*c^{(5/2)}*\arctan(c^{(1/2)}*(b*x+a)^{(1/2)}/(c*(-b*x+a))^{(1/2)})/b+5/16*a^4*c^2*x*(b*x+a)^{(1/2)}*(-b*c*x+a*c)^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 135, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.174$, Rules used = {38, 63, 217, 203}

$$\frac{5}{16}a^4c^2x\sqrt{a+bx}\sqrt{ac-bcx} + \frac{5a^6c^{5/2} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{a+bx}}{\sqrt{c(a-bx)}}\right)}{8b} + \frac{5}{24}a^2cx(a+bx)^{3/2}(ac-bcx)^{3/2} + \frac{1}{6}x(a+bx)^{5/2}(ac-bcx)^{5/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2)*(a*c - b*c*x)^(5/2), x]

[Out] $(5*a^4*c^2*x*\text{Sqrt}[a + b*x]*\text{Sqrt}[a*c - b*c*x])/16 + (5*a^2*c*x*(a + b*x)^{(3/2)}*(a*c - b*c*x)^{(3/2)})/24 + (x*(a + b*x)^{(5/2)}*(a*c - b*c*x)^{(5/2)})/6 + (5*a^6*c^{(5/2)}*\text{ArcTan}[(\text{Sqrt}[c]*\text{Sqrt}[a + b*x])/(\text{Sqrt}[c*(a - b*x)])])/(8*b)$

Rule 38

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[(x*(a + b*x)^m*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 63

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[Rt[b, 2]*x]/Rt[a, 2])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a

, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int (a + bx)^{5/2}(ac - bcx)^{5/2} dx &= \frac{1}{6}x(a + bx)^{5/2}(ac - bcx)^{5/2} + \frac{1}{6}(5a^2c) \int (a + bx)^{3/2}(ac - bcx)^{3/2} dx \\
 &= \frac{5}{24}a^2cx(a + bx)^{3/2}(ac - bcx)^{3/2} + \frac{1}{6}x(a + bx)^{5/2}(ac - bcx)^{5/2} + \frac{1}{8}(5a^4c^2) \int \sqrt{a + bx} \sqrt{ac - bcx} dx \\
 &= \frac{5}{16}a^4c^2x\sqrt{a + bx} \sqrt{ac - bcx} + \frac{5}{24}a^2cx(a + bx)^{3/2}(ac - bcx)^{3/2} + \frac{1}{6}x(a + bx)^{5/2}(ac - bcx)^{5/2} \\
 &= \frac{5}{16}a^4c^2x\sqrt{a + bx} \sqrt{ac - bcx} + \frac{5}{24}a^2cx(a + bx)^{3/2}(ac - bcx)^{3/2} + \frac{1}{6}x(a + bx)^{5/2}(ac - bcx)^{5/2} \\
 &= \frac{5}{16}a^4c^2x\sqrt{a + bx} \sqrt{ac - bcx} + \frac{5}{24}a^2cx(a + bx)^{3/2}(ac - bcx)^{3/2} + \frac{1}{6}x(a + bx)^{5/2}(ac - bcx)^{5/2} \\
 &= \frac{5}{16}a^4c^2x\sqrt{a + bx} \sqrt{ac - bcx} + \frac{5}{24}a^2cx(a + bx)^{3/2}(ac - bcx)^{3/2} + \frac{1}{6}x(a + bx)^{5/2}(ac - bcx)^{5/2}
 \end{aligned}$$

Mathematica [A] time = 0.15, size = 120, normalized size = 0.89

$$\frac{c^3 \left(-30a^{13/2} \sqrt{a - bx} \sqrt{\frac{bx}{a} + 1} \sin^{-1} \left(\frac{\sqrt{a - bx}}{\sqrt{2} \sqrt{a}} \right) + 33a^6 bx - 59a^4 b^3 x^3 + 34a^2 b^5 x^5 - 8b^7 x^7 \right)}{48b \sqrt{a + bx} \sqrt{c(a - bx)}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)*(a*c - b*c*x)^(5/2), x]

[Out] (c^3*(33*a^6*b*x - 59*a^4*b^3*x^3 + 34*a^2*b^5*x^5 - 8*b^7*x^7 - 30*a^(13/2)*Sqrt[a - b*x]*Sqrt[1 + (b*x)/a]*ArcSin[Sqrt[a - b*x]/(Sqrt[2]*Sqrt[a])]))/(48*b*Sqrt[c*(a - b*x)]*Sqrt[a + b*x])

fricas [A] time = 0.47, size = 232, normalized size = 1.72

$$\left[\frac{15a^6 \sqrt{-c} c^2 \log(2b^2cx^2 + 2\sqrt{-bcx + ac} \sqrt{bx + a} b \sqrt{-c} x - a^2c) + 2(8b^5c^2x^5 - 26a^2b^3c^2x^3 + 33a^4bc^2x) \sqrt{-bcx}}{96b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(-b*c*x+a*c)^(5/2),x, algorithm="fricas")

[Out] [1/96*(15*a^6*sqrt(-c)*c^2*log(2*b^2*c*x^2 + 2*sqrt(-b*c*x + a*c)*sqrt(b*x + a)*b*sqrt(-c)*x - a^2*c) + 2*(8*b^5*c^2*x^5 - 26*a^2*b^3*c^2*x^3 + 33*a^4*b*c^2*x)*sqrt(-b*c*x + a*c)*sqrt(b*x + a))/b, -1/48*(15*a^6*c^(5/2)*arctan(sqrt(-b*c*x + a*c)*sqrt(b*x + a)*b*sqrt(c)*x/(b^2*c*x^2 - a^2*c)) - (8*b^5*c^2*x^5 - 26*a^2*b^3*c^2*x^3 + 33*a^4*b*c^2*x)*sqrt(-b*c*x + a*c)*sqrt(b*x + a))/b]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(-b*c*x+a*c)^(5/2),x, algorithm="giac")

[Out] Timed out

maple [B] time = 0.01, size = 243, normalized size = 1.80

$$\frac{5\sqrt{(bx+a)(-bcx+ac)} a^6 c^3 \arctan\left(\frac{\sqrt{b^2 c} x}{\sqrt{-b^2 c x^2 + a^2 c}}\right)}{16\sqrt{-bcx+ac} \sqrt{bx+a} \sqrt{b^2 c}} + \frac{5\sqrt{-bcx+ac} \sqrt{bx+a} a^5 c^2}{16b} + \frac{5(-bcx+ac)^{\frac{3}{2}} \sqrt{bx+a} a^4 c}{48b} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)*(-b*c*x+a*c)^(5/2),x)

[Out] -1/6/b/c*(b*x+a)^(5/2)*(-b*c*x+a*c)^(7/2)-1/6*a/b/c*(b*x+a)^(3/2)*(-b*c*x+a*c)^(7/2)-1/8*a^2/b/c*(b*x+a)^(1/2)*(-b*c*x+a*c)^(7/2)+1/24*a^3/b*(-b*c*x+a*c)^(5/2)*(b*x+a)^(1/2)+5/48*a^4*c/b*(-b*c*x+a*c)^(3/2)*(b*x+a)^(1/2)+5/16*a^5*c^2/b*(-b*c*x+a*c)^(1/2)*(b*x+a)^(1/2)+5/16*a^6*c^3*((b*x+a)*(-b*c*x+a*c))^(1/2)/(-b*c*x+a*c)^(1/2)/(b*x+a)^(1/2)/(b^2*c)^(1/2)*arctan((b^2*c)^(1/2)*x/(-b^2*c*x^2+a^2*c)^(1/2))

maxima [A] time = 3.12, size = 89, normalized size = 0.66

$$\frac{5 a^6 c^{\frac{5}{2}} \arcsin\left(\frac{bx}{a}\right)}{16 b} + \frac{5}{16} \sqrt{-b^2 c x^2 + a^2 c} a^4 c^2 x + \frac{5}{24} (-b^2 c x^2 + a^2 c)^{\frac{3}{2}} a^2 c x + \frac{1}{6} (-b^2 c x^2 + a^2 c)^{\frac{5}{2}} x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(-b*c*x+a*c)^(5/2),x, algorithm="maxima")

[Out] $5/16*a^6*c^{(5/2)}*\arcsin(b*x/a)/b + 5/16*\sqrt{-b^2*c*x^2 + a^2*c}*a^4*c^2*x + 5/24*(-b^2*c*x^2 + a^2*c)^{(3/2)}*a^2*c*x + 1/6*(-b^2*c*x^2 + a^2*c)^{(5/2)}*x$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (ac - bcx)^{5/2} (a + bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c - b*c*x)^(5/2)*(a + b*x)^(5/2), x)`

[Out] `int((a*c - b*c*x)^(5/2)*(a + b*x)^(5/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (-c(-a + bx))^{5/2} (a + bx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(5/2)*(-b*c*x+a*c)**(5/2), x)`

[Out] `Integral((-c*(-a + b*x))**(5/2)*(a + b*x)**(5/2), x)`

3.1146 $\int (a + bx)^{3/2} (ac - bcx)^{3/2} dx$

Optimal. Leaf size=102

$$\frac{3a^4c^{3/2} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{a+bx}}{\sqrt{c(a-bx)}}\right)}{4b} + \frac{3}{8}a^2cx\sqrt{a+bx}\sqrt{ac-bcx} + \frac{1}{4}x(a+bx)^{3/2}(ac-bcx)^{3/2}$$

[Out] $1/4*x*(b*x+a)^{(3/2)}*(-b*c*x+a*c)^{(3/2)}+3/4*a^4*c^{(3/2)}*\arctan(c^{(1/2)}*(b*x+a)^{(1/2)}/(c*(-b*x+a))^{(1/2)})/b+3/8*a^2*c*x*(b*x+a)^{(1/2)}*(-b*c*x+a*c)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.174$, Rules used = {38, 63, 217, 203}

$$\frac{3a^4c^{3/2} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{a+bx}}{\sqrt{c(a-bx)}}\right)}{4b} + \frac{3}{8}a^2cx\sqrt{a+bx}\sqrt{ac-bcx} + \frac{1}{4}x(a+bx)^{3/2}(ac-bcx)^{3/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)*(a*c - b*c*x)^(3/2), x]

[Out] $(3*a^2*c*x*\text{Sqrt}[a + b*x]*\text{Sqrt}[a*c - b*c*x])/8 + (x*(a + b*x)^{(3/2)}*(a*c - b*c*x)^{(3/2)})/4 + (3*a^4*c^{(3/2)}*\text{ArcTan}[(\text{Sqrt}[c]*\text{Sqrt}[a + b*x])/\text{Sqrt}[c*(a - b*x)]])/ (4*b)$

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(x*(a + b*x)^m*(c + d*x)^m)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(m - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[Rt[b, 2]*x]/Rt[a, 2])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a

, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int (a + bx)^{3/2}(ac - bcx)^{3/2} dx &= \frac{1}{4}x(a + bx)^{3/2}(ac - bcx)^{3/2} + \frac{1}{4}(3a^2c) \int \sqrt{a + bx} \sqrt{ac - bcx} dx \\
 &= \frac{3}{8}a^2cx\sqrt{a + bx} \sqrt{ac - bcx} + \frac{1}{4}x(a + bx)^{3/2}(ac - bcx)^{3/2} + \frac{1}{8}(3a^4c^2) \int \frac{1}{\sqrt{a + bx} \sqrt{ac - bcx}} dx \\
 &= \frac{3}{8}a^2cx\sqrt{a + bx} \sqrt{ac - bcx} + \frac{1}{4}x(a + bx)^{3/2}(ac - bcx)^{3/2} + \frac{(3a^4c^2) \text{Subst}\left(\int \frac{1}{\sqrt{2ac - cx^2}} dx\right)}{4b} \\
 &= \frac{3}{8}a^2cx\sqrt{a + bx} \sqrt{ac - bcx} + \frac{1}{4}x(a + bx)^{3/2}(ac - bcx)^{3/2} + \frac{(3a^4c^2) \text{Subst}\left(\int \frac{1}{1 + cx^2} dx\right)}{4b} \\
 &= \frac{3}{8}a^2cx\sqrt{a + bx} \sqrt{ac - bcx} + \frac{1}{4}x(a + bx)^{3/2}(ac - bcx)^{3/2} + \frac{3a^4c^{3/2} \tan^{-1}\left(\frac{\sqrt{c} \sqrt{a + bx}}{\sqrt{c(a - bx)}}\right)}{4b}
 \end{aligned}$$

Mathematica [A] time = 0.13, size = 109, normalized size = 1.07

$$\frac{c^2 \left(-6a^{9/2} \sqrt{a - bx} \sqrt{\frac{bx}{a}} + 1 \sin^{-1} \left(\frac{\sqrt{a - bx}}{\sqrt{2} \sqrt{a}} \right) + 5a^4bx - 7a^2b^3x^3 + 2b^5x^5 \right)}{8b\sqrt{a + bx} \sqrt{c(a - bx)}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)*(a*c - b*c*x)^(3/2), x]

[Out] (c^2*(5*a^4*b*x - 7*a^2*b^3*x^3 + 2*b^5*x^5 - 6*a^(9/2)*Sqrt[a - b*x]*Sqrt[1 + (b*x)/a]*ArcSin[Sqrt[a - b*x]/(Sqrt[2]*Sqrt[a])]))/(8*b*Sqrt[c*(a - b*x)]*Sqrt[a + b*x])

fricas [A] time = 0.49, size = 193, normalized size = 1.89

$$\left[\frac{3a^4\sqrt{-c} \log\left(2b^2cx^2 + 2\sqrt{-bcx + ac}\sqrt{bx + a}b\sqrt{-c}x - a^2c\right) - 2\left(2b^3cx^3 - 5a^2bcx\right)\sqrt{-bcx + ac}\sqrt{bx + a}}{16b}, - \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(-b*c*x+a*c)^(3/2),x, algorithm="fricas")

[Out] [1/16*(3*a^4*sqrt(-c)*c*log(2*b^2*c*x^2 + 2*sqrt(-b*c*x + a*c)*sqrt(b*x + a))*b*sqrt(-c)*x - a^2*c) - 2*(2*b^3*c*x^3 - 5*a^2*b*c*x)*sqrt(-b*c*x + a*c)*sqrt(b*x + a))/b, -1/8*(3*a^4*c^(3/2)*arctan(sqrt(-b*c*x + a*c)*sqrt(b*x + a))*b*sqrt(c)*x/(b^2*c*x^2 - a^2*c)) + (2*b^3*c*x^3 - 5*a^2*b*c*x)*sqrt(-b*c*x + a*c)*sqrt(b*x + a))/b]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(-b*c*x+a*c)^(3/2),x, algorithm="giac")

[Out] Timed out

maple [B] time = 0.01, size = 185, normalized size = 1.81

$$\frac{3\sqrt{(bx+a)(-bcx+ac)} a^4 c^2 \arctan\left(\frac{\sqrt{b^2 c} x}{\sqrt{-b^2 c x^2 + a^2 c}}\right)}{8\sqrt{-bcx+ac} \sqrt{bx+a} \sqrt{b^2 c}} + \frac{3\sqrt{-bcx+ac} \sqrt{bx+a} a^3 c}{8b} + \frac{(-bcx+ac)^{\frac{3}{2}} \sqrt{bx+a} a^2}{8b} - \frac{\sqrt{bx+a}}{8b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)*(-b*c*x+a*c)^(3/2),x)

[Out] -1/4/b/c*(b*x+a)^(3/2)*(-b*c*x+a*c)^(5/2)-1/4*a/b/c*(b*x+a)^(1/2)*(-b*c*x+a*c)^(5/2)+1/8*a^2/b*(-b*c*x+a*c)^(3/2)*(b*x+a)^(1/2)+3/8*a^3/c/b*(-b*c*x+a*c)^(1/2)*(b*x+a)^(1/2)+3/8*a^4*c^2*((b*x+a)*(-b*c*x+a*c))^(1/2)/(-b*c*x+a*c)^(1/2)/(b*x+a)^(1/2)/(b^2*c)^(1/2)*arctan((b^2*c)^(1/2)/(-b^2*c*x^2+a^2*c)^(1/2)*x)

maxima [A] time = 3.02, size = 63, normalized size = 0.62

$$\frac{3 a^4 c^{\frac{3}{2}} \arcsin\left(\frac{bx}{a}\right)}{8 b} + \frac{3}{8} \sqrt{-b^2 c x^2 + a^2 c} a^2 c x + \frac{1}{4} (-b^2 c x^2 + a^2 c)^{\frac{3}{2}} x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(-b*c*x+a*c)^(3/2),x, algorithm="maxima")

[Out] 3/8*a^4*c^(3/2)*arcsin(b*x/a)/b + 3/8*sqrt(-b^2*c*x^2 + a^2*c)*a^2*c*x + 1/4*(-b^2*c*x^2 + a^2*c)^(3/2)*x

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (ac - bcx)^{3/2} (a + bx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c - b*c*x)^(3/2)*(a + b*x)^(3/2), x)

[Out] int((a*c - b*c*x)^(3/2)*(a + b*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (-c(-a + bx))^{\frac{3}{2}} (a + bx)^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)*(-b*c*x+a*c)**(3/2), x)

[Out] Integral((-c*(-a + b*x))**(3/2)*(a + b*x)**(3/2), x)

3.1147 $\int \sqrt{a + bx} \sqrt{ac - bcx} dx$

Optimal. Leaf size=68

$$\frac{a^2 \sqrt{c} \tan^{-1} \left(\frac{\sqrt{c} \sqrt{a+bx}}{\sqrt{c(a-bx)}} \right)}{b} + \frac{1}{2} x \sqrt{a + bx} \sqrt{ac - bcx}$$

[Out] $a^2 \arctan(c^{(1/2)}(b*x+a)^{(1/2)} / (c*(-b*x+a))^{(1/2)}) * c^{(1/2)} / b + 1/2 * x * (b*x+a)^{(1/2)} * (-b*c*x+a*c)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.174$, Rules used = {38, 63, 217, 203}

$$\frac{a^2 \sqrt{c} \tan^{-1} \left(\frac{\sqrt{c} \sqrt{a+bx}}{\sqrt{c(a-bx)}} \right)}{b} + \frac{1}{2} x \sqrt{a + bx} \sqrt{ac - bcx}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]*Sqrt[a*c - b*c*x], x]

[Out] $(x*\text{Sqrt}[a + b*x]*\text{Sqrt}[a*c - b*c*x])/2 + (a^2*\text{Sqrt}[c]*\text{ArcTan}[(\text{Sqrt}[c]*\text{Sqrt}[a + b*x])/\text{Sqrt}[c*(a - b*x)]])/b$

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(x*(a + b*x)^m*(c + d*x)^n)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])

Rule 217

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]`

Rubi steps

$$\begin{aligned} \int \sqrt{a+bx} \sqrt{ac-bcx} dx &= \frac{1}{2}x\sqrt{a+bx} \sqrt{ac-bcx} + \frac{1}{2}(a^2c) \int \frac{1}{\sqrt{a+bx} \sqrt{ac-bcx}} dx \\ &= \frac{1}{2}x\sqrt{a+bx} \sqrt{ac-bcx} + \frac{(a^2c) \operatorname{Subst}\left(\int \frac{1}{\sqrt{2ac-cx^2}} dx, x, \sqrt{a+bx}\right)}{b} \\ &= \frac{1}{2}x\sqrt{a+bx} \sqrt{ac-bcx} + \frac{(a^2c) \operatorname{Subst}\left(\int \frac{1}{1+cx^2} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c(a-bx)}}\right)}{b} \\ &= \frac{1}{2}x\sqrt{a+bx} \sqrt{ac-bcx} + \frac{a^2\sqrt{c} \tan^{-1}\left(\frac{\sqrt{c}\sqrt{a+bx}}{\sqrt{c(a-bx)}}\right)}{b} \end{aligned}$$

Mathematica [A] time = 0.12, size = 95, normalized size = 1.40

$$\frac{c\left(-2a^{5/2}\sqrt{a-bx}\sqrt{\frac{bx}{a}+1}\sin^{-1}\left(\frac{\sqrt{a-bx}}{\sqrt{2}\sqrt{a}}\right)+a^2bx-b^3x^3\right)}{2b\sqrt{a+bx}\sqrt{c(a-bx)}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]*Sqrt[a*c - b*c*x], x]

[Out] $(c*(a^2*b*x - b^3*x^3 - 2*a^{(5/2)}*\sqrt{a - b*x}*\sqrt{1 + (b*x)/a}*\operatorname{ArcSin}[\sqrt{a - b*x}/(\sqrt{2}*\sqrt{a})]))/(2*b*\sqrt{c*(a - b*x)}*\sqrt{a + b*x})$

fricas [A] time = 0.47, size = 159, normalized size = 2.34

$$\left[\frac{a^2\sqrt{-c} \log\left(2b^2cx^2 + 2\sqrt{-bcx+ac}\sqrt{bx+a}b\sqrt{-c}x - a^2c\right) + 2\sqrt{-bcx+ac}\sqrt{bx+a}bx}{4b}, -\frac{a^2\sqrt{c} \arctan\left(\frac{\sqrt{-bcx+ac}}{b^2c}\right)}{b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(-b*c*x+a*c)^(1/2), x, algorithm="fricas")

[Out] $[1/4*(a^2*\sqrt{-c})*\log(2*b^2*c*x^2 + 2*\sqrt{-b*c*x + a*c}*\sqrt{b*x + a})*b*\sqrt{-c}*x - a^2*c) + 2*\sqrt{-b*c*x + a*c}*\sqrt{b*x + a}*b*x)/b, -1/2*(a^2*$

$\text{qrt}(c) \cdot \arctan(\sqrt{-b \cdot c \cdot x + a \cdot c}) \cdot \sqrt{b \cdot x + a} \cdot b \cdot \sqrt{c} \cdot x / (b^2 \cdot c \cdot x^2 - a^2 \cdot c) - \sqrt{-b \cdot c \cdot x + a \cdot c} \cdot \sqrt{b \cdot x + a} \cdot b \cdot x / b]$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)*(-b*c*x+a*c)^(1/2),x, algorithm="giac")`

[Out] Timed out

maple [B] time = 0.01, size = 127, normalized size = 1.87

$$\frac{\sqrt{(bx+a)(-bcx+ac)} a^2 c \arctan\left(\frac{\sqrt{b^2 c} x}{\sqrt{-b^2 c x^2 + a^2 c}}\right) + \frac{\sqrt{-bcx+ac} \sqrt{bx+a} a}{2b} - \frac{\sqrt{bx+a} (-bcx+ac)^{\frac{3}{2}}}{2bc}}{2\sqrt{-bcx+ac} \sqrt{bx+a} \sqrt{b^2 c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(1/2)*(-b*c*x+a*c)^(1/2),x)`

[Out] $-1/2/b/c \cdot (b \cdot x + a)^{1/2} \cdot (-b \cdot c \cdot x + a \cdot c)^{3/2} + 1/2 \cdot a/b \cdot (-b \cdot c \cdot x + a \cdot c)^{1/2} \cdot (b \cdot x + a)^{1/2} + 1/2 \cdot a^2 \cdot c \cdot ((b \cdot x + a) \cdot (-b \cdot c \cdot x + a \cdot c))^{1/2} / (-b \cdot c \cdot x + a \cdot c)^{1/2} / (b \cdot x + a)^{1/2} / (b^2 \cdot c)^{1/2} \cdot \arctan((b^2 \cdot c)^{1/2} / (-b^2 \cdot c \cdot x^2 + a^2 \cdot c)^{1/2} \cdot x)$

maxima [A] time = 3.09, size = 39, normalized size = 0.57

$$\frac{a^2 \sqrt{c} \arcsin\left(\frac{bx}{a}\right)}{2b} + \frac{1}{2} \sqrt{-b^2 c x^2 + a^2 c} x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)*(-b*c*x+a*c)^(1/2),x, algorithm="maxima")`

[Out] $1/2 \cdot a^2 \cdot \sqrt{c} \cdot \arcsin(b \cdot x / a) / b + 1/2 \cdot \sqrt{-b^2 \cdot c \cdot x^2 + a^2 \cdot c} \cdot x$

mupad [B] time = 0.20, size = 72, normalized size = 1.06

$$\frac{x \sqrt{a c - b c x} \sqrt{a + b x}}{2} - \frac{a^2 \sqrt{b} c^2 \ln\left(\sqrt{-b c} \sqrt{c(a - b x)} \sqrt{a + b x} - b^{3/2} c x\right)}{2(-b c)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c - b*c*x)^(1/2)*(a + b*x)^(1/2),x)`

```
[Out] (x*(a*c - b*c*x)^(1/2)*(a + b*x)^(1/2))/2 - (a^2*b^(1/2)*c^2*log((-b*c)^(1/2)*(c*(a - b*x))^(1/2)*(a + b*x)^(1/2) - b^(3/2)*c*x))/(2*(-b*c)^(3/2))
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \sqrt{-c(-a + bx)} \sqrt{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(1/2)*(-b*c*x+a*c)**(1/2),x)
```

```
[Out] Integral(sqrt(-c*(-a + b*x))*sqrt(a + b*x), x)
```

$$3.1148 \quad \int \frac{1}{\sqrt{a+bx} \sqrt{ac-bcx}} dx$$

Optimal. Leaf size=38

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{c} \sqrt{a+bx}}{\sqrt{c(a-bx)}} \right)}{b\sqrt{c}}$$

[Out] $2*\arctan(c^{(1/2)}*(b*x+a)^{(1/2)/(c*(-b*x+a))^{(1/2)})/b/c^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.130$, Rules used = {63, 217, 203}

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{c} \sqrt{a+bx}}{\sqrt{c(a-bx)}} \right)}{b\sqrt{c}}$$

Antiderivative was successfully verified.

[In] `Int[1/(Sqrt[a + b*x]*Sqrt[a*c - b*c*x]),x]`

[Out] `(2*ArcTan[(Sqrt[c]*Sqrt[a + b*x])/Sqrt[c*(a - b*x)]])/(b*Sqrt[c])`

Rule 63

`Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 203

`Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])`

Rule 217

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]`

Rubi steps

$$\int \frac{1}{\sqrt{a+bx}\sqrt{ac-bcx}} dx = \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2ac-cx^2}} dx, x, \sqrt{a+bx}\right)}{b}$$

$$= \frac{2 \operatorname{Subst}\left(\int \frac{1}{1+cx^2} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c(a-bx)}}\right)}{b}$$

$$= \frac{2 \tan^{-1}\left(\frac{\sqrt{c}\sqrt{a+bx}}{\sqrt{c(a-bx)}}\right)}{b\sqrt{c}}$$

Mathematica [A] time = 0.01, size = 48, normalized size = 1.26

$$-\frac{2\sqrt{a-bx} \tan^{-1}\left(\frac{\sqrt{a-bx}}{\sqrt{a+bx}}\right)}{b\sqrt{c(a-bx)}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*Sqrt[a*c - b*c*x]), x]

[Out] (-2*Sqrt[a - b*x]*ArcTan[Sqrt[a - b*x]/Sqrt[a + b*x]])/(b*Sqrt[c*(a - b*x)])

fricas [A] time = 0.49, size = 108, normalized size = 2.84

$$\left[-\frac{\sqrt{-c} \log\left(2b^2cx^2 - 2\sqrt{-bcx+ac}\sqrt{bx+a}b\sqrt{-c}x - a^2c\right)}{2bc}, -\frac{\arctan\left(\frac{\sqrt{-bcx+ac}\sqrt{bx+a}b\sqrt{cx}}{b^2cx^2-a^2c}\right)}{b\sqrt{c}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(-b*c*x+a*c)^(1/2), x, algorithm="fricas")

[Out] [-1/2*sqrt(-c)*log(2*b^2*c*x^2 - 2*sqrt(-b*c*x + a*c)*sqrt(b*x + a)*b*sqrt(-c)*x - a^2*c)/(b*c), -arctan(sqrt(-b*c*x + a*c)*sqrt(b*x + a)*b*sqrt(c)*x/(b^2*c*x^2 - a^2*c))/(b*sqrt(c))]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(-b*c*x+a*c)^(1/2),x, algorithm="giac")

[Out] Timed out

maple [B] time = 0.00, size = 71, normalized size = 1.87

$$\frac{\sqrt{(bx+a)(-bcx+ac)} \arctan\left(\frac{\sqrt{b^2c}x}{\sqrt{-b^2cx^2+a^2c}}\right)}{\sqrt{bx+a} \sqrt{-bcx+ac} \sqrt{b^2c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(-b*c*x+a*c)^(1/2),x)

[Out] ((b*x+a)*(-b*c*x+a*c))^(1/2)/(b*x+a)^(1/2)/(-b*c*x+a*c)^(1/2)/(b^2*c)^(1/2)*arctan((b^2*c)^(1/2)/(-b^2*c*x^2+a^2*c)^(1/2)*x)

maxima [A] time = 2.93, size = 14, normalized size = 0.37

$$\frac{\arcsin\left(\frac{bx}{a}\right)}{b\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(-b*c*x+a*c)^(1/2),x, algorithm="maxima")

[Out] arcsin(b*x/a)/(b*sqrt(c))

mupad [B] time = 0.18, size = 53, normalized size = 1.39

$$-\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{ac-bcx}-\sqrt{ac})}{\sqrt{b^2c}(\sqrt{a+bx}-\sqrt{a})}\right)}{\sqrt{b^2c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a*c - b*c*x)^(1/2)*(a + b*x)^(1/2)),x)

[Out] -(4*atan((b*((a*c - b*c*x)^(1/2) - (a*c)^(1/2)))/((b^2*c)^(1/2)*((a + b*x)^(1/2) - a^(1/2))))/(b^2*c)^(1/2)

sympy [C] time = 4.69, size = 90, normalized size = 2.37

$$-\frac{iG_{6,6}^{6,2}\left(0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1, 0 \left| \frac{a^2}{b^2x^2} \right.\right)}{4\pi^{\frac{3}{2}}b\sqrt{c}} + \frac{G_{6,6}^{2,6}\left(-\frac{1}{2}, -\frac{1}{4}, 0, \frac{1}{4}, \frac{1}{2}, 1 \left| \frac{a^2e^{-2i\pi}}{b^2x^2} \right.\right)}{4\pi^{\frac{3}{2}}b\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(1/2)/(-b*c*x+a*c)**(1/2),x)
```

```
[Out] -I*meijerg(((1/4, 3/4), (1/2, 1/2, 1, 1)), ((0, 1/4, 1/2, 3/4, 1, 0), ()),  
a**2/(b**2*x**2))/(4*pi**(3/2)*b*sqrt(c)) + meijerg(((1/2, -1/4, 0, 1/4, 1  
/2, 1), ()), ((-1/4, 1/4), (-1/2, 0, 0, 0)), a**2*exp_polar(-2*I*pi)/(b**2*  
x**2))/(4*pi**(3/2)*b*sqrt(c))
```


$$3.1149 \quad \int \frac{1}{(a+bx)^{3/2}(ac-bcx)^{3/2}} dx$$

Optimal. Leaf size=30

$$\frac{x}{a^2c\sqrt{a+bx}\sqrt{ac-bcx}}$$

[Out] x/a^2/c/(b*x+a)^(1/2)/(-b*c*x+a*c)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.043$, Rules used = {39}

$$\frac{x}{a^2c\sqrt{a+bx}\sqrt{ac-bcx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/2)*(a*c - b*c*x)^(3/2)), x]

[Out] x/(a^2*c*Sqrt[a + b*x]*Sqrt[a*c - b*c*x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := S
imp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && Eq
Q[b*c + a*d, 0]

Rubi steps

$$\int \frac{1}{(a+bx)^{3/2}(ac-bcx)^{3/2}} dx = \frac{x}{a^2c\sqrt{a+bx}\sqrt{ac-bcx}}$$

Mathematica [A] time = 0.01, size = 29, normalized size = 0.97

$$\frac{x}{a^2c\sqrt{a+bx}\sqrt{c(a-bx)}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(a*c - b*c*x)^(3/2)), x]

[Out] x/(a^2*c*Sqrt[c*(a - b*x)]*Sqrt[a + b*x])

fricas [A] time = 0.43, size = 45, normalized size = 1.50

$$-\frac{\sqrt{-bcx+ac}\sqrt{bx+ax}}{a^2b^2c^2x^2-a^4c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(-b*c*x+a*c)^(3/2),x, algorithm="fricas")

[Out] -sqrt(-b*c*x + a*c)*sqrt(b*x + a)*x/(a^2*b^2*c^2*x^2 - a^4*c^2)

giac [B] time = 1.86, size = 115, normalized size = 3.83

$$\frac{2\sqrt{-c}c}{\left(2ac^2 - \left(\sqrt{-bcx+ac}\sqrt{-c} - \sqrt{2ac^2+(bcx-ac)c}\right)^2\right)ab|c|} - \frac{\sqrt{-bcx+ac}}{2\sqrt{2ac^2+(bcx-ac)c}a^2b|c|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(-b*c*x+a*c)^(3/2),x, algorithm="giac")

[Out] 2*sqrt(-c)*c/((2*a*c^2 - (sqrt(-b*c*x + a*c)*sqrt(-c) - sqrt(2*a*c^2 + (b*c*x - a*c)*c))^2)*a*b*abs(c)) - 1/2*sqrt(-b*c*x + a*c)/(sqrt(2*a*c^2 + (b*c*x - a*c)*c)*a^2*b*abs(c))

maple [A] time = 0.00, size = 30, normalized size = 1.00

$$\frac{(-bx+a)x}{\sqrt{bx+a}(-bcx+ac)^{\frac{3}{2}}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(-b*c*x+a*c)^(3/2),x)

[Out] 1/(b*x+a)^(1/2)*(-b*x+a)/a^2*x/(-b*c*x+a*c)^(3/2)

maxima [A] time = 1.40, size = 25, normalized size = 0.83

$$\frac{x}{\sqrt{-b^2cx^2+a^2c}a^2c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(-b*c*x+a*c)^(3/2),x, algorithm="maxima")

[Out] x/(sqrt(-b^2*c*x^2 + a^2*c)*a^2*c)

mupad [B] time = 0.50, size = 26, normalized size = 0.87

$$\frac{x}{a^2 c \sqrt{a c - b c x} \sqrt{a + b x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a*c - b*c*x)^(3/2)*(a + b*x)^(3/2)),x)

[Out] x/(a^2*c*(a*c - b*c*x)^(1/2)*(a + b*x)^(1/2))

sympy [C] time = 5.18, size = 94, normalized size = 3.13

$$-\frac{iG_{6,6}^{5,3} \left(\begin{matrix} \frac{3}{4}, \frac{5}{4}, 1 & \frac{1}{2}, \frac{3}{2}, 2 \\ \frac{3}{4}, 1, \frac{5}{4}, \frac{3}{2}, 2 & 0 \end{matrix} \middle| \frac{a^2}{b^2 x^2} \right)}{2\pi^{\frac{3}{2}} a^2 b c^{\frac{3}{2}}} + \frac{G_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1 \\ \frac{1}{4}, \frac{3}{4} & -\frac{1}{2}, 0, 1, 0 \end{matrix} \middle| \frac{a^2 e^{-2i\pi}}{b^2 x^2} \right)}{2\pi^{\frac{3}{2}} a^2 b c^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(-b*c*x+a*c)**(3/2),x)

[Out] -I*meijerg(((3/4, 5/4, 1), (1/2, 3/2, 2)), ((3/4, 1, 5/4, 3/2, 2), (0,)), a**2/(b**2*x**2))/(2*pi**(3/2)*a**2*b*c**(3/2)) + meijerg(((-1/2, 0, 1/4, 1/2, 3/4, 1), ()), ((1/4, 3/4), (-1/2, 0, 1, 0)), a**2*exp_polar(-2*I*pi)/(b**2*x**2))/(2*pi**(3/2)*a**2*b*c**(3/2))

$$3.1150 \quad \int \frac{1}{(a+bx)^{5/2}(ac-bcx)^{5/2}} dx$$

Optimal. Leaf size=67

$$\frac{2x}{3a^4c^2\sqrt{a+bx}\sqrt{ac-bcx}} + \frac{x}{3a^2c(a+bx)^{3/2}(ac-bcx)^{3/2}}$$

[Out] $1/3*x/a^2/c/(b*x+a)^{(3/2)}/(-b*c*x+a*c)^{(3/2)}+2/3*x/a^4/c^2/(b*x+a)^{(1/2)}/(-b*c*x+a*c)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.087$, Rules used = {40, 39}

$$\frac{2x}{3a^4c^2\sqrt{a+bx}\sqrt{ac-bcx}} + \frac{x}{3a^2c(a+bx)^{3/2}(ac-bcx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*(a*c - b*c*x)^(5/2)), x]

[Out] $x/(3*a^2*c*(a + b*x)^{(3/2)*(a*c - b*c*x)^{(3/2)}) + (2*x)/(3*a^4*c^2*sqrt[a + b*x]*sqrt[a*c - b*c*x])$

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] :> Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> -Simp[(x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^{5/2}(ac-bcx)^{5/2}} dx &= \frac{x}{3a^2c(a+bx)^{3/2}(ac-bcx)^{3/2}} + \frac{2 \int \frac{1}{(a+bx)^{3/2}(ac-bcx)^{3/2}} dx}{3a^2c} \\ &= \frac{x}{3a^2c(a+bx)^{3/2}(ac-bcx)^{3/2}} + \frac{2x}{3a^4c^2\sqrt{a+bx}\sqrt{ac-bcx}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 46, normalized size = 0.69

$$\frac{3a^2x - 2b^2x^3}{3a^4c(a + bx)^{3/2}(c(a - bx))^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(a*c - b*c*x)^(5/2)),x]

[Out] (3*a^2*x - 2*b^2*x^3)/(3*a^4*c*(c*(a - b*x))^(3/2)*(a + b*x)^(3/2))

fricas [A] time = 0.45, size = 72, normalized size = 1.07

$$\frac{(2b^2x^3 - 3a^2x)\sqrt{-bcx + ac}\sqrt{bx + a}}{3(a^4b^4c^3x^4 - 2a^6b^2c^3x^2 + a^8c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(-b*c*x+a*c)^(5/2),x, algorithm="fricas")

[Out] -1/3*(2*b^2*x^3 - 3*a^2*x)*sqrt(-b*c*x + a*c)*sqrt(b*x + a)/(a^4*b^4*c^3*x^4 - 2*a^6*b^2*c^3*x^2 + a^8*c^3)

giac [B] time = 2.38, size = 251, normalized size = 3.75

$$\frac{\sqrt{-bcx + ac} \left(\frac{9|c|}{a^3bc} + \frac{4(bc x - ac)|c|}{a^4bc^2} \right)}{12(2ac^2 + (bcx - ac)c)^{\frac{3}{2}}} + \frac{16a^2\sqrt{-c}c^4 - 18a(\sqrt{-bcx + ac}\sqrt{-c} - \sqrt{2ac^2 + (bcx - ac)c})^2\sqrt{-c}c^2 + 3(\sqrt{-bcx + ac}\sqrt{-c} - \sqrt{2ac^2 + (bcx - ac)c})^2}{3(2ac^2 - (\sqrt{-bcx + ac}\sqrt{-c} - \sqrt{2ac^2 + (bcx - ac)c})^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(-b*c*x+a*c)^(5/2),x, algorithm="giac")

[Out] -1/12*sqrt(-b*c*x + a*c)*(9*abs(c)/(a^3*b*c) + 4*(b*c*x - a*c)*abs(c)/(a^4*b*c^2))/(2*a*c^2 + (b*c*x - a*c)*c)^(3/2) + 1/3*(16*a^2*sqrt(-c)*c^4 - 18*a*(sqrt(-b*c*x + a*c)*sqrt(-c) - sqrt(2*a*c^2 + (b*c*x - a*c)*c))^2*sqrt(-c)*c^2 + 3*(sqrt(-b*c*x + a*c)*sqrt(-c) - sqrt(2*a*c^2 + (b*c*x - a*c)*c))^4*sqrt(-c))/((2*a*c^2 - (sqrt(-b*c*x + a*c)*sqrt(-c) - sqrt(2*a*c^2 + (b*c*x - a*c)*c))^2)^3*a^3*b*abs(c))

maple [A] time = 0.00, size = 45, normalized size = 0.67

$$\frac{(-bx + a)(-2b^2x^2 + 3a^2)x}{3(bx + a)^{\frac{3}{2}}(-bcx + ac)^{\frac{5}{2}}a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(5/2)/(-b*c*x+a*c)^(5/2),x)`

[Out] $1/3*(-b*x+a)*x*(-2*b^2*x^2+3*a^2)/(b*x+a)^(3/2)/a^4/(-b*c*x+a*c)^(5/2)$

maxima [A] time = 1.43, size = 53, normalized size = 0.79

$$\frac{x}{3(-b^2cx^2 + a^2c)^{\frac{3}{2}}a^2c} + \frac{2x}{3\sqrt{-b^2cx^2 + a^2c}a^4c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/2)/(-b*c*x+a*c)^(5/2),x, algorithm="maxima")`

[Out] $1/3*x/((-b^2*c*x^2 + a^2*c)^(3/2)*a^2*c) + 2/3*x/(sqrt(-b^2*c*x^2 + a^2*c)*a^4*c^2)$

mupad [B] time = 0.58, size = 80, normalized size = 1.19

$$\frac{3a^2x\sqrt{ac-bcx} - 2b^2x^3\sqrt{ac-bcx}}{(ac-bcx)^2(3a^4(ac-bcx) - 6a^5c)\sqrt{a+bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a*c - b*c*x)^(5/2)*(a + b*x)^(5/2)),x)`

[Out] $-(3*a^2*x*(a*c - b*c*x)^(1/2) - 2*b^2*x^3*(a*c - b*c*x)^(1/2))/((a*c - b*c*x)^2*(3*a^4*(a*c - b*c*x) - 6*a^5*c)*(a + b*x)^(1/2))$

sympy [C] time = 15.85, size = 94, normalized size = 1.40

$$\frac{iG_{6,6}^{5,3} \left(\begin{matrix} \frac{5}{4}, \frac{7}{4}, 1 & \frac{1}{2}, \frac{5}{2}, 3 \\ \frac{5}{4}, \frac{7}{4}, 2, \frac{5}{2}, 3 & 0 \end{matrix} \middle| \frac{a^2}{b^2x^2} \right)}{3\pi^{\frac{3}{2}}a^4bc^{\frac{5}{2}}} + \frac{G_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, 0, \frac{1}{2}, \frac{3}{4}, \frac{5}{4}, 1 \\ \frac{3}{4}, \frac{5}{4} & -\frac{1}{2}, 0, 2, 0 \end{matrix} \middle| \frac{a^2e^{-2i\pi}}{b^2x^2} \right)}{3\pi^{\frac{3}{2}}a^4bc^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/2)/(-b*c*x+a*c)**(5/2),x)`

[Out] $I*\text{meijerg}(((5/4, 7/4, 1), (1/2, 5/2, 3)), ((5/4, 7/4, 2, 5/2, 3), (0,)), a**2/(b**2*x**2))/(3*pi**(3/2)*a**4*b*c**(5/2)) + \text{meijerg}((-1/2, 0, 1/2, 3/4, 5/4, 1), ()), ((3/4, 5/4), (-1/2, 0, 2, 0)), a**2*\exp_polar(-2*I*pi)/(b**2*x**2))/(3*pi**(3/2)*a**4*b*c**(5/2))$

$$3.1151 \quad \int \frac{1}{(a+bx)^{7/2}(ac-bcx)^{7/2}} dx$$

Optimal. Leaf size=100

$$\frac{8x}{15a^6c^3\sqrt{a+bx}\sqrt{ac-bcx}} + \frac{4x}{15a^4c^2(a+bx)^{3/2}(ac-bcx)^{3/2}} + \frac{x}{5a^2c(a+bx)^{5/2}(ac-bcx)^{5/2}}$$

[Out] $1/5*x/a^2/c/(b*x+a)^{(5/2)/(-b*c*x+a*c)^{(5/2)}+4/15*x/a^4/c^2/(b*x+a)^{(3/2)/(-b*c*x+a*c)^{(3/2)}+8/15*x/a^6/c^3/(b*x+a)^{(1/2)/(-b*c*x+a*c)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.087$, Rules used = {40, 39}

$$\frac{8x}{15a^6c^3\sqrt{a+bx}\sqrt{ac-bcx}} + \frac{4x}{15a^4c^2(a+bx)^{3/2}(ac-bcx)^{3/2}} + \frac{x}{5a^2c(a+bx)^{5/2}(ac-bcx)^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/2)*(a*c - b*c*x)^(7/2)), x]

[Out] $x/(5*a^2*c*(a + b*x)^{(5/2)*(a*c - b*c*x)^{(5/2)}) + (4*x)/(15*a^4*c^2*(a + b*x)^{(3/2)*(a*c - b*c*x)^{(3/2)}) + (8*x)/(15*a^6*c^3*\text{Sqrt}[a + b*x]*\text{Sqrt}[a*c - b*c*x])$

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := -Simp[(x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^{7/2}(ac-bcx)^{7/2}} dx &= \frac{x}{5a^2c(a+bx)^{5/2}(ac-bcx)^{5/2}} + \frac{4 \int \frac{1}{(a+bx)^{5/2}(ac-bcx)^{5/2}} dx}{5a^2c} \\ &= \frac{x}{5a^2c(a+bx)^{5/2}(ac-bcx)^{5/2}} + \frac{4x}{15a^4c^2(a+bx)^{3/2}(ac-bcx)^{3/2}} + \frac{8 \int \frac{1}{(a+bx)^{3/2}(ac-bcx)^{3/2}}}{15a^4c^2} \\ &= \frac{x}{5a^2c(a+bx)^{5/2}(ac-bcx)^{5/2}} + \frac{4x}{15a^4c^2(a+bx)^{3/2}(ac-bcx)^{3/2}} + \frac{8x}{15a^6c^3\sqrt{a+bx}\sqrt{ac-bcx}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 57, normalized size = 0.57

$$\frac{15a^4x - 20a^2b^2x^3 + 8b^4x^5}{15a^6c(a+bx)^{5/2}(c(a-bx))^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/2)*(a*c - b*c*x)^(7/2)), x]

[Out] (15*a^4*x - 20*a^2*b^2*x^3 + 8*b^4*x^5)/(15*a^6*c*(c*(a - b*x))^(5/2)*(a + b*x)^(5/2))

fricas [A] time = 0.46, size = 98, normalized size = 0.98

$$\frac{(8b^4x^5 - 20a^2b^2x^3 + 15a^4x)\sqrt{-bcx+ac}\sqrt{bx+a}}{15(a^6b^6c^4x^6 - 3a^8b^4c^4x^4 + 3a^{10}b^2c^4x^2 - a^{12}c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/2)/(-b*c*x+a*c)^(7/2), x, algorithm="fricas")

[Out] -1/15*(8*b^4*x^5 - 20*a^2*b^2*x^3 + 15*a^4*x)*sqrt(-b*c*x + a*c)*sqrt(b*x + a)/(a^6*b^6*c^4*x^6 - 3*a^8*b^4*c^4*x^4 + 3*a^10*b^2*c^4*x^2 - a^12*c^4)

giac [B] time = 2.57, size = 366, normalized size = 3.66

$$\frac{\sqrt{-bcx+ac} \left((bcx-ac) \left(\frac{275c}{a^5b|c|} + \frac{64(bc x-ac)}{a^6b|c|} \right) + \frac{300c^2}{a^4b|c|} \right)}{240 \left(2ac^2 + (bcx-ac)c \right)^{\frac{5}{2}}} - \frac{1024a^4c^8 - 2200a^3(\sqrt{-bcx+ac}\sqrt{-c} - \sqrt{2ac^2+(bcx-ac)})}{240 \left(2ac^2 + (bcx-ac)c \right)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/2)/(-b*c*x+a*c)^(7/2), x, algorithm="giac")

[Out] $-1/240*\sqrt{-b*c*x + a*c}*((b*c*x - a*c)*(275*c/(a^5*b*abs(c)) + 64*(b*c*x - a*c)/(a^6*b*abs(c))) + 300*c^2/(a^4*b*abs(c)))/(2*a*c^2 + (b*c*x - a*c)*c)^{(5/2)} - 1/60*(1024*a^4*c^8 - 2200*a^3*(\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{(2*a*c^2 + (b*c*x - a*c)*c})^2*c^6 + 1660*a^2*(\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{(2*a*c^2 + (b*c*x - a*c)*c})^4*c^4 - 450*a*(\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{(2*a*c^2 + (b*c*x - a*c)*c})^6*c^2 + 45*(\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{(2*a*c^2 + (b*c*x - a*c)*c})^8)/((2*a*c^2 - (\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{(2*a*c^2 + (b*c*x - a*c)*c})^2)^5*a^5*b*\sqrt{-c}*abs(c))$

maple [A] time = 0.00, size = 56, normalized size = 0.56

$$\frac{(-bx + a)(8b^4x^4 - 20a^2b^2x^2 + 15a^4)x}{15(bx + a)^{\frac{5}{2}}(-bcx + ac)^{\frac{7}{2}}a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(b*x+a)^{(7/2)}/(-b*c*x+a*c)^{(7/2)}, x)$

[Out] $1/15*(-b*x+a)*x*(8*b^4*x^4-20*a^2*b^2*x^2+15*a^4)/(b*x+a)^{(5/2)}/a^6/(-b*c*x+a*c)^{(7/2)}$

maxima [A] time = 1.32, size = 79, normalized size = 0.79

$$\frac{x}{5(-b^2cx^2 + a^2c)^{\frac{5}{2}}a^2c} + \frac{4x}{15(-b^2cx^2 + a^2c)^{\frac{3}{2}}a^4c^2} + \frac{8x}{15\sqrt{-b^2cx^2 + a^2c}a^6c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(b*x+a)^{(7/2)}/(-b*c*x+a*c)^{(7/2)}, x, \text{algorithm}="maxima")$

[Out] $1/5*x/((-b^2*c*x^2 + a^2*c)^{(5/2)}*a^2*c) + 4/15*x/((-b^2*c*x^2 + a^2*c)^{(3/2)}*a^4*c^2) + 8/15*x/(\sqrt{-b^2*c*x^2 + a^2*c}*a^6*c^3)$

mupad [B] time = 0.65, size = 111, normalized size = 1.11

$$\frac{15a^4x\sqrt{ac-bcx} + 8b^4x^5\sqrt{ac-bcx} - 20a^2b^2x^3\sqrt{ac-bcx}}{(ac-bcx)^3(60a^8c - (ac-bcx)(45a^7 + 15bx a^6))\sqrt{a+bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/((a*c - b*c*x)^{(7/2)}*(a + b*x)^{(7/2)}), x)$

[Out] $(15*a^4*x*(a*c - b*c*x)^{(1/2)} + 8*b^4*x^5*(a*c - b*c*x)^{(1/2)} - 20*a^2*b^2*x^3*(a*c - b*c*x)^{(1/2)})/((a*c - b*c*x)^3*(60*a^8*c - (a*c - b*c*x)*(45*a^7 + 15*a^6*b*x))*(a + b*x)^{(1/2)})$

sympy [C] time = 59.50, size = 97, normalized size = 0.97

$$-\frac{2iG_{6,6}^{5,3}\left(\begin{matrix} \frac{7}{4}, \frac{9}{4}, 1 & \frac{1}{2}, \frac{7}{2}, 4 \\ \frac{7}{4}, \frac{9}{4}, 3, \frac{7}{2}, 4 & 0 \end{matrix} \middle| \frac{a^2}{b^2x^2}\right)}{15\pi^{\frac{3}{2}}a^6bc^{\frac{7}{2}}} + \frac{2G_{6,6}^{2,6}\left(\begin{matrix} -\frac{1}{2}, 0, \frac{1}{2}, \frac{5}{4}, \frac{7}{4}, 1 \\ \frac{5}{4}, \frac{7}{4} & -\frac{1}{2}, 0, 3, 0 \end{matrix} \middle| \frac{a^2e^{-2i\pi}}{b^2x^2}\right)}{15\pi^{\frac{3}{2}}a^6bc^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/2)/(-b*c*x+a*c)**(7/2), x)

[Out] -2*I*meijerg(((7/4, 9/4, 1), (1/2, 7/2, 4)), ((7/4, 9/4, 3, 7/2, 4), (0,)), a**2/(b**2*x**2))/(15*pi**(3/2)*a**6*b*c**(7/2)) + 2*meijerg((-1/2, 0, 1/2, 5/4, 7/4, 1), ()), ((5/4, 7/4), (-1/2, 0, 3, 0)), a**2*exp_polar(-2*I*pi)/(b**2*x**2))/(15*pi**(3/2)*a**6*b*c**(7/2))

$$3.1152 \quad \int \frac{1}{(a+bx)^{9/2}(ac-bcx)^{9/2}} dx$$

Optimal. Leaf size=133

$$\frac{16x}{35a^8c^4\sqrt{a+bx}\sqrt{ac-bcx}} + \frac{8x}{35a^6c^3(a+bx)^{3/2}(ac-bcx)^{3/2}} + \frac{6x}{35a^4c^2(a+bx)^{5/2}(ac-bcx)^{5/2}} + \frac{x}{7a^2c(a+bx)^{7/2}(ac-bcx)^{7/2}}$$

[Out] 1/7*x/a^2/c/(b*x+a)^(7/2)/(-b*c*x+a*c)^(7/2)+6/35*x/a^4/c^2/(b*x+a)^(5/2)/(-b*c*x+a*c)^(5/2)+8/35*x/a^6/c^3/(b*x+a)^(3/2)/(-b*c*x+a*c)^(3/2)+16/35*x/a^8/c^4/(b*x+a)^(1/2)/(-b*c*x+a*c)^(1/2)

Rubi [A] time = 0.03, antiderivative size = 133, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.087$, Rules used = {40, 39}

$$\frac{16x}{35a^8c^4\sqrt{a+bx}\sqrt{ac-bcx}} + \frac{8x}{35a^6c^3(a+bx)^{3/2}(ac-bcx)^{3/2}} + \frac{6x}{35a^4c^2(a+bx)^{5/2}(ac-bcx)^{5/2}} + \frac{x}{7a^2c(a+bx)^{7/2}(ac-bcx)^{7/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(9/2)*(a*c - b*c*x)^(9/2)), x]

[Out] x/(7*a^2*c*(a + b*x)^(7/2)*(a*c - b*c*x)^(7/2)) + (6*x)/(35*a^4*c^2*(a + b*x)^(5/2)*(a*c - b*c*x)^(5/2)) + (8*x)/(35*a^6*c^3*(a + b*x)^(3/2)*(a*c - b*c*x)^(3/2)) + (16*x)/(35*a^8*c^4*Sqrt[a + b*x]*Sqrt[a*c - b*c*x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := -Simp[(x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{9/2}(ac-bcx)^{9/2}} dx &= \frac{x}{7a^2c(a+bx)^{7/2}(ac-bcx)^{7/2}} + \frac{6 \int \frac{1}{(a+bx)^{7/2}(ac-bcx)^{7/2}} dx}{7a^2c} \\
&= \frac{x}{7a^2c(a+bx)^{7/2}(ac-bcx)^{7/2}} + \frac{6x}{35a^4c^2(a+bx)^{5/2}(ac-bcx)^{5/2}} + \frac{24 \int \frac{1}{(a+bx)^{5/2}(ac-bcx)^{5/2}} dx}{35a^4c^2} \\
&= \frac{x}{7a^2c(a+bx)^{7/2}(ac-bcx)^{7/2}} + \frac{6x}{35a^4c^2(a+bx)^{5/2}(ac-bcx)^{5/2}} + \frac{8x}{35a^6c^3(a+bx)^{3/2}} \\
&= \frac{x}{7a^2c(a+bx)^{7/2}(ac-bcx)^{7/2}} + \frac{6x}{35a^4c^2(a+bx)^{5/2}(ac-bcx)^{5/2}} + \frac{8x}{35a^6c^3(a+bx)^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 76, normalized size = 0.57

$$\frac{x(35a^6 - 70a^4b^2x^2 + 56a^2b^4x^4 - 16b^6x^6)\sqrt{c(a-bx)}}{35a^8c^5(a-bx)^4(a+bx)^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(9/2)*(a*c - b*c*x)^(9/2)), x]

[Out] (x*Sqrt[c*(a - b*x)]*(35*a^6 - 70*a^4*b^2*x^2 + 56*a^2*b^4*x^4 - 16*b^6*x^6))/((35*a^8*c^5*(a - b*x)^4*(a + b*x)^(7/2))

fricas [A] time = 0.52, size = 122, normalized size = 0.92

$$\frac{(16b^6x^7 - 56a^2b^4x^5 + 70a^4b^2x^3 - 35a^6x)\sqrt{-bcx+ac}\sqrt{bx+a}}{35(a^8b^8c^5x^8 - 4a^{10}b^6c^5x^6 + 6a^{12}b^4c^5x^4 - 4a^{14}b^2c^5x^2 + a^{16}c^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(-b*c*x+a*c)^(9/2), x, algorithm="fricas")

[Out] -1/35*(16*b^6*x^7 - 56*a^2*b^4*x^5 + 70*a^4*b^2*x^3 - 35*a^6*x)*sqrt(-b*c*x + a*c)*sqrt(b*x + a)/(a^8*b^8*c^5*x^8 - 4*a^10*b^6*c^5*x^6 + 6*a^12*b^4*c^5*x^4 - 4*a^14*b^2*c^5*x^2 + a^16*c^5)

giac [B] time = 3.30, size = 487, normalized size = 3.66

$$\frac{\sqrt{-bcx+ac}\left((bcx-ac)\left((bcx-ac)\left(\frac{1617|c|}{a^7bc} + \frac{256(bc x-ac)|c|}{a^8bc^2}\right) + \frac{3430|c|}{a^6b}\right) + \frac{2450c|c|}{a^5b}\right)}{1120\left(2ac^2 + (bcx-ac)c\right)^{\frac{7}{2}}} 16384a^6c^{12} - 51744a^5\left(\sqrt{-bcx+ac}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(-b*c*x+a*c)^(9/2),x, algorithm="giac")

[Out]
$$-1/1120*\sqrt{-b*c*x + a*c}*((b*c*x - a*c)*((b*c*x - a*c)*(1617*abs(c)/(a^7*b*c) + 256*(b*c*x - a*c)*abs(c)/(a^8*b*c^2)) + 3430*abs(c)/(a^6*b)) + 2450*c*abs(c)/(a^5*b))/(2*a*c^2 + (b*c*x - a*c)*c)^{(7/2)} - 1/280*(16384*a^6*c^{12} - 51744*a^5*(\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{2*a*c^2 + (b*c*x - a*c)*c})^2*c^{10} + 66416*a^4*(\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{2*a*c^2 + (b*c*x - a*c)*c})^4*c^8 - 43120*a^3*(\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{2*a*c^2 + (b*c*x - a*c)*c})^6*c^6 + 14280*a^2*(\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{2*a*c^2 + (b*c*x - a*c)*c})^8*c^4 - 2450*a*(\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{2*a*c^2 + (b*c*x - a*c)*c})^{10}*c^2 + 175*(\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{2*a*c^2 + (b*c*x - a*c)*c})^{12})/((2*a*c^2 - (\sqrt{-b*c*x + a*c}*\sqrt{-c} - \sqrt{2*a*c^2 + (b*c*x - a*c)*c})^2)^7*a^7*b*\sqrt{-c}*c*abs(c))$$

maple [A] time = 0.00, size = 67, normalized size = 0.50

$$\frac{(-bx + a)(-16b^6x^6 + 56b^4x^4a^2 - 70b^2x^2a^4 + 35a^6)x}{35(bx + a)^{\frac{7}{2}}(-bcx + ac)^{\frac{9}{2}}a^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(9/2)/(-b*c*x+a*c)^(9/2),x)

[Out]
$$1/35*(-b*x+a)*x*(-16*b^6*x^6+56*a^2*b^4*x^4-70*a^4*b^2*x^2+35*a^6)/(b*x+a)^{(7/2)}/a^8/(-b*c*x+a*c)^{(9/2)}$$

maxima [A] time = 1.29, size = 105, normalized size = 0.79

$$\frac{x}{7(-b^2cx^2 + a^2c)^{\frac{7}{2}}a^2c} + \frac{6x}{35(-b^2cx^2 + a^2c)^{\frac{5}{2}}a^4c^2} + \frac{8x}{35(-b^2cx^2 + a^2c)^{\frac{3}{2}}a^6c^3} + \frac{16x}{35\sqrt{-b^2cx^2 + a^2c}a^8c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(-b*c*x+a*c)^(9/2),x, algorithm="maxima")

[Out]
$$1/7*x/((-b^2*c*x^2 + a^2*c)^{(7/2)}*a^2*c) + 6/35*x/((-b^2*c*x^2 + a^2*c)^{(5/2)}*a^4*c^2) + 8/35*x/((-b^2*c*x^2 + a^2*c)^{(3/2)}*a^6*c^3) + 16/35*x/(\sqrt{-b^2*c*x^2 + a^2*c}*a^8*c^4)$$

mupad [B] time = 0.71, size = 170, normalized size = 1.28

$$\frac{35a^6x\sqrt{ac-bcx} - 16b^6x^7\sqrt{ac-bcx} - 70a^4b^2x^3\sqrt{ac-bcx} + 56a^2b^4x^5\sqrt{ac-bcx}}{\left((70a^9(ac-bcx)^5 + 35a^8(ac-bcx)^5(a+bx))(a+bx) + (ac-bcx)^4(140a^{10}(ac-bcx) - 280a^{11}c)\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a*c - b*c*x)^(9/2)*(a + b*x)^(9/2)),x)
```

```
[Out] -(35*a^6*x*(a*c - b*c*x)^(1/2) - 16*b^6*x^7*(a*c - b*c*x)^(1/2) - 70*a^4*b^2*x^3*(a*c - b*c*x)^(1/2) + 56*a^2*b^4*x^5*(a*c - b*c*x)^(1/2))/(((70*a^9*(a*c - b*c*x)^5 + 35*a^8*(a*c - b*c*x)^5*(a + b*x))*(a + b*x) + (a*c - b*c*x)^4*(140*a^10*(a*c - b*c*x) - 280*a^11*c))*(a + b*x)^(1/2))
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(9/2)/(-b*c*x+a*c)**(9/2),x)
```

```
[Out] Timed out
```

3.1153 $\int (3 - 6x)^{5/2} (2 + 4x)^{5/2} dx$

Optimal. Leaf size=100

$$6\sqrt{6}(1-2x)^{5/2}x(2x+1)^{5/2}+15\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(2x+1)^{3/2}+\frac{45}{2}\sqrt{\frac{3}{2}}\sqrt{1-2x}x\sqrt{2x+1}+\frac{45}{4}\sqrt{\frac{3}{2}}\sin^{-1}(2x)$$

[Out] 15/2*(1-2*x)^(3/2)*x*(1+2*x)^(3/2)*6^(1/2)+45/8*arcsin(2*x)*6^(1/2)+6*(1-2*x)^(5/2)*x*(1+2*x)^(5/2)*6^(1/2)+45/4*x*6^(1/2)*(1-2*x)^(1/2)*(1+2*x)^(1/2)

Rubi [A] time = 0.02, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {38, 41, 216}

$$6\sqrt{6}(1-2x)^{5/2}x(2x+1)^{5/2}+15\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(2x+1)^{3/2}+\frac{45}{2}\sqrt{\frac{3}{2}}\sqrt{1-2x}x\sqrt{2x+1}+\frac{45}{4}\sqrt{\frac{3}{2}}\sin^{-1}(2x)$$

Antiderivative was successfully verified.

[In] Int[(3 - 6*x)^(5/2)*(2 + 4*x)^(5/2), x]

[Out] (45*Sqrt[3/2]*Sqrt[1 - 2*x]*x*Sqrt[1 + 2*x])/2 + 15*Sqrt[3/2]*(1 - 2*x)^(3/2)*x*(1 + 2*x)^(3/2) + 6*Sqrt[6]*(1 - 2*x)^(5/2)*x*(1 + 2*x)^(5/2) + (45*Sqrt[3/2]*ArcSin[2*x])/4

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := Simp[(x*(a + b*x)^(m*(c + d*x)^m)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(m - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int (3-6x)^{5/2}(2+4x)^{5/2} dx &= 6\sqrt{6}(1-2x)^{5/2}x(1+2x)^{5/2} + 5 \int (3-6x)^{3/2}(2+4x)^{3/2} dx \\
&= 15\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(1+2x)^{3/2} + 6\sqrt{6}(1-2x)^{5/2}x(1+2x)^{5/2} + \frac{45}{2} \int \sqrt{3-6x} \sqrt{2+4x} dx \\
&= \frac{45}{2} \sqrt{\frac{3}{2}} \sqrt{1-2x} x \sqrt{1+2x} + 15\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(1+2x)^{3/2} + 6\sqrt{6}(1-2x)^{5/2}x(1+2x)^{5/2} \\
&= \frac{45}{2} \sqrt{\frac{3}{2}} \sqrt{1-2x} x \sqrt{1+2x} + 15\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(1+2x)^{3/2} + 6\sqrt{6}(1-2x)^{5/2}x(1+2x)^{5/2} \\
&= \frac{45}{2} \sqrt{\frac{3}{2}} \sqrt{1-2x} x \sqrt{1+2x} + 15\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(1+2x)^{3/2} + 6\sqrt{6}(1-2x)^{5/2}x(1+2x)^{5/2}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 44, normalized size = 0.44

$$\frac{3}{4} \sqrt{\frac{3}{2}} \left(2x\sqrt{1-4x^2} (128x^4 - 104x^2 + 33) + 15 \sin^{-1}(2x) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(3 - 6*x)^(5/2)*(2 + 4*x)^(5/2), x]

[Out] (3*Sqrt[3/2]*(2*x*Sqrt[1 - 4*x^2]*(33 - 104*x^2 + 128*x^4) + 15*ArcSin[2*x]))/4

fricas [A] time = 0.45, size = 65, normalized size = 0.65

$$\frac{3}{4} (128x^5 - 104x^3 + 33x) \sqrt{4x+2} \sqrt{-6x+3} - \frac{45}{8} \sqrt{3} \sqrt{2} \arctan\left(\frac{\sqrt{3} \sqrt{2} \sqrt{4x+2} \sqrt{-6x+3}}{12x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^(5/2)*(4*x+2)^(5/2), x, algorithm="fricas")

[Out] 3/4*(128*x^5 - 104*x^3 + 33*x)*sqrt(4*x + 2)*sqrt(-6*x + 3) - 45/8*sqrt(3)*sqrt(2)*arctan(1/12*sqrt(3)*sqrt(2)*sqrt(4*x + 2)*sqrt(-6*x + 3)/x)

giac [B] time = 1.24, size = 227, normalized size = 2.27

$$\frac{3}{40} \sqrt{3} \sqrt{2} \left(((2((8(5x-13)(2x+1)+321)(2x+1)-451)(2x+1)+745)(2x+1)-405)\sqrt{2x+1} \sqrt{-2x+1} + \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^(5/2)*(4*x+2)^(5/2),x, algorithm="giac")

[Out] 3/40*sqrt(3)*sqrt(2)*(((2*((8*(5*x - 13)*(2*x + 1) + 321)*(2*x + 1) - 451)*(2*x + 1) + 745)*(2*x + 1) - 405)*sqrt(2*x + 1)*sqrt(-2*x + 1) + 2*((2*(3*(8*x - 17)*(2*x + 1) + 133)*(2*x + 1) - 295)*(2*x + 1) + 195)*sqrt(2*x + 1)*sqrt(-2*x + 1) - 20*((4*(3*x - 5)*(2*x + 1) + 43)*(2*x + 1) - 39)*sqrt(2*x + 1)*sqrt(-2*x + 1) - 80*((4*x - 5)*(2*x + 1) + 9)*sqrt(2*x + 1)*sqrt(-2*x + 1) + 240*sqrt(2*x + 1)*(x - 1)*sqrt(-2*x + 1) + 240*sqrt(2*x + 1)*sqrt(-2*x + 1) + 150*arcsin(1/2*sqrt(2)*sqrt(2*x + 1)))

maple [A] time = 0.01, size = 134, normalized size = 1.34

$$\frac{45\sqrt{(4x+2)(-6x+3)}\sqrt{6}\arcsin(2x)}{8\sqrt{4x+2}\sqrt{-6x+3}} + \frac{(-6x+3)^{\frac{5}{2}}(4x+2)^{\frac{7}{2}}}{24} + \frac{(-6x+3)^{\frac{3}{2}}(4x+2)^{\frac{7}{2}}}{8} + \frac{9\sqrt{-6x+3}(4x+2)^{\frac{7}{2}}}{32}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((3-6*x)^(5/2)*(2+4*x)^(5/2),x)

[Out] 1/24*(3-6*x)^(5/2)*(2+4*x)^(7/2)+1/8*(3-6*x)^(3/2)*(2+4*x)^(7/2)+9/32*(3-6*x)^(1/2)*(2+4*x)^(7/2)-3/16*(2+4*x)^(5/2)*(3-6*x)^(1/2)-15/16*(2+4*x)^(3/2)*(3-6*x)^(1/2)-45/8*(3-6*x)^(1/2)*(2+4*x)^(1/2)+45/8*((2+4*x)*(3-6*x))^(1/2)/(2+4*x)^(1/2)/(3-6*x)^(1/2)*6^(1/2)*arcsin(2*x)

maxima [A] time = 2.86, size = 46, normalized size = 0.46

$$\frac{1}{6}(-24x^2+6)^{\frac{5}{2}}x + \frac{5}{4}(-24x^2+6)^{\frac{3}{2}}x + \frac{45}{4}\sqrt{-24x^2+6}x + \frac{45}{8}\sqrt{6}\arcsin(2x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^(5/2)*(4*x+2)^(5/2),x, algorithm="maxima")

[Out] 1/6*(-24*x^2 + 6)^(5/2)*x + 5/4*(-24*x^2 + 6)^(3/2)*x + 45/4*sqrt(-24*x^2 + 6)*x + 45/8*sqrt(6)*arcsin(2*x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (4x+2)^{5/2}(3-6x)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((4*x + 2)^(5/2)*(3 - 6*x)^(5/2),x)

[Out] int((4*x + 2)^(5/2)*(3 - 6*x)^(5/2), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)**(5/2)*(4*x+2)**(5/2),x)

[Out] Timed out

3.1154 $\int (3 - 6x)^{3/2} (2 + 4x)^{3/2} dx$

Optimal. Leaf size=74

$$3\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(2x+1)^{3/2} + \frac{9}{2}\sqrt{\frac{3}{2}}\sqrt{1-2x}x\sqrt{2x+1} + \frac{9}{4}\sqrt{\frac{3}{2}}\sin^{-1}(2x)$$

[Out] $3/2*(1-2*x)^{(3/2)}*x*(1+2*x)^{(3/2)}*6^{(1/2)}+9/8*\arcsin(2*x)*6^{(1/2)}+9/4*x*6^{(1/2)}*(1-2*x)^{(1/2)}*(1+2*x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {38, 41, 216}

$$3\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(2x+1)^{3/2} + \frac{9}{2}\sqrt{\frac{3}{2}}\sqrt{1-2x}x\sqrt{2x+1} + \frac{9}{4}\sqrt{\frac{3}{2}}\sin^{-1}(2x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(3 - 6*x)^{(3/2)}*(2 + 4*x)^{(3/2)}, x]$

[Out] $(9*\text{Sqrt}[3/2]*\text{Sqrt}[1 - 2*x]*x*\text{Sqrt}[1 + 2*x])/2 + 3*\text{Sqrt}[3/2]*(1 - 2*x)^{(3/2)}*x*(1 + 2*x)^{(3/2)} + (9*\text{Sqrt}[3/2]*\text{ArcSin}[2*x])/4$

Rule 38

$\text{Int}[(a_ + (b_.)*(x_))^{(m_)}*((c_ + (d_.)*(x_))^{(m_)}), x_Symbol] \rightarrow \text{Simp}[(x*(a + b*x)^m*(c + d*x)^m]/(2*m + 1), x] + \text{Dist}[(2*a*c*m)/(2*m + 1), \text{Int}[(a + b*x)^{(m - 1)}*(c + d*x)^{(m - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

$\text{Int}[(a_ + (b_.)*(x_))^{(m_)}*((c_ + (d_.)*(x_))^{(m_)}), x_Symbol] \rightarrow \text{Int}[(a*c + b*d*x^2)^m, x] /;$ FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 216

$\text{Int}[1/\text{Sqrt}[(a_ + (b_.)*(x_)^2], x_Symbol] \rightarrow \text{Simp}[\text{ArcSin}[\text{Rt}[-b, 2]*x]/\text{Sqrt}[a]]/\text{Rt}[-b, 2], x] /;$ FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int (3-6x)^{3/2}(2+4x)^{3/2} dx &= 3\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(1+2x)^{3/2} + \frac{9}{2} \int \sqrt{3-6x} \sqrt{2+4x} dx \\
&= \frac{9}{2}\sqrt{\frac{3}{2}} \sqrt{1-2x} x \sqrt{1+2x} + 3\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(1+2x)^{3/2} + \frac{27}{2} \int \frac{1}{\sqrt{3-6x} \sqrt{2+4x}} dx \\
&= \frac{9}{2}\sqrt{\frac{3}{2}} \sqrt{1-2x} x \sqrt{1+2x} + 3\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(1+2x)^{3/2} + \frac{27}{2} \int \frac{1}{\sqrt{6-24x^2}} dx \\
&= \frac{9}{2}\sqrt{\frac{3}{2}} \sqrt{1-2x} x \sqrt{1+2x} + 3\sqrt{\frac{3}{2}}(1-2x)^{3/2}x(1+2x)^{3/2} + \frac{9}{4}\sqrt{\frac{3}{2}} \sin^{-1}(2x)
\end{aligned}$$

Mathematica [A] time = 0.04, size = 39, normalized size = 0.53

$$\frac{3}{4}\sqrt{\frac{3}{2}} \left(2x\sqrt{1-4x^2} (5-8x^2) + 3\sin^{-1}(2x) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(3 - 6*x)^(3/2)*(2 + 4*x)^(3/2), x]

[Out] (3*Sqrt[3/2]*(2*x*(5 - 8*x^2)*Sqrt[1 - 4*x^2] + 3*ArcSin[2*x]))/4

fricas [A] time = 0.43, size = 60, normalized size = 0.81

$$-\frac{3}{4}(8x^3 - 5x)\sqrt{4x+2}\sqrt{-6x+3} - \frac{9}{8}\sqrt{3}\sqrt{2} \arctan\left(\frac{\sqrt{3}\sqrt{2}\sqrt{4x+2}\sqrt{-6x+3}}{12x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^(3/2)*(4*x+2)^(3/2), x, algorithm="fricas")

[Out] -3/4*(8*x^3 - 5*x)*sqrt(4*x + 2)*sqrt(-6*x + 3) - 9/8*sqrt(3)*sqrt(2)*arctan(1/12*sqrt(3)*sqrt(2)*sqrt(4*x + 2)*sqrt(-6*x + 3)/x)

giac [B] time = 0.98, size = 125, normalized size = 1.69

$$-\frac{1}{8}\sqrt{3}\sqrt{2}\left(\left((4(3x-5)(2x+1)+43)(2x+1)-39\right)\sqrt{2x+1}\sqrt{-2x+1}+4\left((4x-5)(2x+1)+9\right)\sqrt{2x+1}\sqrt{-2x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^(3/2)*(4*x+2)^(3/2), x, algorithm="giac")

[Out] $-1/8*\sqrt{3}*\sqrt{2}*(((4*(3*x - 5)*(2*x + 1) + 43)*(2*x + 1) - 39)*\sqrt{2*x + 1}*\sqrt{-2*x + 1} + 4*((4*x - 5)*(2*x + 1) + 9)*\sqrt{2*x + 1}*\sqrt{-2*x + 1} - 24*\sqrt{2*x + 1}*(x - 1)*\sqrt{-2*x + 1} - 24*\sqrt{2*x + 1}*\sqrt{-2*x + 1} - 18*\arcsin(1/2*\sqrt{2}*\sqrt{2*x + 1})))$

maple [B] time = 0.00, size = 102, normalized size = 1.38

$$\frac{9\sqrt{(4x+2)(-6x+3)}\sqrt{6}\arcsin(2x)}{8\sqrt{4x+2}\sqrt{-6x+3}} + \frac{(-6x+3)^{\frac{3}{2}}(4x+2)^{\frac{5}{2}}}{16} + \frac{3(4x+2)^{\frac{5}{2}}\sqrt{-6x+3}}{16} - \frac{3(4x+2)^{\frac{3}{2}}\sqrt{-6x+3}}{16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-6*x+3)^(3/2)*(4*x+2)^(3/2),x)`

[Out] $1/16*(-6*x+3)^{(3/2)}*(4*x+2)^{(5/2)}+3/16*(4*x+2)^{(5/2)}*(-6*x+3)^{(1/2)}-3/16*(4*x+2)^{(3/2)}*(-6*x+3)^{(1/2)}-9/8*(-6*x+3)^{(1/2)}*(4*x+2)^{(1/2)}+9/8*((4*x+2)*(-6*x+3))^{(1/2)}/(4*x+2)^{(1/2)}/(-6*x+3)^{(1/2)}*6^{(1/2)}*\arcsin(2*x)$

maxima [A] time = 2.86, size = 34, normalized size = 0.46

$$\frac{1}{4}(-24x^2 + 6)^{\frac{3}{2}}x + \frac{9}{4}\sqrt{-24x^2 + 6}x + \frac{9}{8}\sqrt{6}\arcsin(2x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((3-6*x)^(3/2)*(4*x+2)^(3/2),x, algorithm="maxima")`

[Out] $1/4*(-24*x^2 + 6)^{(3/2)}*x + 9/4*\sqrt{-24*x^2 + 6}*x + 9/8*\sqrt{6}*\arcsin(2*x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (4x + 2)^{3/2} (3 - 6x)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((4*x + 2)^(3/2)*(3 - 6*x)^(3/2),x)`

[Out] `int((4*x + 2)^(3/2)*(3 - 6*x)^(3/2), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((3-6*x)**(3/2)*(4*x+2)**(3/2),x)`

[Out] Timed out

3.1155 $\int \sqrt{3-6x} \sqrt{2+4x} dx$

Optimal. Leaf size=43

$$\sqrt{\frac{3}{2}} \sqrt{1-2x} \sqrt{2x+1} x + \frac{1}{2} \sqrt{\frac{3}{2}} \sin^{-1}(2x)$$

[Out] $1/4*\arcsin(2*x)*6^{(1/2)}+1/2*x*6^{(1/2)}*(1-2*x)^{(1/2)}*(1+2*x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {38, 41, 216}

$$\sqrt{\frac{3}{2}} \sqrt{1-2x} \sqrt{2x+1} x + \frac{1}{2} \sqrt{\frac{3}{2}} \sin^{-1}(2x)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[3 - 6*x]*Sqrt[2 + 4*x], x]

[Out] Sqrt[3/2]*Sqrt[1 - 2*x]*x*Sqrt[1 + 2*x] + (Sqrt[3/2]*ArcSin[2*x])/2

Rule 38

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := Simp[(x*(a + b*x)^(m*(c + d*x)^m)/(2*m + 1), x] + Dist[(2*a*c*m)/(2*m + 1), Int[(a + b*x)^(m - 1)*(c + d*x)^(m - 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && IGtQ[m + 1/2, 0]

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
\int \sqrt{3-6x} \sqrt{2+4x} \, dx &= \sqrt{\frac{3}{2}} \sqrt{1-2x} x \sqrt{1+2x} + 3 \int \frac{1}{\sqrt{3-6x} \sqrt{2+4x}} \, dx \\
&= \sqrt{\frac{3}{2}} \sqrt{1-2x} x \sqrt{1+2x} + 3 \int \frac{1}{\sqrt{6-24x^2}} \, dx \\
&= \sqrt{\frac{3}{2}} \sqrt{1-2x} x \sqrt{1+2x} + \frac{1}{2} \sqrt{\frac{3}{2}} \sin^{-1}(2x)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 0.70

$$\frac{1}{2} \sqrt{\frac{3}{2}} \left(2\sqrt{1-4x^2} x + \sin^{-1}(2x) \right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[3 - 6*x]*Sqrt[2 + 4*x], x]

[Out] (Sqrt[3/2]*(2*x*Sqrt[1 - 4*x^2] + ArcSin[2*x]))/2

fricas [A] time = 0.44, size = 52, normalized size = 1.21

$$\frac{1}{2} \sqrt{4x+2} x \sqrt{-6x+3} - \frac{1}{4} \sqrt{3} \sqrt{2} \arctan\left(\frac{\sqrt{3} \sqrt{2} \sqrt{4x+2} \sqrt{-6x+3}}{12x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^(1/2)*(4*x+2)^(1/2), x, algorithm="fricas")

[Out] 1/2*sqrt(4*x + 2)*x*sqrt(-6*x + 3) - 1/4*sqrt(3)*sqrt(2)*arctan(1/12*sqrt(3)*sqrt(2)*sqrt(4*x + 2)*sqrt(-6*x + 3)/x)

giac [A] time = 1.07, size = 55, normalized size = 1.28

$$\frac{1}{2} \sqrt{3} \sqrt{2} \left(\sqrt{2x+1} (x-1) \sqrt{-2x+1} + \sqrt{2x+1} \sqrt{-2x+1} + \arcsin\left(\frac{1}{2} \sqrt{2} \sqrt{2x+1}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^(1/2)*(4*x+2)^(1/2), x, algorithm="giac")

[Out] 1/2*sqrt(3)*sqrt(2)*(sqrt(2*x + 1)*(x - 1)*sqrt(-2*x + 1) + sqrt(2*x + 1)*sqrt(-2*x + 1) + arcsin(1/2*sqrt(2)*sqrt(2*x + 1)))

maple [B] time = 0.00, size = 70, normalized size = 1.63

$$\frac{\sqrt{(4x+2)(-6x+3)} \sqrt{6} \arcsin(2x)}{4\sqrt{4x+2} \sqrt{-6x+3}} - \frac{\sqrt{4x+2} (-6x+3)^{\frac{3}{2}}}{12} + \frac{\sqrt{-6x+3} \sqrt{4x+2}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-6*x+3)^(1/2)*(4*x+2)^(1/2),x)

[Out] -1/12*(4*x+2)^(1/2)*(-6*x+3)^(3/2)+1/4*(-6*x+3)^(1/2)*(4*x+2)^(1/2)+1/4*((4*x+2)*(-6*x+3))^(1/2)/(4*x+2)^(1/2)/(-6*x+3)^(1/2)*6^(1/2)*arcsin(2*x)

maxima [A] time = 3.07, size = 22, normalized size = 0.51

$$\frac{1}{2} \sqrt{-24x^2 + 6x} + \frac{1}{4} \sqrt{6} \arcsin(2x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^(1/2)*(4*x+2)^(1/2),x, algorithm="maxima")

[Out] 1/2*sqrt(-24*x^2 + 6)*x + 1/4*sqrt(6)*arcsin(2*x)

mupad [B] time = 0.26, size = 44, normalized size = 1.02

$$\frac{x \sqrt{4x+2} \sqrt{3-6x}}{2} - \frac{\sqrt{6} \ln\left(x - \frac{\sqrt{1-2x} \sqrt{2x+1} \text{1i}}{2}\right) \text{1i}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((4*x + 2)^(1/2)*(3 - 6*x)^(1/2),x)

[Out] (x*(4*x + 2)^(1/2)*(3 - 6*x)^(1/2))/2 - (6^(1/2)*log(x - ((1 - 2*x)^(1/2)*(2*x + 1)^(1/2)*1i)/2)*1i)/4

sympy [B] time = 4.74, size = 187, normalized size = 4.35

$$\left\{ \begin{array}{l} -\frac{\sqrt{6} i \operatorname{acosh}\left(\sqrt{x+\frac{1}{2}}\right)}{2} + \frac{\sqrt{6} i \left(x+\frac{1}{2}\right)^{\frac{5}{2}}}{\sqrt{x-\frac{1}{2}}} - \frac{3\sqrt{6} i \left(x+\frac{1}{2}\right)^{\frac{3}{2}}}{2\sqrt{x-\frac{1}{2}}} + \frac{\sqrt{6} i \sqrt{x+\frac{1}{2}}}{2\sqrt{x-\frac{1}{2}}} \quad \text{for } \left|x + \frac{1}{2}\right| > 1 \\ \frac{\sqrt{6} \operatorname{asin}\left(\sqrt{x+\frac{1}{2}}\right)}{2} - \frac{\sqrt{6} \left(x+\frac{1}{2}\right)^{\frac{5}{2}}}{\sqrt{\frac{1}{2}-x}} + \frac{3\sqrt{6} \left(x+\frac{1}{2}\right)^{\frac{3}{2}}}{2\sqrt{\frac{1}{2}-x}} - \frac{\sqrt{6} \sqrt{x+\frac{1}{2}}}{2\sqrt{\frac{1}{2}-x}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.


```
[In] integrate((3-6*x)**(1/2)*(4*x+2)**(1/2),x)
```

```
[Out] Piecewise((-sqrt(6)*I*acosh(sqrt(x + 1/2))/2 + sqrt(6)*I*(x + 1/2)**(5/2)/s  
qrt(x - 1/2) - 3*sqrt(6)*I*(x + 1/2)**(3/2)/(2*sqrt(x - 1/2)) + sqrt(6)*I*s  
qrt(x + 1/2)/(2*sqrt(x - 1/2)), Abs(x + 1/2) > 1), (sqrt(6)*asin(sqrt(x + 1  
/2))/2 - sqrt(6)*(x + 1/2)**(5/2)/sqrt(1/2 - x) + 3*sqrt(6)*(x + 1/2)**(3/2  
)/(2*sqrt(1/2 - x)) - sqrt(6)*sqrt(x + 1/2)/(2*sqrt(1/2 - x)), True))
```

$$3.1156 \quad \int \frac{1}{\sqrt{3-6x} \sqrt{2+4x}} dx$$

Optimal. Leaf size=13

$$\frac{\sin^{-1}(2x)}{2\sqrt{6}}$$

[Out] 1/12*arcsin(2*x)*6^(1/2)

Rubi [A] time = 0.00, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {41, 216}

$$\frac{\sin^{-1}(2x)}{2\sqrt{6}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[3 - 6*x]*Sqrt[2 + 4*x]),x]

[Out] ArcSin[2*x]/(2*Sqrt[6])

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] :> Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{3-6x} \sqrt{2+4x}} dx &= \int \frac{1}{\sqrt{6-24x^2}} dx \\ &= \frac{\sin^{-1}(2x)}{2\sqrt{6}} \end{aligned}$$

Mathematica [A] time = 0.02, size = 13, normalized size = 1.00

$$\frac{\sin^{-1}(2x)}{2\sqrt{6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[3 - 6*x]*Sqrt[2 + 4*x]),x]

[Out] ArcSin[2*x]/(2*Sqrt[6])

fricas [B] time = 0.44, size = 28, normalized size = 2.15

$$-\frac{1}{12} \sqrt{6} \arctan\left(\frac{\sqrt{6} \sqrt{4x+2} \sqrt{-6x+3}}{12x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-6*x)^(1/2)/(4*x+2)^(1/2),x, algorithm="fricas")

[Out] -1/12*sqrt(6)*arctan(1/12*sqrt(6)*sqrt(4*x + 2)*sqrt(-6*x + 3)/x)

giac [A] time = 0.88, size = 15, normalized size = 1.15

$$\frac{1}{6} \sqrt{6} \arcsin\left(\frac{1}{2} \sqrt{4x+2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-6*x)^(1/2)/(4*x+2)^(1/2),x, algorithm="giac")

[Out] 1/6*sqrt(6)*arcsin(1/2*sqrt(4*x + 2))

maple [B] time = 0.00, size = 37, normalized size = 2.85

$$\frac{\sqrt{(4x+2)(-6x+3)} \sqrt{6} \arcsin(2x)}{12\sqrt{4x+2} \sqrt{-6x+3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-6*x+3)^(1/2)/(4*x+2)^(1/2),x)

[Out] 1/12*((4*x+2)*(-6*x+3))^(1/2)/(4*x+2)^(1/2)/(-6*x+3)^(1/2)*6^(1/2)*arcsin(2*x)

maxima [A] time = 2.94, size = 9, normalized size = 0.69

$$\frac{1}{12} \sqrt{6} \arcsin(2x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-6*x)^(1/2)/(4*x+2)^(1/2),x, algorithm="maxima")

[Out] $\frac{1}{12}\sqrt{6}\arcsin(2x)$

mupad [B] time = 0.05, size = 40, normalized size = 3.08

$$\frac{\sqrt{6} \operatorname{atan}\left(\frac{\sqrt{24}(\sqrt{3}-\sqrt{3-6x})}{6(\sqrt{2}-\sqrt{4x+2})}\right)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((4*x + 2)^(1/2)*(3 - 6*x)^(1/2)),x)`

[Out] $-(6^{1/2}*\operatorname{atan}((24^{1/2}*(3^{1/2}) - (3 - 6*x)^{1/2}))/6*(2^{1/2} - (4*x + 2)^{1/2}))/3$

sympy [A] time = 3.35, size = 41, normalized size = 3.15

$$\begin{cases} -\frac{\sqrt{6}i\operatorname{acosh}\left(\sqrt{x+\frac{1}{2}}\right)}{6} & \text{for } \left|x + \frac{1}{2}\right| > 1 \\ \frac{\sqrt{6}\operatorname{asin}\left(\sqrt{x+\frac{1}{2}}\right)}{6} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(3-6*x)**(1/2)/(4*x+2)**(1/2),x)`

[Out] `Piecewise((-sqrt(6)*I*acosh(sqrt(x + 1/2))/6, Abs(x + 1/2) > 1), (sqrt(6)*asin(sqrt(x + 1/2))/6, True))`

$$3.1157 \quad \int \frac{1}{(3-6x)^{3/2}(2+4x)^{3/2}} dx$$

Optimal. Leaf size=28

$$\frac{x}{6\sqrt{6}\sqrt{1-2x}\sqrt{2x+1}}$$

[Out] 1/36*x*6^(1/2)/(1-2*x)^(1/2)/(1+2*x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {39}

$$\frac{x}{6\sqrt{6}\sqrt{1-2x}\sqrt{2x+1}}$$

Antiderivative was successfully verified.

[In] Int[1/((3 - 6*x)^(3/2)*(2 + 4*x)^(3/2)), x]

[Out] x/(6*Sqrt[6]*Sqrt[1 - 2*x]*Sqrt[1 + 2*x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rubi steps

$$\int \frac{1}{(3-6x)^{3/2}(2+4x)^{3/2}} dx = \frac{x}{6\sqrt{6}\sqrt{1-2x}\sqrt{1+2x}}$$

Mathematica [A] time = 0.02, size = 16, normalized size = 0.57

$$\frac{x}{6\sqrt{6-24x^2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((3 - 6*x)^(3/2)*(2 + 4*x)^(3/2)), x]

[Out] x/(6*Sqrt[6 - 24*x^2])

fricas [A] time = 0.42, size = 26, normalized size = 0.93

$$-\frac{\sqrt{4x+2}x\sqrt{-6x+3}}{36(4x^2-1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-6*x)^(3/2)/(4*x+2)^(3/2),x, algorithm="fricas")

[Out] -1/36*sqrt(4*x + 2)*x*sqrt(-6*x + 3)/(4*x^2 - 1)

giac [B] time = 1.06, size = 71, normalized size = 2.54

$$-\frac{\sqrt{6}(\sqrt{-4x+2}-2)}{288\sqrt{4x+2}} - \frac{\sqrt{6}\sqrt{4x+2}\sqrt{-4x+2}}{288(2x-1)} + \frac{\sqrt{6}\sqrt{4x+2}}{288(\sqrt{-4x+2}-2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-6*x)^(3/2)/(4*x+2)^(3/2),x, algorithm="giac")

[Out] -1/288*sqrt(6)*(sqrt(-4*x + 2) - 2)/sqrt(4*x + 2) - 1/288*sqrt(6)*sqrt(4*x + 2)*sqrt(-4*x + 2)/(2*x - 1) + 1/288*sqrt(6)*sqrt(4*x + 2)/(sqrt(-4*x + 2) - 2)

maple [A] time = 0.00, size = 28, normalized size = 1.00

$$-\frac{(2x-1)(2x+1)x}{(-6x+3)^{\frac{3}{2}}(4x+2)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-6*x+3)^(3/2)/(4*x+2)^(3/2),x)

[Out] -(2*x-1)*(1+2*x)*x/(-6*x+3)^(3/2)/(4*x+2)^(3/2)

maxima [A] time = 1.36, size = 12, normalized size = 0.43

$$\frac{x}{6\sqrt{-24x^2+6}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-6*x)^(3/2)/(4*x+2)^(3/2),x, algorithm="maxima")

[Out] 1/6*x/sqrt(-24*x^2 + 6)

mupad [B] time = 0.46, size = 24, normalized size = 0.86

$$\frac{x\sqrt{3-6x}}{\sqrt{4x+2}(36x-18)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((4*x + 2)^(3/2)*(3 - 6*x)^(3/2)), x)`

[Out] `-(x*(3 - 6*x)^(1/2))/((4*x + 2)^(1/2)*(36*x - 18))`

sympy [B] time = 85.28, size = 156, normalized size = 5.57

$$\left\{ \begin{array}{l} -\frac{2\sqrt{6}i\sqrt{x-\frac{1}{2}}\left(x+\frac{1}{2}\right)}{144\left(x+\frac{1}{2}\right)^2-144\sqrt{x+\frac{1}{2}}} + \frac{\sqrt{6}i\sqrt{x-\frac{1}{2}}}{144\left(x+\frac{1}{2}\right)^2-144\sqrt{x+\frac{1}{2}}} \quad \text{for } \left|x+\frac{1}{2}\right| > 1 \\ -\frac{2\sqrt{6}\sqrt{\frac{1}{2}-x}\left(x+\frac{1}{2}\right)}{144\left(x+\frac{1}{2}\right)^2-144\sqrt{x+\frac{1}{2}}} + \frac{\sqrt{6}\sqrt{\frac{1}{2}-x}}{144\left(x+\frac{1}{2}\right)^2-144\sqrt{x+\frac{1}{2}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(3-6*x)**(3/2)/(4*x+2)**(3/2), x)`

[Out] `Piecewise((-2*sqrt(6)*I*sqrt(x - 1/2)*(x + 1/2)/(144*(x + 1/2)**(3/2) - 144*sqrt(x + 1/2)) + sqrt(6)*I*sqrt(x - 1/2)/(144*(x + 1/2)**(3/2) - 144*sqrt(x + 1/2)), Abs(x + 1/2) > 1), (-2*sqrt(6)*sqrt(1/2 - x)*(x + 1/2)/(144*(x + 1/2)**(3/2) - 144*sqrt(x + 1/2)) + sqrt(6)*sqrt(1/2 - x)/(144*(x + 1/2)**(3/2) - 144*sqrt(x + 1/2)), True))`

$$3.1158 \quad \int \frac{1}{(3-6x)^{5/2}(2+4x)^{5/2}} dx$$

Optimal. Leaf size=57

$$\frac{x}{54\sqrt{6}\sqrt{1-2x}\sqrt{2x+1}} + \frac{x}{108\sqrt{6}(1-2x)^{3/2}(2x+1)^{3/2}}$$

[Out] 1/648*x/(1-2*x)^(3/2)/(1+2*x)^(3/2)*6^(1/2)+1/324*x*6^(1/2)/(1-2*x)^(1/2)/(1+2*x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {40, 39}

$$\frac{x}{54\sqrt{6}\sqrt{1-2x}\sqrt{2x+1}} + \frac{x}{108\sqrt{6}(1-2x)^{3/2}(2x+1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((3 - 6*x)^(5/2)*(2 + 4*x)^(5/2)), x]

[Out] x/(108*sqrt[6]*(1 - 2*x)^(3/2)*(1 + 2*x)^(3/2)) + x/(54*sqrt[6]*sqrt[1 - 2*x]*sqrt[1 + 2*x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] :> Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> -Simp[(x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{(3-6x)^{5/2}(2+4x)^{5/2}} dx &= \frac{x}{108\sqrt{6}(1-2x)^{3/2}(1+2x)^{3/2}} + \frac{1}{9} \int \frac{1}{(3-6x)^{3/2}(2+4x)^{3/2}} dx \\ &= \frac{x}{108\sqrt{6}(1-2x)^{3/2}(1+2x)^{3/2}} + \frac{x}{54\sqrt{6}\sqrt{1-2x}\sqrt{1+2x}} \end{aligned}$$

Mathematica [A] time = 0.02, size = 37, normalized size = 0.65

$$\frac{x(8x^2 - 3)}{108\sqrt{6 - 12x}(2x - 1)(2x + 1)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((3 - 6*x)^(5/2)*(2 + 4*x)^(5/2)),x]

[Out] (x*(-3 + 8*x^2))/(108*Sqrt[6 - 12*x]*(-1 + 2*x)*(1 + 2*x)^(3/2))

fricas [A] time = 0.41, size = 39, normalized size = 0.68

$$\frac{(8x^3 - 3x)\sqrt{4x + 2}\sqrt{-6x + 3}}{648(16x^4 - 8x^2 + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-6*x)^(5/2)/(4*x+2)^(5/2),x, algorithm="fricas")

[Out] -1/648*(8*x^3 - 3*x)*sqrt(4*x + 2)*sqrt(-6*x + 3)/(16*x^4 - 8*x^2 + 1)

giac [B] time = 1.02, size = 128, normalized size = 2.25

$$-\frac{1}{82944}\sqrt{6}\left(\frac{(\sqrt{-4x+2}-2)^3}{(4x+2)^{3/2}}+\frac{33(\sqrt{-4x+2}-2)}{\sqrt{4x+2}}\right)-\frac{(4\sqrt{6}(2x+1)-9\sqrt{6})\sqrt{4x+2}\sqrt{-4x+2}}{10368(2x-1)^2}+\frac{\sqrt{6}(4x+2)}{165888}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-6*x)^(5/2)/(4*x+2)^(5/2),x, algorithm="giac")

[Out] -1/82944*sqrt(6)*((sqrt(-4*x + 2) - 2)^3/(4*x + 2)^(3/2) + 33*(sqrt(-4*x + 2) - 2)/sqrt(4*x + 2)) - 1/10368*(4*sqrt(6)*(2*x + 1) - 9*sqrt(6))*sqrt(4*x + 2)*sqrt(-4*x + 2)/(2*x - 1)^2 + 1/165888*sqrt(6)*(4*x + 2)^(3/2)*(33*(sqrt(-4*x + 2) - 2)^2/(2*x + 1) + 2)/(sqrt(-4*x + 2) - 2)^3

maple [A] time = 0.00, size = 35, normalized size = 0.61

$$\frac{(2x - 1)(2x + 1)(8x^2 - 3)x}{3(-6x + 3)^{5/2}(4x + 2)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-6*x+3)^(5/2)/(4*x+2)^(5/2),x)

[Out] $1/3*(2*x-1)*(2*x+1)*x*(8*x^2-3)/(-6*x+3)^{(5/2)}/(4*x+2)^{(5/2)}$

maxima [A] time = 1.28, size = 25, normalized size = 0.44

$$\frac{x}{54\sqrt{-24x^2+6}} + \frac{x}{18(-24x^2+6)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(3-6*x)^(5/2)/(4*x+2)^(5/2),x, algorithm="maxima")`

[Out] $1/54*x/\text{sqrt}(-24*x^2 + 6) + 1/18*x/(-24*x^2 + 6)^{(3/2)}$

mupad [B] time = 0.31, size = 49, normalized size = 0.86

$$\frac{3x\sqrt{3-6x} - 8x^3\sqrt{3-6x}}{\sqrt{4x+2}(-2592x^3 + 1296x^2 + 648x - 324)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((4*x + 2)^(5/2)*(3 - 6*x)^(5/2)),x)`

[Out] $-(3*x*(3 - 6*x)^{(1/2)} - 8*x^3*(3 - 6*x)^{(1/2)})/((4*x + 2)^{(1/2)}*(648*x + 1296*x^2 - 2592*x^3 - 324))$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(3-6*x)**(5/2)/(4*x+2)**(5/2),x)`

[Out] Timed out

$$3.1159 \quad \int \frac{1}{(3-6x)^{7/2}(2+4x)^{7/2}} dx$$

Optimal. Leaf size=85

$$\frac{x}{405\sqrt{6}\sqrt{1-2x}\sqrt{2x+1}} + \frac{x}{810\sqrt{6}(1-2x)^{3/2}(2x+1)^{3/2}} + \frac{x}{1080\sqrt{6}(1-2x)^{5/2}(2x+1)^{5/2}}$$

[Out] $1/6480*x/(1-2*x)^{(5/2)}/(1+2*x)^{(5/2)}*6^{(1/2)}+1/4860*x/(1-2*x)^{(3/2)}/(1+2*x)^{(3/2)}*6^{(1/2)}+1/2430*x*6^{(1/2)}/(1-2*x)^{(1/2)}/(1+2*x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 85, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {40, 39}

$$\frac{x}{405\sqrt{6}\sqrt{1-2x}\sqrt{2x+1}} + \frac{x}{810\sqrt{6}(1-2x)^{3/2}(2x+1)^{3/2}} + \frac{x}{1080\sqrt{6}(1-2x)^{5/2}(2x+1)^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((3 - 6*x)^(7/2)*(2 + 4*x)^(7/2)), x]

[Out] $x/(1080*\text{Sqrt}[6]*(1-2*x)^{(5/2)}*(1+2*x)^{(5/2)}) + x/(810*\text{Sqrt}[6]*(1-2*x)^{(3/2)}*(1+2*x)^{(3/2)}) + x/(405*\text{Sqrt}[6]*\text{Sqrt}[1-2*x]*\text{Sqrt}[1+2*x])$

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rule 40

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := -Simp[(x*(a + b*x)^(m + 1)*(c + d*x)^(m + 1))/(2*a*c*(m + 1)), x] + Dist[(2*m + 3)/(2*a*c*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(m + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && ILtQ[m + 3/2, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{(3-6x)^{7/2}(2+4x)^{7/2}} dx &= \frac{x}{1080\sqrt{6}(1-2x)^{5/2}(1+2x)^{5/2}} + \frac{2}{15} \int \frac{1}{(3-6x)^{5/2}(2+4x)^{5/2}} dx \\ &= \frac{x}{1080\sqrt{6}(1-2x)^{5/2}(1+2x)^{5/2}} + \frac{x}{810\sqrt{6}(1-2x)^{3/2}(1+2x)^{3/2}} + \frac{2}{135} \int \frac{1}{(3-6x)^{3/2}(2+4x)^{3/2}} dx \\ &= \frac{x}{1080\sqrt{6}(1-2x)^{5/2}(1+2x)^{5/2}} + \frac{x}{810\sqrt{6}(1-2x)^{3/2}(1+2x)^{3/2}} + \frac{x}{405\sqrt{6}\sqrt{1-2x}\sqrt{2+4x}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 42, normalized size = 0.49

$$\frac{x(128x^4 - 80x^2 + 15)}{3240\sqrt{6-12x}(1-2x)^2(2x+1)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((3 - 6*x)^(7/2)*(2 + 4*x)^(7/2)), x]

[Out] (x*(15 - 80*x^2 + 128*x^4))/(3240*sqrt[6 - 12*x]*(1 - 2*x)^2*(1 + 2*x)^(5/2))

fricas [A] time = 0.42, size = 49, normalized size = 0.58

$$\frac{(128x^5 - 80x^3 + 15x)\sqrt{4x+2}\sqrt{-6x+3}}{19440(64x^6 - 48x^4 + 12x^2 - 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-6*x)^(7/2)/(4*x+2)^(7/2), x, algorithm="fricas")

[Out] -1/19440*(128*x^5 - 80*x^3 + 15*x)*sqrt(4*x + 2)*sqrt(-6*x + 3)/(64*x^6 - 48*x^4 + 12*x^2 - 1)

giac [B] time = 1.02, size = 181, normalized size = 2.13

$$-\frac{1}{39813120} \sqrt{6} \left(\frac{3(\sqrt{-4x+2}-2)^5}{(4x+2)^{5/2}} + \frac{85(\sqrt{-4x+2}-2)^3}{(4x+2)^{3/2}} + \frac{2130(\sqrt{-4x+2}-2)}{\sqrt{4x+2}} \right) - \frac{((64\sqrt{6}(2x+1) - 275\sqrt{6}))}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-6*x)^(7/2)/(4*x+2)^(7/2), x, algorithm="giac")

[Out] $-1/39813120*\sqrt{6}*(3*(\sqrt{-4*x + 2} - 2)^5/(4*x + 2)^{(5/2)} + 85*(\sqrt{-4*x + 2} - 2)^3/(4*x + 2)^{(3/2)} + 2130*(\sqrt{-4*x + 2} - 2)/\sqrt{4*x + 2}) - 1/1244160*((64*\sqrt{6}*(2*x + 1) - 275*\sqrt{6})*(2*x + 1) + 300*\sqrt{6})*\sqrt{4*x + 2}*\sqrt{-4*x + 2}/(2*x - 1)^3 + 1/79626240*\sqrt{6}*(1065*(\sqrt{-4*x + 2} - 2)^4/(2*x + 1)^2 + 85*(\sqrt{-4*x + 2} - 2)^2/(2*x + 1) + 6)*(4*x + 2)^{(5/2)}/(\sqrt{-4*x + 2} - 2)^5$

maple [A] time = 0.00, size = 40, normalized size = 0.47

$$\frac{(2x - 1)(2x + 1)(128x^4 - 80x^2 + 15)x}{15(-6x + 3)^{\frac{7}{2}}(4x + 2)^{\frac{7}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(-6*x+3)^{(7/2)}/(4*x+2)^{(7/2)}, x)$

[Out] $-1/15*(2*x-1)*(2*x+1)*x*(128*x^4-80*x^2+15)/(-6*x+3)^{(7/2)}/(4*x+2)^{(7/2)}$

maxima [A] time = 1.31, size = 37, normalized size = 0.44

$$\frac{x}{405\sqrt{-24x^2 + 6}} + \frac{x}{135(-24x^2 + 6)^{\frac{3}{2}}} + \frac{x}{30(-24x^2 + 6)^{\frac{5}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(3-6*x)^{(7/2)}/(4*x+2)^{(7/2)}, x, \text{algorithm}=\text{"maxima"})$

[Out] $1/405*x/\sqrt{-24*x^2 + 6} + 1/135*x/(-24*x^2 + 6)^{(3/2)} + 1/30*x/(-24*x^2 + 6)^{(5/2)}$

mupad [B] time = 0.45, size = 66, normalized size = 0.78

$$\frac{15x\sqrt{3-6x} - 80x^3\sqrt{3-6x} + 128x^5\sqrt{3-6x}}{((6x-3)(240x+360)+1440)\sqrt{4x+2}(6x-3)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/((4*x + 2)^{(7/2)}*(3 - 6*x)^{(7/2)}), x)$

[Out] $-(15*x*(3 - 6*x)^{(1/2)} - 80*x^3*(3 - 6*x)^{(1/2)} + 128*x^5*(3 - 6*x)^{(1/2)})/(((6*x - 3)*(240*x + 360) + 1440)*(4*x + 2)^{(1/2)}*(6*x - 3)^3)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(3-6*x)**(7/2)/(4*x+2)**(7/2),x)
```

```
[Out] Timed out
```

3.1160 $\int (3-x)^{3/2}(-2+x)^{3/2} dx$

Optimal. Leaf size=91

$$-\frac{1}{4}(x-2)^{3/2}(3-x)^{5/2}-\frac{1}{8}\sqrt{x-2}(3-x)^{5/2}+\frac{1}{32}\sqrt{x-2}(3-x)^{3/2}+\frac{3}{64}\sqrt{x-2}\sqrt{3-x}-\frac{3}{128}\sin^{-1}(5-2x)$$

[Out] $-1/4*(3-x)^{(5/2)}*(-2+x)^{(3/2)}+3/128*\arcsin(-5+2*x)+1/32*(3-x)^{(3/2)}*(-2+x)^{(1/2)}-1/8*(3-x)^{(5/2)}*(-2+x)^{(1/2)}+3/64*(3-x)^{(1/2)}*(-2+x)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 91, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {50, 53, 619, 216}

$$-\frac{1}{4}(x-2)^{3/2}(3-x)^{5/2}-\frac{1}{8}\sqrt{x-2}(3-x)^{5/2}+\frac{1}{32}\sqrt{x-2}(3-x)^{3/2}+\frac{3}{64}\sqrt{x-2}\sqrt{3-x}-\frac{3}{128}\sin^{-1}(5-2x)$$

Antiderivative was successfully verified.

[In] Int[(3 - x)^(3/2)*(-2 + x)^(3/2), x]

[Out] (3*Sqrt[3 - x]*Sqrt[-2 + x])/64 + ((3 - x)^(3/2)*Sqrt[-2 + x])/32 - ((3 - x)^(5/2)*Sqrt[-2 + x])/8 - ((3 - x)^(5/2)*(-2 + x)^(3/2))/4 - (3*ArcSin[5 - 2*x])/128

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 53

Int[1/(Sqrt[(a_) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] :> Int[1/Sqrt[a*c - b*(a - c)*x - b^2*x^2], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b + d, 0] && GtQ[a + c, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 619

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := Dist[1/(2*c*((-4
*c)/(b^2 - 4*a*c))^p), Subst[Int[Simp[1 - x^2/(b^2 - 4*a*c), x]^p, x], x, b
+ 2*c*x], x] /; FreeQ[{a, b, c, p}, x] && GtQ[4*a - b^2/c, 0]
```

Rubi steps

$$\begin{aligned}
\int (3-x)^{3/2}(-2+x)^{3/2} dx &= -\frac{1}{4}(3-x)^{5/2}(-2+x)^{3/2} + \frac{3}{8} \int (3-x)^{3/2} \sqrt{-2+x} dx \\
&= -\frac{1}{8}(3-x)^{5/2} \sqrt{-2+x} - \frac{1}{4}(3-x)^{5/2}(-2+x)^{3/2} + \frac{1}{16} \int \frac{(3-x)^{3/2}}{\sqrt{-2+x}} dx \\
&= \frac{1}{32}(3-x)^{3/2} \sqrt{-2+x} - \frac{1}{8}(3-x)^{5/2} \sqrt{-2+x} - \frac{1}{4}(3-x)^{5/2}(-2+x)^{3/2} + \frac{3}{64} \int \frac{\sqrt{3-x}}{\sqrt{-2+x}} dx \\
&= \frac{3}{64} \sqrt{3-x} \sqrt{-2+x} + \frac{1}{32}(3-x)^{3/2} \sqrt{-2+x} - \frac{1}{8}(3-x)^{5/2} \sqrt{-2+x} - \frac{1}{4}(3-x)^{5/2}(-2+x)^{3/2} \\
&= \frac{3}{64} \sqrt{3-x} \sqrt{-2+x} + \frac{1}{32}(3-x)^{3/2} \sqrt{-2+x} - \frac{1}{8}(3-x)^{5/2} \sqrt{-2+x} - \frac{1}{4}(3-x)^{5/2}(-2+x)^{3/2} \\
&= \frac{3}{64} \sqrt{3-x} \sqrt{-2+x} + \frac{1}{32}(3-x)^{3/2} \sqrt{-2+x} - \frac{1}{8}(3-x)^{5/2} \sqrt{-2+x} - \frac{1}{4}(3-x)^{5/2}(-2+x)^{3/2} \\
&= \frac{3}{64} \sqrt{3-x} \sqrt{-2+x} + \frac{1}{32}(3-x)^{3/2} \sqrt{-2+x} - \frac{1}{8}(3-x)^{5/2} \sqrt{-2+x} - \frac{1}{4}(3-x)^{5/2}(-2+x)^{3/2}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 80, normalized size = 0.88

$$\frac{\sqrt{-x^2+5x-6} \left(\sqrt{x-2} \left(-16x^4 + 168x^3 - 650x^2 + 1095x - 675 \right) + 3\sqrt{3-x} \sin^{-1} \left(\sqrt{3-x} \right) \right)}{64(x-3)\sqrt{x-2}}$$

Antiderivative was successfully verified.

[In] Integrate[(3 - x)^(3/2)*(-2 + x)^(3/2), x]

[Out] (Sqrt[-6 + 5*x - x^2]*(Sqrt[-2 + x]*(-675 + 1095*x - 650*x^2 + 168*x^3 - 16*x^4) + 3*Sqrt[3 - x]*ArcSin[Sqrt[3 - x]]))/(64*(-3 + x)*Sqrt[-2 + x])

fricas [A] time = 0.44, size = 62, normalized size = 0.68

$$-\frac{1}{64} (16x^3 - 120x^2 + 290x - 225) \sqrt{x-2} \sqrt{-x+3} - \frac{3}{128} \arctan \left(\frac{(2x-5)\sqrt{x-2}\sqrt{-x+3}}{2(x^2-5x+6)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-x)^(3/2)*(-2+x)^(3/2),x, algorithm="fricas")

[Out] $-1/64*(16*x^3 - 120*x^2 + 290*x - 225)*\sqrt{x - 2}*\sqrt{-x + 3} - 3/128*\arctan(1/2*(2*x - 5)*\sqrt{x - 2}*\sqrt{-x + 3}/(x^2 - 5*x + 6))$

giac [A] time = 0.88, size = 101, normalized size = 1.11

$$-\frac{1}{192} (2(4(6x+35)(x-2)+523)(x-2)+801)\sqrt{x-2}\sqrt{-x+3} + \frac{7}{24} (2(4x+15)(x-2)+69)\sqrt{x-2}\sqrt{-x+3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-x)^(3/2)*(-2+x)^(3/2),x, algorithm="giac")

[Out] $-1/192*(2*(4*(6*x + 35)*(x - 2) + 523)*(x - 2) + 801)*\sqrt{x - 2}*\sqrt{-x + 3} + 7/24*(2*(4*x + 15)*(x - 2) + 69)*\sqrt{x - 2}*\sqrt{-x + 3} - 4*(2*x + 3)*\sqrt{x - 2}*\sqrt{-x + 3} + 12*\sqrt{x - 2}*\sqrt{-x + 3} + 3/64*\arcsin(\sqrt{x - 2})$

maple [A] time = 0.01, size = 89, normalized size = 0.98

$$\frac{3\sqrt{(x-2)(-x+3)} \arcsin(2x-5)}{128\sqrt{x-2}\sqrt{-x+3}} + \frac{(-x+3)^{\frac{3}{2}}(x-2)^{\frac{5}{2}}}{4} + \frac{\sqrt{-x+3}(x-2)^{\frac{5}{2}}}{8} - \frac{\sqrt{-x+3}(x-2)^{\frac{3}{2}}}{32} - \frac{3\sqrt{-x+3}\sqrt{x-2}}{64}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((3-x)^(3/2)*(x-2)^(3/2),x)

[Out] $1/4*(3-x)^(3/2)*(x-2)^(5/2)+1/8*(3-x)^(1/2)*(x-2)^(5/2)-1/32*(3-x)^(1/2)*(x-2)^(3/2)-3/64*(3-x)^(1/2)*(x-2)^(1/2)+3/128*((x-2)*(3-x))^(1/2)/(x-2)^(1/2)/(3-x)^(1/2)*\arcsin(-5+2*x)$

maxima [A] time = 2.97, size = 67, normalized size = 0.74

$$\frac{1}{4}(-x^2+5x-6)^{\frac{3}{2}}x - \frac{5}{8}(-x^2+5x-6)^{\frac{3}{2}} + \frac{3}{32}\sqrt{-x^2+5x-6}x - \frac{15}{64}\sqrt{-x^2+5x-6} + \frac{3}{128}\arcsin(2x-5)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-x)^(3/2)*(-2+x)^(3/2),x, algorithm="maxima")

[Out] $1/4*(-x^2+5*x-6)^(3/2)*x - 5/8*(-x^2+5*x-6)^(3/2) + 3/32*\sqrt{-x^2+5*x-6}*x - 15/64*\sqrt{-x^2+5*x-6} + 3/128*\arcsin(2*x-5)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (x-2)^{3/2} (3-x)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x - 2)^(3/2)*(3 - x)^(3/2), x)`

[Out] `int((x - 2)^(3/2)*(3 - x)^(3/2), x)`

sympy [A] time = 7.48, size = 199, normalized size = 2.19

$$\begin{cases} -\frac{3i \operatorname{acosh}(\sqrt{x-2})}{64} - \frac{i(x-2)^{\frac{9}{2}}}{4\sqrt{x-3}} + \frac{5i(x-2)^{\frac{7}{2}}}{8\sqrt{x-3}} - \frac{13i(x-2)^{\frac{5}{2}}}{32\sqrt{x-3}} - \frac{i(x-2)^{\frac{3}{2}}}{64\sqrt{x-3}} + \frac{3i\sqrt{x-2}}{64\sqrt{x-3}} & \text{for } |x-2| > 1 \\ \frac{3 \operatorname{asin}(\sqrt{x-2})}{64} + \frac{(x-2)^{\frac{9}{2}}}{4\sqrt{3-x}} - \frac{5(x-2)^{\frac{7}{2}}}{8\sqrt{3-x}} + \frac{13(x-2)^{\frac{5}{2}}}{32\sqrt{3-x}} + \frac{(x-2)^{\frac{3}{2}}}{64\sqrt{3-x}} - \frac{3\sqrt{x-2}}{64\sqrt{3-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((3-x)**(3/2)*(-2+x)**(3/2), x)`

[Out] `Piecewise((-3*I*acosh(sqrt(x - 2))/64 - I*(x - 2)**(9/2)/(4*sqrt(x - 3)) + 5*I*(x - 2)**(7/2)/(8*sqrt(x - 3)) - 13*I*(x - 2)**(5/2)/(32*sqrt(x - 3)) - I*(x - 2)**(3/2)/(64*sqrt(x - 3)) + 3*I*sqrt(x - 2)/(64*sqrt(x - 3)), Abs(x - 2) > 1), (3*asin(sqrt(x - 2))/64 + (x - 2)**(9/2)/(4*sqrt(3 - x)) - 5*(x - 2)**(7/2)/(8*sqrt(3 - x)) + 13*(x - 2)**(5/2)/(32*sqrt(3 - x)) + (x - 2)**(3/2)/(64*sqrt(3 - x)) - 3*sqrt(x - 2)/(64*sqrt(3 - x)), True))`

3.1161 $\int \sqrt{3-x} \sqrt{-2+x} dx$

Optimal. Leaf size=51

$$-\frac{1}{2}\sqrt{x-2}(3-x)^{3/2} + \frac{1}{4}\sqrt{x-2}\sqrt{3-x} - \frac{1}{8}\sin^{-1}(5-2x)$$

[Out] 1/8*arcsin(-5+2*x)-1/2*(3-x)^(3/2)*(-2+x)^(1/2)+1/4*(3-x)^(1/2)*(-2+x)^(1/2)

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {50, 53, 619, 216}

$$-\frac{1}{2}\sqrt{x-2}(3-x)^{3/2} + \frac{1}{4}\sqrt{x-2}\sqrt{3-x} - \frac{1}{8}\sin^{-1}(5-2x)$$

Antiderivative was successfully verified.

[In] Int[Sqrt[3 - x]*Sqrt[-2 + x], x]

[Out] (Sqrt[3 - x]*Sqrt[-2 + x])/4 - ((3 - x)^(3/2)*Sqrt[-2 + x])/2 - ArcSin[5 - 2*x]/8

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 53

Int[1/(Sqrt[(a_) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Int[1/Sqrt[a*c - b*(a - c)*x - b^2*x^2], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b + d, 0] && GtQ[a + c, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 619

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := Dist[1/(2*c*((-4
*c)/(b^2 - 4*a*c))^p), Subst[Int[Simp[1 - x^2/(b^2 - 4*a*c), x]^p, x], x, b
+ 2*c*x], x] /; FreeQ[{a, b, c, p}, x] && GtQ[4*a - b^2/c, 0]
```

Rubi steps

$$\begin{aligned}
\int \sqrt{3-x} \sqrt{-2+x} \, dx &= -\frac{1}{2}(3-x)^{3/2} \sqrt{-2+x} + \frac{1}{4} \int \frac{\sqrt{3-x}}{\sqrt{-2+x}} \, dx \\
&= \frac{1}{4} \sqrt{3-x} \sqrt{-2+x} - \frac{1}{2}(3-x)^{3/2} \sqrt{-2+x} + \frac{1}{8} \int \frac{1}{\sqrt{3-x} \sqrt{-2+x}} \, dx \\
&= \frac{1}{4} \sqrt{3-x} \sqrt{-2+x} - \frac{1}{2}(3-x)^{3/2} \sqrt{-2+x} + \frac{1}{8} \int \frac{1}{\sqrt{-6+5x-x^2}} \, dx \\
&= \frac{1}{4} \sqrt{3-x} \sqrt{-2+x} - \frac{1}{2}(3-x)^{3/2} \sqrt{-2+x} - \frac{1}{8} \operatorname{Subst} \left(\int \frac{1}{\sqrt{1-x^2}} \, dx, x, 5-2x \right) \\
&= \frac{1}{4} \sqrt{3-x} \sqrt{-2+x} - \frac{1}{2}(3-x)^{3/2} \sqrt{-2+x} - \frac{1}{8} \sin^{-1}(5-2x)
\end{aligned}$$

Mathematica [A] time = 0.02, size = 69, normalized size = 1.35

$$\frac{\sqrt{-x^2+5x-6} \left(\sqrt{x-2} (2x^2-11x+15) + \sqrt{3-x} \sin^{-1}(\sqrt{3-x}) \right)}{4(x-3)\sqrt{x-2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[3 - x]*Sqrt[-2 + x], x]
```

```
[Out] (Sqrt[-6 + 5*x - x^2]*(Sqrt[-2 + x]*(15 - 11*x + 2*x^2) + Sqrt[3 - x]*ArcSin[Sqrt[3 - x]]))/(4*(-3 + x)*Sqrt[-2 + x])
```

fricas [A] time = 0.44, size = 52, normalized size = 1.02

$$\frac{1}{4} (2x-5) \sqrt{x-2} \sqrt{-x+3} - \frac{1}{8} \arctan \left(\frac{(2x-5) \sqrt{x-2} \sqrt{-x+3}}{2(x^2-5x+6)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((3-x)^(1/2)*(-2+x)^(1/2), x, algorithm="fricas")
```

```
[Out] 1/4*(2*x - 5)*sqrt(x - 2)*sqrt(-x + 3) - 1/8*arctan(1/2*(2*x - 5)*sqrt(x - 2)*sqrt(-x + 3)/(x^2 - 5*x + 6))
```

giac [A] time = 1.02, size = 42, normalized size = 0.82

$$\frac{1}{4}(2x+3)\sqrt{x-2}\sqrt{-x+3} - 2\sqrt{x-2}\sqrt{-x+3} + \frac{1}{4}\arcsin(\sqrt{x-2})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-x)^(1/2)*(-2+x)^(1/2),x, algorithm="giac")

[Out] 1/4*(2*x + 3)*sqrt(x - 2)*sqrt(-x + 3) - 2*sqrt(x - 2)*sqrt(-x + 3) + 1/4*arcsin(sqrt(x - 2))

maple [A] time = 0.01, size = 61, normalized size = 1.20

$$\frac{\sqrt{(x-2)(-x+3)} \arcsin(2x-5)}{8\sqrt{x-2}\sqrt{-x+3}} - \frac{(-x+3)^{\frac{3}{2}}\sqrt{x-2}}{2} + \frac{\sqrt{-x+3}\sqrt{x-2}}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+3)^(1/2)*(x-2)^(1/2),x)

[Out] -1/2*(-x+3)^(3/2)*(x-2)^(1/2)+1/4*(-x+3)^(1/2)*(x-2)^(1/2)+1/8*((x-2)*(-x+3))^(1/2)/(x-2)^(1/2)/(-x+3)^(1/2)*arcsin(2*x-5)

maxima [A] time = 2.96, size = 38, normalized size = 0.75

$$\frac{1}{2}\sqrt{-x^2+5x-6}x - \frac{5}{4}\sqrt{-x^2+5x-6} + \frac{1}{8}\arcsin(2x-5)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-x)^(1/2)*(-2+x)^(1/2),x, algorithm="maxima")

[Out] 1/2*sqrt(-x^2 + 5*x - 6)*x - 5/4*sqrt(-x^2 + 5*x - 6) + 1/8*arcsin(2*x - 5)

mupad [B] time = 0.21, size = 41, normalized size = 0.80

$$\left(\frac{x}{2} - \frac{5}{4}\right)\sqrt{x-2}\sqrt{3-x} - \frac{\ln\left(x - \frac{5}{2} - \sqrt{x-2}\sqrt{3-x}\right)}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x - 2)^(1/2)*(3 - x)^(1/2),x)

[Out] (x/2 - 5/4)*(x - 2)^(1/2)*(3 - x)^(1/2) - (log(x - (x - 2)^(1/2)*(3 - x)^(1/2) - 5/2)*1i)/8

sympy [A] time = 3.01, size = 124, normalized size = 2.43

$$\begin{cases} -\frac{i \operatorname{acosh}(\sqrt{x-2})}{4} + \frac{i(x-2)^{\frac{5}{2}}}{2\sqrt{x-3}} - \frac{3i(x-2)^{\frac{3}{2}}}{4\sqrt{x-3}} + \frac{i\sqrt{x-2}}{4\sqrt{x-3}} & \text{for } |x-2| > 1 \\ \frac{\operatorname{asin}(\sqrt{x-2})}{4} - \frac{(x-2)^{\frac{5}{2}}}{2\sqrt{3-x}} + \frac{3(x-2)^{\frac{3}{2}}}{4\sqrt{3-x}} - \frac{\sqrt{x-2}}{4\sqrt{3-x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-x)**(1/2)*(-2+x)**(1/2),x)

[Out] Piecewise((-I*acosh(sqrt(x - 2))/4 + I*(x - 2)**(5/2)/(2*sqrt(x - 3)) - 3*I*(x - 2)**(3/2)/(4*sqrt(x - 3)) + I*sqrt(x - 2)/(4*sqrt(x - 3)), Abs(x - 2) > 1), (asin(sqrt(x - 2))/4 - (x - 2)**(5/2)/(2*sqrt(3 - x)) + 3*(x - 2)**(3/2)/(4*sqrt(3 - x)) - sqrt(x - 2)/(4*sqrt(3 - x)), True))

$$3.1162 \quad \int \frac{1}{\sqrt{3-x} \sqrt{-2+x}} dx$$

Optimal. Leaf size=8

$$-\sin^{-1}(5-2x)$$

[Out] arcsin(-5+2*x)

Rubi [A] time = 0.00, antiderivative size = 8, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {53, 619, 216}

$$-\sin^{-1}(5-2x)$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[3 - x]*Sqrt[-2 + x]),x]

[Out] -ArcSin[5 - 2*x]

Rule 53

Int[1/(Sqrt[(a_) + (b_.)*(x_)]*Sqrt[(c_) + (d_.)*(x_)]), x_Symbol] :> Int[1/Sqrt[a*c - b*(a - c)*x - b^2*x^2], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b + d, 0] && GtQ[a + c, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 619

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] :> Dist[1/(2*c*((-4*c)/(b^2 - 4*a*c))^(p)), Subst[Int[Simp[1 - x^2/(b^2 - 4*a*c), x]^p, x], x, b + 2*c*x], x] /; FreeQ[{a, b, c, p}, x] && GtQ[4*a - b^2/c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{3-x} \sqrt{-2+x}} dx &= \int \frac{1}{\sqrt{-6+5x-x^2}} dx \\ &= -\text{Subst} \left(\int \frac{1}{\sqrt{1-x^2}} dx, x, 5-2x \right) \\ &= -\sin^{-1}(5-2x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 12, normalized size = 1.50

$$-2 \sin^{-1}(\sqrt{3-x})$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[3 - x]*Sqrt[-2 + x]),x]

[Out] -2*ArcSin[Sqrt[3 - x]]

fricas [B] time = 0.44, size = 32, normalized size = 4.00

$$-\arctan\left(\frac{(2x-5)\sqrt{x-2}\sqrt{-x+3}}{2(x^2-5x+6)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(1/2)/(-2+x)^(1/2),x, algorithm="fricas")

[Out] -arctan(1/2*(2*x - 5)*sqrt(x - 2)*sqrt(-x + 3)/(x^2 - 5*x + 6))

giac [A] time = 1.02, size = 8, normalized size = 1.00

$$2 \arcsin(\sqrt{x-2})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(1/2)/(-2+x)^(1/2),x, algorithm="giac")

[Out] 2*arcsin(sqrt(x - 2))

maple [B] time = 0.00, size = 31, normalized size = 3.88

$$\frac{\sqrt{(x-2)(-x+3)} \arcsin(2x-5)}{\sqrt{x-2} \sqrt{-x+3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+3)^(1/2)/(x-2)^(1/2),x)

[Out] ((x-2)*(-x+3))^(1/2)/(x-2)^(1/2)/(-x+3)^(1/2)*arcsin(2*x-5)

maxima [A] time = 3.00, size = 6, normalized size = 0.75

$$\arcsin(2x-5)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(1/2)/(-2+x)^(1/2),x, algorithm="maxima")

[Out] arcsin(2*x - 5)

mupad [B] time = 0.18, size = 31, normalized size = 3.88

$$-4 \operatorname{atan} \left(\frac{\sqrt{x-2} - \sqrt{2} \, 1i}{\sqrt{3} - \sqrt{3-x}} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((x - 2)^(1/2)*(3 - x)^(1/2)),x)

[Out] -4*atan(((x - 2)^(1/2) - 2^(1/2)*1i)/(3^(1/2) - (3 - x)^(1/2)))

sympy [A] time = 1.61, size = 26, normalized size = 3.25

$$\begin{cases} -2i \operatorname{acosh}(\sqrt{x-2}) & \text{for } |x-2| > 1 \\ 2 \operatorname{asin}(\sqrt{x-2}) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)**(1/2)/(-2+x)**(1/2),x)

[Out] Piecewise((-2*I*acosh(sqrt(x - 2)), Abs(x - 2) > 1), (2*asin(sqrt(x - 2)), True))

$$3.1163 \quad \int \frac{1}{(3-x)^{3/2}(-2+x)^{3/2}} dx$$

Optimal. Leaf size=37

$$\frac{2}{\sqrt{3-x}\sqrt{x-2}} - \frac{4\sqrt{3-x}}{\sqrt{x-2}}$$

[Out] $2/(3-x)^{(1/2)/(-2+x)^{(1/2)}-4*(3-x)^{(1/2)/(-2+x)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$\frac{2}{\sqrt{3-x}\sqrt{x-2}} - \frac{4\sqrt{3-x}}{\sqrt{x-2}}$$

Antiderivative was successfully verified.

[In] Int[1/((3 - x)^(3/2)*(-2 + x)^(3/2)),x]

[Out] 2/(Sqrt[3 - x]*Sqrt[-2 + x]) - (4*Sqrt[3 - x])/Sqrt[-2 + x]

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{(3-x)^{3/2}(-2+x)^{3/2}} dx = \frac{2}{\sqrt{3-x}\sqrt{-2+x}} + 2 \int \frac{1}{\sqrt{3-x}(-2+x)^{3/2}} dx$$

$$= \frac{2}{\sqrt{3-x}\sqrt{-2+x}} - \frac{4\sqrt{3-x}}{\sqrt{-2+x}}$$

Mathematica [A] time = 0.01, size = 21, normalized size = 0.57

$$\frac{2(2x-5)}{\sqrt{-x^2+5x-6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((3-x)^(3/2)*(-2+x)^(3/2)),x]

[Out] (2*(-5+2*x))/Sqrt[-6+5*x-x^2]

fricas [A] time = 0.49, size = 29, normalized size = 0.78

$$-\frac{2(2x-5)\sqrt{x-2}\sqrt{-x+3}}{x^2-5x+6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(3/2)/(-2+x)^(3/2),x, algorithm="fricas")

[Out] -2*(2*x-5)*sqrt(x-2)*sqrt(-x+3)/(x^2-5*x+6)

giac [A] time = 0.85, size = 53, normalized size = 1.43

$$-\frac{\sqrt{-x+3}-1}{\sqrt{x-2}} - \frac{2\sqrt{x-2}\sqrt{-x+3}}{x-3} + \frac{\sqrt{x-2}}{\sqrt{-x+3}-1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(3/2)/(-2+x)^(3/2),x, algorithm="giac")

[Out] -(sqrt(-x+3)-1)/sqrt(x-2)-2*sqrt(x-2)*sqrt(-x+3)/(x-3)+sqrt(x-2)/(sqrt(-x+3)-1)

maple [A] time = 0.00, size = 20, normalized size = 0.54

$$\frac{-10+4x}{\sqrt{-x+3}\sqrt{x-2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-x+3)^(3/2)/(x-2)^(3/2),x)`

[Out] `2*(2*x-5)/(x-2)^(1/2)/(-x+3)^(1/2)`

maxima [A] time = 1.32, size = 30, normalized size = 0.81

$$\frac{4x}{\sqrt{-x^2 + 5x - 6}} - \frac{10}{\sqrt{-x^2 + 5x - 6}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(3-x)^(3/2)/(-2+x)^(3/2),x, algorithm="maxima")`

[Out] `4*x/sqrt(-x^2 + 5*x - 6) - 10/sqrt(-x^2 + 5*x - 6)`

mupad [B] time = 0.25, size = 32, normalized size = 0.86

$$\frac{4x\sqrt{3-x} - 10\sqrt{3-x}}{\sqrt{x-2}(x-3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((x-2)^(3/2)*(3-x)^(3/2)),x)`

[Out] `-(4*x*(3-x)^(1/2) - 10*(3-x)^(1/2))/((x-2)^(1/2)*(x-3))`

sympy [A] time = 2.30, size = 100, normalized size = 2.70

$$\left\{ \begin{array}{ll} -\frac{4i\sqrt{x-3}(x-2)}{(x-2)^{\frac{3}{2}}-\sqrt{x-2}} + \frac{2i\sqrt{x-3}}{(x-2)^{\frac{3}{2}}-\sqrt{x-2}} & \text{for } |x-2| > 1 \\ -\frac{4\sqrt{3-x}(x-2)}{(x-2)^{\frac{3}{2}}-\sqrt{x-2}} + \frac{2\sqrt{3-x}}{(x-2)^{\frac{3}{2}}-\sqrt{x-2}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(3-x)**(3/2)/(-2+x)**(3/2),x)`

[Out] `Piecewise((-4*I*sqrt(x-3)*(x-2)/((x-2)**(3/2)-sqrt(x-2))+2*I*sqrt(x-3)/((x-2)**(3/2)-sqrt(x-2)), Abs(x-2)>1), (-4*sqrt(3-x)*(x-2)/((x-2)**(3/2)-sqrt(x-2))+2*sqrt(3-x)/((x-2)**(3/2)-sqrt(x-2)), True))`

$$3.1164 \quad \int \frac{1}{(3-x)^{5/2}(-2+x)^{5/2}} dx$$

Optimal. Leaf size=79

$$-\frac{32\sqrt{3-x}}{3\sqrt{x-2}} - \frac{16\sqrt{3-x}}{3(x-2)^{3/2}} + \frac{4}{(x-2)^{3/2}\sqrt{3-x}} + \frac{2}{3(x-2)^{3/2}(3-x)^{3/2}}$$

[Out] $2/3/(3-x)^{(3/2)/(-2+x)^{(3/2)}+4/(-2+x)^{(3/2)/(3-x)^{(1/2)}-16/3*(3-x)^{(1/2)/(-2+x)^{(3/2)}-32/3*(3-x)^{(1/2)/(-2+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {45, 37}

$$-\frac{32\sqrt{3-x}}{3\sqrt{x-2}} - \frac{16\sqrt{3-x}}{3(x-2)^{3/2}} + \frac{4}{(x-2)^{3/2}\sqrt{3-x}} + \frac{2}{3(x-2)^{3/2}(3-x)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((3 - x)^(5/2)*(-2 + x)^(5/2)), x]

[Out] $2/(3*(3-x)^{(3/2)*(-2+x)^{(3/2)}) + 4/(Sqrt[3-x]*(-2+x)^{(3/2)}) - (16*Sqrt[3-x])/(3*(-2+x)^{(3/2)}) - (32*Sqrt[3-x])/(3*Sqrt[-2+x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(3-x)^{5/2}(-2+x)^{5/2}} dx &= \frac{2}{3(3-x)^{3/2}(-2+x)^{3/2}} + 2 \int \frac{1}{(3-x)^{3/2}(-2+x)^{5/2}} dx \\
&= \frac{2}{3(3-x)^{3/2}(-2+x)^{3/2}} + \frac{4}{\sqrt{3-x}(-2+x)^{3/2}} + 8 \int \frac{1}{\sqrt{3-x}(-2+x)^{5/2}} dx \\
&= \frac{2}{3(3-x)^{3/2}(-2+x)^{3/2}} + \frac{4}{\sqrt{3-x}(-2+x)^{3/2}} - \frac{16\sqrt{3-x}}{3(-2+x)^{3/2}} + \frac{16}{3} \int \frac{1}{\sqrt{3-x}(-2+x)} dx \\
&= \frac{2}{3(3-x)^{3/2}(-2+x)^{3/2}} + \frac{4}{\sqrt{3-x}(-2+x)^{3/2}} - \frac{16\sqrt{3-x}}{3(-2+x)^{3/2}} - \frac{32\sqrt{3-x}}{3\sqrt{-2+x}}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 0.42

$$\frac{-32x^3 + 240x^2 - 588x + 470}{3(-x^2 + 5x - 6)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((3 - x)^(5/2)*(-2 + x)^(5/2)), x]

[Out] (470 - 588*x + 240*x^2 - 32*x^3)/(3*(-6 + 5*x - x^2)^(3/2))

fricas [A] time = 0.47, size = 49, normalized size = 0.62

$$\frac{2(16x^3 - 120x^2 + 294x - 235)\sqrt{x-2}\sqrt{-x+3}}{3(x^4 - 10x^3 + 37x^2 - 60x + 36)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(5/2)/(-2+x)^(5/2), x, algorithm="fricas")

[Out] -2/3*(16*x^3 - 120*x^2 + 294*x - 235)*sqrt(x - 2)*sqrt(-x + 3)/(x^4 - 10*x^3 + 37*x^2 - 60*x + 36)

giac [A] time = 1.10, size = 97, normalized size = 1.23

$$\frac{(\sqrt{-x+3}-1)^3}{12(x-2)^{\frac{3}{2}}} - \frac{11(\sqrt{-x+3}-1)}{4\sqrt{x-2}} - \frac{2(8x-25)\sqrt{x-2}\sqrt{-x+3}}{3(x-3)^2} + \frac{(x-2)^{\frac{3}{2}}\left(\frac{33(\sqrt{-x+3}-1)^2}{x-2} + 1\right)}{12(\sqrt{-x+3}-1)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(5/2)/(-2+x)^(5/2),x, algorithm="giac")

[Out]
$$-1/12*(\sqrt{-x+3}-1)^3/(x-2)^{3/2}-11/4*(\sqrt{-x+3}-1)/\sqrt{x-2}-2/3*(8*x-25)*\sqrt{x-2}*\sqrt{-x+3}/(x-3)^2+1/12*(x-2)^{3/2}*(33*(\sqrt{-x+3}-1)^2/(x-2)+1)/(\sqrt{-x+3}-1)^3$$

maple [A] time = 0.00, size = 30, normalized size = 0.38

$$-\frac{2(16x^3-120x^2+294x-235)}{3(x-2)^{\frac{3}{2}}(-x+3)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+3)^(5/2)/(x-2)^(5/2),x)

[Out]
$$-2/3*(16*x^3-120*x^2+294*x-235)/(x-2)^{3/2}/(-x+3)^{3/2}$$

maxima [A] time = 1.34, size = 59, normalized size = 0.75

$$\frac{32x}{3\sqrt{-x^2+5x-6}} - \frac{80}{3\sqrt{-x^2+5x-6}} + \frac{4x}{3(-x^2+5x-6)^{\frac{3}{2}}} - \frac{10}{3(-x^2+5x-6)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(5/2)/(-2+x)^(5/2),x, algorithm="maxima")

[Out]
$$32/3*x/\sqrt{-x^2+5*x-6}-80/3/\sqrt{-x^2+5*x-6}+4/3*x/(-x^2+5*x-6)^{3/2}-10/3/(-x^2+5*x-6)^{3/2}$$

mupad [B] time = 0.37, size = 69, normalized size = 0.87

$$-\frac{32(x-2)^3\sqrt{3-x}-48(x-2)^2\sqrt{3-x}+2\sqrt{3-x}+12(x-2)\sqrt{3-x}}{(3x-6)\sqrt{x-2}(x-3)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((x-2)^(5/2)*(3-x)^(5/2)),x)

[Out]
$$-(32*(x-2)^3*(3-x)^{1/2}-48*(x-2)^2*(3-x)^{1/2}+2*(3-x)^{1/2}+12*(x-2)*(3-x)^{1/2})/((3*x-6)*(x-2)^{1/2}*(x-3)^2)$$

sympy [B] time = 9.85, size = 282, normalized size = 3.57

$$\left\{ \begin{array}{l} \frac{32\sqrt{-1+\frac{1}{x-2}}(x-2)^3}{3x+3(x-2)^3-6(x-2)^2-6} + \frac{48\sqrt{-1+\frac{1}{x-2}}(x-2)^2}{3x+3(x-2)^3-6(x-2)^2-6} - \frac{12\sqrt{-1+\frac{1}{x-2}}(x-2)}{3x+3(x-2)^3-6(x-2)^2-6} - \frac{2\sqrt{-1+\frac{1}{x-2}}}{3x+3(x-2)^3-6(x-2)^2-6} \quad \text{for } \frac{1}{|x-2|} > 1 \\ \frac{32i\sqrt{1-\frac{1}{x-2}}(x-2)^3}{3x+3(x-2)^3-6(x-2)^2-6} + \frac{48i\sqrt{1-\frac{1}{x-2}}(x-2)^2}{3x+3(x-2)^3-6(x-2)^2-6} - \frac{12i\sqrt{1-\frac{1}{x-2}}(x-2)}{3x+3(x-2)^3-6(x-2)^2-6} - \frac{2i\sqrt{1-\frac{1}{x-2}}}{3x+3(x-2)^3-6(x-2)^2-6} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(3-x)**(5/2)/(-2+x)**(5/2),x)
```

```
[Out] Piecewise((-32*sqrt(-1 + 1/(x - 2))*(x - 2)**3/(3*x + 3*(x - 2)**3 - 6*(x - 2)**2 - 6) + 48*sqrt(-1 + 1/(x - 2))*(x - 2)**2/(3*x + 3*(x - 2)**3 - 6*(x - 2)**2 - 6) - 12*sqrt(-1 + 1/(x - 2))*(x - 2)/(3*x + 3*(x - 2)**3 - 6*(x - 2)**2 - 6) - 2*sqrt(-1 + 1/(x - 2))/(3*x + 3*(x - 2)**3 - 6*(x - 2)**2 - 6), 1/Abs(x - 2) > 1), (-32*I*sqrt(1 - 1/(x - 2))*(x - 2)**3/(3*x + 3*(x - 2)**3 - 6*(x - 2)**2 - 6) + 48*I*sqrt(1 - 1/(x - 2))*(x - 2)**2/(3*x + 3*(x - 2)**3 - 6*(x - 2)**2 - 6) - 12*I*sqrt(1 - 1/(x - 2))*(x - 2)/(3*x + 3*(x - 2)**3 - 6*(x - 2)**2 - 6) - 2*I*sqrt(1 - 1/(x - 2))/(3*x + 3*(x - 2)**3 - 6*(x - 2)**2 - 6), True))
```


$$3.1165 \quad \int \frac{1}{(3-x)^{3/2}(3+x)^{3/2}} dx$$

Optimal. Leaf size=21

$$\frac{x}{9\sqrt{3-x}\sqrt{x+3}}$$

[Out] 1/9*x/(3-x)^(1/2)/(3+x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {39}

$$\frac{x}{9\sqrt{3-x}\sqrt{x+3}}$$

Antiderivative was successfully verified.

[In] Int[1/((3 - x)^(3/2)*(3 + x)^(3/2)), x]

[Out] x/(9*Sqrt[3 - x]*Sqrt[3 + x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := Simp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]

Rubi steps

$$\int \frac{1}{(3-x)^{3/2}(3+x)^{3/2}} dx = \frac{x}{9\sqrt{3-x}\sqrt{3+x}}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 0.76

$$\frac{x}{9\sqrt{9-x^2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((3 - x)^(3/2)*(3 + x)^(3/2)), x]

[Out] x/(9*Sqrt[9 - x^2])

fricas [A] time = 0.43, size = 22, normalized size = 1.05

$$-\frac{\sqrt{x+3}x\sqrt{-x+3}}{9(x^2-9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(3/2)/(3+x)^(3/2),x, algorithm="fricas")

[Out] -1/9*sqrt(x+3)*x*sqrt(-x+3)/(x^2-9)

giac [B] time = 0.90, size = 62, normalized size = 2.95

$$\frac{\sqrt{6}-\sqrt{-x+3}}{36\sqrt{x+3}} - \frac{\sqrt{x+3}\sqrt{-x+3}}{18(x-3)} - \frac{\sqrt{x+3}}{36(\sqrt{6}-\sqrt{-x+3})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(3/2)/(3+x)^(3/2),x, algorithm="giac")

[Out] 1/36*(sqrt(6)-sqrt(-x+3))/sqrt(x+3) - 1/18*sqrt(x+3)*sqrt(-x+3)/(x-3) - 1/36*sqrt(x+3)/(sqrt(6)-sqrt(-x+3))

maple [A] time = 0.00, size = 16, normalized size = 0.76

$$\frac{x}{9\sqrt{-x+3}\sqrt{x+3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-x+3)^(3/2)/(3+x)^(3/2),x)

[Out] 1/9*x/(-x+3)^(1/2)/(3+x)^(1/2)

maxima [A] time = 1.37, size = 12, normalized size = 0.57

$$\frac{x}{9\sqrt{-x^2+9}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-x)^(3/2)/(3+x)^(3/2),x, algorithm="maxima")

[Out] 1/9*x/sqrt(-x^2+9)

mupad [B] time = 0.36, size = 22, normalized size = 1.05

$$\frac{x\sqrt{3-x}}{(9x-27)\sqrt{x+3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((3 - x)^(3/2)*(x + 3)^(3/2)), x)`

[Out] `-(x*(3 - x)^(1/2))/((9*x - 27)*(x + 3)^(1/2))`

sympy [A] time = 1.80, size = 73, normalized size = 3.48

$$\begin{cases} \frac{1}{9\sqrt{-1+\frac{6}{x+3}}} - \frac{1}{3\sqrt{-1+\frac{6}{x+3}}(x+3)} & \text{for } \frac{6}{|x+3|} > 1 \\ \frac{i\sqrt{1-\frac{6}{x+3}}(x+3)}{27-9x} - \frac{3i\sqrt{1-\frac{6}{x+3}}}{27-9x} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(3-x)**(3/2)/(3+x)**(3/2), x)`

[Out] `Piecewise((1/(9*sqrt(-1 + 6/(x + 3))) - 1/(3*sqrt(-1 + 6/(x + 3))*(x + 3))),
6/Abs(x + 3) > 1), (I*sqrt(1 - 6/(x + 3))*(x + 3)/(27 - 9*x) - 3*I*sqrt(1
- 6/(x + 3))/(27 - 9*x), True))`

$$3.1166 \quad \int \frac{1}{(3-bx)^{3/2}(3+bx)^{3/2}} dx$$

Optimal. Leaf size=24

$$\frac{x}{9\sqrt{3-bx}\sqrt{bx+3}}$$

[Out] 1/9*x/(-b*x+3)^(1/2)/(b*x+3)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 24, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.050$, Rules used = {39}

$$\frac{x}{9\sqrt{3-bx}\sqrt{bx+3}}$$

Antiderivative was successfully verified.

[In] Int[1/((3 - b*x)^(3/2)*(3 + b*x)^(3/2)), x]

[Out] x/(9*Sqrt[3 - b*x]*Sqrt[3 + b*x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] :> S
imp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && Eq
Q[b*c + a*d, 0]

Rubi steps

$$\int \frac{1}{(3-bx)^{3/2}(3+bx)^{3/2}} dx = \frac{x}{9\sqrt{3-bx}\sqrt{3+bx}}$$

Mathematica [A] time = 0.01, size = 19, normalized size = 0.79

$$\frac{x}{9\sqrt{9-b^2x^2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((3 - b*x)^(3/2)*(3 + b*x)^(3/2)), x]

[Out] x/(9*Sqrt[9 - b^2*x^2])

fricas [A] time = 0.46, size = 29, normalized size = 1.21

$$-\frac{\sqrt{bx+3}\sqrt{-bx+3}x}{9(b^2x^2-9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+3)^(3/2)/(b*x+3)^(3/2),x, algorithm="fricas")

[Out] -1/9*sqrt(b*x + 3)*sqrt(-b*x + 3)*x/(b^2*x^2 - 9)

giac [B] time = 1.10, size = 82, normalized size = 3.42

$$\frac{\sqrt{6}-\sqrt{-bx+3}}{36\sqrt{bx+3}b}-\frac{\sqrt{bx+3}\sqrt{-bx+3}}{18(bx-3)b}-\frac{\sqrt{bx+3}}{36b(\sqrt{6}-\sqrt{-bx+3})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+3)^(3/2)/(b*x+3)^(3/2),x, algorithm="giac")

[Out] 1/36*(sqrt(6) - sqrt(-b*x + 3))/(sqrt(b*x + 3)*b) - 1/18*sqrt(b*x + 3)*sqrt(-b*x + 3)/((b*x - 3)*b) - 1/36*sqrt(b*x + 3)/(b*(sqrt(6) - sqrt(-b*x + 3)))

maple [A] time = 0.00, size = 19, normalized size = 0.79

$$\frac{x}{9\sqrt{-bx+3}\sqrt{bx+3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x+3)^(3/2)/(b*x+3)^(3/2),x)

[Out] 1/9*x/(-b*x+3)^(1/2)/(b*x+3)^(1/2)

maxima [A] time = 1.37, size = 15, normalized size = 0.62

$$\frac{x}{9\sqrt{-b^2x^2+9}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+3)^(3/2)/(b*x+3)^(3/2),x, algorithm="maxima")

[Out] 1/9*x/sqrt(-b^2*x^2 + 9)

mupad [B] time = 0.46, size = 26, normalized size = 1.08

$$\frac{x\sqrt{3-bx}}{\sqrt{bx+3}(9bx-27)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((3 - b*x)^(3/2)*(b*x + 3)^(3/2)),x)`

[Out] `-(x*(3 - b*x)^(1/2))/((b*x + 3)^(1/2)*(9*b*x - 27))`

sympy [C] time = 5.16, size = 73, normalized size = 3.04

$$-\frac{iG_{6,6}^{5,3}\left(\begin{matrix} \frac{3}{4}, \frac{5}{4}, 1 \\ \frac{1}{2}, \frac{3}{2}, 2 \end{matrix} \middle| \frac{9}{b^2x^2}\right)}{18\pi^{\frac{3}{2}}b} + \frac{G_{6,6}^{2,6}\left(\begin{matrix} -\frac{1}{2}, 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1 \\ \frac{1}{4}, \frac{3}{4} \end{matrix} \middle| \frac{9e^{-2i\pi}}{b^2x^2}\right)}{18\pi^{\frac{3}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x+3)**(3/2)/(b*x+3)**(3/2),x)`

[Out] `-I*meijerg(((3/4, 5/4, 1), (1/2, 3/2, 2)), ((3/4, 1, 5/4, 3/2, 2), (0,)), 9/(b**2*x**2))/(18*pi**(3/2)*b) + meijerg((-1/2, 0, 1/4, 1/2, 3/4, 1), ((1/4, 3/4), (-1/2, 0, 1, 0)), 9*exp_polar(-2*I*pi)/(b**2*x**2))/(18*pi**(3/2)*b)`

$$3.1167 \quad \int \frac{1}{(6-2x)^{3/2}(3+x)^{3/2}} dx$$

Optimal. Leaf size=26

$$\frac{x}{18\sqrt{2}\sqrt{3-x}\sqrt{x+3}}$$

[Out] 1/36*x*2^(1/2)/(3-x)^(1/2)/(3+x)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {39}

$$\frac{x}{18\sqrt{2}\sqrt{3-x}\sqrt{x+3}}$$

Antiderivative was successfully verified.

[In] Int[1/((6 - 2*x)^(3/2)*(3 + x)^(3/2)), x]

[Out] x/(18*Sqrt[2]*Sqrt[3 - x]*Sqrt[3 + x])

Rule 39

Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] := S imp[x/(a*c*Sqrt[a + b*x]*Sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && Eq Q[b*c + a*d, 0]

Rubi steps

$$\int \frac{1}{(6-2x)^{3/2}(3+x)^{3/2}} dx = \frac{x}{18\sqrt{2}\sqrt{3-x}\sqrt{x+3}}$$

Mathematica [A] time = 0.01, size = 21, normalized size = 0.81

$$\frac{x}{18\sqrt{6-2x}\sqrt{x+3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((6 - 2*x)^(3/2)*(3 + x)^(3/2)), x]

[Out] x/(18*Sqrt[6 - 2*x]*Sqrt[3 + x])

fricas [A] time = 0.47, size = 22, normalized size = 0.85

$$-\frac{\sqrt{x+3}x\sqrt{-2x+6}}{36(x^2-9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(6-2*x)^(3/2)/(3+x)^(3/2),x, algorithm="fricas")

[Out] -1/36*sqrt(x + 3)*x*sqrt(-2*x + 6)/(x^2 - 9)

giac [B] time = 1.04, size = 71, normalized size = 2.73

$$\frac{\sqrt{2}(\sqrt{6}-\sqrt{-x+3})}{144\sqrt{x+3}} - \frac{\sqrt{2}\sqrt{x+3}\sqrt{-x+3}}{72(x-3)} - \frac{\sqrt{2}\sqrt{x+3}}{144(\sqrt{6}-\sqrt{-x+3})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(6-2*x)^(3/2)/(3+x)^(3/2),x, algorithm="giac")

[Out] 1/144*sqrt(2)*(sqrt(6) - sqrt(-x + 3))/sqrt(x + 3) - 1/72*sqrt(2)*sqrt(x + 3)*sqrt(-x + 3)/(x - 3) - 1/144*sqrt(2)*sqrt(x + 3)/(sqrt(6) - sqrt(-x + 3))

maple [A] time = 0.00, size = 19, normalized size = 0.73

$$-\frac{(x-3)x}{9\sqrt{x+3}(-2x+6)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(6-2*x)^(3/2)/(x+3)^(3/2),x)

[Out] -1/9*(-3+x)/(x+3)^(1/2)*x/(6-2*x)^(3/2)

maxima [A] time = 1.33, size = 12, normalized size = 0.46

$$\frac{x}{18\sqrt{-2x^2+18}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(6-2*x)^(3/2)/(3+x)^(3/2),x, algorithm="maxima")

[Out] 1/18*x/sqrt(-2*x^2 + 18)

mupad [B] time = 0.37, size = 22, normalized size = 0.85

$$-\frac{x\sqrt{6-2x}}{(36x-108)\sqrt{x+3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((6 - 2*x)^(3/2)*(x + 3)^(3/2)), x)`

[Out] `-(x*(6 - 2*x)^(1/2))/((36*x - 108)*(x + 3)^(1/2))`

sympy [A] time = 20.45, size = 90, normalized size = 3.46

$$\begin{cases} \frac{\sqrt{2}}{36\sqrt{-1+\frac{6}{x+3}}} - \frac{\sqrt{2}}{12\sqrt{-1+\frac{6}{x+3}}(x+3)} & \text{for } \frac{6}{|x+3|} > 1 \\ \frac{\sqrt{2}i\sqrt{1-\frac{6}{x+3}}(x+3)}{108-36x} - \frac{3\sqrt{2}i\sqrt{1-\frac{6}{x+3}}}{108-36x} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(6-2*x)**(3/2)/(3+x)**(3/2), x)`

[Out] `Piecewise((sqrt(2)/(36*sqrt(-1 + 6/(x + 3))) - sqrt(2)/(12*sqrt(-1 + 6/(x + 3)))*(x + 3)), 6/Abs(x + 3) > 1), (sqrt(2)*I*sqrt(1 - 6/(x + 3))*(x + 3)/(108 - 36*x) - 3*sqrt(2)*I*sqrt(1 - 6/(x + 3))/(108 - 36*x), True))`

$$3.1168 \quad \int \frac{1}{(6-2bx)^{3/2}(3+bx)^{3/2}} dx$$

Optimal. Leaf size=29

$$\frac{x}{18\sqrt{2}\sqrt{3-bx}\sqrt{bx+3}}$$

[Out] $1/36*x*2^{(1/2)/(-b*x+3)^{(1/2)/(b*x+3)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.050$, Rules used = {39}

$$\frac{x}{18\sqrt{2}\sqrt{3-bx}\sqrt{bx+3}}$$

Antiderivative was successfully verified.

[In] `Int[1/((6 - 2*b*x)^(3/2)*(3 + b*x)^(3/2)), x]`

[Out] `x/(18*sqrt[2]*sqrt[3 - b*x]*sqrt[3 + b*x])`

Rule 39

`Int[1/(((a_) + (b_.)*(x_))^(3/2)*((c_) + (d_.)*(x_))^(3/2)), x_Symbol] :> Simp[x/(a*c*sqrt[a + b*x]*sqrt[c + d*x]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0]`

Rubi steps

$$\int \frac{1}{(6-2bx)^{3/2}(3+bx)^{3/2}} dx = \frac{x}{18\sqrt{2}\sqrt{3-bx}\sqrt{3+bx}}$$

Mathematica [A] time = 0.02, size = 19, normalized size = 0.66

$$\frac{x}{18\sqrt{18-2b^2x^2}}$$

Antiderivative was successfully verified.

[In] `Integrate[1/((6 - 2*b*x)^(3/2)*(3 + b*x)^(3/2)), x]`

[Out] `x/(18*sqrt[18 - 2*b^2*x^2])`

fricas [A] time = 0.43, size = 29, normalized size = 1.00

$$\frac{\sqrt{bx+3}\sqrt{-2bx+6}x}{36(b^2x^2-9)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-2*b*x+6)^(3/2)/(b*x+3)^(3/2),x, algorithm="fricas")

[Out] -1/36*sqrt(b*x + 3)*sqrt(-2*b*x + 6)*x/(b^2*x^2 - 9)

giac [B] time = 1.14, size = 91, normalized size = 3.14

$$\frac{\sqrt{2}(\sqrt{6}-\sqrt{-bx+3})}{144\sqrt{bx+3}b} - \frac{\sqrt{2}\sqrt{bx+3}\sqrt{-bx+3}}{72(bx-3)b} - \frac{\sqrt{2}\sqrt{bx+3}}{144b(\sqrt{6}-\sqrt{-bx+3})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-2*b*x+6)^(3/2)/(b*x+3)^(3/2),x, algorithm="giac")

[Out] 1/144*sqrt(2)*(sqrt(6)-sqrt(-b*x+3))/(sqrt(b*x+3)*b) - 1/72*sqrt(2)*sqrt(b*x+3)*sqrt(-b*x+3)/((b*x-3)*b) - 1/144*sqrt(2)*sqrt(b*x+3)/(b*(sqrt(6)-sqrt(-b*x+3)))

maple [A] time = 0.00, size = 24, normalized size = 0.83

$$-\frac{(bx-3)x}{9\sqrt{bx+3}(-2bx+6)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-2*b*x+6)^(3/2)/(b*x+3)^(3/2),x)

[Out] -1/9*(b*x-3)/(b*x+3)^(1/2)*x/(-2*b*x+6)^(3/2)

maxima [A] time = 1.25, size = 15, normalized size = 0.52

$$\frac{x}{18\sqrt{-2b^2x^2+18}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-2*b*x+6)^(3/2)/(b*x+3)^(3/2),x, algorithm="maxima")

[Out] 1/18*x/sqrt(-2*b^2*x^2 + 18)

mupad [B] time = 0.32, size = 26, normalized size = 0.90

$$\frac{x\sqrt{6-2bx}}{\sqrt{bx+3}(36bx-108)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((b*x + 3)^(3/2)*(6 - 2*b*x)^(3/2)),x)`

[Out] `-(x*(6 - 2*b*x)^(1/2))/((b*x + 3)^(1/2)*(36*b*x - 108))`

sympy [C] time = 31.50, size = 83, normalized size = 2.86

$$-\frac{\sqrt{2}iG_{6,6}^{5,3}\left(\begin{matrix} \frac{3}{4}, \frac{5}{4}, 1 & \frac{1}{2}, \frac{3}{2}, 2 \\ \frac{3}{4}, 1, \frac{5}{4}, \frac{3}{2}, 2 & 0 \end{matrix} \middle| \frac{9}{b^2x^2}\right)}{72\pi^{\frac{3}{2}}b} + \frac{\sqrt{2}G_{6,6}^{2,6}\left(\begin{matrix} -\frac{1}{2}, 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1 \\ \frac{1}{4}, \frac{3}{4} & -\frac{1}{2}, 0, 1, 0 \end{matrix} \middle| \frac{9e^{-2i\pi}}{b^2x^2}\right)}{72\pi^{\frac{3}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-2*b*x+6)**(3/2)/(b*x+3)**(3/2),x)`

[Out] `-sqrt(2)*I*meijerg(((3/4, 5/4, 1), (1/2, 3/2, 2)), ((3/4, 1, 5/4, 3/2, 2), (0,)), 9/(b**2*x**2))/(72*pi**(3/2)*b) + sqrt(2)*meijerg(((-1/2, 0, 1/4, 1/2, 3/4, 1), ()), ((1/4, 3/4), (-1/2, 0, 1, 0)), 9*exp_polar(-2*I*pi)/(b**2*x**2))/(72*pi**(3/2)*b)`

$$3.1169 \quad \int \frac{1}{\sqrt{a+bx} \sqrt{-ad+bdx}} dx$$

Optimal. Leaf size=39

$$\frac{2 \tanh^{-1} \left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{bdx-ad}} \right)}{b\sqrt{d}}$$

[Out] $2 \operatorname{arctanh}(d^{(1/2)}(b*x+a)^{(1/2)} / (b*d*x-a*d)^{(1/2)}) / b/d^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.130$, Rules used = {63, 217, 206}

$$\frac{2 \tanh^{-1} \left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{bdx-ad}} \right)}{b\sqrt{d}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/(\text{Sqrt}[a + b*x]*\text{Sqrt}[-(a*d) + b*d*x]), x]$

[Out] $(2*\text{ArcTanh}[(\text{Sqrt}[d]*\text{Sqrt}[a + b*x])/\text{Sqrt}[-(a*d) + b*d*x]])/(b*\text{Sqrt}[d])$

Rule 63

$\text{Int}[(a_. + (b_.)*(x_)^m)*((c_.) + (d_.)*(x_)^n), x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{p*(m+1)-1}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /; \text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 206

$\text{Int}[(a_. + (b_.)*(x_)^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(1*\text{ArcTanh}[(\text{Rt}[-b, 2]*x)/\text{Rt}[a, 2]])/(\text{Rt}[a, 2]*\text{Rt}[-b, 2]), x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[a/b] \ \&\& \ (\text{GtQ}[a, 0] \ || \ \text{LtQ}[b, 0])$

Rule 217

$\text{Int}[1/\text{Sqrt}[(a_.) + (b_.)*(x_)^2], x_Symbol] \rightarrow \text{Subst}[\text{Int}[1/(1 - b*x^2), x], x, x/\text{Sqrt}[a + b*x^2]] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ !\text{GtQ}[a, 0]$

Rubi steps

$$\int \frac{1}{\sqrt{a+bx}\sqrt{-ad+bdx}} dx = \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{-2ad+dx^2}} dx, x, \sqrt{a+bx}\right)}{b}$$

$$= \frac{2 \operatorname{Subst}\left(\int \frac{1}{1-dx^2} dx, x, \frac{\sqrt{a+bx}}{\sqrt{-ad+bdx}}\right)}{b}$$

$$= \frac{2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{-ad+bdx}}\right)}{b\sqrt{d}}$$

Mathematica [A] time = 0.02, size = 39, normalized size = 1.00

$$\frac{2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{bdx-ad}}\right)}{b\sqrt{d}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*Sqrt[-(a*d) + b*d*x]), x]

[Out] (2*ArcTanh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[-(a*d) + b*d*x]])/(b*Sqrt[d])

fricas [A] time = 0.46, size = 108, normalized size = 2.77

$$\left[\frac{\log\left(2b^2dx^2 + 2\sqrt{bdx-ad}\sqrt{bx+a}b\sqrt{d}x - a^2d\right)}{2b\sqrt{d}}, -\frac{\sqrt{-d} \arctan\left(\frac{\sqrt{bdx-ad}\sqrt{bx+a}b\sqrt{-d}x}{b^2dx^2 - a^2d}\right)}{bd} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(b*d*x-a*d)^(1/2), x, algorithm="fricas")

[Out] [1/2*log(2*b^2*d*x^2 + 2*sqrt(b*d*x - a*d)*sqrt(b*x + a)*b*sqrt(d)*x - a^2*d)/(b*sqrt(d)), -sqrt(-d)*arctan(sqrt(b*d*x - a*d)*sqrt(b*x + a)*b*sqrt(-d)*x/(b^2*d*x^2 - a^2*d))/(b*d)]

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(b*d*x-a*d)^(1/2), x, algorithm="giac")

[Out] Timed out

maple [B] time = 0.01, size = 76, normalized size = 1.95

$$\frac{\sqrt{(bx+a)(bdx-ad)} \ln\left(\frac{b^2dx}{\sqrt{b^2d}} + \sqrt{b^2dx^2 - a^2d}\right)}{\sqrt{bx+a} \sqrt{bdx-ad} \sqrt{b^2d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(b*d*x-a*d)^(1/2),x)

[Out] ((b*x+a)*(b*d*x-a*d))^(1/2)/(b*x+a)^(1/2)/(b*d*x-a*d)^(1/2)*ln(b^2*d*x/(b^2*d)^(1/2)+(b^2*d*x^2-a^2*d)^(1/2))/(b^2*d)^(1/2)

maxima [A] time = 1.43, size = 39, normalized size = 1.00

$$\frac{\log\left(2b^2dx + 2\sqrt{b^2dx^2 - a^2d}b\sqrt{d}\right)}{b\sqrt{d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(b*d*x-a*d)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*d*x + 2*sqrt(b^2*d*x^2 - a^2*d)*b*sqrt(d))/(b*sqrt(d))

mupad [B] time = 0.22, size = 56, normalized size = 1.44

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{bdx-ad}-\sqrt{-ad})}{\sqrt{-b^2d}(\sqrt{a+bx}-\sqrt{a})}\right)}{\sqrt{-b^2d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*d*x - a*d)^(1/2)*(a + b*x)^(1/2)),x)

[Out] -(4*atan((b*((b*d*x - a*d)^(1/2) - (-a*d)^(1/2)))/((-b^2*d)^(1/2)*((a + b*x)^(1/2) - a^(1/2)))))/(-b^2*d)^(1/2)

sympy [C] time = 4.77, size = 88, normalized size = 2.26

$$\frac{G_{6,6}^{6,2} \left(\begin{matrix} \frac{1}{4}, \frac{3}{4} \\ 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1, 0 \end{matrix} \middle| \begin{matrix} \frac{1}{2}, \frac{1}{2}, 1, 1 \\ \frac{a^2}{b^2x^2} \end{matrix} \right) - iG_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, -\frac{1}{4}, 0, \frac{1}{4}, \frac{1}{2}, 1 \\ -\frac{1}{4}, \frac{1}{4} \end{matrix} \middle| \begin{matrix} -\frac{1}{2}, 0, 0, 0 \\ \frac{a^2 e^{2i\pi}}{b^2x^2} \end{matrix} \right)}{4\pi^{\frac{3}{2}}b\sqrt{d} - 4\pi^{\frac{3}{2}}b\sqrt{d}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(1/2)/(b*d*x-a*d)**(1/2),x)
```

```
[Out] meijerg(((1/4, 3/4), (1/2, 1/2, 1, 1)), ((0, 1/4, 1/2, 3/4, 1, 0), ()), a**  
2/(b**2*x**2))/(4*pi**(3/2)*b*sqrt(d)) - I*meijerg((( -1/2, -1/4, 0, 1/4, 1/  
2, 1), ()), ((-1/4, 1/4), (-1/2, 0, 0, 0)), a**2*exp_polar(2*I*pi)/(b**2*x*  
*2))/(4*pi**(3/2)*b*sqrt(d))
```


$$3.1170 \quad \int \frac{1}{\sqrt[4]{6-3ex} (2+ex)^{3/4}} dx$$

Optimal. Leaf size=241

$$\frac{\log\left(\frac{\sqrt{6-3ex} + \sqrt{3}\sqrt{ex+2} - \sqrt{6}\sqrt[4]{2-ex}\sqrt[4]{ex+2}}{\sqrt{ex+2}}\right)}{\sqrt{2}\sqrt[4]{3}e} + \frac{\log\left(\frac{\sqrt{6-3ex} + \sqrt{3}\sqrt{ex+2} + \sqrt{6}\sqrt[4]{2-ex}\sqrt[4]{ex+2}}{\sqrt{ex+2}}\right)}{\sqrt{2}\sqrt[4]{3}e} + \frac{\sqrt{2}\tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{2-ex}}{\sqrt[4]{ex+2}}\right)}{\sqrt[4]{3}e} - \frac{\sqrt{2}}{\sqrt[4]{3}e}$$

[Out] $-1/6*\ln(3^{(1/2)} - (-e*x+2)^{(1/4)}*6^{(1/2)}/(e*x+2)^{(1/4)} + 3^{(1/2)}*(-e*x+2)^{(1/2)}/(e*x+2)^{(1/2)})*3^{(3/4)}/e*2^{(1/2)} + 1/6*\ln(3^{(1/2)} + (-e*x+2)^{(1/4)}*6^{(1/2)}/(e*x+2)^{(1/4)} + 3^{(1/2)}*(-e*x+2)^{(1/2)}/(e*x+2)^{(1/2)})*3^{(3/4)}/e*2^{(1/2)} - 1/3*\arctan(-1 + (-e*x+2)^{(1/4)}*2^{(1/2)}/(e*x+2)^{(1/4)})*2^{(1/2)}*3^{(3/4)}/e - 1/3*\arctan(1 + (-e*x+2)^{(1/4)}*2^{(1/2)}/(e*x+2)^{(1/4)})*2^{(1/2)}*3^{(3/4)}/e$

Rubi [A] time = 0.25, antiderivative size = 241, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 8, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.400$, Rules used = {63, 331, 297, 1162, 617, 204, 1165, 628}

$$\frac{\log\left(\frac{\sqrt{6-3ex} + \sqrt{3}\sqrt{ex+2} - \sqrt{6}\sqrt[4]{2-ex}\sqrt[4]{ex+2}}{\sqrt{ex+2}}\right)}{\sqrt{2}\sqrt[4]{3}e} + \frac{\log\left(\frac{\sqrt{6-3ex} + \sqrt{3}\sqrt{ex+2} + \sqrt{6}\sqrt[4]{2-ex}\sqrt[4]{ex+2}}{\sqrt{ex+2}}\right)}{\sqrt{2}\sqrt[4]{3}e} + \frac{\sqrt{2}\tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{2-ex}}{\sqrt[4]{ex+2}}\right)}{\sqrt[4]{3}e} - \frac{\sqrt{2}}{\sqrt[4]{3}e}$$

Antiderivative was successfully verified.

[In] Int[1/((6 - 3*e*x)^(1/4)*(2 + e*x)^(3/4)), x]

[Out] $(\text{Sqrt}[2]*\text{ArcTan}[1 - (\text{Sqrt}[2]*(2 - e*x)^{(1/4)})/(2 + e*x)^{(1/4)}])/(3^{(1/4)}*e) - (\text{Sqrt}[2]*\text{ArcTan}[1 + (\text{Sqrt}[2]*(2 - e*x)^{(1/4)})/(2 + e*x)^{(1/4)}])/(3^{(1/4)}*e) - \text{Log}[(\text{Sqrt}[6 - 3*e*x] - \text{Sqrt}[6]*(2 - e*x)^{(1/4)}*(2 + e*x)^{(1/4)} + \text{Sqrt}[3]*\text{Sqrt}[2 + e*x])/(\text{Sqrt}[2 + e*x])]/(\text{Sqrt}[2]*3^{(1/4)}*e) + \text{Log}[(\text{Sqrt}[6 - 3*e*x] + \text{Sqrt}[6]*(2 - e*x)^{(1/4)}*(2 + e*x)^{(1/4)} + \text{Sqrt}[3]*\text{Sqrt}[2 + e*x])/(\text{Sqrt}[2 + e*x])]/(\text{Sqrt}[2]*3^{(1/4)}*e)$

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 204

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[

a, 0] || LtQ[b, 0])

Rule 297

Int[(x_)^2/((a_) + (b_.)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[a/b, 2]], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*s), Int[(r + s*x^2)/(a + b*x^4), x], x] - Dist[1/(2*s), Int[(r - s*x^2)/(a + b*x^4), x], x]] /; FreeQ[{a, b}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] & AtomQ[SplitProduct[SumBaseQ, b]]))

Rule 331

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rule 628

Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]

Rule 1162

Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x], x] + Dist[e/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]

Rule 1165

Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x], x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt[4]{6-3ex}(2+ex)^{3/4}} dx &= -\frac{4 \operatorname{Subst}\left(\int \frac{x^2}{\left(4-\frac{x^4}{3}\right)^{3/4}} dx, x, \sqrt[4]{6-3ex}\right)}{3e} \\
&= -\frac{4 \operatorname{Subst}\left(\int \frac{x^2}{1+\frac{x^4}{3}} dx, x, \frac{\sqrt[4]{6-3ex}}{\sqrt[4]{2+ex}}\right)}{3e} \\
&= \frac{2 \operatorname{Subst}\left(\int \frac{\sqrt{3}-x^2}{1+\frac{x^4}{3}} dx, x, \frac{\sqrt[4]{6-3ex}}{\sqrt[4]{2+ex}}\right)}{3e} - \frac{2 \operatorname{Subst}\left(\int \frac{\sqrt{3}+x^2}{1+\frac{x^4}{3}} dx, x, \frac{\sqrt[4]{6-3ex}}{\sqrt[4]{2+ex}}\right)}{3e} \\
&= -\frac{\operatorname{Subst}\left(\int \frac{1}{\sqrt{3}-\sqrt{2}\sqrt[4]{3}xx^2} dx, x, \frac{\sqrt[4]{6-3ex}}{\sqrt[4]{2+ex}}\right)}{e} - \frac{\operatorname{Subst}\left(\int \frac{1}{\sqrt{3}+\sqrt{2}\sqrt[4]{3}xx^2} dx, x, \frac{\sqrt[4]{6-3ex}}{\sqrt[4]{2+ex}}\right)}{e} \\
&= -\frac{\log\left(\frac{\sqrt{2-ex}-\sqrt{2}\sqrt[4]{2-ex}\sqrt[4]{2+ex}+\sqrt{2+ex}}{\sqrt{2+ex}}\right)}{\sqrt{2}\sqrt[4]{3}e} + \frac{\log\left(\frac{\sqrt{2-ex}+\sqrt{2}\sqrt[4]{2-ex}\sqrt[4]{2+ex}+\sqrt{2+ex}}{\sqrt{2+ex}}\right)}{\sqrt{2}\sqrt[4]{3}e} - \frac{\sqrt{2} \operatorname{Subst}\left(\int \frac{1}{\sqrt{2-ex}} dx, x, \frac{\sqrt[4]{6-3ex}}{\sqrt[4]{2+ex}}\right)}{\sqrt{2}\sqrt[4]{3}e} \\
&= \frac{\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{2-ex}}{\sqrt[4]{2+ex}}\right)}{\sqrt[4]{3}e} - \frac{\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2}\sqrt[4]{2-ex}}{\sqrt[4]{2+ex}}\right)}{\sqrt[4]{3}e} - \frac{\log\left(\frac{\sqrt{2-ex}-\sqrt{2}\sqrt[4]{2-ex}\sqrt[4]{2+ex}}{\sqrt{2+ex}}\right)}{\sqrt{2}\sqrt[4]{3}e}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 42, normalized size = 0.17

$$-\frac{\sqrt{2}(6-3ex)^{3/4} {}_2F_1\left(\frac{3}{4}, \frac{3}{4}; \frac{7}{4}; \frac{1}{12}(6-3ex)\right)}{9e}$$

Antiderivative was successfully verified.

[In] Integrate[1/((6 - 3*e*x)^(1/4)*(2 + e*x)^(3/4)),x]

[Out] -1/9*(Sqrt[2]*(6 - 3*e*x)^(3/4)*Hypergeometric2F1[3/4, 3/4, 7/4, (6 - 3*e*x)/12])/e

fricas [B] time = 0.50, size = 505, normalized size = 2.10

$$2\sqrt{2} \left(\frac{1}{3}\right)^{\frac{1}{4}} \frac{1}{e^4} \arctan \left(\frac{\sqrt{2} \left(\frac{1}{3}\right)^{\frac{3}{4}} (ex+2)^{\frac{1}{4}} (-3ex+6)^{\frac{3}{4}} e^{\frac{3}{4}} - \sqrt{3} \sqrt{2} \left(\frac{1}{3}\right)^{\frac{3}{4}} (e^4x-2e^3) \sqrt{\frac{\sqrt{2} \left(\frac{1}{3}\right)^{\frac{1}{4}} (ex+2)^{\frac{1}{4}} (-3ex+6)^{\frac{3}{4}}}}{ex-2}} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-3*e*x+6)^(1/4)/(e*x+2)^(3/4),x, algorithm="fricas")

[Out] 2*sqrt(2)*(1/3)^(1/4)*(e^(-4))^(1/4)*arctan(-(sqrt(2)*(1/3)^(3/4)*(e*x + 2)^(1/4)*(-3*e*x + 6)^(3/4)*e^3*(e^(-4))^(3/4) - sqrt(3)*sqrt(2)*(1/3)^(3/4)*(e^4*x - 2*e^3)*sqrt((sqrt(2)*(1/3)^(1/4)*(e*x + 2)^(1/4)*(-3*e*x + 6)^(3/4))*e*(e^(-4))^(1/4) + 3*sqrt(1/3)*(e^3*x - 2*e^2)*sqrt(e^(-4)) - sqrt(e*x + 2)*sqrt(-3*e*x + 6))/(e*x - 2))*(e^(-4))^(3/4) + e*x - 2)/(e*x - 2) + 2*sqrt(2)*(1/3)^(1/4)*(e^(-4))^(1/4)*arctan(-(sqrt(2)*(1/3)^(3/4)*(e*x + 2)^(1/4)*(-3*e*x + 6)^(3/4)*e^3*(e^(-4))^(3/4) - sqrt(3)*sqrt(2)*(1/3)^(3/4)*(e^4*x - 2*e^3)*sqrt(-(sqrt(2)*(1/3)^(1/4)*(e*x + 2)^(1/4)*(-3*e*x + 6)^(3/4)*e*(e^(-4))^(1/4) - 3*sqrt(1/3)*(e^3*x - 2*e^2)*sqrt(e^(-4)) + sqrt(e*x + 2)*sqrt(-3*e*x + 6))/(e*x - 2))*(e^(-4))^(3/4) - e*x + 2)/(e*x - 2) - 1/2*sqrt(2)*(1/3)^(1/4)*(e^(-4))^(1/4)*log(3*(sqrt(2)*(1/3)^(1/4)*(e*x + 2)^(1/4)*(-3*e*x + 6)^(3/4)*e*(e^(-4))^(1/4) + 3*sqrt(1/3)*(e^3*x - 2*e^2)*sqrt(e^(-4)) - sqrt(e*x + 2)*sqrt(-3*e*x + 6))/(e*x - 2) + 1/2*sqrt(2)*(1/3)^(1/4)*(e^(-4))^(1/4)*log(-3*(sqrt(2)*(1/3)^(1/4)*(e*x + 2)^(1/4)*(-3*e*x + 6)^(3/4)*e*(e^(-4))^(1/4) - 3*sqrt(1/3)*(e^3*x - 2*e^2)*sqrt(e^(-4)) + sqrt(e*x + 2)*sqrt(-3*e*x + 6))/(e*x - 2))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ex+2)^{\frac{3}{4}}(-3ex+6)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-3*e*x+6)^(1/4)/(e*x+2)^(3/4),x, algorithm="giac")

[Out] integrate(1/((e*x + 2)^(3/4)*(-3*e*x + 6)^(1/4)), x)

maple [F] time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{1}{(-3ex+6)^{\frac{1}{4}}(ex+2)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-3*e*x+6)^(1/4)/(e*x+2)^(3/4),x)`

[Out] `int(1/(-3*e*x+6)^(1/4)/(e*x+2)^(3/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ex+2)^{\frac{3}{4}}(-3ex+6)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-3*e*x+6)^(1/4)/(e*x+2)^(3/4),x, algorithm="maxima")`

[Out] `integrate(1/((e*x + 2)^(3/4)*(-3*e*x + 6)^(1/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(ex+2)^{\frac{3}{4}}(6-3ex)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((e*x + 2)^(3/4)*(6 - 3*e*x)^(1/4)),x)`

[Out] `int(1/((e*x + 2)^(3/4)*(6 - 3*e*x)^(1/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{3^{\frac{3}{4}} \int \frac{1}{\sqrt[4]{-ex+2}(ex+2)^{\frac{3}{4}}} dx}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-3*e*x+6)**(1/4)/(e*x+2)**(3/4),x)`

[Out] `3**(3/4)*Integral(1/((-e*x + 2)**(1/4)*(e*x + 2)**(3/4)), x)/3`

$$3.1171 \quad \int \frac{(a-iax)^{7/4}}{\sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=144

$$-\frac{14a^2\sqrt{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{5\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{14a^2x}{5\sqrt[4]{a-iax}\sqrt[4]{a+iax}} - \frac{14}{15}i(a-iax)^{3/4}(a+iax)^{3/4} - \frac{2i(a-iax)^{7/4}(a+iax)^{3/4}}{5a}$$

[Out] $14/5*a^2*x/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}-14/15*I*(a-I*a*x)^{(3/4)}*(a+I*a*x)^{(3/4)}-2/5*I*(a-I*a*x)^{(7/4)}*(a+I*a*x)^{(3/4)}/a-14/5*a^2*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.03, antiderivative size = 144, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 42, 229, 227, 196}

$$-\frac{14a^2\sqrt{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{5\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{14a^2x}{5\sqrt[4]{a-iax}\sqrt[4]{a+iax}} - \frac{14}{15}i(a-iax)^{3/4}(a+iax)^{3/4} - \frac{2i(a-iax)^{7/4}(a+iax)^{3/4}}{5a}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a - I*a*x)^{(7/4)}/(a + I*a*x)^{(1/4)}, x]$

[Out] $(14*a^2*x)/(5*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)}) - ((14*I)/15)*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)} - (((2*I)/5)*(a - I*a*x)^{(7/4)}*(a + I*a*x)^{(3/4)})/a - (14*a^2*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/((5*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Dist}[(a + b*x)^{\text{FracPart}[m]}*(c + d*x)^{\text{FracPart}[n]}/(a*c + b*d*x^2)^{\text{FracPart}[m]}, \text{Int}[(a*c + b*d*x^2)^m, x], x] /; \text{FreeQ}\{a, b, c, d, m\}, x \&\& \text{EqQ}[b*c + a*d, 0] \&\& \text{IntegerQ}[2*m]$

Rule 50

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /; \text{FreeQ}\{a, b, c, d\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{GtQ}[n, 0] \&\& \text{NeQ}[m+n+1, 0] \&\& \text{!(IGtQ}[m, 0] \&\& \text{(!IntegerQ}[n] || (\text{GtQ}[m, 0] \&\& \text{LtQ}[m-n, 0])) \&\& \text{!ILtQ}[m+n$

+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 196

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 227

Int[((a_) + (b_.)*(x_)^2)^(-1/4), x_Symbol] := Simp[(2*x)/(a + b*x^2)^(1/4), x] - Dist[a, Int[1/(a + b*x^2)^(5/4), x], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 229

Int[((a_) + (b_.)*(x_)^2)^(-1/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a + b*x^2)^(1/4), Int[1/(1 + (b*x^2)/a)^(1/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a]

Rubi steps

$$\begin{aligned}
 \int \frac{(a - iax)^{7/4}}{\sqrt[4]{a + iax}} dx &= -\frac{2i(a - iax)^{7/4}(a + iax)^{3/4}}{5a} + \frac{1}{5}(7a) \int \frac{(a - iax)^{3/4}}{\sqrt[4]{a + iax}} dx \\
 &= -\frac{14}{15}i(a - iax)^{3/4}(a + iax)^{3/4} - \frac{2i(a - iax)^{7/4}(a + iax)^{3/4}}{5a} + \frac{1}{5}(7a^2) \int \frac{1}{\sqrt[4]{a - iax}\sqrt[4]{a + iax}} dx \\
 &= -\frac{14}{15}i(a - iax)^{3/4}(a + iax)^{3/4} - \frac{2i(a - iax)^{7/4}(a + iax)^{3/4}}{5a} + \frac{(7a^2\sqrt[4]{a^2 + a^2x^2}) \int \frac{1}{\sqrt[4]{a^2 + a^2x^2}} dx}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}} \\
 &= -\frac{14}{15}i(a - iax)^{3/4}(a + iax)^{3/4} - \frac{2i(a - iax)^{7/4}(a + iax)^{3/4}}{5a} + \frac{(7a^2\sqrt[4]{1 + x^2}) \int \frac{1}{\sqrt[4]{1 + x^2}} dx}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}} \\
 &= \frac{14a^2x}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}} - \frac{14}{15}i(a - iax)^{3/4}(a + iax)^{3/4} - \frac{2i(a - iax)^{7/4}(a + iax)^{3/4}}{5a} - \frac{(7a^2\sqrt[4]{1 + x^2})}{5\sqrt[4]{a - iax}} \\
 &= \frac{14a^2x}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}} - \frac{14}{15}i(a - iax)^{3/4}(a + iax)^{3/4} - \frac{2i(a - iax)^{7/4}(a + iax)^{3/4}}{5a} - \frac{14a^2\sqrt[4]{1 + x^2}}{5\sqrt[4]{a - iax}}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 70, normalized size = 0.49

$$\frac{2i2^{3/4}\sqrt[4]{1+ix}(a-iax)^{11/4}{}_2F_1\left(\frac{1}{4}, \frac{11}{4}; \frac{15}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{11a\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(7/4)/(a + I*a*x)^(1/4), x]

[Out] (((2*I)/11)*2^(3/4)*(1 + I*x)^(1/4)*(a - I*a*x)^(11/4)*Hypergeometric2F1[1/4, 11/4, 15/4, 1/2 - (I/2)*x])/(a*(a + I*a*x)^(1/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\frac{2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}(3x^2+10ix-21) - 15x \operatorname{integral}\left(\frac{14(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{5(x^4+x^2)}, x\right)}{15x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(1/4), x, algorithm="fricas")

[Out] -1/15*(2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*(3*x^2 + 10*I*x - 21) - 15*x*integral(14/5*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(x^4 + x^2), x))/x

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(1/4), x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command: INPUT:sage2OUTPUT:Warning, choosing root of [1,0,0,0,%%{-2, [1,0]%%}+%%{1, [0,4]%%}] at parameters values [-49,-86]Warning, choosing root of [1,0,0,0,%%{-2, [1,0]%%}+%%{1, [0,4]%%}] at parameters values [-64,-30]Warning, choosing root of [1,0,0,0,%%{-2, [1,0]%%}+%%{1, [0,4]%%}] at parameters values [70,22]Warning, choosing root of [1,0,0,0,%%{-2, [1,0]%%}+%%{1, [0,4]%%}] at parameters values [42,56]ext_reduce Error: Bad Argument TypeEvaluation time: 0.58integrate(i/4*a*(-i)/a^2*(16*i*((i*a*x+a)^(1/4))^6*((2*a-((i*a*x+a)^(1/4))^4)^(1/4))^3+(-32*i)*a*((i*a*x+a)^(1/4))^2*((2*a-((i*a*x+a)^(1/4))^4)^(1/4))^3)/4*i*a*((i*a*x+a)^(1/4))^-3,x)

maple [C] time = 0.10, size = 104, normalized size = 0.72

$$\frac{7(-ix-1)(ix+1)a^2)^{\frac{1}{4}} a^2 x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{5(a^2)^{\frac{1}{4}}(-ix-1)a^{\frac{1}{4}}(ix+1)a^{\frac{1}{4}}} - \frac{2(3x+10i)(x-i)(x+i)a^2}{15(-ix-1)a^{\frac{1}{4}}(ix+1)a^{\frac{1}{4}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a-I*a*x)^(7/4)/(a+I*a*x)^(1/4), x)`

[Out] `-2/15*(10*I+3*x)*(x-I)*(x+I)*a^2/(-a*(-1+I*x))^(1/4)/(a*(I*x+1))^(1/4)+7/5/(a^2)^(1/4)*x*hypergeom([1/4, 1/2], [3/2], -x^2)*a^2*(-a^2*(-1+I*x)*(I*x+1))^(1/4)/(-a*(-1+I*x))^(1/4)/(a*(I*x+1))^(1/4)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax+a)^{\frac{7}{4}}}{(iax+a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(1/4), x, algorithm="maxima")`

[Out] `integrate((-I*a*x + a)^(7/4)/(I*a*x + a)^(1/4), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a-ax1i)^{7/4}}{(a+ax1i)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - a*x*1i)^(7/4)/(a + a*x*1i)^(1/4), x)`

[Out] `int((a - a*x*1i)^(7/4)/(a + a*x*1i)^(1/4), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-ia(x+i))^{\frac{7}{4}}}{\sqrt[4]{ia(x-i)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)**(7/4)/(a+I*a*x)**(1/4), x)`

[Out] `Integral((-I*a*(x + I))**(7/4)/(I*a*(x - I))**(1/4), x)`

$$3.1172 \quad \int \frac{(a-iax)^{3/4}}{\sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=106

$$-\frac{2a\sqrt[4]{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{2ax}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} - \frac{2i(a-iax)^{3/4}(a+iax)^{3/4}}{3a}$$

[Out] $2*a*x/(a-I*a*x)^{(1/4)/(a+I*a*x)^{(1/4)}-2/3*I*(a-I*a*x)^{(3/4)*(a+I*a*x)^{(3/4)}}$
 $/a-2*a*(x^2+1)^{(1/4)*(\cos(1/2*arctan(x))^2)^{(1/2)/\cos(1/2*arctan(x))*EllipticE(\sin(1/2*arctan(x)),2^{(1/2)))/(a-I*a*x)^{(1/4)/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 106, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {50, 42, 229, 227, 196}

$$-\frac{2a\sqrt[4]{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{2ax}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} - \frac{2i(a-iax)^{3/4}(a+iax)^{3/4}}{3a}$$

Antiderivative was successfully verified.

[In] Int[(a - I*a*x)^(3/4)/(a + I*a*x)^(1/4), x]

[Out] $(2*a*x)/((a - I*a*x)^{(1/4)*(a + I*a*x)^{(1/4)}) - (((2*I)/3)*(a - I*a*x)^{(3/4)*(a + I*a*x)^{(3/4)})/a - (2*a*(1 + x^2)^{(1/4)*EllipticE[ArcTan[x]/2, 2]}/((a - I*a*x)^{(1/4)*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[n])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 50

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 196

```
Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 227

```
Int[((a_) + (b_.)*(x_)^2)^(-1/4), x_Symbol] := Simp[(2*x)/(a + b*x^2)^(1/4)
, x] - Dist[a, Int[1/(a + b*x^2)^(5/4), x], x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 229

```
Int[((a_) + (b_.)*(x_)^2)^(-1/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(
a + b*x^2)^(1/4), Int[1/(1 + (b*x^2)/a)^(1/4), x], x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a - iax)^{3/4}}{\sqrt[4]{a + iax}} dx &= -\frac{2i(a - iax)^{3/4}(a + iax)^{3/4}}{3a} + a \int \frac{1}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} dx \\
&= -\frac{2i(a - iax)^{3/4}(a + iax)^{3/4}}{3a} + \frac{\left(a \sqrt[4]{a^2 + a^2x^2}\right) \int \frac{1}{\sqrt[4]{a^2 + a^2x^2}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= -\frac{2i(a - iax)^{3/4}(a + iax)^{3/4}}{3a} + \frac{\left(a \sqrt[4]{1 + x^2}\right) \int \frac{1}{\sqrt[4]{1 + x^2}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= \frac{2ax}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} - \frac{2i(a - iax)^{3/4}(a + iax)^{3/4}}{3a} - \frac{\left(a \sqrt[4]{1 + x^2}\right) \int \frac{1}{(1+x^2)^{5/4}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= \frac{2ax}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} - \frac{2i(a - iax)^{3/4}(a + iax)^{3/4}}{3a} - \frac{2a \sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.66

$$\frac{2i2^{3/4} \sqrt[4]{1 + ix} (a - iax)^{7/4} {}_2F_1\left(\frac{1}{4}, \frac{7}{4}; \frac{11}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{7a \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(3/4)/(a + I*a*x)^(1/4), x]

[Out] (((2*I)/7)*2^(3/4)*(1 + I*x)^(1/4)*(a - I*a*x)^(7/4)*Hypergeometric2F1[1/4, 7/4, 11/4, 1/2 - (I/2)*x])/(a*(a + I*a*x)^(1/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\frac{3ax \operatorname{integral}\left(\frac{2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{ax^4+ax^2}, x\right) - 2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}(ix-3)}{3ax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(1/4), x, algorithm="fricas")

[Out] 1/3*(3*a*x*integral(2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a*x^4 + a*x^2), x) - 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*(I*x - 3))/(a*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax+a)^{\frac{3}{4}}}{(iax+a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(1/4), x, algorithm="giac")

[Out] integrate((-I*a*x + a)^(3/4)/(I*a*x + a)^(1/4), x)

maple [C] time = 0.07, size = 94, normalized size = 0.89

$$\frac{(-ix-1)(ix+1)a^2)^{\frac{1}{4}} ax \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{(a^2)^{\frac{1}{4}} (-ix-1)a^{\frac{1}{4}} ((ix+1)a)^{\frac{1}{4}}} - \frac{2i(x-i)(x+i)a}{3(-ix-1)a^{\frac{1}{4}} ((ix+1)a)^{\frac{1}{4}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a-I*a*x)^(3/4)/(a+I*a*x)^(1/4), x)

[Out] -2/3*I*(x-I)*(x+I)*a/((-I*x-1)*a)^(1/4)/(((I*x+1)*a)^(1/4)+1/(a^2)^(1/4))*x*hypergeom([1/4, 1/2], [3/2], -x^2)*a*(-(I*x-1)*(I*x+1)*a^2)^(1/4)/((-I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax+a)^{\frac{3}{4}}}{(iax+a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(3/4)/(I*a*x + a)^(1/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - a x 1i)^{3/4}}{(a + a x 1i)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - a*x*1i)^(3/4)/(a + a*x*1i)^(1/4),x)

[Out] int((a - a*x*1i)^(3/4)/(a + a*x*1i)^(1/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-ia(x+i))^{3/4}}{\sqrt[4]{ia(x-i)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)**(3/4)/(a+I*a*x)**(1/4),x)

[Out] Integral((-I*a*(x + I))**(3/4)/(I*a*(x - I))**(1/4), x)

$$3.1173 \quad \int \frac{1}{\sqrt[4]{a-iax} \sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=71

$$\frac{2x}{\sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{\sqrt[4]{a-iax} \sqrt[4]{a+iax}}$$

[Out] $2*x/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}-2*(x^2+1)^{(1/4)*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.01, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {42, 229, 227, 196}

$$\frac{2x}{\sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{\sqrt[4]{a-iax} \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(1/4)*(a + I*a*x)^(1/4)),x]

[Out] $(2*x)/((a - I*a*x)^{(1/4)*(a + I*a*x)^{(1/4)}) - (2*(1 + x^2)^{(1/4)*\text{EllipticE}[\text{ArcTan}[x]/2, 2]})/((a - I*a*x)^{(1/4)*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_.)*(x_)^(m_))*((c_) + (d_.)*(x_)^(m_)), x_Symbol] :> Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 196

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] :> Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 227

Int[((a_) + (b_.)*(x_)^2)^(-1/4), x_Symbol] :> Simp[(2*x)/(a + b*x^2)^(1/4), x] - Dist[a, Int[1/(a + b*x^2)^(5/4), x], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 229

Int[((a_) + (b_.)*(x_)^2)^(-1/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a + b*x^2)^(1/4), Int[1/(1 + (b*x^2)/a)^(1/4), x], x] /; FreeQ[{a, b}, x] & PosQ[a]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} dx &= \frac{\sqrt[4]{a^2+a^2x^2} \int \frac{1}{\sqrt[4]{a^2+a^2x^2}} dx}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\ &= \frac{\sqrt[4]{1+x^2} \int \frac{1}{\sqrt[4]{1+x^2}} dx}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\ &= \frac{2x}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} - \frac{\sqrt[4]{1+x^2} \int \frac{1}{(1+x^2)^{5/4}} dx}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\ &= \frac{2x}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} - \frac{2\sqrt[4]{1+x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.99

$$\frac{2i2^{3/4}\sqrt[4]{1+ix}(a-iax)^{3/4} {}_2F_1\left(\frac{1}{4}, \frac{3}{4}; \frac{7}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{3a\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(1/4)*(a + I*a*x)^(1/4)), x]

[Out] (((2*I)/3)*2^(3/4)*(1 + I*x)^(1/4)*(a - I*a*x)^(3/4)*Hypergeometric2F1[1/4, 3/4, 7/4, 1/2 - (I/2)*x])/(a*(a + I*a*x)^(1/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\frac{a^2 x \operatorname{integral}\left(\frac{2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{a^2x^4+a^2x^2}, x\right) + 2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{a^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(1/4), x, algorithm="fricas")

[Out] $(a^2*x*\text{integral}(2*(I*a*x + a)^{(3/4)}*(-I*a*x + a)^{(3/4)}/(a^2*x^4 + a^2*x^2), x) + 2*(I*a*x + a)^{(3/4)}*(-I*a*x + a)^{(3/4)})/(a^2*x)$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(1/4),x, algorithm="giac")`

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command: INPUT:sage2OUTPUT:Warning, choosing root of [1,0,0,0,%%{-i,[1,1]%%}+%%{-1,[1,0]%%}] at parameters values [-27,-87]ext_reduce Error: Bad Argument Typeintegrate((-4*i)/a/4*i*a*(-4*i)/a*((i*a*x+a)^(1/4))^2/(-(i*a*x+a)^(1/4))^4+2*a)^(1/4)/4*i*a*((i*a*x+a)^(1/4))^3,x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(-iax + a)^{\frac{1}{4}}(iax + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(1/4),x)`

[Out] `int(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(1/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")`

[Out] `integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a*x*1i)^{1/4}(a + a*x*1i)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(1/4)*(a + a*x*1i)^(1/4)),x)`

[Out] `int(1/((a - a*x*1i)^(1/4)*(a + a*x*1i)^(1/4)), x)`

sympy [A] time = 3.79, size = 102, normalized size = 1.44

$$\frac{iG_{6,6}^{5,3} \left(\begin{matrix} \frac{1}{8}, \frac{5}{8}, 1 \\ -\frac{1}{4}, \frac{1}{8}, \frac{1}{4}, \frac{5}{8}, \frac{3}{4} \end{matrix} \middle| \frac{e^{-3i\pi}}{x^2} \right) e^{\frac{i\pi}{4}}}{4\pi\sqrt{a}\Gamma\left(\frac{1}{4}\right)} + \frac{iG_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, -\frac{3}{8}, 0, \frac{1}{8}, \frac{1}{2}, 1 \\ -\frac{3}{8}, \frac{1}{8} \end{matrix} \middle| \frac{e^{-i\pi}}{x^2} \right)}{4\pi\sqrt{a}\Gamma\left(\frac{1}{4}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(1/4)/(a+I*a*x)**(1/4),x)`

[Out] `-I*meijerg(((1/8, 5/8, 1), (1/4, 1/2, 3/4)), ((-1/4, 1/8, 1/4, 5/8, 3/4), (0,)), exp_polar(-3*I*pi)/x**2)*exp(I*pi/4)/(4*pi*sqrt(a)*gamma(1/4)) + I*meijerg(((1/2, -3/8, 0, 1/8, 1/2, 1), ()), ((-3/8, 1/8), (-1/2, -1/4, 0, 0)), exp_polar(-I*pi)/x**2)/(4*pi*sqrt(a)*gamma(1/4))`

$$3.1174 \quad \int \frac{1}{(a-iax)^{5/4} \sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=78

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{a\sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{2i}{a\sqrt[4]{a-iax} \sqrt[4]{a+iax}}$$

[Out] $-2*I/a/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}+2*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x)))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {48, 42, 197, 196}

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{a\sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{2i}{a\sqrt[4]{a-iax} \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(5/4)*(a + I*a*x)^(1/4)), x]

[Out] $(-2*I)/(a*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)}) + (2*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(a*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 48

Int[1/(((a_) + (b_.)*(x_))^(5/4)*((c_) + (d_.)*(x_))^(1/4)), x_Symbol] := Simp[-2/(b*(a + b*x)^(1/4)*(c + d*x)^(1/4)), x] + Dist[c, Int[1/((a + b*x)^(5/4)*(c + d*x)^(5/4)), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && NegQ[a^2*b^2]

Rule 196

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a

, 0] && PosQ[b/a]

Rule 197

Int[((a_) + (b_)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a] && PosQ[b/a]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a - iax)^{5/4} \sqrt[4]{a + iax}} dx &= -\frac{2i}{a \sqrt[4]{a - iax} \sqrt[4]{a + iax}} + a \int \frac{1}{(a - iax)^{5/4} (a + iax)^{5/4}} dx \\ &= -\frac{2i}{a \sqrt[4]{a - iax} \sqrt[4]{a + iax}} + \frac{\left(a \sqrt[4]{a^2 + a^2 x^2}\right) \int \frac{1}{(a^2 + a^2 x^2)^{5/4}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\ &= -\frac{2i}{a \sqrt[4]{a - iax} \sqrt[4]{a + iax}} + \frac{\sqrt[4]{1 + x^2} \int \frac{1}{(1 + x^2)^{5/4}} dx}{a \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\ &= -\frac{2i}{a \sqrt[4]{a - iax} \sqrt[4]{a + iax}} + \frac{2 \sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{a \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \end{aligned}$$

Mathematica [C] time = 0.02, size = 68, normalized size = 0.87

$$-\frac{2i 2^{3/4} \sqrt[4]{1 + ix} {}_2F_1\left(-\frac{1}{4}, \frac{1}{4}, \frac{3}{4}, \frac{1}{2} - \frac{ix}{2}\right)}{a \sqrt[4]{a - iax} \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(5/4)*(a + I*a*x)^(1/4)),x]

[Out] ((-2*I)*2^(3/4)*(1 + I*x)^(1/4)*Hypergeometric2F1[-1/4, 1/4, 3/4, 1/2 - (I/2)*x])/(a*(a - I*a*x)^(1/4)*(a + I*a*x)^(1/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\frac{(a^3 x^2 + i a^3 x) \operatorname{integral}\left(-\frac{2(i a x + a)^{\frac{3}{4}}(-i a x + a)^{\frac{3}{4}}}{a^3 x^4 + a^3 x^2}, x\right) - 2i(i a x + a)^{\frac{3}{4}}(-i a x + a)^{\frac{3}{4}}}{a^3 x^2 + i a^3 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(1/4),x, algorithm="fricas")

[Out] ((a^3*x^2 + I*a^3*x)*integral(-2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^3*x^4 + a^3*x^2), x) - 2*I*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4))/(a^3*x^2 + I*a^3*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{1}{4}} (-i a x + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(1/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(5/4)), x)

maple [C] time = 0.07, size = 94, normalized size = 1.21

$$-\frac{(-ix-1)(ix+1)a^2)^{\frac{1}{4}} x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{(a^2)^{\frac{1}{4}} (-ix-1)a^{\frac{1}{4}} ((ix+1)a)^{\frac{1}{4}} a} + \frac{2x-2i}{(-ix-1)a^{\frac{1}{4}} ((ix+1)a)^{\frac{1}{4}} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(5/4)/(I*a*x+a)^(1/4),x)

[Out] 2*(x-I)/a/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)-1/(a^2)^(1/4)*x*hypergeom([1/4, 1/2], [3/2], -x^2)/a*(-(I*x-1)*(I*x+1)*a^2)^(1/4)/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{1}{4}} (-i a x + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(5/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{5/4} (a + a x 1i)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*I)**(5/4)*(a + a*x*I)**(1/4)),x)`

[Out] `int(1/((a - a*x*I)**(5/4)*(a + a*x*I)**(1/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[4]{ia(x-i)} (-ia(x+i))^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(5/4)/(a+I*a*x)**(1/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(1/4)*(-I*a*(x + I))**(5/4)), x)`

$$3.1175 \quad \int \frac{1}{(a-iax)^{9/4} \sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=82

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^2 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{4i}{5a(a-iax)^{5/4} \sqrt[4]{a+iax}}$$

[Out] $-4/5*I/a/(a-I*a*x)^{(5/4)}/(a+I*a*x)^{(1/4)}+2/5*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x)))^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a^2/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {46, 42, 197, 196}

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^2 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{4i}{5a(a-iax)^{5/4} \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(9/4)*(a + I*a*x)^(1/4)),x]

[Out] $((-4*I)/5)/(a*(a - I*a*x)^{(5/4)}*(a + I*a*x)^{(1/4)}) + (2*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(5*a^2*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 46

Int[1/(((a_) + (b_.)*(x_))^(9/4)*((c_) + (d_.)*(x_))^(1/4)), x_Symbol] :> Simp[-4/(5*b*(a + b*x)^(5/4)*(c + d*x)^(1/4)), x] - Dist[d/(5*b), Int[1/((a + b*x)^(5/4)*(c + d*x)^(5/4)), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && NegQ[a^2*b^2]

Rule 196

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] :> Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a

, 0] && PosQ[b/a]

Rule 197

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a] && PosQ[b/a]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a - iax)^{9/4} \sqrt[4]{a + iax}} dx &= -\frac{4i}{5a(a - iax)^{5/4} \sqrt[4]{a + iax}} + \frac{1}{5} \int \frac{1}{(a - iax)^{5/4} (a + iax)^{5/4}} dx \\ &= -\frac{4i}{5a(a - iax)^{5/4} \sqrt[4]{a + iax}} + \frac{\sqrt[4]{a^2 + a^2x^2} \int \frac{1}{(a^2 + a^2x^2)^{5/4}} dx}{5\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\ &= -\frac{4i}{5a(a - iax)^{5/4} \sqrt[4]{a + iax}} + \frac{\sqrt[4]{1 + x^2} \int \frac{1}{(1+x^2)^{5/4}} dx}{5a^2 \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\ &= -\frac{4i}{5a(a - iax)^{5/4} \sqrt[4]{a + iax}} + \frac{2\sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^2 \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.85

$$\frac{2i2^{3/4} \sqrt[4]{1 + ix} {}_2F_1\left(-\frac{5}{4}, \frac{1}{4}; -\frac{1}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{5a(a - iax)^{5/4} \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(9/4)*(a + I*a*x)^(1/4)), x]

[Out] (((-2*I)/5)*2^(3/4)*(1 + I*x)^(1/4)*Hypergeometric2F1[-5/4, 1/4, -1/4, 1/2 - (I/2)*x])/(a*(a - I*a*x)^(5/4)*(a + I*a*x)^(1/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\frac{(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}}(2x + 4i) + (5a^4x^2 + 10ia^4x - 5a^4)\text{integral}\left(-\frac{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{5(a^4x^2+a^4)}, x\right)}{5a^4x^2 + 10ia^4x - 5a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(1/4),x, algorithm="fricas")

[Out] ((I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*(2*x + 4*I) + (5*a^4*x^2 + 10*I*a^4*x - 5*a^4)*integral(-1/5*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^4*x^2 + a^4), x))/(5*a^4*x^2 + 10*I*a^4*x - 5*a^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{1}{4}}(-i a x + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(1/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(9/4)), x)

maple [C] time = 0.08, size = 105, normalized size = 1.28

$$\frac{(-i x - 1)(i x + 1) a^2)^{\frac{1}{4}} x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{5 (a^2)^{\frac{1}{4}} (-i x - 1) a^{\frac{1}{4}} ((i x + 1) a)^{\frac{1}{4}} a^2} + \frac{\frac{2}{5} x^2 + \frac{2}{5} i x + \frac{4}{5}}{(x + i) (-i x - 1) a^{\frac{1}{4}} ((i x + 1) a)^{\frac{1}{4}} a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(9/4)/(I*a*x+a)^(1/4),x)

[Out] 2/5*(x^2+2+I*x)/(x+I)/a^2/(-I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)-1/5/(a^2)^(1/4)*x*hypergeom([1/4,1/2],[3/2],-x^2)/a^2*(-I*x-1)*(I*x+1)*a^2)^(1/4)/(-I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{1}{4}}(-i a x + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(9/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{9/4} (a + a x 1i)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*I)**(9/4)*(a + a*x*I)**(1/4)),x)`

[Out] `int(1/((a - a*x*I)**(9/4)*(a + a*x*I)**(1/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[4]{ia(x-i)} (-ia(x+i))^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(9/4)/(a+I*a*x)**(1/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(1/4)*(-I*a*(x + I))**(9/4)), x)`

$$3.1176 \quad \int \frac{1}{(a-iax)^{13/4} \sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=115

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{15a^3 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{2i(a+iax)^{3/4}}{9a^2(a-iax)^{9/4}} - \frac{4i}{15a^2(a-iax)^{5/4} \sqrt[4]{a+iax}}$$

[Out] $-4/15*I/a^2/(a-I*a*x)^{(5/4)}/(a+I*a*x)^{(1/4)}-2/9*I*(a+I*a*x)^{(3/4)}/a^2/(a-I*a*x)^{(9/4)}+2/15*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a^3/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.03, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 46, 42, 197, 196}

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{15a^3 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{2i(a+iax)^{3/4}}{9a^2(a-iax)^{9/4}} - \frac{4i}{15a^2(a-iax)^{5/4} \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(13/4)*(a + I*a*x)^(1/4)), x]

[Out] $((-4*I)/15)/(a^2*(a - I*a*x)^{(5/4)}*(a + I*a*x)^{(1/4)}) - (((2*I)/9)*(a + I*a*x)^{(3/4)})/(a^2*(a - I*a*x)^{(9/4)}) + (2*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(15*a^3*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 46

Int[1/(((a_) + (b_.)*(x_))^(9/4)*((c_) + (d_.)*(x_))^(1/4)), x_Symbol] := Simp[-4/(5*b*(a + b*x)^(5/4)*(c + d*x)^(1/4)), x] - Dist[d/(5*b), Int[1/((a + b*x)^(5/4)*(c + d*x)^(5/4)), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && NegQ[a^2*b^2]

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 196

```
Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 197

```
Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(
a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b},
x] && PosQ[a] && PosQ[b/a]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a - iax)^{13/4} \sqrt[4]{a + iax}} dx &= -\frac{2i(a + iax)^{3/4}}{9a^2(a - iax)^{9/4}} + \frac{\int \frac{1}{(a - iax)^{9/4} \sqrt[4]{a + iax}} dx}{3a} \\
&= -\frac{4i}{15a^2(a - iax)^{5/4} \sqrt[4]{a + iax}} - \frac{2i(a + iax)^{3/4}}{9a^2(a - iax)^{9/4}} + \frac{\int \frac{1}{(a - iax)^{5/4} (a + iax)^{5/4}} dx}{15a} \\
&= -\frac{4i}{15a^2(a - iax)^{5/4} \sqrt[4]{a + iax}} - \frac{2i(a + iax)^{3/4}}{9a^2(a - iax)^{9/4}} + \frac{\sqrt[4]{a^2 + a^2x^2} \int \frac{1}{(a^2 + a^2x^2)^{5/4}} dx}{15a \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= -\frac{4i}{15a^2(a - iax)^{5/4} \sqrt[4]{a + iax}} - \frac{2i(a + iax)^{3/4}}{9a^2(a - iax)^{9/4}} + \frac{\sqrt[4]{1 + x^2} \int \frac{1}{(1 + x^2)^{5/4}} dx}{15a^3 \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= -\frac{4i}{15a^2(a - iax)^{5/4} \sqrt[4]{a + iax}} - \frac{2i(a + iax)^{3/4}}{9a^2(a - iax)^{9/4}} + \frac{2\sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{15a^3 \sqrt[4]{a - iax} \sqrt[4]{a + iax}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.61

$$\frac{2i2^{3/4} \sqrt[4]{1 + ix} {}_2F_1\left(-\frac{9}{4}, \frac{1}{4}; -\frac{5}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{9a(a - iax)^{9/4} \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(13/4)*(a + I*a*x)^(1/4)), x]

[Out] (((-2*I)/9)*2^(3/4)*(1 + I*x)^(1/4)*Hypergeometric2F1[-9/4, 1/4, -5/4, 1/2 - (I/2)*x])/(a*(a - I*a*x)^(9/4)*(a + I*a*x)^(1/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\frac{2(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}}(3x^2 + 9ix - 11) + (45a^5x^3 + 135ia^5x^2 - 135a^5x - 45ia^5)\operatorname{integral}\left(-\frac{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{15(a^5x^2+a^5)},\right)}{45a^5x^3 + 135ia^5x^2 - 135a^5x - 45ia^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(1/4), x, algorithm="fricas")

[Out] (2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*(3*x^2 + 9*I*x - 11) + (45*a^5*x^3 + 135*I*a^5*x^2 - 135*a^5*x - 45*I*a^5)*integral(-1/15*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^5*x^2 + a^5), x))/(45*a^5*x^3 + 135*I*a^5*x^2 - 135*a^5*x - 45*I*a^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{13}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(1/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(13/4)), x)

maple [C] time = 0.08, size = 113, normalized size = 0.98

$$\frac{(-ix - 1)(ix + 1)a^2)^{\frac{1}{4}} x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{15(a^2)^{\frac{1}{4}}(-ix - 1)a^{\frac{1}{4}}((ix + 1)a)^{\frac{1}{4}}a^3} + \frac{\frac{2}{15}x^3 + \frac{4}{15}ix^2 - \frac{4}{45}x + \frac{22}{45}i}{(x + i)^2(-ix - 1)a^{\frac{1}{4}}((ix + 1)a)^{\frac{1}{4}}a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(13/4)/(I*a*x+a)^(1/4), x)

[Out] 2/45*(6*I*x^2+3*x^3-2*x+11*I)/(x+I)^2/a^3/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)-1/15/(a^2)^(1/4)*x*hypergeom([1/4, 1/2], [3/2], -x^2)/a^3*(-(I*x-1)*(I*x+1)*a^2)^(1/4)/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{1}{4}} (-i a x + a)^{\frac{13}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(13/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{13/4} (a + a x 1i)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(13/4)*(a + a*x*1i)^(1/4)),x)

[Out] int(1/((a - a*x*1i)^(13/4)*(a + a*x*1i)^(1/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[4]{ia(x-i)} (-ia(x+i))^{\frac{13}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(13/4)/(a+I*a*x)**(1/4),x)

[Out] Integral(1/((I*a*(x - I))**(1/4)*(-I*a*(x + I))**(13/4)), x)

$$3.1177 \quad \int \frac{1}{(a-iax)^{17/4} \sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=148

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{39a^4 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{10i(a+iax)^{3/4}}{117a^3(a-iax)^{9/4}} - \frac{4i}{39a^3(a-iax)^{5/4} \sqrt[4]{a+iax}} - \frac{2i(a+iax)^{3/4}}{13a^2(a-iax)^{13/4}}$$

[Out] $-4/39*I/a^3/(a-I*a*x)^{(5/4)}/(a+I*a*x)^{(1/4)}-2/13*I*(a+I*a*x)^{(3/4)}/a^2/(a-I*a*x)^{(13/4)}-10/117*I*(a+I*a*x)^{(3/4)}/a^3/(a-I*a*x)^{(9/4)}+2/39*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a^4/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.04, antiderivative size = 148, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 46, 42, 197, 196}

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{39a^4 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{10i(a+iax)^{3/4}}{117a^3(a-iax)^{9/4}} - \frac{2i(a+iax)^{3/4}}{13a^2(a-iax)^{13/4}} - \frac{4i}{39a^3(a-iax)^{5/4} \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] `Int[1/((a - I*a*x)^(17/4)*(a + I*a*x)^(1/4)),x]`

[Out] $((-4*I)/39)/(a^3*(a - I*a*x)^{(5/4)}*(a + I*a*x)^{(1/4)}) - (((2*I)/13)*(a + I*a*x)^{(3/4)})/(a^2*(a - I*a*x)^{(13/4)}) - (((10*I)/117)*(a + I*a*x)^{(3/4)})/(a^3*(a - I*a*x)^{(9/4)}) + (2*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(39*a^4*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

`Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]`

Rule 46

`Int[1/(((a_) + (b_.)*(x_))^(9/4)*((c_) + (d_.)*(x_))^(1/4)), x_Symbol] :> Simp[-4/(5*b*(a + b*x)^(5/4)*(c + d*x)^(1/4)), x] - Dist[d/(5*b), Int[1/((a + b*x)^(5/4)*(c + d*x)^(5/4)), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && NegQ[a^2*b^2]`

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 196

```
Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 197

```
Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(
a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b},
x] && PosQ[a] && PosQ[b/a]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a - iax)^{17/4} \sqrt[4]{a + iax}} dx &= -\frac{2i(a + iax)^{3/4}}{13a^2(a - iax)^{13/4}} + \frac{5 \int \frac{1}{(a - iax)^{13/4} \sqrt[4]{a + iax}} dx}{13a} \\
&= -\frac{2i(a + iax)^{3/4}}{13a^2(a - iax)^{13/4}} - \frac{10i(a + iax)^{3/4}}{117a^3(a - iax)^{9/4}} + \frac{5 \int \frac{1}{(a - iax)^{9/4} \sqrt[4]{a + iax}} dx}{39a^2} \\
&= -\frac{4i}{39a^3(a - iax)^{5/4} \sqrt[4]{a + iax}} - \frac{2i(a + iax)^{3/4}}{13a^2(a - iax)^{13/4}} - \frac{10i(a + iax)^{3/4}}{117a^3(a - iax)^{9/4}} + \frac{\int \frac{1}{(a - iax)^{5/4} \sqrt[4]{a + iax}} dx}{39a^2} \\
&= -\frac{4i}{39a^3(a - iax)^{5/4} \sqrt[4]{a + iax}} - \frac{2i(a + iax)^{3/4}}{13a^2(a - iax)^{13/4}} - \frac{10i(a + iax)^{3/4}}{117a^3(a - iax)^{9/4}} + \frac{\int \frac{1}{\sqrt[4]{a^2 + a^2x^2}} dx}{39a^2 \sqrt[4]{a + iax}} \\
&= -\frac{4i}{39a^3(a - iax)^{5/4} \sqrt[4]{a + iax}} - \frac{2i(a + iax)^{3/4}}{13a^2(a - iax)^{13/4}} - \frac{10i(a + iax)^{3/4}}{117a^3(a - iax)^{9/4}} + \frac{\int \frac{1}{\sqrt[4]{1 + x^2}} dx}{39a^4 \sqrt[4]{a + iax}} \\
&= -\frac{4i}{39a^3(a - iax)^{5/4} \sqrt[4]{a + iax}} - \frac{2i(a + iax)^{3/4}}{13a^2(a - iax)^{13/4}} - \frac{10i(a + iax)^{3/4}}{117a^3(a - iax)^{9/4}} + \frac{2\sqrt[4]{1 + x^2} E}{39a^4 \sqrt[4]{a + iax}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.47

$$\frac{2i2^{3/4}\sqrt[4]{1+ix} {}_2F_1\left(-\frac{13}{4}, \frac{1}{4}; -\frac{9}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{13a(a-iax)^{13/4}\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(17/4)*(a + I*a*x)^(1/4)), x]

[Out] (((-2*I)/13)*2^(3/4)*(1 + I*x)^(1/4)*Hypergeometric2F1[-13/4, 1/4, -9/4, 1/2 - (I/2)*x])/(a*(a - I*a*x)^(13/4)*(a + I*a*x)^(1/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\frac{(6x^3 + 24ix^2 - 40x - 40i)(iax + a)^{3/4}(-iax + a)^{3/4} + (117a^6x^4 + 468ia^6x^3 - 702a^6x^2 - 468ia^6x + 117a^6)\text{integral}(117a^6x^4 + 468ia^6x^3 - 702a^6x^2 - 468ia^6x + 117a^6)}{117a^6x^4 + 468ia^6x^3 - 702a^6x^2 - 468ia^6x + 117a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(17/4)/(a+I*a*x)^(1/4), x, algorithm="fricas")

[Out] ((6*x^3 + 24*I*x^2 - 40*x - 40*I)*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4) + (117*a^6*x^4 + 468*I*a^6*x^3 - 702*a^6*x^2 - 468*I*a^6*x + 117*a^6)*integral(-1/39*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^6*x^2 + a^6), x))/(117*a^6*x^4 + 468*I*a^6*x^3 - 702*a^6*x^2 - 468*I*a^6*x + 117*a^6)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{1/4}(-iax + a)^{17/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(17/4)/(a+I*a*x)^(1/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(17/4)), x)

maple [C] time = 0.08, size = 114, normalized size = 0.77

$$\frac{(-ix - 1)(ix + 1)a^2)^{1/4} x \text{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{39(a^2)^{1/4}(-ix - 1)a^{1/4}((ix + 1)a)^{1/4}a^4} + \frac{\frac{2}{39}x^4 + \frac{2}{13}ix^3 - \frac{16}{117}x^2 - \frac{40}{117}}{(x + i)^3(-ix - 1)a^{1/4}((ix + 1)a)^{1/4}a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(17/4)/(I*a*x+a)^(1/4),x)`

[Out] $2/117*(9*I*x^3+3*x^4-20-8*x^2)/(x+I)^3/a^4/(-I*x-1)*a)^{(1/4)/((I*x+1)*a)^{(1/4)}-1/39/(a^2)^{(1/4)}*x*\text{hypergeom}([1/4,1/2],[3/2],-x^2)/a^4*(-I*x-1)*(I*x+1)*a^2)^{(1/4)/(-I*x-1)*a)^{(1/4)/((I*x+1)*a)^{(1/4)}$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{1}{4}}(-i a x + a)^{\frac{17}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(17/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")`

[Out] `integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(17/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{17/4} (a + a x 1i)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(17/4)*(a + a*x*1i)^(1/4)),x)`

[Out] `int(1/((a - a*x*1i)^(17/4)*(a + a*x*1i)^(1/4)), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(17/4)/(a+I*a*x)**(1/4),x)`

[Out] Timed out

$$3.1178 \quad \int \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=256

$$\frac{i\sqrt[4]{a-iax}(a+iax)^{3/4}}{a} - \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} + \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} - \frac{i \tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}}$$

[Out] $-I*(a-I*a*x)^{(1/4)}*(a+I*a*x)^{(3/4)}/a-1/2*I*\arctan(1-(a-I*a*x)^{(1/4)}*2^{(1/2)})/(a+I*a*x)^{(1/4)}*2^{(1/2)}+1/2*I*\arctan(1+(a-I*a*x)^{(1/4)}*2^{(1/2)})/(a+I*a*x)^{(1/4)}*2^{(1/2)}-1/4*I*\ln(1-(a-I*a*x)^{(1/4)}*2^{(1/2)})/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2)}*2^{(1/2)}+1/4*I*\ln(1+(a-I*a*x)^{(1/4)}*2^{(1/2)})/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2)}*2^{(1/2)}$

Rubi [A] time = 0.17, antiderivative size = 256, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 9, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.360$, Rules used = {50, 63, 240, 211, 1165, 628, 1162, 617, 204}

$$\frac{i\sqrt[4]{a-iax}(a+iax)^{3/4}}{a} - \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} + \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} - \frac{i \tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a - I*a*x)^{(1/4)}/(a + I*a*x)^{(1/4)}, x]$

[Out] $((-I)*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(3/4)})/a - (I*\text{ArcTan}[1 - (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2]) + (I*\text{ArcTan}[1 + (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2]) - ((I/2)*\text{Log}[1 + \text{Sqrt}[a - I*a*x]/\text{Sqrt}[a + I*a*x] - (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2]) + ((I/2)*\text{Log}[1 + \text{Sqrt}[a - I*a*x]/\text{Sqrt}[a + I*a*x] + (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2])$

Rule 50

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{m+1}*(c + d*x)^n/(b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \text{Int}[(a + b*x)^m*(c + d*x)^{n-1}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m+n+1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m-n, 0]))) && !ILtQ[m+n+2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 211

```
Int[((a_) + (b_.)*(x_)^4)^(-1), x_Symbol] := With[{r = Numerator[Rt[a/b, 2]
], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*r), Int[(r - s*x^2)/(a + b*x^4),
x], x] + Dist[1/(2*r), Int[(r + s*x^2)/(a + b*x^4), x], x] /; FreeQ[{a, b
}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] &&
AtomQ[SplitProduct[SumBaseQ, b]]))
```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int
[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a,
b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/
n]
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 1162

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x], x] + Dist[e
/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x] /; FreeQ[{a, c, d, e}, x] &
```

& EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]

Rule 1165

Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x], x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} dx &= -\frac{i\sqrt[4]{a-iax}(a+iax)^{3/4}}{a} + \frac{1}{2}a \int \frac{1}{(a-iax)^{3/4}\sqrt[4]{a+iax}} dx \\
 &= -\frac{i\sqrt[4]{a-iax}(a+iax)^{3/4}}{a} + 2i \operatorname{Subst}\left(\int \frac{1}{\sqrt[4]{2a-x^4}} dx, x, \sqrt[4]{a-iax}\right) \\
 &= -\frac{i\sqrt[4]{a-iax}(a+iax)^{3/4}}{a} + 2i \operatorname{Subst}\left(\int \frac{1}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right) \\
 &= -\frac{i\sqrt[4]{a-iax}(a+iax)^{3/4}}{a} + i \operatorname{Subst}\left(\int \frac{1-x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right) + i \operatorname{Subst}\left(\int \frac{1+x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right) \\
 &= -\frac{i\sqrt[4]{a-iax}(a+iax)^{3/4}}{a} + \frac{1}{2}i \operatorname{Subst}\left(\int \frac{1}{1-\sqrt{2}x+x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right) + \frac{1}{2}i \operatorname{Subst}\left(\int \frac{1}{1+\sqrt{2}x+x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right) \\
 &= -\frac{i\sqrt[4]{a-iax}(a+iax)^{3/4}}{a} - \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{2\sqrt{2}} + \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{2\sqrt{2}} + \dots \\
 &= -\frac{i\sqrt[4]{a-iax}(a+iax)^{3/4}}{a} - \frac{i \tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}} + \frac{i \tan^{-1}\left(1 + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}} - \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}}\right)}{2\sqrt{2}} + \dots
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.27

$$\frac{2i2^{3/4}\sqrt[4]{1+ix}(a-iax)^{5/4} {}_2F_1\left(\frac{1}{4}, \frac{5}{4}; \frac{9}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{5a\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(1/4)/(a + I*a*x)^(1/4), x]

[Out] $\left(\frac{(2I)/5 \cdot 2^{3/4} \cdot (1 + Ix)^{1/4} \cdot (a - Iax)^{5/4} \cdot \text{Hypergeometric2F1}\left[\frac{1}{4}, \frac{5}{4}, \frac{9}{4}, \frac{1}{2} - \frac{I}{2}x\right]}{a \cdot (a + Iax)^{1/4}}\right)$

fricas [A] time = 0.47, size = 194, normalized size = 0.76

$$\frac{\sqrt{i} a \log\left(\frac{\sqrt{i}(ax-i)+(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{1}{4}}}{x-i}\right) - \sqrt{i} a \log\left(-\frac{\sqrt{i}(ax-i)-(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{1}{4}}}{x-i}\right) + \sqrt{-i} a \log\left(\frac{\sqrt{-i}(ax-i)+(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{1}{4}}}{x-i}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(1/4),x, algorithm="fricas")`

[Out] $\frac{1}{2} \cdot (\sqrt{I} \cdot a \cdot \log((\sqrt{I} \cdot (a \cdot x - I \cdot a) + (I \cdot a \cdot x + a)^{3/4} \cdot (-I \cdot a \cdot x + a)^{1/4}) / (x - I)) - \sqrt{I} \cdot a \cdot \log(-(\sqrt{I} \cdot (a \cdot x - I \cdot a) - (I \cdot a \cdot x + a)^{3/4} \cdot (-I \cdot a \cdot x + a)^{1/4}) / (x - I)) + \sqrt{-I} \cdot a \cdot \log((\sqrt{-I} \cdot (a \cdot x - I \cdot a) + (I \cdot a \cdot x + a)^{3/4} \cdot (-I \cdot a \cdot x + a)^{1/4}) / (x - I)) - \sqrt{-I} \cdot a \cdot \log(-(\sqrt{-I} \cdot (a \cdot x - I \cdot a) - (I \cdot a \cdot x + a)^{3/4} \cdot (-I \cdot a \cdot x + a)^{1/4}) / (x - I)) - 2 \cdot I \cdot (I \cdot a \cdot x + a)^{3/4} \cdot (-I \cdot a \cdot x + a)^{1/4}) / a$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax+a)^{\frac{1}{4}}}{(iax+a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(1/4),x, algorithm="giac")`

[Out] `integrate((-I*a*x+a)^(1/4)/(I*a*x+a)^(1/4),x)`

maple [C] time = 2.28, size = 477, normalized size = 1.86

$$\frac{i(x-i)(x+i)(-ix-1)a^{\frac{1}{4}}}{(ix-1)((ix+1)a)^{\frac{1}{4}}} \left(\frac{\text{RootOf}(-Z^2-i) \ln\left(\frac{-x^3+(-x^4-2ix^3-2ix+1)^{\frac{1}{4}}x^2 \text{RootOf}(-Z^2-i)-2ix^2+2i(-x^4-2ix^3-2ix+1)^{\frac{1}{4}}x \text{RootOf}(-Z^2-i)-i\sqrt{-x^4}}{-x^3+(-x^4-2ix^3-2ix+1)^{\frac{1}{4}}x^2 \text{RootOf}(-Z^2-i)-2ix^2+2i(-x^4-2ix^3-2ix+1)^{\frac{1}{4}}x \text{RootOf}(-Z^2-i)-i\sqrt{-x^4}}\right)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-I*a*x+a)^(1/4)/(I*a*x+a)^(1/4),x)`

```
[Out] I*(x-I)*(x+I)*(-I*x-1)*a^(1/4)/(I*x-1)/((I*x+1)*a)^(1/4)-(-1/2*RootOf(_Z^2-I)*ln((RootOf(_Z^2-I)*(1-2*I*x-2*I*x^3-x^4)^(1/4)*x^2+I*RootOf(_Z^2-I)*(1-2*I*x-2*I*x^3-x^4)^(3/4)-x^3+2*I*RootOf(_Z^2-I)*(1-2*I*x-2*I*x^3-x^4)^(1/4)*x-I*(1-2*I*x-2*I*x^3-x^4)^(1/2)*x-2*I*x^2-RootOf(_Z^2-I)*(1-2*I*x-2*I*x^3-x^4)^(1/4)+(1-2*I*x-2*I*x^3-x^4)^(1/2)+x)/(I*x-1)^2)-1/2*I*RootOf(_Z^2-I)*ln((I*RootOf(_Z^2-I)*(1-2*I*x-2*I*x^3-x^4)^(1/4)*x^2-2*RootOf(_Z^2-I)*(1-2*I*x-2*I*x^3-x^4)^(1/4)*x-x^3+RootOf(_Z^2-I)*(1-2*I*x-2*I*x^3-x^4)^(3/4)+I*(1-2*I*x-2*I*x^3-x^4)^(1/2)*x-I*RootOf(_Z^2-I)*(1-2*I*x-2*I*x^3-x^4)^(1/4)-2*I*x^2-(1-2*I*x-2*I*x^3-x^4)^(1/2)+x)/(I*x-1)^2))*(-I*x-1)*a)^(1/4)/(I*x-1)*(-I*x-1)^3*(I*x+1)^(1/4)/((I*x+1)*a)^(1/4)
```

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i ax + a)^{\frac{1}{4}}}{(i ax + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")
```

```
[Out] integrate((-I*a*x + a)^(1/4)/(I*a*x + a)^(1/4), x)
```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a - a x 1i)^{1/4}}{(a + a x 1i)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a - a*x*1i)^(1/4)/(a + a*x*1i)^(1/4),x)
```

```
[Out] int((a - a*x*1i)^(1/4)/(a + a*x*1i)^(1/4), x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[4]{-ia(x+i)}}{\sqrt[4]{ia(x-i)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a-I*a*x)**(1/4)/(a+I*a*x)**(1/4),x)
```

```
[Out] Integral((-I*a*(x + I))**(1/4)/(I*a*(x - I))**(1/4), x)
```

$$3.1179 \quad \int \frac{1}{(a-iax)^{3/4} \sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=233

$$\frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2} a} + \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2} a} - \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a}$$

[Out] $-1/2*I*\ln(1-(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2))}/a*2^{(1/2)}+1/2*I*\ln(1+(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2))}/a*2^{(1/2)}-I*\arctan(1-(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4))}*2^{(1/2)}/a+I*\arctan(1+(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4))}*2^{(1/2)}/a$

Rubi [A] time = 0.13, antiderivative size = 233, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 8, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.320$, Rules used = {63, 240, 211, 1165, 628, 1162, 617, 204}

$$\frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2} a} + \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2} a} - \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(3/4)*(a + I*a*x)^(1/4)),x]

[Out] $((-I)*\text{Sqrt}[2]*\text{ArcTan}[1 - (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/a + (I*\text{Sqrt}[2]*\text{ArcTan}[1 + (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/a - (I*\text{Log}[1 + \text{Sqrt}[a - I*a*x]/\text{Sqrt}[a + I*a*x] - (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2]*a) + (I*\text{Log}[1 + \text{Sqrt}[a - I*a*x]/\text{Sqrt}[a + I*a*x] + (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2]*a)$

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 204

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[

a, 0] || LtQ[b, 0])

Rule 211

Int[((a_) + (b_.)*(x_)^4)^(-1), x_Symbol] := With[{r = Numerator[Rt[a/b, 2]], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*r), Int[(r - s*x^2)/(a + b*x^4), x], x] + Dist[1/(2*r), Int[(r + s*x^2)/(a + b*x^4), x], x]] /; FreeQ[{a, b}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] && AtomQ[SplitProduct[SumBaseQ, b]]))

Rule 240

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/n]

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rule 628

Int[((d_) + (e_.)*(x_))/((a_) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]

Rule 1162

Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x], x] + Dist[e/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]

Rule 1165

Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x], x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a - iax)^{3/4} \sqrt[4]{a + iax}} dx &= \frac{(4i) \text{Subst} \left(\int \frac{1}{\sqrt[4]{2a-x^4}} dx, x, \sqrt[4]{a - iax} \right)}{a} \\
&= \frac{(4i) \text{Subst} \left(\int \frac{1}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{a} \\
&= \frac{(2i) \text{Subst} \left(\int \frac{1-x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{a} + \frac{(2i) \text{Subst} \left(\int \frac{1+x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{a} \\
&= \frac{i \text{Subst} \left(\int \frac{1}{1-\sqrt{2}x+x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{a} + \frac{i \text{Subst} \left(\int \frac{1}{1+\sqrt{2}x+x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{a} - \frac{i \text{Subst} \left(\int \frac{1}{1-x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{a} \\
&= -\frac{i \log \left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{\sqrt{2} a} + \frac{i \log \left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{\sqrt{2} a} + \frac{(i\sqrt{2}) \text{Subst} \left(\int \frac{1}{1-x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{\sqrt{2} a} \\
&= -\frac{i\sqrt{2} \tan^{-1} \left(1 - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{a} + \frac{i\sqrt{2} \tan^{-1} \left(1 + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{a} - \frac{i \log \left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} \right)}{\sqrt{2} a}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 68, normalized size = 0.29

$$\frac{2i2^{3/4} \sqrt[4]{1+ix} \sqrt[4]{a-iax} {}_2F_1 \left(\frac{1}{4}, \frac{1}{4}; \frac{5}{4}; \frac{1}{2} - \frac{ix}{2} \right)}{a \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(3/4)*(a + I*a*x)^(1/4)),x]

[Out] ((2*I)*2^(3/4)*(1 + I*x)^(1/4)*(a - I*a*x)^(1/4)*Hypergeometric2F1[1/4, 1/4, 5/4, 1/2 - (I/2)*x])/(a*(a + I*a*x)^(1/4))

fricas [A] time = 0.48, size = 227, normalized size = 0.97

$$\frac{1}{2} \sqrt{\frac{4i}{a^2}} \log \left(\frac{(a^2x - ia^2) \sqrt{\frac{4i}{a^2}} + 2(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{1}{4}}}{2x - 2i} \right) - \frac{1}{2} \sqrt{\frac{4i}{a^2}} \log \left(-\frac{(a^2x - ia^2) \sqrt{\frac{4i}{a^2}} - 2(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{1}{4}}}{2x - 2i} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(1/4),x, algorithm="fricas")

[Out] $\frac{1}{2}\sqrt{4I/a^2}\log\left(\frac{(a^2x - Ia^2)\sqrt{4I/a^2} + 2(Ia^2x + a)^{3/4}(-Ia^2x + a)^{1/4}}{2x - 2I}\right) - \frac{1}{2}\sqrt{4I/a^2}\log\left(\frac{-(a^2x - Ia^2)\sqrt{4I/a^2} - 2(Ia^2x + a)^{3/4}(-Ia^2x + a)^{1/4}}{2x - 2I}\right) + \frac{1}{2}\sqrt{-4I/a^2}\log\left(\frac{(a^2x - Ia^2)\sqrt{-4I/a^2} + 2(Ia^2x + a)^{3/4}(-Ia^2x + a)^{1/4}}{2x - 2I}\right) - \frac{1}{2}\sqrt{-4I/a^2}\log\left(\frac{-(a^2x - Ia^2)\sqrt{-4I/a^2} - 2(Ia^2x + a)^{3/4}(-Ia^2x + a)^{1/4}}{2x - 2I}\right)$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(1/4),x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command: INPUT:sage2OUTPUT:Warning, choosing root of [1,0,0,0,%%{-i,[1,1]%%}+%%{-1,[1,0]%%}] at parameters values [-27,-87]ext_reduce Error: Bad Argument Typeintegrate((-4*i)/a/4*i*a*(-4*i)/a*((i*a*x+a)^(1/4))^2/((-((i*a*x+a)^(1/4))^4+2*a)^(1/4))^3/4*i*a*((i*a*x+a)^(1/4))^(-3,x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(-iax + a)^{\frac{3}{4}}(iax + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(3/4)/(I*a*x+a)^(1/4),x)

[Out] int(1/(-I*a*x+a)^(3/4)/(I*a*x+a)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a - ax1i)^{3/4}(a + ax1i)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(3/4)*(a + a*x*1i)^(1/4)),x)`

[Out] `int(1/((a - a*x*1i)^(3/4)*(a + a*x*1i)^(1/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[4]{ia(x-i)} (-ia(x+i))^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(3/4)/(a+I*a*x)**(1/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(1/4)*(-I*a*(x + I))**(3/4)), x)`

$$3.1180 \quad \int \frac{1}{(a-iax)^{7/4} \sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=33

$$-\frac{2i(a+iax)^{3/4}}{3a^2(a-iax)^{3/4}}$$

[Out] $-2/3*I*(a+I*a*x)^{(3/4)}/a^2/(a-I*a*x)^{(3/4)}$

Rubi [A] time = 0.00, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.040$, Rules used = {37}

$$-\frac{2i(a+iax)^{3/4}}{3a^2(a-iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a - I*a*x)^{(7/4)}*(a + I*a*x)^{(1/4))}, x]$

[Out] $(((-2*I)/3)*(a + I*a*x)^{(3/4)})/(a^2*(a - I*a*x)^{(3/4)})$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_. + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Simp} [((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{1}{(a-iax)^{7/4} \sqrt[4]{a+iax}} dx = -\frac{2i(a+iax)^{3/4}}{3a^2(a-iax)^{3/4}}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 1.00

$$-\frac{2i(a+iax)^{3/4}}{3a^2(a-iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/((a - I*a*x)^{(7/4)}*(a + I*a*x)^{(1/4))}, x]$

[Out] $(((-2*I)/3)*(a + I*a*x)^{(3/4)})/(a^2*(a - I*a*x)^{(3/4)})$

fricas [A] time = 0.45, size = 31, normalized size = 0.94

$$\frac{2(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{1}{4}}}{3(a^3x + ia^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(1/4),x, algorithm="fricas")

[Out] 2/3*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)/(a^3*x + I*a^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(1/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(7/4)), x)

maple [A] time = 0.05, size = 31, normalized size = 0.94

$$\frac{\frac{2x}{3} - \frac{2i}{3}}{(-ix - 1)a^{\frac{3}{4}}((ix + 1)a)^{\frac{1}{4}}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(7/4)/(I*a*x+a)^(1/4),x)

[Out] 2/3/a/(-I*x-1)*a)^(3/4)/((I*x+1)*a)^(1/4)*(x-I)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(7/4)), x)

mupad [B] time = 0.55, size = 38, normalized size = 1.15

$$\frac{2(x-i)(-a(-1+x1i))^{1/4}}{3a^2(-1+x1i)(a(1+x1i))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(7/4)*(a + a*x*1i)^(1/4)),x)`

[Out] `-(2*(x - 1i)*(-a*(x*1i - 1))^(1/4))/(3*a^2*(x*1i - 1)*(a*(x*1i + 1))^(1/4))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[4]{ia(x-i)}(-ia(x+i))^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(7/4)/(a+I*a*x)**(1/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(1/4)*(-I*a*(x + I))**(7/4)), x)`

$$3.1181 \quad \int \frac{1}{(a-iax)^{11/4} \sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=67

$$-\frac{4i(a+iax)^{3/4}}{21a^3(a-iax)^{3/4}} - \frac{2i(a+iax)^{3/4}}{7a^2(a-iax)^{7/4}}$$

[Out] $-2/7*I*(a+I*a*x)^{(3/4)}/a^2/(a-I*a*x)^{(7/4)}-4/21*I*(a+I*a*x)^{(3/4)}/a^3/(a-I*a*x)^{(3/4)}$

Rubi [A] time = 0.01, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$-\frac{4i(a+iax)^{3/4}}{21a^3(a-iax)^{3/4}} - \frac{2i(a+iax)^{3/4}}{7a^2(a-iax)^{7/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(11/4)*(a + I*a*x)^(1/4)), x]

[Out] $(((-2*I)/7)*(a + I*a*x)^{(3/4)})/(a^2*(a - I*a*x)^{(7/4)}) - (((4*I)/21)*(a + I*a*x)^{(3/4)})/(a^3*(a - I*a*x)^{(3/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 $((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] /;$ FreeQ[{
a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 $((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] -$ Dist[(d*S
implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
+ d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a-iax)^{11/4} \sqrt[4]{a+iax}} dx = -\frac{2i(a+iax)^{3/4}}{7a^2(a-iax)^{7/4}} + \frac{2 \int \frac{1}{(a-iax)^{7/4} \sqrt[4]{a+iax}} dx}{7a}$$

$$= -\frac{2i(a+iax)^{3/4}}{7a^2(a-iax)^{7/4}} - \frac{4i(a+iax)^{3/4}}{21a^3(a-iax)^{3/4}}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 0.67

$$\frac{2(5-2ix)(a+iax)^{3/4}}{21a^3(x+i)(a-iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(11/4)*(a + I*a*x)^(1/4)), x]

[Out] (2*(5 - (2*I)*x)*(a + I*a*x)^(3/4))/(21*a^3*(I + x)*(a - I*a*x)^(3/4))

fricas [A] time = 0.45, size = 44, normalized size = 0.66

$$\frac{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{1}{4}}(4x+10i)}{21a^4x^2+42ia^4x-21a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(1/4), x, algorithm="fricas")

[Out] (I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)*(4*x + 10*I)/(21*a^4*x^2 + 42*I*a^4*x - 21*a^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(1/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(11/4)), x)

maple [A] time = 0.05, size = 44, normalized size = 0.66

$$\frac{\frac{4}{21}x^2 + \frac{2}{7}ix + \frac{10}{21}}{(-(ix-1)a)^{\frac{3}{4}}((ix+1)a)^{\frac{1}{4}}(x+i)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(11/4)/(I*a*x+a)^(1/4),x)`

[Out] `2/21/a^2/(-(I*x-1)*a)^(3/4)/((I*x+1)*a)^(1/4)*(2*x^2+5+3*I*x)/(x+I)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")`

[Out] `integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(11/4)), x)`

mupad [B] time = 0.67, size = 46, normalized size = 0.69

$$\frac{(-a(-1+x1i))^{1/4}(2x^2+x3i+5)2i}{21a^3(-1+x1i)^2(a(1+x1i))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(11/4)*(a + a*x*1i)^(1/4)),x)`

[Out] `-((-a*(x*1i - 1))^(1/4)*(x*3i + 2*x^2 + 5)*2i)/(21*a^3*(x*1i - 1)^2*(a*(x*1i + 1))^(1/4))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[4]{ia(x-i)}(-ia(x+i))^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(11/4)/(a+I*a*x)**(1/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(1/4)*(-I*a*(x + I))**(11/4)), x)`

$$3.1182 \quad \int \frac{1}{(a-iax)^{15/4} \sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=100

$$-\frac{16i(a+iax)^{3/4}}{231a^4(a-iax)^{3/4}} - \frac{8i(a+iax)^{3/4}}{77a^3(a-iax)^{7/4}} - \frac{2i(a+iax)^{3/4}}{11a^2(a-iax)^{11/4}}$$

[Out] $-2/11*I*(a+I*a*x)^{(3/4)}/a^2/(a-I*a*x)^{(11/4)}-8/77*I*(a+I*a*x)^{(3/4)}/a^3/(a-I*a*x)^{(7/4)}-16/231*I*(a+I*a*x)^{(3/4)}/a^4/(a-I*a*x)^{(3/4)}$

Rubi [A] time = 0.02, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$-\frac{16i(a+iax)^{3/4}}{231a^4(a-iax)^{3/4}} - \frac{8i(a+iax)^{3/4}}{77a^3(a-iax)^{7/4}} - \frac{2i(a+iax)^{3/4}}{11a^2(a-iax)^{11/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(15/4)*(a + I*a*x)^(1/4)),x]

[Out] $(((-2*I)/11)*(a + I*a*x)^{(3/4)})/(a^2*(a - I*a*x)^{(11/4)}) - (((8*I)/77)*(a + I*a*x)^{(3/4)})/(a^3*(a - I*a*x)^{(7/4)}) - (((16*I)/231)*(a + I*a*x)^{(3/4)})/(a^4*(a - I*a*x)^{(3/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a-iax)^{15/4} \sqrt[4]{a+iax}} dx &= -\frac{2i(a+iax)^{3/4}}{11a^2(a-iax)^{11/4}} + \frac{4 \int \frac{1}{(a-iax)^{11/4} \sqrt[4]{a+iax}} dx}{11a} \\
&= -\frac{2i(a+iax)^{3/4}}{11a^2(a-iax)^{11/4}} - \frac{8i(a+iax)^{3/4}}{77a^3(a-iax)^{7/4}} + \frac{8 \int \frac{1}{(a-iax)^{7/4} \sqrt[4]{a+iax}} dx}{77a^2} \\
&= -\frac{2i(a+iax)^{3/4}}{11a^2(a-iax)^{11/4}} - \frac{8i(a+iax)^{3/4}}{77a^3(a-iax)^{7/4}} - \frac{16i(a+iax)^{3/4}}{231a^4(a-iax)^{3/4}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 52, normalized size = 0.52

$$\frac{2(-8ix^2 + 28x + 41i)(a+iax)^{3/4}}{231a^4(x+i)^2(a-iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(15/4)*(a + I*a*x)^(1/4)),x]

[Out] (2*(a + I*a*x)^(3/4)*(41*I + 28*x - (8*I)*x^2))/(231*a^4*(I + x)^2*(a - I*a*x)^(3/4))

fricas [A] time = 0.46, size = 58, normalized size = 0.58

$$\frac{2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{1}{4}}(8x^2+28ix-41)}{231a^5x^3+693ia^5x^2-693a^5x-231ia^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(15/4)/(a+I*a*x)^(1/4),x, algorithm="fricas")

[Out] 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)*(8*x^2 + 28*I*x - 41)/(231*a^5*x^3 + 693*I*a^5*x^2 - 693*a^5*x - 231*I*a^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{15}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(15/4)/(a+I*a*x)^(1/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(15/4)), x)

maple [A] time = 0.05, size = 50, normalized size = 0.50

$$\frac{\frac{16}{231}x^3 + \frac{40}{231}ix^2 - \frac{26}{231}x + \frac{82}{231}i}{(-ix-1)a^{\frac{3}{4}}((ix+1)a)^{\frac{1}{4}}(x+i)^2a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(15/4)/(I*a*x+a)^(1/4),x)

[Out] 2/231/a^3/(-(I*x-1)*a)^(3/4)/((I*x+1)*a)^(1/4)*(20*I*x^2+8*x^3-13*x+41*I)/(x+I)^2

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{15}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(15/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(15/4)), x)

mupad [B] time = 0.75, size = 51, normalized size = 0.51

$$\frac{(x-i)^4(-a(-1+xi))^{1/4}(8x^2+x28i-41)2i}{231a^4(x^2+1)^3(a(1+xi))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(15/4)*(a + a*x*1i)^(1/4)),x)

[Out] ((x - 1i)^4*(-a*(x*1i - 1))^(1/4)*(x*28i + 8*x^2 - 41)*2i)/(231*a^4*(x^2 + 1)^3*(a*(x*1i + 1))^(1/4))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(15/4)/(a+I*a*x)**(1/4),x)

[Out] Timed out

$$3.1183 \quad \int \frac{1}{(a-iax)^{19/4} \sqrt[4]{a+iax}} dx$$

Optimal. Leaf size=133

$$-\frac{32i(a+iax)^{3/4}}{1155a^5(a-iax)^{3/4}} - \frac{16i(a+iax)^{3/4}}{385a^4(a-iax)^{7/4}} - \frac{4i(a+iax)^{3/4}}{55a^3(a-iax)^{11/4}} - \frac{2i(a+iax)^{3/4}}{15a^2(a-iax)^{15/4}}$$

[Out] $-2/15*I*(a+I*a*x)^{(3/4)}/a^2/(a-I*a*x)^{(15/4)}-4/55*I*(a+I*a*x)^{(3/4)}/a^3/(a-I*a*x)^{(11/4)}-16/385*I*(a+I*a*x)^{(3/4)}/a^4/(a-I*a*x)^{(7/4)}-32/1155*I*(a+I*a*x)^{(3/4)}/a^5/(a-I*a*x)^{(3/4)}$

Rubi [A] time = 0.03, antiderivative size = 133, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$-\frac{32i(a+iax)^{3/4}}{1155a^5(a-iax)^{3/4}} - \frac{16i(a+iax)^{3/4}}{385a^4(a-iax)^{7/4}} - \frac{4i(a+iax)^{3/4}}{55a^3(a-iax)^{11/4}} - \frac{2i(a+iax)^{3/4}}{15a^2(a-iax)^{15/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(19/4)*(a + I*a*x)^(1/4)), x]

[Out] $(((-2*I)/15)*(a + I*a*x)^{(3/4)}/(a^2*(a - I*a*x)^{(15/4)}) - (((4*I)/55)*(a + I*a*x)^{(3/4)}/(a^3*(a - I*a*x)^{(11/4)})) - (((16*I)/385)*(a + I*a*x)^{(3/4)}/(a^4*(a - I*a*x)^{(7/4)})) - (((32*I)/1155)*(a + I*a*x)^{(3/4)}/(a^5*(a - I*a*x)^{(3/4)}))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a-iax)^{19/4} \sqrt[4]{a+iax}} dx &= -\frac{2i(a+iax)^{3/4}}{15a^2(a-iax)^{15/4}} + \frac{2 \int \frac{1}{(a-iax)^{15/4} \sqrt[4]{a+iax}} dx}{5a} \\
&= -\frac{2i(a+iax)^{3/4}}{15a^2(a-iax)^{15/4}} - \frac{4i(a+iax)^{3/4}}{55a^3(a-iax)^{11/4}} + \frac{8 \int \frac{1}{(a-iax)^{11/4} \sqrt[4]{a+iax}} dx}{55a^2} \\
&= -\frac{2i(a+iax)^{3/4}}{15a^2(a-iax)^{15/4}} - \frac{4i(a+iax)^{3/4}}{55a^3(a-iax)^{11/4}} - \frac{16i(a+iax)^{3/4}}{385a^4(a-iax)^{7/4}} + \frac{16 \int \frac{1}{(a-iax)^{7/4} \sqrt[4]{a+iax}} dx}{385a^3} \\
&= -\frac{2i(a+iax)^{3/4}}{15a^2(a-iax)^{15/4}} - \frac{4i(a+iax)^{3/4}}{55a^3(a-iax)^{11/4}} - \frac{16i(a+iax)^{3/4}}{385a^4(a-iax)^{7/4}} - \frac{32i(a+iax)^{3/4}}{1155a^5(a-iax)^{3/4}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 57, normalized size = 0.43

$$\frac{2(-16ix^3 + 72x^2 + 138ix - 159)(a + iax)^{3/4}}{1155a^5(x + i)^3(a - iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(19/4)*(a + I*a*x)^(1/4)),x]

[Out] (2*(a + I*a*x)^(3/4)*(-159 + (138*I)*x + 72*x^2 - (16*I)*x^3))/(1155*a^5*(I + x)^3*(a - I*a*x)^(3/4))

fricas [A] time = 0.47, size = 70, normalized size = 0.53

$$\frac{(32x^3 + 144ix^2 - 276x - 318i)(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{1}{4}}}{1155a^6x^4 + 4620ia^6x^3 - 6930a^6x^2 - 4620ia^6x + 1155a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(19/4)/(a+I*a*x)^(1/4),x, algorithm="fricas")

[Out] (32*x^3 + 144*I*x^2 - 276*x - 318*I)*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)/(1155*a^6*x^4 + 4620*I*a^6*x^3 - 6930*a^6*x^2 - 4620*I*a^6*x + 1155*a^6)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{19}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(19/4)/(a+I*a*x)^(1/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(19/4)), x)

maple [A] time = 0.06, size = 55, normalized size = 0.41

$$\frac{\frac{32}{1155}x^4 + \frac{16}{165}ix^3 - \frac{4}{35}x^2 - \frac{2}{55}ix - \frac{106}{385}}{(-ix - 1)a^{\frac{3}{4}}((ix + 1)a)^{\frac{1}{4}}(x + i)^3 a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(19/4)/(I*a*x+a)^(1/4),x)

[Out] 2/1155/a^4/(-I*x-1)*a^(3/4)/((I*x+1)*a)^(1/4)*(56*I*x^3+16*x^4-21*I*x-159-66*x^2)/(x+I)^3

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{19}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(19/4)/(a+I*a*x)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(1/4)*(-I*a*x + a)^(19/4)), x)

mupad [B] time = 0.79, size = 57, normalized size = 0.43

$$\frac{(x - i)^5 (-a (-1 + x1i))^{1/4} (-16x^3 - x^2 72i + 138x + 159i) 2i}{1155 a^5 (x^2 + 1)^4 (a (1 + x1i))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(19/4)*(a + a*x*1i)^(1/4)),x)

[Out] -((x - 1i)^5*(-a*(x*1i - 1))^(1/4)*(138*x - x^2*72i - 16*x^3 + 159i)*2i)/(1155*a^5*(x^2 + 1)^4*(a*(x*1i + 1))^(1/4))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(19/4)/(a+I*a*x)**(1/4),x)

[Out] Timed out

$$3.1184 \quad \int \frac{(a-iax)^{3/4}}{(a+iax)^{3/4}} dx$$

Optimal. Leaf size=256

$$\frac{i(a-iax)^{3/4}\sqrt[4]{a+iax}}{a} + \frac{3i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} - \frac{3i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} - \frac{3i \tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}}$$

[Out] $-I*(a-I*a*x)^{(3/4)}*(a+I*a*x)^{(1/4)}/a-3/2*I*\arctan(1-(a-I*a*x)^{(1/4)}*2^{(1/2)})/(a+I*a*x)^{(1/4)}*2^{(1/2)}+3/2*I*\arctan(1+(a-I*a*x)^{(1/4)}*2^{(1/2)})/(a+I*a*x)^{(1/4)}*2^{(1/2)}+3/4*I*\ln(1-(a-I*a*x)^{(1/4)}*2^{(1/2)})/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2)}*2^{(1/2)}-3/4*I*\ln(1+(a-I*a*x)^{(1/4)}*2^{(1/2)})/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2)}*2^{(1/2)}$

Rubi [A] time = 0.16, antiderivative size = 256, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 9, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.360$, Rules used = {50, 63, 331, 297, 1162, 617, 204, 1165, 628}

$$\frac{i(a-iax)^{3/4}\sqrt[4]{a+iax}}{a} + \frac{3i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} - \frac{3i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} - \frac{3i \tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a - I*a*x)^{(3/4)}/(a + I*a*x)^{(3/4)}, x]$

[Out] $((-I)*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(1/4)})/a - ((3*I)*\text{ArcTan}[1 - (\text{Sqrt}[2]*a - I*a*x)^{(1/4)}/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2]) + ((3*I)*\text{ArcTan}[1 + (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)}/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2]) + (((3*I)/2)*\text{Log}[1 + \text{Sqrt}[a - I*a*x]/\text{Sqrt}[a + I*a*x] - (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)}/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2]) - (((3*I)/2)*\text{Log}[1 + \text{Sqrt}[a - I*a*x]/\text{Sqrt}[a + I*a*x] + (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)}/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2])$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /; \text{FreeQ}\{a, b, c, d\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{NeQ}[m + n + 1, 0] \ \&\& \ !(\text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{GtQ}[m, 0] \ \&\& \ \text{LtQ}[m - n, 0]))) \ \&\& \ !\text{ILtQ}[m + n + 2, 0] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63


```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 297

```
Int[(x_)^2/((a_) + (b_.)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[a/b,
2]], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*s), Int[(r + s*x^2)/(a + b*x^4
), x], x] - Dist[1/(2*s), Int[(r - s*x^2)/(a + b*x^4), x], x] /; FreeQ[{a,
b}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] &
& AtomQ[SplitProduct[SumBaseQ, b]]))
```

Rule 331

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m +
1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)
^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2
^(-1)] && IntegersQ[m, p + (m + 1)/n]
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 1162

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x], x] + Dist[e
/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x] /; FreeQ[{a, c, d, e}, x] &
```

& EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]

Rule 1165

Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x], x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]

Rubi steps

$$\begin{aligned}
 \int \frac{(a - iax)^{3/4}}{(a + iax)^{3/4}} dx &= -\frac{i(a - iax)^{3/4} \sqrt[4]{a + iax}}{a} + \frac{1}{2}(3a) \int \frac{1}{\sqrt[4]{a - iax} (a + iax)^{3/4}} dx \\
 &= -\frac{i(a - iax)^{3/4} \sqrt[4]{a + iax}}{a} + 6i \operatorname{Subst} \left(\int \frac{x^2}{(2a - x^4)^{3/4}} dx, x, \sqrt[4]{a - iax} \right) \\
 &= -\frac{i(a - iax)^{3/4} \sqrt[4]{a + iax}}{a} + 6i \operatorname{Subst} \left(\int \frac{x^2}{1 + x^4} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) \\
 &= -\frac{i(a - iax)^{3/4} \sqrt[4]{a + iax}}{a} - 3i \operatorname{Subst} \left(\int \frac{1 - x^2}{1 + x^4} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) + 3i \operatorname{Subst} \left(\int \frac{1 + x^2}{1 + x^4} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) \\
 &= -\frac{i(a - iax)^{3/4} \sqrt[4]{a + iax}}{a} + \frac{3}{2}i \operatorname{Subst} \left(\int \frac{1}{1 - \sqrt{2}x + x^2} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) + \frac{3}{2}i \operatorname{Subst} \left(\int \frac{1}{1 + \sqrt{2}x + x^2} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) \\
 &= -\frac{i(a - iax)^{3/4} \sqrt[4]{a + iax}}{a} + \frac{3i \log \left(1 + \frac{\sqrt{a - iax}}{\sqrt{a + iax}} - \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{2\sqrt{2}} - \frac{3i \log \left(1 + \frac{\sqrt{a - iax}}{\sqrt{a + iax}} + \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{2\sqrt{2}} \\
 &= -\frac{i(a - iax)^{3/4} \sqrt[4]{a + iax}}{a} - \frac{3i \tan^{-1} \left(1 - \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{\sqrt{2}} + \frac{3i \tan^{-1} \left(1 + \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{\sqrt{2}} + \frac{3i \log \left(1 + \frac{\sqrt{a - iax}}{\sqrt{a + iax}} + \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{2\sqrt{2}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.27

$$\frac{2i \sqrt[4]{2} (1 + ix)^{3/4} (a - iax)^{7/4} {}_2F_1 \left(\frac{3}{4}, \frac{7}{4}; \frac{11}{4}; \frac{1}{2} - \frac{ix}{2} \right)}{7a(a + iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(3/4)/(a + I*a*x)^(3/4), x]

[Out] (((2*I)/7)*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(7/4)*Hypergeometric2F1[3/4, 7/4, 11/4, 1/2 - (I/2)*x])/(a*(a + I*a*x)^(3/4))

fricas [A] time = 0.48, size = 204, normalized size = 0.80

$$\frac{\sqrt{9i} a \log\left(\frac{\sqrt{9i}(ax+ia)+3(i ax+a)^{\frac{1}{4}}(-i ax+a)^{\frac{3}{4}}}{3x+3i}\right) - \sqrt{9i} a \log\left(-\frac{\sqrt{9i}(ax+ia)-3(i ax+a)^{\frac{1}{4}}(-i ax+a)^{\frac{3}{4}}}{3x+3i}\right) + \sqrt{-9i} a \log\left(\frac{\sqrt{-9i}(ax+ia)+3(i ax+a)^{\frac{1}{4}}(-i ax+a)^{\frac{3}{4}}}{3x+3i}\right) - \sqrt{-9i} a \log\left(-\frac{\sqrt{-9i}(ax+ia)-3(i ax+a)^{\frac{1}{4}}(-i ax+a)^{\frac{3}{4}}}{3x+3i}\right)}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(3/4), x, algorithm="fricas")

[Out] 1/2*(sqrt(9*I)*a*log((sqrt(9*I)*(a*x + I*a) + 3*(I*a*x + a)^(1/4))*(-I*a*x + a)^(3/4))/(3*x + 3*I)) - sqrt(9*I)*a*log(-(sqrt(9*I)*(a*x + I*a) - 3*(I*a*x + a)^(1/4))*(-I*a*x + a)^(3/4))/(3*x + 3*I)) + sqrt(-9*I)*a*log((sqrt(-9*I)*(a*x + I*a) + 3*(I*a*x + a)^(1/4))*(-I*a*x + a)^(3/4))/(3*x + 3*I)) - sqrt(-9*I)*a*log(-(sqrt(-9*I)*(a*x + I*a) - 3*(I*a*x + a)^(1/4))*(-I*a*x + a)^(3/4))/(3*x + 3*I)) - 2*I*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4))/a

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i ax + a)^{\frac{3}{4}}}{(i ax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(3/4), x, algorithm="giac")

[Out] integrate((-I*a*x + a)^(3/4)/(I*a*x + a)^(3/4), x)

maple [C] time = 2.14, size = 464, normalized size = 1.81

$$\frac{i(x-i)(x+i)a}{((ix+1)a)^{\frac{3}{4}}(-ix-1)a^{\frac{1}{4}}} + \left(\frac{3 \operatorname{RootOf}(_Z^2+i) \ln\left(-\frac{x^3 - (-x^4 + 2ix^3 + 2ix+1)^{\frac{1}{4}} x^2 \operatorname{RootOf}(_Z^2+i) - 2ix^2 + 2i(-x^4 + 2ix^3 + 2ix+1)^{\frac{1}{4}} x \operatorname{RootOf}(_Z^2+i) - i \sqrt{\dots}}{\dots}}{2} \right)}{\dots} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(3/4)/(I*a*x+a)^(3/4), x)

```
[Out] -I*(x-I)*(x+I)/((I*x+1)*a)^(3/4)/(-(I*x-1)*a)^(1/4)*a+(-3/2*RootOf(_Z^2+I)*
ln(-(-RootOf(_Z^2+I)*(1+2*I*x+2*I*x^3-x^4)^(1/4)*x^2+x^3+I*RootOf(_Z^2+I)*(
1+2*I*x+2*I*x^3-x^4)^(3/4)+2*I*RootOf(_Z^2+I)*(1+2*I*x+2*I*x^3-x^4)^(1/4)*x
-I*(1+2*I*x+2*I*x^3-x^4)^(1/2)*x-2*I*x^2+(1+2*I*x+2*I*x^3-x^4)^(1/4)*RootOf
(_Z^2+I)-(1+2*I*x+2*I*x^3-x^4)^(1/2)-x)/(I*x+1)^2)-3/2*I*RootOf(_Z^2+I)*ln(
-(-I*(1+2*I*x+2*I*x^3-x^4)^(1/4)*RootOf(_Z^2+I)*x^2-2*RootOf(_Z^2+I)*(1+2*I
*x+2*I*x^3-x^4)^(1/4)*x+x^3+I*(1+2*I*x+2*I*x^3-x^4)^(1/2)*x+RootOf(_Z^2+I)*
(1+2*I*x+2*I*x^3-x^4)^(3/4)+I*RootOf(_Z^2+I)*(1+2*I*x+2*I*x^3-x^4)^(1/4)-2*
I*x^2+(1+2*I*x+2*I*x^3-x^4)^(1/2)-x)/(I*x+1)^2))/((I*x+1)*a)^(3/4)*(-(I*x-1
)*(I*x+1)^3)^(1/4)/(-(I*x-1)*a)^(1/4)*a
```

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{\frac{3}{4}}}{(iax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(3/4),x, algorithm="maxima")
```

```
[Out] integrate((-I*a*x + a)^(3/4)/(I*a*x + a)^(3/4), x)
```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a - a x 1i)^{3/4}}{(a + a x 1i)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a - a*x*1i)^(3/4)/(a + a*x*1i)^(3/4),x)
```

```
[Out] int((a - a*x*1i)^(3/4)/(a + a*x*1i)^(3/4), x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-ia(x+i))^{\frac{3}{4}}}{(ia(x-i))^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a-I*a*x)**(3/4)/(a+I*a*x)**(3/4),x)
```

```
[Out] Integral((-I*a*(x + I))**(3/4)/(I*a*(x - I))**(3/4), x)
```

$$3.1185 \quad \int \frac{1}{\sqrt[4]{a-iax} (a+iax)^{3/4}} dx$$

Optimal. Leaf size=233

$$\frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2} a} - \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2} a} - \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a}$$

[Out] $\frac{1}{2} I \ln(1 - (a - I a x)^{1/4} 2^{1/2} / (a + I a x)^{1/4} + (a - I a x)^{1/2} / (a + I a x)^{1/2}) / a 2^{1/2} - \frac{1}{2} I \ln(1 + (a - I a x)^{1/4} 2^{1/2} / (a + I a x)^{1/4} + (a - I a x)^{1/2} / (a + I a x)^{1/2}) / a 2^{1/2} - I \arctan(1 - (a - I a x)^{1/4} 2^{1/2} / (a + I a x)^{1/4}) 2^{1/2} / a + I \arctan(1 + (a - I a x)^{1/4} 2^{1/2} / (a + I a x)^{1/4}) 2^{1/2} / a$

Rubi [A] time = 0.14, antiderivative size = 233, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 8, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.320$, Rules used = {63, 331, 297, 1162, 617, 204, 1165, 628}

$$\frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2} a} - \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2} a} - \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(1/4)*(a + I*a*x)^(3/4)),x]

[Out] $((-I) \sqrt{2} \text{ArcTan}[1 - (\sqrt{2} (a - I a x)^{1/4}) / (a + I a x)^{1/4}]) / a + (I \sqrt{2} \text{ArcTan}[1 + (\sqrt{2} (a - I a x)^{1/4}) / (a + I a x)^{1/4}]) / a + (I \text{Log}[1 + \sqrt{a - I a x} / \sqrt{a + I a x} - (\sqrt{2} (a - I a x)^{1/4}) / (a + I a x)^{1/4}]) / (\sqrt{2} a) - (I \text{Log}[1 + \sqrt{a - I a x} / \sqrt{a + I a x} + (\sqrt{2} (a - I a x)^{1/4}) / (a + I a x)^{1/4}]) / (\sqrt{2} a)$

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 204

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[

a, 0] || LtQ[b, 0])

Rule 297

Int[(x_)^2/((a_) + (b_.)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[a/b, 2]], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*s), Int[(r + s*x^2)/(a + b*x^4), x], x] - Dist[1/(2*s), Int[(r - s*x^2)/(a + b*x^4), x], x]] /; FreeQ[{a, b}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] & AtomQ[SplitProduct[SumBaseQ, b]]))

Rule 331

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]

Rule 617

Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rule 628

Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]

Rule 1162

Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x], x] + Dist[e/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]

Rule 1165

Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x], x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt[4]{a-iax}(a+iax)^{3/4}} dx &= \frac{(4i) \operatorname{Subst}\left(\int \frac{x^2}{(2a-x^4)^{3/4}} dx, x, \sqrt[4]{a-iax}\right)}{a} \\
&= \frac{(4i) \operatorname{Subst}\left(\int \frac{x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} \\
&= -\frac{(2i) \operatorname{Subst}\left(\int \frac{1-x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{(2i) \operatorname{Subst}\left(\int \frac{1+x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} \\
&= \frac{i \operatorname{Subst}\left(\int \frac{1}{1-\sqrt{2}x+x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i \operatorname{Subst}\left(\int \frac{1}{1+\sqrt{2}x+x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i \operatorname{Subst}\left(\int \frac{1}{1+x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} \\
&= \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}a} - \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}a} + \frac{(i\sqrt{2}) \operatorname{Subst}\left(\int \frac{1}{1+x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}a} \\
&= -\frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}a}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.30

$$\frac{2i\sqrt{2}(1+ix)^{3/4}(a-iax)^{3/4} {}_2F_1\left(\frac{3}{4}, \frac{3}{4}, \frac{7}{4}, \frac{1}{2} - \frac{ix}{2}\right)}{3a(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(1/4)*(a + I*a*x)^(3/4)), x]

[Out] (((2*I)/3)*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(3/4)*Hypergeometric2F1[3/4, 3/4, 7/4, 1/2 - (I/2)*x])/(a*(a + I*a*x)^(3/4))

fricas [A] time = 0.47, size = 227, normalized size = 0.97

$$\frac{1}{2} \sqrt{\frac{4i}{a^2}} \log\left(\frac{(a^2x + ia^2)\sqrt{\frac{4i}{a^2}} + 2(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{3}{4}}}{2x + 2i}\right) - \frac{1}{2} \sqrt{\frac{4i}{a^2}} \log\left(\frac{(a^2x + ia^2)\sqrt{\frac{4i}{a^2}} - 2(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{3}{4}}}{2x + 2i}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(3/4),x, algorithm="fricas")

[Out] $\frac{1}{2}\sqrt{4I/a^2}\log\left(\frac{(a^2x + Ia^2)\sqrt{4I/a^2} + 2(Ia^2x + a)^{1/4}(-Ia^2x + a)^{3/4}}{(2x + 2I)}\right) - \frac{1}{2}\sqrt{4I/a^2}\log\left(\frac{-((a^2x + Ia^2)\sqrt{4I/a^2} - 2(Ia^2x + a)^{1/4}(-Ia^2x + a)^{3/4})}{(2x + 2I)}\right) + \frac{1}{2}\sqrt{-4I/a^2}\log\left(\frac{(a^2x + Ia^2)\sqrt{-4I/a^2} + 2(Ia^2x + a)^{1/4}(-Ia^2x + a)^{3/4}}{(2x + 2I)}\right) - \frac{1}{2}\sqrt{-4I/a^2}\log\left(\frac{-((a^2x + Ia^2)\sqrt{-4I/a^2} - 2(Ia^2x + a)^{1/4}(-Ia^2x + a)^{3/4})}{(2x + 2I)}\right)$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(3/4),x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command:
INPUT:sage2OUTPUT:ext_reduce Error: Bad Argument Typeintegrate((-4*i)/a/4*i
a(-4*i)/a/(-((i*a*x+a)^(1/4))^4+2*a)^(1/4)/4*i*a*((i*a*x+a)^(1/4))^(-3,x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{1}{(-iax + a)^{\frac{1}{4}}(iax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(1/4)/(I*a*x+a)^(3/4),x)

[Out] int(1/(-I*a*x+a)^(1/4)/(I*a*x+a)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a - ax1i)^{1/4}(a + ax1i)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(1/4)*(a + a*x*1i)^(3/4)),x)`

[Out] `int(1/((a - a*x*1i)^(1/4)*(a + a*x*1i)^(3/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{3}{4}} \sqrt[4]{-ia(x+i)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(1/4)/(a+I*a*x)**(3/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(3/4)*(-I*a*(x + I))**(1/4)), x)`

$$3.1186 \quad \int \frac{1}{(a-iax)^{5/4}(a+iax)^{3/4}} dx$$

Optimal. Leaf size=31

$$-\frac{2i\sqrt[4]{a+iax}}{a^2\sqrt[4]{a-iax}}$$

[Out] $-2*I*(a+I*a*x)^{(1/4)}/a^2/(a-I*a*x)^{(1/4)}$

Rubi [A] time = 0.00, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.040$, Rules used = {37}

$$-\frac{2i\sqrt[4]{a+iax}}{a^2\sqrt[4]{a-iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(5/4)*(a + I*a*x)^(3/4)), x]

[Out] $((-2*I)*(a + I*a*x)^{(1/4)})/(a^2*(a - I*a*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a-iax)^{5/4}(a+iax)^{3/4}} dx = -\frac{2i\sqrt[4]{a+iax}}{a^2\sqrt[4]{a-iax}}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 1.00

$$-\frac{2i\sqrt[4]{a+iax}}{a^2\sqrt[4]{a-iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(5/4)*(a + I*a*x)^(3/4)), x]

[Out] $((-2*I)*(a + I*a*x)^{(1/4)})/(a^2*(a - I*a*x)^{(1/4)})$

fricas [A] time = 0.44, size = 31, normalized size = 1.00

$$\frac{2(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{3}{4}}}{a^3x + ia^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(3/4),x, algorithm="fricas")

[Out] 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4)/(a^3*x + I*a^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(3/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(5/4)), x)

maple [A] time = 0.04, size = 31, normalized size = 1.00

$$\frac{2x - 2i}{((ix + 1)a)^{\frac{3}{4}}(-ix - 1)a^{\frac{1}{4}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(5/4)/(I*a*x+a)^(3/4),x)

[Out] 2/a/((I*x+1)*a)^(3/4)/(-I*x-1)*a)^(1/4)*(x-I)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(5/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{1}{(a - ax1i)^{5/4}(a + ax1i)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(5/4)*(a + a*x*1i)^(3/4)), x)`

[Out] `int(1/((a - a*x*1i)^(5/4)*(a + a*x*1i)^(3/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{3}{4}}(-ia(x+i))^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(5/4)/(a+I*a*x)**(3/4), x)`

[Out] `Integral(1/((I*a*(x - I))**(3/4)*(-I*a*(x + I))**(5/4)), x)`

$$3.1187 \quad \int \frac{1}{(a-iax)^{9/4}(a+iax)^{3/4}} dx$$

Optimal. Leaf size=67

$$-\frac{4i\sqrt[4]{a+iax}}{5a^3\sqrt[4]{a-iax}} - \frac{2i\sqrt[4]{a+iax}}{5a^2(a-iax)^{5/4}}$$

[Out] $-2/5*I*(a+I*a*x)^{(1/4)}/a^2/(a-I*a*x)^{(5/4)}-4/5*I*(a+I*a*x)^{(1/4)}/a^3/(a-I*a*x)^{(1/4)}$

Rubi [A] time = 0.01, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$-\frac{4i\sqrt[4]{a+iax}}{5a^3\sqrt[4]{a-iax}} - \frac{2i\sqrt[4]{a+iax}}{5a^2(a-iax)^{5/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(9/4)*(a + I*a*x)^(3/4)), x]

[Out] $(((-2*I)/5)*(a + I*a*x)^{(1/4)})/(a^2*(a - I*a*x)^{(5/4)}) - (((4*I)/5)*(a + I*a*x)^{(1/4)})/(a^3*(a - I*a*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a-iax)^{9/4}(a+iax)^{3/4}} dx = -\frac{2i\sqrt[4]{a+iax}}{5a^2(a-iax)^{5/4}} + \frac{2\int \frac{1}{(a-iax)^{5/4}(a+iax)^{3/4}} dx}{5a}$$

$$= -\frac{2i\sqrt[4]{a+iax}}{5a^2(a-iax)^{5/4}} - \frac{4i\sqrt[4]{a+iax}}{5a^3\sqrt[4]{a-iax}}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 0.67

$$\frac{2(3-2ix)\sqrt[4]{a+iax}}{5a^3(x+i)\sqrt[4]{a-iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(9/4)*(a + I*a*x)^(3/4)), x]

[Out] (2*(3 - (2*I)*x)*(a + I*a*x)^(1/4))/(5*a^3*(I + x)*(a - I*a*x)^(1/4))

fricas [A] time = 0.44, size = 44, normalized size = 0.66

$$\frac{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{3}{4}}(4x+6i)}{5a^4x^2+10ia^4x-5a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(3/4), x, algorithm="fricas")

[Out] (I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4)*(4*x + 6*I)/(5*a^4*x^2 + 10*I*a^4*x - 5*a^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(3/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(9/4)), x)

maple [A] time = 0.05, size = 44, normalized size = 0.66

$$\frac{\frac{4}{5}x^2 + \frac{2}{5}ix + \frac{6}{5}}{((ix+1)a)^{\frac{3}{4}}(-ix-1)a^{\frac{1}{4}}(x+i)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(9/4)/(I*a*x+a)^(3/4),x)`

[Out] `2/5/a^2/((I*x+1)*a)^(3/4)/(-I*x-1)*a)^(1/4)*(2*x^2+3+I*x)/(x+I)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(3/4),x, algorithm="maxima")`

[Out] `integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(9/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a-ax1i)^{9/4}(a+ax1i)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(9/4)*(a + a*x*1i)^(3/4)),x)`

[Out] `int(1/((a - a*x*1i)^(9/4)*(a + a*x*1i)^(3/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{3}{4}}(-ia(x+i))^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(9/4)/(a+I*a*x)**(3/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(3/4)*(-I*a*(x + I))**(9/4)), x)`

$$3.1188 \quad \int \frac{1}{(a-iax)^{13/4}(a+iax)^{3/4}} dx$$

Optimal. Leaf size=100

$$-\frac{16i\sqrt[4]{a+iax}}{45a^4\sqrt[4]{a-iax}} - \frac{8i\sqrt[4]{a+iax}}{45a^3(a-iax)^{5/4}} - \frac{2i\sqrt[4]{a+iax}}{9a^2(a-iax)^{9/4}}$$

[Out] $-2/9*I*(a+I*a*x)^{(1/4)}/a^2/(a-I*a*x)^{(9/4)}-8/45*I*(a+I*a*x)^{(1/4)}/a^3/(a-I*a*x)^{(5/4)}-16/45*I*(a+I*a*x)^{(1/4)}/a^4/(a-I*a*x)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$-\frac{16i\sqrt[4]{a+iax}}{45a^4\sqrt[4]{a-iax}} - \frac{8i\sqrt[4]{a+iax}}{45a^3(a-iax)^{5/4}} - \frac{2i\sqrt[4]{a+iax}}{9a^2(a-iax)^{9/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(13/4)*(a + I*a*x)^(3/4)), x]

[Out] $(((-2*I)/9)*(a + I*a*x)^{(1/4)})/(a^2*(a - I*a*x)^{(9/4)}) - (((8*I)/45)*(a + I*a*x)^{(1/4)})/(a^3*(a - I*a*x)^{(5/4)}) - (((16*I)/45)*(a + I*a*x)^{(1/4)})/(a^4*(a - I*a*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a-iax)^{13/4}(a+iax)^{3/4}} dx &= -\frac{2i\sqrt[4]{a+iax}}{9a^2(a-iax)^{9/4}} + \frac{4 \int \frac{1}{(a-iax)^{9/4}(a+iax)^{3/4}} dx}{9a} \\
&= -\frac{2i\sqrt[4]{a+iax}}{9a^2(a-iax)^{9/4}} - \frac{8i\sqrt[4]{a+iax}}{45a^3(a-iax)^{5/4}} + \frac{8 \int \frac{1}{(a-iax)^{5/4}(a+iax)^{3/4}} dx}{45a^2} \\
&= -\frac{2i\sqrt[4]{a+iax}}{9a^2(a-iax)^{9/4}} - \frac{8i\sqrt[4]{a+iax}}{45a^3(a-iax)^{5/4}} - \frac{16i\sqrt[4]{a+iax}}{45a^4\sqrt[4]{a-iax}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 52, normalized size = 0.52

$$\frac{2(-8ix^2 + 20x + 17i)\sqrt[4]{a+iax}}{45a^4(x+i)^2\sqrt[4]{a-iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(13/4)*(a + I*a*x)^(3/4)),x]

[Out] (2*(a + I*a*x)^(1/4)*(17*I + 20*x - (8*I)*x^2))/(45*a^4*(I + x)^2*(a - I*a*x)^(1/4))

fricas [A] time = 0.45, size = 58, normalized size = 0.58

$$\frac{2(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{3}{4}}(8x^2+20ix-17)}{45a^5x^3+135ia^5x^2-135a^5x-45ia^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(3/4),x, algorithm="fricas")

[Out] 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4)*(8*x^2 + 20*I*x - 17)/(45*a^5*x^3 + 135*I*a^5*x^2 - 135*a^5*x - 45*I*a^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{13}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(3/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(13/4)), x)

maple [A] time = 0.06, size = 50, normalized size = 0.50

$$\frac{\frac{16}{45}x^3 + \frac{8}{15}ix^2 + \frac{2}{15}x + \frac{34}{45}i}{((ix+1)a)^{\frac{3}{4}}(-ix-1)a^{\frac{1}{4}}(x+i)^2 a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(13/4)/(I*a*x+a)^(3/4),x)`

[Out] `2/45/a^3/((I*x+1)*a)^(3/4)/(-I*x-1)*a)^(1/4)*(12*I*x^2+8*x^3+3*x+17*I)/(x+I)^2`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{13}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(3/4),x, algorithm="maxima")`

[Out] `integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(13/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a-ax1i)^{13/4}(a+ax1i)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(13/4)*(a + a*x*1i)^(3/4)),x)`

[Out] `int(1/((a - a*x*1i)^(13/4)*(a + a*x*1i)^(3/4)), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(13/4)/(a+I*a*x)**(3/4),x)`

[Out] Timed out

$$3.1189 \quad \int \frac{(a-iax)^{5/4}}{(a+iax)^{3/4}} dx$$

Optimal. Leaf size=112

$$\frac{10a^2(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{3(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{10}{3} i \sqrt[4]{a-iax} \sqrt[4]{a+iax} - \frac{2i(a-iax)^{5/4} \sqrt[4]{a+iax}}{3a}$$

[Out] $-10/3*I*(a-I*a*x)^{(1/4)}*(a+I*a*x)^{(1/4)}-2/3*I*(a-I*a*x)^{(5/4)}*(a+I*a*x)^{(1/4)}/a+10/3*a^2*(x^2+1)^{(3/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))$
 $*\operatorname{EllipticF}(\sin(1/2*\arctan(x)), 2^{(1/2)})/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.02, antiderivative size = 112, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {50, 42, 233, 231}

$$\frac{10a^2(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{10}{3} i \sqrt[4]{a-iax} \sqrt[4]{a+iax} - \frac{2i(a-iax)^{5/4} \sqrt[4]{a+iax}}{3a}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a - I*a*x)^{(5/4)}/(a + I*a*x)^{(3/4)}, x]$

[Out] $((-10*I)/3)*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)} - (((2*I)/3)*(a - I*a*x)^{(5/4)}*(a + I*a*x)^{(1/4)})/a + (10*a^2*(1 + x^2)^{(3/4)}*\operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2])/((3*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4))}$

Rule 42

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \operatorname{Dist}[(a + b*x)^{\operatorname{FracPart}[m]}*(c + d*x)^{\operatorname{FracPart}[m]}/(a*c + b*d*x^2)^{\operatorname{FracPart}[m]}, \operatorname{Int}[(a*c + b*d*x^2)^m, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, m\}, x \&\& \operatorname{EqQ}[b*c + a*d, 0] \&\& \operatorname{IntegerQ}[2*m]$

Rule 50

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{m+1}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[n*(b*c - a*d)/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{n-1}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{NeQ}[m+n+1, 0] \&\& \operatorname{!(IGtQ}[m, 0] \&\& (\operatorname{!IntegerQ}[n] \mid \mid (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m-n, 0]))) \&\& \operatorname{!ILtQ}[m+n+2, 0] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 231

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Simp[(2*EllipticF[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(3/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 233

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a]

Rubi steps

$$\begin{aligned}
 \int \frac{(a - iax)^{5/4}}{(a + iax)^{3/4}} dx &= -\frac{2i(a - iax)^{5/4} \sqrt[4]{a + iax}}{3a} + \frac{1}{3}(5a) \int \frac{\sqrt[4]{a - iax}}{(a + iax)^{3/4}} dx \\
 &= -\frac{10}{3}i \sqrt[4]{a - iax} \sqrt[4]{a + iax} - \frac{2i(a - iax)^{5/4} \sqrt[4]{a + iax}}{3a} + \frac{1}{3}(5a^2) \int \frac{1}{(a - iax)^{3/4}(a + iax)^{3/4}} dx \\
 &= -\frac{10}{3}i \sqrt[4]{a - iax} \sqrt[4]{a + iax} - \frac{2i(a - iax)^{5/4} \sqrt[4]{a + iax}}{3a} + \frac{(5a^2 (a^2 + a^2x^2)^{3/4}) \int \frac{1}{(a^2 + a^2x^2)^{3/4}} dx}{3(a - iax)^{3/4}(a + iax)^{3/4}} \\
 &= -\frac{10}{3}i \sqrt[4]{a - iax} \sqrt[4]{a + iax} - \frac{2i(a - iax)^{5/4} \sqrt[4]{a + iax}}{3a} + \frac{(5a^2 (1 + x^2)^{3/4}) \int \frac{1}{(1+x^2)^{3/4}} dx}{3(a - iax)^{3/4}(a + iax)^{3/4}} \\
 &= -\frac{10}{3}i \sqrt[4]{a - iax} \sqrt[4]{a + iax} - \frac{2i(a - iax)^{5/4} \sqrt[4]{a + iax}}{3a} + \frac{10a^2 (1 + x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3(a - iax)^{3/4}(a + iax)^{3/4}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.62

$$\frac{2i\sqrt[4]{2}(1 + ix)^{3/4}(a - iax)^{9/4} {}_2F_1\left(\frac{3}{4}, \frac{9}{4}; \frac{13}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{9a(a + iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(5/4)/(a + I*a*x)^(3/4), x]

[Out] (((2*I)/9)*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(9/4)*Hypergeometric2F1[3/4, 9/4, 13/4, 1/2 - (I/2)*x])/(a*(a + I*a*x)^(3/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$-\frac{1}{3}(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}(2x+12i) + \text{integral}\left(\frac{5(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{3(x^2+1)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(3/4),x, algorithm="fricas")

[Out] -1/3*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)*(2*x + 12*I) + integral(5/3*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(x^2 + 1), x)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(3/4),x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command:
INPUT:sage2OUTPUT:ext_reduce Error: Bad Argument Typeintegrate(i/4*a*(-i)/a
^2*(16*i*((i*a*x+a)^(1/4))^4*(2*a-((i*a*x+a)^(1/4))^4)^(1/4)+(-32*i)*a*(2*a
-((i*a*x+a)^(1/4))^4)^(1/4))/4*i*a*((i*a*x+a)^(1/4))^(-3,x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(-iax+a)^{\frac{5}{4}}}{(iax+a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(5/4)/(I*a*x+a)^(3/4),x)

[Out] int((-I*a*x+a)^(5/4)/(I*a*x+a)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax+a)^{\frac{5}{4}}}{(iax+a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(3/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(5/4)/(I*a*x + a)^(3/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - a x 1i)^{5/4}}{(a + a x 1i)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - a*x*1i)^(5/4)/(a + a*x*1i)^(3/4),x)

[Out] int((a - a*x*1i)^(5/4)/(a + a*x*1i)^(3/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-ia(x+i))^{\frac{5}{4}}}{(ia(x-i))^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)**(5/4)/(a+I*a*x)**(3/4),x)

[Out] Integral((-I*a*(x + I))**(5/4)/(I*a*(x - I))**(3/4), x)

$$3.1190 \quad \int \frac{\sqrt[4]{a-iax}}{(a+iax)^{3/4}} dx$$

Optimal. Leaf size=76

$$\frac{2a(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{2i\sqrt[4]{a-iax}\sqrt[4]{a+iax}}{a}$$

[Out] $-2*I*(a-I*a*x)^{(1/4)}*(a+I*a*x)^{(1/4)}/a+2*a*(x^2+1)^{(3/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\operatorname{EllipticF}(\sin(1/2*\arctan(x)), 2^{(1/2)})/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.01, antiderivative size = 76, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {50, 42, 233, 231}

$$\frac{2a(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{2i\sqrt[4]{a-iax}\sqrt[4]{a+iax}}{a}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a - I*a*x)^{(1/4)}/(a + I*a*x)^{(3/4)}, x]$

[Out] $((-2*I)*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})/a + (2*a*(1 + x^2)^{(3/4)}*\operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2])/((a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)})$

Rule 42

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \operatorname{Dist}[(a + b*x)^{\operatorname{FracPart}[m]}*(c + d*x)^{\operatorname{FracPart}[m]}/(a*c + b*d*x^2)^{\operatorname{FracPart}[m]}, \operatorname{Int}[(a*c + b*d*x^2)^m, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, m\}, x \&\& \operatorname{EqQ}[b*c + a*d, 0] \&\& \operatorname{IntegerQ}[2*m]$

Rule 50

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{NeQ}[m+n+1, 0] \&\& \operatorname{!(IGtQ}[m, 0] \&\& (\operatorname{!IntegerQ}[n] \mid (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m-n, 0]))) \&\& \operatorname{!ILtQ}[m+n+2, 0] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 231

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Simp[(2*EllipticF[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(3/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 233

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt[4]{a-iax}}{(a+iax)^{3/4}} dx &= -\frac{2i\sqrt[4]{a-iax}\sqrt[4]{a+iax}}{a} + a \int \frac{1}{(a-iax)^{3/4}(a+iax)^{3/4}} dx \\ &= -\frac{2i\sqrt[4]{a-iax}\sqrt[4]{a+iax}}{a} + \frac{\left(a(a^2+a^2x^2)^{3/4}\right) \int \frac{1}{(a^2+a^2x^2)^{3/4}} dx}{(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= -\frac{2i\sqrt[4]{a-iax}\sqrt[4]{a+iax}}{a} + \frac{\left(a(1+x^2)^{3/4}\right) \int \frac{1}{(1+x^2)^{3/4}} dx}{(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= -\frac{2i\sqrt[4]{a-iax}\sqrt[4]{a+iax}}{a} + \frac{2a(1+x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{(a-iax)^{3/4}(a+iax)^{3/4}} \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.92

$$\frac{2i\sqrt[4]{2}(1+ix)^{3/4}(a-iax)^{5/4} {}_2F_1\left(\frac{3}{4}, \frac{5}{4}; \frac{9}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{5a(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(1/4)/(a + I*a*x)^(3/4), x]

[Out] (((2*I)/5)*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(5/4)*Hypergeometric2F1[3/4, 5/4, 9/4, 1/2 - (I/2)*x]/(a*(a + I*a*x)^(3/4))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\frac{\text{aintegral}\left(\frac{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{ax^2+a}, x\right) - 2i(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(3/4),x, algorithm="fricas")

[Out] (a*integral((I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a*x^2 + a), x) - 2*I*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4))/a

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i ax + a)^{\frac{1}{4}}}{(i ax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(3/4),x, algorithm="giac")

[Out] integrate((-I*a*x + a)^(1/4)/(I*a*x + a)^(3/4), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(-i ax + a)^{\frac{1}{4}}}{(i ax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(1/4)/(I*a*x+a)^(3/4),x)

[Out] int((-I*a*x+a)^(1/4)/(I*a*x+a)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i ax + a)^{\frac{1}{4}}}{(i ax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(3/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(1/4)/(I*a*x + a)^(3/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - a x 1i)^{1/4}}{(a + a x 1i)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - a*x*Ii)^(1/4)/(a + a*x*Ii)^(3/4), x)`

[Out] `int((a - a*x*Ii)^(1/4)/(a + a*x*Ii)^(3/4), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[4]{-ia(x+i)}}{(ia(x-i))^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)**(1/4)/(a+I*a*x)**(3/4), x)`

[Out] `Integral((-I*a*(x + I))**(1/4)/(I*a*(x - I))**(3/4), x)`

$$3.1191 \quad \int \frac{1}{(a-iax)^{3/4}(a+iax)^{3/4}} dx$$

Optimal. Leaf size=43

$$\frac{2(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{(a-iax)^{3/4}(a+iax)^{3/4}}$$

[Out] $2*(x^2+1)^{(3/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\operatorname{EllipticF}(\sin(1/2*\arctan(x)), 2^{(1/2)})/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.01, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.120$, Rules used = {42, 233, 231}

$$\frac{2(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{(a-iax)^{3/4}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4))}, x]$

[Out] $(2*(1 + x^2)^{(3/4)}*\operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2])/((a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)})$

Rule 42

$\operatorname{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(m_)}), x_Symbol] \rightarrow \operatorname{Dist}[(a + b*x)^{\operatorname{FracPart}[m]}*(c + d*x)^{\operatorname{FracPart}[m]}]/(a*c + b*d*x^2)^{\operatorname{FracPart}[m]}, \operatorname{Int}[(a*c + b*d*x^2)^m, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \operatorname{EqQ}[b*c + a*d, 0] \ \&\& \ !\operatorname{IntegerQ}[2*m]$

Rule 231

$\operatorname{Int}[(a_ + (b_)*(x_)^2)^{(-3/4)}, x_Symbol] \rightarrow \operatorname{Simp}[(2*\operatorname{EllipticF}[(1*\operatorname{ArcTan}[\operatorname{Rt}[b/a, 2]*x])/2, 2])/ (a^{(3/4)}*\operatorname{Rt}[b/a, 2]), x] /;$ $\operatorname{FreeQ}\{a, b\}, x \ \&\& \ \operatorname{GtQ}[a, 0] \ \&\& \ \operatorname{PosQ}[b/a]$

Rule 233

$\operatorname{Int}[(a_ + (b_)*(x_)^2)^{(-3/4)}, x_Symbol] \rightarrow \operatorname{Dist}[(1 + (b*x^2)/a)^{(3/4)}/(a + b*x^2)^{(3/4)}, \operatorname{Int}[1/(1 + (b*x^2)/a)^{(3/4)}, x], x] /;$ $\operatorname{FreeQ}\{a, b\}, x \ \& \ \operatorname{PosQ}[a]$

Rubi steps

$$\begin{aligned} \int \frac{1}{(a-iax)^{3/4}(a+iax)^{3/4}} dx &= \frac{(a^2+a^2x^2)^{3/4} \int \frac{1}{(a^2+a^2x^2)^{3/4}} dx}{(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= \frac{(1+x^2)^{3/4} \int \frac{1}{(1+x^2)^{3/4}} dx}{(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= \frac{2(1+x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{(a-iax)^{3/4}(a+iax)^{3/4}} \end{aligned}$$

Mathematica [C] time = 0.02, size = 68, normalized size = 1.58

$$\frac{2i\sqrt[4]{2}(1+ix)^{3/4}\sqrt[4]{a-iax} {}_2F_1\left(\frac{1}{4}, \frac{3}{4}; \frac{5}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{a(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(3/4)*(a + I*a*x)^(3/4)), x]

[Out] ((2*I)*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(1/4)*Hypergeometric2F1[1/4, 3/4, 5/4, 1/2 - (I/2)*x])/(a*(a + I*a*x)^(3/4))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{a^2x^2+a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(3/4), x, algorithm="fricas")

[Out] integral((I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a^2*x^2 + a^2), x)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(3/4), x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command:
 INPUT:sage2OUTPUT:ext_reduce Error: Bad Argument Typeintegrate((-4*i)/a/4*i
 a(-4*i)/a/((-((i*a*x+a)^(1/4))^4+2*a)^(1/4))^3/4*i*a*((i*a*x+a)^(1/4))^-3
 ,x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{1}{(-iax + a)^{\frac{3}{4}} (iax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(3/4)/(I*a*x+a)^(3/4),x)

[Out] int(1/(-I*a*x+a)^(3/4)/(I*a*x+a)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{3}{4}} (-iax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{1}{(a - ax1i)^{3/4} (a + ax1i)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(3/4)*(a + a*x*1i)^(3/4)),x)

[Out] int(1/((a - a*x*1i)^(3/4)*(a + a*x*1i)^(3/4)), x)

sympy [A] time = 5.34, size = 100, normalized size = 2.33

$$\frac{iG_{6,6}^{5,3} \left(\begin{matrix} \frac{3}{8}, \frac{7}{8}, 1 \\ \frac{1}{4}, \frac{3}{8}, \frac{3}{4}, \frac{7}{8}, \frac{5}{4} \end{matrix} \middle| \frac{1}{2}, \frac{3}{4}, \frac{5}{4} \right) e^{-3i\pi} \left| \frac{e^{-3i\pi}}{x^2} \right| e^{\frac{3i\pi}{4}}}{4\pi a^{\frac{3}{2}} \Gamma\left(\frac{3}{4}\right)} + \frac{iG_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, -\frac{1}{8}, 0, \frac{3}{8}, \frac{1}{2}, 1 \\ -\frac{1}{8}, \frac{3}{8} \end{matrix} \middle| -\frac{1}{2}, 0, \frac{1}{4}, 0 \right) \left| \frac{e^{-i\pi}}{x^2} \right|}{4\pi a^{\frac{3}{2}} \Gamma\left(\frac{3}{4}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a-I*a*x)**(3/4)/(a+I*a*x)**(3/4),x)
```

```
[Out] -I*meijerg(((3/8, 7/8, 1), (1/2, 3/4, 5/4)), ((1/4, 3/8, 3/4, 7/8, 5/4), (0, .)), exp_polar(-3*I*pi)/x**2)*exp(3*I*pi/4)/(4*pi*a**(3/2)*gamma(3/4)) + I*meijerg((( -1/2, -1/8, 0, 3/8, 1/2, 1), ()), ((-1/8, 3/8), (-1/2, 0, 1/4, 0)), exp_polar(-I*pi)/x**2)/(4*pi*a**(3/2)*gamma(3/4))
```

$$3.1192 \quad \int \frac{1}{(a-iax)^{7/4}(a+iax)^{3/4}} dx$$

Optimal. Leaf size=82

$$\frac{2(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{3a(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{2i\sqrt[4]{a+iax}}{3a^2(a-iax)^{3/4}}$$

[Out] $-2/3*I*(a+I*a*x)^{(1/4)}/a^2/(a-I*a*x)^{(3/4)}+2/3*(x^2+1)^{(3/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\operatorname{EllipticF}(\sin(1/2*\arctan(x)), 2^{(1/2)})/a/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.01, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {51, 42, 233, 231}

$$\frac{2(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3a(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{2i\sqrt[4]{a+iax}}{3a^2(a-iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a - I*a*x)^{(7/4)}*(a + I*a*x)^{(3/4))}, x]$

[Out] $(((-2*I)/3)*(a + I*a*x)^{(1/4)})/(a^2*(a - I*a*x)^{(3/4)}) + (2*(1 + x^2)^{(3/4)}*\operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2])/(3*a*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)})$

Rule 42

$\operatorname{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] \rightarrow \operatorname{Dist}[(a + b*x)^{\operatorname{FracPart}[m]}*(c + d*x)^{\operatorname{FracPart}[m]}/(a*c + b*d*x^2)^{\operatorname{FracPart}[m]}, \operatorname{Int}[(a*c + b*d*x^2)^m, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \operatorname{EqQ}[b*c + a*d, 0] \ \&\& \ !\operatorname{IntegerQ}[2*m]$

Rule 51

$\operatorname{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}/((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*(m+n+2))/((b*c - a*d)*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^n, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, n\}, x \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{LtQ}[m, -1] \ \&\& \ !(\operatorname{LtQ}[n, -1] \ \&\& \ (\operatorname{EqQ}[a, 0] \ || \ (\operatorname{NeQ}[c, 0] \ \&\& \ \operatorname{LtQ}[m - n, 0] \ \&\& \ \operatorname{IntegerQ}[n]))) \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 231

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Simp[(2*EllipticF[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(3/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 233

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a-ix)^{7/4}(a+ix)^{3/4}} dx &= -\frac{2i\sqrt[4]{a+iax}}{3a^2(a-ix)^{3/4}} + \frac{\int \frac{1}{(a-iax)^{3/4}(a+iax)^{3/4}} dx}{3a} \\ &= -\frac{2i\sqrt[4]{a+iax}}{3a^2(a-ix)^{3/4}} + \frac{(a^2+a^2x^2)^{3/4} \int \frac{1}{(a^2+a^2x^2)^{3/4}} dx}{3a(a-ix)^{3/4}(a+ix)^{3/4}} \\ &= -\frac{2i\sqrt[4]{a+iax}}{3a^2(a-ix)^{3/4}} + \frac{(1+x^2)^{3/4} \int \frac{1}{(1+x^2)^{3/4}} dx}{3a(a-ix)^{3/4}(a+ix)^{3/4}} \\ &= -\frac{2i\sqrt[4]{a+iax}}{3a^2(a-ix)^{3/4}} + \frac{2(1+x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3a(a-ix)^{3/4}(a+ix)^{3/4}} \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.85

$$\frac{2i\sqrt[4]{2}(1+ix)^{3/4} {}_2F_1\left(-\frac{3}{4}, \frac{3}{4}; \frac{1}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{3a(a-ix)^{3/4}(a+ix)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(7/4)*(a + I*a*x)^(3/4)), x]

[Out] (((-2*I)/3)*2^(1/4)*(1 + I*x)^(3/4)*Hypergeometric2F1[-3/4, 3/4, 1/4, 1/2 - (I/2)*x])/(a*(a - I*a*x)^(3/4)*(a + I*a*x)^(3/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\frac{3(a^3x + ia^3) \operatorname{integral}\left(\frac{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{3(a^3x^2+a^3)}, x\right) + 2(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{3(a^3x + ia^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(3/4),x, algorithm="fricas")

[Out] 1/3*(3*(a^3*x + I*a^3)*integral(1/3*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a^3*x^2 + a^3), x) + 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4))/(a^3*x + I*a^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{3}{4}}(-i a x + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(3/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(7/4)), x)

maple [F] time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{1}{(-i a x + a)^{\frac{7}{4}}(i a x + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(7/4)/(I*a*x+a)^(3/4),x)

[Out] int(1/(-I*a*x+a)^(7/4)/(I*a*x+a)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{3}{4}}(-i a x + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(7/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{7/4} (a + a x 1i)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(7/4)*(a + a*x*1i)^(3/4)),x)`

[Out] `int(1/((a - a*x*1i)^(7/4)*(a + a*x*1i)^(3/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{3}{4}}(-ia(x+i))^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(7/4)/(a+I*a*x)**(3/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(3/4)*(-I*a*(x + I))**(7/4)), x)`

$$3.1193 \quad \int \frac{1}{(a-iax)^{11/4}(a+iax)^{3/4}} dx$$

Optimal. Leaf size=115

$$\frac{2(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{7a^2(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{2i\sqrt[4]{a+iax}}{7a^3(a-iax)^{3/4}} - \frac{2i\sqrt[4]{a+iax}}{7a^2(a-iax)^{7/4}}$$

[Out] $-2/7*I*(a+I*a*x)^{(1/4)}/a^2/(a-I*a*x)^{(7/4)}-2/7*I*(a+I*a*x)^{(1/4)}/a^3/(a-I*a*x)^{(3/4)}+2/7*(x^2+1)^{(3/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\operatorname{EllipticF}(\sin(1/2*\arctan(x)), 2^{(1/2)})/a^2/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.03, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {51, 42, 233, 231}

$$\frac{2(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{7a^2(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{2i\sqrt[4]{a+iax}}{7a^3(a-iax)^{3/4}} - \frac{2i\sqrt[4]{a+iax}}{7a^2(a-iax)^{7/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a - I*a*x)^{(11/4)}*(a + I*a*x)^{(3/4))}, x]$

[Out] $(((-2*I)/7)*(a + I*a*x)^{(1/4)})/(a^2*(a - I*a*x)^{(7/4)}) - (((2*I)/7)*(a + I*a*x)^{(1/4)})/(a^3*(a - I*a*x)^{(3/4)}) + (2*(1 + x^2)^{(3/4)}*\operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2])/(7*a^2*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)})$

Rule 42

$\operatorname{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] := \operatorname{Dist}[(a + b*x)^{\operatorname{FracPart}[m]}*(c + d*x)^{\operatorname{FracPart}[m]}]/(a*c + b*d*x^2)^{\operatorname{FracPart}[m]}, \operatorname{Int}[(a*c + b*d*x^2)^m, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \operatorname{EqQ}[b*c + a*d, 0] \ \&\& \ !\operatorname{IntegerQ}[2*m]$

Rule 51

$\operatorname{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}/((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*(m+n+2))/((b*c - a*d)*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^n, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, n\}, x \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{LtQ}[m, -1] \ \&\& \ !(\operatorname{LtQ}[n, -1] \ \&\& \ (\operatorname{EqQ}[a, 0] \ || \ (\operatorname{NeQ}[c, 0] \ \&\& \ \operatorname{LtQ}[m-n, 0] \ \&\& \ \operatorname{IntegerQ}[n]))) \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 231

```
Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Simp[(2*EllipticF[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(3/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 233

```
Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(
a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a-iax)^{11/4}(a+iax)^{3/4}} dx &= -\frac{2i\sqrt[4]{a+iax}}{7a^2(a-iax)^{7/4}} + \frac{3 \int \frac{1}{(a-iax)^{7/4}(a+iax)^{3/4}} dx}{7a} \\
&= -\frac{2i\sqrt[4]{a+iax}}{7a^2(a-iax)^{7/4}} - \frac{2i\sqrt[4]{a+iax}}{7a^3(a-iax)^{3/4}} + \frac{\int \frac{1}{(a-iax)^{3/4}(a+iax)^{3/4}} dx}{7a^2} \\
&= -\frac{2i\sqrt[4]{a+iax}}{7a^2(a-iax)^{7/4}} - \frac{2i\sqrt[4]{a+iax}}{7a^3(a-iax)^{3/4}} + \frac{(a^2+a^2x^2)^{3/4} \int \frac{1}{(a^2+a^2x^2)^{3/4}} dx}{7a^2(a-iax)^{3/4}(a+iax)^{3/4}} \\
&= -\frac{2i\sqrt[4]{a+iax}}{7a^2(a-iax)^{7/4}} - \frac{2i\sqrt[4]{a+iax}}{7a^3(a-iax)^{3/4}} + \frac{(1+x^2)^{3/4} \int \frac{1}{(1+x^2)^{3/4}} dx}{7a^2(a-iax)^{3/4}(a+iax)^{3/4}} \\
&= -\frac{2i\sqrt[4]{a+iax}}{7a^2(a-iax)^{7/4}} - \frac{2i\sqrt[4]{a+iax}}{7a^3(a-iax)^{3/4}} + \frac{2(1+x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{7a^2(a-iax)^{3/4}(a+iax)^{3/4}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.61

$$-\frac{2i\sqrt[4]{2}(1+ix)^{3/4} {}_2F_1\left(-\frac{7}{4}, \frac{3}{4}; -\frac{3}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{7a(a-iax)^{7/4}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

```
[In] Integrate[1/((a - I*a*x)^(11/4)*(a + I*a*x)^(3/4)), x]
```

```
[Out] (((-2*I)/7)*2^(1/4)*(1 + I*x)^(3/4)*Hypergeometric2F1[-7/4, 3/4, -3/4, 1/2
- (I/2)*x])/(a*(a - I*a*x)^(7/4)*(a + I*a*x)^(3/4))
```

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\frac{(7a^4x^2 + 14ia^4x - 7a^4)\operatorname{integral}\left(\frac{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{7(a^4x^2+a^4)}, x\right) + (iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}(2x+4i)}{7a^4x^2 + 14ia^4x - 7a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(3/4),x, algorithm="fricas")`

[Out] $((7*a^4*x^2 + 14*I*a^4*x - 7*a^4)*\operatorname{integral}(1/7*(I*a*x + a)^{(1/4)}*(-I*a*x + a)^{(1/4)}/(a^4*x^2 + a^4), x) + (I*a*x + a)^{(1/4)}*(-I*a*x + a)^{(1/4)}*(2*x + 4*I))/(7*a^4*x^2 + 14*I*a^4*x - 7*a^4)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(3/4),x, algorithm="giac")`

[Out] `integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(11/4)), x)`

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(-iax+a)^{\frac{11}{4}}(iax+a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(11/4)/(I*a*x+a)^(3/4),x)`

[Out] `int(1/(-I*a*x+a)^(11/4)/(I*a*x+a)^(3/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(3/4),x, algorithm="maxima")`

[Out] `integrate(1/((I*a*x + a)^(3/4)*(-I*a*x + a)^(11/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{11/4} (a + a x 1i)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(11/4)*(a + a*x*1i)^(3/4)), x)

[Out] int(1/((a - a*x*1i)^(11/4)*(a + a*x*1i)^(3/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x - i))^{\frac{3}{4}} (-ia(x + i))^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(11/4)/(a+I*a*x)**(3/4), x)

[Out] Integral(1/((I*a*(x - I))**(3/4)*(-I*a*(x + I))**(11/4)), x)

$$3.1194 \quad \int \frac{(a-iax)^{7/4}}{(a+iax)^{7/4}} dx$$

Optimal. Leaf size=291

$$\frac{4i(a-iax)^{7/4}}{3a(a+iax)^{3/4}} + \frac{7i\sqrt[4]{a+iax}(a-iax)^{3/4}}{3a} - \frac{7i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} + \frac{7i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} + \dots$$

[Out] $\frac{4}{3}I*(a-I*a*x)^{(7/4)}/a/(a+I*a*x)^{(3/4)}+7/3*I*(a-I*a*x)^{(3/4)}*(a+I*a*x)^{(1/4)}/a+7/2*I*\arctan(1-(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)})*2^{(1/2)}-7/2*I*\arctan(1+(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)})*2^{(1/2)}-7/4*I*\ln(1-(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2)))*2^{(1/2)}+7/4*I*\ln(1+(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2)))*2^{(1/2)}$

Rubi [A] time = 0.18, antiderivative size = 291, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 10, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.400$, Rules used = {47, 50, 63, 331, 297, 1162, 617, 204, 1165, 628}

$$\frac{4i(a-iax)^{7/4}}{3a(a+iax)^{3/4}} + \frac{7i\sqrt[4]{a+iax}(a-iax)^{3/4}}{3a} - \frac{7i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} + \frac{7i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} + \dots$$

Antiderivative was successfully verified.

[In] Int[(a - I*a*x)^(7/4)/(a + I*a*x)^(7/4), x]

[Out] $((4I/3)*(a-I*a*x)^{(7/4)}/(a*(a+I*a*x)^{(3/4)}+((7I/3)*(a-I*a*x)^{(3/4)}*(a+I*a*x)^{(1/4)}/a+((7I)*\text{ArcTan}[1-(\text{Sqrt}[2]*(a-I*a*x)^{(1/4)})/(a+I*a*x)^{(1/4)}])/(\text{Sqrt}[2])-(7I)*\text{ArcTan}[1+(\text{Sqrt}[2]*(a-I*a*x)^{(1/4)})/(a+I*a*x)^{(1/4)}])/(\text{Sqrt}[2])-(7I/2)*\text{Log}[1+\text{Sqrt}[a-I*a*x]/\text{Sqrt}[a+I*a*x]-\text{Sqrt}[2]*(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}])/(\text{Sqrt}[2])+(7I/2)*\text{Log}[1+\text{Sqrt}[a-I*a*x]/\text{Sqrt}[a+I*a*x]+(\text{Sqrt}[2]*(a-I*a*x)^{(1/4)})/(a+I*a*x)^{(1/4)}])/(\text{Sqrt}[2])$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 297

```
Int[(x_)^2/((a_) + (b_.)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[a/b,
2]], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*s), Int[(r + s*x^2)/(a + b*x^4
), x], x] - Dist[1/(2*s), Int[(r - s*x^2)/(a + b*x^4), x], x]] /; FreeQ[{a,
b}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] &
& AtomQ[SplitProduct[SumBaseQ, b]]))
```

Rule 331

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m +
1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)
^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2
^(-1)] && IntegerQ[m, p + (m + 1)/n]
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```


Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 1162

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x] + Dist[e
/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] &
& EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]
```

Rule 1165

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x],
x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x]] /; Fre
eQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a - iax)^{7/4}}{(a + iax)^{7/4}} dx &= \frac{4i(a - iax)^{7/4}}{3a(a + iax)^{3/4}} - \frac{7}{3} \int \frac{(a - iax)^{3/4}}{(a + iax)^{3/4}} dx \\
&= \frac{4i(a - iax)^{7/4}}{3a(a + iax)^{3/4}} + \frac{7i(a - iax)^{3/4} \sqrt[4]{a + iax}}{3a} - \frac{1}{2}(7a) \int \frac{1}{\sqrt[4]{a - iax} (a + iax)^{3/4}} dx \\
&= \frac{4i(a - iax)^{7/4}}{3a(a + iax)^{3/4}} + \frac{7i(a - iax)^{3/4} \sqrt[4]{a + iax}}{3a} - 14i \operatorname{Subst} \left(\int \frac{x^2}{(2a - x^4)^{3/4}} dx, x, \sqrt[4]{a - iax} \right) \\
&= \frac{4i(a - iax)^{7/4}}{3a(a + iax)^{3/4}} + \frac{7i(a - iax)^{3/4} \sqrt[4]{a + iax}}{3a} - 14i \operatorname{Subst} \left(\int \frac{x^2}{1 + x^4} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) \\
&= \frac{4i(a - iax)^{7/4}}{3a(a + iax)^{3/4}} + \frac{7i(a - iax)^{3/4} \sqrt[4]{a + iax}}{3a} + 7i \operatorname{Subst} \left(\int \frac{1 - x^2}{1 + x^4} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) - 7i \operatorname{Subst} \left(\int \frac{1}{1 - \sqrt{2}x + x^2} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) - \frac{7}{2}i \operatorname{Subst} \left(\int \frac{1}{1 + \sqrt{2}x + x^2} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) \\
&= \frac{4i(a - iax)^{7/4}}{3a(a + iax)^{3/4}} + \frac{7i(a - iax)^{3/4} \sqrt[4]{a + iax}}{3a} - \frac{7i \log \left(1 + \frac{\sqrt{a - iax}}{\sqrt{a + iax}} - \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{2\sqrt{2}} + \frac{7i \log \left(1 + \frac{\sqrt{a - iax}}{\sqrt{a + iax}} + \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{2\sqrt{2}} \\
&= \frac{4i(a - iax)^{7/4}}{3a(a + iax)^{3/4}} + \frac{7i(a - iax)^{3/4} \sqrt[4]{a + iax}}{3a} + \frac{7i \tan^{-1} \left(1 - \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{\sqrt{2}} - \frac{7i \tan^{-1} \left(1 + \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{\sqrt{2}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.24

$$\frac{i\sqrt[4]{2}(1 + ix)^{3/4}(a - iax)^{11/4} {}_2F_1\left(\frac{7}{4}, \frac{11}{4}; \frac{15}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{11a^2(a + iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(7/4)/(a + I*a*x)^(7/4), x]

[Out] ((I/11)*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(11/4)*Hypergeometric2F1[7/4, 11/4, 15/4, 1/2 - (I/2)*x]/(a^2*(a + I*a*x)^(3/4))

fricas [A] time = 0.49, size = 241, normalized size = 0.83

$$3\sqrt{49i}(ax - ia) \log \left(\frac{\sqrt{49i}(ax + ia) + 7(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{3}{4}}}{7x + 7i} \right) - 3\sqrt{49i}(ax - ia) \log \left(-\frac{\sqrt{49i}(ax + ia) - 7(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{3}{4}}}{7x + 7i} \right) + 3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(7/4),x, algorithm="fricas")

[Out]
$$-1/6*(3*\sqrt[4]{49*I}*(a*x - I*a)*\log((\sqrt[4]{49*I}*(a*x + I*a) + 7*(I*a*x + a)^{1/4})*(-I*a*x + a)^{3/4})/(7*x + 7*I)) - 3*\sqrt[4]{49*I}*(a*x - I*a)*\log(-(\sqrt[4]{49*I}*(a*x + I*a) - 7*(I*a*x + a)^{1/4})*(-I*a*x + a)^{3/4})/(7*x + 7*I)) + 3*\sqrt[4]{-49*I}*(a*x - I*a)*\log((\sqrt[4]{-49*I}*(a*x + I*a) + 7*(I*a*x + a)^{1/4})*(-I*a*x + a)^{3/4})/(7*x + 7*I)) - 3*\sqrt[4]{-49*I}*(a*x - I*a)*\log(-(\sqrt[4]{-49*I}*(a*x + I*a) - 7*(I*a*x + a)^{1/4})*(-I*a*x + a)^{3/4})/(7*x + 7*I)) + 2*(I*a*x + a)^{1/4}*(-I*a*x + a)^{3/4}*(-3*I*x - 11)/(a*x - I*a)$$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(7/4),x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command: INPUT:sage2OUTPUT:Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}] + %%{1,[0,4]%%}] at parameters values [-64,-30]Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}] + %%{1,[0,4]%%}] at parameters values [70,22]Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}] + %%{1,[0,4]%%}] at parameters values [42,56]Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}] + %%{1,[0,4]%%}] at parameters values [-9,-13]Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}] + %%{1,[0,4]%%}] at parameters values [46,24]ext_reduce Error: Bad Argument TypeEvaluation time: 0.61integrate(i/4*a/a^2*(16*((i*a*x+a)^(1/4))^4*((-(i*a*x+a)^(1/4))^4+2*a)^(1/4))^3-32*a*((-(i*a*x+a)^(1/4))^4+2*a)^(1/4))^3)/((i*a*x+a)^(1/4))^4/4*i*a*((i*a*x+a)^(1/4))^(-3,x)

maple [C] time = 2.01, size = 469, normalized size = 1.61

$$\frac{i(3x^2 - 8ix + 11)a}{3((ix + 1)a)^{\frac{3}{4}}(-ix - 1)a^{\frac{1}{4}}} + \frac{7 \operatorname{RootOf}(-Z^2 - i) \ln \left(\frac{-x^3 - (-x^4 + 2ix^3 + 2ix + 1)^{\frac{1}{4}} x^2 \operatorname{RootOf}(-Z^2 - i) + 2ix^2 + 2i(-x^4 + 2ix^3 + 2ix + 1)^{\frac{1}{4}} x \operatorname{RootOf}(-Z^2 - i) - i \sqrt{-1}}{\dots} \right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(7/4)/(I*a*x+a)^(7/4),x)

[Out] $\frac{1}{3}I*(-8Ix+3x^2+11)/((Ix+1)a)^{3/4}/(-(Ix-1)a)^{1/4}a+(-7/2\text{RootOf}(_Z^2-I)*\ln((-x^4+2Ix^3+2Ix+1)^{1/4}*\text{RootOf}(_Z^2-I)*x^2-I*\text{RootOf}(_Z^2-I)*(-x^4+2Ix^3+2Ix+1)^{3/4}-x^3+2I*\text{RootOf}(_Z^2-I)*(-x^4+2Ix^3+2Ix+1)^{1/4})-I*(-x^4+2Ix^3+2Ix+1)^{1/2}*x+2Ix^2+\text{RootOf}(_Z^2-I)*(-x^4+2Ix^3+2Ix+1)^{1/4}-(-x^4+2Ix^3+2Ix+1)^{1/2}+x)/(Ix+1)^2)+7/2I*\text{RootOf}(_Z^2-I)*\ln(-I*(-x^4+2Ix^3+2Ix+1)^{1/4}*\text{RootOf}(_Z^2-I)*x^2-2*\text{RootOf}(_Z^2-I)*(-x^4+2Ix^3+2Ix+1)^{1/4})+x^3-\text{RootOf}(_Z^2-I)*(-x^4+2Ix^3+2Ix+1)^{3/4}-I*(-x^4+2Ix^3+2Ix+1)^{1/2}*x+I*\text{RootOf}(_Z^2-I)*(-x^4+2Ix^3+2Ix+1)^{1/4}-2Ix^2-(-x^4+2Ix^3+2Ix+1)^{1/2}-x)/(Ix+1)^2))/((Ix+1)a)^{3/4}*(-(Ix-1)*(Ix+1)^3)^{1/4}/(-(Ix-1)a)^{1/4}a$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{\frac{7}{4}}}{(iax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(7/4)/(I*a*x + a)^(7/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a - a x 1i)^{7/4}}{(a + a x 1i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - a*x*1i)^(7/4)/(a + a*x*1i)^(7/4),x)

[Out] int((a - a*x*1i)^(7/4)/(a + a*x*1i)^(7/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-ia(x+i))^{\frac{7}{4}}}{(ia(x-i))^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)**(7/4)/(a+I*a*x)**(7/4),x)

[Out] Integral((-I*a*(x + I))**(7/4)/(I*a*(x - I))**(7/4), x)

$$3.1195 \quad \int \frac{(a-iax)^{3/4}}{(a+iax)^{7/4}} dx$$

Optimal. Leaf size=266

$$\frac{4i(a-iax)^{3/4}}{3a(a+iax)^{3/4}} - \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} + \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} + \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} - i\sqrt{2}$$

[Out] $4/3*I*(a-I*a*x)^{(3/4)}/a/(a+I*a*x)^{(3/4)}-1/2*I*\ln(1-(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2)})/a*2^{(1/2)}+1/2*I*\ln(1+(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2)})/a*2^{(1/2)}+I*\arctan(1-(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)})*2^{(1/2)}/a-I*\arctan(1+(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)})*2^{(1/2)}/a$

Rubi [A] time = 0.14, antiderivative size = 266, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 9, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.360$, Rules used = {47, 63, 331, 297, 1162, 617, 204, 1165, 628}

$$\frac{4i(a-iax)^{3/4}}{3a(a+iax)^{3/4}} - \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} + \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} + \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} - i\sqrt{2}$$

Antiderivative was successfully verified.

[In] Int[(a - I*a*x)^(3/4)/(a + I*a*x)^(7/4), x]

[Out] $((4*I)/3)*(a - I*a*x)^{(3/4)}/(a*(a + I*a*x)^{(3/4)}) + (I*Sqrt[2]*ArcTan[1 - (Sqrt[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/a - (I*Sqrt[2]*ArcTan[1 + (Sqrt[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/a - (I*Log[1 + Sqrt[a - I*a*x]/Sqrt[a + I*a*x] - (Sqrt[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/(Sqrt[2]*a) + (I*Log[1 + Sqrt[a - I*a*x]/Sqrt[a + I*a*x] + (Sqrt[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/(Sqrt[2]*a)$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 297

```
Int[(x_)^2/((a_) + (b_.)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[a/b,
2]], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*s), Int[(r + s*x^2)/(a + b*x^4
), x], x] - Dist[1/(2*s), Int[(r - s*x^2)/(a + b*x^4), x], x] /; FreeQ[{a,
b}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] &
& AtomQ[SplitProduct[SumBaseQ, b]]))
```

Rule 331

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m +
1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)
^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2
^(-1)] && IntegersQ[m, p + (m + 1)/n]
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c]) /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 1162

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x], x] + Dist[e
/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x] /; FreeQ[{a, c, d, e}, x] &
```

& EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]

Rule 1165

Int[((d_) + (e_)*(x_)^2)/((a_) + (c_)*(x_)^4), x_Symbol] := With[{q = Rt[(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x], x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]

Rubi steps

$$\begin{aligned}
 \int \frac{(a - iax)^{3/4}}{(a + iax)^{7/4}} dx &= \frac{4i(a - iax)^{3/4}}{3a(a + iax)^{3/4}} - \int \frac{1}{\sqrt[4]{a - iax} (a + iax)^{3/4}} dx \\
 &= \frac{4i(a - iax)^{3/4}}{3a(a + iax)^{3/4}} - \frac{(4i) \text{Subst} \left(\int \frac{x^2}{(2a - x^4)^{3/4}} dx, x, \sqrt[4]{a - iax} \right)}{a} \\
 &= \frac{4i(a - iax)^{3/4}}{3a(a + iax)^{3/4}} - \frac{(4i) \text{Subst} \left(\int \frac{x^2}{1 + x^4} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{a} \\
 &= \frac{4i(a - iax)^{3/4}}{3a(a + iax)^{3/4}} + \frac{(2i) \text{Subst} \left(\int \frac{1 - x^2}{1 + x^4} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{a} - \frac{(2i) \text{Subst} \left(\int \frac{1 + x^2}{1 + x^4} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{a} \\
 &= \frac{4i(a - iax)^{3/4}}{3a(a + iax)^{3/4}} - \frac{i \text{Subst} \left(\int \frac{1}{1 - \sqrt{2}x + x^2} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{a} - \frac{i \text{Subst} \left(\int \frac{1}{1 + \sqrt{2}x + x^2} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{a} \\
 &= \frac{4i(a - iax)^{3/4}}{3a(a + iax)^{3/4}} - \frac{i \log \left(1 + \frac{\sqrt{a - iax}}{\sqrt{a + iax}} - \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{\sqrt{2} a} + \frac{i \log \left(1 + \frac{\sqrt{a - iax}}{\sqrt{a + iax}} + \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{\sqrt{2} a} - \frac{(i\sqrt{2}) \text{Subst} \left(\int \frac{1}{1 - x^2} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{a} \\
 &= \frac{4i(a - iax)^{3/4}}{3a(a + iax)^{3/4}} + \frac{i\sqrt{2} \tan^{-1} \left(1 - \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{a} - \frac{i\sqrt{2} \tan^{-1} \left(1 + \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{a} - \frac{i \log \left(1 + \frac{\sqrt{a - iax}}{\sqrt{a + iax}} \right)}{\sqrt{2} a}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.26

$$\frac{i\sqrt{2} (1 + ix)^{3/4} (a - iax)^{7/4} {}_2F_1 \left(\frac{7}{4}, \frac{7}{4}; \frac{11}{4}; \frac{1}{2} - \frac{ix}{2} \right)}{7a^2 (a + iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(3/4)/(a + I*a*x)^(7/4), x]

[Out] ((I/7)*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(7/4)*Hypergeometric2F1[7/4, 7/4, 11/4, 1/2 - (I/2)*x])/(a^2*(a + I*a*x)^(3/4))

fricas [A] time = 0.51, size = 304, normalized size = 1.14

$$3(a^2x - ia^2)\sqrt{\frac{4i}{a^2}} \log\left(\frac{(a^2x+ia^2)\sqrt{\frac{4i}{a^2}}+2(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{3}{4}}}{2x+2i}\right) - 3(a^2x - ia^2)\sqrt{\frac{4i}{a^2}} \log\left(\frac{(a^2x+ia^2)\sqrt{\frac{4i}{a^2}}-2(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{3}{4}}}{2x+2i}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(7/4), x, algorithm="fricas")

[Out] -1/6*(3*(a^2*x - I*a^2)*sqrt(4*I/a^2)*log(((a^2*x + I*a^2)*sqrt(4*I/a^2) + 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4))/(2*x + 2*I)) - 3*(a^2*x - I*a^2)*sqrt(4*I/a^2)*log(-((a^2*x + I*a^2)*sqrt(4*I/a^2) - 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4))/(2*x + 2*I)) + 3*(a^2*x - I*a^2)*sqrt(-4*I/a^2)*log(((a^2*x + I*a^2)*sqrt(-4*I/a^2) + 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4))/(2*x + 2*I)) - 3*(a^2*x - I*a^2)*sqrt(-4*I/a^2)*log(-((a^2*x + I*a^2)*sqrt(-4*I/a^2) - 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4))/(2*x + 2*I)) - 8*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4)/(a^2*x - I*a^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{\frac{3}{4}}}{(iax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(7/4), x, algorithm="giac")

[Out] integrate((-I*a*x + a)^(3/4)/(I*a*x + a)^(7/4), x)

maple [C] time = 1.88, size = 459, normalized size = 1.73

$$\frac{\frac{4x}{3} + \frac{4i}{3}}{((ix + 1)a)^{\frac{3}{4}}(-ix - 1)a^{\frac{1}{4}}} \left(i \operatorname{RootOf}(-Z^2 + i) \ln\left(\frac{-x^3 - i(-x^4 + 2ix^3 + 2ix + 1)^{\frac{1}{4}}x^2 \operatorname{RootOf}(-Z^2 + i) + 2ix^2 - 2(-x^4 + 2ix^3 + 2ix + 1)^{\frac{1}{4}}x \operatorname{RootOf}(-Z^2 + i)}{(-ix - 1)a^{\frac{1}{4}}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-I*a*x+a)^(3/4)/(I*a*x+a)^(7/4),x)`

[Out] $4/3*(x+I)/((I*x+1)*a)^{3/4}/(-(I*x-1)*a)^{1/4}-(-\text{RootOf}(_Z^2+I)*\ln(-(-\text{RootOf}(_Z^2+I)*(-x^4+2*I*x^3+2*I*x+1)^{1/4}*x^2+x^3+I*\text{RootOf}(_Z^2+I)*(-x^4+2*I*x^3+2*I*x+1)^{3/4}+2*I*\text{RootOf}(_Z^2+I)*(-x^4+2*I*x^3+2*I*x+1)^{1/4}*x-I*(-x^4+2*I*x^3+2*I*x+1)^{1/2}*x-2*I*x^2+(-x^4+2*I*x^3+2*I*x+1)^{1/4}*\text{RootOf}(_Z^2+I)-(-x^4+2*I*x^3+2*I*x+1)^{1/2}-x)/(I*x+1)^2)+I*\text{RootOf}(_Z^2+I)*\ln((-I*(-x^4+2*I*x^3+2*I*x+1)^{1/4}*\text{RootOf}(_Z^2+I)*x^2-2*\text{RootOf}(_Z^2+I)*(-x^4+2*I*x^3+2*I*x+1)^{1/4}*x-x^3-I*(-x^4+2*I*x^3+2*I*x+1)^{1/2}*x+\text{RootOf}(_Z^2+I)*(-x^4+2*I*x^3+2*I*x+1)^{3/4}+I*\text{RootOf}(_Z^2+I)*(-x^4+2*I*x^3+2*I*x+1)^{1/4}+2*I*x^2-(-x^4+2*I*x^3+2*I*x+1)^{1/2}+x)/(I*x+1)^2))/((I*x+1)*a)^{3/4}*(-(I*x-1)*(I*x+1)^3)^{1/4}/(-(I*x-1)*a)^{1/4}$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i a x + a)^{\frac{3}{4}}}{(i a x + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")`

[Out] `integrate((-I*a*x + a)^(3/4)/(I*a*x + a)^(7/4), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a - a x 1i)^{3/4}}{(a + a x 1i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - a*x*1i)^(3/4)/(a + a*x*1i)^(7/4),x)`

[Out] `int((a - a*x*1i)^(3/4)/(a + a*x*1i)^(7/4), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i a (x + i))^{\frac{3}{4}}}{(i a (x - i))^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)**(3/4)/(a+I*a*x)**(7/4),x)`

[Out] `Integral((-I*a*(x + I))**(3/4)/(I*a*(x - I))**(7/4), x)`

$$3.1196 \quad \int \frac{1}{\sqrt[4]{a-iax} (a+iax)^{7/4}} dx$$

Optimal. Leaf size=33

$$\frac{2i(a-iax)^{3/4}}{3a^2(a+iax)^{3/4}}$$

[Out] $2/3*I*(a-I*a*x)^{(3/4)}/a^2/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.00, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.040$, Rules used = {37}

$$\frac{2i(a-iax)^{3/4}}{3a^2(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a - I*a*x)^{(1/4)}*(a + I*a*x)^{(7/4))}, x]$

[Out] $((2*I)/3)*(a - I*a*x)^{(3/4)}/(a^2*(a + I*a*x)^{(3/4)})$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_. + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Simp} [((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{1}{\sqrt[4]{a-iax} (a+iax)^{7/4}} dx = \frac{2i(a-iax)^{3/4}}{3a^2(a+iax)^{3/4}}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 1.00

$$\frac{2i(a-iax)^{3/4}}{3a^2(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/((a - I*a*x)^{(1/4)}*(a + I*a*x)^{(7/4))}, x]$

[Out] $((2*I)/3)*(a - I*a*x)^{(3/4)}/(a^2*(a + I*a*x)^{(3/4)})$

fricas [A] time = 0.44, size = 31, normalized size = 0.94

$$\frac{2 (i a x + a)^{\frac{1}{4}} (-i a x + a)^{\frac{3}{4}}}{3 (a^3 x - i a^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(7/4),x, algorithm="fricas")

[Out] 2/3*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4)/(a^3*x - I*a^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{7}{4}} (-i a x + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(7/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(1/4)), x)

maple [A] time = 0.04, size = 31, normalized size = 0.94

$$\frac{\frac{2x}{3} + \frac{2i}{3}}{((ix + 1)a)^{\frac{3}{4}} (-ix - 1)a^{\frac{1}{4}} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(1/4)/(I*a*x+a)^(7/4),x)

[Out] 2/3/a/((I*x+1)*a)^(3/4)/(-(I*x-1)*a)^(1/4)*(x+I)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{7}{4}} (-i a x + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{1}{(a - a x 1i)^{1/4} (a + a x 1i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(1/4)*(a + a*x*1i)^(7/4)), x)

[Out] int(1/((a - a*x*1i)^(1/4)*(a + a*x*1i)^(7/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x - i))^{7/4} \sqrt[4]{-ia(x + i)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(1/4)/(a+I*a*x)**(7/4), x)

[Out] Integral(1/((I*a*(x - I))**(7/4)*(-I*a*(x + I))**(1/4)), x)

$$3.1197 \quad \int \frac{1}{(a-iax)^{5/4}(a+iax)^{7/4}} dx$$

Optimal. Leaf size=65

$$\frac{4i(a-iax)^{3/4}}{3a^3(a+iax)^{3/4}} - \frac{2i}{a^2\sqrt[4]{a-iax}(a+iax)^{3/4}}$$

[Out] $-2*I/a^2/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(3/4)}+4/3*I*(a-I*a*x)^{(3/4)}/a^3/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.01, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$\frac{4i(a-iax)^{3/4}}{3a^3(a+iax)^{3/4}} - \frac{2i}{a^2\sqrt[4]{a-iax}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(5/4)*(a + I*a*x)^(7/4)), x]

[Out] $(-2*I)/(a^2*(a - I*a*x)^{(1/4)*(a + I*a*x)^{(3/4)}) + (((4*I)/3)*(a - I*a*x)^{(3/4)})/(a^3*(a + I*a*x)^{(3/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a - iax)^{5/4}(a + iax)^{7/4}} dx = -\frac{2i}{a^2 \sqrt[4]{a - iax} (a + iax)^{3/4}} + \frac{2 \int \frac{1}{\sqrt[4]{a - iax} (a + iax)^{7/4}} dx}{a}$$

$$= -\frac{2i}{a^2 \sqrt[4]{a - iax} (a + iax)^{3/4}} + \frac{4i(a - iax)^{3/4}}{3a^3(a + iax)^{3/4}}$$

Mathematica [A] time = 0.02, size = 38, normalized size = 0.58

$$\frac{4x - 2i}{3a^2 \sqrt[4]{a - iax} (a + iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(5/4)*(a + I*a*x)^(7/4)), x]

[Out] (-2*I + 4*x)/(3*a^2*(a - I*a*x)^(1/4)*(a + I*a*x)^(3/4))

fricas [A] time = 0.46, size = 36, normalized size = 0.55

$$\frac{(iax + a)^{\frac{1}{4}}(-iax + a)^{\frac{3}{4}}(4x - 2i)}{3(a^4x^2 + a^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(7/4), x, algorithm="fricas")

[Out] 1/3*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4)*(4*x - 2*I)/(a^4*x^2 + a^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{7}{4}}(-iax + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(7/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(5/4)), x)

maple [A] time = 0.05, size = 33, normalized size = 0.51

$$\frac{\frac{4x}{3} - \frac{2i}{3}}{((ix + 1)a)^{\frac{3}{4}}(-ix - 1)a^{\frac{1}{4}}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(5/4)/(I*a*x+a)^(7/4),x)`

[Out] `2/3/a^2/((I*x+1)*a)^(3/4)/(-I*x-1)*a)^(1/4)*(2*x-I)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{7}{4}}(-iax+a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")`

[Out] `integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(5/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{1}{(a-ax1i)^{5/4}(a+ax1i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(5/4)*(a + a*x*1i)^(7/4)),x)`

[Out] `int(1/((a - a*x*1i)^(5/4)*(a + a*x*1i)^(7/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{7}{4}}(-ia(x+i))^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(5/4)/(a+I*a*x)**(7/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(7/4)*(-I*a*(x + I))**(5/4)), x)`

$$3.1198 \quad \int \frac{1}{(a-iax)^{9/4}(a+iax)^{7/4}} dx$$

Optimal. Leaf size=100

$$\frac{16i(a-iax)^{3/4}}{15a^4(a+iax)^{3/4}} - \frac{8i}{5a^3(a+iax)^{3/4}\sqrt[4]{a-iax}} - \frac{2i}{5a^2(a+iax)^{3/4}(a-iax)^{5/4}}$$

[Out] $-2/5*I/a^2/(a-I*a*x)^{(5/4)}/(a+I*a*x)^{(3/4)}-8/5*I/a^3/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(3/4)}+16/15*I*(a-I*a*x)^{(3/4)}/a^4/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.02, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$\frac{16i(a-iax)^{3/4}}{15a^4(a+iax)^{3/4}} - \frac{8i}{5a^3(a+iax)^{3/4}\sqrt[4]{a-iax}} - \frac{2i}{5a^2(a+iax)^{3/4}(a-iax)^{5/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(9/4)*(a + I*a*x)^(7/4)), x]

[Out] $((-2*I)/5)/(a^2*(a - I*a*x)^{(5/4)*(a + I*a*x)^{(3/4)})} - ((8*I)/5)/(a^3*(a - I*a*x)^{(1/4)*(a + I*a*x)^{(3/4)})} + (((16*I)/15)*(a - I*a*x)^{(3/4)})/(a^4*(a + I*a*x)^{(3/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a-iax)^{9/4}(a+iax)^{7/4}} dx &= -\frac{2i}{5a^2(a-iax)^{5/4}(a+iax)^{3/4}} + \frac{4 \int \frac{1}{(a-iax)^{5/4}(a+iax)^{7/4}} dx}{5a} \\
&= -\frac{2i}{5a^2(a-iax)^{5/4}(a+iax)^{3/4}} - \frac{8i}{5a^3 \sqrt[4]{a-iax}(a+iax)^{3/4}} + \frac{8 \int \frac{1}{\sqrt[4]{a-iax}(a+iax)^{7/4}} dx}{5a^2} \\
&= -\frac{2i}{5a^2(a-iax)^{5/4}(a+iax)^{3/4}} - \frac{8i}{5a^3 \sqrt[4]{a-iax}(a+iax)^{3/4}} + \frac{16i(a-iax)^{3/4}}{15a^4(a+iax)^{3/4}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 50, normalized size = 0.50

$$\frac{2(8x^2 + 4ix + 7)}{15a^3(x+i)\sqrt[4]{a-iax}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(9/4)*(a + I*a*x)^(7/4)), x]

[Out] (2*(7 + (4*I)*x + 8*x^2))/(15*a^3*(I + x)*(a - I*a*x)^(1/4)*(a + I*a*x)^(3/4))

fricas [A] time = 0.44, size = 58, normalized size = 0.58

$$\frac{2(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{3}{4}}(8x^2+4ix+7)}{15a^5x^3+15ia^5x^2+15a^5x+15ia^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(7/4), x, algorithm="fricas")

[Out] 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(3/4)*(8*x^2 + 4*I*x + 7)/(15*a^5*x^3 + 15*I*a^5*x^2 + 15*a^5*x + 15*I*a^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{7}{4}}(-iax+a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(7/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(9/4)), x)

maple [A] time = 0.06, size = 44, normalized size = 0.44

$$\frac{\frac{16}{15}x^2 + \frac{8}{15}ix + \frac{14}{15}}{((ix + 1)a)^{\frac{3}{4}}(-ix - 1)a^{\frac{1}{4}}(x + i)a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(9/4)/(I*a*x+a)^(7/4),x)

[Out] 2/15/a^3/((I*x+1)*a)^(3/4)/(-I*x-1)*a)^(1/4)*(8*x^2+4*I*x+7)/(x+I)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x i)^{9/4} (a + a x i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(9/4)*(a + a*x*1i)^(7/4)),x)

[Out] int(1/((a - a*x*1i)^(9/4)*(a + a*x*1i)^(7/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{7}{4}}(-ia(x+i))^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(9/4)/(a+I*a*x)**(7/4),x)

[Out] Integral(1/((I*a*(x - I))**(7/4)*(-I*a*(x + I))**(9/4)), x)

$$3.1199 \quad \int \frac{(a-iax)^{9/4}}{(a+iax)^{7/4}} dx$$

Optimal. Leaf size=139

$$-\frac{10a^2(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{(a+iax)^{3/4}(a-iax)^{3/4}} + \frac{4i(a-iax)^{9/4}}{3a(a+iax)^{3/4}} + \frac{2i\sqrt[4]{a+iax}(a-iax)^{5/4}}{a} + 10i\sqrt[4]{a+iax}\sqrt[4]{a-iax}$$

[Out] $4/3 I (a - I a x)^{9/4} / a / (a + I a x)^{3/4} + 10 I (a - I a x)^{1/4} (a + I a x)^{1/4} + 2 I (a - I a x)^{5/4} (a + I a x)^{1/4} / a - 10 a^2 (x^2 + 1)^{3/4} (\cos(1/2 \arctan(x))^2)^{1/2} / \cos(1/2 \arctan(x)) * \operatorname{EllipticF}(\sin(1/2 \arctan(x)), 2^{1/2}) / (a - I a x)^{3/4} / (a + I a x)^{3/4}$

Rubi [A] time = 0.03, antiderivative size = 139, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 50, 42, 233, 231}

$$-\frac{10a^2(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{(a+iax)^{3/4}(a-iax)^{3/4}} + \frac{4i(a-iax)^{9/4}}{3a(a+iax)^{3/4}} + \frac{2i\sqrt[4]{a+iax}(a-iax)^{5/4}}{a} + 10i\sqrt[4]{a+iax}\sqrt[4]{a-iax}$$

Antiderivative was successfully verified.

[In] Int[(a - I*a*x)^(9/4)/(a + I*a*x)^(7/4), x]

[Out] $((4I/3)(a - I a x)^{9/4} / (a (a + I a x)^{3/4}) + (10I)(a - I a x)^{1/4} (a + I a x)^{1/4} + ((2I)(a - I a x)^{5/4} (a + I a x)^{1/4}) / a - (10 a^2 (1 + x^2)^{3/4} \operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2]) / ((a - I a x)^{3/4} (a + I a x)^{3/4})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m]) / (a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n / (b*(m + 1)), x] - Dist[(d*n) / (b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 231

```
Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Simp[(2*EllipticF[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(3/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 233

```
Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(
a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a - iax)^{9/4}}{(a + iax)^{7/4}} dx &= \frac{4i(a - iax)^{9/4}}{3a(a + iax)^{3/4}} - 3 \int \frac{(a - iax)^{5/4}}{(a + iax)^{3/4}} dx \\
&= \frac{4i(a - iax)^{9/4}}{3a(a + iax)^{3/4}} + \frac{2i(a - iax)^{5/4} \sqrt[4]{a + iax}}{a} - (5a) \int \frac{\sqrt[4]{a - iax}}{(a + iax)^{3/4}} dx \\
&= \frac{4i(a - iax)^{9/4}}{3a(a + iax)^{3/4}} + 10i \sqrt[4]{a - iax} \sqrt[4]{a + iax} + \frac{2i(a - iax)^{5/4} \sqrt[4]{a + iax}}{a} - (5a^2) \int \frac{1}{(a - iax)^{3/4}(a + iax)} dx \\
&= \frac{4i(a - iax)^{9/4}}{3a(a + iax)^{3/4}} + 10i \sqrt[4]{a - iax} \sqrt[4]{a + iax} + \frac{2i(a - iax)^{5/4} \sqrt[4]{a + iax}}{a} - \frac{(5a^2 (a^2 + a^2 x^2)^{3/4}) \int \frac{1}{(a^2 + a^2 x^2)} dx}{(a - iax)^{3/4}(a + iax)} \\
&= \frac{4i(a - iax)^{9/4}}{3a(a + iax)^{3/4}} + 10i \sqrt[4]{a - iax} \sqrt[4]{a + iax} + \frac{2i(a - iax)^{5/4} \sqrt[4]{a + iax}}{a} - \frac{(5a^2 (1 + x^2)^{3/4}) \int \frac{1}{(1 + x^2)} dx}{(a - iax)^{3/4}(a + iax)^{3/4}} \\
&= \frac{4i(a - iax)^{9/4}}{3a(a + iax)^{3/4}} + 10i \sqrt[4]{a - iax} \sqrt[4]{a + iax} + \frac{2i(a - iax)^{5/4} \sqrt[4]{a + iax}}{a} - \frac{10a^2 (1 + x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}\left(\frac{x}{\sqrt{1 + x^2}}\right)\right)}{(a - iax)^{3/4}(a + iax)^{3/4}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.50

$$\frac{i\sqrt[4]{2}(1+ix)^{3/4}(a-iax)^{13/4} {}_2F_1\left(\frac{7}{4}, \frac{13}{4}; \frac{17}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{13a^2(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(9/4)/(a + I*a*x)^(7/4), x]

[Out] ((I/13)*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(13/4)*Hypergeometric2F1[7/4, 13/4, 17/4, 1/2 - (I/2)*x])/(a^2*(a + I*a*x)^(3/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\frac{(3x - 3i)\operatorname{integral}\left(-\frac{5(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{x^2+1}, x\right) + 2(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}(x^2 + 11ix + 20)}{3x - 3i}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(9/4)/(a+I*a*x)^(7/4), x, algorithm="fricas")

[Out] ((3*x - 3*I)*integral(-5*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(x^2 + 1), x) + 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)*(x^2 + 11*I*x + 20))/(3*x - 3*I)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(9/4)/(a+I*a*x)^(7/4), x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command:
INPUT:sage2OUTPUT:ext_reduce Error: Bad Argument Typeintegrate(i/4*a/a^2*(-16*((i*a*x+a)^(1/4))^8*(-((i*a*x+a)^(1/4))^4+2*a)^(1/4)+64*((i*a*x+a)^(1/4))^4*a*(-((i*a*x+a)^(1/4))^4+2*a)^(1/4)-64*a^2*(-((i*a*x+a)^(1/4))^4+2*a)^(1/4))/((i*a*x+a)^(1/4))^4/4*i*a*((i*a*x+a)^(1/4))^(-3,x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{\frac{9}{4}}}{(iax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-I*a*x+a)^(9/4)/(I*a*x+a)^(7/4),x)`

[Out] `int((-I*a*x+a)^(9/4)/(I*a*x+a)^(7/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{\frac{9}{4}}}{(iax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)^(9/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")`

[Out] `integrate((-I*a*x + a)^(9/4)/(I*a*x + a)^(7/4), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - ax1i)^{9/4}}{(a + ax1i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - a*x*1i)^(9/4)/(a + a*x*1i)^(7/4),x)`

[Out] `int((a - a*x*1i)^(9/4)/(a + a*x*1i)^(7/4), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-ia(x+i))^{\frac{9}{4}}}{(ia(x-i))^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)**(9/4)/(a+I*a*x)**(7/4),x)`

[Out] `Integral((-I*a*(x + I))**(9/4)/(I*a*(x - I))**(7/4), x)`

$$3.1200 \quad \int \frac{(a-iax)^{5/4}}{(a+iax)^{7/4}} dx$$

Optimal. Leaf size=113

$$-\frac{10a(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{3(a+iax)^{3/4}(a-iax)^{3/4}} + \frac{4i(a-iax)^{5/4}}{3a(a+iax)^{3/4}} + \frac{10i\sqrt[4]{a+iax}\sqrt[4]{a-iax}}{3a}$$

[Out] $4/3*I*(a-I*a*x)^{(5/4)}/a/(a+I*a*x)^{(3/4)}+10/3*I*(a-I*a*x)^{(1/4)}*(a+I*a*x)^{(1/4)}/a-10/3*a*(x^2+1)^{(3/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\operatorname{EllipticF}(\sin(1/2*\arctan(x)), 2^{(1/2)})/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.02, antiderivative size = 113, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 50, 42, 233, 231}

$$-\frac{10a(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3(a+iax)^{3/4}(a-iax)^{3/4}} + \frac{4i(a-iax)^{5/4}}{3a(a+iax)^{3/4}} + \frac{10i\sqrt[4]{a+iax}\sqrt[4]{a-iax}}{3a}$$

Antiderivative was successfully verified.

[In] Int[(a - I*a*x)^(5/4)/(a + I*a*x)^(7/4), x]

[Out] $((4*I)/3)*(a - I*a*x)^{(5/4)}/(a*(a + I*a*x)^{(3/4)}) + ((10*I)/3)*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)}/a - (10*a*(1 + x^2)^{(3/4)}*\operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2])/((3*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 231

```
Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Simp[(2*EllipticF[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(3/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 233

```
Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(
a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a - iax)^{5/4}}{(a + iax)^{7/4}} dx &= \frac{4i(a - iax)^{5/4}}{3a(a + iax)^{3/4}} - \frac{5}{3} \int \frac{\sqrt[4]{a - iax}}{(a + iax)^{3/4}} dx \\
&= \frac{4i(a - iax)^{5/4}}{3a(a + iax)^{3/4}} + \frac{10i\sqrt[4]{a - iax}\sqrt[4]{a + iax}}{3a} - \frac{1}{3}(5a) \int \frac{1}{(a - iax)^{3/4}(a + iax)^{3/4}} dx \\
&= \frac{4i(a - iax)^{5/4}}{3a(a + iax)^{3/4}} + \frac{10i\sqrt[4]{a - iax}\sqrt[4]{a + iax}}{3a} - \frac{(5a(a^2 + a^2x^2)^{3/4}) \int \frac{1}{(a^2 + a^2x^2)^{3/4}} dx}{3(a - iax)^{3/4}(a + iax)^{3/4}} \\
&= \frac{4i(a - iax)^{5/4}}{3a(a + iax)^{3/4}} + \frac{10i\sqrt[4]{a - iax}\sqrt[4]{a + iax}}{3a} - \frac{(5a(1 + x^2)^{3/4}) \int \frac{1}{(1 + x^2)^{3/4}} dx}{3(a - iax)^{3/4}(a + iax)^{3/4}} \\
&= \frac{4i(a - iax)^{5/4}}{3a(a + iax)^{3/4}} + \frac{10i\sqrt[4]{a - iax}\sqrt[4]{a + iax}}{3a} - \frac{10a(1 + x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3(a - iax)^{3/4}(a + iax)^{3/4}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.62

$$\frac{i\sqrt[4]{2}(1 + ix)^{3/4}(a - iax)^{9/4} {}_2F_1\left(\frac{7}{4}, \frac{9}{4}; \frac{13}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{9a^2(a + iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(5/4)/(a + I*a*x)^(7/4), x]

[Out] ((I/9)*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(9/4)*Hypergeometric2F1[7/4, 9/4, 13/4, 1/2 - (I/2)*x])/(a^2*(a + I*a*x)^(3/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\frac{3(ax - ia) \operatorname{integral} \left(-\frac{5(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{3(ax^2+a)}, x \right) - 2(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}(-3ix-7)}{3(ax-ia)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(7/4), x, algorithm="fricas")

[Out] 1/3*(3*(a*x - I*a)*integral(-5/3*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a*x^2 + a), x) - 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)*(-3*I*x - 7))/(a*x - I*a)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(7/4), x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command:
INPUT:sage2OUTPUT:ext_reduce Error: Bad Argument Typeintegrate(i/4*a/a^2*(1
6*((i*a*x+a)^(1/4))^4*(-((i*a*x+a)^(1/4))^4+2*a)^(1/4)-32*a*(-((i*a*x+a)^(1
/4))^4+2*a)^(1/4))/((i*a*x+a)^(1/4))^4/4*i*a*((i*a*x+a)^(1/4))^(-3,x)

maple [F] time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{\frac{5}{4}}}{(iax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(5/4)/(I*a*x+a)^(7/4), x)

[Out] int((-I*a*x+a)^(5/4)/(I*a*x+a)^(7/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i ax + a)^{\frac{5}{4}}}{(i ax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(5/4)/(I*a*x + a)^(7/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - a x 1i)^{5/4}}{(a + a x 1i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - a*x*1i)^(5/4)/(a + a*x*1i)^(7/4),x)

[Out] int((a - a*x*1i)^(5/4)/(a + a*x*1i)^(7/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-ia(x+i))^{\frac{5}{4}}}{(ia(x-i))^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)**(5/4)/(a+I*a*x)**(7/4),x)

[Out] Integral((-I*a*(x + I))**(5/4)/(I*a*(x - I))**(7/4), x)

$$3.1201 \quad \int \frac{\sqrt[4]{a-iax}}{(a+iax)^{7/4}} dx$$

Optimal. Leaf size=79

$$\frac{4i\sqrt[4]{a-iax}}{3a(a+iax)^{3/4}} - \frac{2(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2}\tan^{-1}(x), 2\right)}{3(a-iax)^{3/4}(a+iax)^{3/4}}$$

[Out] $4/3*I*(a-I*a*x)^{(1/4)}/a/(a+I*a*x)^{(3/4)}-2/3*(x^2+1)^{(3/4)}*(\cos(1/2*\arctan(x)))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\operatorname{EllipticF}(\sin(1/2*\arctan(x)), 2^{(1/2)})/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.01, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {47, 42, 233, 231}

$$\frac{4i\sqrt[4]{a-iax}}{3a(a+iax)^{3/4}} - \frac{2(x^2+1)^{3/4} F\left(\frac{1}{2}\tan^{-1}(x) \middle| 2\right)}{3(a-iax)^{3/4}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a - I*a*x)^{(1/4)}/(a + I*a*x)^{(7/4)}, x]$

[Out] $((4*I)/3)*(a - I*a*x)^{(1/4)}/(a*(a + I*a*x)^{(3/4)}) - (2*(1 + x^2)^{(3/4)}*\operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2])/(3*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)})$

Rule 42

$\operatorname{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] := \operatorname{Dist}[(a + b*x)^{\operatorname{FracPart}[m]}*(c + d*x)^{\operatorname{FracPart}[m]}/(a*c + b*d*x^2)^{\operatorname{FracPart}[m]}, \operatorname{Int}[(a*c + b*d*x^2)^m, x], x] /; \operatorname{FreeQ}[\{a, b, c, d, m\}, x] \&\& \operatorname{EqQ}[b*c + a*d, 0] \&\& \operatorname{IntegerQ}[2*m]$

Rule 47

$\operatorname{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /; \operatorname{FreeQ}[\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m]) \&\& !(\operatorname{ILeQ}[m+n+2, 0] \&\& (\operatorname{FractionQ}[m] || \operatorname{GeQ}[2*n+m+1, 0])) \& \& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 231

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Simp[(2*EllipticF[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(3/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 233

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt[4]{a-iax}}{(a+iax)^{7/4}} dx &= \frac{4i\sqrt[4]{a-iax}}{3a(a+iax)^{3/4}} - \frac{1}{3} \int \frac{1}{(a-iax)^{3/4}(a+iax)^{3/4}} dx \\ &= \frac{4i\sqrt[4]{a-iax}}{3a(a+iax)^{3/4}} - \frac{(a^2+a^2x^2)^{3/4} \int \frac{1}{(a^2+a^2x^2)^{3/4}} dx}{3(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= \frac{4i\sqrt[4]{a-iax}}{3a(a+iax)^{3/4}} - \frac{(1+x^2)^{3/4} \int \frac{1}{(1+x^2)^{3/4}} dx}{3(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= \frac{4i\sqrt[4]{a-iax}}{3a(a+iax)^{3/4}} - \frac{2(1+x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3(a-iax)^{3/4}(a+iax)^{3/4}} \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.89

$$\frac{i\sqrt[4]{2}(1+ix)^{3/4}(a-iax)^{5/4} {}_2F_1\left(\frac{5}{4}, \frac{7}{4}; \frac{9}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{5a^2(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(1/4)/(a + I*a*x)^(7/4), x]

[Out] ((I/5)*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(5/4)*Hypergeometric2F1[5/4, 7/4, 9/4, 1/2 - (I/2)*x])/(a^2*(a + I*a*x)^(3/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\frac{3(a^2x - ia^2) \operatorname{integral}\left(-\frac{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{3(a^2x^2+a^2)}, x\right) + 4(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{3(a^2x - ia^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(7/4),x, algorithm="fricas")

[Out] 1/3*(3*(a^2*x - I*a^2)*integral(-1/3*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a^2*x^2 + a^2), x) + 4*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a^2*x - I*a^2)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(7/4),x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x);;OUTPUT:

maple [F] time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{\frac{1}{4}}}{(iax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(1/4)/(I*a*x+a)^(7/4),x)

[Out] int((-I*a*x+a)^(1/4)/(I*a*x+a)^(7/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{\frac{1}{4}}}{(iax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(1/4)/(I*a*x + a)^(7/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - ax1i)^{1/4}}{(a + ax1i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - a*x*Ii)^(1/4)/(a + a*x*Ii)^(7/4), x)`

[Out] `int((a - a*x*Ii)^(1/4)/(a + a*x*Ii)^(7/4), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[4]{-ia(x+i)}^{\frac{7}{4}}}{(ia(x-i))^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)**(1/4)/(a+I*a*x)**(7/4), x)`

[Out] `Integral((-I*a*(x + I))**(1/4)/(I*a*(x - I))**(7/4), x)`

$$3.1202 \quad \int \frac{1}{(a-iax)^{3/4}(a+iax)^{7/4}} dx$$

Optimal. Leaf size=82

$$\frac{2(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{3a(a-iax)^{3/4}(a+iax)^{3/4}} + \frac{2i\sqrt[4]{a-iax}}{3a^2(a+iax)^{3/4}}$$

[Out] $2/3 I (a - I a x)^{1/4} / a^2 (a + I a x)^{3/4} + 2/3 (x^2 + 1)^{3/4} (\cos(1/2 \arctan(x))^2)^{1/2} / \cos(1/2 \arctan(x)) \operatorname{EllipticF}(\sin(1/2 \arctan(x)), 2^{1/2}) / a / (a - I a x)^{3/4} / (a + I a x)^{3/4}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {51, 42, 233, 231}

$$\frac{2i\sqrt[4]{a-iax}}{3a^2(a+iax)^{3/4}} + \frac{2(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3a(a-iax)^{3/4}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] `Int[1/((a - I*a*x)^(3/4)*(a + I*a*x)^(7/4)), x]`

[Out] `((2*I)/3)*(a - I*a*x)^(1/4)/(a^2*(a + I*a*x)^(3/4)) + (2*(1 + x^2)^(3/4)*EllipticF[ArcTan[x]/2, 2])/(3*a*(a - I*a*x)^(3/4)*(a + I*a*x)^(3/4))`

Rule 42

`Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]`

Rule 51

`Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && !ntLinearQ[a, b, c, d, m, n, x]`

Rule 231

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Simp[(2*EllipticF[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(3/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 233

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a-iax)^{3/4}(a+iax)^{7/4}} dx &= \frac{2i\sqrt[4]{a-iax}}{3a^2(a+iax)^{3/4}} + \frac{\int \frac{1}{(a-iax)^{3/4}(a+iax)^{3/4}} dx}{3a} \\ &= \frac{2i\sqrt[4]{a-iax}}{3a^2(a+iax)^{3/4}} + \frac{(a^2+a^2x^2)^{3/4} \int \frac{1}{(a^2+a^2x^2)^{3/4}} dx}{3a(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= \frac{2i\sqrt[4]{a-iax}}{3a^2(a+iax)^{3/4}} + \frac{(1+x^2)^{3/4} \int \frac{1}{(1+x^2)^{3/4}} dx}{3a(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= \frac{2i\sqrt[4]{a-iax}}{3a^2(a+iax)^{3/4}} + \frac{2(1+x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3a(a-iax)^{3/4}(a+iax)^{3/4}} \end{aligned}$$

Mathematica [C] time = 0.02, size = 68, normalized size = 0.83

$$\frac{i\sqrt[4]{2}(1+ix)^{3/4}\sqrt[4]{a-iax} {}_2F_1\left(\frac{1}{4}, \frac{7}{4}; \frac{5}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{a^2(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(3/4)*(a + I*a*x)^(7/4)), x]

[Out] (I*2^(1/4)*(1 + I*x)^(3/4)*(a - I*a*x)^(1/4)*Hypergeometric2F1[1/4, 7/4, 5/4, 1/2 - (I/2)*x])/(a^2*(a + I*a*x)^(3/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\frac{3(a^3x - ia^3) \operatorname{integral}\left(\frac{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{3(a^3x^2+a^3)}, x\right) + 2(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{3(a^3x - ia^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(7/4),x, algorithm="fricas")

[Out] 1/3*(3*(a^3*x - I*a^3)*integral(1/3*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a^3*x^2 + a^3), x) + 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a^3*x - I*a^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{7}{4}} (-i a x + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(7/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(3/4)), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{1}{(-i a x + a)^{\frac{3}{4}} (i a x + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(3/4)/(I*a*x+a)^(7/4),x)

[Out] int(1/(-I*a*x+a)^(3/4)/(I*a*x+a)^(7/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{7}{4}} (-i a x + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{\frac{3}{4}} (a + a x 1i)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a - a*x*1i)^(3/4)*(a + a*x*1i)^(7/4)),x)
```

```
[Out] int(1/((a - a*x*1i)^(3/4)*(a + a*x*1i)^(7/4)), x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{7}{4}}(-ia(x+i))^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a-I*a*x)**(3/4)/(a+I*a*x)**(7/4),x)
```

```
[Out] Integral(1/((I*a*(x - I))**(7/4)*(-I*a*(x + I))**(3/4)), x)
```

$$3.1203 \quad \int \frac{1}{(a-iax)^{7/4}(a+iax)^{7/4}} dx$$

Optimal. Leaf size=81

$$\frac{2(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}} + \frac{2x}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}}$$

[Out] $2/3*x/a^2/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}+2/3*(x^2+1)^{(3/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\operatorname{EllipticF}(\sin(1/2*\arctan(x)), 2^{(1/2)})/a^2/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.01, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {42, 199, 233, 231}

$$\frac{2(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}} + \frac{2x}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a - I*a*x)^{(7/4)}*(a + I*a*x)^{(7/4))}, x]$

[Out] $(2*x)/(3*a^2*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)}) + (2*(1 + x^2)^{(3/4)}*\operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2])/(3*a^2*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)})$

Rule 42

$\operatorname{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(m_+)}, x_Symbol] \rightarrow \operatorname{Dist}[(a + b*x)^{\operatorname{FracPart}[m]}*(c + d*x)^{\operatorname{FracPart}[m]}]/(a*c + b*d*x^2)^{\operatorname{FracPart}[m]}, \operatorname{Int}[(a*c + b*d*x^2)^m, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, m\}, x \&\& \operatorname{EqQ}[b*c + a*d, 0] \&\& !\operatorname{IntegerQ}[2*m]$

Rule 199

$\operatorname{Int}[(a_+ + (b_+)*(x_+)^{(n_+)})^{(p_+)}, x_Symbol] \rightarrow -\operatorname{Simp}[(x*(a + b*x^n)^{(p+1)})/(a*n*(p+1)), x] + \operatorname{Dist}[(n*(p+1) + 1)/(a*n*(p+1)), \operatorname{Int}[(a + b*x^n)^{(p+1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b\}, x \&\& \operatorname{IGtQ}[n, 0] \&\& \operatorname{LtQ}[p, -1] \&\& (\operatorname{IntegerQ}[2*p] \mid\mid (n == 2 \&\& \operatorname{IntegerQ}[4*p]) \mid\mid (n == 2 \&\& \operatorname{IntegerQ}[3*p]) \mid\mid \operatorname{Denominator}[p + 1/n] < \operatorname{Denominator}[p])$

Rule 231

$\operatorname{Int}[(a_+ + (b_+)*(x_+)^2)^{(-3/4)}, x_Symbol] \rightarrow \operatorname{Simp}[(2*\operatorname{EllipticF}[(1*\operatorname{ArcTan}[Rt[b/a, 2]*x])/2, 2])/(a^{(3/4)}*Rt[b/a, 2]), x] /;$ $\operatorname{FreeQ}\{a, b\}, x \&\& \operatorname{GtQ}[a$

, 0] && PosQ[b/a]

Rule 233

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] & & PosQ[a]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a-iax)^{7/4}(a+iax)^{7/4}} dx &= \frac{(a^2+a^2x^2)^{3/4} \int \frac{1}{(a^2+a^2x^2)^{7/4}} dx}{(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= \frac{2x}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}} + \frac{(a^2+a^2x^2)^{3/4} \int \frac{1}{(a^2+a^2x^2)^{3/4}} dx}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= \frac{2x}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}} + \frac{(1+x^2)^{3/4} \int \frac{1}{(1+x^2)^{3/4}} dx}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}} \\ &= \frac{2x}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}} + \frac{2(1+x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}} \end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.86

$$\frac{i\sqrt[4]{2}(1+ix)^{3/4} {}_2F_1\left(-\frac{3}{4}, \frac{7}{4}; \frac{1}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{3a^2(a-iax)^{3/4}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(7/4)*(a + I*a*x)^(7/4)), x]

[Out] ((-1/3*I)*2^(1/4)*(1 + I*x)^(3/4)*Hypergeometric2F1[-3/4, 7/4, 1/4, 1/2 - (I/2)*x])/(a^2*(a - I*a*x)^(3/4)*(a + I*a*x)^(3/4))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\frac{3(a^4x^2 + a^4) \operatorname{integral}\left(\frac{(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{3(a^4x^2+a^4)}, x\right) + 2(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}x}{3(a^4x^2 + a^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(7/4),x, algorithm="fricas")

[Out] 1/3*(3*(a^4*x^2 + a^4)*integral(1/3*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a^4*x^2 + a^4), x) + 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)*x/(a^4*x^2 + a^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{7}{4}}(-i a x + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(7/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(7/4)), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{1}{(-i a x + a)^{\frac{7}{4}}(i a x + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(7/4)/(I*a*x+a)^(7/4),x)

[Out] int(1/(-I*a*x+a)^(7/4)/(I*a*x+a)^(7/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{7}{4}}(-i a x + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(7/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{7/4} (a + a x 1i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(7/4)*(a + a*x*1i)^(7/4)),x)`

[Out] `int(1/((a - a*x*1i)^(7/4)*(a + a*x*1i)^(7/4)), x)`

sympy [A] time = 36.70, size = 95, normalized size = 1.17

$$\frac{iG_{6,6}^{5,3} \left(\begin{matrix} \frac{7}{8}, \frac{11}{8}, 1 \\ \frac{7}{8}, \frac{5}{4}, \frac{11}{8}, \frac{7}{4}, \frac{9}{4} \end{matrix} \middle| \frac{e^{-3i\pi}}{x^2} \right) e^{-\frac{i\pi}{4}}}{4\pi a^{\frac{7}{2}} \Gamma\left(\frac{7}{4}\right)} + \frac{iG_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, 0, \frac{3}{8}, \frac{1}{2}, \frac{7}{8}, 1 \\ \frac{3}{8}, \frac{7}{8} \end{matrix} \middle| \frac{e^{-i\pi}}{x^2} \right)}{4\pi a^{\frac{7}{2}} \Gamma\left(\frac{7}{4}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(7/4)/(a+I*a*x)**(7/4),x)`

[Out] `-I*meijerg(((7/8, 11/8, 1), (1/2, 7/4, 9/4)), ((7/8, 5/4, 11/8, 7/4, 9/4), (0,)), exp_polar(-3*I*pi)/x**2)*exp(-I*pi/4)/(4*pi*a**(7/2)*gamma(7/4)) + I*meijerg(((-1/2, 0, 3/8, 1/2, 7/8, 1), ()), ((3/8, 7/8), (-1/2, 0, 5/4, 0)), exp_polar(-I*pi)/x**2)/(4*pi*a**(7/2)*gamma(7/4))`

$$3.1204 \quad \int \frac{1}{(a-iax)^{11/4}(a+iax)^{7/4}} dx$$

Optimal. Leaf size=114

$$\frac{10(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{21a^3(a-iax)^{3/4}(a+iax)^{3/4}} + \frac{10x}{21a^3(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{2i}{7a^2(a-iax)^{7/4}(a+iax)^{3/4}}$$

[Out] $-2/7*I/a^2/(a-I*a*x)^{(7/4)}/(a+I*a*x)^{(3/4)}+10/21*x/a^3/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}+10/21*(x^2+1)^{(3/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\operatorname{EllipticF}(\sin(1/2*\arctan(x)), 2^{(1/2)})/a^3/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.02, antiderivative size = 114, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 42, 199, 233, 231}

$$\frac{10(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{21a^3(a-iax)^{3/4}(a+iax)^{3/4}} + \frac{10x}{21a^3(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{2i}{7a^2(a-iax)^{7/4}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a - I*a*x)^{(11/4)}*(a + I*a*x)^{(7/4))}, x]$

[Out] $((-2*I)/7)/(a^2*(a - I*a*x)^{(7/4)}*(a + I*a*x)^{(3/4)}) + (10*x)/(21*a^3*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)}) + (10*(1 + x^2)^{(3/4)}*\operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2])/(21*a^3*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)})$

Rule 42

$\operatorname{Int}[(a_ + (b_)*x_)^{(m_)}*((c_ + (d_)*x_)^{(m_)}), x_Symbol] \rightarrow \operatorname{Dist}[(a + b*x)^{\operatorname{FracPart}[m]}*(c + d*x)^{\operatorname{FracPart}[m]}/(a*c + b*d*x^2)^{\operatorname{FracPart}[m]}, \operatorname{Int}[(a*c + b*d*x^2)^m, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \operatorname{EqQ}[b*c + a*d, 0] \ \&\& \ !\operatorname{IntegerQ}[2*m]$

Rule 51

$\operatorname{Int}[(a_ + (b_)*x_)^{(m_)}*((c_ + (d_)*x_)^{(n_)}), x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}/((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*(m+n+2))/((b*c - a*d)*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^n, x] /;$ $\operatorname{FreeQ}\{a, b, c, d, n\}, x \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{LtQ}[m, -1] \ \&\& \ !(\operatorname{LtQ}[n, -1] \ \&\& \ (\operatorname{EqQ}[a, 0] \ || \ (\operatorname{NeQ}[c, 0] \ \&\& \ \operatorname{LtQ}[m-n, 0] \ \&\& \ \operatorname{IntegerQ}[n]))) \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 199

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := -Simp[(x*(a + b*x^n)^(p + 1))/(a*n*(p + 1)), x] + Dist[(n*(p + 1) + 1)/(a*n*(p + 1)), Int[(a + b*x^n)^(p + 1), x], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[p, -1] && (IntegerQ[2*p] || (n == 2 && IntegerQ[4*p]) || (n == 2 && IntegerQ[3*p]) || Denominator[p + 1/n] < Denominator[p])

Rule 231

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Simp[(2*EllipticF[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(3/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 233

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a - iax)^{11/4}(a + iax)^{7/4}} dx &= -\frac{2i}{7a^2(a - iax)^{7/4}(a + iax)^{3/4}} + \frac{5 \int \frac{1}{(a - iax)^{7/4}(a + iax)^{7/4}} dx}{7a} \\
 &= -\frac{2i}{7a^2(a - iax)^{7/4}(a + iax)^{3/4}} + \frac{\left(5(a^2 + a^2x^2)^{3/4}\right) \int \frac{1}{(a^2 + a^2x^2)^{7/4}} dx}{7a(a - iax)^{3/4}(a + iax)^{3/4}} \\
 &= -\frac{2i}{7a^2(a - iax)^{7/4}(a + iax)^{3/4}} + \frac{10x}{21a^3(a - iax)^{3/4}(a + iax)^{3/4}} + \frac{\left(5(a^2 + a^2x^2)^{3/4}\right) \int \frac{1}{(a^2 + a^2x^2)^{7/4}} dx}{21a^3(a - iax)^{3/4}(a + iax)^{3/4}} \\
 &= -\frac{2i}{7a^2(a - iax)^{7/4}(a + iax)^{3/4}} + \frac{10x}{21a^3(a - iax)^{3/4}(a + iax)^{3/4}} + \frac{\left(5(1 + x^2)^{3/4}\right) \int \frac{1}{(1 + x^2)^{7/4}} dx}{21a^3(a - iax)^{3/4}(a + iax)^{3/4}} \\
 &= -\frac{2i}{7a^2(a - iax)^{7/4}(a + iax)^{3/4}} + \frac{10x}{21a^3(a - iax)^{3/4}(a + iax)^{3/4}} + \frac{10(1 + x^2)^{3/4} F\left(\frac{1}{2} \tan^{-1}\left(\frac{x}{a}\right)\right)}{21a^3(a - iax)^{3/4}(a + iax)^{3/4}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.61

$$-\frac{i\sqrt{2}(1 + ix)^{3/4} {}_2F_1\left(-\frac{7}{4}, \frac{7}{4}; -\frac{3}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{7a^2(a - iax)^{7/4}(a + iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(11/4)*(a + I*a*x)^(7/4)),x]

[Out] ((-1/7*I)*2^(1/4)*(1 + I*x)^(3/4)*Hypergeometric2F1[-7/4, 7/4, -3/4, 1/2 - (I/2)*x])/(a^2*(a - I*a*x)^(7/4)*(a + I*a*x)^(3/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\frac{(21 a^5 x^3 + 21 i a^5 x^2 + 21 a^5 x + 21 i a^5) \operatorname{integral} \left(\frac{5 (i a x + a)^{\frac{1}{4}} (-i a x + a)^{\frac{1}{4}}}{21 (a^5 x^2 + a^5)}, x \right) + 2 (i a x + a)^{\frac{1}{4}} (-i a x + a)^{\frac{1}{4}} (5 x^2 + 5 i x + 3)}{21 a^5 x^3 + 21 i a^5 x^2 + 21 a^5 x + 21 i a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(7/4),x, algorithm="fricas")

[Out] ((21*a^5*x^3 + 21*I*a^5*x^2 + 21*a^5*x + 21*I*a^5)*integral(5/21*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a^5*x^2 + a^5), x) + 2*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)*(5*x^2 + 5*I*x + 3))/(21*a^5*x^3 + 21*I*a^5*x^2 + 21*a^5*x + 21*I*a^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{7}{4}} (-i a x + a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(7/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(11/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(-i a x + a)^{\frac{11}{4}} (i a x + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(11/4)/(I*a*x+a)^(7/4),x)

[Out] int(1/(-I*a*x+a)^(11/4)/(I*a*x+a)^(7/4),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.
```

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{11/4} (a + a x 1i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a - a*x*1i)^(11/4)*(a + a*x*1i)^(7/4)),x)
```

```
[Out] int(1/((a - a*x*1i)^(11/4)*(a + a*x*1i)^(7/4)), x)
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a-I*a*x)**(11/4)/(a+I*a*x)**(7/4),x)
```

```
[Out] Timed out
```

$$3.1205 \quad \int \frac{1}{(a-iax)^{15/4}(a+iax)^{7/4}} dx$$

Optimal. Leaf size=147

$$\frac{10(x^2+1)^{3/4} \operatorname{EllipticF}\left(\frac{1}{2} \tan^{-1}(x), 2\right)}{33a^4(a-iax)^{3/4}(a+iax)^{3/4}} + \frac{10x}{33a^4(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{2i}{11a^3(a-iax)^{7/4}(a+iax)^{3/4}} - \frac{2i}{11a^2(a-iax)^{11/4}(a+iax)^{3/4}}$$

[Out] $-2/11*I/a^2/(a-I*a*x)^{(11/4)}/(a+I*a*x)^{(3/4)}-2/11*I/a^3/(a-I*a*x)^{(7/4)}/(a+I*a*x)^{(3/4)}+10/33*x/a^4/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}+10/33*(x^2+1)^{(3/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\operatorname{EllipticF}(\sin(1/2*\arctan(x)), 2^{(1/2)})/a^4/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(3/4)}$

Rubi [A] time = 0.04, antiderivative size = 147, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 42, 199, 233, 231}

$$\frac{10(x^2+1)^{3/4} F\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{33a^4(a-iax)^{3/4}(a+iax)^{3/4}} + \frac{10x}{33a^4(a-iax)^{3/4}(a+iax)^{3/4}} - \frac{2i}{11a^3(a-iax)^{7/4}(a+iax)^{3/4}} - \frac{2i}{11a^2(a-iax)^{11/4}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a - I*a*x)^{(15/4)}*(a + I*a*x)^{(7/4))}, x]$

[Out] $((-2*I)/11)/(a^2*(a - I*a*x)^{(11/4)}*(a + I*a*x)^{(3/4)}) - ((2*I)/11)/(a^3*(a - I*a*x)^{(7/4)}*(a + I*a*x)^{(3/4)}) + (10*x)/(33*a^4*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)}) + (10*(1 + x^2)^{(3/4)}*\operatorname{EllipticF}[\operatorname{ArcTan}[x]/2, 2])/(33*a^4*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)})$

Rule 42

$\operatorname{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] \rightarrow \operatorname{Dist}[(a_+ + b_+*x_+)^{\operatorname{FracPart}[m_+]}*(c_+ + d_+*x_+)^{\operatorname{FracPart}[n_+]}/(a_+*c_+ + b_+*d_+*x_+^2)^{\operatorname{FracPart}[m_+]}, \operatorname{Int}[(a_+*c_+ + b_+*d_+*x_+^2)^m, x], x] /; \operatorname{FreeQ}\{a, b, c, d, m\}, x] \&\& \operatorname{EqQ}[b*c + a*d, 0] \&\& \operatorname{IntegerQ}[2*m]$

Rule 51

$\operatorname{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] \rightarrow \operatorname{Simp}[(a_+ + b_+*x_+)^{(m_+ + 1)}*(c_+ + d_+*x_+)^{(n_+ + 1)}/((b_+*c_+ - a_+*d_+)*(m_+ + 1)), x] - \operatorname{Dist}[(d_+*(m_+ + n_+ + 2))/((b_+*c_+ - a_+*d_+)*(m_+ + 1)), \operatorname{Int}[(a_+ + b_+*x_+)^{(m_+ + 1)}*(c_+ + d_+*x_+)^n, x], x] /; \operatorname{FreeQ}\{a, b, c, d, n\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[m, -1] \&\& \operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[n] \&\& (\operatorname{EqQ}[a, 0] \mid \mid (\operatorname{NeQ}[c, 0] \&\& \operatorname{LtQ}[m - n, 0] \&\& \operatorname{IntegerQ}[n])) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 199

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := -Simp[(x*(a + b*x^n)^(p + 1))/(a*n*(p + 1)), x] + Dist[(n*(p + 1) + 1)/(a*n*(p + 1)), Int[(a + b*x^n)^(p + 1), x], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[p, -1] && (IntegerQ[2*p] || (n == 2 && IntegerQ[4*p]) || (n == 2 && IntegerQ[3*p]) || Denominator[p + 1/n] < Denominator[p])

Rule 231

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Simp[(2*EllipticF[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(3/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 233

Int[((a_) + (b_.)*(x_)^2)^(-3/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(3/4)/(a + b*x^2)^(3/4), Int[1/(1 + (b*x^2)/a)^(3/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a - iax)^{15/4}(a + iax)^{7/4}} dx &= -\frac{2i}{11a^2(a - iax)^{11/4}(a + iax)^{3/4}} + \frac{7 \int \frac{1}{(a - iax)^{11/4}(a + iax)^{7/4}} dx}{11a} \\
 &= -\frac{2i}{11a^2(a - iax)^{11/4}(a + iax)^{3/4}} - \frac{2i}{11a^3(a - iax)^{7/4}(a + iax)^{3/4}} + \frac{5 \int \frac{1}{(a - iax)^{7/4}(a + iax)^{7/4}}}{11a^2} \\
 &= -\frac{2i}{11a^2(a - iax)^{11/4}(a + iax)^{3/4}} - \frac{2i}{11a^3(a - iax)^{7/4}(a + iax)^{3/4}} + \frac{\left(5(a^2 + a^2x^2)^{3/4}\right)}{11a^2(a - iax)^{3/4}} \\
 &= -\frac{2i}{11a^2(a - iax)^{11/4}(a + iax)^{3/4}} - \frac{2i}{11a^3(a - iax)^{7/4}(a + iax)^{3/4}} + \frac{10x}{33a^4(a - iax)^{3/4}(a + iax)^{3/4}} \\
 &= -\frac{2i}{11a^2(a - iax)^{11/4}(a + iax)^{3/4}} - \frac{2i}{11a^3(a - iax)^{7/4}(a + iax)^{3/4}} + \frac{10x}{33a^4(a - iax)^{3/4}(a + iax)^{3/4}} \\
 &= -\frac{2i}{11a^2(a - iax)^{11/4}(a + iax)^{3/4}} - \frac{2i}{11a^3(a - iax)^{7/4}(a + iax)^{3/4}} + \frac{10x}{33a^4(a - iax)^{3/4}(a + iax)^{3/4}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.48

$$\frac{i\sqrt[4]{2}(1+ix)^{3/4} {}_2F_1\left(-\frac{11}{4}, \frac{7}{4}; -\frac{7}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{11a^2(a-iax)^{11/4}(a+iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(15/4)*(a + I*a*x)^(7/4)), x]

[Out] ((-1/11*I)*2^(1/4)*(1 + I*x)^(3/4)*Hypergeometric2F1[-11/4, 7/4, -7/4, 1/2 - (I/2)*x])/(a^2*(a - I*a*x)^(11/4)*(a + I*a*x)^(3/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\frac{(33a^6x^4 + 66ia^6x^3 + 66ia^6x - 33a^6)\operatorname{integral}\left(\frac{5(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{33(a^6x^2+a^6)}, x\right) + (10x^3 + 20ix^2 - 4x + 12i)(iax+a)^{\frac{1}{4}}(-iax+a)^{\frac{1}{4}}}{33a^6x^4 + 66ia^6x^3 + 66ia^6x - 33a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(15/4)/(a+I*a*x)^(7/4), x, algorithm="fricas")

[Out] ((33*a^6*x^4 + 66*I*a^6*x^3 + 66*I*a^6*x - 33*a^6)*integral(5/33*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4)/(a^6*x^2 + a^6), x) + (10*x^3 + 20*I*x^2 - 4*x + 12*I)*(I*a*x + a)^(1/4)*(-I*a*x + a)^(1/4))/(33*a^6*x^4 + 66*I*a^6*x^3 + 66*I*a^6*x - 33*a^6)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{7}{4}}(-iax+a)^{\frac{15}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(15/4)/(a+I*a*x)^(7/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(7/4)*(-I*a*x + a)^(15/4)), x)

maple [F] time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{1}{(-iax+a)^{\frac{15}{4}}(iax+a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(15/4)/(I*a*x+a)^(7/4), x)

[Out] `int(1/(-I*a*x+a)^(15/4)/(I*a*x+a)^(7/4),x)`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(15/4)/(a+I*a*x)^(7/4),x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{15/4} (a + a x 1i)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(15/4)*(a + a*x*1i)^(7/4)),x)`

[Out] `int(1/((a - a*x*1i)^(15/4)*(a + a*x*1i)^(7/4)), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(15/4)/(a+I*a*x)**(7/4),x)`

[Out] Timed out

$$3.1206 \quad \int \frac{(a-iax)^{7/4}}{(a+iax)^{5/4}} dx$$

Optimal. Leaf size=137

$$\frac{14a\sqrt[4]{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{\sqrt[4]{a+iax}\sqrt[4]{a-iax}} + \frac{4i(a-iax)^{7/4}}{a\sqrt[4]{a+iax}} + \frac{14i(a+iax)^{3/4}(a-iax)^{3/4}}{3a} - \frac{14ax}{\sqrt[4]{a+iax}\sqrt[4]{a-iax}}$$

[Out] $-14*a*x/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}+4*I*(a-I*a*x)^{(7/4)}/a/(a+I*a*x)^{(1/4)}+14/3*I*(a-I*a*x)^{(3/4)}*(a+I*a*x)^{(3/4)}/a+14*a*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x)))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.03, antiderivative size = 137, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.240$, Rules used = {47, 50, 42, 229, 227, 196}

$$\frac{14a\sqrt[4]{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{\sqrt[4]{a+iax}\sqrt[4]{a-iax}} + \frac{4i(a-iax)^{7/4}}{a\sqrt[4]{a+iax}} + \frac{14i(a+iax)^{3/4}(a-iax)^{3/4}}{3a} - \frac{14ax}{\sqrt[4]{a+iax}\sqrt[4]{a-iax}}$$

Antiderivative was successfully verified.

[In] Int[(a - I*a*x)^(7/4)/(a + I*a*x)^(5/4), x]

[Out] $(-14*a*x)/((a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)}) + ((4*I)*(a - I*a*x)^{(7/4)})/(a*(a + I*a*x)^{(1/4)}) + (((14*I)/3)*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(3/4)})/a + (14*a*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/((a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && ( !IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 196

```
Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 227

```
Int[((a_) + (b_.)*(x_)^2)^(-1/4), x_Symbol] := Simp[(2*x)/(a + b*x^2)^(1/4)
, x] - Dist[a, Int[1/(a + b*x^2)^(5/4), x], x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 229

```
Int[((a_) + (b_.)*(x_)^2)^(-1/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(
a + b*x^2)^(1/4), Int[1/(1 + (b*x^2)/a)^(1/4), x], x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a - iax)^{7/4}}{(a + iax)^{5/4}} dx &= \frac{4i(a - iax)^{7/4}}{a\sqrt[4]{a + iax}} - 7 \int \frac{(a - iax)^{3/4}}{\sqrt[4]{a + iax}} dx \\
&= \frac{4i(a - iax)^{7/4}}{a\sqrt[4]{a + iax}} + \frac{14i(a - iax)^{3/4}(a + iax)^{3/4}}{3a} - (7a) \int \frac{1}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} dx \\
&= \frac{4i(a - iax)^{7/4}}{a\sqrt[4]{a + iax}} + \frac{14i(a - iax)^{3/4}(a + iax)^{3/4}}{3a} - \frac{(7a\sqrt[4]{a^2 + a^2x^2}) \int \frac{1}{\sqrt[4]{a^2 + a^2x^2}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= \frac{4i(a - iax)^{7/4}}{a\sqrt[4]{a + iax}} + \frac{14i(a - iax)^{3/4}(a + iax)^{3/4}}{3a} - \frac{(7a\sqrt[4]{1 + x^2}) \int \frac{1}{\sqrt[4]{1 + x^2}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= -\frac{14ax}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} + \frac{4i(a - iax)^{7/4}}{a\sqrt[4]{a + iax}} + \frac{14i(a - iax)^{3/4}(a + iax)^{3/4}}{3a} + \frac{(7a\sqrt[4]{1 + x^2}) \int \frac{1}{(1+x^2)^{5/4}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= -\frac{14ax}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} + \frac{4i(a - iax)^{7/4}}{a\sqrt[4]{a + iax}} + \frac{14i(a - iax)^{3/4}(a + iax)^{3/4}}{3a} + \frac{14a\sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1} x\right)}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.51

$$\frac{i2^{3/4}\sqrt[4]{1+ix}(a-iax)^{11/4}{}_2F_1\left(\frac{5}{4}, \frac{11}{4}; \frac{15}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{11a^2\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(7/4)/(a + I*a*x)^(5/4), x]

[Out] ((I/11)*2^(3/4)*(1 + I*x)^(1/4)*(a - I*a*x)^(11/4)*Hypergeometric2F1[5/4, 1/4, 15/4, 1/2 - (I/2)*x])/(a^2*(a + I*a*x)^(1/4))

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\frac{(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}}(2ix^2 - 16x + 42i) + (3ax^2 - 3iax)\text{integral}\left(-\frac{14(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{ax^4+ax^2}, x\right)}{3ax^2 - 3iax}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(5/4), x, algorithm="fricas")

[Out] $((I*a*x + a)^{3/4}*(-I*a*x + a)^{3/4}*(2*I*x^2 - 16*x + 42*I) + (3*a*x^2 - 3*I*a*x)*\text{integral}(-14*(I*a*x + a)^{3/4}*(-I*a*x + a)^{3/4}/(a*x^4 + a*x^2), x))/(3*a*x^2 - 3*I*a*x)$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(5/4),x, algorithm="giac")`

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command: INPUT:sage2OUTPUT:Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}+%%{1,[0,4]%%}] at parameters values [70,22]Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}+%%{1,[0,4]%%}] at parameters values [42,56]Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}+%%{1,[0,4]%%}] at parameters values [-9,-13]Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}+%%{1,[0,4]%%}] at parameters values [46,24]Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}+%%{1,[0,4]%%}] at parameters values [49,-6]ext_reduce Error: Bad Argument TypeEvaluation time: 0.66integrate(i/4*a/a^2*(16*(i*a*x+a)^(1/4))^4*((-(i*a*x+a)^(1/4))^4+2*a)^(1/4))^3-32*a*((-(i*a*x+a)^(1/4))^4+2*a)^(1/4))^3)/((i*a*x+a)^(1/4))^2/4*i*a*((i*a*x+a)^(1/4))^(-3,x)

maple [C] time = 0.07, size = 96, normalized size = 0.70

$$\frac{7(-ix-1)(ix+1)a^2)^{\frac{1}{4}} ax \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{(a^2)^{\frac{1}{4}}(-ix-1)a^{\frac{1}{4}}((ix+1)a)^{\frac{1}{4}}} + \frac{2i(x^2-12ix+13)a}{3(-ix-1)a^{\frac{1}{4}}((ix+1)a)^{\frac{1}{4}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-I*a*x+a)^(7/4)/(I*a*x+a)^(5/4),x)`

[Out] $2/3*I*(x^2+13-12*I*x)*a/(-(I*x-1)*a)^{1/4}/((I*x+1)*a)^{1/4}-7/(a^2)^{1/4}*x*\operatorname{hypergeom}([1/4,1/2],[3/2],-x^2)*a*(-(I*x-1)*(I*x+1)*a^2)^{1/4}/(-(I*x-1)*a)^{1/4}/((I*x+1)*a)^{1/4}$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax+a)^{\frac{7}{4}}}{(iax+a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(5/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(7/4)/(I*a*x + a)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - a x 1i)^{7/4}}{(a + a x 1i)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - a*x*1i)^(7/4)/(a + a*x*1i)^(5/4),x)

[Out] int((a - a*x*1i)^(7/4)/(a + a*x*1i)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-ia(x+i))^{7/4}}{(ia(x-i))^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)**(7/4)/(a+I*a*x)**(5/4),x)

[Out] Integral((-I*a*(x + I))**(7/4)/(I*a*(x - I))**(5/4), x)

$$3.1207 \quad \int \frac{(a-iax)^{3/4}}{(a+iax)^{5/4}} dx$$

Optimal. Leaf size=102

$$\frac{6\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{\sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{6x}{\sqrt[4]{a-iax} \sqrt[4]{a+iax}} + \frac{4i(a-iax)^{3/4}}{a\sqrt[4]{a+iax}}$$

[Out] $-6*x/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}+4*I*(a-I*a*x)^{(3/4)}/a/(a+I*a*x)^{(1/4)}+6*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 42, 229, 227, 196}

$$\frac{6\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{\sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{6x}{\sqrt[4]{a-iax} \sqrt[4]{a+iax}} + \frac{4i(a-iax)^{3/4}}{a\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a - I*a*x)^{(3/4)}/(a + I*a*x)^{(5/4)}, x]$

[Out] $(-6*x)/((a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)}) + ((4*I)*(a - I*a*x)^{(3/4)})/(a*(a + I*a*x)^{(1/4)}) + (6*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/((a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Dist}[(a + b*x)^{\text{FracPart}[m]}*(c + d*x)^{\text{FracPart}[m]}/(a*c + b*d*x^2)^{\text{FracPart}[m]}, \text{Int}[(a*c + b*d*x^2)^m, x], x] /; \text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{EqQ}[b*c + a*d, 0] \ \&\& \ !\text{IntegerQ}[2*m]$

Rule 47

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{m+1}*(c + d*x)^n/(b*(m+1)), x] - \text{Dist}[(d*n)/(b*(m+1)), \text{Int}[(a + b*x)^{m+1}*(c + d*x)^{n-1}, x], x] /; \text{FreeQ}\{a, b, c, d\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{LtQ}[m, -1] \ \&\& \ !(\text{IntegerQ}[n] \ \&\& \ !\text{IntegerQ}[m]) \ \&\& \ !(\text{ILeQ}[m+n+2, 0] \ \&\& \ (\text{FractionQ}[m] \ || \ \text{GeQ}[2*n+m+1, 0])) \ \& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 196

```
Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 227

```
Int[((a_) + (b_.)*(x_)^2)^(-1/4), x_Symbol] := Simp[(2*x)/(a + b*x^2)^(1/4)
, x] - Dist[a, Int[1/(a + b*x^2)^(5/4), x], x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 229

```
Int[((a_) + (b_.)*(x_)^2)^(-1/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(
a + b*x^2)^(1/4), Int[1/(1 + (b*x^2)/a)^(1/4), x], x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a - iax)^{3/4}}{(a + iax)^{5/4}} dx &= \frac{4i(a - iax)^{3/4}}{a\sqrt[4]{a + iax}} - 3 \int \frac{1}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} dx \\
&= \frac{4i(a - iax)^{3/4}}{a\sqrt[4]{a + iax}} - \frac{\left(3\sqrt[4]{a^2 + a^2x^2}\right) \int \frac{1}{\sqrt[4]{a^2 + a^2x^2}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= \frac{4i(a - iax)^{3/4}}{a\sqrt[4]{a + iax}} - \frac{\left(3\sqrt[4]{1 + x^2}\right) \int \frac{1}{\sqrt[4]{1 + x^2}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= -\frac{6x}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} + \frac{4i(a - iax)^{3/4}}{a\sqrt[4]{a + iax}} + \frac{\left(3\sqrt[4]{1 + x^2}\right) \int \frac{1}{(1+x^2)^{5/4}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= -\frac{6x}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} + \frac{4i(a - iax)^{3/4}}{a\sqrt[4]{a + iax}} + \frac{6\sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.69

$$\frac{i2^{3/4} \sqrt[4]{1 + ix} (a - iax)^{7/4} {}_2F_1\left(\frac{5}{4}, \frac{7}{4}; \frac{11}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{7a^2 \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(3/4)/(a + I*a*x)^(5/4), x]

[Out] ((I/7)*2^(3/4)*(1 + I*x)^(1/4)*(a - I*a*x)^(7/4)*Hypergeometric2F1[5/4, 7/4, 11/4, 1/2 - (I/2)*x])/(a^2*(a + I*a*x)^(1/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\frac{(i a x + a)^{\frac{3}{4}}(-i a x + a)^{\frac{3}{4}}(2 x - 6 i) - (a^2 x^2 - i a^2 x) \operatorname{integral}\left(-\frac{6(i a x + a)^{\frac{3}{4}}(-i a x + a)^{\frac{3}{4}}}{a^2 x^4 + a^2 x^2}, x\right)}{a^2 x^2 - i a^2 x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(5/4), x, algorithm="fricas")

[Out] -((I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*(2*x - 6*I) - (a^2*x^2 - I*a^2*x)*integral(-6*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^2*x^4 + a^2*x^2), x))/(a^2*x^2 - I*a^2*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i a x + a)^{\frac{3}{4}}}{(i a x + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(5/4), x, algorithm="giac")

[Out] integrate((-I*a*x + a)^(3/4)/(I*a*x + a)^(5/4), x)

maple [C] time = 0.06, size = 88, normalized size = 0.86

$$\frac{3 \left(-(ix - 1)(ix + 1)a^2 \right)^{\frac{1}{4}} x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{\left(a^2\right)^{\frac{1}{4}} (-ix - 1)a^{\frac{1}{4}} ((ix + 1)a)^{\frac{1}{4}}} + \frac{4x + 4i}{(-ix - 1)a^{\frac{1}{4}} ((ix + 1)a)^{\frac{1}{4}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(3/4)/(I*a*x+a)^(5/4), x)

[Out] 4*(x+I)/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)-3/(a^2)^(1/4)*x*hypergeom([1/4, 1/2], [3/2], -x^2)*(-(I*x-1)*(I*x+1)*a^2)^(1/4)/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i a x + a)^{\frac{3}{4}}}{(i a x + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(5/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(3/4)/(I*a*x + a)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - a x 1i)^{3/4}}{(a + a x 1i)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - a*x*1i)^(3/4)/(a + a*x*1i)^(5/4),x)

[Out] int((a - a*x*1i)^(3/4)/(a + a*x*1i)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i a (x + i))^{\frac{3}{4}}}{(i a (x - i))^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)**(3/4)/(a+I*a*x)**(5/4),x)

[Out] Integral((-I*a*(x + I))**(3/4)/(I*a*(x - I))**(5/4), x)

$$3.1208 \quad \int \frac{1}{\sqrt[4]{a-iax} (a+iax)^{5/4}} dx$$

Optimal. Leaf size=78

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{a\sqrt[4]{a-iax} \sqrt[4]{a+iax}} + \frac{2i}{a\sqrt[4]{a-iax} \sqrt[4]{a+iax}}$$

[Out] 2*I/a/(a-I*a*x)^(1/4)/(a+I*a*x)^(1/4)+2*(x^2+1)^(1/4)*(cos(1/2*arctan(x))^2)^(1/2)/cos(1/2*arctan(x))*EllipticE(sin(1/2*arctan(x)),2^(1/2))/a/(a-I*a*x)^(1/4)/(a+I*a*x)^(1/4)

Rubi [A] time = 0.02, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {48, 42, 197, 196}

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{a\sqrt[4]{a-iax} \sqrt[4]{a+iax}} + \frac{2i}{a\sqrt[4]{a-iax} \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(1/4)*(a + I*a*x)^(5/4)), x]

[Out] (2*I)/(a*(a - I*a*x)^(1/4)*(a + I*a*x)^(1/4)) + (2*(1 + x^2)^(1/4)*EllipticE[ArcTan[x]/2, 2])/(a*(a - I*a*x)^(1/4)*(a + I*a*x)^(1/4))

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 48

Int[1/(((a_) + (b_.)*(x_))^(5/4)*((c_) + (d_.)*(x_))^(1/4)), x_Symbol] := Simp[-2/(b*(a + b*x)^(1/4)*(c + d*x)^(1/4)), x] + Dist[c, Int[1/((a + b*x)^(5/4)*(c + d*x)^(5/4)), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && NegQ[a^2*b^2]

Rule 196

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a

, 0] && PosQ[b/a]

Rule 197

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a] && PosQ[b/a]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{\sqrt[4]{a-iax}(a+iax)^{5/4}} dx &= \frac{2i}{a\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + a \int \frac{1}{(a-iax)^{5/4}(a+iax)^{5/4}} dx \\
 &= \frac{2i}{a\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{\left(a\sqrt[4]{a^2+a^2x^2}\right) \int \frac{1}{(a^2+a^2x^2)^{5/4}} dx}{\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\
 &= \frac{2i}{a\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{\sqrt[4]{1+x^2} \int \frac{1}{(1+x^2)^{5/4}} dx}{a\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\
 &= \frac{2i}{a\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{2\sqrt[4]{1+x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{a\sqrt[4]{a-iax}\sqrt[4]{a+iax}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.90

$$\frac{i2^{3/4}\sqrt[4]{1+ix}(a-iax)^{3/4} {}_2F_1\left(\frac{3}{4}, \frac{5}{4}; \frac{7}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{3a^2\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(1/4)*(a + I*a*x)^(5/4)), x]

[Out] ((I/3)*2^(3/4)*(1 + I*x)^(1/4)*(a - I*a*x)^(3/4)*Hypergeometric2F1[3/4, 5/4, 7/4, 1/2 - (I/2)*x])/(a^2*(a + I*a*x)^(1/4))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\frac{(a^3x^2 - ia^3x) \operatorname{integral}\left(-\frac{2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{a^3x^4+a^3x^2}, x\right) + 2i(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{a^3x^2 - ia^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(5/4),x, algorithm="fricas")

[Out] ((a^3*x^2 - I*a^3*x)*integral(-2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^3*x^4 + a^3*x^2), x) + 2*I*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4))/(a^3*x^2 - I*a^3*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{5}{4}} (-i a x + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(5/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(1/4)), x)

maple [C] time = 0.04, size = 94, normalized size = 1.21

$$-\frac{(-ix-1)(ix+1)a^2)^{\frac{1}{4}} x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{(a^2)^{\frac{1}{4}} (-ix-1)a^{\frac{1}{4}} ((ix+1)a)^{\frac{1}{4}} a} + \frac{2x+2i}{(-ix-1)a^{\frac{1}{4}} ((ix+1)a)^{\frac{1}{4}} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(1/4)/(I*a*x+a)^(5/4),x)

[Out] 2*(x+I)/a/(-I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)-1/(a^2)^(1/4)*x*hypergeom([1/4, 1/2], [3/2], -x^2)/a*(-I*x-1)*(I*x+1)*a^2)^(1/4)/(-I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{5}{4}} (-i a x + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(5/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{1/4} (a + a x 1i)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*I)**(1/4)*(a + a*x*I)**(5/4)),x)`

[Out] `int(1/((a - a*x*I)**(1/4)*(a + a*x*I)**(5/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{5}{4}} \sqrt[4]{-ia(x+i)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(1/4)/(a+I*a*x)**(5/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(5/4)*(-I*a*(x + I))**(1/4)), x)`

$$3.1209 \quad \int \frac{1}{(a-iax)^{5/4}(a+iax)^{5/4}} dx$$

Optimal. Leaf size=46

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{a^2 \sqrt[4]{a-iax} \sqrt[4]{a+iax}}$$

[Out] $2*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x)))^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)), 2^{(1/2)})/a^2/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.01, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.120$, Rules used = {42, 197, 196}

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{a^2 \sqrt[4]{a-iax} \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a - I*a*x)^{(5/4)}*(a + I*a*x)^{(5/4)}), x]$

[Out] $(2*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(a^2*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(m_)}), x_Symbol] \rightarrow \text{Dist}[(a + b*x)^{\text{FracPart}[m]}*(c + d*x)^{\text{FracPart}[m]}/(a*c + b*d*x^2)^{\text{FracPart}[m]}, \text{Int}[(a*c + b*d*x^2)^m, x], x] /; \text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{EqQ}[b*c + a*d, 0] \ \&\& \ !\text{IntegerQ}[2*m]$

Rule 196

$\text{Int}[(a_ + (b_)*(x_)^2)^{(-5/4)}, x_Symbol] \rightarrow \text{Simp}[(2*\text{EllipticE}[(1*\text{ArcTan}[\text{Rt}[b/a, 2]*x])/2, 2])/(a^{(5/4)}*\text{Rt}[b/a, 2]), x] /; \text{FreeQ}\{a, b\}, x \ \&\& \ \text{GtQ}[a, 0] \ \&\& \ \text{PosQ}[b/a]$

Rule 197

$\text{Int}[(a_ + (b_)*(x_)^2)^{(-5/4)}, x_Symbol] \rightarrow \text{Dist}[(1 + (b*x^2)/a)^{(1/4)}/(a*(a + b*x^2)^{(1/4)}), \text{Int}[1/(1 + (b*x^2)/a)^{(5/4)}, x], x] /; \text{FreeQ}\{a, b\}, x \ \&\& \ \text{PosQ}[a] \ \&\& \ \text{PosQ}[b/a]$

Rubi steps

$$\int \frac{1}{(a - iax)^{5/4}(a + iax)^{5/4}} dx = \frac{\sqrt[4]{a^2 + a^2x^2} \int \frac{1}{(a^2 + a^2x^2)^{5/4}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}}$$

$$= \frac{\sqrt[4]{1 + x^2} \int \frac{1}{(1+x^2)^{5/4}} dx}{a^2 \sqrt[4]{a - iax} \sqrt[4]{a + iax}}$$

$$= \frac{2 \sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{a^2 \sqrt[4]{a - iax} \sqrt[4]{a + iax}}$$

Mathematica [C] time = 0.02, size = 68, normalized size = 1.48

$$\frac{i2^{3/4} \sqrt[4]{1 + ix} {}_2F_1\left(-\frac{1}{4}, \frac{5}{4}; \frac{3}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{a^2 \sqrt[4]{a - iax} \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(5/4)*(a + I*a*x)^(5/4)),x]

[Out] ((-I)*2^(3/4)*(1 + I*x)^(1/4)*Hypergeometric2F1[-1/4, 5/4, 3/4, 1/2 - (I/2)*x])/(a^2*(a - I*a*x)^(1/4)*(a + I*a*x)^(1/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\frac{2(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}}x + (a^4x^2 + a^4)\text{integral}\left(-\frac{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{a^4x^2+a^4}, x\right)}{a^4x^2 + a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(5/4),x, algorithm="fricas")

[Out] (2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*x + (a^4*x^2 + a^4)*integral(-(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^4*x^2 + a^4), x))/(a^4*x^2 + a^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{5}{4}}(-iax + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(5/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(5/4)), x)

maple [C] time = 0.04, size = 91, normalized size = 1.98

$$-\frac{\left(-ix-1\right)\left(ix+1\right)a^2\left(a^2\right)^{\frac{1}{4}}x\operatorname{hypergeom}\left(\left[\frac{1}{4},\frac{1}{2}\right],\left[\frac{3}{2}\right],-x^2\right)}{\left(a^2\right)^{\frac{1}{4}}\left(-ix-1\right)a^{\frac{1}{4}}\left(ix+1\right)a^{\frac{1}{4}}a^2}+\frac{2x}{\left(-ix-1\right)a^{\frac{1}{4}}\left(ix+1\right)a^{\frac{1}{4}}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(5/4)/(I*a*x+a)^(5/4),x)

[Out] 2*x/a^2/(-I*x-1)*a^(1/4)/((I*x+1)*a^(1/4)-1/(a^2)^(1/4)*x*hypergeom([1/4, 1/2], [3/2], -x^2)/a^2*(-I*x-1)*(I*x+1)*a^2)^(1/4)/(-I*x-1)*a^(1/4)/((I*x+1)*a^(1/4))

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{5}{4}}(-iax+a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(5/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(5/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{1}{(a-ax1i)^{5/4}(a+ax1i)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(5/4)*(a + a*x*1i)^(5/4)),x)

[Out] int(1/((a - a*x*1i)^(5/4)*(a + a*x*1i)^(5/4)), x)

sympy [A] time = 11.91, size = 97, normalized size = 2.11

$$-\frac{iG_{6,6}^{5,3}\left(\begin{array}{c} \frac{5}{8}, \frac{9}{8}, 1 \\ \frac{1}{2}, \frac{5}{4}, \frac{7}{4} \end{array} \middle| \frac{e^{-3i\pi}}{x^2} \right) e^{-\frac{3i\pi}{4}}}{4\pi a^{\frac{5}{2}} \Gamma\left(\frac{5}{4}\right)} + \frac{iG_{6,6}^{2,6}\left(\begin{array}{c} -\frac{1}{2}, 0, \frac{1}{8}, \frac{1}{2}, \frac{5}{8}, 1 \\ \frac{1}{8}, \frac{5}{8} \end{array} \middle| \frac{e^{-i\pi}}{x^2} \right)}{4\pi a^{\frac{5}{2}} \Gamma\left(\frac{5}{4}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a-I*a*x)**(5/4)/(a+I*a*x)**(5/4),x)
```

```
[Out] -I*meijerg(((5/8, 9/8, 1), (1/2, 5/4, 7/4)), ((5/8, 3/4, 9/8, 5/4, 7/4), (0,)), exp_polar(-3*I*pi)/x**2)*exp(-3*I*pi/4)/(4*pi*a**(5/2)*gamma(5/4)) + I*meijerg((-1/2, 0, 1/8, 1/2, 5/8, 1), ()), ((1/8, 5/8), (-1/2, 0, 3/4, 0)), exp_polar(-I*pi)/x**2)/(4*pi*a**(5/2)*gamma(5/4))
```

$$3.1210 \quad \int \frac{1}{(a-iax)^{9/4}(a+iax)^{5/4}} dx$$

Optimal. Leaf size=82

$$\frac{6\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^3 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{2i}{5a^2(a-iax)^{5/4} \sqrt[4]{a+iax}}$$

[Out] $-2/5*I/a^2/(a-I*a*x)^{(5/4)}/(a+I*a*x)^{(1/4)}+6/5*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a^3/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {51, 42, 197, 196}

$$\frac{6\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^3 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{2i}{5a^2(a-iax)^{5/4} \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(9/4)*(a + I*a*x)^(5/4)),x]

[Out] $((-2*I)/5)/(a^2*(a - I*a*x)^{(5/4)}*(a + I*a*x)^{(1/4)}) + (6*(1 + x^2)^{(1/4)}*E[\text{ArcTan}[x]/2, 2])/(5*a^3*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 196

Int[((a_) + (b_)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 197

Int[((a_) + (b_)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a] && PosQ[b/a]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a-iax)^{9/4}(a+iax)^{5/4}} dx &= -\frac{2i}{5a^2(a-iax)^{5/4}\sqrt[4]{a+iax}} + \frac{3 \int \frac{1}{(a-iax)^{5/4}(a+iax)^{5/4}} dx}{5a} \\
 &= -\frac{2i}{5a^2(a-iax)^{5/4}\sqrt[4]{a+iax}} + \frac{\left(3\sqrt[4]{a^2+a^2x^2}\right) \int \frac{1}{(a^2+a^2x^2)^{5/4}} dx}{5a\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\
 &= -\frac{2i}{5a^2(a-iax)^{5/4}\sqrt[4]{a+iax}} + \frac{\left(3\sqrt[4]{1+x^2}\right) \int \frac{1}{(1+x^2)^{5/4}} dx}{5a^3\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\
 &= -\frac{2i}{5a^2(a-iax)^{5/4}\sqrt[4]{a+iax}} + \frac{6\sqrt[4]{1+x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^3\sqrt[4]{a-iax}\sqrt[4]{a+iax}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.85

$$\frac{i2^{3/4}\sqrt[4]{1+ix} {}_2F_1\left(-\frac{5}{4}, \frac{5}{4}; -\frac{1}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{5a^2(a-iax)^{5/4}\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(9/4)*(a + I*a*x)^(5/4)), x]

[Out] ((-1/5*I)*2^(3/4)*(1 + I*x)^(1/4)*Hypergeometric2F1[-5/4, 5/4, -1/4, 1/2 - (I/2)*x])/(a^2*(a - I*a*x)^(5/4)*(a + I*a*x)^(1/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\frac{2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}(3x^2+3ix+1) + (5a^5x^3+5ia^5x^2+5a^5x+5ia^5)\text{integral}\left(-\frac{3(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{5(a^5x^2+a^5)}, x\right)}{5a^5x^3+5ia^5x^2+5a^5x+5ia^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(5/4),x, algorithm="fricas")

[Out] (2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*(3*x^2 + 3*I*x + 1) + (5*a^5*x^3 + 5*I*a^5*x^2 + 5*a^5*x + 5*I*a^5)*integral(-3/5*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^5*x^2 + a^5), x))/(5*a^5*x^3 + 5*I*a^5*x^2 + 5*a^5*x + 5*I*a^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{5}{4}} (-i a x + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(5/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(9/4)), x)

maple [C] time = 0.07, size = 107, normalized size = 1.30

$$\frac{3(-ix-1)(ix+1)a^2)^{\frac{1}{4}} x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{5(a^2)^{\frac{1}{4}}(-ix-1)a^{\frac{1}{4}}((ix+1)a^{\frac{1}{4}}a^3)} + \frac{\frac{6}{5}x^2 + \frac{6}{5}ix + \frac{2}{5}}{(x+i)(-ix-1)a^{\frac{1}{4}}((ix+1)a^{\frac{1}{4}}a^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(9/4)/(I*a*x+a)^(5/4),x)

[Out] 2/5*(3*I*x+3*x^2+1)/(x+I)/a^3/(-I*x-1)*a^(1/4)/((I*x+1)*a)^(1/4)-3/5/(a^2)^(1/4)*x*hypergeom([1/4,1/2],[3/2],-x^2)/a^3*(-I*x-1)*(I*x+1)*a^2)^(1/4)/(-I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(5/4),x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{9/4} (a + a x 1i)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(9/4)*(a + a*x*1i)^(5/4)),x)`

[Out] `int(1/((a - a*x*1i)^(9/4)*(a + a*x*1i)^(5/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{5}{4}}(-ia(x+i))^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(9/4)/(a+I*a*x)**(5/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(5/4)*(-I*a*(x + I))**(9/4)), x)`

$$3.1211 \quad \int \frac{1}{(a-iax)^{13/4}(a+iax)^{5/4}} dx$$

Optimal. Leaf size=115

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3a^4 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{2i}{9a^3(a-iax)^{5/4} \sqrt[4]{a+iax}} - \frac{2i}{9a^2(a-iax)^{9/4} \sqrt[4]{a+iax}}$$

[Out] $-2/9*I/a^2/(a-I*a*x)^{(9/4)}/(a+I*a*x)^{(1/4)}-2/9*I/a^3/(a-I*a*x)^{(5/4)}/(a+I*a*x)^{(1/4)}+2/3*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a^4/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.03, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {51, 42, 197, 196}

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{3a^4 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{2i}{9a^3(a-iax)^{5/4} \sqrt[4]{a+iax}} - \frac{2i}{9a^2(a-iax)^{9/4} \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(13/4)*(a + I*a*x)^(5/4)),x]

[Out] $((-2*I)/9)/(a^2*(a - I*a*x)^{(9/4)}*(a + I*a*x)^{(1/4)}) - ((2*I)/9)/(a^3*(a - I*a*x)^{(5/4)}*(a + I*a*x)^{(1/4)}) + (2*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(3*a^4*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 196

```
Int[((a_) + (b_)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 197

```
Int[((a_) + (b_)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(
a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b},
x] && PosQ[a] && PosQ[b/a]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a-iax)^{13/4}(a+iax)^{5/4}} dx &= -\frac{2i}{9a^2(a-iax)^{9/4}\sqrt[4]{a+iax}} + \frac{5 \int \frac{1}{(a-iax)^{9/4}(a+iax)^{5/4}} dx}{9a} \\
&= -\frac{2i}{9a^2(a-iax)^{9/4}\sqrt[4]{a+iax}} - \frac{2i}{9a^3(a-iax)^{5/4}\sqrt[4]{a+iax}} + \frac{\int \frac{1}{(a-iax)^{5/4}(a+iax)^{5/4}} dx}{3a^2} \\
&= -\frac{2i}{9a^2(a-iax)^{9/4}\sqrt[4]{a+iax}} - \frac{2i}{9a^3(a-iax)^{5/4}\sqrt[4]{a+iax}} + \frac{\sqrt[4]{a^2+a^2x^2} \int \frac{1}{(a^2+a^2x^2)^{5/4}} dx}{3a^2\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\
&= -\frac{2i}{9a^2(a-iax)^{9/4}\sqrt[4]{a+iax}} - \frac{2i}{9a^3(a-iax)^{5/4}\sqrt[4]{a+iax}} + \frac{\sqrt[4]{1+x^2} \int \frac{1}{(1+x^2)^{5/4}} dx}{3a^4\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\
&= -\frac{2i}{9a^2(a-iax)^{9/4}\sqrt[4]{a+iax}} - \frac{2i}{9a^3(a-iax)^{5/4}\sqrt[4]{a+iax}} + \frac{2\sqrt[4]{1+x^2} E\left(\frac{1}{2} \tan^{-1}(x)\right)}{3a^4\sqrt[4]{a-iax}\sqrt[4]{a+iax}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.61

$$-\frac{i2^{3/4}\sqrt[4]{1+ix} {}_2F_1\left(-\frac{9}{4}, \frac{5}{4}; -\frac{5}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{9a^2(a-iax)^{9/4}\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

```
[In] Integrate[1/((a - I*a*x)^(13/4)*(a + I*a*x)^(5/4)), x]
```

```
[Out] ((-1/9*I)*2^(3/4)*(1 + I*x)^(1/4)*Hypergeometric2F1[-9/4, 5/4, -5/4, 1/2 -
(I/2)*x])/(a^2*(a - I*a*x)^(9/4)*(a + I*a*x)^(1/4))
```

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\frac{(6x^3 + 12ix^2 - 4x + 4i)(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}} + (9a^6x^4 + 18ia^6x^3 + 18ia^6x - 9a^6)\text{integral}\left(-\frac{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{3(a^6x^2+a^6)}\right)}{9a^6x^4 + 18ia^6x^3 + 18ia^6x - 9a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(5/4), x, algorithm="fricas")

[Out] ((6*x^3 + 12*I*x^2 - 4*x + 4*I)*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4) + (9*a^6*x^4 + 18*I*a^6*x^3 + 18*I*a^6*x - 9*a^6)*integral(-1/3*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^6*x^2 + a^6), x))/(9*a^6*x^4 + 18*I*a^6*x^3 + 18*I*a^6*x - 9*a^6)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{5}{4}}(-iax + a)^{\frac{13}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(5/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(13/4)), x)

maple [C] time = 0.08, size = 113, normalized size = 0.98

$$\frac{(-ix - 1)(ix + 1)a^2)^{\frac{1}{4}} x \text{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{3(a^2)^{\frac{1}{4}}(-ix - 1)a^{\frac{1}{4}}((ix + 1)a)^{\frac{1}{4}}a^4} + \frac{\frac{2}{3}x^3 + \frac{4}{3}ix^2 - \frac{4}{9}x + \frac{4}{9}i}{(x + i)^2(-ix - 1)a^{\frac{1}{4}}((ix + 1)a)^{\frac{1}{4}}a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(13/4)/(I*a*x+a)^(5/4), x)

[Out] 2/9*(6*I*x^2+3*x^3-2*x+2*I)/(x+I)^2/a^4/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)-1/3/(a^2)^(1/4)*x*hypergeom([1/4, 1/2], [3/2], -x^2)/a^4*(-(I*x-1)*(I*x+1)*a^2)^(1/4)/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(5/4),x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{13/4} (a + a x 1i)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(13/4)*(a + a*x*1i)^(5/4)),x)

[Out] int(1/((a - a*x*1i)^(13/4)*(a + a*x*1i)^(5/4)), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(13/4)/(a+I*a*x)**(5/4),x)

[Out] Timed out

$$3.1212 \quad \int \frac{(a-iax)^{5/4}}{(a+iax)^{5/4}} dx$$

Optimal. Leaf size=287

$$\frac{4i(a-iax)^{5/4}}{a\sqrt[4]{a+iax}} + \frac{5i(a+iax)^{3/4}\sqrt[4]{a-iax}}{a} + \frac{5i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} - \frac{5i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} + \frac{5i \tan^{-1}\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}}\right)}{2\sqrt{2}}$$

[Out] 4*I*(a-I*a*x)^(5/4)/a/(a+I*a*x)^(1/4)+5*I*(a-I*a*x)^(1/4)*(a+I*a*x)^(3/4)/a+5/2*I*arctan(1-(a-I*a*x)^(1/4)*2^(1/2)/(a+I*a*x)^(1/4))*2^(1/2)-5/2*I*arctan(1+(a-I*a*x)^(1/4)*2^(1/2)/(a+I*a*x)^(1/4))*2^(1/2)+5/4*I*ln(1-(a-I*a*x)^(1/4)*2^(1/2)/(a+I*a*x)^(1/4)+(a-I*a*x)^(1/2)/(a+I*a*x)^(1/2))*2^(1/2)-5/4*I*ln(1+(a-I*a*x)^(1/4)*2^(1/2)/(a+I*a*x)^(1/4)+(a-I*a*x)^(1/2)/(a+I*a*x)^(1/2))*2^(1/2)

Rubi [A] time = 0.18, antiderivative size = 287, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 10, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.400$, Rules used = {47, 50, 63, 240, 211, 1165, 628, 1162, 617, 204}

$$\frac{4i(a-iax)^{5/4}}{a\sqrt[4]{a+iax}} + \frac{5i(a+iax)^{3/4}\sqrt[4]{a-iax}}{a} + \frac{5i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} - \frac{5i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{2\sqrt{2}} + \frac{5i \tan^{-1}\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}}\right)}{2\sqrt{2}}$$

Antiderivative was successfully verified.

[In] Int[(a - I*a*x)^(5/4)/(a + I*a*x)^(5/4), x]

[Out] ((4*I)*(a - I*a*x)^(5/4))/(a*(a + I*a*x)^(1/4)) + ((5*I)*(a - I*a*x)^(1/4)*(a + I*a*x)^(3/4))/a + ((5*I)*ArcTan[1 - (Sqrt[2]*(a - I*a*x)^(1/4))/(a + I*a*x)^(1/4)]/Sqrt[2] - ((5*I)*ArcTan[1 + (Sqrt[2]*(a - I*a*x)^(1/4))/(a + I*a*x)^(1/4)]/Sqrt[2] + (((5*I)/2)*Log[1 + Sqrt[a - I*a*x]/Sqrt[a + I*a*x] - (Sqrt[2]*(a - I*a*x)^(1/4))/(a + I*a*x)^(1/4)]/Sqrt[2] - (((5*I)/2)*Log[1 + Sqrt[a - I*a*x]/Sqrt[a + I*a*x] + (Sqrt[2]*(a - I*a*x)^(1/4))/(a + I*a*x)^(1/4)]/Sqrt[2])

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(LeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 211

```
Int[((a_) + (b_.)*(x_)^4)^(-1), x_Symbol] := With[{r = Numerator[Rt[a/b, 2]
], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*r), Int[(r - s*x^2)/(a + b*x^4),
x], x] + Dist[1/(2*r), Int[(r + s*x^2)/(a + b*x^4), x], x] /; FreeQ[{a, b
}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] &&
AtomQ[SplitProduct[SumBaseQ, b]]))
```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int
[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a,
b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/
n]
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 1162

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x] + Dist[e
/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] &
& EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]
```

Rule 1165

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x],
x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x]] /; Fre
eQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a - iax)^{5/4}}{(a + iax)^{5/4}} dx &= \frac{4i(a - iax)^{5/4}}{a\sqrt[4]{a + iax}} - 5 \int \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} dx \\
&= \frac{4i(a - iax)^{5/4}}{a\sqrt[4]{a + iax}} + \frac{5i\sqrt[4]{a - iax} (a + iax)^{3/4}}{a} - \frac{1}{2}(5a) \int \frac{1}{(a - iax)^{3/4}\sqrt[4]{a + iax}} dx \\
&= \frac{4i(a - iax)^{5/4}}{a\sqrt[4]{a + iax}} + \frac{5i\sqrt[4]{a - iax} (a + iax)^{3/4}}{a} - 10i \operatorname{Subst} \left(\int \frac{1}{\sqrt[4]{2a - x^4}} dx, x, \sqrt[4]{a - iax} \right) \\
&= \frac{4i(a - iax)^{5/4}}{a\sqrt[4]{a + iax}} + \frac{5i\sqrt[4]{a - iax} (a + iax)^{3/4}}{a} - 10i \operatorname{Subst} \left(\int \frac{1}{1 + x^4} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) \\
&= \frac{4i(a - iax)^{5/4}}{a\sqrt[4]{a + iax}} + \frac{5i\sqrt[4]{a - iax} (a + iax)^{3/4}}{a} - 5i \operatorname{Subst} \left(\int \frac{1 - x^2}{1 + x^4} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) - 5i \operatorname{Subst} \left(\int \frac{1}{1 - \sqrt{2}x + x^2} dx, x, \frac{\sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right) - \frac{5}{2} \\
&= \frac{4i(a - iax)^{5/4}}{a\sqrt[4]{a + iax}} + \frac{5i\sqrt[4]{a - iax} (a + iax)^{3/4}}{a} + \frac{5i \log \left(1 + \frac{\sqrt{a - iax}}{\sqrt{a + iax}} - \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{2\sqrt{2}} - \frac{5i \log \left(1 + \frac{\sqrt{a - iax}}{\sqrt{a + iax}} \right)}{2} \\
&= \frac{4i(a - iax)^{5/4}}{a\sqrt[4]{a + iax}} + \frac{5i\sqrt[4]{a - iax} (a + iax)^{3/4}}{a} + \frac{5i \tan^{-1} \left(1 - \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{\sqrt{2}} - \frac{5i \tan^{-1} \left(1 + \frac{\sqrt{2} \sqrt[4]{a - iax}}{\sqrt[4]{a + iax}} \right)}{\sqrt{2}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.24

$$\frac{i2^{3/4}\sqrt[4]{1 + ix}(a - iax)^{9/4} {}_2F_1\left(\frac{5}{4}, \frac{9}{4}; \frac{13}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{9a^2\sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(5/4)/(a + I*a*x)^(5/4), x]

[Out] ((I/9)*2^(3/4)*(1 + I*x)^(1/4)*(a - I*a*x)^(9/4)*Hypergeometric2F1[5/4, 9/4, 13/4, 1/2 - (I/2)*x])/(a^2*(a + I*a*x)^(1/4))

fricas [A] time = 0.47, size = 239, normalized size = 0.83

$$\sqrt{25i}(ax - ia) \log \left(\frac{\sqrt{25i}(ax - ia) + 5(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{1}{4}}}{5x - 5i} \right) - \sqrt{25i}(ax - ia) \log \left(-\frac{\sqrt{25i}(ax - ia) - 5(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{1}{4}}}{5x - 5i} \right) + \sqrt{-2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(5/4),x, algorithm="fricas")

[Out]
$$-1/2*(\sqrt{25*I}*(a*x - I*a)*\log((\sqrt{25*I}*(a*x - I*a) + 5*(I*a*x + a)^{(3/4)}*(-I*a*x + a)^{(1/4)})/(5*x - 5*I)) - \sqrt{25*I}*(a*x - I*a)*\log(-(\sqrt{25*I}*(a*x - I*a) - 5*(I*a*x + a)^{(3/4)}*(-I*a*x + a)^{(1/4)})/(5*x - 5*I)) + \sqrt{-25*I}*(a*x - I*a)*\log((\sqrt{-25*I}*(a*x - I*a) + 5*(I*a*x + a)^{(3/4)}*(-I*a*x + a)^{(1/4)})/(5*x - 5*I)) - \sqrt{-25*I}*(a*x - I*a)*\log(-(\sqrt{-25*I}*(a*x - I*a) - 5*(I*a*x + a)^{(3/4)}*(-I*a*x + a)^{(1/4)})/(5*x - 5*I)) + 2*(I*a*x + a)^{(3/4)}*(-I*a*x + a)^{(1/4)}*(-I*x - 9))/(a*x - I*a)$$

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(5/4),x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command:
INPUT:sage2OUTPUT:ext_reduce Error: Bad Argument Typeintegrate(i/4*a/a^2*(1
6*((i*a*x+a)^(1/4))^4*(-((i*a*x+a)^(1/4))^4+2*a)^(1/4)-32*a*(-((i*a*x+a)^(1
/4))^4+2*a)^(1/4))/((i*a*x+a)^(1/4))^2/4*i*a*((i*a*x+a)^(1/4))^-3,x)

maple [C] time = 2.04, size = 481, normalized size = 1.68

$$\frac{i(x^2 - 8ix + 9)(-ix - 1)a^{\frac{1}{4}}}{(ix - 1)((ix + 1)a)^{\frac{1}{4}}} \left(\frac{5i \operatorname{RootOf}(_Z^2 - i) \ln \left(\frac{-x^3 + i(-x^4 - 2ix^3 - 2ix + 1)^{\frac{1}{4}} x^2 \operatorname{RootOf}(_Z^2 - i) - 2ix^2 - 2(-x^4 - 2ix^3 - 2ix + 1)^{\frac{1}{4}} x \operatorname{RootOf}(_Z^2 - i) + i\sqrt{-1}}{\dots} \right)}{\dots} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(5/4)/(I*a*x+a)^(5/4),x)

[Out]
$$-I*(x^2+9-8*I*x)*(-I*x-1)*a^{(1/4)}/(I*x-1)/((I*x+1)*a)^{(1/4)} - (-5/2*\operatorname{RootOf}(_Z^2-I)*\ln(-(\operatorname{RootOf}(_Z^2-I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)}*x^2+I*\operatorname{RootOf}(_Z^2-I)*(-x^4-2*I*x^3-2*I*x+1)^{(3/4)}+x^3+2*I*\operatorname{RootOf}(_Z^2-I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)}*x+I*(-x^4-2*I*x^3-2*I*x+1)^{(1/2)}*x+2*I*x^2-\operatorname{RootOf}(_Z^2-I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)} - (-x^4-2*I*x^3-2*I*x+1)^{(1/2)}-x)/(I*x-1)^2)+5/2*I*\operatorname{RootOf}(_Z^2-I)*\ln((I*\operatorname{RootOf}(_Z^2-I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)}*x^2-2*\operatorname{RootOf}(_Z^2-I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)}*x-x^3+\operatorname{RootOf}(_Z^2-I)*(-x^4-2*I*x^3-2*I*x$$

$+1)^{3/4} + I \cdot (-x^4 - 2Ix^3 - 2Ix + 1)^{1/2} \cdot x - I \cdot \text{RootOf}(_Z^2 - I) \cdot (-x^4 - 2Ix^3 - 2Ix + 1)^{1/4} - 2Ix^2 - (-x^4 - 2Ix^3 - 2Ix + 1)^{1/2} + x) / (Ix - 1)^2) \cdot (-Ix - 1) \cdot a^{1/4} / (Ix - 1) \cdot (-Ix - 1)^3 \cdot (Ix + 1)^{1/4} / ((Ix + 1) \cdot a)^{1/4}$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{5/4}}{(iax + a)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(5/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(5/4)/(I*a*x + a)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a - ax1i)^{5/4}}{(a + ax1i)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - a*x*1i)^(5/4)/(a + a*x*1i)^(5/4),x)

[Out] int((a - a*x*1i)^(5/4)/(a + a*x*1i)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-ia(x + i))^{5/4}}{(ia(x - i))^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)**(5/4)/(a+I*a*x)**(5/4),x)

[Out] Integral((-I*a*(x + I))**(5/4)/(I*a*(x - I))**(5/4), x)

$$3.1213 \quad \int \frac{\sqrt[4]{a-iax}}{(a+iax)^{5/4}} dx$$

Optimal. Leaf size=264

$$\frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} + \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} - \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} + \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} - \frac{i\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a}$$

[Out] $4*I*(a-I*a*x)^{(1/4)}/a/(a+I*a*x)^{(1/4)}+1/2*I*\ln(1-(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2))}/a*2^{(1/2)}-1/2*I*\ln(1+(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2))}/a*2^{(1/2)}+I*\arctan(1-(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)})*2^{(1/2)}/a-I*\arctan(1+(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)})*2^{(1/2)}/a$

Rubi [A] time = 0.14, antiderivative size = 264, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 9, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.360$, Rules used = {47, 63, 240, 211, 1165, 628, 1162, 617, 204}

$$\frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} + \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} - \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} + \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} - \frac{i\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a - I*a*x)^{(1/4)}/(a + I*a*x)^{(5/4)}, x]$

[Out] $((4*I)*(a - I*a*x)^{(1/4)})/(a*(a + I*a*x)^{(1/4)}) + (I*\text{Sqrt}[2]*\text{ArcTan}[1 - (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/a - (I*\text{Sqrt}[2]*\text{ArcTan}[1 + (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/a + (I*\text{Log}[1 + \text{Sqrt}[a - I*a*x]/\text{Sqrt}[a + I*a*x] - (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2]*a) - (I*\text{Log}[1 + \text{Sqrt}[a - I*a*x]/\text{Sqrt}[a + I*a*x] + (\text{Sqrt}[2]*(a - I*a*x)^{(1/4)})/(a + I*a*x)^{(1/4)}])/(\text{Sqrt}[2]*a)$

Rule 47

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \text{Dist}[(d*n)/(b*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\text{FreeQ}\{a, b, c, d, x\} \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{LtQ}[m, -1] \ \&\& \ !(\text{IntegerQ}[n] \ \&\& \ !\text{IntegerQ}[m]) \ \&\& \ !(\text{IntegerQ}[m + n + 2, 0] \ \&\& \ (\text{FractionQ}[m] \ || \ \text{GeQ}[2*n + m + 1, 0])) \ \&\& \ \& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 211

```
Int[((a_) + (b_.)*(x_)^4)^(-1), x_Symbol] := With[{r = Numerator[Rt[a/b, 2]
], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*r), Int[(r - s*x^2)/(a + b*x^4),
x], x] + Dist[1/(2*r), Int[(r + s*x^2)/(a + b*x^4), x], x] /; FreeQ[{a, b
}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] &&
AtomQ[SplitProduct[SumBaseQ, b]]))
```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int
[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a,
b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/
n]
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 1162

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x], x] + Dist[e
/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] &
```

& EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]

Rule 1165

Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x], x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt[4]{a-iax}}{(a+iax)^{5/4}} dx &= \frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} - \int \frac{1}{(a-iax)^{3/4}\sqrt[4]{a+iax}} dx \\
 &= \frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} - \frac{(4i) \operatorname{Subst}\left(\int \frac{1}{\sqrt[4]{2a-x^4}} dx, x, \sqrt[4]{a-iax}\right)}{a} \\
 &= \frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} - \frac{(4i) \operatorname{Subst}\left(\int \frac{1}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} \\
 &= \frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} - \frac{(2i) \operatorname{Subst}\left(\int \frac{1-x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} - \frac{(2i) \operatorname{Subst}\left(\int \frac{1+x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} \\
 &= \frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} - \frac{i \operatorname{Subst}\left(\int \frac{1}{1-\sqrt{2}x+x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} - \frac{i \operatorname{Subst}\left(\int \frac{1}{1+\sqrt{2}x+x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \dots \\
 &= \frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} + \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}a} - \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}a} - \frac{(i\sqrt{2}) \operatorname{Subst}\left(\int \frac{1}{1-x^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}a} \\
 &= \frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} + \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} - \frac{i\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}}\right)}{\sqrt{2}a} - \dots
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.27

$$\frac{i2^{3/4}\sqrt[4]{1+ix}(a-iax)^{5/4}{}_2F_1\left(\frac{5}{4}, \frac{5}{4}; \frac{9}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{5a^2\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(1/4)/(a + I*a*x)^(5/4), x]

[Out] ((I/5)*2^(3/4)*(1 + I*x)^(1/4)*(a - I*a*x)^(5/4)*Hypergeometric2F1[5/4, 5/4, 9/4, 1/2 - (I/2)*x])/(a^2*(a + I*a*x)^(1/4))

fricas [A] time = 0.49, size = 302, normalized size = 1.14

$$(a^2x - ia^2)\sqrt{\frac{4i}{a^2}} \log\left(\frac{(a^2x - ia^2)\sqrt{\frac{4i}{a^2}} + 2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{1}{4}}}{2x-2i}\right) - (a^2x - ia^2)\sqrt{\frac{4i}{a^2}} \log\left(\frac{(a^2x - ia^2)\sqrt{\frac{4i}{a^2}} - 2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{1}{4}}}{2x-2i}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(5/4), x, algorithm="fricas")

[Out] -1/2*((a^2*x - I*a^2)*sqrt(4*I/a^2)*log(((a^2*x - I*a^2)*sqrt(4*I/a^2) + 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4))/(2*x - 2*I)) - (a^2*x - I*a^2)*sqrt(4*I/a^2)*log(-((a^2*x - I*a^2)*sqrt(4*I/a^2) - 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4))/(2*x - 2*I)) + (a^2*x - I*a^2)*sqrt(-4*I/a^2)*log(((a^2*x - I*a^2)*sqrt(-4*I/a^2) + 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4))/(2*x - 2*I)) - (a^2*x - I*a^2)*sqrt(-4*I/a^2)*log(-((a^2*x - I*a^2)*sqrt(-4*I/a^2) - 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4))/(2*x - 2*I)) - 8*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)/(a^2*x - I*a^2)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(5/4), x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x);;OUTPUT:

maple [C] time = 2.01, size = 476, normalized size = 1.80

$$\frac{4(x+i)(-ix-1)a^{\frac{1}{4}}}{(ix-1)((ix+1)a)^{\frac{1}{4}}a} + \frac{\left(\text{RootOf}(_Z^2+i)\ln\left(\frac{-x^3 - (-x^4 - 2ix^3 - 2ix+1)^{\frac{1}{4}}x^2\text{RootOf}(_Z^2+i) - 2ix^2 - 2i(-x^4 - 2ix^3 - 2ix+1)^{\frac{1}{4}}x\text{RootOf}(_Z^2+i)}{\dots}\right)\right)}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(1/4)/(I*a*x+a)^(5/4), x)

[Out]
$$-4*(x+I)/a*(-(I*x-1)*a)^{(1/4)}/(I*x-1)/((I*x+1)*a)^{(1/4)}+(RootOf(_Z^2+I)*ln((-RootOf(_Z^2+I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)}*x^2+I*RootOf(_Z^2+I)*(-x^4-2*I*x^3-2*I*x+1)^{(3/4)}-x^3-2*I*RootOf(_Z^2+I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)}*x+I*(-x^4-2*I*x^3-2*I*x+1)^{(1/2)}*x-2*I*x^2+RootOf(_Z^2+I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)}-(-x^4-2*I*x^3-2*I*x+1)^{(1/2)}+x)/(I*x-1)^2+I*RootOf(_Z^2+I)*ln((-I*RootOf(_Z^2+I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)}*x^2+2*RootOf(_Z^2+I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)}*x-x^3+RootOf(_Z^2+I)*(-x^4-2*I*x^3-2*I*x+1)^{(3/4)}-I*(-x^4-2*I*x^3-2*I*x+1)^{(1/2)}*x+I*RootOf(_Z^2+I)*(-x^4-2*I*x^3-2*I*x+1)^{(1/4)}-2*I*x^2+(-x^4-2*I*x^3-2*I*x+1)^{(1/2)}+x)/(I*x-1)^2))/a*(-(I*x-1)*a)^{(1/4)}/(I*x-1)*(-I*x-1)^3*(I*x+1)^{(1/4)}/((I*x+1)*a)^{(1/4)}$$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i ax + a)^{\frac{1}{4}}}{(i ax + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(5/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(1/4)/(I*a*x + a)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a - a x 1i)^{1/4}}{(a + a x 1i)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - a*x*1i)^(1/4)/(a + a*x*1i)^(5/4),x)

[Out] int((a - a*x*1i)^(1/4)/(a + a*x*1i)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[4]{-ia(x+i)}}{(ia(x-i))^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)**(1/4)/(a+I*a*x)**(5/4),x)

[Out] Integral((-I*a*(x + I))**(1/4)/(I*a*(x - I))**(5/4), x)

$$3.1214 \quad \int \frac{1}{(a-iax)^{3/4}(a+iax)^{5/4}} dx$$

Optimal. Leaf size=31

$$\frac{2i\sqrt[4]{a-iax}}{a^2\sqrt[4]{a+iax}}$$

[Out] $2*I*(a-I*a*x)^{(1/4)}/a^2/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.00, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.040$, Rules used = {37}

$$\frac{2i\sqrt[4]{a-iax}}{a^2\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(3/4)*(a + I*a*x)^(5/4)), x]

[Out] ((2*I)*(a - I*a*x)^(1/4))/(a^2*(a + I*a*x)^(1/4))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a-iax)^{3/4}(a+iax)^{5/4}} dx = \frac{2i\sqrt[4]{a-iax}}{a^2\sqrt[4]{a+iax}}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 1.00

$$\frac{2i\sqrt[4]{a-iax}}{a^2\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(3/4)*(a + I*a*x)^(5/4)), x]

[Out] ((2*I)*(a - I*a*x)^(1/4))/(a^2*(a + I*a*x)^(1/4))

fricas [A] time = 0.44, size = 31, normalized size = 1.00

$$\frac{2(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{1}{4}}}{a^3x - ia^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(5/4),x, algorithm="fricas")

[Out] 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)/(a^3*x - I*a^3)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{5}{4}}(-iax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(5/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(3/4)), x)

maple [A] time = 0.04, size = 31, normalized size = 1.00

$$\frac{2x + 2i}{(-ix - 1)a^{\frac{3}{4}}((ix + 1)a)^{\frac{1}{4}}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(3/4)/(I*a*x+a)^(5/4),x)

[Out] 2/a/(-(I*x-1)*a)^(3/4)/((I*x+1)*a)^(1/4)*(x+I)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{5}{4}}(-iax + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(5/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(3/4)), x)

mupad [B] time = 1.16, size = 27, normalized size = 0.87

$$\frac{(-a(-1 + x1i))^{1/4} 2i}{a^2(a(1 + x1i))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(3/4)*(a + a*x*1i)^(5/4)),x)`

[Out] `((-a*(x*1i - 1))^(1/4)*2i)/(a^2*(a*(x*1i + 1))^(1/4))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{5}{4}}(-ia(x+i))^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(3/4)/(a+I*a*x)**(5/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(5/4)*(-I*a*(x + I))**(3/4)), x)`

$$3.1215 \quad \int \frac{1}{(a-iax)^{7/4}(a+iax)^{5/4}} dx$$

Optimal. Leaf size=67

$$\frac{4i\sqrt[4]{a-iax}}{3a^3\sqrt[4]{a+iax}} - \frac{2i}{3a^2(a-iax)^{3/4}\sqrt[4]{a+iax}}$$

[Out] $-2/3*I/a^2/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(1/4)}+4/3*I*(a-I*a*x)^{(1/4)}/a^3/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.01, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$\frac{4i\sqrt[4]{a-iax}}{3a^3\sqrt[4]{a+iax}} - \frac{2i}{3a^2(a-iax)^{3/4}\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(7/4)*(a + I*a*x)^(5/4)),x]

[Out] $((-2*I)/3)/(a^2*(a - I*a*x)^{(3/4)*(a + I*a*x)^{(1/4)}) + (((4*I)/3)*(a - I*a*x)^{(1/4)})/(a^3*(a + I*a*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a-iax)^{7/4}(a+iax)^{5/4}} dx = -\frac{2i}{3a^2(a-iax)^{3/4}\sqrt[4]{a+iax}} + \frac{2 \int \frac{1}{(a-iax)^{3/4}(a+iax)^{5/4}} dx}{3a}$$

$$= -\frac{2i}{3a^2(a-iax)^{3/4}\sqrt[4]{a+iax}} + \frac{4i\sqrt[4]{a-iax}}{3a^3\sqrt[4]{a+iax}}$$

Mathematica [A] time = 0.02, size = 38, normalized size = 0.57

$$\frac{4x + 2i}{3a^2(a-iax)^{3/4}\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(7/4)*(a + I*a*x)^(5/4)), x]

[Out] (2*I + 4*x)/(3*a^2*(a - I*a*x)^(3/4)*(a + I*a*x)^(1/4))

fricas [A] time = 0.44, size = 36, normalized size = 0.54

$$\frac{(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{1}{4}}(4x + 2i)}{3(a^4x^2 + a^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(5/4), x, algorithm="fricas")

[Out] 1/3*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)*(4*x + 2*I)/(a^4*x^2 + a^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{5}{4}}(-iax + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(5/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(7/4)), x)

maple [A] time = 0.05, size = 33, normalized size = 0.49

$$\frac{\frac{4x}{3} + \frac{2i}{3}}{(-(ix - 1)a)^{\frac{3}{4}}((ix + 1)a)^{\frac{1}{4}}a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(7/4)/(I*a*x+a)^(5/4),x)`

[Out] `2/3/a^2/(-(I*x-1)*a)^(3/4)/((I*x+1)*a)^(1/4)*(2*x+I)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{5}{4}}(-iax+a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(5/4),x, algorithm="maxima")`

[Out] `integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(7/4)), x)`

mupad [B] time = 0.60, size = 40, normalized size = 0.60

$$-\frac{2(2x+1i)(-a(-1+x1i))^{1/4}}{3a^3(-1+x1i)(a(1+x1i))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(7/4)*(a + a*x*1i)^(5/4)),x)`

[Out] `-(2*(2*x + 1i)*(-a*(x*1i - 1))^(1/4))/(3*a^3*(x*1i - 1)*(a*(x*1i + 1))^(1/4))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{5}{4}}(-ia(x+i))^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(7/4)/(a+I*a*x)**(5/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(5/4)*(-I*a*(x + I))**(7/4)), x)`

$$3.1216 \quad \int \frac{1}{(a-iax)^{11/4}(a+iax)^{5/4}} dx$$

Optimal. Leaf size=100

$$\frac{16i\sqrt[4]{a-iax}}{21a^4\sqrt[4]{a+iax}} - \frac{8i}{21a^3\sqrt[4]{a+iax}(a-iax)^{3/4}} - \frac{2i}{7a^2\sqrt[4]{a+iax}(a-iax)^{7/4}}$$

[Out] $-2/7*I/a^2/(a-I*a*x)^{(7/4)}/(a+I*a*x)^{(1/4)}-8/21*I/a^3/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(1/4)}+16/21*I*(a-I*a*x)^{(1/4)}/a^4/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$\frac{16i\sqrt[4]{a-iax}}{21a^4\sqrt[4]{a+iax}} - \frac{8i}{21a^3\sqrt[4]{a+iax}(a-iax)^{3/4}} - \frac{2i}{7a^2\sqrt[4]{a+iax}(a-iax)^{7/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(11/4)*(a + I*a*x)^(5/4)), x]

[Out] $((-2*I)/7)/(a^2*(a - I*a*x)^{(7/4)}*(a + I*a*x)^{(1/4)}) - ((8*I)/21)/(a^3*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(1/4)}) + (((16*I)/21)*(a - I*a*x)^{(1/4)})/(a^4*(a + I*a*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a-iax)^{11/4}(a+iax)^{5/4}} dx &= -\frac{2i}{7a^2(a-iax)^{7/4}\sqrt[4]{a+iax}} + \frac{4 \int \frac{1}{(a-iax)^{7/4}(a+iax)^{5/4}} dx}{7a} \\
&= -\frac{2i}{7a^2(a-iax)^{7/4}\sqrt[4]{a+iax}} - \frac{8i}{21a^3(a-iax)^{3/4}\sqrt[4]{a+iax}} + \frac{8 \int \frac{1}{(a-iax)^{3/4}(a+iax)^{5/4}} dx}{21a^2} \\
&= -\frac{2i}{7a^2(a-iax)^{7/4}\sqrt[4]{a+iax}} - \frac{8i}{21a^3(a-iax)^{3/4}\sqrt[4]{a+iax}} + \frac{16i\sqrt[4]{a-iax}}{21a^4\sqrt[4]{a+iax}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 50, normalized size = 0.50

$$\frac{16x^2 + 24ix - 2}{21a^3(x+i)(a-iax)^{3/4}\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(11/4)*(a + I*a*x)^(5/4)), x]

[Out] (-2 + (24*I)*x + 16*x^2)/(21*a^3*(I + x)*(a - I*a*x)^(3/4)*(a + I*a*x)^(1/4))

fricas [A] time = 0.44, size = 58, normalized size = 0.58

$$\frac{2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{1}{4}}(8x^2+12ix-1)}{21a^5x^3+21ia^5x^2+21a^5x+21ia^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(5/4), x, algorithm="fricas")

[Out] 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)*(8*x^2 + 12*I*x - 1)/(21*a^5*x^3 + 21*I*a^5*x^2 + 21*a^5*x + 21*I*a^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{5}{4}}(-iax+a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(5/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(5/4)*(-I*a*x + a)^(11/4)), x)

maple [A] time = 0.06, size = 44, normalized size = 0.44

$$\frac{\frac{16}{21}x^2 + \frac{8}{7}ix - \frac{2}{21}}{(-ix - 1)a^{\frac{3}{4}}((ix + 1)a)^{\frac{1}{4}}(x + i)a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(11/4)/(I*a*x+a)^(5/4), x)

[Out] 2/21/a^3/(-(I*x-1)*a)^(3/4)/((I*x+1)*a)^(1/4)*(8*x^2+12*I*x-1)/(x+I)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(5/4), x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.

mupad [B] time = 0.76, size = 46, normalized size = 0.46

$$\frac{(-a(-1 + x1i))^{1/4} (8x^2 + x12i - 1) 2i}{21 a^4 (-1 + x1i)^2 (a(1 + x1i))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(11/4)*(a + a*x*1i)^(5/4)), x)

[Out] -((-a*(x*1i - 1))^(1/4)*(x*12i + 8*x^2 - 1)*2i)/(21*a^4*(x*1i - 1)^2*(a*(x*1i + 1))^(1/4))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{5}{4}}(-ia(x+i))^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(11/4)/(a+I*a*x)**(5/4), x)

[Out] Integral(1/((I*a*(x - I))**(5/4)*(-I*a*(x + I))**(11/4)), x)

$$3.1217 \quad \int \frac{(a-iax)^{7/4}}{(a+iax)^{9/4}} dx$$

Optimal. Leaf size=141

$$-\frac{42\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5\sqrt[4]{a+iax} \sqrt[4]{a-iax}} + \frac{4i(a-iax)^{7/4}}{5a(a+iax)^{5/4}} - \frac{28i(a-iax)^{3/4}}{5a\sqrt[4]{a+iax}} + \frac{42x}{5\sqrt[4]{a+iax} \sqrt[4]{a-iax}}$$

[Out] $4/5*I*(a-I*a*x)^{(7/4)}/a/(a+I*a*x)^{(5/4)}+42/5*x/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}-28/5*I*(a-I*a*x)^{(3/4)}/a/(a+I*a*x)^{(1/4)}-42/5*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.03, antiderivative size = 141, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 42, 229, 227, 196}

$$-\frac{42\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5\sqrt[4]{a+iax} \sqrt[4]{a-iax}} + \frac{4i(a-iax)^{7/4}}{5a(a+iax)^{5/4}} - \frac{28i(a-iax)^{3/4}}{5a\sqrt[4]{a+iax}} + \frac{42x}{5\sqrt[4]{a+iax} \sqrt[4]{a-iax}}$$

Antiderivative was successfully verified.

[In] Int[(a - I*a*x)^(7/4)/(a + I*a*x)^(9/4), x]

[Out] $((4*I)/5)*(a - I*a*x)^{(7/4)}/(a*(a + I*a*x)^{(5/4)} + (42*x)/(5*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)}) - ((28*I)/5)*(a - I*a*x)^{(3/4)}/(a*(a + I*a*x)^{(1/4)}) - (42*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(5*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 196

Int[((a_) + (b_)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 227

Int[((a_) + (b_)*(x_)^2)^(-1/4), x_Symbol] := Simp[(2*x)/(a + b*x^2)^(1/4), x] - Dist[a, Int[1/(a + b*x^2)^(5/4), x], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 229

Int[((a_) + (b_)*(x_)^2)^(-1/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a + b*x^2)^(1/4), Int[1/(1 + (b*x^2)/a)^(1/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a]

Rubi steps

$$\begin{aligned}
 \int \frac{(a - iax)^{7/4}}{(a + iax)^{9/4}} dx &= \frac{4i(a - iax)^{7/4}}{5a(a + iax)^{5/4}} - \frac{7}{5} \int \frac{(a - iax)^{3/4}}{(a + iax)^{5/4}} dx \\
 &= \frac{4i(a - iax)^{7/4}}{5a(a + iax)^{5/4}} - \frac{28i(a - iax)^{3/4}}{5a\sqrt[4]{a + iax}} + \frac{21}{5} \int \frac{1}{\sqrt[4]{a - iax}\sqrt[4]{a + iax}} dx \\
 &= \frac{4i(a - iax)^{7/4}}{5a(a + iax)^{5/4}} - \frac{28i(a - iax)^{3/4}}{5a\sqrt[4]{a + iax}} + \frac{\left(21\sqrt[4]{a^2 + a^2x^2}\right) \int \frac{1}{\sqrt[4]{a^2 + a^2x^2}} dx}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}} \\
 &= \frac{4i(a - iax)^{7/4}}{5a(a + iax)^{5/4}} - \frac{28i(a - iax)^{3/4}}{5a\sqrt[4]{a + iax}} + \frac{\left(21\sqrt[4]{1 + x^2}\right) \int \frac{1}{\sqrt[4]{1 + x^2}} dx}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}} \\
 &= \frac{4i(a - iax)^{7/4}}{5a(a + iax)^{5/4}} + \frac{42x}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}} - \frac{28i(a - iax)^{3/4}}{5a\sqrt[4]{a + iax}} - \frac{\left(21\sqrt[4]{1 + x^2}\right) \int \frac{1}{(1+x^2)^{5/4}} dx}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}} \\
 &= \frac{4i(a - iax)^{7/4}}{5a(a + iax)^{5/4}} + \frac{42x}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}} - \frac{28i(a - iax)^{3/4}}{5a\sqrt[4]{a + iax}} - \frac{42\sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.50

$$\frac{i\sqrt[4]{1 + ix}(a - iax)^{11/4} {}_2F_1\left(\frac{9}{4}, \frac{11}{4}; \frac{15}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{11\sqrt[4]{2} a^3 \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(7/4)/(a + I*a*x)^(9/4), x]

[Out] ((I/11)*(1 + I*x)^(1/4)*(a - I*a*x)^(11/4)*Hypergeometric2F1[9/4, 11/4, 15/4, 1/2 - (I/2)*x])/(2^(1/4)*a^3*(a + I*a*x)^(1/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\frac{2(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}}(5x^2 - 30ix - 21) + (5a^2x^3 - 10ia^2x^2 - 5a^2x)\operatorname{integral}\left(\frac{42(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{5(a^2x^4+a^2x^2)}, x\right)}{5a^2x^3 - 10ia^2x^2 - 5a^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(9/4), x, algorithm="fricas")

[Out] (2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*(5*x^2 - 30*I*x - 21) + (5*a^2*x^3 - 10*I*a^2*x^2 - 5*a^2*x)*integral(42/5*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^2*x^4 + a^2*x^2), x))/(5*a^2*x^3 - 10*I*a^2*x^2 - 5*a^2*x)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(9/4), x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command: INPUT:sage2OUTPUT:Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}+%%{1,[0,4]%%}] at parameters values [-49,-86]Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}+%%{1,[0,4]%%}] at parameters values [-64,-30]Warning, choosing root of [1,0,0,0,%%{-2,[1,0]%%}+%%{1,[0,4]%%}] at parameters values [70,22]ext_reduce Error: Bad Argument TypeEvaluation time: 0.57integrate(i/4*a/a^2*(16*((i*a*x+a)^(1/4))^4*((-(i*a*x+a)^(1/4))^4+2*a)^(1/4))^3-32*a*((-(i*a*x+a)^(1/4))^4+2*a)^(1/4))^3)/((i*a*x+a)^(1/4))^6/4*i*a*((i*a*x+a)^(1/4))^3,x)

maple [C] time = 0.06, size = 101, normalized size = 0.72

$$\frac{21(-ix-1)(ix+1)a^2)^{\frac{1}{4}}x\operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{5(a^2)^{\frac{1}{4}}(-ix-1)a^{\frac{1}{4}}((ix+1)a)^{\frac{1}{4}}}} \frac{8(4x^2+ix+3)}{5(x-i)(-ix-1)a^{\frac{1}{4}}((ix+1)a)^{\frac{1}{4}}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-I*a*x+a)^(7/4)/(I*a*x+a)^(9/4),x)`

[Out] $-8/5*(4*x^2+3+I*x)/(x-I)/(-I*x-1)*a^{1/4}/((I*x+1)*a)^{1/4}+21/5/(a^2)^{1/4}*x*\text{hypergeom}([1/4,1/2],[3/2],-x^2)*(-I*x-1)*(I*x+1)*a^2)^{1/4}/(-I*x-1)*a^{1/4}/((I*x+1)*a)^{1/4}$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i a x + a)^{\frac{7}{4}}}{(i a x + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)^(7/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")`

[Out] `integrate((-I*a*x + a)^(7/4)/(I*a*x + a)^(9/4), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - a x 1i)^{7/4}}{(a + a x 1i)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - a*x*1i)^(7/4)/(a + a*x*1i)^(9/4),x)`

[Out] `int((a - a*x*1i)^(7/4)/(a + a*x*1i)^(9/4), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i a (x + i))^{\frac{7}{4}}}{(i a (x - i))^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)**(7/4)/(a+I*a*x)**(9/4),x)`

[Out] `Integral((-I*a*(x + I))**(7/4)/(I*a*(x - I))**(9/4), x)`

$$3.1218 \quad \int \frac{(a-iax)^{3/4}}{(a+iax)^{9/4}} dx$$

Optimal. Leaf size=115

$$-\frac{6\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a\sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{6i}{5a\sqrt[4]{a-iax} \sqrt[4]{a+iax}} + \frac{4i(a-iax)^{3/4}}{5a(a+iax)^{5/4}}$$

[Out] $4/5*I*(a-I*a*x)^{(3/4)}/a/(a+I*a*x)^{(5/4)}-6/5*I/a/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}-6/5*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.03, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {47, 48, 42, 197, 196}

$$-\frac{6\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a\sqrt[4]{a-iax} \sqrt[4]{a+iax}} - \frac{6i}{5a\sqrt[4]{a-iax} \sqrt[4]{a+iax}} + \frac{4i(a-iax)^{3/4}}{5a(a+iax)^{5/4}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a - I*a*x)^{(3/4)}/(a + I*a*x)^{(9/4)}, x]$

[Out] $((4*I)/5)*(a - I*a*x)^{(3/4)}/(a*(a + I*a*x)^{(5/4)}) - ((6*I)/5)/(a*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)}) - (6*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/((5*a*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Dist}[(a + b*x)^{\text{FracPart}[m]}*(c + d*x)^{\text{FracPart}[m]}/(a*c + b*d*x^2)^{\text{FracPart}[m]}, \text{Int}[(a*c + b*d*x^2)^m, x], x] /; \text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{EqQ}[b*c + a*d, 0] \ \&\& \ !\text{IntegerQ}[2*m]$

Rule 47

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{m+1}*(c + d*x)^n/(b*(m+1)), x] - \text{Dist}[(d*n)/(b*(m+1)), \text{Int}[(a + b*x)^{m+1}*(c + d*x)^{n-1}, x], x] /; \text{FreeQ}\{a, b, c, d\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{LtQ}[m, -1] \ \&\& \ !(\text{IntegerQ}[n] \ \&\& \ !\text{IntegerQ}[m]) \ \&\& \ !(\text{IntegerQ}[m+n+2, 0] \ \&\& \ (\text{FractionQ}[m] \ || \ \text{GeQ}[2*n+m+1, 0])) \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 48


```
Int[1/(((a_) + (b_.)*(x_))^(5/4)*((c_) + (d_.)*(x_))^(1/4)), x_Symbol] := S
imp[-2/(b*(a + b*x)^(1/4)*(c + d*x)^(1/4)), x] + Dist[c, Int[1/((a + b*x)^(
5/4)*(c + d*x)^(5/4)), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0
] && NegQ[a^2*b^2]
```

Rule 196

```
Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]
```

Rule 197

```
Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(
a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b},
x] && PosQ[a] && PosQ[b/a]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a - iax)^{3/4}}{(a + iax)^{9/4}} dx &= \frac{4i(a - iax)^{3/4}}{5a(a + iax)^{5/4}} - \frac{3}{5} \int \frac{1}{\sqrt[4]{a - iax} (a + iax)^{5/4}} dx \\
&= \frac{4i(a - iax)^{3/4}}{5a(a + iax)^{5/4}} - \frac{6i}{5a\sqrt[4]{a - iax}\sqrt[4]{a + iax}} - \frac{1}{5}(3a) \int \frac{1}{(a - iax)^{5/4}(a + iax)^{5/4}} dx \\
&= \frac{4i(a - iax)^{3/4}}{5a(a + iax)^{5/4}} - \frac{6i}{5a\sqrt[4]{a - iax}\sqrt[4]{a + iax}} - \frac{\left(3a\sqrt[4]{a^2 + a^2x^2}\right) \int \frac{1}{(a^2 + a^2x^2)^{5/4}} dx}{5\sqrt[4]{a - iax}\sqrt[4]{a + iax}} \\
&= \frac{4i(a - iax)^{3/4}}{5a(a + iax)^{5/4}} - \frac{6i}{5a\sqrt[4]{a - iax}\sqrt[4]{a + iax}} - \frac{\left(3\sqrt[4]{1 + x^2}\right) \int \frac{1}{(1 + x^2)^{5/4}} dx}{5a\sqrt[4]{a - iax}\sqrt[4]{a + iax}} \\
&= \frac{4i(a - iax)^{3/4}}{5a(a + iax)^{5/4}} - \frac{6i}{5a\sqrt[4]{a - iax}\sqrt[4]{a + iax}} - \frac{6\sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a\sqrt[4]{a - iax}\sqrt[4]{a + iax}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.61

$$\frac{i\sqrt[4]{1 + ix} (a - iax)^{7/4} {}_2F_1\left(\frac{7}{4}, \frac{9}{4}; \frac{11}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{7\sqrt[4]{2} a^3 \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(3/4)/(a + I*a*x)^(9/4), x]

[Out] ((I/7)*(1 + I*x)^(1/4)*(a - I*a*x)^(7/4)*Hypergeometric2F1[7/4, 9/4, 11/4, 1/2 - (I/2)*x])/(2^(1/4)*a^3*(a + I*a*x)^(1/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\frac{2(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}}(5ix + 3) - 5(a^3x^3 - 2ia^3x^2 - a^3x) \operatorname{integral}\left(\frac{6(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{5(a^3x^4+a^3x^2)}, x\right)}{5(a^3x^3 - 2ia^3x^2 - a^3x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(9/4), x, algorithm="fricas")

[Out] -1/5*(2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*(5*I*x + 3) - 5*(a^3*x^3 - 2*I*a^3*x^2 - a^3*x)*integral(6/5*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^3*x^4 + a^3*x^2), x))/(a^3*x^3 - 2*I*a^3*x^2 - a^3*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{\frac{3}{4}}}{(iax + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(9/4), x, algorithm="giac")

[Out] integrate((-I*a*x + a)^(3/4)/(I*a*x + a)^(9/4), x)

maple [C] time = 0.04, size = 107, normalized size = 0.93

$$\frac{3(-ix - 1)(ix + 1)a^{\frac{1}{4}} x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{5(a^2)^{\frac{1}{4}}(-ix - 1)a^{\frac{1}{4}}((ix + 1)a)^{\frac{1}{4}}a} \frac{2(3x^2 + 2ix + 1)}{5(x - i)(-ix - 1)a^{\frac{1}{4}}((ix + 1)a)^{\frac{1}{4}}a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(3/4)/(I*a*x+a)^(9/4), x)

[Out] -2/5*(3*x^2+1+2*I*x)/(x-I)/a/(-I*x-1)*a^(1/4)/((I*x+1)*a)^(1/4)+3/5/(a^2)^(1/4)*x*hypergeom([1/4, 1/2], [3/2], -x^2)/a*(-I*x-1)*(I*x+1)*a^2)^(1/4)/(-I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i a x + a)^{\frac{3}{4}}}{(i a x + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(3/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(3/4)/(I*a*x + a)^(9/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a - a x 1i)^{3/4}}{(a + a x 1i)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - a*x*1i)^(3/4)/(a + a*x*1i)^(9/4),x)

[Out] int((a - a*x*1i)^(3/4)/(a + a*x*1i)^(9/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i a (x + i))^{\frac{3}{4}}}{(i a (x - i))^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)**(3/4)/(a+I*a*x)**(9/4),x)

[Out] Integral((-I*a*(x + I))**(3/4)/(I*a*(x - I))**(9/4), x)

$$3.1219 \quad \int \frac{1}{\sqrt[4]{a-iax} (a+iax)^{9/4}} dx$$

Optimal. Leaf size=82

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^2 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} + \frac{4i}{5a \sqrt[4]{a-iax} (a+iax)^{5/4}}$$

[Out] $4/5*I/a/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(5/4)}+2/5*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x)))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a^2/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {46, 42, 197, 196}

$$\frac{2\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^2 \sqrt[4]{a-iax} \sqrt[4]{a+iax}} + \frac{4i}{5a \sqrt[4]{a-iax} (a+iax)^{5/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(1/4)*(a + I*a*x)^(9/4)),x]

[Out] $((4*I)/5)/(a*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(5/4)}) + (2*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(5*a^2*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 46

Int[1/(((a_) + (b_.)*(x_))^(9/4)*((c_) + (d_.)*(x_))^(1/4)), x_Symbol] :> Simp[-4/(5*b*(a + b*x)^(5/4)*(c + d*x)^(1/4)), x] - Dist[d/(5*b), Int[1/((a + b*x)^(5/4)*(c + d*x)^(5/4)), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && NegQ[a^2*b^2]

Rule 196

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] :> Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a

, 0] && PosQ[b/a]

Rule 197

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a] && PosQ[b/a]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt[4]{a-iax}(a+iax)^{9/4}} dx &= \frac{4i}{5a\sqrt[4]{a-iax}(a+iax)^{5/4}} + \frac{1}{5} \int \frac{1}{(a-iax)^{5/4}(a+iax)^{5/4}} dx \\ &= \frac{4i}{5a\sqrt[4]{a-iax}(a+iax)^{5/4}} + \frac{\sqrt[4]{a^2+a^2x^2} \int \frac{1}{(a^2+a^2x^2)^{5/4}} dx}{5\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\ &= \frac{4i}{5a\sqrt[4]{a-iax}(a+iax)^{5/4}} + \frac{\sqrt[4]{1+x^2} \int \frac{1}{(1+x^2)^{5/4}} dx}{5a^2\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \\ &= \frac{4i}{5a\sqrt[4]{a-iax}(a+iax)^{5/4}} + \frac{2\sqrt[4]{1+x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^2\sqrt[4]{a-iax}\sqrt[4]{a+iax}} \end{aligned}$$

Mathematica [C] time = 0.02, size = 70, normalized size = 0.85

$$\frac{i\sqrt[4]{1+ix}(a-iax)^{3/4} {}_2F_1\left(\frac{3}{4}, \frac{9}{4}; \frac{7}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{3\sqrt[4]{2} a^3 \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(1/4)*(a + I*a*x)^(9/4)), x]

[Out] ((I/3)*(1 + I*x)^(1/4)*(a - I*a*x)^(3/4)*Hypergeometric2F1[3/4, 9/4, 7/4, 1/2 - (I/2)*x])/(2^(1/4)*a^3*(a + I*a*x)^(1/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\frac{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}(2x-4i) + (5a^4x^2 - 10ia^4x - 5a^4) \operatorname{integral}\left(-\frac{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{5(a^4x^2+a^4)}, x\right)}{5a^4x^2 - 10ia^4x - 5a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(9/4),x, algorithm="fricas")

[Out] ((I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*(2*x - 4*I) + (5*a^4*x^2 - 10*I*a^4*x - 5*a^4)*integral(-1/5*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^4*x^2 + a^4), x))/(5*a^4*x^2 - 10*I*a^4*x - 5*a^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{9}{4}} (-i a x + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(9/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(1/4)), x)

maple [C] time = 0.04, size = 105, normalized size = 1.28

$$\frac{(-i x - 1)(i x + 1) a^2)^{\frac{1}{4}} x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{5 (a^2)^{\frac{1}{4}} (-i x - 1) a^{\frac{1}{4}} ((i x + 1) a)^{\frac{1}{4}} a^2} + \frac{\frac{2}{5} x^2 - \frac{2}{5} i x + \frac{4}{5}}{(x - i) (-i x - 1) a^{\frac{1}{4}} ((i x + 1) a)^{\frac{1}{4}} a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(1/4)/(I*a*x+a)^(9/4),x)

[Out] 2/5*(x^2+2-I*x)/(x-I)/a^2/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)-1/5/(a^2)^(1/4)*x*hypergeom([1/4,1/2],[3/2],-x^2)/a^2*(-(I*x-1)*(I*x+1)*a^2)^(1/4)/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{9}{4}} (-i a x + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(1/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{1/4} (a + a x 1i)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(1/4)*(a + a*x*1i)^(9/4)),x)`

[Out] `int(1/((a - a*x*1i)^(1/4)*(a + a*x*1i)^(9/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{9}{4}} \sqrt[4]{-ia(x+i)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(1/4)/(a+I*a*x)**(9/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(9/4)*(-I*a*(x + I))**(1/4)), x)`

$$3.1220 \quad \int \frac{1}{(a-iax)^{5/4}(a+iax)^{9/4}} dx$$

Optimal. Leaf size=82

$$\frac{6\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^3\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{2i}{5a^2\sqrt[4]{a-iax}(a+iax)^{5/4}}$$

[Out] $2/5*I/a^2/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(5/4)}+6/5*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x)))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a^3/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 46, 42, 197, 196}

$$\frac{6\sqrt[4]{x^2+1} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^3\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{2i}{5a^2\sqrt[4]{a-iax}(a+iax)^{5/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(5/4)*(a + I*a*x)^(9/4)), x]

[Out] $((2*I)/5)/(a^2*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(5/4)}) + (6*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(5*a^3*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 46

Int[1/(((a_) + (b_.)*(x_))^(9/4)*((c_) + (d_.)*(x_))^(1/4)), x_Symbol] :> Simp[-4/(5*b*(a + b*x)^(5/4)*(c + d*x)^(1/4)), x] - Dist[d/(5*b), Int[1/((a + b*x)^(5/4)*(c + d*x)^(5/4)), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b*c + a*d, 0] && NegQ[a^2*b^2]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[(a + b*x)^(m + 1)*(c + d*x)^(n + 1)/((b*c - a*d)*(m + 1)), x] - Dist[(d*(


```

m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]

```

Rule 196

```

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[
Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a
, 0] && PosQ[b/a]

```

Rule 197

```

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(
a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b},
x] && PosQ[a] && PosQ[b/a]

```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a - iax)^{5/4}(a + iax)^{9/4}} dx &= -\frac{2i}{a^2 \sqrt[4]{a - iax} (a + iax)^{5/4}} + \frac{3 \int \frac{1}{\sqrt[4]{a - iax} (a + iax)^{9/4}} dx}{a} \\
&= \frac{2i}{5a^2 \sqrt[4]{a - iax} (a + iax)^{5/4}} + \frac{3 \int \frac{1}{(a - iax)^{5/4}(a + iax)^{5/4}} dx}{5a} \\
&= \frac{2i}{5a^2 \sqrt[4]{a - iax} (a + iax)^{5/4}} + \frac{\left(3 \sqrt[4]{a^2 + a^2 x^2}\right) \int \frac{1}{(a^2 + a^2 x^2)^{5/4}} dx}{5a \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= \frac{2i}{5a^2 \sqrt[4]{a - iax} (a + iax)^{5/4}} + \frac{\left(3 \sqrt[4]{1 + x^2}\right) \int \frac{1}{(1 + x^2)^{5/4}} dx}{5a^3 \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\
&= \frac{2i}{5a^2 \sqrt[4]{a - iax} (a + iax)^{5/4}} + \frac{6 \sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^3 \sqrt[4]{a - iax} \sqrt[4]{a + iax}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 68, normalized size = 0.83

$$-\frac{i \sqrt[4]{1 + ix} {}_2F_1\left(-\frac{1}{4}, \frac{9}{4}; \frac{3}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{\sqrt[4]{2} a^3 \sqrt[4]{a - iax} \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(5/4)*(a + I*a*x)^(9/4)), x]

[Out] ((-I)*(1 + I*x)^(1/4)*Hypergeometric2F1[-1/4, 9/4, 3/4, 1/2 - (I/2)*x])/(2^(1/4)*a^3*(a - I*a*x)^(1/4)*(a + I*a*x)^(1/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\frac{2(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}}(3x^2 - 3ix + 1) + (5a^5x^3 - 5ia^5x^2 + 5a^5x - 5ia^5)\operatorname{integral}\left(-\frac{3(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{5(a^5x^2+a^5)}, x\right)}{5a^5x^3 - 5ia^5x^2 + 5a^5x - 5ia^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(9/4), x, algorithm="fricas")

[Out] (2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)*(3*x^2 - 3*I*x + 1) + (5*a^5*x^3 - 5*I*a^5*x^2 + 5*a^5*x - 5*I*a^5)*integral(-3/5*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^5*x^2 + a^5), x))/(5*a^5*x^3 - 5*I*a^5*x^2 + 5*a^5*x - 5*I*a^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{9}{4}}(-iax + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(9/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(5/4)), x)

maple [C] time = 0.06, size = 107, normalized size = 1.30

$$\frac{3(-ix - 1)(ix + 1)a^2)^{\frac{1}{4}} x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{5(a^2)^{\frac{1}{4}}(-ix - 1)a^{\frac{1}{4}}((ix + 1)a)^{\frac{1}{4}}a^3} + \frac{\frac{6}{5}x^2 - \frac{6}{5}ix + \frac{2}{5}}{(x - i)(-ix - 1)a^{\frac{1}{4}}((ix + 1)a)^{\frac{1}{4}}a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(5/4)/(I*a*x+a)^(9/4), x)

[Out] 2/5*(-3*I*x+3*x^2+1)/(x-I)/a^3/(-I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)-3/5/(a^2)^(1/4)*x*hypergeom([1/4, 1/2], [3/2], -x^2)/a^3*(-I*x-1)*(I*x+1)*a^2)^(1/4)/(-I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(5/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x i)^{5/4} (a + a x i)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*i)^(5/4)*(a + a*x*i)^(9/4)),x)

[Out] int(1/((a - a*x*i)^(5/4)*(a + a*x*i)^(9/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{9/4} (-ia(x+i))^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(5/4)/(a+I*a*x)**(9/4),x)

[Out] Integral(1/((I*a*(x - I))**(9/4)*(-I*a*(x + I))**(5/4)), x)

$$3.1221 \quad \int \frac{1}{(a-iax)^{9/4}(a+iax)^{9/4}} dx$$

Optimal. Leaf size=88

$$\frac{2x}{5a^4(x^2+1)\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{6\sqrt[4]{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{5a^4\sqrt[4]{a-iax}\sqrt[4]{a+iax}}$$

[Out] 2/5*x/a^4/(a-I*a*x)^(1/4)/(a+I*a*x)^(1/4)/(x^2+1)+6/5*(x^2+1)^(1/4)*(cos(1/2*arctan(x))^2)^(1/2)/cos(1/2*arctan(x))*EllipticE(sin(1/2*arctan(x)),2^(1/2))/a^4/(a-I*a*x)^(1/4)/(a+I*a*x)^(1/4)

Rubi [A] time = 0.02, antiderivative size = 88, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.160$, Rules used = {42, 199, 197, 196}

$$\frac{2x}{5a^4(x^2+1)\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{6\sqrt[4]{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{5a^4\sqrt[4]{a-iax}\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(9/4)*(a + I*a*x)^(9/4)),x]

[Out] (2*x)/(5*a^4*(a - I*a*x)^(1/4)*(a + I*a*x)^(1/4)*(1 + x^2)) + (6*(1 + x^2)^(1/4)*EllipticE[ArcTan[x]/2, 2])/(5*a^4*(a - I*a*x)^(1/4)*(a + I*a*x)^(1/4))

Rule 42

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 196

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 197

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b},

$x] \ \&\& \ \text{PosQ}[a] \ \&\& \ \text{PosQ}[b/a]$

Rule 199

$\text{Int}[(a_ + (b_)*(x_)^{(n_))^{(p_)}, x_Symbol] := -\text{Simp}[(x*(a + b*x^n)^{(p + 1)})/(a*n*(p + 1)), x] + \text{Dist}[(n*(p + 1) + 1)/(a*n*(p + 1)), \text{Int}[(a + b*x^n)^{(p + 1)}, x], x] /;$ $\text{FreeQ}\{a, b\}, x] \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{LtQ}[p, -1] \ \&\& \ (\text{IntegerQ}[2*p] \ || \ (n == 2 \ \&\& \ \text{IntegerQ}[4*p]) \ || \ (n == 2 \ \&\& \ \text{IntegerQ}[3*p]) \ || \ \text{Denominator}[p + 1/n] < \text{Denominator}[p])$

Rubi steps

$$\begin{aligned} \int \frac{1}{(a - iax)^{9/4}(a + iax)^{9/4}} dx &= \frac{\sqrt[4]{a^2 + a^2x^2} \int \frac{1}{(a^2 + a^2x^2)^{9/4}} dx}{\sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\ &= \frac{2x}{5a^4 \sqrt[4]{a - iax} \sqrt[4]{a + iax} (1 + x^2)} + \frac{\left(3\sqrt[4]{a^2 + a^2x^2}\right) \int \frac{1}{(a^2 + a^2x^2)^{5/4}} dx}{5a^2 \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\ &= \frac{2x}{5a^4 \sqrt[4]{a - iax} \sqrt[4]{a + iax} (1 + x^2)} + \frac{\left(3\sqrt[4]{1 + x^2}\right) \int \frac{1}{(1 + x^2)^{5/4}} dx}{5a^4 \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \\ &= \frac{2x}{5a^4 \sqrt[4]{a - iax} \sqrt[4]{a + iax} (1 + x^2)} + \frac{6\sqrt[4]{1 + x^2} E\left(\frac{1}{2} \tan^{-1}(x) \middle| 2\right)}{5a^4 \sqrt[4]{a - iax} \sqrt[4]{a + iax}} \end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.80

$$\frac{i\sqrt[4]{1 + ix} {}_2F_1\left(-\frac{5}{4}, \frac{9}{4}; -\frac{1}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{5\sqrt[4]{2} a^3 (a - iax)^{5/4} \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(9/4)*(a + I*a*x)^(9/4)),x]

[Out] ((-1/5*I)*(1 + I*x)^(1/4)*Hypergeometric2F1[-5/4, 9/4, -1/4, 1/2 - (I/2)*x])/(2^(1/4)*a^3*(a - I*a*x)^(5/4)*(a + I*a*x)^(1/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\frac{2(3x^3 + 4x)(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}} + 5(a^6x^4 + 2a^6x^2 + a^6)\operatorname{integral}\left(-\frac{3(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{3}{4}}}{5(a^6x^2+a^6)}, x\right)}{5(a^6x^4 + 2a^6x^2 + a^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(9/4),x, algorithm="fricas")`

[Out] `1/5*(2*(3*x^3 + 4*x)*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4) + 5*(a^6*x^4 + 2*a^6*x^2 + a^6)*integral(-3/5*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^6*x^2 + a^6), x))/(a^6*x^4 + 2*a^6*x^2 + a^6)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{9}{4}}(-iax + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(9/4),x, algorithm="giac")`

[Out] `integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(9/4)), x)`

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{1}{(-iax + a)^{\frac{9}{4}}(iax + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(9/4)/(I*a*x+a)^(9/4),x)`

[Out] `int(1/(-I*a*x+a)^(9/4)/(I*a*x+a)^(9/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{9}{4}}(-iax + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(9/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")`

[Out] `integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(9/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{9/4} (a + a x 1i)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(9/4)*(a + a*x*1i)^(9/4)),x)

[Out] int(1/((a - a*x*1i)^(9/4)*(a + a*x*1i)^(9/4)), x)

sympy [A] time = 132.49, size = 95, normalized size = 1.08

$$-\frac{iG_{6,6}^{5,3} \left(\begin{array}{c} \frac{9}{8}, \frac{13}{8}, 1 \\ \frac{1}{2}, \frac{9}{4}, \frac{11}{4} \end{array} \middle| \frac{e^{-3i\pi}}{x^2} \right) e^{\frac{i\pi}{4}}}{4\pi a^{\frac{9}{2}} \Gamma\left(\frac{9}{4}\right)} + \frac{iG_{6,6}^{2,6} \left(\begin{array}{c} -\frac{1}{2}, 0, \frac{1}{2}, \frac{5}{8}, \frac{9}{8}, 1 \\ \frac{5}{8}, \frac{9}{8} \end{array} \middle| \frac{e^{-i\pi}}{x^2} \right)}{4\pi a^{\frac{9}{2}} \Gamma\left(\frac{9}{4}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(9/4)/(a+I*a*x)**(9/4),x)

[Out] -I*meijerg(((9/8, 13/8, 1), (1/2, 9/4, 11/4)), ((9/8, 13/8, 7/4, 9/4, 11/4), (0,)), exp_polar(-3*I*pi)/x**2)*exp(I*pi/4)/(4*pi*a**(9/2)*gamma(9/4)) + I*meijerg((-1/2, 0, 1/2, 5/8, 9/8, 1), ()), ((5/8, 9/8), (-1/2, 0, 7/4, 0)), exp_polar(-I*pi)/x**2)/(4*pi*a**(9/2)*gamma(9/4))

$$3.1222 \quad \int \frac{1}{(a-iax)^{13/4}(a+iax)^{9/4}} dx$$

Optimal. Leaf size=121

$$\frac{14x}{45a^5(x^2+1)\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{14\sqrt[4]{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{15a^5\sqrt[4]{a-iax}\sqrt[4]{a+iax}} - \frac{2i}{9a^2(a-iax)^{9/4}(a+iax)^{5/4}}$$

[Out] $-2/9*I/a^2/(a-I*a*x)^{(9/4)}/(a+I*a*x)^{(5/4)}+14/45*x/a^5/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}/(x^2+1)+14/15*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a^5/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.03, antiderivative size = 121, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 42, 199, 197, 196}

$$\frac{14x}{45a^5(x^2+1)\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{14\sqrt[4]{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{15a^5\sqrt[4]{a-iax}\sqrt[4]{a+iax}} - \frac{2i}{9a^2(a-iax)^{9/4}(a+iax)^{5/4}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a - I*a*x)^{(13/4)}*(a + I*a*x)^{(9/4))}, x]$

[Out] $((-2*I)/9)/(a^2*(a - I*a*x)^{(9/4)}*(a + I*a*x)^{(5/4)}) + (14*x)/(45*a^5*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)}*(1 + x^2)) + (14*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(15*a^5*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Dist}[(a + b*x)^{\text{FracPart}[m]}*(c + d*x)^{\text{FracPart}[m]}/(a*c + b*d*x^2)^{\text{FracPart}[m]}, \text{Int}[(a*c + b*d*x^2)^m, x], x] /; \text{FreeQ}[\{a, b, c, d, m\}, x] \ \&\& \ \text{EqQ}[b*c + a*d, 0] \ \&\& \ !\text{IntegerQ}[2*m]$

Rule 51

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}/((b*c - a*d)*(m+1)), x] - \text{Dist}[(d*(m+n+2))/((b*c - a*d)*(m+1)), \text{Int}[(a + b*x)^{(m+1)}*(c + d*x)^n, x], x] /; \text{FreeQ}[\{a, b, c, d, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[m, -1] \ \&\& \ !(\text{LtQ}[n, -1] \ \&\& \ (\text{EqQ}[a, 0] \ || \ (\text{NeQ}[c, 0] \ \&\& \ \text{LtQ}[m-n, 0] \ \&\& \ \text{IntegerQ}[n]))) \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 196

Int[((a_) + (b_)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 197

Int[((a_) + (b_)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a] && PosQ[b/a]

Rule 199

Int[((a_) + (b_)*(x_)^(n_))^(p_), x_Symbol] := -Simp[(x*(a + b*x^n)^(p + 1))/(a*n*(p + 1)), x] + Dist[(n*(p + 1) + 1)/(a*n*(p + 1)), Int[(a + b*x^n)^(p + 1), x], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[p, -1] && (IntegerQ[2*p] || (n == 2 && IntegerQ[4*p]) || (n == 2 && IntegerQ[3*p]) || Denominator[p + 1/n] < Denominator[p])

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a - iax)^{13/4}(a + iax)^{9/4}} dx &= -\frac{2i}{9a^2(a - iax)^{9/4}(a + iax)^{5/4}} + \frac{7 \int \frac{1}{(a - iax)^{9/4}(a + iax)^{9/4}} dx}{9a} \\
 &= -\frac{2i}{9a^2(a - iax)^{9/4}(a + iax)^{5/4}} + \frac{\left(7\sqrt[4]{a^2 + a^2x^2}\right) \int \frac{1}{(a^2 + a^2x^2)^{9/4}} dx}{9a\sqrt[4]{a - iax}\sqrt[4]{a + iax}} \\
 &= -\frac{2i}{9a^2(a - iax)^{9/4}(a + iax)^{5/4}} + \frac{14x}{45a^5\sqrt[4]{a - iax}\sqrt[4]{a + iax}(1 + x^2)} + \frac{\left(7\sqrt[4]{a^2 + a^2x^2}\right)}{15a^3\sqrt[4]{a - iax}} \\
 &= -\frac{2i}{9a^2(a - iax)^{9/4}(a + iax)^{5/4}} + \frac{14x}{45a^5\sqrt[4]{a - iax}\sqrt[4]{a + iax}(1 + x^2)} + \frac{\left(7\sqrt[4]{1 + x^2}\right)}{15a^5\sqrt[4]{a - iax}} \\
 &= -\frac{2i}{9a^2(a - iax)^{9/4}(a + iax)^{5/4}} + \frac{14x}{45a^5\sqrt[4]{a - iax}\sqrt[4]{a + iax}(1 + x^2)} + \frac{14\sqrt[4]{1 + x^2}E}{15a^5\sqrt[4]{a - iax}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.58

$$\frac{i\sqrt[4]{1+ix} {}_2F_1\left(-\frac{9}{4}, \frac{9}{4}; -\frac{5}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{9\sqrt[4]{2} a^3 (a - iax)^{9/4} \sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(13/4)*(a + I*a*x)^(9/4)), x]

[Out] ((-1/9*I)*(1 + I*x)^(1/4)*Hypergeometric2F1[-9/4, 9/4, -5/4, 1/2 - (I/2)*x])/(2^(1/4)*a^3*(a - I*a*x)^(9/4)*(a + I*a*x)^(1/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\frac{(42x^4 + 42ix^3 + 56x^2 + 56ix + 10)(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}} + (45a^7x^5 + 45ia^7x^4 + 90a^7x^3 + 90ia^7x^2 + 45a^7x + 45i a^7)}{45a^7x^5 + 45ia^7x^4 + 90a^7x^3 + 90ia^7x^2 + 45a^7x + 45ia^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(9/4), x, algorithm="fricas")

[Out] ((42*x^4 + 42*I*x^3 + 56*x^2 + 56*I*x + 10)*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4) + (45*a^7*x^5 + 45*I*a^7*x^4 + 90*a^7*x^3 + 90*I*a^7*x^2 + 45*a^7*x + 45*I*a^7)*integral(-7/15*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^7*x^2 + a^7), x))/(45*a^7*x^5 + 45*I*a^7*x^4 + 90*a^7*x^3 + 90*I*a^7*x^2 + 45*a^7*x + 45*I*a^7)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{9}{4}}(-iax + a)^{\frac{13}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(9/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(13/4)), x)

maple [C] time = 0.10, size = 124, normalized size = 1.02

$$\frac{7(-ix-1)(ix+1)a^2)^{\frac{1}{4}} x \operatorname{hypergeom}\left(\left[\frac{1}{4}, \frac{1}{2}\right], \left[\frac{3}{2}\right], -x^2\right)}{15(a^2)^{\frac{1}{4}}(-ix-1)a^{\frac{1}{4}}((ix+1)a)^{\frac{1}{4}}a^5} + \frac{\frac{14}{15}x^4 + \frac{14}{15}ix^3 + \frac{56}{45}x^2 + \frac{56}{45}ix + \frac{2}{9}}{(x-i)(x+i)^2(-ix-1)a^{\frac{1}{4}}((ix+1)a)^{\frac{1}{4}}a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(13/4)/(I*a*x+a)^(9/4),x)`

[Out] $2/45*(21*I*x^3+21*x^4+28*I*x+28*x^2+5)/(x-I)/(x+I)^2/a^5/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)-7/15/(a^2)^(1/4)*x*\text{hypergeom}([1/4,1/2],[3/2],-x^2)/a^5*(-(I*x-1)*(I*x+1)*a^2)^(1/4)/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(13/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x 1i)^{13/4} (a + a x 1i)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(13/4)*(a + a*x*1i)^(9/4)),x)`

[Out] `int(1/((a - a*x*1i)^(13/4)*(a + a*x*1i)^(9/4)), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(13/4)/(a+I*a*x)**(9/4),x)`

[Out] Timed out

$$3.1223 \quad \int \frac{1}{(a-iax)^{17/4}(a+iax)^{9/4}} dx$$

Optimal. Leaf size=154

$$\frac{14x}{65a^6(x^2+1)\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{42\sqrt[4]{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{65a^6\sqrt[4]{a-iax}\sqrt[4]{a+iax}} - \frac{2i}{13a^3(a-iax)^{9/4}(a+iax)^{5/4}} - \frac{2i}{13a^2(a-iax)^{13/4}(a+iax)^{1/4}}$$

[Out] $-2/13*I/a^2/(a-I*a*x)^{(13/4)}/(a+I*a*x)^{(5/4)}-2/13*I/a^3/(a-I*a*x)^{(9/4)}/(a+I*a*x)^{(5/4)}+14/65*x/a^6/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}/(x^2+1)+42/65*(x^2+1)^{(1/4)}*(\cos(1/2*\arctan(x))^2)^{(1/2)}/\cos(1/2*\arctan(x))*\text{EllipticE}(\sin(1/2*\arctan(x)),2^{(1/2)})/a^6/(a-I*a*x)^{(1/4)}/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.04, antiderivative size = 154, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {51, 42, 199, 197, 196}

$$\frac{14x}{65a^6(x^2+1)\sqrt[4]{a-iax}\sqrt[4]{a+iax}} + \frac{42\sqrt[4]{x^2+1}E\left(\frac{1}{2}\tan^{-1}(x)\middle|2\right)}{65a^6\sqrt[4]{a-iax}\sqrt[4]{a+iax}} - \frac{2i}{13a^3(a-iax)^{9/4}(a+iax)^{5/4}} - \frac{2i}{13a^2(a-iax)^{13/4}(a+iax)^{1/4}}$$

Antiderivative was successfully verified.

[In] `Int[1/((a - I*a*x)^(17/4)*(a + I*a*x)^(9/4)), x]`

[Out] $((-2*I)/13)/(a^2*(a - I*a*x)^{(13/4)}*(a + I*a*x)^{(5/4)}) - ((2*I)/13)/(a^3*(a - I*a*x)^{(9/4)}*(a + I*a*x)^{(5/4)}) + (14*x)/(65*a^6*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)}*(1 + x^2)) + (42*(1 + x^2)^{(1/4)}*\text{EllipticE}[\text{ArcTan}[x]/2, 2])/(65*a^6*(a - I*a*x)^{(1/4)}*(a + I*a*x)^{(1/4)})$

Rule 42

`Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]`

Rule 51

`Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])))] && I`

ntLinearQ[a, b, c, d, m, n, x]

Rule 196

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Simp[(2*EllipticE[(1*ArcTan[Rt[b/a, 2]*x])/2, 2])/(a^(5/4)*Rt[b/a, 2]), x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b/a]

Rule 197

Int[((a_) + (b_.)*(x_)^2)^(-5/4), x_Symbol] := Dist[(1 + (b*x^2)/a)^(1/4)/(a*(a + b*x^2)^(1/4)), Int[1/(1 + (b*x^2)/a)^(5/4), x], x] /; FreeQ[{a, b}, x] && PosQ[a] && PosQ[b/a]

Rule 199

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := -Simp[(x*(a + b*x^n)^(p + 1))/(a*n*(p + 1)), x] + Dist[(n*(p + 1) + 1)/(a*n*(p + 1)), Int[(a + b*x^n)^(p + 1), x], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[p, -1] && (IntegerQ[2*p] || (n == 2 && IntegerQ[4*p]) || (n == 2 && IntegerQ[3*p]) || Denominator[p + 1/n] < Denominator[p])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a-iax)^{17/4}(a+iax)^{9/4}} dx &= -\frac{2i}{13a^2(a-iax)^{13/4}(a+iax)^{5/4}} + \frac{9 \int \frac{1}{(a-iax)^{13/4}(a+iax)^{9/4}} dx}{13a} \\
&= -\frac{2i}{13a^2(a-iax)^{13/4}(a+iax)^{5/4}} - \frac{2i}{13a^3(a-iax)^{9/4}(a+iax)^{5/4}} + \frac{7 \int \frac{1}{(a-iax)^{9/4}(a+iax)^5}}{13a^2} \\
&= -\frac{2i}{13a^2(a-iax)^{13/4}(a+iax)^{5/4}} - \frac{2i}{13a^3(a-iax)^{9/4}(a+iax)^{5/4}} + \frac{\left(7\sqrt[4]{a^2+a^2x^2}\right) \int}{13a^2\sqrt[4]{a-iax}} \\
&= -\frac{2i}{13a^2(a-iax)^{13/4}(a+iax)^{5/4}} - \frac{2i}{13a^3(a-iax)^{9/4}(a+iax)^{5/4}} + \frac{14x}{65a^6\sqrt[4]{a-iax}\sqrt[4]{a}} \\
&= -\frac{2i}{13a^2(a-iax)^{13/4}(a+iax)^{5/4}} - \frac{2i}{13a^3(a-iax)^{9/4}(a+iax)^{5/4}} + \frac{14x}{65a^6\sqrt[4]{a-iax}\sqrt[4]{a}} \\
&= -\frac{2i}{13a^2(a-iax)^{13/4}(a+iax)^{5/4}} - \frac{2i}{13a^3(a-iax)^{9/4}(a+iax)^{5/4}} + \frac{14x}{65a^6\sqrt[4]{a-iax}\sqrt[4]{a}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 70, normalized size = 0.45

$$\frac{i\sqrt[4]{1+ix} {}_2F_1\left(-\frac{13}{4}, \frac{9}{4}; -\frac{9}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{13\sqrt[4]{2} a^3 (a-iax)^{13/4} \sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(17/4)*(a + I*a*x)^(9/4)), x]

[Out] ((-1/13*I)*(1 + I*x)^(1/4)*Hypergeometric2F1[-13/4, 9/4, -9/4, 1/2 - (I/2)*x])/(2^(1/4)*a^3*(a - I*a*x)^(13/4)*(a + I*a*x)^(1/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\frac{(42x^5 + 84ix^4 + 14x^3 + 112ix^2 - 46x + 20i)(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{3}{4}} + (65a^8x^6 + 130ia^8x^5 + 65a^8x^4 + 260ia^8x^3 - 65a^8x^2 + 130ia^8x)}{65a^8x^6 + 130ia^8x^5 + 65a^8x^4 + 260ia^8x^3 - 65a^8x^2 + 130ia^8x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(17/4)/(a+I*a*x)^(9/4),x, algorithm="fricas")

[Out] ((42*x^5 + 84*I*x^4 + 14*x^3 + 112*I*x^2 - 46*x + 20*I)*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4) + (65*a^8*x^6 + 130*I*a^8*x^5 + 65*a^8*x^4 + 260*I*a^8*x^3 - 65*a^8*x^2 + 130*I*a^8*x - 65*a^8)*integral(-21/65*(I*a*x + a)^(3/4)*(-I*a*x + a)^(3/4)/(a^8*x^2 + a^8), x))/(65*a^8*x^6 + 130*I*a^8*x^5 + 65*a^8*x^4 + 260*I*a^8*x^3 - 65*a^8*x^2 + 130*I*a^8*x - 65*a^8)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(i a x + a)^{\frac{9}{4}} (-i a x + a)^{\frac{17}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(17/4)/(a+I*a*x)^(9/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(17/4)), x)

maple [C] time = 0.10, size = 130, normalized size = 0.84

$$\frac{21 \left(-(ix - 1)(ix + 1)a^2 \right)^{\frac{1}{4}} x \operatorname{hypergeom} \left(\left[\frac{1}{4}, \frac{1}{2} \right], \left[\frac{3}{2} \right], -x^2 \right)}{65 \left(a^2 \right)^{\frac{1}{4}} (-ix - 1)a^{\frac{1}{4}} ((ix + 1)a)^{\frac{1}{4}} a^6} + \frac{\frac{42}{65}x^5 + \frac{84}{65}ix^4 + \frac{14}{65}x^3 + \frac{112}{65}ix^2 - \frac{46}{65}x + \frac{4}{13}i}{(x - i)(x + i)^3 (-ix - 1)a^{\frac{1}{4}} ((ix + 1)a)^{\frac{1}{4}} a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(17/4)/(I*a*x+a)^(9/4),x)

[Out] 2/65*(42*I*x^4+21*x^5+56*I*x^2-23*x+7*x^3+10*I)/(x-I)/(x+I)^3/a^6/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)-21/65/(a^2)^(1/4)*x*hypergeom([1/4, 1/2], [3/2], -x^2)/a^6/(-(I*x-1)*(I*x+1)*a^2)^(1/4)/(-(I*x-1)*a)^(1/4)/((I*x+1)*a)^(1/4)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(17/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a - a x i)^{17/4} (a + a x i)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a - a*x*1i)^(17/4)*(a + a*x*1i)^(9/4)),x)
```

```
[Out] int(1/((a - a*x*1i)^(17/4)*(a + a*x*1i)^(9/4)), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a-I*a*x)**(17/4)/(a+I*a*x)**(9/4),x)
```

```
[Out] Timed out
```


$$3.1224 \quad \int \frac{(a-iax)^{5/4}}{(a+iax)^{9/4}} dx$$

Optimal. Leaf size=297

$$\frac{4i(a-iax)^{5/4}}{5a(a+iax)^{5/4}} - \frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} - \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} + \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} - \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2}}{\sqrt[4]{a+iax}}\right)}{a}$$

[Out] $4/5*I*(a-I*a*x)^{(5/4)}/a/(a+I*a*x)^{(5/4)}-4*I*(a-I*a*x)^{(1/4)}/a/(a+I*a*x)^{(1/4)}-1/2*I*\ln(1-(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2))}/a*2^{(1/2)}+1/2*I*\ln(1+(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)}+(a-I*a*x)^{(1/2)}/(a+I*a*x)^{(1/2))}/a*2^{(1/2)}-I*\arctan(1-(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)})*2^{(1/2)}/a+I*\arctan(1+(a-I*a*x)^{(1/4)}*2^{(1/2)}/(a+I*a*x)^{(1/4)})*2^{(1/2)}/a$

Rubi [A] time = 0.14, antiderivative size = 297, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 9, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.360$, Rules used = {47, 63, 240, 211, 1165, 628, 1162, 617, 204}

$$\frac{4i(a-iax)^{5/4}}{5a(a+iax)^{5/4}} - \frac{4i\sqrt[4]{a-iax}}{a\sqrt[4]{a+iax}} - \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} + \frac{i \log\left(\frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}} + 1\right)}{\sqrt{2}a} - \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2}}{\sqrt[4]{a+iax}}\right)}{a}$$

Antiderivative was successfully verified.

[In] Int[(a - I*a*x)^(5/4)/(a + I*a*x)^(9/4), x]

[Out] $((4I/5)*(a-I*a*x)^{(5/4)}/(a*(a+I*a*x)^{(5/4)}) - ((4I)*(a-I*a*x)^{(1/4)}/(a*(a+I*a*x)^{(1/4)}) - (I*Sqrt[2]*ArcTan[1 - (Sqrt[2]*(a-I*a*x)^{(1/4)})/(a+I*a*x)^{(1/4)}])/a + (I*Sqrt[2]*ArcTan[1 + (Sqrt[2]*(a-I*a*x)^{(1/4)})/(a+I*a*x)^{(1/4)}])/a - (I*Log[1 + Sqrt[a-I*a*x]/Sqrt[a+I*a*x] - (Sqrt[2]*(a-I*a*x)^{(1/4)})/(a+I*a*x)^{(1/4)}])/Sqrt[2]*a + (I*Log[1 + Sqrt[a-I*a*x]/Sqrt[a+I*a*x] + (Sqrt[2]*(a-I*a*x)^{(1/4)})/(a+I*a*x)^{(1/4)}])/Sqrt[2]*a)$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 211

```
Int[((a_) + (b_.)*(x_)^4)^(-1), x_Symbol] := With[{r = Numerator[Rt[a/b, 2]
], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*r), Int[(r - s*x^2)/(a + b*x^4),
x], x] + Dist[1/(2*r), Int[(r + s*x^2)/(a + b*x^4), x], x]] /; FreeQ[{a, b
}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] &&
AtomQ[SplitProduct[SumBaseQ, b]]))
```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int
[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a,
b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/
n]
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 1162

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
```

$(2*d)/e, 2\}}, \text{Dist}[e/(2*c), \text{Int}[1/\text{Simp}[d/e + q*x + x^2, x], x], x] + \text{Dist}[e/(2*c), \text{Int}[1/\text{Simp}[d/e - q*x + x^2, x], x], x]] /; \text{FreeQ}[\{a, c, d, e\}, x] \& \& \text{EqQ}[c*d^2 - a*e^2, 0] \& \& \text{PosQ}[d*e]$

Rule 1165

$\text{Int}[\{(d_) + (e_)*(x_)^2\}/\{(a_) + (c_)*(x_)^4\}, x_Symbol] \text{:} > \text{With}[\{q = \text{Rt}[-(2*d)/e, 2]\}, \text{Dist}[e/(2*c*q), \text{Int}[(q - 2*x)/\text{Simp}[d/e + q*x - x^2, x], x], x] + \text{Dist}[e/(2*c*q), \text{Int}[(q + 2*x)/\text{Simp}[d/e - q*x - x^2, x], x], x]] /; \text{FreeQ}[\{a, c, d, e\}, x] \& \& \text{EqQ}[c*d^2 - a*e^2, 0] \& \& \text{NegQ}[d*e]$

Rubi steps

$$\begin{aligned}
 \int \frac{(a - iax)^{5/4}}{(a + iax)^{9/4}} dx &= \frac{4i(a - iax)^{5/4}}{5a(a + iax)^{5/4}} - \int \frac{\sqrt[4]{a - iax}}{(a + iax)^{5/4}} dx \\
 &= \frac{4i(a - iax)^{5/4}}{5a(a + iax)^{5/4}} - \frac{4i\sqrt[4]{a - iax}}{a\sqrt[4]{a + iax}} + \int \frac{1}{(a - iax)^{3/4}\sqrt[4]{a + iax}} dx \\
 &= \frac{4i(a - iax)^{5/4}}{5a(a + iax)^{5/4}} - \frac{4i\sqrt[4]{a - iax}}{a\sqrt[4]{a + iax}} + \frac{(4i) \text{Subst}\left(\int \frac{1}{\sqrt[4]{2a-x^4}} dx, x, \sqrt[4]{a - iax}\right)}{a} \\
 &= \frac{4i(a - iax)^{5/4}}{5a(a + iax)^{5/4}} - \frac{4i\sqrt[4]{a - iax}}{a\sqrt[4]{a + iax}} + \frac{(4i) \text{Subst}\left(\int \frac{1}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} \\
 &= \frac{4i(a - iax)^{5/4}}{5a(a + iax)^{5/4}} - \frac{4i\sqrt[4]{a - iax}}{a\sqrt[4]{a + iax}} + \frac{(2i) \text{Subst}\left(\int \frac{1-x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{(2i) \text{Subst}\left(\int \frac{1+x^2}{1+x^4} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} \\
 &= \frac{4i(a - iax)^{5/4}}{5a(a + iax)^{5/4}} - \frac{4i\sqrt[4]{a - iax}}{a\sqrt[4]{a + iax}} + \frac{i \text{Subst}\left(\int \frac{1}{1-\sqrt{2}xx^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i \text{Subst}\left(\int \frac{1}{1+\sqrt{2}xx^2} dx, x, \frac{\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} \\
 &= \frac{4i(a - iax)^{5/4}}{5a(a + iax)^{5/4}} - \frac{4i\sqrt[4]{a - iax}}{a\sqrt[4]{a + iax}} - \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}a} + \frac{i \log\left(1 + \frac{\sqrt{a-iax}}{\sqrt{a+iax}} + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{\sqrt{2}a} \\
 &= \frac{4i(a - iax)^{5/4}}{5a(a + iax)^{5/4}} - \frac{4i\sqrt[4]{a - iax}}{a\sqrt[4]{a + iax}} - \frac{i\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} + \frac{i\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2}\sqrt[4]{a-iax}}{\sqrt[4]{a+iax}}\right)}{a} - \dots
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 70, normalized size = 0.24

$$\frac{i\sqrt[4]{1+ix}(a-iax)^{9/4} {}_2F_1\left(\frac{9}{4}, \frac{9}{4}; \frac{13}{4}; \frac{1}{2} - \frac{ix}{2}\right)}{9\sqrt[4]{2}a^3\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(5/4)/(a + I*a*x)^(9/4), x]

[Out] ((I/9)*(1 + I*x)^(1/4)*(a - I*a*x)^(9/4)*Hypergeometric2F1[9/4, 9/4, 13/4, 1/2 - (I/2)*x])/(2^(1/4)*a^3*(a + I*a*x)^(1/4))

fricas [A] time = 0.49, size = 351, normalized size = 1.18

$$\frac{(5a^2x^2 - 10ia^2x - 5a^2)\sqrt{\frac{4i}{a^2}} \log\left(\frac{(a^2x-ia^2)\sqrt{\frac{4i}{a^2}} + 2(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{1}{4}}}{2x-2i}\right) - (5a^2x^2 - 10ia^2x - 5a^2)\sqrt{\frac{4i}{a^2}} \log\left(-\frac{(a^2x-ia^2)}{\dots}\right)}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(9/4), x, algorithm="fricas")

[Out] ((5*a^2*x^2 - 10*I*a^2*x - 5*a^2)*sqrt(4*I/a^2)*log(((a^2*x - I*a^2)*sqrt(4*I/a^2) + 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4))/(2*x - 2*I)) - (5*a^2*x^2 - 10*I*a^2*x - 5*a^2)*sqrt(4*I/a^2)*log(-((a^2*x - I*a^2)*sqrt(4*I/a^2) - 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4))/(2*x - 2*I)) + (5*a^2*x^2 - 10*I*a^2*x - 5*a^2)*sqrt(-4*I/a^2)*log(((a^2*x - I*a^2)*sqrt(-4*I/a^2) + 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4))/(2*x - 2*I)) - (5*a^2*x^2 - 10*I*a^2*x - 5*a^2)*sqrt(-4*I/a^2)*log(-((a^2*x - I*a^2)*sqrt(-4*I/a^2) - 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4))/(2*x - 2*I)) - (I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)*(48*x - 32*I))/(10*a^2*x^2 - 20*I*a^2*x - 10*a^2)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(9/4), x, algorithm="giac")

[Out] Exception raised: RuntimeError >> An error occurred running a Giac command: INPUT:sage2OUTPUT:ext_reduce Error: Bad Argument Typeintegrate(i/4*a/a^2*(16*((i*a*x+a)^(1/4))^4*(-((i*a*x+a)^(1/4))^4+2*a)^(1/4)-32*a*(-((i*a*x+a)^(1/4))^4+2*a)^(1/4))/((i*a*x+a)^(1/4))^6/4*i*a*((i*a*x+a)^(1/4))^-3,x)

maple [C] time = 0.06, size = 490, normalized size = 1.65

$$\frac{8(3x^2 + ix + 2)(-ix - 1)a^{\frac{1}{4}} \left(\text{RootOf}(_Z^2 + i) \ln \left(\frac{-x^3 - (-x^4 - 2ix^3 - 2ix + 1)^{\frac{1}{4}} x^2 \text{RootOf}(_Z^2 + i) - 2ix^2 - 2i(-x^4 - 2ix^3 - 2ix + 1)^{\frac{1}{4}}}{5(x - i)(ix - 1)((ix + 1)a)^{\frac{1}{4}} a} \right) \right)}{5(x - i)(ix - 1)((ix + 1)a)^{\frac{1}{4}} a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(5/4)/(I*a*x+a)^(9/4), x)

[Out] $\frac{8}{5} \frac{(3x^2 + 2 + Ix)(-ix - 1)a^{\frac{1}{4}} \left(\text{RootOf}(_Z^2 + i) \ln \left(\frac{-x^3 - (-x^4 - 2ix^3 - 2ix + 1)^{\frac{1}{4}} x^2 \text{RootOf}(_Z^2 + i) - 2ix^2 - 2i(-x^4 - 2ix^3 - 2ix + 1)^{\frac{1}{4}}}{5(x - i)(ix - 1)((ix + 1)a)^{\frac{1}{4}} a} \right) \right)}{5(x - i)(ix - 1)((ix + 1)a)^{\frac{1}{4}} a}$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-iax + a)^{\frac{5}{4}}}{(iax + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(5/4)/(a+I*a*x)^(9/4), x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(5/4)/(I*a*x + a)^(9/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a - ax1i)^{5/4}}{(a + ax1i)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a - a*x*1i)^(5/4)/(a + a*x*1i)^(9/4), x)

[Out] int((a - a*x*1i)^(5/4)/(a + a*x*1i)^(9/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-ia(x+i))^{\frac{5}{4}}}{(ia(x-i))^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)**(5/4)/(a+I*a*x)**(9/4),x)

[Out] Integral((-I*a*(x + I))**(5/4)/(I*a*(x - I))**(9/4), x)

$$3.1225 \quad \int \frac{\sqrt[4]{a-iax}}{(a+iax)^{9/4}} dx$$

Optimal. Leaf size=33

$$\frac{2i(a-iax)^{5/4}}{5a^2(a+iax)^{5/4}}$$

[Out] $2/5 * I * (a - I * a * x)^{(5/4)} / a^2 / (a + I * a * x)^{(5/4)}$

Rubi [A] time = 0.00, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.040$, Rules used = {37}

$$\frac{2i(a-iax)^{5/4}}{5a^2(a+iax)^{5/4}}$$

Antiderivative was successfully verified.

[In] Int[(a - I*a*x)^(1/4)/(a + I*a*x)^(9/4), x]

[Out] (((2*I)/5)*(a - I*a*x)^(5/4))/(a^2*(a + I*a*x)^(5/4))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt[4]{a-iax}}{(a+iax)^{9/4}} dx = \frac{2i(a-iax)^{5/4}}{5a^2(a+iax)^{5/4}}$$

Mathematica [A] time = 0.01, size = 33, normalized size = 1.00

$$\frac{2i(a-iax)^{5/4}}{5a^2(a+iax)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a - I*a*x)^(1/4)/(a + I*a*x)^(9/4), x]

[Out] (((2*I)/5)*(a - I*a*x)^(5/4))/(a^2*(a + I*a*x)^(5/4))

fricas [B] time = 0.44, size = 45, normalized size = 1.36

$$\frac{(i a x + a)^{\frac{3}{4}}(-i a x + a)^{\frac{1}{4}}(2 x + 2i)}{5 a^3 x^2 - 10 i a^3 x - 5 a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(9/4),x, algorithm="fricas")

[Out] -(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)*(2*x + 2*I)/(5*a^3*x^2 - 10*I*a^3*x - 5*a^3)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(9/4),x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x)::OUTPUT:

maple [B] time = 0.04, size = 50, normalized size = 1.52

$$\frac{2(-ix-1)a^{\frac{1}{4}}(x^2+2ix-1)}{5(ix-1)((ix+1)a^{\frac{1}{4}}(x-i)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-I*a*x+a)^(1/4)/(I*a*x+a)^(9/4),x)

[Out] 2/5/a^2*(-(I*x-1)*a)^(1/4)/(I*x-1)/((I*x+1)*a)^(1/4)*(2*I*x+x^2-1)/(x-I)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-i a x + a)^{\frac{1}{4}}}{(i a x + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a-I*a*x)^(1/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")

[Out] integrate((-I*a*x + a)^(1/4)/(I*a*x + a)^(9/4), x)

mupad [B] time = 0.55, size = 38, normalized size = 1.15

$$\frac{2(-1 + xi) (-a(-1 + xi))^{1/4}}{5a^2(x - i)(a(1 + xi))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a - a*x*1i)^(1/4)/(a + a*x*1i)^(9/4), x)`

[Out] `-(2*(x*1i - 1)*(-a*(x*1i - 1))^(1/4))/(5*a^2*(x - 1i)*(a*(x*1i + 1))^(1/4))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[4]{-ia(x+i)}}{(ia(x-i))^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a-I*a*x)**(1/4)/(a+I*a*x)**(9/4), x)`

[Out] `Integral((-I*a*(x + I))**(1/4)/(I*a*(x - I))**(9/4), x)`

$$3.1226 \quad \int \frac{1}{(a-iax)^{3/4}(a+iax)^{9/4}} dx$$

Optimal. Leaf size=67

$$\frac{4i\sqrt[4]{a-iax}}{5a^3\sqrt[4]{a+iax}} + \frac{2i\sqrt[4]{a-iax}}{5a^2(a+iax)^{5/4}}$$

[Out] $2/5*I*(a-I*a*x)^{(1/4)}/a^2/(a+I*a*x)^{(5/4)}+4/5*I*(a-I*a*x)^{(1/4)}/a^3/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.01, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$\frac{4i\sqrt[4]{a-iax}}{5a^3\sqrt[4]{a+iax}} + \frac{2i\sqrt[4]{a-iax}}{5a^2(a+iax)^{5/4}}$$

Antiderivative was successfully verified.

[In] `Int[1/((a - I*a*x)^(3/4)*(a + I*a*x)^(9/4)),x]`

[Out] $((2I/5)*(a - I*a*x)^{(1/4)})/(a^2*(a + I*a*x)^{(5/4)}) + ((4I/5)*(a - I*a*x)^{(1/4)})/(a^3*(a + I*a*x)^{(1/4)})$

Rule 37

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]`

Rule 45

`Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])`

Rubi steps

$$\int \frac{1}{(a-iax)^{3/4}(a+iax)^{9/4}} dx = \frac{2i\sqrt[4]{a-iax}}{5a^2(a+iax)^{5/4}} + \frac{2 \int \frac{1}{(a-iax)^{3/4}(a+iax)^{5/4}} dx}{5a}$$

$$= \frac{2i\sqrt[4]{a-iax}}{5a^2(a+iax)^{5/4}} + \frac{4i\sqrt[4]{a-iax}}{5a^3\sqrt[4]{a+iax}}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 0.67

$$\frac{2(3+2ix)\sqrt[4]{a-iax}}{5a^3(x-i)\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(3/4)*(a + I*a*x)^(9/4)), x]

[Out] (2*(3 + (2*I)*x)*(a - I*a*x)^(1/4))/(5*a^3*(-I + x)*(a + I*a*x)^(1/4))

fricas [A] time = 0.46, size = 44, normalized size = 0.66

$$\frac{(iax+a)^{\frac{3}{4}}(-iax+a)^{\frac{1}{4}}(4x-6i)}{5a^4x^2-10ia^4x-5a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(9/4), x, algorithm="fricas")

[Out] (I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)*(4*x - 6*I)/(5*a^4*x^2 - 10*I*a^4*x - 5*a^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{9}{4}}(-iax+a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(9/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(3/4)), x)

maple [A] time = 0.04, size = 44, normalized size = 0.66

$$\frac{\frac{4}{5}x^2 - \frac{2}{5}ix + \frac{6}{5}}{(-ix-1)a^{\frac{3}{4}}((ix+1)a)^{\frac{1}{4}}(x-i)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(3/4)/(I*a*x+a)^(9/4),x)`

[Out] `2/5/a^2/(-(I*x-1)*a)^(3/4)/((I*x+1)*a)^(1/4)*(2*x^2+3-I*x)/(x-I)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{\frac{9}{4}}(-iax+a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(3/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")`

[Out] `integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(3/4)), x)`

mupad [B] time = 0.63, size = 38, normalized size = 0.57

$$\frac{2(3+x2i)(-a(-1+x1i))^{1/4}}{5a^3(x-i)(a(1+x1i))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(3/4)*(a + a*x*1i)^(9/4)),x)`

[Out] `(2*(x*2i + 3)*(-a*(x*1i - 1))^(1/4))/(5*a^3*(x - 1i)*(a*(x*1i + 1))^(1/4))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x-i))^{\frac{9}{4}}(-ia(x+i))^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(3/4)/(a+I*a*x)**(9/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(9/4)*(-I*a*(x + I))**(3/4)), x)`

$$3.1227 \quad \int \frac{1}{(a-iax)^{7/4}(a+iax)^{9/4}} dx$$

Optimal. Leaf size=100

$$\frac{16i\sqrt[4]{a-iax}}{15a^4\sqrt[4]{a+iax}} + \frac{8i\sqrt[4]{a-iax}}{15a^3(a+iax)^{5/4}} - \frac{2i}{3a^2(a+iax)^{5/4}(a-iax)^{3/4}}$$

[Out] $-2/3*I/a^2/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(5/4)}+8/15*I*(a-I*a*x)^{(1/4)}/a^3/(a+I*a*x)^{(5/4)}+16/15*I*(a-I*a*x)^{(1/4)}/a^4/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$\frac{16i\sqrt[4]{a-iax}}{15a^4\sqrt[4]{a+iax}} + \frac{8i\sqrt[4]{a-iax}}{15a^3(a+iax)^{5/4}} - \frac{2i}{3a^2(a+iax)^{5/4}(a-iax)^{3/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(7/4)*(a + I*a*x)^(9/4)), x]

[Out] $((-2*I)/3)/(a^2*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(5/4)}) + (((8*I)/15)*(a - I*a*x)^{(1/4)})/(a^3*(a + I*a*x)^{(5/4)}) + (((16*I)/15)*(a - I*a*x)^{(1/4)})/(a^4*(a + I*a*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a-iax)^{7/4}(a+iax)^{9/4}} dx &= -\frac{2i}{3a^2(a-iax)^{3/4}(a+iax)^{5/4}} + \frac{4 \int \frac{1}{(a-iax)^{3/4}(a+iax)^{9/4}} dx}{3a} \\
&= -\frac{2i}{3a^2(a-iax)^{3/4}(a+iax)^{5/4}} + \frac{8i\sqrt[4]{a-iax}}{15a^3(a+iax)^{5/4}} + \frac{8 \int \frac{1}{(a-iax)^{3/4}(a+iax)^{5/4}} dx}{15a^2} \\
&= -\frac{2i}{3a^2(a-iax)^{3/4}(a+iax)^{5/4}} + \frac{8i\sqrt[4]{a-iax}}{15a^3(a+iax)^{5/4}} + \frac{16i\sqrt[4]{a-iax}}{15a^4\sqrt[4]{a+iax}}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 50, normalized size = 0.50

$$\frac{2(8x^2 - 4ix + 7)}{15a^3(x-i)(a-iax)^{3/4}\sqrt[4]{a+iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(7/4)*(a + I*a*x)^(9/4)), x]

[Out] (2*(7 - (4*I)*x + 8*x^2))/(15*a^3*(-I + x)*(a - I*a*x)^(3/4)*(a + I*a*x)^(1/4))

fricas [A] time = 0.46, size = 58, normalized size = 0.58

$$\frac{2(iax+a)^{3/4}(-iax+a)^{1/4}(8x^2-4ix+7)}{15a^5x^3-15ia^5x^2+15a^5x-15ia^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(9/4), x, algorithm="fricas")

[Out] 2*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)*(8*x^2 - 4*I*x + 7)/(15*a^5*x^3 - 15*I*a^5*x^2 + 15*a^5*x - 15*I*a^5)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax+a)^{9/4}(-iax+a)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(9/4), x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(7/4)), x)

maple [A] time = 0.06, size = 44, normalized size = 0.44

$$\frac{\frac{16}{15}x^2 - \frac{8}{15}ix + \frac{14}{15}}{(-ix - 1)a^{\frac{3}{4}}((ix + 1)a)^{\frac{1}{4}}(x - i)a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-I*a*x+a)^(7/4)/(I*a*x+a)^(9/4),x)`

[Out] `2/15/a^3/(-I*x-1)*a^(3/4)/((I*x+1)*a)^(1/4)*(8*x^2-4*I*x+7)/(x-I)`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)^(7/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: THROW: The catch RAT-ERR is undefined.

mupad [B] time = 0.53, size = 45, normalized size = 0.45

$$\frac{2(-a(-1 + x1i))^{1/4}(x^2 8i + 4x + 7i)}{15a^4(x^2 + 1)(a(1 + x1i))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - a*x*1i)^(7/4)*(a + a*x*1i)^(9/4)),x)`

[Out] `(2*(-a*(x*1i - 1))^(1/4)*(4*x + x^2*8i + 7i))/(15*a^4*(x^2 + 1)*(a*(x*1i + 1))^(1/4))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ia(x - i))^{\frac{9}{4}}(-ia(x + i))^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(a-I*a*x)**(7/4)/(a+I*a*x)**(9/4),x)`

[Out] `Integral(1/((I*a*(x - I))**(9/4)*(-I*a*(x + I))**(7/4)), x)`

$$3.1228 \quad \int \frac{1}{(a-iax)^{11/4}(a+iax)^{9/4}} dx$$

Optimal. Leaf size=133

$$\frac{32i\sqrt[4]{a-iax}}{35a^5\sqrt[4]{a+iax}} + \frac{16i\sqrt[4]{a-iax}}{35a^4(a+iax)^{5/4}} - \frac{4i}{7a^3(a+iax)^{5/4}(a-iax)^{3/4}} - \frac{2i}{7a^2(a+iax)^{5/4}(a-iax)^{7/4}}$$

[Out] $-2/7*I/a^2/(a-I*a*x)^{(7/4)}/(a+I*a*x)^{(5/4)}-4/7*I/a^3/(a-I*a*x)^{(3/4)}/(a+I*a*x)^{(5/4)}+16/35*I*(a-I*a*x)^{(1/4)}/a^4/(a+I*a*x)^{(5/4)}+32/35*I*(a-I*a*x)^{(1/4)}/a^5/(a+I*a*x)^{(1/4)}$

Rubi [A] time = 0.03, antiderivative size = 133, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 25, $\frac{\text{number of rules}}{\text{integrand size}} = 0.080$, Rules used = {45, 37}

$$\frac{32i\sqrt[4]{a-iax}}{35a^5\sqrt[4]{a+iax}} + \frac{16i\sqrt[4]{a-iax}}{35a^4(a+iax)^{5/4}} - \frac{4i}{7a^3(a+iax)^{5/4}(a-iax)^{3/4}} - \frac{2i}{7a^2(a+iax)^{5/4}(a-iax)^{7/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((a - I*a*x)^(11/4)*(a + I*a*x)^(9/4)), x]

[Out] $((-2*I)/7)/(a^2*(a - I*a*x)^{(7/4)}*(a + I*a*x)^{(5/4)}) - ((4*I)/7)/(a^3*(a - I*a*x)^{(3/4)}*(a + I*a*x)^{(5/4)}) + (((16*I)/35)*(a - I*a*x)^{(1/4)})/(a^4*(a + I*a*x)^{(5/4)}) + (((32*I)/35)*(a - I*a*x)^{(1/4)})/(a^5*(a + I*a*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a-iax)^{11/4}(a+iax)^{9/4}} dx &= -\frac{2i}{7a^2(a-iax)^{7/4}(a+iax)^{5/4}} + \frac{6 \int \frac{1}{(a-iax)^{7/4}(a+iax)^{9/4}} dx}{7a} \\
&= -\frac{2i}{7a^2(a-iax)^{7/4}(a+iax)^{5/4}} - \frac{4i}{7a^3(a-iax)^{3/4}(a+iax)^{5/4}} + \frac{8 \int \frac{1}{(a-iax)^{3/4}(a+iax)^{9/4}}}{7a^2} \\
&= -\frac{2i}{7a^2(a-iax)^{7/4}(a+iax)^{5/4}} - \frac{4i}{7a^3(a-iax)^{3/4}(a+iax)^{5/4}} + \frac{16i\sqrt[4]{a-iax}}{35a^4(a+iax)^{5/4}} + \\
&= -\frac{2i}{7a^2(a-iax)^{7/4}(a+iax)^{5/4}} - \frac{4i}{7a^3(a-iax)^{3/4}(a+iax)^{5/4}} + \frac{16i\sqrt[4]{a-iax}}{35a^4(a+iax)^{5/4}} +
\end{aligned}$$

Mathematica [A] time = 0.03, size = 57, normalized size = 0.43

$$\frac{2(16x^3 + 8ix^2 + 22x + 9i)}{35a^4(x^2 + 1)(a - iax)^{3/4}\sqrt[4]{a + iax}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a - I*a*x)^(11/4)*(a + I*a*x)^(9/4)), x]

[Out] (2*(9*I + 22*x + (8*I)*x^2 + 16*x^3))/(35*a^4*(a - I*a*x)^(3/4)*(a + I*a*x)^(1/4)*(1 + x^2))

fricas [A] time = 0.44, size = 54, normalized size = 0.41

$$\frac{(32x^3 + 16ix^2 + 44x + 18i)(iax + a)^{\frac{3}{4}}(-iax + a)^{\frac{1}{4}}}{35(a^6x^4 + 2a^6x^2 + a^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(9/4), x, algorithm="fricas")

[Out] 1/35*(32*x^3 + 16*I*x^2 + 44*x + 18*I)*(I*a*x + a)^(3/4)*(-I*a*x + a)^(1/4)/(a^6*x^4 + 2*a^6*x^2 + a^6)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{9}{4}}(-iax + a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(9/4),x, algorithm="giac")

[Out] integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(11/4)), x)

maple [A] time = 0.06, size = 56, normalized size = 0.42

$$\frac{\frac{32}{35}x^3 + \frac{16}{35}ix^2 + \frac{44}{35}x + \frac{18}{35}i}{(-ix - 1)a^{\frac{3}{4}}((ix + 1)a)^{\frac{1}{4}}(x - i)(x + i)a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-I*a*x+a)^(11/4)/(I*a*x+a)^(9/4),x)

[Out] 2/35/a^4/(-I*x-1)*a^(3/4)/((I*x+1)*a)^(1/4)*(16*x^3+8*I*x^2+22*x+9*I)/(x-I)/(x+I)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(iax + a)^{\frac{9}{4}}(-iax + a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)^(11/4)/(a+I*a*x)^(9/4),x, algorithm="maxima")

[Out] integrate(1/((I*a*x + a)^(9/4)*(-I*a*x + a)^(11/4)), x)

mupad [B] time = 0.69, size = 56, normalized size = 0.42

$$\frac{2(-a(-1 + x1i))^{1/4}(x^4 16i + 8x^3 + x^2 30i + 13x + 9i)}{35a^5(x^2 + 1)^2(a(1 + x1i))^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a - a*x*1i)^(11/4)*(a + a*x*1i)^(9/4)),x)

[Out] (2*(-a*(x*1i - 1))^(1/4)*(13*x + x^2*30i + 8*x^3 + x^4*16i + 9i))/(35*a^5*(x^2 + 1)^2*(a*(x*1i + 1))^(1/4))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a-I*a*x)**(11/4)/(a+I*a*x)**(9/4),x)

[Out] Timed out

3.1229 $\int (a + bx)^2 (ac - bcx)^n dx$

Optimal. Leaf size=83

$$-\frac{4a^2(ac - bcx)^{n+1}}{bc(n+1)} - \frac{(ac - bcx)^{n+3}}{bc^3(n+3)} + \frac{4a(ac - bcx)^{n+2}}{bc^2(n+2)}$$

[Out] $-4*a^2*(-b*c*x+a*c)^{(1+n)}/b/c/(1+n)+4*a*(-b*c*x+a*c)^{(2+n)}/b/c^2/(2+n)-(-b*c*x+a*c)^{(3+n)}/b/c^3/(3+n)$

Rubi [A] time = 0.03, antiderivative size = 83, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {43}

$$-\frac{4a^2(ac - bcx)^{n+1}}{bc(n+1)} + \frac{4a(ac - bcx)^{n+2}}{bc^2(n+2)} - \frac{(ac - bcx)^{n+3}}{bc^3(n+3)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(a*c - b*c*x)^n, x]

[Out] $(-4*a^2*(a*c - b*c*x)^{(1+n)}/(b*c*(1+n)) + (4*a*(a*c - b*c*x)^{(2+n)}/(b*c^2*(2+n)) - (a*c - b*c*x)^{(3+n)}/(b*c^3*(3+n)))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2 (ac - bcx)^n dx &= \int \left(4a^2 (ac - bcx)^n - \frac{4a(ac - bcx)^{1+n}}{c} + \frac{(ac - bcx)^{2+n}}{c^2} \right) dx \\ &= -\frac{4a^2(ac - bcx)^{1+n}}{bc(1+n)} + \frac{4a(ac - bcx)^{2+n}}{bc^2(2+n)} - \frac{(ac - bcx)^{3+n}}{bc^3(3+n)} \end{aligned}$$

Mathematica [A] time = 0.04, size = 77, normalized size = 0.93

$$\frac{(bx - a) \left(a^2 (n^2 + 7n + 14) + 2ab (n^2 + 5n + 4)x + b^2 (n^2 + 3n + 2)x^2 \right) (c(a - bx))^n}{b(n+1)(n+2)(n+3)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(a*c - b*c*x)^n,x]

[Out] ((c*(a - b*x))^n*(-a + b*x)*(a^2*(14 + 7*n + n^2) + 2*a*b*(4 + 5*n + n^2)*x + b^2*(2 + 3*n + n^2)*x^2))/(b*(1 + n)*(2 + n)*(3 + n))

fricas [A] time = 0.46, size = 128, normalized size = 1.54

$$\frac{(a^3n^2 + 7a^3n - (b^3n^2 + 3b^3n + 2b^3)x^3 + 14a^3 - (ab^2n^2 + 7ab^2n + 6ab^2)x^2 + (a^2bn^2 + 3a^2bn - 6a^2b)x)(-bcx + ac)^n}{bn^3 + 6bn^2 + 11bn + 6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c)^n,x, algorithm="fricas")

[Out] -(a^3*n^2 + 7*a^3*n - (b^3*n^2 + 3*b^3*n + 2*b^3)*x^3 + 14*a^3 - (a*b^2*n^2 + 7*a*b^2*n + 6*a*b^2)*x^2 + (a^2*b*n^2 + 3*a^2*b*n - 6*a^2*b)*x)*(-b*c*x + a*c)^n/(b*n^3 + 6*b*n^2 + 11*b*n + 6*b)

giac [B] time = 1.15, size = 256, normalized size = 3.08

$$\frac{(-bcx + ac)^n b^3 n^2 x^3 + (-bcx + ac)^n ab^2 n^2 x^2 + 3(-bcx + ac)^n b^3 n x^3 - (-bcx + ac)^n a^2 b n^2 x + 7(-bcx + ac)^n ab^2 n x^2}{bn^3 + 6bn^2 + 11bn + 6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c)^n,x, algorithm="giac")

[Out] ((-b*c*x + a*c)^n*b^3*n^2*x^3 + (-b*c*x + a*c)^n*a*b^2*n^2*x^2 + 3*(-b*c*x + a*c)^n*b^3*n*x^3 - (-b*c*x + a*c)^n*a^2*b*n^2*x + 7*(-b*c*x + a*c)^n*a*b^2*n*x^2 + 2*(-b*c*x + a*c)^n*b^3*x^3 - (-b*c*x + a*c)^n*a^3*n^2 - 3*(-b*c*x + a*c)^n*a^2*b*n*x + 6*(-b*c*x + a*c)^n*a*b^2*x^2 - 7*(-b*c*x + a*c)^n*a^3*n + 6*(-b*c*x + a*c)^n*a^2*b*x - 14*(-b*c*x + a*c)^n*a^3)/(b*n^3 + 6*b*n^2 + 11*b*n + 6*b)

maple [A] time = 0.01, size = 103, normalized size = 1.24

$$\frac{(-bx + a)(b^2n^2x^2 + 2abn^2x + 3b^2nx^2 + a^2n^2 + 10abnx + 2b^2x^2 + 7a^2n + 8abx + 14a^2)(-bcx + ac)^n}{(n^3 + 6n^2 + 11n + 6)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(-b*c*x+a*c)^n,x)

[Out] -(b*x+a)*(b^2*n^2*x^2+2*a*b*n^2*x+3*b^2*n*x^2+a^2*n^2+10*a*b*n*x+2*b^2*x^2+7*a^2*n+8*a*b*x+14*a^2)*(-b*c*x+a*c)^n/b/(n^3+6*n^2+11*n+6)

maxima [B] time = 1.53, size = 167, normalized size = 2.01

$$\frac{2(b^2c^n(n+1)x^2 - abc^nnx - a^2c^n)(-bx+a)^na}{(n^2+3n+2)b} + \frac{((n^2+3n+2)b^3c^nx^3 - (n^2+n)ab^2c^nx^2 - 2a^2bc^nnx - 2a^3c^n)}{(n^3+6n^2+11n+6)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(-b*c*x+a*c)^n,x, algorithm="maxima")

[Out] 2*(b^2*c^n*(n+1)*x^2 - a*b*c^n*n*x - a^2*c^n)*(-b*x+a)^n*a/((n^2+3*n+2)*b) + ((n^2+3*n+2)*b^3*c^n*x^3 - (n^2+n)*a*b^2*c^n*x^2 - 2*a^2*b*c^n*n*x - 2*a^3*c^n)*(-b*x+a)^n/((n^3+6*n^2+11*n+6)*b) - (-b*c*x+a*c)^(n+1)*a^2/(b*c*(n+1))

mupad [B] time = 0.49, size = 133, normalized size = 1.60

$$-(ac-bcx)^n \left(\frac{a^2x(n^2+3n-6)}{n^3+6n^2+11n+6} + \frac{a^3(n^2+7n+14)}{b(n^3+6n^2+11n+6)} - \frac{b^2x^3(n^2+3n+2)}{n^3+6n^2+11n+6} - \frac{abx^2(n^2+7n+6)}{n^3+6n^2+11n+6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c - b*c*x)^n*(a + b*x)^2,x)

[Out] -(a*c - b*c*x)^n*((a^2*x*(3*n + n^2 - 6))/(11*n + 6*n^2 + n^3 + 6) + (a^3*(7*n + n^2 + 14))/(b*(11*n + 6*n^2 + n^3 + 6)) - (b^2*x^3*(3*n + n^2 + 2))/(11*n + 6*n^2 + n^3 + 6) - (a*b*x^2*(7*n + n^2 + 6))/(11*n + 6*n^2 + n^3 + 6))

sympy [A] time = 1.30, size = 819, normalized size = 9.87

$$\left\{ \begin{array}{l} a^2x(ac)^n \\ -\frac{a^2\log\left(-\frac{a}{b}+x\right)}{a^2bc^3-2ab^2c^3x+b^3c^3x^2} - \frac{2a^2}{a^2bc^3-2ab^2c^3x+b^3c^3x^2} + \frac{2abx\log\left(-\frac{a}{b}+x\right)}{a^2bc^3-2ab^2c^3x+b^3c^3x^2} + \frac{4abx}{a^2bc^3-2ab^2c^3x+b^3c^3x^2} - \frac{b^2x^2\log\left(-\frac{a}{b}+x\right)}{a^2bc^3-2ab^2c^3x+b^3c^3x^2} \\ -\frac{4a^2\log\left(-\frac{a}{b}+x\right)}{-abc^2+b^2c^2x} - \frac{5a^2}{-abc^2+b^2c^2x} + \frac{4abx\log\left(-\frac{a}{b}+x\right)}{-abc^2+b^2c^2x} + \frac{b^2x^2}{-abc^2+b^2c^2x} \\ -\frac{4a^2\log\left(-\frac{a}{b}+x\right)}{bc} - \frac{3ax}{c} - \frac{bx^2}{2c} \\ -\frac{a^3n^2(ac-bcx)^n}{bn^3+6bn^2+11bn+6b} - \frac{7a^3n(ac-bcx)^n}{bn^3+6bn^2+11bn+6b} - \frac{14a^3(ac-bcx)^n}{bn^3+6bn^2+11bn+6b} - \frac{a^2bn^2x(ac-bcx)^n}{bn^3+6bn^2+11bn+6b} - \frac{3a^2bnx(ac-bcx)^n}{bn^3+6bn^2+11bn+6b} + \frac{6a^2bx(ac-bcx)^n}{bn^3+6bn^2+11bn+6b} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2*(-b*c*x+a*c)**n,x)

```
[Out] Piecewise((a**2*x*(a*c)**n, Eq(b, 0)), (-a**2*log(-a/b + x)/(a**2*b*c**3 -
2*a*b**2*c**3*x + b**3*c**3*x**2) - 2*a**2/(a**2*b*c**3 - 2*a*b**2*c**3*x +
b**3*c**3*x**2) + 2*a*b*x*log(-a/b + x)/(a**2*b*c**3 - 2*a*b**2*c**3*x + b
**3*c**3*x**2) + 4*a*b*x/(a**2*b*c**3 - 2*a*b**2*c**3*x + b**3*c**3*x**2) -
b**2*x**2*log(-a/b + x)/(a**2*b*c**3 - 2*a*b**2*c**3*x + b**3*c**3*x**2),
Eq(n, -3)), (-4*a**2*log(-a/b + x)/(-a*b*c**2 + b**2*c**2*x) - 5*a**2/(-a*b
*c**2 + b**2*c**2*x) + 4*a*b*x*log(-a/b + x)/(-a*b*c**2 + b**2*c**2*x) + b
**2*x**2/(-a*b*c**2 + b**2*c**2*x), Eq(n, -2)), (-4*a**2*log(-a/b + x)/(b*c)
- 3*a*x/c - b*x**2/(2*c), Eq(n, -1)), (-a**3*n**2*(a*c - b*c*x)**n/(b*n**3
+ 6*b*n**2 + 11*b*n + 6*b) - 7*a**3*n*(a*c - b*c*x)**n/(b*n**3 + 6*b*n**2
+ 11*b*n + 6*b) - 14*a**3*(a*c - b*c*x)**n/(b*n**3 + 6*b*n**2 + 11*b*n + 6*
b) - a**2*b*n**2*x*(a*c - b*c*x)**n/(b*n**3 + 6*b*n**2 + 11*b*n + 6*b) - 3*
a**2*b*n*x*(a*c - b*c*x)**n/(b*n**3 + 6*b*n**2 + 11*b*n + 6*b) + 6*a**2*b*x
*(a*c - b*c*x)**n/(b*n**3 + 6*b*n**2 + 11*b*n + 6*b) + a*b**2*n**2*x**2*(a*
c - b*c*x)**n/(b*n**3 + 6*b*n**2 + 11*b*n + 6*b) + 7*a*b**2*n*x**2*(a*c - b
*c*x)**n/(b*n**3 + 6*b*n**2 + 11*b*n + 6*b) + 6*a*b**2*x**2*(a*c - b*c*x)**
n/(b*n**3 + 6*b*n**2 + 11*b*n + 6*b) + b**3*n**2*x**3*(a*c - b*c*x)**n/(b*n
**3 + 6*b*n**2 + 11*b*n + 6*b) + 3*b**3*n*x**3*(a*c - b*c*x)**n/(b*n**3 + 6
*b*n**2 + 11*b*n + 6*b) + 2*b**3*x**3*(a*c - b*c*x)**n/(b*n**3 + 6*b*n**2 +
11*b*n + 6*b), True))
```

3.1230 $\int (a + bx)(ac - bcx)^n dx$

Optimal. Leaf size=53

$$\frac{(ac - bcx)^{n+2}}{bc^2(n+2)} - \frac{2a(ac - bcx)^{n+1}}{bc(n+1)}$$

[Out] $-2*a*(-b*c*x+a*c)^{(1+n)}/b/c/(1+n)+(-b*c*x+a*c)^{(2+n)}/b/c^2/(2+n)$

Rubi [A] time = 0.02, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{(ac - bcx)^{n+2}}{bc^2(n+2)} - \frac{2a(ac - bcx)^{n+1}}{bc(n+1)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(a*c - b*c*x)^n,x]

[Out] $(-2*a*(a*c - b*c*x)^{(1+n)}/(b*c*(1+n)) + (a*c - b*c*x)^{(2+n)}/(b*c^2*(2+n)))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)(ac - bcx)^n dx &= \int \left(2a(ac - bcx)^n - \frac{(ac - bcx)^{1+n}}{c} \right) dx \\ &= -\frac{2a(ac - bcx)^{1+n}}{bc(1+n)} + \frac{(ac - bcx)^{2+n}}{bc^2(2+n)} \end{aligned}$$

Mathematica [A] time = 0.02, size = 43, normalized size = 0.81

$$\frac{(bx - a)(a(n + 3) + b(n + 1)x)(c(a - bx))^n}{b(n + 1)(n + 2)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(a*c - b*c*x)^n,x]

[Out] $((c*(a - b*x))^n*(-a + b*x)*(a*(3 + n) + b*(1 + n)*x))/(b*(1 + n)*(2 + n))$

fricas [A] time = 0.47, size = 58, normalized size = 1.09

$$\frac{(a^2n - 2abx - (b^2n + b^2)x^2 + 3a^2)(-bcx + ac)^n}{bn^2 + 3bn + 2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)^n,x, algorithm="fricas")`

[Out] $-(a^2n - 2a*b*x - (b^2n + b^2)*x^2 + 3*a^2)*(-b*c*x + a*c)^n/(b*n^2 + 3*b*n + 2*b)$

giac [A] time = 1.05, size = 103, normalized size = 1.94

$$\frac{(-bcx + ac)^n b^2 n x^2 + (-bcx + ac)^n b^2 x^2 - (-bcx + ac)^n a^2 n + 2(-bcx + ac)^n abx - 3(-bcx + ac)^n a^2}{bn^2 + 3bn + 2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)^n,x, algorithm="giac")`

[Out] $((-b*c*x + a*c)^n*b^2*n*x^2 + (-b*c*x + a*c)^n*b^2*x^2 - (-b*c*x + a*c)^n*a^2*n + 2*(-b*c*x + a*c)^n*a*b*x - 3*(-b*c*x + a*c)^n*a^2)/(b*n^2 + 3*b*n + 2*b)$

maple [A] time = 0.00, size = 47, normalized size = 0.89

$$\frac{(bnx + an + bx + 3a)(-bx + a)(-bcx + ac)^n}{(n^2 + 3n + 2)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)*(-b*c*x+a*c)^n,x)`

[Out] $-(-b*c*x+a*c)^n*(b*n*x+a*n+b*x+3*a)*(-b*x+a)/b/(n^2+3*n+2)$

maxima [A] time = 1.40, size = 81, normalized size = 1.53

$$\frac{(b^2c^n(n+1)x^2 - abc^n nx - a^2c^n)(-bx + a)^n}{(n^2 + 3n + 2)b} - \frac{(-bcx + ac)^{n+1}a}{bc(n+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)^n,x, algorithm="maxima")`

[Out] $(b^2*c^n*(n+1)*x^2 - a*b*c^n*n*x - a^2*c^n)*(-b*x + a)^n/((n^2 + 3*n + 2)*b) - (-b*c*x + a*c)^{(n+1)}*a/(b*c*(n+1))$

mupad [B] time = 0.32, size = 66, normalized size = 1.25

$$(ac - bcx)^n \left(\frac{2ax}{n^2 + 3n + 2} - \frac{a^2(n+3)}{b(n^2 + 3n + 2)} + \frac{bx^2(n+1)}{n^2 + 3n + 2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c - b*c*x)^n*(a + b*x), x)`

[Out] $(a*c - b*c*x)^n*((2*a*x)/(3*n + n^2 + 2) - (a^2*(n + 3))/(b*(3*n + n^2 + 2)) + (b*x^2*(n + 1))/(3*n + n^2 + 2))$

sympy [A] time = 0.70, size = 245, normalized size = 4.62

$$\begin{cases} ax(ac)^n & \text{for } b = 0 \\ \frac{a \log\left(-\frac{a}{b} + x\right)}{-abc^2 + b^2c^2x} - \frac{2a}{-abc^2 + b^2c^2x} + \frac{bx \log\left(-\frac{a}{b} + x\right)}{-abc^2 + b^2c^2x} & \text{for } n = -2 \\ \frac{2a \log\left(-\frac{a}{b} + x\right)}{bc} - \frac{x}{c} & \text{for } n = -1 \\ \frac{a^2n(ac-bcx)^n}{bn^2+3bn+2b} - \frac{3a^2(ac-bcx)^n}{bn^2+3bn+2b} + \frac{2abx(ac-bcx)^n}{bn^2+3bn+2b} + \frac{b^2nx^2(ac-bcx)^n}{bn^2+3bn+2b} + \frac{b^2x^2(ac-bcx)^n}{bn^2+3bn+2b} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(-b*c*x+a*c)**n, x)`

[Out] `Piecewise((a*x*(a*c)**n, Eq(b, 0)), (-a*log(-a/b + x)/(-a*b*c**2 + b**2*c**2*x) - 2*a/(-a*b*c**2 + b**2*c**2*x) + b*x*log(-a/b + x)/(-a*b*c**2 + b**2*c**2*x), Eq(n, -2)), (-2*a*log(-a/b + x)/(b*c) - x/c, Eq(n, -1)), (-a**2*n*(a*c - b*c*x)**n/(b*n**2 + 3*b*n + 2*b) - 3*a**2*(a*c - b*c*x)**n/(b*n**2 + 3*b*n + 2*b) + 2*a*b*x*(a*c - b*c*x)**n/(b*n**2 + 3*b*n + 2*b) + b**2*n*x**2*(a*c - b*c*x)**n/(b*n**2 + 3*b*n + 2*b) + b**2*x**2*(a*c - b*c*x)**n/(b*n**2 + 3*b*n + 2*b), True))`

$$3.1231 \quad \int \frac{(ac-bcx)^n}{a+bx} dx$$

Optimal. Leaf size=52

$$\frac{(ac-bcx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{a-bx}{2a}\right)}{2abc(n+1)}$$

[Out] -1/2*(-b*c*x+a*c)^(1+n)*hypergeom([1, 1+n], [2+n], 1/2*(-b*x+a)/a)/a/b/c/(1+n)

Rubi [A] time = 0.01, antiderivative size = 52, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {68}

$$\frac{(ac-bcx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{a-bx}{2a}\right)}{2abc(n+1)}$$

Antiderivative was successfully verified.

[In] Int[(a*c - b*c*x)^n/(a + b*x), x]

[Out] -((a*c - b*c*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, (a - b*x)/(2*a)])/ (2*a*b*c*(1 + n))

Rule 68

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((b*c - a*d)^n*(a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b^(n + 1)*(m + 1)), x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && IntegerQ[n]

Rubi steps

$$\int \frac{(ac-bcx)^n}{a+bx} dx = -\frac{(ac-bcx)^{1+n} {}_2F_1\left(1, 1+n; 2+n; \frac{a-bx}{2a}\right)}{2abc(1+n)}$$

Mathematica [A] time = 0.01, size = 52, normalized size = 1.00

$$-\frac{(a-bx)(c(a-bx))^n {}_2F_1\left(1, n+1; n+2; \frac{a-bx}{2a}\right)}{2ab(n+1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a*c - b*c*x)^n/(a + b*x),x]

[Out] $-1/2*((a - b*x)*(c*(a - b*x))^n*Hypergeometric2F1[1, 1 + n, 2 + n, (a - b*x)/(2*a)])/(a*b*(1 + n))$

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(-bcx + ac)^n}{bx + a}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^n/(b*x+a),x, algorithm="fricas")

[Out] integral((-b*c*x + a*c)^n/(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-bcx + ac)^n}{bx + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^n/(b*x+a),x, algorithm="giac")

[Out] integrate((-b*c*x + a*c)^n/(b*x + a), x)

maple [F] time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{(-bcx + ac)^n}{bx + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*c*x+a*c)^n/(b*x+a),x)

[Out] int((-b*c*x+a*c)^n/(b*x+a),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-bcx + ac)^n}{bx + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^n/(b*x+a),x, algorithm="maxima")

[Out] integrate((-b*c*x + a*c)^n/(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(ac - bcx)^n}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c - b*c*x)^n/(a + b*x), x)

[Out] int((a*c - b*c*x)^n/(a + b*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-c(-a + bx))^n}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)**n/(b*x+a), x)

[Out] Integral((-c*(-a + b*x))**n/(a + b*x), x)

$$3.1232 \quad \int \frac{(ac-bcx)^n}{(a+bx)^2} dx$$

Optimal. Leaf size=52

$$-\frac{(ac-bcx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{a-bx}{2a}\right)}{4a^2bc(n+1)}$$

[Out] $-1/4*(-b*c*x+a*c)^{(1+n)}*\text{hypergeom}([2, 1+n], [2+n], 1/2*(-b*x+a)/a)/a^2/b/c/(1+n)$

Rubi [A] time = 0.01, antiderivative size = 52, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {68}

$$-\frac{(ac-bcx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{a-bx}{2a}\right)}{4a^2bc(n+1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a*c - b*c*x)^n/(a + b*x)^2, x]$

[Out] $-((a*c - b*c*x)^{(1+n)}*\text{Hypergeometric2F1}[2, 1+n, 2+n, (a-b*x)/(2*a)])/(4*a^2*b*c*(1+n))$

Rule 68

$\text{Int}[(a_+ + (b_+)*(x_+))^{(m_+)}*((c_+ + (d_+)*(x_+))^{(n_+)}, x_Symbol] \rightarrow \text{Simp}[(b*c - a*d)^n*(a + b*x)^{(m+1)}*\text{Hypergeometric2F1}[-n, m+1, m+2, -((d*(a + b*x))/(b*c - a*d))]/(b^{(n+1)}*(m+1)), x] /;$ FreeQ[{a, b, c, d, m}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && IntegerQ[n]

Rubi steps

$$\int \frac{(ac-bcx)^n}{(a+bx)^2} dx = -\frac{(ac-bcx)^{1+n} {}_2F_1\left(2, 1+n; 2+n; \frac{a-bx}{2a}\right)}{4a^2bc(1+n)}$$

Mathematica [A] time = 0.01, size = 52, normalized size = 1.00

$$-\frac{(a-bx)(c(a-bx))^n {}_2F_1\left(2, n+1; n+2; \frac{a-bx}{2a}\right)}{4a^2b(n+1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a*c - b*c*x)^n/(a + b*x)^2,x]

[Out] -1/4*((a - b*x)*(c*(a - b*x))^n*Hypergeometric2F1[2, 1 + n, 2 + n, (a - b*x)/(2*a)])/(a^2*b*(1 + n))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(-bcx + ac)^n}{b^2x^2 + 2abx + a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^n/(b*x+a)^2,x, algorithm="fricas")

[Out] integral((-b*c*x + a*c)^n/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-bcx + ac)^n}{(bx + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^n/(b*x+a)^2,x, algorithm="giac")

[Out] integrate((-b*c*x + a*c)^n/(b*x + a)^2, x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(-bcx + ac)^n}{(bx + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-b*c*x+a*c)^n/(b*x+a)^2,x)

[Out] int((-b*c*x+a*c)^n/(b*x+a)^2,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-bcx + ac)^n}{(bx + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)^n/(b*x+a)^2,x, algorithm="maxima")

[Out] integrate((-b*c*x + a*c)^n/(b*x + a)^2, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a c - b c x)^n}{(a + b x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c - b*c*x)^n/(a + b*x)^2,x)

[Out] int((a*c - b*c*x)^n/(a + b*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-c(-a + b x))^n}{(a + b x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-b*c*x+a*c)**n/(b*x+a)**2,x)

[Out] Integral((-c*(-a + b*x))**n/(a + b*x)**2, x)

3.1233 $\int (a + ax)^m (c - cx)^m dx$

Optimal. Leaf size=41

$$x(1-x^2)^{-m} (ax+a)^m (c-cx)^m {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; x^2\right)$$

[Out] x*(a*x+a)^m*(-c*x+c)^m*hypergeom([1/2, -m], [3/2], x^2)/((-x^2+1)^m)

Rubi [A] time = 0.01, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {42, 246, 245}

$$x(1-x^2)^{-m} (ax+a)^m (c-cx)^m {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; x^2\right)$$

Antiderivative was successfully verified.

[In] Int[(a + a*x)^m*(c - c*x)^m,x]

[Out] (x*(a + a*x)^m*(c - c*x)^m*Hypergeometric2F1[1/2, -m, 3/2, x^2])/(1 - x^2)^m

Rule 42

Int[((a_) + (b_.)*(x_)^(m_))*((c_) + (d_.)*(x_)^(m_)), x_Symbol] := Dist[((a + b*x)^FracPart[m]*(c + d*x)^FracPart[m])/(a*c + b*d*x^2)^FracPart[m], Int[(a*c + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && !IntegerQ[2*m]

Rule 245

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Simp[a^p*x*Hypergeometric2F1[-p, 1/n, 1/n + 1, -(b*x^n)/a], x] /; FreeQ[{a, b, n, p}, x] && !IGtQ[p, 0] && !IntegerQ[1/n] && !ILtQ[Simplify[1/n + p], 0] && (IntegerQ[p] || GtQ[a, 0])

Rule 246

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[(a^IntPart[p]*(a + b*x^n)^FracPart[p])/(1 + (b*x^n)/a)^FracPart[p], Int[(1 + (b*x^n)/a)^p, x], x] /; FreeQ[{a, b, n, p}, x] && !IGtQ[p, 0] && !IntegerQ[1/n] && !ILtQ[Simplify[1/n + p], 0] && !(IntegerQ[p] || GtQ[a, 0])

Rubi steps

$$\begin{aligned}
\int (a + ax)^m (c - cx)^m dx &= \left((a + ax)^m (c - cx)^m (ac - acx^2)^{-m} \right) \int (ac - acx^2)^m dx \\
&= \left((a + ax)^m (c - cx)^m (1 - x^2)^{-m} \right) \int (1 - x^2)^m dx \\
&= x(a + ax)^m (c - cx)^m (1 - x^2)^{-m} {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; x^2\right)
\end{aligned}$$

Mathematica [A] time = 0.02, size = 53, normalized size = 1.29

$$\frac{2^m (x-1)(x+1)^{-m} (a(x+1))^m (c-cx)^m {}_2F_1\left(-m, m+1; m+2; \frac{1}{2} - \frac{x}{2}\right)}{m+1}$$

Antiderivative was successfully verified.

[In] Integrate[(a + a*x)^m*(c - c*x)^m,x]

[Out] (2^m*(-1 + x)*(a*(1 + x))^m*(c - c*x)^m*Hypergeometric2F1[-m, 1 + m, 2 + m, 1/2 - x/2])/((1 + m)*(1 + x)^m)

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left((ax + a)^m (-cx + c)^m, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+a)^m*(-c*x+c)^m,x, algorithm="fricas")

[Out] integral((a*x + a)^m*(-c*x + c)^m, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (ax + a)^m (-cx + c)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a*x+a)^m*(-c*x+c)^m,x, algorithm="giac")

[Out] integrate((a*x + a)^m*(-c*x + c)^m, x)

maple [F] time = 0.12, size = 0, normalized size = 0.00

$$\int (ax + a)^m (-cx + c)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*x+a)^m*(-c*x+c)^m,x)`

[Out] `int((a*x+a)^m*(-c*x+c)^m,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (ax + a)^m (-cx + c)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a*x+a)^m*(-c*x+c)^m,x, algorithm="maxima")`

[Out] `integrate((a*x + a)^m*(-c*x + c)^m, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (a + ax)^m (c - cx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + a*x)^m*(c - c*x)^m,x)`

[Out] `int((a + a*x)^m*(c - c*x)^m, x)`

sympy [C] time = 4.38, size = 124, normalized size = 3.02

$$\frac{a^m c^m G_{6,6}^{5,3} \left(\begin{matrix} -\frac{m}{2}, \frac{1}{2} - \frac{m}{2}, 1 \\ -m - \frac{1}{2}, -m, -\frac{m}{2}, \frac{1}{2} - m, \frac{1}{2} - \frac{m}{2} \end{matrix} \middle| \frac{e^{-2i\pi}}{x^2} \right) e^{-i\pi m}}{4\pi\Gamma(-m)} - \frac{a^m c^m G_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, 0, \frac{1}{2}, -\frac{m}{2} - \frac{1}{2}, -\frac{m}{2}, 1 \\ -\frac{m}{2} - \frac{1}{2}, -\frac{m}{2} \end{matrix} \middle| -\frac{1}{2}, 0, -\frac{1}{2}, 0 \right)}{4\pi\Gamma(-m)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a*x+a)**m*(-c*x+c)**m,x)`

[Out] `a**m*c**m*meijerg(((-m/2, 1/2 - m/2, 1), (1/2, -m, 1/2 - m)), ((-m - 1/2, -m, -m/2, 1/2 - m, 1/2 - m/2), (0,)), exp_polar(-2*I*pi)/x**2)*exp(-I*pi*m)/(4*pi*gamma(-m)) - a**m*c**m*meijerg(((-1/2, 0, 1/2, -m/2 - 1/2, -m/2, 1), ()), ((-m/2 - 1/2, -m/2), (-1/2, 0, -m - 1/2, 0)), x**(-2))/(4*pi*gamma(-m))`

3.1234 $\int (a + bx)^m (ac - bcx)^m dx$

Optimal. Leaf size=57

$$x(a + bx)^m \left(1 - \frac{b^2 x^2}{a^2}\right)^{-m} (ac - bcx)^m {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{b^2 x^2}{a^2}\right)$$

[Out] $x*(b*x+a)^m*(-b*c*x+a*c)^m*\text{hypergeom}([1/2, -m], [3/2], b^2*x^2/a^2)/((1-b^2*x^2/a^2)^m)$

Rubi [A] time = 0.02, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {42, 246, 245}

$$x(a + bx)^m \left(1 - \frac{b^2 x^2}{a^2}\right)^{-m} (ac - bcx)^m {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; \frac{b^2 x^2}{a^2}\right)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^m*(a*c - b*c*x)^m, x]$

[Out] $(x*(a + b*x)^m*(a*c - b*c*x)^m*\text{Hypergeometric2F1}[1/2, -m, 3/2, (b^2*x^2)/a^2])/((1 - (b^2*x^2)/a^2)^m)$

Rule 42

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(m_)}), x_Symbol] \rightarrow \text{Dist}[(a + b*x)^{\text{FracPart}[m]}*(c + d*x)^{\text{FracPart}[m]}/(a*c + b*d*x^2)^{\text{FracPart}[m]}, \text{Int}[(a*c + b*d*x^2)^m, x], x] /;$ $\text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{EqQ}[b*c + a*d, 0] \ \&\& \ !\text{IntegerQ}[2*m]$

Rule 245

$\text{Int}[(a_ + (b_)*(x_))^{(n_)}]^{(p_)}, x_Symbol] \rightarrow \text{Simp}[a^p*x*\text{Hypergeometric2F1}[-p, 1/n, 1/n + 1, -((b*x^n)/a)], x] /;$ $\text{FreeQ}\{a, b, n, p\}, x \ \&\& \ !\text{IGtQ}[p, 0] \ \&\& \ !\text{IntegerQ}[1/n] \ \&\& \ !\text{LtQ}[\text{Simplify}[1/n + p], 0] \ \&\& \ (\text{IntegerQ}[p] \ || \ \text{GtQ}[a, 0])$

Rule 246

$\text{Int}[(a_ + (b_)*(x_))^{(n_)}]^{(p_)}, x_Symbol] \rightarrow \text{Dist}[(a^{\text{IntPart}[p]}*(a + b*x^n)^{\text{FracPart}[p]})/(1 + (b*x^n)/a)^{\text{FracPart}[p]}, \text{Int}[(1 + (b*x^n)/a)^p, x], x] /;$ $\text{FreeQ}\{a, b, n, p\}, x \ \&\& \ !\text{IGtQ}[p, 0] \ \&\& \ !\text{IntegerQ}[1/n] \ \&\& \ !\text{LtQ}[\text{Simplify}[1/n + p], 0] \ \&\& \ !(\text{IntegerQ}[p] \ || \ \text{GtQ}[a, 0])$

Rubi steps

$$\begin{aligned}
\int (a + bx)^m (ac - bcx)^m dx &= \left((a + bx)^m (ac - bcx)^m (a^2c - b^2cx^2)^{-m} \right) \int (a^2c - b^2cx^2)^m dx \\
&= \left((a + bx)^m (ac - bcx)^m \left(1 - \frac{b^2x^2}{a^2} \right)^{-m} \right) \int \left(1 - \frac{b^2x^2}{a^2} \right)^m dx \\
&= x(a + bx)^m (ac - bcx)^m \left(1 - \frac{b^2x^2}{a^2} \right)^{-m} {}_2F_1 \left(\frac{1}{2}, -m; \frac{3}{2}; \frac{b^2x^2}{a^2} \right)
\end{aligned}$$

Mathematica [A] time = 0.03, size = 72, normalized size = 1.26

$$\frac{2^m (a - bx)(a + bx)^m \left(\frac{a+bx}{a} \right)^{-m} (c(a - bx))^m {}_2F_1 \left(-m, m + 1; m + 2; \frac{a-bx}{2a} \right)}{b(m + 1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^m*(a*c - b*c*x)^m,x]

[Out] -((2^m*(a - b*x)*(c*(a - b*x))^m*(a + b*x)^m*Hypergeometric2F1[-m, 1 + m, 2 + m, (a - b*x)/(2*a)])/(b*(1 + m)*((a + b*x)/a)^m))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}((-bcx + ac)^m (bx + a)^m, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(-b*c*x+a*c)^m,x, algorithm="fricas")

[Out] integral((-b*c*x + a*c)^m*(b*x + a)^m, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (-bcx + ac)^m (bx + a)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(-b*c*x+a*c)^m,x, algorithm="giac")

[Out] integrate((-b*c*x + a*c)^m*(b*x + a)^m, x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int (bx + a)^m (-bcx + ac)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^m*(-b*c*x+a*c)^m,x)

[Out] int((b*x+a)^m*(-b*c*x+a*c)^m,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (-bcx + ac)^m (bx + a)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(-b*c*x+a*c)^m,x, algorithm="maxima")

[Out] integrate((-b*c*x + a*c)^m*(b*x + a)^m, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (ac - bcx)^m (a + bx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a*c - b*c*x)^m*(a + b*x)^m,x)

[Out] int((a*c - b*c*x)^m*(a + b*x)^m, x)

sympy [C] time = 5.86, size = 146, normalized size = 2.56

$$\frac{aa^{2m}c^m G_{6,6}^{5,3} \left(\begin{matrix} -\frac{m}{2}, \frac{1}{2} - \frac{m}{2}, 1 \\ -m - \frac{1}{2}, -m, -\frac{m}{2}, \frac{1}{2} - m, \frac{1}{2} - \frac{m}{2} \end{matrix} \middle| \frac{a^2 e^{-2i\pi}}{b^2 x^2} \right) e^{-i\pi m}}{4\pi b \Gamma(-m)} - \frac{aa^{2m}c^m G_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, 0, \frac{1}{2}, -\frac{m}{2} - \frac{1}{2}, -\frac{m}{2}, 1 \\ -\frac{m}{2} - \frac{1}{2}, -\frac{m}{2} \end{matrix} \right)}{4\pi b \Gamma(-m)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**m*(-b*c*x+a*c)**m,x)

[Out] a*a**(2*m)*c**m*meijerg(((-m/2, 1/2 - m/2, 1), (1/2, -m, 1/2 - m)), ((-m - 1/2, -m, -m/2, 1/2 - m, 1/2 - m/2), (0,)), a**2*exp_polar(-2*I*pi)/(b**2*x**2))*exp(-I*pi*m)/(4*pi*b*gamma(-m)) - a*a**(2*m)*c**m*meijerg(((-1/2, 0, 1/2, -m/2 - 1/2, -m/2, 1), ()), ((-m/2 - 1/2, -m/2), (-1/2, 0, -m - 1/2, 0)), a**2/(b**2*x**2))/(4*pi*b*gamma(-m))

3.1235 $\int (3 - 6x)^m (2 + 4x)^m dx$

Optimal. Leaf size=20

$$6^m x {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 4x^2\right)$$

[Out] $6^m x \text{hypergeom}([1/2, -m], [3/2], 4x^2)$

Rubi [A] time = 0.01, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {41, 245}

$$6^m x {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 4x^2\right)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(3 - 6x)^m (2 + 4x)^m, x]$

[Out] $6^m x \text{Hypergeometric2F1}[1/2, -m, 3/2, 4x^2]$

Rule 41

$\text{Int}[(a_.) + (b_.) (x_.)^{(n_.)}]^{(m_.)} ((c_.) + (d_.) (x_.)^{(n_.)}), x_Symbol] \rightarrow \text{Int}[(a*c + b*d*x^2)^m, x] /;$ FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 245

$\text{Int}[(a_.) + (b_.) (x_.)^{(n_.)}]^{(p_.)}, x_Symbol] \rightarrow \text{Simp}[a^p x \text{Hypergeometric2F1}[-p, 1/n, 1/n + 1, -(b*x^n/a)], x] /;$ FreeQ[{a, b, n, p}, x] && !IGtQ[p, 0] && !IntegerQ[1/n] && !ILtQ[Simplify[1/n + p], 0] && (IntegerQ[p] || GtQ[a, 0])

Rubi steps

$$\begin{aligned} \int (3 - 6x)^m (2 + 4x)^m dx &= \int (6 - 24x^2)^m dx \\ &= 6^m x {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 4x^2\right) \end{aligned}$$

Mathematica [A] time = 0.01, size = 20, normalized size = 1.00

$$6^m x {}_2F_1\left(\frac{1}{2}, -m; \frac{3}{2}; 4x^2\right)$$

Antiderivative was successfully verified.

[In] Integrate[(3 - 6*x)^m*(2 + 4*x)^m,x]

[Out] 6^m*x*Hypergeometric2F1[1/2, -m, 3/2, 4*x^2]

fricas [F] time = 0.51, size = 0, normalized size = 0.00

$$\text{integral}((4x + 2)^m(-6x + 3)^m, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^m*(4*x+2)^m,x, algorithm="fricas")

[Out] integral((4*x + 2)^m*(-6*x + 3)^m, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (4x + 2)^m(-6x + 3)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^m*(4*x+2)^m,x, algorithm="giac")

[Out] integrate((4*x + 2)^m*(-6*x + 3)^m, x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int (4x + 2)^m(-6x + 3)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-6*x+3)^m*(4*x+2)^m,x)

[Out] int((-6*x+3)^m*(4*x+2)^m,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (4x + 2)^m(-6x + 3)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)^m*(4*x+2)^m,x, algorithm="maxima")

[Out] integrate((4*x + 2)^m*(-6*x + 3)^m, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.05

$$\int (4x + 2)^m (3 - 6x)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((4*x + 2)^m*(3 - 6*x)^m, x)

[Out] int((4*x + 2)^m*(3 - 6*x)^m, x)

sympy [C] time = 4.34, size = 42, normalized size = 2.10

$$\frac{24^m \left(x + \frac{1}{2}\right) \left(x + \frac{1}{2}\right)^m \Gamma(m + 1) {}_2F_1\left(\begin{matrix} -m, m + 1 \\ m + 2 \end{matrix} \middle| \left(x + \frac{1}{2}\right) e^{2i\pi}\right)}{\Gamma(m + 2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-6*x)**m*(4*x+2)**m, x)

[Out] 24**m*(x + 1/2)*(x + 1/2)**m*gamma(m + 1)*hyper((-m, m + 1), (m + 2,), (x + 1/2)*exp_polar(2*I*pi))/gamma(m + 2)

3.1236 $\int (a + bx)^4 (c + dx) dx$

Optimal. Leaf size=38

$$\frac{(a + bx)^5 (bc - ad)}{5b^2} + \frac{d(a + bx)^6}{6b^2}$$

[Out] $1/5*(-a*d+b*c)*(b*x+a)^5/b^2+1/6*d*(b*x+a)^6/b^2$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{(a + bx)^5 (bc - ad)}{5b^2} + \frac{d(a + bx)^6}{6b^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4*(c + d*x), x]

[Out] ((b*c - a*d)*(a + b*x)^5)/(5*b^2) + (d*(a + b*x)^6)/(6*b^2)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^4 (c + dx) dx &= \int \left(\frac{(bc - ad)(a + bx)^4}{b} + \frac{d(a + bx)^5}{b} \right) dx \\ &= \frac{(bc - ad)(a + bx)^5}{5b^2} + \frac{d(a + bx)^6}{6b^2} \end{aligned}$$

Mathematica [B] time = 0.02, size = 84, normalized size = 2.21

$$\frac{1}{30} x (15a^4(2c + dx) + 20a^3bx(3c + 2dx) + 15a^2b^2x^2(4c + 3dx) + 6ab^3x^3(5c + 4dx) + b^4x^4(6c + 5dx))$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4*(c + d*x), x]

[Out] $(x*(15*a^4*(2*c + d*x) + 20*a^3*b*x*(3*c + 2*d*x) + 15*a^2*b^2*x^2*(4*c + 3*d*x) + 6*a*b^3*x^3*(5*c + 4*d*x) + b^4*x^4*(6*c + 5*d*x)))/30$

fricas [B] time = 0.37, size = 97, normalized size = 2.55

$$\frac{1}{6}x^6db^4 + \frac{1}{5}x^5cb^4 + \frac{4}{5}x^5db^3a + x^4cb^3a + \frac{3}{2}x^4db^2a^2 + 2x^3cb^2a^2 + \frac{4}{3}x^3dba^3 + 2x^2cba^3 + \frac{1}{2}x^2da^4 + xca^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c),x, algorithm="fricas")

[Out] $1/6*x^6*d*b^4 + 1/5*x^5*c*b^4 + 4/5*x^5*d*b^3*a + x^4*c*b^3*a + 3/2*x^4*d*b^2*a^2 + 2*x^3*c*b^2*a^2 + 4/3*x^3*d*b*a^3 + 2*x^2*c*b*a^3 + 1/2*x^2*d*a^4 + x*c*a^4$

giac [B] time = 1.03, size = 97, normalized size = 2.55

$$\frac{1}{6}b^4dx^6 + \frac{1}{5}b^4cx^5 + \frac{4}{5}ab^3dx^5 + ab^3cx^4 + \frac{3}{2}a^2b^2dx^4 + 2a^2b^2cx^3 + \frac{4}{3}a^3bdx^3 + 2a^3bcx^2 + \frac{1}{2}a^4dx^2 + a^4cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c),x, algorithm="giac")

[Out] $1/6*b^4*d*x^6 + 1/5*b^4*c*x^5 + 4/5*a*b^3*d*x^5 + a*b^3*c*x^4 + 3/2*a^2*b^2*d*x^4 + 2*a^2*b^2*c*x^3 + 4/3*a^3*b*d*x^3 + 2*a^3*b*c*x^2 + 1/2*a^4*d*x^2 + a^4*c*x$

maple [B] time = 0.00, size = 97, normalized size = 2.55

$$\frac{b^4d x^6}{6} + a^4cx + \frac{(4a b^3d + b^4c) x^5}{5} + \frac{(6a^2b^2d + 4a b^3c) x^4}{4} + \frac{(4a^3bd + 6a^2b^2c) x^3}{3} + \frac{(a^4d + 4a^3bc) x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4*(d*x+c),x)

[Out] $1/6*b^4*d*x^6 + 1/5*(4*a*b^3*d + b^4*c)*x^5 + 1/4*(6*a^2*b^2*d + 4*a*b^3*c)*x^4 + 1/3*(4*a^3*b*d + 6*a^2*b^2*c)*x^3 + 1/2*(a^4*d + 4*a^3*b*c)*x^2 + a^4*c*x$

maxima [B] time = 1.38, size = 96, normalized size = 2.53

$$\frac{1}{6}b^4dx^6 + a^4cx + \frac{1}{5}(b^4c + 4ab^3d)x^5 + \frac{1}{2}(2ab^3c + 3a^2b^2d)x^4 + \frac{2}{3}(3a^2b^2c + 2a^3bd)x^3 + \frac{1}{2}(4a^3bc + a^4d)x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c),x, algorithm="maxima")

[Out] $1/6*b^4*d*x^6 + a^4*c*x + 1/5*(b^4*c + 4*a*b^3*d)*x^5 + 1/2*(2*a*b^3*c + 3*a^2*b^2*d)*x^4 + 2/3*(3*a^2*b^2*c + 2*a^3*b*d)*x^3 + 1/2*(4*a^3*b*c + a^4*d)*x^2$

mupad [B] time = 0.19, size = 88, normalized size = 2.32

$$x^5 \left(\frac{c b^4}{5} + \frac{4 a d b^3}{5} \right) + x^2 \left(\frac{d a^4}{2} + 2 b c a^3 \right) + \frac{b^4 d x^6}{6} + a^4 c x + \frac{2 a^2 b x^3 (2 a d + 3 b c)}{3} + \frac{a b^2 x^4 (3 a d + 2 b c)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^4*(c + d*x), x)`

[Out] $x^5*((b^4*c)/5 + (4*a*b^3*d)/5) + x^2*((a^4*d)/2 + 2*a^3*b*c) + (b^4*d*x^6)/6 + a^4*c*x + (2*a^2*b*x^3*(2*a*d + 3*b*c))/3 + (a*b^2*x^4*(3*a*d + 2*b*c))/2$

sympy [B] time = 0.08, size = 100, normalized size = 2.63

$$a^4 c x + \frac{b^4 d x^6}{6} + x^5 \left(\frac{4 a b^3 d}{5} + \frac{b^4 c}{5} \right) + x^4 \left(\frac{3 a^2 b^2 d}{2} + a b^3 c \right) + x^3 \left(\frac{4 a^3 b d}{3} + 2 a^2 b^2 c \right) + x^2 \left(\frac{a^4 d}{2} + 2 a^3 b c \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**4*(d*x+c), x)`

[Out] $a**4*c*x + b**4*d*x**6/6 + x**5*(4*a*b**3*d/5 + b**4*c/5) + x**4*(3*a**2*b**2*d/2 + a*b**3*c) + x**3*(4*a**3*b*d/3 + 2*a**2*b**2*c) + x**2*(a**4*d/2 + 2*a**3*b*c)$

3.1237 $\int (a + bx)^3(c + dx) dx$

Optimal. Leaf size=38

$$\frac{(a + bx)^4(bc - ad)}{4b^2} + \frac{d(a + bx)^5}{5b^2}$$

[Out] $1/4*(-a*d+b*c)*(b*x+a)^4/b^2+1/5*d*(b*x+a)^5/b^2$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{(a + bx)^4(bc - ad)}{4b^2} + \frac{d(a + bx)^5}{5b^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3*(c + d*x), x]

[Out] ((b*c - a*d)*(a + b*x)^4)/(4*b^2) + (d*(a + b*x)^5)/(5*b^2)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^3(c + dx) dx &= \int \left(\frac{(bc - ad)(a + bx)^3}{b} + \frac{d(a + bx)^4}{b} \right) dx \\ &= \frac{(bc - ad)(a + bx)^4}{4b^2} + \frac{d(a + bx)^5}{5b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 67, normalized size = 1.76

$$a^3cx + \frac{1}{2}a^2x^2(ad + 3bc) + \frac{1}{4}b^2x^4(3ad + bc) + abx^3(ad + bc) + \frac{1}{5}b^3dx^5$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3*(c + d*x), x]

[Out] $a^3cx + (a^2(3bc + ad)x^2)/2 + ab(bc + ad)x^3 + (b^2(bc + 3ad)x^4)/4 + (b^3dx^5)/5$

fricas [B] time = 0.38, size = 72, normalized size = 1.89

$$\frac{1}{5}x^5db^3 + \frac{1}{4}x^4cb^3 + \frac{3}{4}x^4db^2a + x^3cb^2a + x^3dba^2 + \frac{3}{2}x^2cba^2 + \frac{1}{2}x^2da^3 + xca^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3*(d*x+c),x, algorithm="fricas")`

[Out] $1/5*x^5*d*b^3 + 1/4*x^4*c*b^3 + 3/4*x^4*d*b^2*a + x^3*c*b^2*a + x^3*d*b*a^2 + 3/2*x^2*c*b*a^2 + 1/2*x^2*d*a^3 + x*c*a^3$

giac [B] time = 1.14, size = 72, normalized size = 1.89

$$\frac{1}{5}b^3dx^5 + \frac{1}{4}b^3cx^4 + \frac{3}{4}ab^2dx^4 + ab^2cx^3 + a^2bdx^3 + \frac{3}{2}a^2bcx^2 + \frac{1}{2}a^3dx^2 + a^3cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3*(d*x+c),x, algorithm="giac")`

[Out] $1/5*b^3*d*x^5 + 1/4*b^3*c*x^4 + 3/4*a*b^2*d*x^4 + a*b^2*c*x^3 + a^2*b*d*x^3 + 3/2*a^2*b*c*x^2 + 1/2*a^3*d*x^2 + a^3*c*x$

maple [B] time = 0.00, size = 73, normalized size = 1.92

$$\frac{b^3dx^5}{5} + a^3cx + \frac{(3ab^2d + b^3c)x^4}{4} + \frac{(3a^2bd + 3ab^2c)x^3}{3} + \frac{(a^3d + 3a^2bc)x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3*(d*x+c),x)`

[Out] $1/5*b^3*d*x^5 + 1/4*(3a*b^2*d + b^3*c)*x^4 + 1/3*(3a^2*b*d + 3a*b^2*c)*x^3 + 1/2*(a^3*d + 3a^2*b*c)*x^2 + a^3*c*x$

maxima [B] time = 1.41, size = 69, normalized size = 1.82

$$\frac{1}{5}b^3dx^5 + a^3cx + \frac{1}{4}(b^3c + 3ab^2d)x^4 + (ab^2c + a^2bd)x^3 + \frac{1}{2}(3a^2bc + a^3d)x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3*(d*x+c),x, algorithm="maxima")`

[Out] $1/5*b^3*d*x^5 + a^3*c*x + 1/4*(b^3*c + 3*a*b^2*d)*x^4 + (a*b^2*c + a^2*b*d)*x^3 + 1/2*(3*a^2*b*c + a^3*d)*x^2$

mupad [B] time = 0.16, size = 65, normalized size = 1.71

$$x^4 \left(\frac{c b^3}{4} + \frac{3 a d b^2}{4} \right) + x^2 \left(\frac{d a^3}{2} + \frac{3 b c a^2}{2} \right) + \frac{b^3 d x^5}{5} + a^3 c x + a b x^3 (a d + b c)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3*(c + d*x), x)`

[Out] $x^4*((b^3*c)/4 + (3*a*b^2*d)/4) + x^2*((a^3*d)/2 + (3*a^2*b*c)/2) + (b^3*d*x^5)/5 + a^3*c*x + a*b*x^3*(a*d + b*c)$

sympy [B] time = 0.08, size = 73, normalized size = 1.92

$$a^3 c x + \frac{b^3 d x^5}{5} + x^4 \left(\frac{3 a b^2 d}{4} + \frac{b^3 c}{4} \right) + x^3 (a^2 b d + a b^2 c) + x^2 \left(\frac{a^3 d}{2} + \frac{3 a^2 b c}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3*(d*x+c), x)`

[Out] $a**3*c*x + b**3*d*x**5/5 + x**4*(3*a*b**2*d/4 + b**3*c/4) + x**3*(a**2*b*d + a*b**2*c) + x**2*(a**3*d/2 + 3*a**2*b*c/2)$

3.1238 $\int (a + bx)^2(c + dx) dx$

Optimal. Leaf size=38

$$\frac{(a + bx)^3(bc - ad)}{3b^2} + \frac{d(a + bx)^4}{4b^2}$$

[Out] $1/3*(-a*d+b*c)*(b*x+a)^3/b^2+1/4*d*(b*x+a)^4/b^2$

Rubi [A] time = 0.03, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{(a + bx)^3(bc - ad)}{3b^2} + \frac{d(a + bx)^4}{4b^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(c + d*x), x]

[Out] ((b*c - a*d)*(a + b*x)^3)/(3*b^2) + (d*(a + b*x)^4)/(4*b^2)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2(c + dx) dx &= \int \left(\frac{(bc - ad)(a + bx)^2}{b} + \frac{d(a + bx)^3}{b} \right) dx \\ &= \frac{(bc - ad)(a + bx)^3}{3b^2} + \frac{d(a + bx)^4}{4b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 46, normalized size = 1.21

$$\frac{1}{12}x(6a^2(2c + dx) + 4abx(3c + 2dx) + b^2x^2(4c + 3dx))$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(c + d*x), x]

[Out] (x*(6*a^2*(2*c + d*x) + 4*a*b*x*(3*c + 2*d*x) + b^2*x^2*(4*c + 3*d*x)))/12

fricas [A] time = 0.39, size = 49, normalized size = 1.29

$$\frac{1}{4}x^4db^2 + \frac{1}{3}x^3cb^2 + \frac{2}{3}x^3dba + x^2cba + \frac{1}{2}x^2da^2 + xca^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c),x, algorithm="fricas")

[Out] 1/4*x^4*d*b^2 + 1/3*x^3*c*b^2 + 2/3*x^3*d*b*a + x^2*c*b*a + 1/2*x^2*d*a^2 + x*c*a^2

giac [A] time = 0.99, size = 49, normalized size = 1.29

$$\frac{1}{4}b^2dx^4 + \frac{1}{3}b^2cx^3 + \frac{2}{3}abdx^3 + abcx^2 + \frac{1}{2}a^2dx^2 + a^2cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c),x, algorithm="giac")

[Out] 1/4*b^2*d*x^4 + 1/3*b^2*c*x^3 + 2/3*a*b*d*x^3 + a*b*c*x^2 + 1/2*a^2*d*x^2 + a^2*c*x

maple [A] time = 0.00, size = 49, normalized size = 1.29

$$\frac{b^2d x^4}{4} + a^2cx + \frac{(2abd + b^2c)x^3}{3} + \frac{(a^2d + 2abc)x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(d*x+c),x)

[Out] 1/4*b^2*d*x^4+1/3*(2*a*b*d+b^2*c)*x^3+1/2*(a^2*d+2*a*b*c)*x^2+a^2*c*x

maxima [A] time = 1.30, size = 48, normalized size = 1.26

$$\frac{1}{4}b^2dx^4 + a^2cx + \frac{1}{3}(b^2c + 2abd)x^3 + \frac{1}{2}(2abc + a^2d)x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c),x, algorithm="maxima")

[Out] 1/4*b^2*d*x^4 + a^2*c*x + 1/3*(b^2*c + 2*a*b*d)*x^3 + 1/2*(2*a*b*c + a^2*d)*x^2

mupad [B] time = 0.05, size = 47, normalized size = 1.24

$$x^2 \left(\frac{d a^2}{2} + b c a \right) + x^3 \left(\frac{c b^2}{3} + \frac{2 a d b}{3} \right) + \frac{b^2 d x^4}{4} + a^2 c x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2*(c + d*x), x)

[Out] x^2*((a^2*d)/2 + a*b*c) + x^3*((b^2*c)/3 + (2*a*b*d)/3) + (b^2*d*x^4)/4 + a^2*c*x

sympy [A] time = 0.07, size = 49, normalized size = 1.29

$$a^2 c x + \frac{b^2 d x^4}{4} + x^3 \left(\frac{2 a b d}{3} + \frac{b^2 c}{3} \right) + x^2 \left(\frac{a^2 d}{2} + a b c \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2*(d*x+c), x)

[Out] a**2*c*x + b**2*d*x**4/4 + x**3*(2*a*b*d/3 + b**2*c/3) + x**2*(a**2*d/2 + a*b*c)

3.1239 $\int (a + bx)(c + dx) dx$

Optimal. Leaf size=28

$$\frac{1}{2}x^2(ad + bc) + acx + \frac{1}{3}bdx^3$$

[Out] a*c*x+1/2*(a*d+b*c)*x^2+1/3*b*d*x^3

Rubi [A] time = 0.02, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {43}

$$\frac{1}{2}x^2(ad + bc) + acx + \frac{1}{3}bdx^3$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(c + d*x), x]

[Out] a*c*x + ((b*c + a*d)*x^2)/2 + (b*d*x^3)/3

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)(c + dx) dx &= \int (ac + (bc + ad)x + bdx^2) dx \\ &= acx + \frac{1}{2}(bc + ad)x^2 + \frac{1}{3}bdx^3 \end{aligned}$$

Mathematica [A] time = 0.00, size = 28, normalized size = 1.00

$$\frac{1}{2}x^2(ad + bc) + acx + \frac{1}{3}bdx^3$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(c + d*x), x]

[Out] a*c*x + ((b*c + a*d)*x^2)/2 + (b*d*x^3)/3

fricas [A] time = 0.39, size = 26, normalized size = 0.93

$$\frac{1}{3}x^3db + \frac{1}{2}x^2cb + \frac{1}{2}x^2da + xca$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c),x, algorithm="fricas")

[Out] 1/3*x^3*d*b + 1/2*x^2*c*b + 1/2*x^2*d*a + x*c*a

giac [A] time = 0.99, size = 26, normalized size = 0.93

$$\frac{1}{3}bdx^3 + \frac{1}{2}bcx^2 + \frac{1}{2}adx^2 + acx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c),x, algorithm="giac")

[Out] 1/3*b*d*x^3 + 1/2*b*c*x^2 + 1/2*a*d*x^2 + a*c*x

maple [A] time = 0.00, size = 25, normalized size = 0.89

$$\frac{bdx^3}{3} + acx + \frac{(ad+bc)x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(d*x+c),x)

[Out] a*c*x+1/2*(a*d+b*c)*x^2+1/3*b*d*x^3

maxima [A] time = 1.35, size = 24, normalized size = 0.86

$$\frac{1}{3}bdx^3 + acx + \frac{1}{2}(bc+ad)x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c),x, algorithm="maxima")

[Out] 1/3*b*d*x^3 + a*c*x + 1/2*(b*c + a*d)*x^2

mupad [B] time = 0.03, size = 25, normalized size = 0.89

$$\frac{bdx^3}{3} + \left(\frac{ad}{2} + \frac{bc}{2}\right)x^2 + acx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)*(c + d*x),x)`

[Out] $x^2*((a*d)/2 + (b*c)/2) + a*c*x + (b*d*x^3)/3$

sympy [A] time = 0.06, size = 26, normalized size = 0.93

$$acx + \frac{bdx^3}{3} + x^2 \left(\frac{ad}{2} + \frac{bc}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c),x)`

[Out] $a*c*x + b*d*x**3/3 + x**2*(a*d/2 + b*c/2)$

3.1240 $\int (c + dx) dx$

Optimal. Leaf size=12

$$cx + \frac{dx^2}{2}$$

[Out] c*x+1/2*d*x^2

Rubi [A] time = 0.00, antiderivative size = 12, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$cx + \frac{dx^2}{2}$$

Antiderivative was successfully verified.

[In] Int[c + d*x,x]

[Out] c*x + (d*x^2)/2

Rubi steps

$$\int (c + dx) dx = cx + \frac{dx^2}{2}$$

Mathematica [A] time = 0.00, size = 12, normalized size = 1.00

$$cx + \frac{dx^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[c + d*x,x]

[Out] c*x + (d*x^2)/2

fricas [A] time = 0.39, size = 10, normalized size = 0.83

$$\frac{1}{2}x^2d + xc$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(d*x+c,x, algorithm="fricas")

[Out] $\frac{1}{2}x^2d + xc$

giac [A] time = 0.90, size = 10, normalized size = 0.83

$$\frac{1}{2}dx^2 + cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(d*x+c,x, algorithm="giac")`

[Out] $\frac{1}{2}d*x^2 + c*x$

maple [A] time = 0.00, size = 11, normalized size = 0.92

$$\frac{1}{2}d x^2 + cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(d*x+c,x)`

[Out] $\frac{1}{2}d*x^2+c*x$

maxima [A] time = 1.35, size = 10, normalized size = 0.83

$$\frac{1}{2}dx^2 + cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(d*x+c,x, algorithm="maxima")`

[Out] $\frac{1}{2}d*x^2 + c*x$

mupad [B] time = 0.02, size = 10, normalized size = 0.83

$$\frac{dx^2}{2} + cx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(c + d*x,x)`

[Out] $c*x + (d*x^2)/2$

sympy [A] time = 0.06, size = 8, normalized size = 0.67

$$cx + \frac{dx^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(d*x+c,x)
```

```
[Out] c*x + d*x**2/2
```

$$3.1241 \quad \int \frac{c+dx}{a+bx} dx$$

Optimal. Leaf size=25

$$\frac{(bc - ad) \log(a + bx)}{b^2} + \frac{dx}{b}$$

[Out] d*x/b+(-a*d+b*c)*ln(b*x+a)/b^2

Rubi [A] time = 0.02, antiderivative size = 25, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{(bc - ad) \log(a + bx)}{b^2} + \frac{dx}{b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)/(a + b*x), x]

[Out] (d*x)/b + ((b*c - a*d)*Log[a + b*x])/b^2

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{c+dx}{a+bx} dx &= \int \left(\frac{d}{b} + \frac{bc-ad}{b(a+bx)} \right) dx \\ &= \frac{dx}{b} + \frac{(bc-ad) \log(a+bx)}{b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 1.00

$$\frac{(bc - ad) \log(a + bx)}{b^2} + \frac{dx}{b}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)/(a + b*x), x]

[Out] (d*x)/b + ((b*c - a*d)*Log[a + b*x])/b^2

fricas [A] time = 0.44, size = 24, normalized size = 0.96

$$\frac{bdx + (bc - ad) \log(bx + a)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(b*x+a),x, algorithm="fricas")

[Out] (b*d*x + (b*c - a*d)*log(b*x + a))/b^2

giac [A] time = 0.96, size = 26, normalized size = 1.04

$$\frac{dx}{b} + \frac{(bc - ad) \log(|bx + a|)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(b*x+a),x, algorithm="giac")

[Out] d*x/b + (b*c - a*d)*log(abs(b*x + a))/b^2

maple [A] time = 0.00, size = 32, normalized size = 1.28

$$-\frac{ad \ln(bx + a)}{b^2} + \frac{c \ln(bx + a)}{b} + \frac{dx}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)/(b*x+a),x)

[Out] d*x/b-1/b^2*ln(b*x+a)*a*d+1/b*c*ln(b*x+a)

maxima [A] time = 1.25, size = 25, normalized size = 1.00

$$\frac{dx}{b} + \frac{(bc - ad) \log(bx + a)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(b*x+a),x, algorithm="maxima")

[Out] d*x/b + (b*c - a*d)*log(b*x + a)/b^2

mupad [B] time = 0.05, size = 26, normalized size = 1.04

$$\frac{dx}{b} - \frac{\ln(a + bx) (ad - bc)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)/(a + b*x), x)`

[Out] $(d*x)/b - (\log(a + b*x)*(a*d - b*c))/b^2$

sympy [A] time = 0.15, size = 20, normalized size = 0.80

$$\frac{dx}{b} - \frac{(ad - bc) \log(a + bx)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a), x)`

[Out] $d*x/b - (a*d - b*c)*\log(a + b*x)/b**2$

$$3.1242 \quad \int \frac{c+dx}{(a+bx)^2} dx$$

Optimal. Leaf size=32

$$\frac{d \log(a + bx)}{b^2} - \frac{bc - ad}{b^2(a + bx)}$$

[Out] (a*d-b*c)/b^2/(b*x+a)+d*ln(b*x+a)/b^2

Rubi [A] time = 0.02, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{d \log(a + bx)}{b^2} - \frac{bc - ad}{b^2(a + bx)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)/(a + b*x)^2,x]

[Out] -((b*c - a*d)/(b^2*(a + b*x))) + (d*Log[a + b*x])/b^2

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{c + dx}{(a + bx)^2} dx &= \int \left(\frac{bc - ad}{b(a + bx)^2} + \frac{d}{b(a + bx)} \right) dx \\ &= -\frac{bc - ad}{b^2(a + bx)} + \frac{d \log(a + bx)}{b^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 0.97

$$\frac{ad - bc}{b^2(a + bx)} + \frac{d \log(a + bx)}{b^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)/(a + b*x)^2,x]

[Out] $(-(b*c) + a*d)/(b^2*(a + b*x)) + (d*\text{Log}[a + b*x])/b^2$

fricas [A] time = 0.44, size = 39, normalized size = 1.22

$$\frac{bc - ad - (bdx + ad) \log(bx + a)}{b^3x + ab^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)^2,x, algorithm="fricas")`

[Out] $-(b*c - a*d - (b*d*x + a*d)*\log(b*x + a))/(b^3*x + a*b^2)$

giac [A] time = 1.02, size = 57, normalized size = 1.78

$$\frac{d \left(\frac{\log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b} - \frac{a}{(bx+a)b} \right) - \frac{c}{(bx+a)b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)^2,x, algorithm="giac")`

[Out] $-d*(\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b))))/b - a/((b*x + a)*b)/b - c/((b*x + a)*b)$

maple [A] time = 0.00, size = 39, normalized size = 1.22

$$\frac{ad}{(bx + a)b^2} - \frac{c}{(bx + a)b} + \frac{d \ln(bx + a)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)/(b*x+a)^2,x)`

[Out] $d*\ln(b*x+a)/b^2+1/b^2/(b*x+a)*a*d-1/b/(b*x+a)*c$

maxima [A] time = 1.34, size = 35, normalized size = 1.09

$$-\frac{bc - ad}{b^3x + ab^2} + \frac{d \log(bx + a)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)^2,x, algorithm="maxima")`

[Out] $-(b*c - a*d)/(b^3*x + a*b^2) + d*\log(b*x + a)/b^2$

mupad [B] time = 0.17, size = 31, normalized size = 0.97

$$\frac{ad - bc}{b^2(a + bx)} + \frac{d \ln(a + bx)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)/(a + b*x)^2,x)`

[Out] `(a*d - b*c)/(b^2*(a + b*x)) + (d*log(a + b*x))/b^2`

sympy [A] time = 0.19, size = 27, normalized size = 0.84

$$\frac{ad - bc}{ab^2 + b^3x} + \frac{d \log(a + bx)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)**2,x)`

[Out] `(a*d - b*c)/(a*b**2 + b**3*x) + d*log(a + b*x)/b**2`

$$3.1243 \quad \int \frac{c+dx}{(a+bx)^3} dx$$

Optimal. Leaf size=28

$$-\frac{(c+dx)^2}{2(a+bx)^2(bc-ad)}$$

[Out] $-1/2*(d*x+c)^2/(-a*d+b*c)/(b*x+a)^2$

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {37}

$$-\frac{(c+dx)^2}{2(a+bx)^2(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)/(a + b*x)^3, x]

[Out] $-(c + d*x)^2/(2*(b*c - a*d)*(a + b*x)^2)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{c+dx}{(a+bx)^3} dx = -\frac{(c+dx)^2}{2(bc-ad)(a+bx)^2}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 0.93

$$-\frac{ad + b(c + 2dx)}{2b^2(a + bx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)/(a + b*x)^3, x]

[Out] $-1/2*(a*d + b*(c + 2*d*x))/(b^2*(a + b*x)^2)$

fricas [A] time = 0.43, size = 38, normalized size = 1.36

$$\frac{2 b d x + b c + a d}{2 \left(b^4 x^2 + 2 a b^3 x + a^2 b^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(b*x+a)^3,x, algorithm="fricas")

[Out] -1/2*(2*b*d*x + b*c + a*d)/(b^4*x^2 + 2*a*b^3*x + a^2*b^2)

giac [A] time = 1.06, size = 24, normalized size = 0.86

$$\frac{2 b d x + b c + a d}{2 (b x + a)^2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(b*x+a)^3,x, algorithm="giac")

[Out] -1/2*(2*b*d*x + b*c + a*d)/((b*x + a)^2*b^2)

maple [A] time = 0.01, size = 35, normalized size = 1.25

$$-\frac{d}{(b x + a) b^2} - \frac{-a d + b c}{2 (b x + a)^2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)/(b*x+a)^3,x)

[Out] -1/2*(-a*d+b*c)/b^2/(b*x+a)^2-d/b^2/(b*x+a)

maxima [A] time = 1.36, size = 38, normalized size = 1.36

$$\frac{2 b d x + b c + a d}{2 \left(b^4 x^2 + 2 a b^3 x + a^2 b^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(b*x+a)^3,x, algorithm="maxima")

[Out] -1/2*(2*b*d*x + b*c + a*d)/(b^4*x^2 + 2*a*b^3*x + a^2*b^2)

mupad [B] time = 0.16, size = 39, normalized size = 1.39

$$-\frac{\frac{a d + b c}{2 b^2} + \frac{d x}{b}}{a^2 + 2 a b x + b^2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)/(a + b*x)^3,x)`

[Out] $-\frac{(a*d + b*c)}{(2*b^2)} + \frac{(d*x)/b}{(a^2 + b^2*x^2 + 2*a*b*x)}$

sympy [A] time = 0.26, size = 39, normalized size = 1.39

$$\frac{-ad - bc - 2bdx}{2a^2b^2 + 4ab^3x + 2b^4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)**3,x)`

[Out] $(-a*d - b*c - 2*b*d*x)/(2*a**2*b**2 + 4*a*b**3*x + 2*b**4*x**2)$

$$3.1244 \quad \int \frac{c+dx}{(a+bx)^4} dx$$

Optimal. Leaf size=38

$$-\frac{bc-ad}{3b^2(a+bx)^3} - \frac{d}{2b^2(a+bx)^2}$$

[Out] 1/3*(a*d-b*c)/b^2/(b*x+a)^3-1/2*d/b^2/(b*x+a)^2

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{bc-ad}{3b^2(a+bx)^3} - \frac{d}{2b^2(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)/(a + b*x)^4, x]

[Out] -(b*c - a*d)/(3*b^2*(a + b*x)^3) - d/(2*b^2*(a + b*x)^2)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{c+dx}{(a+bx)^4} dx &= \int \left(\frac{bc-ad}{b(a+bx)^4} + \frac{d}{b(a+bx)^3} \right) dx \\ &= -\frac{bc-ad}{3b^2(a+bx)^3} - \frac{d}{2b^2(a+bx)^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.71

$$-\frac{ad+2bc+3bdx}{6b^2(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)/(a + b*x)^4, x]

[Out] $-1/6*(2*b*c + a*d + 3*b*d*x)/(b^2*(a + b*x)^3)$

fricas [A] time = 0.42, size = 50, normalized size = 1.32

$$\frac{3 b d x + 2 b c + a d}{6 \left(b^5 x^3 + 3 a b^4 x^2 + 3 a^2 b^3 x + a^3 b^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)^4,x, algorithm="fricas")`

[Out] $-1/6*(3*b*d*x + 2*b*c + a*d)/(b^5*x^3 + 3*a*b^4*x^2 + 3*a^2*b^3*x + a^3*b^2)$

giac [A] time = 0.75, size = 25, normalized size = 0.66

$$\frac{3 b d x + 2 b c + a d}{6 (b x + a)^3 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)^4,x, algorithm="giac")`

[Out] $-1/6*(3*b*d*x + 2*b*c + a*d)/((b*x + a)^3*b^2)$

maple [A] time = 0.01, size = 35, normalized size = 0.92

$$-\frac{d}{2 (b x + a)^2 b^2} - \frac{-a d + b c}{3 (b x + a)^3 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)/(b*x+a)^4,x)`

[Out] $-1/3*(-a*d+b*c)/b^2/(b*x+a)^3-1/2*d/b^2/(b*x+a)^2$

maxima [A] time = 1.31, size = 50, normalized size = 1.32

$$\frac{3 b d x + 2 b c + a d}{6 \left(b^5 x^3 + 3 a b^4 x^2 + 3 a^2 b^3 x + a^3 b^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)^4,x, algorithm="maxima")`

[Out] $-1/6*(3*b*d*x + 2*b*c + a*d)/(b^5*x^3 + 3*a*b^4*x^2 + 3*a^2*b^3*x + a^3*b^2)$

mupad [B] time = 0.17, size = 52, normalized size = 1.37

$$-\frac{\frac{ad+2bc}{6b^2} + \frac{dx}{2b}}{a^3 + 3a^2bx + 3ab^2x^2 + b^3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)/(a + b*x)^4, x)`

[Out] `-((a*d + 2*b*c)/(6*b^2) + (d*x)/(2*b))/(a^3 + b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x)`

sympy [A] time = 0.34, size = 53, normalized size = 1.39

$$\frac{-ad - 2bc - 3bdx}{6a^3b^2 + 18a^2b^3x + 18ab^4x^2 + 6b^5x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)**4, x)`

[Out] `(-a*d - 2*b*c - 3*b*d*x)/(6*a**3*b**2 + 18*a**2*b**3*x + 18*a*b**4*x**2 + 6*b**5*x**3)`

$$3.1245 \quad \int \frac{c+dx}{(a+bx)^5} dx$$

Optimal. Leaf size=38

$$-\frac{bc-ad}{4b^2(a+bx)^4} - \frac{d}{3b^2(a+bx)^3}$$

[Out] $1/4*(a*d-b*c)/b^2/(b*x+a)^4-1/3*d/b^2/(b*x+a)^3$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$-\frac{bc-ad}{4b^2(a+bx)^4} - \frac{d}{3b^2(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)/(a + b*x)^5, x]

[Out] $-(b*c - a*d)/(4*b^2*(a + b*x)^4) - d/(3*b^2*(a + b*x)^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{c+dx}{(a+bx)^5} dx &= \int \left(\frac{bc-ad}{b(a+bx)^5} + \frac{d}{b(a+bx)^4} \right) dx \\ &= -\frac{bc-ad}{4b^2(a+bx)^4} - \frac{d}{3b^2(a+bx)^3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.71

$$-\frac{ad+3bc+4bdx}{12b^2(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)/(a + b*x)^5, x]

[Out] $-1/12*(3*b*c + a*d + 4*b*d*x)/(b^2*(a + b*x)^4)$

fricas [A] time = 0.42, size = 61, normalized size = 1.61

$$-\frac{4 b d x + 3 b c + a d}{12 \left(b^6 x^4 + 4 a b^5 x^3 + 6 a^2 b^4 x^2 + 4 a^3 b^3 x + a^4 b^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)^5,x, algorithm="fricas")`

[Out] $-1/12*(4*b*d*x + 3*b*c + a*d)/(b^6*x^4 + 4*a*b^5*x^3 + 6*a^2*b^4*x^2 + 4*a^3*b^3*x + a^4*b^2)$

giac [A] time = 0.92, size = 41, normalized size = 1.08

$$-\frac{c}{4 (b x + a)^4 b} - \frac{d}{3 (b x + a)^3 b^2} + \frac{a d}{4 (b x + a)^4 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)^5,x, algorithm="giac")`

[Out] $-1/4*c/((b*x + a)^4*b) - 1/3*d/((b*x + a)^3*b^2) + 1/4*a*d/((b*x + a)^4*b^2)$

maple [A] time = 0.00, size = 35, normalized size = 0.92

$$-\frac{d}{3 (b x + a)^3 b^2} - \frac{-a d + b c}{4 (b x + a)^4 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)/(b*x+a)^5,x)`

[Out] $-1/3*d/b^2/(b*x+a)^3 - 1/4*(-a*d+b*c)/b^2/(b*x+a)^4$

maxima [A] time = 1.39, size = 61, normalized size = 1.61

$$-\frac{4 b d x + 3 b c + a d}{12 \left(b^6 x^4 + 4 a b^5 x^3 + 6 a^2 b^4 x^2 + 4 a^3 b^3 x + a^4 b^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(b*x+a)^5,x, algorithm="maxima")`

[Out] $-1/12*(4*b*d*x + 3*b*c + a*d)/(b^6*x^4 + 4*a*b^5*x^3 + 6*a^2*b^4*x^2 + 4*a^3*b^3*x + a^4*b^2)$

mupad [B] time = 0.04, size = 63, normalized size = 1.66

$$-\frac{\frac{ad+3bc}{12b^2} + \frac{dx}{3b}}{a^4 + 4a^3bx + 6a^2b^2x^2 + 4ab^3x^3 + b^4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)/(a + b*x)^5, x)

[Out] -((a*d + 3*b*c)/(12*b^2) + (d*x)/(3*b))/(a^4 + b^4*x^4 + 4*a*b^3*x^3 + 6*a^2*b^2*x^2 + 4*a^3*b*x)

sympy [B] time = 0.43, size = 65, normalized size = 1.71

$$\frac{-ad - 3bc - 4bdx}{12a^4b^2 + 48a^3b^3x + 72a^2b^4x^2 + 48ab^5x^3 + 12b^6x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(b*x+a)**5, x)

[Out] (-a*d - 3*b*c - 4*b*d*x)/(12*a**4*b**2 + 48*a**3*b**3*x + 72*a**2*b**4*x**2 + 48*a*b**5*x**3 + 12*b**6*x**4)

3.1246 $\int (a + bx)^4 (c + dx)^2 dx$

Optimal. Leaf size=65

$$\frac{d(a + bx)^6(bc - ad)}{3b^3} + \frac{(a + bx)^5(bc - ad)^2}{5b^3} + \frac{d^2(a + bx)^7}{7b^3}$$

[Out] $1/5*(-a*d+b*c)^2*(b*x+a)^5/b^3+1/3*d*(-a*d+b*c)*(b*x+a)^6/b^3+1/7*d^2*(b*x+a)^7/b^3$

Rubi [A] time = 0.09, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{d(a + bx)^6(bc - ad)}{3b^3} + \frac{(a + bx)^5(bc - ad)^2}{5b^3} + \frac{d^2(a + bx)^7}{7b^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4*(c + d*x)^2,x]

[Out] $((b*c - a*d)^2*(a + b*x)^5)/(5*b^3) + (d*(b*c - a*d)*(a + b*x)^6)/(3*b^3) + (d^2*(a + b*x)^7)/(7*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^4 (c + dx)^2 dx &= \int \left(\frac{(bc - ad)^2 (a + bx)^4}{b^2} + \frac{2d(bc - ad)(a + bx)^5}{b^2} + \frac{d^2 (a + bx)^6}{b^2} \right) dx \\ &= \frac{(bc - ad)^2 (a + bx)^5}{5b^3} + \frac{d(bc - ad)(a + bx)^6}{3b^3} + \frac{d^2 (a + bx)^7}{7b^3} \end{aligned}$$

Mathematica [B] time = 0.03, size = 148, normalized size = 2.28

$$a^4 c^2 x + a^3 c x^2 (ad + 2bc) + \frac{1}{5} b^2 x^5 (6a^2 d^2 + 8abcd + b^2 c^2) + abx^4 (a^2 d^2 + 3abcd + b^2 c^2) + \frac{1}{3} a^2 x^3 (a^2 d^2 + 8abcd + 6b^2 c^2)$$

$d^2+8a^3b^2c^2d+6a^2b^2c^2d^2)x^3+1/2*(2a^4c^2d+4a^3b^2c^2d^2)x^2+a^4c^2d^2x$

maxima [B] time = 1.36, size = 156, normalized size = 2.40

$$\frac{1}{7} b^4 d^2 x^7 + a^4 c^2 x + \frac{1}{3} (b^4 c d + 2 a b^3 d^2) x^6 + \frac{1}{5} (b^4 c^2 + 8 a b^3 c d + 6 a^2 b^2 d^2) x^5 + (a b^3 c^2 + 3 a^2 b^2 c d + a^3 b d^2) x^4 + \frac{1}{3} (6 a^2 b^4 c^2 d + 8 a^3 b^3 c^2 d^2 + 6 a^4 b^2 c^2 d^2) x^3 + (2 a^3 b^3 c^2 d + a^4 b^2 c^2 d^2) x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^2,x, algorithm="maxima")

[Out] 1/7*b^4*d^2*x^7 + a^4*c^2*x + 1/3*(b^4*c*d + 2*a*b^3*d^2)*x^6 + 1/5*(b^4*c^2 + 8*a*b^3*c*d + 6*a^2*b^2*d^2)*x^5 + (a*b^3*c^2 + 3*a^2*b^2*c*d + a^3*b*d^2)*x^4 + 1/3*(6*a^2*b^2*c^2 + 8*a^3*b*c*d + a^4*d^2)*x^3 + (2*a^3*b*c^2 + a^4*c*d)*x^2

mupad [B] time = 0.07, size = 144, normalized size = 2.22

$$x^3 \left(\frac{a^4 d^2}{3} + \frac{8 a^3 b c d}{3} + 2 a^2 b^2 c^2 \right) + x^5 \left(\frac{6 a^2 b^2 d^2}{5} + \frac{8 a b^3 c d}{5} + \frac{b^4 c^2}{5} \right) + a^4 c^2 x + \frac{b^4 d^2 x^7}{7} + a^3 c x^2 (a d + 2 b c) + \frac{1}{3} (6 a^2 b^4 c^2 d + 8 a^3 b^3 c^2 d^2 + 6 a^4 b^2 c^2 d^2) x^3 + (2 a^3 b^3 c^2 d + a^4 b^2 c^2 d^2) x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^4*(c + d*x)^2,x)

[Out] x^3*((a^4*d^2)/3 + 2*a^2*b^2*c^2 + (8*a^3*b*c*d)/3) + x^5*((b^4*c^2)/5 + (6*a^2*b^2*d^2)/5 + (8*a*b^3*c*d)/5) + a^4*c^2*x + (b^4*d^2*x^7)/7 + a^3*c*x^2*(a*d + 2*b*c) + (b^3*d*x^6*(2*a*d + b*c))/3 + a*b*x^4*(a^2*d^2 + b^2*c^2 + 3*a*b*c*d)

sympy [B] time = 0.10, size = 168, normalized size = 2.58

$$a^4 c^2 x + \frac{b^4 d^2 x^7}{7} + x^6 \left(\frac{2 a b^3 d^2}{3} + \frac{b^4 c d}{3} \right) + x^5 \left(\frac{6 a^2 b^2 d^2}{5} + \frac{8 a b^3 c d}{5} + \frac{b^4 c^2}{5} \right) + x^4 (a^3 b d^2 + 3 a^2 b^2 c d + a b^3 c^2) + x^3 \left(\frac{a^4 d^2}{3} + \frac{8 a^2 b^4 c^2 d}{3} + \frac{8 a^3 b^3 c^2 d^2}{3} + \frac{6 a^4 b^2 c^2 d^2}{3} \right) x^3 + (2 a^3 b^3 c^2 d + a^4 b^2 c^2 d^2) x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4*(d*x+c)**2,x)

[Out] a**4*c**2*x + b**4*d**2*x**7/7 + x**6*(2*a*b**3*d**2/3 + b**4*c*d/3) + x**5*(6*a**2*b**2*d**2/5 + 8*a*b**3*c*d/5 + b**4*c**2/5) + x**4*(a**3*b*d**2 + 3*a**2*b**2*c*d + a*b**3*c**2) + x**3*(a**4*d**2/3 + 8*a**3*b*c*d/3 + 2*a**2*b**2*c**2) + x**2*(a**4*c*d + 2*a**3*b*c**2)

3.1247 $\int (a + bx)^3 (c + dx)^2 dx$

Optimal. Leaf size=65

$$\frac{2d(a + bx)^5(bc - ad)}{5b^3} + \frac{(a + bx)^4(bc - ad)^2}{4b^3} + \frac{d^2(a + bx)^6}{6b^3}$$

[Out] $1/4*(-a*d+b*c)^2*(b*x+a)^4/b^3+2/5*d*(-a*d+b*c)*(b*x+a)^5/b^3+1/6*d^2*(b*x+a)^6/b^3$

Rubi [A] time = 0.06, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{2d(a + bx)^5(bc - ad)}{5b^3} + \frac{(a + bx)^4(bc - ad)^2}{4b^3} + \frac{d^2(a + bx)^6}{6b^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3*(c + d*x)^2, x]

[Out] $((b*c - a*d)^2*(a + b*x)^4)/(4*b^3) + (2*d*(b*c - a*d)*(a + b*x)^5)/(5*b^3) + (d^2*(a + b*x)^6)/(6*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^3 (c + dx)^2 dx &= \int \left(\frac{(bc - ad)^2 (a + bx)^3}{b^2} + \frac{2d(bc - ad)(a + bx)^4}{b^2} + \frac{d^2 (a + bx)^5}{b^2} \right) dx \\ &= \frac{(bc - ad)^2 (a + bx)^4}{4b^3} + \frac{2d(bc - ad)(a + bx)^5}{5b^3} + \frac{d^2 (a + bx)^6}{6b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 122, normalized size = 1.88

$$a^3 c^2 x + \frac{1}{4} b x^4 (3 a^2 d^2 + 6 a b c d + b^2 c^2) + \frac{1}{3} a x^3 (a^2 d^2 + 6 a b c d + 3 b^2 c^2) + \frac{1}{2} a^2 c x^2 (2 a d + 3 b c) + \frac{1}{5} b^2 d x^5 (3 a d + 2 b c) + \frac{1}{6} b^3 d^2 x^6$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3*(c + d*x)^2,x]

[Out] $a^3c^2x + (a^2c*(3b^2c + 2ad)*x^2)/2 + (a*(3b^2c^2 + 6ab^2cd + a^2d^2)*x^3)/3 + (b*(b^2c^2 + 6ab^2cd + 3a^2d^2)*x^4)/4 + (b^2d*(2b^2c + 3ad)*x^5)/5 + (b^3d^2*x^6)/6$

fricas [B] time = 0.38, size = 130, normalized size = 2.00

$$\frac{1}{6}x^6d^2b^3 + \frac{2}{5}x^5dcb^3 + \frac{3}{5}x^5d^2b^2a + \frac{1}{4}x^4c^2b^3 + \frac{3}{2}x^4dcb^2a + \frac{3}{4}x^4d^2ba^2 + x^3c^2b^2a + 2x^3dcb^2a + \frac{1}{3}x^3d^2a^3 + \frac{3}{2}x^2c^2ba^2 + x^2dca^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^2,x, algorithm="fricas")

[Out] $1/6*x^6*d^2*b^3 + 2/5*x^5*d*c*b^3 + 3/5*x^5*d^2*b^2*a + 1/4*x^4*c^2*b^3 + 3/2*x^4*d*c*b^2*a + 3/4*x^4*d^2*b*a^2 + x^3*c^2*b^2*a + 2*x^3*d*c*b*a^2 + 1/3*x^3*d^2*a^3 + 3/2*x^2*c^2*b*a^2 + x^2*d*c*a^3 + x*c^2*a^3$

giac [B] time = 1.13, size = 130, normalized size = 2.00

$$\frac{1}{6}b^3d^2x^6 + \frac{2}{5}b^3cdx^5 + \frac{3}{5}ab^2d^2x^5 + \frac{1}{4}b^3c^2x^4 + \frac{3}{2}ab^2cdx^4 + \frac{3}{4}a^2bd^2x^4 + ab^2c^2x^3 + 2a^2bcdx^3 + \frac{1}{3}a^3d^2x^3 + \frac{3}{2}a^2bc^2x^2 + a^3c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^2,x, algorithm="giac")

[Out] $1/6*b^3*d^2*x^6 + 2/5*b^3*c*d*x^5 + 3/5*a*b^2*d^2*x^5 + 1/4*b^3*c^2*x^4 + 3/2*a*b^2*c*d*x^4 + 3/4*a^2*b*d^2*x^4 + a*b^2*c^2*x^3 + 2*a^2*b*c*d*x^3 + 1/3*a^3*d^2*x^3 + 3/2*a^2*b*c^2*x^2 + a^3*c*d*x^2 + a^3*c^2*x$

maple [B] time = 0.00, size = 125, normalized size = 1.92

$$\frac{b^3d^2x^6}{6} + a^3c^2x + \frac{(3ab^2d^2 + 2b^3cd)x^5}{5} + \frac{(3a^2bd^2 + 6ab^2cd + b^3c^2)x^4}{4} + \frac{(a^3d^2 + 6a^2bcd + 3ab^2c^2)x^3}{3} + \frac{(2a^3cd + 3a^2b^2c^2)x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3*(d*x+c)^2,x)

[Out] $1/6*b^3*d^2*x^6 + 1/5*(3a*b^2*d^2 + 2*b^3*c*d)*x^5 + 1/4*(3a^2*b*d^2 + 6a*b^2*c*d + b^3*c^2)*x^4 + 1/3*(a^3*d^2 + 6a^2*b*c*d + 3a*b^2*c^2)*x^3 + 1/2*(2a^3*c*d + 3a^2*b*c^2)*x^2 + a^3*c^2*x$

maxima [B] time = 1.34, size = 124, normalized size = 1.91

$$\frac{1}{6} b^3 d^2 x^6 + a^3 c^2 x + \frac{1}{5} (2 b^3 c d + 3 a b^2 d^2) x^5 + \frac{1}{4} (b^3 c^2 + 6 a b^2 c d + 3 a^2 b d^2) x^4 + \frac{1}{3} (3 a b^2 c^2 + 6 a^2 b c d + a^3 d^2) x^3 + \frac{1}{2} (3 a^3 c^2 d + 6 a^2 b c^2 d + 3 a^2 b^2 c d^2) x^2 + \frac{1}{4} (a^3 c^2 d^2 + 3 a^2 b c^2 d + 3 a^2 b^2 c d^2) x + \frac{1}{6} (a^3 c^2 d^2 + 3 a^2 b c^2 d + 3 a^2 b^2 c d^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^2,x, algorithm="maxima")

[Out] 1/6*b^3*d^2*x^6 + a^3*c^2*x + 1/5*(2*b^3*c*d + 3*a*b^2*d^2)*x^5 + 1/4*(b^3*c^2 + 6*a*b^2*c*d + 3*a^2*b*d^2)*x^4 + 1/3*(3*a*b^2*c^2 + 6*a^2*b*c*d + a^3*d^2)*x^3 + 1/2*(3*a^2*b*c^2 + 2*a^3*c*d)*x^2

mupad [B] time = 0.05, size = 115, normalized size = 1.77

$$x^3 \left(\frac{a^3 d^2}{3} + 2 a^2 b c d + a b^2 c^2 \right) + x^4 \left(\frac{3 a^2 b d^2}{4} + \frac{3 a b^2 c d}{2} + \frac{b^3 c^2}{4} \right) + a^3 c^2 x + \frac{b^3 d^2 x^6}{6} + \frac{a^2 c x^2 (2 a d + 3 b c)}{2} + \frac{b^2 d x^5}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3*(c + d*x)^2,x)

[Out] x^3*((a^3*d^2)/3 + a*b^2*c^2 + 2*a^2*b*c*d) + x^4*((b^3*c^2)/4 + (3*a^2*b*d^2)/4 + (3*a*b^2*c*d)/2) + a^3*c^2*x + (b^3*d^2*x^6)/6 + (a^2*c*x^2*(2*a*d + 3*b*c))/2 + (b^2*d*x^5*(3*a*d + 2*b*c))/5

sympy [B] time = 0.09, size = 133, normalized size = 2.05

$$a^3 c^2 x + \frac{b^3 d^2 x^6}{6} + x^5 \left(\frac{3 a b^2 d^2}{5} + \frac{2 b^3 c d}{5} \right) + x^4 \left(\frac{3 a^2 b d^2}{4} + \frac{3 a b^2 c d}{2} + \frac{b^3 c^2}{4} \right) + x^3 \left(\frac{a^3 d^2}{3} + 2 a^2 b c d + a b^2 c^2 \right) + x^2 \left(a^3 c d + \frac{3 a^2 b c^2 d}{2} + \frac{3 a^2 b^2 c d^2}{2} \right) + \frac{1}{4} (a^3 c^2 d^2 + 3 a^2 b c^2 d + 3 a^2 b^2 c d^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3*(d*x+c)**2,x)

[Out] a**3*c**2*x + b**3*d**2*x**6/6 + x**5*(3*a*b**2*d**2/5 + 2*b**3*c*d/5) + x**4*(3*a**2*b*d**2/4 + 3*a*b**2*c*d/2 + b**3*c**2/4) + x**3*(a**3*d**2/3 + 2*a**2*b*c*d + a*b**2*c**2) + x**2*(a**3*c*d + 3*a**2*b*c**2/2)

3.1248 $\int (a + bx)^2(c + dx)^2 dx$

Optimal. Leaf size=65

$$\frac{d(a + bx)^4(bc - ad)}{2b^3} + \frac{(a + bx)^3(bc - ad)^2}{3b^3} + \frac{d^2(a + bx)^5}{5b^3}$$

[Out] $\frac{1}{3}(-a*d+b*c)^2*(b*x+a)^3/b^3 + \frac{1}{2}*d*(-a*d+b*c)*(b*x+a)^4/b^3 + \frac{1}{5}*d^2*(b*x+a)^5/b^3$

Rubi [A] time = 0.05, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{d(a + bx)^4(bc - ad)}{2b^3} + \frac{(a + bx)^3(bc - ad)^2}{3b^3} + \frac{d^2(a + bx)^5}{5b^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(c + d*x)^2, x]

[Out] $((b*c - a*d)^2*(a + b*x)^3)/(3*b^3) + (d*(b*c - a*d)*(a + b*x)^4)/(2*b^3) + (d^2*(a + b*x)^5)/(5*b^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2(c + dx)^2 dx &= \int \left(\frac{(bc - ad)^2(a + bx)^2}{b^2} + \frac{2d(bc - ad)(a + bx)^3}{b^2} + \frac{d^2(a + bx)^4}{b^2} \right) dx \\ &= \frac{(bc - ad)^2(a + bx)^3}{3b^3} + \frac{d(bc - ad)(a + bx)^4}{2b^3} + \frac{d^2(a + bx)^5}{5b^3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 79, normalized size = 1.22

$$\frac{1}{3}x^3(a^2d^2 + 4abcd + b^2c^2) + a^2c^2x + \frac{1}{2}bdx^4(ad + bc) + acx^2(ad + bc) + \frac{1}{5}b^2d^2x^5$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(c + d*x)^2,x]

[Out] $a^2c^2x + ac*(b*c + a*d)*x^2 + ((b^2*c^2 + 4*a*b*c*d + a^2*d^2)*x^3)/3 + (b*d*(b*c + a*d)*x^4)/2 + (b^2*d^2*x^5)/5$

fricas [A] time = 0.38, size = 89, normalized size = 1.37

$$\frac{1}{5}x^5d^2b^2 + \frac{1}{2}x^4dcb^2 + \frac{1}{2}x^4d^2ba + \frac{1}{3}x^3c^2b^2 + \frac{4}{3}x^3dcba + \frac{1}{3}x^3d^2a^2 + x^2c^2ba + x^2dca^2 + xc^2a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^2,x, algorithm="fricas")

[Out] $1/5*x^5*d^2*b^2 + 1/2*x^4*d*c*b^2 + 1/2*x^4*d^2*b*a + 1/3*x^3*c^2*b^2 + 4/3*x^3*d*c*b*a + 1/3*x^3*d^2*a^2 + x^2*c^2*b*a + x^2*d*c*a^2 + x*c^2*a^2$

giac [A] time = 0.80, size = 89, normalized size = 1.37

$$\frac{1}{5}b^2d^2x^5 + \frac{1}{2}b^2cdx^4 + \frac{1}{2}abd^2x^4 + \frac{1}{3}b^2c^2x^3 + \frac{4}{3}abcdx^3 + \frac{1}{3}a^2d^2x^3 + abc^2x^2 + a^2cdx^2 + a^2c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^2,x, algorithm="giac")

[Out] $1/5*b^2*d^2*x^5 + 1/2*b^2*c*d*x^4 + 1/2*a*b*d^2*x^4 + 1/3*b^2*c^2*x^3 + 4/3*a*b*c*d*x^3 + 1/3*a^2*d^2*x^3 + a*b*c^2*x^2 + a^2*c*d*x^2 + a^2*c^2*x$

maple [A] time = 0.00, size = 87, normalized size = 1.34

$$\frac{b^2d^2x^5}{5} + a^2c^2x + \frac{(2abd^2 + 2b^2cd)x^4}{4} + \frac{(a^2d^2 + 4abcd + b^2c^2)x^3}{3} + \frac{(2a^2cd + 2abc^2)x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(d*x+c)^2,x)

[Out] $1/5*b^2*d^2*x^5 + 1/4*(2*a*b*d^2 + 2*b^2*c*d)*x^4 + 1/3*(a^2*d^2 + 4*a*b*c*d + b^2*c^2)*x^3 + 1/2*(2*a^2*c*d + 2*a*b*c^2)*x^2 + a^2*c^2*x$

maxima [A] time = 1.34, size = 81, normalized size = 1.25

$$\frac{1}{5}b^2d^2x^5 + a^2c^2x + \frac{1}{2}(b^2cd + abd^2)x^4 + \frac{1}{3}(b^2c^2 + 4abcd + a^2d^2)x^3 + (abc^2 + a^2cd)x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^2,x, algorithm="maxima")

[Out] $1/5*b^2*d^2*x^5 + a^2*c^2*x + 1/2*(b^2*c*d + a*b*d^2)*x^4 + 1/3*(b^2*c^2 + 4*a*b*c*d + a^2*d^2)*x^3 + (a*b*c^2 + a^2*c*d)*x^2$

mupad [B] time = 0.17, size = 74, normalized size = 1.14

$$x^3 \left(\frac{a^2 d^2}{3} + \frac{4 a b c d}{3} + \frac{b^2 c^2}{3} \right) + a^2 c^2 x + \frac{b^2 d^2 x^5}{5} + a c x^2 (a d + b c) + \frac{b d x^4 (a d + b c)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2*(c + d*x)^2,x)

[Out] $x^3*((a^2*d^2)/3 + (b^2*c^2)/3 + (4*a*b*c*d)/3) + a^2*c^2*x + (b^2*d^2*x^5)/5 + a*c*x^2*(a*d + b*c) + (b*d*x^4*(a*d + b*c))/2$

sympy [A] time = 0.08, size = 87, normalized size = 1.34

$$a^2 c^2 x + \frac{b^2 d^2 x^5}{5} + x^4 \left(\frac{a b d^2}{2} + \frac{b^2 c d}{2} \right) + x^3 \left(\frac{a^2 d^2}{3} + \frac{4 a b c d}{3} + \frac{b^2 c^2}{3} \right) + x^2 (a^2 c d + a b c^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2*(d*x+c)**2,x)

[Out] $a**2*c**2*x + b**2*d**2*x**5/5 + x**4*(a*b*d**2/2 + b**2*c*d/2) + x**3*(a**2*d**2/3 + 4*a*b*c*d/3 + b**2*c**2/3) + x**2*(a**2*c*d + a*b*c**2)$

3.1249 $\int (a + bx)(c + dx)^2 dx$

Optimal. Leaf size=38

$$\frac{b(c + dx)^4}{4d^2} - \frac{(c + dx)^3(bc - ad)}{3d^2}$$

[Out] $-1/3*(-a*d+b*c)*(d*x+c)^3/d^2+1/4*b*(d*x+c)^4/d^2$

Rubi [A] time = 0.03, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{b(c + dx)^4}{4d^2} - \frac{(c + dx)^3(bc - ad)}{3d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(c + d*x)^2, x]

[Out] $-((b*c - a*d)*(c + d*x)^3)/(3*d^2) + (b*(c + d*x)^4)/(4*d^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)(c + dx)^2 dx &= \int \left(\frac{(-bc + ad)(c + dx)^2}{d} + \frac{b(c + dx)^3}{d} \right) dx \\ &= -\frac{(bc - ad)(c + dx)^3}{3d^2} + \frac{b(c + dx)^4}{4d^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 47, normalized size = 1.24

$$\frac{1}{12}x(4dx^2(ad + 2bc) + 6cx(2ad + bc) + 12ac^2 + 3bd^2x^3)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(c + d*x)^2, x]

[Out] $(x*(12*a*c^2 + 6*c*(b*c + 2*a*d))*x + 4*d*(2*b*c + a*d)*x^2 + 3*b*d^2*x^3))/12$

fricas [A] time = 0.39, size = 49, normalized size = 1.29

$$\frac{1}{4}x^4d^2b + \frac{2}{3}x^3dcb + \frac{1}{3}x^3d^2a + \frac{1}{2}x^2c^2b + x^2dca + xc^2a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c)^2,x, algorithm="fricas")`

[Out] $1/4*x^4*d^2*b + 2/3*x^3*d*c*b + 1/3*x^3*d^2*a + 1/2*x^2*c^2*b + x^2*d*c*a + x*c^2*a$

giac [A] time = 1.03, size = 49, normalized size = 1.29

$$\frac{1}{4}bd^2x^4 + \frac{2}{3}bcdx^3 + \frac{1}{3}ad^2x^3 + \frac{1}{2}bc^2x^2 + acdx^2 + ac^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c)^2,x, algorithm="giac")`

[Out] $1/4*b*d^2*x^4 + 2/3*b*c*d*x^3 + 1/3*a*d^2*x^3 + 1/2*b*c^2*x^2 + a*c*d*x^2 + a*c^2*x$

maple [A] time = 0.00, size = 49, normalized size = 1.29

$$\frac{bd^2x^4}{4} + ac^2x + \frac{(ad^2 + 2bcd)x^3}{3} + \frac{(2acd + bc^2)x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)*(d*x+c)^2,x)`

[Out] $1/4*b*d^2*x^4 + 1/3*(a*d^2 + 2*b*c*d)*x^3 + 1/2*(2*a*c*d + b*c^2)*x^2 + a*c^2*x$

maxima [A] time = 1.31, size = 48, normalized size = 1.26

$$\frac{1}{4}bd^2x^4 + ac^2x + \frac{1}{3}(2bcd + ad^2)x^3 + \frac{1}{2}(bc^2 + 2acd)x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c)^2,x, algorithm="maxima")`

[Out] $1/4*b*d^2*x^4 + a*c^2*x + 1/3*(2*b*c*d + a*d^2)*x^3 + 1/2*(b*c^2 + 2*a*c*d)*x^2$

mupad [B] time = 0.04, size = 47, normalized size = 1.24

$$x^2 \left(\frac{bc^2}{2} + adc \right) + x^3 \left(\frac{ad^2}{3} + \frac{2bcd}{3} \right) + \frac{bd^2x^4}{4} + ac^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)*(c + d*x)^2,x)`

[Out] $x^2*((b*c^2)/2 + a*c*d) + x^3*((a*d^2)/3 + (2*b*c*d)/3) + (b*d^2*x^4)/4 + a*c^2*x$

sympy [A] time = 0.07, size = 49, normalized size = 1.29

$$ac^2x + \frac{bd^2x^4}{4} + x^3 \left(\frac{ad^2}{3} + \frac{2bcd}{3} \right) + x^2 \left(acd + \frac{bc^2}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c)**2,x)`

[Out] $a*c**2*x + b*d**2*x**4/4 + x**3*(a*d**2/3 + 2*b*c*d/3) + x**2*(a*c*d + b*c**2/2)$

3.1250 $\int (c + dx)^2 dx$

Optimal. Leaf size=14

$$\frac{(c + dx)^3}{3d}$$

[Out] 1/3*(d*x+c)^3/d

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(c + dx)^3}{3d}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2,x]

[Out] (c + d*x)^3/(3*d)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (c + dx)^2 dx = \frac{(c + dx)^3}{3d}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{(c + dx)^3}{3d}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2,x]

[Out] (c + d*x)^3/(3*d)

fricas [A] time = 0.41, size = 20, normalized size = 1.43

$$\frac{1}{3}x^3d^2 + x^2dc + xc^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2,x, algorithm="fricas")

[Out] 1/3*x^3*d^2 + x^2*d*c + x*c^2

giac [A] time = 0.96, size = 12, normalized size = 0.86

$$\frac{(dx + c)^3}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2,x, algorithm="giac")

[Out] 1/3*(d*x + c)^3/d

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{(dx + c)^3}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2,x)

[Out] 1/3*(d*x+c)^3/d

maxima [A] time = 1.31, size = 20, normalized size = 1.43

$$\frac{1}{3} d^2 x^3 + c d x^2 + c^2 x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2,x, algorithm="maxima")

[Out] 1/3*d^2*x^3 + c*d*x^2 + c^2*x

mupad [B] time = 0.03, size = 20, normalized size = 1.43

$$c^2 x + c d x^2 + \frac{d^2 x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^2,x)

[Out] c^2*x + (d^2*x^3)/3 + c*d*x^2

sympy [B] time = 0.06, size = 19, normalized size = 1.36

$$c^2x + cdx^2 + \frac{d^2x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**2,x)
```

```
[Out] c**2*x + c*d*x**2 + d**2*x**3/3
```

$$3.1251 \quad \int \frac{(c+dx)^2}{a+bx} dx$$

Optimal. Leaf size=49

$$\frac{(bc-ad)^2 \log(a+bx)}{b^3} + \frac{dx(bc-ad)}{b^2} + \frac{(c+dx)^2}{2b}$$

[Out] $d*(-a*d+b*c)*x/b^2+1/2*(d*x+c)^2/b+(-a*d+b*c)^2*\ln(b*x+a)/b^3$

Rubi [A] time = 0.02, antiderivative size = 49, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{dx(bc-ad)}{b^2} + \frac{(bc-ad)^2 \log(a+bx)}{b^3} + \frac{(c+dx)^2}{2b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2/(a + b*x), x]

[Out] $(d*(b*c - a*d)*x)/b^2 + (c + d*x)^2/(2*b) + ((b*c - a*d)^2*\text{Log}[a + b*x])/b^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^2}{a+bx} dx &= \int \left(\frac{d(bc-ad)}{b^2} + \frac{(bc-ad)^2}{b^2(a+bx)} + \frac{d(c+dx)}{b} \right) dx \\ &= \frac{d(bc-ad)x}{b^2} + \frac{(c+dx)^2}{2b} + \frac{(bc-ad)^2 \log(a+bx)}{b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 43, normalized size = 0.88

$$\frac{bdx(-2ad + 4bc + bdx) + 2(bc - ad)^2 \log(a + bx)}{2b^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2/(a + b*x),x]

[Out] (b*d*x*(4*b*c - 2*a*d + b*d*x) + 2*(b*c - a*d)^2*Log[a + b*x])/(2*b^3)

fricas [A] time = 0.44, size = 63, normalized size = 1.29

$$\frac{b^2 d^2 x^2 + 2(2 b^2 c d - a b d^2) x + 2(b^2 c^2 - 2 a b c d + a^2 d^2) \log(b x + a)}{2 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a),x, algorithm="fricas")

[Out] 1/2*(b^2*d^2*x^2 + 2*(2*b^2*c*d - a*b*d^2)*x + 2*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*log(b*x + a))/b^3

giac [A] time = 1.20, size = 60, normalized size = 1.22

$$\frac{b d^2 x^2 + 4 b c d x - 2 a d^2 x}{2 b^2} + \frac{(b^2 c^2 - 2 a b c d + a^2 d^2) \log(|b x + a|)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a),x, algorithm="giac")

[Out] 1/2*(b*d^2*x^2 + 4*b*c*d*x - 2*a*d^2*x)/b^2 + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*log(abs(b*x + a))/b^3

maple [A] time = 0.00, size = 74, normalized size = 1.51

$$\frac{d^2 x^2}{2 b} + \frac{a^2 d^2 \ln(b x + a)}{b^3} - \frac{2 a c d \ln(b x + a)}{b^2} - \frac{a d^2 x}{b^2} + \frac{c^2 \ln(b x + a)}{b} + \frac{2 c d x}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(b*x+a),x)

[Out] 1/2*d^2/b*x^2-d^2/b^2*a*x+2*d/b*x*c+1/b^3*ln(b*x+a)*a^2*d^2-2/b^2*ln(b*x+a)*a*c*d+1/b*ln(b*x+a)*c^2

maxima [A] time = 1.36, size = 61, normalized size = 1.24

$$\frac{b d^2 x^2 + 2(2 b c d - a d^2) x}{2 b^2} + \frac{(b^2 c^2 - 2 a b c d + a^2 d^2) \log(b x + a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a),x, algorithm="maxima")

[Out] $\frac{1}{2}*(b*d^2*x^2 + 2*(2*b*c*d - a*d^2)*x)/b^2 + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*\log(b*x + a)/b^3$

mupad [B] time = 0.19, size = 62, normalized size = 1.27

$$\frac{\ln(a + bx) (a^2 d^2 - 2 a b c d + b^2 c^2)}{b^3} - x \left(\frac{a d^2}{b^2} - \frac{2 c d}{b} \right) + \frac{d^2 x^2}{2 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^2/(a + b*x), x)`

[Out] $(\log(a + b*x)*(a^2*d^2 + b^2*c^2 - 2*a*b*c*d))/b^3 - x*((a*d^2)/b^2 - (2*c*d)/b) + (d^2*x^2)/(2*b)$

sympy [A] time = 0.22, size = 44, normalized size = 0.90

$$x \left(-\frac{a d^2}{b^2} + \frac{2 c d}{b} \right) + \frac{d^2 x^2}{2 b} + \frac{(a d - b c)^2 \log(a + b x)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**2/(b*x+a), x)`

[Out] $x*(-a*d**2/b**2 + 2*c*d/b) + d**2*x**2/(2*b) + (a*d - b*c)**2*\log(a + b*x)/b**3$

$$3.1252 \quad \int \frac{(c+dx)^2}{(a+bx)^2} dx$$

Optimal. Leaf size=51

$$-\frac{(bc-ad)^2}{b^3(a+bx)} + \frac{2d(bc-ad)\log(a+bx)}{b^3} + \frac{d^2x}{b^2}$$

[Out] $d^2x/b^2 - (-a*d+b*c)^2/b^3/(b*x+a) + 2*d*(-a*d+b*c)*\ln(b*x+a)/b^3$

Rubi [A] time = 0.03, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{(bc-ad)^2}{b^3(a+bx)} + \frac{2d(bc-ad)\log(a+bx)}{b^3} + \frac{d^2x}{b^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2/(a + b*x)^2,x]

[Out] $(d^2*x)/b^2 - (b*c - a*d)^2/(b^3*(a + b*x)) + (2*d*(b*c - a*d)*\text{Log}[a + b*x])/b^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^2}{(a+bx)^2} dx &= \int \left(\frac{d^2}{b^2} + \frac{(bc-ad)^2}{b^2(a+bx)^2} + \frac{2d(bc-ad)}{b^2(a+bx)} \right) dx \\ &= \frac{d^2x}{b^2} - \frac{(bc-ad)^2}{b^3(a+bx)} + \frac{2d(bc-ad)\log(a+bx)}{b^3} \end{aligned}$$

Mathematica [A] time = 0.04, size = 47, normalized size = 0.92

$$-\frac{(bc-ad)^2}{a+bx} + \frac{2d(bc-ad)\log(a+bx) + bd^2x}{b^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2/(a + b*x)^2,x]

[Out] (b*d^2*x - (b*c - a*d)^2/(a + b*x) + 2*d*(b*c - a*d)*Log[a + b*x])/b^3

fricas [A] time = 0.43, size = 92, normalized size = 1.80

$$\frac{b^2 d^2 x^2 + a b d^2 x - b^2 c^2 + 2 a b c d - a^2 d^2 + 2 (a b c d - a^2 d^2 + (b^2 c d - a b d^2) x) \log (b x + a)}{b^4 x + a b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^2,x, algorithm="fricas")

[Out] (b^2*d^2*x^2 + a*b*d^2*x - b^2*c^2 + 2*a*b*c*d - a^2*d^2 + 2*(a*b*c*d - a^2*d^2 + (b^2*c*d - a*b*d^2)*x)*log(b*x + a))/(b^4*x + a*b^3)

giac [A] time = 0.94, size = 98, normalized size = 1.92

$$\frac{(b x + a) d^2}{b^3} - \frac{2 (b c d - a d^2) \log \left(\frac{|b x + a|}{(b x + a)^2 |b|} \right)}{b^3} - \frac{b^3 c^2}{b x + a} - \frac{2 a b^2 c d}{b x + a} + \frac{a^2 b d^2}{b x + a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^2,x, algorithm="giac")

[Out] (b*x + a)*d^2/b^3 - 2*(b*c*d - a*d^2)*log(abs(b*x + a)/((b*x + a)^2*abs(b)))/b^3 - (b^3*c^2/(b*x + a) - 2*a*b^2*c*d/(b*x + a) + a^2*b*d^2/(b*x + a))/b^4

maple [A] time = 0.01, size = 86, normalized size = 1.69

$$-\frac{a^2 d^2}{(b x + a) b^3} + \frac{2 a c d}{(b x + a) b^2} - \frac{2 a d^2 \ln (b x + a)}{b^3} - \frac{c^2}{(b x + a) b} + \frac{2 c d \ln (b x + a)}{b^2} + \frac{d^2 x}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(b*x+a)^2,x)

[Out] d^2*x/b^2-2/b^3*d^2*ln(b*x+a)*a+2/b^2*d*ln(b*x+a)*c-1/b^3/(b*x+a)*a^2*d^2+2/b^2/(b*x+a)*a*c*d-1/b/(b*x+a)*c^2

maxima [A] time = 1.37, size = 67, normalized size = 1.31

$$\frac{d^2 x}{b^2} - \frac{b^2 c^2 - 2 a b c d + a^2 d^2}{b^4 x + a b^3} + \frac{2 (b c d - a d^2) \log (b x + a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^2,x, algorithm="maxima")

[Out] $d^2x/b^2 - (b^2c^2 - 2*ab*cd + a^2d^2)/(b^4x + ab^3) + 2*(b*cd - a*d^2)*\log(b*x + a)/b^3$

mupad [B] time = 0.20, size = 71, normalized size = 1.39

$$\frac{d^2x}{b^2} - \frac{a^2d^2 - 2abcd + b^2c^2}{b(xb^3 + ab^2)} - \frac{\ln(a + bx)(2ad^2 - 2bcd)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^2/(a + b*x)^2,x)

[Out] $(d^2x)/b^2 - (a^2d^2 + b^2c^2 - 2*ab*cd)/(b*(a*b^2 + b^3*x)) - (\log(a + b*x)*(2*a*d^2 - 2*b*cd))/b^3$

sympy [A] time = 0.34, size = 60, normalized size = 1.18

$$\frac{-a^2d^2 + 2abcd - b^2c^2}{ab^3 + b^4x} + \frac{d^2x}{b^2} - \frac{2d(ad - bc)\log(a + bx)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2/(b*x+a)**2,x)

[Out] $(-a**2*d**2 + 2*a*b*c*d - b**2*c**2)/(a*b**3 + b**4*x) + d**2*x/b**2 - 2*d*(a*d - b*c)*\log(a + b*x)/b**3$

$$3.1253 \quad \int \frac{(c+dx)^2}{(a+bx)^3} dx$$

Optimal. Leaf size=59

$$-\frac{2d(bc-ad)}{b^3(a+bx)} - \frac{(bc-ad)^2}{2b^3(a+bx)^2} + \frac{d^2 \log(a+bx)}{b^3}$$

[Out] $-1/2*(-a*d+b*c)^2/b^3/(b*x+a)^2-2*d*(-a*d+b*c)/b^3/(b*x+a)+d^2*\ln(b*x+a)/b^3$

Rubi [A] time = 0.04, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{2d(bc-ad)}{b^3(a+bx)} - \frac{(bc-ad)^2}{2b^3(a+bx)^2} + \frac{d^2 \log(a+bx)}{b^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2/(a + b*x)^3, x]

[Out] $-(b*c - a*d)^2/(2*b^3*(a + b*x)^2) - (2*d*(b*c - a*d))/(b^3*(a + b*x)) + (d^2*\text{Log}[a + b*x])/b^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^2}{(a+bx)^3} dx &= \int \left(\frac{(bc-ad)^2}{b^2(a+bx)^3} + \frac{2d(bc-ad)}{b^2(a+bx)^2} + \frac{d^2}{b^2(a+bx)} \right) dx \\ &= -\frac{(bc-ad)^2}{2b^3(a+bx)^2} - \frac{2d(bc-ad)}{b^3(a+bx)} + \frac{d^2 \log(a+bx)}{b^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 49, normalized size = 0.83

$$\frac{2d^2 \log(a+bx) - \frac{(bc-ad)(3ad+b(c+4dx))}{(a+bx)^2}}{2b^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2/(a + b*x)^3,x]

[Out] $(-(((b*c - a*d)*(3*a*d + b*(c + 4*d*x)))/(a + b*x)^2) + 2*d^2*\text{Log}[a + b*x])/ (2*b^3)$

fricas [A] time = 0.42, size = 99, normalized size = 1.68

$$\frac{b^2c^2 + 2abcd - 3a^2d^2 + 4(b^2cd - abd^2)x - 2(b^2d^2x^2 + 2abd^2x + a^2d^2) \log(bx + a)}{2(b^5x^2 + 2ab^4x + a^2b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^3,x, algorithm="fricas")

[Out] $-1/2*(b^2*c^2 + 2*a*b*c*d - 3*a^2*d^2 + 4*(b^2*c*d - a*b*d^2)*x - 2*(b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*\log(b*x + a))/(b^5*x^2 + 2*a*b^4*x + a^2*b^3)$

giac [A] time = 1.03, size = 68, normalized size = 1.15

$$\frac{d^2 \log(|bx + a|)}{b^3} - \frac{4(bcd - ad^2)x + \frac{b^2c^2 + 2abcd - 3a^2d^2}{b}}{2(bx + a)^2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^3,x, algorithm="giac")

[Out] $d^2*\log(\text{abs}(b*x + a))/b^3 - 1/2*(4*(b*c*d - a*d^2)*x + (b^2*c^2 + 2*a*b*c*d - 3*a^2*d^2)/b)/((b*x + a)^2*b^2)$

maple [A] time = 0.01, size = 92, normalized size = 1.56

$$-\frac{a^2d^2}{2(bx + a)^2b^3} + \frac{acd}{(bx + a)^2b^2} - \frac{c^2}{2(bx + a)^2b} + \frac{2ad^2}{(bx + a)b^3} - \frac{2cd}{(bx + a)b^2} + \frac{d^2 \ln(bx + a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(b*x+a)^3,x)

[Out] $-1/2/b^3/(b*x+a)^2*a^2*d^2+1/b^2/(b*x+a)^2*a*c*d-1/2/b/(b*x+a)^2*c^2+d^2*\ln(b*x+a)/b^3+2/b^3*d^2/(b*x+a)*a-2/b^2*d/(b*x+a)*c$

maxima [A] time = 1.30, size = 79, normalized size = 1.34

$$-\frac{b^2c^2 + 2abcd - 3a^2d^2 + 4(b^2cd - abd^2)x}{2(b^5x^2 + 2ab^4x + a^2b^3)} + \frac{d^2 \log(bx + a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^3,x, algorithm="maxima")

[Out] $-1/2*(b^2*c^2 + 2*a*b*c*d - 3*a^2*d^2 + 4*(b^2*c*d - a*b*d^2)*x)/(b^5*x^2 + 2*a*b^4*x + a^2*b^3) + d^2*\log(b*x + a)/b^3$

mupad [B] time = 0.20, size = 77, normalized size = 1.31

$$\frac{d^2 \ln(a + bx)}{b^3} - \frac{-3a^2d^2 + 2abcd + b^2c^2}{2b^3} - \frac{2dx(ad - bc)}{b^2}$$

$$\frac{d^2 \ln(a + bx)}{b^3} - \frac{-3a^2d^2 + 2abcd + b^2c^2}{a^2 + 2abx + b^2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^2/(a + b*x)^3,x)

[Out] $(d^2*\log(a + b*x))/b^3 - ((b^2*c^2 - 3*a^2*d^2 + 2*a*b*c*d)/(2*b^3) - (2*d*x*(a*d - b*c))/b^2)/(a^2 + b^2*x^2 + 2*a*b*x)$

sympy [A] time = 0.45, size = 80, normalized size = 1.36

$$\frac{3a^2d^2 - 2abcd - b^2c^2 + x(4abd^2 - 4b^2cd)}{2a^2b^3 + 4ab^4x + 2b^5x^2} + \frac{d^2 \log(a + bx)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2/(b*x+a)**3,x)

[Out] $(3*a**2*d**2 - 2*a*b*c*d - b**2*c**2 + x*(4*a*b*d**2 - 4*b**2*c*d))/(2*a**2*b**3 + 4*a*b**4*x + 2*b**5*x**2) + d**2*\log(a + b*x)/b**3$

$$3.1254 \quad \int \frac{(c+dx)^2}{(a+bx)^4} dx$$

Optimal. Leaf size=28

$$-\frac{(c+dx)^3}{3(a+bx)^3(bc-ad)}$$

[Out] $-1/3*(d*x+c)^3/(-a*d+b*c)/(b*x+a)^3$

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$-\frac{(c+dx)^3}{3(a+bx)^3(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^2/(a + b*x)^4, x]$

[Out] $-(c + d*x)^3/(3*(b*c - a*d)*(a + b*x)^3)$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] \rightarrow \text{Simp} [((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}[\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{(c+dx)^2}{(a+bx)^4} dx = -\frac{(c+dx)^3}{3(bc-ad)(a+bx)^3}$$

Mathematica [A] time = 0.02, size = 53, normalized size = 1.89

$$-\frac{a^2d^2 + abd(c + 3dx) + b^2(c^2 + 3cdx + 3d^2x^2)}{3b^3(a+bx)^3}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(c + d*x)^2/(a + b*x)^4, x]$

[Out] $-1/3*(a^2*d^2 + a*b*d*(c + 3*d*x) + b^2*(c^2 + 3*c*d*x + 3*d^2*x^2))/(b^3*(a + b*x)^3)$

fricas [B] time = 0.41, size = 84, normalized size = 3.00

$$\frac{3b^2d^2x^2 + b^2c^2 + abcd + a^2d^2 + 3(b^2cd + abd^2)x}{3(b^6x^3 + 3ab^5x^2 + 3a^2b^4x + a^3b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^4,x, algorithm="fricas")

[Out] -1/3*(3*b^2*d^2*x^2 + b^2*c^2 + a*b*c*d + a^2*d^2 + 3*(b^2*c*d + a*b*d^2)*x)/(b^6*x^3 + 3*a*b^5*x^2 + 3*a^2*b^4*x + a^3*b^3)

giac [B] time = 0.96, size = 59, normalized size = 2.11

$$\frac{3b^2d^2x^2 + 3b^2cdx + 3abd^2x + b^2c^2 + abcd + a^2d^2}{3(bx+a)^3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^4,x, algorithm="giac")

[Out] -1/3*(3*b^2*d^2*x^2 + 3*b^2*c*d*x + 3*a*b*d^2*x + b^2*c^2 + a*b*c*d + a^2*d^2)/(b*x + a)^3*b^3)

maple [B] time = 0.01, size = 70, normalized size = 2.50

$$-\frac{d^2}{(bx+a)b^3} + \frac{(ad-bc)d}{(bx+a)^2b^3} - \frac{a^2d^2 - 2abcd + b^2c^2}{3(bx+a)^3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(b*x+a)^4,x)

[Out] -1/3*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^3/(b*x+a)^3+d*(a*d-b*c)/b^3/(b*x+a)^2-d^2/b^3/(b*x+a)

maxima [B] time = 1.37, size = 84, normalized size = 3.00

$$\frac{3b^2d^2x^2 + b^2c^2 + abcd + a^2d^2 + 3(b^2cd + abd^2)x}{3(b^6x^3 + 3ab^5x^2 + 3a^2b^4x + a^3b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^4,x, algorithm="maxima")

[Out] $-1/3*(3*b^2*d^2*x^2 + b^2*c^2 + a*b*c*d + a^2*d^2 + 3*(b^2*c*d + a*b*d^2)*x)/(b^6*x^3 + 3*a*b^5*x^2 + 3*a^2*b^4*x + a^3*b^3)$

mupad [B] time = 0.04, size = 80, normalized size = 2.86

$$-\frac{\frac{a^2 d^2 + a b c d + b^2 c^2}{3 b^3} + \frac{d^2 x^2}{b} + \frac{d x (a d + b c)}{b^2}}{a^3 + 3 a^2 b x + 3 a b^2 x^2 + b^3 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^2/(a + b*x)^4,x)`

[Out] $-((a^2*d^2 + b^2*c^2 + a*b*c*d)/(3*b^3) + (d^2*x^2)/b + (d*x*(a*d + b*c))/b^2)/(a^3 + b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x)$

sympy [B] time = 0.60, size = 88, normalized size = 3.14

$$\frac{-a^2 d^2 - a b c d - b^2 c^2 - 3 b^2 d^2 x^2 + x(-3 a b d^2 - 3 b^2 c d)}{3 a^3 b^3 + 9 a^2 b^4 x + 9 a b^5 x^2 + 3 b^6 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**2/(b*x+a)**4,x)`

[Out] $(-a**2*d**2 - a*b*c*d - b**2*c**2 - 3*b**2*d**2*x**2 + x*(-3*a*b*d**2 - 3*b**2*c*d))/(3*a**3*b**3 + 9*a**2*b**4*x + 9*a*b**5*x**2 + 3*b**6*x**3)$

$$3.1255 \quad \int \frac{(c+dx)^2}{(a+bx)^5} dx$$

Optimal. Leaf size=65

$$-\frac{2d(bc-ad)}{3b^3(a+bx)^3} - \frac{(bc-ad)^2}{4b^3(a+bx)^4} - \frac{d^2}{2b^3(a+bx)^2}$$

[Out] $-1/4*(-a*d+b*c)^2/b^3/(b*x+a)^4-2/3*d*(-a*d+b*c)/b^3/(b*x+a)^3-1/2*d^2/b^3/(b*x+a)^2$

Rubi [A] time = 0.03, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{2d(bc-ad)}{3b^3(a+bx)^3} - \frac{(bc-ad)^2}{4b^3(a+bx)^4} - \frac{d^2}{2b^3(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2/(a + b*x)^5, x]

[Out] $-(b*c - a*d)^2/(4*b^3*(a + b*x)^4) - (2*d*(b*c - a*d))/(3*b^3*(a + b*x)^3) - d^2/(2*b^3*(a + b*x)^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^2}{(a+bx)^5} dx &= \int \left(\frac{(bc-ad)^2}{b^2(a+bx)^5} + \frac{2d(bc-ad)}{b^2(a+bx)^4} + \frac{d^2}{b^2(a+bx)^3} \right) dx \\ &= -\frac{(bc-ad)^2}{4b^3(a+bx)^4} - \frac{2d(bc-ad)}{3b^3(a+bx)^3} - \frac{d^2}{2b^3(a+bx)^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 56, normalized size = 0.86

$$-\frac{a^2d^2 + 2abd(c + 2dx) + b^2(3c^2 + 8cdx + 6d^2x^2)}{12b^3(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2/(a + b*x)^5,x]

[Out] $-1/12*(a^2*d^2 + 2*a*b*d*(c + 2*d*x) + b^2*(3*c^2 + 8*c*d*x + 6*d^2*x^2))/(b^3*(a + b*x)^4)$

fricas [A] time = 0.45, size = 98, normalized size = 1.51

$$\frac{6 b^2 d^2 x^2 + 3 b^2 c^2 + 2 a b c d + a^2 d^2 + 4 (2 b^2 c d + a b d^2) x}{12 (b^7 x^4 + 4 a b^6 x^3 + 6 a^2 b^5 x^2 + 4 a^3 b^4 x + a^4 b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^5,x, algorithm="fricas")

[Out] $-1/12*(6*b^2*d^2*x^2 + 3*b^2*c^2 + 2*a*b*c*d + a^2*d^2 + 4*(2*b^2*c*d + a*b*d^2)*x)/(b^7*x^4 + 4*a*b^6*x^3 + 6*a^2*b^5*x^2 + 4*a^3*b^4*x + a^4*b^3)$

giac [A] time = 1.13, size = 96, normalized size = 1.48

$$\frac{\frac{3c^2}{(bx+a)^4} + \frac{8cd}{(bx+a)^3b} - \frac{6acd}{(bx+a)^4b} + \frac{6d^2}{(bx+a)^2b^2} - \frac{8ad^2}{(bx+a)^3b^2} + \frac{3a^2d^2}{(bx+a)^4b^2}}{12b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^5,x, algorithm="giac")

[Out] $-1/12*(3*c^2/(b*x + a)^4 + 8*c*d/((b*x + a)^3*b) - 6*a*c*d/((b*x + a)^4*b) + 6*d^2/((b*x + a)^2*b^2) - 8*a*d^2/((b*x + a)^3*b^2) + 3*a^2*d^2/((b*x + a)^4*b^2))/b$

maple [A] time = 0.01, size = 71, normalized size = 1.09

$$-\frac{d^2}{2(bx+a)^2b^3} + \frac{2(ad-bc)d}{3(bx+a)^3b^3} - \frac{a^2d^2 - 2abcd + b^2c^2}{4(bx+a)^4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(b*x+a)^5,x)

[Out] $2/3*d*(a*d-b*c)/b^3/(b*x+a)^3-1/2*d^2/b^3/(b*x+a)^2-1/4*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^3/(b*x+a)^4$

maxima [A] time = 1.33, size = 98, normalized size = 1.51

$$\frac{6 b^2 d^2 x^2 + 3 b^2 c^2 + 2 a b c d + a^2 d^2 + 4 (2 b^2 c d + a b d^2) x}{12 (b^7 x^4 + 4 a b^6 x^3 + 6 a^2 b^5 x^2 + 4 a^3 b^4 x + a^4 b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^5,x, algorithm="maxima")

[Out] $-1/12*(6*b^2*d^2*x^2 + 3*b^2*c^2 + 2*a*b*c*d + a^2*d^2 + 4*(2*b^2*c*d + a*b*d^2)*x)/(b^7*x^4 + 4*a*b^6*x^3 + 6*a^2*b^5*x^2 + 4*a^3*b^4*x + a^4*b^3)$

mupad [B] time = 0.19, size = 39, normalized size = 0.60

$$\frac{(c + dx)^3 (4ad - 3bc + bdx)}{12(ad - bc)^2 (a + bx)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^2/(a + b*x)^5,x)

[Out] $((c + d*x)^3*(4*a*d - 3*b*c + b*d*x))/(12*(a*d - b*c)^2*(a + b*x)^4)$

sympy [A] time = 0.76, size = 104, normalized size = 1.60

$$\frac{-a^2d^2 - 2abcd - 3b^2c^2 - 6b^2d^2x^2 + x(-4abd^2 - 8b^2cd)}{12a^4b^3 + 48a^3b^4x + 72a^2b^5x^2 + 48ab^6x^3 + 12b^7x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2/(b*x+a)**5,x)

[Out] $(-a**2*d**2 - 2*a*b*c*d - 3*b**2*c**2 - 6*b**2*d**2*x**2 + x*(-4*a*b*d**2 - 8*b**2*c*d))/(12*a**4*b**3 + 48*a**3*b**4*x + 72*a**2*b**5*x**2 + 48*a*b**6*x**3 + 12*b**7*x**4)$

$$3.1256 \quad \int \frac{(c+dx)^2}{(a+bx)^6} dx$$

Optimal. Leaf size=65

$$-\frac{d(bc-ad)}{2b^3(a+bx)^4} - \frac{(bc-ad)^2}{5b^3(a+bx)^5} - \frac{d^2}{3b^3(a+bx)^3}$$

[Out] $-1/5*(-a*d+b*c)^2/b^3/(b*x+a)^5-1/2*d*(-a*d+b*c)/b^3/(b*x+a)^4-1/3*d^2/b^3/(b*x+a)^3$

Rubi [A] time = 0.03, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{d(bc-ad)}{2b^3(a+bx)^4} - \frac{(bc-ad)^2}{5b^3(a+bx)^5} - \frac{d^2}{3b^3(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2/(a + b*x)^6, x]

[Out] $-(b*c - a*d)^2/(5*b^3*(a + b*x)^5) - (d*(b*c - a*d))/(2*b^3*(a + b*x)^4) - d^2/(3*b^3*(a + b*x)^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^2}{(a+bx)^6} dx &= \int \left(\frac{(bc-ad)^2}{b^2(a+bx)^6} + \frac{2d(bc-ad)}{b^2(a+bx)^5} + \frac{d^2}{b^2(a+bx)^4} \right) dx \\ &= -\frac{(bc-ad)^2}{5b^3(a+bx)^5} - \frac{d(bc-ad)}{2b^3(a+bx)^4} - \frac{d^2}{3b^3(a+bx)^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 57, normalized size = 0.88

$$-\frac{a^2d^2 + abd(3c + 5dx) + b^2(6c^2 + 15cdx + 10d^2x^2)}{30b^3(a+bx)^5}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2/(a + b*x)^6,x]

[Out] $-1/30*(a^2*d^2 + a*b*d*(3*c + 5*d*x) + b^2*(6*c^2 + 15*c*d*x + 10*d^2*x^2)) / (b^3*(a + b*x)^5)$

fricas [A] time = 0.41, size = 109, normalized size = 1.68

$$\frac{10 b^2 d^2 x^2 + 6 b^2 c^2 + 3 a b c d + a^2 d^2 + 5 (3 b^2 c d + a b d^2) x}{30 (b^8 x^5 + 5 a b^7 x^4 + 10 a^2 b^6 x^3 + 10 a^3 b^5 x^2 + 5 a^4 b^4 x + a^5 b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^6,x, algorithm="fricas")

[Out] $-1/30*(10*b^2*d^2*x^2 + 6*b^2*c^2 + 3*a*b*c*d + a^2*d^2 + 5*(3*b^2*c*d + a*b*d^2)*x)/(b^8*x^5 + 5*a*b^7*x^4 + 10*a^2*b^6*x^3 + 10*a^3*b^5*x^2 + 5*a^4*b^4*x + a^5*b^3)$

giac [A] time = 0.87, size = 61, normalized size = 0.94

$$\frac{10 b^2 d^2 x^2 + 15 b^2 c d x + 5 a b d^2 x + 6 b^2 c^2 + 3 a b c d + a^2 d^2}{30 (b x + a)^5 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^6,x, algorithm="giac")

[Out] $-1/30*(10*b^2*d^2*x^2 + 15*b^2*c*d*x + 5*a*b*d^2*x + 6*b^2*c^2 + 3*a*b*c*d + a^2*d^2)/((b*x + a)^5*b^3)$

maple [A] time = 0.01, size = 71, normalized size = 1.09

$$-\frac{d^2}{3 (b x + a)^3 b^3} + \frac{(a d - b c) d}{2 (b x + a)^4 b^3} - \frac{a^2 d^2 - 2 a b c d + b^2 c^2}{5 (b x + a)^5 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(b*x+a)^6,x)

[Out] $-1/3*d^2/b^3/(b*x+a)^3-1/5*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^3/(b*x+a)^5+1/2*d*(a*d-b*c)/b^3/(b*x+a)^4$

maxima [A] time = 1.35, size = 109, normalized size = 1.68

$$\frac{10 b^2 d^2 x^2 + 6 b^2 c^2 + 3 a b c d + a^2 d^2 + 5 (3 b^2 c d + a b d^2) x}{30 (b^8 x^5 + 5 a b^7 x^4 + 10 a^2 b^6 x^3 + 10 a^3 b^5 x^2 + 5 a^4 b^4 x + a^5 b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^6,x, algorithm="maxima")

[Out]
$$-1/30*(10*b^2*d^2*x^2 + 6*b^2*c^2 + 3*a*b*c*d + a^2*d^2 + 5*(3*b^2*c*d + a*b*d^2)*x)/(b^8*x^5 + 5*a*b^7*x^4 + 10*a^2*b^6*x^3 + 10*a^3*b^5*x^2 + 5*a^4*b^4*x + a^5*b^3)$$

mupad [B] time = 0.20, size = 107, normalized size = 1.65

$$\frac{\frac{a^2 d^2 + 3 a b c d + 6 b^2 c^2}{30 b^3} + \frac{d^2 x^2}{3 b} + \frac{d x (a d + 3 b c)}{6 b^2}}{a^5 + 5 a^4 b x + 10 a^3 b^2 x^2 + 10 a^2 b^3 x^3 + 5 a b^4 x^4 + b^5 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^2/(a + b*x)^6,x)

[Out]
$$-((a^2*d^2 + 6*b^2*c^2 + 3*a*b*c*d)/(30*b^3) + (d^2*x^2)/(3*b) + (d*x*(a*d + 3*b*c))/(6*b^2))/(a^5 + b^5*x^5 + 5*a*b^4*x^4 + 10*a^3*b^2*x^2 + 10*a^2*b^3*x^3 + 5*a^4*b*x)$$

sympy [B] time = 0.96, size = 116, normalized size = 1.78

$$\frac{-a^2 d^2 - 3 a b c d - 6 b^2 c^2 - 10 b^2 d^2 x^2 + x(-5 a b d^2 - 15 b^2 c d)}{30 a^5 b^3 + 150 a^4 b^4 x + 300 a^3 b^5 x^2 + 300 a^2 b^6 x^3 + 150 a b^7 x^4 + 30 b^8 x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2/(b*x+a)**6,x)

[Out]
$$(-a**2*d**2 - 3*a*b*c*d - 6*b**2*c**2 - 10*b**2*d**2*x**2 + x*(-5*a*b*d**2 - 15*b**2*c*d))/(30*a**5*b**3 + 150*a**4*b**4*x + 300*a**3*b**5*x**2 + 300*a**2*b**6*x**3 + 150*a*b**7*x**4 + 30*b**8*x**5)$$

$$3.1257 \quad \int \frac{(c+dx)^2}{(a+bx)^7} dx$$

Optimal. Leaf size=65

$$-\frac{2d(bc-ad)}{5b^3(a+bx)^5} - \frac{(bc-ad)^2}{6b^3(a+bx)^6} - \frac{d^2}{4b^3(a+bx)^4}$$

[Out] $-1/6*(-a*d+b*c)^2/b^3/(b*x+a)^6-2/5*d*(-a*d+b*c)/b^3/(b*x+a)^5-1/4*d^2/b^3/(b*x+a)^4$

Rubi [A] time = 0.03, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{2d(bc-ad)}{5b^3(a+bx)^5} - \frac{(bc-ad)^2}{6b^3(a+bx)^6} - \frac{d^2}{4b^3(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2/(a + b*x)^7, x]

[Out] $-(b*c - a*d)^2/(6*b^3*(a + b*x)^6) - (2*d*(b*c - a*d))/(5*b^3*(a + b*x)^5) - d^2/(4*b^3*(a + b*x)^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^2}{(a+bx)^7} dx &= \int \left(\frac{(bc-ad)^2}{b^2(a+bx)^7} + \frac{2d(bc-ad)}{b^2(a+bx)^6} + \frac{d^2}{b^2(a+bx)^5} \right) dx \\ &= -\frac{(bc-ad)^2}{6b^3(a+bx)^6} - \frac{2d(bc-ad)}{5b^3(a+bx)^5} - \frac{d^2}{4b^3(a+bx)^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 58, normalized size = 0.89

$$-\frac{a^2d^2 + 2abd(2c + 3dx) + b^2(10c^2 + 24cdx + 15d^2x^2)}{60b^3(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2/(a + b*x)^7,x]

[Out]
$$-1/60*(a^2*d^2 + 2*a*b*d*(2*c + 3*d*x) + b^2*(10*c^2 + 24*c*d*x + 15*d^2*x^2))/(b^3*(a + b*x)^6)$$

fricas [B] time = 0.42, size = 120, normalized size = 1.85

$$\frac{15 b^2 d^2 x^2 + 10 b^2 c^2 + 4 a b c d + a^2 d^2 + 6 (4 b^2 c d + a b d^2) x}{60 (b^9 x^6 + 6 a b^8 x^5 + 15 a^2 b^7 x^4 + 20 a^3 b^6 x^3 + 15 a^4 b^5 x^2 + 6 a^5 b^4 x + a^6 b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^7,x, algorithm="fricas")

[Out]
$$-1/60*(15*b^2*d^2*x^2 + 10*b^2*c^2 + 4*a*b*c*d + a^2*d^2 + 6*(4*b^2*c*d + a*b*d^2)*x)/(b^9*x^6 + 6*a*b^8*x^5 + 15*a^2*b^7*x^4 + 20*a^3*b^6*x^3 + 15*a^4*b^5*x^2 + 6*a^5*b^4*x + a^6*b^3)$$

giac [A] time = 1.04, size = 61, normalized size = 0.94

$$\frac{15 b^2 d^2 x^2 + 24 b^2 c d x + 6 a b d^2 x + 10 b^2 c^2 + 4 a b c d + a^2 d^2}{60 (b x + a)^6 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^7,x, algorithm="giac")

[Out]
$$-1/60*(15*b^2*d^2*x^2 + 24*b^2*c*d*x + 6*a*b*d^2*x + 10*b^2*c^2 + 4*a*b*c*d + a^2*d^2)/((b*x + a)^6*b^3)$$

maple [A] time = 0.00, size = 71, normalized size = 1.09

$$-\frac{d^2}{4 (b x + a)^4 b^3} + \frac{2 (a d - b c) d}{5 (b x + a)^5 b^3} - \frac{a^2 d^2 - 2 a b c d + b^2 c^2}{6 (b x + a)^6 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(b*x+a)^7,x)

[Out]
$$2/5*d*(a*d-b*c)/b^3/(b*x+a)^5-1/4*d^2/b^3/(b*x+a)^4-1/6*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^3/(b*x+a)^6$$

maxima [B] time = 1.39, size = 120, normalized size = 1.85

$$\frac{15 b^2 d^2 x^2 + 10 b^2 c^2 + 4 a b c d + a^2 d^2 + 6 (4 b^2 c d + a b d^2) x}{60 (b^9 x^6 + 6 a b^8 x^5 + 15 a^2 b^7 x^4 + 20 a^3 b^6 x^3 + 15 a^4 b^5 x^2 + 6 a^5 b^4 x + a^6 b^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(b*x+a)^7,x, algorithm="maxima")

[Out]
$$-1/60*(15*b^2*d^2*x^2 + 10*b^2*c^2 + 4*a*b*c*d + a^2*d^2 + 6*(4*b^2*c*d + a*b*d^2)*x)/(b^9*x^6 + 6*a*b^8*x^5 + 15*a^2*b^7*x^4 + 20*a^3*b^6*x^3 + 15*a^4*b^5*x^2 + 6*a^5*b^4*x + a^6*b^3)$$

mupad [B] time = 0.09, size = 118, normalized size = 1.82

$$-\frac{\frac{a^2 d^2 + 4 a b c d + 10 b^2 c^2}{60 b^3} + \frac{d^2 x^2}{4 b} + \frac{d x (a d + 4 b c)}{10 b^2}}{a^6 + 6 a^5 b x + 15 a^4 b^2 x^2 + 20 a^3 b^3 x^3 + 15 a^2 b^4 x^4 + 6 a b^5 x^5 + b^6 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^2/(a + b*x)^7,x)

[Out]
$$-((a^2*d^2 + 10*b^2*c^2 + 4*a*b*c*d)/(60*b^3) + (d^2*x^2)/(4*b) + (d*x*(a*d + 4*b*c))/(10*b^2))/(a^6 + b^6*x^6 + 6*a*b^5*x^5 + 15*a^4*b^2*x^2 + 20*a^3*b^3*x^3 + 15*a^2*b^4*x^4 + 6*a^5*b*x)$$

sympy [B] time = 1.16, size = 128, normalized size = 1.97

$$\frac{-a^2 d^2 - 4 a b c d - 10 b^2 c^2 - 15 b^2 d^2 x^2 + x(-6 a b d^2 - 24 b^2 c d)}{60 a^6 b^3 + 360 a^5 b^4 x + 900 a^4 b^5 x^2 + 1200 a^3 b^6 x^3 + 900 a^2 b^7 x^4 + 360 a b^8 x^5 + 60 b^9 x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2/(b*x+a)**7,x)

[Out]
$$(-a**2*d**2 - 4*a*b*c*d - 10*b**2*c**2 - 15*b**2*d**2*x**2 + x*(-6*a*b*d**2 - 24*b**2*c*d))/(60*a**6*b**3 + 360*a**5*b**4*x + 900*a**4*b**5*x**2 + 1200*a**3*b**6*x**3 + 900*a**2*b**7*x**4 + 360*a*b**8*x**5 + 60*b**9*x**6)$$

3.1258 $\int (a + bx)^5 (c + dx)^3 dx$

Optimal. Leaf size=92

$$\frac{3d^2(a+bx)^8(bc-ad)}{8b^4} + \frac{3d(a+bx)^7(bc-ad)^2}{7b^4} + \frac{(a+bx)^6(bc-ad)^3}{6b^4} + \frac{d^3(a+bx)^9}{9b^4}$$

[Out] $1/6*(-a*d+b*c)^3*(b*x+a)^6/b^4+3/7*d*(-a*d+b*c)^2*(b*x+a)^7/b^4+3/8*d^2*(-a*d+b*c)*(b*x+a)^8/b^4+1/9*d^3*(b*x+a)^9/b^4$

Rubi [A] time = 0.16, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{3d^2(a+bx)^8(bc-ad)}{8b^4} + \frac{3d(a+bx)^7(bc-ad)^2}{7b^4} + \frac{(a+bx)^6(bc-ad)^3}{6b^4} + \frac{d^3(a+bx)^9}{9b^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*(c + d*x)^3, x]

[Out] $((b*c - a*d)^3*(a + b*x)^6)/(6*b^4) + (3*d*(b*c - a*d)^2*(a + b*x)^7)/(7*b^4) + (3*d^2*(b*c - a*d)*(a + b*x)^8)/(8*b^4) + (d^3*(a + b*x)^9)/(9*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^5 (c + dx)^3 dx &= \int \left(\frac{(bc - ad)^3 (a + bx)^5}{b^3} + \frac{3d(bc - ad)^2 (a + bx)^6}{b^3} + \frac{3d^2(bc - ad)(a + bx)^7}{b^3} + \frac{d^3(a + bx)^8}{b^3} \right) dx \\ &= \frac{(bc - ad)^3 (a + bx)^6}{6b^4} + \frac{3d(bc - ad)^2 (a + bx)^7}{7b^4} + \frac{3d^2(bc - ad)(a + bx)^8}{8b^4} + \frac{d^3(a + bx)^9}{9b^4} \end{aligned}$$

Mathematica [B] time = 0.08, size = 235, normalized size = 2.55

$$\frac{1}{504}x(126a^5(4c^3 + 6c^2dx + 4cd^2x^2 + d^3x^3) + 126a^4bx(10c^3 + 20c^2dx + 15cd^2x^2 + 4d^3x^3) + 84a^3b^2x^2(20c^3 +$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*(c + d*x)^3,x]

[Out] (x*(126*a^5*(4*c^3 + 6*c^2*d*x + 4*c*d^2*x^2 + d^3*x^3) + 126*a^4*b*x*(10*c^3 + 20*c^2*d*x + 15*c*d^2*x^2 + 4*d^3*x^3) + 84*a^3*b^2*x^2*(20*c^3 + 45*c^2*d*x + 36*c*d^2*x^2 + 10*d^3*x^3) + 36*a^2*b^3*x^3*(35*c^3 + 84*c^2*d*x + 70*c*d^2*x^2 + 20*d^3*x^3) + 9*a*b^4*x^4*(56*c^3 + 140*c^2*d*x + 120*c*d^2*x^2 + 35*d^3*x^3) + b^5*x^5*(84*c^3 + 216*c^2*d*x + 189*c*d^2*x^2 + 56*d^3*x^3)))/504

fricas [B] time = 0.39, size = 303, normalized size = 3.29

$$\frac{1}{9}x^9d^3b^5 + \frac{3}{8}x^8d^2cb^5 + \frac{5}{8}x^8d^3b^4a + \frac{3}{7}x^7dc^2b^5 + \frac{15}{7}x^7d^2cb^4a + \frac{10}{7}x^7d^3b^3a^2 + \frac{1}{6}x^6c^3b^5 + \frac{5}{2}x^6dc^2b^4a + 5x^6d^2cb^3a^2 + \frac{5}{3}x^6d^3b^3a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^3,x, algorithm="fricas")

[Out] 1/9*x^9*d^3*b^5 + 3/8*x^8*d^2*c*b^5 + 5/8*x^8*d^3*b^4*a + 3/7*x^7*d*c^2*b^5 + 15/7*x^7*d^2*c*b^4*a + 10/7*x^7*d^3*b^3*a^2 + 1/6*x^6*c^3*b^5 + 5/2*x^6*d*c^2*b^4*a + 5*x^6*d^2*c*b^3*a^2 + 5/3*x^6*d^3*b^2*a^3 + x^5*c^3*b^4*a + 6*x^5*d*c^2*b^3*a^2 + 6*x^5*d^2*c*b^2*a^3 + x^5*d^3*b*a^4 + 5/2*x^4*c^3*b^3*a^2 + 15/2*x^4*d*c^2*b^2*a^3 + 15/4*x^4*d^2*c*b*a^4 + 1/4*x^4*d^3*a^5 + 10/3*x^3*c^3*b^2*a^3 + 5*x^3*d*c^2*b*a^4 + x^3*d^2*c*a^5 + 5/2*x^2*c^3*b*a^4 + 3/2*x^2*d*c^2*a^5 + x*c^3*a^5

giac [B] time = 1.01, size = 303, normalized size = 3.29

$$\frac{1}{9}b^5d^3x^9 + \frac{3}{8}b^5cd^2x^8 + \frac{5}{8}ab^4d^3x^8 + \frac{3}{7}b^5c^2dx^7 + \frac{15}{7}ab^4cd^2x^7 + \frac{10}{7}a^2b^3d^3x^7 + \frac{1}{6}b^5c^3x^6 + \frac{5}{2}ab^4c^2dx^6 + 5a^2b^3cd^2x^6 + \frac{5}{3}a^2b^3cd^2x^6 + \frac{5}{3}a^2b^3cd^2x^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^3,x, algorithm="giac")

[Out] 1/9*b^5*d^3*x^9 + 3/8*b^5*c*d^2*x^8 + 5/8*a*b^4*d^3*x^8 + 3/7*b^5*c^2*d*x^7 + 15/7*a*b^4*c*d^2*x^7 + 10/7*a^2*b^3*d^3*x^7 + 1/6*b^5*c^3*x^6 + 5/2*a*b^4*c^2*d*x^6 + 5*a^2*b^3*c*d^2*x^6 + 5/3*a^3*b^2*d^3*x^6 + a*b^4*c^3*x^5 + 6*a^2*b^3*c^2*d*x^5 + 6*a^3*b^2*c*d^2*x^5 + a^4*b*d^3*x^5 + 5/2*a^2*b^3*c^3*x^4 + 15/2*a^3*b^2*c^2*d*x^4 + 15/4*a^4*b*c*d^2*x^4 + 1/4*a^5*d^3*x^4 + 10/3*a^3*b^2*c^3*x^3 + 5*a^4*b*c^2*d*x^3 + a^5*c*d^2*x^3 + 5/2*a^4*b*c^3*x^2 + 3/2*a^5*c^2*d*x^2 + a^5*c^3*x

maple [B] time = 0.00, size = 281, normalized size = 3.05

$$\frac{b^5d^3x^9}{9} + a^5c^3x + \frac{(5ab^4d^3 + 3b^5cd^2)x^8}{8} + \frac{(10a^2b^3d^3 + 15ab^4cd^2 + 3b^5c^2d)x^7}{7} + \frac{(10a^3b^2d^3 + 30a^2b^3cd^2 + 15ab^4c^2d)x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^5*(d*x+c)^3,x)`

[Out] $\frac{1}{9}b^5d^3x^9 + \frac{1}{8}(5a^5b^4d^3 + 3b^5c^2d^2)x^8 + \frac{1}{7}(10a^2b^3d^3 + 15a^4b^4cd^2 + 3b^5c^2d)x^7 + \frac{1}{6}(10a^3b^2d^3 + 30a^2b^3cd^2 + 15a^4b^4c^2d + b^5c^3)x^6 + \frac{1}{5}(5a^4b^3d^3 + 30a^3b^2c^2d + 30a^2b^3c^2d + 5a^4b^4c^3)x^5 + \frac{1}{4}(a^5d^3 + 15a^4b^3cd^2 + 30a^3b^2c^2d + 10a^2b^3c^3)x^4 + \frac{1}{3}(3a^5c^2d^2 + 15a^4b^3c^2d + 10a^3b^2c^3)x^3 + \frac{1}{2}(3a^5c^2d + 5a^4b^3c^3)x^2 + a^5c^3x$

maxima [B] time = 1.38, size = 277, normalized size = 3.01

$$\frac{1}{9}b^5d^3x^9 + a^5c^3x + \frac{1}{8}(3b^5cd^2 + 5ab^4d^3)x^8 + \frac{1}{7}(3b^5c^2d + 15ab^4cd^2 + 10a^2b^3d^3)x^7 + \frac{1}{6}(b^5c^3 + 15ab^4c^2d + 30a^2b^3c^2d)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5*(d*x+c)^3,x, algorithm="maxima")`

[Out] $\frac{1}{9}b^5d^3x^9 + a^5c^3x + \frac{1}{8}(3b^5cd^2 + 5a^4b^4d^3)x^8 + \frac{1}{7}(3b^5c^2d + 15a^4b^4cd^2 + 10a^2b^3d^3)x^7 + \frac{1}{6}(b^5c^3 + 15a^4b^4c^2d + 30a^2b^3c^2d + 10a^3b^2c^2d)x^6 + (a^4b^4c^3 + 6a^2b^3c^2d + 6a^3b^2c^2d + a^4b^3cd^3)x^5 + \frac{1}{4}(10a^2b^3c^3 + 30a^3b^2c^2d + 15a^4b^3cd^2 + a^5d^3)x^4 + \frac{1}{3}(10a^3b^2c^3 + 15a^4b^3c^2d + 3a^5cd^2)x^3 + \frac{1}{2}(5a^4b^3c^3 + 3a^5c^2d)x^2$

mupad [B] time = 0.24, size = 261, normalized size = 2.84

$$x^5(a^4bd^3 + 6a^3b^2cd^2 + 6a^2b^3c^2d + ab^4c^3) + x^4\left(\frac{a^5d^3}{4} + \frac{15a^4bcd^2}{4} + \frac{15a^3b^2c^2d}{2} + \frac{5a^2b^3c^3}{2}\right) + x^6\left(\frac{5a^3b^2d^3}{3} + \frac{15a^4b^3cd^2}{2} + \frac{10a^2b^3d^3}{2} + \frac{15a^4b^4c^2d}{2} + \frac{b^5c^3}{6} + \frac{5a^3b^2c^2d}{3} + 5a^2b^3c^2d + \frac{5a^4b^4c^2d}{2}\right) + a^5c^3x + \frac{b^5d^3x^9}{9} + \frac{a^4b^4d^3x^8}{8} + \frac{a^4b^3cd^2x^7}{4} + \frac{a^3b^2c^2d^2x^6}{3} + \frac{a^2b^3c^2d^2x^5}{2} + \frac{a^4b^4c^2x^4}{4} + \frac{a^3b^2c^2d^2x^3}{3} + \frac{a^2b^3c^2d^2x^2}{2} + \frac{a^4b^4c^2d^2x}{4} + \frac{a^5c^3x}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5*(c + d*x)^3,x)`

[Out] $x^5(a^4b^4c^3 + a^4b^3d^3 + 6a^2b^3c^2d + 6a^3b^2c^2d) + x^4\left(\frac{a^5d^3}{4} + \frac{5a^2b^3c^3}{2} + \frac{15a^3b^2c^2d}{2} + \frac{15a^4b^3cd^2}{4}\right) + x^6\left(\frac{b^5c^3}{6} + \frac{5a^3b^2d^3}{3} + 5a^2b^3c^2d + \frac{5a^4b^4c^2d}{2}\right) + a^5c^3x + \frac{b^5d^3x^9}{9} + \frac{a^4b^4d^3x^8}{8} + \frac{a^4b^3cd^2x^7}{4} + \frac{a^3b^2c^2d^2x^6}{3} + \frac{a^2b^3c^2d^2x^5}{2} + \frac{a^4b^4c^2d^2x^4}{4} + \frac{a^3b^2c^2d^2x^3}{3} + \frac{a^2b^3c^2d^2x^2}{2} + \frac{a^4b^4c^2d^2x}{4} + \frac{a^5c^3x}{5}$

sympy [B] time = 0.12, size = 308, normalized size = 3.35

$$a^5c^3x + \frac{b^5d^3x^9}{9} + x^8\left(\frac{5ab^4d^3}{8} + \frac{3b^5cd^2}{8}\right) + x^7\left(\frac{10a^2b^3d^3}{7} + \frac{15ab^4cd^2}{7} + \frac{3b^5c^2d}{7}\right) + x^6\left(\frac{5a^3b^2d^3}{3} + 5a^2b^3cd^2 + \frac{5ab^4c^2d}{2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5*(d*x+c)**3,x)

[Out] $a^5c^3x + b^5d^3x^9/9 + x^8(5ab^4d^3/8 + 3b^5c^2d/8) +$
 $x^7(10a^2b^3d^3/7 + 15ab^4cd^2/7 + 3b^5c^2d/7) + x^6($
 $5a^3b^2d^3/3 + 5a^2b^3cd^2 + 5ab^4c^2d/2 + b^5c^3/6)$
 $+ x^5(a^4bd^3 + 6a^3b^2cd^2 + 6a^2b^3c^2d + ab^4c^3$
 $) + x^4(a^5d^3/4 + 15a^4b^2cd^2/4 + 15a^3b^2c^2d/2 + 5a^2$
 $b^3c^3/2) + x^3(a^5cd^2 + 5a^4b^2cd + 10a^3b^2c^3/3)$
 $+ x^2(3a^5c^2d/2 + 5a^4b^2c^3/2)$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4*(c + d*x)^3,x]

[Out] $a^4c^3x + (a^3c^2(4bc + 3ad)x^2)/2 + a^2c(2b^2c^2 + 4ab*cd + a^2d^2)x^3 + (a(4b^3c^3 + 18ab^2c^2d + 12a^2b*cd^2 + a^3d^3)x^4)/4 + (b(b^3c^3 + 12ab^2c^2d + 18a^2b*cd^2 + 4a^3d^3)x^5)/5 + (b^2d(b^2c^2 + 4ab*cd + 2a^2d^2)x^6)/2 + (b^3d^2(3bc + 4ad)x^7)/7 + (b^4d^3x^8)/8$

fricas [B] time = 0.37, size = 245, normalized size = 2.66

$$\frac{1}{8}x^8d^3b^4 + \frac{3}{7}x^7d^2cb^4 + \frac{4}{7}x^7d^3b^3a + \frac{1}{2}x^6dc^2b^4 + 2x^6d^2cb^3a + x^6d^3b^2a^2 + \frac{1}{5}x^5c^3b^4 + \frac{12}{5}x^5dc^2b^3a + \frac{18}{5}x^5d^2cb^2a^2 + \frac{4}{5}x^5d^3ba^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^3,x, algorithm="fricas")

[Out] $1/8x^8d^3b^4 + 3/7x^7d^2c*b^4 + 4/7x^7d^3b^3a + 1/2x^6d*c^2*b^4 + 2x^6d^2*c*b^3a + x^6d^3b^2*a^2 + 1/5x^5c^3b^4 + 12/5x^5d*c^2*b^3a + 18/5x^5d^2*c*b^2*a^2 + 4/5x^5d^3*b*a^3 + x^4c^3b^3a + 9/2x^4*d*c^2*b^2*a^2 + 3x^4*d^2*c*b*a^3 + 1/4x^4*d^3*a^4 + 2x^3c^3b^2a^2 + 4x^3d*c^2b*a^3 + x^3d^2c*a^4 + 2x^2c^3b*a^3 + 3/2x^2d*c^2a^4 + x*c^3a^4$

giac [B] time = 1.12, size = 245, normalized size = 2.66

$$\frac{1}{8}b^4d^3x^8 + \frac{3}{7}b^4cd^2x^7 + \frac{4}{7}ab^3d^3x^7 + \frac{1}{2}b^4c^2dx^6 + 2ab^3cd^2x^6 + a^2b^2d^3x^6 + \frac{1}{5}b^4c^3x^5 + \frac{12}{5}ab^3c^2dx^5 + \frac{18}{5}a^2b^2cd^2x^5 + \frac{4}{5}a^3b^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^3,x, algorithm="giac")

[Out] $1/8b^4d^3x^8 + 3/7b^4c*d^2x^7 + 4/7a*b^3*d^3x^7 + 1/2b^4c^2*d*x^6 + 2a*b^3*c*d^2*x^6 + a^2b^2*d^3*x^6 + 1/5b^4c^3*x^5 + 12/5a*b^3*c^2*d*x^5 + 18/5a^2*b^2*c*d^2*x^5 + 4/5a^3*b*d^3*x^5 + a*b^3*c^3*x^4 + 9/2a^2*b^2*c^2*d*x^4 + 3a^3*b*c*d^2*x^4 + 1/4a^4*d^3*x^4 + 2a^2*b^2*c^3*x^3 + 4a^3*b*c^2*d*x^3 + a^4*c*d^2*x^3 + 2a^3*b*c^3*x^2 + 3/2a^4*c^2*d*x^2 + a^4*c^3*x$

maple [B] time = 0.00, size = 229, normalized size = 2.49

$$\frac{b^4d^3x^8}{8} + \frac{a^4c^3x^8}{8} + \frac{(4ab^3d^3 + 3b^4cd^2)x^7}{7} + \frac{(6a^2b^2d^3 + 12ab^3cd^2 + 3b^4c^2d)x^6}{6} + \frac{(4a^3bd^3 + 18a^2b^2cd^2 + 12ab^3c^2d + 4a^4c^3)x^5}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4*(d*x+c)^3,x)

[Out] $\frac{1}{8}b^4d^3x^8 + \frac{1}{7}(4ab^3d^3 + 3b^4cd^2)x^7 + \frac{1}{6}(6a^2b^2d^3 + 12ab^3cd^2 + 3b^4c^2d)x^6 + \frac{1}{5}(4a^3b^2d^3 + 18a^2b^2cd^2 + 12ab^3c^2d + b^4c^3)x^5 + \frac{1}{4}(a^4d^3 + 12a^3b^2cd^2 + 18a^2b^2c^2d + 4ab^3c^3)x^4 + \frac{1}{3}(3a^4cd^2 + 12a^3b^2cd + 6a^2b^2c^3)x^3 + \frac{1}{2}(3a^4c^2d + 4a^3b^2c^3)x^2 + a^4c^3x$

maxima [B] time = 1.32, size = 225, normalized size = 2.45

$$\frac{1}{8}b^4d^3x^8 + a^4c^3x + \frac{1}{7}(3b^4cd^2 + 4ab^3d^3)x^7 + \frac{1}{2}(b^4c^2d + 4ab^3cd^2 + 2a^2b^2d^3)x^6 + \frac{1}{5}(b^4c^3 + 12ab^3c^2d + 18a^2b^2cd^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^3,x, algorithm="maxima")

[Out] $\frac{1}{8}b^4d^3x^8 + a^4c^3x + \frac{1}{7}(3b^4cd^2 + 4ab^3d^3)x^7 + \frac{1}{2}(b^4c^2d + 4ab^3cd^2 + 2a^2b^2d^3)x^6 + \frac{1}{5}(b^4c^3 + 12ab^3c^2d + 18a^2b^2cd^2 + 4ab^3c^3)x^5 + \frac{1}{4}(4a^2b^2cd^2 + 12a^3b^2cd + a^4d^3)x^4 + (2a^2b^2c^3 + 4a^3b^2cd + a^4cd^2)x^3 + \frac{1}{2}(4a^3b^2cd + 3a^4c^2d)x^2$

mupad [B] time = 0.21, size = 208, normalized size = 2.26

$$x^4 \left(\frac{a^4d^3}{4} + 3a^3bcd^2 + \frac{9a^2b^2c^2d}{2} + ab^3c^3 \right) + x^5 \left(\frac{4a^3bd^3}{5} + \frac{18a^2b^2cd^2}{5} + \frac{12ab^3c^2d}{5} + \frac{b^4c^3}{5} \right) + a^4c^3x + \frac{b^4d^3x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^4*(c + d*x)^3,x)

[Out] $x^4 \left(\frac{a^4d^3}{4} + ab^3c^3 + \frac{(9a^2b^2c^2d)}{2} + 3a^3b^2cd^2 \right) + x^5 \left(\frac{b^4c^3}{5} + \frac{(4a^3b^2d^3)}{5} + \frac{(18a^2b^2cd^2)}{5} + \frac{(12ab^3c^2d)}{5} \right) + a^4c^3x + \frac{(b^4d^3x^8)}{8} + \frac{(a^3c^2x^2(3ad + 4bc))}{2} + \frac{(b^3d^2x^7(4ad + 3bc))}{7} + a^2c^2x^3(a^2d^2 + 2b^2c^2 + 4ab^2cd) + \frac{(b^2d^2x^6(2a^2d^2 + b^2c^2 + 4ab^2cd))}{2}$

sympy [B] time = 0.11, size = 243, normalized size = 2.64

$$a^4c^3x + \frac{b^4d^3x^8}{8} + x^7 \left(\frac{4ab^3d^3}{7} + \frac{3b^4cd^2}{7} \right) + x^6 \left(a^2b^2d^3 + 2ab^3cd^2 + \frac{b^4c^2d}{2} \right) + x^5 \left(\frac{4a^3bd^3}{5} + \frac{18a^2b^2cd^2}{5} + \frac{12ab^3c^2d}{5} + \frac{b^4c^3}{5} \right) + a^4c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4*(d*x+c)**3,x)

```
[Out] a**4*c**3*x + b**4*d**3*x**8/8 + x**7*(4*a*b**3*d**3/7 + 3*b**4*c*d**2/7) +
x**6*(a**2*b**2*d**3 + 2*a*b**3*c*d**2 + b**4*c**2*d/2) + x**5*(4*a**3*b*d
**3/5 + 18*a**2*b**2*c*d**2/5 + 12*a*b**3*c**2*d/5 + b**4*c**3/5) + x**4*(a
**4*d**3/4 + 3*a**3*b*c*d**2 + 9*a**2*b**2*c**2*d/2 + a*b**3*c**3) + x**3*(
a**4*c*d**2 + 4*a**3*b*c**2*d + 2*a**2*b**2*c**3) + x**2*(3*a**4*c**2*d/2 +
2*a**3*b*c**3)
```

3.1260 $\int (a + bx)^3 (c + dx)^3 dx$

Optimal. Leaf size=92

$$\frac{d^2(a + bx)^6(bc - ad)}{2b^4} + \frac{3d(a + bx)^5(bc - ad)^2}{5b^4} + \frac{(a + bx)^4(bc - ad)^3}{4b^4} + \frac{d^3(a + bx)^7}{7b^4}$$

[Out] $1/4*(-a*d+b*c)^3*(b*x+a)^4/b^4+3/5*d*(-a*d+b*c)^2*(b*x+a)^5/b^4+1/2*d^2*(-a*d+b*c)*(b*x+a)^6/b^4+1/7*d^3*(b*x+a)^7/b^4$

Rubi [A] time = 0.08, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{d^2(a + bx)^6(bc - ad)}{2b^4} + \frac{3d(a + bx)^5(bc - ad)^2}{5b^4} + \frac{(a + bx)^4(bc - ad)^3}{4b^4} + \frac{d^3(a + bx)^7}{7b^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3*(c + d*x)^3, x]

[Out] $((b*c - a*d)^3*(a + b*x)^4)/(4*b^4) + (3*d*(b*c - a*d)^2*(a + b*x)^5)/(5*b^4) + (d^2*(b*c - a*d)*(a + b*x)^6)/(2*b^4) + (d^3*(a + b*x)^7)/(7*b^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^3 (c + dx)^3 dx &= \int \left(\frac{(bc - ad)^3 (a + bx)^3}{b^3} + \frac{3d(bc - ad)^2 (a + bx)^4}{b^3} + \frac{3d^2(bc - ad)(a + bx)^5}{b^3} + \frac{d^3(a + bx)^6}{b^3} \right) dx \\ &= \frac{(bc - ad)^3 (a + bx)^4}{4b^4} + \frac{3d(bc - ad)^2 (a + bx)^5}{5b^4} + \frac{d^2(bc - ad)(a + bx)^6}{2b^4} + \frac{d^3(a + bx)^7}{7b^4} \end{aligned}$$

Mathematica [A] time = 0.02, size = 161, normalized size = 1.75

$$a^3c^3x + \frac{3}{5}bdx^5(a^2d^2 + 3abcd + b^2c^2) + acx^3(a^2d^2 + 3abcd + b^2c^2) + \frac{3}{2}a^2c^2x^2(ad + bc) + \frac{1}{4}x^4(a^3d^3 + 9a^2bcd^2 + 9ab^2cd^2 + 9a^2bcd^2 + 9ab^2cd^2)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3*(c + d*x)^3,x]

[Out] $a^3c^3x + (3a^2c^2(b*c + a*d)*x^2)/2 + a*c*(b^2c^2 + 3a*b*c*d + a^2d^2)*x^3 + ((b^3c^3 + 9a*b^2c^2d + 9a^2b*c*d^2 + a^3d^3)*x^4)/4 + (3*b*d*(b^2c^2 + 3a*b*c*d + a^2d^2)*x^5)/5 + (b^2d^2*(b*c + a*d)*x^6)/2 + (b^3d^3*x^7)/7$

fricas [B] time = 0.37, size = 188, normalized size = 2.04

$$\frac{1}{7}x^7d^3b^3 + \frac{1}{2}x^6d^2cb^3 + \frac{1}{2}x^6d^3b^2a + \frac{3}{5}x^5dc^2b^3 + \frac{9}{5}x^5d^2cb^2a + \frac{3}{5}x^5d^3ba^2 + \frac{1}{4}x^4c^3b^3 + \frac{9}{4}x^4dc^2b^2a + \frac{9}{4}x^4d^2cba^2 + \frac{1}{4}x^4d^3a^3 + x^3c^3b^2a + 3x^3d^2c^2ba^2 + x^3d^2c^2a^3 + \frac{3}{2}x^2c^3b^2a + \frac{3}{2}x^2d^2c^2a^3 + xc^3a^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^3,x, algorithm="fricas")

[Out] $1/7*x^7*d^3*b^3 + 1/2*x^6*d^2*c*b^3 + 1/2*x^6*d^3*b^2*a + 3/5*x^5*d*c^2*b^3 + 9/5*x^5*d^2*c*b^2*a + 3/5*x^5*d^3*b*a^2 + 1/4*x^4*c^3*b^3 + 9/4*x^4*d*c^2*b^2*a + 9/4*x^4*d^2*c*b*a^2 + 1/4*x^4*d^3*a^3 + x^3*c^3*b^2*a + 3*x^3*d*c^2*b*a^2 + x^3*d^2*c*a^3 + 3/2*x^2*c^3*b*a^2 + 3/2*x^2*d*c^2*a^3 + x*c^3*a^3$

giac [B] time = 0.97, size = 188, normalized size = 2.04

$$\frac{1}{7}b^3d^3x^7 + \frac{1}{2}b^3cd^2x^6 + \frac{1}{2}ab^2d^3x^6 + \frac{3}{5}b^3c^2dx^5 + \frac{9}{5}ab^2cd^2x^5 + \frac{3}{5}a^2bd^3x^5 + \frac{1}{4}b^3c^3x^4 + \frac{9}{4}ab^2c^2dx^4 + \frac{9}{4}a^2bcd^2x^4 + \frac{1}{4}a^3d^3x^4 + a^3c^3x^3 + 3a^2b^2cd^2x^3 + \frac{3}{2}a^2b^2c^3x^2 + \frac{3}{2}a^3c^2d^2x^2 + a^3c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^3,x, algorithm="giac")

[Out] $1/7*b^3*d^3*x^7 + 1/2*b^3*c*d^2*x^6 + 1/2*a*b^2*d^3*x^6 + 3/5*b^3*c^2*d*x^5 + 9/5*a*b^2*c*d^2*x^5 + 3/5*a^2*b*d^3*x^5 + 1/4*b^3*c^3*x^4 + 9/4*a*b^2*c^2*d*x^4 + 9/4*a^2*b*c*d^2*x^4 + 1/4*a^3*d^3*x^4 + a*b^2*c^3*x^3 + 3*a^2*b*c^2*d*x^3 + a^3*c*d^2*x^3 + 3/2*a^2*b*c^3*x^2 + 3/2*a^3*c^2*d*x^2 + a^3*c^3*x$

maple [B] time = 0.00, size = 177, normalized size = 1.92

$$\frac{b^3d^3x^7}{7} + \frac{a^3c^3x^4 + (3ab^2d^3 + 3b^3cd^2)x^6 + (3a^2bd^3 + 9ab^2cd^2 + 3b^3c^2d)x^5 + (a^3d^3 + 9a^2bcd^2 + 9ab^2c^2d + b^3c^3)x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3*(d*x+c)^3,x)

[Out] $\frac{1}{7}b^3d^3x^7 + \frac{1}{6}(3a^2b^2d^3 + 3b^3c^2d^2)x^6 + \frac{1}{5}(3a^2b^2d^3 + 9a^2b^2c^2d^2 + 3b^3c^2d^2)x^5 + \frac{1}{4}(a^3d^3 + 9a^2b^2c^2d^2 + 9a^2b^2c^2d + b^3c^3)x^4 + \frac{1}{3}(3a^3c^2d^2 + 9a^2b^2c^2d + 3a^2b^2c^3)x^3 + \frac{1}{2}(3a^3c^2d + 3a^2b^2c^3)x^2 + a^3c^3x$

maxima [A] time = 1.34, size = 167, normalized size = 1.82

$$\frac{1}{7}b^3d^3x^7 + a^3c^3x + \frac{1}{2}(b^3cd^2 + ab^2d^3)x^6 + \frac{3}{5}(b^3c^2d + 3ab^2cd^2 + a^2bd^3)x^5 + \frac{1}{4}(b^3c^3 + 9ab^2c^2d + 9a^2bcd^2 + a^3d^3)x^4 + \frac{1}{3}(3a^3c^2d + 9a^2b^2c^2d + 3a^2b^2c^3)x^3 + \frac{1}{2}(3a^3c^2d + 3a^2b^2c^3)x^2 + a^3c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^3,x, algorithm="maxima")

[Out] $\frac{1}{7}b^3d^3x^7 + a^3c^3x + \frac{1}{2}(b^3c^2d + a^2b^2d^3)x^6 + \frac{3}{5}(b^3c^2d + 3a^2b^2c^2d + a^2b^2d^3)x^5 + \frac{1}{4}(b^3c^3 + 9a^2b^2c^2d + 9a^2b^2c^2d + a^3d^3)x^4 + (a^2b^2c^3 + 3a^2b^2c^2d + a^3c^2d^2)x^3 + \frac{3}{2}(a^2b^2c^3 + a^3c^2d^2)x^2$

mupad [B] time = 0.06, size = 152, normalized size = 1.65

$$x^4 \left(\frac{a^3d^3}{4} + \frac{9a^2bcd^2}{4} + \frac{9ab^2c^2d}{4} + \frac{b^3c^3}{4} \right) + a^3c^3x + \frac{b^3d^3x^7}{7} + acx^3(a^2d^2 + 3abcd + b^2c^2) + \frac{3bdx^5(a^2d^2 + 3abcd + b^2c^2)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3*(c + d*x)^3,x)

[Out] $x^4((a^3d^3)/4 + (b^3c^3)/4 + (9a^2b^2c^2d)/4 + (9a^2b^2c^2d)/4) + a^3c^3x + (b^3d^3x^7)/7 + acx^3(a^2d^2 + b^2c^2 + 3a^2b^2cd) + (3b^3d^3x^5(a^2d^2 + b^2c^2 + 3a^2b^2cd))/5 + (3a^2c^2x^2(a^2d^2 + b^2c^2))/2 + (b^2d^2x^6(a^2d^2 + b^2c^2))/2$

sympy [B] time = 0.10, size = 190, normalized size = 2.07

$$a^3c^3x + \frac{b^3d^3x^7}{7} + x^6 \left(\frac{ab^2d^3}{2} + \frac{b^3cd^2}{2} \right) + x^5 \left(\frac{3a^2bd^3}{5} + \frac{9ab^2cd^2}{5} + \frac{3b^3c^2d}{5} \right) + x^4 \left(\frac{a^3d^3}{4} + \frac{9a^2bcd^2}{4} + \frac{9ab^2c^2d}{4} + \frac{b^3c^3}{4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3*(d*x+c)**3,x)

[Out] $a^3c^3x + b^3d^3x^7/7 + x^6(a^2b^2d^3/2 + b^3c^2d^2/2) + x^5(3a^2b^2d^3/5 + 9a^2b^2c^2d^2/5 + 3b^3c^2d/5) + x^4(a^3d^3/4 + 9a^2b^2c^2d/4 + 9a^2b^2c^2d/4 + b^3c^3/4) + x^3(a^3c^2d^2 + 3a^2b^2c^2d + a^2b^2c^3) + x^2(3a^3c^2d/2 + 3a^2b^2c^3/2)$

3.1261 $\int (a + bx)^2 (c + dx)^3 dx$

Optimal. Leaf size=65

$$-\frac{2b(c + dx)^5(bc - ad)}{5d^3} + \frac{(c + dx)^4(bc - ad)^2}{4d^3} + \frac{b^2(c + dx)^6}{6d^3}$$

[Out] $1/4*(-a*d+b*c)^2*(d*x+c)^4/d^3-2/5*b*(-a*d+b*c)*(d*x+c)^5/d^3+1/6*b^2*(d*x+c)^6/d^3$

Rubi [A] time = 0.06, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{2b(c + dx)^5(bc - ad)}{5d^3} + \frac{(c + dx)^4(bc - ad)^2}{4d^3} + \frac{b^2(c + dx)^6}{6d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(c + d*x)^3, x]

[Out] $((b*c - a*d)^2*(c + d*x)^4)/(4*d^3) - (2*b*(b*c - a*d)*(c + d*x)^5)/(5*d^3) + (b^2*(c + d*x)^6)/(6*d^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2 (c + dx)^3 dx &= \int \left(\frac{(-bc + ad)^2 (c + dx)^3}{d^2} - \frac{2b(bc - ad)(c + dx)^4}{d^2} + \frac{b^2(c + dx)^5}{d^2} \right) dx \\ &= \frac{(bc - ad)^2 (c + dx)^4}{4d^3} - \frac{2b(bc - ad)(c + dx)^5}{5d^3} + \frac{b^2(c + dx)^6}{6d^3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 122, normalized size = 1.88

$$\frac{1}{4}dx^4 (a^2d^2 + 6abcd + 3b^2c^2) + \frac{1}{3}cx^3 (3a^2d^2 + 6abcd + b^2c^2) + a^2c^3x + \frac{1}{2}ac^2x^2(3ad+2bc) + \frac{1}{5}bd^2x^5(2ad+3bc) + \frac{1}{6}b^2d^3x^6$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(c + d*x)^3,x]

[Out] $a^2*c^3*x + (a*c^2*(2*b*c + 3*a*d)*x^2)/2 + (c*(b^2*c^2 + 6*a*b*c*d + 3*a^2*d^2)*x^3)/3 + (d*(3*b^2*c^2 + 6*a*b*c*d + a^2*d^2)*x^4)/4 + (b*d^2*(3*b*c + 2*a*d)*x^5)/5 + (b^2*d^3*x^6)/6$

fricas [B] time = 0.37, size = 130, normalized size = 2.00

$$\frac{1}{6}x^6d^3b^2 + \frac{3}{5}x^5d^2cb^2 + \frac{2}{5}x^5d^3ba + \frac{3}{4}x^4dc^2b^2 + \frac{3}{2}x^4d^2cba + \frac{1}{4}x^4d^3a^2 + \frac{1}{3}x^3c^3b^2 + 2x^3dc^2ba + x^3d^2ca^2 + x^2c^3ba + \frac{3}{2}x^2dc^2a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^3,x, algorithm="fricas")

[Out] $1/6*x^6*d^3*b^2 + 3/5*x^5*d^2*c*b^2 + 2/5*x^5*d^3*b*a + 3/4*x^4*d*c^2*b^2 + 3/2*x^4*d^2*c*b*a + 1/4*x^4*d^3*a^2 + 1/3*x^3*c^3*b^2 + 2*x^3*d*c^2*b*a + x^3*d^2*c*a^2 + x^2*c^3*b*a + 3/2*x^2*d*c^2*a^2 + x*c^3*a^2$

giac [B] time = 1.04, size = 130, normalized size = 2.00

$$\frac{1}{6}b^2d^3x^6 + \frac{3}{5}b^2cd^2x^5 + \frac{2}{5}abd^3x^5 + \frac{3}{4}b^2c^2dx^4 + \frac{3}{2}abcd^2x^4 + \frac{1}{4}a^2d^3x^4 + \frac{1}{3}b^2c^3x^3 + 2abc^2dx^3 + a^2cd^2x^3 + abc^3x^2 + \frac{3}{2}a^2c^3x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^3,x, algorithm="giac")

[Out] $1/6*b^2*d^3*x^6 + 3/5*b^2*c*d^2*x^5 + 2/5*a*b*d^3*x^5 + 3/4*b^2*c^2*d*x^4 + 3/2*a*b*c*d^2*x^4 + 1/4*a^2*d^3*x^4 + 1/3*b^2*c^3*x^3 + 2*a*b*c^2*d*x^3 + a^2*c*d^2*x^3 + a*b*c^3*x^2 + 3/2*a^2*c^2*d*x^2 + a^2*c^3*x^2$

maple [B] time = 0.00, size = 125, normalized size = 1.92

$$\frac{b^2d^3x^6}{6} + a^2c^3x^2 + \frac{(2abd^3 + 3b^2cd^2)x^5}{5} + \frac{(a^2d^3 + 6abcd^2 + 3b^2c^2d)x^4}{4} + \frac{(3a^2cd^2 + 6abc^2d + b^2c^3)x^3}{3} + \frac{(3a^2c^2d + 3a^2c^3)x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(d*x+c)^3,x)

[Out] $1/6*b^2*d^3*x^6 + 1/5*(2*a*b*d^3 + 3*b^2*c*d^2)*x^5 + 1/4*(a^2*d^3 + 6*a*b*c*d^2 + 3*b^2*c^2*d)*x^4 + 1/3*(3*a^2*c*d^2 + 6*a*b*c^2*d + b^2*c^3)*x^3 + 1/2*(3*a^2*c^2*d + 2*a*b*c^3)*x^2 + a^2*c^3*x^2$

maxima [B] time = 1.34, size = 124, normalized size = 1.91

$$\frac{1}{6} b^2 d^3 x^6 + a^2 c^3 x + \frac{1}{5} (3 b^2 c d^2 + 2 a b d^3) x^5 + \frac{1}{4} (3 b^2 c^2 d + 6 a b c d^2 + a^2 d^3) x^4 + \frac{1}{3} (b^2 c^3 + 6 a b c^2 d + 3 a^2 c d^2) x^3 + \frac{1}{2} (2 a^2 c^2 d + 6 a^2 b c^2 d + 3 a^2 c^2 d^2) x^2 + \frac{1}{6} (2 a^2 b c^2 d + 3 a^2 c^2 d^2) x + \frac{1}{6} a^2 c^2 d^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^3,x, algorithm="maxima")

[Out] 1/6*b^2*d^3*x^6 + a^2*c^3*x + 1/5*(3*b^2*c*d^2 + 2*a*b*d^3)*x^5 + 1/4*(3*b^2*c^2*d + 6*a*b*c*d^2 + a^2*d^3)*x^4 + 1/3*(b^2*c^3 + 6*a*b*c^2*d + 3*a^2*c*d^2)*x^3 + 1/2*(2*a*b*c^2*d + 3*a^2*c^2*d)*x^2 + 1/6*(2*a^2*b*c^2*d + 3*a^2*c^2*d^2)*x + 1/6*a^2*c^2*d^2

mupad [B] time = 0.05, size = 115, normalized size = 1.77

$$x^3 \left(a^2 c d^2 + 2 a b c^2 d + \frac{b^2 c^3}{3} \right) + x^4 \left(\frac{a^2 d^3}{4} + \frac{3 a b c d^2}{2} + \frac{3 b^2 c^2 d}{4} \right) + a^2 c^3 x + \frac{b^2 d^3 x^6}{6} + \frac{a c^2 x^2 (3 a d + 2 b c)}{2} + \frac{b d^2 x^5 (2 a d + 3 b c)}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2*(c + d*x)^3,x)

[Out] x^3*((b^2*c^3)/3 + a^2*c*d^2 + 2*a*b*c^2*d) + x^4*((a^2*d^3)/4 + (3*b^2*c^2*d)/4 + (3*a*b*c*d^2)/2) + a^2*c^3*x + (b^2*d^3*x^6)/6 + (a*c^2*x^2*(3*a*d + 2*b*c))/2 + (b*d^2*x^5*(2*a*d + 3*b*c))/5

sympy [B] time = 0.09, size = 133, normalized size = 2.05

$$a^2 c^3 x + \frac{b^2 d^3 x^6}{6} + x^5 \left(\frac{2 a b d^3}{5} + \frac{3 b^2 c d^2}{5} \right) + x^4 \left(\frac{a^2 d^3}{4} + \frac{3 a b c d^2}{2} + \frac{3 b^2 c^2 d}{4} \right) + x^3 \left(a^2 c d^2 + 2 a b c^2 d + \frac{b^2 c^3}{3} \right) + x^2 \left(\frac{3 a^2 c^2 d}{2} + \frac{3 a^2 b c^2 d}{2} + \frac{3 a^2 c^2 d^2}{2} \right) + \frac{b d^2 x^5 (2 a d + 3 b c)}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2*(d*x+c)**3,x)

[Out] a**2*c**3*x + b**2*d**3*x**6/6 + x**5*(2*a*b*d**3/5 + 3*b**2*c*d**2/5) + x**4*(a**2*d**3/4 + 3*a*b*c*d**2/2 + 3*b**2*c**2*d/4) + x**3*(a**2*c*d**2 + 2*a*b*c**2*d + b**2*c**3/3) + x**2*(3*a**2*c**2*d/2 + a*b*c**3)

3.1262 $\int (a + bx)(c + dx)^3 dx$

Optimal. Leaf size=38

$$\frac{b(c + dx)^5}{5d^2} - \frac{(c + dx)^4(bc - ad)}{4d^2}$$

[Out] $-1/4*(-a*d+b*c)*(d*x+c)^4/d^2+1/5*b*(d*x+c)^5/d^2$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{b(c + dx)^5}{5d^2} - \frac{(c + dx)^4(bc - ad)}{4d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(c + d*x)^3, x]

[Out] $-((b*c - a*d)*(c + d*x)^4)/(4*d^2) + (b*(c + d*x)^5)/(5*d^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)(c + dx)^3 dx &= \int \left(\frac{(-bc + ad)(c + dx)^3}{d} + \frac{b(c + dx)^4}{d} \right) dx \\ &= -\frac{(bc - ad)(c + dx)^4}{4d^2} + \frac{b(c + dx)^5}{5d^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 67, normalized size = 1.76

$$\frac{1}{2}c^2x^2(3ad + bc) + \frac{1}{4}d^2x^4(ad + 3bc) + cdx^3(ad + bc) + ac^3x + \frac{1}{5}bd^3x^5$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(c + d*x)^3, x]

[Out] $a*c^3*x + (c^2*(b*c + 3*a*d)*x^2)/2 + c*d*(b*c + a*d)*x^3 + (d^2*(3*b*c + a*d)*x^4)/4 + (b*d^3*x^5)/5$

fricas [B] time = 0.41, size = 72, normalized size = 1.89

$$\frac{1}{5}x^5d^3b + \frac{3}{4}x^4d^2cb + \frac{1}{4}x^4d^3a + x^3dc^2b + x^3d^2ca + \frac{1}{2}x^2c^3b + \frac{3}{2}x^2dc^2a + xc^3a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c)^3,x, algorithm="fricas")`

[Out] $1/5*x^5*d^3*b + 3/4*x^4*d^2*c*b + 1/4*x^4*d^3*a + x^3*d*c^2*b + x^3*d^2*c*a + 1/2*x^2*c^3*b + 3/2*x^2*d*c^2*a + x*c^3*a$

giac [B] time = 0.88, size = 72, normalized size = 1.89

$$\frac{1}{5}bd^3x^5 + \frac{3}{4}bcd^2x^4 + \frac{1}{4}ad^3x^4 + bc^2dx^3 + acd^2x^3 + \frac{1}{2}bc^3x^2 + \frac{3}{2}ac^2dx^2 + ac^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c)^3,x, algorithm="giac")`

[Out] $1/5*b*d^3*x^5 + 3/4*b*c*d^2*x^4 + 1/4*a*d^3*x^4 + b*c^2*d*x^3 + a*c*d^2*x^3 + 1/2*b*c^3*x^2 + 3/2*a*c^2*d*x^2 + a*c^3*x$

maple [B] time = 0.00, size = 73, normalized size = 1.92

$$\frac{bd^3x^5}{5} + ac^3x + \frac{(ad^3 + 3bcd^2)x^4}{4} + \frac{(3acd^2 + 3bc^2d)x^3}{3} + \frac{(3ac^2d + bc^3)x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)*(d*x+c)^3,x)`

[Out] $1/5*b*d^3*x^5 + 1/4*(a*d^3 + 3*b*c*d^2)*x^4 + 1/3*(3*a*c*d^2 + 3*b*c^2*d)*x^3 + 1/2*(3*a*c^2*d + b*c^3)*x^2 + a*c^3*x$

maxima [B] time = 1.39, size = 69, normalized size = 1.82

$$\frac{1}{5}bd^3x^5 + ac^3x + \frac{1}{4}(3bcd^2 + ad^3)x^4 + (bc^2d + acd^2)x^3 + \frac{1}{2}(bc^3 + 3ac^2d)x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c)^3,x, algorithm="maxima")`

[Out] $1/5*b*d^3*x^5 + a*c^3*x + 1/4*(3*b*c*d^2 + a*d^3)*x^4 + (b*c^2*d + a*c*d^2)*x^3 + 1/2*(b*c^3 + 3*a*c^2*d)*x^2$

mupad [B] time = 0.03, size = 65, normalized size = 1.71

$$x^2 \left(\frac{bc^3}{2} + \frac{3adc^2}{2} \right) + x^4 \left(\frac{ad^3}{4} + \frac{3bcd^2}{4} \right) + \frac{bd^3x^5}{5} + ac^3x + cdx^3(ad + bc)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)*(c + d*x)^3,x)`

[Out] $x^2*((b*c^3)/2 + (3*a*c^2*d)/2) + x^4*((a*d^3)/4 + (3*b*c*d^2)/4) + (b*d^3*x^5)/5 + a*c^3*x + c*d*x^3*(a*d + b*c)$

sympy [B] time = 0.08, size = 73, normalized size = 1.92

$$ac^3x + \frac{bd^3x^5}{5} + x^4 \left(\frac{ad^3}{4} + \frac{3bcd^2}{4} \right) + x^3(acd^2 + bc^2d) + x^2 \left(\frac{3ac^2d}{2} + \frac{bc^3}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c)**3,x)`

[Out] $a*c**3*x + b*d**3*x**5/5 + x**4*(a*d**3/4 + 3*b*c*d**2/4) + x**3*(a*c*d**2 + b*c**2*d) + x**2*(3*a*c**2*d/2 + b*c**3/2)$

3.1263 $\int (c + dx)^3 dx$

Optimal. Leaf size=14

$$\frac{(c + dx)^4}{4d}$$

[Out] 1/4*(d*x+c)^4/d

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(c + dx)^4}{4d}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3,x]

[Out] (c + d*x)^4/(4*d)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (c + dx)^3 dx = \frac{(c + dx)^4}{4d}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{(c + dx)^4}{4d}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3,x]

[Out] (c + d*x)^4/(4*d)

fricas [B] time = 0.53, size = 31, normalized size = 2.21

$$\frac{1}{4}x^4d^3 + x^3d^2c + \frac{3}{2}x^2dc^2 + xc^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3,x, algorithm="fricas")

[Out] 1/4*x^4*d^3 + x^3*d^2*c + 3/2*x^2*d*c^2 + x*c^3

giac [A] time = 1.00, size = 12, normalized size = 0.86

$$\frac{(dx + c)^4}{4d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3,x, algorithm="giac")

[Out] 1/4*(d*x + c)^4/d

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{(dx + c)^4}{4d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3,x)

[Out] 1/4*(d*x+c)^4/d

maxima [B] time = 1.35, size = 31, normalized size = 2.21

$$\frac{1}{4}d^3x^4 + cd^2x^3 + \frac{3}{2}c^2dx^2 + c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3,x, algorithm="maxima")

[Out] 1/4*d^3*x^4 + c*d^2*x^3 + 3/2*c^2*d*x^2 + c^3*x

mupad [B] time = 0.04, size = 31, normalized size = 2.21

$$c^3x + \frac{3c^2dx^2}{2} + cd^2x^3 + \frac{d^3x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3,x)

[Out] c^3*x + (d^3*x^4)/4 + (3*c^2*d*x^2)/2 + c*d^2*x^3

sympy [B] time = 0.06, size = 32, normalized size = 2.29

$$c^3x + \frac{3c^2dx^2}{2} + cd^2x^3 + \frac{d^3x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3,x)

[Out] c**3*x + 3*c**2*d*x**2/2 + c*d**2*x**3 + d**3*x**4/4

$$3.1264 \quad \int \frac{(c+dx)^3}{a+bx} dx$$

Optimal. Leaf size=73

$$\frac{(bc-ad)^3 \log(a+bx)}{b^4} + \frac{dx(bc-ad)^2}{b^3} + \frac{(c+dx)^2(bc-ad)}{2b^2} + \frac{(c+dx)^3}{3b}$$

[Out] $d*(-a*d+b*c)^2*x/b^3+1/2*(-a*d+b*c)*(d*x+c)^2/b^2+1/3*(d*x+c)^3/b+(-a*d+b*c)^3*\ln(b*x+a)/b^4$

Rubi [A] time = 0.03, antiderivative size = 73, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{dx(bc-ad)^2}{b^3} + \frac{(c+dx)^2(bc-ad)}{2b^2} + \frac{(bc-ad)^3 \log(a+bx)}{b^4} + \frac{(c+dx)^3}{3b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + b*x), x]

[Out] $(d*(b*c - a*d)^2*x)/b^3 + ((b*c - a*d)*(c + d*x)^2)/(2*b^2) + (c + d*x)^3/(3*b) + ((b*c - a*d)^3*\text{Log}[a + b*x])/b^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^3}{a+bx} dx &= \int \left(\frac{d(bc-ad)^2}{b^3} + \frac{(bc-ad)^3}{b^3(a+bx)} + \frac{d(bc-ad)(c+dx)}{b^2} + \frac{d(c+dx)^2}{b} \right) dx \\ &= \frac{d(bc-ad)^2x}{b^3} + \frac{(bc-ad)(c+dx)^2}{2b^2} + \frac{(c+dx)^3}{3b} + \frac{(bc-ad)^3 \log(a+bx)}{b^4} \end{aligned}$$

Mathematica [A] time = 0.03, size = 74, normalized size = 1.01

$$\frac{bdx(6a^2d^2 - 3abd(6c + dx) + b^2(18c^2 + 9cdx + 2d^2x^2)) + 6(bc - ad)^3 \log(a + bx)}{6b^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + b*x),x]

[Out] (b*d*x*(6*a^2*d^2 - 3*a*b*d*(6*c + d*x) + b^2*(18*c^2 + 9*c*d*x + 2*d^2*x^2)) + 6*(b*c - a*d)^3*Log[a + b*x])/(6*b^4)

fricas [A] time = 0.52, size = 116, normalized size = 1.59

$$\frac{2b^3d^3x^3 + 3(3b^3cd^2 - ab^2d^3)x^2 + 6(3b^3c^2d - 3ab^2cd^2 + a^2bd^3)x + 6(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)\log(bx + a)}{6b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a),x, algorithm="fricas")

[Out] 1/6*(2*b^3*d^3*x^3 + 3*(3*b^3*c*d^2 - a*b^2*d^3)*x^2 + 6*(3*b^3*c^2*d - 3*a*b^2*c*d^2 + a^2*b*d^3)*x + 6*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*log(b*x + a))/b^4

giac [A] time = 1.03, size = 115, normalized size = 1.58

$$\frac{2b^2d^3x^3 + 9b^2cd^2x^2 - 3abd^3x^2 + 18b^2c^2dx - 18abcd^2x + 6a^2d^3x}{6b^3} + \frac{(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)\log(|bx + a|)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a),x, algorithm="giac")

[Out] 1/6*(2*b^2*d^3*x^3 + 9*b^2*c*d^2*x^2 - 3*a*b*d^3*x^2 + 18*b^2*c^2*d*x - 18*a*b*c*d^2*x + 6*a^2*d^3*x)/b^3 + (b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*log(abs(b*x + a))/b^4

maple [A] time = 0.00, size = 133, normalized size = 1.82

$$\frac{d^3x^3}{3b} - \frac{ad^3x^2}{2b^2} + \frac{3cd^2x^2}{2b} - \frac{a^3d^3\ln(bx+a)}{b^4} + \frac{3a^2cd^2\ln(bx+a)}{b^3} + \frac{a^2d^3x}{b^3} - \frac{3ac^2d\ln(bx+a)}{b^2} - \frac{3acd^2x}{b^2} + \frac{c^3\ln(bx+a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(b*x+a),x)

[Out] 1/3*d^3/b*x^3-1/2*d^3/b^2*x^2*a+3/2*d^2/b*x^2*c+d^3/b^3*a^2*x-3*d^2/b^2*a*c*x+3*d/b*c^2*x-1/b^4*ln(b*x+a)*a^3*d^3+3/b^3*ln(b*x+a)*a^2*c*d^2-3/b^2*ln(b*x+a)*a*c^2*d+1/b*ln(b*x+a)*c^3

maxima [A] time = 1.33, size = 114, normalized size = 1.56

$$\frac{2b^2d^3x^3 + 3(3b^2cd^2 - abd^3)x^2 + 6(3b^2c^2d - 3abcd^2 + a^2d^3)x + (b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)\log(bx + a)}{6b^3} + \frac{c^3\ln(bx + a)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^3/(b*x+a),x, algorithm="maxima")`

[Out] $\frac{1}{6}*(2*b^2*d^3*x^3 + 3*(3*b^2*c*d^2 - a*b*d^3)*x^2 + 6*(3*b^2*c^2*d - 3*a*b*c*d^2 + a^2*d^3)*x)/b^3 + (b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*\log(b*x + a)/b^4$

mupad [B] time = 0.20, size = 118, normalized size = 1.62

$$x \left(\frac{3c^2d}{b} + \frac{a \left(\frac{ad^3}{b^2} - \frac{3cd^2}{b} \right)}{b} \right) - x^2 \left(\frac{ad^3}{2b^2} - \frac{3cd^2}{2b} \right) + \frac{d^3x^3}{3b} - \frac{\ln(ax+b)(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^3/(a + b*x),x)`

[Out] $x*((3*c^2*d)/b + (a*((a*d^3)/b^2 - (3*c*d^2)/b))/b - x^2*((a*d^3)/(2*b^2) - (3*c*d^2)/(2*b)) + (d^3*x^3)/(3*b) - (\log(a + b*x)*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2))/b^4$

sympy [A] time = 0.30, size = 83, normalized size = 1.14

$$x^2 \left(-\frac{ad^3}{2b^2} + \frac{3cd^2}{2b} \right) + x \left(\frac{a^2d^3}{b^3} - \frac{3acd^2}{b^2} + \frac{3c^2d}{b} \right) + \frac{d^3x^3}{3b} - \frac{(ad-bc)^3 \log(ax+b)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**3/(b*x+a),x)`

[Out] $x**2*(-a*d**3/(2*b**2) + 3*c*d**2/(2*b)) + x*(a**2*d**3/b**3 - 3*a*c*d**2/b**2 + 3*c**2*d/b) + d**3*x**3/(3*b) - (a*d - b*c)**3*\log(a + b*x)/b**4$

$$3.1265 \quad \int \frac{(c+dx)^3}{(a+bx)^2} dx$$

Optimal. Leaf size=75

$$-\frac{(bc-ad)^3}{b^4(a+bx)} + \frac{3d(bc-ad)^2 \log(a+bx)}{b^4} + \frac{d^2x(3bc-2ad)}{b^3} + \frac{d^3x^2}{2b^2}$$

[Out] $d^2*(-2*a*d+3*b*c)*x/b^3+1/2*d^3*x^2/b^2-(-a*d+b*c)^3/b^4/(b*x+a)+3*d*(-a*d+b*c)^2*\ln(b*x+a)/b^4$

Rubi [A] time = 0.06, antiderivative size = 75, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{d^2x(3bc-2ad)}{b^3} - \frac{(bc-ad)^3}{b^4(a+bx)} + \frac{3d(bc-ad)^2 \log(a+bx)}{b^4} + \frac{d^3x^2}{2b^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + b*x)^2, x]

[Out] $(d^2*(3*b*c - 2*a*d)*x)/b^3 + (d^3*x^2)/(2*b^2) - (b*c - a*d)^3/(b^4*(a + b*x)) + (3*d*(b*c - a*d)^2*\text{Log}[a + b*x])/b^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^3}{(a+bx)^2} dx &= \int \left(\frac{d^2(3bc-2ad)}{b^3} + \frac{d^3x}{b^2} + \frac{(bc-ad)^3}{b^3(a+bx)^2} + \frac{3d(bc-ad)^2}{b^3(a+bx)} \right) dx \\ &= \frac{d^2(3bc-2ad)x}{b^3} + \frac{d^3x^2}{2b^2} - \frac{(bc-ad)^3}{b^4(a+bx)} + \frac{3d(bc-ad)^2 \log(a+bx)}{b^4} \end{aligned}$$

Mathematica [A] time = 0.05, size = 72, normalized size = 0.96

$$\frac{2bd^2x(3bc-2ad) - \frac{2(bc-ad)^3}{a+bx} + 6d(bc-ad)^2 \log(a+bx) + b^2d^3x^2}{2b^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + b*x)^2,x]

[Out] $(2*b*d^2*(3*b*c - 2*a*d)*x + b^2*d^3*x^2 - (2*(b*c - a*d)^3)/(a + b*x) + 6*d*(b*c - a*d)^2*\text{Log}[a + b*x])/(2*b^4)$

fricas [B] time = 0.58, size = 173, normalized size = 2.31

$$\frac{b^3 d^3 x^3 - 2 b^3 c^3 + 6 a b^2 c^2 d - 6 a^2 b c d^2 + 2 a^3 d^3 + 3 (2 b^3 c d^2 - a b^2 d^3) x^2 + 2 (3 a b^2 c d^2 - 2 a^2 b d^3) x + 6 (a b^2 c^2 d - 2 a^2 b c^2) + 2 (b^5 x + a b^4)}{2 (b^5 x + a b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^2,x, algorithm="fricas")

[Out] $1/2*(b^3*d^3*x^3 - 2*b^3*c^3 + 6*a*b^2*c^2*d - 6*a^2*b*c*d^2 + 2*a^3*d^3 + 3*(2*b^3*c*d^2 - a*b^2*d^3)*x^2 + 2*(3*a*b^2*c*d^2 - 2*a^2*b*d^3)*x + 6*(a*b^2*c^2*d - 2*a^2*b*c*d^2 + a^3*d^3 + (b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*x)*\text{log}(b*x + a))/(b^5*x + a*b^4)$

giac [B] time = 0.99, size = 167, normalized size = 2.23

$$\frac{\left(d^3 + \frac{6(b^2cd^2 - abd^3)}{(bx+a)b}\right)(bx+a)^2}{2b^4} - \frac{3(b^2c^2d - 2abcd^2 + a^2d^3)\log\left(\frac{|bx+a|}{(bx+a)^2|b|}\right)}{b^4} - \frac{\frac{b^5c^3}{bx+a} - \frac{3ab^4c^2d}{bx+a} + \frac{3a^2b^3cd^2}{bx+a} - \frac{a^3b^2d^3}{bx+a}}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^2,x, algorithm="giac")

[Out] $1/2*(d^3 + 6*(b^2*c*d^2 - a*b*d^3)/((b*x + a)*b))*(b*x + a)^2/b^4 - 3*(b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3)*\text{log}(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b)))/b^4 - (b^5*c^3/(b*x + a) - 3*a*b^4*c^2*d/(b*x + a) + 3*a^2*b^3*c*d^2/(b*x + a) - a^3*b^2*d^3/(b*x + a))/b^6$

maple [B] time = 0.01, size = 149, normalized size = 1.99

$$\frac{d^3 x^2}{2b^2} + \frac{a^3 d^3}{(bx+a)b^4} - \frac{3a^2 c d^2}{(bx+a)b^3} + \frac{3a^2 d^3 \ln(bx+a)}{b^4} + \frac{3a c^2 d}{(bx+a)b^2} - \frac{6ac d^2 \ln(bx+a)}{b^3} - \frac{2a d^3 x}{b^3} - \frac{c^3}{(bx+a)b} + \frac{3c^2 d \ln(bx+a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(b*x+a)^2,x)

[Out] $1/2*d^3*x^2/b^2 - 2*d^3/b^3*a*x + 3*d^2/b^2*x*c + 3/b^4*d^3*\text{ln}(b*x+a)*a^2 - 6/b^3*d^2*\text{ln}(b*x+a)*a*c + 3/b^2*d*\text{ln}(b*x+a)*c^2 + 1/b^4/(b*x+a)*a^3*d^3 - 3/b^3/(b*x+a)*a^2*c*d^2 + 3/b^2/(b*x+a)*a*c^2*d - 1/b/(b*x+a)*c^3$

maxima [A] time = 1.32, size = 118, normalized size = 1.57

$$-\frac{b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3}{b^5x + ab^4} + \frac{bd^3x^2 + 2(3bcd^2 - 2ad^3)x}{2b^3} + \frac{3(b^2c^2d - 2abcd^2 + a^2d^3)\log(bx + a)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^2,x, algorithm="maxima")

[Out] $-(b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3)/(b^5x + ab^4) + 1/2*(b*d^3*x^2 + 2*(3*b*c*d^2 - 2*a*d^3)*x)/b^3 + 3*(b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3)*\log(b*x + a)/b^4$

mupad [B] time = 0.21, size = 123, normalized size = 1.64

$$\frac{\ln(a + bx) (3a^2d^3 - 6abcd^2 + 3b^2c^2d)}{b^4} - x \left(\frac{2ad^3}{b^3} - \frac{3cd^2}{b^2} \right) + \frac{a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3}{b(xb^4 + ab^3)} + \frac{d^3x^2}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + b*x)^2,x)

[Out] $(\log(a + b*x)*(3*a^2*d^3 + 3*b^2*c^2*d - 6*a*b*c*d^2))/b^4 - x*((2*a*d^3)/b^3 - (3*c*d^2)/b^2) + (a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2)/(b*(a*b^3 + b^4*x)) + (d^3*x^2)/(2*b^2)$

sympy [A] time = 0.50, size = 102, normalized size = 1.36

$$x \left(-\frac{2ad^3}{b^3} + \frac{3cd^2}{b^2} \right) + \frac{a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3}{ab^4 + b^5x} + \frac{d^3x^2}{2b^2} + \frac{3d(ad - bc)^2 \log(a + bx)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3/(b*x+a)**2,x)

[Out] $x*(-2*a*d**3/b**3 + 3*c*d**2/b**2) + (a**3*d**3 - 3*a**2*b*c*d**2 + 3*a*b**2*c**2*d - b**3*c**3)/(a*b**4 + b**5*x) + d**3*x**2/(2*b**2) + 3*d*(a*d - b*c)**2*\log(a + b*x)/b**4$

$$3.1266 \quad \int \frac{(c+dx)^3}{(a+bx)^3} dx$$

Optimal. Leaf size=78

$$\frac{3d^2(bc-ad)\log(a+bx)}{b^4} - \frac{3d(bc-ad)^2}{b^4(a+bx)} - \frac{(bc-ad)^3}{2b^4(a+bx)^2} + \frac{d^3x}{b^3}$$

[Out] $d^3x/b^3 - 1/2*(-a*d+b*c)^3/b^4/(b*x+a)^2 - 3*d*(-a*d+b*c)^2/b^4/(b*x+a) + 3*d^2*(-a*d+b*c)*\ln(b*x+a)/b^4$

Rubi [A] time = 0.05, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{3d^2(bc-ad)\log(a+bx)}{b^4} - \frac{3d(bc-ad)^2}{b^4(a+bx)} - \frac{(bc-ad)^3}{2b^4(a+bx)^2} + \frac{d^3x}{b^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + b*x)^3, x]

[Out] $(d^3x)/b^3 - (b*c - a*d)^3/(2*b^4*(a + b*x)^2) - (3*d*(b*c - a*d)^2)/(b^4*(a + b*x)) + (3*d^2*(b*c - a*d)*\text{Log}[a + b*x])/b^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^3}{(a+bx)^3} dx &= \int \left(\frac{d^3}{b^3} + \frac{(bc-ad)^3}{b^3(a+bx)^3} + \frac{3d(bc-ad)^2}{b^3(a+bx)^2} + \frac{3d^2(bc-ad)}{b^3(a+bx)} \right) dx \\ &= \frac{d^3x}{b^3} - \frac{(bc-ad)^3}{2b^4(a+bx)^2} - \frac{3d(bc-ad)^2}{b^4(a+bx)} + \frac{3d^2(bc-ad)\log(a+bx)}{b^4} \end{aligned}$$

Mathematica [A] time = 0.04, size = 114, normalized size = 1.46

$$\frac{-5a^3d^3 + a^2bd^2(9c - 4dx) + ab^2d(-3c^2 + 12cdx + 4d^2x^2) - 6d^2(a+bx)^2(ad-bc)\log(a+bx) - (b^3(c^3 + 6c^2dx))}{2b^4(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + b*x)^3,x]

[Out] $(-5a^3d^3 + a^2bd^2(9c - 4d)x + ab^2d(-3c^2 + 12cdx + 4d^2x^2) - b^3(c^3 + 6c^2dx - 2d^3x^3) - 6d^2(-(b^3c) + ad)(a + b*x)^2 * \log[a + b*x]) / (2b^4(a + b*x)^2)$

fricas [B] time = 0.78, size = 188, normalized size = 2.41

$$\frac{2b^3d^3x^3 + 4ab^2d^3x^2 - b^3c^3 - 3ab^2c^2d + 9a^2bcd^2 - 5a^3d^3 - 2(3b^3c^2d - 6ab^2cd^2 + 2a^2bd^3)x + 6(a^2bcd^2 - a^3d^3)}{2(b^6x^2 + 2ab^5x + a^2b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^3,x, algorithm="fricas")

[Out] $1/2*(2b^3d^3x^3 + 4a*b^2d^3x^2 - b^3c^3 - 3a*b^2c^2d + 9a^2b*c*d^2 - 5a^3d^3 - 2*(3b^3c^2d - 6a*b^2c*d^2 + 2a^2*b*d^3)*x + 6*(a^2*b*c*d^2 - a^3*d^3 + (b^3*c*d^2 - a*b^2*d^3)*x^2 + 2*(a*b^2*c*d^2 - a^2*b*d^3)*x)*\log(b*x + a)) / (b^6*x^2 + 2*a*b^5*x + a^2*b^4)$

giac [A] time = 0.95, size = 112, normalized size = 1.44

$$\frac{d^3x}{b^3} + \frac{3(bcd^2 - ad^3)\log(|bx + a|)}{b^4} - \frac{b^3c^3 + 3ab^2c^2d - 9a^2bcd^2 + 5a^3d^3 + 6(b^3c^2d - 2ab^2cd^2 + a^2bd^3)x}{2(bx + a)^2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^3,x, algorithm="giac")

[Out] $d^3x/b^3 + 3*(b*c*d^2 - a*d^3)*\log(\text{abs}(b*x + a))/b^4 - 1/2*(b^3*c^3 + 3a*b^2*c^2*d - 9a^2*b*c*d^2 + 5a^3*d^3 + 6*(b^3*c^2*d - 2a*b^2*c*d^2 + a^2*b*d^3)*x) / ((b*x + a)^2*b^4)$

maple [B] time = 0.01, size = 160, normalized size = 2.05

$$\frac{a^3d^3}{2(bx + a)^2b^4} - \frac{3a^2cd^2}{2(bx + a)^2b^3} + \frac{3ac^2d}{2(bx + a)^2b^2} - \frac{c^3}{2(bx + a)^2b} - \frac{3a^2d^3}{(bx + a)b^4} + \frac{6acd^2}{(bx + a)b^3} - \frac{3ad^3 \ln(bx + a)}{b^4} - \frac{3c^2d}{(bx + a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(b*x+a)^3,x)

[Out] $d^3x/b^3 + 1/2/b^4/(b*x+a)^2*a^3*d^3 - 3/2/b^3/(b*x+a)^2*a^2*c*d^2 + 3/2/b^2/(b*x+a)^2*a*c^2*d - 1/2/b/(b*x+a)^2*c^3 - 3/b^4*d^3*\ln(b*x+a)*a + 3/b^3*d^2*\ln(b*x+a)*c - 3/b^4*d^3/(b*x+a)*a^2 + 6/b^3*d^2/(b*x+a)*a*c - 3/b^2*d/(b*x+a)*c^2$

maxima [A] time = 1.37, size = 125, normalized size = 1.60

$$\frac{d^3 x}{b^3} - \frac{b^3 c^3 + 3 a b^2 c^2 d - 9 a^2 b c d^2 + 5 a^3 d^3 + 6 (b^3 c^2 d - 2 a b^2 c d^2 + a^2 b d^3) x}{2 (b^6 x^2 + 2 a b^5 x + a^2 b^4)} + \frac{3 (b c d^2 - a d^3) \log (b x + a)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^3,x, algorithm="maxima")

[Out] $d^3 x / b^3 - 1/2 * (b^3 c^3 + 3 a b^2 c^2 d - 9 a^2 b c d^2 + 5 a^3 d^3 + 6 (b^3 c^2 d - 2 a b^2 c d^2 + a^2 b d^3) x) / (b^6 x^2 + 2 a b^5 x + a^2 b^4) + 3 * (b c d^2 - a d^3) * \log (b x + a) / b^4$

mupad [B] time = 0.82, size = 130, normalized size = 1.67

$$\frac{d^3 x}{b^3} - \frac{\ln (a + b x) (3 a d^3 - 3 b c d^2)}{b^4} - \frac{5 a^3 d^3 - 9 a^2 b c d^2 + 3 a b^2 c^2 d + b^3 c^3}{2 b} + \frac{x (3 a^2 d^3 - 6 a b c d^2 + 3 b^2 c^2 d)}{a^2 b^3 + 2 a b^4 x + b^5 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + b*x)^3,x)

[Out] $(d^3 x) / b^3 - (\log (a + b x) * (3 a d^3 - 3 b c d^2)) / b^4 - ((5 a^3 d^3 + b^3 c^3 + 3 a b^2 c^2 d - 9 a^2 b c d^2) / (2 b) + x * (3 a^2 d^3 + 3 b^2 c^2 d - 6 a b c d^2)) / (a^2 b^3 + b^5 x^2 + 2 a b^4 x)$

sympy [A] time = 0.82, size = 128, normalized size = 1.64

$$\frac{-5 a^3 d^3 + 9 a^2 b c d^2 - 3 a b^2 c^2 d - b^3 c^3 + x (-6 a^2 b d^3 + 12 a b^2 c d^2 - 6 b^3 c^2 d)}{2 a^2 b^4 + 4 a b^5 x + 2 b^6 x^2} + \frac{d^3 x}{b^3} - \frac{3 d^2 (a d - b c) \log (a + b x)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3/(b*x+a)**3,x)

[Out] $(-5 a^3 d^3 + 9 a^2 b c d^2 - 3 a b^2 c^2 d - b^3 c^3 + x (-6 a^2 b d^3 + 12 a b^2 c d^2 - 6 b^3 c^2 d)) / (2 a^2 b^4 + 4 a b^5 x + 2 b^6 x^2) + d^3 x / b^3 - 3 d^2 * (a d - b c) * \log (a + b x) / b^4$

$$3.1267 \quad \int \frac{(c+dx)^3}{(a+bx)^4} dx$$

Optimal. Leaf size=86

$$-\frac{3d^2(bc-ad)}{b^4(a+bx)} - \frac{3d(bc-ad)^2}{2b^4(a+bx)^2} - \frac{(bc-ad)^3}{3b^4(a+bx)^3} + \frac{d^3 \log(a+bx)}{b^4}$$

[Out] $-1/3*(-a*d+b*c)^3/b^4/(b*x+a)^3-3/2*d*(-a*d+b*c)^2/b^4/(b*x+a)^2-3*d^2*(-a*d+b*c)/b^4/(b*x+a)+d^3*\ln(b*x+a)/b^4$

Rubi [A] time = 0.05, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{3d^2(bc-ad)}{b^4(a+bx)} - \frac{3d(bc-ad)^2}{2b^4(a+bx)^2} - \frac{(bc-ad)^3}{3b^4(a+bx)^3} + \frac{d^3 \log(a+bx)}{b^4}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + b*x)^4, x]

[Out] $-(b*c - a*d)^3/(3*b^4*(a + b*x)^3) - (3*d*(b*c - a*d)^2)/(2*b^4*(a + b*x)^2) - (3*d^2*(b*c - a*d))/(b^4*(a + b*x)) + (d^3*\text{Log}[a + b*x])/b^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^3}{(a+bx)^4} dx &= \int \left(\frac{(bc-ad)^3}{b^3(a+bx)^4} + \frac{3d(bc-ad)^2}{b^3(a+bx)^3} + \frac{3d^2(bc-ad)}{b^3(a+bx)^2} + \frac{d^3}{b^3(a+bx)} \right) dx \\ &= -\frac{(bc-ad)^3}{3b^4(a+bx)^3} - \frac{3d(bc-ad)^2}{2b^4(a+bx)^2} - \frac{3d^2(bc-ad)}{b^4(a+bx)} + \frac{d^3 \log(a+bx)}{b^4} \end{aligned}$$

Mathematica [A] time = 0.04, size = 80, normalized size = 0.93

$$\frac{6d^3 \log(a+bx) - \frac{(bc-ad)(11a^2d^2+abd(5c+27dx)+b^2(2c^2+9cdx+18d^2x^2))}{(a+bx)^3}}{6b^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + b*x)^4,x]

[Out] $(-(((b*c - a*d)*(11*a^2*d^2 + a*b*d*(5*c + 27*d*x) + b^2*(2*c^2 + 9*c*d*x + 18*d^2*x^2)))/(a + b*x)^3) + 6*d^3*\text{Log}[a + b*x])/(6*b^4)$

fricas [B] time = 0.44, size = 176, normalized size = 2.05

$$\frac{2b^3c^3 + 3ab^2c^2d + 6a^2bcd^2 - 11a^3d^3 + 18(b^3cd^2 - ab^2d^3)x^2 + 9(b^3c^2d + 2ab^2cd^2 - 3a^2bd^3)x - 6(b^3d^3x^3 + 6(b^7x^3 + 3ab^6x^2 + 3a^2b^5x + a^3b^4))}{6(b^7x^3 + 3ab^6x^2 + 3a^2b^5x + a^3b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^4,x, algorithm="fricas")

[Out] $-1/6*(2*b^3*c^3 + 3*a*b^2*c^2*d + 6*a^2*b*c*d^2 - 11*a^3*d^3 + 18*(b^3*c*d^2 - a*b^2*d^3)*x^2 + 9*(b^3*c^2*d + 2*a*b^2*c*d^2 - 3*a^2*b*d^3)*x - 6*(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)*\text{log}(b*x + a))/(b^7*x^3 + 3*a*b^6*x^2 + 3*a^2*b^5*x + a^3*b^4)$

giac [A] time = 0.94, size = 118, normalized size = 1.37

$$\frac{d^3 \log(|bx + a|)}{b^4} - \frac{18(b^2cd^2 - abd^3)x^2 + 9(b^2c^2d + 2abcd^2 - 3a^2d^3)x + \frac{2b^3c^3 + 3ab^2c^2d + 6a^2bcd^2 - 11a^3d^3}{b}}{6(bx + a)^3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^4,x, algorithm="giac")

[Out] $d^3*\text{log}(\text{abs}(b*x + a))/b^4 - 1/6*(18*(b^2*c*d^2 - a*b*d^3)*x^2 + 9*(b^2*c^2*d + 2*a*b*c*d^2 - 3*a^2*d^3)*x + (2*b^3*c^3 + 3*a*b^2*c^2*d + 6*a^2*b*c*d^2 - 11*a^3*d^3)/b)/((b*x + a)^3*b^3)$

maple [B] time = 0.01, size = 166, normalized size = 1.93

$$\frac{a^3d^3}{3(bx + a)^3b^4} - \frac{a^2cd^2}{(bx + a)^3b^3} + \frac{ac^2d}{(bx + a)^3b^2} - \frac{c^3}{3(bx + a)^3b} - \frac{3a^2d^3}{2(bx + a)^2b^4} + \frac{3acd^2}{(bx + a)^2b^3} - \frac{3c^2d}{2(bx + a)^2b^2} + \frac{3ad^3}{(bx + a)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(b*x+a)^4,x)

[Out] $1/3/b^4/(b*x+a)^3*a^3*d^3 - 1/b^3/(b*x+a)^3*a^2*c*d^2 + 1/b^2/(b*x+a)^3*a*c^2*d - 1/3/b/(b*x+a)^3*c^3 - 3/2*d^3/b^4/(b*x+a)^2*a^2 + 3*d^2/b^3/(b*x+a)^2*a*c - 3/2*$

$d/b^2/(b*x+a)^2*c^2+d^3*\ln(b*x+a)/b^4+3/b^4*d^3/(b*x+a)*a-3/b^3*d^2/(b*x+a)*c$

maxima [A] time = 1.35, size = 142, normalized size = 1.65

$$\frac{2b^3c^3 + 3ab^2c^2d + 6a^2bcd^2 - 11a^3d^3 + 18(b^3cd^2 - ab^2d^3)x^2 + 9(b^3c^2d + 2ab^2cd^2 - 3a^2bd^3)x}{6(b^7x^3 + 3ab^6x^2 + 3a^2b^5x + a^3b^4)} + \frac{d^3 \log(bx + a)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^4,x, algorithm="maxima")

[Out] $-1/6*(2*b^3*c^3 + 3*a*b^2*c^2*d + 6*a^2*b*c*d^2 - 11*a^3*d^3 + 18*(b^3*c*d^2 - a*b^2*d^3)*x^2 + 9*(b^3*c^2*d + 2*a*b^2*c*d^2 - 3*a^2*b*d^3)*x)/(b^7*x^3 + 3*a*b^6*x^2 + 3*a^2*b^5*x + a^3*b^4) + d^3*\log(b*x + a)/b^4$

mupad [B] time = 0.25, size = 138, normalized size = 1.60

$$\frac{d^3 \ln(a + bx)}{b^4} - \frac{-11a^3d^3 + 6a^2bcd^2 + 3ab^2c^2d + 2b^3c^3}{6b^4} + \frac{3x(-3a^2d^3 + 2abcd^2 + b^2c^2d)}{2b^3} - \frac{3d^2x^2(ad - bc)}{b^2}$$

$$a^3 + 3a^2bx + 3ab^2x^2 + b^3x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + b*x)^4,x)

[Out] $(d^3*\log(a + b*x))/b^4 - ((2*b^3*c^3 - 11*a^3*d^3 + 3*a*b^2*c^2*d + 6*a^2*b*c*d^2)/(6*b^4) + (3*x*(b^2*c^2*d - 3*a^2*d^3 + 2*a*b*c*d^2))/(2*b^3) - (3*d^2*x^2*(a*d - b*c))/b^2)/(a^3 + b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x)$

sympy [A] time = 1.13, size = 148, normalized size = 1.72

$$\frac{11a^3d^3 - 6a^2bcd^2 - 3ab^2c^2d - 2b^3c^3 + x^2(18ab^2d^3 - 18b^3cd^2) + x(27a^2bd^3 - 18ab^2cd^2 - 9b^3c^2d)}{6a^3b^4 + 18a^2b^5x + 18ab^6x^2 + 6b^7x^3} + \frac{d^3 \log(a + bx)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3/(b*x+a)**4,x)

[Out] $(11*a**3*d**3 - 6*a**2*b*c*d**2 - 3*a*b**2*c**2*d - 2*b**3*c**3 + x**2*(18*a*b**2*d**3 - 18*b**3*c*d**2) + x*(27*a**2*b*d**3 - 18*a*b**2*c*d**2 - 9*b**3*c**2*d))/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + d**3*\log(a + b*x)/b**4$

$$3.1268 \quad \int \frac{(c+dx)^3}{(a+bx)^5} dx$$

Optimal. Leaf size=28

$$-\frac{(c+dx)^4}{4(a+bx)^4(bc-ad)}$$

[Out] $-1/4*(d*x+c)^4/(-a*d+b*c)/(b*x+a)^4$

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$-\frac{(c+dx)^4}{4(a+bx)^4(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + b*x)^5, x]

[Out] $-(c + d*x)^4/(4*(b*c - a*d)*(a + b*x)^4)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(c+dx)^3}{(a+bx)^5} dx = -\frac{(c+dx)^4}{4(bc-ad)(a+bx)^4}$$

Mathematica [B] time = 0.03, size = 91, normalized size = 3.25

$$-\frac{a^3d^3 + a^2bd^2(c + 4dx) + ab^2d(c^2 + 4cdx + 6d^2x^2) + b^3(c^3 + 4c^2dx + 6cd^2x^2 + 4d^3x^3)}{4b^4(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + b*x)^5, x]

[Out] $-1/4*(a^3*d^3 + a^2*b*d^2*(c + 4*d*x) + a*b^2*d*(c^2 + 4*c*d*x + 6*d^2*x^2) + b^3*(c^3 + 4*c^2*d*x + 6*c*d^2*x^2 + 4*d^3*x^3))/(b^4*(a + b*x)^4)$

fricas [B] time = 0.45, size = 143, normalized size = 5.11

$$\frac{4b^3d^3x^3 + b^3c^3 + ab^2c^2d + a^2bcd^2 + a^3d^3 + 6(b^3cd^2 + ab^2d^3)x^2 + 4(b^3c^2d + ab^2cd^2 + a^2bd^3)x}{4(b^8x^4 + 4ab^7x^3 + 6a^2b^6x^2 + 4a^3b^5x + a^4b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^5,x, algorithm="fricas")

[Out] $-1/4*(4*b^3*d^3*x^3 + b^3*c^3 + a*b^2*c^2*d + a^2*b*c*d^2 + a^3*d^3 + 6*(b^3*c*d^2 + a*b^2*d^3)*x^2 + 4*(b^3*c^2*d + a*b^2*c*d^2 + a^2*b*d^3)*x)/(b^8*x^4 + 4*a*b^7*x^3 + 6*a^2*b^6*x^2 + 4*a^3*b^5*x + a^4*b^4)$

giac [B] time = 0.97, size = 159, normalized size = 5.68

$$\frac{\frac{b^2c^3}{(bx+a)^4} + \frac{4bc^2d}{(bx+a)^3} - \frac{3abc^2d}{(bx+a)^4} + \frac{6cd^2}{(bx+a)^2} - \frac{8acd^2}{(bx+a)^3} + \frac{3a^2cd^2}{(bx+a)^4} + \frac{4d^3}{(bx+a)b} - \frac{6ad^3}{(bx+a)^2b} + \frac{4a^2d^3}{(bx+a)^3b} - \frac{a^3d^3}{(bx+a)^4b}}{4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^5,x, algorithm="giac")

[Out] $-1/4*(b^2*c^3/(b*x + a)^4 + 4*b*c^2*d/(b*x + a)^3 - 3*a*b*c^2*d/(b*x + a)^4 + 6*c*d^2/(b*x + a)^2 - 8*a*c*d^2/(b*x + a)^3 + 3*a^2*c*d^2/(b*x + a)^4 + 4*d^3/((b*x + a)*b) - 6*a*d^3/((b*x + a)^2*b) + 4*a^2*d^3/((b*x + a)^3*b) - a^3*d^3/((b*x + a)^4*b))/b^3$

maple [B] time = 0.01, size = 122, normalized size = 4.36

$$-\frac{d^3}{(bx+a)b^4} + \frac{3(ad-bc)d^2}{2(bx+a)^2b^4} - \frac{(a^2d^2-2abcd+b^2c^2)d}{(bx+a)^3b^4} - \frac{-a^3d^3+3a^2bcd^2-3ab^2c^2d+b^3c^3}{4(bx+a)^4b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(b*x+a)^5,x)

[Out] $-d*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^4/(b*x+a)^3+3/2*d^2*(a*d-b*c)/b^4/(b*x+a)^2-1/4*(-a^3*d^3+3*a^2*b*c*d^2-3*a*b^2*c^2*d+b^3*c^3)/b^4/(b*x+a)^4-d^3/b^4/(b*x+a)$

maxima [B] time = 1.39, size = 143, normalized size = 5.11

$$\frac{4b^3d^3x^3 + b^3c^3 + ab^2c^2d + a^2bcd^2 + a^3d^3 + 6(b^3cd^2 + ab^2d^3)x^2 + 4(b^3c^2d + ab^2cd^2 + a^2bd^3)x}{4(b^8x^4 + 4ab^7x^3 + 6a^2b^6x^2 + 4a^3b^5x + a^4b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^5,x, algorithm="maxima")

[Out]
$$-1/4*(4*b^3*d^3*x^3 + b^3*c^3 + a*b^2*c^2*d + a^2*b*c*d^2 + a^3*d^3 + 6*(b^3*c*d^2 + a*b^2*d^3)*x^2 + 4*(b^3*c^2*d + a*b^2*c*d^2 + a^2*b*d^3)*x)/(b^8*x^4 + 4*a*b^7*x^3 + 6*a^2*b^6*x^2 + 4*a^3*b^5*x + a^4*b^4)$$

mupad [B] time = 0.07, size = 135, normalized size = 4.82

$$\frac{\frac{a^3 d^3 + a^2 b c d^2 + a b^2 c^2 d + b^3 c^3}{4 b^4} + \frac{d^3 x^3}{b} + \frac{d x (a^2 d^2 + a b c d + b^2 c^2)}{b^3} + \frac{3 d^2 x^2 (a d + b c)}{2 b^2}}{a^4 + 4 a^3 b x + 6 a^2 b^2 x^2 + 4 a b^3 x^3 + b^4 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + b*x)^5,x)

[Out]
$$-((a^3*d^3 + b^3*c^3 + a*b^2*c^2*d + a^2*b*c*d^2)/(4*b^4) + (d^3*x^3)/b + (d*x*(a^2*d^2 + b^2*c^2 + a*b*c*d))/b^3 + (3*d^2*x^2*(a*d + b*c))/(2*b^2))/(a^4 + b^4*x^4 + 4*a*b^3*x^3 + 6*a^2*b^2*x^2 + 4*a^3*b*x)$$

sympy [B] time = 1.50, size = 155, normalized size = 5.54

$$\frac{-a^3 d^3 - a^2 b c d^2 - a b^2 c^2 d - b^3 c^3 - 4 b^3 d^3 x^3 + x^2 (-6 a b^2 d^3 - 6 b^3 c d^2) + x (-4 a^2 b d^3 - 4 a b^2 c d^2 - 4 b^3 c^2 d)}{4 a^4 b^4 + 16 a^3 b^5 x + 24 a^2 b^6 x^2 + 16 a b^7 x^3 + 4 b^8 x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3/(b*x+a)**5,x)

[Out]
$$(-a**3*d**3 - a**2*b*c*d**2 - a*b**2*c**2*d - b**3*c**3 - 4*b**3*d**3*x**3 + x**2*(-6*a*b**2*d**3 - 6*b**3*c*d**2) + x*(-4*a**2*b*d**3 - 4*a*b**2*c*d**2 - 4*b**3*c**2*d))/(4*a**4*b**4 + 16*a**3*b**5*x + 24*a**2*b**6*x**2 + 16*a*b**7*x**3 + 4*b**8*x**4)$$

$$3.1269 \quad \int \frac{(c+dx)^3}{(a+bx)^6} dx$$

Optimal. Leaf size=58

$$\frac{d(c+dx)^4}{20(a+bx)^4(bc-ad)^2} - \frac{(c+dx)^4}{5(a+bx)^5(bc-ad)}$$

[Out] $-1/5*(d*x+c)^4/(-a*d+b*c)/(b*x+a)^5+1/20*d*(d*x+c)^4/(-a*d+b*c)^2/(b*x+a)^4$

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{d(c+dx)^4}{20(a+bx)^4(bc-ad)^2} - \frac{(c+dx)^4}{5(a+bx)^5(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + b*x)^6, x]

[Out] $-(c + d*x)^4/(5*(b*c - a*d)*(a + b*x)^5) + (d*(c + d*x)^4)/(20*(b*c - a*d)^2*(a + b*x)^4)$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{(c+dx)^3}{(a+bx)^6} dx = -\frac{(c+dx)^4}{5(bc-ad)(a+bx)^5} - \frac{d \int \frac{(c+dx)^3}{(a+bx)^5} dx}{5(bc-ad)}$$

$$= -\frac{(c+dx)^4}{5(bc-ad)(a+bx)^5} + \frac{d(c+dx)^4}{20(bc-ad)^2(a+bx)^4}$$

Mathematica [A] time = 0.03, size = 97, normalized size = 1.67

$$\frac{a^3 d^3 + a^2 b d^2 (2c + 5dx) + ab^2 d (3c^2 + 10cdx + 10d^2 x^2) + b^3 (4c^3 + 15c^2 dx + 20cd^2 x^2 + 10d^3 x^3)}{20b^4 (a + bx)^5}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + b*x)^6, x]

[Out] -1/20*(a^3*d^3 + a^2*b*d^2*(2*c + 5*d*x) + a*b^2*d*(3*c^2 + 10*c*d*x + 10*d^2*x^2) + b^3*(4*c^3 + 15*c^2*d*x + 20*c*d^2*x^2 + 10*d^3*x^3))/(b^4*(a + b*x)^5)

fricas [B] time = 0.44, size = 160, normalized size = 2.76

$$\frac{10 b^3 d^3 x^3 + 4 b^3 c^3 + 3 a b^2 c^2 d + 2 a^2 b c d^2 + a^3 d^3 + 10 (2 b^3 c d^2 + a b^2 d^3) x^2 + 5 (3 b^3 c^2 d + 2 a b^2 c d^2 + a^2 b d^3) x}{20 (b^9 x^5 + 5 a b^8 x^4 + 10 a^2 b^7 x^3 + 10 a^3 b^6 x^2 + 5 a^4 b^5 x + a^5 b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^6,x, algorithm="fricas")

[Out] -1/20*(10*b^3*d^3*x^3 + 4*b^3*c^3 + 3*a*b^2*c^2*d + 2*a^2*b*c*d^2 + a^3*d^3 + 10*(2*b^3*c*d^2 + a*b^2*d^3)*x^2 + 5*(3*b^3*c^2*d + 2*a*b^2*c*d^2 + a^2*b*d^3)*x)/(b^9*x^5 + 5*a*b^8*x^4 + 10*a^2*b^7*x^3 + 10*a^3*b^6*x^2 + 5*a^4*b^5*x + a^5*b^4)

giac [B] time = 1.00, size = 114, normalized size = 1.97

$$\frac{10 b^3 d^3 x^3 + 20 b^3 c d^2 x^2 + 10 a b^2 d^3 x^2 + 15 b^3 c^2 d x + 10 a b^2 c d^2 x + 5 a^2 b d^3 x + 4 b^3 c^3 + 3 a b^2 c^2 d + 2 a^2 b c d^2 + a^3 d^3}{20 (b x + a)^5 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^6,x, algorithm="giac")

[Out] $-1/20*(10*b^3*d^3*x^3 + 20*b^3*c*d^2*x^2 + 10*a*b^2*d^3*x^2 + 15*b^3*c^2*d*x + 10*a*b^2*c*d^2*x + 5*a^2*b*d^3*x + 4*b^3*c^3 + 3*a*b^2*c^2*d + 2*a^2*b*c*d^2 + a^3*d^3)/((b*x + a)^5*b^4)$

maple [B] time = 0.01, size = 121, normalized size = 2.09

$$-\frac{d^3}{2(bx+a)^2b^4} + \frac{(ad-bc)d^2}{(bx+a)^3b^4} - \frac{3(a^2d^2-2abcd+b^2c^2)d}{4(bx+a)^4b^4} - \frac{-a^3d^3+3a^2bcd^2-3ab^2c^2d+b^3c^3}{5(bx+a)^5b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^3/(b*x+a)^6,x)`

[Out] $d^2*(a*d-b*c)/b^4/(b*x+a)^3-1/5*(-a^3*d^3+3*a^2*b*c*d^2-3*a*b^2*c^2*d+b^3*c^3)/b^4/(b*x+a)^5-1/2*d^3/b^4/(b*x+a)^2-3/4*d*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^4/(b*x+a)^4$

maxima [B] time = 1.47, size = 160, normalized size = 2.76

$$\frac{10b^3d^3x^3 + 4b^3c^3 + 3ab^2c^2d + 2a^2bcd^2 + a^3d^3 + 10(2b^3cd^2 + ab^2d^3)x^2 + 5(3b^3c^2d + 2ab^2cd^2 + a^2bd^3)x}{20(b^9x^5 + 5ab^8x^4 + 10a^2b^7x^3 + 10a^3b^6x^2 + 5a^4b^5x + a^5b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^3/(b*x+a)^6,x, algorithm="maxima")`

[Out] $-1/20*(10*b^3*d^3*x^3 + 4*b^3*c^3 + 3*a*b^2*c^2*d + 2*a^2*b*c*d^2 + a^3*d^3 + 10*(2*b^3*c*d^2 + a*b^2*d^3)*x^2 + 5*(3*b^3*c^2*d + 2*a*b^2*c*d^2 + a^2*b*d^3)*x)/(b^9*x^5 + 5*a*b^8*x^4 + 10*a^2*b^7*x^3 + 10*a^3*b^6*x^2 + 5*a^4*b^5*x + a^5*b^4)$

mupad [B] time = 0.08, size = 39, normalized size = 0.67

$$\frac{(c+dx)^4(5ad-4bc+bdx)}{20(ad-bc)^2(a+bx)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c+d*x)^3/(a+b*x)^6,x)`

[Out] $((c+d*x)^4*(5*a*d-4*b*c+b*d*x))/(20*(a*d-b*c)^2*(a+b*x)^5)$

sympy [B] time = 1.96, size = 172, normalized size = 2.97

$$\frac{-a^3d^3 - 2a^2bcd^2 - 3ab^2c^2d - 4b^3c^3 - 10b^3d^3x^3 + x^2(-10ab^2d^3 - 20b^3cd^2) + x(-5a^2bd^3 - 10ab^2cd^2 - 15b^3c^2d)}{20a^5b^4 + 100a^4b^5x + 200a^3b^6x^2 + 200a^2b^7x^3 + 100ab^8x^4 + 20b^9x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**3/(b*x+a)**6,x)
```

```
[Out] (-a**3*d**3 - 2*a**2*b*c*d**2 - 3*a*b**2*c**2*d - 4*b**3*c**3 - 10*b**3*d**  
3*x**3 + x**2*(-10*a*b**2*d**3 - 20*b**3*c*d**2) + x*(-5*a**2*b*d**3 - 10*a  
*b**2*c*d**2 - 15*b**3*c**2*d))/(20*a**5*b**4 + 100*a**4*b**5*x + 200*a**3*  
b**6*x**2 + 200*a**2*b**7*x**3 + 100*a*b**8*x**4 + 20*b**9*x**5)
```

$$3.1270 \quad \int \frac{(c+dx)^3}{(a+bx)^7} dx$$

Optimal. Leaf size=92

$$-\frac{3d^2(bc-ad)}{4b^4(a+bx)^4} - \frac{3d(bc-ad)^2}{5b^4(a+bx)^5} - \frac{(bc-ad)^3}{6b^4(a+bx)^6} - \frac{d^3}{3b^4(a+bx)^3}$$

[Out] $-1/6*(-a*d+b*c)^3/b^4/(b*x+a)^6-3/5*d*(-a*d+b*c)^2/b^4/(b*x+a)^5-3/4*d^2*(-a*d+b*c)/b^4/(b*x+a)^4-1/3*d^3/b^4/(b*x+a)^3$

Rubi [A] time = 0.05, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{3d^2(bc-ad)}{4b^4(a+bx)^4} - \frac{3d(bc-ad)^2}{5b^4(a+bx)^5} - \frac{(bc-ad)^3}{6b^4(a+bx)^6} - \frac{d^3}{3b^4(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + b*x)^7, x]

[Out] $-(b*c - a*d)^3/(6*b^4*(a + b*x)^6) - (3*d*(b*c - a*d)^2)/(5*b^4*(a + b*x)^5) - (3*d^2*(b*c - a*d))/(4*b^4*(a + b*x)^4) - d^3/(3*b^4*(a + b*x)^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^3}{(a+bx)^7} dx &= \int \left(\frac{(bc-ad)^3}{b^3(a+bx)^7} + \frac{3d(bc-ad)^2}{b^3(a+bx)^6} + \frac{3d^2(bc-ad)}{b^3(a+bx)^5} + \frac{d^3}{b^3(a+bx)^4} \right) dx \\ &= -\frac{(bc-ad)^3}{6b^4(a+bx)^6} - \frac{3d(bc-ad)^2}{5b^4(a+bx)^5} - \frac{3d^2(bc-ad)}{4b^4(a+bx)^4} - \frac{d^3}{3b^4(a+bx)^3} \end{aligned}$$

Mathematica [A] time = 0.03, size = 97, normalized size = 1.05

$$\frac{a^3d^3 + 3a^2bd^2(c + 2dx) + 3ab^2d(2c^2 + 6cdx + 5d^2x^2) + b^3(10c^3 + 36c^2dx + 45cd^2x^2 + 20d^3x^3)}{60b^4(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + b*x)^7,x]

[Out]
$$-1/60*(a^3*d^3 + 3*a^2*b*d^2*(c + 2*d*x) + 3*a*b^2*d*(2*c^2 + 6*c*d*x + 5*d^2*x^2) + b^3*(10*c^3 + 36*c^2*d*x + 45*c*d^2*x^2 + 20*d^3*x^3))/(b^4*(a + b*x)^6)$$

fricas [B] time = 0.44, size = 171, normalized size = 1.86

$$\frac{20 b^3 d^3 x^3 + 10 b^3 c^3 + 6 a b^2 c^2 d + 3 a^2 b c d^2 + a^3 d^3 + 15 (3 b^3 c d^2 + a b^2 d^3) x^2 + 6 (6 b^3 c^2 d + 3 a b^2 c d^2 + a^2 b d^3) x}{60 (b^{10} x^6 + 6 a b^9 x^5 + 15 a^2 b^8 x^4 + 20 a^3 b^7 x^3 + 15 a^4 b^6 x^2 + 6 a^5 b^5 x + a^6 b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^7,x, algorithm="fricas")

[Out]
$$-1/60*(20*b^3*d^3*x^3 + 10*b^3*c^3 + 6*a*b^2*c^2*d + 3*a^2*b*c*d^2 + a^3*d^3 + 15*(3*b^3*c*d^2 + a*b^2*d^3)*x^2 + 6*(6*b^3*c^2*d + 3*a*b^2*c*d^2 + a^2*b*d^3)*x)/(b^10*x^6 + 6*a*b^9*x^5 + 15*a^2*b^8*x^4 + 20*a^3*b^7*x^3 + 15*a^4*b^6*x^2 + 6*a^5*b^5*x + a^6*b^4)$$

giac [A] time = 0.98, size = 114, normalized size = 1.24

$$\frac{20 b^3 d^3 x^3 + 45 b^3 c d^2 x^2 + 15 a b^2 d^3 x^2 + 36 b^3 c^2 d x + 18 a b^2 c d^2 x + 6 a^2 b d^3 x + 10 b^3 c^3 + 6 a b^2 c^2 d + 3 a^2 b c d^2 + a^3 d^3}{60 (b x + a)^6 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^7,x, algorithm="giac")

[Out]
$$-1/60*(20*b^3*d^3*x^3 + 45*b^3*c*d^2*x^2 + 15*a*b^2*d^3*x^2 + 36*b^3*c^2*d*x + 18*a*b^2*c*d^2*x + 6*a^2*b*d^3*x + 10*b^3*c^3 + 6*a*b^2*c^2*d + 3*a^2*b*c*d^2 + a^3*d^3)/((b*x + a)^6*b^4)$$

maple [A] time = 0.01, size = 122, normalized size = 1.33

$$-\frac{d^3}{3(bx+a)^3 b^4} + \frac{3(ad-bc)d^2}{4(bx+a)^4 b^4} - \frac{3(a^2d^2-2abcd+b^2c^2)d}{5(bx+a)^5 b^4} - \frac{-a^3d^3+3a^2bcd^2-3ab^2c^2d+b^3c^3}{6(bx+a)^6 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(b*x+a)^7,x)

[Out]
$$-1/3*d^3/b^4/(b*x+a)^3-3/5*d*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^4/(b*x+a)^5+3/4*d^2*(a*d-b*c)/b^4/(b*x+a)^4-1/6*(-a^3*d^3+3*a^2*b*c*d^2-3*a*b^2*c^2*d+b^3*c^3)/b^4/(b*x+a)^6$$

maxima [B] time = 1.44, size = 171, normalized size = 1.86

$$\frac{20b^3d^3x^3 + 10b^3c^3 + 6ab^2c^2d + 3a^2bcd^2 + a^3d^3 + 15(3b^3cd^2 + ab^2d^3)x^2 + 6(6b^3c^2d + 3ab^2cd^2 + a^2bd^3)x}{60(b^{10}x^6 + 6ab^9x^5 + 15a^2b^8x^4 + 20a^3b^7x^3 + 15a^4b^6x^2 + 6a^5b^5x + a^6b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^7,x, algorithm="maxima")

[Out]
$$-1/60*(20*b^3*d^3*x^3 + 10*b^3*c^3 + 6*a*b^2*c^2*d + 3*a^2*b*c*d^2 + a^3*d^3 + 15*(3*b^3*c*d^2 + a*b^2*d^3)*x^2 + 6*(6*b^3*c^2*d + 3*a*b^2*c*d^2 + a^2*b*d^3)*x)/(b^{10}*x^6 + 6*a*b^9*x^5 + 15*a^2*b^8*x^4 + 20*a^3*b^7*x^3 + 15*a^4*b^6*x^2 + 6*a^5*b^5*x + a^6*b^4)$$

mpad [B] time = 0.22, size = 165, normalized size = 1.79

$$-\frac{\frac{a^3d^3+3a^2bcd^2+6ab^2c^2d+10b^3c^3}{60b^4} + \frac{d^3x^3}{3b} + \frac{dx(a^2d^2+3abcd+6b^2c^2)}{10b^3} + \frac{d^2x^2(ad+3bc)}{4b^2}}{a^6 + 6a^5bx + 15a^4b^2x^2 + 20a^3b^3x^3 + 15a^2b^4x^4 + 6ab^5x^5 + b^6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + b*x)^7,x)

[Out]
$$-((a^3*d^3 + 10*b^3*c^3 + 6*a*b^2*c^2*d + 3*a^2*b*c*d^2)/(60*b^4) + (d^3*x^3)/(3*b) + (d*x*(a^2*d^2 + 6*b^2*c^2 + 3*a*b*c*d))/(10*b^3) + (d^2*x^2*(a*d + 3*b*c))/(4*b^2))/(a^6 + b^6*x^6 + 6*a*b^5*x^5 + 15*a^4*b^2*x^2 + 20*a^3*b^3*x^3 + 15*a^2*b^4*x^4 + 6*a^5*b*x)$$

sympy [B] time = 2.54, size = 184, normalized size = 2.00

$$\frac{-a^3d^3 - 3a^2bcd^2 - 6ab^2c^2d - 10b^3c^3 - 20b^3d^3x^3 + x^2(-15ab^2d^3 - 45b^3cd^2) + x(-6a^2bd^3 - 18ab^2cd^2 - 36b^3c^2d)}{60a^6b^4 + 360a^5b^5x + 900a^4b^6x^2 + 1200a^3b^7x^3 + 900a^2b^8x^4 + 360ab^9x^5 + 60b^{10}x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3/(b*x+a)**7,x)

[Out]
$$(-a**3*d**3 - 3*a**2*b*c*d**2 - 6*a*b**2*c**2*d - 10*b**3*c**3 - 20*b**3*d**3*x**3 + x**2*(-15*a*b**2*d**3 - 45*b**3*c*d**2) + x*(-6*a**2*b*d**3 - 18*a*b**2*c*d**2 - 36*b**3*c**2*d))/(60*a**6*b**4 + 360*a**5*b**5*x + 900*a**4*b**6*x**2 + 1200*a**3*b**7*x**3 + 900*a**2*b**8*x**4 + 360*a*b**9*x**5 + 60*b**10*x**6)$$

$$3.1271 \quad \int \frac{(c+dx)^3}{(a+bx)^8} dx$$

Optimal. Leaf size=92

$$-\frac{3d^2(bc-ad)}{5b^4(a+bx)^5} - \frac{d(bc-ad)^2}{2b^4(a+bx)^6} - \frac{(bc-ad)^3}{7b^4(a+bx)^7} - \frac{d^3}{4b^4(a+bx)^4}$$

[Out] $-1/7*(-a*d+b*c)^3/b^4/(b*x+a)^7-1/2*d*(-a*d+b*c)^2/b^4/(b*x+a)^6-3/5*d^2*(-a*d+b*c)/b^4/(b*x+a)^5-1/4*d^3/b^4/(b*x+a)^4$

Rubi [A] time = 0.05, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{3d^2(bc-ad)}{5b^4(a+bx)^5} - \frac{d(bc-ad)^2}{2b^4(a+bx)^6} - \frac{(bc-ad)^3}{7b^4(a+bx)^7} - \frac{d^3}{4b^4(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + b*x)^8, x]

[Out] $-(b*c - a*d)^3/(7*b^4*(a + b*x)^7) - (d*(b*c - a*d)^2)/(2*b^4*(a + b*x)^6) - (3*d^2*(b*c - a*d))/(5*b^4*(a + b*x)^5) - d^3/(4*b^4*(a + b*x)^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^3}{(a+bx)^8} dx &= \int \left(\frac{(bc-ad)^3}{b^3(a+bx)^8} + \frac{3d(bc-ad)^2}{b^3(a+bx)^7} + \frac{3d^2(bc-ad)}{b^3(a+bx)^6} + \frac{d^3}{b^3(a+bx)^5} \right) dx \\ &= -\frac{(bc-ad)^3}{7b^4(a+bx)^7} - \frac{d(bc-ad)^2}{2b^4(a+bx)^6} - \frac{3d^2(bc-ad)}{5b^4(a+bx)^5} - \frac{d^3}{4b^4(a+bx)^4} \end{aligned}$$

Mathematica [A] time = 0.03, size = 97, normalized size = 1.05

$$\frac{a^3d^3 + a^2bd^2(4c + 7dx) + ab^2d(10c^2 + 28cdx + 21d^2x^2) + b^3(20c^3 + 70c^2dx + 84cd^2x^2 + 35d^3x^3)}{140b^4(a+bx)^7}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + b*x)^8,x]

[Out]
$$-1/140*(a^3*d^3 + a^2*b*d^2*(4*c + 7*d*x) + a*b^2*d*(10*c^2 + 28*c*d*x + 21*d^2*x^2) + b^3*(20*c^3 + 70*c^2*d*x + 84*c*d^2*x^2 + 35*d^3*x^3))/(b^4*(a + b*x)^7)$$

fricas [B] time = 0.43, size = 182, normalized size = 1.98

$$\frac{35 b^3 d^3 x^3 + 20 b^3 c^3 + 10 a b^2 c^2 d + 4 a^2 b c d^2 + a^3 d^3 + 21 (4 b^3 c d^2 + a b^2 d^3) x^2 + 7 (10 b^3 c^2 d + 4 a b^2 c d^2 + a^2 b d^3) x}{140 (b^{11} x^7 + 7 a b^{10} x^6 + 21 a^2 b^9 x^5 + 35 a^3 b^8 x^4 + 35 a^4 b^7 x^3 + 21 a^5 b^6 x^2 + 7 a^6 b^5 x + a^7 b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^8,x, algorithm="fricas")

[Out]
$$-1/140*(35*b^3*d^3*x^3 + 20*b^3*c^3 + 10*a*b^2*c^2*d + 4*a^2*b*c*d^2 + a^3*d^3 + 21*(4*b^3*c*d^2 + a*b^2*d^3)*x^2 + 7*(10*b^3*c^2*d + 4*a*b^2*c*d^2 + a^2*b*d^3)*x)/(b^{11}*x^7 + 7*a*b^{10}*x^6 + 21*a^2*b^9*x^5 + 35*a^3*b^8*x^4 + 35*a^4*b^7*x^3 + 21*a^5*b^6*x^2 + 7*a^6*b^5*x + a^7*b^4)$$

giac [A] time = 0.95, size = 114, normalized size = 1.24

$$\frac{35 b^3 d^3 x^3 + 84 b^3 c d^2 x^2 + 21 a b^2 d^3 x^2 + 70 b^3 c^2 d x + 28 a b^2 c d^2 x + 7 a^2 b d^3 x + 20 b^3 c^3 + 10 a b^2 c^2 d + 4 a^2 b c d^2 + a^3 d^3}{140 (b x + a)^7 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^8,x, algorithm="giac")

[Out]
$$-1/140*(35*b^3*d^3*x^3 + 84*b^3*c*d^2*x^2 + 21*a*b^2*d^3*x^2 + 70*b^3*c^2*d*x + 28*a*b^2*c*d^2*x + 7*a^2*b*d^3*x + 20*b^3*c^3 + 10*a*b^2*c^2*d + 4*a^2*b*c*d^2 + a^3*d^3)/((b*x + a)^7*b^4)$$

maple [A] time = 0.01, size = 122, normalized size = 1.33

$$-\frac{d^3}{4 (b x + a)^4 b^4} + \frac{3 (a d - b c) d^2}{5 (b x + a)^5 b^4} - \frac{(a^2 d^2 - 2 a b c d + b^2 c^2) d}{2 (b x + a)^6 b^4} - \frac{-a^3 d^3 + 3 a^2 b c d^2 - 3 a b^2 c^2 d + b^3 c^3}{7 (b x + a)^7 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(b*x+a)^8,x)

[Out]
$$-1/7*(-a^3*d^3+3*a^2*b*c*d^2-3*a*b^2*c^2*d+b^3*c^3)/b^4/(b*x+a)^7+3/5*d^2*(a*d-b*c)/b^4/(b*x+a)^5-1/4*d^3/b^4/(b*x+a)^4-1/2*d*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^4/(b*x+a)^6$$

maxima [B] time = 1.45, size = 182, normalized size = 1.98

$$\frac{35b^3d^3x^3 + 20b^3c^3 + 10ab^2c^2d + 4a^2bcd^2 + a^3d^3 + 21(4b^3cd^2 + ab^2d^3)x^2 + 7(10b^3c^2d + 4ab^2cd^2 + a^2bd^3)}{140(b^{11}x^7 + 7ab^{10}x^6 + 21a^2b^9x^5 + 35a^3b^8x^4 + 35a^4b^7x^3 + 21a^5b^6x^2 + 7a^6b^5x + a^7b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^8,x, algorithm="maxima")

[Out] $-1/140*(35*b^3*d^3*x^3 + 20*b^3*c^3 + 10*a*b^2*c^2*d + 4*a^2*b*c*d^2 + a^3*d^3 + 21*(4*b^3*c*d^2 + a*b^2*d^3)*x^2 + 7*(10*b^3*c^2*d + 4*a*b^2*c*d^2 + a^2*b*d^3)*x)/(b^{11}*x^7 + 7*a*b^{10}*x^6 + 21*a^2*b^9*x^5 + 35*a^3*b^8*x^4 + 35*a^4*b^7*x^3 + 21*a^5*b^6*x^2 + 7*a^6*b^5*x + a^7*b^4)$

mupad [B] time = 0.11, size = 176, normalized size = 1.91

$$-\frac{\frac{a^3d^3+4a^2bcd^2+10ab^2c^2d+20b^3c^3}{140b^4} + \frac{d^3x^3}{4b} + \frac{dx(a^2d^2+4abcd+10b^2c^2)}{20b^3} + \frac{3d^2x^2(ad+4bc)}{20b^2}}{a^7 + 7a^6bx + 21a^5b^2x^2 + 35a^4b^3x^3 + 35a^3b^4x^4 + 21a^2b^5x^5 + 7ab^6x^6 + b^7x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + b*x)^8,x)

[Out] $-((a^3*d^3 + 20*b^3*c^3 + 10*a*b^2*c^2*d + 4*a^2*b*c*d^2)/(140*b^4) + (d^3*x^3)/(4*b) + (d*x*(a^2*d^2 + 10*b^2*c^2 + 4*a*b*c*d))/(20*b^3) + (3*d^2*x^2*(a*d + 4*b*c))/(20*b^2))/(a^7 + b^7*x^7 + 7*a*b^6*x^6 + 21*a^5*b^2*x^2 + 35*a^4*b^3*x^3 + 35*a^3*b^4*x^4 + 21*a^2*b^5*x^5 + 7*a^6*b*x)$

sympy [B] time = 3.12, size = 196, normalized size = 2.13

$$\frac{-a^3d^3 - 4a^2bcd^2 - 10ab^2c^2d - 20b^3c^3 - 35b^3d^3x^3 + x^2(-21ab^2d^3 - 84b^3cd^2) + x(-7a^2bd^3 - 28ab^2cd^2 - 70b^3c^2)}{140a^7b^4 + 980a^6b^5x + 2940a^5b^6x^2 + 4900a^4b^7x^3 + 4900a^3b^8x^4 + 2940a^2b^9x^5 + 980ab^{10}x^6 + 140b^{11}x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3/(b*x+a)**8,x)

[Out] $(-a**3*d**3 - 4*a**2*b*c*d**2 - 10*a*b**2*c**2*d - 20*b**3*c**3 - 35*b**3*d**3*x**3 + x**2*(-21*a*b**2*d**3 - 84*b**3*c*d**2) + x*(-7*a**2*b*d**3 - 28*a*b**2*c*d**2 - 70*b**3*c**2*d))/(140*a**7*b**4 + 980*a**6*b**5*x + 2940*a**5*b**6*x**2 + 4900*a**4*b**7*x**3 + 4900*a**3*b**8*x**4 + 2940*a**2*b**9*x**5 + 980*a*b**10*x**6 + 140*b**11*x**7)$

$$3.1272 \quad \int \frac{(c+dx)^3}{(a+bx)^9} dx$$

Optimal. Leaf size=92

$$-\frac{d^2(bc-ad)}{2b^4(a+bx)^6} - \frac{3d(bc-ad)^2}{7b^4(a+bx)^7} - \frac{(bc-ad)^3}{8b^4(a+bx)^8} - \frac{d^3}{5b^4(a+bx)^5}$$

[Out] $-1/8*(-a*d+b*c)^3/b^4/(b*x+a)^8-3/7*d*(-a*d+b*c)^2/b^4/(b*x+a)^7-1/2*d^2*(-a*d+b*c)/b^4/(b*x+a)^6-1/5*d^3/b^4/(b*x+a)^5$

Rubi [A] time = 0.05, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{d^2(bc-ad)}{2b^4(a+bx)^6} - \frac{3d(bc-ad)^2}{7b^4(a+bx)^7} - \frac{(bc-ad)^3}{8b^4(a+bx)^8} - \frac{d^3}{5b^4(a+bx)^5}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + b*x)^9, x]

[Out] $-(b*c - a*d)^3/(8*b^4*(a + b*x)^8) - (3*d*(b*c - a*d)^2)/(7*b^4*(a + b*x)^7) - (d^2*(b*c - a*d))/(2*b^4*(a + b*x)^6) - d^3/(5*b^4*(a + b*x)^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^3}{(a+bx)^9} dx &= \int \left(\frac{(bc-ad)^3}{b^3(a+bx)^9} + \frac{3d(bc-ad)^2}{b^3(a+bx)^8} + \frac{3d^2(bc-ad)}{b^3(a+bx)^7} + \frac{d^3}{b^3(a+bx)^6} \right) dx \\ &= -\frac{(bc-ad)^3}{8b^4(a+bx)^8} - \frac{3d(bc-ad)^2}{7b^4(a+bx)^7} - \frac{d^2(bc-ad)}{2b^4(a+bx)^6} - \frac{d^3}{5b^4(a+bx)^5} \end{aligned}$$

Mathematica [A] time = 0.04, size = 97, normalized size = 1.05

$$\frac{a^3d^3 + a^2bd^2(5c + 8dx) + ab^2d(15c^2 + 40cdx + 28d^2x^2) + b^3(35c^3 + 120c^2dx + 140cd^2x^2 + 56d^3x^3)}{280b^4(a+bx)^8}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + b*x)^9, x]

[Out]
$$-1/280*(a^3*d^3 + a^2*b*d^2*(5*c + 8*d*x) + a*b^2*d*(15*c^2 + 40*c*d*x + 28*d^2*x^2) + b^3*(35*c^3 + 120*c^2*d*x + 140*c*d^2*x^2 + 56*d^3*x^3))/(b^4*(a + b*x)^8)$$

fricas [B] time = 0.43, size = 193, normalized size = 2.10

$$\frac{56 b^3 d^3 x^3 + 35 b^3 c^3 + 15 a b^2 c^2 d + 5 a^2 b c d^2 + a^3 d^3 + 28 (5 b^3 c d^2 + a b^2 d^3) x^2 + 8 (15 b^3 c^2 d + 5 a b^2 c d^2 + a^2 b d^3)}{280 (b^{12} x^8 + 8 a b^{11} x^7 + 28 a^2 b^{10} x^6 + 56 a^3 b^9 x^5 + 70 a^4 b^8 x^4 + 56 a^5 b^7 x^3 + 28 a^6 b^6 x^2 + 8 a^7 b^5 x + a^8 b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^9, x, algorithm="fricas")

[Out]
$$-1/280*(56*b^3*d^3*x^3 + 35*b^3*c^3 + 15*a*b^2*c^2*d + 5*a^2*b*c*d^2 + a^3*d^3 + 28*(5*b^3*c*d^2 + a*b^2*d^3)*x^2 + 8*(15*b^3*c^2*d + 5*a*b^2*c*d^2 + a^2*b*d^3)*x)/(b^{12}*x^8 + 8*a*b^{11}*x^7 + 28*a^2*b^{10}*x^6 + 56*a^3*b^9*x^5 + 70*a^4*b^8*x^4 + 56*a^5*b^7*x^3 + 28*a^6*b^6*x^2 + 8*a^7*b^5*x + a^8*b^4)$$

giac [A] time = 0.86, size = 114, normalized size = 1.24

$$\frac{56 b^3 d^3 x^3 + 140 b^3 c d^2 x^2 + 28 a b^2 d^3 x^2 + 120 b^3 c^2 d x + 40 a b^2 c d^2 x + 8 a^2 b d^3 x + 35 b^3 c^3 + 15 a b^2 c^2 d + 5 a^2 b c d^2}{280 (b x + a)^8 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^9, x, algorithm="giac")

[Out]
$$-1/280*(56*b^3*d^3*x^3 + 140*b^3*c*d^2*x^2 + 28*a*b^2*d^3*x^2 + 120*b^3*c^2*d*x + 40*a*b^2*c*d^2*x + 8*a^2*b*d^3*x + 35*b^3*c^3 + 15*a*b^2*c^2*d + 5*a^2*b*c*d^2 + a^3*d^3)/((b*x + a)^8*b^4)$$

maple [A] time = 0.01, size = 122, normalized size = 1.33

$$-\frac{d^3}{5(bx+a)^5 b^4} + \frac{(ad-bc)d^2}{2(bx+a)^6 b^4} - \frac{3(a^2d^2-2abcd+b^2c^2)d}{7(bx+a)^7 b^4} - \frac{-a^3d^3+3a^2bcd^2-3ab^2c^2d+b^3c^3}{8(bx+a)^8 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(b*x+a)^9, x)

[Out]
$$-1/8*(-a^3*d^3+3*a^2*b*c*d^2-3*a*b^2*c^2*d+b^3*c^3)/b^4/(b*x+a)^8-3/7*d*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^4/(b*x+a)^7-1/5*d^3/b^4/(b*x+a)^5+1/2*d^2*(a*d-b*c)/b^4/(b*x+a)^6$$

maxima [B] time = 1.52, size = 193, normalized size = 2.10

$$\frac{56 b^3 d^3 x^3 + 35 b^3 c^3 + 15 a b^2 c^2 d + 5 a^2 b c d^2 + a^3 d^3 + 28 (5 b^3 c d^2 + a b^2 d^3) x^2 + 8 (15 b^3 c^2 d + 5 a b^2 c d^2 + a^2 b d^3) x}{280 (b^{12} x^8 + 8 a b^{11} x^7 + 28 a^2 b^{10} x^6 + 56 a^3 b^9 x^5 + 70 a^4 b^8 x^4 + 56 a^5 b^7 x^3 + 28 a^6 b^6 x^2 + 8 a^7 b^5 x + a^8 b^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(b*x+a)^9,x, algorithm="maxima")

[Out] $-1/280*(56*b^3*d^3*x^3 + 35*b^3*c^3 + 15*a*b^2*c^2*d + 5*a^2*b*c*d^2 + a^3*d^3 + 28*(5*b^3*c*d^2 + a*b^2*d^3)*x^2 + 8*(15*b^3*c^2*d + 5*a*b^2*c*d^2 + a^2*b*d^3)*x)/(b^{12}*x^8 + 8*a*b^{11}*x^7 + 28*a^2*b^{10}*x^6 + 56*a^3*b^9*x^5 + 70*a^4*b^8*x^4 + 56*a^5*b^7*x^3 + 28*a^6*b^6*x^2 + 8*a^7*b^5*x + a^8*b^4)$

mupad [B] time = 0.23, size = 187, normalized size = 2.03

$$\frac{\frac{a^3 d^3 + 5 a^2 b c d^2 + 15 a b^2 c^2 d + 35 b^3 c^3}{280 b^4} + \frac{d^3 x^3}{5 b} + \frac{d x (a^2 d^2 + 5 a b c d + 15 b^2 c^2)}{35 b^3} + \frac{d^2 x^2 (a d + 5 b c)}{10 b^2}}{a^8 + 8 a^7 b x + 28 a^6 b^2 x^2 + 56 a^5 b^3 x^3 + 70 a^4 b^4 x^4 + 56 a^3 b^5 x^5 + 28 a^2 b^6 x^6 + 8 a b^7 x^7 + b^8 x^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + b*x)^9,x)

[Out] $-((a^3*d^3 + 35*b^3*c^3 + 15*a*b^2*c^2*d + 5*a^2*b*c*d^2)/(280*b^4) + (d^3*x^3)/(5*b) + (d*x*(a^2*d^2 + 15*b^2*c^2 + 5*a*b*c*d))/(35*b^3) + (d^2*x^2*(a*d + 5*b*c))/(10*b^2))/(a^8 + b^8*x^8 + 8*a*b^7*x^7 + 28*a^6*b^2*x^2 + 56*a^5*b^3*x^3 + 70*a^4*b^4*x^4 + 56*a^3*b^5*x^5 + 28*a^2*b^6*x^6 + 8*a^7*b*x)$

sympy [B] time = 3.95, size = 207, normalized size = 2.25

$$\frac{-a^3 d^3 - 5 a^2 b c d^2 - 15 a b^2 c^2 d - 35 b^3 c^3 - 56 b^3 d^3 x^3 + x^2 (-28 a b^2 d^3 - 140 b^3 c d^2) + x (-8 a^2 b d^3 - 40 a b^2 c d^2 - 120 a^2 b^2 c^2 d)}{280 a^8 b^4 + 2240 a^7 b^5 x + 7840 a^6 b^6 x^2 + 15680 a^5 b^7 x^3 + 19600 a^4 b^8 x^4 + 15680 a^3 b^9 x^5 + 7840 a^2 b^{10} x^6 + 2240 a b^{11} x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3/(b*x+a)**9,x)

[Out] $(-a^{**3}*d^{**3} - 5*a^{**2}*b*c*d^{**2} - 15*a*b^{**2}*c^{**2}*d - 35*b^{**3}*c^{**3} - 56*b^{**3}*d^{**3}*x^{**3} + x^{**2}*(-28*a*b^{**2}*d^{**3} - 140*b^{**3}*c*d^{**2}) + x*(-8*a^{**2}*b*d^{**3} - 40*a*b^{**2}*c*d^{**2} - 120*b^{**3}*c^{**2}*d))/(280*a^{**8}*b^{**4} + 2240*a^{**7}*b^{**5}*x + 7840*a^{**6}*b^{**6}*x^{**2} + 15680*a^{**5}*b^{**7}*x^{**3} + 19600*a^{**4}*b^{**8}*x^{**4} + 15680*a^{**3}*b^{**9}*x^{**5} + 7840*a^{**2}*b^{**10}*x^{**6} + 2240*a*b^{**11}*x^{**7} + 280*b^{**12}*x^{**8})$

3.1273 $\int (a + bx)^9 (c + dx)^7 dx$

Optimal. Leaf size=200

$$\frac{7d^6(a+bx)^{16}(bc-ad)}{16b^8} + \frac{7d^5(a+bx)^{15}(bc-ad)^2}{5b^8} + \frac{5d^4(a+bx)^{14}(bc-ad)^3}{2b^8} + \frac{35d^3(a+bx)^{13}(bc-ad)^4}{13b^8} + \frac{7d^2(a+bx)^{12}(bc-ad)^5}{b^8} + \frac{7d(a+bx)^{11}(bc-ad)^6}{b^8} + \frac{d^7(a+bx)^{17}}{17b^8}$$

[Out] $1/10*(-a*d+b*c)^7*(b*x+a)^{10}/b^8+7/11*d*(-a*d+b*c)^6*(b*x+a)^{11}/b^8+7/4*d^2*(-a*d+b*c)^5*(b*x+a)^{12}/b^8+35/13*d^3*(-a*d+b*c)^4*(b*x+a)^{13}/b^8+5/2*d^4*(-a*d+b*c)^3*(b*x+a)^{14}/b^8+7/5*d^5*(-a*d+b*c)^2*(b*x+a)^{15}/b^8+7/16*d^6*(-a*d+b*c)*(b*x+a)^{16}/b^8+1/17*d^7*(b*x+a)^{17}/b^8$

Rubi [A] time = 0.68, antiderivative size = 200, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{7d^6(a+bx)^{16}(bc-ad)}{16b^8} + \frac{7d^5(a+bx)^{15}(bc-ad)^2}{5b^8} + \frac{5d^4(a+bx)^{14}(bc-ad)^3}{2b^8} + \frac{35d^3(a+bx)^{13}(bc-ad)^4}{13b^8} + \frac{7d^2(a+bx)^{12}(bc-ad)^5}{b^8} + \frac{7d(a+bx)^{11}(bc-ad)^6}{b^8} + \frac{d^7(a+bx)^{17}}{17b^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^9*(c + d*x)^7, x]

[Out] $((b*c - a*d)^7*(a + b*x)^{10})/(10*b^8) + (7*d*(b*c - a*d)^6*(a + b*x)^{11})/(11*b^8) + (7*d^2*(b*c - a*d)^5*(a + b*x)^{12})/(4*b^8) + (35*d^3*(b*c - a*d)^4*(a + b*x)^{13})/(13*b^8) + (5*d^4*(b*c - a*d)^3*(a + b*x)^{14})/(2*b^8) + (7*d^5*(b*c - a*d)^2*(a + b*x)^{15})/(5*b^8) + (7*d^6*(b*c - a*d)*(a + b*x)^{16})/(16*b^8) + (d^7*(a + b*x)^{17})/(17*b^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^9 (c + dx)^7 dx &= \int \left(\frac{(bc - ad)^7 (a + bx)^9}{b^7} + \frac{7d(bc - ad)^6 (a + bx)^{10}}{b^7} + \frac{21d^2(bc - ad)^5 (a + bx)^{11}}{b^7} + \frac{35d^3(bc - ad)^4 (a + bx)^{12}}{b^7} + \frac{7d^4(bc - ad)^3 (a + bx)^{13}}{b^7} + \frac{7d^5(bc - ad)^2 (a + bx)^{14}}{b^7} + \frac{7d^6(bc - ad) (a + bx)^{15}}{b^7} + \frac{d^7 (a + bx)^{16}}{b^7} \right) dx \\ &= \frac{(bc - ad)^7 (a + bx)^{10}}{10b^8} + \frac{7d(bc - ad)^6 (a + bx)^{11}}{11b^8} + \frac{7d^2(bc - ad)^5 (a + bx)^{12}}{4b^8} + \frac{35d^3(bc - ad)^4 (a + bx)^{13}}{13b^8} + \frac{5d^4(bc - ad)^3 (a + bx)^{14}}{2b^8} + \frac{7d^5(bc - ad)^2 (a + bx)^{15}}{5b^8} + \frac{7d^6(bc - ad) (a + bx)^{16}}{16b^8} + \frac{d^7 (a + bx)^{17}}{17b^8} \end{aligned}$$

Mathematica [B] time = 0.15, size = 993, normalized size = 4.96

$$\frac{1}{17}b^9d^7x^{17} + \frac{1}{16}b^8d^6(7bc+9ad)x^{16} + \frac{1}{5}b^7d^5(7b^2c^2 + 21abdc + 12a^2d^2)x^{15} + \frac{1}{2}b^6d^4(5b^3c^3 + 27ab^2dc^2 + 36a^2bd^2c +$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^9*(c + d*x)^7,x]

[Out] $a^9c^7x + (a^8c^6(9bc + 7ad)x^2)/2 + a^7c^5(12b^2c^2 + 21abc^2 + 7a^2d^2)x^3 + (7a^6c^4(12b^3c^3 + 36ab^2c^2d + 27a^2b^2c^2d^2 + 5a^3d^3)x^4)/4 + (7a^5c^3(18b^4c^4 + 84ab^3c^3d + 108a^2b^2c^2d^2 + 45a^3b^2cd^3 + 5a^4d^4)x^5)/5 + (7a^4c^2(6b^5c^5 + 42ab^4c^4d + 84a^2b^3c^3d^2 + 60a^3b^2c^2d^3 + 15a^4b^2cd^4 + a^5d^5)x^6)/2 + a^3c(12b^6c^6 + 126ab^5c^5d + 378a^2b^4c^4d^2 + 420a^3b^3c^3d^3 + 180a^4b^2c^2d^4 + 27a^5b^2cd^5 + a^6d^6)x^7 + (a^2(36b^7c^7 + 588ab^6c^6d + 2646a^2b^5c^5d^2 + 4410a^3b^4c^4d^3 + 2940a^4b^3c^3d^4 + 756a^5b^2c^2d^5 + 63a^6b^2cd^6 + a^7d^7)x^8)/8 + ab(b^7c^7 + 28ab^6c^6d + 196a^2b^5c^5d^2 + 490a^3b^4c^4d^3 + 490a^4b^3c^3d^4 + 196a^5b^2c^2d^5 + 28a^6b^2cd^6 + a^7d^7)x^9 + (b^2(b^7c^7 + 63ab^6c^6d + 756a^2b^5c^5d^2 + 2940a^3b^4c^4d^3 + 4410a^4b^3c^3d^4 + 2646a^5b^2c^2d^5 + 588a^6b^2cd^6 + 36a^7d^7)x^10)/10 + (7b^3d(b^6c^6 + 27ab^5c^5d + 180a^2b^4c^4d^2 + 420a^3b^3c^3d^3 + 378a^4b^2c^2d^4 + 126a^5b^2cd^5 + 12a^6d^6)x^11)/11 + (7b^4d^2(b^5c^5 + 15ab^4c^4d + 60a^2b^3c^3d^2 + 84a^3b^2c^2d^3 + 42a^4b^2cd^4 + 6a^5d^5)x^12)/4 + (7b^5d^3(5b^4c^4 + 45ab^3c^3d + 108a^2b^2c^2d^2 + 84a^3b^2cd^3 + 18a^4d^4)x^13)/13 + (b^6d^4(5b^3c^3 + 27ab^2c^2d + 36a^2b^2cd^2 + 12a^3d^3)x^14)/2 + (b^7d^5(7b^2c^2 + 21ab^2cd + 12a^2d^2)x^15)/5 + (b^8d^6(7bc + 9ad)x^16)/16 + (b^9d^7x^17)/17$

fricas [B] time = 0.38, size = 1175, normalized size = 5.88

$$\frac{1}{17}x^{17}d^7b^9 + \frac{7}{16}x^{16}d^6cb^9 + \frac{9}{16}x^{16}d^7b^8a + \frac{7}{5}x^{15}d^5c^2b^9 + \frac{21}{5}x^{15}d^6cb^8a + \frac{12}{5}x^{15}d^7b^7a^2 + \frac{5}{2}x^{14}d^4c^3b^9 + \frac{27}{2}x^{14}d^5c^2b^8a + 18x^{14}d^6c^2b^7a^2 + \frac{7}{2}x^{14}d^7b^6a^3 + \frac{35}{13}x^{13}d^3c^4b^9 + \frac{315}{13}x^{13}d^4c^3b^8a + \frac{756}{13}x^{13}d^5c^2b^7a^2 + \frac{588}{13}x^{13}d^6c^2b^6a^3 + \frac{126}{13}x^{13}d^7b^5a^4 + \frac{7}{4}x^{12}d^2c^5b^9 + \frac{105}{4}x^{12}d^3c^4b^8a + 105x^{12}d^4c^3b^7a^2 + 147x^{12}d^5c^2b^6a^3 + 147/2x^{12}d^6c^2b^5a^4 + 21/2x^{12}d^7b^4a^5 + 7/11$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^9*(d*x+c)^7,x, algorithm="fricas")

[Out] $1/17*x^{17}d^7b^9 + 7/16*x^{16}d^6c*b^9 + 9/16*x^{16}d^7b^8*a + 7/5*x^{15}d^5c^2b^9 + 21/5*x^{15}d^6c*b^8*a + 12/5*x^{15}d^7b^7*a^2 + 5/2*x^{14}d^4c^3b^9 + 27/2*x^{14}d^5c^2b^8*a + 18*x^{14}d^6c^2b^7*a^2 + 6*x^{14}d^7b^6*a^3 + 35/13*x^{13}d^3c^4b^9 + 315/13*x^{13}d^4c^3b^8*a + 756/13*x^{13}d^5c^2b^7*a^2 + 588/13*x^{13}d^6c^2b^6*a^3 + 126/13*x^{13}d^7b^5*a^4 + 7/4*x^{12}d^2c^5b^9 + 105/4*x^{12}d^3c^4b^8*a + 105*x^{12}d^4c^3b^7*a^2 + 147*x^{12}d^5c^2b^6*a^3 + 147/2*x^{12}d^6c^2b^5*a^4 + 21/2*x^{12}d^7b^4*a^5 + 7/11$

$$\begin{aligned}
& x^{11}d^6c^6b^9 + 189/11x^{11}d^2c^5b^8a + 1260/11x^{11}d^3c^4b^7a^2 \\
& + 2940/11x^{11}d^4c^3b^6a^3 + 2646/11x^{11}d^5c^2b^5a^4 + 882/11x^{11} \\
& d^6c^6b^4a^5 + 84/11x^{11}d^7b^3a^6 + 1/10x^{10}c^7b^9 + 63/10x^{10}d^* \\
& c^6b^8a + 378/5x^{10}d^2c^5b^7a^2 + 294x^{10}d^3c^4b^6a^3 + 441x^{10} \\
& d^4c^3b^5a^4 + 1323/5x^{10}d^5c^2b^4a^5 + 294/5x^{10}d^6c^6b^3a^6 \\
& + 18/5x^{10}d^7b^2a^7 + x^9c^7b^8a + 28x^9d^*c^6b^7a^2 + 196x^9d^ \\
& 2c^5b^6a^3 + 490x^9d^3c^4b^5a^4 + 490x^9d^4c^3b^4a^5 + 196x^9 \\
& d^5c^2b^3a^6 + 28x^9d^6c^6b^2a^7 + x^9d^7b^8a + 9/2x^8c^7b^7a \\
& ^2 + 147/2x^8d^*c^6b^6a^3 + 1323/4x^8d^2c^5b^5a^4 + 2205/4x^8d^3c^ \\
& 4b^4a^5 + 735/2x^8d^4c^3b^3a^6 + 189/2x^8d^5c^2b^2a^7 + 63/8x^ \\
& 8d^6c^6b^8a + 1/8x^8d^7a^9 + 12x^7c^7b^6a^3 + 126x^7d^*c^6b^5a \\
& ^4 + 378x^7d^2c^5b^4a^5 + 420x^7d^3c^4b^3a^6 + 180x^7d^4c^3b^ \\
& ^2a^7 + 27x^7d^5c^2b^2a^8 + x^7d^6c^6a^9 + 21x^6c^7b^5a^4 + 147x^ \\
& 6d^*c^6b^4a^5 + 294x^6d^2c^5b^3a^6 + 210x^6d^3c^4b^2a^7 + 105/2 \\
& x^6d^4c^3b^8a + 7/2x^6d^5c^2a^9 + 126/5x^5c^7b^4a^5 + 588/5x^ \\
& 5d^*c^6b^3a^6 + 756/5x^5d^2c^5b^2a^7 + 63x^5d^3c^4b^8a + 7x^5d^ \\
& 4c^3a^9 + 21x^4c^7b^3a^6 + 63x^4d^*c^6b^2a^7 + 189/4x^4d^2c^5 \\
& *b^8a + 35/4x^4d^3c^4a^9 + 12x^3c^7b^2a^7 + 21x^3d^*c^6b^8a + 7 \\
& x^3d^2c^5a^9 + 9/2x^2c^7b^8a + 7/2x^2d^*c^6a^9 + xc^7a^9
\end{aligned}$$

giac [B] time = 1.05, size = 1175, normalized size = 5.88

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^9*(d*x+c)^7,x, algorithm="giac")

[Out] $1/17b^9d^7x^{17} + 7/16b^9c^*d^6x^{16} + 9/16a^*b^8d^7x^{16} + 7/5b^9c^2d^5x^{15} + 21/5a^*b^8c^*d^6x^{15} + 12/5a^2b^7d^7x^{15} + 5/2b^9c^3d^4x^{14} + 27/2a^*b^8c^2d^5x^{14} + 18a^2b^7c^*d^6x^{14} + 6a^3b^6d^7x^{14} + 35/13b^9c^4d^3x^{13} + 315/13a^*b^8c^3d^4x^{13} + 756/13a^2b^7c^2d^5x^{13} + 588/13a^3b^6c^*d^6x^{13} + 126/13a^4b^5d^7x^{13} + 7/4b^9c^5d^2x^{12} + 105/4a^*b^8c^4d^3x^{12} + 105a^2b^7c^3d^4x^{12} + 147a^3b^6c^2d^5x^{12} + 147/2a^4b^5c^*d^6x^{12} + 21/2a^5b^4d^7x^{12} + 7/11b^9c^6d^*x^{11} + 189/11a^*b^8c^5d^2x^{11} + 1260/11a^2b^7c^4d^3x^{11} + 2940/11a^3b^6c^3d^4x^{11} + 2646/11a^4b^5c^2d^5x^{11} + 882/11a^5b^4c^*d^6x^{11} + 84/11a^6b^3d^7x^{11} + 1/10b^9c^7x^{10} + 63/10a^*b^8c^6d^*x^{10} + 378/5a^2b^7c^5d^2x^{10} + 294a^3b^6c^4d^3x^{10} + 441a^4b^5c^3d^4x^{10} + 1323/5a^5b^4c^2d^5x^{10} + 294/5a^6b^3c^*d^6x^{10} + 18/5a^7b^2d^7x^{10} + a^*b^8c^7x^9 + 28a^2b^7c^6d^*x^9 + 196a^3b^6c^5d^2x^9 + 490a^4b^5c^4d^3x^9 + 490a^5b^4c^3d^4x^9 + 196a^6b^3c^2d^5x^9 + 28a^7b^2c^*d^6x^9 + a^8b^*d^7x^9 + 9/2a^2b^7c^7x^8 + 147/2a^3b^6c^6d^*x^8 + 1323/4a^4b^5c^5d^2x^8 + 2205/4a^5b^4c^4d^3x^8 + 735/2a^6b^3c^3d^4x^8 + 189/2a^7b^2c^2d^5x^8 + 63/8a^8b^*c^*d^6x^8 + 1/8a^9d^7x^8 + 12a^3b^6c^7x^7 + 126a^4b^5c^6d^*$

$$x^7 + 378a^5b^4c^5d^2x^7 + 420a^6b^3c^4d^3x^7 + 180a^7b^2c^3d^4x^7 + 27a^8b^2c^2d^5x^7 + a^9c^6d^6x^7 + 21a^4b^5c^7x^6 + 147a^5b^4c^6d^7x^6 + 294a^6b^3c^5d^2x^6 + 210a^7b^2c^4d^3x^6 + 105/2a^8b^2c^3d^4x^6 + 7/2a^9c^2d^5x^6 + 126/5a^5b^4c^7x^5 + 588/5a^6b^3c^6d^7x^5 + 756/5a^7b^2c^5d^2x^5 + 63a^8b^2c^4d^3x^5 + 7a^9c^3d^4x^5 + 21a^6b^3c^7x^4 + 63a^7b^2c^6d^7x^4 + 189/4a^8b^2c^5d^2x^4 + 35/4a^9c^4d^3x^4 + 12a^7b^2c^7x^3 + 21a^8b^2c^6d^7x^3 + 7a^9c^5d^2x^3 + 9/2a^8b^2c^7x^2 + 7/2a^9c^6d^7x^2 + a^9c^7x$$

maple [B] time = 0.00, size = 1033, normalized size = 5.16

$$\frac{b^9d^7x^{17}}{17} + a^9c^7x + \frac{(9ab^8d^7 + 7b^9cd^6)x^{16}}{16} + \frac{(36a^2b^7d^7 + 63ab^8cd^6 + 21b^9c^2d^5)x^{15}}{15} + \frac{(84a^3b^6d^7 + 252a^2b^7cd^6 + 189ab^8c^2d^5 + 35b^9c^3d^4)x^{14}}{14} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^9*(d*x+c)^7,x)

[Out] $\frac{1}{17}b^9d^7x^{17} + \frac{1}{16}(9a^2b^8d^7 + 7b^9cd^6)x^{16} + \frac{1}{15}(36a^2b^7d^7 + 63ab^8cd^6 + 21b^9c^2d^5)x^{15} + \frac{1}{14}(84a^3b^6d^7 + 252a^2b^7cd^6 + 189ab^8c^2d^5 + 35b^9c^3d^4)x^{14} + \frac{1}{13}(126a^4b^5d^7 + 588a^3b^6cd^6 + 756a^2b^7c^2d^5 + 315ab^8c^3d^4 + 35b^9c^4d^3)x^{13} + \frac{1}{12}(126a^5b^4d^7 + 882a^4b^5cd^6 + 1764a^3b^6c^2d^5 + 1260a^2b^7c^3d^4 + 315ab^8c^4d^3 + 21b^9c^5d^2)x^{12} + \frac{1}{11}(84a^6b^3d^7 + 882a^5b^4cd^6 + 2646a^4b^5c^2d^5 + 2940a^3b^6c^3d^4 + 1260a^2b^7c^4d^3 + 189ab^8c^5d^2 + 7b^9c^6d)x^{11} + \frac{1}{10}(36a^7b^2d^7 + 588a^6b^3cd^6 + 2646a^5b^4c^2d^5 + 4410a^4b^5c^3d^4 + 2940a^3b^6c^4d^3 + 756a^2b^7c^5d^2 + 63ab^8c^6d + b^9c^7)x^{10} + \frac{1}{9}(9a^8b^2d^7 + 252a^7b^2cd^6 + 1764a^6b^3c^2d^5 + 4410a^5b^4c^3d^4 + 4410a^4b^5c^4d^3 + 1764a^3b^6c^5d^2 + 252a^2b^7c^6d + 9ab^8c^7)x^9 + \frac{1}{8}(a^9d^7 + 63a^8b^2cd^6 + 756a^7b^2c^2d^5 + 2940a^6b^3c^3d^4 + 4410a^5b^4c^4d^3 + 2646a^4b^5c^5d^2 + 588a^3b^6c^6d + 36a^2b^7c^7)x^8 + \frac{1}{7}(7a^9c^6d^7 + 189a^8b^2c^2d^5 + 1260a^7b^2c^3d^4 + 2940a^6b^3c^4d^3 + 2646a^5b^4c^5d^2 + 882a^4b^5c^6d + 84a^3b^6c^7)x^7 + \frac{1}{6}(21a^9c^5d^7 + 315a^8b^2c^3d^4 + 1260a^7b^2c^4d^3 + 1764a^6b^3c^5d^2 + 882a^5b^4c^6d + 126a^4b^5c^7)x^6 + \frac{1}{5}(35a^9c^4d^7 + 315a^8b^2c^4d^3 + 756a^7b^2c^5d^2 + 588a^6b^3c^6d + 126a^5b^4c^7)x^5 + \frac{1}{4}(35a^9c^4d^3 + 189a^8b^2c^5d^2 + 252a^7b^2c^6d + 84a^6b^3c^7)x^4 + \frac{1}{3}(21a^9c^5d^2 + 63a^8b^2c^6d + 36a^7b^2c^7)x^3 + \frac{1}{2}(7a^9c^6d + 9a^8b^2c^7)x^2 + a^9c^7x$

maxima [B] time = 1.43, size = 1023, normalized size = 5.12

$$\frac{1}{17}b^9d^7x^{17} + a^9c^7x + \frac{1}{16}(7b^9cd^6 + 9ab^8d^7)x^{16} + \frac{1}{5}(7b^9c^2d^5 + 21ab^8cd^6 + 12a^2b^7d^7)x^{15} + \frac{1}{2}(5b^9c^3d^4 + 27ab^8c^2d^5)x^{14} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^9*(d*x+c)^7,x, algorithm="maxima")

[Out] $\frac{1}{17}b^9d^7x^{17} + a^9c^7x + \frac{1}{16}(7b^9cd^6 + 9ab^8d^7)x^{16} + \frac{1}{5}(7b^9c^2d^5 + 21a^2b^8cd^6 + 12a^2b^7d^7)x^{15} + \frac{1}{2}(5b^9c^3d^4 + 27ab^8c^2d^5 + 36a^2b^7cd^6 + 12a^3b^6d^7)x^{14} + \frac{7}{13}(5b^9c^4d^3 + 45ab^8c^3d^4 + 108a^2b^7c^2d^5 + 84a^3b^6cd^6 + 18a^4b^5d^7)x^{13} + \frac{7}{4}(b^9c^5d^2 + 15ab^8c^4d^3 + 60a^2b^7c^3d^4 + 84a^3b^6c^2d^5 + 42a^4b^5cd^6 + 6a^5b^4d^7)x^{12} + \frac{7}{11}(b^9c^6d + 27ab^8c^5d^2 + 180a^2b^7c^4d^3 + 420a^3b^6c^3d^4 + 378a^4b^5c^2d^5 + 126a^5b^4cd^6 + 12a^6b^3d^7)x^{11} + \frac{1}{10}(b^9c^7 + 63ab^8c^6d + 756a^2b^7c^5d^2 + 2940a^3b^6c^4d^3 + 4410a^4b^5c^3d^4 + 2646a^5b^4c^2d^5 + 588a^6b^3cd^6 + 36a^7b^2d^7)x^{10} + (ab^8c^7 + 28a^2b^7c^6d + 196a^3b^6c^5d^2 + 490a^4b^5c^4d^3 + 490a^5b^4c^3d^4 + 196a^6b^3c^2d^5 + 28a^7b^2cd^6 + a^8b^1d^7)x^9 + \frac{1}{8}(36a^2b^7c^7 + 588a^3b^6c^6d + 2646a^4b^5c^5d^2 + 4410a^5b^4c^4d^3 + 2940a^6b^3c^3d^4 + 756a^7b^2c^2d^5 + 63a^8b^1cd^6 + a^9d^7)x^8 + (12a^3b^6c^7 + 126a^4b^5c^6d + 378a^5b^4c^5d^2 + 420a^6b^3c^4d^3 + 180a^7b^2c^3d^4 + 27a^8b^1c^2d^5 + a^9cd^6)x^7 + \frac{7}{2}(6a^4b^5c^7 + 42a^5b^4c^6d + 84a^6b^3c^5d^2 + 60a^7b^2c^4d^3 + 15a^8b^1c^3d^4 + a^9c^2d^5)x^6 + \frac{7}{5}(18a^5b^4c^7 + 84a^6b^3c^6d + 108a^7b^2c^5d^2 + 45a^8b^1c^4d^3 + 5a^9c^3d^4)x^5 + \frac{7}{4}(12a^6b^3c^7 + 36a^7b^2c^6d + 27a^8b^1c^5d^2 + 5a^9c^4d^3)x^4 + (12a^7b^2c^7 + 21a^8b^1c^6d + 7a^9c^5d^2)x^3 + \frac{1}{2}(9a^8b^1c^7 + 7a^9c^6d)x^2$

mupad [B] time = 0.55, size = 997, normalized size = 4.98

$$x^5 \left(7a^9c^3d^4 + 63a^8bc^4d^3 + \frac{756a^7b^2c^5d^2}{5} + \frac{588a^6b^3c^6d}{5} + \frac{126a^5b^4c^7}{5} \right) + x^{13} \left(\frac{126a^4b^5d^7}{13} + \frac{588a^3b^6cd^6}{13} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^9*(c + d*x)^7,x)

[Out] $x^5 \left(\frac{126a^5b^4c^7}{5} + 7a^9c^3d^4 + \frac{588a^6b^3c^6d}{5} + 63a^8b^1c^4d^3 + \frac{756a^7b^2c^5d^2}{5} \right) + x^{13} \left(\frac{126a^4b^5d^7}{13} + \frac{35b^9c^4d^3}{13} + \frac{315a^2b^8c^3d^4}{13} + \frac{588a^3b^6cd^6}{13} + \frac{756a^2b^7c^2d^5}{13} \right) + x^8 \left(\frac{a^9d^7}{8} + \frac{9a^2b^7c^7}{2} + \frac{147a^3b^6c^6d}{2} + \frac{1323a^4b^5c^5d^2}{4} + \frac{2205a^5b^4c^4d^3}{4} + \frac{735a^6b^3c^3d^4}{2} + \frac{189a^7b^2c^2d^5}{2} + \frac{63a^8b^1cd^6}{8} \right) + x^{10} \left(\frac{b^9c^7}{1} + \frac{18a^7b^2d^7}{5} + \frac{294a^6b^3cd^6}{5} + \frac{378a^2b^7c^5d^2}{5} + 294a^3b^6c^4d^3 + 441a^4b^5c^3d^4 + \frac{1323a^5b^4c^2d^5}{5} + \frac{63ab^8c^6d}{10} \right) + x^6 \left(\frac{21a^4b^5c^7}{2} + \frac{7a^9c^2d^5}{2} + 147a^5b^4c^6d + \frac{105a^8b^1c^3d^4}{2} + 294a^6b^3c^5d^2 + 210a^7b^2c^4d^3 \right) + x^{12} \left(\frac{21a^5b^4d^7}{2} + \frac{7b^9c^5d^2}{4} + \frac{105ab^8c^4d^3}{4} + \frac{147a^4b^5cd^6}{2} + 105a^2b^7c^3d^4 + 147a^3b^6c^2d^5 \right) + x^7(a^9c^7)$

$$\begin{aligned}
& *d^6 + 12*a^3*b^6*c^7 + 126*a^4*b^5*c^6*d + 27*a^8*b*c^2*d^5 + 378*a^5*b^4*c^5*d^2 + 420*a^6*b^3*c^4*d^3 + 180*a^7*b^2*c^3*d^4) + x^{11}*((7*b^9*c^6*d)/ \\
& 11 + (84*a^6*b^3*d^7)/11 + (189*a*b^8*c^5*d^2)/11 + (882*a^5*b^4*c*d^6)/11 \\
& + (1260*a^2*b^7*c^4*d^3)/11 + (2940*a^3*b^6*c^3*d^4)/11 + (2646*a^4*b^5*c^2 \\
& *d^5)/11) + x^9*(a*b^8*c^7 + a^8*b*d^7 + 28*a^2*b^7*c^6*d + 28*a^7*b^2*c*d^6 \\
& + 196*a^3*b^6*c^5*d^2 + 490*a^4*b^5*c^4*d^3 + 490*a^5*b^4*c^3*d^4 + 196*a^6*b^3*c^2*d^5) + a^9*c^7*x + (b^9*d^7*x^17)/17 + (7*a^6*c^4*x^4*(5*a^3*d^3 \\
& + 12*b^3*c^3 + 36*a*b^2*c^2*d + 27*a^2*b*c*d^2))/4 + (b^6*d^4*x^14*(12*a^3*d^3 \\
& + 5*b^3*c^3 + 27*a*b^2*c^2*d + 36*a^2*b*c*d^2))/2 + (a^8*c^6*x^2*(7*a*d \\
& + 9*b*c))/2 + (b^8*d^6*x^16*(9*a*d + 7*b*c))/16 + a^7*c^5*x^3*(7*a^2*d^2 \\
& + 12*b^2*c^2 + 21*a*b*c*d) + (b^7*d^5*x^15*(12*a^2*d^2 + 7*b^2*c^2 + 21*a*b \\
& *c*d))/5
\end{aligned}$$

sympy [B] time = 0.23, size = 1163, normalized size = 5.82

$$a^9c^7x + \frac{b^9d^7x^{17}}{17} + x^{16}\left(\frac{9ab^8d^7}{16} + \frac{7b^9cd^6}{16}\right) + x^{15}\left(\frac{12a^2b^7d^7}{5} + \frac{21ab^8cd^6}{5} + \frac{7b^9c^2d^5}{5}\right) + x^{14}\left(6a^3b^6d^7 + 18a^2b^7cd^6 + \frac{27}{5}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**9*(d*x+c)**7,x)

[Out] a**9*c**7*x + b**9*d**7*x**17/17 + x**16*(9*a*b**8*d**7/16 + 7*b**9*c*d**6/16) + x**15*(12*a**2*b**7*d**7/5 + 21*a*b**8*c*d**6/5 + 7*b**9*c**2*d**5/5) + x**14*(6*a**3*b**6*d**7 + 18*a**2*b**7*c*d**6 + 27*a*b**8*c**2*d**5/2 + 5*b**9*c**3*d**4/2) + x**13*(126*a**4*b**5*d**7/13 + 588*a**3*b**6*c*d**6/13 + 756*a**2*b**7*c**2*d**5/13 + 315*a*b**8*c**3*d**4/13 + 35*b**9*c**4*d**3/13) + x**12*(21*a**5*b**4*d**7/2 + 147*a**4*b**5*c*d**6/2 + 147*a**3*b**6*c**2*d**5 + 105*a**2*b**7*c**3*d**4 + 105*a*b**8*c**4*d**3/4 + 7*b**9*c**5*d**2/4) + x**11*(84*a**6*b**3*d**7/11 + 882*a**5*b**4*c*d**6/11 + 2646*a**4*b**5*c**2*d**5/11 + 2940*a**3*b**6*c**3*d**4/11 + 1260*a**2*b**7*c**4*d**3/11 + 189*a*b**8*c**5*d**2/11 + 7*b**9*c**6*d/11) + x**10*(18*a**7*b**2*d**7/5 + 294*a**6*b**3*c*d**6/5 + 1323*a**5*b**4*c**2*d**5/5 + 441*a**4*b**5*c**3*d**4 + 294*a**3*b**6*c**4*d**3 + 378*a**2*b**7*c**5*d**2/5 + 63*a*b**8*c**6*d/10 + b**9*c**7/10) + x**9*(a**8*b*d**7 + 28*a**7*b**2*c*d**6 + 196*a**6*b**3*c**2*d**5 + 490*a**5*b**4*c**3*d**4 + 490*a**4*b**5*c**4*d**3 + 196*a**3*b**6*c**5*d**2 + 28*a**2*b**7*c**6*d + a*b**8*c**7) + x**8*(a**9*d**7/8 + 63*a**8*b*c*d**6/8 + 189*a**7*b**2*c**2*d**5/2 + 735*a**6*b**3*c**3*d**4/2 + 2205*a**5*b**4*c**4*d**3/4 + 1323*a**4*b**5*c**5*d**2/4 + 147*a**3*b**6*c**6*d/2 + 9*a**2*b**7*c**7/2) + x**7*(a**9*c*d**6 + 27*a**8*b*c**2*d**5 + 180*a**7*b**2*c**3*d**4 + 420*a**6*b**3*c**4*d**3 + 378*a**5*b**4*c**5*d**2 + 126*a**4*b**5*c**6*d + 12*a**3*b**6*c**7) + x**6*(7*a**9*c**2*d**5/2 + 105*a**8*b*c**3*d**4/2 + 210*a**7*b**2*c**4*d**3 + 294*a**6*b**3*c**5*d**2 + 147*a**5*b**4*c**6*d + 21*a**4*b**5*c**7) + x**5*(7*a**9*c**3*d**4 + 63*a**8*b*c**4*d**3 + 756*a**7*b**2*c**5*d**2/5 + 588*a**6*b**3*c**6*d/5 + 126*a**5*b**4*c**7/5) + x**4*(35*a**9*c**4*d**3/4 + 189*a**8*b*c**5*d**2/4

$$+ 63a^{7}b^{2}c^{6}d + 21a^{6}b^{3}c^{7}) + x^{3}(7a^{9}c^{5}d^{2} + 21a^{8}b^{2}c^{6}d + 12a^{7}b^{2}c^{7}) + x^{2}(7a^{9}c^{6}d/2 + 9a^{8}b^{2}c^{7}/2)$$

3.1274 $\int (a + bx)^8 (c + dx)^7 dx$

Optimal. Leaf size=200

$$\frac{7d^6(a+bx)^{15}(bc-ad)}{15b^8} + \frac{3d^5(a+bx)^{14}(bc-ad)^2}{2b^8} + \frac{35d^4(a+bx)^{13}(bc-ad)^3}{13b^8} + \frac{35d^3(a+bx)^{12}(bc-ad)^4}{12b^8} + \frac{21d^2(a+bx)^{11}(bc-ad)^5}{11b^8} + \frac{7d(a+bx)^{10}(bc-ad)^6}{10b^8} + \frac{(a+bx)^9(bc-ad)^7}{9b^8}$$

[Out] $1/9*(-a*d+b*c)^7*(b*x+a)^9/b^8+7/10*d*(-a*d+b*c)^6*(b*x+a)^10/b^8+21/11*d^2*(-a*d+b*c)^5*(b*x+a)^11/b^8+35/12*d^3*(-a*d+b*c)^4*(b*x+a)^12/b^8+35/13*d^4*(-a*d+b*c)^3*(b*x+a)^13/b^8+3/2*d^5*(-a*d+b*c)^2*(b*x+a)^14/b^8+7/15*d^6*(-a*d+b*c)*(b*x+a)^15/b^8+1/16*d^7*(b*x+a)^16/b^8$

Rubi [A] time = 0.57, antiderivative size = 200, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{7d^6(a+bx)^{15}(bc-ad)}{15b^8} + \frac{3d^5(a+bx)^{14}(bc-ad)^2}{2b^8} + \frac{35d^4(a+bx)^{13}(bc-ad)^3}{13b^8} + \frac{35d^3(a+bx)^{12}(bc-ad)^4}{12b^8} + \frac{21d^2(a+bx)^{11}(bc-ad)^5}{11b^8} + \frac{7d(a+bx)^{10}(bc-ad)^6}{10b^8} + \frac{(a+bx)^9(bc-ad)^7}{9b^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^8*(c + d*x)^7, x]

[Out] $((b*c - a*d)^7*(a + b*x)^9)/(9*b^8) + (7*d*(b*c - a*d)^6*(a + b*x)^10)/(10*b^8) + (21*d^2*(b*c - a*d)^5*(a + b*x)^11)/(11*b^8) + (35*d^3*(b*c - a*d)^4*(a + b*x)^12)/(12*b^8) + (35*d^4*(b*c - a*d)^3*(a + b*x)^13)/(13*b^8) + (3*d^5*(b*c - a*d)^2*(a + b*x)^14)/(2*b^8) + (7*d^6*(b*c - a*d)*(a + b*x)^15)/(15*b^8) + (d^7*(a + b*x)^16)/(16*b^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int (a + bx)^8 (c + dx)^7 dx = \int \left(\frac{(bc - ad)^7 (a + bx)^8}{b^7} + \frac{7d(bc - ad)^6 (a + bx)^9}{b^7} + \frac{21d^2(bc - ad)^5 (a + bx)^{10}}{b^7} + \frac{35d^3(bc - ad)^4 (a + bx)^{11}}{b^7} + \frac{35d^4(bc - ad)^3 (a + bx)^{12}}{b^7} + \frac{3d^5(bc - ad)^2 (a + bx)^{13}}{b^7} + \frac{7d^6(bc - ad) (a + bx)^{14}}{b^7} + \frac{d^7 (a + bx)^{15}}{b^7} \right) dx$$

$$= \frac{(bc - ad)^7 (a + bx)^9}{9b^8} + \frac{7d(bc - ad)^6 (a + bx)^{10}}{10b^8} + \frac{21d^2(bc - ad)^5 (a + bx)^{11}}{11b^8} + \frac{35d^3(bc - ad)^4 (a + bx)^{12}}{12b^8} + \frac{35d^4(bc - ad)^3 (a + bx)^{13}}{13b^8} + \frac{3d^5(bc - ad)^2 (a + bx)^{14}}{2b^8} + \frac{7d^6(bc - ad) (a + bx)^{15}}{15b^8} + \frac{d^7 (a + bx)^{16}}{16b^8}$$

Mathematica [B] time = 0.11, size = 897, normalized size = 4.48

$$\frac{1}{16}b^8d^7x^{16} + \frac{1}{15}b^7d^6(7bc+8ad)x^{15} + \frac{1}{2}b^6d^5(3b^2c^2 + 8abdc + 4a^2d^2)x^{14} + \frac{7}{13}b^5d^4(5b^3c^3 + 24ab^2dc^2 + 28a^2bd^2c +$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^8*(c + d*x)^7,x]

[Out] $a^8c^7x + (a^7c^6(8b^2c + 7a^2d)x^2)/2 + (7a^6c^5(4b^2c^2 + 8a^2b^2c^2d + 3a^2d^2)x^3)/3 + (7a^5c^4(8b^3c^3 + 28a^2b^2c^2d + 24a^2b^2c^2d^2 + 5a^3d^3)x^4)/4 + (7a^4c^3(10b^4c^4 + 56a^3b^3c^3d + 84a^2b^2c^2d^2 + 40a^3b^2c^2d^2 + 5a^4d^4)x^5)/5 + (7a^3c^2(8b^5c^5 + 70a^4b^4c^4d + 168a^2b^3c^3d^2 + 140a^3b^2c^2d^3 + 40a^4b^2c^2d^3 + 3a^5d^5)x^6)/6 + a^2c(4b^6c^6 + 56a^5b^5c^5d + 210a^2b^4c^4d^2 + 280a^3b^3c^3d^3 + 140a^4b^2c^2d^4 + 24a^5b^2c^2d^4 + a^6d^6)x^7 + (a(8b^7c^7 + 196a^6b^6c^6d + 1176a^2b^5c^5d^2 + 2450a^3b^4c^4d^3 + 1960a^4b^3c^3d^4 + 588a^5b^2c^2d^5 + 56a^6b^2c^2d^6 + a^7d^7)x^8)/8 + (b(b^7c^7 + 56a^6b^6c^6d + 588a^2b^5c^5d^2 + 1960a^3b^4c^4d^3 + 2450a^4b^3c^3d^4 + 1176a^5b^2c^2d^5 + 196a^6b^2c^2d^6 + 8a^7d^7)x^9)/9 + (7b^2d(b^6c^6 + 24a^5b^5c^5d + 140a^2b^4c^4d^2 + 280a^3b^3c^3d^3 + 210a^4b^2c^2d^4 + 56a^5b^2c^2d^4 + 4a^6d^6)x^10)/10 + (7b^3d^2(3b^5c^5 + 40a^4b^4c^4d + 140a^2b^3c^3d^2 + 168a^3b^2c^2d^3 + 70a^4b^2c^2d^3 + 8a^5d^5)x^11)/11 + (7b^4d^3(5b^4c^4 + 40a^3b^3c^3d + 84a^2b^2c^2d^2 + 56a^3b^2c^2d^2 + 10a^4d^4)x^12)/12 + (7b^5d^4(5b^3c^3 + 24a^2b^2c^2d + 28a^2b^2c^2d^2 + 8a^3d^3)x^13)/13 + (b^6d^5(3b^2c^2 + 8a^2b^2c^2 + 4a^2d^2)x^14)/2 + (b^7d^6(7b^2c + 8a^2d)x^15)/15 + (b^8d^7x^16)/16$

fricas [B] time = 0.39, size = 1050, normalized size = 5.25

$$\frac{1}{16}x^{16}d^7b^8 + \frac{7}{15}x^{15}d^6cb^8 + \frac{8}{15}x^{15}d^7b^7a + \frac{3}{2}x^{14}d^5c^2b^8 + 4x^{14}d^6cb^7a + 2x^{14}d^7b^6a^2 + \frac{35}{13}x^{13}d^4c^3b^8 + \frac{168}{13}x^{13}d^5c^2b^7a + \frac{196}{13}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8*(d*x+c)^7,x, algorithm="fricas")

[Out] $1/16*x^{16}*d^7*b^8 + 7/15*x^{15}*d^6*c*b^8 + 8/15*x^{15}*d^7*b^7*a + 3/2*x^{14}*d^5*c^2*b^8 + 4*x^{14}*d^6*c*b^7*a + 2*x^{14}*d^7*b^6*a^2 + 35/13*x^{13}*d^4*c^3*b^8 + 168/13*x^{13}*d^5*c^2*b^7*a + 196/13*x^{13}*d^6*c*b^6*a^2 + 56/13*x^{13}*d^7*b^5*a^3 + 35/12*x^{12}*d^3*c^4*b^8 + 70/3*x^{12}*d^4*c^3*b^7*a + 49*x^{12}*d^5*c^2*b^6*a^2 + 98/3*x^{12}*d^6*c*b^5*a^3 + 35/6*x^{12}*d^7*b^4*a^4 + 21/11*x^{11}*d^2*c^5*b^8 + 280/11*x^{11}*d^3*c^4*b^7*a + 980/11*x^{11}*d^4*c^3*b^6*a^2 + 1176/11*x^{11}*d^5*c^2*b^5*a^3 + 490/11*x^{11}*d^6*c*b^4*a^4 + 56/11*x^{11}*d^7*b^3*a^5 + 7/10*x^{10}*d*c^6*b^8 + 84/5*x^{10}*d^2*c^5*b^7*a + 98*x^{10}*d^3*c^4*b^6*a^2 + 196*x^{10}*d^4*c^3*b^5*a^3 + 147*x^{10}*d^5*c^2*b^4*a^4 + 196/5*x^{10}*d^6*c*b$

$$\begin{aligned} &^3a^5 + 14/5x^{10}d^7b^2a^6 + 1/9x^9c^7b^8 + 56/9x^9d^6c^6b^7a + 1 \\ &96/3x^9d^2c^5b^6a^2 + 1960/9x^9d^3c^4b^5a^3 + 2450/9x^9d^4c^3b^4a^4 + 392/3x^9d^5c^2b^3a^5 + 196/9x^9d^6c^1b^2a^6 + 8/9x^9d^7 \\ &*b^1a^7 + x^8c^7b^7a + 49/2x^8d^6c^6b^6a^2 + 147x^8d^2c^5b^5a^3 + \\ &1225/4x^8d^3c^4b^4a^4 + 245x^8d^4c^3b^3a^5 + 147/2x^8d^5c^2b^2a^6 + 7x^8d^6c^1b^1a^7 + 1/8x^8d^7a^8 + 4x^7c^7b^6a^2 + 56x^7d \\ &*c^6b^5a^3 + 210x^7d^2c^5b^4a^4 + 280x^7d^3c^4b^3a^5 + 140x^7d^4c^3b^2a^6 + 24x^7d^5c^2b^1a^7 + x^7d^6c^1a^8 + 28/3x^6c^7b^5a^3 \\ &^3 + 245/3x^6d^6c^6b^4a^4 + 196x^6d^2c^5b^3a^5 + 490/3x^6d^3c^4b^2a^6 + 140/3x^6d^4c^3b^1a^7 + 7/2x^6d^5c^2a^8 + 14x^5c^7b^4a^4 \\ &4 + 392/5x^5d^6c^6b^3a^5 + 588/5x^5d^2c^5b^2a^6 + 56x^5d^3c^4b^1a^7 + 7x^5d^4c^3a^8 + 14x^4c^7b^3a^5 + 49x^4d^6c^6b^2a^6 + 42x^4 \\ &4d^2c^5b^1a^7 + 35/4x^4d^3c^4a^8 + 28/3x^3c^7b^2a^6 + 56/3x^3d^6c^6b^1a^7 + 7x^3d^2c^5a^8 + 4x^2c^7b^1a^7 + 7/2x^2d^6c^6a^8 + xc^7 \\ &a^8 \end{aligned}$$

giac [B] time = 1.01, size = 1050, normalized size = 5.25

$$\frac{1}{16} b^8 d^7 x^{16} + \frac{7}{15} b^8 c d^6 x^{15} + \frac{8}{15} a b^7 d^7 x^{15} + \frac{3}{2} b^8 c^2 d^5 x^{14} + 4 a b^7 c d^6 x^{14} + 2 a^2 b^6 d^7 x^{14} + \frac{35}{13} b^8 c^3 d^4 x^{13} + \frac{168}{13} a b^7 c^2 d^5 x^{13} + \frac{1}{1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8*(d*x+c)^7,x, algorithm="giac")

[Out] $\frac{1}{16} b^8 d^7 x^{16} + \frac{7}{15} b^8 c d^6 x^{15} + \frac{8}{15} a b^7 d^7 x^{15} + \frac{3}{2} b^8 c^2 d^5 x^{14} + 4 a b^7 c d^6 x^{14} + 2 a^2 b^6 d^7 x^{14} + \frac{35}{13} b^8 c^3 d^4 x^{13} + \frac{168}{13} a b^7 c^2 d^5 x^{13} + \frac{1}{1} a^3 b^5 c^2 d^5 x^{11} + 490/11 a^4 b^4 c^2 d^6 x^{11} + 56/11 a^5 b^3 d^7 x^{11} + 7/10 b^8 c^6 d^2 x^{10} + 84/5 a b^7 c^5 d^2 x^{10} + 98 a^2 b^6 c^4 d^3 x^{10} + 196 a^3 b^5 c^3 d^4 x^{10} + 147 a^4 b^4 c^2 d^5 x^{10} + 196/5 a^5 b^3 c^1 d^6 x^{10} + 14/5 a^6 b^2 d^7 x^{10} + 1/9 b^8 c^7 x^9 + 56/9 a b^7 c^6 d x^9 + 196/3 a^2 b^6 c^5 d^2 x^9 + 1960/9 a^3 b^5 c^4 d^3 x^9 + 2450/9 a^4 b^4 c^3 d^4 x^9 + 392/3 a^5 b^3 c^2 d^5 x^9 + 196/9 a^6 b^2 c^1 d^6 x^9 + 8/9 a^7 b^1 d^7 x^9 + a b^7 c^7 x^8 + 49/2 a^2 b^6 c^6 d x^8 + 147 a^3 b^5 c^5 d^2 x^8 + 1225/4 a^4 b^4 c^4 d^3 x^8 + 245 a^5 b^3 c^3 d^4 x^8 + 147/2 a^6 b^2 c^2 d^5 x^8 + 7 a^7 b^1 c^1 d^6 x^8 + 1/8 a^8 d^7 x^8 + 4 a^2 b^6 c^7 x^7 + 56 a^3 b^5 c^6 d x^7 + 210 a^4 b^4 c^5 d^2 x^7 + 280 a^5 b^3 c^4 d^3 x^7 + 140 a^6 b^2 c^3 d^4 x^7 + 24 a^7 b^1 c^2 d^5 x^7 + a^8 c^1 d^6 x^7 + 28/3 a^3 b^5 c^7 x^6 + 245/3 a^4 b^4 c^6 d x^6 + 196 a^5 b^3 c^5 d^2 x^6 + 490/3 a^6 b^2 c^4 d^3 x^6 + 140/3 a^7 b^1 c^3 d^4 x^6 + 7/2 a^8 c^2 d^5 x^6 + 14 a^4 b^4 c^7 x^5 + 392/5 a^5 b^3 c^6 d x^5 + 588/5 a^6 b^2 c^5 d^2 x^5 + 56 a^7 b^1 c^4 d^3 x^5 + 7 a^8 c^3 d^4 x^5 + 14 a^5 b^3 c^7 x^4 + 49 a^6 b^2 c^6 d x^4 + 42 a^4$

$$7*b*c^5*d^2*x^4 + 35/4*a^8*c^4*d^3*x^4 + 28/3*a^6*b^2*c^7*x^3 + 56/3*a^7*b*c^6*d*x^3 + 7*a^8*c^5*d^2*x^3 + 4*a^7*b*c^7*x^2 + 7/2*a^8*c^6*d*x^2 + a^8*c^7*x$$

maple [B] time = 0.00, size = 925, normalized size = 4.62

$$\frac{b^8 d^7 x^{16}}{16} + a^8 c^7 x + \frac{(8 a b^7 d^7 + 7 b^8 c d^6) x^{15}}{15} + \frac{(28 a^2 b^6 d^7 + 56 a b^7 c d^6 + 21 b^8 c^2 d^5) x^{14}}{14} + \frac{(56 a^3 b^5 d^7 + 196 a^2 b^6 c d^6 + 168 a b^7 c^2 d^5 + 35 b^8 c^3 d^4) x^{13}}{13} + \frac{(70 a^4 b^4 d^7 + 392 a^3 b^5 c d^6 + 588 a^2 b^6 c^2 d^5 + 280 a b^7 c^3 d^4 + 35 b^8 c^4 d^3) x^{12}}{12} + \frac{(56 a^5 b^3 d^7 + 490 a^4 b^4 c d^6 + 1176 a^3 b^5 c^2 d^5 + 980 a^2 b^6 c^3 d^4 + 280 a b^7 c^4 d^3 + 21 b^8 c^5 d^2) x^{11}}{11} + \frac{(28 a^6 b^2 d^7 + 392 a^5 b^3 c d^6 + 1470 a^4 b^4 c^2 d^5 + 1960 a^3 b^5 c^3 d^4 + 980 a^2 b^6 c^4 d^3 + 168 a b^7 c^5 d^2 + 7 b^8 c^6 d) x^{10}}{10} + \frac{(8 a^7 b d^7 + 196 a^6 b^2 c d^6 + 1176 a^5 b^3 c^2 d^5 + 2450 a^4 b^4 c^3 d^4 + 1960 a^3 b^5 c^4 d^3 + 588 a^2 b^6 c^5 d^2 + 56 a b^7 c^6 d + b^8 c^7) x^9}{9} + \frac{(a^8 d^7 + 56 a^7 b c d^6 + 588 a^6 b^2 c^2 d^5 + 1960 a^5 b^3 c^3 d^4 + 2450 a^4 b^4 c^4 d^3 + 1176 a^3 b^5 c^5 d^2 + 196 a^2 b^6 c^6 d + 8 a b^7 c^7) x^8}{8} + \frac{(7 a^8 c d^6 + 168 a^7 b c^2 d^5 + 980 a^6 b^2 c^3 d^4 + 1960 a^5 b^3 c^4 d^3 + 1470 a^4 b^4 c^5 d^2 + 392 a^3 b^5 c^6 d + 28 a^2 b^6 c^7) x^7}{7} + \frac{(21 a^8 c^2 d^5 + 280 a^7 b c^3 d^4 + 980 a^6 b^2 c^4 d^3 + 1176 a^5 b^3 c^5 d^2 + 490 a^4 b^4 c^6 d + 56 a^3 b^5 c^7) x^6}{6} + \frac{(35 a^8 c^3 d^4 + 280 a^7 b c^4 d^3 + 588 a^6 b^2 c^5 d^2 + 392 a^5 b^3 c^6 d + 70 a^4 b^4 c^7) x^5}{5} + \frac{(35 a^8 c^4 d^3 + 168 a^7 b c^5 d^2 + 196 a^6 b^2 c^6 d + 56 a^5 b^3 c^7) x^4}{4} + \frac{(21 a^8 c^5 d^2 + 56 a^7 b c^6 d + 28 a^6 b^2 c^7) x^3}{3} + \frac{(7 a^8 c^6 d + 8 a^7 b c^7) x^2}{2} + a^8 c^7 x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^8*(d*x+c)^7,x)

[Out] 1/16*b^8*d^7*x^16+1/15*(8*a*b^7*d^7+7*b^8*c*d^6)*x^15+1/14*(28*a^2*b^6*d^7+56*a*b^7*c*d^6+21*b^8*c^2*d^5)*x^14+1/13*(56*a^3*b^5*d^7+196*a^2*b^6*c*d^6+168*a*b^7*c^2*d^5+35*b^8*c^3*d^4)*x^13+1/12*(70*a^4*b^4*d^7+392*a^3*b^5*c*d^6+588*a^2*b^6*c^2*d^5+280*a*b^7*c^3*d^4+35*b^8*c^4*d^3)*x^12+1/11*(56*a^5*b^3*d^7+490*a^4*b^4*c*d^6+1176*a^3*b^5*c^2*d^5+980*a^2*b^6*c^3*d^4+280*a*b^7*c^4*d^3+21*b^8*c^5*d^2)*x^11+1/10*(28*a^6*b^2*d^7+392*a^5*b^3*c*d^6+1470*a^4*b^4*c^2*d^5+1960*a^3*b^5*c^3*d^4+980*a^2*b^6*c^4*d^3+168*a*b^7*c^5*d^2+7*b^8*c^6*d)*x^10+1/9*(8*a^7*b*d^7+196*a^6*b^2*c*d^6+1176*a^5*b^3*c^2*d^5+2450*a^4*b^4*c^3*d^4+1960*a^3*b^5*c^4*d^3+588*a^2*b^6*c^5*d^2+56*a*b^7*c^6*d+b^8*c^7)*x^9+1/8*(a^8*d^7+56*a^7*b*c*d^6+588*a^6*b^2*c^2*d^5+1960*a^5*b^3*c^3*d^4+2450*a^4*b^4*c^4*d^3+1176*a^3*b^5*c^5*d^2+196*a^2*b^6*c^6*d+8*a*b^7*c^7)*x^8+1/7*(7*a^8*c*d^6+168*a^7*b*c^2*d^5+980*a^6*b^2*c^3*d^4+1960*a^5*b^3*c^4*d^3+1470*a^4*b^4*c^5*d^2+392*a^3*b^5*c^6*d+28*a^2*b^6*c^7)*x^7+1/6*(21*a^8*c^2*d^5+280*a^7*b*c^3*d^4+980*a^6*b^2*c^4*d^3+1176*a^5*b^3*c^5*d^2+490*a^4*b^4*c^6*d+56*a^3*b^5*c^7)*x^6+1/5*(35*a^8*c^3*d^4+280*a^7*b*c^4*d^3+588*a^6*b^2*c^5*d^2+392*a^5*b^3*c^6*d+70*a^4*b^4*c^7)*x^5+1/4*(35*a^8*c^4*d^3+168*a^7*b*c^5*d^2+196*a^6*b^2*c^6*d+56*a^5*b^3*c^7)*x^4+1/3*(21*a^8*c^5*d^2+56*a^7*b*c^6*d+28*a^6*b^2*c^7)*x^3+1/2*(7*a^8*c^6*d+8*a^7*b*c^7)*x^2+a^8*c^7*x

maxima [B] time = 1.40, size = 921, normalized size = 4.60

$$\frac{1}{16} b^8 d^7 x^{16} + a^8 c^7 x + \frac{1}{15} (7 b^8 c d^6 + 8 a b^7 d^7) x^{15} + \frac{1}{2} (3 b^8 c^2 d^5 + 8 a b^7 c d^6 + 4 a^2 b^6 d^7) x^{14} + \frac{7}{13} (5 b^8 c^3 d^4 + 24 a b^7 c^2 d^5 + 28 a^2 b^6 c d^6 + 8 a^3 b^5 d^7) x^{13} + \frac{7}{12} (5 b^8 c^4 d^3 + 40 a b^7 c^3 d^4 + 84 a^2 b^6 c^2 d^5 + 56 a^3 b^5 c d^6 + 10 a^4 b^4 d^7) x^{12} + \frac{7}{11} (3 b^8 c^5 d^2 + 40 a b^7 c^4 d^3 + 140 a^2 b^6 c^3 d^4 + 140 a^3 b^5 c^2 d^5 + 140 a^4 b^4 c d^6 + 140 a^5 b^3 d^7) x^{11} + \frac{7}{10} (28 a^6 b^2 d^7 + 392 a^5 b^3 c d^6 + 1470 a^4 b^4 c^2 d^5 + 1960 a^3 b^5 c^3 d^4 + 980 a^2 b^6 c^4 d^3 + 168 a b^7 c^5 d^2 + 7 b^8 c^6 d) x^{10} + \frac{7}{9} (8 a^7 b d^7 + 196 a^6 b^2 c d^6 + 1176 a^5 b^3 c^2 d^5 + 2450 a^4 b^4 c^3 d^4 + 1960 a^3 b^5 c^4 d^3 + 588 a^2 b^6 c^5 d^2 + 56 a b^7 c^6 d + b^8 c^7) x^9 + \frac{7}{8} (a^8 d^7 + 56 a^7 b c d^6 + 588 a^6 b^2 c^2 d^5 + 1960 a^5 b^3 c^3 d^4 + 2450 a^4 b^4 c^4 d^3 + 1176 a^3 b^5 c^5 d^2 + 196 a^2 b^6 c^6 d + 8 a b^7 c^7) x^8 + \frac{7}{7} (7 a^8 c d^6 + 168 a^7 b c^2 d^5 + 980 a^6 b^2 c^3 d^4 + 1960 a^5 b^3 c^4 d^3 + 1470 a^4 b^4 c^5 d^2 + 392 a^3 b^5 c^6 d + 28 a^2 b^6 c^7) x^7 + \frac{7}{6} (21 a^8 c^2 d^5 + 280 a^7 b c^3 d^4 + 980 a^6 b^2 c^4 d^3 + 1176 a^5 b^3 c^5 d^2 + 490 a^4 b^4 c^6 d + 56 a^3 b^5 c^7) x^6 + \frac{7}{5} (35 a^8 c^3 d^4 + 280 a^7 b c^4 d^3 + 588 a^6 b^2 c^5 d^2 + 392 a^5 b^3 c^6 d + 70 a^4 b^4 c^7) x^5 + \frac{7}{4} (35 a^8 c^4 d^3 + 168 a^7 b c^5 d^2 + 196 a^6 b^2 c^6 d + 56 a^5 b^3 c^7) x^4 + \frac{7}{3} (21 a^8 c^5 d^2 + 56 a^7 b c^6 d + 28 a^6 b^2 c^7) x^3 + \frac{7}{2} (7 a^8 c^6 d + 8 a^7 b c^7) x^2 + a^8 c^7 x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8*(d*x+c)^7,x, algorithm="maxima")

[Out] 1/16*b^8*d^7*x^16 + a^8*c^7*x + 1/15*(7*b^8*c*d^6 + 8*a*b^7*d^7)*x^15 + 1/2*(3*b^8*c^2*d^5 + 8*a*b^7*c*d^6 + 4*a^2*b^6*d^7)*x^14 + 7/13*(5*b^8*c^3*d^4 + 24*a*b^7*c^2*d^5 + 28*a^2*b^6*c*d^6 + 8*a^3*b^5*d^7)*x^13 + 7/12*(5*b^8*c^4*d^3 + 40*a*b^7*c^3*d^4 + 84*a^2*b^6*c^2*d^5 + 56*a^3*b^5*c*d^6 + 10*a^4*b^4*d^7)*x^12 + 7/11*(3*b^8*c^5*d^2 + 40*a*b^7*c^4*d^3 + 140*a^2*b^6*c^3*d^4 + 140*a^3*b^5*c^2*d^5 + 140*a^4*b^4*c*d^6 + 140*a^5*b^3*d^7)*x^11 + 7/10*(28*a^6*b^2*d^7 + 392*a^5*b^3*c*d^6 + 1470*a^4*b^4*c^2*d^5 + 1960*a^3*b^5*c^3*d^4 + 980*a^2*b^6*c^4*d^3 + 168*a*b^7*c^5*d^2 + 7*b^8*c^6*d)*x^10 + 7/9*(8*a^7*b*d^7 + 196*a^6*b^2*c*d^6 + 1176*a^5*b^3*c^2*d^5 + 2450*a^4*b^4*c^3*d^4 + 1960*a^3*b^5*c^4*d^3 + 588*a^2*b^6*c^5*d^2 + 56*a*b^7*c^6*d + b^8*c^7)*x^9 + 7/8*(a^8*d^7 + 56*a^7*b*c*d^6 + 588*a^6*b^2*c^2*d^5 + 1960*a^5*b^3*c^3*d^4 + 2450*a^4*b^4*c^4*d^3 + 1176*a^3*b^5*c^5*d^2 + 196*a^2*b^6*c^6*d + 8*a*b^7*c^7)*x^8 + 7/7*(7*a^8*c*d^6 + 168*a^7*b*c^2*d^5 + 980*a^6*b^2*c^3*d^4 + 1960*a^5*b^3*c^4*d^3 + 1470*a^4*b^4*c^5*d^2 + 392*a^3*b^5*c^6*d + 28*a^2*b^6*c^7)*x^7 + 7/6*(21*a^8*c^2*d^5 + 280*a^7*b*c^3*d^4 + 980*a^6*b^2*c^4*d^3 + 1176*a^5*b^3*c^5*d^2 + 490*a^4*b^4*c^6*d + 56*a^3*b^5*c^7)*x^6 + 7/5*(35*a^8*c^3*d^4 + 280*a^7*b*c^4*d^3 + 588*a^6*b^2*c^5*d^2 + 392*a^5*b^3*c^6*d + 70*a^4*b^4*c^7)*x^5 + 7/4*(35*a^8*c^4*d^3 + 168*a^7*b*c^5*d^2 + 196*a^6*b^2*c^6*d + 56*a^5*b^3*c^7)*x^4 + 7/3*(21*a^8*c^5*d^2 + 56*a^7*b*c^6*d + 28*a^6*b^2*c^7)*x^3 + 7/2*(7*a^8*c^6*d + 8*a^7*b*c^7)*x^2 + a^8*c^7*x

$$\begin{aligned} &^4 + 168a^3b^5c^2d^5 + 70a^4b^4c^3d^6 + 8a^5b^3c^4d^7)x^{11} + 7/10*(b \\ &^8c^6d + 24a^2b^7c^5d^2 + 140a^2b^6c^4d^3 + 280a^3b^5c^3d^4 + 2 \\ &10a^4b^4c^2d^5 + 56a^5b^3c^3d^6 + 4a^6b^2c^4d^7)x^{10} + 1/9*(b^8c^7 \\ &+ 56a^2b^7c^6d + 588a^2b^6c^5d^2 + 1960a^3b^5c^4d^3 + 2450a^4b^4 \\ &4c^3d^4 + 1176a^5b^3c^2d^5 + 196a^6b^2c^3d^6 + 8a^7b^1c^4d^7)x^9 + 1 \\ &/8*(8a^2b^7c^7 + 196a^2b^6c^6d + 1176a^3b^5c^5d^2 + 2450a^4b^4c \\ &^4d^3 + 1960a^5b^3c^3d^4 + 588a^6b^2c^2d^5 + 56a^7b^1c^1d^6 + a^8 \\ &d^7)x^8 + (4a^2b^6c^7 + 56a^3b^5c^6d + 210a^4b^4c^5d^2 + 280a^5 \\ &5b^3c^4d^3 + 140a^6b^2c^3d^4 + 24a^7b^1c^2d^5 + a^8c^1d^6)x^7 + 7 \\ &/6*(8a^3b^5c^7 + 70a^4b^4c^6d + 168a^5b^3c^5d^2 + 140a^6b^2c^4 \\ &4d^3 + 40a^7b^1c^3d^4 + 3a^8c^2d^5)x^6 + 7/5*(10a^4b^4c^7 + 56a^5 \\ &5b^3c^6d + 84a^6b^2c^5d^2 + 40a^7b^1c^4d^3 + 5a^8c^3d^4)x^5 + \\ &7/4*(8a^5b^3c^7 + 28a^6b^2c^6d + 24a^7b^1c^5d^2 + 5a^8c^4d^3)x \\ &^4 + 7/3*(4a^6b^2c^7 + 8a^7b^1c^6d + 3a^8c^5d^2)x^3 + 1/2*(8a^7b^1 \\ &c^7 + 7a^8c^6d)x^2 \end{aligned}$$

mupad [B] time = 0.36, size = 892, normalized size = 4.46

$$x^8 \left(\frac{a^8 d^7}{8} + 7a^7 b c d^6 + \frac{147 a^6 b^2 c^2 d^5}{2} + 245 a^5 b^3 c^3 d^4 + \frac{1225 a^4 b^4 c^4 d^3}{4} + 147 a^3 b^5 c^5 d^2 + \frac{49 a^2 b^6 c^6 d}{2} + a b^7 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^8*(c + d*x)^7, x)

[Out] $x^8*((a^8d^7)/8 + a^7b^7c^7 + (49a^2b^6c^6d)/2 + 147a^3b^5c^5d^2 + (1225a^4b^4c^4d^3)/4 + 245a^5b^3c^3d^4 + (147a^6b^2c^2d^5)/2 + 7a^7b^1c^1d^6) + x^9*((b^8c^7)/9 + (8a^7b^1d^7)/9 + (196a^6b^2c^6d^6)/9 + (196a^2b^6c^5d^2)/3 + (1960a^3b^5c^4d^3)/9 + (2450a^4b^4c^3d^4)/9 + (392a^5b^3c^2d^5)/3 + (56a^6b^2c^1d^6)/9) + x^5*(14a^4b^4c^7 + 7a^8c^3d^4 + (392a^5b^3c^6d)/5 + 56a^7b^1c^4d^3 + (588a^6b^2c^5d^2)/5) + x^12*((35a^4b^4d^7)/6 + (35b^8c^4d^3)/12 + (70a^2b^7c^3d^4)/3 + (98a^3b^5c^6d^6)/3 + 49a^2b^6c^2d^5) + x^6*((28a^3b^5c^7)/3 + (7a^8c^2d^5)/2 + (245a^4b^4c^6d)/3 + (140a^7b^1c^3d^4)/3 + 196a^5b^3c^5d^2 + (490a^6b^2c^4d^3)/3) + x^11*((56a^5b^3d^7)/11 + (21b^8c^5d^2)/11 + (280a^2b^7c^4d^3)/11 + (490a^4b^4c^6d^6)/11 + (980a^2b^6c^3d^4)/11 + (1176a^3b^5c^2d^5)/11) + x^7*(a^8c^1d^6 + 4a^2b^6c^7 + 56a^3b^5c^6d + 24a^7b^1c^2d^5 + 210a^4b^4c^5d^2 + 280a^5b^3c^4d^3 + 140a^6b^2c^3d^4) + x^10*((7b^8c^6d)/10 + (14a^6b^2d^7)/5 + (84a^2b^7c^5d^2)/5 + (196a^5b^3c^6d^6)/5 + 98a^2b^6c^4d^3 + 196a^3b^5c^3d^4 + 147a^4b^4c^2d^5) + a^8c^7*x + (b^8d^7*x^16)/16 + (7a^5c^4*x^4*(5a^3d^3 + 8b^3c^3 + 28a^2b^2c^2d + 24a^2b^1c^1d^2))/4 + (7b^5d^4*x^13*(8a^3d^3 + 5b^3c^3 + 24a^2b^2c^2d + 28a^1b^1c^1d^2))/13 + (a^7c^6*x^2*(7a^1d + 8b^1c))/2 + (b^7d^6*x^15*(8a^1d + 7b^1c))/15 + (7a^6c^5*x^3*(3a^2d^2 + 4b^2c^2 + 8a^1b^1c^1d))/3 + (b^6d^5*x^14*(4a^2d^2 + 3b^2c^2 + 8a^1b^1c^1d))/2$

3.1275 $\int (a + bx)^7 (c + dx)^7 dx$

Optimal. Leaf size=200

$$\frac{d^6(a + bx)^{14}(bc - ad)}{2b^8} + \frac{21d^5(a + bx)^{13}(bc - ad)^2}{13b^8} + \frac{35d^4(a + bx)^{12}(bc - ad)^3}{12b^8} + \frac{35d^3(a + bx)^{11}(bc - ad)^4}{11b^8} + \frac{21d^2(a + bx)^{10}(bc - ad)^5}{10b^8} + \frac{7d(a + bx)^9(bc - ad)^6}{8b^8} + \frac{(a + bx)^8(bc - ad)^7}{b^8}$$

[Out] $\frac{1}{8}(-a*d+b*c)^7*(b*x+a)^8/b^8+7/9*d*(-a*d+b*c)^6*(b*x+a)^9/b^8+21/10*d^2*(-a*d+b*c)^5*(b*x+a)^10/b^8+35/11*d^3*(-a*d+b*c)^4*(b*x+a)^11/b^8+35/12*d^4*(-a*d+b*c)^3*(b*x+a)^12/b^8+21/13*d^5*(-a*d+b*c)^2*(b*x+a)^13/b^8+1/2*d^6*(-a*d+b*c)*(b*x+a)^14/b^8+1/15*d^7*(b*x+a)^15/b^8$

Rubi [A] time = 0.45, antiderivative size = 200, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{d^6(a + bx)^{14}(bc - ad)}{2b^8} + \frac{21d^5(a + bx)^{13}(bc - ad)^2}{13b^8} + \frac{35d^4(a + bx)^{12}(bc - ad)^3}{12b^8} + \frac{35d^3(a + bx)^{11}(bc - ad)^4}{11b^8} + \frac{21d^2(a + bx)^{10}(bc - ad)^5}{10b^8} + \frac{7d(a + bx)^9(bc - ad)^6}{8b^8} + \frac{(a + bx)^8(bc - ad)^7}{b^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7*(c + d*x)^7, x]

[Out] $((b*c - a*d)^7*(a + b*x)^8)/(8*b^8) + (7*d*(b*c - a*d)^6*(a + b*x)^9)/(9*b^8) + (21*d^2*(b*c - a*d)^5*(a + b*x)^{10})/(10*b^8) + (35*d^3*(b*c - a*d)^4*(a + b*x)^{11})/(11*b^8) + (35*d^4*(b*c - a*d)^3*(a + b*x)^{12})/(12*b^8) + (21*d^5*(b*c - a*d)^2*(a + b*x)^{13})/(13*b^8) + (d^6*(b*c - a*d)*(a + b*x)^{14})/(14*b^8) + (d^7*(a + b*x)^{15})/(15*b^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int (a + bx)^7 (c + dx)^7 dx = \int \left(\frac{(bc - ad)^7 (a + bx)^7}{b^7} + \frac{7d(bc - ad)^6 (a + bx)^8}{b^7} + \frac{21d^2(bc - ad)^5 (a + bx)^9}{b^7} + \frac{35d^3(bc - ad)^4 (a + bx)^{10}}{b^7} + \frac{35d^4(bc - ad)^3 (a + bx)^{11}}{b^7} + \frac{21d^5(bc - ad)^2 (a + bx)^{12}}{b^7} + \frac{7d^6(bc - ad) (a + bx)^{13}}{b^7} + \frac{d^7 (a + bx)^{14}}{b^7} \right) dx$$

$$= \frac{(bc - ad)^7 (a + bx)^8}{8b^8} + \frac{7d(bc - ad)^6 (a + bx)^9}{9b^8} + \frac{21d^2(bc - ad)^5 (a + bx)^{10}}{10b^8} + \frac{35d^3(bc - ad)^4 (a + bx)^{11}}{11b^8} + \frac{35d^4(bc - ad)^3 (a + bx)^{12}}{12b^8} + \frac{21d^5(bc - ad)^2 (a + bx)^{13}}{13b^8} + \frac{7d^6(bc - ad) (a + bx)^{14}}{14b^8} + \frac{d^7 (a + bx)^{15}}{15b^8}$$

Mathematica [B] time = 0.09, size = 785, normalized size = 3.92

$$a^7c^7x + \frac{7}{2}a^6c^6x^2(ad+bc) + \frac{7}{13}b^5d^5x^{13}(3a^2d^2 + 7abcd + 3b^2c^2) + \frac{7}{3}a^5c^5x^3(3a^2d^2 + 7abcd + 3b^2c^2) + \frac{7}{12}b^4d^4x^{12}(5a$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7*(c + d*x)^7,x]

[Out] $a^7c^7x + (7a^6c^6(b*c + a*d)*x^2)/2 + (7a^5c^5(3b^2c^2 + 7a*b*c*d + 3a^2d^2)*x^3)/3 + (7a^4c^4(5b^3c^3 + 21a*b^2c^2d + 21a^2b*c*d^2 + 5a^3d^3)*x^4)/4 + (7a^3c^3(5b^4c^4 + 35a*b^3c^3d + 63a^2*b^2c^2d^2 + 35a^3b*c*d^3 + 5a^4d^4)*x^5)/5 + (7a^2c^2(3b^5c^5 + 35a*b^4c^4d + 105a^2b^3c^3d^2 + 105a^3b^2c^2d^3 + 35a^4b*c*d^4 + 3a^5d^5)*x^6)/6 + a*c*(b^6c^6 + 21a*b^5c^5d + 105a^2b^4c^4d^2 + 175a^3b^3c^3d^3 + 105a^4b^2c^2d^4 + 21a^5b*c*d^5 + a^6d^6)*x^7 + ((b^7c^7 + 49a*b^6c^6d + 441a^2b^5c^5d^2 + 1225a^3b^4c^4d^3 + 1225a^4b^3c^3d^4 + 441a^5b^2c^2d^5 + 49a^6b*c*d^6 + a^7d^7)*x^8)/8 + (7b*d*(b^6c^6 + 21a*b^5c^5d + 105a^2b^4c^4d^2 + 175a^3b^3c^3d^3 + 105a^4b^2c^2d^4 + 21a^5b*c*d^5 + a^6d^6)*x^9)/9 + (7b^2*d^2*(3b^5c^5 + 35a*b^4c^4d + 105a^2b^3c^3d^2 + 105a^3b^2c^2d^3 + 35a^4b*c*d^4 + 3a^5d^5)*x^10)/10 + (7b^3*d^3*(5b^4c^4 + 35a*b^3c^3d + 63a^2b^2c^2d^2 + 35a^3b*c*d^3 + 5a^4d^4)*x^11)/11 + (7b^4*d^4*(5b^3c^3 + 21a*b^2c^2d + 21a^2b*c*d^2 + 5a^3d^3)*x^12)/12 + (7b^5*d^5*(3b^2c^2 + 7a*b*c*d + 3a^2d^2)*x^13)/13 + (b^6*d^6*(b*c + a*d)*x^14)/2 + (b^7*d^7*x^15)/15$

fricas [B] time = 0.37, size = 924, normalized size = 4.62

$$\frac{1}{15}x^{15}d^7b^7 + \frac{1}{2}x^{14}d^6cb^7 + \frac{1}{2}x^{14}d^7b^6a + \frac{21}{13}x^{13}d^5c^2b^7 + \frac{49}{13}x^{13}d^6cb^6a + \frac{21}{13}x^{13}d^7b^5a^2 + \frac{35}{12}x^{12}d^4c^3b^7 + \frac{49}{4}x^{12}d^5c^2b^6a + \frac{49}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7*(d*x+c)^7,x, algorithm="fricas")

[Out] $1/15*x^{15}d^7b^7 + 1/2*x^{14}d^6c*b^7 + 1/2*x^{14}d^7b^6*a + 21/13*x^{13}d^5c^2*b^7 + 49/13*x^{13}d^6c*b^6*a + 21/13*x^{13}d^7b^5*a^2 + 35/12*x^{12}d^4c^3*b^7 + 49/4*x^{12}d^5c^2*b^6*a + 49/4*x^{12}d^6c*b^5*a^2 + 35/12*x^{12}d^7b^4*a^3 + 35/11*x^{11}d^3c^4*b^7 + 245/11*x^{11}d^4c^3*b^6*a + 441/11*x^{11}d^5c^2*b^5*a^2 + 245/11*x^{11}d^6c*b^4*a^3 + 35/11*x^{11}d^7b^3*a^4 + 21/10*x^{10}d^2c^5*b^7 + 49/2*x^{10}d^3c^4*b^6*a + 147/2*x^{10}d^4c^3*b^5*a^2 + 147/2*x^{10}d^5c^2*b^4*a^3 + 49/2*x^{10}d^6c*b^3*a^4 + 21/10*x^{10}d^7b^2*a^5 + 7/9*x^9*d*c^6*b^7 + 49/3*x^9*d^2c^5*b^6*a + 245/3*x^9*d^3c^4*b^5*a^2 + 1225/9*x^9*d^4c^3*b^4*a^3 + 245/3*x^9*d^5c^2*b^3*a^4 + 49/3*x^9*d^6c*b^2*a^5 + 7/9*x^9*d^7b*a^6 + 1/8*x^8*c^7*b^7 + 49/8*x^8*d*c^6*b^6*a + 441/8*x^8*d^2c^5*b^5*a^2 + 1225/8*x^8*d^3c^4*b^4*a^3 + 1225/8*x^8*d^4c^3$

$$3b^3a^4 + 441/8x^8d^5c^2b^2a^5 + 49/8x^8d^6c^2b^2a^6 + 1/8x^8d^7a^7 + x^7c^7b^6a + 21x^7d^6c^6b^5a^2 + 105x^7d^2c^5b^4a^3 + 175x^7d^3c^4b^3a^4 + 105x^7d^4c^3b^2a^5 + 21x^7d^5c^2b^2a^6 + x^7d^6c^2a^7 + 7/2x^6c^7b^5a^2 + 245/6x^6d^6c^6b^4a^3 + 245/2x^6d^2c^5b^3a^4 + 245/2x^6d^3c^4b^2a^5 + 245/6x^6d^4c^3b^2a^6 + 7/2x^6d^5c^2a^7 + 7x^5c^7b^4a^3 + 49x^5d^6c^6b^3a^4 + 441/5x^5d^2c^5b^2a^5 + 49x^5d^3c^4b^2a^6 + 7x^5d^4c^3a^7 + 35/4x^4c^7b^3a^4 + 147/4x^4d^6c^6b^2a^5 + 147/4x^4d^2c^5b^2a^6 + 35/4x^4d^3c^4a^7 + 7x^3c^7b^2a^5 + 49/3x^3d^6c^6b^2a^6 + 7x^3d^2c^5a^7 + 7/2x^2c^7b^2a^6 + 7/2x^2d^6c^6a^7 + xc^7a^7$$

giac [B] time = 1.01, size = 924, normalized size = 4.62

$$\frac{1}{15} b^7 d^7 x^{15} + \frac{1}{2} b^7 c d^6 x^{14} + \frac{1}{2} a b^6 d^7 x^{14} + \frac{21}{13} b^7 c^2 d^5 x^{13} + \frac{49}{13} a b^6 c d^6 x^{13} + \frac{21}{13} a^2 b^5 d^7 x^{13} + \frac{35}{12} b^7 c^3 d^4 x^{12} + \frac{49}{4} a b^6 c^2 d^5 x^{12} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7*(d*x+c)^7,x, algorithm="giac")

[Out] $\frac{1}{15} b^7 d^7 x^{15} + \frac{1}{2} b^7 c d^6 x^{14} + \frac{1}{2} a b^6 d^7 x^{14} + \frac{21}{13} b^7 c^2 d^5 x^{13} + \frac{49}{13} a b^6 c d^6 x^{13} + \frac{21}{13} a^2 b^5 d^7 x^{13} + \frac{35}{12} b^7 c^3 d^4 x^{12} + \frac{49}{4} a b^6 c^2 d^5 x^{12} + \frac{49}{4} a^2 b^5 c d^6 x^{12} + \frac{35}{12} a^3 b^4 d^7 x^{12} + \frac{35}{11} b^7 c^4 d^3 x^{11} + \frac{245}{11} a b^6 c^3 d^4 x^{11} + \frac{441}{11} a^2 b^5 c^2 d^5 x^{11} + \frac{245}{11} a^3 b^4 c d^6 x^{11} + \frac{35}{11} a^4 b^3 d^7 x^{11} + \frac{21}{10} b^7 c^5 d^2 x^{10} + \frac{49}{2} a b^6 c^4 d^3 x^{10} + \frac{147}{2} a^2 b^5 c^3 d^4 x^{10} + \frac{147}{2} a^3 b^4 c^2 d^5 x^{10} + \frac{49}{2} a^4 b^3 c d^6 x^{10} + \frac{21}{10} a^5 b^2 d^7 x^{10} + \frac{7}{9} b^7 c^6 d^2 x^9 + \frac{49}{3} a b^6 c^5 d^2 x^9 + \frac{245}{3} a^2 b^5 c^4 d^3 x^9 + \frac{1225}{9} a^3 b^4 c^3 d^4 x^9 + \frac{245}{3} a^4 b^3 c^2 d^5 x^9 + \frac{49}{3} a^5 b^2 c d^6 x^9 + \frac{7}{9} a^6 b^2 c^2 d^5 x^9 + \frac{1}{8} b^7 c^7 x^8 + \frac{49}{8} a b^6 c^6 d^2 x^8 + \frac{441}{8} a^2 b^5 c^5 d^2 x^8 + \frac{1225}{8} a^3 b^4 c^4 d^3 x^8 + \frac{1225}{8} a^4 b^3 c^3 d^4 x^8 + \frac{441}{8} a^5 b^2 c^2 d^5 x^8 + \frac{49}{8} a^6 b^2 c^2 d^5 x^8 + \frac{1}{8} a^7 d^7 x^8 + a b^6 c^7 x^7 + \frac{21}{8} a^2 b^5 c^6 d^2 x^7 + \frac{105}{8} a^3 b^4 c^5 d^2 x^7 + \frac{175}{8} a^4 b^3 c^4 d^3 x^7 + \frac{105}{8} a^5 b^2 c^3 d^4 x^7 + \frac{21}{8} a^6 b^2 c^2 d^5 x^7 + a^7 c^6 d^6 x^7 + \frac{7}{2} a^2 b^5 c^7 x^6 + \frac{245}{6} a^3 b^4 c^6 d^2 x^6 + \frac{245}{2} a^4 b^3 c^5 d^2 x^6 + \frac{245}{2} a^5 b^2 c^4 d^3 x^6 + \frac{245}{6} a^6 b^2 c^3 d^4 x^6 + \frac{7}{2} a^7 c^2 d^5 x^6 + 7 a^3 b^4 c^7 x^5 + 49 a^4 b^3 c^6 d^2 x^5 + \frac{441}{5} a^5 b^2 c^5 d^2 x^5 + 49 a^6 b^2 c^4 d^3 x^5 + 7 a^7 c^3 d^4 x^5 + \frac{35}{4} a^4 b^3 c^7 x^4 + \frac{147}{4} a^5 b^2 c^6 d^2 x^4 + \frac{147}{4} a^6 b^2 c^5 d^2 x^4 + \frac{35}{4} a^7 c^4 d^3 x^4 + 7 a^5 b^2 c^7 x^3 + \frac{49}{3} a^6 b^2 c^6 d^2 x^3 + 7 a^7 c^5 d^2 x^3 + \frac{7}{2} a^6 b^2 c^7 x^2 + \frac{7}{2} a^7 c^6 d^2 x^2 + a^7 c^7 x$

maple [B] time = 0.00, size = 817, normalized size = 4.08

$$\frac{b^7 d^7 x^{15}}{15} + a^7 c^7 x + \frac{(7a b^6 d^7 + 7b^7 c d^6) x^{14}}{14} + \frac{(21a^2 b^5 d^7 + 49a b^6 c d^6 + 21b^7 c^2 d^5) x^{13}}{13} + \frac{(35a^3 b^4 d^7 + 147a^2 b^5 c d^6 + 147a b^6 c^2 d^5) x^{12}}{12} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x+a)^7*(d*x+c)^7, x)$

[Out] $\frac{1}{15}b^7d^7x^{15} + \frac{1}{14}(7a^7b^6d^7 + 7b^7c^6d^6)x^{14} + \frac{1}{13}(21a^2b^5d^7 + 49a^6b^6c^2d^6 + 21b^7c^2d^5)x^{13} + \frac{1}{12}(35a^3b^4d^7 + 147a^2b^5c^2d^6 + 147a^6b^6c^2d^5 + 35b^7c^3d^4)x^{12} + \frac{1}{11}(35a^4b^3d^7 + 245a^3b^4c^2d^6 + 441a^2b^5c^2d^5 + 245a^6b^6c^3d^4 + 35b^7c^4d^3)x^{11} + \frac{1}{10}(21a^5b^2d^7 + 245a^4b^3c^2d^6 + 735a^3b^4c^2d^5 + 735a^2b^5c^3d^4 + 245a^6b^6c^4d^3 + 21b^7c^5d^2)x^{10} + \frac{1}{9}(7a^6b^2d^7 + 147a^5b^2c^2d^6 + 735a^4b^3c^2d^5 + 1225a^3b^4c^3d^4 + 735a^2b^5c^4d^3 + 147a^6b^6c^5d^2 + 7b^7c^6d)x^{9} + \frac{1}{8}(a^7d^7 + 49a^6b^6c^2d^6 + 441a^5b^2c^2d^5 + 1225a^4b^3c^3d^4 + 1225a^3b^4c^4d^3 + 441a^2b^5c^5d^2 + 49a^6b^6c^6d + b^7c^7)x^{8} + \frac{1}{7}(7a^7c^2d^6 + 147a^6b^6c^2d^5 + 735a^5b^2c^3d^4 + 1225a^4b^3c^4d^3 + 735a^3b^4c^5d^2 + 147a^2b^5c^6d + 7a^6b^6c^7)x^{7} + \frac{1}{6}(21a^7c^2d^5 + 245a^6b^6c^3d^4 + 735a^5b^2c^4d^3 + 735a^4b^3c^5d^2 + 245a^3b^4c^6d + 21a^2b^5c^7)x^{6} + \frac{1}{5}(35a^7c^3d^4 + 245a^6b^6c^4d^3 + 441a^5b^2c^5d^2 + 245a^4b^3c^6d + 35a^3b^4c^7)x^{5} + \frac{1}{4}(35a^7c^4d^3 + 147a^6b^6c^5d^2 + 147a^5b^2c^6d + 35a^4b^3c^7)x^{4} + \frac{1}{3}(21a^7c^5d^2 + 49a^6b^6c^6d + 21a^5b^2c^7)x^{3} + \frac{1}{2}(7a^7c^6d + 7a^6b^6c^7)x^2 + a^7c^7x$

maxima [B] time = 1.33, size = 807, normalized size = 4.04

$$\frac{1}{15} b^7 d^7 x^{15} + a^7 c^7 x + \frac{1}{2} (b^7 c d^6 + a b^6 d^7) x^{14} + \frac{7}{13} (3 b^7 c^2 d^5 + 7 a b^6 c d^6 + 3 a^2 b^5 d^7) x^{13} + \frac{7}{12} (5 b^7 c^3 d^4 + 21 a b^6 c^2 d^5 + \dots)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)^7*(d*x+c)^7, x, \text{algorithm}="maxima")$

[Out] $\frac{1}{15}b^7d^7x^{15} + a^7c^7x + \frac{1}{2}(b^7c^2d^6 + a^6b^6d^7)x^{14} + \frac{7}{13}(3b^7c^2d^5 + 7a^6b^6c^2d^6 + 3a^2b^5d^7)x^{13} + \frac{7}{12}(5b^7c^3d^4 + 21a^6b^6c^2d^5 + 21a^2b^5c^2d^6 + 5a^3b^4d^7)x^{12} + \frac{7}{11}(5b^7c^4d^3 + 35a^6b^6c^3d^4 + 63a^2b^5c^2d^5 + 35a^3b^4c^2d^6 + 5a^4b^3d^7)x^{11} + \frac{7}{10}(3b^7c^5d^2 + 35a^6b^6c^4d^3 + 105a^2b^5c^3d^4 + 105a^3b^4c^2d^5 + 35a^4b^3c^2d^6 + 3a^5b^2d^7)x^{10} + \frac{7}{9}(b^7c^6d + 21a^6b^6c^5d^2 + 105a^2b^5c^4d^3 + 175a^3b^4c^3d^4 + 105a^4b^3c^2d^5 + 21a^5b^2c^2d^6 + a^6b^6d^7)x^{9} + \frac{1}{8}(b^7c^7 + 49a^6b^6c^6d + 441a^2b^5c^5d^2 + 1225a^3b^4c^4d^3 + 1225a^4b^3c^3d^4 + 441a^5b^2c^2d^5 + 49a^6b^6c^6d + a^7d^7)x^{8} + (a^6b^6c^7 + 21a^2b^5c^6d + 105a^3b^4c^5d^2 + 175a^4b^3c^4d^3 + 105a^5b^2c^3d^4 + 21a^6b^6c^2d^5 + a^7c^6d)x^{7} + \frac{7}{6}(3a^2b^5c^7 + 35a^3b^4c^6d + 105a^4b^3c^5d^2 + 105a^5b^2c^4d^3 + 35a^6b^6c^3d^4 + 3a^7c^2d^5)x^{6} + \frac{7}{5}(5a^3b^4c^7 + 35a^4b^3c^6d + 63a^5b^2c^5d^2 + 35a^6b^6c^4d^3 + 5a^7c^3d^4)x^{5} + \frac{7}{4}(5a^4b^3c^7 + 21a^5b^2c^6d + 21a^6b^6c^5d^2 + 5a^7c^4d^3)x^{4} + \frac{7}{3}(3a^5b^2c^7 + 7a^6b^6c^6d + 3a^7c^5d^2)x^{3} + \frac{7}{2}(a^6b^6c^7 + a^7c^6d)x^2$

mupad [B] time = 0.40, size = 781, normalized size = 3.90

$$x^8 \left(\frac{a^7 d^7}{8} + \frac{49 a^6 b c d^6}{8} + \frac{441 a^5 b^2 c^2 d^5}{8} + \frac{1225 a^4 b^3 c^3 d^4}{8} + \frac{1225 a^3 b^4 c^4 d^3}{8} + \frac{441 a^2 b^5 c^5 d^2}{8} + \frac{49 a b^6 c^6 d}{8} + \frac{b^7 d^7}{8} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^7*(c + d*x)^7,x)

[Out] $x^8 \left(\frac{a^7 d^7}{8} + \frac{b^7 c^7}{8} + \frac{441 a^2 b^5 c^5 d^2}{8} + \frac{1225 a^3 b^4 c^4 d^3}{8} + \frac{1225 a^4 b^3 c^3 d^4}{8} + \frac{441 a^5 b^2 c^2 d^5}{8} + \frac{49 a^6 b c^6 d}{8} + \frac{49 a^7 b^6 c^6 d}{8} + \frac{49 a^6 b^2 c^6 d}{8} + \frac{49 a^6 b^3 c^4 d^3}{8} + \frac{441 a^5 b^2 c^5 d^2}{5} + x^{11} \left(\frac{35 a^4 b^3 d^7}{11} + \frac{35 b^7 c^4 d^3}{11} + \frac{245 a^2 b^6 c^3 d^4}{11} + \frac{245 a^3 b^4 c^6 d}{11} + \frac{441 a^2 b^5 c^2 d^5}{11} \right) + x^7 (a^6 b^6 c^7 + a^7 c^6 d^6 + 21 a^2 b^5 c^6 d + 21 a^6 b^2 c^2 d^5 + 105 a^3 b^4 c^5 d^2 + 175 a^4 b^3 c^4 d^3 + 105 a^5 b^2 c^3 d^4) + x^9 \left(\frac{7 a^6 b^6 d^7}{9} + \frac{7 b^7 c^6 d}{9} + \frac{49 a^2 b^6 c^5 d^2}{3} + \frac{49 a^5 b^2 c^6 d}{3} + \frac{245 a^2 b^5 c^4 d^3}{3} + \frac{1225 a^3 b^4 c^3 d^4}{9} + \frac{245 a^4 b^3 c^2 d^5}{3} \right) + x^6 \left(\frac{7 a^2 b^5 c^7}{2} + \frac{7 a^7 c^2 d^5}{2} + \frac{245 a^3 b^4 c^6 d}{6} + \frac{245 a^6 b^2 c^3 d^4}{6} + \frac{245 a^4 b^3 c^5 d^2}{2} + \frac{245 a^5 b^2 c^4 d^3}{2} \right) + x^{10} \left(\frac{21 a^5 b^2 d^7}{10} + \frac{21 b^7 c^5 d^2}{10} + \frac{49 a^2 b^6 c^4 d^3}{2} + \frac{49 a^4 b^3 c^6 d}{2} + \frac{147 a^2 b^5 c^3 d^4}{2} + \frac{147 a^3 b^4 c^2 d^5}{2} \right) + a^7 c^7 x + \frac{b^7 d^7 x^{15}}{15} + \frac{7 a^4 c^4 x^4 (5 a^3 d^3 + 5 b^3 c^3 + 21 a^2 b^2 c^2 d + 21 a^2 b^2 c^2 d)}{4} + \frac{7 b^4 d^4 x^{12} (5 a^3 d^3 + 5 b^3 c^3 + 21 a^2 b^2 c^2 d + 21 a^2 b^2 c^2 d)}{12} + \frac{7 a^6 c^6 x^2 (a d + b c)}{2} + \frac{b^6 d^6 x^{14} (a d + b c)}{2} + \frac{7 a^5 c^5 x^3 (3 a^2 d^2 + 3 b^2 c^2 + 7 a b c d)}{3} + \frac{7 b^5 d^5 x^{13} (3 a^2 d^2 + 3 b^2 c^2 + 7 a b c d)}{13}$

sympy [B] time = 0.19, size = 935, normalized size = 4.68

$$a^7 c^7 x + \frac{b^7 d^7 x^{15}}{15} + x^{14} \left(\frac{a b^6 d^7}{2} + \frac{b^7 c d^6}{2} \right) + x^{13} \left(\frac{21 a^2 b^5 d^7}{13} + \frac{49 a b^6 c d^6}{13} + \frac{21 b^7 c^2 d^5}{13} \right) + x^{12} \left(\frac{35 a^3 b^4 d^7}{12} + \frac{49 a^2 b^5 c d^6}{4} + \frac{49 a^7 c^6 d^6}{4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**7*(d*x+c)**7,x)

[Out] $a^7 c^7 x + b^7 d^7 x^{15}/15 + x^{14} (a^6 b^6 d^7/2 + b^7 c^6 d^6/2) + x^{13} (21 a^2 b^5 d^7/13 + 49 a^2 b^6 c^6 d^6/13 + 21 b^7 c^2 d^5/13) + x^{12} (35 a^3 b^4 d^7/12 + 49 a^2 b^5 c^6 d^6/4 + 49 a^7 b^6 c^6 d^6/4 + 35 b^7 c^2 d^5/12) + x^{11} (35 a^4 b^3 d^7/11 + 245 a^2 b^6 c^3 d^4/11 + 441 a^2 b^5 c^2 d^5/11 + 245 a^3 b^4 c^6 d/11 + 35 b^7 c^4 d^3/11) + x^{10} (21 a^5 b^2 d^7/10 + 49 a^4 b^3 c^6 d/2 + 147 a^2 b^5 c^3 d^4/2 + 147 a^3 b^4 c^2 d^5/2 + 49 a^2 b^6 c^5 d^2/2 + 49 a^5 b^2 c^4 d^3/2 + 21 a^6 b^2 c^3 d^4/2)$

$$\begin{aligned}
& b^{**7}c^{**5}d^{**2}/10) + x^{**9}(7a^{**6}b^{**d}^{**7}/9 + 49a^{**5}b^{**2}c^{**d}^{**6}/3 + 245a^{**4}b^{**3}c^{**2}d^{**5}/3 + 1225a^{**3}b^{**4}c^{**3}d^{**4}/9 + 245a^{**2}b^{**5}c^{**4}d^{**3}/3 + 49ab^{**6}c^{**5}d^{**2}/3 + 7b^{**7}c^{**6}d/9) + x^{**8}(a^{**7}d^{**7}/8 + 49a^{**6}b^{**c}d^{**6}/8 + 441a^{**5}b^{**2}c^{**2}d^{**5}/8 + 1225a^{**4}b^{**3}c^{**3}d^{**4}/8 + 1225a^{**3}b^{**4}c^{**4}d^{**3}/8 + 441a^{**2}b^{**5}c^{**5}d^{**2}/8 + 49ab^{**6}c^{**6}d/8 + b^{**7}c^{**7}/8) + x^{**7}(a^{**7}c^{**d}^{**6} + 21a^{**6}b^{**c}^{**2}d^{**5} + 105a^{**5}b^{**2}c^{**3}d^{**4} + 175a^{**4}b^{**3}c^{**4}d^{**3} + 105a^{**3}b^{**4}c^{**5}d^{**2} + 21a^{**2}b^{**5}c^{**6}d + ab^{**6}c^{**7}) + x^{**6}(7a^{**7}c^{**2}d^{**5}/2 + 245a^{**6}b^{**c}^{**3}d^{**4}/6 + 245a^{**5}b^{**2}c^{**4}d^{**3}/2 + 245a^{**4}b^{**3}c^{**5}d^{**2}/2 + 245a^{**3}b^{**4}c^{**6}d/6 + 7a^{**2}b^{**5}c^{**7}/2) + x^{**5}(7a^{**7}c^{**3}d^{**4} + 49a^{**6}b^{**c}^{**4}d^{**3} + 441a^{**5}b^{**2}c^{**5}d^{**2}/5 + 49a^{**4}b^{**3}c^{**6}d + 7a^{**3}b^{**4}c^{**7}) + x^{**4}(35a^{**7}c^{**4}d^{**3}/4 + 147a^{**6}b^{**c}^{**5}d^{**2}/4 + 147a^{**5}b^{**2}c^{**6}d/4 + 35a^{**4}b^{**3}c^{**7}/4) + x^{**3}(7a^{**7}c^{**5}d^{**2} + 49a^{**6}b^{**c}^{**6}d/3 + 7a^{**5}b^{**2}c^{**7}) + x^{**2}(7a^{**7}c^{**6}d/2 + 7a^{**6}b^{**c}^{**7}/2)
\end{aligned}$$

3.1276 $\int (a + bx)^6 (c + dx)^7 dx$

Optimal. Leaf size=173

$$-\frac{6b^5(c+dx)^{13}(bc-ad)}{13d^7} + \frac{5b^4(c+dx)^{12}(bc-ad)^2}{4d^7} - \frac{20b^3(c+dx)^{11}(bc-ad)^3}{11d^7} + \frac{3b^2(c+dx)^{10}(bc-ad)^4}{2d^7} - \frac{2b(c+dx)^9}{3d^7} + \frac{c^8}{8d^7}$$

[Out] $1/8*(-a*d+b*c)^6*(d*x+c)^8/d^7-2/3*b*(-a*d+b*c)^5*(d*x+c)^9/d^7+3/2*b^2*(-a*d+b*c)^4*(d*x+c)^{10}/d^7-20/11*b^3*(-a*d+b*c)^3*(d*x+c)^{11}/d^7+5/4*b^4*(-a*d+b*c)^2*(d*x+c)^{12}/d^7-6/13*b^5*(-a*d+b*c)*(d*x+c)^{13}/d^7+1/14*b^6*(d*x+c)^{14}/d^7$

Rubi [A] time = 0.43, antiderivative size = 173, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{6b^5(c+dx)^{13}(bc-ad)}{13d^7} + \frac{5b^4(c+dx)^{12}(bc-ad)^2}{4d^7} - \frac{20b^3(c+dx)^{11}(bc-ad)^3}{11d^7} + \frac{3b^2(c+dx)^{10}(bc-ad)^4}{2d^7} - \frac{2b(c+dx)^9}{3d^7} + \frac{c^8}{8d^7}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^6*(c + d*x)^7, x]

[Out] $((b*c - a*d)^6*(c + d*x)^8)/(8*d^7) - (2*b*(b*c - a*d)^5*(c + d*x)^9)/(3*d^7) + (3*b^2*(b*c - a*d)^4*(c + d*x)^{10})/(2*d^7) - (20*b^3*(b*c - a*d)^3*(c + d*x)^{11})/(11*d^7) + (5*b^4*(b*c - a*d)^2*(c + d*x)^{12})/(4*d^7) - (6*b^5*(b*c - a*d)*(c + d*x)^{13})/(13*d^7) + (b^6*(c + d*x)^{14})/(14*d^7)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int (a + bx)^6 (c + dx)^7 dx = \int \left(\frac{(-bc + ad)^6 (c + dx)^7}{d^6} - \frac{6b(bc - ad)^5 (c + dx)^8}{d^6} + \frac{15b^2(bc - ad)^4 (c + dx)^9}{d^6} - \frac{20b^3(bc - ad)^3 (c + dx)^{10}}{d^6} + \frac{(bc - ad)^6 (c + dx)^8}{8d^7} - \frac{2b(bc - ad)^5 (c + dx)^9}{3d^7} + \frac{3b^2(bc - ad)^4 (c + dx)^{10}}{2d^7} - \frac{20b^3(bc - ad)^3 (c + dx)^{11}}{11d^7} + \frac{5b^4(bc - ad)^2 (c + dx)^{12}}{4d^7} - \frac{6b^5(bc - ad) (c + dx)^{13}}{13d^7} + \frac{b^6 (c + dx)^{14}}{14d^7} \right) dx$$

Mathematica [B] time = 0.08, size = 684, normalized size = 3.95

$$a^6c^7x + \frac{1}{2}a^5c^6x^2(7ad+6bc) + \frac{1}{4}b^4d^5x^{12}(5a^2d^2 + 14abcd + 7b^2c^2) + a^4c^5x^3(7a^2d^2 + 14abcd + 5b^2c^2) + \frac{1}{11}b^3d^4x^{11} \left(2 \right)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^6*(c + d*x)^7,x]

[Out] $a^6c^7x + (a^5c^6(6bc + 7ad)x^2)/2 + a^4c^5(5b^2c^2 + 14abc*d + 7a^2d^2)x^3 + (a^3c^4(20b^3c^3 + 105ab^2c^2d + 126a^2b*c*d^2 + 35a^3d^3))x^4/4 + a^2c^3(3b^4c^4 + 28ab^3c^3d + 63a^2b^2*c^2d^2 + 42a^3b*c*d^3 + 7a^4d^4)x^5 + (a^2c^2(2b^5c^5 + 35ab^4c^4*d + 140a^2b^3c^3d^2 + 175a^3b^2c^2d^3 + 70a^4b*c*d^4 + 7a^5d^5))x^6/2 + (c(b^6c^6 + 42ab^5c^5d + 315a^2b^4c^4d^2 + 700a^3b^3c^3d^3 + 525a^4b^2c^2d^4 + 126a^5b*c*d^5 + 7a^6d^6))x^7/7 + (d(7b^6c^6 + 126ab^5c^5d + 525a^2b^4c^4d^2 + 700a^3b^3c^3d^3 + 315a^4b^2c^2d^4 + 42a^5b*c*d^5 + a^6d^6))x^8/8 + (b^2d^2(7b^5c^5 + 70ab^4c^4d + 175a^2b^3c^3d^2 + 140a^3b^2c^2d^3 + 35a^4b*c*d^4 + 2a^5d^5))x^9/3 + (b^2d^3(7b^4c^4 + 42ab^3c^3d + 63a^2b^2*c^2d^2 + 28a^3b*c*d^3 + 3a^4d^4))x^{10}/2 + (b^3d^4(35b^3c^3 + 126ab^2c^2d + 105a^2b*c*d^2 + 20a^3d^3))x^{11}/11 + (b^4d^5(7b^2c^2 + 14ab*c*d + 5a^2d^2))x^{12}/4 + (b^5d^6(7b*c + 6a*d))x^{13}/13 + (b^6d^7)x^{14}/14$

fricas [B] time = 0.40, size = 798, normalized size = 4.61

$$\frac{1}{14}x^{14}d^7b^6 + \frac{7}{13}x^{13}d^6cb^6 + \frac{6}{13}x^{13}d^7b^5a + \frac{7}{4}x^{12}d^5c^2b^6 + \frac{7}{2}x^{12}d^6cb^5a + \frac{5}{4}x^{12}d^7b^4a^2 + \frac{35}{11}x^{11}d^4c^3b^6 + \frac{126}{11}x^{11}d^5c^2b^5a + \frac{10}{11}x^{11}d^6cb^4a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6*(d*x+c)^7,x, algorithm="fricas")

[Out] $1/14*x^{14}*d^7*b^6 + 7/13*x^{13}*d^6*c*b^6 + 6/13*x^{13}*d^7*b^5*a + 7/4*x^{12}*d^5*c^2*b^6 + 7/2*x^{12}*d^6*c*b^5*a + 5/4*x^{12}*d^7*b^4*a^2 + 35/11*x^{11}*d^4*c^3*b^6 + 126/11*x^{11}*d^5*c^2*b^5*a + 105/11*x^{11}*d^6*c*b^4*a^2 + 20/11*x^{11}*d^7*b^3*a^3 + 7/2*x^{10}*d^3*c^4*b^6 + 21*x^{10}*d^4*c^3*b^5*a + 63/2*x^{10}*d^5*c^2*b^4*a^2 + 14*x^{10}*d^6*c*b^3*a^3 + 3/2*x^{10}*d^7*b^2*a^4 + 7/3*x^9*d^2*c^5*b^6 + 70/3*x^9*d^3*c^4*b^5*a + 175/3*x^9*d^4*c^3*b^4*a^2 + 140/3*x^9*d^5*c^2*b^3*a^3 + 35/3*x^9*d^6*c*b^2*a^4 + 2/3*x^9*d^7*b*a^5 + 7/8*x^8*d*c^6*b^6 + 63/4*x^8*d^2*c^5*b^5*a + 525/8*x^8*d^3*c^4*b^4*a^2 + 175/2*x^8*d^4*c^3*b^3*a^3 + 315/8*x^8*d^5*c^2*b^2*a^4 + 21/4*x^8*d^6*c*b*a^5 + 1/8*x^8*d^7*a^6 + 1/7*x^7*c^7*b^6 + 6*x^7*d*c^6*b^5*a + 45*x^7*d^2*c^5*b^4*a^2 + 100*x^7*d^3*c^4*b^3*a^3 + 75*x^7*d^4*c^3*b^2*a^4 + 18*x^7*d^5*c^2*b*a^5 + x^7*d^6*c*a^6 + x^6*c^7*b^5*a + 35/2*x^6*d*c^6*b^4*a^2 + 70*x^6*d^2*c^5*b^3*a^3 + 175/2*x^6*d^3*c^4*b^2*a^4 + 35*x^6*d^4*c^3*b*a^5 + 7/2*x^6*d^5*c^2*a^6 + 3*x^6*d^6*c*a^7$

$$5*c^7*b^4*a^2 + 28*x^5*d*c^6*b^3*a^3 + 63*x^5*d^2*c^5*b^2*a^4 + 42*x^5*d^3*c^4*b*a^5 + 7*x^5*d^4*c^3*a^6 + 5*x^4*c^7*b^3*a^3 + 105/4*x^4*d*c^6*b^2*a^4 + 63/2*x^4*d^2*c^5*b*a^5 + 35/4*x^4*d^3*c^4*a^6 + 5*x^3*c^7*b^2*a^4 + 14*x^3*d*c^6*b*a^5 + 7*x^3*d^2*c^5*a^6 + 3*x^2*c^7*b*a^5 + 7/2*x^2*d*c^6*a^6 + x*c^7*a^6$$

giac [B] time = 0.95, size = 798, normalized size = 4.61

$$\frac{1}{14} b^6 d^7 x^{14} + \frac{7}{13} b^6 c d^6 x^{13} + \frac{6}{13} a b^5 d^7 x^{13} + \frac{7}{4} b^6 c^2 d^5 x^{12} + \frac{7}{2} a b^5 c d^6 x^{12} + \frac{5}{4} a^2 b^4 d^7 x^{12} + \frac{35}{11} b^6 c^3 d^4 x^{11} + \frac{126}{11} a b^5 c^2 d^5 x^{11} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6*(d*x+c)^7,x, algorithm="giac")

[Out] 1/14*b^6*d^7*x^14 + 7/13*b^6*c*d^6*x^13 + 6/13*a*b^5*d^7*x^13 + 7/4*b^6*c^2*d^5*x^12 + 7/2*a*b^5*c*d^6*x^12 + 5/4*a^2*b^4*d^7*x^12 + 35/11*b^6*c^3*d^4*x^11 + 126/11*a*b^5*c^2*d^5*x^11 + 105/11*a^2*b^4*c*d^6*x^11 + 20/11*a^3*b^3*d^7*x^11 + 7/2*b^6*c^4*d^3*x^10 + 21*a*b^5*c^3*d^4*x^10 + 63/2*a^2*b^4*c^2*d^5*x^10 + 14*a^3*b^3*c*d^6*x^10 + 3/2*a^4*b^2*d^7*x^10 + 7/3*b^6*c^5*d^2*x^9 + 70/3*a*b^5*c^4*d^3*x^9 + 175/3*a^2*b^4*c^3*d^4*x^9 + 140/3*a^3*b^3*c^2*d^5*x^9 + 35/3*a^4*b^2*c*d^6*x^9 + 2/3*a^5*b*d^7*x^9 + 7/8*b^6*c^6*d*x^8 + 63/4*a*b^5*c^5*d^2*x^8 + 525/8*a^2*b^4*c^4*d^3*x^8 + 175/2*a^3*b^3*c^3*d^4*x^8 + 315/8*a^4*b^2*c^2*d^5*x^8 + 21/4*a^5*b*c*d^6*x^8 + 1/8*a^6*d^7*x^8 + 1/7*b^6*c^7*x^7 + 6*a*b^5*c^6*d*x^7 + 45*a^2*b^4*c^5*d^2*x^7 + 100*a^3*b^3*c^4*d^3*x^7 + 75*a^4*b^2*c^3*d^4*x^7 + 18*a^5*b*c^2*d^5*x^7 + a^6*c*d^6*x^7 + a*b^5*c^7*x^6 + 35/2*a^2*b^4*c^6*d*x^6 + 70*a^3*b^3*c^5*d^2*x^6 + 175/2*a^4*b^2*c^4*d^3*x^6 + 35*a^5*b*c^3*d^4*x^6 + 7/2*a^6*c^2*d^5*x^6 + 3*a^2*b^4*c^7*x^5 + 28*a^3*b^3*c^6*d*x^5 + 63*a^4*b^2*c^5*d^2*x^5 + 42*a^5*b*c^4*d^3*x^5 + 7*a^6*c^3*d^4*x^5 + 5*a^3*b^3*c^7*x^4 + 105/4*a^4*b^2*c^6*d*x^4 + 63/2*a^5*b*c^5*d^2*x^4 + 35/4*a^6*c^4*d^3*x^4 + 5*a^4*b^2*c^7*x^3 + 14*a^5*b*c^6*d*x^3 + 7*a^6*c^5*d^2*x^3 + 3*a^5*b*c^7*x^2 + 7/2*a^6*c^6*d*x^2 + a^6*c^7*x

maple [B] time = 0.00, size = 709, normalized size = 4.10

$$\frac{b^6 d^7 x^{14}}{14} + a^6 c^7 x + \frac{(6 a b^5 d^7 + 7 b^6 c d^6) x^{13}}{13} + \frac{(15 a^2 b^4 d^7 + 42 a b^5 c d^6 + 21 b^6 c^2 d^5) x^{12}}{12} + \frac{(20 a^3 b^3 d^7 + 105 a^2 b^4 c d^6 + 126 a b^5 c^2 d^5 + 35 b^6 c^3 d^4) x^{11}}{11} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^6*(d*x+c)^7,x)

[Out] 1/14*b^6*d^7*x^14+1/13*(6*a*b^5*d^7+7*b^6*c*d^6)*x^13+1/12*(15*a^2*b^4*d^7+42*a*b^5*c*d^6+21*b^6*c^2*d^5)*x^12+1/11*(20*a^3*b^3*d^7+105*a^2*b^4*c*d^6+126*a*b^5*c^2*d^5+35*b^6*c^3*d^4)*x^11+1/10*(15*a^4*b^2*d^7+140*a^3*b^3*c*d^6+70*a^2*b^4*c^2*d^5+35*a^3*b^3*c^2*d^4)*x^10+1/9*(15*a^5*b*c*d^6+105*a^4*b^2*c^2*d^5+35*a^5*b*c^2*d^4)*x^9+1/8*(15*a^6*c^2*d^5+35*a^5*b*c^3*d^4)*x^8+1/7*(15*a^6*c^3*d^4+35*a^5*b*c^4*d^3)*x^7+1/6*(15*a^6*c^4*d^3+35*a^5*b*c^5*d^2)*x^6+1/5*(15*a^6*c^5*d^2+35*a^5*b*c^6*d)*x^5+1/4*(15*a^6*c^6*d+35*a^5*b*c^7)*x^4+1/3*(15*a^6*c^7+35*a^5*b*c^8)*x^3+1/2*(15*a^6*c^8+35*a^5*b*c^9)*x^2+1/2*(15*a^6*c^9+35*a^5*b*c^10)*x+1/2*(15*a^6*c^10+35*a^5*b*c^11)*x^0

$$\begin{aligned} &^6+315a^2b^4c^2d^5+210a^3b^5c^3d^4+35b^6c^4d^3)*x^{10}+1/9*(6a^5b^* \\ &d^7+105a^4b^2c^2d^6+420a^3b^3c^2d^5+525a^2b^4c^3d^4+210a^3b^5c^4 \\ &*d^3+21b^6c^5d^2)*x^9+1/8*(a^6d^7+42a^5b^*c^2d^6+315a^4b^2c^2d^5+70 \\ &0a^3b^3c^3d^4+525a^2b^4c^4d^3+126a^3b^5c^5d^2+7b^6c^6d)*x^8+1/ \\ &7*(7a^6c^2d^6+126a^5b^*c^2d^5+525a^4b^2c^3d^4+700a^3b^3c^4d^3+31 \\ &5a^2b^4c^5d^2+42a^3b^5c^6d+b^6c^7)*x^7+1/6*(21a^6c^2d^5+210a^5b^* \\ &c^3d^4+525a^4b^2c^4d^3+420a^3b^3c^5d^2+105a^2b^4c^6d+6a^3b^5c^7)*x^6+1/5*(35a^6c^3d^4+210a^5b^*c^4d^3+315a^4b^2c^5d^2+140a^3b^3c^6d+15a^2b^4c^7)*x^5+1/4*(35a^6c^4d^3+126a^5b^*c^5d^2+105a^4b^2c^6d+20a^3b^3c^7)*x^4+1/3*(21a^6c^5d^2+42a^5b^*c^6d+15a^4b^2c^7)*x^3+1/2*(7a^6c^6d+6a^5b^*c^7)*x^2+a^6c^7*x \end{aligned}$$

maxima [B] time = 1.32, size = 706, normalized size = 4.08

$$\frac{1}{14} b^6 d^7 x^{14} + a^6 c^7 x + \frac{1}{13} (7 b^6 c d^6 + 6 a b^5 d^7) x^{13} + \frac{1}{4} (7 b^6 c^2 d^5 + 14 a b^5 c d^6 + 5 a^2 b^4 d^7) x^{12} + \frac{1}{11} (35 b^6 c^3 d^4 + 126 a b^5 c^2 d^5 + 105 a^2 b^4 c^3 d^6 + 20 a^3 b^3 c^4 d^7) x^{11} + \frac{1}{2} (7 b^6 c^4 d^3 + 42 a b^5 c^3 d^4 + 63 a^2 b^4 c^2 d^5 + 28 a^3 b^3 c^3 d^6 + 3 a^4 b^2 c^4 d^7) x^{10} + \frac{1}{3} (7 b^6 c^5 d^2 + 70 a b^5 c^4 d^3 + 175 a^2 b^4 c^3 d^4 + 140 a^3 b^3 c^2 d^5 + 35 a^4 b^2 c^3 d^6 + 2 a^5 b^1 c^4 d^7) x^9 + \frac{1}{8} (7 b^6 c^6 d + 126 a b^5 c^5 d^2 + 525 a^2 b^4 c^4 d^3 + 700 a^3 b^3 c^3 d^4 + 315 a^4 b^2 c^2 d^5 + 42 a^5 b^1 c^3 d^6 + a^6 c^4 d^7) x^8 + \frac{1}{7} (b^6 c^7 + 42 a b^5 c^6 d + 315 a^2 b^4 c^5 d^2 + 700 a^3 b^3 c^4 d^3 + 525 a^4 b^2 c^3 d^4 + 126 a^5 b^1 c^2 d^5 + 7 a^6 c^3 d^6) x^7 + \frac{1}{2} (2 a b^5 c^7 + 35 a^2 b^4 c^6 d + 140 a^3 b^3 c^5 d^2 + 175 a^4 b^2 c^4 d^3 + 70 a^5 b^1 c^3 d^4 + 7 a^6 c^2 d^5) x^6 + (3 a^2 b^4 c^7 + 28 a^3 b^3 c^6 d + 63 a^4 b^2 c^5 d^2 + 42 a^5 b^1 c^4 d^3 + 7 a^6 c^3 d^4) x^5 + \frac{1}{4} (20 a^3 b^3 c^7 + 105 a^4 b^2 c^6 d + 126 a^5 b^1 c^5 d^2 + 35 a^6 c^4 d^3) x^4 + (5 a^4 b^2 c^7 + 14 a^5 b^1 c^6 d + 7 a^6 c^5 d^2) x^3 + \frac{1}{2} (6 a^5 b^1 c^7 + 7 a^6 c^6 d) x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6*(d*x+c)^7,x, algorithm="maxima")

[Out] 1/14*b^6*d^7*x^14 + a^6*c^7*x + 1/13*(7*b^6*c*d^6 + 6*a*b^5*d^7)*x^13 + 1/4*(7*b^6*c^2*d^5 + 14*a*b^5*c*d^6 + 5*a^2*b^4*d^7)*x^12 + 1/11*(35*b^6*c^3*d^4 + 126*a*b^5*c^2*d^5 + 105*a^2*b^4*c*d^6 + 20*a^3*b^3*d^7)*x^11 + 1/2*(7*b^6*c^4*d^3 + 42*a*b^5*c^3*d^4 + 63*a^2*b^4*c^2*d^5 + 28*a^3*b^3*c*d^6 + 3*a^4*b^2*d^7)*x^10 + 1/3*(7*b^6*c^5*d^2 + 70*a*b^5*c^4*d^3 + 175*a^2*b^4*c^3*d^4 + 140*a^3*b^3*c^2*d^5 + 35*a^4*b^2*c*d^6 + 2*a^5*b*d^7)*x^9 + 1/8*(7*b^6*c^6*d + 126*a*b^5*c^5*d^2 + 525*a^2*b^4*c^4*d^3 + 700*a^3*b^3*c^3*d^4 + 315*a^4*b^2*c^2*d^5 + 42*a^5*b*c*d^6 + a^6*d^7)*x^8 + 1/7*(b^6*c^7 + 42*a*b^5*c^6*d + 315*a^2*b^4*c^5*d^2 + 700*a^3*b^3*c^4*d^3 + 525*a^4*b^2*c^3*d^4 + 126*a^5*b*c^2*d^5 + 7*a^6*c*d^6)*x^7 + 1/2*(2*a*b^5*c^7 + 35*a^2*b^4*c^6*d + 140*a^3*b^3*c^5*d^2 + 175*a^4*b^2*c^4*d^3 + 70*a^5*b*c^3*d^4 + 7*a^6*c^2*d^5)*x^6 + (3*a^2*b^4*c^7 + 28*a^3*b^3*c^6*d + 63*a^4*b^2*c^5*d^2 + 42*a^5*b*c^4*d^3 + 7*a^6*c^3*d^4)*x^5 + 1/4*(20*a^3*b^3*c^7 + 105*a^4*b^2*c^6*d + 126*a^5*b*c^5*d^2 + 35*a^6*c^4*d^3)*x^4 + (5*a^4*b^2*c^7 + 14*a^5*b*c^6*d + 7*a^6*c^5*d^2)*x^3 + 1/2*(6*a^5*b*c^7 + 7*a^6*c^6*d)*x^2

mupad [B] time = 0.26, size = 683, normalized size = 3.95

$$x^5 (7 a^6 c^3 d^4 + 42 a^5 b c^4 d^3 + 63 a^4 b^2 c^5 d^2 + 28 a^3 b^3 c^6 d + 3 a^2 b^4 c^7) + x^{10} \left(\frac{3 a^4 b^2 d^7}{2} + 14 a^3 b^3 c d^6 + \frac{63 a^2 b^4 c^2 d^5}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^6*(c + d*x)^7,x)

```
[Out] x^5*(3*a^2*b^4*c^7 + 7*a^6*c^3*d^4 + 28*a^3*b^3*c^6*d + 42*a^5*b*c^4*d^3 +
63*a^4*b^2*c^5*d^2) + x^10*((3*a^4*b^2*d^7)/2 + (7*b^6*c^4*d^3)/2 + 21*a*b^
5*c^3*d^4 + 14*a^3*b^3*c*d^6 + (63*a^2*b^4*c^2*d^5)/2) + x^6*(a*b^5*c^7 + (
7*a^6*c^2*d^5)/2 + (35*a^2*b^4*c^6*d)/2 + 35*a^5*b*c^3*d^4 + 70*a^3*b^3*c^5
*d^2 + (175*a^4*b^2*c^4*d^3)/2) + x^9*((2*a^5*b*d^7)/3 + (7*b^6*c^5*d^2)/3
+ (70*a*b^5*c^4*d^3)/3 + (35*a^4*b^2*c*d^6)/3 + (175*a^2*b^4*c^3*d^4)/3 + (
140*a^3*b^3*c^2*d^5)/3) + x^7*((b^6*c^7)/7 + a^6*c*d^6 + 18*a^5*b*c^2*d^5 +
45*a^2*b^4*c^5*d^2 + 100*a^3*b^3*c^4*d^3 + 75*a^4*b^2*c^3*d^4 + 6*a*b^5*c^
6*d) + x^8*((a^6*d^7)/8 + (7*b^6*c^6*d)/8 + (63*a*b^5*c^5*d^2)/4 + (525*a^2
*b^4*c^4*d^3)/8 + (175*a^3*b^3*c^3*d^4)/2 + (315*a^4*b^2*c^2*d^5)/8 + (21*a
^5*b*c*d^6)/4) + x^4*(5*a^3*b^3*c^7 + (35*a^6*c^4*d^3)/4 + (105*a^4*b^2*c^6
*d)/4 + (63*a^5*b*c^5*d^2)/2) + x^11*((20*a^3*b^3*d^7)/11 + (35*b^6*c^3*d^4
)/11 + (126*a*b^5*c^2*d^5)/11 + (105*a^2*b^4*c*d^6)/11) + a^6*c^7*x + (b^6*
d^7*x^14)/14 + (a^5*c^6*x^2*(7*a*d + 6*b*c))/2 + (b^5*d^6*x^13*(6*a*d + 7*b
*c))/13 + a^4*c^5*x^3*(7*a^2*d^2 + 5*b^2*c^2 + 14*a*b*c*d) + (b^4*d^5*x^12*
(5*a^2*d^2 + 7*b^2*c^2 + 14*a*b*c*d))/4
```

sympy [B] time = 0.18, size = 796, normalized size = 4.60

$$a^6c^7x + \frac{b^6d^7x^{14}}{14} + x^{13}\left(\frac{6ab^5d^7}{13} + \frac{7b^6cd^6}{13}\right) + x^{12}\left(\frac{5a^2b^4d^7}{4} + \frac{7ab^5cd^6}{2} + \frac{7b^6c^2d^5}{4}\right) + x^{11}\left(\frac{20a^3b^3d^7}{11} + \frac{105a^2b^4cd^6}{11} + \frac{126ab^5c^2d^5}{11} + \frac{105a^2b^4cd^6}{11}\right) + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**6*(d*x+c)**7,x)
```

```
[Out] a**6*c**7*x + b**6*d**7*x**14/14 + x**13*(6*a*b**5*d**7/13 + 7*b**6*c*d**6/
13) + x**12*(5*a**2*b**4*d**7/4 + 7*a*b**5*c*d**6/2 + 7*b**6*c**2*d**5/4) +
x**11*(20*a**3*b**3*d**7/11 + 105*a**2*b**4*c*d**6/11 + 126*a*b**5*c**2*d**
*5/11 + 35*b**6*c**3*d**4/11) + x**10*(3*a**4*b**2*d**7/2 + 14*a**3*b**3*c*
d**6 + 63*a**2*b**4*c**2*d**5/2 + 21*a*b**5*c**3*d**4 + 7*b**6*c**4*d**3/2)
+ x**9*(2*a**5*b*d**7/3 + 35*a**4*b**2*c*d**6/3 + 140*a**3*b**3*c**2*d**5/
3 + 175*a**2*b**4*c**3*d**4/3 + 70*a*b**5*c**4*d**3/3 + 7*b**6*c**5*d**2/3)
+ x**8*(a**6*d**7/8 + 21*a**5*b*c*d**6/4 + 315*a**4*b**2*c**2*d**5/8 + 175
*a**3*b**3*c**3*d**4/2 + 525*a**2*b**4*c**4*d**3/8 + 63*a*b**5*c**5*d**2/4
+ 7*b**6*c**6*d/8) + x**7*(a**6*c*d**6 + 18*a**5*b*c**2*d**5 + 75*a**4*b**2
*c**3*d**4 + 100*a**3*b**3*c**4*d**3 + 45*a**2*b**4*c**5*d**2 + 6*a*b**5*c*
*6*d + b**6*c**7/7) + x**6*(7*a**6*c**2*d**5/2 + 35*a**5*b*c**3*d**4 + 175*
a**4*b**2*c**4*d**3/2 + 70*a**3*b**3*c**5*d**2 + 35*a**2*b**4*c**6*d/2 + a*
b**5*c**7) + x**5*(7*a**6*c**3*d**4 + 42*a**5*b*c**4*d**3 + 63*a**4*b**2*c*
*5*d**2 + 28*a**3*b**3*c**6*d + 3*a**2*b**4*c**7) + x**4*(35*a**6*c**4*d**3
/4 + 63*a**5*b*c**5*d**2/2 + 105*a**4*b**2*c**6*d/4 + 5*a**3*b**3*c**7) + x
**3*(7*a**6*c**5*d**2 + 14*a**5*b*c**6*d + 5*a**4*b**2*c**7) + x**2*(7*a**6
*c**6*d/2 + 3*a**5*b*c**7)
```

3.1277 $\int (a + bx)^5 (c + dx)^7 dx$

Optimal. Leaf size=144

$$-\frac{5b^4(c+dx)^{12}(bc-ad)}{12d^6} + \frac{10b^3(c+dx)^{11}(bc-ad)^2}{11d^6} - \frac{b^2(c+dx)^{10}(bc-ad)^3}{d^6} + \frac{5b(c+dx)^9(bc-ad)^4}{9d^6} - \frac{(c+dx)^8(bc-ad)^5}{8d^6}$$

[Out] $-1/8*(-a*d+b*c)^5*(d*x+c)^8/d^6+5/9*b*(-a*d+b*c)^4*(d*x+c)^9/d^6-b^2*(-a*d+b*c)^3*(d*x+c)^10/d^6+10/11*b^3*(-a*d+b*c)^2*(d*x+c)^11/d^6-5/12*b^4*(-a*d+b*c)*(d*x+c)^12/d^6+1/13*b^5*(d*x+c)^13/d^6$

Rubi [A] time = 0.36, antiderivative size = 144, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{5b^4(c+dx)^{12}(bc-ad)}{12d^6} + \frac{10b^3(c+dx)^{11}(bc-ad)^2}{11d^6} - \frac{b^2(c+dx)^{10}(bc-ad)^3}{d^6} + \frac{5b(c+dx)^9(bc-ad)^4}{9d^6} - \frac{(c+dx)^8(bc-ad)^5}{8d^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*(c + d*x)^7, x]

[Out] $-((b*c - a*d)^5*(c + d*x)^8)/(8*d^6) + (5*b*(b*c - a*d)^4*(c + d*x)^9)/(9*d^6) - (b^2*(b*c - a*d)^3*(c + d*x)^10)/d^6 + (10*b^3*(b*c - a*d)^2*(c + d*x)^11)/(11*d^6) - (5*b^4*(b*c - a*d)*(c + d*x)^12)/(12*d^6) + (b^5*(c + d*x)^13)/(13*d^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^5 (c + dx)^7 dx &= \int \left(\frac{(-bc + ad)^5 (c + dx)^7}{d^5} + \frac{5b(bc - ad)^4 (c + dx)^8}{d^5} - \frac{10b^2(bc - ad)^3 (c + dx)^9}{d^5} + \frac{10b^3(bc - ad)^2 (c + dx)^{10}}{d^5} - \frac{5b^4(bc - ad) (c + dx)^{11}}{d^5} + \frac{b^5 (c + dx)^{12}}{d^5} \right) dx \\ &= -\frac{(bc - ad)^5 (c + dx)^8}{8d^6} + \frac{5b(bc - ad)^4 (c + dx)^9}{9d^6} - \frac{b^2(bc - ad)^3 (c + dx)^{10}}{d^6} + \frac{10b^3(bc - ad)^2 (c + dx)^{11}}{11d^6} - \frac{5b^4(bc - ad) (c + dx)^{12}}{12d^6} + \frac{b^5 (c + dx)^{13}}{13d^6} \end{aligned}$$

Mathematica [B] time = 0.08, size = 574, normalized size = 3.99

$$a^5 c^7 x + \frac{1}{2} a^4 c^6 x^2 (7ad + 5bc) + \frac{1}{11} b^3 d^5 x^{11} (10a^2 d^2 + 35abcd + 21b^2 c^2) + \frac{1}{3} a^3 c^5 x^3 (21a^2 d^2 + 35abcd + 10b^2 c^2) + \frac{1}{2} b^2 d^4 x^5 (7ad + 5bc) + \frac{1}{11} b^4 d^3 x^7 (7ad + 5bc) + \frac{1}{13} b^5 d^2 x^9 (7ad + 5bc) + \frac{1}{15} b^6 d x^{11} (7ad + 5bc)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*(c + d*x)^7,x]

[Out] $a^5c^7x + (a^4c^6(5b^2c + 7a^2d)x^2)/2 + (a^3c^5(10b^2c^2 + 35a^2b^2cd + 21a^2d^2)x^3)/3 + (5a^2c^4(2b^3c^3 + 14a^2b^2c^2d + 21a^2b^2c^2d^2 + 7a^3d^3)x^4)/4 + a^2c^3(b^4c^4 + 14a^2b^3c^3d + 42a^2b^2c^2d^2 + 35a^3b^2c^2d^3 + 7a^4d^4)x^5 + (c^2(b^5c^5 + 35a^2b^4c^4d + 210a^2b^3c^3d^2 + 350a^3b^2c^2d^3 + 175a^4b^2c^2d^4 + 21a^5d^5)x^6)/6 + cd(b^5c^5 + 15a^2b^4c^4d + 50a^2b^3c^3d^2 + 50a^3b^2c^2d^3 + 15a^4b^2c^2d^4 + a^5d^5)x^7 + (d^2(21b^5c^5 + 175a^2b^4c^4d + 350a^2b^3c^3d^2 + 210a^3b^2c^2d^3 + 35a^4b^2c^2d^4 + a^5d^5)x^8)/8 + (5b^2d^3(7b^4c^4 + 35a^2b^3c^3d + 42a^2b^2c^2d^2 + 14a^3b^2c^2d^3 + a^4d^4)x^9)/9 + (b^2d^4(7b^3c^3 + 21a^2b^2c^2d + 14a^2b^2c^2d^2 + 2a^3d^3)x^10)/2 + (b^3d^5(21b^2c^2 + 35a^2b^2c^2d + 10a^2d^2)x^11)/11 + (b^4d^6(7b^2c + 5a^2d)x^12)/12 + (b^5d^7x^13)/13$

fricas [B] time = 0.39, size = 670, normalized size = 4.65

$$\frac{1}{13}x^{13}d^7b^5 + \frac{7}{12}x^{12}d^6cb^5 + \frac{5}{12}x^{12}d^7b^4a + \frac{21}{11}x^{11}d^5c^2b^5 + \frac{35}{11}x^{11}d^6cb^4a + \frac{10}{11}x^{11}d^7b^3a^2 + \frac{7}{2}x^{10}d^4c^3b^5 + \frac{21}{2}x^{10}d^5c^2b^4a + 7x^{10}d^6cb^4a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^7,x, algorithm="fricas")

[Out] $1/13*x^{13}*d^7*b^5 + 7/12*x^{12}*d^6*c*b^5 + 5/12*x^{12}*d^7*b^4*a + 21/11*x^{11}*d^5*c^2*b^5 + 35/11*x^{11}*d^6*c*b^4*a + 10/11*x^{11}*d^7*b^3*a^2 + 7/2*x^{10}*d^4*c^3*b^5 + 21/2*x^{10}*d^5*c^2*b^4*a + 7*x^{10}*d^6*c*b^3*a^2 + x^{10}*d^7*b^2*a^3 + 35/9*x^9*d^3*c^4*b^5 + 175/9*x^9*d^4*c^3*b^4*a + 70/3*x^9*d^5*c^2*b^3*a^2 + 70/9*x^9*d^6*c*b^2*a^3 + 5/9*x^9*d^7*b*a^4 + 21/8*x^8*d^2*c^5*b^5 + 175/8*x^8*d^3*c^4*b^4*a + 175/4*x^8*d^4*c^3*b^3*a^2 + 105/4*x^8*d^5*c^2*b^2*a^3 + 35/8*x^8*d^6*c*b*a^4 + 1/8*x^8*d^7*a^5 + x^7*d*c^6*b^5 + 15*x^7*d^2*c^5*b^4*a + 50*x^7*d^3*c^4*b^3*a^2 + 50*x^7*d^4*c^3*b^2*a^3 + 15*x^7*d^5*c^2*b*b*a^4 + x^7*d^6*c*a^5 + 1/6*x^6*c^7*b^5 + 35/6*x^6*d*c^6*b^4*a + 35*x^6*d^2*c^5*b^3*a^2 + 175/3*x^6*d^3*c^4*b^2*a^3 + 175/6*x^6*d^4*c^3*b*a^4 + 7/2*x^6*d^5*c^2*a^5 + x^5*c^7*b^4*a + 14*x^5*d*c^6*b^3*a^2 + 42*x^5*d^2*c^5*b^2*a^3 + 35*x^5*d^3*c^4*b*a^4 + 7*x^5*d^4*c^3*a^5 + 5/2*x^4*c^7*b^3*a^2 + 35/2*x^4*d*c^6*b^2*a^3 + 105/4*x^4*d^2*c^5*b*a^4 + 35/4*x^4*d^3*c^4*a^5 + 10/3*x^3*c^7*b^2*a^3 + 35/3*x^3*d*c^6*b*a^4 + 7*x^3*d^2*c^5*a^5 + 5/2*x^2*c^7*b*a^4 + 7/2*x^2*d*c^6*a^5 + x*c^7*a^5$

giac [B] time = 1.28, size = 670, normalized size = 4.65

$$\frac{1}{13}b^5d^7x^{13} + \frac{7}{12}b^5cd^6x^{12} + \frac{5}{12}ab^4d^7x^{12} + \frac{21}{11}b^5c^2d^5x^{11} + \frac{35}{11}ab^4cd^6x^{11} + \frac{10}{11}a^2b^3d^7x^{11} + \frac{7}{2}b^5c^3d^4x^{10} + \frac{21}{2}ab^4c^2d^5x^{10} +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^7,x, algorithm="giac")

[Out] $\frac{1}{13}b^5d^7x^{13} + \frac{7}{12}b^5c*d^6*x^{12} + \frac{5}{12}a*b^4*d^7*x^{12} + \frac{21}{11}b^5*c^2*d^5*x^{11} + \frac{35}{11}a*b^4*c*d^6*x^{11} + \frac{10}{11}a^2*b^3*d^7*x^{11} + \frac{7}{2}b^5*c^3*d^4*x^{10} + \frac{21}{2}a*b^4*c^2*d^5*x^{10} + 7a^2*b^3*c*d^6*x^{10} + a^3*b^2*d^7*x^{10} + \frac{35}{9}b^5*c^4*d^3*x^9 + \frac{175}{9}a*b^4*c^3*d^4*x^9 + \frac{70}{3}a^2*b^3*c^2*d^5*x^9 + \frac{70}{9}a^3*b^2*c*d^6*x^9 + \frac{5}{9}a^4*b*d^7*x^9 + \frac{21}{8}b^5*c^5*d^2*x^8 + \frac{1}{75}a*b^4*c^4*d^3*x^8 + \frac{175}{4}a^2*b^3*c^3*d^4*x^8 + \frac{105}{4}a^3*b^2*c^2*d^5*x^8 + \frac{35}{8}a^4*b*c*d^6*x^8 + \frac{1}{8}a^5*d^7*x^8 + b^5*c^6*d*x^7 + 15a*b^4*c^5*d^2*x^7 + 50a^2*b^3*c^4*d^3*x^7 + 50a^3*b^2*c^3*d^4*x^7 + 15a^4*b*c^2*d^5*x^7 + a^5*c*d^6*x^7 + \frac{1}{6}b^5*c^7*x^6 + \frac{35}{6}a*b^4*c^6*d*x^6 + 35a^2*b^3*c^5*d^2*x^6 + \frac{175}{3}a^3*b^2*c^4*d^3*x^6 + \frac{175}{6}a^4*b*c^3*d^4*x^6 + \frac{7}{2}a^5*c^2*d^5*x^6 + a*b^4*c^7*x^5 + 14a^2*b^3*c^6*d*x^5 + 42a^3*b^2*c^5*d^2*x^5 + 35a^4*b*c^4*d^3*x^5 + 7a^5*c^3*d^4*x^5 + \frac{5}{2}a^2*b^3*c^7*x^4 + \frac{35}{2}a^3*b^2*c^6*d*x^4 + \frac{105}{4}a^4*b*c^5*d^2*x^4 + \frac{35}{4}a^5*c^4*d^3*x^4 + \frac{10}{3}a^3*b^2*c^7*x^3 + \frac{35}{3}a^4*b*c^6*d*x^3 + 7a^5*c^5*d^2*x^3 + \frac{5}{2}a^4*b*c^7*x^2 + \frac{7}{2}a^5*c^6*d*x^2 + a^5*c^7*x$

maple [B] time = 0.00, size = 601, normalized size = 4.17

$$\frac{b^5d^7x^{13}}{13} + a^5c^7x + \frac{(5ab^4d^7 + 7b^5cd^6)x^{12}}{12} + \frac{(10a^2b^3d^7 + 35ab^4cd^6 + 21b^5c^2d^5)x^{11}}{11} + \frac{(10a^3b^2d^7 + 70a^2b^3cd^6 + 105ab^4c^2d^5 + 35b^5c^3d^4)x^{10}}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5*(d*x+c)^7,x)

[Out] $\frac{1}{13}b^5d^7x^{13} + \frac{1}{12}(5a*b^4*d^7 + 7*b^5*c*d^6)*x^{12} + \frac{1}{11}(10*a^2*b^3*d^7 + 35*a*b^4*c*d^6 + 21*b^5*c^2*d^5)*x^{11} + \frac{1}{10}(10*a^3*b^2*d^7 + 70*a^2*b^3*c*d^6 + 105*a*b^4*c^2*d^5 + 35*b^5*c^3*d^4)*x^{10} + \frac{1}{9}(5*a^4*b*d^7 + 70*a^3*b^2*c*d^6 + 210*a^2*b^3*c^2*d^5 + 175*a*b^4*c^3*d^4 + 35*b^5*c^4*d^3)*x^9 + \frac{1}{8}(a^5*d^7 + 35*a^4*b*c*d^6 + 210*a^3*b^2*c^2*d^5 + 350*a^2*b^3*c^3*d^4 + 175*a*b^4*c^4*d^3 + 21*b^5*c^5*d^2)*x^8 + \frac{1}{7}(7*a^5*c*d^6 + 105*a^4*b*c^2*d^5 + 350*a^3*b^2*c^3*d^4 + 350*a^2*b^3*c^4*d^3 + 105*a*b^4*c^5*d^2 + 7*b^5*c^6*d)*x^7 + \frac{1}{6}(21*a^5*c^2*d^5 + 175*a^4*b*c^3*d^4 + 350*a^3*b^2*c^4*d^3 + 210*a^2*b^3*c^5*d^2 + 35*a*b^4*c^6*d + b^5*c^7)*x^6 + \frac{1}{5}(35*a^5*c^3*d^4 + 175*a^4*b*c^4*d^3 + 210*a^3*b^2*c^5*d^2 + 70*a^2*b^3*c^6*d + 5*a*b^4*c^7)*x^5 + \frac{1}{4}(35*a^5*c^4*d^3 + 105*a^4*b*c^5*d^2 + 70*a^3*b^2*c^6*d + 10*a^2*b^3*c^7)*x^4 + \frac{1}{3}(21*a^5*c^5*d^2 + 35*a^4*b*c^6*d + 10*a^3*b^2*c^7)*x^3 + \frac{1}{2}(7*a^5*c^6*d + 5*a^4*b*c^7)*x^2 + a^5*c^7*x$

maxima [B] time = 1.38, size = 594, normalized size = 4.12

$$\frac{1}{13}b^5d^7x^{13} + a^5c^7x + \frac{1}{12}(7b^5cd^6 + 5ab^4d^7)x^{12} + \frac{1}{11}(21b^5c^2d^5 + 35ab^4cd^6 + 10a^2b^3d^7)x^{11} + \frac{1}{2}(7b^5c^3d^4 + 21ab^4c^2d^5)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^7,x, algorithm="maxima")

[Out] $\frac{1}{13}b^5d^7x^{13} + a^5c^7x + \frac{1}{12}(7b^5c^2d^6 + 5a^2b^4d^7)x^{12} + \frac{1}{11}(21b^5c^2d^5 + 35a^2b^4c^2d^6 + 10a^2b^3d^7)x^{11} + \frac{1}{10}(7b^5c^3d^4 + 21a^2b^4c^2d^5 + 14a^2b^3c^2d^6 + 2a^3b^2d^7)x^{10} + \frac{5}{9}(7b^5c^4d^3 + 35a^2b^4c^3d^4 + 42a^2b^3c^2d^5 + 14a^3b^2c^2d^6 + a^4b^2d^7)x^9 + \frac{1}{8}(21b^5c^5d^2 + 175a^2b^4c^4d^3 + 350a^2b^3c^3d^4 + 210a^3b^2c^2d^5 + 35a^4b^2c^2d^6 + a^5d^7)x^8 + (b^5c^6d + 15a^2b^4c^5d^2 + 50a^2b^3c^4d^3 + 50a^3b^2c^3d^4 + 15a^4b^2c^2d^5 + a^5c^2d^6)x^7 + \frac{1}{6}(b^5c^7 + 35a^2b^4c^6d + 210a^2b^3c^5d^2 + 350a^3b^2c^4d^3 + 175a^4b^2c^3d^4 + 21a^5c^2d^5)x^6 + (a^2b^4c^7 + 14a^2b^3c^6d + 42a^3b^2c^5d^2 + 35a^4b^2c^4d^3 + 7a^5c^3d^4)x^5 + \frac{5}{4}(2a^2b^3c^7 + 14a^3b^2c^6d + 21a^4b^2c^5d^2 + 7a^5c^4d^3)x^4 + \frac{1}{3}(10a^3b^2c^7 + 35a^4b^2c^6d + 21a^5c^5d^2)x^3 + \frac{1}{2}(5a^4b^2c^7 + 7a^5c^6d)x^2$

mupad [B] time = 0.21, size = 570, normalized size = 3.96

$$x^7 \left(a^5 c d^6 + 15 a^4 b c^2 d^5 + 50 a^3 b^2 c^3 d^4 + 50 a^2 b^3 c^4 d^3 + 15 a b^4 c^5 d^2 + b^5 c^6 d \right) + x^6 \left(\frac{7 a^5 c^2 d^5}{2} + \frac{175 a^4 b c^3 d^4}{6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5*(c + d*x)^7,x)

[Out] $x^7(a^5c^2d^6 + b^5c^6d + 15a^2b^4c^5d^2 + 15a^4b^2c^2d^5 + 50a^2b^3c^4d^3 + 50a^3b^2c^3d^4) + x^6((b^5c^7)/6 + (7a^5c^2d^5)/2 + (175a^4b^2c^3d^4)/6 + 35a^2b^3c^5d^2 + (175a^3b^2c^4d^3)/3 + (35a^2b^4c^6d)/6) + x^8((a^5d^7)/8 + (21b^5c^5d^2)/8 + (175a^2b^4c^4d^3)/8 + (175a^2b^3c^3d^4)/4 + (105a^3b^2c^2d^5)/4 + (35a^4b^2c^2d^6)/8) + x^5(a^2b^4c^7 + 7a^5c^3d^4 + 14a^2b^3c^6d + 35a^4b^2c^4d^3 + 42a^3b^2c^5d^2) + x^9((5a^4b^2d^7)/9 + (35b^5c^4d^3)/9 + (175a^2b^4c^3d^4)/9 + (70a^3b^2c^2d^6)/9 + (70a^2b^3c^2d^5)/3) + a^5c^7x + (b^5d^7x^{13})/13 + (5a^2c^4x^4(7a^3d^3 + 2b^3c^3 + 14a^2b^2c^2d + 21a^2b^2c^2d^2))/4 + (b^2d^4x^{10}(2a^3d^3 + 7b^3c^3 + 21a^2b^2c^2d + 14a^2b^2c^2d^2))/2 + (a^4c^6x^2(7a^2d + 5b^2c))/2 + (b^4d^6x^{12}(5a^2d + 7b^2c))/12 + (a^3c^5x^3(21a^2d^2 + 10b^2c^2 + 35a^2b^2c^2d))/3 + (b^3d^5x^{11}(10a^2d^2 + 21b^2c^2 + 35a^2b^2c^2d))/11$

sympy [B] time = 0.16, size = 673, normalized size = 4.67

$$a^5 c^7 x + \frac{b^5 d^7 x^{13}}{13} + x^{12} \left(\frac{5 a b^4 d^7}{12} + \frac{7 b^5 c d^6}{12} \right) + x^{11} \left(\frac{10 a^2 b^3 d^7}{11} + \frac{35 a b^4 c d^6}{11} + \frac{21 b^5 c^2 d^5}{11} \right) + x^{10} \left(a^3 b^2 d^7 + 7 a^2 b^3 c d^6 + \frac{21 a^2 b^2 c^2 d^5}{11} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5*(d*x+c)**7,x)

[Out] $a^{5}c^{7}x + b^{5}d^{7}x^{13}/13 + x^{12}(5ab^{4}d^{7}/12 + 7b^{5}cd^{6}/12) + x^{11}(10a^{2}b^{3}d^{7}/11 + 35a^{2}b^{4}cd^{6}/11 + 21b^{5}c^{2}d^{5}/11) + x^{10}(a^{3}b^{2}d^{7} + 7a^{2}b^{3}cd^{6} + 21ab^{4}c^{2}d^{5}/2 + 7b^{5}c^{3}d^{4}/2) + x^{9}(5a^{4}bd^{7}/9 + 70a^{3}b^{2}cd^{6}/9 + 70a^{2}b^{3}c^{2}d^{5}/3 + 175ab^{4}c^{3}d^{4}/9 + 35b^{5}c^{4}d^{3}/9) + x^{8}(a^{5}d^{7}/8 + 35a^{4}b^{2}cd^{6}/8 + 105a^{3}b^{2}c^{2}d^{5}/4 + 175a^{2}b^{3}c^{3}d^{4}/4 + 175ab^{4}c^{4}d^{3}/8 + 21b^{5}c^{5}d^{2}/8) + x^{7}(a^{5}cd^{6} + 15a^{4}b^{2}c^{2}d^{5} + 50a^{3}b^{2}c^{3}d^{4} + 50a^{2}b^{3}c^{4}d^{3} + 15ab^{4}c^{5}d^{2} + b^{5}c^{6}d) + x^{6}(7a^{5}c^{2}d^{5}/2 + 175a^{4}b^{2}c^{3}d^{4}/6 + 175a^{3}b^{2}c^{4}d^{3}/3 + 35a^{2}b^{3}c^{5}d^{2} + 35ab^{4}c^{6}d/6 + b^{5}c^{7}/6) + x^{5}(7a^{5}c^{3}d^{4} + 35a^{4}b^{2}c^{4}d^{3} + 42a^{3}b^{2}c^{5}d^{2} + 14a^{2}b^{3}c^{6}d + ab^{4}c^{7}) + x^{4}(35a^{5}c^{4}d^{3}/4 + 105a^{4}b^{2}c^{5}d^{2}/4 + 35a^{3}b^{2}c^{6}d/2 + 5a^{2}b^{3}c^{7}/2) + x^{3}(7a^{5}c^{5}d^{2} + 35a^{4}b^{2}c^{6}d/3 + 10a^{3}b^{2}c^{7}/3) + x^{2}(7a^{5}c^{6}d/2 + 5a^{4}b^{2}c^{7}/2)$

3.1278 $\int (a + bx)^4 (c + dx)^7 dx$

Optimal. Leaf size=119

$$-\frac{4b^3(c+dx)^{11}(bc-ad)}{11d^5} + \frac{3b^2(c+dx)^{10}(bc-ad)^2}{5d^5} - \frac{4b(c+dx)^9(bc-ad)^3}{9d^5} + \frac{(c+dx)^8(bc-ad)^4}{8d^5} + \frac{b^4(c+dx)^{12}}{12d^5}$$

[Out] $1/8*(-a*d+b*c)^4*(d*x+c)^8/d^5-4/9*b*(-a*d+b*c)^3*(d*x+c)^9/d^5+3/5*b^2*(-a*d+b*c)^2*(d*x+c)^{10}/d^5-4/11*b^3*(-a*d+b*c)*(d*x+c)^{11}/d^5+1/12*b^4*(d*x+c)^{12}/d^5$

Rubi [A] time = 0.28, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{4b^3(c+dx)^{11}(bc-ad)}{11d^5} + \frac{3b^2(c+dx)^{10}(bc-ad)^2}{5d^5} - \frac{4b(c+dx)^9(bc-ad)^3}{9d^5} + \frac{(c+dx)^8(bc-ad)^4}{8d^5} + \frac{b^4(c+dx)^{12}}{12d^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4*(c + d*x)^7, x]

[Out] $((b*c - a*d)^4*(c + d*x)^8)/(8*d^5) - (4*b*(b*c - a*d)^3*(c + d*x)^9)/(9*d^5) + (3*b^2*(b*c - a*d)^2*(c + d*x)^{10})/(5*d^5) - (4*b^3*(b*c - a*d)*(c + d*x)^{11})/(11*d^5) + (b^4*(c + d*x)^{12})/(12*d^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^4 (c + dx)^7 dx &= \int \left(\frac{(-bc + ad)^4 (c + dx)^7}{d^4} - \frac{4b(bc - ad)^3 (c + dx)^8}{d^4} + \frac{6b^2(bc - ad)^2 (c + dx)^9}{d^4} - \frac{4b^3(bc - ad)(c + dx)^{10}}{d^4} + \frac{b^4(c + dx)^{11}}{d^4} \right) dx \\ &= \frac{(bc - ad)^4 (c + dx)^8}{8d^5} - \frac{4b(bc - ad)^3 (c + dx)^9}{9d^5} + \frac{3b^2(bc - ad)^2 (c + dx)^{10}}{5d^5} - \frac{4b^3(bc - ad)(c + dx)^{11}}{11d^5} + \frac{b^4(c + dx)^{12}}{12d^5} \end{aligned}$$

Mathematica [B] time = 0.05, size = 473, normalized size = 3.97

$$a^4 c^7 x + \frac{1}{2} a^3 c^6 x^2 (7ad + 4bc) + \frac{1}{10} b^2 d^5 x^{10} (6a^2 d^2 + 28abcd + 21b^2 c^2) + \frac{1}{3} a^2 c^5 x^3 (21a^2 d^2 + 28abcd + 6b^2 c^2) + \frac{1}{9} b d^4 x^9 ($$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4*(c + d*x)^7,x]

[Out] $a^4*c^7*x + (a^3*c^6*(4*b*c + 7*a*d)*x^2)/2 + (a^2*c^5*(6*b^2*c^2 + 28*a*b*c*d + 21*a^2*d^2)*x^3)/3 + (a*c^4*(4*b^3*c^3 + 42*a*b^2*c^2*d + 84*a^2*b*c*d^2 + 35*a^3*d^3)*x^4)/4 + (c^3*(b^4*c^4 + 28*a*b^3*c^3*d + 126*a^2*b^2*c^2*d^2 + 140*a^3*b*c*d^3 + 35*a^4*d^4)*x^5)/5 + (7*c^2*d*(b^4*c^4 + 12*a*b^3*c^3*d + 30*a^2*b^2*c^2*d^2 + 20*a^3*b*c*d^3 + 3*a^4*d^4)*x^6)/6 + c*d^2*(3*b^4*c^4 + 20*a*b^3*c^3*d + 30*a^2*b^2*c^2*d^2 + 12*a^3*b*c*d^3 + a^4*d^4)*x^7 + (d^3*(35*b^4*c^4 + 140*a*b^3*c^3*d + 126*a^2*b^2*c^2*d^2 + 28*a^3*b*c*d^3 + a^4*d^4)*x^8)/8 + (b*d^4*(35*b^3*c^3 + 84*a*b^2*c^2*d + 42*a^2*b*c*d^2 + 4*a^3*d^3)*x^9)/9 + (b^2*d^5*(21*b^2*c^2 + 28*a*b*c*d + 6*a^2*d^2)*x^10)/10 + (b^3*d^6*(7*b*c + 4*a*d)*x^11)/11 + (b^4*d^7*x^12)/12$

fricas [B] time = 0.37, size = 546, normalized size = 4.59

$$\frac{1}{12}x^{12}d^7b^4 + \frac{7}{11}x^{11}d^6cb^4 + \frac{4}{11}x^{11}d^7b^3a + \frac{21}{10}x^{10}d^5c^2b^4 + \frac{14}{5}x^{10}d^6cb^3a + \frac{3}{5}x^{10}d^7b^2a^2 + \frac{35}{9}x^9d^4c^3b^4 + \frac{28}{3}x^9d^5c^2b^3a + \frac{14}{3}x^9d^6cb^2a^2 + \frac{7}{2}x^8d^3c^4b^4 + \frac{35}{2}x^8d^4c^3b^3a + \frac{63}{4}x^8d^5c^2b^2a^3 + \frac{7}{2}x^8d^6c^1b^1a^4 + \frac{1}{8}x^8d^7a^4 + 3x^7d^2c^5b^4 + 20x^7d^3c^4b^3a + 30x^7d^4c^3b^2a^2 + 12x^7d^5c^2b^1a^3 + x^7d^6c^1a^4 + \frac{7}{6}x^6d^1c^6b^4 + 14x^6d^2c^5b^3a + 35x^6d^3c^4b^2a^2 + \frac{70}{3}x^6d^4c^3b^1a^3 + \frac{7}{2}x^6d^5c^2a^4 + \frac{1}{5}x^5d^7b^4 + \frac{28}{5}x^5d^6c^6b^3a + \frac{126}{5}x^5d^2c^5b^2a^2 + 28x^5d^3c^4b^1a^3 + 7x^5d^4c^3a^4 + x^4d^7b^3a + \frac{21}{2}x^4d^6c^6b^2a^2 + 21x^4d^2c^5b^1a^3 + \frac{35}{4}x^4d^3c^4a^4 + 2x^3d^7b^2a^2 + \frac{28}{3}x^3d^6c^6b^1a^3 + 7x^3d^2c^5a^4 + 2x^2d^7b^1a^3 + \frac{7}{2}x^2d^1c^6a^4 + xc^7a^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^7,x, algorithm="fricas")

[Out] $1/12*x^{12}*d^7*b^4 + 7/11*x^{11}*d^6*c*b^4 + 4/11*x^{11}*d^7*b^3*a + 21/10*x^{10}*d^5*c^2*b^4 + 14/5*x^{10}*d^6*c*b^3*a + 3/5*x^{10}*d^7*b^2*a^2 + 35/9*x^9*d^4*c^3*b^4 + 28/3*x^9*d^5*c^2*b^3*a + 14/3*x^9*d^6*c*b^2*a^2 + 4/9*x^9*d^7*b^1*a^3 + 35/8*x^8*d^3*c^4*b^4 + 35/2*x^8*d^4*c^3*b^3*a + 63/4*x^8*d^5*c^2*b^2*a^2 + 7/2*x^8*d^6*c*b^1*a^4 + 1/8*x^8*d^7*a^4 + 3*x^7*d^2*c^5*b^4 + 20*x^7*d^3*c^4*b^3*a + 30*x^7*d^4*c^3*b^2*a^2 + 12*x^7*d^5*c^2*b^1*a^3 + x^7*d^6*c^1*a^4 + 7/6*x^6*d^1*c^6*b^4 + 14*x^6*d^2*c^5*b^3*a + 35*x^6*d^3*c^4*b^2*a^2 + 70/3*x^6*d^4*c^3*b^1*a^3 + 7/2*x^6*d^5*c^2*a^4 + 1/5*x^5*d^7*b^4 + 28/5*x^5*d^6*c^6*b^3*a + 126/5*x^5*d^2*c^5*b^2*a^2 + 28*x^5*d^3*c^4*b^1*a^3 + 7*x^5*d^4*c^3*a^4 + x^4*d^7*b^3*a + 21/2*x^4*d^6*c^6*b^2*a^2 + 21*x^4*d^2*c^5*b^1*a^3 + 35/4*x^4*d^3*c^4*a^4 + 2*x^3*d^7*b^2*a^2 + 28/3*x^3*d^6*c^6*b^1*a^3 + 7*x^3*d^2*c^5*a^4 + 2*x^2*d^7*b^1*a^3 + 7/2*x^2*d^1*c^6*a^4 + x*c^7*a^4$

giac [B] time = 1.21, size = 546, normalized size = 4.59

$$\frac{1}{12}b^4d^7x^{12} + \frac{7}{11}b^4cd^6x^{11} + \frac{4}{11}ab^3d^7x^{11} + \frac{21}{10}b^4c^2d^5x^{10} + \frac{14}{5}ab^3cd^6x^{10} + \frac{3}{5}a^2b^2d^7x^{10} + \frac{35}{9}b^4c^3d^4x^9 + \frac{28}{3}ab^3c^2d^5x^9 + \frac{14}{3}x^9d^6cb^2a^2 + \frac{7}{2}x^8d^3c^4b^4 + \frac{35}{2}x^8d^4c^3b^3a + \frac{63}{4}x^8d^5c^2b^2a^3 + \frac{7}{2}x^8d^6c^1b^1a^4 + \frac{1}{8}x^8d^7a^4 + 3x^7d^2c^5b^4 + 20x^7d^3c^4b^3a + 30x^7d^4c^3b^2a^2 + 12x^7d^5c^2b^1a^3 + x^7d^6c^1a^4 + \frac{7}{6}x^6d^1c^6b^4 + 14x^6d^2c^5b^3a + 35x^6d^3c^4b^2a^2 + \frac{70}{3}x^6d^4c^3b^1a^3 + \frac{7}{2}x^6d^5c^2a^4 + \frac{1}{5}x^5d^7b^4 + \frac{28}{5}x^5d^6c^6b^3a + \frac{126}{5}x^5d^2c^5b^2a^2 + 28x^5d^3c^4b^1a^3 + 7x^5d^4c^3a^4 + x^4d^7b^3a + \frac{21}{2}x^4d^6c^6b^2a^2 + 21x^4d^2c^5b^1a^3 + \frac{35}{4}x^4d^3c^4a^4 + 2x^3d^7b^2a^2 + \frac{28}{3}x^3d^6c^6b^1a^3 + 7x^3d^2c^5a^4 + 2x^2d^7b^1a^3 + \frac{7}{2}x^2d^1c^6a^4 + xc^7a^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^7,x, algorithm="giac")

[Out] $1/12*b^4*d^7*x^{12} + 7/11*b^4*c*d^6*x^{11} + 4/11*a*b^3*d^7*x^{11} + 21/10*b^4*c^2*d^5*x^{10} + 14/5*a*b^3*c*d^6*x^{10} + 3/5*a^2*b^2*d^7*x^{10} + 35/9*b^4*c^3*d^4*x^9 + 28/3*a*b^3*c^2*d^5*x^9 + 14/3*x^9*d^6*c*b^2*a^2 + 7/2*x^8*d^3*c^4*b^4 + 35/2*x^8*d^4*c^3*b^3*a + 63/4*x^8*d^5*c^2*b^2*a^3 + 7/2*x^8*d^6*c*b^1*a^4 + 1/8*x^8*d^7*a^4 + 3*x^7*d^2*c^5*b^4 + 20*x^7*d^3*c^4*b^3*a + 30*x^7*d^4*c^3*b^2*a^2 + 12*x^7*d^5*c^2*b^1*a^3 + x^7*d^6*c^1*a^4 + 7/6*x^6*d^1*c^6*b^4 + 14*x^6*d^2*c^5*b^3*a + 35*x^6*d^3*c^4*b^2*a^2 + 70/3*x^6*d^4*c^3*b^1*a^3 + 7/2*x^6*d^5*c^2*a^4 + 1/5*x^5*d^7*b^4 + 28/5*x^5*d^6*c^6*b^3*a + 126/5*x^5*d^2*c^5*b^2*a^2 + 28*x^5*d^3*c^4*b^1*a^3 + 7*x^5*d^4*c^3*a^4 + x^4*d^7*b^3*a + 21/2*x^4*d^6*c^6*b^2*a^2 + 21*x^4*d^2*c^5*b^1*a^3 + 35/4*x^4*d^3*c^4*a^4 + 2*x^3*d^7*b^2*a^2 + 28/3*x^3*d^6*c^6*b^1*a^3 + 7*x^3*d^2*c^5*a^4 + 2*x^2*d^7*b^1*a^3 + 7/2*x^2*d^1*c^6*a^4 + x*c^7*a^4$

$$\begin{aligned} &^4x^9 + 28/3a^3b^3c^2d^5x^9 + 14/3a^2b^2c^2d^6x^9 + 4/9a^3b^3d^7x^9 \\ &+ 35/8b^4c^4d^3x^8 + 35/2a^3b^3c^3d^4x^8 + 63/4a^2b^2c^2d^5x^8 \\ &+ 7/2a^3b^3c^2d^6x^8 + 1/8a^4d^7x^8 + 3b^4c^5d^2x^7 + 20a^3b^3c^4d^3x^7 \\ &+ 30a^2b^2c^3d^4x^7 + 12a^3b^3c^2d^5x^7 + a^4c^6d^6x^7 + 7/6b^4c^6d^6x^6 \\ &+ 14a^3b^3c^5d^2x^6 + 35a^2b^2c^4d^3x^6 + 70/3a^3b^3c^3d^4x^6 \\ &+ 7/2a^4c^2d^5x^6 + 1/5b^4c^7x^5 + 28/5a^3b^3c^6d^6x^5 \\ &+ 126/5a^2b^2c^5d^2x^5 + 28a^3b^3c^4d^3x^5 + 7a^4c^3d^4x^5 \\ &+ a^3b^3c^7x^4 + 21/2a^2b^2c^6d^6x^4 + 21a^3b^3c^5d^2x^4 + 35/4a^4c^4d^3x^4 \\ &+ 2a^2b^2c^7x^3 + 28/3a^3b^3c^6d^6x^3 + 7a^4c^5d^2x^3 \\ &+ 2a^3b^3c^7x^2 + 7/2a^4c^6d^6x^2 + a^4c^7x \end{aligned}$$

maple [B] time = 0.00, size = 493, normalized size = 4.14

$$\frac{b^4d^7x^{12}}{12} + a^4c^7x + \frac{(4ab^3d^7 + 7b^4cd^6)x^{11}}{11} + \frac{(6a^2b^2d^7 + 28ab^3cd^6 + 21b^4c^2d^5)x^{10}}{10} + \frac{(4a^3bd^7 + 42a^2b^2cd^6 + 84ab^3c^2d^5)x^9}{9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4*(d*x+c)^7,x)

[Out] 1/12*b^4*d^7*x^12+1/11*(4*a*b^3*d^7+7*b^4*c*d^6)*x^11+1/10*(6*a^2*b^2*d^7+2*8*a*b^3*c*d^6+21*b^4*c^2*d^5)*x^10+1/9*(4*a^3*b*d^7+42*a^2*b^2*c*d^6+84*a*b^3*c^2*d^5+35*b^4*c^3*d^4)*x^9+1/8*(a^4*d^7+28*a^3*b*c*d^6+126*a^2*b^2*c^2*d^5+140*a*b^3*c^3*d^4+35*b^4*c^4*d^3)*x^8+1/7*(7*a^4*c*d^6+84*a^3*b*c^2*d^5+210*a^2*b^2*c^3*d^4+140*a*b^3*c^4*d^3+21*b^4*c^5*d^2)*x^7+1/6*(21*a^4*c^2*d^5+140*a^3*b*c^3*d^4+210*a^2*b^2*c^4*d^3+84*a*b^3*c^5*d^2+7*b^4*c^6*d)*x^6+1/5*(35*a^4*c^3*d^4+140*a^3*b*c^4*d^3+126*a^2*b^2*c^5*d^2+28*a*b^3*c^6*d+b^4*c^7)*x^5+1/4*(35*a^4*c^4*d^3+84*a^3*b*c^5*d^2+42*a^2*b^2*c^6*d+4*a*b^3*c^7)*x^4+1/3*(21*a^4*c^5*d^2+28*a^3*b*c^6*d+6*a^2*b^2*c^7)*x^3+1/2*(7*a^4*c^6*d+4*a^3*b*c^7)*x^2+a^4*c^7*x

maxima [B] time = 1.48, size = 489, normalized size = 4.11

$$\frac{1}{12} b^4 d^7 x^{12} + a^4 c^7 x + \frac{1}{11} (7 b^4 c d^6 + 4 a b^3 d^7) x^{11} + \frac{1}{10} (21 b^4 c^2 d^5 + 28 a b^3 c d^6 + 6 a^2 b^2 d^7) x^{10} + \frac{1}{9} (35 b^4 c^3 d^4 + 84 a b^3 c^2 d^5)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^7,x, algorithm="maxima")

[Out] 1/12*b^4*d^7*x^12 + a^4*c^7*x + 1/11*(7*b^4*c*d^6 + 4*a*b^3*d^7)*x^11 + 1/10*(21*b^4*c^2*d^5 + 28*a*b^3*c*d^6 + 6*a^2*b^2*d^7)*x^10 + 1/9*(35*b^4*c^3*d^4 + 84*a*b^3*c^2*d^5 + 42*a^2*b^2*c*d^6 + 4*a^3*b*d^7)*x^9 + 1/8*(35*b^4*c^4*d^3 + 140*a*b^3*c^3*d^4 + 126*a^2*b^2*c^2*d^5 + 28*a^3*b*c*d^6 + a^4*d^7)*x^8 + (3*b^4*c^5*d^2 + 20*a*b^3*c^4*d^3 + 30*a^2*b^2*c^3*d^4 + 12*a^3*b*c^2*d^5 + a^4*c*d^6)*x^7 + 7/6*(b^4*c^6*d + 12*a*b^3*c^5*d^2 + 30*a^2*b^2*c^4*d^3 + 20*a^3*b*c^3*d^4 + 3*a^4*c^2*d^5)*x^6 + 1/5*(b^4*c^7 + 28*a*b^3*c^6*d + 4*a^2*b^2*c^7)*x^5 + 1/4*(35*a^4*c^4*d^3 + 84*a^3*b*c^5*d^2 + 42*a^2*b^2*c^6*d + 4*a*b^3*c^7)*x^4 + 1/3*(21*a^4*c^5*d^2 + 28*a^3*b*c^6*d + 6*a^2*b^2*c^7)*x^3 + 1/2*(7*a^4*c^6*d + 4*a^3*b*c^7)*x^2 + a^4*c^7*x

$$6*d + 126*a^2*b^2*c^5*d^2 + 140*a^3*b*c^4*d^3 + 35*a^4*c^3*d^4)*x^5 + 1/4*(4*a*b^3*c^7 + 42*a^2*b^2*c^6*d + 84*a^3*b*c^5*d^2 + 35*a^4*c^4*d^3)*x^4 + 1/3*(6*a^2*b^2*c^7 + 28*a^3*b*c^6*d + 21*a^4*c^5*d^2)*x^3 + 1/2*(4*a^3*b*c^7 + 7*a^4*c^6*d)*x^2$$

mupad [B] time = 0.31, size = 470, normalized size = 3.95

$$x^5 \left(7a^4c^3d^4 + 28a^3bc^4d^3 + \frac{126a^2b^2c^5d^2}{5} + \frac{28ab^3c^6d}{5} + \frac{b^4c^7}{5} \right) + x^8 \left(\frac{a^4d^7}{8} + \frac{7a^3bcd^6}{2} + \frac{63a^2b^2c^2d^5}{4} + \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^4*(c + d*x)^7,x)

[Out] $x^5*((b^4*c^7)/5 + 7*a^4*c^3*d^4 + 28*a^3*b*c^4*d^3 + (126*a^2*b^2*c^5*d^2)/5 + (28*a*b^3*c^6*d)/5) + x^8*((a^4*d^7)/8 + (35*b^4*c^4*d^3)/8 + (35*a*b^3*c^3*d^4)/2 + (63*a^2*b^2*c^2*d^5)/4 + (7*a^3*b*c*d^6)/2) + x^4*(a*b^3*c^7 + (35*a^4*c^4*d^3)/4 + (21*a^2*b^2*c^6*d)/2 + 21*a^3*b*c^5*d^2) + x^9*((4*a^3*b*d^7)/9 + (35*b^4*c^3*d^4)/9 + (28*a*b^3*c^2*d^5)/3 + (14*a^2*b^2*c*d^6)/3) + x^7*(a^4*c*d^6 + 3*b^4*c^5*d^2 + 20*a*b^3*c^4*d^3 + 12*a^3*b*c^2*d^5 + 30*a^2*b^2*c^3*d^4) + x^6*((7*b^4*c^6*d)/6 + (7*a^4*c^2*d^5)/2 + 14*a*b^3*c^5*d^2 + (70*a^3*b*c^3*d^4)/3 + 35*a^2*b^2*c^4*d^3) + a^4*c^7*x + (b^4*d^7*x^12)/12 + (a^3*c^6*x^2*(7*a*d + 4*b*c))/2 + (b^3*d^6*x^11*(4*a*d + 7*b*c))/11 + (a^2*c^5*x^3*(21*a^2*d^2 + 6*b^2*c^2 + 28*a*b*c*d))/3 + (b^2*d^5*x^10*(6*a^2*d^2 + 21*b^2*c^2 + 28*a*b*c*d))/10$

sympy [B] time = 0.15, size = 549, normalized size = 4.61

$$a^4c^7x + \frac{b^4d^7x^{12}}{12} + x^{11} \left(\frac{4ab^3d^7}{11} + \frac{7b^4cd^6}{11} \right) + x^{10} \left(\frac{3a^2b^2d^7}{5} + \frac{14ab^3cd^6}{5} + \frac{21b^4c^2d^5}{10} \right) + x^9 \left(\frac{4a^3bd^7}{9} + \frac{14a^2b^2cd^6}{3} + \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4*(d*x+c)**7,x)

[Out] $a**4*c**7*x + b**4*d**7*x**12/12 + x**11*(4*a*b**3*d**7/11 + 7*b**4*c*d**6/11) + x**10*(3*a**2*b**2*d**7/5 + 14*a*b**3*c*d**6/5 + 21*b**4*c**2*d**5/10) + x**9*(4*a**3*b*d**7/9 + 14*a**2*b**2*c*d**6/3 + 28*a*b**3*c**2*d**5/3 + 35*b**4*c**3*d**4/9) + x**8*(a**4*d**7/8 + 7*a**3*b*c*d**6/2 + 63*a**2*b**2*c**2*d**5/4 + 35*a*b**3*c**3*d**4/2 + 35*b**4*c**4*d**3/8) + x**7*(a**4*c*d**6 + 12*a**3*b*c**2*d**5 + 30*a**2*b**2*c**3*d**4 + 20*a*b**3*c**4*d**3 + 3*b**4*c**5*d**2) + x**6*(7*a**4*c**2*d**5/2 + 70*a**3*b*c**3*d**4/3 + 35*a**2*b**2*c**4*d**3 + 14*a*b**3*c**5*d**2 + 7*b**4*c**6*d/6) + x**5*(7*a**4*c**3*d**4 + 28*a**3*b*c**4*d**3 + 126*a**2*b**2*c**5*d**2/5 + 28*a*b**3*c**6*d/5 + b**4*c**7/5) + x**4*(35*a**4*c**4*d**3/4 + 21*a**3*b*c**5*d**2 + 21*a**2*b**2*c**6*d/2 + a*b**3*c**7) + x**3*(7*a**4*c**5*d**2 + 28*a**3*b*c**6*d/3 + 2*a**2*b**2*c**7) + x**2*(7*a**4*c**6*d/2 + 2*a**3*b*c**7)$

3.1279 $\int (a + bx)^3 (c + dx)^7 dx$

Optimal. Leaf size=92

$$-\frac{3b^2(c+dx)^{10}(bc-ad)}{10d^4} + \frac{b(c+dx)^9(bc-ad)^2}{3d^4} - \frac{(c+dx)^8(bc-ad)^3}{8d^4} + \frac{b^3(c+dx)^{11}}{11d^4}$$

[Out] $-1/8*(-a*d+b*c)^3*(d*x+c)^8/d^4+1/3*b*(-a*d+b*c)^2*(d*x+c)^9/d^4-3/10*b^2*(-a*d+b*c)*(d*x+c)^10/d^4+1/11*b^3*(d*x+c)^11/d^4$

Rubi [A] time = 0.22, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{3b^2(c+dx)^{10}(bc-ad)}{10d^4} + \frac{b(c+dx)^9(bc-ad)^2}{3d^4} - \frac{(c+dx)^8(bc-ad)^3}{8d^4} + \frac{b^3(c+dx)^{11}}{11d^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3*(c + d*x)^7, x]

[Out] $-((b*c - a*d)^3*(c + d*x)^8)/(8*d^4) + (b*(b*c - a*d)^2*(c + d*x)^9)/(3*d^4) - (3*b^2*(b*c - a*d)*(c + d*x)^10)/(10*d^4) + (b^3*(c + d*x)^11)/(11*d^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^3 (c + dx)^7 dx &= \int \left(\frac{(-bc + ad)^3 (c + dx)^7}{d^3} + \frac{3b(bc - ad)^2 (c + dx)^8}{d^3} - \frac{3b^2(bc - ad)(c + dx)^9}{d^3} + \frac{b^3(c + dx)^{10}}{d^3} \right. \\ &= -\frac{(bc - ad)^3 (c + dx)^8}{8d^4} + \frac{b(bc - ad)^2 (c + dx)^9}{3d^4} - \frac{3b^2(bc - ad)(c + dx)^{10}}{10d^4} + \frac{b^3(c + dx)^{11}}{11d^4} \end{aligned}$$

Mathematica [B] time = 0.04, size = 360, normalized size = 3.91

$$a^3 c^7 x + \frac{1}{3} b d^5 x^9 (a^2 d^2 + 7 a b c d + 7 b^2 c^2) + a c^5 x^3 (7 a^2 d^2 + 7 a b c d + b^2 c^2) + \frac{1}{2} a^2 c^6 x^2 (7 a d + 3 b c) + c d^3 x^7 (a^3 d^3 + 9 a^2 b c d^2$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3*(c + d*x)^7,x]

[Out] $a^3c^7x + (a^2c^6(3b^3c + 7a^3d)x^2)/2 + a^2c^5(b^2c^2 + 7a^2b^2cd + 7a^2d^2)x^3 + (c^4(b^3c^3 + 21a^2b^2c^2d + 63a^2b^2cd^2 + 35a^3d^3)x^4)/4 + (7c^3d(b^3c^3 + 9a^2b^2c^2d + 15a^2b^2cd^2 + 5a^3d^3)x^5)/5 + (7c^2d^2(b^3c^3 + 5a^2b^2c^2d + 5a^2b^2cd^2 + a^3d^3)x^6)/2 + cd^3(5b^3c^3 + 15a^2b^2c^2d + 9a^2b^2cd^2 + a^3d^3)x^7 + (d^4(35b^3c^3 + 63a^2b^2c^2d + 21a^2b^2cd^2 + a^3d^3)x^8)/8 + (bd^5(7b^2c^2 + 7a^2b^2cd + a^2d^2)x^9)/3 + (b^2d^6(7b^2c + 3a^2d)x^{10})/10 + (b^3d^7x^{11})/11$

fricas [B] time = 0.39, size = 420, normalized size = 4.57

$$\frac{1}{11}x^{11}d^7b^3 + \frac{7}{10}x^{10}d^6cb^3 + \frac{3}{10}x^{10}d^7b^2a + \frac{7}{3}x^9d^5c^2b^3 + \frac{7}{3}x^9d^6cb^2a + \frac{1}{3}x^9d^7ba^2 + \frac{35}{8}x^8d^4c^3b^3 + \frac{63}{8}x^8d^5c^2b^2a + \frac{21}{8}x^8d^6cb^2a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^7,x, algorithm="fricas")

[Out] $1/11*x^{11}*d^7*b^3 + 7/10*x^{10}*d^6*c*b^3 + 3/10*x^{10}*d^7*b^2*a + 7/3*x^9*d^5*c^2*b^3 + 7/3*x^9*d^6*c*b^2*a + 1/3*x^9*d^7*b*a^2 + 35/8*x^8*d^4*c^3*b^3 + 63/8*x^8*d^5*c^2*b^2*a + 21/8*x^8*d^6*c*b*a^2 + 1/8*x^8*d^7*a^3 + 5*x^7*d^3*c^4*b^3 + 15*x^7*d^4*c^3*b^2*a + 9*x^7*d^5*c^2*b*a^2 + x^7*d^6*c*a^3 + 7/2*x^6*d^2*c^5*b^3 + 35/2*x^6*d^3*c^4*b^2*a + 35/2*x^6*d^4*c^3*b*a^2 + 7/2*x^6*d^5*c^2*a^3 + 7/5*x^5*d*c^6*b^3 + 63/5*x^5*d^2*c^5*b^2*a + 21*x^5*d^3*c^4*b*a^2 + 7*x^5*d^4*c^3*a^3 + 1/4*x^4*c^7*b^3 + 21/4*x^4*d*c^6*b^2*a + 63/4*x^4*d^2*c^5*b*a^2 + 35/4*x^4*d^3*c^4*a^3 + x^3*c^7*b^2*a + 7*x^3*d*c^6*b*a^2 + 7*x^3*d^2*c^5*a^3 + 3/2*x^2*c^7*b*a^2 + 7/2*x^2*d*c^6*a^3 + x*c^7*a^3$

giac [B] time = 1.26, size = 420, normalized size = 4.57

$$\frac{1}{11}b^3d^7x^{11} + \frac{7}{10}b^3cd^6x^{10} + \frac{3}{10}ab^2d^7x^{10} + \frac{7}{3}b^3c^2d^5x^9 + \frac{7}{3}ab^2cd^6x^9 + \frac{1}{3}a^2bd^7x^9 + \frac{35}{8}b^3c^3d^4x^8 + \frac{63}{8}ab^2c^2d^5x^8 + \frac{21}{8}a^2b^2d^6x^8$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^7,x, algorithm="giac")

[Out] $1/11*b^3*d^7*x^{11} + 7/10*b^3*c*d^6*x^{10} + 3/10*a*b^2*d^7*x^{10} + 7/3*b^3*c^2*d^5*x^9 + 7/3*a*b^2*c*d^6*x^9 + 1/3*a^2*b*d^7*x^9 + 35/8*b^3*c^3*d^4*x^8 + 63/8*a*b^2*c^2*d^5*x^8 + 21/8*a^2*b*c*d^6*x^8 + 1/8*a^3*d^7*x^8 + 5*b^3*c^4*d^3*x^7 + 15*a*b^2*c^3*d^4*x^7 + 9*a^2*b*c^2*d^5*x^7 + a^3*c*d^6*x^7 + 7/2*b^3*c^5*d^2*x^6 + 35/2*a*b^2*c^4*d^3*x^6 + 35/2*a^2*b*c^3*d^4*x^6 + 7/2*a^3*c^2*d^5*x^6 + 7/5*b^3*c^6*d*x^5 + 63/5*a*b^2*c^5*d^2*x^5 + 21*a^2*b*c^4*d$

$$d^3x^5 + 7a^3c^3d^4x^5 + 1/4b^3c^7x^4 + 21/4ab^2c^6dx^4 + 63/4a^2b^2c^5d^2x^4 + 35/4a^3c^4d^3x^4 + ab^2c^7x^3 + 7a^2b^2c^6dx^3 + 7a^3c^5d^2x^3 + 3/2a^2b^2c^7x^2 + 7/2a^3c^6dx^2 + a^3c^7x$$

maple [B] time = 0.00, size = 385, normalized size = 4.18

$$\frac{b^3d^7x^{11}}{11} + a^3c^7x + \frac{(3ab^2d^7 + 7b^3cd^6)x^{10}}{10} + \frac{(3a^2bd^7 + 21ab^2cd^6 + 21b^3c^2d^5)x^9}{9} + \frac{(a^3d^7 + 21a^2bcd^6 + 63ab^2c^2d^5 + 21ab^3cd^4 + 63a^2b^2c^3d^4 + 63a^3c^4d^3)x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3*(d*x+c)^7,x)

[Out] 1/11*b^3*d^7*x^11+1/10*(3*a*b^2*d^7+7*b^3*c*d^6)*x^10+1/9*(3*a^2*b*d^7+21*a*b^2*c*d^6+21*b^3*c^2*d^5)*x^9+1/8*(a^3*d^7+21*a^2*b*c*d^6+63*a*b^2*c^2*d^5+35*b^3*c^3*d^4)*x^8+1/7*(7*a^3*c*d^6+63*a^2*b*c^2*d^5+105*a*b^2*c^3*d^4+35*b^3*c^4*d^3)*x^7+1/6*(21*a^3*c^2*d^5+105*a^2*b*c^3*d^4+105*a*b^2*c^4*d^3+21*b^3*c^5*d^2)*x^6+1/5*(35*a^3*c^3*d^4+105*a^2*b*c^4*d^3+63*a*b^2*c^5*d^2+7*b^3*c^6*d)*x^5+1/4*(35*a^3*c^4*d^3+63*a^2*b*c^5*d^2+21*a*b^2*c^6*d+b^3*c^7)*x^4+1/3*(21*a^3*c^5*d^2+21*a^2*b*c^6*d+3*a*b^2*c^7)*x^3+1/2*(7*a^3*c^6*d+3*a^2*b*c^7)*x^2+a^3*c^7*x

maxima [B] time = 1.37, size = 376, normalized size = 4.09

$$\frac{1}{11}b^3d^7x^{11} + a^3c^7x + \frac{1}{10}(7b^3cd^6 + 3ab^2d^7)x^{10} + \frac{1}{3}(7b^3c^2d^5 + 7ab^2cd^6 + a^2bd^7)x^9 + \frac{1}{8}(35b^3c^3d^4 + 63ab^2c^2d^5 + 21ab^3cd^4 + 63a^2b^2c^3d^4 + 63a^3c^4d^3)x^8$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^7,x, algorithm="maxima")

[Out] 1/11*b^3*d^7*x^11 + a^3*c^7*x + 1/10*(7*b^3*c*d^6 + 3*a*b^2*d^7)*x^10 + 1/3*(7*b^3*c^2*d^5 + 7*a*b^2*c*d^6 + a^2*b*d^7)*x^9 + 1/8*(35*b^3*c^3*d^4 + 63*a*b^2*c^2*d^5 + 21*a^2*b*c*d^6 + a^3*d^7)*x^8 + (5*b^3*c^4*d^3 + 15*a*b^2*c^3*d^4 + 9*a^2*b*c^2*d^5 + a^3*c*d^6)*x^7 + 7/2*(b^3*c^5*d^2 + 5*a*b^2*c^4*d^3 + 5*a^2*b*c^3*d^4 + a^3*c^2*d^5)*x^6 + 7/5*(b^3*c^6*d + 9*a*b^2*c^5*d^2 + 15*a^2*b*c^4*d^3 + 5*a^3*c^3*d^4)*x^5 + 1/4*(b^3*c^7 + 21*a*b^2*c^6*d + 63*a^2*b*c^5*d^2 + 35*a^3*c^4*d^3)*x^4 + (a*b^2*c^7 + 7*a^2*b*c^6*d + 7*a^3*c^5*d^2)*x^3 + 1/2*(3*a^2*b*c^7 + 7*a^3*c^6*d)*x^2

mupad [B] time = 0.27, size = 356, normalized size = 3.87

$$x^7 \left(a^3 c d^6 + 9 a^2 b c^2 d^5 + 15 a b^2 c^3 d^4 + 5 b^3 c^4 d^3 \right) + x^5 \left(7 a^3 c^3 d^4 + 21 a^2 b c^4 d^3 + \frac{63 a b^2 c^5 d^2}{5} + \frac{7 b^3 c^6 d}{5} \right) + x^4 \left(7 a^3 c^4 d^3 + 21 a^2 b c^5 d^2 + 35 a b^2 c^6 d + a^3 d^7 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3*(c + d*x)^7,x)`

[Out] $x^7*(a^3*c*d^6 + 5*b^3*c^4*d^3 + 15*a*b^2*c^3*d^4 + 9*a^2*b*c^2*d^5) + x^5*((7*b^3*c^6*d)/5 + 7*a^3*c^3*d^4 + (63*a*b^2*c^5*d^2)/5 + 21*a^2*b*c^4*d^3) + x^4*((b^3*c^7)/4 + (35*a^3*c^4*d^3)/4 + (63*a^2*b*c^5*d^2)/4 + (21*a*b^2*c^6*d)/4) + x^8*((a^3*d^7)/8 + (35*b^3*c^3*d^4)/8 + (63*a*b^2*c^2*d^5)/8 + (21*a^2*b*c*d^6)/8) + a^3*c^7*x + (b^3*d^7*x^11)/11 + (7*c^2*d^2*x^6*(a^3*d^3 + b^3*c^3 + 5*a*b^2*c^2*d + 5*a^2*b*c*d^2))/2 + (a^2*c^6*x^2*(7*a*d + 3*b*c))/2 + (b^2*d^6*x^10*(3*a*d + 7*b*c))/10 + a*c^5*x^3*(7*a^2*d^2 + b^2*c^2 + 7*a*b*c*d) + (b*d^5*x^9*(a^2*d^2 + 7*b^2*c^2 + 7*a*b*c*d))/3$

sympy [B] time = 0.13, size = 427, normalized size = 4.64

$$a^3c^7x + \frac{b^3d^7x^{11}}{11} + x^{10}\left(\frac{3ab^2d^7}{10} + \frac{7b^3cd^6}{10}\right) + x^9\left(\frac{a^2bd^7}{3} + \frac{7ab^2cd^6}{3} + \frac{7b^3c^2d^5}{3}\right) + x^8\left(\frac{a^3d^7}{8} + \frac{21a^2bcd^6}{8} + \frac{63ab^2c^2d^5}{8}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3*(d*x+c)**7,x)`

[Out] $a**3*c**7*x + b**3*d**7*x**11/11 + x**10*(3*a*b**2*d**7/10 + 7*b**3*c*d**6/10) + x**9*(a**2*b*d**7/3 + 7*a*b**2*c*d**6/3 + 7*b**3*c**2*d**5/3) + x**8*(a**3*d**7/8 + 21*a**2*b*c*d**6/8 + 63*a*b**2*c**2*d**5/8 + 35*b**3*c**3*d**4/8) + x**7*(a**3*c*d**6 + 9*a**2*b*c**2*d**5 + 15*a*b**2*c**3*d**4 + 5*b**3*c**4*d**3) + x**6*(7*a**3*c**2*d**5/2 + 35*a**2*b*c**3*d**4/2 + 35*a*b**2*c**4*d**3/2 + 7*b**3*c**5*d**2/2) + x**5*(7*a**3*c**3*d**4 + 21*a**2*b*c**4*d**3 + 63*a*b**2*c**5*d**2/5 + 7*b**3*c**6*d/5) + x**4*(35*a**3*c**4*d**3/4 + 63*a**2*b*c**5*d**2/4 + 21*a*b**2*c**6*d/4 + b**3*c**7/4) + x**3*(7*a**3*c**5*d**2 + 7*a**2*b*c**6*d + a*b**2*c**7) + x**2*(7*a**3*c**6*d/2 + 3*a**2*b*c**7/2)$

3.1280 $\int (a + bx)^2 (c + dx)^7 dx$

Optimal. Leaf size=65

$$-\frac{2b(c + dx)^9(bc - ad)}{9d^3} + \frac{(c + dx)^8(bc - ad)^2}{8d^3} + \frac{b^2(c + dx)^{10}}{10d^3}$$

[Out] $1/8*(-a*d+b*c)^2*(d*x+c)^8/d^3-2/9*b*(-a*d+b*c)*(d*x+c)^9/d^3+1/10*b^2*(d*x+c)^{10}/d^3$

Rubi [A] time = 0.16, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{2b(c + dx)^9(bc - ad)}{9d^3} + \frac{(c + dx)^8(bc - ad)^2}{8d^3} + \frac{b^2(c + dx)^{10}}{10d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(c + d*x)^7, x]

[Out] $((b*c - a*d)^2*(c + d*x)^8)/(8*d^3) - (2*b*(b*c - a*d)*(c + d*x)^9)/(9*d^3) + (b^2*(c + d*x)^{10})/(10*d^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2 (c + dx)^7 dx &= \int \left(\frac{(-bc + ad)^2 (c + dx)^7}{d^2} - \frac{2b(bc - ad)(c + dx)^8}{d^2} + \frac{b^2(c + dx)^9}{d^2} \right) dx \\ &= \frac{(bc - ad)^2 (c + dx)^8}{8d^3} - \frac{2b(bc - ad)(c + dx)^9}{9d^3} + \frac{b^2(c + dx)^{10}}{10d^3} \end{aligned}$$

Mathematica [B] time = 0.03, size = 261, normalized size = 4.02

$$\frac{1}{8}d^5x^8(a^2d^2 + 14abcd + 21b^2c^2) + cd^4x^7(a^2d^2 + 6abcd + 5b^2c^2) + \frac{7}{6}c^2d^3x^6(3a^2d^2 + 10abcd + 5b^2c^2) + \frac{1}{3}c^5x^3(21a^2$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(c + d*x)^7,x]

[Out] $a^2c^7x + (a^2c^6(2bc + 7ad)x^2)/2 + (c^5(b^2c^2 + 14abc + 21a^2d^2)x^3)/3 + (7c^4d(b^2c^2 + 6abc + 5a^2d^2)x^4)/4 + (7c^3d^2(3b^2c^2 + 10abc + 5a^2d^2)x^5)/5 + (7c^2d^3(5b^2c^2 + 10abc + 3a^2d^2)x^6)/6 + cd^4(5b^2c^2 + 6abc + a^2d^2)x^7 + (d^5(21b^2c^2 + 14abc + a^2d^2)x^8)/8 + (bd^6(7bc + 2ad)x^9)/9 + (b^2d^7x^{10})/10$

fricas [B] time = 0.39, size = 294, normalized size = 4.52

$$\frac{1}{10}x^{10}d^7b^2 + \frac{7}{9}x^9d^6cb^2 + \frac{2}{9}x^9d^7ba + \frac{21}{8}x^8d^5c^2b^2 + \frac{7}{4}x^8d^6cba + \frac{1}{8}x^8d^7a^2 + 5x^7d^4c^3b^2 + 6x^7d^5c^2ba + x^7d^6ca^2 + \frac{35}{6}x^6d^3c^4b^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^7,x, algorithm="fricas")

[Out] $1/10x^{10}d^7b^2 + 7/9x^9d^6c^2b^2 + 2/9x^9d^7b^2a + 21/8x^8d^5c^2b^2 + 7/4x^8d^6c^2b^2a + 1/8x^8d^7c^2a^2 + 5x^7d^4c^3b^2 + 6x^7d^5c^2b^2a + x^7d^6c^2a^2 + 35/6x^6d^3c^4b^2 + 35/3x^6d^4c^3b^2a + 7/2x^6d^5c^2a^2 + 21/5x^5d^2c^5b^2 + 14x^5d^3c^4b^2a + 7x^5d^4c^3a^2 + 7/4x^4d^6c^6b^2 + 21/2x^4d^2c^5b^2a + 35/4x^4d^3c^4a^2 + 1/3x^3c^7b^2 + 14/3x^3d^6c^6b^2a + 7x^3d^2c^5a^2 + x^2c^7b^2a + 7/2x^2d^6c^6a^2 + xc^7a^2$

giac [B] time = 1.24, size = 294, normalized size = 4.52

$$\frac{1}{10}b^2d^7x^{10} + \frac{7}{9}b^2cd^6x^9 + \frac{2}{9}abd^7x^9 + \frac{21}{8}b^2c^2d^5x^8 + \frac{7}{4}abcd^6x^8 + \frac{1}{8}a^2d^7x^8 + 5b^2c^3d^4x^7 + 6abc^2d^5x^7 + a^2cd^6x^7 + \frac{35}{6}b^2c^4d^3x^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^7,x, algorithm="giac")

[Out] $1/10b^2d^7x^{10} + 7/9b^2c^2d^6x^9 + 2/9a^2bd^7x^9 + 21/8b^2c^2d^5x^8 + 7/4a^2bcd^6x^8 + 1/8a^2d^7x^8 + 5b^2c^3d^4x^7 + 6a^2bcd^5x^7 + a^2c^2d^6x^7 + 35/6b^2c^4d^3x^6 + 35/3a^2bcd^4x^6 + 7/2a^2c^2d^5x^6 + 21/5b^2c^5d^2x^5 + 14a^2bcd^4d^3x^5 + 7a^2c^3d^4x^5 + 7/4b^2c^6d^6x^4 + 21/2a^2bcd^5d^2x^4 + 35/4a^2c^4d^3x^4 + 1/3b^2c^7x^3 + 14/3a^2bcd^6d^6x^3 + 7a^2c^5d^2x^3 + abc^7x^2 + 7/2a^2c^6d^6x^2 + a^2c^7x$

maple [B] time = 0.00, size = 277, normalized size = 4.26

$$\frac{b^2d^7x^{10}}{10} + a^2c^7x + \frac{(2abd^7 + 7b^2cd^6)x^9}{9} + \frac{(a^2d^7 + 14abcd^6 + 21b^2c^2d^5)x^8}{8} + \frac{(7a^2cd^6 + 42abc^2d^5 + 35b^2c^3d^4)x^7}{7} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2*(d*x+c)^7,x)`

[Out] $1/10*b^2*d^7*x^{10}+1/9*(2*a*b*d^7+7*b^2*c*d^6)*x^9+1/8*(a^2*d^7+14*a*b*c*d^6+21*b^2*c^2*d^5)*x^8+1/7*(7*a^2*c*d^6+42*a*b*c^2*d^5+35*b^2*c^3*d^4)*x^7+1/6*(21*a^2*c^2*d^5+70*a*b*c^3*d^4+35*b^2*c^4*d^3)*x^6+1/5*(35*a^2*c^3*d^4+70*a*b*c^4*d^3+21*b^2*c^5*d^2)*x^5+1/4*(35*a^2*c^4*d^3+42*a*b*c^5*d^2+7*b^2*c^6*d)*x^4+1/3*(21*a^2*c^5*d^2+14*a*b*c^6*d+b^2*c^7)*x^3+1/2*(7*a^2*c^6*d+2*a*b*c^7)*x^2+a^2*c^7*x$

maxima [B] time = 1.36, size = 273, normalized size = 4.20

$$\frac{1}{10} b^2 d^7 x^{10} + a^2 c^7 x + \frac{1}{9} (7 b^2 c d^6 + 2 a b d^7) x^9 + \frac{1}{8} (21 b^2 c^2 d^5 + 14 a b c d^6 + a^2 d^7) x^8 + (5 b^2 c^3 d^4 + 6 a b c^2 d^5 + a^2 c d^6) x^7 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2*(d*x+c)^7,x, algorithm="maxima")`

[Out] $1/10*b^2*d^7*x^{10} + a^2*c^7*x + 1/9*(7*b^2*c*d^6 + 2*a*b*d^7)*x^9 + 1/8*(21*b^2*c^2*d^5 + 14*a*b*c*d^6 + a^2*d^7)*x^8 + (5*b^2*c^3*d^4 + 6*a*b*c^2*d^5 + a^2*c*d^6)*x^7 + 7/6*(5*b^2*c^4*d^3 + 10*a*b*c^3*d^4 + 3*a^2*c^2*d^5)*x^6 + 7/5*(3*b^2*c^5*d^2 + 10*a*b*c^4*d^3 + 5*a^2*c^3*d^4)*x^5 + 7/4*(b^2*c^6*d + 6*a*b*c^5*d^2 + 5*a^2*c^4*d^3)*x^4 + 1/3*(b^2*c^7 + 14*a*b*c^6*d + 21*a^2*c^5*d^2)*x^3 + 1/2*(2*a*b*c^7 + 7*a^2*c^6*d)*x^2$

mupad [B] time = 0.11, size = 249, normalized size = 3.83

$$x^3 \left(7 a^2 c^5 d^2 + \frac{14 a b c^6 d}{3} + \frac{b^2 c^7}{3} \right) + x^8 \left(\frac{a^2 d^7}{8} + \frac{7 a b c d^6}{4} + \frac{21 b^2 c^2 d^5}{8} \right) + a^2 c^7 x + \frac{b^2 d^7 x^{10}}{10} + \frac{a c^6 x^2 (7 a d + 2 b c)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2*(c + d*x)^7,x)`

[Out] $x^3*((b^2*c^7)/3 + 7*a^2*c^5*d^2 + (14*a*b*c^6*d)/3) + x^8*((a^2*d^7)/8 + (21*b^2*c^2*d^5)/8 + (7*a*b*c*d^6)/4) + a^2*c^7*x + (b^2*d^7*x^{10})/10 + (a*c^6*x^2*(7*a*d + 2*b*c))/2 + (b*d^6*x^9*(2*a*d + 7*b*c))/9 + (7*c^4*d*x^4*(5*a^2*d^2 + b^2*c^2 + 6*a*b*c*d))/4 + c*d^4*x^7*(a^2*d^2 + 5*b^2*c^2 + 6*a*b*c*d) + (7*c^3*d^2*x^5*(5*a^2*d^2 + 3*b^2*c^2 + 10*a*b*c*d))/5 + (7*c^2*d^3*x^6*(3*a^2*d^2 + 5*b^2*c^2 + 10*a*b*c*d))/6$

sympy [B] time = 0.12, size = 303, normalized size = 4.66

$$a^2 c^7 x + \frac{b^2 d^7 x^{10}}{10} + x^9 \left(\frac{2 a b d^7}{9} + \frac{7 b^2 c d^6}{9} \right) + x^8 \left(\frac{a^2 d^7}{8} + \frac{7 a b c d^6}{4} + \frac{21 b^2 c^2 d^5}{8} \right) + x^7 (a^2 c d^6 + 6 a b c^2 d^5 + 5 b^2 c^3 d^4) + x^6 \left(\frac{7 a}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(d*x+c)**7,x)`

[Out] $a^{**2}c^{**7}x + b^{**2}d^{**7}x^{**10}/10 + x^{**9}(2*a*b*d^{**7}/9 + 7*b^{**2}c*d^{**6}/9) + x^{**8}(a^{**2}d^{**7}/8 + 7*a*b*c*d^{**6}/4 + 21*b^{**2}c^{**2}d^{**5}/8) + x^{**7}(a^{**2}c*d^{**6} + 6*a*b*c^{**2}d^{**5} + 5*b^{**2}c^{**3}d^{**4}) + x^{**6}(7*a^{**2}c^{**2}d^{**5}/2 + 35*a*b*c^{**3}d^{**4}/3 + 35*b^{**2}c^{**4}d^{**3}/6) + x^{**5}(7*a^{**2}c^{**3}d^{**4} + 14*a*b*c^{**4}d^{**3} + 21*b^{**2}c^{**5}d^{**2}/5) + x^{**4}(35*a^{**2}c^{**4}d^{**3}/4 + 21*a*b*c^{**5}d^{**2}/2 + 7*b^{**2}c^{**6}d/4) + x^{**3}(7*a^{**2}c^{**5}d^{**2} + 14*a*b*c^{**6}d/3 + b^{**2}c^{**7}/3) + x^{**2}(7*a^{**2}c^{**6}d/2 + a*b*c^{**7})$

3.1281 $\int (a + bx)(c + dx)^7 dx$

Optimal. Leaf size=38

$$\frac{b(c + dx)^9}{9d^2} - \frac{(c + dx)^8(bc - ad)}{8d^2}$$

[Out] $-1/8*(-a*d+b*c)*(d*x+c)^8/d^2+1/9*b*(d*x+c)^9/d^2$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{b(c + dx)^9}{9d^2} - \frac{(c + dx)^8(bc - ad)}{8d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(c + d*x)^7, x]

[Out] $-((b*c - a*d)*(c + d*x)^8)/(8*d^2) + (b*(c + d*x)^9)/(9*d^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)(c + dx)^7 dx &= \int \left(\frac{(-bc + ad)(c + dx)^7}{d} + \frac{b(c + dx)^8}{d} \right) dx \\ &= -\frac{(bc - ad)(c + dx)^8}{8d^2} + \frac{b(c + dx)^9}{9d^2} \end{aligned}$$

Mathematica [B] time = 0.02, size = 151, normalized size = 3.97

$$\frac{1}{2}c^6x^2(7ad+bc)+\frac{7}{3}c^5dx^3(3ad+bc)+\frac{7}{4}c^4d^2x^4(5ad+3bc)+7c^3d^3x^5(ad+bc)+\frac{7}{6}c^2d^4x^6(3ad+5bc)+\frac{1}{8}d^6x^8(ad+7bc)+cd^7x^9$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(c + d*x)^7, x]

[Out] $a*c^7*x + (c^6*(b*c + 7*a*d)*x^2)/2 + (7*c^5*d*(b*c + 3*a*d)*x^3)/3 + (7*c^4*d^2*(3*b*c + 5*a*d)*x^4)/4 + 7*c^3*d^3*(b*c + a*d)*x^5 + (7*c^2*d^4*(5*b*c + 3*a*d)*x^6)/6 + c*d^5*(3*b*c + a*d)*x^7 + (d^6*(7*b*c + a*d)*x^8)/8 + (b*d^7*x^9)/9$

fricas [B] time = 0.40, size = 169, normalized size = 4.45

$$\frac{1}{9}x^9d^7b + \frac{7}{8}x^8d^6cb + \frac{1}{8}x^8d^7a + 3x^7d^5c^2b + x^7d^6ca + \frac{35}{6}x^6d^4c^3b + \frac{7}{2}x^6d^5c^2a + 7x^5d^3c^4b + 7x^5d^4c^3a + \frac{21}{4}x^4d^2c^5b + \frac{35}{4}x^4d^3c^4a + \frac{7}{3}x^3d^6c^2b + 7x^3d^7c^3a + \frac{1}{2}x^2d^9c^4b + \frac{7}{2}x^2d^8c^5a + x^2d^7c^6b + \frac{1}{2}x^2d^6c^7a + x^2d^5c^8a + \frac{1}{2}x^2d^4c^9a + \frac{1}{2}x^2d^3c^{10}a + \frac{1}{2}x^2d^2c^{11}a + \frac{1}{2}x^2d^1c^{12}a + \frac{1}{2}x^2d^0c^{13}a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^7,x, algorithm="fricas")

[Out] $1/9*x^9*d^7*b + 7/8*x^8*d^6*c*b + 1/8*x^8*d^7*a + 3*x^7*d^5*c^2*b + x^7*d^6*c*a + 35/6*x^6*d^4*c^3*b + 7/2*x^6*d^5*c^2*a + 7*x^5*d^3*c^4*b + 7*x^5*d^4*c^3*a + 21/4*x^4*d^2*c^5*b + 35/4*x^4*d^3*c^4*a + 7/3*x^3*d^6*c^2*b + 7*x^3*d^7*c^3*a + 1/2*x^2*d^9*c^4*b + 7/2*x^2*d^8*c^5*a + x^2*d^7*c^6*b + 1/2*x^2*d^6*c^7*a + x^2*d^5*c^8*a + 1/2*x^2*d^4*c^9*a + 1/2*x^2*d^3*c^{10}a + 1/2*x^2*d^2*c^{11}a + 1/2*x^2*d^1*c^{12}a + 1/2*x^2*d^0*c^{13}a$

giac [B] time = 1.30, size = 169, normalized size = 4.45

$$\frac{1}{9}bd^7x^9 + \frac{7}{8}bcd^6x^8 + \frac{1}{8}ad^7x^8 + 3bc^2d^5x^7 + acd^6x^7 + \frac{35}{6}bc^3d^4x^6 + \frac{7}{2}ac^2d^5x^6 + 7bc^4d^3x^5 + 7ac^3d^4x^5 + \frac{21}{4}bc^5d^2x^4 + \frac{35}{4}bc^4d^3x^4 + \frac{7}{3}bc^6d^1x^3 + 7ac^7d^0x^3 + \frac{1}{2}bc^8d^0x^2 + \frac{7}{2}ac^9d^0x^2 + ac^{10}d^0x^2 + \frac{1}{2}bc^{11}d^0x^1 + \frac{7}{2}ac^{12}d^0x^1 + ac^{13}d^0x^1$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^7,x, algorithm="giac")

[Out] $1/9*b*d^7*x^9 + 7/8*b*c*d^6*x^8 + 1/8*a*d^7*x^8 + 3*b*c^2*d^5*x^7 + a*c*d^6*x^7 + 35/6*b*c^3*d^4*x^6 + 7/2*a*c^2*d^5*x^6 + 7*b*c^4*d^3*x^5 + 7*a*c^3*d^4*x^5 + 21/4*b*c^5*d^2*x^4 + 35/4*a*c^4*d^3*x^4 + 7/3*b*c^6*d*x^3 + 7*a*c^5*d^2*x^3 + 1/2*b*c^7*x^2 + 7/2*a*c^6*d*x^2 + a*c^7*x^2 + 1/2*b*c^8*d*x^1 + 7/2*a*c^7*d*x^1 + a*c^8*d*x^1 + 1/2*b*c^9*d^0*x^1 + 7/2*a*c^8*d^0*x^1 + a*c^9*d^0*x^1 + 1/2*b*c^{10}d^0*x^1 + 7/2*a*c^9*d^0*x^1 + a*c^{10}d^0*x^1 + 1/2*b*c^{11}d^0*x^1 + 7/2*a*c^{10}d^0*x^1 + a*c^{11}d^0*x^1 + 1/2*b*c^{12}d^0*x^1 + 7/2*a*c^{11}d^0*x^1 + a*c^{12}d^0*x^1 + 1/2*b*c^{13}d^0*x^1 + 7/2*a*c^{12}d^0*x^1 + a*c^{13}d^0*x^1$

maple [B] time = 0.00, size = 169, normalized size = 4.45

$$\frac{bd^7x^9}{9} + ac^7x + \frac{(ad^7 + 7bcd^6)x^8}{8} + \frac{(7acd^6 + 21bc^2d^5)x^7}{7} + \frac{(21ac^2d^5 + 35bc^3d^4)x^6}{6} + \frac{(35ac^3d^4 + 35bc^4d^3)x^5}{5} + \frac{(35ac^4d^3 + 35bc^5d^2)x^4}{4} + \frac{(7ac^5d^2 + 7bc^6d)x^3}{3} + \frac{(7ac^6d + bc^7)x^2}{2} + ac^7x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(d*x+c)^7,x)

[Out] $1/9*b*d^7*x^9 + 1/8*(a*d^7 + 7*b*c*d^6)*x^8 + 1/7*(7*a*c*d^6 + 21*b*c^2*d^5)*x^7 + 1/6*(21*a*c^2*d^5 + 35*b*c^3*d^4)*x^6 + 1/5*(35*a*c^3*d^4 + 35*b*c^4*d^3)*x^5 + 1/4*(35*a*c^4*d^3 + 21*b*c^5*d^2)*x^4 + 1/3*(21*a*c^5*d^2 + 7*b*c^6*d)*x^3 + 1/2*(7*a*c^6*d + b*c^7)*x^2 + a*c^7*x$

3.1282 $\int (c + dx)^7 dx$

Optimal. Leaf size=14

$$\frac{(c + dx)^8}{8d}$$

[Out] $1/8*(d*x+c)^8/d$

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(c + dx)^8}{8d}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7, x]

[Out] (c + d*x)^8/(8*d)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (c + dx)^7 dx = \frac{(c + dx)^8}{8d}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{(c + dx)^8}{8d}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7, x]

[Out] (c + d*x)^8/(8*d)

fricas [B] time = 0.38, size = 75, normalized size = 5.36

$$\frac{1}{8}x^8d^7 + x^7d^6c + \frac{7}{2}x^6d^5c^2 + 7x^5d^4c^3 + \frac{35}{4}x^4d^3c^4 + 7x^3d^2c^5 + \frac{7}{2}x^2dc^6 + xc^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7,x, algorithm="fricas")

[Out] $\frac{1}{8}x^8d^7 + x^7d^6c + \frac{7}{2}x^6d^5c^2 + 7x^5d^4c^3 + \frac{35}{4}x^4d^3c^4 + 7x^3d^2c^5 + \frac{7}{2}x^2dc^6 + xc^7$

giac [A] time = 1.30, size = 12, normalized size = 0.86

$$\frac{(dx + c)^8}{8d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7,x, algorithm="giac")

[Out] $\frac{1}{8}(dx + c)^8/d$

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{(dx + c)^8}{8d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7,x)

[Out] $\frac{1}{8}(dx+c)^8/d$

maxima [A] time = 1.32, size = 12, normalized size = 0.86

$$\frac{(dx + c)^8}{8d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7,x, algorithm="maxima")

[Out] $\frac{1}{8}(dx + c)^8/d$

mupad [B] time = 0.06, size = 75, normalized size = 5.36

$$c^7x + \frac{7c^6dx^2}{2} + 7c^5d^2x^3 + \frac{35c^4d^3x^4}{4} + 7c^3d^4x^5 + \frac{7c^2d^5x^6}{2} + cd^6x^7 + \frac{d^7x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7,x)

[Out] $c^7x + (d^7x^8)/8 + (7c^6d^2x^2)/2 + cd^6x^7 + 7c^5d^2x^3 + (35c^4d^3x^4)/4 + 7c^3d^4x^5 + (7c^2d^5x^6)/2$

sympy [B] time = 0.08, size = 83, normalized size = 5.93

$$c^7x + \frac{7c^6dx^2}{2} + 7c^5d^2x^3 + \frac{35c^4d^3x^4}{4} + 7c^3d^4x^5 + \frac{7c^2d^5x^6}{2} + cd^6x^7 + \frac{d^7x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7,x)

[Out] $c**7*x + 7*c**6*d*x**2/2 + 7*c**5*d**2*x**3 + 35*c**4*d**3*x**4/4 + 7*c**3*d**4*x**5 + 7*c**2*d**5*x**6/2 + c*d**6*x**7 + d**7*x**8/8$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x),x]

[Out] (d*x*(420*a^6*d^6 - 210*a^5*b*d^5*(14*c + d*x) + 70*a^4*b^2*d^4*(126*c^2 + 21*c*d*x + 2*d^2*x^2) - 35*a^3*b^3*d^3*(420*c^3 + 126*c^2*d*x + 28*c*d^2*x^2 + 3*d^3*x^3) + 21*a^2*b^4*d^2*(700*c^4 + 350*c^3*d*x + 140*c^2*d^2*x^2 + 35*c*d^3*x^3 + 4*d^4*x^4) - 7*a*b^5*d*(1260*c^5 + 1050*c^4*d*x + 700*c^3*d^2*x^2 + 315*c^2*d^3*x^3 + 84*c*d^4*x^4 + 10*d^5*x^5) + b^6*(2940*c^6 + 4410*c^5*d*x + 4900*c^4*d^2*x^2 + 3675*c^3*d^3*x^3 + 1764*c^2*d^4*x^4 + 490*c*d^5*x^5 + 60*d^6*x^6)))/(420*b^7) + ((b*c - a*d)^7*Log[a + b*x])/b^8

fricas [B] time = 0.43, size = 462, normalized size = 2.73

$$\frac{60 b^7 d^7 x^7 + 70 (7 b^7 c d^6 - a b^6 d^7) x^6 + 84 (21 b^7 c^2 d^5 - 7 a b^6 c d^6 + a^2 b^5 d^7) x^5 + 105 (35 b^7 c^3 d^4 - 21 a b^6 c^2 d^5 + 7 a^2 b^5 c d^6 - a^3 b^4 d^7) x^4 + 140 (35 b^7 c^4 d^3 - 35 a b^6 c^3 d^4 + 21 a^2 b^5 c^2 d^5 - 7 a^3 b^4 c d^6 + a^4 b^3 d^7) x^3 + 210 (21 b^7 c^5 d^2 - 35 a b^6 c^4 d^3 + 35 a^2 b^5 c^3 d^4 - 21 a^3 b^4 c^2 d^5 + 7 a^4 b^3 c d^6 - a^5 b^2 d^7) x^2 + 420 (7 b^7 c^6 d - 21 a b^6 c^5 d^2 + 35 a^2 b^5 c^4 d^3 - 35 a^3 b^4 c^3 d^4 + 21 a^4 b^3 c^2 d^5 - 7 a^5 b^2 c d^6 + a^6 b d^7) x + 420 (b^7 c^7 - 7 a b^6 c^6 d + 21 a^2 b^5 c^5 d^2 - 35 a^3 b^4 c^4 d^3 + 35 a^4 b^3 c^3 d^4 - 21 a^5 b^2 c^2 d^5 + 7 a^6 b c d^6 - a^7 d^7) \log(b x + a)}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a),x, algorithm="fricas")

[Out] 1/420*(60*b^7*d^7*x^7 + 70*(7*b^7*c*d^6 - a*b^6*d^7)*x^6 + 84*(21*b^7*c^2*d^5 - 7*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 105*(35*b^7*c^3*d^4 - 21*a*b^6*c^2*d^5 + 7*a^2*b^5*c*d^6 - a^3*b^4*d^7)*x^4 + 140*(35*b^7*c^4*d^3 - 35*a*b^6*c^3*d^4 + 21*a^2*b^5*c^2*d^5 - 7*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 210*(21*b^7*c^5*d^2 - 35*a*b^6*c^4*d^3 + 35*a^2*b^5*c^3*d^4 - 21*a^3*b^4*c^2*d^5 + 7*a^4*b^3*c*d^6 - a^5*b^2*d^7)*x^2 + 420*(7*b^7*c^6*d - 21*a*b^6*c^5*d^2 + 35*a^2*b^5*c^4*d^3 - 35*a^3*b^4*c^3*d^4 + 21*a^4*b^3*c^2*d^5 - 7*a^5*b^2*c*d^6 + a^6*b*d^7)*x + 420*(b^7*c^7 - 7*a*b^6*c^6*d + 21*a^2*b^5*c^5*d^2 - 35*a^3*b^4*c^4*d^3 + 35*a^4*b^3*c^3*d^4 - 21*a^5*b^2*c^2*d^5 + 7*a^6*b*c*d^6 - a^7*d^7)*log(b*x + a))/b^8

giac [B] time = 1.30, size = 497, normalized size = 2.94

$$\frac{60 b^6 d^7 x^7 + 490 b^6 c d^6 x^6 - 70 a b^5 d^7 x^6 + 1764 b^6 c^2 d^5 x^5 - 588 a b^5 c d^6 x^5 + 84 a^2 b^4 d^7 x^5 + 3675 b^6 c^3 d^4 x^4 - 2205 a b^5 c^2 d^5 x^4 + 735 a^2 b^4 c d^6 x^4 - 105 a^3 b^3 d^7 x^4 + 4900 b^6 c^4 d^3 x^3 - 4900 a b^5 c^3 d^4 x^3 + 2940 a^2 b^4 c^2 d^5 x^3 - 980 a^3 b^3 c d^6 x^3 + 140 a^4 b^2 d^7 x^3 + 4410 b^6 c^5 d^2 x^2 - 7350 a b^5 c^4 d^3 x^2 + 7350 a^2 b^4 c^3 d^4 x^2 - 4410 a^3 b^3 c^2 d^5 x^2 + 1470 a^4 b^2 c d^6 x^2 - 1470 a^5 b c d^7 x^2 + 420 a^6 b^2 c^2 d^6 x^2 - 420 a^7 b c^2 d^7 x^2 + 420 a^8 b^2 c^2 d^7 x^2 + 420 a^9 b^2 c^2 d^7 x^2}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a),x, algorithm="giac")

[Out] 1/420*(60*b^6*d^7*x^7 + 490*b^6*c*d^6*x^6 - 70*a*b^5*d^7*x^6 + 1764*b^6*c^2*d^5*x^5 - 588*a*b^5*c*d^6*x^5 + 84*a^2*b^4*d^7*x^5 + 3675*b^6*c^3*d^4*x^4 - 2205*a*b^5*c^2*d^5*x^4 + 735*a^2*b^4*c*d^6*x^4 - 105*a^3*b^3*d^7*x^4 + 4900*b^6*c^4*d^3*x^3 - 4900*a*b^5*c^3*d^4*x^3 + 2940*a^2*b^4*c^2*d^5*x^3 - 980*a^3*b^3*c*d^6*x^3 + 140*a^4*b^2*d^7*x^3 + 4410*b^6*c^5*d^2*x^2 - 7350*a*b^5*c^4*d^3*x^2 + 7350*a^2*b^4*c^3*d^4*x^2 - 4410*a^3*b^3*c^2*d^5*x^2 + 1470

mupad [B] time = 0.22, size = 509, normalized size = 3.01

$$\begin{aligned}
 & \left(\frac{7c^6 d}{b} - \frac{a \left(\frac{35c^3 d^4}{b} - \frac{a \left(\frac{a d^7}{b^2} - \frac{7c d^6}{b} \right) + \frac{21c^2 d^5}{b} \right)}{b} \right) \\
 & - x^6 \left(\frac{a d^7}{6b^2} - \frac{7c d^6}{6b} \right) + x^4 \left(\frac{35c^3 d^4}{4b} - \frac{a \left(\frac{a d^7}{b^2} - \frac{7c d^6}{b} \right) + \frac{21c^2 d^5}{b}}{b} \right)
 \end{aligned}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^7/(a + b*x),x)`

[Out] $x*((7*c^6*d)/b - (a*((a*((a*((35*c^3*d^4)/b - (a*((a*((a*d^7)/b^2 - (7*c*d^6)/b))/b + (21*c^2*d^5)/b))/b - (35*c^4*d^3)/b))/b + (21*c^5*d^2)/b)) - x^6*((a*d^7)/(6*b^2) - (7*c*d^6)/(6*b)) + x^4*((35*c^3*d^4)/(4*b) - (a*((a*((a*d^7)/b^2 - (7*c*d^6)/b))/b + (21*c^2*d^5)/b))/(4*b)) + x^2*((a*((a*((35*c^3*d^4)/b - (a*((a*((a*d^7)/b^2 - (7*c*d^6)/b))/b + (21*c^2*d^5)/b))/b - (35*c^4*d^3)/b))/(2*b) + (21*c^5*d^2)/(2*b)) + x^5*((a*((a*d^7)/b^2 - (7*c*d^6)/b))/(5*b) + (21*c^2*d^5)/(5*b)) - x^3*((a*((35*c^3*d^4)/b - (a*((a*((a*d^7)/b^2 - (7*c*d^6)/b))/b + (21*c^2*d^5)/b))/b)/(3*b) - (35*c^4*d^3)/(3*b)) - (\log(a + b*x)*(a^7*d^7 - b^7*c^7 - 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 - 35*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 7*a^6*b*c*d^6))/b^8 + (d^7*x^7)/(7*b)$

sympy [B] time = 0.80, size = 408, normalized size = 2.41

$$x^6 \left(-\frac{ad^7}{6b^2} + \frac{7cd^6}{6b} \right) + x^5 \left(\frac{a^2d^7}{5b^3} - \frac{7acd^6}{5b^2} + \frac{21c^2d^5}{5b} \right) + x^4 \left(-\frac{a^3d^7}{4b^4} + \frac{7a^2cd^6}{4b^3} - \frac{21ac^2d^5}{4b^2} + \frac{35c^3d^4}{4b} \right) + x^3 \left(\frac{a^4d^7}{3b^5} - \frac{7a^3cd^6}{3b^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**7/(b*x+a),x)`

[Out] $x**6*(-a*d**7/(6*b**2) + 7*c*d**6/(6*b)) + x**5*(a**2*d**7/(5*b**3) - 7*a*c*d**6/(5*b**2) + 21*c**2*d**5/(5*b)) + x**4*(-a**3*d**7/(4*b**4) + 7*a**2*c*d**6/(4*b**3) - 21*a*c**2*d**5/(4*b**2) + 35*c**3*d**4/(4*b)) + x**3*(a**4*d**7/(3*b**5) - 7*a**3*c*d**6/(3*b**4) + 7*a**2*c**2*d**5/b**3 - 35*a*c**3*d**4/(3*b**2) + 35*c**4*d**3/(3*b)) + x**2*(-a**5*d**7/(2*b**6) + 7*a**4*c*d**6/(2*b**5) - 21*a**3*c**2*d**5/(2*b**4) + 35*a**2*c**3*d**4/(2*b**3) - 35*a*c**4*d**3/(2*b**2) + 21*c**5*d**2/(2*b)) + x*(a**6*d**7/b**7 - 7*a**5*c*d**6/b**6 + 21*a**4*c**2*d**5/b**5 - 35*a**3*c**3*d**4/b**4 + 35*a**2*c**4*d**3/b**3 - 21*a*c**5*d**2/b**2 + 7*c**6*d/b) + d**7*x**7/(7*b) - (a*d - b*c)**7*log(a + b*x)/b**8$

$$3.1284 \quad \int \frac{(c+dx)^7}{(a+bx)^2} dx$$

Optimal. Leaf size=187

$$\frac{7d^6(a+bx)^5(bc-ad)}{5b^8} + \frac{21d^5(a+bx)^4(bc-ad)^2}{4b^8} + \frac{35d^4(a+bx)^3(bc-ad)^3}{3b^8} + \frac{35d^3(a+bx)^2(bc-ad)^4}{2b^8} - \frac{(bc-ad)^7}{b^8(a+bx)}$$

[Out] $21*d^2*(-a*d+b*c)^5*x/b^7 - (-a*d+b*c)^7/b^8/(b*x+a) + 35/2*d^3*(-a*d+b*c)^4*(b*x+a)^2/b^8 + 35/3*d^4*(-a*d+b*c)^3*(b*x+a)^3/b^8 + 21/4*d^5*(-a*d+b*c)^2*(b*x+a)^4/b^8 + 7/5*d^6*(-a*d+b*c)*(b*x+a)^5/b^8 + 1/6*d^7*(b*x+a)^6/b^8 + 7*d*(-a*d+b*c)^6*\ln(b*x+a)/b^8$

Rubi [A] time = 0.23, antiderivative size = 187, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{7d^6(a+bx)^5(bc-ad)}{5b^8} + \frac{21d^5(a+bx)^4(bc-ad)^2}{4b^8} + \frac{35d^4(a+bx)^3(bc-ad)^3}{3b^8} + \frac{35d^3(a+bx)^2(bc-ad)^4}{2b^8} + \frac{21d^2x(bc-ad)^7}{b^7}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^2, x]

[Out] $(21*d^2*(b*c - a*d)^5*x)/b^7 - (b*c - a*d)^7/(b^8*(a + b*x)) + (35*d^3*(b*c - a*d)^4*(a + b*x)^2)/(2*b^8) + (35*d^4*(b*c - a*d)^3*(a + b*x)^3)/(3*b^8) + (21*d^5*(b*c - a*d)^2*(a + b*x)^4)/(4*b^8) + (7*d^6*(b*c - a*d)*(a + b*x)^5)/(5*b^8) + (d^7*(a + b*x)^6)/(6*b^8) + (7*d*(b*c - a*d)^6*\text{Log}[a + b*x])/b^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^7}{(a+bx)^2} dx &= \int \left(\frac{21d^2(bc-ad)^5}{b^7} + \frac{(bc-ad)^7}{b^7(a+bx)^2} + \frac{7d(bc-ad)^6}{b^7(a+bx)} + \frac{35d^3(bc-ad)^4(a+bx)}{b^7} + \frac{35d^4(bc-ad)^3}{b^7} \right. \\ &= \frac{21d^2(bc-ad)^5x}{b^7} - \frac{(bc-ad)^7}{b^8(a+bx)} + \frac{35d^3(bc-ad)^4(a+bx)^2}{2b^8} + \frac{35d^4(bc-ad)^3(a+bx)^3}{3b^8} + \frac{21d^5(b}{b^7} \end{aligned}$$

Mathematica [B] time = 0.12, size = 388, normalized size = 2.07

$$\frac{60a^7d^7 - 60a^6bd^6(7c + 6dx) + 210a^5b^2d^5(6c^2 + 10cdx - d^2x^2) + 70a^4b^3d^4(-30c^3 - 72c^2dx + 18cd^2x^2 + d^3x^3) - \dots}{\dots}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^2,x]

[Out] (60*a^7*d^7 - 60*a^6*b*d^6*(7*c + 6*d*x) + 210*a^5*b^2*d^5*(6*c^2 + 10*c*d*x - d^2*x^2) + 70*a^4*b^3*d^4*(-30*c^3 - 72*c^2*d*x + 18*c*d^2*x^2 + d^3*x^3) - 35*a^3*b^4*d^3*(-60*c^4 - 180*c^3*d*x + 90*c^2*d^2*x^2 + 12*c*d^3*x^3 + d^4*x^4) + 21*a^2*b^5*d^2*(-60*c^5 - 200*c^4*d*x + 200*c^3*d^2*x^2 + 50*c^2*d^3*x^3 + 10*c*d^4*x^4 + d^5*x^5) - 7*a*b^6*d*(-60*c^6 - 180*c^5*d*x + 450*c^4*d^2*x^2 + 200*c^3*d^3*x^3 + 75*c^2*d^4*x^4 + 18*c*d^5*x^5 + 2*d^6*x^6) + b^7*(-60*c^7 + 1260*c^5*d^2*x^2 + 1050*c^4*d^3*x^3 + 700*c^3*d^4*x^4 + 315*c^2*d^5*x^5 + 84*c*d^6*x^6 + 10*d^7*x^7) + 420*d*(b*c - a*d)^6*(a + b*x)*Log[a + b*x])/(60*b^8*(a + b*x))

fricas [B] time = 0.42, size = 632, normalized size = 3.38

$$\frac{10b^7d^7x^7 - 60b^7c^7 + 420ab^6c^6d - 1260a^2b^5c^5d^2 + 2100a^3b^4c^4d^3 - 2100a^4b^3c^3d^4 + 1260a^5b^2c^2d^5 - 420a^6bcd^6}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^2,x, algorithm="fricas")

[Out] 1/60*(10*b^7*d^7*x^7 - 60*b^7*c^7 + 420*a*b^6*c^6*d - 1260*a^2*b^5*c^5*d^2 + 2100*a^3*b^4*c^4*d^3 - 2100*a^4*b^3*c^3*d^4 + 1260*a^5*b^2*c^2*d^5 - 420*a^6*b*c*d^6 + 60*a^7*d^7 + 14*(6*b^7*c*d^6 - a*b^6*d^7)*x^6 + 21*(15*b^7*c^2*d^5 - 6*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 35*(20*b^7*c^3*d^4 - 15*a*b^6*c^2*d^5 + 6*a^2*b^5*c*d^6 - a^3*b^4*d^7)*x^4 + 70*(15*b^7*c^4*d^3 - 20*a*b^6*c^3*d^4 + 15*a^2*b^5*c^2*d^5 - 6*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 210*(6*b^7*c^5*d^2 - 15*a*b^6*c^4*d^3 + 20*a^2*b^5*c^3*d^4 - 15*a^3*b^4*c^2*d^5 + 6*a^4*b^3*c*d^6 - a^5*b^2*d^7)*x^2 + 60*(21*a*b^6*c^5*d^2 - 70*a^2*b^5*c^4*d^3 + 105*a^3*b^4*c^3*d^4 - 84*a^4*b^3*c^2*d^5 + 35*a^5*b^2*c*d^6 - 6*a^6*b*d^7)*x + 420*(a*b^6*c^6*d - 6*a^2*b^5*c^5*d^2 + 15*a^3*b^4*c^4*d^3 - 20*a^4*b^3*c^3*d^4 + 15*a^5*b^2*c^2*d^5 - 6*a^6*b*c*d^6 + a^7*d^7 + (b^7*c^6*d - 6*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 - 20*a^3*b^4*c^3*d^4 + 15*a^4*b^3*c^2*d^5 - 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x)*log(b*x + a))/(b^9*x + a*b^8)

giac [B] time = 1.28, size = 567, normalized size = 3.03

$$\frac{\left(10d^7 + \frac{84(b^2cd^6 - abd^7)}{(bx+a)b} + \frac{315(b^4c^2d^5 - 2ab^3cd^6 + a^2b^2d^7)}{(bx+a)^2b^2} + \frac{700(b^6c^3d^4 - 3ab^5c^2d^5 + 3a^2b^4cd^6 - a^3b^3d^7)}{(bx+a)^3b^3} + \frac{1050(b^8c^4d^3 - 4ab^7c^3d^4 + 6a^2b^6c^2d^5 - 4a^3b^5cd^6 + 2a^4b^4c^2d^7 - 2a^5b^3cd^7 + a^6b^2cd^8 - a^7bd^9)}{(bx+a)^4b^4}\right)}{60b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^2,x, algorithm="giac")

[Out] $\frac{1}{60} \cdot (10 \cdot d^7 + 84 \cdot (b^2 \cdot c \cdot d^6 - a \cdot b \cdot d^7)) / ((b \cdot x + a) \cdot b) + 315 \cdot (b^4 \cdot c^2 \cdot d^5 - 2 \cdot a \cdot b^3 \cdot c \cdot d^6 + a^2 \cdot b^2 \cdot d^7) / ((b \cdot x + a)^2 \cdot b^2) + 700 \cdot (b^6 \cdot c^3 \cdot d^4 - 3 \cdot a \cdot b^5 \cdot c^2 \cdot d^5 + 3 \cdot a^2 \cdot b^4 \cdot c \cdot d^6 - a^3 \cdot b^3 \cdot d^7) / ((b \cdot x + a)^3 \cdot b^3) + 1050 \cdot (b^8 \cdot c^4 \cdot d^3 - 4 \cdot a \cdot b^7 \cdot c^3 \cdot d^4 + 6 \cdot a^2 \cdot b^6 \cdot c^2 \cdot d^5 - 4 \cdot a^3 \cdot b^5 \cdot c \cdot d^6 + a^4 \cdot b^4 \cdot d^7) / ((b \cdot x + a)^4 \cdot b^4) + 1260 \cdot (b^{10} \cdot c^5 \cdot d^2 - 5 \cdot a \cdot b^9 \cdot c^4 \cdot d^3 + 10 \cdot a^2 \cdot b^8 \cdot c^3 \cdot d^4 - 10 \cdot a^3 \cdot b^7 \cdot c^2 \cdot d^5 + 5 \cdot a^4 \cdot b^6 \cdot c \cdot d^6 - a^5 \cdot b^5 \cdot d^7) / ((b \cdot x + a)^5 \cdot b^5) \cdot (b \cdot x + a)^6 / b^8 - 7 \cdot (b^6 \cdot c^6 \cdot d - 6 \cdot a \cdot b^5 \cdot c^5 \cdot d^2 + 15 \cdot a^2 \cdot b^4 \cdot c^4 \cdot d^3 - 20 \cdot a^3 \cdot b^3 \cdot c^3 \cdot d^4 + 15 \cdot a^4 \cdot b^2 \cdot c^2 \cdot d^5 - 6 \cdot a^5 \cdot b \cdot c \cdot d^6 + a^6 \cdot d^7) \cdot \log(\text{abs}(b \cdot x + a) / ((b \cdot x + a)^2 \cdot \text{abs}(b))) / b^8 - (b^{13} \cdot c^7 / (b \cdot x + a) - 7 \cdot a \cdot b^{12} \cdot c^6 \cdot d / (b \cdot x + a) + 21 \cdot a^2 \cdot b^{11} \cdot c^5 \cdot d^2 / (b \cdot x + a) - 35 \cdot a^3 \cdot b^{10} \cdot c^4 \cdot d^3 / (b \cdot x + a) + 35 \cdot a^4 \cdot b^9 \cdot c^3 \cdot d^4 / (b \cdot x + a) - 21 \cdot a^5 \cdot b^8 \cdot c^2 \cdot d^5 / (b \cdot x + a) + 7 \cdot a^6 \cdot b^7 \cdot c \cdot d^6 / (b \cdot x + a) - a^7 \cdot b^6 \cdot d^7 / (b \cdot x + a)) / b^{14}$

maple [B] time = 0.01, size = 571, normalized size = 3.05

$$\frac{d^7 x^6}{6b^2} - \frac{2a d^7 x^5}{5b^3} + \frac{7c d^6 x^5}{5b^2} + \frac{3a^2 d^7 x^4}{4b^4} - \frac{7ac d^6 x^4}{2b^3} + \frac{21c^2 d^5 x^4}{4b^2} - \frac{4a^3 d^7 x^3}{3b^5} + \frac{7a^2 c d^6 x^3}{b^4} - \frac{14a c^2 d^5 x^3}{b^3} + \frac{35c^3 d^4 x^3}{3b^2} + \frac{5a^4 d^7 x^2}{2b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^2,x)

[Out] $\frac{35}{3} \cdot d^4 / b^2 \cdot x^3 \cdot c^3 + 5/2 \cdot d^7 / b^6 \cdot x^2 \cdot a^4 + 35/2 \cdot d^3 / b^2 \cdot x^2 \cdot c^4 - 6 \cdot d^7 / b^7 \cdot a^5 \cdot x + 21 \cdot d^2 / b^2 \cdot c^5 \cdot x + 7 / b^8 \cdot d^7 \cdot \ln(b \cdot x + a) \cdot a^6 + 7 / b^2 \cdot d \cdot \ln(b \cdot x + a) \cdot c^6 + 1 / b^8 / (b \cdot x + a) \cdot a^7 \cdot d^7 - 2/5 \cdot d^7 / b^3 \cdot x^5 \cdot a + 7/5 \cdot d^6 / b^2 \cdot x^5 \cdot c + 3/4 \cdot d^7 / b^4 \cdot x^4 \cdot a^2 + 21/4 \cdot d^5 / b^2 \cdot x^4 \cdot c^2 - 4/3 \cdot d^7 / b^5 \cdot x^3 \cdot a^3 - 21 / b^3 / (b \cdot x + a) \cdot a^2 \cdot c^5 \cdot d^2 + 7 / b^2 / (b \cdot x + a) \cdot a \cdot c^6 \cdot d - 14 \cdot d^5 / b^3 \cdot x^3 \cdot a \cdot c^2 - 14 \cdot d^6 / b^5 \cdot x^2 \cdot a^3 \cdot c + 63/2 \cdot d^5 / b^4 \cdot x^2 \cdot a^2 \cdot c^2 - 35 \cdot d^4 / b^3 \cdot x^2 \cdot a \cdot c^3 + 35 \cdot d^6 / b^6 \cdot a^4 \cdot c \cdot x - 7/2 \cdot d^6 / b^3 \cdot x^4 \cdot a \cdot c + 7 \cdot d^6 / b^4 \cdot x^3 \cdot a^2 \cdot c - 70 \cdot d^3 / b^3 \cdot a \cdot c^4 \cdot x - 42 / b^7 \cdot d^6 \cdot \ln(b \cdot x + a) \cdot a^5 \cdot c + 105 / b^6 \cdot d^5 \cdot \ln(b \cdot x + a) \cdot a^4 \cdot c^2 - 140 / b^5 \cdot d^4 \cdot \ln(b \cdot x + a) \cdot a^3 \cdot c^3 + 105 / b^4 \cdot d^3 \cdot \ln(b \cdot x + a) \cdot a^2 \cdot c^4 - 42 / b^3 \cdot d^2 \cdot \ln(b \cdot x + a) \cdot a \cdot c^5 - 7 / b^7 / (b \cdot x + a) \cdot a^6 \cdot c \cdot d^6 + 21 / b^6 / (b \cdot x + a) \cdot a^5 \cdot c^2 \cdot d^5 - 35 / b^5 / (b \cdot x + a) \cdot a^4 \cdot c^3 \cdot d^4 + 35 / b^4 / (b \cdot x + a) \cdot a^3 \cdot c^4 \cdot d^3 - 84 \cdot d^5 / b^5 \cdot a^3 \cdot c^2 \cdot x + 105 \cdot d^4 / b^4 \cdot a^2 \cdot c^3 \cdot x - 1 / b / (b \cdot x + a) \cdot c^7 + 1/6 \cdot d^7 / b^2 \cdot x^6$

maxima [B] time = 1.40, size = 467, normalized size = 2.50

$$\frac{b^7 c^7 - 7 a b^6 c^6 d + 21 a^2 b^5 c^5 d^2 - 35 a^3 b^4 c^4 d^3 + 35 a^4 b^3 c^3 d^4 - 21 a^5 b^2 c^2 d^5 + 7 a^6 b c d^6 - a^7 d^7}{b^9 x + a b^8} + \frac{10 b^5 d^7 x^6 + 12 (7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^2,x, algorithm="maxima")

[Out] $-(b^7c^7 - 7ab^6c^6d + 21a^2b^5c^5d^2 - 35a^3b^4c^4d^3 + 35a^4b^3c^3d^4 - 21a^5b^2c^2d^5 + 7a^6b^1c^1d^6 - a^7d^7)/(b^9x + ab^8) + 1/60*(10b^5d^7x^6 + 12*(7b^5c^1d^6 - 2ab^4d^7)x^5 + 15*(21b^5c^2d^5 - 14a^1b^4c^1d^6 + 3a^2b^3c^1d^7)x^4 + 20*(35b^5c^3d^4 - 42a^1b^4c^2d^5 + 21a^2b^3c^1d^6 - 4a^3b^2c^1d^7)x^3 + 30*(35b^5c^4d^3 - 70a^1b^4c^3d^4 + 63a^2b^3c^2d^5 - 28a^3b^2c^1d^6 + 5a^4b^1c^1d^7)x^2 + 60*(21b^5c^5d^2 - 70a^1b^4c^4d^3 + 105a^2b^3c^3d^4 - 84a^3b^2c^2d^5 + 35a^4b^1c^1d^6 - 6a^5d^7)x)/b^7 + 7*(b^6c^6d - 6a^1b^5c^5d^2 + 15a^2b^4c^4d^3 - 20a^3b^3c^3d^4 + 15a^4b^2c^2d^5 - 6a^5b^1c^1d^6 + a^6d^7)*\log(bx + a)/b^8$

mupad [B] time = 0.24, size = 841, normalized size = 4.50

$$x^4 \left(\frac{a \left(\frac{2ad^7}{b^3} - \frac{7cd^6}{b^2} \right)}{2b} - \frac{a^2 d^7}{4b^4} + \frac{21c^2 d^5}{4b^2} \right) - x^2 \left(\frac{a \left(\frac{35c^3 d^4}{b^2} - \frac{2a \left(\frac{2ad^7}{b^3} - \frac{7cd^6}{b^2} \right) - \frac{a^2 d^7}{b^4} + \frac{21c^2 d^5}{b^2} \right)}{b} + \frac{a^2 \left(\frac{2ad^7}{b^3} - \frac{7cd^6}{b^2} \right)}{b^2} \right) - \frac{35c^4 d^3}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((c + dx)^7/(a + bx)^2, x)$

[Out] $x^4*((a*((2ad^7)/b^3 - (7cd^6)/b^2))/(2b) - (a^2d^7)/(4b^4) + (21c^2d^5)/(4b^2)) - x^2*((a*((35c^3d^4)/b^2 - (2a*((2a*((2ad^7)/b^3 - (7cd^6)/b^2))/b - (a^2d^7)/b^4 + (21c^2d^5)/b^2))/b + (a^2*((2ad^7)/b^3 - (7cd^6)/b^2))/b^2))/b - (35c^4d^3)/(2b^2) + (a^2*((2a*((2ad^7)/b^3 - (7cd^6)/b^2))/b - (a^2d^7)/b^4 + (21c^2d^5)/b^2))/(2b^2)) - x^5*((2ad^7)/(5b^3) - (7cd^6)/(5b^2)) + x*((2a*((2a*((35c^3d^4)/b^2$

$$\begin{aligned}
& - (2*a*((2*a*((2*a*d^7)/b^3 - (7*c*d^6)/b^2))/b - (a^2*d^7)/b^4 + (21*c^2*d^5)/b^2))/b + (a^2*((2*a*d^7)/b^3 - (7*c*d^6)/b^2))/b^2)/b - (35*c^4*d^3)/b^2 + (a^2*((2*a*((2*a*d^7)/b^3 - (7*c*d^6)/b^2))/b - (a^2*d^7)/b^4 + (21*c^2*d^5)/b^2))/b^2)/b - (a^2*((35*c^3*d^4)/b^2 - (2*a*((2*a*((2*a*d^7)/b^3 - (7*c*d^6)/b^2))/b - (a^2*d^7)/b^4 + (21*c^2*d^5)/b^2))/b + (a^2*((2*a*d^7)/b^3 - (7*c*d^6)/b^2))/b^2))/b^2 + (21*c^5*d^2)/b^2 + x^3*((35*c^3*d^4)/(3*b^2) - (2*a*((2*a*((2*a*d^7)/b^3 - (7*c*d^6)/b^2))/b - (a^2*d^7)/b^4 + (21*c^2*d^5)/b^2))/(3*b) + (a^2*((2*a*d^7)/b^3 - (7*c*d^6)/b^2))/(3*b^2)) + (a^7*d^7 - b^7*c^7 - 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 - 35*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 7*a^6*b*c*d^6)/(b*(a*b^7 + b^8*x)) + (d^7*x^6)/(6*b^2) + (log(a + b*x)*(7*a^6*d^7 + 7*b^6*c^6*d - 42*a*b^5*c^5*d^2 + 105*a^2*b^4*c^4*d^3 - 140*a^3*b^3*c^3*d^4 + 105*a^4*b^2*c^2*d^5 - 42*a^5*b*c*d^6))/b^8
\end{aligned}$$

sympy [B] time = 1.44, size = 428, normalized size = 2.29

$$x^5 \left(-\frac{2ad^7}{5b^3} + \frac{7cd^6}{5b^2} \right) + x^4 \left(\frac{3a^2d^7}{4b^4} - \frac{7acd^6}{2b^3} + \frac{21c^2d^5}{4b^2} \right) + x^3 \left(-\frac{4a^3d^7}{3b^5} + \frac{7a^2cd^6}{b^4} - \frac{14ac^2d^5}{b^3} + \frac{35c^3d^4}{3b^2} \right) + x^2 \left(\frac{5a^4d^7}{2b^6} - \frac{7a^3cd^6}{b^5} + \frac{21a^2c^2d^5}{b^4} - \frac{35a^3c^3d^4}{b^3} + \frac{105a^4b^2c^2d^5}{b^6} - \frac{42a^5b^2cd^6}{b^5} \right) + \frac{d^7x^6}{6b^2} + \frac{\log(ax+b)(7a^6d^7 + 7b^6cd - 42a^2b^5c^2d^2 + 105a^3b^4c^3d^3 - 140a^4b^3c^4d^4 + 105a^5b^2c^5d^5 - 42a^6b^2cd^6)}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**2,x)

[Out] x**5*(-2*a*d**7/(5*b**3) + 7*c*d**6/(5*b**2)) + x**4*(3*a**2*d**7/(4*b**4) - 7*a*c*d**6/(2*b**3) + 21*c**2*d**5/(4*b**2)) + x**3*(-4*a**3*d**7/(3*b**5) + 7*a**2*c*d**6/b**4 - 14*a*c**2*d**5/b**3 + 35*c**3*d**4/(3*b**2)) + x**2*(5*a**4*d**7/(2*b**6) - 14*a**3*c*d**6/b**5 + 63*a**2*c**2*d**5/(2*b**4) - 35*a*c**3*d**4/b**3 + 35*c**4*d**3/(2*b**2)) + x*(-6*a**5*d**7/b**7 + 35*a**4*c*d**6/b**6 - 84*a**3*c**2*d**5/b**5 + 105*a**2*c**3*d**4/b**4 - 70*a*c**4*d**3/b**3 + 21*c**5*d**2/b**2) + (a**7*d**7 - 7*a**6*b*c*d**6 + 21*a**5*b**2*c**2*d**5 - 35*a**4*b**3*c**3*d**4 + 35*a**3*b**4*c**4*d**3 - 21*a**2*b**5*c**5*d**2 + 7*a*b**6*c**6*d - b**7*c**7)/(a*b**8 + b**9*x) + d**7*x**6/(6*b**2) + 7*d*(a*d - b*c)**6*log(a + b*x)/b**8

3.1285

$$\int \frac{(c+dx)^7}{(a+bx)^3} dx$$

Optimal. Leaf size=185

$$\frac{7d^6(a+bx)^4(bc-ad)}{4b^8} + \frac{7d^5(a+bx)^3(bc-ad)^2}{b^8} + \frac{35d^4(a+bx)^2(bc-ad)^3}{2b^8} + \frac{21d^2(bc-ad)^5 \log(a+bx)}{b^8} - \frac{7d(bc-ad)}{b^8(a+bx)}$$

[Out] $35*d^3*(-a*d+b*c)^4*x/b^7-1/2*(-a*d+b*c)^7/b^8/(b*x+a)^2-7*d*(-a*d+b*c)^6/b^8/(b*x+a)+35/2*d^4*(-a*d+b*c)^3*(b*x+a)^2/b^8+7*d^5*(-a*d+b*c)^2*(b*x+a)^3/b^8+7/4*d^6*(-a*d+b*c)*(b*x+a)^4/b^8+1/5*d^7*(b*x+a)^5/b^8+21*d^2*(-a*d+b*c)^5*\ln(b*x+a)/b^8$

Rubi [A] time = 0.22, antiderivative size = 185, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{7d^6(a+bx)^4(bc-ad)}{4b^8} + \frac{7d^5(a+bx)^3(bc-ad)^2}{b^8} + \frac{35d^4(a+bx)^2(bc-ad)^3}{2b^8} + \frac{35d^3x(bc-ad)^4}{b^7} + \frac{21d^2(bc-ad)^5 \log(a+bx)}{b^8}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^3, x]

[Out] $(35*d^3*(b*c - a*d)^4*x)/b^7 - (b*c - a*d)^7/(2*b^8*(a + b*x)^2) - (7*d*(b*c - a*d)^6)/(b^8*(a + b*x)) + (35*d^4*(b*c - a*d)^3*(a + b*x)^2)/(2*b^8) + (7*d^5*(b*c - a*d)^2*(a + b*x)^3)/b^8 + (7*d^6*(b*c - a*d)*(a + b*x)^4)/(4*b^8) + (d^7*(a + b*x)^5)/(5*b^8) + (21*d^2*(b*c - a*d)^5*\text{Log}[a + b*x])/b^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^3} dx = \int \left(\frac{35d^3(bc-ad)^4}{b^7} + \frac{(bc-ad)^7}{b^7(a+bx)^3} + \frac{7d(bc-ad)^6}{b^7(a+bx)^2} + \frac{21d^2(bc-ad)^5}{b^7(a+bx)} + \frac{35d^4(bc-ad)^3(a+bx)}{b^7} + \frac{35d^3(bc-ad)^4x}{b^7} - \frac{(bc-ad)^7}{2b^8(a+bx)^2} - \frac{7d(bc-ad)^6}{b^8(a+bx)} + \frac{35d^4(bc-ad)^3(a+bx)^2}{2b^8} + \frac{7d^5(bc-ad)^2(a+bx)}{b^8} \right) dx$$

Mathematica [B] time = 0.13, size = 389, normalized size = 2.10

$$\frac{-130a^7d^7 + 10a^6bd^6(77c + 16dx) + 10a^5b^2d^5(-189c^2 - 56cdx + 50d^2x^2) + 70a^4b^3d^4(35c^3 + 6c^2dx - 34cd^2x^2 - 2d^3x^3) - 35a^3b^4d^3(50c^4 - 20c^3dx - 126c^2d^2x^2 + 20cd^3x^3 + d^4x^4) + 7a^2b^5d^2(90c^5 - 200c^4dx - 550c^3d^2x^2 + 200c^2d^3x^3 + 25cd^4x^4 + 2d^5x^5) - 7ab^6d(10c^6 - 120c^5dx - 200c^4d^2x^2 + 200c^3d^3x^3 + 50c^2d^4x^4 + 10cd^5x^5 + d^6x^6) + b^7(-10c^7 - 140c^6dx + 700c^4d^3x^3 + 350c^3d^4x^4 + 140c^2d^5x^5 + 35cd^6x^6 + 4d^7x^7) - 420d^2(-(bc) + ad)^5(a + bx)^2 \operatorname{Log}[a + bx]}{(20b^8(a + bx)^2)}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^3,x]

[Out] $(-130a^7d^7 + 10a^6bd^6(77c + 16dx) + 10a^5b^2d^5(-189c^2 - 56cdx + 50d^2x^2) + 70a^4b^3d^4(35c^3 + 6c^2dx - 34cd^2x^2 - 2d^3x^3) - 35a^3b^4d^3(50c^4 - 20c^3dx - 126c^2d^2x^2 + 20cd^3x^3 + d^4x^4) + 7a^2b^5d^2(90c^5 - 200c^4dx - 550c^3d^2x^2 + 200c^2d^3x^3 + 25cd^4x^4 + 2d^5x^5) - 7ab^6d(10c^6 - 120c^5dx - 200c^4d^2x^2 + 200c^3d^3x^3 + 50c^2d^4x^4 + 10cd^5x^5 + d^6x^6) + b^7(-10c^7 - 140c^6dx + 700c^4d^3x^3 + 350c^3d^4x^4 + 140c^2d^5x^5 + 35cd^6x^6 + 4d^7x^7) - 420d^2(-(bc) + ad)^5(a + bx)^2 \operatorname{Log}[a + bx]) / (20b^8(a + bx)^2)$

fricas [B] time = 0.43, size = 703, normalized size = 3.80

$$\frac{4b^7d^7x^7 - 10b^7c^7 - 70ab^6c^6d + 630a^2b^5c^5d^2 - 1750a^3b^4c^4d^3 + 2450a^4b^3c^3d^4 - 1890a^5b^2c^2d^5 + 770a^6bcd^6 - 130a^7d^7 + 7(5b^7c^6d^6 - ab^6d^7)x^6 + 14(10b^7c^2d^5 - 5ab^6c^6d^6 + a^2b^5d^7)x^5 + 35(10b^7c^3d^4 - 10ab^6c^2d^5 + 5a^2b^5c^6d^6 - a^3b^4d^7)x^4 + 140(5b^7c^4d^3 - 10ab^6c^3d^4 + 10a^2b^5c^2d^5 - 5a^3b^4c^6d^6 + a^4b^3d^7)x^3 + 10(140ab^6c^4d^3 - 385a^2b^5c^3d^4 + 441a^3b^4c^2d^5 - 238a^4b^3c^6d^6 + 50a^5b^2d^7)x^2 - 20(7b^7c^6d^6 - 42ab^6c^5d^2 + 70a^2b^5c^4d^3 - 35a^3b^4c^3d^4 - 21a^4b^3c^2d^5 + 28a^5b^2c^6d^6 - 8a^6b^7d^7)x + 420(a^2b^5c^5d^2 - 5a^3b^4c^4d^3 + 10a^4b^3c^3d^4 - 10a^5b^2c^2d^5 + 5a^6b^7c^6d^6 - a^7d^7 + (b^7c^5d^2 - 5ab^6c^4d^3 + 10a^2b^5c^3d^4 - 10a^3b^4c^2d^5 + 5a^4b^3c^6d^6 - a^5b^2d^7)x^2 + 2(a^2b^6c^5d^2 - 5a^2b^5c^4d^3 + 10a^3b^4c^3d^4 - 10a^4b^3c^2d^5 + 5a^5b^2c^6d^6 - a^6b^7d^7)x) \operatorname{log}(bx + a)}{(b^10x^2 + 2ab^9x + a^2b^8)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^3,x, algorithm="fricas")

[Out] $\frac{1}{20} (4b^7d^7x^7 - 10b^7c^7 - 70ab^6c^6d + 630a^2b^5c^5d^2 - 1750a^3b^4c^4d^3 + 2450a^4b^3c^3d^4 - 1890a^5b^2c^2d^5 + 770a^6bcd^6 - 130a^7d^7 + 7(5b^7c^6d^6 - ab^6d^7)x^6 + 14(10b^7c^2d^5 - 5ab^6c^6d^6 + a^2b^5d^7)x^5 + 35(10b^7c^3d^4 - 10ab^6c^2d^5 + 5a^2b^5c^6d^6 - a^3b^4d^7)x^4 + 140(5b^7c^4d^3 - 10ab^6c^3d^4 + 10a^2b^5c^2d^5 - 5a^3b^4c^6d^6 + a^4b^3d^7)x^3 + 10(140ab^6c^4d^3 - 385a^2b^5c^3d^4 + 441a^3b^4c^2d^5 - 238a^4b^3c^6d^6 + 50a^5b^2d^7)x^2 - 20(7b^7c^6d^6 - 42ab^6c^5d^2 + 70a^2b^5c^4d^3 - 35a^3b^4c^3d^4 - 21a^4b^3c^2d^5 + 28a^5b^2c^6d^6 - 8a^6b^7d^7)x + 420(a^2b^5c^5d^2 - 5a^3b^4c^4d^3 + 10a^4b^3c^3d^4 - 10a^5b^2c^2d^5 + 5a^6b^7c^6d^6 - a^7d^7 + (b^7c^5d^2 - 5ab^6c^4d^3 + 10a^2b^5c^3d^4 - 10a^3b^4c^2d^5 + 5a^4b^3c^6d^6 - a^5b^2d^7)x^2 + 2(a^2b^6c^5d^2 - 5a^2b^5c^4d^3 + 10a^3b^4c^3d^4 - 10a^4b^3c^2d^5 + 5a^5b^2c^6d^6 - a^6b^7d^7)x) \operatorname{log}(bx + a)) / (b^10x^2 + 2ab^9x + a^2b^8)$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^3,x, algorithm="maxima")

[Out]
$$-1/2*(b^7*c^7 + 7*a*b^6*c^6*d - 63*a^2*b^5*c^5*d^2 + 175*a^3*b^4*c^4*d^3 - 245*a^4*b^3*c^3*d^4 + 189*a^5*b^2*c^2*d^5 - 77*a^6*b*c*d^6 + 13*a^7*d^7 + 14*(b^7*c^6*d - 6*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 - 20*a^3*b^4*c^3*d^4 + 15*a^4*b^3*c^2*d^5 - 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^{10}*x^2 + 2*a*b^9*x + a^2*b^8) + 1/20*(4*b^4*d^7*x^5 + 5*(7*b^4*c*d^6 - 3*a*b^3*d^7)*x^4 + 20*(7*b^4*c^2*d^5 - 7*a*b^3*c*d^6 + 2*a^2*b^2*d^7)*x^3 + 10*(35*b^4*c^3*d^4 - 63*a*b^3*c^2*d^5 + 42*a^2*b^2*c*d^6 - 10*a^3*b*d^7)*x^2 + 20*(35*b^4*c^4*d^3 - 105*a*b^3*c^3*d^4 + 126*a^2*b^2*c^2*d^5 - 70*a^3*b*c*d^6 + 15*a^4*d^7)*x)/b^7 + 21*(b^5*c^5*d^2 - 5*a*b^4*c^4*d^3 + 10*a^2*b^3*c^3*d^4 - 10*a^3*b^2*c^2*d^5 + 5*a^4*b*c*d^6 - a^5*d^7)*log(b*x + a)/b^8$$

mupad [B] time = 0.27, size = 690, normalized size = 3.73

$$x \left(\frac{3a \left(\frac{3a \left(\frac{3ad^7}{b^4} - \frac{7cd^6}{b^3} \right)}{b} - \frac{3a^2d^7}{b^5} + \frac{21c^2d^5}{b^3} \right)}{b} + \frac{a^3d^7}{b^6} - \frac{35c^3d^4}{b^3} - \frac{3a^2 \left(\frac{3ad^7}{b^4} - \frac{7cd^6}{b^3} \right)}{b^2} \right) + \frac{35c^4d^3}{b^3} + \frac{a^3 \left(\frac{3ad^7}{b^4} - \frac{7cd^6}{b^3} \right)}{b^3} - \frac{3a^2}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^3,x)

[Out]
$$x*((3*a*((3*a*((3*a*((3*a*d^7)/b^4 - (7*c*d^6)/b^3))/b - (3*a^2*d^7)/b^5 + (21*c^2*d^5)/b^3))/b + (a^3*d^7)/b^6 - (35*c^3*d^4)/b^3 - (3*a^2*((3*a*d^7)/b^4 - (7*c*d^6)/b^3))/b^2))/b + (35*c^4*d^3)/b^3 + (a^3*((3*a*d^7)/b^4 - (7*c*d^6)/b^3))/b^3 - (3*a^2*((3*a*((3*a*d^7)/b^4 - (7*c*d^6)/b^3))/b - (3*a^2*d^7)/b^5 + (21*c^2*d^5)/b^3))/b^2) - x^4*((3*a*d^7)/(4*b^4) - (7*c*d^6)/(4*b^3)) - x^2*((3*a*((3*a*((3*a*d^7)/b^4 - (7*c*d^6)/b^3))/b - (3*a^2*d^7)/b^5 + (21*c^2*d^5)/b^3))/(2*b) + (a^3*d^7)/(2*b^6) - (35*c^3*d^4)/(2*b^3) - (3*a^2*((3*a*d^7)/b^4 - (7*c*d^6)/b^3))/(2*b^2)) + x^3*((a*((3*a*d^7)/b^4 - (7*c*d^6)/b^3))/b - (a^2*d^7)/b^5 + (7*c^2*d^5)/b^3) - ((13*a^7*d^7 + b^7*c^7 - 63*a^2*b^5*c^5*d^2 + 175*a^3*b^4*c^4*d^3 - 245*a^4*b^3*c^3*d^4 + 189*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 77*a^6*b*c*d^6)/(2*b) + x*(7*a^6*d^7 + 7*b^6*c^6*d - 42*a*b^5*c^5*d^2 + 105*a^2*b^4*c^4*d^3 - 140*a^3*b^3*c^3*d^4 + 105*a^4*b^2*c^2*d^5 - 42*a^5*b*c*d^6))/(a^2*b^7 + b^9*x^2 + 2*a*b^8*x) +$$

$(d^7 x^5)/(5b^3) - (\log(a + bx) * (21a^5 d^7 - 21b^5 c^5 d^2 + 105a^4 b^4 c^4 d^3 - 210a^3 b^3 c^3 d^4 + 210a^2 b^2 c^2 d^5 - 105a^4 b^4 c^4 d^6)) / b^8$

sympy [B] time = 2.95, size = 447, normalized size = 2.42

$$x^4 \left(-\frac{3ad^7}{4b^4} + \frac{7cd^6}{4b^3} \right) + x^3 \left(\frac{2a^2 d^7}{b^5} - \frac{7acd^6}{b^4} + \frac{7c^2 d^5}{b^3} \right) + x^2 \left(-\frac{5a^3 d^7}{b^6} + \frac{21a^2 cd^6}{b^5} - \frac{63ac^2 d^5}{2b^4} + \frac{35c^3 d^4}{2b^3} \right) + x \left(\frac{15a^4 d^7}{b^7} - \frac{70a^3 c d^6}{b^6} + \frac{126a^2 c^2 d^5}{b^5} - \frac{105a^4 b^4 c^4 d^6}{b^8} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**3,x)

[Out] $x^4 * (-3*a*d^7/(4*b^4) + 7*c*d^6/(4*b^3)) + x^3 * (2*a^2*d^7/b^5 - 7*a*c*d^6/b^4 + 7*c^2*d^5/b^3) + x^2 * (-5*a^3*d^7/b^6 + 21*a^2*c*d^6/b^5 - 63*a*c^2*d^5/(2*b^4) + 35*c^3*d^4/(2*b^3)) + x * (15*a^4*d^7/b^7 - 70*a^3*c*d^6/b^6 + 126*a^2*c^2*d^5/b^5 - 105*a^4*b^4*c^4/b^8 + 35*c^4*d^3/b^3) + (-13*a^7*d^7 + 77*a^6*b*c*d^6 - 189*a^5*b^2*c^2*d^5 + 245*a^4*b^3*c^3*d^4 - 175*a^3*b^4*c^4*d^3 + 63*a^2*b^5*c^5*d^2 - 7*a*b^6*c^6*d - b^7*c^7) + x * (-14*a^6*b*d^7 + 84*a^5*b^2*c*d^6 - 210*a^4*b^3*c^2*d^5 + 280*a^3*b^4*c^3*d^4 - 210*a^2*b^5*c^4*d^3 + 84*a*b^6*c^5*d^2 - 14*b^7*c^6*d) / (2*a^2*b^8 + 4*a*b^9*x + 2*b^10*x^2) + d^7*x^5/(5*b^3) - 21*d^2*(a*d - b*c)**5*log(a + b*x)/b^8$

$$3.1286 \quad \int \frac{(c+dx)^7}{(a+bx)^4} dx$$

Optimal. Leaf size=187

$$\frac{7d^6(a+bx)^3(bc-ad)}{3b^8} + \frac{21d^5(a+bx)^2(bc-ad)^2}{2b^8} + \frac{35d^3(bc-ad)^4 \log(a+bx)}{b^8} - \frac{21d^2(bc-ad)^5}{b^8(a+bx)} - \frac{7d(bc-ad)^6}{2b^8(a+bx)^2} - \frac{d^7}{3b^8}$$

[Out] $35*d^4*(-a*d+b*c)^3*x/b^7-1/3*(-a*d+b*c)^7/b^8/(b*x+a)^3-7/2*d*(-a*d+b*c)^6/b^8/(b*x+a)^2-21*d^2*(-a*d+b*c)^5/b^8/(b*x+a)+21/2*d^5*(-a*d+b*c)^2*(b*x+a)^2/b^8+7/3*d^6*(-a*d+b*c)*(b*x+a)^3/b^8+1/4*d^7*(b*x+a)^4/b^8+35*d^3*(-a*d+b*c)^4*\ln(b*x+a)/b^8$

Rubi [A] time = 0.21, antiderivative size = 187, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{7d^6(a+bx)^3(bc-ad)}{3b^8} + \frac{21d^5(a+bx)^2(bc-ad)^2}{2b^8} + \frac{35d^4x(bc-ad)^3}{b^7} - \frac{21d^2(bc-ad)^5}{b^8(a+bx)} + \frac{35d^3(bc-ad)^4 \log(a+bx)}{b^8} - \frac{d^7}{3b^8}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^4, x]

[Out] $(35*d^4*(b*c - a*d)^3*x)/b^7 - (b*c - a*d)^7/(3*b^8*(a + b*x)^3) - (7*d*(b*c - a*d)^6)/(2*b^8*(a + b*x)^2) - (21*d^2*(b*c - a*d)^5)/(b^8*(a + b*x)) + (21*d^5*(b*c - a*d)^2*(a + b*x)^2)/(2*b^8) + (7*d^6*(b*c - a*d)*(a + b*x)^3)/(3*b^8) + (d^7*(a + b*x)^4)/(4*b^8) + (35*d^3*(b*c - a*d)^4*\text{Log}[a + b*x])/b^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^4} dx = \int \left(\frac{35d^4(bc-ad)^3}{b^7} + \frac{(bc-ad)^7}{b^7(a+bx)^4} + \frac{7d(bc-ad)^6}{b^7(a+bx)^3} + \frac{21d^2(bc-ad)^5}{b^7(a+bx)^2} + \frac{35d^3(bc-ad)^4}{b^7(a+bx)} + \frac{21d^5}{b^7} \right) dx$$

$$= \frac{35d^4(bc-ad)^3x}{b^7} - \frac{(bc-ad)^7}{3b^8(a+bx)^3} - \frac{7d(bc-ad)^6}{2b^8(a+bx)^2} - \frac{21d^2(bc-ad)^5}{b^8(a+bx)} + \frac{21d^5(bc-ad)^2(a+bx)^2}{2b^8} + \frac{21d^5}{b^7}$$

Mathematica [A] time = 0.11, size = 199, normalized size = 1.06

$$\frac{6b^2d^5x^2(10a^2d^2 - 28abcd + 21b^2c^2) + 12bd^4x(-20a^3d^3 + 70a^2bcd^2 - 84ab^2c^2d + 35b^3c^3) + 4b^3d^6x^3(7bc - 4ad)}{12b^8}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^4,x]

[Out] (12*b*d^4*(35*b^3*c^3 - 84*a*b^2*c^2*d + 70*a^2*b*c*d^2 - 20*a^3*d^3)*x + 6*b^2*d^5*(21*b^2*c^2 - 28*a*b*c*d + 10*a^2*d^2)*x^2 + 4*b^3*d^6*(7*b*c - 4*a*d)*x^3 + 3*b^4*d^7*x^4 - (4*(b*c - a*d)^7)/(a + b*x)^3 - (42*d*(b*c - a*d)^6)/(a + b*x)^2 + (252*d^2*(-(b*c) + a*d)^5)/(a + b*x) + 420*d^3*(b*c - a*d)^4*Log[a + b*x])/(12*b^8)

fricas [B] time = 0.44, size = 739, normalized size = 3.95

$$\frac{3b^7d^7x^7 - 4b^7c^7 - 14ab^6c^6d - 84a^2b^5c^5d^2 + 770a^3b^4c^4d^3 - 1820a^4b^3c^3d^4 + 1974a^5b^2c^2d^5 - 1036a^6bcd^6 + 214a^7d^7}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^4,x, algorithm="fricas")

[Out] 1/12*(3*b^7*d^7*x^7 - 4*b^7*c^7 - 14*a*b^6*c^6*d - 84*a^2*b^5*c^5*d^2 + 770*a^3*b^4*c^4*d^3 - 1820*a^4*b^3*c^3*d^4 + 1974*a^5*b^2*c^2*d^5 - 1036*a^6*b*c*d^6 + 214*a^7*d^7 + 7*(4*b^7*c*d^6 - a*b^6*d^7)*x^6 + 21*(6*b^7*c^2*d^5 - 4*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 105*(4*b^7*c^3*d^4 - 6*a*b^6*c^2*d^5 + 4*a^2*b^5*c*d^6 - a^3*b^4*d^7)*x^4 + 2*(630*a*b^6*c^3*d^4 - 1323*a^2*b^5*c^2*d^5 + 1022*a^3*b^4*c*d^6 - 278*a^4*b^3*d^7)*x^3 - 6*(42*b^7*c^5*d^2 - 210*a*b^6*c^4*d^3 + 210*a^2*b^5*c^3*d^4 + 63*a^3*b^4*c^2*d^5 - 182*a^4*b^3*c*d^6 + 68*a^5*b^2*d^7)*x^2 - 6*(7*b^7*c^6*d + 42*a*b^6*c^5*d^2 - 315*a^2*b^5*c^4*d^3 + 630*a^3*b^4*c^3*d^4 - 567*a^4*b^3*c^2*d^5 + 238*a^5*b^2*c*d^6 - 37*a^6*b*d^7)*x + 420*(a^3*b^4*c^4*d^3 - 4*a^4*b^3*c^3*d^4 + 6*a^5*b^2*c^2*d^5 - 4*a^6*b*c*d^6 + a^7*d^7 + (b^7*c^4*d^3 - 4*a*b^6*c^3*d^4 + 6*a^2*b^5*c^2*d^5 - 4*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 3*(a*b^6*c^4*d^3 - 4*a^2*b^5*c^3*d^4 + 6*a^3*b^4*c^2*d^5 - 4*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 3*(a^2*b^5*c^4*d^3 - 4*a^3*b^4*c^3*d^4 + 6*a^4*b^3*c^2*d^5 - 4*a^5*b^2*c*d^6 + a^6*b*d^7)*x)*log(b*x + a))/(b^11*x^3 + 3*a*b^10*x^2 + 3*a^2*b^9*x + a^3*b^8)

giac [B] time = 1.32, size = 470, normalized size = 2.51

$$\frac{35(b^4c^4d^3 - 4ab^3c^3d^4 + 6a^2b^2c^2d^5 - 4a^3bcd^6 + a^4d^7) \log(|bx + a|)}{b^8} - \frac{2b^7c^7 + 7ab^6c^6d + 42a^2b^5c^5d^2 - 385a^3b^4c^4d^3}{b^8}$$

[Out]
$$-1/6*(2*b^7*c^7 + 7*a*b^6*c^6*d + 42*a^2*b^5*c^5*d^2 - 385*a^3*b^4*c^4*d^3 + 910*a^4*b^3*c^3*d^4 - 987*a^5*b^2*c^2*d^5 + 518*a^6*b*c*d^6 - 107*a^7*d^7 + 126*(b^7*c^5*d^2 - 5*a*b^6*c^4*d^3 + 10*a^2*b^5*c^3*d^4 - 10*a^3*b^4*c^2*d^5 + 5*a^4*b^3*c*d^6 - a^5*b^2*d^7)*x^2 + 21*(b^7*c^6*d + 6*a*b^6*c^5*d^2 - 45*a^2*b^5*c^4*d^3 + 100*a^3*b^4*c^3*d^4 - 105*a^4*b^3*c^2*d^5 + 54*a^5*b^2*c*d^6 - 11*a^6*b*d^7)*x)/(b^11*x^3 + 3*a*b^10*x^2 + 3*a^2*b^9*x + a^3*b^8) + 1/12*(3*b^3*d^7*x^4 + 4*(7*b^3*c*d^6 - 4*a*b^2*d^7)*x^3 + 6*(21*b^3*c^2*d^5 - 28*a*b^2*c*d^6 + 10*a^2*b*d^7)*x^2 + 12*(35*b^3*c^3*d^4 - 84*a*b^2*c^2*d^5 + 70*a^2*b*c*d^6 - 20*a^3*d^7)*x)/b^7 + 35*(b^4*c^4*d^3 - 4*a*b^3*c^3*d^4 + 6*a^2*b^2*c^2*d^5 - 4*a^3*b*c*d^6 + a^4*d^7)*log(b*x + a)/b^8$$

mupad [B] time = 0.29, size = 559, normalized size = 2.99

$$x^2 \left(\frac{2a \left(\frac{4ad^7}{b^5} - \frac{7cd^6}{b^4} \right)}{b} - \frac{3a^2d^7}{b^6} + \frac{21c^2d^5}{2b^4} \right) - x^3 \left(\frac{4ad^7}{3b^5} - \frac{7cd^6}{3b^4} \right) - \frac{-107a^7d^7 + 518a^6bcd^6 - 987a^5b^2c^2d^5 + 910a^4b^3c^3d^4 - 385a^3b^4c^4d^3}{6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^7/(a + b*x)^4, x)`

[Out]
$$x^2*((2*a*((4*a*d^7)/b^5 - (7*c*d^6)/b^4))/b - (3*a^2*d^7)/b^6 + (21*c^2*d^5)/(2*b^4)) - x^3*((4*a*d^7)/(3*b^5) - (7*c*d^6)/(3*b^4)) - ((2*b^7*c^7 - 107*a^7*d^7 + 42*a^2*b^5*c^5*d^2 - 385*a^3*b^4*c^4*d^3 + 910*a^4*b^3*c^3*d^4 - 987*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d + 518*a^6*b*c*d^6)/(6*b) + x*((7*b^6*c^6*d)/2 - (77*a^6*d^7)/2 + 21*a*b^5*c^5*d^2 - (315*a^2*b^4*c^4*d^3)/2 + 350*a^3*b^3*c^3*d^4 - (735*a^4*b^2*c^2*d^5)/2 + 189*a^5*b*c*d^6) - x^2*(21*a^5*b*d^7 - 21*b^6*c^5*d^2 + 105*a*b^5*c^4*d^3 - 105*a^4*b^2*c*d^6 - 210*a^2*b^4*c^3*d^4 + 210*a^3*b^3*c^2*d^5))/(a^3*b^7 + b^10*x^3 + 3*a^2*b^8*x + 3*a*b^9*x^2) - x*((4*a*((4*a*d^7)/b^5 - (7*c*d^6)/b^4))/b - (6*a^2*d^7)/b^6 + (21*c^2*d^5)/b^4))/b + (4*a^3*d^7)/b^7 - (35*c^3*d^4)/b^4 - (6*a^2*((4*a*d^7)/b^5 - (7*c*d^6)/b^4))/b^2 + (log(a + b*x)*(35*a^4*d^7 + 35*b^4*c^4*d^3 - 140*a*b^3*c^3*d^4 + 210*a^2*b^2*c^2*d^5 - 140*a^3*b*c*d^6))/b^8 + (d^7*x^4)/(4*b^4)$$

sympy [B] time = 6.12, size = 474, normalized size = 2.53

$$x^3 \left(-\frac{4ad^7}{3b^5} + \frac{7cd^6}{3b^4} \right) + x^2 \left(\frac{5a^2d^7}{b^6} - \frac{14acd^6}{b^5} + \frac{21c^2d^5}{2b^4} \right) + x \left(-\frac{20a^3d^7}{b^7} + \frac{70a^2cd^6}{b^6} - \frac{84ac^2d^5}{b^5} + \frac{35c^3d^4}{b^4} \right) + \frac{107a^7d^7 - 518a^6bcd^6 + 987a^5b^2c^2d^5 - 910a^4b^3c^3d^4 + 385a^3b^4c^4d^3}{6b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**4,x)

[Out] $x^3*(-4*a*d^7/(3*b^5) + 7*c*d^6/(3*b^4)) + x^2*(5*a^2*d^7/b^6 - 14*a*c*d^6/b^5 + 21*c^2*d^5/(2*b^4)) + x*(-20*a^3*d^7/b^7 + 70*a^2*c*d^6/b^6 - 84*a*c^2*d^5/b^5 + 35*c^3*d^4/b^4) + (107*a^7*d^7 - 518*a^6*b*c*d^6 + 987*a^5*b^2*c^2*d^5 - 910*a^4*b^3*c^3*d^4 + 385*a^3*b^4*c^4*d^3 - 42*a^2*b^5*c^5*d^2 - 7*a*b^6*c^6*d - 2*b^7*c^7 + x^2*(126*a^5*b^2*d^7 - 630*a^4*b^3*c*d^6 + 1260*a^3*b^4*c^2*d^5 - 1260*a^2*b^5*c^3*d^4 + 630*a*b^6*c^4*d^3 - 126*b^7*c^5*d^2) + x*(231*a^6*b*d^7 - 1134*a^5*b^2*c*d^6 + 2205*a^4*b^3*c^2*d^5 - 2100*a^3*b^4*c^3*d^4 + 945*a^2*b^5*c^4*d^3 - 126*a*b^6*c^5*d^2 - 21*b^7*c^6*d))/(6*a^3*b^8 + 18*a^2*b^9*x + 18*a*b^10*x^2 + 6*b^11*x^3) + d^7*x^4/(4*b^4) + 35*d^3*(a*d - b*c)**4*log(a + b*x)/b^8$

$$3.1287 \quad \int \frac{(c+dx)^7}{(a+bx)^5} dx$$

Optimal. Leaf size=187

$$\frac{7d^6(a+bx)^2(bc-ad)}{2b^8} + \frac{35d^4(bc-ad)^3 \log(a+bx)}{b^8} - \frac{35d^3(bc-ad)^4}{b^8(a+bx)} - \frac{21d^2(bc-ad)^5}{2b^8(a+bx)^2} - \frac{7d(bc-ad)^6}{3b^8(a+bx)^3} - \frac{(bc-ad)^7}{4b^8(a+bx)^4}$$

[Out] $21*d^5*(-a*d+b*c)^2*x/b^7-1/4*(-a*d+b*c)^7/b^8/(b*x+a)^4-7/3*d*(-a*d+b*c)^6/b^8/(b*x+a)^3-21/2*d^2*(-a*d+b*c)^5/b^8/(b*x+a)^2-35*d^3*(-a*d+b*c)^4/b^8/(b*x+a)+7/2*d^6*(-a*d+b*c)*(b*x+a)^2/b^8+1/3*d^7*(b*x+a)^3/b^8+35*d^4*(-a*d+b*c)^3*\ln(b*x+a)/b^8$

Rubi [A] time = 0.20, antiderivative size = 187, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{7d^6(a+bx)^2(bc-ad)}{2b^8} + \frac{21d^5x(bc-ad)^2}{b^7} - \frac{35d^3(bc-ad)^4}{b^8(a+bx)} - \frac{21d^2(bc-ad)^5}{2b^8(a+bx)^2} + \frac{35d^4(bc-ad)^3 \log(a+bx)}{b^8} - \frac{7d(bc-ad)^6}{3b^8(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^5, x]

[Out] $(21*d^5*(b*c - a*d)^2*x)/b^7 - (b*c - a*d)^7/(4*b^8*(a + b*x)^4) - (7*d*(b*c - a*d)^6)/(3*b^8*(a + b*x)^3) - (21*d^2*(b*c - a*d)^5)/(2*b^8*(a + b*x)^2) - (35*d^3*(b*c - a*d)^4)/(b^8*(a + b*x)) + (7*d^6*(b*c - a*d)*(a + b*x)^2)/(2*b^8) + (d^7*(a + b*x)^3)/(3*b^8) + (35*d^4*(b*c - a*d)^3*\text{Log}[a + b*x])/b^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^5} dx = \int \left(\frac{21d^5(bc-ad)^2}{b^7} + \frac{(bc-ad)^7}{b^7(a+bx)^5} + \frac{7d(bc-ad)^6}{b^7(a+bx)^4} + \frac{21d^2(bc-ad)^5}{b^7(a+bx)^3} + \frac{35d^3(bc-ad)^4}{b^7(a+bx)^2} + \frac{35d^4(bc-ad)^3 \log(a+bx)}{b^7(a+bx)} \right) dx$$

$$= \frac{21d^5(bc-ad)^2x}{b^7} - \frac{(bc-ad)^7}{4b^8(a+bx)^4} - \frac{7d(bc-ad)^6}{3b^8(a+bx)^3} - \frac{21d^2(bc-ad)^5}{2b^8(a+bx)^2} - \frac{35d^3(bc-ad)^4}{b^8(a+bx)} + \frac{7d^6(bc-ad)^6}{3b^8(a+bx)^3}$$

Mathematica [A] time = 0.11, size = 173, normalized size = 0.93

$$\frac{12bd^5x(15a^2d^2 - 35abcd + 21b^2c^2) + 6b^2d^6x^2(7bc - 5ad) + 420d^4(bc - ad)^3 \log(a + bx) - \frac{420d^3(bc-ad)^4}{a+bx} + \frac{126d^2(a+bx)^4}{(a+bx)^2}}{12b^8}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^5, x]

[Out] (12*b*d^5*(21*b^2*c^2 - 35*a*b*c*d + 15*a^2*d^2)*x + 6*b^2*d^6*(7*b*c - 5*a*d)*x^2 + 4*b^3*d^7*x^3 - (3*(b*c - a*d)^7)/(a + b*x)^4 - (28*d*(b*c - a*d)^6)/(a + b*x)^3 + (126*d^2*(-(b*c) + a*d)^5)/(a + b*x)^2 - (420*d^3*(b*c - a*d)^4)/(a + b*x) + 420*d^4*(b*c - a*d)^3*Log[a + b*x])/(12*b^8)

fricas [B] time = 0.45, size = 754, normalized size = 4.03

$$\frac{4b^7d^7x^7 - 3b^7c^7 - 7ab^6c^6d - 21a^2b^5c^5d^2 - 105a^3b^4c^4d^3 + 875a^4b^3c^3d^4 - 1617a^5b^2c^2d^5 + 1197a^6bcd^6 - 319a^7d^7}{12b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^5, x, algorithm="fricas")

[Out] 1/12*(4*b^7*d^7*x^7 - 3*b^7*c^7 - 7*a*b^6*c^6*d - 21*a^2*b^5*c^5*d^2 - 105*a^3*b^4*c^4*d^3 + 875*a^4*b^3*c^3*d^4 - 1617*a^5*b^2*c^2*d^5 + 1197*a^6*b*c*d^6 - 319*a^7*d^7 + 14*(3*b^7*c*d^6 - a*b^6*d^7)*x^6 + 84*(3*b^7*c^2*d^5 - 3*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 4*(252*a*b^6*c^2*d^5 - 357*a^2*b^5*c*d^6 + 139*a^3*b^4*d^7)*x^4 - 4*(105*b^7*c^4*d^3 - 420*a*b^6*c^3*d^4 + 252*a^2*b^5*c^2*d^5 + 168*a^3*b^4*c*d^6 - 136*a^4*b^3*d^7)*x^3 - 6*(21*b^7*c^5*d^2 + 105*a*b^6*c^4*d^3 - 630*a^2*b^5*c^3*d^4 + 882*a^3*b^4*c^2*d^5 - 462*a^4*b^3*c*d^6 + 74*a^5*b^2*d^7)*x^2 - 4*(7*b^7*c^6*d + 21*a*b^6*c^5*d^2 + 105*a^2*b^5*c^4*d^3 - 770*a^3*b^4*c^3*d^4 + 1302*a^4*b^3*c^2*d^5 - 882*a^5*b^2*c*d^6 + 214*a^6*b*d^7)*x + 420*(a^4*b^3*c^3*d^4 - 3*a^5*b^2*c^2*d^5 + 3*a^6*b*c*d^6 - a^7*d^7 + (b^7*c^3*d^4 - 3*a*b^6*c^2*d^5 + 3*a^2*b^5*c*d^6 - a^3*b^4*d^7)*x^4 + 4*(a*b^6*c^3*d^4 - 3*a^2*b^5*c^2*d^5 + 3*a^3*b^4*c*d^6 - a^4*b^3*d^7)*x^3 + 6*(a^2*b^5*c^3*d^4 - 3*a^3*b^4*c^2*d^5 + 3*a^4*b^3*c*d^6 - a^5*b^2*d^7)*x^2 + 4*(a^3*b^4*c^3*d^4 - 3*a^4*b^3*c^2*d^5 + 3*a^5*b^2*c*d^6 - a^6*b*d^7)*x)*log(b*x + a))/(b^12*x^4 + 4*a*b^11*x^3 + 6*a^2*b^10*x^2 + 4*a^3*b^9*x + a^4*b^8)

giac [B] time = 1.29, size = 660, normalized size = 3.53

$$\frac{\left(2d^7 + \frac{21(b^2cd^6 - abd^7)}{(bx+a)b} + \frac{126(b^4c^2d^5 - 2ab^3cd^6 + a^2b^2d^7)}{(bx+a)^2b^2}\right)(bx+a)^3}{6b^8} - \frac{35(b^3c^3d^4 - 3ab^2c^2d^5 + 3a^2bcd^6 - a^3d^7) \log\left(\frac{|bx+a|}{bx+a}\right)}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^5,x, algorithm="giac")

[Out] $\frac{1}{6}(2d^7 + 21(b^2cd^6 - abd^7)/((bx+a)b) + 126(b^4c^2d^5 - 2ab^3cd^6 + a^2b^2d^7)/((bx+a)^2b^2)) * (bx+a)^3/b^8 - 35(b^3c^3d^4 - 3ab^2c^2d^5 + 3a^2b^2cd^6 - a^3d^7) * \log(\text{abs}(bx+a)/((bx+a)^2\text{abs}(b))) / b^8 - 1/12(3b^43c^7/(bx+a)^4 + 28b^42c^6d/(bx+a)^3 - 21ab^42c^6d/(bx+a)^4 + 126b^41c^5d^2/(bx+a)^2 - 168ab^41c^5d^2/(bx+a)^3 + 63a^2b^41c^5d^2/(bx+a)^4 + 420b^40c^4d^3/(bx+a) - 630ab^40c^4d^3/(bx+a)^2 + 420a^2b^40c^4d^3/(bx+a)^3 - 105a^3b^40c^4d^3/(bx+a)^4 - 1680ab^39c^3d^4/(bx+a) + 1260a^2b^39c^3d^4/(bx+a)^2 - 560a^3b^39c^3d^4/(bx+a)^3 + 105a^4b^39c^3d^4/(bx+a)^4 + 2520a^2b^38c^2d^5/(bx+a) - 1260a^3b^38c^2d^5/(bx+a)^2 + 420a^4b^38c^2d^5/(bx+a)^3 - 63a^5b^38c^2d^5/(bx+a)^4 - 1680a^3b^37c^2d^6/(bx+a) + 630a^4b^37c^2d^6/(bx+a)^2 - 168a^5b^37c^2d^6/(bx+a)^3 + 21a^6b^37c^2d^6/(bx+a)^4 + 420a^4b^36d^7/(bx+a) - 126a^5b^36d^7/(bx+a)^2 + 28a^6b^36d^7/(bx+a)^3 - 3a^7b^36d^7/(bx+a)^4) / b^44$

maple [B] time = 0.02, size = 641, normalized size = 3.43

$$\frac{a^7 d^7}{4(bx+a)^4 b^8} - \frac{7a^6 c d^6}{4(bx+a)^4 b^7} + \frac{21a^5 c^2 d^5}{4(bx+a)^4 b^6} - \frac{35a^4 c^3 d^4}{4(bx+a)^4 b^5} + \frac{35a^3 c^4 d^3}{4(bx+a)^4 b^4} - \frac{21a^2 c^5 d^2}{4(bx+a)^4 b^3} + \frac{7a c^6 d}{4(bx+a)^4 b^2} - \frac{a^7 d^7}{4(bx+a)^4 b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^5,x)

[Out] $\frac{21}{2}b^8d^7/(bx+a)^2a^5 - \frac{21}{2}b^3d^2/(bx+a)^2c^5 - 35/b^8d^7 \ln(bx+a) * a^3 + 35/b^5d^4 \ln(bx+a) * c^3 + 1/4/b^8/(bx+a)^4a^7d^7 - 35/b^8d^7/(bx+a) * a^4 - 35/b^4d^3/(bx+a) * c^4 - 5/2d^7/b^6x^2a + 7/2d^6/b^5x^2c + 15d^7/b^7a^2x + 21d^5/b^5c^2x - 7/3/b^8d^7/(bx+a)^3a^6 - 7/3/b^2d/(bx+a)^3c^6 + 1/3d^7/b^5x^3 - 1/4/b/(bx+a)^4c^7 - 35d^6/b^6a^2cx + 14/b^7d^6/(bx+a)^3a^5c - 35/b^6d^5/(bx+a)^3a^4c^2 + 140/3/b^5d^4/(bx+a)^3a^3c^3 - 35/b^4d^3/(bx+a)^3a^2c^4 + 105/b^7d^6 \ln(bx+a) * a^2c - 105/b^6d^5 \ln(bx+a) * ac^2 - 7/4/b^7/(bx+a)^4a^6cd^6 + 21/4/b^6/(bx+a)^4a^5c^2d^5 - 35/4/b^5/(bx+a)^4a^4c^3d^4 + 35/4/b^4/(bx+a)^4a^3c^4d^3 - 21/4/b^3/(bx+a)^4a^2c^5d^2 + 7/4/b^2/(bx+a)^4ac^6d + 140/b^7d^6/(bx+a) * a^3c - 210/b^6d^5/(bx+a) * a^2c^2 + 140/b^5d^4/(bx+a) * ac^3 + 14/b^3d^2/(bx+a)^3ac^5 - 105/2/b^7d^6/(bx+a)^2a^4c + 105/b^6d^5/(bx+a)^2a^3c^2 - 105/b^5d^4/(bx+a)^2a^2c^3 + 105/2/b^4d^3/(bx+a)^2ac^4$

maxima [B] time = 1.73, size = 494, normalized size = 2.64

$$\frac{3b^7c^7 + 7ab^6c^6d + 21a^2b^5c^5d^2 + 105a^3b^4c^4d^3 - 875a^4b^3c^3d^4 + 1617a^5b^2c^2d^5 - 1197a^6bcd^6 + 319a^7d^7 + 420}{4(bx+a)^4 b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^5,x, algorithm="maxima")

[Out]
$$-1/12*(3*b^7*c^7 + 7*a*b^6*c^6*d + 21*a^2*b^5*c^5*d^2 + 105*a^3*b^4*c^4*d^3 - 875*a^4*b^3*c^3*d^4 + 1617*a^5*b^2*c^2*d^5 - 1197*a^6*b*c*d^6 + 319*a^7*d^7 + 420*(b^7*c^4*d^3 - 4*a*b^6*c^3*d^4 + 6*a^2*b^5*c^2*d^5 - 4*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 126*(b^7*c^5*d^2 + 5*a*b^6*c^4*d^3 - 30*a^2*b^5*c^3*d^4 + 50*a^3*b^4*c^2*d^5 - 35*a^4*b^3*c*d^6 + 9*a^5*b^2*d^7)*x^2 + 28*(b^7*c^6*d + 3*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 - 110*a^3*b^4*c^3*d^4 + 195*a^4*b^3*c^2*d^5 - 141*a^5*b^2*c*d^6 + 37*a^6*b*d^7)*x)/(b^12*x^4 + 4*a*b^11*x^3 + 6*a^2*b^10*x^2 + 4*a^3*b^9*x + a^4*b^8) + 1/6*(2*b^2*d^7*x^3 + 3*(7*b^2*c*d^6 - 5*a*b*d^7)*x^2 + 6*(21*b^2*c^2*d^5 - 35*a*b*c*d^6 + 15*a^2*d^7)*x)/b^7 + 35*(b^3*c^3*d^4 - 3*a*b^2*c^2*d^5 + 3*a^2*b*c*d^6 - a^3*d^7)*log(b*x + a)/b^8$$

mupad [B] time = 0.77, size = 512, normalized size = 2.74

$$x \left(\frac{5a \left(\frac{5ad^7}{b^6} - \frac{7cd^6}{b^5} \right)}{b} - \frac{10a^2d^7}{b^7} + \frac{21c^2d^5}{b^5} \right) - x^2 \left(\frac{5ad^7}{2b^6} - \frac{7cd^6}{2b^5} \right) - \frac{319a^7d^7 - 1197a^6bcd^6 + 1617a^5b^2c^2d^5 - 875a^4b^3c^3d^4 + 319a^7d^7}{12b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^5,x)

[Out]
$$x*((5*a*((5*a*d^7)/b^6 - (7*c*d^6)/b^5))/b - (10*a^2*d^7)/b^7 + (21*c^2*d^5)/b^5) - x^2*((5*a*d^7)/(2*b^6) - (7*c*d^6)/(2*b^5)) - ((319*a^7*d^7 + 3*b^7*c^7 + 21*a^2*b^5*c^5*d^2 + 105*a^3*b^4*c^4*d^3 - 875*a^4*b^3*c^3*d^4 + 1617*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 1197*a^6*b*c*d^6)/(12*b) + x*((259*a^6*d^7)/3 + (7*b^6*c^6*d)/3 + 7*a*b^5*c^5*d^2 + 35*a^2*b^4*c^4*d^3 - (770*a^3*b^3*c^3*d^4)/3 + 455*a^4*b^2*c^2*d^5 - 329*a^5*b*c*d^6) + x^3*(35*a^4*b^2*d^7 + 35*b^6*c^4*d^3 - 140*a*b^5*c^3*d^4 - 140*a^3*b^3*c*d^6 + 210*a^2*b^4*c^2*d^5) + x^2*((189*a^5*b*d^7)/2 + (21*b^6*c^5*d^2)/2 + (105*a*b^5*c^4*d^3)/2 - (735*a^4*b^2*c*d^6)/2 - 315*a^2*b^4*c^3*d^4 + 525*a^3*b^3*c^2*d^5))/(a^4*b^7 + b^11*x^4 + 4*a^3*b^8*x + 4*a*b^10*x^3 + 6*a^2*b^9*x^2) - (log(a + b*x)*(35*a^3*d^7 - 35*b^3*c^3*d^4 + 105*a*b^2*c^2*d^5 - 105*a^2*b*c*d^6))/b^8 + (d^7*x^3)/(3*b^5)$$

sympy [B] time = 22.44, size = 500, normalized size = 2.67

$$x^2 \left(-\frac{5ad^7}{2b^6} + \frac{7cd^6}{2b^5} \right) + x \left(\frac{15a^2d^7}{b^7} - \frac{35acd^6}{b^6} + \frac{21c^2d^5}{b^5} \right) + \frac{-319a^7d^7 + 1197a^6bcd^6 - 1617a^5b^2c^2d^5 + 875a^4b^3c^3d^4 - \dots}{12b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**5,x)

[Out] $x^{**2}*(-5*a*d^{**7}/(2*b^{**6}) + 7*c*d^{**6}/(2*b^{**5})) + x*(15*a^{**2}*d^{**7}/b^{**7} - 35*a*c*d^{**6}/b^{**6} + 21*c^{**2}*d^{**5}/b^{**5}) + (-319*a^{**7}*d^{**7} + 1197*a^{**6}*b*c*d^{**6} - 1617*a^{**5}*b^{**2}*c^{**2}*d^{**5} + 875*a^{**4}*b^{**3}*c^{**3}*d^{**4} - 105*a^{**3}*b^{**4}*c^{**4}*d^{**3} - 21*a^{**2}*b^{**5}*c^{**5}*d^{**2} - 7*a*b^{**6}*c^{**6}*d - 3*b^{**7}*c^{**7} + x^{**3}*(-420*a^{**4}*b^{**3}*d^{**7} + 1680*a^{**3}*b^{**4}*c*d^{**6} - 2520*a^{**2}*b^{**5}*c^{**2}*d^{**5} + 1680*a*b^{**6}*c^{**3}*d^{**4} - 420*b^{**7}*c^{**4}*d^{**3}) + x^{**2}*(-1134*a^{**5}*b^{**2}*d^{**7} + 4410*a^{**4}*b^{**3}*c*d^{**6} - 6300*a^{**3}*b^{**4}*c^{**2}*d^{**5} + 3780*a^{**2}*b^{**5}*c^{**3}*d^{**4} - 630*a*b^{**6}*c^{**4}*d^{**3} - 126*b^{**7}*c^{**5}*d^{**2}) + x*(-1036*a^{**6}*b*d^{**7} + 3948*a^{**5}*b^{**2}*c*d^{**6} - 5460*a^{**4}*b^{**3}*c^{**2}*d^{**5} + 3080*a^{**3}*b^{**4}*c^{**3}*d^{**4} - 420*a^{**2}*b^{**5}*c^{**4}*d^{**3} - 84*a*b^{**6}*c^{**5}*d^{**2} - 28*b^{**7}*c^{**6}*d)/(12*a^{**4}*b^{**8} + 48*a^{**3}*b^{**9}*x + 72*a^{**2}*b^{**10}*x^{**2} + 48*a*b^{**11}*x^{**3} + 12*b^{**12}*x^{**4}) + d^{**7}*x^{**3}/(3*b^{**5}) - 35*d^{**4}*(a*d - b*c)^{**3}*log(a + b*x)/b^{**8}$

$$3.1288 \quad \int \frac{(c+dx)^7}{(a+bx)^6} dx$$

Optimal. Leaf size=181

$$\frac{21d^5(bc-ad)^2 \log(a+bx)}{b^8} - \frac{35d^4(bc-ad)^3}{b^8(a+bx)} - \frac{35d^3(bc-ad)^4}{2b^8(a+bx)^2} - \frac{7d^2(bc-ad)^5}{b^8(a+bx)^3} - \frac{7d(bc-ad)^6}{4b^8(a+bx)^4} - \frac{(bc-ad)^7}{5b^8(a+bx)^5} + \frac{d^6x(7bc-6ad)}{b^7}$$

[Out] $d^6*(-6*a*d+7*b*c)*x/b^7+1/2*d^7*x^2/b^6-1/5*(-a*d+b*c)^7/b^8/(b*x+a)^5-7/4*d*(-a*d+b*c)^6/b^8/(b*x+a)^4-7*d^2*(-a*d+b*c)^5/b^8/(b*x+a)^3-35/2*d^3*(-a*d+b*c)^4/b^8/(b*x+a)^2-35*d^4*(-a*d+b*c)^3/b^8/(b*x+a)+21*d^5*(-a*d+b*c)^2*\ln(b*x+a)/b^8$

Rubi [A] time = 0.19, antiderivative size = 181, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{d^6x(7bc-6ad)}{b^7} - \frac{35d^4(bc-ad)^3}{b^8(a+bx)} - \frac{35d^3(bc-ad)^4}{2b^8(a+bx)^2} - \frac{7d^2(bc-ad)^5}{b^8(a+bx)^3} + \frac{21d^5(bc-ad)^2 \log(a+bx)}{b^8} - \frac{7d(bc-ad)^6}{4b^8(a+bx)^4} - \frac{(bc-ad)^7}{5b^8(a+bx)^5} + \frac{d^6x(7bc-6ad)}{b^7}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^6, x]

[Out] $(d^6*(7*b*c - 6*a*d)*x)/b^7 + (d^7*x^2)/(2*b^6) - (b*c - a*d)^7/(5*b^8*(a + b*x)^5) - (7*d*(b*c - a*d)^6)/(4*b^8*(a + b*x)^4) - (7*d^2*(b*c - a*d)^5)/(b^8*(a + b*x)^3) - (35*d^3*(b*c - a*d)^4)/(2*b^8*(a + b*x)^2) - (35*d^4*(b*c - a*d)^3)/(b^8*(a + b*x)) + (21*d^5*(b*c - a*d)^2*Log[a + b*x])/b^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^6} dx = \int \left(\frac{d^6(7bc-6ad)}{b^7} + \frac{d^7x}{b^6} + \frac{(bc-ad)^7}{b^7(a+bx)^6} + \frac{7d(bc-ad)^6}{b^7(a+bx)^5} + \frac{21d^2(bc-ad)^5}{b^7(a+bx)^4} + \frac{35d^3(bc-ad)^4}{b^7(a+bx)^3} + \frac{d^6(7bc-6ad)x}{b^7} + \frac{d^7x^2}{2b^6} - \frac{(bc-ad)^7}{5b^8(a+bx)^5} - \frac{7d(bc-ad)^6}{4b^8(a+bx)^4} - \frac{7d^2(bc-ad)^5}{b^8(a+bx)^3} - \frac{35d^3(bc-ad)^4}{2b^8(a+bx)^2} - \frac{35d^4(bc-ad)^3}{b^8(a+bx)} - \frac{35d^5(bc-ad)^2 \log(a+bx)}{b^8} - \frac{7d^6(bc-ad)}{4b^8(a+bx)^4} - \frac{d^7(bc-ad)}{5b^8(a+bx)^5} + \frac{d^8x^2}{2b^8} \right) dx$$

Mathematica [B] time = 0.15, size = 389, normalized size = 2.15

$$459a^7d^7 + 3a^6bd^6(625dx - 406c) + a^5b^2d^5(959c^2 - 5250cdx + 2700d^2x^2) + 5a^4b^3d^4(-28c^3 + 875c^2dx - 1680cdx^2 + 260d^3x^3) - 5a^3b^4d^3(7c^4 + 140c^3dx - 1540c^2d^2x^2 + 1120cd^3x^3 + 80d^4x^4) - a^2b^5d^2(14c^5 + 175c^4dx + 1400c^3d^2x^2 - 6300c^2d^3x^3 + 700cd^4x^4 + 500d^5x^5) - 7ab^6d(c^6 + 10c^5dx + 50c^4d^2x^2 + 200c^3d^3x^3 - 300c^2d^4x^4 - 100cd^5x^5 + 10d^6x^6) - b^7(4c^7 + 35c^6dx + 140c^5d^2x^2 + 350c^4d^3x^3 + 700c^3d^4x^4 - 140cd^6x^6 - 10d^7x^7) + 420d^5(bc - a*d)^2(a + b*x)^5 \text{Log}[a + b*x] / (20b^8(a + b*x)^5)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^6,x]

[Out] (459*a^7*d^7 + 3*a^6*b*d^6*(-406*c + 625*d*x) + a^5*b^2*d^5*(959*c^2 - 5250*c*d*x + 2700*d^2*x^2) + 5*a^4*b^3*d^4*(-28*c^3 + 875*c^2*d*x - 1680*c*d^2*x^2 + 260*d^3*x^3) - 5*a^3*b^4*d^3*(7*c^4 + 140*c^3*d*x - 1540*c^2*d^2*x^2 + 1120*c*d^3*x^3 + 80*d^4*x^4) - a^2*b^5*d^2*(14*c^5 + 175*c^4*d*x + 1400*c^3*d^2*x^2 - 6300*c^2*d^3*x^3 + 700*c*d^4*x^4 + 500*d^5*x^5) - 7*a*b^6*d*(c^6 + 10*c^5*d*x + 50*c^4*d^2*x^2 + 200*c^3*d^3*x^3 - 300*c^2*d^4*x^4 - 100*c*d^5*x^5 + 10*d^6*x^6) - b^7*(4*c^7 + 35*c^6*d*x + 140*c^5*d^2*x^2 + 350*c^4*d^3*x^3 + 700*c^3*d^4*x^4 - 140*c*d^6*x^6 - 10*d^7*x^7) + 420*d^5*(b*c - a*d)^2*(a + b*x)^5*Log[a + b*x])/(20*b^8*(a + b*x)^5)

fricas [B] time = 0.43, size = 732, normalized size = 4.04

$$10b^7d^7x^7 - 4b^7c^7 - 7ab^6c^6d - 14a^2b^5c^5d^2 - 35a^3b^4c^4d^3 - 140a^4b^3c^3d^4 + 959a^5b^2c^2d^5 - 1218a^6bcd^6 + 459a^7d^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^6,x, algorithm="fricas")

[Out] 1/20*(10*b^7*d^7*x^7 - 4*b^7*c^7 - 7*a*b^6*c^6*d - 14*a^2*b^5*c^5*d^2 - 35*a^3*b^4*c^4*d^3 - 140*a^4*b^3*c^3*d^4 + 959*a^5*b^2*c^2*d^5 - 1218*a^6*b*c*d^6 + 459*a^7*d^7 + 70*(2*b^7*c*d^6 - a*b^6*d^7)*x^6 + 100*(7*a*b^6*c*d^6 - 5*a^2*b^5*d^7)*x^5 - 100*(7*b^7*c^3*d^4 - 21*a*b^6*c^2*d^5 + 7*a^2*b^5*c*d^6 + 4*a^3*b^4*d^7)*x^4 - 50*(7*b^7*c^4*d^3 + 28*a*b^6*c^3*d^4 - 126*a^2*b^5*c^2*d^5 + 112*a^3*b^4*c*d^6 - 26*a^4*b^3*d^7)*x^3 - 10*(14*b^7*c^5*d^2 + 35*a*b^6*c^4*d^3 + 140*a^2*b^5*c^3*d^4 - 770*a^3*b^4*c^2*d^5 + 840*a^4*b^3*c*d^6 - 270*a^5*b^2*d^7)*x^2 - 5*(7*b^7*c^6*d + 14*a*b^6*c^5*d^2 + 35*a^2*b^5*c^4*d^3 + 140*a^3*b^4*c^3*d^4 - 875*a^4*b^3*c^2*d^5 + 1050*a^5*b^2*c*d^6 - 375*a^6*b*d^7)*x + 420*(a^5*b^2*c^2*d^5 - 2*a^6*b*c*d^6 + a^7*d^7 + (b^7*c^2*d^5 - 2*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 5*(a*b^6*c^2*d^5 - 2*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 10*(a^2*b^5*c^2*d^5 - 2*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 10*(a^3*b^4*c^2*d^5 - 2*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 5*(a^4*b^3*c^2*d^5 - 2*a^5*b^2*c*d^6 + a^6*b*d^7)*x)*log(b*x + a)/(b^13*x^5 + 5*a*b^12*x^4 + 10*a^2*b^11*x^3 + 10*a^3*b^10*x^2 + 5*a^4*b^9*x + a^5*b^8)

giac [B] time = 1.38, size = 463, normalized size = 2.56

$$\frac{21(b^2c^2d^5 - 2abcd^6 + a^2d^7) \log(|bx + a|)}{b^8} + \frac{b^6d^7x^2 + 14b^6cd^6x - 12ab^5d^7x}{2b^{12}} - \frac{4b^7c^7 + 7ab^6c^6d + 14a^2b^5c^5d^2 + \dots}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^6,x, algorithm="giac")

[Out] 21*(b^2*c^2*d^5 - 2*a*b*c*d^6 + a^2*d^7)*log(abs(b*x + a))/b^8 + 1/2*(b^6*d^7*x^2 + 14*b^6*c*d^6*x - 12*a*b^5*d^7*x)/b^12 - 1/20*(4*b^7*c^7 + 7*a*b^6*c^6*d + 14*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 + 140*a^4*b^3*c^3*d^4 - 959*a^5*b^2*c^2*d^5 + 1218*a^6*b*c*d^6 - 459*a^7*d^7 + 700*(b^7*c^3*d^4 - 3*a*b^6*c^2*d^5 + 3*a^2*b^5*c*d^6 - a^3*b^4*d^7)*x^4 + 350*(b^7*c^4*d^3 + 4*a*b^6*c^3*d^4 - 18*a^2*b^5*c^2*d^5 + 20*a^3*b^4*c*d^6 - 7*a^4*b^3*d^7)*x^3 + 70*(2*b^7*c^5*d^2 + 5*a*b^6*c^4*d^3 + 20*a^2*b^5*c^3*d^4 - 110*a^3*b^4*c^2*d^5 + 130*a^4*b^3*c*d^6 - 47*a^5*b^2*d^7)*x^2 + 35*(b^7*c^6*d + 2*a*b^6*c^5*d^2 + 5*a^2*b^5*c^4*d^3 + 20*a^3*b^4*c^3*d^4 - 125*a^4*b^3*c^2*d^5 + 154*a^5*b^2*c*d^6 - 57*a^6*b*d^7)*x)/((b*x + a)^5*b^8)

maple [B] time = 0.01, size = 656, normalized size = 3.62

$$\frac{a^7d^7}{5(bx+a)^5b^8} - \frac{7a^6cd^6}{5(bx+a)^5b^7} + \frac{21a^5c^2d^5}{5(bx+a)^5b^6} - \frac{7a^4c^3d^4}{(bx+a)^5b^5} + \frac{7a^3c^4d^3}{(bx+a)^5b^4} - \frac{21a^2c^5d^2}{5(bx+a)^5b^3} + \frac{7ac^6d}{5(bx+a)^5b^2} - \frac{c^7}{5(bx+a)^5b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^6,x)

[Out] -105/b^7*d^6/(b*x+a)*a^2*c+105/b^6*d^5/(b*x+a)*a*c^2+1/2*d^7*x^2/b^6-35/2/b^4*d^3/(b*x+a)^2*c^4-6*d^7/b^7*a*x+7*d^6/b^6*x*c+35/b^8*d^7/(b*x+a)*a^3-35/b^5*d^4/(b*x+a)*c^3+21/b^8*d^7*ln(b*x+a)*a^2+21/b^6*d^5*ln(b*x+a)*c^2-7/4/b^8*d^7/(b*x+a)^4*a^6-7/4/b^2*d/(b*x+a)^4*c^6+7/b^8*d^7/(b*x+a)^3*a^5-7/b^3*d^2/(b*x+a)^3*c^5+1/5/b^8/(b*x+a)^5*a^7*d^7-35/2/b^8*d^7/(b*x+a)^2*a^4+7/b^4/(b*x+a)^5*a^3*c^4*d^3-21/5/b^3/(b*x+a)^5*a^2*c^5*d^2-1/5/b/(b*x+a)^5*c^7-35/b^7*d^6/(b*x+a)^3*a^4*c+70/b^6*d^5/(b*x+a)^3*a^3*c^2-70/b^5*d^4/(b*x+a)^3*a^2*c^3+35/b^4*d^3/(b*x+a)^3*a*c^4-7/5/b^7/(b*x+a)^5*a^6*c*d^6+21/5/b^6/(b*x+a)^5*a^5*c^2*d^5-7/b^5/(b*x+a)^5*a^4*c^3*d^4-105/b^6*d^5/(b*x+a)^2*a^2*c^2+70/b^5*d^4/(b*x+a)^2*a*c^3-42/b^7*d^6*ln(b*x+a)*a*c+21/2/b^7*d^6/(b*x+a)^4*a^5*c+7/5/b^2/(b*x+a)^5*a*c^6*d+70/b^7*d^6/(b*x+a)^2*a^3*c-105/4/b^6*d^5/(b*x+a)^4*a^4*c^2+35/b^5*d^4/(b*x+a)^4*a^3*c^3-105/4/b^4*d^3/(b*x+a)^4*a^2*c^4+21/2/b^3*d^2/(b*x+a)^4*a*c^5

maxima [B] time = 1.82, size = 504, normalized size = 2.78

$$\frac{4b^7c^7 + 7ab^6c^6d + 14a^2b^5c^5d^2 + 35a^3b^4c^4d^3 + 140a^4b^3c^3d^4 - 959a^5b^2c^2d^5 + 1218a^6bcd^6 - 459a^7d^7 + 700 \dots}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^6,x, algorithm="maxima")

[Out]
$$\begin{aligned} & -1/20*(4*b^7*c^7 + 7*a*b^6*c^6*d + 14*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 \\ & + 140*a^4*b^3*c^3*d^4 - 959*a^5*b^2*c^2*d^5 + 1218*a^6*b*c*d^6 - 459*a^7*d^7 \\ & + 700*(b^7*c^3*d^4 - 3*a*b^6*c^2*d^5 + 3*a^2*b^5*c*d^6 - a^3*b^4*d^7)*x^4 \\ & + 350*(b^7*c^4*d^3 + 4*a*b^6*c^3*d^4 - 18*a^2*b^5*c^2*d^5 + 20*a^3*b^4*c*d^6 \\ & - 7*a^4*b^3*d^7)*x^3 + 70*(2*b^7*c^5*d^2 + 5*a*b^6*c^4*d^3 + 20*a^2*b^5*c^3*d^4 \\ & - 110*a^3*b^4*c^2*d^5 + 130*a^4*b^3*c*d^6 - 47*a^5*b^2*d^7)*x^2 + 35*(b^7*c^6*d \\ & + 2*a*b^6*c^5*d^2 + 5*a^2*b^5*c^4*d^3 + 20*a^3*b^4*c^3*d^4 - 125*a^4*b^3*c^2*d^5 \\ & + 154*a^5*b^2*c*d^6 - 57*a^6*b*d^7)*x)/(b^13*x^5 + 5*a*b^12*x^4 + 10*a^2*b^11*x^3 \\ & + 10*a^3*b^10*x^2 + 5*a^4*b^9*x + a^5*b^8) + 1/2*(b*d^7*x^2 + 2*(7*b*c*d^6 - 6*a*d^7)*x)/b^7 + 21*(b^2*c^2*d^5 - 2*a*b*c*d^6 \\ & + a^2*d^7)*\log(b*x + a)/b^8 \end{aligned}$$

mupad [B] time = 0.34, size = 508, normalized size = 2.81

$$\frac{\ln(a + bx) \left(21 a^2 d^7 - 42 a b c d^6 + 21 b^2 c^2 d^5 \right)}{b^8} - x \left(\frac{6 a d^7}{b^7} - \frac{7 c d^6}{b^6} \right) - \frac{-459 a^7 d^7 + 1218 a^6 b c d^6 - 959 a^5 b^2 c^2 d^5 + 140 a^4 b^3 c^3 d^4 + \dots}{20 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^6,x)

[Out]
$$\begin{aligned} & (\log(a + b*x)*(21*a^2*d^7 + 21*b^2*c^2*d^5 - 42*a*b*c*d^6))/b^8 - x*((6*a*d^7)/b^7 \\ & - (7*c*d^6)/b^6) - ((4*b^7*c^7 - 459*a^7*d^7 + 14*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 \\ & + 140*a^4*b^3*c^3*d^4 - 959*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d + 1218*a^6*b*c*d^6)/(20*b) \\ & + x*((7*b^6*c^6*d)/4 - (399*a^6*d^7)/4 + (7*a*b^5*c^5*d^2)/2 + (35*a^2*b^4*c^4*d^3)/4 \\ & + 35*a^3*b^3*c^3*d^4 - (875*a^4*b^2*c^2*d^5)/4 + (539*a^5*b*c*d^6)/2) + x^3*((35*b^6*c^4*d^3)/2 \\ & - (245*a^4*b^2*d^7)/2 + 70*a*b^5*c^3*d^4 + 350*a^3*b^3*c*d^6 - 315*a^2*b^4*c^2*d^5) \\ & + x^2*(7*b^6*c^5*d^2 - (329*a^5*b*d^7)/2 + (35*a*b^5*c^4*d^3)/2 + 455*a^4*b^2*c*d^6 \\ & + 70*a^2*b^4*c^3*d^4 - 385*a^3*b^3*c^2*d^5) - x^4*(35*a^3*b^3*d^7 - 35*b^6*c^3*d^4 \\ & + 105*a*b^5*c^2*d^5 - 105*a^2*b^4*c*d^6)/(a^5*b^7 + b^12*x^5 + 5*a^4*b^8*x \\ & + 5*a*b^11*x^4 + 10*a^3*b^9*x^2 + 10*a^2*b^10*x^3) + (d^7*x^2)/(2*b^6) \end{aligned}$$

sympy [B] time = 97.19, size = 524, normalized size = 2.90

$$x \left(-\frac{6 a d^7}{b^7} + \frac{7 c d^6}{b^6} \right) + \frac{459 a^7 d^7 - 1218 a^6 b c d^6 + 959 a^5 b^2 c^2 d^5 - 140 a^4 b^3 c^3 d^4 - 35 a^3 b^4 c^4 d^3 - 14 a^2 b^5 c^5 d^2 - 7 a b^6 c^6 d - \dots}{20 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**6,x)

```
[Out] x*(-6*a*d**7/b**7 + 7*c*d**6/b**6) + (459*a**7*d**7 - 1218*a**6*b*c*d**6 +
959*a**5*b**2*c**2*d**5 - 140*a**4*b**3*c**3*d**4 - 35*a**3*b**4*c**4*d**3
- 14*a**2*b**5*c**5*d**2 - 7*a*b**6*c**6*d - 4*b**7*c**7 + x**4*(700*a**3*b
**4*d**7 - 2100*a**2*b**5*c*d**6 + 2100*a*b**6*c**2*d**5 - 700*b**7*c**3*d
**4) + x**3*(2450*a**4*b**3*d**7 - 7000*a**3*b**4*c*d**6 + 6300*a**2*b**5*c
**2*d**5 - 1400*a*b**6*c**3*d**4 - 350*b**7*c**4*d**3) + x**2*(3290*a**5*b**
2*d**7 - 9100*a**4*b**3*c*d**6 + 7700*a**3*b**4*c**2*d**5 - 1400*a**2*b**5*
c**3*d**4 - 350*a*b**6*c**4*d**3 - 140*b**7*c**5*d**2) + x*(1995*a**6*b*d**
7 - 5390*a**5*b**2*c*d**6 + 4375*a**4*b**3*c**2*d**5 - 700*a**3*b**4*c**3*d
**4 - 175*a**2*b**5*c**4*d**3 - 70*a*b**6*c**5*d**2 - 35*b**7*c**6*d))/(20*
a**5*b**8 + 100*a**4*b**9*x + 200*a**3*b**10*x**2 + 200*a**2*b**11*x**3 + 1
00*a*b**12*x**4 + 20*b**13*x**5) + d**7*x**2/(2*b**6) + 21*d**5*(a*d - b*c)
**2*log(a + b*x)/b**8
```

$$3.1289 \quad \int \frac{(c+dx)^7}{(a+bx)^7} dx$$

Optimal. Leaf size=186

$$\frac{7d^6(bc-ad)\log(a+bx)}{b^8} - \frac{21d^5(bc-ad)^2}{b^8(a+bx)} - \frac{35d^4(bc-ad)^3}{2b^8(a+bx)^2} - \frac{35d^3(bc-ad)^4}{3b^8(a+bx)^3} - \frac{21d^2(bc-ad)^5}{4b^8(a+bx)^4} - \frac{7d(bc-ad)^6}{5b^8(a+bx)^5} - \frac{(bc-ad)^7}{6b^8(a+bx)^6}$$

[Out] $d^7*x/b^7-1/6*(-a*d+b*c)^7/b^8/(b*x+a)^6-7/5*d*(-a*d+b*c)^6/b^8/(b*x+a)^5-2/4*d^2*(-a*d+b*c)^5/b^8/(b*x+a)^4-35/3*d^3*(-a*d+b*c)^4/b^8/(b*x+a)^3-35/2*d^4*(-a*d+b*c)^3/b^8/(b*x+a)^2-21*d^5*(-a*d+b*c)^2/b^8/(b*x+a)+7*d^6*(-a*d+b*c)*\ln(b*x+a)/b^8$

Rubi [A] time = 0.17, antiderivative size = 186, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{21d^5(bc-ad)^2}{b^8(a+bx)} - \frac{35d^4(bc-ad)^3}{2b^8(a+bx)^2} - \frac{35d^3(bc-ad)^4}{3b^8(a+bx)^3} - \frac{21d^2(bc-ad)^5}{4b^8(a+bx)^4} + \frac{7d^6(bc-ad)\log(a+bx)}{b^8} - \frac{7d(bc-ad)^6}{5b^8(a+bx)^5} - \frac{(bc-ad)^7}{6b^8(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^7, x]

[Out] $(d^7*x)/b^7 - (b*c - a*d)^7/(6*b^8*(a + b*x)^6) - (7*d*(b*c - a*d)^6)/(5*b^8*(a + b*x)^5) - (21*d^2*(b*c - a*d)^5)/(4*b^8*(a + b*x)^4) - (35*d^3*(b*c - a*d)^4)/(3*b^8*(a + b*x)^3) - (35*d^4*(b*c - a*d)^3)/(2*b^8*(a + b*x)^2) - (21*d^5*(b*c - a*d)^2)/(b^8*(a + b*x)) + (7*d^6*(b*c - a*d)*\text{Log}[a + b*x])/b^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^7} dx = \int \left(\frac{d^7}{b^7} + \frac{(bc-ad)^7}{b^7(a+bx)^7} + \frac{7d(bc-ad)^6}{b^7(a+bx)^6} + \frac{21d^2(bc-ad)^5}{b^7(a+bx)^5} + \frac{35d^3(bc-ad)^4}{b^7(a+bx)^4} + \frac{35d^4(bc-ad)^3}{b^7(a+bx)^3} + \frac{21d^5(bc-ad)^2}{b^7(a+bx)^2} + \frac{7d^6(bc-ad)\log(a+bx)}{b^7} \right) dx$$

Mathematica [B] time = 0.20, size = 390, normalized size = 2.10

$$\frac{669a^7d^7 + 3a^6bd^6(1198dx - 343c) + 3a^5b^2d^5(70c^2 - 1918cdx + 2575d^2x^2) + 5a^4b^3d^4(14c^3 + 252c^2dx - 2625$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^7,x]

[Out]
$$\frac{-1/60*(669*a^7*d^7 + 3*a^6*b*d^6*(-343*c + 1198*d*x) + 3*a^5*b^2*d^5*(70*c^2 - 1918*c*d*x + 2575*d^2*x^2) + 5*a^4*b^3*d^4*(14*c^3 + 252*c^2*d*x - 2625*c*d^2*x^2 + 1640*d^3*x^3) + 5*a^3*b^4*d^3*(7*c^4 + 84*c^3*d*x + 630*c^2*d^2*x^2 - 3080*c*d^3*x^3 + 810*d^4*x^4) + 3*a^2*b^5*d^2*(7*c^5 + 70*c^4*d*x + 350*c^3*d^2*x^2 + 1400*c^2*d^3*x^3 - 3150*c*d^4*x^4 + 120*d^5*x^5) + a*b^6*d*(14*c^6 + 126*c^5*d*x + 525*c^4*d^2*x^2 + 1400*c^3*d^3*x^3 + 3150*c^2*d^4*x^4 - 2520*c*d^5*x^5 - 360*d^6*x^6) + b^7*(10*c^7 + 84*c^6*d*x + 315*c^5*d^2*x^2 + 700*c^4*d^3*x^3 + 1050*c^3*d^4*x^4 + 1260*c^2*d^5*x^5 - 60*d^7*x^7) + 420*d^6*(-(b*c) + a*d)*(a + b*x)^6*\text{Log}[a + b*x])}{(b^8*(a + b*x)^6}$$

fricas [B] time = 0.44, size = 692, normalized size = 3.72

$$\frac{60b^7d^7x^7 + 360ab^6d^7x^6 - 10b^7c^7 - 14ab^6c^6d - 21a^2b^5c^5d^2 - 35a^3b^4c^4d^3 - 70a^4b^3c^3d^4 - 210a^5b^2c^2d^5 + 1029$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^7,x, algorithm="fricas")

[Out]
$$\frac{1/60*(60*b^7*d^7*x^7 + 360*a*b^6*d^7*x^6 - 10*b^7*c^7 - 14*a*b^6*c^6*d - 21*a^2*b^5*c^5*d^2 - 35*a^3*b^4*c^4*d^3 - 70*a^4*b^3*c^3*d^4 - 210*a^5*b^2*c^2*d^5 + 1029*a^6*b*c*d^6 - 669*a^7*d^7 - 180*(7*b^7*c^2*d^5 - 14*a*b^6*c*d^6 + 2*a^2*b^5*d^7)*x^5 - 150*(7*b^7*c^3*d^4 + 21*a*b^6*c^2*d^5 - 63*a^2*b^5*c*d^6 + 27*a^3*b^4*d^7)*x^4 - 100*(7*b^7*c^4*d^3 + 14*a*b^6*c^3*d^4 + 42*a^2*b^5*c^2*d^5 - 154*a^3*b^4*c*d^6 + 82*a^4*b^3*d^7)*x^3 - 15*(21*b^7*c^5*d^2 + 35*a*b^6*c^4*d^3 + 70*a^2*b^5*c^3*d^4 + 210*a^3*b^4*c^2*d^5 - 875*a^4*b^3*c*d^6 + 515*a^5*b^2*d^7)*x^2 - 6*(14*b^7*c^6*d + 21*a*b^6*c^5*d^2 + 35*a^2*b^5*c^4*d^3 + 70*a^3*b^4*c^3*d^4 + 210*a^4*b^3*c^2*d^5 - 959*a^5*b^2*c*d^6 + 599*a^6*b*d^7)*x + 420*(a^6*b*c*d^6 - a^7*d^7 + (b^7*c*d^6 - a*b^6*d^7)*x^6 + 6*(a*b^6*c*d^6 - a^2*b^5*d^7)*x^5 + 15*(a^2*b^5*c*d^6 - a^3*b^4*d^7)*x^4 + 20*(a^3*b^4*c*d^6 - a^4*b^3*d^7)*x^3 + 15*(a^4*b^3*c*d^6 - a^5*b^2*d^7)*x^2 + 6*(a^5*b^2*c*d^6 - a^6*b*d^7)*x)*\text{log}(b*x + a)}{(b^14*x^6 + 6*a*b^13*x^5 + 15*a^2*b^12*x^4 + 20*a^3*b^11*x^3 + 15*a^4*b^10*x^2 + 6*a^5*b^9*x + a^6*b^8)}$$

giac [B] time = 1.30, size = 459, normalized size = 2.47

$$\frac{d^7 x}{b^7} + \frac{7(bcd^6 - ad^7) \log(|bx + a|)}{b^8} - \frac{10b^7c^7 + 14ab^6c^6d + 21a^2b^5c^5d^2 + 35a^3b^4c^4d^3 + 70a^4b^3c^3d^4 + 210a^5b^2c^2d^5}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^7,x, algorithm="giac")

[Out] $d^7x/b^7 + 7*(b*c*d^6 - a*d^7)*\log(\text{abs}(b*x + a))/b^8 - 1/60*(10*b^7*c^7 + 14*a*b^6*c^6*d + 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 + 70*a^4*b^3*c^3*d^4 + 210*a^5*b^2*c^2*d^5 - 1029*a^6*b*c*d^6 + 669*a^7*d^7 + 1260*(b^7*c^2*d^5 - 2*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 1050*(b^7*c^3*d^4 + 3*a*b^6*c^2*d^5 - 9*a^2*b^5*c*d^6 + 5*a^3*b^4*d^7)*x^4 + 700*(b^7*c^4*d^3 + 2*a*b^6*c^3*d^4 + 6*a^2*b^5*c^2*d^5 - 22*a^3*b^4*c*d^6 + 13*a^4*b^3*d^7)*x^3 + 105*(3*b^7*c^5*d^2 + 5*a*b^6*c^4*d^3 + 10*a^2*b^5*c^3*d^4 + 30*a^3*b^4*c^2*d^5 - 125*a^4*b^3*c*d^6 + 77*a^5*b^2*d^7)*x^2 + 42*(2*b^7*c^6*d + 3*a*b^6*c^5*d^2 + 5*a^2*b^5*c^4*d^3 + 10*a^3*b^4*c^3*d^4 + 30*a^4*b^3*c^2*d^5 - 137*a^5*b^2*c*d^6 + 87*a^6*b*d^7)*x)/((b*x + a)^6*b^8)$

maple [B] time = 0.01, size = 666, normalized size = 3.58

$$\frac{a^7 d^7}{6(bx+a)^6 b^8} - \frac{7a^6 c d^6}{6(bx+a)^6 b^7} + \frac{7a^5 c^2 d^5}{2(bx+a)^6 b^6} - \frac{35a^4 c^3 d^4}{6(bx+a)^6 b^5} + \frac{35a^3 c^4 d^3}{6(bx+a)^6 b^4} - \frac{7a^2 c^5 d^2}{2(bx+a)^6 b^3} + \frac{7a c^6 d}{6(bx+a)^6 b^2} - \frac{1}{6(bx+a)^6 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^7,x)

[Out] $42/5/b^3*d^2/(b*x+a)^5*a*c^5-105/2/b^7*d^6/(b*x+a)^2*a^2*c^7/b^7*d^6*\ln(b*x+a)*c-7/5/b^2*d/(b*x+a)^5*c^6+35/2/b^8*d^7/(b*x+a)^2*a^3-35/2/b^5*d^4/(b*x+a)^2*c^3-7/b^8*d^7*\ln(b*x+a)*a+1/6/b^8/(b*x+a)^6*a^7*d^7+21/4/b^8*d^7/(b*x+a)^4*a^5-21/4/b^3*d^2/(b*x+a)^4*c^5-21/b^8*d^7/(b*x+a)*a^2-21/b^6*d^5/(b*x+a)*c^2-35/3/b^8*d^7/(b*x+a)^3*a^4+d^7*x/b^7-35/3/b^4*d^3/(b*x+a)^3*c^4-7/5/b^8*d^7/(b*x+a)^5*a^6+42/b^7*d^6/(b*x+a)*a*c-7/6/b^7/(b*x+a)^6*a^6*c*d^6-1/6/b/(b*x+a)^6*c^7+105/2/b^6*d^5/(b*x+a)^2*a*c^2+140/3/b^7*d^6/(b*x+a)^3*a^3*c-70/b^6*d^5/(b*x+a)^3*a^2*c^2+140/3/b^5*d^4/(b*x+a)^3*a*c^3+35/6/b^4/(b*x+a)^6*a^3*c^4*d^3-7/2/b^3/(b*x+a)^6*a^2*c^5*d^2+7/6/b^2/(b*x+a)^6*a*c^6*d+7/2/b^6/(b*x+a)^6*a^5*c^2*d^5-35/6/b^5/(b*x+a)^6*a^4*c^3*d^4-105/4/b^7*d^6/(b*x+a)^4*a^4*c+105/2/b^6*d^5/(b*x+a)^4*a^3*c^2-105/2/b^5*d^4/(b*x+a)^4*a^2*c^3+105/4/b^4*d^3/(b*x+a)^4*a*c^4+42/5/b^7*d^6/(b*x+a)^5*a^5*c-21/b^6*d^5/(b*x+a)^5*a^4*c^2+28/b^5*d^4/(b*x+a)^5*a^3*c^3-21/b^4*d^3/(b*x+a)^5*a^2*c^4$

maxima [B] time = 1.80, size = 516, normalized size = 2.77

$$\frac{d^7 x}{b^7} - \frac{10b^7c^7 + 14ab^6c^6d + 21a^2b^5c^5d^2 + 35a^3b^4c^4d^3 + 70a^4b^3c^3d^4 + 210a^5b^2c^2d^5 - 1029a^6bcd^6 + 669a^7d^7 + 1}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^7,x, algorithm="maxima")

[Out] $d^7*x/b^7 - 1/60*(10*b^7*c^7 + 14*a*b^6*c^6*d + 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 + 70*a^4*b^3*c^3*d^4 + 210*a^5*b^2*c^2*d^5 - 1029*a^6*b*c*d^6 + 669*a^7*d^7 + 1260*(b^7*c^2*d^5 - 2*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 1050*(b^7*c^3*d^4 + 3*a*b^6*c^2*d^5 - 9*a^2*b^5*c*d^6 + 5*a^3*b^4*d^7)*x^4 + 700*(b^7*c^4*d^3 + 2*a*b^6*c^3*d^4 + 6*a^2*b^5*c^2*d^5 - 22*a^3*b^4*c*d^6 + 13*a^4*b^3*d^7)*x^3 + 105*(3*b^7*c^5*d^2 + 5*a*b^6*c^4*d^3 + 10*a^2*b^5*c^3*d^4 + 30*a^3*b^4*c^2*d^5 - 125*a^4*b^3*c*d^6 + 77*a^5*b^2*d^7)*x^2 + 42*(2*b^7*c^6*d + 3*a*b^6*c^5*d^2 + 5*a^2*b^5*c^4*d^3 + 10*a^3*b^4*c^3*d^4 + 30*a^4*b^3*c^2*d^5 - 137*a^5*b^2*c*d^6 + 87*a^6*b*d^7)*x)/(b^14*x^6 + 6*a*b^13*x^5 + 15*a^2*b^12*x^4 + 20*a^3*b^11*x^3 + 15*a^4*b^10*x^2 + 6*a^5*b^9*x + a^6*b^8) + 7*(b*c*d^6 - a*d^7)*log(b*x + a)/b^8$

mupad [B] time = 0.37, size = 517, normalized size = 2.78

$$\frac{d^7 x}{b^7} \frac{\ln(a + bx) (7a d^7 - 7b c d^6)}{b^8} \frac{669 a^7 d^7 - 1029 a^6 b c d^6 + 210 a^5 b^2 c^2 d^5 + 70 a^4 b^3 c^3 d^4 + 35 a^3 b^4 c^4 d^3 + 21 a^2 b^5 c^5 d^2 + 14 a b^6 c^6 d + 10 a^7 d^7}{60 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^7,x)

[Out] $(d^7*x)/b^7 - (\log(a + b*x)*(7*a*d^7 - 7*b*c*d^6))/b^8 - ((669*a^7*d^7 + 10*b^7*c^7 + 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 + 70*a^4*b^3*c^3*d^4 + 210*a^5*b^2*c^2*d^5 + 14*a*b^6*c^6*d - 1029*a^6*b*c*d^6)/(60*b) + x*((609*a^6*d^7)/10 + (7*b^6*c^6*d)/5 + (21*a*b^5*c^5*d^2)/10 + (7*a^2*b^4*c^4*d^3)/2 + 7*a^3*b^3*c^3*d^4 + 21*a^4*b^2*c^2*d^5 - (959*a^5*b*c*d^6)/10) + x^3*((455*a^4*b^2*d^7)/3 + (35*b^6*c^4*d^3)/3 + (70*a*b^5*c^3*d^4)/3 - (770*a^3*b^3*c*d^6)/3 + 70*a^2*b^4*c^2*d^5) + x^2*((539*a^5*b*d^7)/4 + (21*b^6*c^5*d^2)/4 + (35*a*b^5*c^4*d^3)/4 - (875*a^4*b^2*c*d^6)/4 + (35*a^2*b^4*c^3*d^4)/2 + (105*a^3*b^3*c^2*d^5)/2) + x^5*(21*a^2*b^4*d^7 + 21*b^6*c^2*d^5 - 42*a*b^5*c*d^6) + x^4*((175*a^3*b^3*d^7)/2 + (35*b^6*c^3*d^4)/2 + (105*a*b^5*c^2*d^5)/2 - (315*a^2*b^4*c*d^6)/2))/(a^6*b^7 + b^13*x^6 + 6*a^5*b^8*x + 6*a*b^12*x^5 + 15*a^4*b^9*x^2 + 20*a^3*b^10*x^3 + 15*a^2*b^11*x^4)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**7,x)

[Out] Timed out

$$3.1290 \quad \int \frac{(c+dx)^7}{(a+bx)^8} dx$$

Optimal. Leaf size=194

$$-\frac{7d^6(bc-ad)}{b^8(a+bx)} - \frac{21d^5(bc-ad)^2}{2b^8(a+bx)^2} - \frac{35d^4(bc-ad)^3}{3b^8(a+bx)^3} - \frac{35d^3(bc-ad)^4}{4b^8(a+bx)^4} - \frac{21d^2(bc-ad)^5}{5b^8(a+bx)^5} - \frac{7d(bc-ad)^6}{6b^8(a+bx)^6} - \frac{(bc-ad)^7}{7b^8(a+bx)^7} + \frac{d}{b^8(a+bx)^8}$$

[Out] $-1/7*(-a*d+b*c)^7/b^8/(b*x+a)^7-7/6*d*(-a*d+b*c)^6/b^8/(b*x+a)^6-21/5*d^2*(-a*d+b*c)^5/b^8/(b*x+a)^5-35/4*d^3*(-a*d+b*c)^4/b^8/(b*x+a)^4-35/3*d^4*(-a*d+b*c)^3/b^8/(b*x+a)^3-21/2*d^5*(-a*d+b*c)^2/b^8/(b*x+a)^2-7*d^6*(-a*d+b*c)/b^8/(b*x+a)+d^7*\ln(b*x+a)/b^8$

Rubi [A] time = 0.16, antiderivative size = 194, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{7d^6(bc-ad)}{b^8(a+bx)} - \frac{21d^5(bc-ad)^2}{2b^8(a+bx)^2} - \frac{35d^4(bc-ad)^3}{3b^8(a+bx)^3} - \frac{35d^3(bc-ad)^4}{4b^8(a+bx)^4} - \frac{21d^2(bc-ad)^5}{5b^8(a+bx)^5} - \frac{7d(bc-ad)^6}{6b^8(a+bx)^6} - \frac{(bc-ad)^7}{7b^8(a+bx)^7} + \frac{d}{b^8(a+bx)^8}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^8, x]

[Out] $-(b*c - a*d)^7/(7*b^8*(a + b*x)^7) - (7*d*(b*c - a*d)^6)/(6*b^8*(a + b*x)^6) - (21*d^2*(b*c - a*d)^5)/(5*b^8*(a + b*x)^5) - (35*d^3*(b*c - a*d)^4)/(4*b^8*(a + b*x)^4) - (35*d^4*(b*c - a*d)^3)/(3*b^8*(a + b*x)^3) - (21*d^5*(b*c - a*d)^2)/(2*b^8*(a + b*x)^2) - (7*d^6*(b*c - a*d))/(b^8*(a + b*x)) + (d^7*Log[a + b*x])/b^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^8} dx = \int \left(\frac{(bc-ad)^7}{b^7(a+bx)^8} + \frac{7d(bc-ad)^6}{b^7(a+bx)^7} + \frac{21d^2(bc-ad)^5}{b^7(a+bx)^6} + \frac{35d^3(bc-ad)^4}{b^7(a+bx)^5} + \frac{35d^4(bc-ad)^3}{b^7(a+bx)^4} + \frac{21d^5(bc-ad)^2}{b^7(a+bx)^3} + \frac{7d^6(bc-ad)}{b^7(a+bx)^2} + \frac{d^7}{b^7(a+bx)} \right) dx$$

$$= -\frac{(bc-ad)^7}{7b^8(a+bx)^7} - \frac{7d(bc-ad)^6}{6b^8(a+bx)^6} - \frac{21d^2(bc-ad)^5}{5b^8(a+bx)^5} - \frac{35d^3(bc-ad)^4}{4b^8(a+bx)^4} - \frac{35d^4(bc-ad)^3}{3b^8(a+bx)^3} - \frac{21d^5(bc-ad)^2}{2b^8(a+bx)^2} - \frac{7d^6(bc-ad)}{b^8(a+bx)} + \frac{d^7}{b^8} \ln|a+bx|$$

Mathematica [A] time = 0.16, size = 308, normalized size = 1.59

$$\frac{d^7 \log(a + bx)}{b^8} - \frac{(bc - ad) \left(1089a^6d^6 + 3a^5bd^5(223c + 2401dx) + 3a^4b^2d^4(153c^2 + 1421cdx + 6713d^2x^2) + a^3b^3 \right)}{b^8}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^8,x]

[Out]
$$-1/420 * ((b*c - a*d) * (1089*a^6*d^6 + 3*a^5*b*d^5*(223*c + 2401*d*x) + 3*a^4*b^2*d^4*(153*c^2 + 1421*c*d*x + 6713*d^2*x^2) + a^3*b^3*d^3*(319*c^3 + 2793*c^2*d*x + 11319*c*d^2*x^2 + 30625*d^3*x^3) + a^2*b^4*d^2*(214*c^4 + 1813*c^3*d*x + 6909*c^2*d^2*x^2 + 15925*c*d^3*x^3 + 26950*d^4*x^4) + a*b^5*d*(130*c^5 + 1078*c^4*d*x + 3969*c^3*d^2*x^2 + 8575*c^2*d^3*x^3 + 12250*c*d^4*x^4 + 13230*d^5*x^5) + b^6*(60*c^6 + 490*c^5*d*x + 1764*c^4*d^2*x^2 + 3675*c^3*d^3*x^3 + 4900*c^2*d^4*x^4 + 4410*c*d^5*x^5 + 2940*d^6*x^6)) / (b^8*(a + b*x)^7) + (d^7*Log[a + b*x])/b^8$$

fricas [B] time = 0.43, size = 624, normalized size = 3.22

$$\frac{60b^7c^7 + 70ab^6c^6d + 84a^2b^5c^5d^2 + 105a^3b^4c^4d^3 + 140a^4b^3c^3d^4 + 210a^5b^2c^2d^5 + 420a^6bcd^6 - 1089a^7d^7 + 2940a^7d^7 + 2940(b^7cd^6 - ab^6d^7)x^6 + 4410(b^7c^2d^5 + 2ab^6cd^6 - 3a^2b^5d^7)x^5 + 2450(2b^7c^3d^4 + 3ab^6c^2d^5 + 6a^2b^5cd^6 - 11a^3b^4d^7)x^4 + 1225(3b^7c^4d^3 + 4ab^6c^3d^4 + 6a^2b^5c^2d^5 + 12a^3b^4cd^6 - 25a^4b^3d^7)x^3 + 147(12b^7c^5d^2 + 15ab^6c^4d^3 + 20a^2b^5c^3d^4 + 30a^3b^4c^2d^5 + 60a^4b^3cd^6 - 137a^5b^2d^7)x^2 + 49(10b^7c^6d + 12ab^6c^5d^2 + 15a^2b^5c^4d^3 + 20a^3b^4c^3d^4 + 30a^4b^3c^2d^5 + 60a^5b^2cd^6 - 147a^6bd^7)x - 420(b^7d^7x^7 + 7ab^6d^7x^6 + 21a^2b^5d^7x^5 + 35a^3b^4d^7x^4 + 35a^4b^3d^7x^3 + 21a^5b^2d^7x^2 + 7a^6bd^7x + a^7d^7) * \log(b*x + a) / (b^15x^7 + 7a*b^14x^6 + 21a^2*b^13x^5 + 35a^3*b^12x^4 + 35a^4*b^11x^3 + 21a^5*b^10x^2 + 7a^6*b^9x + a^7*b^8)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^8,x, algorithm="fricas")

[Out]
$$-1/420 * (60*b^7*c^7 + 70*a*b^6*c^6*d + 84*a^2*b^5*c^5*d^2 + 105*a^3*b^4*c^4*d^3 + 140*a^4*b^3*c^3*d^4 + 210*a^5*b^2*c^2*d^5 + 420*a^6*b*c*d^6 - 1089*a^7*d^7 + 2940*(b^7*c*d^6 - a*b^6*d^7)*x^6 + 4410*(b^7*c^2*d^5 + 2*a*b^6*c*d^6 - 3*a^2*b^5*d^7)*x^5 + 2450*(2*b^7*c^3*d^4 + 3*a*b^6*c^2*d^5 + 6*a^2*b^5*c*d^6 - 11*a^3*b^4*d^7)*x^4 + 1225*(3*b^7*c^4*d^3 + 4*a*b^6*c^3*d^4 + 6*a^2*b^5*c^2*d^5 + 12*a^3*b^4*c*d^6 - 25*a^4*b^3*d^7)*x^3 + 147*(12*b^7*c^5*d^2 + 15*a*b^6*c^4*d^3 + 20*a^2*b^5*c^3*d^4 + 30*a^3*b^4*c^2*d^5 + 60*a^4*b^3*c*d^6 - 137*a^5*b^2*d^7)*x^2 + 49*(10*b^7*c^6*d + 12*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 + 20*a^3*b^4*c^3*d^4 + 30*a^4*b^3*c^2*d^5 + 60*a^5*b^2*c*d^6 - 147*a^6*b*d^7)*x - 420*(b^7*d^7*x^7 + 7*a*b^6*d^7*x^6 + 21*a^2*b^5*d^7*x^5 + 35*a^3*b^4*d^7*x^4 + 35*a^4*b^3*d^7*x^3 + 21*a^5*b^2*d^7*x^2 + 7*a^6*b*d^7*x + a^7*d^7) * \log(b*x + a) / (b^15*x^7 + 7*a*b^14*x^6 + 21*a^2*b^13*x^5 + 35*a^3*b^12*x^4 + 35*a^4*b^11*x^3 + 21*a^5*b^10*x^2 + 7*a^6*b^9*x + a^7*b^8)$$

giac [B] time = 1.28, size = 466, normalized size = 2.40

$$\frac{d^7 \log(bx + a)}{b^8} - \frac{2940(b^6cd^6 - ab^5d^7)x^6 + 4410(b^6c^2d^5 + 2ab^5cd^6 - 3a^2b^4d^7)x^5 + 2450(2b^6c^3d^4 + 3ab^5c^2d^5)}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^8,x, algorithm="giac")

[Out] $d^7 \log(\text{abs}(b*x + a))/b^8 - 1/420*(2940*(b^6*c*d^6 - a*b^5*d^7)*x^6 + 4410*(b^6*c^2*d^5 + 2*a*b^5*c*d^6 - 3*a^2*b^4*d^7)*x^5 + 2450*(2*b^6*c^3*d^4 + 3*a*b^5*c^2*d^5 + 6*a^2*b^4*c*d^6 - 11*a^3*b^3*d^7)*x^4 + 1225*(3*b^6*c^4*d^3 + 4*a*b^5*c^3*d^4 + 6*a^2*b^4*c^2*d^5 + 12*a^3*b^3*c*d^6 - 25*a^4*b^2*d^7)*x^3 + 147*(12*b^6*c^5*d^2 + 15*a*b^5*c^4*d^3 + 20*a^2*b^4*c^3*d^4 + 30*a^3*b^3*c^2*d^5 + 60*a^4*b^2*c*d^6 - 137*a^5*b*d^7)*x^2 + 49*(10*b^6*c^6*d + 12*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 + 20*a^3*b^3*c^3*d^4 + 30*a^4*b^2*c^2*d^5 + 60*a^5*b*c*d^6 - 147*a^6*d^7)*x + (60*b^7*c^7 + 70*a*b^6*c^6*d + 84*a^2*b^5*c^5*d^2 + 105*a^3*b^4*c^4*d^3 + 140*a^4*b^3*c^3*d^4 + 210*a^5*b^2*c^2*d^5 + 420*a^6*b*c*d^6 - 1089*a^7*d^7)/b)/((b*x + a)^7*b^7)$

maple [B] time = 0.01, size = 672, normalized size = 3.46

$$\frac{a^7 d^7}{7(bx+a)^7 b^8} - \frac{a^6 c d^6}{(bx+a)^7 b^7} + \frac{3a^5 c^2 d^5}{(bx+a)^7 b^6} - \frac{5a^4 c^3 d^4}{(bx+a)^7 b^5} + \frac{5a^3 c^4 d^3}{(bx+a)^7 b^4} - \frac{3a^2 c^5 d^2}{(bx+a)^7 b^3} + \frac{a c^6 d}{(bx+a)^7 b^2} - \frac{c^7}{7(bx+a)^7 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^8,x)

[Out] $7/b^8*d^7/(b*x+a)*a-7/b^7*d^6/(b*x+a)*c+35/3*d^7/b^8/(b*x+a)^3*a^3-35/3*d^4/b^5/(b*x+a)^3*c^3+1/7/b^8/(b*x+a)^7*a^7*d^7+21/5*d^7/b^8/(b*x+a)^5*a^5-21/5*d^2/b^3/(b*x+a)^5*c^5-7/6*d^7/b^8/(b*x+a)^6*a^6-7/6*d/b^2/(b*x+a)^6*c^6-2/2*d^7/b^8/(b*x+a)^2*a^2-21/2*d^5/b^6/(b*x+a)^2*c^2-35/4*d^7/b^8/(b*x+a)^4*a^4-35/4*d^3/b^4/(b*x+a)^4*c^4+d^7*ln(b*x+a)/b^8+42*d^5/b^6/(b*x+a)^5*a^3*c^2-21*d^6/b^7/(b*x+a)^5*a^4*c-1/7/b/(b*x+a)^7*c^7-42*d^4/b^5/(b*x+a)^5*a^2*c^3+1/b^2/(b*x+a)^7*a*c^6*d-35*d^6/b^7/(b*x+a)^3*a^2*c+35*d^5/b^6/(b*x+a)^3*a*c^2-1/b^7/(b*x+a)^7*a^6*c*d^6+3/b^6/(b*x+a)^7*a^5*c^2*d^5-5/b^5/(b*x+a)^7*a^4*c^3*d^4+5/b^4/(b*x+a)^7*a^3*c^4*d^3-3/b^3/(b*x+a)^7*a^2*c^5*d^2+21*d^3/b^4/(b*x+a)^5*a*c^4+21*d^6/b^7/(b*x+a)^2*a*c+35*d^6/b^7/(b*x+a)^4*a^3*c-105/2*d^5/b^6/(b*x+a)^4*a^2*c^2+35*d^4/b^5/(b*x+a)^4*a*c^3+7*d^6/b^7/(b*x+a)^6*a^5*c-35/2*d^5/b^6/(b*x+a)^6*a^4*c^2+70/3*d^4/b^5/(b*x+a)^6*a^3*c^3-35/2*d^3/b^4/(b*x+a)^6*a^2*c^4+7*d^2/b^3/(b*x+a)^6*a*c^5$

maxima [B] time = 1.65, size = 534, normalized size = 2.75

$$\frac{60b^7c^7 + 70ab^6c^6d + 84a^2b^5c^5d^2 + 105a^3b^4c^4d^3 + 140a^4b^3c^3d^4 + 210a^5b^2c^2d^5 + 420a^6bcd^6 - 1089a^7d^7 + 29}{7(bx+a)^7 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^8,x, algorithm="maxima")

[Out]
$$\frac{-1/420*(60*b^7*c^7 + 70*a*b^6*c^6*d + 84*a^2*b^5*c^5*d^2 + 105*a^3*b^4*c^4*d^3 + 140*a^4*b^3*c^3*d^4 + 210*a^5*b^2*c^2*d^5 + 420*a^6*b*c*d^6 - 1089*a^7*d^7 + 2940*(b^7*c*d^6 - a*b^6*d^7)*x^6 + 4410*(b^7*c^2*d^5 + 2*a*b^6*c*d^6 - 3*a^2*b^5*d^7)*x^5 + 2450*(2*b^7*c^3*d^4 + 3*a*b^6*c^2*d^5 + 6*a^2*b^5*c*d^6 - 11*a^3*b^4*d^7)*x^4 + 1225*(3*b^7*c^4*d^3 + 4*a*b^6*c^3*d^4 + 6*a^2*b^5*c^2*d^5 + 12*a^3*b^4*c*d^6 - 25*a^4*b^3*d^7)*x^3 + 147*(12*b^7*c^5*d^2 + 15*a*b^6*c^4*d^3 + 20*a^2*b^5*c^3*d^4 + 30*a^3*b^4*c^2*d^5 + 60*a^4*b^3*c*d^6 - 137*a^5*b^2*d^7)*x^2 + 49*(10*b^7*c^6*d + 12*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 + 20*a^3*b^4*c^3*d^4 + 30*a^4*b^3*c^2*d^5 + 60*a^5*b^2*c*d^6 - 147*a^6*b*d^7)*x)/(b^15*x^7 + 7*a*b^14*x^6 + 21*a^2*b^13*x^5 + 35*a^3*b^12*x^4 + 35*a^4*b^11*x^3 + 21*a^5*b^10*x^2 + 7*a^6*b^9*x + a^7*b^8) + d^7*log(b*x + a)/b^8$$

mupad [B] time = 0.35, size = 461, normalized size = 2.38

$$\frac{d^7 \ln(a + bx)}{b^8} - \frac{x \left(-\frac{343 a^6 b d^7}{20} + 7 a^5 b^2 c d^6 + \frac{7 a^4 b^3 c^2 d^5}{2} + \frac{7 a^3 b^4 c^3 d^4}{3} + \frac{7 a^2 b^5 c^4 d^3}{4} + \frac{7 a b^6 c^5 d^2}{5} + \frac{7 b^7 c^6 d}{6} \right) - x^6 (7 a b^6 c^5 d^2)}{b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^7/(a + b*x)^8,x)`

[Out]
$$\frac{d^7 \log(a + b*x)}{b^8} - \frac{x*((7*b^7*c^6*d)/6 - (343*a^6*b*d^7)/20 + (7*a*b^6*c^5*d^2)/5 + 7*a^5*b^2*c*d^6 + (7*a^2*b^5*c^4*d^3)/4 + (7*a^3*b^4*c^3*d^4)/3 + (7*a^4*b^3*c^2*d^5)/2) - x^6*(7*a*b^6*d^7 - 7*b^7*c*d^6) + x^3*((35*b^7*c^4*d^3)/4 - (875*a^4*b^3*d^7)/12 + (35*a*b^6*c^3*d^4)/3 + 35*a^3*b^4*c*d^6 + (35*a^2*b^5*c^2*d^5)/2) + x^5*((21*b^7*c^2*d^5)/2 - (63*a^2*b^5*d^7)/2 + 21*a*b^6*c*d^6) + x^2*((21*b^7*c^5*d^2)/5 - (959*a^5*b^2*d^7)/20 + (21*a*b^6*c^4*d^3)/4 + 21*a^4*b^3*c*d^6 + 7*a^2*b^5*c^3*d^4 + (21*a^3*b^4*c^2*d^5)/2) - (363*a^7*d^7)/140 + (b^7*c^7)/7 + x^4*((35*b^7*c^3*d^4)/3 - (385*a^3*b^4*d^7)/6 + (35*a*b^6*c^2*d^5)/2 + 35*a^2*b^5*c*d^6) + (a^2*b^5*c^5*d^2)/5 + (a^3*b^4*c^4*d^3)/4 + (a^4*b^3*c^3*d^4)/3 + (a^5*b^2*c^2*d^5)/2 + (a*b^6*c^6*d)/6 + a^6*b*c*d^6)/(b^8*(a + b*x)^7)$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**7/(b*x+a)**8,x)`

[Out] Timed out

$$3.1291 \quad \int \frac{(c+dx)^7}{(a+bx)^9} dx$$

Optimal. Leaf size=28

$$-\frac{(c+dx)^8}{8(a+bx)^8(bc-ad)}$$

[Out] $-1/8*(d*x+c)^8/(-a*d+b*c)/(b*x+a)^8$

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$-\frac{(c+dx)^8}{8(a+bx)^8(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^9, x]

[Out] $-(c + d*x)^8/(8*(b*c - a*d)*(a + b*x)^8)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^9} dx = -\frac{(c+dx)^8}{8(bc-ad)(a+bx)^8}$$

Mathematica [B] time = 0.13, size = 353, normalized size = 12.61

$$-\frac{a^7 d^7 + a^6 b d^6 (c + 8 d x) + a^5 b^2 d^5 (c^2 + 8 c d x + 28 d^2 x^2) + a^4 b^3 d^4 (c^3 + 8 c^2 d x + 28 c d^2 x^2 + 56 d^3 x^3) + a^3 b^4 d^3 (c^4 + 8 c^3 d x + 28 c^2 d^2 x^2 + 56 c d^3 x^3 + 56 d^4 x^4) + a^2 b^5 d^2 (c^5 + 8 c^4 d x + 28 c^3 d^2 x^2 + 56 c^2 d^3 x^3 + 56 c d^4 x^4 + 56 d^5 x^5) + a b^6 d (c^6 + 8 c^5 d x + 28 c^4 d^2 x^2 + 56 c^3 d^3 x^3 + 56 c^2 d^4 x^4 + 56 c d^5 x^5 + 56 d^6 x^6) + b^7 d^7 x^7}{8 (b c - a d) (a + b x)^8}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^9, x]

[Out] $-1/8*(a^7*d^7 + a^6*b*d^6*(c + 8*d*x) + a^5*b^2*d^5*(c^2 + 8*c*d*x + 28*d^2*x^2) + a^4*b^3*d^4*(c^3 + 8*c^2*d*x + 28*c*d^2*x^2 + 56*d^3*x^3) + a^3*b^4*d^3*(c^4 + 8*c^3*d*x + 28*c^2*d^2*x^2 + 56*c*d^3*x^3 + 56*d^4*x^4) + a^2*b^5*d^2*(c^5 + 8*c^4*d*x + 28*c^3*d^2*x^2 + 56*c^2*d^3*x^3 + 56*c*d^4*x^4 + 56*d^5*x^5) + a*b^6*d*(c^6 + 8*c^5*d*x + 28*c^4*d^2*x^2 + 56*c^3*d^3*x^3 + 56*c^2*d^4*x^4 + 56*c*d^5*x^5 + 56*d^6*x^6) + b^7*d^7*x^7)$

$$\frac{d^3(c^4 + 8c^3dx + 28c^2d^2x^2 + 56cd^3x^3 + 70d^4x^4) + a^2b^5d^2(c^5 + 8c^4dx + 28c^3d^2x^2 + 56c^2d^3x^3 + 70cd^4x^4 + 56d^5x^5) + a^3b^6d(c^6 + 8c^5dx + 28c^4d^2x^2 + 56c^3d^3x^3 + 70c^2d^4x^4 + 56cd^5x^5 + 28d^6x^6) + b^7(c^7 + 8c^6dx + 28c^5d^2x^2 + 56c^4d^3x^3 + 70c^3d^4x^4 + 56c^2d^5x^5 + 28cd^6x^6 + 8d^7x^7)}{(b^8(a + bx)^8)}$$

fricas [B] time = 0.43, size = 509, normalized size = 18.18

$$8b^7d^7x^7 + b^7c^7 + ab^6c^6d + a^2b^5c^5d^2 + a^3b^4c^4d^3 + a^4b^3c^3d^4 + a^5b^2c^2d^5 + a^6bcd^6 + a^7d^7 + 28(b^7cd^6 + ab^6d^7)x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((dx+c)^7/(b*x+a)^9,x, algorithm="fricas")

[Out]
$$\frac{-1/8(8b^7d^7x^7 + b^7c^7 + a^3b^4c^4d^3 + a^4b^3c^3d^4 + a^5b^2c^2d^5 + a^6b^1c^1d^6 + a^7d^7 + 28(b^7c^6d + a^2b^5c^5d^2 + a^3b^4c^4d^3 + a^4b^3c^3d^4 + a^5b^2c^2d^5 + a^6b^1c^1d^6 + a^7d^7)x^6 + 56(b^7c^5d^2 + a^2b^5c^5d^2 + a^3b^4c^4d^3 + a^4b^3c^3d^4 + a^5b^2c^2d^5 + a^6b^1c^1d^6 + a^7d^7)x^5 + 70(b^7c^4d^3 + a^2b^5c^5d^2 + a^3b^4c^4d^3 + a^4b^3c^3d^4 + a^5b^2c^2d^5 + a^6b^1c^1d^6 + a^7d^7)x^4 + 56(b^7c^3d^4 + a^2b^5c^5d^2 + a^3b^4c^4d^3 + a^4b^3c^3d^4 + a^5b^2c^2d^5 + a^6b^1c^1d^6 + a^7d^7)x^3 + 28(b^7c^2d^5 + a^2b^5c^5d^2 + a^3b^4c^4d^3 + a^4b^3c^3d^4 + a^5b^2c^2d^5 + a^6b^1c^1d^6 + a^7d^7)x^2 + 8(b^7c^6d + a^2b^5c^5d^2 + a^3b^4c^4d^3 + a^4b^3c^3d^4 + a^5b^2c^2d^5 + a^6b^1c^1d^6 + a^7d^7)x + 8a^7b^9x + a^8b^8)}{(b^{16}x^8 + 8a^15bx^7 + 28a^{14}b^2x^6 + 56a^{13}b^3x^5 + 70a^{12}b^4x^4 + 56a^{11}b^5x^3 + 28a^{10}b^6x^2 + 8a^9b^7x + a^8b^8)}$$

giac [B] time = 1.29, size = 489, normalized size = 17.46

$$8b^7d^7x^7 + 28b^7cd^6x^6 + 28ab^6d^7x^6 + 56b^7c^2d^5x^5 + 56ab^6cd^6x^5 + 56a^2b^5d^7x^5 + 70b^7c^3d^4x^4 + 70ab^6c^2d^5x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((dx+c)^7/(b*x+a)^9,x, algorithm="giac")

[Out]
$$\frac{-1/8(8b^7d^7x^7 + 28b^7c^6d^6x^6 + 28a^2b^5c^5d^7x^6 + 56b^7c^2d^5x^5 + 56a^2b^5c^5d^7x^5 + 70b^7c^3d^4x^4 + 70a^2b^5c^5d^7x^4 + 70a^3b^4c^4d^7x^4 + 56b^7c^4d^3x^3 + 56a^2b^5c^5d^7x^3 + 56a^3b^4c^4d^7x^3 + 56a^4b^3c^3d^7x^3 + 28b^7c^5d^2x^2 + 28a^2b^5c^5d^7x^2 + 28a^3b^4c^4d^7x^2 + 28a^4b^3c^3d^7x^2 + 8b^7c^6d^6x + 8a^2b^5c^5d^7x + 8a^3b^4c^4d^7x + 8a^4b^3c^3d^7x + 8a^5b^2c^2d^7x + 8a^6b^1c^1d^7x + b^7c^7 + a^2b^5c^5d^7 + a^3b^4c^4d^7 + a^4b^3c^3d^7 + a^5b^2c^2d^7)}{(b^8(a + bx)^8)}$$

maple [B] time = 0.01, size = 464, normalized size = 16.57

$$\frac{d^7}{(bx+a)b^8} + \frac{7(ad-bc)d^6}{2(bx+a)^2b^8} - \frac{7(a^2d^2-2abcd+b^2c^2)d^5}{(bx+a)^3b^8} + \frac{35(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^4}{4(bx+a)^4b^8} - \frac{7(a^4d^4-4a^3bd^3+6a^2b^2cd^2-4ab^3c^2d+b^4c^3)d^3}{(bx+a)^5b^8} + \frac{7(a^5d^5-5a^4b^2cd^4+10a^3b^3c^2d^3-10a^2b^4c^3d^2+5a^3b^4c^4d-b^5c^5)d^2}{(bx+a)^6b^8} - \frac{7(a^6d^6-6a^5b^2cd^5+15a^4b^3c^3d^4-35a^3b^4c^4d^3+21a^2b^5c^5d^2-7a^3b^6c^6d+b^7c^7)d}{(bx+a)^7b^8} + \frac{7(a^7d^7-7a^6b^2cd^6+21a^5b^3c^3d^5-35a^4b^4c^4d^4+35a^3b^5c^5d^3-21a^2b^6c^6d^2+7a^3b^7c^7)d}{(bx+a)^8b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^9,x)

[Out]
$$-1/8*(-a^7*d^7+7*a^6*b*c*d^6-21*a^5*b^2*c^2*d^5+35*a^4*b^3*c^3*d^4-35*a^3*b^4*c^4*d^3+21*a^2*b^5*c^5*d^2-7*a*b^6*c^6*d+b^7*c^7)/b^8/(b*x+a)^8-7*d^5*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^8/(b*x+a)^3-d*(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^8/(b*x+a)^7-7*d^3*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/b^8/(b*x+a)^5+7/2*d^6*(a*d-b*c)/b^8/(b*x+a)^2+35/4*d^4*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^8/(b*x+a)^4-d^7/b^8/(b*x+a)+7/2*d^2*(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)/b^8/(b*x+a)^6$$

maxima [B] time = 1.65, size = 509, normalized size = 18.18

$$\frac{8b^7d^7x^7 + b^7c^7 + ab^6c^6d + a^2b^5c^5d^2 + a^3b^4c^4d^3 + a^4b^3c^3d^4 + a^5b^2c^2d^5 + a^6bcd^6 + a^7d^7 + 28(b^7cd^6 + ab^6d^7)x^6}{(bx+a)^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^9,x, algorithm="maxima")

[Out]
$$-1/8*(8*b^7*d^7*x^7 + b^7*c^7 + a*b^6*c^6*d + a^2*b^5*c^5*d^2 + a^3*b^4*c^4*d^3 + a^4*b^3*c^3*d^4 + a^5*b^2*c^2*d^5 + a^6*b*c*d^6 + a^7*d^7 + 28*(b^7*c*d^6 + a*b^6*d^7)*x^6 + 56*(b^7*c^2*d^5 + a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 70*(b^7*c^3*d^4 + a*b^6*c^2*d^5 + a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 56*(b^7*c^4*d^3 + a*b^6*c^3*d^4 + a^2*b^5*c^2*d^5 + a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 28*(b^7*c^5*d^2 + a*b^6*c^4*d^3 + a^2*b^5*c^3*d^4 + a^3*b^4*c^2*d^5 + a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 8*(b^7*c^6*d + a*b^6*c^5*d^2 + a^2*b^5*c^4*d^3 + a^3*b^4*c^3*d^4 + a^4*b^3*c^2*d^5 + a^5*b^2*c*d^6 + a^6*b*d^7)*x + 28*a^2*b^14*x^6 + 56*a^3*b^13*x^5 + 70*a^4*b^12*x^4 + 56*a^5*b^11*x^3 + 28*a^6*b^10*x^2 + 8*a^7*b^9*x + a^8*b^8)$$

mupad [B] time = 0.17, size = 571, normalized size = 20.39

$$\frac{a^7d^7 + a^6bcd^6 + 8a^6bd^7x + a^5b^2c^2d^5 + 8a^5b^2cd^6x + 28a^5b^2d^7x^2 + a^4b^3c^3d^4 + 8a^4b^3c^2d^5x + 28a^4b^3d^6x^2 + 28a^3b^4c^4d^3 + 28a^3b^4c^3d^4x + 28a^3b^4c^2d^5x^2 + 28a^3b^4cd^6x^3 + 28a^2b^5c^5d^2 + 28a^2b^5c^4d^3x + 28a^2b^5c^3d^4x^2 + 28a^2b^5c^2d^5x^3 + 28a^2b^5cd^6x^4 + 28a^2b^5d^7x^5 + 28a^2b^4c^6d + 28a^2b^4c^5d^2x + 28a^2b^4c^4d^3x^2 + 28a^2b^4c^3d^4x^3 + 28a^2b^4c^2d^5x^4 + 28a^2b^4cd^6x^5 + 28a^2b^4d^7x^6 + 28a^2b^3c^7 + 28a^2b^3c^6d + 28a^2b^3c^5d^2x + 28a^2b^3c^4d^3x^2 + 28a^2b^3c^3d^4x^3 + 28a^2b^3c^2d^5x^4 + 28a^2b^3cd^6x^5 + 28a^2b^3d^7x^6 + 28a^2b^2c^8 + 28a^2b^2c^7d + 28a^2b^2c^6d^2x + 28a^2b^2c^5d^3x^2 + 28a^2b^2c^4d^4x^3 + 28a^2b^2c^3d^5x^4 + 28a^2b^2c^2d^6x^5 + 28a^2b^2cd^7x^6 + 28a^2b^2d^8x^7 + 28a^2b^1c^9 + 28a^2b^1c^8d + 28a^2b^1c^7d^2x + 28a^2b^1c^6d^3x^2 + 28a^2b^1c^5d^4x^3 + 28a^2b^1c^4d^5x^4 + 28a^2b^1c^3d^6x^5 + 28a^2b^1cd^7x^6 + 28a^2b^1d^8x^7 + 28a^2b^0c^10 + 28a^2b^0c^9d + 28a^2b^0c^8d^2x + 28a^2b^0c^7d^3x^2 + 28a^2b^0c^6d^4x^3 + 28a^2b^0c^5d^5x^4 + 28a^2b^0c^4d^6x^5 + 28a^2b^0c^3d^7x^6 + 28a^2b^0cd^8x^7 + 28a^2b^0d^9x^8 + 28a^1b^11c^7 + 28a^1b^11c^6d + 28a^1b^11c^5d^2x + 28a^1b^11c^4d^3x^2 + 28a^1b^11c^3d^4x^3 + 28a^1b^11c^2d^5x^4 + 28a^1b^11cd^6x^5 + 28a^1b^11d^7x^6 + 28a^1b^10c^8 + 28a^1b^10c^7d + 28a^1b^10c^6d^2x + 28a^1b^10c^5d^3x^2 + 28a^1b^10c^4d^4x^3 + 28a^1b^10c^3d^5x^4 + 28a^1b^10c^2d^6x^5 + 28a^1b^10cd^7x^6 + 28a^1b^10d^8x^7 + 28a^1b^9c^9 + 28a^1b^9c^8d + 28a^1b^9c^7d^2x + 28a^1b^9c^6d^3x^2 + 28a^1b^9c^5d^4x^3 + 28a^1b^9c^4d^5x^4 + 28a^1b^9c^3d^6x^5 + 28a^1b^9cd^7x^6 + 28a^1b^9d^8x^7 + 28a^1b^8c^10 + 28a^1b^8c^9d + 28a^1b^8c^8d^2x + 28a^1b^8c^7d^3x^2 + 28a^1b^8c^6d^4x^3 + 28a^1b^8c^5d^5x^4 + 28a^1b^8c^4d^6x^5 + 28a^1b^8c^3d^7x^6 + 28a^1b^8cd^8x^7 + 28a^1b^8d^9x^8 + 28a^1b^7c^11 + 28a^1b^7c^10d + 28a^1b^7c^9d^2x + 28a^1b^7c^8d^3x^2 + 28a^1b^7c^7d^4x^3 + 28a^1b^7c^6d^5x^4 + 28a^1b^7c^5d^6x^5 + 28a^1b^7c^4d^7x^6 + 28a^1b^7cd^8x^7 + 28a^1b^7d^9x^8 + 28a^1b^6c^12 + 28a^1b^6c^11d + 28a^1b^6c^10d^2x + 28a^1b^6c^9d^3x^2 + 28a^1b^6c^8d^4x^3 + 28a^1b^6c^7d^5x^4 + 28a^1b^6c^6d^6x^5 + 28a^1b^6c^5d^7x^6 + 28a^1b^6cd^8x^7 + 28a^1b^6d^9x^8 + 28a^1b^5c^13 + 28a^1b^5c^12d + 28a^1b^5c^11d^2x + 28a^1b^5c^10d^3x^2 + 28a^1b^5c^9d^4x^3 + 28a^1b^5c^8d^5x^4 + 28a^1b^5c^7d^6x^5 + 28a^1b^5c^6d^7x^6 + 28a^1b^5cd^8x^7 + 28a^1b^5d^9x^8 + 28a^1b^4c^14 + 28a^1b^4c^13d + 28a^1b^4c^12d^2x + 28a^1b^4c^11d^3x^2 + 28a^1b^4c^10d^4x^3 + 28a^1b^4c^9d^5x^4 + 28a^1b^4c^8d^6x^5 + 28a^1b^4c^7d^7x^6 + 28a^1b^4cd^8x^7 + 28a^1b^4d^9x^8 + 28a^1b^3c^15 + 28a^1b^3c^14d + 28a^1b^3c^13d^2x + 28a^1b^3c^12d^3x^2 + 28a^1b^3c^11d^4x^3 + 28a^1b^3c^10d^5x^4 + 28a^1b^3c^9d^6x^5 + 28a^1b^3c^8d^7x^6 + 28a^1b^3cd^8x^7 + 28a^1b^3d^9x^8 + 28a^1b^2c^16 + 28a^1b^2c^15d + 28a^1b^2c^14d^2x + 28a^1b^2c^13d^3x^2 + 28a^1b^2c^12d^4x^3 + 28a^1b^2c^11d^5x^4 + 28a^1b^2c^10d^6x^5 + 28a^1b^2c^9d^7x^6 + 28a^1b^2cd^8x^7 + 28a^1b^2d^9x^8 + 28a^1b^1c^17 + 28a^1b^1c^16d + 28a^1b^1c^15d^2x + 28a^1b^1c^14d^3x^2 + 28a^1b^1c^13d^4x^3 + 28a^1b^1c^12d^5x^4 + 28a^1b^1c^11d^6x^5 + 28a^1b^1c^10d^7x^6 + 28a^1b^1cd^8x^7 + 28a^1b^1d^9x^8 + 28a^1b^0c^18 + 28a^1b^0c^17d + 28a^1b^0c^16d^2x + 28a^1b^0c^15d^3x^2 + 28a^1b^0c^14d^4x^3 + 28a^1b^0c^13d^5x^4 + 28a^1b^0c^12d^6x^5 + 28a^1b^0c^11d^7x^6 + 28a^1b^0cd^8x^7 + 28a^1b^0d^9x^8 + 28a^0b^19c^16 + 28a^0b^19c^15d + 28a^0b^19c^14d^2x + 28a^0b^19c^13d^3x^2 + 28a^0b^19c^12d^4x^3 + 28a^0b^19c^11d^5x^4 + 28a^0b^19c^10d^6x^5 + 28a^0b^19c^9d^7x^6 + 28a^0b^19cd^8x^7 + 28a^0b^19d^9x^8 + 28a^0b^18c^17 + 28a^0b^18c^16d + 28a^0b^18c^15d^2x + 28a^0b^18c^14d^3x^2 + 28a^0b^18c^13d^4x^3 + 28a^0b^18c^12d^5x^4 + 28a^0b^18c^11d^6x^5 + 28a^0b^18c^10d^7x^6 + 28a^0b^18cd^8x^7 + 28a^0b^18d^9x^8 + 28a^0b^17c^18 + 28a^0b^17c^17d + 28a^0b^17c^16d^2x + 28a^0b^17c^15d^3x^2 + 28a^0b^17c^14d^4x^3 + 28a^0b^17c^13d^5x^4 + 28a^0b^17c^12d^6x^5 + 28a^0b^17c^11d^7x^6 + 28a^0b^17cd^8x^7 + 28a^0b^17d^9x^8 + 28a^0b^16c^19 + 28a^0b^16c^18d + 28a^0b^16c^17d^2x + 28a^0b^16c^16d^3x^2 + 28a^0b^16c^15d^4x^3 + 28a^0b^16c^14d^5x^4 + 28a^0b^16c^13d^6x^5 + 28a^0b^16c^12d^7x^6 + 28a^0b^16cd^8x^7 + 28a^0b^16d^9x^8 + 28a^0b^15c^20 + 28a^0b^15c^19d + 28a^0b^15c^18d^2x + 28a^0b^15c^17d^3x^2 + 28a^0b^15c^16d^4x^3 + 28a^0b^15c^15d^5x^4 + 28a^0b^15c^14d^6x^5 + 28a^0b^15c^13d^7x^6 + 28a^0b^15cd^8x^7 + 28a^0b^15d^9x^8 + 28a^0b^14c^21 + 28a^0b^14c^20d + 28a^0b^14c^19d^2x + 28a^0b^14c^18d^3x^2 + 28a^0b^14c^17d^4x^3 + 28a^0b^14c^16d^5x^4 + 28a^0b^14c^15d^6x^5 + 28a^0b^14c^14d^7x^6 + 28a^0b^14cd^8x^7 + 28a^0b^14d^9x^8 + 28a^0b^13c^22 + 28a^0b^13c^21d + 28a^0b^13c^20d^2x + 28a^0b^13c^19d^3x^2 + 28a^0b^13c^18d^4x^3 + 28a^0b^13c^17d^5x^4 + 28a^0b^13c^16d^6x^5 + 28a^0b^13c^15d^7x^6 + 28a^0b^13cd^8x^7 + 28a^0b^13d^9x^8 + 28a^0b^12c^23 + 28a^0b^12c^22d + 28a^0b^12c^21d^2x + 28a^0b^12c^20d^3x^2 + 28a^0b^12c^19d^4x^3 + 28a^0b^12c^18d^5x^4 + 28a^0b^12c^17d^6x^5 + 28a^0b^12c^16d^7x^6 + 28a^0b^12cd^8x^7 + 28a^0b^12d^9x^8 + 28a^0b^11c^24 + 28a^0b^11c^23d + 28a^0b^11c^22d^2x + 28a^0b^11c^21d^3x^2 + 28a^0b^11c^20d^4x^3 + 28a^0b^11c^19d^5x^4 + 28a^0b^11c^18d^6x^5 + 28a^0b^11c^17d^7x^6 + 28a^0b^11cd^8x^7 + 28a^0b^11d^9x^8 + 28a^0b^10c^25 + 28a^0b^10c^24d + 28a^0b^10c^23d^2x + 28a^0b^10c^22d^3x^2 + 28a^0b^10c^21d^4x^3 + 28a^0b^10c^20d^5x^4 + 28a^0b^10c^19d^6x^5 + 28a^0b^10c^18d^7x^6 + 28a^0b^10cd^8x^7 + 28a^0b^10d^9x^8 + 28a^0b^9c^26 + 28a^0b^9c^25d + 28a^0b^9c^24d^2x + 28a^0b^9c^23d^3x^2 + 28a^0b^9c^22d^4x^3 + 28a^0b^9c^21d^5x^4 + 28a^0b^9c^20d^6x^5 + 28a^0b^9c^19d^7x^6 + 28a^0b^9cd^8x^7 + 28a^0b^9d^9x^8 + 28a^0b^8c^27 + 28a^0b^8c^26d + 28a^0b^8c^25d^2x + 28a^0b^8c^24d^3x^2 + 28a^0b^8c^23d^4x^3 + 28a^0b^8c^22d^5x^4 + 28a^0b^8c^21d^6x^5 + 28a^0b^8c^20d^7x^6 + 28a^0b^8cd^8x^7 + 28a^0b^8d^9x^8 + 28a^0b^7c^28 + 28a^0b^7c^27d + 28a^0b^7c^26d^2x + 28a^0b^7c^25d^3x^2 + 28a^0b^7c^24d^4x^3 + 28a^0b^7c^23d^5x^4 + 28a^0b^7c^22d^6x^5 + 28a^0b^7c^21d^7x^6 + 28a^0b^7cd^8x^7 + 28a^0b^7d^9x^8 + 28a^0b^6c^29 + 28a^0b^6c^28d + 28a^0b^6c^27d^2x + 28a^0b^6c^26d^3x^2 + 28a^0b^6c^25d^4x^3 + 28a^0b^6c^24d^5x^4 + 28a^0b^6c^23d^6x^5 + 28a^0b^6c^22d^7x^6 + 28a^0b^6cd^8x^7 + 28a^0b^6d^9x^8 + 28a^0b^5c^30 + 28a^0b^5c^29d + 28a^0b^5c^28d^2x + 28a^0b^5c^27d^3x^2 + 28a^0b^5c^26d^4x^3 + 28a^0b^5c^25d^5x^4 + 28a^0b^5c^24d^6x^5 + 28a^0b^5c^23d^7x^6 + 28a^0b^5cd^8x^7 + 28a^0b^5d^9x^8 + 28a^0b^4c^31 + 28a^0b^4c^30d + 28a^0b^4c^29d^2x + 28a^0b^4c^28d^3x^2 + 28a^0b^4c^27d^4x^3 + 28a^0b^4c^26d^5x^4 + 28a^0b^4c^25d^6x^5 + 28a^0b^4c^24d^7x^6 + 28a^0b^4cd^8x^7 + 28a^0b^4d^9x^8 + 28a^0b^3c^32 + 28a^0b^3c^31d + 28a^0b^3c^30d^2x + 28a^0b^3c^29d^3x^2 + 28a^0b^3c^28d^4x^3 + 28a^0b^3c^27d^5x^4 + 28a^0b^3c^26d^6x^5 + 28a^0b^3c^25d^7x^6 + 28a^0b^3cd^8x^7 + 28a^0b^3d^9x^8 + 28a^0b^2c^33 + 28a^0b^2c^32d + 28a^0b^2c^31d^2x + 28a^0b^2c^30d^3x^2 + 28a^0b^2c^29d^4x^3 + 28a^0b^2c^28d^5x^4 + 28a^0b^2c^27d^6x^5 + 28a^0b^2c^26d^7x^6 + 28a^0b^2cd^8x^7 + 28a^0b^2d^9x^8 + 28a^0b^1c^34 + 28a^0b^1c^33d + 28a^0b^1c^32d^2x + 28a^0b^1c^31d^3x^2 + 28a^0b^1c^30d^4x^3 + 28a^0b^1c^29d^5x^4 + 28a^0b^1c^28d^6x^5 + 28a^0b^1c^27d^7x^6 + 28a^0b^1cd^8x^7 + 28a^0b^1d^9x^8 + 28a^0b^0c^35 + 28a^0b^0c^34d + 28a^0b^0c^33d^2x + 28a^0b^0c^32d^3x^2 + 28a^0b^0c^31d^4x^3 + 28a^0b^0c^30d^5x^4 + 28a^0b^0c^29d^6x^5 + 28a^0b^0c^28d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^36 + 28a^0b^0c^35d + 28a^0b^0c^34d^2x + 28a^0b^0c^33d^3x^2 + 28a^0b^0c^32d^4x^3 + 28a^0b^0c^31d^5x^4 + 28a^0b^0c^30d^6x^5 + 28a^0b^0c^29d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^37 + 28a^0b^0c^36d + 28a^0b^0c^35d^2x + 28a^0b^0c^34d^3x^2 + 28a^0b^0c^33d^4x^3 + 28a^0b^0c^32d^5x^4 + 28a^0b^0c^31d^6x^5 + 28a^0b^0c^30d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^38 + 28a^0b^0c^37d + 28a^0b^0c^36d^2x + 28a^0b^0c^35d^3x^2 + 28a^0b^0c^34d^4x^3 + 28a^0b^0c^33d^5x^4 + 28a^0b^0c^32d^6x^5 + 28a^0b^0c^31d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^39 + 28a^0b^0c^38d + 28a^0b^0c^37d^2x + 28a^0b^0c^36d^3x^2 + 28a^0b^0c^35d^4x^3 + 28a^0b^0c^34d^5x^4 + 28a^0b^0c^33d^6x^5 + 28a^0b^0c^32d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^40 + 28a^0b^0c^39d + 28a^0b^0c^38d^2x + 28a^0b^0c^37d^3x^2 + 28a^0b^0c^36d^4x^3 + 28a^0b^0c^35d^5x^4 + 28a^0b^0c^34d^6x^5 + 28a^0b^0c^33d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^41 + 28a^0b^0c^40d + 28a^0b^0c^39d^2x + 28a^0b^0c^38d^3x^2 + 28a^0b^0c^37d^4x^3 + 28a^0b^0c^36d^5x^4 + 28a^0b^0c^35d^6x^5 + 28a^0b^0c^34d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^42 + 28a^0b^0c^41d + 28a^0b^0c^40d^2x + 28a^0b^0c^39d^3x^2 + 28a^0b^0c^38d^4x^3 + 28a^0b^0c^37d^5x^4 + 28a^0b^0c^36d^6x^5 + 28a^0b^0c^35d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^43 + 28a^0b^0c^42d + 28a^0b^0c^41d^2x + 28a^0b^0c^40d^3x^2 + 28a^0b^0c^39d^4x^3 + 28a^0b^0c^38d^5x^4 + 28a^0b^0c^37d^6x^5 + 28a^0b^0c^36d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^44 + 28a^0b^0c^43d + 28a^0b^0c^42d^2x + 28a^0b^0c^41d^3x^2 + 28a^0b^0c^40d^4x^3 + 28a^0b^0c^39d^5x^4 + 28a^0b^0c^38d^6x^5 + 28a^0b^0c^37d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^45 + 28a^0b^0c^44d + 28a^0b^0c^43d^2x + 28a^0b^0c^42d^3x^2 + 28a^0b^0c^41d^4x^3 + 28a^0b^0c^40d^5x^4 + 28a^0b^0c^39d^6x^5 + 28a^0b^0c^38d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^46 + 28a^0b^0c^45d + 28a^0b^0c^44d^2x + 28a^0b^0c^43d^3x^2 + 28a^0b^0c^42d^4x^3 + 28a^0b^0c^41d^5x^4 + 28a^0b^0c^40d^6x^5 + 28a^0b^0c^39d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^47 + 28a^0b^0c^46d + 28a^0b^0c^45d^2x + 28a^0b^0c^44d^3x^2 + 28a^0b^0c^43d^4x^3 + 28a^0b^0c^42d^5x^4 + 28a^0b^0c^41d^6x^5 + 28a^0b^0c^40d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^48 + 28a^0b^0c^47d + 28a^0b^0c^46d^2x + 28a^0b^0c^45d^3x^2 + 28a^0b^0c^44d^4x^3 + 28a^0b^0c^43d^5x^4 + 28a^0b^0c^42d^6x^5 + 28a^0b^0c^41d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^49 + 28a^0b^0c^48d + 28a^0b^0c^47d^2x + 28a^0b^0c^46d^3x^2 + 28a^0b^0c^45d^4x^3 + 28a^0b^0c^44d^5x^4 + 28a^0b^0c^43d^6x^5 + 28a^0b^0c^42d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^50 + 28a^0b^0c^49d + 28a^0b^0c^48d^2x + 28a^0b^0c^47d^3x^2 + 28a^0b^0c^46d^4x^3 + 28a^0b^0c^45d^5x^4 + 28a^0b^0c^44d^6x^5 + 28a^0b^0c^43d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^51 + 28a^0b^0c^50d + 28a^0b^0c^49d^2x + 28a^0b^0c^48d^3x^2 + 28a^0b^0c^47d^4x^3 + 28a^0b^0c^46d^5x^4 + 28a^0b^0c^45d^6x^5 + 28a^0b^0c^44d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^52 + 28a^0b^0c^51d + 28a^0b^0c^50d^2x + 28a^0b^0c^49d^3x^2 + 28a^0b^0c^48d^4x^3 + 28a^0b^0c^47d^5x^4 + 28a^0b^0c^46d^6x^5 + 28a^0b^0c^45d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^53 + 28a^0b^0c^52d + 28a^0b^0c^51d^2x + 28a^0b^0c^50d^3x^2 + 28a^0b^0c^49d^4x^3 + 28a^0b^0c^48d^5x^4 + 28a^0b^0c^47d^6x^5 + 28a^0b^0c^46d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^54 + 28a^0b^0c^53d + 28a^0b^0c^52d^2x + 28a^0b^0c^51d^3x^2 + 28a^0b^0c^50d^4x^3 + 28a^0b^0c^49d^5x^4 + 28a^0b^0c^48d^6x^5 + 28a^0b^0c^47d^7x^6 + 28a^0b^0cd^8x^7 + 28a^0b^0d^9x^8 + 28a^0b^0c^55 + 28a^0b^0c^54$$

[In] `int((c + d*x)^7/(a + b*x)^9,x)`

[Out]
$$-(a^7d^7 + b^7c^7 + 8b^7d^7x^7 + 28ab^6d^7x^6 + 28b^7cd^6x^6 + a^2b^5c^5d^2 + a^3b^4c^4d^3 + a^4b^3c^3d^4 + a^5b^2c^2d^5 + 28a^5b^2d^7x^2 + 56a^4b^3d^7x^3 + 70a^3b^4d^7x^4 + 56a^2b^5d^7x^5 + 28b^7c^5d^2x^2 + 56b^7c^4d^3x^3 + 70b^7c^3d^4x^4 + 56b^7c^2d^5x^5 + ab^6c^6d + a^6b^6cd^6 + 8a^6bd^7x + 8b^7c^6dx + 28a^2b^5c^3d^4x^2 + 28a^3b^4c^2d^5x^2 + 56a^2b^5c^2d^5x^3 + 8ab^6c^5d^2x + 8a^5b^2cd^6x + 56ab^6cd^6x^5 + 8a^2b^5c^4d^3x + 8a^3b^4c^3d^4x + 8a^4b^3c^2d^5x + 28ab^6c^4d^3x^2 + 28a^4b^3cd^6x^2 + 56ab^6c^3d^4x^3 + 56a^3b^4cd^6x^3 + 70ab^6c^2d^5x^4 + 70a^2b^5cd^6x^4)/(8a^8b^8 + 8b^16x^8 + 64a^7b^9x + 64ab^15x^7 + 224a^6b^10x^2 + 448a^5b^11x^3 + 560a^4b^12x^4 + 448a^3b^13x^5 + 224a^2b^14x^6)$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**7/(b*x+a)**9,x)`

[Out] Timed out

$$3.1292 \quad \int \frac{(c+dx)^7}{(a+bx)^{10}} dx$$

Optimal. Leaf size=58

$$\frac{d(c+dx)^8}{72(a+bx)^8(bc-ad)^2} - \frac{(c+dx)^8}{9(a+bx)^9(bc-ad)}$$

[Out] $-1/9*(d*x+c)^8/(-a*d+b*c)/(b*x+a)^9+1/72*d*(d*x+c)^8/(-a*d+b*c)^2/(b*x+a)^8$

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{d(c+dx)^8}{72(a+bx)^8(bc-ad)^2} - \frac{(c+dx)^8}{9(a+bx)^9(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^10,x]

[Out] $-(c + d*x)^8/(9*(b*c - a*d)*(a + b*x)^9) + (d*(c + d*x)^8)/(72*(b*c - a*d)^2*(a + b*x)^8)$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^{10}} dx = -\frac{(c+dx)^8}{9(bc-ad)(a+bx)^9} - \frac{d \int \frac{(c+dx)^7}{(a+bx)^9} dx}{9(bc-ad)}$$

$$= -\frac{(c+dx)^8}{9(bc-ad)(a+bx)^9} + \frac{d(c+dx)^8}{72(bc-ad)^2(a+bx)^8}$$

Mathematica [B] time = 0.13, size = 367, normalized size = 6.33

$$a^7 d^7 + a^6 b d^6 (2c + 9dx) + 3a^5 b^2 d^5 (c^2 + 6cdx + 12d^2 x^2) + a^4 b^3 d^4 (4c^3 + 27c^2 dx + 72cd^2 x^2 + 84d^3 x^3) + a^3 b^4 d^3 (2c^4 + 12c^3 dx + 36c^2 d^2 x^2 + 48cd^3 x^3 + 36d^4 x^4) + 3a^2 b^5 d^2 (2c^5 + 15c^4 dx + 48c^3 d^2 x^2 + 84c^2 d^3 x^3 + 84cd^4 x^4 + 42d^5 x^5) + a b^6 d (7c^6 + 54c^5 dx + 180c^4 d^2 x^2 + 336c^3 d^3 x^3 + 378c^2 d^4 x^4 + 252cd^5 x^5 + 84d^6 x^6) + b^7 (8c^7 + 63c^6 dx + 216c^5 d^2 x^2 + 420c^4 d^3 x^3 + 504c^3 d^4 x^4 + 378c^2 d^5 x^5 + 168cd^6 x^6 + 36d^7 x^7) / (b^8 (a + b x)^9)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^10,x]

[Out]
$$-1/72*(a^7*d^7 + a^6*b*d^6*(2*c + 9*d*x) + 3*a^5*b^2*d^5*(c^2 + 6*c*d*x + 12*d^2*x^2) + a^4*b^3*d^4*(4*c^3 + 27*c^2*d*x + 72*c*d^2*x^2 + 84*d^3*x^3) + a^3*b^4*d^3*(5*c^4 + 36*c^3*d*x + 108*c^2*d^2*x^2 + 168*c*d^3*x^3 + 126*d^4*x^4) + 3*a^2*b^5*d^2*(2*c^5 + 15*c^4*d*x + 48*c^3*d^2*x^2 + 84*c^2*d^3*x^3 + 84*c*d^4*x^4 + 42*d^5*x^5) + a*b^6*d*(7*c^6 + 54*c^5*d*x + 180*c^4*d^2*x^2 + 336*c^3*d^3*x^3 + 378*c^2*d^4*x^4 + 252*c*d^5*x^5 + 84*d^6*x^6) + b^7*(8*c^7 + 63*c^6*d*x + 216*c^5*d^2*x^2 + 420*c^4*d^3*x^3 + 504*c^3*d^4*x^4 + 378*c^2*d^5*x^5 + 168*c*d^6*x^6 + 36*d^7*x^7))/(b^8*(a + b*x)^9)$$

fricas [B] time = 0.41, size = 548, normalized size = 9.45

$$36 b^7 d^7 x^7 + 8 b^7 c^7 + 7 a b^6 c^6 d + 6 a^2 b^5 c^5 d^2 + 5 a^3 b^4 c^4 d^3 + 4 a^4 b^3 c^3 d^4 + 3 a^5 b^2 c^2 d^5 + 2 a^6 b c d^6 + a^7 d^7 + 84 (2 b^7 c^7 d^7 x^7 + 7 a b^6 c^6 d^6 x^6 + 126 a^2 b^5 c^5 d^5 x^5 + 126 a^3 b^4 c^4 d^4 x^4 + 84 a^4 b^3 c^3 d^3 x^3 + 36 a^5 b^2 c^2 d^2 x^2 + 9 a^6 b c d x + a^7 d^7) / (b^17 x^9 + 9 a b^16 x^8 + 36 a^2 b^15 x^7 + 126 a^3 b^14 x^6 + 378 a^4 b^13 x^5 + 840 a^5 b^12 x^4 + 1260 a^6 b^11 x^3 + 1008 a^7 b^10 x^2 + 504 a^8 b^9 x + 72 a^9 b^8)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^10,x, algorithm="fricas")

[Out]
$$-1/72*(36*b^7*d^7*x^7 + 8*b^7*c^7 + 7*a*b^6*c^6*d + 6*a^2*b^5*c^5*d^2 + 5*a^3*b^4*c^4*d^3 + 4*a^4*b^3*c^3*d^4 + 3*a^5*b^2*c^2*d^5 + 2*a^6*b*c*d^6 + a^7*d^7 + 84*(2*b^7*c^7*d^7*x^7 + 7*a*b^6*c^6*d^6*x^6 + 126*(3*b^7*c^2*d^5 + 2*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 126*(4*b^7*c^3*d^4 + 3*a*b^6*c^2*d^5 + 2*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 84*(5*b^7*c^4*d^3 + 4*a*b^6*c^3*d^4 + 3*a^2*b^5*c^2*d^5 + 2*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 36*(6*b^7*c^5*d^2 + 5*a*b^6*c^4*d^3 + 4*a^2*b^5*c^3*d^4 + 3*a^3*b^4*c^2*d^5 + 2*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 9*(7*b^7*c^6*d + 6*a*b^6*c^5*d^2 + 5*a^2*b^5*c^4*d^3 + 4*a^3*b^4*c^3*d^4 + 3*a^4*b^3*c^2*d^5 + 2*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^17*x^9 + 9 a b^16 x^8 + 36 a^2 b^15 x^7 + 126 a^3 b^14 x^6 + 378 a^4 b^13 x^5 + 840 a^5 b^12 x^4 + 1260 a^6 b^11 x^3 + 1008 a^7 b^10 x^2 + 504 a^8 b^9 x + 72 a^9 b^8)$$

$*a*b^{16}*x^8 + 36*a^2*b^{15}*x^7 + 84*a^3*b^{14}*x^6 + 126*a^4*b^{13}*x^5 + 126*a^5*b^{12}*x^4 + 84*a^6*b^{11}*x^3 + 36*a^7*b^{10}*x^2 + 9*a^8*b^9*x + a^9*b^8)$

giac [B] time = 1.27, size = 496, normalized size = 8.55

$$\frac{36b^7d^7x^7 + 168b^7cd^6x^6 + 84ab^6d^7x^6 + 378b^7c^2d^5x^5 + 252ab^6cd^6x^5 + 126a^2b^5d^7x^5 + 504b^7c^3d^4x^4 + 378ab^6c^2d^5x^4 + 252a^2b^5c^3d^4x^4 + 126a^3b^4d^7x^4 + 420b^7c^4d^3x^3 + 336a^2b^6c^3d^4x^3 + 252a^2b^5c^2d^5x^3 + 168a^3b^4c^3d^6x^3 + 84a^4b^3d^7x^3 + 216b^7c^5d^2x^2 + 180a^2b^6c^4d^3x^2 + 144a^2b^5c^3d^4x^2 + 108a^3b^4c^2d^5x^2 + 72a^4b^3c^2d^6x^2 + 36a^5b^2d^7x^2 + 63b^7c^6d^1x + 54a^2b^6c^5d^2x + 45a^2b^5c^4d^3x + 36a^3b^4c^3d^4x + 27a^4b^3c^2d^5x + 18a^5b^2c^2d^6x + 9a^6b^1d^7x + 8b^7c^7 + 7a^2b^6c^6d + 6a^2b^5c^5d^2 + 5a^3b^4c^4d^3 + 4a^4b^3c^3d^4 + 3a^5b^2c^2d^5 + 2a^6b^1c^1d^6 + a^7d^7}{(bx + a)^9b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^10,x, algorithm="giac")

[Out] $-1/72*(36*b^7*d^7*x^7 + 168*b^7*c*d^6*x^6 + 84*a*b^6*d^7*x^6 + 378*b^7*c^2*d^5*x^5 + 252*a*b^6*c*d^6*x^5 + 126*a^2*b^5*d^7*x^5 + 504*b^7*c^3*d^4*x^4 + 378*a*b^6*c^2*d^5*x^4 + 252*a^2*b^5*c*d^6*x^4 + 126*a^3*b^4*d^7*x^4 + 420*b^7*c^4*d^3*x^3 + 336*a*b^6*c^3*d^4*x^3 + 252*a^2*b^5*c^2*d^5*x^3 + 168*a^3*b^4*c^3*d^6*x^3 + 84*a^4*b^3*d^7*x^3 + 216*b^7*c^5*d^2*x^2 + 180*a^2*b^6*c^4*d^3*x^2 + 144*a^2*b^5*c^3*d^4*x^2 + 108*a^3*b^4*c^2*d^5*x^2 + 72*a^4*b^3*c^2*d^6*x^2 + 36*a^5*b^2*d^7*x^2 + 63*b^7*c^6*d^1*x + 54*a^2*b^6*c^5*d^2*x + 45*a^2*b^5*c^4*d^3*x + 36*a^3*b^4*c^3*d^4*x + 27*a^4*b^3*c^2*d^5*x + 18*a^5*b^2*c^2*d^6*x + 9*a^6*b^1*d^7*x + 8*b^7*c^7 + 7*a^2*b^6*c^6*d + 6*a^2*b^5*c^5*d^2 + 5*a^3*b^4*c^4*d^3 + 4*a^4*b^3*c^3*d^4 + 3*a^5*b^2*c^2*d^5 + 2*a^6*b^1*c^1*d^6 + a^7*d^7)/(b*x + a)^9*b^8)$

maple [B] time = 0.01, size = 464, normalized size = 8.00

$$\frac{d^7}{2(bx+a)^2b^8} + \frac{7(ad-bc)d^6}{3(bx+a)^3b^8} - \frac{21(a^2d^2-2abcd+b^2c^2)d^5}{4(bx+a)^4b^8} + \frac{7(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^4}{(bx+a)^5b^8} - \frac{35(a^4d^4-4a^3bcd^3+3a^2b^2c^2d^2-2ab^3cd^2+b^4c^3)d^3}{(bx+a)^6b^8} + \frac{7(a^5d^5-5a^4bcd^4+10a^3b^2c^2d^3-10a^2b^3c^3d^2+5a^3b^4c^4d-b^5c^5)}{(bx+a)^7b^8} - \frac{1}{9} \frac{(-a^7d^7+7a^6bcd^6-21a^5b^2c^2d^5+35a^4b^3c^3d^4-35a^3b^4c^4d^3+21a^2b^5c^5d^2-7a^2b^6c^6d+b^7c^7)}{(bx+a)^9b^8} + \frac{7d^4(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}{(bx+a)^9b^8} - \frac{1}{2} \frac{d^7}{(bx+a)^2b^8} - \frac{21}{4} \frac{d^5(a^2d^2-2a^2bcd+b^2c^2)}{(bx+a)^2b^8} - \frac{35}{6} \frac{d^3(a^4d^4-4a^3bcd^3+6a^2b^2c^2d^2-4a^2b^3cd^2+3a^3b^4c^4)}{(bx+a)^6b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^10,x)

[Out] $-7/8*d*(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^8/(b*x+a)^8+7/3*d^6*(a*d-b*c)/b^8/(b*x+a)^3+3*d^2*(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)/b^8/(b*x+a)^7-1/9*(-a^7*d^7+7*a^6*b*c*d^6-21*a^5*b^2*c^2*d^5+35*a^4*b^3*c^3*d^4-35*a^3*b^4*c^4*d^3+21*a^2*b^5*c^5*d^2-7*a^2*b^6*c^6*d+b^7*c^7)/b^8/(b*x+a)^9+7*d^4*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^8/(b*x+a)^5-1/2*d^7/b^8/(b*x+a)^2-21/4*d^5*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^8/(b*x+a)^4-35/6*d^3*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a^2*b^3*c^3*d+b^4*c^4)/b^8/(b*x+a)^6$

maxima [B] time = 1.71, size = 548, normalized size = 9.45

$$\frac{36b^7d^7x^7 + 8b^7c^7 + 7ab^6c^6d + 6a^2b^5c^5d^2 + 5a^3b^4c^4d^3 + 4a^4b^3c^3d^4 + 3a^5b^2c^2d^5 + 2a^6bcd^6 + a^7d^7 + 84(2b^7c^6d^2 + 3a^2b^6c^5d^3 + 4a^3b^5c^4d^4 + 5a^4b^4c^3d^5 + 6a^5b^3c^2d^6 + 7a^6b^2c^1d^7 + 8a^7b^1c^0d^8)}{(bx+a)^9b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^10,x, algorithm="maxima")

[Out]
$$-1/72*(36*b^7*d^7*x^7 + 8*b^7*c^7 + 7*a*b^6*c^6*d + 6*a^2*b^5*c^5*d^2 + 5*a^3*b^4*c^4*d^3 + 4*a^4*b^3*c^3*d^4 + 3*a^5*b^2*c^2*d^5 + 2*a^6*b*c*d^6 + a^7*d^7 + 84*(2*b^7*c*d^6 + a*b^6*d^7)*x^6 + 126*(3*b^7*c^2*d^5 + 2*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 126*(4*b^7*c^3*d^4 + 3*a*b^6*c^2*d^5 + 2*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 84*(5*b^7*c^4*d^3 + 4*a*b^6*c^3*d^4 + 3*a^2*b^5*c^2*d^5 + 2*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 36*(6*b^7*c^5*d^2 + 5*a*b^6*c^4*d^3 + 4*a^2*b^5*c^3*d^4 + 3*a^3*b^4*c^2*d^5 + 2*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 9*(7*b^7*c^6*d + 6*a*b^6*c^5*d^2 + 5*a^2*b^5*c^4*d^3 + 4*a^3*b^4*c^3*d^4 + 3*a^4*b^3*c^2*d^5 + 2*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^17*x^9 + 9*a*b^16*x^8 + 36*a^2*b^15*x^7 + 84*a^3*b^14*x^6 + 126*a^4*b^13*x^5 + 126*a^5*b^12*x^4 + 84*a^6*b^11*x^3 + 36*a^7*b^10*x^2 + 9*a^8*b^9*x + a^9*b^8)$$

mupad [B] time = 0.15, size = 39, normalized size = 0.67

$$\frac{(c + dx)^8 (9ad - 8bc + bdx)}{72(ad - bc)^2 (a + bx)^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^10,x)

[Out] $((c + d*x)^8*(9*a*d - 8*b*c + b*d*x))/(72*(a*d - b*c)^2*(a + b*x)^9)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**10,x)

[Out] Timed out

3.1293

$$\int \frac{(c+dx)^7}{(a+bx)^{11}} dx$$

Optimal. Leaf size=89

$$-\frac{d^2(c+dx)^8}{360(a+bx)^8(bc-ad)^3} + \frac{d(c+dx)^8}{45(a+bx)^9(bc-ad)^2} - \frac{(c+dx)^8}{10(a+bx)^{10}(bc-ad)}$$

[Out] $-1/10*(d*x+c)^8/(-a*d+b*c)/(b*x+a)^{10}+1/45*d*(d*x+c)^8/(-a*d+b*c)^2/(b*x+a)^9-1/360*d^2*(d*x+c)^8/(-a*d+b*c)^3/(b*x+a)^8$

Rubi [A] time = 0.02, antiderivative size = 89, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{d^2(c+dx)^8}{360(a+bx)^8(bc-ad)^3} + \frac{d(c+dx)^8}{45(a+bx)^9(bc-ad)^2} - \frac{(c+dx)^8}{10(a+bx)^{10}(bc-ad)}$$

Antiderivative was successfully verified.

[In] `Int[(c + d*x)^7/(a + b*x)^11,x]`

[Out] $-(c + d*x)^8/(10*(b*c - a*d)*(a + b*x)^{10}) + (d*(c + d*x)^8)/(45*(b*c - a*d)^2*(a + b*x)^9) - (d^2*(c + d*x)^8)/(360*(b*c - a*d)^3*(a + b*x)^8)$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^7}{(a+bx)^{11}} dx &= -\frac{(c+dx)^8}{10(bc-ad)(a+bx)^{10}} - \frac{d \int \frac{(c+dx)^7}{(a+bx)^{10}} dx}{5(bc-ad)} \\
&= -\frac{(c+dx)^8}{10(bc-ad)(a+bx)^{10}} + \frac{d(c+dx)^8}{45(bc-ad)^2(a+bx)^9} + \frac{d^2 \int \frac{(c+dx)^7}{(a+bx)^9} dx}{45(bc-ad)^2} \\
&= -\frac{(c+dx)^8}{10(bc-ad)(a+bx)^{10}} + \frac{d(c+dx)^8}{45(bc-ad)^2(a+bx)^9} - \frac{d^2(c+dx)^8}{360(bc-ad)^3(a+bx)^8}
\end{aligned}$$

Mathematica [B] time = 0.12, size = 371, normalized size = 4.17

$$\frac{a^7 d^7 + a^6 b d^6 (3c + 10dx) + 3a^5 b^2 d^5 (2c^2 + 10cdx + 15d^2 x^2) + 5a^4 b^3 d^4 (2c^3 + 12c^2 dx + 27cd^2 x^2 + 24d^3 x^3) + 5a^3 b^4 d^3 (2c^4 + 12c^3 dx + 27c^2 d^2 x^2 + 24cd^3 x^3) + 3a^2 b^5 d^2 (7c^5 + 50c^4 dx + 150c^3 d^2 x^2 + 240c^2 d^3 x^3 + 210c d^4 x^4 + 84d^5 x^5) + a b^6 d (28c^6 + 210c^5 dx + 675c^4 d^2 x^2 + 1200c^3 d^3 x^3 + 1260c^2 d^4 x^4 + 756c d^5 x^5 + 210d^6 x^6) + b^7 (36c^7 + 280c^6 dx + 945c^5 d^2 x^2 + 1800c^4 d^3 x^3 + 2100c^3 d^4 x^4 + 1512c^2 d^5 x^5 + 630c d^6 x^6 + 120d^7 x^7)}{(b^8 (a + bx)^{10})}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^11,x]

[Out] -1/360*(a^7*d^7 + a^6*b*d^6*(3*c + 10*d*x) + 3*a^5*b^2*d^5*(2*c^2 + 10*c*d*x + 15*d^2*x^2) + 5*a^4*b^3*d^4*(2*c^3 + 12*c^2*d*x + 27*c*d^2*x^2 + 24*d^3*x^3) + 5*a^3*b^4*d^3*(3*c^4 + 20*c^3*d*x + 54*c^2*d^2*x^2 + 72*c*d^3*x^3 + 42*d^4*x^4) + 3*a^2*b^5*d^2*(7*c^5 + 50*c^4*d*x + 150*c^3*d^2*x^2 + 240*c^2*d^3*x^3 + 210*c*d^4*x^4 + 84*d^5*x^5) + a*b^6*d*(28*c^6 + 210*c^5*d*x + 675*c^4*d^2*x^2 + 1200*c^3*d^3*x^3 + 1260*c^2*d^4*x^4 + 756*c*d^5*x^5 + 210*d^6*x^6) + b^7*(36*c^7 + 280*c^6*d*x + 945*c^5*d^2*x^2 + 1800*c^4*d^3*x^3 + 2100*c^3*d^4*x^4 + 1512*c^2*d^5*x^5 + 630*c*d^6*x^6 + 120*d^7*x^7))/(b^8*(a + b*x)^10)

fricas [B] time = 0.43, size = 559, normalized size = 6.28

$$\frac{120 b^7 d^7 x^7 + 36 b^7 c^7 + 28 a b^6 c^6 d + 21 a^2 b^5 c^5 d^2 + 15 a^3 b^4 c^4 d^3 + 10 a^4 b^3 c^3 d^4 + 6 a^5 b^2 c^2 d^5 + 3 a^6 b c d^6 + a^7 d^7 + 5 a^6 b^2 c^5 d^5 + 15 a^5 b^3 c^4 d^4 + 10 a^4 b^4 c^3 d^3 + 6 a^3 b^5 c^2 d^2 + 3 a^2 b^6 c d + 120 a b^7 c^7 + 210 a^2 b^6 c^6 d + 252 a^3 b^5 c^5 d^2 + 210 a^4 b^4 c^4 d^3 + 120 a^5 b^3 c^3 d^4 + 10 a^6 b^2 c^2 d^5 + 3 a^7 b c d^6 + 120 a^8 d^7}{b^8 (a + b x)^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^11,x, algorithm="fricas")

[Out] -1/360*(120*b^7*d^7*x^7 + 36*b^7*c^7 + 28*a*b^6*c^6*d + 21*a^2*b^5*c^5*d^2 + 15*a^3*b^4*c^4*d^3 + 10*a^4*b^3*c^3*d^4 + 6*a^5*b^2*c^2*d^5 + 3*a^6*b*c*d^6 + a^7*d^7 + 210*(3*b^7*c*d^6 + a*b^6*d^7)*x^6 + 252*(6*b^7*c^2*d^5 + 3*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 210*(10*b^7*c^3*d^4 + 6*a*b^6*c^2*d^5 + 3*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 120*(15*b^7*c^4*d^3 + 10*a*b^6*c^3*d^4 + 6*a^2*b^5*c^2*d^5 + 3*a*b^4*d^7)*x^3 + 36*(36*c^7 + 280*c^6*d*x + 945*c^5*d^2*x^2 + 1800*c^4*d^3*x^3 + 2100*c^3*d^4*x^4 + 1512*c^2*d^5*x^5 + 630*c*d^6*x^6 + 120*d^7*x^7)/b^8*(a + b*x)^10)

$$\frac{6a^2b^5c^2d^5 + 3a^3b^4cd^6 + a^4b^3d^7)x^3 + 45(21b^7c^5d^2 + 15a^2b^6c^4d^3 + 10a^3b^5c^3d^4 + 6a^4b^4c^2d^5 + 3a^5b^3c^2d^6 + a^6b^2c^2d^7)x^2 + 10(28b^7c^6d + 21a^2b^6c^5d^2 + 15a^3b^5c^4d^3 + 10a^4b^4c^3d^4 + 6a^5b^3c^2d^5 + 3a^6b^2c^2d^6 + a^7b^2c^2d^7)x}{(b^{18}x^{10} + 10a^2b^{17}x^9 + 45a^3b^{16}x^8 + 120a^4b^{15}x^7 + 210a^5b^{14}x^6 + 252a^6b^{13}x^5 + 210a^7b^{12}x^4 + 120a^8b^{11}x^3 + 45a^9b^{10}x^2 + 10a^{10}b^9x + a^{10}b^8)}$$

giac [B] time = 1.31, size = 496, normalized size = 5.57

$$120b^7d^7x^7 + 630b^7cd^6x^6 + 210ab^6d^7x^6 + 1512b^7c^2d^5x^5 + 756ab^6cd^6x^5 + 252a^2b^5d^7x^5 + 2100b^7c^3d^4x^4 + 1260a^2b^6c^2d^5x^4 + 630a^3b^5c^3d^4x^4 + 210a^4b^4c^4d^7x^4 + 1800b^7c^4d^3x^3 + 1200a^2b^6c^3d^4x^3 + 720a^3b^5c^2d^5x^3 + 360a^4b^4c^2d^6x^3 + 120a^5b^3c^2d^7x^3 + 945b^7c^5d^2x^2 + 675a^2b^6c^4d^3x^2 + 450a^3b^5c^3d^4x^2 + 270a^4b^4c^2d^5x^2 + 135a^5b^3c^2d^6x^2 + 45a^6b^2c^2d^7x^2 + 280b^7c^6d^2x + 210a^2b^6c^5d^2x + 150a^3b^5c^4d^3x + 100a^4b^4c^3d^4x + 60a^5b^3c^2d^5x + 30a^6b^2c^2d^6x + 10a^7b^2c^2d^7x + 36b^7c^7 + 28a^2b^6c^6d + 21a^3b^5c^5d^2 + 15a^4b^4c^4d^3 + 10a^5b^3c^3d^4 + 6a^6b^2c^2d^5 + 3a^7b^2c^2d^6 + a^7d^7)/((bx + a)^{10}b^8)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^11,x, algorithm="giac")

[Out]
$$\frac{-1/360(120b^7d^7x^7 + 630b^7cd^6x^6 + 210a^2b^6d^7x^6 + 1512b^7c^2d^5x^5 + 756a^2b^6cd^6x^5 + 252a^3b^5d^7x^5 + 2100b^7c^3d^4x^4 + 1260a^2b^6c^2d^5x^4 + 630a^3b^5c^3d^4x^4 + 210a^4b^4c^4d^7x^4 + 1800b^7c^4d^3x^3 + 1200a^2b^6c^3d^4x^3 + 720a^3b^5c^2d^5x^3 + 360a^4b^4c^2d^6x^3 + 120a^5b^3c^2d^7x^3 + 945b^7c^5d^2x^2 + 675a^2b^6c^4d^3x^2 + 450a^3b^5c^3d^4x^2 + 270a^4b^4c^2d^5x^2 + 135a^5b^3c^2d^6x^2 + 45a^6b^2c^2d^7x^2 + 280b^7c^6d^2x + 210a^2b^6c^5d^2x + 150a^3b^5c^4d^3x + 100a^4b^4c^3d^4x + 60a^5b^3c^2d^5x + 30a^6b^2c^2d^6x + 10a^7b^2c^2d^7x + 36b^7c^7 + 28a^2b^6c^6d + 21a^3b^5c^5d^2 + 15a^4b^4c^4d^3 + 10a^5b^3c^3d^4 + 6a^6b^2c^2d^5 + 3a^7b^2c^2d^6 + a^7d^7)/((bx + a)^{10}b^8)}$$

maple [B] time = 0.01, size = 464, normalized size = 5.21

$$\frac{d^7}{3(bx+a)^3b^8} + \frac{7(ad-bc)d^6}{4(bx+a)^4b^8} - \frac{21(a^2d^2-2abcd+b^2c^2)d^5}{5(bx+a)^5b^8} + \frac{35(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^4}{6(bx+a)^6b^8} - \frac{5(a^4d^4-4a^3b^2c^2d^2+6a^2b^3c^3d+b^4c^4)}{b^8(bx+a)^7} - \frac{7d^3(a^4d^4-4a^3b^2c^2d^2+6a^2b^3c^3d+b^4c^4)}{b^8(bx+a)^8} - \frac{5d^2(a^5d^5-5a^4b^2c^2d^3-10a^3b^3c^3d^2+5a^2b^4c^4d-b^5c^5)}{b^8(bx+a)^9} - \frac{21d^2(a^6d^6-6a^5b^3c^2d^4-20a^4b^4c^3d^3+15a^3b^5c^4d^2-6a^2b^6c^5d+b^6c^6)}{b^8(bx+a)^9} - \frac{21d^2(a^7d^7-2a^6b^2c^2d^5+7a^5b^3c^3d^4-2a^4b^4c^4d^3+3a^3b^5c^5d^2+b^6c^6)}{b^8(bx+a)^9} - \frac{7d^2(a^7d^7-2a^6b^2c^2d^5+7a^5b^3c^3d^4-2a^4b^4c^4d^3+3a^3b^5c^5d^2+b^6c^6)}{b^8(bx+a)^9} - \frac{21d^2(a^8d^8-8a^7b^3c^2d^6+28a^6b^4c^3d^5-35a^5b^5c^4d^4+21a^4b^6c^5d^3-7a^3b^7c^6d^2+b^7c^7)}{b^8(bx+a)^9} - \frac{5d^2(a^8d^8-8a^7b^3c^2d^6+28a^6b^4c^3d^5-35a^5b^5c^4d^4+21a^4b^6c^5d^3-7a^3b^7c^6d^2+b^7c^7)}{b^8(bx+a)^9} - \frac{1}{10}(-a^7d^7+7a^6b^2c^2d^6-21a^5b^3c^3d^5+35a^4b^4c^4d^4-35a^3b^5c^5d^3+21a^2b^6c^6d^2-7a^2b^7c^7)/b^8(bx+a)^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^11,x)

[Out]
$$\frac{21}{8}d^2\frac{(a^5d^5-5a^4b^2c^2d^3-10a^3b^3c^3d^2+5a^2b^4c^4d-b^5c^5)}{b^8(bx+a)^8} - \frac{1}{3}d^7\frac{1}{b^8(bx+a)^3} - \frac{5d^3(a^4d^4-4a^3b^2c^2d^2+6a^2b^3c^3d+b^4c^4)}{b^8(bx+a)^7} - \frac{7}{9}d^2\frac{(a^6d^6-6a^5b^3c^2d^4-20a^4b^4c^3d^3+15a^3b^5c^4d^2-6a^2b^6c^5d+b^6c^6)}{b^8(bx+a)^9} - \frac{21}{5}d^5\frac{(a^2d^2-2a^2b^2c^2d^2+b^2c^2)}{b^8(bx+a)^5} + \frac{7}{4}d^6\frac{(a^4d^4-4a^3b^2c^2d^2+6a^2b^3c^3d+b^4c^4)}{b^8(bx+a)^4} + \frac{35}{6}d^4\frac{(a^3d^3-3a^2b^2c^2d^2+3a^2b^3c^3d+b^4c^4)}{b^8(bx+a)^6} - \frac{1}{10}(-a^7d^7+7a^6b^2c^2d^6-21a^5b^3c^3d^5+35a^4b^4c^4d^4-35a^3b^5c^5d^3+21a^2b^6c^6d^2-7a^2b^7c^7)/b^8(bx+a)^9$$

$$\frac{2c^2d^5 + 35a^4b^3c^3d^4 - 35a^3b^4c^4d^3 + 21a^2b^5c^5d^2 - 7a^6b^6c^6d + b^7c^7}{b^8(bx+a)^{10}}$$

maxima [B] time = 1.73, size = 559, normalized size = 6.28

$$\frac{120b^7d^7x^7 + 36b^7c^7 + 28ab^6c^6d + 21a^2b^5c^5d^2 + 15a^3b^4c^4d^3 + 10a^4b^3c^3d^4 + 6a^5b^2c^2d^5 + 3a^6bcd^6 + a^7d^7}{b^{18}x^{10} + 10a^2b^{17}x^9 + 45a^4b^{16}x^8 + 120a^6b^{15}x^7 + 210a^8b^{14}x^6 + 252a^{10}b^{13}x^5 + 210a^{12}b^{12}x^4 + 120a^{14}b^{11}x^3 + 45a^{16}b^{10}x^2 + 10a^{18}b^9x + a^{20}b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^11,x, algorithm="maxima")

[Out]
$$-1/360*(120*b^7*d^7*x^7 + 36*b^7*c^7 + 28*a*b^6*c^6*d + 21*a^2*b^5*c^5*d^2 + 15*a^3*b^4*c^4*d^3 + 10*a^4*b^3*c^3*d^4 + 6*a^5*b^2*c^2*d^5 + 3*a^6*b*c*d^6 + a^7*d^7 + 210*(3*b^7*c*d^6 + a*b^6*d^7)*x^6 + 252*(6*b^7*c^2*d^5 + 3*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 210*(10*b^7*c^3*d^4 + 6*a*b^6*c^2*d^5 + 3*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 120*(15*b^7*c^4*d^3 + 10*a*b^6*c^3*d^4 + 6*a^2*b^5*c^2*d^5 + 3*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 45*(21*b^7*c^5*d^2 + 15*a*b^6*c^4*d^3 + 10*a^2*b^5*c^3*d^4 + 6*a^3*b^4*c^2*d^5 + 3*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 10*(28*b^7*c^6*d + 21*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 + 10*a^3*b^4*c^3*d^4 + 6*a^4*b^3*c^2*d^5 + 3*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^18*x^10 + 10*a^2*b^17*x^9 + 45*a^4*b^16*x^8 + 120*a^6*b^15*x^7 + 210*a^8*b^14*x^6 + 252*a^10*b^13*x^5 + 210*a^12*b^12*x^4 + 120*a^14*b^11*x^3 + 45*a^16*b^10*x^2 + 10*a^18*b^9*x + a^20*b^8)$$

mupad [B] time = 0.45, size = 600, normalized size = 6.74

$$\frac{a^7 d^7 + 3a^6 b c d^6 + 10a^6 b d^7 x + 6a^5 b^2 c^2 d^5 + 30a^5 b^2 c d^6 x + 45a^5 b^2 d^7 x^2 + 10a^4 b^3 c^3 d^4 + 60a^4 b^3 c^2 d^5 x}{b^{18}x^{10} + 10a^2b^{17}x^9 + 45a^4b^{16}x^8 + 120a^6b^{15}x^7 + 210a^8b^{14}x^6 + 252a^{10}b^{13}x^5 + 210a^{12}b^{12}x^4 + 120a^{14}b^{11}x^3 + 45a^{16}b^{10}x^2 + 10a^{18}b^9x + a^{20}b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^11,x)

[Out]
$$-(a^7*d^7 + 36*b^7*c^7 + 120*b^7*d^7*x^7 + 210*a*b^6*d^7*x^6 + 630*b^7*c*d^6*x^6 + 21*a^2*b^5*c^5*d^2 + 15*a^3*b^4*c^4*d^3 + 10*a^4*b^3*c^3*d^4 + 6*a^5*b^2*c^2*d^5 + 45*a^5*b^2*d^7*x^2 + 120*a^4*b^3*d^7*x^3 + 210*a^3*b^4*d^7*x^4 + 252*a^2*b^5*d^7*x^5 + 945*b^7*c^5*d^2*x^2 + 1800*b^7*c^4*d^3*x^3 + 2100*b^7*c^3*d^4*x^4 + 1512*b^7*c^2*d^5*x^5 + 28*a*b^6*c^6*d + 3*a^6*b*c*d^6 + 10*a^6*b*d^7*x + 280*b^7*c^6*d*x + 450*a^2*b^5*c^3*d^4*x^2 + 270*a^3*b^4*c^2*d^5*x^2 + 720*a^2*b^5*c^2*d^5*x^3 + 210*a*b^6*c^5*d^2*x + 30*a^5*b^2*c*d^6*x + 756*a*b^6*c*d^6*x^5 + 150*a^2*b^5*c^4*d^3*x + 100*a^3*b^4*c^3*d^4*x + 60*a^4*b^3*c^2*d^5*x + 675*a*b^6*c^4*d^3*x^2 + 135*a^4*b^3*c*d^6*x^2 + 1200*a*b^6*c^3*d^4*x^3 + 360*a^3*b^4*c*d^6*x^3 + 1260*a*b^6*c^2*d^5*x^4 + 630*a^2*b^5*c*d^6*x^4)/(360*a^10*b^8 + 360*b^18*x^10 + 3600*a^9*b^9*x + 3600*a*b^17*x^9 + 16200*a^8*b^10*x^2 + 43200*a^7*b^11*x^3 + 75600*a^6*b^12*x^4 +$$

```
90720*a^5*b^13*x^5 + 75600*a^4*b^14*x^6 + 43200*a^3*b^15*x^7 + 16200*a^2*b^16*x^8)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**7/(b*x+a)**11,x)
```

```
[Out] Timed out
```

$$3.1294 \quad \int \frac{(c+dx)^7}{(a+bx)^{12}} dx$$

Optimal. Leaf size=120

$$\frac{d^3(c+dx)^8}{1320(a+bx)^8(bc-ad)^4} - \frac{d^2(c+dx)^8}{165(a+bx)^9(bc-ad)^3} + \frac{3d(c+dx)^8}{110(a+bx)^{10}(bc-ad)^2} - \frac{(c+dx)^8}{11(a+bx)^{11}(bc-ad)}$$

[Out] $-1/11*(d*x+c)^8/(-a*d+b*c)/(b*x+a)^{11}+3/110*d*(d*x+c)^8/(-a*d+b*c)^2/(b*x+a)^{10}-1/165*d^2*(d*x+c)^8/(-a*d+b*c)^3/(b*x+a)^9+1/1320*d^3*(d*x+c)^8/(-a*d+b*c)^4/(b*x+a)^8$

Rubi [A] time = 0.03, antiderivative size = 120, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{d^3(c+dx)^8}{1320(a+bx)^8(bc-ad)^4} - \frac{d^2(c+dx)^8}{165(a+bx)^9(bc-ad)^3} + \frac{3d(c+dx)^8}{110(a+bx)^{10}(bc-ad)^2} - \frac{(c+dx)^8}{11(a+bx)^{11}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^12, x]

[Out] $-(c+d*x)^8/(11*(b*c-a*d)*(a+b*x)^{11}) + (3*d*(c+d*x)^8)/(110*(b*c-a*d)^2*(a+b*x)^{10}) - (d^2*(c+d*x)^8)/(165*(b*c-a*d)^3*(a+b*x)^9) + (d^3*(c+d*x)^8)/(1320*(b*c-a*d)^4*(a+b*x)^8)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^7}{(a+bx)^{12}} dx &= \frac{(c+dx)^8}{11(bc-ad)(a+bx)^{11}} - \frac{(3d) \int \frac{(c+dx)^7}{(a+bx)^{11}} dx}{11(bc-ad)} \\
&= -\frac{(c+dx)^8}{11(bc-ad)(a+bx)^{11}} + \frac{3d(c+dx)^8}{110(bc-ad)^2(a+bx)^{10}} + \frac{(3d^2) \int \frac{(c+dx)^7}{(a+bx)^{10}} dx}{55(bc-ad)^2} \\
&= -\frac{(c+dx)^8}{11(bc-ad)(a+bx)^{11}} + \frac{3d(c+dx)^8}{110(bc-ad)^2(a+bx)^{10}} - \frac{d^2(c+dx)^8}{165(bc-ad)^3(a+bx)^9} - \frac{d^3 \int \frac{(c+dx)^7}{(a+bx)^9} dx}{165(bc-ad)^3} \\
&= -\frac{(c+dx)^8}{11(bc-ad)(a+bx)^{11}} + \frac{3d(c+dx)^8}{110(bc-ad)^2(a+bx)^{10}} - \frac{d^2(c+dx)^8}{165(bc-ad)^3(a+bx)^9} + \frac{d^3(c+dx)^8}{1320(bc-ad)^4}
\end{aligned}$$

Mathematica [B] time = 0.12, size = 369, normalized size = 3.08

$$\frac{a^7 d^7 + a^6 b d^6 (4c + 11dx) + a^5 b^2 d^5 (10c^2 + 44cdx + 55d^2 x^2) + 5a^4 b^3 d^4 (4c^3 + 22c^2 dx + 44cd^2 x^2 + 33d^3 x^3) + 5a^3 b^4 d^3 (7c^4 + 44c^3 dx + 110c^2 d^2 x^2 + 132cd^3 x^3 + 66d^4 x^4) + a^2 b^5 d^2 (56c^5 + 385c^4 dx + 1100c^3 d^2 x^2 + 1650c^2 d^3 x^3 + 1320cd^4 x^4 + 462d^5 x^5) + a b^6 d (84c^6 + 616c^5 dx + 1925c^4 d^2 x^2 + 3300c^3 d^3 x^3 + 3300c^2 d^4 x^4 + 1848cd^5 x^5 + 462d^6 x^6) + b^7 (120c^7 + 924c^6 dx + 3080c^5 d^2 x^2 + 5775c^4 d^3 x^3 + 6600c^3 d^4 x^4 + 4620c^2 d^5 x^5 + 1848cd^6 x^6 + 330d^7 x^7)}{(b^8 (a + bx)^{11})}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^12,x]

[Out] -1/1320*(a^7*d^7 + a^6*b*d^6*(4*c + 11*d*x) + a^5*b^2*d^5*(10*c^2 + 44*c*d*x + 55*d^2*x^2) + 5*a^4*b^3*d^4*(4*c^3 + 22*c^2*d*x + 44*c*d^2*x^2 + 33*d^3*x^3) + 5*a^3*b^4*d^3*(7*c^4 + 44*c^3*d*x + 110*c^2*d^2*x^2 + 132*c*d^3*x^3 + 66*d^4*x^4) + a^2*b^5*d^2*(56*c^5 + 385*c^4*d*x + 1100*c^3*d^2*x^2 + 1650*c^2*d^3*x^3 + 1320*c*d^4*x^4 + 462*d^5*x^5) + a*b^6*d*(84*c^6 + 616*c^5*d*x + 1925*c^4*d^2*x^2 + 3300*c^3*d^3*x^3 + 3300*c^2*d^4*x^4 + 1848*c*d^5*x^5 + 462*d^6*x^6) + b^7*(120*c^7 + 924*c^6*d*x + 3080*c^5*d^2*x^2 + 5775*c^4*d^3*x^3 + 6600*c^3*d^4*x^4 + 4620*c^2*d^5*x^5 + 1848*c*d^6*x^6 + 330*d^7*x^7))/(b^8*(a + b*x)^11)

fricas [B] time = 0.46, size = 570, normalized size = 4.75

$$\frac{330 b^7 d^7 x^7 + 120 b^7 c^7 + 84 a b^6 c^6 d + 56 a^2 b^5 c^5 d^2 + 35 a^3 b^4 c^4 d^3 + 20 a^4 b^3 c^3 d^4 + 10 a^5 b^2 c^2 d^5 + 4 a^6 b c d^6 + a^7 d^7}{b^8 (a + b x)^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^12,x, algorithm="fricas")

[Out] -1/1320*(330*b^7*d^7*x^7 + 120*b^7*c^7 + 84*a*b^6*c^6*d + 56*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 + 20*a^4*b^3*c^3*d^4 + 10*a^5*b^2*c^2*d^5 + 4*a^6*b*c*d^6 + a^7*d^7)/(b^8*(a + b*x)^11)

$$c*d^6 + a^7*d^7 + 462*(4*b^7*c*d^6 + a*b^6*d^7)*x^6 + 462*(10*b^7*c^2*d^5 + 4*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 330*(20*b^7*c^3*d^4 + 10*a*b^6*c^2*d^5 + 4*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 165*(35*b^7*c^4*d^3 + 20*a*b^6*c^3*d^4 + 10*a^2*b^5*c^2*d^5 + 4*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 55*(56*b^7*c^5*d^2 + 35*a*b^6*c^4*d^3 + 20*a^2*b^5*c^3*d^4 + 10*a^3*b^4*c^2*d^5 + 4*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 11*(84*b^7*c^6*d + 56*a*b^6*c^5*d^2 + 35*a^2*b^5*c^4*d^3 + 20*a^3*b^4*c^3*d^4 + 10*a^4*b^3*c^2*d^5 + 4*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^19*x^11 + 11*a*b^18*x^10 + 55*a^2*b^17*x^9 + 165*a^3*b^16*x^8 + 330*a^4*b^15*x^7 + 462*a^5*b^14*x^6 + 462*a^6*b^13*x^5 + 330*a^7*b^12*x^4 + 165*a^8*b^11*x^3 + 55*a^9*b^10*x^2 + 11*a^10*b^9*x + a^11*b^8)$$

giac [B] time = 1.30, size = 496, normalized size = 4.13

$$\frac{330 b^7 d^7 x^7 + 1848 b^7 c d^6 x^6 + 462 a b^6 d^7 x^6 + 4620 b^7 c^2 d^5 x^5 + 1848 a b^6 c d^6 x^5 + 462 a^2 b^5 d^7 x^5 + 6600 b^7 c^3 d^4 x^4 + \dots}{(b^{19} x^{11} + 11 a b^{18} x^{10} + 55 a^2 b^{17} x^9 + 165 a^3 b^{16} x^8 + 330 a^4 b^{15} x^7 + 462 a^5 b^{14} x^6 + 462 a^6 b^{13} x^5 + 330 a^7 b^{12} x^4 + 165 a^8 b^{11} x^3 + 55 a^9 b^{10} x^2 + 11 a^{10} b^9 x + a^{11} b^8)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^12,x, algorithm="giac")

[Out]
$$-1/1320*(330*b^7*d^7*x^7 + 1848*b^7*c*d^6*x^6 + 462*a*b^6*d^7*x^6 + 4620*b^7*c^2*d^5*x^5 + 1848*a*b^6*c*d^6*x^5 + 462*a^2*b^5*d^7*x^5 + 6600*b^7*c^3*d^4*x^4 + 3300*a*b^6*c^2*d^5*x^4 + 1320*a^2*b^5*c*d^6*x^4 + 330*a^3*b^4*d^7*x^4 + 5775*b^7*c^4*d^3*x^3 + 3300*a*b^6*c^3*d^4*x^3 + 1650*a^2*b^5*c^2*d^5*x^3 + 660*a^3*b^4*c*d^6*x^3 + 165*a^4*b^3*d^7*x^3 + 3080*b^7*c^5*d^2*x^2 + 1925*a*b^6*c^4*d^3*x^2 + 1100*a^2*b^5*c^3*d^4*x^2 + 550*a^3*b^4*c^2*d^5*x^2 + 220*a^4*b^3*c*d^6*x^2 + 55*a^5*b^2*d^7*x^2 + 924*b^7*c^6*d*x + 616*a*b^6*c^5*d^2*x + 385*a^2*b^5*c^4*d^3*x + 220*a^3*b^4*c^3*d^4*x + 110*a^4*b^3*c^2*d^5*x + 44*a^5*b^2*c*d^6*x + 11*a^6*b*d^7*x + 120*b^7*c^7 + 84*a*b^6*c^6*d + 56*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 + 20*a^4*b^3*c^3*d^4 + 10*a^5*b^2*c^2*d^5 + 4*a^6*b*c*d^6 + a^7*d^7)/(b*x + a)^11*b^8)$$

maple [B] time = 0.00, size = 464, normalized size = 3.87

$$\frac{d^7}{4(bx+a)^4 b^8} + \frac{7(ad-bc)d^6}{5(bx+a)^5 b^8} - \frac{7(a^2d^2-2abcd+b^2c^2)d^5}{2(bx+a)^6 b^8} + \frac{5(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^4}{(bx+a)^7 b^8} - \frac{35(a^4d^4)}{(bx+a)^8 b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^12,x)

[Out]
$$-35/8*d^3*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/b^8/(b*x+a)^8+5*d^4*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^8/(b*x+a)^7+7/3*d^2*(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)/b^8/(b*x+a)^9+7/5*d^6*(a*d-b*c)/b^8/(b*x+a)^5-1/4*d^7/b^8/(b*x+a)^4-1/11*(-a^7*d^7+7*a^6*b*c*d^6-21*a^5*b^2*c^2*d^5+35*a^4*b^3*c^2*d^4-42*a^3*b^4*c^3*d^3+35*a^2*b^5*c^4*d^2-21*a*b^6*c^5*d+b^7*c^6)$$

$$3*d^4-35*a^3*b^4*c^4*d^3+21*a^2*b^5*c^5*d^2-7*a*b^6*c^6*d+b^7*c^7)/b^8/(b*x+a)^{11-7/2*d^5*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^8/(b*x+a)^6-7/10*d*(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^8/(b*x+a)^{10}}$$

maxima [B] time = 1.81, size = 570, normalized size = 4.75

$$330 b^7 d^7 x^7 + 120 b^7 c^7 + 84 a b^6 c^6 d + 56 a^2 b^5 c^5 d^2 + 35 a^3 b^4 c^4 d^3 + 20 a^4 b^3 c^3 d^4 + 10 a^5 b^2 c^2 d^5 + 4 a^6 b c d^6 + a^7 d^7 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^12,x, algorithm="maxima")

[Out]
$$-1/1320*(330*b^7*d^7*x^7 + 120*b^7*c^7 + 84*a*b^6*c^6*d + 56*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 + 20*a^4*b^3*c^3*d^4 + 10*a^5*b^2*c^2*d^5 + 4*a^6*b*c*d^6 + a^7*d^7 + 462*(4*b^7*c*d^6 + a*b^6*d^7)*x^6 + 462*(10*b^7*c^2*d^5 + 4*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 330*(20*b^7*c^3*d^4 + 10*a*b^6*c^2*d^5 + 4*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 165*(35*b^7*c^4*d^3 + 20*a*b^6*c^3*d^4 + 10*a^2*b^5*c^2*d^5 + 4*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 55*(56*b^7*c^5*d^2 + 35*a*b^6*c^4*d^3 + 20*a^2*b^5*c^3*d^4 + 10*a^3*b^4*c^2*d^5 + 4*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 11*(84*b^7*c^6*d + 56*a*b^6*c^5*d^2 + 35*a^2*b^5*c^4*d^3 + 20*a^3*b^4*c^3*d^4 + 10*a^4*b^3*c^2*d^5 + 4*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^19*x^11 + 11*a*b^18*x^10 + 55*a^2*b^17*x^9 + 165*a^3*b^16*x^8 + 330*a^4*b^15*x^7 + 462*a^5*b^14*x^6 + 462*a^6*b^13*x^5 + 330*a^7*b^12*x^4 + 165*a^8*b^11*x^3 + 55*a^9*b^10*x^2 + 11*a^10*b^9*x + a^11*b^8)$$

mupad [B] time = 0.52, size = 548, normalized size = 4.57

$$\frac{a^7 d^7 + 4 a^6 b c d^6 + 10 a^5 b^2 c^2 d^5 + 20 a^4 b^3 c^3 d^4 + 35 a^3 b^4 c^4 d^3 + 56 a^2 b^5 c^5 d^2 + 84 a b^6 c^6 d + 120 b^7 c^7}{1320 b^8} + \frac{d^7 x^7}{4 b} + \frac{d^2 x^2 (a^5 d^5 + 4 a^4 b c d^4 + 10 a^3 b^2 c^2 d^3 + 20 a^2 b^3 c^3 d^2 + 10 a b^4 c^4 d + 4 a^4 b^3 c^4 d^3 + 20 a^3 b^2 c^2 d^5 + 84 a^2 b^5 c^5 d^2 + 4 a^6 b^3 c^3 d^4 + 10 a^5 b^2 c^2 d^5 + 4 a^4 b^3 c^3 d^4 + 10 a^3 b^4 c^2 d^5 + 4 a^2 b^5 c^2 d^5 + 4 a^3 b^4 c^2 d^5 + 4 a^4 b^3 c^2 d^5 + 4 a^5 b^2 c^2 d^5 + 4 a^6 b^3 c^2 d^5 + 4 a^7 b^4 c^2 d^5 + 4 a^8 b^5 c^2 d^5 + 4 a^9 b^6 c^2 d^5 + 4 a^{10} b^7 c^2 d^5 + 4 a^{11} b^8 c^2 d^5)}{a^{11} + 11 a^{10} b x + 55 a^9 b^2 x^2 + 165 a^8 b^3 x^3 + 330 a^7 b^4 x^4 + 462 a^6 b^5 x^5 + 462 a^5 b^6 x^6 + 330 a^4 b^7 x^7 + 165 a^3 b^8 x^8 + 55 a^2 b^9 x^9 + 11 a b^{10} x^{10} + a^{11} b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^12,x)

[Out]
$$-((a^7*d^7 + 120*b^7*c^7 + 56*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 + 20*a^4*b^3*c^3*d^4 + 10*a^5*b^2*c^2*d^5 + 84*a*b^6*c^6*d + 4*a^6*b*c*d^6)/(1320*b^8) + (d^7*x^7)/(4*b) + (d^2*x^2*(a^5*d^5 + 56*b^5*c^5 + 20*a^2*b^3*c^3*d^2 + 10*a^3*b^2*c^2*d^3 + 35*a*b^4*c^4*d + 4*a^4*b^3*c^4*d^3 + 10*a^5*b^2*c^2*d^5 + 4*a^6*b^3*c^2*d^5 + 4*a^7*b^4*c^2*d^5 + 4*a^8*b^5*c^2*d^5 + 4*a^9*b^6*c^2*d^5 + 4*a^{10}b^7*c^2*d^5 + 4*a^{11}b^8*c^2*d^5))/(24*b^6) + (d^4*x^4*(a^3*d^3 + 20*b^3*c^3 + 10*a*b^2*c^2*d + 4*a^2*b*c*d^2))/(4*b^4) + (7*d^6*x^6*(a*d + 4*b*c))/(20*b^2) + (d^3*x^3*(a^4*d^4 + 35*b^4*c^4 + 10*a^2*b^2*c^2*d^2 + 20*a*b^3*c^3*d + 4*a^3*b^2*c^3*d^3))/(8*b^5) + (d*x*(a^6*d^6 + 84*b^6*c^6 + 35*a^2*b^4*c^4*d^2 + 20*a^3*b^3*c^3*d^3 + 10*a^4*b^2*c^2*d^4 + 56*a^5*b^5*c^5*d + 4*a^6*b^6*c^6*d^6))/(120*b^7) + (7*d^5*x^5*(a^2*d^2 + 10*b^2*c^2 +$$


```
4*a*b*c*d)/(20*b^3))/(a^11 + b^11*x^11 + 11*a*b^10*x^10 + 55*a^9*b^2*x^2 +  
165*a^8*b^3*x^3 + 330*a^7*b^4*x^4 + 462*a^6*b^5*x^5 + 462*a^5*b^6*x^6 + 33  
0*a^4*b^7*x^7 + 165*a^3*b^8*x^8 + 55*a^2*b^9*x^9 + 11*a^10*b*x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**7/(b*x+a)**12,x)
```

```
[Out] Timed out
```

3.1295

$$\int \frac{(c+dx)^7}{(a+bx)^{13}} dx$$

Optimal. Leaf size=151

$$-\frac{d^4(c+dx)^8}{3960(a+bx)^8(bc-ad)^5} + \frac{d^3(c+dx)^8}{495(a+bx)^9(bc-ad)^4} - \frac{d^2(c+dx)^8}{110(a+bx)^{10}(bc-ad)^3} + \frac{d(c+dx)^8}{33(a+bx)^{11}(bc-ad)^2} - \frac{(c+dx)^8}{12(a+bx)}$$

[Out] $-1/12*(d*x+c)^8/(-a*d+b*c)/(b*x+a)^{12}+1/33*d*(d*x+c)^8/(-a*d+b*c)^2/(b*x+a)^{11}-1/110*d^2*(d*x+c)^8/(-a*d+b*c)^3/(b*x+a)^{10}+1/495*d^3*(d*x+c)^8/(-a*d+b*c)^4/(b*x+a)^9-1/3960*d^4*(d*x+c)^8/(-a*d+b*c)^5/(b*x+a)^8$

Rubi [A] time = 0.05, antiderivative size = 151, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{d^4(c+dx)^8}{3960(a+bx)^8(bc-ad)^5} + \frac{d^3(c+dx)^8}{495(a+bx)^9(bc-ad)^4} - \frac{d^2(c+dx)^8}{110(a+bx)^{10}(bc-ad)^3} + \frac{d(c+dx)^8}{33(a+bx)^{11}(bc-ad)^2} - \frac{(c+dx)^8}{12(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^13, x]

[Out] $-(c+d*x)^8/(12*(b*c-a*d)*(a+b*x)^{12}) + (d*(c+d*x)^8)/(33*(b*c-a*d)^2*(a+b*x)^{11}) - (d^2*(c+d*x)^8)/(110*(b*c-a*d)^3*(a+b*x)^{10}) + (d^3*(c+d*x)^8)/(495*(b*c-a*d)^4*(a+b*x)^9) - (d^4*(c+d*x)^8)/(3960*(b*c-a*d)^5*(a+b*x)^8)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^7}{(a+bx)^{13}} dx &= -\frac{(c+dx)^8}{12(bc-ad)(a+bx)^{12}} - \frac{d \int \frac{(c+dx)^7}{(a+bx)^{12}} dx}{3(bc-ad)} \\
&= -\frac{(c+dx)^8}{12(bc-ad)(a+bx)^{12}} + \frac{d(c+dx)^8}{33(bc-ad)^2(a+bx)^{11}} + \frac{d^2 \int \frac{(c+dx)^7}{(a+bx)^{11}} dx}{11(bc-ad)^2} \\
&= -\frac{(c+dx)^8}{12(bc-ad)(a+bx)^{12}} + \frac{d(c+dx)^8}{33(bc-ad)^2(a+bx)^{11}} - \frac{d^2(c+dx)^8}{110(bc-ad)^3(a+bx)^{10}} - \frac{d^3 \int \frac{(c+dx)^7}{(a+bx)^{10}} dx}{55(bc-ad)^3} \\
&= -\frac{(c+dx)^8}{12(bc-ad)(a+bx)^{12}} + \frac{d(c+dx)^8}{33(bc-ad)^2(a+bx)^{11}} - \frac{d^2(c+dx)^8}{110(bc-ad)^3(a+bx)^{10}} + \frac{d^3(c+dx)^8}{495(bc-ad)^4} \\
&= -\frac{(c+dx)^8}{12(bc-ad)(a+bx)^{12}} + \frac{d(c+dx)^8}{33(bc-ad)^2(a+bx)^{11}} - \frac{d^2(c+dx)^8}{110(bc-ad)^3(a+bx)^{10}} + \frac{d^3(c+dx)^8}{495(bc-ad)^4}
\end{aligned}$$

Mathematica [B] time = 0.13, size = 371, normalized size = 2.46

$$\frac{a^7 d^7 + a^6 b d^6 (5c + 12dx) + 3a^5 b^2 d^5 (5c^2 + 20cdx + 22d^2 x^2) + 5a^4 b^3 d^4 (7c^3 + 36c^2 dx + 66cd^2 x^2 + 44d^3 x^3) + 5a^3 b^4 d^3 (14c^4 + 84c^3 dx + 198c^2 d^2 x^2 + 220c d^3 x^3 + 99d^4 x^4) + 3a^2 b^5 d^2 (42c^5 + 280c^4 dx + 770c^3 d^2 x^2 + 1100c^2 d^3 x^3 + 825c d^4 x^4 + 264d^5 x^5) + a b^6 d (210c^6 + 1512c^5 dx + 4620c^4 d^2 x^2 + 7700c^3 d^3 x^3 + 7425c^2 d^4 x^4 + 3960c d^5 x^5 + 924d^6 x^6) + b^7 (330c^7 + 2520c^6 dx + 8316c^5 d^2 x^2 + 15400c^4 d^3 x^3 + 17325c^3 d^4 x^4 + 11880c^2 d^5 x^5 + 4620c d^6 x^6 + 792d^7 x^7)}{(b^8 (a + bx)^{12})}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^13,x]

[Out] -1/3960*(a^7*d^7 + a^6*b*d^6*(5*c + 12*d*x) + 3*a^5*b^2*d^5*(5*c^2 + 20*c*d*x + 22*d^2*x^2) + 5*a^4*b^3*d^4*(7*c^3 + 36*c^2*d*x + 66*c*d^2*x^2 + 44*d^3*x^3) + 5*a^3*b^4*d^3*(14*c^4 + 84*c^3*d*x + 198*c^2*d^2*x^2 + 220*c*d^3*x^3 + 99*d^4*x^4) + 3*a^2*b^5*d^2*(42*c^5 + 280*c^4*d*x + 770*c^3*d^2*x^2 + 1100*c^2*d^3*x^3 + 825*c*d^4*x^4 + 264*d^5*x^5) + a*b^6*d*(210*c^6 + 1512*c^5*d*x + 4620*c^4*d^2*x^2 + 7700*c^3*d^3*x^3 + 7425*c^2*d^4*x^4 + 3960*c*d^5*x^5 + 924*d^6*x^6) + b^7*(330*c^7 + 2520*c^6*d*x + 8316*c^5*d^2*x^2 + 15400*c^4*d^3*x^3 + 17325*c^3*d^4*x^4 + 11880*c^2*d^5*x^5 + 4620*c*d^6*x^6 + 792*d^7*x^7))/(b^8*(a + b*x)^12)

fricas [B] time = 0.44, size = 581, normalized size = 3.85

$$\frac{792 b^7 d^7 x^7 + 330 b^7 c^7 + 210 a b^6 c^6 d + 126 a^2 b^5 c^5 d^2 + 70 a^3 b^4 c^4 d^3 + 35 a^4 b^3 c^3 d^4 + 15 a^5 b^2 c^2 d^5 + 5 a^6 b c d^6 + a^7}{b^8 (a + b x)^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^13,x, algorithm="fricas")

[Out]
$$\frac{-1/3960*(792*b^7*d^7*x^7 + 330*b^7*c^7 + 210*a*b^6*c^6*d + 126*a^2*b^5*c^5*d^2 + 70*a^3*b^4*c^4*d^3 + 35*a^4*b^3*c^3*d^4 + 15*a^5*b^2*c^2*d^5 + 5*a^6*b*c*d^6 + a^7*d^7 + 924*(5*b^7*c*d^6 + a*b^6*d^7)*x^6 + 792*(15*b^7*c^2*d^5 + 5*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 495*(35*b^7*c^3*d^4 + 15*a*b^6*c^2*d^5 + 5*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 220*(70*b^7*c^4*d^3 + 35*a*b^6*c^3*d^4 + 15*a^2*b^5*c^2*d^5 + 5*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 66*(126*b^7*c^5*d^2 + 70*a*b^6*c^4*d^3 + 35*a^2*b^5*c^3*d^4 + 15*a^3*b^4*c^2*d^5 + 5*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 12*(210*b^7*c^6*d + 126*a*b^6*c^5*d^2 + 70*a^2*b^5*c^4*d^3 + 35*a^3*b^4*c^3*d^4 + 15*a^4*b^3*c^2*d^5 + 5*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^20*x^12 + 12*a*b^19*x^11 + 66*a^2*b^18*x^10 + 220*a^3*b^17*x^9 + 495*a^4*b^16*x^8 + 792*a^5*b^15*x^7 + 924*a^6*b^14*x^6 + 792*a^7*b^13*x^5 + 495*a^8*b^12*x^4 + 220*a^9*b^11*x^3 + 66*a^10*b^10*x^2 + 12*a^11*b^9*x + a^12*b^8)$$

giac [B] time = 1.26, size = 496, normalized size = 3.28

$$\frac{792 b^7 d^7 x^7 + 4620 b^7 c d^6 x^6 + 924 a b^6 d^7 x^6 + 11880 b^7 c^2 d^5 x^5 + 3960 a b^6 c d^6 x^5 + 792 a^2 b^5 d^7 x^5 + 17325 b^7 c^3 d^4 x^4}{b^{20} x^{12} + 12 a b^{19} x^{11} + 66 a^2 b^{18} x^{10} + 220 a^3 b^{17} x^9 + 495 a^4 b^{16} x^8 + 792 a^5 b^{15} x^7 + 924 a^6 b^{14} x^6 + 792 a^7 b^{13} x^5 + 495 a^8 b^{12} x^4 + 220 a^9 b^{11} x^3 + 66 a^{10} b^{10} x^2 + 12 a^{11} b^9 x + a^{12} b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^13,x, algorithm="giac")

[Out]
$$\frac{-1/3960*(792*b^7*d^7*x^7 + 4620*b^7*c*d^6*x^6 + 924*a*b^6*d^7*x^6 + 11880*b^7*c^2*d^5*x^5 + 3960*a*b^6*c*d^6*x^5 + 792*a^2*b^5*d^7*x^5 + 17325*b^7*c^3*d^4*x^4 + 7425*a*b^6*c^2*d^5*x^4 + 2475*a^2*b^5*c*d^6*x^4 + 495*a^3*b^4*d^7*x^4 + 15400*b^7*c^4*d^3*x^3 + 7700*a*b^6*c^3*d^4*x^3 + 3300*a^2*b^5*c^2*d^5*x^3 + 1100*a^3*b^4*c*d^6*x^3 + 220*a^4*b^3*d^7*x^3 + 8316*b^7*c^5*d^2*x^2 + 4620*a*b^6*c^4*d^3*x^2 + 2310*a^2*b^5*c^3*d^4*x^2 + 990*a^3*b^4*c^2*d^5*x^2 + 330*a^4*b^3*c*d^6*x^2 + 66*a^5*b^2*d^7*x^2 + 2520*b^7*c^6*d*x + 1512*a*b^6*c^5*d^2*x + 840*a^2*b^5*c^4*d^3*x + 420*a^3*b^4*c^3*d^4*x + 180*a^4*b^3*c^2*d^5*x + 60*a^5*b^2*c*d^6*x + 12*a^6*b*d^7*x + 330*b^7*c^7 + 210*a*b^6*c^6*d + 126*a^2*b^5*c^5*d^2 + 70*a^3*b^4*c^4*d^3 + 35*a^4*b^3*c^3*d^4 + 15*a^5*b^2*c^2*d^5 + 5*a^6*b*c*d^6 + a^7*d^7)/((b*x + a)^12*b^8)$$

maple [B] time = 0.01, size = 464, normalized size = 3.07

$$\frac{d^7}{5(bx+a)^5 b^8} + \frac{7(ad-bc)d^6}{6(bx+a)^6 b^8} - \frac{3(a^2 d^2 - 2abcd + b^2 c^2)d^5}{(bx+a)^7 b^8} + \frac{35(a^3 d^3 - 3a^2 bc d^2 + 3a b^2 c^2 d - b^3 c^3)d^4}{8(bx+a)^8 b^8} - \frac{35(a^4 d^4)}{8(bx+a)^8 b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^13,x)

[Out]
$$\frac{35}{8}d^4*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^8/(b*x+a)^8-3*d^5*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^8/(b*x+a)^7-35/9*d^3*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-3*a*b^3*c^3*d-b^4*c^4)/b^8/(b*x+a)^6$$

$$\frac{a^2 b^2 c^2 d^2 - 4 a^3 b^3 c^3 d + b^4 c^4}{b^8 (b x + a)^9} - \frac{1}{5} \frac{d^7}{b^8 (b x + a)^5} - \frac{7}{11} \frac{d^6 (a^6 d^6 - 6 a^5 b^3 c^3 d^5 + 15 a^4 b^2 c^2 d^4 - 20 a^3 b^3 c^3 d^3 + 15 a^2 b^4 c^4 d^2 - 6 a^5 b^5 c^5 d + b^6 c^6)}{b^8 (b x + a)^{11}} - \frac{1}{12} \frac{(-a^7 d^7 + 7 a^6 b^3 c^3 d^6 - 21 a^5 b^2 c^2 d^5 + 35 a^4 b^3 c^3 d^4 - 35 a^3 b^4 c^4 d^3 + 21 a^2 b^5 c^5 d^2 - 7 a^5 b^6 c^6 d + b^7 c^7)}{b^8 (b x + a)^{12}} + \frac{7}{6} \frac{d^6 (a d - b c)}{b^8 (b x + a)^6} + \frac{21}{10} \frac{d^2 (a^5 d^5 - 5 a^4 b^3 c^3 d^4 + 10 a^3 b^2 c^2 d^3 - 10 a^2 b^3 c^3 d^2 + 5 a^4 b^4 c^4 d - b^5 c^5)}{b^8 (b x + a)^{10}}$$

maxima [B] time = 1.76, size = 581, normalized size = 3.85

$$792 b^7 d^7 x^7 + 330 b^7 c^7 + 210 a b^6 c^6 d + 126 a^2 b^5 c^5 d^2 + 70 a^3 b^4 c^4 d^3 + 35 a^4 b^3 c^3 d^4 + 15 a^5 b^2 c^2 d^5 + 5 a^6 b c d^6 + a^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^13,x, algorithm="maxima")

[Out]
$$\frac{-1/3960*(792*b^7*d^7*x^7 + 330*b^7*c^7 + 210*a*b^6*c^6*d + 126*a^2*b^5*c^5*d^2 + 70*a^3*b^4*c^4*d^3 + 35*a^4*b^3*c^3*d^4 + 15*a^5*b^2*c^2*d^5 + 5*a^6*b*c*d^6 + a^7*d^7 + 924*(5*b^7*c*d^6 + a*b^6*d^7)*x^6 + 792*(15*b^7*c^2*d^5 + 5*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 495*(35*b^7*c^3*d^4 + 15*a*b^6*c^2*d^5 + 5*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 220*(70*b^7*c^4*d^3 + 35*a*b^6*c^3*d^4 + 15*a^2*b^5*c^2*d^5 + 5*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 66*(126*b^7*c^5*d^2 + 70*a*b^6*c^4*d^3 + 35*a^2*b^5*c^3*d^4 + 15*a^3*b^4*c^2*d^5 + 5*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 12*(210*b^7*c^6*d + 126*a*b^6*c^5*d^2 + 70*a^2*b^5*c^4*d^3 + 35*a^3*b^4*c^3*d^4 + 15*a^4*b^3*c^2*d^5 + 5*a^5*b^2*c*d^6 + a^6*b*d^7)*x}{(b^20*x^12 + 12*a*b^19*x^11 + 66*a^2*b^18*x^10 + 220*a^3*b^17*x^9 + 495*a^4*b^16*x^8 + 792*a^5*b^15*x^7 + 924*a^6*b^14*x^6 + 792*a^7*b^13*x^5 + 495*a^8*b^12*x^4 + 220*a^9*b^11*x^3 + 66*a^10*b^10*x^2 + 12*a^11*b^9*x + a^12*b^8)}$$

mupad [B] time = 0.23, size = 559, normalized size = 3.70

$$\frac{a^7 d^7 + 5 a^6 b c d^6 + 15 a^5 b^2 c^2 d^5 + 35 a^4 b^3 c^3 d^4 + 70 a^3 b^4 c^4 d^3 + 126 a^2 b^5 c^5 d^2 + 210 a b^6 c^6 d + 330 b^7 c^7}{3960 b^8} + \frac{d^7 x^7}{5 b} + \frac{d^2 x^2 (a^5 d^5 + 5 a^4 b c d^4 + 15 a^3 b^2 c^2 d^3 + 15 a^2 b^3 c^3 d^2 + 15 a^3 b^2 c^2 d^3 + 70 a^4 b^3 c^3 d^2 + 15 a^5 b^4 c^4 d + 5 a^6 b^5 c^5 d^2)}{(60 b^6) + (d^4 x^4 (a^3 d^3 + 35 b^3 c^3 + 15 a^4 b^2 c^2 d + 5 a^5 b^3 c^3 d^2))}{(8 b^4) + (7 a^{12} + 12 a^{11} b x + 66 a^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^13,x)

[Out]
$$-\frac{(a^7 d^7 + 330 b^7 c^7 + 126 a^2 b^5 c^5 d^2 + 70 a^3 b^4 c^4 d^3 + 35 a^4 b^3 c^3 d^4 + 15 a^5 b^2 c^2 d^5 + 210 a^6 b^3 c^3 d^4 + 5 a^6 b^4 c^4 d^3 + 5 a^6 b^5 c^5 d^2 + 5 a^6 b^6 c^6 d + 5 a^6 b^7 c^7)}{(3960 b^8) + (d^7 x^7)/(5 b) + (d^2 x^2 (a^5 d^5 + 126 b^5 c^5 + 35 a^2 b^3 c^3 d^2 + 15 a^3 b^2 c^2 d^3 + 70 a^4 b^3 c^3 d^2 + 15 a^5 b^4 c^4 d + 5 a^6 b^5 c^5 d^2))}{(60 b^6) + (d^4 x^4 (a^3 d^3 + 35 b^3 c^3 + 15 a^4 b^2 c^2 d + 5 a^5 b^3 c^3 d^2))}{(8 b^4) + (7$$

$$\begin{aligned} & d^6 x^6 (a d + 5 b c) / (30 b^2) + (d^3 x^3 (a^4 d^4 + 70 b^4 c^4 + 15 a^2 b^2 c^2 d^2 + 35 a b^3 c^3 d + 5 a^3 b c d^3)) / (18 b^5) + (d x (a^6 d^6 + 210 b^6 c^6 + 70 a^2 b^4 c^4 d^2 + 35 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 + 126 a b^5 c^5 d + 5 a^5 b c d^5)) / (330 b^7) + (d^5 x^5 (a^2 d^2 + 15 b^2 c^2 + 5 a b c d)) / (5 b^3) / (a^{12} + b^{12} x^{12} + 12 a b^{11} x^{11} + 66 a^{10} b^2 x^2 + 220 a^9 b^3 x^3 + 495 a^8 b^4 x^4 + 792 a^7 b^5 x^5 + 924 a^6 b^6 x^6 + 792 a^5 b^7 x^7 + 495 a^4 b^8 x^8 + 220 a^3 b^9 x^9 + 66 a^2 b^{10} x^{10} + 12 a^{11} b x) \end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**13,x)

[Out] Timed out

$$3.1296 \quad \int \frac{(c+dx)^7}{(a+bx)^{14}} dx$$

Optimal. Leaf size=198

$$\frac{d^6(bc-ad)}{b^8(a+bx)^7} - \frac{21d^5(bc-ad)^2}{8b^8(a+bx)^8} - \frac{35d^4(bc-ad)^3}{9b^8(a+bx)^9} - \frac{7d^3(bc-ad)^4}{2b^8(a+bx)^{10}} - \frac{21d^2(bc-ad)^5}{11b^8(a+bx)^{11}} - \frac{7d(bc-ad)^6}{12b^8(a+bx)^{12}} - \frac{(bc-ad)^7}{13b^8(a+bx)^{13}}$$

[Out] $-1/13*(-a*d+b*c)^7/b^8/(b*x+a)^{13}-7/12*d*(-a*d+b*c)^6/b^8/(b*x+a)^{12}-21/11*d^2*(-a*d+b*c)^5/b^8/(b*x+a)^{11}-7/2*d^3*(-a*d+b*c)^4/b^8/(b*x+a)^{10}-35/9*d^4*(-a*d+b*c)^3/b^8/(b*x+a)^9-21/8*d^5*(-a*d+b*c)^2/b^8/(b*x+a)^8-d^6*(-a*d+b*c)/b^8/(b*x+a)^7-1/6*d^7/b^8/(b*x+a)^6$

Rubi [A] time = 0.15, antiderivative size = 198, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{d^6(bc-ad)}{b^8(a+bx)^7} - \frac{21d^5(bc-ad)^2}{8b^8(a+bx)^8} - \frac{35d^4(bc-ad)^3}{9b^8(a+bx)^9} - \frac{7d^3(bc-ad)^4}{2b^8(a+bx)^{10}} - \frac{21d^2(bc-ad)^5}{11b^8(a+bx)^{11}} - \frac{7d(bc-ad)^6}{12b^8(a+bx)^{12}} - \frac{(bc-ad)^7}{13b^8(a+bx)^{13}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^14, x]

[Out] $-(b*c - a*d)^7/(13*b^8*(a + b*x)^{13}) - (7*d*(b*c - a*d)^6)/(12*b^8*(a + b*x)^{12}) - (21*d^2*(b*c - a*d)^5)/(11*b^8*(a + b*x)^{11}) - (7*d^3*(b*c - a*d)^4)/(2*b^8*(a + b*x)^{10}) - (35*d^4*(b*c - a*d)^3)/(9*b^8*(a + b*x)^9) - (21*d^5*(b*c - a*d)^2)/(8*b^8*(a + b*x)^8) - (d^6*(b*c - a*d))/(b^8*(a + b*x)^7) - d^7/(6*b^8*(a + b*x)^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^{14}} dx = \int \left(\frac{(bc-ad)^7}{b^7(a+bx)^{14}} + \frac{7d(bc-ad)^6}{b^7(a+bx)^{13}} + \frac{21d^2(bc-ad)^5}{b^7(a+bx)^{12}} + \frac{35d^3(bc-ad)^4}{b^7(a+bx)^{11}} + \frac{35d^4(bc-ad)^3}{b^7(a+bx)^{10}} + \frac{21d^5(bc-ad)^2}{b^7(a+bx)^9} + \frac{7d^6(bc-ad)}{b^7(a+bx)^8} + \frac{d^7}{b^7(a+bx)^7} \right) dx$$

$$= -\frac{(bc-ad)^7}{13b^8(a+bx)^{13}} - \frac{7d(bc-ad)^6}{12b^8(a+bx)^{12}} - \frac{21d^2(bc-ad)^5}{11b^8(a+bx)^{11}} - \frac{7d^3(bc-ad)^4}{2b^8(a+bx)^{10}} - \frac{35d^4(bc-ad)^3}{9b^8(a+bx)^9} - \frac{21d^5(bc-ad)^2}{8b^8(a+bx)^8} - \frac{7d^6(bc-ad)}{b^8(a+bx)^7} - \frac{d^7}{6b^8(a+bx)^6}$$

Mathematica [A] time = 0.13, size = 369, normalized size = 1.86

$$\frac{a^7 d^7 + a^6 b d^6 (6c + 13dx) + 3a^5 b^2 d^5 (7c^2 + 26cdx + 26d^2 x^2) + a^4 b^3 d^4 (56c^3 + 273c^2 dx + 468cd^2 x^2 + 286d^3 x^3) - \dots}{\dots}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^14,x]

[Out]
$$-1/10296*(a^7*d^7 + a^6*b*d^6*(6*c + 13*d*x) + 3*a^5*b^2*d^5*(7*c^2 + 26*c*d*x + 26*d^2*x^2) + a^4*b^3*d^4*(56*c^3 + 273*c^2*d*x + 468*c*d^2*x^2 + 286*d^3*x^3) + a^3*b^4*d^3*(126*c^4 + 728*c^3*d*x + 1638*c^2*d^2*x^2 + 1716*c*d^3*x^3 + 715*d^4*x^4) + 3*a^2*b^5*d^2*(84*c^5 + 546*c^4*d*x + 1456*c^3*d^2*x^2 + 2002*c^2*d^3*x^3 + 1430*c*d^4*x^4 + 429*d^5*x^5) + a*b^6*d*(462*c^6 + 3276*c^5*d*x + 9828*c^4*d^2*x^2 + 16016*c^3*d^3*x^3 + 15015*c^2*d^4*x^4 + 7722*c*d^5*x^5 + 1716*d^6*x^6) + b^7*(792*c^7 + 6006*c^6*d*x + 19656*c^5*d^2*x^2 + 36036*c^4*d^3*x^3 + 40040*c^3*d^4*x^4 + 27027*c^2*d^5*x^5 + 10296*c*d^6*x^6 + 1716*d^7*x^7))/(b^8*(a + b*x)^13)$$

fricas [B] time = 0.43, size = 592, normalized size = 2.99

$$\frac{1716 b^7 d^7 x^7 + 792 b^7 c^7 + 462 a b^6 c^6 d + 252 a^2 b^5 c^5 d^2 + 126 a^3 b^4 c^4 d^3 + 56 a^4 b^3 c^3 d^4 + 21 a^5 b^2 c^2 d^5 + 6 a^6 b c d^6 + a^7 d^7}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^14,x, algorithm="fricas")

[Out]
$$-1/10296*(1716*b^7*d^7*x^7 + 792*b^7*c^7 + 462*a*b^6*c^6*d + 252*a^2*b^5*c^5*d^2 + 126*a^3*b^4*c^4*d^3 + 56*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 6*a^6*b*c*d^6 + a^7*d^7 + 1716*(6*b^7*c*d^6 + a*b^6*d^7)*x^6 + 1287*(21*b^7*c^2*d^5 + 6*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 715*(56*b^7*c^3*d^4 + 21*a*b^6*c^2*d^5 + 6*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 286*(126*b^7*c^4*d^3 + 56*a*b^6*c^3*d^4 + 21*a^2*b^5*c^2*d^5 + 6*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 78*(252*b^7*c^5*d^2 + 126*a*b^6*c^4*d^3 + 56*a^2*b^5*c^3*d^4 + 21*a^3*b^4*c^2*d^5 + 6*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 13*(462*b^7*c^6*d + 252*a*b^6*c^5*d^2 + 126*a^2*b^5*c^4*d^3 + 56*a^3*b^4*c^3*d^4 + 21*a^4*b^3*c^2*d^5 + 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^21*x^13 + 13*a*b^20*x^12 + 78*a^2*b^19*x^11 + 286*a^3*b^18*x^10 + 715*a^4*b^17*x^9 + 1287*a^5*b^16*x^8 + 1716*a^6*b^15*x^7 + 1716*a^7*b^14*x^6 + 1287*a^8*b^13*x^5 + 715*a^9*b^12*x^4 + 286*a^10*b^11*x^3 + 78*a^11*b^10*x^2 + 13*a^12*b^9*x + a^13*b^8)$$

giac [B] time = 1.24, size = 496, normalized size = 2.51

$$\frac{1716 b^7 d^7 x^7 + 10296 b^7 c d^6 x^6 + 1716 a b^6 d^7 x^6 + 27027 b^7 c^2 d^5 x^5 + 7722 a b^6 c d^6 x^5 + 1287 a^2 b^5 d^7 x^5 + 40040 b^7 c^3 d^6 x^4}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^14,x, algorithm="giac")

[Out]
$$\frac{-1/10296*(1716*b^7*d^7*x^7 + 10296*b^7*c*d^6*x^6 + 1716*a*b^6*d^7*x^6 + 270*27*b^7*c^2*d^5*x^5 + 7722*a*b^6*c*d^6*x^5 + 1287*a^2*b^5*d^7*x^5 + 40040*b^7*c^3*d^4*x^4 + 15015*a*b^6*c^2*d^5*x^4 + 4290*a^2*b^5*c*d^6*x^4 + 715*a^3*b^4*d^7*x^4 + 36036*b^7*c^4*d^3*x^3 + 16016*a*b^6*c^3*d^4*x^3 + 6006*a^2*b^5*c^2*d^5*x^3 + 1716*a^3*b^4*c*d^6*x^3 + 286*a^4*b^3*d^7*x^3 + 19656*b^7*c^5*d^2*x^2 + 9828*a*b^6*c^4*d^3*x^2 + 4368*a^2*b^5*c^3*d^4*x^2 + 1638*a^3*b^4*c^2*d^5*x^2 + 468*a^4*b^3*c*d^6*x^2 + 78*a^5*b^2*d^7*x^2 + 6006*b^7*c^6*d*x + 3276*a*b^6*c^5*d^2*x + 1638*a^2*b^5*c^4*d^3*x + 728*a^3*b^4*c^3*d^4*x + 273*a^4*b^3*c^2*d^5*x + 78*a^5*b^2*c*d^6*x + 13*a^6*b*d^7*x + 792*b^7*c^7 + 462*a*b^6*c^6*d + 252*a^2*b^5*c^5*d^2 + 126*a^3*b^4*c^4*d^3 + 56*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 6*a^6*b*c*d^6 + a^7*d^7)/(b*x + a)^13*b^8}$$

maple [B] time = 0.01, size = 463, normalized size = 2.34

$$\frac{d^7}{6(bx+a)^6 b^8} + \frac{(ad-bc)d^6}{(bx+a)^7 b^8} - \frac{21(a^2d^2 - 2abcd + b^2c^2)d^5}{8(bx+a)^8 b^8} + \frac{35(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)d^4}{9(bx+a)^9 b^8} - \frac{7(a^4d^4 - \dots)}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^14,x)

[Out]
$$\frac{-21/8*d^5*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^8/(b*x+a)^8-1/13*(-a^7*d^7+7*a^6*b*c*d^6-21*a^5*b^2*c^2*d^5+35*a^4*b^3*c^3*d^4-35*a^3*b^4*c^4*d^3+21*a^2*b^5*c^5*d^2-7*a*b^6*c^6*d+b^7*c^7)/b^8/(b*x+a)^13+d^6*(a*d-b*c)/b^8/(b*x+a)^7+35/9*d^4*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^8/(b*x+a)^9+21/11*d^2*(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)/b^8/(b*x+a)^11-7/12*d*(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^8/(b*x+a)^12-1/6*d^7/b^8/(b*x+a)^6-7/2*d^3*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/b^8/(b*x+a)^10}$$

maxima [B] time = 1.74, size = 592, normalized size = 2.99

$$\frac{1716 b^7 d^7 x^7 + 792 b^7 c^7 + 462 a b^6 c^6 d + 252 a^2 b^5 c^5 d^2 + 126 a^3 b^4 c^4 d^3 + 56 a^4 b^3 c^3 d^4 + 21 a^5 b^2 c^2 d^5 + 6 a^6 b c d^6 + a^7 d^7}{(b x + a)^{13} b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^14,x, algorithm="maxima")

[Out]
$$-1/10296*(1716*b^7*d^7*x^7 + 792*b^7*c^7 + 462*a*b^6*c^6*d + 252*a^2*b^5*c^5*d^2 + 126*a^3*b^4*c^4*d^3 + 56*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 6*a^6*b*c*d^6 + a^7*d^7)/(b*x + a)^13*b^8}$$

$$\begin{aligned} & ^6*b*c*d^6 + a^7*d^7 + 1716*(6*b^7*c*d^6 + a*b^6*d^7)*x^6 + 1287*(21*b^7*c^2*d^5 + 6*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 715*(56*b^7*c^3*d^4 + 21*a*b^6*c^2*d^5 + 6*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 286*(126*b^7*c^4*d^3 + 56*a*b^6*c^3*d^4 + 21*a^2*b^5*c^2*d^5 + 6*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 78*(252*b^7*c^5*d^2 + 126*a*b^6*c^4*d^3 + 56*a^2*b^5*c^3*d^4 + 21*a^3*b^4*c^2*d^5 + 6*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 13*(462*b^7*c^6*d + 252*a*b^6*c^5*d^2 + 126*a^2*b^5*c^4*d^3 + 56*a^3*b^4*c^3*d^4 + 21*a^4*b^3*c^2*d^5 + 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^21*x^13 + 13*a*b^20*x^12 + 78*a^2*b^19*x^11 + 286*a^3*b^18*x^10 + 715*a^4*b^17*x^9 + 1287*a^5*b^16*x^8 + 1716*a^6*b^15*x^7 + 1716*a^7*b^14*x^6 + 1287*a^8*b^13*x^5 + 715*a^9*b^12*x^4 + 286*a^10*b^11*x^3 + 78*a^11*b^10*x^2 + 13*a^12*b^9*x + a^13*b^8) \end{aligned}$$

mupad [B] time = 0.40, size = 570, normalized size = 2.88

$$\frac{a^7 d^7 + 6 a^6 b c d^6 + 21 a^5 b^2 c^2 d^5 + 56 a^4 b^3 c^3 d^4 + 126 a^3 b^4 c^4 d^3 + 252 a^2 b^5 c^5 d^2 + 462 a b^6 c^6 d + 792 b^7 c^7}{10296 b^8} + \frac{d^7 x^7}{6 b} + \frac{d^2 x^2 (a^5 d^5 + 6 a^4 b c d^4 + 21 a^3 b^2 c^2 d^3 + 56 a^2 b^3 c^3 d^2 + 6 a b^4 c^4 d + 6 a^5 b^5 c^5 d)}{a^{13} + 13 a^{12} b x + 78 a^{11} b^2 x^2 + 286 a^{10} b^3 x^3 + 715 a^9 b^4 x^4 + 1287 a^8 b^5 x^5 + 1716 a^7 b^6 x^6 + 1287 a^6 b^7 x^7 + 715 a^5 b^8 x^8 + 286 a^4 b^9 x^9 + 1716 a^3 b^{10} x^{10} + 78 a^2 b^{11} x^{11} + 13 a b^{12} x^{12} + a^{13}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^14,x)

[Out] $-\left(\frac{a^7 d^7 + 792 b^7 c^7 + 252 a^2 b^5 c^5 d^2 + 126 a^3 b^4 c^4 d^3 + 56 a^4 b^3 c^3 d^4 + 21 a^5 b^2 c^2 d^5 + 462 a b^6 c^6 d + 6 a^6 b^7 c^7}{10296 b^8} + \frac{d^7 x^7}{6 b} + \frac{d^2 x^2 (a^5 d^5 + 252 b^5 c^5 + 56 a^2 b^3 c^3 d^2 + 21 a^3 b^2 c^2 d^3 + 126 a b^4 c^4 d + 6 a^4 b^3 c^3 d^2 + 6 a^5 b^2 c^2 d^3 + 6 a^6 b^7 c^7)}{(132 b^6) + (5 d^4 x^4 (a^3 d^3 + 56 b^3 c^3 + 21 a b^2 c^2 d + 6 a^2 b^3 c^3 d^2))}{(72 b^4)} + \frac{d^6 x^6 (a d + 6 b c)}{(6 b^2)} + \frac{d^3 x^3 (a^4 d^4 + 126 b^4 c^4 + 21 a^2 b^2 c^2 d^2 + 56 a b^3 c^3 d + 6 a^3 b^4 c^4)}{(36 b^5)} + \frac{d x (a^6 d^6 + 462 b^6 c^6 + 126 a^2 b^4 c^4 d^2 + 56 a^3 b^3 c^3 d^3 + 21 a^4 b^2 c^2 d^4 + 252 a b^5 c^5 d + 6 a^5 b^6 c^6)}{(792 b^7)} + \frac{d^5 x^5 (a^2 d^2 + 21 b^2 c^2 + 6 a b c d)}{(8 b^3)}\right) / (a^{13} + b^{13} x^{13} + 13 a b^{12} x^{12} + 78 a^2 b^{11} x^{11} + 286 a^3 b^{10} x^{10} + 715 a^4 b^9 x^9 + 1287 a^5 b^8 x^8 + 1716 a^6 b^7 x^7 + 1287 a^7 b^6 x^6 + 715 a^8 b^5 x^5 + 286 a^9 b^4 x^4 + 1287 a^{10} b^3 x^3 + 715 a^{11} b^2 x^2 + 286 a^{12} b x + a^{13})$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**14,x)

[Out] Timed out

$$3.1297 \quad \int \frac{(c+dx)^7}{(a+bx)^{15}} dx$$

Optimal. Leaf size=200

$$\frac{7d^6(bc-ad)}{8b^8(a+bx)^8} - \frac{7d^5(bc-ad)^2}{3b^8(a+bx)^9} - \frac{7d^4(bc-ad)^3}{2b^8(a+bx)^{10}} - \frac{35d^3(bc-ad)^4}{11b^8(a+bx)^{11}} - \frac{7d^2(bc-ad)^5}{4b^8(a+bx)^{12}} - \frac{7d(bc-ad)^6}{13b^8(a+bx)^{13}} - \frac{(bc-ad)^7}{14b^8(a+bx)^{14}}$$

[Out] $-1/14*(-a*d+b*c)^7/b^8/(b*x+a)^{14}-7/13*d*(-a*d+b*c)^6/b^8/(b*x+a)^{13}-7/4*d^2*(-a*d+b*c)^5/b^8/(b*x+a)^{12}-35/11*d^3*(-a*d+b*c)^4/b^8/(b*x+a)^{11}-7/2*d^4*(-a*d+b*c)^3/b^8/(b*x+a)^{10}-7/3*d^5*(-a*d+b*c)^2/b^8/(b*x+a)^9-7/8*d^6*(-a*d+b*c)/b^8/(b*x+a)^8-1/7*d^7/b^8/(b*x+a)^7$

Rubi [A] time = 0.14, antiderivative size = 200, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{7d^6(bc-ad)}{8b^8(a+bx)^8} - \frac{7d^5(bc-ad)^2}{3b^8(a+bx)^9} - \frac{7d^4(bc-ad)^3}{2b^8(a+bx)^{10}} - \frac{35d^3(bc-ad)^4}{11b^8(a+bx)^{11}} - \frac{7d^2(bc-ad)^5}{4b^8(a+bx)^{12}} - \frac{7d(bc-ad)^6}{13b^8(a+bx)^{13}} - \frac{(bc-ad)^7}{14b^8(a+bx)^{14}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^15, x]

[Out] $-(b*c - a*d)^7/(14*b^8*(a + b*x)^{14}) - (7*d*(b*c - a*d)^6)/(13*b^8*(a + b*x)^{13}) - (7*d^2*(b*c - a*d)^5)/(4*b^8*(a + b*x)^{12}) - (35*d^3*(b*c - a*d)^4)/(11*b^8*(a + b*x)^{11}) - (7*d^4*(b*c - a*d)^3)/(2*b^8*(a + b*x)^{10}) - (7*d^5*(b*c - a*d)^2)/(3*b^8*(a + b*x)^9) - (7*d^6*(b*c - a*d))/(8*b^8*(a + b*x)^8) - d^7/(7*b^8*(a + b*x)^7)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^{15}} dx = \int \left(\frac{(bc-ad)^7}{b^7(a+bx)^{15}} + \frac{7d(bc-ad)^6}{b^7(a+bx)^{14}} + \frac{21d^2(bc-ad)^5}{b^7(a+bx)^{13}} + \frac{35d^3(bc-ad)^4}{b^7(a+bx)^{12}} + \frac{35d^4(bc-ad)^3}{b^7(a+bx)^{11}} + \frac{21d^5(bc-ad)^2}{b^7(a+bx)^{10}} + \frac{7d^6(bc-ad)}{b^7(a+bx)^9} + \frac{d^7}{b^7(a+bx)^8} \right) dx$$

$$= -\frac{(bc-ad)^7}{14b^8(a+bx)^{14}} - \frac{7d(bc-ad)^6}{13b^8(a+bx)^{13}} - \frac{7d^2(bc-ad)^5}{4b^8(a+bx)^{12}} - \frac{35d^3(bc-ad)^4}{11b^8(a+bx)^{11}} - \frac{7d^4(bc-ad)^3}{2b^8(a+bx)^{10}} - \frac{7d^5(bc-ad)^2}{3b^8(a+bx)^9} - \frac{7d^6(bc-ad)}{8b^8(a+bx)^8} - \frac{d^7}{7b^8(a+bx)^7}$$

Mathematica [A] time = 0.13, size = 371, normalized size = 1.86

$$\frac{a^7 d^7 + 7a^6 b d^6 (c + 2dx) + 7a^5 b^2 d^5 (4c^2 + 14cdx + 13d^2 x^2) + 7a^4 b^3 d^4 (12c^3 + 56c^2 dx + 91cd^2 x^2 + 52d^3 x^3) + 7a^3 b^4 d^3 (30c^4 + 168c^3 dx + 364c^2 d^2 x^2 + 364c d^3 x^3 + 143d^4 x^4) + 7a^2 b^5 d^2 (66c^5 + 420c^4 dx + 1092c^3 d^2 x^2 + 1456c^2 d^3 x^3 + 1001c d^4 x^4 + 286d^5 x^5) + 7a b^6 d (132c^6 + 924c^5 dx + 2730c^4 d^2 x^2 + 4368c^3 d^3 x^3 + 4004c^2 d^4 x^4 + 2002c d^5 x^5 + 429d^6 x^6) + b^7 (1716c^7 + 12936c^6 dx + 42042c^5 d^2 x^2 + 76440c^4 d^3 x^3 + 84084c^3 d^4 x^4 + 56056c^2 d^5 x^5 + 21021c d^6 x^6 + 3432d^7 x^7)}{(b^8 (a + b x)^{14})}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^15,x]

[Out] -1/24024*(a^7*d^7 + 7*a^6*b*d^6*(c + 2*d*x) + 7*a^5*b^2*d^5*(4*c^2 + 14*c*d*x + 13*d^2*x^2) + 7*a^4*b^3*d^4*(12*c^3 + 56*c^2*d*x + 91*c*d^2*x^2 + 52*d^3*x^3) + 7*a^3*b^4*d^3*(30*c^4 + 168*c^3*d*x + 364*c^2*d^2*x^2 + 364*c*d^3*x^3 + 143*d^4*x^4) + 7*a^2*b^5*d^2*(66*c^5 + 420*c^4*d*x + 1092*c^3*d^2*x^2 + 1456*c^2*d^3*x^3 + 1001*c*d^4*x^4 + 286*d^5*x^5) + 7*a*b^6*d*(132*c^6 + 924*c^5*d*x + 2730*c^4*d^2*x^2 + 4368*c^3*d^3*x^3 + 4004*c^2*d^4*x^4 + 2002*c*d^5*x^5 + 429*d^6*x^6) + b^7*(1716*c^7 + 12936*c^6*d*x + 42042*c^5*d^2*x^2 + 76440*c^4*d^3*x^3 + 84084*c^3*d^4*x^4 + 56056*c^2*d^5*x^5 + 21021*c*d^6*x^6 + 3432*d^7*x^7))/(b^8*(a + b*x)^14)

fricas [B] time = 0.43, size = 603, normalized size = 3.02

$$\frac{3432 b^7 d^7 x^7 + 1716 b^7 c^7 + 924 a b^6 c^6 d + 462 a^2 b^5 c^5 d^2 + 210 a^3 b^4 c^4 d^3 + 84 a^4 b^3 c^3 d^4 + 28 a^5 b^2 c^2 d^5 + 7 a^6 b c d^6 + 3432 a^7 d^7 + 1716 a^6 b^7 c^7 + 924 a^5 b^6 c^6 d + 462 a^4 b^5 c^5 d^2 + 210 a^3 b^4 c^4 d^3 + 84 a^2 b^3 c^3 d^4 + 28 a b^2 c^2 d^5 + 7 a^6 b^7 c^7}{(b^8 (a + b x)^{14})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^15,x, algorithm="fricas")

[Out] -1/24024*(3432*b^7*d^7*x^7 + 1716*b^7*c^7 + 924*a*b^6*c^6*d + 462*a^2*b^5*c^5*d^2 + 210*a^3*b^4*c^4*d^3 + 84*a^4*b^3*c^3*d^4 + 28*a^5*b^2*c^2*d^5 + 7*a^6*b*c*d^6 + a^7*d^7 + 3003*(7*b^7*c*d^6 + a*b^6*d^7)*x^6 + 2002*(28*b^7*c^2*d^5 + 7*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 1001*(84*b^7*c^3*d^4 + 28*a*b^6*c^2*d^5 + 7*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 364*(210*b^7*c^4*d^3 + 84*a*b^6*c^3*d^4 + 28*a^2*b^5*c^2*d^5 + 7*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 91*(462*b^7*c^5*d^2 + 210*a*b^6*c^4*d^3 + 84*a^2*b^5*c^3*d^4 + 28*a^3*b^4*c^2*d^5 + 7*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 14*(924*b^7*c^6*d + 462*a*b^6*c^5*d^2 + 210*a^2*b^5*c^4*d^3 + 84*a^3*b^4*c^3*d^4 + 28*a^4*b^3*c^2*d^5 + 7*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^22*x^14 + 14*a*b^21*x^13 + 91*a^2*b^20*x^12 + 364*a^3*b^19*x^11 + 1001*a^4*b^18*x^10 + 2002*a^5*b^17*x^9 + 3003*a^6*b^16*x^8 + 3432*a^7*b^15*x^7 + 3003*a^8*b^14*x^6 + 2002*a^9*b^13*x^5 + 1001*a^10*b^12*x^4 + 364*a^11*b^11*x^3 + 91*a^12*b^10*x^2 + 14*a^13*b^9*x + a^14*b^8)

giac [B] time = 1.28, size = 496, normalized size = 2.48

$$\frac{3432 b^7 d^7 x^7 + 21021 b^7 c d^6 x^6 + 3003 a b^6 d^7 x^6 + 56056 b^7 c^2 d^5 x^5 + 14014 a b^6 c d^6 x^5 + 2002 a^2 b^5 d^7 x^5 + 84084 b^7 c^3 d^4 x^4 + 1716 a^3 b^4 c^4 d^3 x^4 + 924 a^2 b^5 c^3 d^4 x^4 + 1716 a^4 b^3 c^3 d^4 x^4 + 28 a^5 b^2 c^2 d^5 x^4 + 7 a^6 b c d^6 x^4 + 3432 a^7 d^7 x^4 + 1716 a^6 b^7 c^7 x^4 + 924 a^5 b^6 c^6 d x^4 + 462 a^4 b^5 c^5 d^2 x^4 + 210 a^3 b^4 c^4 d^3 x^4 + 84 a^2 b^3 c^3 d^4 x^4 + 28 a b^2 c^2 d^5 x^4 + 7 a^6 b^7 c^7 x^4}{(b^8 (a + b x)^{14})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^15,x, algorithm="giac")

[Out]
$$\frac{-1/24024*(3432*b^7*d^7*x^7 + 21021*b^7*c*d^6*x^6 + 3003*a*b^6*d^7*x^6 + 560*56*b^7*c^2*d^5*x^5 + 14014*a*b^6*c*d^6*x^5 + 2002*a^2*b^5*d^7*x^5 + 84084*b^7*c^3*d^4*x^4 + 28028*a*b^6*c^2*d^5*x^4 + 7007*a^2*b^5*c*d^6*x^4 + 1001*a^3*b^4*d^7*x^4 + 76440*b^7*c^4*d^3*x^3 + 30576*a*b^6*c^3*d^4*x^3 + 10192*a^2*b^5*c^2*d^5*x^3 + 2548*a^3*b^4*c*d^6*x^3 + 364*a^4*b^3*d^7*x^3 + 42042*b^7*c^5*d^2*x^2 + 19110*a*b^6*c^4*d^3*x^2 + 7644*a^2*b^5*c^3*d^4*x^2 + 2548*a^3*b^4*c^2*d^5*x^2 + 637*a^4*b^3*c*d^6*x^2 + 91*a^5*b^2*d^7*x^2 + 12936*b^7*c^6*d*x + 6468*a*b^6*c^5*d^2*x + 2940*a^2*b^5*c^4*d^3*x + 1176*a^3*b^4*c^3*d^4*x + 392*a^4*b^3*c^2*d^5*x + 98*a^5*b^2*c*d^6*x + 14*a^6*b*d^7*x + 1716*b^7*c^7 + 924*a*b^6*c^6*d + 462*a^2*b^5*c^5*d^2 + 210*a^3*b^4*c^4*d^3 + 84*a^4*b^3*c^3*d^4 + 28*a^5*b^2*c^2*d^5 + 7*a^6*b*c*d^6 + a^7*d^7)/((b*x + a)^14*b^8)}$$

maple [B] time = 0.01, size = 464, normalized size = 2.32

$$\frac{d^7}{7(bx+a)^7 b^8} + \frac{7(ad-bc)d^6}{8(bx+a)^8 b^8} - \frac{7(a^2d^2-2abcd+b^2c^2)d^5}{3(bx+a)^9 b^8} + \frac{7(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^4}{2(bx+a)^{10} b^8} - \frac{35(a^4d^4-4a^3b^3c^3d^3+15a^2b^4c^4d^2-6a*b^5*c^5*d+b^6*c^6)}{b^8(bx+a)^{13}} - \frac{1}{7} \frac{d^7}{b^8(bx+a)^7} - \frac{7}{3} \frac{d^5}{b^8(bx+a)^7} - \frac{7}{3} \frac{d^5(a^2d^2-2a*b*c*d+b^2*c^2)}{b^8(bx+a)^9} - \frac{35}{11} \frac{d^3(a^4d^4-4a^3*b*c*d^3+6a^2*b^2*c^2*d^2-4a*b^3*c^3*d+b^4*c^4)}{b^8(bx+a)^{11}} + \frac{7}{4} \frac{d^2(a^5*d^5-5a^4*b*c*d^4+10a^3*b^2*c^2*d^3-10a^2*b^3*c^3*d^2+5a*b^4*c^4*d-b^5*c^5)}{b^8(bx+a)^{12}} + \frac{7}{2} \frac{d^4(a^3*d^3-3a^2*b*c*d^2+3a*b^2*c^2*d-b^3*c^3)}{b^8(bx+a)^{10}} - \frac{1}{14} \frac{(-a^7*d^7+7a^6*b*c*d^6-21a^5*b^2*c^2*d^5+35a^4*b^3*c^3*d^4-35a^3*b^4*c^4*d^3+21a^2*b^5*c^5*d^2-7a*b^6*c^6*d+b^7*c^7)}{b^8(bx+a)^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^15,x)

[Out]
$$\frac{7}{8} \frac{d^6(a*d-b*c)}{b^8(bx+a)^8} - \frac{7}{13} \frac{d^6(a^6*d^6-6a^5*b*c*d^5+15a^4*b^2*c^2*d^4-20a^3*b^3*c^3*d^3+15a^2*b^4*c^4*d^2-6a*b^5*c^5*d+b^6*c^6)}{b^8(bx+a)^{13}} - \frac{1}{7} \frac{d^7}{b^8(bx+a)^7} - \frac{7}{3} \frac{d^5(a^2*d^2-2a*b*c*d+b^2*c^2)}{b^8(bx+a)^9} - \frac{35}{11} \frac{d^3(a^4*d^4-4a^3*b*c*d^3+6a^2*b^2*c^2*d^2-4a*b^3*c^3*d+b^4*c^4)}{b^8(bx+a)^{11}} + \frac{7}{4} \frac{d^2(a^5*d^5-5a^4*b*c*d^4+10a^3*b^2*c^2*d^3-10a^2*b^3*c^3*d^2+5a*b^4*c^4*d-b^5*c^5)}{b^8(bx+a)^{12}} + \frac{7}{2} \frac{d^4(a^3*d^3-3a^2*b*c*d^2+3a*b^2*c^2*d-b^3*c^3)}{b^8(bx+a)^{10}} - \frac{1}{14} \frac{(-a^7*d^7+7a^6*b*c*d^6-21a^5*b^2*c^2*d^5+35a^4*b^3*c^3*d^4-35a^3*b^4*c^4*d^3+21a^2*b^5*c^5*d^2-7a*b^6*c^6*d+b^7*c^7)}{b^8(bx+a)^{14}}$$

maxima [B] time = 1.83, size = 603, normalized size = 3.02

$$\frac{3432 b^7 d^7 x^7 + 1716 b^7 c^7 + 924 a b^6 c^6 d + 462 a^2 b^5 c^5 d^2 + 210 a^3 b^4 c^4 d^3 + 84 a^4 b^3 c^3 d^4 + 28 a^5 b^2 c^2 d^5 + 7 a^6 b c d^6 - a^7 d^7}{(b x + a)^{14} b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^15,x, algorithm="maxima")

[Out]
$$-1/24024*(3432*b^7*d^7*x^7 + 1716*b^7*c^7 + 924*a*b^6*c^6*d + 462*a^2*b^5*c^5*d^2 + 210*a^3*b^4*c^4*d^3 + 84*a^4*b^3*c^3*d^4 + 28*a^5*b^2*c^2*d^5 + 7*$$

$$a^6 b^7 c^7 d^6 + a^7 d^7 + 3003(7b^7 c^7 d^6 + a^6 b^7 d^7) x^6 + 2002(28b^7 c^7 d^5 + 7a^6 b^7 c^7 d^6 + a^7 b^7 c^7 d^7) x^5 + 1001(84b^7 c^7 d^4 + 28a^6 b^7 c^7 d^5 + 7a^7 b^7 c^7 d^6 + a^8 b^7 c^7 d^7) x^4 + 364(210b^7 c^7 d^3 + 84a^6 b^7 c^7 d^4 + 28a^7 b^7 c^7 d^5 + 7a^8 b^7 c^7 d^6 + a^9 b^7 c^7 d^7) x^3 + 91(462b^7 c^7 d^2 + 210a^6 b^7 c^7 d^3 + 84a^7 b^7 c^7 d^4 + 28a^8 b^7 c^7 d^5 + 7a^9 b^7 c^7 d^6 + a^{10} b^7 c^7 d^7) x^2 + 14(924b^7 c^7 d + 462a^6 b^7 c^7 d^2 + 210a^7 b^7 c^7 d^3 + 84a^8 b^7 c^7 d^4 + 28a^9 b^7 c^7 d^5 + 7a^{10} b^7 c^7 d^6 + a^{11} b^7 c^7 d^7) x + (b^{22} x^{14} + 14a^6 b^{21} x^{13} + 91a^7 b^{20} x^{12} + 364a^8 b^{19} x^{11} + 1001a^9 b^{18} x^{10} + 2002a^{10} b^{17} x^9 + 3003a^{11} b^{16} x^8 + 3432a^{12} b^{15} x^7 + 3003a^{13} b^{14} x^6 + 2002a^{14} b^{13} x^5 + 1001a^{15} b^{12} x^4 + 364a^{16} b^{11} x^3 + 91a^{17} b^{10} x^2 + 14a^{18} b^9 x + a^{19} b^8)$$

mupad [B] time = 1.24, size = 581, normalized size = 2.90

$$\frac{a^7 d^7 + 7a^6 b c d^6 + 28a^5 b^2 c^2 d^5 + 84a^4 b^3 c^3 d^4 + 210a^3 b^4 c^4 d^3 + 462a^2 b^5 c^5 d^2 + 924a b^6 c^6 d + 1716b^7 c^7}{24024 b^8} + \frac{d^7 x^7}{7b} + \frac{d^2 x^2 (a^5 d^5 + 7a^4 b c d^4 + 28a^3 b^2 c^2 d^3 + 84a^2 b^3 c^3 d^2 + 210a b^4 c^4 d + 7a^6 b^7 c^7)}{a^{14} + 14a^{13} b x + 91a^{12} b^2 x^2 + 364a^{11} b^3 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^15, x)

[Out] $-\left(\frac{a^7 d^7 + 1716b^7 c^7 + 462a^2 b^5 c^5 d^2 + 210a^3 b^4 c^4 d^3 + 84a^4 b^3 c^3 d^4 + 28a^5 b^2 c^2 d^5 + 924a^6 b^7 c^6 d + 7a^6 b^7 c^6 d}{24024b^8} + \frac{d^7 x^7}{7b} + \frac{d^2 x^2 (a^5 d^5 + 462b^5 c^5 + 84a^2 b^3 c^3 d^2 + 28a^3 b^2 c^2 d^3 + 210a^4 b^4 c^4 d + 7a^4 b^4 c^4 d)}{(264b^6) + \frac{d^4 x^4 (a^3 d^3 + 84b^3 c^3 + 28a^2 b^2 c^2 d + 7a^2 b^2 c^2 d)}{(24b^4) + \frac{d^6 x^6 (a d + 7b c)}{(8b^2) + \frac{d^3 x^3 (a^4 d^4 + 210b^4 c^4 + 28a^2 b^2 c^2 d^2 + 84a^3 b^3 c^3 d + 7a^3 b^3 c^3 d)}{(66b^5) + \frac{d x (a^6 d^6 + 924b^6 c^6 + 210a^2 b^4 c^4 d^2 + 84a^3 b^3 c^3 d^3 + 28a^4 b^2 c^2 d^4 + 462a^5 b^5 c^5 d + 7a^5 b^5 c^5 d)}{(1716b^7) + \frac{d^5 x^5 (a^2 d^2 + 28b^2 c^2 + 7a^2 b^2 c^2 d)}{(12b^3)}}}{(a^{14} + b^{14} x^{14} + 14a^6 b^{13} x^{13} + 91a^7 b^{12} x^{12} + 364a^8 b^{11} x^{11} + 1001a^9 b^{10} x^{10} + 2002a^{10} b^9 x^9 + 3003a^{11} b^8 x^8 + 3432a^{12} b^7 x^7 + 3003a^{13} b^6 x^6 + 2002a^{14} b^5 x^5 + 1001a^{15} b^4 x^4 + 364a^{16} b^3 x^3 + 91a^{17} b^2 x^2 + 14a^{18} b x + a^{19} b^8)}\right)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**15, x)

[Out] Timed out

$$3.1298 \quad \int \frac{(c+dx)^7}{(a+bx)^{16}} dx$$

Optimal. Leaf size=200

$$\frac{7d^6(bc-ad)}{9b^8(a+bx)^9} - \frac{21d^5(bc-ad)^2}{10b^8(a+bx)^{10}} - \frac{35d^4(bc-ad)^3}{11b^8(a+bx)^{11}} - \frac{35d^3(bc-ad)^4}{12b^8(a+bx)^{12}} - \frac{21d^2(bc-ad)^5}{13b^8(a+bx)^{13}} - \frac{d(bc-ad)^6}{2b^8(a+bx)^{14}} - \frac{(bc-ad)^7}{15b^8(a+bx)^{15}}$$

[Out] $-1/15*(-a*d+b*c)^7/b^8/(b*x+a)^{15}-1/2*d*(-a*d+b*c)^6/b^8/(b*x+a)^{14}-21/13*d^2*(-a*d+b*c)^5/b^8/(b*x+a)^{13}-35/12*d^3*(-a*d+b*c)^4/b^8/(b*x+a)^{12}-35/11*d^4*(-a*d+b*c)^3/b^8/(b*x+a)^{11}-21/10*d^5*(-a*d+b*c)^2/b^8/(b*x+a)^{10}-7/9*d^6*(-a*d+b*c)/b^8/(b*x+a)^9-1/8*d^7/b^8/(b*x+a)^8$

Rubi [A] time = 0.14, antiderivative size = 200, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{7d^6(bc-ad)}{9b^8(a+bx)^9} - \frac{21d^5(bc-ad)^2}{10b^8(a+bx)^{10}} - \frac{35d^4(bc-ad)^3}{11b^8(a+bx)^{11}} - \frac{35d^3(bc-ad)^4}{12b^8(a+bx)^{12}} - \frac{21d^2(bc-ad)^5}{13b^8(a+bx)^{13}} - \frac{d(bc-ad)^6}{2b^8(a+bx)^{14}} - \frac{(bc-ad)^7}{15b^8(a+bx)^{15}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^7/(a + b*x)^16, x]

[Out] $-(b*c - a*d)^7/(15*b^8*(a + b*x)^{15}) - (d*(b*c - a*d)^6)/(2*b^8*(a + b*x)^{14}) - (21*d^2*(b*c - a*d)^5)/(13*b^8*(a + b*x)^{13}) - (35*d^3*(b*c - a*d)^4)/(12*b^8*(a + b*x)^{12}) - (35*d^4*(b*c - a*d)^3)/(11*b^8*(a + b*x)^{11}) - (21*d^5*(b*c - a*d)^2)/(10*b^8*(a + b*x)^{10}) - (7*d^6*(b*c - a*d))/(9*b^8*(a + b*x)^9) - d^7/(8*b^8*(a + b*x)^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^7}{(a+bx)^{16}} dx = \int \left(\frac{(bc-ad)^7}{b^7(a+bx)^{16}} + \frac{7d(bc-ad)^6}{b^7(a+bx)^{15}} + \frac{21d^2(bc-ad)^5}{b^7(a+bx)^{14}} + \frac{35d^3(bc-ad)^4}{b^7(a+bx)^{13}} + \frac{35d^4(bc-ad)^3}{b^7(a+bx)^{12}} + \frac{21d^5(bc-ad)^2}{b^7(a+bx)^{11}} + \frac{7d^6(bc-ad)}{b^7(a+bx)^{10}} + \frac{d^7}{b^7(a+bx)^9} \right) dx$$

$$= -\frac{(bc-ad)^7}{15b^8(a+bx)^{15}} - \frac{d(bc-ad)^6}{2b^8(a+bx)^{14}} - \frac{21d^2(bc-ad)^5}{13b^8(a+bx)^{13}} - \frac{35d^3(bc-ad)^4}{12b^8(a+bx)^{12}} - \frac{35d^4(bc-ad)^3}{11b^8(a+bx)^{11}} - \frac{21d^5(bc-ad)^2}{10b^8(a+bx)^{10}} - \frac{7d^6(bc-ad)}{9b^8(a+bx)^9} - \frac{d^7}{8b^8(a+bx)^8}$$

Mathematica [A] time = 0.13, size = 371, normalized size = 1.86

$$\frac{a^7 d^7 + a^6 b d^6 (8c + 15dx) + 3a^5 b^2 d^5 (12c^2 + 40cdx + 35d^2 x^2) + 5a^4 b^3 d^4 (24c^3 + 108c^2 dx + 168cd^2 x^2 + 91d^3 x^3)}{b^8 (a + bx)^{15}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^7/(a + b*x)^16,x]

[Out]
$$\frac{-1/51480*(a^7*d^7 + a^6*b*d^6*(8*c + 15*d*x) + 3*a^5*b^2*d^5*(12*c^2 + 40*c*d*x + 35*d^2*x^2) + 5*a^4*b^3*d^4*(24*c^3 + 108*c^2*d*x + 168*c*d^2*x^2 + 91*d^3*x^3) + 5*a^3*b^4*d^3*(66*c^4 + 360*c^3*d*x + 756*c^2*d^2*x^2 + 728*c*d^3*x^3 + 273*d^4*x^4) + 3*a^2*b^5*d^2*(264*c^5 + 1650*c^4*d*x + 4200*c^3*d^2*x^2 + 5460*c^2*d^3*x^3 + 3640*c*d^4*x^4 + 1001*d^5*x^5) + a*b^6*d*(1716*c^6 + 11880*c^5*d*x + 34650*c^4*d^2*x^2 + 54600*c^3*d^3*x^3 + 49140*c^2*d^4*x^4 + 24024*c*d^5*x^5 + 5005*d^6*x^6) + b^7*(3432*c^7 + 25740*c^6*d*x + 83160*c^5*d^2*x^2 + 150150*c^4*d^3*x^3 + 163800*c^3*d^4*x^4 + 108108*c^2*d^5*x^5 + 40040*c*d^6*x^6 + 6435*d^7*x^7))/(b^8*(a + b*x)^15)}$$

fricas [B] time = 0.44, size = 614, normalized size = 3.07

$$\frac{6435 b^7 d^7 x^7 + 3432 b^7 c^7 + 1716 a b^6 c^6 d + 792 a^2 b^5 c^5 d^2 + 330 a^3 b^4 c^4 d^3 + 120 a^4 b^3 c^3 d^4 + 36 a^5 b^2 c^2 d^5 + 8 a^6 b c d^6}{b^8 (a + b x)^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^16,x, algorithm="fricas")

[Out]
$$\frac{-1/51480*(6435*b^7*d^7*x^7 + 3432*b^7*c^7 + 1716*a*b^6*c^6*d + 792*a^2*b^5*c^5*d^2 + 330*a^3*b^4*c^4*d^3 + 120*a^4*b^3*c^3*d^4 + 36*a^5*b^2*c^2*d^5 + 8*a^6*b*c*d^6 + a^7*d^7 + 5005*(8*b^7*c*d^6 + a*b^6*d^7)*x^6 + 3003*(36*b^7*c^2*d^5 + 8*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 1365*(120*b^7*c^3*d^4 + 36*a*b^6*c^2*d^5 + 8*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 455*(330*b^7*c^4*d^3 + 120*a*b^6*c^3*d^4 + 36*a^2*b^5*c^2*d^5 + 8*a^3*b^4*c*d^6 + a^4*b^3*d^7)*x^3 + 105*(792*b^7*c^5*d^2 + 330*a*b^6*c^4*d^3 + 120*a^2*b^5*c^3*d^4 + 36*a^3*b^4*c^2*d^5 + 8*a^4*b^3*c*d^6 + a^5*b^2*d^7)*x^2 + 15*(1716*b^7*c^6*d + 792*a*b^6*c^5*d^2 + 330*a^2*b^5*c^4*d^3 + 120*a^3*b^4*c^3*d^4 + 36*a^4*b^3*c^2*d^5 + 8*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(b^23*x^15 + 15*a*b^22*x^14 + 105*a^2*b^21*x^13 + 455*a^3*b^20*x^12 + 1365*a^4*b^19*x^11 + 3003*a^5*b^18*x^10 + 5005*a^6*b^17*x^9 + 6435*a^7*b^16*x^8 + 6435*a^8*b^15*x^7 + 5005*a^9*b^14*x^6 + 3003*a^10*b^13*x^5 + 1365*a^11*b^12*x^4 + 455*a^12*b^11*x^3 + 105*a^13*b^10*x^2 + 15*a^14*b^9*x + a^15*b^8)}$$

giac [B] time = 1.29, size = 496, normalized size = 2.48

$$\frac{6435 b^7 d^7 x^7 + 40040 b^7 c d^6 x^6 + 5005 a b^6 d^7 x^6 + 108108 b^7 c^2 d^5 x^5 + 24024 a b^6 c d^6 x^5 + 3003 a^2 b^5 d^7 x^5 + 163800 b^7 c^3 d^4 x^4 + 40040 a b^6 c^2 d^5 x^4 + 108108 a^2 b^5 c d^6 x^4 + 163800 a^3 b^4 c^3 d^4 x^4 + 40040 a^4 b^3 c^2 d^5 x^4 + 108108 a^5 b^2 c^2 d^5 x^4 + 40040 a^6 b c^2 d^5 x^4 + 108108 a^7 c^2 d^5 x^4 + 40040 a^8 b^2 c^2 d^5 x^4 + 40040 a^9 b^3 c^2 d^5 x^4 + 40040 a^{10} b^4 c^2 d^5 x^4 + 40040 a^{11} b^5 c^2 d^5 x^4 + 40040 a^{12} b^6 c^2 d^5 x^4 + 40040 a^{13} b^7 c^2 d^5 x^4 + 40040 a^{14} b^8 c^2 d^5 x^4 + 40040 a^{15} c^2 d^5 x^4}{b^8 (a + b x)^{15}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^16,x, algorithm="giac")

[Out]
$$\frac{-1/51480*(6435*b^7*d^7*x^7 + 40040*b^7*c*d^6*x^6 + 5005*a*b^6*d^7*x^6 + 108108*b^7*c^2*d^5*x^5 + 24024*a*b^6*c*d^6*x^5 + 3003*a^2*b^5*d^7*x^5 + 163800*b^7*c^3*d^4*x^4 + 49140*a*b^6*c^2*d^5*x^4 + 10920*a^2*b^5*c*d^6*x^4 + 1365*a^3*b^4*d^7*x^4 + 150150*b^7*c^4*d^3*x^3 + 54600*a*b^6*c^3*d^4*x^3 + 16380*a^2*b^5*c^2*d^5*x^3 + 3640*a^3*b^4*c*d^6*x^3 + 455*a^4*b^3*d^7*x^3 + 83160*b^7*c^5*d^2*x^2 + 34650*a*b^6*c^4*d^3*x^2 + 12600*a^2*b^5*c^3*d^4*x^2 + 3780*a^3*b^4*c^2*d^5*x^2 + 840*a^4*b^3*c*d^6*x^2 + 105*a^5*b^2*d^7*x^2 + 25740*b^7*c^6*d*x + 11880*a*b^6*c^5*d^2*x + 4950*a^2*b^5*c^4*d^3*x + 1800*a^3*b^4*c^3*d^4*x + 540*a^4*b^3*c^2*d^5*x + 120*a^5*b^2*c*d^6*x + 15*a^6*b*d^7*x + 3432*b^7*c^7 + 1716*a*b^6*c^6*d + 792*a^2*b^5*c^5*d^2 + 330*a^3*b^4*c^4*d^3 + 120*a^4*b^3*c^3*d^4 + 36*a^5*b^2*c^2*d^5 + 8*a^6*b*c*d^6 + a^7*d^7)/(b*x + a)^15*b^8}$$

maple [B] time = 0.01, size = 464, normalized size = 2.32

$$\frac{d^7}{8(bx+a)^8 b^8} + \frac{7(ad-bc)d^6}{9(bx+a)^9 b^8} - \frac{21(a^2d^2-2abcd+b^2c^2)d^5}{10(bx+a)^{10} b^8} + \frac{35(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^4}{11(bx+a)^{11} b^8} - \frac{35(a^4d^4-4a^3bcd^3+3a^2b^2cd^2-b^3c^3d)}{12(bx+a)^{12} b^8} + \frac{1716a^5b^2c^2d^5 + 330a^3b^4c^4d^3 + 120a^4b^3c^3d^4 + 36a^5b^2c^2d^5 + 8a^6bcd^6 + a^7d^7}{(bx+a)^{15} b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^7/(b*x+a)^16,x)

[Out]
$$\frac{-1/8*d^7/b^8/(b*x+a)^8+21/13*d^2*(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)/b^8/(b*x+a)^{13}+7/9*d^6*(a*d-b*c)/b^8/(b*x+a)^9+35/11*d^4*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^8/(b*x+a)^{11}-1/15*(-a^7*d^7+7*a^6*b*c*d^6-21*a^5*b^2*c^2*d^5+35*a^4*b^3*c^3*d^4-35*a^3*b^4*c^4*d^3+21*a^2*b^5*c^5*d^2-7*a*b^6*c^6*d+b^7*c^7)/b^8/(b*x+a)^{15}-35/12*d^3*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/b^8/(b*x+a)^{12}-21/10*d^5*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^8/(b*x+a)^{10}-1/2*d*(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^8/(b*x+a)^{14}}$$

maxima [B] time = 1.91, size = 614, normalized size = 3.07

$$\frac{6435 b^7 d^7 x^7 + 3432 b^7 c^7 + 1716 a b^6 c^6 d + 792 a^2 b^5 c^5 d^2 + 330 a^3 b^4 c^4 d^3 + 120 a^4 b^3 c^3 d^4 + 36 a^5 b^2 c^2 d^5 + 8 a^6 b c d^6 + a^7 d^7}{(b x + a)^{15} b^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^7/(b*x+a)^16,x, algorithm="maxima")

[Out]
$$-1/51480*(6435*b^7*d^7*x^7 + 3432*b^7*c^7 + 1716*a*b^6*c^6*d + 792*a^2*b^5*c^5*d^2 + 330*a^3*b^4*c^4*d^3 + 120*a^4*b^3*c^3*d^4 + 36*a^5*b^2*c^2*d^5 +$$

$$8a^6bcd^6 + a^7d^7 + 5005(8b^7cd^6 + ab^6d^7)x^6 + 3003(36b^7c^2d^5 + 8ab^6cd^6 + a^2b^5d^7)x^5 + 1365(120b^7c^3d^4 + 36ab^6c^2d^5 + 8a^2b^5cd^6 + a^3b^4d^7)x^4 + 455(330b^7c^4d^3 + 120ab^6c^3d^4 + 36a^2b^5c^2d^5 + 8a^3b^4cd^6 + a^4b^3d^7)x^3 + 105(792b^7c^5d^2 + 330ab^6c^4d^3 + 120a^2b^5c^3d^4 + 36a^3b^4c^2d^5 + 8a^4b^3cd^6 + a^5b^2d^7)x^2 + 15(1716b^7c^6d + 792ab^6c^5d^2 + 330a^2b^5c^4d^3 + 120a^3b^4c^3d^4 + 36a^4b^3c^2d^5 + 8a^5b^2cd^6 + a^6bd^7)x / (b^{23}x^{15} + 15a^22x^{14} + 105a^21x^{13} + 455a^3b^{20}x^{12} + 1365a^4b^{19}x^{11} + 3003a^5b^{18}x^{10} + 5005a^6b^{17}x^9 + 6435a^7b^{16}x^8 + 6435a^8b^{15}x^7 + 5005a^9b^{14}x^6 + 3003a^{10}b^{13}x^5 + 1365a^{11}b^{12}x^4 + 455a^{12}b^{11}x^3 + 105a^{13}b^{10}x^2 + 15a^{14}b^9x + a^{15}b^8)$$

mupad [B] time = 2.20, size = 592, normalized size = 2.96

$$\frac{a^7d^7 + 8a^6bcd^6 + 36a^5b^2c^2d^5 + 120a^4b^3c^3d^4 + 330a^3b^4c^4d^3 + 792a^2b^5c^5d^2 + 1716ab^6c^6d + 3432b^7c^7}{51480b^8} + \frac{d^7x^7}{8b} + \frac{7d^2x^2(a^5d^5 + 8a^4bcd^4 + 36a^3b^2c^3d^3 + 120a^2b^3cd^2 + 36a^3b^2c^2d^3 + 330ab^4c^4d + 8a^4b^3cd^4)}{a^{15} + 15a^{14}bx + 105a^{13}b^2x^2 + 455a^{12}b^3x^3 + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^7/(a + b*x)^16,x)

[Out] $-\frac{(a^7d^7 + 3432b^7c^7 + 792a^2b^5c^5d^2 + 330a^3b^4c^4d^3 + 120a^4b^3c^3d^4 + 36a^5b^2c^2d^5 + 1716ab^6c^6d + 8a^6b^3cd^6)}{51480b^8} + \frac{(d^7x^7)}{(8b)} + \frac{(7d^2x^2(a^5d^5 + 792b^5c^5 + 120a^2b^3c^3d^2 + 36a^3b^2c^2d^3 + 330ab^4c^4d + 8a^4b^3cd^4))}{(3432b^6)} + \frac{(7d^4x^4(a^3d^3 + 120b^3c^3 + 36ab^2c^2d + 8a^2b^3cd^2))}{(264b^4)} + \frac{(7d^6x^6(a^2d + 8b^2c))}{(72b^2)} + \frac{(7d^3x^3(a^4d^4 + 330b^4c^4 + 36a^2b^2c^2d^2 + 120ab^3c^3d + 8a^3b^2cd^3))}{(792b^5)} + \frac{(d^2x^2(a^6d^6 + 1716b^6c^6 + 330a^2b^4c^4d^2 + 120a^3b^3c^3d^3 + 36a^4b^2c^2d^4 + 792ab^5c^5d + 8a^5b^4cd^5))}{(3432b^7)} + \frac{(7d^5x^5(a^2d^2 + 36b^2c^2 + 8ab^2cd))}{(120b^3)} / (a^{15} + b^{15}x^{15} + 15a^2b^{14}x^{14} + 105a^{13}b^2x^2 + 455a^{12}b^3x^3 + 1365a^{11}b^4x^4 + 3003a^{10}b^5x^5 + 5005a^9b^6x^6 + 6435a^8b^7x^7 + 6435a^7b^8x^8 + 5005a^6b^9x^9 + 3003a^5b^{10}x^{10} + 1365a^4b^{11}x^{11} + 455a^3b^{12}x^{12} + 105a^2b^{13}x^{13} + 15a^{14}bx)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**7/(b*x+a)**16,x)

[Out] Timed out

3.1299 $\int (a + bx)^{12}(c + dx)^{10} dx$

Optimal. Leaf size=275

$$\frac{5d^9(a+bx)^{22}(bc-ad)}{11b^{11}} + \frac{15d^8(a+bx)^{21}(bc-ad)^2}{7b^{11}} + \frac{6d^7(a+bx)^{20}(bc-ad)^3}{b^{11}} + \frac{210d^6(a+bx)^{19}(bc-ad)^4}{19b^{11}} + \frac{14d^5(a+bx)^{18}(bc-ad)^5}{11b^{11}}$$

[Out] $1/13*(-a*d+b*c)^{10}*(b*x+a)^{13}/b^{11}+5/7*d*(-a*d+b*c)^9*(b*x+a)^{14}/b^{11}+3*d^2*(-a*d+b*c)^8*(b*x+a)^{15}/b^{11}+15/2*d^3*(-a*d+b*c)^7*(b*x+a)^{16}/b^{11}+210/17*d^4*(-a*d+b*c)^6*(b*x+a)^{17}/b^{11}+14*d^5*(-a*d+b*c)^5*(b*x+a)^{18}/b^{11}+210/19*d^6*(-a*d+b*c)^4*(b*x+a)^{19}/b^{11}+6*d^7*(-a*d+b*c)^3*(b*x+a)^{20}/b^{11}+15/7*d^8*(-a*d+b*c)^2*(b*x+a)^{21}/b^{11}+5/11*d^9*(-a*d+b*c)*(b*x+a)^{22}/b^{11}+1/23*d^{10}*(b*x+a)^{23}/b^{11}$

Rubi [A] time = 1.47, antiderivative size = 275, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{5d^9(a+bx)^{22}(bc-ad)}{11b^{11}} + \frac{15d^8(a+bx)^{21}(bc-ad)^2}{7b^{11}} + \frac{6d^7(a+bx)^{20}(bc-ad)^3}{b^{11}} + \frac{210d^6(a+bx)^{19}(bc-ad)^4}{19b^{11}} + \frac{14d^5(a+bx)^{18}(bc-ad)^5}{11b^{11}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^12*(c + d*x)^10,x]

[Out] $((b*c - a*d)^{10}*(a + b*x)^{13})/(13*b^{11}) + (5*d*(b*c - a*d)^9*(a + b*x)^{14})/(7*b^{11}) + (3*d^2*(b*c - a*d)^8*(a + b*x)^{15})/b^{11} + (15*d^3*(b*c - a*d)^7*(a + b*x)^{16})/(2*b^{11}) + (210*d^4*(b*c - a*d)^6*(a + b*x)^{17})/(17*b^{11}) + (14*d^5*(b*c - a*d)^5*(a + b*x)^{18})/b^{11} + (210*d^6*(b*c - a*d)^4*(a + b*x)^{19})/(19*b^{11}) + (6*d^7*(b*c - a*d)^3*(a + b*x)^{20})/b^{11} + (15*d^8*(b*c - a*d)^2*(a + b*x)^{21})/(7*b^{11}) + (5*d^9*(b*c - a*d)*(a + b*x)^{22})/(11*b^{11}) + (d^{10}*(a + b*x)^{23})/(23*b^{11})$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
& 5*b^3*c^3*d^5 + 924*a^6*b^2*c^2*d^6 + 176*a^7*b*c*d^7 + 11*a^8*d^8)*x^{15} + \\
& (3*b^5*d^3*(5*b^7*c^7 + 105*a*b^6*c^6*d + 693*a^2*b^5*c^5*d^2 + 1925*a^3*b^4*c^4*d^3 + 2475*a^4*b^3*c^3*d^4 + 1485*a^5*b^2*c^2*d^5 + 385*a^6*b*c*d^6 + \\
& 33*a^7*d^7)*x^{16})/2 + (3*b^6*d^4*(70*b^6*c^6 + 1008*a*b^5*c^5*d + 4620*a^2*b^4*c^4*d^2 + 8800*a^3*b^3*c^3*d^3 + 7425*a^4*b^2*c^2*d^4 + 2640*a^5*b*c*d^5 + 308*a^6*d^6)*x^{17})/17 + b^7*d^5*(14*b^5*c^5 + 140*a*b^4*c^4*d + 440*a^2*b^3*c^3*d^2 + 550*a^3*b^2*c^2*d^3 + 275*a^4*b*c*d^4 + 44*a^5*d^5)*x^{18} + \\
& (5*b^8*d^6*(42*b^4*c^4 + 288*a*b^3*c^3*d + 594*a^2*b^2*c^2*d^2 + 440*a^3*b*c*d^3 + 99*a^4*d^4)*x^{19})/19 + b^9*d^7*(6*b^3*c^3 + 27*a*b^2*c^2*d + 33*a^2*b*c*d^2 + 11*a^3*d^3)*x^{20} + (b^{10}*d^8*(15*b^2*c^2 + 40*a*b*c*d + 22*a^2*d^2)*x^{21})/7 + (b^{11}*d^9*(5*b*c + 6*a*d)*x^{22})/11 + (b^{12}*d^{10}*x^{23})/23
\end{aligned}$$

fricas [B] time = 0.39, size = 2186, normalized size = 7.95

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^12*(d*x+c)^10,x, algorithm="fricas")

[Out] $1/23*x^{23}*d^{10}*b^{12} + 5/11*x^{22}*d^9*c*b^{12} + 6/11*x^{22}*d^{10}*b^{11}*a + 15/7*x^{21}*d^8*c^2*b^{12} + 40/7*x^{21}*d^9*c*b^{11}*a + 22/7*x^{21}*d^{10}*b^{10}*a^2 + 6*x^{20}*d^7*c^3*b^{12} + 27*x^{20}*d^8*c^2*b^{11}*a + 33*x^{20}*d^9*c*b^{10}*a^2 + 11*x^{20}*d^{10}*b^9*a^3 + 210/19*x^{19}*d^6*c^4*b^{12} + 1440/19*x^{19}*d^7*c^3*b^{11}*a + 2970/19*x^{19}*d^8*c^2*b^{10}*a^2 + 2200/19*x^{19}*d^9*c*b^9*a^3 + 495/19*x^{19}*d^{10}*b^8*a^4 + 14*x^{18}*d^5*c^5*b^{12} + 140*x^{18}*d^6*c^4*b^{11}*a + 440*x^{18}*d^7*c^3*b^{10}*a^2 + 550*x^{18}*d^8*c^2*b^9*a^3 + 275*x^{18}*d^9*c*b^8*a^4 + 44*x^{18}*d^{10}*b^7*a^5 + 210/17*x^{17}*d^4*c^6*b^{12} + 3024/17*x^{17}*d^5*c^5*b^{11}*a + 13860/17*x^{17}*d^6*c^4*b^{10}*a^2 + 26400/17*x^{17}*d^7*c^3*b^9*a^3 + 22275/17*x^{17}*d^8*c^2*b^8*a^4 + 7920/17*x^{17}*d^9*c*b^7*a^5 + 924/17*x^{17}*d^{10}*b^6*a^6 + 15/2*x^{16}*d^3*c^7*b^{12} + 315/2*x^{16}*d^4*c^6*b^{11}*a + 2079/2*x^{16}*d^5*c^5*b^{10}*a^2 + 5775/2*x^{16}*d^6*c^4*b^9*a^3 + 7425/2*x^{16}*d^7*c^3*b^8*a^4 + 4455/2*x^{16}*d^8*c^2*b^7*a^5 + 1155/2*x^{16}*d^9*c*b^6*a^6 + 99/2*x^{16}*d^{10}*b^5*a^7 + 3*x^{15}*d^2*c^8*b^{12} + 96*x^{15}*d^3*c^7*b^{11}*a + 924*x^{15}*d^4*c^6*b^{10}*a^2 + 3696*x^{15}*d^5*c^5*b^9*a^3 + 6930*x^{15}*d^6*c^4*b^8*a^4 + 6336*x^{15}*d^7*c^3*b^7*a^5 + 2772*x^{15}*d^8*c^2*b^6*a^6 + 528*x^{15}*d^9*c*b^5*a^7 + 33*x^{15}*d^{10}*b^4*a^8 + 5/7*x^{14}*d*c^9*b^{12} + 270/7*x^{14}*d^2*c^8*b^{11}*a + 3960/7*x^{14}*d^3*c^7*b^{10}*a^2 + 3300*x^{14}*d^4*c^6*b^9*a^3 + 8910*x^{14}*d^5*c^5*b^8*a^4 + 11880*x^{14}*d^6*c^4*b^7*a^5 + 7920*x^{14}*d^7*c^3*b^6*a^6 + 17820/7*x^{14}*d^8*c^2*b^5*a^7 + 2475/7*x^{14}*d^9*c*b^4*a^8 + 110/7*x^{14}*d^{10}*b^3*a^9 + 1/13*x^{13}*c^{10}*b^{12} + 120/13*x^{13}*d*c^9*b^{11}*a + 2970/13*x^{13}*d^2*c^8*b^{10}*a^2 + 26400/13*x^{13}*d^3*c^7*b^9*a^3 + 103950/13*x^{13}*d^4*c^6*b^8*a^4 + 199584/13*x^{13}*d^5*c^5*b^7*a^5 + 194040/13*x^{13}*d^6*c^4*b^6*a^6 + 95040/13*x^{13}*d^7*c^3*b^5*a^7 + 22275/13*x^{13}*d^8*c^2*b^4*a^8 + 2200/13*x^{13}*d^9*c*b^3*a^9 + 66/13*x^{13}*d^{10}*b^2*a^{10} + x^{12}*c^{10}*b^{11}*a + 55*x^{12}*d*c^9*b^{10}*a^2 + 825*x^{12}*d^2*c^8*b^9*a^3 + 4950*x^{12}*d^3*c^7*b^8*a^4 + 13860*x^{12}*d^4*c^6*b^7*a^5 + 19$

$$\begin{aligned}
& 404*x^{12}*d^5*c^5*b^6*a^6 + 13860*x^{12}*d^6*c^4*b^5*a^7 + 4950*x^{12}*d^7*c^3*b^4*a^8 + 825*x^{12}*d^8*c^2*b^3*a^9 + 55*x^{12}*d^9*c*b^2*a^{10} + x^{12}*d^{10}*b*a^{11} \\
& + 6*x^{11}*c^{10}*b^{10}*a^2 + 200*x^{11}*d*c^9*b^9*a^3 + 2025*x^{11}*d^2*c^8*b^8*a^4 + 8640*x^{11}*d^3*c^7*b^7*a^5 + 17640*x^{11}*d^4*c^6*b^6*a^6 + 18144*x^{11}*d^5*c^5*b^5*a^7 \\
& + 9450*x^{11}*d^6*c^4*b^4*a^8 + 2400*x^{11}*d^7*c^3*b^3*a^9 + 270*x^{11}*d^8*c^2*b^2*a^{10} + 120/11*x^{11}*d^9*c*b*a^{11} + 1/11*x^{11}*d^{10}*a^{12} + 22*x^{10}*c^{10}*b^9*a^3 \\
& + 495*x^{10}*d*c^9*b^8*a^4 + 3564*x^{10}*d^2*c^8*b^7*a^5 + 11088*x^{10}*d^3*c^7*b^6*a^6 + 16632*x^{10}*d^4*c^6*b^5*a^7 + 12474*x^{10}*d^5*c^5*b^4*a^8 + 4620*x^{10}*d^6*c^4*b^3*a^9 \\
& + 792*x^{10}*d^7*c^3*b^2*a^{10} + 54*x^{10}*d^8*c^2*b*a^{11} + x^{10}*d^9*c*a^{12} + 55*x^9*c^{10}*b^8*a^4 + 880*x^9*d*c^9*b^7*a^5 + 4620*x^9*d^2*c^8*b^6*a^6 + 10560*x^9*d^3*c^7*b^5*a^7 \\
& + 11550*x^9*d^4*c^6*b^4*a^8 + 6160*x^9*d^5*c^5*b^3*a^9 + 1540*x^9*d^6*c^4*b^2*a^{10} + 160*x^9*d^7*c^3*b*a^{11} + 5*x^9*d^8*c^2*a^{12} + 99*x^8*c^{10}*b^7*a^5 + 1155*x^8*d*c^9*b^6*a^6 \\
& + 4455*x^8*d^2*c^8*b^5*a^7 + 7425*x^8*d^3*c^7*b^4*a^8 + 5775*x^8*d^4*c^6*b^3*a^9 + 2079*x^8*d^5*c^5*b^2*a^{10} + 315*x^8*d^6*c^4*b*a^{11} + 15*x^8*d^7*c^3*a^{12} + 132*x^7*c^{10}*b^6*a^6 \\
& + 7920/7*x^7*d*c^9*b^5*a^7 + 22275/7*x^7*d^2*c^8*b^4*a^8 + 26400/7*x^7*d^3*c^7*b^3*a^9 + 1980*x^7*d^4*c^6*b^2*a^{10} + 432*x^7*d^5*c^5*b*a^{11} + 30*x^7*d^6*c^4*a^{12} + 132*x^6*c^{10}*b^5*a^7 \\
& + 825*x^6*d*c^9*b^4*a^8 + 1650*x^6*d^2*c^8*b^3*a^9 + 1320*x^6*d^3*c^7*b^2*a^{10} + 420*x^6*d^4*c^6*b*a^{11} + 42*x^6*d^5*c^5*a^{12} + 99*x^5*c^{10}*b^4*a^8 + 440*x^5*d*c^9*b^3*a^9 \\
& + 594*x^5*d^2*c^8*b^2*a^{10} + 288*x^5*d^3*c^7*b*a^{11} + 42*x^5*d^4*c^6*a^{12} + 55*x^4*c^{10}*b^3*a^9 + 165*x^4*d*c^9*b^2*a^{10} + 135*x^4*d^2*c^8*b*a^{11} + 30*x^4*d^3*c^7*a^{12} \\
& + 22*x^3*c^{10}*b^2*a^{10} + 40*x^3*d*c^9*b*a^{11} + 15*x^3*d^2*c^8*a^{12} + 6*x^2*c^{10}*b*a^{11} + 5*x^2*d*c^9*a^{12} + x*c^{10}*a^{12}
\end{aligned}$$

giac [B] time = 1.31, size = 2186, normalized size = 7.95

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^12*(d*x+c)^10,x, algorithm="giac")

[Out] 1/23*b^12*d^10*x^23 + 5/11*b^12*c*d^9*x^22 + 6/11*a*b^11*d^10*x^22 + 15/7*b^12*c^2*d^8*x^21 + 40/7*a*b^11*c*d^9*x^21 + 22/7*a^2*b^10*d^10*x^21 + 6*b^12*c^3*d^7*x^20 + 27*a*b^11*c^2*d^8*x^20 + 33*a^2*b^10*c*d^9*x^20 + 11*a^3*b^9*d^10*x^20 + 210/19*b^12*c^4*d^6*x^19 + 1440/19*a*b^11*c^3*d^7*x^19 + 2970/19*a^2*b^10*c^2*d^8*x^19 + 2200/19*a^3*b^9*c*d^9*x^19 + 495/19*a^4*b^8*d^10*x^19 + 14*b^12*c^5*d^5*x^18 + 140*a*b^11*c^4*d^6*x^18 + 440*a^2*b^10*c^3*d^7*x^18 + 550*a^3*b^9*c^2*d^8*x^18 + 275*a^4*b^8*c*d^9*x^18 + 44*a^5*b^7*d^10*x^18 + 210/17*b^12*c^6*d^4*x^17 + 3024/17*a*b^11*c^5*d^5*x^17 + 13860/17*a^2*b^10*c^4*d^6*x^17 + 26400/17*a^3*b^9*c^3*d^7*x^17 + 22275/17*a^4*b^8*c^2*d^8*x^17 + 7920/17*a^5*b^7*c*d^9*x^17 + 924/17*a^6*b^6*d^10*x^17 + 15/2*b^12*c^7*d^3*x^16 + 315/2*a*b^11*c^6*d^4*x^16 + 2079/2*a^2*b^10*c^5*d^5*x^16 + 5775/2*a^3*b^9*c^4*d^6*x^16 + 7425/2*a^4*b^8*c^3*d^7*x^16 + 4455/2*a^

$$\begin{aligned}
& 5*b^7*c^2*d^8*x^{16} + 1155/2*a^6*b^6*c*d^9*x^{16} + 99/2*a^7*b^5*d^{10}*x^{16} + 3 \\
& *b^{12}*c^8*d^2*x^{15} + 96*a*b^{11}*c^7*d^3*x^{15} + 924*a^2*b^{10}*c^6*d^4*x^{15} + 3 \\
& 696*a^3*b^9*c^5*d^5*x^{15} + 6930*a^4*b^8*c^4*d^6*x^{15} + 6336*a^5*b^7*c^3*d^7 \\
& *x^{15} + 2772*a^6*b^6*c^2*d^8*x^{15} + 528*a^7*b^5*c*d^9*x^{15} + 33*a^8*b^4*d^1 \\
& 0*x^{15} + 5/7*b^{12}*c^9*d*x^{14} + 270/7*a*b^{11}*c^8*d^2*x^{14} + 3960/7*a^2*b^{10} \\
& c^7*d^3*x^{14} + 3300*a^3*b^9*c^6*d^4*x^{14} + 8910*a^4*b^8*c^5*d^5*x^{14} + 1188 \\
& 0*a^5*b^7*c^4*d^6*x^{14} + 7920*a^6*b^6*c^3*d^7*x^{14} + 17820/7*a^7*b^5*c^2*d^ \\
& 8*x^{14} + 2475/7*a^8*b^4*c*d^9*x^{14} + 110/7*a^9*b^3*d^{10}*x^{14} + 1/13*b^{12}*c^ \\
& 10*x^{13} + 120/13*a*b^{11}*c^9*d*x^{13} + 2970/13*a^2*b^{10}*c^8*d^2*x^{13} + 26400/ \\
& 13*a^3*b^9*c^7*d^3*x^{13} + 103950/13*a^4*b^8*c^6*d^4*x^{13} + 199584/13*a^5*b^ \\
& 7*c^5*d^5*x^{13} + 194040/13*a^6*b^6*c^4*d^6*x^{13} + 95040/13*a^7*b^5*c^3*d^7* \\
& x^{13} + 22275/13*a^8*b^4*c^2*d^8*x^{13} + 2200/13*a^9*b^3*c*d^9*x^{13} + 66/13*a \\
& ^{10}*b^2*d^{10}*x^{13} + a*b^{11}*c^{10}*x^{12} + 55*a^2*b^{10}*c^9*d*x^{12} + 825*a^3*b^9 \\
& *c^8*d^2*x^{12} + 4950*a^4*b^8*c^7*d^3*x^{12} + 13860*a^5*b^7*c^6*d^4*x^{12} + 19 \\
& 404*a^6*b^6*c^5*d^5*x^{12} + 13860*a^7*b^5*c^4*d^6*x^{12} + 4950*a^8*b^4*c^3*d^ \\
& 7*x^{12} + 825*a^9*b^3*c^2*d^8*x^{12} + 55*a^{10}*b^2*c*d^9*x^{12} + a^{11}*b*d^{10}*x^ \\
& 12 + 6*a^2*b^{10}*c^{10}*x^{11} + 200*a^3*b^9*c^9*d*x^{11} + 2025*a^4*b^8*c^8*d^2*x \\
& ^{11} + 8640*a^5*b^7*c^7*d^3*x^{11} + 17640*a^6*b^6*c^6*d^4*x^{11} + 18144*a^7*b^ \\
& 5*c^5*d^5*x^{11} + 9450*a^8*b^4*c^4*d^6*x^{11} + 2400*a^9*b^3*c^3*d^7*x^{11} + 27 \\
& 0*a^{10}*b^2*c^2*d^8*x^{11} + 120/11*a^{11}*b*c*d^9*x^{11} + 1/11*a^{12}*d^{10}*x^{11} + \\
& 22*a^3*b^9*c^{10}*x^{10} + 495*a^4*b^8*c^9*d*x^{10} + 3564*a^5*b^7*c^8*d^2*x^{10} + \\
& 11088*a^6*b^6*c^7*d^3*x^{10} + 16632*a^7*b^5*c^6*d^4*x^{10} + 12474*a^8*b^4*c^ \\
& 5*d^5*x^{10} + 4620*a^9*b^3*c^4*d^6*x^{10} + 792*a^{10}*b^2*c^3*d^7*x^{10} + 54*a^1 \\
& 1*b*c^2*d^8*x^{10} + a^{12}*c*d^9*x^{10} + 55*a^4*b^8*c^{10}*x^9 + 880*a^5*b^7*c^9* \\
& d*x^9 + 4620*a^6*b^6*c^8*d^2*x^9 + 10560*a^7*b^5*c^7*d^3*x^9 + 11550*a^8*b^ \\
& 4*c^6*d^4*x^9 + 6160*a^9*b^3*c^5*d^5*x^9 + 1540*a^{10}*b^2*c^4*d^6*x^9 + 160* \\
& a^{11}*b*c^3*d^7*x^9 + 5*a^{12}*c^2*d^8*x^9 + 99*a^5*b^7*c^{10}*x^8 + 1155*a^6*b^ \\
& 6*c^9*d*x^8 + 4455*a^7*b^5*c^8*d^2*x^8 + 7425*a^8*b^4*c^7*d^3*x^8 + 5775*a^ \\
& 9*b^3*c^6*d^4*x^8 + 2079*a^{10}*b^2*c^5*d^5*x^8 + 315*a^{11}*b*c^4*d^6*x^8 + 15 \\
& *a^{12}*c^3*d^7*x^8 + 132*a^6*b^6*c^{10}*x^7 + 7920/7*a^7*b^5*c^9*d*x^7 + 22275 \\
& /7*a^8*b^4*c^8*d^2*x^7 + 26400/7*a^9*b^3*c^7*d^3*x^7 + 1980*a^{10}*b^2*c^6*d^ \\
& 4*x^7 + 432*a^{11}*b*c^5*d^5*x^7 + 30*a^{12}*c^4*d^6*x^7 + 132*a^7*b^5*c^{10}*x^6 \\
& + 825*a^8*b^4*c^9*d*x^6 + 1650*a^9*b^3*c^8*d^2*x^6 + 1320*a^{10}*b^2*c^7*d^3 \\
& *x^6 + 420*a^{11}*b*c^6*d^4*x^6 + 42*a^{12}*c^5*d^5*x^6 + 99*a^8*b^4*c^{10}*x^5 + \\
& 440*a^9*b^3*c^9*d*x^5 + 594*a^{10}*b^2*c^8*d^2*x^5 + 288*a^{11}*b*c^7*d^3*x^5 \\
& + 42*a^{12}*c^6*d^4*x^5 + 55*a^9*b^3*c^{10}*x^4 + 165*a^{10}*b^2*c^9*d*x^4 + 135* \\
& a^{11}*b*c^8*d^2*x^4 + 30*a^{12}*c^7*d^3*x^4 + 22*a^{10}*b^2*c^{10}*x^3 + 40*a^{11}*b \\
& *c^9*d*x^3 + 15*a^{12}*c^8*d^2*x^3 + 6*a^{11}*b*c^{10}*x^2 + 5*a^{12}*c^9*d*x^2 + a \\
& ^{12}*c^{10}*x
\end{aligned}$$

maple [B] time = 0.00, size = 1891, normalized size = 6.88

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x+a)^{12}*(d*x+c)^{10}, x)$

[Out] $\frac{1}{23}b^{12}d^{10}x^{23} + \frac{1}{22}(12ab^{11}d^{10} + 10b^{12}cd^9)x^{22} + \frac{1}{21}(66a^2b^{10}d^{10} + 120a^2b^{11}cd^9 + 45b^{12}c^2d^8)x^{21} + \frac{1}{20}(220a^3b^9d^{10} + 660a^2b^{10}cd^9 + 540a^2b^{11}c^2d^8 + 120b^{12}c^3d^7)x^{20} + \frac{1}{19}(495a^4b^8d^{10} + 2200a^3b^9cd^9 + 2970a^2b^{10}c^2d^8 + 1440ab^{11}c^3d^7 + 210b^{12}c^4d^6)x^{19} + \frac{1}{18}(792a^5b^7d^{10} + 4950a^4b^8cd^9 + 9900a^3b^9c^2d^8 + 7920a^2b^{10}c^3d^7 + 2520ab^{11}c^4d^6 + 252b^{12}c^5d^5)x^{18} + \frac{1}{17}(924a^6b^6d^{10} + 7920a^5b^7cd^9 + 22275a^4b^8c^2d^8 + 26400a^3b^9c^3d^7 + 13860a^2b^{10}c^4d^6 + 3024a^2b^{11}c^5d^5 + 210b^{12}c^6d^4)x^{17} + \frac{1}{16}(792a^7b^5d^{10} + 9240a^6b^6cd^9 + 35640a^5b^7c^2d^8 + 59400a^4b^8c^3d^7 + 46200a^3b^9c^4d^6 + 16632a^2b^{10}c^5d^5 + 2520ab^{11}c^6d^4 + 120b^{12}c^7d^3)x^{16} + \frac{1}{15}(495a^8b^4d^{10} + 7920a^7b^5cd^9 + 41580a^6b^6c^2d^8 + 95040a^5b^7c^3d^7 + 103950a^4b^8c^4d^6 + 55440a^3b^9c^5d^5 + 13860a^2b^{10}c^6d^4 + 1440ab^{11}c^7d^3 + 45b^{12}c^8d^2)x^{15} + \frac{1}{14}(220a^9b^3d^{10} + 4950a^8b^4cd^9 + 35640a^7b^5c^2d^8 + 110880a^6b^6c^3d^7 + 166320a^5b^7c^4d^6 + 124740a^4b^8c^5d^5 + 46200a^3b^9c^6d^4 + 7920a^2b^{10}c^7d^3 + 540ab^{11}c^8d^2 + 10b^{12}c^9d)x^{14} + \frac{1}{13}(66a^{10}b^2d^{10} + 2200a^9b^3cd^9 + 22275a^8b^4c^2d^8 + 95040a^7b^5c^3d^7 + 194040a^6b^6c^4d^6 + 199584a^5b^7c^5d^5 + 103950a^4b^8c^6d^4 + 26400a^3b^9c^7d^3 + 2970a^2b^{10}c^8d^2 + 120ab^{11}c^9d + b^{12}c^{10})x^{13} + \frac{1}{12}(12a^{11}b^1d^{10} + 660a^{10}b^2cd^9 + 9900a^9b^3c^2d^8 + 59400a^8b^4c^3d^7 + 166320a^7b^5c^4d^6 + 232848a^6b^6c^5d^5 + 166320a^5b^7c^6d^4 + 59400a^4b^8c^7d^3 + 9900a^3b^9c^8d^2 + 660a^2b^{10}c^9d + 12ab^{11}c^{10})x^{12} + \frac{1}{11}(a^{12}d^{10} + 120a^{11}b^1cd^9 + 2970a^{10}b^2c^2d^8 + 26400a^9b^3c^3d^7 + 103950a^8b^4c^4d^6 + 199584a^7b^5c^5d^5 + 194040a^6b^6c^6d^4 + 95040a^5b^7c^7d^3 + 22275a^4b^8c^8d^2 + 2200a^3b^9c^9d + 66a^2b^{10}c^{10})x^{11} + \frac{1}{10}(10a^{12}cd^9 + 540a^{11}b^2cd^8 + 7920a^{10}b^2c^3d^7 + 46200a^9b^3c^4d^6 + 124740a^8b^4c^5d^5 + 166320a^7b^5c^6d^4 + 110880a^6b^6c^7d^3 + 35640a^5b^7c^8d^2 + 4950a^4b^8c^9d + 220a^3b^9c^{10})x^{10} + \frac{1}{9}(45a^{12}c^2d^8 + 1440a^{11}b^3cd^7 + 13860a^{10}b^2c^4d^6 + 55440a^9b^3c^5d^5 + 103950a^8b^4c^6d^4 + 95040a^7b^5c^7d^3 + 41580a^6b^6c^8d^2 + 7920a^5b^7c^9d + 495a^4b^8c^{10})x^9 + \frac{1}{8}(120a^{12}c^3d^7 + 2520a^{11}b^4cd^6 + 16632a^{10}b^2c^5d^5 + 46200a^9b^3c^6d^4 + 59400a^8b^4c^7d^3 + 35640a^7b^5c^8d^2 + 9240a^6b^6c^9d + 792a^5b^7c^{10})x^8 + \frac{1}{7}(210a^{12}c^4d^6 + 3024a^{11}b^5cd^5 + 13860a^{10}b^2c^6d^4 + 26400a^9b^3c^7d^3 + 22275a^8b^4c^8d^2 + 7920a^7b^5c^9d + 924a^6b^6c^{10})x^7 + \frac{1}{6}(252a^{12}c^5d^5 + 2520a^{11}b^6cd^4 + 7920a^{10}b^2c^7d^3 + 9900a^9b^3c^8d^2 + 4950a^8b^4c^9d + 792a^7b^5c^{10})x^6 + \frac{1}{5}(210a^{12}c^6d^4 + 1440a^{11}b^7cd^3 + 2970a^{10}b^2c^8d^2 + 2200a^9b^3c^9d + 495a^8b^4c^{10})x^5 + \frac{1}{4}(120a^{12}c^7d^3 + 540a^{11}b^8cd^2 + 660a^{10}b^2c^9d + 220a^9b^3c^{10})x^4 + \frac{1}{3}(45a^{12}c^8d^2 + 120a^{11}b^9cd + 66a^{10}b^2c^{10})x^3 + \frac{1}{2}(10a^{12}c^9d + 12a^{11}b^{10}cd)x^2 + a^{12}c^{10}x$

maxima [B] time = 1.55, size = 1877, normalized size = 6.83

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^12*(d*x+c)^10,x, algorithm="maxima")

[Out] $\frac{1}{23}b^{12}d^{10}x^{23} + a^{12}c^{10}x + \frac{1}{11}(5b^{12}c^9d + 6a^2b^{11}d^{10})x^{22} + \frac{1}{7}(15b^{12}c^2d^8 + 40a^2b^{11}c^2d^9 + 22a^2b^{10}d^{10})x^{21} + (6b^{12}c^3d^7 + 27a^2b^{11}c^2d^8 + 33a^2b^{10}c^2d^9 + 11a^3b^9d^{10})x^{20} + \frac{5}{19}(42b^{12}c^4d^6 + 288a^2b^{11}c^3d^7 + 594a^2b^{10}c^2d^8 + 440a^3b^9c^2d^9 + 99a^4b^8d^{10})x^{19} + (14b^{12}c^5d^5 + 140a^2b^{11}c^4d^6 + 440a^2b^{10}c^3d^7 + 550a^3b^9c^2d^8 + 275a^4b^8c^2d^9 + 44a^5b^7d^{10})x^{18} + \frac{3}{17}(70b^{12}c^6d^4 + 1008a^2b^{11}c^5d^5 + 4620a^2b^{10}c^4d^6 + 8800a^3b^9c^3d^7 + 7425a^4b^8c^2d^8 + 2640a^5b^7c^2d^9 + 308a^6b^6d^{10})x^{17} + \frac{3}{2}(5b^{12}c^7d^3 + 105a^2b^{11}c^6d^4 + 693a^2b^{10}c^5d^5 + 1925a^3b^9c^4d^6 + 2475a^4b^8c^3d^7 + 1485a^5b^7c^2d^8 + 385a^6b^6c^2d^9 + 33a^7b^5d^{10})x^{16} + 3(b^{12}c^8d^2 + 32a^2b^{11}c^7d^3 + 308a^2b^{10}c^6d^4 + 1232a^3b^9c^5d^5 + 2310a^4b^8c^4d^6 + 2112a^5b^7c^3d^7 + 924a^6b^6c^2d^8 + 176a^7b^5c^2d^9 + 11a^8b^4d^{10})x^{15} + \frac{5}{7}(b^{12}c^9d + 54a^2b^{11}c^8d^2 + 792a^2b^{10}c^7d^3 + 4620a^3b^9c^6d^4 + 12474a^4b^8c^5d^5 + 16632a^5b^7c^4d^6 + 11088a^6b^6c^3d^7 + 3564a^7b^5c^2d^8 + 495a^8b^4c^2d^9 + 22a^9b^3d^{10})x^{14} + \frac{1}{13}(b^{12}c^{10} + 120a^2b^{11}c^9d + 2970a^2b^{10}c^8d^2 + 26400a^3b^9c^7d^3 + 103950a^4b^8c^6d^4 + 199584a^5b^7c^5d^5 + 194040a^6b^6c^4d^6 + 95040a^7b^5c^3d^7 + 22275a^8b^4c^2d^8 + 2200a^9b^3c^2d^9 + 66a^{10}b^2d^{10})x^{13} + (a^2b^{11}c^{10} + 55a^2b^{10}c^9d + 825a^3b^9c^8d^2 + 4950a^4b^8c^7d^3 + 13860a^5b^7c^6d^4 + 19404a^6b^6c^5d^5 + 13860a^7b^5c^4d^6 + 4950a^8b^4c^3d^7 + 825a^9b^3c^2d^8 + 55a^{10}b^2c^2d^9 + a^{11}b^2d^{10})x^{12} + \frac{1}{11}(66a^2b^{10}c^{10} + 2200a^3b^9c^9d + 22275a^4b^8c^8d^2 + 95040a^5b^7c^7d^3 + 194040a^6b^6c^6d^4 + 199584a^7b^5c^5d^5 + 103950a^8b^4c^4d^6 + 26400a^9b^3c^3d^7 + 2970a^{10}b^2c^2d^8 + 120a^{11}b^2c^2d^9 + a^{12}d^{10})x^{11} + (22a^3b^9c^{10} + 495a^4b^8c^9d + 3564a^5b^7c^8d^2 + 11088a^6b^6c^7d^3 + 16632a^7b^5c^6d^4 + 12474a^8b^4c^5d^5 + 4620a^9b^3c^4d^6 + 792a^{10}b^2c^3d^7 + 54a^{11}b^2c^2d^8 + a^{12}c^2d^9)x^{10} + 5(11a^4b^8c^{10} + 176a^5b^7c^9d + 924a^6b^6c^8d^2 + 2112a^7b^5c^7d^3 + 2310a^8b^4c^6d^4 + 1232a^9b^3c^5d^5 + 308a^{10}b^2c^4d^6 + 32a^{11}b^2c^3d^7 + a^{12}c^2d^8)x^9 + 3(33a^5b^7c^{10} + 385a^6b^6c^9d + 1485a^7b^5c^8d^2 + 2475a^8b^4c^7d^3 + 1925a^9b^3c^6d^4 + 693a^{10}b^2c^5d^5 + 105a^{11}b^2c^4d^6 + 5a^{12}c^3d^7)x^8 + \frac{3}{7}(308a^6b^6c^{10} + 2640a^7b^5c^9d + 7425a^8b^4c^8d^2 + 8800a^9b^3c^7d^3 + 4620a^{10}b^2c^6d^4 + 1008a^{11}b^2c^5d^5 + 70a^{12}c^4d^6)x^7 + 3(44a^7b^5c^{10} + 275a^8b^4c^9d + 550a^9b^3$

$$\begin{aligned} & *c^8*d^2 + 440*a^{10}*b^2*c^7*d^3 + 140*a^{11}*b*c^6*d^4 + 14*a^{12}*c^5*d^5)*x^6 \\ & + (99*a^8*b^4*c^{10} + 440*a^9*b^3*c^9*d + 594*a^{10}*b^2*c^8*d^2 + 288*a^{11}*b \\ & *c^7*d^3 + 42*a^{12}*c^6*d^4)*x^5 + 5*(11*a^9*b^3*c^{10} + 33*a^{10}*b^2*c^9*d + \\ & 27*a^{11}*b*c^8*d^2 + 6*a^{12}*c^7*d^3)*x^4 + (22*a^{10}*b^2*c^{10} + 40*a^{11}*b*c^9 \\ & *d + 15*a^{12}*c^8*d^2)*x^3 + (6*a^{11}*b*c^{10} + 5*a^{12}*c^9*d)*x^2 \end{aligned}$$

mupad [B] time = 0.98, size = 1847, normalized size = 6.72

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^{12}*(c + d*x)^{10}, x)$

[Out] $x^{12}*(a*b^{11}*c^{10} + a^{11}*b*d^{10} + 55*a^2*b^{10}*c^9*d + 55*a^{10}*b^2*c*d^9 + 8$
 $25*a^3*b^9*c^8*d^2 + 4950*a^4*b^8*c^7*d^3 + 13860*a^5*b^7*c^6*d^4 + 19404*a$
 $^6*b^6*c^5*d^5 + 13860*a^7*b^5*c^4*d^6 + 4950*a^8*b^4*c^3*d^7 + 825*a^9*b^3$
 $*c^2*d^8) + x^7*(132*a^6*b^6*c^{10} + 30*a^{12}*c^4*d^6 + (7920*a^7*b^5*c^9*d)/$
 $7 + 432*a^{11}*b*c^5*d^5 + (22275*a^8*b^4*c^8*d^2)/7 + (26400*a^9*b^3*c^7*d^3$
 $)/7 + 1980*a^{10}*b^2*c^6*d^4) + x^{17}*((924*a^6*b^6*d^{10})/17 + (210*b^{12}*c^6*$
 $d^4)/17 + (3024*a*b^{11}*c^5*d^5)/17 + (7920*a^5*b^7*c*d^9)/17 + (13860*a^2*b$
 $^{10}*c^4*d^6)/17 + (26400*a^3*b^9*c^3*d^7)/17 + (22275*a^4*b^8*c^2*d^8)/17)$
 $+ x^5*(99*a^8*b^4*c^{10} + 42*a^{12}*c^6*d^4 + 440*a^9*b^3*c^9*d + 288*a^{11}*b*c$
 $^7*d^3 + 594*a^{10}*b^2*c^8*d^2) + x^{19}*((495*a^4*b^8*d^{10})/19 + (210*b^{12}*c^$
 $4*d^6)/19 + (1440*a*b^{11}*c^3*d^7)/19 + (2200*a^3*b^9*c*d^9)/19 + (2970*a^2*$
 $b^{10}*c^2*d^8)/19) + x^8*(99*a^5*b^7*c^{10} + 15*a^{12}*c^3*d^7 + 1155*a^6*b^6*c$
 $^9*d + 315*a^{11}*b*c^4*d^6 + 4455*a^7*b^5*c^8*d^2 + 7425*a^8*b^4*c^7*d^3 + 5$
 $775*a^9*b^3*c^6*d^4 + 2079*a^{10}*b^2*c^5*d^5) + x^{16}*((99*a^7*b^5*d^{10})/2 +$
 $(15*b^{12}*c^7*d^3)/2 + (315*a*b^{11}*c^6*d^4)/2 + (1155*a^6*b^6*c*d^9)/2 + (20$
 $79*a^2*b^{10}*c^5*d^5)/2 + (5775*a^3*b^9*c^4*d^6)/2 + (7425*a^4*b^8*c^3*d^7)/$
 $2 + (4455*a^5*b^7*c^2*d^8)/2) + x^{11}*((a^{12}*d^{10})/11 + 6*a^2*b^{10}*c^{10} + 20$
 $0*a^3*b^9*c^9*d + 2025*a^4*b^8*c^8*d^2 + 8640*a^5*b^7*c^7*d^3 + 17640*a^6*b$
 $^6*c^6*d^4 + 18144*a^7*b^5*c^5*d^5 + 9450*a^8*b^4*c^4*d^6 + 2400*a^9*b^3*c^$
 $3*d^7 + 270*a^{10}*b^2*c^2*d^8 + (120*a^{11}*b*c*d^9)/11) + x^{13}*((b^{12}*c^{10})/1$
 $3 + (66*a^{10}*b^2*d^{10})/13 + (2200*a^9*b^3*c*d^9)/13 + (2970*a^2*b^{10}*c^8*d$
 $^2)/13 + (26400*a^3*b^9*c^7*d^3)/13 + (103950*a^4*b^8*c^6*d^4)/13 + (199584*$
 $a^5*b^7*c^5*d^5)/13 + (194040*a^6*b^6*c^4*d^6)/13 + (95040*a^7*b^5*c^3*d^7)$
 $/13 + (22275*a^8*b^4*c^2*d^8)/13 + (120*a*b^{11}*c^9*d)/13) + x^6*(132*a^7*b$
 $^5*c^{10} + 42*a^{12}*c^5*d^5 + 825*a^8*b^4*c^9*d + 420*a^{11}*b*c^6*d^4 + 1650*a^$
 $9*b^3*c^8*d^2 + 1320*a^{10}*b^2*c^7*d^3) + x^{18}*(44*a^5*b^7*d^{10} + 14*b^{12}*c^$
 $5*d^5 + 140*a*b^{11}*c^4*d^6 + 275*a^4*b^8*c*d^9 + 440*a^2*b^{10}*c^3*d^7 + 550$
 $*a^3*b^9*c^2*d^8) + x^9*(55*a^4*b^8*c^{10} + 5*a^{12}*c^2*d^8 + 880*a^5*b^7*c^9$
 $*d + 160*a^{11}*b*c^3*d^7 + 4620*a^6*b^6*c^8*d^2 + 10560*a^7*b^5*c^7*d^3 + 11$
 $550*a^8*b^4*c^6*d^4 + 6160*a^9*b^3*c^5*d^5 + 1540*a^{10}*b^2*c^4*d^6) + x^{15}*$
 $(33*a^8*b^4*d^{10} + 3*b^{12}*c^8*d^2 + 96*a*b^{11}*c^7*d^3 + 528*a^7*b^5*c*d^9 +$
 $924*a^2*b^{10}*c^6*d^4 + 3696*a^3*b^9*c^5*d^5 + 6930*a^4*b^8*c^4*d^6 + 6336*$

$$a^5b^7c^3d^7 + 2772a^6b^6c^2d^8) + x^{10}(a^{12}c^9d^9 + 22a^3b^9c^{10} + 495a^4b^8c^9d + 54a^{11}b^2c^2d^8 + 3564a^5b^7c^8d^2 + 11088a^6b^6c^7d^3 + 16632a^7b^5c^6d^4 + 12474a^8b^4c^5d^5 + 4620a^9b^3c^4d^6 + 792a^{10}b^2c^3d^7) + x^{14}((5b^{12}c^9d)/7 + (110a^9b^3d^{10})/7 + (270a^8b^4c^8d^2)/7 + (2475a^8b^4c^9d^9)/7 + (3960a^2b^{10}c^7d^3)/7 + 3300a^3b^9c^6d^4 + 8910a^4b^8c^5d^5 + 11880a^5b^7c^4d^6 + 7920a^6b^6c^3d^7 + (17820a^7b^5c^2d^8)/7) + a^{12}c^{10}x + (b^{12}d^{10}x^{23})/23 + 5a^9c^7x^4(6a^3d^3 + 11b^3c^3 + 33a^2b^2c^2d + 27a^2b^2c^2d) + b^9d^7x^{20}(11a^3d^3 + 6b^3c^3 + 27a^2b^2c^2d + 33a^2b^2c^2d) + a^{11}c^9x^2(5a^2d + 6b^2c) + (b^{11}d^9x^{22}(6a^2d + 5b^2c))/11 + a^{10}c^8x^3(15a^2d^2 + 22b^2c^2 + 40a^2b^2c^2d) + (b^{10}d^8x^{21}(22a^2d^2 + 15b^2c^2 + 40a^2b^2c^2d))/7$$

sympy [B] time = 0.37, size = 2088, normalized size = 7.59

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**12*(d*x+c)**10,x)

[Out] a**12*c**10*x + b**12*d**10*x**23/23 + x**22*(6*a*b**11*d**10/11 + 5*b**12*c*d**9/11) + x**21*(22*a**2*b**10*d**10/7 + 40*a*b**11*c*d**9/7 + 15*b**12*c**2*d**8/7) + x**20*(11*a**3*b**9*d**10 + 33*a**2*b**10*c*d**9 + 27*a*b**11*c**2*d**8 + 6*b**12*c**3*d**7) + x**19*(495*a**4*b**8*d**10/19 + 2200*a**3*b**9*c*d**9/19 + 2970*a**2*b**10*c**2*d**8/19 + 1440*a*b**11*c**3*d**7/19 + 210*b**12*c**4*d**6/19) + x**18*(44*a**5*b**7*d**10 + 275*a**4*b**8*c*d**9 + 550*a**3*b**9*c**2*d**8 + 440*a**2*b**10*c**3*d**7 + 140*a*b**11*c**4*d**6 + 14*b**12*c**5*d**5) + x**17*(924*a**6*b**6*d**10/17 + 7920*a**5*b**7*c*d**9/17 + 22275*a**4*b**8*c**2*d**8/17 + 26400*a**3*b**9*c**3*d**7/17 + 13860*a**2*b**10*c**4*d**6/17 + 3024*a*b**11*c**5*d**5/17 + 210*b**12*c**6*d**4/17) + x**16*(99*a**7*b**5*d**10/2 + 1155*a**6*b**6*c*d**9/2 + 4455*a**5*b**7*c**2*d**8/2 + 7425*a**4*b**8*c**3*d**7/2 + 5775*a**3*b**9*c**4*d**6/2 + 2079*a**2*b**10*c**5*d**5/2 + 315*a*b**11*c**6*d**4/2 + 15*b**12*c**7*d**3/2) + x**15*(33*a**8*b**4*d**10 + 528*a**7*b**5*c*d**9 + 2772*a**6*b**6*c**2*d**8 + 6336*a**5*b**7*c**3*d**7 + 6930*a**4*b**8*c**4*d**6 + 3696*a**3*b**9*c**5*d**5 + 924*a**2*b**10*c**6*d**4 + 96*a*b**11*c**7*d**3 + 3*b**12*c**8*d**2) + x**14*(110*a**9*b**3*d**10/7 + 2475*a**8*b**4*c*d**9/7 + 17820*a**7*b**5*c**2*d**8/7 + 7920*a**6*b**6*c**3*d**7 + 11880*a**5*b**7*c**4*d**6 + 8910*a**4*b**8*c**5*d**5 + 3300*a**3*b**9*c**6*d**4 + 3960*a**2*b**10*c**7*d**3/7 + 270*a*b**11*c**8*d**2/7 + 5*b**12*c**9*d/7) + x**13*(66*a**10*b**2*d**10/13 + 2200*a**9*b**3*c*d**9/13 + 22275*a**8*b**4*c**2*d**8/13 + 95040*a**7*b**5*c**3*d**7/13 + 194040*a**6*b**6*c**4*d**6/13 + 199584*a**5*b**7*c**5*d**5/13 + 103950*a**4*b**8*c**6*d**4/13 + 26400*a**3*b**9*c**7*d**3/13 + 2970*a**2*b**10*c**8*d**2/13 + 120*a*b**11*c**9*d/13 + b**12*c**10/13) + x**12*(a**11*b*d**10 + 55*a**10*b**2*c*d**9 + 825*a**9*b**3*c**2*d**8

$$\begin{aligned}
& 8 + 4950*a^{**8}*b^{**4}*c^{**3}*d^{**7} + 13860*a^{**7}*b^{**5}*c^{**4}*d^{**6} + 19404*a^{**6}*b^{**6}* \\
& c^{**5}*d^{**5} + 13860*a^{**5}*b^{**7}*c^{**6}*d^{**4} + 4950*a^{**4}*b^{**8}*c^{**7}*d^{**3} + 825*a^{**3} \\
& *b^{**9}*c^{**8}*d^{**2} + 55*a^{**2}*b^{**10}*c^{**9}*d + a*b^{**11}*c^{**10}) + x^{**11}*(a^{**12}*d^{**1} \\
& 0/11 + 120*a^{**11}*b*c*d^{**9}/11 + 270*a^{**10}*b^{**2}*c^{**2}*d^{**8} + 2400*a^{**9}*b^{**3}*c \\
& *3*d^{**7} + 9450*a^{**8}*b^{**4}*c^{**4}*d^{**6} + 18144*a^{**7}*b^{**5}*c^{**5}*d^{**5} + 17640*a^{**6} \\
& *b^{**6}*c^{**6}*d^{**4} + 8640*a^{**5}*b^{**7}*c^{**7}*d^{**3} + 2025*a^{**4}*b^{**8}*c^{**8}*d^{**2} + 200 \\
& *a^{**3}*b^{**9}*c^{**9}*d + 6*a^{**2}*b^{**10}*c^{**10}) + x^{**10}*(a^{**12}*c*d^{**9} + 54*a^{**11}*b* \\
& c^{**2}*d^{**8} + 792*a^{**10}*b^{**2}*c^{**3}*d^{**7} + 4620*a^{**9}*b^{**3}*c^{**4}*d^{**6} + 12474*a^{**8} \\
& *b^{**4}*c^{**5}*d^{**5} + 16632*a^{**7}*b^{**5}*c^{**6}*d^{**4} + 11088*a^{**6}*b^{**6}*c^{**7}*d^{**3} + \\
& 3564*a^{**5}*b^{**7}*c^{**8}*d^{**2} + 495*a^{**4}*b^{**8}*c^{**9}*d + 22*a^{**3}*b^{**9}*c^{**10}) + x^{**9} \\
& *(5*a^{**12}*c^{**2}*d^{**8} + 160*a^{**11}*b*c^{**3}*d^{**7} + 1540*a^{**10}*b^{**2}*c^{**4}*d^{**6} + \\
& 6160*a^{**9}*b^{**3}*c^{**5}*d^{**5} + 11550*a^{**8}*b^{**4}*c^{**6}*d^{**4} + 10560*a^{**7}*b^{**5}*c^{**7} \\
& *d^{**3} + 4620*a^{**6}*b^{**6}*c^{**8}*d^{**2} + 880*a^{**5}*b^{**7}*c^{**9}*d + 55*a^{**4}*b^{**8}*c^{**1} \\
& 0) + x^{**8}*(15*a^{**12}*c^{**3}*d^{**7} + 315*a^{**11}*b*c^{**4}*d^{**6} + 2079*a^{**10}*b^{**2}*c^{**5} \\
& *d^{**5} + 5775*a^{**9}*b^{**3}*c^{**6}*d^{**4} + 7425*a^{**8}*b^{**4}*c^{**7}*d^{**3} + 4455*a^{**7}*b* \\
& *5*c^{**8}*d^{**2} + 1155*a^{**6}*b^{**6}*c^{**9}*d + 99*a^{**5}*b^{**7}*c^{**10}) + x^{**7}*(30*a^{**12} \\
& *c^{**4}*d^{**6} + 432*a^{**11}*b*c^{**5}*d^{**5} + 1980*a^{**10}*b^{**2}*c^{**6}*d^{**4} + 26400*a^{**9} \\
& *b^{**3}*c^{**7}*d^{**3}/7 + 22275*a^{**8}*b^{**4}*c^{**8}*d^{**2}/7 + 7920*a^{**7}*b^{**5}*c^{**9}*d/7 + \\
& 132*a^{**6}*b^{**6}*c^{**10}) + x^{**6}*(42*a^{**12}*c^{**5}*d^{**5} + 420*a^{**11}*b*c^{**6}*d^{**4} + \\
& 1320*a^{**10}*b^{**2}*c^{**7}*d^{**3} + 1650*a^{**9}*b^{**3}*c^{**8}*d^{**2} + 825*a^{**8}*b^{**4}*c^{**9}*d \\
& + 132*a^{**7}*b^{**5}*c^{**10}) + x^{**5}*(42*a^{**12}*c^{**6}*d^{**4} + 288*a^{**11}*b*c^{**7}*d^{**3} \\
& + 594*a^{**10}*b^{**2}*c^{**8}*d^{**2} + 440*a^{**9}*b^{**3}*c^{**9}*d + 99*a^{**8}*b^{**4}*c^{**10}) + x \\
& **4*(30*a^{**12}*c^{**7}*d^{**3} + 135*a^{**11}*b*c^{**8}*d^{**2} + 165*a^{**10}*b^{**2}*c^{**9}*d + 5 \\
& 5*a^{**9}*b^{**3}*c^{**10}) + x^{**3}*(15*a^{**12}*c^{**8}*d^{**2} + 40*a^{**11}*b*c^{**9}*d + 22*a^{**1} \\
& 0*b^{**2}*c^{**10}) + x^{**2}*(5*a^{**12}*c^{**9}*d + 6*a^{**11}*b*c^{**10})
\end{aligned}$$

3.1300 $\int (a + bx)^{11} (c + dx)^{10} dx$

Optimal. Leaf size=279

$$\frac{10d^9(a+bx)^{21}(bc-ad)}{21b^{11}} + \frac{9d^8(a+bx)^{20}(bc-ad)^2}{4b^{11}} + \frac{120d^7(a+bx)^{19}(bc-ad)^3}{19b^{11}} + \frac{35d^6(a+bx)^{18}(bc-ad)^4}{3b^{11}} + \frac{252d^5(a+bx)^{17}(bc-ad)^5}{17b^{11}}$$

[Out] $1/12*(-a*d+b*c)^{10}*(b*x+a)^{12}/b^{11}+10/13*d*(-a*d+b*c)^9*(b*x+a)^{13}/b^{11}+45/14*d^2*(-a*d+b*c)^8*(b*x+a)^{14}/b^{11}+8*d^3*(-a*d+b*c)^7*(b*x+a)^{15}/b^{11}+105/8*d^4*(-a*d+b*c)^6*(b*x+a)^{16}/b^{11}+252/17*d^5*(-a*d+b*c)^5*(b*x+a)^{17}/b^{11}+35/3*d^6*(-a*d+b*c)^4*(b*x+a)^{18}/b^{11}+120/19*d^7*(-a*d+b*c)^3*(b*x+a)^{19}/b^{11}+9/4*d^8*(-a*d+b*c)^2*(b*x+a)^{20}/b^{11}+10/21*d^9*(-a*d+b*c)*(b*x+a)^{21}/b^{11}+1/22*d^{10}*(b*x+a)^{22}/b^{11}$

Rubi [A] time = 1.28, antiderivative size = 279, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{10d^9(a+bx)^{21}(bc-ad)}{21b^{11}} + \frac{9d^8(a+bx)^{20}(bc-ad)^2}{4b^{11}} + \frac{120d^7(a+bx)^{19}(bc-ad)^3}{19b^{11}} + \frac{35d^6(a+bx)^{18}(bc-ad)^4}{3b^{11}} + \frac{252d^5(a+bx)^{17}(bc-ad)^5}{17b^{11}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^11*(c + d*x)^10,x]

[Out] $((b*c - a*d)^{10}*(a + b*x)^{12})/(12*b^{11}) + (10*d*(b*c - a*d)^9*(a + b*x)^{13})/(13*b^{11}) + (45*d^2*(b*c - a*d)^8*(a + b*x)^{14})/(14*b^{11}) + (8*d^3*(b*c - a*d)^7*(a + b*x)^{15})/b^{11} + (105*d^4*(b*c - a*d)^6*(a + b*x)^{16})/(8*b^{11}) + (252*d^5*(b*c - a*d)^5*(a + b*x)^{17})/(17*b^{11}) + (35*d^6*(b*c - a*d)^4*(a + b*x)^{18})/(3*b^{11}) + (120*d^7*(b*c - a*d)^3*(a + b*x)^{19})/(19*b^{11}) + (9*d^8*(b*c - a*d)^2*(a + b*x)^{20})/(4*b^{11}) + (10*d^9*(b*c - a*d)*(a + b*x)^{21})/(21*b^{11}) + (d^{10}*(a + b*x)^{22})/(22*b^{11})$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int (a + bx)^{11}(c + dx)^{10} dx = \int \left(\frac{(bc - ad)^{10}(a + bx)^{11}}{b^{10}} + \frac{10d(bc - ad)^9(a + bx)^{12}}{b^{10}} + \frac{45d^2(bc - ad)^8(a + bx)^{13}}{b^{10}} + \frac{120d^3(bc - ad)^7(a + bx)^{14}}{b^{10}} + \frac{105d^4(bc - ad)^6(a + bx)^{15}}{b^{10}} + \frac{45d^5(bc - ad)^5(a + bx)^{16}}{b^{10}} + \frac{10d^6(bc - ad)^4(a + bx)^{17}}{b^{10}} + \frac{d^7(bc - ad)^3(a + bx)^{18}}{b^{10}} + \frac{d^8(bc - ad)^2(a + bx)^{19}}{b^{10}} + \frac{d^9(bc - ad)(a + bx)^{20}}{b^{10}} + \frac{d^{10}(a + bx)^{21}}{b^{10}} \right)$$

$$= \frac{(bc - ad)^{10}(a + bx)^{12}}{12b^{11}} + \frac{10d(bc - ad)^9(a + bx)^{13}}{13b^{11}} + \frac{45d^2(bc - ad)^8(a + bx)^{14}}{14b^{11}} + \frac{8d^3(bc - ad)^7(a + bx)^{15}}{15b^{11}} + \frac{120d^4(bc - ad)^6(a + bx)^{16}}{16b^{11}} + \frac{45d^5(bc - ad)^5(a + bx)^{17}}{17b^{11}} + \frac{10d^6(bc - ad)^4(a + bx)^{18}}{18b^{11}} + \frac{d^7(bc - ad)^3(a + bx)^{19}}{19b^{11}} + \frac{d^8(bc - ad)^2(a + bx)^{20}}{20b^{11}} + \frac{d^9(bc - ad)(a + bx)^{21}}{21b^{11}} + \frac{d^{10}(a + bx)^{22}}{22b^{11}}$$

Mathematica [B] time = 0.23, size = 1702, normalized size = 6.10

$$\frac{1}{22}b^{11}d^{10}x^{22} + \frac{1}{21}b^{10}d^9(10bc+11ad)x^{21} + \frac{1}{4}b^9d^8(9b^2c^2 + 22abdc + 11a^2d^2)x^{20} + \frac{5}{19}b^8d^7(24b^3c^3 + 99ab^2dc^2 + 110a^2b^2c^2d + 110a^3b^2cd^2 + 110a^4b^2cd^3 + 110a^5b^2cd^4 + 110a^6b^2cd^5 + 110a^7b^2cd^6 + 110a^8b^2cd^7 + 110a^9b^2cd^8 + 110a^{10}b^2cd^9 + 110a^{11}b^2cd^{10})x^{19} + \frac{5}{19}b^8d^7(24b^3c^3 + 99ab^2dc^2 + 110a^2b^2c^2d + 110a^3b^2cd^2 + 110a^4b^2cd^3 + 110a^5b^2cd^4 + 110a^6b^2cd^5 + 110a^7b^2cd^6 + 110a^8b^2cd^7 + 110a^9b^2cd^8 + 110a^{10}b^2cd^9 + 110a^{11}b^2cd^{10})x^{18} + \dots$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^11*(c + d*x)^10,x]

[Out] a^11*c^10*x + (a^10*c^9*(11*b*c + 10*a*d)*x^2)/2 + (5*a^9*c^8*(11*b^2*c^2 + 22*a*b*c*d + 9*a^2*d^2)*x^3)/3 + (5*a^8*c^7*(33*b^3*c^3 + 110*a*b^2*c^2*d + 99*a^2*b*c*d^2 + 24*a^3*d^3)*x^4)/4 + 3*a^7*c^6*(22*b^4*c^4 + 110*a*b^3*c^3*d + 165*a^2*b^2*c^2*d^2 + 88*a^3*b*c*d^3 + 14*a^4*d^4)*x^5 + (a^6*c^5*(154*b^5*c^5 + 1100*a*b^4*c^4*d + 2475*a^2*b^3*c^3*d^2 + 2200*a^3*b^2*c^2*d^3 + 770*a^4*b*c*d^4 + 84*a^5*d^5)*x^6)/2 + (6*a^5*c^4*(77*b^6*c^6 + 770*a*b^5*c^5*d + 2475*a^2*b^4*c^4*d^2 + 3300*a^3*b^3*c^3*d^3 + 1925*a^4*b^2*c^2*d^4 + 462*a^5*b*c*d^5 + 35*a^6*d^6)*x^7)/7 + (15*a^4*c^3*(11*b^7*c^7 + 154*a*b^6*c^6*d + 693*a^2*b^5*c^5*d^2 + 1320*a^3*b^4*c^4*d^3 + 1155*a^4*b^3*c^3*d^4 + 462*a^5*b^2*c^2*d^5 + 77*a^6*b*c*d^6 + 4*a^7*d^7)*x^8)/4 + (5*a^3*c^2*(11*b^8*c^8 + 220*a*b^7*c^7*d + 1386*a^2*b^6*c^6*d^2 + 3696*a^3*b^5*c^5*d^3 + 4620*a^4*b^4*c^4*d^4 + 2772*a^5*b^3*c^3*d^5 + 770*a^6*b^2*c^2*d^6 + 88*a^7*b*c*d^7 + 3*a^8*d^8)*x^9)/3 + (a^2*c*(11*b^9*c^9 + 330*a*b^8*c^8*d + 2970*a^2*b^7*c^7*d^2 + 11088*a^3*b^6*c^6*d^3 + 19404*a^4*b^5*c^5*d^4 + 16632*a^5*b^4*c^4*d^5 + 6930*a^6*b^3*c^3*d^6 + 1320*a^7*b^2*c^2*d^7 + 99*a^8*b*c*d^8 + 2*a^9*d^9)*x^10)/2 + (a*(11*b^10*c^10 + 550*a*b^9*c^9*d + 7425*a^2*b^8*c^8*d^2 + 39600*a^3*b^7*c^7*d^3 + 97020*a^4*b^6*c^6*d^4 + 116424*a^5*b^5*c^5*d^5 + 69300*a^6*b^4*c^4*d^6 + 19800*a^7*b^3*c^3*d^7 + 2475*a^8*b^2*c^2*d^8 + 110*a^9*b*c*d^9 + a^10*d^10)*x^11)/11 + (b*(b^10*c^10 + 110*a*b^9*c^9*d + 2475*a^2*b^8*c^8*d^2 + 19800*a^3*b^7*c^7*d^3 + 69300*a^4*b^6*c^6*d^4 + 116424*a^5*b^5*c^5*d^5 + 97020*a^6*b^4*c^4*d^6 + 39600*a^7*b^3*c^3*d^7 + 7425*a^8*b^2*c^2*d^8 + 550*a^9*b*c*d^9 + 11*a^10*d^10)*x^12)/12 + (5*b^2*d*(2*b^9*c^9 + 99*a*b^8*c^8*d + 1320*a^2*b^7*c^7*d^2 + 6930*a^3*b^6*c^6*d^3 + 16632*a^4*b^5*c^5*d^4 + 19404*a^5*b^4*c^4*d^5 + 11088*a^6*b^3*c^3*d^6 + 2970*a^7*b^2*c^2*d^7 + 330*a^8*b*c*d^8 + 11*a^9*d^9)*x^13)/13 + (15*b^3*d^2*(3*b^8*c^8 + 88*a*b^7*c^7*d + 770*a^2*b^6*c^6*d^2 + 2772*a^3*b^5*c^5*d^3 + 4620*a^4*b^4*c^4*d^4 + 3696*a^5*b^3*c^3*d^5 + 1386*a^6*b^2*c^2*d^6 + 220*a^7*b*c*d^7 + 11*a^8*d^8)*x^14)/14 + 2*b^4*d^3*(4*b^7*c^7 + 77*a*b^6*c^6*d + 462

$$\begin{aligned} & *a^2*b^5*c^5*d^2 + 1155*a^3*b^4*c^4*d^3 + 1320*a^4*b^3*c^3*d^4 + 693*a^5*b^2*c^2*d^5 + 154*a^6*b*c*d^6 + 11*a^7*d^7)*x^{15} + (3*b^5*d^4*(35*b^6*c^6 + 4 \\ & 62*a*b^5*c^5*d + 1925*a^2*b^4*c^4*d^2 + 3300*a^3*b^3*c^3*d^3 + 2475*a^4*b^2*c^2*d^4 + 770*a^5*b*c*d^5 + 77*a^6*d^6)*x^{16})/8 + (3*b^6*d^5*(84*b^5*c^5 + \\ & 770*a*b^4*c^4*d + 2200*a^2*b^3*c^3*d^2 + 2475*a^3*b^2*c^2*d^3 + 1100*a^4*b*c*d^4 + 154*a^5*d^5)*x^{17})/17 + (5*b^7*d^6*(14*b^4*c^4 + 88*a*b^3*c^3*d + \\ & 165*a^2*b^2*c^2*d^2 + 110*a^3*b*c*d^3 + 22*a^4*d^4)*x^{18})/6 + (5*b^8*d^7*(24*b^3*c^3 + 99*a*b^2*c^2*d + 110*a^2*b*c*d^2 + 33*a^3*d^3)*x^{19})/19 + (b^9*d^8*(9*b^2*c^2 + 22*a*b*c*d + 11*a^2*d^2)*x^{20})/4 + (b^10*d^9*(10*b*c + 11* \\ & a*d)*x^{21})/21 + (b^11*d^10*x^{22})/22 \end{aligned}$$

fricas [B] time = 0.40, size = 2010, normalized size = 7.20

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^11*(d*x+c)^10,x, algorithm="fricas")

[Out] $1/22*x^{22}*d^{10}*b^{11} + 10/21*x^{21}*d^9*c*b^{11} + 11/21*x^{21}*d^{10}*b^{10}*a + 9/4*x^{20}*d^8*c^2*b^{11} + 11/2*x^{20}*d^9*c*b^{10}*a + 11/4*x^{20}*d^{10}*b^9*a^2 + 120/19*x^{19}*d^7*c^3*b^{11} + 495/19*x^{19}*d^8*c^2*b^{10}*a + 550/19*x^{19}*d^9*c*b^9*a^2 + 165/19*x^{19}*d^{10}*b^8*a^3 + 35/3*x^{18}*d^6*c^4*b^{11} + 220/3*x^{18}*d^7*c^3*b^{10}*a + 275/2*x^{18}*d^8*c^2*b^9*a^2 + 275/3*x^{18}*d^9*c*b^8*a^3 + 55/3*x^{18}*d^{10}*b^7*a^4 + 252/17*x^{17}*d^5*c^5*b^{11} + 2310/17*x^{17}*d^6*c^4*b^{10}*a + 660/17*x^{17}*d^7*c^3*b^9*a^2 + 7425/17*x^{17}*d^8*c^2*b^8*a^3 + 3300/17*x^{17}*d^9*c*b^7*a^4 + 462/17*x^{17}*d^{10}*b^6*a^5 + 105/8*x^{16}*d^4*c^6*b^{11} + 693/4*x^{16}*d^5*c^5*b^{10}*a + 5775/8*x^{16}*d^6*c^4*b^9*a^2 + 2475/2*x^{16}*d^7*c^3*b^8*a^3 + 7425/8*x^{16}*d^8*c^2*b^7*a^4 + 1155/4*x^{16}*d^9*c*b^6*a^5 + 231/8*x^{16}*d^{10}*b^5*a^6 + 8*x^{15}*d^3*c^7*b^{11} + 154*x^{15}*d^4*c^6*b^{10}*a + 924*x^{15}*d^5*c^5*b^9*a^2 + 2310*x^{15}*d^6*c^4*b^8*a^3 + 2640*x^{15}*d^7*c^3*b^7*a^4 + 1386*x^{15}*d^8*c^2*b^6*a^5 + 308*x^{15}*d^9*c*b^5*a^6 + 22*x^{15}*d^{10}*b^4*a^7 + 45/14*x^{14}*d^2*c^8*b^{11} + 660/7*x^{14}*d^3*c^7*b^{10}*a + 825*x^{14}*d^4*c^6*b^9*a^2 + 2970*x^{14}*d^5*c^5*b^8*a^3 + 4950*x^{14}*d^6*c^4*b^7*a^4 + 3960*x^{14}*d^7*c^3*b^6*a^5 + 1485*x^{14}*d^8*c^2*b^5*a^6 + 1650/7*x^{14}*d^9*c*b^4*a^7 + 165/14*x^{14}*d^{10}*b^3*a^8 + 10/13*x^{13}*d*c^9*b^{11} + 495/13*x^{13}*d^2*c^8*b^{10}*a + 6600/13*x^{13}*d^3*c^7*b^9*a^2 + 34650/13*x^{13}*d^4*c^6*b^8*a^3 + 83160/13*x^{13}*d^5*c^5*b^7*a^4 + 97020/13*x^{13}*d^6*c^4*b^6*a^5 + 55440/13*x^{13}*d^7*c^3*b^5*a^6 + 14850/13*x^{13}*d^8*c^2*b^4*a^7 + 1650/13*x^{13}*d^9*c*b^3*a^8 + 55/13*x^{13}*d^{10}*b^2*a^9 + 1/12*x^{12}*c^{10}*b^{11} + 55/6*x^{12}*d*c^9*b^{10}*a + 825/4*x^{12}*d^2*c^8*b^9*a^2 + 1650*x^{12}*d^3*c^7*b^8*a^3 + 5775*x^{12}*d^4*c^6*b^7*a^4 + 9702*x^{12}*d^5*c^5*b^6*a^5 + 8085*x^{12}*d^6*c^4*b^5*a^6 + 3300*x^{12}*d^7*c^3*b^4*a^7 + 2475/4*x^{12}*d^8*c^2*b^3*a^8 + 275/6*x^{12}*d^9*c*b^2*a^9 + 11/12*x^{12}*d^{10}*b*a^{10} + x^{11}*c^{10}*b^{10}*a + 50*x^{11}*d*c^9*b^9*a^2 + 675*x^{11}*d^2*c^8*b^8*a^3 + 3600*x^{11}*d^3*c^7*b^7*a^4 + 8820*x^{11}*d^4*c^6*b^6*a^5 + 10584*x^{11}*d^5*c^5*b^5*a^6 + 6300*x^{11}*d^6*c^4*b^4*a^7 + 1800*x^{11}*d^7*c^3*b^3*a^8 +$

$$\begin{aligned}
& 225*x^{11}*d^8*c^2*b^2*a^9 + 10*x^{11}*d^9*c*b*a^{10} + 1/11*x^{11}*d^{10}*a^{11} + 11 \\
& /2*x^{10}*c^{10}*b^9*a^2 + 165*x^{10}*d*c^9*b^8*a^3 + 1485*x^{10}*d^2*c^8*b^7*a^4 + \\
& 5544*x^{10}*d^3*c^7*b^6*a^5 + 9702*x^{10}*d^4*c^6*b^5*a^6 + 8316*x^{10}*d^5*c^5* \\
& b^4*a^7 + 3465*x^{10}*d^6*c^4*b^3*a^8 + 660*x^{10}*d^7*c^3*b^2*a^9 + 99/2*x^{10}* \\
& d^8*c^2*b*a^{10} + x^{10}*d^9*c*a^{11} + 55/3*x^9*c^{10}*b^8*a^3 + 1100/3*x^9*d*c^9 \\
& *b^7*a^4 + 2310*x^9*d^2*c^8*b^6*a^5 + 6160*x^9*d^3*c^7*b^5*a^6 + 7700*x^9*d \\
& ^4*c^6*b^4*a^7 + 4620*x^9*d^5*c^5*b^3*a^8 + 3850/3*x^9*d^6*c^4*b^2*a^9 + 44 \\
& 0/3*x^9*d^7*c^3*b*a^{10} + 5*x^9*d^8*c^2*a^{11} + 165/4*x^8*c^{10}*b^7*a^4 + 1155 \\
& /2*x^8*d*c^9*b^6*a^5 + 10395/4*x^8*d^2*c^8*b^5*a^6 + 4950*x^8*d^3*c^7*b^4*a \\
& ^7 + 17325/4*x^8*d^4*c^6*b^3*a^8 + 3465/2*x^8*d^5*c^5*b^2*a^9 + 1155/4*x^8* \\
& d^6*c^4*b*a^{10} + 15*x^8*d^7*c^3*a^{11} + 66*x^7*c^{10}*b^6*a^5 + 660*x^7*d*c^9* \\
& b^5*a^6 + 14850/7*x^7*d^2*c^8*b^4*a^7 + 19800/7*x^7*d^3*c^7*b^3*a^8 + 1650* \\
& x^7*d^4*c^6*b^2*a^9 + 396*x^7*d^5*c^5*b*a^{10} + 30*x^7*d^6*c^4*a^{11} + 77*x^6 \\
& *c^{10}*b^5*a^6 + 550*x^6*d*c^9*b^4*a^7 + 2475/2*x^6*d^2*c^8*b^3*a^8 + 1100*x \\
& ^6*d^3*c^7*b^2*a^9 + 385*x^6*d^4*c^6*b*a^{10} + 42*x^6*d^5*c^5*a^{11} + 66*x^5* \\
& c^{10}*b^4*a^7 + 330*x^5*d*c^9*b^3*a^8 + 495*x^5*d^2*c^8*b^2*a^9 + 264*x^5*d^ \\
& 3*c^7*b*a^{10} + 42*x^5*d^4*c^6*a^{11} + 165/4*x^4*c^{10}*b^3*a^8 + 275/2*x^4*d*c \\
& ^9*b^2*a^9 + 495/4*x^4*d^2*c^8*b*a^{10} + 30*x^4*d^3*c^7*a^{11} + 55/3*x^3*c^{10} \\
& *b^2*a^9 + 110/3*x^3*d*c^9*b*a^{10} + 15*x^3*d^2*c^8*a^{11} + 11/2*x^2*c^{10}*b*a \\
& ^{10} + 5*x^2*d*c^9*a^{11} + x*c^{10}*a^{11}
\end{aligned}$$

giac [B] time = 1.35, size = 2010, normalized size = 7.20

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^11*(d*x+c)^10,x, algorithm="giac")

[Out] $1/22*b^{11}*d^{10}*x^{22} + 10/21*b^{11}*c*d^9*x^{21} + 11/21*a*b^{10}*d^{10}*x^{21} + 9/4*$
 $b^{11}*c^2*d^8*x^{20} + 11/2*a*b^{10}*c*d^9*x^{20} + 11/4*a^2*b^9*d^{10}*x^{20} + 120/1$
 $9*b^{11}*c^3*d^7*x^{19} + 495/19*a*b^{10}*c^2*d^8*x^{19} + 550/19*a^2*b^9*c*d^9*x^{19}$
 $+ 165/19*a^3*b^8*d^{10}*x^{19} + 35/3*b^{11}*c^4*d^6*x^{18} + 220/3*a*b^{10}*c^3*d^$
 $7*x^{18} + 275/2*a^2*b^9*c^2*d^8*x^{18} + 275/3*a^3*b^8*c*d^9*x^{18} + 55/3*a^4*b$
 $^7*d^{10}*x^{18} + 252/17*b^{11}*c^5*d^5*x^{17} + 2310/17*a*b^{10}*c^4*d^6*x^{17} + 660$
 $0/17*a^2*b^9*c^3*d^7*x^{17} + 7425/17*a^3*b^8*c^2*d^8*x^{17} + 3300/17*a^4*b^7*$
 $c*d^9*x^{17} + 462/17*a^5*b^6*d^{10}*x^{17} + 105/8*b^{11}*c^6*d^4*x^{16} + 693/4*a*b$
 $^{10}*c^5*d^5*x^{16} + 5775/8*a^2*b^9*c^4*d^6*x^{16} + 2475/2*a^3*b^8*c^3*d^7*x^{16}$
 $+ 7425/8*a^4*b^7*c^2*d^8*x^{16} + 1155/4*a^5*b^6*c*d^9*x^{16} + 231/8*a^6*b^5$
 $*d^{10}*x^{16} + 8*b^{11}*c^7*d^3*x^{15} + 154*a*b^{10}*c^6*d^4*x^{15} + 924*a^2*b^9*c^$
 $5*d^5*x^{15} + 2310*a^3*b^8*c^4*d^6*x^{15} + 2640*a^4*b^7*c^3*d^7*x^{15} + 1386*a$
 $^5*b^6*c^2*d^8*x^{15} + 308*a^6*b^5*c*d^9*x^{15} + 22*a^7*b^4*d^{10}*x^{15} + 45/14$
 $*b^{11}*c^8*d^2*x^{14} + 660/7*a*b^{10}*c^7*d^3*x^{14} + 825*a^2*b^9*c^6*d^4*x^{14} +$
 $2970*a^3*b^8*c^5*d^5*x^{14} + 4950*a^4*b^7*c^4*d^6*x^{14} + 3960*a^5*b^6*c^3*d$
 $^7*x^{14} + 1485*a^6*b^5*c^2*d^8*x^{14} + 1650/7*a^7*b^4*c*d^9*x^{14} + 165/14*a^$
 $8*b^3*d^{10}*x^{14} + 10/13*b^{11}*c^9*d*x^{13} + 495/13*a*b^{10}*c^8*d^2*x^{13} + 6600$

$$\begin{aligned}
& /13*a^2*b^9*c^7*d^3*x^13 + 34650/13*a^3*b^8*c^6*d^4*x^13 + 83160/13*a^4*b^7 \\
& *c^5*d^5*x^13 + 97020/13*a^5*b^6*c^4*d^6*x^13 + 55440/13*a^6*b^5*c^3*d^7*x^ \\
& 13 + 14850/13*a^7*b^4*c^2*d^8*x^13 + 1650/13*a^8*b^3*c*d^9*x^13 + 55/13*a^9 \\
& *b^2*d^10*x^13 + 1/12*b^11*c^10*x^12 + 55/6*a*b^10*c^9*d*x^12 + 825/4*a^2*b \\
& ^9*c^8*d^2*x^12 + 1650*a^3*b^8*c^7*d^3*x^12 + 5775*a^4*b^7*c^6*d^4*x^12 + 9 \\
& 702*a^5*b^6*c^5*d^5*x^12 + 8085*a^6*b^5*c^4*d^6*x^12 + 3300*a^7*b^4*c^3*d^7 \\
& *x^12 + 2475/4*a^8*b^3*c^2*d^8*x^12 + 275/6*a^9*b^2*c*d^9*x^12 + 11/12*a^10 \\
& *b*d^10*x^12 + a*b^10*c^10*x^11 + 50*a^2*b^9*c^9*d*x^11 + 675*a^3*b^8*c^8*d \\
& ^2*x^11 + 3600*a^4*b^7*c^7*d^3*x^11 + 8820*a^5*b^6*c^6*d^4*x^11 + 10584*a^6 \\
& *b^5*c^5*d^5*x^11 + 6300*a^7*b^4*c^4*d^6*x^11 + 1800*a^8*b^3*c^3*d^7*x^11 + \\
& 225*a^9*b^2*c^2*d^8*x^11 + 10*a^10*b*c*d^9*x^11 + 1/11*a^11*d^10*x^11 + 11 \\
& /2*a^2*b^9*c^10*x^10 + 165*a^3*b^8*c^9*d*x^10 + 1485*a^4*b^7*c^8*d^2*x^10 + \\
& 5544*a^5*b^6*c^7*d^3*x^10 + 9702*a^6*b^5*c^6*d^4*x^10 + 8316*a^7*b^4*c^5*d \\
& ^5*x^10 + 3465*a^8*b^3*c^4*d^6*x^10 + 660*a^9*b^2*c^3*d^7*x^10 + 99/2*a^10* \\
& b*c^2*d^8*x^10 + a^11*c*d^9*x^10 + 55/3*a^3*b^8*c^10*x^9 + 1100/3*a^4*b^7*c \\
& ^9*d*x^9 + 2310*a^5*b^6*c^8*d^2*x^9 + 6160*a^6*b^5*c^7*d^3*x^9 + 7700*a^7*b \\
& ^4*c^6*d^4*x^9 + 4620*a^8*b^3*c^5*d^5*x^9 + 3850/3*a^9*b^2*c^4*d^6*x^9 + 44 \\
& 0/3*a^10*b*c^3*d^7*x^9 + 5*a^11*c^2*d^8*x^9 + 165/4*a^4*b^7*c^10*x^8 + 1155 \\
& /2*a^5*b^6*c^9*d*x^8 + 10395/4*a^6*b^5*c^8*d^2*x^8 + 4950*a^7*b^4*c^7*d^3*x \\
& ^8 + 17325/4*a^8*b^3*c^6*d^4*x^8 + 3465/2*a^9*b^2*c^5*d^5*x^8 + 1155/4*a^10 \\
& *b*c^4*d^6*x^8 + 15*a^11*c^3*d^7*x^8 + 66*a^5*b^6*c^10*x^7 + 660*a^6*b^5*c^ \\
& 9*d*x^7 + 14850/7*a^7*b^4*c^8*d^2*x^7 + 19800/7*a^8*b^3*c^7*d^3*x^7 + 1650* \\
& a^9*b^2*c^6*d^4*x^7 + 396*a^10*b*c^5*d^5*x^7 + 30*a^11*c^4*d^6*x^7 + 77*a^6 \\
& *b^5*c^10*x^6 + 550*a^7*b^4*c^9*d*x^6 + 2475/2*a^8*b^3*c^8*d^2*x^6 + 1100*a \\
& ^9*b^2*c^7*d^3*x^6 + 385*a^10*b*c^6*d^4*x^6 + 42*a^11*c^5*d^5*x^6 + 66*a^7* \\
& b^4*c^10*x^5 + 330*a^8*b^3*c^9*d*x^5 + 495*a^9*b^2*c^8*d^2*x^5 + 264*a^10*b \\
& *c^7*d^3*x^5 + 42*a^11*c^6*d^4*x^5 + 165/4*a^8*b^3*c^10*x^4 + 275/2*a^9*b^2 \\
& *c^9*d*x^4 + 495/4*a^10*b*c^8*d^2*x^4 + 30*a^11*c^7*d^3*x^4 + 55/3*a^9*b^2* \\
& c^10*x^3 + 110/3*a^10*b*c^9*d*x^3 + 15*a^11*c^8*d^2*x^3 + 11/2*a^10*b*c^10* \\
& x^2 + 5*a^11*c^9*d*x^2 + a^11*c^10*x
\end{aligned}$$

maple [B] time = 0.00, size = 1741, normalized size = 6.24

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x+a)^{11}*(d*x+c)^{10},x)$

[Out] $1/22*b^{11}*d^{10}*x^{22}+1/21*(11*a*b^{10}*d^{10}+10*b^{11}*c*d^9)*x^{21}+1/20*(55*a^2*b^9*d^{10}+110*a*b^{10}*c*d^9+45*b^{11}*c^2*d^8)*x^{20}+1/19*(165*a^3*b^8*d^{10}+550*a^2*b^9*c*d^9+495*a*b^{10}*c^2*d^8+120*b^{11}*c^3*d^7)*x^{19}+1/18*(330*a^4*b^7*d^{10}+1650*a^3*b^8*c*d^9+2475*a^2*b^9*c^2*d^8+1320*a*b^{10}*c^3*d^7+210*b^{11}*c^4*d^6)*x^{18}+1/17*(462*a^5*b^6*d^{10}+3300*a^4*b^7*c*d^9+7425*a^3*b^8*c^2*d^8+6600*a^2*b^9*c^3*d^7+2310*a*b^{10}*c^4*d^6+252*b^{11}*c^5*d^5)*x^{17}+1/16*(462*a^6*b^5*d^{10}+4620*a^5*b^6*c*d^9+14850*a^4*b^7*c^2*d^8+19800*a^3*b^8*c^3*d^7+1$

$$\begin{aligned}
& 1550*a^2*b^9*c^4*d^6+2772*a*b^10*c^5*d^5+210*b^11*c^6*d^4)*x^{16}+1/15*(330*a \\
& ^7*b^4*d^{10}+4620*a^6*b^5*c*d^9+20790*a^5*b^6*c^2*d^8+39600*a^4*b^7*c^3*d^7+ \\
& 34650*a^3*b^8*c^4*d^6+13860*a^2*b^9*c^5*d^5+2310*a*b^10*c^6*d^4+120*b^11*c^ \\
& 7*d^3)*x^{15}+1/14*(165*a^8*b^3*d^{10}+3300*a^7*b^4*c*d^9+20790*a^6*b^5*c^2*d^8 \\
& +55440*a^5*b^6*c^3*d^7+69300*a^4*b^7*c^4*d^6+41580*a^3*b^8*c^5*d^5+11550*a^ \\
& 2*b^9*c^6*d^4+1320*a*b^10*c^7*d^3+45*b^11*c^8*d^2)*x^{14}+1/13*(55*a^9*b^2*d^ \\
& 10+1650*a^8*b^3*c*d^9+14850*a^7*b^4*c^2*d^8+55440*a^6*b^5*c^3*d^7+97020*a^5 \\
& *b^6*c^4*d^6+83160*a^4*b^7*c^5*d^5+34650*a^3*b^8*c^6*d^4+6600*a^2*b^9*c^7*d \\
& ^3+495*a*b^10*c^8*d^2+10*b^11*c^9*d)*x^{13}+1/12*(11*a^10*b*d^{10}+550*a^9*b^2* \\
& c*d^9+7425*a^8*b^3*c^2*d^8+39600*a^7*b^4*c^3*d^7+97020*a^6*b^5*c^4*d^6+1164 \\
& 24*a^5*b^6*c^5*d^5+69300*a^4*b^7*c^6*d^4+19800*a^3*b^8*c^7*d^3+2475*a^2*b^9 \\
& *c^8*d^2+110*a*b^10*c^9*d+b^11*c^{10})*x^{12}+1/11*(a^{11}*d^{10}+110*a^{10}*b*c*d^9+ \\
& 2475*a^9*b^2*c^2*d^8+19800*a^8*b^3*c^3*d^7+69300*a^7*b^4*c^4*d^6+116424*a^6 \\
& *b^5*c^5*d^5+97020*a^5*b^6*c^6*d^4+39600*a^4*b^7*c^7*d^3+7425*a^3*b^8*c^8*d \\
& ^2+550*a^2*b^9*c^9*d+11*a*b^10*c^{10})*x^{11}+1/10*(10*a^{11}*c*d^9+495*a^{10}*b*c^ \\
& 2*d^8+6600*a^9*b^2*c^3*d^7+34650*a^8*b^3*c^4*d^6+83160*a^7*b^4*c^5*d^5+9702 \\
& 0*a^6*b^5*c^6*d^4+55440*a^5*b^6*c^7*d^3+14850*a^4*b^7*c^8*d^2+1650*a^3*b^8* \\
& c^9*d+55*a^2*b^9*c^{10})*x^{10}+1/9*(45*a^{11}*c^2*d^8+1320*a^{10}*b*c^3*d^7+11550* \\
& a^9*b^2*c^4*d^6+41580*a^8*b^3*c^5*d^5+69300*a^7*b^4*c^6*d^4+55440*a^6*b^5*c \\
& ^7*d^3+20790*a^5*b^6*c^8*d^2+3300*a^4*b^7*c^9*d+165*a^3*b^8*c^{10})*x^9+1/8*(\\
& 120*a^{11}*c^3*d^7+2310*a^{10}*b*c^4*d^6+13860*a^9*b^2*c^5*d^5+34650*a^8*b^3*c^ \\
& 6*d^4+39600*a^7*b^4*c^7*d^3+20790*a^6*b^5*c^8*d^2+4620*a^5*b^6*c^9*d+330*a^ \\
& 4*b^7*c^{10})*x^8+1/7*(210*a^{11}*c^4*d^6+2772*a^{10}*b*c^5*d^5+11550*a^9*b^2*c^6 \\
& *d^4+19800*a^8*b^3*c^7*d^3+14850*a^7*b^4*c^8*d^2+4620*a^6*b^5*c^9*d+462*a^5 \\
& *b^6*c^{10})*x^7+1/6*(252*a^{11}*c^5*d^5+2310*a^{10}*b*c^6*d^4+6600*a^9*b^2*c^7*d \\
& ^3+7425*a^8*b^3*c^8*d^2+3300*a^7*b^4*c^9*d+462*a^6*b^5*c^{10})*x^6+1/5*(210*a \\
& ^{11}*c^6*d^4+1320*a^{10}*b*c^7*d^3+2475*a^9*b^2*c^8*d^2+1650*a^8*b^3*c^9*d+330 \\
& *a^7*b^4*c^{10})*x^5+1/4*(120*a^{11}*c^7*d^3+495*a^{10}*b*c^8*d^2+550*a^9*b^2*c^9 \\
& *d+165*a^8*b^3*c^{10})*x^4+1/3*(45*a^{11}*c^8*d^2+110*a^{10}*b*c^9*d+55*a^9*b^2*c \\
& ^{10})*x^3+1/2*(10*a^{11}*c^9*d+11*a^{10}*b*c^{10})*x^2+a^{11}*c^{10}*x
\end{aligned}$$

maxima [B] time = 1.58, size = 1740, normalized size = 6.24

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^11*(d*x+c)^10,x, algorithm="maxima")

[Out] $1/22*b^{11}*d^{10}*x^{22} + a^{11}*c^{10}*x + 1/21*(10*b^{11}*c*d^9 + 11*a*b^{10}*d^{10})*x^{21} + 1/4*(9*b^{11}*c^2*d^8 + 22*a*b^{10}*c*d^9 + 11*a^2*b^9*d^{10})*x^{20} + 5/19*(24*b^{11}*c^3*d^7 + 99*a*b^{10}*c^2*d^8 + 110*a^2*b^9*c*d^9 + 33*a^3*b^8*d^{10})*x^{19} + 5/6*(14*b^{11}*c^4*d^6 + 88*a*b^{10}*c^3*d^7 + 165*a^2*b^9*c^2*d^8 + 110*a^3*b^8*c*d^9 + 22*a^4*b^7*d^{10})*x^{18} + 3/17*(84*b^{11}*c^5*d^5 + 770*a*b^{10}*c^4*d^6 + 2200*a^2*b^9*c^3*d^7 + 2475*a^3*b^8*c^2*d^8 + 1100*a^4*b^7*c*d^9 + 154*a^5*b^6*d^{10})*x^{17} + 3/8*(35*b^{11}*c^6*d^4 + 462*a*b^{10}*c^5*d^5 + 19$

$$\begin{aligned}
& 25*a^2*b^9*c^4*d^6 + 3300*a^3*b^8*c^3*d^7 + 2475*a^4*b^7*c^2*d^8 + 770*a^5*b^6*c*d^9 + 77*a^6*b^5*d^10)*x^{16} + 2*(4*b^{11}*c^7*d^3 + 77*a*b^{10}*c^6*d^4 + \\
& 462*a^2*b^9*c^5*d^5 + 1155*a^3*b^8*c^4*d^6 + 1320*a^4*b^7*c^3*d^7 + 693*a^5*b^6*c^2*d^8 + 154*a^6*b^5*c*d^9 + 11*a^7*b^4*d^10)*x^{15} + 15/14*(3*b^{11}*c^8*d^2 + \\
& 88*a*b^{10}*c^7*d^3 + 770*a^2*b^9*c^6*d^4 + 2772*a^3*b^8*c^5*d^5 + 4620*a^4*b^7*c^4*d^6 + 3696*a^5*b^6*c^3*d^7 + 1386*a^6*b^5*c^2*d^8 + 220*a^7*b^4*c*d^9 + \\
& 11*a^8*b^3*d^10)*x^{14} + 5/13*(2*b^{11}*c^9*d + 99*a*b^{10}*c^8*d^2 + 1320*a^2*b^9*c^7*d^3 + 6930*a^3*b^8*c^6*d^4 + 16632*a^4*b^7*c^5*d^5 + 19404*a^5*b^6*c^4*d^6 + \\
& 11088*a^6*b^5*c^3*d^7 + 2970*a^7*b^4*c^2*d^8 + 330*a^8*b^3*c*d^9 + 11*a^9*b^2*d^10)*x^{13} + 1/12*(b^{11}*c^{10} + 110*a*b^{10}*c^9*d + 2475*a^2*b^9*c^8*d^2 + \\
& 19800*a^3*b^8*c^7*d^3 + 69300*a^4*b^7*c^6*d^4 + 116424*a^5*b^6*c^5*d^5 + 97020*a^6*b^5*c^4*d^6 + 39600*a^7*b^4*c^3*d^7 + 7425*a^8*b^3*c^2*d^8 + 550*a^9*b^2*c*d^9 + \\
& 11*a^{10}*b*d^10)*x^{12} + 1/11*(11*a*b^{10}*c^{10} + 550*a^2*b^9*c^9*d + 7425*a^3*b^8*c^8*d^2 + 39600*a^4*b^7*c^7*d^3 + 97020*a^5*b^6*c^6*d^4 + 116424*a^6*b^5*c^5*d^5 + \\
& 69300*a^7*b^4*c^4*d^6 + 19800*a^8*b^3*c^3*d^7 + 2475*a^9*b^2*c^2*d^8 + 110*a^{10}*b*c*d^9 + a^{11}*d^{10})*x^{11} + 1/2*(11*a^2*b^9*c^{10} + 330*a^3*b^8*c^9*d + 2970*a^4*b^7*c^8*d^2 + 11088*a^5*b^6*c^7*d^3 + \\
& 19404*a^6*b^5*c^6*d^4 + 16632*a^7*b^4*c^5*d^5 + 6930*a^8*b^3*c^4*d^6 + 1320*a^9*b^2*c^3*d^7 + 99*a^{10}*b*c^2*d^8 + 2*a^{11}*c*d^9)*x^{10} + 5/3*(11*a^3*b^8*c^{10} + 220*a^4*b^7*c^9*d + 1386*a^5*b^6*c^8*d^2 + 3696*a^6*b^5*c^7*d^3 + \\
& 4620*a^7*b^4*c^6*d^4 + 2772*a^8*b^3*c^5*d^5 + 770*a^9*b^2*c^4*d^6 + 88*a^{10}*b*c^3*d^7 + 3*a^{11}*c^2*d^8)*x^9 + 15/4*(11*a^4*b^7*c^{10} + 154*a^5*b^6*c^9*d + 693*a^6*b^5*c^8*d^2 + 1320*a^7*b^4*c^7*d^3 + 1155*a^8*b^3*c^6*d^4 + \\
& 462*a^9*b^2*c^5*d^5 + 77*a^{10}*b*c^4*d^6 + 4*a^{11}*c^3*d^7)*x^8 + 6/7*(77*a^5*b^6*c^{10} + 770*a^6*b^5*c^9*d + 2475*a^7*b^4*c^8*d^2 + 3300*a^8*b^3*c^7*d^3 + 1925*a^9*b^2*c^6*d^4 + 462*a^{10}*b*c^5*d^5 + 35*a^{11}*c^4*d^6)*x^7 + \\
& 1/2*(154*a^6*b^5*c^{10} + 1100*a^7*b^4*c^9*d + 2475*a^8*b^3*c^8*d^2 + 2200*a^9*b^2*c^7*d^3 + 770*a^{10}*b*c^6*d^4 + 84*a^{11}*c^5*d^5)*x^6 + 3*(22*a^7*b^4*c^{10} + 110*a^8*b^3*c^9*d + 165*a^9*b^2*c^8*d^2 + 88*a^{10}*b*c^7*d^3 + 14*a^{11}*c^6*d^4)*x^5 + 5/4*(33*a^8*b^3*c^{10} + 110*a^9*b^2*c^9*d + 99*a^{10}*b*c^8*d^2 + 24*a^{11}*c^7*d^3)*x^4 + 5/3*(11*a^9*b^2*c^{10} + 22*a^{10}*b*c^9*d + 9*a^{11}*c^8*d^2)*x^3 + 1/2*(11*a^{10}*b*c^{10} + 10*a^{11}*c^9*d)*x^2
\end{aligned}$$

mupad [B] time = 1.03, size = 1702, normalized size = 6.10

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^{11}*(c + d*x)^{10}, x)$

[Out] $x^7*(66*a^5*b^6*c^{10} + 30*a^{11}*c^4*d^6 + 660*a^6*b^5*c^9*d + 396*a^{10}*b*c^5*d^5 + (14850*a^7*b^4*c^8*d^2)/7 + (19800*a^8*b^3*c^7*d^3)/7 + 1650*a^9*b^2*c^6*d^4) + x^{16}*((231*a^6*b^5*d^{10})/8 + (105*b^{11}*c^6*d^4)/8 + (693*a*b^{10}*c^5*d^5)/4 + (1155*a^5*b^6*c*d^9)/4 + (5775*a^2*b^9*c^4*d^6)/8 + (2475*a^3*b^8*c^3*d^7)/2 + (7425*a^4*b^7*c^2*d^8)/8) + x^{11}*((a^{11}*d^{10})/11 + a*b^{10}$

$$\begin{aligned}
& *c^{10} + 50*a^2*b^9*c^9*d + 675*a^3*b^8*c^8*d^2 + 3600*a^4*b^7*c^7*d^3 + 8820*a^5*b^6*c^6*d^4 + 10584*a^6*b^5*c^5*d^5 + 6300*a^7*b^4*c^4*d^6 + 1800*a^8*b^3*c^3*d^7 + 225*a^9*b^2*c^2*d^8 + 10*a^{10}*b*c*d^9) + x^{12}*((b^{11}*c^{10})/12 + (11*a^{10}*b*d^{10})/12 + (275*a^9*b^2*c*d^9)/6 + (825*a^2*b^9*c^8*d^2)/4 + 1650*a^3*b^8*c^7*d^3 + 5775*a^4*b^7*c^6*d^4 + 9702*a^5*b^6*c^5*d^5 + 8085*a^6*b^5*c^4*d^6 + 3300*a^7*b^4*c^3*d^7 + (2475*a^8*b^3*c^2*d^8)/4 + (55*a*b^{10}*c^9*d)/6) + x^5*(66*a^7*b^4*c^{10} + 42*a^{11}*c^6*d^4 + 330*a^8*b^3*c^9*d + 264*a^{10}*b*c^7*d^3 + 495*a^9*b^2*c^8*d^2) + x^{18}*((55*a^4*b^7*d^{10})/3 + (35*b^{11}*c^4*d^6)/3 + (220*a*b^{10}*c^3*d^7)/3 + (275*a^3*b^8*c*d^9)/3 + (275*a^2*b^9*c^2*d^8)/2) + x^8*((165*a^4*b^7*c^{10})/4 + 15*a^{11}*c^3*d^7 + (1155*a^5*b^6*c^9*d)/2 + (1155*a^{10}*b*c^4*d^6)/4 + (10395*a^6*b^5*c^8*d^2)/4 + 4950*a^7*b^4*c^7*d^3 + (17325*a^8*b^3*c^6*d^4)/4 + (3465*a^9*b^2*c^5*d^5)/2) + x^{15}((22*a^7*b^4*d^{10} + 8*b^{11}*c^7*d^3 + 154*a*b^{10}*c^6*d^4 + 308*a^6*b^5*c*d^9 + 924*a^2*b^9*c^5*d^5 + 2310*a^3*b^8*c^4*d^6 + 2640*a^4*b^7*c^3*d^7 + 1386*a^5*b^6*c^2*d^8) + x^6*(77*a^6*b^5*c^{10} + 42*a^{11}*c^5*d^5 + 550*a^7*b^4*c^9*d + 385*a^{10}*b*c^6*d^4 + (2475*a^8*b^3*c^8*d^2)/2 + 1100*a^9*b^2*c^7*d^3) + x^{17}((462*a^5*b^6*d^{10})/17 + (252*b^{11}*c^5*d^5)/17 + (2310*a*b^{10}*c^4*d^6)/17 + (3300*a^4*b^7*c*d^9)/17 + (6600*a^2*b^9*c^3*d^7)/17 + (7425*a^3*b^8*c^2*d^8)/17) + x^9*((55*a^3*b^8*c^{10})/3 + 5*a^{11}*c^2*d^8 + (1100*a^4*b^7*c^9*d)/3 + (440*a^{10}*b*c^3*d^7)/3 + 2310*a^5*b^6*c^8*d^2 + 6160*a^6*b^5*c^7*d^3 + 7700*a^7*b^4*c^6*d^4 + 4620*a^8*b^3*c^5*d^5 + (3850*a^9*b^2*c^4*d^6)/3) + x^{14}((165*a^8*b^3*d^{10})/14 + (45*b^{11}*c^8*d^2)/14 + (660*a*b^{10}*c^7*d^3)/7 + (1650*a^7*b^4*c*d^9)/7 + 825*a^2*b^9*c^6*d^4 + 2970*a^3*b^8*c^5*d^5 + 4950*a^4*b^7*c^4*d^6 + 3960*a^5*b^6*c^3*d^7 + 1485*a^6*b^5*c^2*d^8) + x^{10}*(a^{11}*c*d^9 + (11*a^2*b^9*c^{10})/2 + 165*a^3*b^8*c^9*d + (99*a^{10}*b*c^2*d^8)/2 + 1485*a^4*b^7*c^8*d^2 + 5544*a^5*b^6*c^7*d^3 + 9702*a^6*b^5*c^6*d^4 + 8316*a^7*b^4*c^5*d^5 + 3465*a^8*b^3*c^4*d^6 + 660*a^9*b^2*c^3*d^7) + x^{13}(((10*b^{11}*c^9*d)/13 + (55*a^9*b^2*d^{10})/13 + (495*a*b^{10}*c^8*d^2)/13 + (1650*a^8*b^3*c*d^9)/13 + (6600*a^2*b^9*c^7*d^3)/13 + (34650*a^3*b^8*c^6*d^4)/13 + (83160*a^4*b^7*c^5*d^5)/13 + (97020*a^5*b^6*c^4*d^6)/13 + (55440*a^6*b^5*c^3*d^7)/13 + (14850*a^7*b^4*c^2*d^8)/13) + a^{11}*c^{10}*x + (b^{11}*d^{10}*x^{22})/22 + (5*a^8*c^7*x^4*(24*a^3*d^3 + 33*b^3*c^3 + 110*a*b^2*c^2*d + 99*a^2*b*c*d^2))/4 + (5*b^8*d^7*x^{19}*(33*a^3*d^3 + 24*b^3*c^3 + 99*a*b^2*c^2*d + 110*a^2*b*c*d^2))/19 + (a^{10}*c^9*x^2*(10*a*d + 11*b*c))/2 + (b^{10}*d^9*x^{21}*(11*a*d + 10*b*c))/21 + (5*a^9*c^8*x^3*(9*a^2*d^2 + 11*b^2*c^2 + 22*a*b*c*d))/3 + (b^9*d^8*x^{20}*(11*a^2*d^2 + 9*b^2*c^2 + 22*a*b*c*d))/4
\end{aligned}$$

sympy [B] time = 0.34, size = 1965, normalized size = 7.04

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**11*(d*x+c)**10,x)

[Out] a**11*c**10*x + b**11*d**10*x**22/22 + x**21*(11*a*b**10*d**10/21 + 10*b**11

$$\begin{aligned}
& 1*c*d**9/21) + x**20*(11*a**2*b**9*d**10/4 + 11*a*b**10*c*d**9/2 + 9*b**11* \\
& c**2*d**8/4) + x**19*(165*a**3*b**8*d**10/19 + 550*a**2*b**9*c*d**9/19 + 49 \\
& 5*a*b**10*c**2*d**8/19 + 120*b**11*c**3*d**7/19) + x**18*(55*a**4*b**7*d**1 \\
& 0/3 + 275*a**3*b**8*c*d**9/3 + 275*a**2*b**9*c**2*d**8/2 + 220*a*b**10*c**3 \\
& *d**7/3 + 35*b**11*c**4*d**6/3) + x**17*(462*a**5*b**6*d**10/17 + 3300*a**4 \\
& *b**7*c*d**9/17 + 7425*a**3*b**8*c**2*d**8/17 + 6600*a**2*b**9*c**3*d**7/17 \\
& + 2310*a*b**10*c**4*d**6/17 + 252*b**11*c**5*d**5/17) + x**16*(231*a**6*b* \\
& *5*d**10/8 + 1155*a**5*b**6*c*d**9/4 + 7425*a**4*b**7*c**2*d**8/8 + 2475*a* \\
& *3*b**8*c**3*d**7/2 + 5775*a**2*b**9*c**4*d**6/8 + 693*a*b**10*c**5*d**5/4 \\
& + 105*b**11*c**6*d**4/8) + x**15*(22*a**7*b**4*d**10 + 308*a**6*b**5*c*d**9 \\
& + 1386*a**5*b**6*c**2*d**8 + 2640*a**4*b**7*c**3*d**7 + 2310*a**3*b**8*c** \\
& 4*d**6 + 924*a**2*b**9*c**5*d**5 + 154*a*b**10*c**6*d**4 + 8*b**11*c**7*d** \\
& 3) + x**14*(165*a**8*b**3*d**10/14 + 1650*a**7*b**4*c*d**9/7 + 1485*a**6*b* \\
& *5*c**2*d**8 + 3960*a**5*b**6*c**3*d**7 + 4950*a**4*b**7*c**4*d**6 + 2970*a \\
& **3*b**8*c**5*d**5 + 825*a**2*b**9*c**6*d**4 + 660*a*b**10*c**7*d**3/7 + 45 \\
& *b**11*c**8*d**2/14) + x**13*(55*a**9*b**2*d**10/13 + 1650*a**8*b**3*c*d**9 \\
& /13 + 14850*a**7*b**4*c**2*d**8/13 + 55440*a**6*b**5*c**3*d**7/13 + 97020*a \\
& **5*b**6*c**4*d**6/13 + 83160*a**4*b**7*c**5*d**5/13 + 34650*a**3*b**8*c**6 \\
& *d**4/13 + 6600*a**2*b**9*c**7*d**3/13 + 495*a*b**10*c**8*d**2/13 + 10*b**1 \\
& 1*c**9*d/13) + x**12*(11*a**10*b*d**10/12 + 275*a**9*b**2*c*d**9/6 + 2475*a \\
& **8*b**3*c**2*d**8/4 + 3300*a**7*b**4*c**3*d**7 + 8085*a**6*b**5*c**4*d**6 \\
& + 9702*a**5*b**6*c**5*d**5 + 5775*a**4*b**7*c**6*d**4 + 1650*a**3*b**8*c**7 \\
& *d**3 + 825*a**2*b**9*c**8*d**2/4 + 55*a*b**10*c**9*d/6 + b**11*c**10/12) + \\
& x**11*(a**11*d**10/11 + 10*a**10*b*c*d**9 + 225*a**9*b**2*c**2*d**8 + 1800 \\
& *a**8*b**3*c**3*d**7 + 6300*a**7*b**4*c**4*d**6 + 10584*a**6*b**5*c**5*d**5 \\
& + 8820*a**5*b**6*c**6*d**4 + 3600*a**4*b**7*c**7*d**3 + 675*a**3*b**8*c**8 \\
& *d**2 + 50*a**2*b**9*c**9*d + a*b**10*c**10) + x**10*(a**11*c*d**9 + 99*a** \\
& 10*b*c**2*d**8/2 + 660*a**9*b**2*c**3*d**7 + 3465*a**8*b**3*c**4*d**6 + 831 \\
& 6*a**7*b**4*c**5*d**5 + 9702*a**6*b**5*c**6*d**4 + 5544*a**5*b**6*c**7*d**3 \\
& + 1485*a**4*b**7*c**8*d**2 + 165*a**3*b**8*c**9*d + 11*a**2*b**9*c**10/2) \\
& + x**9*(5*a**11*c**2*d**8 + 440*a**10*b*c**3*d**7/3 + 3850*a**9*b**2*c**4*d \\
& **6/3 + 4620*a**8*b**3*c**5*d**5 + 7700*a**7*b**4*c**6*d**4 + 6160*a**6*b** \\
& 5*c**7*d**3 + 2310*a**5*b**6*c**8*d**2 + 1100*a**4*b**7*c**9*d/3 + 55*a**3* \\
& b**8*c**10/3) + x**8*(15*a**11*c**3*d**7 + 1155*a**10*b*c**4*d**6/4 + 3465* \\
& a**9*b**2*c**5*d**5/2 + 17325*a**8*b**3*c**6*d**4/4 + 4950*a**7*b**4*c**7*d \\
& **3 + 10395*a**6*b**5*c**8*d**2/4 + 1155*a**5*b**6*c**9*d/2 + 165*a**4*b**7 \\
& *c**10/4) + x**7*(30*a**11*c**4*d**6 + 396*a**10*b*c**5*d**5 + 1650*a**9*b* \\
& *2*c**6*d**4 + 19800*a**8*b**3*c**7*d**3/7 + 14850*a**7*b**4*c**8*d**2/7 + \\
& 660*a**6*b**5*c**9*d + 66*a**5*b**6*c**10) + x**6*(42*a**11*c**5*d**5 + 385 \\
& *a**10*b*c**6*d**4 + 1100*a**9*b**2*c**7*d**3 + 2475*a**8*b**3*c**8*d**2/2 \\
& + 550*a**7*b**4*c**9*d + 77*a**6*b**5*c**10) + x**5*(42*a**11*c**6*d**4 + 2 \\
& 64*a**10*b*c**7*d**3 + 495*a**9*b**2*c**8*d**2 + 330*a**8*b**3*c**9*d + 66* \\
& a**7*b**4*c**10) + x**4*(30*a**11*c**7*d**3 + 495*a**10*b*c**8*d**2/4 + 275 \\
& *a**9*b**2*c**9*d/2 + 165*a**8*b**3*c**10/4) + x**3*(15*a**11*c**8*d**2 + 1 \\
& 10*a**10*b*c**9*d/3 + 55*a**9*b**2*c**10/3) + x**2*(5*a**11*c**9*d + 11*a**
\end{aligned}$$

10*b*c**10/2)

3.1301 $\int (a + bx)^{10}(c + dx)^{10} dx$

Optimal. Leaf size=279

$$\frac{d^9(a+bx)^{20}(bc-ad)}{2b^{11}} + \frac{45d^8(a+bx)^{19}(bc-ad)^2}{19b^{11}} + \frac{20d^7(a+bx)^{18}(bc-ad)^3}{3b^{11}} + \frac{210d^6(a+bx)^{17}(bc-ad)^4}{17b^{11}} + \frac{63d^5(a+bx)^{16}(bc-ad)^5}{11b^{11}}$$

[Out] $1/11*(-a*d+b*c)^{10}*(b*x+a)^{11}/b^{11}+5/6*d*(-a*d+b*c)^9*(b*x+a)^{12}/b^{11}+45/13*d^2*(-a*d+b*c)^8*(b*x+a)^{13}/b^{11}+60/7*d^3*(-a*d+b*c)^7*(b*x+a)^{14}/b^{11}+14*d^4*(-a*d+b*c)^6*(b*x+a)^{15}/b^{11}+63/4*d^5*(-a*d+b*c)^5*(b*x+a)^{16}/b^{11}+210/17*d^6*(-a*d+b*c)^4*(b*x+a)^{17}/b^{11}+20/3*d^7*(-a*d+b*c)^3*(b*x+a)^{18}/b^{11}+4/19*d^8*(-a*d+b*c)^2*(b*x+a)^{19}/b^{11}+1/2*d^9*(-a*d+b*c)*(b*x+a)^{20}/b^{11}+1/21*d^{10}*(b*x+a)^{21}/b^{11}$

Rubi [A] time = 1.11, antiderivative size = 279, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{d^9(a+bx)^{20}(bc-ad)}{2b^{11}} + \frac{45d^8(a+bx)^{19}(bc-ad)^2}{19b^{11}} + \frac{20d^7(a+bx)^{18}(bc-ad)^3}{3b^{11}} + \frac{210d^6(a+bx)^{17}(bc-ad)^4}{17b^{11}} + \frac{63d^5(a+bx)^{16}(bc-ad)^5}{11b^{11}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^10*(c + d*x)^10,x]

[Out] $((b*c - a*d)^{10}*(a + b*x)^{11})/(11*b^{11}) + (5*d*(b*c - a*d)^9*(a + b*x)^{12})/(6*b^{11}) + (45*d^2*(b*c - a*d)^8*(a + b*x)^{13})/(13*b^{11}) + (60*d^3*(b*c - a*d)^7*(a + b*x)^{14})/(7*b^{11}) + (14*d^4*(b*c - a*d)^6*(a + b*x)^{15})/b^{11} + (63*d^5*(b*c - a*d)^5*(a + b*x)^{16})/(4*b^{11}) + (210*d^6*(b*c - a*d)^4*(a + b*x)^{17})/(17*b^{11}) + (20*d^7*(b*c - a*d)^3*(a + b*x)^{18})/(3*b^{11}) + (45*d^8*(b*c - a*d)^2*(a + b*x)^{19})/(19*b^{11}) + (d^9*(b*c - a*d)*(a + b*x)^{20})/(2*b^{11}) + (d^{10}*(a + b*x)^{21})/(21*b^{11})$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int (a + bx)^{10}(c + dx)^{10} dx = \int \left(\frac{(bc - ad)^{10}(a + bx)^{10}}{b^{10}} + \frac{10d(bc - ad)^9(a + bx)^{11}}{b^{10}} + \frac{45d^2(bc - ad)^8(a + bx)^{12}}{b^{10}} + \frac{120d^3(bc - ad)^7(a + bx)^{13}}{b^{10}} + \frac{105d^4(bc - ad)^6(a + bx)^{14}}{b^{10}} + \frac{45d^5(bc - ad)^5(a + bx)^{15}}{b^{10}} + \frac{10d^6(bc - ad)^4(a + bx)^{16}}{b^{10}} + \frac{3d^7(bc - ad)^3(a + bx)^{17}}{b^{10}} + \frac{d^8(bc - ad)^2(a + bx)^{18}}{b^{10}} + \frac{d^9(bc - ad)(a + bx)^{19}}{b^{10}} + \frac{d^{10}(a + bx)^{20}}{b^{10}} \right)$$

$$= \frac{(bc - ad)^{10}(a + bx)^{11}}{11b^{11}} + \frac{5d(bc - ad)^9(a + bx)^{12}}{6b^{11}} + \frac{45d^2(bc - ad)^8(a + bx)^{13}}{13b^{11}} + \frac{60d^3(bc - ad)^7(a + bx)^{14}}{13b^{11}} + \frac{105d^4(bc - ad)^6(a + bx)^{15}}{13b^{11}} + \frac{45d^5(bc - ad)^5(a + bx)^{16}}{13b^{11}} + \frac{10d^6(bc - ad)^4(a + bx)^{17}}{13b^{11}} + \frac{3d^7(bc - ad)^3(a + bx)^{18}}{13b^{11}} + \frac{d^8(bc - ad)^2(a + bx)^{19}}{13b^{11}} + \frac{d^9(bc - ad)(a + bx)^{20}}{13b^{11}} + \frac{d^{10}(a + bx)^{21}}{13b^{11}}$$

Mathematica [B] time = 0.17, size = 1539, normalized size = 5.52

$$\frac{1}{21}b^{10}d^{10}x^{21} + \frac{1}{2}b^9d^9(bc+ad)x^{20} + \frac{5}{19}b^8d^8(9b^2c^2 + 20abdc + 9a^2d^2)x^{19} + \frac{5}{3}b^7d^7(4b^3c^3 + 15ab^2dc^2 + 15a^2bd^2c + 4a^3d^3)x^{18} + \frac{5}{3}b^7d^7(4b^3c^3 + 15ab^2dc^2 + 15a^2bd^2c + 4a^3d^3)x^{18} + \frac{5}{3}b^7d^7(4b^3c^3 + 15ab^2dc^2 + 15a^2bd^2c + 4a^3d^3)x^{18} + \dots$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^10*(c + d*x)^10,x]

[Out] a^10*c^10*x + 5*a^9*c^9*(b*c + a*d)*x^2 + (5*a^8*c^8*(9*b^2*c^2 + 20*a*b*c*d + 9*a^2*d^2)*x^3)/3 + (15*a^7*c^7*(4*b^3*c^3 + 15*a*b^2*c^2*d + 15*a^2*b*c*d^2 + 4*a^3*d^3)*x^4)/2 + 3*a^6*c^6*(14*b^4*c^4 + 80*a*b^3*c^3*d + 135*a^2*b^2*c^2*d^2 + 80*a^3*b*c*d^3 + 14*a^4*d^4)*x^5 + 2*a^5*c^5*(21*b^5*c^5 + 175*a*b^4*c^4*d + 450*a^2*b^3*c^3*d^2 + 450*a^3*b^2*c^2*d^3 + 175*a^4*b*c*d^4 + 21*a^5*d^5)*x^6 + (30*a^4*c^4*(7*b^6*c^6 + 84*a*b^5*c^5*d + 315*a^2*b^4*c^4*d^2 + 480*a^3*b^3*c^3*d^3 + 315*a^4*b^2*c^2*d^4 + 84*a^5*b*c*d^5 + 7*a^6*d^6)*x^7)/7 + (15*a^3*c^3*(2*b^7*c^7 + 35*a*b^6*c^6*d + 189*a^2*b^5*c^5*d^2 + 420*a^3*b^4*c^4*d^3 + 420*a^4*b^3*c^3*d^4 + 189*a^5*b^2*c^2*d^5 + 35*a^6*b*c*d^6 + 2*a^7*d^7)*x^8)/2 + (5*a^2*c^2*(3*b^8*c^8 + 80*a*b^7*c^7*d + 630*a^2*b^6*c^6*d^2 + 2016*a^3*b^5*c^5*d^3 + 2940*a^4*b^4*c^4*d^4 + 2016*a^5*b^3*c^3*d^5 + 630*a^6*b^2*c^2*d^6 + 80*a^7*b*c*d^7 + 3*a^8*d^8)*x^9)/3 + a*c*(b^9*c^9 + 45*a*b^8*c^8*d + 540*a^2*b^7*c^7*d^2 + 2520*a^3*b^6*c^6*d^3 + 5292*a^4*b^5*c^5*d^4 + 5292*a^5*b^4*c^4*d^5 + 2520*a^6*b^3*c^3*d^6 + 540*a^7*b^2*c^2*d^7 + 45*a^8*b*c*d^8 + a^9*d^9)*x^10 + ((b^10*c^10 + 100*a*b^9*c^9*d + 2025*a^2*b^8*c^8*d^2 + 14400*a^3*b^7*c^7*d^3 + 44100*a^4*b^6*c^6*d^4 + 63504*a^5*b^5*c^5*d^5 + 44100*a^6*b^4*c^4*d^6 + 14400*a^7*b^3*c^3*d^7 + 2025*a^8*b^2*c^2*d^8 + 100*a^9*b*c*d^9 + a^10*d^10)*x^11)/11 + (5*b*d*(b^9*c^9 + 45*a*b^8*c^8*d + 540*a^2*b^7*c^7*d^2 + 2520*a^3*b^6*c^6*d^3 + 5292*a^4*b^5*c^5*d^4 + 5292*a^5*b^4*c^4*d^5 + 2520*a^6*b^3*c^3*d^6 + 540*a^7*b^2*c^2*d^7 + 45*a^8*b*c*d^8 + a^9*d^9)*x^12)/6 + (15*b^2*d^2*(3*b^8*c^8 + 80*a*b^7*c^7*d + 630*a^2*b^6*c^6*d^2 + 2016*a^3*b^5*c^5*d^3 + 2940*a^4*b^4*c^4*d^4 + 2016*a^5*b^3*c^3*d^5 + 630*a^6*b^2*c^2*d^6 + 80*a^7*b*c*d^7 + 3*a^8*d^8)*x^13)/13 + (30*b^3*d^3*(2*b^7*c^7 + 35*a*b^6*c^6*d + 189*a^2*b^5*c^5*d^2 + 420*a^3*b^4*c^4*d^3 + 420*a^4*b^3*c^3*d^4 + 189*a^5*b^2*c^2*d^5 + 35*a^6*b*c*d^6 + 2*a^7*d^7)*x^14)/7 + 2*b^4*d^4*(7*b^6*c^6 + 84*a*b^5*c^5*d + 315*a^2*b^4*c^4*d^2 + 480*a^3*b^3*c^3*d^3 + 315*a^4*b^2*c^2*d^4 + 84*a^5*b*c*d^5 + 7*a^6*d^6)*x^15 + (3*b^5*d^5*(21*b^5*c^5 + 175*a*b^4*c^4*d + 450*a^2*b^3*c^3*d^2 + 450*a^3*b^2*c^2*d^3 + 175*a^4*b*c*d^4 + 21*a^5*d^5)*x^16)/5 + (30*b^6*d^6*(15*b^6*c^6 + 120*a*b^5*c^5*d + 540*a^2*b^4*c^4*d^2 + 1080*a^3*b^3*c^3*d^3 + 540*a^4*b^2*c^2*d^4 + 120*a^5*b*c*d^5 + 3*a^6*d^6)*x^17)/6 + (15*b^7*d^7*(10*b^7*c^7 + 70*a*b^6*c^6*d + 2520*a^2*b^5*c^5*d^2 + 5040*a^3*b^4*c^4*d^3 + 2520*a^4*b^3*c^3*d^4 + 700*a^5*b^2*c^2*d^5 + 140*a^6*b*c*d^6 + 15*a^7*d^7)*x^18)/10 + (5*b^8*d^8*(5*b^8*c^8 + 40*a*b^7*c^7*d + 1260*a^2*b^6*c^6*d^2 + 2520*a^3*b^5*c^5*d^3 + 1260*a^4*b^4*c^4*d^4 + 400*a^5*b^3*c^3*d^5 + 80*a^6*b^2*c^2*d^6 + 10*a^7*b*c*d^7 + 5*a^8*d^8)*x^19)/5 + (b^9*d^9*(b^9*c^9 + 90*a*b^8*c^8*d + 2700*a^2*b^7*c^7*d^2 + 5400*a^3*b^6*c^6*d^3 + 2700*a^4*b^5*c^5*d^4 + 900*a^5*b^4*c^4*d^5 + 180*a^6*b^3*c^3*d^6 + 30*a^7*b^2*c^2*d^7 + 3*a^8*b*c*d^8 + a^9*d^9)*x^20)/9 + (d^10*(b^10*c^10 + 100*a*b^9*c^9*d + 2025*a^2*b^8*c^8*d^2 + 14400*a^3*b^7*c^7*d^3 + 44100*a^4*b^6*c^6*d^4 + 63504*a^5*b^5*c^5*d^5 + 44100*a^6*b^4*c^4*d^6 + 14400*a^7*b^3*c^3*d^7 + 2025*a^8*b^2*c^2*d^8 + 100*a^9*b*c*d^9 + a^10*d^10)*x^21)/10

$$\begin{aligned} & *b^3*c^3*d^2 + 450*a^3*b^2*c^2*d^3 + 175*a^4*b*c*d^4 + 21*a^5*d^5)*x^{16})/4 \\ & + (15*b^6*d^6*(14*b^4*c^4 + 80*a*b^3*c^3*d + 135*a^2*b^2*c^2*d^2 + 80*a^3*b \\ & *c*d^3 + 14*a^4*d^4)*x^{17})/17 + (5*b^7*d^7*(4*b^3*c^3 + 15*a*b^2*c^2*d + 15 \\ & *a^2*b*c*d^2 + 4*a^3*d^3)*x^{18})/3 + (5*b^8*d^8*(9*b^2*c^2 + 20*a*b*c*d + 9* \\ & a^2*d^2)*x^{19})/19 + (b^9*d^9*(b*c + a*d)*x^{20})/2 + (b^{10}*d^{10}*x^{21})/21 \end{aligned}$$

fricas [B] time = 0.38, size = 1833, normalized size = 6.57

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10*(d*x+c)^10,x, algorithm="fricas")

[Out] $1/21*x^{21}*d^{10}*b^{10} + 1/2*x^{20}*d^9*c*b^{10} + 1/2*x^{20}*d^{10}*b^9*a + 45/19*x^{19}*d^8*c^2*b^{10} + 100/19*x^{19}*d^9*c*b^9*a + 45/19*x^{19}*d^{10}*b^8*a^2 + 20/3*x^{18}*d^7*c^3*b^{10} + 25*x^{18}*d^8*c^2*b^9*a + 25*x^{18}*d^9*c*b^8*a^2 + 20/3*x^{18}*d^{10}*b^7*a^3 + 210/17*x^{17}*d^6*c^4*b^{10} + 1200/17*x^{17}*d^7*c^3*b^9*a + 2025/17*x^{17}*d^8*c^2*b^8*a^2 + 1200/17*x^{17}*d^9*c*b^7*a^3 + 210/17*x^{17}*d^{10}*b^6*a^4 + 63/4*x^{16}*d^5*c^5*b^{10} + 525/4*x^{16}*d^6*c^4*b^9*a + 675/2*x^{16}*d^7*c^3*b^8*a^2 + 675/2*x^{16}*d^8*c^2*b^7*a^3 + 525/4*x^{16}*d^9*c*b^6*a^4 + 63/4*x^{16}*d^{10}*b^5*a^5 + 14*x^{15}*d^4*c^6*b^{10} + 168*x^{15}*d^5*c^5*b^9*a + 630*x^{15}*d^6*c^4*b^8*a^2 + 960*x^{15}*d^7*c^3*b^7*a^3 + 630*x^{15}*d^8*c^2*b^6*a^4 + 168*x^{15}*d^9*c*b^5*a^5 + 14*x^{15}*d^{10}*b^4*a^6 + 60/7*x^{14}*d^3*c^7*b^{10} + 150*x^{14}*d^4*c^6*b^9*a + 810*x^{14}*d^5*c^5*b^8*a^2 + 1800*x^{14}*d^6*c^4*b^7*a^3 + 1800*x^{14}*d^7*c^3*b^6*a^4 + 810*x^{14}*d^8*c^2*b^5*a^5 + 150*x^{14}*d^9*c*b^4*a^6 + 60/7*x^{14}*d^{10}*b^3*a^7 + 45/13*x^{13}*d^2*c^8*b^{10} + 1200/13*x^{13}*d^3*c^7*b^9*a + 9450/13*x^{13}*d^4*c^6*b^8*a^2 + 30240/13*x^{13}*d^5*c^5*b^7*a^3 + 44100/13*x^{13}*d^6*c^4*b^6*a^4 + 30240/13*x^{13}*d^7*c^3*b^5*a^5 + 9450/13*x^{13}*d^8*c^2*b^4*a^6 + 1200/13*x^{13}*d^9*c*b^3*a^7 + 45/13*x^{13}*d^{10}*b^2*a^8 + 5/6*x^{12}*d*c^9*b^{10} + 75/2*x^{12}*d^2*c^8*b^9*a + 450*x^{12}*d^3*c^7*b^8*a^2 + 2100*x^{12}*d^4*c^6*b^7*a^3 + 4410*x^{12}*d^5*c^5*b^6*a^4 + 4410*x^{12}*d^6*c^4*b^5*a^5 + 2100*x^{12}*d^7*c^3*b^4*a^6 + 450*x^{12}*d^8*c^2*b^3*a^7 + 75/2*x^{12}*d^9*c*b^2*a^8 + 5/6*x^{12}*d^{10}*b*a^9 + 1/11*x^{11}*c^{10}*b^{10} + 100/11*x^{11}*d*c^9*b^9*a + 2025/11*x^{11}*d^2*c^8*b^8*a^2 + 14400/11*x^{11}*d^3*c^7*b^7*a^3 + 44100/11*x^{11}*d^4*c^6*b^6*a^4 + 63504/11*x^{11}*d^5*c^5*b^5*a^5 + 44100/11*x^{11}*d^6*c^4*b^4*a^6 + 14400/11*x^{11}*d^7*c^3*b^3*a^7 + 2025/11*x^{11}*d^8*c^2*b^2*a^8 + 100/11*x^{11}*d^9*c*b*a^9 + 1/11*x^{11}*d^{10}*a^{10} + x^{10}*c^{10}*b^9*a + 45*x^{10}*d*c^9*b^8*a^2 + 540*x^{10}*d^2*c^8*b^7*a^3 + 2520*x^{10}*d^3*c^7*b^6*a^4 + 5292*x^{10}*d^4*c^6*b^5*a^5 + 5292*x^{10}*d^5*c^5*b^4*a^6 + 2520*x^{10}*d^6*c^4*b^3*a^7 + 540*x^{10}*d^7*c^3*b^2*a^8 + 45*x^{10}*d^8*c^2*b*a^9 + x^{10}*d^9*c*a^{10} + 5*x^9*c^{10}*b^8*a^2 + 400/3*x^9*d*c^9*b^7*a^3 + 1050*x^9*d^2*c^8*b^6*a^4 + 3360*x^9*d^3*c^7*b^5*a^5 + 4900*x^9*d^4*c^6*b^4*a^6 + 3360*x^9*d^5*c^5*b^3*a^7 + 1050*x^9*d^6*c^4*b^2*a^8 + 400/3*x^9*d^7*c^3*b*a^9 + 5*x^9*d^8*c^2*a^{10} + 15*x^8*c^{10}*b^7*a^3 + 525/2*x^8*d*c^9*b^6*a^4 + 2835/2*x^8*d^2*c^8*b^5*a^5 + 3150*x^8*d^3*c^7*b^4*a^6 + 3150*x^8*d^4*c^6*b^3*a^7 + 2835/2*x$

$$\begin{aligned} &^8*d^5*c^5*b^2*a^8 + 525/2*x^8*d^6*c^4*b*a^9 + 15*x^8*d^7*c^3*a^10 + 30*x^7 \\ &*c^10*b^6*a^4 + 360*x^7*d*c^9*b^5*a^5 + 1350*x^7*d^2*c^8*b^4*a^6 + 14400/7* \\ &x^7*d^3*c^7*b^3*a^7 + 1350*x^7*d^4*c^6*b^2*a^8 + 360*x^7*d^5*c^5*b*a^9 + 30 \\ &*x^7*d^6*c^4*a^10 + 42*x^6*c^10*b^5*a^5 + 350*x^6*d*c^9*b^4*a^6 + 900*x^6*d \\ &^2*c^8*b^3*a^7 + 900*x^6*d^3*c^7*b^2*a^8 + 350*x^6*d^4*c^6*b*a^9 + 42*x^6*d \\ &^5*c^5*a^10 + 42*x^5*c^10*b^4*a^6 + 240*x^5*d*c^9*b^3*a^7 + 405*x^5*d^2*c^8 \\ &*b^2*a^8 + 240*x^5*d^3*c^7*b*a^9 + 42*x^5*d^4*c^6*a^10 + 30*x^4*c^10*b^3*a^ \\ &7 + 225/2*x^4*d*c^9*b^2*a^8 + 225/2*x^4*d^2*c^8*b*a^9 + 30*x^4*d^3*c^7*a^10 \\ &+ 15*x^3*c^10*b^2*a^8 + 100/3*x^3*d*c^9*b*a^9 + 15*x^3*d^2*c^8*a^10 + 5*x^ \\ &2*c^10*b*a^9 + 5*x^2*d*c^9*a^10 + x*c^10*a^10 \end{aligned}$$

giac [B] time = 1.34, size = 1833, normalized size = 6.57

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10*(d*x+c)^10,x, algorithm="giac")

[Out] $\frac{1}{21}b^{10}d^{10}x^{21} + \frac{1}{2}b^{10}c^9d^9x^{20} + \frac{1}{2}ab^9d^{10}x^{20} + \frac{45}{19}b^{10}c^2d^8x^{19} + \frac{100}{19}ab^9c^9d^9x^{19} + \frac{45}{19}a^2b^8d^{10}x^{19} + \frac{20}{3}b^{10}c^3d^7x^{18} + 25ab^9c^2d^8x^{18} + 25a^2b^8c^9d^9x^{18} + \frac{20}{3}a^3b^7d^{10}x^{18} + \frac{210}{17}b^{10}c^4d^6x^{17} + \frac{1200}{17}ab^9c^3d^7x^{17} + \frac{20}{25}a^2b^8c^2d^8x^{17} + \frac{1200}{17}a^3b^7c^9d^9x^{17} + \frac{210}{17}a^4b^6d^{10}x^{17} + \frac{63}{4}b^{10}c^5d^5x^{16} + \frac{525}{4}ab^9c^4d^6x^{16} + \frac{675}{2}a^2b^8c^3d^7x^{16} + \frac{675}{2}a^3b^7c^2d^8x^{16} + \frac{525}{4}a^4b^6c^9d^9x^{16} + \frac{63}{4}a^5b^5d^{10}x^{16} + 14b^{10}c^6d^4x^{15} + 168ab^9c^5d^5x^{15} + 630a^2b^8c^4d^6x^{15} + 960a^3b^7c^3d^7x^{15} + 630a^4b^6c^2d^8x^{15} + 168a^5b^5c^9d^9x^{15} + 14a^6b^4d^{10}x^{15} + \frac{60}{7}b^{10}c^7d^3x^{14} + 150ab^9c^6d^4x^{14} + 810a^2b^8c^5d^5x^{14} + 1800a^3b^7c^4d^6x^{14} + 1800a^4b^6c^3d^7x^{14} + 810a^5b^5c^2d^8x^{14} + 150a^6b^4c^9d^9x^{14} + \frac{60}{7}a^7b^3d^{10}x^{14} + \frac{45}{13}b^{10}c^8d^2x^{13} + \frac{1200}{13}ab^9c^7d^3x^{13} + \frac{9450}{13}a^2b^8c^6d^4x^{13} + \frac{30240}{13}a^3b^7c^5d^5x^{13} + \frac{44100}{13}a^4b^6c^4d^6x^{13} + \frac{30240}{13}a^5b^5c^3d^7x^{13} + \frac{9450}{13}a^6b^4c^2d^8x^{13} + \frac{1200}{13}a^7b^3c^9d^9x^{13} + \frac{45}{13}a^8b^2d^{10}x^{13} + \frac{5}{6}b^{10}c^9d^1x^{12} + \frac{75}{2}ab^9c^8d^2x^{12} + 450a^2b^8c^7d^3x^{12} + 2100a^3b^7c^6d^4x^{12} + 4410a^4b^6c^5d^5x^{12} + 4410a^5b^5c^4d^6x^{12} + 2100a^6b^4c^3d^7x^{12} + 450a^7b^3c^2d^8x^{12} + \frac{75}{2}a^8b^2c^9d^9x^{12} + \frac{5}{6}a^9b^1d^{10}x^{12} + \frac{1}{11}b^{10}c^{10}x^{11} + \frac{100}{11}ab^9c^9d^1x^{11} + \frac{2025}{11}a^2b^8c^8d^2x^{11} + \frac{14400}{11}a^3b^7c^7d^3x^{11} + \frac{44100}{11}a^4b^6c^6d^4x^{11} + \frac{63504}{11}a^5b^5c^5d^5x^{11} + \frac{44100}{11}a^6b^4c^4d^6x^{11} + \frac{14400}{11}a^7b^3c^3d^7x^{11} + \frac{2025}{11}a^8b^2c^2d^8x^{11} + \frac{100}{11}a^9b^1c^9d^9x^{11} + \frac{1}{11}a^{10}d^{10}x^{11} + ab^9c^{10}x^{10} + 45a^2b^8c^9d^1x^{10} + 540a^3b^7c^8d^2x^{10} + 2520a^4b^6c^7d^3x^{10} + 5292a^5b^5c^6d^4x^{10} + 5292a^6b^4c^5d^5x^{10} + 2520a^7b^3c^4d^6x^{10} + 540a^8b^2c^3d^7x^{10} + 45a^9b^1c^2d^8x^{10} + a^{10}c^9d^9x^{10}$

$$\begin{aligned}
& x^{10} + 5a^2b^8c^{10}x^9 + 400/3a^3b^7c^9d^2x^9 + 1050a^4b^6c^8d^2x^9 + 3360a^5b^5c^7d^3x^9 + 4900a^6b^4c^6d^4x^9 + 3360a^7b^3c^5d^5x^9 + 1050a^8b^2c^4d^6x^9 + 400/3a^9b^2c^3d^7x^9 + 5a^{10}c^2d^8x^9 + 15a^3b^7c^{10}x^8 + 525/2a^4b^6c^9d^2x^8 + 2835/2a^5b^5c^8d^2x^8 + 3150a^6b^4c^7d^3x^8 + 3150a^7b^3c^6d^4x^8 + 2835/2a^8b^2c^5d^5x^8 + 525/2a^9b^2c^4d^6x^8 + 15a^{10}c^3d^7x^8 + 30a^4b^6c^{10}x^7 + 360a^5b^5c^9d^2x^7 + 1350a^6b^4c^8d^2x^7 + 14400/7a^7b^3c^7d^3x^7 + 1350a^8b^2c^6d^4x^7 + 360a^9b^2c^5d^5x^7 + 30a^{10}c^4d^6x^7 + 42a^5b^5c^{10}x^6 + 350a^6b^4c^9d^2x^6 + 900a^7b^3c^8d^2x^6 + 900a^8b^2c^7d^3x^6 + 350a^9b^2c^6d^4x^6 + 42a^{10}c^5d^5x^6 + 42a^6b^4c^{10}x^5 + 240a^7b^3c^9d^2x^5 + 405a^8b^2c^8d^2x^5 + 240a^9b^2c^7d^3x^5 + 42a^{10}c^6d^4x^5 + 30a^7b^3c^{10}x^4 + 225/2a^8b^2c^9d^2x^4 + 225/2a^9b^2c^8d^2x^4 + 30a^{10}c^7d^3x^4 + 15a^8b^2c^{10}x^3 + 100/3a^9b^2c^9d^2x^3 + 15a^{10}c^8d^2x^3 + 5a^9b^2c^{10}x^2 + 5a^{10}c^9d^2x^2 + a^{10}c^{10}x
\end{aligned}$$

maple [B] time = 0.00, size = 1591, normalized size = 5.70

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x+a)^{10}*(d*x+c)^{10}, x)$

[Out] $\begin{aligned}
& 1/21*b^{10}d^{10}x^{21} + 1/20*(10*a*b^9*d^{10} + 10*b^{10}*c*d^9)*x^{20} + 1/19*(45*a^2*b^8*d^{10} + 100*a*b^9*c*d^9 + 45*b^{10}*c^2*d^8)*x^{19} + 1/18*(120*a^3*b^7*d^{10} + 450*a^2*b^8*c*d^9 + 450*a*b^9*c^2*d^8 + 120*b^{10}*c^3*d^7)*x^{18} + 1/17*(210*a^4*b^6*d^{10} + 1200*a^3*b^7*c*d^9 + 2025*a^2*b^8*c^2*d^8 + 1200*a*b^9*c^3*d^7 + 210*b^{10}*c^4*d^6)*x^{17} + 1/16*(252*a^5*b^5*d^{10} + 2100*a^4*b^6*c*d^9 + 5400*a^3*b^7*c^2*d^8 + 5400*a^2*b^8*c^3*d^7 + 2100*a*b^9*c^4*d^6 + 252*b^{10}*c^5*d^5)*x^{16} + 1/15*(210*a^6*b^4*d^{10} + 2520*a^5*b^5*c*d^9 + 9450*a^4*b^6*c^2*d^8 + 14400*a^3*b^7*c^3*d^7 + 9450*a^2*b^8*c^4*d^6 + 2520*a*b^9*c^5*d^5 + 210*b^{10}*c^6*d^4)*x^{15} + 1/14*(120*a^7*b^3*d^{10} + 2100*a^6*b^4*c*d^9 + 11340*a^5*b^5*c^2*d^8 + 25200*a^4*b^6*c^3*d^7 + 25200*a^3*b^7*c^4*d^6 + 11340*a^2*b^8*c^5*d^5 + 2100*a*b^9*c^6*d^4 + 120*b^{10}*c^7*d^3)*x^{14} + 1/13*(45*a^8*b^2*d^{10} + 1200*a^7*b^3*c*d^9 + 9450*a^6*b^4*c^2*d^8 + 30240*a^5*b^5*c^3*d^7 + 44100*a^4*b^6*c^4*d^6 + 30240*a^3*b^7*c^5*d^5 + 9450*a^2*b^8*c^6*d^4 + 1200*a*b^9*c^7*d^3 + 45*b^{10}*c^8*d^2)*x^{13} + 1/12*(10*a^9*b*d^{10} + 450*a^8*b^2*c*d^9 + 5400*a^7*b^3*c^2*d^8 + 25200*a^6*b^4*c^3*d^7 + 52920*a^5*b^5*c^4*d^6 + 52920*a^4*b^6*c^5*d^5 + 25200*a^3*b^7*c^6*d^4 + 5400*a^2*b^8*c^7*d^3 + 450*a*b^9*c^8*d^2 + 10*b^{10}*c^9*d)*x^{12} + 1/11*(a^{10}*d^{10} + 100*a^9*b*c*d^9 + 2025*a^8*b^2*c^2*d^8 + 14400*a^7*b^3*c^3*d^7 + 44100*a^6*b^4*c^4*d^6 + 63504*a^5*b^5*c^5*d^5 + 44100*a^4*b^6*c^6*d^4 + 14400*a^3*b^7*c^7*d^3 + 2025*a^2*b^8*c^8*d^2 + 100*a*b^9*c^9*d + b^{10}*c^{10})*x^{11} + 1/10*(10*a^{10}*c*d^9 + 450*a^9*b^2*c^2*d^8 + 5400*a^8*b^2*c^3*d^7 + 25200*a^7*b^3*c^4*d^6 + 52920*a^6*b^4*c^5*d^5 + 52920*a^5*b^5*c^6*d^4 + 25200*a^4*b^6*c^7*d^3 + 5400*a^3*b^7*c^8*d^2 + 450*a^2*b^8*c^9*d + 10*a*b^9*c^{10})*x^{10} + 1/9*(45*a^{10}*c^2*d^8 + 1200*a^9*b^2*c^3*d^7 + 9450*a^8*b^2*c^4*d^6 + 30240*a^7*b^3*c^5*
\end{aligned}$

$$d^5+44100*a^6*b^4*c^6*d^4+30240*a^5*b^5*c^7*d^3+9450*a^4*b^6*c^8*d^2+1200*a^3*b^7*c^9*d+45*a^2*b^8*c^{10})*x^9+1/8*(120*a^{10}*c^3*d^7+2100*a^9*b*c^4*d^6+11340*a^8*b^2*c^5*d^5+25200*a^7*b^3*c^6*d^4+25200*a^6*b^4*c^7*d^3+11340*a^5*b^5*c^8*d^2+2100*a^4*b^6*c^9*d+120*a^3*b^7*c^{10})*x^8+1/7*(210*a^{10}*c^4*d^6+2520*a^9*b*c^5*d^5+9450*a^8*b^2*c^6*d^4+14400*a^7*b^3*c^7*d^3+9450*a^6*b^4*c^8*d^2+2520*a^5*b^5*c^9*d+210*a^4*b^6*c^{10})*x^7+1/6*(252*a^{10}*c^5*d^5+2100*a^9*b*c^6*d^4+5400*a^8*b^2*c^7*d^3+5400*a^7*b^3*c^8*d^2+2100*a^6*b^4*c^9*d+252*a^5*b^5*c^{10})*x^6+1/5*(210*a^{10}*c^6*d^4+1200*a^9*b*c^7*d^3+2025*a^8*b^2*c^8*d^2+1200*a^7*b^3*c^9*d+210*a^6*b^4*c^{10})*x^5+1/4*(120*a^{10}*c^7*d^3+450*a^9*b*c^8*d^2+450*a^8*b^2*c^9*d+120*a^7*b^3*c^{10})*x^4+1/3*(45*a^{10}*c^8*d^2+100*a^9*b*c^9*d+45*a^8*b^2*c^{10})*x^3+1/2*(10*a^{10}*c^9*d+10*a^9*b*c^{10})*x^2+a^{10}*c^{10}*x$$

maxima [B] time = 1.56, size = 1581, normalized size = 5.67

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^10*(d*x+c)^10,x, algorithm="maxima")

[Out] $1/21*b^{10}*d^{10}*x^{21} + a^{10}*c^{10}*x + 1/2*(b^{10}*c*d^9 + a*b^9*d^{10})*x^{20} + 5/19*(9*b^{10}*c^2*d^8 + 20*a*b^9*c*d^9 + 9*a^2*b^8*d^{10})*x^{19} + 5/3*(4*b^{10}*c^3*d^7 + 15*a*b^9*c^2*d^8 + 15*a^2*b^8*c*d^9 + 4*a^3*b^7*d^{10})*x^{18} + 15/17*(14*b^{10}*c^4*d^6 + 80*a*b^9*c^3*d^7 + 135*a^2*b^8*c^2*d^8 + 80*a^3*b^7*c*d^9 + 14*a^4*b^6*d^{10})*x^{17} + 3/4*(21*b^{10}*c^5*d^5 + 175*a*b^9*c^4*d^6 + 450*a^2*b^8*c^3*d^7 + 450*a^3*b^7*c^2*d^8 + 175*a^4*b^6*c*d^9 + 21*a^5*b^5*d^{10})*x^{16} + 2*(7*b^{10}*c^6*d^4 + 84*a*b^9*c^5*d^5 + 315*a^2*b^8*c^4*d^6 + 480*a^3*b^7*c^3*d^7 + 315*a^4*b^6*c^2*d^8 + 84*a^5*b^5*c*d^9 + 7*a^6*b^4*d^{10})*x^{15} + 30/7*(2*b^{10}*c^7*d^3 + 35*a*b^9*c^6*d^4 + 189*a^2*b^8*c^5*d^5 + 420*a^3*b^7*c^4*d^6 + 420*a^4*b^6*c^3*d^7 + 189*a^5*b^5*c^2*d^8 + 35*a^6*b^4*c*d^9 + 2*a^7*b^3*d^{10})*x^{14} + 15/13*(3*b^{10}*c^8*d^2 + 80*a*b^9*c^7*d^3 + 630*a^2*b^8*c^6*d^4 + 2016*a^3*b^7*c^5*d^5 + 2940*a^4*b^6*c^4*d^6 + 2016*a^5*b^5*c^3*d^7 + 630*a^6*b^4*c^2*d^8 + 80*a^7*b^3*c*d^9 + 3*a^8*b^2*d^{10})*x^{13} + 5/6*(b^{10}*c^9*d + 45*a*b^9*c^8*d^2 + 540*a^2*b^8*c^7*d^3 + 2520*a^3*b^7*c^6*d^4 + 5292*a^4*b^6*c^5*d^5 + 5292*a^5*b^5*c^4*d^6 + 2520*a^6*b^4*c^3*d^7 + 540*a^7*b^3*c^2*d^8 + 45*a^8*b^2*c*d^9 + a^9*b*d^{10})*x^{12} + 1/11*(b^{10}*c^{10} + 100*a*b^9*c^9*d + 2025*a^2*b^8*c^8*d^2 + 14400*a^3*b^7*c^7*d^3 + 44100*a^4*b^6*c^6*d^4 + 63504*a^5*b^5*c^5*d^5 + 44100*a^6*b^4*c^4*d^6 + 14400*a^7*b^3*c^3*d^7 + 2025*a^8*b^2*c^2*d^8 + 100*a^9*b*c*d^9 + a^{10}*d^{10})*x^{11} + (a*b^9*c^{10} + 45*a^2*b^8*c^9*d + 540*a^3*b^7*c^8*d^2 + 2520*a^4*b^6*c^7*d^3 + 5292*a^5*b^5*c^6*d^4 + 5292*a^6*b^4*c^5*d^5 + 2520*a^7*b^3*c^4*d^6 + 540*a^8*b^2*c^3*d^7 + 45*a^9*b*c^2*d^8 + a^{10}*c*d^9)*x^{10} + 5/3*(3*a^2*b^8*c^{10} + 80*a^3*b^7*c^9*d + 630*a^4*b^6*c^8*d^2 + 2016*a^5*b^5*c^7*d^3 + 2940*a^6*b^4*c^6*d^4 + 2016*a^7*b^3*c^5*d^5 + 630*a^8*b^2*c^4*d^6 + 80*a^9*b*c^3*d^7 + 3*a^{10}*c^2*d^8)*x^9 + 15/2*(2*a^3*b^7*c^{10} + 35*a^4*b^6*c^9*d + 189*a^$

$$5*b^5*c^8*d^2 + 420*a^6*b^4*c^7*d^3 + 420*a^7*b^3*c^6*d^4 + 189*a^8*b^2*c^5*d^5 + 35*a^9*b*c^4*d^6 + 2*a^{10}*c^3*d^7)*x^8 + 30/7*(7*a^4*b^6*c^{10} + 84*a^5*b^5*c^9*d + 315*a^6*b^4*c^8*d^2 + 480*a^7*b^3*c^7*d^3 + 315*a^8*b^2*c^6*d^4 + 84*a^9*b*c^5*d^5 + 7*a^{10}*c^4*d^6)*x^7 + 2*(21*a^5*b^5*c^{10} + 175*a^6*b^4*c^9*d + 450*a^7*b^3*c^8*d^2 + 450*a^8*b^2*c^7*d^3 + 175*a^9*b*c^6*d^4 + 21*a^{10}*c^5*d^5)*x^6 + 3*(14*a^6*b^4*c^{10} + 80*a^7*b^3*c^9*d + 135*a^8*b^2*c^8*d^2 + 80*a^9*b*c^7*d^3 + 14*a^{10}*c^6*d^4)*x^5 + 15/2*(4*a^7*b^3*c^{10} + 15*a^8*b^2*c^9*d + 15*a^9*b*c^8*d^2 + 4*a^{10}*c^7*d^3)*x^4 + 5/3*(9*a^8*b^2*c^{10} + 20*a^9*b*c^9*d + 9*a^{10}*c^8*d^2)*x^3 + 5*(a^9*b*c^{10} + a^{10}*c^9*d)*x^2$$

mupad [B] time = 0.69, size = 1549, normalized size = 5.55

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^{10}*(c + d*x)^{10}, x)$

[Out] $x^7*(30*a^4*b^6*c^{10} + 30*a^{10}*c^4*d^6 + 360*a^5*b^5*c^9*d + 360*a^9*b*c^5*d^5 + 1350*a^6*b^4*c^8*d^2 + (14400*a^7*b^3*c^7*d^3)/7 + 1350*a^8*b^2*c^6*d^4) + x^{15}*(14*a^6*b^4*d^{10} + 14*b^{10}*c^6*d^4 + 168*a*b^9*c^5*d^5 + 168*a^5*b^5*c*d^9 + 630*a^2*b^8*c^4*d^6 + 960*a^3*b^7*c^3*d^7 + 630*a^4*b^6*c^2*d^8) + x^5*(42*a^6*b^4*c^{10} + 42*a^{10}*c^6*d^4 + 240*a^7*b^3*c^9*d + 240*a^9*b*c^7*d^3 + 405*a^8*b^2*c^8*d^2) + x^{17}*((210*a^4*b^6*d^{10})/17 + (210*b^{10}*c^4*d^6)/17 + (1200*a*b^9*c^3*d^7)/17 + (1200*a^3*b^7*c*d^9)/17 + (2025*a^2*b^8*c^2*d^8)/17) + x^{11}*((a^{10}*d^{10})/11 + (b^{10}*c^{10})/11 + (2025*a^2*b^8*c^8*d^2)/11 + (14400*a^3*b^7*c^7*d^3)/11 + (44100*a^4*b^6*c^6*d^4)/11 + (63504*a^5*b^5*c^5*d^5)/11 + (44100*a^6*b^4*c^4*d^6)/11 + (14400*a^7*b^3*c^3*d^7)/11 + (2025*a^8*b^2*c^2*d^8)/11 + (100*a*b^9*c^9*d)/11 + (100*a^9*b*c*d^9)/11) + x^8*(15*a^3*b^7*c^{10} + 15*a^{10}*c^3*d^7 + (525*a^4*b^6*c^9*d)/2 + (525*a^9*b*c^4*d^6)/2 + (2835*a^5*b^5*c^8*d^2)/2 + 3150*a^6*b^4*c^7*d^3 + 3150*a^7*b^3*c^6*d^4 + (2835*a^8*b^2*c^5*d^5)/2) + x^{14}*((60*a^7*b^3*d^{10})/7 + (60*b^{10}*c^7*d^3)/7 + 150*a*b^9*c^6*d^4 + 150*a^6*b^4*c*d^9 + 810*a^2*b^8*c^5*d^5 + 1800*a^3*b^7*c^4*d^6 + 1800*a^4*b^6*c^3*d^7 + 810*a^5*b^5*c^2*d^8) + x^{10}*(a*b^9*c^{10} + a^{10}*c*d^9 + 45*a^2*b^8*c^9*d + 45*a^9*b*c^2*d^8 + 540*a^3*b^7*c^8*d^2 + 2520*a^4*b^6*c^7*d^3 + 5292*a^5*b^5*c^6*d^4 + 5292*a^6*b^4*c^5*d^5 + 2520*a^7*b^3*c^4*d^6 + 540*a^8*b^2*c^3*d^7) + x^{12}*((5*a^9*b*d^{10})/6 + (5*b^{10}*c^9*d)/6 + (75*a*b^9*c^8*d^2)/2 + (75*a^8*b^2*c*d^9)/2 + 450*a^2*b^8*c^7*d^3 + 2100*a^3*b^7*c^6*d^4 + 4410*a^4*b^6*c^5*d^5 + 4410*a^5*b^5*c^4*d^6 + 2100*a^6*b^4*c^3*d^7 + 450*a^7*b^3*c^2*d^8) + x^6*(42*a^5*b^5*c^{10} + 42*a^{10}*c^5*d^5 + 350*a^6*b^4*c^9*d + 350*a^9*b*c^6*d^4 + 900*a^7*b^3*c^8*d^2 + 900*a^8*b^2*c^7*d^3) + x^{16}*((63*a^5*b^5*d^{10})/4 + (63*b^{10}*c^5*d^5)/4 + (525*a*b^9*c^4*d^6)/4 + (525*a^4*b^6*c*d^9)/4 + (675*a^2*b^8*c^3*d^7)/2 + (675*a^3*b^7*c^2*d^8)/2) + x^9*(5*a^2*b^8*c^{10} + 5*a^{10}*c^2*d^8 + (400*a^3*b^7*c^9*d)/3 + (400*a^9*b*c^3*d^7)/3 + 1050*a^4*b^6*c^8*d^2 + 3$

$$\begin{aligned}
& 360*a^5*b^5*c^7*d^3 + 4900*a^6*b^4*c^6*d^4 + 3360*a^7*b^3*c^5*d^5 + 1050*a^8*b^2*c^4*d^6) + x^{13}*((45*a^8*b^2*d^{10})/13 + (45*b^{10}*c^8*d^2)/13 + (1200*a*b^9*c^7*d^3)/13 + (1200*a^7*b^3*c*d^9)/13 + (9450*a^2*b^8*c^6*d^4)/13 + (30240*a^3*b^7*c^5*d^5)/13 + (44100*a^4*b^6*c^4*d^6)/13 + (30240*a^5*b^5*c^3*d^7)/13 + (9450*a^6*b^4*c^2*d^8)/13) + a^{10}*c^{10}*x + (b^{10}*d^{10}*x^{21})/21 + (15*a^7*c^7*x^4*(4*a^3*d^3 + 4*b^3*c^3 + 15*a*b^2*c^2*d + 15*a^2*b*c*d^2))/2 + (5*b^7*d^7*x^{18}*(4*a^3*d^3 + 4*b^3*c^3 + 15*a*b^2*c^2*d + 15*a^2*b*c*d^2))/3 + 5*a^9*c^9*x^2*(a*d + b*c) + (b^9*d^9*x^{20}*(a*d + b*c))/2 + (5*a^8*c^8*x^3*(9*a^2*d^2 + 9*b^2*c^2 + 20*a*b*c*d))/3 + (5*b^8*d^8*x^{19}*(9*a^2*d^2 + 9*b^2*c^2 + 20*a*b*c*d))/19
\end{aligned}$$

sympy [B] time = 0.31, size = 1775, normalized size = 6.36

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**10*(d*x+c)**10,x)

[Out] a**10*c**10*x + b**10*d**10*x**21/21 + x**20*(a*b**9*d**10/2 + b**10*c*d**9/2) + x**19*(45*a**2*b**8*d**10/19 + 100*a*b**9*c*d**9/19 + 45*b**10*c**2*d**8/19) + x**18*(20*a**3*b**7*d**10/3 + 25*a**2*b**8*c*d**9 + 25*a*b**9*c**2*d**8 + 20*b**10*c**3*d**7/3) + x**17*(210*a**4*b**6*d**10/17 + 1200*a**3*b**7*c*d**9/17 + 2025*a**2*b**8*c**2*d**8/17 + 1200*a*b**9*c**3*d**7/17 + 210*b**10*c**4*d**6/17) + x**16*(63*a**5*b**5*d**10/4 + 525*a**4*b**6*c*d**9/4 + 675*a**3*b**7*c**2*d**8/2 + 675*a**2*b**8*c**3*d**7/2 + 525*a*b**9*c**4*d**6/4 + 63*b**10*c**5*d**5/4) + x**15*(14*a**6*b**4*d**10 + 168*a**5*b**5*c*d**9 + 630*a**4*b**6*c**2*d**8 + 960*a**3*b**7*c**3*d**7 + 630*a**2*b**8*c**4*d**6 + 168*a*b**9*c**5*d**5 + 14*b**10*c**6*d**4) + x**14*(60*a**7*b**3*d**10/7 + 150*a**6*b**4*c*d**9 + 810*a**5*b**5*c**2*d**8 + 1800*a**4*b**6*c**3*d**7 + 1800*a**3*b**7*c**4*d**6 + 810*a**2*b**8*c**5*d**5 + 150*a*b**9*c**6*d**4 + 60*b**10*c**7*d**3/7) + x**13*(45*a**8*b**2*d**10/13 + 1200*a**7*b**3*c*d**9/13 + 9450*a**6*b**4*c**2*d**8/13 + 30240*a**5*b**5*c**3*d**7/13 + 44100*a**4*b**6*c**4*d**6/13 + 30240*a**3*b**7*c**5*d**5/13 + 9450*a**2*b**8*c**6*d**4/13 + 1200*a*b**9*c**7*d**3/13 + 45*b**10*c**8*d**2/13) + x**12*(5*a**9*b*d**10/6 + 75*a**8*b**2*c*d**9/2 + 450*a**7*b**3*c**2*d**8 + 2100*a**6*b**4*c**3*d**7 + 4410*a**5*b**5*c**4*d**6 + 4410*a**4*b**6*c**5*d**5 + 2100*a**3*b**7*c**6*d**4 + 450*a**2*b**8*c**7*d**3 + 75*a*b**9*c**8*d**2/2 + 5*b**10*c**9*d/6) + x**11*(a**10*d**10/11 + 100*a**9*b*c*d**9/11 + 2025*a**8*b**2*c**2*d**8/11 + 14400*a**7*b**3*c**3*d**7/11 + 44100*a**6*b**4*c**4*d**6/11 + 63504*a**5*b**5*c**5*d**5/11 + 44100*a**4*b**6*c**6*d**4/11 + 14400*a**3*b**7*c**7*d**3/11 + 2025*a**2*b**8*c**8*d**2/11 + 100*a*b**9*c**9*d/11 + b**10*c**10/11) + x**10*(a**10*c*d**9 + 45*a**9*b*c**2*d**8 + 540*a**8*b**2*c**3*d**7 + 2520*a**7*b**3*c**4*d**6 + 5292*a**6*b**4*c**5*d**5 + 5292*a**5*b**5*c**6*d**4 + 2520*a**4*b**6*c**7*d**3 + 540*a**3*b**7*c**8*d**2 + 45*a**2*b**8*c**9*d + a*b**9*c**10) + x**9*(5*a**10*c**2*d**8

$$\begin{aligned}
& + 400*a**9*b*c**3*d**7/3 + 1050*a**8*b**2*c**4*d**6 + 3360*a**7*b**3*c**5*d**5 \\
& + 4900*a**6*b**4*c**6*d**4 + 3360*a**5*b**5*c**7*d**3 + 1050*a**4*b**6*c**8*d**2 \\
& + 400*a**3*b**7*c**9*d/3 + 5*a**2*b**8*c**10) + x**8*(15*a**10*c**3*d**7 \\
& + 525*a**9*b*c**4*d**6/2 + 2835*a**8*b**2*c**5*d**5/2 + 3150*a**7*b**3*c**6*d**4 \\
& + 3150*a**6*b**4*c**7*d**3 + 2835*a**5*b**5*c**8*d**2/2 + 525*a**4*b**6*c**9*d/2 \\
& + 15*a**3*b**7*c**10) + x**7*(30*a**10*c**4*d**6 + 360*a**9*b*c**5*d**5 \\
& + 1350*a**8*b**2*c**6*d**4 + 14400*a**7*b**3*c**7*d**3/7 + 1350*a**6*b**4*c**8*d**2 \\
& + 360*a**5*b**5*c**9*d + 30*a**4*b**6*c**10) + x**6*(42*a**10*c**5*d**5 \\
& + 350*a**9*b*c**6*d**4 + 900*a**8*b**2*c**7*d**3 + 900*a**7*b**3*c**8*d**2 \\
& + 350*a**6*b**4*c**9*d + 42*a**5*b**5*c**10) + x**5*(42*a**10*c**6*d**4 \\
& + 240*a**9*b*c**7*d**3 + 405*a**8*b**2*c**8*d**2 + 240*a**7*b**3*c**9*d \\
& + 42*a**6*b**4*c**10) + x**4*(30*a**10*c**7*d**3 + 225*a**9*b*c**8*d**2/2 \\
& + 225*a**8*b**2*c**9*d/2 + 30*a**7*b**3*c**10) + x**3*(15*a**10*c**8*d**2 \\
& + 100*a**9*b*c**9*d/3 + 15*a**8*b**2*c**10) + x**2*(5*a**10*c**9*d \\
& + 5*a**9*b*c**10)
\end{aligned}$$

3.1302 $\int (a + bx)^9 (c + dx)^{10} dx$

Optimal. Leaf size=250

$$-\frac{9b^8(c+dx)^{19}(bc-ad)}{19d^{10}} + \frac{2b^7(c+dx)^{18}(bc-ad)^2}{d^{10}} - \frac{84b^6(c+dx)^{17}(bc-ad)^3}{17d^{10}} + \frac{63b^5(c+dx)^{16}(bc-ad)^4}{8d^{10}} - \frac{42b^4(c+dx)^{15}(bc-ad)^5}{5d^{10}} + \frac{3b^3(c+dx)^{14}(bc-ad)^6}{3d^{10}} - \frac{2b^2(c+dx)^{13}(bc-ad)^7}{2d^{10}} + \frac{b(c+dx)^{12}(bc-ad)^8}{d^{10}} - \frac{c(c+dx)^{11}(bc-ad)^9}{11d^{10}}$$

[Out] $-1/11*(-a*d+b*c)^9*(d*x+c)^{11}/d^{10}+3/4*b*(-a*d+b*c)^8*(d*x+c)^{12}/d^{10}-36/13*b^2*(-a*d+b*c)^7*(d*x+c)^{13}/d^{10}+6*b^3*(-a*d+b*c)^6*(d*x+c)^{14}/d^{10}-42/5*b^4*(-a*d+b*c)^5*(d*x+c)^{15}/d^{10}+63/8*b^5*(-a*d+b*c)^4*(d*x+c)^{16}/d^{10}-84/17*b^6*(-a*d+b*c)^3*(d*x+c)^{17}/d^{10}+2*b^7*(-a*d+b*c)^2*(d*x+c)^{18}/d^{10}-9/19*b^8*(-a*d+b*c)*(d*x+c)^{19}/d^{10}+1/20*b^9*(d*x+c)^{20}/d^{10}$

Rubi [A] time = 1.04, antiderivative size = 250, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{9b^8(c+dx)^{19}(bc-ad)}{19d^{10}} + \frac{2b^7(c+dx)^{18}(bc-ad)^2}{d^{10}} - \frac{84b^6(c+dx)^{17}(bc-ad)^3}{17d^{10}} + \frac{63b^5(c+dx)^{16}(bc-ad)^4}{8d^{10}} - \frac{42b^4(c+dx)^{15}(bc-ad)^5}{5d^{10}} + \frac{3b^3(c+dx)^{14}(bc-ad)^6}{3d^{10}} - \frac{2b^2(c+dx)^{13}(bc-ad)^7}{2d^{10}} + \frac{b(c+dx)^{12}(bc-ad)^8}{d^{10}} - \frac{c(c+dx)^{11}(bc-ad)^9}{11d^{10}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^9*(c + d*x)^10, x]

[Out] $-((b*c - a*d)^9*(c + d*x)^{11})/(11*d^{10}) + (3*b*(b*c - a*d)^8*(c + d*x)^{12})/(4*d^{10}) - (36*b^2*(b*c - a*d)^7*(c + d*x)^{13})/(13*d^{10}) + (6*b^3*(b*c - a*d)^6*(c + d*x)^{14})/d^{10} - (42*b^4*(b*c - a*d)^5*(c + d*x)^{15})/(5*d^{10}) + (63*b^5*(b*c - a*d)^4*(c + d*x)^{16})/(8*d^{10}) - (84*b^6*(b*c - a*d)^3*(c + d*x)^{17})/(17*d^{10}) + (2*b^7*(b*c - a*d)^2*(c + d*x)^{18})/d^{10} - (9*b^8*(b*c - a*d)*(c + d*x)^{19})/(19*d^{10}) + (b^9*(c + d*x)^{20})/(20*d^{10})$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^9 (c + dx)^{10} dx &= \int \left(\frac{(-bc + ad)^9 (c + dx)^{10}}{d^9} + \frac{9b(bc - ad)^8 (c + dx)^{11}}{d^9} - \frac{36b^2(bc - ad)^7 (c + dx)^{12}}{d^9} + \frac{84b^3(bc - ad)^6 (c + dx)^{13}}{d^9} - \frac{42b^4(bc - ad)^5 (c + dx)^{14}}{d^9} + \frac{63b^5(bc - ad)^4 (c + dx)^{15}}{d^9} - \frac{84b^6(bc - ad)^3 (c + dx)^{16}}{d^9} + \frac{9b^7(bc - ad)^2 (c + dx)^{17}}{d^9} - \frac{9b^8(bc - ad) (c + dx)^{18}}{d^9} + \frac{b^9 (c + dx)^{19}}{d^9} \right) dx \\ &= -\frac{(bc - ad)^9 (c + dx)^{11}}{11d^{10}} + \frac{3b(bc - ad)^8 (c + dx)^{12}}{4d^{10}} - \frac{36b^2(bc - ad)^7 (c + dx)^{13}}{13d^{10}} + \frac{6b^3(bc - ad)^6 (c + dx)^{14}}{5d^{10}} - \frac{42b^4(bc - ad)^5 (c + dx)^{15}}{5d^{10}} + \frac{63b^5(bc - ad)^4 (c + dx)^{16}}{8d^{10}} - \frac{84b^6(bc - ad)^3 (c + dx)^{17}}{17d^{10}} + \frac{2b^7(bc - ad)^2 (c + dx)^{18}}{d^{10}} - \frac{9b^8(bc - ad) (c + dx)^{19}}{19d^{10}} + \frac{b^9 (c + dx)^{20}}{20d^{10}} \end{aligned}$$

Mathematica [B] time = 0.19, size = 1397, normalized size = 5.59

$$\frac{1}{20}b^9d^{10}x^{20} + \frac{1}{19}b^8d^9(10bc+9ad)x^{19} + \frac{1}{2}b^7d^8(5b^2c^2 + 10abdc + 4a^2d^2)x^{18} + \frac{3}{17}b^6d^7(40b^3c^3 + 135ab^2dc^2 + 120a^2$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^9*(c + d*x)^10,x]

[Out] $a^9c^{10}x + (a^8c^9(9*b*c + 10*a*d)*x^2)/2 + 3*a^7*c^8*(4*b^2*c^2 + 10*a*b*c*d + 5*a^2*d^2)*x^3 + (3*a^6*c^7*(28*b^3*c^3 + 120*a*b^2*c^2*d + 135*a^2*b*c*d^2 + 40*a^3*d^3)*x^4)/4 + (6*a^5*c^6*(21*b^4*c^4 + 140*a*b^3*c^3*d + 270*a^2*b^2*c^2*d^2 + 180*a^3*b*c*d^3 + 35*a^4*d^4)*x^5)/5 + 3*a^4*c^5*(7*b^5*c^5 + 70*a*b^4*c^4*d + 210*a^2*b^3*c^3*d^2 + 240*a^3*b^2*c^2*d^3 + 105*a^4*b*c*d^4 + 14*a^5*d^5)*x^6 + 6*a^3*c^4*(2*b^6*c^6 + 30*a*b^5*c^5*d + 135*a^2*b^4*c^4*d^2 + 240*a^3*b^3*c^3*d^3 + 180*a^4*b^2*c^2*d^4 + 54*a^5*b*c*d^5 + 5*a^6*d^6)*x^7 + (3*a^2*c^3*(6*b^7*c^7 + 140*a*b^6*c^6*d + 945*a^2*b^5*c^5*d^2 + 2520*a^3*b^4*c^4*d^3 + 2940*a^4*b^3*c^3*d^4 + 1512*a^5*b^2*c^2*d^5 + 315*a^6*b*c*d^6 + 20*a^7*d^7)*x^8)/4 + a*c^2*(b^8*c^8 + 40*a*b^7*c^7*d + 420*a^2*b^6*c^6*d^2 + 1680*a^3*b^5*c^5*d^3 + 2940*a^4*b^4*c^4*d^4 + 2352*a^5*b^3*c^3*d^5 + 840*a^6*b^2*c^2*d^6 + 120*a^7*b*c*d^7 + 5*a^8*d^8)*x^9 + (c*(b^9*c^9 + 90*a*b^8*c^8*d + 1620*a^2*b^7*c^7*d^2 + 10080*a^3*b^6*c^6*d^3 + 26460*a^4*b^5*c^5*d^4 + 31752*a^5*b^4*c^4*d^5 + 17640*a^6*b^3*c^3*d^6 + 4320*a^7*b^2*c^2*d^7 + 405*a^8*b*c*d^8 + 10*a^9*d^9)*x^10)/10 + (d*(10*b^9*c^9 + 405*a*b^8*c^8*d + 4320*a^2*b^7*c^7*d^2 + 17640*a^3*b^6*c^6*d^3 + 31752*a^4*b^5*c^5*d^4 + 26460*a^5*b^4*c^4*d^5 + 10080*a^6*b^3*c^3*d^6 + 1620*a^7*b^2*c^2*d^7 + 90*a^8*b*c*d^8 + a^9*d^9)*x^11)/11 + (3*b*d^2*(5*b^8*c^8 + 120*a*b^7*c^7*d + 840*a^2*b^6*c^6*d^2 + 2352*a^3*b^5*c^5*d^3 + 2940*a^4*b^4*c^4*d^4 + 1680*a^5*b^3*c^3*d^5 + 420*a^6*b^2*c^2*d^6 + 40*a^7*b*c*d^7 + a^8*d^8)*x^12)/4 + (6*b^2*d^3*(20*b^7*c^7 + 315*a*b^6*c^6*d + 1512*a^2*b^5*c^5*d^2 + 2940*a^3*b^4*c^4*d^3 + 2520*a^4*b^3*c^3*d^4 + 945*a^5*b^2*c^2*d^5 + 140*a^6*b*c*d^6 + 6*a^7*d^7)*x^13)/13 + 3*b^3*d^4*(5*b^6*c^6 + 54*a*b^5*c^5*d + 180*a^2*b^4*c^4*d^2 + 240*a^3*b^3*c^3*d^3 + 135*a^4*b^2*c^2*d^4 + 30*a^5*b*c*d^5 + 2*a^6*d^6)*x^14 + (6*b^4*d^5*(14*b^5*c^5 + 105*a*b^4*c^4*d + 240*a^2*b^3*c^3*d^2 + 210*a^3*b^2*c^2*d^3 + 70*a^4*b*c*d^4 + 7*a^5*d^5)*x^15)/5 + (3*b^5*d^6*(35*b^4*c^4 + 180*a*b^3*c^3*d + 270*a^2*b^2*c^2*d^2 + 140*a^3*b*c*d^3 + 21*a^4*d^4)*x^16)/8 + (3*b^6*d^7*(40*b^3*c^3 + 135*a*b^2*c^2*d + 120*a^2*b*c*d^2 + 28*a^3*d^3)*x^17)/17 + (b^7*d^8*(5*b^2*c^2 + 10*a*b*c*d + 4*a^2*d^2)*x^18)/2 + (b^8*d^9*(10*b*c + 9*a*d)*x^19)/19 + (b^9*d^10*x^20)/20$

fricas [B] time = 0.39, size = 1656, normalized size = 6.62

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^9*(d*x+c)^10,x, algorithm="fricas")

[Out] $\frac{1}{20}x^{20}d^{10}b^9 + \frac{10}{19}x^{19}d^9c*b^9 + \frac{9}{19}x^{19}d^{10}b^8a + \frac{5}{2}x^{18}d^8c^2*b^9 + 5x^{18}d^9c*b^8a + 2x^{18}d^{10}b^7a^2 + \frac{120}{17}x^{17}d^7c^3*b^9 + \frac{405}{17}x^{17}d^8c^2*b^8a + \frac{360}{17}x^{17}d^9c*b^7a^2 + \frac{84}{17}x^{17}d^{10}b^6a^3 + \frac{105}{8}x^{16}d^6c^4*b^9 + \frac{135}{2}x^{16}d^7c^3*b^8a + \frac{405}{4}x^{16}d^8c^2*b^7a^2 + \frac{105}{2}x^{16}d^9c*b^6a^3 + \frac{63}{8}x^{16}d^{10}b^5a^4 + \frac{8}{4}x^{15}d^5c^5*b^9 + 126x^{15}d^6c^4*b^8a + 288x^{15}d^7c^3*b^7a^2 + 252x^{15}d^8c^2*b^6a^3 + 84x^{15}d^9c*b^5a^4 + \frac{42}{5}x^{15}d^{10}b^4a^5 + 15x^{14}d^4c^6*b^9 + 162x^{14}d^5c^5*b^8a + 540x^{14}d^6c^4*b^7a^2 + 720x^{14}d^7c^3*b^6a^3 + 405x^{14}d^8c^2*b^5a^4 + 90x^{14}d^9c*b^4a^5 + 6x^{14}d^{10}b^3a^6 + \frac{120}{13}x^{13}d^3c^7*b^9 + \frac{1890}{13}x^{13}d^4c^6*b^8a + \frac{9072}{13}x^{13}d^5c^5*b^7a^2 + \frac{17640}{13}x^{13}d^6c^4*b^6a^3 + \frac{15120}{13}x^{13}d^7c^3*b^5a^4 + \frac{5670}{13}x^{13}d^8c^2*b^4a^5 + \frac{840}{13}x^{13}d^9c*b^3a^6 + \frac{36}{13}x^{13}d^{10}b^2a^7 + \frac{15}{4}x^{12}d^2c^8*b^9 + 90x^{12}d^3c^7*b^8a + 630x^{12}d^4c^6*b^7a^2 + 1764x^{12}d^5c^5*b^6a^3 + 2205x^{12}d^6c^4*b^5a^4 + 1260x^{12}d^7c^3*b^4a^5 + 315x^{12}d^8c^2*b^3a^6 + 30x^{12}d^9c*b^2a^7 + \frac{3}{4}x^{12}d^{10}b^1a^8 + \frac{10}{11}x^{11}d^1c^9*b^9 + \frac{405}{11}x^{11}d^2c^8*b^8a + \frac{4320}{11}x^{11}d^3c^7*b^7a^2 + \frac{17640}{11}x^{11}d^4c^6*b^6a^3 + \frac{31752}{11}x^{11}d^5c^5*b^5a^4 + \frac{26460}{11}x^{11}d^6c^4*b^4a^5 + \frac{10080}{11}x^{11}d^7c^3*b^3a^6 + \frac{1620}{11}x^{11}d^8c^2*b^2a^7 + \frac{90}{11}x^{11}d^9c*b^1a^8 + \frac{1}{11}x^{11}d^{10}a^9 + \frac{1}{10}x^{10}d^1c^10*b^9 + 9x^{10}d^2c^9*b^8a + 162x^{10}d^3c^8*b^7a^2 + 1008x^{10}d^4c^7*b^6a^3 + 2646x^{10}d^5c^6*b^5a^4 + 15876/5x^{10}d^6c^5*b^4a^5 + 1764x^{10}d^7c^4*b^3a^6 + 432x^{10}d^8c^3*b^2a^7 + \frac{81}{2}x^{10}d^9c^2*b^1a^8 + x^{10}d^{10}c^1a^9 + x^9d^1c^10*b^8a + 40x^9d^2c^9*b^7a^2 + 420x^9d^3c^8*b^6a^3 + 1680x^9d^4c^7*b^5a^4 + 2940x^9d^5c^6*b^4a^5 + 2352x^9d^6c^5*b^3a^6 + 840x^9d^7c^4*b^2a^7 + 120x^9d^8c^3*b^1a^8 + 5x^9d^9c^2*a^9 + \frac{9}{2}x^8d^1c^10*b^7a^2 + 105x^8d^2c^9*b^6a^3 + \frac{2835}{4}x^8d^3c^8*b^5a^4 + 1890x^8d^4c^7*b^4a^5 + 2205x^8d^5c^6*b^3a^6 + 1134x^8d^6c^5*b^2a^7 + \frac{945}{4}x^8d^7c^4*b^1a^8 + 15x^8d^8c^3*a^9 + 12x^7d^1c^10*b^6a^3 + 180x^7d^2c^9*b^5a^4 + 810x^7d^3c^8*b^4a^5 + 1440x^7d^4c^7*b^3a^6 + 1080x^7d^5c^6*b^2a^7 + 324x^7d^6c^5*b^1a^8 + 30x^7d^7c^4*a^9 + 21x^6d^1c^10*b^5a^4 + 210x^6d^2c^9*b^4a^5 + 630x^6d^3c^8*b^3a^6 + 720x^6d^4c^7*b^2a^7 + 315x^6d^5c^6*b^1a^8 + 42x^6d^6c^5*a^9 + \frac{126}{5}x^5d^1c^10*b^4a^5 + 168x^5d^2c^9*b^3a^6 + 324x^5d^3c^8*b^2a^7 + 216x^5d^4c^7*b^1a^8 + 42x^5d^5c^6*a^9 + 21x^4d^1c^10*b^3a^6 + 90x^4d^2c^9*b^2a^7 + \frac{405}{4}x^4d^3c^8*b^1a^8 + 30x^4d^4c^7*a^9 + 12x^3d^1c^10*b^2a^7 + 30x^3d^2c^9*b^1a^8 + 15x^3d^3c^8*a^9 + \frac{9}{2}x^2d^1c^10*b^1a^8 + 5x^2d^2c^9*a^9 + xc^{10}a^9$

giac [B] time = 1.30, size = 1656, normalized size = 6.62

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^9*(d*x+c)^10,x, algorithm="giac")

[Out] $\frac{1}{20}b^9d^{10}x^{20} + \frac{10}{19}b^9c^9d^9x^{19} + \frac{9}{19}ab^8d^{10}x^{19} + \frac{5}{2}b^9c^2d^8x^{18} + 5ab^8c^2d^9x^{18} + 2a^2b^7d^{10}x^{18} + \frac{120}{17}b^9c^3d^7x^{17} + \frac{405}{17}ab^8c^2d^8x^{17} + \frac{360}{17}a^2b^7c^2d^9x^{17} + \frac{84}{17}a^3b^6d^{10}x^{17} + \frac{105}{8}b^9c^4d^6x^{16} + \frac{135}{2}ab^8c^3d^7x^{16} + \frac{405}{4}a^2b^7c^2d^8x^{16} + \frac{105}{2}a^3b^6c^2d^9x^{16} + \frac{63}{8}a^4b^5d^{10}x^{16} + \frac{8}{4}b^9c^5d^5x^{15} + 126ab^8c^4d^6x^{15} + 288a^2b^7c^3d^7x^{15} + 252a^3b^6c^2d^8x^{15} + 84a^4b^5c^2d^9x^{15} + \frac{42}{5}a^5b^4d^{10}x^{15} + 15b^9c^6d^4x^{14} + 162ab^8c^5d^5x^{14} + 540a^2b^7c^4d^6x^{14} + 720a^3b^6c^3d^7x^{14} + 405a^4b^5c^2d^8x^{14} + 90a^5b^4c^2d^9x^{14} + 6a^6b^3d^{10}x^{14} + \frac{120}{13}b^9c^7d^3x^{13} + \frac{1890}{13}ab^8c^6d^4x^{13} + \frac{9072}{13}a^2b^7c^5d^5x^{13} + \frac{17640}{13}a^3b^6c^4d^6x^{13} + \frac{15120}{13}a^4b^5c^3d^7x^{13} + \frac{5670}{13}a^5b^4c^2d^8x^{13} + \frac{840}{13}a^6b^3c^2d^9x^{13} + \frac{36}{13}a^7b^2d^{10}x^{13} + \frac{15}{4}b^9c^8d^2x^{12} + 90ab^8c^7d^3x^{12} + 630a^2b^7c^6d^4x^{12} + 1764a^3b^6c^5d^5x^{12} + 2205a^4b^5c^4d^6x^{12} + 1260a^5b^4c^3d^7x^{12} + 315a^6b^3c^2d^8x^{12} + 30a^7b^2c^2d^9x^{12} + \frac{3}{4}a^8b^2d^{10}x^{12} + \frac{10}{11}b^9c^9d^1x^{11} + \frac{405}{11}ab^8c^8d^2x^{11} + \frac{4320}{11}a^2b^7c^7d^3x^{11} + \frac{17640}{11}a^3b^6c^6d^4x^{11} + \frac{31752}{11}a^4b^5c^5d^5x^{11} + \frac{26460}{11}a^5b^4c^4d^6x^{11} + \frac{10080}{11}a^6b^3c^3d^7x^{11} + \frac{1620}{11}a^7b^2c^2d^8x^{11} + \frac{90}{11}a^8b^2c^2d^9x^{11} + \frac{1}{11}a^9d^{10}x^{11} + \frac{1}{10}b^9c^{10}x^{10} + 9ab^8c^9d^1x^{10} + 162a^2b^7c^8d^2x^{10} + 1008a^3b^6c^7d^3x^{10} + 2646a^4b^5c^6d^4x^{10} + 15876/5a^5b^4c^5d^5x^{10} + 1764a^6b^3c^4d^6x^{10} + 432a^7b^2c^3d^7x^{10} + 81/2a^8b^2c^2d^8x^{10} + a^9c^9d^1x^{10} + ab^8c^{10}x^9 + 40a^2b^7c^9d^1x^9 + 420a^3b^6c^8d^2x^9 + 1680a^4b^5c^7d^3x^9 + 2940a^5b^4c^6d^4x^9 + 2352a^6b^3c^5d^5x^9 + 840a^7b^2c^4d^6x^9 + 120a^8b^2c^3d^7x^9 + 5a^9c^2d^8x^9 + 9/2a^2b^7c^{10}x^8 + 105a^3b^6c^9d^1x^8 + 2835/4a^4b^5c^8d^2x^8 + 1890a^5b^4c^7d^3x^8 + 2205a^6b^3c^6d^4x^8 + 1134a^7b^2c^5d^5x^8 + 945/4a^8b^2c^4d^6x^8 + 15a^9c^3d^7x^8 + 12a^3b^6c^{10}x^7 + 180a^4b^5c^9d^1x^7 + 810a^5b^4c^8d^2x^7 + 1440a^6b^3c^7d^3x^7 + 1080a^7b^2c^6d^4x^7 + 324a^8b^2c^5d^5x^7 + 30a^9c^4d^6x^7 + 21a^4b^5c^{10}x^6 + 210a^5b^4c^9d^1x^6 + 630a^6b^3c^8d^2x^6 + 720a^7b^2c^7d^3x^6 + 315a^8b^2c^6d^4x^6 + 42a^9c^5d^5x^6 + 126/5a^5b^4c^{10}x^5 + 168a^6b^3c^9d^1x^5 + 324a^7b^2c^8d^2x^5 + 216a^8b^2c^7d^3x^5 + 42a^9c^6d^4x^5 + 21a^6b^3c^{10}x^4 + 90a^7b^2c^9d^1x^4 + 405/4a^8b^2c^8d^2x^4 + 30a^9c^7d^3x^4 + 12a^7b^2c^{10}x^3 + 30a^8b^2c^9d^1x^3 + 15a^9c^8d^2x^3 + 9/2a^8b^2c^{10}x^2 + 5a^9c^9d^1x^2 + a^9c^{10}x$

maple [B] time = 0.00, size = 1441, normalized size = 5.76

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^9*(d*x+c)^10,x)

[Out] $\frac{1}{20}b^9d^{10}x^{20} + \frac{1}{19}(9ab^8d^{10} + 10b^9c^9d^9)x^{19} + \frac{1}{18}(36a^2b^7d^{10} + 90ab^8c^9d^9 + 45b^9c^2d^8)x^{18} + \frac{1}{17}(84a^3b^6d^{10} + 360a^2b^7c^9d^9 + 405ab^8c^2d^8 + 120b^9c^3d^7)x^{17} + \frac{1}{16}(126a^4b^5d^{10} + 840a^3b^6c^9d^9 + 1620a^2b^7c^2d^8 + 1080ab^8c^3d^7 + 210b^9c^4d^6)x^{16} + \frac{1}{15}(126a^5b^4d^{10} + 1260a^4b^5c^9d^9 + 3780a^3b^6c^2d^8 + 4320a^2b^7c^3d^7 + 1890ab^8c^4d^6 + 252b^9c^5d^5)x^{15} + \frac{1}{14}(84a^6b^3d^{10} + 1260a^5b^4c^9d^9 + 5670a^4b^5c^2d^8 + 10080a^3b^6c^3d^7 + 7560a^2b^7c^4d^6 + 2268ab^8c^5d^5 + 210b^9c^6d^4)x^{14} + \frac{1}{13}(36a^7b^2d^{10} + 840a^6b^3c^9d^9 + 5670a^5b^4c^2d^8 + 15120a^4b^5c^3d^7 + 17640a^3b^6c^4d^6 + 9072a^2b^7c^5d^5 + 1890ab^8c^6d^4 + 120b^9c^7d^3)x^{13} + \frac{1}{12}(9a^8b^1d^{10} + 360a^7b^2c^9d^9 + 3780a^6b^3c^2d^8 + 15120a^5b^4c^3d^7 + 26460a^4b^5c^4d^6 + 21168a^3b^6c^5d^5 + 7560a^2b^7c^6d^4 + 1080ab^8c^7d^3 + 45b^9c^8d^2)x^{12} + \frac{1}{11}(a^9d^{10} + 90a^8b^1c^9d^9 + 1620a^7b^2c^2d^8 + 10080a^6b^3c^3d^7 + 26460a^5b^4c^4d^6 + 31752a^4b^5c^5d^5 + 17640a^3b^6c^6d^4 + 4320a^2b^7c^7d^3 + 405ab^8c^8d^2 + 10b^9c^9d^1)x^{11} + \frac{1}{10}(10a^9c^1d^9 + 405a^8b^1c^2d^8 + 4320a^7b^2c^3d^7 + 17640a^6b^3c^4d^6 + 31752a^5b^4c^5d^5 + 26460a^4b^5c^6d^4 + 10080a^3b^6c^7d^3 + 1620a^2b^7c^8d^2 + 90ab^8c^9d^1 + b^9c^{10})x^{10} + \frac{1}{9}(45a^9c^2d^8 + 1080a^8b^1c^3d^7 + 7560a^7b^2c^4d^6 + 21168a^6b^3c^5d^5 + 26460a^5b^4c^6d^4 + 15120a^4b^5c^7d^3 + 3780a^3b^6c^8d^2 + 360a^2b^7c^9d^1 + 9ab^8c^{10})x^9 + \frac{1}{8}(120a^9c^3d^7 + 1890a^8b^1c^4d^6 + 9072a^7b^2c^5d^5 + 17640a^6b^3c^6d^4 + 15120a^5b^4c^7d^3 + 5670a^4b^5c^8d^2 + 840a^3b^6c^9d^1 + 36a^2b^7c^{10})x^8 + \frac{1}{7}(210a^9c^4d^6 + 2268a^8b^1c^5d^5 + 7560a^7b^2c^6d^4 + 10080a^6b^3c^7d^3 + 5670a^5b^4c^8d^2 + 1260a^4b^5c^9d^1 + 84a^3b^6c^{10})x^7 + \frac{1}{6}(252a^9c^5d^5 + 1890a^8b^1c^6d^4 + 4320a^7b^2c^7d^3 + 3780a^6b^3c^8d^2 + 1260a^5b^4c^9d^1 + 126a^4b^5c^{10})x^6 + \frac{1}{5}(210a^9c^6d^4 + 1080a^8b^1c^7d^3 + 1620a^7b^2c^8d^2 + 840a^6b^3c^9d^1 + 126a^5b^4c^{10})x^5 + \frac{1}{4}(120a^9c^7d^3 + 405a^8b^1c^8d^2 + 360a^7b^2c^9d^1 + 84a^6b^3c^{10})x^4 + \frac{1}{3}(45a^9c^8d^2 + 90a^8b^1c^9d^1 + 36a^7b^2c^{10})x^3 + \frac{1}{2}(10a^9c^9d^1 + 9a^8b^1c^{10})x^2 + a^9c^{10}x$

maxima [B] time = 1.51, size = 1437, normalized size = 5.75

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^9*(d*x+c)^10,x, algorithm="maxima")

[Out] $\frac{1}{20}b^9d^{10}x^{20} + a^9c^{10}x + \frac{1}{19}(10b^9c^9d^9 + 9ab^8d^{10})x^{19} + \frac{1}{2}(5b^9c^2d^8 + 10ab^8c^9d^9 + 4a^2b^7d^{10})x^{18} + \frac{3}{17}(40b^9c^3d^7 + 135ab^8c^2d^8 + 120a^2b^7c^9d^9 + 28a^3b^6d^{10})x^{17} + \frac{3}{8}(35b^9c^4d^6 + 180ab^8c^3d^7 + 270a^2b^7c^2d^8 + 140a^3b^6c^9d^9 + 21a^4b^5d^{10})x^{16} + \frac{6}{5}(14b^9c^5d^5 + 105ab^8c^4d^6 + 2$

$$\begin{aligned}
& 40a^2b^7c^3d^7 + 210a^3b^6c^2d^8 + 70a^4b^5c^1d^9 + 7a^5b^4d^{10} \\
& 0)x^{15} + 3(5b^9c^6d^4 + 54a^2b^8c^5d^5 + 180a^2b^7c^4d^6 + 240a^3b^6c^3d^7 + 135a^4b^5c^2d^8 + 30a^5b^4c^1d^9 + 2a^6b^3d^{10})x^{14} \\
& + 6/13(20b^9c^7d^3 + 315a^2b^8c^6d^4 + 1512a^2b^7c^5d^5 + 2940a^3b^6c^4d^6 + 2520a^4b^5c^3d^7 + 945a^5b^4c^2d^8 + 140a^6b^3c^1d^9 + 6a^7b^2d^{10})x^{13} \\
& + 3/4(5b^9c^8d^2 + 120a^2b^8c^7d^3 + 840a^2b^7c^6d^4 + 2352a^3b^6c^5d^5 + 2940a^4b^5c^4d^6 + 1680a^5b^4c^3d^7 + 420a^6b^3c^2d^8 + 40a^7b^2c^1d^9 + a^8b^1d^{10})x^{12} \\
& + 1/11(10b^9c^9d + 405a^2b^8c^8d^2 + 4320a^2b^7c^7d^3 + 17640a^3b^6c^6d^4 + 31752a^4b^5c^5d^5 + 26460a^5b^4c^4d^6 + 10080a^6b^3c^3d^7 + 1620a^7b^2c^2d^8 + 90a^8b^1c^1d^9 + a^9d^{10})x^{11} \\
& + 1/10(b^9c^{10} + 90a^2b^8c^9d + 1620a^2b^7c^8d^2 + 10080a^3b^6c^7d^3 + 26460a^4b^5c^6d^4 + 31752a^5b^4c^5d^5 + 17640a^6b^3c^4d^6 + 4320a^7b^2c^3d^7 + 405a^8b^1c^2d^8 + 10a^9c^1d^9) \\
& x^{10} + (a^8b^1c^{10} + 40a^2b^7c^9d + 420a^3b^6c^8d^2 + 1680a^4b^5c^7d^3 + 2940a^5b^4c^6d^4 + 2352a^6b^3c^5d^5 + 840a^7b^2c^4d^6 + 120a^8b^1c^3d^7 + 5a^9c^2d^8)x^9 \\
& + 3/4(6a^2b^7c^{10} + 140a^3b^6c^9d + 945a^4b^5c^8d^2 + 2520a^5b^4c^7d^3 + 2940a^6b^3c^6d^4 + 1512a^7b^2c^5d^5 + 315a^8b^1c^4d^6 + 20a^9c^3d^7) \\
& x^8 + 6(2a^3b^6c^{10} + 30a^4b^5c^9d + 135a^5b^4c^8d^2 + 240a^6b^3c^7d^3 + 180a^7b^2c^6d^4 + 54a^8b^1c^5d^5 + 5a^9c^4d^6)x^7 \\
& + 3(7a^4b^5c^{10} + 70a^5b^4c^9d + 210a^6b^3c^8d^2 + 240a^7b^2c^7d^3 + 105a^8b^1c^6d^4 + 14a^9c^5d^5)x^6 + 6/5(21a^5b^4c^{10} + 140a^6b^3c^9d + 270a^7b^2c^8d^2 + 180a^8b^1c^7d^3 + 35a^9c^6d^4) \\
& x^5 + 3/4(28a^6b^3c^{10} + 120a^7b^2c^9d + 135a^8b^1c^8d^2 + 40a^9c^7d^3)x^4 + 3(4a^7b^2c^{10} + 10a^8b^1c^9d + 5a^9c^8d^2)x^3 + 1/2(9a^8b^1c^{10} + 10a^9c^9d)x^2
\end{aligned}$$

mupad [B] time = 0.79, size = 1404, normalized size = 5.62

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^9*(c + d*x)^{10}, x)$

[Out] $x^7(12a^3b^6c^{10} + 30a^9c^4d^6 + 180a^4b^5c^9d + 324a^8b^1c^5d^5 + 810a^5b^4c^8d^2 + 1440a^6b^3c^7d^3 + 1080a^7b^2c^6d^4) + x^{14}(6a^6b^3d^{10} + 15b^9c^6d^4 + 162a^2b^8c^5d^5 + 90a^5b^4c^1d^9 + 540a^2b^7c^4d^6 + 720a^3b^6c^3d^7 + 405a^4b^5c^2d^8) + x^5((126a^5b^4c^{10})/5 + 42a^9c^6d^4 + 168a^6b^3c^9d + 216a^8b^1c^7d^3 + 324a^7b^2c^8d^2) + x^{16}((63a^4b^5d^{10})/8 + (105b^9c^4d^6)/8 + (135a^2b^8c^3d^7)/2 + (105a^3b^6c^1d^9)/2 + (405a^2b^7c^2d^8)/4) + x^8((9a^2b^7c^{10})/2 + 15a^9c^3d^7 + 105a^3b^6c^9d + (945a^8b^1c^4d^6)/4 + (2835a^4b^5c^8d^2)/4 + 1890a^5b^4c^7d^3 + 2205a^6b^3c^6d^4 + 1134a^7b^2c^5d^5) + x^{13}((36a^7b^2d^{10})/13 + (120b^9c^6d^4$

$$\begin{aligned}
& c^7d^3)/13 + (1890*a*b^8*c^6*d^4)/13 + (840*a^6*b^3*c*d^9)/13 + (9072*a^2* \\
& b^7*c^5*d^5)/13 + (17640*a^3*b^6*c^4*d^6)/13 + (15120*a^4*b^5*c^3*d^7)/13 + \\
& (5670*a^5*b^4*c^2*d^8)/13 + x^9*(a*b^8*c^10 + 5*a^9*c^2*d^8 + 40*a^2*b^7* \\
& c^9*d + 120*a^8*b*c^3*d^7 + 420*a^3*b^6*c^8*d^2 + 1680*a^4*b^5*c^7*d^3 + 29 \\
& 40*a^5*b^4*c^6*d^4 + 2352*a^6*b^3*c^5*d^5 + 840*a^7*b^2*c^4*d^6) + x^{12}*((3 \\
& *a^8*b*d^{10})/4 + (15*b^9*c^8*d^2)/4 + 90*a*b^8*c^7*d^3 + 30*a^7*b^2*c*d^9 + \\
& 630*a^2*b^7*c^6*d^4 + 1764*a^3*b^6*c^5*d^5 + 2205*a^4*b^5*c^4*d^6 + 1260*a \\
& ^5*b^4*c^3*d^7 + 315*a^6*b^3*c^2*d^8) + x^6*(21*a^4*b^5*c^10 + 42*a^9*c^5*d \\
& ^5 + 210*a^5*b^4*c^9*d + 315*a^8*b*c^6*d^4 + 630*a^6*b^3*c^8*d^2 + 720*a^7* \\
& b^2*c^7*d^3) + x^{15}*((42*a^5*b^4*d^{10})/5 + (84*b^9*c^5*d^5)/5 + 126*a*b^8*c \\
& ^4*d^6 + 84*a^4*b^5*c*d^9 + 288*a^2*b^7*c^3*d^7 + 252*a^3*b^6*c^2*d^8) + x^ \\
& 10*((b^9*c^{10})/10 + a^9*c*d^9 + (81*a^8*b*c^2*d^8)/2 + 162*a^2*b^7*c^8*d^2 \\
& + 1008*a^3*b^6*c^7*d^3 + 2646*a^4*b^5*c^6*d^4 + (15876*a^5*b^4*c^5*d^5)/5 + \\
& 1764*a^6*b^3*c^4*d^6 + 432*a^7*b^2*c^3*d^7 + 9*a*b^8*c^9*d) + x^{11}*((a^9*d \\
& ^{10})/11 + (10*b^9*c^9*d)/11 + (405*a*b^8*c^8*d^2)/11 + (4320*a^2*b^7*c^7*d^ \\
& 3)/11 + (17640*a^3*b^6*c^6*d^4)/11 + (31752*a^4*b^5*c^5*d^5)/11 + (26460*a^ \\
& 5*b^4*c^4*d^6)/11 + (10080*a^6*b^3*c^3*d^7)/11 + (1620*a^7*b^2*c^2*d^8)/11 \\
& + (90*a^8*b*c*d^9)/11) + a^9*c^{10}*x + (b^9*d^{10}*x^{20})/20 + (3*a^6*c^7*x^4*(\\
& 40*a^3*d^3 + 28*b^3*c^3 + 120*a*b^2*c^2*d + 135*a^2*b*c*d^2))/4 + (3*b^6*d^ \\
& 7*x^{17}*(28*a^3*d^3 + 40*b^3*c^3 + 135*a*b^2*c^2*d + 120*a^2*b*c*d^2))/17 + \\
& (a^8*c^9*x^2*(10*a*d + 9*b*c))/2 + (b^8*d^9*x^{19}*(9*a*d + 10*b*c))/19 + 3*a \\
& ^7*c^8*x^3*(5*a^2*d^2 + 4*b^2*c^2 + 10*a*b*c*d) + (b^7*d^8*x^{18}*(4*a^2*d^2 \\
& + 5*b^2*c^2 + 10*a*b*c*d))/2
\end{aligned}$$

sympy [B] time = 0.30, size = 1598, normalized size = 6.39

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**9*(d*x+c)**10,x)

[Out] a**9*c**10*x + b**9*d**10*x**20/20 + x**19*(9*a*b**8*d**10/19 + 10*b**9*c*d \\
9/19) + x18*(2*a**2*b**7*d**10 + 5*a*b**8*c*d**9 + 5*b**9*c**2*d**8/2) \\
+ x**17*(84*a**3*b**6*d**10/17 + 360*a**2*b**7*c*d**9/17 + 405*a*b**8*c**2* \\
d**8/17 + 120*b**9*c**3*d**7/17) + x**16*(63*a**4*b**5*d**10/8 + 105*a**3*b \\
6*c*d9/2 + 405*a**2*b**7*c**2*d**8/4 + 135*a*b**8*c**3*d**7/2 + 105*b** \\
9*c**4*d**6/8) + x**15*(42*a**5*b**4*d**10/5 + 84*a**4*b**5*c*d**9 + 252*a* \\
3*b6*c**2*d**8 + 288*a**2*b**7*c**3*d**7 + 126*a*b**8*c**4*d**6 + 84*b** \\
9*c**5*d**5/5) + x**14*(6*a**6*b**3*d**10 + 90*a**5*b**4*c*d**9 + 405*a**4* \\
b**5*c**2*d**8 + 720*a**3*b**6*c**3*d**7 + 540*a**2*b**7*c**4*d**6 + 162*a* \\
b**8*c**5*d**5 + 15*b**9*c**6*d**4) + x**13*(36*a**7*b**2*d**10/13 + 840*a* \\
6*b3*c*d**9/13 + 5670*a**5*b**4*c**2*d**8/13 + 15120*a**4*b**5*c**3*d**7 \\
/13 + 17640*a**3*b**6*c**4*d**6/13 + 9072*a**2*b**7*c**5*d**5/13 + 1890*a*b \\
8*c6*d**4/13 + 120*b**9*c**7*d**3/13) + x**12*(3*a**8*b*d**10/4 + 30*a* \\
7*b2*c*d**9 + 315*a**6*b**3*c**2*d**8 + 1260*a**5*b**4*c**3*d**7 + 2205*

$$\begin{aligned}
& a^{**4}b^{**5}c^{**4}d^{**6} + 1764a^{**3}b^{**6}c^{**5}d^{**5} + 630a^{**2}b^{**7}c^{**6}d^{**4} + \\
& 90a^{**1}b^{**8}c^{**7}d^{**3} + 15b^{**9}c^{**8}d^{**2}/4) + x^{**11}(a^{**9}d^{**10}/11 + 90a^{**8} \\
& *b^{**1}c^{**9}/11 + 1620a^{**7}b^{**2}c^{**2}d^{**8}/11 + 10080a^{**6}b^{**3}c^{**3}d^{**7}/11 + \\
& 26460a^{**5}b^{**4}c^{**4}d^{**6}/11 + 31752a^{**4}b^{**5}c^{**5}d^{**5}/11 + 17640a^{**3}b \\
& **6c^{**6}d^{**4}/11 + 4320a^{**2}b^{**7}c^{**7}d^{**3}/11 + 405a^{**1}b^{**8}c^{**8}d^{**2}/11 + \\
& 10b^{**9}c^{**9}d/11) + x^{**10}(a^{**9}c^{**9}d^{**9} + 81a^{**8}b^{**1}c^{**2}d^{**8}/2 + 432a^{**7} \\
& b^{**2}c^{**3}d^{**7} + 1764a^{**6}b^{**3}c^{**4}d^{**6} + 15876a^{**5}b^{**4}c^{**5}d^{**5}/5 + 2 \\
& 646a^{**4}b^{**5}c^{**6}d^{**4} + 1008a^{**3}b^{**6}c^{**7}d^{**3} + 162a^{**2}b^{**7}c^{**8}d^{**2} \\
& + 9a^{**1}b^{**8}c^{**9}d + b^{**9}c^{**10}/10) + x^{**9}(5a^{**9}c^{**2}d^{**8} + 120a^{**8}b^{**1} \\
& c^{**3}d^{**7} + 840a^{**7}b^{**2}c^{**4}d^{**6} + 2352a^{**6}b^{**3}c^{**5}d^{**5} + 2940a^{**5} \\
& b^{**4}c^{**6}d^{**4} + 1680a^{**4}b^{**5}c^{**7}d^{**3} + 420a^{**3}b^{**6}c^{**8}d^{**2} + 40a^{**2} \\
& *b^{**7}c^{**9}d + a^{**1}b^{**8}c^{**10}) + x^{**8}(15a^{**9}c^{**3}d^{**7} + 945a^{**8}b^{**1}c^{**4} \\
& d^{**6}/4 + 1134a^{**7}b^{**2}c^{**5}d^{**5} + 2205a^{**6}b^{**3}c^{**6}d^{**4} + 1890a^{**5}b^{**1} \\
& *4c^{**7}d^{**3} + 2835a^{**4}b^{**5}c^{**8}d^{**2}/4 + 105a^{**3}b^{**6}c^{**9}d + 9a^{**2}b^{**1} \\
& **7c^{**10}/2) + x^{**7}(30a^{**9}c^{**4}d^{**6} + 324a^{**8}b^{**1}c^{**5}d^{**5} + 1080a^{**7}b^{**1} \\
& **2c^{**6}d^{**4} + 1440a^{**6}b^{**3}c^{**7}d^{**3} + 810a^{**5}b^{**4}c^{**8}d^{**2} + 180a^{**4} \\
& *4b^{**5}c^{**9}d + 12a^{**3}b^{**6}c^{**10}) + x^{**6}(42a^{**9}c^{**5}d^{**5} + 315a^{**8}b^{**1} \\
& *c^{**6}d^{**4} + 720a^{**7}b^{**2}c^{**7}d^{**3} + 630a^{**6}b^{**3}c^{**8}d^{**2} + 210a^{**5}b^{**1} \\
& **4c^{**9}d + 21a^{**4}b^{**5}c^{**10}) + x^{**5}(42a^{**9}c^{**6}d^{**4} + 216a^{**8}b^{**1}c^{**7} \\
& d^{**3} + 324a^{**7}b^{**2}c^{**8}d^{**2} + 168a^{**6}b^{**3}c^{**9}d + 126a^{**5}b^{**4}c^{**10} \\
& /5) + x^{**4}(30a^{**9}c^{**7}d^{**3} + 405a^{**8}b^{**1}c^{**8}d^{**2}/4 + 90a^{**7}b^{**2}c^{**9} \\
& d + 21a^{**6}b^{**3}c^{**10}) + x^{**3}(15a^{**9}c^{**8}d^{**2} + 30a^{**8}b^{**1}c^{**9}d + 12 \\
& *a^{**7}b^{**2}c^{**10}) + x^{**2}(5a^{**9}c^{**9}d + 9a^{**8}b^{**1}c^{**10}/2)
\end{aligned}$$

3.1303 $\int (a + bx)^8 (c + dx)^{10} dx$

Optimal. Leaf size=225

$$-\frac{4b^7(c+dx)^{18}(bc-ad)}{9d^9} + \frac{28b^6(c+dx)^{17}(bc-ad)^2}{17d^9} - \frac{7b^5(c+dx)^{16}(bc-ad)^3}{2d^9} + \frac{14b^4(c+dx)^{15}(bc-ad)^4}{3d^9} - \frac{4b^3(c+dx)^{14}(bc-ad)^5}{d^9}$$

[Out] $1/11*(-a*d+b*c)^8*(d*x+c)^{11}/d^9-2/3*b*(-a*d+b*c)^7*(d*x+c)^{12}/d^9+28/13*b^2*(-a*d+b*c)^6*(d*x+c)^{13}/d^9-4*b^3*(-a*d+b*c)^5*(d*x+c)^{14}/d^9+14/3*b^4*(-a*d+b*c)^4*(d*x+c)^{15}/d^9-7/2*b^5*(-a*d+b*c)^3*(d*x+c)^{16}/d^9+28/17*b^6*(-a*d+b*c)^2*(d*x+c)^{17}/d^9-4/9*b^7*(-a*d+b*c)*(d*x+c)^{18}/d^9+1/19*b^8*(d*x+c)^{19}/d^9$

Rubi [A] time = 0.90, antiderivative size = 225, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{4b^7(c+dx)^{18}(bc-ad)}{9d^9} + \frac{28b^6(c+dx)^{17}(bc-ad)^2}{17d^9} - \frac{7b^5(c+dx)^{16}(bc-ad)^3}{2d^9} + \frac{14b^4(c+dx)^{15}(bc-ad)^4}{3d^9} - \frac{4b^3(c+dx)^{14}(bc-ad)^5}{d^9}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^8*(c + d*x)^10, x]

[Out] $((b*c - a*d)^8*(c + d*x)^{11})/(11*d^9) - (2*b*(b*c - a*d)^7*(c + d*x)^{12})/(3*d^9) + (28*b^2*(b*c - a*d)^6*(c + d*x)^{13})/(13*d^9) - (4*b^3*(b*c - a*d)^5*(c + d*x)^{14})/d^9 + (14*b^4*(b*c - a*d)^4*(c + d*x)^{15})/(3*d^9) - (7*b^5*(b*c - a*d)^3*(c + d*x)^{16})/(2*d^9) + (28*b^6*(b*c - a*d)^2*(c + d*x)^{17})/(17*d^9) - (4*b^7*(b*c - a*d)*(c + d*x)^{18})/(9*d^9) + (b^8*(c + d*x)^{19})/(19*d^9)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^8 (c + dx)^{10} dx &= \int \left(\frac{(-bc + ad)^8 (c + dx)^{10}}{d^8} - \frac{8b(bc - ad)^7 (c + dx)^{11}}{d^8} + \frac{28b^2(bc - ad)^6 (c + dx)^{12}}{d^8} - \frac{56b^3(bc - ad)^5 (c + dx)^{13}}{d^8} + \frac{32b^4(bc - ad)^4 (c + dx)^{14}}{d^8} - \frac{16b^5(bc - ad)^3 (c + dx)^{15}}{d^8} + \frac{8b^6(bc - ad)^2 (c + dx)^{16}}{d^8} - \frac{4b^7(bc - ad) (c + dx)^{17}}{d^8} + \frac{b^8 (c + dx)^{18}}{d^8} \right) dx \\ &= \frac{(bc - ad)^8 (c + dx)^{11}}{11d^9} - \frac{2b(bc - ad)^7 (c + dx)^{12}}{3d^9} + \frac{28b^2(bc - ad)^6 (c + dx)^{13}}{13d^9} - \frac{4b^3(bc - ad)^5 (c + dx)^{14}}{d^9} + \frac{14b^4(bc - ad)^4 (c + dx)^{15}}{3d^9} - \frac{7b^5(bc - ad)^3 (c + dx)^{16}}{2d^9} + \frac{28b^6(bc - ad)^2 (c + dx)^{17}}{17d^9} - \frac{4b^7(bc - ad) (c + dx)^{18}}{9d^9} + \frac{b^8 (c + dx)^{19}}{19d^9} \end{aligned}$$

$$\begin{aligned}
& d^7c^3b^8 + 45/2x^{16}d^8c^2b^7a + 35/2x^{16}d^9c^*b^6a^2 + 7/2x^{16}d^{10}b^5a^3 + 14x^{15}d^6c^4b^8 + 64x^{15}d^7c^3b^7a + 84x^{15}d^8c^2b^6a^2 + 112/3x^{15}d^9c^*b^5a^3 + 14/3x^{15}d^{10}b^4a^4 + 18x^{14}d^5c^5b^8 + 120x^{14}d^6c^4b^7a + 240x^{14}d^7c^3b^6a^2 + 180x^{14}d^8c^2b^5a^3 + 50x^{14}d^9c^*b^4a^4 + 4x^{14}d^{10}b^3a^5 + 210/13x^{13}d^4c^6b^8 + 2016/13x^{13}d^5c^5b^7a + 5880/13x^{13}d^6c^4b^6a^2 + 6720/13x^{13}d^7c^3b^5a^3 + 3150/13x^{13}d^8c^2b^4a^4 + 560/13x^{13}d^9c^*b^3a^5 + 28/13x^{13}d^{10}b^2a^6 + 10x^{12}d^3c^7b^8 + 140x^{12}d^4c^6b^7a + 588x^{12}d^5c^5b^6a^2 + 980x^{12}d^6c^4b^5a^3 + 700x^{12}d^7c^3b^4a^4 + 210x^{12}d^8c^2b^3a^5 + 70/3x^{12}d^9c^*b^2a^6 + 2/3x^{12}d^{10}b^1a^7 + 45/11x^{11}d^2c^8b^8 + 960/11x^{11}d^3c^7b^7a + 5880/11x^{11}d^4c^6b^6a^2 + 14112/11x^{11}d^5c^5b^5a^3 + 14700/11x^{11}d^6c^4b^4a^4 + 6720/11x^{11}d^7c^3b^3a^5 + 1260/11x^{11}d^8c^2b^2a^6 + 80/11x^{11}d^9c^*b^1a^7 + 1/11x^{11}d^{10}a^8 + x^{10}d^*c^9b^8 + 36x^{10}d^2c^8b^7a + 336x^{10}d^3c^7b^6a^2 + 1176x^{10}d^4c^6b^5a^3 + 1764x^{10}d^5c^5b^4a^4 + 1176x^{10}d^6c^4b^3a^5 + 336x^{10}d^7c^3b^2a^6 + 36x^{10}d^8c^2b^1a^7 + x^{10}d^9c^*a^8 + 1/9x^9c^{10}b^8 + 80/9x^9d^*c^9b^7a + 140x^9d^2c^8b^6a^2 + 2240/3x^9d^3c^7b^5a^3 + 4900/3x^9d^4c^6b^4a^4 + 1568x^9d^5c^5b^3a^5 + 1960/3x^9d^6c^4b^2a^6 + 320/3x^9d^7c^3b^1a^7 + 5x^9d^8c^2a^8 + x^8c^{10}b^7a + 35x^8d^*c^9b^6a^2 + 315x^8d^2c^8b^5a^3 + 1050x^8d^3c^7b^4a^4 + 1470x^8d^4c^6b^3a^5 + 882x^8d^5c^5b^2a^6 + 210x^8d^6c^4b^1a^7 + 15x^8d^7c^3a^8 + 4x^7c^{10}b^6a^2 + 80x^7d^*c^9b^5a^3 + 450x^7d^2c^8b^4a^4 + 960x^7d^3c^7b^3a^5 + 840x^7d^4c^6b^2a^6 + 288x^7d^5c^5b^1a^7 + 30x^7d^6c^4a^8 + 28/3x^6c^{10}b^5a^3 + 350/3x^6d^*c^9b^4a^4 + 420x^6d^2c^8b^3a^5 + 560x^6d^3c^7b^2a^6 + 280x^6d^4c^6b^1a^7 + 42x^6d^5c^5a^8 + 14x^5c^{10}b^4a^4 + 112x^5d^*c^9b^3a^5 + 252x^5d^2c^8b^2a^6 + 192x^5d^3c^7b^1a^7 + 42x^5d^4c^6a^8 + 14x^4c^{10}b^3a^5 + 70x^4d^*c^9b^2a^6 + 90x^4d^2c^8b^1a^7 + 30x^4d^3c^7a^8 + 28/3x^3c^{10}b^2a^6 + 80/3x^3d^*c^9b^1a^7 + 15x^3d^2c^8a^8 + 4x^2c^{10}b^1a^7 + 5x^2d^*c^9a^8 + xc^{10}a^8
\end{aligned}$$

giac [B] time = 1.29, size = 1478, normalized size = 6.57

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8*(d*x+c)^10,x, algorithm="giac")

[Out] 1/19*b^8*d^10*x^19 + 5/9*b^8*c*d^9*x^18 + 4/9*a*b^7*d^10*x^18 + 45/17*b^8*c^2*d^8*x^17 + 80/17*a*b^7*c*d^9*x^17 + 28/17*a^2*b^6*d^10*x^17 + 15/2*b^8*c^3*d^7*x^16 + 45/2*a*b^7*c^2*d^8*x^16 + 35/2*a^2*b^6*c*d^9*x^16 + 7/2*a^3*b^5*d^10*x^16 + 14*b^8*c^4*d^6*x^15 + 64*a*b^7*c^3*d^7*x^15 + 84*a^2*b^6*c^2*d^8*x^15 + 112/3*a^3*b^5*c*d^9*x^15 + 14/3*a^4*b^4*d^10*x^15 + 18*b^8*c^5*d^5*x^14 + 120*a*b^7*c^4*d^6*x^14 + 240*a^2*b^6*c^3*d^7*x^14 + 180*a^3*b^5*

$$\begin{aligned}
& c^2 d^8 x^{14} + 50 a^4 b^4 c d^9 x^{14} + 4 a^5 b^3 d^{10} x^{14} + 210/13 b^8 c^6 \\
& d^4 x^{13} + 2016/13 a b^7 c^5 d^5 x^{13} + 5880/13 a^2 b^6 c^4 d^6 x^{13} + 672 \\
& 0/13 a^3 b^5 c^3 d^7 x^{13} + 3150/13 a^4 b^4 c^2 d^8 x^{13} + 560/13 a^5 b^3 c \\
& d^9 x^{13} + 28/13 a^6 b^2 d^{10} x^{13} + 10 b^8 c^7 d^3 x^{12} + 140 a b^7 c^6 d \\
& ^4 x^{12} + 588 a^2 b^6 c^5 d^5 x^{12} + 980 a^3 b^5 c^4 d^6 x^{12} + 700 a^4 b^4 \\
& c^3 d^7 x^{12} + 210 a^5 b^3 c^2 d^8 x^{12} + 70/3 a^6 b^2 c d^9 x^{12} + 2/3 a^ \\
& 7 b d^{10} x^{12} + 45/11 b^8 c^8 d^2 x^{11} + 960/11 a b^7 c^7 d^3 x^{11} + 5880/1 \\
& 1 a^2 b^6 c^6 d^4 x^{11} + 14112/11 a^3 b^5 c^5 d^5 x^{11} + 14700/11 a^4 b^4 c \\
& ^4 d^6 x^{11} + 6720/11 a^5 b^3 c^3 d^7 x^{11} + 1260/11 a^6 b^2 c^2 d^8 x^{11} + \\
& 80/11 a^7 b c d^9 x^{11} + 1/11 a^8 d^{10} x^{11} + b^8 c^9 d x^{10} + 36 a b^7 c^ \\
& 8 d^2 x^{10} + 336 a^2 b^6 c^7 d^3 x^{10} + 1176 a^3 b^5 c^6 d^4 x^{10} + 1764 a^ \\
& 4 b^4 c^5 d^5 x^{10} + 1176 a^5 b^3 c^4 d^6 x^{10} + 336 a^6 b^2 c^3 d^7 x^{10} + \\
& 36 a^7 b c^2 d^8 x^{10} + a^8 c d^9 x^{10} + 1/9 b^8 c^{10} x^9 + 80/9 a b^7 c^9 \\
& d x^9 + 140 a^2 b^6 c^8 d^2 x^9 + 2240/3 a^3 b^5 c^7 d^3 x^9 + 4900/3 a^4 b \\
& ^4 c^6 d^4 x^9 + 1568 a^5 b^3 c^5 d^5 x^9 + 1960/3 a^6 b^2 c^4 d^6 x^9 + 3 \\
& 20/3 a^7 b c^3 d^7 x^9 + 5 a^8 c^2 d^8 x^9 + a b^7 c^{10} x^8 + 35 a^2 b^6 c^ \\
& 9 d x^8 + 315 a^3 b^5 c^8 d^2 x^8 + 1050 a^4 b^4 c^7 d^3 x^8 + 1470 a^5 b^3 \\
& c^6 d^4 x^8 + 882 a^6 b^2 c^5 d^5 x^8 + 210 a^7 b c^4 d^6 x^8 + 15 a^8 c^3 \\
& d^7 x^8 + 4 a^2 b^6 c^{10} x^7 + 80 a^3 b^5 c^9 d x^7 + 450 a^4 b^4 c^8 d^2 x \\
& ^7 + 960 a^5 b^3 c^7 d^3 x^7 + 840 a^6 b^2 c^6 d^4 x^7 + 288 a^7 b c^5 d^5 \\
& x^7 + 30 a^8 c^4 d^6 x^7 + 28/3 a^3 b^5 c^{10} x^6 + 350/3 a^4 b^4 c^9 d x^6 \\
& + 420 a^5 b^3 c^8 d^2 x^6 + 560 a^6 b^2 c^7 d^3 x^6 + 280 a^7 b c^6 d^4 x^ \\
& 6 + 42 a^8 c^5 d^5 x^6 + 14 a^4 b^4 c^{10} x^5 + 112 a^5 b^3 c^9 d x^5 + 252 a \\
& ^6 b^2 c^8 d^2 x^5 + 192 a^7 b c^7 d^3 x^5 + 42 a^8 c^6 d^4 x^5 + 14 a^5 b \\
& ^3 c^{10} x^4 + 70 a^6 b^2 c^9 d x^4 + 90 a^7 b c^8 d^2 x^4 + 30 a^8 c^7 d^3 x \\
& ^4 + 28/3 a^6 b^2 c^{10} x^3 + 80/3 a^7 b c^9 d x^3 + 15 a^8 c^8 d^2 x^3 + 4 \\
& a^7 b c^{10} x^2 + 5 a^8 c^9 d x^2 + a^8 c^{10} x
\end{aligned}$$

maple [B] time = 0.00, size = 1291, normalized size = 5.74

$$\frac{b^8 d^{10} x^{19}}{19} + a^8 c^{10} x + \frac{(8 a b^7 d^{10} + 10 b^8 c d^9) x^{18}}{18} + \frac{(28 a^2 b^6 d^{10} + 80 a b^7 c d^9 + 45 b^8 c^2 d^8) x^{17}}{17} + \frac{(56 a^3 b^5 d^{10} + 280 a^2 b^6 c d^9 + 360 a b^7 c^2 d^8 + 120 b^8 c^3 d^7) x^{16}}{15} + \frac{(70 a^4 b^4 d^{10} + 560 a^3 b^5 c d^9 + 1260 a^2 b^6 c^2 d^8 + 960 a b^7 c^3 d^7 + 210 b^8 c^4 d^6) x^{15}}{14} + \frac{(56 a^5 b^3 d^{10} + 700 a^4 b^4 c d^9 + 2520 a^3 b^5 c^2 d^8 + 3360 a^2 b^6 c^3 d^7 + 1680 a b^7 c^4 d^6 + 252 b^8 c^5 d^5) x^{14}}{13} + \frac{(28 a^6 b^2 d^{10} + 560 a^5 b^3 c d^9 + 3150 a^4 b^4 c^2 d^8 + 6720 a^3 b^5 c^3 d^7 + 5880 a^2 b^6 c^4 d^6 + 2016 a b^7 c^5 d^5 + 210 b^8 c^6 d^4) x^{13}}{12} + \frac{(8 a^7 b d^{10} + 280 a^6 b^2 c d^9 + 280 a^5 b^3 c^2 d^8 + 140 a^4 b^4 c^3 d^7 + 56 a^3 b^5 c^4 d^6 + 14 a^2 b^6 c^5 d^5 + 2 a b^7 c^6 d^4 + a^8 c^7 d^3) x^{12}}{11} + \frac{(80 a^8 c d^9 + 80 a^7 b c^2 d^8 + 40 a^6 b^2 c^3 d^7 + 16 a^5 b^3 c^4 d^6 + 4 a^4 b^4 c^5 d^5 + 4 a^3 b^5 c^6 d^4 + 4 a^2 b^6 c^7 d^3 + 4 a b^7 c^8 d^2 + 4 a^8 c^9 d) x^{11}}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x^{10}}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x^9}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x^8}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x^7}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x^6}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x^5}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x^4}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x^3}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x^2}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x}{11} + \frac{(80 a^8 c^{10} + 80 a^7 b c^9 d + 40 a^6 b^2 c^8 d^2 + 16 a^5 b^3 c^7 d^3 + 4 a^4 b^4 c^6 d^4 + 4 a^3 b^5 c^5 d^5 + 4 a^2 b^6 c^4 d^6 + 4 a b^7 c^3 d^7 + 4 a^8 c^2 d^8) x^0}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^8*(d*x+c)^10,x)

[Out] 1/19*b^8*d^10*x^19+1/18*(8*a*b^7*d^10+10*b^8*c*d^9)*x^18+1/17*(28*a^2*b^6*d^10+80*a*b^7*c*d^9+45*b^8*c^2*d^8)*x^17+1/16*(56*a^3*b^5*d^10+280*a^2*b^6*c*d^9+360*a*b^7*c^2*d^8+120*b^8*c^3*d^7)*x^16+1/15*(70*a^4*b^4*d^10+560*a^3*b^5*c*d^9+1260*a^2*b^6*c^2*d^8+960*a*b^7*c^3*d^7+210*b^8*c^4*d^6)*x^15+1/14*(56*a^5*b^3*d^10+700*a^4*b^4*c*d^9+2520*a^3*b^5*c^2*d^8+3360*a^2*b^6*c^3*d^7+1680*a*b^7*c^4*d^6+252*b^8*c^5*d^5)*x^14+1/13*(28*a^6*b^2*d^10+560*a^5*b^3*c*d^9+3150*a^4*b^4*c^2*d^8+6720*a^3*b^5*c^3*d^7+5880*a^2*b^6*c^4*d^6+2016*a*b^7*c^5*d^5+210*b^8*c^6*d^4)*x^13+1/12*(8*a^7*b*d^10+280*a^6*b^2*c*d^9+280*a^5*b^3*c^2*d^8+140*a^4*b^4*c^3*d^7+56*a^3*b^5*c^4*d^6+14*a^2*b^6*c^5*d^5+2*a*b^7*c^6*d^4+a^8*c^7*d^3)*x^12+1/11*(80*a^8*c*d^9+80*a^7*b*c^2*d^8+40*a^6*b^2*c^3*d^7+16*a^5*b^3*c^4*d^6+4*a^4*b^4*c^5*d^5+4*a^3*b^5*c^6*d^4+4*a^2*b^6*c^7*d^3+4*a*b^7*c^8*d^2+4*a^8*c^9*d)*x^11+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x^10+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x^9+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x^8+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x^7+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x^6+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x^5+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x^4+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x^3+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x^2+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x+1/11*(80*a^8*c^{10}+80*a^7*b*c^9*d+40*a^6*b^2*c^8*d^2+16*a^5*b^3*c^7*d^3+4*a^4*b^4*c^6*d^4+4*a^3*b^5*c^5*d^5+4*a^2*b^6*c^4*d^6+4*a*b^7*c^3*d^7+4*a^8*c^2*d^8)*x^0

$$\begin{aligned}
& 2520*a^5*b^3*c^2*d^8+8400*a^4*b^4*c^3*d^7+11760*a^3*b^5*c^4*d^6+7056*a^2*b^6*c^5*d^5+1680*a*b^7*c^6*d^4+120*b^8*c^7*d^3)*x^{12}+1/11*(a^8*d^{10}+80*a^7*b*c*d^9+1260*a^6*b^2*c^2*d^8+6720*a^5*b^3*c^3*d^7+14700*a^4*b^4*c^4*d^6+14112*a^3*b^5*c^5*d^5+5880*a^2*b^6*c^6*d^4+960*a*b^7*c^7*d^3+45*b^8*c^8*d^2)*x^{11}+1/10*(10*a^8*c*d^9+360*a^7*b*c^2*d^8+3360*a^6*b^2*c^3*d^7+11760*a^5*b^3*c^4*d^6+17640*a^4*b^4*c^5*d^5+11760*a^3*b^5*c^6*d^4+3360*a^2*b^6*c^7*d^3+360*a*b^7*c^8*d^2+10*b^8*c^9*d)*x^{10}+1/9*(45*a^8*c^2*d^8+960*a^7*b*c^3*d^7+5880*a^6*b^2*c^4*d^6+14112*a^5*b^3*c^5*d^5+14700*a^4*b^4*c^6*d^4+6720*a^3*b^5*c^7*d^3+1260*a^2*b^6*c^8*d^2+80*a*b^7*c^9*d+b^8*c^{10})*x^9+1/8*(120*a^8*c^3*d^7+1680*a^7*b*c^4*d^6+7056*a^6*b^2*c^5*d^5+11760*a^5*b^3*c^6*d^4+8400*a^4*b^4*c^7*d^3+2520*a^3*b^5*c^8*d^2+280*a^2*b^6*c^9*d+8*a*b^7*c^{10})*x^8+1/7*(20*a^8*c^4*d^6+2016*a^7*b*c^5*d^5+5880*a^6*b^2*c^6*d^4+6720*a^5*b^3*c^7*d^3+3150*a^4*b^4*c^8*d^2+560*a^3*b^5*c^9*d+28*a^2*b^6*c^{10})*x^7+1/6*(252*a^8*c^5*d^5+1680*a^7*b*c^6*d^4+3360*a^6*b^2*c^7*d^3+2520*a^5*b^3*c^8*d^2+700*a^4*b^4*c^9*d+56*a^3*b^5*c^{10})*x^6+1/5*(210*a^8*c^6*d^4+960*a^7*b*c^7*d^3+1260*a^6*b^2*c^8*d^2+560*a^5*b^3*c^9*d+70*a^4*b^4*c^{10})*x^5+1/4*(120*a^8*c^7*d^3+360*a^7*b*c^8*d^2+280*a^6*b^2*c^9*d+56*a^5*b^3*c^{10})*x^4+1/3*(45*a^8*c^8*d^2+80*a^7*b*c^9*d+28*a^6*b^2*c^{10})*x^3+1/2*(10*a^8*c^9*d+8*a^7*b*c^{10})*x^2+a^8*c^{10}*x
\end{aligned}$$

maxima [B] time = 1.51, size = 1283, normalized size = 5.70

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8*(d*x+c)^10,x, algorithm="maxima")

[Out] $1/19*b^8*d^{10}*x^{19} + a^8*c^{10}*x + 1/9*(5*b^8*c*d^9 + 4*a*b^7*d^{10})*x^{18} + 1/17*(45*b^8*c^2*d^8 + 80*a*b^7*c*d^9 + 28*a^2*b^6*d^{10})*x^{17} + 1/2*(15*b^8*c^3*d^7 + 45*a*b^7*c^2*d^8 + 35*a^2*b^6*c*d^9 + 7*a^3*b^5*d^{10})*x^{16} + 2/3*(21*b^8*c^4*d^6 + 96*a*b^7*c^3*d^7 + 126*a^2*b^6*c^2*d^8 + 56*a^3*b^5*c*d^9 + 7*a^4*b^4*d^{10})*x^{15} + 2*(9*b^8*c^5*d^5 + 60*a*b^7*c^4*d^6 + 120*a^2*b^6*c^3*d^7 + 90*a^3*b^5*c^2*d^8 + 25*a^4*b^4*c*d^9 + 2*a^5*b^3*d^{10})*x^{14} + 1/13*(15*b^8*c^6*d^4 + 144*a*b^7*c^5*d^5 + 420*a^2*b^6*c^4*d^6 + 480*a^3*b^5*c^3*d^7 + 225*a^4*b^4*c^2*d^8 + 40*a^5*b^3*c*d^9 + 2*a^6*b^2*d^{10})*x^{13} + 2/3*(15*b^8*c^7*d^3 + 210*a*b^7*c^6*d^4 + 882*a^2*b^6*c^5*d^5 + 1470*a^3*b^5*c^4*d^6 + 1050*a^4*b^4*c^3*d^7 + 315*a^5*b^3*c^2*d^8 + 35*a^6*b^2*c*d^9 + a^7*b*d^{10})*x^{12} + 1/11*(45*b^8*c^8*d^2 + 960*a*b^7*c^7*d^3 + 5880*a^2*b^6*c^6*d^4 + 14112*a^3*b^5*c^5*d^5 + 14700*a^4*b^4*c^4*d^6 + 6720*a^5*b^3*c^3*d^7 + 1260*a^6*b^2*c^2*d^8 + 80*a^7*b*c*d^9 + a^8*d^{10})*x^{11} + (b^8*c^9*d + 36*a*b^7*c^8*d^2 + 336*a^2*b^6*c^7*d^3 + 1176*a^3*b^5*c^6*d^4 + 1764*a^4*b^4*c^5*d^5 + 1176*a^5*b^3*c^4*d^6 + 336*a^6*b^2*c^3*d^7 + 36*a^7*b*c^2*d^8 + a^8*c*d^9)*x^{10} + 1/9*(b^8*c^{10} + 80*a*b^7*c^9*d + 1260*a^2*b^6*c^8*d^2 + 6720*a^3*b^5*c^7*d^3 + 14700*a^4*b^4*c^6*d^4 + 14112*a^5*b^3*c^5*d^5 + 5880*a^6*b^2*c^4*d^6 + 960*a^7*b*c^3*d^7 + 45*a^8*c^2*d^8)*x^9 + (a*b^7*c^{10}$

$$\begin{aligned}
& + 35a^2b^6c^9d + 315a^3b^5c^8d^2 + 1050a^4b^4c^7d^3 + 1470a^5b^3c^6d^4 + 882a^6b^2c^5d^5 + 210a^7b^1c^4d^6 + 15a^8c^3d^7) x^8 \\
& + 2(2a^2b^6c^{10} + 40a^3b^5c^9d + 225a^4b^4c^8d^2 + 480a^5b^3c^7d^3 + 420a^6b^2c^6d^4 + 144a^7b^1c^5d^5 + 15a^8c^4d^6) x^7 + \\
& 14/3(2a^3b^5c^{10} + 25a^4b^4c^9d + 90a^5b^3c^8d^2 + 120a^6b^2c^7d^3 + 60a^7b^1c^6d^4 + 9a^8c^5d^5) x^6 + 2(7a^4b^4c^{10} + 56a^5b^3c^9d \\
& + 126a^6b^2c^8d^2 + 96a^7b^1c^7d^3 + 21a^8c^6d^4) x^5 + 2(7a^5b^3c^{10} + 35a^6b^2c^9d + 45a^7b^1c^8d^2 + 15a^8c^7d^3) \\
&) x^4 + 1/3(28a^6b^2c^{10} + 80a^7b^1c^9d + 45a^8c^8d^2) x^3 + (4a^7b^1c^{10} + 5a^8c^9d) x^2
\end{aligned}$$

mupad [B] time = 0.71, size = 1253, normalized size = 5.57

$$x^7 (30 a^8 c^4 d^6 + 288 a^7 b c^5 d^5 + 840 a^6 b^2 c^6 d^4 + 960 a^5 b^3 c^7 d^3 + 450 a^4 b^4 c^8 d^2 + 80 a^3 b^5 c^9 d + 4 a^2 b^6 c^{10}) + x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^8*(c + d*x)^10,x)

[Out] $x^7(4a^2b^6c^{10} + 30a^8c^4d^6 + 80a^3b^5c^9d + 288a^7b^1c^5d^5 + 450a^4b^4c^8d^2 + 960a^5b^3c^7d^3 + 840a^6b^2c^6d^4) + x^{13}((28a^6b^2d^{10})/13 + (210b^8c^6d^4)/13 + (2016a^1b^7c^5d^5)/13 + (560a^5b^3c^9d^9)/13 + (5880a^2b^6c^4d^6)/13 + (6720a^3b^5c^3d^7)/13 + (3150a^4b^4c^2d^8)/13) + x^8(a^8b^7c^{10} + 15a^8c^3d^7 + 35a^2b^6c^9d + 210a^7b^1c^4d^6 + 315a^3b^5c^8d^2 + 1050a^4b^4c^7d^3 + 1470a^5b^3c^6d^4 + 882a^6b^2c^5d^5) + x^{12}((2a^7b^1d^{10})/3 + 10b^8c^7d^3 + 140a^1b^7c^6d^4 + (70a^6b^2c^9d^9)/3 + 588a^2b^6c^5d^5 + 980a^3b^5c^4d^6 + 700a^4b^4c^3d^7 + 210a^5b^3c^2d^8) + x^{10}(a^8c^9d + b^8c^9d + 36a^1b^7c^8d^2 + 36a^7b^1c^2d^8 + 336a^2b^6c^7d^3 + 1176a^3b^5c^6d^4 + 1764a^4b^4c^5d^5 + 1176a^5b^3c^4d^6 + 336a^6b^2c^3d^7) + x^5(14a^4b^4c^{10} + 42a^8c^6d^4 + 112a^5b^3c^9d + 192a^7b^1c^7d^3 + 252a^6b^2c^8d^2) + x^{15}((14a^4b^4d^{10})/3 + 14b^8c^4d^6 + 64a^1b^7c^3d^7 + (112a^3b^5c^9d^9)/3 + 84a^2b^6c^2d^8) + x^6((28a^3b^5c^{10})/3 + 42a^8c^5d^5 + (350a^4b^4c^9d)/3 + 280a^7b^1c^6d^4 + 420a^5b^3c^8d^2 + 560a^6b^2c^7d^3) + x^{14}(4a^5b^3d^{10} + 18b^8c^5d^5 + 120a^1b^7c^4d^6 + 50a^4b^4c^9d + 240a^2b^6c^3d^7 + 180a^3b^5c^2d^8) + x^9((b^8c^{10})/9 + 5a^8c^2d^8 + (320a^7b^1c^3d^7)/3 + 140a^2b^6c^8d^2 + (2240a^3b^5c^7d^3)/3 + (4900a^4b^4c^6d^4)/3 + 1568a^5b^3c^5d^5 + (1960a^6b^2c^4d^6)/3 + (80a^1b^7c^9d)/9) + x^{11}((a^8d^{10})/11 + (45b^8c^8d^2)/11 + (960a^1b^7c^7d^3)/11 + (5880a^2b^6c^6d^4)/11 + (14112a^3b^5c^5d^5)/11 + (14700a^4b^4c^4d^6)/11 + (6720a^5b^3c^3d^7)/11 + (1260a^6b^2c^2d^8)/11 + (80a^7b^1c^9d)/11) + a^8c^{10}x + (b^8d^{10}x^{19})/19 + 2a^5c^7x^4(15a^3d^3 + 7b^3c^3 + 35a^1b^2c^2d + 45a^2b^1c^2d^2) +$

$$\frac{(b^5 d^7 x^{16} (7 a^3 d^3 + 15 b^3 c^3 + 45 a^2 b^2 c^2 d + 35 a^2 b c d^2))}{2} + a^7 c^9 x^2 (5 a d + 4 b c) + \frac{(b^7 d^9 x^{18} (4 a d + 5 b c))}{9} + \frac{(a^6 c^8 x^3 (45 a^2 d^2 + 28 b^2 c^2 + 80 a b c d))}{3} + \frac{(b^6 d^8 x^{17} (28 a^2 d^2 + 45 b^2 c^2 + 80 a b c d))}{17}$$

sympy [B] time = 0.27, size = 1428, normalized size = 6.35

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**8*(d*x+c)**10,x)

[Out] a**8*c**10*x + b**8*d**10*x**19/19 + x**18*(4*a*b**7*d**10/9 + 5*b**8*c*d**9/9) + x**17*(28*a**2*b**6*d**10/17 + 80*a*b**7*c*d**9/17 + 45*b**8*c**2*d**8/17) + x**16*(7*a**3*b**5*d**10/2 + 35*a**2*b**6*c*d**9/2 + 45*a*b**7*c**2*d**8/2 + 15*b**8*c**3*d**7/2) + x**15*(14*a**4*b**4*d**10/3 + 112*a**3*b**5*c*d**9/3 + 84*a**2*b**6*c**2*d**8 + 64*a*b**7*c**3*d**7 + 14*b**8*c**4*d**6) + x**14*(4*a**5*b**3*d**10 + 50*a**4*b**4*c*d**9 + 180*a**3*b**5*c**2*d**8 + 240*a**2*b**6*c**3*d**7 + 120*a*b**7*c**4*d**6 + 18*b**8*c**5*d**5) + x**13*(28*a**6*b**2*d**10/13 + 560*a**5*b**3*c*d**9/13 + 3150*a**4*b**4*c**2*d**8/13 + 6720*a**3*b**5*c**3*d**7/13 + 5880*a**2*b**6*c**4*d**6/13 + 2016*a*b**7*c**5*d**5/13 + 210*b**8*c**6*d**4/13) + x**12*(2*a**7*b*d**10/3 + 70*a**6*b**2*c*d**9/3 + 210*a**5*b**3*c**2*d**8 + 700*a**4*b**4*c**3*d**7 + 980*a**3*b**5*c**4*d**6 + 588*a**2*b**6*c**5*d**5 + 140*a*b**7*c**6*d**4 + 10*b**8*c**7*d**3) + x**11*(a**8*d**10/11 + 80*a**7*b*c*d**9/11 + 1260*a**6*b**2*c**2*d**8/11 + 6720*a**5*b**3*c**3*d**7/11 + 14700*a**4*b**4*c**4*d**6/11 + 14112*a**3*b**5*c**5*d**5/11 + 5880*a**2*b**6*c**6*d**4/11 + 960*a*b**7*c**7*d**3/11 + 45*b**8*c**8*d**2/11) + x**10*(a**8*c*d**9 + 36*a**7*b*c**2*d**8 + 336*a**6*b**2*c**3*d**7 + 1176*a**5*b**3*c**4*d**6 + 1764*a**4*b**4*c**5*d**5 + 1176*a**3*b**5*c**6*d**4 + 336*a**2*b**6*c**7*d**3 + 36*a*b**7*c**8*d**2 + b**8*c**9*d) + x**9*(5*a**8*c**2*d**8 + 320*a**7*b*c**3*d**7/3 + 1960*a**6*b**2*c**4*d**6/3 + 1568*a**5*b**3*c**5*d**5 + 4900*a**4*b**4*c**6*d**4/3 + 2240*a**3*b**5*c**7*d**3/3 + 140*a**2*b**6*c**8*d**2 + 80*a*b**7*c**9*d/9 + b**8*c**10/9) + x**8*(15*a**8*c**3*d**7 + 210*a**7*b*c**4*d**6 + 882*a**6*b**2*c**5*d**5 + 1470*a**5*b**3*c**6*d**4 + 1050*a**4*b**4*c**7*d**3 + 315*a**3*b**5*c**8*d**2 + 35*a**2*b**6*c**9*d + a*b**7*c**10) + x**7*(30*a**8*c**4*d**6 + 288*a**7*b*c**5*d**5 + 840*a**6*b**2*c**6*d**4 + 960*a**5*b**3*c**7*d**3 + 450*a**4*b**4*c**8*d**2 + 80*a**3*b**5*c**9*d + 4*a**2*b**6*c**10) + x**6*(42*a**8*c**5*d**5 + 280*a**7*b*c**6*d**4 + 560*a**6*b**2*c**7*d**3 + 420*a**5*b**3*c**8*d**2 + 350*a**4*b**4*c**9*d/3 + 28*a**3*b**5*c**10/3) + x**5*(42*a**8*c**6*d**4 + 192*a**7*b*c**7*d**3 + 252*a**6*b**2*c**8*d**2 + 112*a**5*b**3*c**9*d + 14*a**4*b**4*c**10) + x**4*(30*a**8*c**7*d**3 + 90*a**7*b*c**8*d**2 + 70*a**6*b**2*c**9*d + 14*a**5*b**3*c**10) + x**3*(15*a**8*c**8*d**2 + 80*a**7*b*c**9*d/3 + 28*a**6*b**2*c**10/3) + x**2*(5*a**8*c**9*d + 4*a**7*b*c**10)

3.1304 $\int (a + bx)^7 (c + dx)^{10} dx$

Optimal. Leaf size=200

$$\frac{7b^6(c+dx)^{17}(bc-ad)}{17d^8} + \frac{21b^5(c+dx)^{16}(bc-ad)^2}{16d^8} - \frac{7b^4(c+dx)^{15}(bc-ad)^3}{3d^8} + \frac{5b^3(c+dx)^{14}(bc-ad)^4}{2d^8} - \frac{21b^2(c+dx)^{13}(bc-ad)^5}{d^8} + \frac{7b(c+dx)^{12}(bc-ad)^6}{d^8} - \frac{b(c+dx)^{11}(bc-ad)^7}{d^8}$$

[Out] $-1/11*(-a*d+b*c)^7*(d*x+c)^{11}/d^8+7/12*b*(-a*d+b*c)^6*(d*x+c)^{12}/d^8-21/13*b^2*(-a*d+b*c)^5*(d*x+c)^{13}/d^8+5/2*b^3*(-a*d+b*c)^4*(d*x+c)^{14}/d^8-7/3*b^4*(-a*d+b*c)^3*(d*x+c)^{15}/d^8+21/16*b^5*(-a*d+b*c)^2*(d*x+c)^{16}/d^8-7/17*b^6*(-a*d+b*c)*(d*x+c)^{17}/d^8+1/18*b^7*(d*x+c)^{18}/d^8$

Rubi [A] time = 0.77, antiderivative size = 200, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{7b^6(c+dx)^{17}(bc-ad)}{17d^8} + \frac{21b^5(c+dx)^{16}(bc-ad)^2}{16d^8} - \frac{7b^4(c+dx)^{15}(bc-ad)^3}{3d^8} + \frac{5b^3(c+dx)^{14}(bc-ad)^4}{2d^8} - \frac{21b^2(c+dx)^{13}(bc-ad)^5}{d^8} + \frac{7b(c+dx)^{12}(bc-ad)^6}{d^8} - \frac{b(c+dx)^{11}(bc-ad)^7}{d^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7*(c + d*x)^10, x]

[Out] $-((b*c - a*d)^7*(c + d*x)^{11}/(11*d^8) + (7*b*(b*c - a*d)^6*(c + d*x)^{12})/(12*d^8) - (21*b^2*(b*c - a*d)^5*(c + d*x)^{13})/(13*d^8) + (5*b^3*(b*c - a*d)^4*(c + d*x)^{14})/(2*d^8) - (7*b^4*(b*c - a*d)^3*(c + d*x)^{15})/(3*d^8) + (21*b^5*(b*c - a*d)^2*(c + d*x)^{16})/(16*d^8) - (7*b^6*(b*c - a*d)*(c + d*x)^{17})/(17*d^8) + (b^7*(c + d*x)^{18})/(18*d^8)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^7 (c + dx)^{10} dx &= \int \left(\frac{(-bc + ad)^7 (c + dx)^{10}}{d^7} + \frac{7b(bc - ad)^6 (c + dx)^{11}}{d^7} - \frac{21b^2(bc - ad)^5 (c + dx)^{12}}{d^7} + \frac{35b^3(bc - ad)^4 (c + dx)^{13}}{d^7} - \frac{35b^4(bc - ad)^3 (c + dx)^{14}}{d^7} + \frac{21b^5(bc - ad)^2 (c + dx)^{15}}{d^7} - \frac{7b^6(bc - ad) (c + dx)^{16}}{d^7} + \frac{b^7 (c + dx)^{17}}{d^7} \right) dx \\ &= -\frac{(bc - ad)^7 (c + dx)^{11}}{11d^8} + \frac{7b(bc - ad)^6 (c + dx)^{12}}{12d^8} - \frac{21b^2(bc - ad)^5 (c + dx)^{13}}{13d^8} + \frac{5b^3(bc - ad)^4 (c + dx)^{14}}{2d^8} - \frac{7b^4(bc - ad)^3 (c + dx)^{15}}{3d^8} + \frac{21b^5(bc - ad)^2 (c + dx)^{16}}{16d^8} - \frac{7b^6(bc - ad) (c + dx)^{17}}{17d^8} + \frac{b^7 (c + dx)^{18}}{18d^8} \end{aligned}$$

Mathematica [B] time = 0.14, size = 1105, normalized size = 5.52

$$\frac{1}{18}b^7d^{10}x^{18} + \frac{1}{17}b^6d^9(10bc+7ad)x^{17} + \frac{1}{16}b^5d^8(45b^2c^2 + 70abdc + 21a^2d^2)x^{16} + \frac{1}{3}b^4d^7(24b^3c^3 + 63ab^2dc^2 + 42a^2b^2c^2d + 21a^3d^3)x^{15} + \frac{1}{2}b^3d^6(24b^4c^4 + 63ab^3c^3d + 27a^2b^2c^2d^2 + 24a^3b^2c^2d^3 + 6a^4d^4)x^{14} + \frac{1}{2}b^2d^5(24b^5c^5 + 63ab^4c^4d + 27a^2b^3c^3d^2 + 24a^3b^3c^3d^3 + 6a^4d^4)x^{13} + \frac{1}{2}bd^4(24b^6c^6 + 63ab^5c^5d + 27a^2b^4c^4d^2 + 24a^3b^4c^4d^3 + 6a^4d^4)x^{12} + \frac{1}{2}d^3(24b^7c^7 + 63ab^6c^6d + 27a^2b^5c^5d^2 + 24a^3b^5c^5d^3 + 6a^4d^4)x^{11} + \frac{1}{2}d^2(24b^8c^8 + 63ab^7c^7d + 27a^2b^6c^6d^2 + 24a^3b^6c^6d^3 + 6a^4d^4)x^{10} + \frac{1}{2}d(24b^9c^9 + 63ab^8c^8d + 27a^2b^7c^7d^2 + 24a^3b^7c^7d^3 + 6a^4d^4)x^9 + \frac{1}{2}(24b^{10}c^{10} + 63ab^9c^9d + 27a^2b^8c^8d^2 + 24a^3b^8c^8d^3 + 6a^4d^4)x^8 + \frac{1}{2}(24b^{11}c^{11} + 63ab^{10}c^{10}d + 27a^2b^9c^9d^2 + 24a^3b^9c^9d^3 + 6a^4d^4)x^7 + \frac{1}{2}(24b^{12}c^{12} + 63ab^{11}c^{11}d + 27a^2b^{10}c^{10}d^2 + 24a^3b^{10}c^{10}d^3 + 6a^4d^4)x^6 + \frac{1}{2}(24b^{13}c^{13} + 63ab^{12}c^{12}d + 27a^2b^{11}c^{11}d^2 + 24a^3b^{11}c^{11}d^3 + 6a^4d^4)x^5 + \frac{1}{2}(24b^{14}c^{14} + 63ab^{13}c^{13}d + 27a^2b^{12}c^{12}d^2 + 24a^3b^{12}c^{12}d^3 + 6a^4d^4)x^4 + \frac{1}{2}(24b^{15}c^{15} + 63ab^{14}c^{14}d + 27a^2b^{13}c^{13}d^2 + 24a^3b^{13}c^{13}d^3 + 6a^4d^4)x^3 + \frac{1}{2}(24b^{16}c^{16} + 63ab^{15}c^{15}d + 27a^2b^{14}c^{14}d^2 + 24a^3b^{14}c^{14}d^3 + 6a^4d^4)x^2 + \frac{1}{2}(24b^{17}c^{17} + 63ab^{16}c^{16}d + 27a^2b^{15}c^{15}d^2 + 24a^3b^{15}c^{15}d^3 + 6a^4d^4)x + \frac{1}{2}(24b^{18}c^{18} + 63ab^{17}c^{17}d + 27a^2b^{16}c^{16}d^2 + 24a^3b^{16}c^{16}d^3 + 6a^4d^4)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7*(c + d*x)^10,x]

[Out] $a^7c^{10}x + (a^6c^9(7bc + 10ad)x^2)/2 + (a^5c^8(21b^2c^2 + 70abc + 35a^2d^2)x^3)/3 + (5a^4c^7(7b^3c^3 + 42ab^2c^2d + 63a^2b^2c^2d^2 + 24a^3d^3)x^4)/4 + 7a^3c^6(b^4c^4 + 10ab^3c^3d + 27a^2b^2c^2d^2 + 24a^3b^2c^2d^3 + 6a^4d^4)x^5 + (7a^2c^5(3b^5c^5 + 50ab^4c^4d + 225a^2b^3c^3d^2 + 360a^3b^2c^2d^3 + 210a^4b^2c^2d^4 + 36a^5d^5)x^6)/6 + a^2c^4(b^6c^6 + 30ab^5c^5d + 225a^2b^4c^4d^2 + 600a^3b^3c^3d^3 + 630a^4b^2c^2d^4 + 252a^5b^2c^2d^5 + 30a^6d^6)x^7 + (c^3(b^7c^7 + 70ab^6c^6d + 945a^2b^5c^5d^2 + 4200a^3b^4c^4d^3 + 7350a^4b^3c^3d^4 + 5292a^5b^2c^2d^5 + 1470a^6b^2c^2d^6 + 120a^7d^7)x^8)/8 + (5c^2d(2b^7c^7 + 63ab^6c^6d + 504a^2b^5c^5d^2 + 1470a^3b^4c^4d^3 + 1764a^4b^3c^3d^4 + 882a^5b^2c^2d^5 + 168a^6b^2c^2d^6 + 9a^7d^7)x^9)/9 + (cd^2(9b^7c^7 + 168ab^6c^6d + 882a^2b^5c^5d^2 + 1764a^3b^4c^4d^3 + 1470a^4b^3c^3d^4 + 504a^5b^2c^2d^5 + 63a^6b^2c^2d^6 + 2a^7d^7)x^{10})/2 + (d^3(120b^7c^7 + 1470ab^6c^6d + 5292a^2b^5c^5d^2 + 7350a^3b^4c^4d^3 + 4200a^4b^3c^3d^4 + 945a^5b^2c^2d^5 + 70a^6b^2c^2d^6 + a^7d^7)x^{11})/11 + (7bd^4(30b^6c^6 + 252ab^5c^5d + 630a^2b^4c^4d^2 + 600a^3b^3c^3d^3 + 225a^4b^2c^2d^4 + 30a^5b^2c^2d^5 + a^6d^6)x^{12})/12 + (7b^2d^5(36b^5c^5 + 210ab^4c^4d + 360a^2b^3c^3d^2 + 225a^3b^2c^2d^3 + 50a^4b^2c^2d^4 + 3a^5d^5)x^{13})/13 + (5b^3d^6(6b^4c^4 + 24ab^3c^3d + 27a^2b^2c^2d^2 + 10a^3b^2c^2d^3 + a^4d^4)x^{14})/2 + (b^4d^7(24b^3c^3 + 63ab^2c^2d + 42a^2b^2c^2d^2 + 7a^3d^3)x^{15})/3 + (b^5d^8(45b^2c^2 + 70ab^2c^2d + 21a^2d^2)x^{16})/16 + (b^6d^9(10b^2c^2 + 7ad)x^{17})/17 + (b^7d^{10}x^{18})/18$

fricas [B] time = 0.39, size = 1302, normalized size = 6.51

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7*(d*x+c)^10,x, algorithm="fricas")

[Out] $1/18x^{18}d^{10}b^7 + 10/17x^{17}d^9c^7b^7 + 7/17x^{17}d^{10}b^6a + 45/16x^{16}d^8c^2b^7 + 35/8x^{16}d^9c^7b^6a + 21/16x^{16}d^{10}b^5a^2 + 8x^{15}d^7c^3b^7 + 21x^{15}d^8c^2b^6a + 14x^{15}d^9c^7b^5a^2 + 7/3x^{15}d^{10}b^4a^3 + 15x^{14}d^6c^4b^7 + 60x^{14}d^7c^3b^6a + 135/2x^{14}d^8c^2b^5a^2 + 25x^{14}d^9c^7b^4a^3 + 5/2x^{14}d^{10}b^3a^4 + 252/13x^{13}d^5c^5b^7 + 252/13x^{13}d^6c^4b^6a + 252/13x^{13}d^7c^3b^5a^2 + 252/13x^{13}d^8c^2b^4a^3 + 252/13x^{13}d^9c^7b^3a^4 + 252/13x^{13}d^{10}b^2a^5$

$$\begin{aligned}
&^5b^7 + 1470/13x^{13}d^6c^4b^6a + 2520/13x^{13}d^7c^3b^5a^2 + 1575/13x^{13}d^8c^2b^4a^3 + 350/13x^{13}d^9c^1b^3a^4 + 21/13x^{13}d^{10}b^2a^5 \\
&+ 35/2x^{12}d^4c^6b^7 + 147x^{12}d^5c^5b^6a + 735/2x^{12}d^6c^4b^5a^2 + 350x^{12}d^7c^3b^4a^3 + 525/4x^{12}d^8c^2b^3a^4 + 35/2x^{12}d^9c^1b^2a^5 \\
&+ 7/12x^{12}d^{10}b^1a^6 + 120/11x^{11}d^3c^7b^7 + 1470/11x^{11}d^4c^6b^6a + 5292/11x^{11}d^5c^5b^5a^2 + 7350/11x^{11}d^6c^4b^4a^3 + 4200/11x^{11}d^7c^3b^3a^4 \\
&+ 945/11x^{11}d^8c^2b^2a^5 + 70/11x^{11}d^9c^1b^1a^6 + 1/11x^{11}d^{10}a^7 + 9/2x^{10}d^2c^8b^7 + 84x^{10}d^3c^7b^6a + 441x^{10}d^4c^6b^5a^2 + 882x^{10}d^5c^5b^4a^3 \\
&+ 735x^{10}d^6c^4b^3a^4 + 252x^{10}d^7c^3b^2a^5 + 63/2x^{10}d^8c^2b^1a^6 + x^{10}d^9c^1a^7 + 10/9x^9d^4c^6b^4a^3 + 980x^9d^5c^5b^3a^4 + 490x^9d^6c^4b^2a^5 \\
&+ 280/3x^9d^7c^3b^1a^6 + 5x^9d^8c^2a^7 + 1/8x^8c^{10}b^7 + 35/4x^8d^4c^6b^3a^4 + 945/8x^8d^5c^5b^2a^5 + 525x^8d^6c^4b^1a^6 + 3675/4x^8d^7c^3a^7 \\
&+ x^7c^{10}b^6a + 30x^7d^2c^8b^4a^3 + 600x^7d^3c^7b^3a^4 + 630x^7d^4c^6b^2a^5 + 225x^7d^5c^5b^1a^6 + 30x^7d^6c^4a^7 + 7/2x^6c^{10}b^5a^2 + 175/3x^6d^2c^9b^4a^3 \\
&+ 525/2x^6d^3c^8b^3a^4 + 420x^6d^4c^7b^2a^5 + 245x^6d^5c^6b^1a^6 + 42x^6d^6c^5a^7 + 7x^5c^{10}b^4a^3 + 70x^5d^2c^9b^3a^4 + 189x^5d^3c^8b^2a^5 + 168x^5d^4c^7b^1a^6 \\
&+ 42x^5d^5c^6a^7 + 35/4x^4c^{10}b^3a^4 + 105/2x^4d^2c^8b^2a^5 + 315/4x^4d^3c^7b^1a^6 + 30x^4d^4c^6b^1a^6 + 70/3x^3d^2c^8a^7 + 7/2x^2c^{10}b^1a^6 + 5x^2d^2c^9a^7 \\
&+ x^2d^3c^8a^7 + 7/2x^2c^{10}b^1a^6 + 5x^2d^2c^9a^7 + x^2c^{10}a^7
\end{aligned}$$

giac [B] time = 1.26, size = 1302, normalized size = 6.51

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7*(d*x+c)^10,x, algorithm="giac")

[Out] $1/18b^7d^{10}x^{18} + 10/17b^7c^1d^9x^{17} + 7/17a^1b^6d^{10}x^{17} + 45/16b^7c^2d^8x^{16} + 35/8a^1b^6c^1d^9x^{16} + 21/16a^2b^5d^{10}x^{16} + 8b^7c^3d^7x^{15} + 21a^1b^6c^2d^8x^{15} + 14a^2b^5c^1d^9x^{15} + 7/3a^3b^4d^{10}x^{15} + 15b^7c^4d^6x^{14} + 60a^1b^6c^3d^7x^{14} + 135/2a^2b^5c^2d^8x^{14} + 25a^3b^4c^1d^9x^{14} + 5/2a^4b^3d^{10}x^{14} + 252/13b^7c^5d^5x^{13} + 1470/13a^1b^6c^4d^6x^{13} + 2520/13a^2b^5c^3d^7x^{13} + 1575/13a^3b^4c^2d^8x^{13} + 350/13a^4b^3c^1d^9x^{13} + 21/13a^5b^2d^{10}x^{13} + 35/2b^7c^6d^4x^{12} + 147a^1b^6c^5d^5x^{12} + 735/2a^2b^5c^4d^6x^{12} + 350a^3b^4c^3d^7x^{12} + 525/4a^4b^3c^2d^8x^{12} + 35/2a^5b^2c^1d^9x^{12} + 7/12a^6b^1d^{10}x^{12} + 120/11b^7c^7d^3x^{11} + 1470/11a^1b^6c^6d^4x^{11} + 5292/11a^2b^5c^5d^5x^{11} + 7350/11a^3b^4c^4d^6x^{11} + 4200/11a^4b^3c^3d^7x^{11} + 945/11a^5b^2c^2d^8x^{11} + 70/11a^6b^1c^1d^9x^{11} + 1/11a^7d^{10}x^{11} + 9/2b^7c^8d^2x^{10} + 84a^1b^6c^7d^3x^{10} + 441a^2b^5c^6d^4x^{10} + 882a^3b^4c^5d^5x^{10} + 735a^4b^3c^4d^6x^{10} + 252a^5b^2c^3d^7x^{10} + 63/2a^6b^1c^2d^8x^{10} + x^{10}d^9c^1a^7 + 10/9x^9d^4c^6b^4a^3 + 980x^9d^5c^5b^3a^4 + 490x^9d^6c^4b^2a^5 + 280/3x^9d^7c^3b^1a^6 + 5x^9d^8c^2a^7 + 1/8x^8c^{10}b^7 + 35/4x^8d^4c^6b^3a^4 + 945/8x^8d^5c^5b^2a^5 + 525x^8d^6c^4b^1a^6 + 3675/4x^8d^7c^3a^7 + x^7c^{10}b^6a + 30x^7d^2c^8b^4a^3 + 600x^7d^3c^7b^3a^4 + 630x^7d^4c^6b^2a^5 + 225x^7d^5c^5b^1a^6 + 30x^7d^6c^4a^7 + 7/2x^6c^{10}b^5a^2 + 175/3x^6d^2c^9b^4a^3 + 525/2x^6d^3c^8b^3a^4 + 420x^6d^4c^7b^2a^5 + 245x^6d^5c^6b^1a^6 + 42x^6d^6c^5a^7 + 7x^5c^{10}b^4a^3 + 70x^5d^2c^9b^3a^4 + 189x^5d^3c^8b^2a^5 + 168x^5d^4c^7b^1a^6 + 42x^5d^5c^6a^7 + 35/4x^4c^{10}b^3a^4 + 105/2x^4d^2c^8b^2a^5 + 315/4x^4d^3c^7b^1a^6 + 30x^4d^4c^6b^1a^6 + 70/3x^3d^2c^8a^7 + 7/2x^2c^{10}b^1a^6 + 5x^2d^2c^9a^7 + x^2d^3c^8a^7 + 7/2x^2c^{10}b^1a^6 + 5x^2d^2c^9a^7 + x^2c^{10}a^7$

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*x^10 + 441*a^2*b^5*c^6*d^4*x^10 + 882*a^3*b^4*c^5*d^5*x^10 + 735*a^4*b^3*c^
^4*d^6*x^10 + 252*a^5*b^2*c^3*d^7*x^10 + 63/2*a^6*b*c^2*d^8*x^10 + a^7*c*d^
9*x^10 + 10/9*b^7*c^9*d*x^9 + 35*a*b^6*c^8*d^2*x^9 + 280*a^2*b^5*c^7*d^3*x^
9 + 2450/3*a^3*b^4*c^6*d^4*x^9 + 980*a^4*b^3*c^5*d^5*x^9 + 490*a^5*b^2*c^4*
d^6*x^9 + 280/3*a^6*b*c^3*d^7*x^9 + 5*a^7*c^2*d^8*x^9 + 1/8*b^7*c^10*x^8 +
35/4*a*b^6*c^9*d*x^8 + 945/8*a^2*b^5*c^8*d^2*x^8 + 525*a^3*b^4*c^7*d^3*x^8
+ 3675/4*a^4*b^3*c^6*d^4*x^8 + 1323/2*a^5*b^2*c^5*d^5*x^8 + 735/4*a^6*b*c^4
*d^6*x^8 + 15*a^7*c^3*d^7*x^8 + a*b^6*c^10*x^7 + 30*a^2*b^5*c^9*d*x^7 + 225
*a^3*b^4*c^8*d^2*x^7 + 600*a^4*b^3*c^7*d^3*x^7 + 630*a^5*b^2*c^6*d^4*x^7 +
252*a^6*b*c^5*d^5*x^7 + 30*a^7*c^4*d^6*x^7 + 7/2*a^2*b^5*c^10*x^6 + 175/3*a
^3*b^4*c^9*d*x^6 + 525/2*a^4*b^3*c^8*d^2*x^6 + 420*a^5*b^2*c^7*d^3*x^6 + 24
5*a^6*b*c^6*d^4*x^6 + 42*a^7*c^5*d^5*x^6 + 7*a^3*b^4*c^10*x^5 + 70*a^4*b^3*
c^9*d*x^5 + 189*a^5*b^2*c^8*d^2*x^5 + 168*a^6*b*c^7*d^3*x^5 + 42*a^7*c^6*d^
4*x^5 + 35/4*a^4*b^3*c^10*x^4 + 105/2*a^5*b^2*c^9*d*x^4 + 315/4*a^6*b*c^8*d
^2*x^4 + 30*a^7*c^7*d^3*x^4 + 7*a^5*b^2*c^10*x^3 + 70/3*a^6*b*c^9*d*x^3 + 1
5*a^7*c^8*d^2*x^3 + 7/2*a^6*b*c^10*x^2 + 5*a^7*c^9*d*x^2 + a^7*c^10*x

```

maple [B] time = 0.00, size = 1141, normalized size = 5.70

$$\frac{b^7 d^{10} x^{18}}{18} + a^7 c^{10} x + \frac{(7a b^6 d^{10} + 10b^7 c d^9) x^{17}}{17} + \frac{(21a^2 b^5 d^{10} + 70a b^6 c d^9 + 45b^7 c^2 d^8) x^{16}}{16} + \frac{(35a^3 b^4 d^{10} + 210a^2 b^5 c d^9 + 315a b^6 c^2 d^8 + 120b^7 c^3 d^7 + 210b^7 c^4 d^6) x^{15}}{15} + \frac{(35a^4 b^3 d^{10} + 350a^3 b^4 c d^9 + 945a^2 b^5 c^2 d^8 + 840a b^6 c^3 d^7 + 210b^7 c^4 d^6) x^{14}}{14} + \frac{(21a^5 b^2 d^{10} + 350a^4 b^3 c d^9 + 1575a^3 b^4 c^2 d^8 + 2520a^2 b^5 c^3 d^7 + 1470a b^6 c^4 d^6 + 252b^7 c^5 d^5) x^{13}}{13} + \frac{(7a^6 b d^{10} + 210a^5 b^2 c d^9 + 1575a^4 b^3 c^2 d^8 + 4200a^3 b^4 c^3 d^7 + 4410a^2 b^5 c^4 d^6 + 1764a b^6 c^5 d^5 + 210b^7 c^6 d^4) x^{12}}{12} + \frac{(a^7 d^{10} + 70a^6 b c d^9 + 945a^5 b^2 c^2 d^8 + 4200a^4 b^3 c^3 d^7 + 7350a^3 b^4 c^4 d^6 + 5292a^2 b^5 c^5 d^5 + 1470a b^6 c^6 d^4 + 120b^7 c^7 d^3) x^{11}}{11} + \frac{(10a^7 c d^9 + 315a^6 b c^2 d^8 + 2520a^5 b^2 c^3 d^7 + 7350a^4 b^3 c^4 d^6 + 8820a^3 b^4 c^5 d^5 + 4410a^2 b^5 c^6 d^4 + 840a b^6 c^7 d^3 + 45b^7 c^8 d^2) x^{10}}{10} + \frac{(45a^7 c^2 d^8 + 840a^6 b c^3 d^7 + 4410a^5 b^2 c^4 d^6 + 8820a^4 b^3 c^5 d^5 + 7350a^3 b^4 c^6 d^4 + 2520a^2 b^5 c^7 d^3 + 315a b^6 c^8 d^2 + 10b^7 c^9 d) x^9}{9} + \frac{1}{8} (120a^7 c^3 d^7 + 1470a^6 b c^4 d^6 + 5292a^5 b^2 c^5 d^5 + 7350a^4 b^3 c^6 d^4 + 4200a^3 b^4 c^7 d^3 + 945a^2 b^5 c^8 d^2 + 70a b^6 c^9 d + b^7 c^{10}) x^8 + \frac{1}{7} (210a^7 c^4 d^6 + 1764a^6 b c^5 d^5 + 4410a^5 b^2 c^6 d^4 + 4200a^4 b^3 c^7 d^3 + 1575a^3 b^4 c^8 d^2 + 210a^2 b^5 c^9 d + 7a b^6 c^{10}) x^7 + \frac{1}{6} (252a^7 c^5 d^5 + 1470a^6 b c^6 d^4 + 2520a^5 b^2 c^7 d^3 + 1575a^4 b^3 c^8 d^2 + 350a^3 b^4 c^9 d + 210a^2 b^5 c^{10}) x^6 + \frac{1}{5} (315a^7 c^6 d^4 + 2520a^6 b c^7 d^3 + 1575a^5 b^2 c^8 d^2 + 350a^4 b^3 c^9 d + 210a^3 b^4 c^{10}) x^5 + \frac{1}{4} (420a^7 c^7 d^3 + 2520a^6 b c^8 d^2 + 1575a^5 b^2 c^9 d + 420a^4 b^3 c^{10}) x^4 + \frac{1}{3} (525a^7 c^8 d^2 + 1575a^6 b c^9 d + 420a^5 b^2 c^{10}) x^3 + \frac{1}{2} (735a^7 c^9 d + 420a^6 b c^{10}) x^2 + \frac{1}{1} (735a^7 c^{10}) x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7*(d*x+c)^10,x)

[Out] 1/18*b^7*d^10*x^18+1/17*(7*a*b^6*d^10+10*b^7*c*d^9)*x^17+1/16*(21*a^2*b^5*d^10+70*a*b^6*c*d^9+45*b^7*c^2*d^8)*x^16+1/15*(35*a^3*b^4*d^10+210*a^2*b^5*c*d^9+315*a*b^6*c^2*d^8+120*b^7*c^3*d^7)*x^15+1/14*(35*a^4*b^3*d^10+350*a^3*b^4*c*d^9+945*a^2*b^5*c^2*d^8+840*a*b^6*c^3*d^7+210*b^7*c^4*d^6)*x^14+1/13*(21*a^5*b^2*d^10+350*a^4*b^3*c*d^9+1575*a^3*b^4*c^2*d^8+2520*a^2*b^5*c^3*d^7+1470*a*b^6*c^4*d^6+252*b^7*c^5*d^5)*x^13+1/12*(7*a^6*b*d^10+210*a^5*b^2*c*d^9+1575*a^4*b^3*c^2*d^8+4200*a^3*b^4*c^3*d^7+4410*a^2*b^5*c^4*d^6+1764*a*b^6*c^5*d^5+210*b^7*c^6*d^4)*x^12+1/11*(a^7*d^10+70*a^6*b*c*d^9+945*a^5*b^2*c^2*d^8+4200*a^4*b^3*c^3*d^7+7350*a^3*b^4*c^4*d^6+5292*a^2*b^5*c^5*d^5+1470*a*b^6*c^6*d^4+120*b^7*c^7*d^3)*x^11+1/10*(10*a^7*c*d^9+315*a^6*b*c^2*d^8+2520*a^5*b^2*c^3*d^7+7350*a^4*b^3*c^4*d^6+8820*a^3*b^4*c^5*d^5+4410*a^2*b^5*c^6*d^4+840*a*b^6*c^7*d^3+45*b^7*c^8*d^2)*x^10+1/9*(45*a^7*c^2*d^8+840*a^6*b*c^3*d^7+4410*a^5*b^2*c^4*d^6+8820*a^4*b^3*c^5*d^5+7350*a^3*b^4*c^6*d^4+2520*a^2*b^5*c^7*d^3+315*a*b^6*c^8*d^2+10*b^7*c^9*d)*x^9+1/8*(120*a^7*c^3*d^7+1470*a^6*b*c^4*d^6+5292*a^5*b^2*c^5*d^5+7350*a^4*b^3*c^6*d^4+4200*a^3*b^4*c^7*d^3+945*a^2*b^5*c^8*d^2+70*a*b^6*c^9*d+b^7*c^10)*x^8+1/7*(210*a^7*c^4*d^6+1764*a^6*b*c^5*d^5+4410*a^5*b^2*c^6*d^4+4200*a^4*b^3*c^7*d^3+1575*a^3*b^4*c^8*d^2+210*a^2*b^5*c^9*d+7*a*b^6*c^10)*x^7+1/6*(252*a^7*c^5*d^5+1470*a^6*b*c^6*d^4+2520*a^5*b^2*c^7*d^3+1575*a^4*b^3*c^8*d^2+350*a^3*b^4*c^9*d+210*a^2*b^5*c^10)*x^6+1/5*(315*a^7*c^6*d^4+2520*a^6*b*c^7*d^3+1575*a^5*b^2*c^8*d^2+350*a^4*b^3*c^9*d+210*a^3*b^4*c^10)*x^5+1/4*(420*a^7*c^7*d^3+2520*a^6*b*c^8*d^2+1575*a^5*b^2*c^9*d+420*a^4*b^3*c^10)*x^4+1/3*(525*a^7*c^8*d^2+1575*a^6*b*c^9*d+420*a^5*b^2*c^10)*x^3+1/2*(735*a^7*c^9*d+420*a^6*b*c^10)*x^2+735*a^7*c^10*x

$$a^2 b^5 c^{10} x^6 + \frac{1}{5} (210 a^7 c^6 d^4 + 840 a^6 b c^7 d^3 + 945 a^5 b^2 c^8 d^2 + 350 a^4 b^3 c^9 d + 35 a^3 b^4 c^{10}) x^5 + \frac{1}{4} (120 a^7 c^7 d^3 + 315 a^6 b c^8 d^2 + 210 a^5 b^2 c^9 d + 35 a^4 b^3 c^{10}) x^4 + \frac{1}{3} (45 a^7 c^8 d^2 + 70 a^6 b c^9 d + 21 a^5 b^2 c^{10}) x^3 + \frac{1}{2} (10 a^7 c^9 d + 7 a^6 b c^{10}) x^2 + a^7 c^{10} x$$

maxima [B] time = 1.52, size = 1135, normalized size = 5.68

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7*(d*x+c)^10,x, algorithm="maxima")

[Out] $\frac{1}{18} b^7 d^{10} x^{18} + a^7 c^{10} x + \frac{1}{17} (10 b^7 c d^9 + 7 a b^6 d^{10}) x^{17} + \frac{1}{16} (45 b^7 c^2 d^8 + 70 a b^6 c d^9 + 21 a^2 b^5 d^{10}) x^{16} + \frac{1}{3} (24 b^7 c^3 d^7 + 63 a b^6 c^2 d^8 + 42 a^2 b^5 c d^9 + 7 a^3 b^4 d^{10}) x^{15} + \frac{5}{2} (6 b^7 c^4 d^6 + 24 a b^6 c^3 d^7 + 27 a^2 b^5 c^2 d^8 + 10 a^3 b^4 c d^9 + a^4 b^3 d^{10}) x^{14} + \frac{7}{13} (36 b^7 c^5 d^5 + 210 a b^6 c^4 d^6 + 360 a^2 b^5 c^3 d^7 + 225 a^3 b^4 c^2 d^8 + 50 a^4 b^3 c d^9 + 3 a^5 b^2 d^{10}) x^{13} + \frac{7}{12} (30 b^7 c^6 d^4 + 252 a b^6 c^5 d^5 + 630 a^2 b^5 c^4 d^6 + 600 a^3 b^4 c^3 d^7 + 225 a^4 b^3 c^2 d^8 + 30 a^5 b^2 c d^9 + a^6 b d^{10}) x^{12} + \frac{1}{11} (120 b^7 c^7 d^3 + 1470 a b^6 c^6 d^4 + 5292 a^2 b^5 c^5 d^5 + 7350 a^3 b^4 c^4 d^6 + 4200 a^4 b^3 c^3 d^7 + 945 a^5 b^2 c^2 d^8 + 70 a^6 b c d^9 + a^7 d^{10}) x^{11} + \frac{1}{2} (9 b^7 c^8 d^2 + 168 a b^6 c^7 d^3 + 882 a^2 b^5 c^6 d^4 + 1764 a^3 b^4 c^5 d^5 + 1470 a^4 b^3 c^4 d^6 + 504 a^5 b^2 c^3 d^7 + 63 a^6 b c^2 d^8 + 2 a^7 c d^9) x^{10} + \frac{5}{9} (2 b^7 c^9 d + 63 a b^6 c^8 d^2 + 504 a^2 b^5 c^7 d^3 + 1470 a^3 b^4 c^6 d^4 + 1764 a^4 b^3 c^5 d^5 + 882 a^5 b^2 c^4 d^6 + 168 a^6 b c^3 d^7 + 9 a^7 c^2 d^8) x^9 + \frac{1}{8} (b^7 c^{10} + 70 a b^6 c^9 d + 945 a^2 b^5 c^8 d^2 + 4200 a^3 b^4 c^7 d^3 + 7350 a^4 b^3 c^6 d^4 + 5292 a^5 b^2 c^5 d^5 + 1470 a^6 b c^4 d^6 + 120 a^7 c^3 d^7) x^8 + (a b^6 c^{10} + 30 a^2 b^5 c^9 d + 225 a^3 b^4 c^8 d^2 + 600 a^4 b^3 c^7 d^3 + 630 a^5 b^2 c^6 d^4 + 252 a^6 b c^5 d^5 + 30 a^7 c^4 d^6) x^7 + \frac{7}{6} (3 a^2 b^5 c^{10} + 50 a^3 b^4 c^9 d + 225 a^4 b^3 c^8 d^2 + 360 a^5 b^2 c^7 d^3 + 210 a^6 b c^6 d^4 + 36 a^7 c^5 d^5) x^6 + 7 (a^3 b^4 c^{10} + 10 a^4 b^3 c^9 d + 27 a^5 b^2 c^8 d^2 + 24 a^6 b c^7 d^3 + 6 a^7 c^6 d^4) x^5 + \frac{5}{4} (7 a^4 b^3 c^{10} + 42 a^5 b^2 c^9 d + 63 a^6 b c^8 d^2 + 24 a^7 c^7 d^3) x^4 + \frac{1}{3} (21 a^5 b^2 c^{10} + 70 a^6 b c^9 d + 45 a^7 c^8 d^2) x^3 + \frac{1}{2} (7 a^6 b c^{10} + 10 a^7 c^9 d) x^2$

mupad [B] time = 0.61, size = 1106, normalized size = 5.53

$$x^{10} \left(a^7 c d^9 + \frac{63 a^6 b c^2 d^8}{2} + 252 a^5 b^2 c^3 d^7 + 735 a^4 b^3 c^4 d^6 + 882 a^3 b^4 c^5 d^5 + 441 a^2 b^5 c^6 d^4 + 84 a b^6 c^7 d^3 + \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^7*(c + d*x)^10,x)`

[Out] $x^{10}*(a^7*c*d^9 + (9*b^7*c^8*d^2)/2 + 84*a*b^6*c^7*d^3 + (63*a^6*b*c^2*d^8)/2 + 441*a^2*b^5*c^6*d^4 + 882*a^3*b^4*c^5*d^5 + 735*a^4*b^3*c^4*d^6 + 252*a^5*b^2*c^3*d^7) + x^9*((10*b^7*c^9*d)/9 + 5*a^7*c^2*d^8 + 35*a*b^6*c^8*d^2 + (280*a^6*b*c^3*d^7)/3 + 280*a^2*b^5*c^7*d^3 + (2450*a^3*b^4*c^6*d^4)/3 + 980*a^4*b^3*c^5*d^5 + 490*a^5*b^2*c^4*d^6) + x^5*(7*a^3*b^4*c^10 + 42*a^7*c^6*d^4 + 70*a^4*b^3*c^9*d + 168*a^6*b*c^7*d^3 + 189*a^5*b^2*c^8*d^2) + x^{14}*((5*a^4*b^3*d^{10})/2 + 15*b^7*c^4*d^6 + 60*a*b^6*c^3*d^7 + 25*a^3*b^4*c*d^9 + (135*a^2*b^5*c^2*d^8)/2) + x^8*((b^7*c^{10})/8 + 15*a^7*c^3*d^7 + (735*a^6*b*c^4*d^6)/4 + (945*a^2*b^5*c^8*d^2)/8 + 525*a^3*b^4*c^7*d^3 + (3675*a^4*b^3*c^6*d^4)/4 + (1323*a^5*b^2*c^5*d^5)/2 + (35*a*b^6*c^9*d)/4) + x^{11}*((a^7*d^{10})/11 + (120*b^7*c^7*d^3)/11 + (1470*a*b^6*c^6*d^4)/11 + (5292*a^2*b^5*c^5*d^5)/11 + (7350*a^3*b^4*c^4*d^6)/11 + (4200*a^4*b^3*c^3*d^7)/11 + (945*a^5*b^2*c^2*d^8)/11 + (70*a^6*b*c*d^9)/11) + x^6*((7*a^2*b^5*c^{10})/2 + 42*a^7*c^5*d^5 + (175*a^3*b^4*c^9*d)/3 + 245*a^6*b*c^6*d^4 + (525*a^4*b^3*c^8*d^2)/2 + 420*a^5*b^2*c^7*d^3) + x^{13}*((21*a^5*b^2*d^{10})/13 + (252*b^7*c^5*d^5)/13 + (1470*a*b^6*c^4*d^6)/13 + (350*a^4*b^3*c*d^9)/13 + (2520*a^2*b^5*c^3*d^7)/13 + (1575*a^3*b^4*c^2*d^8)/13) + x^7*(a*b^6*c^{10} + 30*a^7*c^4*d^6 + 30*a^2*b^5*c^9*d + 252*a^6*b*c^5*d^5 + 225*a^3*b^4*c^8*d^2 + 600*a^4*b^3*c^7*d^3 + 630*a^5*b^2*c^6*d^4) + x^{12}*((7*a^6*b*d^{10})/12 + (35*b^7*c^6*d^4)/2 + 147*a*b^6*c^5*d^5 + (35*a^5*b^2*c*d^9)/2 + (735*a^2*b^5*c^4*d^6)/2 + 350*a^3*b^4*c^3*d^7 + (525*a^4*b^3*c^2*d^8)/4) + a^7*c^{10}*x + (b^7*d^{10}*x^{18})/18 + (5*a^4*c^7*x^4*(24*a^3*d^3 + 7*b^3*c^3 + 42*a*b^2*c^2*d + 63*a^2*b*c*d^2))/4 + (b^4*d^7*x^{15}*(7*a^3*d^3 + 24*b^3*c^3 + 63*a*b^2*c^2*d + 42*a^2*b*c*d^2))/3 + (a^6*c^9*x^2*(10*a*d + 7*b*c))/2 + (b^6*d^9*x^{17}*(7*a*d + 10*b*c))/17 + (a^5*c^8*x^3*(45*a^2*d^2 + 21*b^2*c^2 + 70*a*b*c*d))/3 + (b^5*d^8*x^{16}*(21*a^2*d^2 + 45*b^2*c^2 + 70*a*b*c*d))/16$

sympy [B] time = 0.25, size = 1280, normalized size = 6.40

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**7*(d*x+c)**10,x)`

[Out] $a**7*c**10*x + b**7*d**10*x**18/18 + x**17*(7*a*b**6*d**10/17 + 10*b**7*c*d**9/17) + x**16*(21*a**2*b**5*d**10/16 + 35*a*b**6*c*d**9/8 + 45*b**7*c**2*d**8/16) + x**15*(7*a**3*b**4*d**10/3 + 14*a**2*b**5*c*d**9 + 21*a*b**6*c**2*d**8 + 8*b**7*c**3*d**7) + x**14*(5*a**4*b**3*d**10/2 + 25*a**3*b**4*c*d**9 + 135*a**2*b**5*c**2*d**8/2 + 60*a*b**6*c**3*d**7 + 15*b**7*c**4*d**6) + x**13*(21*a**5*b**2*d**10/13 + 350*a**4*b**3*c*d**9/13 + 1575*a**3*b**4*c**2*d**8/13 + 2520*a**2*b**5*c**3*d**7/13 + 1470*a*b**6*c**4*d**6/13 + 252*b**7*c**5*d**5/13) + x**12*(7*a**6*b*d**10/12 + 35*a**5*b**2*c*d**9/2 + 525*a**4*b**3*c**2*d**8/4 + 350*a**3*b**4*c**3*d**7 + 735*a**2*b**5*c**4*d**6/2$

$$\begin{aligned}
& + 147*a*b**6*c**5*d**5 + 35*b**7*c**6*d**4/2) + x**11*(a**7*d**10/11 + 70* \\
& a**6*b*c*d**9/11 + 945*a**5*b**2*c**2*d**8/11 + 4200*a**4*b**3*c**3*d**7/11 \\
& + 7350*a**3*b**4*c**4*d**6/11 + 5292*a**2*b**5*c**5*d**5/11 + 1470*a*b**6* \\
& c**6*d**4/11 + 120*b**7*c**7*d**3/11) + x**10*(a**7*c*d**9 + 63*a**6*b*c**2 \\
& *d**8/2 + 252*a**5*b**2*c**3*d**7 + 735*a**4*b**3*c**4*d**6 + 882*a**3*b**4 \\
& *c**5*d**5 + 441*a**2*b**5*c**6*d**4 + 84*a*b**6*c**7*d**3 + 9*b**7*c**8*d \\
& *2/2) + x**9*(5*a**7*c**2*d**8 + 280*a**6*b*c**3*d**7/3 + 490*a**5*b**2*c** \\
& 4*d**6 + 980*a**4*b**3*c**5*d**5 + 2450*a**3*b**4*c**6*d**4/3 + 280*a**2*b \\
& *5*c**7*d**3 + 35*a*b**6*c**8*d**2 + 10*b**7*c**9*d/9) + x**8*(15*a**7*c**3 \\
& *d**7 + 735*a**6*b*c**4*d**6/4 + 1323*a**5*b**2*c**5*d**5/2 + 3675*a**4*b** \\
& 3*c**6*d**4/4 + 525*a**3*b**4*c**7*d**3 + 945*a**2*b**5*c**8*d**2/8 + 35*a \\
& b**6*c**9*d/4 + b**7*c**10/8) + x**7*(30*a**7*c**4*d**6 + 252*a**6*b*c**5*d \\
& **5 + 630*a**5*b**2*c**6*d**4 + 600*a**4*b**3*c**7*d**3 + 225*a**3*b**4*c** \\
& 8*d**2 + 30*a**2*b**5*c**9*d + a*b**6*c**10) + x**6*(42*a**7*c**5*d**5 + 24 \\
& 5*a**6*b*c**6*d**4 + 420*a**5*b**2*c**7*d**3 + 525*a**4*b**3*c**8*d**2/2 + \\
& 175*a**3*b**4*c**9*d/3 + 7*a**2*b**5*c**10/2) + x**5*(42*a**7*c**6*d**4 + 1 \\
& 68*a**6*b*c**7*d**3 + 189*a**5*b**2*c**8*d**2 + 70*a**4*b**3*c**9*d + 7*a** \\
& 3*b**4*c**10) + x**4*(30*a**7*c**7*d**3 + 315*a**6*b*c**8*d**2/4 + 105*a**5 \\
& *b**2*c**9*d/2 + 35*a**4*b**3*c**10/4) + x**3*(15*a**7*c**8*d**2 + 70*a**6* \\
& b*c**9*d/3 + 7*a**5*b**2*c**10) + x**2*(5*a**7*c**9*d + 7*a**6*b*c**10/2)
\end{aligned}$$

3.1305 $\int (a + bx)^6 (c + dx)^{10} dx$

Optimal. Leaf size=170

$$-\frac{3b^5(c+dx)^{16}(bc-ad)}{8d^7} + \frac{b^4(c+dx)^{15}(bc-ad)^2}{d^7} - \frac{10b^3(c+dx)^{14}(bc-ad)^3}{7d^7} + \frac{15b^2(c+dx)^{13}(bc-ad)^4}{13d^7} - \frac{b(c+dx)^{12}(bc-ad)^5}{17d^7} + \frac{3b^5(c+dx)^{16}(bc-ad)}{8d^7} + \frac{b^4(c+dx)^{15}(bc-ad)^2}{d^7} - \frac{10b^3(c+dx)^{14}(bc-ad)^3}{7d^7} + \frac{15b^2(c+dx)^{13}(bc-ad)^4}{13d^7} - \frac{b(c+dx)^{12}(bc-ad)^5}{17d^7} + \dots$$

[Out] $1/11*(-a*d+b*c)^6*(d*x+c)^{11}/d^7 - 1/2*b*(-a*d+b*c)^5*(d*x+c)^{12}/d^7 + 15/13*b^2*(-a*d+b*c)^4*(d*x+c)^{13}/d^7 - 10/7*b^3*(-a*d+b*c)^3*(d*x+c)^{14}/d^7 + b^4*(-a*d+b*c)^2*(d*x+c)^{15}/d^7 - 3/8*b^5*(-a*d+b*c)*(d*x+c)^{16}/d^7 + 1/17*b^6*(d*x+c)^{17}/d^7$

Rubi [A] time = 0.67, antiderivative size = 170, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{3b^5(c+dx)^{16}(bc-ad)}{8d^7} + \frac{b^4(c+dx)^{15}(bc-ad)^2}{d^7} - \frac{10b^3(c+dx)^{14}(bc-ad)^3}{7d^7} + \frac{15b^2(c+dx)^{13}(bc-ad)^4}{13d^7} - \frac{b(c+dx)^{12}(bc-ad)^5}{17d^7} + \dots$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^6*(c + d*x)^10, x]

[Out] $((b*c - a*d)^6*(c + d*x)^{11})/(11*d^7) - (b*(b*c - a*d)^5*(c + d*x)^{12})/(2*d^7) + (15*b^2*(b*c - a*d)^4*(c + d*x)^{13})/(13*d^7) - (10*b^3*(b*c - a*d)^3*(c + d*x)^{14})/(7*d^7) + (b^4*(b*c - a*d)^2*(c + d*x)^{15})/d^7 - (3*b^5*(b*c - a*d)*(c + d*x)^{16})/(8*d^7) + (b^6*(c + d*x)^{17})/(17*d^7)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int (a + bx)^6 (c + dx)^{10} dx = \int \left(\frac{(-bc + ad)^6 (c + dx)^{10}}{d^6} - \frac{6b(bc - ad)^5 (c + dx)^{11}}{d^6} + \frac{15b^2(bc - ad)^4 (c + dx)^{12}}{d^6} - \frac{20b^3(bc - ad)^3 (c + dx)^{13}}{d^6} + \frac{(bc - ad)^6 (c + dx)^{11}}{11d^7} - \frac{b(bc - ad)^5 (c + dx)^{12}}{2d^7} + \frac{15b^2(bc - ad)^4 (c + dx)^{13}}{13d^7} - \frac{10b^3(bc - ad)^3 (c + dx)^{14}}{7d^7} + \frac{b^4(bc - ad)^2 (c + dx)^{15}}{d^7} - \frac{3b^5(bc - ad) (c + dx)^{16}}{8d^7} + \frac{b^6 (c + dx)^{17}}{17d^7} \right) dx$$

Mathematica [B] time = 0.12, size = 939, normalized size = 5.52

$$\frac{1}{17}b^6d^{10}x^{17} + \frac{1}{8}b^5d^9(5bc+3ad)x^{16} + b^4d^8(3b^2c^2 + 4abdc + a^2d^2)x^{15} + \frac{5}{7}b^3d^7(12b^3c^3 + 27ab^2dc^2 + 15a^2bd^2c + 2a^3d^3)x^{14} + \frac{5}{8}b^2d^6(12b^2c^2d + 27ab^2cd + 15a^2bd^2)x^{13} + \frac{5}{8}bd^5(12b^2cd^2 + 27abd^2c + 15a^2bd^2)x^{12} + \frac{5}{8}d^4(12bcd^2 + 27abd^2 + 15a^2bd^2)x^{11} + \frac{5}{8}d^3(12bcd^2 + 27abd^2 + 15a^2bd^2)x^{10} + \frac{5}{8}d^2(12bcd^2 + 27abd^2 + 15a^2bd^2)x^9 + \frac{5}{8}d(12bcd^2 + 27abd^2 + 15a^2bd^2)x^8 + \frac{5}{8}(12bcd^2 + 27abd^2 + 15a^2bd^2)x^7 + \frac{5}{8}(12bcd^2 + 27abd^2 + 15a^2bd^2)x^6 + \frac{5}{8}(12bcd^2 + 27abd^2 + 15a^2bd^2)x^5 + \frac{5}{8}(12bcd^2 + 27abd^2 + 15a^2bd^2)x^4 + \frac{5}{8}(12bcd^2 + 27abd^2 + 15a^2bd^2)x^3 + \frac{5}{8}(12bcd^2 + 27abd^2 + 15a^2bd^2)x^2 + \frac{5}{8}(12bcd^2 + 27abd^2 + 15a^2bd^2)x + \frac{5}{8}(12bcd^2 + 27abd^2 + 15a^2bd^2)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^6*(c + d*x)^10,x]

[Out] a^6*c^10*x + a^5*c^9*(3*b*c + 5*a*d)*x^2 + 5*a^4*c^8*(b^2*c^2 + 4*a*b*c*d + 3*a^2*d^2)*x^3 + (5*a^3*c^7*(2*b^3*c^3 + 15*a*b^2*c^2*d + 27*a^2*b*c*d^2 + 12*a^3*d^3)*x^4)/2 + a^2*c^6*(3*b^4*c^4 + 40*a*b^3*c^3*d + 135*a^2*b^2*c^2*d^2 + 144*a^3*b*c*d^3 + 42*a^4*d^4)*x^5 + a*c^5*(b^5*c^5 + 25*a*b^4*c^4*d + 150*a^2*b^3*c^3*d^2 + 300*a^3*b^2*c^2*d^3 + 210*a^4*b*c*d^4 + 42*a^5*d^5)*x^6 + (c^4*(b^6*c^6 + 60*a*b^5*c^5*d + 675*a^2*b^4*c^4*d^2 + 2400*a^3*b^3*c^3*d^3 + 3150*a^4*b^2*c^2*d^4 + 1512*a^5*b*c*d^5 + 210*a^6*d^6)*x^7)/7 + (5*c^3*d*(b^6*c^6 + 27*a*b^5*c^5*d + 180*a^2*b^4*c^4*d^2 + 420*a^3*b^3*c^3*d^3 + 378*a^4*b^2*c^2*d^4 + 126*a^5*b*c*d^5 + 12*a^6*d^6)*x^8)/4 + 5*c^2*d^2*(b^6*c^6 + 16*a*b^5*c^5*d + 70*a^2*b^4*c^4*d^2 + 112*a^3*b^3*c^3*d^3 + 70*a^4*b^2*c^2*d^4 + 16*a^5*b*c*d^5 + a^6*d^6)*x^9 + c*d^3*(12*b^6*c^6 + 126*a*b^5*c^5*d + 378*a^2*b^4*c^4*d^2 + 420*a^3*b^3*c^3*d^3 + 180*a^4*b^2*c^2*d^4 + 27*a^5*b*c*d^5 + a^6*d^6)*x^10 + (d^4*(210*b^6*c^6 + 1512*a*b^5*c^5*d + 3150*a^2*b^4*c^4*d^2 + 2400*a^3*b^3*c^3*d^3 + 675*a^4*b^2*c^2*d^4 + 60*a^5*b*c*d^5 + a^6*d^6)*x^11)/11 + (b*d^5*(42*b^5*c^5 + 210*a*b^4*c^4*d + 300*a^2*b^3*c^3*d^2 + 150*a^3*b^2*c^2*d^3 + 25*a^4*b*c*d^4 + a^5*d^5)*x^12)/2 + (5*b^2*d^6*(42*b^4*c^4 + 144*a*b^3*c^3*d + 135*a^2*b^2*c^2*d^2 + 40*a^3*b*c*d^3 + 3*a^4*d^4)*x^13)/13 + (5*b^3*d^7*(12*b^3*c^3 + 27*a*b^2*c^2*d + 15*a^2*b*c*d^2 + 2*a^3*d^3)*x^14)/7 + b^4*d^8*(3*b^2*c^2 + 4*a*b*c*d + a^2*d^2)*x^15 + (b^5*d^9*(5*b*c + 3*a*d)*x^16)/8 + (b^6*d^10*x^17)/17

fricas [B] time = 0.39, size = 1124, normalized size = 6.61

$$\frac{1}{17}x^{17}d^{10}b^6 + \frac{5}{8}x^{16}d^9cb^6 + \frac{3}{8}x^{16}d^{10}b^5a + 3x^{15}d^8c^2b^6 + 4x^{15}d^9cb^5a + x^{15}d^{10}b^4a^2 + \frac{60}{7}x^{14}d^7c^3b^6 + \frac{135}{7}x^{14}d^8c^2b^5a + \frac{75}{7}x^{14}d^9cb^4a^2 + \frac{10}{7}x^{14}d^{10}b^3a^3 + \frac{210}{13}x^{13}d^6c^4b^6 + \frac{720}{13}x^{13}d^7c^3b^5a + \frac{675}{13}x^{13}d^8c^2b^4a^2 + \frac{200}{13}x^{13}d^9c^2b^3a^3 + \frac{15}{13}x^{13}d^{10}b^2a^4 + 21x^{12}d^5c^5b^6 + 105x^{12}d^6c^4b^5a + 150x^{12}d^7c^3b^4a^2 + 75x^{12}d^8c^2b^3a^3 + 25/2x^{12}d^9c^2b^2a^4 + 1/2x^{12}d^{10}b^2a^5 + 210/11x^{11}d^4c^6b^6 + 1512/11x^{11}d^5c^5b^5a + 3150/11x^{11}d^6c^4b^4a^2 + 210/11x^{11}d^7c^3b^3a^3 + 105/11x^{11}d^8c^2b^2a^4 + 21/11x^{11}d^9cb^2a^5 + 210/11x^{11}d^{10}b^2a^6 + 105/11x^{10}d^5c^5b^5a + 1050/11x^{10}d^6c^4b^4a^2 + 1050/11x^{10}d^7c^3b^3a^3 + 1050/11x^{10}d^8c^2b^2a^4 + 1050/11x^{10}d^9cb^2a^5 + 1050/11x^{10}d^{10}b^2a^6 + 1050/11x^9d^4c^6b^6 + 1050/11x^9d^5c^5b^5a + 1050/11x^9d^6c^4b^4a^2 + 1050/11x^9d^7c^3b^3a^3 + 1050/11x^9d^8c^2b^2a^4 + 1050/11x^9d^9cb^2a^5 + 1050/11x^9d^{10}b^2a^6 + 1050/11x^8d^4c^6b^6 + 1050/11x^8d^5c^5b^5a + 1050/11x^8d^6c^4b^4a^2 + 1050/11x^8d^7c^3b^3a^3 + 1050/11x^8d^8c^2b^2a^4 + 1050/11x^8d^9cb^2a^5 + 1050/11x^8d^{10}b^2a^6 + 1050/11x^7d^4c^6b^6 + 1050/11x^7d^5c^5b^5a + 1050/11x^7d^6c^4b^4a^2 + 1050/11x^7d^7c^3b^3a^3 + 1050/11x^7d^8c^2b^2a^4 + 1050/11x^7d^9cb^2a^5 + 1050/11x^7d^{10}b^2a^6 + 1050/11x^6d^4c^6b^6 + 1050/11x^6d^5c^5b^5a + 1050/11x^6d^6c^4b^4a^2 + 1050/11x^6d^7c^3b^3a^3 + 1050/11x^6d^8c^2b^2a^4 + 1050/11x^6d^9cb^2a^5 + 1050/11x^6d^{10}b^2a^6 + 1050/11x^5d^4c^6b^6 + 1050/11x^5d^5c^5b^5a + 1050/11x^5d^6c^4b^4a^2 + 1050/11x^5d^7c^3b^3a^3 + 1050/11x^5d^8c^2b^2a^4 + 1050/11x^5d^9cb^2a^5 + 1050/11x^5d^{10}b^2a^6 + 1050/11x^4d^4c^6b^6 + 1050/11x^4d^5c^5b^5a + 1050/11x^4d^6c^4b^4a^2 + 1050/11x^4d^7c^3b^3a^3 + 1050/11x^4d^8c^2b^2a^4 + 1050/11x^4d^9cb^2a^5 + 1050/11x^4d^{10}b^2a^6 + 1050/11x^3d^4c^6b^6 + 1050/11x^3d^5c^5b^5a + 1050/11x^3d^6c^4b^4a^2 + 1050/11x^3d^7c^3b^3a^3 + 1050/11x^3d^8c^2b^2a^4 + 1050/11x^3d^9cb^2a^5 + 1050/11x^3d^{10}b^2a^6 + 1050/11x^2d^4c^6b^6 + 1050/11x^2d^5c^5b^5a + 1050/11x^2d^6c^4b^4a^2 + 1050/11x^2d^7c^3b^3a^3 + 1050/11x^2d^8c^2b^2a^4 + 1050/11x^2d^9cb^2a^5 + 1050/11x^2d^{10}b^2a^6 + 1050/11xd^4c^6b^6 + 1050/11xd^5c^5b^5a + 1050/11xd^6c^4b^4a^2 + 1050/11xd^7c^3b^3a^3 + 1050/11xd^8c^2b^2a^4 + 1050/11xd^9cb^2a^5 + 1050/11xd^{10}b^2a^6 + 1050/11d^4c^6b^6 + 1050/11d^5c^5b^5a + 1050/11d^6c^4b^4a^2 + 1050/11d^7c^3b^3a^3 + 1050/11d^8c^2b^2a^4 + 1050/11d^9cb^2a^5 + 1050/11d^{10}b^2a^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6*(d*x+c)^10,x, algorithm="fricas")

[Out] 1/17*x^17*d^10*b^6 + 5/8*x^16*d^9*c*b^6 + 3/8*x^16*d^10*b^5*a + 3*x^15*d^8*c^2*b^6 + 4*x^15*d^9*c*b^5*a + x^15*d^10*b^4*a^2 + 60/7*x^14*d^7*c^3*b^6 + 135/7*x^14*d^8*c^2*b^5*a + 75/7*x^14*d^9*c*b^4*a^2 + 10/7*x^14*d^10*b^3*a^3 + 210/13*x^13*d^6*c^4*b^6 + 720/13*x^13*d^7*c^3*b^5*a + 675/13*x^13*d^8*c^2*b^4*a^2 + 200/13*x^13*d^9*c*b^3*a^3 + 15/13*x^13*d^10*b^2*a^4 + 21*x^12*d^5*c^5*b^6 + 105*x^12*d^6*c^4*b^5*a + 150*x^12*d^7*c^3*b^4*a^2 + 75*x^12*d^8*c^2*b^3*a^3 + 25/2*x^12*d^9*c*b^2*a^4 + 1/2*x^12*d^10*b*a^5 + 210/11*x^11*d^4*c^6*b^6 + 1512/11*x^11*d^5*c^5*b^5*a + 3150/11*x^11*d^6*c^4*b^4*a^2 + 210/11*x^11*d^7*c^3*b^3*a^3 + 105/11*x^11*d^8*c^2*b^2*a^4 + 21/11*x^11*d^9*c*b^2*a^5 + 210/11*x^11*d^10*b^2*a^6 + 105/11*x^10*d^5*c^5*b^5*a + 1050/11*x^10*d^6*c^4*b^4*a^2 + 1050/11*x^10*d^7*c^3*b^3*a^3 + 1050/11*x^10*d^8*c^2*b^2*a^4 + 1050/11*x^10*d^9*c*b^2*a^5 + 1050/11*x^10*d^10*b^2*a^6 + 1050/11*x^9*d^4*c^6*b^6 + 1050/11*x^9*d^5*c^5*b^5*a + 1050/11*x^9*d^6*c^4*b^4*a^2 + 1050/11*x^9*d^7*c^3*b^3*a^3 + 1050/11*x^9*d^8*c^2*b^2*a^4 + 1050/11*x^9*d^9*c*b^2*a^5 + 1050/11*x^9*d^10*b^2*a^6 + 1050/11*x^8*d^4*c^6*b^6 + 1050/11*x^8*d^5*c^5*b^5*a + 1050/11*x^8*d^6*c^4*b^4*a^2 + 1050/11*x^8*d^7*c^3*b^3*a^3 + 1050/11*x^8*d^8*c^2*b^2*a^4 + 1050/11*x^8*d^9*c*b^2*a^5 + 1050/11*x^8*d^10*b^2*a^6 + 1050/11*x^7*d^4*c^6*b^6 + 1050/11*x^7*d^5*c^5*b^5*a + 1050/11*x^7*d^6*c^4*b^4*a^2 + 1050/11*x^7*d^7*c^3*b^3*a^3 + 1050/11*x^7*d^8*c^2*b^2*a^4 + 1050/11*x^7*d^9*c*b^2*a^5 + 1050/11*x^7*d^10*b^2*a^6 + 1050/11*x^6*d^4*c^6*b^6 + 1050/11*x^6*d^5*c^5*b^5*a + 1050/11*x^6*d^6*c^4*b^4*a^2 + 1050/11*x^6*d^7*c^3*b^3*a^3 + 1050/11*x^6*d^8*c^2*b^2*a^4 + 1050/11*x^6*d^9*c*b^2*a^5 + 1050/11*x^6*d^10*b^2*a^6 + 1050/11*x^5*d^4*c^6*b^6 + 1050/11*x^5*d^5*c^5*b^5*a + 1050/11*x^5*d^6*c^4*b^4*a^2 + 1050/11*x^5*d^7*c^3*b^3*a^3 + 1050/11*x^5*d^8*c^2*b^2*a^4 + 1050/11*x^5*d^9*c*b^2*a^5 + 1050/11*x^5*d^10*b^2*a^6 + 1050/11*x^4*d^4*c^6*b^6 + 1050/11*x^4*d^5*c^5*b^5*a + 1050/11*x^4*d^6*c^4*b^4*a^2 + 1050/11*x^4*d^7*c^3*b^3*a^3 + 1050/11*x^4*d^8*c^2*b^2*a^4 + 1050/11*x^4*d^9*c*b^2*a^5 + 1050/11*x^4*d^10*b^2*a^6 + 1050/11*x^3*d^4*c^6*b^6 + 1050/11*x^3*d^5*c^5*b^5*a + 1050/11*x^3*d^6*c^4*b^4*a^2 + 1050/11*x^3*d^7*c^3*b^3*a^3 + 1050/11*x^3*d^8*c^2*b^2*a^4 + 1050/11*x^3*d^9*c*b^2*a^5 + 1050/11*x^3*d^10*b^2*a^6 + 1050/11*x^2*d^4*c^6*b^6 + 1050/11*x^2*d^5*c^5*b^5*a + 1050/11*x^2*d^6*c^4*b^4*a^2 + 1050/11*x^2*d^7*c^3*b^3*a^3 + 1050/11*x^2*d^8*c^2*b^2*a^4 + 1050/11*x^2*d^9*c*b^2*a^5 + 1050/11*x^2*d^10*b^2*a^6 + 1050/11*x*d^4*c^6*b^6 + 1050/11*x*d^5*c^5*b^5*a + 1050/11*x*d^6*c^4*b^4*a^2 + 1050/11*x*d^7*c^3*b^3*a^3 + 1050/11*x*d^8*c^2*b^2*a^4 + 1050/11*x*d^9*c*b^2*a^5 + 1050/11*x*d^10*b^2*a^6 + 1050/11*d^4*c^6*b^6 + 1050/11*d^5*c^5*b^5*a + 1050/11*d^6*c^4*b^4*a^2 + 1050/11*d^7*c^3*b^3*a^3 + 1050/11*d^8*c^2*b^2*a^4 + 1050/11*d^9*c*b^2*a^5 + 1050/11*d^10*b^2*a^6

$2400/11*x^{11}*d^7*c^3*b^3*a^3 + 675/11*x^{11}*d^8*c^2*b^2*a^4 + 60/11*x^{11}*d^9*c*b*a^5 + 1/11*x^{11}*d^{10}*a^6 + 12*x^{10}*d^3*c^7*b^6 + 126*x^{10}*d^4*c^6*b^5*a + 378*x^{10}*d^5*c^5*b^4*a^2 + 420*x^{10}*d^6*c^4*b^3*a^3 + 180*x^{10}*d^7*c^3*b^2*a^4 + 27*x^{10}*d^8*c^2*b*a^5 + x^{10}*d^9*c*a^6 + 5*x^9*d^2*c^8*b^6 + 80*x^9*d^3*c^7*b^5*a + 350*x^9*d^4*c^6*b^4*a^2 + 560*x^9*d^5*c^5*b^3*a^3 + 350*x^9*d^6*c^4*b^2*a^4 + 80*x^9*d^7*c^3*b*a^5 + 5*x^9*d^8*c^2*a^6 + 5/4*x^8*d*c^9*b^6 + 135/4*x^8*d^2*c^8*b^5*a + 225*x^8*d^3*c^7*b^4*a^2 + 525*x^8*d^4*c^6*b^3*a^3 + 945/2*x^8*d^5*c^5*b^2*a^4 + 315/2*x^8*d^6*c^4*b*a^5 + 15*x^8*d^7*c^3*a^6 + 1/7*x^7*c^10*b^6 + 60/7*x^7*d*c^9*b^5*a + 675/7*x^7*d^2*c^8*b^4*a^2 + 2400/7*x^7*d^3*c^7*b^3*a^3 + 450*x^7*d^4*c^6*b^2*a^4 + 216*x^7*d^5*c^5*b*a^5 + 30*x^7*d^6*c^4*a^6 + x^6*c^10*b^5*a + 25*x^6*d*c^9*b^4*a^2 + 150*x^6*d^2*c^8*b^3*a^3 + 300*x^6*d^3*c^7*b^2*a^4 + 210*x^6*d^4*c^6*b*a^5 + 42*x^6*d^5*c^5*a^6 + 3*x^5*c^10*b^4*a^2 + 40*x^5*d*c^9*b^3*a^3 + 135*x^5*d^2*c^8*b^2*a^4 + 144*x^5*d^3*c^7*b*a^5 + 42*x^5*d^4*c^6*a^6 + 5*x^4*c^10*b^3*a^3 + 75/2*x^4*d*c^9*b^2*a^4 + 135/2*x^4*d^2*c^8*b*a^5 + 30*x^4*d^3*c^7*a^6 + 5*x^3*c^10*b^2*a^4 + 20*x^3*d*c^9*b*a^5 + 15*x^3*d^2*c^8*a^6 + 3*x^2*c^10*b*a^5 + 5*x^2*d*c^9*a^6 + x*c^10*a^6$

giac [B] time = 1.30, size = 1124, normalized size = 6.61

$$\frac{1}{17} b^6 d^{10} x^{17} + \frac{5}{8} b^6 c d^9 x^{16} + \frac{3}{8} a b^5 d^{10} x^{16} + 3 b^6 c^2 d^8 x^{15} + 4 a b^5 c d^9 x^{15} + a^2 b^4 d^{10} x^{15} + \frac{60}{7} b^6 c^3 d^7 x^{14} + \frac{135}{7} a b^5 c^2 d^8 x^{14} + \frac{75}{7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6*(d*x+c)^10,x, algorithm="giac")

[Out] $1/17*b^6*d^{10}*x^{17} + 5/8*b^6*c*d^9*x^{16} + 3/8*a*b^5*d^{10}*x^{16} + 3*b^6*c^2*d^8*x^{15} + 4*a*b^5*c*d^9*x^{15} + a^2*b^4*d^{10}*x^{15} + 60/7*b^6*c^3*d^7*x^{14} + 135/7*a*b^5*c^2*d^8*x^{14} + 75/7*a^2*b^4*c*d^9*x^{14} + 10/7*a^3*b^3*d^{10}*x^{14} + 210/13*b^6*c^4*d^6*x^{13} + 720/13*a*b^5*c^3*d^7*x^{13} + 675/13*a^2*b^4*c^2*d^8*x^{13} + 200/13*a^3*b^3*c*d^9*x^{13} + 15/13*a^4*b^2*d^{10}*x^{13} + 21*b^6*c^5*d^5*x^{12} + 105*a*b^5*c^4*d^6*x^{12} + 150*a^2*b^4*c^3*d^7*x^{12} + 75*a^3*b^3*c^2*d^8*x^{12} + 25/2*a^4*b^2*c*d^9*x^{12} + 1/2*a^5*b*d^{10}*x^{12} + 210/11*b^6*c^6*d^4*x^{11} + 1512/11*a*b^5*c^5*d^5*x^{11} + 3150/11*a^2*b^4*c^4*d^6*x^{11} + 2400/11*a^3*b^3*c^3*d^7*x^{11} + 675/11*a^4*b^2*c^2*d^8*x^{11} + 60/11*a^5*b*c*d^9*x^{11} + 1/11*a^6*d^{10}*x^{11} + 12*b^6*c^7*d^3*x^{10} + 126*a*b^5*c^6*d^4*x^{10} + 378*a^2*b^4*c^5*d^5*x^{10} + 420*a^3*b^3*c^4*d^6*x^{10} + 180*a^4*b^2*c^3*d^7*x^{10} + 27*a^5*b*c^2*d^8*x^{10} + a^6*c*d^9*x^{10} + 5*b^6*c^8*d^2*x^9 + 80*a*b^5*c^7*d^3*x^9 + 350*a^2*b^4*c^6*d^4*x^9 + 560*a^3*b^3*c^5*d^5*x^9 + 350*a^4*b^2*c^4*d^6*x^9 + 80*a^5*b*c^3*d^7*x^9 + 5*a^6*c^2*d^8*x^9 + 5/4*b^6*c^9*d*x^8 + 135/4*a*b^5*c^8*d^2*x^8 + 225*a^2*b^4*c^7*d^3*x^8 + 525*a^3*b^3*c^6*d^4*x^8 + 945/2*a^4*b^2*c^5*d^5*x^8 + 315/2*a^5*b*c^4*d^6*x^8 + 15*a^6*c^3*d^7*x^8 + 1/7*b^6*c^10*x^7 + 60/7*a*b^5*c^9*d*x^7 + 675/7*a^2*b^4*c^8*d^2*x^7 + 2400/7*a^3*b^3*c^7*d^3*x^7 + 450*a^4*b^2*c^6*d^4*x^7 + 216*a^5*b*c^5*d^5*x^7 + 30*a^6*c^4*d^6*x^7 + a*b^5*c^10*x^6 + 25*a^2*b^4*c^9*d*x^6 + 15$

$$0*a^3*b^3*c^8*d^2*x^6 + 300*a^4*b^2*c^7*d^3*x^6 + 210*a^5*b*c^6*d^4*x^6 + 42*a^6*c^5*d^5*x^6 + 3*a^2*b^4*c^10*x^5 + 40*a^3*b^3*c^9*d*x^5 + 135*a^4*b^2*c^8*d^2*x^5 + 144*a^5*b*c^7*d^3*x^5 + 42*a^6*c^6*d^4*x^5 + 5*a^3*b^3*c^10*x^4 + 75/2*a^4*b^2*c^9*d*x^4 + 135/2*a^5*b*c^8*d^2*x^4 + 30*a^6*c^7*d^3*x^4 + 5*a^4*b^2*c^10*x^3 + 20*a^5*b*c^9*d*x^3 + 15*a^6*c^8*d^2*x^3 + 3*a^5*b*c^10*x^2 + 5*a^6*c^9*d*x^2 + a^6*c^10*x$$

maple [B] time = 0.00, size = 991, normalized size = 5.83

$$\frac{b^6 d^{10} x^{17}}{17} + a^6 c^{10} x + \frac{(6a b^5 d^{10} + 10b^6 c d^9) x^{16}}{16} + \frac{(15a^2 b^4 d^{10} + 60a b^5 c d^9 + 45b^6 c^2 d^8) x^{15}}{15} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^{14}}{14} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^{13}}{13} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^{12}}{12} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^{11}}{11} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^{10}}{10} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^9}{9} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^8}{8} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^7}{7} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^6}{6} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^5}{5} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^4}{4} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^3}{3} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x^2}{2} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10}) x}{1} + \frac{(20a^3 b^3 d^{10} + 150a^2 b^4 c d^9 + 450a b^5 c^2 d^8 + 15a^6 c^{10})}{0}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^6*(d*x+c)^10,x)

[Out] 1/17*b^6*d^10*x^17+1/16*(6*a*b^5*d^10+10*b^6*c*d^9)*x^16+1/15*(15*a^2*b^4*d^10+60*a*b^5*c*d^9+45*b^6*c^2*d^8)*x^15+1/14*(20*a^3*b^3*d^10+150*a^2*b^4*c*d^9+270*a*b^5*c^2*d^8+120*b^6*c^3*d^7)*x^14+1/13*(15*a^4*b^2*d^10+200*a^3*b^3*c*d^9+675*a^2*b^4*c^2*d^8+720*a*b^5*c^3*d^7+210*b^6*c^4*d^6)*x^13+1/12*(6*a^5*b*d^10+150*a^4*b^2*c*d^9+900*a^3*b^3*c^2*d^8+1800*a^2*b^4*c^3*d^7+1260*a*b^5*c^4*d^6+252*b^6*c^5*d^5)*x^12+1/11*(a^6*d^10+60*a^5*b*c*d^9+675*a^4*b^2*c^2*d^8+2400*a^3*b^3*c^3*d^7+3150*a^2*b^4*c^4*d^6+1512*a*b^5*c^5*d^5+210*b^6*c^6*d^4)*x^11+1/10*(10*a^6*c*d^9+270*a^5*b*c^2*d^8+1800*a^4*b^2*c^3*d^7+4200*a^3*b^3*c^4*d^6+3780*a^2*b^4*c^5*d^5+1260*a*b^5*c^6*d^4+120*b^6*c^7*d^3)*x^10+1/9*(45*a^6*c^2*d^8+720*a^5*b*c^3*d^7+3150*a^4*b^2*c^4*d^6+5040*a^3*b^3*c^5*d^5+3150*a^2*b^4*c^6*d^4+720*a*b^5*c^7*d^3+45*b^6*c^8*d^2)*x^9+1/8*(120*a^6*c^3*d^7+1260*a^5*b*c^4*d^6+3780*a^4*b^2*c^5*d^5+4200*a^3*b^3*c^6*d^4+1800*a^2*b^4*c^7*d^3+270*a*b^5*c^8*d^2+10*b^6*c^9*d)*x^8+1/7*(210*a^6*c^4*d^6+1512*a^5*b*c^5*d^5+3150*a^4*b^2*c^6*d^4+2400*a^3*b^3*c^7*d^3+675*a^2*b^4*c^8*d^2+60*a*b^5*c^9*d+b^6*c^10)*x^7+1/6*(252*a^6*c^5*d^5+1260*a^5*b*c^6*d^4+1800*a^4*b^2*c^7*d^3+900*a^3*b^3*c^8*d^2+150*a^2*b^4*c^9*d+6*a*b^5*c^10)*x^6+1/5*(210*a^6*c^6*d^4+720*a^5*b*c^7*d^3+675*a^4*b^2*c^8*d^2+200*a^3*b^3*c^9*d+15*a^2*b^4*c^10)*x^5+1/4*(120*a^6*c^7*d^3+270*a^5*b*c^8*d^2+150*a^4*b^2*c^9*d+20*a^3*b^3*c^10)*x^4+1/3*(45*a^6*c^8*d^2+60*a^5*b*c^9*d+15*a^4*b^2*c^10)*x^3+1/2*(10*a^6*c^9*d+6*a^5*b*c^10)*x^2+a^6*c^10*x

maxima [B] time = 1.44, size = 977, normalized size = 5.75

$$\frac{1}{17} b^6 d^{10} x^{17} + a^6 c^{10} x + \frac{1}{8} (5 b^6 c d^9 + 3 a b^5 d^{10}) x^{16} + (3 b^6 c^2 d^8 + 4 a b^5 c d^9 + a^2 b^4 d^{10}) x^{15} + \frac{5}{7} (12 b^6 c^3 d^7 + 27 a b^5 c^2 d^8 + 15 a^2 b^4 c d^9 + 6 a^3 b^3 d^{10}) x^{14} + \frac{5}{6} (15 a^4 b^2 d^{10} + 200 a^3 b^3 c d^9 + 675 a^2 b^4 c^2 d^8 + 720 a b^5 c^3 d^7 + 210 b^6 c^4 d^6) x^{13} + \frac{5}{5} (15 a^5 b d^{10} + 150 a^4 b^2 c d^9 + 900 a^3 b^3 c^2 d^8 + 1800 a^2 b^4 c^3 d^7 + 1260 a b^5 c^4 d^6 + 252 b^6 c^5 d^5) x^{12} + \frac{5}{4} (a^6 d^{10} + 60 a^5 b c d^9 + 675 a^4 b^2 c^2 d^8 + 2400 a^3 b^3 c^3 d^7 + 3150 a^2 b^4 c^4 d^6 + 1512 a b^5 c^5 d^5 + 210 b^6 c^6 d^4) x^{11} + \frac{5}{3} (10 a^6 c d^9 + 270 a^5 b c^2 d^8 + 1800 a^4 b^2 c^3 d^7 + 4200 a^3 b^3 c^4 d^6 + 3780 a^2 b^4 c^5 d^5 + 1260 a b^5 c^6 d^4 + 120 b^6 c^7 d^3) x^{10} + \frac{5}{2} (45 a^6 c^2 d^8 + 720 a^5 b c^3 d^7 + 3150 a^4 b^2 c^4 d^6 + 5040 a^3 b^3 c^5 d^5 + 3150 a^2 b^4 c^6 d^4 + 720 a b^5 c^7 d^3 + 45 b^6 c^8 d^2) x^9 + \frac{5}{1} (120 a^6 c^3 d^7 + 1260 a^5 b c^4 d^6 + 3780 a^4 b^2 c^5 d^5 + 4200 a^3 b^3 c^6 d^4 + 1800 a^2 b^4 c^7 d^3 + 270 a b^5 c^8 d^2 + 10 b^6 c^9 d) x^8 + \frac{5}{0} (210 a^6 c^4 d^6 + 1512 a^5 b c^5 d^5 + 3150 a^4 b^2 c^6 d^4 + 2400 a^3 b^3 c^7 d^3 + 675 a^2 b^4 c^8 d^2 + 60 a b^5 c^9 d + b^6 c^{10}) x^7 + \frac{5}{-1} (252 a^6 c^5 d^5 + 1260 a^5 b c^6 d^4 + 1800 a^4 b^2 c^7 d^3 + 900 a^3 b^3 c^8 d^2 + 150 a^2 b^4 c^9 d + 6 a b^5 c^{10}) x^6 + \frac{5}{-2} (210 a^6 c^6 d^4 + 720 a^5 b c^7 d^3 + 675 a^4 b^2 c^8 d^2 + 200 a^3 b^3 c^9 d + 15 a^2 b^4 c^{10}) x^5 + \frac{5}{-3} (120 a^6 c^7 d^3 + 270 a^5 b c^8 d^2 + 150 a^4 b^2 c^9 d + 20 a^3 b^3 c^{10}) x^4 + \frac{5}{-4} (45 a^6 c^8 d^2 + 60 a^5 b c^9 d + 15 a^4 b^2 c^{10}) x^3 + \frac{5}{-5} (10 a^6 c^9 d + 6 a^5 b c^{10}) x^2 + \frac{5}{-6} a^6 c^{10} x + \frac{5}{-7} a^6 c^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6*(d*x+c)^10,x, algorithm="maxima")

```
[Out] 1/17*b^6*d^10*x^17 + a^6*c^10*x + 1/8*(5*b^6*c*d^9 + 3*a*b^5*d^10)*x^16 + (
3*b^6*c^2*d^8 + 4*a*b^5*c*d^9 + a^2*b^4*d^10)*x^15 + 5/7*(12*b^6*c^3*d^7 +
27*a*b^5*c^2*d^8 + 15*a^2*b^4*c*d^9 + 2*a^3*b^3*d^10)*x^14 + 5/13*(42*b^6*c
^4*d^6 + 144*a*b^5*c^3*d^7 + 135*a^2*b^4*c^2*d^8 + 40*a^3*b^3*c*d^9 + 3*a^4
*b^2*d^10)*x^13 + 1/2*(42*b^6*c^5*d^5 + 210*a*b^5*c^4*d^6 + 300*a^2*b^4*c^3
*d^7 + 150*a^3*b^3*c^2*d^8 + 25*a^4*b^2*c*d^9 + a^5*b*d^10)*x^12 + 1/11*(21
0*b^6*c^6*d^4 + 1512*a*b^5*c^5*d^5 + 3150*a^2*b^4*c^4*d^6 + 2400*a^3*b^3*c^
3*d^7 + 675*a^4*b^2*c^2*d^8 + 60*a^5*b*c*d^9 + a^6*d^10)*x^11 + (12*b^6*c^7
*d^3 + 126*a*b^5*c^6*d^4 + 378*a^2*b^4*c^5*d^5 + 420*a^3*b^3*c^4*d^6 + 180*
a^4*b^2*c^3*d^7 + 27*a^5*b*c^2*d^8 + a^6*c*d^9)*x^10 + 5*(b^6*c^8*d^2 + 16*
a*b^5*c^7*d^3 + 70*a^2*b^4*c^6*d^4 + 112*a^3*b^3*c^5*d^5 + 70*a^4*b^2*c^4*d
^6 + 16*a^5*b*c^3*d^7 + a^6*c^2*d^8)*x^9 + 5/4*(b^6*c^9*d + 27*a*b^5*c^8*d^
2 + 180*a^2*b^4*c^7*d^3 + 420*a^3*b^3*c^6*d^4 + 378*a^4*b^2*c^5*d^5 + 126*a
^5*b*c^4*d^6 + 12*a^6*c^3*d^7)*x^8 + 1/7*(b^6*c^10 + 60*a*b^5*c^9*d + 675*a
^2*b^4*c^8*d^2 + 2400*a^3*b^3*c^7*d^3 + 3150*a^4*b^2*c^6*d^4 + 1512*a^5*b*c
^5*d^5 + 210*a^6*c^4*d^6)*x^7 + (a*b^5*c^10 + 25*a^2*b^4*c^9*d + 150*a^3*b^
3*c^8*d^2 + 300*a^4*b^2*c^7*d^3 + 210*a^5*b*c^6*d^4 + 42*a^6*c^5*d^5)*x^6 +
(3*a^2*b^4*c^10 + 40*a^3*b^3*c^9*d + 135*a^4*b^2*c^8*d^2 + 144*a^5*b*c^7*d
^3 + 42*a^6*c^6*d^4)*x^5 + 5/2*(2*a^3*b^3*c^10 + 15*a^4*b^2*c^9*d + 27*a^5*
b*c^8*d^2 + 12*a^6*c^7*d^3)*x^4 + 5*(a^4*b^2*c^10 + 4*a^5*b*c^9*d + 3*a^6*c
^8*d^2)*x^3 + (3*a^5*b*c^10 + 5*a^6*c^9*d)*x^2
```

mupad [B] time = 0.53, size = 953, normalized size = 5.61

$$x^7 \left(30 a^6 c^4 d^6 + 216 a^5 b c^5 d^5 + 450 a^4 b^2 c^6 d^4 + \frac{2400 a^3 b^3 c^7 d^3}{7} + \frac{675 a^2 b^4 c^8 d^2}{7} + \frac{60 a b^5 c^9 d}{7} + \frac{b^6 c^{10}}{7} \right) + x^{11}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^6*(c + d*x)^10,x)
```

```
[Out] x^7*((b^6*c^10)/7 + 30*a^6*c^4*d^6 + 216*a^5*b*c^5*d^5 + (675*a^2*b^4*c^8*d
^2)/7 + (2400*a^3*b^3*c^7*d^3)/7 + 450*a^4*b^2*c^6*d^4 + (60*a*b^5*c^9*d)/7
) + x^11*((a^6*d^10)/11 + (210*b^6*c^6*d^4)/11 + (1512*a*b^5*c^5*d^5)/11 +
(3150*a^2*b^4*c^4*d^6)/11 + (2400*a^3*b^3*c^3*d^7)/11 + (675*a^4*b^2*c^2*d^
8)/11 + (60*a^5*b*c*d^9)/11) + x^9*(5*a^6*c^2*d^8 + 5*b^6*c^8*d^2 + 80*a*b^
5*c^7*d^3 + 80*a^5*b*c^3*d^7 + 350*a^2*b^4*c^6*d^4 + 560*a^3*b^3*c^5*d^5 +
350*a^4*b^2*c^4*d^6) + x^5*(3*a^2*b^4*c^10 + 42*a^6*c^6*d^4 + 40*a^3*b^3*c^
9*d + 144*a^5*b*c^7*d^3 + 135*a^4*b^2*c^8*d^2) + x^13*((15*a^4*b^2*d^10)/13
+ (210*b^6*c^4*d^6)/13 + (720*a*b^5*c^3*d^7)/13 + (200*a^3*b^3*c*d^9)/13 +
(675*a^2*b^4*c^2*d^8)/13) + x^6*(a*b^5*c^10 + 42*a^6*c^5*d^5 + 25*a^2*b^4*
c^9*d + 210*a^5*b*c^6*d^4 + 150*a^3*b^3*c^8*d^2 + 300*a^4*b^2*c^7*d^3) + x^
12*((a^5*b*d^10)/2 + 21*b^6*c^5*d^5 + 105*a*b^5*c^4*d^6 + (25*a^4*b^2*c*d^9
)/2 + 150*a^2*b^4*c^3*d^7 + 75*a^3*b^3*c^2*d^8) + x^10*(a^6*c*d^9 + 12*b^6*
c^7*d^3 + 126*a*b^5*c^6*d^4 + 27*a^5*b*c^2*d^8 + 378*a^2*b^4*c^5*d^5 + 420*
```

$$a^3b^3c^4d^6 + 180a^4b^2c^3d^7) + x^8((5b^6c^9d)/4 + 15a^6c^3d^7 + (135ab^5c^8d^2)/4 + (315a^5b^4c^6d^6)/2 + 225a^2b^4c^7d^3 + 525a^3b^3c^6d^4 + (945a^4b^2c^5d^5)/2) + a^6c^{10}x + (b^6d^{10}x^{17})/17 + (5a^3c^7x^4(12a^3d^3 + 2b^3c^3 + 15ab^2c^2d + 27a^2b^2c^2d^2))/2 + (5b^3d^7x^{14}(2a^3d^3 + 12b^3c^3 + 27ab^2c^2d + 15a^2b^2c^2d^2))/7 + a^5c^9x^2(5ad + 3bc) + (b^5d^9x^{16}(3ad + 5bc))/8 + 5a^4c^8x^3(3a^2d^2 + b^2c^2 + 4ab^2cd) + b^4d^8x^{15}(a^2d^2 + 3b^2c^2 + 4ab^2cd)$$

sympy [B] time = 0.23, size = 1088, normalized size = 6.40

$$a^6c^{10}x + \frac{b^6d^{10}x^{17}}{17} + x^{16}\left(\frac{3ab^5d^{10}}{8} + \frac{5b^6cd^9}{8}\right) + x^{15}(a^2b^4d^{10} + 4ab^5cd^9 + 3b^6c^2d^8) + x^{14}\left(\frac{10a^3b^3d^{10}}{7} + \frac{75a^2b^4cd^9}{7} + \dots\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**6*(d*x+c)**10,x)

[Out] a**6*c**10*x + b**6*d**10*x**17/17 + x**16*(3*a*b**5*d**10/8 + 5*b**6*c*d**9/8) + x**15*(a**2*b**4*d**10 + 4*a*b**5*c*d**9 + 3*b**6*c**2*d**8) + x**14*(10*a**3*b**3*d**10/7 + 75*a**2*b**4*c*d**9/7 + 135*a*b**5*c**2*d**8/7 + 60*b**6*c**3*d**7/7) + x**13*(15*a**4*b**2*d**10/13 + 200*a**3*b**3*c*d**9/13 + 675*a**2*b**4*c**2*d**8/13 + 720*a*b**5*c**3*d**7/13 + 210*b**6*c**4*d**6/13) + x**12*(a**5*b*d**10/2 + 25*a**4*b**2*c*d**9/2 + 75*a**3*b**3*c**2*d**8 + 150*a**2*b**4*c**3*d**7 + 105*a*b**5*c**4*d**6 + 21*b**6*c**5*d**5) + x**11*(a**6*d**10/11 + 60*a**5*b*c*d**9/11 + 675*a**4*b**2*c**2*d**8/11 + 2400*a**3*b**3*c**3*d**7/11 + 3150*a**2*b**4*c**4*d**6/11 + 1512*a*b**5*c**5*d**5/11 + 210*b**6*c**6*d**4/11) + x**10*(a**6*c*d**9 + 27*a**5*b*c**2*d**8 + 180*a**4*b**2*c**3*d**7 + 420*a**3*b**3*c**4*d**6 + 378*a**2*b**4*c**5*d**5 + 126*a*b**5*c**6*d**4 + 12*b**6*c**7*d**3) + x**9*(5*a**6*c**2*d**8 + 80*a**5*b*c**3*d**7 + 350*a**4*b**2*c**4*d**6 + 560*a**3*b**3*c**5*d**5 + 350*a**2*b**4*c**6*d**4 + 80*a*b**5*c**7*d**3 + 5*b**6*c**8*d**2) + x**8*(15*a**6*c**3*d**7 + 315*a**5*b*c**4*d**6/2 + 945*a**4*b**2*c**5*d**5/2 + 525*a**3*b**3*c**6*d**4 + 225*a**2*b**4*c**7*d**3 + 135*a*b**5*c**8*d**2/4 + 5*b**6*c**9*d/4) + x**7*(30*a**6*c**4*d**6 + 216*a**5*b*c**5*d**5 + 450*a**4*b**2*c**6*d**4 + 2400*a**3*b**3*c**7*d**3/7 + 675*a**2*b**4*c**8*d**2/7 + 60*a*b**5*c**9*d/7 + b**6*c**10/7) + x**6*(42*a**6*c**5*d**5 + 210*a**5*b*c**6*d**4 + 300*a**4*b**2*c**7*d**3 + 150*a**3*b**3*c**8*d**2 + 25*a**2*b**4*c**9*d + a*b**5*c**10) + x**5*(42*a**6*c**6*d**4 + 144*a**5*b*c**7*d**3 + 135*a**4*b**2*c**8*d**2 + 40*a**3*b**3*c**9*d + 3*a**2*b**4*c**10) + x**4*(30*a**6*c**7*d**3 + 135*a**5*b*c**8*d**2/2 + 75*a**4*b**2*c**9*d/2 + 5*a**3*b**3*c**10) + x**3*(15*a**6*c**8*d**2 + 20*a**5*b*c**9*d + 5*a**4*b**2*c**10) + x**2*(5*a**6*c**9*d + 3*a**5*b*c**10)

3.1306 $\int (a + bx)^5 (c + dx)^{10} dx$

Optimal. Leaf size=146

$$-\frac{b^4(c+dx)^{15}(bc-ad)}{3d^6} + \frac{5b^3(c+dx)^{14}(bc-ad)^2}{7d^6} - \frac{10b^2(c+dx)^{13}(bc-ad)^3}{13d^6} + \frac{5b(c+dx)^{12}(bc-ad)^4}{12d^6} - \frac{(c+dx)^{11}(bc-ad)^5}{11d^6}$$

[Out] $-1/11*(-a*d+b*c)^5*(d*x+c)^{11}/d^6+5/12*b*(-a*d+b*c)^4*(d*x+c)^{12}/d^6-10/13*b^2*(-a*d+b*c)^3*(d*x+c)^{13}/d^6+5/7*b^3*(-a*d+b*c)^2*(d*x+c)^{14}/d^6-1/3*b^4*(-a*d+b*c)*(d*x+c)^{15}/d^6+1/16*b^5*(d*x+c)^{16}/d^6$

Rubi [A] time = 0.53, antiderivative size = 146, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{b^4(c+dx)^{15}(bc-ad)}{3d^6} + \frac{5b^3(c+dx)^{14}(bc-ad)^2}{7d^6} - \frac{10b^2(c+dx)^{13}(bc-ad)^3}{13d^6} + \frac{5b(c+dx)^{12}(bc-ad)^4}{12d^6} - \frac{(c+dx)^{11}(bc-ad)^5}{11d^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*(c + d*x)^10, x]

[Out] $-\frac{(b*c - a*d)^5*(c + d*x)^{11}}{(11*d^6)} + \frac{(5*b*(b*c - a*d)^4*(c + d*x)^{12}}{(12*d^6)} - \frac{(10*b^2*(b*c - a*d)^3*(c + d*x)^{13}}{(13*d^6)} + \frac{(5*b^3*(b*c - a*d)^2*(c + d*x)^{14}}{(7*d^6)} - \frac{(b^4*(b*c - a*d)*(c + d*x)^{15}}{(3*d^6)} + \frac{(b^5*(c + d*x)^{16}}{(16*d^6)}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^5 (c + dx)^{10} dx &= \int \left(\frac{(-bc + ad)^5 (c + dx)^{10}}{d^5} + \frac{5b(bc - ad)^4 (c + dx)^{11}}{d^5} - \frac{10b^2(bc - ad)^3 (c + dx)^{12}}{d^5} + \frac{10b^3(bc - ad)^2 (c + dx)^{13}}{d^5} - \frac{5b^4(bc - ad) (c + dx)^{14}}{d^5} + \frac{b^5 (c + dx)^{15}}{d^5} \right) dx \\ &= -\frac{(bc - ad)^5 (c + dx)^{11}}{11d^6} + \frac{5b(bc - ad)^4 (c + dx)^{12}}{12d^6} - \frac{10b^2(bc - ad)^3 (c + dx)^{13}}{13d^6} + \frac{5b^3(bc - ad)^2 (c + dx)^{14}}{14d^6} - \frac{b^4(bc - ad) (c + dx)^{15}}{15d^6} + \frac{b^5 (c + dx)^{16}}{16d^6} \end{aligned}$$

Mathematica [B] time = 0.09, size = 811, normalized size = 5.55

$$\frac{1}{16}b^5d^{10}x^{16} + \frac{1}{3}b^4d^9(2bc+ad)x^{15} + \frac{5}{14}b^3d^8(9b^2c^2 + 10abdc + 2a^2d^2)x^{14} + \frac{5}{13}b^2d^7(24b^3c^3 + 45ab^2dc^2 + 20a^2bd^2c + 10a^3d^3)x^{13} + \frac{5}{12}bd^6(15b^4c^4 + 20a^2b^3cd^2 + 10a^3b^2d^3)x^{12} + \frac{5}{11}b^5d^5(10b^4c^5 + 15a^2b^3cd^3 + 10a^3b^2d^4)x^{11} + \frac{5}{10}b^6d^4(5b^5c^6 + 10a^2b^4cd^4 + 10a^3b^3d^5)x^{10} + \frac{5}{9}b^7d^3(3b^6c^7 + 7a^2b^5cd^5 + 7a^3b^4d^6)x^9 + \frac{5}{8}b^8d^2(2b^7c^8 + 4a^2b^6cd^6 + 4a^3b^5d^7)x^8 + \frac{5}{7}b^9d(10b^8c^9 + 10a^2b^7cd^7 + 10a^3b^6d^8)x^7 + \frac{5}{6}b^{10}d^0(5b^9c^{10} + 10a^2b^8cd^8 + 10a^3b^7d^9)x^6 + \frac{5}{5}b^{11}d^{-1}(b^{10}c^{11} + 10a^2b^9cd^9 + 10a^3b^8d^{10})x^5 + \frac{5}{4}b^{12}d^{-2}(5b^{11}c^{12} + 10a^2b^{10}cd^{10} + 10a^3b^9d^{11})x^4 + \frac{5}{3}b^{13}d^{-3}(3b^{12}c^{13} + 6a^2b^{11}cd^{11} + 6a^3b^{10}d^{12})x^3 + \frac{5}{2}b^{14}d^{-4}(2b^{13}c^{14} + 4a^2b^{12}cd^{12} + 4a^3b^{11}d^{13})x^2 + \frac{5}{1}b^{15}d^{-5}(b^{14}c^{15} + 2a^2b^{13}cd^{13} + 2a^3b^{12}d^{14})x + \frac{5}{0}b^{16}d^{-6}(b^{15}c^{16} + a^2b^{14}cd^{14} + a^3b^{13}d^{15})$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*(c + d*x)^10,x]

[Out] $a^5c^{10}x + (5a^4c^9(b*c + 2*a*d)*x^2)/2 + (5a^3c^8(2*b^2c^2 + 10*a*b*c*d + 9a^2d^2)*x^3)/3 + (5a^2c^7(2*b^3c^3 + 20*a*b^2c^2*d + 45a^2*b^2*c*d^2 + 24a^3d^3)*x^4)/4 + a*c^6(b^4c^4 + 20*a*b^3c^3*d + 90a^2*b^2*c^2*d^2 + 120a^3*b*c*d^3 + 42a^4d^4)*x^5 + (c^5(b^5c^5 + 50*a*b^4c^4*d + 450a^2*b^3c^3*d^2 + 1200a^3*b^2c^2*d^3 + 1050a^4*b*c*d^4 + 252a^5d^5)*x^6)/6 + (5c^4*d*(2*b^5c^5 + 45*a*b^4c^4*d + 240a^2*b^3c^3*d^2 + 420a^3*b^2c^2*d^3 + 252a^4*b*c*d^4 + 42a^5d^5)*x^7)/7 + (15c^3*d^2*(3*b^5c^5 + 40*a*b^4c^4*d + 140a^2*b^3c^3*d^2 + 168a^3*b^2c^2*d^3 + 70a^4*b*c*d^4 + 8a^5d^5)*x^8)/8 + (5c^2*d^3*(8*b^5c^5 + 70*a*b^4c^4*d + 168a^2*b^3c^3*d^2 + 140a^3*b^2c^2*d^3 + 40a^4*b*c*d^4 + 3a^5d^5)*x^9)/3 + (c*d^4*(42*b^5c^5 + 252*a*b^4c^4*d + 420a^2*b^3c^3*d^2 + 240a^3*b^2c^2*d^3 + 45a^4*b*c*d^4 + 2a^5d^5)*x^10)/2 + (d^5*(252*b^5c^5 + 1050*a*b^4c^4*d + 1200a^2*b^3c^3*d^2 + 450a^3*b^2c^2*d^3 + 50a^4*b*c*d^4 + a^5d^5)*x^11)/11 + (5*b*d^6*(42*b^4c^4 + 120*a*b^3c^3*d + 90a^2*b^2c^2*d^2 + 20a^3*b*c*d^3 + a^4d^4)*x^12)/12 + (5*b^2*d^7*(24*b^3c^3 + 45*a*b^2c^2*d + 20a^2*b*c*d^2 + 2a^3d^3)*x^13)/13 + (5*b^3*d^8*(9*b^2c^2 + 10*a*b*c*d + 2a^2d^2)*x^14)/14 + (b^4*d^9*(2*b*c + a*d)*x^15)/3 + (b^5*d^10*x^16)/16$

fricas [B] time = 0.37, size = 948, normalized size = 6.49

$$\frac{1}{16}x^{16}d^{10}b^5 + \frac{2}{3}x^{15}d^9cb^5 + \frac{1}{3}x^{15}d^{10}b^4a + \frac{45}{14}x^{14}d^8c^2b^5 + \frac{25}{7}x^{14}d^9cb^4a + \frac{5}{7}x^{14}d^{10}b^3a^2 + \frac{120}{13}x^{13}d^7c^3b^5 + \frac{225}{13}x^{13}d^8c^2b^4a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^10,x, algorithm="fricas")

[Out] $1/16*x^{16}*d^{10}*b^5 + 2/3*x^{15}*d^9*c*b^5 + 1/3*x^{15}*d^{10}*b^4*a + 45/14*x^{14}*d^8*c^2*b^5 + 25/7*x^{14}*d^9*c*b^4*a + 5/7*x^{14}*d^{10}*b^3*a^2 + 120/13*x^{13}*d^7*c^3*b^5 + 225/13*x^{13}*d^8*c^2*b^4*a + 100/13*x^{13}*d^9*c*b^3*a^2 + 10/13*x^{13}*d^{10}*b^2*a^3 + 35/2*x^{12}*d^6*c^4*b^5 + 50*x^{12}*d^7*c^3*b^4*a + 75/2*x^{12}*d^8*c^2*b^3*a^2 + 25/3*x^{12}*d^9*c*b^2*a^3 + 5/12*x^{12}*d^{10}*b*a^4 + 252/11*x^{11}*d^5*c^5*b^5 + 1050/11*x^{11}*d^6*c^4*b^4*a + 1200/11*x^{11}*d^7*c^3*b^3*a^2 + 450/11*x^{11}*d^8*c^2*b^2*a^3 + 50/11*x^{11}*d^9*c*b*a^4 + 1/11*x^{11}*d^{10}*a^5 + 21*x^{10}*d^4*c^6*b^5 + 126*x^{10}*d^5*c^5*b^4*a + 210*x^{10}*d^6*c^4*b^3*a^2 + 120*x^{10}*d^7*c^3*b^2*a^3 + 45/2*x^{10}*d^8*c^2*b*a^4 + x^{10}*d^9*c*a^5 + 40/3*x^9*d^3*c^7*b^5 + 350/3*x^9*d^4*c^6*b^4*a + 280*x^9*d^5*c^5*b^3*a^2 + 700/3*x^9*d^6*c^4*b^2*a^3 + 200/3*x^9*d^7*c^3*b*a^4 + 5*x^9*d^8*c^2*a^5 + 45/8*x^8*d^2*c^8*b^5 + 75*x^8*d^3*c^7*b^4*a + 525/2*x^8*d^4*c^6*b^3*a^2 + 315*x^8*d^5*c^5*b^2*a^3 + 525/4*x^8*d^6*c^4*b*a^4 + 15*x^8*d^7*c^3*a^5 + 10/7*x^7*d*c^9*b^5 + 225/7*x^7*d^2*c^8*b^4*a + 1200/7*x^7*d^3*c^7*b^3*a^2 + 300*x^7*d^4*c^6*b^2*a^3 + 180*x^7*d^5*c^5*b*a^4 + 30*x^7*d^6*c^4*a^5 + 1/6*x^$

$$6c^{10}b^5 + 25/3x^6d^4c^9b^4a + 75x^6d^2c^8b^3a^2 + 200x^6d^3c^7b^2a^3 + 175x^6d^4c^6b^2a^4 + 42x^6d^5c^5a^5 + x^5c^{10}b^4a + 20x^5d^4c^9b^3a^2 + 90x^5d^2c^8b^2a^3 + 120x^5d^3c^7b^2a^4 + 42x^5d^4c^6b^2a^5 + 5/2x^4d^4c^10b^3a^2 + 25x^4d^4c^9b^2a^3 + 225/4x^4d^2c^8b^2a^4 + 30x^4d^3c^7a^5 + 10/3x^3c^10b^2a^3 + 50/3x^3d^4c^9b^2a^4 + 15x^3d^2c^8a^5 + 5/2x^2c^10b^2a^4 + 5x^2d^4c^9a^5 + x^2c^{10}a^5$$

giac [B] time = 1.32, size = 948, normalized size = 6.49

$$\frac{1}{16} b^5 d^{10} x^{16} + \frac{2}{3} b^5 c d^9 x^{15} + \frac{1}{3} a b^4 d^{10} x^{15} + \frac{45}{14} b^5 c^2 d^8 x^{14} + \frac{25}{7} a b^4 c d^9 x^{14} + \frac{5}{7} a^2 b^3 d^{10} x^{14} + \frac{120}{13} b^5 c^3 d^7 x^{13} + \frac{225}{13} a b^4 c^2 d^8 x^{13}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^10,x, algorithm="giac")

[Out] 1/16*b^5*d^10*x^16 + 2/3*b^5*c*d^9*x^15 + 1/3*a*b^4*d^10*x^15 + 45/14*b^5*c^2*d^8*x^14 + 25/7*a*b^4*c*d^9*x^14 + 5/7*a^2*b^3*d^10*x^14 + 120/13*b^5*c^3*d^7*x^13 + 225/13*a*b^4*c^2*d^8*x^13 + 100/13*a^2*b^3*c*d^9*x^13 + 10/13*a^3*b^2*d^10*x^13 + 35/2*b^5*c^4*d^6*x^12 + 50*a*b^4*c^3*d^7*x^12 + 75/2*a^2*b^3*c^2*d^8*x^12 + 25/3*a^3*b^2*c*d^9*x^12 + 5/12*a^4*b*d^10*x^12 + 252/11*b^5*c^5*d^5*x^11 + 1050/11*a*b^4*c^4*d^6*x^11 + 1200/11*a^2*b^3*c^3*d^7*x^11 + 450/11*a^3*b^2*c^2*d^8*x^11 + 50/11*a^4*b*c*d^9*x^11 + 1/11*a^5*d^10*x^11 + 21*b^5*c^6*d^4*x^10 + 126*a*b^4*c^5*d^5*x^10 + 210*a^2*b^3*c^4*d^6*x^10 + 120*a^3*b^2*c^3*d^7*x^10 + 45/2*a^4*b*c^2*d^8*x^10 + a^5*c*d^9*x^10 + 40/3*b^5*c^7*d^3*x^9 + 350/3*a*b^4*c^6*d^4*x^9 + 280*a^2*b^3*c^5*d^5*x^9 + 700/3*a^3*b^2*c^4*d^6*x^9 + 200/3*a^4*b*c^3*d^7*x^9 + 5*a^5*c^2*d^8*x^9 + 45/8*b^5*c^8*d^2*x^8 + 75*a*b^4*c^7*d^3*x^8 + 525/2*a^2*b^3*c^6*d^4*x^8 + 315*a^3*b^2*c^5*d^5*x^8 + 525/4*a^4*b*c^4*d^6*x^8 + 15*a^5*c^3*d^7*x^8 + 10/7*b^5*c^9*d*x^7 + 225/7*a*b^4*c^8*d^2*x^7 + 1200/7*a^2*b^3*c^7*d^3*x^7 + 300*a^3*b^2*c^6*d^4*x^7 + 180*a^4*b*c^5*d^5*x^7 + 30*a^5*c^4*d^6*x^7 + 1/6*b^5*c^10*x^6 + 25/3*a*b^4*c^9*d*x^6 + 75*a^2*b^3*c^8*d^2*x^6 + 200*a^3*b^2*c^7*d^3*x^6 + 175*a^4*b*c^6*d^4*x^6 + 42*a^5*c^5*d^5*x^6 + a*b^4*c^10*x^5 + 20*a^2*b^3*c^9*d*x^5 + 90*a^3*b^2*c^8*d^2*x^5 + 120*a^4*b*c^7*d^3*x^5 + 42*a^5*c^6*d^4*x^5 + 5/2*a^2*b^3*c^10*x^4 + 25*a^3*b^2*c^9*d*x^4 + 225/4*a^4*b*c^8*d^2*x^4 + 30*a^5*c^7*d^3*x^4 + 10/3*a^3*b^2*c^10*x^3 + 50/3*a^4*b*c^9*d*x^3 + 15*a^5*c^8*d^2*x^3 + 5/2*a^4*b*c^10*x^2 + 5*a^5*c^9*d*x^2 + a^5*c^10*x

maple [B] time = 0.00, size = 841, normalized size = 5.76

$$\frac{b^5 d^{10} x^{16}}{16} + a^5 c^{10} x + \frac{(5a b^4 d^{10} + 10b^5 c d^9) x^{15}}{15} + \frac{(10a^2 b^3 d^{10} + 50a b^4 c d^9 + 45b^5 c^2 d^8) x^{14}}{14} + \frac{(10a^3 b^2 d^{10} + 100a^2 b^3 c d^9) x^{13}}{13}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5*(d*x+c)^10,x)

[Out] $\frac{1}{16}b^5d^{10}x^{16} + \frac{1}{15}(5ab^4cd^9 + a^5c^{10})x^{15} + \frac{1}{14}(10a^2b^3cd^9 + 50a^2b^4c^2d^8 + 45b^5c^2d^8) x^{14} + \frac{1}{13}(10a^3b^2d^9 + 100a^2b^3cd^9 + 225a^2b^4c^2d^8 + 120b^5c^3d^7) x^{13} + \frac{1}{12}(5a^4b^2d^9 + 100a^3b^2cd^9 + 450a^2b^3c^2d^8 + 600a^2b^4c^3d^7 + 210b^5c^4d^6) x^{12} + \frac{1}{11}(a^5d^{10} + 50a^4b^2cd^9 + 450a^3b^2c^2d^8 + 1200a^2b^3c^3d^7 + 1050a^2b^4c^4d^6 + 252b^5c^5d^5) x^{11} + \frac{1}{10}(10a^5c^2d^9 + 225a^4b^2c^2d^8 + 1200a^3b^2c^3d^7 + 2100a^2b^3c^4d^6 + 1260a^2b^4c^5d^5 + 210b^5c^6d^4) x^{10} + \frac{1}{9}(45a^5c^2d^8 + 600a^4b^2c^3d^7 + 2100a^3b^2c^4d^6 + 2520a^2b^3c^5d^5 + 1050a^2b^4c^6d^4 + 120b^5c^7d^3) x^9 + \frac{1}{8}(120a^5c^3d^7 + 1050a^4b^2c^4d^6 + 2520a^3b^2c^5d^5 + 2100a^2b^3c^6d^4 + 600a^2b^4c^7d^3 + 45b^5c^8d^2) x^8 + \frac{1}{7}(210a^5c^4d^6 + 1260a^4b^2c^5d^5 + 2100a^3b^2c^6d^4 + 1200a^2b^3c^7d^3 + 225a^2b^4c^8d^2 + 10b^5c^9d) x^7 + \frac{1}{6}(252a^5c^5d^5 + 1050a^4b^2c^6d^4 + 1200a^3b^2c^7d^3 + 450a^2b^3c^8d^2 + 50a^2b^4c^9d + b^5c^{10}) x^6 + \frac{1}{5}(210a^5c^6d^4 + 600a^4b^2c^7d^3 + 450a^3b^2c^8d^2 + 100a^2b^3c^9d + 5a^2b^4c^{10}) x^5 + \frac{1}{4}(120a^5c^7d^3 + 225a^4b^2c^8d^2 + 100a^3b^2c^9d + 10a^2b^3c^{10}) x^4 + \frac{1}{3}(45a^5c^8d^2 + 50a^4b^2c^9d + 10a^3b^2c^{10}) x^3 + \frac{1}{2}(10a^5c^9d + 5a^4b^2c^{10}) x^2 + a^5c^{10}x$

maxima [B] time = 1.46, size = 835, normalized size = 5.72

$$\frac{1}{16}b^5d^{10}x^{16} + a^5c^{10}x + \frac{1}{3}(2b^5cd^9 + ab^4d^{10})x^{15} + \frac{5}{14}(9b^5c^2d^8 + 10ab^4cd^9 + 2a^2b^3d^{10})x^{14} + \frac{5}{13}(24b^5c^3d^7 + 45ab^4cd^9 + 10a^2b^3cd^9 + 100a^2b^4c^2d^8 + 45b^5c^2d^8) x^{13} + \frac{5}{12}(42b^5c^4d^6 + 120a^2b^3cd^9 + 2a^3b^2d^{10}) x^{12} + \frac{1}{11}(252b^5c^5d^5 + 1050a^2b^3c^3d^7 + 450a^3b^2c^2d^8 + 50a^4b^2cd^9 + a^5d^{10}) x^{11} + \frac{1}{10}(42b^5c^6d^4 + 252a^2b^3c^4d^6 + 240a^3b^2c^3d^7 + 45a^4b^2c^2d^8 + 2a^5c^2d^9) x^{10} + \frac{5}{3}(8b^5c^7d^3 + 70a^2b^3c^6d^4 + 168a^2b^3c^5d^5 + 140a^3b^2c^4d^6 + 40a^4b^2c^3d^7 + 3a^5c^2d^8) x^9 + \frac{15}{8}(3b^5c^8d^2 + 40a^2b^3c^7d^3 + 140a^2b^3c^6d^4 + 168a^3b^2c^5d^5 + 70a^4b^2c^4d^6 + 8a^5c^3d^7) x^8 + \frac{5}{7}(2b^5c^9d + 45a^2b^3c^8d^2 + 240a^2b^3c^7d^3 + 420a^3b^2c^6d^4 + 252a^4b^2c^5d^5 + 42a^5c^4d^6) x^7 + \frac{1}{6}(b^5c^{10} + 50a^2b^3c^9d + 450a^2b^3c^8d^2 + 1200a^3b^2c^7d^3 + 1050a^4b^2c^6d^4 + 252a^5c^5d^5) x^6 + (a^2b^3c^{10} + 20a^2b^3c^9d + 90a^3b^2c^8d^2 + 120a^4b^2c^7d^3 + 42a^5c^6d^4) x^5 + \frac{5}{4}(2a^2b^3c^{10} + 20a^3b^2c^9d + 45a^4b^2c^8d^2 + 24a^5c^7d^3) x^4 + \frac{5}{3}(2a^3b^2c^{10} + 10a^4b^2c^9d + 9a^5c^8d^2) x^3 + \frac{5}{2}(a^4b^2c^{10} + 2a^5c^9d) x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^10,x, algorithm="maxima")

[Out] $\frac{1}{16}b^5d^{10}x^{16} + a^5c^{10}x + \frac{1}{3}(2b^5cd^9 + ab^4d^{10})x^{15} + \frac{5}{14}(9b^5c^2d^8 + 10ab^4cd^9 + 2a^2b^3d^{10})x^{14} + \frac{5}{13}(24b^5c^3d^7 + 45ab^4cd^9 + 10a^2b^3cd^9 + 100a^2b^4c^2d^8 + 45b^5c^2d^8) x^{13} + \frac{5}{12}(42b^5c^4d^6 + 120a^2b^3cd^9 + 2a^3b^2d^{10}) x^{12} + \frac{1}{11}(252b^5c^5d^5 + 1050a^2b^3c^3d^7 + 450a^3b^2c^2d^8 + 50a^4b^2cd^9 + a^5d^{10}) x^{11} + \frac{1}{10}(42b^5c^6d^4 + 252a^2b^3c^4d^6 + 240a^3b^2c^3d^7 + 45a^4b^2c^2d^8 + 2a^5c^2d^9) x^{10} + \frac{5}{3}(8b^5c^7d^3 + 70a^2b^3c^6d^4 + 168a^2b^3c^5d^5 + 140a^3b^2c^4d^6 + 40a^4b^2c^3d^7 + 3a^5c^2d^8) x^9 + \frac{15}{8}(3b^5c^8d^2 + 40a^2b^3c^7d^3 + 140a^2b^3c^6d^4 + 168a^3b^2c^5d^5 + 70a^4b^2c^4d^6 + 8a^5c^3d^7) x^8 + \frac{5}{7}(2b^5c^9d + 45a^2b^3c^8d^2 + 240a^2b^3c^7d^3 + 420a^3b^2c^6d^4 + 252a^4b^2c^5d^5 + 42a^5c^4d^6) x^7 + \frac{1}{6}(b^5c^{10} + 50a^2b^3c^9d + 450a^2b^3c^8d^2 + 1200a^3b^2c^7d^3 + 1050a^4b^2c^6d^4 + 252a^5c^5d^5) x^6 + (a^2b^3c^{10} + 20a^2b^3c^9d + 90a^3b^2c^8d^2 + 120a^4b^2c^7d^3 + 42a^5c^6d^4) x^5 + \frac{5}{4}(2a^2b^3c^{10} + 20a^3b^2c^9d + 45a^4b^2c^8d^2 + 24a^5c^7d^3) x^4 + \frac{5}{3}(2a^3b^2c^{10} + 10a^4b^2c^9d + 9a^5c^8d^2) x^3 + \frac{5}{2}(a^4b^2c^{10} + 2a^5c^9d) x^2$

$$\begin{aligned}
& c^{**5}d^{**5}/11) + x^{**10}*(a^{**5}c^{**d**9} + 45*a^{**4}b^{**c**2}d^{**8}/2 + 120*a^{**3}b^{**2} \\
& c^{**3}d^{**7} + 210*a^{**2}b^{**3}c^{**4}d^{**6} + 126*a^{**b**4}c^{**5}d^{**5} + 21*b^{**5}c^{**6}d \\
& **4) + x^{**9}*(5*a^{**5}c^{**2}d^{**8} + 200*a^{**4}b^{**c**3}d^{**7}/3 + 700*a^{**3}b^{**2}c^{**4} \\
& *d^{**6}/3 + 280*a^{**2}b^{**3}c^{**5}d^{**5} + 350*a^{**b**4}c^{**6}d^{**4}/3 + 40*b^{**5}c^{**7}d \\
& **3/3) + x^{**8}*(15*a^{**5}c^{**3}d^{**7} + 525*a^{**4}b^{**c**4}d^{**6}/4 + 315*a^{**3}b^{**2}c \\
& **5}d^{**5} + 525*a^{**2}b^{**3}c^{**6}d^{**4}/2 + 75*a^{**b**4}c^{**7}d^{**3} + 45*b^{**5}c^{**8}d \\
& **2/8) + x^{**7}*(30*a^{**5}c^{**4}d^{**6} + 180*a^{**4}b^{**c**5}d^{**5} + 300*a^{**3}b^{**2}c^{** \\
& 6}d^{**4} + 1200*a^{**2}b^{**3}c^{**7}d^{**3}/7 + 225*a^{**b**4}c^{**8}d^{**2}/7 + 10*b^{**5}c^{**9} \\
& *d/7) + x^{**6}*(42*a^{**5}c^{**5}d^{**5} + 175*a^{**4}b^{**c**6}d^{**4} + 200*a^{**3}b^{**2}c^{**7} \\
& *d^{**3} + 75*a^{**2}b^{**3}c^{**8}d^{**2} + 25*a^{**b**4}c^{**9}d/3 + b^{**5}c^{**10}/6) + x^{**5} \\
& (42*a^{**5}c^{**6}d^{**4} + 120*a^{**4}b^{**c**7}d^{**3} + 90*a^{**3}b^{**2}c^{**8}d^{**2} + 20*a^{** \\
& 2}b^{**3}c^{**9}d + a^{**b**4}c^{**10}) + x^{**4}*(30*a^{**5}c^{**7}d^{**3} + 225*a^{**4}b^{**c**8}d \\
& **2/4 + 25*a^{**3}b^{**2}c^{**9}d + 5*a^{**2}b^{**3}c^{**10}/2) + x^{**3}*(15*a^{**5}c^{**8}d^{** \\
& 2 + 50*a^{**4}b^{**c**9}d/3 + 10*a^{**3}b^{**2}c^{**10}/3) + x^{**2}*(5*a^{**5}c^{**9}d + 5*a^{** \\
& 4}b^{**c**10}/2)
\end{aligned}$$

3.1307 $\int (a + bx)^4 (c + dx)^{10} dx$

Optimal. Leaf size=119

$$-\frac{2b^3(c+dx)^{14}(bc-ad)}{7d^5} + \frac{6b^2(c+dx)^{13}(bc-ad)^2}{13d^5} - \frac{b(c+dx)^{12}(bc-ad)^3}{3d^5} + \frac{(c+dx)^{11}(bc-ad)^4}{11d^5} + \frac{b^4(c+dx)^{15}}{15d^5}$$

[Out] $1/11*(-a*d+b*c)^4*(d*x+c)^{11}/d^5-1/3*b*(-a*d+b*c)^3*(d*x+c)^{12}/d^5+6/13*b^2*(-a*d+b*c)^2*(d*x+c)^{13}/d^5-2/7*b^3*(-a*d+b*c)*(d*x+c)^{14}/d^5+1/15*b^4*(d*x+c)^{15}/d^5$

Rubi [A] time = 0.44, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{2b^3(c+dx)^{14}(bc-ad)}{7d^5} + \frac{6b^2(c+dx)^{13}(bc-ad)^2}{13d^5} - \frac{b(c+dx)^{12}(bc-ad)^3}{3d^5} + \frac{(c+dx)^{11}(bc-ad)^4}{11d^5} + \frac{b^4(c+dx)^{15}}{15d^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4*(c + d*x)^10, x]

[Out] $((b*c - a*d)^4*(c + d*x)^{11})/(11*d^5) - (b*(b*c - a*d)^3*(c + d*x)^{12})/(3*d^5) + (6*b^2*(b*c - a*d)^2*(c + d*x)^{13})/(13*d^5) - (2*b^3*(b*c - a*d)*(c + d*x)^{14})/(7*d^5) + (b^4*(c + d*x)^{15})/(15*d^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^4 (c + dx)^{10} dx &= \int \left(\frac{(-bc + ad)^4 (c + dx)^{10}}{d^4} - \frac{4b(bc - ad)^3 (c + dx)^{11}}{d^4} + \frac{6b^2(bc - ad)^2 (c + dx)^{12}}{d^4} - \frac{4b^3(bc - ad)(c + dx)^{13}}{d^4} + \frac{b^4(c + dx)^{14}}{d^4} \right) dx \\ &= \frac{(bc - ad)^4 (c + dx)^{11}}{11d^5} - \frac{b(bc - ad)^3 (c + dx)^{12}}{3d^5} + \frac{6b^2(bc - ad)^2 (c + dx)^{13}}{13d^5} - \frac{2b^3(bc - ad)(c + dx)^{14}}{7d^5} + \frac{b^4(c + dx)^{15}}{15d^5} \end{aligned}$$

Mathematica [B] time = 0.08, size = 660, normalized size = 5.55

$$a^4 c^{10} x + a^3 c^9 x^2 (5ad + 2bc) + \frac{1}{13} b^2 d^8 x^{13} (6a^2 d^2 + 40abcd + 45b^2 c^2) + \frac{1}{3} a^2 c^8 x^3 (45a^2 d^2 + 40abcd + 6b^2 c^2) + \frac{1}{3} b d^7 x^{12}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4*(c + d*x)^10,x]

[Out] $a^4c^{10}x + a^3c^9(2b^2c + 5a^2d)x^2 + (a^2c^8(6b^2c^2 + 40ab^2cd + 45a^2d^2)x^3)/3 + a^2c^7(b^3c^3 + 15ab^2c^2d + 45a^2b^2cd^2 + 30a^3d^3)x^4 + (c^6(b^4c^4 + 40ab^3c^3d + 270a^2b^2c^2d^2 + 480a^3b^2cd^3 + 210a^4d^4)x^5)/5 + (c^5d(5b^4c^4 + 90ab^3c^3d + 360a^2b^2c^2d^2 + 420a^3b^2cd^3 + 126a^4d^4)x^6)/3 + (3c^4d^2(15b^4c^4 + 160ab^3c^3d + 420a^2b^2c^2d^2 + 336a^3b^2cd^3 + 70a^4d^4)x^7)/7 + 3c^3d^3(5b^4c^4 + 35ab^3c^3d + 63a^2b^2c^2d^2 + 35a^3b^2cd^3 + 5a^4d^4)x^8 + (c^2d^4(70b^4c^4 + 336ab^3c^3d + 420a^2b^2c^2d^2 + 160a^3b^2cd^3 + 15a^4d^4)x^9)/3 + (cd^5(126b^4c^4 + 420ab^3c^3d + 360a^2b^2c^2d^2 + 90a^3b^2cd^3 + 5a^4d^4)x^10)/5 + (d^6(210b^4c^4 + 480ab^3c^3d + 270a^2b^2c^2d^2 + 40a^3b^2cd^3 + a^4d^4)x^11)/11 + (b^2d^7(30b^3c^3 + 45ab^2c^2d + 15a^2b^2cd^2 + a^3d^3)x^12)/3 + (b^2d^8(45b^2c^2 + 40ab^2cd + 6a^2d^2)x^13)/13 + (b^3d^9(5b^2c + 2a^2d)x^14)/7 + (b^4d^10x^15)/15$

fricas [B] time = 0.39, size = 771, normalized size = 6.48

$$\frac{1}{15}x^{15}d^{10}b^4 + \frac{5}{7}x^{14}d^9cb^4 + \frac{2}{7}x^{14}d^{10}b^3a + \frac{45}{13}x^{13}d^8c^2b^4 + \frac{40}{13}x^{13}d^9cb^3a + \frac{6}{13}x^{13}d^{10}b^2a^2 + 10x^{12}d^7c^3b^4 + 15x^{12}d^8c^2b^3a + 5x^{12}d^9cb^2a^2 + 10x^{11}d^6c^4b^4 + 480x^{11}d^7c^3b^3a + 270x^{11}d^8c^2b^2a^2 + 40x^{11}d^9c^2b^2a^3 + 126x^{10}d^5c^5b^4 + 84x^{10}d^6c^4b^3a + 72x^{10}d^7c^3b^2a^2 + 18x^{10}d^8c^2b^2a^3 + x^{10}d^9c^2b^2a^4 + 70x^9d^4c^6b^4 + 112x^9d^5c^5b^3a + 140x^9d^6c^4b^2a^2 + 160x^9d^7c^3b^2a^3 + 5x^9d^8c^2a^4 + 15x^8d^3c^7b^4 + 105x^8d^4c^6b^3a + 189x^8d^5c^5b^2a^2 + 105x^8d^6c^4b^2a^3 + 15x^8d^7c^3a^4 + 45x^7d^2c^8b^4 + 480x^7d^3c^7b^3a + 180x^7d^4c^6b^2a^2 + 144x^7d^5c^5b^2a^3 + 30x^7d^6c^4a^4 + 5x^6d^9c^9b^4 + 30x^6d^2c^8b^3a + 120x^6d^3c^7b^2a^2 + 140x^6d^4c^6b^2a^3 + 42x^6d^5c^5a^4 + 15x^5d^10c^10b^4 + 8x^5d^9c^9b^3a + 54x^5d^2c^8b^2a^2 + 96x^5d^3c^7b^2a^3 + 42x^5d^4c^6a^4 + x^4d^10c^10b^3a + 15x^4d^9c^9b^2a^2 + 45x^4d^2c^8b^2a^3 + 30x^4d^3c^7a^4 + 2x^3d^10c^10b^2a^2 + 40x^3d^9c^9b^2a^3 + 15x^3d^2c^8a^4 + 2x^2d^10c^10b^2a^3 + 5x^2d^9c^9a^4 + x^2d^10c^10a^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^10,x, algorithm="fricas")

[Out] $1/15x^{15}d^{10}b^4 + 5/7x^{14}d^9c^2b^4 + 2/7x^{14}d^{10}b^3a + 45/13x^{13}d^8c^2b^4 + 40/13x^{13}d^9c^2b^3a + 6/13x^{13}d^{10}b^2a^2 + 10x^{12}d^7c^3b^4 + 15x^{12}d^8c^2b^3a + 5x^{12}d^9c^2b^2a^2 + 1/3x^{12}d^{10}b^2a^3 + 210/11x^{11}d^6c^4b^4 + 480/11x^{11}d^7c^3b^3a + 270/11x^{11}d^8c^2b^2a^2 + 40/11x^{11}d^9c^2b^2a^3 + 1/11x^{11}d^{10}a^4 + 126/5x^{10}d^5c^5b^4 + 84x^{10}d^6c^4b^3a + 72x^{10}d^7c^3b^2a^2 + 18x^{10}d^8c^2b^2a^3 + x^{10}d^9c^2b^2a^4 + 70/3x^9d^4c^6b^4 + 112x^9d^5c^5b^3a + 140x^9d^6c^4b^2a^2 + 160/3x^9d^7c^3b^2a^3 + 5x^9d^8c^2a^4 + 15x^8d^3c^7b^4 + 105x^8d^4c^6b^3a + 189x^8d^5c^5b^2a^2 + 105x^8d^6c^4b^2a^3 + 15x^8d^7c^3a^4 + 45/7x^7d^2c^8b^4 + 480/7x^7d^3c^7b^3a + 180x^7d^4c^6b^2a^2 + 144x^7d^5c^5b^2a^3 + 30x^7d^6c^4a^4 + 5/3x^6d^9c^9b^4 + 30x^6d^2c^8b^3a + 120x^6d^3c^7b^2a^2 + 140x^6d^4c^6b^2a^3 + 42x^6d^5c^5a^4 + 1/5x^5d^10c^10b^4 + 8x^5d^9c^9b^3a + 54x^5d^2c^8b^2a^2 + 96x^5d^3c^7b^2a^3 + 42x^5d^4c^6a^4 + x^4d^10c^10b^3a + 15x^4d^9c^9b^2a^2 + 45x^4d^2c^8b^2a^3 + 30x^4d^3c^7a^4 + 2x^3d^10c^10b^2a^2 + 40/3x^3d^9c^9b^2a^3 + 15x^3d^2c^8a^4 + 2x^2d^10c^10b^2a^3 + 5x^2d^9c^9a^4 + x^2d^10c^10a^4$

giac [B] time = 1.27, size = 771, normalized size = 6.48

$$\frac{1}{15} b^4 d^{10} x^{15} + \frac{5}{7} b^4 c d^9 x^{14} + \frac{2}{7} a b^3 d^{10} x^{14} + \frac{45}{13} b^4 c^2 d^8 x^{13} + \frac{40}{13} a b^3 c d^9 x^{13} + \frac{6}{13} a^2 b^2 d^{10} x^{13} + 10 b^4 c^3 d^7 x^{12} + 15 a b^3 c^2 d^8 x^{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^10,x, algorithm="giac")

[Out] $\frac{1}{15} b^4 d^{10} x^{15} + \frac{5}{7} b^4 c d^9 x^{14} + \frac{2}{7} a b^3 d^{10} x^{14} + \frac{45}{13} b^4 c^2 d^8 x^{13} + \frac{40}{13} a b^3 c d^9 x^{13} + \frac{6}{13} a^2 b^2 d^{10} x^{13} + 10 b^4 c^3 d^7 x^{12} + 15 a b^3 c^2 d^8 x^{12} + 210/11 b^4 c^4 d^6 x^{11} + 480/11 a b^3 c^3 d^7 x^{11} + 270/11 a^2 b^2 c^2 d^8 x^{11} + 40/11 a^3 b c^2 d^9 x^{11} + 1/11 a^4 d^{10} x^{11} + 126/5 b^4 c^5 d^5 x^{10} + 84 a b^3 c^4 d^6 x^{10} + 72 a^2 b^2 c^3 d^7 x^{10} + 18 a^3 b c^2 d^8 x^{10} + a^4 c d^9 x^{10} + 70/3 b^4 c^6 d^4 x^9 + 112 a b^3 c^5 d^5 x^9 + 140 a^2 b^2 c^4 d^6 x^9 + 160/3 a^3 b c^3 d^7 x^9 + 5 a^4 c^2 d^8 x^9 + 15 b^4 c^7 d^3 x^8 + 105 a b^3 c^6 d^4 x^8 + 189 a^2 b^2 c^5 d^5 x^8 + 105 a^3 b c^4 d^6 x^8 + 15 a^4 c^3 d^7 x^8 + 45/7 b^4 c^8 d^2 x^7 + 480/7 a b^3 c^7 d^3 x^7 + 180 a^2 b^2 c^6 d^4 x^7 + 144 a^3 b c^5 d^5 x^7 + 30 a^4 c^4 d^6 x^7 + 5/3 b^4 c^9 d x^6 + 30 a b^3 c^8 d^2 x^6 + 120 a^2 b^2 c^7 d^3 x^6 + 140 a^3 b c^6 d^4 x^6 + 42 a^4 c^5 d^5 x^6 + 1/5 b^4 c^{10} x^5 + 8 a b^3 c^9 d x^5 + 54 a^2 b^2 c^8 d^2 x^5 + 96 a^3 b c^7 d^3 x^5 + 42 a^4 c^6 d^4 x^5 + a b^3 c^{10} x^4 + 15 a^2 b^2 c^9 d x^4 + 45 a^3 b c^8 d^2 x^4 + 30 a^4 c^7 d^3 x^4 + 2 a^2 b^2 c^{10} x^3 + 40/3 a^3 b c^9 d x^3 + 15 a^4 c^8 d^2 x^3 + 2 a^3 b c^{10} x^2 + 5 a^4 c^9 d x^2 + a^4 c^{10} x$

maple [B] time = 0.00, size = 691, normalized size = 5.81

$$\frac{b^4 d^{10} x^{15}}{15} + a^4 c^{10} x + \frac{(4 a b^3 d^{10} + 10 b^4 c d^9) x^{14}}{14} + \frac{(6 a^2 b^2 d^{10} + 40 a b^3 c d^9 + 45 b^4 c^2 d^8) x^{13}}{13} + \frac{(4 a^3 b d^{10} + 60 a^2 b^2 c d^9 + 180 a b^3 c^2 d^8 + 120 b^4 c^3 d^7) x^{12}}{12} + \frac{(4 a^4 d^{10} + 40 a^3 b c d^9 + 270 a^2 b^2 c^2 d^8 + 480 a b^3 c^3 d^7 + 210 b^4 c^4 d^6) x^{11}}{11} + \frac{(10 a^4 c d^9 + 180 a^3 b c^2 d^8 + 720 a^2 b^2 c^3 d^7 + 840 a b^3 c^4 d^6 + 252 b^4 c^5 d^5) x^{10}}{10} + \frac{(45 a^4 c^2 d^8 + 480 a^3 b c^3 d^7 + 1260 a^2 b^2 c^4 d^6 + 1008 a b^3 c^5 d^5 + 210 b^4 c^6 d^4) x^9}{9} + \frac{(120 a^4 c^3 d^7 + 840 a^3 b c^4 d^6 + 1512 a^2 b^2 c^5 d^5 + 840 a b^3 c^6 d^4 + 120 b^4 c^7 d^3) x^8}{8} + \frac{(210 a^4 c^4 d^6 + 1008 a^3 b c^5 d^5 + 1260 a^2 b^2 c^6 d^4 + 480 a b^3 c^7 d^3 + 45 b^4 c^8 d^2) x^7}{7} + \frac{(252 a^4 c^5 d^5 + 840 a^3 b c^6 d^4 + 720 a^2 b^2 c^7 d^3 + 180 a b^3 c^8 d^2) x^6}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4*(d*x+c)^10,x)

[Out] $\frac{1}{15} b^4 d^{10} x^{15} + \frac{1}{14} (4 a b^3 d^{10} + 10 b^4 c d^9) x^{14} + \frac{1}{13} (6 a^2 b^2 d^{10} + 40 a b^3 c d^9 + 45 b^4 c^2 d^8) x^{13} + \frac{1}{12} (4 a^3 b d^{10} + 60 a^2 b^2 c d^9 + 180 a b^3 c^2 d^8 + 120 b^4 c^3 d^7) x^{12} + \frac{1}{11} (a^4 d^{10} + 40 a^3 b c d^9 + 270 a^2 b^2 c^2 d^8 + 480 a b^3 c^3 d^7 + 210 b^4 c^4 d^6) x^{11} + \frac{1}{10} (10 a^4 c d^9 + 180 a^3 b c^2 d^8 + 720 a^2 b^2 c^3 d^7 + 840 a b^3 c^4 d^6 + 252 b^4 c^5 d^5) x^{10} + \frac{1}{9} (45 a^4 c^2 d^8 + 480 a^3 b c^3 d^7 + 1260 a^2 b^2 c^4 d^6 + 1008 a b^3 c^5 d^5 + 210 b^4 c^6 d^4) x^9 + \frac{1}{8} (120 a^4 c^3 d^7 + 840 a^3 b c^4 d^6 + 1512 a^2 b^2 c^5 d^5 + 840 a b^3 c^6 d^4 + 120 b^4 c^7 d^3) x^8 + \frac{1}{7} (210 a^4 c^4 d^6 + 1008 a^3 b c^5 d^5 + 1260 a^2 b^2 c^6 d^4 + 480 a b^3 c^7 d^3 + 45 b^4 c^8 d^2) x^7 + \frac{1}{6} (252 a^4 c^5 d^5 + 840 a^3 b c^6 d^4 + 720 a^2 b^2 c^7 d^3 + 180 a b^3 c^8 d^2) x^6$

+10*b^4*c^9*d)*x^6+1/5*(210*a^4*c^6*d^4+480*a^3*b*c^7*d^3+270*a^2*b^2*c^8*d^2+40*a*b^3*c^9*d+b^4*c^10)*x^5+1/4*(120*a^4*c^7*d^3+180*a^3*b*c^8*d^2+60*a^2*b^2*c^9*d+4*a*b^3*c^10)*x^4+1/3*(45*a^4*c^8*d^2+40*a^3*b*c^9*d+6*a^2*b^2*c^10)*x^3+1/2*(10*a^4*c^9*d+4*a^3*b*c^10)*x^2+a^4*c^10*x

maxima [B] time = 1.42, size = 686, normalized size = 5.76

$$\frac{1}{15} b^4 d^{10} x^{15} + a^4 c^{10} x + \frac{1}{7} (5 b^4 c d^9 + 2 a b^3 d^{10}) x^{14} + \frac{1}{13} (45 b^4 c^2 d^8 + 40 a b^3 c d^9 + 6 a^2 b^2 d^{10}) x^{13} + \frac{1}{3} (30 b^4 c^3 d^7 + 45 a b^3 c^2 d^8 + 15 a^2 b^2 c d^9 + a^3 b d^{10}) x^{12} + \frac{1}{11} (210 b^4 c^4 d^6 + 480 a b^3 c^3 d^7 + 270 a^2 b^2 c^2 d^8 + 40 a^3 b c d^9 + a^4 d^{10}) x^{11} + \frac{1}{5} (126 b^4 c^5 d^5 + 420 a b^3 c^4 d^6 + 360 a^2 b^2 c^3 d^7 + 90 a^3 b c^2 d^8 + 5 a^4 c d^9) x^{10} + \frac{1}{3} (70 b^4 c^6 d^4 + 336 a b^3 c^5 d^5 + 420 a^2 b^2 c^4 d^6 + 160 a^3 b c^3 d^7 + 15 a^4 c^2 d^8) x^9 + 3 (5 b^4 c^7 d^3 + 35 a b^3 c^6 d^4 + 63 a^2 b^2 c^5 d^5 + 35 a^3 b c^4 d^6 + 5 a^4 c^3 d^7) x^8 + \frac{3}{7} (15 b^4 c^8 d^2 + 160 a b^3 c^7 d^3 + 420 a^2 b^2 c^6 d^4 + 336 a^3 b c^5 d^5 + 70 a^4 c^4 d^6) x^7 + \frac{1}{3} (5 b^4 c^9 d + 90 a b^3 c^8 d^2 + 360 a^2 b^2 c^7 d^3 + 420 a^3 b c^6 d^4 + 126 a^4 c^5 d^5) x^6 + \frac{1}{5} (b^4 c^{10} + 40 a b^3 c^9 d + 270 a^2 b^2 c^8 d^2 + 480 a^3 b c^7 d^3 + 210 a^4 c^6 d^4) x^5 + (a b^3 c^{10} + 15 a^2 b^2 c^9 d + 45 a^3 b c^8 d^2 + 30 a^4 c^7 d^3) x^4 + \frac{1}{3} (6 a^2 b^2 c^{10} + 40 a^3 b c^9 d + 45 a^4 c^8 d^2) x^3 + (2 a^3 b c^{10} + 5 a^4 c^9 d) x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^10,x, algorithm="maxima")

[Out] 1/15*b^4*d^10*x^15 + a^4*c^10*x + 1/7*(5*b^4*c*d^9 + 2*a*b^3*d^10)*x^14 + 1/13*(45*b^4*c^2*d^8 + 40*a*b^3*c*d^9 + 6*a^2*b^2*d^10)*x^13 + 1/3*(30*b^4*c^3*d^7 + 45*a*b^3*c^2*d^8 + 15*a^2*b^2*c*d^9 + a^3*b*d^10)*x^12 + 1/11*(210*b^4*c^4*d^6 + 480*a*b^3*c^3*d^7 + 270*a^2*b^2*c^2*d^8 + 40*a^3*b*c*d^9 + a^4*d^10)*x^11 + 1/5*(126*b^4*c^5*d^5 + 420*a*b^3*c^4*d^6 + 360*a^2*b^2*c^3*d^7 + 90*a^3*b*c^2*d^8 + 5*a^4*c*d^9)*x^10 + 1/3*(70*b^4*c^6*d^4 + 336*a*b^3*c^5*d^5 + 420*a^2*b^2*c^4*d^6 + 160*a^3*b*c^3*d^7 + 15*a^4*c^2*d^8)*x^9 + 3*(5*b^4*c^7*d^3 + 35*a*b^3*c^6*d^4 + 63*a^2*b^2*c^5*d^5 + 35*a^3*b*c^4*d^6 + 5*a^4*c^3*d^7)*x^8 + 3/7*(15*b^4*c^8*d^2 + 160*a*b^3*c^7*d^3 + 420*a^2*b^2*c^6*d^4 + 336*a^3*b*c^5*d^5 + 70*a^4*c^4*d^6)*x^7 + 1/3*(5*b^4*c^9*d + 90*a*b^3*c^8*d^2 + 360*a^2*b^2*c^7*d^3 + 420*a^3*b*c^6*d^4 + 126*a^4*c^5*d^5)*x^6 + 1/5*(b^4*c^10 + 40*a*b^3*c^9*d + 270*a^2*b^2*c^8*d^2 + 480*a^3*b*c^7*d^3 + 210*a^4*c^6*d^4)*x^5 + (a*b^3*c^10 + 15*a^2*b^2*c^9*d + 45*a^3*b*c^8*d^2 + 30*a^4*c^7*d^3)*x^4 + 1/3*(6*a^2*b^2*c^10 + 40*a^3*b*c^9*d + 45*a^4*c^8*d^2)*x^3 + (2*a^3*b*c^10 + 5*a^4*c^9*d)*x^2

mupad [B] time = 0.43, size = 664, normalized size = 5.58

$$x^5 \left(42 a^4 c^6 d^4 + 96 a^3 b c^7 d^3 + 54 a^2 b^2 c^8 d^2 + 8 a b^3 c^9 d + \frac{b^4 c^{10}}{5} \right) + x^{11} \left(\frac{a^4 d^{10}}{11} + \frac{40 a^3 b c d^9}{11} + \frac{270 a^2 b^2 c^2 d^8}{11} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^4*(c + d*x)^10,x)

[Out] x^5*((b^4*c^10)/5 + 42*a^4*c^6*d^4 + 96*a^3*b*c^7*d^3 + 54*a^2*b^2*c^8*d^2 + 8*a*b^3*c^9*d) + x^11*((a^4*d^10)/11 + (210*b^4*c^4*d^6)/11 + (480*a*b^3*c^3*d^7)/11 + (270*a^2*b^2*c^2*d^8)/11 + (40*a^3*b*c*d^9)/11) + x^8*(15*a^4*c^3*d^7 + 15*b^4*c^7*d^3 + 105*a*b^3*c^6*d^4 + 105*a^3*b*c^4*d^6 + 189*a^2*b^2*c^5*d^5) + x^9*(5*a^4*c^2*d^8 + (70*b^4*c^6*d^4)/3 + 112*a*b^3*c^5*d^5 + (160*a^3*b*c^3*d^7)/3 + 140*a^2*b^2*c^4*d^6) + x^7*(30*a^4*c^4*d^6 + (45*b^4*c^8*d^2)/7 + (480*a*b^3*c^7*d^3)/7 + 144*a^3*b*c^5*d^5 + 180*a^2*b^2*c

$$\begin{aligned} & ^6*d^4) + x^4*(a*b^3*c^10 + 30*a^4*c^7*d^3 + 15*a^2*b^2*c^9*d + 45*a^3*b*c^8*d^2) + x^{12}*((a^3*b*d^10)/3 + 10*b^4*c^3*d^7 + 15*a*b^3*c^2*d^8 + 5*a^2*b^2*c*d^9) + x^{10}*(a^4*c*d^9 + (126*b^4*c^5*d^5)/5 + 84*a*b^3*c^4*d^6 + 18*a^3*b*c^2*d^8 + 72*a^2*b^2*c^3*d^7) + x^6*((5*b^4*c^9*d)/3 + 42*a^4*c^5*d^5 + 30*a*b^3*c^8*d^2 + 140*a^3*b*c^6*d^4 + 120*a^2*b^2*c^7*d^3) + a^4*c^10*x + (b^4*d^10*x^15)/15 + a^3*c^9*x^2*(5*a*d + 2*b*c) + (b^3*d^9*x^14*(2*a*d + 5*b*c))/7 + (a^2*c^8*x^3*(45*a^2*d^2 + 6*b^2*c^2 + 40*a*b*c*d))/3 + (b^2*d^8*x^13*(6*a^2*d^2 + 45*b^2*c^2 + 40*a*b*c*d))/13 \end{aligned}$$

sympy [B] time = 0.18, size = 748, normalized size = 6.29

$$a^4c^{10}x + \frac{b^4d^{10}x^{15}}{15} + x^{14} \left(\frac{2ab^3d^{10}}{7} + \frac{5b^4cd^9}{7} \right) + x^{13} \left(\frac{6a^2b^2d^{10}}{13} + \frac{40ab^3cd^9}{13} + \frac{45b^4c^2d^8}{13} \right) + x^{12} \left(\frac{a^3bd^{10}}{3} + 5a^2b^2cd^9 + 1 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4*(d*x+c)**10,x)

[Out] a**4*c**10*x + b**4*d**10*x**15/15 + x**14*(2*a*b**3*d**10/7 + 5*b**4*c*d**9/7) + x**13*(6*a**2*b**2*d**10/13 + 40*a*b**3*c*d**9/13 + 45*b**4*c**2*d**8/13) + x**12*(a**3*b*d**10/3 + 5*a**2*b**2*c*d**9 + 15*a*b**3*c**2*d**8 + 10*b**4*c**3*d**7) + x**11*(a**4*d**10/11 + 40*a**3*b*c*d**9/11 + 270*a**2*b**2*c**2*d**8/11 + 480*a*b**3*c**3*d**7/11 + 210*b**4*c**4*d**6/11) + x**10*(a**4*c*d**9 + 18*a**3*b*c**2*d**8 + 72*a**2*b**2*c**3*d**7 + 84*a*b**3*c**4*d**6 + 126*b**4*c**5*d**5/5) + x**9*(5*a**4*c**2*d**8 + 160*a**3*b*c**3*d**7/3 + 140*a**2*b**2*c**4*d**6 + 112*a*b**3*c**5*d**5 + 70*b**4*c**6*d**4/3) + x**8*(15*a**4*c**3*d**7 + 105*a**3*b*c**4*d**6 + 189*a**2*b**2*c**5*d**5 + 105*a*b**3*c**6*d**4 + 15*b**4*c**7*d**3) + x**7*(30*a**4*c**4*d**6 + 144*a**3*b*c**5*d**5 + 180*a**2*b**2*c**6*d**4 + 480*a*b**3*c**7*d**3/7 + 45*b**4*c**8*d**2/7) + x**6*(42*a**4*c**5*d**5 + 140*a**3*b*c**6*d**4 + 120*a**2*b**2*c**7*d**3 + 30*a*b**3*c**8*d**2 + 5*b**4*c**9*d/3) + x**5*(42*a**4*c**6*d**4 + 96*a**3*b*c**7*d**3 + 54*a**2*b**2*c**8*d**2 + 8*a*b**3*c**9*d + b**4*c**10/5) + x**4*(30*a**4*c**7*d**3 + 45*a**3*b*c**8*d**2 + 15*a**2*b**2*c**9*d + a*b**3*c**10) + x**3*(15*a**4*c**8*d**2 + 40*a**3*b*c**9*d/3 + 2*a**2*b**2*c**10) + x**2*(5*a**4*c**9*d + 2*a**3*b*c**10)

3.1308 $\int (a + bx)^3 (c + dx)^{10} dx$

Optimal. Leaf size=92

$$-\frac{3b^2(c+dx)^{13}(bc-ad)}{13d^4} + \frac{b(c+dx)^{12}(bc-ad)^2}{4d^4} - \frac{(c+dx)^{11}(bc-ad)^3}{11d^4} + \frac{b^3(c+dx)^{14}}{14d^4}$$

[Out] $-1/11*(-a*d+b*c)^3*(d*x+c)^{11}/d^4+1/4*b*(-a*d+b*c)^2*(d*x+c)^{12}/d^4-3/13*b^2*(-a*d+b*c)*(d*x+c)^{13}/d^4+1/14*b^3*(d*x+c)^{14}/d^4$

Rubi [A] time = 0.35, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{3b^2(c+dx)^{13}(bc-ad)}{13d^4} + \frac{b(c+dx)^{12}(bc-ad)^2}{4d^4} - \frac{(c+dx)^{11}(bc-ad)^3}{11d^4} + \frac{b^3(c+dx)^{14}}{14d^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3*(c + d*x)^10, x]

[Out] $-((b*c - a*d)^3*(c + d*x)^{11})/(11*d^4) + (b*(b*c - a*d)^2*(c + d*x)^{12})/(4*d^4) - (3*b^2*(b*c - a*d)*(c + d*x)^{13})/(13*d^4) + (b^3*(c + d*x)^{14})/(14*d^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^3 (c + dx)^{10} dx &= \int \left(\frac{(-bc + ad)^3 (c + dx)^{10}}{d^3} + \frac{3b(bc - ad)^2 (c + dx)^{11}}{d^3} - \frac{3b^2(bc - ad)(c + dx)^{12}}{d^3} + \frac{b^3(c + dx)^{13}}{d^3} \right) dx \\ &= -\frac{(bc - ad)^3 (c + dx)^{11}}{11d^4} + \frac{b(bc - ad)^2 (c + dx)^{12}}{4d^4} - \frac{3b^2(bc - ad)(c + dx)^{13}}{13d^4} + \frac{b^3(c + dx)^{14}}{14d^4} \end{aligned}$$

Mathematica [B] time = 0.07, size = 511, normalized size = 5.55

$$a^3 c^{10} x + \frac{1}{4} b d^8 x^{12} (a^2 d^2 + 10 a b c d + 15 b^2 c^2) + a c^8 x^3 (15 a^2 d^2 + 10 a b c d + b^2 c^2) + \frac{1}{2} a^2 c^9 x^2 (10 a d + 3 b c) + \frac{1}{11} d^7 x^{11} (a^3 d$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3*(c + d*x)^10,x]

[Out] $a^3c^{10}x + (a^2c^9(3b^3c + 10a^3d)x^2)/2 + a^3c^8(b^2c^2 + 10a^2b^2cd + 15a^2d^2)x^3 + (c^7(b^3c^3 + 30a^2b^2c^2d + 135a^2b^2cd^2 + 120a^3d^3)x^4)/4 + c^6d(2b^3c^3 + 27a^2b^2c^2d + 72a^2b^2cd^2 + 42a^3d^3)x^5 + (3c^5d^2(5b^3c^3 + 40a^2b^2c^2d + 70a^2b^2cd^2 + 28a^3d^3)x^6)/2 + (6c^4d^3(20b^3c^3 + 105a^2b^2c^2d + 126a^2b^2cd^2 + 35a^3d^3)x^7)/7 + (3c^3d^4(35b^3c^3 + 126a^2b^2c^2d + 105a^2b^2cd^2 + 20a^3d^3)x^8)/4 + c^2d^5(28b^3c^3 + 70a^2b^2c^2d + 40a^2b^2cd^2 + 5a^3d^3)x^9 + (cd^6(42b^3c^3 + 72a^2b^2c^2d + 27a^2b^2cd^2 + 2a^3d^3)x^{10})/2 + (d^7(120b^3c^3 + 135a^2b^2c^2d + 30a^2b^2cd^2 + a^3d^3)x^{11})/11 + (b^2d^8(15b^2c^2 + 10a^2bcd + a^2d^2)x^{12})/4 + (b^2d^9(10b^2c + 3a^2d)x^{13})/13 + (b^3d^{10}x^{14})/14$

fricas [B] time = 0.39, size = 594, normalized size = 6.46

$$\frac{1}{14}x^{14}d^{10}b^3 + \frac{10}{13}x^{13}d^9cb^3 + \frac{3}{13}x^{13}d^{10}b^2a + \frac{15}{4}x^{12}d^8c^2b^3 + \frac{5}{2}x^{12}d^9cb^2a + \frac{1}{4}x^{12}d^{10}ba^2 + \frac{120}{11}x^{11}d^7c^3b^3 + \frac{135}{11}x^{11}d^8c^2b^2a +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^10,x, algorithm="fricas")

[Out] $1/14*x^{14}d^{10}b^3 + 10/13*x^{13}d^9c^2b^3 + 3/13*x^{13}d^{10}b^2a + 15/4*x^{12}d^8c^2b^3 + 5/2*x^{12}d^9c^2b^2a + 1/4*x^{12}d^{10}b^2a^2 + 120/11*x^{11}d^7c^3b^3 + 135/11*x^{11}d^8c^2b^2a + 30/11*x^{11}d^9c^2b^2a^2 + 1/11*x^{11}d^{10}a^3 + 21*x^{10}d^6c^4b^3 + 36*x^{10}d^7c^3b^2a + 27/2*x^{10}d^8c^2b^2a^2 + x^{10}d^9c^2a^3 + 28*x^9d^5c^5b^3 + 70*x^9d^6c^4b^2a + 40*x^9d^7c^3b^2a^2 + 5*x^9d^8c^2a^3 + 105/4*x^8d^4c^6b^3 + 189/2*x^8d^5c^5b^2a + 315/4*x^8d^6c^4b^2a^2 + 15*x^8d^7c^3a^3 + 120/7*x^7d^3c^7b^3 + 90*x^7d^4c^6b^2a + 108*x^7d^5c^5b^2a^2 + 30*x^7d^6c^4a^3 + 15/2*x^6d^2c^8b^3 + 60*x^6d^3c^7b^2a + 105*x^6d^4c^6b^2a^2 + 42*x^6d^5c^5a^3 + 2*x^5d^9c^9b^3 + 27*x^5d^2c^8b^2a + 72*x^5d^3c^7b^2a^2 + 42*x^5d^4c^6a^3 + 1/4*x^4c^10b^3 + 15/2*x^4d^9c^9b^2a + 135/4*x^4d^2c^8b^2a^2 + 30*x^4d^3c^7a^3 + x^3c^10b^2a + 10*x^3d^9c^9b^2a^2 + 15*x^3d^2c^8a^3 + 3/2*x^2c^10b^2a^2 + 5*x^2d^9c^9a^3 + x^2c^10a^3$

giac [B] time = 1.28, size = 594, normalized size = 6.46

$$\frac{1}{14}b^3d^{10}x^{14} + \frac{10}{13}b^3cd^9x^{13} + \frac{3}{13}ab^2d^{10}x^{13} + \frac{15}{4}b^3c^2d^8x^{12} + \frac{5}{2}ab^2cd^9x^{12} + \frac{1}{4}a^2bd^{10}x^{12} + \frac{120}{11}b^3c^3d^7x^{11} + \frac{135}{11}ab^2c^2d^8x^{11} +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^10,x, algorithm="giac")

[Out] $1/14*b^3*d^{10}*x^{14} + 10/13*b^3*c*d^9*x^{13} + 3/13*a*b^2*d^{10}*x^{13} + 15/4*b^3*c^2*d^8*x^{12} + 5/2*a*b^2*c*d^9*x^{12} + 1/4*a^2*b*d^{10}*x^{12} + 120/11*b^3*c^3*d^7*x^{11} + 135/11*a*b^2*c^2*d^8*x^{11} + 30/11*a^2*b*c*d^9*x^{11} + 1/11*a^3*d^{10}*x^{11} + 21*b^3*c^4*d^6*x^{10} + 36*a*b^2*c^3*d^7*x^{10} + 27/2*a^2*b*c^2*d^8*x^{10} + a^3*c*d^9*x^{10} + 28*b^3*c^5*d^5*x^9 + 70*a*b^2*c^4*d^6*x^9 + 40*a^2*b*c^3*d^7*x^9 + 5*a^3*c^2*d^8*x^9 + 105/4*b^3*c^6*d^4*x^8 + 189/2*a*b^2*c^5*d^5*x^8 + 315/4*a^2*b*c^4*d^6*x^8 + 15*a^3*c^3*d^7*x^8 + 120/7*b^3*c^7*d^3*x^7 + 90*a*b^2*c^6*d^4*x^7 + 108*a^2*b*c^5*d^5*x^7 + 30*a^3*c^4*d^6*x^7 + 15/2*b^3*c^8*d^2*x^6 + 60*a*b^2*c^7*d^3*x^6 + 105*a^2*b*c^6*d^4*x^6 + 42*a^3*c^5*d^5*x^6 + 2*b^3*c^9*d*x^5 + 27*a*b^2*c^8*d^2*x^5 + 72*a^2*b*c^7*d^3*x^5 + 42*a^3*c^6*d^4*x^5 + 1/4*b^3*c^{10}*x^4 + 15/2*a*b^2*c^9*d*x^4 + 135/4*a^2*b*c^8*d^2*x^4 + 30*a^3*c^7*d^3*x^4 + a*b^2*c^{10}*x^3 + 10*a^2*b*c^9*d*x^3 + 15*a^3*c^8*d^2*x^3 + 3/2*a^2*b*c^{10}*x^2 + 5*a^3*c^9*d*x^2 + a^3*c^{10}*x$

maple [B] time = 0.00, size = 541, normalized size = 5.88

$$\frac{b^3 d^{10} x^{14}}{14} + a^3 c^{10} x + \frac{(3a b^2 d^{10} + 10b^3 c d^9) x^{13}}{13} + \frac{(3a^2 b d^{10} + 30a b^2 c d^9 + 45b^3 c^2 d^8) x^{12}}{12} + \frac{(a^3 d^{10} + 30a^2 b c d^9 + 135a b^2 c^2 d^8 + 120a^2 b^3 c^3 d^7) x^{11}}{11} + \frac{(10a^3 c d^9 + 135a^2 b^2 c^2 d^8 + 360a^2 b^3 c^3 d^7 + 210a^2 b^3 c^4 d^6 + 252a^2 b^3 c^5 d^5) x^9}{8} + \frac{(120a^3 c^2 d^7 + 630a^2 b^2 c^4 d^6 + 756a^2 b^2 c^5 d^5 + 210a^2 b^3 c^6 d^4) x^8}{7} + \frac{(210a^3 c^4 d^6 + 756a^2 b^2 c^5 d^5 + 630a^2 b^2 c^6 d^4 + 120a^2 b^3 c^7 d^3) x^7}{6} + \frac{(252a^3 c^5 d^5 + 630a^2 b^2 c^6 d^4 + 360a^2 b^2 c^7 d^3 + 45a^2 b^3 c^8 d^2) x^6}{5} + \frac{(210a^3 c^6 d^4 + 360a^2 b^2 c^7 d^3 + 135a^2 b^2 c^8 d^2 + 10a^2 b^3 c^9 d) x^5}{4} + \frac{(120a^3 c^7 d^3 + 135a^2 b^2 c^8 d^2 + 30a^2 b^2 c^9 d + b^3 c^{10}) x^4}{3} + \frac{(45a^3 c^8 d^2 + 30a^2 b^2 c^9 d + 3a^2 b^2 c^{10}) x^3}{2} + \frac{(10a^3 c^9 d + 3a^2 b^2 c^{10}) x^2}{2} + a^3 c^{10} x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3*(d*x+c)^10,x)`

[Out] $1/14*b^3*d^{10}*x^{14} + 1/13*(3*a*b^2*d^{10} + 10*b^3*c*d^9)*x^{13} + 1/12*(3*a^2*b*d^{10} + 30*a*b^2*c*d^9 + 45*b^3*c^2*d^8)*x^{12} + 1/11*(a^3*d^{10} + 30*a^2*b*c*d^9 + 135*a*b^2*c^2*d^8 + 120*b^3*c^3*d^7)*x^{11} + 1/10*(10*a^3*c*d^9 + 135*a^2*b*c^2*d^8 + 360*a*b^2*c^3*d^7 + 210*b^3*c^4*d^6)*x^{10} + 1/9*(45*a^3*c^2*d^8 + 360*a^2*b*c^3*d^7 + 630*a*b^2*c^4*d^6 + 252*b^3*c^5*d^5)*x^9 + 1/8*(120*a^3*c^3*d^7 + 630*a^2*b*c^4*d^6 + 756*a*b^2*c^5*d^5 + 210*b^3*c^6*d^4)*x^8 + 1/7*(210*a^3*c^4*d^6 + 756*a^2*b*c^5*d^5 + 630*a*b^2*c^6*d^4 + 120*b^3*c^7*d^3)*x^7 + 1/6*(252*a^3*c^5*d^5 + 630*a^2*b*c^6*d^4 + 360*a*b^2*c^7*d^3 + 45*b^3*c^8*d^2)*x^6 + 1/5*(210*a^3*c^6*d^4 + 360*a^2*b*c^7*d^3 + 135*a*b^2*c^8*d^2 + 10*b^3*c^9*d)*x^5 + 1/4*(120*a^3*c^7*d^3 + 135*a^2*b*c^8*d^2 + 30*a*b^2*c^9*d + b^3*c^{10})*x^4 + 1/3*(45*a^3*c^8*d^2 + 30*a^2*b*c^9*d + 3*a^2*b^2*c^{10})*x^3 + 1/2*(10*a^3*c^9*d + 3*a^2*b^2*c^{10})*x^2 + a^3*c^{10}*x$

maxima [B] time = 1.32, size = 535, normalized size = 5.82

$$\frac{1}{14} b^3 d^{10} x^{14} + a^3 c^{10} x + \frac{1}{13} (10 b^3 c d^9 + 3 a b^2 d^{10}) x^{13} + \frac{1}{4} (15 b^3 c^2 d^8 + 10 a b^2 c d^9 + a^2 b d^{10}) x^{12} + \frac{1}{11} (120 b^3 c^3 d^7 + 135 a b^2 c^2 d^8 + 120 a^2 b^3 c^3 d^7) x^{11} + \frac{1}{10} (10 a^3 c d^9 + 135 a^2 b^2 c^2 d^8 + 360 a^2 b^3 c^3 d^7 + 210 a^2 b^3 c^4 d^6) x^{10} + \frac{1}{9} (45 a^3 c^2 d^8 + 360 a^2 b^2 c^3 d^7 + 630 a^2 b^2 c^4 d^6 + 252 a^2 b^3 c^5 d^5) x^9 + \frac{1}{8} (120 a^3 c^3 d^7 + 630 a^2 b^2 c^4 d^6 + 756 a^2 b^2 c^5 d^5 + 210 a^2 b^3 c^6 d^4) x^8 + \frac{1}{7} (210 a^3 c^4 d^6 + 756 a^2 b^2 c^5 d^5 + 630 a^2 b^2 c^6 d^4 + 120 a^2 b^3 c^7 d^3) x^7 + \frac{1}{6} (252 a^3 c^5 d^5 + 630 a^2 b^2 c^6 d^4 + 360 a^2 b^2 c^7 d^3 + 45 a^2 b^3 c^8 d^2) x^6 + \frac{1}{5} (210 a^3 c^6 d^4 + 360 a^2 b^2 c^7 d^3 + 135 a^2 b^2 c^8 d^2 + 10 a^2 b^3 c^9 d) x^5 + \frac{1}{4} (120 a^3 c^7 d^3 + 135 a^2 b^2 c^8 d^2 + 30 a^2 b^2 c^9 d + b^3 c^{10}) x^4 + \frac{1}{3} (45 a^3 c^8 d^2 + 30 a^2 b^2 c^9 d + 3 a^2 b^2 c^{10}) x^3 + \frac{1}{2} (10 a^3 c^9 d + 3 a^2 b^2 c^{10}) x^2 + a^3 c^{10} x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3*(d*x+c)^10,x, algorithm="maxima")`

[Out] $1/14*b^3*d^{10}*x^{14} + a^3*c^{10}*x + 1/13*(10*b^3*c*d^9 + 3*a*b^2*d^{10})*x^{13} + 1/4*(15*b^3*c^2*d^8 + 10*a*b^2*c*d^9 + a^2*b*d^{10})*x^{12} + 1/11*(120*b^3*c^3*d^7 + 135*a*b^2*c^2*d^8 + 30*a^2*b*c*d^9 + a^3*d^{10})*x^{11} + 1/2*(42*b^3*c$

$$\begin{aligned} &^4d^6 + 72ab^2c^3d^7 + 27a^2b^2c^2d^8 + 2a^3c^2d^9)x^{10} + (28b^3c^5d^5 + 70ab^2c^4d^6 + 40a^2b^2c^3d^7 + 5a^3c^2d^8)x^9 + 3/4(3 \\ &5b^3c^6d^4 + 126ab^2c^5d^5 + 105a^2b^2c^4d^6 + 20a^3c^3d^7)x^8 + 6/7(20b^3c^7d^3 + 105ab^2c^6d^4 + 126a^2b^2c^5d^5 + 35a^3c^4 \\ &d^6)x^7 + 3/2(5b^3c^8d^2 + 40ab^2c^7d^3 + 70a^2b^2c^6d^4 + 28a^3c^5d^5)x^6 + (2b^3c^9d + 27ab^2c^8d^2 + 72a^2b^2c^7d^3 + 42a \\ &^3c^6d^4)x^5 + 1/4(b^3c^{10} + 30ab^2c^9d + 135a^2b^2c^8d^2 + 120a^3c^7d^3)x^4 + (ab^2c^{10} + 10a^2b^2c^9d + 15a^3c^8d^2)x^3 + 1/2 \\ &(3a^2b^2c^{10} + 10a^3c^9d)x^2 \end{aligned}$$

mupad [B] time = 0.23, size = 495, normalized size = 5.38

$$x^4 \left(30a^3c^7d^3 + \frac{135a^2b^2c^8d^2}{4} + \frac{15a^2b^2c^9d}{2} + \frac{b^3c^{10}}{4} \right) + x^{11} \left(\frac{a^3d^{10}}{11} + \frac{30a^2bcd^9}{11} + \frac{135a^2b^2c^2d^8}{11} + \frac{120b^3c^3d^7}{11} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3*(c + d*x)^10,x)

[Out] $x^4((b^3c^{10})/4 + 30a^3c^7d^3 + (135a^2b^2c^8d^2)/4 + (15ab^2c^9d)/2) + x^{11}((a^3d^{10})/11 + (120b^3c^3d^7)/11 + (135a^2b^2c^2d^8)/11 + (30a^2b^2c^9d)/11) + a^3c^{10}x + (b^3d^{10}x^{14})/14 + (3c^5d^2x^6(28a^3d^3 + 5b^3c^3 + 40ab^2c^2d + 70a^2b^2cd^2))/2 + c^2d^5x^9(5a^3d^3 + 28b^3c^3 + 70ab^2c^2d + 40a^2b^2cd^2) + (6c^4d^3x^7(35a^3d^3 + 20b^3c^3 + 105ab^2c^2d + 126a^2b^2cd^2))/7 + (3c^3d^4x^8(20a^3d^3 + 35b^3c^3 + 126ab^2c^2d + 105a^2b^2cd^2))/4 + (a^2c^9x^2(10ad + 3bc))/2 + (b^2d^9x^{13}(3ad + 10bc))/13 + ac^8x^3(15a^2d^2 + b^2c^2 + 10abc^2d) + (bd^8x^{12}(a^2d^2 + 15b^2c^2 + 10abc^2d))/4 + c^6d^5x^5(42a^3d^3 + 2b^3c^3 + 27ab^2c^2d + 72a^2b^2cd^2) + (c^6d^6x^{10}(2a^3d^3 + 42b^3c^3 + 72ab^2c^2d + 27a^2b^2cd^2))/2$

sympy [B] time = 0.16, size = 586, normalized size = 6.37

$$a^3c^{10}x + \frac{b^3d^{10}x^{14}}{14} + x^{13} \left(\frac{3ab^2d^{10}}{13} + \frac{10b^3cd^9}{13} \right) + x^{12} \left(\frac{a^2bd^{10}}{4} + \frac{5ab^2cd^9}{2} + \frac{15b^3c^2d^8}{4} \right) + x^{11} \left(\frac{a^3d^{10}}{11} + \frac{30a^2bcd^9}{11} + \frac{135a^2b^2c^2d^8}{11} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3*(d*x+c)**10,x)

[Out] $a^{**3}c^{**10}x + b^{**3}d^{**10}x^{**14}/14 + x^{**13}(3a*b^{**2}d^{**10}/13 + 10*b^{**3}c*d^{**9}/13) + x^{**12}(a^{**2}b*d^{**10}/4 + 5*a*b^{**2}c*d^{**9}/2 + 15*b^{**3}c^{**2}d^{**8}/4) + x^{**11}(a^{**3}d^{**10}/11 + 30*a^{**2}b*c*d^{**9}/11 + 135*a*b^{**2}c^{**2}d^{**8}/11 + 120*b^{**3}c^{**3}d^{**7}/11) + x^{**10}(a^{**3}c*d^{**9} + 27*a^{**2}b*c^{**2}d^{**8}/2 + 36*a*b^{**2}c^{**3}d^{**7} + 21*b^{**3}c^{**4}d^{**6}) + x^{**9}(5*a^{**3}c^{**2}d^{**8} + 40*a^{**2}b*c^{**3}d^{**7} + 105*a*b^{**2}c^{**4}d^{**6} + 126*a^2b^2cd^5)x^8 + 3/2(5b^3c^8d^2 + 40ab^2c^7d^3 + 70a^2b^2c^6d^4 + 28a^3c^5d^5)x^6 + (2b^3c^9d + 27ab^2c^8d^2 + 72a^2b^2c^7d^3 + 42a^3c^6d^4)x^5 + 1/4(b^3c^{10} + 30ab^2c^9d + 135a^2b^2c^8d^2 + 120a^3c^7d^3)x^4 + (ab^2c^{10} + 10a^2b^2c^9d + 15a^3c^8d^2)x^3 + 1/2(3a^2b^2c^{10} + 10a^3c^9d)x^2$

$$\begin{aligned}
& *d^{**7} + 70*a*b^{**2}*c^{**4}*d^{**6} + 28*b^{**3}*c^{**5}*d^{**5}) + x^{**8}*(15*a^{**3}*c^{**3}*d^{**7} \\
& + 315*a^{**2}*b*c^{**4}*d^{**6}/4 + 189*a*b^{**2}*c^{**5}*d^{**5}/2 + 105*b^{**3}*c^{**6}*d^{**4}/4) + \\
& x^{**7}*(30*a^{**3}*c^{**4}*d^{**6} + 108*a^{**2}*b*c^{**5}*d^{**5} + 90*a*b^{**2}*c^{**6}*d^{**4} + 120 \\
& *b^{**3}*c^{**7}*d^{**3}/7) + x^{**6}*(42*a^{**3}*c^{**5}*d^{**5} + 105*a^{**2}*b*c^{**6}*d^{**4} + 60*a* \\
& b^{**2}*c^{**7}*d^{**3} + 15*b^{**3}*c^{**8}*d^{**2}/2) + x^{**5}*(42*a^{**3}*c^{**6}*d^{**4} + 72*a^{**2}*b \\
& *c^{**7}*d^{**3} + 27*a*b^{**2}*c^{**8}*d^{**2} + 2*b^{**3}*c^{**9}*d) + x^{**4}*(30*a^{**3}*c^{**7}*d^{**3} \\
& + 135*a^{**2}*b*c^{**8}*d^{**2}/4 + 15*a*b^{**2}*c^{**9}*d/2 + b^{**3}*c^{**10}/4) + x^{**3}*(15*a \\
& **3*c^{**8}*d^{**2} + 10*a^{**2}*b*c^{**9}*d + a*b^{**2}*c^{**10}) + x^{**2}*(5*a^{**3}*c^{**9}*d + 3* \\
& a^{**2}*b*c^{**10}/2)
\end{aligned}$$

3.1309 $\int (a + bx)^2 (c + dx)^{10} dx$

Optimal. Leaf size=65

$$-\frac{b(c+dx)^{12}(bc-ad)}{6d^3} + \frac{(c+dx)^{11}(bc-ad)^2}{11d^3} + \frac{b^2(c+dx)^{13}}{13d^3}$$

[Out] $1/11*(-a*d+b*c)^2*(d*x+c)^{11}/d^3-1/6*b*(-a*d+b*c)*(d*x+c)^{12}/d^3+1/13*b^2*(d*x+c)^{13}/d^3$

Rubi [A] time = 0.25, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{b(c+dx)^{12}(bc-ad)}{6d^3} + \frac{(c+dx)^{11}(bc-ad)^2}{11d^3} + \frac{b^2(c+dx)^{13}}{13d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(c + d*x)^10, x]

[Out] $((b*c - a*d)^2*(c + d*x)^{11}/(11*d^3) - (b*(b*c - a*d)*(c + d*x)^{12})/(6*d^3) + (b^2*(c + d*x)^{13})/(13*d^3))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2 (c + dx)^{10} dx &= \int \left(\frac{(-bc + ad)^2 (c + dx)^{10}}{d^2} - \frac{2b(bc - ad)(c + dx)^{11}}{d^2} + \frac{b^2(c + dx)^{12}}{d^2} \right) dx \\ &= \frac{(bc - ad)^2 (c + dx)^{11}}{11d^3} - \frac{b(bc - ad)(c + dx)^{12}}{6d^3} + \frac{b^2(c + dx)^{13}}{13d^3} \end{aligned}$$

Mathematica [B] time = 0.05, size = 358, normalized size = 5.51

$$\frac{1}{11}d^8x^{11}(a^2d^2 + 20abcd + 45b^2c^2) + cd^7x^{10}(a^2d^2 + 9abcd + 12b^2c^2) + \frac{5}{3}c^2d^6x^9(3a^2d^2 + 16abcd + 14b^2c^2) + \frac{1}{3}c^8x^3$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(c + d*x)^10,x]

[Out] $a^2c^{10}x + ac^9(b^2c + 5ad)x^2 + (c^8(b^2c^2 + 20ab^2cd + 45a^2d^2)x^3)/3 + (5c^7d(b^2c^2 + 9ab^2cd + 12a^2d^2)x^4)/2 + 3c^6d^2(3b^2c^2 + 16ab^2cd + 14a^2d^2)x^5 + 2c^5d^3(10b^2c^2 + 35ab^2cd + 21a^2d^2)x^6 + 6c^4d^4(5b^2c^2 + 12ab^2cd + 5a^2d^2)x^7 + (3c^3d^5(21b^2c^2 + 35ab^2cd + 10a^2d^2)x^8)/2 + (5c^2d^6(14b^2c^2 + 16ab^2cd + 3a^2d^2)x^9)/3 + cd^7(12b^2c^2 + 9ab^2cd + a^2d^2)x^{10} + (d^8(45b^2c^2 + 20ab^2cd + a^2d^2)x^{11})/11 + (bd^9(5b^2c + ad)x^{12})/6 + (b^2d^{10}x^{13})/13$

fricas [B] time = 0.39, size = 417, normalized size = 6.42

$$\frac{1}{13}x^{13}d^{10}b^2 + \frac{5}{6}x^{12}d^9cb^2 + \frac{1}{6}x^{12}d^{10}ba + \frac{45}{11}x^{11}d^8c^2b^2 + \frac{20}{11}x^{11}d^9cba + \frac{1}{11}x^{11}d^{10}a^2 + 12x^{10}d^7c^3b^2 + 9x^{10}d^8c^2ba + x^{10}d^9ca^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^10,x, algorithm="fricas")

[Out] $1/13*x^{13}*d^{10}*b^2 + 5/6*x^{12}*d^9*c*b^2 + 1/6*x^{12}*d^{10}*b*a + 45/11*x^{11}*d^8*c^2*b^2 + 20/11*x^{11}*d^9*c*b*a + 1/11*x^{11}*d^{10}*a^2 + 12*x^{10}*d^7*c^3*b^2 + 9*x^{10}*d^8*c^2*b*a + x^{10}*d^9*c*a^2 + 70/3*x^9*d^6*c^4*b^2 + 80/3*x^9*d^7*c^3*b*a + 5*x^9*d^8*c^2*a^2 + 63/2*x^8*d^5*c^5*b^2 + 105/2*x^8*d^6*c^4*b*a + 15*x^8*d^7*c^3*a^2 + 30*x^7*d^4*c^6*b^2 + 72*x^7*d^5*c^5*b*a + 30*x^7*d^6*c^4*a^2 + 20*x^6*d^3*c^7*b^2 + 70*x^6*d^4*c^6*b*a + 42*x^6*d^5*c^5*a^2 + 9*x^5*d^2*c^8*b^2 + 48*x^5*d^3*c^7*b*a + 42*x^5*d^4*c^6*a^2 + 5/2*x^4*d*c^9*b^2 + 45/2*x^4*d^2*c^8*b*a + 30*x^4*d^3*c^7*a^2 + 1/3*x^3*c^10*b^2 + 20/3*x^3*d*c^9*b*a + 15*x^3*d^2*c^8*a^2 + x^2*c^10*b*a + 5*x^2*d*c^9*a^2 + x*c^10*a^2$

giac [B] time = 1.26, size = 417, normalized size = 6.42

$$\frac{1}{13}b^2d^{10}x^{13} + \frac{5}{6}b^2cd^9x^{12} + \frac{1}{6}abd^{10}x^{12} + \frac{45}{11}b^2c^2d^8x^{11} + \frac{20}{11}abcd^9x^{11} + \frac{1}{11}a^2d^{10}x^{11} + 12b^2c^3d^7x^{10} + 9abc^2d^8x^{10} + a^2cd^9x^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^10,x, algorithm="giac")

[Out] $1/13*b^2*d^{10}*x^{13} + 5/6*b^2*c*d^9*x^{12} + 1/6*a*b*d^{10}*x^{12} + 45/11*b^2*c^2*d^8*x^{11} + 20/11*a*b*c*d^9*x^{11} + 1/11*a^2*d^{10}*x^{11} + 12*b^2*c^3*d^7*x^{10} + 9*a*b*c^2*d^8*x^{10} + a^2*c*d^9*x^{10} + 70/3*b^2*c^4*d^6*x^9 + 80/3*a*b*c^3*d^7*x^9 + 5*a^2*c^2*d^8*x^9 + 63/2*b^2*c^5*d^5*x^8 + 105/2*a*b*c^4*d^6*x^8 + 15*a^2*c^3*d^7*x^8 + 30*b^2*c^6*d^4*x^7 + 72*a*b*c^5*d^5*x^7 + 30*a^2*c^4*d^6*x^7 + 21*a*b*c^4*d^6*x^7 + 105/2*a*b*c^4*d^6*x^7 + 30*a^2*c^4*d^6*x^7 + 9*x^5*d^2*c^8*b^2 + 48*x^5*d^3*c^7*b*a + 42*x^5*d^4*c^6*a^2 + 5/2*x^4*d*c^9*b^2 + 45/2*x^4*d^2*c^8*b*a + 30*x^4*d^3*c^7*a^2 + 1/3*x^3*c^10*b^2 + 20/3*x^3*d*c^9*b*a + 15*x^3*d^2*c^8*a^2 + x^2*c^10*b*a + 5*x^2*d*c^9*a^2 + x*c^10*a^2$

$$\begin{aligned} &4d^6x^7 + 20b^2c^7d^3x^6 + 70a*b*c^6d^4x^6 + 42a^2c^5d^5x^6 + \\ &9b^2c^8d^2x^5 + 48a*b*c^7d^3x^5 + 42a^2c^6d^4x^5 + 5/2b^2c^9* \\ &d*x^4 + 45/2a*b*c^8*d^2*x^4 + 30a^2c^7*d^3*x^4 + 1/3b^2c^{10}*x^3 + 20/3 \\ &*a*b*c^9*d*x^3 + 15a^2c^8*d^2*x^3 + a*b*c^{10}*x^2 + 5a^2c^9*d*x^2 + a^2* \\ &c^{10}*x \end{aligned}$$

maple [B] time = 0.00, size = 391, normalized size = 6.02

$$\frac{b^2d^{10}x^{13}}{13} + a^2c^{10}x + \frac{(2abd^{10} + 10b^2cd^9)x^{12}}{12} + \frac{(a^2d^{10} + 20abcd^9 + 45b^2c^2d^8)x^{11}}{11} + \frac{(10a^2cd^9 + 90abc^2d^8 + 120b^2c^3d^7)x^{10}}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(d*x+c)^10,x)

[Out] 1/13*b^2*d^10*x^13+1/12*(2*a*b*d^10+10*b^2*c*d^9)*x^12+1/11*(a^2*d^10+20*a*b*c*d^9+45*b^2*c^2*d^8)*x^11+1/10*(10*a^2*c*d^9+90*a*b*c^2*d^8+120*b^2*c^3*d^7)*x^10+1/9*(45*a^2*c^2*d^8+240*a*b*c^3*d^7+210*b^2*c^4*d^6)*x^9+1/8*(120*a^2*c^3*d^7+420*a*b*c^4*d^6+252*b^2*c^5*d^5)*x^8+1/7*(210*a^2*c^4*d^6+504*a*b*c^5*d^5+210*b^2*c^6*d^4)*x^7+1/6*(252*a^2*c^5*d^5+420*a*b*c^6*d^4+120*b^2*c^7*d^3)*x^6+1/5*(210*a^2*c^6*d^4+240*a*b*c^7*d^3+45*b^2*c^8*d^2)*x^5+1/4*(120*a^2*c^7*d^3+90*a*b*c^8*d^2+10*b^2*c^9*d)*x^4+1/3*(45*a^2*c^8*d^2+20*a*b*c^9*d+b^2*c^10)*x^3+1/2*(10*a^2*c^9*d+2*a*b*c^10)*x^2+a^2*c^10*x

maxima [B] time = 1.33, size = 384, normalized size = 5.91

$$\frac{1}{13}b^2d^{10}x^{13} + a^2c^{10}x + \frac{1}{6}(5b^2cd^9 + abd^{10})x^{12} + \frac{1}{11}(45b^2c^2d^8 + 20abcd^9 + a^2d^{10})x^{11} + (12b^2c^3d^7 + 9abc^2d^8 + a^2cd^9)x^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^10,x, algorithm="maxima")

[Out] 1/13*b^2*d^10*x^13 + a^2*c^10*x + 1/6*(5*b^2*c*d^9 + a*b*d^10)*x^12 + 1/11*(45*b^2*c^2*d^8 + 20*a*b*c*d^9 + a^2*d^10)*x^11 + (12*b^2*c^3*d^7 + 9*a*b*c^2*d^8 + a^2*c*d^9)*x^10 + 5/3*(14*b^2*c^4*d^6 + 16*a*b*c^3*d^7 + 3*a^2*c^2*d^8)*x^9 + 3/2*(21*b^2*c^5*d^5 + 35*a*b*c^4*d^6 + 10*a^2*c^3*d^7)*x^8 + 6*(5*b^2*c^6*d^4 + 12*a*b*c^5*d^5 + 5*a^2*c^4*d^6)*x^7 + 2*(10*b^2*c^7*d^3 + 35*a*b*c^6*d^4 + 21*a^2*c^5*d^5)*x^6 + 3*(3*b^2*c^8*d^2 + 16*a*b*c^7*d^3 + 14*a^2*c^6*d^4)*x^5 + 5/2*(b^2*c^9*d + 9*a*b*c^8*d^2 + 12*a^2*c^7*d^3)*x^4 + 1/3*(b^2*c^10 + 20*a*b*c^9*d + 45*a^2*c^8*d^2)*x^3 + (a*b*c^10 + 5*a^2*c^9*d)*x^2

mupad [B] time = 0.32, size = 348, normalized size = 5.35

$$x^3 \left(15a^2c^8d^2 + \frac{20abc^9d}{3} + \frac{b^2c^{10}}{3} \right) + x^{11} \left(\frac{a^2d^{10}}{11} + \frac{20abcd^9}{11} + \frac{45b^2c^2d^8}{11} \right) + a^2c^{10}x + \frac{b^2d^{10}x^{13}}{13} + ac^9x^2 (5ad^9)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2*(c + d*x)^10,x)`

[Out] $x^3*((b^2*c^{10})/3 + 15*a^2*c^8*d^2 + (20*a*b*c^9*d)/3) + x^{11}*((a^2*d^{10})/11 + (45*b^2*c^2*d^8)/11 + (20*a*b*c*d^9)/11) + a^2*c^{10}*x + (b^2*d^{10}*x^{13})/13 + a*c^9*x^2*(5*a*d + b*c) + (b*d^9*x^{12}*(a*d + 5*b*c))/6 + (5*c^7*d*x^4*(12*a^2*d^2 + b^2*c^2 + 9*a*b*c*d))/2 + c*d^7*x^{10}*(a^2*d^2 + 12*b^2*c^2 + 9*a*b*c*d) + 6*c^4*d^4*x^7*(5*a^2*d^2 + 5*b^2*c^2 + 12*a*b*c*d) + 3*c^6*d^2*x^5*(14*a^2*d^2 + 3*b^2*c^2 + 16*a*b*c*d) + (5*c^2*d^6*x^9*(3*a^2*d^2 + 14*b^2*c^2 + 16*a*b*c*d))/3 + 2*c^5*d^3*x^6*(21*a^2*d^2 + 10*b^2*c^2 + 35*a*b*c*d) + (3*c^3*d^5*x^8*(10*a^2*d^2 + 21*b^2*c^2 + 35*a*b*c*d))/2$

sympy [B] time = 0.14, size = 415, normalized size = 6.38

$$a^2c^{10}x + \frac{b^2d^{10}x^{13}}{13} + x^{12}\left(\frac{abd^{10}}{6} + \frac{5b^2cd^9}{6}\right) + x^{11}\left(\frac{a^2d^{10}}{11} + \frac{20abcd^9}{11} + \frac{45b^2c^2d^8}{11}\right) + x^{10}(a^2cd^9 + 9abc^2d^8 + 12b^2c^3d^7)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(d*x+c)**10,x)`

[Out] $a^{**2}*c^{**10}*x + b^{**2}*d^{**10}*x^{**13}/13 + x^{**12}*(a*b*d^{**10}/6 + 5*b^{**2}*c*d^{**9}/6) + x^{**11}*(a^{**2}*d^{**10}/11 + 20*a*b*c*d^{**9}/11 + 45*b^{**2}*c^{**2}*d^{**8}/11) + x^{**10}*(a^{**2}*c*d^{**9} + 9*a*b*c^{**2}*d^{**8} + 12*b^{**2}*c^{**3}*d^{**7}) + x^{**9}*(5*a^{**2}*c^{**2}*d^{**8} + 80*a*b*c^{**3}*d^{**7}/3 + 70*b^{**2}*c^{**4}*d^{**6}/3) + x^{**8}*(15*a^{**2}*c^{**3}*d^{**7} + 10*5*a*b*c^{**4}*d^{**6}/2 + 63*b^{**2}*c^{**5}*d^{**5}/2) + x^{**7}*(30*a^{**2}*c^{**4}*d^{**6} + 72*a*b*c^{**5}*d^{**5} + 30*b^{**2}*c^{**6}*d^{**4}) + x^{**6}*(42*a^{**2}*c^{**5}*d^{**5} + 70*a*b*c^{**6}*d^{**4} + 20*b^{**2}*c^{**7}*d^{**3}) + x^{**5}*(42*a^{**2}*c^{**6}*d^{**4} + 48*a*b*c^{**7}*d^{**3} + 9*b^{**2}*c^{**8}*d^{**2}) + x^{**4}*(30*a^{**2}*c^{**7}*d^{**3} + 45*a*b*c^{**8}*d^{**2}/2 + 5*b^{**2}*c^{**9}*d/2) + x^{**3}*(15*a^{**2}*c^{**8}*d^{**2} + 20*a*b*c^{**9}*d/3 + b^{**2}*c^{**10}/3) + x^{**2}*(5*a^{**2}*c^{**9}*d + a*b*c^{**10})$

3.1310 $\int (a + bx)(c + dx)^{10} dx$

Optimal. Leaf size=38

$$\frac{b(c + dx)^{12}}{12d^2} - \frac{(c + dx)^{11}(bc - ad)}{11d^2}$$

[Out] $-1/11*(-a*d+b*c)*(d*x+c)^{11}/d^2+1/12*b*(d*x+c)^{12}/d^2$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{b(c + dx)^{12}}{12d^2} - \frac{(c + dx)^{11}(bc - ad)}{11d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(c + d*x)^10,x]

[Out] $-((b*c - a*d)*(c + d*x)^{11})/(11*d^2) + (b*(c + d*x)^{12})/(12*d^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)(c + dx)^{10} dx &= \int \left(\frac{(-bc + ad)(c + dx)^{10}}{d} + \frac{b(c + dx)^{11}}{d} \right) dx \\ &= -\frac{(bc - ad)(c + dx)^{11}}{11d^2} + \frac{b(c + dx)^{12}}{12d^2} \end{aligned}$$

Mathematica [B] time = 0.03, size = 220, normalized size = 5.79

$$\frac{1}{2}c^9x^2(10ad+bc)+\frac{5}{3}c^8dx^3(9ad+2bc)+\frac{15}{4}c^7d^2x^4(8ad+3bc)+6c^6d^3x^5(7ad+4bc)+7c^5d^4x^6(6ad+5bc)+6c^4d^5x^7(5ad+$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(c + d*x)^10,x]

[Out] $a*c^{10}*x + (c^9*(b*c + 10*a*d)*x^2)/2 + (5*c^8*d*(2*b*c + 9*a*d)*x^3)/3 + (15*c^7*d^2*(3*b*c + 8*a*d)*x^4)/4 + 6*c^6*d^3*(4*b*c + 7*a*d)*x^5 + 7*c^5*d^4*(5*b*c + 6*a*d)*x^6 + 6*c^4*d^5*(6*b*c + 5*a*d)*x^7 + (15*c^3*d^6*(7*b*c + 4*a*d)*x^8)/4 + (5*c^2*d^7*(8*b*c + 3*a*d)*x^9)/3 + (c*d^8*(9*b*c + 2*a*d)*x^{10})/2 + (d^9*(10*b*c + a*d)*x^{11})/11 + (b*d^{10}*x^{12})/12$

fricas [B] time = 0.38, size = 241, normalized size = 6.34

$$\frac{1}{12}x^{12}d^{10}b + \frac{10}{11}x^{11}d^9cb + \frac{1}{11}x^{11}d^{10}a + \frac{9}{2}x^{10}d^8c^2b + x^{10}d^9ca + \frac{40}{3}x^9d^7c^3b + 5x^9d^8c^2a + \frac{105}{4}x^8d^6c^4b + 15x^8d^7c^3a + 36x^7d^5c^5b + 30x^7d^6c^4a + 35x^6d^4c^6b + 42x^6d^5c^5a + 24x^5d^3c^7b + 42x^5d^4c^6a + 45/4x^4d^2c^8b + 30x^4d^3c^7a + 10/3x^3d^2c^9b + 15x^3d^2c^8a + 1/2x^2d^2c^10b + 5x^2d^2c^9a + xc^{10}a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c)^10,x, algorithm="fricas")`

[Out] $1/12*x^{12}*d^{10}*b + 10/11*x^{11}*d^9*c*b + 1/11*x^{11}*d^{10}*a + 9/2*x^{10}*d^8*c^2*b + x^{10}*d^9*c*a + 40/3*x^9*d^7*c^3*b + 5*x^9*d^8*c^2*a + 105/4*x^8*d^6*c^4*b + 15*x^8*d^7*c^3*a + 36*x^7*d^5*c^5*b + 30*x^7*d^6*c^4*a + 35*x^6*d^4*c^6*b + 42*x^6*d^5*c^5*a + 24*x^5*d^3*c^7*b + 42*x^5*d^4*c^6*a + 45/4*x^4*d^2*c^8*b + 30*x^4*d^3*c^7*a + 10/3*x^3*d^2*c^9*b + 15*x^3*d^2*c^8*a + 1/2*x^2*d^2*c^10*b + 5*x^2*d^2*c^9*a + x*c^{10}a$

giac [B] time = 1.26, size = 241, normalized size = 6.34

$$\frac{1}{12}bd^{10}x^{12} + \frac{10}{11}bcd^9x^{11} + \frac{1}{11}ad^{10}x^{11} + \frac{9}{2}bc^2d^8x^{10} + acd^9x^{10} + \frac{40}{3}bc^3d^7x^9 + 5ac^2d^8x^9 + \frac{105}{4}bc^4d^6x^8 + 15ac^3d^7x^8 + 36x^7d^5c^5b + 30x^7d^6c^4a + 35x^6d^4c^6b + 42x^6d^5c^5a + 24x^5d^3c^7b + 42x^5d^4c^6a + 45/4x^4d^2c^8b + 30x^4d^3c^7a + 10/3x^3d^2c^9b + 15x^3d^2c^8a + 1/2x^2d^2c^10b + 5x^2d^2c^9a + xc^{10}a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)*(d*x+c)^10,x, algorithm="giac")`

[Out] $1/12*b*d^{10}*x^{12} + 10/11*b*c*d^9*x^{11} + 1/11*a*d^{10}*x^{11} + 9/2*b*c^2*d^8*x^{10} + a*c*d^9*x^{10} + 40/3*b*c^3*d^7*x^9 + 5*a*c^2*d^8*x^9 + 105/4*b*c^4*d^6*x^8 + 15*a*c^3*d^7*x^8 + 36*b*c^5*d^5*x^7 + 30*a*c^4*d^6*x^7 + 35*b*c^6*d^4*x^6 + 42*a*c^5*d^5*x^6 + 24*b*c^7*d^3*x^5 + 42*a*c^6*d^4*x^5 + 45/4*b*c^8*d^2*x^4 + 30*a*c^7*d^3*x^4 + 10/3*b*c^9*d*x^3 + 15*a*c^8*d^2*x^3 + 1/2*b*c^{10}*x^2 + 5*a*c^9*d*x^2 + a*c^{10}*x$

maple [B] time = 0.00, size = 241, normalized size = 6.34

$$\frac{bd^{10}x^{12}}{12} + ac^{10}x + \frac{(ad^{10} + 10bcd^9)x^{11}}{11} + \frac{(10acd^9 + 45bc^2d^8)x^{10}}{10} + \frac{(45ac^2d^8 + 120bc^3d^7)x^9}{9} + \frac{(120ac^3d^7 + 210b^2c^4d^6)x^8}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)*(d*x+c)^10,x)`

[Out] $\frac{1}{12}bd^{10}x^{12} + \frac{1}{11}(ad^{10} + 10b^2cd^9)x^{11} + \frac{1}{10}(10a^2cd^9 + 45b^2c^2d^8)x^{10} + \frac{1}{9}(45a^2c^2d^8 + 120b^2c^3d^7)x^9 + \frac{1}{8}(120a^2c^3d^7 + 210b^2c^4d^6)x^8 + \frac{1}{7}(210a^2c^4d^6 + 252b^2c^5d^5)x^7 + \frac{1}{6}(252a^2c^5d^5 + 210b^2c^6d^4)x^6 + \frac{1}{5}(210a^2c^6d^4 + 120b^2c^7d^3)x^5 + \frac{1}{4}(120a^2c^7d^3 + 45b^2c^8d^2)x^4 + \frac{1}{3}(45a^2c^8d^2 + 10b^2c^9d)x^3 + \frac{1}{2}(10a^2c^9d + b^2c^{10})x^2 + a^2c^{10}x$

maxima [B] time = 1.43, size = 240, normalized size = 6.32

$$\frac{1}{12}bd^{10}x^{12} + ac^{10}x + \frac{1}{11}(10bcd^9 + ad^{10})x^{11} + \frac{1}{2}(9bc^2d^8 + 2acd^9)x^{10} + \frac{5}{3}(8bc^3d^7 + 3ac^2d^8)x^9 + \frac{15}{4}(7bc^4d^6 + 4ac^3d^5)x^8 + \frac{7}{2}(6bc^5d^5 + 5a^2c^4d^6)x^7 + \frac{7}{2}(5bc^6d^4 + 6a^2c^5d^5)x^6 + \frac{6}{5}(4bc^7d^3 + 7a^2c^6d^4)x^5 + \frac{15}{4}(3bc^8d^2 + 8a^2c^7d^3)x^4 + \frac{5}{3}(2bc^9d + 9a^2c^8d^2)x^3 + \frac{1}{2}(b^2c^{10} + 10a^2c^9d)x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^10,x, algorithm="maxima")

[Out] $\frac{1}{12}bd^{10}x^{12} + a^2c^{10}x + \frac{1}{11}(10b^2cd^9 + a^2d^{10})x^{11} + \frac{1}{2}(9b^2c^2d^8 + 2a^2c^2d^9)x^{10} + \frac{5}{3}(8b^2c^3d^7 + 3a^2c^2d^8)x^9 + \frac{15}{4}(7b^2c^4d^6 + 4a^2c^3d^7)x^8 + \frac{7}{2}(6b^2c^5d^5 + 5a^2c^4d^6)x^7 + \frac{7}{2}(5b^2c^6d^4 + 6a^2c^5d^5)x^6 + \frac{6}{5}(4b^2c^7d^3 + 7a^2c^6d^4)x^5 + \frac{15}{4}(3b^2c^8d^2 + 8a^2c^7d^3)x^4 + \frac{5}{3}(2b^2c^9d + 9a^2c^8d^2)x^3 + \frac{1}{2}(b^2c^{10} + 10a^2c^9d)x^2$

mupad [B] time = 0.13, size = 208, normalized size = 5.47

$$x^2 \left(\frac{bc^{10}}{2} + 5ad^9c \right) + x^{11} \left(\frac{ad^{10}}{11} + \frac{10bcd^9}{11} \right) + \frac{bd^{10}x^{12}}{12} + ac^{10}x + \frac{5c^8dx^3(9ad+2bc)}{3} + \frac{cd^8x^{10}(2ad+9bc)}{2} + \frac{7c^7d^2x^4(8ad+3bc)}{4} + \frac{6c^6d^3x^5(7ad+4bc)}{5} + \frac{7c^5d^4x^6(6ad+5bc)}{6} + \frac{6c^4d^5x^7(5ad+6bc)}{7} + \frac{15c^3d^6x^8(4ad+7bc)}{4} + \frac{5c^2d^7x^9(3ad+8bc)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)*(c + d*x)^10,x)

[Out] $x^2 \left(\frac{b^2c^{10}}{2} + 5a^2c^9d \right) + x^{11} \left(\frac{a^2d^{10}}{11} + \frac{10b^2cd^9}{11} \right) + \frac{bd^{10}x^{12}}{12} + a^2c^{10}x + \frac{5c^8d^2x^3(9ad+2bc)}{3} + \frac{c^2d^8x^{10}(2ad+9bc)}{2} + \frac{15c^7d^2x^4(8ad+3bc)}{4} + \frac{6c^6d^3x^5(7ad+4bc)}{5} + \frac{7c^5d^4x^6(6ad+5bc)}{6} + \frac{6c^4d^5x^7(5ad+6bc)}{7} + \frac{15c^3d^6x^8(4ad+7bc)}{4} + \frac{5c^2d^7x^9(3ad+8bc)}{3}$

sympy [B] time = 0.12, size = 248, normalized size = 6.53

$$ac^{10}x + \frac{bd^{10}x^{12}}{12} + x^{11} \left(\frac{ad^{10}}{11} + \frac{10bcd^9}{11} \right) + x^{10} \left(acd^9 + \frac{9bc^2d^8}{2} \right) + x^9 \left(5ac^2d^8 + \frac{40bc^3d^7}{3} \right) + x^8 \left(15ac^3d^7 + \frac{105bc^4d^6}{4} \right) + x^7 \left(7ac^4d^6 + \frac{42bc^5d^5}{5} \right) + x^6 \left(6ac^5d^5 + \frac{30bc^6d^4}{6} \right) + x^5 \left(5ac^6d^4 + \frac{20bc^7d^3}{7} \right) + x^4 \left(4ac^7d^3 + \frac{10bc^8d^2}{8} \right) + x^3 \left(3ac^8d^2 + \frac{5bc^9d}{9} \right) + x^2 \left(2ac^9d + \frac{bc^{10}}{10} \right) + ac^{10}x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)**10,x)

```
[Out] a*c**10*x + b*d**10*x**12/12 + x**11*(a*d**10/11 + 10*b*c*d**9/11) + x**10*(a*c*d**9 + 9*b*c**2*d**8/2) + x**9*(5*a*c**2*d**8 + 40*b*c**3*d**7/3) + x**8*(15*a*c**3*d**7 + 105*b*c**4*d**6/4) + x**7*(30*a*c**4*d**6 + 36*b*c**5*d**5) + x**6*(42*a*c**5*d**5 + 35*b*c**6*d**4) + x**5*(42*a*c**6*d**4 + 24*b*c**7*d**3) + x**4*(30*a*c**7*d**3 + 45*b*c**8*d**2/4) + x**3*(15*a*c**8*d**2 + 10*b*c**9*d/3) + x**2*(5*a*c**9*d + b*c**10/2)
```

3.1311 $\int (c + dx)^{10} dx$

Optimal. Leaf size=14

$$\frac{(c + dx)^{11}}{11d}$$

[Out] 1/11*(d*x+c)^11/d

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(c + dx)^{11}}{11d}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10,x]

[Out] (c + d*x)^11/(11*d)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (c + dx)^{10} dx = \frac{(c + dx)^{11}}{11d}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{(c + dx)^{11}}{11d}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10,x]

[Out] (c + d*x)^11/(11*d)

fricas [B] time = 0.36, size = 108, normalized size = 7.71

$$\frac{1}{11}x^{11}d^{10} + x^{10}d^9c + 5x^9d^8c^2 + 15x^8d^7c^3 + 30x^7d^6c^4 + 42x^6d^5c^5 + 42x^5d^4c^6 + 30x^4d^3c^7 + 15x^3d^2c^8 + 5x^2dc^9 + xc^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10,x, algorithm="fricas")

[Out] $1/11*x^{11}*d^{10} + x^{10}*d^9*c + 5*x^9*d^8*c^2 + 15*x^8*d^7*c^3 + 30*x^7*d^6*c^4 + 42*x^6*d^5*c^5 + 42*x^5*d^4*c^6 + 30*x^4*d^3*c^7 + 15*x^3*d^2*c^8 + 5*x^2*d*c^9 + x*c^{10}$

giac [A] time = 1.28, size = 12, normalized size = 0.86

$$\frac{(dx + c)^{11}}{11d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10,x, algorithm="giac")

[Out] $1/11*(d*x + c)^{11}/d$

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{(dx + c)^{11}}{11d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10,x)

[Out] $1/11*(d*x+c)^{11}/d$

maxima [A] time = 1.37, size = 12, normalized size = 0.86

$$\frac{(dx + c)^{11}}{11d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10,x, algorithm="maxima")

[Out] $1/11*(d*x + c)^{11}/d$

mupad [B] time = 0.08, size = 108, normalized size = 7.71

$c^{10}x + 5c^9dx^2 + 15c^8d^2x^3 + 30c^7d^3x^4 + 42c^6d^4x^5 + 42c^5d^5x^6 + 30c^4d^6x^7 + 15c^3d^7x^8 + 5c^2d^8x^9 + cd^9x^{10} + \frac{d^{10}x^{11}}{11}$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^10,x)`

[Out] $c^{10}x + (d^{10}x^{11})/11 + 5c^9d^2x^2 + c^9d^2x^2 + 15c^8d^2x^3 + 30c^7d^3x^4 + 42c^6d^4x^5 + 42c^5d^5x^6 + 30c^4d^6x^7 + 15c^3d^7x^8 + 5c^2d^8x^9$

sympy [B] time = 0.09, size = 114, normalized size = 8.14

$$c^{10}x + 5c^9d^2x^2 + 15c^8d^2x^3 + 30c^7d^3x^4 + 42c^6d^4x^5 + 42c^5d^5x^6 + 30c^4d^6x^7 + 15c^3d^7x^8 + 5c^2d^8x^9 + cd^9x^{10} + \frac{d^{10}x^{11}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**10,x)`

[Out] $c^{10}x + 5c^9d^2x^2 + 15c^8d^2x^3 + 30c^7d^3x^4 + 42c^6d^4x^5 + 42c^5d^5x^6 + 30c^4d^6x^7 + 15c^3d^7x^8 + 5c^2d^8x^9 + c^9d^2x^2 + d^{10}x^{11}/11$

$$3.1312 \quad \int \frac{(c+dx)^{10}}{a+bx} dx$$

Optimal. Leaf size=241

$$\frac{(bc-ad)^{10} \log(a+bx)}{b^{11}} + \frac{dx(bc-ad)^9}{b^{10}} + \frac{(c+dx)^2(bc-ad)^8}{2b^9} + \frac{(c+dx)^3(bc-ad)^7}{3b^8} + \frac{(c+dx)^4(bc-ad)^6}{4b^7} + \frac{(c+dx)^5(bc-ad)^5}{5b^6} + \frac{(c+dx)^6(bc-ad)^4}{6b^5} + \frac{(c+dx)^7(bc-ad)^3}{7b^4} + \frac{(c+dx)^8(bc-ad)^2}{8b^3} + \frac{(c+dx)^9(bc-ad)}{9b^2} + \frac{(c+dx)^{10}}{10b}$$

[Out] $d*(-a*d+b*c)^9*x/b^{10}+1/2*(-a*d+b*c)^8*(d*x+c)^2/b^9+1/3*(-a*d+b*c)^7*(d*x+c)^3/b^8+1/4*(-a*d+b*c)^6*(d*x+c)^4/b^7+1/5*(-a*d+b*c)^5*(d*x+c)^5/b^6+1/6*(-a*d+b*c)^4*(d*x+c)^6/b^5+1/7*(-a*d+b*c)^3*(d*x+c)^7/b^4+1/8*(-a*d+b*c)^2*(d*x+c)^8/b^3+1/9*(-a*d+b*c)*(d*x+c)^9/b^2+1/10*(d*x+c)^{10}/b+(-a*d+b*c)^{10}*\ln(b*x+a)/b^{11}$

Rubi [A] time = 0.10, antiderivative size = 241, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{dx(bc-ad)^9}{b^{10}} + \frac{(c+dx)^2(bc-ad)^8}{2b^9} + \frac{(c+dx)^3(bc-ad)^7}{3b^8} + \frac{(c+dx)^4(bc-ad)^6}{4b^7} + \frac{(c+dx)^5(bc-ad)^5}{5b^6} + \frac{(c+dx)^6(bc-ad)^4}{6b^5} + \frac{(c+dx)^7(bc-ad)^3}{7b^4} + \frac{(c+dx)^8(bc-ad)^2}{8b^3} + \frac{(c+dx)^9(bc-ad)}{9b^2} + \frac{(c+dx)^{10}}{10b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x), x]

[Out] $(d*(b*c - a*d)^9*x)/b^{10} + ((b*c - a*d)^8*(c + d*x)^2)/(2*b^9) + ((b*c - a*d)^7*(c + d*x)^3)/(3*b^8) + ((b*c - a*d)^6*(c + d*x)^4)/(4*b^7) + ((b*c - a*d)^5*(c + d*x)^5)/(5*b^6) + ((b*c - a*d)^4*(c + d*x)^6)/(6*b^5) + ((b*c - a*d)^3*(c + d*x)^7)/(7*b^4) + ((b*c - a*d)^2*(c + d*x)^8)/(8*b^3) + ((b*c - a*d)*(c + d*x)^9)/(9*b^2) + (c + d*x)^{10}/(10*b) + ((b*c - a*d)^{10}*\text{Log}[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^{10}}{a+bx} dx &= \int \left(\frac{d(bc-ad)^9}{b^{10}} + \frac{(bc-ad)^{10}}{b^{10}(a+bx)} + \frac{d(bc-ad)^8(c+dx)}{b^9} + \frac{d(bc-ad)^7(c+dx)^2}{b^8} + \frac{d(bc-ad)^6(c+dx)^3}{b^7} \right. \\ &= \frac{d(bc-ad)^9x}{b^{10}} + \frac{(bc-ad)^8(c+dx)^2}{2b^9} + \frac{(bc-ad)^7(c+dx)^3}{3b^8} + \frac{(bc-ad)^6(c+dx)^4}{4b^7} + \frac{(bc-ad)^5(c+dx)^5}{5b^6} + \frac{(bc-ad)^4(c+dx)^6}{6b^5} + \frac{(bc-ad)^3(c+dx)^7}{7b^4} + \frac{(bc-ad)^2(c+dx)^8}{8b^3} + \frac{(bc-ad)(c+dx)^9}{9b^2} + \frac{(c+dx)^{10}}{10b} \end{aligned}$$

Mathematica [B] time = 0.34, size = 591, normalized size = 2.45

$$dx \left(-2520a^9d^9 + 1260a^8bd^8(20c + dx) - 840a^7b^2d^7(135c^2 + 15cdx + d^2x^2) + 210a^6b^3d^6(1440c^3 + 270c^2dx + 40c^2d^2x^2 + 3d^3x^3) - 252a^5b^4d^5(2100c^4 + 600c^3dx + 150c^2d^2x^2 + 25cd^3x^3 + 2d^4x^4) + 210a^4b^5d^4(3024c^5 + 1260c^4dx + 480c^3d^2x^2 + 135c^2d^3x^3 + 24cd^4x^4 + 2d^5x^5) - 120a^3b^6d^3(4410c^6 + 2646c^5dx + 1470c^4d^2x^2 + 630c^3d^3x^3 + 189c^2d^4x^4 + 35cd^5x^5 + 3d^6x^6) + 45a^2b^7d^2(6720c^7 + 5880c^6dx + 4704c^5d^2x^2 + 2940c^4d^3x^3 + 1344c^3d^4x^4 + 420c^2d^5x^5 + 80cd^6x^6 + 7d^7x^7) - 10ab^8d(11340c^8 + 15120c^7dx + 17640c^6d^2x^2 + 15876c^5d^3x^3 + 10584c^4d^4x^4 + 5040c^3d^5x^5 + 1620c^2d^6x^6 + 315cd^7x^7 + 28d^8x^8) + b^9(25200c^9 + 56700c^8dx + 100800c^7d^2x^2 + 132300c^6d^3x^3 + 127008c^5d^4x^4 + 88200c^4d^5x^5 + 43200c^3d^6x^6 + 14175c^2d^7x^7 + 2800cd^8x^8 + 252d^9x^9) \right) / (2520b^{10}) + ((b^9c - a^9d)^{10} \text{Log}[a + b^9x]) / b^{11}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x),x]

[Out] (d*x*(-2520*a^9*d^9 + 1260*a^8*b*d^8*(20*c + d*x) - 840*a^7*b^2*d^7*(135*c^2 + 15*c*d*x + d^2*x^2) + 210*a^6*b^3*d^6*(1440*c^3 + 270*c^2*d*x + 40*c*d^2*x^2 + 3*d^3*x^3) - 252*a^5*b^4*d^5*(2100*c^4 + 600*c^3*d*x + 150*c^2*d^2*x^2 + 25*c*d^3*x^3 + 2*d^4*x^4) + 210*a^4*b^5*d^4*(3024*c^5 + 1260*c^4*d*x + 480*c^3*d^2*x^2 + 135*c^2*d^3*x^3 + 24*c*d^4*x^4 + 2*d^5*x^5) - 120*a^3*b^6*d^3*(4410*c^6 + 2646*c^5*d*x + 1470*c^4*d^2*x^2 + 630*c^3*d^3*x^3 + 189*c^2*d^4*x^4 + 35*c*d^5*x^5 + 3*d^6*x^6) + 45*a^2*b^7*d^2*(6720*c^7 + 5880*c^6*d*x + 4704*c^5*d^2*x^2 + 2940*c^4*d^3*x^3 + 1344*c^3*d^4*x^4 + 420*c^2*d^5*x^5 + 80*c*d^6*x^6 + 7*d^7*x^7) - 10*a*b^8*d*(11340*c^8 + 15120*c^7*d*x + 17640*c^6*d^2*x^2 + 15876*c^5*d^3*x^3 + 10584*c^4*d^4*x^4 + 5040*c^3*d^5*x^5 + 1620*c^2*d^6*x^6 + 315*c*d^7*x^7 + 28*d^8*x^8) + b^9*(25200*c^9 + 56700*c^8*d*x + 100800*c^7*d^2*x^2 + 132300*c^6*d^3*x^3 + 127008*c^5*d^4*x^4 + 88200*c^4*d^5*x^5 + 43200*c^3*d^6*x^6 + 14175*c^2*d^7*x^7 + 2800*c*d^8*x^8 + 252*d^9*x^9))/(2520*b^10) + ((b*c - a*d)^10*Log[a + b*x])/b^11

fricas [B] time = 0.45, size = 868, normalized size = 3.60

$$252b^{10}d^{10}x^{10} + 280(10b^{10}cd^9 - ab^9d^{10})x^9 + 315(45b^{10}c^2d^8 - 10ab^9cd^9 + a^2b^8d^{10})x^8 + 360(120b^{10}c^3d^7 - 45a^2b^9c^2d^8 + 10a^2b^8cd^9 - a^3b^7d^{10})x^7 + 420(210b^{10}c^4d^6 - 120ab^9c^3d^7 + 45a^2b^8c^2d^8 - 10a^3b^7cd^9 + a^4b^6d^{10})x^6 + 504(252b^{10}c^5d^5 - 210a^2b^9c^4d^6 + 120a^2b^8c^3d^7 - 45a^3b^7c^2d^8 + 10a^4b^6cd^9 - a^5b^5d^{10})x^5 + 630(210b^{10}c^6d^4 - 252a^2b^9c^5d^5 + 210a^2b^8c^4d^6 - 120a^3b^7c^3d^7 + 45a^4b^6c^2d^8 - 10a^5b^5cd^9 + a^6b^4d^{10})x^4 + 840(120b^{10}c^7d^3 - 210a^2b^9c^6d^4 + 252a^2b^8c^5d^5 - 210a^3b^7c^4d^6 + 120a^4b^6c^3d^7 - 45a^5b^5c^2d^8 + 10a^6b^4cd^9 - a^7b^3d^{10})x^3 + 1260(45b^{10}c^8d^2 - 120a^2b^9c^7d^3 + 210a^2b^8c^6d^4 - 252a^3b^7c^5d^5 + 210a^4b^6c^4d^6 - 120a^5b^5c^3d^7 + 45a^6b^4c^2d^8 - 10a^7b^3cd^9 + a^8b^2d^{10})x^2 + 2520(10b^{10}c^9d - 45a^2b^9c^8d^2 + 45a^2b^8cd^9 - a^3b^7d^{10})x + 25200c^9 + 56700c^8dx + 100800c^7d^2x^2 + 132300c^6d^3x^3 + 127008c^5d^4x^4 + 88200c^4d^5x^5 + 43200c^3d^6x^6 + 14175c^2d^7x^7 + 2800cd^8x^8 + 252d^9x^9$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a),x, algorithm="fricas")

[Out] 1/2520*(252*b^10*d^10*x^10 + 280*(10*b^10*c*d^9 - a*b^9*d^10)*x^9 + 315*(45*b^10*c^2*d^8 - 10*a*b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 360*(120*b^10*c^3*d^7 - 45*a*b^9*c^2*d^8 + 10*a^2*b^8*c*d^9 - a^3*b^7*d^10)*x^7 + 420*(210*b^10*c^4*d^6 - 120*a*b^9*c^3*d^7 + 45*a^2*b^8*c^2*d^8 - 10*a^3*b^7*c*d^9 + a^4*b^6*d^10)*x^6 + 504*(252*b^10*c^5*d^5 - 210*a*b^9*c^4*d^6 + 120*a^2*b^8*c^3*d^7 - 45*a^3*b^7*c^2*d^8 + 10*a^4*b^6*c*d^9 - a^5*b^5*d^10)*x^5 + 630*(210*b^10*c^6*d^4 - 252*a*b^9*c^5*d^5 + 210*a^2*b^8*c^4*d^6 - 120*a^3*b^7*c^3*d^7 + 45*a^4*b^6*c^2*d^8 - 10*a^5*b^5*c*d^9 + a^6*b^4*d^10)*x^4 + 840*(120*b^10*c^7*d^3 - 210*a*b^9*c^6*d^4 + 252*a^2*b^8*c^5*d^5 - 210*a^3*b^7*c^4*d^6 + 120*a^4*b^6*c^3*d^7 - 45*a^5*b^5*c^2*d^8 + 10*a^6*b^4*c*d^9 - a^7*b^3*d^10)*x^3 + 1260*(45*b^10*c^8*d^2 - 120*a*b^9*c^7*d^3 + 210*a^2*b^8*c^6*d^4 - 252*a^3*b^7*c^5*d^5 + 210*a^4*b^6*c^4*d^6 - 120*a^5*b^5*c^3*d^7 + 45*a^6*b^4*c^2*d^8 - 10*a^7*b^3*c*d^9 + a^8*b^2*d^10)*x^2 + 2520*(10*b^10*c^9*d - 45*a^2*b^9*c^8*d^2 + 45*a^2*b^8cd^9 - a^3b^7d^{10})x + 25200c^9 + 56700c^8dx + 100800c^7d^2x^2 + 132300c^6d^3x^3 + 127008c^5d^4x^4 + 88200c^4d^5x^5 + 43200c^3d^6x^6 + 14175c^2d^7x^7 + 2800cd^8x^8 + 252d^9x^9

$$a*b^9*c^8*d^2 + 120*a^2*b^8*c^7*d^3 - 210*a^3*b^7*c^6*d^4 + 252*a^4*b^6*c^5*d^5 - 210*a^5*b^5*c^4*d^6 + 120*a^6*b^4*c^3*d^7 - 45*a^7*b^3*c^2*d^8 + 10*a^8*b^2*c*d^9 - a^9*b*d^{10})*x + 2520*(b^{10}*c^{10} - 10*a*b^9*c^9*d + 45*a^2*b^8*c^8*d^2 - 120*a^3*b^7*c^7*d^3 + 210*a^4*b^6*c^6*d^4 - 252*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 - 120*a^7*b^3*c^3*d^7 + 45*a^8*b^2*c^2*d^8 - 10*a^9*b*c*d^9 + a^{10}*d^{10})*\log(b*x + a))/b^{11}$$

giac [B] time = 1.35, size = 961, normalized size = 3.99

$$252 b^9 d^{10} x^{10} + 2800 b^9 c d^9 x^9 - 280 a b^8 d^{10} x^9 + 14175 b^9 c^2 d^8 x^8 - 3150 a b^8 c d^9 x^8 + 315 a^2 b^7 d^{10} x^8 + 43200 b^9 c^3 d^7 x^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a),x, algorithm="giac")

[Out] 1/2520*(252*b^9*d^10*x^10 + 2800*b^9*c*d^9*x^9 - 280*a*b^8*d^10*x^9 + 14175*b^9*c^2*d^8*x^8 - 3150*a*b^8*c*d^9*x^8 + 315*a^2*b^7*d^10*x^8 + 43200*b^9*c^3*d^7*x^7 - 16200*a*b^8*c^2*d^8*x^7 + 3600*a^2*b^7*c*d^9*x^7 - 360*a^3*b^6*d^10*x^7 + 88200*b^9*c^4*d^6*x^6 - 50400*a*b^8*c^3*d^7*x^6 + 18900*a^2*b^7*c^2*d^8*x^6 - 4200*a^3*b^6*c*d^9*x^6 + 420*a^4*b^5*d^10*x^6 + 127008*b^9*c^5*d^5*x^5 - 105840*a*b^8*c^4*d^6*x^5 + 60480*a^2*b^7*c^3*d^7*x^5 - 22680*a^3*b^6*c^2*d^8*x^5 + 5040*a^4*b^5*c*d^9*x^5 - 504*a^5*b^4*d^10*x^5 + 132300*b^9*c^6*d^4*x^4 - 158760*a*b^8*c^5*d^5*x^4 + 132300*a^2*b^7*c^4*d^6*x^4 - 75600*a^3*b^6*c^3*d^7*x^4 + 28350*a^4*b^5*c^2*d^8*x^4 - 6300*a^5*b^4*c*d^9*x^4 + 630*a^6*b^3*d^10*x^4 + 100800*b^9*c^7*d^3*x^3 - 176400*a*b^8*c^6*d^4*x^3 + 211680*a^2*b^7*c^5*d^5*x^3 - 176400*a^3*b^6*c^4*d^6*x^3 + 100800*a^4*b^5*c^3*d^7*x^3 - 37800*a^5*b^4*c^2*d^8*x^3 + 8400*a^6*b^3*c*d^9*x^3 - 840*a^7*b^2*d^10*x^3 + 56700*b^9*c^8*d^2*x^2 - 151200*a*b^8*c^7*d^3*x^2 + 264600*a^2*b^7*c^6*d^4*x^2 - 317520*a^3*b^6*c^5*d^5*x^2 + 264600*a^4*b^5*c^4*d^6*x^2 - 151200*a^5*b^4*c^3*d^7*x^2 + 56700*a^6*b^3*c^2*d^8*x^2 - 12600*a^7*b^2*c*d^9*x^2 + 1260*a^8*b*d^10*x^2 + 25200*b^9*c^9*d*x - 113400*a*b^8*c^8*d^2*x + 302400*a^2*b^7*c^7*d^3*x - 529200*a^3*b^6*c^6*d^4*x + 635040*a^4*b^5*c^5*d^5*x - 529200*a^5*b^4*c^4*d^6*x + 302400*a^6*b^3*c^3*d^7*x - 113400*a^7*b^2*c^2*d^8*x + 25200*a^8*b*c*d^9*x - 2520*a^9*d^10*x)/b^10 + (b^{10}*c^{10} - 10*a*b^9*c^9*d + 45*a^2*b^8*c^8*d^2 - 120*a^3*b^7*c^7*d^3 + 210*a^4*b^6*c^6*d^4 - 252*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 - 120*a^7*b^3*c^3*d^7 + 45*a^8*b^2*c^2*d^8 - 10*a^9*b*c*d^9 + a^{10}*d^{10})*\log(abs(b*x + a))/b^{11}

maple [B] time = 0.01, size = 1022, normalized size = 4.24

$$\frac{d^{10}x^{10}}{10b} - \frac{a d^{10}x^9}{9b^2} + \frac{10c d^9x^9}{9b} + \frac{a^2 d^{10}x^8}{8b^3} - \frac{5ac d^9x^8}{4b^2} + \frac{45c^2 d^8x^8}{8b} - \frac{a^3 d^{10}x^7}{7b^4} + \frac{10a^2c d^9x^7}{7b^3} - \frac{45a c^2 d^8x^7}{7b^2} + \frac{120c^3 d^7x^7}{7b} + \frac{a^4 d^{10}x^6}{6b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a),x)

[Out] $105/2*d^4/b*x^4*c^6-1/3*d^10/b^8*x^3*a^7+40*d^3/b*x^3*c^7+1/2*d^10/b^9*x^2*a^8+45/2*d^2/b*x^2*c^8+1/8*d^10/b^3*x^8*a^2+45/8*d^8/b*x^8*c^2-1/7*d^10/b^4*x^7*a^3+120/7*d^7/b*x^7*c^3+1/6*d^10/b^5*x^6*a^4+35*d^6/b*x^6*c^4-1/5*d^10/b^6*x^5*a^5+252/5*d^5/b*x^5*c^5+1/4*d^10/b^7*x^4*a^6-1/9*d^10/b^2*x^9*a+10/9*d^9/b*x^9*c+1/b^11*\ln(b*x+a)*a^10*d^10+10*d/b*c^9*x-d^10/b^10*a^9*x-42*d^6/b^2*x^5*a*c^4-5/2*d^9/b^6*x^4*a^5*c+10/3*d^9/b^7*x^3*a^6*c-15*d^8/b^6*x^3*a^5*c^2+24*d^7/b^3*x^5*a^2*c^3+40*d^7/b^5*x^3*a^4*c^3-30*d^7/b^4*x^4*a^3*c^3+105/2*d^6/b^3*x^4*a^2*c^4-63*d^5/b^2*x^4*a*c^5-5/4*d^9/b^2*x^8*a*c+2*d^9/b^5*x^5*a^4*c-9*d^8/b^4*x^5*a^3*c^2-5/3*d^9/b^4*x^6*a^3*c+15/2*d^8/b^3*x^6*a^2*c^2-20*d^7/b^2*x^6*a*c^3+10/7*d^9/b^3*x^7*a^2*c-45/7*d^8/b^2*x^7*a*c^2-120/b^8*\ln(b*x+a)*a^7*c^3*d^7+210/b^7*\ln(b*x+a)*a^6*c^4*d^6-252/b^6*\ln(b*x+a)*a^5*c^5*d^5+210/b^5*\ln(b*x+a)*a^4*c^6*d^4-120/b^4*\ln(b*x+a)*a^3*c^7*d^3+45/b^3*\ln(b*x+a)*a^2*c^8*d^2-10/b^2*\ln(b*x+a)*a*c^9*d-10/b^10*\ln(b*x+a)*a^9*c*d^9+45/b^9*\ln(b*x+a)*a^8*c^2*d^8+1/10*d^10/b*x^10+1/b*\ln(b*x+a)*c^10+45/4*d^8/b^5*x^4*a^4*c^2+120*d^3/b^3*a^2*c^7*x-45*d^2/b^2*a*c^8*x-70*d^4/b^2*x^3*a*c^6-5*d^9/b^8*x^2*a^7*c+45/2*d^8/b^7*x^2*a^6*c^2-60*d^7/b^6*x^2*a^5*c^3+105*d^6/b^5*x^2*a^4*c^4-126*d^5/b^4*x^2*a^3*c^5+105*d^4/b^3*x^2*a^2*c^6-60*d^3/b^2*x^2*a*c^7+10*d^9/b^9*a^8*c*x-45*d^8/b^8*a^7*c^2*x+120*d^7/b^7*a^6*c^3*x-210*d^6/b^6*a^5*c^4*x-70*d^6/b^4*x^3*a^3*c^4+84*d^5/b^3*x^3*a^2*c^5+252*d^5/b^5*a^4*c^5*x-210*d^4/b^4*a^3*c^6*x$

maxima [B] time = 1.52, size = 866, normalized size = 3.59

$$252b^9d^{10}x^{10} + 280(10b^9cd^9 - ab^8d^{10})x^9 + 315(45b^9c^2d^8 - 10ab^8cd^9 + a^2b^7d^{10})x^8 + 360(120b^9c^3d^7 - 45ab^8c^2d^8 + 10a^2b^7c^3d^7 - 45a^3b^6cd^9 + a^4b^5d^{10})x^7 + 420(210b^9c^4d^6 - 120ab^8c^3d^7 + 45a^2b^7c^2d^8 - 10a^3b^6c^2d^9 + a^4b^5d^{10})x^6 + 504(252b^9c^5d^5 - 210ab^8c^4d^6 + 120a^2b^7c^3d^7 - 45a^3b^6c^2d^8 + 10a^4b^5c^2d^9 - a^5b^4d^{10})x^5 + 630(210b^9c^6d^4 - 252ab^8c^5d^5 + 210a^2b^7c^4d^6 - 120a^3b^6c^3d^7 + 45a^4b^5c^2d^8 - 10a^5b^4c^2d^9 + a^6b^3d^{10})x^4 + 840(120b^9c^7d^3 - 210ab^8c^6d^4 + 252a^2b^7c^5d^5 - 210a^3b^6c^4d^6 + 120a^4b^5c^3d^7 - 45a^5b^4c^2d^8 + 10a^6b^3c^2d^9 - a^7b^2d^{10})x^3 + 1260(45b^9c^8d^2 - 120ab^8c^7d^3 + 210a^2b^7c^6d^4 - 252a^3b^6c^5d^5 + 210a^4b^5c^4d^6 - 120a^5b^4c^3d^7 + 45a^6b^3c^2d^8 - 10a^7b^2c^2d^9 + a^8b^2d^{10})x^2 + 2520(10b^9c^9d - 45ab^8c^8d^2 + 120a^2b^7c^7d^3 - 210a^3b^6c^6d^4 + 252a^4b^5c^5d^5 - 210a^5b^4c^4d^6 + 120a^6b^3c^3d^7 - 45a^7b^2c^2d^8 + 10a^8b^2d^{10})x + 1050(10b^9c^{10} - 45ab^8c^9d + 120a^2b^7c^8d^2 - 210a^3b^6c^7d^3 + 252a^4b^5c^6d^4 - 210a^5b^4c^5d^5 + 120a^6b^3c^4d^6 - 45a^7b^2c^3d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{11} - 45ab^8c^{10}d + 120a^2b^7c^9d^2 - 210a^3b^6c^8d^3 + 252a^4b^5c^7d^4 - 210a^5b^4c^6d^5 + 120a^6b^3c^5d^6 - 45a^7b^2c^4d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{12} - 45ab^8c^{11}d + 120a^2b^7c^{10}d^2 - 210a^3b^6c^9d^3 + 252a^4b^5c^8d^4 - 210a^5b^4c^7d^5 + 120a^6b^3c^6d^6 - 45a^7b^2c^5d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{13} - 45ab^8c^{12}d + 120a^2b^7c^{11}d^2 - 210a^3b^6c^{10}d^3 + 252a^4b^5c^9d^4 - 210a^5b^4c^8d^5 + 120a^6b^3c^7d^6 - 45a^7b^2c^6d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{14} - 45ab^8c^{13}d + 120a^2b^7c^{12}d^2 - 210a^3b^6c^{11}d^3 + 252a^4b^5c^{10}d^4 - 210a^5b^4c^9d^5 + 120a^6b^3c^8d^6 - 45a^7b^2c^7d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{15} - 45ab^8c^{14}d + 120a^2b^7c^{13}d^2 - 210a^3b^6c^{12}d^3 + 252a^4b^5c^{11}d^4 - 210a^5b^4c^{10}d^5 + 120a^6b^3c^9d^6 - 45a^7b^2c^8d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{16} - 45ab^8c^{15}d + 120a^2b^7c^{14}d^2 - 210a^3b^6c^{13}d^3 + 252a^4b^5c^{12}d^4 - 210a^5b^4c^{11}d^5 + 120a^6b^3c^{10}d^6 - 45a^7b^2c^9d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{17} - 45ab^8c^{16}d + 120a^2b^7c^{15}d^2 - 210a^3b^6c^{14}d^3 + 252a^4b^5c^{13}d^4 - 210a^5b^4c^{12}d^5 + 120a^6b^3c^{11}d^6 - 45a^7b^2c^{10}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{18} - 45ab^8c^{17}d + 120a^2b^7c^{16}d^2 - 210a^3b^6c^{15}d^3 + 252a^4b^5c^{14}d^4 - 210a^5b^4c^{13}d^5 + 120a^6b^3c^{12}d^6 - 45a^7b^2c^{11}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{19} - 45ab^8c^{18}d + 120a^2b^7c^{17}d^2 - 210a^3b^6c^{16}d^3 + 252a^4b^5c^{15}d^4 - 210a^5b^4c^{14}d^5 + 120a^6b^3c^{13}d^6 - 45a^7b^2c^{12}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{20} - 45ab^8c^{19}d + 120a^2b^7c^{18}d^2 - 210a^3b^6c^{17}d^3 + 252a^4b^5c^{16}d^4 - 210a^5b^4c^{15}d^5 + 120a^6b^3c^{14}d^6 - 45a^7b^2c^{13}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{21} - 45ab^8c^{20}d + 120a^2b^7c^{19}d^2 - 210a^3b^6c^{18}d^3 + 252a^4b^5c^{17}d^4 - 210a^5b^4c^{16}d^5 + 120a^6b^3c^{15}d^6 - 45a^7b^2c^{14}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{22} - 45ab^8c^{21}d + 120a^2b^7c^{20}d^2 - 210a^3b^6c^{19}d^3 + 252a^4b^5c^{18}d^4 - 210a^5b^4c^{17}d^5 + 120a^6b^3c^{16}d^6 - 45a^7b^2c^{15}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{23} - 45ab^8c^{22}d + 120a^2b^7c^{21}d^2 - 210a^3b^6c^{20}d^3 + 252a^4b^5c^{19}d^4 - 210a^5b^4c^{18}d^5 + 120a^6b^3c^{17}d^6 - 45a^7b^2c^{16}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{24} - 45ab^8c^{23}d + 120a^2b^7c^{22}d^2 - 210a^3b^6c^{21}d^3 + 252a^4b^5c^{20}d^4 - 210a^5b^4c^{19}d^5 + 120a^6b^3c^{18}d^6 - 45a^7b^2c^{17}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{25} - 45ab^8c^{24}d + 120a^2b^7c^{23}d^2 - 210a^3b^6c^{22}d^3 + 252a^4b^5c^{21}d^4 - 210a^5b^4c^{20}d^5 + 120a^6b^3c^{19}d^6 - 45a^7b^2c^{18}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{26} - 45ab^8c^{25}d + 120a^2b^7c^{24}d^2 - 210a^3b^6c^{23}d^3 + 252a^4b^5c^{22}d^4 - 210a^5b^4c^{21}d^5 + 120a^6b^3c^{20}d^6 - 45a^7b^2c^{19}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{27} - 45ab^8c^{26}d + 120a^2b^7c^{25}d^2 - 210a^3b^6c^{24}d^3 + 252a^4b^5c^{23}d^4 - 210a^5b^4c^{22}d^5 + 120a^6b^3c^{21}d^6 - 45a^7b^2c^{20}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{28} - 45ab^8c^{27}d + 120a^2b^7c^{26}d^2 - 210a^3b^6c^{25}d^3 + 252a^4b^5c^{24}d^4 - 210a^5b^4c^{23}d^5 + 120a^6b^3c^{22}d^6 - 45a^7b^2c^{21}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{29} - 45ab^8c^{28}d + 120a^2b^7c^{27}d^2 - 210a^3b^6c^{26}d^3 + 252a^4b^5c^{25}d^4 - 210a^5b^4c^{24}d^5 + 120a^6b^3c^{23}d^6 - 45a^7b^2c^{22}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{30} - 45ab^8c^{29}d + 120a^2b^7c^{28}d^2 - 210a^3b^6c^{27}d^3 + 252a^4b^5c^{26}d^4 - 210a^5b^4c^{25}d^5 + 120a^6b^3c^{24}d^6 - 45a^7b^2c^{23}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{31} - 45ab^8c^{30}d + 120a^2b^7c^{29}d^2 - 210a^3b^6c^{28}d^3 + 252a^4b^5c^{27}d^4 - 210a^5b^4c^{26}d^5 + 120a^6b^3c^{25}d^6 - 45a^7b^2c^{24}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{32} - 45ab^8c^{31}d + 120a^2b^7c^{30}d^2 - 210a^3b^6c^{29}d^3 + 252a^4b^5c^{28}d^4 - 210a^5b^4c^{27}d^5 + 120a^6b^3c^{26}d^6 - 45a^7b^2c^{25}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{33} - 45ab^8c^{32}d + 120a^2b^7c^{31}d^2 - 210a^3b^6c^{30}d^3 + 252a^4b^5c^{29}d^4 - 210a^5b^4c^{28}d^5 + 120a^6b^3c^{27}d^6 - 45a^7b^2c^{26}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{34} - 45ab^8c^{33}d + 120a^2b^7c^{32}d^2 - 210a^3b^6c^{31}d^3 + 252a^4b^5c^{30}d^4 - 210a^5b^4c^{29}d^5 + 120a^6b^3c^{28}d^6 - 45a^7b^2c^{27}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{35} - 45ab^8c^{34}d + 120a^2b^7c^{33}d^2 - 210a^3b^6c^{32}d^3 + 252a^4b^5c^{31}d^4 - 210a^5b^4c^{30}d^5 + 120a^6b^3c^{29}d^6 - 45a^7b^2c^{28}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{36} - 45ab^8c^{35}d + 120a^2b^7c^{34}d^2 - 210a^3b^6c^{33}d^3 + 252a^4b^5c^{32}d^4 - 210a^5b^4c^{31}d^5 + 120a^6b^3c^{30}d^6 - 45a^7b^2c^{29}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{37} - 45ab^8c^{36}d + 120a^2b^7c^{35}d^2 - 210a^3b^6c^{34}d^3 + 252a^4b^5c^{33}d^4 - 210a^5b^4c^{32}d^5 + 120a^6b^3c^{31}d^6 - 45a^7b^2c^{30}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{38} - 45ab^8c^{37}d + 120a^2b^7c^{36}d^2 - 210a^3b^6c^{35}d^3 + 252a^4b^5c^{34}d^4 - 210a^5b^4c^{33}d^5 + 120a^6b^3c^{32}d^6 - 45a^7b^2c^{31}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{39} - 45ab^8c^{38}d + 120a^2b^7c^{37}d^2 - 210a^3b^6c^{36}d^3 + 252a^4b^5c^{35}d^4 - 210a^5b^4c^{34}d^5 + 120a^6b^3c^{33}d^6 - 45a^7b^2c^{32}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{40} - 45ab^8c^{39}d + 120a^2b^7c^{38}d^2 - 210a^3b^6c^{37}d^3 + 252a^4b^5c^{36}d^4 - 210a^5b^4c^{35}d^5 + 120a^6b^3c^{34}d^6 - 45a^7b^2c^{33}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{41} - 45ab^8c^{40}d + 120a^2b^7c^{39}d^2 - 210a^3b^6c^{38}d^3 + 252a^4b^5c^{37}d^4 - 210a^5b^4c^{36}d^5 + 120a^6b^3c^{35}d^6 - 45a^7b^2c^{34}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{42} - 45ab^8c^{41}d + 120a^2b^7c^{40}d^2 - 210a^3b^6c^{39}d^3 + 252a^4b^5c^{38}d^4 - 210a^5b^4c^{37}d^5 + 120a^6b^3c^{36}d^6 - 45a^7b^2c^{35}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{43} - 45ab^8c^{42}d + 120a^2b^7c^{41}d^2 - 210a^3b^6c^{40}d^3 + 252a^4b^5c^{39}d^4 - 210a^5b^4c^{38}d^5 + 120a^6b^3c^{37}d^6 - 45a^7b^2c^{36}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{44} - 45ab^8c^{43}d + 120a^2b^7c^{42}d^2 - 210a^3b^6c^{41}d^3 + 252a^4b^5c^{40}d^4 - 210a^5b^4c^{39}d^5 + 120a^6b^3c^{38}d^6 - 45a^7b^2c^{37}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{45} - 45ab^8c^{44}d + 120a^2b^7c^{43}d^2 - 210a^3b^6c^{42}d^3 + 252a^4b^5c^{41}d^4 - 210a^5b^4c^{40}d^5 + 120a^6b^3c^{39}d^6 - 45a^7b^2c^{38}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{46} - 45ab^8c^{45}d + 120a^2b^7c^{44}d^2 - 210a^3b^6c^{43}d^3 + 252a^4b^5c^{42}d^4 - 210a^5b^4c^{41}d^5 + 120a^6b^3c^{40}d^6 - 45a^7b^2c^{39}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{47} - 45ab^8c^{46}d + 120a^2b^7c^{45}d^2 - 210a^3b^6c^{44}d^3 + 252a^4b^5c^{43}d^4 - 210a^5b^4c^{42}d^5 + 120a^6b^3c^{41}d^6 - 45a^7b^2c^{40}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{48} - 45ab^8c^{47}d + 120a^2b^7c^{46}d^2 - 210a^3b^6c^{45}d^3 + 252a^4b^5c^{44}d^4 - 210a^5b^4c^{43}d^5 + 120a^6b^3c^{42}d^6 - 45a^7b^2c^{41}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{49} - 45ab^8c^{48}d + 120a^2b^7c^{47}d^2 - 210a^3b^6c^{46}d^3 + 252a^4b^5c^{45}d^4 - 210a^5b^4c^{44}d^5 + 120a^6b^3c^{43}d^6 - 45a^7b^2c^{42}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{50} - 45ab^8c^{49}d + 120a^2b^7c^{48}d^2 - 210a^3b^6c^{47}d^3 + 252a^4b^5c^{46}d^4 - 210a^5b^4c^{45}d^5 + 120a^6b^3c^{44}d^6 - 45a^7b^2c^{43}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{51} - 45ab^8c^{50}d + 120a^2b^7c^{49}d^2 - 210a^3b^6c^{48}d^3 + 252a^4b^5c^{47}d^4 - 210a^5b^4c^{46}d^5 + 120a^6b^3c^{45}d^6 - 45a^7b^2c^{44}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{52} - 45ab^8c^{51}d + 120a^2b^7c^{50}d^2 - 210a^3b^6c^{49}d^3 + 252a^4b^5c^{48}d^4 - 210a^5b^4c^{47}d^5 + 120a^6b^3c^{46}d^6 - 45a^7b^2c^{45}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{53} - 45ab^8c^{52}d + 120a^2b^7c^{51}d^2 - 210a^3b^6c^{50}d^3 + 252a^4b^5c^{49}d^4 - 210a^5b^4c^{48}d^5 + 120a^6b^3c^{47}d^6 - 45a^7b^2c^{46}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{54} - 45ab^8c^{53}d + 120a^2b^7c^{52}d^2 - 210a^3b^6c^{51}d^3 + 252a^4b^5c^{50}d^4 - 210a^5b^4c^{49}d^5 + 120a^6b^3c^{48}d^6 - 45a^7b^2c^{47}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{55} - 45ab^8c^{54}d + 120a^2b^7c^{53}d^2 - 210a^3b^6c^{52}d^3 + 252a^4b^5c^{51}d^4 - 210a^5b^4c^{50}d^5 + 120a^6b^3c^{49}d^6 - 45a^7b^2c^{48}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{56} - 45ab^8c^{55}d + 120a^2b^7c^{54}d^2 - 210a^3b^6c^{53}d^3 + 252a^4b^5c^{52}d^4 - 210a^5b^4c^{51}d^5 + 120a^6b^3c^{50}d^6 - 45a^7b^2c^{49}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{57} - 45ab^8c^{56}d + 120a^2b^7c^{55}d^2 - 210a^3b^6c^{54}d^3 + 252a^4b^5c^{53}d^4 - 210a^5b^4c^{52}d^5 + 120a^6b^3c^{51}d^6 - 45a^7b^2c^{50}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{58} - 45ab^8c^{57}d + 120a^2b^7c^{56}d^2 - 210a^3b^6c^{55}d^3 + 252a^4b^5c^{54}d^4 - 210a^5b^4c^{53}d^5 + 120a^6b^3c^{52}d^6 - 45a^7b^2c^{51}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{59} - 45ab^8c^{58}d + 120a^2b^7c^{57}d^2 - 210a^3b^6c^{56}d^3 + 252a^4b^5c^{55}d^4 - 210a^5b^4c^{54}d^5 + 120a^6b^3c^{53}d^6 - 45a^7b^2c^{52}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{60} - 45ab^8c^{59}d + 120a^2b^7c^{58}d^2 - 210a^3b^6c^{57}d^3 + 252a^4b^5c^{56}d^4 - 210a^5b^4c^{55}d^5 + 120a^6b^3c^{54}d^6 - 45a^7b^2c^{53}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{61} - 45ab^8c^{60}d + 120a^2b^7c^{59}d^2 - 210a^3b^6c^{58}d^3 + 252a^4b^5c^{57}d^4 - 210a^5b^4c^{56}d^5 + 120a^6b^3c^{55}d^6 - 45a^7b^2c^{54}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{62} - 45ab^8c^{61}d + 120a^2b^7c^{60}d^2 - 210a^3b^6c^{59}d^3 + 252a^4b^5c^{58}d^4 - 210a^5b^4c^{57}d^5 + 120a^6b^3c^{56}d^6 - 45a^7b^2c^{55}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{63} - 45ab^8c^{62}d + 120a^2b^7c^{61}d^2 - 210a^3b^6c^{60}d^3 + 252a^4b^5c^{59}d^4 - 210a^5b^4c^{58}d^5 + 120a^6b^3c^{57}d^6 - 45a^7b^2c^{56}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{64} - 45ab^8c^{63}d + 120a^2b^7c^{62}d^2 - 210a^3b^6c^{61}d^3 + 252a^4b^5c^{60}d^4 - 210a^5b^4c^{59}d^5 + 120a^6b^3c^{58}d^6 - 45a^7b^2c^{57}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{65} - 45ab^8c^{64}d + 120a^2b^7c^{63}d^2 - 210a^3b^6c^{62}d^3 + 252a^4b^5c^{61}d^4 - 210a^5b^4c^{60}d^5 + 120a^6b^3c^{59}d^6 - 45a^7b^2c^{58}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{66} - 45ab^8c^{65}d + 120a^2b^7c^{64}d^2 - 210a^3b^6c^{63}d^3 + 252a^4b^5c^{62}d^4 - 210a^5b^4c^{61}d^5 + 120a^6b^3c^{60}d^6 - 45a^7b^2c^{59}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{67} - 45ab^8c^{66}d + 120a^2b^7c^{65}d^2 - 210a^3b^6c^{64}d^3 + 252a^4b^5c^{63}d^4 - 210a^5b^4c^{62}d^5 + 120a^6b^3c^{61}d^6 - 45a^7b^2c^{60}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{68} - 45ab^8c^{67}d + 120a^2b^7c^{66}d^2 - 210a^3b^6c^{65}d^3 + 252a^4b^5c^{64}d^4 - 210a^5b^4c^{63}d^5 + 120a^6b^3c^{62}d^6 - 45a^7b^2c^{61}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{69} - 45ab^8c^{68}d + 120a^2b^7c^{67}d^2 - 210a^3b^6c^{66}d^3 + 252a^4b^5c^{65}d^4 - 210a^5b^4c^{64}d^5 + 120a^6b^3c^{63}d^6 - 45a^7b^2c^{62}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{70} - 45ab^8c^{69}d + 120a^2b^7c^{68}d^2 - 210a^3b^6c^{67}d^3 + 252a^4b^5c^{66}d^4 - 210a^5b^4c^{65}d^5 + 120a^6b^3c^{64}d^6 - 45a^7b^2c^{63}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{71} - 45ab^8c^{70}d + 120a^2b^7c^{69}d^2 - 210a^3b^6c^{68}d^3 + 252a^4b^5c^{67}d^4 - 210a^5b^4c^{66}d^5 + 120a^6b^3c^{65}d^6 - 45a^7b^2c^{64}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{72} - 45ab^8c^{71}d + 120a^2b^7c^{70}d^2 - 210a^3b^6c^{69}d^3 + 252a^4b^5c^{68}d^4 - 210a^5b^4c^{67}d^5 + 120a^6b^3c^{66}d^6 - 45a^7b^2c^{65}d^7 + 10a^8b^2d^{10})x + 450(10b^9c^{73} - 45ab^8c^{72}d + 120a^2b^7c^{71}d^2 - 210a^3b^6c^{70}d^3 + 252a^4b^5c^{69}d^4 - 210a^5b^4c^{68}d^5 + 120a^6b^3c^{67}d^6 - 45a^7b^2c^{66}d^7 + 10a^8b^2d^{10})x + 1050(10b^9c^{74} - 45ab^8c^{73}d + 120a^2b^7c^{72}d^2 - 210a$$

$$\begin{aligned} & ^5b^4c^4d^6 + 120a^6b^3c^3d^7 - 45a^7b^2c^2d^8 + 10a^8b^2c^2d^9 \\ & - a^9d^{10})x)/b^{10} + (b^{10}c^{10} - 10a^9b^9c^9d + 45a^8b^8c^8d^2 - 12 \\ & 0a^7b^7c^7d^3 + 210a^6b^6c^6d^4 - 252a^5b^5c^5d^5 + 210a^4b^4 \\ & c^4d^6 - 120a^3b^3c^3d^7 + 45a^2b^2c^2d^8 - 10a^9b^2c^2d^9 + a^{10} \\ & d^{10})\log(bx + a)/b^{11} \end{aligned}$$

mupad [B] time = 0.13, size = 979, normalized size = 4.06

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^10/(a + b*x),x)`

[Out] $x^7 \left(\frac{120c^3d^7}{7b} - \frac{a \left(\frac{a^2d^{10}}{b^2} - \frac{10cd^9}{b} \right)}{b} + \frac{45c^2d^8}{b} \right) / (7b) - x^9 \left(\frac{a^2d^{10}}{9b^2} - \frac{10cd^9}{9b} \right) + x^5 \left(\frac{a \left(\frac{a \left(\frac{120c^3d^7}{b} - \frac{a \left(\frac{a^2d^{10}}{b^2} - \frac{10cd^9}{b} \right)}{b} + \frac{45c^2d^8}{b} \right)}{b} \right)}{b} - \frac{210c^4d^6}{b} \right) / (5b) + \frac{252c^5d^5}{5b} + x^3 \left(\frac{a \left(\frac{a \left(\frac{a \left(\frac{120c^3d^7}{b} - \frac{a \left(\frac{a^2d^{10}}{b^2} - \frac{10cd^9}{b} \right)}{b} + \frac{45c^2d^8}{b} \right)}{b} \right)}{b} - \frac{210c^4d^6}{b} \right)}{b} + \frac{252c^5d^5}{b} \right) / b - \frac{210c^6d^4}{b} \right) / (3b) + \frac{40c^7d^3}{b} + x \left(\frac{a \left(\frac{a \left(\frac{a \left(\frac{a \left(\frac{120c^3d^7}{b} - \frac{a \left(\frac{a^2d^{10}}{b^2} - \frac{10cd^9}{b} \right)}{b} + \frac{45c^2d^8}{b} \right)}{b} \right)}{b} - \frac{210c^4d^6}{b} \right)}{b} + \frac{252c^5d^5}{b} \right)}{b} - \frac{210c^6d^4}{b} \right) / b + \frac{120c^7d^3}{b} \right) / b - \frac{45c^8d^2}{b} \right) / b + \frac{10cd^9}{b} + x^8 \left(\frac{a \left(\frac{a^2d^{10}}{b^2} - \frac{10cd^9}{b} \right)}{8b} + \frac{45c^2d^8}{8b} \right) - x^6 \left(\frac{a \left(\frac{a \left(\frac{120c^3d^7}{b} - \frac{a \left(\frac{a^2d^{10}}{b^2} - \frac{10cd^9}{b} \right)}{b} + \frac{45c^2d^8}{b} \right)}{b} \right)}{6b} - \frac{35c^4d^6}{b} \right) - x^4 \left(\frac{a \left(\frac{a \left(\frac{a \left(\frac{120c^3d^7}{b} - \frac{a \left(\frac{a^2d^{10}}{b^2} - \frac{10cd^9}{b} \right)}{b} + \frac{45c^2d^8}{b} \right)}{b} \right)}{b} - \frac{210c^4d^6}{b} \right)}{b} + \frac{252c^5d^5}{b} \right) / (4b) - \frac{105c^6d^4}{2b} - x^2 \left(\frac{a \left(\frac{a \left(\frac{a \left(\frac{a \left(\frac{120c^3d^7}{b} - \frac{a \left(\frac{a^2d^{10}}{b^2} - \frac{10cd^9}{b} \right)}{b} + \frac{45c^2d^8}{b} \right)}{b} \right)}{b} - \frac{210c^4d^6}{b} \right)}{b} + \frac{252c^5d^5}{b} \right)}{b} - \frac{210c^6d^4}{b} \right) / b + \frac{120c^7d^3}{b} \right) / (2b) - \frac{45c^8d^2}{2b} + \frac{d^{10}x^{10}}{10b} + \frac{\log(a + bx)(a^{10}d^{10} + b^{10}c^{10} + 45a^2b^8c^8d^2 - 120a^3b^7c^7d^3 + 210a^4b^6c^6d^4 - 252a^5b^5c^5d^5 + 210a^6b^4c^4d^6 - 120a^7b^3c^3d^7 + 45a^8b^2c^2d^8 - 10a^9b^1c^1d^9)}{b^{11}}$

sympy [B] time = 1.42, size = 799, normalized size = 3.32

$$x^9 \left(-\frac{ad^{10}}{9b^2} + \frac{10cd^9}{9b} \right) + x^8 \left(\frac{a^2d^{10}}{8b^3} - \frac{5acd^9}{4b^2} + \frac{45c^2d^8}{8b} \right) + x^7 \left(-\frac{a^3d^{10}}{7b^4} + \frac{10a^2cd^9}{7b^3} - \frac{45ac^2d^8}{7b^2} + \frac{120c^3d^7}{7b} \right) + x^6 \left(\frac{a^4d^{10}}{6b^5} - \frac{15a^3cd^9}{6b^4} + \frac{45a^2c^2d^8}{6b^3} - \frac{120a^3c^3d^7}{6b^2} + \frac{120a^4c^4d^6}{6b} - \frac{45a^5c^5d^5}{6} + \frac{10a^6c^6d^4}{6} - \frac{10a^7c^7d^3}{6} + \frac{10a^8c^8d^2}{6} - \frac{10a^9c^9d}{6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**10/(b*x+a),x)`

[Out] $x^9 \left(-\frac{ad^{10}}{9b^2} + \frac{10cd^9}{9b} \right) + x^8 \left(\frac{a^2d^{10}}{8b^3} - \frac{5acd^9}{4b^2} + \frac{45c^2d^8}{8b} \right) + x^7 \left(-\frac{a^3d^{10}}{7b^4} + \frac{10a^2cd^9}{7b^3} - \frac{45ac^2d^8}{7b^2} + \frac{120c^3d^7}{7b} \right) + x^6 \left(\frac{a^4d^{10}}{6b^5} - \frac{15a^3cd^9}{6b^4} + \frac{45a^2c^2d^8}{6b^3} - \frac{120a^3c^3d^7}{6b^2} + \frac{120a^4c^4d^6}{6b} - \frac{45a^5c^5d^5}{6} + \frac{10a^6c^6d^4}{6} - \frac{10a^7c^7d^3}{6} + \frac{10a^8c^8d^2}{6} - \frac{10a^9c^9d}{6} \right)$

$$\begin{aligned}
& 0*a*c**6*d**4/b**2 + 40*c**7*d**3/b) + x**2*(a**8*d**10/(2*b**9) - 5*a**7*c \\
& *d**9/b**8 + 45*a**6*c**2*d**8/(2*b**7) - 60*a**5*c**3*d**7/b**6 + 105*a**4 \\
& *c**4*d**6/b**5 - 126*a**3*c**5*d**5/b**4 + 105*a**2*c**6*d**4/b**3 - 60*a* \\
& c**7*d**3/b**2 + 45*c**8*d**2/(2*b)) + x*(-a**9*d**10/b**10 + 10*a**8*c*d** \\
& 9/b**9 - 45*a**7*c**2*d**8/b**8 + 120*a**6*c**3*d**7/b**7 - 210*a**5*c**4*d \\
& **6/b**6 + 252*a**4*c**5*d**5/b**5 - 210*a**3*c**6*d**4/b**4 + 120*a**2*c** \\
& 7*d**3/b**3 - 45*a*c**8*d**2/b**2 + 10*c**9*d/b) + d**10*x**10/(10*b) + (a* \\
& d - b*c)**10*log(a + b*x)/b**11
\end{aligned}$$

$$3.1313 \quad \int \frac{(c+dx)^{10}}{(a+bx)^2} dx$$

Optimal. Leaf size=258

$$\frac{5d^9(a+bx)^8(bc-ad)}{4b^{11}} + \frac{45d^8(a+bx)^7(bc-ad)^2}{7b^{11}} + \frac{20d^7(a+bx)^6(bc-ad)^3}{b^{11}} + \frac{42d^6(a+bx)^5(bc-ad)^4}{b^{11}} + \frac{63d^5(a+bx)^4(bc-ad)^5}{b^{11}} + \frac{45d^4(a+bx)^3(bc-ad)^6}{b^{11}} + \frac{20d^3(a+bx)^2(bc-ad)^7}{b^{11}} + \frac{7d^2(a+bx)(bc-ad)^8}{b^{11}} + \frac{d(bc-ad)^9}{b^{11}} + \frac{10d^9(a+bx)^9 \ln(bx+a)}{b^{11}}$$

[Out] $45*d^2*(-a*d+b*c)^8*x/b^{10} - (-a*d+b*c)^{10}/b^{11}/(b*x+a) + 60*d^3*(-a*d+b*c)^7*(b*x+a)^2/b^{11} + 70*d^4*(-a*d+b*c)^6*(b*x+a)^3/b^{11} + 63*d^5*(-a*d+b*c)^5*(b*x+a)^4/b^{11} + 42*d^6*(-a*d+b*c)^4*(b*x+a)^5/b^{11} + 20*d^7*(-a*d+b*c)^3*(b*x+a)^6/b^{11} + 45/7*d^8*(-a*d+b*c)^2*(b*x+a)^7/b^{11} + 5/4*d^9*(-a*d+b*c)*(b*x+a)^8/b^{11} + 1/9*d^{10}*(b*x+a)^9/b^{11} + 10*d*(-a*d+b*c)^9*\ln(b*x+a)/b^{11}$

Rubi [A] time = 0.47, antiderivative size = 258, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{5d^9(a+bx)^8(bc-ad)}{4b^{11}} + \frac{45d^8(a+bx)^7(bc-ad)^2}{7b^{11}} + \frac{20d^7(a+bx)^6(bc-ad)^3}{b^{11}} + \frac{42d^6(a+bx)^5(bc-ad)^4}{b^{11}} + \frac{63d^5(a+bx)^4(bc-ad)^5}{b^{11}} + \frac{45d^4(a+bx)^3(bc-ad)^6}{b^{11}} + \frac{20d^3(a+bx)^2(bc-ad)^7}{b^{11}} + \frac{7d^2(a+bx)(bc-ad)^8}{b^{11}} + \frac{d(bc-ad)^9}{b^{11}} + \frac{10d^9(a+bx)^9 \ln(bx+a)}{b^{11}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^2,x]

[Out] $(45*d^2*(b*c - a*d)^8*x)/b^{10} - (b*c - a*d)^{10}/(b^{11}*(a + b*x)) + (60*d^3*(b*c - a*d)^7*(a + b*x)^2)/b^{11} + (70*d^4*(b*c - a*d)^6*(a + b*x)^3)/b^{11} + (63*d^5*(b*c - a*d)^5*(a + b*x)^4)/b^{11} + (42*d^6*(b*c - a*d)^4*(a + b*x)^5)/b^{11} + (20*d^7*(b*c - a*d)^3*(a + b*x)^6)/b^{11} + (45*d^8*(b*c - a*d)^2*(a + b*x)^7)/(7*b^{11}) + (5*d^9*(b*c - a*d)*(a + b*x)^8)/(4*b^{11}) + (d^{10}*(a + b*x)^9)/(9*b^{11}) + (10*d*(b*c - a*d)^9*\Log[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c + dx)^{10}}{(a + bx)^2} dx = \int \left(\frac{45d^2(bc - ad)^8}{b^{10}} + \frac{(bc - ad)^{10}}{b^{10}(a + bx)^2} + \frac{10d(bc - ad)^9}{b^{10}(a + bx)} + \frac{120d^3(bc - ad)^7(a + bx)}{b^{10}} + \frac{210d^4(bc - ad)^6(a + bx)^2}{b^{10}} + \frac{150d^5(bc - ad)^5(a + bx)^3}{b^{10}} + \frac{63d^6(bc - ad)^4(a + bx)^4}{b^{10}} + \frac{15d^7(bc - ad)^3(a + bx)^5}{b^{10}} + \frac{3d^8(bc - ad)^2(a + bx)^6}{b^{10}} + \frac{d^9(bc - ad)(a + bx)^7}{b^{10}} + \frac{d^{10}(a + bx)^8}{b^{10}} \right) dx$$

$$= \frac{45d^2(bc - ad)^8 x}{b^{10}} - \frac{(bc - ad)^{10}}{b^{11}(a + bx)} + \frac{60d^3(bc - ad)^7(a + bx)^2}{b^{11}} + \frac{70d^4(bc - ad)^6(a + bx)^3}{b^{11}} + \frac{63d^5(bc - ad)^5(a + bx)^4}{b^{11}} + \frac{15d^6(bc - ad)^4(a + bx)^5}{b^{11}} + \frac{3d^7(bc - ad)^3(a + bx)^6}{b^{11}} + \frac{d^8(bc - ad)^2(a + bx)^7}{b^{11}} + \frac{d^9(bc - ad)(a + bx)^8}{b^{11}} + \frac{d^{10}(a + bx)^9}{b^{11}}$$

Mathematica [B] time = 0.24, size = 708, normalized size = 2.74

$$\frac{-252a^{10}d^{10} + 252a^9bd^9(10c + 9dx) + 1260a^8b^2d^8(-9c^2 - 16cdx + d^2x^2) - 420a^7b^3d^7(-72c^3 - 189c^2dx + 27cd^2x^2) + 210a^6b^4d^6(-252c^4 - 864c^3dx + 216c^2d^2x^2 + 18cd^3x^3 + d^4x^4) - 126a^5b^5d^5(-504c^5 - 2100c^4dx + 840c^3d^2x^2 + 120c^2d^3x^3 + 15cd^4x^4 + d^5x^5) + 42a^4b^6d^4(-1260c^6 - 6048c^5dx + 3780c^4d^2x^2 + 840c^3d^3x^3 + 180c^2d^4x^4 + 27cd^5x^5 + 2d^6x^6) - 12a^3b^7d^3(-2520c^7 - 13230c^6dx + 13230c^5d^2x^2 + 4410c^4d^3x^3 + 1470c^3d^4x^4 + 378c^2d^5x^5 + 63cd^6x^6 + 5d^7x^7) + 9a^2b^8d^2(-1260c^8 - 6720c^7dx + 11760c^6d^2x^2 + 5880c^5d^3x^3 + 2940c^4d^4x^4 + 1176c^3d^5x^5 + 336c^2d^6x^6 + 60cd^7x^7 + 5d^8x^8) - ab^9d(-2520c^9 - 11340c^8dx + 45360c^7d^2x^2 + 35280c^6d^3x^3 + 26460c^5d^4x^4 + 15876c^4d^5x^5 + 7056c^3d^6x^6 + 2160c^2d^7x^7 + 405cd^8x^8 + 35d^9x^9) + b^{10}(-252c^{10} + 11340c^8d^2x^2 + 15120c^7d^3x^3 + 17640c^6d^4x^4 + 15876c^5d^5x^5 + 10584c^4d^6x^6 + 5040c^3d^7x^7 + 1620c^2d^8x^8 + 315cd^9x^9 + 28d^{10}x^{10}) - 2520d(-b^9c + ab^8d)^9(a + bx)^9 \cdot \text{Log}[a + bx]}{(252b^{11}(a + bx))^{10}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^2,x]

[Out] (-252*a^10*d^10 + 252*a^9*b*d^9*(10*c + 9*d*x) + 1260*a^8*b^2*d^8*(-9*c^2 - 16*c*d*x + d^2*x^2) - 420*a^7*b^3*d^7*(-72*c^3 - 189*c^2*d*x + 27*c*d^2*x^2 + d^3*x^3) + 210*a^6*b^4*d^6*(-252*c^4 - 864*c^3*d*x + 216*c^2*d^2*x^2 + 18*c*d^3*x^3 + d^4*x^4) - 126*a^5*b^5*d^5*(-504*c^5 - 2100*c^4*d*x + 840*c^3*d^2*x^2 + 120*c^2*d^3*x^3 + 15*c*d^4*x^4 + d^5*x^5) + 42*a^4*b^6*d^4*(-1260*c^6 - 6048*c^5*d*x + 3780*c^4*d^2*x^2 + 840*c^3*d^3*x^3 + 180*c^2*d^4*x^4 + 27*c*d^5*x^5 + 2*d^6*x^6) - 12*a^3*b^7*d^3*(-2520*c^7 - 13230*c^6*d*x + 13230*c^5*d^2*x^2 + 4410*c^4*d^3*x^3 + 1470*c^3*d^4*x^4 + 378*c^2*d^5*x^5 + 63*c*d^6*x^6 + 5*d^7*x^7) + 9*a^2*b^8*d^2*(-1260*c^8 - 6720*c^7*d*x + 11760*c^6*d^2*x^2 + 5880*c^5*d^3*x^3 + 2940*c^4*d^4*x^4 + 1176*c^3*d^5*x^5 + 336*c^2*d^6*x^6 + 60*c*d^7*x^7 + 5*d^8*x^8) - a*b^9*d*(-2520*c^9 - 11340*c^8*d*x + 45360*c^7*d^2*x^2 + 35280*c^6*d^3*x^3 + 26460*c^5*d^4*x^4 + 15876*c^4*d^5*x^5 + 7056*c^3*d^6*x^6 + 2160*c^2*d^7*x^7 + 405*c*d^8*x^8 + 35*d^9*x^9) + b^10*(-252*c^10 + 11340*c^8*d^2*x^2 + 15120*c^7*d^3*x^3 + 17640*c^6*d^4*x^4 + 15876*c^5*d^5*x^5 + 10584*c^4*d^6*x^6 + 5040*c^3*d^7*x^7 + 1620*c^2*d^8*x^8 + 315*c*d^9*x^9 + 28*d^10*x^10) - 2520*d*(-b*c + a*d)^9*(a + b*x)*Log[a + b*x])/(252*b^11*(a + b*x))

fricas [B] time = 0.44, size = 1124, normalized size = 4.36

$$\frac{28b^{10}d^{10}x^{10} - 252b^{10}c^{10} + 2520ab^9c^9d - 11340a^2b^8c^8d^2 + 30240a^3b^7c^7d^3 - 52920a^4b^6c^6d^4 + 63504a^5b^5c^5d^5 - 45360a^6b^4c^4d^6 + 26460a^7b^3c^3d^7 - 15876a^8b^2c^2d^8 + 7056a^9b^1c^1d^9 - 2520a^{10}b^0c^0d^{10} + 11340a^8b^2c^2d^8x^2 + 15120a^7b^3c^3d^7x^3 + 17640a^6b^4c^4d^6x^4 + 15876a^5b^5c^5d^5x^5 + 10584a^4b^6c^6d^4x^6 + 5040a^3b^7c^7d^3x^7 + 1620a^2b^8c^8d^2x^8 + 315ab^9c^9d^1x^9 + 28a^{10}b^0c^0d^{10}x^{10} - 2520d(-b^9c + ab^8d)^9(a + bx)^9 \cdot \text{Log}[a + bx]}{(252b^{11}(a + bx))^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^2,x, algorithm="fricas")


```
[Out] 1/252*(28*b^10*d^10*x^10 - 252*b^10*c^10 + 2520*a*b^9*c^9*d - 11340*a^2*b^8*c^8*d^2 + 30240*a^3*b^7*c^7*d^3 - 52920*a^4*b^6*c^6*d^4 + 63504*a^5*b^5*c^5*d^5 - 52920*a^6*b^4*c^4*d^6 + 30240*a^7*b^3*c^3*d^7 - 11340*a^8*b^2*c^2*d^8 + 2520*a^9*b*c*d^9 - 252*a^10*d^10 + 35*(9*b^10*c*d^9 - a*b^9*d^10)*x^9 + 45*(36*b^10*c^2*d^8 - 9*a*b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 60*(84*b^10*c^3*d^7 - 36*a*b^9*c^2*d^8 + 9*a^2*b^8*c*d^9 - a^3*b^7*d^10)*x^7 + 84*(126*b^10*c^4*d^6 - 84*a*b^9*c^3*d^7 + 36*a^2*b^8*c^2*d^8 - 9*a^3*b^7*c*d^9 + a^4*b^6*d^10)*x^6 + 126*(126*b^10*c^5*d^5 - 126*a*b^9*c^4*d^6 + 84*a^2*b^8*c^3*d^7 - 36*a^3*b^7*c^2*d^8 + 9*a^4*b^6*c*d^9 - a^5*b^5*d^10)*x^5 + 210*(84*b^10*c^6*d^4 - 126*a*b^9*c^5*d^5 + 126*a^2*b^8*c^4*d^6 - 84*a^3*b^7*c^3*d^7 + 36*a^4*b^6*c^2*d^8 - 9*a^5*b^5*c*d^9 + a^6*b^4*d^10)*x^4 + 420*(36*b^10*c^7*d^3 - 84*a*b^9*c^6*d^4 + 126*a^2*b^8*c^5*d^5 - 126*a^3*b^7*c^4*d^6 + 84*a^4*b^6*c^3*d^7 - 36*a^5*b^5*c^2*d^8 + 9*a^6*b^4*c*d^9 - a^7*b^3*d^10)*x^3 + 1260*(9*b^10*c^8*d^2 - 36*a*b^9*c^7*d^3 + 84*a^2*b^8*c^6*d^4 - 126*a^3*b^7*c^5*d^5 + 126*a^4*b^6*c^4*d^6 - 84*a^5*b^5*c^3*d^7 + 36*a^6*b^4*c^2*d^8 - 9*a^7*b^3*c*d^9 + a^8*b^2*d^10)*x^2 + 252*(45*a*b^9*c^8*d^2 - 240*a^2*b^8*c^7*d^3 + 630*a^3*b^7*c^6*d^4 - 1008*a^4*b^6*c^5*d^5 + 1050*a^5*b^5*c^4*d^6 - 720*a^6*b^4*c^3*d^7 + 315*a^7*b^3*c^2*d^8 - 80*a^8*b^2*c*d^9 + 9*a^9*b*d^10)*x + 2520*(a*b^9*c^9*d - 9*a^2*b^8*c^8*d^2 + 36*a^3*b^7*c^7*d^3 - 84*a^4*b^6*c^6*d^4 + 126*a^5*b^5*c^5*d^5 - 126*a^6*b^4*c^4*d^6 + 84*a^7*b^3*c^3*d^7 - 36*a^8*b^2*c^2*d^8 + 9*a^9*b*c*d^9 - a^10*d^10 + (b^10*c^9*d - 9*a*b^9*c^8*d^2 + 36*a^2*b^8*c^7*d^3 - 84*a^3*b^7*c^6*d^4 + 126*a^4*b^6*c^5*d^5 - 126*a^5*b^5*c^4*d^6 + 84*a^6*b^4*c^3*d^7 - 36*a^7*b^3*c^2*d^8 + 9*a^8*b^2*c*d^9 - a^9*b*d^10)*x)*log(b*x + a))/(b^12*x + a*b^11)
```

giac [B] time = 1.27, size = 1012, normalized size = 3.92

$$\frac{\left(28d^{10} + \frac{315(b^2cd^9 - abd^{10})}{(bx+a)b} + \frac{1620(b^4c^2d^8 - 2ab^3cd^9 + a^2b^2d^{10})}{(bx+a)^2b^2} + \frac{5040(b^6c^3d^7 - 3ab^5c^2d^8 + 3a^2b^4cd^9 - a^3b^3d^{10})}{(bx+a)^3b^3} + \frac{10584(b^8c^4d^6 - 4ab^7c^3d^7)}{(bx+a)^4b^4} + \frac{15876(b^{10}c^5d^5 - 5a^2b^8c^3d^7 - 10a^3b^7c^2d^8 + 5a^4b^6c*d^9 - a^5b^5d^{10})}{(bx+a)^5b^5} + \frac{17640(b^{12}c^6d^4 - 6a^2b^{11}c^5d^5 + 15a^2b^{10}c^4d^6 - 20a^3b^9c^3d^7 + 15a^4b^8c^2d^8 - 6a^5b^7c*d^9 + a^6b^6d^{10})}{(bx+a)^6b^6} + \frac{15120(b^{14}c^7d^3 - 7a^2b^{13}c^6d^4 + 21a^2b^{12}c^5d^5 - 35a^3b^{11}c^4d^6 + 35a^4b^{10}c^3d^7 - 21a^5b^9c^2d^8 + 7a^6b^8c*d^9 - a^7b^7d^{10})}{(bx+a)^7b^7} + 11340(b^{16}c^8d^2 - 8$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^10/(b*x+a)^2,x, algorithm="giac")
```

```
[Out] 1/252*(28*d^10 + 315*(b^2*c*d^9 - a*b*d^10)/((b*x + a)*b) + 1620*(b^4*c^2*d^8 - 2*a*b^3*c*d^9 + a^2*b^2*d^10)/((b*x + a)^2*b^2) + 5040*(b^6*c^3*d^7 - 3*a*b^5*c^2*d^8 + 3*a^2*b^4*c*d^9 - a^3*b^3*d^10)/((b*x + a)^3*b^3) + 10584*(b^8*c^4*d^6 - 4*a*b^7*c^3*d^7 + 6*a^2*b^6*c^2*d^8 - 4*a^3*b^5*c*d^9 + a^4*b^4*d^10)/((b*x + a)^4*b^4) + 15876*(b^10*c^5*d^5 - 5*a*b^9*c^4*d^6 + 10*a^2*b^8*c^3*d^7 - 10*a^3*b^7*c^2*d^8 + 5*a^4*b^6*c*d^9 - a^5*b^5*d^10)/((b*x + a)^5*b^5) + 17640*(b^12*c^6*d^4 - 6*a*b^11*c^5*d^5 + 15*a^2*b^10*c^4*d^6 - 20*a^3*b^9*c^3*d^7 + 15*a^4*b^8*c^2*d^8 - 6*a^5*b^7*c*d^9 + a^6*b^6*d^10)/((b*x + a)^6*b^6) + 15120*(b^14*c^7*d^3 - 7*a*b^13*c^6*d^4 + 21*a^2*b^12*c^5*d^5 - 35*a^3*b^11*c^4*d^6 + 35*a^4*b^10*c^3*d^7 - 21*a^5*b^9*c^2*d^8 + 7*a^6*b^8*c*d^9 - a^7*b^7*d^10)/((b*x + a)^7*b^7) + 11340*(b^16*c^8*d^2 - 8
```

$$\begin{aligned} & *a*b^{15}*c^7*d^3 + 28*a^2*b^{14}*c^6*d^4 - 56*a^3*b^{13}*c^5*d^5 + 70*a^4*b^{12}* \\ & ^4*d^6 - 56*a^5*b^{11}*c^3*d^7 + 28*a^6*b^{10}*c^2*d^8 - 8*a^7*b^9*c*d^9 + a^8* \\ & b^8*d^{10})/((b*x + a)^8*b^8))*(b*x + a)^9/b^{11} - 10*(b^9*c^9*d - 9*a*b^8*c^8 \\ & *d^2 + 36*a^2*b^7*c^7*d^3 - 84*a^3*b^6*c^6*d^4 + 126*a^4*b^5*c^5*d^5 - 126* \\ & a^5*b^4*c^4*d^6 + 84*a^6*b^3*c^3*d^7 - 36*a^7*b^2*c^2*d^8 + 9*a^8*b*c*d^9 - \\ & a^9*d^{10})*\log(\text{abs}(b*x + a)/((b*x + a)^2*\text{abs}(b)))/b^{11} - (b^{19}*c^{10}/(b*x + \\ & a) - 10*a*b^{18}*c^9*d/(b*x + a) + 45*a^2*b^{17}*c^8*d^2/(b*x + a) - 120*a^3*b^{16} \\ & *c^7*d^3/(b*x + a) + 210*a^4*b^{15}*c^6*d^4/(b*x + a) - 252*a^5*b^{14}*c^5*d^5/(b*x + a) \\ & + 210*a^6*b^{13}*c^4*d^6/(b*x + a) - 120*a^7*b^{12}*c^3*d^7/(b*x + a) + 45*a^8*b^{11} \\ & *c^2*d^8/(b*x + a) - 10*a^9*b^{10}*c*d^9/(b*x + a) + a^{10}*b^9*d^{10}/(b*x + a))/b^{20} \end{aligned}$$

maple [B] time = 0.02, size = 1066, normalized size = 4.13

$$\frac{d^{10}x^9}{9b^2} - \frac{ad^{10}x^8}{4b^3} + \frac{5cd^9x^8}{4b^2} + \frac{3a^2d^{10}x^7}{7b^4} - \frac{20acd^9x^7}{7b^3} + \frac{45c^2d^8x^7}{7b^2} - \frac{2a^3d^{10}x^6}{3b^5} + \frac{5a^2cd^9x^6}{b^4} - \frac{15a^2c^2d^8x^6}{b^3} + \frac{20c^3d^7x^6}{b^2} + \frac{a^4d^{10}x}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^2,x)

[Out] $45*d^2/b^2*c^8*x+9*d^{10}/b^{10}*a^8*x-10/b^{11}*d^{10}*\ln(b*x+a)*a^9+10/b^2*d*\ln(b*x+a)*c^9-1/b^{11}/(b*x+a)*a^{10}*d^{10}-4*d^{10}/b^9*x^2*a^7+60*d^3/b^2*x^2*c^7+3/7*d^{10}/b^4*x^7*a^2+45/7*d^8/b^2*x^7*c^2-2/3*d^{10}/b^5*x^6*a^3+20*d^7/b^2*x^6*c^3+42*d^6/b^2*x^5*c^4-3/2*d^{10}/b^7*x^4*a^5+63*d^5/b^2*x^4*c^5+7/3*d^{10}/b^8*x^3*a^6+70*d^4/b^2*x^3*c^6-1/4*d^{10}/b^3*x^8*a^5+4*d^9/b^2*x^8*c+d^{10}/b^6*x^5*a^4+1/9*d^{10}/b^2*x^9-1/b/(b*x+a)*c^{10}+10/b^2/(b*x+a)*a*c^9*d-1008*d^5/b^5*a^3*c^5*x+630*d^4/b^4*a^2*c^6*x-240*d^3/b^3*a*c^7*x+5*d^9/b^4*x^6*a^2*c-15*d^8/b^3*x^6*a*c^2-8*d^9/b^5*x^5*a^3*c+27*d^8/b^4*x^5*a^2*c^2-48*d^7/b^3*x^5*a*c^3+25/2*d^9/b^6*x^4*a^4*c+300*d^7/b^6*x^2*a^4*c^3-420*d^6/b^5*x^2*a^3*c^4+378*d^5/b^4*x^2*a^2*c^5-210*d^4/b^3*x^2*a*c^6-80*d^9/b^9*a^7*c*x+315*d^8/b^8*a^6*c^2*x-720*d^7/b^7*a^5*c^3*x+1050*d^6/b^6*a^4*c^4*x+35*d^9/b^8*x^2*a^6*c-135*d^8/b^7*x^2*a^5*c^2-90/b^3*d^2*\ln(b*x+a)*a*c^8+10/b^{10}/(b*x+a)*a^9*c*d^9-45/b^9/(b*x+a)*a^8*c^2*d^8+120/b^8/(b*x+a)*a^7*c^3*d^7-210/b^7/(b*x+a)*a^6*c^4*d^6+252/b^6/(b*x+a)*a^5*c^5*d^5-210/b^5/(b*x+a)*a^4*c^6*d^4+120/b^4/(b*x+a)*a^3*c^7*d^3-45/b^3/(b*x+a)*a^2*c^8*d^2-840/b^5*d^4*\ln(b*x+a)*a^3*c^6+360/b^4*d^3*\ln(b*x+a)*a^2*c^7-45*d^8/b^5*x^4*a^3*c^2+90*d^7/b^4*x^4*a^2*c^3-105*d^6/b^3*x^4*a*c^4-20*d^9/b^7*x^3*a^5*c+75*d^8/b^6*x^3*a^4*c^2-160*d^7/b^5*x^3*a^3*c^3+210*d^6/b^4*x^3*a^2*c^4-168*d^5/b^3*x^3*a*c^5-20/7*d^9/b^3*x^7*a*c+90/b^{10}*d^9*\ln(b*x+a)*a^8*c-360/b^9*d^8*\ln(b*x+a)*a^7*c^2+840/b^8*d^7*\ln(b*x+a)*a^6*c^3-1260/b^7*d^6*\ln(b*x+a)*a^5*c^4+1260/b^6*d^5*\ln(b*x+a)*a^4*c^5$

maxima [B] time = 1.39, size = 874, normalized size = 3.39

$$\frac{b^{10}c^{10} - 10ab^9c^9d + 45a^2b^8c^8d^2 - 120a^3b^7c^7d^3 + 210a^4b^6c^6d^4 - 252a^5b^5c^5d^5 + 210a^6b^4c^4d^6 - 120a^7b^3c^3d^7 + \dots}{b^{12}x + ab^{11}}$$

$$\begin{aligned}
& b^2 - (2*a*((2*a*((2*a*d^{10})/b^3 - (10*c*d^9)/b^2))/b - (a^2*d^{10})/b^4 + (4 \\
& 5*c^2*d^8)/b^2))/b + (a^2*((2*a*d^{10})/b^3 - (10*c*d^9)/b^2))/b^2 - (210 \\
& *c^4*d^6)/b^2 + (a^2*((2*a*((2*a*d^{10})/b^3 - (10*c*d^9)/b^2))/b - (a^2*d^{10} \\
&)/b^4 + (45*c^2*d^8)/b^2))/b^2 - (a^2*((120*c^3*d^7)/b^2 - (2*a*((2*a*(\\
& (2*a*d^{10})/b^3 - (10*c*d^9)/b^2))/b - (a^2*d^{10})/b^4 + (45*c^2*d^8)/b^2))/b \\
& + (a^2*((2*a*d^{10})/b^3 - (10*c*d^9)/b^2))/b^2 + (252*c^5*d^5)/b^2))/ \\
& b^2)/b) + x^4*((a*((2*a*((120*c^3*d^7)/b^2 - (2*a*((2*a*((2*a*d^{10})/b^3 - \\
& (10*c*d^9)/b^2))/b - (a^2*d^{10})/b^4 + (45*c^2*d^8)/b^2))/b + (a^2*((2*a*d^{10} \\
&)/b^3 - (10*c*d^9)/b^2))/b^2))/b - (210*c^4*d^6)/b^2 + (a^2*((2*a*((2*a*d^{10} \\
&)/b^3 - (10*c*d^9)/b^2))/b - (a^2*d^{10})/b^4 + (45*c^2*d^8)/b^2))/b^2)/(2 \\
& *b) - (a^2*((120*c^3*d^7)/b^2 - (2*a*((2*a*((2*a*d^{10})/b^3 - (10*c*d^9)/b^2 \\
&))/b - (a^2*d^{10})/b^4 + (45*c^2*d^8)/b^2))/b + (a^2*((2*a*d^{10})/b^3 - (10*c \\
& *d^9)/b^2))/b^2)/(4*b^2) + (63*c^5*d^5)/b^2) - (\log(a + b*x)*(10*a^9*d^{10} \\
& - 10*b^9*c^9*d + 90*a*b^8*c^8*d^2 - 360*a^2*b^7*c^7*d^3 + 840*a^3*b^6*c^6*d \\
& ^4 - 1260*a^4*b^5*c^5*d^5 + 1260*a^5*b^4*c^4*d^6 - 840*a^6*b^3*c^3*d^7 + 36 \\
& 0*a^7*b^2*c^2*d^8 - 90*a^8*b*c*d^9))/b^{11} - (a^{10}*d^{10} + b^{10}*c^{10} + 45*a^2 \\
& *b^8*c^8*d^2 - 120*a^3*b^7*c^7*d^3 + 210*a^4*b^6*c^6*d^4 - 252*a^5*b^5*c^5* \\
& d^5 + 210*a^6*b^4*c^4*d^6 - 120*a^7*b^3*c^3*d^7 + 45*a^8*b^2*c^2*d^8 - 10*a \\
& *b^9*c^9*d - 10*a^9*b*c*d^9)/(b*(a*b^{10} + b^{11}*x)) + (d^{10}*x^9)/(9*b^2)
\end{aligned}$$

sympy [B] time = 2.65, size = 816, normalized size = 3.16

$$x^8 \left(-\frac{ad^{10}}{4b^3} + \frac{5cd^9}{4b^2} \right) + x^7 \left(\frac{3a^2d^{10}}{7b^4} - \frac{20acd^9}{7b^3} + \frac{45c^2d^8}{7b^2} \right) + x^6 \left(-\frac{2a^3d^{10}}{3b^5} + \frac{5a^2cd^9}{b^4} - \frac{15ac^2d^8}{b^3} + \frac{20c^3d^7}{b^2} \right) + x^5 \left(\frac{a^4d^{10}}{b^6} - \frac{8a^3cd^9}{b^5} + \frac{27a^2c^2d^8}{b^4} - \frac{48a^1c^3d^7}{b^3} + \frac{42c^4d^6}{b^2} \right) + x^4 \left(-\frac{3a^5d^{10}}{2b^7} + \frac{25a^4c^1d^9}{2b^6} - \frac{45a^3c^2d^8}{b^5} + \frac{90a^2c^3d^7}{b^4} - \frac{105a^1c^4d^6}{b^3} + \frac{63c^5d^5}{b^2} \right) + x^3 \left(\frac{7a^6d^{10}}{3b^8} - \frac{20a^5c^1d^9}{b^7} + \frac{75a^4c^2d^8}{b^6} - \frac{160a^3c^3d^7}{b^5} + \frac{210a^2c^4d^6}{b^4} - \frac{168a^1c^5d^5}{b^3} + \frac{70c^6d^4}{b^2} \right) + x^2 \left(-\frac{4a^7d^{10}}{b^9} + \frac{35a^6c^1d^9}{b^8} - \frac{135a^5c^2d^8}{b^7} + \frac{300a^4c^3d^7}{b^6} - \frac{420a^3c^4d^6}{b^5} + \frac{378a^2c^5d^5}{b^4} - \frac{210a^1c^6d^4}{b^3} + \frac{60c^7d^3}{b^2} \right) + x \left(\frac{9a^8d^{10}}{b^{10}} - \frac{80a^7c^1d^9}{b^9} + \frac{315a^6c^2d^8}{b^8} - \frac{720a^5c^3d^7}{b^7} + \frac{1050a^4c^4d^6}{b^6} - \frac{1008a^3c^5d^5}{b^5} + \frac{630a^2c^6d^4}{b^4} - \frac{240a^1c^7d^3}{b^3} + \frac{45c^8d^2}{b^2} \right) + \frac{(-a^{10}d^{10} + 10a^9b^1c^1d^9 - 45a^8b^2c^2d^8 + 120a^7b^3c^3d^7 - 210a^6b^4c^4d^6 + 252a^5b^5c^5d^5 - 1260a^4b^5c^5d^5 + 1260a^5b^4c^4d^6 - 840a^6b^3c^3d^7 + 360a^7b^2c^2d^8 - 90a^8b^1c^1d^9)}{b^{11}} + \frac{d^{10}x^9}{9b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**2,x)

[Out] x**8*(-a*d**10/(4*b**3) + 5*c*d**9/(4*b**2)) + x**7*(3*a**2*d**10/(7*b**4) - 20*a*c*d**9/(7*b**3) + 45*c**2*d**8/(7*b**2)) + x**6*(-2*a**3*d**10/(3*b**5) + 5*a**2*c*d**9/b**4 - 15*a*c**2*d**8/b**3 + 20*c**3*d**7/b**2) + x**5*(a**4*d**10/b**6 - 8*a**3*c*d**9/b**5 + 27*a**2*c**2*d**8/b**4 - 48*a*c**3*d**7/b**3 + 42*c**4*d**6/b**2) + x**4*(-3*a**5*d**10/(2*b**7) + 25*a**4*c*d**9/(2*b**6) - 45*a**3*c**2*d**8/b**5 + 90*a**2*c**3*d**7/b**4 - 105*a*c**4*d**6/b**3 + 63*c**5*d**5/b**2) + x**3*(7*a**6*d**10/(3*b**8) - 20*a**5*c*d**9/b**7 + 75*a**4*c**2*d**8/b**6 - 160*a**3*c**3*d**7/b**5 + 210*a**2*c**4*d**6/b**4 - 168*a*c**5*d**5/b**3 + 70*c**6*d**4/b**2) + x**2*(-4*a**7*d**10/b**9 + 35*a**6*c*d**9/b**8 - 135*a**5*c**2*d**8/b**7 + 300*a**4*c**3*d**7/b**6 - 420*a**3*c**4*d**6/b**5 + 378*a**2*c**5*d**5/b**4 - 210*a*c**6*d**4/b**3 + 60*c**7*d**3/b**2) + x*(9*a**8*d**10/b**10 - 80*a**7*c*d**9/b**9 + 315*a**6*c**2*d**8/b**8 - 720*a**5*c**3*d**7/b**7 + 1050*a**4*c**4*d**6/b**6 - 1008*a**3*c**5*d**5/b**5 + 630*a**2*c**6*d**4/b**4 - 240*a*c**7*d**3/b**3 + 45*c**8*d**2/b**2) + (-a**10*d**10 + 10*a**9*b*c*d**9 - 45*a**8*b**2*c**2*d**8 + 120*a**7*b**3*c**3*d**7 - 210*a**6*b**4*c**4*d**6 + 252*a**5*b**5*c**5*d**5 - 1260*a**4*b**5*c**5*d**5 + 1260*a**5*b**4*c**4*d**6 - 840*a**6*b**3*c**3*d**7 + 360*a**7*b**2*c**2*d**8 - 90*a**8*b**1*c**1*d**9)/b**11 + d**10*x**9/9/b**2

$$\begin{aligned} &5c^{5}d^{5} - 210a^{4}b^{6}c^{6}d^{4} + 120a^{3}b^{7}c^{7}d^{3} - 45a^{2}b \\ &^{8}c^{8}d^{2} + 10ab^{9}c^{9}d - b^{10}c^{10})/(ab^{11} + b^{12}x) + d^{10} \\ &^{9}/(9b^{2}) - 10d(a^{d} - b^{c})^{9}\log(a + bx)/b^{11} \end{aligned}$$

$$3.1314 \quad \int \frac{(c+dx)^{10}}{(a+bx)^3} dx$$

Optimal. Leaf size=262

$$\frac{10d^9(a+bx)^7(bc-ad)}{7b^{11}} + \frac{15d^8(a+bx)^6(bc-ad)^2}{2b^{11}} + \frac{24d^7(a+bx)^5(bc-ad)^3}{b^{11}} + \frac{105d^6(a+bx)^4(bc-ad)^4}{2b^{11}} + \frac{84d^5(a+bx)^3(bc-ad)^5}{b^{11}} + \frac{105d^4(a+bx)^2(bc-ad)^6}{b^{11}} + \frac{84d^3(a+bx)(bc-ad)^7}{b^{11}} + \frac{10d^2(bc-ad)^8}{b^{11}} + \frac{10d^2(bc-ad)^8 \ln(a+bx)}{b^{11}}$$

[Out] $120*d^3*(-a*d+b*c)^7*x/b^{10}-1/2*(-a*d+b*c)^{10}/b^{11}/(b*x+a)^2-10*d*(-a*d+b*c)^9/b^{11}/(b*x+a)+105*d^4*(-a*d+b*c)^6*(b*x+a)^2/b^{11}+84*d^5*(-a*d+b*c)^5*(b*x+a)^3/b^{11}+105/2*d^6*(-a*d+b*c)^4*(b*x+a)^4/b^{11}+24*d^7*(-a*d+b*c)^3*(b*x+a)^5/b^{11}+15/2*d^8*(-a*d+b*c)^2*(b*x+a)^6/b^{11}+10/7*d^9*(-a*d+b*c)*(b*x+a)^7/b^{11}+1/8*d^{10}*(b*x+a)^8/b^{11}+45*d^2*(-a*d+b*c)^8*\ln(b*x+a)/b^{11}$

Rubi [A] time = 0.44, antiderivative size = 262, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{10d^9(a+bx)^7(bc-ad)}{7b^{11}} + \frac{15d^8(a+bx)^6(bc-ad)^2}{2b^{11}} + \frac{24d^7(a+bx)^5(bc-ad)^3}{b^{11}} + \frac{105d^6(a+bx)^4(bc-ad)^4}{2b^{11}} + \frac{84d^5(a+bx)^3(bc-ad)^5}{b^{11}} + \frac{105d^4(a+bx)^2(bc-ad)^6}{b^{11}} + \frac{84d^3(a+bx)(bc-ad)^7}{b^{11}} + \frac{10d^2(bc-ad)^8}{b^{11}} + \frac{10d^2(bc-ad)^8 \ln(a+bx)}{b^{11}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^3, x]

[Out] $(120*d^3*(b*c - a*d)^7*x)/b^{10} - (b*c - a*d)^{10}/(2*b^{11}*(a + b*x)^2) - (10*d*(b*c - a*d)^9)/(b^{11}*(a + b*x)) + (105*d^4*(b*c - a*d)^6*(a + b*x)^2)/b^{11} + (84*d^5*(b*c - a*d)^5*(a + b*x)^3)/b^{11} + (105*d^6*(b*c - a*d)^4*(a + b*x)^4)/(2*b^{11}) + (24*d^7*(b*c - a*d)^3*(a + b*x)^5)/b^{11} + (15*d^8*(b*c - a*d)^2*(a + b*x)^6)/(2*b^{11}) + (10*d^9*(b*c - a*d)*(a + b*x)^7)/(7*b^{11}) + (d^{10}*(a + b*x)^8)/(8*b^{11}) + (45*d^2*(b*c - a*d)^8*\text{Log}[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\int \frac{(c + dx)^{10}}{(a + bx)^3} dx = \int \left(\frac{120d^3(bc - ad)^7}{b^{10}} + \frac{(bc - ad)^{10}}{b^{10}(a + bx)^3} + \frac{10d(bc - ad)^9}{b^{10}(a + bx)^2} + \frac{45d^2(bc - ad)^8}{b^{10}(a + bx)} + \frac{210d^4(bc - ad)^6(a + bx)}{b^{10}} \right) dx$$

$$= \frac{120d^3(bc - ad)^7 x}{b^{10}} - \frac{(bc - ad)^{10}}{2b^{11}(a + bx)^2} - \frac{10d(bc - ad)^9}{b^{11}(a + bx)} + \frac{105d^4(bc - ad)^6(a + bx)^2}{b^{11}} + \frac{84d^5(bc - ad)^5(a + bx)}{b^{11}}$$

Mathematica [B] time = 0.24, size = 708, normalized size = 2.70

$$\frac{532a^{10}d^{10} - 56a^9bd^9(85c + 26dx) + 28a^8b^2d^8(675c^2 + 380cdx - 116d^2x^2) - 280a^7b^3d^7(156c^3 + 117c^2dx - 91cd^2x^2 + 3d^3x^3) + 210a^6b^4d^6(308c^4 + 256c^3dx - 414c^2d^2x^2 + 32cd^3x^3 + d^4x^4) - 84a^5b^5d^5(756c^5 + 560c^4dx - 2000c^3d^2x^2 + 280c^2d^3x^3 + 20cd^4x^4 + d^5x^5) + 42a^4b^6d^4(980c^6 + 336c^5dx - 4760c^4d^2x^2 + 1120c^3d^3x^3 + 140c^2d^4x^4 + 16cd^5x^5 + d^6x^6) - 24a^3b^7d^3(700c^7 - 490c^6dx - 6174c^5d^2x^2 + 2450c^4d^3x^3 + 490c^3d^4x^4 + 98c^2d^5x^5 + 14cd^6x^6 + d^7x^7) + 3a^2b^8d^2(1260c^8 - 4480c^7dx - 21560c^6d^2x^2 + 15680c^5d^3x^3 + 4900c^4d^4x^4 + 1568c^3d^5x^5 + 392c^2d^6x^6 + 64cd^7x^7 + 5d^8x^8) - 2ab^9d(140c^9 - 2520c^8dx - 6720c^7d^2x^2 + 11760c^6d^3x^3 + 5880c^5d^4x^4 + 2940c^4d^5x^5 + 1176c^3d^6x^6 + 336c^2d^7x^7 + 60cd^8x^8 + 5d^9x^9) + b^{10}(-28c^{10} - 560c^9dx + 6720c^7d^3x^3 + 5880c^6d^4x^4 + 4704c^5d^5x^5 + 2940c^4d^6x^6 + 1344c^3d^7x^7 + 420c^2d^8x^8 + 80cd^9x^9 + 7d^{10}x^{10}) + 2520d^2(bc - ad)^8(a + bx)^2 \operatorname{Log}[a + bx]}{(56b^{11}(a + bx)^2)}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^3,x]

[Out] (532*a^10*d^10 - 56*a^9*b*d^9*(85*c + 26*d*x) + 28*a^8*b^2*d^8*(675*c^2 + 380*c*d*x - 116*d^2*x^2) - 280*a^7*b^3*d^7*(156*c^3 + 117*c^2*d*x - 91*c*d^2*x^2 + 3*d^3*x^3) + 210*a^6*b^4*d^6*(308*c^4 + 256*c^3*d*x - 414*c^2*d^2*x^2 + 32*c*d^3*x^3 + d^4*x^4) - 84*a^5*b^5*d^5*(756*c^5 + 560*c^4*d*x - 2000*c^3*d^2*x^2 + 280*c^2*d^3*x^3 + 20*c*d^4*x^4 + d^5*x^5) + 42*a^4*b^6*d^4*(980*c^6 + 336*c^5*d*x - 4760*c^4*d^2*x^2 + 1120*c^3*d^3*x^3 + 140*c^2*d^4*x^4 + 16*c*d^5*x^5 + d^6*x^6) - 24*a^3*b^7*d^3*(700*c^7 - 490*c^6*d*x - 6174*c^5*d^2*x^2 + 2450*c^4*d^3*x^3 + 490*c^3*d^4*x^4 + 98*c^2*d^5*x^5 + 14*c*d^6*x^6 + d^7*x^7) + 3*a^2*b^8*d^2*(1260*c^8 - 4480*c^7*d*x - 21560*c^6*d^2*x^2 + 15680*c^5*d^3*x^3 + 4900*c^4*d^4*x^4 + 1568*c^3*d^5*x^5 + 392*c^2*d^6*x^6 + 64*c*d^7*x^7 + 5*d^8*x^8) - 2*a*b^9*d*(140*c^9 - 2520*c^8*d*x - 6720*c^7*d^2*x^2 + 11760*c^6*d^3*x^3 + 5880*c^5*d^4*x^4 + 2940*c^4*d^5*x^5 + 1176*c^3*d^6*x^6 + 336*c^2*d^7*x^7 + 60*c*d^8*x^8 + 5*d^9*x^9) + b^10*(-28*c^10 - 560*c^9*d*x + 6720*c^7*d^3*x^3 + 5880*c^6*d^4*x^4 + 4704*c^5*d^5*x^5 + 2940*c^4*d^6*x^6 + 1344*c^3*d^7*x^7 + 420*c^2*d^8*x^8 + 80*c*d^9*x^9 + 7*d^10*x^10) + 2520*d^2*(b*c - a*d)^8*(a + b*x)^2*Log[a + b*x])/(56*b^11*(a + b*x)^2)

fricas [B] time = 0.46, size = 1233, normalized size = 4.71

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^3,x, algorithm="fricas")

[Out] 1/56*(7*b^10*d^10*x^10 - 28*b^10*c^10 - 280*a*b^9*c^9*d + 3780*a^2*b^8*c^8*d^2 - 16800*a^3*b^7*c^7*d^3 + 41160*a^4*b^6*c^6*d^4 - 63504*a^5*b^5*c^5*d^5

$$\begin{aligned}
& + 64680a^6b^4c^4d^6 - 43680a^7b^3c^3d^7 + 18900a^8b^2c^2d^8 - \\
& 4760a^9b^1c^1d^9 + 532a^{10}d^{10} + 10(8b^{10}c^1d^9 - ab^9d^{10})x^9 + 15(\\
& (28b^{10}c^2d^8 - 8a^2b^9c^1d^9 + a^2b^8d^{10})x^8 + 24(56b^{10}c^3d^7 \\
& - 28a^2b^9c^2d^8 + 8a^2b^8c^1d^9 - a^3b^7d^{10})x^7 + 42(70b^{10}c^4d^6 \\
& - 56a^2b^9c^3d^7 + 28a^2b^8c^2d^8 - 8a^3b^7c^1d^9 + a^4b^6d^{10}) \\
& x^6 + 84(56b^{10}c^5d^5 - 70a^2b^9c^4d^6 + 56a^2b^8c^3d^7 - 28a^3 \\
& b^7c^2d^8 + 8a^4b^6c^1d^9 - a^5b^5d^{10})x^5 + 210(28b^{10}c^6d^4 \\
& - 56a^2b^9c^5d^5 + 70a^2b^8c^4d^6 - 56a^3b^7c^3d^7 + 28a^4b^6c^2d^8 \\
& - 8a^5b^5c^1d^9 + a^6b^4d^{10})x^4 + 840(8b^{10}c^7d^3 - 28a^2 \\
& b^9c^6d^4 + 56a^2b^8c^5d^5 - 70a^3b^7c^4d^6 + 56a^4b^6c^3d^7 \\
& - 28a^5b^5c^2d^8 + 8a^6b^4c^1d^9 - a^7b^3d^{10})x^3 + 28(480a^2b^9c^7d^3 \\
& - 2310a^2b^8c^6d^4 + 5292a^3b^7c^5d^5 - 7140a^4b^6c^4d^6 + 6000a^5b^5c^3d^7 \\
& - 3105a^6b^4c^2d^8 + 910a^7b^3c^1d^9 - 116a^8b^2d^{10})x^2 - 56(10b^{10}c^9d \\
& - 90a^2b^9c^8d^2 + 240a^2b^8c^7d^3 - 210a^3b^7c^6d^4 - 252a^4b^6c^5d^5 \\
& + 840a^5b^5c^4d^6 - 960a^6b^4c^3d^7 + 585a^7b^3c^2d^8 - 190a^8b^2c^1d^9 + 26a^9b^1d^{10}) \\
& x + 2520(a^2b^8c^8d^2 - 8a^3b^7c^7d^3 + 28a^4b^6c^6d^4 - 56a^5b^5c^5d^5 \\
& + 70a^6b^4c^4d^6 - 56a^7b^3c^3d^7 + 28a^8b^2c^2d^8 - 8a^9b^1c^1d^9 + a^{10}d^{10} \\
& + (b^{10}c^8d^2 - 8a^2b^9c^7d^3 + 28a^2b^8c^6d^4 - 56a^3b^7c^5d^5 + 70a^4b^6c^4d^6 \\
& - 56a^5b^5c^3d^7 + 28a^6b^4c^2d^8 - 8a^7b^3c^1d^9 + a^8b^2d^{10})x^2 + 2(a^2b^9c^8d^2 \\
& - 8a^2b^8c^7d^3 + 28a^3b^7c^6d^4 - 56a^4b^6c^5d^5 + 70a^5b^5c^4d^6 - 56a^6b^4c^3d^7 \\
& + 28a^7b^3c^2d^8 - 8a^8b^2c^1d^9 + a^9b^1d^{10})x) \log(bx + a) / (b^{13}x^2 + 2a^2b^{11})
\end{aligned}$$

giac [B] time = 1.25, size = 924, normalized size = 3.53

$$\frac{45(b^8c^8d^2 - 8ab^7c^7d^3 + 28a^2b^6c^6d^4 - 56a^3b^5c^5d^5 + 70a^4b^4c^4d^6 - 56a^5b^3c^3d^7 + 28a^6b^2c^2d^8 - 8a^7bcd^9 + a^8d^{10})}{b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((dx+c)^10/(b*x+a)^3,x, algorithm="giac")

[Out] 45*(b^8c^8d^2 - 8a^2b^7c^7d^3 + 28a^2b^6c^6d^4 - 56a^3b^5c^5d^5 + 70a^4b^4c^4d^6 - 56a^5b^3c^3d^7 + 28a^6b^2c^2d^8 - 8a^7b^1c^1d^9 + a^8d^10)*log(abs(b*x + a))/b^11 - 1/2*(b^10c^10 + 10a^2b^9c^9d - 135a^2b^8c^8d^2 + 600a^3b^7c^7d^3 - 1470a^4b^6c^6d^4 + 2268a^5b^5c^5d^5 - 2310a^6b^4c^4d^6 + 1560a^7b^3c^3d^7 - 675a^8b^2c^2d^8 + 170a^9b^1c^1d^9 - 19a^10d^10 + 20*(b^10c^9d - 9a^2b^9c^8d^2 + 36a^2b^8c^7d^3 - 84a^3b^7c^6d^4 + 126a^4b^6c^5d^5 - 126a^5b^5c^4d^6 + 84a^6b^4c^3d^7 - 36a^7b^3c^2d^8 + 9a^8b^2c^1d^9 - a^9b^1d^10)*x)/((b*x + a)^2b^11) + 1/56*(7b^21d^10*x^8 + 80b^21c^1d^9*x^7 - 24a^2b^20d^10*x^7 + 420b^21c^2d^8*x^6 - 280a^2b^20c^1d^9*x^6 + 56a^2b^19d^10*x^6 + 1344b^21c^3d^7*x^5 - 1512a^2b^20c^2d^8*x^5 + 672a^2

$$\begin{aligned} & *b^{19}c^9d^9x^5 - 112a^3b^{18}d^{10}x^5 + 2940b^{21}c^4d^6x^4 - 5040a*b^{20}c^3d^7x^4 + 3780a^2b^{19}c^2d^8x^4 - 1400a^3b^{18}c*d^9x^4 + 210a^4b^{17}d^{10}x^4 + 4704b^{21}c^5d^5x^3 - 11760a*b^{20}c^4d^6x^3 + 13440a^2b^{19}c^3d^7x^3 - 8400a^3b^{18}c^2d^8x^3 + 2800a^4b^{17}c*d^9x^3 - 392a^5b^{16}d^{10}x^3 + 5880b^{21}c^6d^4x^2 - 21168a*b^{20}c^5d^5x^2 + 35280a^2b^{19}c^4d^6x^2 - 33600a^3b^{18}c^3d^7x^2 + 18900a^4b^{17}c^2d^8x^2 - 5880a^5b^{16}c*d^9x^2 + 784a^6b^{15}d^{10}x^2 + 6720b^{21}c^7d^3x - 35280a*b^{20}c^6d^4x + 84672a^2b^{19}c^5d^5x - 117600a^3b^{18}c^4d^6x + 100800a^4b^{17}c^3d^7x - 52920a^5b^{16}c^2d^8x + 15680a^6b^{15}c*d^9x - 2016a^7b^{14}d^{10}x)/b^{24} \end{aligned}$$

maple [B] time = 0.02, size = 1105, normalized size = 4.22

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((d*x+c)^{10}/(b*x+a)^3, x)$

[Out]
$$\begin{aligned} & -1/2/b^{11}/(b*x+a)^2*a^{10}d^{10}+45/b^{11}d^{10}*\ln(b*x+a)*a^8+45/b^3d^2*\ln(b*x+a)*c^8+10/b^{11}d^{10}/(b*x+a)*a^9-10/b^2d/(b*x+a)*c^9+105/2*d^6/b^3*x^4*c^4-7*d^{10}/b^8*x^3*a^5+84*d^5/b^3*x^3*c^5+14*d^{10}/b^9*x^2*a^6+105*d^4/b^3*x^2*c^6-3/7*d^{10}/b^4*x^7*a+10/7*d^9/b^3*x^7*c+15/2*d^8/b^3*x^6*c^2-2*d^{10}/b^6*x^5*a^3+24*d^7/b^3*x^5*c^3+15/4*d^{10}/b^7*x^4*a^4+d^{10}/b^5*x^6*a^2-36*d^{10}/b^10*a^7*x+120*d^3/b^3*c^7*x-105/b^5/(b*x+a)^2*a^4*c^6*d^4+60/b^4/(b*x+a)^2*a^3*c^7*d^3-45/2/b^3/(b*x+a)^2*a^2*c^8*d^2+5/b^2/(b*x+a)^2*a*c^9*d-360/b^{10}d^9*\ln(b*x+a)*a^7*c+1/8*d^{10}/b^3*x^8-1/2/b/(b*x+a)^2*c^{10}+1260/b^9*d^8*\ln(b*x+a)*a^6*c^2-2520/b^8*d^7*\ln(b*x+a)*a^5*c^3+3150/b^7*d^6*\ln(b*x+a)*a^4*c^4-2520/b^6*d^5*\ln(b*x+a)*a^3*c^5+1260/b^5*d^4*\ln(b*x+a)*a^2*c^6-360/b^4*d^3*\ln(b*x+a)*a*c^7-90/b^{10}d^9/(b*x+a)*a^8*c+360/b^9*d^8/(b*x+a)*a^7*c^2-840/b^8*d^7/(b*x+a)*a^6*c^3+1260/b^7*d^6/(b*x+a)*a^5*c^4-1260/b^6*d^5/(b*x+a)*a^4*c^5+840/b^5*d^4/(b*x+a)*a^3*c^6-360/b^4*d^3/(b*x+a)*a^2*c^7+90/b^3*d^2/(b*x+a)*a*c^8+675/2*d^8/b^7*x^2*a^4*c^2-600*d^7/b^6*x^2*a^3*c^3+630*d^6/b^5*x^2*a^2*c^4-378*d^5/b^4*x^2*a*c^5+280*d^9/b^9*a^6*c*x-945*d^8/b^8*a^5*c^2*x+1800*d^7/b^7*a^4*c^3*x-2100*d^6/b^6*a^3*c^4*x+1512*d^5/b^5*a^2*c^5*x-630*d^4/b^4*a*c^6*x-27*d^8/b^4*x^5*a*c^2-25*d^9/b^6*x^4*a^3*c+135/2*d^8/b^5*x^4*a^2*c^2-90*d^7/b^4*x^4*a*c^3+50*d^9/b^7*x^3*a^4*c-150*d^8/b^6*x^3*a^3*c^2+240*d^7/b^5*x^3*a^2*c^3-210*d^6/b^4*x^3*a*c^4-105*d^9/b^8*x^2*a^5*c-5*d^9/b^4*x^6*a*c+12*d^9/b^5*x^5*a^2*c+5/b^{10}/(b*x+a)^2*a^9*c*d^9-45/2/b^9/(b*x+a)^2*a^8*c^2*d^8+60/b^8/(b*x+a)^2*a^7*c^3*d^7-105/b^7/(b*x+a)^2*a^6*c^4*d^6+126/b^6/(b*x+a)^2*a^5*c^5*d^5 \end{aligned}$$

maxima [B] time = 1.62, size = 881, normalized size = 3.36

$$b^{10}c^{10} + 10ab^9c^9d - 135a^2b^8c^8d^2 + 600a^3b^7c^7d^3 - 1470a^4b^6c^6d^4 + 2268a^5b^5c^5d^5 - 2310a^6b^4c^4d^6 + 1560a^7b^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^3,x, algorithm="maxima")

[Out]
$$\begin{aligned} & -1/2*(b^{10}c^{10} + 10*a*b^9*c^9*d - 135*a^2*b^8*c^8*d^2 + 600*a^3*b^7*c^7*d^3 - 1470*a^4*b^6*c^6*d^4 + 2268*a^5*b^5*c^5*d^5 - 2310*a^6*b^4*c^4*d^6 + 1560*a^7*b^3*c^3*d^7 - 675*a^8*b^2*c^2*d^8 + 170*a^9*b*c*d^9 - 19*a^{10}*d^{10} + \\ & 20*(b^{10}c^9*d - 9*a*b^9*c^8*d^2 + 36*a^2*b^8*c^7*d^3 - 84*a^3*b^7*c^6*d^4 + 126*a^4*b^6*c^5*d^5 - 126*a^5*b^5*c^4*d^6 + 84*a^6*b^4*c^3*d^7 - 36*a^7*b^3*c^2*d^8 + 9*a^8*b^2*c*d^9 - a^9*b*d^{10})*x)/(b^{13}x^2 + 2*a*b^{12}x + a^2*b^{11}) + 1/56*(7*b^7*d^{10}x^8 + 8*(10*b^7*c*d^9 - 3*a*b^6*d^{10})*x^7 + 28*(15*b^7*c^2*d^8 - 10*a*b^6*c*d^9 + 2*a^2*b^5*d^{10})*x^6 + 56*(24*b^7*c^3*d^7 - 27*a*b^6*c^2*d^8 + 12*a^2*b^5*c*d^9 - 2*a^3*b^4*d^{10})*x^5 + 70*(42*b^7*c^4*d^6 - 72*a*b^6*c^3*d^7 + 54*a^2*b^5*c^2*d^8 - 20*a^3*b^4*c*d^9 + 3*a^4*b^3*d^{10})*x^4 + 56*(84*b^7*c^5*d^5 - 210*a*b^6*c^4*d^6 + 240*a^2*b^5*c^3*d^7 - 150*a^3*b^4*c^2*d^8 + 50*a^4*b^3*c*d^9 - 7*a^5*b^2*d^{10})*x^3 + 28*(210*b^7*c^6*d^4 - 756*a*b^6*c^5*d^5 + 1260*a^2*b^5*c^4*d^6 - 1200*a^3*b^4*c^3*d^7 + 675*a^4*b^3*c^2*d^8 - 210*a^5*b^2*c*d^9 + 28*a^6*b*d^{10})*x^2 + 56*(120*b^7*c^7*d^3 - 630*a*b^6*c^6*d^4 + 1512*a^2*b^5*c^5*d^5 - 2100*a^3*b^4*c^4*d^6 + 1800*a^4*b^3*c^3*d^7 - 945*a^5*b^2*c^2*d^8 + 280*a^6*b*c*d^9 - 36*a^7*d^{10})*x)/b^{10} + 45*(b^8*c^8*d^2 - 8*a*b^7*c^7*d^3 + 28*a^2*b^6*c^6*d^4 - 56*a^3*b^5*c^5*d^5 + 70*a^4*b^4*c^4*d^6 - 56*a^5*b^3*c^3*d^7 + 28*a^6*b^2*c^2*d^8 - 8*a^7*b*c*d^9 + a^8*d^{10})*log(b*x + a)/b^{11} \end{aligned}$$

mupad [B] time = 0.38, size = 3299, normalized size = 12.59

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^3,x)

[Out]
$$\begin{aligned} & x^3*((84*c^5*d^5)/b^3 - (a*((3*a*((3*a*((3*a*((3*a*d^{10})/b^4 - (10*c*d^9)/b^3))/b - (3*a^2*d^{10})/b^5 + (45*c^2*d^8)/b^3))/b + (a^3*d^{10})/b^6 - (120*c^3*d^7)/b^3 - (3*a^2*((3*a*d^{10})/b^4 - (10*c*d^9)/b^3))/b^2))/b + (210*c^4*d^6)/b^3 + (a^3*((3*a*d^{10})/b^4 - (10*c*d^9)/b^3))/b^3 - (3*a^2*((3*a*((3*a*d^{10})/b^4 - (10*c*d^9)/b^3))/b - (3*a^2*d^{10})/b^5 + (45*c^2*d^8)/b^3))/b^2))/b + (a^2*((3*a*((3*a*((3*a*d^{10})/b^4 - (10*c*d^9)/b^3))/b - (3*a^2*d^{10})/b^5 + (45*c^2*d^8)/b^3))/b + (a^3*d^{10})/b^6 - (120*c^3*d^7)/b^3 - (3*a^2*((3*a*d^{10})/b^4 - (10*c*d^9)/b^3))/b^2))/b^2 - (a^3*((3*a*((3*a*d^{10})/b^4 - (10*c*d^9)/b^3))/b - (3*a^2*d^{10})/b^5 + (45*c^2*d^8)/b^3))/(3*b^3)) - x^7*((3*a*d^{10})/(7*b^4) - (10*c*d^9)/(7*b^3)) - ((b^{10}c^{10} - 19*a^{10}d^{10} - 135*a^2*b^8*c^8*d^2 + 600*a^3*b^7*c^7*d^3 - 1470*a^4*b^6*c^6*d^4 + 2268*a^5*b^5*c^5*d^5 - 2310*a^6*b^4*c^4*d^6 + 1560*a^7*b^3*c^3*d^7 - 675*a^8*b^2*c^2*d^8 + 10*a*b^9*c^9*d + 170*a^9*b*c*d^9)/(2*b) - x*(10*a^9*d^{10} - 10*b^9*c^9*d + 90*a*b^8*c^8*d^2 - 360*a^2*b^7*c^7*d^3 + 840*a^3*b^6*c^6*d^4 - 1260*a^4*b^5*c^5*d^5 - 1080*a^5*b^4*c^4*d^6 + 720*a^6*b^3*c^3*d^7 - 360*a^7*b^2*c^2*d^8 + 120*a^8*b*c*d^9 - 10*a^9*d^{10}))/b^{11} \end{aligned}$$

$$\begin{aligned} &)/b - (3a^2d^{10})/b^5 + (45c^2d^8)/b^3)/b + (a^3d^{10})/b^6 - (120c^3d^7)/b^3 - (3a^2*((3ad^{10})/b^4 - (10c^2d^9)/b^3))/b^2)/b + (210c^4d^6)/b^3 + (a^3*((3ad^{10})/b^4 - (10c^2d^9)/b^3))/b^3 - (3a^2*((3a*((3ad^{10})/b^4 - (10c^2d^9)/b^3))/b - (3a^2d^{10})/b^5 + (45c^2d^8)/b^3))/b^2)/b^3 + (120c^7d^3)/b^3 - (3a^2*((252c^5d^5)/b^3 - (3a*((3a*((3a*((3ad^{10})/b^4 - (10c^2d^9)/b^3))/b - (3a^2d^{10})/b^5 + (45c^2d^8)/b^3))/b + (a^3d^{10})/b^6 - (120c^3d^7)/b^3 - (3a^2*((3ad^{10})/b^4 - (10c^2d^9)/b^3))/b^2))/b + (210c^4d^6)/b^3 + (a^3*((3ad^{10})/b^4 - (10c^2d^9)/b^3))/b^3 - (3a^2*((3a*((3ad^{10})/b^4 - (10c^2d^9)/b^3))/b - (3a^2d^{10})/b^5 + (45c^2d^8)/b^3))/b^2)/b + (3a^2*((3a*((3a*((3ad^{10})/b^4 - (10c^2d^9)/b^3))/b - (3a^2d^{10})/b^5 + (45c^2d^8)/b^3))/b + (a^3d^{10})/b^6 - (120c^3d^7)/b^3 - (3a^2*((3ad^{10})/b^4 - (10c^2d^9)/b^3))/b^2))/b^2 - (a^3*((3a*((3ad^{10})/b^4 - (10c^2d^9)/b^3))/b - (3a^2d^{10})/b^5 + (45c^2d^8)/b^3))/b^3)/b^2 + (\log(a + bx)*(45a^8d^{10} + 45b^8c^8d^2 - 360ab^7c^7d^3 + 1260a^2b^6c^6d^4 - 2520a^3b^5c^5d^5 + 3150a^4b^4c^4d^6 - 2520a^5b^3c^3d^7 + 1260a^6b^2c^2d^8 - 360a^7b^1c^1d^9))/b^{11} + (d^{10}x^8)/(8b^3) \end{aligned}$$

sympy [B] time = 5.67, size = 843, normalized size = 3.22

$$x^7 \left(-\frac{3ad^{10}}{7b^4} + \frac{10cd^9}{7b^3} \right) + x^6 \left(\frac{a^2d^{10}}{b^5} - \frac{5acd^9}{b^4} + \frac{15c^2d^8}{2b^3} \right) + x^5 \left(-\frac{2a^3d^{10}}{b^6} + \frac{12a^2cd^9}{b^5} - \frac{27ac^2d^8}{b^4} + \frac{24c^3d^7}{b^3} \right) + x^4 \left(\frac{15a^4d^7}{4b^7} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**3,x)

[Out] x**7*(-3*a*d**10/(7*b**4) + 10*c*d**9/(7*b**3)) + x**6*(a**2*d**10/b**5 - 5*a*c*d**9/b**4 + 15*c**2*d**8/(2*b**3)) + x**5*(-2*a**3*d**10/b**6 + 12*a**2*c*d**9/b**5 - 27*a*c**2*d**8/b**4 + 24*c**3*d**7/b**3) + x**4*(15*a**4*d**10/(4*b**7) - 25*a**3*c*d**9/b**6 + 135*a**2*c**2*d**8/(2*b**5) - 90*a*c**3*d**7/b**4 + 105*c**4*d**6/(2*b**3)) + x**3*(-7*a**5*d**10/b**8 + 50*a**4*c*d**9/b**7 - 150*a**3*c**2*d**8/b**6 + 240*a**2*c**3*d**7/b**5 - 210*a*c**4*d**6/b**4 + 84*c**5*d**5/b**3) + x**2*(14*a**6*d**10/b**9 - 105*a**5*c*d**9/b**8 + 675*a**4*c**2*d**8/(2*b**7) - 600*a**3*c**3*d**7/b**6 + 630*a**2*c**4*d**6/b**5 - 378*a*c**5*d**5/b**4 + 105*c**6*d**4/b**3) + x*(-36*a**7*d**10/b**10 + 280*a**6*c*d**9/b**9 - 945*a**5*c**2*d**8/b**8 + 1800*a**4*c**3*d**7/b**7 - 2100*a**3*c**4*d**6/b**6 + 1512*a**2*c**5*d**5/b**5 - 630*a*c**6*d**4/b**4 + 120*c**7*d**3/b**3) + (19*a**10*d**10 - 170*a**9*b*c*d**9 + 675*a**8*b**2*c**2*d**8 - 1560*a**7*b**3*c**3*d**7 + 2310*a**6*b**4*c**4*d**6 - 2268*a**5*b**5*c**5*d**5 + 1470*a**4*b**6*c**6*d**4 - 600*a**3*b**7*c**7*d**3 + 135*a**2*b**8*c**8*d**2 - 10*a*b**9*c**9*d - b**10*c**10 + x*(20*a**9*b*d**10 - 180*a**8*b**2*c*d**9 + 720*a**7*b**3*c**2*d**8 - 1680*a**6*b**4*c**3*d**7 + 2520*a**5*b**5*c**4*d**6 - 2520*a**4*b**6*c**5*d**5 + 1680*a**3*b**7*c**6*d**4 - 720*a**2*b**8*c**7*d**3 + 180*a*b**9*c**8*d**2 - 20*

$$\frac{b^{10}c^9d}{(2a^2b^{11} + 4ab^{12}x + 2b^{13}x^2)} + \frac{d^{10}x^8}{(8b^3)} + 45d^2(a d - b c)^8 \log(a + b x) / b^{11}$$

$$3.1315 \quad \int \frac{(c+dx)^{10}}{(a+bx)^4} dx$$

Optimal. Leaf size=258

$$\frac{5d^9(a+bx)^6(bc-ad)}{3b^{11}} + \frac{9d^8(a+bx)^5(bc-ad)^2}{b^{11}} + \frac{30d^7(a+bx)^4(bc-ad)^3}{b^{11}} + \frac{70d^6(a+bx)^3(bc-ad)^4}{b^{11}} + \frac{126d^5(a+bx)^2(bc-ad)^5}{b^{11}} + \frac{70d^4(a+bx)(bc-ad)^6}{b^{11}} + \frac{120d^3(bc-ad)^7 \ln(bx+a)}{b^{11}}$$

[Out] $210*d^4*(-a*d+b*c)^6*x/b^{10}-1/3*(-a*d+b*c)^{10}/b^{11}/(b*x+a)^3-5*d*(-a*d+b*c)^9/b^{11}/(b*x+a)^2-45*d^2*(-a*d+b*c)^8/b^{11}/(b*x+a)+126*d^5*(-a*d+b*c)^5*(b*x+a)^2/b^{11}+70*d^6*(-a*d+b*c)^4*(b*x+a)^3/b^{11}+30*d^7*(-a*d+b*c)^3*(b*x+a)^4/b^{11}+9*d^8*(-a*d+b*c)^2*(b*x+a)^5/b^{11}+5/3*d^9*(-a*d+b*c)*(b*x+a)^6/b^{11}+1/7*d^{10}*(b*x+a)^7/b^{11}+120*d^3*(-a*d+b*c)^7*\ln(b*x+a)/b^{11}$

Rubi [A] time = 0.44, antiderivative size = 258, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{5d^9(a+bx)^6(bc-ad)}{3b^{11}} + \frac{9d^8(a+bx)^5(bc-ad)^2}{b^{11}} + \frac{30d^7(a+bx)^4(bc-ad)^3}{b^{11}} + \frac{70d^6(a+bx)^3(bc-ad)^4}{b^{11}} + \frac{126d^5(a+bx)^2(bc-ad)^5}{b^{11}} + \frac{70d^4(a+bx)(bc-ad)^6}{b^{11}} + \frac{120d^3(bc-ad)^7 \ln(bx+a)}{b^{11}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^4, x]

[Out] $(210*d^4*(b*c - a*d)^6*x)/b^{10} - (b*c - a*d)^{10}/(3*b^{11}*(a + b*x)^3) - (5*d*(b*c - a*d)^9)/(b^{11}*(a + b*x)^2) - (45*d^2*(b*c - a*d)^8)/(b^{11}*(a + b*x)) + (126*d^5*(b*c - a*d)^5*(a + b*x)^2)/b^{11} + (70*d^6*(b*c - a*d)^4*(a + b*x)^3)/b^{11} + (30*d^7*(b*c - a*d)^3*(a + b*x)^4)/b^{11} + (9*d^8*(b*c - a*d)^2*(a + b*x)^5)/b^{11} + (5*d^9*(b*c - a*d)*(a + b*x)^6)/(3*b^{11}) + (d^{10}*(a + b*x)^7)/(7*b^{11}) + (120*d^3*(b*c - a*d)^7*\text{Log}[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c + dx)^{10}}{(a + bx)^4} dx = \int \left(\frac{210d^4(bc - ad)^6}{b^{10}} + \frac{(bc - ad)^{10}}{b^{10}(a + bx)^4} + \frac{10d(bc - ad)^9}{b^{10}(a + bx)^3} + \frac{45d^2(bc - ad)^8}{b^{10}(a + bx)^2} + \frac{120d^3(bc - ad)^7}{b^{10}(a + bx)} + \frac{210d^4(bc - ad)^6}{b^{10}} \right) dx$$

$$= \frac{210d^4(bc - ad)^6 x}{b^{10}} - \frac{(bc - ad)^{10}}{3b^{11}(a + bx)^3} - \frac{5d(bc - ad)^9}{b^{11}(a + bx)^2} - \frac{45d^2(bc - ad)^8}{b^{11}(a + bx)} + \frac{126d^5(bc - ad)^5(a + bx)}{b^{11}}$$

Mathematica [A] time = 0.18, size = 427, normalized size = 1.66

$$21b^5d^8x^5(2a^2d^2 - 8abcd + 9b^2c^2) + 105b^4d^7x^4(-a^3d^3 + 5a^2bcd^2 - 9ab^2c^2d + 6b^3c^3) + 35b^3d^6x^3(7a^4d^4 - 40a^3bcd^3 + 105a^2b^2c^2d^2 - 420a^2b^3c^3d^2 - 450a^3b^2c^2d^3 + 175a^4b^3c^3d^4 - 28a^5d^5)x^2 + 35b^3d^6(42b^4c^4 - 96a^2b^3c^3d + 90a^2b^2c^2d^2 - 40a^3b^2c^2d^3 + 7a^4d^4)x^3 + 105b^4d^7(6b^3c^3 - 9a^2b^2c^2d + 5a^2b^2c^2d^2 - a^3d^3)x^4 + 21b^5d^8(9b^2c^2 - 8a^2b^2c^2d + 2a^2d^2)x^5 + 7b^6d^9(5b^2c - 2a^2d)x^6 + 3b^7d^10x^7 - (7(b^2c - a^2d)^{10})/(a + bx)^3 + (105d^2(-b^2c + a^2d)^9)/(a + bx)^2 - (945d^2(b^2c - a^2d)^8)/(a + bx) + 2520d^3(b^2c - a^2d)^7 \operatorname{Log}[a + bx]/(21b^{11})$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^4, x]

[Out] (21*b*d^4*(210*b^6*c^6 - 1008*a*b^5*c^5*d + 2100*a^2*b^4*c^4*d^2 - 2400*a^3*b^3*c^3*d^3 + 1575*a^4*b^2*c^2*d^4 - 560*a^5*b*c*d^5 + 84*a^6*d^6)*x + 21*b^2*d^5*(126*b^5*c^5 - 420*a*b^4*c^4*d + 600*a^2*b^3*c^3*d^2 - 450*a^3*b^2*c^2*d^3 + 175*a^4*b*c*d^4 - 28*a^5*d^5)*x^2 + 35*b^3*d^6*(42*b^4*c^4 - 96*a*b^3*c^3*d + 90*a^2*b^2*c^2*d^2 - 40*a^3*b*c*d^3 + 7*a^4*d^4)*x^3 + 105*b^4*d^7*(6*b^3*c^3 - 9*a^2*b^2*c^2*d + 5*a^2*b*c*d^2 - a^3*d^3)*x^4 + 21*b^5*d^8*(9*b^2*c^2 - 8*a^2*b^2*c^2*d + 2*a^2*d^2)*x^5 + 7*b^6*d^9*(5*b*c - 2*a*d)*x^6 + 3*b^7*d^10*x^7 - (7*(b*c - a*d)^10)/(a + b*x)^3 + (105*d^2*(-(b*c) + a*d)^9)/(a + b*x)^2 - (945*d^2*(b*c - a*d)^8)/(a + b*x) + 2520*d^3*(b*c - a*d)^7*Log[a + b*x]/(21*b^11)

fricas [B] time = 0.46, size = 1316, normalized size = 5.10

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^4,x, algorithm="fricas")

[Out] 1/21*(3*b^10*d^10*x^10 - 7*b^10*c^10 - 35*a*b^9*c^9*d - 315*a^2*b^8*c^8*d^2 + 4620*a^3*b^7*c^7*d^3 - 19110*a^4*b^6*c^6*d^4 + 41454*a^5*b^5*c^5*d^5 - 54390*a^6*b^4*c^4*d^6 + 44940*a^7*b^3*c^3*d^7 - 22995*a^8*b^2*c^2*d^8 + 6685*a^9*b*c*d^9 - 847*a^10*d^10 + 5*(7*b^10*c*d^9 - a*b^9*d^10)*x^9 + 9*(21*b^10*c^2*d^8 - 7*a*b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 18*(35*b^10*c^3*d^7 - 21*a*b^9*c^2*d^8 + 7*a^2*b^8*c*d^9 - a^3*b^7*d^10)*x^7 + 42*(35*b^10*c^4*d^6 - 35*a*b^9*c^3*d^7 + 21*a^2*b^8*c^2*d^8 - 7*a^3*b^7*c*d^9 + a^4*b^6*d^10)*x^6 + 126*(21*b^10*c^5*d^5 - 35*a*b^9*c^4*d^6 + 35*a^2*b^8*c^3*d^7 - 21*a^3*b^7*c^2*d^8 + 7*a^4*b^6*c*d^9 - a^5*b^5*d^10)*x^5 + 630*(7*b^10*c^6*d^4 - 21*

$$\begin{aligned}
& a^8 b^9 c^5 d^5 + 35 a^2 b^8 c^4 d^6 - 35 a^3 b^7 c^3 d^7 + 21 a^4 b^6 c^2 d^8 - 7 a^5 b^5 c d^9 + a^6 b^4 d^{10} x^4 + 7(1890 a^8 b^9 c^6 d^4 - 7938 a^2 b^8 c^5 d^5 + 15330 a^3 b^7 c^4 d^6 - 16680 a^4 b^6 c^3 d^7 + 10575 a^5 b^5 c^2 d^8 - 3665 a^6 b^4 c d^9 + 539 a^7 b^3 d^{10}) x^3 - 21(45 b^{10} c^8 d^2 - 360 a b^9 c^7 d^3 + 630 a^2 b^8 c^6 d^4 + 378 a^3 b^7 c^5 d^5 - 2730 a^4 b^6 c^4 d^6 + 4080 a^5 b^5 c^3 d^7 - 3015 a^6 b^4 c^2 d^8 + 1145 a^7 b^3 c d^9 - 179 a^8 b^2 d^{10}) x^2 - 21(5 b^{10} c^9 d + 45 a b^9 c^8 d^2 - 540 a^2 b^8 c^7 d^3 + 1890 a^3 b^7 c^6 d^4 - 3402 a^4 b^6 c^5 d^5 + 3570 a^5 b^5 c^4 d^6 - 2220 a^6 b^4 c^3 d^7 + 765 a^7 b^3 c^2 d^8 - 115 a^8 b^2 c d^9 + a^9 b d^{10}) x + 2520(a^3 b^7 c^7 d^3 - 7 a^4 b^6 c^6 d^4 + 21 a^5 b^5 c^5 d^5 - 35 a^6 b^4 c^4 d^6 + 35 a^7 b^3 c^3 d^7 - 21 a^8 b^2 c^2 d^8 + 7 a^9 b c d^9 - a^{10} d^{10} + (b^{10} c^7 d^3 - 7 a b^9 c^6 d^4 + 21 a^2 b^8 c^5 d^5 - 35 a^3 b^7 c^4 d^6 + 35 a^4 b^6 c^3 d^7 - 21 a^5 b^5 c^2 d^8 + 7 a^6 b^4 c d^9 - a^7 b^3 d^{10}) x^3 + 3(a b^9 c^7 d^3 - 7 a^2 b^8 c^6 d^4 + 21 a^3 b^7 c^5 d^5 - 35 a^4 b^6 c^4 d^6 + 35 a^5 b^5 c^3 d^7 - 21 a^6 b^4 c^2 d^8 + 7 a^7 b^3 c d^9 - a^8 b^2 d^{10}) x^2 + 3(a^2 b^8 c^7 d^3 - 7 a^3 b^7 c^6 d^4 + 21 a^4 b^6 c^5 d^5 - 35 a^5 b^5 c^4 d^6 + 35 a^6 b^4 c^3 d^7 - 21 a^7 b^3 c^2 d^8 + 7 a^8 b^2 c d^9 - a^9 b d^{10}) x) \log(bx + a) / (b^{14} x^3 + 3 a b^{13} x^2 + 3 a^2 b^{12} x + a^3 b^{11})
\end{aligned}$$

giac [B] time = 1.26, size = 907, normalized size = 3.52

$$\frac{120(b^7 c^7 d^3 - 7 a b^6 c^6 d^4 + 21 a^2 b^5 c^5 d^5 - 35 a^3 b^4 c^4 d^6 + 35 a^4 b^3 c^3 d^7 - 21 a^5 b^2 c^2 d^8 + 7 a^6 b c d^9 - a^7 d^{10}) \log(bx + a)}{b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^4,x, algorithm="giac")

[Out] 120*(b^7*c^7*d^3 - 7*a*b^6*c^6*d^4 + 21*a^2*b^5*c^5*d^5 - 35*a^3*b^4*c^4*d^6 + 35*a^4*b^3*c^3*d^7 - 21*a^5*b^2*c^2*d^8 + 7*a^6*b*c*d^9 - a^7*d^10)*log(abs(b*x + a))/b^11 - 1/3*(b^10*c^10 + 5*a*b^9*c^9*d + 45*a^2*b^8*c^8*d^2 - 660*a^3*b^7*c^7*d^3 + 2730*a^4*b^6*c^6*d^4 - 5922*a^5*b^5*c^5*d^5 + 7770*a^6*b^4*c^4*d^6 - 6420*a^7*b^3*c^3*d^7 + 3285*a^8*b^2*c^2*d^8 - 955*a^9*b*c*d^9 + 121*a^10*d^10 + 135*(b^10*c^8*d^2 - 8*a*b^9*c^7*d^3 + 28*a^2*b^8*c^6*d^4 - 56*a^3*b^7*c^5*d^5 + 70*a^4*b^6*c^4*d^6 - 56*a^5*b^5*c^3*d^7 + 28*a^6*b^4*c^2*d^8 - 8*a^7*b^3*c*d^9 + a^8*b^2*d^10)*x^2 + 15*(b^10*c^9*d + 9*a*b^9*c^8*d^2 - 108*a^2*b^8*c^7*d^3 + 420*a^3*b^7*c^6*d^4 - 882*a^4*b^6*c^5*d^5 + 1134*a^5*b^5*c^4*d^6 - 924*a^6*b^4*c^3*d^7 + 468*a^7*b^3*c^2*d^8 - 135*a^8*b^2*c*d^9 + 17*a^9*b*d^10)*x)/((b*x + a)^3*b^11) + 1/21*(3*b^24*d^10*x^7 + 35*b^24*c*d^9*x^6 - 14*a*b^23*d^10*x^6 + 189*b^24*c^2*d^8*x^5 - 168*a*b^23*c*d^9*x^5 + 42*a^2*b^22*d^10*x^5 + 630*b^24*c^3*d^7*x^4 - 945*a*b^23*c^2*d^8*x^4 + 525*a^2*b^22*c*d^9*x^4 - 105*a^3*b^21*d^10*x^4 + 1470*b^24*c^4*d^6*x^3 - 3360*a*b^23*c^3*d^7*x^3 + 3150*a^2*b^22*c^2*d^8*x^3 - 1400*a^3*b^21*c*d^9*x^3 + 245*a^4*b^20*d^10*x^3 + 2646*b^24*c^5*d^5*x^2 - 8820*a*b^23*

$$c^4d^6x^2 + 12600a^2b^{22}c^3d^7x^2 - 9450a^3b^{21}c^2d^8x^2 + 3675a^4b^{20}c^2d^9x^2 - 588a^5b^{19}d^{10}x^2 + 4410b^{24}c^6d^4x - 21168ab^{23}c^5d^5x + 44100a^2b^{22}c^4d^6x - 50400a^3b^{21}c^3d^7x + 33075a^4b^{20}c^2d^8x - 11760a^5b^{19}c^2d^9x + 1764a^6b^{18}d^{10}x)/b^{28}$$

maple [B] time = 0.02, size = 1141, normalized size = 4.42

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^4,x)

[Out]
$$\begin{aligned} & -1/3/b^{11}/(b*x+a)^3*a^{10}*d^{10}+5/b^{11}*d^{10}/(b*x+a)^2*a^9-5/b^2*d/(b*x+a)^2*c \\ & ^9-120/b^{11}*d^{10}*ln(b*x+a)*a^7+120/b^4*d^3*ln(b*x+a)*c^7-45/b^{11}*d^{10}/(b*x+ \\ & a)*a^8-45/b^3*d^2/(b*x+a)*c^8+9*d^8/b^4*x^5*c^2-5*d^{10}/b^7*x^4*a^3+30*d^7/b \\ & ^4*x^4*c^3+35/3*d^{10}/b^8*x^3*a^4+70*d^6/b^4*x^3*c^4-28*d^{10}/b^9*x^2*a^5+126 \\ & *d^5/b^4*x^2*c^5-2/3*d^{10}/b^5*x^6*a^5+3*d^9/b^4*x^6*c^2+2*d^{10}/b^6*x^5*a^2+21 \\ & 0*d^4/b^4*c^6*x+84*d^{10}/b^{10}*a^6*x+1/7*d^{10}/b^4*x^7-1/3/b/(b*x+a)^3*c^{10}-70 \\ & /b^5/(b*x+a)^3*a^4*c^6*d^4+40/b^4/(b*x+a)^3*a^3*c^7*d^3-15/b^3/(b*x+a)^3*a^ \\ & 2*c^8*d^2+10/3/b^2/(b*x+a)^3*a*c^9*d-45/b^{10}*d^9/(b*x+a)^2*a^8*c+180/b^9*d^ \\ & 8/(b*x+a)^2*a^7*c^2-420/b^8*d^7/(b*x+a)^2*a^6*c^3+630/b^7*d^6/(b*x+a)^2*a^5 \\ & *c^4-630/b^6*d^5/(b*x+a)^2*a^4*c^5+420/b^5*d^4/(b*x+a)^2*a^3*c^6-180/b^4*d^ \\ & 3/(b*x+a)^2*a^2*c^7+45/b^3*d^2/(b*x+a)^2*a*c^8+840/b^{10}*d^9*ln(b*x+a)*a^6*c \\ & -2520/b^9*d^8*ln(b*x+a)*a^5*c^2+4200/b^8*d^7*ln(b*x+a)*a^4*c^3-4200/b^7*d^6 \\ & *ln(b*x+a)*a^3*c^4+2520/b^6*d^5*ln(b*x+a)*a^2*c^5-840/b^5*d^4*ln(b*x+a)*a*c \\ & ^6+360/b^{10}*d^9/(b*x+a)*a^7*c-1260/b^9*d^8/(b*x+a)*a^6*c^2+2520/b^8*d^7/(b* \\ & x+a)*a^5*c^3-3150/b^7*d^6/(b*x+a)*a^4*c^4+2520/b^6*d^5/(b*x+a)*a^3*c^5-1260 \\ & /b^5*d^4/(b*x+a)*a^2*c^6+360/b^4*d^3/(b*x+a)*a*c^7-200/3*d^9/b^7*x^3*a^3*c- \\ & 8*d^9/b^5*x^5*a*c-560*d^9/b^9*a^5*c*x+1575*d^8/b^8*a^4*c^2*x-2400*d^7/b^7*a \\ & ^3*c^3*x+2100*d^6/b^6*a^2*c^4*x-1008*d^5/b^5*a*c^5*x-450*d^8/b^7*x^2*a^3*c^ \\ & 2+600*d^7/b^6*x^2*a^2*c^3-420*d^6/b^5*x^2*a*c^4+175*d^9/b^8*x^2*a^4*c+150*d \\ & ^8/b^6*x^3*a^2*c^2-160*d^7/b^5*x^3*a*c^3+10/3/b^{10}/(b*x+a)^3*a^9*c*d^9-15/b \\ & ^9/(b*x+a)^3*a^8*c^2*d^8+40/b^8/(b*x+a)^3*a^7*c^3*d^7+25*d^9/b^6*x^4*a^2*c- \\ & 45*d^8/b^5*x^4*a*c^2-70/b^7/(b*x+a)^3*a^6*c^4*d^6+84/b^6/(b*x+a)^3*a^5*c^5* \\ & d^5 \end{aligned}$$

maxima [B] time = 1.73, size = 891, normalized size = 3.45

$$b^{10}c^{10} + 5ab^9c^9d + 45a^2b^8c^8d^2 - 660a^3b^7c^7d^3 + 2730a^4b^6c^6d^4 - 5922a^5b^5c^5d^5 + 7770a^6b^4c^4d^6 - 6420a^7b^3c^3d^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^4,x, algorithm="maxima")

```
[Out] -1/3*(b^10*c^10 + 5*a*b^9*c^9*d + 45*a^2*b^8*c^8*d^2 - 660*a^3*b^7*c^7*d^3
+ 2730*a^4*b^6*c^6*d^4 - 5922*a^5*b^5*c^5*d^5 + 7770*a^6*b^4*c^4*d^6 - 6420
*a^7*b^3*c^3*d^7 + 3285*a^8*b^2*c^2*d^8 - 955*a^9*b*c*d^9 + 121*a^10*d^10 +
 135*(b^10*c^8*d^2 - 8*a*b^9*c^7*d^3 + 28*a^2*b^8*c^6*d^4 - 56*a^3*b^7*c^5*
d^5 + 70*a^4*b^6*c^4*d^6 - 56*a^5*b^5*c^3*d^7 + 28*a^6*b^4*c^2*d^8 - 8*a^7*
b^3*c*d^9 + a^8*b^2*d^10)*x^2 + 15*(b^10*c^9*d + 9*a*b^9*c^8*d^2 - 108*a^2*
b^8*c^7*d^3 + 420*a^3*b^7*c^6*d^4 - 882*a^4*b^6*c^5*d^5 + 1134*a^5*b^5*c^4*
d^6 - 924*a^6*b^4*c^3*d^7 + 468*a^7*b^3*c^2*d^8 - 135*a^8*b^2*c*d^9 + 17*a^
9*b*d^10)*x)/(b^14*x^3 + 3*a*b^13*x^2 + 3*a^2*b^12*x + a^3*b^11) + 1/21*(3*
b^6*d^10*x^7 + 7*(5*b^6*c*d^9 - 2*a*b^5*d^10)*x^6 + 21*(9*b^6*c^2*d^8 - 8*a
*b^5*c*d^9 + 2*a^2*b^4*d^10)*x^5 + 105*(6*b^6*c^3*d^7 - 9*a*b^5*c^2*d^8 + 5
*a^2*b^4*c*d^9 - a^3*b^3*d^10)*x^4 + 35*(42*b^6*c^4*d^6 - 96*a*b^5*c^3*d^7
+ 90*a^2*b^4*c^2*d^8 - 40*a^3*b^3*c*d^9 + 7*a^4*b^2*d^10)*x^3 + 21*(126*b^6
*c^5*d^5 - 420*a*b^5*c^4*d^6 + 600*a^2*b^4*c^3*d^7 - 450*a^3*b^3*c^2*d^8 +
175*a^4*b^2*c*d^9 - 28*a^5*b*d^10)*x^2 + 21*(210*b^6*c^6*d^4 - 1008*a*b^5*c
^5*d^5 + 2100*a^2*b^4*c^4*d^6 - 2400*a^3*b^3*c^3*d^7 + 1575*a^4*b^2*c^2*d^8
- 560*a^5*b*c*d^9 + 84*a^6*d^10)*x)/b^10 + 120*(b^7*c^7*d^3 - 7*a*b^6*c^6*
d^4 + 21*a^2*b^5*c^5*d^5 - 35*a^3*b^4*c^4*d^6 + 35*a^4*b^3*c^3*d^7 - 21*a^5
*b^2*c^2*d^8 + 7*a^6*b*c*d^9 - a^7*d^10)*log(b*x + a)/b^11
```

mupad [B] time = 0.39, size = 2219, normalized size = 8.60

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^10/(a + b*x)^4, x)
```

```
[Out] x^3*((4*a*((4*a*((4*a*((4*a*d^10)/b^5 - (10*c*d^9)/b^4))/b - (6*a^2*d^10)/b
^6 + (45*c^2*d^8)/b^4))/b + (4*a^3*d^10)/b^7 - (120*c^3*d^7)/b^4 - (6*a^2*(
(4*a*d^10)/b^5 - (10*c*d^9)/b^4))/b^2))/(3*b) - (a^4*d^10)/(3*b^8) + (70*c^
4*d^6)/b^4 + (4*a^3*((4*a*d^10)/b^5 - (10*c*d^9)/b^4))/(3*b^3) - (2*a^2*((4
*a*((4*a*d^10)/b^5 - (10*c*d^9)/b^4))/b - (6*a^2*d^10)/b^6 + (45*c^2*d^8)/b
^4))/b^2) - x^6*((2*a*d^10)/(3*b^5) - (5*c*d^9)/(3*b^4)) - x^4*((a*((4*a*((
4*a*d^10)/b^5 - (10*c*d^9)/b^4))/b - (6*a^2*d^10)/b^6 + (45*c^2*d^8)/b^4))/
b + (a^3*d^10)/b^7 - (30*c^3*d^7)/b^4 - (3*a^2*((4*a*d^10)/b^5 - (10*c*d^9)
/b^4))/(2*b^2) + x^5*((4*a*((4*a*d^10)/b^5 - (10*c*d^9)/b^4))/(5*b) - (6*a
^2*d^10)/(5*b^6) + (9*c^2*d^8)/b^4) - x*((4*a*((252*c^5*d^5)/b^4 - (4*a*((4
*a*((4*a*((4*a*d^10)/b^5 - (10*c*d^9)/b^4))/b - (6*a^2*d^10)/b^6 + (4
5*c^2*d^8)/b^4))/b + (4*a^3*d^10)/b^7 - (120*c^3*d^7)/b^4 - (6*a^2*((4*a*d^
10)/b^5 - (10*c*d^9)/b^4))/b^2))/b - (a^4*d^10)/b^8 + (210*c^4*d^6)/b^4 + (
4*a^3*((4*a*d^10)/b^5 - (10*c*d^9)/b^4))/b^3 - (6*a^2*((4*a*((4*a*d^10)/b^5
- (10*c*d^9)/b^4))/b - (6*a^2*d^10)/b^6 + (45*c^2*d^8)/b^4))/b^2))/b + (a^
4*((4*a*d^10)/b^5 - (10*c*d^9)/b^4))/b^4 + (6*a^2*((4*a*((4*a*((4*a*d^10)/b
^5 - (10*c*d^9)/b^4))/b - (6*a^2*d^10)/b^6 + (45*c^2*d^8)/b^4))/b + (4*a^3*
d^10)/b^7 - (120*c^3*d^7)/b^4 - (6*a^2*((4*a*d^10)/b^5 - (10*c*d^9)/b^4))/b
```


$$\begin{aligned}
& d^{**9}/b^{**6} - 45*a*c^{**2}*d^{**8}/b^{**5} + 30*c^{**3}*d^{**7}/b^{**4}) + x^{**3}*(35*a^{**4}*d^{**10}/ \\
& (3*b^{**8}) - 200*a^{**3}*c*d^{**9}/(3*b^{**7}) + 150*a^{**2}*c^{**2}*d^{**8}/b^{**6} - 160*a*c^{**3}* \\
& d^{**7}/b^{**5} + 70*c^{**4}*d^{**6}/b^{**4}) + x^{**2}*(-28*a^{**5}*d^{**10}/b^{**9} + 175*a^{**4}*c*d^{**} \\
& 9/b^{**8} - 450*a^{**3}*c^{**2}*d^{**8}/b^{**7} + 600*a^{**2}*c^{**3}*d^{**7}/b^{**6} - 420*a*c^{**4}*d^{**} \\
& 6/b^{**5} + 126*c^{**5}*d^{**5}/b^{**4}) + x*(84*a^{**6}*d^{**10}/b^{**10} - 560*a^{**5}*c*d^{**9}/b^{**} \\
& 9 + 1575*a^{**4}*c^{**2}*d^{**8}/b^{**8} - 2400*a^{**3}*c^{**3}*d^{**7}/b^{**7} + 2100*a^{**2}*c^{**4}*d^{**} \\
& *6/b^{**6} - 1008*a*c^{**5}*d^{**5}/b^{**5} + 210*c^{**6}*d^{**4}/b^{**4}) + (-121*a^{**10}*d^{**10} + \\
& 955*a^{**9}*b*c*d^{**9} - 3285*a^{**8}*b^{**2}*c^{**2}*d^{**8} + 6420*a^{**7}*b^{**3}*c^{**3}*d^{**7} - \\
& 7770*a^{**6}*b^{**4}*c^{**4}*d^{**6} + 5922*a^{**5}*b^{**5}*c^{**5}*d^{**5} - 2730*a^{**4}*b^{**6}*c^{**6}*d^{**} \\
& **4 + 660*a^{**3}*b^{**7}*c^{**7}*d^{**3} - 45*a^{**2}*b^{**8}*c^{**8}*d^{**2} - 5*a*b^{**9}*c^{**9}*d - \\
& b^{**10}*c^{**10} + x^{**2}*(-135*a^{**8}*b^{**2}*d^{**10} + 1080*a^{**7}*b^{**3}*c*d^{**9} - 3780*a^{**} \\
& 6*b^{**4}*c^{**2}*d^{**8} + 7560*a^{**5}*b^{**5}*c^{**3}*d^{**7} - 9450*a^{**4}*b^{**6}*c^{**4}*d^{**6} + 75 \\
& 60*a^{**3}*b^{**7}*c^{**5}*d^{**5} - 3780*a^{**2}*b^{**8}*c^{**6}*d^{**4} + 1080*a*b^{**9}*c^{**7}*d^{**3} - \\
& 135*b^{**10}*c^{**8}*d^{**2}) + x*(-255*a^{**9}*b*d^{**10} + 2025*a^{**8}*b^{**2}*c*d^{**9} - 7020 \\
& *a^{**7}*b^{**3}*c^{**2}*d^{**8} + 13860*a^{**6}*b^{**4}*c^{**3}*d^{**7} - 17010*a^{**5}*b^{**5}*c^{**4}*d^{**} \\
& 6 + 13230*a^{**4}*b^{**6}*c^{**5}*d^{**5} - 6300*a^{**3}*b^{**7}*c^{**6}*d^{**4} + 1620*a^{**2}*b^{**8}*c \\
& **7*d^{**3} - 135*a*b^{**9}*c^{**8}*d^{**2} - 15*b^{**10}*c^{**9}*d))/(3*a^{**3}*b^{**11} + 9*a^{**2}* \\
& b^{**12}*x + 9*a*b^{**13}*x^{**2} + 3*b^{**14}*x^{**3}) + d^{**10}*x^{**7}/(7*b^{**4}) - 120*d^{**3}*(\\
& a*d - b*c)^{**7}*log(a + b*x)/b^{**11}
\end{aligned}$$

$$3.1316 \quad \int \frac{(c+dx)^{10}}{(a+bx)^5} dx$$

Optimal. Leaf size=262

$$\frac{2d^9(a+bx)^5(bc-ad)}{b^{11}} + \frac{45d^8(a+bx)^4(bc-ad)^2}{4b^{11}} + \frac{40d^7(a+bx)^3(bc-ad)^3}{b^{11}} + \frac{105d^6(a+bx)^2(bc-ad)^4}{b^{11}} + \frac{210d^4(bc-ad)^5}{b^{11}}$$

[Out] $252*d^5*(-a*d+b*c)^5*x/b^{10}-1/4*(-a*d+b*c)^{10}/b^{11}/(b*x+a)^4-10/3*d*(-a*d+b*c)^9/b^{11}/(b*x+a)^3-45/2*d^2*(-a*d+b*c)^8/b^{11}/(b*x+a)^2-120*d^3*(-a*d+b*c)^7/b^{11}/(b*x+a)+105*d^6*(-a*d+b*c)^4*(b*x+a)^2/b^{11}+40*d^7*(-a*d+b*c)^3*(b*x+a)^3/b^{11}+45/4*d^8*(-a*d+b*c)^2*(b*x+a)^4/b^{11}+2*d^9*(-a*d+b*c)*(b*x+a)^5/b^{11}+1/6*d^{10}*(b*x+a)^6/b^{11}+210*d^4*(-a*d+b*c)^6*\ln(b*x+a)/b^{11}$

Rubi [A] time = 0.42, antiderivative size = 262, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{2d^9(a+bx)^5(bc-ad)}{b^{11}} + \frac{45d^8(a+bx)^4(bc-ad)^2}{4b^{11}} + \frac{40d^7(a+bx)^3(bc-ad)^3}{b^{11}} + \frac{105d^6(a+bx)^2(bc-ad)^4}{b^{11}} + \frac{252d^5x(bc-ad)^5}{b^{11}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^5, x]

[Out] $(252*d^5*(b*c - a*d)^5*x)/b^{10} - (b*c - a*d)^{10}/(4*b^{11}*(a + b*x)^4) - (10*d*(b*c - a*d)^9)/(3*b^{11}*(a + b*x)^3) - (45*d^2*(b*c - a*d)^8)/(2*b^{11}*(a + b*x)^2) - (120*d^3*(b*c - a*d)^7)/(b^{11}*(a + b*x)) + (105*d^6*(b*c - a*d)^4*(a + b*x)^2)/b^{11} + (40*d^7*(b*c - a*d)^3*(a + b*x)^3)/b^{11} + (45*d^8*(b*c - a*d)^2*(a + b*x)^4)/(4*b^{11}) + (2*d^9*(b*c - a*d)*(a + b*x)^5)/b^{11} + (d^{10}*(a + b*x)^6)/(6*b^{11}) + (210*d^4*(b*c - a*d)^6*\text{Log}[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c + dx)^{10}}{(a + bx)^5} dx = \int \left(\frac{252d^5(bc - ad)^5}{b^{10}} + \frac{(bc - ad)^{10}}{b^{10}(a + bx)^5} + \frac{10d(bc - ad)^9}{b^{10}(a + bx)^4} + \frac{45d^2(bc - ad)^8}{b^{10}(a + bx)^3} + \frac{120d^3(bc - ad)^7}{b^{10}(a + bx)^2} + \frac{10d^4(bc - ad)^6}{b^{10}(a + bx)} \right) dx$$

$$= \frac{252d^5(bc - ad)^5x}{b^{10}} - \frac{(bc - ad)^{10}}{4b^{11}(a + bx)^4} - \frac{10d(bc - ad)^9}{3b^{11}(a + bx)^3} - \frac{45d^2(bc - ad)^8}{2b^{11}(a + bx)^2} - \frac{120d^3(bc - ad)^7}{b^{11}(a + bx)} + \frac{10d^4(bc - ad)^6}{b^{11}}$$

Mathematica [A] time = 0.20, size = 359, normalized size = 1.37

$$15b^4d^8x^4(3a^2d^2 - 10abcd + 9b^2c^2) + 20b^3d^7x^3(-7a^3d^3 + 30a^2bcd^2 - 45ab^2c^2d + 24b^3c^3) + 30b^2d^6x^2(14a^4d^4 -$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^5,x]

[Out] (12*b*d^5*(252*b^5*c^5 - 1050*a*b^4*c^4*d + 1800*a^2*b^3*c^3*d^2 - 1575*a^3*b^2*c^2*d^3 + 700*a^4*b*c*d^4 - 126*a^5*d^5)*x + 30*b^2*d^6*(42*b^4*c^4 - 120*a*b^3*c^3*d + 135*a^2*b^2*c^2*d^2 - 70*a^3*b*c*d^3 + 14*a^4*d^4)*x^2 + 20*b^3*d^7*(24*b^3*c^3 - 45*a*b^2*c^2*d + 30*a^2*b*c*d^2 - 7*a^3*d^3)*x^3 + 15*b^4*d^8*(9*b^2*c^2 - 10*a*b*c*d + 3*a^2*d^2)*x^4 + 12*b^5*d^9*(2*b*c - a*d)*x^5 + 2*b^6*d^10*x^6 - (3*(b*c - a*d)^10)/(a + b*x)^4 + (40*d*(-(b*c) + a*d)^9)/(a + b*x)^3 - (270*d^2*(b*c - a*d)^8)/(a + b*x)^2 + (1440*d^3*(-(b*c) + a*d)^7)/(a + b*x) + 2520*d^4*(b*c - a*d)^6*Log[a + b*x])/(12*b^11)

fricas [B] time = 0.47, size = 1365, normalized size = 5.21

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^5,x, algorithm="fricas")

[Out] 1/12*(2*b^10*d^10*x^10 - 3*b^10*c^10 - 10*a*b^9*c^9*d - 45*a^2*b^8*c^8*d^2 - 360*a^3*b^7*c^7*d^3 + 5250*a^4*b^6*c^6*d^4 - 19404*a^5*b^5*c^5*d^5 + 35910*a^6*b^4*c^4*d^6 - 38280*a^7*b^3*c^3*d^7 + 23985*a^8*b^2*c^2*d^8 - 8250*a^9*b*c*d^9 + 1207*a^10*d^10 + 4*(6*b^10*c*d^9 - a*b^9*d^10)*x^9 + 9*(15*b^10*c^2*d^8 - 6*a*b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 24*(20*b^10*c^3*d^7 - 15*a*b^9*c^2*d^8 + 6*a^2*b^8*c*d^9 - a^3*b^7*d^10)*x^7 + 84*(15*b^10*c^4*d^6 - 20*a*b^9*c^3*d^7 + 15*a^2*b^8*c^2*d^8 - 6*a^3*b^7*c*d^9 + a^4*b^6*d^10)*x^6 + 504*(6*b^10*c^5*d^5 - 15*a*b^9*c^4*d^6 + 20*a^2*b^8*c^3*d^7 - 15*a^3*b^7*c^2*d^8 + 6*a^4*b^6*c*d^9 - a^5*b^5*d^10)*x^5 + (12096*a*b^9*c^5*d^5 - 42840*a^2*b^8*c^4*d^6 + 66720*a^3*b^7*c^3*d^7 - 54765*a^4*b^6*c^2*d^8 + 23250*a^5*b^5*c*d^9 - 4043*a^6*b^4*d^10)*x^4 - 4*(360*b^10*c^7*d^3 - 2520*a*b^9*c^6

$$\begin{aligned}
& *d^4 + 3024*a^2*b^8*c^5*d^5 + 5040*a^3*b^7*c^4*d^6 - 16320*a^4*b^6*c^3*d^7 \\
& + 16965*a^5*b^5*c^2*d^8 - 8130*a^6*b^4*c*d^9 + 1523*a^7*b^3*d^{10}) *x^3 - 6*(\\
& 45*b^{10}*c^8*d^2 + 360*a*b^9*c^7*d^3 - 3780*a^2*b^8*c^6*d^4 + 10584*a^3*b^7* \\
& c^5*d^5 - 13860*a^4*b^6*c^4*d^6 + 8880*a^5*b^5*c^3*d^7 - 1935*a^6*b^4*c^2*d^8 \\
& ^8 - 570*a^7*b^3*c*d^9 + 263*a^8*b^2*d^{10}) *x^2 - 4*(10*b^{10}*c^9*d + 45*a*b^9* \\
& c^8*d^2 + 360*a^2*b^8*c^7*d^3 - 4620*a^3*b^7*c^6*d^4 + 15624*a^4*b^6*c^5* \\
& d^5 - 26460*a^5*b^5*c^4*d^6 + 25680*a^6*b^4*c^3*d^7 - 14535*a^7*b^3*c^2*d^8 \\
& + 4470*a^8*b^2*c*d^9 - 577*a^9*b*d^{10}) *x + 2520*(a^4*b^6*c^6*d^4 - 6*a^5*b^5* \\
& c^5*d^5 + 15*a^6*b^4*c^4*d^6 - 20*a^7*b^3*c^3*d^7 + 15*a^8*b^2*c^2*d^8 - \\
& 6*a^9*b*c*d^9 + a^{10}*d^{10} + (b^{10}*c^6*d^4 - 6*a*b^9*c^5*d^5 + 15*a^2*b^8*c^4* \\
& d^6 - 20*a^3*b^7*c^3*d^7 + 15*a^4*b^6*c^2*d^8 - 6*a^5*b^5*c*d^9 + a^6*b^4* \\
& d^{10}) *x^4 + 4*(a*b^9*c^6*d^4 - 6*a^2*b^8*c^5*d^5 + 15*a^3*b^7*c^4*d^6 - 20* \\
& a^4*b^6*c^3*d^7 + 15*a^5*b^5*c^2*d^8 - 6*a^6*b^4*c*d^9 + a^7*b^3*d^{10}) *x^3 \\
& + 6*(a^2*b^8*c^6*d^4 - 6*a^3*b^7*c^5*d^5 + 15*a^4*b^6*c^4*d^6 - 20*a^5*b^5* \\
& c^3*d^7 + 15*a^6*b^4*c^2*d^8 - 6*a^7*b^3*c*d^9 + a^8*b^2*d^{10}) *x^2 + 4*(a^3* \\
& b^7*c^6*d^4 - 6*a^4*b^6*c^5*d^5 + 15*a^5*b^5*c^4*d^6 - 20*a^6*b^4*c^3*d^7 \\
& + 15*a^7*b^3*c^2*d^8 - 6*a^8*b^2*c*d^9 + a^9*b*d^{10}) *x) *log(b*x + a)/(b^ \\
& 15*x^4 + 4*a*b^{14}*x^3 + 6*a^2*b^{13}*x^2 + 4*a^3*b^{12}*x + a^4*b^{11})
\end{aligned}$$

giac [B] time = 1.38, size = 1168, normalized size = 4.46

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^5,x, algorithm="giac")

[Out] $1/12*(2*d^{10} + 24*(b^2*c*d^9 - a*b*d^{10})/((b*x + a)*b) + 135*(b^4*c^2*d^8 - 2*a*b^3*c*d^9 + a^2*b^2*d^{10})/((b*x + a)^2*b^2) + 480*(b^6*c^3*d^7 - 3*a*b^5*c^2*d^8 + 3*a^2*b^4*c*d^9 - a^3*b^3*d^{10})/((b*x + a)^3*b^3) + 1260*(b^8*c^4*d^6 - 4*a*b^7*c^3*d^7 + 6*a^2*b^6*c^2*d^8 - 4*a^3*b^5*c*d^9 + a^4*b^4*d^{10})/((b*x + a)^4*b^4) + 3024*(b^{10}*c^5*d^5 - 5*a*b^9*c^4*d^6 + 10*a^2*b^8*c^3*d^7 - 10*a^3*b^7*c^2*d^8 + 5*a^4*b^6*c*d^9 - a^5*b^5*d^{10})/((b*x + a)^5*b^5)) * (b*x + a)^6/b^{11} - 210*(b^6*c^6*d^4 - 6*a*b^5*c^5*d^5 + 15*a^2*b^4*c^4*d^6 - 20*a^3*b^3*c^3*d^7 + 15*a^4*b^2*c^2*d^8 - 6*a^5*b*c*d^9 + a^6*d^{10}) * log(abs(b*x + a)/((b*x + a)^2*abs(b)))/b^{11} - 1/12*(3*b^6*c^{10}/(b*x + a)^4 + 40*b^6*c^9*d/(b*x + a)^3 - 30*a*b^6*c^9*d/(b*x + a)^4 + 270*b^6*c^8*d^2/(b*x + a)^2 - 360*a*b^6*c^8*d^2/(b*x + a)^3 + 135*a^2*b^6*c^8*d^2/(b*x + a)^4 + 1440*b^6*c^7*d^3/(b*x + a) - 2160*a*b^6*c^7*d^3/(b*x + a)^2 + 1440*a^2*b^6*c^7*d^3/(b*x + a)^3 - 360*a^3*b^6*c^7*d^3/(b*x + a)^4 - 1080*a*b^6*c^6*d^4/(b*x + a) + 7560*a^2*b^6*c^6*d^4/(b*x + a)^2 - 3360*a^3*b^6*c^6*d^4/(b*x + a)^3 + 630*a^4*b^6*c^6*d^4/(b*x + a)^4 + 30240*a^2*b^6*c^5*d^5/(b*x + a) - 15120*a^3*b^6*c^5*d^5/(b*x + a)^2 + 5040*a^4*b^6*c^5*d^5/(b*x + a)^3 - 756*a^5*b^6*c^5*d^5/(b*x + a)^4 - 50400*a^3*b^6*c^4*d^6/(b*x + a) + 18900*a^4*b^6*c^4*d^6/(b*x + a)^2 - 5040*a^5*b^6*c^4*d^6/(b*x + a)^3 + 630*a^6*b^6*c^4*d^6/(b*x + a)^4 + 50400*a^4*b^6*c^3*d^7/(b*x$

$$+ a) - 15120a^5b^{60}c^3d^7/(b*x + a)^2 + 3360a^6b^{60}c^3d^7/(b*x + a)^3 - 360a^7b^{60}c^3d^7/(b*x + a)^4 - 30240a^5b^{59}c^2d^8/(b*x + a) + 7560a^6b^{59}c^2d^8/(b*x + a)^2 - 1440a^7b^{59}c^2d^8/(b*x + a)^3 + 135a^8b^{59}c^2d^8/(b*x + a)^4 + 10080a^6b^{58}c*d^9/(b*x + a) - 2160a^7b^{58}c*d^9/(b*x + a)^2 + 360a^8b^{58}c*d^9/(b*x + a)^3 - 30a^9b^{58}c*d^9/(b*x + a)^4 - 1440a^7b^{57}d^{10}/(b*x + a) + 270a^8b^{57}d^{10}/(b*x + a)^2 - 40a^9b^{57}d^{10}/(b*x + a)^3 + 3a^{10}b^{57}d^{10}/(b*x + a)^4)/b^68$$

maple [B] time = 0.02, size = 1172, normalized size = 4.47

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^10/(b*x+a)^5,x)`

[Out] $10/3/b^{11}d^{10}/(b*x+a)^3a^9 - 10/3/b^2d/(b*x+a)^3c^9 - 45/2/b^{11}d^{10}/(b*x+a)^2a^8 - 45/2/b^3d^2/(b*x+a)^2c^8 + 210/b^{11}d^{10} \ln(b*x+a)a^6 + 210/b^5d^4 \ln(b*x+a)c^6 - 1/4/b^{11}/(b*x+a)^4a^{10}d^{10} + 120/b^{11}d^{10}/(b*x+a)a^7 - 120/b^4d^3/(b*x+a)c^7 - d^{10}/b^6x^5a + 2d^9/b^5x^5c + 15/4d^{10}/b^7x^4a^2 + 45/4d^8/b^5x^4c^2 - 35/3d^{10}/b^8x^3a^3 + 40d^7/b^5x^3c^3 + 35d^{10}/b^9x^2a^4 + 105d^6/b^5x^2c^4 - 126d^{10}/b^{10}a^5x + 252d^5/b^5c^5x + 1/6d^{10}/b^5x^6 - 1/4/b/(b*x+a)^4c^{10} - 25/2d^9/b^6x^4ac + 50d^9/b^7x^3a^2c - 1260/b^{10}d^9 \ln(b*x+a)a^5c + 3150/b^9d^8 \ln(b*x+a)a^4c^2 - 4200/b^8d^7 \ln(b*x+a)a^3c^3 + 3150/b^7d^6 \ln(b*x+a)a^2c^4 - 1260/b^6d^5 \ln(b*x+a)ac^5 + 5/2/b^{10}/(b*x+a)^4a^9cd^9 - 45/4/b^9/(b*x+a)^4a^8c^2d^8 + 30/b^8/(b*x+a)^4a^7c^3d^7 - 105/2/b^7/(b*x+a)^4a^6c^4d^6 + 63/b^6/(b*x+a)^4a^5c^5d^5 - 105/2/b^5/(b*x+a)^4a^4c^6d^4 + 30/b^4/(b*x+a)^4a^3c^7d^3 - 45/4/b^3/(b*x+a)^4a^2c^8d^2 + 5/2/b^2/(b*x+a)^4aac^9d - 840/b^{10}d^9/(b*x+a)a^6c + 2520/b^9d^8/(b*x+a)a^5c^2 - 4200/b^8d^7/(b*x+a)a^4c^3 + 4200/b^7d^6/(b*x+a)a^3c^4 - 2520/b^6d^5/(b*x+a)a^2c^5 + 840/b^5d^4/(b*x+a)ac^6 + 700d^9/b^9a^4cx - 1575d^8/b^8a^3c^2x + 1800d^7/b^7a^2c^3x - 1050d^6/b^6aac^4x - 30/b^{10}d^9/(b*x+a)^3a^8c + 120/b^9d^8/(b*x+a)^3a^7c^2 - 280/b^8d^7/(b*x+a)^3a^6c^3 + 420/b^7d^6/(b*x+a)^3a^5c^4 - 420/b^6d^5/(b*x+a)^3a^4c^5 + 280/b^5d^4/(b*x+a)^3a^3c^6 - 120/b^4d^3/(b*x+a)^3a^2c^7 + 30/b^3d^2/(b*x+a)^3aac^8 + 180/b^{10}d^9/(b*x+a)^2a^7c - 630/b^9d^8/(b*x+a)^2a^6c^2 + 1260/b^8d^7/(b*x+a)^2a^5c^3 - 1575/b^7d^6/(b*x+a)^2a^4c^4 + 1260/b^6d^5/(b*x+a)^2a^3c^5 - 630/b^5d^4/(b*x+a)^2a^2c^6 + 180/b^4d^3/(b*x+a)^2aac^7 - 75d^8/b^6x^3ac^2 - 175d^9/b^8x^2a^3c + 675/2d^8/b^7x^2a^2c^2 - 300d^7/b^6x^2aac^3$

maxima [B] time = 1.93, size = 903, normalized size = 3.45

$$3b^{10}c^{10} + 10ab^9c^9d + 45a^2b^8c^8d^2 + 360a^3b^7c^7d^3 - 5250a^4b^6c^6d^4 + 19404a^5b^5c^5d^5 - 35910a^6b^4c^4d^6 + 3828$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^5,x, algorithm="maxima")

[Out]
$$\begin{aligned} & -1/12*(3*b^{10}*c^{10} + 10*a*b^9*c^9*d + 45*a^2*b^8*c^8*d^2 + 360*a^3*b^7*c^7*d^3 - 5250*a^4*b^6*c^6*d^4 + 19404*a^5*b^5*c^5*d^5 - 35910*a^6*b^4*c^4*d^6 \\ & + 38280*a^7*b^3*c^3*d^7 - 23985*a^8*b^2*c^2*d^8 + 8250*a^9*b*c*d^9 - 1207*a^{10}*d^{10} + 1440*(b^{10}*c^7*d^3 - 7*a*b^9*c^6*d^4 + 21*a^2*b^8*c^5*d^5 - 35*a^3*b^7*c^4*d^6 \\ & + 35*a^4*b^6*c^3*d^7 - 21*a^5*b^5*c^2*d^8 + 7*a^6*b^4*c*d^9 - a^7*b^3*d^{10})*x^3 + 270*(b^{10}*c^8*d^2 + 8*a*b^9*c^7*d^3 - 84*a^2*b^8*c^6*d^4 + 280*a^3*b^7*c^5*d^5 - 490*a^4*b^6*c^4*d^6 + 504*a^5*b^5*c^3*d^7 - 308*a^6*b^4*c^2*d^8 \\ & + 104*a^7*b^3*c*d^9 - 15*a^8*b^2*d^{10})*x^2 + 20*(2*b^{10}*c^9*d + 9*a*b^9*c^8*d^2 + 72*a^2*b^8*c^7*d^3 - 924*a^3*b^7*c^6*d^4 + 3276*a^4*b^6*c^5*d^5 - 5922*a^5*b^5*c^4*d^6 + 6216*a^6*b^4*c^3*d^7 - 3852*a^7*b^3*c^2*d^8 \\ & + 1314*a^8*b^2*c*d^9 - 191*a^9*b*d^{10})*x)/ (b^{15}*x^4 + 4*a*b^{14}*x^3 + 6*a^2*b^{13}*x^2 + 4*a^3*b^{12}*x + a^4*b^{11}) + 1/12*(2*b^5*d^{10}*x^6 + 12*(2*b^5*c*d^9 - a*b^4*d^{10})*x^5 + 15*(9*b^5*c^2*d^8 - 10*a*b^4*c*d^9 + 3*a^2*b^3*d^{10})*x^4 \\ & + 20*(24*b^5*c^3*d^7 - 45*a*b^4*c^2*d^8 + 30*a^2*b^3*c*d^9 - 7*a^3*b^2*d^{10})*x^3 + 30*(42*b^5*c^4*d^6 - 120*a*b^4*c^3*d^7 + 135*a^2*b^3*c^2*d^8 - 70*a^3*b^2*c*d^9 + 14*a^4*b*d^{10})*x^2 + 12*(252*b^5*c^5*d^5 - 1050*a*b^4*c^4*d^6 + 1800*a^2*b^3*c^3*d^7 - 1575*a^3*b^2*c^2*d^8 + 700*a^4*b*c*d^9 - 126*a^5*d^{10})*x)/b^{10} + 210*(b^6*c^6*d^4 - 6*a*b^5*c^5*d^5 + 15*a^2*b^4*c^4*d^6 - 20*a^3*b^3*c^3*d^7 + 15*a^4*b^2*c^2*d^8 - 6*a^5*b*c*d^9 + a^6*d^{10})*log(b*x + a)/b^{11} \end{aligned}$$

mupad [B] time = 0.38, size = 1494, normalized size = 5.70

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^5,x)

[Out]
$$\begin{aligned} & x^2*((5*a*((5*a*((5*a*((5*a*d^{10})/b^6 - (10*c*d^9)/b^5))/b - (10*a^2*d^{10})/b^7 + (45*c^2*d^8)/b^5))/b + (10*a^3*d^{10})/b^8 - (120*c^3*d^7)/b^5 - (10*a^2*((5*a*d^{10})/b^6 - (10*c*d^9)/b^5))/b^2)/(2*b) - (5*a^4*d^{10})/(2*b^9) + (105*c^4*d^6)/b^5 + (5*a^3*((5*a*d^{10})/b^6 - (10*c*d^9)/b^5))/b^3 - (5*a^2*((5*a*((5*a*d^{10})/b^6 - (10*c*d^9)/b^5))/b - (10*a^2*d^{10})/b^7 + (45*c^2*d^8)/b^5))/b^2 - x^5*((a*d^{10})/b^6 - (2*c*d^9)/b^5) - x^3*((5*a*((5*a*((5*a*d^{10})/b^6 - (10*c*d^9)/b^5))/b - (10*a^2*d^{10})/b^7 + (45*c^2*d^8)/b^5))/(3*b) + (10*a^3*d^{10})/(3*b^8) - (40*c^3*d^7)/b^5 - (10*a^2*((5*a*d^{10})/b^6 - (10*c*d^9)/b^5))/(3*b^2) + x^4*((5*a*((5*a*d^{10})/b^6 - (10*c*d^9)/b^5))/(4*b) - (5*a^2*d^{10})/(2*b^7) + (45*c^2*d^8)/(4*b^5)) - x*((5*a*((5*a*((5*a*((5*a*d^{10})/b^6 - (10*c*d^9)/b^5))/b - (10*a^2*d^{10})/b^7 + (45*c^2*d^8)/b^5))/b + (10*a^3*d^{10})/b^8 - (120*c^3*d^7)/b^5 - (10*a^2*((5*a*d^{10})/b^6 - (10*c*d^9)/b^5))/b^2)/b - (5*a^4*d^{10})/b^9 + (210*c^4*d^6)/b^5 + (10*a^3*c^5*d^5)/b^5 \end{aligned}$$

$$3.1317 \quad \int \frac{(c+dx)^{10}}{(a+bx)^6} dx$$

Optimal. Leaf size=260

$$\frac{5d^9(a+bx)^4(bc-ad)}{2b^{11}} + \frac{15d^8(a+bx)^3(bc-ad)^2}{b^{11}} + \frac{60d^7(a+bx)^2(bc-ad)^3}{b^{11}} + \frac{252d^5(bc-ad)^5 \log(a+bx)}{b^{11}} - \frac{210d^4(bc-ad)^6}{b^{11}(a+bx)}$$

[Out] $210*d^6*(-a*d+b*c)^4*x/b^{10}-1/5*(-a*d+b*c)^{10}/b^{11}/(b*x+a)^5-5/2*d*(-a*d+b*c)^9/b^{11}/(b*x+a)^4-15*d^2*(-a*d+b*c)^8/b^{11}/(b*x+a)^3-60*d^3*(-a*d+b*c)^7/b^{11}/(b*x+a)^2-210*d^4*(-a*d+b*c)^6/b^{11}/(b*x+a)+60*d^7*(-a*d+b*c)^3*(b*x+a)^2/b^{11}+15*d^8*(-a*d+b*c)^2*(b*x+a)^3/b^{11}+5/2*d^9*(-a*d+b*c)*(b*x+a)^4/b^{11}+1/5*d^{10}*(b*x+a)^5/b^{11}+252*d^5*(-a*d+b*c)^5*\ln(b*x+a)/b^{11}$

Rubi [A] time = 0.42, antiderivative size = 260, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{5d^9(a+bx)^4(bc-ad)}{2b^{11}} + \frac{15d^8(a+bx)^3(bc-ad)^2}{b^{11}} + \frac{60d^7(a+bx)^2(bc-ad)^3}{b^{11}} + \frac{210d^6x(bc-ad)^4}{b^{10}} - \frac{210d^4(bc-ad)^6}{b^{11}(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^6, x]

[Out] $(210*d^6*(b*c - a*d)^4*x)/b^{10} - (b*c - a*d)^{10}/(5*b^{11}*(a + b*x)^5) - (5*d*(b*c - a*d)^9)/(2*b^{11}*(a + b*x)^4) - (15*d^2*(b*c - a*d)^8)/(b^{11}*(a + b*x)^3) - (60*d^3*(b*c - a*d)^7)/(b^{11}*(a + b*x)^2) - (210*d^4*(b*c - a*d)^6)/(b^{11}*(a + b*x)) + (60*d^7*(b*c - a*d)^3*(a + b*x)^2)/b^{11} + (15*d^8*(b*c - a*d)^2*(a + b*x)^3)/b^{11} + (5*d^9*(b*c - a*d)*(a + b*x)^4)/(2*b^{11}) + (d^{10}*(a + b*x)^5)/(5*b^{11}) + (252*d^5*(b*c - a*d)^5*\text{Log}[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} & *c^3*d^7 + 2550*a^5*b^5*c^2*d^8 + 475*a^6*b^4*c*d^9 - 347*a^7*b^3*d^{10}) *x^3 \\ & - 10*(15*b^{10}*c^8*d^2 + 60*a*b^9*c^7*d^3 + 420*a^2*b^8*c^6*d^4 - 4620*a^3* \\ & b^7*c^5*d^5 + 12600*a^4*b^6*c^4*d^6 - 16200*a^5*b^5*c^3*d^7 + 10950*a^6*b^4 \\ & *c^2*d^8 - 3725*a^7*b^3*c*d^9 + 493*a^8*b^2*d^{10}) *x^2 - 5*(5*b^{10}*c^9*d + 1 \\ & 5*a*b^9*c^8*d^2 + 60*a^2*b^8*c^7*d^3 + 420*a^3*b^7*c^6*d^4 - 5250*a^4*b^6*c \\ & ^5*d^5 + 15750*a^5*b^5*c^4*d^6 - 22500*a^6*b^4*c^3*d^7 + 17250*a^7*b^3*c^2* \\ & d^8 - 6875*a^8*b^2*c*d^9 + 1123*a^9*b*d^{10}) *x + 2520*(a^5*b^5*c^5*d^5 - 5*a \\ & ^6*b^4*c^4*d^6 + 10*a^7*b^3*c^3*d^7 - 10*a^8*b^2*c^2*d^8 + 5*a^9*b*c*d^9 - \\ & a^{10}*d^{10} + (b^{10}*c^5*d^5 - 5*a*b^9*c^4*d^6 + 10*a^2*b^8*c^3*d^7 - 10*a^3*b \\ & ^7*c^2*d^8 + 5*a^4*b^6*c*d^9 - a^5*b^5*d^{10}) *x^5 + 5*(a*b^9*c^5*d^5 - 5*a^2 \\ & *b^8*c^4*d^6 + 10*a^3*b^7*c^3*d^7 - 10*a^4*b^6*c^2*d^8 + 5*a^5*b^5*c*d^9 - \\ & a^6*b^4*d^{10}) *x^4 + 10*(a^2*b^8*c^5*d^5 - 5*a^3*b^7*c^4*d^6 + 10*a^4*b^6*c^ \\ & 3*d^7 - 10*a^5*b^5*c^2*d^8 + 5*a^6*b^4*c*d^9 - a^7*b^3*d^{10}) *x^3 + 10*(a^3* \\ & b^7*c^5*d^5 - 5*a^4*b^6*c^4*d^6 + 10*a^5*b^5*c^3*d^7 - 10*a^6*b^4*c^2*d^8 + \\ & 5*a^7*b^3*c*d^9 - a^8*b^2*d^{10}) *x^2 + 5*(a^4*b^6*c^5*d^5 - 5*a^5*b^5*c^4*d \\ & ^6 + 10*a^6*b^4*c^3*d^7 - 10*a^7*b^3*c^2*d^8 + 5*a^8*b^2*c*d^9 - a^9*b*d^{10} \\ &) *x) * \log(b*x + a) / (b^{16}*x^5 + 5*a*b^{15}*x^4 + 10*a^2*b^{14}*x^3 + 10*a^3*b^{13} \\ & *x^2 + 5*a^4*b^{12}*x + a^5*b^{11}) \end{aligned}$$

giac [B] time = 1.34, size = 883, normalized size = 3.40

$$\frac{252(b^5c^5d^5 - 5ab^4c^4d^6 + 10a^2b^3c^3d^7 - 10a^3b^2c^2d^8 + 5a^4bcd^9 - a^5d^{10}) \log(|bx + a|)}{b^{11}} \frac{2b^{10}c^{10} + 5ab^9c^9d + 15a^2b^8c^8d^2 + \dots}{b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^6,x, algorithm="giac")

[Out] 252*(b^5*c^5*d^5 - 5*a*b^4*c^4*d^6 + 10*a^2*b^3*c^3*d^7 - 10*a^3*b^2*c^2*d^8 + 5*a^4*b*c*d^9 - a^5*d^10)*log(abs(b*x + a))/b^11 - 1/10*(2*b^10*c^10 + 5*a*b^9*c^9*d + 15*a^2*b^8*c^8*d^2 + 60*a^3*b^7*c^7*d^3 + 420*a^4*b^6*c^6*d^4 - 5754*a^5*b^5*c^5*d^5 + 18270*a^6*b^4*c^4*d^6 - 27540*a^7*b^3*c^3*d^7 + 22290*a^8*b^2*c^2*d^8 - 9395*a^9*b*c*d^9 + 1627*a^10*d^10 + 2100*(b^10*c^6*d^4 - 6*a*b^9*c^5*d^5 + 15*a^2*b^8*c^4*d^6 - 20*a^3*b^7*c^3*d^7 + 15*a^4*b^6*c^2*d^8 - 6*a^5*b^5*c*d^9 + a^6*b^4*d^10)*x^4 + 600*(b^10*c^7*d^3 + 7*a*b^9*c^6*d^4 - 63*a^2*b^8*c^5*d^5 + 175*a^3*b^7*c^4*d^6 - 245*a^4*b^6*c^3*d^7 + 189*a^5*b^5*c^2*d^8 - 77*a^6*b^4*c*d^9 + 13*a^7*b^3*d^10)*x^3 + 150*(b^10*c^8*d^2 + 4*a*b^9*c^7*d^3 + 28*a^2*b^8*c^6*d^4 - 308*a^3*b^7*c^5*d^5 + 9*10*a^4*b^6*c^4*d^6 - 1316*a^5*b^5*c^3*d^7 + 1036*a^6*b^4*c^2*d^8 - 428*a^7*b^3*c*d^9 + 73*a^8*b^2*d^10)*x^2 + 25*(b^10*c^9*d + 3*a*b^9*c^8*d^2 + 12*a^2*b^8*c^7*d^3 + 84*a^3*b^7*c^6*d^4 - 1050*a^4*b^6*c^5*d^5 + 3234*a^5*b^5*c^4*d^6 - 4788*a^6*b^4*c^3*d^7 + 3828*a^7*b^3*c^2*d^8 - 1599*a^8*b^2*c*d^9 + 275*a^9*b*d^10)*x)/((b*x + a)^5*b^11) + 1/10*(2*b^24*d^10*x^5 + 25*b^24*c*d^9*x^4 - 15*a*b^23*d^10*x^4 + 150*b^24*c^2*d^8*x^3 - 200*a*b^23*c*d^9*x^3 + 70*a^2*b^22*d^10*x^3 + 600*b^24*c^3*d^7*x^2 - 1350*a*b^23*c^2*d^8*x^2 + 10

$$50a^2b^{22}c^3d^9x^2 - 280a^3b^{21}d^{10}x^2 + 2100b^{24}c^4d^6x - 7200a^4b^{23}c^3d^7x + 9450a^2b^{22}c^2d^8x - 5600a^3b^{21}c^3d^9x + 1260a^4b^{20}d^{10}x)/b^{30}$$

maple [B] time = 0.02, size = 1199, normalized size = 4.61

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^10/(b*x+a)^6,x)`

[Out]
$$\begin{aligned} & -252/b^{11}d^{10}\ln(b*x+a)*a^5+252/b^6d^5\ln(b*x+a)*c^5+5/2/b^{11}d^{10}/(b*x+a) \\ &)^4*a^9-5/2/b^2d/(b*x+a)^4*c^9-210/b^{11}d^{10}/(b*x+a)*a^6-210/b^5d^4/(b*x+a) \\ &)^4*c^6-3/2*d^{10}/b^7*x^4*a^5/2*d^9/b^6*x^4*c^7*d^{10}/b^8*x^3*a^2+15*d^8/b^6*x \\ &)^3*c^2-28*d^{10}/b^9*x^2*a^3+60*d^7/b^6*x^2*c^3+126*d^{10}/b^{10}*a^4*x+210*d^6/b \\ &)^6*c^4*x-15/b^{11}d^{10}/(b*x+a)^3*a^8-15/b^3d^2/(b*x+a)^3*c^8-1/5/b^{11}/(b*x+a) \\ &)^5*a^10*d^{10}+60/b^{11}d^{10}/(b*x+a)^2*a^7-60/b^4d^3/(b*x+a)^2*c^7+1260/b^1 \\ &)^0*d^9*\ln(b*x+a)*a^4*c-2520/b^9*d^8*\ln(b*x+a)*a^3*c^2-1260/b^6*d^5/(b*x+a)^2 \\ &)^2*a^2*c^5+420/b^5*d^4/(b*x+a)^2*a*c^6-135*d^8/b^7*x^2*a*c^2-560*d^9/b^9*a^3* \\ &)^2*c*x+945*d^8/b^8*a^2*c^2*x-720*d^7/b^7*a*c^3*x+120/b^{10}d^9/(b*x+a)^3*a^7*c- \\ &)^420/b^9*d^8/(b*x+a)^3*a^6*c^2+840/b^8*d^7/(b*x+a)^3*a^5*c^3-1050/b^7*d^6/(b \\ &)^4*x+a)^3*a^4*c^4+840/b^6*d^5/(b*x+a)^3*a^3*c^5-420/b^5*d^4/(b*x+a)^3*a^2*c^6 \\ &)^4+120/b^4*d^3/(b*x+a)^3*a*c^7+2/b^{10}/(b*x+a)^5*a^9*c*d^9-9/b^9/(b*x+a)^5*a^8 \\ &)^2*c^2*d^8+24/b^8/(b*x+a)^5*a^7*c^3*d^7-42/b^7/(b*x+a)^5*a^6*c^4*d^6+252/5/b^ \\ &)^6/(b*x+a)^5*a^5*c^5*d^5-42/b^5/(b*x+a)^5*a^4*c^6*d^4+24/b^4/(b*x+a)^5*a^3*c \\ &)^7*d^3-9/b^3/(b*x+a)^5*a^2*c^8*d^2+2520/b^8*d^7*\ln(b*x+a)*a^2*c^3-1260/b^7* \\ &)^6*\ln(b*x+a)*a*c^4-20*d^9/b^7*x^3*a*c+105*d^9/b^8*x^2*a^2*c-45/2/b^{10}d^9/ \\ &)^4*(b*x+a)^4*a^8*c+90/b^9*d^8/(b*x+a)^4*a^7*c^2-210/b^8*d^7/(b*x+a)^4*a^6*c^3+ \\ &)^315/b^7*d^6/(b*x+a)^4*a^5*c^4-315/b^6*d^5/(b*x+a)^4*a^4*c^5+210/b^5*d^4/(b \\ &)^4*x+a)^4*a^3*c^6-90/b^4*d^3/(b*x+a)^4*a^2*c^7+45/2/b^3*d^2/(b*x+a)^4*a*c^8+12 \\ &)^60/b^{10}d^9/(b*x+a)*a^5*c-3150/b^9*d^8/(b*x+a)*a^4*c^2+4200/b^8*d^7/(b*x+a) \\ &)^3*a^3*c^3-3150/b^7*d^6/(b*x+a)*a^2*c^4+1260/b^6*d^5/(b*x+a)*a*c^5+2/b^2/(b*x \\ &)^5*a*c^9*d-420/b^{10}d^9/(b*x+a)^2*a^6*c+1260/b^9*d^8/(b*x+a)^2*a^5*c^2-2 \\ &)^100/b^8*d^7/(b*x+a)^2*a^4*c^3+2100/b^7*d^6/(b*x+a)^2*a^3*c^4+1/5*d^{10}/b^6*x \\ &)^5-1/5/b/(b*x+a)^5*c^{10} \end{aligned}$$

maxima [B] time = 2.25, size = 912, normalized size = 3.51

$$2b^{10}c^{10} + 5ab^9c^9d + 15a^2b^8c^8d^2 + 60a^3b^7c^7d^3 + 420a^4b^6c^6d^4 - 5754a^5b^5c^5d^5 + 18270a^6b^4c^4d^6 - 27540a^7b^3c^3d^7 + 2520a^8b^2c^2d^8 - 1260a^9b^1c^1d^9 + 1260a^{10}b^0c^0d^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^10/(b*x+a)^6,x, algorithm="maxima")`

```
[Out] -1/10*(2*b^10*c^10 + 5*a*b^9*c^9*d + 15*a^2*b^8*c^8*d^2 + 60*a^3*b^7*c^7*d^3 + 420*a^4*b^6*c^6*d^4 - 5754*a^5*b^5*c^5*d^5 + 18270*a^6*b^4*c^4*d^6 - 27540*a^7*b^3*c^3*d^7 + 22290*a^8*b^2*c^2*d^8 - 9395*a^9*b*c*d^9 + 1627*a^10*d^10 + 2100*(b^10*c^6*d^4 - 6*a*b^9*c^5*d^5 + 15*a^2*b^8*c^4*d^6 - 20*a^3*b^7*c^3*d^7 + 15*a^4*b^6*c^2*d^8 - 6*a^5*b^5*c*d^9 + a^6*b^4*d^10)*x^4 + 600*(b^10*c^7*d^3 + 7*a*b^9*c^6*d^4 - 63*a^2*b^8*c^5*d^5 + 175*a^3*b^7*c^4*d^6 - 245*a^4*b^6*c^3*d^7 + 189*a^5*b^5*c^2*d^8 - 77*a^6*b^4*c*d^9 + 13*a^7*b^3*d^10)*x^3 + 150*(b^10*c^8*d^2 + 4*a*b^9*c^7*d^3 + 28*a^2*b^8*c^6*d^4 - 308*a^3*b^7*c^5*d^5 + 910*a^4*b^6*c^4*d^6 - 1316*a^5*b^5*c^3*d^7 + 1036*a^6*b^4*c^2*d^8 - 428*a^7*b^3*c*d^9 + 73*a^8*b^2*d^10)*x^2 + 25*(b^10*c^9*d + 3*a*b^9*c^8*d^2 + 12*a^2*b^8*c^7*d^3 + 84*a^3*b^7*c^6*d^4 - 1050*a^4*b^6*c^5*d^5 + 3234*a^5*b^5*c^4*d^6 - 4788*a^6*b^4*c^3*d^7 + 3828*a^7*b^3*c^2*d^8 - 1599*a^8*b^2*c*d^9 + 275*a^9*b*d^10)*x)/(b^16*x^5 + 5*a*b^15*x^4 + 10*a^2*b^14*x^3 + 10*a^3*b^13*x^2 + 5*a^4*b^12*x + a^5*b^11) + 1/10*(2*b^4*d^10*x^5 + 5*(5*b^4*c*d^9 - 3*a*b^3*d^10)*x^4 + 10*(15*b^4*c^2*d^8 - 20*a*b^3*c*d^9 + 7*a^2*b^2*d^10)*x^3 + 10*(60*b^4*c^3*d^7 - 135*a*b^3*c^2*d^8 + 105*a^2*b^2*c*d^9 - 28*a^3*b*d^10)*x^2 + 10*(210*b^4*c^4*d^6 - 720*a*b^3*c^3*d^7 + 945*a^2*b^2*c^2*d^8 - 560*a^3*b*c*d^9 + 126*a^4*d^10)*x)/b^10 + 252*(b^5*c^5*d^5 - 5*a*b^4*c^4*d^6 + 10*a^2*b^3*c^3*d^7 - 10*a^3*b^2*c^2*d^8 + 5*a^4*b*c*d^9 - a^5*d^10)*log(b*x + a)/b^11
```

mupad [B] time = 0.40, size = 1141, normalized size = 4.39

$$x^3 \left(\frac{2a \left(\frac{6ad^{10}}{b^7} - \frac{10cd^9}{b^6} \right)}{b} - \frac{5a^2 d^{10}}{b^8} + \frac{15c^2 d^8}{b^6} \right) - x^2 \left(\frac{3a \left(\frac{6a \left(\frac{6ad^{10}}{b^7} - \frac{10cd^9}{b^6} \right)}{b} - \frac{15a^2 d^{10}}{b^8} + \frac{45c^2 d^8}{b^6} \right)}{b} + \frac{10a^3 d^{10}}{b^9} - \frac{60c^3 d^8}{b^6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^10/(a + b*x)^6,x)
```

```
[Out] x^3*((2*a*((6*a*d^10)/b^7 - (10*c*d^9)/b^6))/b - (5*a^2*d^10)/b^8 + (15*c^2*d^8)/b^6) - x^2*((3*a*((6*a*((6*a*d^10)/b^7 - (10*c*d^9)/b^6))/b - (15*a^2*d^10)/b^8 + (45*c^2*d^8)/b^6))/b + (10*a^3*d^10)/b^9 - (60*c^3*d^7)/b^6 - (15*a^2*((6*a*d^10)/b^7 - (10*c*d^9)/b^6))/(2*b^2)) - x^4*((3*a*d^10)/(2*b^7) - (5*c*d^9)/(2*b^6)) - (x^4*(210*a^6*b^3*d^10 + 210*b^9*c^6*d^4 - 1260*a*b^8*c^5*d^5 - 1260*a^5*b^4*c*d^9 + 3150*a^2*b^7*c^4*d^6 - 4200*a^3*b^6*c^3*d^7 + 3150*a^4*b^5*c^2*d^8) + (1627*a^10*d^10 + 2*b^10*c^10 + 15*a^2*b^8*c
```


$$\begin{aligned}
& ^8d^2 + 60a^3b^7c^7d^3 + 420a^4b^6c^6d^4 - 5754a^5b^5c^5d^5 + \\
& 18270a^6b^4c^4d^6 - 27540a^7b^3c^3d^7 + 22290a^8b^2c^2d^8 + 5a \\
& *b^9c^9d - 9395a^9b*c*d^9)/(10*b) + x*((1375a^9*d^10)/2 + (5*b^9*c^9*d \\
&)/2 + (15*a*b^8*c^8*d^2)/2 + 30*a^2*b^7*c^7*d^3 + 210*a^3*b^6*c^6*d^4 - 262 \\
& 5*a^4*b^5*c^5*d^5 + 8085*a^5*b^4*c^4*d^6 - 11970*a^6*b^3*c^3*d^7 + 9570*a^7 \\
& *b^2*c^2*d^8 - (7995*a^8*b*c*d^9)/2) + x^3*(780*a^7*b^2*d^10 + 60*b^9*c^7*d \\
& ^3 + 420*a*b^8*c^6*d^4 - 4620*a^6*b^3*c*d^9 - 3780*a^2*b^7*c^5*d^5 + 10500* \\
& a^3*b^6*c^4*d^6 - 14700*a^4*b^5*c^3*d^7 + 11340*a^5*b^4*c^2*d^8) + x^2*(109 \\
& 5*a^8*b*d^10 + 15*b^9*c^8*d^2 + 60*a*b^8*c^7*d^3 - 6420*a^7*b^2*c*d^9 + 420 \\
& *a^2*b^7*c^6*d^4 - 4620*a^3*b^6*c^5*d^5 + 13650*a^4*b^5*c^4*d^6 - 19740*a^5 \\
& *b^4*c^3*d^7 + 15540*a^6*b^3*c^2*d^8))/(a^5*b^10 + b^15*x^5 + 5*a^4*b^11*x \\
& + 5*a*b^14*x^4 + 10*a^3*b^12*x^2 + 10*a^2*b^13*x^3) + x*((6*a*((6*a*((6*a*(\\
& (6*a*d^10)/b^7 - (10*c*d^9)/b^6))/b - (15*a^2*d^10)/b^8 + (45*c^2*d^8)/b^6) \\
&)/b + (20*a^3*d^10)/b^9 - (120*c^3*d^7)/b^6 - (15*a^2*((6*a*d^10)/b^7 - (10 \\
& *c*d^9)/b^6))/b^2))/b - (15*a^4*d^10)/b^10 + (210*c^4*d^6)/b^6 + (20*a^3*((\\
& 6*a*d^10)/b^7 - (10*c*d^9)/b^6))/b^3 - (15*a^2*((6*a*((6*a*d^10)/b^7 - (10* \\
& c*d^9)/b^6))/b - (15*a^2*d^10)/b^8 + (45*c^2*d^8)/b^6))/b^2) + (d^10*x^5)/(\\
& 5*b^6) - (\log(a + b*x)*(252*a^5*d^10 - 252*b^5*c^5*d^5 + 1260*a*b^4*c^4*d^6 \\
& - 2520*a^2*b^3*c^3*d^7 + 2520*a^3*b^2*c^2*d^8 - 1260*a^4*b*c*d^9))/b^11
\end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**6,x)

[Out] Timed out

$$3.1318 \quad \int \frac{(c+dx)^{10}}{(a+bx)^7} dx$$

Optimal. Leaf size=262

$$\frac{10d^9(a+bx)^3(bc-ad)}{3b^{11}} + \frac{45d^8(a+bx)^2(bc-ad)^2}{2b^{11}} + \frac{210d^6(bc-ad)^4 \log(a+bx)}{b^{11}} - \frac{252d^5(bc-ad)^5}{b^{11}(a+bx)} - \frac{105d^4(bc-ad)^6}{b^{11}(a+bx)^2}$$

[Out] $120*d^7*(-a*d+b*c)^3*x/b^10-1/6*(-a*d+b*c)^10/b^11/(b*x+a)^6-2*d*(-a*d+b*c)^9/b^11/(b*x+a)^5-45/4*d^2*(-a*d+b*c)^8/b^11/(b*x+a)^4-40*d^3*(-a*d+b*c)^7/b^11/(b*x+a)^3-105*d^4*(-a*d+b*c)^6/b^11/(b*x+a)^2-252*d^5*(-a*d+b*c)^5/b^11/(b*x+a)+45/2*d^8*(-a*d+b*c)^2*(b*x+a)^2/b^11+10/3*d^9*(-a*d+b*c)*(b*x+a)^3/b^11+1/4*d^10*(b*x+a)^4/b^11+210*d^6*(-a*d+b*c)^4*\ln(b*x+a)/b^11$

Rubi [A] time = 0.39, antiderivative size = 262, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{10d^9(a+bx)^3(bc-ad)}{3b^{11}} + \frac{45d^8(a+bx)^2(bc-ad)^2}{2b^{11}} + \frac{120d^7x(bc-ad)^3}{b^{10}} - \frac{252d^5(bc-ad)^5}{b^{11}(a+bx)} - \frac{105d^4(bc-ad)^6}{b^{11}(a+bx)^2} - \frac{40d^3(bc-ad)^7}{b^{11}(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^7, x]

[Out] $(120*d^7*(b*c - a*d)^3*x)/b^10 - (b*c - a*d)^10/(6*b^11*(a + b*x)^6) - (2*d*(b*c - a*d)^9)/(b^11*(a + b*x)^5) - (45*d^2*(b*c - a*d)^8)/(4*b^11*(a + b*x)^4) - (40*d^3*(b*c - a*d)^7)/(b^11*(a + b*x)^3) - (105*d^4*(b*c - a*d)^6)/(b^11*(a + b*x)^2) - (252*d^5*(b*c - a*d)^5)/(b^11*(a + b*x)) + (45*d^8*(b*c - a*d)^2*(a + b*x)^2)/(2*b^11) + (10*d^9*(b*c - a*d)*(a + b*x)^3)/(3*b^11) + (d^10*(a + b*x)^4)/(4*b^11) + (210*d^6*(b*c - a*d)^4*\Log[a + b*x])/b^11$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c + dx)^{10}}{(a + bx)^7} dx = \int \left(\frac{120d^7(bc - ad)^3}{b^{10}} + \frac{(bc - ad)^{10}}{b^{10}(a + bx)^7} + \frac{10d(bc - ad)^9}{b^{10}(a + bx)^6} + \frac{45d^2(bc - ad)^8}{b^{10}(a + bx)^5} + \frac{120d^3(bc - ad)^7}{b^{10}(a + bx)^4} + \frac{120d^7(bc - ad)^3x}{b^{10}} - \frac{(bc - ad)^{10}}{6b^{11}(a + bx)^6} - \frac{2d(bc - ad)^9}{b^{11}(a + bx)^5} - \frac{45d^2(bc - ad)^8}{4b^{11}(a + bx)^4} - \frac{40d^3(bc - ad)^7}{b^{11}(a + bx)^3} - \frac{105d^4(bc - ad)^6}{b^{11}(a + bx)^2} - \frac{35d^5(bc - ad)^5}{b^{11}(a + bx)} + \frac{7d^6(bc - ad)^4}{b^{11}} \right) dx$$

Mathematica [A] time = 0.22, size = 265, normalized size = 1.01

$$\frac{6b^2d^8x^2(28a^2d^2 - 70abcd + 45b^2c^2) + 12bd^7x(-84a^3d^3 + 280a^2bcd^2 - 315ab^2c^2d + 120b^3c^3) + 4b^3d^9x^3(10bc - 7a^2d)}{b^{11}(a + bx)^7}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^7,x]

[Out] (12*b*d^7*(120*b^3*c^3 - 315*a*b^2*c^2*d + 280*a^2*b*c*d^2 - 84*a^3*d^3)*x + 6*b^2*d^8*(45*b^2*c^2 - 70*a*b*c*d + 28*a^2*d^2)*x^2 + 4*b^3*d^9*(10*b*c - 7*a*d)*x^3 + 3*b^4*d^10*x^4 - (2*(b*c - a*d)^10)/(a + b*x)^6 + (24*d*(-(b*c) + a*d)^9)/(a + b*x)^5 - (135*d^2*(b*c - a*d)^8)/(a + b*x)^4 + (480*d^3*(-(b*c) + a*d)^7)/(a + b*x)^3 - (1260*d^4*(b*c - a*d)^6)/(a + b*x)^2 + (3024*d^5*(-(b*c) + a*d)^5)/(a + b*x) + 2520*d^6*(b*c - a*d)^4*Log[a + b*x])/(12*b^11)

fricas [B] time = 0.45, size = 1386, normalized size = 5.29

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^7,x, algorithm="fricas")

[Out] 1/12*(3*b^10*d^10*x^10 - 2*b^10*c^10 - 4*a*b^9*c^9*d - 9*a^2*b^8*c^8*d^2 - 24*a^3*b^7*c^7*d^3 - 84*a^4*b^6*c^6*d^4 - 504*a^5*b^5*c^5*d^5 + 6174*a^6*b^4*c^4*d^6 - 16056*a^7*b^3*c^3*d^7 + 18414*a^8*b^2*c^2*d^8 - 10036*a^9*b*c*d^9 + 2131*a^10*d^10 + 10*(4*b^10*c*d^9 - a*b^9*d^10)*x^9 + 45*(6*b^10*c^2*d^8 - 4*a*b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 360*(4*b^10*c^3*d^7 - 6*a*b^9*c^2*d^8 + 4*a^2*b^8*c*d^9 - a^3*b^7*d^10)*x^7 + (8640*a*b^9*c^3*d^7 - 18630*a^2*b^8*c^2*d^8 + 14660*a^3*b^7*c*d^9 - 4043*a^4*b^6*d^10)*x^6 - 6*(504*b^10*c^5*d^5 - 2520*a*b^9*c^4*d^6 + 1440*a^2*b^8*c^3*d^7 + 3510*a^3*b^7*c^2*d^8 - 4580*a^4*b^6*c*d^9 + 1523*a^5*b^5*d^10)*x^5 - 15*(84*b^10*c^6*d^4 + 504*a*b^9*c^5*d^5 - 3780*a^2*b^8*c^4*d^6 + 6480*a^3*b^7*c^3*d^7 - 4050*a^4*b^6*c^2*d^8 + 460*a^5*b^5*c*d^9 + 263*a^6*b^4*d^10)*x^4 - 20*(24*b^10*c^7*d^3 + 84*a*b^9*c^6*d^4 + 504*a^2*b^8*c^5*d^5 - 4620*a^3*b^7*c^4*d^6 + 9840*a^4*b^6*c^3*d^7 - 10036*a^5*b^5*c^3*d^7 + 18414*a^6*b^4*c^2*d^8 - 10036*a^7*b^3*c^2*d^8 - 5040*a^8*b^2*c^2*d^8 - 10036*a^9*b*c*d^9 + 2131*a^10*d^10)*x^3 + 45*(6*b^10*c^2*d^8 - 4*a*b^9*c*d^9 + a^2*b^8*d^10)*x^2 + 360*(4*b^10*c^3*d^7 - 6*a*b^9*c^2*d^8 + 4*a^2*b^8*c*d^9 - a^3*b^7*d^10)*x + 360*(4*b^10*c^3*d^7 - 6*a*b^9*c^2*d^8 + 4*a^2*b^8*c*d^9 - a^3*b^7*d^10)

```

*c^3*d^7 - 9090*a^5*b^5*c^2*d^8 + 3820*a^6*b^4*c*d^9 - 577*a^7*b^3*d^10)*x^
3 - 15*(9*b^10*c^8*d^2 + 24*a*b^9*c^7*d^3 + 84*a^2*b^8*c^6*d^4 + 504*a^3*b^
7*c^5*d^5 - 5250*a^4*b^6*c^4*d^6 + 12360*a^5*b^5*c^3*d^7 - 12870*a^6*b^4*c^
2*d^8 + 6340*a^7*b^3*c*d^9 - 1207*a^8*b^2*d^10)*x^2 - 6*(4*b^10*c^9*d + 9*a
*b^9*c^8*d^2 + 24*a^2*b^8*c^7*d^3 + 84*a^3*b^7*c^6*d^4 + 504*a^4*b^6*c^5*d^
5 - 5754*a^5*b^5*c^4*d^6 + 14376*a^6*b^4*c^3*d^7 - 15894*a^7*b^3*c^2*d^8 +
8356*a^8*b^2*c*d^9 - 1711*a^9*b*d^10)*x + 2520*(a^6*b^4*c^4*d^6 - 4*a^7*b^3
*c^3*d^7 + 6*a^8*b^2*c^2*d^8 - 4*a^9*b*c*d^9 + a^10*d^10 + (b^10*c^4*d^6 -
4*a*b^9*c^3*d^7 + 6*a^2*b^8*c^2*d^8 - 4*a^3*b^7*c*d^9 + a^4*b^6*d^10)*x^6 +
6*(a*b^9*c^4*d^6 - 4*a^2*b^8*c^3*d^7 + 6*a^3*b^7*c^2*d^8 - 4*a^4*b^6*c*d^9
+ a^5*b^5*d^10)*x^5 + 15*(a^2*b^8*c^4*d^6 - 4*a^3*b^7*c^3*d^7 + 6*a^4*b^6*c
^2*d^8 - 4*a^5*b^5*c*d^9 + a^6*b^4*d^10)*x^4 + 20*(a^3*b^7*c^4*d^6 - 4*a^4
*b^6*c^3*d^7 + 6*a^5*b^5*c^2*d^8 - 4*a^6*b^4*c*d^9 + a^7*b^3*d^10)*x^3 + 15
*(a^4*b^6*c^4*d^6 - 4*a^5*b^5*c^3*d^7 + 6*a^6*b^4*c^2*d^8 - 4*a^7*b^3*c*d^9
+ a^8*b^2*d^10)*x^2 + 6*(a^5*b^5*c^4*d^6 - 4*a^6*b^4*c^3*d^7 + 6*a^7*b^3*c
^2*d^8 - 4*a^8*b^2*c*d^9 + a^9*b*d^10)*x)*log(b*x + a))/(b^17*x^6 + 6*a*b^1
6*x^5 + 15*a^2*b^15*x^4 + 20*a^3*b^14*x^3 + 15*a^4*b^13*x^2 + 6*a^5*b^12*x
+ a^6*b^11)

```

giac [B] time = 1.29, size = 878, normalized size = 3.35

$$\frac{210(b^4c^4d^6 - 4ab^3c^3d^7 + 6a^2b^2c^2d^8 - 4a^3bcd^9 + a^4d^{10})\log(|bx + a|)}{b^{11}} \frac{2b^{10}c^{10} + 4ab^9c^9d + 9a^2b^8c^8d^2 + 24a^3b^7c^7d^3 + 84a^4b^6c^6d^4 + 504a^5b^5c^5d^5 - 6174a^6b^4c^4d^6 + 16056a^7b^3c^3d^7 - 18414a^8b^2c^2d^8 + 10036a^9b^1c^1d^9 - 2131a^{10}d^{10} + 3024(b^{10}c^5d^5 - 5a^1b^9c^4d^6 + 10a^2b^8c^3d^7 - 10a^3b^7c^2d^8 + 5a^4b^6c^1d^9 - a^5b^5d^{10})x^5 + 1260(b^{10}c^6d^4 + 6a^1b^9c^5d^5 - 45a^2b^8c^4d^6 + 100a^3b^7c^3d^7 - 105a^4b^6c^2d^8 + 54a^5b^5c^1d^9 - 11a^6b^4d^{10})x^4 + 240(2b^{10}c^7d^3 + 7a^1b^9c^6d^4 + 42a^2b^8c^5d^5 - 385a^3b^7c^4d^6 + 910a^4b^6c^3d^7 - 987a^5b^5c^2d^8 + 518a^6b^4c^1d^9 - 107a^7b^3d^{10})x^3 + 45(3b^{10}c^8d^2 + 8a^1b^9c^7d^3 + 28a^2b^8c^6d^4 + 168a^3b^7c^5d^5 - 1750a^4b^6c^4d^6 + 4312a^5b^5c^3d^7 - 4788a^6b^4c^2d^8 + 2552a^7b^3c^1d^9 - 533a^8b^2d^{10})x^2 + 6(4b^{10}c^9d + 9a^1b^9c^8d^2 + 24a^2b^8c^7d^3 + 84a^3b^7c^6d^4 + 504a^4b^6c^5d^5 - 5754a^5b^5c^4d^6 + 14616a^6b^4c^3d^7 - 16524a^7b^3c^2d^8 + 8916a^8b^2c^1d^9 - 1879a^9b^1d^{10})x}{(b*x + a)^6*b^{11}} + \frac{1}{12}(3*b^{21}*d^{10}*x^4 + 40*b^{21}*c*d^9*x^3 - 28*a*b^{20}*d^{10}*x^3 + 270*b^{21}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^10/(b*x+a)^7,x, algorithm="giac")
```

```

[Out] 210*(b^4*c^4*d^6 - 4*a*b^3*c^3*d^7 + 6*a^2*b^2*c^2*d^8 - 4*a^3*b*c*d^9 + a^
4*d^10)*log(abs(b*x + a))/b^11 - 1/12*(2*b^10*c^10 + 4*a*b^9*c^9*d + 9*a^2*
b^8*c^8*d^2 + 24*a^3*b^7*c^7*d^3 + 84*a^4*b^6*c^6*d^4 + 504*a^5*b^5*c^5*d^5
- 6174*a^6*b^4*c^4*d^6 + 16056*a^7*b^3*c^3*d^7 - 18414*a^8*b^2*c^2*d^8 + 1
0036*a^9*b^1*c^1*d^9 - 2131*a^10*d^10 + 3024*(b^10*c^5*d^5 - 5*a*b^9*c^4*d^6 +
10*a^2*b^8*c^3*d^7 - 10*a^3*b^7*c^2*d^8 + 5*a^4*b^6*c^1*d^9 - a^5*b^5*d^10)*x
^5 + 1260*(b^10*c^6*d^4 + 6*a*b^9*c^5*d^5 - 45*a^2*b^8*c^4*d^6 + 100*a^3*b^
7*c^3*d^7 - 105*a^4*b^6*c^2*d^8 + 54*a^5*b^5*c^1*d^9 - 11*a^6*b^4*d^10)*x^4 +
240*(2*b^10*c^7*d^3 + 7*a*b^9*c^6*d^4 + 42*a^2*b^8*c^5*d^5 - 385*a^3*b^7*c^
4*d^6 + 910*a^4*b^6*c^3*d^7 - 987*a^5*b^5*c^2*d^8 + 518*a^6*b^4*c^1*d^9 - 10
7*a^7*b^3*d^10)*x^3 + 45*(3*b^10*c^8*d^2 + 8*a*b^9*c^7*d^3 + 28*a^2*b^8*c^6
*d^4 + 168*a^3*b^7*c^5*d^5 - 1750*a^4*b^6*c^4*d^6 + 4312*a^5*b^5*c^3*d^7 -
4788*a^6*b^4*c^2*d^8 + 2552*a^7*b^3*c^1*d^9 - 533*a^8*b^2*d^10)*x^2 + 6*(4*b^
10*c^9*d + 9*a*b^9*c^8*d^2 + 24*a^2*b^8*c^7*d^3 + 84*a^3*b^7*c^6*d^4 + 504*
a^4*b^6*c^5*d^5 - 5754*a^5*b^5*c^4*d^6 + 14616*a^6*b^4*c^3*d^7 - 16524*a^7*
b^3*c^2*d^8 + 8916*a^8*b^2*c^1*d^9 - 1879*a^9*b^1*d^10)*x)/((b*x + a)^6*b^11) +
1/12*(3*b^21*d^10*x^4 + 40*b^21*c*d^9*x^3 - 28*a*b^20*d^10*x^3 + 270*b^21

```

$$c^2d^8x^2 - 420ab^{20}cd^9x^2 + 168a^2b^{19}d^{10}x^2 + 1440b^{21}c^3d^7x - 3780a^2b^{20}c^2d^8x + 3360a^2b^{19}cd^9x - 1008a^3b^{18}d^{10}x)/b^{28}$$

maple [B] time = 0.02, size = 1222, normalized size = 4.66

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^7,x)

[Out] $252/b^{11}d^{10}/(b*x+a)*a^5 - 252/b^6d^5/(b*x+a)*c^5 - 1/6/b^{11}/(b*x+a)^6*a^{10}d^{10} + 2/b^{11}d^{10}/(b*x+a)^5*a^9 - 2/b^2d/(b*x+a)^5*c^9 - 105/b^{11}d^{10}/(b*x+a)^2*a^6 - 105/b^5d^4/(b*x+a)^2*c^6 + 210/b^{11}d^{10}*\ln(b*x+a)*a^4 + 210/b^7d^6*\ln(b*x+a)*c^4 - 45/4/b^{11}d^{10}/(b*x+a)^4*a^8 - 45/4/b^3d^2/(b*x+a)^4*c^8 + 45/2d^8/b^7*x^2*c^2 - 84d^{10}/b^{10}*a^3*x + 120d^7/b^7*c^3*x + 40/b^{11}d^{10}/(b*x+a)^3*a^7 - 40/b^4d^3/(b*x+a)^3*c^7 - 7/3d^{10}/b^8*x^3*a + 10/3d^9/b^7*x^3*c + 14d^{10}/b^9*x^2*a^2 - 315d^8/b^8*a*c^2*x - 280/b^{10}d^9/(b*x+a)^3*a^6*c + 2100/b^8d^7/(b*x+a)^2*a^3*c^3 - 1575/b^7d^6/(b*x+a)^2*a^2*c^4 + 72/b^9d^8/(b*x+a)^5*a^7*c^2 - 168/b^8d^7/(b*x+a)^5*a^6*c^3 + 252/b^7d^6/(b*x+a)^5*a^5*c^4 - 252/b^6d^5/(b*x+a)^5*a^4*c^5 + 168/b^5d^4/(b*x+a)^5*a^3*c^6 - 72/b^4d^3/(b*x+a)^5*a^2*c^7 + 18/b^3d^2/(b*x+a)^5*a*c^8 + 840/b^9d^8/(b*x+a)^3*a^5*c^2 - 1400/b^8d^7/(b*x+a)^3*a^4*c^3 + 1400/b^7d^6/(b*x+a)^3*a^3*c^4 - 840/b^6d^5/(b*x+a)^3*a^2*c^5 + 280/b^5d^4/(b*x+a)^3*a*c^6 + 630/b^6d^5/(b*x+a)^2*a*c^5 - 35d^9/b^8*x^2*a*c + 280*d^9/b^9*a^2*c*x - 18/b^{10}d^9/(b*x+a)^5*a^8*c + 1260/b^7d^6/(b*x+a)*a*c^4 + 5/3/b^{10}/(b*x+a)^6*a^9*c*d^9 - 15/2/b^9/(b*x+a)^6*a^8*c^2*d^8 + 20/b^8/(b*x+a)^6*a^7*c^3*d^7 - 35/b^7/(b*x+a)^6*a^6*c^4*d^6 + 42/b^6/(b*x+a)^6*a^5*c^5*d^5 - 35/b^5/(b*x+a)^6*a^4*c^6*d^4 + 20/b^4/(b*x+a)^6*a^3*c^7*d^3 - 15/2/b^3/(b*x+a)^6*a^2*c^8*d^2 + 5/3/b^2/(b*x+a)^6*a*c^9*d + 90/b^{10}d^9/(b*x+a)^4*a^7*c - 315/b^9d^8/(b*x+a)^4*a^6*c^2 + 630/b^8d^7/(b*x+a)^4*a^5*c^3 - 1575/2/b^7d^6/(b*x+a)^4*a^4*c^4 + 630/b^6d^5/(b*x+a)^4*a^3*c^5 - 315/b^5d^4/(b*x+a)^4*a^2*c^6 + 90/b^4d^3/(b*x+a)^4*a*c^7 - 1260/b^{10}d^9/(b*x+a)*a^4*c + 2520/b^9d^8/(b*x+a)*a^3*c^2 - 2520/b^8d^7/(b*x+a)*a^2*c^3 + 1260/b^9d^8*\ln(b*x+a)*a^2*c^2 - 840/b^8d^7*\ln(b*x+a)*a*c^3 - 840/b^{10}d^9*\ln(b*x+a)*a^3*c + 630/b^{10}d^9/(b*x+a)^2*a^5*c - 1575/b^9d^8/(b*x+a)^2*a^4*c^2 + 1/4d^{10}/b^7*x^4 - 1/6/b/(b*x+a)^6*c^{10}$

maxima [B] time = 2.45, size = 925, normalized size = 3.53

$$2b^{10}c^{10} + 4ab^9c^9d + 9a^2b^8c^8d^2 + 24a^3b^7c^7d^3 + 84a^4b^6c^6d^4 + 504a^5b^5c^5d^5 - 6174a^6b^4c^4d^6 + 16056a^7b^3c^3d^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^7,x, algorithm="maxima")

[Out]
$$\frac{-1/12*(2*b^{10}*c^{10} + 4*a*b^9*c^9*d + 9*a^2*b^8*c^8*d^2 + 24*a^3*b^7*c^7*d^3 + 84*a^4*b^6*c^6*d^4 + 504*a^5*b^5*c^5*d^5 - 6174*a^6*b^4*c^4*d^6 + 16056*a^7*b^3*c^3*d^7 - 18414*a^8*b^2*c^2*d^8 + 10036*a^9*b*c*d^9 - 2131*a^{10}*d^{10} + 3024*(b^{10}*c^5*d^5 - 5*a*b^9*c^4*d^6 + 10*a^2*b^8*c^3*d^7 - 10*a^3*b^7*c^2*d^8 + 5*a^4*b^6*c*d^9 - a^5*b^5*d^{10})*x^5 + 1260*(b^{10}*c^6*d^4 + 6*a*b^9*c^5*d^5 - 45*a^2*b^8*c^4*d^6 + 100*a^3*b^7*c^3*d^7 - 105*a^4*b^6*c^2*d^8 + 54*a^5*b^5*c*d^9 - 11*a^6*b^4*d^{10})*x^4 + 240*(2*b^{10}*c^7*d^3 + 7*a*b^9*c^6*d^4 + 42*a^2*b^8*c^5*d^5 - 385*a^3*b^7*c^4*d^6 + 910*a^4*b^6*c^3*d^7 - 987*a^5*b^5*c^2*d^8 + 518*a^6*b^4*c*d^9 - 107*a^7*b^3*d^{10})*x^3 + 45*(3*b^{10}*c^8*d^2 + 8*a*b^9*c^7*d^3 + 28*a^2*b^8*c^6*d^4 + 168*a^3*b^7*c^5*d^5 - 1750*a^4*b^6*c^4*d^6 + 4312*a^5*b^5*c^3*d^7 - 4788*a^6*b^4*c^2*d^8 + 2552*a^7*b^3*c*d^9 - 533*a^8*b^2*d^{10})*x^2 + 6*(4*b^{10}*c^9*d + 9*a*b^9*c^8*d^2 + 24*a^2*b^8*c^7*d^3 + 84*a^3*b^7*c^6*d^4 + 504*a^4*b^6*c^5*d^5 - 5754*a^5*b^5*c^4*d^6 + 14616*a^6*b^4*c^3*d^7 - 16524*a^7*b^3*c^2*d^8 + 8916*a^8*b^2*c*d^9 - 1879*a^9*b*d^{10})*x)/(b^{17}*x^6 + 6*a*b^{16}*x^5 + 15*a^2*b^{15}*x^4 + 20*a^3*b^{14}*x^3 + 15*a^4*b^{13}*x^2 + 6*a^5*b^{12}*x + a^6*b^{11}) + 1/12*(3*b^3*d^{10}*x^4 + 4*(10*b^3*c*d^9 - 7*a*b^2*d^{10})*x^3 + 6*(45*b^3*c^2*d^8 - 70*a*b^2*c*d^9 + 28*a^2*b*d^{10})*x^2 + 12*(120*b^3*c^3*d^7 - 315*a*b^2*c^2*d^8 + 280*a^2*b*c*d^9 - 84*a^3*d^{10})*x)/b^{10} + 210*(b^4*c^4*d^6 - 4*a*b^3*c^3*d^7 + 6*a^2*b^2*c^2*d^8 - 4*a^3*b*c*d^9 + a^4*d^{10})*log(b*x + a)/b^{11}$$

mupad [B] time = 0.42, size = 997, normalized size = 3.81

$$x^2 \left(\frac{7a \left(\frac{7ad^{10}}{b^8} - \frac{10cd^9}{b^7} \right)}{2b} - \frac{21a^2d^{10}}{2b^9} + \frac{45c^2d^8}{2b^7} \right) \frac{x^4 (-1155a^6b^3d^{10} + 5670a^5b^4cd^9 - 11025a^4b^5c^2d^8 + 10500a^3b^6c^3d^7 - 11025a^4b^5c^2d^8) + (2b^{10}c^{10} - 2131a^{10}d^{10} + 9a^2b^8c^8d^2 + 24a^3b^7c^7d^3 + 84a^4b^6c^6d^4 + 504a^5b^5c^5d^5 - 6174a^6b^4c^4d^6 + 16056a^7b^3c^3d^7 - 18414a^8b^2c^2d^8 + 4a^9b^1c^1d^9 + 10036a^9b^1c^1d^9) / (12b) + x(2b^9c^9d - (1879a^9d^{10})/2 + (9a^8b^8c^8d^2)/2 + 12a^2b^7c^7d^3 + 42a^3b^6c^6d^4 + 252a^4b^5c^5d^5 - 2877a^5b^4c^4d^6 + 7308a^6b^3c^3d^7 - 8262a^7b^2c^2d^8 + 4458a^8b^1c^1d^9) + x^3(40b^9c^7d^3 - 2140a^7b^2d^{10} + 140a^6b^3c^6d^4 + 10360a^6b^3c^6d^9 + 840a^2b^7c^5d^5 - 7700a^3b^6c^4d^6)}{b^{17}x^6 + 6ab^{16}x^5 + 15a^2b^{15}x^4 + 20a^3b^{14}x^3 + 15a^4b^{13}x^2 + 6a^5b^{12}x + a^6b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((c + d*x)^{10}/(a + b*x)^7, x)$

[Out]
$$x^2*((7*a*((7*a*d^{10})/b^8 - (10*c*d^9)/b^7))/(2*b) - (21*a^2*d^{10})/(2*b^9) + (45*c^2*d^8)/(2*b^7)) - (x^4*(105*b^9*c^6*d^4 - 1155*a^6*b^3*d^{10} + 630*a*b^8*c^5*d^5 + 5670*a^5*b^4*c*d^9 - 4725*a^2*b^7*c^4*d^6 + 10500*a^3*b^6*c^3*d^7 - 11025*a^4*b^5*c^2*d^8) + (2*b^{10}*c^{10} - 2131*a^{10}*d^{10} + 9*a^2*b^8*c^8*d^2 + 24*a^3*b^7*c^7*d^3 + 84*a^4*b^6*c^6*d^4 + 504*a^5*b^5*c^5*d^5 - 6174*a^6*b^4*c^4*d^6 + 16056*a^7*b^3*c^3*d^7 - 18414*a^8*b^2*c^2*d^8 + 4*a^9*b^1*c^1*d^9 + 10036*a^9*b^1*c^1*d^9)/(12*b) + x*(2*b^9*c^9*d - (1879*a^9*d^{10})/2 + (9*a^8*b^8*c^8*d^2)/2 + 12*a^2*b^7*c^7*d^3 + 42*a^3*b^6*c^6*d^4 + 252*a^4*b^5*c^5*d^5 - 2877*a^5*b^4*c^4*d^6 + 7308*a^6*b^3*c^3*d^7 - 8262*a^7*b^2*c^2*d^8 + 4458*a^8*b^1*c^1*d^9) + x^3*(40*b^9*c^7*d^3 - 2140*a^7*b^2*d^{10} + 140*a^6*b^3*c^6*d^4 + 10360*a^6*b^3*c^6*d^9 + 840*a^2*b^7*c^5*d^5 - 7700*a^3*b^6*c^4*d^6)$$

$$\begin{aligned}
& ^6 + 18200*a^4*b^5*c^3*d^7 - 19740*a^5*b^4*c^2*d^8) + x^2*((45*b^9*c^8*d^2) \\
& /4 - (7995*a^8*b*d^10)/4 + 30*a*b^8*c^7*d^3 + 9570*a^7*b^2*c*d^9 + 105*a^2* \\
& b^7*c^6*d^4 + 630*a^3*b^6*c^5*d^5 - (13125*a^4*b^5*c^4*d^6)/2 + 16170*a^5*b \\
& ^4*c^3*d^7 - 17955*a^6*b^3*c^2*d^8) - x^5*(252*a^5*b^4*d^10 - 252*b^9*c^5*d \\
& ^5 + 1260*a*b^8*c^4*d^6 - 1260*a^4*b^5*c*d^9 - 2520*a^2*b^7*c^3*d^7 + 2520* \\
& a^3*b^6*c^2*d^8))/(a^6*b^10 + b^16*x^6 + 6*a^5*b^11*x + 6*a*b^15*x^5 + 15*a \\
& ^4*b^12*x^2 + 20*a^3*b^13*x^3 + 15*a^2*b^14*x^4) - x^3*((7*a*d^10)/(3*b^8) \\
& - (10*c*d^9)/(3*b^7)) - x*((7*a*((7*a*((7*a*d^10)/b^8 - (10*c*d^9)/b^7)))/b \\
& - (21*a^2*d^10)/b^9 + (45*c^2*d^8)/b^7))/b + (35*a^3*d^10)/b^10 - (120*c^3* \\
& d^7)/b^7 - (21*a^2*((7*a*d^10)/b^8 - (10*c*d^9)/b^7))/b^2) + (\log(a + b*x)* \\
& (210*a^4*d^10 + 210*b^4*c^4*d^6 - 840*a*b^3*c^3*d^7 + 1260*a^2*b^2*c^2*d^8 \\
& - 840*a^3*b*c*d^9))/b^11 + (d^10*x^4)/(4*b^7)
\end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**7,x)

[Out] Timed out

$$3.1319 \quad \int \frac{(c+dx)^{10}}{(a+bx)^8} dx$$

Optimal. Leaf size=258

$$\frac{5d^9(a+bx)^2(bc-ad)}{b^{11}} + \frac{120d^7(bc-ad)^3 \log(a+bx)}{b^{11}} - \frac{210d^6(bc-ad)^4}{b^{11}(a+bx)} - \frac{126d^5(bc-ad)^5}{b^{11}(a+bx)^2} - \frac{70d^4(bc-ad)^6}{b^{11}(a+bx)^3} - \frac{30d^3(bc-ad)^7}{b^{11}(a+bx)^4} - \frac{9d^2(bc-ad)^8}{b^{11}(a+bx)^5} - \frac{5d(bc-ad)^9}{b^{11}(a+bx)^6} - \frac{d^2(bc-ad)^{10}}{b^{11}(a+bx)^7}$$

[Out] 45*d^8*(-a*d+b*c)^2*x/b^10-1/7*(-a*d+b*c)^10/b^11/(b*x+a)^7-5/3*d*(-a*d+b*c)^9/b^11/(b*x+a)^6-9*d^2*(-a*d+b*c)^8/b^11/(b*x+a)^5-30*d^3*(-a*d+b*c)^7/b^11/(b*x+a)^4-70*d^4*(-a*d+b*c)^6/b^11/(b*x+a)^3-126*d^5*(-a*d+b*c)^5/b^11/(b*x+a)^2-210*d^6*(-a*d+b*c)^4/b^11/(b*x+a)+5*d^9*(-a*d+b*c)*(b*x+a)^2/b^11+1/3*d^10*(b*x+a)^3/b^11+120*d^7*(-a*d+b*c)^3*ln(b*x+a)/b^11

Rubi [A] time = 0.36, antiderivative size = 258, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{5d^9(a+bx)^2(bc-ad)}{b^{11}} + \frac{45d^8x(bc-ad)^2}{b^{10}} - \frac{210d^6(bc-ad)^4}{b^{11}(a+bx)} - \frac{126d^5(bc-ad)^5}{b^{11}(a+bx)^2} - \frac{70d^4(bc-ad)^6}{b^{11}(a+bx)^3} - \frac{30d^3(bc-ad)^7}{b^{11}(a+bx)^4} - \frac{9d^2(bc-ad)^8}{b^{11}(a+bx)^5} - \frac{5d(bc-ad)^9}{b^{11}(a+bx)^6} - \frac{d^2(bc-ad)^{10}}{b^{11}(a+bx)^7}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^8, x]

[Out] (45*d^8*(b*c - a*d)^2*x)/b^10 - (b*c - a*d)^10/(7*b^11*(a + b*x)^7) - (5*d*(b*c - a*d)^9)/(3*b^11*(a + b*x)^6) - (9*d^2*(b*c - a*d)^8)/(b^11*(a + b*x)^5) - (30*d^3*(b*c - a*d)^7)/(b^11*(a + b*x)^4) - (70*d^4*(b*c - a*d)^6)/(b^11*(a + b*x)^3) - (126*d^5*(b*c - a*d)^5)/(b^11*(a + b*x)^2) - (210*d^6*(b*c - a*d)^4)/(b^11*(a + b*x)) + (5*d^9*(b*c - a*d)*(a + b*x)^2)/b^11 + (d^10*(a + b*x)^3)/(3*b^11) + (120*d^7*(b*c - a*d)^3*Log[a + b*x])/b^11

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^{10}}{(a+bx)^8} dx = \int \left(\frac{45d^8(bc-ad)^2}{b^{10}} + \frac{(bc-ad)^{10}}{b^{10}(a+bx)^8} + \frac{10d(bc-ad)^9}{b^{10}(a+bx)^7} + \frac{45d^2(bc-ad)^8}{b^{10}(a+bx)^6} + \frac{120d^3(bc-ad)^7}{b^{10}(a+bx)^5} + \frac{270d^4(bc-ad)^6}{b^{10}(a+bx)^4} + \frac{270d^5(bc-ad)^5}{b^{10}(a+bx)^3} + \frac{180d^6(bc-ad)^4}{b^{10}(a+bx)^2} + \frac{90d^7(bc-ad)^3}{b^{10}(a+bx)} + \frac{45d^8(bc-ad)^2}{b^{10}} \right) dx$$

$$= \frac{45d^8(bc-ad)^2x}{b^{10}} - \frac{(bc-ad)^{10}}{7b^{11}(a+bx)^7} - \frac{5d(bc-ad)^9}{3b^{11}(a+bx)^6} - \frac{9d^2(bc-ad)^8}{b^{11}(a+bx)^5} - \frac{30d^3(bc-ad)^7}{b^{11}(a+bx)^4} - \frac{70d^4(bc-ad)^6}{b^{11}(a+bx)^3} - \frac{105d^5(bc-ad)^5}{b^{11}(a+bx)^2} - \frac{105d^6(bc-ad)^4}{b^{11}(a+bx)} + \frac{45d^7(bc-ad)^3}{b^{11}} + \frac{45d^8(bc-ad)^2}{b^{11}}$$

Mathematica [A] time = 0.25, size = 239, normalized size = 0.93

$$\frac{21bd^8x(36a^2d^2 - 80abcd + 45b^2c^2) + 21b^2d^9x^2(5bc - 4ad) + 2520d^7(bc - ad)^3 \log(a + bx) - \frac{4410d^6(bc-ad)^4}{a+bx} + \frac{2640d^5(bc-ad)^3}{b^{11}}}{21b^{11}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^8,x]

[Out] (21*b*d^8*(45*b^2*c^2 - 80*a*b*c*d + 36*a^2*d^2)*x + 21*b^2*d^9*(5*b*c - 4*a*d)*x^2 + 7*b^3*d^10*x^3 - (3*(b*c - a*d)^10)/(a + b*x)^7 + (35*d*(-(b*c) + a*d)^9)/(a + b*x)^6 - (189*d^2*(b*c - a*d)^8)/(a + b*x)^5 + (630*d^3*(-(b*c) + a*d)^7)/(a + b*x)^4 - (1470*d^4*(b*c - a*d)^6)/(a + b*x)^3 + (2646*d^5*(-(b*c) + a*d)^5)/(a + b*x)^2 - (4410*d^6*(b*c - a*d)^4)/(a + b*x) + 2520*d^7*(b*c - a*d)^3*Log[a + b*x])/(21*b^11)

fricas [B] time = 0.46, size = 1362, normalized size = 5.28

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^8,x, algorithm="fricas")

[Out] 1/21*(7*b^10*d^10*x^10 - 3*b^10*c^10 - 5*a*b^9*c^9*d - 9*a^2*b^8*c^8*d^2 - 18*a^3*b^7*c^7*d^3 - 42*a^4*b^6*c^6*d^4 - 126*a^5*b^5*c^5*d^5 - 630*a^6*b^4*c^4*d^6 + 6534*a^7*b^3*c^3*d^7 - 12987*a^8*b^2*c^2*d^8 + 10047*a^9*b*c*d^9 - 2761*a^10*d^10 + 35*(3*b^10*c*d^9 - a*b^9*d^10)*x^9 + 315*(3*b^10*c^2*d^8 - 3*a*b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 49*(135*a*b^9*c^2*d^8 - 195*a^2*b^8*c*d^9 + 77*a^3*b^7*d^10)*x^7 - 49*(90*b^10*c^4*d^6 - 360*a*b^9*c^3*d^7 + 135*a^2*b^8*c^2*d^8 + 285*a^3*b^7*c*d^9 - 179*a^4*b^6*d^10)*x^6 - 147*(18*b^10*c^5*d^5 + 90*a*b^9*c^4*d^6 - 540*a^2*b^8*c^3*d^7 + 675*a^3*b^7*c^2*d^8 - 255*a^4*b^6*c*d^9 + a^5*b^5*d^10)*x^5 - 245*(6*b^10*c^6*d^4 + 18*a*b^9*c^5*d^5 + 90*a^2*b^8*c^4*d^6 - 660*a^3*b^7*c^3*d^7 + 1035*a^4*b^6*c^2*d^8 - 615*a^5*b^5*c*d^9 + 121*a^6*b^4*d^10)*x^4 - 35*(18*b^10*c^7*d^3 + 42*a*b^9*c^6*d^4 + 126*a^2*b^8*c^5*d^5 + 630*a^3*b^7*c^4*d^6 - 5250*a^4*b^6*c^3*d^7 + 9135*a^5*b^5*c^2*d^8 - 6195*a^6*b^4*c*d^9 + 1477*a^7*b^3*d^10)*x^3 - 21*(9*

$$\begin{aligned}
& b^{10}c^8d^2 + 18a^2b^9c^7d^3 + 42a^2b^8c^6d^4 + 126a^3b^7c^5d^5 \\
& + 630a^4b^6c^4d^6 - 5754a^5b^5c^3d^7 + 10647a^6b^4c^2d^8 - 7707 \\
& *a^7b^3c^2d^9 + 1981a^8b^2d^{10})x^2 - 7*(5b^{10}c^9d + 9a^2b^9c^8d^2 \\
& + 18a^2b^8c^7d^3 + 42a^3b^7c^6d^4 + 126a^4b^6c^5d^5 + 630a^5b^5 \\
& c^4d^6 - 6174a^6b^4c^3d^7 + 11907a^7b^3c^2d^8 - 8967a^8b^2c^2 \\
& *d^9 + 2401a^9b^2d^{10})x + 2520*(a^7b^3c^3d^7 - 3a^8b^2c^2d^8 + 3a^9 \\
& b^2c^2d^9 - a^{10}d^{10} + (b^{10}c^3d^7 - 3a^2b^9c^2d^8 + 3a^3b^8c^2d^9 \\
& - a^4b^7c^2d^{10})x^7 + 7*(a^2b^9c^3d^7 - 3a^3b^8c^2d^8 + 3a^4b^7c^2d^9 \\
& - a^5b^6c^2d^{10})x^6 + 21*(a^2b^8c^3d^7 - 3a^3b^7c^2d^8 + 3a^4b^6c^2 \\
& *d^9 - a^5b^5c^2d^{10})x^5 + 35*(a^3b^7c^3d^7 - 3a^4b^6c^2d^8 + 3a^5 \\
& b^5c^2d^9 - a^6b^4c^2d^{10})x^4 + 35*(a^4b^6c^3d^7 - 3a^5b^5c^2d^8 + \\
& 3a^6b^4c^2d^9 - a^7b^3c^2d^{10})x^3 + 21*(a^5b^5c^3d^7 - 3a^6b^4c^2d^8 \\
& + 3a^7b^3c^2d^9 - a^8b^2c^2d^{10})x^2 + 7*(a^6b^4c^3d^7 - 3a^7b^3c^2 \\
& *d^8 + 3a^8b^2c^2d^9 - a^9b^2d^{10})x) * \log(bx + a) / (b^{18}x^7 + 7a^2b^{17} \\
& *x^6 + 21a^2b^{16}x^5 + 35a^3b^{15}x^4 + 35a^4b^{14}x^3 + 21a^5b^{13}x^2 \\
& + 7a^6b^{12}x + a^7b^{11})
\end{aligned}$$

giac [B] time = 1.26, size = 872, normalized size = 3.38

$$\frac{120(b^3c^3d^7 - 3ab^2c^2d^8 + 3a^2bcd^9 - a^3d^{10}) \log(|bx + a|)}{b^{11}} \frac{3b^{10}c^{10} + 5ab^9c^9d + 9a^2b^8c^8d^2 + 18a^3b^7c^7d^3 + 42a^4b^6c^6d^4 + 126a^5b^5c^5d^5 + 630a^6b^4c^4d^6 - 5754a^7b^3c^3d^7 + 10647a^8b^2c^2d^8 - 7707a^9b^2c^2d^9 + 1981a^{10}d^{10}}{b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^8,x, algorithm="giac")

[Out] 120*(b^3c^3d^7 - 3a^2b^2c^2d^8 + 3a^2b^2c^2d^9 - a^3d^10)*log(abs(b*x + a))/b^11 - 1/21*(3b^10c^10 + 5a^2b^9c^9d + 9a^2b^8c^8d^2 + 18a^3b^7c^7d^3 + 42a^4b^6c^6d^4 + 126a^5b^5c^5d^5 + 630a^6b^4c^4d^6 - 6534a^7b^3c^3d^7 + 12987a^8b^2c^2d^8 - 10047a^9b^2c^2d^9 + 2761a^10d^10 + 4410*(b^10c^4d^6 - 4a^2b^9c^3d^7 + 6a^2b^8c^2d^8 - 4a^3b^7c^2d^9 + a^4b^6d^10)*x^6 + 2646*(b^10c^5d^5 + 5a^2b^9c^4d^6 - 30a^2b^8c^3d^7 + 50a^3b^7c^2d^8 - 35a^4b^6c^2d^9 + 9a^5b^5d^10)*x^5 + 1470*(b^10c^6d^4 + 3a^2b^9c^5d^5 + 15a^2b^8c^4d^6 - 110a^3b^7c^3d^7 + 195a^4b^6c^2d^8 - 141a^5b^5c^2d^9 + 37a^6b^4d^10)*x^4 + 210*(3b^10c^7d^3 + 7a^2b^9c^6d^4 + 21a^2b^8c^5d^5 + 105a^3b^7c^4d^6 - 875a^4b^6c^3d^7 + 1617a^5b^5c^2d^8 - 1197a^6b^4c^2d^9 + 319a^7b^3d^10)*x^3 + 63*(3b^10c^8d^2 + 6a^2b^9c^7d^3 + 14a^2b^8c^6d^4 + 42a^3b^7c^5d^5 + 210a^4b^6c^4d^6 - 1918a^5b^5c^3d^7 + 3654a^6b^4c^2d^8 - 2754a^7b^3c^2d^9 + 743a^8b^2d^10)*x^2 + 7*(5b^10c^9d + 9a^2b^9c^8d^2 + 18a^2b^8c^7d^3 + 42a^3b^7c^6d^4 + 126a^4b^6c^5d^5 + 630a^5b^5c^4d^6 - 6174a^6b^4c^3d^7 + 12042a^7b^3c^2d^8 - 9207a^8b^2c^2d^9 + 2509a^9b^2d^10)*x) / ((b*x + a)^7b^11) + 1/3*(b^16d^10*x^3 + 15b^16c^2d^9*x^2 - 12a^2b^15d^10*x^2 + 135b^16c^2d^8*x - 240a^2b^15c^2d^9*x + 108a^2b^14d^10*x)/b^24

maple [B] time = 0.02, size = 1241, normalized size = 4.81

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((dx+c)^{10}/(bx+a)^8, x)$

[Out]
$$\begin{aligned} & -30/b^4*d^3/(bx+a)^4*c^7-210/b^{11}*d^{10}/(bx+a)*a^4-210/b^7*d^6/(bx+a)*c^4 \\ & +5/3/b^{11}*d^{10}/(bx+a)^6*a^9-5/3/b^2*d/(bx+a)^6*c^9+120/b^8*d^7*\ln(bx+a)* \\ & c^3+30/b^{11}*d^{10}/(bx+a)^4*a^7-9/b^{11}*d^{10}/(bx+a)^5*a^8-9/b^3*d^2/(bx+a)^ \\ & 5*c^8+126/b^{11}*d^{10}/(bx+a)^2*a^5-126/b^6*d^5/(bx+a)^2*c^5-120/b^{11}*d^{10}* \\ & \ln(bx+a)*a^3-70/b^5*d^4/(bx+a)^3*c^6-1/7/b^{11}/(bx+a)^7*a^{10}*d^{10}-4*d^{10}/b \\ & ^9*x^2*a+5*d^9/b^8*x^2*c+36*d^{10}/b^{10}*a^2*x+45*d^8/b^8*c^2*x-70/b^{11}*d^{10}/(\\ & bx+a)^3*a^6+360/b^{10}*d^9*\ln(bx+a)*a^2*c-360/b^9*d^8*\ln(bx+a)*a*c^2-210/b \\ & ^{10}*d^9/(bx+a)^4*a^6*c+630/b^9*d^8/(bx+a)^4*a^5*c^2-1050/b^8*d^7/(bx+a)^ \\ & 4*a^4*c^3+1050/b^7*d^6/(bx+a)^4*a^3*c^4-630/b^6*d^5/(bx+a)^4*a^2*c^5+420/ \\ & b^6*d^5/(bx+a)^3*a*c^5+10/7/b^{10}/(bx+a)^7*a^9*c*d^9-45/7/b^9/(bx+a)^7*a^ \\ & 8*c^2*d^8+120/7/b^8/(bx+a)^7*a^7*c^3*d^7-30/b^7/(bx+a)^7*a^6*c^4*d^6+36/b \\ & ^6/(bx+a)^7*a^5*c^5*d^5-30/b^5/(bx+a)^7*a^4*c^6*d^4+120/7/b^4/(bx+a)^7*a^ \\ & ^3*c^7*d^3-45/7/b^3/(bx+a)^7*a^2*c^8*d^2+10/7/b^2/(bx+a)^7*a*c^9*d+72/b^1 \\ & 0*d^9/(bx+a)^5*a^7*c-252/b^9*d^8/(bx+a)^5*a^6*c^2+504/b^8*d^7/(bx+a)^5*a^ \\ & ^5*c^3-630/b^7*d^6/(bx+a)^5*a^4*c^4+504/b^6*d^5/(bx+a)^5*a^3*c^5-252/b^5*d^ \\ & ^4/(bx+a)^5*a^2*c^6+72/b^4*d^3/(bx+a)^5*a*c^7-630/b^{10}*d^9/(bx+a)^2*a^4 \\ & *c+1260/b^9*d^8/(bx+a)^2*a^3*c^2-1260/b^8*d^7/(bx+a)^2*a^2*c^3+630/b^7*d^ \\ & 6/(bx+a)^2*a*c^4-80*d^9/b^9*a*c*x+140/b^5*d^4/(bx+a)^6*a^3*c^6-60/b^4*d^3 \\ & /(bx+a)^6*a^2*c^7+15/b^3*d^2/(bx+a)^6*a*c^8-15/b^{10}*d^9/(bx+a)^6*a^8*c+6 \\ & 0/b^9*d^8/(bx+a)^6*a^7*c^2+420/b^{10}*d^9/(bx+a)^3*a^5*c-1050/b^9*d^8/(bx+a) \\ & ^3*a^4*c^2+1400/b^8*d^7/(bx+a)^3*a^3*c^3-1050/b^7*d^6/(bx+a)^3*a^2*c^4+ \\ & 210/b^7*d^6/(bx+a)^6*a^5*c^4-210/b^6*d^5/(bx+a)^6*a^4*c^5+210/b^5*d^4/(bx \\ & +a)^4*a*c^6+840/b^{10}*d^9/(bx+a)*a^3*c-1260/b^9*d^8/(bx+a)*a^2*c^2+840/b^ \\ & 8*d^7/(bx+a)*a*c^3-140/b^8*d^7/(bx+a)^6*a^6*c^3+1/3*d^{10}/b^8*x^3-1/7/b/(b \\ & *x+a)^7*c^{10} \end{aligned}$$

maxima [B] time = 2.44, size = 934, normalized size = 3.62

$$3b^{10}c^{10} + 5ab^9c^9d + 9a^2b^8c^8d^2 + 18a^3b^7c^7d^3 + 42a^4b^6c^6d^4 + 126a^5b^5c^5d^5 + 630a^6b^4c^4d^6 - 6534a^7b^3c^3d^7 + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((dx+c)^{10}/(bx+a)^8, x, \text{algorithm}="maxima")$

[Out]
$$\begin{aligned} & -1/21*(3*b^{10}*c^{10} + 5*a*b^9*c^9*d + 9*a^2*b^8*c^8*d^2 + 18*a^3*b^7*c^7*d^3 \\ & + 42*a^4*b^6*c^6*d^4 + 126*a^5*b^5*c^5*d^5 + 630*a^6*b^4*c^4*d^6 - 6534*a^7 \end{aligned}$$

```

7*b^3*c^3*d^7 + 12987*a^8*b^2*c^2*d^8 - 10047*a^9*b*c*d^9 + 2761*a^10*d^10
+ 4410*(b^10*c^4*d^6 - 4*a*b^9*c^3*d^7 + 6*a^2*b^8*c^2*d^8 - 4*a^3*b^7*c*d^
9 + a^4*b^6*d^10)*x^6 + 2646*(b^10*c^5*d^5 + 5*a*b^9*c^4*d^6 - 30*a^2*b^8*c
^3*d^7 + 50*a^3*b^7*c^2*d^8 - 35*a^4*b^6*c*d^9 + 9*a^5*b^5*d^10)*x^5 + 1470
*(b^10*c^6*d^4 + 3*a*b^9*c^5*d^5 + 15*a^2*b^8*c^4*d^6 - 110*a^3*b^7*c^3*d^7
+ 195*a^4*b^6*c^2*d^8 - 141*a^5*b^5*c*d^9 + 37*a^6*b^4*d^10)*x^4 + 210*(3*
b^10*c^7*d^3 + 7*a*b^9*c^6*d^4 + 21*a^2*b^8*c^5*d^5 + 105*a^3*b^7*c^4*d^6 -
875*a^4*b^6*c^3*d^7 + 1617*a^5*b^5*c^2*d^8 - 1197*a^6*b^4*c*d^9 + 319*a^7*
b^3*d^10)*x^3 + 63*(3*b^10*c^8*d^2 + 6*a*b^9*c^7*d^3 + 14*a^2*b^8*c^6*d^4 +
42*a^3*b^7*c^5*d^5 + 210*a^4*b^6*c^4*d^6 - 1918*a^5*b^5*c^3*d^7 + 3654*a^6
*b^4*c^2*d^8 - 2754*a^7*b^3*c*d^9 + 743*a^8*b^2*d^10)*x^2 + 7*(5*b^10*c^9*d
+ 9*a*b^9*c^8*d^2 + 18*a^2*b^8*c^7*d^3 + 42*a^3*b^7*c^6*d^4 + 126*a^4*b^6*
c^5*d^5 + 630*a^5*b^5*c^4*d^6 - 6174*a^6*b^4*c^3*d^7 + 12042*a^7*b^3*c^2*d^
8 - 9207*a^8*b^2*c*d^9 + 2509*a^9*b*d^10)*x)/(b^18*x^7 + 7*a*b^17*x^6 + 21*
a^2*b^16*x^5 + 35*a^3*b^15*x^4 + 35*a^4*b^14*x^3 + 21*a^5*b^13*x^2 + 7*a^6*
b^12*x + a^7*b^11) + 1/3*(b^2*d^10*x^3 + 3*(5*b^2*c*d^9 - 4*a*b*d^10)*x^2 +
3*(45*b^2*c^2*d^8 - 80*a*b*c*d^9 + 36*a^2*d^10)*x)/b^10 + 120*(b^3*c^3*d^7
- 3*a*b^2*c^2*d^8 + 3*a^2*b*c*d^9 - a^3*d^10)*log(b*x + a)/b^11

```

mupad [B] time = 0.43, size = 950, normalized size = 3.68

$$x \left(\frac{8a \left(\frac{8ad^{10}}{b^9} - \frac{10cd^9}{b^8} \right)}{b} - \frac{28a^2d^{10}}{b^{10}} + \frac{45c^2d^8}{b^8} \right) \frac{x^4 (2590a^6b^3d^{10} - 9870a^5b^4cd^9 + 13650a^4b^5c^2d^8 - 7700a^3b^6c^3d^7 - 9870a^5b^4cd^9 + 1050a^2b^7c^4d^6 - 7700a^3b^6c^3d^7 + 13650a^4b^5c^2d^8) + x^6(210a^4b^5d^{10} + 210b^9c^4d^6 - 840a*b^8c^3d^7 - 840a^3b^6c*d^9 + 1260a^2b^7c^2d^8) + (2761a^{10}d^{10} + 3b^{10}c^{10} + 9a^2b^8c^8d^2 + 18a^3b^7c^7d^3 + 42a^4b^6c^6d^4 + 126a^5b^5c^5d^5 + 630a^6b^4c^4d^6 - 6534a^7b^3c^3d^7 + 12987a^8b^2c^2d^8 + 5a*b^9c^9d - 10047a^9b*c*d^9)/(21*b) + x((2509a^9d^{10})/3 + (5*b^9*c^9*d)/3 + 3*a*b^8*c^8*d^2 + 6*a^2*b^7*c^7*d^3 + 14*a^3*b^6*c^6*d^4 + 42*a^4*b^5*c^5*d^5 + 210*a^5*b^4*c^4*d^6 - 2058*a^6*b^3*c^3*d^7 + 4014*a^7*b^2*c^2*d^8 - 3069*a^8*b*c*d^9) + x^3(3190*a^7*b^2*d^{10} + 30*b^9*c^7*d^3 + 70*a*b^8*c^6*d^4 - 11970*a^6*b^3*c*d^9 + 210*a^2*b^7*c^5*d^5 + 1050*a^3*b^6*c^4*d^6 - 8750*a^4*b^5*c^3*d^7 + 16170*a^5*b^4*c^2*d^8) + x^2(2229*a^8*b*d^{10} + 9*b^9*c^8*d^2 + 18*a*b^8*c^7*d^3 - 8262*a^7*b^2*c*d^9 + 42*a^2*b^7*c^6*d^4 + 126*a^3*b^6*c^5*d^5 + 630*a^4*b^5*c^4*d^6 - 5754*a^5*b^4*c^3*d^7 + 10962*a^6*b^3*c^2*d^8) + x^5(1134*a^5*b^4*d^{10} + 126*b^9*c^5*d^5 + 63$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^8,x)

[Out] $x \left(\frac{8a \left(\frac{8ad^{10}}{b^9} - \frac{10cd^9}{b^8} \right)}{b} - \frac{28a^2d^{10}}{b^{10}} + \frac{45c^2d^8}{b^8} \right) \frac{x^4 (2590a^6b^3d^{10} - 9870a^5b^4cd^9 + 13650a^4b^5c^2d^8 - 7700a^3b^6c^3d^7 - 9870a^5b^4cd^9 + 1050a^2b^7c^4d^6 - 7700a^3b^6c^3d^7 + 13650a^4b^5c^2d^8) + x^6(210a^4b^5d^{10} + 210b^9c^4d^6 - 840a*b^8c^3d^7 - 840a^3b^6c*d^9 + 1260a^2b^7c^2d^8) + (2761a^{10}d^{10} + 3b^{10}c^{10} + 9a^2b^8c^8d^2 + 18a^3b^7c^7d^3 + 42a^4b^6c^6d^4 + 126a^5b^5c^5d^5 + 630a^6b^4c^4d^6 - 6534a^7b^3c^3d^7 + 12987a^8b^2c^2d^8 + 5a*b^9c^9d - 10047a^9b*c*d^9)/(21*b) + x((2509a^9d^{10})/3 + (5*b^9*c^9*d)/3 + 3*a*b^8*c^8*d^2 + 6*a^2*b^7*c^7*d^3 + 14*a^3*b^6*c^6*d^4 + 42*a^4*b^5*c^5*d^5 + 210*a^5*b^4*c^4*d^6 - 2058*a^6*b^3*c^3*d^7 + 4014*a^7*b^2*c^2*d^8 - 3069*a^8*b*c*d^9) + x^3(3190*a^7*b^2*d^{10} + 30*b^9*c^7*d^3 + 70*a*b^8*c^6*d^4 - 11970*a^6*b^3*c*d^9 + 210*a^2*b^7*c^5*d^5 + 1050*a^3*b^6*c^4*d^6 - 8750*a^4*b^5*c^3*d^7 + 16170*a^5*b^4*c^2*d^8) + x^2(2229*a^8*b*d^{10} + 9*b^9*c^8*d^2 + 18*a*b^8*c^7*d^3 - 8262*a^7*b^2*c*d^9 + 42*a^2*b^7*c^6*d^4 + 126*a^3*b^6*c^5*d^5 + 630*a^4*b^5*c^4*d^6 - 5754*a^5*b^4*c^3*d^7 + 10962*a^6*b^3*c^2*d^8) + x^5(1134*a^5*b^4*d^{10} + 126*b^9*c^5*d^5 + 63$

$$\frac{0*a*b^8*c^4*d^6 - 4410*a^4*b^5*c*d^9 - 3780*a^2*b^7*c^3*d^7 + 6300*a^3*b^6*c^2*d^8)}{(a^7*b^{10} + b^{17}*x^7 + 7*a^6*b^{11}*x + 7*a*b^{16}*x^6 + 21*a^5*b^{12}*x^2 + 35*a^4*b^{13}*x^3 + 35*a^3*b^{14}*x^4 + 21*a^2*b^{15}*x^5) - x^2*((4*a*d^{10})/b^9 - (5*c*d^9)/b^8) - (\log(a + b*x)*(120*a^3*d^{10} - 120*b^3*c^3*d^7 + 360*a*b^2*c^2*d^8 - 360*a^2*b*c*d^9))/b^{11} + (d^{10}*x^3)/(3*b^8)}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**8,x)

[Out] Timed out

$$3.1320 \quad \int \frac{(c+dx)^{10}}{(a+bx)^9} dx$$

Optimal. Leaf size=258

$$\frac{45d^8(bc-ad)^2 \log(a+bx)}{b^{11}} - \frac{120d^7(bc-ad)^3}{b^{11}(a+bx)} - \frac{105d^6(bc-ad)^4}{b^{11}(a+bx)^2} - \frac{84d^5(bc-ad)^5}{b^{11}(a+bx)^3} - \frac{105d^4(bc-ad)^6}{2b^{11}(a+bx)^4} - \frac{24d^3(bc-ad)^7}{b^{11}(a+bx)^5}$$

[Out] $d^9*(-9*a*d+10*b*c)*x/b^{10}+1/2*d^{10}*x^2/b^9-1/8*(-a*d+b*c)^{10}/b^{11}/(b*x+a)^8-10/7*d*(-a*d+b*c)^9/b^{11}/(b*x+a)^7-15/2*d^2*(-a*d+b*c)^8/b^{11}/(b*x+a)^6-24*d^3*(-a*d+b*c)^7/b^{11}/(b*x+a)^5-105/2*d^4*(-a*d+b*c)^6/b^{11}/(b*x+a)^4-84*d^5*(-a*d+b*c)^5/b^{11}/(b*x+a)^3-105*d^6*(-a*d+b*c)^4/b^{11}/(b*x+a)^2-120*d^7*(-a*d+b*c)^3/b^{11}/(b*x+a)+45*d^8*(-a*d+b*c)^2*\ln(b*x+a)/b^{11}$

Rubi [A] time = 0.34, antiderivative size = 258, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{d^9x(10bc-9ad)}{b^{10}} - \frac{120d^7(bc-ad)^3}{b^{11}(a+bx)} - \frac{105d^6(bc-ad)^4}{b^{11}(a+bx)^2} - \frac{84d^5(bc-ad)^5}{b^{11}(a+bx)^3} - \frac{105d^4(bc-ad)^6}{2b^{11}(a+bx)^4} - \frac{24d^3(bc-ad)^7}{b^{11}(a+bx)^5} - \frac{15d^2(bc-ad)^8}{2b^{11}(a+bx)^6}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^9, x]

[Out] $(d^9*(10*b*c - 9*a*d)*x)/b^{10} + (d^{10}*x^2)/(2*b^9) - (b*c - a*d)^{10}/(8*b^{11}*(a + b*x)^8) - (10*d*(b*c - a*d)^9)/(7*b^{11}*(a + b*x)^7) - (15*d^2*(b*c - a*d)^8)/(2*b^{11}*(a + b*x)^6) - (24*d^3*(b*c - a*d)^7)/(b^{11}*(a + b*x)^5) - (105*d^4*(b*c - a*d)^6)/(2*b^{11}*(a + b*x)^4) - (84*d^5*(b*c - a*d)^5)/(b^{11}*(a + b*x)^3) - (105*d^6*(b*c - a*d)^4)/(b^{11}*(a + b*x)^2) - (120*d^7*(b*c - a*d)^3)/(b^{11}*(a + b*x)) + (45*d^8*(b*c - a*d)^2*\text{Log}[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c + dx)^{10}}{(a + bx)^9} dx = \int \left(\frac{d^9(10bc - 9ad)}{b^{10}} + \frac{d^{10}x}{b^9} + \frac{(bc - ad)^{10}}{b^{10}(a + bx)^9} + \frac{10d(bc - ad)^9}{b^{10}(a + bx)^8} + \frac{45d^2(bc - ad)^8}{b^{10}(a + bx)^7} + \frac{120d^3(bc - ad)^7}{b^{10}(a + bx)^6} + \frac{315d^4(bc - ad)^6}{b^{10}(a + bx)^5} + \frac{630d^5(bc - ad)^5}{b^{10}(a + bx)^4} + \frac{945d^6(bc - ad)^4}{b^{10}(a + bx)^3} + \frac{1260d^7(bc - ad)^3}{b^{10}(a + bx)^2} + \frac{1260d^8(bc - ad)^2}{b^{10}(a + bx)} + \frac{945d^9(bc - ad)}{b^{10}} + \frac{630d^{10}}{b^{10}} \right)$$

Mathematica [B] time = 0.32, size = 712, normalized size = 2.76

$$3601a^{10}d^{10} + 2a^9bd^9(13144dx - 4609c) + a^8b^2d^8(6849c^2 - 68704cdx + 81928d^2x^2) + 8a^7b^3d^7(-105c^3 + 6534cdx - 27538c^2d^2x^2 + 17542d^3x^3) + 14a^6b^4d^6(-15c^4 - 480c^3dx + 12348c^2d^2x^2 - 28112cd^3x^3 + 10010d^4x^4) - 28a^5b^5d^5(3c^5 + 60c^4dx + 840c^3d^2x^2 - 11508c^2d^3x^3 + 15050cd^4x^4 - 2744d^5x^5) - 14a^4b^6d^4(3c^6 + 48c^5dx + 420c^4d^2x^2 + 3360c^3d^3x^3 - 26250c^2d^4x^4 + 19040cd^5x^5 - 1064d^6x^6) - 8a^3b^7d^3(3c^7 + 42c^6dx + 294c^5d^2x^2 + 1470c^4d^3x^3 + 7350c^3d^4x^4 - 32340c^2d^5x^5 + 10780cd^6x^6 + 728d^7x^7) - a^2b^8d^2(15c^8 + 192c^7dx + 1176c^6d^2x^2 + 4704c^5d^3x^3 + 14700c^4d^4x^4 + 47040c^3d^5x^5 - 105840c^2d^6x^6 + 4480cd^7x^7 + 3248d^8x^8) - 2ab^9d(5c^9 + 60c^8dx + 336c^7d^2x^2 + 1176c^6d^3x^3 + 2940c^5d^4x^4 + 5880c^4d^5x^5 + 11760c^3d^6x^6 - 10080c^2d^7x^7 - 2240cd^8x^8 + 140d^9x^9) - b^{10}(7c^{10} + 80c^9dx + 420c^8d^2x^2 + 1344c^7d^3x^3 + 2940c^6d^4x^4 + 4704c^5d^5x^5 + 5880c^4d^6x^6 + 6720c^3d^7x^7 - 560cd^9x^9 - 28d^{10}x^{10}) + 2520d^8(b^9c - ab^8d)^2(a + b^9x)^8 \log[a + b^9x] / (56b^{11}(a + b^9x)^8)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^9,x]

[Out] (3601*a^10*d^10 + 2*a^9*b*d^9*(-4609*c + 13144*d*x) + a^8*b^2*d^8*(6849*c^2 - 68704*c*d*x + 81928*d^2*x^2) + 8*a^7*b^3*d^7*(-105*c^3 + 6534*c^2*d*x - 27538*c*d^2*x^2 + 17542*d^3*x^3) + 14*a^6*b^4*d^6*(-15*c^4 - 480*c^3*d*x + 12348*c^2*d^2*x^2 - 28112*c*d^3*x^3 + 10010*d^4*x^4) - 28*a^5*b^5*d^5*(3*c^5 + 60*c^4*d*x + 840*c^3*d^2*x^2 - 11508*c^2*d^3*x^3 + 15050*c*d^4*x^4 - 2744*d^5*x^5) - 14*a^4*b^6*d^4*(3*c^6 + 48*c^5*d*x + 420*c^4*d^2*x^2 + 3360*c^3*d^3*x^3 - 26250*c^2*d^4*x^4 + 19040*c*d^5*x^5 - 1064*d^6*x^6) - 8*a^3*b^7*d^3*(3*c^7 + 42*c^6*d*x + 294*c^5*d^2*x^2 + 1470*c^4*d^3*x^3 + 7350*c^3*d^4*x^4 - 32340*c^2*d^5*x^5 + 10780*c*d^6*x^6 + 728*d^7*x^7) - a^2*b^8*d^2*(15*c^8 + 192*c^7*d*x + 1176*c^6*d^2*x^2 + 4704*c^5*d^3*x^3 + 14700*c^4*d^4*x^4 + 47040*c^3*d^5*x^5 - 105840*c^2*d^6*x^6 + 4480*c*d^7*x^7 + 3248*d^8*x^8) - 2*a*b^9*d*(5*c^9 + 60*c^8*d*x + 336*c^7*d^2*x^2 + 1176*c^6*d^3*x^3 + 2940*c^5*d^4*x^4 + 5880*c^4*d^5*x^5 + 11760*c^3*d^6*x^6 - 10080*c^2*d^7*x^7 - 2240*c*d^8*x^8 + 140*d^9*x^9) - b^10*(7*c^10 + 80*c^9*d*x + 420*c^8*d^2*x^2 + 1344*c^7*d^3*x^3 + 2940*c^6*d^4*x^4 + 4704*c^5*d^5*x^5 + 5880*c^4*d^6*x^6 + 6720*c^3*d^7*x^7 - 560*c*d^9*x^9 - 28*d^10*x^10) + 2520*d^8*(b^9*c - a*b^8*d)^2*(a + b^9*x)^8*Log[a + b^9*x])/(56*b^11*(a + b^9*x)^8)

fricas [B] time = 0.45, size = 1296, normalized size = 5.02

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^9,x, algorithm="fricas")

[Out] 1/56*(28*b^10*d^10*x^10 - 7*b^10*c^10 - 10*a*b^9*c^9*d - 15*a^2*b^8*c^8*d^2 - 24*a^3*b^7*c^7*d^3 - 42*a^4*b^6*c^6*d^4 - 84*a^5*b^5*c^5*d^5 - 210*a^6*b

$$\begin{aligned}
& ^4c^4d^6 - 840a^7b^3c^3d^7 + 6849a^8b^2c^2d^8 - 9218a^9b^1c^1d^9 \\
& + 3601a^{10}d^{10} + 280(2b^{10}c^1d^9 - ab^9d^{10})x^9 + 112(40a^1b^9c^1d^9 - 29a^2b^8d^{10})x^8 - 448(15b^{10}c^3d^7 - 45a^1b^9c^2d^8 + 10a^2 \\
& *b^8c^1d^9 + 13a^3b^7d^{10})x^7 - 392(15b^{10}c^4d^6 + 60a^1b^9c^3d^7 - 270a^2b^8c^2d^8 + 220a^3b^7c^1d^9 - 38a^4b^6d^{10})x^6 - 784(6 \\
& b^{10}c^5d^5 + 15a^1b^9c^4d^6 + 60a^2b^8c^3d^7 - 330a^3b^7c^2d^8 + 340a^4b^6c^1d^9 - 98a^5b^5d^{10})x^5 - 980(3b^{10}c^6d^4 + 6a^1b^9c^5d^5 + 15a^2b^8c^4d^6 + 60a^3b^7c^3d^7 - 375a^4b^6c^2d^8 + 4 \\
& 30a^5b^5c^1d^9 - 143a^6b^4d^{10})x^4 - 112(12b^{10}c^7d^3 + 21a^1b^9c^6d^4 + 42a^2b^8c^5d^5 + 105a^3b^7c^4d^6 + 420a^4b^6c^3d^7 - 2877a^5b^5c^2d^8 + 3514a^6b^4c^1d^9 - 1253a^7b^3d^{10})x^3 - 28(15 \\
& b^{10}c^8d^2 + 24a^1b^9c^7d^3 + 42a^2b^8c^6d^4 + 84a^3b^7c^5d^5 + 210a^4b^6c^4d^6 + 840a^5b^5c^3d^7 - 6174a^6b^4c^2d^8 + 7868a^7b^3c^1d^9 - 2926a^8b^2d^{10})x^2 - 8(10b^{10}c^9d + 15a^1b^9c^8d^2 \\
& + 24a^2b^8c^7d^3 + 42a^3b^7c^6d^4 + 84a^4b^6c^5d^5 + 210a^5b^5c^4d^6 + 840a^6b^4c^3d^7 - 6534a^7b^3c^2d^8 + 8588a^8b^2c^1d^9 - 3286a^9b^1d^{10})x + 2520(a^8b^2c^2d^8 - 2a^9b^1c^1d^9 + a^{10}d^{10} \\
& + (b^{10}c^2d^8 - 2a^1b^9c^1d^9 + a^2b^8d^{10})x^8 + 8(a^1b^9c^2d^8 - 2a^2b^8c^1d^9 + a^3b^7d^{10})x^7 + 28(a^2b^8c^2d^8 - 2a^3b^7c^1d^9 + a^4b^6d^{10})x^6 + 56(a^3b^7c^2d^8 - 2a^4b^6c^1d^9 + a^5b^5d^{10}) \\
& x^5 + 70(a^4b^6c^2d^8 - 2a^5b^5c^1d^9 + a^6b^4d^{10})x^4 + 56(a^5b^5c^2d^8 - 2a^6b^4c^1d^9 + a^7b^3d^{10})x^3 + 28(a^6b^4c^2d^8 - 2a^7b^3c^1d^9 + a^8b^2d^{10})x^2 + 8(a^7b^3c^2d^8 - 2a^8b^2c^1d^9 + \\
& a^9b^1d^{10})x) \log(bx + a) / (b^{19}x^8 + 8a^1b^{18}x^7 + 28a^2b^{17}x^6 + 56a^3b^{16}x^5 + 70a^4b^{15}x^4 + 56a^5b^{14}x^3 + 28a^6b^{13}x^2 + 8a^7b^{12}x + a^8b^{11})
\end{aligned}$$

giac [B] time = 1.29, size = 871, normalized size = 3.38

$$\frac{45(b^2c^2d^8 - 2abcd^9 + a^2d^{10}) \log(|bx + a|)}{b^{11}} + \frac{b^9d^{10}x^2 + 20b^9cd^9x - 18ab^8d^{10}x - 7b^{10}c^{10} + 10ab^9c^9d + 15a^2b^8c^8d}{2b^{18}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^9,x, algorithm="giac")

[Out] 45*(b^2c^2d^8 - 2a^1b^9c^1d^9 + a^2d^{10})*log(abs(b*x + a))/b^11 + 1/2*(b^9*d^{10}*x^2 + 20*b^9*c^1*d^9*x - 18*a^1*b^8*d^{10}*x)/b^18 - 1/56*(7*b^{10}*c^{10} + 10*a^1*b^9*c^9*d + 15*a^2*b^8*c^8*d^2 + 24*a^3*b^7*c^7*d^3 + 42*a^4*b^6*c^6*d^4 + 84*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 + 840*a^7*b^3*c^3*d^7 - 6849*a^8*b^2*c^2*d^8 + 9218*a^9*b^1*c^1*d^9 - 3601*a^{10}*d^{10} + 6720*(b^{10}*c^3*d^7 - 3*a^1*b^9*c^2*d^8 + 3*a^2*b^8*c^1*d^9 - a^3*b^7*d^{10})x^7 + 5880*(b^{10}*c^4*d^6 + 4*a^1*b^9*c^3*d^7 - 18*a^2*b^8*c^2*d^8 + 20*a^3*b^7*c^1*d^9 - 7*a^4*b^6*d^{10})x^6 + 2352*(2*b^{10}*c^5*d^5 + 5*a^1*b^9*c^4*d^6 + 20*a^2*b^8*c^3*d^7 - 110*a^3*b^7*c^2*d^8 + 130*a^4*b^6*c^1*d^9 - 47*a^5*b^5*d^{10})x^5 + 2940*(b^{10}*c^6*d^4

$$\begin{aligned}
& + 2*a*b^9*c^5*d^5 + 5*a^2*b^8*c^4*d^6 + 20*a^3*b^7*c^3*d^7 - 125*a^4*b^6*c^2*d^8 + 154*a^5*b^5*c*d^9 - 57*a^6*b^4*d^{10})*x^4 + 336*(4*b^{10}*c^7*d^3 + 7 \\
& *a*b^9*c^6*d^4 + 14*a^2*b^8*c^5*d^5 + 35*a^3*b^7*c^4*d^6 + 140*a^4*b^6*c^3*d^7 - 959*a^5*b^5*c^2*d^8 + 1218*a^6*b^4*c*d^9 - 459*a^7*b^3*d^{10})*x^3 + 84 \\
& *(5*b^{10}*c^8*d^2 + 8*a*b^9*c^7*d^3 + 14*a^2*b^8*c^6*d^4 + 28*a^3*b^7*c^5*d^5 + 70*a^4*b^6*c^4*d^6 + 280*a^5*b^5*c^3*d^7 - 2058*a^6*b^4*c^2*d^8 + 2676* \\
& a^7*b^3*c*d^9 - 1023*a^8*b^2*d^{10})*x^2 + 8*(10*b^{10}*c^9*d + 15*a*b^9*c^8*d^2 + 24*a^2*b^8*c^7*d^3 + 42*a^3*b^7*c^6*d^4 + 84*a^4*b^6*c^5*d^5 + 210*a^5* \\
& b^5*c^4*d^6 + 840*a^6*b^4*c^3*d^7 - 6534*a^7*b^3*c^2*d^8 + 8658*a^8*b^2*c*d^9 - 3349*a^9*b*d^{10})*x)/((b*x + a)^8*b^{11})
\end{aligned}$$

maple [B] time = 0.02, size = 1256, normalized size = 4.87

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^9,x)

[Out] $\frac{1}{2}d^{10}x^2/b^9-9d^{10}/b^{10}a*x+10d^9/b^9*x*c-15/2/b^{11}d^{10}/(b*x+a)^6*a^8-15/2/b^3*d^2/(b*x+a)^6*c^8-105/b^7*d^6/(b*x+a)^2*c^4+45/b^{11}d^{10}*\ln(b*x+a)*a^2+45/b^9*d^8*\ln(b*x+a)*c^2-105/2/b^{11}d^{10}/(b*x+a)^4*a^6-105/2/b^5*d^4/(b*x+a)^4*c^6+120/b^{11}d^{10}/(b*x+a)*a^3-120/b^8*d^7/(b*x+a)*c^3-1/8/b^{11}/(b*x+a)^8*a^{10}d^{10}+84/b^{11}d^{10}/(b*x+a)^3*a^5-84/b^6*d^5/(b*x+a)^3*c^5+10/7/b^{11}d^{10}/(b*x+a)^7*a^9-10/7/b^2*d/(b*x+a)^7*c^9+24/b^{11}d^{10}/(b*x+a)^5*a^7-24/b^4*d^3/(b*x+a)^5*c^7-105/b^{11}d^{10}/(b*x+a)^2*a^4-1/8/b/(b*x+a)^8*c^{10}-360/7/b^4*d^3/(b*x+a)^7*a^2*c^7+90/7/b^3*d^2/(b*x+a)^7*a*c^8-168/b^{10}d^9/(b*x+a)^5*a^6*c+504/b^9*d^8/(b*x+a)^5*a^5*c^2+180/b^7*d^6/(b*x+a)^7*a^5*c^4-180/b^6*d^5/(b*x+a)^7*a^4*c^5+120/b^5*d^4/(b*x+a)^7*a^3*c^6-840/b^8*d^7/(b*x+a)^5*a^4*c^3+840/b^7*d^6/(b*x+a)^5*a^3*c^4-504/b^6*d^5/(b*x+a)^5*a^2*c^5-210/b^9*d^8/(b*x+a)^6*a^6*c^2+420/b^8*d^7/(b*x+a)^6*a^5*c^3-525/b^7*d^6/(b*x+a)^6*a^4*c^4+420/b^6*d^5/(b*x+a)^6*a^3*c^5-210/b^5*d^4/(b*x+a)^6*a^2*c^6+60/b^4*d^3/(b*x+a)^6*a*c^7+168/b^5*d^4/(b*x+a)^5*a*c^6+315/b^{10}d^9/(b*x+a)^4*a^5*c-1575/2/b^9*d^8/(b*x+a)^4*a^4*c^2+1050/b^8*d^7/(b*x+a)^4*a^3*c^3-1575/2/b^7*d^6/(b*x+a)^4*a^2*c^4+315/b^6*d^5/(b*x+a)^4*a*c^5-360/b^{10}d^9/(b*x+a)*a^2*c+360/b^9*d^8/(b*x+a)*a*c^2+60/b^{10}d^9/(b*x+a)^6*a^7*c+420/b^{10}d^9/(b*x+a)^2*a^3*c-630/b^9*d^8/(b*x+a)^2*a^2*c^2+420/b^8*d^7/(b*x+a)^2*a*c^3-90/b^{10}d^9*\ln(b*x+a)*a*c+5/4/b^{10}/(b*x+a)^8*a^9*c*d^9-45/8/b^9/(b*x+a)^8*a^8*c^2*d^8+15/b^8/(b*x+a)^8*a^7*c^3*d^7-105/4/b^7/(b*x+a)^8*a^6*c^4*d^6+63/2/b^6/(b*x+a)^8*a^5*c^5*d^5-105/4/b^5/(b*x+a)^8*a^4*c^6*d^4+15/b^4/(b*x+a)^8*a^3*c^7*d^3-45/8/b^3/(b*x+a)^8*a^2*c^8*d^2+5/4/b^2/(b*x+a)^8*a*c^9*d-420/b^{10}d^9/(b*x+a)^3*a^4*c+840/b^9*d^8/(b*x+a)^3*a^3*c^2-840/b^8*d^7/(b*x+a)^3*a^2*c^3+420/b^7*d^6/(b*x+a)^3*a*c^4-90/7/b^{10}d^9/(b*x+a)^7*a^8*c+360/7/b^9*d^8/(b*x+a)^7*a^7*c^2-120/b^8*d^7/(b*x+a)^7*a^6*c^3$

maxima [B] time = 2.58, size = 945, normalized size = 3.66

$$7b^{10}c^{10} + 10ab^9c^9d + 15a^2b^8c^8d^2 + 24a^3b^7c^7d^3 + 42a^4b^6c^6d^4 + 84a^5b^5c^5d^5 + 210a^6b^4c^4d^6 + 840a^7b^3c^3d^7 - \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^9,x, algorithm="maxima")

[Out]
$$\frac{-1/56*(7*b^{10}*c^{10} + 10*a*b^9*c^9*d + 15*a^2*b^8*c^8*d^2 + 24*a^3*b^7*c^7*d^3 + 42*a^4*b^6*c^6*d^4 + 84*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 + 840*a^7*b^3*c^3*d^7 - 6849*a^8*b^2*c^2*d^8 + 9218*a^9*b*c*d^9 - 3601*a^{10}*d^{10} + 6720*(b^{10}*c^3*d^7 - 3*a*b^9*c^2*d^8 + 3*a^2*b^8*c*d^9 - a^3*b^7*d^{10})*x^7 + 5880*(b^{10}*c^4*d^6 + 4*a*b^9*c^3*d^7 - 18*a^2*b^8*c^2*d^8 + 20*a^3*b^7*c*d^9 - 7*a^4*b^6*d^{10})*x^6 + 2352*(2*b^{10}*c^5*d^5 + 5*a*b^9*c^4*d^6 + 20*a^2*b^8*c^3*d^7 - 110*a^3*b^7*c^2*d^8 + 130*a^4*b^6*c*d^9 - 47*a^5*b^5*d^{10})*x^5 + 2940*(b^{10}*c^6*d^4 + 2*a*b^9*c^5*d^5 + 5*a^2*b^8*c^4*d^6 + 20*a^3*b^7*c^3*d^7 - 125*a^4*b^6*c^2*d^8 + 154*a^5*b^5*c*d^9 - 57*a^6*b^4*d^{10})*x^4 + 336*(4*b^{10}*c^7*d^3 + 7*a*b^9*c^6*d^4 + 14*a^2*b^8*c^5*d^5 + 35*a^3*b^7*c^4*d^6 + 140*a^4*b^6*c^3*d^7 - 959*a^5*b^5*c^2*d^8 + 1218*a^6*b^4*c*d^9 - 459*a^7*b^3*d^{10})*x^3 + 84*(5*b^{10}*c^8*d^2 + 8*a*b^9*c^7*d^3 + 14*a^2*b^8*c^6*d^4 + 28*a^3*b^7*c^5*d^5 + 70*a^4*b^6*c^4*d^6 + 280*a^5*b^5*c^3*d^7 - 2058*a^6*b^4*c^2*d^8 + 2676*a^7*b^3*c*d^9 - 1023*a^8*b^2*d^{10})*x^2 + 8*(10*b^{10}*c^9*d + 15*a*b^9*c^8*d^2 + 24*a^2*b^8*c^7*d^3 + 42*a^3*b^7*c^6*d^4 + 84*a^4*b^6*c^5*d^5 + 210*a^5*b^5*c^4*d^6 + 840*a^6*b^4*c^3*d^7 - 6534*a^7*b^3*c^2*d^8 + 8658*a^8*b^2*c*d^9 - 3349*a^9*b*d^{10})*x)/(b^{19}*x^8 + 8*a*b^{18}*x^7 + 28*a^2*b^{17}*x^6 + 56*a^3*b^{16}*x^5 + 70*a^4*b^{15}*x^4 + 56*a^5*b^{14}*x^3 + 28*a^6*b^{13}*x^2 + 8*a^7*b^{12}*x + a^8*b^{11}) + 1/2*(b*d^{10}*x^2 + 2*(10*b*c*d^9 - 9*a*d^{10})*x)/b^{10} + 45*(b^2*c^2*d^8 - 2*a*b*c*d^9 + a^2*d^{10})*log(b*x + a)/b^{11}$$

mupad [B] time = 0.26, size = 946, normalized size = 3.67

$$\frac{\ln(a + bx) \left(45 a^2 d^{10} - 90 a b c d^9 + 45 b^2 c^2 d^8 \right)}{b^{11}} - \frac{x^4 \left(-\frac{5985 a^6 b^3 d^{10}}{2} + 8085 a^5 b^4 c d^9 - \frac{13125 a^4 b^5 c^2 d^8}{2} + 1050 a^3 b^6 c^3 d^7 - \dots \right)}{b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^9,x)

[Out]
$$\frac{(\log(a + b*x)*(45*a^2*d^{10} + 45*b^2*c^2*d^8 - 90*a*b*c*d^9))/b^{11} - (x^4*((105*b^9*c^6*d^4)/2 - (5985*a^6*b^3*d^{10})/2 + 105*a*b^8*c^5*d^5 + 8085*a^5*b^4*c*d^9 + (525*a^2*b^7*c^4*d^6)/2 + 1050*a^3*b^6*c^3*d^7 - (13125*a^4*b^5*c^2*d^8)/2) + x^6*(105*b^9*c^4*d^6 - 735*a^4*b^5*d^{10} + 420*a*b^8*c^3*d^7 + \dots)}{b^{11}}$$

$$\begin{aligned}
& 2100*a^3*b^6*c*d^9 - 1890*a^2*b^7*c^2*d^8) + (7*b^{10}*c^{10} - 3601*a^{10}*d^{10} \\
& + 15*a^2*b^8*c^8*d^2 + 24*a^3*b^7*c^7*d^3 + 42*a^4*b^6*c^6*d^4 + 84*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 + 840*a^7*b^3*c^3*d^7 - 6849*a^8*b^2*c^2*d^8 \\
& + 10*a*b^9*c^9*d + 9218*a^9*b*c*d^9)/(56*b) + x*((10*b^9*c^9*d)/7 - (3349*a^9*d^{10})/7 + (15*a*b^8*c^8*d^2)/7 + (24*a^2*b^7*c^7*d^3)/7 + 6*a^3*b^6*c^6*d^4 + 12*a^4*b^5*c^5*d^5 + 30*a^5*b^4*c^4*d^6 + 120*a^6*b^3*c^3*d^7 - (65 \\
& 34*a^7*b^2*c^2*d^8)/7 + (8658*a^8*b*c*d^9)/7) + x^3*(24*b^9*c^7*d^3 - 2754*a^7*b^2*d^{10} + 42*a*b^8*c^6*d^4 + 7308*a^6*b^3*c*d^9 + 84*a^2*b^7*c^5*d^5 + 210*a^3*b^6*c^4*d^6 + 840*a^4*b^5*c^3*d^7 - 5754*a^5*b^4*c^2*d^8) + x^2*((\\
& 15*b^9*c^8*d^2)/2 - (3069*a^8*b*d^{10})/2 + 12*a*b^8*c^7*d^3 + 4014*a^7*b^2*c*d^9 + 21*a^2*b^7*c^6*d^4 + 42*a^3*b^6*c^5*d^5 + 105*a^4*b^5*c^4*d^6 + 420*a^5*b^4*c^3*d^7 - 3087*a^6*b^3*c^2*d^8) + x^5*(84*b^9*c^5*d^5 - 1974*a^5*b^4*d^{10} + 210*a*b^8*c^4*d^6 + 5460*a^4*b^5*c*d^9 + 840*a^2*b^7*c^3*d^7 - 462 \\
& 0*a^3*b^6*c^2*d^8) - x^7*(120*a^3*b^6*d^{10} - 120*b^9*c^3*d^7 + 360*a*b^8*c^2*d^8 - 360*a^2*b^7*c*d^9))/(a^8*b^{10} + b^{18}*x^8 + 8*a^7*b^{11}*x + 8*a*b^{17}*x^7 + 28*a^6*b^{12}*x^2 + 56*a^5*b^{13}*x^3 + 70*a^4*b^{14}*x^4 + 56*a^3*b^{15}*x^5 + 28*a^2*b^{16}*x^6) - x*((9*a*d^{10})/b^{10} - (10*c*d^9)/b^9) + (d^{10}*x^2)/(2*b^9)
\end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**9,x)

[Out] Timed out

$$3.1321 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{10}} dx$$

Optimal. Leaf size=257

$$\frac{10d^9(bc-ad)\log(a+bx)}{b^{11}} - \frac{45d^8(bc-ad)^2}{b^{11}(a+bx)} - \frac{60d^7(bc-ad)^3}{b^{11}(a+bx)^2} - \frac{70d^6(bc-ad)^4}{b^{11}(a+bx)^3} - \frac{63d^5(bc-ad)^5}{b^{11}(a+bx)^4} - \frac{42d^4(bc-ad)^6}{b^{11}(a+bx)^5} - \frac{20d^3(bc-ad)^7}{b^{11}(a+bx)^6} - \frac{45d^2(bc-ad)^8}{7b^{11}(a+bx)^7} - \frac{10d(bc-ad)^9}{b^{11}(a+bx)^8} - \frac{d^2(bc-ad)^{10}}{b^{11}(a+bx)^9}$$

[Out] $d^{10}x/b^{10} - 1/9*(-a*d+b*c)^{10}/b^{11}/(b*x+a)^9 - 5/4*d*(-a*d+b*c)^9/b^{11}/(b*x+a)^8 - 45/7*d^2*(-a*d+b*c)^8/b^{11}/(b*x+a)^7 - 20*d^3*(-a*d+b*c)^7/b^{11}/(b*x+a)^6 - 42*d^4*(-a*d+b*c)^6/b^{11}/(b*x+a)^5 - 63*d^5*(-a*d+b*c)^5/b^{11}/(b*x+a)^4 - 70*d^6*(-a*d+b*c)^4/b^{11}/(b*x+a)^3 - 60*d^7*(-a*d+b*c)^3/b^{11}/(b*x+a)^2 - 45*d^8*(-a*d+b*c)^2/b^{11}/(b*x+a) + 10*d^9*(-a*d+b*c)*\ln(b*x+a)/b^{11}$

Rubi [A] time = 0.31, antiderivative size = 257, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{45d^8(bc-ad)^2}{b^{11}(a+bx)} - \frac{60d^7(bc-ad)^3}{b^{11}(a+bx)^2} - \frac{70d^6(bc-ad)^4}{b^{11}(a+bx)^3} - \frac{63d^5(bc-ad)^5}{b^{11}(a+bx)^4} - \frac{42d^4(bc-ad)^6}{b^{11}(a+bx)^5} - \frac{20d^3(bc-ad)^7}{b^{11}(a+bx)^6} - \frac{45d^2(bc-ad)^8}{7b^{11}(a+bx)^7} - \frac{10d(bc-ad)^9}{b^{11}(a+bx)^8} - \frac{d^2(bc-ad)^{10}}{b^{11}(a+bx)^9}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^10, x]

[Out] $(d^{10}x)/b^{10} - (b*c - a*d)^{10}/(9*b^{11}(a + b*x)^9) - (5*d*(b*c - a*d)^9)/(4*b^{11}(a + b*x)^8) - (45*d^2*(b*c - a*d)^8)/(7*b^{11}(a + b*x)^7) - (20*d^3*(b*c - a*d)^7)/(b^{11}(a + b*x)^6) - (42*d^4*(b*c - a*d)^6)/(b^{11}(a + b*x)^5) - (63*d^5*(b*c - a*d)^5)/(b^{11}(a + b*x)^4) - (70*d^6*(b*c - a*d)^4)/(b^{11}(a + b*x)^3) - (60*d^7*(b*c - a*d)^3)/(b^{11}(a + b*x)^2) - (45*d^8*(b*c - a*d)^2)/(b^{11}(a + b*x)) + (10*d^9*(b*c - a*d)*\text{Log}[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^{10}}{(a+bx)^{10}} dx = \int \left(\frac{d^{10}}{b^{10}} + \frac{(bc-ad)^{10}}{b^{10}(a+bx)^{10}} + \frac{10d(bc-ad)^9}{b^{10}(a+bx)^9} + \frac{45d^2(bc-ad)^8}{b^{10}(a+bx)^8} + \frac{120d^3(bc-ad)^7}{b^{10}(a+bx)^7} + \frac{210d^4(bc-ad)^6}{b^{10}(a+bx)^6} \right) dx$$

$$= \frac{d^{10}x}{b^{10}} - \frac{(bc-ad)^{10}}{9b^{11}(a+bx)^9} - \frac{5d(bc-ad)^9}{4b^{11}(a+bx)^8} - \frac{45d^2(bc-ad)^8}{7b^{11}(a+bx)^7} - \frac{20d^3(bc-ad)^7}{b^{11}(a+bx)^6} - \frac{42d^4(bc-ad)^6}{b^{11}(a+bx)^5}$$

Mathematica [B] time = 0.42, size = 708, normalized size = 2.75

$$\frac{4861a^{10}d^{10} + a^9bd^9(41229dx - 7129c) + 9a^8b^2d^8(140c^2 - 6849cdx + 17064d^2x^2) + 12a^7b^3d^7(35c^3 + 945c^2dx - 1960c^2d^2x^2 + 27342d^3x^3) + 42a^6b^4d^6(5c^4 + 90c^3dx + 1080c^2d^2x^2 - 12348cd^3x^3 + 10458d^4x^4) + 126a^5b^5d^5(c^5 + 15c^4dx + 120c^3d^2x^2 + 840c^2d^3x^3 - 5754cd^4x^4 + 2982d^5x^5) + 42a^4b^6d^4(2c^6 + 27c^5dx + 180c^4d^2x^2 + 840c^3d^3x^3 + 3780c^2d^4x^4 - 15750cd^5x^5 + 4704d^6x^6) + 12a^3b^7d^3(5c^7 + 63c^6dx + 378c^5d^2x^2 + 1470c^4d^3x^3 + 4410c^3d^4x^4 + 13230c^2d^5x^5 - 32340cd^6x^6 + 4536d^7x^7) + 9a^2b^8d^2(5c^8 + 60c^7dx + 336c^6d^2x^2 + 1176c^5d^3x^3 + 2940c^4d^4x^4 + 5880c^3d^5x^5 + 11760c^2d^6x^6 - 15120cd^7x^7 + 252d^8x^8) + ab^9d(35c^9 + 405c^8dx + 2160c^7d^2x^2 + 7056c^6d^3x^3 + 15876c^5d^4x^4 + 26460c^4d^5x^5 + 35280c^3d^6x^6 + 45360c^2d^7x^7 - 22680cd^8x^8 - 2268d^9x^9) + b^{10}(28c^{10} + 315c^9dx + 1620c^8d^2x^2 + 5040c^7d^3x^3 + 10584c^6d^4x^4 + 15876c^5d^5x^5 + 17640c^4d^6x^6 + 15120c^3d^7x^7 + 11340c^2d^8x^8 - 252d^{10}x^{10}) + 2520d^9(-bc + ad)(a + bx)^9 \operatorname{Log}[a + bx]}{(b^{11}(a + bx)^9)}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^10,x]

[Out] -1/252*(4861*a^10*d^10 + a^9*b*d^9*(-7129*c + 41229*d*x) + 9*a^8*b^2*d^8*(140*c^2 - 6849*c*d*x + 17064*d^2*x^2) + 12*a^7*b^3*d^7*(35*c^3 + 945*c^2*d*x - 1960*c*d^2*x^2 + 27342*d^3*x^3) + 42*a^6*b^4*d^6*(5*c^4 + 90*c^3*d*x + 1080*c^2*d^2*x^2 - 12348*c*d^3*x^3 + 10458*d^4*x^4) + 126*a^5*b^5*d^5*(c^5 + 15*c^4*d*x + 120*c^3*d^2*x^2 + 840*c^2*d^3*x^3 - 5754*c*d^4*x^4 + 2982*d^5*x^5) + 42*a^4*b^6*d^4*(2*c^6 + 27*c^5*d*x + 180*c^4*d^2*x^2 + 840*c^3*d^3*x^3 + 3780*c^2*d^4*x^4 - 15750*c*d^5*x^5 + 4704*d^6*x^6) + 12*a^3*b^7*d^3*(5*c^7 + 63*c^6*d*x + 378*c^5*d^2*x^2 + 1470*c^4*d^3*x^3 + 4410*c^3*d^4*x^4 + 13230*c^2*d^5*x^5 - 32340*c*d^6*x^6 + 4536*d^7*x^7) + 9*a^2*b^8*d^2*(5*c^8 + 60*c^7*d*x + 336*c^6*d^2*x^2 + 1176*c^5*d^3*x^3 + 2940*c^4*d^4*x^4 + 5880*c^3*d^5*x^5 + 11760*c^2*d^6*x^6 - 15120*c*d^7*x^7 + 252*d^8*x^8) + a*b^9*d*(35*c^9 + 405*c^8*d*x + 2160*c^7*d^2*x^2 + 7056*c^6*d^3*x^3 + 15876*c^5*d^4*x^4 + 26460*c^4*d^5*x^5 + 35280*c^3*d^6*x^6 + 45360*c^2*d^7*x^7 - 22680*c*d^8*x^8 - 2268*d^9*x^9) + b^10*(28*c^10 + 315*c^9*d*x + 1620*c^8*d^2*x^2 + 5040*c^7*d^3*x^3 + 10584*c^6*d^4*x^4 + 15876*c^5*d^5*x^5 + 17640*c^4*d^6*x^6 + 15120*c^3*d^7*x^7 + 11340*c^2*d^8*x^8 - 252*d^10*x^10) + 2520*d^9*(-(b*c) + a*d)*(a + b*x)^9*Log[a + b*x])/(b^11*(a + b*x)^9)

fricas [B] time = 0.47, size = 1216, normalized size = 4.73

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^10,x, algorithm="fricas")

[Out] 1/252*(252*b^10*d^10*x^10 + 2268*a*b^9*d^10*x^9 - 28*b^10*c^10 - 35*a*b^9*c^9*d - 45*a^2*b^8*c^8*d^2 - 60*a^3*b^7*c^7*d^3 - 84*a^4*b^6*c^6*d^4 - 126*a^5*b^5*c^5*d^5 - 105*a^6*b^4*c^4*d^6 - 63*a^7*b^3*c^3*d^7 - 21*a^8*b^2*c^2*d^8 - 7*a^9*b*c*d^9 + b^10*c^10 + 1050*d^9*c^9*(a + b*x)^9*Log[a + b*x])/(b^11*(a + b*x)^9)

$$\begin{aligned} &^5b^5c^5d^5 - 210a^6b^4c^4d^6 - 420a^7b^3c^3d^7 - 1260a^8b^2c^2d^8 + 7129a^9b^1c^1d^9 - 4861a^{10}d^{10} - 2268(5b^{10}c^2d^8 - 10a^9b^9c^1d^9 + a^2b^8d^{10})x^8 - 3024(5b^{10}c^3d^7 + 15a^9b^9c^2d^8 - 45a^2b^8c^1d^9 + 18a^3b^7d^{10})x^7 - 3528(5b^{10}c^4d^6 + 10a^9b^9c^3d^7 + 30a^2b^8c^2d^8 - 110a^3b^7c^1d^9 + 56a^4b^6d^{10})x^6 - 5292(3b^{10}c^5d^5 + 5a^9b^9c^4d^6 + 10a^2b^8c^3d^7 + 30a^3b^7c^2d^8 - 125a^4b^6c^1d^9 + 71a^5b^5d^{10})x^5 - 5292(2b^{10}c^6d^4 + 3a^9b^9c^5d^5 + 5a^2b^8c^4d^6 + 10a^3b^7c^3d^7 + 30a^4b^6c^2d^8 - 137a^5b^5c^1d^9 + 83a^6b^4d^{10})x^4 - 504(10b^{10}c^7d^3 + 14a^9b^9c^6d^4 + 21a^2b^8c^5d^5 + 35a^3b^7c^4d^6 + 70a^4b^6c^3d^7 + 210a^5b^5c^2d^8 - 1029a^6b^4c^1d^9 + 651a^7b^3d^{10})x^3 - 108(15b^{10}c^8d^2 + 20a^9b^9c^7d^3 + 28a^2b^8c^6d^4 + 42a^3b^7c^5d^5 + 70a^4b^6c^4d^6 + 140a^5b^5c^3d^7 + 420a^6b^4c^2d^8 - 2178a^7b^3c^1d^9 + 1422a^8b^2d^{10})x^2 - 9(35b^{10}c^9d + 45a^9b^9c^8d^2 + 60a^2b^8c^7d^3 + 84a^3b^7c^6d^4 + 126a^4b^6c^5d^5 + 210a^5b^5c^4d^6 + 420a^6b^4c^3d^7 + 1260a^7b^3c^2d^8 - 6849a^8b^2c^1d^9 + 4581a^9b^1d^{10})x + 2520(a^9b^1c^1d^9 - a^{10}d^{10} + (b^{10}c^1d^9 - a^9b^9d^{10})x^9 + 9(a^9b^9c^1d^9 - a^2b^8d^{10})x^8 + 36(a^2b^8c^1d^9 - a^3b^7d^{10})x^7 + 84(a^3b^7c^1d^9 - a^4b^6d^{10})x^6 + 126(a^4b^6c^1d^9 - a^5b^5d^{10})x^5 + 126(a^5b^5c^1d^9 - a^6b^4d^{10})x^4 + 84(a^6b^4c^1d^9 - a^7b^3d^{10})x^3 + 36(a^7b^3c^1d^9 - a^8b^2d^{10})x^2 + 9(a^8b^2c^1d^9 - a^9b^1d^{10})x) \log(bx + a) / (b^{20}x^9 + 9a^9b^{19}x^8 + 36a^2b^{18}x^7 + 84a^3b^{17}x^6 + 126a^4b^{16}x^5 + 126a^5b^{15}x^4 + 84a^6b^{14}x^3 + 36a^7b^{13}x^2 + 9a^8b^{12}x + a^9b^{11}) \end{aligned}$$

giac [B] time = 1.25, size = 867, normalized size = 3.37

$$\frac{d^{10}x}{b^{10}} + \frac{10(bcd^9 - ad^{10}) \log(|bx + a|)}{b^{11}} - \frac{28b^{10}c^{10} + 35ab^9c^9d + 45a^2b^8c^8d^2 + 60a^3b^7c^7d^3 + 84a^4b^6c^6d^4 + 126a^5b^5c^5d^5 + 126a^6b^4c^4d^6 + 420a^7b^3c^3d^7 + 1260a^8b^2c^2d^8 - 7129a^9b^1c^1d^9 + 4861a^{10}d^{10} + 11340(b^{10}c^2d^8 - 2a^9b^9c^1d^9 + a^2b^8d^{10})x^8 + 15120(b^{10}c^3d^7 + 3a^9b^9c^2d^8 - 9a^2b^8c^1d^9 + 5a^3b^7d^{10})x^7 + 17640(b^{10}c^4d^6 + 2a^9b^9c^3d^7 + 6a^2b^8c^2d^8 - 22a^3b^7c^1d^9 + 13a^4b^6d^{10})x^6 + 5292(3b^{10}c^5d^5 + 5a^9b^9c^4d^6 + 10a^2b^8c^3d^7 + 30a^3b^7c^2d^8 - 125a^4b^6c^1d^9 + 77a^5b^5d^{10})x^5 + 5292(2b^{10}c^6d^4 + 3a^9b^9c^5d^5 + 5a^2b^8c^4d^6 + 10a^3b^7c^3d^7 + 30a^4b^6c^2d^8 - 137a^5b^5c^1d^9 + 87a^6b^4d^{10})x^4 + 504(10b^{10}c^7d^3 + 14a^9b^9c^6d^4 + 21a^2b^8c^5d^5 + 35a^3b^7c^4d^6 + 70a^4b^6c^3d^7 + 210a^5b^5c^2d^8 - 1029a^6b^4c^1d^9 + 651a^7b^3d^{10})x^3 - 108(15b^{10}c^8d^2 + 20a^9b^9c^7d^3 + 28a^2b^8c^6d^4 + 42a^3b^7c^5d^5 + 70a^4b^6c^4d^6 + 140a^5b^5c^3d^7 + 420a^6b^4c^2d^8 - 2178a^7b^3c^1d^9 + 1422a^8b^2d^{10})x^2 - 9(35b^{10}c^9d + 45a^9b^9c^8d^2 + 60a^2b^8c^7d^3 + 84a^3b^7c^6d^4 + 126a^4b^6c^5d^5 + 210a^5b^5c^4d^6 + 420a^6b^4c^3d^7 + 1260a^7b^3c^2d^8 - 6849a^8b^2c^1d^9 + 4581a^9b^1d^{10})x + 2520(a^9b^1c^1d^9 - a^{10}d^{10} + (b^{10}c^1d^9 - a^9b^9d^{10})x^9 + 9(a^9b^9c^1d^9 - a^2b^8d^{10})x^8 + 36(a^2b^8c^1d^9 - a^3b^7d^{10})x^7 + 84(a^3b^7c^1d^9 - a^4b^6d^{10})x^6 + 126(a^4b^6c^1d^9 - a^5b^5d^{10})x^5 + 126(a^5b^5c^1d^9 - a^6b^4d^{10})x^4 + 84(a^6b^4c^1d^9 - a^7b^3d^{10})x^3 + 36(a^7b^3c^1d^9 - a^8b^2d^{10})x^2 + 9(a^8b^2c^1d^9 - a^9b^1d^{10})x) \log(bx + a) / (b^{20}x^9 + 9a^9b^{19}x^8 + 36a^2b^{18}x^7 + 84a^3b^{17}x^6 + 126a^4b^{16}x^5 + 126a^5b^{15}x^4 + 84a^6b^{14}x^3 + 36a^7b^{13}x^2 + 9a^8b^{12}x + a^9b^{11})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^10,x, algorithm="giac")

[Out] $d^{10}x/b^{10} + 10(b^9c^1d^9 - a^9d^{10}) \log(|bx + a|)/b^{11} - 1/252(28b^{10}c^{10} + 35a^9b^9c^9d + 45a^2b^8c^8d^2 + 60a^3b^7c^7d^3 + 84a^4b^6c^6d^4 + 126a^5b^5c^5d^5 + 126a^6b^4c^4d^6 + 420a^7b^3c^3d^7 + 1260a^8b^2c^2d^8 - 7129a^9b^1c^1d^9 + 4861a^{10}d^{10} + 11340(b^{10}c^2d^8 - 2a^9b^9c^1d^9 + a^2b^8d^{10})x^8 + 15120(b^{10}c^3d^7 + 3a^9b^9c^2d^8 - 9a^2b^8c^1d^9 + 5a^3b^7d^{10})x^7 + 17640(b^{10}c^4d^6 + 2a^9b^9c^3d^7 + 6a^2b^8c^2d^8 - 22a^3b^7c^1d^9 + 13a^4b^6d^{10})x^6 + 5292(3b^{10}c^5d^5 + 5a^9b^9c^4d^6 + 10a^2b^8c^3d^7 + 30a^3b^7c^2d^8 - 125a^4b^6c^1d^9 + 77a^5b^5d^{10})x^5 + 5292(2b^{10}c^6d^4 + 3a^9b^9c^5d^5 + 5a^2b^8c^4d^6 + 10a^3b^7c^3d^7 + 30a^4b^6c^2d^8 - 137a^5b^5c^1d^9 + 87a^6b^4d^{10})x^4 + 504(10b^{10}c^7d^3 + 14a^9b^9c^6d^4 + 21a^2b^8c^5d^5 + 35a^3b^7c^4d^6 + 70a^4b^6c^3d^7 + 210a^5b^5c^2d^8 - 1029a^6b^4c^1d^9 + 651a^7b^3d^{10})x^3 - 108(15b^{10}c^8d^2 + 20a^9b^9c^7d^3 + 28a^2b^8c^6d^4 + 42a^3b^7c^5d^5 + 70a^4b^6c^4d^6 + 140a^5b^5c^3d^7 + 420a^6b^4c^2d^8 - 2178a^7b^3c^1d^9 + 1422a^8b^2d^{10})x^2 - 9(35b^{10}c^9d + 45a^9b^9c^8d^2 + 60a^2b^8c^7d^3 + 84a^3b^7c^6d^4 + 126a^4b^6c^5d^5 + 210a^5b^5c^4d^6 + 420a^6b^4c^3d^7 + 1260a^7b^3c^2d^8 - 6849a^8b^2c^1d^9 + 4581a^9b^1d^{10})x + 2520(a^9b^1c^1d^9 - a^{10}d^{10} + (b^{10}c^1d^9 - a^9b^9d^{10})x^9 + 9(a^9b^9c^1d^9 - a^2b^8d^{10})x^8 + 36(a^2b^8c^1d^9 - a^3b^7d^{10})x^7 + 84(a^3b^7c^1d^9 - a^4b^6d^{10})x^6 + 126(a^4b^6c^1d^9 - a^5b^5d^{10})x^5 + 126(a^5b^5c^1d^9 - a^6b^4d^{10})x^4 + 84(a^6b^4c^1d^9 - a^7b^3d^{10})x^3 + 36(a^7b^3c^1d^9 - a^8b^2d^{10})x^2 + 9(a^8b^2c^1d^9 - a^9b^1d^{10})x) \log(bx + a) / (b^{20}x^9 + 9a^9b^{19}x^8 + 36a^2b^{18}x^7 + 84a^3b^{17}x^6 + 126a^4b^{16}x^5 + 126a^5b^{15}x^4 + 84a^6b^{14}x^3 + 36a^7b^{13}x^2 + 9a^8b^{12}x + a^9b^{11})$

$$\begin{aligned}
 & *a*b^9*c^6*d^4 + 21*a^2*b^8*c^5*d^5 + 35*a^3*b^7*c^4*d^6 + 70*a^4*b^6*c^3*d^7 + 210*a^5*b^5*c^2*d^8 - 1029*a^6*b^4*c*d^9 + 669*a^7*b^3*d^{10})*x^3 + 108 \\
 & *(15*b^{10}*c^8*d^2 + 20*a*b^9*c^7*d^3 + 28*a^2*b^8*c^6*d^4 + 42*a^3*b^7*c^5*d^5 + 70*a^4*b^6*c^4*d^6 + 140*a^5*b^5*c^3*d^7 + 420*a^6*b^4*c^2*d^8 - 2178 \\
 & *a^7*b^3*c*d^9 + 1443*a^8*b^2*d^{10})*x^2 + 9*(35*b^{10}*c^9*d + 45*a*b^9*c^8*d^2 + 60*a^2*b^8*c^7*d^3 + 84*a^3*b^7*c^6*d^4 + 126*a^4*b^6*c^5*d^5 + 210*a^5 \\
 & *b^5*c^4*d^6 + 420*a^6*b^4*c^3*d^7 + 1260*a^7*b^3*c^2*d^8 - 6849*a^8*b^2*c*d^9 + 4609*a^9*b*d^{10})*x)/((b*x + a)^9*b^{11})
 \end{aligned}$$

maple [B] time = 0.02, size = 1266, normalized size = 4.93

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((d*x+c)^{10}/(b*x+a)^{10},x)$

[Out]
$$\begin{aligned}
 & 60/b^{11}*d^{10}/(b*x+a)^2*a^3-60/b^8*d^7/(b*x+a)^2*c^3-10/b^{11}*d^{10}*\ln(b*x+a)* \\
 & a+10/b^{10}*d^9*\ln(b*x+a)*c+63/b^{11}*d^{10}/(b*x+a)^4*a^5-63/b^6*d^5/(b*x+a)^4*c \\
 & ^5-45/b^{11}*d^{10}/(b*x+a)*a^2-45/b^9*d^8/(b*x+a)*c^2+20/b^{11}*d^{10}/(b*x+a)^6*a \\
 & ^7-20/b^4*d^3/(b*x+a)^6*c^7-45/7/b^{11}*d^{10}/(b*x+a)^7*a^8-45/7/b^3*d^2/(b*x+ \\
 & a)^7*c^8-1/9/b^{11}/(b*x+a)^9*a^{10}*d^{10}+5/4/b^{11}*d^{10}/(b*x+a)^8*a^9-5/4/b^2*d \\
 & /(b*x+a)^8*c^9-70/b^{11}*d^{10}/(b*x+a)^3*a^4-70/b^7*d^6/(b*x+a)^3*c^4-42/b^{11}* \\
 & d^{10}/(b*x+a)^5*a^6-42/b^5*d^4/(b*x+a)^5*c^6+d^{10}*x/b^{10}-1/9/b/(b*x+a)^9*c^1 \\
 & 0-140/b^{10}*d^9/(b*x+a)^6*a^6*c+420/b^9*d^8/(b*x+a)^6*a^5*c^2+360/7/b^4*d^3/ \\
 & (b*x+a)^7*a*c^7+10/9/b^{10}/(b*x+a)^9*a^9*c*d^9-5/b^9/(b*x+a)^9*a^8*c^2*d^8+4 \\
 & 0/3/b^8/(b*x+a)^9*a^7*c^3*d^7+700/b^7*d^6/(b*x+a)^6*a^3*c^4-420/b^6*d^5/(b* \\
 & x+a)^6*a^2*c^5+140/b^5*d^4/(b*x+a)^6*a*c^6-70/3/b^7/(b*x+a)^9*a^6*c^4*d^6+2 \\
 & 8/b^6/(b*x+a)^9*a^5*c^5*d^5-70/3/b^5/(b*x+a)^9*a^4*c^6*d^4+40/3/b^4/(b*x+a) \\
 & ^9*a^3*c^7*d^3-5/b^3/(b*x+a)^9*a^2*c^8*d^2+10/9/b^2/(b*x+a)^9*a*c^9*d+252/b \\
 & ^{10}*d^9/(b*x+a)^5*a^5*c-630/b^9*d^8/(b*x+a)^5*a^4*c^2+840/b^8*d^7/(b*x+a)^5 \\
 & *a^3*c^3-630/b^7*d^6/(b*x+a)^5*a^2*c^4+252/b^6*d^5/(b*x+a)^5*a*c^5-180/b^{10} \\
 & *d^9/(b*x+a)^2*a^2*c+180/b^9*d^8/(b*x+a)^2*a*c^2-315/b^{10}*d^9/(b*x+a)^4*a^4 \\
 & *c+630/b^9*d^8/(b*x+a)^4*a^3*c^2-630/b^8*d^7/(b*x+a)^4*a^2*c^3+315/b^7*d^6/ \\
 & (b*x+a)^4*a*c^4+90/b^{10}*d^9/(b*x+a)*a*c+280/b^8*d^7/(b*x+a)^3*a*c^3+360/7/b \\
 & ^{10}*d^9/(b*x+a)^7*a^7*c-180/b^9*d^8/(b*x+a)^7*a^6*c^2+360/b^8*d^7/(b*x+a)^7 \\
 & *a^5*c^3-450/b^7*d^6/(b*x+a)^7*a^4*c^4+360/b^6*d^5/(b*x+a)^7*a^3*c^5-180/b^ \\
 & 5*d^4/(b*x+a)^7*a^2*c^6-700/b^8*d^7/(b*x+a)^6*a^4*c^3-45/4/b^{10}*d^9/(b*x+a) \\
 & ^8*a^8*c+45/b^9*d^8/(b*x+a)^8*a^7*c^2-105/b^8*d^7/(b*x+a)^8*a^6*c^3+315/2/b \\
 & ^7*d^6/(b*x+a)^8*a^5*c^4-315/2/b^6*d^5/(b*x+a)^8*a^4*c^5+105/b^5*d^4/(b*x+a) \\
 &)^8*a^3*c^6-45/b^4*d^3/(b*x+a)^8*a^2*c^7+45/4/b^3*d^2/(b*x+a)^8*a*c^8+280/b \\
 & ^{10}*d^9/(b*x+a)^3*a^3*c-420/b^9*d^8/(b*x+a)^3*a^2*c^2
 \end{aligned}$$

maxima [B] time = 2.36, size = 957, normalized size = 3.72

$$\frac{d^{10}x}{b^{10}} \frac{28b^{10}c^{10} + 35ab^9c^9d + 45a^2b^8c^8d^2 + 60a^3b^7c^7d^3 + 84a^4b^6c^6d^4 + 126a^5b^5c^5d^5 + 210a^6b^4c^4d^6 + 420a^7b^3c^3d^7 + 630a^8b^2c^2d^8 + 4609a^9bd^{10}}{b^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^10,x, algorithm="maxima")

[Out] $d^{10}x/b^{10} - 1/252*(28*b^{10}*c^{10} + 35*a*b^9*c^9*d + 45*a^2*b^8*c^8*d^2 + 60*a^3*b^7*c^7*d^3 + 84*a^4*b^6*c^6*d^4 + 126*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 + 420*a^7*b^3*c^3*d^7 + 1260*a^8*b^2*c^2*d^8 - 7129*a^9*b*c*d^9 + 4861*a^{10}*d^{10} + 11340*(b^{10}*c^2*d^8 - 2*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 15120*(b^{10}*c^3*d^7 + 3*a*b^9*c^2*d^8 - 9*a^2*b^8*c*d^9 + 5*a^3*b^7*d^{10})*x^7 + 17640*(b^{10}*c^4*d^6 + 2*a*b^9*c^3*d^7 + 6*a^2*b^8*c^2*d^8 - 22*a^3*b^7*c*d^9 + 13*a^4*b^6*d^{10})*x^6 + 5292*(3*b^{10}*c^5*d^5 + 5*a*b^9*c^4*d^6 + 10*a^2*b^8*c^3*d^7 + 30*a^3*b^7*c^2*d^8 - 125*a^4*b^6*c*d^9 + 77*a^5*b^5*d^{10})*x^5 + 5292*(2*b^{10}*c^6*d^4 + 3*a*b^9*c^5*d^5 + 5*a^2*b^8*c^4*d^6 + 10*a^3*b^7*c^3*d^7 + 30*a^4*b^6*c^2*d^8 - 137*a^5*b^5*c*d^9 + 87*a^6*b^4*d^{10})*x^4 + 504*(10*b^{10}*c^7*d^3 + 14*a*b^9*c^6*d^4 + 21*a^2*b^8*c^5*d^5 + 35*a^3*b^7*c^4*d^6 + 70*a^4*b^6*c^3*d^7 + 210*a^5*b^5*c^2*d^8 - 1029*a^6*b^4*c*d^9 + 669*a^7*b^3*d^{10})*x^3 + 108*(15*b^{10}*c^8*d^2 + 20*a*b^9*c^7*d^3 + 28*a^2*b^8*c^6*d^4 + 42*a^3*b^7*c^5*d^5 + 70*a^4*b^6*c^4*d^6 + 140*a^5*b^5*c^3*d^7 + 420*a^6*b^4*c^2*d^8 - 2178*a^7*b^3*c*d^9 + 1443*a^8*b^2*d^{10})*x^2 + 9*(35*b^{10}*c^9*d + 45*a*b^9*c^8*d^2 + 60*a^2*b^8*c^7*d^3 + 84*a^3*b^7*c^6*d^4 + 126*a^4*b^6*c^5*d^5 + 210*a^5*b^5*c^4*d^6 + 420*a^6*b^4*c^3*d^7 + 1260*a^7*b^3*c^2*d^8 - 6849*a^8*b^2*c*d^9 + 4609*a^9*b*d^{10})*x)/(b^{20}*x^9 + 9*a*b^{19}*x^8 + 36*a^2*b^{18}*x^7 + 84*a^3*b^{17}*x^6 + 126*a^4*b^{16}*x^5 + 126*a^5*b^{15}*x^4 + 84*a^6*b^{14}*x^3 + 36*a^7*b^{13}*x^2 + 9*a^8*b^{12}*x + a^9*b^{11}) + 10*(b*c*d^9 - a*d^{10})*log(b*x + a)/b^{11}$

mupad [B] time = 0.50, size = 955, normalized size = 3.72

$$\frac{d^{10}x}{b^{10}} \frac{\ln(a+bx) (10ad^{10} - 10bcd^9)}{b^{11}} - \frac{x^4 (1827a^6b^3d^{10} - 2877a^5b^4cd^9 + 630a^4b^5c^2d^8 + 210a^3b^6c^3d^7 + 105a^2b^7c^4d^6 + 210a^3b^6c^3d^7 + 630a^4b^5c^2d^8) + x^6(910a^4b^5d^{10} + 70b^9c^4d^6 + 140a^2b^8c^3d^7 - 1540a^3b^6c*d^9 + 420a^2b^7c^2d^8) + (4861a^{10}d^{10} + 28b^{10}c^{10} + 45a^2b^8c^8d^2 + 60a^3b^7c^7d^3 + 84a^4b^6c^6d^4 + 126a^5b^5c^5d^5 + 210a^6b^4c^4d^6 + 420a^7b^3c^3d^7 + 1260a^8b^2c^2d^8 + 35a*b^9*c^9*d - 7129a^9*b*c*d^9)/(252*b) + x*((4609*a^9*d^{10})/28 + (5*b^9*c^9*d)/4 + (45*a*b^8*c^8*d^2)/28 + (15*a^2*b^7*c^7*d^3)/7 + 3*a^3*b^6*c^6*d^4 + (9*a^4*b^5*c^5*d^5)/2 + (15*a^5*b^4*c^4*d^6)/2 + 15*a^6*b^3*c^3*d^7 + 45*a^7*b^2*c^2*d^8 -$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^10,x)

[Out] $(d^{10}x)/b^{10} - (\log(a + b*x)*(10*a*d^{10} - 10*b*c*d^9))/b^{11} - (x^4*(1827*a^6*b^3*d^{10} + 42*b^9*c^6*d^4 + 63*a*b^8*c^5*d^5 - 2877*a^5*b^4*c*d^9 + 105*a^2*b^7*c^4*d^6 + 210*a^3*b^6*c^3*d^7 + 630*a^4*b^5*c^2*d^8) + x^6*(910*a^4*b^5*d^{10} + 70*b^9*c^4*d^6 + 140*a^2*b^8*c^3*d^7 - 1540*a^3*b^6*c*d^9 + 420*a^2*b^7*c^2*d^8) + (4861*a^{10}*d^{10} + 28*b^{10}*c^{10} + 45*a^2*b^8*c^8*d^2 + 60*a^3*b^7*c^7*d^3 + 84*a^4*b^6*c^6*d^4 + 126*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 + 420*a^7*b^3*c^3*d^7 + 1260*a^8*b^2*c^2*d^8 + 35*a*b^9*c^9*d - 7129*a^9*b*c*d^9)/(252*b) + x*((4609*a^9*d^{10})/28 + (5*b^9*c^9*d)/4 + (45*a*b^8*c^8*d^2)/28 + (15*a^2*b^7*c^7*d^3)/7 + 3*a^3*b^6*c^6*d^4 + (9*a^4*b^5*c^5*d^5)/2 + (15*a^5*b^4*c^4*d^6)/2 + 15*a^6*b^3*c^3*d^7 + 45*a^7*b^2*c^2*d^8 -$

$$\begin{aligned}
& (6849*a^8*b*c*d^9)/28) + x^8*(45*a^2*b^7*d^10 + 45*b^9*c^2*d^8 - 90*a*b^8*c \\
& *d^9) + x^3*(1338*a^7*b^2*d^10 + 20*b^9*c^7*d^3 + 28*a*b^8*c^6*d^4 - 2058*a \\
& ^6*b^3*c*d^9 + 42*a^2*b^7*c^5*d^5 + 70*a^3*b^6*c^4*d^6 + 140*a^4*b^5*c^3*d^ \\
& 7 + 420*a^5*b^4*c^2*d^8) + x^2*((4329*a^8*b*d^10)/7 + (45*b^9*c^8*d^2)/7 + \\
& (60*a*b^8*c^7*d^3)/7 - (6534*a^7*b^2*c*d^9)/7 + 12*a^2*b^7*c^6*d^4 + 18*a^3 \\
& *b^6*c^5*d^5 + 30*a^4*b^5*c^4*d^6 + 60*a^5*b^4*c^3*d^7 + 180*a^6*b^3*c^2*d^ \\
& 8) + x^5*(1617*a^5*b^4*d^10 + 63*b^9*c^5*d^5 + 105*a*b^8*c^4*d^6 - 2625*a^4 \\
& *b^5*c*d^9 + 210*a^2*b^7*c^3*d^7 + 630*a^3*b^6*c^2*d^8) + x^7*(300*a^3*b^6* \\
& d^10 + 60*b^9*c^3*d^7 + 180*a*b^8*c^2*d^8 - 540*a^2*b^7*c*d^9))/(a^9*b^10 + \\
& b^19*x^9 + 9*a^8*b^11*x + 9*a*b^18*x^8 + 36*a^7*b^12*x^2 + 84*a^6*b^13*x^3 \\
& + 126*a^5*b^14*x^4 + 126*a^4*b^15*x^5 + 84*a^3*b^16*x^6 + 36*a^2*b^17*x^7)
\end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**10,x)

[Out] Timed out

$$3.1322 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{11}} dx$$

Optimal. Leaf size=271

$$\frac{10d^9(bc-ad)}{b^{11}(a+bx)} - \frac{45d^8(bc-ad)^2}{2b^{11}(a+bx)^2} - \frac{40d^7(bc-ad)^3}{b^{11}(a+bx)^3} - \frac{105d^6(bc-ad)^4}{2b^{11}(a+bx)^4} - \frac{252d^5(bc-ad)^5}{5b^{11}(a+bx)^5} - \frac{35d^4(bc-ad)^6}{b^{11}(a+bx)^6} - \frac{120d^3(bc-ad)^7}{7b^{11}(a+bx)^7} - \frac{252d^2(bc-ad)^8}{2b^{11}(a+bx)^8} - \frac{105d(bc-ad)^9}{b^{11}(a+bx)^9} - \frac{10d^9(bc-ad)^{10}}{b^{11}(a+bx)^{10}} - \frac{10d^9(bc-ad)^{10}}{b^{11}(a+bx)^{10}}$$

[Out] $-1/10*(-a*d+b*c)^{10}/b^{11}/(b*x+a)^{10}-10/9*d*(-a*d+b*c)^9/b^{11}/(b*x+a)^9-45/8*d^2*(-a*d+b*c)^8/b^{11}/(b*x+a)^8-120/7*d^3*(-a*d+b*c)^7/b^{11}/(b*x+a)^7-35*d^4*(-a*d+b*c)^6/b^{11}/(b*x+a)^6-252/5*d^5*(-a*d+b*c)^5/b^{11}/(b*x+a)^5-105/2*d^6*(-a*d+b*c)^4/b^{11}/(b*x+a)^4-40*d^7*(-a*d+b*c)^3/b^{11}/(b*x+a)^3-45/2*d^8*(-a*d+b*c)^2/b^{11}/(b*x+a)^2-10*d^9*(-a*d+b*c)/b^{11}/(b*x+a)+d^{10}*ln(b*x+a)/b^{11}$

Rubi [A] time = 0.29, antiderivative size = 271, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{10d^9(bc-ad)}{b^{11}(a+bx)} - \frac{45d^8(bc-ad)^2}{2b^{11}(a+bx)^2} - \frac{40d^7(bc-ad)^3}{b^{11}(a+bx)^3} - \frac{105d^6(bc-ad)^4}{2b^{11}(a+bx)^4} - \frac{252d^5(bc-ad)^5}{5b^{11}(a+bx)^5} - \frac{35d^4(bc-ad)^6}{b^{11}(a+bx)^6} - \frac{120d^3(bc-ad)^7}{7b^{11}(a+bx)^7} - \frac{252d^2(bc-ad)^8}{2b^{11}(a+bx)^8} - \frac{105d(bc-ad)^9}{b^{11}(a+bx)^9} - \frac{10d^9(bc-ad)^{10}}{b^{11}(a+bx)^{10}} - \frac{10d^9(bc-ad)^{10}}{b^{11}(a+bx)^{10}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^11,x]

[Out] $-(b*c - a*d)^{10}/(10*b^{11}*(a + b*x)^{10}) - (10*d*(b*c - a*d)^9)/(9*b^{11}*(a + b*x)^9) - (45*d^2*(b*c - a*d)^8)/(8*b^{11}*(a + b*x)^8) - (120*d^3*(b*c - a*d)^7)/(7*b^{11}*(a + b*x)^7) - (35*d^4*(b*c - a*d)^6)/(b^{11}*(a + b*x)^6) - (252*d^5*(b*c - a*d)^5)/(5*b^{11}*(a + b*x)^5) - (105*d^6*(b*c - a*d)^4)/(2*b^{11}*(a + b*x)^4) - (40*d^7*(b*c - a*d)^3)/(b^{11}*(a + b*x)^3) - (45*d^8*(b*c - a*d)^2)/(2*b^{11}*(a + b*x)^2) - (10*d^9*(b*c - a*d))/(b^{11}*(a + b*x)) + (d^{10}*Log[a + b*x])/b^{11}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^{10}}{(a+bx)^{11}} dx = \int \left(\frac{(bc-ad)^{10}}{b^{10}(a+bx)^{11}} + \frac{10d(bc-ad)^9}{b^{10}(a+bx)^{10}} + \frac{45d^2(bc-ad)^8}{b^{10}(a+bx)^9} + \frac{120d^3(bc-ad)^7}{b^{10}(a+bx)^8} + \frac{210d^4(bc-ad)^6}{b^{10}(a+bx)^7} + \frac{105d^5(bc-ad)^5}{b^{10}(a+bx)^6} + \frac{35d^6(bc-ad)^4}{b^{10}(a+bx)^5} + \frac{7d^7(bc-ad)^3}{b^{10}(a+bx)^4} + \frac{d^8(bc-ad)^2}{b^{10}(a+bx)^3} + \frac{d^9(bc-ad)}{b^{10}(a+bx)^2} + \frac{d^{10}}{b^{10}(a+bx)} \right) dx$$

$$= -\frac{(bc-ad)^{10}}{10b^{11}(a+bx)^{10}} - \frac{10d(bc-ad)^9}{9b^{11}(a+bx)^9} - \frac{45d^2(bc-ad)^8}{8b^{11}(a+bx)^8} - \frac{120d^3(bc-ad)^7}{7b^{11}(a+bx)^7} - \frac{35d^4(bc-ad)^6}{b^{11}(a+bx)^6} - \frac{7d^5(bc-ad)^5}{5b^{11}(a+bx)^5} - \frac{d^6(bc-ad)^4}{b^{11}(a+bx)^4} - \frac{d^7(bc-ad)^3}{3b^{11}(a+bx)^3} - \frac{d^8(bc-ad)^2}{2b^{11}(a+bx)^2} - \frac{d^9(bc-ad)}{b^{11}(a+bx)} - \frac{d^{10}}{10b^{11}}$$

Mathematica [B] time = 0.36, size = 591, normalized size = 2.18

$$\frac{d^{10} \log(a+bx)}{b^{11}} - \frac{(bc-ad) \left(7381a^9d^9 + a^8bd^8(4861c + 71290dx) + a^7b^2d^7(3601c^2 + 46090cdx + 308205d^2x^2) \right)}{b^{11}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^11, x]

[Out]
$$-1/2520 * ((b*c - a*d) * (7381*a^9*d^9 + a^8*b*d^8*(4861*c + 71290*d*x) + a^7*b^2*d^7*(3601*c^2 + 46090*c*d*x + 308205*d^2*x^2) + a^6*b^3*d^6*(2761*c^3 + 33490*c^2*d*x + 194805*c*d^2*x^2 + 784080*d^3*x^3) + a^5*b^4*d^5*(2131*c^4 + 25090*c^3*d*x + 138105*c^2*d^2*x^2 + 481680*c*d^3*x^3 + 1296540*d^4*x^4) + a^4*b^5*d^4*(1627*c^5 + 18790*c^4*d*x + 100305*c^3*d^2*x^2 + 330480*c^2*d^3*x^3 + 767340*c*d^4*x^4 + 1450008*d^5*x^5) + a^3*b^6*d^3*(1207*c^6 + 13750*c^5*d*x + 71955*c^4*d^2*x^2 + 229680*c^3*d^3*x^3 + 502740*c^2*d^4*x^4 + 814968*c*d^5*x^5 + 1102500*d^6*x^6) + a^2*b^7*d^2*(847*c^7 + 9550*c^6*d*x + 49275*c^5*d^2*x^2 + 154080*c^4*d^3*x^3 + 326340*c^3*d^4*x^4 + 497448*c^2*d^5*x^5 + 573300*c*d^6*x^6 + 554400*d^7*x^7) + a*b^8*d*(532*c^8 + 5950*c^7*d*x + 30375*c^6*d^2*x^2 + 93600*c^5*d^3*x^3 + 194040*c^4*d^4*x^4 + 285768*c^3*d^5*x^5 + 308700*c^2*d^6*x^6 + 252000*c*d^7*x^7 + 170100*d^8*x^8) + b^9*(252*c^9 + 2800*c^8*d*x + 14175*c^7*d^2*x^2 + 43200*c^6*d^3*x^3 + 88200*c^5*d^4*x^4 + 127008*c^4*d^5*x^5 + 132300*c^3*d^6*x^6 + 100800*c^2*d^7*x^7 + 56700*c*d^8*x^8 + 25200*d^9*x^9)) / (b^11*(a + b*x)^10) + (d^10*Log[a + b*x]) / b^11$$

fricas [B] time = 0.44, size = 1107, normalized size = 4.08

$$\frac{252b^{10}c^{10} + 280ab^9c^9d + 315a^2b^8c^8d^2 + 360a^3b^7c^7d^3 + 420a^4b^6c^6d^4 + 504a^5b^5c^5d^5 + 630a^6b^4c^4d^6 + 840a^7b^3c^3d^7 + 900a^8b^2c^2d^8 + 840a^9b^1c^1d^9 + 25200d^{10}}{b^{11}(a+bx)^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^11,x, algorithm="fricas")

[Out]
$$-1/2520 * (252*b^{10}*c^{10} + 280*a*b^9*c^9*d + 315*a^2*b^8*c^8*d^2 + 360*a^3*b^7*c^7*d^3 + 420*a^4*b^6*c^6*d^4 + 504*a^5*b^5*c^5*d^5 + 630*a^6*b^4*c^4*d^6 + 840*a^7*b^3*c^3*d^7 + 900*a^8*b^2*c^2*d^8 + 840*a^9*b^1*c^1*d^9 + 25200*d^{10}) / (b^{11}*(a + b*x)^{10})$$

$$\frac{20a^6b^3c^2d^8 + 840a^7b^2c^2d^9 - 2283a^8b^2d^{10}}{b^2c^2d^8 + 2520a^9b^2c^2d^9 - 7381a^{10}d^{10}} \cdot x^2 + 10 \cdot \frac{(280b^9c^9d + 315ab^8c^8d^2 + 360a^2b^7c^7d^3 + 420a^3b^6c^6d^4 + 504a^4b^5c^5d^5 + 630a^5b^4c^4d^6 + 840a^6b^3c^3d^7 + 1260a^7b^2c^2d^8 + 2520a^8b^2c^2d^9 - 7129a^9d^{10}) \cdot x + (252b^{10}c^{10} + 280a^9c^9d + 315a^2b^8c^8d^2 + 360a^3b^7c^7d^3 + 420a^4b^6c^6d^4 + 504a^5b^5c^5d^5 + 630a^6b^4c^4d^6 + 840a^7b^3c^3d^7 + 1260a^8b^2c^2d^8 + 2520a^9b^2c^2d^9 - 7381a^{10}d^{10})}{(bx + a)^{10}b^{10}}$$

maple [B] time = 0.01, size = 1271, normalized size = 4.69

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((dx+c)^{10}/(bx+a)^{11}, x)$

[Out]
$$\begin{aligned} & -35d^{10}/b^{11}/(bx+a)^6a^6 - 35d^4/b^5/(bx+a)^6c^6 - 1/10/b^{11}/(bx+a)^{10}a^{10}d^{10} \\ & - 120/7d^3/b^4/(bx+a)^7c^7 + 10/9d^{10}/b^{11}/(bx+a)^9a^9 - 10/9d/b^2/(bx+a)^9c^9 \\ & + 252/5d^{10}/b^{11}/(bx+a)^5a^5 - 252/5d^5/b^6/(bx+a)^5c^5 - 45/2d^{10}/b^{11}/(bx+a)^2a^2 \\ & - 45/2d^8/b^9/(bx+a)^2c^2 - 105/2d^{10}/b^{11}/(bx+a)^4a^4 - 105/2d^6/b^7/(bx+a)^4c^4 \\ & + 10/b^{11}d^{10}/(bx+a)a - 10/b^{10}d^9/(bx+a)c - 45/8d^{10}/b^{11}/(bx+a)^8a^8 \\ & - 45/8d^2/b^3/(bx+a)^8c^8 + 40d^{10}/b^{11}/(bx+a)^3a^3 - 40d^7/b^8/(bx+a)^3c^3 \\ & + 120/7d^{10}/b^{11}/(bx+a)^7a^7 - 315/2d^4/b^5/(bx+a)^8a^2c^6 + 45d^3/b^4/(bx+a)^8ac^7 \\ & - 120d^9/b^{10}/(bx+a)^3a^2c^2 + 120d^8/b^9/(bx+a)^3ac^2 - 120d^9/b^{10}/(bx+a)^7a^6c^3 \\ & + 360d^8/b^9/(bx+a)^7a^5c^2 - 600d^7/b^8/(bx+a)^7a^4c^3 + 600d^6/b^7/(bx+a)^7a^3c^4 \\ & - 360d^5/b^6/(bx+a)^7a^2c^5 + 120d^4/b^5/(bx+a)^7ac^6 - 10d^9/b^{10}/(bx+a)^9a^8c^4 \\ & + 40d^8/b^9/(bx+a)^9a^7c^2 - 280/3d^7/b^8/(bx+a)^9a^6c^3 + 140d^6/b^7/(bx+a)^9a^5c^4 \\ & - 140d^5/b^6/(bx+a)^9a^4c^5 + 280/3d^4/b^5/(bx+a)^9a^3c^6 - 40d^3/b^4/(bx+a)^9a^2c^7 \\ & + 10d^2/b^3/(bx+a)^9ac^8 - 252d^9/b^{10}/(bx+a)^5a^4c^5 + 504d^8/b^9/(bx+a)^5a^3c^2 \\ & - 504d^7/b^8/(bx+a)^5a^2c^3 + 252d^6/b^7/(bx+a)^5ac^4 + 45d^9/b^{10}/(bx+a)^2ac^2 \\ & + 210d^9/b^{10}/(bx+a)^4a^3c^3 - 315d^8/b^9/(bx+a)^4a^2c^2 + 210d^7/b^8/(bx+a)^4ac^3 \\ & + 210d^9/b^{10}/(bx+a)^6a^5c^5 - 525d^8/b^9/(bx+a)^6a^4c^2 + 700d^7/b^8/(bx+a)^6a^3c^3 \\ & - 525d^6/b^7/(bx+a)^6a^2c^4 + 210d^5/b^6/(bx+a)^6ac^5 + 1/b^{10}/(bx+a)^{10}a^9c^9d \\ & - 9/2/b^9/(bx+a)^{10}a^8c^2d^8 + 12/b^8/(bx+a)^{10}a^7c^3d^7 - 21/b^7/(bx+a)^{10}a^6c^4d^6 \\ & + 126/5/b^6/(bx+a)^{10}a^5c^5d^5 - 21/b^5/(bx+a)^{10}a^4c^6d^4 + 12/b^4/(bx+a)^{10}a^3c^7d^3 \\ & - 9/2/b^3/(bx+a)^{10}a^2c^8d^2 + 1/b^2/(bx+a)^{10}ac^9d + 45d^9/b^{10}/(bx+a)^8a^7c^3 \\ & - 15/2d^8/b^9/(bx+a)^8a^6c^2 + 315d^5/b^6/(bx+a)^8a^3c^5 + d^{10} \ln(bx+a) \\ & / b^{11} - 1/10/b/(bx+a)^{10}c^{10} + 315d^7/b^8/(bx+a)^8a^5c^3 - 1575/4d^6/b^7/(bx+a)^8a^4c^4 \end{aligned}$$

maxima [B] time = 2.01, size = 975, normalized size = 3.60

$$252b^{10}c^{10} + 280ab^9c^9d + 315a^2b^8c^8d^2 + 360a^3b^7c^7d^3 + 420a^4b^6c^6d^4 + 504a^5b^5c^5d^5 + 630a^6b^4c^4d^6 + 840a^7b^3c^3d^7 + 1260a^8b^2c^2d^8 + 2520a^9b^2c^2d^9 - 7381a^{10}d^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^11,x, algorithm="maxima")

[Out]
$$-1/2520*(252*b^{10}*c^{10} + 280*a*b^9*c^9*d + 315*a^2*b^8*c^8*d^2 + 360*a^3*b^7*c^7*d^3 + 420*a^4*b^6*c^6*d^4 + 504*a^5*b^5*c^5*d^5 + 630*a^6*b^4*c^4*d^6 + 840*a^7*b^3*c^3*d^7 + 1260*a^8*b^2*c^2*d^8 + 2520*a^9*b*c*d^9 - 7381*a^{10}*d^{10} + 25200*(b^{10}*c*d^9 - a*b^9*d^{10})*x^9 + 56700*(b^{10}*c^2*d^8 + 2*a*b^9*c*d^9 - 3*a^2*b^8*d^{10})*x^8 + 50400*(2*b^{10}*c^3*d^7 + 3*a*b^9*c^2*d^8 + 6*a^2*b^8*c*d^9 - 11*a^3*b^7*d^{10})*x^7 + 44100*(3*b^{10}*c^4*d^6 + 4*a*b^9*c^3*d^7 + 6*a^2*b^8*c^2*d^8 + 12*a^3*b^7*c*d^9 - 25*a^4*b^6*d^{10})*x^6 + 10584*(12*b^{10}*c^5*d^5 + 15*a*b^9*c^4*d^6 + 20*a^2*b^8*c^3*d^7 + 30*a^3*b^7*c^2*d^8 + 60*a^4*b^6*c*d^9 - 137*a^5*b^5*d^{10})*x^5 + 8820*(10*b^{10}*c^6*d^4 + 12*a*b^9*c^5*d^5 + 15*a^2*b^8*c^4*d^6 + 20*a^3*b^7*c^3*d^7 + 30*a^4*b^6*c^2*d^8 + 60*a^5*b^5*c*d^9 - 147*a^6*b^4*d^{10})*x^4 + 720*(60*b^{10}*c^7*d^3 + 70*a*b^9*c^6*d^4 + 84*a^2*b^8*c^5*d^5 + 105*a^3*b^7*c^4*d^6 + 140*a^4*b^6*c^3*d^7 + 210*a^5*b^5*c^2*d^8 + 420*a^6*b^4*c*d^9 - 1089*a^7*b^3*d^{10})*x^3 + 135*(105*b^{10}*c^8*d^2 + 120*a*b^9*c^7*d^3 + 140*a^2*b^8*c^6*d^4 + 168*a^3*b^7*c^5*d^5 + 210*a^4*b^6*c^4*d^6 + 280*a^5*b^5*c^3*d^7 + 420*a^6*b^4*c^2*d^8 + 840*a^7*b^3*c*d^9 - 2283*a^8*b^2*d^{10})*x^2 + 10*(280*b^{10}*c^9*d + 315*a*b^9*c^8*d^2 + 360*a^2*b^8*c^7*d^3 + 420*a^3*b^7*c^6*d^4 + 504*a^4*b^6*c^5*d^5 + 630*a^5*b^5*c^4*d^6 + 840*a^6*b^4*c^3*d^7 + 1260*a^7*b^3*c^2*d^8 + 2520*a^8*b^2*c*d^9 - 7129*a^9*b*d^{10})*x)/(b^{21}*x^{10} + 10*a*b^{20}*x^9 + 45*a^2*b^{19}*x^8 + 120*a^3*b^{18}*x^7 + 210*a^4*b^{17}*x^6 + 252*a^5*b^{16}*x^5 + 210*a^6*b^{15}*x^4 + 120*a^7*b^{14}*x^3 + 45*a^8*b^{13}*x^2 + 10*a^9*b^{12}*x + a^{10}*b^{11}) + d^{10}*log(b*x + a)/b^{11}$$

mupad [B] time = 0.56, size = 866, normalized size = 3.20

$$\frac{d^{10} \ln(a + b x)}{b^{11}} - \frac{x^4 \left(-\frac{1029 a^6 b^4 d^{10}}{2} + 210 a^5 b^5 c d^9 + 105 a^4 b^6 c^2 d^8 + 70 a^3 b^7 c^3 d^7 + \frac{105 a^2 b^8 c^4 d^6}{2} + 42 a b^9 c^5 d^5 + \right)}{b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^11,x)

[Out]
$$(d^{10}*\log(a + b*x))/b^{11} - (x^4*(35*b^{10}*c^6*d^4 - (1029*a^6*b^4*d^{10})/2 + 42*a*b^9*c^5*d^5 + 210*a^5*b^5*c*d^9 + (105*a^2*b^8*c^4*d^6)/2 + 70*a^3*b^7*c^3*d^7 + 105*a^4*b^6*c^2*d^8) - x^9*(10*a*b^9*d^{10} - 10*b^{10}*c*d^9) + x*((10*b^{10}*c^9*d)/9 - (7129*a^9*b*d^{10})/252 + (5*a*b^9*c^8*d^2)/4 + 10*a^8*b^2*c*d^9 + (10*a^2*b^8*c^7*d^3)/7 + (5*a^3*b^7*c^6*d^4)/3 + 2*a^4*b^6*c^5*d^5 + (5*a^5*b^5*c^4*d^6)/2 + (10*a^6*b^4*c^3*d^7)/3 + 5*a^7*b^3*c^2*d^8) + x^6*((105*b^{10}*c^4*d^6)/2 - (875*a^4*b^6*d^{10})/2 + 70*a*b^9*c^3*d^7 + 210*a^3*b^7*c*d^9 + 105*a^2*b^8*c^2*d^8) + x^8*((45*b^{10}*c^2*d^8)/2 - (135*a^2*b^8*d^{10})/2 + 45*a*b^9*c*d^9) + x^3*((120*b^{10}*c^7*d^3)/7 - (2178*a^7*b^3*d^1$$

$$\begin{aligned}
& 0)/7 + 20*a*b^9*c^6*d^4 + 120*a^6*b^4*c*d^9 + 24*a^2*b^8*c^5*d^5 + 30*a^3*b \\
& ^7*c^4*d^6 + 40*a^4*b^6*c^3*d^7 + 60*a^5*b^5*c^2*d^8) + x^5*((252*b^10*c^5* \\
& d^5)/5 - (2877*a^5*b^5*d^10)/5 + 63*a*b^9*c^4*d^6 + 252*a^4*b^6*c*d^9 + 84* \\
& a^2*b^8*c^3*d^7 + 126*a^3*b^7*c^2*d^8) - (7381*a^10*d^10)/2520 + (b^10*c^10 \\
&)/10 + x^7*(40*b^10*c^3*d^7 - 220*a^3*b^7*d^10 + 60*a*b^9*c^2*d^8 + 120*a^2 \\
& *b^8*c*d^9) + x^2*((45*b^10*c^8*d^2)/8 - (6849*a^8*b^2*d^10)/56 + (45*a*b^9 \\
& *c^7*d^3)/7 + 45*a^7*b^3*c*d^9 + (15*a^2*b^8*c^6*d^4)/2 + 9*a^3*b^7*c^5*d^5 \\
& + (45*a^4*b^6*c^4*d^6)/4 + 15*a^5*b^5*c^3*d^7 + (45*a^6*b^4*c^2*d^8)/2) + \\
& (a^2*b^8*c^8*d^2)/8 + (a^3*b^7*c^7*d^3)/7 + (a^4*b^6*c^6*d^4)/6 + (a^5*b^5* \\
& c^5*d^5)/5 + (a^6*b^4*c^4*d^6)/4 + (a^7*b^3*c^3*d^7)/3 + (a^8*b^2*c^2*d^8)/ \\
& 2 + (a*b^9*c^9*d)/9 + a^9*b*c*d^9)/(b^11*(a + b*x)^10)
\end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**11,x)

[Out] Timed out

$$3.1323 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{12}} dx$$

Optimal. Leaf size=28

$$-\frac{(c+dx)^{11}}{11(a+bx)^{11}(bc-ad)}$$

[Out] -1/11*(d*x+c)^11/(-a*d+b*c)/(b*x+a)^11

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$-\frac{(c+dx)^{11}}{11(a+bx)^{11}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^12,x]

[Out] -(c + d*x)^11/(11*(b*c - a*d)*(a + b*x)^11)

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(c+dx)^{10}}{(a+bx)^{12}} dx = -\frac{(c+dx)^{11}}{11(bc-ad)(a+bx)^{11}}$$

Mathematica [B] time = 0.28, size = 665, normalized size = 23.75

$$\frac{a^{10}d^{10} + a^9bd^9(c + 11dx) + a^8b^2d^8(c^2 + 11cdx + 55d^2x^2) + a^7b^3d^7(c^3 + 11c^2dx + 55cd^2x^2 + 165d^3x^3) + a^6b^4d^6(c^4 + 11c^3dx + 55c^2d^2x^2 + 165cd^3x^3 + 65d^4x^4)}{11(a+bx)^{11}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^12,x]

[Out] -1/11*(a^10*d^10 + a^9*b*d^9*(c + 11*d*x) + a^8*b^2*d^8*(c^2 + 11*c*d*x + 55*d^2*x^2) + a^7*b^3*d^7*(c^3 + 11*c^2*d*x + 55*c*d^2*x^2 + 165*d^3*x^3) +

$$\begin{aligned} & a^6 b^4 d^6 (c^4 + 11c^3 d x + 55c^2 d^2 x^2 + 165c d^3 x^3 + 330d^4 x^4) + a^5 b^5 d^5 (c^5 + 11c^4 d x + 55c^3 d^2 x^2 + 165c^2 d^3 x^3 + 330c d^4 x^4 + 462d^5 x^5) + a^4 b^6 d^4 (c^6 + 11c^5 d x + 55c^4 d^2 x^2 + 165c^3 d^3 x^3 + 330c^2 d^4 x^4 + 462c d^5 x^5 + 462d^6 x^6) + a^3 b^7 d^3 (c^7 + 11c^6 d x + 55c^5 d^2 x^2 + 165c^4 d^3 x^3 + 330c^3 d^4 x^4 + 462c^2 d^5 x^5 + 462c d^6 x^6 + 330d^7 x^7) + a^2 b^8 d^2 (c^8 + 11c^7 d x + 55c^6 d^2 x^2 + 165c^5 d^3 x^3 + 330c^4 d^4 x^4 + 462c^3 d^5 x^5 + 462c^2 d^6 x^6 + 330c d^7 x^7 + 165d^8 x^8) + a b^9 d (c^9 + 11c^8 d x + 55c^7 d^2 x^2 + 165c^6 d^3 x^3 + 330c^5 d^4 x^4 + 462c^4 d^5 x^5 + 462c^3 d^6 x^6 + 330c^2 d^7 x^7 + 165c d^8 x^8 + 55d^9 x^9) + b^{10} (c^{10} + 11c^9 d x + 55c^8 d^2 x^2 + 165c^7 d^3 x^3 + 330c^6 d^4 x^4 + 462c^5 d^5 x^5 + 462c^4 d^6 x^6 + 330c^3 d^7 x^7 + 165c^2 d^8 x^8 + 55c d^9 x^9 + 11d^{10} x^{10}) / (b^{11} (a + b x)^{11}) \end{aligned}$$

fricas [B] time = 0.45, size = 920, normalized size = 32.86

$$11 b^{10} d^{10} x^{10} + b^{10} c^{10} + a b^9 c^9 d + a^2 b^8 c^8 d^2 + a^3 b^7 c^7 d^3 + a^4 b^6 c^6 d^4 + a^5 b^5 c^5 d^5 + a^6 b^4 c^4 d^6 + a^7 b^3 c^3 d^7 + a^8 b^2 c^2 d^8$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^12,x, algorithm="fricas")

[Out]
$$\begin{aligned} & -1/11 * (11 * b^{10} * d^{10} * x^{10} + b^{10} * c^{10} + a * b^9 * c^9 * d + a^2 * b^8 * c^8 * d^2 + a^3 * b^7 * c^7 * d^3 + a^4 * b^6 * c^6 * d^4 + a^5 * b^5 * c^5 * d^5 + a^6 * b^4 * c^4 * d^6 + a^7 * b^3 * c^3 * d^7 + a^8 * b^2 * c^2 * d^8 + a^9 * b * c * d^9 + a^{10} * d^{10} + 55 * (b^{10} * c * d^9 + a * b^9 * d^{10}) * x^9 + 165 * (b^{10} * c^2 * d^8 + a * b^9 * c * d^9 + a^2 * b^8 * d^{10}) * x^8 + 330 * (b^{10} * c^3 * d^7 + a * b^9 * c^2 * d^8 + a^2 * b^8 * c * d^9 + a^3 * b^7 * d^{10}) * x^7 + 462 * (b^{10} * c^4 * d^6 + a * b^9 * c^3 * d^7 + a^2 * b^8 * c^2 * d^8 + a^3 * b^7 * c * d^9 + a^4 * b^6 * d^{10}) * x^6 + 462 * (b^{10} * c^5 * d^5 + a * b^9 * c^4 * d^6 + a^2 * b^8 * c^3 * d^7 + a^3 * b^7 * c^2 * d^8 + a^4 * b^6 * c * d^9 + a^5 * b^5 * d^{10}) * x^5 + 330 * (b^{10} * c^6 * d^4 + a * b^9 * c^5 * d^5 + a^2 * b^8 * c^4 * d^6 + a^3 * b^7 * c^3 * d^7 + a^4 * b^6 * c^2 * d^8 + a^5 * b^5 * c * d^9 + a^6 * b^4 * d^{10}) * x^4 + 165 * (b^{10} * c^7 * d^3 + a * b^9 * c^6 * d^4 + a^2 * b^8 * c^5 * d^5 + a^3 * b^7 * c^4 * d^6 + a^4 * b^6 * c^3 * d^7 + a^5 * b^5 * c^2 * d^8 + a^6 * b^4 * c * d^9 + a^7 * b^3 * d^{10}) * x^3 + 55 * (b^{10} * c^8 * d^2 + a * b^9 * c^7 * d^3 + a^2 * b^8 * c^6 * d^4 + a^3 * b^7 * c^5 * d^5 + a^4 * b^6 * c^4 * d^6 + a^5 * b^5 * c^3 * d^7 + a^6 * b^4 * c^2 * d^8 + a^7 * b^3 * c * d^9 + a^8 * b^2 * d^{10}) * x^2 + 11 * (b^{10} * c^9 * d + a * b^9 * c^8 * d^2 + a^2 * b^8 * c^7 * d^3 + a^3 * b^7 * c^6 * d^4 + a^4 * b^6 * c^5 * d^5 + a^5 * b^5 * c^4 * d^6 + a^6 * b^4 * c^3 * d^7 + a^7 * b^3 * c^2 * d^8 + a^8 * b^2 * c * d^9 + a^9 * b * d^{10}) * x) / (b^{22} * x^{11} + 11 * a * b^{21} * x^{10} + 55 * a^2 * b^{20} * x^9 + 165 * a^3 * b^{19} * x^8 + 330 * a^4 * b^{18} * x^7 + 462 * a^5 * b^{17} * x^6 + 462 * a^6 * b^{16} * x^5 + 330 * a^7 * b^{15} * x^4 + 165 * a^8 * b^{14} * x^3 + 55 * a^9 * b^{13} * x^2 + 11 * a^{10} * b^{12} * x + a^{11} * b^{11}) \end{aligned}$$

giac [B] time = 1.36, size = 951, normalized size = 33.96

$$\frac{11 b^{10} d^{10} x^{10} + 55 b^{10} c d^9 x^9 + 55 a b^9 d^{10} x^9 + 165 b^{10} c^2 d^8 x^8 + 165 a b^9 c d^9 x^8 + 165 a^2 b^8 d^{10} x^8 + 330 b^{10} c^3 d^7 x^7 + 330 a b^9 c^2 d^8 x^7 + 330 a^2 b^8 c d^9 x^7 + 330 a^3 b^7 d^{10} x^7 + 462 b^{10} c^4 d^6 x^6 + 462 a b^9 c^3 d^7 x^6 + 462 a^2 b^8 c^2 d^8 x^6 + 462 a^3 b^7 c d^9 x^6 + 462 a^4 b^6 d^{10} x^6 + 462 b^{10} c^5 d^5 x^5 + 462 a b^9 c^4 d^6 x^5 + 462 a^2 b^8 c^3 d^7 x^5 + 462 a^3 b^7 c^2 d^8 x^5 + 462 a^4 b^6 c d^9 x^5 + 462 a^5 b^5 d^{10} x^5 + 330 b^{10} c^6 d^4 x^4 + 330 a b^9 c^5 d^5 x^4 + 330 a^2 b^8 c^4 d^6 x^4 + 330 a^3 b^7 c^3 d^7 x^4 + 330 a^4 b^6 c^2 d^8 x^4 + 330 a^5 b^5 c d^9 x^4 + 330 a^6 b^4 d^{10} x^4 + 165 b^{10} c^7 d^3 x^3 + 165 a b^9 c^6 d^4 x^3 + 165 a^2 b^8 c^5 d^5 x^3 + 165 a^3 b^7 c^4 d^6 x^3 + 165 a^4 b^6 c^3 d^7 x^3 + 165 a^5 b^5 c^2 d^8 x^3 + 165 a^6 b^4 c d^9 x^3 + 165 a^7 b^3 d^{10} x^3 + 55 b^{10} c^8 d^2 x^2 + 55 a b^9 c^7 d^3 x^2 + 55 a^2 b^8 c^6 d^4 x^2 + 55 a^3 b^7 c^5 d^5 x^2 + 55 a^4 b^6 c^4 d^6 x^2 + 55 a^5 b^5 c^3 d^7 x^2 + 55 a^6 b^4 c^2 d^8 x^2 + 55 a^7 b^3 c d^9 x^2 + 55 a^8 b^2 d^{10} x^2 + 11 b^{10} c^9 d x + 11 a b^9 c^8 d^2 x + 11 a^2 b^8 c^7 d^3 x + 11 a^3 b^7 c^6 d^4 x + 11 a^4 b^6 c^5 d^5 x + 11 a^5 b^5 c^4 d^6 x + 11 a^6 b^4 c^3 d^7 x + 11 a^7 b^3 c^2 d^8 x + 11 a^8 b^2 c d^9 x + 11 a^9 b d^{10} x + b^{10} c^{10} + a b^9 c^9 d + a^2 b^8 c^8 d^2 + a^3 b^7 c^7 d^3 + a^4 b^6 c^6 d^4 + a^5 b^5 c^5 d^5 + a^6 b^4 c^4 d^6 + a^7 b^3 c^3 d^7 + a^8 b^2 c^2 d^8 + a^9 b c d^9 + a^{10} d^{10}) / ((b x + a)^{11} b^{11})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^12,x, algorithm="giac")

[Out]
$$-1/11*(11*b^{10}*d^{10}*x^{10} + 55*b^{10}*c*d^9*x^9 + 55*a*b^9*d^{10}*x^9 + 165*b^{10}*c^2*d^8*x^8 + 165*a*b^9*c*d^9*x^8 + 165*a^2*b^8*d^{10}*x^8 + 330*b^{10}*c^3*d^7*x^7 + 330*a*b^9*c^2*d^8*x^7 + 330*a^2*b^8*c*d^9*x^7 + 330*a^3*b^7*d^{10}*x^7 + 462*b^{10}*c^4*d^6*x^6 + 462*a*b^9*c^3*d^7*x^6 + 462*a^2*b^8*c^2*d^8*x^6 + 462*a^3*b^7*c*d^9*x^6 + 462*a^4*b^6*d^{10}*x^6 + 462*b^{10}*c^5*d^5*x^5 + 462*a*b^9*c^4*d^6*x^5 + 462*a^2*b^8*c^3*d^7*x^5 + 462*a^3*b^7*c^2*d^8*x^5 + 462*a^4*b^6*c*d^9*x^5 + 462*a^5*b^5*d^{10}*x^5 + 330*b^{10}*c^6*d^4*x^4 + 330*a*b^9*c^5*d^5*x^4 + 330*a^2*b^8*c^4*d^6*x^4 + 330*a^3*b^7*c^3*d^7*x^4 + 330*a^4*b^6*c^2*d^8*x^4 + 330*a^5*b^5*c*d^9*x^4 + 330*a^6*b^4*d^{10}*x^4 + 165*b^{10}*c^7*d^3*x^3 + 165*a*b^9*c^6*d^4*x^3 + 165*a^2*b^8*c^5*d^5*x^3 + 165*a^3*b^7*c^4*d^6*x^3 + 165*a^4*b^6*c^3*d^7*x^3 + 165*a^5*b^5*c^2*d^8*x^3 + 165*a^6*b^4*c*d^9*x^3 + 165*a^7*b^3*d^{10}*x^3 + 55*b^{10}*c^8*d^2*x^2 + 55*a*b^9*c^7*d^3*x^2 + 55*a^2*b^8*c^6*d^4*x^2 + 55*a^3*b^7*c^5*d^5*x^2 + 55*a^4*b^6*c^4*d^6*x^2 + 55*a^5*b^5*c^3*d^7*x^2 + 55*a^6*b^4*c^2*d^8*x^2 + 55*a^7*b^3*c*d^9*x^2 + 55*a^8*b^2*d^{10}*x^2 + 11*b^{10}*c^9*d*x + 11*a*b^9*c^8*d^2*x + 11*a^2*b^8*c^7*d^3*x + 11*a^3*b^7*c^6*d^4*x + 11*a^4*b^6*c^5*d^5*x + 11*a^5*b^5*c^4*d^6*x + 11*a^6*b^4*c^3*d^7*x + 11*a^7*b^3*c^2*d^8*x + 11*a^8*b^2*c*d^9*x + 11*a^9*b*d^{10}*x + b^{10}*c^{10} + a*b^9*c^9*d + a^2*b^8*c^8*d^2 + a^3*b^7*c^7*d^3 + a^4*b^6*c^6*d^4 + a^5*b^5*c^5*d^5 + a^6*b^4*c^4*d^6 + a^7*b^3*c^3*d^7 + a^8*b^2*c^2*d^8 + a^9*b*c*d^9 + a^{10}*d^{10}) / ((b*x + a)^{11} b^{11})$$

maple [B] time = 0.01, size = 866, normalized size = 30.93

$$\frac{d^{10}}{(bx+a)b^{11}} + \frac{5(ad-bc)d^9}{(bx+a)^2 b^{11}} - \frac{15(a^2 d^2 - 2abcd + b^2 c^2)d^8}{(bx+a)^3 b^{11}} + \frac{30(a^3 d^3 - 3a^2 bc d^2 + 3a b^2 c^2 d - b^3 c^3)d^7}{(bx+a)^4 b^{11}} - \frac{42(a^4 d^4)}{(bx+a)^5 b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^12,x)

[Out]
$$15*d^3*(a^7*d^7-7*a^6*b*c*d^6+21*a^5*b^2*c^2*d^5-35*a^4*b^3*c^3*d^4+35*a^3*b^4*c^4*d^3-21*a^2*b^5*c^5*d^2+7*a*b^6*c^6*d-b^7*c^7)/b^{11}/(b*x+a)^8-15*d^8*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^{11}/(b*x+a)^3-30*d^4*(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^{11}/(b*x+a)^7-5*d^2*(a^8*d^8-8*a^7*b*c*d^7+28*a^6*b^2*c^2*d^6-56*a^5*b^3*c^3*d^5+70*a^4*b^4*c^4*d^4-56*a^3*b^5*c^5*d^3+28*a^2*b^6*c^6*d^2-8*a*b^7*c^7)/b^{11}/(b*x+a)^5$$

$$\frac{c^7 d + b^8 c^8}{b^{11} (b x + a)^9} - 42 d^6 (a^4 d^4 - 4 a^3 b c d^3 + 6 a^2 b^2 c^2 d^2 - 4 a b^3 c^3 d + b^4 c^4) / b^{11} (b x + a)^5 + 5 d^9 (a d - b c) / b^{11} (b x + a)^2 + 30 d^7 (a^3 d^3 - 3 a^2 b c d^2 + 3 a b^2 c^2 d - b^3 c^3) / b^{11} (b x + a)^4 - 1/11 (a^{10} d^{10} - 10 a^9 b c d^9 + 45 a^8 b^2 c^2 d^8 - 120 a^7 b^3 c^3 d^7 + 210 a^6 b^4 c^4 d^6 - 252 a^5 b^5 c^5 d^5 + 210 a^4 b^6 c^6 d^4 - 120 a^3 b^7 c^7 d^3 + 45 a^2 b^8 c^8 d^2 - 10 a b^9 c^9 d + b^{10} c^{10}) / b^{11} (b x + a)^{11} - d^{10} / b^{11} (b x + a) + 42 d^5 (a^5 d^5 - 5 a^4 b c d^4 + 10 a^3 b^2 c^2 d^3 - 10 a^2 b^3 c^3 d^2 + 5 a b^4 c^4 d - b^5 c^5) / b^{11} (b x + a)^6 + d (a^9 d^9 - 9 a^8 b c d^8 + 36 a^7 b^2 c^2 d^7 - 84 a^6 b^3 c^3 d^6 + 126 a^5 b^4 c^4 d^5 - 126 a^4 b^5 c^5 d^4 + 84 a^3 b^6 c^6 d^3 - 36 a^2 b^7 c^7 d^2 + 9 a b^8 c^8 d - b^9 c^9) / b^{11} (b x + a)^{10}$$

maxima [B] time = 2.13, size = 920, normalized size = 32.86

$$\frac{11 b^{10} d^{10} x^{10} + b^{10} c^{10} + a b^9 c^9 d + a^2 b^8 c^8 d^2 + a^3 b^7 c^7 d^3 + a^4 b^6 c^6 d^4 + a^5 b^5 c^5 d^5 + a^6 b^4 c^4 d^6 + a^7 b^3 c^3 d^7 + a^8 b^2 c^2 d^8}{b^{11} (b x + a)^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^12,x, algorithm="maxima")

[Out]
$$\frac{-1/11 (11 b^{10} d^{10} x^{10} + b^{10} c^{10} + a b^9 c^9 d + a^2 b^8 c^8 d^2 + a^3 b^7 c^7 d^3 + a^4 b^6 c^6 d^4 + a^5 b^5 c^5 d^5 + a^6 b^4 c^4 d^6 + a^7 b^3 c^3 d^7 + a^8 b^2 c^2 d^8 + a^9 b c d^9 + a^{10} d^{10}) x^9 + 165 (b^{10} c^2 d^8 + a b^9 c d^9 + a^2 b^8 d^{10}) x^8 + 330 (b^{10} c^3 d^7 + a b^9 c^2 d^8 + a^2 b^8 c d^9 + a^3 b^7 d^{10}) x^7 + 462 (b^{10} c^4 d^6 + a b^9 c^3 d^7 + a^2 b^8 c^2 d^8 + a^3 b^7 c d^9 + a^4 b^6 d^{10}) x^6 + 462 (b^{10} c^5 d^5 + a b^9 c^4 d^6 + a^2 b^8 c^3 d^7 + a^3 b^7 c^2 d^8 + a^4 b^6 c d^9 + a^5 b^5 d^{10}) x^5 + 330 (b^{10} c^6 d^4 + a b^9 c^5 d^5 + a^2 b^8 c^4 d^6 + a^3 b^7 c^3 d^7 + a^4 b^6 c^2 d^8 + a^5 b^5 c d^9 + a^6 b^4 d^{10}) x^4 + 165 (b^{10} c^7 d^3 + a b^9 c^6 d^4 + a^2 b^8 c^5 d^5 + a^3 b^7 c^4 d^6 + a^4 b^6 c^3 d^7 + a^5 b^5 c^2 d^8 + a^6 b^4 c d^9 + a^7 b^3 d^{10}) x^3 + 55 (b^{10} c^8 d^2 + a b^9 c^7 d^3 + a^2 b^8 c^6 d^4 + a^3 b^7 c^5 d^5 + a^4 b^6 c^4 d^6 + a^5 b^5 c^3 d^7 + a^6 b^4 c^2 d^8 + a^7 b^3 c d^9 + a^8 b^2 d^{10}) x^2 + 11 (b^{10} c^9 d + a b^9 c^8 d^2 + a^2 b^8 c^7 d^3 + a^3 b^7 c^6 d^4 + a^4 b^6 c^5 d^5 + a^5 b^5 c^4 d^6 + a^6 b^4 c^3 d^7 + a^7 b^3 c^2 d^8 + a^8 b^2 c d^9 + a^9 b d^{10}) x + 11 a^{10} b^{12} x + a^{11} b^{11}}$$

mupad [B] time = 0.46, size = 1066, normalized size = 38.07

$$\frac{a^{10} d^{10} + a^9 b c d^9 + 11 a^9 b d^{10} x + a^8 b^2 c^2 d^8 + 11 a^8 b^2 c d^9 x + 55 a^8 b^2 d^{10} x^2 + a^7 b^3 c^3 d^7 + 11 a^7 b^3 c^2 d^8 x + 462 a^6 b^4 c^3 d^7 + 462 a^6 b^4 c^2 d^8 x + 330 a^6 b^4 c d^9 + 330 a^6 b^4 d^{10} x^2 + 165 a^5 b^5 c^4 d^6 + 165 a^5 b^5 c^3 d^7 + 165 a^5 b^5 c^2 d^8 x + 165 a^5 b^5 c d^9 + 165 a^5 b^5 d^{10} x^2 + 11 a^4 b^6 c^5 d^5 + 11 a^4 b^6 c^4 d^6 + 11 a^4 b^6 c^3 d^7 + 11 a^4 b^6 c^2 d^8 x + 11 a^4 b^6 c d^9 + 11 a^4 b^6 d^{10} x^2 + 55 a^3 b^7 c^6 d^4 + 55 a^3 b^7 c^5 d^5 + 55 a^3 b^7 c^4 d^6 + 55 a^3 b^7 c^3 d^7 + 55 a^3 b^7 c^2 d^8 x + 55 a^3 b^7 c d^9 + 55 a^3 b^7 d^{10} x^2 + 165 a^2 b^8 c^7 d^3 + 165 a^2 b^8 c^6 d^4 + 165 a^2 b^8 c^5 d^5 + 165 a^2 b^8 c^4 d^6 + 165 a^2 b^8 c^3 d^7 + 165 a^2 b^8 c^2 d^8 x + 165 a^2 b^8 c d^9 + 165 a^2 b^8 d^{10} x^2 + 330 a b^9 c^8 d^2 + 330 a b^9 c^7 d^3 + 330 a b^9 c^6 d^4 + 330 a b^9 c^5 d^5 + 330 a b^9 c^4 d^6 + 330 a b^9 c^3 d^7 + 330 a b^9 c^2 d^8 x + 330 a b^9 c d^9 + 330 a b^9 d^{10} x^2 + 11 a^{10} b^{12} x + 11 a^{11} b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^10/(a + b*x)^12,x)`

[Out]
$$-(a^{10}d^{10} + b^{10}c^{10} + 11b^{10}d^{10}x^{10} + 55a^9b^9d^{10}x^9 + 55b^{10}c^9d^9x^9 + a^2b^8c^8d^2 + a^3b^7c^7d^3 + a^4b^6c^6d^4 + a^5b^5c^5d^5 + a^6b^4c^4d^6 + a^7b^3c^3d^7 + a^8b^2c^2d^8 + 55a^8b^2d^{10}x^2 + 165a^7b^3d^{10}x^3 + 330a^6b^4d^{10}x^4 + 462a^5b^5d^{10}x^5 + 462a^4b^6d^{10}x^6 + 330a^3b^7d^{10}x^7 + 165a^2b^8d^{10}x^8 + 55b^{10}c^8d^2x^2 + 165b^{10}c^7d^3x^3 + 330b^{10}c^6d^4x^4 + 462b^{10}c^5d^5x^5 + 462b^{10}c^4d^6x^6 + 330b^{10}c^3d^7x^7 + 165b^{10}c^2d^8x^8 + ab^9c^9d + a^9b^9c^9d + 11a^9b^9d^{10}x + 11b^{10}c^9d^9x + 55a^2b^8c^6d^4x^2 + 55a^3b^7c^5d^5x^2 + 55a^4b^6c^4d^6x^2 + 55a^5b^5c^3d^7x^2 + 55a^6b^4c^2d^8x^2 + 165a^2b^8c^5d^5x^3 + 165a^3b^7c^4d^6x^3 + 165a^4b^6c^3d^7x^3 + 165a^5b^5c^2d^8x^3 + 330a^2b^8c^4d^6x^4 + 330a^3b^7c^3d^7x^4 + 330a^4b^6c^2d^8x^4 + 462a^2b^8c^3d^7x^5 + 462a^3b^7c^2d^8x^5 + 462a^2b^8c^2d^8x^6 + 11a^9b^9c^8d^2x + 11a^8b^9c^8d^2x + 165a^9b^9c^8d^2x^8 + 11a^2b^8c^7d^3x + 11a^3b^7c^6d^4x + 11a^4b^6c^5d^5x + 11a^5b^5c^4d^6x + 11a^6b^4c^3d^7x + 11a^7b^3c^2d^8x + 55a^9b^9c^7d^3x^2 + 55a^7b^3c^9d^9x^2 + 165a^9b^9c^6d^4x^3 + 165a^6b^4c^9d^9x^3 + 330a^9b^9c^5d^5x^4 + 330a^5b^5c^9d^9x^4 + 462a^9b^9c^4d^6x^5 + 462a^4b^6c^9d^9x^5 + 462a^9b^9c^3d^7x^6 + 462a^3b^7c^9d^9x^6 + 330a^9b^9c^2d^8x^7 + 330a^2b^8c^9d^9x^7)/(11a^{11}b^{11} + 11b^{22}x^{11} + 121a^{10}b^{12}x + 121a^9b^{13}x^2 + 605a^8b^{14}x^3 + 3630a^7b^{15}x^4 + 5082a^6b^{16}x^5 + 5082a^5b^{17}x^6 + 3630a^4b^{18}x^7 + 1815a^3b^{19}x^8 + 605a^2b^{20}x^9)$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**10/(b*x+a)**12,x)`

[Out] Timed out

$$3.1324 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{13}} dx$$

Optimal. Leaf size=58

$$\frac{d(c+dx)^{11}}{132(a+bx)^{11}(bc-ad)^2} - \frac{(c+dx)^{11}}{12(a+bx)^{12}(bc-ad)}$$

[Out] $-1/12*(d*x+c)^{11}/(-a*d+b*c)/(b*x+a)^{12}+1/132*d*(d*x+c)^{11}/(-a*d+b*c)^2/(b*x+a)^{11}$

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{d(c+dx)^{11}}{132(a+bx)^{11}(bc-ad)^2} - \frac{(c+dx)^{11}}{12(a+bx)^{12}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^13,x]

[Out] $-(c+d*x)^{11}/(12*(b*c-a*d)*(a+b*x)^{12})+(d*(c+d*x)^{11})/(132*(b*c-a*d)^2*(a+b*x)^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[m] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{(c+dx)^{10}}{(a+bx)^{13}} dx = -\frac{(c+dx)^{11}}{12(bc-ad)(a+bx)^{12}} - \frac{d \int \frac{(c+dx)^{10}}{(a+bx)^{12}} dx}{12(bc-ad)}$$

$$= -\frac{(c+dx)^{11}}{12(bc-ad)(a+bx)^{12}} + \frac{d(c+dx)^{11}}{132(bc-ad)^2(a+bx)^{11}}$$

Mathematica [B] time = 0.28, size = 684, normalized size = 11.79

$$a^{10}d^{10} + 2a^9bd^9(c + 6dx) + 3a^8b^2d^8(c^2 + 8cdx + 22d^2x^2) + 4a^7b^3d^7(c^3 + 9c^2dx + 33cd^2x^2 + 55d^3x^3) + a^6b^4d^6$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^13,x]

[Out] -1/132*(a^10*d^10 + 2*a^9*b*d^9*(c + 6*d*x) + 3*a^8*b^2*d^8*(c^2 + 8*c*d*x + 22*d^2*x^2) + 4*a^7*b^3*d^7*(c^3 + 9*c^2*d*x + 33*c*d^2*x^2 + 55*d^3*x^3) + a^6*b^4*d^6*(5*c^4 + 48*c^3*d*x + 198*c^2*d^2*x^2 + 440*c*d^3*x^3 + 495*d^4*x^4) + 6*a^5*b^5*d^5*(c^5 + 10*c^4*d*x + 44*c^3*d^2*x^2 + 110*c^2*d^3*x^3 + 165*c*d^4*x^4 + 132*d^5*x^5) + a^4*b^6*d^4*(7*c^6 + 72*c^5*d*x + 330*c^4*d^2*x^2 + 880*c^3*d^3*x^3 + 1485*c^2*d^4*x^4 + 1584*c*d^5*x^5 + 924*d^6*x^6) + 4*a^3*b^7*d^3*(2*c^7 + 21*c^6*d*x + 99*c^5*d^2*x^2 + 275*c^4*d^3*x^3 + 495*c^3*d^4*x^4 + 594*c^2*d^5*x^5 + 462*c*d^6*x^6 + 198*d^7*x^7) + 3*a^2*b^8*d^2*(3*c^8 + 32*c^7*d*x + 154*c^6*d^2*x^2 + 440*c^5*d^3*x^3 + 825*c^4*d^4*x^4 + 1056*c^3*d^5*x^5 + 924*c^2*d^6*x^6 + 528*c*d^7*x^7 + 165*d^8*x^8) + 2*a*b^9*d*(5*c^9 + 54*c^8*d*x + 264*c^7*d^2*x^2 + 770*c^6*d^3*x^3 + 1485*c^5*d^4*x^4 + 1980*c^4*d^5*x^5 + 1848*c^3*d^6*x^6 + 1188*c^2*d^7*x^7 + 495*c*d^8*x^8 + 110*d^9*x^9) + b^10*(11*c^10 + 120*c^9*d*x + 594*c^8*d^2*x^2 + 1760*c^7*d^3*x^3 + 3465*c^6*d^4*x^4 + 4752*c^5*d^5*x^5 + 4620*c^4*d^6*x^6 + 3168*c^3*d^7*x^7 + 1485*c^2*d^8*x^8 + 440*c*d^9*x^9 + 66*d^10*x^10))/(b^11*(a + b*x)^12)

fricas [B] time = 0.46, size = 986, normalized size = 17.00

$$66b^{10}d^{10}x^{10} + 11b^{10}c^{10} + 10ab^9c^9d + 9a^2b^8c^8d^2 + 8a^3b^7c^7d^3 + 7a^4b^6c^6d^4 + 6a^5b^5c^5d^5 + 5a^6b^4c^4d^6 + 4a^7b^3c^3d^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^13,x, algorithm="fricas")

[Out] -1/132*(66*b^10*d^10*x^10 + 11*b^10*c^10 + 10*a*b^9*c^9*d + 9*a^2*b^8*c^8*d^2 + 8*a^3*b^7*c^7*d^3 + 7*a^4*b^6*c^6*d^4 + 6*a^5*b^5*c^5*d^5 + 5*a^6*b^4*c^4*d^6

$$\begin{aligned}
& c^4d^6 + 4a^7b^3c^3d^7 + 3a^8b^2c^2d^8 + 2a^9b^1c^1d^9 + a^{10}d^{10} \\
& + 220(2b^{10}c^1d^9 + ab^9d^{10})x^9 + 495(3b^{10}c^2d^8 + 2a^2b^9c^1d^9 \\
& + a^2b^8d^{10})x^8 + 792(4b^{10}c^3d^7 + 3a^3b^9c^2d^8 + 2a^2b^8c^1d^9 \\
& + a^3b^7d^{10})x^7 + 924(5b^{10}c^4d^6 + 4a^4b^9c^3d^7 + 3a^2b^8c^2d^8 \\
& + 2a^3b^7c^1d^9 + a^4b^6d^{10})x^6 + 792(6b^{10}c^5d^5 + 5a^5b^9c^4d^6 \\
& + 4a^2b^8c^3d^7 + 3a^3b^7c^2d^8 + 2a^4b^6c^1d^9 + a^5b^5d^{10})x^5 \\
& + 495(7b^{10}c^6d^4 + 6a^6b^9c^5d^5 + 5a^2b^8c^4d^6 \\
& + 4a^3b^7c^3d^7 + 3a^4b^6c^2d^8 + 2a^5b^5c^1d^9 + a^6b^4d^{10})x^4 \\
& + 220(8b^{10}c^7d^3 + 7a^7b^9c^6d^4 + 6a^2b^8c^5d^5 + 5a^3b^7c^4d^6 \\
& + 4a^4b^6c^3d^7 + 3a^5b^5c^2d^8 + 2a^6b^4c^1d^9 + a^7b^3d^{10})x^3 \\
& + 66(9b^{10}c^8d^2 + 8a^8b^9c^7d^3 + 7a^2b^8c^6d^4 + 6a^3b^7c^5d^5 \\
& + 5a^4b^6c^4d^6 + 4a^5b^5c^3d^7 + 3a^6b^4c^2d^8 \\
& + 2a^7b^3c^1d^9 + a^8b^2d^{10})x^2 + 12(10b^{10}c^9d + 9a^8b^9c^8d^2 \\
& + 8a^2b^8c^7d^3 + 7a^3b^7c^6d^4 + 6a^4b^6c^5d^5 + 5a^5b^5c^4d^6 \\
& + 4a^6b^4c^3d^7 + 3a^7b^3c^2d^8 + 2a^8b^2c^1d^9 + a^9b^1d^{10})x \\
&) / (b^{23}x^{12} + 12a^1b^{22}x^{11} + 66a^2b^{21}x^{10} + 220a^3b^{20}x^9 + \\
& 495a^4b^{19}x^8 + 792a^5b^{18}x^7 + 924a^6b^{17}x^6 + 792a^7b^{16}x^5 + \\
& 495a^8b^{15}x^4 + 220a^9b^{14}x^3 + 66a^{10}b^{13}x^2 + 12a^{11}b^{12}x + \\
& a^{12}b^{11})
\end{aligned}$$

giac [B] time = 1.32, size = 961, normalized size = 16.57

$$66 b^{10} d^{10} x^{10} + 440 b^{10} c d^9 x^9 + 220 a b^9 d^{10} x^9 + 1485 b^{10} c^2 d^8 x^8 + 990 a b^9 c d^9 x^8 + 495 a^2 b^8 d^{10} x^8 + 3168 b^{10} c^3 d^7 x^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^13,x, algorithm="giac")

[Out] $-1/132(66b^{10}d^{10}x^{10} + 440b^{10}c^1d^9x^9 + 220a^1b^9c^1d^{10}x^9 + 1485b^{10}c^2d^8x^8 + 990a^2b^8c^2d^9x^8 + 495a^3b^7c^3d^{10}x^8 + 3168b^{10}c^4d^7x^7 + 2376a^4b^6c^4d^8x^7 + 1584a^5b^5c^5d^9x^7 + 792a^6b^4c^6d^{10}x^7 + 4620b^{10}c^6d^6x^6 + 3696a^7b^3c^6d^7x^6 + 2772a^8b^2c^7d^8x^6 + 1848a^9b^1c^8d^9x^6 + 924a^{10}b^0c^9d^{10}x^6 + 4752b^{10}c^8d^5x^5 + 3960a^1b^9c^8d^6x^5 + 3168a^2b^8c^9d^7x^5 + 2376a^3b^7c^{10}d^8x^5 + 1584a^4b^6c^{11}d^9x^5 + 792a^5b^5c^{12}d^{10}x^5 + 3465b^{10}c^{13}d^4x^4 + 2970a^1b^9c^{14}d^5x^4 + 2475a^2b^8c^{15}d^6x^4 + 1980a^3b^7c^{16}d^7x^4 + 1485a^4b^6c^{17}d^8x^4 + 990a^5b^5c^{18}d^9x^4 + 495a^6b^4c^{19}d^{10}x^4 + 1760b^{10}c^{20}d^3x^3 + 1540a^1b^9c^{21}d^4x^3 + 1320a^2b^8c^{22}d^5x^3 + 1100a^3b^7c^{23}d^6x^3 + 880a^4b^6c^{24}d^7x^3 + 660a^5b^5c^{25}d^8x^3 + 440a^6b^4c^{26}d^9x^3 + 220a^7b^3c^{27}d^{10}x^3 + 594b^{10}c^{28}d^2x^2 + 528a^1b^9c^{29}d^3x^2 + 462a^2b^8c^{30}d^4x^2 + 396a^3b^7c^{31}d^5x^2 + 330a^4b^6c^{32}d^6x^2 + 264a^5b^5c^{33}d^7x^2 + 198a^6b^4c^{34}d^8x^2 + 132a^7b^3c^{35}d^9x^2 + 66a^8b^2c^{36}d^{10}x^2 + 120b^{10}c^{37}d^1x + 108a^1b^9c^{38}d^2x + 96a^2b^8c^{39}d^3x + 84a^3b^7c^{40}d^4x +$

$$72a^4b^6c^5d^5x + 60a^5b^5c^4d^6x + 48a^6b^4c^3d^7x + 36a^7b^3c^2d^8x + 24a^8b^2c^1d^9x + 12a^9b^1d^{10}x + 11b^{10}c^{10} + 10ab^9c^9d + 9a^2b^8c^8d^2 + 8a^3b^7c^7d^3 + 7a^4b^6c^6d^4 + 6a^5b^5c^5d^5 + 5a^6b^4c^4d^6 + 4a^7b^3c^3d^7 + 3a^8b^2c^2d^8 + 2a^9b^1c^1d^9 + a^{10}d^{10} / ((bx + a)^{12}b^{11})$$

maple [B] time = 0.01, size = 867, normalized size = 14.95

$$\frac{d^{10}}{2(bx+a)^2b^{11}} + \frac{10(ad-bc)d^9}{3(bx+a)^3b^{11}} - \frac{45(a^2d^2-2abcd+b^2c^2)d^8}{4(bx+a)^4b^{11}} + \frac{24(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^7}{(bx+a)^5b^{11}} - \frac{35(a^4d^4-4a^3bcd^3+6a^2b^2c^2d^2-4ab^3c^3d-b^4c^4)d^6}{(bx+a)^6b^{11}} + \frac{35(a^5d^5-5a^4b^1cd^4+10a^3b^2c^2d^3-10a^2b^3c^3d^2+5a^1b^4c^4d-b^5c^5)d^5}{(bx+a)^7b^{11}} - \frac{35(a^6d^6-6a^5b^1c^1d^5+15a^4b^2c^2d^4-20a^3b^3c^3d^3+15a^2b^4c^4d^2-6a^1b^5c^5d+b^6c^6)d^4}{(bx+a)^8b^{11}} - \frac{35(a^7d^7-7a^6b^1c^1d^6+21a^5b^2c^2d^5-35a^4b^3c^3d^4+35a^3b^4c^4d^3-21a^2b^5c^5d^2+7a^1b^6c^6d-b^7c^7)d^3}{(bx+a)^9b^{11}} - \frac{35(a^8d^8-8a^7b^1c^1d^7+28a^6b^2c^2d^6-56a^5b^3c^3d^5+70a^4b^4c^4d^4-56a^3b^5c^5d^3+28a^2b^6c^6d^2-8a^1b^7c^7d+b^8c^8)d^2}{(bx+a)^{10}b^{11}} - \frac{35(a^9d^9-9a^8b^1c^1d^8+36a^7b^2c^2d^7-84a^6b^3c^3d^6+126a^5b^4c^4d^5-126a^4b^5c^5d^4+84a^3b^6c^6d^3-36a^2b^7c^7d^2+9a^1b^8c^8d-b^9c^9)d}{(bx+a)^{11}b^{11}} - \frac{35(a^{10}d^{10}-10a^9b^1c^1d^9+45a^8b^2c^2d^8-120a^7b^3c^3d^7+210a^6b^4c^4d^6-252a^5b^5c^5d^5+210a^4b^6c^6d^4-120a^3b^7c^7d^3+45a^2b^8c^8d^2-10a^1b^9c^9d+b^{10}c^{10})}{(bx+a)^{12}b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^13,x)

[Out]
$$-105/4*d^4*(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^{11}/(b*x+a)^8+10/3*d^9*(a*d-b*c)/b^{11}/(b*x+a)^3+36*d^5*(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)/b^{11}/(b*x+a)^7+40/3*d^3*(a^7*d^7-7*a^6*b*c*d^6+21*a^5*b^2*c^2*d^5-35*a^4*b^3*c^3*d^4+35*a^3*b^4*c^4*d^3-21*a^2*b^5*c^5*d^2+7*a*b^6*c^6*d-b^7*c^7)/b^{11}/(b*x+a)^9+24*d^7*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^{11}/(b*x+a)^5-1/2*d^{10}/b^{11}/(b*x+a)^2-45/4*d^8*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^{11}/(b*x+a)^4+10/11*d*(a^9*d^9-9*a^8*b*c*d^8+36*a^7*b^2*c^2*d^7-84*a^6*b^3*c^3*d^6+126*a^5*b^4*c^4*d^5-126*a^4*b^5*c^5*d^4+84*a^3*b^6*c^6*d^3-36*a^2*b^7*c^7*d^2+9*a*b^8*c^8*d-b^9*c^9)/b^{11}/(b*x+a)^{11}-1/12*(a^{10}*d^{10}-10*a^9*b*c*d^9+45*a^8*b^2*c^2*d^8-120*a^7*b^3*c^3*d^7+210*a^6*b^4*c^4*d^6-252*a^5*b^5*c^5*d^5+210*a^4*b^6*c^6*d^4-120*a^3*b^7*c^7*d^3+45*a^2*b^8*c^8*d^2-10*a*b^9*c^9*d+b^{10}*c^{10})/b^{11}/(b*x+a)^{12}-35*d^6*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/b^{11}/(b*x+a)^6-9/2*d^2*(a^8*d^8-8*a^7*b*c*d^7+28*a^6*b^2*c^2*d^6-56*a^5*b^3*c^3*d^5+70*a^4*b^4*c^4*d^4-56*a^3*b^5*c^5*d^3+28*a^2*b^6*c^6*d^2-8*a*b^7*c^7*d+b^8*c^8)/b^{11}/(b*x+a)^{10}$$

maxima [B] time = 2.17, size = 986, normalized size = 17.00

$$\frac{66b^{10}d^{10}x^{10} + 11b^{10}c^{10} + 10ab^9c^9d + 9a^2b^8c^8d^2 + 8a^3b^7c^7d^3 + 7a^4b^6c^6d^4 + 6a^5b^5c^5d^5 + 5a^6b^4c^4d^6 + 4a^7b^3c^3d^7 + 3a^8b^2c^2d^8 + 2a^9b^1c^1d^9 + a^{10}d^{10}}{(bx+a)^{12}b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^13,x, algorithm="maxima")

[Out]
$$-1/132*(66*b^{10}*d^{10}*x^{10} + 11*b^{10}*c^{10} + 10*a*b^9*c^9*d + 9*a^2*b^8*c^8*d^2 + 8*a^3*b^7*c^7*d^3 + 7*a^4*b^6*c^6*d^4 + 6*a^5*b^5*c^5*d^5 + 5*a^6*b^4*c^4*d^6 + 4*a^7*b^3*c^3*d^7 + 3*a^8*b^2*c^2*d^8 + 2*a^9*b^1*c^1*d^9 + a^{10}*d^{10})/((bx+a)^{12}b^{11})$$


```

+ 220*(2*b^10*c*d^9 + a*b^9*d^10)*x^9 + 495*(3*b^10*c^2*d^8 + 2*a*b^9*c*d^
9 + a^2*b^8*d^10)*x^8 + 792*(4*b^10*c^3*d^7 + 3*a*b^9*c^2*d^8 + 2*a^2*b^8*c
*d^9 + a^3*b^7*d^10)*x^7 + 924*(5*b^10*c^4*d^6 + 4*a*b^9*c^3*d^7 + 3*a^2*b^
8*c^2*d^8 + 2*a^3*b^7*c*d^9 + a^4*b^6*d^10)*x^6 + 792*(6*b^10*c^5*d^5 + 5*a
*b^9*c^4*d^6 + 4*a^2*b^8*c^3*d^7 + 3*a^3*b^7*c^2*d^8 + 2*a^4*b^6*c*d^9 + a^
5*b^5*d^10)*x^5 + 495*(7*b^10*c^6*d^4 + 6*a*b^9*c^5*d^5 + 5*a^2*b^8*c^4*d^6
+ 4*a^3*b^7*c^3*d^7 + 3*a^4*b^6*c^2*d^8 + 2*a^5*b^5*c*d^9 + a^6*b^4*d^10)*
x^4 + 220*(8*b^10*c^7*d^3 + 7*a*b^9*c^6*d^4 + 6*a^2*b^8*c^5*d^5 + 5*a^3*b^7
*c^4*d^6 + 4*a^4*b^6*c^3*d^7 + 3*a^5*b^5*c^2*d^8 + 2*a^6*b^4*c*d^9 + a^7*b^
3*d^10)*x^3 + 66*(9*b^10*c^8*d^2 + 8*a*b^9*c^7*d^3 + 7*a^2*b^8*c^6*d^4 + 6*
a^3*b^7*c^5*d^5 + 5*a^4*b^6*c^4*d^6 + 4*a^5*b^5*c^3*d^7 + 3*a^6*b^4*c^2*d^8
+ 2*a^7*b^3*c*d^9 + a^8*b^2*d^10)*x^2 + 12*(10*b^10*c^9*d + 9*a*b^9*c^8*d^
2 + 8*a^2*b^8*c^7*d^3 + 7*a^3*b^7*c^6*d^4 + 6*a^4*b^6*c^5*d^5 + 5*a^5*b^5*c
^4*d^6 + 4*a^6*b^4*c^3*d^7 + 3*a^7*b^3*c^2*d^8 + 2*a^8*b^2*c*d^9 + a^9*b*d^
10)*x)/(b^23*x^12 + 12*a*b^22*x^11 + 66*a^2*b^21*x^10 + 220*a^3*b^20*x^9 +
495*a^4*b^19*x^8 + 792*a^5*b^18*x^7 + 924*a^6*b^17*x^6 + 792*a^7*b^16*x^5 +
495*a^8*b^15*x^4 + 220*a^9*b^14*x^3 + 66*a^10*b^13*x^2 + 12*a^11*b^12*x +
a^12*b^11)

```

mupad [B] time = 0.39, size = 39, normalized size = 0.67

$$\frac{(c + dx)^{11} (12ad - 11bc + bdx)}{132(ad - bc)^2 (a + bx)^{12}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^13,x)

[Out] ((c + d*x)^11*(12*a*d - 11*b*c + b*d*x))/(132*(a*d - b*c)^2*(a + b*x)^12)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**13,x)

[Out] Timed out

$$3.1325 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{14}} dx$$

Optimal. Leaf size=89

$$-\frac{d^2(c+dx)^{11}}{858(a+bx)^{11}(bc-ad)^3} + \frac{d(c+dx)^{11}}{78(a+bx)^{12}(bc-ad)^2} - \frac{(c+dx)^{11}}{13(a+bx)^{13}(bc-ad)}$$

[Out] $-1/13*(d*x+c)^{11}/(-a*d+b*c)/(b*x+a)^{13}+1/78*d*(d*x+c)^{11}/(-a*d+b*c)^2/(b*x+a)^{12}-1/858*d^2*(d*x+c)^{11}/(-a*d+b*c)^3/(b*x+a)^{11}$

Rubi [A] time = 0.02, antiderivative size = 89, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{d^2(c+dx)^{11}}{858(a+bx)^{11}(bc-ad)^3} + \frac{d(c+dx)^{11}}{78(a+bx)^{12}(bc-ad)^2} - \frac{(c+dx)^{11}}{13(a+bx)^{13}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^14, x]

[Out] $-(c + d*x)^{11}/(13*(b*c - a*d)*(a + b*x)^{13}) + (d*(c + d*x)^{11})/(78*(b*c - a*d)^2*(a + b*x)^{12}) - (d^2*(c + d*x)^{11})/(858*(b*c - a*d)^3*(a + b*x)^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{10}}{(a+bx)^{14}} dx &= -\frac{(c+dx)^{11}}{13(bc-ad)(a+bx)^{13}} - \frac{(2d) \int \frac{(c+dx)^{10}}{(a+bx)^{13}} dx}{13(bc-ad)} \\
&= -\frac{(c+dx)^{11}}{13(bc-ad)(a+bx)^{13}} + \frac{d(c+dx)^{11}}{78(bc-ad)^2(a+bx)^{12}} + \frac{d^2 \int \frac{(c+dx)^{10}}{(a+bx)^{12}} dx}{78(bc-ad)^2} \\
&= -\frac{(c+dx)^{11}}{13(bc-ad)(a+bx)^{13}} + \frac{d(c+dx)^{11}}{78(bc-ad)^2(a+bx)^{12}} - \frac{d^2(c+dx)^{11}}{858(bc-ad)^3(a+bx)^{11}}
\end{aligned}$$

Mathematica [B] time = 0.29, size = 690, normalized size = 7.75

$$a^{10}d^{10} + a^9bd^9(3c + 13dx) + 3a^8b^2d^8(2c^2 + 13cdx + 26d^2x^2) + 2a^7b^3d^7(5c^3 + 39c^2dx + 117cd^2x^2 + 143d^3x^3)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^14,x]

[Out]
$$\begin{aligned}
& -1/858*(a^{10}*d^{10} + a^9*b*d^9*(3*c + 13*d*x) + 3*a^8*b^2*d^8*(2*c^2 + 13*c*d*x + 26*d^2*x^2) + 2*a^7*b^3*d^7*(5*c^3 + 39*c^2*d*x + 117*c*d^2*x^2 + 143*d^3*x^3) \\
& + a^6*b^4*d^6*(15*c^4 + 130*c^3*d*x + 468*c^2*d^2*x^2 + 858*c*d^3*x^3 + 715*d^4*x^4) + 3*a^5*b^5*d^5*(7*c^5 + 65*c^4*d*x + 260*c^3*d^2*x^2 + 572*c^2*d^3*x^3 + 715*c*d^4*x^4 + 429*d^5*x^5) \\
& + a^4*b^6*d^4*(28*c^6 + 273*c^5*d*x + 1170*c^4*d^2*x^2 + 2860*c^3*d^3*x^3 + 4290*c^2*d^4*x^4 + 3861*c*d^5*x^5 + 1716*d^6*x^6) + 2*a^3*b^7*d^3*(18*c^7 + 182*c^6*d*x + 819*c^5*d^2*x^2 + 2145*c^4*d^3*x^3 + 3575*c^3*d^4*x^4 + 3861*c^2*d^5*x^5 + 2574*c*d^6*x^6 + 858*d^7*x^7) \\
& + 3*a^2*b^8*d^2*(15*c^8 + 156*c^7*d*x + 728*c^6*d^2*x^2 + 2002*c^5*d^3*x^3 + 3575*c^4*d^4*x^4 + 4290*c^3*d^5*x^5 + 3432*c^2*d^6*x^6 + 1716*c*d^7*x^7 + 429*d^8*x^8) \\
& + a*b^9*d*(55*c^9 + 585*c^8*d*x + 2808*c^7*d^2*x^2 + 8008*c^6*d^3*x^3 + 15015*c^5*d^4*x^4 + 19305*c^4*d^5*x^5 + 17160*c^3*d^6*x^6 + 10296*c^2*d^7*x^7 + 3861*c*d^8*x^8 + 715*d^9*x^9) \\
& + b^{10}*(66*c^{10} + 715*c^9*d*x + 3510*c^8*d^2*x^2 + 10296*c^7*d^3*x^3 + 20020*c^6*d^4*x^4 + 27027*c^5*d^5*x^5 + 25740*c^4*d^6*x^6 + 17160*c^3*d^7*x^7 + 7722*c^2*d^8*x^8 + 2145*c*d^9*x^9 + 286*d^{10}*x^{10})) / (b^{11}*(a + b*x)^{13})
\end{aligned}$$

fricas [B] time = 0.45, size = 997, normalized size = 11.20

$$286 b^{10} d^{10} x^{10} + 66 b^{10} c^{10} + 55 a b^9 c^9 d + 45 a^2 b^8 c^8 d^2 + 36 a^3 b^7 c^7 d^3 + 28 a^4 b^6 c^6 d^4 + 21 a^5 b^5 c^5 d^5 + 15 a^6 b^4 c^4 d^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^14,x, algorithm="fricas")

[Out]
$$-1/858*(286*b^{10}*d^{10}*x^{10} + 66*b^{10}*c^{10} + 55*a*b^9*c^9*d + 45*a^2*b^8*c^8*d^2 + 36*a^3*b^7*c^7*d^3 + 28*a^4*b^6*c^6*d^4 + 21*a^5*b^5*c^5*d^5 + 15*a^6*b^4*c^4*d^6 + 10*a^7*b^3*c^3*d^7 + 6*a^8*b^2*c^2*d^8 + 3*a^9*b*c*d^9 + a^{10}*d^{10} + 715*(3*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 + 1287*(6*b^{10}*c^2*d^8 + 3*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 1716*(10*b^{10}*c^3*d^7 + 6*a*b^9*c^2*d^8 + 3*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 1716*(15*b^{10}*c^4*d^6 + 10*a*b^9*c^3*d^7 + 6*a^2*b^8*c^2*d^8 + 3*a^3*b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 1287*(21*b^{10}*c^5*d^5 + 15*a*b^9*c^4*d^6 + 10*a^2*b^8*c^3*d^7 + 6*a^3*b^7*c^2*d^8 + 3*a^4*b^6*c*d^9 + a^5*b^5*d^{10})*x^5 + 715*(28*b^{10}*c^6*d^4 + 21*a*b^9*c^5*d^5 + 15*a^2*b^8*c^4*d^6 + 10*a^3*b^7*c^3*d^7 + 6*a^4*b^6*c^2*d^8 + 3*a^5*b^5*c*d^9 + a^6*b^4*d^{10})*x^4 + 286*(36*b^{10}*c^7*d^3 + 28*a*b^9*c^6*d^4 + 21*a^2*b^8*c^5*d^5 + 15*a^3*b^7*c^4*d^6 + 10*a^4*b^6*c^3*d^7 + 6*a^5*b^5*c^2*d^8 + 3*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + 78*(45*b^{10}*c^8*d^2 + 36*a*b^9*c^7*d^3 + 28*a^2*b^8*c^6*d^4 + 21*a^3*b^7*c^5*d^5 + 15*a^4*b^6*c^4*d^6 + 10*a^5*b^5*c^3*d^7 + 6*a^6*b^4*c^2*d^8 + 3*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 + 13*(55*b^{10}*c^9*d + 45*a*b^9*c^8*d^2 + 36*a^2*b^8*c^7*d^3 + 28*a^3*b^7*c^6*d^4 + 21*a^4*b^6*c^5*d^5 + 15*a^5*b^5*c^4*d^6 + 10*a^6*b^4*c^3*d^7 + 6*a^7*b^3*c^2*d^8 + 3*a^8*b^2*c*d^9 + a^9*b*d^{10})*x)/(b^{24}*x^{13} + 13*a*b^{23}*x^{12} + 78*a^2*b^{22}*x^{11} + 286*a^3*b^{21}*x^{10} + 715*a^4*b^{20}*x^9 + 1287*a^5*b^{19}*x^8 + 1716*a^6*b^{18}*x^7 + 1716*a^7*b^{17}*x^6 + 1287*a^8*b^{16}*x^5 + 715*a^9*b^{15}*x^4 + 286*a^{10}*b^{14}*x^3 + 78*a^{11}*b^{13}*x^2 + 13*a^{12}*b^{12}*x + a^{13}*b^{11})$$

giac [B] time = 1.28, size = 961, normalized size = 10.80

$$286 b^{10} d^{10} x^{10} + 2145 b^{10} c d^9 x^9 + 715 a b^9 d^{10} x^9 + 7722 b^{10} c^2 d^8 x^8 + 3861 a b^9 c d^9 x^8 + 1287 a^2 b^8 d^{10} x^8 + 17160 b^{10} c^3 d^7 x^7 + 10296 a b^9 c^2 d^8 x^7 + 5148 a^2 b^8 c d^9 x^7 + 1716 a^3 b^7 d^{10} x^7 + 25740 b^{10} c^4 d^6 x^6 + 17160 a b^9 c^3 d^7 x^6 + 10296 a^2 b^8 c^2 d^8 x^6 + 5148 a^3 b^7 c^2 d^9 x^6 + 1716 a^4 b^6 d^{10} x^6 + 2702 7 b^{10} c^5 d^5 x^5 + 19305 a b^9 c^4 d^6 x^5 + 12870 a^2 b^8 c^3 d^7 x^5 + 7722 a^3 b^7 c^2 d^8 x^5 + 3861 a^4 b^6 c^2 d^9 x^5 + 1287 a^5 b^5 d^{10} x^5 + 20020 b^{10} c^6 d^4 x^4 + 15015 a b^9 c^5 d^5 x^4 + 10725 a^2 b^8 c^4 d^6 x^4 + 7150 a^3 b^7 c^3 d^7 x^4 + 4290 a^4 b^6 c^2 d^8 x^4 + 2145 a^5 b^5 c^2 d^9 x^4 + 715 a^6 b^4 d^{10} x^4 + 10296 b^{10} c^7 d^3 x^3 + 8008 a b^9 c^6 d^4 x^3 + 6006 a^2 b^8 c^5 d^5 x^3 + 4290 a^3 b^7 c^4 d^6 x^3 + 2860 a^4 b^6 c^3 d^7 x^3 + 1716 a^5 b^5 c^2 d^8 x^3 + 858 a^6 b^4 c^2 d^9 x^3 + 286 a^7 b^3 c^2 d^{10} x^3 + 3510 b^{10} c^8 d^2 x^2 + 2808 a b^9 c^7 d^3 x^2 + 2184 a^2 b^8 c^6 d^4 x^2 + 1287 a^3 b^7 c^5 d^5 x^2 + 7722 a^4 b^6 c^4 d^6 x^2 + 25740 a^5 b^5 c^3 d^7 x^2 + 17160 a^6 b^4 c^2 d^8 x^2 + 5148 a^7 b^3 c^2 d^9 x^2 + 1716 a^8 b^2 d^{10} x^2 + 78 a^9 b^2 c^2 d^{10} x^2 + 13 a^{10} b^2 d^{10} x^2 + 13 a^{11} b^2 c^2 d^{10} x^2 + 13 a^{12} b^2 c^2 d^{10} x^2 + 13 a^{13} b^2 c^2 d^{10} x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^14,x, algorithm="giac")

[Out]
$$-1/858*(286*b^{10}*d^{10}*x^{10} + 2145*b^{10}*c*d^9*x^9 + 715*a*b^9*d^{10}*x^9 + 7722*b^{10}*c^2*d^8*x^8 + 3861*a*b^9*c*d^9*x^8 + 1287*a^2*b^8*d^{10}*x^8 + 17160*b^{10}*c^3*d^7*x^7 + 10296*a*b^9*c^2*d^8*x^7 + 5148*a^2*b^8*c*d^9*x^7 + 1716*a^3*b^7*d^{10}*x^7 + 25740*b^{10}*c^4*d^6*x^6 + 17160*a*b^9*c^3*d^7*x^6 + 10296*a^2*b^8*c^2*d^8*x^6 + 5148*a^3*b^7*c^2*d^9*x^6 + 1716*a^4*b^6*d^{10}*x^6 + 27027*b^{10}*c^5*d^5*x^5 + 19305*a*b^9*c^4*d^6*x^5 + 12870*a^2*b^8*c^3*d^7*x^5 + 7722*a^3*b^7*c^2*d^8*x^5 + 3861*a^4*b^6*c^2*d^9*x^5 + 1287*a^5*b^5*d^{10}*x^5 + 20020*b^{10}*c^6*d^4*x^4 + 15015*a*b^9*c^5*d^5*x^4 + 10725*a^2*b^8*c^4*d^6*x^4 + 7150*a^3*b^7*c^3*d^7*x^4 + 4290*a^4*b^6*c^2*d^8*x^4 + 2145*a^5*b^5*c^2*d^9*x^4 + 715*a^6*b^4*d^{10}*x^4 + 10296*b^{10}*c^7*d^3*x^3 + 8008*a*b^9*c^6*d^4*x^3 + 6006*a^2*b^8*c^5*d^5*x^3 + 4290*a^3*b^7*c^4*d^6*x^3 + 2860*a^4*b^6*c^3*d^7*x^3 + 1716*a^5*b^5*c^2*d^8*x^3 + 858*a^6*b^4*c^2*d^9*x^3 + 286*a^7*b^3*c^2*d^{10}*x^3 + 3510*b^{10}*c^8*d^2*x^2 + 2808*a*b^9*c^7*d^3*x^2 + 2184*a^2*b^8*c^6*d^4*x^2 + 1287*a^3*b^7*c^5*d^5*x^2 + 7722*a^4*b^6*c^4*d^6*x^2 + 25740*a^5*b^5*c^3*d^7*x^2 + 17160*a^6*b^4*c^2*d^8*x^2 + 5148*a^7*b^3*c^2*d^9*x^2 + 1716*a^8*b^2*d^{10}*x^2 + 78*a^9*b^2*c^2*d^{10}*x^2 + 13*a^{10}*b^2*d^{10}*x^2 + 13*a^{11}*b^2*c^2*d^{10}*x^2 + 13*a^{12}*b^2*c^2*d^{10}*x^2 + 13*a^{13}*b^2*c^2*d^{10}*x^2)$$

$$\begin{aligned} & 6d^4x^2 + 1638a^3b^7c^5d^5x^2 + 1170a^4b^6c^4d^6x^2 + 780a^5b^5c^3d^7x^2 + 468a^6b^4c^2d^8x^2 + 234a^7b^3c^1d^9x^2 + 78a^8b^2d^{10}x^2 \\ & + 715b^{10}c^9dx + 585a^9b^8c^7d^3x + 468a^2b^8c^7d^3x + 364a^3b^7c^6d^4x + 273a^4b^6c^5d^5x + 195a^5b^5c^4d^6x \\ & + 130a^6b^4c^3d^7x + 78a^7b^3c^2d^8x + 39a^8b^2c^1d^9x + 13a^9b^1d^{10}x + 66b^{10}c^{10} + 55a^9b^9c^9d \\ & + 45a^2b^8c^8d^2 + 36a^3b^7c^7d^3 + 28a^4b^6c^6d^4 + 21a^5b^5c^5d^5 + 15a^6b^4c^4d^6 + 10a^7b^3c^3d^7 \\ & + 6a^8b^2c^2d^8 + 3a^9b^1c^1d^9 + a^{10}d^{10} / ((bx + a)^{13}b^{11}) \end{aligned}$$

maple [B] time = 0.01, size = 867, normalized size = 9.74

$$\frac{d^{10}}{3(bx+a)^3b^{11}} + \frac{5(ad-bc)d^9}{2(bx+a)^4b^{11}} - \frac{9(a^2d^2-2abcd+b^2c^2)d^8}{(bx+a)^5b^{11}} + \frac{20(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^7}{(bx+a)^6b^{11}} - \frac{30(a^4d^4-4a^3bcd^3+6a^2b^2c^2d^2-4a^1b^3c^3d+b^4c^4)}{(bx+a)^7b^{11}} + \frac{70(a^5d^5-5a^4b^1c^4d+10a^3b^2c^3d^2+5a^2b^3c^2d^3-10a^1b^4c^1d^4+b^5c^5)}{(bx+a)^8b^{11}} - \frac{113(a^6d^6-6a^5b^1c^5d+15a^4b^2c^4d^2-20a^3b^3c^3d^3+15a^2b^4c^2d^4-20a^1b^5c^1d^5+b^6c^6)}{(bx+a)^9b^{11}} + \frac{210(a^7d^7-7a^6b^1c^6d+21a^5b^2c^5d^2-36a^4b^3c^4d^3+36a^3b^4c^3d^4-84a^2b^5c^2d^5+84a^1b^6c^1d^6+b^7c^7)}{(bx+a)^{10}b^{11}} - \frac{252(a^8d^8-8a^7b^1c^7d+28a^6b^2c^6d^2-56a^5b^3c^5d^3+56a^4b^4c^4d^4-56a^3b^5c^3d^5+28a^2b^6c^2d^6-56a^1b^7c^1d^7+b^8c^8)}{(bx+a)^{11}b^{11}} + \frac{70(a^9d^9-9a^8b^1c^8d+36a^7b^2c^7d^2-84a^6b^3c^6d^3+126a^5b^4c^5d^4-126a^4b^5c^4d^5+84a^3b^6c^3d^6-36a^2b^7c^2d^7+84a^1b^8c^1d^8+b^9c^9)}{(bx+a)^{12}b^{11}} - \frac{20(a^{10}d^{10}-10a^9b^1c^9d+45a^8b^2c^8d^2-10a^7b^3c^7d^3+45a^6b^4c^6d^4-10a^5b^5c^5d^5+21a^4b^6c^4d^6-10a^3b^7c^3d^7+10a^2b^8c^2d^8-10a^1b^9c^1d^9+b^{10}c^{10})}{(bx+a)^{13}b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^14,x)

[Out]
$$\frac{63}{2}d^5(a^5d^5-5a^4b^1c^4d+10a^3b^2c^3d^2+5a^2b^3c^2d^3-10a^1b^4c^1d^4+b^5c^5)/b^{11}/(bx+a)^8 - \frac{113}{13}(a^{10}d^{10}-10a^9b^1c^9d+45a^8b^2c^8d^2-10a^7b^3c^7d^3+45a^6b^4c^6d^4-10a^5b^5c^5d^5+21a^4b^6c^4d^6-10a^3b^7c^3d^7+10a^2b^8c^2d^8-10a^1b^9c^1d^9+b^{10}c^{10})/b^{11}/(bx+a)^{13} - \frac{1}{3}d^{10}/b^{11}/(bx+a)^3 - \frac{5}{3}d^9/b^{11}/(bx+a)^4 - \frac{9}{3}d^8/b^{11}/(bx+a)^5 - \frac{20}{3}d^7/b^{11}/(bx+a)^6 - \frac{70}{3}d^6/b^{11}/(bx+a)^7 - \frac{252}{3}d^5/b^{11}/(bx+a)^8 - \frac{113}{3}d^4/b^{11}/(bx+a)^9 - \frac{70}{3}d^3/b^{11}/(bx+a)^{10} - \frac{20}{3}d^2/b^{11}/(bx+a)^{11} - \frac{1}{3}d/b^{11}/(bx+a)^{12} - \frac{1}{3}b^{10}c^{10}/b^{11}/(bx+a)^{13}$$

maxima [B] time = 2.21, size = 997, normalized size = 11.20

$$\frac{286b^{10}d^{10}x^{10} + 66b^{10}c^{10} + 55ab^9c^9d + 45a^2b^8c^8d^2 + 36a^3b^7c^7d^3 + 28a^4b^6c^6d^4 + 21a^5b^5c^5d^5 + 15a^6b^4c^4d^6}{(bx+a)^{13}b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^14,x, algorithm="maxima")

```
[Out] -1/858*(286*b^10*d^10*x^10 + 66*b^10*c^10 + 55*a*b^9*c^9*d + 45*a^2*b^8*c^8
*d^2 + 36*a^3*b^7*c^7*d^3 + 28*a^4*b^6*c^6*d^4 + 21*a^5*b^5*c^5*d^5 + 15*a^
6*b^4*c^4*d^6 + 10*a^7*b^3*c^3*d^7 + 6*a^8*b^2*c^2*d^8 + 3*a^9*b*c*d^9 + a^
10*d^10 + 715*(3*b^10*c*d^9 + a*b^9*d^10)*x^9 + 1287*(6*b^10*c^2*d^8 + 3*a*
b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 1716*(10*b^10*c^3*d^7 + 6*a*b^9*c^2*d^8 + 3
*a^2*b^8*c*d^9 + a^3*b^7*d^10)*x^7 + 1716*(15*b^10*c^4*d^6 + 10*a*b^9*c^3*d
^7 + 6*a^2*b^8*c^2*d^8 + 3*a^3*b^7*c*d^9 + a^4*b^6*d^10)*x^6 + 1287*(21*b^1
0*c^5*d^5 + 15*a*b^9*c^4*d^6 + 10*a^2*b^8*c^3*d^7 + 6*a^3*b^7*c^2*d^8 + 3*a
^4*b^6*c*d^9 + a^5*b^5*d^10)*x^5 + 715*(28*b^10*c^6*d^4 + 21*a*b^9*c^5*d^5
+ 15*a^2*b^8*c^4*d^6 + 10*a^3*b^7*c^3*d^7 + 6*a^4*b^6*c^2*d^8 + 3*a^5*b^5*c
*d^9 + a^6*b^4*d^10)*x^4 + 286*(36*b^10*c^7*d^3 + 28*a*b^9*c^6*d^4 + 21*a^2
*b^8*c^5*d^5 + 15*a^3*b^7*c^4*d^6 + 10*a^4*b^6*c^3*d^7 + 6*a^5*b^5*c^2*d^8
+ 3*a^6*b^4*c*d^9 + a^7*b^3*d^10)*x^3 + 78*(45*b^10*c^8*d^2 + 36*a*b^9*c^7*
d^3 + 28*a^2*b^8*c^6*d^4 + 21*a^3*b^7*c^5*d^5 + 15*a^4*b^6*c^4*d^6 + 10*a^5
*b^5*c^3*d^7 + 6*a^6*b^4*c^2*d^8 + 3*a^7*b^3*c*d^9 + a^8*b^2*d^10)*x^2 + 13
*(55*b^10*c^9*d + 45*a*b^9*c^8*d^2 + 36*a^2*b^8*c^7*d^3 + 28*a^3*b^7*c^6*d^
4 + 21*a^4*b^6*c^5*d^5 + 15*a^5*b^5*c^4*d^6 + 10*a^6*b^4*c^3*d^7 + 6*a^7*b^
3*c^2*d^8 + 3*a^8*b^2*c*d^9 + a^9*b*d^10)*x)/(b^24*x^13 + 13*a*b^23*x^12 +
78*a^2*b^22*x^11 + 286*a^3*b^21*x^10 + 715*a^4*b^20*x^9 + 1287*a^5*b^19*x^8
+ 1716*a^6*b^18*x^7 + 1716*a^7*b^17*x^6 + 1287*a^8*b^16*x^5 + 715*a^9*b^15
*x^4 + 286*a^10*b^14*x^3 + 78*a^11*b^13*x^2 + 13*a^12*b^12*x + a^13*b^11)
```

mupad [B] time = 0.48, size = 1098, normalized size = 12.34

$$\frac{a^{10} d^{10} + 3 a^9 b c d^9 + 13 a^9 b d^{10} x + 6 a^8 b^2 c^2 d^8 + 39 a^8 b^2 c d^9 x + 78 a^8 b^2 d^{10} x^2 + 10 a^7 b^3 c^3 d^7 + 78 a^7 b^3 c^2 d^8 x + 10 a^7 b^3 c^2 d^8 x^2 + 10 a^7 b^3 c^2 d^8 x^3 + 10 a^7 b^3 c^2 d^8 x^4 + 10 a^7 b^3 c^2 d^8 x^5 + 10 a^7 b^3 c^2 d^8 x^6 + 10 a^7 b^3 c^2 d^8 x^7 + 10 a^7 b^3 c^2 d^8 x^8 + 10 a^7 b^3 c^2 d^8 x^9 + 10 a^7 b^3 c^2 d^8 x^{10} + 10 a^7 b^3 c^2 d^8 x^{11} + 10 a^7 b^3 c^2 d^8 x^{12} + 10 a^7 b^3 c^2 d^8 x^{13} + 10 a^7 b^3 c^2 d^8 x^{14} + 10 a^7 b^3 c^2 d^8 x^{15} + 10 a^7 b^3 c^2 d^8 x^{16} + 10 a^7 b^3 c^2 d^8 x^{17} + 10 a^7 b^3 c^2 d^8 x^{18} + 10 a^7 b^3 c^2 d^8 x^{19} + 10 a^7 b^3 c^2 d^8 x^{20} + 10 a^7 b^3 c^2 d^8 x^{21} + 10 a^7 b^3 c^2 d^8 x^{22} + 10 a^7 b^3 c^2 d^8 x^{23} + 10 a^7 b^3 c^2 d^8 x^{24} + 10 a^7 b^3 c^2 d^8 x^{25} + 10 a^7 b^3 c^2 d^8 x^{26} + 10 a^7 b^3 c^2 d^8 x^{27} + 10 a^7 b^3 c^2 d^8 x^{28} + 10 a^7 b^3 c^2 d^8 x^{29} + 10 a^7 b^3 c^2 d^8 x^{30} + 10 a^7 b^3 c^2 d^8 x^{31} + 10 a^7 b^3 c^2 d^8 x^{32} + 10 a^7 b^3 c^2 d^8 x^{33} + 10 a^7 b^3 c^2 d^8 x^{34} + 10 a^7 b^3 c^2 d^8 x^{35} + 10 a^7 b^3 c^2 d^8 x^{36} + 10 a^7 b^3 c^2 d^8 x^{37} + 10 a^7 b^3 c^2 d^8 x^{38} + 10 a^7 b^3 c^2 d^8 x^{39} + 10 a^7 b^3 c^2 d^8 x^{40} + 10 a^7 b^3 c^2 d^8 x^{41} + 10 a^7 b^3 c^2 d^8 x^{42} + 10 a^7 b^3 c^2 d^8 x^{43} + 10 a^7 b^3 c^2 d^8 x^{44} + 10 a^7 b^3 c^2 d^8 x^{45} + 10 a^7 b^3 c^2 d^8 x^{46} + 10 a^7 b^3 c^2 d^8 x^{47} + 10 a^7 b^3 c^2 d^8 x^{48} + 10 a^7 b^3 c^2 d^8 x^{49} + 10 a^7 b^3 c^2 d^8 x^{50} + 10 a^7 b^3 c^2 d^8 x^{51} + 10 a^7 b^3 c^2 d^8 x^{52} + 10 a^7 b^3 c^2 d^8 x^{53} + 10 a^7 b^3 c^2 d^8 x^{54} + 10 a^7 b^3 c^2 d^8 x^{55} + 10 a^7 b^3 c^2 d^8 x^{56} + 10 a^7 b^3 c^2 d^8 x^{57} + 10 a^7 b^3 c^2 d^8 x^{58} + 10 a^7 b^3 c^2 d^8 x^{59} + 10 a^7 b^3 c^2 d^8 x^{60} + 10 a^7 b^3 c^2 d^8 x^{61} + 10 a^7 b^3 c^2 d^8 x^{62} + 10 a^7 b^3 c^2 d^8 x^{63} + 10 a^7 b^3 c^2 d^8 x^{64} + 10 a^7 b^3 c^2 d^8 x^{65} + 10 a^7 b^3 c^2 d^8 x^{66} + 10 a^7 b^3 c^2 d^8 x^{67} + 10 a^7 b^3 c^2 d^8 x^{68} + 10 a^7 b^3 c^2 d^8 x^{69} + 10 a^7 b^3 c^2 d^8 x^{70} + 10 a^7 b^3 c^2 d^8 x^{71} + 10 a^7 b^3 c^2 d^8 x^{72} + 10 a^7 b^3 c^2 d^8 x^{73} + 10 a^7 b^3 c^2 d^8 x^{74} + 10 a^7 b^3 c^2 d^8 x^{75} + 10 a^7 b^3 c^2 d^8 x^{76} + 10 a^7 b^3 c^2 d^8 x^{77} + 10 a^7 b^3 c^2 d^8 x^{78} + 10 a^7 b^3 c^2 d^8 x^{79} + 10 a^7 b^3 c^2 d^8 x^{80} + 10 a^7 b^3 c^2 d^8 x^{81} + 10 a^7 b^3 c^2 d^8 x^{82} + 10 a^7 b^3 c^2 d^8 x^{83} + 10 a^7 b^3 c^2 d^8 x^{84} + 10 a^7 b^3 c^2 d^8 x^{85} + 10 a^7 b^3 c^2 d^8 x^{86} + 10 a^7 b^3 c^2 d^8 x^{87} + 10 a^7 b^3 c^2 d^8 x^{88} + 10 a^7 b^3 c^2 d^8 x^{89} + 10 a^7 b^3 c^2 d^8 x^{90} + 10 a^7 b^3 c^2 d^8 x^{91} + 10 a^7 b^3 c^2 d^8 x^{92} + 10 a^7 b^3 c^2 d^8 x^{93} + 10 a^7 b^3 c^2 d^8 x^{94} + 10 a^7 b^3 c^2 d^8 x^{95} + 10 a^7 b^3 c^2 d^8 x^{96} + 10 a^7 b^3 c^2 d^8 x^{97} + 10 a^7 b^3 c^2 d^8 x^{98} + 10 a^7 b^3 c^2 d^8 x^{99} + 10 a^7 b^3 c^2 d^8 x^{100}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^10/(a + b*x)^14,x)
```

```
[Out] -(a^10*d^10 + 66*b^10*c^10 + 286*b^10*d^10*x^10 + 715*a*b^9*d^10*x^9 + 2145
*b^10*c*d^9*x^9 + 45*a^2*b^8*c^8*d^2 + 36*a^3*b^7*c^7*d^3 + 28*a^4*b^6*c^6*
d^4 + 21*a^5*b^5*c^5*d^5 + 15*a^6*b^4*c^4*d^6 + 10*a^7*b^3*c^3*d^7 + 6*a^8*
b^2*c^2*d^8 + 78*a^8*b^2*d^10*x^2 + 286*a^7*b^3*d^10*x^3 + 715*a^6*b^4*d^10
*x^4 + 1287*a^5*b^5*d^10*x^5 + 1716*a^4*b^6*d^10*x^6 + 1716*a^3*b^7*d^10*x^
7 + 1287*a^2*b^8*d^10*x^8 + 3510*b^10*c^8*d^2*x^2 + 10296*b^10*c^7*d^3*x^3
+ 20020*b^10*c^6*d^4*x^4 + 27027*b^10*c^5*d^5*x^5 + 25740*b^10*c^4*d^6*x^6
+ 17160*b^10*c^3*d^7*x^7 + 7722*b^10*c^2*d^8*x^8 + 55*a*b^9*c^9*d + 3*a^9*b
*c*d^9 + 13*a^9*b*d^10*x + 715*b^10*c^9*d*x + 2184*a^2*b^8*c^6*d^4*x^2 + 16
38*a^3*b^7*c^5*d^5*x^2 + 1170*a^4*b^6*c^4*d^6*x^2 + 780*a^5*b^5*c^3*d^7*x^2
+ 468*a^6*b^4*c^2*d^8*x^2 + 6006*a^2*b^8*c^5*d^5*x^3 + 4290*a^3*b^7*c^4*d^
6*x^3 + 2860*a^4*b^6*c^3*d^7*x^3 + 1716*a^5*b^5*c^2*d^8*x^3 + 10725*a^2*b^8
*c^4*d^6*x^4 + 7150*a^3*b^7*c^3*d^7*x^4 + 4290*a^4*b^6*c^2*d^8*x^4 + 12870*
a^2*b^8*c^3*d^7*x^5 + 7722*a^3*b^7*c^2*d^8*x^5 + 10296*a^2*b^8*c^2*d^8*x^6
+ 585*a*b^9*c^8*d^2*x + 39*a^8*b^2*c*d^9*x + 3861*a*b^9*c*d^9*x^8 + 468*a^2
```

$$\begin{aligned} & *b^8*c^7*d^3*x + 364*a^3*b^7*c^6*d^4*x + 273*a^4*b^6*c^5*d^5*x + 195*a^5*b^5*c^4*d^6*x + 130*a^6*b^4*c^3*d^7*x + 78*a^7*b^3*c^2*d^8*x + 2808*a*b^9*c^7 \\ & *d^3*x^2 + 234*a^7*b^3*c*d^9*x^2 + 8008*a*b^9*c^6*d^4*x^3 + 858*a^6*b^4*c*d^9*x^3 + 15015*a*b^9*c^5*d^5*x^4 + 2145*a^5*b^5*c*d^9*x^4 + 19305*a*b^9*c^4 \\ & *d^6*x^5 + 3861*a^4*b^6*c*d^9*x^5 + 17160*a*b^9*c^3*d^7*x^6 + 5148*a^3*b^7*c*d^9*x^6 + 10296*a*b^9*c^2*d^8*x^7 + 5148*a^2*b^8*c*d^9*x^7) / (858*a^13*b^1 \\ & 1 + 858*b^24*x^13 + 11154*a^12*b^12*x + 11154*a*b^23*x^12 + 66924*a^11*b^13 \\ & *x^2 + 245388*a^10*b^14*x^3 + 613470*a^9*b^15*x^4 + 1104246*a^8*b^16*x^5 + \\ & 1472328*a^7*b^17*x^6 + 1472328*a^6*b^18*x^7 + 1104246*a^5*b^19*x^8 + 613470 \\ & *a^4*b^20*x^9 + 245388*a^3*b^21*x^10 + 66924*a^2*b^22*x^11) \end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**14,x)

[Out] Timed out

$$3.1326 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{15}} dx$$

Optimal. Leaf size=120

$$\frac{d^3(c+dx)^{11}}{4004(a+bx)^{11}(bc-ad)^4} - \frac{d^2(c+dx)^{11}}{364(a+bx)^{12}(bc-ad)^3} + \frac{3d(c+dx)^{11}}{182(a+bx)^{13}(bc-ad)^2} - \frac{(c+dx)^{11}}{14(a+bx)^{14}(bc-ad)}$$

[Out] $-1/14*(d*x+c)^{11}/(-a*d+b*c)/(b*x+a)^{14}+3/182*d*(d*x+c)^{11}/(-a*d+b*c)^2/(b*x+a)^{13}-1/364*d^2*(d*x+c)^{11}/(-a*d+b*c)^3/(b*x+a)^{12}+1/4004*d^3*(d*x+c)^{11}/(-a*d+b*c)^4/(b*x+a)^{11}$

Rubi [A] time = 0.03, antiderivative size = 120, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{d^3(c+dx)^{11}}{4004(a+bx)^{11}(bc-ad)^4} - \frac{d^2(c+dx)^{11}}{364(a+bx)^{12}(bc-ad)^3} + \frac{3d(c+dx)^{11}}{182(a+bx)^{13}(bc-ad)^2} - \frac{(c+dx)^{11}}{14(a+bx)^{14}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^15, x]

[Out] $-(c + d*x)^{11}/(14*(b*c - a*d)*(a + b*x)^{14}) + (3*d*(c + d*x)^{11})/(182*(b*c - a*d)^2*(a + b*x)^{13}) - (d^2*(c + d*x)^{11})/(364*(b*c - a*d)^3*(a + b*x)^{12}) + (d^3*(c + d*x)^{11})/(4004*(b*c - a*d)^4*(a + b*x)^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{10}}{(a+bx)^{15}} dx &= -\frac{(c+dx)^{11}}{14(bc-ad)(a+bx)^{14}} - \frac{(3d) \int \frac{(c+dx)^{10}}{(a+bx)^{14}} dx}{14(bc-ad)} \\
&= -\frac{(c+dx)^{11}}{14(bc-ad)(a+bx)^{14}} + \frac{3d(c+dx)^{11}}{182(bc-ad)^2(a+bx)^{13}} + \frac{(3d^2) \int \frac{(c+dx)^{10}}{(a+bx)^{13}} dx}{91(bc-ad)^2} \\
&= -\frac{(c+dx)^{11}}{14(bc-ad)(a+bx)^{14}} + \frac{3d(c+dx)^{11}}{182(bc-ad)^2(a+bx)^{13}} - \frac{d^2(c+dx)^{11}}{364(bc-ad)^3(a+bx)^{12}} - \frac{d^3 \int \frac{(c+dx)^{10}}{(a+bx)^{12}} dx}{364(bc-ad)^3} \\
&= -\frac{(c+dx)^{11}}{14(bc-ad)(a+bx)^{14}} + \frac{3d(c+dx)^{11}}{182(bc-ad)^2(a+bx)^{13}} - \frac{d^2(c+dx)^{11}}{364(bc-ad)^3(a+bx)^{12}} + \frac{d^3(c+dx)^{11}}{4004(bc-ad)^4(a+bx)^{11}}
\end{aligned}$$

Mathematica [B] time = 0.29, size = 692, normalized size = 5.77

$$\frac{a^{10}d^{10} + 2a^9bd^9(2c + 7dx) + a^8b^2d^8(10c^2 + 56cdx + 91d^2x^2) + 4a^7b^3d^7(5c^3 + 35c^2dx + 91cd^2x^2 + 91d^3x^3) + \dots}{(a+bx)^{14}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^15,x]

[Out]
$$\begin{aligned}
& -1/4004*(a^{10}d^{10} + 2*a^9*b*d^9*(2*c + 7*d*x) + a^8*b^2*d^8*(10*c^2 + 56*c \\
& *d*x + 91*d^2*x^2) + 4*a^7*b^3*d^7*(5*c^3 + 35*c^2*d*x + 91*c*d^2*x^2 + 91* \\
& d^3*x^3) + 7*a^6*b^4*d^6*(5*c^4 + 40*c^3*d*x + 130*c^2*d^2*x^2 + 208*c*d^3* \\
& x^3 + 143*d^4*x^4) + 14*a^5*b^5*d^5*(4*c^5 + 35*c^4*d*x + 130*c^3*d^2*x^2 + \\
& 260*c^2*d^3*x^3 + 286*c*d^4*x^4 + 143*d^5*x^5) + 7*a^4*b^6*d^4*(12*c^6 + 1 \\
& 12*c^5*d*x + 455*c^4*d^2*x^2 + 1040*c^3*d^3*x^3 + 1430*c^2*d^4*x^4 + 1144*c \\
& *d^5*x^5 + 429*d^6*x^6) + 4*a^3*b^7*d^3*(30*c^7 + 294*c^6*d*x + 1274*c^5*d^ \\
& 2*x^2 + 3185*c^4*d^3*x^3 + 5005*c^3*d^4*x^4 + 5005*c^2*d^5*x^5 + 3003*c*d^6 \\
& *x^6 + 858*d^7*x^7) + a^2*b^8*d^2*(165*c^8 + 1680*c^7*d*x + 7644*c^6*d^2*x^ \\
& 2 + 20384*c^5*d^3*x^3 + 35035*c^4*d^4*x^4 + 40040*c^3*d^5*x^5 + 30030*c^2*d \\
& ^6*x^6 + 13728*c*d^7*x^7 + 3003*d^8*x^8) + 2*a*b^9*d*(110*c^9 + 1155*c^8*d* \\
& x + 5460*c^7*d^2*x^2 + 15288*c^6*d^3*x^3 + 28028*c^5*d^4*x^4 + 35035*c^4*d^ \\
& 5*x^5 + 30030*c^3*d^6*x^6 + 17160*c^2*d^7*x^7 + 6006*c*d^8*x^8 + 1001*d^9*x \\
& ^9) + b^{10}*(286*c^{10} + 3080*c^9*d*x + 15015*c^8*d^2*x^2 + 43680*c^7*d^3*x^3 \\
& + 84084*c^6*d^4*x^4 + 112112*c^5*d^5*x^5 + 105105*c^4*d^6*x^6 + 68640*c^3* \\
& d^7*x^7 + 30030*c^2*d^8*x^8 + 8008*c*d^9*x^9 + 1001*d^{10}*x^{10}))/ (b^{11}*(a + \\
& b*x)^{14})
\end{aligned}$$

fricas [B] time = 0.46, size = 1008, normalized size = 8.40

$$\frac{1001 b^{10} d^{10} x^{10} + 286 b^{10} c^{10} + 220 a b^9 c^9 d + 165 a^2 b^8 c^8 d^2 + 120 a^3 b^7 c^7 d^3 + 84 a^4 b^6 c^6 d^4 + 56 a^5 b^5 c^5 d^5 + 35 a^6 b^4 c^4 d^6 + \dots}{(a+bx)^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^15,x, algorithm="fricas")

[Out]
$$\begin{aligned} & -1/4004*(1001*b^{10}*d^{10}*x^{10} + 286*b^{10}*c^{10} + 220*a*b^9*c^9*d + 165*a^2*b^8*c^8*d^2 + 120*a^3*b^7*c^7*d^3 + 84*a^4*b^6*c^6*d^4 + 56*a^5*b^5*c^5*d^5 + \\ & 35*a^6*b^4*c^4*d^6 + 20*a^7*b^3*c^3*d^7 + 10*a^8*b^2*c^2*d^8 + 4*a^9*b*c*d^9 + a^{10}*d^{10} + 2002*(4*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 + 3003*(10*b^{10}*c^2*d^8 + \\ & 4*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 3432*(20*b^{10}*c^3*d^7 + 10*a*b^9*c^2*d^8 + 4*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 3003*(35*b^{10}*c^4*d^6 + 20*a*b^9*c^3*d^7 + \\ & 10*a^2*b^8*c^2*d^8 + 4*a^3*b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 2002*(56*b^{10}*c^5*d^5 + 35*a*b^9*c^4*d^6 + 20*a^2*b^8*c^3*d^7 + 10*a^3*b^7*c^2*d^8 + 4*a^4*b^6*c*d^9 + \\ & a^5*b^5*d^{10})*x^5 + 1001*(84*b^{10}*c^6*d^4 + 56*a*b^9*c^5*d^5 + 35*a^2*b^8*c^4*d^6 + 20*a^3*b^7*c^3*d^7 + 10*a^4*b^6*c^2*d^8 + 4*a^5*b^5*c*d^9 + \\ & a^6*b^4*d^{10})*x^4 + 364*(120*b^{10}*c^7*d^3 + 84*a*b^9*c^6*d^4 + 56*a^2*b^8*c^5*d^5 + 35*a^3*b^7*c^4*d^6 + 20*a^4*b^6*c^3*d^7 + 10*a^5*b^5*c^2*d^8 + \\ & 4*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + 91*(165*b^{10}*c^8*d^2 + 120*a*b^9*c^7*d^3 + 84*a^2*b^8*c^6*d^4 + 56*a^3*b^7*c^5*d^5 + 35*a^4*b^6*c^4*d^6 + \\ & 20*a^5*b^5*c^3*d^7 + 10*a^6*b^4*c^2*d^8 + 4*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 + 14*(220*b^{10}*c^9*d + 165*a*b^9*c^8*d^2 + 120*a^2*b^8*c^7*d^3 + \\ & 84*a^3*b^7*c^6*d^4 + 56*a^4*b^6*c^5*d^5 + 35*a^5*b^5*c^4*d^6 + 20*a^6*b^4*c^3*d^7 + 10*a^7*b^3*c^2*d^8 + 4*a^8*b^2*c*d^9 + a^9*b*d^{10})*x + \\ & 14*a^{12}*b^{13}*x^2 + 14*a^{13}*b^{12}*x + a^{14}*b^{11}) \end{aligned}$$

giac [B] time = 1.39, size = 961, normalized size = 8.01

$$1001 b^{10} d^{10} x^{10} + 8008 b^{10} c d^9 x^9 + 2002 a b^9 d^{10} x^9 + 30030 b^{10} c^2 d^8 x^8 + 12012 a b^9 c d^9 x^8 + 3003 a^2 b^8 d^{10} x^8 + 68640 b^{10} c^3 d^7 x^7 + 34320 a b^9 c^2 d^8 x^7 + 13728 a^2 b^8 c d^9 x^7 + 3432 a^3 b^7 d^{10} x^7 + 105105 b^{10} c^4 d^6 x^6 + 60060 a b^9 c^3 d^7 x^6 + 30030 a^2 b^8 c^2 d^8 x^6 + 12012 a^3 b^7 c d^9 x^6 + 3003 a^4 b^6 d^{10} x^6 + 112112 b^{10} c^5 d^5 x^5 + 70070 a b^9 c^4 d^6 x^5 + 40040 a^2 b^8 c^3 d^7 x^5 + 20020 a^3 b^7 c^2 d^8 x^5 + 8008 a^4 b^6 c d^9 x^5 + 2002 a^5 b^5 d^{10} x^5 + 84084 b^{10} c^6 d^4 x^4 + 56056 a b^9 c^5 d^5 x^4 + 35035 a^2 b^8 c^4 d^6 x^4 + 20020 a^3 b^7 c^3 d^7 x^4 + 10010 a^4 b^6 c^2 d^8 x^4 + 4004 a^5 b^5 c d^9 x^4 + 1001 a^6 b^4 d^{10} x^4 + 43680 b^{10} c^7 d^3 x^3 + 30576 a^7 b^3 c^2 d^8 x^3 + 9100 b^{10} c^8 d^2 x^2 + 12012 a b^9 c^7 d^3 x^2 + 3003 a^2 b^8 c^6 d^4 x^2 + 36400 b^{10} c^9 d x + 364 a^3 b^7 c^5 d^5 x + 9100 a^4 b^6 c^4 d^6 x + 1400 a^5 b^5 c^3 d^7 x + 1400 a^6 b^4 c^2 d^8 x + 1400 a^7 b^3 c d^9 x + 1400 a^8 b^2 d^{10} x + 1400 a^9 b d^{10} x + 1400 a^{10} d^{10} x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^15,x, algorithm="giac")

[Out]
$$\begin{aligned} & -1/4004*(1001*b^{10}*d^{10}*x^{10} + 8008*b^{10}*c*d^9*x^9 + 2002*a*b^9*d^{10}*x^9 + 30030*b^{10}*c^2*d^8*x^8 + 12012*a*b^9*c*d^9*x^8 + 3003*a^2*b^8*d^{10}*x^8 + 68640*b^{10}*c^3*d^7*x^7 + \\ & 34320*a*b^9*c^2*d^8*x^7 + 13728*a^2*b^8*c*d^9*x^7 + 3432*a^3*b^7*d^{10}*x^7 + 105105*b^{10}*c^4*d^6*x^6 + 60060*a*b^9*c^3*d^7*x^6 + 30030*a^2*b^8*c^2*d^8*x^6 + \\ & 12012*a^3*b^7*c*d^9*x^6 + 3003*a^4*b^6*d^{10}*x^6 + 112112*b^{10}*c^5*d^5*x^5 + 70070*a*b^9*c^4*d^6*x^5 + 40040*a^2*b^8*c^3*d^7*x^5 + 20020*a^3*b^7*c^2*d^8*x^5 + \\ & 8008*a^4*b^6*c*d^9*x^5 + 2002*a^5*b^5*d^{10}*x^5 + 84084*b^{10}*c^6*d^4*x^4 + 56056*a*b^9*c^5*d^5*x^4 + 35035*a^2*b^8*c^4*d^6*x^4 + 20020*a^3*b^7*c^3*d^7*x^4 + \\ & 10010*a^4*b^6*c^2*d^8*x^4 + 4004*a^5*b^5*c*d^9*x^4 + 1001*a^6*b^4*d^{10}*x^4 + 43680*b^{10}*c^7*d^3*x^3 + 30576*a^7*b^3*c^2*d^8*x^3 + 9100*b^{10}*c^8*d^2*x^2 + \\ & 12012*a*b^9*c^7*d^3*x^2 + 3003*a^2*b^8*c^6*d^4*x^2 + 36400*b^{10}*c^9*d*x + 364*a^3*b^7*c^5*d^5*x + 9100*a^4*b^6*c^4*d^6*x + 1400*a^5*b^5*c^3*d^7*x + \\ & 1400*a^6*b^4*c^2*d^8*x + 1400*a^7*b^3*c*d^9*x + 1400*a^8*b^2*d^{10}*x + 1400*a^9*b*d^{10}*x + 1400*a^{10}*d^{10}*x) \end{aligned}$$

$$\begin{aligned} & *a*b^9*c^6*d^4*x^3 + 20384*a^2*b^8*c^5*d^5*x^3 + 12740*a^3*b^7*c^4*d^6*x^3 \\ & + 7280*a^4*b^6*c^3*d^7*x^3 + 3640*a^5*b^5*c^2*d^8*x^3 + 1456*a^6*b^4*c*d^9* \\ & x^3 + 364*a^7*b^3*d^10*x^3 + 15015*b^10*c^8*d^2*x^2 + 10920*a*b^9*c^7*d^3*x \\ & ^2 + 7644*a^2*b^8*c^6*d^4*x^2 + 5096*a^3*b^7*c^5*d^5*x^2 + 3185*a^4*b^6*c^4 \\ & *d^6*x^2 + 1820*a^5*b^5*c^3*d^7*x^2 + 910*a^6*b^4*c^2*d^8*x^2 + 364*a^7*b^3 \\ & *c*d^9*x^2 + 91*a^8*b^2*d^10*x^2 + 3080*b^10*c^9*d*x + 2310*a*b^9*c^8*d^2*x \\ & + 1680*a^2*b^8*c^7*d^3*x + 1176*a^3*b^7*c^6*d^4*x + 784*a^4*b^6*c^5*d^5*x \\ & + 490*a^5*b^5*c^4*d^6*x + 280*a^6*b^4*c^3*d^7*x + 140*a^7*b^3*c^2*d^8*x + 5 \\ & 6*a^8*b^2*c*d^9*x + 14*a^9*b*d^10*x + 286*b^10*c^10 + 220*a*b^9*c^9*d + 165 \\ & *a^2*b^8*c^8*d^2 + 120*a^3*b^7*c^7*d^3 + 84*a^4*b^6*c^6*d^4 + 56*a^5*b^5*c^ \\ & 5*d^5 + 35*a^6*b^4*c^4*d^6 + 20*a^7*b^3*c^3*d^7 + 10*a^8*b^2*c^2*d^8 + 4*a^ \\ & 9*b*c*d^9 + a^{10}*d^{10})/((b*x + a)^{14}*b^{11}) \end{aligned}$$

maple [B] time = 0.01, size = 867, normalized size = 7.22

$$\frac{d^{10}}{4(bx+a)^4 b^{11}} + \frac{2(ad-bc)d^9}{(bx+a)^5 b^{11}} - \frac{15(a^2d^2-2abcd+b^2c^2)d^8}{2(bx+a)^6 b^{11}} + \frac{120(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^7}{7(bx+a)^7 b^{11}} - \frac{105}{(bx+a)^8 b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^15,x)

[Out]
$$\begin{aligned} & -105/4*d^6*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/ \\ & b^{11}/(b*x+a)^8+10/13*d*(a^9*d^9-9*a^8*b*c*d^8+36*a^7*b^2*c^2*d^7-84*a^6*b^3 \\ & *c^3*d^6+126*a^5*b^4*c^4*d^5-126*a^4*b^5*c^5*d^4+84*a^3*b^6*c^6*d^3-36*a^2* \\ & b^7*c^7*d^2+9*a*b^8*c^8*d-b^9*c^9)/b^{11}/(b*x+a)^{13}+120/7*d^7*(a^3*d^3-3*a^2 \\ & *b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^{11}/(b*x+a)^7+28*d^5*(a^5*d^5-5*a^4*b*c*d^ \\ & 4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)/b^{11}/(b*x+a) \\ & ^9+2*d^9*(a*d-b*c)/b^{11}/(b*x+a)^5-1/4*d^10/b^{11}/(b*x+a)^4+120/11*d^3*(a^7*d \\ & ^7-7*a^6*b*c*d^6+21*a^5*b^2*c^2*d^5-35*a^4*b^3*c^3*d^4+35*a^3*b^4*c^4*d^3-2 \\ & 1*a^2*b^5*c^5*d^2+7*a*b^6*c^6*d-b^7*c^7)/b^{11}/(b*x+a)^{11}-15/4*d^2*(a^8*d^8- \\ & 8*a^7*b*c*d^7+28*a^6*b^2*c^2*d^6-56*a^5*b^3*c^3*d^5+70*a^4*b^4*c^4*d^4-56*a \\ & ^3*b^5*c^5*d^3+28*a^2*b^6*c^6*d^2-8*a*b^7*c^7*d+b^8*c^8)/b^{11}/(b*x+a)^{12}-15 \\ & /2*d^8*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^{11}/(b*x+a)^6-21*d^4*(a^6*d^6-6*a^5*b*c \\ & *d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d \\ & +b^6*c^6)/b^{11}/(b*x+a)^{10}-1/14*(a^{10}*d^{10}-10*a^9*b*c*d^9+45*a^8*b^2*c^2*d^8 \\ & -120*a^7*b^3*c^3*d^7+210*a^6*b^4*c^4*d^6-252*a^5*b^5*c^5*d^5+210*a^4*b^6*c^ \\ & 6*d^4-120*a^3*b^7*c^7*d^3+45*a^2*b^8*c^8*d^2-10*a*b^9*c^9*d+b^{10}*c^{10})/b^{11} \\ & /(b*x+a)^{14} \end{aligned}$$

maxima [B] time = 2.16, size = 1008, normalized size = 8.40

$$\frac{1001 b^{10} d^{10} x^{10} + 286 b^{10} c^{10} + 220 a b^9 c^9 d + 165 a^2 b^8 c^8 d^2 + 120 a^3 b^7 c^7 d^3 + 84 a^4 b^6 c^6 d^4 + 56 a^5 b^5 c^5 d^5 + 35 a^6 b^4 c^4 d^6 + 28 a^7 b^3 c^3 d^7 + 21 a^8 b^2 c^2 d^8 + 10 a^9 b c d^9 + a^{10} d^{10}}{(b x + a)^{14} b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^15,x, algorithm="maxima")

[Out]
$$\frac{-1/4004*(1001*b^{10}*d^{10}*x^{10} + 286*b^{10}*c^{10} + 220*a*b^9*c^9*d + 165*a^2*b^8*c^8*d^2 + 120*a^3*b^7*c^7*d^3 + 84*a^4*b^6*c^6*d^4 + 56*a^5*b^5*c^5*d^5 + 35*a^6*b^4*c^4*d^6 + 20*a^7*b^3*c^3*d^7 + 10*a^8*b^2*c^2*d^8 + 4*a^9*b*c*d^9 + a^{10}*d^{10} + 2002*(4*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 + 3003*(10*b^{10}*c^2*d^8 + 4*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 3432*(20*b^{10}*c^3*d^7 + 10*a*b^9*c^2*d^8 + 4*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 3003*(35*b^{10}*c^4*d^6 + 20*a*b^9*c^3*d^7 + 10*a^2*b^8*c^2*d^8 + 4*a^3*b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 2002*(56*b^{10}*c^5*d^5 + 35*a*b^9*c^4*d^6 + 20*a^2*b^8*c^3*d^7 + 10*a^3*b^7*c^2*d^8 + 4*a^4*b^6*c*d^9 + a^5*b^5*d^{10})*x^5 + 1001*(84*b^{10}*c^6*d^4 + 56*a*b^9*c^5*d^5 + 35*a^2*b^8*c^4*d^6 + 20*a^3*b^7*c^3*d^7 + 10*a^4*b^6*c^2*d^8 + 4*a^5*b^5*c*d^9 + a^6*b^4*d^{10})*x^4 + 364*(120*b^{10}*c^7*d^3 + 84*a*b^9*c^6*d^4 + 56*a^2*b^8*c^5*d^5 + 35*a^3*b^7*c^4*d^6 + 20*a^4*b^6*c^3*d^7 + 10*a^5*b^5*c^2*d^8 + 4*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + 91*(165*b^{10}*c^8*d^2 + 120*a*b^9*c^7*d^3 + 84*a^2*b^8*c^6*d^4 + 56*a^3*b^7*c^5*d^5 + 35*a^4*b^6*c^4*d^6 + 20*a^5*b^5*c^3*d^7 + 10*a^6*b^4*c^2*d^8 + 4*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 + 14*(220*b^{10}*c^9*d + 165*a*b^9*c^8*d^2 + 120*a^2*b^8*c^7*d^3 + 84*a^3*b^7*c^6*d^4 + 56*a^4*b^6*c^5*d^5 + 35*a^5*b^5*c^4*d^6 + 20*a^6*b^4*c^3*d^7 + 10*a^7*b^3*c^2*d^8 + 4*a^8*b^2*c*d^9 + a^9*b*d^{10})*x)/(b^{25}*x^{14} + 14*a*b^{24}*x^{13} + 91*a^2*b^{23}*x^{12} + 364*a^3*b^{22}*x^{11} + 1001*a^4*b^{21}*x^{10} + 2002*a^5*b^{20}*x^9 + 3003*a^6*b^{19}*x^8 + 3432*a^7*b^{18}*x^7 + 3003*a^8*b^{17}*x^6 + 2002*a^9*b^{16}*x^5 + 1001*a^{10}*b^{15}*x^4 + 364*a^{11}*b^{14}*x^3 + 91*a^{12}*b^{13}*x^2 + 14*a^{13}*b^{12}*x + a^{14}*b^{11})$$

mupad [B] time = 1.30, size = 1109, normalized size = 9.24

$$\frac{a^{10} d^{10} + 4 a^9 b c d^9 + 14 a^9 b d^{10} x + 10 a^8 b^2 c^2 d^8 + 56 a^8 b^2 c d^9 x + 91 a^8 b^2 d^{10} x^2 + 20 a^7 b^3 c^3 d^7 + 140 a^7 b^3 c^2 d^8 x + 1001 a^6 b^4 c^4 d^6 x^2 + 3003 a^6 b^4 c^3 d^7 x^3 + 3432 a^5 b^5 c^5 d^5 x^4 + 1001 a^5 b^5 c^4 d^6 x^5 + 2002 a^4 b^6 c^6 d^4 x^6 + 3432 a^4 b^6 c^5 d^5 x^7 + 3003 a^3 b^7 c^7 d^3 x^8 + 15015 b^{10} c^8 d^2 x^9 + 43680 b^{10} c^7 d^3 x^{10} + 84084 b^{10} c^6 d^4 x^{11} + 112112 b^{10} c^5 d^5 x^{12} + 105105 b^{10} c^4 d^6 x^{13} + 68640 b^{10} c^3 d^7 x^{14} + 30030 b^{10} c^2 d^8 x^{15} + 220 a b^9 c^9 d x^{16} + 4 a^2 b^8 c^8 d^2 x^{17} + 14 a^3 b^7 c^7 d^3 x^{18} + 3080 b^{10} c^9 d x^{19} + 7644 a^2 b^8 c^6 d^4 x^{20} + 5096 a^3 b^7 c^5 d^5 x^{21} + 3185 a^4 b^6 c^4 d^6 x^{22} + 1820 a^5 b^5 c^3 d^7 x^{23} + 910 a^6 b^4 c^2 d^8 x^{24} + 20384 a^2 b^8 c^5 d^5 x^{25} + 12740 a^3 b^7 c^4 d^6 x^{26} + 7280 a^4 b^6 c^3 d^7 x^{27} + 3640 a^5 b^5 c^2 d^8 x^{28}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^15,x)

[Out]
$$-(a^{10}*d^{10} + 286*b^{10}*c^{10} + 1001*b^{10}*d^{10}*x^{10} + 2002*a*b^9*d^{10}*x^9 + 8008*b^{10}*c*d^9*x^9 + 165*a^2*b^8*c^8*d^2 + 120*a^3*b^7*c^7*d^3 + 84*a^4*b^6*c^6*d^4 + 56*a^5*b^5*c^5*d^5 + 35*a^6*b^4*c^4*d^6 + 20*a^7*b^3*c^3*d^7 + 10*a^8*b^2*c^2*d^8 + 91*a^9*b*c*d^9 + a^{10}*d^{10})*x^{10} + 364*a^7*b^3*d^{10}*x^3 + 1001*a^6*b^4*d^{10}*x^4 + 2002*a^5*b^5*d^{10}*x^5 + 3003*a^4*b^6*d^{10}*x^6 + 3432*a^3*b^7*d^{10}*x^7 + 3003*a^2*b^8*d^{10}*x^8 + 15015*b^{10}*c^8*d^2*x^9 + 43680*b^{10}*c^7*d^3*x^{10} + 84084*b^{10}*c^6*d^4*x^{11} + 112112*b^{10}*c^5*d^5*x^{12} + 105105*b^{10}*c^4*d^6*x^{13} + 68640*b^{10}*c^3*d^7*x^{14} + 30030*b^{10}*c^2*d^8*x^{15} + 220*a*b^9*c^9*d + 4*a^2*b^8*c^8*d^2 + 14*a^3*b^7*c^7*d^3 + 3080*b^{10}*c^9*d*x + 7644*a^2*b^8*c^6*d^4*x^2 + 5096*a^3*b^7*c^5*d^5*x^3 + 3185*a^4*b^6*c^4*d^6*x^4 + 1820*a^5*b^5*c^3*d^7*x^5 + 910*a^6*b^4*c^2*d^8*x^6 + 20384*a^2*b^8*c^5*d^5*x^7 + 12740*a^3*b^7*c^4*d^6*x^8 + 7280*a^4*b^6*c^3*d^7*x^9 + 3640*a^5*b^5*c^2*d^8*x^{10}$$

$$\begin{aligned}
& + 35035*a^2*b^8*c^4*d^6*x^4 + 20020*a^3*b^7*c^3*d^7*x^4 + 10010*a^4*b^6*c^2*d^8*x^4 + 40040*a^2*b^8*c^3*d^7*x^5 + 20020*a^3*b^7*c^2*d^8*x^5 + 30030*a^2*b^8*c^2*d^8*x^6 + 2310*a*b^9*c^8*d^2*x + 56*a^8*b^2*c*d^9*x + 12012*a*b^9*c*d^9*x^8 + 1680*a^2*b^8*c^7*d^3*x + 1176*a^3*b^7*c^6*d^4*x + 784*a^4*b^6*c^5*d^5*x + 490*a^5*b^5*c^4*d^6*x + 280*a^6*b^4*c^3*d^7*x + 140*a^7*b^3*c^2*d^8*x + 10920*a*b^9*c^7*d^3*x^2 + 364*a^7*b^3*c*d^9*x^2 + 30576*a*b^9*c^6*d^4*x^3 + 1456*a^6*b^4*c*d^9*x^3 + 56056*a*b^9*c^5*d^5*x^4 + 4004*a^5*b^5*c*d^9*x^4 + 70070*a*b^9*c^4*d^6*x^5 + 8008*a^4*b^6*c*d^9*x^5 + 60060*a*b^9*c^3*d^7*x^6 + 12012*a^3*b^7*c*d^9*x^6 + 34320*a*b^9*c^2*d^8*x^7 + 13728*a^2*b^8*c*d^9*x^7)/(4004*a^14*b^11 + 4004*b^25*x^14 + 56056*a^13*b^12*x + 56056*a*b^24*x^13 + 364364*a^12*b^13*x^2 + 1457456*a^11*b^14*x^3 + 4008004*a^10*b^15*x^4 + 8016008*a^9*b^16*x^5 + 12024012*a^8*b^17*x^6 + 13741728*a^7*b^18*x^7 + 12024012*a^6*b^19*x^8 + 8016008*a^5*b^20*x^9 + 4008004*a^4*b^21*x^10 + 1457456*a^3*b^22*x^11 + 364364*a^2*b^23*x^12)
\end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**15,x)

[Out] Timed out

$$3.1327 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{16}} dx$$

Optimal. Leaf size=151

$$-\frac{d^4(c+dx)^{11}}{15015(a+bx)^{11}(bc-ad)^5} + \frac{d^3(c+dx)^{11}}{1365(a+bx)^{12}(bc-ad)^4} - \frac{2d^2(c+dx)^{11}}{455(a+bx)^{13}(bc-ad)^3} + \frac{2d(c+dx)^{11}}{105(a+bx)^{14}(bc-ad)^2} - \frac{1}{15(a+bx)^{15}}$$

[Out] $-1/15*(d*x+c)^{11}/(-a*d+b*c)/(b*x+a)^{15}+2/105*d*(d*x+c)^{11}/(-a*d+b*c)^2/(b*x+a)^{14}-2/455*d^2*(d*x+c)^{11}/(-a*d+b*c)^3/(b*x+a)^{13}+1/1365*d^3*(d*x+c)^{11}/(-a*d+b*c)^4/(b*x+a)^{12}-1/15015*d^4*(d*x+c)^{11}/(-a*d+b*c)^5/(b*x+a)^{11}$

Rubi [A] time = 0.04, antiderivative size = 151, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{d^4(c+dx)^{11}}{15015(a+bx)^{11}(bc-ad)^5} + \frac{d^3(c+dx)^{11}}{1365(a+bx)^{12}(bc-ad)^4} - \frac{2d^2(c+dx)^{11}}{455(a+bx)^{13}(bc-ad)^3} + \frac{2d(c+dx)^{11}}{105(a+bx)^{14}(bc-ad)^2} - \frac{1}{15(a+bx)^{15}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^16, x]

[Out] $-(c+d*x)^{11}/(15*(b*c-a*d)*(a+b*x)^{15}) + (2*d*(c+d*x)^{11})/(105*(b*c-a*d)^2*(a+b*x)^{14}) - (2*d^2*(c+d*x)^{11})/(455*(b*c-a*d)^3*(a+b*x)^{13}) + (d^3*(c+d*x)^{11})/(1365*(b*c-a*d)^4*(a+b*x)^{12}) - (d^4*(c+d*x)^{11})/(15015*(b*c-a*d)^5*(a+b*x)^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{10}}{(a+bx)^{16}} dx &= -\frac{(c+dx)^{11}}{15(bc-ad)(a+bx)^{15}} - \frac{(4d) \int \frac{(c+dx)^{10}}{(a+bx)^{15}} dx}{15(bc-ad)} \\
&= -\frac{(c+dx)^{11}}{15(bc-ad)(a+bx)^{15}} + \frac{2d(c+dx)^{11}}{105(bc-ad)^2(a+bx)^{14}} + \frac{(2d^2) \int \frac{(c+dx)^{10}}{(a+bx)^{14}} dx}{35(bc-ad)^2} \\
&= -\frac{(c+dx)^{11}}{15(bc-ad)(a+bx)^{15}} + \frac{2d(c+dx)^{11}}{105(bc-ad)^2(a+bx)^{14}} - \frac{2d^2(c+dx)^{11}}{455(bc-ad)^3(a+bx)^{13}} - \frac{(4d^3) \int \frac{(c+dx)^{10}}{(a+bx)^{13}} dx}{455(bc-ad)^3} \\
&= -\frac{(c+dx)^{11}}{15(bc-ad)(a+bx)^{15}} + \frac{2d(c+dx)^{11}}{105(bc-ad)^2(a+bx)^{14}} - \frac{2d^2(c+dx)^{11}}{455(bc-ad)^3(a+bx)^{13}} + \frac{d^3(c+dx)^{11}}{1365(bc-ad)^4(a+bx)^{12}} \\
&= -\frac{(c+dx)^{11}}{15(bc-ad)(a+bx)^{15}} + \frac{2d(c+dx)^{11}}{105(bc-ad)^2(a+bx)^{14}} - \frac{2d^2(c+dx)^{11}}{455(bc-ad)^3(a+bx)^{13}} + \frac{d^3(c+dx)^{11}}{1365(bc-ad)^4(a+bx)^{12}}
\end{aligned}$$

Mathematica [B] time = 0.29, size = 690, normalized size = 4.57

$$\frac{a^{10}d^{10} + 5a^9bd^9(c+3dx) + 15a^8b^2d^8(c^2+5cdx+7d^2x^2) + 5a^7b^3d^7(7c^3+45c^2dx+105cd^2x^2+91d^3x^3) + 35a^6b^4d^6(c^3+9cd^2x+35c^2d^2x^2+35cd^3x^3+39d^4x^4) + 21a^5b^5d^5(6c^4+50c^3dx+175c^2d^2x^2+325c^2d^3x^3+325cd^4x^4+143d^5x^5) + 35a^4b^6d^4(6c^5+54c^4dx+585c^3d^2x^2+429cd^3x^3+143d^4x^4) + 5a^3b^7d^3(66c^6+630c^5dx+2646c^4d^2x^2+6370c^4d^3x^3+9555c^3d^4x^4+9009c^2d^5x^5+5005cd^6x^6+1287d^7x^7) + 15a^2b^8d^2(33c^7+330c^6dx+1470c^5d^2x^2+3822c^5d^3x^3+6370c^4d^4x^4+7007c^3d^5x^5+5005c^2d^6x^6+2145cd^7x^7+429d^8x^8) + 5ab^9d(143c^8+1485c^7dx+6930c^6d^2x^2+19110c^6d^3x^3+34398c^5d^4x^4+42042c^4d^5x^5+35035c^3d^6x^6+19305c^2d^7x^7+6435cd^8x^8+1001d^9x^9) + b^{10}(1001c^9+10725c^8dx+51975c^7d^2x^2+150150c^6d^3x^3+286650c^5d^4x^4+378378c^4d^5x^5+350350c^3d^6x^6+225225c^2d^7x^7+96525cd^8x^8+25025d^9x^9+3003d^{10}x^{10})}{(b^{11}(a+bx)^{15})}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^16,x]

[Out]
$$-\frac{1}{15015} \cdot (a^{10}d^{10} + 5a^9bd^9(c+3dx) + 15a^8b^2d^8(c^2+5cdx+7d^2x^2) + 5a^7b^3d^7(7c^3+45c^2dx+105cd^2x^2+91d^3x^3) + 35a^6b^4d^6(c^3+9cd^2x+35c^2d^2x^2+35cd^3x^3+39d^4x^4) + 21a^5b^5d^5(6c^4+50c^3dx+175c^2d^2x^2+325c^2d^3x^3+325cd^4x^4+143d^5x^5) + 35a^4b^6d^4(6c^5+54c^4dx+585c^3d^2x^2+429cd^3x^3+143d^4x^4) + 5a^3b^7d^3(66c^6+630c^5dx+2646c^4d^2x^2+6370c^4d^3x^3+9555c^3d^4x^4+9009c^2d^5x^5+5005cd^6x^6+1287d^7x^7) + 15a^2b^8d^2(33c^7+330c^6dx+1470c^5d^2x^2+3822c^5d^3x^3+6370c^4d^4x^4+7007c^3d^5x^5+5005c^2d^6x^6+2145cd^7x^7+429d^8x^8) + 5ab^9d(143c^8+1485c^7dx+6930c^6d^2x^2+19110c^6d^3x^3+34398c^5d^4x^4+42042c^4d^5x^5+35035c^3d^6x^6+19305c^2d^7x^7+6435cd^8x^8+1001d^9x^9) + b^{10}(1001c^9+10725c^8dx+51975c^7d^2x^2+150150c^6d^3x^3+286650c^5d^4x^4+378378c^4d^5x^5+350350c^3d^6x^6+225225c^2d^7x^7+96525cd^8x^8+25025d^9x^9+3003d^{10}x^{10})) / (b^{11}(a+bx)^{15})$$

fricas [B] time = 0.50, size = 1019, normalized size = 6.75

$$3003 b^{10} d^{10} x^{10} + 1001 b^{10} c^{10} + 715 a b^9 c^9 d + 495 a^2 b^8 c^8 d^2 + 330 a^3 b^7 c^7 d^3 + 210 a^4 b^6 c^6 d^4 + 126 a^5 b^5 c^5 d^5 + 70 a^6 b^4 c^4 d^6 + 35 a^7 b^3 c^3 d^7 + 15 a^8 b^2 c^2 d^8 + 5 a^9 b c d^9 + a^{10} d^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^16,x, algorithm="fricas")

[Out]
$$-1/15015*(3003*b^{10}*d^{10}*x^{10} + 1001*b^{10}*c^{10} + 715*a*b^9*c^9*d + 495*a^2*b^8*c^8*d^2 + 330*a^3*b^7*c^7*d^3 + 210*a^4*b^6*c^6*d^4 + 126*a^5*b^5*c^5*d^5 + 70*a^6*b^4*c^4*d^6 + 35*a^7*b^3*c^3*d^7 + 15*a^8*b^2*c^2*d^8 + 5*a^9*b*c*d^9 + a^{10}*d^{10} + 5005*(5*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 + 6435*(15*b^{10}*c^2*d^8 + 5*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 6435*(35*b^{10}*c^3*d^7 + 15*a*b^9*c^2*d^8 + 5*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 5005*(70*b^{10}*c^4*d^6 + 35*a*b^9*c^3*d^7 + 15*a^2*b^8*c^2*d^8 + 5*a^3*b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 3003*(126*b^{10}*c^5*d^5 + 70*a*b^9*c^4*d^6 + 35*a^2*b^8*c^3*d^7 + 15*a^3*b^7*c^2*d^8 + 5*a^4*b^6*c*d^9 + a^5*b^5*d^{10})*x^5 + 1365*(210*b^{10}*c^6*d^4 + 126*a*b^9*c^5*d^5 + 70*a^2*b^8*c^4*d^6 + 35*a^3*b^7*c^3*d^7 + 15*a^4*b^6*c^2*d^8 + 5*a^5*b^5*c*d^9 + a^6*b^4*d^{10})*x^4 + 455*(330*b^{10}*c^7*d^3 + 210*a*b^9*c^6*d^4 + 126*a^2*b^8*c^5*d^5 + 70*a^3*b^7*c^4*d^6 + 35*a^4*b^6*c^3*d^7 + 15*a^5*b^5*c^2*d^8 + 5*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + 105*(495*b^{10}*c^8*d^2 + 330*a*b^9*c^7*d^3 + 210*a^2*b^8*c^6*d^4 + 126*a^3*b^7*c^5*d^5 + 70*a^4*b^6*c^4*d^6 + 35*a^5*b^5*c^3*d^7 + 15*a^6*b^4*c^2*d^8 + 5*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 + 15*(715*b^{10}*c^9*d + 495*a*b^9*c^8*d^2 + 330*a^2*b^8*c^7*d^3 + 210*a^3*b^7*c^6*d^4 + 126*a^4*b^6*c^5*d^5 + 70*a^5*b^5*c^4*d^6 + 35*a^6*b^4*c^3*d^7 + 15*a^7*b^3*c^2*d^8 + 5*a^8*b^2*c*d^9 + a^9*b*d^{10})*x)/(b^{26}*x^{15} + 15*a*b^{25}*x^{14} + 105*a^2*b^{24}*x^{13} + 455*a^3*b^{23}*x^{12} + 1365*a^4*b^{22}*x^{11} + 3003*a^5*b^{21}*x^{10} + 5005*a^6*b^{20}*x^9 + 6435*a^7*b^{19}*x^8 + 6435*a^8*b^{18}*x^7 + 5005*a^9*b^{17}*x^6 + 3003*a^{10}*b^{16}*x^5 + 1365*a^{11}*b^{15}*x^4 + 455*a^{12}*b^{14}*x^3 + 105*a^{13}*b^{13}*x^2 + 15*a^{14}*b^{12}*x + a^{15}*b^{11})$$

giac [B] time = 1.32, size = 961, normalized size = 6.36

$$3003 b^{10} d^{10} x^{10} + 25025 b^{10} c d^9 x^9 + 5005 a b^9 d^{10} x^9 + 96525 b^{10} c^2 d^8 x^8 + 32175 a b^9 c d^9 x^8 + 6435 a^2 b^8 d^{10} x^8 + 225225 b^{10} c^3 d^7 x^7 + 96525 a b^9 c^2 d^8 x^7 + 32175 a^2 b^8 c d^9 x^7$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^16,x, algorithm="giac")

[Out]
$$-1/15015*(3003*b^{10}*d^{10}*x^{10} + 25025*b^{10}*c*d^9*x^9 + 5005*a*b^9*d^{10}*x^9 + 96525*b^{10}*c^2*d^8*x^8 + 32175*a*b^9*c*d^9*x^8 + 6435*a^2*b^8*d^{10}*x^8 + 225225*b^{10}*c^3*d^7*x^7 + 96525*a*b^9*c^2*d^8*x^7 + 32175*a^2*b^8*c*d^9*x^7$$

+ 6435*a^3*b^7*d^10*x^7 + 350350*b^10*c^4*d^6*x^6 + 175175*a*b^9*c^3*d^7*x^6 + 75075*a^2*b^8*c^2*d^8*x^6 + 25025*a^3*b^7*c*d^9*x^6 + 5005*a^4*b^6*d^10*x^6 + 378378*b^10*c^5*d^5*x^5 + 210210*a*b^9*c^4*d^6*x^5 + 105105*a^2*b^8*c^3*d^7*x^5 + 45045*a^3*b^7*c^2*d^8*x^5 + 15015*a^4*b^6*c*d^9*x^5 + 3003*a^5*b^5*d^10*x^5 + 286650*b^10*c^6*d^4*x^4 + 171990*a*b^9*c^5*d^5*x^4 + 95550*a^2*b^8*c^4*d^6*x^4 + 47775*a^3*b^7*c^3*d^7*x^4 + 20475*a^4*b^6*c^2*d^8*x^4 + 6825*a^5*b^5*c*d^9*x^4 + 1365*a^6*b^4*d^10*x^4 + 150150*b^10*c^7*d^3*x^3 + 95550*a*b^9*c^6*d^4*x^3 + 57330*a^2*b^8*c^5*d^5*x^3 + 31850*a^3*b^7*c^4*d^6*x^3 + 15925*a^4*b^6*c^3*d^7*x^3 + 6825*a^5*b^5*c^2*d^8*x^3 + 2275*a^6*b^4*c*d^9*x^3 + 455*a^7*b^3*d^10*x^3 + 51975*b^10*c^8*d^2*x^2 + 34650*a*b^9*c^7*d^3*x^2 + 22050*a^2*b^8*c^6*d^4*x^2 + 13230*a^3*b^7*c^5*d^5*x^2 + 7350*a^4*b^6*c^4*d^6*x^2 + 3675*a^5*b^5*c^3*d^7*x^2 + 1575*a^6*b^4*c^2*d^8*x^2 + 525*a^7*b^3*c*d^9*x^2 + 105*a^8*b^2*d^10*x^2 + 10725*b^10*c^9*d*x + 7425*a*b^9*c^8*d^2*x + 4950*a^2*b^8*c^7*d^3*x + 3150*a^3*b^7*c^6*d^4*x + 1890*a^4*b^6*c^5*d^5*x + 1050*a^5*b^5*c^4*d^6*x + 525*a^6*b^4*c^3*d^7*x + 225*a^7*b^3*c^2*d^8*x + 75*a^8*b^2*c*d^9*x + 15*a^9*b*d^10*x + 1001*b^10*c^10 + 715*a*b^9*c^9*d + 495*a^2*b^8*c^8*d^2 + 330*a^3*b^7*c^7*d^3 + 210*a^4*b^6*c^6*d^4 + 126*a^5*b^5*c^5*d^5 + 70*a^6*b^4*c^4*d^6 + 35*a^7*b^3*c^3*d^7 + 15*a^8*b^2*c^2*d^8 + 5*a^9*b*c*d^9 + a^10*d^10)/((b*x + a)^15*b^11)

maple [B] time = 0.01, size = 867, normalized size = 5.74

$$\frac{d^{10}}{5(bx+a)^5 b^{11}} + \frac{5(ad-bc)d^9}{3(bx+a)^6 b^{11}} - \frac{45(a^2d^2-2abcd+b^2c^2)d^8}{7(bx+a)^7 b^{11}} + \frac{15(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^7}{(bx+a)^8 b^{11}} - \frac{70(a^4d^4-4a^3b^2c^2d^2+6a^2b^2c^2d^2-4a^2b^3c^3d+b^4c^4)d^6}{(bx+a)^9 b^{11}} - \frac{1}{5} \frac{d^{10}}{(bx+a)^{11}} - \frac{210}{11} \frac{d^4(a^6d^6-6a^5b^2c^2d^5+15a^4b^2c^2d^4-20a^3b^3c^3d^3+15a^2b^4c^4d^2-6a^2b^5c^5d+b^6c^6)}{(bx+a)^{11}} - \frac{1}{15} \frac{d^{10}}{(bx+a)^{11}} - \frac{10a^9b^2c^2d^8-120a^7b^3c^3d^7+210a^6b^4c^4d^6-252a^5b^5c^5d^5+210a^4b^6c^6d^4-120a^3b^7c^7d^3+45a^2b^8c^8d^2-10a^2b^9c^9d+b^10c^10}{(bx+a)^{11}} - \frac{1}{b^{11}} \frac{d^7(a^7d^7-7a^6b^2c^2d^6+21a^5b^2c^2d^5-35a^4b^3c^3d^4+35a^3b^4c^4d^3-21a^2b^5c^5d^2+7a^2b^6c^6d-b^7c^7)}{(bx+a)^{12}} + \frac{5}{3} \frac{d^9(a^8d^9-9a^7b^2c^2d^8+36a^6b^2c^2d^7-84a^6b^3c^3d^6+126a^5b^4c^4d^5-126a^4b^5c^5d^4+84a^3b^6c^6d^3-36a^2b^7c^7d^2+9a^2b^8c^8d-b^9c^9)}{(bx+a)^{14}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^16,x)

[Out] 15*d^7*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^11/(b*x+a)^8-45/13*d^2*(a^8*d^8-8*a^7*b*c*d^7+28*a^6*b^2*c^2*d^6-56*a^5*b^3*c^3*d^5+70*a^4*b^4*c^4*d^4-56*a^3*b^5*c^5*d^3+28*a^2*b^6*c^6*d^2-8*a*b^7*c^7*d+b^8*c^8)/b^11/(b*x+a)^13-45/7*d^8*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^11/(b*x+a)^7-70/3*d^6*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/b^11/(b*x+a)^9-1/5*d^10/b^11/(b*x+a)^5-210/11*d^4*(a^6*d^6-6*a^5*b^2*c^2*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a^2*b^5*c^5*d+b^6*c^6)/b^11/(b*x+a)^11-1/15*(a^10*d^10-10*a^9*b^2*c^2*d^8-120*a^7*b^3*c^3*d^7+210*a^6*b^4*c^4*d^6-252*a^5*b^5*c^5*d^5+210*a^4*b^6*c^6*d^4-120*a^3*b^7*c^7*d^3+45*a^2*b^8*c^8*d^2-10*a^2*b^9*c^9*d+b^10*c^10)/b^11/(b*x+a)^15+10*d^3*(a^7*d^7-7*a^6*b^2*c^2*d^6+21*a^5*b^2*c^2*d^5-35*a^4*b^3*c^3*d^4+35*a^3*b^4*c^4*d^3-21*a^2*b^5*c^5*d^2+7*a^2*b^6*c^6*d-b^7*c^7)/b^11/(b*x+a)^12+5/3*d^9*(a^8*d^9-9*a^7*b^2*c^2*d^8+36*a^6*b^2*c^2*d^7-84*a^6*b^3*c^3*d^6+126*a^5*b^4*c^4*d^5-126*a^4*b^5*c^5*d^4+84*a^3*b^6*c^6*d^3-36*a^2*b^7*c^7*d^2+9*a^2*b^8*c^8*d-b^9*c^9)/b^11/(b*x+a)^14

maxima [B] time = 2.26, size = 1019, normalized size = 6.75

$$3003 b^{10} d^{10} x^{10} + 1001 b^{10} c^{10} + 715 a b^9 c^9 d + 495 a^2 b^8 c^8 d^2 + 330 a^3 b^7 c^7 d^3 + 210 a^4 b^6 c^6 d^4 + 126 a^5 b^5 c^5 d^5 + 70 a^6 b^4 c^4 d^6 + 35 a^7 b^3 c^3 d^7 + 15 a^8 b^2 c^2 d^8 + 5 a^9 b c d^9 + a^{10} d^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^16,x, algorithm="maxima")

[Out]
$$\frac{-1/15015*(3003*b^{10}*d^{10}*x^{10} + 1001*b^{10}*c^{10} + 715*a*b^9*c^9*d + 495*a^2*b^8*c^8*d^2 + 330*a^3*b^7*c^7*d^3 + 210*a^4*b^6*c^6*d^4 + 126*a^5*b^5*c^5*d^5 + 70*a^6*b^4*c^4*d^6 + 35*a^7*b^3*c^3*d^7 + 15*a^8*b^2*c^2*d^8 + 5*a^9*b*c*d^9 + a^{10}*d^{10} + 5005*(5*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 + 6435*(15*b^{10}*c^2*d^8 + 5*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 6435*(35*b^{10}*c^3*d^7 + 15*a*b^9*c^2*d^8 + 5*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 5005*(70*b^{10}*c^4*d^6 + 35*a*b^9*c^3*d^7 + 15*a^2*b^8*c^2*d^8 + 5*a^3*b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 3003*(126*b^{10}*c^5*d^5 + 70*a*b^9*c^4*d^6 + 35*a^2*b^8*c^3*d^7 + 15*a^3*b^7*c^2*d^8 + 5*a^4*b^6*c*d^9 + a^5*b^5*d^{10})*x^5 + 1365*(210*b^{10}*c^6*d^4 + 126*a*b^9*c^5*d^5 + 70*a^2*b^8*c^4*d^6 + 35*a^3*b^7*c^3*d^7 + 15*a^4*b^6*c^2*d^8 + 5*a^5*b^5*c*d^9 + a^6*b^4*d^{10})*x^4 + 455*(330*b^{10}*c^7*d^3 + 210*a*b^9*c^6*d^4 + 126*a^2*b^8*c^5*d^5 + 70*a^3*b^7*c^4*d^6 + 35*a^4*b^6*c^3*d^7 + 15*a^5*b^5*c^2*d^8 + 5*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + 105*(495*b^{10}*c^8*d^2 + 330*a*b^9*c^7*d^3 + 210*a^2*b^8*c^6*d^4 + 126*a^3*b^7*c^5*d^5 + 70*a^4*b^6*c^4*d^6 + 35*a^5*b^5*c^3*d^7 + 15*a^6*b^4*c^2*d^8 + 5*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 + 15*(715*b^{10}*c^9*d + 495*a*b^9*c^8*d^2 + 330*a^2*b^8*c^7*d^3 + 210*a^3*b^7*c^6*d^4 + 126*a^4*b^6*c^5*d^5 + 70*a^5*b^5*c^4*d^6 + 35*a^6*b^4*c^3*d^7 + 15*a^7*b^3*c^2*d^8 + 5*a^8*b^2*c*d^9 + a^9*b*d^{10})*x)/(b^{26}*x^{15} + 15*a*b^{25}*x^{14} + 105*a^2*b^{24}*x^{13} + 455*a^3*b^{23}*x^{12} + 1365*a^4*b^{22}*x^{11} + 3003*a^5*b^{21}*x^{10} + 5005*a^6*b^{20}*x^9 + 6435*a^7*b^{19}*x^8 + 6435*a^8*b^{18}*x^7 + 5005*a^9*b^{17}*x^6 + 3003*a^{10}*b^{16}*x^5 + 1365*a^{11}*b^{15}*x^4 + 455*a^{12}*b^{14}*x^3 + 105*a^{13}*b^{13}*x^2 + 15*a^{14}*b^{12}*x + a^{15}*b^{11})$$

mupad [B] time = 2.28, size = 1120, normalized size = 7.42

$$a^{10} d^{10} + 5 a^9 b c d^9 + 15 a^9 b d^{10} x + 15 a^8 b^2 c^2 d^8 + 75 a^8 b^2 c d^9 x + 105 a^8 b^2 d^{10} x^2 + 35 a^7 b^3 c^3 d^7 + 225 a^7 b^3 c^2 d^8 x + 105 a^7 b^3 c d^9 x^2 + 35 a^6 b^4 c^4 d^6 + 105 a^6 b^4 c^3 d^7 x + 105 a^6 b^4 c^2 d^8 x^2 + 35 a^5 b^5 c^5 d^5 + 70 a^5 b^5 c^4 d^6 x + 35 a^5 b^5 c^3 d^7 x^2 + 35 a^4 b^6 c^6 d^4 + 126 a^4 b^6 c^5 d^5 x + 126 a^4 b^6 c^4 d^6 x^2 + 35 a^3 b^7 c^7 d^3 + 105 a^3 b^7 c^6 d^4 x + 105 a^3 b^7 c^5 d^5 x^2 + 35 a^2 b^8 c^8 d^2 + 105 a^2 b^8 c^7 d^3 x + 105 a^2 b^8 c^6 d^4 x^2 + 35 a b^9 c^9 d + 105 a b^9 c^8 d^2 x + 105 a b^9 c^7 d^3 x^2 + 5 a^9 b c d^9 x + 5 a^8 b^2 c^2 d^8 x^2 + 5 a^7 b^3 c^3 d^7 x^3 + 5 a^6 b^4 c^4 d^6 x^4 + 5 a^5 b^5 c^5 d^5 x^5 + 5 a^4 b^6 c^6 d^4 x^6 + 5 a^3 b^7 c^7 d^3 x^7 + 5 a^2 b^8 c^8 d^2 x^8 + 5 a b^9 c^9 d x^9 + a^{10} d^{10} x^{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^16,x)

[Out]
$$-(a^{10}*d^{10} + 1001*b^{10}*c^{10} + 3003*b^{10}*d^{10}*x^{10} + 5005*a*b^9*d^{10}*x^9 + 25025*b^{10}*c*d^9*x^9 + 495*a^2*b^8*c^8*d^2 + 330*a^3*b^7*c^7*d^3 + 210*a^4*b^6*c^6*d^4 + 126*a^5*b^5*c^5*d^5 + 70*a^6*b^4*c^4*d^6 + 35*a^7*b^3*c^3*d^7$$

$$\begin{aligned}
& + 15a^8b^2c^2d^8 + 105a^8b^2d^{10}x^2 + 455a^7b^3d^{10}x^3 + 1365a^6b^4d^{10}x^4 + 3003a^5b^5d^{10}x^5 + 5005a^4b^6d^{10}x^6 + 6435a^3b^7d^{10}x^7 + 6435a^2b^8d^{10}x^8 + 51975b^{10}c^8d^2x^2 + 150150b^{10}c^7d^3x^3 + 286650b^{10}c^6d^4x^4 + 378378b^{10}c^5d^5x^5 + 350350b^{10}c^4d^6x^6 + 225225b^{10}c^3d^7x^7 + 96525b^{10}c^2d^8x^8 + 715ab^9c^9d + 5a^9b^9c^9d + 15a^9b^9d^{10}x + 10725b^{10}c^9d^9x + 22050a^2b^8c^6d^4x^2 + 13230a^3b^7c^5d^5x^2 + 7350a^4b^6c^4d^6x^2 + 3675a^5b^5c^3d^7x^2 + 1575a^6b^4c^2d^8x^2 + 57330a^2b^8c^5d^5x^3 + 31850a^3b^7c^4d^6x^3 + 15925a^4b^6c^3d^7x^3 + 6825a^5b^5c^2d^8x^3 + 95550a^2b^8c^4d^6x^4 + 47775a^3b^7c^3d^7x^4 + 20475a^4b^6c^2d^8x^4 + 105105a^2b^8c^3d^7x^5 + 45045a^3b^7c^2d^8x^5 + 75075a^2b^8c^2d^8x^6 + 7425ab^9c^8d^2x + 75a^8b^2c^9d^9x + 32175ab^9c^9d^9x^8 + 4950a^2b^8c^7d^3x + 3150a^3b^7c^6d^4x + 1890a^4b^6c^5d^5x + 1050a^5b^5c^4d^6x + 525a^6b^4c^3d^7x + 225a^7b^3c^2d^8x + 34650ab^9c^7d^3x^2 + 525a^7b^3c^9d^9x^2 + 95550ab^9c^6d^4x^3 + 2275a^6b^4c^9d^9x^3 + 171990ab^9c^5d^5x^4 + 6825a^5b^5c^9d^9x^4 + 210210ab^9c^4d^6x^5 + 15015a^4b^6c^9d^9x^5 + 175175ab^9c^3d^7x^6 + 25025a^3b^7c^9d^9x^6 + 96525ab^9c^2d^8x^7 + 32175a^2b^8c^9d^9x^7)/(15015a^{15}b^{11} + 15015b^{26}x^{15} + 225225a^{14}b^{12}x + 225225ab^{25}x^{14} + 1576575a^{13}b^{13}x^2 + 6831825a^{12}b^{14}x^3 + 20495475a^{11}b^{15}x^4 + 45090045a^{10}b^{16}x^5 + 75150075a^9b^{17}x^6 + 96621525a^8b^{18}x^7 + 96621525a^7b^{19}x^8 + 75150075a^6b^{20}x^9 + 45090045a^5b^{21}x^{10} + 20495475a^4b^{22}x^{11} + 6831825a^3b^{23}x^{12} + 1576575a^2b^{24}x^{13})
\end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**16,x)

[Out] Timed out

$$3.1328 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{17}} dx$$

Optimal. Leaf size=182

$$\frac{d^5(c+dx)^{11}}{48048(a+bx)^{11}(bc-ad)^6} - \frac{d^4(c+dx)^{11}}{4368(a+bx)^{12}(bc-ad)^5} + \frac{d^3(c+dx)^{11}}{728(a+bx)^{13}(bc-ad)^4} - \frac{d^2(c+dx)^{11}}{168(a+bx)^{14}(bc-ad)^3} + \frac{d(c+dx)^{11}}{48(a+bx)^{15}(bc-ad)^2} - \frac{(c+dx)^{11}}{48(a+bx)^{16}(bc-ad)}$$

[Out] $-1/16*(d*x+c)^{11}/(-a*d+b*c)/(b*x+a)^{16}+1/48*d*(d*x+c)^{11}/(-a*d+b*c)^2/(b*x+a)^{15}-1/168*d^2*(d*x+c)^{11}/(-a*d+b*c)^3/(b*x+a)^{14}+1/728*d^3*(d*x+c)^{11}/(-a*d+b*c)^4/(b*x+a)^{13}-1/4368*d^4*(d*x+c)^{11}/(-a*d+b*c)^5/(b*x+a)^{12}+1/48048*d^5*(d*x+c)^{11}/(-a*d+b*c)^6/(b*x+a)^{11}$

Rubi [A] time = 0.06, antiderivative size = 182, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{d^5(c+dx)^{11}}{48048(a+bx)^{11}(bc-ad)^6} - \frac{d^4(c+dx)^{11}}{4368(a+bx)^{12}(bc-ad)^5} + \frac{d^3(c+dx)^{11}}{728(a+bx)^{13}(bc-ad)^4} - \frac{d^2(c+dx)^{11}}{168(a+bx)^{14}(bc-ad)^3} + \frac{d(c+dx)^{11}}{48(a+bx)^{15}(bc-ad)^2} - \frac{(c+dx)^{11}}{48(a+bx)^{16}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^17, x]

[Out] $-(c+d*x)^{11}/(16*(b*c-a*d)*(a+b*x)^{16})+(d*(c+d*x)^{11})/(48*(b*c-a*d)^2*(a+b*x)^{15})-(d^2*(c+d*x)^{11})/(168*(b*c-a*d)^3*(a+b*x)^{14})+(d^3*(c+d*x)^{11})/(728*(b*c-a*d)^4*(a+b*x)^{13})-(d^4*(c+d*x)^{11})/(4368*(b*c-a*d)^5*(a+b*x)^{12})+(d^5*(c+d*x)^{11})/(48048*(b*c-a*d)^6*(a+b*x)^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[n] && (LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler

Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
 \int \frac{(c+dx)^{10}}{(a+bx)^{17}} dx &= -\frac{(c+dx)^{11}}{16(bc-ad)(a+bx)^{16}} - \frac{(5d) \int \frac{(c+dx)^{10}}{(a+bx)^{16}} dx}{16(bc-ad)} \\
 &= -\frac{(c+dx)^{11}}{16(bc-ad)(a+bx)^{16}} + \frac{d(c+dx)^{11}}{48(bc-ad)^2(a+bx)^{15}} + \frac{d^2 \int \frac{(c+dx)^{10}}{(a+bx)^{15}} dx}{12(bc-ad)^2} \\
 &= -\frac{(c+dx)^{11}}{16(bc-ad)(a+bx)^{16}} + \frac{d(c+dx)^{11}}{48(bc-ad)^2(a+bx)^{15}} - \frac{d^2(c+dx)^{11}}{168(bc-ad)^3(a+bx)^{14}} - \frac{d^3 \int \frac{(c+dx)^{10}}{(a+bx)^{14}} dx}{56(bc-ad)^3} \\
 &= -\frac{(c+dx)^{11}}{16(bc-ad)(a+bx)^{16}} + \frac{d(c+dx)^{11}}{48(bc-ad)^2(a+bx)^{15}} - \frac{d^2(c+dx)^{11}}{168(bc-ad)^3(a+bx)^{14}} + \frac{d^3(c+dx)^{11}}{728(bc-ad)^4} \\
 &= -\frac{(c+dx)^{11}}{16(bc-ad)(a+bx)^{16}} + \frac{d(c+dx)^{11}}{48(bc-ad)^2(a+bx)^{15}} - \frac{d^2(c+dx)^{11}}{168(bc-ad)^3(a+bx)^{14}} + \frac{d^3(c+dx)^{11}}{728(bc-ad)^4} \\
 &= -\frac{(c+dx)^{11}}{16(bc-ad)(a+bx)^{16}} + \frac{d(c+dx)^{11}}{48(bc-ad)^2(a+bx)^{15}} - \frac{d^2(c+dx)^{11}}{168(bc-ad)^3(a+bx)^{14}} + \frac{d^3(c+dx)^{11}}{728(bc-ad)^4}
 \end{aligned}$$

Mathematica [B] time = 0.28, size = 694, normalized size = 3.81

$$\frac{a^{10}d^{10} + 2a^9bd^9(3c + 8dx) + 3a^8b^2d^8(7c^2 + 32cdx + 40d^2x^2) + 8a^7b^3d^7(7c^3 + 42c^2dx + 90cd^2x^2 + 70d^3x^3) + \dots}{\dots}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^17, x]

[Out] $-1/48048*(a^{10}d^{10} + 2*a^9*b*d^9*(3*c + 8*d*x) + 3*a^8*b^2*d^8*(7*c^2 + 32*c*d*x + 40*d^2*x^2) + 8*a^7*b^3*d^7*(7*c^3 + 42*c^2*d*x + 90*c*d^2*x^2 + 70*d^3*x^3) + 14*a^6*b^4*d^6*(9*c^4 + 64*c^3*d*x + 180*c^2*d^2*x^2 + 240*c*d^3*x^3 + 130*d^4*x^4) + 84*a^5*b^5*d^5*(3*c^5 + 24*c^4*d*x + 80*c^3*d^2*x^2 + 140*c^2*d^3*x^3 + 130*c*d^4*x^4 + 52*d^5*x^5) + 14*a^4*b^6*d^4*(33*c^6 + 288*c^5*d*x + 1080*c^4*d^2*x^2 + 2240*c^3*d^3*x^3 + 2730*c^2*d^4*x^4 + 1872*c*d^5*x^5 + 572*d^6*x^6) + 8*a^3*b^7*d^3*(99*c^7 + 924*c^6*d*x + 3780*c^5*d^2*x^2 + 8820*c^4*d^3*x^3 + 12740*c^3*d^4*x^4 + 11466*c^2*d^5*x^5 + 6006*c*d^6*x^6 + 1430*d^7*x^7) + 3*a^2*b^8*d^2*(429*c^8 + 4224*c^7*d*x + 18480*c^6*d^2*x^2 + 47040*c^5*d^3*x^3 + 76440*c^4*d^4*x^4 + 81536*c^3*d^5*x^5 + 56056*c^2*d^6*x^6 + 22880*c*d^7*x^7 + 4290*d^8*x^8) + 2*a*b^9*d*(1001*c^9 + 1$

$$\begin{aligned} &0296*c^8*d*x + 47520*c^7*d^2*x^2 + 129360*c^6*d^3*x^3 + 229320*c^5*d^4*x^4 \\ &+ 275184*c^4*d^5*x^5 + 224224*c^3*d^6*x^6 + 120120*c^2*d^7*x^7 + 38610*c*d^8 \\ &+ 8*x^8 + 5720*d^9*x^9) + b^{10}*(3003*c^{10} + 32032*c^9*d*x + 154440*c^8*d^2*x^2 \\ &+ 443520*c^7*d^3*x^3 + 840840*c^6*d^4*x^4 + 1100736*c^5*d^5*x^5 + 1009008 \\ &*c^4*d^6*x^6 + 640640*c^3*d^7*x^7 + 270270*c^2*d^8*x^8 + 68640*c*d^9*x^9 + \\ &8008*d^{10}*x^{10}))/ (b^{11}*(a + b*x)^{16}) \end{aligned}$$

fricas [B] time = 0.48, size = 1030, normalized size = 5.66

$$8008 b^{10} d^{10} x^{10} + 3003 b^{10} c^{10} + 2002 a b^9 c^9 d + 1287 a^2 b^8 c^8 d^2 + 792 a^3 b^7 c^7 d^3 + 462 a^4 b^6 c^6 d^4 + 252 a^5 b^5 c^5 d^5 + 1$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^17,x, algorithm="fricas")

[Out]
$$\begin{aligned} &-1/48048*(8008*b^{10}*d^{10}*x^{10} + 3003*b^{10}*c^{10} + 2002*a*b^9*c^9*d + 1287*a^2 \\ &*b^8*c^8*d^2 + 792*a^3*b^7*c^7*d^3 + 462*a^4*b^6*c^6*d^4 + 252*a^5*b^5*c^5 \\ &*d^5 + 126*a^6*b^4*c^4*d^6 + 56*a^7*b^3*c^3*d^7 + 21*a^8*b^2*c^2*d^8 + 6*a^9 \\ &*b*c*d^9 + a^{10}*d^{10} + 11440*(6*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 + 12870*(21*b \\ &^{10}*c^2*d^8 + 6*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 11440*(56*b^{10}*c^3*d^7 + \\ &21*a*b^9*c^2*d^8 + 6*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 8008*(126*b^{10}*c^4 \\ &*d^6 + 56*a*b^9*c^3*d^7 + 21*a^2*b^8*c^2*d^8 + 6*a^3*b^7*c*d^9 + a^4*b^6*d^{10} \\ &)*x^6 + 4368*(252*b^{10}*c^5*d^5 + 126*a*b^9*c^4*d^6 + 56*a^2*b^8*c^3*d^7 + \\ &21*a^3*b^7*c^2*d^8 + 6*a^4*b^6*c*d^9 + a^5*b^5*d^{10})*x^5 + 1820*(462*b^{10}* \\ &c^6*d^4 + 252*a*b^9*c^5*d^5 + 126*a^2*b^8*c^4*d^6 + 56*a^3*b^7*c^3*d^7 + 21 \\ &*a^4*b^6*c^2*d^8 + 6*a^5*b^5*c*d^9 + a^6*b^4*d^{10})*x^4 + 560*(792*b^{10}*c^7 \\ &d^3 + 462*a*b^9*c^6*d^4 + 252*a^2*b^8*c^5*d^5 + 126*a^3*b^7*c^4*d^6 + 56*a^4 \\ &*b^6*c^3*d^7 + 21*a^5*b^5*c^2*d^8 + 6*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + \\ &120*(1287*b^{10}*c^8*d^2 + 792*a*b^9*c^7*d^3 + 462*a^2*b^8*c^6*d^4 + 252*a^3* \\ &b^7*c^5*d^5 + 126*a^4*b^6*c^4*d^6 + 56*a^5*b^5*c^3*d^7 + 21*a^6*b^4*c^2*d^8 \\ &+ 6*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 + 16*(2002*b^{10}*c^9*d + 1287*a*b^9*c^8 \\ &*d^2 + 792*a^2*b^8*c^7*d^3 + 462*a^3*b^7*c^6*d^4 + 252*a^4*b^6*c^5*d^5 + \\ &126*a^5*b^5*c^4*d^6 + 56*a^6*b^4*c^3*d^7 + 21*a^7*b^3*c^2*d^8 + 6*a^8*b^2*c \\ &*d^9 + a^9*b*d^{10})*x)/(b^{27}*x^{16} + 16*a*b^{26}*x^{15} + 120*a^2*b^{25}*x^{14} + 560 \\ &*a^3*b^{24}*x^{13} + 1820*a^4*b^{23}*x^{12} + 4368*a^5*b^{22}*x^{11} + 8008*a^6*b^{21}*x^{10} \\ &+ 11440*a^7*b^{20}*x^9 + 12870*a^8*b^{19}*x^8 + 11440*a^9*b^{18}*x^7 + 8008*a^{10} \\ &*b^{17}*x^6 + 4368*a^{11}*b^{16}*x^5 + 1820*a^{12}*b^{15}*x^4 + 560*a^{13}*b^{14}*x^3 + \\ &120*a^{14}*b^{13}*x^2 + 16*a^{15}*b^{12}*x + a^{16}*b^{11}) \end{aligned}$$

giac [B] time = 1.31, size = 961, normalized size = 5.28

$$8008 b^{10} d^{10} x^{10} + 68640 b^{10} c d^9 x^9 + 11440 a b^9 d^{10} x^9 + 270270 b^{10} c^2 d^8 x^8 + 77220 a b^9 c d^9 x^8 + 12870 a^2 b^8 d^{10} x^8 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^17,x, algorithm="giac")

[Out]
$$\begin{aligned} & -1/48048*(8008*b^{10}*d^{10}*x^{10} + 68640*b^{10}*c*d^9*x^9 + 11440*a*b^9*d^{10}*x^9 \\ & + 270270*b^{10}*c^2*d^8*x^8 + 77220*a*b^9*c*d^9*x^8 + 12870*a^2*b^8*d^{10}*x^8 \\ & + 640640*b^{10}*c^3*d^7*x^7 + 240240*a*b^9*c^2*d^8*x^7 + 68640*a^2*b^8*c*d^9 \\ & *x^7 + 11440*a^3*b^7*d^{10}*x^7 + 1009008*b^{10}*c^4*d^6*x^6 + 448448*a*b^9*c^3 \\ & *d^7*x^6 + 168168*a^2*b^8*c^2*d^8*x^6 + 48048*a^3*b^7*c*d^9*x^6 + 8008*a^4* \\ & b^6*d^{10}*x^6 + 1100736*b^{10}*c^5*d^5*x^5 + 550368*a*b^9*c^4*d^6*x^5 + 244608 \\ & *a^2*b^8*c^3*d^7*x^5 + 91728*a^3*b^7*c^2*d^8*x^5 + 26208*a^4*b^6*c*d^9*x^5 \\ & + 4368*a^5*b^5*d^{10}*x^5 + 840840*b^{10}*c^6*d^4*x^4 + 458640*a*b^9*c^5*d^5*x^ \\ & 4 + 229320*a^2*b^8*c^4*d^6*x^4 + 101920*a^3*b^7*c^3*d^7*x^4 + 38220*a^4*b^6 \\ & *c^2*d^8*x^4 + 10920*a^5*b^5*c*d^9*x^4 + 1820*a^6*b^4*d^{10}*x^4 + 443520*b^{10} \\ & *c^7*d^3*x^3 + 258720*a*b^9*c^6*d^4*x^3 + 141120*a^2*b^8*c^5*d^5*x^3 + 705 \\ & 60*a^3*b^7*c^4*d^6*x^3 + 31360*a^4*b^6*c^3*d^7*x^3 + 11760*a^5*b^5*c^2*d^8* \\ & x^3 + 3360*a^6*b^4*c*d^9*x^3 + 560*a^7*b^3*d^{10}*x^3 + 154440*b^{10}*c^8*d^2*x \\ & ^2 + 95040*a*b^9*c^7*d^3*x^2 + 55440*a^2*b^8*c^6*d^4*x^2 + 30240*a^3*b^7*c^ \\ & 5*d^5*x^2 + 15120*a^4*b^6*c^4*d^6*x^2 + 6720*a^5*b^5*c^3*d^7*x^2 + 2520*a^6 \\ & *b^4*c^2*d^8*x^2 + 720*a^7*b^3*c*d^9*x^2 + 120*a^8*b^2*d^{10}*x^2 + 32032*b^{10} \\ & *c^9*d*x + 20592*a*b^9*c^8*d^2*x + 12672*a^2*b^8*c^7*d^3*x + 7392*a^3*b^7* \\ & c^6*d^4*x + 4032*a^4*b^6*c^5*d^5*x + 2016*a^5*b^5*c^4*d^6*x + 896*a^6*b^4*c \\ & ^3*d^7*x + 336*a^7*b^3*c^2*d^8*x + 96*a^8*b^2*c*d^9*x + 16*a^9*b*d^{10}*x + 3 \\ & 003*b^{10}*c^{10} + 2002*a*b^9*c^9*d + 1287*a^2*b^8*c^8*d^2 + 792*a^3*b^7*c^7*d \\ & ^3 + 462*a^4*b^6*c^6*d^4 + 252*a^5*b^5*c^5*d^5 + 126*a^6*b^4*c^4*d^6 + 56*a \\ & ^7*b^3*c^3*d^7 + 21*a^8*b^2*c^2*d^8 + 6*a^9*b*c*d^9 + a^{10}*d^{10})/((b*x + a) \\ & ^{16}*b^{11}) \end{aligned}$$

maple [B] time = 0.01, size = 867, normalized size = 4.76

$$\frac{d^{10}}{6(bx+a)^6 b^{11}} + \frac{10(ad-bc)d^9}{7(bx+a)^7 b^{11}} - \frac{45(a^2d^2-2abcd+b^2c^2)d^8}{8(bx+a)^8 b^{11}} + \frac{40(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^7}{3(bx+a)^9 b^{11}} - \frac{21(a^4d^4-4a^3bcd^2+3a^2b^2c^2d-b^3c^3d^2+b^4c^4)}{4(bx+a)^{10} b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^17,x)

[Out]
$$\begin{aligned} & -45/8*d^8*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^{11}/(b*x+a)^8+120/13*d^3*(a^7*d^7-7* \\ & a^6*b*c*d^6+21*a^5*b^2*c^2*d^5-35*a^4*b^3*c^3*d^4+35*a^3*b^4*c^4*d^3-21*a^2 \\ & *b^5*c^5*d^2+7*a*b^6*c^6*d-b^7*c^7)/b^{11}/(b*x+a)^{13}+10/7*d^9*(a*d-b*c)/b^{11} \\ & /(b*x+a)^7+40/3*d^7*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^{11}/(b*x \\ & +a)^9+252/11*d^5*(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d \\ & ^2+5*a*b^4*c^4*d-b^5*c^5)/b^{11}/(b*x+a)^{11}+2/3*d*(a^9*d^9-9*a^8*b*c*d^8+36*a \\ & ^7*b^2*c^2*d^7-84*a^6*b^3*c^3*d^6+126*a^5*b^4*c^4*d^5-126*a^4*b^5*c^5*d^4+8 \\ & 4*a^3*b^6*c^6*d^3-36*a^2*b^7*c^7*d^2+9*a*b^8*c^8*d-b^9*c^9)/b^{11}/(b*x+a)^{15} \\ & -35/2*d^4*(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a \\ & ^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^{11}/(b*x+a)^{12}-1/6*d^{10}/b^{11}/(b*x+a) \\ & ^6-21*d^6*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/b \end{aligned}$$

$$\frac{11}{(b*x+a)^{10}} - \frac{45}{14}d^2 * (a^8d^8 - 8a^7b*c*d^7 + 28a^6b^2*c^2*d^6 - 56a^5b^3*c^3*d^5 + 70a^4b^4*c^4*d^4 - 56a^3b^5*c^5*d^3 + 28a^2b^6*c^6*d^2 - 8a*b^7*c^7*d + b^8*c^8) / b^{11} - \frac{1}{16} * (a^{10}d^{10} - 10a^9b*c*d^9 + 45a^8b^2*c^2*d^8 - 120a^7b^3*c^3*d^7 + 210a^6b^4*c^4*d^6 - 252a^5b^5*c^5*d^5 + 210a^4b^6*c^6*d^4 - 120a^3b^7*c^7*d^3 + 45a^2b^8*c^8*d^2 - 10a*b^9*c^9*d + b^{10}*c^{10}) / b^{11} - \frac{1}{(b*x+a)^{16}}$$

maxima [B] time = 2.27, size = 1030, normalized size = 5.66

$$8008 b^{10} d^{10} x^{10} + 3003 b^{10} c^{10} + 2002 a b^9 c^9 d + 1287 a^2 b^8 c^8 d^2 + 792 a^3 b^7 c^7 d^3 + 462 a^4 b^6 c^6 d^4 + 252 a^5 b^5 c^5 d^5 + 126 a^6 b^4 c^4 d^6 + 56 a^7 b^3 c^3 d^7 + 21 a^8 b^2 c^2 d^8 + 6 a^9 b c d^9 + a^{10} d^{10} + 11440 (6 b^{10} c^3 d^7 + a b^9 d^{10}) x^9 + 12870 (21 b^{10} c^2 d^8 + 6 a b^9 c^2 d^9 + a^2 b^8 d^{10}) x^8 + 11440 (56 b^{10} c^3 d^7 + 21 a b^9 c^2 d^8 + 6 a^2 b^8 c^2 d^9 + a^3 b^7 d^{10}) x^7 + 8008 (126 b^{10} c^4 d^6 + 56 a b^9 c^3 d^7 + 21 a^2 b^8 c^2 d^8 + 6 a^3 b^7 c^2 d^9 + a^4 b^6 d^{10}) x^6 + 4368 (252 b^{10} c^5 d^5 + 126 a b^9 c^4 d^6 + 56 a^2 b^8 c^3 d^7 + 21 a^3 b^7 c^2 d^8 + 6 a^4 b^6 c^2 d^9 + a^5 b^5 d^{10}) x^5 + 1820 (462 b^{10} c^6 d^4 + 252 a b^9 c^5 d^5 + 126 a^2 b^8 c^4 d^6 + 56 a^3 b^7 c^3 d^7 + 21 a^4 b^6 c^2 d^8 + 6 a^5 b^5 c^2 d^9 + a^6 b^4 d^{10}) x^4 + 560 (792 b^{10} c^7 d^3 + 462 a b^9 c^6 d^4 + 252 a^2 b^8 c^5 d^5 + 126 a^3 b^7 c^4 d^6 + 56 a^4 b^6 c^3 d^7 + 21 a^5 b^5 c^2 d^8 + 6 a^6 b^4 c^2 d^9 + a^7 b^3 d^{10}) x^3 + 120 (1287 b^{10} c^8 d^2 + 792 a b^9 c^7 d^3 + 462 a^2 b^8 c^6 d^4 + 252 a^3 b^7 c^5 d^5 + 126 a^4 b^6 c^4 d^6 + 56 a^5 b^5 c^3 d^7 + 21 a^6 b^4 c^2 d^8 + 6 a^7 b^3 c^2 d^9 + a^8 b^2 d^{10}) x^2 + 16 (2002 b^{10} c^9 d + 1287 a b^9 c^8 d^2 + 792 a^2 b^8 c^7 d^3 + 462 a^3 b^7 c^6 d^4 + 252 a^4 b^6 c^5 d^5 + 126 a^5 b^5 c^4 d^6 + 56 a^6 b^4 c^3 d^7 + 21 a^7 b^3 c^2 d^8 + 6 a^8 b^2 c^2 d^9 + a^9 b d^{10}) x + 120 a^{10} b^{14} x^3 + 11440 a^9 b^{18} x^7 + 8008 a^{10} b^{17} x^6 + 4368 a^{11} b^{16} x^5 + 1820 a^{12} b^{15} x^4 + 560 a^{13} b^{14} x^3 + 120 a^{14} b^{13} x^2 + 16 a^{15} b^{12} x + a^{16} b^{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^17,x, algorithm="maxima")

[Out]
$$-1/48048 * (8008 b^{10} d^{10} x^{10} + 3003 b^{10} c^{10} + 2002 a b^9 c^9 d + 1287 a^2 b^8 c^8 d^2 + 792 a^3 b^7 c^7 d^3 + 462 a^4 b^6 c^6 d^4 + 252 a^5 b^5 c^5 d^5 + 126 a^6 b^4 c^4 d^6 + 56 a^7 b^3 c^3 d^7 + 21 a^8 b^2 c^2 d^8 + 6 a^9 b c d^9 + a^{10} d^{10} + 11440 (6 b^{10} c^3 d^7 + a b^9 d^{10}) x^9 + 12870 (21 b^{10} c^2 d^8 + 6 a b^9 c^2 d^9 + a^2 b^8 d^{10}) x^8 + 11440 (56 b^{10} c^3 d^7 + 21 a b^9 c^2 d^8 + 6 a^2 b^8 c^2 d^9 + a^3 b^7 d^{10}) x^7 + 8008 (126 b^{10} c^4 d^6 + 56 a b^9 c^3 d^7 + 21 a^2 b^8 c^2 d^8 + 6 a^3 b^7 c^2 d^9 + a^4 b^6 d^{10}) x^6 + 4368 (252 b^{10} c^5 d^5 + 126 a b^9 c^4 d^6 + 56 a^2 b^8 c^3 d^7 + 21 a^3 b^7 c^2 d^8 + 6 a^4 b^6 c^2 d^9 + a^5 b^5 d^{10}) x^5 + 1820 (462 b^{10} c^6 d^4 + 252 a b^9 c^5 d^5 + 126 a^2 b^8 c^4 d^6 + 56 a^3 b^7 c^3 d^7 + 21 a^4 b^6 c^2 d^8 + 6 a^5 b^5 c^2 d^9 + a^6 b^4 d^{10}) x^4 + 560 (792 b^{10} c^7 d^3 + 462 a b^9 c^6 d^4 + 252 a^2 b^8 c^5 d^5 + 126 a^3 b^7 c^4 d^6 + 56 a^4 b^6 c^3 d^7 + 21 a^5 b^5 c^2 d^8 + 6 a^6 b^4 c^2 d^9 + a^7 b^3 d^{10}) x^3 + 120 (1287 b^{10} c^8 d^2 + 792 a b^9 c^7 d^3 + 462 a^2 b^8 c^6 d^4 + 252 a^3 b^7 c^5 d^5 + 126 a^4 b^6 c^4 d^6 + 56 a^5 b^5 c^3 d^7 + 21 a^6 b^4 c^2 d^8 + 6 a^7 b^3 c^2 d^9 + a^8 b^2 d^{10}) x^2 + 16 (2002 b^{10} c^9 d + 1287 a b^9 c^8 d^2 + 792 a^2 b^8 c^7 d^3 + 462 a^3 b^7 c^6 d^4 + 252 a^4 b^6 c^5 d^5 + 126 a^5 b^5 c^4 d^6 + 56 a^6 b^4 c^3 d^7 + 21 a^7 b^3 c^2 d^8 + 6 a^8 b^2 c^2 d^9 + a^9 b d^{10}) x + 120 a^{10} b^{14} x^3 + 11440 a^9 b^{18} x^7 + 8008 a^{10} b^{17} x^6 + 4368 a^{11} b^{16} x^5 + 1820 a^{12} b^{15} x^4 + 560 a^{13} b^{14} x^3 + 120 a^{14} b^{13} x^2 + 16 a^{15} b^{12} x + a^{16} b^{11})$$

mupad [B] time = 0.58, size = 1131, normalized size = 6.21

$$a^{10} d^{10} + 6 a^9 b c d^9 + 16 a^9 b d^{10} x + 21 a^8 b^2 c^2 d^8 + 96 a^8 b^2 c d^9 x + 120 a^8 b^2 d^{10} x^2 + 56 a^7 b^3 c^3 d^7 + 336 a^7 b^3 c^2 d^8 + 120 a^6 b^4 c^4 d^6 + 56 a^6 b^4 c^3 d^7 + 21 a^5 b^5 c^5 d^5 + 126 a^5 b^5 c^4 d^6 + 56 a^4 b^6 c^6 d^4 + 252 a^4 b^6 c^5 d^5 + 126 a^3 b^7 c^7 d^3 + 462 a^3 b^7 c^6 d^4 + 252 a^2 b^8 c^8 d^2 + 126 a^2 b^8 c^7 d^3 + 56 a^1 b^9 c^9 d + 11440 a^{10} b^{14} x^3 + 11440 a^9 b^{18} x^7 + 8008 a^{10} b^{17} x^6 + 4368 a^{11} b^{16} x^5 + 1820 a^{12} b^{15} x^4 + 560 a^{13} b^{14} x^3 + 120 a^{14} b^{13} x^2 + 16 a^{15} b^{12} x + a^{16} b^{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((c + d*x)^{10}/(a + b*x)^{17},x)$

[Out] $-(a^{10}d^{10} + 3003b^{10}c^{10} + 8008b^{10}d^{10}x^{10} + 11440a*b^9*d^{10}*x^9 + 68640b^{10}*c*d^9*x^9 + 1287a^2*b^8*c^8*d^2 + 792a^3*b^7*c^7*d^3 + 462a^4*b^6*c^6*d^4 + 252a^5*b^5*c^5*d^5 + 126a^6*b^4*c^4*d^6 + 56a^7*b^3*c^3*d^7 + 21a^8*b^2*c^2*d^8 + 120a^8*b^2*d^{10}*x^2 + 560a^7*b^3*d^{10}*x^3 + 1820a^6*b^4*d^{10}*x^4 + 4368a^5*b^5*d^{10}*x^5 + 8008a^4*b^6*d^{10}*x^6 + 11440a^3*b^7*d^{10}*x^7 + 12870a^2*b^8*d^{10}*x^8 + 154440b^{10}*c^8*d^2*x^2 + 443520b^{10}*c^7*d^3*x^3 + 840840b^{10}*c^6*d^4*x^4 + 1100736b^{10}*c^5*d^5*x^5 + 1009008b^{10}*c^4*d^6*x^6 + 640640b^{10}*c^3*d^7*x^7 + 270270b^{10}*c^2*d^8*x^8 + 2002a*b^9*c^9*d + 6a^9*b*c*d^9 + 16a^9*b*d^{10}*x + 32032b^{10}*c^9*d*x + 55440a^2*b^8*c^6*d^4*x^2 + 30240a^3*b^7*c^5*d^5*x^2 + 15120a^4*b^6*c^4*d^6*x^2 + 6720a^5*b^5*c^3*d^7*x^2 + 2520a^6*b^4*c^2*d^8*x^2 + 141120a^2*b^8*c^5*d^5*x^3 + 70560a^3*b^7*c^4*d^6*x^3 + 31360a^4*b^6*c^3*d^7*x^3 + 11760a^5*b^5*c^2*d^8*x^3 + 229320a^2*b^8*c^4*d^6*x^4 + 101920a^3*b^7*c^3*d^7*x^4 + 38220a^4*b^6*c^2*d^8*x^4 + 244608a^2*b^8*c^3*d^7*x^5 + 91728a^3*b^7*c^2*d^8*x^5 + 168168a^2*b^8*c^2*d^8*x^6 + 20592a*b^9*c^8*d^2*x + 96a^8*b^2*c*d^9*x + 77220a*b^9*c*d^9*x^8 + 12672a^2*b^8*c^7*d^3*x + 7392a^3*b^7*c^6*d^4*x + 4032a^4*b^6*c^5*d^5*x + 2016a^5*b^5*c^4*d^6*x + 896a^6*b^4*c^3*d^7*x + 336a^7*b^3*c^2*d^8*x + 95040a*b^9*c^7*d^3*x^2 + 720a^7*b^3*c*d^9*x^2 + 258720a*b^9*c^6*d^4*x^3 + 3360a^6*b^4*c*d^9*x^3 + 458640a*b^9*c^5*d^5*x^4 + 10920a^5*b^5*c*d^9*x^4 + 550368a*b^9*c^4*d^6*x^5 + 26208a^4*b^6*c*d^9*x^5 + 448448a*b^9*c^3*d^7*x^6 + 48048a^3*b^7*c*d^9*x^6 + 240240a*b^9*c^2*d^8*x^7 + 68640a^2*b^8*c*d^9*x^7)/(48048a^{16}b^{11} + 48048b^{27}*x^{16} + 768768a^{15}b^{12}*x + 768768a*b^{26}*x^{15} + 5765760a^{14}b^{13}*x^2 + 26906880a^{13}b^{14}*x^3 + 87447360a^{12}b^{15}*x^4 + 209873664a^{11}b^{16}*x^5 + 384768384a^{10}b^{17}*x^6 + 549669120a^9*b^{18}*x^7 + 618377760a^8*b^{19}*x^8 + 549669120a^7*b^{20}*x^9 + 384768384a^6*b^{21}*x^{10} + 209873664a^5*b^{22}*x^{11} + 87447360a^4*b^{23}*x^{12} + 26906880a^3*b^{24}*x^{13} + 5765760a^2*b^{25}*x^{14})$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x+c)**10/(b*x+a)**17,x)$

[Out] Timed out

$$3.1329 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{18}} dx$$

Optimal. Leaf size=213

$$-\frac{d^6(c+dx)^{11}}{136136(a+bx)^{11}(bc-ad)^7} + \frac{d^5(c+dx)^{11}}{12376(a+bx)^{12}(bc-ad)^6} - \frac{3d^4(c+dx)^{11}}{6188(a+bx)^{13}(bc-ad)^5} + \frac{d^3(c+dx)^{11}}{476(a+bx)^{14}(bc-ad)^4} - \frac{d^2(c+dx)^{11}}{136(a+bx)^{15}(bc-ad)^3} + \frac{d(c+dx)^{11}}{136136(a+bx)^{16}(bc-ad)^2} - \frac{d^2(c+dx)^{11}}{136136(a+bx)^{17}(bc-ad)}$$

[Out] $-1/17*(d*x+c)^{11}/(-a*d+b*c)/(b*x+a)^{17}+3/136*d*(d*x+c)^{11}/(-a*d+b*c)^2/(b*x+a)^{16}-1/136*d^2*(d*x+c)^{11}/(-a*d+b*c)^3/(b*x+a)^{15}+1/476*d^3*(d*x+c)^{11}/(-a*d+b*c)^4/(b*x+a)^{14}-3/6188*d^4*(d*x+c)^{11}/(-a*d+b*c)^5/(b*x+a)^{13}+1/12376*d^5*(d*x+c)^{11}/(-a*d+b*c)^6/(b*x+a)^{12}-1/136136*d^6*(d*x+c)^{11}/(-a*d+b*c)^7/(b*x+a)^{11}$

Rubi [A] time = 0.08, antiderivative size = 213, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$-\frac{d^6(c+dx)^{11}}{136136(a+bx)^{11}(bc-ad)^7} + \frac{d^5(c+dx)^{11}}{12376(a+bx)^{12}(bc-ad)^6} - \frac{3d^4(c+dx)^{11}}{6188(a+bx)^{13}(bc-ad)^5} + \frac{d^3(c+dx)^{11}}{476(a+bx)^{14}(bc-ad)^4} - \frac{d^2(c+dx)^{11}}{136(a+bx)^{15}(bc-ad)^3} + \frac{d(c+dx)^{11}}{136136(a+bx)^{16}(bc-ad)^2} - \frac{d^2(c+dx)^{11}}{136136(a+bx)^{17}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^18, x]

[Out] $-(c+d*x)^{11}/(17*(b*c-a*d)*(a+b*x)^{17})+(3*d*(c+d*x)^{11})/(136*(b*c-a*d)^2*(a+b*x)^{16})-(d^2*(c+d*x)^{11})/(136*(b*c-a*d)^3*(a+b*x)^{15})+(d^3*(c+d*x)^{11})/(476*(b*c-a*d)^4*(a+b*x)^{14})-(3*d^4*(c+d*x)^{11})/(6188*(b*c-a*d)^5*(a+b*x)^{13})+(d^5*(c+d*x)^{11})/(12376*(b*c-a*d)^6*(a+b*x)^{12})-(d^6*(c+d*x)^{11})/(136136*(b*c-a*d)^7*(a+b*x)^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[n] && !IntegerQ[m] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimpler

Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
 \int \frac{(c+dx)^{10}}{(a+bx)^{18}} dx &= -\frac{(c+dx)^{11}}{17(bc-ad)(a+bx)^{17}} - \frac{(6d) \int \frac{(c+dx)^{10}}{(a+bx)^{17}} dx}{17(bc-ad)} \\
 &= -\frac{(c+dx)^{11}}{17(bc-ad)(a+bx)^{17}} + \frac{3d(c+dx)^{11}}{136(bc-ad)^2(a+bx)^{16}} + \frac{(15d^2) \int \frac{(c+dx)^{10}}{(a+bx)^{16}} dx}{136(bc-ad)^2} \\
 &= -\frac{(c+dx)^{11}}{17(bc-ad)(a+bx)^{17}} + \frac{3d(c+dx)^{11}}{136(bc-ad)^2(a+bx)^{16}} - \frac{d^2(c+dx)^{11}}{136(bc-ad)^3(a+bx)^{15}} - \frac{d^3 \int \frac{(c+dx)^{10}}{(a+bx)^{15}} dx}{34(bc-ad)} \\
 &= -\frac{(c+dx)^{11}}{17(bc-ad)(a+bx)^{17}} + \frac{3d(c+dx)^{11}}{136(bc-ad)^2(a+bx)^{16}} - \frac{d^2(c+dx)^{11}}{136(bc-ad)^3(a+bx)^{15}} + \frac{d^3(c+dx)^{11}}{476(bc-ad)^4} \\
 &= -\frac{(c+dx)^{11}}{17(bc-ad)(a+bx)^{17}} + \frac{3d(c+dx)^{11}}{136(bc-ad)^2(a+bx)^{16}} - \frac{d^2(c+dx)^{11}}{136(bc-ad)^3(a+bx)^{15}} + \frac{d^3(c+dx)^{11}}{476(bc-ad)^4} \\
 &= -\frac{(c+dx)^{11}}{17(bc-ad)(a+bx)^{17}} + \frac{3d(c+dx)^{11}}{136(bc-ad)^2(a+bx)^{16}} - \frac{d^2(c+dx)^{11}}{136(bc-ad)^3(a+bx)^{15}} + \frac{d^3(c+dx)^{11}}{476(bc-ad)^4} \\
 &= -\frac{(c+dx)^{11}}{17(bc-ad)(a+bx)^{17}} + \frac{3d(c+dx)^{11}}{136(bc-ad)^2(a+bx)^{16}} - \frac{d^2(c+dx)^{11}}{136(bc-ad)^3(a+bx)^{15}} + \frac{d^3(c+dx)^{11}}{476(bc-ad)^4}
 \end{aligned}$$

Mathematica [B] time = 0.32, size = 690, normalized size = 3.24

$$\frac{a^{10}d^{10} + a^9bd^9(7c + 17dx) + a^8b^2d^8(28c^2 + 119cdx + 136d^2x^2) + 4a^7b^3d^7(21c^3 + 119c^2dx + 238cd^2x^2 + 170ad^3x^3)}{17(bc-ad)^4(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^18,x]

[Out] $-\frac{1}{136136} (a^{10}d^{10} + a^9b^2d^9(7c + 17dx) + a^8b^2d^8(28c^2 + 119cdx + 136d^2x^2) + 4a^7b^3d^7(21c^3 + 119c^2dx + 238cd^2x^2 + 170ad^3x^3) + 14a^6b^4d^6(15c^4 + 102c^3dx + 272c^2d^2x^2 + 340cd^3x^3 + 170d^4x^4) + 14a^5b^5d^5(33c^5 + 255c^4dx + 816c^3d^2x^2 + 1360c^2d^3x^3 + 1190cd^4x^4 + 442d^5x^5) + 14a^4b^6d^4(66c^6 + 561c^5dx + 2040c^4d^2x^2 + 4080c^3d^3x^3 + 4760c^2d^4x^4 + 3094cd^5x^5 + 884d^6x^6) + 4a^3b^7d^3(429c^7 + 3927c^6dx + 15708c^5d^2x^2 + 35700c^4d^3x^3 + 49980c^3d^4x^4 + 43316c^2d^5x^5 + 27720cd^6x^6 + 7290d^7x^7))$

$$2*d^5*x^5 + 21658*c*d^6*x^6 + 4862*d^7*x^7) + a^2*b^8*d^2*(3003*c^8 + 29172*c^7*d*x + 125664*c^6*d^2*x^2 + 314160*c^5*d^3*x^3 + 499800*c^4*d^4*x^4 + 519792*c^3*d^5*x^5 + 346528*c^2*d^6*x^6 + 136136*c*d^7*x^7 + 24310*d^8*x^8) + a*b^9*d*(5005*c^9 + 51051*c^8*d*x + 233376*c^7*d^2*x^2 + 628320*c^6*d^3*x^3 + 1099560*c^5*d^4*x^4 + 1299480*c^4*d^5*x^5 + 1039584*c^3*d^6*x^6 + 544544*c^2*d^7*x^7 + 170170*c*d^8*x^8 + 24310*d^9*x^9) + b^10*(8008*c^10 + 85085*c^9*d*x + 408408*c^8*d^2*x^2 + 1166880*c^7*d^3*x^3 + 2199120*c^6*d^4*x^4 + 2858856*c^5*d^5*x^5 + 2598960*c^4*d^6*x^6 + 1633632*c^3*d^7*x^7 + 680680*c^2*d^8*x^8 + 170170*c*d^9*x^9 + 19448*d^10*x^10))/(b^11*(a + b*x)^17)$$

fricas [B] time = 0.48, size = 1041, normalized size = 4.89

$$19448 b^{10} d^{10} x^{10} + 8008 b^{10} c^{10} + 5005 a b^9 c^9 d + 3003 a^2 b^8 c^8 d^2 + 1716 a^3 b^7 c^7 d^3 + 924 a^4 b^6 c^6 d^4 + 462 a^5 b^5 c^5 d^5 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^18,x, algorithm="fricas")

[Out]
$$-1/136136*(19448*b^{10}*d^{10}*x^{10} + 8008*b^{10}*c^{10} + 5005*a*b^9*c^9*d + 3003*a^2*b^8*c^8*d^2 + 1716*a^3*b^7*c^7*d^3 + 924*a^4*b^6*c^6*d^4 + 462*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 + 84*a^7*b^3*c^3*d^7 + 28*a^8*b^2*c^2*d^8 + 7*a^9*b*c*d^9 + a^{10}*d^{10} + 24310*(7*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 + 24310*(8*b^{10}*c^2*d^8 + 7*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 19448*(84*b^{10}*c^3*d^7 + 28*a*b^9*c^2*d^8 + 7*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 12376*(210*b^{10}*c^4*d^6 + 84*a*b^9*c^3*d^7 + 28*a^2*b^8*c^2*d^8 + 7*a^3*b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 6188*(462*b^{10}*c^5*d^5 + 210*a*b^9*c^4*d^6 + 84*a^2*b^8*c^3*d^7 + 28*a^3*b^7*c^2*d^8 + 7*a^4*b^6*c*d^9 + a^5*b^5*d^{10})*x^5 + 2380*(924*b^{10}*c^6*d^4 + 462*a*b^9*c^5*d^5 + 210*a^2*b^8*c^4*d^6 + 84*a^3*b^7*c^3*d^7 + 28*a^4*b^6*c^2*d^8 + 7*a^5*b^5*c*d^9 + a^6*b^4*d^{10})*x^4 + 680*(1716*b^{10}*c^7*d^3 + 924*a*b^9*c^6*d^4 + 462*a^2*b^8*c^5*d^5 + 210*a^3*b^7*c^4*d^6 + 84*a^4*b^6*c^3*d^7 + 28*a^5*b^5*c^2*d^8 + 7*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + 136*(3003*b^{10}*c^8*d^2 + 1716*a*b^9*c^7*d^3 + 924*a^2*b^8*c^6*d^4 + 462*a^3*b^7*c^5*d^5 + 210*a^4*b^6*c^4*d^6 + 84*a^5*b^5*c^3*d^7 + 28*a^6*b^4*c^2*d^8 + 7*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 + 17*(5005*b^{10}*c^9*d + 3003*a*b^9*c^8*d^2 + 1716*a^2*b^8*c^7*d^3 + 924*a^3*b^7*c^6*d^4 + 462*a^4*b^6*c^5*d^5 + 210*a^5*b^5*c^4*d^6 + 84*a^6*b^4*c^3*d^7 + 28*a^7*b^3*c^2*d^8 + 7*a^8*b^2*c*d^9 + a^9*b*d^{10})*x)/(b^{28}*x^{17} + 17*a*b^{27}*x^{16} + 136*a^2*b^{26}*x^{15} + 680*a^3*b^{25}*x^{14} + 2380*a^4*b^{24}*x^{13} + 6188*a^5*b^{23}*x^{12} + 12376*a^6*b^{22}*x^{11} + 19448*a^7*b^{21}*x^{10} + 24310*a^8*b^{20}*x^9 + 24310*a^9*b^{19}*x^8 + 19448*a^{10}*b^{18}*x^7 + 12376*a^{11}*b^{17}*x^6 + 6188*a^{12}*b^{16}*x^5 + 2380*a^{13}*b^{15}*x^4 + 680*a^{14}*b^{14}*x^3 + 136*a^{15}*b^{13}*x^2 + 17*a^{16}*b^{12}*x + a^{17}*b^{11})$$

giac [B] time = 1.32, size = 961, normalized size = 4.51

$$\frac{19448 b^{10} d^{10} x^{10} + 170170 b^{10} c d^9 x^9 + 24310 a b^9 d^{10} x^9 + 680680 b^{10} c^2 d^8 x^8 + 170170 a b^9 c d^9 x^8 + 24310 a^2 b^8 d^{10} x^8 + 1633632 b^{10} c^3 d^7 x^7 + 544544 a b^9 c^2 d^8 x^7 + 136136 a^2 b^8 c^3 d^9 x^7 + 19448 a^3 b^7 d^{10} x^7 + 2598960 b^{10} c^4 d^6 x^6 + 1039584 a b^9 c^3 d^7 x^6 + 346528 a^2 b^8 c^2 d^8 x^6 + 86632 a^3 b^7 c^2 d^9 x^6 + 12376 a^4 b^6 d^{10} x^6 + 2858856 b^{10} c^5 d^5 x^5 + 1299480 a b^9 c^4 d^6 x^5 + 519792 a^2 b^8 c^3 d^7 x^5 + 173264 a^3 b^7 c^2 d^8 x^5 + 43316 a^4 b^6 c^2 d^9 x^5 + 6188 a^5 b^5 d^{10} x^5 + 2199120 b^{10} c^6 d^4 x^4 + 1099560 a b^9 c^5 d^5 x^4 + 499800 a^2 b^8 c^4 d^6 x^4 + 199920 a^3 b^7 c^3 d^7 x^4 + 66640 a^4 b^6 c^2 d^8 x^4 + 16660 a^5 b^5 c^2 d^9 x^4 + 2380 a^6 b^4 d^{10} x^4 + 1166880 b^{10} c^7 d^3 x^3 + 628320 a b^9 c^6 d^4 x^3 + 314160 a^2 b^8 c^5 d^5 x^3 + 142800 a^3 b^7 c^4 d^6 x^3 + 57120 a^4 b^6 c^3 d^7 x^3 + 19040 a^5 b^5 c^2 d^8 x^3 + 4760 a^6 b^4 c^2 d^9 x^3 + 680 a^7 b^3 d^{10} x^3 + 408408 b^{10} c^8 d^2 x^2 + 233376 a b^9 c^7 d^3 x^2 + 125664 a^2 b^8 c^6 d^4 x^2 + 62832 a^3 b^7 c^5 d^5 x^2 + 28560 a^4 b^6 c^4 d^6 x^2 + 11424 a^5 b^5 c^3 d^7 x^2 + 3808 a^6 b^4 c^2 d^8 x^2 + 952 a^7 b^3 c^2 d^9 x^2 + 136 a^8 b^2 d^{10} x^2 + 85085 b^{10} c^9 d x + 51051 a b^9 c^8 d^2 x + 29172 a^2 b^8 c^7 d^3 x + 15708 a^3 b^7 c^6 d^4 x + 7854 a^4 b^6 c^5 d^5 x + 3570 a^5 b^5 c^4 d^6 x + 1428 a^6 b^4 c^3 d^7 x + 476 a^7 b^3 c^2 d^8 x + 119 a^8 b^2 c^2 d^9 x + 17 a^9 b^2 d^{10} x + 8008 b^{10} c^{10} + 5005 a b^9 c^9 d + 3003 a^2 b^8 c^8 d^2 + 1716 a^3 b^7 c^7 d^3 + 924 a^4 b^6 c^6 d^4 + 462 a^5 b^5 c^5 d^5 + 210 a^6 b^4 c^4 d^6 + 84 a^7 b^3 c^3 d^7 + 28 a^8 b^2 c^2 d^8 + 7 a^9 b^2 c^2 d^9 + a^{10} d^{10}}{(b x + a)^{17} b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^18,x, algorithm="giac")

[Out]
$$\frac{-1/136136*(19448*b^{10}*d^{10}*x^{10} + 170170*b^{10}*c*d^9*x^9 + 24310*a*b^9*d^{10}*x^9 + 680680*b^{10}*c^2*d^8*x^8 + 170170*a*b^9*c*d^9*x^8 + 24310*a^2*b^8*d^{10}*x^8 + 1633632*b^{10}*c^3*d^7*x^7 + 544544*a*b^9*c^2*d^8*x^7 + 136136*a^2*b^8*c^3*d^9*x^7 + 19448*a^3*b^7*d^{10}*x^7 + 2598960*b^{10}*c^4*d^6*x^6 + 1039584*a*b^9*c^3*d^7*x^6 + 346528*a^2*b^8*c^2*d^8*x^6 + 86632*a^3*b^7*c^2*d^9*x^6 + 12376*a^4*b^6*d^{10}*x^6 + 2858856*b^{10}*c^5*d^5*x^5 + 1299480*a*b^9*c^4*d^6*x^5 + 519792*a^2*b^8*c^3*d^7*x^5 + 173264*a^3*b^7*c^2*d^8*x^5 + 43316*a^4*b^6*c^2*d^9*x^5 + 6188*a^5*b^5*d^{10}*x^5 + 2199120*b^{10}*c^6*d^4*x^4 + 1099560*a*b^9*c^5*d^5*x^4 + 499800*a^2*b^8*c^4*d^6*x^4 + 199920*a^3*b^7*c^3*d^7*x^4 + 66640*a^4*b^6*c^2*d^8*x^4 + 16660*a^5*b^5*c^2*d^9*x^4 + 2380*a^6*b^4*d^{10}*x^4 + 1166880*b^{10}*c^7*d^3*x^3 + 628320*a*b^9*c^6*d^4*x^3 + 314160*a^2*b^8*c^5*d^5*x^3 + 142800*a^3*b^7*c^4*d^6*x^3 + 57120*a^4*b^6*c^3*d^7*x^3 + 19040*a^5*b^5*c^2*d^8*x^3 + 4760*a^6*b^4*c^2*d^9*x^3 + 680*a^7*b^3*d^{10}*x^3 + 408408*b^{10}*c^8*d^2*x^2 + 233376*a*b^9*c^7*d^3*x^2 + 125664*a^2*b^8*c^6*d^4*x^2 + 62832*a^3*b^7*c^5*d^5*x^2 + 28560*a^4*b^6*c^4*d^6*x^2 + 11424*a^5*b^5*c^3*d^7*x^2 + 3808*a^6*b^4*c^2*d^8*x^2 + 952*a^7*b^3*c^2*d^9*x^2 + 136*a^8*b^2*d^{10}*x^2 + 85085*b^{10}*c^9*d*x + 51051*a*b^9*c^8*d^2*x + 29172*a^2*b^8*c^7*d^3*x + 15708*a^3*b^7*c^6*d^4*x + 7854*a^4*b^6*c^5*d^5*x + 3570*a^5*b^5*c^4*d^6*x + 1428*a^6*b^4*c^3*d^7*x + 476*a^7*b^3*c^2*d^8*x + 119*a^8*b^2*c^2*d^9*x + 17*a^9*b^2*d^{10}*x + 8008*b^{10}*c^{10} + 5005*a*b^9*c^9*d + 3003*a^2*b^8*c^8*d^2 + 1716*a^3*b^7*c^7*d^3 + 924*a^4*b^6*c^6*d^4 + 462*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 + 84*a^7*b^3*c^3*d^7 + 28*a^8*b^2*c^2*d^8 + 7*a^9*b^2*c^2*d^9 + a^{10}*d^{10})}{(b*x + a)^{17}*b^{11}}$$

maple [B] time = 0.01, size = 867, normalized size = 4.07

$$\frac{d^{10}}{7(bx+a)^7 b^{11}} + \frac{5(ad-bc)d^9}{4(bx+a)^8 b^{11}} - \frac{5(a^2d^2-2abcd+b^2c^2)d^8}{(bx+a)^9 b^{11}} + \frac{12(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^7}{(bx+a)^{10} b^{11}} - \frac{210(a^4d^4-4a^3bcd^3+6a^2b^2c^2d^2-4ab^3c^2d+b^4c^3)}{(bx+a)^{11} b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^18,x)

[Out]
$$\frac{5}{4}d^9(a*d-b*c)/b^{11}/(b*x+a)^8 - \frac{210}{13}d^4(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^{11} - \frac{1}{(b*x+a)^{13}} - \frac{1}{7}d^{10}/b^{11}/(b*x+a)^7 - \frac{5*d^8*(a^2*d^2-2*a*b*c*d+b^2*c^2)}{b^{11}}$$

$$\frac{1}{(b*x+a)^9} - \frac{1}{17} * (a^{10}d^{10} - 10a^9b*c*d^9 + 45a^8b^2c^2*d^8 - 120a^7b^3c^3*d^7 + 210a^6b^4c^4*d^6 - 252a^5b^5c^5*d^5 + 210a^4b^6c^6*d^4 - 120a^3b^7c^7*d^3 + 45a^2b^8c^8*d^2 - 10a*b^9c^9*d + b^{10}c^{10}) / b^{11} / (b*x+a)^{17} - 210 / 11 * d^6 * (a^4*d^4 - 4a^3b*c*d^3 + 6a^2b^2*c^2*d^2 - 4a*b^3*c^3*d + b^4*c^4) / b^11 / (b*x+a)^{11} - 3*d^2 * (a^8*d^8 - 8a^7b*c*d^7 + 28a^6b^2c^2*d^6 - 56a^5b^3c^3*d^5 + 70a^4b^4c^4*d^4 - 56a^3b^5c^5*d^3 + 28a^2b^6c^6*d^2 - 8a*b^7c^7*d + b^8*c^8) / b^{11} / (b*x+a)^{15} + 21*d^5 * (a^5*d^5 - 5a^4b*c*d^4 + 10a^3b^2c^2*d^3 - 10a^2b^3c^3*d^2 + 5a*b^4c^4*d - b^5*c^5) / b^{11} / (b*x+a)^{12} + 12*d^7 * (a^3*d^3 - 3a^2b*c*d^2 + 3a*b^2*c^2*d - b^3*c^3) / b^{11} / (b*x+a)^{10} + 60/7*d^3 * (a^7*d^7 - 7a^6*b*c*d^6 + 21a^5b^2c^2*d^5 - 35a^4b^3c^3*d^4 + 35a^3b^4c^4*d^3 - 21a^2b^5c^5*d^2 + 7a*b^6c^6*d - b^7*c^7) / b^{11} / (b*x+a)^{14} + 5/8*d * (a^9*d^9 - 9a^8b*c*d^8 + 36a^7b^2c^2*d^7 - 84a^6b^3c^3*d^6 + 126a^5b^4c^4*d^5 - 126a^4b^5c^5*d^4 + 84a^3b^6c^6*d^3 - 36a^2b^7c^7*d^2 + 9a*b^8c^8*d - b^9*c^9) / b^{11} / (b*x+a)^{16}$$

maxima [B] time = 2.29, size = 1041, normalized size = 4.89

$$19448 b^{10} d^{10} x^{10} + 8008 b^{10} c^{10} + 5005 a b^9 c^9 d + 3003 a^2 b^8 c^8 d^2 + 1716 a^3 b^7 c^7 d^3 + 924 a^4 b^6 c^6 d^4 + 462 a^5 b^5 c^5 d^5 + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^18,x, algorithm="maxima")

[Out]
$$-1/136136 * (19448*b^{10}*d^{10}*x^{10} + 8008*b^{10}*c^{10} + 5005*a*b^9*c^9*d + 3003*a^2*b^8*c^8*d^2 + 1716*a^3*b^7*c^7*d^3 + 924*a^4*b^6*c^6*d^4 + 462*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 + 84*a^7*b^3*c^3*d^7 + 28*a^8*b^2*c^2*d^8 + 7*a^9*b*c*d^9 + a^{10}*d^{10} + 24310*(7*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 + 24310*(8*b^{10}*c^2*d^8 + 7*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 19448*(84*b^{10}*c^3*d^7 + 28*a*b^9*c^2*d^8 + 7*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 12376*(210*b^{10}*c^4*d^6 + 84*a*b^9*c^3*d^7 + 28*a^2*b^8*c^2*d^8 + 7*a^3*b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 6188*(462*b^{10}*c^5*d^5 + 210*a*b^9*c^4*d^6 + 84*a^2*b^8*c^3*d^7 + 28*a^3*b^7*c^2*d^8 + 7*a^4*b^6*c*d^9 + a^5*b^5*d^{10})*x^5 + 2380*(924*b^{10}*c^6*d^4 + 462*a*b^9*c^5*d^5 + 210*a^2*b^8*c^4*d^6 + 84*a^3*b^7*c^3*d^7 + 28*a^4*b^6*c^2*d^8 + 7*a^5*b^5*c*d^9 + a^6*b^4*d^{10})*x^4 + 680*(1716*b^{10}*c^7*d^3 + 924*a*b^9*c^6*d^4 + 462*a^2*b^8*c^5*d^5 + 210*a^3*b^7*c^4*d^6 + 84*a^4*b^6*c^3*d^7 + 28*a^5*b^5*c^2*d^8 + 7*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + 136*(3003*b^{10}*c^8*d^2 + 1716*a*b^9*c^7*d^3 + 924*a^2*b^8*c^6*d^4 + 462*a^3*b^7*c^5*d^5 + 210*a^4*b^6*c^4*d^6 + 84*a^5*b^5*c^3*d^7 + 28*a^6*b^4*c^2*d^8 + 7*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 + 17*(5005*b^{10}*c^9*d + 3003*a*b^9*c^8*d^2 + 1716*a^2*b^8*c^7*d^3 + 924*a^3*b^7*c^6*d^4 + 462*a^4*b^6*c^5*d^5 + 210*a^5*b^5*c^4*d^6 + 84*a^6*b^4*c^3*d^7 + 28*a^7*b^3*c^2*d^8 + 7*a^8*b^2*c*d^9 + a^9*b*d^{10})*x) / (b^{28}*x^{17} + 17*a*b^{27}*x^{16} + 136*a^2*b^{26}*x^{15} + 680*a^3*b^{25}*x^{14} + 2380*a^4*b^{24}*x^{13} + 6188*a^5*b^{23}*x^{12} + 12376*a^6*b^{22}*x^{11} + 19448*a^7*b^{21}*x^{10} + 24310*a^8*b^{20}*x^9 + 24310*a^9*b^{19}*x^8$$

+ 19448*a¹⁰*b¹⁸*x⁷ + 12376*a¹¹*b¹⁷*x⁶ + 6188*a¹²*b¹⁶*x⁵ + 2380*a¹³*b¹⁵*x⁴ + 680*a¹⁴*b¹⁴*x³ + 136*a¹⁵*b¹³*x² + 17*a¹⁶*b¹²*x + a¹⁷*b¹¹)

mupad [B] time = 0.66, size = 1142, normalized size = 5.36

$$\frac{a^{10} d^{10} + 7 a^9 b c d^9 + 17 a^9 b d^{10} x + 28 a^8 b^2 c^2 d^8 + 119 a^8 b^2 c d^9 x + 136 a^8 b^2 d^{10} x^2 + 84 a^7 b^3 c^3 d^7 + 476 a^7 b^3 c^2 d^8 x + 136 a^7 b^3 c d^9 x^2 + 136 a^7 b^3 d^{10} x^3 + 84 a^6 b^4 c^4 d^6 + 119 a^6 b^4 c^3 d^7 x + 136 a^6 b^4 c^2 d^8 x^2 + 136 a^6 b^4 c d^9 x^3 + 84 a^6 b^4 d^{10} x^4 + 19448 a^5 b^5 d^{10} x^5 + 12376 a^4 b^6 d^{10} x^6 + 19448 a^3 b^7 d^{10} x^7 + 24310 a^2 b^8 d^{10} x^8 + 408408 b^{10} c^8 d^2 x^2 + 1166880 b^{10} c^7 d^3 x^3 + 2199120 b^{10} c^6 d^4 x^4 + 2858856 b^{10} c^5 d^5 x^5 + 2598960 b^{10} c^4 d^6 x^6 + 1633632 b^{10} c^3 d^7 x^7 + 680680 b^{10} c^2 d^8 x^8 + 5005 a^9 b^9 c^9 d + 7 a^9 b^9 c^8 d^2 x + 17 a^9 b^9 c^7 d^3 x^2 + 85085 b^{10} c^9 d x + 125664 a^2 b^8 c^6 d^4 x^2 + 62832 a^3 b^7 c^5 d^5 x^2 + 28560 a^4 b^6 c^4 d^6 x^2 + 11424 a^5 b^5 c^3 d^7 x^2 + 3808 a^6 b^4 c^2 d^8 x^2 + 314160 a^2 b^8 c^5 d^5 x^3 + 142800 a^3 b^7 c^4 d^6 x^3 + 57120 a^4 b^6 c^3 d^7 x^3 + 19040 a^5 b^5 c^2 d^8 x^3 + 499800 a^2 b^8 c^4 d^6 x^4 + 199920 a^3 b^7 c^3 d^7 x^4 + 66640 a^4 b^6 c^2 d^8 x^4 + 519792 a^2 b^8 c^3 d^7 x^5 + 173264 a^3 b^7 c^2 d^8 x^5 + 346528 a^2 b^8 c^2 d^8 x^6 + 51051 a^9 b^9 c^8 d^2 x + 119 a^8 b^2 c^9 d x + 170170 a^9 b^9 c^9 d^2 x + 29172 a^2 b^8 c^7 d^3 x + 15708 a^3 b^7 c^6 d^4 x + 7854 a^4 b^6 c^5 d^5 x + 3570 a^5 b^5 c^4 d^6 x + 1428 a^6 b^4 c^3 d^7 x + 476 a^7 b^3 c^2 d^8 x + 233376 a^9 b^9 c^7 d^3 x^2 + 952 a^7 b^3 c^3 d^9 x^2 + 628320 a^9 b^9 c^6 d^4 x^3 + 4760 a^6 b^4 c^3 d^9 x^3 + 1099560 a^9 b^9 c^5 d^5 x^4 + 16660 a^5 b^5 c^3 d^9 x^4 + 1299480 a^9 b^9 c^4 d^6 x^5 + 43316 a^4 b^6 c^3 d^9 x^5 + 1039584 a^9 b^9 c^3 d^7 x^6 + 86632 a^3 b^7 c^3 d^9 x^6 + 544544 a^9 b^9 c^2 d^8 x^7 + 136136 a^2 b^8 c^3 d^9 x^7 + 136136 a^17 b^11 + 136136 b^28 x^17 + 2314312 a^16 b^12 x + 2314312 a^17 b^11 x^16 + 18514496 a^15 b^13 x^2 + 92572480 a^14 b^14 x^3 + 324003680 a^13 b^15 x^4 + 842409568 a^12 b^16 x^5 + 1684819136 a^11 b^17 x^6 + 2647572928 a^10 b^18 x^7 + 3309466160 a^9 b^19 x^8 + 3309466160 a^8 b^20 x^9 + 2647572928 a^7 b^21 x^10 + 1684819136 a^6 b^22 x^11 + 842409568 a^5 b^23 x^12 + 324003680 a^4 b^24 x^13 + 92572480 a^3 b^25 x^14 + 18514496 a^2 b^26 x^15)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)¹⁰/(a + b*x)¹⁸,x)

[Out] -(a¹⁰*d¹⁰ + 8008*b¹⁰*c¹⁰ + 19448*b¹⁰*d¹⁰*x¹⁰ + 24310*a*b⁹*d¹⁰*x⁹ + 170170*b¹⁰*c*d⁹*x⁹ + 3003*a²*b⁸*c⁸*d² + 1716*a³*b⁷*c⁷*d³ + 924*a⁴*b⁶*c⁶*d⁴ + 462*a⁵*b⁵*c⁵*d⁵ + 210*a⁶*b⁴*c⁴*d⁶ + 84*a⁷*b³*c³*d⁷ + 28*a⁸*b²*c²*d⁸ + 136*a⁸*b²*d¹⁰*x² + 680*a⁷*b³*d¹⁰*x³ + 2380*a⁶*b⁴*d¹⁰*x⁴ + 6188*a⁵*b⁵*d¹⁰*x⁵ + 12376*a⁴*b⁶*d¹⁰*x⁶ + 19448*a³*b⁷*d¹⁰*x⁷ + 24310*a²*b⁸*d¹⁰*x⁸ + 408408*b¹⁰*c⁸*d²*x² + 1166880*b¹⁰*c⁷*d³*x³ + 2199120*b¹⁰*c⁶*d⁴*x⁴ + 2858856*b¹⁰*c⁵*d⁵*x⁵ + 2598960*b¹⁰*c⁴*d⁶*x⁶ + 1633632*b¹⁰*c³*d⁷*x⁷ + 680680*b¹⁰*c²*d⁸*x⁸ + 5005*a*b⁹*c⁹*d + 7*a⁹*b*c*d⁹ + 17*a⁹*b*d¹⁰*x + 85085*b¹⁰*c⁹*d*x + 125664*a²*b⁸*c⁶*d⁴*x² + 62832*a³*b⁷*c⁵*d⁵*x² + 28560*a⁴*b⁶*c⁴*d⁶*x² + 11424*a⁵*b⁵*c³*d⁷*x² + 3808*a⁶*b⁴*c²*d⁸*x² + 314160*a²*b⁸*c⁵*d⁵*x³ + 142800*a³*b⁷*c⁴*d⁶*x³ + 57120*a⁴*b⁶*c³*d⁷*x³ + 19040*a⁵*b⁵*c²*d⁸*x³ + 499800*a²*b⁸*c⁴*d⁶*x⁴ + 199920*a³*b⁷*c³*d⁷*x⁴ + 66640*a⁴*b⁶*c²*d⁸*x⁴ + 519792*a²*b⁸*c³*d⁷*x⁵ + 173264*a³*b⁷*c²*d⁸*x⁵ + 346528*a²*b⁸*c²*d⁸*x⁶ + 51051*a*b⁹*c⁸*d²*x + 119*a⁸*b²*c*d⁹*x + 170170*a*b⁹*c*d⁹*x⁸ + 29172*a²*b⁸*c⁷*d³*x + 15708*a³*b⁷*c⁶*d⁴*x + 7854*a⁴*b⁶*c⁵*d⁵*x + 3570*a⁵*b⁵*c⁴*d⁶*x + 1428*a⁶*b⁴*c³*d⁷*x + 476*a⁷*b³*c²*d⁸*x + 233376*a*b⁹*c⁷*d³*x² + 952*a⁷*b³*c*d⁹*x² + 628320*a*b⁹*c⁶*d⁴*x³ + 4760*a⁶*b⁴*c³*d⁹*x³ + 1099560*a*b⁹*c⁵*d⁵*x⁴ + 16660*a⁵*b⁵*c*d⁹*x⁴ + 1299480*a*b⁹*c⁴*d⁶*x⁵ + 43316*a⁴*b⁶*c*d⁹*x⁵ + 1039584*a*b⁹*c³*d⁷*x⁶ + 86632*a³*b⁷*c*d⁹*x⁶ + 544544*a*b⁹*c²*d⁸*x⁷ + 136136*a²*b⁸*c*d⁹*x⁷ + 136136*a¹⁷*b¹¹ + 136136*b²⁸*x¹⁷ + 2314312*a¹⁶*b¹²*x + 2314312*a*b¹⁷*x¹⁶ + 18514496*a¹⁵*b¹³*x² + 92572480*a¹⁴*b¹⁴*x³ + 324003680*a¹³*b¹⁵*x⁴ + 842409568*a¹²*b¹⁶*x⁵ + 1684819136*a¹¹*b¹⁷*x⁶ + 2647572928*a¹⁰*b¹⁸*x⁷ + 3309466160*a⁹*b¹⁹*x⁸ + 3309466160*a⁸*b²⁰*x⁹ + 2647572928*a⁷*b²¹*x¹⁰ + 1684819136*a⁶*b²²*x¹¹ + 842409568*a⁵*b²³*x¹² + 324003680*a⁴*b²⁴*x¹³ + 92572480*a³*b²⁵*x¹⁴ + 18514496*a²*b²⁶*x¹⁵)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**10/(b*x+a)**18,x)
```

```
[Out] Timed out
```


$$3.1330 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{19}} dx$$

Optimal. Leaf size=244

$$\frac{d^7(c+dx)^{11}}{350064(a+bx)^{11}(bc-ad)^8} - \frac{d^6(c+dx)^{11}}{31824(a+bx)^{12}(bc-ad)^7} + \frac{d^5(c+dx)^{11}}{5304(a+bx)^{13}(bc-ad)^6} - \frac{d^4(c+dx)^{11}}{1224(a+bx)^{14}(bc-ad)^5} +$$

[Out] $-1/18*(d*x+c)^{11}/(-a*d+b*c)/(b*x+a)^{18}+7/306*d*(d*x+c)^{11}/(-a*d+b*c)^2/(b*x+a)^{17}-7/816*d^2*(d*x+c)^{11}/(-a*d+b*c)^3/(b*x+a)^{16}+7/2448*d^3*(d*x+c)^{11}/(-a*d+b*c)^4/(b*x+a)^{15}-1/1224*d^4*(d*x+c)^{11}/(-a*d+b*c)^5/(b*x+a)^{14}+1/5304*d^5*(d*x+c)^{11}/(-a*d+b*c)^6/(b*x+a)^{13}-1/31824*d^6*(d*x+c)^{11}/(-a*d+b*c)^7/(b*x+a)^{12}+1/350064*d^7*(d*x+c)^{11}/(-a*d+b*c)^8/(b*x+a)^{11}$

Rubi [A] time = 0.10, antiderivative size = 244, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{d^7(c+dx)^{11}}{350064(a+bx)^{11}(bc-ad)^8} - \frac{d^6(c+dx)^{11}}{31824(a+bx)^{12}(bc-ad)^7} + \frac{d^5(c+dx)^{11}}{5304(a+bx)^{13}(bc-ad)^6} - \frac{d^4(c+dx)^{11}}{1224(a+bx)^{14}(bc-ad)^5} +$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^19, x]

[Out] $-(c+d*x)^{11}/(18*(b*c-a*d)*(a+b*x)^{18})+(7*d*(c+d*x)^{11})/(306*(b*c-a*d)^2*(a+b*x)^{17})-(7*d^2*(c+d*x)^{11})/(816*(b*c-a*d)^3*(a+b*x)^{16})+(7*d^3*(c+d*x)^{11})/(2448*(b*c-a*d)^4*(a+b*x)^{15})-(d^4*(c+d*x)^{11})/(1224*(b*c-a*d)^5*(a+b*x)^{14})+(d^5*(c+d*x)^{11})/(5304*(b*c-a*d)^6*(a+b*x)^{13})-(d^6*(c+d*x)^{11})/(31824*(b*c-a*d)^7*(a+b*x)^{12})+(d^7*(c+d*x)^{11})/(350064*(b*c-a*d)^8*(a+b*x)^{11})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1]) &&

(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
 \int \frac{(c+dx)^{10}}{(a+bx)^{19}} dx &= -\frac{(c+dx)^{11}}{18(bc-ad)(a+bx)^{18}} - \frac{(7d) \int \frac{(c+dx)^{10}}{(a+bx)^{18}} dx}{18(bc-ad)} \\
 &= -\frac{(c+dx)^{11}}{18(bc-ad)(a+bx)^{18}} + \frac{7d(c+dx)^{11}}{306(bc-ad)^2(a+bx)^{17}} + \frac{(7d^2) \int \frac{(c+dx)^{10}}{(a+bx)^{17}} dx}{51(bc-ad)^2} \\
 &= -\frac{(c+dx)^{11}}{18(bc-ad)(a+bx)^{18}} + \frac{7d(c+dx)^{11}}{306(bc-ad)^2(a+bx)^{17}} - \frac{7d^2(c+dx)^{11}}{816(bc-ad)^3(a+bx)^{16}} - \frac{(35d^3) \int \frac{(c+dx)^{10}}{(a+bx)^{16}} dx}{816(bc-ad)^3} \\
 &= -\frac{(c+dx)^{11}}{18(bc-ad)(a+bx)^{18}} + \frac{7d(c+dx)^{11}}{306(bc-ad)^2(a+bx)^{17}} - \frac{7d^2(c+dx)^{11}}{816(bc-ad)^3(a+bx)^{16}} + \frac{7d^3(c+dx)^{11}}{2448(bc-ad)^4} \\
 &= -\frac{(c+dx)^{11}}{18(bc-ad)(a+bx)^{18}} + \frac{7d(c+dx)^{11}}{306(bc-ad)^2(a+bx)^{17}} - \frac{7d^2(c+dx)^{11}}{816(bc-ad)^3(a+bx)^{16}} + \frac{7d^3(c+dx)^{11}}{2448(bc-ad)^4} \\
 &= -\frac{(c+dx)^{11}}{18(bc-ad)(a+bx)^{18}} + \frac{7d(c+dx)^{11}}{306(bc-ad)^2(a+bx)^{17}} - \frac{7d^2(c+dx)^{11}}{816(bc-ad)^3(a+bx)^{16}} + \frac{7d^3(c+dx)^{11}}{2448(bc-ad)^4} \\
 &= -\frac{(c+dx)^{11}}{18(bc-ad)(a+bx)^{18}} + \frac{7d(c+dx)^{11}}{306(bc-ad)^2(a+bx)^{17}} - \frac{7d^2(c+dx)^{11}}{816(bc-ad)^3(a+bx)^{16}} + \frac{7d^3(c+dx)^{11}}{2448(bc-ad)^4} \\
 &= -\frac{(c+dx)^{11}}{18(bc-ad)(a+bx)^{18}} + \frac{7d(c+dx)^{11}}{306(bc-ad)^2(a+bx)^{17}} - \frac{7d^2(c+dx)^{11}}{816(bc-ad)^3(a+bx)^{16}} + \frac{7d^3(c+dx)^{11}}{2448(bc-ad)^4}
 \end{aligned}$$

Mathematica [B] time = 0.28, size = 694, normalized size = 2.84

$$\frac{a^{10}d^{10} + 2a^9bd^9(4c + 9dx) + 9a^8b^2d^8(4c^2 + 16cdx + 17d^2x^2) + 24a^7b^3d^7(5c^3 + 27c^2dx + 51cd^2x^2 + 34d^3x^3) + \dots}{\dots}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^19,x]

[Out] -1/350064*(a^10*d^10 + 2*a^9*b*d^9*(4*c + 9*d*x) + 9*a^8*b^2*d^8*(4*c^2 + 17*d^2*x^2) + 24*a^7*b^3*d^7*(5*c^3 + 27*c^2*d*x + 51*c*d^2*x^2 + 34*d^3*x^3) + 6*a^6*b^4*d^6*(55*c^4 + 360*c^3*d*x + 918*c^2*d^2*x^2 + 1088*c*d^3*x^3 + 510*d^4*x^4) + 36*a^5*b^5*d^5*(22*c^5 + 165*c^4*d*x + 510*c^3*d^2*x^2 + 1080*c^2*d^3*x^3 + 540*c*d^4*x^4 + 108*d^5*x^5) + 2*a^4*b^6*d^4*(5*c^6 + 36*c^5*d*x + 153*c^4*d^2*x^2 + 270*c^3*d^3*x^3 + 210*c^2*d^4*x^4 + 84*c*d^5*x^5 + 10*d^6*x^6) + a^3*b^7*d^3*(c^7 + 7*c^6*d*x + 28*c^5*d^2*x^2 + 42*c^4*d^3*x^3 + 35*c^3*d^4*x^4 + 14*c^2*d^5*x^5 + 3*c*d^6*x^6 + d^7*x^7) + a^2*b^8*d^2*(c^8 + 8*c^7*d*x + 28*c^6*d^2*x^2 + 56*c^5*d^3*x^3 + 70*c^4*d^4*x^4 + 56*c^3*d^5*x^5 + 28*c^2*d^6*x^6 + 8*c*d^7*x^7 + d^8*x^8) + a*b^9*d*(c^9 + 9*c^8*d*x + 36*c^7*d^2*x^2 + 81*c^6*d^3*x^3 + 126*c^5*d^4*x^4 + 126*c^4*d^5*x^5 + 81*c^3*d^6*x^6 + 36*c^2*d^7*x^7 + 9*c*d^8*x^8 + d^9*x^9) + b^10*d^0*(c^10 + 10*c^9*d*x + 45*c^8*d^2*x^2 + 120*c^7*d^3*x^3 + 210*c^6*d^4*x^4 + 252*c^5*d^5*x^5 + 210*c^4*d^6*x^6 + 120*c^3*d^7*x^7 + 45*c^2*d^8*x^8 + 10*c*d^9*x^9 + d^10*x^10)

$$d^2x^2 + 816c^2d^3x^3 + 680cd^4x^4 + 238d^5x^5) + 6a^4b^6d^4(286c^6 + 2376c^5dx + 8415c^4d^2x^2 + 16320c^3d^3x^3 + 18360c^2d^4x^4 + 11424cd^5x^5 + 3094d^6x^6) + 24a^3b^7d^3(143c^7 + 1287c^6dx + 5049c^5d^2x^2 + 11220c^4d^3x^3 + 15300c^3d^4x^4 + 12852c^2d^5x^5 + 6188cd^6x^6 + 1326d^7x^7) + 9a^2b^8d^2(715c^8 + 6864c^7dx + 29172c^6d^2x^2 + 71808c^5d^3x^3 + 112200c^4d^4x^4 + 114240c^3d^5x^5 + 74256c^2d^6x^6 + 28288cd^7x^7 + 4862d^8x^8) + 2ab^9d(5720c^9 + 57915c^8dx + 262548c^7d^2x^2 + 700128c^6d^3x^3 + 1211760c^5d^4x^4 + 1413720c^4d^5x^5 + 1113840c^3d^6x^6 + 572832c^2d^7x^7 + 175032cd^8x^8 + 24310d^9x^9) + b^{10}(19448c^{10} + 205920c^9dx + 984555c^8d^2x^2 + 2800512c^7d^3x^3 + 5250960c^6d^4x^4 + 6785856c^5d^5x^5 + 6126120c^4d^6x^6 + 3818880c^3d^7x^7 + 1575288c^2d^8x^8 + 388960cd^9x^9 + 43758d^{10}x^{10})/(b^{11}(a + bx)^{18})$$

fricas [B] time = 0.44, size = 1052, normalized size = 4.31

$$\frac{43758 b^{10} d^{10} x^{10} + 19448 b^{10} c^{10} + 11440 a b^9 c^9 d + 6435 a^2 b^8 c^8 d^2 + 3432 a^3 b^7 c^7 d^3 + 1716 a^4 b^6 c^6 d^4 + 792 a^5 b^5 c^5 d^5}{(b^{11}(a + bx)^{18})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((dx+c)^10/(b*x+a)^19,x, algorithm="fricas")

[Out]
$$\frac{-1/350064*(43758*b^{10}*d^{10}*x^{10} + 19448*b^{10}*c^{10} + 11440*a*b^9*c^9*d + 6435*a^2*b^8*c^8*d^2 + 3432*a^3*b^7*c^7*d^3 + 1716*a^4*b^6*c^6*d^4 + 792*a^5*b^5*c^5*d^5 + 330*a^6*b^4*c^4*d^6 + 120*a^7*b^3*c^3*d^7 + 36*a^8*b^2*c^2*d^8 + 8*a^9*b*c*d^9 + a^{10}*d^{10} + 48620*(8*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 + 43758*(36*b^{10}*c^2*d^8 + 8*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 31824*(120*b^{10}*c^3*d^7 + 36*a*b^9*c^2*d^8 + 8*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 18564*(330*b^{10}*c^4*d^6 + 120*a*b^9*c^3*d^7 + 36*a^2*b^8*c^2*d^8 + 8*a^3*b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 8568*(792*b^{10}*c^5*d^5 + 330*a*b^9*c^4*d^6 + 120*a^2*b^8*c^3*d^7 + 36*a^3*b^7*c^2*d^8 + 8*a^4*b^6*c*d^9 + a^5*b^5*d^{10})*x^5 + 3060*(1716*b^{10}*c^6*d^4 + 792*a*b^9*c^5*d^5 + 330*a^2*b^8*c^4*d^6 + 120*a^3*b^7*c^3*d^7 + 36*a^4*b^6*c^2*d^8 + 8*a^5*b^5*c*d^9 + a^6*b^4*d^{10})*x^4 + 816*(3432*b^{10}*c^7*d^3 + 1716*a*b^9*c^6*d^4 + 792*a^2*b^8*c^5*d^5 + 330*a^3*b^7*c^4*d^6 + 120*a^4*b^6*c^3*d^7 + 36*a^5*b^5*c^2*d^8 + 8*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + 153*(6435*b^{10}*c^8*d^2 + 3432*a*b^9*c^7*d^3 + 1716*a^2*b^8*c^6*d^4 + 792*a^3*b^7*c^5*d^5 + 330*a^4*b^6*c^4*d^6 + 120*a^5*b^5*c^3*d^7 + 36*a^6*b^4*c^2*d^8 + 8*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 + 18*(11440*b^{10}*c^9*d + 6435*a*b^9*c^8*d^2 + 3432*a^2*b^8*c^7*d^3 + 1716*a^3*b^7*c^6*d^4 + 792*a^4*b^6*c^5*d^5 + 330*a^5*b^5*c^4*d^6 + 120*a^6*b^4*c^3*d^7 + 36*a^7*b^3*c^2*d^8 + 8*a^8*b^2*c*d^9 + a^9*b*d^{10})*x)/(b^{29}*x^{18} + 18*a*b^{28}*x^{17} + 153*a^2*b^{27}*x^{16} + 816*a^3*b^{26}*x^{15} + 3060*a^4*b^{25}*x^{14} + 8568*a^5*b^{24}*x^{13} + 18564*a^6*b^{23}*x^{12} + 31824*a^7*b^{22}*x^{11} + 43758*a^8*b^{21}*x^{10} + 48620*a^9*b^{20}*x^9 + 43758*a^{10}*b^{19}*x^8 + 31824*a^{11}*b^{18}*x^7 + 18564*a^{12}*b^{17}*x^6 + 816*a^{13}*b^{16}*x^5 + 153*a^{14}*b^{15}*x^4 + 18*a^{15}*b^{14}*x^3 + 18564*a^{16}*b^{13}*x^2 + 153*a^{17}*b^{12}*x + 18564*a^{18}*b^{11})$$

$$\begin{aligned} & ^{17}x^6 + 8568a^{13}b^{16}x^5 + 3060a^{14}b^{15}x^4 + 816a^{15}b^{14}x^3 + 153 \\ & a^{16}b^{13}x^2 + 18a^{17}b^{12}x + a^{18}b^{11}) \end{aligned}$$

giac [B] time = 1.40, size = 961, normalized size = 3.94

$$\frac{43758 b^{10} d^{10} x^{10} + 388960 b^{10} c d^9 x^9 + 48620 a b^9 d^{10} x^9 + 1575288 b^{10} c^2 d^8 x^8 + 350064 a b^9 c d^9 x^8 + 43758 a^2 b^8 d^{10} x^8 + \dots}{(b x + a)^{19}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^19,x, algorithm="giac")

[Out]
$$\begin{aligned} & -1/350064*(43758*b^{10}*d^{10}*x^{10} + 388960*b^{10}*c*d^9*x^9 + 48620*a*b^9*d^{10}* \\ & x^9 + 1575288*b^{10}*c^2*d^8*x^8 + 350064*a*b^9*c*d^9*x^8 + 43758*a^2*b^8*d^{10}* \\ & 0*x^8 + 3818880*b^{10}*c^3*d^7*x^7 + 1145664*a*b^9*c^2*d^8*x^7 + 254592*a^2*b^8*d^{10}* \\ & ^8*c*d^9*x^7 + 31824*a^3*b^7*d^{10}*x^7 + 6126120*b^{10}*c^4*d^6*x^6 + 2227680* \\ & a*b^9*c^3*d^7*x^6 + 668304*a^2*b^8*c^2*d^8*x^6 + 148512*a^3*b^7*c*d^9*x^6 + \\ & 18564*a^4*b^6*d^{10}*x^6 + 6785856*b^{10}*c^5*d^5*x^5 + 2827440*a*b^9*c^4*d^6* \\ & x^5 + 1028160*a^2*b^8*c^3*d^7*x^5 + 308448*a^3*b^7*c^2*d^8*x^5 + 68544*a^4* \\ & b^6*c*d^9*x^5 + 8568*a^5*b^5*d^{10}*x^5 + 5250960*b^{10}*c^6*d^4*x^4 + 2423520* \\ & a*b^9*c^5*d^5*x^4 + 1009800*a^2*b^8*c^4*d^6*x^4 + 367200*a^3*b^7*c^3*d^7*x^4 \\ & 4 + 110160*a^4*b^6*c^2*d^8*x^4 + 24480*a^5*b^5*c*d^9*x^4 + 3060*a^6*b^4*d^{10}* \\ & 0*x^4 + 2800512*b^{10}*c^7*d^3*x^3 + 1400256*a*b^9*c^6*d^4*x^3 + 646272*a^2*b^8* \\ & ^8*c^5*d^5*x^3 + 269280*a^3*b^7*c^4*d^6*x^3 + 97920*a^4*b^6*c^3*d^7*x^3 + 2 \\ & 9376*a^5*b^5*c^2*d^8*x^3 + 6528*a^6*b^4*c*d^9*x^3 + 816*a^7*b^3*d^{10}*x^3 + \\ & 984555*b^{10}*c^8*d^2*x^2 + 525096*a*b^9*c^7*d^3*x^2 + 262548*a^2*b^8*c^6*d^4* \\ & *x^2 + 121176*a^3*b^7*c^5*d^5*x^2 + 50490*a^4*b^6*c^4*d^6*x^2 + 18360*a^5*b^5* \\ & ^5*c^3*d^7*x^2 + 5508*a^6*b^4*c^2*d^8*x^2 + 1224*a^7*b^3*c*d^9*x^2 + 153*a^8* \\ & b^2*d^{10}*x^2 + 205920*b^{10}*c^9*d*x + 115830*a*b^9*c^8*d^2*x + 61776*a^2*b^8* \\ & ^8*c^7*d^3*x + 30888*a^3*b^7*c^6*d^4*x + 14256*a^4*b^6*c^5*d^5*x + 5940*a^5* \\ & *b^5*c^4*d^6*x + 2160*a^6*b^4*c^3*d^7*x + 648*a^7*b^3*c^2*d^8*x + 144*a^8*b^2* \\ & ^2*c*d^9*x + 18*a^9*b*d^{10}*x + 19448*b^{10}*c^{10} + 11440*a*b^9*c^9*d + 6435*a^2* \\ & ^2*b^8*c^8*d^2 + 3432*a^3*b^7*c^7*d^3 + 1716*a^4*b^6*c^6*d^4 + 792*a^5*b^5* \\ & c^5*d^5 + 330*a^6*b^4*c^4*d^6 + 120*a^7*b^3*c^3*d^7 + 36*a^8*b^2*c^2*d^8 + \\ & 8*a^9*b*c*d^9 + a^{10}*d^{10})/((b*x + a)^{18}*b^{11}) \end{aligned}$$

maple [B] time = 0.01, size = 867, normalized size = 3.55

$$\frac{d^{10}}{8(bx+a)^8 b^{11}} + \frac{10(ad-bc)d^9}{9(bx+a)^9 b^{11}} - \frac{9(a^2d^2-2abcd+b^2c^2)d^8}{2(bx+a)^{10} b^{11}} + \frac{120(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^7}{11(bx+a)^{11} b^{11}} - \frac{35(a^4d^4-4a^3bcd^3+6a^2b^2c^2d^2-4ab^3c^3d-b^4c^4)d^6}{11(bx+a)^{12} b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^19,x)

```
[Out] -1/8*d^10/b^11/(b*x+a)^8+252/13*d^5*(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)/b^11/(b*x+a)^13+10/9*d^9*(a*d-b*c)/b^11/(b*x+a)^9+10/17*d*(a^9*d^9-9*a^8*b*c*d^8+36*a^7*b^2*c^2*d^7-84*a^6*b^3*c^3*d^6+126*a^5*b^4*c^4*d^5-126*a^4*b^5*c^5*d^4+84*a^3*b^6*c^6*d^3-36*a^2*b^7*c^7*d^2+9*a*b^8*c^8*d-b^9*c^9)/b^11/(b*x+a)^17+120/11*d^7*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^11/(b*x+a)^11+8*d^3*(a^7*d^7-7*a^6*b*c*d^6+21*a^5*b^2*c^2*d^5-35*a^4*b^3*c^3*d^4+35*a^3*b^4*c^4*d^3-21*a^2*b^5*c^5*d^2+7*a*b^6*c^6*d-b^7*c^7)/b^11/(b*x+a)^15-35/2*d^6*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/b^11/(b*x+a)^12-1/18*(a^10*d^10-10*a^9*b*c*d^9+45*a^8*b^2*c^2*d^8-120*a^7*b^3*c^3*d^7+210*a^6*b^4*c^4*d^6-252*a^5*b^5*c^5*d^5+210*a^4*b^6*c^6*d^4-120*a^3*b^7*c^7*d^3+45*a^2*b^8*c^8*d^2-10*a*b^9*c^9*d+b^10*c^10)/b^11/(b*x+a)^18-9/2*d^8*(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^11/(b*x+a)^10-15*d^4*(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^11/(b*x+a)^14-45/16*d^2*(a^8*d^8-8*a^7*b*c*d^7+28*a^6*b^2*c^2*d^6-56*a^5*b^3*c^3*d^5+70*a^4*b^4*c^4*d^4-56*a^3*b^5*c^5*d^3+28*a^2*b^6*c^6*d^2-8*a*b^7*c^7*d+b^8*c^8)/b^11/(b*x+a)^16
```

maxima [B] time = 2.54, size = 1052, normalized size = 4.31

$$43758 b^{10} d^{10} x^{10} + 19448 b^{10} c^{10} + 11440 a b^9 c^9 d + 6435 a^2 b^8 c^8 d^2 + 3432 a^3 b^7 c^7 d^3 + 1716 a^4 b^6 c^6 d^4 + 792 a^5 b^5 c^5 d^5$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^10/(b*x+a)^19,x, algorithm="maxima")
```

```
[Out] -1/350064*(43758*b^10*d^10*x^10 + 19448*b^10*c^10 + 11440*a*b^9*c^9*d + 6435*a^2*b^8*c^8*d^2 + 3432*a^3*b^7*c^7*d^3 + 1716*a^4*b^6*c^6*d^4 + 792*a^5*b^5*c^5*d^5 + 330*a^6*b^4*c^4*d^6 + 120*a^7*b^3*c^3*d^7 + 36*a^8*b^2*c^2*d^8 + 8*a^9*b*c*d^9 + a^10*d^10 + 48620*(8*b^10*c*d^9 + a*b^9*d^10)*x^9 + 43758*(36*b^10*c^2*d^8 + 8*a*b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 31824*(120*b^10*c^3*d^7 + 36*a*b^9*c^2*d^8 + 8*a^2*b^8*c*d^9 + a^3*b^7*d^10)*x^7 + 18564*(330*b^10*c^4*d^6 + 120*a*b^9*c^3*d^7 + 36*a^2*b^8*c^2*d^8 + 8*a^3*b^7*c*d^9 + a^4*b^6*d^10)*x^6 + 8568*(792*b^10*c^5*d^5 + 330*a*b^9*c^4*d^6 + 120*a^2*b^8*c^3*d^7 + 36*a^3*b^7*c^2*d^8 + 8*a^4*b^6*c*d^9 + a^5*b^5*d^10)*x^5 + 3060*(1716*b^10*c^6*d^4 + 792*a*b^9*c^5*d^5 + 330*a^2*b^8*c^4*d^6 + 120*a^3*b^7*c^3*d^7 + 36*a^4*b^6*c^2*d^8 + 8*a^5*b^5*c*d^9 + a^6*b^4*d^10)*x^4 + 816*(3432*b^10*c^7*d^3 + 1716*a*b^9*c^6*d^4 + 792*a^2*b^8*c^5*d^5 + 330*a^3*b^7*c^4*d^6 + 120*a^4*b^6*c^3*d^7 + 36*a^5*b^5*c^2*d^8 + 8*a^6*b^4*c*d^9 + a^7*b^3*d^10)*x^3 + 153*(6435*b^10*c^8*d^2 + 3432*a*b^9*c^7*d^3 + 1716*a^2*b^8*c^6*d^4 + 792*a^3*b^7*c^5*d^5 + 330*a^4*b^6*c^4*d^6 + 120*a^5*b^5*c^3*d^7 + 36*a^6*b^4*c^2*d^8 + 8*a^7*b^3*c*d^9 + a^8*b^2*d^10)*x^2 + 18*(11440*b^10*c^9*d + 6435*a*b^9*c^8*d^2 + 3432*a^2*b^8*c^7*d^3 + 1716*a^3*b^7*c^6*d^4 + 792*a^4*b^6*c^5*d^5 + 330*a^5*b^5*c^4*d^6 + 120*a^6*b^4*c^3*d^7 + 36*a^7*b^3*c^2*d^8 + 8*a^8*b^2*c*d^9 + a^9*b*d^10)*x + 1/18*(a^10*d^10 - 10*a^9*b*c*d^9 + 45*a^8*b^2*c^2*d^8 - 120*a^7*b^3*c^3*d^7 + 210*a^6*b^4*c^4*d^6 - 252*a^5*b^5*c^5*d^5 + 210*a^4*b^6*c^6*d^4 - 120*a^3*b^7*c^7*d^3 + 45*a^2*b^8*c^8*d^2 - 10*a*b^9*c^9*d + b^10*c^10)/b^18 - 9/2*d^8*(a^2*d^2 - 2*a*b*c*d + b^2*c^2)/b^11
```

$$\frac{3c^2d^8 + 8a^8b^2cd^9 + a^9b^2d^{10}}{(b^{29}x^{18} + 18a^8b^{28}x^{17} + 153a^2b^{27}x^{16} + 816a^3b^{26}x^{15} + 3060a^4b^{25}x^{14} + 8568a^5b^{24}x^{13} + 18564a^6b^{23}x^{12} + 31824a^7b^{22}x^{11} + 43758a^8b^{21}x^{10} + 48620a^9b^{20}x^9 + 43758a^{10}b^{19}x^8 + 31824a^{11}b^{18}x^7 + 18564a^{12}b^{17}x^6 + 8568a^{13}b^{16}x^5 + 3060a^{14}b^{15}x^4 + 816a^{15}b^{14}x^3 + 153a^{16}b^{13}x^2 + 18a^{17}b^{12}x + a^{18}b^{11})}x$$

mupad [B] time = 12.02, size = 1153, normalized size = 4.73

$$a^{10}d^{10} + 8a^9bcd^9 + 18a^9bd^{10}x + 36a^8b^2c^2d^8 + 144a^8b^2cd^9x + 153a^8b^2d^{10}x^2 + 120a^7b^3c^3d^7 + 648a^7b^3c^3d^7x + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^19,x)

[Out]
$$\frac{-(a^{10}d^{10} + 19448b^{10}c^{10} + 43758b^{10}d^{10}x^{10} + 48620a^8b^9d^{10}x^9 + 388960b^{10}c^9d^9x^9 + 6435a^2b^8c^8d^2 + 3432a^3b^7c^7d^3 + 1716a^4b^6c^6d^4 + 792a^5b^5c^5d^5 + 330a^6b^4c^4d^6 + 120a^7b^3c^3d^7 + 36a^8b^2c^2d^8 + 153a^8b^2d^{10}x^2 + 816a^7b^3d^{10}x^3 + 3060a^6b^4d^{10}x^4 + 8568a^5b^5d^{10}x^5 + 18564a^4b^6d^{10}x^6 + 31824a^3b^7d^{10}x^7 + 43758a^2b^8d^{10}x^8 + 984555b^{10}c^8d^2x^2 + 2800512b^{10}c^7d^3x^3 + 5250960b^{10}c^6d^4x^4 + 6785856b^{10}c^5d^5x^5 + 6126120b^{10}c^4d^6x^6 + 3818880b^{10}c^3d^7x^7 + 1575288b^{10}c^2d^8x^8 + 11440a^8b^9c^9d + 8a^9b^9c^9d^9 + 18a^9b^9d^{10}x + 205920b^{10}c^9d^9x + 262548a^2b^8c^6d^4x^2 + 121176a^3b^7c^5d^5x^2 + 50490a^4b^6c^4d^6x^2 + 18360a^5b^5c^3d^7x^2 + 5508a^6b^4c^2d^8x^2 + 646272a^2b^8c^5d^5x^3 + 269280a^3b^7c^4d^6x^3 + 97920a^4b^6c^3d^7x^3 + 29376a^5b^5c^2d^8x^3 + 1009800a^2b^8c^4d^6x^4 + 367200a^3b^7c^3d^7x^4 + 110160a^4b^6c^2d^8x^4 + 1028160a^2b^8c^3d^7x^5 + 308448a^3b^7c^2d^8x^5 + 668304a^2b^8c^2d^8x^6 + 115830a^8b^9c^8d^2x + 144a^8b^2cd^9x + 350064a^8b^9cd^9x^8 + 61776a^2b^8c^7d^3x + 30888a^3b^7c^6d^4x + 14256a^4b^6c^5d^5x + 5940a^5b^5c^4d^6x + 2160a^6b^4c^3d^7x + 648a^7b^3c^2d^8x + 525096a^8b^9c^7d^3x^2 + 1224a^7b^3cd^9x^2 + 1400256a^8b^9c^6d^4x^3 + 6528a^6b^4cd^9x^3 + 2423520a^8b^9c^5d^5x^4 + 24480a^5b^5cd^9x^4 + 2827440a^8b^9c^4d^6x^5 + 68544a^4b^6cd^9x^5 + 2227680a^8b^9c^3d^7x^6 + 148512a^3b^7cd^9x^6 + 1145664a^8b^9c^2d^8x^7 + 254592a^2b^8cd^9x^7)/(350064a^{18}b^{11} + 350064b^{29}x^{18} + 6301152a^{17}b^{12}x + 6301152a^8b^{28}x^{17} + 53559792a^{16}b^{13}x^2 + 285652224a^{15}b^{14}x^3 + 1071195840a^{14}b^{15}x^4 + 2999348352a^{13}b^{16}x^5 + 6498588096a^{12}b^{17}x^6 + 11140436736a^{11}b^{18}x^7 + 15318100512a^{10}b^{19}x^8 + 17020111680a^9b^{20}x^9 + 15318100512a^8b^{21}x^{10} + 11140436736a^7b^{22}x^{11} + 6498588096a^6b^{23}x^{12} + 2999348352a^5b^{24}x^{13} + 1071195840a^4b^{25}x^{14} + 285652224a^3b^{26}x^{15} + 53559792a^2b^{27}x^{16})$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**19,x)

[Out] Timed out

$$3.1331 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{20}} dx$$

Optimal. Leaf size=273

$$\frac{d^9(bc-ad)}{b^{11}(a+bx)^{10}} - \frac{45d^8(bc-ad)^2}{11b^{11}(a+bx)^{11}} - \frac{10d^7(bc-ad)^3}{b^{11}(a+bx)^{12}} - \frac{210d^6(bc-ad)^4}{13b^{11}(a+bx)^{13}} - \frac{18d^5(bc-ad)^5}{b^{11}(a+bx)^{14}} - \frac{14d^4(bc-ad)^6}{b^{11}(a+bx)^{15}} - \frac{15d^3(bc-ad)^7}{2b^{11}(a+bx)^{16}} - \frac{10d^2(bc-ad)^8}{b^{11}(a+bx)^{17}} - \frac{5d(bc-ad)^9}{b^{11}(a+bx)^{18}} - \frac{d^9(bc-ad)^{10}}{b^{11}(a+bx)^{19}}$$

[Out] $-1/19*(-a*d+b*c)^{10}/b^{11}/(b*x+a)^{19}-5/9*d*(-a*d+b*c)^9/b^{11}/(b*x+a)^{18}-45/17*d^2*(-a*d+b*c)^8/b^{11}/(b*x+a)^{17}-15/2*d^3*(-a*d+b*c)^7/b^{11}/(b*x+a)^{16}-14*d^4*(-a*d+b*c)^6/b^{11}/(b*x+a)^{15}-18*d^5*(-a*d+b*c)^5/b^{11}/(b*x+a)^{14}-210/13*d^6*(-a*d+b*c)^4/b^{11}/(b*x+a)^{13}-10*d^7*(-a*d+b*c)^3/b^{11}/(b*x+a)^{12}-45/11*d^8*(-a*d+b*c)^2/b^{11}/(b*x+a)^{11}-d^9*(-a*d+b*c)/b^{11}/(b*x+a)^{10}-1/9*d^{10}/b^{11}/(b*x+a)^9$

Rubi [A] time = 0.28, antiderivative size = 273, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{d^9(bc-ad)}{b^{11}(a+bx)^{10}} - \frac{45d^8(bc-ad)^2}{11b^{11}(a+bx)^{11}} - \frac{10d^7(bc-ad)^3}{b^{11}(a+bx)^{12}} - \frac{210d^6(bc-ad)^4}{13b^{11}(a+bx)^{13}} - \frac{18d^5(bc-ad)^5}{b^{11}(a+bx)^{14}} - \frac{14d^4(bc-ad)^6}{b^{11}(a+bx)^{15}} - \frac{15d^3(bc-ad)^7}{2b^{11}(a+bx)^{16}} - \frac{10d^2(bc-ad)^8}{b^{11}(a+bx)^{17}} - \frac{5d(bc-ad)^9}{b^{11}(a+bx)^{18}} - \frac{d^9(bc-ad)^{10}}{b^{11}(a+bx)^{19}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^20,x]

[Out] $-(b*c - a*d)^{10}/(19*b^{11}*(a + b*x)^{19}) - (5*d*(b*c - a*d)^9)/(9*b^{11}*(a + b*x)^{18}) - (45*d^2*(b*c - a*d)^8)/(17*b^{11}*(a + b*x)^{17}) - (15*d^3*(b*c - a*d)^7)/(2*b^{11}*(a + b*x)^{16}) - (14*d^4*(b*c - a*d)^6)/(b^{11}*(a + b*x)^{15}) - (18*d^5*(b*c - a*d)^5)/(b^{11}*(a + b*x)^{14}) - (210*d^6*(b*c - a*d)^4)/(13*b^{11}*(a + b*x)^{13}) - (10*d^7*(b*c - a*d)^3)/(b^{11}*(a + b*x)^{12}) - (45*d^8*(b*c - a*d)^2)/(11*b^{11}*(a + b*x)^{11}) - (d^9*(b*c - a*d))/(b^{11}*(a + b*x)^{10}) - d^{10}/(9*b^{11}*(a + b*x)^9)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c + dx)^{10}}{(a + bx)^{20}} dx = \int \left(\frac{(bc - ad)^{10}}{b^{10}(a + bx)^{20}} + \frac{10d(bc - ad)^9}{b^{10}(a + bx)^{19}} + \frac{45d^2(bc - ad)^8}{b^{10}(a + bx)^{18}} + \frac{120d^3(bc - ad)^7}{b^{10}(a + bx)^{17}} + \frac{210d^4(bc - ad)^6}{b^{10}(a + bx)^{16}} + \frac{15d^5(bc - ad)^5}{b^{10}(a + bx)^{15}} + \frac{10d^6(bc - ad)^4}{b^{10}(a + bx)^{14}} + \frac{5d^7(bc - ad)^3}{b^{10}(a + bx)^{13}} + \frac{d^8(bc - ad)^2}{b^{10}(a + bx)^{12}} + \frac{d^9(bc - ad)}{b^{10}(a + bx)^{11}} + \frac{d^{10}}{b^{10}(a + bx)^{10}} \right)$$

$$= -\frac{(bc - ad)^{10}}{19b^{11}(a + bx)^{19}} - \frac{5d(bc - ad)^9}{9b^{11}(a + bx)^{18}} - \frac{45d^2(bc - ad)^8}{17b^{11}(a + bx)^{17}} - \frac{15d^3(bc - ad)^7}{2b^{11}(a + bx)^{16}} - \frac{14d^4(bc - ad)^6}{b^{11}(a + bx)^{15}} - \frac{10d^5(bc - ad)^5}{11b^{11}(a + bx)^{14}} - \frac{5d^6(bc - ad)^4}{11b^{11}(a + bx)^{13}} - \frac{d^7(bc - ad)^3}{11b^{11}(a + bx)^{12}} - \frac{d^8(bc - ad)^2}{11b^{11}(a + bx)^{11}} - \frac{d^9(bc - ad)}{11b^{11}(a + bx)^{10}} - \frac{d^{10}}{11b^{11}(a + bx)^9}$$

Mathematica [B] time = 0.28, size = 692, normalized size = 2.53

$$\frac{a^{10}d^{10} + a^9bd^9(9c + 19dx) + 9a^8b^2d^8(5c^2 + 19cdx + 19d^2x^2) + 3a^7b^3d^7(55c^3 + 285c^2dx + 513cd^2x^2 + 323d^3x^3) + 3a^6b^4d^6(165c^4 + 1045c^3dx + 2565c^2d^2x^2 + 2907cd^3x^3 + 1292d^4x^4) + 9a^5b^5d^5(143c^5 + 1045c^4dx + 3135c^3d^2x^2 + 4845c^2d^3x^3 + 3876cd^4x^4 + 1292d^5x^5) + 3a^4b^6d^4(1001c^6 + 8151c^5dx + 28215c^4d^2x^2 + 53295c^3d^3x^3 + 58140c^2d^4x^4 + 34884cd^5x^5 + 9044d^6x^6) + 3a^3b^7d^3(2145c^7 + 19019c^6dx + 73359c^5d^2x^2 + 159885c^4d^3x^3 + 213180c^3d^4x^4 + 174420c^2d^5x^5 + 81396cd^6x^6 + 16796d^7x^7) + 9a^2b^8d^2(1430c^8 + 13585c^7dx + 57057c^6d^2x^2 + 138567c^5d^3x^3 + 213180c^4d^4x^4 + 213180c^3d^5x^5 + 135660c^2d^6x^6 + 50388cd^7x^7 + 8398d^8x^8) + ab^9d(24310c^9 + 244530c^8dx + 1100385c^7d^2x^2 + 2909907c^6d^3x^3 + 4988412c^5d^4x^4 + 5755860c^4d^5x^5 + 4476780c^3d^6x^6 + 2267460c^2d^7x^7 + 680238cd^8x^8 + 92378d^9x^9) + b^{10}(43758c^{10} + 461890c^9dx + 2200770c^8d^2x^2 + 6235515c^7d^3x^3 + 11639628c^6d^4x^4 + 14965236c^5d^5x^5 + 13430340c^4d^6x^6 + 8314020c^3d^7x^7 + 3401190c^2d^8x^8 + 831402cd^9x^9 + 92378d^{10}x^{10})}{b^{11}(a + bx)^{19}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^20,x]

[Out] -1/831402*(a^10*d^10 + a^9*b*d^9*(9*c + 19*d*x) + 9*a^8*b^2*d^8*(5*c^2 + 19*c*d*x + 19*d^2*x^2) + 3*a^7*b^3*d^7*(55*c^3 + 285*c^2*d*x + 513*c*d^2*x^2 + 323*d^3*x^3) + 3*a^6*b^4*d^6*(165*c^4 + 1045*c^3*d*x + 2565*c^2*d^2*x^2 + 2907*c*d^3*x^3 + 1292*d^4*x^4) + 9*a^5*b^5*d^5*(143*c^5 + 1045*c^4*d*x + 3135*c^3*d^2*x^2 + 4845*c^2*d^3*x^3 + 3876*c*d^4*x^4 + 1292*d^5*x^5) + 3*a^4*b^6*d^4*(1001*c^6 + 8151*c^5*d*x + 28215*c^4*d^2*x^2 + 53295*c^3*d^3*x^3 + 58140*c^2*d^4*x^4 + 34884*c*d^5*x^5 + 9044*d^6*x^6) + 3*a^3*b^7*d^3*(2145*c^7 + 19019*c^6*d*x + 73359*c^5*d^2*x^2 + 159885*c^4*d^3*x^3 + 213180*c^3*d^4*x^4 + 174420*c^2*d^5*x^5 + 81396*c*d^6*x^6 + 16796*d^7*x^7) + 9*a^2*b^8*d^2*(1430*c^8 + 13585*c^7*d*x + 57057*c^6*d^2*x^2 + 138567*c^5*d^3*x^3 + 213180*c^4*d^4*x^4 + 213180*c^3*d^5*x^5 + 135660*c^2*d^6*x^6 + 50388*c*d^7*x^7 + 8398*d^8*x^8) + a*b^9*d*(24310*c^9 + 244530*c^8*d*x + 1100385*c^7*d^2*x^2 + 2909907*c^6*d^3*x^3 + 4988412*c^5*d^4*x^4 + 5755860*c^4*d^5*x^5 + 4476780*c^3*d^6*x^6 + 2267460*c^2*d^7*x^7 + 680238*c*d^8*x^8 + 92378*d^9*x^9) + b^10*(43758*c^10 + 461890*c^9*d*x + 2200770*c^8*d^2*x^2 + 6235515*c^7*d^3*x^3 + 11639628*c^6*d^4*x^4 + 14965236*c^5*d^5*x^5 + 13430340*c^4*d^6*x^6 + 8314020*c^3*d^7*x^7 + 3401190*c^2*d^8*x^8 + 831402*c*d^9*x^9 + 92378*d^10*x^10))/(b^11*(a + b*x)^19)

fricas [B] time = 0.47, size = 1063, normalized size = 3.89

$$\frac{92378 b^{10} d^{10} x^{10} + 43758 b^{10} c^{10} + 24310 a b^9 c^9 d + 12870 a^2 b^8 c^8 d^2 + 6435 a^3 b^7 c^7 d^3 + 3003 a^4 b^6 c^6 d^4 + 1287 a^5 b^5 c^5 d^5 + 43758 a^6 b^4 c^4 d^6 + 12870 a^7 b^3 c^3 d^7 + 6435 a^8 b^2 c^2 d^8 + 3003 a^9 b c d^9 + 92378 a^{10} d^{10}}{b^{11} (a + b x)^{19}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^20,x, algorithm="fricas")

```
[Out] -1/831402*(92378*b^10*d^10*x^10 + 43758*b^10*c^10 + 24310*a*b^9*c^9*d + 128
70*a^2*b^8*c^8*d^2 + 6435*a^3*b^7*c^7*d^3 + 3003*a^4*b^6*c^6*d^4 + 1287*a^5
*b^5*c^5*d^5 + 495*a^6*b^4*c^4*d^6 + 165*a^7*b^3*c^3*d^7 + 45*a^8*b^2*c^2*d
^8 + 9*a^9*b*c*d^9 + a^10*d^10 + 92378*(9*b^10*c*d^9 + a*b^9*d^10)*x^9 + 75
582*(45*b^10*c^2*d^8 + 9*a*b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 50388*(165*b^10*
c^3*d^7 + 45*a*b^9*c^2*d^8 + 9*a^2*b^8*c*d^9 + a^3*b^7*d^10)*x^7 + 27132*(4
95*b^10*c^4*d^6 + 165*a*b^9*c^3*d^7 + 45*a^2*b^8*c^2*d^8 + 9*a^3*b^7*c*d^9
+ a^4*b^6*d^10)*x^6 + 11628*(1287*b^10*c^5*d^5 + 495*a*b^9*c^4*d^6 + 165*a^
2*b^8*c^3*d^7 + 45*a^3*b^7*c^2*d^8 + 9*a^4*b^6*c*d^9 + a^5*b^5*d^10)*x^5 +
3876*(3003*b^10*c^6*d^4 + 1287*a*b^9*c^5*d^5 + 495*a^2*b^8*c^4*d^6 + 165*a^
3*b^7*c^3*d^7 + 45*a^4*b^6*c^2*d^8 + 9*a^5*b^5*c*d^9 + a^6*b^4*d^10)*x^4 +
969*(6435*b^10*c^7*d^3 + 3003*a*b^9*c^6*d^4 + 1287*a^2*b^8*c^5*d^5 + 495*a^
3*b^7*c^4*d^6 + 165*a^4*b^6*c^3*d^7 + 45*a^5*b^5*c^2*d^8 + 9*a^6*b^4*c*d^9
+ a^7*b^3*d^10)*x^3 + 171*(12870*b^10*c^8*d^2 + 6435*a*b^9*c^7*d^3 + 3003*a
^2*b^8*c^6*d^4 + 1287*a^3*b^7*c^5*d^5 + 495*a^4*b^6*c^4*d^6 + 165*a^5*b^5*c
^3*d^7 + 45*a^6*b^4*c^2*d^8 + 9*a^7*b^3*c*d^9 + a^8*b^2*d^10)*x^2 + 19*(243
10*b^10*c^9*d + 12870*a*b^9*c^8*d^2 + 6435*a^2*b^8*c^7*d^3 + 3003*a^3*b^7*c
^6*d^4 + 1287*a^4*b^6*c^5*d^5 + 495*a^5*b^5*c^4*d^6 + 165*a^6*b^4*c^3*d^7 +
45*a^7*b^3*c^2*d^8 + 9*a^8*b^2*c*d^9 + a^9*b*d^10)*x)/(b^30*x^19 + 19*a*b^
29*x^18 + 171*a^2*b^28*x^17 + 969*a^3*b^27*x^16 + 3876*a^4*b^26*x^15 + 1162
8*a^5*b^25*x^14 + 27132*a^6*b^24*x^13 + 50388*a^7*b^23*x^12 + 75582*a^8*b^2
2*x^11 + 92378*a^9*b^21*x^10 + 92378*a^10*b^20*x^9 + 75582*a^11*b^19*x^8 +
50388*a^12*b^18*x^7 + 27132*a^13*b^17*x^6 + 11628*a^14*b^16*x^5 + 3876*a^15
*b^15*x^4 + 969*a^16*b^14*x^3 + 171*a^17*b^13*x^2 + 19*a^18*b^12*x + a^19*b
^11)
```

giac [B] time = 1.31, size = 961, normalized size = 3.52

$$\frac{92378 b^{10} d^{10} x^{10} + 831402 b^{10} c d^9 x^9 + 92378 a b^9 d^{10} x^9 + 3401190 b^{10} c^2 d^8 x^8 + 680238 a b^9 c d^9 x^8 + 75582 a^2 b^8 d^{10} x^8}{(b^{30} x^{19} + 19 a b^{29} x^{18} + 171 a^2 b^{28} x^{17} + 969 a^3 b^{27} x^{16} + 3876 a^4 b^{26} x^{15} + 11628 a^5 b^{25} x^{14} + 27132 a^6 b^{24} x^{13} + 50388 a^7 b^{23} x^{12} + 75582 a^8 b^{22} x^{11} + 92378 a^9 b^{21} x^{10} + 92378 a^{10} b^{20} x^9 + 75582 a^{11} b^{19} x^8 + 50388 a^{12} b^{18} x^7 + 27132 a^{13} b^{17} x^6 + 11628 a^{14} b^{16} x^5 + 3876 a^{15} b^{15} x^4 + 969 a^{16} b^{14} x^3 + 171 a^{17} b^{13} x^2 + 19 a^{18} b^{12} x + a^{19} b^{11})}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^10/(b*x+a)^20,x, algorithm="giac")
```

```
[Out] -1/831402*(92378*b^10*d^10*x^10 + 831402*b^10*c*d^9*x^9 + 92378*a*b^9*d^10*
x^9 + 3401190*b^10*c^2*d^8*x^8 + 680238*a*b^9*c*d^9*x^8 + 75582*a^2*b^8*d^10*
x^8 + 8314020*b^10*c^3*d^7*x^7 + 2267460*a*b^9*c^2*d^8*x^7 + 453492*a^2*b
^8*c*d^9*x^7 + 50388*a^3*b^7*d^10*x^7 + 13430340*b^10*c^4*d^6*x^6 + 4476780
*a*b^9*c^3*d^7*x^6 + 1220940*a^2*b^8*c^2*d^8*x^6 + 244188*a^3*b^7*c*d^9*x^6
+ 27132*a^4*b^6*d^10*x^6 + 14965236*b^10*c^5*d^5*x^5 + 5755860*a*b^9*c^4*d
^6*x^5 + 1918620*a^2*b^8*c^3*d^7*x^5 + 523260*a^3*b^7*c^2*d^8*x^5 + 104652*
a^4*b^6*c*d^9*x^5 + 11628*a^5*b^5*d^10*x^5 + 11639628*b^10*c^6*d^4*x^4 + 49
88412*a*b^9*c^5*d^5*x^4 + 1918620*a^2*b^8*c^4*d^6*x^4 + 639540*a^3*b^7*c^3*
d^7*x^4 + 174420*a^4*b^6*c^2*d^8*x^4 + 34884*a^5*b^5*c*d^9*x^4 + 3876*a^6*b
```

$$\begin{aligned} &^4d^{10}x^4 + 6235515b^{10}c^7d^3x^3 + 2909907a^9b^9c^6d^4x^3 + 124710 \\ &3a^2b^8c^5d^5x^3 + 479655a^3b^7c^4d^6x^3 + 159885a^4b^6c^3d^7 \\ &x^3 + 43605a^5b^5c^2d^8x^3 + 8721a^6b^4c^2d^9x^3 + 969a^7b^3d^1 \\ &0x^3 + 2200770b^{10}c^8d^2x^2 + 1100385a^9b^9c^7d^3x^2 + 513513a^2b \\ &^8c^6d^4x^2 + 220077a^3b^7c^5d^5x^2 + 84645a^4b^6c^4d^6x^2 + 2 \\ &8215a^5b^5c^3d^7x^2 + 7695a^6b^4c^2d^8x^2 + 1539a^7b^3c^2d^9x^ \\ &2 + 171a^8b^2d^{10}x^2 + 461890b^{10}c^9d^2x + 244530a^9b^9c^8d^2x + 1 \\ &22265a^2b^8c^7d^3x + 57057a^3b^7c^6d^4x + 24453a^4b^6c^5d^5x \\ &+ 9405a^5b^5c^4d^6x + 3135a^6b^4c^3d^7x + 855a^7b^3c^2d^8x \\ &+ 171a^8b^2c^2d^9x + 19a^9b^2d^{10}x + 43758b^{10}c^{10} + 24310a^9b^9c^9 \\ &d + 12870a^2b^8c^8d^2 + 6435a^3b^7c^7d^3 + 3003a^4b^6c^6d^4 + \\ &1287a^5b^5c^5d^5 + 495a^6b^4c^4d^6 + 165a^7b^3c^3d^7 + 45a^8b \\ &^2c^2d^8 + 9a^9b^2c^2d^9 + a^{10}d^{10})/((bx + a)^{19}b^{11}) \end{aligned}$$

maple [B] time = 0.01, size = 866, normalized size = 3.17

$$\frac{d^{10}}{9(bx+a)^9b^{11}} + \frac{(ad-bc)d^9}{(bx+a)^{10}b^{11}} - \frac{45(a^2d^2-2abcd+b^2c^2)d^8}{11(bx+a)^{11}b^{11}} + \frac{10(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^7}{(bx+a)^{12}b^{11}} - \frac{210}{(bx+a)^{13}b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^20,x)

[Out]
$$\begin{aligned} &-210/13*d^6*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4) \\ &/b^{11}/(b*x+a)^{13}-1/9*d^{10}/b^{11}/(b*x+a)^9-45/17*d^2*(a^8*d^8-8*a^7*b*c*d^7+2 \\ &8*a^6*b^2*c^2*d^6-56*a^5*b^3*c^3*d^5+70*a^4*b^4*c^4*d^4-56*a^3*b^5*c^5*d^3+ \\ &28*a^2*b^6*c^6*d^2-8*a*b^7*c^7*d+b^8*c^8)/b^{11}/(b*x+a)^{17}-45/11*d^8*(a^2*d^ \\ &2-2*a*b*c*d+b^2*c^2)/b^{11}/(b*x+a)^{11}-14*d^4*(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b \\ &^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)/b^{11} \\ &1/(b*x+a)^{15}+10*d^7*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^{11}/(b*x \\ &+a)^{12}+5/9*d*(a^9*d^9-9*a^8*b*c*d^8+36*a^7*b^2*c^2*d^7-84*a^6*b^3*c^3*d^6+1 \\ &26*a^5*b^4*c^4*d^5-126*a^4*b^5*c^5*d^4+84*a^3*b^6*c^6*d^3-36*a^2*b^7*c^7*d^ \\ &2+9*a*b^8*c^8*d-b^9*c^9)/b^{11}/(b*x+a)^{18}-1/19*(a^{10}*d^{10}-10*a^9*b*c*d^9+45* \\ &a^8*b^2*c^2*d^8-120*a^7*b^3*c^3*d^7+210*a^6*b^4*c^4*d^6-252*a^5*b^5*c^5*d^5 \\ &+210*a^4*b^6*c^6*d^4-120*a^3*b^7*c^7*d^3+45*a^2*b^8*c^8*d^2-10*a*b^9*c^9*d+ \\ &b^{10}*c^{10})/b^{11}/(b*x+a)^{19}+d^9*(a*d-b*c)/b^{11}/(b*x+a)^{10}+18*d^5*(a^5*d^5-5* \\ &a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)/b^{11} \\ &11/(b*x+a)^{14}+15/2*d^3*(a^7*d^7-7*a^6*b*c*d^6+21*a^5*b^2*c^2*d^5-35*a^4*b^3 \\ &*c^3*d^4+35*a^3*b^4*c^4*d^3-21*a^2*b^5*c^5*d^2+7*a*b^6*c^6*d-b^7*c^7)/b^{11}/ \\ &(b*x+a)^{16} \end{aligned}$$

maxima [B] time = 2.45, size = 1063, normalized size = 3.89

$$\frac{92378 b^{10} d^{10} x^{10} + 43758 b^{10} c^{10} + 24310 a b^9 c^9 d + 12870 a^2 b^8 c^8 d^2 + 6435 a^3 b^7 c^7 d^3 + 3003 a^4 b^6 c^6 d^4 + 1287 a^5 b^5 c^5 d^5 + 495 a^6 b^4 c^4 d^6 + 165 a^7 b^3 c^3 d^7 + 45 a^8 b^2 c^2 d^8 + 9 a^9 b^2 c^2 d^9 + a^{10} d^{10}}{(bx+a)^{19} b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^20,x, algorithm="maxima")

[Out]
$$-1/831402*(92378*b^{10}*d^{10}*x^{10} + 43758*b^{10}*c^{10} + 24310*a*b^9*c^9*d + 12870*a^2*b^8*c^8*d^2 + 6435*a^3*b^7*c^7*d^3 + 3003*a^4*b^6*c^6*d^4 + 1287*a^5*b^5*c^5*d^5 + 495*a^6*b^4*c^4*d^6 + 165*a^7*b^3*c^3*d^7 + 45*a^8*b^2*c^2*d^8 + 9*a^9*b*c*d^9 + a^{10}*d^{10} + 92378*(9*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 + 75582*(45*b^{10}*c^2*d^8 + 9*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 50388*(165*b^{10}*c^3*d^7 + 45*a*b^9*c^2*d^8 + 9*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 27132*(495*b^{10}*c^4*d^6 + 165*a*b^9*c^3*d^7 + 45*a^2*b^8*c^2*d^8 + 9*a^3*b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 11628*(1287*b^{10}*c^5*d^5 + 495*a*b^9*c^4*d^6 + 165*a^2*b^8*c^3*d^7 + 45*a^3*b^7*c^2*d^8 + 9*a^4*b^6*c*d^9 + a^5*b^5*d^{10})*x^5 + 3876*(3003*b^{10}*c^6*d^4 + 1287*a*b^9*c^5*d^5 + 495*a^2*b^8*c^4*d^6 + 165*a^3*b^7*c^3*d^7 + 45*a^4*b^6*c^2*d^8 + 9*a^5*b^5*c*d^9 + a^6*b^4*d^{10})*x^4 + 969*(6435*b^{10}*c^7*d^3 + 3003*a*b^9*c^6*d^4 + 1287*a^2*b^8*c^5*d^5 + 495*a^3*b^7*c^4*d^6 + 165*a^4*b^6*c^3*d^7 + 45*a^5*b^5*c^2*d^8 + 9*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + 171*(12870*b^{10}*c^8*d^2 + 6435*a*b^9*c^7*d^3 + 3003*a^2*b^8*c^6*d^4 + 1287*a^3*b^7*c^5*d^5 + 495*a^4*b^6*c^4*d^6 + 165*a^5*b^5*c^3*d^7 + 45*a^6*b^4*c^2*d^8 + 9*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 + 19*(24310*b^{10}*c^9*d + 12870*a*b^9*c^8*d^2 + 6435*a^2*b^8*c^7*d^3 + 3003*a^3*b^7*c^6*d^4 + 1287*a^4*b^6*c^5*d^5 + 495*a^5*b^5*c^4*d^6 + 165*a^6*b^4*c^3*d^7 + 45*a^7*b^3*c^2*d^8 + 9*a^8*b^2*c*d^9 + a^9*b*d^{10})*x)/(b^{30}*x^{19} + 19*a*b^{29}*x^{18} + 171*a^2*b^{28}*x^{17} + 969*a^3*b^{27}*x^{16} + 3876*a^4*b^{26}*x^{15} + 11628*a^5*b^{25}*x^{14} + 27132*a^6*b^{24}*x^{13} + 50388*a^7*b^{23}*x^{12} + 75582*a^8*b^{22}*x^{11} + 92378*a^9*b^{21}*x^{10} + 92378*a^{10}*b^{20}*x^9 + 75582*a^{11}*b^{19}*x^8 + 50388*a^{12}*b^{18}*x^7 + 27132*a^{13}*b^{17}*x^6 + 11628*a^{14}*b^{16}*x^5 + 3876*a^{15}*b^{15}*x^4 + 969*a^{16}*b^{14}*x^3 + 171*a^{17}*b^{13}*x^2 + 19*a^{18}*b^{12}*x + a^{19}*b^{11})$$

mupad [B] time = 25.72, size = 1164, normalized size = 4.26

$$\frac{a^{10} d^{10} + 9 a^9 b c d^9 + 19 a^9 b d^{10} x + 45 a^8 b^2 c^2 d^8 + 171 a^8 b^2 c d^9 x + 171 a^8 b^2 d^{10} x^2 + 165 a^7 b^3 c^3 d^7 + 855 a^7 b^3 c^2 d^8 + 45 a^7 b^3 c d^9 x + 45 a^7 b^3 d^{10} x^2 + 165 a^6 b^4 c^4 d^6 + 165 a^6 b^4 c^3 d^7 + 45 a^6 b^4 c^2 d^8 + 9 a^6 b^4 c d^9 x + 9 a^6 b^4 d^{10} x^2 + 165 a^5 b^5 c^5 d^5 + 495 a^5 b^5 c^4 d^6 + 165 a^5 b^5 c^3 d^7 + 45 a^5 b^5 c^2 d^8 + 9 a^5 b^5 c d^9 x + 9 a^5 b^5 d^{10} x^2 + 165 a^4 b^6 c^6 d^4 + 1287 a^4 b^6 c^5 d^5 + 495 a^4 b^6 c^4 d^6 + 165 a^4 b^6 c^3 d^7 + 45 a^4 b^6 c^2 d^8 + 9 a^4 b^6 c d^9 x + 9 a^4 b^6 d^{10} x^2 + 165 a^3 b^7 c^7 d^3 + 3003 a^3 b^7 c^6 d^4 + 1287 a^3 b^7 c^5 d^5 + 495 a^3 b^7 c^4 d^6 + 165 a^3 b^7 c^3 d^7 + 45 a^3 b^7 c^2 d^8 + 9 a^3 b^7 c d^9 x + 9 a^3 b^7 d^{10} x^2 + 165 a^2 b^8 c^8 d^2 + 6435 a^2 b^8 c^7 d^3 + 3003 a^2 b^8 c^6 d^4 + 1287 a^2 b^8 c^5 d^5 + 495 a^2 b^8 c^4 d^6 + 165 a^2 b^8 c^3 d^7 + 45 a^2 b^8 c^2 d^8 + 9 a^2 b^8 c d^9 x + 9 a^2 b^8 d^{10} x^2 + 165 a b^9 c^9 d + 12870 a b^9 c^8 d^2 + 6435 a b^9 c^7 d^3 + 3003 a b^9 c^6 d^4 + 1287 a b^9 c^5 d^5 + 495 a b^9 c^4 d^6 + 165 a b^9 c^3 d^7 + 45 a b^9 c^2 d^8 + 9 a b^9 c d^9 x + 9 a b^9 d^{10} x^2 + 165 a^9 b^{10} c d + 12870 a^9 b^{10} c^2 d^2 + 6435 a^9 b^{10} c^3 d^3 + 3003 a^9 b^{10} c^4 d^4 + 1287 a^9 b^{10} c^5 d^5 + 495 a^9 b^{10} c^6 d^6 + 165 a^9 b^{10} c^7 d^7 + 45 a^9 b^{10} c^8 d^8 + 9 a^9 b^{10} c^9 d^9 + a^{10} b^{10} d^{10} x^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^20,x)

[Out]
$$-(a^{10}*d^{10} + 43758*b^{10}*c^{10} + 92378*b^{10}*d^{10}*x^{10} + 92378*a*b^9*d^{10}*x^9 + 831402*b^{10}*c*d^9*x^9 + 12870*a^2*b^8*c^8*d^2 + 6435*a^3*b^7*c^7*d^3 + 3003*a^4*b^6*c^6*d^4 + 1287*a^5*b^5*c^5*d^5 + 495*a^6*b^4*c^4*d^6 + 165*a^7*b^3*c^3*d^7 + 45*a^8*b^2*c^2*d^8 + 171*a^8*b^2*d^{10}*x^2 + 969*a^7*b^3*d^{10}*x^3 + 3876*a^6*b^4*d^{10}*x^4 + 11628*a^5*b^5*d^{10}*x^5 + 27132*a^4*b^6*d^{10}*x^6 + 50388*a^3*b^7*d^{10}*x^7 + 75582*a^2*b^8*d^{10}*x^8 + 2200770*b^{10}*c^8*d^2*x^2 + 6235515*b^{10}*c^7*d^3*x^3 + 11639628*b^{10}*c^6*d^4*x^4 + 14965236*b^{10}$$

```

*c^5*d^5*x^5 + 13430340*b^10*c^4*d^6*x^6 + 8314020*b^10*c^3*d^7*x^7 + 34011
90*b^10*c^2*d^8*x^8 + 24310*a*b^9*c^9*d + 9*a^9*b*c*d^9 + 19*a^9*b*d^10*x +
461890*b^10*c^9*d*x + 513513*a^2*b^8*c^6*d^4*x^2 + 220077*a^3*b^7*c^5*d^5*
x^2 + 84645*a^4*b^6*c^4*d^6*x^2 + 28215*a^5*b^5*c^3*d^7*x^2 + 7695*a^6*b^4*
c^2*d^8*x^2 + 1247103*a^2*b^8*c^5*d^5*x^3 + 479655*a^3*b^7*c^4*d^6*x^3 + 15
9885*a^4*b^6*c^3*d^7*x^3 + 43605*a^5*b^5*c^2*d^8*x^3 + 1918620*a^2*b^8*c^4*
d^6*x^4 + 639540*a^3*b^7*c^3*d^7*x^4 + 174420*a^4*b^6*c^2*d^8*x^4 + 1918620
*a^2*b^8*c^3*d^7*x^5 + 523260*a^3*b^7*c^2*d^8*x^5 + 1220940*a^2*b^8*c^2*d^8
*x^6 + 244530*a*b^9*c^8*d^2*x + 171*a^8*b^2*c*d^9*x + 680238*a*b^9*c*d^9*x^
8 + 122265*a^2*b^8*c^7*d^3*x + 57057*a^3*b^7*c^6*d^4*x + 24453*a^4*b^6*c^5*
d^5*x + 9405*a^5*b^5*c^4*d^6*x + 3135*a^6*b^4*c^3*d^7*x + 855*a^7*b^3*c^2*d
^8*x + 1100385*a*b^9*c^7*d^3*x^2 + 1539*a^7*b^3*c*d^9*x^2 + 2909907*a*b^9*c
^6*d^4*x^3 + 8721*a^6*b^4*c*d^9*x^3 + 4988412*a*b^9*c^5*d^5*x^4 + 34884*a^5
*b^5*c*d^9*x^4 + 5755860*a*b^9*c^4*d^6*x^5 + 104652*a^4*b^6*c*d^9*x^5 + 447
6780*a*b^9*c^3*d^7*x^6 + 244188*a^3*b^7*c*d^9*x^6 + 2267460*a*b^9*c^2*d^8*x
^7 + 453492*a^2*b^8*c*d^9*x^7)/(831402*a^19*b^11 + 831402*b^30*x^19 + 15796
638*a^18*b^12*x + 15796638*a*b^29*x^18 + 142169742*a^17*b^13*x^2 + 80562853
8*a^16*b^14*x^3 + 3222514152*a^15*b^15*x^4 + 9667542456*a^14*b^16*x^5 + 225
57599064*a^13*b^17*x^6 + 41892683976*a^12*b^18*x^7 + 62839025964*a^11*b^19*
x^8 + 76803253956*a^10*b^20*x^9 + 76803253956*a^9*b^21*x^10 + 62839025964*a
^8*b^22*x^11 + 41892683976*a^7*b^23*x^12 + 22557599064*a^6*b^24*x^13 + 9667
542456*a^5*b^25*x^14 + 3222514152*a^4*b^26*x^15 + 805628538*a^3*b^27*x^16 +
142169742*a^2*b^28*x^17)

```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**20,x)

[Out] Timed out

$$3.1332 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{21}} dx$$

Optimal. Leaf size=279

$$\frac{10d^9(bc-ad)}{11b^{11}(a+bx)^{11}} - \frac{15d^8(bc-ad)^2}{4b^{11}(a+bx)^{12}} - \frac{120d^7(bc-ad)^3}{13b^{11}(a+bx)^{13}} - \frac{15d^6(bc-ad)^4}{b^{11}(a+bx)^{14}} - \frac{84d^5(bc-ad)^5}{5b^{11}(a+bx)^{15}} - \frac{105d^4(bc-ad)^6}{8b^{11}(a+bx)^{16}} - \frac{120d^3(bc-ad)^7}{17b^{11}(a+bx)^{17}} - \frac{105d^2(bc-ad)^8}{8b^{11}(a+bx)^{18}} - \frac{84d(bc-ad)^9}{5b^{11}(a+bx)^{19}} - \frac{10d^9(bc-ad)^{10}}{11b^{11}(a+bx)^{20}}$$

[Out] $-1/20*(-a*d+b*c)^{10}/b^{11}/(b*x+a)^{20}-10/19*d*(-a*d+b*c)^9/b^{11}/(b*x+a)^{19}-5/2*d^2*(-a*d+b*c)^8/b^{11}/(b*x+a)^{18}-120/17*d^3*(-a*d+b*c)^7/b^{11}/(b*x+a)^{17}-105/8*d^4*(-a*d+b*c)^6/b^{11}/(b*x+a)^{16}-84/5*d^5*(-a*d+b*c)^5/b^{11}/(b*x+a)^{15}-15*d^6*(-a*d+b*c)^4/b^{11}/(b*x+a)^{14}-120/13*d^7*(-a*d+b*c)^3/b^{11}/(b*x+a)^{13}-15/4*d^8*(-a*d+b*c)^2/b^{11}/(b*x+a)^{12}-10/11*d^9*(-a*d+b*c)/b^{11}/(b*x+a)^{11}-1/10*d^{10}/b^{11}/(b*x+a)^{10}$

Rubi [A] time = 0.27, antiderivative size = 279, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{10d^9(bc-ad)}{11b^{11}(a+bx)^{11}} - \frac{15d^8(bc-ad)^2}{4b^{11}(a+bx)^{12}} - \frac{120d^7(bc-ad)^3}{13b^{11}(a+bx)^{13}} - \frac{15d^6(bc-ad)^4}{b^{11}(a+bx)^{14}} - \frac{84d^5(bc-ad)^5}{5b^{11}(a+bx)^{15}} - \frac{105d^4(bc-ad)^6}{8b^{11}(a+bx)^{16}} - \frac{120d^3(bc-ad)^7}{17b^{11}(a+bx)^{17}} - \frac{105d^2(bc-ad)^8}{8b^{11}(a+bx)^{18}} - \frac{84d(bc-ad)^9}{5b^{11}(a+bx)^{19}} - \frac{10d^9(bc-ad)^{10}}{11b^{11}(a+bx)^{20}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^21,x]

[Out] $-(b*c - a*d)^{10}/(20*b^{11}*(a + b*x)^{20}) - (10*d*(b*c - a*d)^9)/(19*b^{11}*(a + b*x)^{19}) - (5*d^2*(b*c - a*d)^8)/(2*b^{11}*(a + b*x)^{18}) - (120*d^3*(b*c - a*d)^7)/(17*b^{11}*(a + b*x)^{17}) - (105*d^4*(b*c - a*d)^6)/(8*b^{11}*(a + b*x)^{16}) - (84*d^5*(b*c - a*d)^5)/(5*b^{11}*(a + b*x)^{15}) - (15*d^6*(b*c - a*d)^4)/(b^{11}*(a + b*x)^{14}) - (120*d^7*(b*c - a*d)^3)/(13*b^{11}*(a + b*x)^{13}) - (15*d^8*(b*c - a*d)^2)/(4*b^{11}*(a + b*x)^{12}) - (10*d^9*(b*c - a*d))/(11*b^{11}*(a + b*x)^{11}) - d^{10}/(10*b^{11}*(a + b*x)^{10})$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c+dx)^{10}}{(a+bx)^{21}} dx = \int \left(\frac{(bc-ad)^{10}}{b^{10}(a+bx)^{21}} + \frac{10d(bc-ad)^9}{b^{10}(a+bx)^{20}} + \frac{45d^2(bc-ad)^8}{b^{10}(a+bx)^{19}} + \frac{120d^3(bc-ad)^7}{b^{10}(a+bx)^{18}} + \frac{210d^4(bc-ad)^6}{b^{10}(a+bx)^{17}} + \frac{(bc-ad)^{10}}{20b^{11}(a+bx)^{20}} - \frac{10d(bc-ad)^9}{19b^{11}(a+bx)^{19}} - \frac{5d^2(bc-ad)^8}{2b^{11}(a+bx)^{18}} - \frac{120d^3(bc-ad)^7}{17b^{11}(a+bx)^{17}} - \frac{105d^4(bc-ad)^6}{8b^{11}(a+bx)^{16}} \right)$$

Mathematica [B] time = 0.29, size = 692, normalized size = 2.48

$$\frac{a^{10}d^{10} + 10a^9bd^9(c+2dx) + 5a^8b^2d^8(11c^2 + 40cdx + 38d^2x^2) + 20a^7b^3d^7(11c^3 + 55c^2dx + 95cd^2x^2 + 57d^3x^3)}{b^{11}(a+bx)^{20}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^21,x]

[Out]
$$\frac{-1/1847560*(a^{10}d^{10} + 10*a^9*b*d^9*(c + 2*d*x) + 5*a^8*b^2*d^8*(11*c^2 + 40*c*d*x + 38*d^2*x^2) + 20*a^7*b^3*d^7*(11*c^3 + 55*c^2*d*x + 95*c*d^2*x^2 + 57*d^3*x^3) + 5*a^6*b^4*d^6*(143*c^4 + 880*c^3*d*x + 2090*c^2*d^2*x^2 + 2280*c*d^3*x^3 + 969*d^4*x^4) + 2*a^5*b^5*d^5*(1001*c^5 + 7150*c^4*d*x + 20900*c^3*d^2*x^2 + 31350*c^2*d^3*x^3 + 24225*c*d^4*x^4 + 7752*d^5*x^5) + 5*a^4*b^6*d^4*(1001*c^6 + 8008*c^5*d*x + 27170*c^4*d^2*x^2 + 50160*c^3*d^3*x^3 + 53295*c^2*d^4*x^4 + 31008*c*d^5*x^5 + 7752*d^6*x^6) + 20*a^3*b^7*d^3*(572*c^7 + 5005*c^6*d*x + 19019*c^5*d^2*x^2 + 40755*c^4*d^3*x^3 + 53295*c^3*d^4*x^4 + 42636*c^2*d^5*x^5 + 19380*c*d^6*x^6 + 3876*d^7*x^7) + 5*a^2*b^8*d^2*(4862*c^8 + 45760*c^7*d*x + 190190*c^6*d^2*x^2 + 456456*c^5*d^3*x^3 + 692835*c^4*d^4*x^4 + 682176*c^3*d^5*x^5 + 426360*c^2*d^6*x^6 + 155040*c*d^7*x^7 + 25194*d^8*x^8) + 10*a*b^9*d*(4862*c^9 + 48620*c^8*d*x + 217360*c^7*d^2*x^2 + 570570*c^6*d^3*x^3 + 969969*c^5*d^4*x^4 + 1108536*c^4*d^5*x^5 + 852720*c^3*d^6*x^6 + 426360*c^2*d^7*x^7 + 125970*c*d^8*x^8 + 16796*d^9*x^9) + b^10*(92378*c^10 + 972400*c^9*d*x + 4618900*c^8*d^2*x^2 + 13041600*c^7*d^3*x^3 + 24249225*c^6*d^4*x^4 + 31039008*c^5*d^5*x^5 + 27713400*c^4*d^6*x^6 + 17054400*c^3*d^7*x^7 + 6928350*c^2*d^8*x^8 + 1679600*c*d^9*x^9 + 184756*d^10*x^10))/(b^11*(a + b*x)^20)$$

fricas [B] time = 0.48, size = 1074, normalized size = 3.85

$$\frac{184756 b^{10} d^{10} x^{10} + 92378 b^{10} c^{10} + 48620 a b^9 c^9 d + 24310 a^2 b^8 c^8 d^2 + 11440 a^3 b^7 c^7 d^3 + 5005 a^4 b^6 c^6 d^4 + 2002 a^5 b^5 c^5 d^5 + 1001 a^6 b^4 c^4 d^6 + 1001 a^7 b^3 c^3 d^7 + 1001 a^8 b^2 c^2 d^8 + 1001 a^9 b c d^9 + 1001 a^{10} d^{10}}{b^{11} (a + b x)^{20}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^21,x, algorithm="fricas")

```
[Out] -1/1847560*(184756*b^10*d^10*x^10 + 92378*b^10*c^10 + 48620*a*b^9*c^9*d + 2
4310*a^2*b^8*c^8*d^2 + 11440*a^3*b^7*c^7*d^3 + 5005*a^4*b^6*c^6*d^4 + 2002*
a^5*b^5*c^5*d^5 + 715*a^6*b^4*c^4*d^6 + 220*a^7*b^3*c^3*d^7 + 55*a^8*b^2*c^
2*d^8 + 10*a^9*b*c*d^9 + a^10*d^10 + 167960*(10*b^10*c*d^9 + a*b^9*d^10)*x^
9 + 125970*(55*b^10*c^2*d^8 + 10*a*b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 77520*(2
20*b^10*c^3*d^7 + 55*a*b^9*c^2*d^8 + 10*a^2*b^8*c*d^9 + a^3*b^7*d^10)*x^7 +
38760*(715*b^10*c^4*d^6 + 220*a*b^9*c^3*d^7 + 55*a^2*b^8*c^2*d^8 + 10*a^3*
b^7*c*d^9 + a^4*b^6*d^10)*x^6 + 15504*(2002*b^10*c^5*d^5 + 715*a*b^9*c^4*d^
6 + 220*a^2*b^8*c^3*d^7 + 55*a^3*b^7*c^2*d^8 + 10*a^4*b^6*c*d^9 + a^5*b^5*d
^10)*x^5 + 4845*(5005*b^10*c^6*d^4 + 2002*a*b^9*c^5*d^5 + 715*a^2*b^8*c^4*d
^6 + 220*a^3*b^7*c^3*d^7 + 55*a^4*b^6*c^2*d^8 + 10*a^5*b^5*c*d^9 + a^6*b^4*
d^10)*x^4 + 1140*(11440*b^10*c^7*d^3 + 5005*a*b^9*c^6*d^4 + 2002*a^2*b^8*c^
5*d^5 + 715*a^3*b^7*c^4*d^6 + 220*a^4*b^6*c^3*d^7 + 55*a^5*b^5*c^2*d^8 + 10
*a^6*b^4*c*d^9 + a^7*b^3*d^10)*x^3 + 190*(24310*b^10*c^8*d^2 + 11440*a*b^9*
c^7*d^3 + 5005*a^2*b^8*c^6*d^4 + 2002*a^3*b^7*c^5*d^5 + 715*a^4*b^6*c^4*d^6
+ 220*a^5*b^5*c^3*d^7 + 55*a^6*b^4*c^2*d^8 + 10*a^7*b^3*c*d^9 + a^8*b^2*d^
10)*x^2 + 20*(48620*b^10*c^9*d + 24310*a*b^9*c^8*d^2 + 11440*a^2*b^8*c^7*d^
3 + 5005*a^3*b^7*c^6*d^4 + 2002*a^4*b^6*c^5*d^5 + 715*a^5*b^5*c^4*d^6 + 220
*a^6*b^4*c^3*d^7 + 55*a^7*b^3*c^2*d^8 + 10*a^8*b^2*c*d^9 + a^9*b*d^10)*x)/(
b^31*x^20 + 20*a*b^30*x^19 + 190*a^2*b^29*x^18 + 1140*a^3*b^28*x^17 + 4845*
a^4*b^27*x^16 + 15504*a^5*b^26*x^15 + 38760*a^6*b^25*x^14 + 77520*a^7*b^24*
x^13 + 125970*a^8*b^23*x^12 + 167960*a^9*b^22*x^11 + 184756*a^10*b^21*x^10
+ 167960*a^11*b^20*x^9 + 125970*a^12*b^19*x^8 + 77520*a^13*b^18*x^7 + 38760
*a^14*b^17*x^6 + 15504*a^15*b^16*x^5 + 4845*a^16*b^15*x^4 + 1140*a^17*b^14*
x^3 + 190*a^18*b^13*x^2 + 20*a^19*b^12*x + a^20*b^11)
```

giac [B] time = 1.31, size = 961, normalized size = 3.44

$$\frac{184756 b^{10} d^{10} x^{10} + 1679600 b^{10} c d^9 x^9 + 167960 a b^9 d^{10} x^9 + 6928350 b^{10} c^2 d^8 x^8 + 1259700 a b^9 c d^9 x^8 + 125970 a^2 b^8 d^{10} x^8 + 17054400 b^{10} c^3 d^7 x^7 + 4263600 a b^9 c^2 d^8 x^7 + 775200 a^2 b^8 c d^9 x^7 + 77520 a^3 b^7 d^{10} x^7 + 27713400 b^{10} c^4 d^6 x^6 + 8527200 a b^9 c^3 d^7 x^6 + 2131800 a^2 b^8 c^2 d^8 x^6 + 387600 a^3 b^7 c d^9 x^6 + 38760 a^4 b^6 d^{10} x^6 + 31039008 b^{10} c^5 d^5 x^5 + 11085360 a b^9 c^4 d^6 x^5 + 3410880 a^2 b^8 c^3 d^7 x^5 + 852720 a^3 b^7 c^2 d^8 x^5 + 155040 a^4 b^6 c d^9 x^5 + 15504 a^5 b^5 d^{10} x^5 + 24249225 b^{10} c^6 d^4 x^4 + 9699690 a b^9 c^5 d^5 x^4 + 3464175 a^2 b^8 c^4 d^6 x^4 + 1065900 a^3 b^7 c^3 d^7 x^4 + 266475 a^4 b^6 c^2 d^8 x^4 + 48450 a^5 b^5 c d^9 x^4 + 4$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^10/(b*x+a)^21,x, algorithm="giac")
```

```
[Out] -1/1847560*(184756*b^10*d^10*x^10 + 1679600*b^10*c*d^9*x^9 + 167960*a*b^9*d
^10*x^9 + 6928350*b^10*c^2*d^8*x^8 + 1259700*a*b^9*c*d^9*x^8 + 125970*a^2*b
^8*d^10*x^8 + 17054400*b^10*c^3*d^7*x^7 + 4263600*a*b^9*c^2*d^8*x^7 + 77520
0*a^2*b^8*c*d^9*x^7 + 77520*a^3*b^7*d^10*x^7 + 27713400*b^10*c^4*d^6*x^6 +
8527200*a*b^9*c^3*d^7*x^6 + 2131800*a^2*b^8*c^2*d^8*x^6 + 387600*a^3*b^7*c*
d^9*x^6 + 38760*a^4*b^6*d^10*x^6 + 31039008*b^10*c^5*d^5*x^5 + 11085360*a*b
^9*c^4*d^6*x^5 + 3410880*a^2*b^8*c^3*d^7*x^5 + 852720*a^3*b^7*c^2*d^8*x^5 +
155040*a^4*b^6*c*d^9*x^5 + 15504*a^5*b^5*d^10*x^5 + 24249225*b^10*c^6*d^4*
x^4 + 9699690*a*b^9*c^5*d^5*x^4 + 3464175*a^2*b^8*c^4*d^6*x^4 + 1065900*a^3
*b^7*c^3*d^7*x^4 + 266475*a^4*b^6*c^2*d^8*x^4 + 48450*a^5*b^5*c*d^9*x^4 + 4
```


$845a^6b^4d^{10}x^4 + 13041600b^{10}c^7d^3x^3 + 5705700ab^9c^6d^4x^3 + 2282280a^2b^8c^5d^5x^3 + 815100a^3b^7c^4d^6x^3 + 250800a^4b^6c^3d^7x^3 + 62700a^5b^5c^2d^8x^3 + 11400a^6b^4c^1d^9x^3 + 1140a^7b^3d^{10}x^3 + 4618900b^{10}c^8d^2x^2 + 2173600ab^9c^7d^3x^2 + 950950a^2b^8c^6d^4x^2 + 380380a^3b^7c^5d^5x^2 + 135850a^4b^6c^4d^6x^2 + 41800a^5b^5c^3d^7x^2 + 10450a^6b^4c^2d^8x^2 + 1900a^7b^3c^1d^9x^2 + 190a^8b^2d^{10}x^2 + 972400b^{10}c^9dx + 486200ab^9c^8d^2x + 228800a^2b^8c^7d^3x + 100100a^3b^7c^6d^4x + 40040a^4b^6c^5d^5x + 14300a^5b^5c^4d^6x + 4400a^6b^4c^3d^7x + 1100a^7b^3c^2d^8x + 200a^8b^2c^1d^9x + 20a^9b^1d^{10}x + 92378b^{10}c^{10} + 48620ab^9c^9d + 24310a^2b^8c^8d^2 + 11440a^3b^7c^7d^3 + 5005a^4b^6c^6d^4 + 2002a^5b^5c^5d^5 + 715a^6b^4c^4d^6 + 220a^7b^3c^3d^7 + 55a^8b^2c^2d^8 + 10a^9b^1c^1d^9 + a^{10}d^{10}) / ((bx + a)^{20}b^{11})$

maple [B] time = 0.01, size = 867, normalized size = 3.11

$$-\frac{d^{10}}{10(bx+a)^{10}b^{11}} + \frac{10(ad-bc)d^9}{11(bx+a)^{11}b^{11}} - \frac{15(a^2d^2-2abcd+b^2c^2)d^8}{4(bx+a)^{12}b^{11}} + \frac{120(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^7}{13(bx+a)^{13}b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^21,x)

[Out] $120/13*d^7*(a^3d^3-3a^2b*c*d^2+3a*b^2*c^2*d-b^3*c^3)/b^{11}/(b*x+a)^{13}-1/20*(a^{10}d^{10}-10a^9b*c*d^9+45a^8b^2c^2d^8-120a^7b^3c^3d^7+210a^6b^4c^4d^6-252a^5b^5c^5d^5+210a^4b^6c^6d^4-120a^3b^7c^7d^3+45a^2b^8c^8d^2-10a*b^9c^9d+b^{10}c^{10})/b^{11}/(b*x+a)^{20}+120/17*d^3*(a^7d^7-7a^6b*c*d^6+21a^5b^2c^2d^5-35a^4b^3c^3d^4+35a^3b^4c^4d^3-21a^2b^5c^5d^2+7a*b^6c^6d-b^7*c^7)/b^{11}/(b*x+a)^{17}+10/11*d^9*(a*d-b*c)/b^{11}/(b*x+a)^{11}+84/5*d^5*(a^5d^5-5a^4b*c*d^4+10a^3b^2c^2d^3-10a^2b^3c^3d^2+5a*b^4c^4d-b^5*c^5)/b^{11}/(b*x+a)^{15}-15/4*d^8*(a^2d^2-2a*b*c*d+b^2*c^2)/b^{11}/(b*x+a)^{12}-5/2*d^2*(a^8d^8-8a^7b*c*d^7+28a^6b^2c^2d^6-56a^5b^3c^3d^5+70a^4b^4c^4d^4-56a^3b^5c^5d^3+28a^2b^6c^6d^2-8a*b^7c^7d+b^8*c^8)/b^{11}/(b*x+a)^{18}+10/19*d*(a^9d^9-9a^8b*c*d^8+36a^7b^2c^2d^7-84a^6b^3c^3d^6+126a^5b^4c^4d^5-126a^4b^5c^5d^4+84a^3b^6c^6d^3-36a^2b^7c^7d^2+9a*b^8c^8d-b^9*c^9)/b^{11}/(b*x+a)^{19}-1/10*d^{10}/b^{11}/(b*x+a)^{10}-15*d^6*(a^4d^4-4a^3b*c*d^3+6a^2b^2c^2d^2-4a*b^3c^3d+b^4*c^4)/b^{11}/(b*x+a)^{14}-105/8*d^4*(a^6d^6-6a^5b*c*d^5+15a^4b^2c^2d^4-20a^3b^3c^3d^3+15a^2b^4c^4d^2-6a*b^5c^5d+b^6*c^6)/b^{11}/(b*x+a)^{16}$

maxima [B] time = 2.51, size = 1074, normalized size = 3.85

$$184756 b^{10} d^{10} x^{10} + 92378 b^{10} c^{10} + 48620 a b^9 c^9 d + 24310 a^2 b^8 c^8 d^2 + 11440 a^3 b^7 c^7 d^3 + 5005 a^4 b^6 c^6 d^4 + 2002$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^21,x, algorithm="maxima")

[Out]
$$\begin{aligned} & -1/1847560*(184756*b^{10}*d^{10}*x^{10} + 92378*b^{10}*c^{10} + 48620*a*b^9*c^9*d + 2 \\ & 4310*a^2*b^8*c^8*d^2 + 11440*a^3*b^7*c^7*d^3 + 5005*a^4*b^6*c^6*d^4 + 2002* \\ & a^5*b^5*c^5*d^5 + 715*a^6*b^4*c^4*d^6 + 220*a^7*b^3*c^3*d^7 + 55*a^8*b^2*c^2* \\ & d^8 + 10*a^9*b*c*d^9 + a^{10}*d^{10} + 167960*(10*b^{10}*c*d^9 + a*b^9*d^{10})*x^9 \\ & + 125970*(55*b^{10}*c^2*d^8 + 10*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 77520*(2 \\ & 20*b^{10}*c^3*d^7 + 55*a*b^9*c^2*d^8 + 10*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + \\ & 38760*(715*b^{10}*c^4*d^6 + 220*a*b^9*c^3*d^7 + 55*a^2*b^8*c^2*d^8 + 10*a^3* \\ & b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 15504*(2002*b^{10}*c^5*d^5 + 715*a*b^9*c^4*d^6 \\ & + 220*a^2*b^8*c^3*d^7 + 55*a^3*b^7*c^2*d^8 + 10*a^4*b^6*c*d^9 + a^5*b^5*d^{10})*x^5 \\ & + 4845*(5005*b^{10}*c^6*d^4 + 2002*a*b^9*c^5*d^5 + 715*a^2*b^8*c^4*d^6 \\ & + 220*a^3*b^7*c^3*d^7 + 55*a^4*b^6*c^2*d^8 + 10*a^5*b^5*c*d^9 + a^6*b^4*d^{10})*x^4 \\ & + 1140*(11440*b^{10}*c^7*d^3 + 5005*a*b^9*c^6*d^4 + 2002*a^2*b^8*c^5*d^5 + 715*a^3*b^7*c^4*d^6 \\ & + 220*a^4*b^6*c^3*d^7 + 55*a^5*b^5*c^2*d^8 + 10*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 \\ & + 190*(24310*b^{10}*c^8*d^2 + 11440*a*b^9*c^7*d^3 + 5005*a^2*b^8*c^6*d^4 + 2002*a^3*b^7*c^5*d^5 \\ & + 715*a^4*b^6*c^4*d^6 + 220*a^5*b^5*c^3*d^7 + 55*a^6*b^4*c^2*d^8 + 10*a^7*b^3*c*d^9 + a^8*b^2*d^{10})*x^2 \\ & + 20*(48620*b^{10}*c^9*d + 24310*a*b^9*c^8*d^2 + 11440*a^2*b^8*c^7*d^3 + 5005*a^3*b^7*c^6*d^4 \\ & + 2002*a^4*b^6*c^5*d^5 + 715*a^5*b^5*c^4*d^6 + 220*a^6*b^4*c^3*d^7 + 55*a^7*b^3*c^2*d^8 \\ & + 10*a^8*b^2*c*d^9 + a^9*b*d^{10})*x) / (\\ & b^{31}*x^{20} + 20*a*b^{30}*x^{19} + 190*a^2*b^{29}*x^{18} + 1140*a^3*b^{28}*x^{17} + 4845* \\ & a^4*b^{27}*x^{16} + 15504*a^5*b^{26}*x^{15} + 38760*a^6*b^{25}*x^{14} + 77520*a^7*b^{24}* \\ & x^{13} + 125970*a^8*b^{23}*x^{12} + 167960*a^9*b^{22}*x^{11} + 184756*a^{10}*b^{21}*x^{10} \\ & + 167960*a^{11}*b^{20}*x^9 + 125970*a^{12}*b^{19}*x^8 + 77520*a^{13}*b^{18}*x^7 + 38760* \\ & a^{14}*b^{17}*x^6 + 15504*a^{15}*b^{16}*x^5 + 4845*a^{16}*b^{15}*x^4 + 1140*a^{17}*b^{14}* \\ & x^3 + 190*a^{18}*b^{13}*x^2 + 20*a^{19}*b^{12}*x + a^{20}*b^{11}) \end{aligned}$$

mupad [B] time = 0.80, size = 1175, normalized size = 4.21

$$\frac{a^{10} d^{10} + 10 a^9 b c d^9 + 20 a^9 b d^{10} x + 55 a^8 b^2 c^2 d^8 + 200 a^8 b^2 c d^9 x + 190 a^8 b^2 d^{10} x^2 + 220 a^7 b^3 c^3 d^7 + 1100 a^7 b^3 c^2 d^8 + 1100 a^7 b^3 c d^9 x + 1100 a^7 b^3 d^{10} x^2 + 1100 a^6 b^4 c^4 d^6 + 1100 a^6 b^4 c^3 d^7 + 1100 a^6 b^4 c^2 d^8 + 1100 a^6 b^4 c d^9 x + 1100 a^6 b^4 d^{10} x^2 + 1100 a^5 b^5 c^5 d^5 + 1100 a^5 b^5 c^4 d^6 + 1100 a^5 b^5 c^3 d^7 + 1100 a^5 b^5 c^2 d^8 + 1100 a^5 b^5 c d^9 x + 1100 a^5 b^5 d^{10} x^2 + 1100 a^4 b^6 c^6 d^4 + 1100 a^4 b^6 c^5 d^5 + 1100 a^4 b^6 c^4 d^6 + 1100 a^4 b^6 c^3 d^7 + 1100 a^4 b^6 c^2 d^8 + 1100 a^4 b^6 c d^9 x + 1100 a^4 b^6 d^{10} x^2 + 1100 a^3 b^7 c^7 d^3 + 1100 a^3 b^7 c^6 d^4 + 1100 a^3 b^7 c^5 d^5 + 1100 a^3 b^7 c^4 d^6 + 1100 a^3 b^7 c^3 d^7 + 1100 a^3 b^7 c^2 d^8 + 1100 a^3 b^7 c d^9 x + 1100 a^3 b^7 d^{10} x^2 + 1100 a^2 b^8 c^8 d^2 + 1100 a^2 b^8 c^7 d^3 + 1100 a^2 b^8 c^6 d^4 + 1100 a^2 b^8 c^5 d^5 + 1100 a^2 b^8 c^4 d^6 + 1100 a^2 b^8 c^3 d^7 + 1100 a^2 b^8 c^2 d^8 + 1100 a^2 b^8 c d^9 x + 1100 a^2 b^8 d^{10} x^2 + 1100 a b^9 c^9 d + 1100 a b^9 c^8 d^2 + 1100 a b^9 c^7 d^3 + 1100 a b^9 c^6 d^4 + 1100 a b^9 c^5 d^5 + 1100 a b^9 c^4 d^6 + 1100 a b^9 c^3 d^7 + 1100 a b^9 c^2 d^8 + 1100 a b^9 c d^9 x + 1100 a b^9 d^{10} x^2 + 1100 a^9 b^{10} c^{10} + 1100 a^9 b^{10} c^9 d + 1100 a^9 b^{10} c^8 d^2 + 1100 a^9 b^{10} c^7 d^3 + 1100 a^9 b^{10} c^6 d^4 + 1100 a^9 b^{10} c^5 d^5 + 1100 a^9 b^{10} c^4 d^6 + 1100 a^9 b^{10} c^3 d^7 + 1100 a^9 b^{10} c^2 d^8 + 1100 a^9 b^{10} c d^9 x + 1100 a^9 b^{10} d^{10} x^2 + 1100 a^{10} b^{11} c^{11} + 1100 a^{10} b^{11} c^{10} d + 1100 a^{10} b^{11} c^9 d^2 + 1100 a^{10} b^{11} c^8 d^3 + 1100 a^{10} b^{11} c^7 d^4 + 1100 a^{10} b^{11} c^6 d^5 + 1100 a^{10} b^{11} c^5 d^6 + 1100 a^{10} b^{11} c^4 d^7 + 1100 a^{10} b^{11} c^3 d^8 + 1100 a^{10} b^{11} c^2 d^9 + 1100 a^{10} b^{11} c d^{10} + 1100 a^{10} b^{11} d^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^21,x)

[Out]
$$\begin{aligned} & -(a^{10}*d^{10} + 92378*b^{10}*c^{10} + 184756*b^{10}*d^{10}*x^{10} + 167960*a*b^9*d^{10}*x \\ & ^9 + 1679600*b^{10}*c*d^9*x^9 + 24310*a^2*b^8*c^8*d^2 + 11440*a^3*b^7*c^7*d^3 \\ & + 5005*a^4*b^6*c^6*d^4 + 2002*a^5*b^5*c^5*d^5 + 715*a^6*b^4*c^4*d^6 + 220* \\ & a^7*b^3*c^3*d^7 + 55*a^8*b^2*c^2*d^8 + 190*a^8*b^2*d^{10}*x^2 + 1140*a^7*b^3* \\ & d^{10}*x^3 + 4845*a^6*b^4*d^{10}*x^4 + 15504*a^5*b^5*d^{10}*x^5 + 38760*a^4*b^6*d^{10}*x^6 \\ & + 77520*a^3*b^7*d^{10}*x^7 + 125970*a^2*b^8*d^{10}*x^8 + 4618900*b^{10}*c^8*d^2*x^2 \\ & + 13041600*b^{10}*c^7*d^3*x^3 + 24249225*b^{10}*c^6*d^4*x^4 + 310390 \end{aligned}$$

$$\begin{aligned}
& 08*b^{10}*c^5*d^5*x^5 + 27713400*b^{10}*c^4*d^6*x^6 + 17054400*b^{10}*c^3*d^7*x^7 \\
& + 6928350*b^{10}*c^2*d^8*x^8 + 48620*a*b^9*c^9*d + 10*a^9*b*c*d^9 + 20*a^9*b \\
& *d^{10}*x + 972400*b^{10}*c^9*d*x + 950950*a^2*b^8*c^6*d^4*x^2 + 380380*a^3*b^7 \\
& *c^5*d^5*x^2 + 135850*a^4*b^6*c^4*d^6*x^2 + 41800*a^5*b^5*c^3*d^7*x^2 + 104 \\
& 50*a^6*b^4*c^2*d^8*x^2 + 2282280*a^2*b^8*c^5*d^5*x^3 + 815100*a^3*b^7*c^4*d \\
& ^6*x^3 + 250800*a^4*b^6*c^3*d^7*x^3 + 62700*a^5*b^5*c^2*d^8*x^3 + 3464175*a \\
& ^2*b^8*c^4*d^6*x^4 + 1065900*a^3*b^7*c^3*d^7*x^4 + 266475*a^4*b^6*c^2*d^8*x \\
& ^4 + 3410880*a^2*b^8*c^3*d^7*x^5 + 852720*a^3*b^7*c^2*d^8*x^5 + 2131800*a^2 \\
& *b^8*c^2*d^8*x^6 + 486200*a*b^9*c^8*d^2*x + 200*a^8*b^2*c*d^9*x + 1259700*a \\
& *b^9*c*d^9*x^8 + 228800*a^2*b^8*c^7*d^3*x + 100100*a^3*b^7*c^6*d^4*x + 4004 \\
& 0*a^4*b^6*c^5*d^5*x + 14300*a^5*b^5*c^4*d^6*x + 4400*a^6*b^4*c^3*d^7*x + 11 \\
& 00*a^7*b^3*c^2*d^8*x + 2173600*a*b^9*c^7*d^3*x^2 + 1900*a^7*b^3*c*d^9*x^2 + \\
& 5705700*a*b^9*c^6*d^4*x^3 + 11400*a^6*b^4*c*d^9*x^3 + 9699690*a*b^9*c^5*d^ \\
& 5*x^4 + 48450*a^5*b^5*c*d^9*x^4 + 11085360*a*b^9*c^4*d^6*x^5 + 155040*a^4*b \\
& ^6*c*d^9*x^5 + 8527200*a*b^9*c^3*d^7*x^6 + 387600*a^3*b^7*c*d^9*x^6 + 42636 \\
& 00*a*b^9*c^2*d^8*x^7 + 775200*a^2*b^8*c*d^9*x^7)/(1847560*a^20*b^11 + 18475 \\
& 60*b^31*x^20 + 36951200*a^19*b^12*x + 36951200*a*b^30*x^19 + 351036400*a^18 \\
& *b^13*x^2 + 2106218400*a^17*b^14*x^3 + 8951428200*a^16*b^15*x^4 + 286445702 \\
& 40*a^15*b^16*x^5 + 71611425600*a^14*b^17*x^6 + 143222851200*a^13*b^18*x^7 + \\
& 232737133200*a^12*b^19*x^8 + 310316177600*a^11*b^20*x^9 + 341347795360*a^1 \\
& 0*b^21*x^10 + 310316177600*a^9*b^22*x^11 + 232737133200*a^8*b^23*x^12 + 143 \\
& 222851200*a^7*b^24*x^13 + 71611425600*a^6*b^25*x^14 + 28644570240*a^5*b^26* \\
& x^15 + 8951428200*a^4*b^27*x^16 + 2106218400*a^3*b^28*x^17 + 351036400*a^2* \\
& b^29*x^18)
\end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**10/(b*x+a)**21,x)

[Out] Timed out

$$3.1333 \quad \int \frac{(c+dx)^{10}}{(a+bx)^{22}} dx$$

Optimal. Leaf size=279

$$\frac{5d^9(bc-ad)}{6b^{11}(a+bx)^{12}} - \frac{45d^8(bc-ad)^2}{13b^{11}(a+bx)^{13}} - \frac{60d^7(bc-ad)^3}{7b^{11}(a+bx)^{14}} - \frac{14d^6(bc-ad)^4}{b^{11}(a+bx)^{15}} - \frac{63d^5(bc-ad)^5}{4b^{11}(a+bx)^{16}} - \frac{210d^4(bc-ad)^6}{17b^{11}(a+bx)^{17}} - \frac{20d^3(bc-ad)^7}{3b^{11}(a+bx)^{18}} - \frac{63d^2(bc-ad)^8}{11b^{11}(a+bx)^{19}} - \frac{14d(bc-ad)^9}{2b^{11}(a+bx)^{20}} - \frac{d^2(bc-ad)^{10}}{b^{11}(a+bx)^{21}}$$

[Out] $-1/21*(-a*d+b*c)^{10}/b^{11}/(b*x+a)^{21}-1/2*d*(-a*d+b*c)^9/b^{11}/(b*x+a)^{20}-45/19*d^2*(-a*d+b*c)^8/b^{11}/(b*x+a)^{19}-20/3*d^3*(-a*d+b*c)^7/b^{11}/(b*x+a)^{18}-210/17*d^4*(-a*d+b*c)^6/b^{11}/(b*x+a)^{17}-63/4*d^5*(-a*d+b*c)^5/b^{11}/(b*x+a)^{16}-14*d^6*(-a*d+b*c)^4/b^{11}/(b*x+a)^{15}-60/7*d^7*(-a*d+b*c)^3/b^{11}/(b*x+a)^{14}-45/13*d^8*(-a*d+b*c)^2/b^{11}/(b*x+a)^{13}-5/6*d^9*(-a*d+b*c)/b^{11}/(b*x+a)^{12}-1/11*d^{10}/b^{11}/(b*x+a)^{11}$

Rubi [A] time = 0.27, antiderivative size = 279, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{5d^9(bc-ad)}{6b^{11}(a+bx)^{12}} - \frac{45d^8(bc-ad)^2}{13b^{11}(a+bx)^{13}} - \frac{60d^7(bc-ad)^3}{7b^{11}(a+bx)^{14}} - \frac{14d^6(bc-ad)^4}{b^{11}(a+bx)^{15}} - \frac{63d^5(bc-ad)^5}{4b^{11}(a+bx)^{16}} - \frac{210d^4(bc-ad)^6}{17b^{11}(a+bx)^{17}} - \frac{20d^3(bc-ad)^7}{3b^{11}(a+bx)^{18}} - \frac{63d^2(bc-ad)^8}{11b^{11}(a+bx)^{19}} - \frac{14d(bc-ad)^9}{2b^{11}(a+bx)^{20}} - \frac{d^2(bc-ad)^{10}}{b^{11}(a+bx)^{21}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^10/(a + b*x)^22,x]

[Out] $-(b*c - a*d)^{10}/(21*b^{11}*(a + b*x)^{21}) - (d*(b*c - a*d)^9)/(2*b^{11}*(a + b*x)^{20}) - (45*d^2*(b*c - a*d)^8)/(19*b^{11}*(a + b*x)^{19}) - (20*d^3*(b*c - a*d)^7)/(3*b^{11}*(a + b*x)^{18}) - (210*d^4*(b*c - a*d)^6)/(17*b^{11}*(a + b*x)^{17}) - (63*d^5*(b*c - a*d)^5)/(4*b^{11}*(a + b*x)^{16}) - (14*d^6*(b*c - a*d)^4)/(b^{11}*(a + b*x)^{15}) - (60*d^7*(b*c - a*d)^3)/(7*b^{11}*(a + b*x)^{14}) - (45*d^8*(b*c - a*d)^2)/(13*b^{11}*(a + b*x)^{13}) - (5*d^9*(b*c - a*d))/(6*b^{11}*(a + b*x)^{12}) - d^{10}/(11*b^{11}*(a + b*x)^{11})$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(c + dx)^{10}}{(a + bx)^{22}} dx = \int \left(\frac{(bc - ad)^{10}}{b^{10}(a + bx)^{22}} + \frac{10d(bc - ad)^9}{b^{10}(a + bx)^{21}} + \frac{45d^2(bc - ad)^8}{b^{10}(a + bx)^{20}} + \frac{120d^3(bc - ad)^7}{b^{10}(a + bx)^{19}} + \frac{210d^4(bc - ad)^6}{b^{10}(a + bx)^{18}} + \dots \right)$$

$$= -\frac{(bc - ad)^{10}}{21b^{11}(a + bx)^{21}} - \frac{d(bc - ad)^9}{2b^{11}(a + bx)^{20}} - \frac{45d^2(bc - ad)^8}{19b^{11}(a + bx)^{19}} - \frac{20d^3(bc - ad)^7}{3b^{11}(a + bx)^{18}} - \frac{210d^4(bc - ad)^6}{17b^{11}(a + bx)^{17}} - \dots$$

Mathematica [B] time = 0.30, size = 692, normalized size = 2.48

$$\frac{a^{10}d^{10} + a^9bd^9(11c + 21dx) + 3a^8b^2d^8(22c^2 + 77cdx + 70d^2x^2) + 2a^7b^3d^7(143c^3 + 693c^2dx + 1155cd^2x^2 + 600d^3x^3) + \dots}{(a + bx)^{21}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^10/(a + b*x)^22,x]

[Out]
$$\frac{-1/3879876(a^{10}d^{10} + a^9b^2d^9(11c + 21dx) + 3a^8b^3d^8(22c^2 + 77cdx + 70d^2x^2) + 2a^7b^4d^7(143c^3 + 693c^2dx + 1155cd^2x^2 + 665d^3x^3) + 7a^6b^5d^6(143c^4 + 858c^3dx + 1980c^2d^2x^2 + 2090cd^3x^3 + 855d^4x^4) + 21a^5b^6d^5(143c^5 + 1001c^4dx + 2860c^3d^2x^2 + 4180c^2d^3x^3 + 3135cd^4x^4 + 969d^5x^5) + 7a^4b^7d^4(1144c^6 + 9009c^5dx + 30030c^4d^2x^2 + 54340c^3d^3x^3 + 56430c^2d^4x^4 + 31977cd^5x^5 + 7752d^6x^6) + 2a^3b^8d^3(9724c^7 + 84084c^6dx + 315315c^5d^2x^2 + 665665c^4d^3x^3 + 855855c^3d^4x^4 + 671517c^2d^5x^5 + 298452cd^6x^6 + 58140d^7x^7) + 3a^2b^9d^2(14586c^8 + 136136c^7dx + 560560c^6d^2x^2 + 1331330c^5d^3x^3 + 1996995c^4d^4x^4 + 1939938c^3d^5x^5 + 1193808c^2d^6x^6 + 426360cd^7x^7 + 67830d^8x^8) + ab^9d(92378c^9 + 918918c^8dx + 4084080c^7d^2x^2 + 10650640c^6d^3x^3 + 17972955c^5d^4x^4 + 20369349c^4d^5x^5 + 15519504c^3d^6x^6 + 7674480c^2d^7x^7 + 2238390cd^8x^8 + 293930d^9x^9) + b^{10}(184756c^{10} + 1939938c^9dx + 9189180c^8d^2x^2 + 25865840c^7d^3x^3 + 47927880c^6d^4x^4 + 61108047c^5d^5x^5 + 54318264c^4d^6x^6 + 33256080c^3d^7x^7 + 13430340c^2d^8x^8 + 3233230cd^9x^9 + 352716d^{10}x^{10})}{(b^{11}(a + b*x)^{21})}$$

fricas [B] time = 0.46, size = 1085, normalized size = 3.89

$$\frac{352716 b^{10} d^{10} x^{10} + 184756 b^{10} c^{10} + 92378 a b^9 c^9 d + 43758 a^2 b^8 c^8 d^2 + 19448 a^3 b^7 c^7 d^3 + 8008 a^4 b^6 c^6 d^4 + 3000 a^5 b^5 c^5 d^5 + \dots}{(b^{11}(a + b*x)^{21})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^22,x, algorithm="fricas")

```
[Out] -1/3879876*(352716*b^10*d^10*x^10 + 184756*b^10*c^10 + 92378*a*b^9*c^9*d +
43758*a^2*b^8*c^8*d^2 + 19448*a^3*b^7*c^7*d^3 + 8008*a^4*b^6*c^6*d^4 + 3003
*a^5*b^5*c^5*d^5 + 1001*a^6*b^4*c^4*d^6 + 286*a^7*b^3*c^3*d^7 + 66*a^8*b^2*
c^2*d^8 + 11*a^9*b*c*d^9 + a^10*d^10 + 293930*(11*b^10*c*d^9 + a*b^9*d^10)*
x^9 + 203490*(66*b^10*c^2*d^8 + 11*a*b^9*c*d^9 + a^2*b^8*d^10)*x^8 + 116280
*(286*b^10*c^3*d^7 + 66*a*b^9*c^2*d^8 + 11*a^2*b^8*c*d^9 + a^3*b^7*d^10)*x^
7 + 54264*(1001*b^10*c^4*d^6 + 286*a*b^9*c^3*d^7 + 66*a^2*b^8*c^2*d^8 + 11*
a^3*b^7*c*d^9 + a^4*b^6*d^10)*x^6 + 20349*(3003*b^10*c^5*d^5 + 1001*a*b^9*c
^4*d^6 + 286*a^2*b^8*c^3*d^7 + 66*a^3*b^7*c^2*d^8 + 11*a^4*b^6*c*d^9 + a^5*
b^5*d^10)*x^5 + 5985*(8008*b^10*c^6*d^4 + 3003*a*b^9*c^5*d^5 + 1001*a^2*b^8
*c^4*d^6 + 286*a^3*b^7*c^3*d^7 + 66*a^4*b^6*c^2*d^8 + 11*a^5*b^5*c*d^9 + a^
6*b^4*d^10)*x^4 + 1330*(19448*b^10*c^7*d^3 + 8008*a*b^9*c^6*d^4 + 3003*a^2*
b^8*c^5*d^5 + 1001*a^3*b^7*c^4*d^6 + 286*a^4*b^6*c^3*d^7 + 66*a^5*b^5*c^2*d
^8 + 11*a^6*b^4*c*d^9 + a^7*b^3*d^10)*x^3 + 210*(43758*b^10*c^8*d^2 + 19448
*a*b^9*c^7*d^3 + 8008*a^2*b^8*c^6*d^4 + 3003*a^3*b^7*c^5*d^5 + 1001*a^4*b^6
*c^4*d^6 + 286*a^5*b^5*c^3*d^7 + 66*a^6*b^4*c^2*d^8 + 11*a^7*b^3*c*d^9 + a^
8*b^2*d^10)*x^2 + 21*(92378*b^10*c^9*d + 43758*a*b^9*c^8*d^2 + 19448*a^2*b^
8*c^7*d^3 + 8008*a^3*b^7*c^6*d^4 + 3003*a^4*b^6*c^5*d^5 + 1001*a^5*b^5*c^4*
d^6 + 286*a^6*b^4*c^3*d^7 + 66*a^7*b^3*c^2*d^8 + 11*a^8*b^2*c*d^9 + a^9*b*d
^10)*x)/(b^32*x^21 + 21*a*b^31*x^20 + 210*a^2*b^30*x^19 + 1330*a^3*b^29*x^1
8 + 5985*a^4*b^28*x^17 + 20349*a^5*b^27*x^16 + 54264*a^6*b^26*x^15 + 116280
*a^7*b^25*x^14 + 203490*a^8*b^24*x^13 + 293930*a^9*b^23*x^12 + 352716*a^10*
b^22*x^11 + 352716*a^11*b^21*x^10 + 293930*a^12*b^20*x^9 + 203490*a^13*b^19
*x^8 + 116280*a^14*b^18*x^7 + 54264*a^15*b^17*x^6 + 20349*a^16*b^16*x^5 + 5
985*a^17*b^15*x^4 + 1330*a^18*b^14*x^3 + 210*a^19*b^13*x^2 + 21*a^20*b^12*x
+ a^21*b^11)
```

giac [B] time = 1.30, size = 961, normalized size = 3.44

$$\frac{352716 b^{10} d^{10} x^{10} + 3233230 b^{10} c d^9 x^9 + 293930 a b^9 d^{10} x^9 + 13430340 b^{10} c^2 d^8 x^8 + 2238390 a b^9 c d^9 x^8 + 203490 a^2 b^8 d^{10} x^8 + 33256080 b^{10} c^3 d^7 x^7 + 7674480 a b^9 c^2 d^8 x^7 + 1279080 a^2 b^8 c d^9 x^7 + 116280 a^3 b^7 d^{10} x^7 + 54318264 b^{10} c^4 d^6 x^6 + 15519504 a b^9 c^3 d^7 x^6 + 3581424 a^2 b^8 c^2 d^8 x^6 + 596904 a^3 b^7 c d^9 x^6 + 54264 a^4 b^6 d^{10} x^6 + 61108047 b^{10} c^5 d^5 x^5 + 20369349 a b^9 c^4 d^6 x^5 + 5819814 a^2 b^8 c^3 d^7 x^5 + 1343034 a^3 b^7 c^2 d^8 x^5 + 223839 a^4 b^6 c d^9 x^5 + 20349 a^5 b^5 d^{10} x^5 + 47927880 b^{10} c^6 d^4 x^4 + 17972955 a b^9 c^5 d^5 x^4 + 5990985 a^2 b^8 c^4 d^6 x^4 + 17117$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^10/(b*x+a)^22,x, algorithm="giac")
```

```
[Out] -1/3879876*(352716*b^10*d^10*x^10 + 3233230*b^10*c*d^9*x^9 + 293930*a*b^9*d
^10*x^9 + 13430340*b^10*c^2*d^8*x^8 + 2238390*a*b^9*c*d^9*x^8 + 203490*a^2*
b^8*d^10*x^8 + 33256080*b^10*c^3*d^7*x^7 + 7674480*a*b^9*c^2*d^8*x^7 + 1279
080*a^2*b^8*c*d^9*x^7 + 116280*a^3*b^7*d^10*x^7 + 54318264*b^10*c^4*d^6*x^6
+ 15519504*a*b^9*c^3*d^7*x^6 + 3581424*a^2*b^8*c^2*d^8*x^6 + 596904*a^3*b^
7*c*d^9*x^6 + 54264*a^4*b^6*d^10*x^6 + 61108047*b^10*c^5*d^5*x^5 + 20369349
*a*b^9*c^4*d^6*x^5 + 5819814*a^2*b^8*c^3*d^7*x^5 + 1343034*a^3*b^7*c^2*d^8*
x^5 + 223839*a^4*b^6*c*d^9*x^5 + 20349*a^5*b^5*d^10*x^5 + 47927880*b^10*c^6
*d^4*x^4 + 17972955*a*b^9*c^5*d^5*x^4 + 5990985*a^2*b^8*c^4*d^6*x^4 + 17117
```

$10a^3b^7c^3d^7x^4 + 395010a^4b^6c^2d^8x^4 + 65835a^5b^5c^3d^9x^4 + 5985a^6b^4d^{10}x^4 + 25865840b^{10}c^7d^3x^3 + 10650640a^9c^6d^4x^3 + 3993990a^2b^8c^5d^5x^3 + 1331330a^3b^7c^4d^6x^3 + 380380a^4b^6c^3d^7x^3 + 87780a^5b^5c^2d^8x^3 + 14630a^6b^4c^3d^9x^3 + 1330a^7b^3d^{10}x^3 + 9189180b^{10}c^8d^2x^2 + 4084080a^9c^7d^3x^2 + 1681680a^2b^8c^6d^4x^2 + 630630a^3b^7c^5d^5x^2 + 210210a^4b^6c^4d^6x^2 + 60060a^5b^5c^3d^7x^2 + 13860a^6b^4c^2d^8x^2 + 2310a^7b^3c^2d^9x^2 + 210a^8b^2d^{10}x^2 + 1939938b^{10}c^9dx + 918918a^9c^8d^2x + 408408a^2b^8c^7d^3x + 168168a^3b^7c^6d^4x + 63063a^4b^6c^5d^5x + 21021a^5b^5c^4d^6x + 6006a^6b^4c^3d^7x + 1386a^7b^3c^2d^8x + 231a^8b^2c^2d^9x + 21a^9b^2d^{10}x + 184756b^{10}c^{10} + 92378a^9c^9d + 43758a^2b^8c^8d^2 + 19448a^3b^7c^7d^3 + 8008a^4b^6c^6d^4 + 3003a^5b^5c^5d^5 + 1001a^6b^4c^4d^6 + 286a^7b^3c^3d^7 + 66a^8b^2c^2d^8 + 11a^9b^2c^2d^9 + a^{10}d^{10}) / ((bx + a)^{21}b^{11})$

maple [B] time = 0.01, size = 867, normalized size = 3.11

$$-\frac{d^{10}}{11(bx+a)^{11}b^{11}} + \frac{5(ad-bc)d^9}{6(bx+a)^{12}b^{11}} - \frac{45(a^2d^2-2abcd+b^2c^2)d^8}{13(bx+a)^{13}b^{11}} + \frac{60(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)d^7}{7(bx+a)^{14}b^{11}} - \frac{14(a^4d^4-4a^3bcd^3+6a^2b^2c^2d^2-4ab^3c^3d+b^4c^4)}{7(bx+a)^{15}b^{11}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^10/(b*x+a)^22,x)

[Out] $-45/13d^8(a^2d^2-2abc^2d+b^2c^2)/b^{11}/(bx+a)^{13}+1/2d*(a^9d^9-9a^8b^8c^8d+36a^7b^7c^7d^2-84a^6b^6c^6d^3+126a^5b^5c^5d^4-126a^4b^4c^4d^5-126a^3b^3c^3d^6+84a^2b^2c^2d^7-84a^2b^7c^7d^2+9a^9b^8c^8d-b^9c^9)/b^{11}/(bx+a)^{20}-1/21*(a^{10}d^{10}-10a^9b^8c^8d^9+45a^8b^7c^7d^8-120a^7b^6c^6d^7+210a^6b^5c^5d^6-252a^5b^4c^4d^5+210a^4b^3c^3d^4-120a^3b^2c^2d^3+45a^2b^2c^2d^8-10a^2b^8c^8d^2-10a^9b^8c^8d+b^{10}c^{10})/b^{11}/(bx+a)^{21}-210/17d^4*(a^6d^6-6a^5b^5c^5d^5+15a^4b^4c^4d^4-20a^3b^3c^3d^3+15a^2b^2c^2d^2-6a^2b^5c^5d+b^6c^6)/b^{11}/(bx+a)^{17}-1/11*d^{10}/b^{11}/(bx+a)^{11}-14d^6*(a^4d^4-4a^3b^3c^3d^3+6a^2b^2c^2d^2-4a^2b^3c^3d+b^4c^4)/b^{11}/(bx+a)^{15}+5/6*d^9*(a*d-b*c)/b^{11}/(bx+a)^{12}+20/3*d^3*(a^7d^7-7a^6b^6c^6d^6+21a^5b^5c^5d^5-35a^4b^4c^4d^4+35a^3b^3c^3d^3-21a^2b^2c^2d^2+7a^2b^6c^6d-b^7c^7)/b^{11}/(bx+a)^{18}-45/19*d^2*(a^8d^8-8a^7b^7c^7d^7+28a^6b^6c^6d^6-56a^5b^5c^5d^5+70a^4b^4c^4d^4-56a^3b^3c^3d^3+28a^2b^2c^2d^2-8a^2b^7c^7d+b^8c^8)/b^{11}/(bx+a)^{19}+60/7*d^7*(a^3d^3-3a^2b^2c^2d^2+3a^2b^2c^2d-b^3c^3)/b^{11}/(bx+a)^{14}+63/4*d^5*(a^5d^5-5a^4b^4c^4d^4+10a^3b^3c^3d^3-10a^2b^3c^3d^2+5a^2b^4c^4d-b^5c^5)/b^{11}/(bx+a)^{16}$

maxima [B] time = 2.46, size = 1085, normalized size = 3.89

$$352716 b^{10} d^{10} x^{10} + 184756 b^{10} c^{10} + 92378 a b^9 c^9 d + 43758 a^2 b^8 c^8 d^2 + 19448 a^3 b^7 c^7 d^3 + 8008 a^4 b^6 c^6 d^4 + 3003$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^10/(b*x+a)^22,x, algorithm="maxima")

[Out]
$$\begin{aligned} & -1/3879876*(352716*b^{10}*d^{10}*x^{10} + 184756*b^{10}*c^{10} + 92378*a*b^9*c^9*d + \\ & 43758*a^2*b^8*c^8*d^2 + 19448*a^3*b^7*c^7*d^3 + 8008*a^4*b^6*c^6*d^4 + 3003 \\ & *a^5*b^5*c^5*d^5 + 1001*a^6*b^4*c^4*d^6 + 286*a^7*b^3*c^3*d^7 + 66*a^8*b^2*c^2*d^8 + 11*a^9*b*c*d^9 + a^{10}*d^{10} + 293930*(11*b^{10}*c*d^9 + a*b^9*d^{10})* \\ & x^9 + 203490*(66*b^{10}*c^2*d^8 + 11*a*b^9*c*d^9 + a^2*b^8*d^{10})*x^8 + 116280 \\ & *(286*b^{10}*c^3*d^7 + 66*a*b^9*c^2*d^8 + 11*a^2*b^8*c*d^9 + a^3*b^7*d^{10})*x^7 + 54264*(1001*b^{10}*c^4*d^6 + 286*a*b^9*c^3*d^7 + 66*a^2*b^8*c^2*d^8 + 11* \\ & a^3*b^7*c*d^9 + a^4*b^6*d^{10})*x^6 + 20349*(3003*b^{10}*c^5*d^5 + 1001*a*b^9*c^4*d^6 + 286*a^2*b^8*c^3*d^7 + 66*a^3*b^7*c^2*d^8 + 11*a^4*b^6*c*d^9 + a^5* \\ & b^5*d^{10})*x^5 + 5985*(8008*b^{10}*c^6*d^4 + 3003*a*b^9*c^5*d^5 + 1001*a^2*b^8*c^4*d^6 + 286*a^3*b^7*c^3*d^7 + 66*a^4*b^6*c^2*d^8 + 11*a^5*b^5*c*d^9 + a^6* \\ & b^4*d^{10})*x^4 + 1330*(19448*b^{10}*c^7*d^3 + 8008*a*b^9*c^6*d^4 + 3003*a^2*b^8*c^5*d^5 + 1001*a^3*b^7*c^4*d^6 + 286*a^4*b^6*c^3*d^7 + 66*a^5*b^5*c^2*d^8 + 11*a^6*b^4*c*d^9 + a^7*b^3*d^{10})*x^3 + 210*(43758*b^{10}*c^8*d^2 + 19448 \\ & *a*b^9*c^7*d^3 + 8008*a^2*b^8*c^6*d^4 + 3003*a^3*b^7*c^5*d^5 + 1001*a^4*b^6*c^4*d^6 + 286*a^5*b^5*c^3*d^7 + 66*a^6*b^4*c^2*d^8 + 11*a^7*b^3*c*d^9 + a^8* \\ & b^2*d^{10})*x^2 + 21*(92378*b^{10}*c^9*d + 43758*a*b^9*c^8*d^2 + 19448*a^2*b^8*c^7*d^3 + 8008*a^3*b^7*c^6*d^4 + 3003*a^4*b^6*c^5*d^5 + 1001*a^5*b^5*c^4*d^6 + 286*a^6*b^4*c^3*d^7 + 66*a^7*b^3*c^2*d^8 + 11*a^8*b^2*c*d^9 + a^9*b*d^{10})*x \\ & + 352716*a^{10}*d^{10} + 184756*a^{11}*c^{10} + 92378*a^{12}*b^9*c^9*d + 43758*a^{13}*b^8*c^8*d^2 + 19448*a^{14}*b^7*c^7*d^3 + 8008*a^{15}*b^6*c^6*d^4 + 3003*a^{16}*b^5*c^5*d^5 + 1001*a^{17}*b^4*c^4*d^6 + 286*a^{18}*b^3*c^3*d^7 + 66*a^{19}*b^2*c^2*d^8 + 11*a^{20}*b*c*d^9 + a^{21}*d^{10})/(b^{32}*x^{21} + 21*a*b^{31}*x^{20} + 210*a^2*b^{30}*x^{19} + 1330*a^3*b^{29}*x^{18} + 5985*a^4*b^{28}*x^{17} + 20349*a^5*b^{27}*x^{16} + 54264*a^6*b^{26}*x^{15} + 116280*a^7*b^{25}*x^{14} + 203490*a^8*b^{24}*x^{13} + 293930*a^9*b^{23}*x^{12} + 352716*a^{10}*b^{22}*x^{11} + 352716*a^{11}*b^{21}*x^{10} + 293930*a^{12}*b^{20}*x^9 + 203490*a^{13}*b^{19}*x^8 + 116280*a^{14}*b^{18}*x^7 + 54264*a^{15}*b^{17}*x^6 + 20349*a^{16}*b^{16}*x^5 + 5985*a^{17}*b^{15}*x^4 + 1330*a^{18}*b^{14}*x^3 + 210*a^{19}*b^{13}*x^2 + 21*a^{20}*b^{12}*x + a^{21}*b^{11}) \end{aligned}$$

mupad [B] time = 1.04, size = 1186, normalized size = 4.25

$$a^{10} d^{10} + 11 a^9 b c d^9 + 21 a^9 b d^{10} x + 66 a^8 b^2 c^2 d^8 + 231 a^8 b^2 c d^9 x + 210 a^8 b^2 d^{10} x^2 + 286 a^7 b^3 c^3 d^7 + 1386 a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^10/(a + b*x)^22,x)


```
[Out] -(a^10*d^10 + 184756*b^10*c^10 + 352716*b^10*d^10*x^10 + 293930*a*b^9*d^10*x^9 + 3233230*b^10*c*d^9*x^9 + 43758*a^2*b^8*c^8*d^2 + 19448*a^3*b^7*c^7*d^3 + 8008*a^4*b^6*c^6*d^4 + 3003*a^5*b^5*c^5*d^5 + 1001*a^6*b^4*c^4*d^6 + 286*a^7*b^3*c^3*d^7 + 66*a^8*b^2*c^2*d^8 + 210*a^8*b^2*d^10*x^2 + 1330*a^7*b^3*d^10*x^3 + 5985*a^6*b^4*d^10*x^4 + 20349*a^5*b^5*d^10*x^5 + 54264*a^4*b^6*d^10*x^6 + 116280*a^3*b^7*d^10*x^7 + 203490*a^2*b^8*d^10*x^8 + 9189180*b^10*c^8*d^2*x^2 + 25865840*b^10*c^7*d^3*x^3 + 47927880*b^10*c^6*d^4*x^4 + 61108047*b^10*c^5*d^5*x^5 + 54318264*b^10*c^4*d^6*x^6 + 33256080*b^10*c^3*d^7*x^7 + 13430340*b^10*c^2*d^8*x^8 + 92378*a*b^9*c^9*d + 11*a^9*b*c*d^9 + 21*a^9*b*d^10*x + 1939938*b^10*c^9*d*x + 1681680*a^2*b^8*c^6*d^4*x^2 + 630630*a^3*b^7*c^5*d^5*x^2 + 210210*a^4*b^6*c^4*d^6*x^2 + 60060*a^5*b^5*c^3*d^7*x^2 + 13860*a^6*b^4*c^2*d^8*x^2 + 3993990*a^2*b^8*c^5*d^5*x^3 + 1331330*a^3*b^7*c^4*d^6*x^3 + 380380*a^4*b^6*c^3*d^7*x^3 + 87780*a^5*b^5*c^2*d^8*x^3 + 5990985*a^2*b^8*c^4*d^6*x^4 + 1711710*a^3*b^7*c^3*d^7*x^4 + 395010*a^4*b^6*c^2*d^8*x^4 + 5819814*a^2*b^8*c^3*d^7*x^5 + 1343034*a^3*b^7*c^2*d^8*x^5 + 3581424*a^2*b^8*c^2*d^8*x^6 + 918918*a*b^9*c^8*d^2*x + 231*a^8*b^2*c*d^9*x + 2238390*a*b^9*c*d^9*x^8 + 408408*a^2*b^8*c^7*d^3*x + 168168*a^3*b^7*c^6*d^4*x + 63063*a^4*b^6*c^5*d^5*x + 21021*a^5*b^5*c^4*d^6*x + 6006*a^6*b^4*c^3*d^7*x + 1386*a^7*b^3*c^2*d^8*x + 4084080*a*b^9*c^7*d^3*x^2 + 2310*a^7*b^3*c*d^9*x^2 + 10650640*a*b^9*c^6*d^4*x^3 + 14630*a^6*b^4*c*d^9*x^3 + 17972955*a*b^9*c^5*d^5*x^4 + 65835*a^5*b^5*c*d^9*x^4 + 20369349*a*b^9*c^4*d^6*x^5 + 223839*a^4*b^6*c*d^9*x^5 + 15519504*a*b^9*c^3*d^7*x^6 + 596904*a^3*b^7*c*d^9*x^6 + 7674480*a*b^9*c^2*d^8*x^7 + 1279080*a^2*b^8*c*d^9*x^7)/(3879876*a^21*b^11 + 3879876*b^32*x^21 + 81477396*a^20*b^12*x + 81477396*a*b^31*x^20 + 814773960*a^19*b^13*x^2 + 5160235080*a^18*b^14*x^3 + 23221057860*a^17*b^15*x^4 + 78951596724*a^16*b^16*x^5 + 210537591264*a^15*b^17*x^6 + 451151981280*a^14*b^18*x^7 + 789515967240*a^13*b^19*x^8 + 1140411952680*a^12*b^20*x^9 + 1368494343216*a^11*b^21*x^10 + 1368494343216*a^10*b^22*x^11 + 1140411952680*a^9*b^23*x^12 + 789515967240*a^8*b^24*x^13 + 451151981280*a^7*b^25*x^14 + 210537591264*a^6*b^26*x^15 + 78951596724*a^5*b^27*x^16 + 23221057860*a^4*b^28*x^17 + 5160235080*a^3*b^29*x^18 + 814773960*a^2*b^30*x^19)
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**10/(b*x+a)**22,x)
```

```
[Out] Timed out
```

$$3.1334 \quad \int \frac{(a+bx)^5}{c+dx} dx$$

Optimal. Leaf size=122

$$-\frac{(bc-ad)^5 \log(c+dx)}{d^6} + \frac{bx(bc-ad)^4}{d^5} - \frac{(a+bx)^2(bc-ad)^3}{2d^4} + \frac{(a+bx)^3(bc-ad)^2}{3d^3} - \frac{(a+bx)^4(bc-ad)}{4d^2} + \frac{(a+bx)^5}{5d}$$

[Out] b*(-a*d+b*c)^4*x/d^5-1/2*(-a*d+b*c)^3*(b*x+a)^2/d^4+1/3*(-a*d+b*c)^2*(b*x+a)^3/d^3-1/4*(-a*d+b*c)*(b*x+a)^4/d^2+1/5*(b*x+a)^5/d-(-a*d+b*c)^5*ln(d*x+c)/d^6

Rubi [A] time = 0.05, antiderivative size = 122, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{bx(bc-ad)^4}{d^5} - \frac{(a+bx)^2(bc-ad)^3}{2d^4} + \frac{(a+bx)^3(bc-ad)^2}{3d^3} - \frac{(a+bx)^4(bc-ad)}{4d^2} - \frac{(bc-ad)^5 \log(c+dx)}{d^6} + \frac{(a+bx)^5}{5d}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(c + d*x), x]

[Out] (b*(b*c - a*d)^4*x)/d^5 - ((b*c - a*d)^3*(a + b*x)^2)/(2*d^4) + ((b*c - a*d)^2*(a + b*x)^3)/(3*d^3) - ((b*c - a*d)*(a + b*x)^4)/(4*d^2) + (a + b*x)^5/(5*d) - ((b*c - a*d)^5*Log[c + d*x])/d^6

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{c+dx} dx &= \int \left(\frac{b(bc-ad)^4}{d^5} - \frac{b(bc-ad)^3(a+bx)}{d^4} + \frac{b(bc-ad)^2(a+bx)^2}{d^3} - \frac{b(bc-ad)(a+bx)^3}{d^2} + \frac{b(a+bx)^4}{d} \right. \\ &= \frac{b(bc-ad)^4 x}{d^5} - \frac{(bc-ad)^3(a+bx)^2}{2d^4} + \frac{(bc-ad)^2(a+bx)^3}{3d^3} - \frac{(bc-ad)(a+bx)^4}{4d^2} + \frac{(a+bx)^5}{5d} - \frac{(bc-ad)^5 \log(c+dx)}{d^6} \end{aligned}$$

Mathematica [A] time = 0.07, size = 167, normalized size = 1.37

$$\frac{bdx(300a^4d^4 + 300a^3bd^3(dx - 2c) + 100a^2b^2d^2(6c^2 - 3cdx + 2d^2x^2) + 25ab^3d(-12c^3 + 6c^2dx - 4cd^2x^2 + 3d^3x^3))}{60d^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(c + d*x),x]

[Out] (b*d*x*(300*a^4*d^4 + 300*a^3*b*d^3*(-2*c + d*x) + 100*a^2*b^2*d^2*(6*c^2 - 3*c*d*x + 2*d^2*x^2) + 25*a*b^3*d*(-12*c^3 + 6*c^2*d*x - 4*c*d^2*x^2 + 3*d^3*x^3) + b^4*(60*c^4 - 30*c^3*d*x + 20*c^2*d^2*x^2 - 15*c*d^3*x^3 + 12*d^4*x^4)) - 60*(b*c - a*d)^5*Log[c + d*x])/(60*d^6)

fricas [B] time = 0.44, size = 259, normalized size = 2.12

$$\frac{12 b^5 d^5 x^5 - 15 (b^5 c d^4 - 5 a b^4 d^5) x^4 + 20 (b^5 c^2 d^3 - 5 a b^4 c d^4 + 10 a^2 b^3 d^5) x^3 - 30 (b^5 c^3 d^2 - 5 a b^4 c^2 d^3 + 10 a^2 b^3 c d^4 - 5 a^3 b^2 d^5) x^2 + 60 (b^5 c^4 d - 5 a b^4 c^3 d^2 + 10 a^2 b^3 c^2 d^3 - 10 a^3 b^2 c d^4 + 5 a^4 b c d^5) x - 60 (b^5 c^5 - 5 a b^4 c^4 d + 10 a^2 b^3 c^3 d^2 - 10 a^3 b^2 c^2 d^3 + 5 a^4 b c d^4 - a^5 d^5) \log(d x + c)}{60 d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c),x, algorithm="fricas")

[Out] 1/60*(12*b^5*d^5*x^5 - 15*(b^5*c*d^4 - 5*a*b^4*d^5)*x^4 + 20*(b^5*c^2*d^3 - 5*a*b^4*c*d^4 + 10*a^2*b^3*d^5)*x^3 - 30*(b^5*c^3*d^2 - 5*a*b^4*c^2*d^3 + 10*a^2*b^3*c*d^4 - 10*a^3*b^2*d^5)*x^2 + 60*(b^5*c^4*d - 5*a*b^4*c^3*d^2 + 10*a^2*b^3*c^2*d^3 - 10*a^3*b^2*c*d^4 + 5*a^4*b*d^5)*x - 60*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)*log(d*x + c))/d^6

giac [B] time = 1.26, size = 273, normalized size = 2.24

$$\frac{12 b^5 d^4 x^5 - 15 b^5 c d^3 x^4 + 75 a b^4 d^4 x^4 + 20 b^5 c^2 d^2 x^3 - 100 a b^4 c d^3 x^3 + 200 a^2 b^3 d^4 x^3 - 30 b^5 c^3 d x^2 + 150 a b^4 c^2 d^2 x^2 - 300 a^2 b^3 c^2 d x^2 - 300 a^3 b^2 c d^3 x^2 + 600 a^2 b^3 c^2 d^2 x^2 - 600 a^3 b^2 c d^3 x^2 + 300 a^4 b c d^4 x^2}{60 d^5} - (b^5 c^5 - 5 a b^4 c^4 d + 10 a^2 b^3 c^3 d^2 - 10 a^3 b^2 c^2 d^3 + 5 a^4 b c d^4 - a^5 d^5) \log(\text{abs}(d x + c)) / d^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c),x, algorithm="giac")

[Out] 1/60*(12*b^5*d^4*x^5 - 15*b^5*c*d^3*x^4 + 75*a*b^4*d^4*x^4 + 20*b^5*c^2*d^2*x^3 - 100*a*b^4*c*d^3*x^3 + 200*a^2*b^3*d^4*x^3 - 30*b^5*c^3*d*x^2 + 150*a*b^4*c^2*d^2*x^2 - 300*a^2*b^3*c*d^3*x^2 + 300*a^3*b^2*d^4*x^2 + 60*b^5*c^4*x - 300*a*b^4*c^3*d*x + 600*a^2*b^3*c^2*d^2*x - 600*a^3*b^2*c*d^3*x + 300*a^4*b*d^4*x)/d^5 - (b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)*log(abs(d*x + c))/d^6

maple [B] time = 0.00, size = 302, normalized size = 2.48

$$\frac{b^5 x^5}{5d} + \frac{5a b^4 x^4}{4d} - \frac{b^5 c x^4}{4d^2} + \frac{10a^2 b^3 x^3}{3d} - \frac{5a b^4 c x^3}{3d^2} + \frac{b^5 c^2 x^3}{3d^3} + \frac{5a^3 b^2 x^2}{d} - \frac{5a^2 b^3 c x^2}{d^2} + \frac{5a b^4 c^2 x^2}{2d^3} - \frac{b^5 c^3 x^2}{2d^4} + \frac{a^5 \ln(dx + c)}{d} - \frac{(b^5 c^5 - 5 a b^4 c^4 d + 10 a^2 b^3 c^3 d^2 - 10 a^3 b^2 c^2 d^3 + 5 a^4 b c d^4 - a^5 d^5) \log(\text{abs}(d x + c))}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^5/(d*x+c),x)`

[Out] $\frac{1}{5}b^5/d^5x^5 + \frac{5}{4}b^4/d^4x^4 + \frac{1}{4}b^5/d^2x^4c + \frac{10}{3}b^3/d^3x^3a^2 - \frac{5}{3}b^4/d^2x^3ac + \frac{1}{3}b^5/d^3x^3c^2 + 5b^2/d^2x^2a^3 - 5b^3/d^2x^2a^2c + 5/2b^4/d^3x^2ac^2 - 1/2b^5/d^4x^2c^3 + 5b/d^4ax - 10b^2/d^2a^3cx + 10b^3/d^3a^2c^2x - 5b^4/d^4ac^3x + b^5/d^5c^4x + 1/d \ln(d*x+c) * a^5 - 5/d^2 \ln(d*x+c) * a^4 * b * c + 10/d^3 \ln(d*x+c) * a^3 * b^2 * c^2 - 10/d^4 \ln(d*x+c) * a^2 * b^3 * c^3 + 5/d^5 \ln(d*x+c) * a * b^4 * c^4 - 1/d^6 \ln(d*x+c) * b^5 * c^5$

maxima [B] time = 1.35, size = 258, normalized size = 2.11

$$\frac{12b^5d^4x^5 - 15(b^5cd^3 - 5ab^4d^4)x^4 + 20(b^5c^2d^2 - 5ab^4cd^3 + 10a^2b^3d^4)x^3 - 30(b^5c^3d - 5ab^4c^2d^2 + 10a^2b^3cd^3 - 5a^3b^4c^2d^2 + 10a^2b^3c^2d^3 - 10a^3b^2c^2d^4)x^2 + 60(b^5c^4 - 5a^4b^4c^3d + 10a^2b^3c^2d^2 - 10a^3b^2c^2d^3 + 5a^4b^4c^3d^4)x - (b^5c^5 - 5a^4b^4c^4d + 10a^2b^3c^3d^2 - 10a^3b^2c^2d^3 + 5a^4b^4c^3d^4 - a^5d^5) \log(d*x + c)}{60d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5/(d*x+c),x, algorithm="maxima")`

[Out] $\frac{1}{60} * (12b^5d^4x^5 - 15(b^5cd^3 - 5a^4b^4d^4)x^4 + 20(b^5c^2d^2 - 5a^4b^4c^3d + 10a^2b^3c^2d^2 - 10a^3b^2c^2d^3 + 5a^4b^4c^3d^4)x^3 - 30(b^5c^3d - 5a^4b^4c^2d^2 + 10a^2b^3c^2d^3 - 10a^3b^2c^2d^4)x^2 + 60(b^5c^4 - 5a^4b^4c^3d + 10a^2b^3c^2d^2 - 10a^3b^2c^2d^3 + 5a^4b^4c^3d^4)x - (b^5c^5 - 5a^4b^4c^4d + 10a^2b^3c^3d^2 - 10a^3b^2c^2d^3 + 5a^4b^4c^3d^4 - a^5d^5) \log(d*x + c)) / d^6$

mupad [B] time = 0.07, size = 280, normalized size = 2.30

$$x \left(\frac{5a^4b}{d} - \frac{c \left(\frac{10a^3b^2}{d} + \frac{c \left(\frac{5ab^4}{d} - \frac{b^5c}{d^2} \right) - \frac{10a^2b^3}{d}}{d} \right)}{d} \right) + x^4 \left(\frac{5ab^4}{4d} - \frac{b^5c}{4d^2} \right) + x^2 \left(\frac{5a^3b^2}{d} + \frac{c \left(\frac{5ab^4}{d} - \frac{b^5c}{d^2} \right) - \frac{10a^2b^3}{d}}{2d} \right) - x^3 \left(\dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(c + d*x),x)`

[Out] $x^5 * ((5a^4b)/d - (c * ((10a^3b^2)/d + (c * ((c * ((5ab^4)/d - (b^5c)/d^2)) / d - (10a^2b^3)/d)) / d)) / d) + x^4 * ((5a^4b^4)/(4d) - (b^5c)/(4d^2)) + x^2 * ((5a^3b^2)/d + (c * ((c * ((5ab^4)/d - (b^5c)/d^2)) / d - (10a^2b^3)/d)) / (2d)) - x^3 * ((c * ((5ab^4)/d - (b^5c)/d^2)) / (3d) - (10a^2b^3)/(3d)) + \dots$

$$\frac{(b^5 x^5)/(5d) + (\log(c + dx)(a^5 d^5 - b^5 c^5 - 10a^2 b^3 c^3 d^2 + 10a^3 b^2 c^2 d^3 + 5a^4 b^4 c^4 d - 5a^4 b^4 c^4 d - 5a^4 b^4 c^4 d))}{d^6}$$

sympy [B] time = 0.50, size = 209, normalized size = 1.71

$$\frac{b^5 x^5}{5d} + x^4 \left(\frac{5ab^4}{4d} - \frac{b^5 c}{4d^2} \right) + x^3 \left(\frac{10a^2 b^3}{3d} - \frac{5ab^4 c}{3d^2} + \frac{b^5 c^2}{3d^3} \right) + x^2 \left(\frac{5a^3 b^2}{d} - \frac{5a^2 b^3 c}{d^2} + \frac{5ab^4 c^2}{2d^3} - \frac{b^5 c^3}{2d^4} \right) + x \left(\frac{5a^4 b}{d} - \frac{10a^3 b^2}{d^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/(d*x+c), x)

[Out] b**5*x**5/(5*d) + x**4*(5*a*b**4/(4*d) - b**5*c/(4*d**2)) + x**3*(10*a**2*b**3/(3*d) - 5*a*b**4*c/(3*d**2) + b**5*c**2/(3*d**3)) + x**2*(5*a**3*b**2/d - 5*a**2*b**3*c/d**2 + 5*a*b**4*c**2/(2*d**3) - b**5*c**3/(2*d**4)) + x*(5*a**4*b/d - 10*a**3*b**2*c/d**2 + 10*a**2*b**3*c**2/d**3 - 5*a*b**4*c**3/d**4 + b**5*c**4/d**5) + (a*d - b*c)**5*log(c + d*x)/d**6

$$3.1335 \quad \int \frac{(a+bx)^4}{c+dx} dx$$

Optimal. Leaf size=98

$$\frac{(bc-ad)^4 \log(c+dx)}{d^5} - \frac{bx(bc-ad)^3}{d^4} + \frac{(a+bx)^2(bc-ad)^2}{2d^3} - \frac{(a+bx)^3(bc-ad)}{3d^2} + \frac{(a+bx)^4}{4d}$$

[Out] $-b*(-a*d+b*c)^3*x/d^4+1/2*(-a*d+b*c)^2*(b*x+a)^2/d^3-1/3*(-a*d+b*c)*(b*x+a)^3/d^2+1/4*(b*x+a)^4/d+(-a*d+b*c)^4*\ln(d*x+c)/d^5$

Rubi [A] time = 0.04, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{bx(bc-ad)^3}{d^4} + \frac{(a+bx)^2(bc-ad)^2}{2d^3} - \frac{(a+bx)^3(bc-ad)}{3d^2} + \frac{(bc-ad)^4 \log(c+dx)}{d^5} + \frac{(a+bx)^4}{4d}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4/(c + d*x), x]

[Out] $-((b*(b*c - a*d)^3*x)/d^4) + ((b*c - a*d)^2*(a + b*x)^2)/(2*d^3) - ((b*c - a*d)*(a + b*x)^3)/(3*d^2) + (a + b*x)^4/(4*d) + ((b*c - a*d)^4*\text{Log}[c + d*x])/d^5$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^4}{c+dx} dx = \int \left(-\frac{b(bc-ad)^3}{d^4} + \frac{b(bc-ad)^2(a+bx)}{d^3} - \frac{b(bc-ad)(a+bx)^2}{d^2} + \frac{b(a+bx)^3}{d} + \frac{(-bc+ad)^4}{d^4(c+dx)} \right) dx$$

$$= -\frac{b(bc-ad)^3x}{d^4} + \frac{(bc-ad)^2(a+bx)^2}{2d^3} - \frac{(bc-ad)(a+bx)^3}{3d^2} + \frac{(a+bx)^4}{4d} + \frac{(bc-ad)^4 \log(c+dx)}{d^5}$$

Mathematica [A] time = 0.04, size = 115, normalized size = 1.17

$$\frac{bdx(48a^3d^3 + 36a^2bd^2(dx - 2c) + 8ab^2d(6c^2 - 3cdx + 2d^2x^2) + b^3(-12c^3 + 6c^2dx - 4cd^2x^2 + 3d^3x^3)) + 12(bc - ad)^4 \log(c + dx)}{12d^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4/(c + d*x), x]

[Out] (b*d*x*(48*a^3*d^3 + 36*a^2*b*d^2*(-2*c + d*x) + 8*a*b^2*d*(6*c^2 - 3*c*d*x + 2*d^2*x^2) + b^3*(-12*c^3 + 6*c^2*d*x - 4*c*d^2*x^2 + 3*d^3*x^3)) + 12*(b*c - a*d)^4*Log[c + d*x])/(12*d^5)

fricas [A] time = 0.45, size = 179, normalized size = 1.83

$$\frac{3b^4d^4x^4 - 4(b^4cd^3 - 4ab^3d^4)x^3 + 6(b^4c^2d^2 - 4ab^3cd^3 + 6a^2b^2d^4)x^2 - 12(b^4c^3d - 4ab^3c^2d^2 + 6a^2b^2cd^3 - 4a^3b^2c^2d^2 - 4a^3b^2c^2d^2 + a^4d^4)\log(c + d*x)}{12d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c), x, algorithm="fricas")

[Out] 1/12*(3*b^4*d^4*x^4 - 4*(b^4*c*d^3 - 4*a*b^3*d^4)*x^3 + 6*(b^4*c^2*d^2 - 4*a*b^3*c*d^3 + 6*a^2*b^2*d^4)*x^2 - 12*(b^4*c^3*d - 4*a*b^3*c^2*d^2 + 6*a^2*b^2*c*d^3 - 4*a^3*b*d^4)*x + 12*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*log(d*x + c))/d^5

giac [A] time = 1.23, size = 184, normalized size = 1.88

$$\frac{3b^4d^3x^4 - 4b^4cd^2x^3 + 16ab^3d^3x^3 + 6b^4c^2dx^2 - 24ab^3cd^2x^2 + 36a^2b^2d^3x^2 - 12b^4c^3x + 48ab^3c^2dx - 72a^2b^2cd^3}{12d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c), x, algorithm="giac")

[Out] 1/12*(3*b^4*d^3*x^4 - 4*b^4*c*d^2*x^3 + 16*a*b^3*d^3*x^3 + 6*b^4*c^2*d*x^2 - 24*a*b^3*c*d^2*x^2 + 36*a^2*b^2*d^3*x^2 - 12*b^4*c^3*x + 48*a*b^3*c^2*d*x - 72*a^2*b^2*c*d^2*x + 48*a^3*b*d^3*x)/d^4 + (b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*log(abs(d*x + c))/d^5

maple [B] time = 0.00, size = 209, normalized size = 2.13

$$\frac{b^4x^4}{4d} + \frac{4ab^3x^3}{3d} - \frac{b^4cx^3}{3d^2} + \frac{3a^2b^2x^2}{d} - \frac{2ab^3cx^2}{d^2} + \frac{b^4c^2x^2}{2d^3} + \frac{a^4 \ln(dx + c)}{d} - \frac{4a^3bc \ln(dx + c)}{d^2} + \frac{4a^3bx}{d} + \frac{6a^2b^2c^2 \ln(dx + c)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4/(d*x+c), x)

[Out] 1/4*b^4/d*x^4+4/3*b^3/d*x^3*a-1/3*b^4/d^2*x^3*c+3*b^2/d*x^2*a^2-2*b^3/d^2*x^2*a*c+1/2*b^4/d^3*x^2*c^2+4*b/d*a^3*x-6*b^2/d^2*a^2*c*x+4*b^3/d^3*a*c^2*x-

$b^4/d^4*c^3*x+1/d*\ln(d*x+c)*a^4-4/d^2*\ln(d*x+c)*a^3*b*c+6/d^3*\ln(d*x+c)*a^2$
 $*b^2*c^2-4/d^4*\ln(d*x+c)*a*b^3*c^3+1/d^5*\ln(d*x+c)*b^4*c^4$

maxima [A] time = 1.41, size = 177, normalized size = 1.81

$$\frac{3b^4d^3x^4 - 4(b^4cd^2 - 4ab^3d^3)x^3 + 6(b^4c^2d - 4ab^3cd^2 + 6a^2b^2d^3)x^2 - 12(b^4c^3 - 4ab^3c^2d + 6a^2b^2cd^2 - 4a^3bd^3)}{12d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c),x, algorithm="maxima")

[Out] $1/12*(3*b^4*d^3*x^4 - 4*(b^4*c*d^2 - 4*a*b^3*d^3)*x^3 + 6*(b^4*c^2*d - 4*a*b^3*c*d^2 + 6*a^2*b^2*d^3)*x^2 - 12*(b^4*c^3 - 4*a*b^3*c^2*d + 6*a^2*b^2*c*d^2 - 4*a^3*b*d^3)*x)/d^4 + (b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*\log(d*x + c)/d^5$

mupad [B] time = 0.22, size = 189, normalized size = 1.93

$$x^3 \left(\frac{4ab^3}{3d} - \frac{b^4c}{3d^2} \right) + x \left(\frac{4a^3b}{d} + \frac{c \left(\frac{4ab^3}{d} - \frac{b^4c}{d^2} \right) - \frac{6a^2b^2}{d}}{d} \right) - x^2 \left(\frac{c \left(\frac{4ab^3}{d} - \frac{b^4c}{d^2} \right) - \frac{3a^2b^2}{d}}{2d} \right) + \frac{\ln(c + dx) (a^4d^4 - 4a^3bd^3)}{d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^4/(c + d*x),x)

[Out] $x^3*((4*a*b^3)/(3*d) - (b^4*c)/(3*d^2)) + x*((4*a^3*b)/d + (c*((c*((4*a*b^3)/d - (b^4*c)/d^2))/d - (6*a^2*b^2)/d))/d - x^2*((c*((4*a*b^3)/d - (b^4*c)/d^2))/(2*d) - (3*a^2*b^2)/d) + (\log(c + d*x)*(a^4*d^4 + b^4*c^4 + 6*a^2*b^2*c^2*d^2 - 4*a*b^3*c^3*d - 4*a^3*b*c*d^3))/d^5 + (b^4*x^4)/(4*d)$

sympy [A] time = 0.39, size = 136, normalized size = 1.39

$$\frac{b^4x^4}{4d} + x^3 \left(\frac{4ab^3}{3d} - \frac{b^4c}{3d^2} \right) + x^2 \left(\frac{3a^2b^2}{d} - \frac{2ab^3c}{d^2} + \frac{b^4c^2}{2d^3} \right) + x \left(\frac{4a^3b}{d} - \frac{6a^2b^2c}{d^2} + \frac{4ab^3c^2}{d^3} - \frac{b^4c^3}{d^4} \right) + \frac{(ad - bc)^4 \log(c + dx)}{d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4/(d*x+c),x)

[Out] $b**4*x**4/(4*d) + x**3*(4*a*b**3/(3*d) - b**4*c/(3*d**2)) + x**2*(3*a**2*b**2/d - 2*a*b**3*c/d**2 + b**4*c**2/(2*d**3)) + x*(4*a**3*b/d - 6*a**2*b**2*c/d**2 + 4*a*b**3*c**2/d**3 - b**4*c**3/d**4) + (a*d - b*c)**4*log(c + d*x)/d**5$

$$3.1336 \quad \int \frac{(a+bx)^3}{c+dx} dx$$

Optimal. Leaf size=74

$$-\frac{(bc-ad)^3 \log(c+dx)}{d^4} + \frac{bx(bc-ad)^2}{d^3} - \frac{(a+bx)^2(bc-ad)}{2d^2} + \frac{(a+bx)^3}{3d}$$

[Out] $b*(-a*d+b*c)^2*x/d^3-1/2*(-a*d+b*c)*(b*x+a)^2/d^2+1/3*(b*x+a)^3/d-(-a*d+b*c)^3*\ln(d*x+c)/d^4$

Rubi [A] time = 0.03, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{bx(bc-ad)^2}{d^3} - \frac{(a+bx)^2(bc-ad)}{2d^2} - \frac{(bc-ad)^3 \log(c+dx)}{d^4} + \frac{(a+bx)^3}{3d}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/(c + d*x), x]

[Out] $(b*(b*c - a*d)^2*x)/d^3 - ((b*c - a*d)*(a + b*x)^2)/(2*d^2) + (a + b*x)^3/(3*d) - ((b*c - a*d)^3*\text{Log}[c + d*x])/d^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{c+dx} dx &= \int \left(\frac{b(bc-ad)^2}{d^3} - \frac{b(bc-ad)(a+bx)}{d^2} + \frac{b(a+bx)^2}{d} + \frac{(-bc+ad)^3}{d^3(c+dx)} \right) dx \\ &= \frac{b(bc-ad)^2x}{d^3} - \frac{(bc-ad)(a+bx)^2}{2d^2} + \frac{(a+bx)^3}{3d} - \frac{(bc-ad)^3 \log(c+dx)}{d^4} \end{aligned}$$

Mathematica [A] time = 0.03, size = 74, normalized size = 1.00

$$\frac{bdx(18a^2d^2 + 9abd(dx - 2c) + b^2(6c^2 - 3cdx + 2d^2x^2)) - 6(bc - ad)^3 \log(c + dx)}{6d^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/(c + d*x), x]

[Out] (b*d*x*(18*a^2*d^2 + 9*a*b*d*(-2*c + d*x) + b^2*(6*c^2 - 3*c*d*x + 2*d^2*x^2)) - 6*(b*c - a*d)^3*Log[c + d*x])/(6*d^4)

fricas [A] time = 0.43, size = 115, normalized size = 1.55

$$\frac{2b^3d^3x^3 - 3(b^3cd^2 - 3ab^2d^3)x^2 + 6(b^3c^2d - 3ab^2cd^2 + 3a^2bd^3)x - 6(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3) \log(dx + c)}{6d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c), x, algorithm="fricas")

[Out] 1/6*(2*b^3*d^3*x^3 - 3*(b^3*c*d^2 - 3*a*b^2*d^3)*x^2 + 6*(b^3*c^2*d - 3*a*b^2*c*d^2 + 3*a^2*b*d^3)*x - 6*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*log(d*x + c))/d^4

giac [A] time = 1.20, size = 116, normalized size = 1.57

$$\frac{2b^3d^2x^3 - 3b^3cdx^2 + 9ab^2d^2x^2 + 6b^3c^2x - 18ab^2cdx + 18a^2bd^2x}{6d^3} - \frac{(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3) \log(|dx + c|)}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c), x, algorithm="giac")

[Out] 1/6*(2*b^3*d^2*x^3 - 3*b^3*c*d*x^2 + 9*a*b^2*d^2*x^2 + 6*b^3*c^2*x - 18*a*b^2*c*d*x + 18*a^2*b*d^2*x)/d^3 - (b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*log(abs(dx + c))/d^4

maple [A] time = 0.00, size = 133, normalized size = 1.80

$$\frac{b^3x^3}{3d} + \frac{3ab^2x^2}{2d} - \frac{b^3cx^2}{2d^2} + \frac{a^3 \ln(dx + c)}{d} - \frac{3a^2bc \ln(dx + c)}{d^2} + \frac{3a^2bx}{d} + \frac{3ab^2c^2 \ln(dx + c)}{d^3} - \frac{3ab^2cx}{d^2} - \frac{b^3c^3 \ln(dx + c)}{d^4} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/(d*x+c), x)

[Out] 1/3*b^3/d*x^3+3/2*b^2/d*x^2*a-1/2*b^3/d^2*x^2*c+3*b/d*a^2*x-3*b^2/d^2*a*c*x+b^3/d^3*c^2*x+1/d*ln(d*x+c)*a^3-3/d^2*ln(d*x+c)*a^2*b*c+3/d^3*ln(d*x+c)*a*b^2*c^2-1/d^4*ln(d*x+c)*b^3*c^3

maxima [A] time = 1.30, size = 114, normalized size = 1.54

$$\frac{2b^3d^2x^3 - 3(b^3cd - 3ab^2d^2)x^2 + 6(b^3c^2 - 3ab^2cd + 3a^2bd^2)x}{6d^3} - \frac{(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3) \log(dx + c)}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c),x, algorithm="maxima")

[Out] $\frac{1}{6}*(2*b^3*d^2*x^3 - 3*(b^3*c*d - 3*a*b^2*d^2)*x^2 + 6*(b^3*c^2 - 3*a*b^2*c*d + 3*a^2*b*d^2)*x)/d^3 - (b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*\log(d*x + c)/d^4$

mupad [B] time = 0.07, size = 118, normalized size = 1.59

$$x^2 \left(\frac{3ab^2}{2d} - \frac{b^3c}{2d^2} \right) + x \left(\frac{3a^2b}{d} - \frac{c \left(\frac{3ab^2}{d} - \frac{b^3c}{d^2} \right)}{d} \right) + \frac{\ln(c + dx) (a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)}{d^4} + \frac{b^3x^3}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3/(c + d*x),x)

[Out] $x^2*((3*a*b^2)/(2*d) - (b^3*c)/(2*d^2)) + x*((3*a^2*b)/d - (c*((3*a*b^2)/d - (b^3*c)/d^2))/d + (\log(c + d*x)*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2))/d^4 + (b^3*x^3)/(3*d)$

sympy [A] time = 0.30, size = 83, normalized size = 1.12

$$\frac{b^3x^3}{3d} + x^2 \left(\frac{3ab^2}{2d} - \frac{b^3c}{2d^2} \right) + x \left(\frac{3a^2b}{d} - \frac{3ab^2c}{d^2} + \frac{b^3c^2}{d^3} \right) + \frac{(ad - bc)^3 \log(c + dx)}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3/(d*x+c),x)

[Out] $b**3*x**3/(3*d) + x**2*(3*a*b**2/(2*d) - b**3*c/(2*d**2)) + x*(3*a**2*b/d - 3*a*b**2*c/d**2 + b**3*c**2/d**3) + (a*d - b*c)**3*log(c + d*x)/d**4$

$$3.1337 \quad \int \frac{(a+bx)^2}{c+dx} dx$$

Optimal. Leaf size=50

$$\frac{(bc-ad)^2 \log(c+dx)}{d^3} - \frac{bx(bc-ad)}{d^2} + \frac{(a+bx)^2}{2d}$$

[Out] $-b*(-a*d+b*c)*x/d^2+1/2*(b*x+a)^2/d+(-a*d+b*c)^2*\ln(d*x+c)/d^3$

Rubi [A] time = 0.02, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{bx(bc-ad)}{d^2} + \frac{(bc-ad)^2 \log(c+dx)}{d^3} + \frac{(a+bx)^2}{2d}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(c + d*x), x]

[Out] $-((b*(b*c - a*d)*x)/d^2) + (a + b*x)^2/(2*d) + ((b*c - a*d)^2*\text{Log}[c + d*x])/d^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{c+dx} dx &= \int \left(-\frac{b(bc-ad)}{d^2} + \frac{b(a+bx)}{d} + \frac{(-bc+ad)^2}{d^2(c+dx)} \right) dx \\ &= -\frac{b(bc-ad)x}{d^2} + \frac{(a+bx)^2}{2d} + \frac{(bc-ad)^2 \log(c+dx)}{d^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 43, normalized size = 0.86

$$\frac{bdx(4ad - 2bc + bdx) + 2(bc - ad)^2 \log(c + dx)}{2d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(c + d*x),x]

[Out] (b*d*x*(-2*b*c + 4*a*d + b*d*x) + 2*(b*c - a*d)^2*Log[c + d*x])/(2*d^3)

fricas [A] time = 0.43, size = 62, normalized size = 1.24

$$\frac{b^2 d^2 x^2 - 2(b^2 c d - 2 a b d^2) x + 2(b^2 c^2 - 2 a b c d + a^2 d^2) \log(dx + c)}{2 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c),x, algorithm="fricas")

[Out] 1/2*(b^2*d^2*x^2 - 2*(b^2*c*d - 2*a*b*d^2)*x + 2*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*log(d*x + c))/d^3

giac [A] time = 1.21, size = 60, normalized size = 1.20

$$\frac{b^2 d x^2 - 2 b^2 c x + 4 a b d x}{2 d^2} + \frac{(b^2 c^2 - 2 a b c d + a^2 d^2) \log(|d x + c|)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c),x, algorithm="giac")

[Out] 1/2*(b^2*d*x^2 - 2*b^2*c*x + 4*a*b*d*x)/d^2 + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*log(abs(d*x + c))/d^3

maple [A] time = 0.00, size = 74, normalized size = 1.48

$$\frac{b^2 x^2}{2d} + \frac{a^2 \ln(dx + c)}{d} - \frac{2abc \ln(dx + c)}{d^2} + \frac{2abx}{d} + \frac{b^2 c^2 \ln(dx + c)}{d^3} - \frac{b^2 cx}{d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(d*x+c),x)

[Out] 1/2*b^2/d*x^2+2*b/d*a*x-b^2/d^2*x*c+1/d*ln(d*x+c)*a^2-2/d^2*ln(d*x+c)*a*b*c+1/d^3*ln(d*x+c)*b^2*c^2

maxima [A] time = 1.35, size = 60, normalized size = 1.20

$$\frac{b^2 d x^2 - 2(b^2 c - 2 a b d) x}{2 d^2} + \frac{(b^2 c^2 - 2 a b c d + a^2 d^2) \log(dx + c)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c),x, algorithm="maxima")

[Out] $\frac{1}{2}(b^2 d x^2 - 2(b^2 c - 2 a b d) x) / d^2 + (b^2 c^2 - 2 a b c d + a^2 d^2) \log(d x + c) / d^3$

mupad [B] time = 0.22, size = 62, normalized size = 1.24

$$\frac{\ln(c + dx) (a^2 d^2 - 2 a b c d + b^2 c^2)}{d^3} - x \left(\frac{b^2 c}{d^2} - \frac{2 a b}{d} \right) + \frac{b^2 x^2}{2 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2/(c + d*x), x)`

[Out] $(\log(c + dx) (a^2 d^2 + b^2 c^2 - 2 a b c d)) / d^3 - x((b^2 c) / d^2 - (2 a b) / d) + (b^2 x^2) / (2 d)$

sympy [A] time = 0.22, size = 44, normalized size = 0.88

$$\frac{b^2 x^2}{2 d} + x \left(\frac{2 a b}{d} - \frac{b^2 c}{d^2} \right) + \frac{(a d - b c)^2 \log(c + dx)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2/(d*x+c), x)`

[Out] $b**2*x**2/(2*d) + x*(2*a*b/d - b**2*c/d**2) + (a*d - b*c)**2*log(c + d*x)/d**3$

$$3.1338 \quad \int \frac{a+bx}{c+dx} dx$$

Optimal. Leaf size=26

$$\frac{bx}{d} - \frac{(bc - ad) \log(c + dx)}{d^2}$$

[Out] b*x/d - (-a*d+b*c)*ln(d*x+c)/d^2

Rubi [A] time = 0.02, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{bx}{d} - \frac{(bc - ad) \log(c + dx)}{d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(c + d*x), x]

[Out] (b*x)/d - ((b*c - a*d)*Log[c + d*x])/d^2

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{c+dx} dx &= \int \left(\frac{b}{d} + \frac{-bc+ad}{d(c+dx)} \right) dx \\ &= \frac{bx}{d} - \frac{(bc-ad) \log(c+dx)}{d^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 0.96

$$\frac{(ad - bc) \log(c + dx)}{d^2} + \frac{bx}{d}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(c + d*x), x]

[Out] (b*x)/d + ((-b*c) + a*d)*Log[c + d*x])/d^2

fricas [A] time = 0.48, size = 25, normalized size = 0.96

$$\frac{bdx - (bc - ad) \log(dx + c)}{d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c),x, algorithm="fricas")

[Out] (b*d*x - (b*c - a*d)*log(d*x + c))/d^2

giac [A] time = 1.20, size = 27, normalized size = 1.04

$$\frac{bx}{d} - \frac{(bc - ad) \log(|dx + c|)}{d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c),x, algorithm="giac")

[Out] b*x/d - (b*c - a*d)*log(abs(d*x + c))/d^2

maple [A] time = 0.00, size = 32, normalized size = 1.23

$$\frac{a \ln(dx + c)}{d} - \frac{bc \ln(dx + c)}{d^2} + \frac{bx}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/(d*x+c),x)

[Out] b*x/d+1/d*ln(d*x+c)*a-1/d^2*ln(d*x+c)*b*c

maxima [A] time = 1.32, size = 26, normalized size = 1.00

$$\frac{bx}{d} - \frac{(bc - ad) \log(dx + c)}{d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c),x, algorithm="maxima")

[Out] b*x/d - (b*c - a*d)*log(d*x + c)/d^2

mupad [B] time = 0.20, size = 25, normalized size = 0.96

$$\frac{\ln(c + dx) (ad - bc)}{d^2} + \frac{bx}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)/(c + d*x),x)
```

```
[Out] (log(c + d*x)*(a*d - b*c))/d^2 + (b*x)/d
```

```
sympy [A] time = 0.15, size = 20, normalized size = 0.77
```

$$\frac{bx}{d} + \frac{(ad - bc) \log(c + dx)}{d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)/(d*x+c),x)
```

```
[Out] b*x/d + (a*d - b*c)*log(c + d*x)/d**2
```

$$3.1339 \quad \int \frac{1}{c+dx} dx$$

Optimal. Leaf size=10

$$\frac{\log(c + dx)}{d}$$

[Out] ln(d*x+c)/d

Rubi [A] time = 0.00, antiderivative size = 10, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {31}

$$\frac{\log(c + dx)}{d}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(-1), x]

[Out] Log[c + d*x]/d

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] :> Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \frac{1}{c + dx} dx = \frac{\log(c + dx)}{d}$$

Mathematica [A] time = 0.00, size = 10, normalized size = 1.00

$$\frac{\log(c + dx)}{d}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(-1), x]

[Out] Log[c + d*x]/d

fricas [A] time = 0.42, size = 10, normalized size = 1.00

$$\frac{\log(dx + c)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c),x, algorithm="fricas")

[Out] log(d*x + c)/d

giac [A] time = 1.26, size = 11, normalized size = 1.10

$$\frac{\log(|dx + c|)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c),x, algorithm="giac")

[Out] log(abs(d*x + c))/d

maple [A] time = 0.00, size = 11, normalized size = 1.10

$$\frac{\ln(dx + c)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c),x)

[Out] ln(d*x+c)/d

maxima [A] time = 1.30, size = 10, normalized size = 1.00

$$\frac{\log(dx + c)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c),x, algorithm="maxima")

[Out] log(d*x + c)/d

mupad [B] time = 0.02, size = 10, normalized size = 1.00

$$\frac{\ln(c + dx)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c + d*x),x)

[Out] log(c + d*x)/d

sympy [A] time = 0.06, size = 7, normalized size = 0.70

$$\frac{\log(c + dx)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c),x)

[Out] log(c + d*x)/d

$$3.1340 \quad \int \frac{1}{(a+bx)(c+dx)} dx$$

Optimal. Leaf size=36

$$\frac{\log(a+bx)}{bc-ad} - \frac{\log(c+dx)}{bc-ad}$$

[Out] $\ln(b*x+a)/(-a*d+b*c) - \ln(d*x+c)/(-a*d+b*c)$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {36, 31}

$$\frac{\log(a+bx)}{bc-ad} - \frac{\log(c+dx)}{bc-ad}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)*(c + d*x)), x]$

[Out] $\text{Log}[a + b*x]/(b*c - a*d) - \text{Log}[c + d*x]/(b*c - a*d)$

Rule 31

$\text{Int}[(a + b*x)^{-1}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] /; \text{FreeQ}\{a, b\}, x]$

Rule 36

$\text{Int}[1/((a + b*x)*(c + d*x)), x_Symbol] \rightarrow \text{Dist}[b/(b*c - a*d), \text{Int}[1/(a + b*x), x], x] - \text{Dist}[d/(b*c - a*d), \text{Int}[1/(c + d*x), x], x] /; \text{FreeQ}\{a, b, c, d\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0]$

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)(c+dx)} dx &= \frac{b \int \frac{1}{a+bx} dx}{bc-ad} - \frac{d \int \frac{1}{c+dx} dx}{bc-ad} \\ &= \frac{\log(a+bx)}{bc-ad} - \frac{\log(c+dx)}{bc-ad} \end{aligned}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 0.72

$$\frac{\log(a+bx) - \log(c+dx)}{bc-ad}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*(c + d*x)),x]

[Out] (Log[a + b*x] - Log[c + d*x])/(b*c - a*d)

fricas [A] time = 0.45, size = 26, normalized size = 0.72

$$\frac{\log(bx + a) - \log(dx + c)}{bc - ad}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c),x, algorithm="fricas")

[Out] (log(b*x + a) - log(d*x + c))/(b*c - a*d)

giac [A] time = 1.24, size = 46, normalized size = 1.28

$$\frac{b \log(|bx + a|)}{b^2c - abd} - \frac{d \log(|dx + c|)}{bcd - ad^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c),x, algorithm="giac")

[Out] b*log(abs(b*x + a))/(b^2*c - a*b*d) - d*log(abs(d*x + c))/(b*c*d - a*d^2)

maple [A] time = 0.01, size = 37, normalized size = 1.03

$$-\frac{\ln(bx + a)}{ad - bc} + \frac{\ln(dx + c)}{ad - bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)/(d*x+c),x)

[Out] 1/(a*d-b*c)*ln(d*x+c)-1/(a*d-b*c)*ln(b*x+a)

maxima [A] time = 1.36, size = 36, normalized size = 1.00

$$\frac{\log(bx + a)}{bc - ad} - \frac{\log(dx + c)}{bc - ad}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c),x, algorithm="maxima")

[Out] log(b*x + a)/(b*c - a*d) - log(d*x + c)/(b*c - a*d)

mupad [B] time = 0.26, size = 25, normalized size = 0.69

$$\frac{\ln\left(\frac{c+dx}{a+bx}\right)}{ad-bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)*(c + d*x)),x)

[Out] log((c + d*x)/(a + b*x))/(a*d - b*c)

sympy [B] time = 0.33, size = 128, normalized size = 3.56

$$\frac{\log\left(x + \frac{-\frac{a^2d^2}{ad-bc} + \frac{2abcd}{ad-bc} + ad - \frac{b^2c^2}{ad-bc} + bc}{2bd}\right)}{ad-bc} - \frac{\log\left(x + \frac{\frac{a^2d^2}{ad-bc} - \frac{2abcd}{ad-bc} + ad + \frac{b^2c^2}{ad-bc} + bc}{2bd}\right)}{ad-bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c),x)

[Out] log(x + (-a**2*d**2/(a*d - b*c) + 2*a*b*c*d/(a*d - b*c) + a*d - b**2*c**2/(a*d - b*c) + b*c)/(2*b*d))/(a*d - b*c) - log(x + (a**2*d**2/(a*d - b*c) - 2*a*b*c*d/(a*d - b*c) + a*d + b**2*c**2/(a*d - b*c) + b*c)/(2*b*d))/(a*d - b*c)

$$3.1341 \quad \int \frac{1}{(a+bx)^2(c+dx)} dx$$

Optimal. Leaf size=57

$$-\frac{1}{(a+bx)(bc-ad)} - \frac{d \log(a+bx)}{(bc-ad)^2} + \frac{d \log(c+dx)}{(bc-ad)^2}$$

[Out] $-1/(-a*d+b*c)/(b*x+a)-d*\ln(b*x+a)/(-a*d+b*c)^2+d*\ln(d*x+c)/(-a*d+b*c)^2$

Rubi [A] time = 0.03, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$-\frac{1}{(a+bx)(bc-ad)} - \frac{d \log(a+bx)}{(bc-ad)^2} + \frac{d \log(c+dx)}{(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^2*(c + d*x)),x]

[Out] $-(1/((b*c - a*d)*(a + b*x))) - (d*\text{Log}[a + b*x])/(b*c - a*d)^2 + (d*\text{Log}[c + d*x])/(b*c - a*d)^2$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{(a+bx)^2(c+dx)} dx = \int \left(\frac{b}{(bc-ad)(a+bx)^2} - \frac{bd}{(bc-ad)^2(a+bx)} + \frac{d^2}{(bc-ad)^2(c+dx)} \right) dx$$

$$= -\frac{1}{(bc-ad)(a+bx)} - \frac{d \log(a+bx)}{(bc-ad)^2} + \frac{d \log(c+dx)}{(bc-ad)^2}$$

Mathematica [A] time = 0.02, size = 53, normalized size = 0.93

$$\frac{d(a+bx) \log(c+dx) - d(a+bx) \log(a+bx) + ad - bc}{(a+bx)(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*(c + d*x)),x]

[Out] $(-(b*c) + a*d - d*(a + b*x)*\text{Log}[a + b*x] + d*(a + b*x)*\text{Log}[c + d*x])/((b*c - a*d)^2*(a + b*x))$

fricas [A] time = 0.46, size = 93, normalized size = 1.63

$$-\frac{bc - ad + (bdx + ad) \log (bx + a) - (bdx + ad) \log (dx + c)}{ab^2c^2 - 2a^2bcd + a^3d^2 + (b^3c^2 - 2ab^2cd + a^2bd^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c),x, algorithm="fricas")

[Out] $-(b*c - a*d + (b*d*x + a*d)*\log(b*x + a) - (b*d*x + a*d)*\log(d*x + c))/(a*b^2*c^2 - 2*a^2*b*c*d + a^3*d^2 + (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*x)$

giac [A] time = 1.32, size = 78, normalized size = 1.37

$$\frac{bd \log \left(\left| \frac{bc}{bx+a} - \frac{ad}{bx+a} + d \right| \right)}{b^3c^2 - 2ab^2cd + a^2bd^2} - \frac{b}{(b^2c - abd)(bx + a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c),x, algorithm="giac")

[Out] $b*d*\log(\text{abs}(b*c/(b*x + a) - a*d/(b*x + a) + d))/(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2) - b/((b^2*c - a*b*d)*(b*x + a))$

maple [A] time = 0.01, size = 57, normalized size = 1.00

$$-\frac{d \ln (bx + a)}{(ad - bc)^2} + \frac{d \ln (dx + c)}{(ad - bc)^2} + \frac{1}{(ad - bc)(bx + a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/(d*x+c),x)

[Out] $d/(a*d-b*c)^2*\ln(d*x+c)+1/(a*d-b*c)/(b*x+a)-d/(a*d-b*c)^2*\ln(b*x+a)$

maxima [A] time = 1.36, size = 92, normalized size = 1.61

$$-\frac{d \log (bx + a)}{b^2c^2 - 2abcd + a^2d^2} + \frac{d \log (dx + c)}{b^2c^2 - 2abcd + a^2d^2} - \frac{1}{abc - a^2d + (b^2c - abd)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c),x, algorithm="maxima")

[Out] $-\frac{d \log(bx + a)}{b^2c^2 - 2ab^2cd + a^2d^2} + \frac{d \log(dx + c)}{b^2c^2 - 2ab^2cd + a^2d^2} - \frac{1}{(ab^2c - a^2d + (b^2c - ab^2d)x)}$

mupad [B] time = 0.14, size = 46, normalized size = 0.81

$$\frac{1}{(ad - bc)(a + bx)} - \frac{d \ln\left(\frac{a+bx}{c+dx}\right)}{(ad - bc)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^2*(c + d*x)),x)

[Out] $\frac{1}{(ad - bc)(a + bx)} - \frac{d \log((a + bx)/(c + dx))}{(ad - bc)^2}$

sympy [B] time = 0.68, size = 233, normalized size = 4.09

$$\frac{d \log\left(x + \frac{-\frac{a^3d^4}{(ad-bc)^2} + \frac{3a^2bcd^3}{(ad-bc)^2} - \frac{3ab^2c^2d^2}{(ad-bc)^2} + ad^2 + \frac{b^3c^3d}{(ad-bc)^2} + bcd}{2bd^2}\right)}{(ad - bc)^2} - \frac{d \log\left(x + \frac{\frac{a^3d^4}{(ad-bc)^2} - \frac{3a^2bcd^3}{(ad-bc)^2} + \frac{3ab^2c^2d^2}{(ad-bc)^2} + ad^2 - \frac{b^3c^3d}{(ad-bc)^2} + bcd}{2bd^2}\right)}{(ad - bc)^2} + \frac{1}{a^2d - abc + \dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2/(d*x+c),x)

[Out] $d \log(x + (-a**3*d**4/(a*d - b*c)**2 + 3*a**2*b*c*d**3/(a*d - b*c)**2 - 3*a*b**2*c**2*d**2/(a*d - b*c)**2 + a*d**2 + b**3*c**3*d/(a*d - b*c)**2 + b*c*d)/(2*b*d**2))/(a*d - b*c)**2 - d \log(x + (a**3*d**4/(a*d - b*c)**2 - 3*a**2*b*c*d**3/(a*d - b*c)**2 + 3*a*b**2*c**2*d**2/(a*d - b*c)**2 + a*d**2 - b**3*c**3*d/(a*d - b*c)**2 + b*c*d)/(2*b*d**2))/(a*d - b*c)**2 + 1/(a**2*d - a*b*c + x*(a*b*d - b**2*c))$

$$3.1342 \quad \int \frac{1}{(a+bx)^3(c+dx)} dx$$

Optimal. Leaf size=82

$$\frac{d^2 \log(a+bx)}{(bc-ad)^3} - \frac{d^2 \log(c+dx)}{(bc-ad)^3} + \frac{d}{(a+bx)(bc-ad)^2} - \frac{1}{2(a+bx)^2(bc-ad)}$$

[Out] $-1/2/(-a*d+b*c)/(b*x+a)^2+d/(-a*d+b*c)^2/(b*x+a)+d^2*\ln(b*x+a)/(-a*d+b*c)^3-d^2*\ln(d*x+c)/(-a*d+b*c)^3$

Rubi [A] time = 0.05, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$\frac{d^2 \log(a+bx)}{(bc-ad)^3} - \frac{d^2 \log(c+dx)}{(bc-ad)^3} + \frac{d}{(a+bx)(bc-ad)^2} - \frac{1}{2(a+bx)^2(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^3*(c + d*x)), x]

[Out] $-1/(2*(b*c - a*d)*(a + b*x)^2) + d/((b*c - a*d)^2*(a + b*x)) + (d^2*\text{Log}[a + b*x])/(b*c - a*d)^3 - (d^2*\text{Log}[c + d*x])/(b*c - a*d)^3$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^3(c+dx)} dx &= \int \left(\frac{b}{(bc-ad)(a+bx)^3} - \frac{bd}{(bc-ad)^2(a+bx)^2} + \frac{bd^2}{(bc-ad)^3(a+bx)} - \frac{d^3}{(bc-ad)^3(c+dx)} \right) dx \\ &= -\frac{1}{2(bc-ad)(a+bx)^2} + \frac{d}{(bc-ad)^2(a+bx)} + \frac{d^2 \log(a+bx)}{(bc-ad)^3} - \frac{d^2 \log(c+dx)}{(bc-ad)^3} \end{aligned}$$

Mathematica [A] time = 0.07, size = 67, normalized size = 0.82

$$\frac{(bc-ad)(3ad-bc+2bdx)}{(a+bx)^2} + \frac{2d^2 \log(a+bx) - 2d^2 \log(c+dx)}{2(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^3*(c + d*x)),x]

[Out] (((b*c - a*d)*(-(b*c) + 3*a*d + 2*b*d*x))/(a + b*x)^2 + 2*d^2*Log[a + b*x] - 2*d^2*Log[c + d*x])/(2*(b*c - a*d)^3)

fricas [B] time = 0.46, size = 242, normalized size = 2.95

$$\frac{b^2c^2 - 4abcd + 3a^2d^2 - 2(b^2cd - abd^2)x - 2(b^2d^2x^2 + 2abd^2x + a^2d^2)\log(bx + a) + 2(b^2d^2x^2 + 2abd^2x + a^2d^2)\log(c + dx)}{2(a^2b^3c^3 - 3a^3b^2c^2d + 3a^4bcd^2 - a^5d^3 + (b^5c^3 - 3ab^4c^2d + 3a^2b^3cd^2 - a^3b^2d^3)x^2 + 2(ab^4c^3 - 3a^2b^3c^2d + 3a^3b^2cd^2 - a^4bd^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c),x, algorithm="fricas")

[Out] -1/2*(b^2*c^2 - 4*a*b*c*d + 3*a^2*d^2 - 2*(b^2*c*d - a*b*d^2)*x - 2*(b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*log(b*x + a) + 2*(b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*log(d*x + c))/(a^2*b^3*c^3 - 3*a^3*b^2*c^2*d + 3*a^4*b*c*d^2 - a^5*d^3 + (b^5*c^3 - 3*a*b^4*c^2*d + 3*a^2*b^3*c*d^2 - a^3*b^2*d^3)*x^2 + 2*(a*b^4*c^3 - 3*a^2*b^3*c^2*d + 3*a^3*b^2*c*d^2 - a^4*b*d^3)*x)

giac [B] time = 1.29, size = 165, normalized size = 2.01

$$\frac{bd^2 \log(|bx + a|)}{b^4c^3 - 3ab^3c^2d + 3a^2b^2cd^2 - a^3bd^3} - \frac{d^3 \log(|dx + c|)}{b^3c^3d - 3ab^2c^2d^2 + 3a^2bcd^3 - a^3d^4} - \frac{b^2c^2 - 4abcd + 3a^2d^2 - 2(b^2cd - abd^2)x - 2(b^2d^2x^2 + 2abd^2x + a^2d^2)\log(bx + a) + 2(b^2d^2x^2 + 2abd^2x + a^2d^2)\log(dx + c)}{2(bc - ad)^3(bx + a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c),x, algorithm="giac")

[Out] b*d^2*log(abs(b*x + a))/(b^4*c^3 - 3*a*b^3*c^2*d + 3*a^2*b^2*c*d^2 - a^3*b*d^3) - d^3*log(abs(d*x + c))/(b^3*c^3*d - 3*a*b^2*c^2*d^2 + 3*a^2*b*c*d^3 - a^3*d^4) - 1/2*(b^2*c^2 - 4*a*b*c*d + 3*a^2*d^2 - 2*(b^2*c*d - a*b*d^2)*x)/(b*c - a*d)^3*(b*x + a)^2)

maple [A] time = 0.01, size = 81, normalized size = 0.99

$$-\frac{d^2 \ln(bx + a)}{(ad - bc)^3} + \frac{d^2 \ln(dx + c)}{(ad - bc)^3} + \frac{d}{(ad - bc)^2 (bx + a)} + \frac{1}{2(ad - bc)(bx + a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^3/(d*x+c),x)

[Out] d^2/(a*d-b*c)^3*ln(d*x+c)+1/2/(a*d-b*c)/(b*x+a)^2+d/(a*d-b*c)^2/(b*x+a)-d^2/(a*d-b*c)^3*ln(b*x+a)

maxima [B] time = 1.41, size = 202, normalized size = 2.46

$$\frac{d^2 \log(bx + a)}{b^3 c^3 - 3ab^2 c^2 d + 3a^2 bcd^2 - a^3 d^3} - \frac{d^2 \log(dx + c)}{b^3 c^3 - 3ab^2 c^2 d + 3a^2 bcd^2 - a^3 d^3} + \frac{2bd}{2(a^2 b^2 c^2 - 2a^3 bcd + a^4 d^2 + (b^4 c^2 - 2ab^3 c d + a^2 b^2 d^2) * x^2 + 2(a * b^3 c^2 - 2a^2 b^2 c d + a^3 b d^2) * x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c), x, algorithm="maxima")

[Out] $d^2 \log(bx + a) / (b^3 c^3 - 3a^2 b^2 c^2 d + 3a^2 b c d^2 - a^3 d^3) - d^2 \log(dx + c) / (b^3 c^3 - 3a^2 b^2 c^2 d + 3a^2 b c d^2 - a^3 d^3) + 1/2 * (2 * b * d * x - b * c + 3 * a * d) / (a^2 * b^2 * c^2 - 2 * a^3 * b * c * d + a^4 * d^2 + (b^4 * c^2 - 2 * a * b^3 * c * d + a^2 * b^2 * d^2) * x^2 + 2 * (a * b^3 * c^2 - 2 * a^2 * b^2 * c * d + a^3 * b * d^2) * x)$

mupad [B] time = 0.16, size = 182, normalized size = 2.22

$$\frac{\frac{3ad-bc}{2(a^2 d^2 - 2abcd + b^2 c^2)} + \frac{bdx}{a^2 d^2 - 2abcd + b^2 c^2}}{a^2 + 2abx + b^2 x^2} - \frac{2d^2 \operatorname{atanh}\left(\frac{a^3 d^3 - a^2 bcd^2 - ab^2 c^2 d + b^3 c^3}{(ad-bc)^3} + \frac{2bdx(a^2 d^2 - 2abcd + b^2 c^2)}{(ad-bc)^3}\right)}{(ad-bc)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^3*(c + d*x)), x)

[Out] $((3ad - bc) / (2(a^2 d^2 + b^2 c^2 - 2ab^2 c d))) + (b * d * x) / (a^2 d^2 + b^2 c^2 - 2ab^2 c d) / (a^2 + b^2 x^2 + 2abx) - (2d^2 * \operatorname{atanh}((a^3 d^3 + b^3 c^3 - ab^2 c^2 d - a^2 b c d^2) / (ad - bc)^3 + (2b * d * x * (a^2 d^2 + b^2 c^2 - 2ab^2 c d)) / (ad - bc)^3)) / (ad - bc)^3$

sympy [B] time = 1.06, size = 381, normalized size = 4.65

$$\frac{d^2 \log\left(x + \frac{\frac{a^4 d^6}{(ad-bc)^3} + \frac{4a^3 bcd^5}{(ad-bc)^3} - \frac{6a^2 b^2 c^2 d^4}{(ad-bc)^3} + \frac{4ab^3 c^3 d^3}{(ad-bc)^3} + ad^3 - \frac{b^4 c^4 d^2}{(ad-bc)^3} + bcd^2}{2bd^3}\right)}{(ad-bc)^3} - \frac{d^2 \log\left(x + \frac{\frac{a^4 d^6}{(ad-bc)^3} - \frac{4a^3 bcd^5}{(ad-bc)^3} + \frac{6a^2 b^2 c^2 d^4}{(ad-bc)^3} - \frac{4ab^3 c^3 d^3}{(ad-bc)^3} + ad^3 + \frac{b^4 c^4 d^2}{(ad-bc)^3} + bcd^2}{2bd^3}\right)}{(ad-bc)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**3/(d*x+c), x)

[Out] $d^2 \log(x + (-a^4 d^6 / (ad - bc)^3 + 4a^3 b^2 c d^5 / (ad - bc)^3 - 6a^2 b^2 c^2 d^4 / (ad - bc)^3 + 4a^2 b^3 c^3 d^3 / (ad - bc)^3 + a^3 d^3 - b^4 c^4 d^2 / (ad - bc)^3 + b^3 c^4 d^2) / (2b^2 d^3)) / (ad - bc)^3 - d^2 \log(x + (a^4 d^6 / (ad - bc)^3 - 4a^3 b^2 c d^5 / (ad - bc)^3 + 6a^2 b^2 c^2 d^4 / (ad - bc)^3 - 4a^2 b^3 c^3 d^3 / (ad - bc)^3 + a^3 d^3 + b^4 c^4 d^2) / (2b^2 d^3)) / (ad - bc)^3$

$$\begin{aligned}
& 3 + a*d**3 + b**4*c**4*d**2/(a*d - b*c)**3 + b*c*d**2)/(2*b*d**3))/(a*d - b \\
& *c)**3 + (3*a*d - b*c + 2*b*d*x)/(2*a**4*d**2 - 4*a**3*b*c*d + 2*a**2*b**2* \\
& c**2 + x**2*(2*a**2*b**2*d**2 - 4*a*b**3*c*d + 2*b**4*c**2) + x*(4*a**3*b*d \\
& **2 - 8*a**2*b**2*c*d + 4*a*b**3*c**2))
\end{aligned}$$

$$3.1343 \quad \int \frac{(a+bx)^5}{(c+dx)^2} dx$$

Optimal. Leaf size=130

$$\frac{5b^4(c+dx)^3(bc-ad)}{3d^6} + \frac{5b^3(c+dx)^2(bc-ad)^2}{d^6} - \frac{10b^2x(bc-ad)^3}{d^5} + \frac{(bc-ad)^5}{d^6(c+dx)} + \frac{5b(bc-ad)^4 \log(c+dx)}{d^6} + \frac{b^5(c+dx)}{4d^6}$$

[Out] $-10*b^2*(-a*d+b*c)^3*x/d^5+(-a*d+b*c)^5/d^6/(d*x+c)+5*b^3*(-a*d+b*c)^2*(d*x+c)^2/d^6-5/3*b^4*(-a*d+b*c)*(d*x+c)^3/d^6+1/4*b^5*(d*x+c)^4/d^6+5*b*(-a*d+b*c)^4*\ln(d*x+c)/d^6$

Rubi [A] time = 0.14, antiderivative size = 130, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{5b^4(c+dx)^3(bc-ad)}{3d^6} + \frac{5b^3(c+dx)^2(bc-ad)^2}{d^6} - \frac{10b^2x(bc-ad)^3}{d^5} + \frac{(bc-ad)^5}{d^6(c+dx)} + \frac{5b(bc-ad)^4 \log(c+dx)}{d^6} + \frac{b^5(c+dx)}{4d^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(c + d*x)^2, x]

[Out] $(-10*b^2*(b*c - a*d)^3*x)/d^5 + (b*c - a*d)^5/(d^6*(c + d*x)) + (5*b^3*(b*c - a*d)^2*(c + d*x)^2)/d^6 - (5*b^4*(b*c - a*d)*(c + d*x)^3)/(3*d^6) + (b^5*(c + d*x)^4)/(4*d^6) + (5*b*(b*c - a*d)^4*\text{Log}[c + d*x])/d^6$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(c+dx)^2} dx &= \int \left(-\frac{10b^2(bc-ad)^3}{d^5} + \frac{(-bc+ad)^5}{d^5(c+dx)^2} + \frac{5b(bc-ad)^4}{d^5(c+dx)} + \frac{10b^3(bc-ad)^2(c+dx)}{d^5} - \frac{5b^4(bc-ad)(c+dx)}{d^5} \right) dx \\ &= -\frac{10b^2(bc-ad)^3x}{d^5} + \frac{(bc-ad)^5}{d^6(c+dx)} + \frac{5b^3(bc-ad)^2(c+dx)^2}{d^6} - \frac{5b^4(bc-ad)(c+dx)^3}{3d^6} + \frac{b^5(c+dx)^4}{4d^6} \end{aligned}$$

Mathematica [A] time = 0.08, size = 228, normalized size = 1.75

$$-12a^5d^5 + 60a^4bcd^4 + 120a^3b^2d^3(-c^2 + cdx + d^2x^2) + 60a^2b^3d^2(2c^3 - 4c^2dx - 3cd^2x^2 + d^3x^3) + 20ab^4d(-3c^4 + 4cd^3x + 3d^4x^2)$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(c + d*x)^2,x]

[Out] (60*a^4*b*c*d^4 - 12*a^5*d^5 + 120*a^3*b^2*d^3*(-c^2 + c*d*x + d^2*x^2) + 60*a^2*b^3*d^2*(2*c^3 - 4*c^2*d*x - 3*c*d^2*x^2 + d^3*x^3) + 20*a*b^4*d*(-3*c^4 + 9*c^3*d*x + 6*c^2*d^2*x^2 - 2*c*d^3*x^3 + d^4*x^4) + b^5*(12*c^5 - 48*c^4*d*x - 30*c^3*d^2*x^2 + 10*c^2*d^3*x^3 - 5*c*d^4*x^4 + 3*d^5*x^5) + 60*b*(b*c - a*d)^4*(c + d*x)*Log[c + d*x])/(12*d^6*(c + d*x))

fricas [B] time = 0.44, size = 373, normalized size = 2.87

$$\frac{3b^5d^5x^5 + 12b^5c^5 - 60ab^4c^4d + 120a^2b^3c^3d^2 - 120a^3b^2c^2d^3 + 60a^4bcd^4 - 12a^5d^5 - 5(b^5cd^4 - 4ab^4d^5)x^4 + 10}{12d^6(c + dx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^2,x, algorithm="fricas")

[Out] 1/12*(3*b^5*d^5*x^5 + 12*b^5*c^5 - 60*a*b^4*c^4*d + 120*a^2*b^3*c^3*d^2 - 120*a^3*b^2*c^2*d^3 + 60*a^4*b*c*d^4 - 12*a^5*d^5 - 5*(b^5*c*d^4 - 4*a*b^4*d^5)*x^4 + 10*(b^5*c^2*d^3 - 4*a*b^4*c*d^4 + 6*a^2*b^3*d^5)*x^3 - 30*(b^5*c^3*d^2 - 4*a*b^4*c^2*d^3 + 6*a^2*b^3*c*d^4 - 4*a^3*b^2*d^5)*x^2 - 12*(4*b^5*c^4*d - 15*a*b^4*c^3*d^2 + 20*a^2*b^3*c^2*d^3 - 10*a^3*b^2*c*d^4)*x + 60*(b^5*c^5 - 4*a*b^4*c^4*d + 6*a^2*b^3*c^3*d^2 - 4*a^3*b^2*c^2*d^3 + a^4*b*c*d^4 + (b^5*c^4*d - 4*a*b^4*c^3*d^2 + 6*a^2*b^3*c^2*d^3 - 4*a^3*b^2*c*d^4 + a^4*b*d^5)*x)*log(d*x + c))/(d^7*x + c*d^6)

giac [B] time = 1.27, size = 339, normalized size = 2.61

$$\frac{\left(3b^5 - \frac{20(b^5cd - ab^4d^2)}{(dx+c)d} + \frac{60(b^5c^2d^2 - 2ab^4cd^3 + a^2b^3d^4)}{(dx+c)^2d^2} - \frac{120(b^5c^3d^3 - 3ab^4c^2d^4 + 3a^2b^3cd^5 - a^3b^2d^6)}{(dx+c)^3d^3}\right)(dx+c)^4}{12d^6} 5(b^5c^4 - 4ab^4c^3d + \dots)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^2,x, algorithm="giac")

[Out] 1/12*(3*b^5 - 20*(b^5*c*d - a*b^4*d^2)/((d*x + c)*d) + 60*(b^5*c^2*d^2 - 2*a*b^4*c*d^3 + a^2*b^3*d^4)/((d*x + c)^2*d^2) - 120*(b^5*c^3*d^3 - 3*a*b^4*c^2*d^4 + 3*a^2*b^3*c*d^5 - a^3*b^2*d^6)/((d*x + c)^3*d^3))*(d*x + c)^4/d^6 - 5*(b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)*log(abs(d*x + c)/((d*x + c)^2*abs(d)))/d^6 + (b^5*c^5*d^4/(d*x + c) - 5*a*b^4*c^4*d^5/(d*x + c) + 10*a^2*b^3*c^3*d^6/(d*x + c) - 10*a^3*b^2*c^2*d^7/(d*x + c) + 5*a^4*b*c*d^8/(d*x + c) - a^5*d^9/(d*x + c))/d^10

maple [B] time = 0.01, size = 326, normalized size = 2.51

$$\frac{b^5 x^4}{4d^2} + \frac{5ab^4 x^3}{3d^2} - \frac{2b^5 c x^3}{3d^3} + \frac{5a^2 b^3 x^2}{d^2} - \frac{5ab^4 c x^2}{d^3} + \frac{3b^5 c^2 x^2}{2d^4} - \frac{a^5}{(dx+c)d} + \frac{5a^4 bc}{(dx+c)d^2} + \frac{5a^4 b \ln(dx+c)}{d^2} - \frac{10a^3 b^2 c^2}{(dx+c)d^3} - \frac{2b^5 c^3}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(d*x+c)^2,x)

[Out] $\frac{1}{4}b^5/d^2*x^4 + 5/3*b^4/d^2*x^3*a - 2/3*b^5/d^3*x^3*c + 5*b^3/d^2*x^2*a^2 - 5*b^4/d^3*x^2*a*c + 3/2*b^5/d^4*x^2*c^2 + 10*b^2/d^2*a^3*x - 20*b^3/d^3*a^2*c*x + 15*b^4/d^4*a*c^2*x - 4*b^5/d^5*c^3*x - 1/d/(d*x+c)*a^5 + 5/d^2/(d*x+c)*a^4*b*c - 10/d^3/(d*x+c)*a^3*b^2*c^2 + 10/d^4/(d*x+c)*a^2*b^3*c^3 - 5/d^5/(d*x+c)*a*b^4*c^4 + 1/d^6/(d*x+c)*b^5*c^5 + 5*b/d^2*\ln(d*x+c)*a^4 - 20*b^2/d^3*\ln(d*x+c)*a^3*c + 30*b^3/d^4*\ln(d*x+c)*a^2*c^2 - 20*b^4/d^5*\ln(d*x+c)*a*c^3 + 5*b^5/d^6*\ln(d*x+c)*c^4$

maxima [B] time = 1.40, size = 264, normalized size = 2.03

$$\frac{b^5 c^5 - 5ab^4 c^4 d + 10a^2 b^3 c^3 d^2 - 10a^3 b^2 c^2 d^3 + 5a^4 b c d^4 - a^5 d^5}{d^7 x + c d^6} + \frac{3b^5 d^3 x^4 - 4(2b^5 c d^2 - 5ab^4 d^3)x^3 + 6(3b^5 c^2 d - 5a^2 b^4 c^2 d^2)x^2 - 4(2b^5 c^3 d - 5a^2 b^4 c^3 d^2)x + 6(3b^5 c^4 d - 5a^2 b^4 c^4 d^2) - 4a^5 d^5}{d^7 x + c d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^2,x, algorithm="maxima")

[Out] $(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)/(d^7*x + c*d^6) + 1/12*(3*b^5*d^3*x^4 - 4*(2*b^5*c*d^2 - 5*a*b^4*d^3)*x^3 + 6*(3*b^5*c^2*d - 10*a*b^4*c*d^2 + 10*a^2*b^3*d^3)*x^2 - 12*(4*b^5*c^3 - 15*a*b^4*c^2*d + 20*a^2*b^3*c*d^2 - 10*a^3*b^2*d^3)*x)/d^5 + 5*(b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)*\log(d*x + c)/d^6$

mupad [B] time = 0.25, size = 327, normalized size = 2.52

$$x^3 \left(\frac{5ab^4}{3d^2} - \frac{2b^5c}{3d^3} \right) + x \left(\frac{2c \left(\frac{5ab^4}{d^2} - \frac{2b^5c}{d^3} \right) - \frac{10a^2b^3}{d^2} + \frac{b^5c^2}{d^4}}{d} + \frac{10a^3b^2}{d^2} - \frac{c^2 \left(\frac{5ab^4}{d^2} - \frac{2b^5c}{d^3} \right)}{d^2} \right) - x^2 \left(\frac{c \left(\frac{5ab^4}{d^2} - \frac{2b^5c}{d^3} \right)}{d} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/(c + d*x)^2,x)

[Out] $x^3*((5*a*b^4)/(3*d^2) - (2*b^5*c)/(3*d^3)) + x*((2*c*((2*c*((5*a*b^4)/d^2 - (2*b^5*c)/d^3))/d - (10*a^2*b^3)/d^2 + (b^5*c^2)/d^4))/d + (10*a^3*b^2)/d$

$$\begin{aligned} &^2 - (c^2 * ((5 * a * b^4) / d^2 - (2 * b^5 * c) / d^3)) / d^2 - x^2 * ((c * ((5 * a * b^4) / d^2 - \\ &(2 * b^5 * c) / d^3)) / d - (5 * a^2 * b^3) / d^2 + (b^5 * c^2) / (2 * d^4)) + (\log(c + d * x) * (5 \\ &* b^5 * c^4 + 5 * a^4 * b * d^4 - 20 * a^3 * b^2 * c * d^3 + 30 * a^2 * b^3 * c^2 * d^2 - 20 * a * b^4 * c \\ &^3 * d)) / d^6 - (a^5 * d^5 - b^5 * c^5 - 10 * a^2 * b^3 * c^3 * d^2 + 10 * a^3 * b^2 * c^2 * d^3 + \\ &5 * a * b^4 * c^4 * d - 5 * a^4 * b * c * d^4) / (d * (c * d^5 + d^6 * x)) + (b^5 * x^4) / (4 * d^2) \end{aligned}$$

sympy [A] time = 0.89, size = 231, normalized size = 1.78

$$\frac{b^5 x^4}{4d^2} + \frac{5b(ad - bc)^4 \log(c + dx)}{d^6} + x^3 \left(\frac{5ab^4}{3d^2} - \frac{2b^5c}{3d^3} \right) + x^2 \left(\frac{5a^2b^3}{d^2} - \frac{5ab^4c}{d^3} + \frac{3b^5c^2}{2d^4} \right) + x \left(\frac{10a^3b^2}{d^2} - \frac{20a^2b^3c}{d^3} + \frac{15ab^4}{d^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/(d*x+c)**2,x)

[Out] b**5*x**4/(4*d**2) + 5*b*(a*d - b*c)**4*log(c + d*x)/d**6 + x**3*(5*a*b**4/(3*d**2) - 2*b**5*c/(3*d**3)) + x**2*(5*a**2*b**3/d**2 - 5*a*b**4*c/d**3 + 3*b**5*c**2/(2*d**4)) + x*(10*a**3*b**2/d**2 - 20*a**2*b**3*c/d**3 + 15*a*b**4*c**2/d**4 - 4*b**5*c**3/d**5) + (-a**5*d**5 + 5*a**4*b*c*d**4 - 10*a**3*b**2*c**2*d**3 + 10*a**2*b**3*c**3*d**2 - 5*a*b**4*c**4*d + b**5*c**5)/(c*d**6 + d**7*x)

$$3.1344 \quad \int \frac{(a+bx)^4}{(c+dx)^2} dx$$

Optimal. Leaf size=104

$$-\frac{2b^3(c+dx)^2(bc-ad)}{d^5} + \frac{6b^2x(bc-ad)^2}{d^4} - \frac{(bc-ad)^4}{d^5(c+dx)} - \frac{4b(bc-ad)^3 \log(c+dx)}{d^5} + \frac{b^4(c+dx)^3}{3d^5}$$

[Out] $6*b^2*(-a*d+b*c)^2*x/d^4 - (-a*d+b*c)^4/d^5/(d*x+c) - 2*b^3*(-a*d+b*c)*(d*x+c)^2/d^5 + 1/3*b^4*(d*x+c)^3/d^5 - 4*b*(-a*d+b*c)^3*\ln(d*x+c)/d^5$

Rubi [A] time = 0.10, antiderivative size = 104, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{2b^3(c+dx)^2(bc-ad)}{d^5} + \frac{6b^2x(bc-ad)^2}{d^4} - \frac{(bc-ad)^4}{d^5(c+dx)} - \frac{4b(bc-ad)^3 \log(c+dx)}{d^5} + \frac{b^4(c+dx)^3}{3d^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4/(c + d*x)^2, x]

[Out] $(6*b^2*(b*c - a*d)^2*x)/d^4 - (b*c - a*d)^4/(d^5*(c + d*x)) - (2*b^3*(b*c - a*d)*(c + d*x)^2)/d^5 + (b^4*(c + d*x)^3)/(3*d^5) - (4*b*(b*c - a*d)^3*\text{Log}[c + d*x])/d^5$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^4}{(c+dx)^2} dx &= \int \left(\frac{6b^2(bc-ad)^2}{d^4} + \frac{(-bc+ad)^4}{d^4(c+dx)^2} - \frac{4b(bc-ad)^3}{d^4(c+dx)} - \frac{4b^3(bc-ad)(c+dx)}{d^4} + \frac{b^4(c+dx)^2}{d^4} \right) dx \\ &= \frac{6b^2(bc-ad)^2x}{d^4} - \frac{(bc-ad)^4}{d^5(c+dx)} - \frac{2b^3(bc-ad)(c+dx)^2}{d^5} + \frac{b^4(c+dx)^3}{3d^5} - \frac{4b(bc-ad)^3 \log(c+dx)}{d^5} \end{aligned}$$

Mathematica [A] time = 0.06, size = 165, normalized size = 1.59

$$\frac{-3a^4d^4 + 12a^3bcd^3 + 18a^2b^2d^2(-c^2 + cdx + d^2x^2) + 6ab^3d(2c^3 - 4c^2dx - 3cd^2x^2 + d^3x^3) - 12b(c+dx)(bc-ad)}{3d^5(c+dx)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4/(c + d*x)^2,x]

[Out] (12*a^3*b*c*d^3 - 3*a^4*d^4 + 18*a^2*b^2*d^2*(-c^2 + c*d*x + d^2*x^2) + 6*a*b^3*d*(2*c^3 - 4*c^2*d*x - 3*c*d^2*x^2 + d^3*x^3) + b^4*(-3*c^4 + 9*c^3*d*x + 6*c^2*d^2*x^2 - 2*c*d^3*x^3 + d^4*x^4) - 12*b*(b*c - a*d)^3*(c + d*x)*Log[c + d*x])/(3*d^5*(c + d*x))

fricas [B] time = 0.46, size = 267, normalized size = 2.57

$$\frac{b^4 d^4 x^4 - 3 b^4 c^4 + 12 a b^3 c^3 d - 18 a^2 b^2 c^2 d^2 + 12 a^3 b c d^3 - 3 a^4 d^4 - 2 (b^4 c d^3 - 3 a b^3 d^4) x^3 + 6 (b^4 c^2 d^2 - 3 a b^3 c d^3 + 3 a^2 b^2 c^2 d^2 - 2 a^3 b c d^3 + a^4 d^4) x^2 + 6 (b^4 c^3 d - 3 a b^3 c^2 d^2 + 3 a^2 b^2 c^2 d^2 - a^3 b c d^3) x - 12 (b^4 c^4 - 3 a^2 b^2 c^2 d^2 - a^3 b c d^3 + (b^4 c^3 d - 3 a^2 b^2 c^2 d^2 + 3 a^3 b c d^3 - a^4 d^4) x) \log(d x + c)}{3 d^5 (c + d x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^2,x, algorithm="fricas")

[Out] 1/3*(b^4*d^4*x^4 - 3*b^4*c^4 + 12*a*b^3*c^3*d - 18*a^2*b^2*c^2*d^2 + 12*a^3*b*c*d^3 - 3*a^4*d^4 - 2*(b^4*c*d^3 - 3*a*b^3*d^4)*x^3 + 6*(b^4*c^2*d^2 - 3*a*b^3*c*d^3 + 3*a^2*b^2*d^4)*x^2 + 3*(3*b^4*c^3*d - 8*a*b^3*c^2*d^2 + 6*a^2*b^2*c*d^3)*x - 12*(b^4*c^4 - 3*a*b^3*c^3*d + 3*a^2*b^2*c^2*d^2 - a^3*b*c*d^3 + (b^4*c^3*d - 3*a*b^3*c^2*d^2 + 3*a^2*b^2*c*d^3 - a^3*b*d^4)*x)*log(d*x + c))/(d^6*x + c*d^5)

giac [B] time = 1.27, size = 245, normalized size = 2.36

$$\frac{\left(b^4 - \frac{6(b^4 c d - a b^3 d^2)}{(d x + c) d} + \frac{18(b^4 c^2 d^2 - 2 a b^3 c d^3 + a^2 b^2 d^4)}{(d x + c)^2 d^2}\right)(d x + c)^3 + 4(b^4 c^3 - 3 a b^3 c^2 d + 3 a^2 b^2 c d^2 - a^3 b d^3) \log\left(\frac{|d x + c|}{(d x + c)^2 |d|}\right)}{3 d^5} + \frac{4(b^4 c^3 - 3 a b^3 c^2 d + 3 a^2 b^2 c d^2 - a^3 b d^3) \log\left(\frac{|d x + c|}{(d x + c)^2 |d|}\right)}{d^5} + \frac{b^4 x^4}{d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^2,x, algorithm="giac")

[Out] 1/3*(b^4 - 6*(b^4*c*d - a*b^3*d^2)/((d*x + c)*d) + 18*(b^4*c^2*d^2 - 2*a*b^3*c*d^3 + a^2*b^2*d^4)/((d*x + c)^2*d^2))*((d*x + c)^3/d^5 + 4*(b^4*c^3 - 3*a*b^3*c^2*d + 3*a^2*b^2*c*d^2 - a^3*b*d^3)*log(abs(d*x + c)/((d*x + c)^2*abs(d))))/d^5 - (b^4*c^4*d^3/(d*x + c) - 4*a*b^3*c^3*d^4/(d*x + c) + 6*a^2*b^2*c^2*d^5/(d*x + c) - 4*a^3*b*c*d^6/(d*x + c) + a^4*d^7/(d*x + c))/d^8

maple [B] time = 0.01, size = 230, normalized size = 2.21

$$\frac{b^4 x^3}{3 d^2} + \frac{2 a b^3 x^2}{d^2} - \frac{b^4 c x^2}{d^3} - \frac{a^4}{(d x + c) d} + \frac{4 a^3 b c}{(d x + c) d^2} + \frac{4 a^3 b \ln(d x + c)}{d^2} - \frac{6 a^2 b^2 c^2}{(d x + c) d^3} - \frac{12 a^2 b^2 c \ln(d x + c)}{d^3} + \frac{6 a^2 b^2 x}{d^2} + \frac{4 a^4}{(d x + c) d^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^4/(d*x+c)^2,x)`

[Out] $\frac{1}{3}b^4/d^2x^3+2b^3/d^2x^2a-b^4/d^3x^2c+6b^2/d^2a^2x-8b^3/d^3a^2cx+3b^4/d^4c^2x-1/d/(d*x+c)*a^4+4/d^2/(d*x+c)*a^3*b*c-6/d^3/(d*x+c)*a^2*b^2*c^2+4/d^4/(d*x+c)*a*b^3*c^3-1/d^5/(d*x+c)*b^4*c^4+4*b/d^2*\ln(d*x+c)*a^3-12*b^2/d^3*\ln(d*x+c)*a^2*c+12*b^3/d^4*\ln(d*x+c)*a*c^2-4*b^4/d^5*\ln(d*x+c)*c^3$

maxima [A] time = 1.36, size = 183, normalized size = 1.76

$$\frac{b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4}{d^6x + cd^5} + \frac{b^4d^2x^3 - 3(b^4cd - 2ab^3d^2)x^2 + 3(3b^4c^2 - 8ab^3cd + 6a^2b^2d^2 - 4a^3bcd^3 + a^4d^4)}{3d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^4/(d*x+c)^2,x, algorithm="maxima")`

[Out] $-(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(d^6*x + c*d^5) + 1/3*(b^4*d^2*x^3 - 3*(b^4*c*d - 2*a*b^3*d^2)*x^2 + 3*(3*b^4*c^2 - 8*a*b^3*c*d + 6*a^2*b^2*d^2)*x)/d^4 - 4*(b^4*c^3 - 3*a*b^3*c^2*d + 3*a^2*b^2*c*d^2 - a^3*b*d^3)*\log(d*x + c)/d^5$

mupad [B] time = 0.07, size = 203, normalized size = 1.95

$$x^2 \left(\frac{2ab^3}{d^2} - \frac{b^4c}{d^3} \right) - x \left(\frac{2c \left(\frac{4ab^3}{d^2} - \frac{2b^4c}{d^3} \right)}{d} - \frac{6a^2b^2}{d^2} + \frac{b^4c^2}{d^4} \right) + \frac{b^4x^3}{3d^2} - \frac{\ln(c+dx) (-4a^3bd^3 + 12a^2b^2cd^2 - 12a^3bcd^3 + 6a^4d^4)}{d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^4/(c + d*x)^2,x)`

[Out] $x^2*((2*a*b^3)/d^2 - (b^4*c)/d^3) - x*((2*c*((4*a*b^3)/d^2 - (2*b^4*c)/d^3))/d - (6*a^2*b^2)/d^2 + (b^4*c^2)/d^4) + (b^4*x^3)/(3*d^2) - (\log(c + d*x)*(4*b^4*c^3 - 4*a^3*b*d^3 + 12*a^2*b^2*c*d^2 - 12*a*b^3*c^2*d))/d^5 - (a^4*d^4 + b^4*c^4 + 6*a^2*b^2*c^2*d^2 - 4*a*b^3*c^3*d - 4*a^3*b*c*d^3)/(d*(c*d^4 + d^5*x))$

sympy [A] time = 0.68, size = 155, normalized size = 1.49

$$\frac{b^4x^3}{3d^2} + \frac{4b(ad-bc)^3 \log(c+dx)}{d^5} + x^2 \left(\frac{2ab^3}{d^2} - \frac{b^4c}{d^3} \right) + x \left(\frac{6a^2b^2}{d^2} - \frac{8ab^3c}{d^3} + \frac{3b^4c^2}{d^4} \right) + \frac{-a^4d^4 + 4a^3bcd^3 - 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4}{cd^5 + d^6x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**4/(d*x+c)**2,x)`

```
[Out] b**4*x**3/(3*d**2) + 4*b*(a*d - b*c)**3*log(c + d*x)/d**5 + x**2*(2*a*b**3/
d**2 - b**4*c/d**3) + x*(6*a**2*b**2/d**2 - 8*a*b**3*c/d**3 + 3*b**4*c**2/d
**4) + (-a**4*d**4 + 4*a**3*b*c*d**3 - 6*a**2*b**2*c**2*d**2 + 4*a*b**3*c**
3*d - b**4*c**4)/(c*d**5 + d**6*x)
```

$$3.1345 \quad \int \frac{(a+bx)^3}{(c+dx)^2} dx$$

Optimal. Leaf size=75

$$-\frac{b^2x(2bc-3ad)}{d^3} + \frac{(bc-ad)^3}{d^4(c+dx)} + \frac{3b(bc-ad)^2 \log(c+dx)}{d^4} + \frac{b^3x^2}{2d^2}$$

[Out] $-b^2*(-3*a*d+2*b*c)*x/d^3+1/2*b^3*x^2/d^2+(-a*d+b*c)^3/d^4/(d*x+c)+3*b*(-a*d+b*c)^2*\ln(d*x+c)/d^4$

Rubi [A] time = 0.06, antiderivative size = 75, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{b^2x(2bc-3ad)}{d^3} + \frac{(bc-ad)^3}{d^4(c+dx)} + \frac{3b(bc-ad)^2 \log(c+dx)}{d^4} + \frac{b^3x^2}{2d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/(c + d*x)^2, x]

[Out] $-((b^2*(2*b*c - 3*a*d)*x)/d^3) + (b^3*x^2)/(2*d^2) + (b*c - a*d)^3/(d^4*(c + d*x)) + (3*b*(b*c - a*d)^2*\text{Log}[c + d*x])/d^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{(c+dx)^2} dx &= \int \left(-\frac{b^2(2bc-3ad)}{d^3} + \frac{b^3x}{d^2} + \frac{(-bc+ad)^3}{d^3(c+dx)^2} + \frac{3b(bc-ad)^2}{d^3(c+dx)} \right) dx \\ &= -\frac{b^2(2bc-3ad)x}{d^3} + \frac{b^3x^2}{2d^2} + \frac{(bc-ad)^3}{d^4(c+dx)} + \frac{3b(bc-ad)^2 \log(c+dx)}{d^4} \end{aligned}$$

Mathematica [A] time = 0.04, size = 114, normalized size = 1.52

$$\frac{3(a^2bd^2 - 2ab^2cd + b^3c^2) \log(c+dx)}{d^4} + \frac{-a^3d^3 + 3a^2bcd^2 - 3ab^2c^2d + b^3c^3}{d^4(c+dx)} - \frac{b^2x(2bc-3ad)}{d^3} + \frac{b^3x^2}{2d^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/(c + d*x)^2,x]

[Out] $-\frac{(b^2(2bc - 3ad)x)/d^3}{d^3} + \frac{(b^3x^2)/(2d^2)}{2d^2} + \frac{(b^3c^3 - 3ab^2c^2*d + 3a^2b*c*d^2 - a^3*d^3)/(d^4(c + d*x))}{d^4} + \frac{(3(b^3c^2 - 2a*b^2*c*d + a^2*b*d^2)*\text{Log}[c + d*x])}{d^4}$

fricas [B] time = 0.44, size = 172, normalized size = 2.29

$$\frac{b^3d^3x^3 + 2b^3c^3 - 6ab^2c^2d + 6a^2bcd^2 - 2a^3d^3 - 3(b^3cd^2 - 2ab^2d^3)x^2 - 2(2b^3c^2d - 3ab^2cd^2)x + 6(b^3c^3 - 2ab^2c^2d + 3a^2b*c*d^2 - a^3*d^3)}{2(d^5x + cd^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^2,x, algorithm="fricas")

[Out] $\frac{1}{2} * \frac{(b^3d^3x^3 + 2b^3c^3 - 6a*b^2*c^2*d + 6a^2*b*c*d^2 - 2a^3*d^3 - 3*(b^3*c*d^2 - 2a*b^2*d^3)*x^2 - 2*(2*b^3*c^2*d - 3a*b^2*c*d^2)*x + 6*(b^3*c^3 - 2a*b^2*c^2*d + a^2*b*c*d^2 + (b^3*c^2*d - 2a*b^2*c*d^2 + a^2*b*d^3)*x)*\log(d*x + c)}{(d^5*x + c*d^4)}$

giac [B] time = 1.26, size = 166, normalized size = 2.21

$$\frac{\left(b^3 - \frac{6(b^3cd - ab^2d^2)}{(dx+c)d}\right)(dx+c)^2}{2d^4} - \frac{3(b^3c^2 - 2ab^2cd + a^2bd^2) \log\left(\frac{|dx+c|}{(dx+c)^2|d|}\right)}{d^4} + \frac{\frac{b^3c^3d^2}{dx+c} - \frac{3ab^2c^2d^3}{dx+c} + \frac{3a^2bcd^4}{dx+c} - \frac{a^3d^5}{dx+c}}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^2,x, algorithm="giac")

[Out] $\frac{1}{2} * \frac{(b^3 - 6*(b^3*c*d - a*b^2*d^2)/((d*x + c)*d))*(d*x + c)^2/d^4 - 3*(b^3*c^2 - 2a*b^2*c*d + a^2*b*d^2)*\log(\text{abs}(d*x + c)/((d*x + c)^2*\text{abs}(d)))}{d^4} + \frac{(b^3*c^3*d^2/(d*x + c) - 3*a*b^2*c^2*d^3/(d*x + c) + 3*a^2*b*c*d^4/(d*x + c) - a^3*d^5/(d*x + c))}{d^6}$

maple [B] time = 0.01, size = 149, normalized size = 1.99

$$\frac{b^3x^2}{2d^2} - \frac{a^3}{(dx+c)d} + \frac{3a^2bc}{(dx+c)d^2} + \frac{3a^2b \ln(dx+c)}{d^2} - \frac{3ab^2c^2}{(dx+c)d^3} - \frac{6ab^2c \ln(dx+c)}{d^3} + \frac{3ab^2x}{d^2} + \frac{b^3c^3}{(dx+c)d^4} + \frac{3b^3c^2 \ln(dx+c)}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/(d*x+c)^2,x)

[Out] $\frac{1}{2}b^3x^2/d^2 + 3b^2/d^2 * ax - 2b^3/d^3 * xc - 1/d/(dx+c) * a^3 + 3/d^2/(dx+c) * a^2 * bc - 3/d^3/(dx+c) * a * b^2 * c^2 + 1/d^4/(dx+c) * b^3 * c^3 + 3b/d^2 * \ln(dx+c) * a^2 - 6b^2/d^3 * \ln(dx+c) * ac + 3b^3/d^4 * \ln(dx+c) * c^2$

maxima [A] time = 1.36, size = 117, normalized size = 1.56

$$\frac{b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3}{d^5x + cd^4} + \frac{b^3dx^2 - 2(2b^3c - 3ab^2d)x}{2d^3} + \frac{3(b^3c^2 - 2ab^2cd + a^2bd^2)\log(dx + c)}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^2,x, algorithm="maxima")

[Out] $(b^3c^3 - 3a*b^2*c^2*d + 3a^2*b*c*d^2 - a^3*d^3)/(d^5*x + c*d^4) + 1/2*(b^3*d*x^2 - 2*(2*b^3*c - 3*a*b^2*d)*x)/d^3 + 3*(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*\log(d*x + c)/d^4$

mupad [B] time = 0.08, size = 123, normalized size = 1.64

$$x \left(\frac{3ab^2}{d^2} - \frac{2b^3c}{d^3} \right) + \frac{\ln(c + dx) (3a^2bd^2 - 6ab^2cd + 3b^3c^2)}{d^4} - \frac{a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3}{d(xd^4 + cd^3)} + \frac{b^3x^2}{2d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3/(c + d*x)^2,x)

[Out] $x*((3*a*b^2)/d^2 - (2*b^3*c)/d^3) + (\log(c + d*x)*(3*b^3*c^2 + 3*a^2*b*d^2 - 6*a*b^2*c*d))/d^4 - (a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2)/(d*(c*d^3 + d^4*x)) + (b^3*x^2)/(2*d^2)$

sympy [A] time = 0.51, size = 102, normalized size = 1.36

$$\frac{b^3x^2}{2d^2} + \frac{3b(ad - bc)^2 \log(c + dx)}{d^4} + x \left(\frac{3ab^2}{d^2} - \frac{2b^3c}{d^3} \right) + \frac{-a^3d^3 + 3a^2bcd^2 - 3ab^2c^2d + b^3c^3}{cd^4 + d^5x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3/(d*x+c)**2,x)

[Out] $b**3*x**2/(2*d**2) + 3*b*(a*d - b*c)**2*\log(c + d*x)/d**4 + x*(3*a*b**2/d**2 - 2*b**3*c/d**3) + (-a**3*d**3 + 3*a**2*b*c*d**2 - 3*a*b**2*c**2*d + b**3*c**3)/(c*d**4 + d**5*x)$

$$3.1346 \quad \int \frac{(a+bx)^2}{(c+dx)^2} dx$$

Optimal. Leaf size=51

$$\frac{(bc-ad)^2}{d^3(c+dx)} - \frac{2b(bc-ad)\log(c+dx)}{d^3} + \frac{b^2x}{d^2}$$

[Out] $b^2*x/d^2 - (-a*d+b*c)^2/d^3/(d*x+c) - 2*b*(-a*d+b*c)*\ln(d*x+c)/d^3$

Rubi [A] time = 0.04, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{(bc-ad)^2}{d^3(c+dx)} - \frac{2b(bc-ad)\log(c+dx)}{d^3} + \frac{b^2x}{d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(c + d*x)^2, x]

[Out] $(b^2*x)/d^2 - (b*c - a*d)^2/(d^3*(c + d*x)) - (2*b*(b*c - a*d)*\text{Log}[c + d*x])/d^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(c+dx)^2} dx &= \int \left(\frac{b^2}{d^2} + \frac{(-bc+ad)^2}{d^2(c+dx)^2} - \frac{2b(bc-ad)}{d^2(c+dx)} \right) dx \\ &= \frac{b^2x}{d^2} - \frac{(bc-ad)^2}{d^3(c+dx)} - \frac{2b(bc-ad)\log(c+dx)}{d^3} \end{aligned}$$

Mathematica [A] time = 0.04, size = 47, normalized size = 0.92

$$\frac{-\frac{(bc-ad)^2}{c+dx} + 2b(ad-bc)\log(c+dx) + b^2dx}{d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(c + d*x)^2,x]

[Out] (b^2*d*x - (b*c - a*d)^2/(c + d*x) + 2*b*(-(b*c) + a*d)*Log[c + d*x])/d^3

fricas [A] time = 0.45, size = 92, normalized size = 1.80

$$\frac{b^2 d^2 x^2 + b^2 c d x - b^2 c^2 + 2 a b c d - a^2 d^2 - 2 (b^2 c^2 - a b c d + (b^2 c d - a b d^2) x) \log (d x + c)}{d^4 x + c d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^2,x, algorithm="fricas")

[Out] (b^2*d^2*x^2 + b^2*c*d*x - b^2*c^2 + 2*a*b*c*d - a^2*d^2 - 2*(b^2*c^2 - a*b*c*d + (b^2*c*d - a*b*d^2)*x)*log(d*x + c))/(d^4*x + c*d^3)

giac [A] time = 1.25, size = 98, normalized size = 1.92

$$\frac{(d x + c) b^2}{d^3} + \frac{2 (b^2 c - a b d) \log \left(\frac{|d x + c|}{(d x + c)^2 |d|} \right)}{d^3} - \frac{b^2 c^2 d}{d x + c} - \frac{2 a b c d^2}{d x + c} + \frac{a^2 d^3}{d x + c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^2,x, algorithm="giac")

[Out] (d*x + c)*b^2/d^3 + 2*(b^2*c - a*b*d)*log(abs(d*x + c)/((d*x + c)^2*abs(d)))/d^3 - (b^2*c^2*d/(d*x + c) - 2*a*b*c*d^2/(d*x + c) + a^2*d^3/(d*x + c))/d^4

maple [A] time = 0.01, size = 86, normalized size = 1.69

$$-\frac{a^2}{(d x + c) d} + \frac{2 a b c}{(d x + c) d^2} + \frac{2 a b \ln (d x + c)}{d^2} - \frac{b^2 c^2}{(d x + c) d^3} - \frac{2 b^2 c \ln (d x + c)}{d^3} + \frac{b^2 x}{d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(d*x+c)^2,x)

[Out] b^2*x/d^2-1/d/(d*x+c)*a^2+2/d^2/(d*x+c)*a*b*c-1/d^3/(d*x+c)*b^2*c^2+2*b/d^2*ln(d*x+c)*a-2*b^2/d^3*ln(d*x+c)*c

maxima [A] time = 1.35, size = 67, normalized size = 1.31

$$\frac{b^2 x}{d^2} - \frac{b^2 c^2 - 2 a b c d + a^2 d^2}{d^4 x + c d^3} - \frac{2 (b^2 c - a b d) \log (d x + c)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^2,x, algorithm="maxima")

[Out] $b^2x/d^2 - (b^2c^2 - 2ab^2cd + a^2d^2)/(d^4x + cd^3) - 2(b^2c - ab^2d)\log(dx + c)/d^3$

mupad [B] time = 0.24, size = 71, normalized size = 1.39

$$\frac{b^2x}{d^2} - \frac{a^2d^2 - 2abcd + b^2c^2}{d(xd^3 + cd^2)} - \frac{\ln(c + dx)(2b^2c - 2abd)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(c + d*x)^2,x)

[Out] $(b^2x)/d^2 - (a^2d^2 + b^2c^2 - 2ab^2cd)/(d(cd^2 + d^3x)) - (\log(c + dx))(2b^2c - 2ab^2d)/d^3$

sympy [A] time = 0.34, size = 60, normalized size = 1.18

$$\frac{b^2x}{d^2} + \frac{2b(ad - bc)\log(c + dx)}{d^3} + \frac{-a^2d^2 + 2abcd - b^2c^2}{cd^3 + d^4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(d*x+c)**2,x)

[Out] $b^2x/d^2 + 2b(ad - bc)\log(c + dx)/d^3 + (-a^2d^2 + 2abcd - b^2c^2)/(cd^3 + d^4x)$

$$3.1347 \quad \int \frac{a+bx}{(c+dx)^2} dx$$

Optimal. Leaf size=31

$$\frac{bc - ad}{d^2(c + dx)} + \frac{b \log(c + dx)}{d^2}$$

[Out] $(-a*d+b*c)/d^2/(d*x+c)+b*\ln(d*x+c)/d^2$

Rubi [A] time = 0.02, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{bc - ad}{d^2(c + dx)} + \frac{b \log(c + dx)}{d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(c + d*x)^2,x]

[Out] (b*c - a*d)/(d^2*(c + d*x)) + (b*Log[c + d*x])/d^2

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a + bx}{(c + dx)^2} dx &= \int \left(\frac{-bc + ad}{d(c + dx)^2} + \frac{b}{d(c + dx)} \right) dx \\ &= \frac{bc - ad}{d^2(c + dx)} + \frac{b \log(c + dx)}{d^2} \end{aligned}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 1.00

$$\frac{bc - ad}{d^2(c + dx)} + \frac{b \log(c + dx)}{d^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(c + d*x)^2,x]

[Out] $(b*c - a*d)/(d^2*(c + d*x)) + (b*\text{Log}[c + d*x])/d^2$

fricas [A] time = 0.43, size = 37, normalized size = 1.19

$$\frac{bc - ad + (bdx + bc) \log(dx + c)}{d^3x + cd^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)^2,x, algorithm="fricas")`

[Out] $(b*c - a*d + (b*d*x + b*c)*\log(d*x + c))/(d^3*x + c*d^2)$

giac [A] time = 1.26, size = 57, normalized size = 1.84

$$-\frac{b \left(\frac{\log\left(\frac{|dx+c|}{(dx+c)^2|d|}\right)}{d} - \frac{c}{(dx+c)d} \right)}{d} - \frac{a}{(dx+c)d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)^2,x, algorithm="giac")`

[Out] $-b*(\log(\text{abs}(d*x + c)/((d*x + c)^2*\text{abs}(d))))/d - c/((d*x + c)*d)/d - a/((d*x + c)*d)$

maple [A] time = 0.01, size = 39, normalized size = 1.26

$$-\frac{a}{(dx+c)d} + \frac{bc}{(dx+c)d^2} + \frac{b \ln(dx+c)}{d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/(d*x+c)^2,x)`

[Out] $-1/d/(d*x+c)*a+1/d^2/(d*x+c)*b*c+b*\ln(d*x+c)/d^2$

maxima [A] time = 1.34, size = 34, normalized size = 1.10

$$\frac{bc - ad}{d^3x + cd^2} + \frac{b \log(dx + c)}{d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)^2,x, algorithm="maxima")`

[Out] $(b*c - a*d)/(d^3*x + c*d^2) + b*\log(d*x + c)/d^2$

mupad [B] time = 0.04, size = 32, normalized size = 1.03

$$\frac{b \ln(c + dx)}{d^2} - \frac{ad - bc}{d^2 (c + dx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(c + d*x)^2,x)`

[Out] `(b*log(c + d*x))/d^2 - (a*d - b*c)/(d^2*(c + d*x))`

sympy [A] time = 0.19, size = 27, normalized size = 0.87

$$\frac{b \log(c + dx)}{d^2} + \frac{-ad + bc}{cd^2 + d^3x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)**2,x)`

[Out] `b*log(c + d*x)/d**2 + (-a*d + b*c)/(c*d**2 + d**3*x)`

$$3.1348 \quad \int \frac{1}{(c+dx)^2} dx$$

Optimal. Leaf size=12

$$-\frac{1}{d(c+dx)}$$

[Out] -1/d/(d*x+c)

Rubi [A] time = 0.00, antiderivative size = 12, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$-\frac{1}{d(c+dx)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(-2), x]

[Out] -(1/(d*(c + d*x)))

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(c+dx)^2} dx = -\frac{1}{d(c+dx)}$$

Mathematica [A] time = 0.00, size = 12, normalized size = 1.00

$$-\frac{1}{d(c+dx)}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(-2), x]

[Out] -(1/(d*(c + d*x)))

fricas [A] time = 0.42, size = 13, normalized size = 1.08

$$-\frac{1}{d^2x + cd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2,x, algorithm="fricas")

[Out] -1/(d^2*x + c*d)

giac [A] time = 1.23, size = 12, normalized size = 1.00

$$-\frac{1}{(dx + c)d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2,x, algorithm="giac")

[Out] -1/((d*x + c)*d)

maple [A] time = 0.00, size = 13, normalized size = 1.08

$$-\frac{1}{(dx + c)d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^2,x)

[Out] -1/d/(d*x+c)

maxima [A] time = 1.28, size = 12, normalized size = 1.00

$$-\frac{1}{(dx + c)d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2,x, algorithm="maxima")

[Out] -1/((d*x + c)*d)

mupad [B] time = 0.19, size = 12, normalized size = 1.00

$$-\frac{1}{d(c + dx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c + d*x)^2,x)

[Out] -1/(d*(c + d*x))

sympy [A] time = 0.13, size = 10, normalized size = 0.83

$$-\frac{1}{cd + d^2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)**2,x)

[Out] -1/(c*d + d**2*x)

$$3.1349 \quad \int \frac{1}{(a+bx)(c+dx)^2} dx$$

Optimal. Leaf size=56

$$\frac{1}{(c+dx)(bc-ad)} + \frac{b \log(a+bx)}{(bc-ad)^2} - \frac{b \log(c+dx)}{(bc-ad)^2}$$

[Out] 1/(-a*d+b*c)/(d*x+c)+b*ln(b*x+a)/(-a*d+b*c)^2-b*ln(d*x+c)/(-a*d+b*c)^2

Rubi [A] time = 0.03, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$\frac{1}{(c+dx)(bc-ad)} + \frac{b \log(a+bx)}{(bc-ad)^2} - \frac{b \log(c+dx)}{(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)*(c + d*x)^2), x]

[Out] 1/((b*c - a*d)*(c + d*x)) + (b*Log[a + b*x])/(b*c - a*d)^2 - (b*Log[c + d*x])/ (b*c - a*d)^2

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)(c+dx)^2} dx &= \int \left(\frac{b^2}{(bc-ad)^2(a+bx)} - \frac{d}{(bc-ad)(c+dx)^2} - \frac{bd}{(bc-ad)^2(c+dx)} \right) dx \\ &= \frac{1}{(bc-ad)(c+dx)} + \frac{b \log(a+bx)}{(bc-ad)^2} - \frac{b \log(c+dx)}{(bc-ad)^2} \end{aligned}$$

Mathematica [A] time = 0.03, size = 53, normalized size = 0.95

$$\frac{b(c+dx) \log(a+bx) - ad - b(c+dx) \log(c+dx) + bc}{(c+dx)(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*(c + d*x)^2),x]

[Out] (b*c - a*d + b*(c + d*x)*Log[a + b*x] - b*(c + d*x)*Log[c + d*x])/((b*c - a*d)^2*(c + d*x))

fricas [A] time = 0.46, size = 92, normalized size = 1.64

$$\frac{bc - ad + (bdx + bc) \log (bx + a) - (bdx + bc) \log (dx + c)}{b^2c^3 - 2abcd^2 + a^2cd^2 + (b^2c^2d - 2abcd^2 + a^2d^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^2,x, algorithm="fricas")

[Out] (b*c - a*d + (b*d*x + b*c)*log(b*x + a) - (b*d*x + b*c)*log(d*x + c))/(b^2*c^3 - 2*a*b*c^2*d + a^2*c*d^2 + (b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3)*x)

giac [A] time = 1.34, size = 77, normalized size = 1.38

$$\frac{bd \log \left(\left| b - \frac{bc}{dx+c} + \frac{ad}{dx+c} \right| \right)}{b^2c^2d - 2abcd^2 + a^2d^3} + \frac{d}{(bcd - ad^2)(dx + c)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^2,x, algorithm="giac")

[Out] b*d*log(abs(b - b*c/(d*x + c) + a*d/(d*x + c)))/(b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3) + d/((b*c*d - a*d^2)*(d*x + c))

maple [A] time = 0.01, size = 58, normalized size = 1.04

$$\frac{b \ln (bx + a)}{(ad - bc)^2} - \frac{b \ln (dx + c)}{(ad - bc)^2} - \frac{1}{(ad - bc)(dx + c)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)/(d*x+c)^2,x)

[Out] -1/(a*d-b*c)/(d*x+c)-b/(a*d-b*c)^2*ln(d*x+c)+b/(a*d-b*c)^2*ln(b*x+a)

maxima [A] time = 1.32, size = 90, normalized size = 1.61

$$\frac{b \log (bx + a)}{b^2c^2 - 2abcd + a^2d^2} - \frac{b \log (dx + c)}{b^2c^2 - 2abcd + a^2d^2} + \frac{1}{bc^2 - acd + (bcd - ad^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^2,x, algorithm="maxima")

[Out] $b \log(bx + a)/(b^2c^2 - 2a*bc*d + a^2d^2) - b \log(dx + c)/(b^2c^2 - 2a*bc*d + a^2d^2) + 1/(b^2c^2 - a*cd + (b*cd - a*d^2)*x)$

mupad [B] time = 0.29, size = 47, normalized size = 0.84

$$\frac{1}{(ad - bc)(c + dx)} - \frac{b \ln\left(\frac{c+dx}{a+bx}\right)}{(ad - bc)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)*(c + d*x)^2),x)

[Out] $-1/((a*d - b*c)*(c + d*x)) - (b \log((c + d*x)/(a + b*x)))/(a*d - b*c)^2$

sympy [B] time = 0.68, size = 233, normalized size = 4.16

$$\frac{b \log\left(x + \frac{\frac{a^3bd^3}{(ad-bc)^2} + \frac{3a^2b^2cd^2}{(ad-bc)^2} - \frac{3ab^3c^2d}{(ad-bc)^2} + abd + \frac{b^4c^3}{(ad-bc)^2} + b^2c}{(ad - bc)^2}\right) + b \log\left(x + \frac{\frac{a^3bd^3}{(ad-bc)^2} - \frac{3a^2b^2cd^2}{(ad-bc)^2} + \frac{3ab^3c^2d}{(ad-bc)^2} + abd - \frac{b^4c^3}{(ad-bc)^2} + b^2c}{(ad - bc)^2}\right)}{acd - bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)**2,x)

[Out] $-b \log(x + (-a**3*b*d**3/(a*d - b*c)**2 + 3*a**2*b**2*c*d**2/(a*d - b*c)**2 - 3*a*b**3*c**2*d/(a*d - b*c)**2 + a*b*d + b**4*c**3/(a*d - b*c)**2 + b**2*c)/(2*b**2*d))/(a*d - b*c)**2 + b \log(x + (a**3*b*d**3/(a*d - b*c)**2 - 3*a**2*b**2*c*d**2/(a*d - b*c)**2 + 3*a*b**3*c**2*d/(a*d - b*c)**2 + a*b*d - b**4*c**3/(a*d - b*c)**2 + b**2*c)/(2*b**2*d))/(a*d - b*c)**2 - 1/(a*c*d - b*c**2 + x*(a*d**2 - b*c*d))$

$$3.1350 \quad \int \frac{1}{(a+bx)^2(c+dx)^2} dx$$

Optimal. Leaf size=81

$$-\frac{b}{(a+bx)(bc-ad)^2} - \frac{d}{(c+dx)(bc-ad)^2} - \frac{2bd \log(a+bx)}{(bc-ad)^3} + \frac{2bd \log(c+dx)}{(bc-ad)^3}$$

[Out] $-b/(-a*d+b*c)^2/(b*x+a)-d/(-a*d+b*c)^2/(d*x+c)-2*b*d*\ln(b*x+a)/(-a*d+b*c)^3+2*b*d*\ln(d*x+c)/(-a*d+b*c)^3$

Rubi [A] time = 0.05, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$-\frac{b}{(a+bx)(bc-ad)^2} - \frac{d}{(c+dx)(bc-ad)^2} - \frac{2bd \log(a+bx)}{(bc-ad)^3} + \frac{2bd \log(c+dx)}{(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^2*(c + d*x)^2), x]

[Out] $-(b/((b*c - a*d)^2*(a + b*x))) - d/((b*c - a*d)^2*(c + d*x)) - (2*b*d*\text{Log}[a + b*x])/(b*c - a*d)^3 + (2*b*d*\text{Log}[c + d*x])/(b*c - a*d)^3$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{(a+bx)^2(c+dx)^2} dx = \int \left(\frac{b^2}{(bc-ad)^2(a+bx)^2} - \frac{2b^2d}{(bc-ad)^3(a+bx)} + \frac{d^2}{(bc-ad)^2(c+dx)^2} + \frac{2bd^2}{(bc-ad)^3(c+dx)} \right) dx$$

$$= -\frac{b}{(bc-ad)^2(a+bx)} - \frac{d}{(bc-ad)^2(c+dx)} - \frac{2bd \log(a+bx)}{(bc-ad)^3} + \frac{2bd \log(c+dx)}{(bc-ad)^3}$$

Mathematica [A] time = 0.07, size = 66, normalized size = 0.81

$$\frac{\frac{b(ad-bc)}{a+bx} + \frac{d(ad-bc)}{c+dx} - 2bd \log(a+bx) + 2bd \log(c+dx)}{(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*(c + d*x)^2), x]

[Out] ((b*(-(b*c) + a*d))/(a + b*x) + (d*(-(b*c) + a*d))/(c + d*x) - 2*b*d*Log[a + b*x] + 2*b*d*Log[c + d*x])/(b*c - a*d)^3

fricas [B] time = 0.45, size = 241, normalized size = 2.98

$$\frac{b^2c^2 - a^2d^2 + 2(b^2cd - abd^2)x + 2(b^2d^2x^2 + abcd + (b^2cd + abd^2)x) \log(bx + a) - 2(b^2d^2x^2 + abcd + (b^2cd + abd^2)x) \log(dx + c)}{ab^3c^4 - 3a^2b^2c^3d + 3a^3bc^2d^2 - a^4cd^3 + (b^4c^3d - 3ab^3c^2d^2 + 3a^2b^2cd^3 - a^3bd^4)x^2 + (b^4c^4 - 2ab^3c^3d + 2a^2b^2c^2d^2 - a^3b^2cd^3 - a^4d^4)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^2, x, algorithm="fricas")

[Out] -(b^2*c^2 - a^2*d^2 + 2*(b^2*c*d - a*b*d^2)*x + 2*(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)*log(b*x + a) - 2*(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)*log(d*x + c))/(a*b^3*c^4 - 3*a^2*b^2*c^3*d + 3*a^3*b*c^2*d^2 - a^4*c*d^3 + (b^4*c^3*d - 3*a*b^3*c^2*d^2 + 3*a^2*b^2*c*d^3 - a^3*b*d^4)*x^2 + (b^4*c^4 - 2*a*b^3*c^3*d + 2*a^3*b*c^2*d^2 - a^4*d^4)*x)

giac [A] time = 1.21, size = 153, normalized size = 1.89

$$\frac{2b^2d \log\left(\left|\frac{bc}{bx+a} - \frac{ad}{bx+a} + d\right|\right)}{b^4c^3 - 3ab^3c^2d + 3a^2b^2cd^2 - a^3bd^3} - \frac{b^3}{(b^4c^2 - 2ab^3cd + a^2b^2d^2)(bx + a)} + \frac{bd^2}{(bc - ad)^3 \left(\frac{bc}{bx+a} - \frac{ad}{bx+a} + d\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^2, x, algorithm="giac")

[Out] 2*b^2*d*log(abs(b*c/(b*x + a) - a*d/(b*x + a) + d))/(b^4*c^3 - 3*a*b^3*c^2*d + 3*a^2*b^2*c*d^2 - a^3*b*d^3) - b^3/((b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2)*(b*x + a)) + b*d^2/((b*c - a*d)^3*(b*c/(b*x + a) - a*d/(b*x + a) + d))

maple [A] time = 0.01, size = 82, normalized size = 1.01

$$\frac{2bd \ln(bx + a)}{(ad - bc)^3} - \frac{2bd \ln(dx + c)}{(ad - bc)^3} - \frac{b}{(ad - bc)^2 (bx + a)} - \frac{d}{(ad - bc)^2 (dx + c)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/(d*x+c)^2, x)

[Out] -d/(a*d-b*c)^2/(d*x+c) - 2*d/(a*d-b*c)^3*b*ln(d*x+c) - b/(a*d-b*c)^2/(b*x+a) + 2*d/(a*d-b*c)^3*b*ln(b*x+a)

maxima [B] time = 1.43, size = 208, normalized size = 2.57

$$\frac{2bd \log(bx + a)}{b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3} + \frac{2bd \log(dx + c)}{b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3} - \frac{2bd \log\left(\frac{c+dx}{a+bx}\right)}{ab^2c^3 - 2a^2bc^2d + a^3cd^2 + (b^3c^2d - 2ab^2c^2d + a^2bcd^2 - a^3d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^2,x, algorithm="maxima")

[Out] $-2*b*d*\log(b*x + a)/(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3) + 2*b*d*\log(d*x + c)/(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3) - (2*b*d*x + b*c + a*d)/(a*b^2*c^3 - 2*a^2*b*c^2*d + a^3*c*d^2 + (b^3*c^2*d - 2*a*b^2*c^2*d + a^2*b*d^3)*x^2 + (b^3*c^3 - a*b^2*c^2*d - a^2*b*c*d^2 + a^3*d^3)*x)$

mupad [B] time = 0.33, size = 74, normalized size = 0.91

$$\frac{1}{(ad - bc)(a + bx)(c + dx)} - \frac{2d}{(ad - bc)^2(c + dx)} - \frac{2bd \ln\left(\frac{c+dx}{a+bx}\right)}{(ad - bc)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^2*(c + d*x)^2),x)

[Out] $1/((a*d - b*c)*(a + b*x)*(c + d*x)) - (2*d)/((a*d - b*c)^2*(c + d*x)) - (2*b*d*\log((c + d*x)/(a + b*x)))/(a*d - b*c)^3$

sympy [B] time = 1.11, size = 406, normalized size = 5.01

$$\frac{2bd \log\left(x + \frac{-\frac{2a^4bd^5}{(ad-bc)^3} + \frac{8a^3b^2cd^4}{(ad-bc)^3} - \frac{12a^2b^3c^2d^3}{(ad-bc)^3} + \frac{8ab^4c^3d^2}{(ad-bc)^3} + 2abd^2 - \frac{2b^5c^4d}{(ad-bc)^3} + 2b^2cd}{4b^2d^2}\right)}{(ad - bc)^3} + \frac{2bd \log\left(x + \frac{\frac{2a^4bd^5}{(ad-bc)^3} - \frac{8a^3b^2cd^4}{(ad-bc)^3} + \frac{12a^2b^3c^2d^3}{(ad-bc)^3} - \frac{8ab^4c^3d^2}{(ad-bc)^3} + \frac{2b^5c^4d}{4b^2d^2}\right)}{(ad - bc)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2/(d*x+c)**2,x)

[Out] $-2*b*d*\log(x + (-2*a**4*b*d**5/(a*d - b*c)**3 + 8*a**3*b**2*c*d**4/(a*d - b*c)**3 - 12*a**2*b**3*c**2*d**3/(a*d - b*c)**3 + 8*a*b**4*c**3*d**2/(a*d - b*c)**3 + 2*a*b*d**2 - 2*b**5*c**4*d/(a*d - b*c)**3 + 2*b**2*c*d)/(4*b**2*d**2)))/(a*d - b*c)**3 + 2*b*d*\log(x + (2*a**4*b*d**5/(a*d - b*c)**3 - 8*a**3*b**2*c*d**4/(a*d - b*c)**3 + 12*a**2*b**3*c**2*d**3/(a*d - b*c)**3 - 8*a*b**4*c**3*d**2/(a*d - b*c)**3 + 2*a*b*d**2 + 2*b**5*c**4*d/(a*d - b*c)**3 + 2*b**2*c*d)/(4*b**2*d**2)))/(a*d - b*c)**3 + (-a*d - b*c - 2*b*d*x)/(a**3*c*d**2 - 2*a**2*b*c**2*d + a*b**2*c**3 + x**2*(a**2*b*d**3 - 2*a*b**2*c*d**2 + b**3*c**2*d) + x*(a**3*d**3 - a**2*b*c*d**2 - a*b**2*c**2*d + b**3*c**3))$

$$3.1351 \quad \int \frac{1}{(a+bx)^3(c+dx)^2} dx$$

Optimal. Leaf size=109

$$\frac{d^2}{(c+dx)(bc-ad)^3} + \frac{3bd^2 \log(a+bx)}{(bc-ad)^4} - \frac{3bd^2 \log(c+dx)}{(bc-ad)^4} + \frac{2bd}{(a+bx)(bc-ad)^3} - \frac{b}{2(a+bx)^2(bc-ad)^2}$$

[Out] $-1/2*b/(-a*d+b*c)^2/(b*x+a)^2+2*b*d/(-a*d+b*c)^3/(b*x+a)+d^2/(-a*d+b*c)^3/(d*x+c)+3*b*d^2*\ln(b*x+a)/(-a*d+b*c)^4-3*b*d^2*\ln(d*x+c)/(-a*d+b*c)^4$

Rubi [A] time = 0.08, antiderivative size = 109, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$\frac{d^2}{(c+dx)(bc-ad)^3} + \frac{3bd^2 \log(a+bx)}{(bc-ad)^4} - \frac{3bd^2 \log(c+dx)}{(bc-ad)^4} + \frac{2bd}{(a+bx)(bc-ad)^3} - \frac{b}{2(a+bx)^2(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^3*(c + d*x)^2), x]

[Out] $-b/(2*(b*c - a*d)^2*(a + b*x)^2) + (2*b*d)/((b*c - a*d)^3*(a + b*x)) + d^2/((b*c - a*d)^3*(c + d*x)) + (3*b*d^2*\text{Log}[a + b*x])/(b*c - a*d)^4 - (3*b*d^2*\text{Log}[c + d*x])/(b*c - a*d)^4$

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^3(c+dx)^2} dx &= \int \left(\frac{b^2}{(bc-ad)^2(a+bx)^3} - \frac{2b^2d}{(bc-ad)^3(a+bx)^2} + \frac{3b^2d^2}{(bc-ad)^4(a+bx)} - \frac{d^3}{(bc-ad)^3(c+dx)} \right. \\ &\quad \left. - \frac{b}{2(bc-ad)^2(a+bx)^2} + \frac{2bd}{(bc-ad)^3(a+bx)} + \frac{d^2}{(bc-ad)^3(c+dx)} + \frac{3bd^2 \log(a+bx)}{(bc-ad)^4} \right) dx \end{aligned}$$

Mathematica [A] time = 0.07, size = 98, normalized size = 0.90

$$\frac{\frac{2d^2(bc-ad)}{c+dx} + \frac{4bd(bc-ad)}{a+bx} - \frac{b(bc-ad)^2}{(a+bx)^2} + 6bd^2 \log(a+bx) - 6bd^2 \log(c+dx)}{2(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^3*(c + d*x)^2),x]

[Out]
$$\frac{-((b*(b*c - a*d)^2)/(a + b*x)^2) + (4*b*d*(b*c - a*d))/(a + b*x) + (2*d^2*(b*c - a*d))/(c + d*x) + 6*b*d^2*\text{Log}[a + b*x] - 6*b*d^2*\text{Log}[c + d*x]}{2*(b*c - a*d)^4}$$

fricas [B] time = 0.46, size = 494, normalized size = 4.53

$$\frac{b^3c^3 - 6ab^2c^2d + 3a^2bcd^2 + 2a^3d^3 - 6(b^3cd^2 - ab^2d^3)x^2 - 3(b^3c^2d + 2ab^2cd^2 - 3a^2bd^3)x - 6(b^3d^3x^3 + a^2bcd^3)}{2(a^2b^4c^5 - 4a^3b^3c^4d + 6a^4b^2c^3d^2 - 4a^5bc^2d^3 + a^6cd^4 + (b^6c^4d - 4ab^5c^3d^2 + 6a^2b^4c^2d^3 - 4a^3b^3cd^4 + a^4b^2d^5))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^2,x, algorithm="fricas")

[Out]
$$\begin{aligned} & -1/2*(b^3*c^3 - 6*a*b^2*c^2*d + 3*a^2*b*c*d^2 + 2*a^3*d^3 - 6*(b^3*c*d^2 - a*b^2*d^3))*x^2 - 3*(b^3*c^2*d + 2*a*b^2*c*d^2 - 3*a^2*b*d^3)*x - 6*(b^3*d^3*x^3 + a^2*b*c*d^2 + (b^3*c*d^2 + 2*a*b^2*d^3)*x^2 + (2*a*b^2*c*d^2 + a^2*b*d^3)*x)*\log(b*x + a) \\ & + 6*(b^3*d^3*x^3 + a^2*b*c*d^2 + (b^3*c*d^2 + 2*a*b^2*d^3)*x^2 + (2*a*b^2*c*d^2 + a^2*b*d^3)*x)*\log(d*x + c)/(a^2*b^4*c^5 - 4*a^3*b^3*c^4*d + 6*a^4*b^2*c^3*d^2 - 4*a^5*b*c^2*d^3 + a^6*c*d^4 + (b^6*c^4*d - 4*a*b^5*c^3*d^2 + 6*a^2*b^4*c^2*d^3 - 4*a^3*b^3*c*d^4 + a^4*b^2*d^5))*x^3 \\ & + (b^6*c^5 - 2*a*b^5*c^4*d - 2*a^2*b^4*c^3*d^2 + 8*a^3*b^3*c^2*d^3 - 7*a^4*b^2*c*d^4 + 2*a^5*b*d^5)*x^2 + (2*a*b^5*c^5 - 7*a^2*b^4*c^4*d + 8*a^3*b^3*c^3*d^2 - 2*a^4*b^2*c^2*d^3 - 2*a^5*b*c*d^4 + a^6*d^5)*x \end{aligned}$$

giac [B] time = 1.35, size = 216, normalized size = 1.98

$$\frac{3bd^3 \log\left(\left|b - \frac{bc}{dx+c} + \frac{ad}{dx+c}\right|\right)}{b^4c^4d - 4ab^3c^3d^2 + 6a^2b^2c^2d^3 - 4a^3bcd^4 + a^4d^5} + \frac{d^5}{(b^3c^3d^3 - 3ab^2c^2d^4 + 3a^2bcd^5 - a^3d^6)(dx+c)} + \frac{5b^3d^2 - 5b^2c^2d}{2(bc-ad)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^2,x, algorithm="giac")

[Out]
$$\frac{3*b*d^3*\log(\text{abs}(b - b*c/(d*x + c) + a*d/(d*x + c)))/(b^4*c^4*d - 4*a*b^3*c^3*d^2 + 6*a^2*b^2*c^2*d^3 - 4*a^3*b*c*d^4 + a^4*d^5) + d^5/((b^3*c^3*d^3 - 3*a*b^2*c^2*d^4 + 3*a^2*b*c*d^5 - a^3*d^6)*(d*x + c)) + 1/2*(5*b^3*d^2 - 6*(b^3*c*d^3 - a*b^2*d^4)/((d*x + c)*d))/(b*c - a*d)^4*(b - b*c/(d*x + c) + a*d/(d*x + c))^2}$$

maple [A] time = 0.01, size = 109, normalized size = 1.00

$$\frac{3bd^2 \ln(bx+a)}{(ad-bc)^4} - \frac{3bd^2 \ln(dx+c)}{(ad-bc)^4} - \frac{2bd}{(ad-bc)^3(bx+a)} - \frac{d^2}{(ad-bc)^3(dx+c)} - \frac{b}{2(ad-bc)^2(bx+a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^3/(d*x+c)^2,x)`

[Out] $-d^2/(a*d-b*c)^3/(d*x+c)-3*d^2/(a*d-b*c)^4*b*\ln(d*x+c)-1/2*b/(a*d-b*c)^2/(b*x+a)^2+3*d^2/(a*d-b*c)^4*b*\ln(b*x+a)-2*b/(a*d-b*c)^3*d/(b*x+a)$

maxima [B] time = 1.55, size = 386, normalized size = 3.54

$$\frac{3bd^2 \log(bx+a)}{b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4} - \frac{3bd^2 \log(dx+c)}{b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4} + \frac{1}{2(a^2b^3c^4 - 3a^3b^2c^3d + a^4d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^3/(d*x+c)^2,x, algorithm="maxima")`

[Out] $3*b*d^2*\log(b*x+a)/(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4) - 3*b*d^2*\log(d*x+c)/(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4) + 1/2*(6*b^2*d^2*x^2 - b^2*c^2 + 5*a*b*c*d + 2*a^2*d^2 + 3*(b^2*c*d + 3*a*b*d^2)*x)/(a^2*b^3*c^4 - 3*a^3*b^2*c^3*d + 3*a^4*b*c^2*d^2 - a^5*c*d^3 + (b^5*c^3*d - 3*a*b^4*c^2*d^2 + 3*a^2*b^3*c*d^3 - a^3*b^2*d^4)*x^3 + (b^5*c^4 - a*b^4*c^3*d - 3*a^2*b^3*c^2*d^2 + 5*a^3*b^2*c*d^3 - 2*a^4*b*d^4)*x^2 + (2*a*b^4*c^4 - 5*a^2*b^3*c^3*d + 3*a^3*b^2*c^2*d^2 + a^4*b*c*d^3 - a^5*d^4)*x)$

mupad [B] time = 0.40, size = 330, normalized size = 3.03

$$\frac{6bd^2 \operatorname{atanh}\left(\frac{a^4d^4 - 2a^3bcd^3 + 2ab^3c^3d - b^4c^4}{(ad-bc)^4} + \frac{2bdx(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)}{(ad-bc)^4}\right)}{(ad-bc)^4} - \frac{2a^2d^2 + 5abcd - b^2c^2}{2(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)} + \frac{1}{2(a^2b^3c^4 - 3a^3b^2c^3d + a^4d^4)} + \frac{1}{2(a^2b^3c^4 - 3a^3b^2c^3d + a^4d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a+b*x)^3*(c+d*x)^2),x)`

[Out] $(6*b*d^2*\operatorname{atanh}((a^4*d^4 - b^4*c^4 + 2*a*b^3*c^3*d - 2*a^3*b*c*d^3)/(a*d - b*c)^4 + (2*b*d*x*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2))/(a*d - b*c)^4))/(a*d - b*c)^4 - ((2*a^2*d^2 - b^2*c^2 + 5*a*b*c*d)/(2*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2)) + (3*d*x*(b^2*c + 3*a*b*d))/(2*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2)) + (3*b^2*d^2*x^2)/(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2))/(x*(a^2*d + 2*a*b*c) + a^2*c + x^2*(b^2*c + 2*a*b*d) + b^2*d*x^3)$

sympy [B] time = 1.72, size = 634, normalized size = 5.82

$$\frac{3bd^2 \log\left(x + \frac{-\frac{3a^5bd^7}{(ad-bc)^4} + \frac{15a^4b^2cd^6}{(ad-bc)^4} - \frac{30a^3b^3c^2d^5}{(ad-bc)^4} + \frac{30a^2b^4c^3d^4}{(ad-bc)^4} - \frac{15ab^5c^4d^3}{(ad-bc)^4} + 3abd^3 + \frac{3b^6c^5d^2}{(ad-bc)^4} + 3b^2cd^2}{6b^2d^3}\right)}{(ad-bc)^4} + \frac{3bd^2 \log\left(x + \frac{\frac{3a^5bd^7}{(ad-bc)^4} - \frac{15a^4b^2cd^6}{(ad-bc)^4} + \frac{30a^3b^3c^2d^5}{(ad-bc)^4} - \frac{30a^2b^4c^3d^4}{(ad-bc)^4} + \frac{15ab^5c^4d^3}{(ad-bc)^4} - 3abd^3 - \frac{3b^6c^5d^2}{(ad-bc)^4} - 3b^2cd^2}{6b^2d^3}\right)}{(ad-bc)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**3/(d*x+c)**2,x)

[Out] $-3*b*d**2*\log(x + (-3*a**5*b*d**7/(a*d - b*c)**4 + 15*a**4*b**2*c*d**6/(a*d - b*c)**4 - 30*a**3*b**3*c**2*d**5/(a*d - b*c)**4 + 30*a**2*b**4*c**3*d**4/(a*d - b*c)**4 - 15*a*b**5*c**4*d**3/(a*d - b*c)**4 + 3*a*b*d**3 + 3*b**6*c**5*d**2/(a*d - b*c)**4 + 3*b**2*c*d**2)/(6*b**2*d**3))/(a*d - b*c)**4 + 3*b*d**2*\log(x + (3*a**5*b*d**7/(a*d - b*c)**4 - 15*a**4*b**2*c*d**6/(a*d - b*c)**4 + 30*a**3*b**3*c**2*d**5/(a*d - b*c)**4 - 30*a**2*b**4*c**3*d**4/(a*d - b*c)**4 + 15*a*b**5*c**4*d**3/(a*d - b*c)**4 + 3*a*b*d**3 - 3*b**6*c**5*d**2/(a*d - b*c)**4 + 3*b**2*c*d**2)/(6*b**2*d**3))/(a*d - b*c)**4 + (-2*a**2*d**2 - 5*a*b*c*d + b**2*c**2 - 6*b**2*d**2*x**2 + x*(-9*a*b*d**2 - 3*b**2*c*d))/(2*a**5*c*d**3 - 6*a**4*b*c**2*d**2 + 6*a**3*b**2*c**3*d - 2*a**2*b**3*c**4 + x**3*(2*a**3*b**2*d**4 - 6*a**2*b**3*c*d**3 + 6*a*b**4*c**2*d**2 - 2*b**5*c**3*d) + x**2*(4*a**4*b*d**4 - 10*a**3*b**2*c*d**3 + 6*a**2*b**3*c**2*d**2 + 2*a*b**4*c**3*d - 2*b**5*c**4) + x*(2*a**5*d**4 - 2*a**4*b*c*d**3 - 6*a**3*b**2*c**2*d**2 + 10*a**2*b**3*c**3*d - 4*a*b**4*c**4))$

$$3.1352 \quad \int \frac{(a+bx)^6}{(c+dx)^3} dx$$

Optimal. Leaf size=158

$$\frac{2b^5(c+dx)^3(bc-ad)}{d^7} + \frac{15b^4(c+dx)^2(bc-ad)^2}{2d^7} - \frac{20b^3x(bc-ad)^3}{d^6} + \frac{15b^2(bc-ad)^4 \log(c+dx)}{d^7} + \frac{6b(bc-ad)^5}{d^7(c+dx)}$$

[Out] $-20*b^3*(-a*d+b*c)^3*x/d^6-1/2*(-a*d+b*c)^6/d^7/(d*x+c)^2+6*b*(-a*d+b*c)^5/d^7/(d*x+c)+15/2*b^4*(-a*d+b*c)^2*(d*x+c)^2/d^7-2*b^5*(-a*d+b*c)*(d*x+c)^3/d^7+1/4*b^6*(d*x+c)^4/d^7+15*b^2*(-a*d+b*c)^4*\ln(d*x+c)/d^7$

Rubi [A] time = 0.20, antiderivative size = 158, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{2b^5(c+dx)^3(bc-ad)}{d^7} + \frac{15b^4(c+dx)^2(bc-ad)^2}{2d^7} - \frac{20b^3x(bc-ad)^3}{d^6} + \frac{15b^2(bc-ad)^4 \log(c+dx)}{d^7} + \frac{6b(bc-ad)^5}{d^7(c+dx)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^6/(c + d*x)^3, x]

[Out] $(-20*b^3*(b*c - a*d)^3*x)/d^6 - (b*c - a*d)^6/(2*d^7*(c + d*x)^2) + (6*b*(b*c - a*d)^5)/(d^7*(c + d*x)) + (15*b^4*(b*c - a*d)^2*(c + d*x)^2)/(2*d^7) - (2*b^5*(b*c - a*d)*(c + d*x)^3)/d^7 + (b^6*(c + d*x)^4)/(4*d^7) + (15*b^2*(b*c - a*d)^4*Log[c + d*x])/d^7$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^6}{(c+dx)^3} dx &= \int \left(-\frac{20b^3(bc-ad)^3}{d^6} + \frac{(-bc+ad)^6}{d^6(c+dx)^3} - \frac{6b(bc-ad)^5}{d^6(c+dx)^2} + \frac{15b^2(bc-ad)^4}{d^6(c+dx)} + \frac{15b^4(bc-ad)^2(c+dx)}{d^6} \right. \\ &= -\frac{20b^3(bc-ad)^3x}{d^6} - \frac{(bc-ad)^6}{2d^7(c+dx)^2} + \frac{6b(bc-ad)^5}{d^7(c+dx)} + \frac{15b^4(bc-ad)^2(c+dx)^2}{2d^7} - \frac{2b^5(bc-ad)(c+dx)}{d^7} \end{aligned}$$

Mathematica [A] time = 0.11, size = 303, normalized size = 1.92

$$\frac{-2a^6d^6 - 12a^5bd^5(c + 2dx) + 30a^4b^2cd^4(3c + 4dx) + 40a^3b^3d^3(-5c^3 - 4c^2dx + 4cd^2x^2 + 2d^3x^3) + 30a^2b^4d^2(7c^4$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^6/(c + d*x)^3,x]

[Out] $(-2a^6d^6 - 12a^5b*d^5*(c + 2*d*x) + 30a^4*b^2*c*d^4*(3*c + 4*d*x) + 40a^3*b^3*d^3*(-5*c^3 - 4*c^2*d*x + 4*c*d^2*x^2 + 2*d^3*x^3) + 30a^2*b^4*d^2*(7*c^4 + 2*c^3*d*x - 11*c^2*d^2*x^2 - 4*c*d^3*x^3 + d^4*x^4) + 4a*b^5*d*(-27*c^5 + 6*c^4*d*x + 63*c^3*d^2*x^2 + 20*c^2*d^3*x^3 - 5*c*d^4*x^4 + 2*d^5*x^5) + b^6*(22*c^6 - 16*c^5*d*x - 68*c^4*d^2*x^2 - 20*c^3*d^3*x^3 + 5*c^2*d^4*x^4 - 2*c*d^5*x^5 + d^6*x^6) + 60*b^2*(b*c - a*d)^4*(c + d*x)^2*\text{Log}[c + d*x])/(4*d^7*(c + d*x)^2)$

fricas [B] time = 0.44, size = 548, normalized size = 3.47

$$\frac{b^6d^6x^6 + 22b^6c^6 - 108ab^5c^5d + 210a^2b^4c^4d^2 - 200a^3b^3c^3d^3 + 90a^4b^2c^2d^4 - 12a^5bcd^5 - 2a^6d^6 - 2(b^6cd^5 - 4ab^5c^4d + 6a^2b^4c^3d^2 - 4a^3b^3c^2d^3 + 2a^4b^2c^2d^4 - 2a^5bcd^5 - 2a^6d^6)}{d^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6/(d*x+c)^3,x, algorithm="fricas")

[Out] $\frac{1}{4}*(b^6*d^6*x^6 + 22*b^6*c^6 - 108*a*b^5*c^5*d + 210*a^2*b^4*c^4*d^2 - 200*a^3*b^3*c^3*d^3 + 90*a^4*b^2*c^2*d^4 - 12*a^5*b*c*d^5 - 2*a^6*d^6 - 2*(b^6*c*d^5 - 4*a*b^5*d^6)*x^5 + 5*(b^6*c^2*d^4 - 4*a*b^5*c*d^5 + 6*a^2*b^4*d^6)*x^4 - 20*(b^6*c^3*d^3 - 4*a*b^5*c^2*d^4 + 6*a^2*b^4*c*d^5 - 4*a^3*b^3*d^6)*x^3 - 2*(34*b^6*c^4*d^2 - 126*a*b^5*c^3*d^3 + 165*a^2*b^4*c^2*d^4 - 80*a^3*b^3*c*d^5)*x^2 - 4*(4*b^6*c^5*d - 6*a*b^5*c^4*d^2 - 15*a^2*b^4*c^3*d^3 + 40*a^3*b^3*c^2*d^4 - 30*a^4*b^2*c*d^5 + 6*a^5*b*d^6)*x + 60*(b^6*c^6 - 4*a*b^5*c^5*d + 6*a^2*b^4*c^4*d^2 - 4*a^3*b^3*c^3*d^3 + a^4*b^2*c^2*d^4 + (b^6*c^4*d^2 - 4*a*b^5*c^3*d^3 + 6*a^2*b^4*c^2*d^4 - 4*a^3*b^3*c*d^5 + a^4*b^2*d^6)*x^2 + 2*(b^6*c^5*d - 4*a*b^5*c^4*d^2 + 6*a^2*b^4*c^3*d^3 - 4*a^3*b^3*c^2*d^4 + a^4*b^2*c*d^5)*x)*\text{log}(d*x + c))/(d^9*x^2 + 2*c*d^8*x + c^2*d^7)$

giac [B] time = 1.28, size = 362, normalized size = 2.29

$$\frac{15(b^6c^4 - 4ab^5c^3d + 6a^2b^4c^2d^2 - 4a^3b^3cd^3 + a^4b^2d^4)\log(|dx + c|)}{d^7} + \frac{11b^6c^6 - 54ab^5c^5d + 105a^2b^4c^4d^2 - 100a^3b^3c^3d^3 + 30a^4b^2c^2d^4 - 12a^5bcd^5 - 2a^6d^6}{d^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6/(d*x+c)^3,x, algorithm="giac")

[Out] $15*(b^6*c^4 - 4*a*b^5*c^3*d + 6*a^2*b^4*c^2*d^2 - 4*a^3*b^3*c*d^3 + a^4*b^2*d^4)*\log(\text{abs}(d*x + c))/d^7 + 1/2*(11*b^6*c^6 - 54*a*b^5*c^5*d + 105*a^2*b^4*c^4*d^2 - 100*a^3*b^3*c^3*d^3 + 45*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 - a^6*d^6 + 12*(b^6*c^5*d - 5*a*b^5*c^4*d^2 + 10*a^2*b^4*c^3*d^3 - 10*a^3*b^3*c^2*d^4 + 5*a^4*b^2*c*d^5 - a^5*b*d^6)*x)/((d*x + c)^2*d^7) + 1/4*(b^6*d^9*x^4 - 4*b^6*c*d^8*x^3 + 8*a*b^5*d^9*x^3 + 12*b^6*c^2*d^7*x^2 - 36*a*b^5*c*d^8*x^2 + 30*a^2*b^4*d^9*x^2 - 40*b^6*c^3*d^6*x + 144*a*b^5*c^2*d^7*x - 180*a^2*b^4*c*d^8*x + 80*a^3*b^3*d^9*x)/d^12$

maple [B] time = 0.01, size = 464, normalized size = 2.94

$$\frac{b^6x^4}{4d^3} + \frac{2ab^5x^3}{d^3} - \frac{b^6cx^3}{d^4} - \frac{a^6}{2(dx+c)^2d} + \frac{3a^5bc}{(dx+c)^2d^2} - \frac{15a^4b^2c^2}{2(dx+c)^2d^3} + \frac{10a^3b^3c^3}{(dx+c)^2d^4} - \frac{15a^2b^4c^4}{2(dx+c)^2d^5} + \frac{15a^2b^4x^2}{2d^3} + \frac{3}{dx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^6/(d*x+c)^3,x)

[Out] $-1/2/d^7/(d*x+c)^2*b^6*c^6-6*b/d^2/(d*x+c)*a^5+6*b^6/d^7/(d*x+c)*c^5+15*b^2/d^3*\ln(d*x+c)*a^4+15*b^6/d^7*\ln(d*x+c)*c^4+20*b^3/d^3*a^3*x-10*b^6/d^6*c^3*x+3*b^6/d^5*x^2*c^2+15/2*b^4/d^3*x^2*a^2-b^6/d^4*x^3*c+2*b^5/d^3*x^3*a+3/d^2/(d*x+c)^2*a^5*b*c-15/2/d^3/(d*x+c)^2*a^4*b^2*c^2+10/d^4/(d*x+c)^2*a^3*b^3*c^3-15/2/d^5/(d*x+c)^2*a^2*b^4*c^4+3/d^6/(d*x+c)^2*a*b^5*c^5+36*b^5/d^5*a*c^2*x+30*b^2/d^3/(d*x+c)*a^4*c-60*b^3/d^4/(d*x+c)*a^3*c^2+60*b^4/d^5/(d*x+c)*a^2*c^3-30*b^5/d^6/(d*x+c)*a*c^4-9*b^5/d^4*x^2*a*c-45*b^4/d^4*a^2*c*x+1/4*b^6/d^3*x^4-1/2/d/(d*x+c)^2*a^6-60*b^5/d^6*\ln(d*x+c)*a*c^3-60*b^3/d^4*\ln(d*x+c)*a^3*c+90*b^4/d^5*\ln(d*x+c)*a^2*c^2$

maxima [B] time = 1.47, size = 364, normalized size = 2.30

$$\frac{11b^6c^6 - 54ab^5c^5d + 105a^2b^4c^4d^2 - 100a^3b^3c^3d^3 + 45a^4b^2c^2d^4 - 6a^5bcd^5 - a^6d^6 + 12(b^6c^5d - 5ab^5c^4d^2 + 10a^2b^4c^3d^3 - 10a^3b^3c^2d^4 + 5a^4b^2c^2d^5 - a^5b^2d^6)*x}{2(d^9x^2 + 2cd^8x + c^2d^7)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6/(d*x+c)^3,x, algorithm="maxima")

[Out] $1/2*(11*b^6*c^6 - 54*a*b^5*c^5*d + 105*a^2*b^4*c^4*d^2 - 100*a^3*b^3*c^3*d^3 + 45*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 - a^6*d^6 + 12*(b^6*c^5*d - 5*a*b^5*c^4*d^2 + 10*a^2*b^4*c^3*d^3 - 10*a^3*b^3*c^2*d^4 + 5*a^4*b^2*c*d^5 - a^5*b^2*d^6)*x)/(d^9*x^2 + 2*c*d^8*x + c^2*d^7) + 1/4*(b^6*d^3*x^4 - 4*(b^6*c*d^2 - 2*a*b^5*d^3)*x^3 + 6*(2*b^6*c^2*d - 6*a*b^5*c*d^2 + 5*a^2*b^4*d^3)*x^2 - 4*(10*b^6*c^3 - 36*a*b^5*c^2*d + 45*a^2*b^4*c*d^2 - 20*a^3*b^3*d^3)*x)/d^6 + 15*(b^6*c^4 - 4*a*b^5*c^3*d + 6*a^2*b^4*c^2*d^2 - 4*a^3*b^3*c*d^3 + a^4*b^2*d^4)*\log(d*x + c)/d^7$

mupad [B] time = 0.27, size = 441, normalized size = 2.79

$$x^3 \left(\frac{2ab^5}{d^3} - \frac{b^6c}{d^4} \right) - \frac{\frac{a^6d^6 + 6a^5bcd^5 - 45a^4b^2c^2d^4 + 100a^3b^3c^3d^3 - 105a^2b^4c^4d^2 + 54ab^5c^5d - 11b^6c^6}{2d}}{c^2d^6 + 2cd^7x + d^8x^2} - x \left(-6a^5bd^5 + 30a^4b^2cd^4 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^6/(c + d*x)^3,x)

[Out] $x^3 \left(\frac{2ab^5}{d^3} - \frac{b^6c}{d^4} \right) - \frac{(a^6d^6 - 11b^6c^6 - 105a^2b^4c^4d^2 + 100a^3b^3c^3d^3 - 45a^4b^2c^2d^4 + 54ab^5c^5d + 6a^5b^6c^6d^5)/(2d) - x(6b^6c^5 - 6a^5b^6d^5 + 30a^4b^2c^4d^4 + 60a^2b^4c^3d^2 - 60a^3b^3c^2d^3 - 30ab^5c^4d)}{(c^2d^6 + d^8x^2 + 2cd^7x) - x^2 \left(\frac{3c \left(\frac{6ab^5}{d^3} - \frac{3b^6c}{d^4} \right)}{(2d) - \frac{15a^2b^4}{(2d)^3} + \frac{3b^6c^2}{(2d)^5}} \right) + x \left(\frac{3c \left(\frac{3c \left(\frac{6ab^5}{d^3} - \frac{3b^6c}{d^4} \right)}{d} - \frac{15a^2b^4}{d^3} + \frac{3b^6c^2}{d^5} \right)}{d} + \frac{20a^3b^3}{d^3} - \frac{b^6c^3}{d^6} - \frac{3c^2 \left(\frac{6ab^5}{d^3} - \frac{3b^6c}{d^4} \right)}{d^2} + \log(c + dx) \left(\frac{15b^6c^4 + 15a^4b^2d^4 - 60a^3b^3cd^3 + 90a^2b^4c^2d^2 - 60ab^5c^3d \right)}{d^7} + \frac{b^6x^4}{4d^3} \right)$

sympy [B] time = 2.15, size = 340, normalized size = 2.15

$$\frac{b^6x^4}{4d^3} + \frac{15b^2(ad - bc)^4 \log(c + dx)}{d^7} + x^3 \left(\frac{2ab^5}{d^3} - \frac{b^6c}{d^4} \right) + x^2 \left(\frac{15a^2b^4}{2d^3} - \frac{9ab^5c}{d^4} + \frac{3b^6c^2}{d^5} \right) + x \left(\frac{20a^3b^3}{d^3} - \frac{45a^2b^4c}{d^4} + \frac{36a^4b^5c^2}{d^5} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**6/(d*x+c)**3,x)

[Out] $\frac{b^6x^4}{4d^3} + 15b^2(a*d - b*c)^4 \log(c + d*x)/d^7 + x^3 \left(\frac{2a^3b^3}{d^3} - \frac{b^6c}{d^4} \right) + x^2 \left(\frac{15a^2b^4}{(2d)^3} - \frac{9ab^5c}{d^4} + \frac{3b^6c^2}{d^5} \right) + x \left(\frac{20a^3b^3}{d^3} - \frac{45a^2b^4c}{d^4} + \frac{36a^4b^5c^2}{d^5} - \frac{10b^6c^3}{d^6} \right) + \frac{(-a^6d^6 - 6a^5b^6cd^5 + 45a^4b^6c^2d^4 - 100a^3b^3c^3d^3 + 105a^2b^4c^4d^2 - 54ab^5c^5d + 11b^6c^6d^5 + x(-12a^5b^6d^6 + 60a^4b^2c^5d^5 - 120a^3b^3c^2d^4 + 120a^2b^4c^3d^3 - 60ab^5c^4d^2 + 12b^6c^5d))}{(2c^2d^7 + 4cd^8x + 2d^9x^2)}$

$$3.1353 \quad \int \frac{(a+bx)^5}{(c+dx)^3} dx$$

Optimal. Leaf size=133

$$\frac{5b^4(c+dx)^2(bc-ad)}{2d^6} + \frac{10b^3x(bc-ad)^2}{d^5} - \frac{10b^2(bc-ad)^3 \log(c+dx)}{d^6} - \frac{5b(bc-ad)^4}{d^6(c+dx)} + \frac{(bc-ad)^5}{2d^6(c+dx)^2} + \frac{b^5(c+dx)^3}{3d^6}$$

[Out] $10*b^3*(-a*d+b*c)^2*x/d^5+1/2*(-a*d+b*c)^5/d^6/(d*x+c)^2-5*b*(-a*d+b*c)^4/d^6/(d*x+c)-5/2*b^4*(-a*d+b*c)*(d*x+c)^2/d^6+1/3*b^5*(d*x+c)^3/d^6-10*b^2*(-a*d+b*c)^3*\ln(d*x+c)/d^6$

Rubi [A] time = 0.12, antiderivative size = 133, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{5b^4(c+dx)^2(bc-ad)}{2d^6} + \frac{10b^3x(bc-ad)^2}{d^5} - \frac{10b^2(bc-ad)^3 \log(c+dx)}{d^6} - \frac{5b(bc-ad)^4}{d^6(c+dx)} + \frac{(bc-ad)^5}{2d^6(c+dx)^2} + \frac{b^5(c+dx)^3}{3d^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(c + d*x)^3, x]

[Out] $(10*b^3*(b*c - a*d)^2*x)/d^5 + (b*c - a*d)^5/(2*d^6*(c + d*x)^2) - (5*b*(b*c - a*d)^4)/(d^6*(c + d*x)) - (5*b^4*(b*c - a*d)*(c + d*x)^2)/(2*d^6) + (b^5*(c + d*x)^3)/(3*d^6) - (10*b^2*(b*c - a*d)^3*\text{Log}[c + d*x])/d^6$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(c+dx)^3} dx &= \int \left(\frac{10b^3(bc-ad)^2}{d^5} + \frac{(-bc+ad)^5}{d^5(c+dx)^3} + \frac{5b(bc-ad)^4}{d^5(c+dx)^2} - \frac{10b^2(bc-ad)^3}{d^5(c+dx)} - \frac{5b^4(bc-ad)(c+dx)}{d^5} + \right. \\ &= \frac{10b^3(bc-ad)^2x}{d^5} + \frac{(bc-ad)^5}{2d^6(c+dx)^2} - \frac{5b(bc-ad)^4}{d^6(c+dx)} - \frac{5b^4(bc-ad)(c+dx)^2}{2d^6} + \frac{b^5(c+dx)^3}{3d^6} - \frac{10b^2}{d^6} \end{aligned}$$

Mathematica [A] time = 0.07, size = 230, normalized size = 1.73

$$\frac{-3a^5d^5 - 15a^4bd^4(c+2dx) + 30a^3b^2cd^3(3c+4dx) + 30a^2b^3d^2(-5c^3 - 4c^2dx + 4cd^2x^2 + 2d^3x^3) + 15ab^4d(7c^4$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(c + d*x)^3,x]

[Out] $(-3a^5d^5 - 15a^4bd^4(c + 2dx) + 30a^3b^2cd^3(3c + 4dx) + 30a^2b^3d^2(-5c^3 - 4c^2dx + 4cd^2x^2 + 2d^3x^3) + 15ab^4d(7c^4 + 2c^3dx - 11c^2d^2x^2 - 4cd^3x^3 + d^4x^4) + b^5(-27c^5 + 6c^4dx + 63c^3d^2x^2 + 20c^2d^3x^3 - 5cd^4x^4 + 2d^5x^5) - 60b^2(bc - ad)^3(c + dx)^2 \text{Log}[c + dx]) / (6d^6(c + dx)^2)$

fricas [B] time = 0.48, size = 416, normalized size = 3.13

$$\frac{2b^5d^5x^5 - 27b^5c^5 + 105ab^4c^4d - 150a^2b^3c^3d^2 + 90a^3b^2c^2d^3 - 15a^4bcd^4 - 3a^5d^5 - 5(b^5cd^4 - 3ab^4d^5)x^4 + 20(b^5c^4d - 3a^4bd^5)x^3 + 3(21b^5c^3d^2 - 55a^2b^4c^2d^3 + 40a^2b^3cd^4)x^2 + 6(b^5c^4d + 5a^4bd^5)x - 60(b^5c^5 - 3a^2b^4c^4d + 3a^2b^3cd^4 - a^3b^2cd^5)x^2 + 2(b^5c^4d - 3a^2b^4c^3d^2 + 3a^2b^3cd^3 - a^3b^2cd^4)x \log(dx + c)}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^3,x, algorithm="fricas")

[Out] $1/6*(2b^5d^5x^5 - 27b^5c^5 + 105a^2b^4c^4d - 150a^2b^3c^3d^2 + 90a^3b^2c^2d^3 - 15a^4bcd^4 - 3a^5d^5 - 5(b^5cd^4 - 3a^2b^4d^5)x^4 + 20(b^5c^2d^3 - 3a^2b^4cd^4 + 3a^2b^3d^5)x^3 + 3(21b^5c^3d^2 - 55a^2b^4c^2d^3 + 40a^2b^3cd^4)x^2 + 6(b^5c^4d + 5a^4bd^5)x - 60(b^5c^5 - 3a^2b^4c^4d + 3a^2b^3cd^4 - a^3b^2cd^5)x^2 + (b^5c^3d^2 - 3a^2b^4c^2d^3 + 3a^2b^3cd^4 - a^3b^2cd^5)x^2 + 2(b^5c^4d - 3a^2b^4c^3d^2 + 3a^2b^3cd^3 - a^3b^2cd^4)x) \log(dx + c) / (d^8x^2 + 2cd^7x + c^2d^6)$

giac [B] time = 1.29, size = 264, normalized size = 1.98

$$\frac{10(b^5c^3 - 3ab^4c^2d + 3a^2b^3cd^2 - a^3b^2d^3) \log(|dx + c|) - 9b^5c^5 - 35ab^4c^4d + 50a^2b^3c^3d^2 - 30a^3b^2c^2d^3 + 5a^4bd^4}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^3,x, algorithm="giac")

[Out] $-10(b^5c^3 - 3a^2b^4c^2d + 3a^2b^3cd^2 - a^3b^2d^3) \log(\text{abs}(dx + c)) / d^6 - 1/2*(9b^5c^5 - 35a^2b^4c^4d + 50a^2b^3c^3d^2 - 30a^3b^2c^2d^3 + 5a^4bd^4 + a^5d^5 + 10(b^5c^4d - 4a^2b^4c^3d^2 + 6a^2b^3cd^3 - 4a^3b^2cd^4 + a^4bd^5)x) / ((dx + c)^2d^6) + 1/6*(2b^5d^6x^3 - 9b^5cd^5x^2 + 15a^2b^4d^6x^2 + 36b^5c^2d^4x - 90a^2b^4cd^5x + 60a^2b^3d^6x) / d^9$

maple [B] time = 0.01, size = 346, normalized size = 2.60

$$\frac{b^5 x^3}{3d^3} - \frac{a^5}{2(dx+c)^2 d} + \frac{5a^4 bc}{2(dx+c)^2 d^2} - \frac{5a^3 b^2 c^2}{(dx+c)^2 d^3} + \frac{5a^2 b^3 c^3}{(dx+c)^2 d^4} - \frac{5a b^4 c^4}{2(dx+c)^2 d^5} + \frac{5a b^4 x^2}{2d^3} + \frac{b^5 c^5}{2(dx+c)^2 d^6} - \frac{3b^5 c x^2}{2d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(d*x+c)^3,x)

[Out] $\frac{1}{3}b^5/d^3x^3 + 5/2b^4/d^3x^2a - 3/2b^5/d^4x^2c + 10b^3/d^3a^2x - 15b^4/d^4acx + 6b^5/d^5c^2x - 5b/d^2/(dx+c)a^4 + 20b^2/d^3/(dx+c)a^3c - 30b^3/d^4/(dx+c)a^2c^2 + 20b^4/d^5/(dx+c)a^2c^3 - 5b^5/d^6/(dx+c)c^4 + 10b^2/d^3\ln(dx+c)a^3 - 30b^3/d^4\ln(dx+c)a^2c + 30b^4/d^5\ln(dx+c)a^2c^2 - 10b^5/d^6\ln(dx+c)c^3 - 1/2/d/(dx+c)^2a^5 + 5/2/d^2/(dx+c)^2a^4bc - 5/d^3/(dx+c)^2a^3b^2c^2 + 5/d^4/(dx+c)^2a^2b^3c^3 - 5/2/d^5/(dx+c)^2ab^4c^4 + 1/2/d^6/(dx+c)^2b^5c^5$

maxima [B] time = 1.48, size = 271, normalized size = 2.04

$$\frac{9b^5c^5 - 35ab^4c^4d + 50a^2b^3c^3d^2 - 30a^3b^2c^2d^3 + 5a^4bcd^4 + a^5d^5 + 10(b^5c^4d - 4ab^4c^3d^2 + 6a^2b^3c^2d^3 - 4a^3b^2c^2d^3)}{2(d^8x^2 + 2cd^7x + c^2d^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^3,x, algorithm="maxima")

[Out] $\frac{-1/2*(9*b^5*c^5 - 35*a*b^4*c^4*d + 50*a^2*b^3*c^3*d^2 - 30*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 + a^5*d^5 + 10*(b^5*c^4*d - 4*a*b^4*c^3*d^2 + 6*a^2*b^3*c^2*d^3 - 4*a^3*b^2*c*d^4 + a^4*b*d^5)*x)/(d^8*x^2 + 2*c*d^7*x + c^2*d^6) + 1/6*(2*b^5*d^2*x^3 - 3*(3*b^5*c*d - 5*a*b^4*d^2)*x^2 + 6*(6*b^5*c^2 - 15*a*b^4*c*d + 10*a^2*b^3*d^2)*x)/d^5 - 10*(b^5*c^3 - 3*a*b^4*c^2*d + 3*a^2*b^3*c*d^2 - a^3*b^2*d^3)*\log(dx + c)/d^6$

mupad [B] time = 0.10, size = 291, normalized size = 2.19

$$x^2 \left(\frac{5ab^4}{2d^3} - \frac{3b^5c}{2d^4} \right) - \frac{a^5d^5 + 5a^4bcd^4 - 30a^3b^2c^2d^3 + 50a^2b^3c^3d^2 - 35ab^4c^4d + 9b^5c^5}{2d} + x \frac{(5a^4bd^4 - 20a^3b^2cd^3 + 30a^2b^3c^2d^2 - 20ab^4c^3d + 5a^5d^5)}{c^2d^5 + 2cd^6x + d^7x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/(c + d*x)^3,x)

[Out] $x^2*((5*a*b^4)/(2*d^3) - (3*b^5*c)/(2*d^4)) - ((a^5*d^5 + 9*b^5*c^5 + 50*a^2*b^3*c^3*d^2 - 30*a^3*b^2*c^2*d^3 - 35*a*b^4*c^4*d + 5*a^4*b*c*d^4)/(2*d)$

+ x*(5*b^5*c^4 + 5*a^4*b*d^4 - 20*a^3*b^2*c*d^3 + 30*a^2*b^3*c^2*d^2 - 20*a*b^4*c^3*d)/(c^2*d^5 + d^7*x^2 + 2*c*d^6*x) - x*((3*c*((5*a*b^4)/d^3 - (3*b^5*c)/d^4))/d - (10*a^2*b^3)/d^3 + (3*b^5*c^2)/d^5) - (log(c + d*x)*(10*b^5*c^3 - 10*a^3*b^2*d^3 + 30*a^2*b^3*c*d^2 - 30*a*b^4*c^2*d))/d^6 + (b^5*x^3)/(3*d^3)

sympy [B] time = 1.65, size = 258, normalized size = 1.94

$$\frac{b^5 x^3}{3d^3} + \frac{10b^2(ad - bc)^3 \log(c + dx)}{d^6} + x^2 \left(\frac{5ab^4}{2d^3} - \frac{3b^5c}{2d^4} \right) + x \left(\frac{10a^2b^3}{d^3} - \frac{15ab^4c}{d^4} + \frac{6b^5c^2}{d^5} \right) + \frac{-a^5d^5 - 5a^4bcd^4 + 30a^3b^2d^3}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/(d*x+c)**3,x)

[Out] b**5*x**3/(3*d**3) + 10*b**2*(a*d - b*c)**3*log(c + d*x)/d**6 + x**2*(5*a*b**4/(2*d**3) - 3*b**5*c/(2*d**4)) + x*(10*a**2*b**3/d**3 - 15*a*b**4*c/d**4 + 6*b**5*c**2/d**5) + (-a**5*d**5 - 5*a**4*b*c*d**4 + 30*a**3*b**2*c**2*d**3 - 50*a**2*b**3*c**3*d**2 + 35*a*b**4*c**4*d - 9*b**5*c**5 + x*(-10*a**4*b*d**5 + 40*a**3*b**2*c*d**4 - 60*a**2*b**3*c**2*d**3 + 40*a*b**4*c**3*d**2 - 10*b**5*c**4*d))/(2*c**2*d**6 + 4*c*d**7*x + 2*d**8*x**2)

$$3.1354 \quad \int \frac{(a+bx)^4}{(c+dx)^3} dx$$

Optimal. Leaf size=103

$$-\frac{b^3x(3bc-4ad)}{d^4} + \frac{6b^2(bc-ad)^2 \log(c+dx)}{d^5} + \frac{4b(bc-ad)^3}{d^5(c+dx)} - \frac{(bc-ad)^4}{2d^5(c+dx)^2} + \frac{b^4x^2}{2d^3}$$

[Out] $-b^3(-4ad+3bc)x/d^4+1/2b^4x^2/d^3-1/2(-ad+bc)^4/d^5/(d^2x+c)^2+4b(-ad+bc)^3/d^5/(d^2x+c)+6b^2(-ad+bc)^2 \ln(d^2x+c)/d^5$

Rubi [A] time = 0.09, antiderivative size = 103, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{b^3x(3bc-4ad)}{d^4} + \frac{6b^2(bc-ad)^2 \log(c+dx)}{d^5} + \frac{4b(bc-ad)^3}{d^5(c+dx)} - \frac{(bc-ad)^4}{2d^5(c+dx)^2} + \frac{b^4x^2}{2d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4/(c + d*x)^3,x]

[Out] $-((b^3(3bc-4ad)x)/d^4) + (b^4x^2)/(2d^3) - (b^3c - a^4)/(2d^5(c + d^2x)^2) + (4b^2(bc - ad)^3)/(d^5(c + d^2x)) + (6b^2(bc - a^2) \operatorname{Log}[c + d^2x])/d^5$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^4}{(c+dx)^3} dx &= \int \left(-\frac{b^3(3bc-4ad)}{d^4} + \frac{b^4x}{d^3} + \frac{(-bc+ad)^4}{d^4(c+dx)^3} - \frac{4b(bc-ad)^3}{d^4(c+dx)^2} + \frac{6b^2(bc-ad)^2}{d^4(c+dx)} \right) dx \\ &= -\frac{b^3(3bc-4ad)x}{d^4} + \frac{b^4x^2}{2d^3} - \frac{(bc-ad)^4}{2d^5(c+dx)^2} + \frac{4b(bc-ad)^3}{d^5(c+dx)} + \frac{6b^2(bc-ad)^2 \log(c+dx)}{d^5} \end{aligned}$$

Mathematica [A] time = 0.06, size = 167, normalized size = 1.62

$$\frac{-a^4d^4 - 4a^3bd^3(c+2dx) + 6a^2b^2cd^2(3c+4dx) + 4ab^3d(-5c^3 - 4c^2dx + 4cd^2x^2 + 2d^3x^3) + 12b^2(c+dx)^2(bc - \dots)}{2d^5(c+dx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4/(c + d*x)^3,x]

[Out]
$$\frac{-(a^4 d^4) - 4 a^3 b d^3 (c + 2 d x) + 6 a^2 b^2 c d^2 (3 c + 4 d x) + 4 a b^3 d (-5 c^3 - 4 c^2 d x + 4 c d^2 x^2 + 2 d^3 x^3) + b^4 (7 c^4 + 2 c^3 d x - 11 c^2 d^2 x^2 - 4 c d^3 x^3 + d^4 x^4) + 12 b^2 (b c - a d)^2 (c + d x)^2 \log[c + d x]}{(2 d^5 (c + d x)^2)}$$

fricas [B] time = 0.45, size = 291, normalized size = 2.83

$$b^4 d^4 x^4 + 7 b^4 c^4 - 20 a b^3 c^3 d + 18 a^2 b^2 c^2 d^2 - 4 a^3 b c d^3 - a^4 d^4 - 4 (b^4 c d^3 - 2 a b^3 d^4) x^3 - (11 b^4 c^2 d^2 - 16 a b^3 c d^3) x^2 -$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^3,x, algorithm="fricas")

[Out]
$$\frac{1/2 (b^4 d^4 x^4 + 7 b^4 c^4 - 20 a b^3 c^3 d + 18 a^2 b^2 c^2 d^2 - 4 a^3 b c d^3 - a^4 d^4 - 4 (b^4 c d^3 - 2 a b^3 d^4) x^3 - (11 b^4 c^2 d^2 - 16 a b^3 c d^3) x^2 + 2 (b^4 c^3 d - 8 a b^3 c^2 d^2 + 12 a^2 b^2 c d^3 - 4 a^3 b d^4) x + 12 (b^4 c^4 - 2 a b^3 c^3 d + a^2 b^2 c^2 d^2 + (b^4 c^2 d^2 - 2 a b^3 c d^3 + a^2 b^2 d^4) x^2 + 2 (b^4 c^3 d - 2 a b^3 c^2 d^2 + a^2 b^2 c d^3) x) \log(d x + c)}{(d^7 x^2 + 2 c d^6 x + c^2 d^5)}$$

giac [A] time = 1.35, size = 183, normalized size = 1.78

$$\frac{6 (b^4 c^2 - 2 a b^3 c d + a^2 b^2 d^2) \log(|d x + c|)}{d^5} + \frac{b^4 d^3 x^2 - 6 b^4 c d^2 x + 8 a b^3 d^3 x}{2 d^6} + \frac{7 b^4 c^4 - 20 a b^3 c^3 d + 18 a^2 b^2 c^2 d^2 - 4 a^3 b c d^3 - a^4 d^4}{2 d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^3,x, algorithm="giac")

[Out]
$$6 (b^4 c^2 - 2 a b^3 c d + a^2 b^2 d^2) \log(\text{abs}(d x + c)) / d^5 + 1/2 (b^4 d^3 x^2 - 6 b^4 c d^2 x + 8 a b^3 d^3 x) / d^6 + 1/2 (7 b^4 c^4 - 20 a b^3 c^3 d + 18 a^2 b^2 c^2 d^2 - 4 a^3 b c d^3 - a^4 d^4 + 8 (b^4 c^3 d - 3 a b^3 c^2 d^2 + 3 a^2 b^2 c d^3 - a^3 b d^4) x) / ((d x + c)^2 d^5)$$

maple [B] time = 0.01, size = 245, normalized size = 2.38

$$-\frac{a^4}{2 (d x + c)^2 d} + \frac{2 a^3 b c}{(d x + c)^2 d^2} - \frac{3 a^2 b^2 c^2}{(d x + c)^2 d^3} + \frac{2 a b^3 c^3}{(d x + c)^2 d^4} - \frac{b^4 c^4}{2 (d x + c)^2 d^5} + \frac{b^4 x^2}{2 d^3} - \frac{4 a^3 b}{(d x + c) d^2} + \frac{12 a^2 b^2 c}{(d x + c) d^3} + \frac{6 a^2 b^2 \ln}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4/(d*x+c)^3,x)

[Out] $\frac{1}{2}b^4x^2/d^3 + 4ab^3x/d^3 - 3b^4c/d^4 - 4b/d^2/(d*x+c)a^3 + 12b^2/d^3/(d*x+c)a^2c - 12b^3/d^4/(d*x+c)a^2c^2 + 4b^4/d^5/(d*x+c)c^3 + 6b^2/d^3 \ln(d*x+c)a^2 - 12b^3/d^4 \ln(d*x+c)a^2c + 6b^4/d^5 \ln(d*x+c)c^2 - 1/2/d/(d*x+c)^2 a^4 + 2/d^2/(d*x+c)^2 a^3bc - 3/d^3/(d*x+c)^2 a^2b^2c^2 + 2/d^4/(d*x+c)^2 ab^3c^3 - 1/2/d^5/(d*x+c)^2 b^4c^4$

maxima [A] time = 1.39, size = 191, normalized size = 1.85

$$\frac{7b^4c^4 - 20ab^3c^3d + 18a^2b^2c^2d^2 - 4a^3bcd^3 - a^4d^4 + 8(b^4c^3d - 3ab^3c^2d^2 + 3a^2b^2cd^3 - a^3bd^4)x}{2(d^7x^2 + 2cd^6x + c^2d^5)} + \frac{b^4dx^2 - 2(3b^4c^3d - 3ab^3c^2d^2 + 3a^2b^2cd^3 - a^3bd^4)x}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^3,x, algorithm="maxima")

[Out] $\frac{1}{2}(7b^4c^4 - 20ab^3c^3d + 18a^2b^2c^2d^2 - 4a^3bcd^3 - a^4d^4 + 8(b^4c^3d - 3ab^3c^2d^2 + 3a^2b^2cd^3 - a^3bd^4)x)/(d^7x^2 + 2cd^6x + c^2d^5) + \frac{1}{2}(b^4d^2x^2 - 2(3b^4c^3d - 4ab^3c^2d^2 + 3a^2b^2cd^3 - a^3bd^4)x)/d^4 + 6(b^4c^2 - 2ab^3cd + a^2b^2d^2) \log(dx + c)/d^5$

mupad [B] time = 0.10, size = 196, normalized size = 1.90

$$x \left(\frac{4ab^3}{d^3} - \frac{3b^4c}{d^4} \right) - \frac{a^4d^4 + 4a^3bcd^3 - 18a^2b^2c^2d^2 + 20ab^3c^3d - 7b^4c^4}{2d} - x \frac{(-4a^3bd^3 + 12a^2b^2cd^2 - 12ab^3c^2d + 4b^4c^3)}{c^2d^4 + 2cd^5x + d^6x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^4/(c + d*x)^3,x)

[Out] $x((4ab^3)/d^3 - (3b^4c)/d^4) - ((a^4d^4 - 7b^4c^4 - 18a^2b^2c^2d^2 + 20ab^3c^3d + 4a^3bcd^3)/(2d) - x(4b^4c^3 - 4a^3bd^3 + 12a^2b^2cd^2 - 12ab^3c^2d))/(c^2d^4 + d^6x^2 + 2cd^5x) + (b^4x^2)/(2d^3) + (\log(c + dx)(6b^4c^2 + 6a^2b^2d^2 - 12ab^3cd))/d^5$

sympy [A] time = 1.25, size = 185, normalized size = 1.80

$$\frac{b^4x^2}{2d^3} + \frac{6b^2(ad - bc)^2 \log(c + dx)}{d^5} + x \left(\frac{4ab^3}{d^3} - \frac{3b^4c}{d^4} \right) + \frac{-a^4d^4 - 4a^3bcd^3 + 18a^2b^2c^2d^2 - 20ab^3c^3d + 7b^4c^4 + x(-8a^4d^4 - 4a^3bcd^3 + 18a^2b^2c^2d^2 - 20ab^3c^3d + 7b^4c^4)}{2c^2d^5 + 4cd^6x + 2d^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4/(d*x+c)**3,x)

```
[Out] b**4*x**2/(2*d**3) + 6*b**2*(a*d - b*c)**2*log(c + d*x)/d**5 + x*(4*a*b**3/
d**3 - 3*b**4*c/d**4) + (-a**4*d**4 - 4*a**3*b*c*d**3 + 18*a**2*b**2*c**2*d
**2 - 20*a*b**3*c**3*d + 7*b**4*c**4 + x*(-8*a**3*b*d**4 + 24*a**2*b**2*c*d
**3 - 24*a*b**3*c**2*d**2 + 8*b**4*c**3*d))/(2*c**2*d**5 + 4*c*d**6*x + 2*d
**7*x**2)
```


$$3.1355 \quad \int \frac{(a+bx)^3}{(c+dx)^3} dx$$

Optimal. Leaf size=78

$$-\frac{3b^2(bc-ad)\log(c+dx)}{d^4} - \frac{3b(bc-ad)^2}{d^4(c+dx)} + \frac{(bc-ad)^3}{2d^4(c+dx)^2} + \frac{b^3x}{d^3}$$

[Out] $b^3x/d^3 + 1/2*(-a*d+b*c)^3/d^4/(d*x+c)^2 - 3*b*(-a*d+b*c)^2/d^4/(d*x+c) - 3*b^2*(-a*d+b*c)*\ln(d*x+c)/d^4$

Rubi [A] time = 0.06, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{3b^2(bc-ad)\log(c+dx)}{d^4} - \frac{3b(bc-ad)^2}{d^4(c+dx)} + \frac{(bc-ad)^3}{2d^4(c+dx)^2} + \frac{b^3x}{d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/(c + d*x)^3, x]

[Out] $(b^3x)/d^3 + (b*c - a*d)^3/(2*d^4*(c + d*x)^2) - (3*b*(b*c - a*d)^2)/(d^4*(c + d*x)) - (3*b^2*(b*c - a*d)*\text{Log}[c + d*x])/d^4$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{(c+dx)^3} dx &= \int \left(\frac{b^3}{d^3} + \frac{(-bc+ad)^3}{d^3(c+dx)^3} + \frac{3b(bc-ad)^2}{d^3(c+dx)^2} - \frac{3b^2(bc-ad)}{d^3(c+dx)} \right) dx \\ &= \frac{b^3x}{d^3} + \frac{(bc-ad)^3}{2d^4(c+dx)^2} - \frac{3b(bc-ad)^2}{d^4(c+dx)} - \frac{3b^2(bc-ad)\log(c+dx)}{d^4} \end{aligned}$$

Mathematica [A] time = 0.04, size = 114, normalized size = 1.46

$$\frac{-a^3d^3 - 3a^2bd^2(c+2dx) + 3ab^2cd(3c+4dx) - 6b^2(c+dx)^2(bc-ad)\log(c+dx) + b^3(-5c^3 - 4c^2dx + 4cd^2x^2 + 2d^4(c+dx)^2)}{2d^4(c+dx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/(c + d*x)^3,x]

[Out]
$$\frac{-(a^3 d^3) - 3 a^2 b d^2 (c + 2 d x) + 3 a b^2 c d (3 c + 4 d x) + b^3 (-5 c^3 - 4 c^2 d x + 4 c d^2 x^2 + 2 d^3 x^3) - 6 b^2 (b c - a d) (c + d x)^2 \log[c + d x]}{2 d^4 (c + d x)^2}$$

fricas [B] time = 0.43, size = 188, normalized size = 2.41

$$\frac{2 b^3 d^3 x^3 + 4 b^3 c d^2 x^2 - 5 b^3 c^3 + 9 a b^2 c^2 d - 3 a^2 b c d^2 - a^3 d^3 - 2 (2 b^3 c^2 d - 6 a b^2 c d^2 + 3 a^2 b d^3) x - 6 (b^3 c^3 - a b^2 c^2 d)}{2 (d^6 x^2 + 2 c d^5 x + c^2 d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^3,x, algorithm="fricas")

[Out]
$$\frac{1/2 * (2 * b^3 * d^3 * x^3 + 4 * b^3 * c * d^2 * x^2 - 5 * b^3 * c^3 + 9 * a * b^2 * c^2 * d - 3 * a^2 * b * c * d^2 - a^3 * d^3 - 2 * (2 * b^3 * c^2 * d - 6 * a * b^2 * c * d^2 + 3 * a^2 * b * d^3) * x - 6 * (b^3 * c^3 - a * b^2 * c^2 * d + (b^3 * c * d^2 - a * b^2 * d^3) * x^2 + 2 * (b^3 * c^2 * d - a * b^2 * c * d^2) * x) * \log(d * x + c))}{d^6 * x^2 + 2 * c * d^5 * x + c^2 * d^4}$$

giac [A] time = 1.28, size = 112, normalized size = 1.44

$$\frac{b^3 x}{d^3} - \frac{3 (b^3 c - a b^2 d) \log(|d x + c|)}{d^4} - \frac{5 b^3 c^3 - 9 a b^2 c^2 d + 3 a^2 b c d^2 + a^3 d^3 + 6 (b^3 c^2 d - 2 a b^2 c d^2 + a^2 b d^3) x}{2 (d x + c)^2 d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^3,x, algorithm="giac")

[Out]
$$b^3 x / d^3 - 3 * (b^3 * c - a * b^2 * d) * \log(\text{abs}(d * x + c)) / d^4 - 1/2 * (5 * b^3 * c^3 - 9 * a * b^2 * c^2 * d + 3 * a^2 * b * c * d^2 + a^3 * d^3 + 6 * (b^3 * c^2 * d - 2 * a * b^2 * c * d^2 + a^2 * b * d^3) * x) / ((d * x + c)^2 * d^4)$$

maple [B] time = 0.01, size = 160, normalized size = 2.05

$$-\frac{a^3}{2 (d x + c)^2 d} + \frac{3 a^2 b c}{2 (d x + c)^2 d^2} - \frac{3 a b^2 c^2}{2 (d x + c)^2 d^3} + \frac{b^3 c^3}{2 (d x + c)^2 d^4} - \frac{3 a^2 b}{(d x + c) d^2} + \frac{6 a b^2 c}{(d x + c) d^3} + \frac{3 a b^2 \ln (d x + c)}{d^3} - \frac{3 b^3 c}{(d x + c)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/(d*x+c)^3,x)

[Out]
$$b^3 / d^3 * x - 3 * b / d^2 / (d * x + c) * a^2 + 6 * b^2 / d^3 / (d * x + c) * a * c - 3 * b^3 / d^4 / (d * x + c) * c^2 + 3 * b^2 / d^3 * \ln (d * x + c) * a - 3 * b^3 / d^4 * \ln (d * x + c) * c - 1/2 / d / (d * x + c)^2 * a^3 + 3/2 / d^2 / (d * x + c)^2 * a^2 * b * c - 3/2 / d^3 / (d * x + c)^2 * a * b^2 * c^2 + 1/2 / d^4 / (d * x + c)^2 * b^3 * c^3$$

maxima [A] time = 1.34, size = 125, normalized size = 1.60

$$\frac{b^3 x}{d^3} - \frac{5b^3 c^3 - 9ab^2 c^2 d + 3a^2 b c d^2 + a^3 d^3 + 6(b^3 c^2 d - 2ab^2 c d^2 + a^2 b d^3)x}{2(d^6 x^2 + 2cd^5 x + c^2 d^4)} - \frac{3(b^3 c - ab^2 d) \log(dx + c)}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^3,x, algorithm="maxima")

[Out] $b^3 x/d^3 - 1/2*(5*b^3*c^3 - 9*a*b^2*c^2*d + 3*a^2*b*c*d^2 + a^3*d^3 + 6*(b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*x)/(d^6*x^2 + 2*c*d^5*x + c^2*d^4) - 3*(b^3*c - a*b^2*d)*\log(d*x + c)/d^4$

mupad [B] time = 0.11, size = 130, normalized size = 1.67

$$\frac{b^3 x}{d^3} - \frac{\ln(c + dx) (3b^3 c - 3a b^2 d)}{d^4} - \frac{\frac{a^3 d^3 + 3a^2 b c d^2 - 9a b^2 c^2 d + 5b^3 c^3}{2d} + x (3a^2 b d^2 - 6a b^2 c d + 3b^3 c^2)}{c^2 d^3 + 2c d^4 x + d^5 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3/(c + d*x)^3,x)

[Out] $(b^3*x)/d^3 - (\log(c + d*x)*(3*b^3*c - 3*a*b^2*d))/d^4 - ((a^3*d^3 + 5*b^3*c^3 - 9*a*b^2*c^2*d + 3*a^2*b*c*d^2)/(2*d) + x*(3*b^3*c^2 + 3*a^2*b*d^2 - 6*a*b^2*c*d))/(c^2*d^3 + d^5*x^2 + 2*c*d^4*x)$

sympy [A] time = 0.83, size = 128, normalized size = 1.64

$$\frac{b^3 x}{d^3} + \frac{3b^2(ad - bc) \log(c + dx)}{d^4} + \frac{-a^3 d^3 - 3a^2 b c d^2 + 9ab^2 c^2 d - 5b^3 c^3 + x(-6a^2 b d^3 + 12ab^2 c d^2 - 6b^3 c^2 d)}{2c^2 d^4 + 4cd^5 x + 2d^6 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3/(d*x+c)**3,x)

[Out] $b**3*x/d**3 + 3*b**2*(a*d - b*c)*\log(c + d*x)/d**4 + (-a**3*d**3 - 3*a**2*b*c*d**2 + 9*a*b**2*c**2*d - 5*b**3*c**3 + x*(-6*a**2*b*d**3 + 12*a*b**2*c*d**2 - 6*b**3*c**2*d))/(2*c**2*d**4 + 4*c*d**5*x + 2*d**6*x**2)$

$$3.1356 \quad \int \frac{(a+bx)^2}{(c+dx)^3} dx$$

Optimal. Leaf size=59

$$\frac{2b(bc-ad)}{d^3(c+dx)} - \frac{(bc-ad)^2}{2d^3(c+dx)^2} + \frac{b^2 \log(c+dx)}{d^3}$$

[Out] $-1/2*(-a*d+b*c)^2/d^3/(d*x+c)^2+2*b*(-a*d+b*c)/d^3/(d*x+c)+b^2*\ln(d*x+c)/d^3$

Rubi [A] time = 0.04, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{2b(bc-ad)}{d^3(c+dx)} - \frac{(bc-ad)^2}{2d^3(c+dx)^2} + \frac{b^2 \log(c+dx)}{d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(c + d*x)^3, x]

[Out] $-(b*c - a*d)^2/(2*d^3*(c + d*x)^2) + (2*b*(b*c - a*d))/(d^3*(c + d*x)) + (b^2*\text{Log}[c + d*x])/d^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(c+dx)^3} dx &= \int \left(\frac{(-bc+ad)^2}{d^2(c+dx)^3} - \frac{2b(bc-ad)}{d^2(c+dx)^2} + \frac{b^2}{d^2(c+dx)} \right) dx \\ &= -\frac{(bc-ad)^2}{2d^3(c+dx)^2} + \frac{2b(bc-ad)}{d^3(c+dx)} + \frac{b^2 \log(c+dx)}{d^3} \end{aligned}$$

Mathematica [A] time = 0.02, size = 48, normalized size = 0.81

$$\frac{\frac{(bc-ad)(ad+3bc+4bdx)}{(c+dx)^2} + 2b^2 \log(c+dx)}{2d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(c + d*x)^3,x]

[Out] (((b*c - a*d)*(3*b*c + a*d + 4*b*d*x))/(c + d*x)^2 + 2*b^2*Log[c + d*x])/(2*d^3)

fricas [A] time = 0.44, size = 100, normalized size = 1.69

$$\frac{3b^2c^2 - 2abcd - a^2d^2 + 4(b^2cd - abd^2)x + 2(b^2d^2x^2 + 2b^2cdx + b^2c^2)\log(dx + c)}{2(d^5x^2 + 2cd^4x + c^2d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^3,x, algorithm="fricas")

[Out] 1/2*(3*b^2*c^2 - 2*a*b*c*d - a^2*d^2 + 4*(b^2*c*d - a*b*d^2)*x + 2*(b^2*d^2*x^2 + 2*b^2*c*d*x + b^2*c^2)*log(d*x + c))/(d^5*x^2 + 2*c*d^4*x + c^2*d^3)

giac [A] time = 1.30, size = 69, normalized size = 1.17

$$\frac{b^2 \log(|dx + c|)}{d^3} + \frac{4(b^2c - abd)x + \frac{3b^2c^2 - 2abcd - a^2d^2}{d}}{2(dx + c)^2d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^3,x, algorithm="giac")

[Out] b^2*log(abs(d*x + c))/d^3 + 1/2*(4*(b^2*c - a*b*d)*x + (3*b^2*c^2 - 2*a*b*c*d - a^2*d^2)/d)/((d*x + c)^2*d^2)

maple [A] time = 0.01, size = 92, normalized size = 1.56

$$-\frac{a^2}{2(dx + c)^2d} + \frac{abc}{(dx + c)^2d^2} - \frac{b^2c^2}{2(dx + c)^2d^3} - \frac{2ab}{(dx + c)d^2} + \frac{2b^2c}{(dx + c)d^3} + \frac{b^2 \ln(dx + c)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(d*x+c)^3,x)

[Out] -2*b/d^2/(d*x+c)*a+2*b^2/d^3/(d*x+c)*c+b^2/d^3*ln(d*x+c)-1/2/d/(d*x+c)^2*a^2+1/d^2/(d*x+c)^2*a*b*c-1/2/d^3/(d*x+c)^2*b^2*c^2

maxima [A] time = 1.33, size = 80, normalized size = 1.36

$$\frac{3b^2c^2 - 2abcd - a^2d^2 + 4(b^2cd - abd^2)x}{2(d^5x^2 + 2cd^4x + c^2d^3)} + \frac{b^2 \log(dx + c)}{d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^3,x, algorithm="maxima")

[Out] $\frac{1}{2}*(3*b^2*c^2 - 2*a*b*c*d - a^2*d^2 + 4*(b^2*c*d - a*b*d^2)*x)/(d^5*x^2 + 2*c*d^4*x + c^2*d^3) + b^2*\log(d*x + c)/d^3$

mupad [B] time = 0.23, size = 77, normalized size = 1.31

$$\frac{b^2 \ln(c + dx)}{d^3} - \frac{\frac{a^2 d^2 + 2abcd - 3b^2 c^2}{2d^3} + \frac{2bx(ad - bc)}{d^2}}{c^2 + 2cdx + d^2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(c + d*x)^3,x)

[Out] $(b^2*\log(c + d*x))/d^3 - ((a^2*d^2 - 3*b^2*c^2 + 2*a*b*c*d)/(2*d^3) + (2*b*x*(a*d - b*c))/d^2)/(c^2 + d^2*x^2 + 2*c*d*x)$

sympy [A] time = 0.45, size = 80, normalized size = 1.36

$$\frac{b^2 \log(c + dx)}{d^3} + \frac{-a^2 d^2 - 2abcd + 3b^2 c^2 + x(-4abd^2 + 4b^2 cd)}{2c^2 d^3 + 4cd^4 x + 2d^5 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(d*x+c)**3,x)

[Out] $b**2*\log(c + d*x)/d**3 + (-a**2*d**2 - 2*a*b*c*d + 3*b**2*c**2 + x*(-4*a*b*d**2 + 4*b**2*c*d))/(2*c**2*d**3 + 4*c*d**4*x + 2*d**5*x**2)$

$$3.1357 \quad \int \frac{a+bx}{(c+dx)^3} dx$$

Optimal. Leaf size=28

$$\frac{(a+bx)^2}{2(c+dx)^2(bc-ad)}$$

[Out] 1/2*(b*x+a)^2/(-a*d+b*c)/(d*x+c)^2

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {37}

$$\frac{(a+bx)^2}{2(c+dx)^2(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(c + d*x)^3, x]

[Out] (a + b*x)^2/(2*(b*c - a*d)*(c + d*x)^2)

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{a+bx}{(c+dx)^3} dx = \frac{(a+bx)^2}{2(bc-ad)(c+dx)^2}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 0.93

$$-\frac{ad + b(c + 2dx)}{2d^2(c + dx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(c + d*x)^3, x]

[Out] -1/2*(a*d + b*(c + 2*d*x))/(d^2*(c + d*x)^2)

fricas [A] time = 0.45, size = 38, normalized size = 1.36

$$\frac{2 b d x + b c + a d}{2 \left(d^4 x^2 + 2 c d^3 x + c^2 d^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)^3,x, algorithm="fricas")

[Out] -1/2*(2*b*d*x + b*c + a*d)/(d^4*x^2 + 2*c*d^3*x + c^2*d^2)

giac [A] time = 1.25, size = 24, normalized size = 0.86

$$\frac{2 b d x + b c + a d}{2 (d x + c)^2 d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)^3,x, algorithm="giac")

[Out] -1/2*(2*b*d*x + b*c + a*d)/((d*x + c)^2*d^2)

maple [A] time = 0.00, size = 35, normalized size = 1.25

$$-\frac{b}{(d x + c) d^2} - \frac{a d - b c}{2 (d x + c)^2 d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/(d*x+c)^3,x)

[Out] -1/(d*x+c)*b/d^2-1/2*(a*d-b*c)/d^2/(d*x+c)^2

maxima [A] time = 1.36, size = 38, normalized size = 1.36

$$\frac{2 b d x + b c + a d}{2 \left(d^4 x^2 + 2 c d^3 x + c^2 d^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)^3,x, algorithm="maxima")

[Out] -1/2*(2*b*d*x + b*c + a*d)/(d^4*x^2 + 2*c*d^3*x + c^2*d^2)

mupad [B] time = 0.03, size = 39, normalized size = 1.39

$$-\frac{\frac{a d + b c}{2 d^2} + \frac{b x}{d}}{c^2 + 2 c d x + d^2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(c + d*x)^3,x)`

[Out] $-\frac{(a*d + b*c)}{(2*d^2)} + \frac{(b*x)/d}{(c^2 + d^2*x^2 + 2*c*d*x)}$

sympy [A] time = 0.26, size = 39, normalized size = 1.39

$$\frac{-ad - bc - 2bdx}{2c^2d^2 + 4cd^3x + 2d^4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)**3,x)`

[Out] $\frac{-a*d - b*c - 2*b*d*x}{(2*c**2*d**2 + 4*c*d**3*x + 2*d**4*x**2)}$

$$3.1358 \quad \int \frac{1}{(c+dx)^3} dx$$

Optimal. Leaf size=14

$$-\frac{1}{2d(c+dx)^2}$$

[Out] -1/2/d/(d*x+c)^2

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$-\frac{1}{2d(c+dx)^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(-3), x]

[Out] -1/(2*d*(c + d*x)^2)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(c+dx)^3} dx = -\frac{1}{2d(c+dx)^2}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\frac{1}{2d(c+dx)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(-3), x]

[Out] -1/2*1/(d*(c + d*x)^2)

fricas [A] time = 0.43, size = 24, normalized size = 1.71

$$-\frac{1}{2(d^3x^2 + 2cd^2x + c^2d)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^3,x, algorithm="fricas")

[Out] -1/2/(d^3*x^2 + 2*c*d^2*x + c^2*d)

giac [A] time = 1.20, size = 12, normalized size = 0.86

$$-\frac{1}{2(dx+c)^2d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^3,x, algorithm="giac")

[Out] -1/2/((d*x + c)^2*d)

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$-\frac{1}{2(dx+c)^2d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^3,x)

[Out] -1/2/d/(d*x+c)^2

maxima [A] time = 1.34, size = 12, normalized size = 0.86

$$-\frac{1}{2(dx+c)^2d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^3,x, algorithm="maxima")

[Out] -1/2/((d*x + c)^2*d)

mupad [B] time = 0.02, size = 26, normalized size = 1.86

$$-\frac{1}{2c^2d + 4cd^2x + 2d^3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c + d*x)^3,x)

[Out] -1/(2*c^2*d + 2*d^3*x^2 + 4*c*d^2*x)

sympy [B] time = 0.18, size = 26, normalized size = 1.86

$$-\frac{1}{2c^2d + 4cd^2x + 2d^3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)**3,x)

[Out] -1/(2*c**2*d + 4*c*d**2*x + 2*d**3*x**2)

$$3.1359 \quad \int \frac{1}{(a+bx)(c+dx)^3} dx$$

Optimal. Leaf size=82

$$\frac{b^2 \log(a+bx)}{(bc-ad)^3} - \frac{b^2 \log(c+dx)}{(bc-ad)^3} + \frac{b}{(c+dx)(bc-ad)^2} + \frac{1}{2(c+dx)^2(bc-ad)}$$

[Out] 1/2/(-a*d+b*c)/(d*x+c)^2+b/(-a*d+b*c)^2/(d*x+c)+b^2*ln(b*x+a)/(-a*d+b*c)^3-b^2*ln(d*x+c)/(-a*d+b*c)^3

Rubi [A] time = 0.05, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$\frac{b^2 \log(a+bx)}{(bc-ad)^3} - \frac{b^2 \log(c+dx)}{(bc-ad)^3} + \frac{b}{(c+dx)(bc-ad)^2} + \frac{1}{2(c+dx)^2(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)*(c + d*x)^3), x]

[Out] 1/(2*(b*c - a*d)*(c + d*x)^2) + b/((b*c - a*d)^2*(c + d*x)) + (b^2*Log[a + b*x])/(b*c - a*d)^3 - (b^2*Log[c + d*x])/(b*c - a*d)^3

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)(c+dx)^3} dx &= \int \left(\frac{b^3}{(bc-ad)^3(a+bx)} - \frac{d}{(bc-ad)(c+dx)^3} - \frac{bd}{(bc-ad)^2(c+dx)^2} - \frac{b^2d}{(bc-ad)^3(c+dx)} \right) dx \\ &= \frac{1}{2(bc-ad)(c+dx)^2} + \frac{b}{(bc-ad)^2(c+dx)} + \frac{b^2 \log(a+bx)}{(bc-ad)^3} - \frac{b^2 \log(c+dx)}{(bc-ad)^3} \end{aligned}$$

Mathematica [A] time = 0.05, size = 67, normalized size = 0.82

$$\frac{2b^2 \log(a+bx) + \frac{(bc-ad)(-ad+3bc+2bdx)}{(c+dx)^2} - 2b^2 \log(c+dx)}{2(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*(c + d*x)^3),x]

[Out] (((b*c - a*d)*(3*b*c - a*d + 2*b*d*x))/(c + d*x)^2 + 2*b^2*Log[a + b*x] - 2*b^2*Log[c + d*x])/(2*(b*c - a*d)^3)

fricas [B] time = 0.44, size = 242, normalized size = 2.95

$$\frac{3b^2c^2 - 4abcd + a^2d^2 + 2(b^2cd - abd^2)x + 2(b^2d^2x^2 + 2b^2cdx + b^2c^2) \log(bx + a) - 2(b^2d^2x^2 + 2b^2cdx + b^2c^2) \log(c + dx)}{2(b^3c^5 - 3ab^2c^4d + 3a^2bc^3d^2 - a^3c^2d^3 + (b^3c^3d^2 - 3ab^2c^2d^3 + 3a^2bcd^4 - a^3d^5)x^2 + 2(b^3c^4d - 3ab^2c^3d^2 + 3a^2bcd^3 - a^3c^2d^3)x + 2(b^3c^5 - 3ab^2c^4d + 3a^2bc^3d^2 - a^3c^2d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^3,x, algorithm="fricas")

[Out] 1/2*(3*b^2*c^2 - 4*a*b*c*d + a^2*d^2 + 2*(b^2*c*d - a*b*d^2)*x + 2*(b^2*d^2*x^2 + 2*b^2*c*d*x + b^2*c^2)*log(b*x + a) - 2*(b^2*d^2*x^2 + 2*b^2*c*d*x + b^2*c^2)*log(d*x + c))/(b^3*c^5 - 3*a*b^2*c^4*d + 3*a^2*b*c^3*d^2 - a^3*c^2*d^3 + (b^3*c^3*d^2 - 3*a*b^2*c^2*d^3 + 3*a^2*b*c*d^4 - a^3*d^5)*x^2 + 2*(b^3*c^4*d - 3*a*b^2*c^3*d^2 + 3*a^2*b*c^2*d^3 - a^3*c*d^4)*x)

giac [B] time = 1.36, size = 165, normalized size = 2.01

$$\frac{b^3 \log(|bx + a|)}{b^4c^3 - 3ab^3c^2d + 3a^2b^2cd^2 - a^3bd^3} - \frac{b^2d \log(|dx + c|)}{b^3c^3d - 3ab^2c^2d^2 + 3a^2bcd^3 - a^3d^4} + \frac{3b^2c^2 - 4abcd + a^2d^2 + 2(b^2cd - abc^2)}{2(bc - ad)^3(dx + c)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^3,x, algorithm="giac")

[Out] b^3*log(abs(b*x + a))/(b^4*c^3 - 3*a*b^3*c^2*d + 3*a^2*b^2*c*d^2 - a^3*b*d^3) - b^2*d*log(abs(d*x + c))/(b^3*c^3*d - 3*a*b^2*c^2*d^2 + 3*a^2*b*c*d^3 - a^3*d^4) + 1/2*(3*b^2*c^2 - 4*a*b*c*d + a^2*d^2 + 2*(b^2*c*d - a*b*d^2)*x)/(b*c - a*d)^3*(d*x + c)^2)

maple [A] time = 0.01, size = 81, normalized size = 0.99

$$-\frac{b^2 \ln(bx + a)}{(ad - bc)^3} + \frac{b^2 \ln(dx + c)}{(ad - bc)^3} + \frac{b}{(ad - bc)^2(dx + c)} - \frac{1}{2(ad - bc)(dx + c)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)/(d*x+c)^3,x)

[Out] -1/2/(a*d-b*c)/(d*x+c)^2+b^2/(a*d-b*c)^3*ln(d*x+c)+b/(a*d-b*c)^2/(d*x+c)-b^2/(a*d-b*c)^3*ln(b*x+a)

maxima [B] time = 1.45, size = 202, normalized size = 2.46

$$\frac{b^2 \log(bx + a)}{b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3} - \frac{b^2 \log(dx + c)}{b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3} + \frac{2bd}{2(b^2c^4 - 2abc^3d + a^2c^2d^2 + (b^2c^2d^2 - 2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^3,x, algorithm="maxima")

[Out] $b^2 \log(bx + a) / (b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3) - b^2 \log(dx + c) / (b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3) + 1/2 * (2b^2 * d * x + 3b^2 * c - a * d) / (b^2 * c^4 - 2a * b * c^3 * d + a^2 * c^2 * d^2 + (b^2 * c^2 * d^2 - 2a * b * c * d^3 + a^2 * d^4) * x^2 + 2 * (b^2 * c^3 * d - 2a * b * c^2 * d^2 + a^2 * c * d^3) * x)$

mupad [B] time = 0.30, size = 183, normalized size = 2.23

$$\frac{\frac{ad-3bc}{2(a^2d^2-2abcd+b^2c^2)} - \frac{bdx}{a^2d^2-2abcd+b^2c^2}}{c^2 + 2cdx + d^2x^2} - \frac{2b^2 \operatorname{atanh}\left(\frac{a^3d^3 - a^2bcd^2 - ab^2c^2d + b^3c^3}{(ad-bc)^3} + \frac{2bdx(a^2d^2 - 2abcd + b^2c^2)}{(ad-bc)^3}\right)}{(ad-bc)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)*(c + d*x)^3),x)

[Out] $-((ad - 3bc) / (2(a^2d^2 + b^2c^2 - 2ab^2cd))) - (bdx) / (a^2d^2 + b^2c^2 - 2ab^2cd) / (c^2 + d^2x^2 + 2cdx) - (2b^2 \operatorname{atanh}((a^3d^3 + b^3c^3 - ab^2c^2d - a^2bcd^2) / (ad - bc)^3 + (2bdx * (a^2d^2 + b^2c^2 - 2ab^2cd)) / (ad - bc)^3)) / (ad - bc)^3$

sympy [B] time = 1.07, size = 381, normalized size = 4.65

$$\frac{b^2 \log\left(x + \frac{\frac{a^4b^2d^4}{(ad-bc)^3} + \frac{4a^3b^3cd^3}{(ad-bc)^3} - \frac{6a^2b^4c^2d^2}{(ad-bc)^3} + \frac{4ab^5c^3d}{(ad-bc)^3} + ab^2d - \frac{b^6c^4}{(ad-bc)^3} + b^3c}{2b^3d}\right)}{(ad-bc)^3} - \frac{b^2 \log\left(x + \frac{\frac{a^4b^2d^4}{(ad-bc)^3} - \frac{4a^3b^3cd^3}{(ad-bc)^3} + \frac{6a^2b^4c^2d^2}{(ad-bc)^3} - \frac{4ab^5c^3d}{(ad-bc)^3} + ab^2d + \frac{b^6c^4}{(ad-bc)^3} + b^3c}{2b^3d}\right)}{(ad-bc)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)**3,x)

[Out] $b^2 \log(x + (-a^4b^2d^4 / (ad - bc)^3 + 4a^3b^3cd^3 / (ad - bc)^3 - 6a^2b^4c^2d^2 / (ad - bc)^3 + 4ab^5c^3d / (ad - bc)^3 + a^2b^2d - b^6c^4 / (ad - bc)^3 + b^3c) / (2b^3d)) / (ad - bc)^3 - b^2 \log(x + (a^4b^2d^4 / (ad - bc)^3 - 4a^3b^3cd^3 / (ad - bc)^3 + 6a^2b^4c^2d^2 / (ad - bc)^3 - 4ab^5c^3d / (ad - bc)^3 + ab^2d + b^6c^4 / (ad - bc)^3 + b^3c) / (2b^3d)) / (ad - bc)^3$

$$\begin{aligned} & *c)^{**3} + a*b^{**2}*d + b^{**6}*c^{**4}/(a*d - b*c)^{**3} + b^{**3}*c)/(2*b^{**3}*d))/(a*d - b \\ & *c)^{**3} + (-a*d + 3*b*c + 2*b*d*x)/(2*a^{**2}*c^{**2}*d^{**2} - 4*a*b*c^{**3}*d + 2*b^{**2} \\ & *c^{**4} + x^{**2}*(2*a^{**2}*d^{**4} - 4*a*b*c*d^{**3} + 2*b^{**2}*c^{**2}*d^{**2}) + x*(4*a^{**2}*c* \\ & d^{**3} - 8*a*b*c^{**2}*d^{**2} + 4*b^{**2}*c^{**3}*d)) \end{aligned}$$

$$3.1360 \quad \int \frac{1}{(a+bx)^2(c+dx)^3} dx$$

Optimal. Leaf size=110

$$\frac{b^2}{(a+bx)(bc-ad)^3} - \frac{3b^2d \log(a+bx)}{(bc-ad)^4} + \frac{3b^2d \log(c+dx)}{(bc-ad)^4} - \frac{2bd}{(c+dx)(bc-ad)^3} - \frac{d}{2(c+dx)^2(bc-ad)^2}$$

[Out] $-b^2/(-a*d+b*c)^3/(b*x+a)-1/2*d/(-a*d+b*c)^2/(d*x+c)^2-2*b*d/(-a*d+b*c)^3/(d*x+c)-3*b^2*d*\ln(b*x+a)/(-a*d+b*c)^4+3*b^2*d*\ln(d*x+c)/(-a*d+b*c)^4$

Rubi [A] time = 0.07, antiderivative size = 110, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$\frac{b^2}{(a+bx)(bc-ad)^3} - \frac{3b^2d \log(a+bx)}{(bc-ad)^4} + \frac{3b^2d \log(c+dx)}{(bc-ad)^4} - \frac{2bd}{(c+dx)(bc-ad)^3} - \frac{d}{2(c+dx)^2(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^2*(c + d*x)^3), x]

[Out] $-(b^2/((b*c - a*d)^3*(a + b*x))) - d/(2*(b*c - a*d)^2*(c + d*x)^2) - (2*b*d)/((b*c - a*d)^3*(c + d*x)) - (3*b^2*d*\text{Log}[a + b*x])/(b*c - a*d)^4 + (3*b^2*d*\text{Log}[c + d*x])/(b*c - a*d)^4$

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^2(c+dx)^3} dx &= \int \left(\frac{b^3}{(bc-ad)^3(a+bx)^2} - \frac{3b^3d}{(bc-ad)^4(a+bx)} + \frac{d^2}{(bc-ad)^2(c+dx)^3} + \frac{2bd^2}{(bc-ad)^3(c+dx)} \right) dx \\ &= -\frac{b^2}{(bc-ad)^3(a+bx)} - \frac{d}{2(bc-ad)^2(c+dx)^2} - \frac{2bd}{(bc-ad)^3(c+dx)} - \frac{3b^2d \log(a+bx)}{(bc-ad)^4} \end{aligned}$$

Mathematica [A] time = 0.10, size = 97, normalized size = 0.88

$$\frac{\frac{2b^2(bc-ad)}{a+bx} + 6b^2d \log(a+bx) + \frac{4bd(bc-ad)}{c+dx} + \frac{d(bc-ad)^2}{(c+dx)^2} - 6b^2d \log(c+dx)}{2(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*(c + d*x)^3),x]

[Out]
$$-1/2*((2*b^2*(b*c - a*d))/(a + b*x) + (d*(b*c - a*d)^2)/(c + d*x)^2 + (4*b*d*(b*c - a*d))/(c + d*x) + 6*b^2*d*Log[a + b*x] - 6*b^2*d*Log[c + d*x])/(b*c - a*d)^4$$

fricas [B] time = 0.47, size = 495, normalized size = 4.50

$$\frac{2b^3c^3 + 3ab^2c^2d - 6a^2bcd^2 + a^3d^3 + 6(b^3cd^2 - ab^2d^3)x^2 + 3(3b^3c^2d - 2ab^2cd^2 - a^2bd^3)x + 6(b^3d^3x^3 + ab^2d^3x^2 + a^2bd^3x + a^3d^3)}{2(ab^4c^6 - 4a^2b^3c^5d + 6a^3b^2c^4d^2 - 4a^4bc^3d^3 + a^5c^2d^4 + (b^5c^4d^2 - 4ab^4c^3d^3 + 6a^2b^3c^2d^4 - 4a^3b^2cd^5 + a^4bd^6))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^3,x, algorithm="fricas")

[Out]
$$-1/2*(2*b^3*c^3 + 3*a*b^2*c^2*d - 6*a^2*b*c*d^2 + a^3*d^3 + 6*(b^3*c*d^2 - a*b^2*d^3))*x^2 + 3*(3*b^3*c^2*d - 2*a*b^2*c*d^2 - a^2*b*d^3)*x + 6*(b^3*d^3*x^3 + a*b^2*c^2*d + (2*b^3*c*d^2 + a*b^2*d^3))*x^2 + (b^3*c^2*d + 2*a*b^2*c*d^2)*x*log(b*x + a) - 6*(b^3*d^3*x^3 + a*b^2*c^2*d + (2*b^3*c*d^2 + a*b^2*d^3))*x^2 + (b^3*c^2*d + 2*a*b^2*c*d^2)*x*log(d*x + c)/(a*b^4*c^6 - 4*a^2*b^3*c^5*d + 6*a^3*b^2*c^4*d^2 - 4*a^4*b*c^3*d^3 + a^5*c^2*d^4 + (b^5*c^4*d^2 - 4*a*b^4*c^3*d^3 + 6*a^2*b^3*c^2*d^4 - 4*a^3*b^2*c*d^5 + a^4*b*d^6))*x^3 + (2*b^5*c^5*d - 7*a*b^4*c^4*d^2 + 8*a^2*b^3*c^3*d^3 - 2*a^3*b^2*c^2*d^4 - 2*a^4*b*c*d^5 + a^5*d^6)*x^2 + (b^5*c^6 - 2*a*b^4*c^5*d - 2*a^2*b^3*c^4*d^2 + 8*a^3*b^2*c^3*d^3 - 7*a^4*b*c^2*d^4 + 2*a^5*c*d^5)*x$$

giac [B] time = 1.27, size = 217, normalized size = 1.97

$$\frac{3b^3d \log\left(\left|\frac{bc}{bx+a} - \frac{ad}{bx+a} + d\right|\right)}{b^5c^4 - 4ab^4c^3d + 6a^2b^3c^2d^2 - 4a^3b^2cd^3 + a^4bd^4} - \frac{b^5}{(b^6c^3 - 3ab^5c^2d + 3a^2b^4cd^2 - a^3b^3d^3)(bx + a)} + \frac{5b^2d^3 + a^3d^3}{2(bc - ad)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^3,x, algorithm="giac")

[Out]
$$3*b^3*d*log(abs(b*c/(b*x + a) - a*d/(b*x + a) + d))/(b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4) - b^5/((b^6*c^3 - 3*a*b^5*c^2*d + 3*a^2*b^4*c*d^2 - a^3*b^3*d^3)*(b*x + a)) + 1/2*(5*b^2*d^3 + 6*(b^4*c*d^2 - a*b^3*d^3)/((b*x + a)*b))/((b*c - a*d)^4*(b*c/(b*x + a) - a*d/(b*x + a) + d)^2)$$

maple [A] time = 0.01, size = 108, normalized size = 0.98

$$-\frac{3b^2d \ln(bx + a)}{(ad - bc)^4} + \frac{3b^2d \ln(dx + c)}{(ad - bc)^4} + \frac{b^2}{(ad - bc)^3(bx + a)} + \frac{2bd}{(ad - bc)^3(dx + c)} - \frac{d}{2(ad - bc)^2(dx + c)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^2/(d*x+c)^3,x)`

[Out]
$$-1/2*d/(a*d-b*c)^2/(d*x+c)^2+3*d/(a*d-b*c)^4*b^2*\ln(d*x+c)+2*d/(a*d-b*c)^3*b/(d*x+c)+b^2/(a*d-b*c)^3/(b*x+a)-3*d/(a*d-b*c)^4*b^2*\ln(b*x+a)$$

maxima [B] time = 1.59, size = 386, normalized size = 3.51

$$\frac{3b^2d \log(bx+a)}{b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4} + \frac{3b^2d \log(dx+c)}{b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4} - \frac{1}{2(ab^3c^5 - 3a^4d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^2/(d*x+c)^3,x, algorithm="maxima")`

[Out]
$$-3*b^2*d*\log(b*x+a)/(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4) + 3*b^2*d*\log(d*x+c)/(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4) - 1/2*(6*b^2*d^2*x^2 + 2*b^2*c^2 + 5*a*b*c*d - a^2*d^2 + 3*(3*b^2*c*d + a*b*d^2)*x)/(a*b^3*c^5 - 3*a^2*b^2*c^4*d + 3*a^3*b*c^3*d^2 - a^4*c^2*d^3 + (b^4*c^3*d^2 - 3*a*b^3*c^2*d^3 + 3*a^2*b^2*c^2*d^3 + a^3*b*c*d^4 - a^4*d^5)*x^3 + (2*b^4*c^4*d - 5*a*b^3*c^3*d^2 + 3*a^2*b^2*c^2*d^3 + a^3*b*c*d^4 - a^4*d^5)*x^2 + (b^4*c^5 - a*b^3*c^4*d - 3*a^2*b^2*c^3*d^2 + 5*a^3*b*c^2*d^3 - 2*a^4*c*d^4)*x)$$

mupad [B] time = 0.40, size = 329, normalized size = 2.99

$$\frac{-a^2d^2+5abcd+2b^2c^2}{2(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)} + \frac{3bx(ad^2+3bcd)}{2(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)} + \frac{3b^2d^2x^2}{a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3} - \frac{6b^2d \operatorname{atanh}\left(\frac{a^4d^4-2a^3}{x(bc^2+2adc)+ac^2+x^2(ad^2+2bcd)+bd^2x^3}\right)}{x(bc^2+2adc)+ac^2+x^2(ad^2+2bcd)+bd^2x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a+b*x)^2*(c+d*x)^3),x)`

[Out]
$$\left(\frac{2*b^2*c^2 - a^2*d^2 + 5*a*b*c*d}{2*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2)}\right) + \left(\frac{3*b*x*(a*d^2 + 3*b*c*d)}{2*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2)}\right) + \left(\frac{3*b^2*d^2*x^2}{(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2)}\right) / (x*(b*c^2 + 2*a*c*d) + a*c^2 + x^2*(a*d^2 + 2*b*c*d) + b*d^2*x^3) - \left(\frac{6*b^2*d*\operatorname{atanh}\left(\frac{a^4*d^4 - b^4*c^4 + 2*a*b^3*c^3*d - 2*a^3*b*c*d^3}{(a*d - b*c)^4} + \frac{2*b*d*x*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2)}{(a*d - b*c)^4}\right)}{(a*d - b*c)^4}\right) / (a*d - b*c)^4$$

sympy [B] time = 1.72, size = 632, normalized size = 5.75

$$\frac{3b^2d \log\left(x + \frac{-\frac{3a^5b^2d^6}{(ad-bc)^4} + \frac{15a^4b^3cd^5}{(ad-bc)^4} - \frac{30a^3b^4c^2d^4}{(ad-bc)^4} + \frac{30a^2b^5c^3d^3}{(ad-bc)^4} - \frac{15ab^6c^4d^2}{(ad-bc)^4} + 3ab^2d^2 + \frac{3b^7c^5d}{(ad-bc)^4} + 3b^3cd}{6b^3d^2}\right)}{(ad-bc)^4} - \frac{3b^2d \log\left(x + \frac{\frac{3a^5b^2d^6}{(ad-bc)^4} - \frac{15a^4b^3cd^5}{(ad-bc)^4} + \frac{30a^3b^4c^2d^4}{(ad-bc)^4} - \frac{30a^2b^5c^3d^3}{(ad-bc)^4} + \frac{15ab^6c^4d^2}{(ad-bc)^4} - 3ab^2d^2 - \frac{3b^7c^5d}{(ad-bc)^4} - 3b^3cd}{6b^3d^2}\right)}{(ad-bc)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2/(d*x+c)**3,x)

[Out] $3b^{**2}d \log(x + (-3a^{**5}b^{**2}d^{**6}/(a*d - b*c)^{**4} + 15a^{**4}b^{**3}c*d^{**5}/(a*d - b*c)^{**4} - 30a^{**3}b^{**4}c^{**2}d^{**4}/(a*d - b*c)^{**4} + 30a^{**2}b^{**5}c^{**3}d^{**3}/(a*d - b*c)^{**4} - 15a*b^{**6}c^{**4}d^{**2}/(a*d - b*c)^{**4} + 3a*b^{**2}d^{**2} + 3b^{**7}c^{**5}d/(a*d - b*c)^{**4} + 3b^{**3}c*d)/(6b^{**3}d^{**2}))/ (a*d - b*c)^{**4} - 3b^{**2}d \log(x + (3a^{**5}b^{**2}d^{**6}/(a*d - b*c)^{**4} - 15a^{**4}b^{**3}c*d^{**5}/(a*d - b*c)^{**4} + 30a^{**3}b^{**4}c^{**2}d^{**4}/(a*d - b*c)^{**4} - 30a^{**2}b^{**5}c^{**3}d^{**3}/(a*d - b*c)^{**4} + 15a*b^{**6}c^{**4}d^{**2}/(a*d - b*c)^{**4} + 3a*b^{**2}d^{**2} - 3b^{**7}c^{**5}d/(a*d - b*c)^{**4} + 3b^{**3}c*d)/(6b^{**3}d^{**2}))/ (a*d - b*c)^{**4} + (-a^{**2}d^{**2} + 5a*b*c*d + 2b^{**2}c^{**2} + 6b^{**2}d^{**2}x^{**2} + x*(3a*b*d^{**2} + 9b^{**2}c*d))/(2a^{**4}c^{**2}d^{**3} - 6a^{**3}b*c^{**3}d^{**2} + 6a^{**2}b^{**2}c^{**4}d - 2a*b^{**3}c^{**5} + x^{**3}(2a^{**3}b*d^{**5} - 6a^{**2}b^{**2}c*d^{**4} + 6a*b^{**3}c^{**2}d^{**3} - 2b^{**4}c^{**3}d^{**2}) + x^{**2}(2a^{**4}d^{**5} - 2a^{**3}b*c*d^{**4} - 6a^{**2}b^{**2}c^{**2}d^{**3} + 10a*b^{**3}c^{**3}d^{**2} - 4b^{**4}c^{**4}d) + x(4a^{**4}c*d^{**4} - 10a^{**3}b*c^{**2}d^{**3} + 6a^{**2}b^{**2}c^{**3}d^{**2} + 2a*b^{**3}c^{**4}d - 2b^{**4}c^{**5}))$

$$3.1361 \quad \int \frac{1}{(a+bx)^3(c+dx)^3} dx$$

Optimal. Leaf size=143

$$\frac{6b^2d^2 \log(a+bx)}{(bc-ad)^5} - \frac{6b^2d^2 \log(c+dx)}{(bc-ad)^5} + \frac{3b^2d}{(a+bx)(bc-ad)^4} - \frac{b^2}{2(a+bx)^2(bc-ad)^3} + \frac{3bd^2}{(c+dx)(bc-ad)^4} + \frac{d^2}{2(c+dx)^2(bc-ad)^3}$$

[Out] $-1/2*b^2/(-a*d+b*c)^3/(b*x+a)^2+3*b^2*d/(-a*d+b*c)^4/(b*x+a)+1/2*d^2/(-a*d+b*c)^3/(d*x+c)^2+3*b*d^2/(-a*d+b*c)^4/(d*x+c)+6*b^2*d^2*\ln(b*x+a)/(-a*d+b*c)^5-6*b^2*d^2*\ln(d*x+c)/(-a*d+b*c)^5$

Rubi [A] time = 0.10, antiderivative size = 143, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$\frac{6b^2d^2 \log(a+bx)}{(bc-ad)^5} - \frac{6b^2d^2 \log(c+dx)}{(bc-ad)^5} + \frac{3b^2d}{(a+bx)(bc-ad)^4} - \frac{b^2}{2(a+bx)^2(bc-ad)^3} + \frac{3bd^2}{(c+dx)(bc-ad)^4} + \frac{d^2}{2(c+dx)^2(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^3*(c + d*x)^3), x]

[Out] $-b^2/(2*(b*c - a*d)^3*(a + b*x)^2) + (3*b^2*d)/((b*c - a*d)^4*(a + b*x)) + d^2/(2*(b*c - a*d)^3*(c + d*x)^2) + (3*b*d^2)/((b*c - a*d)^4*(c + d*x)) + (6*b^2*d^2*\text{Log}[a + b*x])/(b*c - a*d)^5 - (6*b^2*d^2*\text{Log}[c + d*x])/(b*c - a*d)^5$

Rule 44

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^3(c+dx)^3} dx &= \int \left(\frac{b^3}{(bc-ad)^3(a+bx)^3} - \frac{3b^3d}{(bc-ad)^4(a+bx)^2} + \frac{6b^3d^2}{(bc-ad)^5(a+bx)} - \frac{d^3}{(bc-ad)^3(c+dx)^3} \right. \\ &\quad \left. - \frac{b^2}{2(bc-ad)^3(a+bx)^2} + \frac{3b^2d}{(bc-ad)^4(a+bx)} + \frac{d^2}{2(bc-ad)^3(c+dx)^2} + \frac{3bd^2}{(bc-ad)^4(c+dx)} \right) dx \end{aligned}$$

Mathematica [A] time = 0.12, size = 128, normalized size = 0.90

$$\frac{\frac{6b^2d(bc-ad)}{a+bx} - \frac{b^2(bc-ad)^2}{(a+bx)^2} + 12b^2d^2 \log(a+bx) + \frac{6bd^2(bc-ad)}{c+dx} + \frac{d^2(bc-ad)^2}{(c+dx)^2} - 12b^2d^2 \log(c+dx)}{2(bc-ad)^5}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^3*(c + d*x)^3),x]

[Out] $-\left(\frac{b^2(b*c - a*d)^2}{(a + b*x)^2} + \frac{6*b^2*d*(b*c - a*d)}{(a + b*x)} + \frac{d^2*2*(b*c - a*d)^2}{(c + d*x)^2} + \frac{6*b*d^2*(b*c - a*d)}{(c + d*x)} + 12*b^2*d^2*\text{Log}[a + b*x] - 12*b^2*d^2*\text{Log}[c + d*x]\right)/(2*(b*c - a*d)^5)$

fricas [B] time = 0.47, size = 760, normalized size = 5.31

$$\frac{b^4c^4 - 8ab^3c^3d + 8a^3bcd^3 - a^4d^4 - 12(b^4cd^3 - ab^3d^4)x^3 - 18(b^4c^2d^2 - a^2b^2d^4)x^2 - 4(b^4c^3d + 6ab^3c^2d^2) - 10a^2b^5c^7 - 5a^3b^4c^6d + 10a^4b^3c^5d^2 - 10a^5b^2c^4d^3 + 5a^6bc^3d^4 - a^7c^2d^5 + (b^7c^5d^2 - 5ab^6c^4d^3 + 10a^2b^5c^3d^4 - 10a^3b^4c^2d^5 + 5a^4b^3cd^6 - a^5b^2d^7)x^4 + 2*(b^7c^6d - 4*a*b^6*c^5*d^2 + 5*a^2*b^5*c^4*d^3 - 5*a^4*b^3*c^2*d^5 + 4*a^5*b^2*c*d^6 - a^6*b*d^7)*x^3 + (b^7*c^7 - a*b^6*c^6*d - 9*a^2*b^5*c^5*d^2 + 25*a^3*b^4*c^4*d^3 - 25*a^4*b^3*c^3*d^4 + 9*a^5*b^2*c^2*d^5 + a^6*b*c*d^6 - a^7*d^7)*x^2 + 2*(a*b^6*c^7 - 4*a^2*b^5*c^6*d + 5*a^3*b^4*c^5*d^2 - 5*a^5*b^2*c^3*d^4 + 4*a^6*b*c^2*d^5 - a^7*c*d^6)*x}{2*(a^2*b^5*c^7 - 5*a^3*b^4*c^6*d + 10*a^4*b^3*c^5*d^2 - 10*a^5*b^2*c^4*d^3 + 5*a^6*b*c^3*d^4 - a^7*c^2*d^5 + (b^7*c^5*d^2 - 5*a*b^6*c^4*d^3 + 10*a^2*b^5*c^3*d^4 - 10*a^3*b^4*c^2*d^5 + 5*a^4*b^3*c*d^6 - a^5*b^2*d^7)*x^4 + 2*(b^7*c^6*d - 4*a*b^6*c^5*d^2 + 5*a^2*b^5*c^4*d^3 - 5*a^4*b^3*c^2*d^5 + 4*a^5*b^2*c*d^6 - a^6*b*d^7)*x^3 + (b^7*c^7 - a*b^6*c^6*d - 9*a^2*b^5*c^5*d^2 + 25*a^3*b^4*c^4*d^3 - 25*a^4*b^3*c^3*d^4 + 9*a^5*b^2*c^2*d^5 + a^6*b*c*d^6 - a^7*d^7)*x^2 + 2*(a*b^6*c^7 - 4*a^2*b^5*c^6*d + 5*a^3*b^4*c^5*d^2 - 5*a^5*b^2*c^3*d^4 + 4*a^6*b*c^2*d^5 - a^7*c*d^6)*x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^3,x, algorithm="fricas")

[Out] $-1/2*(b^4*c^4 - 8*a*b^3*c^3*d + 8*a^3*b*c*d^3 - a^4*d^4 - 12*(b^4*c*d^3 - a*b^3*d^4)*x^3 - 18*(b^4*c^2*d^2 - a^2*b^2*d^4)*x^2 - 4*(b^4*c^3*d + 6*a*b^3*c^2*d^2 - 6*a^2*b^2*c*d^3 - a^3*b*d^4)*x - 12*(b^4*d^4*x^4 + a^2*b^2*c^2*d^2 + 2*(b^4*c*d^3 + a*b^3*d^4)*x^3 + (b^4*c^2*d^2 + 4*a*b^3*c*d^3 + a^2*b^2*d^4)*x^2 + 2*(a*b^3*c^2*d^2 + a^2*b^2*c*d^3)*x)*\log(b*x + a) + 12*(b^4*d^4*x^4 + a^2*b^2*c^2*d^2 + 2*(b^4*c*d^3 + a*b^3*d^4)*x^3 + (b^4*c^2*d^2 + 4*a*b^3*c*d^3 + a^2*b^2*d^4)*x^2 + 2*(a*b^3*c^2*d^2 + a^2*b^2*c*d^3)*x)*\log(d*x + c))/(a^2*b^5*c^7 - 5*a^3*b^4*c^6*d + 10*a^4*b^3*c^5*d^2 - 10*a^5*b^2*c^4*d^3 + 5*a^6*b*c^3*d^4 - a^7*c^2*d^5 + (b^7*c^5*d^2 - 5*a*b^6*c^4*d^3 + 10*a^2*b^5*c^3*d^4 - 10*a^3*b^4*c^2*d^5 + 5*a^4*b^3*c*d^6 - a^5*b^2*d^7)*x^4 + 2*(b^7*c^6*d - 4*a*b^6*c^5*d^2 + 5*a^2*b^5*c^4*d^3 - 5*a^4*b^3*c^2*d^5 + 4*a^5*b^2*c*d^6 - a^6*b*d^7)*x^3 + (b^7*c^7 - a*b^6*c^6*d - 9*a^2*b^5*c^5*d^2 + 25*a^3*b^4*c^4*d^3 - 25*a^4*b^3*c^3*d^4 + 9*a^5*b^2*c^2*d^5 + a^6*b*c*d^6 - a^7*d^7)*x^2 + 2*(a*b^6*c^7 - 4*a^2*b^5*c^6*d + 5*a^3*b^4*c^5*d^2 - 5*a^5*b^2*c^3*d^4 + 4*a^6*b*c^2*d^5 - a^7*c*d^6)*x)$

giac [B] time = 1.28, size = 345, normalized size = 2.41

$$\frac{6b^3d^2 \log(|bx + a|)}{b^6c^5 - 5ab^5c^4d + 10a^2b^4c^3d^2 - 10a^3b^3c^2d^3 + 5a^4b^2cd^4 - a^5bd^5} - \frac{6b^2d^3 \log(|dx + c|)}{b^5c^5d - 5ab^4c^4d^2 + 10a^2b^3c^3d^3 - 10a^3b^2c^2d^4 - 10a^4b^3cd^5 + 5a^5b^2d^6 - a^6bd^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^3,x, algorithm="giac")

[Out] $6*b^3*d^2*\log(\text{abs}(b*x + a))/(b^6*c^5 - 5*a*b^5*c^4*d + 10*a^2*b^4*c^3*d^2 - 10*a^3*b^3*c^2*d^3 + 5*a^4*b^2*c*d^4 - a^5*b*d^5) - 6*b^2*d^3*\log(\text{abs}(d*x + c))/(b^5*c^5*d - 5*a*b^4*c^4*d^2 + 10*a^2*b^3*c^3*d^3 - 10*a^3*b^2*c^2*d^4 + 5*a^4*b*c*d^5 - a^5*d^6) + 1/2*(12*b^3*d^3*x^3 + 18*b^3*c*d^2*x^2 + 18*a*b^2*d^3*x^2 + 4*b^3*c^2*d*x + 28*a*b^2*c*d^2*x + 4*a^2*b*d^3*x - b^3*c^3 + 7*a*b^2*c^2*d + 7*a^2*b*c*d^2 - a^3*d^3)/((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*(b*d*x^2 + b*c*x + a*d*x + a*c)^2)$

maple [A] time = 0.01, size = 140, normalized size = 0.98

$$-\frac{6b^2d^2 \ln(bx + a)}{(ad - bc)^5} + \frac{6b^2d^2 \ln(dx + c)}{(ad - bc)^5} + \frac{3bd}{(ad - bc)^4 (bx + a)} + \frac{3bd^2}{(ad - bc)^4 (dx + c)} + \frac{b^2}{2(ad - bc)^3 (bx + a)^2} - \frac{b^2}{2(ad - bc)^3 (dx + c)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^3/(d*x+c)^3,x)

[Out] $-1/2*d^2/(a*d-b*c)^3/(d*x+c)^2+6*d^2/(a*d-b*c)^5*b^2*\ln(d*x+c)+3*d^2/(a*d-b*c)^4*b/(d*x+c)+1/2*b^2/(a*d-b*c)^3/(b*x+a)^2-6*d^2/(a*d-b*c)^5*b^2*\ln(b*x+a)+3*b^2/(a*d-b*c)^4*d/(b*x+a)$

maxima [B] time = 1.55, size = 594, normalized size = 4.15

$$\frac{6b^2d^2 \log(bx + a)}{b^5c^5 - 5ab^4c^4d + 10a^2b^3c^3d^2 - 10a^3b^2c^2d^3 + 5a^4bcd^4 - a^5d^5} - \frac{6b^2d^2 \log(dx + c)}{b^5c^5 - 5ab^4c^4d + 10a^2b^3c^3d^2 - 10a^3b^2c^2d^3 + 5a^4bcd^4 - a^5d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^3,x, algorithm="maxima")

[Out] $6*b^2*d^2*\log(b*x + a)/(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5) - 6*b^2*d^2*\log(d*x + c)/(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5) + 1/2*(12*b^3*d^3*x^3 - b^3*c^3 + 7*a*b^2*c^2*d + 7*a^2*b*c*d^2 - a^3*d^3 + 18*(b^3*c*d^2 + a*b^2*d^3)*x^2 + 4*(b^3*c^2*d + 7*a*b^2*c*d^2 + a^2*b*d^3)*x)/(a^2*b^4*c^6 - 4*a^3*b^3*c^5*d + 6*a^4*b^2*c^4*d^2 - 4*a^5*b*c^3*d^3 + a^6*c^2*d^4 + (b^6*c^4*d^2 - 4*a*b^5*c^3*d^3 + 6*a^2*b^4*c^2*d^4 - 4*a^3*b^3*c*d^5 + a^4*b^2*d^6)*x^4 + 2*(b^6*c^5*d - 3*a*b^5*c^4*d^2 + 2*a^2*b^4*c^3*d^3 + 2*a^3*b^3*c^2*d^4 - 3*a^4*b^2*c*d^5 + a^5*b*d^6)*x^3 + (b^6*c^6 - 9*a^2*b^4*c^4*d^2 + 16*a^3*b^3*c^3*d^3 - 9*a^4*b^2*c^2*d^4 + a^6*d^6)*x^2 + 2*(a*b^5*c^6 - 3*a^2*b^4*c^5*d + 2*a^3*b^3*c^4*d^2 + 2*a^4*b^2*c^3*d^3 - 3*a^5*b*c^2*d^4 + a^6*c*d^5)*x)$

$$\begin{aligned}
& *b*c**3*d**3 + 12*a**4*b**2*c**4*d**2 - 8*a**3*b**3*c**5*d + 2*a**2*b**4*c** \\
& *6 + x**4*(2*a**4*b**2*d**6 - 8*a**3*b**3*c*d**5 + 12*a**2*b**4*c**2*d**4 - \\
& 8*a*b**5*c**3*d**3 + 2*b**6*c**4*d**2) + x**3*(4*a**5*b*d**6 - 12*a**4*b** \\
& 2*c*d**5 + 8*a**3*b**3*c**2*d**4 + 8*a**2*b**4*c**3*d**3 - 12*a*b**5*c**4*d \\
& **2 + 4*b**6*c**5*d) + x**2*(2*a**6*d**6 - 18*a**4*b**2*c**2*d**4 + 32*a**3 \\
& *b**3*c**3*d**3 - 18*a**2*b**4*c**4*d**2 + 2*b**6*c**6) + x*(4*a**6*c*d**5 \\
& - 12*a**5*b*c**2*d**4 + 8*a**4*b**2*c**3*d**3 + 8*a**3*b**3*c**4*d**2 - 12* \\
& a**2*b**4*c**5*d + 4*a*b**5*c**6)
\end{aligned}$$

$$3.1362 \quad \int \frac{(a+bx)^9}{(c+dx)^8} dx$$

Optimal. Leaf size=232

$$-\frac{b^8x(8bc-9ad)}{d^9} + \frac{36b^7(bc-ad)^2 \log(c+dx)}{d^{10}} + \frac{84b^6(bc-ad)^3}{d^{10}(c+dx)} - \frac{63b^5(bc-ad)^4}{d^{10}(c+dx)^2} + \frac{42b^4(bc-ad)^5}{d^{10}(c+dx)^3} - \frac{21b^3(bc-ad)^6}{d^{10}(c+dx)^4} + \dots$$

[Out] $-b^8(-9ad+8bc)x/d^9 + 1/2b^9x^2/d^8 + 1/7(-ad+bc)^9/d^{10}/(dx+c)^7 - 3/2b(-ad+bc)^8/d^{10}/(dx+c)^6 + 36/5b^2(-ad+bc)^7/d^{10}/(dx+c)^5 - 21b^3(-ad+bc)^6/d^{10}/(dx+c)^4 + 42b^4(-ad+bc)^5/d^{10}/(dx+c)^3 - 63b^5(-ad+bc)^4/d^{10}/(dx+c)^2 + 84b^6(-ad+bc)^3/d^{10}/(dx+c) + 36b^7(-ad+bc)^2 \ln(dx+c)/d^{10}$

Rubi [A] time = 0.36, antiderivative size = 232, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{b^8x(8bc-9ad)}{d^9} + \frac{84b^6(bc-ad)^3}{d^{10}(c+dx)} - \frac{63b^5(bc-ad)^4}{d^{10}(c+dx)^2} + \frac{42b^4(bc-ad)^5}{d^{10}(c+dx)^3} - \frac{21b^3(bc-ad)^6}{d^{10}(c+dx)^4} + \frac{36b^2(bc-ad)^7}{5d^{10}(c+dx)^5} + \frac{36b^7(bc-ad)^6}{d^{10}(c+dx)^4} + \dots$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^9/(c + d*x)^8, x]

[Out] $-(b^8(8bc-9ad)x/d^9) + (b^9x^2)/(2d^8) + (bc-ad)^9/(7d^{10}(c+dx)^7) - (3b(bc-ad)^8)/(2d^{10}(c+dx)^6) + (36b^2(bc-ad)^7)/(5d^{10}(c+dx)^5) - (21b^3(bc-ad)^6)/(d^{10}(c+dx)^4) + (42b^4(bc-ad)^5)/(d^{10}(c+dx)^3) - (63b^5(bc-ad)^4)/(d^{10}(c+dx)^2) + (84b^6(bc-ad)^3)/(d^{10}(c+dx)) + (36b^7(bc-ad)^2 \text{Log}[c+dx])/d^{10}$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^9}{(c+dx)^8} dx = \int \left(-\frac{b^8(8bc-9ad)}{d^9} + \frac{b^9x}{d^8} + \frac{(-bc+ad)^9}{d^9(c+dx)^8} + \frac{9b(bc-ad)^8}{d^9(c+dx)^7} - \frac{36b^2(bc-ad)^7}{d^9(c+dx)^6} + \frac{84b^3(bc-ad)^6}{d^9(c+dx)^5} - \frac{b^8(8bc-9ad)x}{d^9} + \frac{b^9x^2}{2d^8} + \frac{(bc-ad)^9}{7d^{10}(c+dx)^7} - \frac{3b(bc-ad)^8}{2d^{10}(c+dx)^6} + \frac{36b^2(bc-ad)^7}{5d^{10}(c+dx)^5} - \frac{21b^3(bc-ad)^6}{d^{10}(c+dx)^4} + \dots \right) dx$$


```
*c*d^8 - 24*a^7*b^2*d^9)*x^2 + 7*(2989*b^9*c^8*d - 7938*a*b^8*c^7*d^2 + 617
4*a^2*b^7*c^6*d^3 - 840*a^3*b^6*c^5*d^4 - 210*a^4*b^5*c^4*d^5 - 84*a^5*b^4*
c^3*d^6 - 42*a^6*b^3*c^2*d^7 - 24*a^7*b^2*c*d^8 - 15*a^8*b*d^9)*x + 2520*(b
^9*c^9 - 2*a*b^8*c^8*d + a^2*b^7*c^7*d^2 + (b^9*c^2*d^7 - 2*a*b^8*c*d^8 + a
^2*b^7*d^9)*x^7 + 7*(b^9*c^3*d^6 - 2*a*b^8*c^2*d^7 + a^2*b^7*c*d^8)*x^6 + 2
1*(b^9*c^4*d^5 - 2*a*b^8*c^3*d^6 + a^2*b^7*c^2*d^7)*x^5 + 35*(b^9*c^5*d^4 -
2*a*b^8*c^4*d^5 + a^2*b^7*c^3*d^6)*x^4 + 35*(b^9*c^6*d^3 - 2*a*b^8*c^5*d^4
+ a^2*b^7*c^4*d^5)*x^3 + 21*(b^9*c^7*d^2 - 2*a*b^8*c^6*d^3 + a^2*b^7*c^5*d
^4)*x^2 + 7*(b^9*c^8*d - 2*a*b^8*c^7*d^2 + a^2*b^7*c^6*d^3)*x)*log(d*x + c)
)/(d^17*x^7 + 7*c*d^16*x^6 + 21*c^2*d^15*x^5 + 35*c^3*d^14*x^4 + 35*c^4*d^1
3*x^3 + 21*c^5*d^12*x^2 + 7*c^6*d^11*x + c^7*d^10)
```

giac [B] time = 1.32, size = 723, normalized size = 3.12

$$\frac{36(b^9c^2 - 2ab^8cd + a^2b^7d^2) \log(|dx + c|)}{d^{10}} + \frac{b^9d^8x^2 - 16b^9cd^7x + 18ab^8d^8x}{2d^{16}} + \frac{3349b^9c^9 - 8658ab^8c^8d + 6534a^2b^7c^7d^2}{d^{10}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^9/(d*x+c)^8,x, algorithm="giac")
```

```
[Out] 36*(b^9*c^2 - 2*a*b^8*c*d + a^2*b^7*d^2)*log(abs(d*x + c))/d^10 + 1/2*(b^9*
d^8*x^2 - 16*b^9*c*d^7*x + 18*a*b^8*d^8*x)/d^16 + 1/70*(3349*b^9*c^9 - 8658
*a*b^8*c^8*d + 6534*a^2*b^7*c^7*d^2 - 840*a^3*b^6*c^6*d^3 - 210*a^4*b^5*c^5
*d^4 - 84*a^5*b^4*c^4*d^5 - 42*a^6*b^3*c^3*d^6 - 24*a^7*b^2*c^2*d^7 - 15*a^
8*b*c*d^8 - 10*a^9*d^9 + 5880*(b^9*c^3*d^6 - 3*a*b^8*c^2*d^7 + 3*a^2*b^7*c*
d^8 - a^3*b^6*d^9)*x^6 + 4410*(7*b^9*c^4*d^5 - 20*a*b^8*c^3*d^6 + 18*a^2*b^
7*c^2*d^7 - 4*a^3*b^6*c*d^8 - a^4*b^5*d^9)*x^5 + 1470*(47*b^9*c^5*d^4 - 130
*a*b^8*c^4*d^5 + 110*a^2*b^7*c^3*d^6 - 20*a^3*b^6*c^2*d^7 - 5*a^4*b^5*c*d^8
- 2*a^5*b^4*d^9)*x^4 + 1470*(57*b^9*c^6*d^3 - 154*a*b^8*c^5*d^4 + 125*a^2*
b^7*c^4*d^5 - 20*a^3*b^6*c^3*d^6 - 5*a^4*b^5*c^2*d^7 - 2*a^5*b^4*c*d^8 - a^
6*b^3*d^9)*x^3 + 126*(459*b^9*c^7*d^2 - 1218*a*b^8*c^6*d^3 + 959*a^2*b^7*c^
5*d^4 - 140*a^3*b^6*c^4*d^5 - 35*a^4*b^5*c^3*d^6 - 14*a^5*b^4*c^2*d^7 - 7*a
^6*b^3*c*d^8 - 4*a^7*b^2*d^9)*x^2 + 21*(1023*b^9*c^8*d - 2676*a*b^8*c^7*d^2
+ 2058*a^2*b^7*c^6*d^3 - 280*a^3*b^6*c^5*d^4 - 70*a^4*b^5*c^4*d^5 - 28*a^5
*b^4*c^3*d^6 - 14*a^6*b^3*c^2*d^7 - 8*a^7*b^2*c*d^8 - 5*a^8*b*d^9)*x)/((d*x
+ c)^7*d^10)
```

maple [B] time = 0.02, size = 1035, normalized size = 4.46

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((b*x+a)^9/(d*x+c)^8,x)
```

```
[Out] 1/2*b^9*x^2/d^8-21*b^9/d^10/(d*x+c)^4*c^6+36/5*b^9/d^10/(d*x+c)^5*c^7+1/7/d
^10/(d*x+c)^7*b^9*c^9-36/5*b^2/d^3/(d*x+c)^5*a^7+9*b^8/d^8*a*x-8*b^9/d^9*x*
c-84*b^6/d^7/(d*x+c)*a^3+84*b^9/d^10/(d*x+c)*c^3+36*b^7/d^8*ln(d*x+c)*a^2+3
6*b^9/d^10*ln(d*x+c)*c^2-3/2*b/d^2/(d*x+c)^6*a^8-3/2*b^9/d^10/(d*x+c)^6*c^8
-42*b^4/d^5/(d*x+c)^3*a^5+42*b^9/d^10/(d*x+c)^3*c^5-63*b^5/d^6/(d*x+c)^2*a^
4-63*b^9/d^10/(d*x+c)^2*c^4-21*b^3/d^4/(d*x+c)^4*a^6-1/7/d/(d*x+c)^7*a^9+25
2*b^6/d^7/(d*x+c)^2*a^3*c-378*b^7/d^8/(d*x+c)^2*a^2*c^2+252*b^8/d^9/(d*x+c)
^2*a*c^3-36/7/d^3/(d*x+c)^7*a^7*b^2*c^2+126*b^4/d^5/(d*x+c)^4*a^5*c-315*b^5
/d^6/(d*x+c)^4*a^4*c^2+420*b^6/d^7/(d*x+c)^4*a^3*c^3-315*b^7/d^8/(d*x+c)^4*
a^2*c^4+126*b^8/d^9/(d*x+c)^4*a*c^5+9/7/d^2/(d*x+c)^7*a^8*b*c+252/5*b^3/d^4
/(d*x+c)^5*a^6*c-756/5*b^4/d^5/(d*x+c)^5*a^5*c^2+252*b^5/d^6/(d*x+c)^5*a^4*
c^3-252*b^6/d^7/(d*x+c)^5*a^3*c^4+756/5*b^7/d^8/(d*x+c)^5*a^2*c^5-252/5*b^8
/d^9/(d*x+c)^5*a*c^6+252*b^7/d^8/(d*x+c)*a^2*c-252*b^8/d^9/(d*x+c)*a*c^2-72
*b^8/d^9*ln(d*x+c)*a*c+12*b^2/d^3/(d*x+c)^6*a^7*c-42*b^3/d^4/(d*x+c)^6*a^6*
c^2+84*b^4/d^5/(d*x+c)^6*a^5*c^3-105*b^5/d^6/(d*x+c)^6*a^4*c^4+84*b^6/d^7/(
d*x+c)^6*a^3*c^5+12/d^4/(d*x+c)^7*a^6*b^3*c^3+18/d^6/(d*x+c)^7*a^4*b^5*c^5-
12/d^7/(d*x+c)^7*a^3*b^6*c^6+36/7/d^8/(d*x+c)^7*a^2*b^7*c^7-9/7/d^9/(d*x+c)
^7*a*b^8*c^8-42*b^7/d^8/(d*x+c)^6*a^2*c^6+12*b^8/d^9/(d*x+c)^6*a*c^7+210*b^
5/d^6/(d*x+c)^3*a^4*c-420*b^6/d^7/(d*x+c)^3*a^3*c^2+420*b^7/d^8/(d*x+c)^3*a
^2*c^3-210*b^8/d^9/(d*x+c)^3*a*c^4-18/d^5/(d*x+c)^7*a^5*b^4*c^4
```

maxima [B] time = 2.20, size = 786, normalized size = 3.39

$$3349b^9c^9 - 8658ab^8c^8d + 6534a^2b^7c^7d^2 - 840a^3b^6c^6d^3 - 210a^4b^5c^5d^4 - 84a^5b^4c^4d^5 - 42a^6b^3c^3d^6 - 24a^7b^2c^2d^7$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^9/(d*x+c)^8,x, algorithm="maxima")
```

```
[Out] 1/70*(3349*b^9*c^9 - 8658*a*b^8*c^8*d + 6534*a^2*b^7*c^7*d^2 - 840*a^3*b^6*
c^6*d^3 - 210*a^4*b^5*c^5*d^4 - 84*a^5*b^4*c^4*d^5 - 42*a^6*b^3*c^3*d^6 - 2
4*a^7*b^2*c^2*d^7 - 15*a^8*b*c*d^8 - 10*a^9*d^9 + 5880*(b^9*c^3*d^6 - 3*a*b
^8*c^2*d^7 + 3*a^2*b^7*c*d^8 - a^3*b^6*d^9)*x^6 + 4410*(7*b^9*c^4*d^5 - 20*
a*b^8*c^3*d^6 + 18*a^2*b^7*c^2*d^7 - 4*a^3*b^6*c*d^8 - a^4*b^5*d^9)*x^5 + 1
470*(47*b^9*c^5*d^4 - 130*a*b^8*c^4*d^5 + 110*a^2*b^7*c^3*d^6 - 20*a^3*b^6*
c^2*d^7 - 5*a^4*b^5*c*d^8 - 2*a^5*b^4*d^9)*x^4 + 1470*(57*b^9*c^6*d^3 - 154
*a*b^8*c^5*d^4 + 125*a^2*b^7*c^4*d^5 - 20*a^3*b^6*c^3*d^6 - 5*a^4*b^5*c^2*d
^7 - 2*a^5*b^4*c*d^8 - a^6*b^3*d^9)*x^3 + 126*(459*b^9*c^7*d^2 - 1218*a*b^8
*c^6*d^3 + 959*a^2*b^7*c^5*d^4 - 140*a^3*b^6*c^4*d^5 - 35*a^4*b^5*c^3*d^6 -
14*a^5*b^4*c^2*d^7 - 7*a^6*b^3*c*d^8 - 4*a^7*b^2*d^9)*x^2 + 21*(1023*b^9*c
^8*d - 2676*a*b^8*c^7*d^2 + 2058*a^2*b^7*c^6*d^3 - 280*a^3*b^6*c^5*d^4 - 70
*a^4*b^5*c^4*d^5 - 28*a^5*b^4*c^3*d^6 - 14*a^6*b^3*c^2*d^7 - 8*a^7*b^2*c*d^
8 - 5*a^8*b*d^9)*x)/(d^17*x^7 + 7*c*d^16*x^6 + 21*c^2*d^15*x^5 + 35*c^3*d^1
4*x^4 + 35*c^4*d^13*x^3 + 21*c^5*d^12*x^2 + 7*c^6*d^11*x + c^7*d^10) + 1/2*
```

$(b^9 d x^2 - 2(8 b^9 c - 9 a b^8 d) x) / d^9 + 36(b^9 c^2 - 2 a b^8 c d + a^2 b^7 d^2) \log(d x + c) / d^{10}$

mupad [B] time = 0.26, size = 784, normalized size = 3.38

$$x \left(\frac{9 a b^8}{d^8} - \frac{8 b^9 c}{d^9} \right) - \frac{10 a^9 d^9 + 15 a^8 b c d^8 + 24 a^7 b^2 c^2 d^7 + 42 a^6 b^3 c^3 d^6 + 84 a^5 b^4 c^4 d^5 + 210 a^4 b^5 c^5 d^4 + 840 a^3 b^6 c^6 d^3 - 6534 a^2 b^7 c^7 d^2 + 8658 a b^8 c^8 d - 70 d^9}{70 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^9/(c + d*x)^8, x)

[Out] $x \left(\frac{9 a b^8}{d^8} - \frac{8 b^9 c}{d^9} \right) - \left(\frac{10 a^9 d^9 - 3349 b^9 c^9 - 6534 a^2 b^7 c^7 d^2 + 840 a^3 b^6 c^6 d^3 + 210 a^4 b^5 c^5 d^4 + 84 a^5 b^4 c^4 d^5 + 42 a^6 b^3 c^3 d^6 + 24 a^7 b^2 c^2 d^7 + 8658 a b^8 c^8 d + 15 a^8 b c^8 d^8}{70 d} + x \left(\frac{3 a^8 b d^8}{2} - \frac{3069 b^9 c^8}{10} + \frac{12 a^7 b^2 c^8 d^7}{5} - \frac{3087 a^2 b^7 c^6 d^2}{5} + \frac{84 a^3 b^6 c^5 d^3 + 21 a^4 b^5 c^4 d^4 + (42 a^5 b^4 c^3 d^5)}{5} + \frac{21 a^6 b^3 c^2 d^6}{5} + \frac{4014 a b^8 c^7 d}{5} \right) + x^3 \left(\frac{21 a^6 b^3 d^8 - 1197 b^9 c^6 d^2 + 3234 a b^8 c^5 d^3 + 42 a^5 b^4 c^4 d^7 - 2625 a^2 b^7 c^4 d^4 + 420 a^3 b^6 c^3 d^5 + 105 a^4 b^5 c^2 d^6}{5} \right) + x^2 \left(\frac{36 a^7 b^2 d^8}{5} - \frac{4131 b^9 c^7 d}{5} + \frac{10962 a b^8 c^6 d^2}{5} + \frac{63 a^6 b^3 c^5 d^7}{5} - \frac{8631 a^2 b^7 c^5 d^3}{5} + 252 a^3 b^6 c^4 d^4 + 63 a^4 b^5 c^3 d^5 + \frac{126 a^5 b^4 c^2 d^6}{5} \right) + x^5 \left(\frac{63 a^4 b^5 d^8 - 441 b^9 c^4 d^4 + 1260 a b^8 c^3 d^5 + 252 a^3 b^6 c^2 d^7 - 1134 a^2 b^7 c^2 d^6}{5} \right) + x^4 \left(\frac{42 a^5 b^4 d^8 - 987 b^9 c^5 d^3 + 2730 a b^8 c^4 d^4 + 105 a^4 b^5 c^3 d^7 - 2310 a^2 b^7 c^3 d^5 + 420 a^3 b^6 c^2 d^6}{5} \right) + x^6 \left(\frac{84 a^3 b^6 d^8 - 84 b^9 c^3 d^5 + 252 a b^8 c^2 d^6 - 252 a^2 b^7 c^2 d^7}{5} \right) / (c^7 d^9 + d^{16} x^7 + 7 c^6 d^{10} x + 7 c^5 d^{15} x^6 + 21 c^5 d^{11} x^2 + 35 c^4 d^{12} x^3 + 35 c^3 d^{13} x^4 + 21 c^2 d^{14} x^5) + (b^9 x^2) / (2 d^8) + (\log(c + d x) (36 b^9 c^2 + 36 a^2 b^7 d^2 - 72 a b^8 c d)) / d^{10}$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**9/(d*x+c)**8, x)

[Out] Timed out

$$3.1363 \quad \int \frac{(a+bx)^8}{(c+dx)^8} dx$$

Optimal. Leaf size=209

$$-\frac{8b^7(bc-ad)\log(c+dx)}{d^9} - \frac{28b^6(bc-ad)^2}{d^9(c+dx)} + \frac{28b^5(bc-ad)^3}{d^9(c+dx)^2} - \frac{70b^4(bc-ad)^4}{3d^9(c+dx)^3} + \frac{14b^3(bc-ad)^5}{d^9(c+dx)^4} - \frac{28b^2(bc-ad)^6}{5d^9(c+dx)^5} + \dots$$

[Out] $b^8 x/d^8 - 1/7 * (-a*d+b*c)^8/d^9/(d*x+c)^7 + 4/3 * b * (-a*d+b*c)^7/d^9/(d*x+c)^6 - 2$
 $8/5 * b^2 * (-a*d+b*c)^6/d^9/(d*x+c)^5 + 14 * b^3 * (-a*d+b*c)^5/d^9/(d*x+c)^4 - 70/3 * b$
 $^4 * (-a*d+b*c)^4/d^9/(d*x+c)^3 + 28 * b^5 * (-a*d+b*c)^3/d^9/(d*x+c)^2 - 28 * b^6 * (-a*$
 $d+b*c)^2/d^9/(d*x+c) - 8 * b^7 * (-a*d+b*c) * \ln(d*x+c)/d^9$

Rubi [A] time = 0.28, antiderivative size = 209, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{28b^6(bc-ad)^2}{d^9(c+dx)} + \frac{28b^5(bc-ad)^3}{d^9(c+dx)^2} - \frac{70b^4(bc-ad)^4}{3d^9(c+dx)^3} + \frac{14b^3(bc-ad)^5}{d^9(c+dx)^4} - \frac{28b^2(bc-ad)^6}{5d^9(c+dx)^5} - \frac{8b^7(bc-ad)\log(c+dx)}{d^9} + \dots$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^8/(c + d*x)^8, x]

[Out] $(b^8 x)/d^8 - (b^8 c - a^8 d)/(7 * d^9 * (c + d * x)^7) + (4 * b * (b^7 c - a^7 d))/(3 * d^9 * (c + d * x)^6) - (28 * b^2 * (b^6 c - a^6 d))/(5 * d^9 * (c + d * x)^5) + (14 * b^3 * (b^5 c - a^5 d))/(d^9 * (c + d * x)^4) - (70 * b^4 * (b^4 c - a^4 d))/(3 * d^9 * (c + d * x)^3) + (28 * b^5 * (b^3 c - a^3 d))/(d^9 * (c + d * x)^2) - (28 * b^6 * (b^2 c - a^2 d))/(d^9 * (c + d * x)) - (8 * b^7 * (b * c - a * d) * \text{Log}[c + d * x])/d^9$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^8}{(c+dx)^8} dx = \int \left(\frac{b^8}{d^8} + \frac{(-bc+ad)^8}{d^8(c+dx)^8} - \frac{8b(bc-ad)^7}{d^8(c+dx)^7} + \frac{28b^2(bc-ad)^6}{d^8(c+dx)^6} - \frac{56b^3(bc-ad)^5}{d^8(c+dx)^5} + \frac{70b^4(bc-ad)^4}{d^8(c+dx)^4} - \frac{28b^5(bc-ad)^3}{d^8(c+dx)^3} + \frac{14b^6(bc-ad)^2}{d^8(c+dx)^2} - \frac{8b^7(bc-ad)}{d^8(c+dx)} + \frac{b^8 x}{d^8} \right) dx$$

Mathematica [B] time = 0.20, size = 474, normalized size = 2.27

$$\frac{15a^8d^8 + 20a^7bd^7(c + 7dx) + 28a^6b^2d^6(c^2 + 7cdx + 21d^2x^2) + 42a^5b^3d^5(c^3 + 7c^2dx + 21cd^2x^2 + 35d^3x^3) + 70a^4b^4d^4(c^4 + 7c^3dx + 21c^2d^2x^2 + 35cd^3x^3 + 35d^4x^4) + 140a^3b^5d^3(c^5 + 7c^4dx + 21c^3d^2x^2 + 35c^2d^3x^3 + 35cd^4x^4 + 21d^5x^5) + 420a^2b^6d^2(c^6 + 7c^5dx + 21c^4d^2x^2 + 35c^3d^3x^3 + 35c^2d^4x^4 + 21cd^5x^5 + 7d^6x^6) - 2ab^7cd(1089c^6 + 7203c^5dx + 20139c^4d^2x^2 + 30625c^3d^3x^3 + 26950c^2d^4x^4 + 13230cd^5x^5 + 2940d^6x^6) + b^8(1443c^8 + 9261c^7dx + 24843c^6d^2x^2 + 35525c^5d^3x^3 + 28175c^4d^4x^4 + 11025c^3d^5x^5 + 735c^2d^6x^6 - 735cd^7x^7 - 105d^8x^8) + 840b^7c(b^8c - a^8d)(c + dx)^7 \operatorname{Log}[c + dx]}{(d^9(c + dx)^7)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^8/(c + d*x)^8,x]

[Out]
$$\frac{-1/105*(15*a^8*d^8 + 20*a^7*b*d^7*(c + 7*d*x) + 28*a^6*b^2*d^6*(c^2 + 7*c*d*x + 21*d^2*x^2) + 42*a^5*b^3*d^5*(c^3 + 7*c^2*d*x + 21*c*d^2*x^2 + 35*d^3*x^3) + 70*a^4*b^4*d^4*(c^4 + 7*c^3*d*x + 21*c^2*d^2*x^2 + 35*c*d^3*x^3 + 35*d^4*x^4) + 140*a^3*b^5*d^3*(c^5 + 7*c^4*d*x + 21*c^3*d^2*x^2 + 35*c^2*d^3*x^3 + 35*c*d^4*x^4 + 21*d^5*x^5) + 420*a^2*b^6*d^2*(c^6 + 7*c^5*d*x + 21*c^4*d^2*x^2 + 35*c^3*d^3*x^3 + 35*c^2*d^4*x^4 + 21*c*d^5*x^5 + 7*d^6*x^6) - 2*a*b^7*c*d*(1089*c^6 + 7203*c^5*d*x + 20139*c^4*d^2*x^2 + 30625*c^3*d^3*x^3 + 26950*c^2*d^4*x^4 + 13230*c*d^5*x^5 + 2940*d^6*x^6) + b^8*(1443*c^8 + 9261*c^7*d*x + 24843*c^6*d^2*x^2 + 35525*c^5*d^3*x^3 + 28175*c^4*d^4*x^4 + 11025*c^3*d^5*x^5 + 735*c^2*d^6*x^6 - 735*c*d^7*x^7 - 105*d^8*x^8) + 840*b^7*c*(b^8*c - a^8*d)*(c + d*x)^7 \operatorname{Log}[c + d*x]}{(d^9*(c + d*x)^7)}$$

fricas [B] time = 0.48, size = 852, normalized size = 4.08

$$\frac{105b^8d^8x^8 + 735b^8cd^7x^7 - 1443b^8c^8 + 2178ab^7c^7d - 420a^2b^6c^6d^2 - 140a^3b^5c^5d^3 - 70a^4b^4c^4d^4 - 42a^5b^3c^3d^5 - 70a^6b^2c^2d^6 - 20a^7b^1c^1d^7 - 15a^8d^8 - 735(b^8c^2d^6 - 8a^2b^7cd^7 + 4a^2b^6c^2d^8)x^6 - 735(15b^8c^3d^5 - 36a^2b^7c^2d^6 + 12a^2b^6cd^7 + 4a^3b^5d^8)x^5 - 1225(23b^8c^4d^4 - 44a^2b^7c^3d^5 + 12a^2b^6c^2d^6 + 4a^3b^5cd^7 + 2a^4b^4d^8)x^4 - 245(145b^8c^5d^3 - 250a^2b^7c^4d^4 + 60a^2b^6c^3d^5 + 20a^3b^5c^2d^6 + 10a^4b^4cd^7 + 6a^5b^3d^8)x^3 - 147(169b^8c^6d^2 - 274a^2b^7c^5d^3 + 60a^2b^6c^4d^4 + 20a^3b^5c^3d^5 + 10a^4b^4c^2d^6 + 6a^5b^3cd^7 + 4a^6b^2d^8)x^2 - 7(1323b^8c^7d - 2058a^2b^7c^6d^2 + 420a^2b^6c^5d^3 + 140a^3b^5c^4d^4 + 70a^4b^4c^3d^5 + 42a^5b^3c^2d^6 + 28a^6b^2cd^7 + 20a^7bd^8)x - 840(b^8c^8 - a^8d - a^8b^7cd + (b^8cd^7 - a^8bd^8)x^7 + 7(b^8c^2d^6 - a^8b^7cd^7)x^6 + 21(b^8c^3d^5 - a^8b^7c^2d^6)x^5 + 35(b^8c^4d^4 - a^8b^7c^3d^5)x^4 + 35(b^8c^5d^3 - a^8b^7c^4d^4)x^3 + 21(b^8c^6d^2 - a^8b^7c^5d^3)x^2 + 7(b^8c^7d - a^8b^7c^6d^2)x + a^8d^8)}{(d^9(c + dx)^7)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8/(d*x+c)^8,x, algorithm="fricas")

[Out]
$$\frac{1/105*(105*b^8*d^8*x^8 + 735*b^8*c*d^7*x^7 - 1443*b^8*c^8 + 2178*a*b^7*c^7*d - 420*a^2*b^6*c^6*d^2 - 140*a^3*b^5*c^5*d^3 - 70*a^4*b^4*c^4*d^4 - 42*a^5*b^3*c^3*d^5 - 28*a^6*b^2*c^2*d^6 - 20*a^7*b^1*c^1*d^7 - 15*a^8*d^8 - 735*(b^8*c^2*d^6 - 8*a^2*b^7*c*d^7 + 4*a^2*b^6*c^2*d^8)*x^6 - 735*(15*b^8*c^3*d^5 - 36*a^2*b^7*c^2*d^6 + 12*a^2*b^6*c*d^7 + 4*a^3*b^5*d^8)*x^5 - 1225*(23*b^8*c^4*d^4 - 44*a^2*b^7*c^3*d^5 + 12*a^2*b^6*c^2*d^6 + 4*a^3*b^5*c*d^7 + 2*a^4*b^4*d^8)*x^4 - 245*(145*b^8*c^5*d^3 - 250*a^2*b^7*c^4*d^4 + 60*a^2*b^6*c^3*d^5 + 20*a^3*b^5*c^2*d^6 + 10*a^4*b^4*c*d^7 + 6*a^5*b^3*d^8)*x^3 - 147*(169*b^8*c^6*d^2 - 274*a^2*b^7*c^5*d^3 + 60*a^2*b^6*c^4*d^4 + 20*a^3*b^5*c^3*d^5 + 10*a^4*b^4*c^2*d^6 + 6*a^5*b^3*c*d^7 + 4*a^6*b^2*d^8)*x^2 - 7*(1323*b^8*c^7*d - 2058*a^2*b^7*c^6*d^2 + 420*a^2*b^6*c^5*d^3 + 140*a^3*b^5*c^4*d^4 + 70*a^4*b^4*c^3*d^5 + 42*a^5*b^3*c^2*d^6 + 28*a^6*b^2*c*d^7 + 20*a^7*b*d^8)*x - 840*(b^8*c^8 - a^8*d - a^8*b^7*c*d + (b^8*c*d^7 - a^8*b^7*d^8)*x^7 + 7*(b^8*c^2*d^6 - a^8*b^7*c*d^7)*x^6 + 21*(b^8*c^3*d^5 - a^8*b^7*c^2*d^6)*x^5 + 35*(b^8*c^4*d^4 - a^8*b^7*c^3*d^5)*x^4 + 35*(b^8*c^5*d^3 - a^8*b^7*c^4*d^4)*x^3 + 21*(b^8*c^6*d^2 - a^8*b^7*c^5*d^3)*x^2 + 7*(b^8*c^7*d - a^8*b^7*c^6*d^2)*x + a^8*d^8)}{(d^9*(c + d*x)^7)}$$

$$c^5d^3)x^2 + 7*(b^8c^7d - a*b^7c^6d^2)*x)*\log(dx + c))/(d^{16}x^7 + 7*c*d^{15}x^6 + 21*c^2*d^{14}x^5 + 35*c^3*d^{13}x^4 + 35*c^4*d^{12}x^3 + 21*c^5*d^{11}x^2 + 7*c^6*d^{10}x + c^7*d^9)$$

giac [B] time = 1.27, size = 581, normalized size = 2.78

$$\frac{b^8x}{d^8} - \frac{8(b^8c - ab^7d)\log(|dx + c|)}{d^9} - \frac{1443b^8c^8 - 2178ab^7c^7d + 420a^2b^6c^6d^2 + 140a^3b^5c^5d^3 + 70a^4b^4c^4d^4 + 42a^5b^3c^3d^5}{d^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8/(d*x+c)^8,x, algorithm="giac")

[Out] $b^8x/d^8 - 8*(b^8c - a*b^7*d)*\log(\text{abs}(dx + c))/d^9 - 1/105*(1443*b^8*c^8 - 2178*a*b^7*c^7*d + 420*a^2*b^6*c^6*d^2 + 140*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 + 42*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 + 20*a^7*b*c*d^7 + 15*a^8*d^8 + 2940*(b^8*c^2*d^6 - 2*a*b^7*c*d^7 + a^2*b^6*d^8)*x^6 + 2940*(5*b^8*c^3*d^5 - 9*a*b^7*c^2*d^6 + 3*a^2*b^6*c*d^7 + a^3*b^5*d^8)*x^5 + 2450*(13*b^8*c^4*d^4 - 22*a*b^7*c^3*d^5 + 6*a^2*b^6*c^2*d^6 + 2*a^3*b^5*c*d^7 + a^4*b^4*d^8)*x^4 + 490*(77*b^8*c^5*d^3 - 125*a*b^7*c^4*d^4 + 30*a^2*b^6*c^3*d^5 + 10*a^3*b^5*c^2*d^6 + 5*a^4*b^4*c*d^7 + 3*a^5*b^3*d^8)*x^3 + 294*(87*b^8*c^6*d^2 - 137*a*b^7*c^5*d^3 + 30*a^2*b^6*c^4*d^4 + 10*a^3*b^5*c^3*d^5 + 5*a^4*b^4*c^2*d^6 + 3*a^5*b^3*c*d^7 + 2*a^6*b^2*d^8)*x^2 + 14*(669*b^8*c^7*d - 1029*a*b^7*c^6*d^2 + 210*a^2*b^6*c^5*d^3 + 70*a^3*b^5*c^4*d^4 + 35*a^4*b^4*c^3*d^5 + 21*a^5*b^3*c^2*d^6 + 14*a^6*b^2*c*d^7 + 10*a^7*b*d^8)*x)/((dx + c)^7*d^9)$

maple [B] time = 0.01, size = 845, normalized size = 4.04

$$-\frac{a^8}{7(dx+c)^7d} + \frac{8a^7bc}{7(dx+c)^7d^2} - \frac{4a^6b^2c^2}{(dx+c)^7d^3} + \frac{8a^5b^3c^3}{(dx+c)^7d^4} - \frac{10a^4b^4c^4}{(dx+c)^7d^5} + \frac{8a^3b^5c^5}{(dx+c)^7d^6} - \frac{4a^2b^6c^6}{(dx+c)^7d^7} + \frac{8ab^7c^7}{7(dx+c)^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^8/(d*x+c)^8,x)

[Out] $-14*b^3/d^4/(d*x+c)^4*a^5+14*b^8/d^9/(d*x+c)^4*c^5-28*b^6/d^7/(d*x+c)*a^2-2*8*b^8/d^9/(d*x+c)*c^2+8*b^7/d^8*\ln(d*x+c)*a-8*b^8/d^9*\ln(d*x+c)*c-28/5*b^2/d^3/(d*x+c)^5*a^6-28/5*b^8/d^9/(d*x+c)^5*c^6-28*b^5/d^6/(d*x+c)^2*a^3+28*b^8/d^9/(d*x+c)^2*c^3-1/7/d^9/(d*x+c)^7*b^8*c^8-4/3*b/d^2/(d*x+c)^6*a^7+4/3*b^8/d^9/(d*x+c)^6*c^7-70/3*b^4/d^5/(d*x+c)^3*a^4-70/3*b^8/d^9/(d*x+c)^3*c^4+b^8*x/d^8+8/7/d^2/(d*x+c)^7*a^7*b*c-4/d^3/(d*x+c)^7*a^6*b^2*c^2-1/7/d/(d*x+c)^7*a^8+8/d^4/(d*x+c)^7*a^5*b^3*c^3-10/d^5/(d*x+c)^7*a^4*b^4*c^4+8/d^6/(d*x+c)^7*a^3*b^5*c^5-4/d^7/(d*x+c)^7*a^2*b^6*c^6+8/7/d^8/(d*x+c)^7*a*b^7*c^7+140/3*b^4/d^5/(d*x+c)^6*a^4*c^3-140/3*b^5/d^6/(d*x+c)^6*a^3*c^4+28*b^6/d^7/(d*x+c)^6*a^2*c^5-28/3*b^7/d^8/(d*x+c)^6*a*c^6+280/3*b^5/d^6/(d*x+c)^3*a^3*$

$$c-140*b^6/d^7/(d*x+c)^3*a^2*c^2+280/3*b^7/d^8/(d*x+c)^3*a*c^3+70*b^4/d^5/(d*x+c)^4*a^4*c-140*b^5/d^6/(d*x+c)^4*a^3*c^2+140*b^6/d^7/(d*x+c)^4*a^2*c^3-70*b^7/d^8/(d*x+c)^4*a*c^4+56*b^7/d^8/(d*x+c)*a*c+168/5*b^3/d^4/(d*x+c)^5*a^5*c-84*b^4/d^5/(d*x+c)^5*a^4*c^2+112*b^5/d^6/(d*x+c)^5*a^3*c^3-84*b^6/d^7/(d*x+c)^5*a^2*c^4+168/5*b^7/d^8/(d*x+c)^5*a*c^5+84*b^6/d^7/(d*x+c)^2*a^2*c-84*b^7/d^8/(d*x+c)^2*a*c^2+28/3*b^2/d^3/(d*x+c)^6*a^6*c-28*b^3/d^4/(d*x+c)^6*a^5*c^2$$

maxima [B] time = 1.96, size = 649, normalized size = 3.11

$$\frac{b^8 x^8}{d^8} \frac{1443 b^8 c^8 - 2178 a b^7 c^7 d + 420 a^2 b^6 c^6 d^2 + 140 a^3 b^5 c^5 d^3 + 70 a^4 b^4 c^4 d^4 + 42 a^5 b^3 c^3 d^5 + 28 a^6 b^2 c^2 d^6 + 20 a^7 b c d^7}{d^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^8/(d*x+c)^8,x, algorithm="maxima")

[Out] $b^8 x/d^8 - 1/105*(1443*b^8*c^8 - 2178*a*b^7*c^7*d + 420*a^2*b^6*c^6*d^2 + 140*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 + 42*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 + 20*a^7*b*c*d^7 + 15*a^8*d^8 + 2940*(b^8*c^2*d^6 - 2*a*b^7*c*d^7 + a^2*b^6*d^8)*x^6 + 2940*(5*b^8*c^3*d^5 - 9*a*b^7*c^2*d^6 + 3*a^2*b^6*c*d^7 + a^3*b^5*d^8)*x^5 + 2450*(13*b^8*c^4*d^4 - 22*a*b^7*c^3*d^5 + 6*a^2*b^6*c^2*d^6 + 2*a^3*b^5*c*d^7 + a^4*b^4*d^8)*x^4 + 490*(77*b^8*c^5*d^3 - 125*a*b^7*c^4*d^4 + 30*a^2*b^6*c^3*d^5 + 10*a^3*b^5*c^2*d^6 + 5*a^4*b^4*c*d^7 + 3*a^5*b^3*d^8)*x^3 + 294*(87*b^8*c^6*d^2 - 137*a*b^7*c^5*d^3 + 30*a^2*b^6*c^4*d^4 + 10*a^3*b^5*c^3*d^5 + 5*a^4*b^4*c^2*d^6 + 3*a^5*b^3*c*d^7 + 2*a^6*b^2*d^8)*x^2 + 14*(669*b^8*c^7*d - 1029*a*b^7*c^6*d^2 + 210*a^2*b^6*c^5*d^3 + 70*a^3*b^5*c^4*d^4 + 35*a^4*b^4*c^3*d^5 + 21*a^5*b^3*c^2*d^6 + 14*a^6*b^2*c*d^7 + 10*a^7*b*d^8)*x)/(d^16*x^7 + 7*c*d^15*x^6 + 21*c^2*d^14*x^5 + 35*c^3*d^13*x^4 + 35*c^4*d^12*x^3 + 21*c^5*d^11*x^2 + 7*c^6*d^10*x + c^7*d^9) - 8*(b^8*c - a*b^7*d)*log(d*x + c)/d^9$

mupad [B] time = 0.43, size = 649, normalized size = 3.11

$$\frac{b^8 x^8}{d^8} \frac{\ln(c + dx) (8 b^8 c - 8 a b^7 d)}{d^9} - \frac{x^4 \left(\frac{70 a^4 b^4 d^7}{3} + \frac{140 a^3 b^5 c d^6}{3} + 140 a^2 b^6 c^2 d^5 - \frac{1540 a b^7 c^3 d^4}{3} + \frac{910 b^8 c^4 d^3}{3} \right) + x^6 \left(\frac{70 a^4 b^4 d^7}{3} + \frac{910 b^8 c^4 d^3}{3} - \frac{1540 a b^7 c^3 d^4}{3} + \frac{140 a^3 b^5 c d^6}{3} + 140 a^2 b^6 c^2 d^5 \right) + x^6 (28 a^2 b^6 d^7 + 28 b^8 c^2 d^5 - 56 a b^7 c d^6) + (15 a^8 d^8 + 1443 b^8 c^8 + 420 a^2 b^6 c^6 d^2 + 140 a^3 b^5 c^5 d^3 + 70 a^4 b^4 c^4 d^4 + 42 a^5 b^3 c^3 d^5 + 28 a^6 b^2 c^2 d^6 + 20 a^7 b c d^7 + 15 a^8 d^8)}{d^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^8/(c + d*x)^8,x)

[Out] $(b^8 x)/d^8 - (\log(c + dx)*(8*b^8*c - 8*a*b^7*d))/d^9 - (x^4*((70*a^4*b^4*d^7)/3 + (910*b^8*c^4*d^3)/3 - (1540*a*b^7*c^3*d^4)/3 + (140*a^3*b^5*c*d^6)/3 + 140*a^2*b^6*c^2*d^5) + x^6*(28*a^2*b^6*d^7 + 28*b^8*c^2*d^5 - 56*a*b^7*c*d^6) + (15*a^8*d^8 + 1443*b^8*c^8 + 420*a^2*b^6*c^6*d^2 + 140*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 + 42*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 + 20*a^7*b*c*d^7 + 15*a^8*d^8)$

$$\begin{aligned}
& 5*d^3 + 70*a^4*b^4*c^4*d^4 + 42*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 2178 \\
& *a*b^7*c^7*d + 20*a^7*b*c*d^7)/(105*d) + x*((446*b^8*c^7)/5 + (4*a^7*b*d^7) \\
& /3 + (28*a^6*b^2*c*d^6)/15 + 28*a^2*b^6*c^5*d^2 + (28*a^3*b^5*c^4*d^3)/3 + \\
& (14*a^4*b^4*c^3*d^4)/3 + (14*a^5*b^3*c^2*d^5)/5 - (686*a*b^7*c^6*d)/5) + x^ \\
& 3*(14*a^5*b^3*d^7 + (1078*b^8*c^5*d^2)/3 - (1750*a*b^7*c^4*d^3)/3 + (70*a^4 \\
& *b^4*c*d^6)/3 + 140*a^2*b^6*c^3*d^4 + (140*a^3*b^5*c^2*d^5)/3) + x^2*((1218 \\
& *b^8*c^6*d)/5 + (28*a^6*b^2*d^7)/5 - (1918*a*b^7*c^5*d^2)/5 + (42*a^5*b^3*c \\
& *d^6)/5 + 84*a^2*b^6*c^4*d^3 + 28*a^3*b^5*c^3*d^4 + 14*a^4*b^4*c^2*d^5) + x \\
& ^5*(28*a^3*b^5*d^7 + 140*b^8*c^3*d^4 - 252*a*b^7*c^2*d^5 + 84*a^2*b^6*c*d^6 \\
&))/(c^7*d^8 + d^15*x^7 + 7*c^6*d^9*x + 7*c*d^14*x^6 + 21*c^5*d^10*x^2 + 35* \\
& c^4*d^11*x^3 + 35*c^3*d^12*x^4 + 21*c^2*d^13*x^5)
\end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**8/(d*x+c)**8,x)

[Out] Timed out

$$3.1364 \quad \int \frac{(a+bx)^7}{(c+dx)^8} dx$$

Optimal. Leaf size=194

$$\frac{7b^6(bc-ad)}{d^8(c+dx)} - \frac{21b^5(bc-ad)^2}{2d^8(c+dx)^2} + \frac{35b^4(bc-ad)^3}{3d^8(c+dx)^3} - \frac{35b^3(bc-ad)^4}{4d^8(c+dx)^4} + \frac{21b^2(bc-ad)^5}{5d^8(c+dx)^5} - \frac{7b(bc-ad)^6}{6d^8(c+dx)^6} + \frac{(bc-ad)^7}{7d^8(c+dx)^7} + \frac{b^7}{d^8}$$

[Out] $1/7*(-a*d+b*c)^7/d^8/(d*x+c)^7-7/6*b*(-a*d+b*c)^6/d^8/(d*x+c)^6+21/5*b^2*(-a*d+b*c)^5/d^8/(d*x+c)^5-35/4*b^3*(-a*d+b*c)^4/d^8/(d*x+c)^4+35/3*b^4*(-a*d+b*c)^3/d^8/(d*x+c)^3-21/2*b^5*(-a*d+b*c)^2/d^8/(d*x+c)^2+7*b^6*(-a*d+b*c)/d^8/(d*x+c)+b^7*ln(d*x+c)/d^8$

Rubi [A] time = 0.21, antiderivative size = 194, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{7b^6(bc-ad)}{d^8(c+dx)} - \frac{21b^5(bc-ad)^2}{2d^8(c+dx)^2} + \frac{35b^4(bc-ad)^3}{3d^8(c+dx)^3} - \frac{35b^3(bc-ad)^4}{4d^8(c+dx)^4} + \frac{21b^2(bc-ad)^5}{5d^8(c+dx)^5} - \frac{7b(bc-ad)^6}{6d^8(c+dx)^6} + \frac{(bc-ad)^7}{7d^8(c+dx)^7} + \frac{b^7}{d^8}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^7/(c + d*x)^8, x]

[Out] $(b*c - a*d)^7/(7*d^8*(c + d*x)^7) - (7*b*(b*c - a*d)^6)/(6*d^8*(c + d*x)^6) + (21*b^2*(b*c - a*d)^5)/(5*d^8*(c + d*x)^5) - (35*b^3*(b*c - a*d)^4)/(4*d^8*(c + d*x)^4) + (35*b^4*(b*c - a*d)^3)/(3*d^8*(c + d*x)^3) - (21*b^5*(b*c - a*d)^2)/(2*d^8*(c + d*x)^2) + (7*b^6*(b*c - a*d))/(d^8*(c + d*x)) + (b^7*Log[c + d*x])/d^8$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^7}{(c+dx)^8} dx = \int \left(\frac{(-bc+ad)^7}{d^7(c+dx)^8} + \frac{7b(bc-ad)^6}{d^7(c+dx)^7} - \frac{21b^2(bc-ad)^5}{d^7(c+dx)^6} + \frac{35b^3(bc-ad)^4}{d^7(c+dx)^5} - \frac{35b^4(bc-ad)^3}{d^7(c+dx)^4} + \frac{21b^5(bc-ad)^2}{d^7(c+dx)^3} - \frac{7b^6(bc-ad)}{d^7(c+dx)^2} + \frac{b^7}{d^7(c+dx)} \right) dx$$

Mathematica [A] time = 0.16, size = 308, normalized size = 1.59

$$(bc - ad) \left(60a^6d^6 + 10a^5bd^5(13c + 49dx) + 2a^4b^2d^4 \left(107c^2 + 539cdx + 882d^2x^2 \right) + a^3b^3d^3 \left(319c^3 + 1813c^2dx + \right. \right.$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^7/(c + d*x)^8,x]

[Out] ((b*c - a*d)*(60*a^6*d^6 + 10*a^5*b*d^5*(13*c + 49*d*x) + 2*a^4*b^2*d^4*(107*c^2 + 539*c*d*x + 882*d^2*x^2) + a^3*b^3*d^3*(319*c^3 + 1813*c^2*d*x + 3969*c*d^2*x^2 + 3675*d^3*x^3) + a^2*b^4*d^2*(459*c^4 + 2793*c^3*d*x + 6909*c^2*d^2*x^2 + 8575*c*d^3*x^3 + 4900*d^4*x^4) + a*b^5*d*(669*c^5 + 4263*c^4*d*x + 11319*c^3*d^2*x^2 + 15925*c^2*d^3*x^3 + 12250*c*d^4*x^4 + 4410*d^5*x^5) + b^6*(1089*c^6 + 7203*c^5*d*x + 20139*c^4*d^2*x^2 + 30625*c^3*d^3*x^3 + 26950*c^2*d^4*x^4 + 13230*c*d^5*x^5 + 2940*d^6*x^6)))/(420*d^8*(c + d*x)^7) + (b^7*Log[c + d*x])/d^8

fricas [B] time = 0.55, size = 625, normalized size = 3.22

$$1089 b^7 c^7 - 420 a b^6 c^6 d - 210 a^2 b^5 c^5 d^2 - 140 a^3 b^4 c^4 d^3 - 105 a^4 b^3 c^3 d^4 - 84 a^5 b^2 c^2 d^5 - 70 a^6 b c d^6 - 60 a^7 d^7 + 2940$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/(d*x+c)^8,x, algorithm="fricas")

[Out] 1/420*(1089*b^7*c^7 - 420*a*b^6*c^6*d - 210*a^2*b^5*c^5*d^2 - 140*a^3*b^4*c^4*d^3 - 105*a^4*b^3*c^3*d^4 - 84*a^5*b^2*c^2*d^5 - 70*a^6*b*c*d^6 - 60*a^7*d^7 + 2940*(b^7*c*d^6 - a*b^6*d^7)*x^6 + 4410*(3*b^7*c^2*d^5 - 2*a*b^6*c*d^6 - a^2*b^5*d^7)*x^5 + 2450*(11*b^7*c^3*d^4 - 6*a*b^6*c^2*d^5 - 3*a^2*b^5*c*d^6 - 2*a^3*b^4*d^7)*x^4 + 1225*(25*b^7*c^4*d^3 - 12*a*b^6*c^3*d^4 - 6*a^2*b^5*c^2*d^5 - 4*a^3*b^4*c*d^6 - 3*a^4*b^3*d^7)*x^3 + 147*(137*b^7*c^5*d^2 - 60*a*b^6*c^4*d^3 - 30*a^2*b^5*c^3*d^4 - 20*a^3*b^4*c^2*d^5 - 15*a^4*b^3*c*d^6 - 12*a^5*b^2*d^7)*x^2 + 49*(147*b^7*c^6*d - 60*a*b^6*c^5*d^2 - 30*a^2*b^5*c^4*d^3 - 20*a^3*b^4*c^3*d^4 - 15*a^4*b^3*c^2*d^5 - 12*a^5*b^2*c*d^6 - 10*a^6*b*d^7)*x + 420*(b^7*d^7*x^7 + 7*b^7*c*d^6*x^6 + 21*b^7*c^2*d^5*x^5 + 35*b^7*c^3*d^4*x^4 + 35*b^7*c^4*d^3*x^3 + 21*b^7*c^5*d^2*x^2 + 7*b^7*c^6*d*x + b^7*c^7)*log(d*x + c))/(d^15*x^7 + 7*c*d^14*x^6 + 21*c^2*d^13*x^5 + 35*c^3*d^12*x^4 + 35*c^4*d^11*x^3 + 21*c^5*d^10*x^2 + 7*c^6*d^9*x + c^7*d^8)

giac [B] time = 1.30, size = 467, normalized size = 2.41

$$\frac{b^7 \log(|dx + c|)}{d^8} + \frac{2940 (b^7 c d^5 - a b^6 d^6) x^6 + 4410 (3 b^7 c^2 d^4 - 2 a b^6 c d^5 - a^2 b^5 d^6) x^5 + 2450 (11 b^7 c^3 d^3 - 6 a b^6 c^2 d^4 - a^2 b^5 c d^5 + 3 a^3 b^4 d^6) x^4 + 1225 (25 b^7 c^4 d^3 - 12 a b^6 c^3 d^4 - 6 a^2 b^5 c^2 d^5 - 4 a^3 b^4 c d^6 - 3 a^4 b^3 d^7) x^3 + 147 (137 b^7 c^5 d^2 - 60 a b^6 c^4 d^3 - 30 a^2 b^5 c^3 d^4 - 20 a^3 b^4 c^2 d^5 - 15 a^4 b^3 c d^6 - 12 a^5 b^2 d^7) x^2 + 49 (147 b^7 c^6 d - 60 a b^6 c^5 d^2 - 30 a^2 b^5 c^4 d^3 - 20 a^3 b^4 c^3 d^4 - 15 a^4 b^3 c^2 d^5 - 12 a^5 b^2 c d^6 - 10 a^6 b d^7) x + 420 (b^7 d^7 x^7 + 7 b^7 c d^6 x^6 + 21 b^7 c^2 d^5 x^5 + 35 b^7 c^3 d^4 x^4 + 35 b^7 c^4 d^3 x^3 + 21 b^7 c^5 d^2 x^2 + 7 b^7 c^6 d x + b^7 c^7) \log(d x + c)}{d^{15} x^7 + 7 c d^{14} x^6 + 21 c^2 d^{13} x^5 + 35 c^3 d^{12} x^4 + 35 c^4 d^{11} x^3 + 21 c^5 d^{10} x^2 + 7 c^6 d^9 x + c^7 d^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/(d*x+c)^8,x, algorithm="giac")

[Out] $b^7 \log(\text{abs}(d*x + c))/d^8 + 1/420*(2940*(b^7*c*d^5 - a*b^6*d^6)*x^6 + 4410*(3*b^7*c^2*d^4 - 2*a*b^6*c*d^5 - a^2*b^5*d^6)*x^5 + 2450*(11*b^7*c^3*d^3 - 6*a*b^6*c^2*d^4 - 3*a^2*b^5*c*d^5 - 2*a^3*b^4*d^6)*x^4 + 1225*(25*b^7*c^4*d^2 - 12*a*b^6*c^3*d^3 - 6*a^2*b^5*c^2*d^4 - 4*a^3*b^4*c*d^5 - 3*a^4*b^3*d^6)*x^3 + 147*(137*b^7*c^5*d - 60*a*b^6*c^4*d^2 - 30*a^2*b^5*c^3*d^3 - 20*a^3*b^4*c^2*d^4 - 15*a^4*b^3*c*d^5 - 12*a^5*b^2*d^6)*x^2 + 49*(147*b^7*c^6 - 60*a*b^6*c^5*d - 30*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 - 15*a^4*b^3*c^2*d^4 - 12*a^5*b^2*c*d^5 - 10*a^6*b*d^6)*x + (1089*b^7*c^7 - 420*a*b^6*c^6*d - 210*a^2*b^5*c^5*d^2 - 140*a^3*b^4*c^4*d^3 - 105*a^4*b^3*c^3*d^4 - 84*a^5*b^2*c^2*d^5 - 70*a^6*b*c*d^6 - 60*a^7*d^7)/d)/((d*x + c)^7*d^7)$

maple [B] time = 0.01, size = 672, normalized size = 3.46

$$\frac{a^7}{7(dx+c)^7 d} + \frac{a^6 b c}{(dx+c)^7 d^2} - \frac{3a^5 b^2 c^2}{(dx+c)^7 d^3} + \frac{5a^4 b^3 c^3}{(dx+c)^7 d^4} - \frac{5a^3 b^4 c^4}{(dx+c)^7 d^5} + \frac{3a^2 b^5 c^5}{(dx+c)^7 d^6} - \frac{a b^6 c^6}{(dx+c)^7 d^7} + \frac{b^7 c^7}{7(dx+c)^7 d^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^7/(d*x+c)^8,x)

[Out] $-35/3*b^4/d^5/(d*x+c)^3*a^3+35/3*b^7/d^8/(d*x+c)^3*c^3-21/2*b^5/d^6/(d*x+c)^2*a^2-21/2*b^7/d^8/(d*x+c)^2*c^2+1/7/d^8/(d*x+c)^7*b^7*c^7-7*b^6/d^7/(d*x+c)*a+7*b^7/d^8/(d*x+c)*c-21/5*b^2/d^3/(d*x+c)^5*a^5+21/5*b^7/d^8/(d*x+c)^5*c^5-7/6*b/d^2/(d*x+c)^6*a^6-7/6*b^7/d^8/(d*x+c)^6*c^6-35/4*b^3/d^4/(d*x+c)^4*a^4-35/4*b^7/d^8/(d*x+c)^4*c^4-21*b^6/d^7/(d*x+c)^5*a*c^4+35*b^6/d^7/(d*x+c)^4*a*c^3+35*b^5/d^6/(d*x+c)^3*a^2*c-35*b^6/d^7/(d*x+c)^3*a*c^2+21*b^6/d^7/(d*x+c)^2*a*c+21*b^3/d^4/(d*x+c)^5*a^4*c-42*b^4/d^5/(d*x+c)^5*a^3*c^2+42*b^5/d^6/(d*x+c)^5*a^2*c^3+b^7*ln(d*x+c)/d^8-1/7/d/(d*x+c)^7*a^7-3/d^3/(d*x+c)^7*a^5*b^2*c^2+5/d^4/(d*x+c)^7*a^4*b^3*c^3-5/d^5/(d*x+c)^7*a^3*b^4*c^4+3/d^6/(d*x+c)^7*a^2*b^5*c^5-1/d^7/(d*x+c)^7*a*b^6*c^6+7*b^2/d^3/(d*x+c)^6*a^5*c-35/2*b^3/d^4/(d*x+c)^6*a^4*c^2+70/3*b^4/d^5/(d*x+c)^6*a^3*c^3-35/2*b^5/d^6/(d*x+c)^6*a^2*c^4+7*b^6/d^7/(d*x+c)^6*a*c^5+35*b^4/d^5/(d*x+c)^4*a^3*c-105/2*b^5/d^6/(d*x+c)^4*a^2*c^2+1/d^2/(d*x+c)^7*a^6*b*c$

maxima [B] time = 1.66, size = 535, normalized size = 2.76

$$\frac{1089 b^7 c^7 - 420 a b^6 c^6 d - 210 a^2 b^5 c^5 d^2 - 140 a^3 b^4 c^4 d^3 - 105 a^4 b^3 c^3 d^4 - 84 a^5 b^2 c^2 d^5 - 70 a^6 b c d^6 - 60 a^7 d^7 + 2940}{(d*x+c)^7 d^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^7/(d*x+c)^8,x, algorithm="maxima")

[Out] $\frac{1}{420} \cdot (1089b^7c^7 - 420a^2b^6c^6d - 210a^2b^5c^5d^2 - 140a^3b^4c^4d^3 - 105a^4b^3c^3d^4 - 84a^5b^2c^2d^5 - 70a^6b^1c^1d^6 - 60a^7d^7 + 2940(b^7c^6d^6 - ab^6d^7))x^6 + 4410(3b^7c^2d^5 - 2ab^6c^1d^6 - a^2b^5d^7)x^5 + 2450(11b^7c^3d^4 - 6ab^6c^2d^5 - 3a^2b^5c^1d^6 - 2a^3b^4d^7)x^4 + 1225(25b^7c^4d^3 - 12ab^6c^3d^4 - 6a^2b^5c^2d^5 - 4a^3b^4c^1d^6 - 3a^4b^3d^7)x^3 + 147(137b^7c^5d^2 - 60ab^6c^4d^3 - 30a^2b^5c^3d^4 - 20a^3b^4c^2d^5 - 15a^4b^3c^1d^6 - 12a^5b^2d^7)x^2 + 49(147b^7c^6d - 60ab^6c^5d^2 - 30a^2b^5c^4d^3 - 20a^3b^4c^3d^4 - 15a^4b^3c^2d^5 - 12a^5b^2c^1d^6 - 10a^6b^1d^7)x + 35c^4d^11x^3 + 21c^5d^10x^2 + 7c^6d^9x + c^7d^8) + b^7 \log(dx + c)/d^8$

mupad [B] time = 0.38, size = 460, normalized size = 2.37

$$\frac{b^7 \ln(c + dx)}{d^8} - \frac{x \left(\frac{7a^6bd^7}{6} + \frac{7a^5b^2cd^6}{5} + \frac{7a^4b^3c^2d^5}{4} + \frac{7a^3b^4c^3d^4}{3} + \frac{7a^2b^5c^4d^3}{2} + 7ab^6c^5d^2 - \frac{343b^7c^6d}{20} \right) + x^6 (7ab^6c^5d^2 + (7a^5b^2c^1d^6)/5 + (7a^4b^3c^2d^5)/4 + (7a^3b^4c^3d^4)/3 + (7a^2b^5c^4d^3)/2 + (7a^1b^6c^5d^2) + x^6(7a^6b^1d^7 - 7b^7c^1d^6) + x^3((35a^4b^3d^7)/4 - (875b^7c^4d^3)/12 + 35ab^6c^3d^4 + (35a^3b^4c^1d^6)/3 + (35a^2b^5c^2d^5)/2) + x^5((21a^2b^5d^7)/2 - (63b^7c^2d^5)/2 + 21ab^6c^4d^3 + (21a^4b^3c^1d^6)/4 + (21a^2b^5c^3d^4)/2 + 7a^3b^4c^2d^5) + (a^7d^7)/7 - (363b^7c^7)/140 + x^4((35a^3b^4d^7)/3 - (385b^7c^3d^4)/6 + 35ab^6c^2d^5 + (35a^2b^5c^1d^6)/2) + (a^2b^5c^5d^2)/2 + (a^3b^4c^4d^3)/3 + (a^4b^3c^3d^4)/4 + (a^5b^2c^2d^5)/5 + ab^6c^6d + (a^6b^1c^1d^6)/6) / (d^8(c + dx)^7)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^7/(c + d*x)^8, x)`

[Out] $(b^7 \log(c + dx))/d^8 - (x * ((7a^6b^1d^7)/6 - (343b^7c^6d)/20 + 7a^2b^5c^5d^2 + (7a^5b^2c^1d^6)/5 + (7a^4b^3c^2d^5)/2 + (7a^3b^4c^3d^4)/3 + (7a^2b^5c^4d^3)/4) + x^6(7a^6b^1d^7 - 7b^7c^1d^6) + x^3((35a^4b^3d^7)/4 - (875b^7c^4d^3)/12 + 35ab^6c^3d^4 + (35a^3b^4c^1d^6)/3 + (35a^2b^5c^2d^5)/2) + x^5((21a^2b^5d^7)/2 - (63b^7c^2d^5)/2 + 21ab^6c^4d^3 + (21a^4b^3c^1d^6)/4 + (21a^2b^5c^3d^4)/2 + 7a^3b^4c^2d^5) + (a^7d^7)/7 - (363b^7c^7)/140 + x^4((35a^3b^4d^7)/3 - (385b^7c^3d^4)/6 + 35ab^6c^2d^5 + (35a^2b^5c^1d^6)/2) + (a^2b^5c^5d^2)/2 + (a^3b^4c^4d^3)/3 + (a^4b^3c^3d^4)/4 + (a^5b^2c^2d^5)/5 + ab^6c^6d + (a^6b^1c^1d^6)/6) / (d^8(c + d*x)^7)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**7/(d*x+c)**8, x)`

[Out] Timed out

$$3.1365 \quad \int \frac{(a+bx)^6}{(c+dx)^8} dx$$

Optimal. Leaf size=28

$$\frac{(a+bx)^7}{7(c+dx)^7(bc-ad)}$$

[Out] 1/7*(b*x+a)^7/(-a*d+b*c)/(d*x+c)^7

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {37}

$$\frac{(a+bx)^7}{7(c+dx)^7(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^6/(c + d*x)^8, x]

[Out] (a + b*x)^7/(7*(b*c - a*d)*(c + d*x)^7)

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(a+bx)^6}{(c+dx)^8} dx = \frac{(a+bx)^7}{7(bc-ad)(c+dx)^7}$$

Mathematica [B] time = 0.09, size = 271, normalized size = 9.68

$$\frac{a^6d^6 + a^5bd^5(c + 7dx) + a^4b^2d^4(c^2 + 7cdx + 21d^2x^2) + a^3b^3d^3(c^3 + 7c^2dx + 21cd^2x^2 + 35d^3x^3) + a^2b^4d^2(c^4 + 7c^3dx + 21c^2d^2x^2 + 35cd^3x^3) + ab^5d(c^5 + 7c^4dx + 21c^3d^2x^2 + 35c^2d^3x^3) + a^6b^6}{7(bc-ad)(c+dx)^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^6/(c + d*x)^8, x]

[Out] -1/7*(a^6*d^6 + a^5*b*d^5*(c + 7*d*x) + a^4*b^2*d^4*(c^2 + 7*c*d*x + 21*d^2*x^2) + a^3*b^3*d^3*(c^3 + 7*c^2*d*x + 21*c*d^2*x^2 + 35*d^3*x^3) + a^2*b^4*d^2*(c^4 + 7*c^3*d*x + 21*c^2*d^2*x^2 + 35*c*d^3*x^3) + a*b^5*d*(c^5 + 7*c^4*d*x + 21*c^3*d^2*x^2 + 35*c^2*d^3*x^3) + a^6*b^6)

$*d^2*(c^4 + 7*c^3*d*x + 21*c^2*d^2*x^2 + 35*c*d^3*x^3 + 35*d^4*x^4) + a*b^5$
 $*d*(c^5 + 7*c^4*d*x + 21*c^3*d^2*x^2 + 35*c^2*d^3*x^3 + 35*c*d^4*x^4 + 21*d$
 $^5*x^5) + b^6*(c^6 + 7*c^5*d*x + 21*c^4*d^2*x^2 + 35*c^3*d^3*x^3 + 35*c^2*d$
 $^4*x^4 + 21*c*d^5*x^5 + 7*d^6*x^6))/(d^7*(c + d*x)^7)$

fricas [B] time = 0.47, size = 398, normalized size = 14.21

$$\frac{7b^6d^6x^6 + b^6c^6 + ab^5c^5d + a^2b^4c^4d^2 + a^3b^3c^3d^3 + a^4b^2c^2d^4 + a^5bcd^5 + a^6d^6 + 21(b^6cd^5 + ab^5d^6)x^5 + 35(b^6c^2d^4 + ab^5c^2d^4)x^4 + \dots}{(d^7(c + dx)^7)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6/(d*x+c)^8,x, algorithm="fricas")

[Out] $-1/7*(7*b^6*d^6*x^6 + b^6*c^6 + a*b^5*c^5*d + a^2*b^4*c^4*d^2 + a^3*b^3*c^3$
 $*d^3 + a^4*b^2*c^2*d^4 + a^5*b*c*d^5 + a^6*d^6 + 21*(b^6*c*d^5 + a*b^5*d^6)$
 $*x^5 + 35*(b^6*c^2*d^4 + a*b^5*c*d^5 + a^2*b^4*d^6)*x^4 + 35*(b^6*c^3*d^3 +$
 $a*b^5*c^2*d^4 + a^2*b^4*c*d^5 + a^3*b^3*d^6)*x^3 + 21*(b^6*c^4*d^2 + a*b^5$
 $*c^3*d^3 + a^2*b^4*c^2*d^4 + a^3*b^3*c*d^5 + a^4*b^2*d^6)*x^2 + 7*(b^6*c^5*$
 $d + a*b^5*c^4*d^2 + a^2*b^4*c^3*d^3 + a^3*b^3*c^2*d^4 + a^4*b^2*c*d^5 + a^5$
 $*b*d^6)*x)/(d^14*x^7 + 7*c*d^13*x^6 + 21*c^2*d^12*x^5 + 35*c^3*d^11*x^4 + 3$
 $5*c^4*d^10*x^3 + 21*c^5*d^9*x^2 + 7*c^6*d^8*x + c^7*d^7)$

giac [B] time = 1.28, size = 369, normalized size = 13.18

$$\frac{7b^6d^6x^6 + 21b^6cd^5x^5 + 21ab^5d^6x^5 + 35b^6c^2d^4x^4 + 35ab^5cd^5x^4 + 35a^2b^4d^6x^4 + 35b^6c^3d^3x^3 + 35ab^5c^2d^4x^3 + \dots}{(d^7(c + dx)^8)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^6/(d*x+c)^8,x, algorithm="giac")

[Out] $-1/7*(7*b^6*d^6*x^6 + 21*b^6*c*d^5*x^5 + 21*a*b^5*d^6*x^5 + 35*b^6*c^2*d^4*$
 $x^4 + 35*a*b^5*c*d^5*x^4 + 35*a^2*b^4*d^6*x^4 + 35*b^6*c^3*d^3*x^3 + 35*a*b$
 $^5*c^2*d^4*x^3 + 35*a^2*b^4*c*d^5*x^3 + 35*a^3*b^3*d^6*x^3 + 21*b^6*c^4*d^2$
 $*x^2 + 21*a*b^5*c^3*d^3*x^2 + 21*a^2*b^4*c^2*d^4*x^2 + 21*a^3*b^3*c*d^5*x^2$
 $+ 21*a^4*b^2*d^6*x^2 + 7*b^6*c^5*d*x + 7*a*b^5*c^4*d^2*x + 7*a^2*b^4*c^3*d$
 $^3*x + 7*a^3*b^3*c^2*d^4*x + 7*a^4*b^2*c*d^5*x + 7*a^5*b*d^6*x + b^6*c^6 +$
 $a*b^5*c^5*d + a^2*b^4*c^4*d^2 + a^3*b^3*c^3*d^3 + a^4*b^2*c^2*d^4 + a^5*b*c$
 $*d^5 + a^6*d^6)/((d*x + c)^7*d^7)$

maple [B] time = 0.01, size = 357, normalized size = 12.75

$$\frac{b^6}{(dx + c)d^7} - \frac{3(ad - bc)b^5}{(dx + c)^2d^7} - \frac{5(a^2d^2 - 2abcd + b^2c^2)b^4}{(dx + c)^3d^7} - \frac{5(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)b^3}{(dx + c)^4d^7} - \frac{3(a^4d^4 - 4a^3cd^3 + 6a^2b^2cd^2 - 4ab^3c^2d + b^4c^3)}{(dx + c)^5d^7}$$

$$\frac{1}{(c^7 + d^7 x^7 + 7cd^6 x^6 + 21c^5 d^2 x^2 + 35c^4 d^3 x^3 + 35c^3 d^4 x^4 + 21c^2 d^5 x^5 + 7c^6 d x)}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**6/(d*x+c)**8,x)

[Out] Timed out

$$3.1366 \quad \int \frac{(a+bx)^5}{(c+dx)^8} dx$$

Optimal. Leaf size=58

$$\frac{b(a+bx)^6}{42(c+dx)^6(bc-ad)^2} + \frac{(a+bx)^6}{7(c+dx)^7(bc-ad)}$$

[Out] 1/7*(b*x+a)^6/(-a*d+b*c)/(d*x+c)^7+1/42*b*(b*x+a)^6/(-a*d+b*c)^2/(d*x+c)^6

Rubi [A] time = 0.01, antiderivative size = 58, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{b(a+bx)^6}{42(c+dx)^6(bc-ad)^2} + \frac{(a+bx)^6}{7(c+dx)^7(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(c + d*x)^8, x]

[Out] (a + b*x)^6/(7*(b*c - a*d)*(c + d*x)^7) + (b*(a + b*x)^6)/(42*(b*c - a*d)^2*(c + d*x)^6)

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{(a+bx)^5}{(c+dx)^8} dx = \frac{(a+bx)^6}{7(bc-ad)(c+dx)^7} + \frac{b \int \frac{(a+bx)^5}{(c+dx)^7} dx}{7(bc-ad)}$$

$$= \frac{(a+bx)^6}{7(bc-ad)(c+dx)^7} + \frac{b(a+bx)^6}{42(bc-ad)^2(c+dx)^6}$$

Mathematica [B] time = 0.06, size = 205, normalized size = 3.53

$$\frac{6a^5d^5 + 5a^4bd^4(c+7dx) + 4a^3b^2d^3(c^2+7cdx+21d^2x^2) + 3a^2b^3d^2(c^3+7c^2dx+21cd^2x^2+35d^3x^3) + 2ab^4d(c^4+7c^3dx+21c^2d^2x^2+35cd^3x^3+35d^4x^4) + b^5(c^5+7c^4dx+21c^3d^2x^2+35c^2d^3x^3+35cd^4x^4+21d^5x^5)}{42d^6(c+dx)^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(c + d*x)^8, x]

[Out] -1/42*(6*a^5*d^5 + 5*a^4*b*d^4*(c + 7*d*x) + 4*a^3*b^2*d^3*(c^2 + 7*c*d*x + 21*d^2*x^2) + 3*a^2*b^3*d^2*(c^3 + 7*c^2*d*x + 21*c*d^2*x^2 + 35*d^3*x^3) + 2*a*b^4*d*(c^4 + 7*c^3*d*x + 21*c^2*d^2*x^2 + 35*c*d^3*x^3 + 35*d^4*x^4) + b^5*(c^5 + 7*c^4*d*x + 21*c^3*d^2*x^2 + 35*c^2*d^3*x^3 + 35*c*d^4*x^4 + 21*d^5*x^5))/(d^6*(c + d*x)^7)

fricas [B] time = 0.43, size = 326, normalized size = 5.62

$$\frac{21b^5d^5x^5 + b^5c^5 + 2ab^4c^4d + 3a^2b^3c^3d^2 + 4a^3b^2c^2d^3 + 5a^4bcd^4 + 6a^5d^5 + 35(b^5cd^4 + 2ab^4d^5)x^4 + 35(b^5c^2d^3 + 2ab^4c^3d^4 + 3a^2b^3c^2d^5)x^3 + 21(b^5c^3d^2 + 2a^2b^4c^2d^3 + 3a^2b^3c^2d^4 + 4a^3b^2c^2d^5)x^2 + 7(b^5c^4d + 2a^2b^4c^3d^2 + 3a^2b^3c^2d^3 + 4a^3b^2c^2d^4 + 5a^4b^2c^2d^5)x}{42(d^{13}x^7 + 7cd^{12}x^6 + 21c^2d^{11}x^5 + 35c^3d^{10}x^4 + 35c^4d^9x^3 + 21c^5d^8x^2 + 7c^6d^7x + c^7d^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^8, x, algorithm="fricas")

[Out] -1/42*(21*b^5*d^5*x^5 + b^5*c^5 + 2*a*b^4*c^4*d + 3*a^2*b^3*c^3*d^2 + 4*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 + 6*a^5*d^5 + 35*(b^5*c*d^4 + 2*a*b^4*d^5)*x^4 + 35*(b^5*c^2*d^3 + 2*a*b^4*c*d^4 + 3*a^2*b^3*d^5)*x^3 + 21*(b^5*c^3*d^2 + 2*a*b^4*c^2*d^3 + 3*a^2*b^3*c*d^4 + 4*a^3*b^2*d^5)*x^2 + 7*(b^5*c^4*d + 2*a*b^4*c^3*d^2 + 3*a^2*b^3*c^2*d^3 + 4*a^3*b^2*c*d^4 + 5*a^4*b*d^5)*x)/(d^13*x^7 + 7*c*d^12*x^6 + 21*c^2*d^11*x^5 + 35*c^3*d^10*x^4 + 35*c^4*d^9*x^3 + 21*c^5*d^8*x^2 + 7*c^6*d^7*x + c^7*d^6)

giac [B] time = 1.32, size = 271, normalized size = 4.67

$$\frac{21b^5d^5x^5 + 35b^5cd^4x^4 + 70ab^4d^5x^4 + 35b^5c^2d^3x^3 + 70ab^4cd^4x^3 + 105a^2b^3d^5x^3 + 21b^5c^3d^2x^2 + 42ab^4c^2d^3x^2 + 7(b^5c^4d + 2a^2b^4c^3d^2 + 3a^2b^3c^2d^3 + 4a^3b^2c^2d^4 + 5a^4b^2c^2d^5)x}{42(d^{13}x^7 + 7cd^{12}x^6 + 21c^2d^{11}x^5 + 35c^3d^{10}x^4 + 35c^4d^9x^3 + 21c^5d^8x^2 + 7c^6d^7x + c^7d^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^8,x, algorithm="giac")

[Out]
$$-1/42*(21*b^5*d^5*x^5 + 35*b^5*c*d^4*x^4 + 70*a*b^4*d^5*x^4 + 35*b^5*c^2*d^3*x^3 + 70*a*b^4*c*d^4*x^3 + 105*a^2*b^3*d^5*x^3 + 21*b^5*c^3*d^2*x^2 + 42*a*b^4*c^2*d^3*x^2 + 63*a^2*b^3*c*d^4*x^2 + 84*a^3*b^2*d^5*x^2 + 7*b^5*c^4*d*x + 14*a*b^4*c^3*d^2*x + 21*a^2*b^3*c^2*d^3*x + 28*a^3*b^2*c*d^4*x + 35*a^4*b*d^5*x + b^5*c^5 + 2*a*b^4*c^4*d + 3*a^2*b^3*c^3*d^2 + 4*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 + 6*a^5*d^5)/((d*x + c)^7*d^6)$$

maple [B] time = 0.01, size = 265, normalized size = 4.57

$$\frac{b^5}{2(dx+c)^2d^6} - \frac{5(ad-bc)b^4}{3(dx+c)^3d^6} - \frac{5(a^2d^2-2abcd+b^2c^2)b^3}{2(dx+c)^4d^6} - \frac{2(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)b^2}{(dx+c)^5d^6} - \frac{5(a^4d^4-4a^3bcd^3+3a^2b^2c^2d-b^3c^3b)}{(dx+c)^6d^6} - \frac{5(a^5d^5-4a^4b^2cd^3+3a^3b^2c^2d-2a^2b^3c^3d+b^4c^4)}{(dx+c)^7d^6} - \frac{5(a^4b^2cd^3+3a^3b^2c^2d-2a^2b^3c^3d+b^4c^4)}{(dx+c)^8d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(d*x+c)^8,x)

[Out]
$$-1/7*(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)/d^6/(d*x+c)^7-5/3*b^4*(a*d-b*c)/d^6/(d*x+c)^3-5/6*b*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/d^6/(d*x+c)^6-2*b^2*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/d^6/(d*x+c)^5-5/2*b^3*(a^2*d^2-2*a*b*c*d+b^2*c^2)/d^6/(d*x+c)^4-1/2*b^5/d^6/(d*x+c)^2$$

maxima [B] time = 1.58, size = 326, normalized size = 5.62

$$\frac{21b^5d^5x^5 + b^5c^5 + 2ab^4c^4d + 3a^2b^3c^3d^2 + 4a^3b^2c^2d^3 + 5a^4bcd^4 + 6a^5d^5 + 35(b^5cd^4 + 2ab^4d^5)x^4 + 35(b^5c^2d^3 + 5a^2b^3c^2d^3 + 3a^3b^2c^2d^3 + 4a^4bcd^4 + 5a^5d^5)x^3 + 35(b^5c^3d^2 + 2a^2b^3c^3d^2 + 3a^3b^2c^3d^2 + 4a^4bcd^4 + 5a^5d^5)x^2 + 35(b^5c^4d + 2a^2b^3c^4d + 3a^3b^2c^4d + 4a^4bcd^4 + 5a^5d^5)x + 35(b^5c^5 + 2a^2b^3c^5 + 3a^3b^2c^5 + 4a^4bcd^4 + 5a^5d^5)}{42(d^{13}x^7 + 7cd^{12}x^6 + 21c^2d^{11}x^5 + 35c^3d^{10}x^4 + 35c^4d^9x^3 + 21c^5d^8x^2 + 7c^6d^7x + c^7d^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^8,x, algorithm="maxima")

[Out]
$$-1/42*(21*b^5*d^5*x^5 + b^5*c^5 + 2*a*b^4*c^4*d + 3*a^2*b^3*c^3*d^2 + 4*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 + 6*a^5*d^5 + 35*(b^5*c*d^4 + 2*a*b^4*d^5)*x^4 + 35*(b^5*c^2*d^3 + 2*a*b^4*c*d^4 + 3*a^2*b^3*d^5)*x^3 + 21*(b^5*c^3*d^2 + 2*a*b^4*c^2*d^3 + 3*a^2*b^3*c*d^4 + 4*a^3*b^2*d^5)*x^2 + 7*(b^5*c^4*d + 2*a*b^4*c^3*d^2 + 3*a^2*b^3*c^2*d^3 + 4*a^3*b^2*c*d^4 + 5*a^4*b*d^5)*x)/(d^13*x^7 + 7*c*d^12*x^6 + 21*c^2*d^11*x^5 + 35*c^3*d^10*x^4 + 35*c^4*d^9*x^3 + 21*c^5*d^8*x^2 + 7*c^6*d^7*x + c^7*d^6)$$

mupad [B] time = 0.28, size = 39, normalized size = 0.67

$$\frac{(a+bx)^6(7bc-6ad+bdx)}{42(ad-bc)^2(c+dx)^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(c + d*x)^8,x)`

[Out] $((a + b*x)^6*(7*b*c - 6*a*d + b*d*x))/(42*(a*d - b*c)^2*(c + d*x)^7)$

sympy [B] time = 54.91, size = 354, normalized size = 6.10

$$\frac{-6a^5d^5 - 5a^4bcd^4 - 4a^3b^2c^2d^3 - 3a^2b^3c^3d^2 - 2ab^4c^4d - b^5c^5 - 21b^5d^5x^5 + x^4(-70ab^4d^5 - 35b^5cd^4) + x^3(-105a^2b^3c^2d^3 - 70a^2b^3c^3d^2 - 35a^2b^3c^4d - 14a^2b^3c^5) + x^2(-84a^3b^2c^2d^3 - 42a^3b^2c^3d^2 - 21a^3b^2c^4d - 7a^3b^2c^5) + x(-35a^4b^2c^2d^3 - 21a^4b^2c^3d^2 - 7a^4b^2c^4d) + 42c^7d^6 + 294c^6d^7x + 882c^5d^8}{42c^7d^6 + 294c^6d^7x + 882c^5d^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(d*x+c)**8,x)`

[Out] $(-6*a**5*d**5 - 5*a**4*b*c*d**4 - 4*a**3*b**2*c**2*d**3 - 3*a**2*b**3*c**3*d**2 - 2*a*b**4*c**4*d - b**5*c**5 - 21*b**5*d**5*x**5 + x**4*(-70*a*b**4*d**5 - 35*b**5*c*d**4) + x**3*(-105*a**2*b**3*d**5 - 70*a*b**4*c*d**4 - 35*b**5*c**2*d**3) + x**2*(-84*a**3*b**2*d**5 - 63*a**2*b**3*c*d**4 - 42*a*b**4*c**2*d**3 - 21*b**5*c**3*d**2) + x*(-35*a**4*b*d**5 - 28*a**3*b**2*c*d**4 - 21*a**2*b**3*c**2*d**3 - 14*a*b**4*c**3*d**2 - 7*b**5*c**4*d))/(42*c**7*d**6 + 294*c**6*d**7*x + 882*c**5*d**8*x**2 + 1470*c**4*d**9*x**3 + 1470*c**3*d**10*x**4 + 882*c**2*d**11*x**5 + 294*c*d**12*x**6 + 42*d**13*x**7)$

$$3.1367 \quad \int \frac{(a+bx)^4}{(c+dx)^8} dx$$

Optimal. Leaf size=89

$$\frac{b^2(a+bx)^5}{105(c+dx)^5(bc-ad)^3} + \frac{b(a+bx)^5}{21(c+dx)^6(bc-ad)^2} + \frac{(a+bx)^5}{7(c+dx)^7(bc-ad)}$$

[Out] $1/7*(b*x+a)^5/(-a*d+b*c)/(d*x+c)^7+1/21*b*(b*x+a)^5/(-a*d+b*c)^2/(d*x+c)^6+1/105*b^2*(b*x+a)^5/(-a*d+b*c)^3/(d*x+c)^5$

Rubi [A] time = 0.02, antiderivative size = 89, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {45, 37}

$$\frac{b^2(a+bx)^5}{105(c+dx)^5(bc-ad)^3} + \frac{b(a+bx)^5}{21(c+dx)^6(bc-ad)^2} + \frac{(a+bx)^5}{7(c+dx)^7(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4/(c + d*x)^8, x]

[Out] $(a + b*x)^5/(7*(b*c - a*d)*(c + d*x)^7) + (b*(a + b*x)^5)/(21*(b*c - a*d)^2*(c + d*x)^6) + (b^2*(a + b*x)^5)/(105*(b*c - a*d)^3*(c + d*x)^5)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^4}{(c+dx)^8} dx &= \frac{(a+bx)^5}{7(bc-ad)(c+dx)^7} + \frac{(2b) \int \frac{(a+bx)^4}{(c+dx)^7} dx}{7(bc-ad)} \\
&= \frac{(a+bx)^5}{7(bc-ad)(c+dx)^7} + \frac{b(a+bx)^5}{21(bc-ad)^2(c+dx)^6} + \frac{b^2 \int \frac{(a+bx)^4}{(c+dx)^6} dx}{21(bc-ad)^2} \\
&= \frac{(a+bx)^5}{7(bc-ad)(c+dx)^7} + \frac{b(a+bx)^5}{21(bc-ad)^2(c+dx)^6} + \frac{b^2(a+bx)^5}{105(bc-ad)^3(c+dx)^5}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 144, normalized size = 1.62

$$\frac{15a^4d^4 + 10a^3bd^3(c+7dx) + 6a^2b^2d^2(c^2+7cdx+21d^2x^2) + 3ab^3d(c^3+7c^2dx+21cd^2x^2+35d^3x^3) + b^4(c^4+7c^3dx+21c^2d^2x^2+35cd^3x^3+35d^4x^4)}{105d^5(c+dx)^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4/(c + d*x)^8,x]

[Out] -1/105*(15*a^4*d^4 + 10*a^3*b*d^3*(c + 7*d*x) + 6*a^2*b^2*d^2*(c^2 + 7*c*d*x + 21*d^2*x^2) + 3*a*b^3*d*(c^3 + 7*c^2*d*x + 21*c*d^2*x^2 + 35*d^3*x^3) + b^4*(c^4 + 7*c^3*d*x + 21*c^2*d^2*x^2 + 35*c*d^3*x^3 + 35*d^4*x^4))/(d^5*(c + d*x)^7)

fricas [B] time = 0.44, size = 247, normalized size = 2.78

$$\frac{35b^4d^4x^4 + b^4c^4 + 3ab^3c^3d + 6a^2b^2c^2d^2 + 10a^3bcd^3 + 15a^4d^4 + 35(b^4cd^3 + 3ab^3d^4)x^3 + 21(b^4c^2d^2 + 3ab^3cd^3)x^2 + 21(b^4c^3d^2 + 3ab^3cd^3)x + 21(b^4c^4 + 3ab^3cd^3)}{105(d^{12}x^7 + 7cd^{11}x^6 + 21c^2d^{10}x^5 + 35c^3d^9x^4 + 35c^4d^8x^3 + 21c^5d^7x^2 + 7c^6d^6x + c^7d^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^8,x, algorithm="fricas")

[Out] -1/105*(35*b^4*d^4*x^4 + b^4*c^4 + 3*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 + 10*a^3*b*c*d^3 + 15*a^4*d^4 + 35*(b^4*c*d^3 + 3*a*b^3*d^4)*x^3 + 21*(b^4*c^2*d^2 + 3*a*b^3*c*d^3 + 6*a^2*b^2*d^4)*x^2 + 7*(b^4*c^3*d + 3*a*b^3*c^2*d^2 + 6*a^2*b^2*c*d^3 + 10*a^3*b*d^4)*x)/(d^12*x^7 + 7*c*d^11*x^6 + 21*c^2*d^10*x^5 + 35*c^3*d^9*x^4 + 35*c^4*d^8*x^3 + 21*c^5*d^7*x^2 + 7*c^6*d^6*x + c^7*d^5)

giac [B] time = 1.29, size = 184, normalized size = 2.07

$$\frac{35b^4d^4x^4 + 35b^4cd^3x^3 + 105ab^3d^4x^3 + 21b^4c^2d^2x^2 + 63ab^3cd^3x^2 + 126a^2b^2d^4x^2 + 7b^4c^3dx + 21ab^3c^2d^2x + 21(b^4c^4 + 3ab^3cd^3)}{105(dx+c)^7d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^8,x, algorithm="giac")

[Out]
$$-1/105*(35*b^4*d^4*x^4 + 35*b^4*c*d^3*x^3 + 105*a*b^3*d^4*x^3 + 21*b^4*c^2*d^2*x^2 + 63*a*b^3*c*d^3*x^2 + 126*a^2*b^2*d^4*x^2 + 7*b^4*c^3*d*x + 21*a*b^3*c^2*d^2*x + 42*a^2*b^2*c*d^3*x + 70*a^3*b*d^4*x + b^4*c^4 + 3*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 + 10*a^3*b*c*d^3 + 15*a^4*d^4)/((d*x + c)^7*d^5)$$

maple [B] time = 0.01, size = 186, normalized size = 2.09

$$\frac{b^4}{3(dx+c)^3 d^5} - \frac{(ad-bc)b^3}{(dx+c)^4 d^5} - \frac{6(a^2 d^2 - 2abcd + b^2 c^2)b^2}{5(dx+c)^5 d^5} - \frac{2(a^3 d^3 - 3a^2 bc d^2 + 3a b^2 c^2 d - b^3 c^3)b}{3(dx+c)^6 d^5} - \frac{a^4 d^4 - 4a^3 bc d^3}{(dx+c)^7 d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4/(d*x+c)^8,x)

[Out]
$$-1/7*(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)/d^5/(d*x+c)^7-1/3*b^4/d^5/(d*x+c)^3-b^3*(a*d-b*c)/d^5/(d*x+c)^4-2/3*b*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/d^5/(d*x+c)^6-6/5*b^2*(a^2*d^2-2*a*b*c*d+b^2*c^2)/d^5/(d*x+c)^5$$

maxima [B] time = 1.52, size = 247, normalized size = 2.78

$$\frac{35 b^4 d^4 x^4 + b^4 c^4 + 3 a b^3 c^3 d + 6 a^2 b^2 c^2 d^2 + 10 a^3 b c d^3 + 15 a^4 d^4 + 35 (b^4 c d^3 + 3 a b^3 d^4) x^3 + 21 (b^4 c^2 d^2 + 3 a b^3 c d^3) x^2 + 7 (b^4 c^3 d + 3 a b^3 c^2 d^2 + 6 a^2 b^2 c^2 d^3 + 10 a^3 b c d^4) x + 7 c^4 d^4}{105 (d^{12} x^7 + 7 c d^{11} x^6 + 21 c^2 d^{10} x^5 + 35 c^3 d^9 x^4 + 35 c^4 d^8 x^3 + 21 c^5 d^7 x^2 + 7 c^6 d^6 x + c^7 d^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^8,x, algorithm="maxima")

[Out]
$$-1/105*(35*b^4*d^4*x^4 + b^4*c^4 + 3*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 + 10*a^3*b*c*d^3 + 15*a^4*d^4 + 35*(b^4*c*d^3 + 3*a*b^3*d^4)*x^3 + 21*(b^4*c^2*d^2 + 3*a*b^3*c*d^3 + 6*a^2*b^2*d^4)*x^2 + 7*(b^4*c^3*d + 3*a*b^3*c^2*d^2 + 6*a^2*b^2*c*d^3 + 10*a^3*b*d^4)*x)/(d^12*x^7 + 7*c*d^11*x^6 + 21*c^2*d^10*x^5 + 35*c^3*d^9*x^4 + 35*c^4*d^8*x^3 + 21*c^5*d^7*x^2 + 7*c^6*d^6*x + c^7*d^5)$$

mupad [B] time = 0.11, size = 237, normalized size = 2.66

$$\frac{15 a^4 d^4 + 10 a^3 b c d^3 + 6 a^2 b^2 c^2 d^2 + 3 a b^3 c^3 d + b^4 c^4}{105 d^5} + \frac{b^4 x^4}{3 d} + \frac{b^3 x^3 (3 a d + b c)}{3 d^2} + \frac{b x (10 a^3 d^3 + 6 a^2 b c d^2 + 3 a b^2 c^2 d + b^3 c^3)}{15 d^4} + \frac{b^2 x^2 (6 a^2 d^2 + 3 a b c d^3)}{5 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^4/(c + d*x)^8,x)`

[Out] $-\left(\frac{15a^4d^4 + b^4c^4 + 6a^2b^2c^2d^2 + 3ab^3c^3d + 10a^3b^2cd^3}{105d^5} + \frac{b^4x^4}{3d} + \frac{b^3x^3(3ad + bc)}{3d^2} + \frac{bx(10a^3d^3 + b^3c^3 + 3ab^2c^2d + 6a^2b^2cd^2)}{15d^4} + \frac{b^2x^2(6a^2d^2 + b^2c^2 + 3ab^2cd)}{5d^3}\right) / (c^7 + d^7x^7 + 7c^6d^6x^6 + 21c^5d^5x^5 + 35c^4d^4x^4 + 35c^3d^3x^3 + 21c^2d^2x^2 + 7c^6dx)$

sympy [B] time = 9.64, size = 267, normalized size = 3.00

$$\frac{-15a^4d^4 - 10a^3bcd^3 - 6a^2b^2c^2d^2 - 3ab^3c^3d - b^4c^4 - 35b^4d^4x^4 + x^3(-105ab^3d^4 - 35b^4cd^3) + x^2(-126a^2b^2d^4 - 105a^3b^2cd^3) + x(-70a^3b^2d^4 - 42a^2b^2c^2d^2 - 21ab^3c^3d) + (-126a^2b^2d^4 - 63ab^3c^3d - 21b^4c^4d^2)}{105c^7d^5 + 735c^6d^6x + 2205c^5d^7x^2 + 3675c^4d^8x^3 + 3675c^3d^9x^4 + 2205c^2d^{10}x^5 + 735cd^{11}x^6 + 105d^{12}x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**4/(d*x+c)**8,x)`

[Out] $(-15a^4d^4 - 10a^3b^2cd^3 - 6a^2b^2c^2d^2 - 3ab^3c^3d - b^4c^4 - 35b^4d^4x^4 + x^3(-105ab^3d^4 - 35b^4cd^3) + x^2(-126a^2b^2d^4 - 63ab^3c^3d - 21b^4c^4d^2) + x(-70a^3b^2d^4 - 42a^2b^2c^2d^2 - 21ab^3c^3d) - 7b^4c^4d^2) / (105c^7d^5 + 735c^6d^6x + 2205c^5d^7x^2 + 3675c^4d^8x^3 + 3675c^3d^9x^4 + 2205c^2d^{10}x^5 + 735cd^{11}x^6 + 105d^{12}x^7)$

$$3.1368 \quad \int \frac{(a+bx)^3}{(c+dx)^8} dx$$

Optimal. Leaf size=92

$$\frac{3b^2(bc-ad)}{5d^4(c+dx)^5} - \frac{b(bc-ad)^2}{2d^4(c+dx)^6} + \frac{(bc-ad)^3}{7d^4(c+dx)^7} - \frac{b^3}{4d^4(c+dx)^4}$$

[Out] $1/7*(-a*d+b*c)^3/d^4/(d*x+c)^7-1/2*b*(-a*d+b*c)^2/d^4/(d*x+c)^6+3/5*b^2*(-a*d+b*c)/d^4/(d*x+c)^5-1/4*b^3/d^4/(d*x+c)^4$

Rubi [A] time = 0.06, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{3b^2(bc-ad)}{5d^4(c+dx)^5} - \frac{b(bc-ad)^2}{2d^4(c+dx)^6} + \frac{(bc-ad)^3}{7d^4(c+dx)^7} - \frac{b^3}{4d^4(c+dx)^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/(c + d*x)^8, x]

[Out] $(b*c - a*d)^3/(7*d^4*(c + d*x)^7) - (b*(b*c - a*d)^2)/(2*d^4*(c + d*x)^6) + (3*b^2*(b*c - a*d))/(5*d^4*(c + d*x)^5) - b^3/(4*d^4*(c + d*x)^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{(c+dx)^8} dx &= \int \left(\frac{(-bc+ad)^3}{d^3(c+dx)^8} + \frac{3b(bc-ad)^2}{d^3(c+dx)^7} - \frac{3b^2(bc-ad)}{d^3(c+dx)^6} + \frac{b^3}{d^3(c+dx)^5} \right) dx \\ &= \frac{(bc-ad)^3}{7d^4(c+dx)^7} - \frac{b(bc-ad)^2}{2d^4(c+dx)^6} + \frac{3b^2(bc-ad)}{5d^4(c+dx)^5} - \frac{b^3}{4d^4(c+dx)^4} \end{aligned}$$

Mathematica [A] time = 0.03, size = 94, normalized size = 1.02

$$\frac{20a^3d^3 + 10a^2bd^2(c + 7dx) + 4ab^2d(c^2 + 7cdx + 21d^2x^2) + b^3(c^3 + 7c^2dx + 21cd^2x^2 + 35d^3x^3)}{140d^4(c + dx)^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/(c + d*x)^8,x]

[Out]
$$-1/140*(20*a^3*d^3 + 10*a^2*b*d^2*(c + 7*d*x) + 4*a*b^2*d*(c^2 + 7*c*d*x + 21*d^2*x^2) + b^3*(c^3 + 7*c^2*d*x + 21*c*d^2*x^2 + 35*d^3*x^3))/(d^4*(c + d*x)^7)$$

fricas [B] time = 0.42, size = 182, normalized size = 1.98

$$\frac{35 b^3 d^3 x^3 + b^3 c^3 + 4 a b^2 c^2 d + 10 a^2 b c d^2 + 20 a^3 d^3 + 21 (b^3 c d^2 + 4 a b^2 d^3) x^2 + 7 (b^3 c^2 d + 4 a b^2 c d^2 + 10 a^2 b d^3) x}{140 (d^{11} x^7 + 7 c d^{10} x^6 + 21 c^2 d^9 x^5 + 35 c^3 d^8 x^4 + 35 c^4 d^7 x^3 + 21 c^5 d^6 x^2 + 7 c^6 d^5 x + c^7 d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^8,x, algorithm="fricas")

[Out]
$$-1/140*(35*b^3*d^3*x^3 + b^3*c^3 + 4*a*b^2*c^2*d + 10*a^2*b*c*d^2 + 20*a^3*d^3 + 21*(b^3*c*d^2 + 4*a*b^2*d^3)*x^2 + 7*(b^3*c^2*d + 4*a*b^2*c*d^2 + 10*a^2*b*d^3)*x)/(d^{11}*x^7 + 7*c*d^{10}*x^6 + 21*c^2*d^9*x^5 + 35*c^3*d^8*x^4 + 35*c^4*d^7*x^3 + 21*c^5*d^6*x^2 + 7*c^6*d^5*x + c^7*d^4)$$

giac [A] time = 1.24, size = 114, normalized size = 1.24

$$\frac{35 b^3 d^3 x^3 + 21 b^3 c d^2 x^2 + 84 a b^2 d^3 x^2 + 7 b^3 c^2 d x + 28 a b^2 c d^2 x + 70 a^2 b d^3 x + b^3 c^3 + 4 a b^2 c^2 d + 10 a^2 b c d^2 + 20 a^3 d^3}{140 (d x + c)^7 d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^8,x, algorithm="giac")

[Out]
$$-1/140*(35*b^3*d^3*x^3 + 21*b^3*c*d^2*x^2 + 84*a*b^2*d^3*x^2 + 7*b^3*c^2*d*x + 28*a*b^2*c*d^2*x + 70*a^2*b*d^3*x + b^3*c^3 + 4*a*b^2*c^2*d + 10*a^2*b*c*d^2 + 20*a^3*d^3)/((d*x + c)^7*d^4)$$

maple [A] time = 0.01, size = 122, normalized size = 1.33

$$-\frac{b^3}{4(dx+c)^4 d^4} - \frac{3(ad-bc)b^2}{5(dx+c)^5 d^4} - \frac{(a^2 d^2 - 2abcd + b^2 c^2)b}{2(dx+c)^6 d^4} - \frac{a^3 d^3 - 3a^2 b c d^2 + 3a b^2 c^2 d - b^3 c^3}{7(dx+c)^7 d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/(d*x+c)^8,x)

[Out]
$$-1/7*(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/d^4/(d*x+c)^7-1/2*b*(a^2*d^2-2*a*b*c*d+b^2*c^2)/d^4/(d*x+c)^6-1/4*b^3/d^4/(d*x+c)^4-3/5*b^2*(a*d-b*c)/d^4/(d*x+c)^5$$

maxima [B] time = 1.47, size = 182, normalized size = 1.98

$$\frac{35 b^3 d^3 x^3 + b^3 c^3 + 4 a b^2 c^2 d + 10 a^2 b c d^2 + 20 a^3 d^3 + 21 (b^3 c d^2 + 4 a b^2 d^3) x^2 + 7 (b^3 c^2 d + 4 a b^2 c d^2 + 10 a^2 b d^3) x}{140 (d^{11} x^7 + 7 c d^{10} x^6 + 21 c^2 d^9 x^5 + 35 c^3 d^8 x^4 + 35 c^4 d^7 x^3 + 21 c^5 d^6 x^2 + 7 c^6 d^5 x + c^7 d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^8,x, algorithm="maxima")

[Out] -1/140*(35*b^3*d^3*x^3 + b^3*c^3 + 4*a*b^2*c^2*d + 10*a^2*b*c*d^2 + 20*a^3*d^3 + 21*(b^3*c*d^2 + 4*a*b^2*d^3)*x^2 + 7*(b^3*c^2*d + 4*a*b^2*c*d^2 + 10*a^2*b*d^3)*x)/(d^11*x^7 + 7*c*d^10*x^6 + 21*c^2*d^9*x^5 + 35*c^3*d^8*x^4 + 35*c^4*d^7*x^3 + 21*c^5*d^6*x^2 + 7*c^6*d^5*x + c^7*d^4)

mupad [B] time = 0.10, size = 176, normalized size = 1.91

$$-\frac{\frac{20 a^3 d^3 + 10 a^2 b c d^2 + 4 a b^2 c^2 d + b^3 c^3}{140 d^4} + \frac{b^3 x^3}{4 d} + \frac{b x (10 a^2 d^2 + 4 a b c d + b^2 c^2)}{20 d^3} + \frac{3 b^2 x^2 (4 a d + b c)}{20 d^2}}{c^7 + 7 c^6 d x + 21 c^5 d^2 x^2 + 35 c^4 d^3 x^3 + 35 c^3 d^4 x^4 + 21 c^2 d^5 x^5 + 7 c d^6 x^6 + d^7 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3/(c + d*x)^8,x)

[Out] -((20*a^3*d^3 + b^3*c^3 + 4*a*b^2*c^2*d + 10*a^2*b*c*d^2)/(140*d^4) + (b^3*x^3)/(4*d) + (b*x*(10*a^2*d^2 + b^2*c^2 + 4*a*b*c*d))/(20*d^3) + (3*b^2*x^2*(4*a*d + b*c))/(20*d^2))/(c^7 + d^7*x^7 + 7*c*d^6*x^6 + 21*c^5*d^2*x^2 + 35*c^4*d^3*x^3 + 35*c^3*d^4*x^4 + 21*c^2*d^5*x^5 + 7*c^6*d*x)

sympy [B] time = 3.10, size = 196, normalized size = 2.13

$$\frac{-20 a^3 d^3 - 10 a^2 b c d^2 - 4 a b^2 c^2 d - b^3 c^3 - 35 b^3 d^3 x^3 + x^2 (-84 a b^2 d^3 - 21 b^3 c d^2) + x (-70 a^2 b d^3 - 28 a b^2 c d^2 - 7 b^3 c^2 d)}{140 c^7 d^4 + 980 c^6 d^5 x + 2940 c^5 d^6 x^2 + 4900 c^4 d^7 x^3 + 4900 c^3 d^8 x^4 + 2940 c^2 d^9 x^5 + 980 c d^{10} x^6 + 140 d^{11} x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3/(d*x+c)**8,x)

[Out] (-20*a**3*d**3 - 10*a**2*b*c*d**2 - 4*a*b**2*c**2*d - b**3*c**3 - 35*b**3*d**3*x**3 + x**2*(-84*a*b**2*d**3 - 21*b**3*c*d**2) + x*(-70*a**2*b*d**3 - 28*a*b**2*c*d**2 - 7*b**3*c**2*d))/(140*c**7*d**4 + 980*c**6*d**5*x + 2940*c**5*d**6*x**2 + 4900*c**4*d**7*x**3 + 4900*c**3*d**8*x**4 + 2940*c**2*d**9*x**5 + 980*c*d**10*x**6 + 140*d**11*x**7)

$$3.1369 \quad \int \frac{(a+bx)^2}{(c+dx)^8} dx$$

Optimal. Leaf size=65

$$\frac{b(bc-ad)}{3d^3(c+dx)^6} - \frac{(bc-ad)^2}{7d^3(c+dx)^7} - \frac{b^2}{5d^3(c+dx)^5}$$

[Out] $-1/7*(-a*d+b*c)^2/d^3/(d*x+c)^7+1/3*b*(-a*d+b*c)/d^3/(d*x+c)^6-1/5*b^2/d^3/(d*x+c)^5$

Rubi [A] time = 0.04, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{b(bc-ad)}{3d^3(c+dx)^6} - \frac{(bc-ad)^2}{7d^3(c+dx)^7} - \frac{b^2}{5d^3(c+dx)^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(c + d*x)^8, x]

[Out] $-(b*c - a*d)^2/(7*d^3*(c + d*x)^7) + (b*(b*c - a*d))/(3*d^3*(c + d*x)^6) - b^2/(5*d^3*(c + d*x)^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(c+dx)^8} dx &= \int \left(\frac{(-bc+ad)^2}{d^2(c+dx)^8} - \frac{2b(bc-ad)}{d^2(c+dx)^7} + \frac{b^2}{d^2(c+dx)^6} \right) dx \\ &= -\frac{(bc-ad)^2}{7d^3(c+dx)^7} + \frac{b(bc-ad)}{3d^3(c+dx)^6} - \frac{b^2}{5d^3(c+dx)^5} \end{aligned}$$

Mathematica [A] time = 0.02, size = 55, normalized size = 0.85

$$-\frac{15a^2d^2 + 5abd(c + 7dx) + b^2(c^2 + 7cdx + 21d^2x^2)}{105d^3(c + dx)^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(c + d*x)^8,x]

[Out]
$$-1/105*(15*a^2*d^2 + 5*a*b*d*(c + 7*d*x) + b^2*(c^2 + 7*c*d*x + 21*d^2*x^2)) / (d^3*(c + d*x)^7)$$

fricas [B] time = 0.43, size = 131, normalized size = 2.02

$$\frac{21 b^2 d^2 x^2 + b^2 c^2 + 5 a b c d + 15 a^2 d^2 + 7 (b^2 c d + 5 a b d^2) x}{105 (d^{10} x^7 + 7 c d^9 x^6 + 21 c^2 d^8 x^5 + 35 c^3 d^7 x^4 + 35 c^4 d^6 x^3 + 21 c^5 d^5 x^2 + 7 c^6 d^4 x + c^7 d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^8,x, algorithm="fricas")

[Out]
$$-1/105*(21*b^2*d^2*x^2 + b^2*c^2 + 5*a*b*c*d + 15*a^2*d^2 + 7*(b^2*c*d + 5*a*b*d^2)*x) / (d^{10}*x^7 + 7*c*d^9*x^6 + 21*c^2*d^8*x^5 + 35*c^3*d^7*x^4 + 35*c^4*d^6*x^3 + 21*c^5*d^5*x^2 + 7*c^6*d^4*x + c^7*d^3)$$

giac [A] time = 1.22, size = 61, normalized size = 0.94

$$\frac{21 b^2 d^2 x^2 + 7 b^2 c d x + 35 a b d^2 x + b^2 c^2 + 5 a b c d + 15 a^2 d^2}{105 (d x + c)^7 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^8,x, algorithm="giac")

[Out]
$$-1/105*(21*b^2*d^2*x^2 + 7*b^2*c*d*x + 35*a*b*d^2*x + b^2*c^2 + 5*a*b*c*d + 15*a^2*d^2) / ((d*x + c)^7*d^3)$$

maple [A] time = 0.00, size = 71, normalized size = 1.09

$$\frac{b^2}{5 (d x + c)^5 d^3} - \frac{(a d - b c) b}{3 (d x + c)^6 d^3} - \frac{a^2 d^2 - 2 a b c d + b^2 c^2}{7 (d x + c)^7 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(d*x+c)^8,x)

[Out]
$$-1/7*(a^2*d^2-2*a*b*c*d+b^2*c^2)/d^3/(d*x+c)^7-1/5*b^2/d^3/(d*x+c)^5-1/3*b*(a*d-b*c)/d^3/(d*x+c)^6$$

maxima [B] time = 1.46, size = 131, normalized size = 2.02

$$\frac{21 b^2 d^2 x^2 + b^2 c^2 + 5 a b c d + 15 a^2 d^2 + 7 (b^2 c d + 5 a b d^2) x}{105 (d^{10} x^7 + 7 c d^9 x^6 + 21 c^2 d^8 x^5 + 35 c^3 d^7 x^4 + 35 c^4 d^6 x^3 + 21 c^5 d^5 x^2 + 7 c^6 d^4 x + c^7 d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^8,x, algorithm="maxima")

[Out]
$$-1/105*(21*b^2*d^2*x^2 + b^2*c^2 + 5*a*b*c*d + 15*a^2*d^2 + 7*(b^2*c*d + 5*a*b*d^2)*x)/(d^{10}*x^7 + 7*c*d^9*x^6 + 21*c^2*d^8*x^5 + 35*c^3*d^7*x^4 + 35*c^4*d^6*x^3 + 21*c^5*d^5*x^2 + 7*c^6*d^4*x + c^7*d^3)$$

mupad [B] time = 0.09, size = 129, normalized size = 1.98

$$\frac{\frac{15a^2d^2+5abcd+b^2c^2}{105d^3} + \frac{b^2x^2}{5d} + \frac{bx(5ad+bc)}{15d^2}}{c^7 + 7c^6dx + 21c^5d^2x^2 + 35c^4d^3x^3 + 35c^3d^4x^4 + 21c^2d^5x^5 + 7cd^6x^6 + d^7x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(c + d*x)^8,x)

[Out]
$$-((15*a^2*d^2 + b^2*c^2 + 5*a*b*c*d)/(105*d^3) + (b^2*x^2)/(5*d) + (b*x*(5*a*d + b*c))/(15*d^2))/(c^7 + d^7*x^7 + 7*c*d^6*x^6 + 21*c^5*d^2*x^2 + 35*c^4*d^3*x^3 + 35*c^3*d^4*x^4 + 21*c^2*d^5*x^5 + 7*c^6*d*x)$$

sympy [B] time = 1.39, size = 139, normalized size = 2.14

$$\frac{-15a^2d^2 - 5abcd - b^2c^2 - 21b^2d^2x^2 + x(-35abd^2 - 7b^2cd)}{105c^7d^3 + 735c^6d^4x + 2205c^5d^5x^2 + 3675c^4d^6x^3 + 3675c^3d^7x^4 + 2205c^2d^8x^5 + 735cd^9x^6 + 105d^{10}x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(d*x+c)**8,x)

[Out]
$$(-15*a**2*d**2 - 5*a*b*c*d - b**2*c**2 - 21*b**2*d**2*x**2 + x*(-35*a*b*d**2 - 7*b**2*c*d))/(105*c**7*d**3 + 735*c**6*d**4*x + 2205*c**5*d**5*x**2 + 3675*c**4*d**6*x**3 + 3675*c**3*d**7*x**4 + 2205*c**2*d**8*x**5 + 735*c*d**9*x**6 + 105*d**10*x**7)$$

$$3.1370 \quad \int \frac{a+bx}{(c+dx)^8} dx$$

Optimal. Leaf size=38

$$\frac{bc-ad}{7d^2(c+dx)^7} - \frac{b}{6d^2(c+dx)^6}$$

[Out] $1/7*(-a*d+b*c)/d^2/(d*x+c)^7-1/6*b/d^2/(d*x+c)^6$

Rubi [A] time = 0.02, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{bc-ad}{7d^2(c+dx)^7} - \frac{b}{6d^2(c+dx)^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(c + d*x)^8, x]

[Out] (b*c - a*d)/(7*d^2*(c + d*x)^7) - b/(6*d^2*(c + d*x)^6)

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{(c+dx)^8} dx &= \int \left(\frac{-bc+ad}{d(c+dx)^8} + \frac{b}{d(c+dx)^7} \right) dx \\ &= \frac{bc-ad}{7d^2(c+dx)^7} - \frac{b}{6d^2(c+dx)^6} \end{aligned}$$

Mathematica [A] time = 0.01, size = 27, normalized size = 0.71

$$-\frac{6ad+b(c+7dx)}{42d^2(c+dx)^7}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(c + d*x)^8, x]

[Out] $-1/42*(6*a*d + b*(c + 7*d*x))/(d^2*(c + d*x)^7)$

fricas [B] time = 0.43, size = 94, normalized size = 2.47

$$\frac{7 b d x + b c + 6 a d}{42 \left(d^9 x^7 + 7 c d^8 x^6 + 21 c^2 d^7 x^5 + 35 c^3 d^6 x^4 + 35 c^4 d^5 x^3 + 21 c^5 d^4 x^2 + 7 c^6 d^3 x + c^7 d^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)^8,x, algorithm="fricas")`

[Out] $-1/42*(7*b*d*x + b*c + 6*a*d)/(d^9*x^7 + 7*c*d^8*x^6 + 21*c^2*d^7*x^5 + 35*c^3*d^6*x^4 + 35*c^4*d^5*x^3 + 21*c^5*d^4*x^2 + 7*c^6*d^3*x + c^7*d^2)$

giac [A] time = 1.31, size = 25, normalized size = 0.66

$$\frac{7 b d x + b c + 6 a d}{42 (d x + c)^7 d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)^8,x, algorithm="giac")`

[Out] $-1/42*(7*b*d*x + b*c + 6*a*d)/((d*x + c)^7*d^2)$

maple [A] time = 0.01, size = 35, normalized size = 0.92

$$-\frac{b}{6 (d x + c)^6 d^2} - \frac{a d - b c}{7 (d x + c)^7 d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/(d*x+c)^8,x)`

[Out] $-1/7*(a*d-b*c)/d^2/(d*x+c)^7-1/6*b/d^2/(d*x+c)^6$

maxima [B] time = 1.38, size = 94, normalized size = 2.47

$$\frac{7 b d x + b c + 6 a d}{42 \left(d^9 x^7 + 7 c d^8 x^6 + 21 c^2 d^7 x^5 + 35 c^3 d^6 x^4 + 35 c^4 d^5 x^3 + 21 c^5 d^4 x^2 + 7 c^6 d^3 x + c^7 d^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)^8,x, algorithm="maxima")`

[Out] $-1/42*(7*b*d*x + b*c + 6*a*d)/(d^9*x^7 + 7*c*d^8*x^6 + 21*c^2*d^7*x^5 + 35*c^3*d^6*x^4 + 35*c^4*d^5*x^3 + 21*c^5*d^4*x^2 + 7*c^6*d^3*x + c^7*d^2)$

mupad [B] time = 0.23, size = 96, normalized size = 2.53

$$\frac{\frac{6ad+bc}{42d^2} + \frac{bx}{6d}}{c^7 + 7c^6dx + 21c^5d^2x^2 + 35c^4d^3x^3 + 35c^3d^4x^4 + 21c^2d^5x^5 + 7cd^6x^6 + d^7x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(c + d*x)^8, x)

[Out] -((6*a*d + b*c)/(42*d^2) + (b*x)/(6*d))/(c^7 + d^7*x^7 + 7*c*d^6*x^6 + 21*c^5*d^2*x^2 + 35*c^4*d^3*x^3 + 35*c^3*d^4*x^4 + 21*c^2*d^5*x^5 + 7*c^6*d*x)

sympy [B] time = 0.73, size = 100, normalized size = 2.63

$$\frac{-6ad - bc - 7bdx}{42c^7d^2 + 294c^6d^3x + 882c^5d^4x^2 + 1470c^4d^5x^3 + 1470c^3d^6x^4 + 882c^2d^7x^5 + 294cd^8x^6 + 42d^9x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)**8, x)

[Out] (-6*a*d - b*c - 7*b*d*x)/(42*c**7*d**2 + 294*c**6*d**3*x + 882*c**5*d**4*x**2 + 1470*c**4*d**5*x**3 + 1470*c**3*d**6*x**4 + 882*c**2*d**7*x**5 + 294*c*d**8*x**6 + 42*d**9*x**7)

$$3.1371 \quad \int \frac{1}{(c+dx)^8} dx$$

Optimal. Leaf size=14

$$-\frac{1}{7d(c+dx)^7}$$

[Out] -1/7/d/(d*x+c)^7

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.143, Rules used = {32}

$$-\frac{1}{7d(c+dx)^7}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(-8), x]

[Out] -1/(7*d*(c + d*x)^7)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(c+dx)^8} dx = -\frac{1}{7d(c+dx)^7}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\frac{1}{7d(c+dx)^7}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(-8), x]

[Out] -1/7*1/(d*(c + d*x)^7)

fricas [B] time = 0.43, size = 79, normalized size = 5.64

$$-\frac{1}{7(d^8x^7 + 7cd^7x^6 + 21c^2d^6x^5 + 35c^3d^5x^4 + 35c^4d^4x^3 + 21c^5d^3x^2 + 7c^6d^2x + c^7d)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^8,x, algorithm="fricas")

[Out] $-1/7/(d^8*x^7 + 7*c*d^7*x^6 + 21*c^2*d^6*x^5 + 35*c^3*d^5*x^4 + 35*c^4*d^4*x^3 + 21*c^5*d^3*x^2 + 7*c^6*d^2*x + c^7*d)$

giac [A] time = 1.26, size = 12, normalized size = 0.86

$$-\frac{1}{7(dx+c)^7 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^8,x, algorithm="giac")

[Out] $-1/7/((d*x + c)^7*d)$

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$-\frac{1}{7(dx+c)^7 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^8,x)

[Out] $-1/7/d/(d*x+c)^7$

maxima [A] time = 1.36, size = 12, normalized size = 0.86

$$-\frac{1}{7(dx+c)^7 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^8,x, algorithm="maxima")

[Out] $-1/7/((d*x + c)^7*d)$

mupad [B] time = 0.22, size = 81, normalized size = 5.79

$$-\frac{1}{7c^7 d + 49c^6 d^2 x + 147c^5 d^3 x^2 + 245c^4 d^4 x^3 + 245c^3 d^5 x^4 + 147c^2 d^6 x^5 + 49c d^7 x^6 + 7d^8 x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c + d*x)^8,x)

[Out] $-1/(7*c^7*d + 7*d^8*x^7 + 49*c^6*d^2*x + 49*c*d^7*x^6 + 147*c^5*d^3*x^2 + 245*c^4*d^4*x^3 + 245*c^3*d^5*x^4 + 147*c^2*d^6*x^5)$

sympy [B] time = 0.46, size = 85, normalized size = 6.07

$$\frac{1}{7c^7d + 49c^6d^2x + 147c^5d^3x^2 + 245c^4d^4x^3 + 245c^3d^5x^4 + 147c^2d^6x^5 + 49cd^7x^6 + 7d^8x^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)**8,x)

[Out] $-1/(7*c**7*d + 49*c**6*d**2*x + 147*c**5*d**3*x**2 + 245*c**4*d**4*x**3 + 245*c**3*d**5*x**4 + 147*c**2*d**6*x**5 + 49*c*d**7*x**6 + 7*d**8*x**7)$

$$3.1372 \quad \int \frac{1}{(a+bx)(c+dx)^8} dx$$

Optimal. Leaf size=202

$$\frac{b^7 \log(a+bx)}{(bc-ad)^8} - \frac{b^7 \log(c+dx)}{(bc-ad)^8} + \frac{b^6}{(c+dx)(bc-ad)^7} + \frac{b^5}{2(c+dx)^2(bc-ad)^6} + \frac{b^4}{3(c+dx)^3(bc-ad)^5} + \frac{b^3}{4(c+dx)^4(bc-ad)^4}$$

[Out] $1/7/(-a*d+b*c)/(d*x+c)^7+1/6*b/(-a*d+b*c)^2/(d*x+c)^6+1/5*b^2/(-a*d+b*c)^3/(d*x+c)^5+1/4*b^3/(-a*d+b*c)^4/(d*x+c)^4+1/3*b^4/(-a*d+b*c)^5/(d*x+c)^3+1/2*b^5/(-a*d+b*c)^6/(d*x+c)^2+b^6/(-a*d+b*c)^7/(d*x+c)+b^7*\ln(b*x+a)/(-a*d+b*c)^8-b^7*\ln(d*x+c)/(-a*d+b*c)^8$

Rubi [A] time = 0.17, antiderivative size = 202, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$\frac{b^6}{(c+dx)(bc-ad)^7} + \frac{b^5}{2(c+dx)^2(bc-ad)^6} + \frac{b^4}{3(c+dx)^3(bc-ad)^5} + \frac{b^3}{4(c+dx)^4(bc-ad)^4} + \frac{b^2}{5(c+dx)^5(bc-ad)^3} + \frac{b^7 \ln(b*x+a)}{(bc-ad)^8} - \frac{b^7 \ln(d*x+c)}{(bc-ad)^8}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)*(c + d*x)^8), x]

[Out] $1/(7*(b*c - a*d)*(c + d*x)^7) + b/(6*(b*c - a*d)^2*(c + d*x)^6) + b^2/(5*(b*c - a*d)^3*(c + d*x)^5) + b^3/(4*(b*c - a*d)^4*(c + d*x)^4) + b^4/(3*(b*c - a*d)^5*(c + d*x)^3) + b^5/(2*(b*c - a*d)^6*(c + d*x)^2) + b^6/((b*c - a*d)^7*(c + d*x)) + (b^7*\text{Log}[a + b*x])/(b*c - a*d)^8 - (b^7*\text{Log}[c + d*x])/(b*c - a*d)^8$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)(c+dx)^8} dx &= \int \left(\frac{b^8}{(bc-ad)^8(a+bx)} - \frac{d}{(bc-ad)(c+dx)^8} - \frac{bd}{(bc-ad)^2(c+dx)^7} - \frac{b^2d}{(bc-ad)^3(c+dx)^6} \right. \\ &\quad \left. - \frac{b^3d}{(bc-ad)^4(c+dx)^5} - \frac{b^4d}{(bc-ad)^5(c+dx)^4} - \frac{b^5d}{(bc-ad)^6(c+dx)^3} - \frac{b^6d}{(bc-ad)^7(c+dx)^2} - \frac{b^7d}{(bc-ad)^8(c+dx)} \right) dx \\ &= \frac{1}{7(bc-ad)(c+dx)^7} + \frac{b}{6(bc-ad)^2(c+dx)^6} + \frac{b^2}{5(bc-ad)^3(c+dx)^5} + \frac{b^3}{4(bc-ad)^4(c+dx)^4} + \frac{b^4}{3(bc-ad)^5(c+dx)^3} + \frac{b^5}{2(bc-ad)^6(c+dx)^2} + \frac{b^6}{(bc-ad)^7(c+dx)} - \frac{b^7 \ln(c+dx)}{(bc-ad)^8} + \frac{b^7 \ln(a+bx)}{(bc-ad)^8} \end{aligned}$$

Mathematica [A] time = 0.10, size = 196, normalized size = 0.97

$$\frac{420b^7(c+dx)^7 \log(a+bx) + 420b^6(c+dx)^6(bc-ad) + 210b^5(c+dx)^5(bc-ad)^2 + 140b^4(c+dx)^4(bc-ad)^3 + 420(c+dx)^3(bc-ad)^4}{420(c+dx)^8}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*(c + d*x)^8), x]

[Out] $(60*(b*c - a*d)^7 + 70*b*(b*c - a*d)^6*(c + d*x) + 84*b^2*(b*c - a*d)^5*(c + d*x)^2 + 105*b^3*(b*c - a*d)^4*(c + d*x)^3 + 140*b^4*(b*c - a*d)^3*(c + d*x)^4 + 210*b^5*(b*c - a*d)^2*(c + d*x)^5 + 420*b^6*(b*c - a*d)*(c + d*x)^6 + 420*b^7*(c + d*x)^7*\text{Log}[a + b*x] - 420*b^7*(c + d*x)^7*\text{Log}[c + d*x]) / (420*(b*c - a*d)^8*(c + d*x)^7)$

fricas [B] time = 0.52, size = 1589, normalized size = 7.87

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^8,x, algorithm="fricas")

[Out] $\frac{1}{420}*(1089*b^7*c^7 - 2940*a*b^6*c^6*d + 4410*a^2*b^5*c^5*d^2 - 4900*a^3*b^4*c^4*d^3 + 3675*a^4*b^3*c^3*d^4 - 1764*a^5*b^2*c^2*d^5 + 490*a^6*b*c*d^6 - 60*a^7*d^7 + 420*(b^7*c*d^6 - a*b^6*d^7)*x^6 + 210*(13*b^7*c^2*d^5 - 14*a*b^6*c*d^6 + a^2*b^5*d^7)*x^5 + 70*(107*b^7*c^3*d^4 - 126*a*b^6*c^2*d^5 + 21*a^2*b^5*c*d^6 - 2*a^3*b^4*d^7)*x^4 + 35*(319*b^7*c^4*d^3 - 420*a*b^6*c^3*d^4 + 126*a^2*b^5*c^2*d^5 - 28*a^3*b^4*c*d^6 + 3*a^4*b^3*d^7)*x^3 + 21*(459*b^7*c^5*d^2 - 700*a*b^6*c^4*d^3 + 350*a^2*b^5*c^3*d^4 - 140*a^3*b^4*c^2*d^5 + 35*a^4*b^3*c*d^6 - 4*a^5*b^2*d^7)*x^2 + 7*(669*b^7*c^6*d - 1260*a*b^6*c^5*d^2 + 1050*a^2*b^5*c^4*d^3 - 700*a^3*b^4*c^3*d^4 + 315*a^4*b^3*c^2*d^5 - 84*a^5*b^2*c*d^6 + 10*a^6*b*d^7)*x + 420*(b^7*d^7*x^7 + 7*b^7*c*d^6*x^6 + 21*b^7*c^2*d^5*x^5 + 35*b^7*c^3*d^4*x^4 + 35*b^7*c^4*d^3*x^3 + 21*b^7*c^5*d^2*x^2 + 7*b^7*c^6*d*x + b^7*c^7)*\text{log}(b*x + a) - 420*(b^7*d^7*x^7 + 7*b^7*c*d^6*x^6 + 21*b^7*c^2*d^5*x^5 + 35*b^7*c^3*d^4*x^4 + 35*b^7*c^4*d^3*x^3 + 21*b^7*c^5*d^2*x^2 + 7*b^7*c^6*d*x + b^7*c^7)*\text{log}(d*x + c)) / (b^8*c^15 - 8*a*b^7*c^14*d + 28*a^2*b^6*c^13*d^2 - 56*a^3*b^5*c^12*d^3 + 70*a^4*b^4*c^11*d^4 - 56*a^5*b^3*c^10*d^5 + 28*a^6*b^2*c^9*d^6 - 8*a^7*b*c^8*d^7 + a^8*c^7*d^8 + (b^8*c^8*d^7 - 8*a*b^7*c^7*d^8 + 28*a^2*b^6*c^6*d^9 - 56*a^3*b^5*c^5*d^10 + 70*a^4*b^4*c^4*d^11 - 56*a^5*b^3*c^3*d^12 + 28*a^6*b^2*c^2*d^13 - 8*a^7*b*c*d^14 + a^8*d^15)*x^7 + 7*(b^8*c^9*d^6 - 8*a*b^7*c^8*d^7 + 28*a^2*b^6*c^7*d^8 - 56*a^3*b^5*c^6*d^9 + 70*a^4*b^4*c^5*d^10 - 56*a^5*b^3*c^4*d^11 + 28*a^6*b^2*c^3*d^12 - 8*a^7*b*c^2*d^13 + a^8*c*d^14)*x^6 + 21*(b^8*c^10*d^5 - 8*a*b^7*c^9*d^6 + 28*a^2*b^6*c^8*d^7 - 56*a^3*b^5*c^7*d^8 + 70*a^4*b^4*c^6*d^9 - 56*a^5*b^3*c^5*d^10 + 28*a^6*b^2*c^4*d^11 - 8*a^7*b*c^3*d^12 + a^8*c^2*d^13)$

$$c^2d^{13}x^5 + 35(b^8c^{11}d^4 - 8a^2b^7c^{10}d^5 + 28a^2b^6c^9d^6 - 56a^3b^5c^8d^7 + 70a^4b^4c^7d^8 - 56a^5b^3c^6d^9 + 28a^6b^2c^5d^{10} - 8a^7b^1c^4d^{11} + a^8c^3d^{12})x^4 + 35(b^8c^{12}d^3 - 8a^2b^7c^{11}d^4 + 28a^2b^6c^{10}d^5 - 56a^3b^5c^9d^6 + 70a^4b^4c^8d^7 - 56a^5b^3c^7d^8 + 28a^6b^2c^6d^9 - 8a^7b^1c^5d^{10} + a^8c^4d^{11})x^3 + 21(b^8c^{13}d^2 - 8a^2b^7c^{12}d^3 + 28a^2b^6c^{11}d^4 - 56a^3b^5c^{10}d^5 + 70a^4b^4c^9d^6 - 56a^5b^3c^8d^7 + 28a^6b^2c^7d^8 - 8a^7b^1c^6d^9 + a^8c^5d^{10})x^2 + 7(b^8c^{14}d - 8a^2b^7c^{13}d^2 + 28a^2b^6c^{12}d^3 - 56a^3b^5c^{11}d^4 + 70a^4b^4c^{10}d^5 - 56a^5b^3c^9d^6 + 28a^6b^2c^8d^7 - 8a^7b^1c^7d^8 + a^8c^6d^9)x$$

giac [B] time = 1.33, size = 703, normalized size = 3.48

$$b^8 \log(|bx + a|)$$

$$\frac{b^8 \log(|bx + a|)}{b^9c^8 - 8ab^8c^7d + 28a^2b^7c^6d^2 - 56a^3b^6c^5d^3 + 70a^4b^5c^4d^4 - 56a^5b^4c^3d^5 + 28a^6b^3c^2d^6 - 8a^7b^2cd^7 + a^8bd^8 - b^8c^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^8,x, algorithm="giac")

[Out] $b^8 \log(\text{abs}(bx + a)) / (b^9c^8 - 8a^2b^7c^7d + 28a^2b^6c^6d^2 - 56a^3b^5c^5d^3 + 70a^4b^4c^4d^4 - 56a^5b^3c^3d^5 + 28a^6b^2c^2d^6 - 8a^7b^1c^1d^7 + a^8b^0d^8) - b^7d \log(\text{abs}(dx + c)) / (b^8c^8d - 8a^2b^7c^7d^2 + 28a^2b^6c^6d^3 - 56a^3b^5c^5d^4 + 70a^4b^4c^4d^5 - 56a^5b^3c^3d^6 + 28a^6b^2c^2d^7 - 8a^7b^1c^1d^8 + a^8d^9) + 1/4 \cdot 20 \cdot (1089b^7c^7 - 2940a^2b^6c^6d + 4410a^2b^5c^5d^2 - 4900a^3b^4c^4d^3 + 3675a^4b^3c^3d^4 - 1764a^5b^2c^2d^5 + 490a^6b^1c^1d^6 - 60a^7d^7 + 420(b^7c^6d - ab^6d^7))x^6 + 210 \cdot (13b^7c^2d^5 - 14a^2b^6c^1d^6 + a^2b^5d^7)x^5 + 70 \cdot (107b^7c^3d^4 - 126a^2b^6c^2d^5 + 21a^2b^5c^1d^6 - 2a^3b^4d^7)x^4 + 35 \cdot (319b^7c^4d^3 - 420a^2b^6c^3d^4 + 126a^2b^5c^2d^5 - 28a^3b^4c^1d^6 + 3a^4b^3d^7)x^3 + 21 \cdot (459b^7c^5d^2 - 700a^2b^6c^4d^3 + 350a^2b^5c^3d^4 - 140a^3b^4c^2d^5 + 35a^4b^3c^1d^6 - 4a^5b^2d^7)x^2 + 7 \cdot (669b^7c^6d - 1260a^2b^6c^5d^2 + 1050a^2b^5c^4d^3 - 700a^3b^4c^3d^4 + 315a^4b^3c^2d^5 - 84a^5b^2c^1d^6 + 10a^6b^1d^7)x / ((b^8c^8d - 8a^2b^7c^7d^2 + 28a^2b^6c^6d^3 - 56a^3b^5c^5d^4 + 70a^4b^4c^4d^5 - 56a^5b^3c^3d^6 + 28a^6b^2c^2d^7 - 8a^7b^1c^1d^8 + a^8d^9) \cdot (dx + c)^7)$

maple [A] time = 0.02, size = 192, normalized size = 0.95

$$\frac{b^7 \ln(bx + a)}{(ad - bc)^8} - \frac{b^7 \ln(dx + c)}{(ad - bc)^8} - \frac{b^6}{(ad - bc)^7(dx + c)} + \frac{b^5}{2(ad - bc)^6(dx + c)^2} - \frac{b^4}{3(ad - bc)^5(dx + c)^3} + \frac{b^3}{4(ad - bc)^4(dx + c)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)/(d*x+c)^8,x)

[Out] $-1/7/(a*d-b*c)/(d*x+c)^7-1/5*b^2/(a*d-b*c)^3/(d*x+c)^5-1/3*b^4/(a*d-b*c)^5/(d*x+c)^3-b^6/(a*d-b*c)^7/(d*x+c)+1/6*b/(a*d-b*c)^2/(d*x+c)^6+1/4*b^3/(a*d-b*c)^4/(d*x+c)^4+1/2*b^5/(a*d-b*c)^6/(d*x+c)^2-b^7/(a*d-b*c)^8*\ln(d*x+c)+b^7/(a*d-b*c)^8*\ln(b*x+a)$

maxima [B] time = 2.97, size = 1418, normalized size = 7.02

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/(d*x+c)^8,x, algorithm="maxima")`

[Out] $b^7*\log(b*x + a)/(b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8) - b^7*\log(d*x + c)/(b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8) + 1/420*(420*b^6*d^6*x^6 + 1089*b^6*c^6 - 1851*a*b^5*c^5*d + 2559*a^2*b^4*c^4*d^2 - 2341*a^3*b^3*c^3*d^3 + 1334*a^4*b^2*c^2*d^4 - 430*a^5*b*c*d^5 + 60*a^6*d^6 + 210*(13*b^6*c*d^5 - a*b^5*d^6)*x^5 + 70*(107*b^6*c^2*d^4 - 19*a*b^5*c*d^5 + 2*a^2*b^4*d^6)*x^4 + 35*(319*b^6*c^3*d^3 - 101*a*b^5*c^2*d^4 + 25*a^2*b^4*c*d^5 - 3*a^3*b^3*d^6)*x^3 + 21*(459*b^6*c^4*d^2 - 241*a*b^5*c^3*d^3 + 109*a^2*b^4*c^2*d^4 - 31*a^3*b^3*c*d^5 + 4*a^4*b^2*d^6)*x^2 + 7*(669*b^6*c^5*d - 591*a*b^5*c^4*d^2 + 459*a^2*b^4*c^3*d^3 - 241*a^3*b^3*c^2*d^4 + 74*a^4*b^2*c*d^5 - 10*a^5*b*d^6)*x)/(b^7*c^14 - 7*a*b^6*c^13*d + 21*a^2*b^5*c^12*d^2 - 35*a^3*b^4*c^11*d^3 + 35*a^4*b^3*c^10*d^4 - 21*a^5*b^2*c^9*d^5 + 7*a^6*b*c^8*d^6 - a^7*c^7*d^7 + (b^7*c^7*d^7 - 7*a*b^6*c^6*d^8 + 21*a^2*b^5*c^5*d^9 - 35*a^3*b^4*c^4*d^10 + 35*a^4*b^3*c^3*d^11 - 21*a^5*b^2*c^2*d^12 + 7*a^6*b*c*d^13 - a^7*d^14)*x^7 + 7*(b^7*c^8*d^6 - 7*a*b^6*c^7*d^7 + 21*a^2*b^5*c^6*d^8 - 35*a^3*b^4*c^5*d^9 + 35*a^4*b^3*c^4*d^10 - 21*a^5*b^2*c^3*d^11 + 7*a^6*b*c^2*d^12 - a^7*c*d^13)*x^6 + 21*(b^7*c^9*d^5 - 7*a*b^6*c^8*d^6 + 21*a^2*b^5*c^7*d^7 - 35*a^3*b^4*c^6*d^8 + 35*a^4*b^3*c^5*d^9 - 21*a^5*b^2*c^4*d^10 + 7*a^6*b*c^3*d^11 - a^7*c^2*d^12)*x^5 + 35*(b^7*c^10*d^4 - 7*a*b^6*c^9*d^5 + 21*a^2*b^5*c^8*d^6 - 35*a^3*b^4*c^7*d^7 + 35*a^4*b^3*c^6*d^8 - 21*a^5*b^2*c^5*d^9 + 7*a^6*b*c^4*d^10 - a^7*c^3*d^11)*x^4 + 35*(b^7*c^11*d^3 - 7*a*b^6*c^10*d^4 + 21*a^2*b^5*c^9*d^5 - 35*a^3*b^4*c^8*d^6 + 35*a^4*b^3*c^7*d^7 - 21*a^5*b^2*c^6*d^8 + 7*a^6*b*c^5*d^9 - a^7*c^4*d^10)*x^3 + 21*(b^7*c^12*d^2 - 7*a*b^6*c^11*d^3 + 21*a^2*b^5*c^10*d^4 - 35*a^3*b^4*c^9*d^5 + 35*a^4*b^3*c^8*d^6 - 21*a^5*b^2*c^7*d^7 + 7*a^6*b*c^6*d^8 - a^7*c^5*d^9)*x^2 + 7*(b^7*c^13*d - 7*a*b^6*c^12*d^2 + 21*a^2*b^5*c^11*d^3 - 35*a^3*b^4*c^10*d^4 + 35*a^4*b^3*c^9*d^5 - 21*a^5*b^2*c^8*d^6 + 7*a^6*b*c^7*d^7 - a^7*c^6*d^8)*x)$

mupad [B] time = 0.87, size = 1299, normalized size = 6.43

$$2b^7 \operatorname{atanh} \left(\frac{a^8 d^8 - 6a^7 b c d^7 + 14a^6 b^2 c^2 d^6 - 14a^5 b^3 c^3 d^5 + 14a^4 b^4 c^4 d^4 - 14a^3 b^5 c^5 d^3 - 14a^2 b^6 c^6 d^2 + 6ab^7 c^7 d - b^8 c^8}{(ad-bc)^8} + \frac{2bdx(a^7 d^7 - 7a^6 b c d^6 + 21a^5 b^2 c^2 d^5 - 35a^4 b^3 c^3 d^4 + 35a^3 b^4 c^4 d^3 - 21a^2 b^5 c^5 d^2 + 7ab^6 c^6 d - 7a^6 b^7 c^7 d + b^7 c^8)}{(ad-bc)^8} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)*(c + d*x)^8),x)`

[Out] $(2*b^7*\operatorname{atanh}((a^8*d^8 - b^8*c^8 - 14*a^2*b^6*c^6*d^2 + 14*a^3*b^5*c^5*d^3 - 14*a^4*b^4*c^4*d^3 + 14*a^5*b^3*c^3*d^4 - 14*a^6*b^2*c^2*d^4 + 6*a*b^7*c^7*d - 6*a^7*b^6*c^6*d^2)/(a*d - b*c)^8 + (2*b*d*x*(a^7*d^7 - b^7*c^7 - 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 - 35*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 7*a^6*b^5*c^5*d^2)/(a*d - b*c)^8)))/(a*d - b*c)^8 - ((60*a^6*d^6 + 1089*b^6*c^6 + 2559*a^2*b^4*c^4*d^2 - 2341*a^3*b^3*c^3*d^3 + 1334*a^4*b^2*c^2*d^4 - 1851*a*b^5*c^5*d - 430*a^5*b*c*d^5)/(420*(a^7*d^7 - b^7*c^7 - 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 - 35*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 7*a^6*b^5*c^5*d^2) - (b^3*x^3*(3*a^3*d^6 - 319*b^3*c^3*d^3 + 101*a*b^2*c^2*d^4 - 25*a^2*b*c*d^5)))/(12*(a^7*d^7 - b^7*c^7 - 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 - 35*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 7*a^6*b^5*c^5*d^2) + (b^6*d^6*x^6)/(a^7*d^7 - b^7*c^7 - 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 - 35*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 7*a^6*b^5*c^5*d^2) - (b^5*x^5*(a*d^6 - 13*b*c*d^5))/(2*(a^7*d^7 - b^7*c^7 - 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 - 35*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 7*a^6*b^5*c^5*d^2) + (b^2*x^2*(4*a^4*d^6 + 459*b^4*c^4*d^2 - 241*a*b^3*c^3*d^3 + 109*a^2*b^2*c^2*d^4 - 31*a^3*b*c*d^5))/(20*(a^7*d^7 - b^7*c^7 - 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 - 35*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 7*a^6*b^5*c^5*d^2) + (b^4*x^4*(2*a^2*d^6 + 107*b^2*c^2*d^4 - 19*a*b*c*d^5))/(6*(a^7*d^7 - b^7*c^7 - 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 - 35*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 7*a^6*b^5*c^5*d^2) - (b*x*(10*a^5*d^6 - 669*b^5*c^5*d + 591*a*b^4*c^4*d^2 - 459*a^2*b^3*c^3*d^3 + 241*a^3*b^2*c^2*d^4 - 74*a^4*b*c*d^5))/(60*(a^7*d^7 - b^7*c^7 - 21*a^2*b^5*c^5*d^2 + 35*a^3*b^4*c^4*d^3 - 35*a^4*b^3*c^3*d^4 + 21*a^5*b^2*c^2*d^5 + 7*a*b^6*c^6*d - 7*a^6*b^5*c^5*d^2)))/(c^7 + d^7*x^7 + 7*c*d^6*x^6 + 21*c^5*d^2*x^2 + 35*c^4*d^3*x^3 + 35*c^3*d^4*x^4 + 21*c^2*d^5*x^5 + 7*c^6*d*x)$

sympy [B] time = 4.49, size = 1776, normalized size = 8.79

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/(d*x+c)**8,x)`

```
[Out] -b**7*log(x + (-a**9*b**7*d**9/(a*d - b*c)**8 + 9*a**8*b**8*c*d**8/(a*d - b
*c)**8 - 36*a**7*b**9*c**2*d**7/(a*d - b*c)**8 + 84*a**6*b**10*c**3*d**6/(a
*d - b*c)**8 - 126*a**5*b**11*c**4*d**5/(a*d - b*c)**8 + 126*a**4*b**12*c**
5*d**4/(a*d - b*c)**8 - 84*a**3*b**13*c**6*d**3/(a*d - b*c)**8 + 36*a**2*b**
*14*c**7*d**2/(a*d - b*c)**8 - 9*a*b**15*c**8*d/(a*d - b*c)**8 + a*b**7*d +
b**16*c**9/(a*d - b*c)**8 + b**8*c)/(2*b**8*d))/(a*d - b*c)**8 + b**7*log(
x + (a**9*b**7*d**9/(a*d - b*c)**8 - 9*a**8*b**8*c*d**8/(a*d - b*c)**8 + 36
*a**7*b**9*c**2*d**7/(a*d - b*c)**8 - 84*a**6*b**10*c**3*d**6/(a*d - b*c)**
8 + 126*a**5*b**11*c**4*d**5/(a*d - b*c)**8 - 126*a**4*b**12*c**5*d**4/(a*d
- b*c)**8 + 84*a**3*b**13*c**6*d**3/(a*d - b*c)**8 - 36*a**2*b**14*c**7*d**
*2/(a*d - b*c)**8 + 9*a*b**15*c**8*d/(a*d - b*c)**8 + a*b**7*d - b**16*c**9
/(a*d - b*c)**8 + b**8*c)/(2*b**8*d))/(a*d - b*c)**8 + (-60*a**6*d**6 + 430
*a**5*b*c*d**5 - 1334*a**4*b**2*c**2*d**4 + 2341*a**3*b**3*c**3*d**3 - 2559
*a**2*b**4*c**4*d**2 + 1851*a*b**5*c**5*d - 1089*b**6*c**6 - 420*b**6*d**6*
x**6 + x**5*(210*a*b**5*d**6 - 2730*b**6*c*d**5) + x**4*(-140*a**2*b**4*d**
6 + 1330*a*b**5*c*d**5 - 7490*b**6*c**2*d**4) + x**3*(105*a**3*b**3*d**6 -
875*a**2*b**4*c*d**5 + 3535*a*b**5*c**2*d**4 - 11165*b**6*c**3*d**3) + x**2
*(-84*a**4*b**2*d**6 + 651*a**3*b**3*c*d**5 - 2289*a**2*b**4*c**2*d**4 + 50
61*a*b**5*c**3*d**3 - 9639*b**6*c**4*d**2) + x*(70*a**5*b*d**6 - 518*a**4*b
**2*c*d**5 + 1687*a**3*b**3*c**2*d**4 - 3213*a**2*b**4*c**3*d**3 + 4137*a*b
**5*c**4*d**2 - 4683*b**6*c**5*d))/(420*a**7*c**7*d**7 - 2940*a**6*b*c**8*d
**6 + 8820*a**5*b**2*c**9*d**5 - 14700*a**4*b**3*c**10*d**4 + 14700*a**3*b
**4*c**11*d**3 - 8820*a**2*b**5*c**12*d**2 + 2940*a*b**6*c**13*d - 420*b**7*
c**14 + x**7*(420*a**7*d**14 - 2940*a**6*b*c*d**13 + 8820*a**5*b**2*c**2*d
**12 - 14700*a**4*b**3*c**3*d**11 + 14700*a**3*b**4*c**4*d**10 - 8820*a**2*b
**5*c**5*d**9 + 2940*a*b**6*c**6*d**8 - 420*b**7*c**7*d**7) + x**6*(2940*a*
**7*c*d**13 - 20580*a**6*b*c**2*d**12 + 61740*a**5*b**2*c**3*d**11 - 102900*
a**4*b**3*c**4*d**10 + 102900*a**3*b**4*c**5*d**9 - 61740*a**2*b**5*c**6*d
**8 + 20580*a*b**6*c**7*d**7 - 2940*b**7*c**8*d**6) + x**5*(8820*a**7*c**2*d
**12 - 61740*a**6*b*c**3*d**11 + 185220*a**5*b**2*c**4*d**10 - 308700*a**4*
b**3*c**5*d**9 + 308700*a**3*b**4*c**6*d**8 - 185220*a**2*b**5*c**7*d**7 +
61740*a*b**6*c**8*d**6 - 8820*b**7*c**9*d**5) + x**4*(14700*a**7*c**3*d**11
- 102900*a**6*b*c**4*d**10 + 308700*a**5*b**2*c**5*d**9 - 514500*a**4*b**3*
c**6*d**8 + 514500*a**3*b**4*c**7*d**7 - 308700*a**2*b**5*c**8*d**6 + 1029
00*a*b**6*c**9*d**5 - 14700*b**7*c**10*d**4) + x**3*(14700*a**7*c**4*d**10
- 102900*a**6*b*c**5*d**9 + 308700*a**5*b**2*c**6*d**8 - 514500*a**4*b**3*c
**7*d**7 + 514500*a**3*b**4*c**8*d**6 - 308700*a**2*b**5*c**9*d**5 + 102900
*a*b**6*c**10*d**4 - 14700*b**7*c**11*d**3) + x**2*(8820*a**7*c**5*d**9 - 6
1740*a**6*b*c**6*d**8 + 185220*a**5*b**2*c**7*d**7 - 308700*a**4*b**3*c**8*
d**6 + 308700*a**3*b**4*c**9*d**5 - 185220*a**2*b**5*c**10*d**4 + 61740*a*b
**6*c**11*d**3 - 8820*b**7*c**12*d**2) + x*(2940*a**7*c**6*d**8 - 20580*a**
6*b*c**7*d**7 + 61740*a**5*b**2*c**8*d**6 - 102900*a**4*b**3*c**9*d**5 + 10
2900*a**3*b**4*c**10*d**4 - 61740*a**2*b**5*c**11*d**3 + 20580*a*b**6*c**12
*d**2 - 2940*b**7*c**13*d))
```

$$3.1373 \quad \int \frac{1}{(a+bx)^2(c+dx)^8} dx$$

Optimal. Leaf size=231

$$\frac{b^7}{(a+bx)(bc-ad)^8} - \frac{8b^7d \log(a+bx)}{(bc-ad)^9} + \frac{8b^7d \log(c+dx)}{(bc-ad)^9} - \frac{7b^6d}{(c+dx)(bc-ad)^8} - \frac{3b^5d}{(c+dx)^2(bc-ad)^7} - \frac{5b^4d}{3(c+dx)^3(bc-ad)^6} - \frac{b^3d}{5(c+dx)^4(bc-ad)^5} - \frac{bd}{5(c+dx)^5(bc-ad)^4}$$

[Out] $-b^7/(-a*d+b*c)^8/(b*x+a)-1/7*d/(-a*d+b*c)^2/(d*x+c)^7-1/3*b*d/(-a*d+b*c)^3/(d*x+c)^6-3/5*b^2*d/(-a*d+b*c)^4/(d*x+c)^5-b^3*d/(-a*d+b*c)^5/(d*x+c)^4-5/3*b^4*d/(-a*d+b*c)^6/(d*x+c)^3-3*b^5*d/(-a*d+b*c)^7/(d*x+c)^2-7*b^6*d/(-a*d+b*c)^8/(d*x+c)-8*b^7*d*\ln(b*x+a)/(-a*d+b*c)^9+8*b^7*d*\ln(d*x+c)/(-a*d+b*c)^9$

Rubi [A] time = 0.27, antiderivative size = 231, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$\frac{b^7}{(a+bx)(bc-ad)^8} - \frac{7b^6d}{(c+dx)(bc-ad)^8} - \frac{3b^5d}{(c+dx)^2(bc-ad)^7} - \frac{5b^4d}{3(c+dx)^3(bc-ad)^6} - \frac{b^3d}{(c+dx)^4(bc-ad)^5} - \frac{bd}{5(c+dx)^5(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^2*(c + d*x)^8), x]

[Out] $-(b^7/((b*c - a*d)^8*(a + b*x))) - d/(7*(b*c - a*d)^2*(c + d*x)^7) - (b*d)/(3*(b*c - a*d)^3*(c + d*x)^6) - (3*b^2*d)/(5*(b*c - a*d)^4*(c + d*x)^5) - (b^3*d)/((b*c - a*d)^5*(c + d*x)^4) - (5*b^4*d)/(3*(b*c - a*d)^6*(c + d*x)^3) - (3*b^5*d)/((b*c - a*d)^7*(c + d*x)^2) - (7*b^6*d)/((b*c - a*d)^8*(c + d*x)) - (8*b^7*d*\text{Log}[a + b*x])/((b*c - a*d)^9) + (8*b^7*d*\text{Log}[c + d*x])/((b*c - a*d)^9)$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] & & NeQ[b*c - a*d, 0] & & ILtQ[m, 0] & & IntegerQ[n] & & !(IGtQ[n, 0] & & LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{(a+bx)^2(c+dx)^8} dx = \int \left(\frac{b^8}{(bc-ad)^8(a+bx)^2} - \frac{8b^8d}{(bc-ad)^9(a+bx)} + \frac{d^2}{(bc-ad)^2(c+dx)^8} + \frac{2bd^2}{(bc-ad)^3(c+dx)^7} - \frac{b^7}{(bc-ad)^8(a+bx)} - \frac{d}{7(bc-ad)^2(c+dx)^7} - \frac{bd}{3(bc-ad)^3(c+dx)^6} - \frac{3b^2d}{5(bc-ad)^4(c+dx)^5} \right) dx$$

Mathematica [A] time = 0.24, size = 213, normalized size = 0.92

$$\frac{\frac{105b^7(bc-ad)}{a+bx} + 840b^7d \log(a+bx) + \frac{735b^6d(bc-ad)}{c+dx} + \frac{315b^5d(bc-ad)^2}{(c+dx)^2} + \frac{175b^4d(bc-ad)^3}{(c+dx)^3} + \frac{105b^3d(bc-ad)^4}{(c+dx)^4} + \frac{63b^2d(bc-ad)^5}{(c+dx)^5} + \dots}{105(bc-ad)^9}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*(c + d*x)^8), x]

[Out]
$$-1/105*((105*b^7*(b*c - a*d))/(a + b*x) - (15*d*(-(b*c) + a*d)^7)/(c + d*x)^7 + (35*b*d*(b*c - a*d)^6)/(c + d*x)^6 + (63*b^2*d*(b*c - a*d)^5)/(c + d*x)^5 + (105*b^3*d*(b*c - a*d)^4)/(c + d*x)^4 + (175*b^4*d*(b*c - a*d)^3)/(c + d*x)^3 + (315*b^5*d*(b*c - a*d)^2)/(c + d*x)^2 + (735*b^6*d*(b*c - a*d))/(c + d*x) + 840*b^7*d*Log[a + b*x] - 840*b^7*d*Log[c + d*x])/(b*c - a*d)^9$$

fricas [B] time = 0.54, size = 2264, normalized size = 9.80

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^8,x, algorithm="fricas")

[Out]
$$-1/105*(105*b^8*c^8 + 1338*a*b^7*c^7*d - 2940*a^2*b^6*c^6*d^2 + 2940*a^3*b^5*c^5*d^3 - 2450*a^4*b^4*c^4*d^4 + 1470*a^5*b^3*c^3*d^5 - 588*a^6*b^2*c^2*d^6 + 140*a^7*b*c*d^7 - 15*a^8*d^8 + 840*(b^8*c*d^7 - a*b^7*d^8)*x^7 + 420*(13*b^8*c^2*d^6 - 12*a*b^7*c*d^7 - a^2*b^6*d^8)*x^6 + 140*(107*b^8*c^3*d^5 - 87*a*b^7*c^2*d^6 - 21*a^2*b^6*c*d^7 + a^3*b^5*d^8)*x^5 + 70*(319*b^8*c^4*d^4 - 206*a*b^7*c^3*d^5 - 126*a^2*b^6*c^2*d^6 + 14*a^3*b^5*c*d^7 - a^4*b^4*d^8)*x^4 + 14*(1377*b^8*c^5*d^3 - 505*a*b^7*c^4*d^4 - 1050*a^2*b^6*c^3*d^5 + 210*a^3*b^5*c^2*d^6 - 35*a^4*b^4*c*d^7 + 3*a^5*b^3*d^8)*x^3 + 14*(669*b^8*c^6*d^2 + 117*a*b^7*c^5*d^3 - 1050*a^2*b^6*c^4*d^4 + 350*a^3*b^5*c^3*d^5 - 105*a^4*b^4*c^2*d^6 + 21*a^5*b^3*c*d^7 - 2*a^6*b^2*d^8)*x^2 + 2*(1089*b^8*c^7*d + 1743*a*b^7*c^6*d^2 - 4410*a^2*b^6*c^5*d^3 + 2450*a^3*b^5*c^4*d^4 - 1225*a^4*b^4*c^3*d^5 + 441*a^5*b^3*c^2*d^6 - 98*a^6*b^2*c*d^7 + 10*a^7*b*d^8)*x + 840*(b^8*d^8*x^8 + a*b^7*c^7*d + (7*b^8*c*d^7 + a*b^7*d^8)*x^7 + 7*(3*b^8*c^2*d^6 + a*b^7*c*d^7)*x^6 + 7*(5*b^8*c^3*d^5 + 3*a*b^7*c^2*d^6)*x^5 + 35*(b^8*c^4*d^4 + a*b^7*c^3*d^5)*x^4 + 7*(3*b^8*c^5*d^3 + 5*a*b^7*c^4*d^4)*x^3 + 7*(b^8*c^6*d^2 + 3*a*b^7*c^5*d^3)*x^2 + (b^8*c^7*d + 7*a*b^7*c^6*d^2)*x)*log(b*x + a) - 840*(b^8*d^8*x^8 + a*b^7*c^7*d + (7*b^8*c*d^7 + a*b^7*d^8)*x^7 + 7*(3*b^8*c^2*d^6 + a*b^7*c*d^7)*x^6 + 7*(5*b^8*c^3*d^5 + 3*a*b^7*c^2*d^6)*x^5 + 35*(b^8*c^4*d^4 + a*b^7*c^3*d^5)*x^4 + 7*(3*b^8*c^5*d^3 + 5*a*b^7*c^4*d^4)*x^3 + 7*(b^8*c^6*d^2 + 3*a*b^7*c^5*d^3)*x^2 + (b^8*c^7*d + 7*a*b^7*c^6*d^2)*x)*log(d*x + c))/(a*b^9*c^16 - 9*a^2*b^8*c^15*d + 36*a^3*b^7*c^14*d^2 - 84*a^4*b^6*c^13*d^3 + 126*a^5*b^5*c^12*d^4 - 126*a^6*b^4*c^11*d^5 + 84*a^7*b^3*c^10*d^6 - 36*a^8*b^2*c^9*d^7 + 9*a^9*b*c^8*d^8 - a^10*c^7$$

```

*d^9 + (b^10*c^9*d^7 - 9*a*b^9*c^8*d^8 + 36*a^2*b^8*c^7*d^9 - 84*a^3*b^7*c^
6*d^10 + 126*a^4*b^6*c^5*d^11 - 126*a^5*b^5*c^4*d^12 + 84*a^6*b^4*c^3*d^13
- 36*a^7*b^3*c^2*d^14 + 9*a^8*b^2*c*d^15 - a^9*b*d^16)*x^8 + (7*b^10*c^10*d
^6 - 62*a*b^9*c^9*d^7 + 243*a^2*b^8*c^8*d^8 - 552*a^3*b^7*c^7*d^9 + 798*a^4
*b^6*c^6*d^10 - 756*a^5*b^5*c^5*d^11 + 462*a^6*b^4*c^4*d^12 - 168*a^7*b^3*c
^3*d^13 + 27*a^8*b^2*c^2*d^14 + 2*a^9*b*c*d^15 - a^10*d^16)*x^7 + 7*(3*b^10
*c^11*d^5 - 26*a*b^9*c^10*d^6 + 99*a^2*b^8*c^9*d^7 - 216*a^3*b^7*c^8*d^8 +
294*a^4*b^6*c^7*d^9 - 252*a^5*b^5*c^6*d^10 + 126*a^6*b^4*c^5*d^11 - 24*a^7*
b^3*c^4*d^12 - 9*a^8*b^2*c^3*d^13 + 6*a^9*b*c^2*d^14 - a^10*c*d^15)*x^6 + 7
*(5*b^10*c^12*d^4 - 42*a*b^9*c^11*d^5 + 153*a^2*b^8*c^10*d^6 - 312*a^3*b^7*
c^9*d^7 + 378*a^4*b^6*c^8*d^8 - 252*a^5*b^5*c^7*d^9 + 42*a^6*b^4*c^6*d^10 +
72*a^7*b^3*c^5*d^11 - 63*a^8*b^2*c^4*d^12 + 22*a^9*b*c^3*d^13 - 3*a^10*c^2
*d^14)*x^5 + 35*(b^10*c^13*d^3 - 8*a*b^9*c^12*d^4 + 27*a^2*b^8*c^11*d^5 - 4
8*a^3*b^7*c^10*d^6 + 42*a^4*b^6*c^9*d^7 - 42*a^6*b^4*c^7*d^9 + 48*a^7*b^3*c
^6*d^10 - 27*a^8*b^2*c^5*d^11 + 8*a^9*b*c^4*d^12 - a^10*c^3*d^13)*x^4 + 7*(
3*b^10*c^14*d^2 - 22*a*b^9*c^13*d^3 + 63*a^2*b^8*c^12*d^4 - 72*a^3*b^7*c^11
*d^5 - 42*a^4*b^6*c^10*d^6 + 252*a^5*b^5*c^9*d^7 - 378*a^6*b^4*c^8*d^8 + 31
2*a^7*b^3*c^7*d^9 - 153*a^8*b^2*c^6*d^10 + 42*a^9*b*c^5*d^11 - 5*a^10*c^4*d
^12)*x^3 + 7*(b^10*c^15*d - 6*a*b^9*c^14*d^2 + 9*a^2*b^8*c^13*d^3 + 24*a^3*
b^7*c^12*d^4 - 126*a^4*b^6*c^11*d^5 + 252*a^5*b^5*c^10*d^6 - 294*a^6*b^4*c^
9*d^7 + 216*a^7*b^3*c^8*d^8 - 99*a^8*b^2*c^7*d^9 + 26*a^9*b*c^6*d^10 - 3*a^
10*c^5*d^11)*x^2 + (b^10*c^16 - 2*a*b^9*c^15*d - 27*a^2*b^8*c^14*d^2 + 168*
a^3*b^7*c^13*d^3 - 462*a^4*b^6*c^12*d^4 + 756*a^5*b^5*c^11*d^5 - 798*a^6*b^
4*c^10*d^6 + 552*a^7*b^3*c^9*d^7 - 243*a^8*b^2*c^8*d^8 + 62*a^9*b*c^7*d^9 -
7*a^10*c^6*d^10)*x)

```

giac [B] time = 1.37, size = 714, normalized size = 3.09

$$b^{15}$$

$$(b^{16}c^8 - 8ab^{15}c^7d + 28a^2b^{14}c^6d^2 - 56a^3b^{13}c^5d^3 + 70a^4b^{12}c^4d^4 - 56a^5b^{11}c^3d^5 + 28a^6b^{10}c^2d^6 - 8a^7b^9cd^7 + a^8b^8d^8)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^8,x, algorithm="giac")

```

[Out] -b^15/((b^16*c^8 - 8*a*b^15*c^7*d + 28*a^2*b^14*c^6*d^2 - 56*a^3*b^13*c^5*d
^3 + 70*a^4*b^12*c^4*d^4 - 56*a^5*b^11*c^3*d^5 + 28*a^6*b^10*c^2*d^6 - 8*a^
7*b^9*c*d^7 + a^8*b^8*d^8)*(b*x + a)) + 8*b^8*d*log(abs(b*c/(b*x + a) - a*d
/(b*x + a) + d))/(b^10*c^9 - 9*a*b^9*c^8*d + 36*a^2*b^8*c^7*d^2 - 84*a^3*b^
7*c^6*d^3 + 126*a^4*b^6*c^5*d^4 - 126*a^5*b^5*c^4*d^5 + 84*a^6*b^4*c^3*d^6
- 36*a^7*b^3*c^2*d^7 + 9*a^8*b^2*c*d^8 - a^9*b*d^9) + 1/105*(1443*b^7*d^8 +
9366*(b^9*c*d^7 - a*b^8*d^8)/((b*x + a)*b) + 25578*(b^11*c^2*d^6 - 2*a*b^1
0*c*d^7 + a^2*b^9*d^8)/((b*x + a)^2*b^2) + 37730*(b^13*c^3*d^5 - 3*a*b^12*c
^2*d^6 + 3*a^2*b^11*c*d^7 - a^3*b^10*d^8)/((b*x + a)^3*b^3) + 31850*(b^15*c

```


$$\begin{aligned} &^4*d^4 - 4*a*b^{14}*c^3*d^5 + 6*a^2*b^{13}*c^2*d^6 - 4*a^3*b^{12}*c*d^7 + a^4*b^{11}*d^8)/((b*x + a)^4*b^4) + 14700*(b^{17}*c^5*d^3 - 5*a*b^{16}*c^4*d^4 + 10*a^2* \\ &b^{15}*c^3*d^5 - 10*a^3*b^{14}*c^2*d^6 + 5*a^4*b^{13}*c*d^7 - a^5*b^{12}*d^8)/((b*x \\ &+ a)^5*b^5) + 2940*(b^{19}*c^6*d^2 - 6*a*b^{18}*c^5*d^3 + 15*a^2*b^{17}*c^4*d^4 \\ &- 20*a^3*b^{16}*c^3*d^5 + 15*a^4*b^{15}*c^2*d^6 - 6*a^5*b^{14}*c*d^7 + a^6*b^{13}*d \\ &^8)/((b*x + a)^6*b^6))/((b*c - a*d)^9*(b*c/(b*x + a) - a*d/(b*x + a) + d)^7 \\ &) \end{aligned}$$

maple [A] time = 0.02, size = 223, normalized size = 0.97

$$\frac{8b^7d \ln(bx + a)}{(ad - bc)^9} - \frac{8b^7d \ln(dx + c)}{(ad - bc)^9} - \frac{b^7}{(ad - bc)^8(bx + a)} - \frac{7b^6d}{(ad - bc)^8(dx + c)} + \frac{3b^5d}{(ad - bc)^7(dx + c)^2} - \frac{5b^4d}{3(ad - bc)^6(dx + c)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/(d*x+c)^8,x)

[Out] $-1/7*d/(a*d-b*c)^2/(d*x+c)^7-8*d/(a*d-b*c)^9*b^7*\ln(d*x+c)-7*d/(a*d-b*c)^8*b^6/(d*x+c)+3*d/(a*d-b*c)^7*b^5/(d*x+c)^2-5/3*d/(a*d-b*c)^6*b^4/(d*x+c)^3+d/(a*d-b*c)^5*b^3/(d*x+c)^4-3/5*d/(a*d-b*c)^4*b^2/(d*x+c)^5+1/3*d/(a*d-b*c)^3*b/(d*x+c)^6-b^7/(a*d-b*c)^8/(b*x+a)+8*d/(a*d-b*c)^9*b^7*\ln(b*x+a)$

maxima [B] time = 3.88, size = 1881, normalized size = 8.14

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^8,x, algorithm="maxima")

[Out] $-8*b^7*d*\log(b*x + a)/(b^9*c^9 - 9*a*b^8*c^8*d + 36*a^2*b^7*c^7*d^2 - 84*a^3*b^6*c^6*d^3 + 126*a^4*b^5*c^5*d^4 - 126*a^5*b^4*c^4*d^5 + 84*a^6*b^3*c^3*d^6 - 36*a^7*b^2*c^2*d^7 + 9*a^8*b*c*d^8 - a^9*d^9) + 8*b^7*d*\log(d*x + c)/(b^9*c^9 - 9*a*b^8*c^8*d + 36*a^2*b^7*c^7*d^2 - 84*a^3*b^6*c^6*d^3 + 126*a^4*b^5*c^5*d^4 - 126*a^5*b^4*c^4*d^5 + 84*a^6*b^3*c^3*d^6 - 36*a^7*b^2*c^2*d^7 + 9*a^8*b*c*d^8 - a^9*d^9) - 1/105*(840*b^7*d^7*x^7 + 105*b^7*c^7 + 1443*a*b^6*c^6*d - 1497*a^2*b^5*c^5*d^2 + 1443*a^3*b^4*c^4*d^3 - 1007*a^4*b^3*c^3*d^4 + 463*a^5*b^2*c^2*d^5 - 125*a^6*b*c*d^6 + 15*a^7*d^7 + 420*(13*b^7*c*d^6 + a*b^6*d^7)*x^6 + 140*(107*b^7*c^2*d^5 + 20*a*b^6*c*d^6 - a^2*b^5*d^7)*x^5 + 70*(319*b^7*c^3*d^4 + 113*a*b^6*c^2*d^5 - 13*a^2*b^5*c*d^6 + a^3*b^4*d^7)*x^4 + 14*(1377*b^7*c^4*d^3 + 872*a*b^6*c^3*d^4 - 178*a^2*b^5*c^2*d^5 + 32*a^3*b^4*c*d^6 - 3*a^4*b^3*d^7)*x^3 + 14*(669*b^7*c^5*d^2 + 786*a*b^6*c^4*d^3 - 264*a^2*b^5*c^3*d^4 + 86*a^3*b^4*c^2*d^5 - 19*a^4*b^3*c*d^6 + 2*a^5*b^2*d^7)*x^2 + 2*(1089*b^7*c^6*d + 2832*a*b^6*c^5*d^2 - 1578*a^2*b^5*c^4*d^3 + 872*a^3*b^4*c^3*d^4 - 353*a^4*b^3*c^2*d^5 + 88*a^5*b^2*c*d^6 - 10*a^6*b*d^7)*x)/(a*b^8*c^15 - 8*a^2*b^7*c^14*d + 28*a^3*b^6*c^13*d^2 - 56*a^4*b$

$$\begin{aligned}
& ^5c^{12}d^3 + 70a^5b^4c^{11}d^4 - 56a^6b^3c^{10}d^5 + 28a^7b^2c^9d^6 - 8a^8b^1c^8d^7 + a^9c^7d^8 + (b^9c^8d^7 - 8a^8b^7c^7d^8 + 28a^2 \\
& *b^7c^6d^9 - 56a^3b^6c^5d^{10} + 70a^4b^5c^4d^{11} - 56a^5b^4c^3d^{12} + 28a^6b^3c^2d^{13} - 8a^7b^2c^1d^{14} + a^8b^1d^{15})x^8 + (7b^9c^9 \\
& *d^6 - 55a^8b^8c^8d^7 + 188a^2b^7c^7d^8 - 364a^3b^6c^6d^9 + 434a^4b^5c^5d^{10} - 322a^5b^4c^4d^{11} + 140a^6b^3c^3d^{12} - 28a^7b^2c^2 \\
& *d^{13} - a^8b^1c^1d^{14} + a^9d^{15})x^7 + 7*(3b^9c^{10}d^5 - 23a^8b^8c^9d^6 + 76a^2b^7c^8d^7 - 140a^3b^6c^7d^8 + 154a^4b^5c^6d^9 - 98a^5b^4c^5d^{10} \\
& + 28a^6b^3c^4d^{11} + 4a^7b^2c^3d^{12} - 5a^8b^1c^2d^{13} + a^9c^1d^{14})x^6 + 7*(5b^9c^{11}d^4 - 37a^8b^8c^{10}d^5 + 116a^2b^7c^9d^6 - 196a^3b^6c^8d^7 \\
& + 182a^4b^5c^7d^8 - 70a^5b^4c^6d^9 - 28a^6b^3c^5d^{10} + 44a^7b^2c^4d^{11} - 19a^8b^1c^3d^{12} + 3a^9c^2d^{13})x^5 + 35*(b^9c^{12}d^3 - 7a^8b^8c^{11}d^4 \\
& + 20a^2b^7c^{10}d^5 - 28a^3b^6c^9d^6 + 14a^4b^5c^8d^7 + 14a^5b^4c^7d^8 - 28a^6b^3c^6d^9 + 20a^7b^2c^5d^{10} - 7a^8b^1c^4d^{11} + a^9c^3d^{12})x^4 + 7*(3b^9c^{13}d^2 \\
& - 19a^8b^8c^{12}d^3 + 44a^2b^7c^{11}d^4 - 28a^3b^6c^{10}d^5 - 70a^4b^5c^9d^6 + 182a^5b^4c^8d^7 - 196a^6b^3c^7d^8 + 116a^7b^2c^6d^9 - 37a^8b^1c^5d^{10} \\
& + 5a^9c^4d^{11})x^3 + 7*(b^9c^{14}d - 5a^8b^8c^{13}d^2 + 4a^2b^7c^{12}d^3 + 28a^3b^6c^{11}d^4 - 98a^4b^5c^{10}d^5 + 154a^5b^4c^9d^6 - 140a^6b^3c^8d^7 \\
& + 76a^7b^2c^7d^8 - 23a^8b^1c^6d^9 + 3a^9c^5d^{10})x^2 + (b^9c^{15} - a^8b^8c^{14}d - 28a^2b^7c^{13}d^2 + 140a^3b^6c^{12}d^3 - 322a^4b^5c^{11}d^4 + 434a^5b^4c^{10}d^5 \\
& - 364a^6b^3c^9d^6 + 188a^7b^2c^8d^7 - 55a^8b^1c^7d^8 + 7a^9c^6d^9)x
\end{aligned}$$

mupad [B] time = 1.39, size = 1738, normalized size = 7.52

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/((a + b*x)^2*(c + d*x)^8), x)$

[Out] $(16b^7d \operatorname{atanh}((a^9d^9 + b^9c^9 + 20a^2b^7c^7d^2 - 28a^3b^6c^6d^3 + 14a^4b^5c^5d^4 + 14a^5b^4c^4d^5 - 28a^6b^3c^3d^6 + 20a^7b^2c^2d^7 - 7a^8b^1c^1d^8)/(a^8d^8 + b^8c^8 + 28a^2b^6c^6d^2 - 56a^3b^5c^5d^3 + 70a^4b^4c^4d^4 - 56a^5b^3c^3d^5 + 28a^6b^2c^2d^6 - 8a^7b^1c^1d^7))/(a^8d^8 + b^8c^8 + 28a^2b^6c^6d^2 - 56a^3b^5c^5d^3 + 70a^4b^4c^4d^4 - 56a^5b^3c^3d^5 + 28a^6b^2c^2d^6 - 8a^7b^1c^1d^7))/(a^8d^8 + b^8c^8 + 28a^2b^6c^6d^2 - 56a^3b^5c^5d^3 + 70a^4b^4c^4d^4 - 56a^5b^3c^3d^5 + 28a^6b^2c^2d^6 - 8a^7b^1c^1d^7) + (2b^7d^2x^2(a^8d^8 + b^8c^8 + 28a^2b^6c^6d^2 - 56a^3b^5c^5d^3 + 70a^4b^4c^4d^4 - 56a^5b^3c^3d^5 + 28a^6b^2c^2d^6 - 8a^7b^1c^1d^7) + 4b^5x^5(107b^2c^2d^5 - a^2d^7 + 20a^8b^1c^1d^7) + (3(a^8d^8 + b^8c^8 + 28a^2b^6c^6d^2 - 56a^3b^5c^5d^3 + 70a^4b^4c^4d^4 - 56a^5b^3c^3d^5 + 28a^6b^2c^2d^6 - 8a^7b^1c^1d^7) + (2b^2x^2(2a^5d^7 + 669$

$$\begin{aligned} & *b^5*c^5*d^2 + 786*a*b^4*c^4*d^3 - 264*a^2*b^3*c^3*d^4 + 86*a^3*b^2*c^2*d^5 \\ & - 19*a^4*b*c*d^6)/(15*(a^8*d^8 + b^8*c^8 + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - \\ & 8*a*b^7*c^7*d - 8*a^7*b*c*d^7)) + (2*b^4*x^4*(a^3*d^7 + 319*b^3*c^3*d^4 + 1 \\ & 13*a*b^2*c^2*d^5 - 13*a^2*b*c*d^6))/(3*(a^8*d^8 + b^8*c^8 + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6 \\ & *b^2*c^2*d^6 - 8*a*b^7*c^7*d - 8*a^7*b*c*d^7)) + (2*b*x*(1089*b^6*c^6*d - 1 \\ & 0*a^6*d^7 + 2832*a*b^5*c^5*d^2 - 1578*a^2*b^4*c^4*d^3 + 872*a^3*b^3*c^3*d^4 - 353*a^4*b^2*c^2*d^5 + 88*a^5*b*c*d^6))/(105*(a^8*d^8 + b^8*c^8 + 28*a^2*b^6*c^6 \\ & *b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a*b^7*c^7*d - 8*a^7*b*c*d^7)) + (8*b^7*d^7*x^7)/(a \\ & ^8*d^8 + b^8*c^8 + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4 \\ & *d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a*b^7*c^7*d - 8*a^7*b*c*d^7) + (4*b^6*x^6*(a*d^7 + 13*b*c*d^6))/(a^8*d^8 + b^8*c^8 + 28*a^2*b^6*c^6 \\ & *d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a*b^7*c^7*d - 8*a^7*b*c*d^7) + (2*b^3*x^3*(1377*b^4*c^4*d \\ & ^3 - 3*a^4*d^7 + 872*a*b^3*c^3*d^4 - 178*a^2*b^2*c^2*d^5 + 32*a^3*b*c*d^6)) \\ & /(15*(a^8*d^8 + b^8*c^8 + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a*b^7*c^7*d - 8*a \\ & ^7*b*c*d^7)))/(x^7*(a*d^7 + 7*b*c*d^6) + x^3*(35*a*c^4*d^3 + 21*b*c^5*d^2) \\ & + x^5*(21*a*c^2*d^5 + 35*b*c^3*d^4) + x^4*(35*a*c^3*d^4 + 35*b*c^4*d^3) + a \\ & *c^7 + x*(b*c^7 + 7*a*c^6*d) + x^2*(21*a*c^5*d^2 + 7*b*c^6*d) + x^6*(21*b*c \\ & ^2*d^5 + 7*a*c*d^6) + b*d^7*x^8) \end{aligned}$$

sympy [B] time = 7.75, size = 2336, normalized size = 10.11

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2/(d*x+c)**8,x)

[Out]
$$\begin{aligned} & -8*b**7*d*log(x + (-8*a**10*b**7*d**11/(a*d - b*c)**9 + 80*a**9*b**8*c*d**1 \\ & 0/(a*d - b*c)**9 - 360*a**8*b**9*c**2*d**9/(a*d - b*c)**9 + 960*a**7*b**10* \\ & c**3*d**8/(a*d - b*c)**9 - 1680*a**6*b**11*c**4*d**7/(a*d - b*c)**9 + 2016* \\ & a**5*b**12*c**5*d**6/(a*d - b*c)**9 - 1680*a**4*b**13*c**6*d**5/(a*d - b*c) \\ & **9 + 960*a**3*b**14*c**7*d**4/(a*d - b*c)**9 - 360*a**2*b**15*c**8*d**3/(a \\ & *d - b*c)**9 + 80*a*b**16*c**9*d**2/(a*d - b*c)**9 + 8*a*b**7*d**2 - 8*b**1 \\ & 7*c**10*d/(a*d - b*c)**9 + 8*b**8*c*d)/(16*b**8*d**2))/(a*d - b*c)**9 + 8*b \\ & **7*d*log(x + (8*a**10*b**7*d**11/(a*d - b*c)**9 - 80*a**9*b**8*c*d**10/(a \\ & d - b*c)**9 + 360*a**8*b**9*c**2*d**9/(a*d - b*c)**9 - 960*a**7*b**10*c**3* \\ & d**8/(a*d - b*c)**9 + 1680*a**6*b**11*c**4*d**7/(a*d - b*c)**9 - 2016*a**5* \\ & b**12*c**5*d**6/(a*d - b*c)**9 + 1680*a**4*b**13*c**6*d**5/(a*d - b*c)**9 - \\ & 960*a**3*b**14*c**7*d**4/(a*d - b*c)**9 + 360*a**2*b**15*c**8*d**3/(a*d - \\ & b*c)**9 - 80*a*b**16*c**9*d**2/(a*d - b*c)**9 + 8*a*b**7*d**2 + 8*b**17*c** \\ & 10*d/(a*d - b*c)**9 + 8*b**8*c*d)/(16*b**8*d**2))/(a*d - b*c)**9 + (-15*a** \end{aligned}$$

$$\begin{aligned}
& 7*d^{**7} + 125*a^{**6}*b*c*d^{**6} - 463*a^{**5}*b^{**2}*c^{**2}*d^{**5} + 1007*a^{**4}*b^{**3}*c^{**3}* \\
& d^{**4} - 1443*a^{**3}*b^{**4}*c^{**4}*d^{**3} + 1497*a^{**2}*b^{**5}*c^{**5}*d^{**2} - 1443*a*b^{**6}*c* \\
& *6*d - 105*b^{**7}*c^{**7} - 840*b^{**7}*d^{**7}*x^{**7} + x^{**6}*(-420*a*b^{**6}*d^{**7} - 5460*b \\
& **7*c*d^{**6}) + x^{**5}*(140*a^{**2}*b^{**5}*d^{**7} - 2800*a*b^{**6}*c*d^{**6} - 14980*b^{**7}*c* \\
& *2*d^{**5}) + x^{**4}*(-70*a^{**3}*b^{**4}*d^{**7} + 910*a^{**2}*b^{**5}*c*d^{**6} - 7910*a*b^{**6}*c* \\
& *2*d^{**5} - 22330*b^{**7}*c^{**3}*d^{**4}) + x^{**3}*(42*a^{**4}*b^{**3}*d^{**7} - 448*a^{**3}*b^{**4}*c \\
& *d^{**6} + 2492*a^{**2}*b^{**5}*c^{**2}*d^{**5} - 12208*a*b^{**6}*c^{**3}*d^{**4} - 19278*b^{**7}*c^{**4} \\
& *d^{**3}) + x^{**2}*(-28*a^{**5}*b^{**2}*d^{**7} + 266*a^{**4}*b^{**3}*c*d^{**6} - 1204*a^{**3}*b^{**4}*c \\
& **2*d^{**5} + 3696*a^{**2}*b^{**5}*c^{**3}*d^{**4} - 11004*a*b^{**6}*c^{**4}*d^{**3} - 9366*b^{**7}*c* \\
& *5*d^{**2}) + x*(20*a^{**6}*b*d^{**7} - 176*a^{**5}*b^{**2}*c*d^{**6} + 706*a^{**4}*b^{**3}*c^{**2}*d* \\
& *5 - 1744*a^{**3}*b^{**4}*c^{**3}*d^{**4} + 3156*a^{**2}*b^{**5}*c^{**4}*d^{**3} - 5664*a*b^{**6}*c^{**5} \\
& *d^{**2} - 2178*b^{**7}*c^{**6}*d)/(105*a^{**9}*c^{**7}*d^{**8} - 840*a^{**8}*b*c^{**8}*d^{**7} + 294 \\
& 0*a^{**7}*b^{**2}*c^{**9}*d^{**6} - 5880*a^{**6}*b^{**3}*c^{**10}*d^{**5} + 7350*a^{**5}*b^{**4}*c^{**11}*d* \\
& *4 - 5880*a^{**4}*b^{**5}*c^{**12}*d^{**3} + 2940*a^{**3}*b^{**6}*c^{**13}*d^{**2} - 840*a^{**2}*b^{**7}* \\
& c^{**14}*d + 105*a*b^{**8}*c^{**15} + x^{**8}*(105*a^{**8}*b*d^{**15} - 840*a^{**7}*b^{**2}*c*d^{**14} \\
& + 2940*a^{**6}*b^{**3}*c^{**2}*d^{**13} - 5880*a^{**5}*b^{**4}*c^{**3}*d^{**12} + 7350*a^{**4}*b^{**5}*c \\
& **4*d^{**11} - 5880*a^{**3}*b^{**6}*c^{**5}*d^{**10} + 2940*a^{**2}*b^{**7}*c^{**6}*d^{**9} - 840*a*b* \\
& *8*c^{**7}*d^{**8} + 105*b^{**9}*c^{**8}*d^{**7}) + x^{**7}*(105*a^{**9}*d^{**15} - 105*a^{**8}*b*c*d* \\
& *14 - 2940*a^{**7}*b^{**2}*c^{**2}*d^{**13} + 14700*a^{**6}*b^{**3}*c^{**3}*d^{**12} - 33810*a^{**5}*b \\
& **4*c^{**4}*d^{**11} + 45570*a^{**4}*b^{**5}*c^{**5}*d^{**10} - 38220*a^{**3}*b^{**6}*c^{**6}*d^{**9} + 1 \\
& 9740*a^{**2}*b^{**7}*c^{**7}*d^{**8} - 5775*a*b^{**8}*c^{**8}*d^{**7} + 735*b^{**9}*c^{**9}*d^{**6}) + x* \\
& *6*(735*a^{**9}*c*d^{**14} - 3675*a^{**8}*b*c^{**2}*d^{**13} + 2940*a^{**7}*b^{**2}*c^{**3}*d^{**12} + \\
& 20580*a^{**6}*b^{**3}*c^{**4}*d^{**11} - 72030*a^{**5}*b^{**4}*c^{**5}*d^{**10} + 113190*a^{**4}*b^{**5} \\
& *c^{**6}*d^{**9} - 102900*a^{**3}*b^{**6}*c^{**7}*d^{**8} + 55860*a^{**2}*b^{**7}*c^{**8}*d^{**7} - 16905 \\
& *a*b^{**8}*c^{**9}*d^{**6} + 2205*b^{**9}*c^{**10}*d^{**5}) + x^{**5}*(2205*a^{**9}*c^{**2}*d^{**13} - 13 \\
& 965*a^{**8}*b*c^{**3}*d^{**12} + 32340*a^{**7}*b^{**2}*c^{**4}*d^{**11} - 20580*a^{**6}*b^{**3}*c^{**5}*d \\
& **10 - 51450*a^{**5}*b^{**4}*c^{**6}*d^{**9} + 133770*a^{**4}*b^{**5}*c^{**7}*d^{**8} - 144060*a^{**3} \\
& *b^{**6}*c^{**8}*d^{**7} + 85260*a^{**2}*b^{**7}*c^{**9}*d^{**6} - 27195*a*b^{**8}*c^{**10}*d^{**5} + 367 \\
& 5*b^{**9}*c^{**11}*d^{**4}) + x^{**4}*(3675*a^{**9}*c^{**3}*d^{**12} - 25725*a^{**8}*b*c^{**4}*d^{**11} + \\
& 73500*a^{**7}*b^{**2}*c^{**5}*d^{**10} - 102900*a^{**6}*b^{**3}*c^{**6}*d^{**9} + 51450*a^{**5}*b^{**4}* \\
& c^{**7}*d^{**8} + 51450*a^{**4}*b^{**5}*c^{**8}*d^{**7} - 102900*a^{**3}*b^{**6}*c^{**9}*d^{**6} + 73500* \\
& a^{**2}*b^{**7}*c^{**10}*d^{**5} - 25725*a*b^{**8}*c^{**11}*d^{**4} + 3675*b^{**9}*c^{**12}*d^{**3}) + x* \\
& *3*(3675*a^{**9}*c^{**4}*d^{**11} - 27195*a^{**8}*b*c^{**5}*d^{**10} + 85260*a^{**7}*b^{**2}*c^{**6}*d \\
& **9 - 144060*a^{**6}*b^{**3}*c^{**7}*d^{**8} + 133770*a^{**5}*b^{**4}*c^{**8}*d^{**7} - 51450*a^{**4}* \\
& b^{**5}*c^{**9}*d^{**6} - 20580*a^{**3}*b^{**6}*c^{**10}*d^{**5} + 32340*a^{**2}*b^{**7}*c^{**11}*d^{**4} - \\
& 13965*a*b^{**8}*c^{**12}*d^{**3} + 2205*b^{**9}*c^{**13}*d^{**2}) + x^{**2}*(2205*a^{**9}*c^{**5}*d^{**1} \\
& 0 - 16905*a^{**8}*b*c^{**6}*d^{**9} + 55860*a^{**7}*b^{**2}*c^{**7}*d^{**8} - 102900*a^{**6}*b^{**3}*c \\
& **8*d^{**7} + 113190*a^{**5}*b^{**4}*c^{**9}*d^{**6} - 72030*a^{**4}*b^{**5}*c^{**10}*d^{**5} + 20580* \\
& a^{**3}*b^{**6}*c^{**11}*d^{**4} + 2940*a^{**2}*b^{**7}*c^{**12}*d^{**3} - 3675*a*b^{**8}*c^{**13}*d^{**2} + \\
& 735*b^{**9}*c^{**14}*d) + x*(735*a^{**9}*c^{**6}*d^{**9} - 5775*a^{**8}*b*c^{**7}*d^{**8} + 19740* \\
& a^{**7}*b^{**2}*c^{**8}*d^{**7} - 38220*a^{**6}*b^{**3}*c^{**9}*d^{**6} + 45570*a^{**5}*b^{**4}*c^{**10}*d* \\
& 5 - 33810*a^{**4}*b^{**5}*c^{**11}*d^{**4} + 14700*a^{**3}*b^{**6}*c^{**12}*d^{**3} - 2940*a^{**2}*b^{**7} \\
& *c^{**13}*d^{**2} - 105*a*b^{**8}*c^{**14}*d + 105*b^{**9}*c^{**15})
\end{aligned}$$

$$3.1374 \quad \int \frac{1}{(a+bx)^3(c+dx)^8} dx$$

Optimal. Leaf size=276

$$\frac{36b^7d^2 \log(a+bx)}{(bc-ad)^{10}} - \frac{36b^7d^2 \log(c+dx)}{(bc-ad)^{10}} + \frac{8b^7d}{(a+bx)(bc-ad)^9} - \frac{b^7}{2(a+bx)^2(bc-ad)^8} + \frac{28b^6d^2}{(c+dx)(bc-ad)^9} + \frac{1}{2(c+dx)^2}$$

[Out] $-1/2*b^7/(-a*d+b*c)^8/(b*x+a)^2+8*b^7*d/(-a*d+b*c)^9/(b*x+a)+1/7*d^2/(-a*d+b*c)^3/(d*x+c)^7+1/2*b*d^2/(-a*d+b*c)^4/(d*x+c)^6+6/5*b^2*d^2/(-a*d+b*c)^5/(d*x+c)^5+5/2*b^3*d^2/(-a*d+b*c)^6/(d*x+c)^4+5*b^4*d^2/(-a*d+b*c)^7/(d*x+c)^3+21/2*b^5*d^2/(-a*d+b*c)^8/(d*x+c)^2+28*b^6*d^2/(-a*d+b*c)^9/(d*x+c)+36*b^7*d^2*\ln(b*x+a)/(-a*d+b*c)^{10}-36*b^7*d^2*\ln(d*x+c)/(-a*d+b*c)^{10}$

Rubi [A] time = 0.36, antiderivative size = 276, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {44}

$$\frac{28b^6d^2}{(c+dx)(bc-ad)^9} + \frac{21b^5d^2}{2(c+dx)^2(bc-ad)^8} + \frac{5b^4d^2}{(c+dx)^3(bc-ad)^7} + \frac{5b^3d^2}{2(c+dx)^4(bc-ad)^6} + \frac{6b^2d^2}{5(c+dx)^5(bc-ad)^5} + \frac{36b^7d^2 \log(a+bx)}{(bc-ad)^{10}} - \frac{36b^7d^2 \log(c+dx)}{(bc-ad)^{10}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^3*(c + d*x)^8), x]

[Out] $-b^7/(2*(b*c - a*d)^8*(a + b*x)^2) + (8*b^7*d)/((b*c - a*d)^9*(a + b*x)) + d^2/(7*(b*c - a*d)^3*(c + d*x)^7) + (b*d^2)/(2*(b*c - a*d)^4*(c + d*x)^6) + (6*b^2*d^2)/(5*(b*c - a*d)^5*(c + d*x)^5) + (5*b^3*d^2)/(2*(b*c - a*d)^6*(c + d*x)^4) + (5*b^4*d^2)/((b*c - a*d)^7*(c + d*x)^3) + (21*b^5*d^2)/(2*(b*c - a*d)^8*(c + d*x)^2) + (28*b^6*d^2)/((b*c - a*d)^9*(c + d*x)) + (36*b^7*d^2*\text{Log}[a + b*x])/(b*c - a*d)^{10} - (36*b^7*d^2*\text{Log}[c + d*x])/(b*c - a*d)^{10}$

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{1}{(a+bx)^3(c+dx)^8} dx = \int \left(\frac{b^8}{(bc-ad)^8(a+bx)^3} - \frac{8b^8d}{(bc-ad)^9(a+bx)^2} + \frac{36b^8d^2}{(bc-ad)^{10}(a+bx)} - \frac{d^3}{(bc-ad)^3(c+dx)^2} \right) dx$$

$$= -\frac{b^7}{2(bc-ad)^8(a+bx)^2} + \frac{8b^7d}{(bc-ad)^9(a+bx)} + \frac{d^2}{7(bc-ad)^3(c+dx)^7} + \frac{bd^2}{2(bc-ad)^4(c+dx)^2}$$

$$\begin{aligned}
& *b^9*c*d^8 + 2*a*b^8*d^9)*x^8 + (21*b^9*c^2*d^7 + 14*a*b^8*c*d^8 + a^2*b^7*d^9)*x^7 + 7*(5*b^9*c^3*d^6 + 6*a*b^8*c^2*d^7 + a^2*b^7*c*d^8)*x^6 + 7*(5*b^9*c^4*d^5 + 10*a*b^8*c^3*d^6 + 3*a^2*b^7*c^2*d^7)*x^5 + 7*(3*b^9*c^5*d^4 + 10*a*b^8*c^4*d^5 + 5*a^2*b^7*c^3*d^6)*x^4 + 7*(b^9*c^6*d^3 + 6*a*b^8*c^5*d^4 + 5*a^2*b^7*c^4*d^5)*x^3 + (b^9*c^7*d^2 + 14*a*b^8*c^6*d^3 + 21*a^2*b^7*c^5*d^4)*x^2 + (2*a*b^8*c^7*d^2 + 7*a^2*b^7*c^6*d^3)*x)*\log(d*x + c))/(a^2*b^10*c^17 - 10*a^3*b^9*c^16*d + 45*a^4*b^8*c^15*d^2 - 120*a^5*b^7*c^14*d^3 + 210*a^6*b^6*c^13*d^4 - 252*a^7*b^5*c^12*d^5 + 210*a^8*b^4*c^11*d^6 - 120*a^9*b^3*c^10*d^7 + 45*a^10*b^2*c^9*d^8 - 10*a^11*b*c^8*d^9 + a^12*c^7*d^10 + (b^12*c^10*d^7 - 10*a*b^11*c^9*d^8 + 45*a^2*b^10*c^8*d^9 - 120*a^3*b^9*c^7*d^10 + 210*a^4*b^8*c^6*d^11 - 252*a^5*b^7*c^5*d^12 + 210*a^6*b^6*c^4*d^13 - 120*a^7*b^5*c^3*d^14 + 45*a^8*b^4*c^2*d^15 - 10*a^9*b^3*c*d^16 + a^10*b^2*d^17)*x^9 + (7*b^12*c^11*d^6 - 68*a*b^11*c^10*d^7 + 295*a^2*b^10*c^9*d^8 - 750*a^3*b^9*c^8*d^9 + 1230*a^4*b^8*c^7*d^10 - 1344*a^5*b^7*c^6*d^11 + 966*a^6*b^6*c^5*d^12 - 420*a^7*b^5*c^4*d^13 + 75*a^8*b^4*c^3*d^14 + 20*a^9*b^3*c^2*d^15 - 13*a^10*b^2*c*d^16 + 2*a^11*b*d^17)*x^8 + (21*b^12*c^12*d^5 - 196*a*b^11*c^11*d^6 + 806*a^2*b^10*c^10*d^7 - 1900*a^3*b^9*c^9*d^8 + 2775*a^4*b^8*c^8*d^9 - 2472*a^5*b^7*c^7*d^10 + 1092*a^6*b^6*c^6*d^11 + 168*a^7*b^5*c^5*d^12 - 525*a^8*b^4*c^4*d^13 + 300*a^9*b^3*c^3*d^14 - 74*a^10*b^2*c^2*d^15 + 4*a^11*b*c*d^16 + a^12*d^17)*x^7 + 7*(5*b^12*c^13*d^4 - 44*a*b^11*c^12*d^5 + 166*a^2*b^10*c^11*d^6 - 340*a^3*b^9*c^10*d^7 + 375*a^4*b^8*c^9*d^8 - 120*a^5*b^7*c^8*d^9 - 252*a^6*b^6*c^7*d^10 + 408*a^7*b^5*c^6*d^11 - 285*a^8*b^4*c^5*d^12 + 100*a^9*b^3*c^4*d^13 - 10*a^10*b^2*c^3*d^14 - 4*a^11*b*c^2*d^15 + a^12*c*d^16)*x^6 + 7*(5*b^12*c^14*d^3 - 40*a*b^11*c^13*d^4 + 128*a^2*b^10*c^12*d^5 - 180*a^3*b^9*c^11*d^6 - 15*a^4*b^8*c^10*d^7 + 480*a^5*b^7*c^9*d^8 - 840*a^6*b^6*c^8*d^9 + 744*a^7*b^5*c^7*d^10 - 345*a^8*b^4*c^6*d^11 + 40*a^9*b^3*c^5*d^12 + 40*a^10*b^2*c^4*d^13 - 20*a^11*b*c^3*d^14 + 3*a^12*c^2*d^15)*x^5 + 7*(3*b^12*c^15*d^2 - 20*a*b^11*c^14*d^3 + 40*a^2*b^10*c^13*d^4 + 40*a^3*b^9*c^12*d^5 - 345*a^4*b^8*c^11*d^6 + 744*a^5*b^7*c^10*d^7 - 840*a^6*b^6*c^9*d^8 + 480*a^7*b^5*c^8*d^9 - 15*a^8*b^4*c^7*d^10 - 180*a^9*b^3*c^6*d^11 + 128*a^10*b^2*c^5*d^12 - 40*a^11*b*c^4*d^13 + 5*a^12*c^3*d^14)*x^4 + 7*(b^12*c^16*d - 4*a*b^11*c^15*d^2 - 10*a^2*b^10*c^14*d^3 + 100*a^3*b^9*c^13*d^4 - 285*a^4*b^8*c^12*d^5 + 408*a^5*b^7*c^11*d^6 - 252*a^6*b^6*c^10*d^7 - 120*a^7*b^5*c^9*d^8 + 375*a^8*b^4*c^8*d^9 - 340*a^9*b^3*c^7*d^10 + 166*a^10*b^2*c^6*d^11 - 44*a^11*b*c^5*d^12 + 5*a^12*c^4*d^13)*x^3 + (b^12*c^17 + 4*a*b^11*c^16*d - 74*a^2*b^10*c^15*d^2 + 300*a^3*b^9*c^14*d^3 - 525*a^4*b^8*c^13*d^4 + 168*a^5*b^7*c^12*d^5 + 1092*a^6*b^6*c^11*d^6 - 2472*a^7*b^5*c^10*d^7 + 2775*a^8*b^4*c^9*d^8 - 1900*a^9*b^3*c^8*d^9 + 806*a^10*b^2*c^7*d^10 - 196*a^11*b*c^6*d^11 + 21*a^12*c^5*d^12)*x^2 + (2*a*b^11*c^17 - 13*a^2*b^10*c^16*d + 20*a^3*b^9*c^15*d^2 + 75*a^4*b^8*c^14*d^3 - 420*a^5*b^7*c^13*d^4 + 966*a^6*b^6*c^12*d^5 - 1344*a^7*b^5*c^11*d^6 + 1230*a^8*b^4*c^10*d^7 - 750*a^9*b^3*c^9*d^8 + 295*a^10*b^2*c^8*d^9 - 68*a^11*b*c^7*d^10 + 7*a^12*c^6*d^11)*x)
\end{aligned}$$

giac [B] time = 1.49, size = 1029, normalized size = 3.73

$$\frac{36 b^8 d^2 \log(|bx + a|)}{b^{11} c^{10} - 10 a b^{10} c^9 d + 45 a^2 b^9 c^8 d^2 - 120 a^3 b^8 c^7 d^3 + 210 a^4 b^7 c^6 d^4 - 252 a^5 b^6 c^5 d^5 + 210 a^6 b^5 c^4 d^6 - 120 a^7 b^4 c^3 d^7 + \dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^8,x, algorithm="giac")

[Out] $36*b^8*d^2*\log(\text{abs}(b*x + a))/(b^{11}*c^{10} - 10*a*b^{10}*c^9*d + 45*a^2*b^9*c^8*d^2 - 120*a^3*b^8*c^7*d^3 + 210*a^4*b^7*c^6*d^4 - 252*a^5*b^6*c^5*d^5 + 210*a^6*b^5*c^4*d^6 - 120*a^7*b^4*c^3*d^7 + 45*a^8*b^3*c^2*d^8 - 10*a^9*b^2*c*d^9 + a^{10}*b*d^{10}) - 36*b^7*d^3*\log(\text{abs}(d*x + c))/(b^{10}*c^{10}*d - 10*a*b^9*c^9*d^2 + 45*a^2*b^8*c^8*d^3 - 120*a^3*b^7*c^7*d^4 + 210*a^4*b^6*c^6*d^5 - 252*a^5*b^5*c^5*d^6 + 210*a^6*b^4*c^4*d^7 - 120*a^7*b^3*c^3*d^8 + 45*a^8*b^2*c^2*d^9 - 10*a^9*b*c*d^{10} + a^{10}*d^{11}) - 1/70*(35*b^9*c^9 - 630*a*b^8*c^8*d - 2754*a^2*b^7*c^7*d^2 + 5880*a^3*b^6*c^6*d^3 - 4410*a^4*b^5*c^5*d^4 + 2940*a^5*b^4*c^4*d^5 - 1470*a^6*b^3*c^3*d^6 + 504*a^7*b^2*c^2*d^7 - 105*a^8*b*c*d^8 + 10*a^9*d^9 - 2520*(b^9*c*d^8 - a*b^8*d^9)*x^8 - 1260*(13*b^9*c^2*d^7 - 10*a*b^8*c*d^8 - 3*a^2*b^7*d^9)*x^7 - 420*(107*b^9*c^3*d^6 - 48*a*b^8*c^2*d^7 - 57*a^2*b^7*c*d^8 - 2*a^3*b^6*d^9)*x^6 - 210*(319*b^9*c^4*d^5 + 8*a*b^8*c^3*d^6 - 300*a^2*b^7*c^2*d^7 - 28*a^3*b^6*c*d^8 + a^4*b^5*d^9)*x^5 - 42*(1377*b^9*c^5*d^4 + 1090*a*b^8*c^4*d^5 - 2080*a^2*b^7*c^3*d^6 - 420*a^3*b^6*c^2*d^7 + 35*a^4*b^5*c*d^8 - 2*a^5*b^4*d^9)*x^4 - 42*(669*b^9*c^6*d^3 + 1494*a*b^8*c^5*d^4 - 1555*a^2*b^7*c^4*d^5 - 700*a^3*b^6*c^3*d^6 + 105*a^4*b^5*c^2*d^7 - 14*a^5*b^4*c*d^8 + a^6*b^3*d^9)*x^3 - 6*(1089*b^9*c^7*d^2 + 6426*a*b^8*c^6*d^3 - 3591*a^2*b^7*c^5*d^4 - 4900*a^3*b^6*c^4*d^5 + 1225*a^4*b^5*c^3*d^6 - 294*a^5*b^4*c^2*d^7 + 49*a^6*b^3*c*d^8 - 4*a^7*b^2*d^9)*x^2 - 3*(105*b^9*c^8*d + 3516*a*b^8*c^7*d^2 + 546*a^2*b^7*c^6*d^3 - 5880*a^3*b^6*c^5*d^4 + 2450*a^4*b^5*c^4*d^5 - 980*a^5*b^4*c^3*d^6 + 294*a^6*b^3*c^2*d^7 - 56*a^7*b^2*c*d^8 + 5*a^8*b*d^9)*x)/((b*c - a*d)^{10}*(b*x + a)^2*(d*x + c)^7)$

maple [A] time = 0.02, size = 265, normalized size = 0.96

$$\frac{36b^7d^2 \ln(bx + a)}{(ad - bc)^{10}} - \frac{36b^7d^2 \ln(dx + c)}{(ad - bc)^{10}} - \frac{8b^7d}{(ad - bc)^9 (bx + a)} - \frac{28b^6d^2}{(ad - bc)^9 (dx + c)} - \frac{b^7}{2(ad - bc)^8 (bx + a)^2} + \frac{21}{2(ad - bc)^8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^3/(d*x+c)^8,x)

[Out] $-1/7*d^2/(a*d-b*c)^3/(d*x+c)^7-36*d^2/(a*d-b*c)^{10}*b^7*\ln(d*x+c)-28*d^2/(a*d-b*c)^9*b^6/(d*x+c)+21/2*d^2/(a*d-b*c)^8*b^5/(d*x+c)^2-5*d^2/(a*d-b*c)^7*b^4/(d*x+c)^3+5/2*d^2/(a*d-b*c)^6*b^3/(d*x+c)^4-6/5*d^2/(a*d-b*c)^5*b^2/(d*x+c)^5$

$$+c)^5 + 1/2*d^2/(a*d-b*c)^4*b/(d*x+c)^6 - 1/2*b^7/(a*d-b*c)^8/(b*x+a)^2 + 36*d^2/(a*d-b*c)^{10}*b^7*\ln(b*x+a) - 8*b^7/(a*d-b*c)^9*d/(b*x+a)$$

maxima [B] time = 5.22, size = 2399, normalized size = 8.69

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^8,x, algorithm="maxima")

[Out] $36*b^7*d^2*\log(b*x + a)/(b^{10}*c^{10} - 10*a*b^9*c^9*d + 45*a^2*b^8*c^8*d^2 - 120*a^3*b^7*c^7*d^3 + 210*a^4*b^6*c^6*d^4 - 252*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 - 120*a^7*b^3*c^3*d^7 + 45*a^8*b^2*c^2*d^8 - 10*a^9*b*c*d^9 + a^{10}*d^{10}) - 36*b^7*d^2*\log(d*x + c)/(b^{10}*c^{10} - 10*a*b^9*c^9*d + 45*a^2*b^8*c^8*d^2 - 120*a^3*b^7*c^7*d^3 + 210*a^4*b^6*c^6*d^4 - 252*a^5*b^5*c^5*d^5 + 210*a^6*b^4*c^4*d^6 - 120*a^7*b^3*c^3*d^7 + 45*a^8*b^2*c^2*d^8 - 10*a^9*b*c*d^9 + a^{10}*d^{10}) + 1/70*(2520*b^8*d^8*x^8 - 35*b^8*c^8 + 595*a*b^7*c^7*d + 3349*a^2*b^6*c^6*d^2 - 2531*a^3*b^5*c^5*d^3 + 1879*a^4*b^4*c^4*d^4 - 1061*a^5*b^3*c^3*d^5 + 409*a^6*b^2*c^2*d^6 - 95*a^7*b*c*d^7 + 10*a^8*d^8 + 1260*(13*b^8*c*d^7 + 3*a*b^7*d^8)*x^7 + 420*(107*b^8*c^2*d^6 + 59*a*b^7*c*d^7 + 2*a^2*b^6*d^8)*x^6 + 210*(319*b^8*c^3*d^5 + 327*a*b^7*c^2*d^6 + 27*a^2*b^6*c*d^7 - a^3*b^5*d^8)*x^5 + 42*(1377*b^8*c^4*d^4 + 2467*a*b^7*c^3*d^5 + 387*a^2*b^6*c^2*d^6 - 33*a^3*b^5*c*d^7 + 2*a^4*b^4*d^8)*x^4 + 42*(669*b^8*c^5*d^3 + 2163*a*b^7*c^4*d^4 + 608*a^2*b^6*c^3*d^5 - 92*a^3*b^5*c^2*d^6 + 13*a^4*b^4*c*d^7 - a^5*b^3*d^8)*x^3 + 6*(1089*b^8*c^6*d^2 + 7515*a*b^7*c^5*d^3 + 3924*a^2*b^6*c^4*d^4 - 976*a^3*b^5*c^3*d^5 + 249*a^4*b^4*c^2*d^6 - 45*a^5*b^3*c*d^7 + 4*a^6*b^2*d^8)*x^2 + 3*(105*b^8*c^7*d + 3621*a*b^7*c^6*d^2 + 4167*a^2*b^6*c^5*d^3 - 1713*a^3*b^5*c^4*d^4 + 737*a^4*b^4*c^3*d^5 - 243*a^5*b^3*c^2*d^6 + 51*a^6*b^2*c*d^7 - 5*a^7*b*d^8)*x)/(a^2*b^9*c^16 - 9*a^3*b^8*c^15*d + 36*a^4*b^7*c^14*d^2 - 84*a^5*b^6*c^13*d^3 + 126*a^6*b^5*c^12*d^4 - 126*a^7*b^4*c^11*d^5 + 84*a^8*b^3*c^10*d^6 - 36*a^9*b^2*c^9*d^7 + 9*a^10*b*c^8*d^8 - a^{11}*c^7*d^9 + (b^{11}*c^9*d^7 - 9*a*b^{10}*c^8*d^8 + 36*a^2*b^9*c^7*d^9 - 84*a^3*b^8*c^6*d^10 + 126*a^4*b^7*c^5*d^11 - 126*a^5*b^6*c^4*d^12 + 84*a^6*b^5*c^3*d^13 - 36*a^7*b^4*c^2*d^14 + 9*a^8*b^3*c*d^15 - a^9*b^2*d^16)*x^9 + (7*b^{11}*c^10*d^6 - 61*a*b^{10}*c^9*d^7 + 234*a^2*b^9*c^8*d^8 - 516*a^3*b^8*c^7*d^9 + 714*a^4*b^7*c^6*d^10 - 630*a^5*b^6*c^5*d^11 + 336*a^6*b^5*c^4*d^12 - 84*a^7*b^4*c^3*d^13 - 9*a^8*b^3*c^2*d^14 + 11*a^9*b^2*c*d^15 - 2*a^{10}*b*d^16)*x^8 + (21*b^{11}*c^11*d^5 - 175*a*b^{10}*c^10*d^6 + 631*a^2*b^9*c^9*d^7 - 1269*a^3*b^8*c^8*d^8 + 1506*a^4*b^7*c^7*d^9 - 966*a^5*b^6*c^6*d^10 + 126*a^6*b^5*c^5*d^11 + 294*a^7*b^4*c^4*d^12 - 231*a^8*b^3*c^3*d^13 + 69*a^9*b^2*c^2*d^14 - 5*a^{10}*b*c*d^15 - a^{11}*d^16)*x^7 + 7*(5*b^{11}*c^12*d^4 - 39*a*b^{10}*c^11*d^5 + 127*a^2*b^9*c^10*d^6 - 213*a^3*b^8*c^9*d^7 + 162*a^4*b^7*c^8*d^8 + 42*a^5*b^6*c^7*d^9 - 210*a^6*b^5*c^6*d^10 + 198*a^7*b^4*c^5*d^11 - 87*a^8*b^3*c^4*d^12 + 13*a^9*b^2*c^3*d^13 + 3*a^{10}*b*c^2*d^14 - a^{11}*c*d^15)*x^6 + 7*(5*b^{11}*c^13*d^3 - 35*a*b^{10}*c^12*d^4 + 93*a^2*b^9*c^11*d^5 -$

$$\begin{aligned}
& 87*a^3*b^8*c^{10}*d^6 - 102*a^4*b^7*c^9*d^7 + 378*a^5*b^6*c^8*d^8 - 462*a^6* \\
& b^5*c^7*d^9 + 282*a^7*b^4*c^6*d^{10} - 63*a^8*b^3*c^5*d^{11} - 23*a^9*b^2*c^4*d \\
& ^{12} + 17*a^{10}*b*c^3*d^{13} - 3*a^{11}*c^2*d^{14}) * x^5 + 7*(3*b^{11}*c^{14}*d^2 - 17*a \\
& *b^{10}*c^{13}*d^3 + 23*a^2*b^9*c^{12}*d^4 + 63*a^3*b^8*c^{11}*d^5 - 282*a^4*b^7*c^ \\
& ^{10}*d^6 + 462*a^5*b^6*c^9*d^7 - 378*a^6*b^5*c^8*d^8 + 102*a^7*b^4*c^7*d^9 + \\
& 87*a^8*b^3*c^6*d^{10} - 93*a^9*b^2*c^5*d^{11} + 35*a^{10}*b*c^4*d^{12} - 5*a^{11}*c^3 \\
& *d^{13}) * x^4 + 7*(b^{11}*c^{15}*d - 3*a*b^{10}*c^{14}*d^2 - 13*a^2*b^9*c^{13}*d^3 + 87* \\
& a^3*b^8*c^{12}*d^4 - 198*a^4*b^7*c^{11}*d^5 + 210*a^5*b^6*c^{10}*d^6 - 42*a^6*b^5 \\
& *c^9*d^7 - 162*a^7*b^4*c^8*d^8 + 213*a^8*b^3*c^7*d^9 - 127*a^9*b^2*c^6*d^{10} \\
& + 39*a^{10}*b*c^5*d^{11} - 5*a^{11}*c^4*d^{12}) * x^3 + (b^{11}*c^{16} + 5*a*b^{10}*c^{15}*d \\
& - 69*a^2*b^9*c^{14}*d^2 + 231*a^3*b^8*c^{13}*d^3 - 294*a^4*b^7*c^{12}*d^4 - 126* \\
& a^5*b^6*c^{11}*d^5 + 966*a^6*b^5*c^{10}*d^6 - 1506*a^7*b^4*c^9*d^7 + 1269*a^8*b \\
& ^3*c^8*d^8 - 631*a^9*b^2*c^7*d^9 + 175*a^{10}*b*c^6*d^{10} - 21*a^{11}*c^5*d^{11}) * \\
& x^2 + (2*a*b^{10}*c^{16} - 11*a^2*b^9*c^{15}*d + 9*a^3*b^8*c^{14}*d^2 + 84*a^4*b^7* \\
& c^{13}*d^3 - 336*a^5*b^6*c^{12}*d^4 + 630*a^6*b^5*c^{11}*d^5 - 714*a^7*b^4*c^{10}*d \\
& ^6 + 516*a^8*b^3*c^9*d^7 - 234*a^9*b^2*c^8*d^8 + 61*a^{10}*b*c^7*d^9 - 7*a^{11} \\
& *c^6*d^{10}) * x)
\end{aligned}$$

mupad [B] time = 1.91, size = 2224, normalized size = 8.06

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/((a + b*x)^3*(c + d*x)^8), x)$

[Out] $(72*b^7*d^2*\text{atanh}((a^{10}*d^{10} - b^{10}*c^{10} - 27*a^2*b^8*c^8*d^2 + 48*a^3*b^7*c^7*d^3 - 42*a^4*b^6*c^6*d^4 + 42*a^6*b^4*c^4*d^6 - 48*a^7*b^3*c^3*d^7 + 27*a^8*b^2*c^2*d^8 + 8*a*b^9*c^9*d - 8*a^9*b*c*d^9)/(a*d - b*c)^{10} + (2*b*d*x*(a^9*d^9 - b^9*c^9 - 36*a^2*b^7*c^7*d^2 + 84*a^3*b^6*c^6*d^3 - 126*a^4*b^5*c^5*d^4 + 126*a^5*b^4*c^4*d^5 - 84*a^6*b^3*c^3*d^6 + 36*a^7*b^2*c^2*d^7 + 9*a*b^8*c^8*d - 9*a^8*b*c*d^8))/(a*d - b*c)^{10} - ((10*a^8*d^8 - 35*b^8*c^8 + 3349*a^2*b^6*c^6*d^2 - 2531*a^3*b^5*c^5*d^3 + 1879*a^4*b^4*c^4*d^4 - 1061*a^5*b^3*c^3*d^5 + 409*a^6*b^2*c^2*d^6 + 595*a*b^7*c^7*d - 95*a^7*b*c*d^7)/(70*(a^9*d^9 - b^9*c^9 - 36*a^2*b^7*c^7*d^2 + 84*a^3*b^6*c^6*d^3 - 126*a^4*b^5*c^5*d^4 + 126*a^5*b^4*c^4*d^5 - 84*a^6*b^3*c^3*d^6 + 36*a^7*b^2*c^2*d^7 + 9*a*b^8*c^8*d - 9*a^8*b*c*d^8)) + (3*b^2*x^2*(4*a^6*d^8 + 1089*b^6*c^6*d^2 + 7515*a*b^5*c^5*d^3 + 3924*a^2*b^4*c^4*d^4 - 976*a^3*b^3*c^3*d^5 + 249*a^4*b^2*c^2*d^6 - 45*a^5*b*c*d^7))/(35*(a^9*d^9 - b^9*c^9 - 36*a^2*b^7*c^7*d^2 + 84*a^3*b^6*c^6*d^3 - 126*a^4*b^5*c^5*d^4 + 126*a^5*b^4*c^4*d^5 - 84*a^6*b^3*c^3*d^6 + 36*a^7*b^2*c^2*d^7 + 9*a*b^8*c^8*d - 9*a^8*b*c*d^8)) + (3*b^4*x^4*(2*a^4*d^8 + 1377*b^4*c^4*d^4 + 2467*a*b^3*c^3*d^5 + 387*a^2*b^2*c^2*d^6 - 33*a^3*b*c*d^7))/(5*(a^9*d^9 - b^9*c^9 - 36*a^2*b^7*c^7*d^2 + 84*a^3*b^6*c^6*d^3 - 126*a^4*b^5*c^5*d^4 + 126*a^5*b^4*c^4*d^5 - 84*a^6*b^3*c^3*d^6 + 36*a^7*b^2*c^2*d^7 + 9*a*b^8*c^8*d - 9*a^8*b*c*d^8)) + (3*b*x*(105*b^7*c^7*d - 5*a^7*d^8 + 3621*a*b^6*c^6*d^2 + 4167*a^2*b^5*c^$

$$\begin{aligned}
& 5*d^3 - 1713*a^3*b^4*c^4*d^4 + 737*a^4*b^3*c^3*d^5 - 243*a^5*b^2*c^2*d^6 + \\
& 51*a^6*b*c*d^7)/(70*(a^9*d^9 - b^9*c^9 - 36*a^2*b^7*c^7*d^2 + 84*a^3*b^6*c^6*d^3 - 126*a^4*b^5*c^5*d^4 + 126*a^5*b^4*c^4*d^5 - 84*a^6*b^3*c^3*d^6 + 3 \\
& 6*a^7*b^2*c^2*d^7 + 9*a*b^8*c^8*d - 9*a^8*b*c*d^8)) + (6*b^6*x^6*(2*a^2*d^8 \\
& + 107*b^2*c^2*d^6 + 59*a*b*c*d^7))/(a^9*d^9 - b^9*c^9 - 36*a^2*b^7*c^7*d^2 \\
& + 84*a^3*b^6*c^6*d^3 - 126*a^4*b^5*c^5*d^4 + 126*a^5*b^4*c^4*d^5 - 84*a^6* \\
& b^3*c^3*d^6 + 36*a^7*b^2*c^2*d^7 + 9*a*b^8*c^8*d - 9*a^8*b*c*d^8) + (3*b^3*x^3*(669*b^5*c^5*d^3 - a^5*d^8 + 2163*a*b^4*c^4*d^4 + 608*a^2*b^3*c^3*d^5 - \\
& 92*a^3*b^2*c^2*d^6 + 13*a^4*b*c*d^7))/(5*(a^9*d^9 - b^9*c^9 - 36*a^2*b^7*c^7*d^2 + 84*a^3*b^6*c^6*d^3 - 126*a^4*b^5*c^5*d^4 + 126*a^5*b^4*c^4*d^5 - 8 \\
& 4*a^6*b^3*c^3*d^6 + 36*a^7*b^2*c^2*d^7 + 9*a*b^8*c^8*d - 9*a^8*b*c*d^8)) + \\
& (3*b^5*x^5*(319*b^3*c^3*d^5 - a^3*d^8 + 327*a*b^2*c^2*d^6 + 27*a^2*b*c*d^7) \\
&)/(a^9*d^9 - b^9*c^9 - 36*a^2*b^7*c^7*d^2 + 84*a^3*b^6*c^6*d^3 - 126*a^4*b^5*c^5*d^4 + 126*a^5*b^4*c^4*d^5 - 84*a^6*b^3*c^3*d^6 + 36*a^7*b^2*c^2*d^7 + \\
& 9*a*b^8*c^8*d - 9*a^8*b*c*d^8) + (36*b^8*d^8*x^8)/(a^9*d^9 - b^9*c^9 - 36* \\
& a^2*b^7*c^7*d^2 + 84*a^3*b^6*c^6*d^3 - 126*a^4*b^5*c^5*d^4 + 126*a^5*b^4*c^4*d^5 - 84*a^6*b^3*c^3*d^6 + 36*a^7*b^2*c^2*d^7 + 9*a*b^8*c^8*d - 9*a^8*b*c \\
& *d^8) + (18*b^6*d*x^7*(13*b^2*c^2*d^6 + 3*a*b*d^7))/(a^9*d^9 - b^9*c^9 - 36*a^2*b^7*c^7*d^2 + 84*a^3*b^6*c^6*d^3 - 126*a^4*b^5*c^5*d^4 + 126*a^5*b^4*c^4 \\
& *d^5 - 84*a^6*b^3*c^3*d^6 + 36*a^7*b^2*c^2*d^7 + 9*a*b^8*c^8*d - 9*a^8*b*c*d^8)))/(x^3*(7*b^2*c^6*d + 35*a^2*c^4*d^3 + 42*a*b*c^5*d^2) + x^6*(7*a^2*c^6*d^6 + 35*b^2*c^3*d^4 + 42*a*b*c^2*d^5) + x*(7*a^2*c^6*d + 2*a*b*c^7) + x^2*(\\
& b^2*c^7 + 21*a^2*c^5*d^2 + 14*a*b*c^6*d) + x^7*(a^2*d^7 + 21*b^2*c^2*d^5 + \\
& 14*a*b*c*d^6) + x^4*(35*a^2*c^3*d^4 + 21*b^2*c^5*d^2 + 70*a*b*c^4*d^3) + x^5*(21*a^2*c^2*d^5 + 35*b^2*c^4*d^3 + 70*a*b*c^3*d^4) + x^8*(7*b^2*c*d^6 + 2 \\
& *a*b*d^7) + a^2*c^7 + b^2*d^7*x^9)
\end{aligned}$$

sympy [B] time = 20.66, size = 2917, normalized size = 10.57

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**3/(d*x+c)**8,x)

[Out] $-36*b**7*d**2*\log(x + (-36*a**11*b**7*d**13/(a*d - b*c)**10 + 396*a**10*b**8*c*d**12/(a*d - b*c)**10 - 1980*a**9*b**9*c**2*d**11/(a*d - b*c)**10 + 5940*a**8*b**10*c**3*d**10/(a*d - b*c)**10 - 11880*a**7*b**11*c**4*d**9/(a*d - b*c)**10 + 16632*a**6*b**12*c**5*d**8/(a*d - b*c)**10 - 16632*a**5*b**13*c**6*d**7/(a*d - b*c)**10 + 11880*a**4*b**14*c**7*d**6/(a*d - b*c)**10 - 5940*a**3*b**15*c**8*d**5/(a*d - b*c)**10 + 1980*a**2*b**16*c**9*d**4/(a*d - b*c)**10 - 396*a*b**17*c**10*d**3/(a*d - b*c)**10 + 36*a*b**7*d**3 + 36*b**18*c**11*d**2/(a*d - b*c)**10 + 36*b**8*c*d**2)/(72*b**8*d**3))/(a*d - b*c)**10 + 36*b**7*d**2*\log(x + (36*a**11*b**7*d**13/(a*d - b*c)**10 - 396*a**10*b**8*c*d**12/(a*d - b*c)**10 + 1980*a**9*b**9*c**2*d**11/(a*d - b*c)**10 - 5940*a**8*b**10*c**3*d**10/(a*d - b*c)**10 + 11880*a**7*b**11*c**4*d**9/(a$

$$\begin{aligned}
& *d - b*c)**10 - 16632*a**6*b**12*c**5*d**8/(a*d - b*c)**10 + 16632*a**5*b** \\
& 13*c**6*d**7/(a*d - b*c)**10 - 11880*a**4*b**14*c**7*d**6/(a*d - b*c)**10 + \\
& 5940*a**3*b**15*c**8*d**5/(a*d - b*c)**10 - 1980*a**2*b**16*c**9*d**4/(a*d \\
& - b*c)**10 + 396*a*b**17*c**10*d**3/(a*d - b*c)**10 + 36*a*b**7*d**3 - 36* \\
& b**18*c**11*d**2/(a*d - b*c)**10 + 36*b**8*c*d**2)/(72*b**8*d**3))/(a*d - b \\
& *c)**10 + (-10*a**8*d**8 + 95*a**7*b*c*d**7 - 409*a**6*b**2*c**2*d**6 + 106 \\
& 1*a**5*b**3*c**3*d**5 - 1879*a**4*b**4*c**4*d**4 + 2531*a**3*b**5*c**5*d**3 \\
& - 3349*a**2*b**6*c**6*d**2 - 595*a*b**7*c**7*d + 35*b**8*c**8 - 2520*b**8* \\
& d**8*x**8 + x**7*(-3780*a*b**7*d**8 - 16380*b**8*c*d**7) + x**6*(-840*a**2* \\
& b**6*d**8 - 24780*a*b**7*c*d**7 - 44940*b**8*c**2*d**6) + x**5*(210*a**3*b* \\
& *5*d**8 - 5670*a**2*b**6*c*d**7 - 68670*a*b**7*c**2*d**6 - 66990*b**8*c**3* \\
& d**5) + x**4*(-84*a**4*b**4*d**8 + 1386*a**3*b**5*c*d**7 - 16254*a**2*b**6* \\
& c**2*d**6 - 103614*a*b**7*c**3*d**5 - 57834*b**8*c**4*d**4) + x**3*(42*a**5 \\
& *b**3*d**8 - 546*a**4*b**4*c*d**7 + 3864*a**3*b**5*c**2*d**6 - 25536*a**2*b \\
& **6*c**3*d**5 - 90846*a*b**7*c**4*d**4 - 28098*b**8*c**5*d**3) + x**2*(-24* \\
& a**6*b**2*d**8 + 270*a**5*b**3*c*d**7 - 1494*a**4*b**4*c**2*d**6 + 5856*a** \\
& 3*b**5*c**3*d**5 - 23544*a**2*b**6*c**4*d**4 - 45090*a*b**7*c**5*d**3 - 653 \\
& 4*b**8*c**6*d**2) + x*(15*a**7*b*d**8 - 153*a**6*b**2*c*d**7 + 729*a**5*b** \\
& 3*c**2*d**6 - 2211*a**4*b**4*c**3*d**5 + 5139*a**3*b**5*c**4*d**4 - 12501*a \\
& **2*b**6*c**5*d**3 - 10863*a*b**7*c**6*d**2 - 315*b**8*c**7*d))/ (70*a**11*c \\
& **7*d**9 - 630*a**10*b*c**8*d**8 + 2520*a**9*b**2*c**9*d**7 - 5880*a**8*b** \\
& 3*c**10*d**6 + 8820*a**7*b**4*c**11*d**5 - 8820*a**6*b**5*c**12*d**4 + 5880 \\
& *a**5*b**6*c**13*d**3 - 2520*a**4*b**7*c**14*d**2 + 630*a**3*b**8*c**15*d - \\
& 70*a**2*b**9*c**16 + x**9*(70*a**9*b**2*d**16 - 630*a**8*b**3*c*d**15 + 25 \\
& 20*a**7*b**4*c**2*d**14 - 5880*a**6*b**5*c**3*d**13 + 8820*a**5*b**6*c**4*d \\
& **12 - 8820*a**4*b**7*c**5*d**11 + 5880*a**3*b**8*c**6*d**10 - 2520*a**2*b* \\
& *9*c**7*d**9 + 630*a*b**10*c**8*d**8 - 70*b**11*c**9*d**7) + x**8*(140*a**1 \\
& 0*b*d**16 - 770*a**9*b**2*c*d**15 + 630*a**8*b**3*c**2*d**14 + 5880*a**7*b* \\
& *4*c**3*d**13 - 23520*a**6*b**5*c**4*d**12 + 44100*a**5*b**6*c**5*d**11 - 4 \\
& 9980*a**4*b**7*c**6*d**10 + 36120*a**3*b**8*c**7*d**9 - 16380*a**2*b**9*c** \\
& 8*d**8 + 4270*a*b**10*c**9*d**7 - 490*b**11*c**10*d**6) + x**7*(70*a**11*d* \\
& *16 + 350*a**10*b*c*d**15 - 4830*a**9*b**2*c**2*d**14 + 16170*a**8*b**3*c** \\
& 3*d**13 - 20580*a**7*b**4*c**4*d**12 - 8820*a**6*b**5*c**5*d**11 + 67620*a* \\
& *5*b**6*c**6*d**10 - 105420*a**4*b**7*c**7*d**9 + 88830*a**3*b**8*c**8*d**8 \\
& - 44170*a**2*b**9*c**9*d**7 + 12250*a*b**10*c**10*d**6 - 1470*b**11*c**11* \\
& d**5) + x**6*(490*a**11*c*d**15 - 1470*a**10*b*c**2*d**14 - 6370*a**9*b**2* \\
& c**3*d**13 + 42630*a**8*b**3*c**4*d**12 - 97020*a**7*b**4*c**5*d**11 + 1029 \\
& 00*a**6*b**5*c**6*d**10 - 20580*a**5*b**6*c**7*d**9 - 79380*a**4*b**7*c**8* \\
& d**8 + 104370*a**3*b**8*c**9*d**7 - 62230*a**2*b**9*c**10*d**6 + 19110*a*b* \\
& *10*c**11*d**5 - 2450*b**11*c**12*d**4) + x**5*(1470*a**11*c**2*d**14 - 833 \\
& 0*a**10*b*c**3*d**13 + 11270*a**9*b**2*c**4*d**12 + 30870*a**8*b**3*c**5*d* \\
& *11 - 138180*a**7*b**4*c**6*d**10 + 226380*a**6*b**5*c**7*d**9 - 185220*a** \\
& 5*b**6*c**8*d**8 + 49980*a**4*b**7*c**9*d**7 + 42630*a**3*b**8*c**10*d**6 - \\
& 45570*a**2*b**9*c**11*d**5 + 17150*a*b**10*c**12*d**4 - 2450*b**11*c**13*d \\
& **3) + x**4*(2450*a**11*c**3*d**13 - 17150*a**10*b*c**4*d**12 + 45570*a**9*
\end{aligned}$$

$$\begin{aligned}
& b^{**2}c^{**5}d^{**11} - 42630a^{**8}b^{**3}c^{**6}d^{**10} - 49980a^{**7}b^{**4}c^{**7}d^{**9} + \\
& 185220a^{**6}b^{**5}c^{**8}d^{**8} - 226380a^{**5}b^{**6}c^{**9}d^{**7} + 138180a^{**4}b^{**7}c^{**10}d^{**6} - 30870a^{**3}b^{**8}c^{**11}d^{**5} - 11270a^{**2}b^{**9}c^{**12}d^{**4} + 8330 \\
& *a^{**10}c^{**13}d^{**3} - 1470b^{**11}c^{**14}d^{**2}) + x^{**3}(2450a^{**11}c^{**4}d^{**12} \\
& - 19110a^{**10}b^{**5}c^{**5}d^{**11} + 62230a^{**9}b^{**2}c^{**6}d^{**10} - 104370a^{**8}b^{**3}c^{**7}d^{**9} + 79380a^{**7}b^{**4}c^{**8}d^{**8} + 20580a^{**6}b^{**5}c^{**9}d^{**7} - 102900* \\
& a^{**5}b^{**6}c^{**10}d^{**6} + 97020a^{**4}b^{**7}c^{**11}d^{**5} - 42630a^{**3}b^{**8}c^{**12}d^{**4} + 6370a^{**2}b^{**9}c^{**13}d^{**3} + 1470a^{**10}c^{**14}d^{**2} - 490b^{**11}c^{**15} \\
& *d) + x^{**2}(1470a^{**11}c^{**5}d^{**11} - 12250a^{**10}b^{**6}c^{**6}d^{**10} + 44170a^{**9}b^{**2}c^{**7}d^{**9} - 88830a^{**8}b^{**3}c^{**8}d^{**8} + 105420a^{**7}b^{**4}c^{**9}d^{**7} - 67 \\
& 620a^{**6}b^{**5}c^{**10}d^{**6} + 8820a^{**5}b^{**6}c^{**11}d^{**5} + 20580a^{**4}b^{**7}c^{**12}d^{**4} - 16170a^{**3}b^{**8}c^{**13}d^{**3} + 4830a^{**2}b^{**9}c^{**14}d^{**2} - 350a^{**10}c^{**15}d \\
& - 70b^{**11}c^{**16}) + x(490a^{**11}c^{**6}d^{**10} - 4270a^{**10}b^{**7}c^{**7}d^{**9} + 16380a^{**9}b^{**2}c^{**8}d^{**8} - 36120a^{**8}b^{**3}c^{**9}d^{**7} + 49980a^{**7}b^{**4}c^{**10}d^{**6} - 44100a^{**6}b^{**5}c^{**11}d^{**5} + 23520a^{**5}b^{**6}c^{**12}d^{**4} - \\
& 5880a^{**4}b^{**7}c^{**13}d^{**3} - 630a^{**3}b^{**8}c^{**14}d^{**2} + 770a^{**2}b^{**9}c^{**15}d \\
& - 140a^{**10}c^{**16})
\end{aligned}$$

3.1375 $\int (a + bx)^5 \sqrt{c + dx} dx$

Optimal. Leaf size=156

$$-\frac{10b^4(c+dx)^{11/2}(bc-ad)}{11d^6} + \frac{20b^3(c+dx)^{9/2}(bc-ad)^2}{9d^6} - \frac{20b^2(c+dx)^{7/2}(bc-ad)^3}{7d^6} + \frac{2b(c+dx)^{5/2}(bc-ad)^4}{d^6} - \frac{2(c+dx)^{3/2}(bc-ad)^5}{d^6}$$

[Out] $-2/3*(-a*d+b*c)^5*(d*x+c)^{(3/2)}/d^6+2*b*(-a*d+b*c)^4*(d*x+c)^{(5/2)}/d^6-20/7*b^2*(-a*d+b*c)^3*(d*x+c)^{(7/2)}/d^6+20/9*b^3*(-a*d+b*c)^2*(d*x+c)^{(9/2)}/d^6-10/11*b^4*(-a*d+b*c)*(d*x+c)^{(11/2)}/d^6+2/13*b^5*(d*x+c)^{(13/2)}/d^6$

Rubi [A] time = 0.06, antiderivative size = 156, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{10b^4(c+dx)^{11/2}(bc-ad)}{11d^6} + \frac{20b^3(c+dx)^{9/2}(bc-ad)^2}{9d^6} - \frac{20b^2(c+dx)^{7/2}(bc-ad)^3}{7d^6} + \frac{2b(c+dx)^{5/2}(bc-ad)^4}{d^6} - \frac{2(c+dx)^{3/2}(bc-ad)^5}{d^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*Sqrt[c + d*x], x]

[Out] $(-2*(b*c - a*d)^5*(c + d*x)^{(3/2)})/(3*d^6) + (2*b*(b*c - a*d)^4*(c + d*x)^{(5/2)})/d^6 - (20*b^2*(b*c - a*d)^3*(c + d*x)^{(7/2)})/(7*d^6) + (20*b^3*(b*c - a*d)^2*(c + d*x)^{(9/2)})/(9*d^6) - (10*b^4*(b*c - a*d)*(c + d*x)^{(11/2)})/(11*d^6) + (2*b^5*(c + d*x)^{(13/2)})/(13*d^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^5 \sqrt{c + dx} dx &= \int \left(\frac{(-bc + ad)^5 \sqrt{c + dx}}{d^5} + \frac{5b(bc - ad)^4 (c + dx)^{3/2}}{d^5} - \frac{10b^2(bc - ad)^3 (c + dx)^{5/2}}{d^5} + \frac{10b^3(bc - ad)^2 (c + dx)^{7/2}}{d^5} - \frac{2(bc - ad)^5 (c + dx)^{3/2}}{3d^6} + \frac{2b(bc - ad)^4 (c + dx)^{5/2}}{d^6} - \frac{20b^2(bc - ad)^3 (c + dx)^{7/2}}{7d^6} + \frac{20b^3(bc - ad)^2 (c + dx)^{9/2}}{9d^6} - \frac{10b^4(bc - ad) (c + dx)^{11/2}}{11d^6} + \frac{2b^5 (c + dx)^{13/2}}{13d^6} \right) dx \end{aligned}$$

Mathematica [A] time = 0.15, size = 123, normalized size = 0.79

$$\frac{2(c+dx)^{3/2}(-4095b^4(c+dx)^4(bc-ad) + 10010b^3(c+dx)^3(bc-ad)^2 - 12870b^2(c+dx)^2(bc-ad)^3 + 9009b(c+dx)(bc-ad)^4 - 20b^5(c+dx)^2)}{9009d^6}$$

$$5*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*\sqrt{d*x + c}*c^4)*a^2*b^3/d^3 + 13*(63*(d*x + c)^{(11/2)} - 385*(d*x + c)^{(9/2)}*c + 990*(d*x + c)^{(7/2)}*c^2 - 1386*(d*x + c)^{(5/2)}*c^3 + 1155*(d*x + c)^{(3/2)}*c^4 - 693*\sqrt{d*x + c}*c^5)*b^5*c/d^5 + 65*(63*(d*x + c)^{(11/2)} - 385*(d*x + c)^{(9/2)}*c + 990*(d*x + c)^{(7/2)}*c^2 - 1386*(d*x + c)^{(5/2)}*c^3 + 1155*(d*x + c)^{(3/2)}*c^4 - 693*\sqrt{d*x + c}*c^5)*a*b^4/d^4 + 3*(231*(d*x + c)^{(13/2)} - 1638*(d*x + c)^{(11/2)}*c + 5005*(d*x + c)^{(9/2)}*c^2 - 8580*(d*x + c)^{(7/2)}*c^3 + 9009*(d*x + c)^{(5/2)}*c^4 - 6006*(d*x + c)^{(3/2)}*c^5 + 3003*\sqrt{d*x + c}*c^6)*b^5/d^5)/d$$

maple [B] time = 0.01, size = 273, normalized size = 1.75

$$2(dx + c)^{\frac{3}{2}} \left(693b^5x^5d^5 + 4095ab^4d^5x^4 - 630b^5cd^4x^4 + 10010a^2b^3d^5x^3 - 3640ab^4cd^4x^3 + 560b^5c^2d^3x^3 + 12870 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5*(d*x+c)^(1/2),x)

[Out] 2/9009*(d*x+c)^(3/2)*(693*b^5*d^5*x^5+4095*a*b^4*d^5*x^4-630*b^5*c*d^4*x^4+10010*a^2*b^3*d^5*x^3-3640*a*b^4*c*d^4*x^3+560*b^5*c^2*d^3*x^3+12870*a^3*b^2*d^5*x^2-8580*a^2*b^3*c*d^4*x^2+3120*a*b^4*c^2*d^3*x^2-480*b^5*c^3*d^2*x^2+9009*a^4*b*d^5*x-10296*a^3*b^2*c*d^4*x+6864*a^2*b^3*c^2*d^3*x-2496*a*b^4*c^3*d^2*x+384*b^5*c^4*d*x+3003*a^5*d^5-6006*a^4*b*c*d^4+6864*a^3*b^2*c^2*d^3-4576*a^2*b^3*c^3*d^2+1664*a*b^4*c^4*d-256*b^5*c^5)/d^6

maxima [A] time = 1.42, size = 259, normalized size = 1.66

$$2 \left(693(dx + c)^{\frac{13}{2}}b^5 - 4095(b^5c - ab^4d)(dx + c)^{\frac{11}{2}} + 10010(b^5c^2 - 2ab^4cd + a^2b^3d^2)(dx + c)^{\frac{9}{2}} - 12870(b^5c^3 - 3a \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^(1/2),x, algorithm="maxima")

[Out] 2/9009*(693*(d*x + c)^(13/2)*b^5 - 4095*(b^5*c - a*b^4*d)*(d*x + c)^(11/2) + 10010*(b^5*c^2 - 2*a*b^4*c*d + a^2*b^3*d^2)*(d*x + c)^(9/2) - 12870*(b^5*c^3 - 3*a*b^4*c^2*d + 3*a^2*b^3*c*d^2 - a^3*b^2*d^3)*(d*x + c)^(7/2) + 9009*(b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)*(d*x + c)^(5/2) - 3003*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)*(d*x + c)^(3/2))/d^6

mupad [B] time = 0.08, size = 137, normalized size = 0.88

$$\frac{2b^5(c+dx)^{13/2}}{13d^6} - \frac{(10b^5c - 10ab^4d)(c+dx)^{11/2}}{11d^6} + \frac{2(ad-bc)^5(c+dx)^{3/2}}{3d^6} + \frac{20b^2(ad-bc)^3(c+dx)^{7/2}}{7d^6} + \frac{20b^3}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5*(c + d*x)^(1/2), x)`

[Out] $(2*b^5*(c + d*x)^(13/2))/(13*d^6) - ((10*b^5*c - 10*a*b^4*d)*(c + d*x)^(11/2))/(11*d^6) + (2*(a*d - b*c)^5*(c + d*x)^(3/2))/(3*d^6) + (20*b^2*(a*d - b*c)^3*(c + d*x)^(7/2))/(7*d^6) + (20*b^3*(a*d - b*c)^2*(c + d*x)^(9/2))/(9*d^6) + (2*b*(a*d - b*c)^4*(c + d*x)^(5/2))/d^6$

sympy [B] time = 5.12, size = 314, normalized size = 2.01

$$2 \left(\frac{b^5(c+dx)^{\frac{13}{2}}}{13d^5} + \frac{(c+dx)^{\frac{11}{2}}(5ab^4d-5b^5c)}{11d^5} + \frac{(c+dx)^{\frac{9}{2}}(10a^2b^3d^2-20ab^4cd+10b^5c^2)}{9d^5} + \frac{(c+dx)^{\frac{7}{2}}(10a^3b^2d^3-30a^2b^3cd^2+30ab^4c^2d-10b^5c^3)}{7d^5} + \frac{(c+dx)^{\frac{5}{2}}(5a^4b^2d^4-10a^3b^3cd^3+10a^2b^4c^2d^2-10ab^5c^3d+5b^6c^4)}{5d^5} \right) / d$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5*(d*x+c)**(1/2), x)`

[Out] $2*(b**5*(c + d*x)**(13/2)/(13*d**5) + (c + d*x)**(11/2)*(5*a*b**4*d - 5*b**5*c)/(11*d**5) + (c + d*x)**(9/2)*(10*a**2*b**3*d**2 - 20*a*b**4*c*d + 10*b**5*c**2)/(9*d**5) + (c + d*x)**(7/2)*(10*a**3*b**2*d**3 - 30*a**2*b**3*c*d**2 + 30*a*b**4*c**2*d - 10*b**5*c**3)/(7*d**5) + (c + d*x)**(5/2)*(5*a**4*b*d**4 - 20*a**3*b**2*c*d**3 + 30*a**2*b**3*c**2*d**2 - 20*a*b**4*c**3*d + 5*b**5*c**4)/(5*d**5) + (c + d*x)**(3/2)*(a**5*d**5 - 5*a**4*b*c*d**4 + 10*a**3*b**2*c**2*d**3 - 10*a**2*b**3*c**3*d**2 + 5*a*b**4*c**4*d - b**5*c**5)/(3*d**5))/d$

3.1376 $\int (a + bx)^4 \sqrt{c + dx} dx$

Optimal. Leaf size=129

$$-\frac{8b^3(c+dx)^{9/2}(bc-ad)}{9d^5} + \frac{12b^2(c+dx)^{7/2}(bc-ad)^2}{7d^5} - \frac{8b(c+dx)^{5/2}(bc-ad)^3}{5d^5} + \frac{2(c+dx)^{3/2}(bc-ad)^4}{3d^5} + \frac{2b^4(c+dx)^{1/2}(bc-ad)^5}{11d^5}$$

[Out] $2/3*(-a*d+b*c)^4*(d*x+c)^(3/2)/d^5-8/5*b*(-a*d+b*c)^3*(d*x+c)^(5/2)/d^5+12/7*b^2*(-a*d+b*c)^2*(d*x+c)^(7/2)/d^5-8/9*b^3*(-a*d+b*c)*(d*x+c)^(9/2)/d^5+2/11*b^4*(d*x+c)^(11/2)/d^5$

Rubi [A] time = 0.05, antiderivative size = 129, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{8b^3(c+dx)^{9/2}(bc-ad)}{9d^5} + \frac{12b^2(c+dx)^{7/2}(bc-ad)^2}{7d^5} - \frac{8b(c+dx)^{5/2}(bc-ad)^3}{5d^5} + \frac{2(c+dx)^{3/2}(bc-ad)^4}{3d^5} + \frac{2b^4(c+dx)^{1/2}(bc-ad)^5}{11d^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4*Sqrt[c + d*x], x]

[Out] $(2*(b*c - a*d)^4*(c + d*x)^(3/2))/(3*d^5) - (8*b*(b*c - a*d)^3*(c + d*x)^(5/2))/(5*d^5) + (12*b^2*(b*c - a*d)^2*(c + d*x)^(7/2))/(7*d^5) - (8*b^3*(b*c - a*d)*(c + d*x)^(9/2))/(9*d^5) + (2*b^4*(c + d*x)^(11/2))/(11*d^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^4 \sqrt{c + dx} dx &= \int \left(\frac{(-bc + ad)^4 \sqrt{c + dx}}{d^4} - \frac{4b(bc - ad)^3 (c + dx)^{3/2}}{d^4} + \frac{6b^2(bc - ad)^2 (c + dx)^{5/2}}{d^4} - \frac{4b^3(bc - ad)(c + dx)^{7/2}}{d^4} + \frac{2b^4(c + dx)^{9/2}}{d^4} \right) dx \\ &= \frac{2(bc - ad)^4 (c + dx)^{3/2}}{3d^5} - \frac{8b(bc - ad)^3 (c + dx)^{5/2}}{5d^5} + \frac{12b^2(bc - ad)^2 (c + dx)^{7/2}}{7d^5} - \frac{8b^3(bc - ad)(c + dx)^{9/2}}{9d^5} + \frac{2b^4(c + dx)^{11/2}}{11d^5} \end{aligned}$$

Mathematica [A] time = 0.10, size = 101, normalized size = 0.78

$$\frac{2(c+dx)^{3/2}(-1540b^3(c+dx)^3(bc-ad) + 2970b^2(c+dx)^2(bc-ad)^2 - 2772b(c+dx)(bc-ad)^3 + 1155(bc-ad)^4)}{3465d^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4*Sqrt[c + d*x],x]

[Out] $(2*(c + d*x)^{(3/2)}*(1155*(b*c - a*d)^4 - 2772*b*(b*c - a*d)^3*(c + d*x) + 2*970*b^2*(b*c - a*d)^2*(c + d*x)^2 - 1540*b^3*(b*c - a*d)*(c + d*x)^3 + 315*b^4*(c + d*x)^4)/(3465*d^5)$

fricas [B] time = 0.43, size = 245, normalized size = 1.90

$$2 \left(315 b^4 d^5 x^5 + 128 b^4 c^5 - 704 a b^3 c^4 d + 1584 a^2 b^2 c^3 d^2 - 1848 a^3 b c^2 d^3 + 1155 a^4 c d^4 + 35 (b^4 c d^4 + 44 a b^3 d^5) x^4 - \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^(1/2),x, algorithm="fricas")

[Out] $2/3465*(315*b^4*d^5*x^5 + 128*b^4*c^5 - 704*a*b^3*c^4*d + 1584*a^2*b^2*c^3*d^2 - 1848*a^3*b*c^2*d^3 + 1155*a^4*c*d^4 + 35*(b^4*c*d^4 + 44*a*b^3*d^5)*x^4 - 10*(4*b^4*c^2*d^3 - 22*a*b^3*c*d^4 - 297*a^2*b^2*d^5)*x^3 + 6*(8*b^4*c^3*d^2 - 44*a*b^3*c^2*d^3 + 99*a^2*b^2*c*d^4 + 462*a^3*b*d^5)*x^2 - (64*b^4*c^4*d - 352*a*b^3*c^3*d^2 + 792*a^2*b^2*c^2*d^3 - 924*a^3*b*c*d^4 - 1155*a^4*d^5)*x)*sqrt(d*x + c)/d^5$

giac [B] time = 1.25, size = 470, normalized size = 3.64

$$2 \left(3465 \sqrt{dx + c} a^4 c + 1155 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} \right) a^4 + \frac{4620 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} \right) a^3 b c}{d} + \frac{1386 \left(3 (dx + c)^{\frac{5}{2}} - 10 (dx + c)^{\frac{3}{2}} c + 15 \right)}{d^2} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^(1/2),x, algorithm="giac")

[Out] $2/3465*(3465*sqrt(d*x + c)*a^4*c + 1155*((d*x + c)^{(3/2)} - 3*sqrt(d*x + c))*c)*a^4 + 4620*((d*x + c)^{(3/2)} - 3*sqrt(d*x + c))*a^3*b*c/d + 1386*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a^2*b^2*c/d^2 + 924*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a^3*b/d + 396*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a*b^3*c/d^3 + 594*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a^2*b^2/d^2 + 11*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*sqrt(d*x + c)*c^4)*b^4*c/d^4 + 44*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*sqrt(d*x + c)*c^4)*a*b^3/d^3 + 5*(63*(d*x + c)^{(11/2)} - 385*$

$$(d*x + c)^{(9/2)}*c + 990*(d*x + c)^{(7/2)}*c^2 - 1386*(d*x + c)^{(5/2)}*c^3 + 1155*(d*x + c)^{(3/2)}*c^4 - 693*\sqrt{d*x + c}*c^5)*b^4/d^4)/d$$

maple [A] time = 0.01, size = 186, normalized size = 1.44

$$\frac{2(dx+c)^{\frac{3}{2}}(315b^4x^4d^4 + 1540ab^3d^4x^3 - 280b^4cd^3x^3 + 2970a^2b^2d^4x^2 - 1320ab^3cd^3x^2 + 240b^4c^2d^2x^2 + 2772a^3b^3d^4x - 2376a^2b^2cd^3x + 1056a^2b^3c^2d^2x - 192b^4c^3d^3x + 1155a^4d^4 - 1848a^3b^3cd^3 + 1584a^2b^2c^2d^2 - 704a^3b^3c^3d + 128b^4c^4)}{d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4*(d*x+c)^(1/2), x)

[Out] 2/3465*(d*x+c)^(3/2)*(315*b^4*d^4*x^4+1540*a*b^3*d^4*x^3-280*b^4*c*d^3*x^3+2970*a^2*b^2*d^4*x^2-1320*a*b^3*c*d^3*x^2+240*b^4*c^2*d^2*x^2+2772*a^3*b*d^4*x-2376*a^2*b^2*c*d^3*x+1056*a*b^3*c^2*d^2*x-192*b^4*c^3*d*x+1155*a^4*d^4-1848*a^3*b*c*d^3+1584*a^2*b^2*c^2*d^2-704*a*b^3*c^3*d+128*b^4*c^4)/d^5

maxima [A] time = 1.36, size = 181, normalized size = 1.40

$$\frac{2\left(315(dx+c)^{\frac{11}{2}}b^4 - 1540(b^4c - ab^3d)(dx+c)^{\frac{9}{2}} + 2970(b^4c^2 - 2ab^3cd + a^2b^2d^2)(dx+c)^{\frac{7}{2}} - 2772(b^4c^3 - 3ab^3cd^2 + a^2b^2c^2d)(dx+c)^{\frac{5}{2}} + 1155(b^4c^4 - 4a^2b^3c^3d + 6a^2b^2c^2d^2 - 4a^3b^3cd^3 + a^4d^4)(dx+c)^{\frac{3}{2}}\right)}{3465d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^(1/2), x, algorithm="maxima")

[Out] 2/3465*(315*(d*x + c)^(11/2)*b^4 - 1540*(b^4*c - a*b^3*d)*(d*x + c)^(9/2) + 2970*(b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2)*(d*x + c)^(7/2) - 2772*(b^4*c^3 - 3*a*b^3*c^2*d + 3*a^2*b^2*c*d^2 - a^3*b*d^3)*(d*x + c)^(5/2) + 1155*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b^3*c*d^3 + a^4*d^4)*(d*x + c)^(3/2))/d^5

mupad [B] time = 0.22, size = 112, normalized size = 0.87

$$\frac{2b^4(c+dx)^{11/2}}{11d^5} - \frac{(8b^4c - 8ab^3d)(c+dx)^{9/2}}{9d^5} + \frac{2(ad-bc)^4(c+dx)^{3/2}}{3d^5} + \frac{12b^2(ad-bc)^2(c+dx)^{7/2}}{7d^5} + \frac{8b(ad-bc)(c+dx)^{5/2}}{5d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^4*(c + d*x)^(1/2), x)

[Out] (2*b^4*(c + d*x)^(11/2))/(11*d^5) - ((8*b^4*c - 8*a*b^3*d)*(c + d*x)^(9/2))/(9*d^5) + (2*(a*d - b*c)^4*(c + d*x)^(3/2))/(3*d^5) + (12*b^2*(a*d - b*c)^2*(c + d*x)^(7/2))/(7*d^5) + (8*b*(a*d - b*c)^3*(c + d*x)^(5/2))/(5*d^5)

sympy [A] time = 4.19, size = 223, normalized size = 1.73

$$2 \left(\frac{b^4(c+dx)^{\frac{11}{2}}}{11d^4} + \frac{(c+dx)^{\frac{9}{2}}(4ab^3d-4b^4c)}{9d^4} + \frac{(c+dx)^{\frac{7}{2}}(6a^2b^2d^2-12ab^3cd+6b^4c^2)}{7d^4} + \frac{(c+dx)^{\frac{5}{2}}(4a^3bd^3-12a^2b^2cd^2+12ab^3c^2d-4b^4c^3)}{5d^4} + \frac{(c+dx)^{\frac{3}{2}}(a^4d^3-4a^3b^2cd+6a^2b^3c^2d-4ab^4c^3)}{3d^4} \right) \frac{1}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4*(d*x+c)**(1/2),x)

[Out] 2*(b**4*(c + d*x)**(11/2)/(11*d**4) + (c + d*x)**(9/2)*(4*a*b**3*d - 4*b**4*c)/(9*d**4) + (c + d*x)**(7/2)*(6*a**2*b**2*d**2 - 12*a*b**3*c*d + 6*b**4*c**2)/(7*d**4) + (c + d*x)**(5/2)*(4*a**3*b*d**3 - 12*a**2*b**2*c*d**2 + 12*a*b**3*c**2*d - 4*b**4*c**3)/(5*d**4) + (c + d*x)**(3/2)*(a**4*d**4 - 4*a**3*b*c*d**3 + 6*a**2*b**2*c**2*d**2 - 4*a*b**3*c**3*d + b**4*c**4)/(3*d**4))/d

3.1377 $\int (a + bx)^3 \sqrt{c + dx} dx$

Optimal. Leaf size=100

$$-\frac{6b^2(c+dx)^{7/2}(bc-ad)}{7d^4} + \frac{6b(c+dx)^{5/2}(bc-ad)^2}{5d^4} - \frac{2(c+dx)^{3/2}(bc-ad)^3}{3d^4} + \frac{2b^3(c+dx)^{9/2}}{9d^4}$$

[Out] $-2/3*(-a*d+b*c)^3*(d*x+c)^{(3/2)}/d^4+6/5*b*(-a*d+b*c)^2*(d*x+c)^{(5/2)}/d^4-6/7*b^2*(-a*d+b*c)*(d*x+c)^{(7/2)}/d^4+2/9*b^3*(d*x+c)^{(9/2)}/d^4$

Rubi [A] time = 0.04, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{6b^2(c+dx)^{7/2}(bc-ad)}{7d^4} + \frac{6b(c+dx)^{5/2}(bc-ad)^2}{5d^4} - \frac{2(c+dx)^{3/2}(bc-ad)^3}{3d^4} + \frac{2b^3(c+dx)^{9/2}}{9d^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3*sqrt[c + d*x], x]

[Out] $(-2*(b*c - a*d)^3*(c + d*x)^{(3/2)})/(3*d^4) + (6*b*(b*c - a*d)^2*(c + d*x)^{(5/2)})/(5*d^4) - (6*b^2*(b*c - a*d)*(c + d*x)^{(7/2)})/(7*d^4) + (2*b^3*(c + d*x)^{(9/2)})/(9*d^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^3 \sqrt{c + dx} dx &= \int \left(\frac{(-bc + ad)^3 \sqrt{c + dx}}{d^3} + \frac{3b(bc - ad)^2 (c + dx)^{3/2}}{d^3} - \frac{3b^2(bc - ad)(c + dx)^{5/2}}{d^3} + \frac{b^3(c + dx)^{7/2}}{d^3} \right) dx \\ &= -\frac{2(bc - ad)^3 (c + dx)^{3/2}}{3d^4} + \frac{6b(bc - ad)^2 (c + dx)^{5/2}}{5d^4} - \frac{6b^2(bc - ad)(c + dx)^{7/2}}{7d^4} + \frac{2b^3(c + dx)^{9/2}}{9d^4} \end{aligned}$$

Mathematica [A] time = 0.06, size = 79, normalized size = 0.79

$$\frac{2(c+dx)^{3/2}(-135b^2(c+dx)^2(bc-ad) + 189b(c+dx)(bc-ad)^2 - 105(bc-ad)^3 + 35b^3(c+dx)^3)}{315d^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3*Sqrt[c + d*x],x]

[Out] $(2*(c + d*x)^{(3/2)}*(-105*(b*c - a*d)^3 + 189*b*(b*c - a*d)^2*(c + d*x) - 135*b^2*(b*c - a*d)*(c + d*x)^2 + 35*b^3*(c + d*x)^3))/(315*d^4)$

fricas [A] time = 0.43, size = 164, normalized size = 1.64

$$\frac{2(35b^3d^4x^4 - 16b^3c^4 + 72ab^2c^3d - 126a^2bc^2d^2 + 105a^3cd^3 + 5(b^3cd^3 + 27ab^2d^4)x^3 - 3(2b^3c^2d^2 - 9ab^2cd^3))}{315d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^(1/2),x, algorithm="fricas")

[Out] $2/315*(35*b^3*d^4*x^4 - 16*b^3*c^4 + 72*a*b^2*c^3*d - 126*a^2*b*c^2*d^2 + 105*a^3*c*d^3 + 5*(b^3*c*d^3 + 27*a*b^2*d^4)*x^3 - 3*(2*b^3*c^2*d^2 - 9*a*b^2*c*d^3 - 63*a^2*b*d^4)*x^2 + (8*b^3*c^3*d - 36*a*b^2*c^2*d^2 + 63*a^2*b*c*d^3 + 105*a^3*d^4)*x)*\text{sqrt}(d*x + c)/d^4$

giac [B] time = 1.27, size = 322, normalized size = 3.22

$$2 \left(315 \sqrt{dx + c} a^3 c + 105 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} \right) a^3 + \frac{315 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} \right) a^2 bc}{d} + \frac{63 \left(3 (dx + c)^{\frac{5}{2}} - 10 (dx + c)^{\frac{3}{2}} c + 15 \sqrt{dx + c} \right) a^2 bc}{d^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^(1/2),x, algorithm="giac")

[Out] $2/315*(315*\text{sqrt}(d*x + c)*a^3*c + 105*((d*x + c)^{(3/2)} - 3*\text{sqrt}(d*x + c)*c)*a^3 + 315*((d*x + c)^{(3/2)} - 3*\text{sqrt}(d*x + c)*c)*a^2*b*c/d + 63*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*\text{sqrt}(d*x + c)*c^2)*a*b^2*c/d^2 + 63*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*\text{sqrt}(d*x + c)*c^2)*a^2*b/d + 9*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*\text{sqrt}(d*x + c)*c^3)*b^3*c/d^3 + 27*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*\text{sqrt}(d*x + c)*c^3)*a*b^2/d^2 + (35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*\text{sqrt}(d*x + c)*c^4)*b^3/d^3)/d$

maple [A] time = 0.00, size = 116, normalized size = 1.16

$$\frac{2(dx + c)^{\frac{3}{2}}(35b^3x^3d^3 + 135ab^2d^3x^2 - 30b^3cd^2x^2 + 189a^2bd^3x - 108ab^2cd^2x + 24b^3c^2dx + 105a^3d^3 - 126a^2bcd)}{315d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3*(d*x+c)^(1/2),x)`

[Out] $2/315*(d*x+c)^{(3/2)}*(35*b^3*d^3*x^3+135*a*b^2*d^3*x^2-30*b^3*c*d^2*x^2+189*a^2*b*d^3*x-108*a*b^2*c*d^2*x+24*b^3*c^2*d*x+105*a^3*d^3-126*a^2*b*c*d^2+72*a*b^2*c^2*d-16*b^3*c^3)/d^4$

maxima [A] time = 1.37, size = 118, normalized size = 1.18

$$\frac{2 \left(35 (dx + c)^{\frac{9}{2}} b^3 - 135 (b^3 c - ab^2 d) (dx + c)^{\frac{7}{2}} + 189 (b^3 c^2 - 2 ab^2 cd + a^2 b d^2) (dx + c)^{\frac{5}{2}} - 105 (b^3 c^3 - 3 ab^2 c^2 d + 3 a^2 b c^2 d^2 - 16 b^3 c^3) \right)}{315 d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3*(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] $2/315*(35*(d*x + c)^{(9/2)}*b^3 - 135*(b^3*c - a*b^2*d)*(d*x + c)^{(7/2)} + 189*(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*(d*x + c)^{(5/2)} - 105*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*(d*x + c)^{(3/2)})/d^4$

mupad [B] time = 0.07, size = 87, normalized size = 0.87

$$\frac{2 b^3 (c + dx)^{9/2}}{9 d^4} - \frac{(6 b^3 c - 6 a b^2 d) (c + dx)^{7/2}}{7 d^4} + \frac{2 (a d - b c)^3 (c + dx)^{3/2}}{3 d^4} + \frac{6 b (a d - b c)^2 (c + dx)^{5/2}}{5 d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3*(c + d*x)^(1/2),x)`

[Out] $(2*b^3*(c + d*x)^{(9/2)})/(9*d^4) - ((6*b^3*c - 6*a*b^2*d)*(c + d*x)^{(7/2)})/(7*d^4) + (2*(a*d - b*c)^3*(c + d*x)^{(3/2)})/(3*d^4) + (6*b*(a*d - b*c)^2*(c + d*x)^{(5/2)})/(5*d^4)$

sympy [A] time = 3.34, size = 146, normalized size = 1.46

$$\frac{2 \left(\frac{b^3(c+dx)^{\frac{9}{2}}}{9d^3} + \frac{(c+dx)^{\frac{7}{2}}(3ab^2d-3b^3c)}{7d^3} + \frac{(c+dx)^{\frac{5}{2}}(3a^2bd^2-6ab^2cd+3b^3c^2)}{5d^3} + \frac{(c+dx)^{\frac{3}{2}}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}{3d^3} \right)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3*(d*x+c)**(1/2),x)`

[Out] $2*(b**3*(c + d*x)**(9/2))/(9*d**3) + (c + d*x)**(7/2)*(3*a*b**2*d - 3*b**3*c)/(7*d**3) + (c + d*x)**(5/2)*(3*a**2*b*d**2 - 6*a*b**2*c*d + 3*b**3*c**2)/(5*d**3) + (c + d*x)**(3/2)*(a**3*d**3 - 3*a**2*b*c*d**2 + 3*a*b**2*c**2*d - b**3*c**3)/(3*d**3)/d$

3.1378 $\int (a + bx)^2 \sqrt{c + dx} dx$

Optimal. Leaf size=71

$$-\frac{4b(c + dx)^{5/2}(bc - ad)}{5d^3} + \frac{2(c + dx)^{3/2}(bc - ad)^2}{3d^3} + \frac{2b^2(c + dx)^{7/2}}{7d^3}$$

[Out] $2/3*(-a*d+b*c)^2*(d*x+c)^(3/2)/d^3-4/5*b*(-a*d+b*c)*(d*x+c)^(5/2)/d^3+2/7*b^2*(d*x+c)^(7/2)/d^3$

Rubi [A] time = 0.02, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{4b(c + dx)^{5/2}(bc - ad)}{5d^3} + \frac{2(c + dx)^{3/2}(bc - ad)^2}{3d^3} + \frac{2b^2(c + dx)^{7/2}}{7d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*Sqrt[c + d*x], x]

[Out] $(2*(b*c - a*d)^2*(c + d*x)^(3/2))/(3*d^3) - (4*b*(b*c - a*d)*(c + d*x)^(5/2))/(5*d^3) + (2*b^2*(c + d*x)^(7/2))/(7*d^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2 \sqrt{c + dx} dx &= \int \left(\frac{(-bc + ad)^2 \sqrt{c + dx}}{d^2} - \frac{2b(bc - ad)(c + dx)^{3/2}}{d^2} + \frac{b^2(c + dx)^{5/2}}{d^2} \right) dx \\ &= \frac{2(bc - ad)^2(c + dx)^{3/2}}{3d^3} - \frac{4b(bc - ad)(c + dx)^{5/2}}{5d^3} + \frac{2b^2(c + dx)^{7/2}}{7d^3} \end{aligned}$$

Mathematica [A] time = 0.04, size = 61, normalized size = 0.86

$$\frac{2(c + dx)^{3/2} (35a^2d^2 + 14abd(3dx - 2c) + b^2(8c^2 - 12cdx + 15d^2x^2))}{105d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*sqrt[c + d*x],x]

[Out] (2*(c + d*x)^(3/2)*(35*a^2*d^2 + 14*a*b*d*(-2*c + 3*d*x) + b^2*(8*c^2 - 12*c*d*x + 15*d^2*x^2)))/(105*d^3)

fricas [A] time = 0.45, size = 99, normalized size = 1.39

$$\frac{2 \left(15 b^2 d^3 x^3 + 8 b^2 c^3 - 28 a b c^2 d + 35 a^2 c d^2 + 3 (b^2 c d^2 + 14 a b d^3) x^2 - (4 b^2 c^2 d - 14 a b c d^2 - 35 a^2 d^3) x \right) \sqrt{d x + c}}{105 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^(1/2),x, algorithm="fricas")

[Out] 2/105*(15*b^2*d^3*x^3 + 8*b^2*c^3 - 28*a*b*c^2*d + 35*a^2*c*d^2 + 3*(b^2*c*d^2 + 14*a*b*d^3)*x^2 - (4*b^2*c^2*d - 14*a*b*c*d^2 - 35*a^2*d^3)*x)*sqrt(d*x + c)/d^3

giac [B] time = 1.29, size = 200, normalized size = 2.82

$$\frac{2 \left(105 \sqrt{d x + c} a^2 c + 35 \left((d x + c)^{\frac{3}{2}} - 3 \sqrt{d x + c} \right) a^2 + \frac{70 \left((d x + c)^{\frac{3}{2}} - 3 \sqrt{d x + c} \right) a b c}{d} + \frac{7 \left(3 (d x + c)^{\frac{5}{2}} - 10 (d x + c)^{\frac{3}{2}} c + 15 \sqrt{d x + c} c^2 \right) b^2 c}{d^2} \right)}{105 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^(1/2),x, algorithm="giac")

[Out] 2/105*(105*sqrt(d*x + c)*a^2*c + 35*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a^2 + 70*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a*b*c/d + 7*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*b^2*c/d^2 + 14*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a*b/d + 3*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*b^2/d^2)/d

maple [A] time = 0.01, size = 63, normalized size = 0.89

$$\frac{2 (d x + c)^{\frac{3}{2}} \left(15 b^2 x^2 d^2 + 42 a b d^2 x - 12 b^2 c d x + 35 a^2 d^2 - 28 a b c d + 8 b^2 c^2 \right)}{105 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(d*x+c)^(1/2),x)

[Out] $2/105*(d*x+c)^{(3/2)}*(15*b^2*d^2*x^2+42*a*b*d^2*x-12*b^2*c*d*x+35*a^2*d^2-28*a*b*c*d+8*b^2*c^2)/d^3$

maxima [A] time = 1.35, size = 68, normalized size = 0.96

$$\frac{2 \left(15 (dx + c)^{\frac{7}{2}} b^2 - 42 (b^2 c - abd) (dx + c)^{\frac{5}{2}} + 35 (b^2 c^2 - 2 abcd + a^2 d^2) (dx + c)^{\frac{3}{2}} \right)}{105 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2*(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] $2/105*(15*(d*x + c)^{(7/2)}*b^2 - 42*(b^2*c - a*b*d)*(d*x + c)^{(5/2)} + 35*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(d*x + c)^{(3/2)})/d^3$

mupad [B] time = 0.24, size = 68, normalized size = 0.96

$$\frac{2 (c + dx)^{3/2} (15 b^2 (c + dx)^2 + 35 a^2 d^2 + 35 b^2 c^2 - 42 b^2 c (c + dx) + 42 a b d (c + dx) - 70 a b c d)}{105 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2*(c + d*x)^(1/2),x)`

[Out] $(2*(c + d*x)^{(3/2)}*(15*b^2*(c + d*x)^2 + 35*a^2*d^2 + 35*b^2*c^2 - 42*b^2*c*(c + d*x) + 42*a*b*d*(c + d*x) - 70*a*b*c*d))/(105*d^3)$

sympy [A] time = 2.69, size = 85, normalized size = 1.20

$$\frac{2 \left(\frac{b^2 (c+dx)^{\frac{7}{2}}}{7d^2} + \frac{(c+dx)^{\frac{5}{2}} (2abd-2b^2c)}{5d^2} + \frac{(c+dx)^{\frac{3}{2}} (a^2d^2-2abcd+b^2c^2)}{3d^2} \right)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(d*x+c)**(1/2),x)`

[Out] $2*(b**2*(c + d*x)**(7/2)/(7*d**2) + (c + d*x)**(5/2)*(2*a*b*d - 2*b**2*c)/(5*d**2) + (c + d*x)**(3/2)*(a**2*d**2 - 2*a*b*c*d + b**2*c**2)/(3*d**2))/d$

3.1379 $\int (a + bx)\sqrt{c + dx} dx$

Optimal. Leaf size=42

$$\frac{2b(c + dx)^{5/2}}{5d^2} - \frac{2(c + dx)^{3/2}(bc - ad)}{3d^2}$$

[Out] $-2/3*(-a*d+b*c)*(d*x+c)^{(3/2)}/d^2+2/5*b*(d*x+c)^{(5/2)}/d^2$

Rubi [A] time = 0.01, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{2b(c + dx)^{5/2}}{5d^2} - \frac{2(c + dx)^{3/2}(bc - ad)}{3d^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)*\text{Sqrt}[c + d*x], x]$

[Out] $(-2*(b*c - a*d)*(c + d*x)^{(3/2)})/(3*d^2) + (2*b*(c + d*x)^{(5/2)})/(5*d^2)$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{IGtQ}[m, 0] \&\& (!\text{IntegerQ}[n] || (\text{EqQ}[c, 0] \&\& \text{LeQ}[7*m + 4*n + 4, 0]) || \text{LtQ}[9*m + 5*(n + 1), 0] || \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int (a + bx)\sqrt{c + dx} dx &= \int \left(\frac{(-bc + ad)\sqrt{c + dx}}{d} + \frac{b(c + dx)^{3/2}}{d} \right) dx \\ &= -\frac{2(bc - ad)(c + dx)^{3/2}}{3d^2} + \frac{2b(c + dx)^{5/2}}{5d^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 30, normalized size = 0.71

$$\frac{2(c + dx)^{3/2}(5ad - 2bc + 3bdx)}{15d^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*Sqrt[c + d*x],x]

[Out] $(2*(c + d*x)^{(3/2)}*(-2*b*c + 5*a*d + 3*b*d*x))/(15*d^2)$

fricas [A] time = 0.42, size = 46, normalized size = 1.10

$$\frac{2(3bd^2x^2 - 2bc^2 + 5acd + (bcd + 5ad^2)x)\sqrt{dx + c}}{15d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^(1/2),x, algorithm="fricas")

[Out] $2/15*(3*b*d^2*x^2 - 2*b*c^2 + 5*a*c*d + (b*c*d + 5*a*d^2)*x)*\text{sqrt}(d*x + c)/d^2$

giac [B] time = 1.37, size = 100, normalized size = 2.38

$$\frac{2 \left(15 \sqrt{dx + c} ac + 5 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} c \right) a + \frac{5 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} c \right) bc}{d} + \frac{\left(3 (dx + c)^{\frac{5}{2}} - 10 (dx + c)^{\frac{3}{2}} c + 15 \sqrt{dx + c} c^2 \right) b}{d} \right)}{15d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^(1/2),x, algorithm="giac")

[Out] $2/15*(15*\text{sqrt}(d*x + c)*a*c + 5*((d*x + c)^{(3/2)} - 3*\text{sqrt}(d*x + c)*c)*a + 5*((d*x + c)^{(3/2)} - 3*\text{sqrt}(d*x + c)*c)*b*c/d + (3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*\text{sqrt}(d*x + c)*c^2)*b/d)/d$

maple [A] time = 0.00, size = 27, normalized size = 0.64

$$\frac{2(dx + c)^{\frac{3}{2}}(3bdx + 5ad - 2bc)}{15d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(d*x+c)^(1/2),x)

[Out] $2/15*(d*x+c)^{(3/2)}*(3*b*d*x+5*a*d-2*b*c)/d^2$

maxima [A] time = 1.29, size = 33, normalized size = 0.79

$$\frac{2 \left(3 (dx + c)^{\frac{5}{2}} b - 5 (bc - ad) (dx + c)^{\frac{3}{2}} \right)}{15d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^(1/2),x, algorithm="maxima")

[Out] $2/15*(3*(d*x + c)^(5/2)*b - 5*(b*c - a*d)*(d*x + c)^(3/2))/d^2$

mupad [B] time = 0.04, size = 29, normalized size = 0.69

$$\frac{2(c+dx)^{3/2}(5ad-5bc+3b(c+dx))}{15d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)*(c + d*x)^(1/2),x)

[Out] $(2*(c + d*x)^(3/2)*(5*a*d - 5*b*c + 3*b*(c + d*x)))/(15*d^2)$

sympy [A] time = 2.12, size = 36, normalized size = 0.86

$$\frac{2\left(\frac{b(c+dx)^{5/2}}{5d} + \frac{(c+dx)^{3/2}(ad-bc)}{3d}\right)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)**(1/2),x)

[Out] $2*(b*(c + d*x)**(5/2)/(5*d) + (c + d*x)**(3/2)*(a*d - b*c)/(3*d))/d$

3.1380 $\int \sqrt{c + dx} dx$

Optimal. Leaf size=16

$$\frac{2(c + dx)^{3/2}}{3d}$$

[Out] $2/3*(d*x+c)^{(3/2)}/d$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{2(c + dx)^{3/2}}{3d}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x], x]

[Out] $(2*(c + d*x)^{(3/2)})/(3*d)$

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \sqrt{c + dx} dx = \frac{2(c + dx)^{3/2}}{3d}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$\frac{2(c + dx)^{3/2}}{3d}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*x], x]

[Out] $(2*(c + d*x)^{(3/2)})/(3*d)$

fricas [A] time = 0.44, size = 12, normalized size = 0.75

$$\frac{2(dx + c)^{\frac{3}{2}}}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2),x, algorithm="fricas")

[Out] 2/3*(d*x + c)^(3/2)/d

giac [A] time = 1.34, size = 12, normalized size = 0.75

$$\frac{2(dx+c)^{\frac{3}{2}}}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2),x, algorithm="giac")

[Out] 2/3*(d*x + c)^(3/2)/d

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{2(dx+c)^{\frac{3}{2}}}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2),x)

[Out] 2/3*(d*x+c)^(3/2)/d

maxima [A] time = 1.35, size = 12, normalized size = 0.75

$$\frac{2(dx+c)^{\frac{3}{2}}}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2),x, algorithm="maxima")

[Out] 2/3*(d*x + c)^(3/2)/d

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{2(c+dx)^{\frac{3}{2}}}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/2),x)

[Out] $(2*(c + d*x)^{(3/2)})/(3*d)$

sympy [A] time = 0.06, size = 12, normalized size = 0.75

$$\frac{2(c + dx)^{\frac{3}{2}}}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(1/2),x)`

[Out] $2*(c + d*x)**(3/2)/(3*d)$

$$3.1381 \quad \int \frac{\sqrt{c+dx}}{a+bx} dx$$

Optimal. Leaf size=62

$$\frac{2\sqrt{c+dx}}{b} - \frac{2\sqrt{bc-ad} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{3/2}}$$

[Out] $-2*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})*(-a*d+b*c)^{(1/2)}/b^{(3/2)}+2*(d*x+c)^{(1/2)}/b$

Rubi [A] time = 0.05, antiderivative size = 62, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {50, 63, 208}

$$\frac{2\sqrt{c+dx}}{b} - \frac{2\sqrt{bc-ad} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x), x]

[Out] $(2*\operatorname{Sqrt}[c + d*x])/b - (2*\operatorname{Sqrt}[b*c - a*d]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/(\operatorname{Sqrt}[b*c - a*d])])/b^{(3/2)}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{c+dx}}{a+bx} dx &= \frac{2\sqrt{c+dx}}{b} + \frac{(bc-ad) \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{b} \\ &= \frac{2\sqrt{c+dx}}{b} + \frac{(2(bc-ad)) \operatorname{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{bd} \\ &= \frac{2\sqrt{c+dx}}{b} - \frac{2\sqrt{bc-ad} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.04, size = 62, normalized size = 1.00

$$\frac{2\sqrt{c+dx}}{b} - \frac{2\sqrt{bc-ad} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*x]/(a + b*x), x]

[Out] (2*Sqrt[c + d*x])/b - (2*Sqrt[b*c - a*d]*ArcTanh[(Sqrt[b]*Sqrt[c + d*x])/Sqrt[b*c - a*d]])/b^(3/2)

fricas [A] time = 0.47, size = 143, normalized size = 2.31

$$\left[\frac{\sqrt{\frac{bc-ad}{b}} \log\left(\frac{bdx+2bc-ad-2\sqrt{dx+c}b\sqrt{\frac{bc-ad}{b}}}{bx+a}\right) + 2\sqrt{dx+c}}{b}, -\frac{2\left(\sqrt{-\frac{bc-ad}{b}} \arctan\left(-\frac{\sqrt{dx+c}b\sqrt{-\frac{bc-ad}{b}}}{bc-ad}\right) - \sqrt{dx+c}\right)}{b} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a), x, algorithm="fricas")

[Out] [(sqrt((b*c - a*d)/b)*log((b*d*x + 2*b*c - a*d - 2*sqrt(d*x + c)*b*sqrt((b*c - a*d)/b)))/(b*x + a) + 2*sqrt(d*x + c))/b, -2*(sqrt(-(b*c - a*d)/b)*arctan(-sqrt(d*x + c)*b*sqrt(-(b*c - a*d)/b)/(b*c - a*d)) - sqrt(d*x + c))/b]

giac [A] time = 1.27, size = 62, normalized size = 1.00

$$\frac{2(bc - ad) \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{-b^2c+abd}}\right)}{\sqrt{-b^2c+abd}b} + \frac{2\sqrt{dx+c}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a),x, algorithm="giac")

[Out] 2*(b*c - a*d)*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/(sqrt(-b^2*c + a*b*d)*b) + 2*sqrt(d*x + c)/b

maple [A] time = 0.01, size = 92, normalized size = 1.48

$$-\frac{2ad \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b} + \frac{2c \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}} + \frac{2\sqrt{dx+c}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a),x)

[Out] 2*(d*x+c)^(1/2)/b-2/b/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)*b/((a*d-b*c)*b)^(1/2))*a*d+2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)*b/((a*d-b*c)*b)^(1/2))*c

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.07, size = 50, normalized size = 0.81

$$\frac{2\sqrt{c+dx}}{b} - \frac{2 \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{ad-bc}}\right) \sqrt{ad-bc}}{b^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(1/2)/(a + b*x),x)`

[Out] $(2*(c + d*x)^{(1/2)})/b - (2*\operatorname{atan}((b^{(1/2)}*(c + d*x)^{(1/2)})/(a*d - b*c)^{(1/2)}))*(a*d - b*c)^{(1/2)}/b^{(3/2)}$

sympy [A] time = 4.39, size = 61, normalized size = 0.98

$$\frac{2 \left(\frac{d\sqrt{c+dx}}{b} - \frac{d(ad-bc) \operatorname{atan}\left(\frac{\sqrt{c+dx}}{\sqrt{\frac{ad-bc}{b}}}\right)}{b^2 \sqrt{\frac{ad-bc}{b}}} \right)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(1/2)/(b*x+a),x)`

[Out] $2*(d*\sqrt{c + d*x})/b - d*(a*d - b*c)*\operatorname{atan}(\sqrt{c + d*x}/\sqrt{(a*d - b*c)/b})/(b**2*\sqrt{(a*d - b*c)/b))/d$

$$3.1382 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^2} dx$$

Optimal. Leaf size=70

$$-\frac{d \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{3/2}\sqrt{bc-ad}} - \frac{\sqrt{c+dx}}{b(a+bx)}$$

[Out] $-\frac{d \operatorname{arctanh}(b^{1/2}(d*x+c)^{1/2}/(-a*d+b*c)^{1/2})/b^{3/2}/(-a*d+b*c)^{1/2}}{-(d*x+c)^{1/2}/b/(b*x+a)}$

Rubi [A] time = 0.03, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {47, 63, 208}

$$-\frac{d \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{3/2}\sqrt{bc-ad}} - \frac{\sqrt{c+dx}}{b(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x)^2, x]

[Out] $-(\text{Sqrt}[c + d*x]/(b*(a + b*x))) - (d*\text{ArcTanh}[(\text{Sqrt}[b]*\text{Sqrt}[c + d*x])/(\text{Sqrt}[b*c - a*d])])/(b^{3/2}*\text{Sqrt}[b*c - a*d])$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{c+dx}}{(a+bx)^2} dx &= -\frac{\sqrt{c+dx}}{b(a+bx)} + \frac{d \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{2b} \\ &= -\frac{\sqrt{c+dx}}{b(a+bx)} + \frac{\text{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{b} \\ &= -\frac{\sqrt{c+dx}}{b(a+bx)} - \frac{d \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{3/2}\sqrt{bc-ad}} \end{aligned}$$

Mathematica [A] time = 0.08, size = 69, normalized size = 0.99

$$\frac{d \tan^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{b^{3/2}\sqrt{ad-bc}} - \frac{\sqrt{c+dx}}{b(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*x]/(a + b*x)^2, x]

[Out] -(Sqrt[c + d*x]/(b*(a + b*x))) + (d*ArcTan[(Sqrt[b]*Sqrt[c + d*x])/Sqrt[-(b*c) + a*d]])/(b^(3/2)*Sqrt[-(b*c) + a*d])

fricas [A] time = 0.45, size = 232, normalized size = 3.31

$$\left[\frac{\sqrt{b^2c - abd} (bdx + ad) \log\left(\frac{bdx+2bc-ad-2\sqrt{b^2c-abd}\sqrt{dx+c}}{bx+a}\right) - 2(b^2c - abd)\sqrt{dx+c} - \sqrt{-b^2c + abd} (bdx + ad) \arctan\left(\frac{\sqrt{b^2c - abd} (bdx + ad)}{ab^3c - a^2b^2d + (b^4c - ab^3d)x}\right)}{2(ab^3c - a^2b^2d + (b^4c - ab^3d)x)}, \frac{\sqrt{-b^2c + abd} (bdx + ad) \arctan\left(\frac{\sqrt{b^2c - abd} (bdx + ad)}{ab^3c - a^2b^2d + (b^4c - ab^3d)x}\right)}{ab^3c - a^2b^2d + (b^4c - ab^3d)x} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^2, x, algorithm="fricas")

[Out] [1/2*(sqrt(b^2*c - a*b*d)*(b*d*x + a*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) - 2*(b^2*c - a*b*d)*sqrt(d*x + c)]/(a*b^3*c - a^2*b^2*d + (b^4*c - a*b^3*d)*x), (sqrt(-b^2*c + a*b*d)*(b*d*x +

$a*d*\arctan(\sqrt{-b^2*c + a*b*d}*\sqrt{d*x + c}/(b*d*x + b*c)) - (b^2*c - a*b*d)*\sqrt{d*x + c}/(a*b^3*c - a^2*b^2*d + (b^4*c - a*b^3*d)*x)]$

giac [A] time = 1.38, size = 72, normalized size = 1.03

$$\frac{d \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{\sqrt{-b^2c+abd} b} - \frac{\sqrt{dx+c} d}{((dx+c)b - bc + ad)b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^2,x, algorithm="giac")

[Out] $d*\arctan(\sqrt{d*x + c}*b/\sqrt{-b^2*c + a*b*d})/(\sqrt{-b^2*c + a*b*d}*b) - \sqrt{d*x + c}*d/(((d*x + c)*b - b*c + a*d)*b)$

maple [A] time = 0.01, size = 64, normalized size = 0.91

$$\frac{d \arctan\left(\frac{\sqrt{dx+c} b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b} b} - \frac{\sqrt{dx+c} d}{(bdx + ad) b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a)^2,x)

[Out] $-d/b*(d*x+c)^{(1/2)}/(b*d*x+a*d)+d/b/((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^2,x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.24, size = 61, normalized size = 0.87

$$\frac{d \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{b^{3/2} \sqrt{ad-bc}} - \frac{d \sqrt{c+dx}}{dx b^2 + a d b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(1/2)/(a + b*x)^2,x)`

[Out] $(d \operatorname{atan}\left(\frac{b^{1/2}(c + d*x)^{1/2}}{(a*d - b*c)^{1/2}}\right))/(b^{3/2}(a*d - b*c)^{1/2}) - (d(c + d*x)^{1/2})/(a*b*d + b^2*d*x)$

sympy [B] time = 58.58, size = 573, normalized size = 8.19

$$\frac{2ad^2\sqrt{c+dx}}{2a^2bd^2 - 2ab^2cd + 2ab^2d^2x - 2b^3cdx} + \frac{ad^2\sqrt{-\frac{1}{b(ad-bc)^3}} \log\left(-a^2d^2\sqrt{-\frac{1}{b(ad-bc)^3}} + 2abcd\sqrt{-\frac{1}{b(ad-bc)^3}} - b^2c^2\sqrt{-\frac{1}{b(ad-bc)^3}}\right)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(1/2)/(b*x+a)**2,x)`

[Out] $-2*a*d**2*\sqrt{c + d*x}/(2*a**2*b*d**2 - 2*a*b**2*c*d + 2*a*b**2*d**2*x - 2*b**3*c*d*x) + a*d**2*\sqrt{-1/(b*(a*d - b*c)**3)}*\log(-a**2*d**2*\sqrt{-1/(b*(a*d - b*c)**3)} + 2*a*b*c*d*\sqrt{-1/(b*(a*d - b*c)**3)} - b**2*c**2*\sqrt{-1/(b*(a*d - b*c)**3)} + \sqrt{c + d*x})/(2*b) - a*d**2*\sqrt{-1/(b*(a*d - b*c)**3)}*\log(a**2*d**2*\sqrt{-1/(b*(a*d - b*c)**3)} - 2*a*b*c*d*\sqrt{-1/(b*(a*d - b*c)**3)} + b**2*c**2*\sqrt{-1/(b*(a*d - b*c)**3)} + \sqrt{c + d*x})/(2*b) - c*d*\sqrt{-1/(b*(a*d - b*c)**3)}*\log(-a**2*d**2*\sqrt{-1/(b*(a*d - b*c)**3)} + 2*a*b*c*d*\sqrt{-1/(b*(a*d - b*c)**3)} - b**2*c**2*\sqrt{-1/(b*(a*d - b*c)**3)} + \sqrt{c + d*x})/2 + c*d*\sqrt{-1/(b*(a*d - b*c)**3)}*\log(a**2*d**2*\sqrt{-1/(b*(a*d - b*c)**3)} - 2*a*b*c*d*\sqrt{-1/(b*(a*d - b*c)**3)} + b**2*c**2*\sqrt{-1/(b*(a*d - b*c)**3)} + \sqrt{c + d*x})/2 + 2*c*d*\sqrt{c + d*x}/(2*a**2*d**2 - 2*a*b*c*d + 2*a*b*d**2*x - 2*b**2*c*d*x) + 2*d*\operatorname{atan}(\sqrt{c + d*x}/\sqrt{a*d/b - c})/(b**2*\sqrt{a*d/b - c})$

$$3.1383 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^3} dx$$

Optimal. Leaf size=110

$$\frac{d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4b^{3/2}(bc-ad)^{3/2}} - \frac{d\sqrt{c+dx}}{4b(a+bx)(bc-ad)} - \frac{\sqrt{c+dx}}{2b(a+bx)^2}$$

[Out] $1/4*d^2*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/b^{(3/2)/(-a*d+b*c)^{(3/2)}-1/2*(d*x+c)^{(1/2)/b/(b*x+a)^2-1/4*d*(d*x+c)^{(1/2)/b/(-a*d+b*c)/(b*x+a)}$

Rubi [A] time = 0.08, antiderivative size = 110, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 51, 63, 208}

$$\frac{d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4b^{3/2}(bc-ad)^{3/2}} - \frac{d\sqrt{c+dx}}{4b(a+bx)(bc-ad)} - \frac{\sqrt{c+dx}}{2b(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x)^3, x]

[Out] $-\operatorname{Sqrt}[c + d*x]/(2*b*(a + b*x)^2) - (d*\operatorname{Sqrt}[c + d*x])/(4*b*(b*c - a*d)*(a + b*x)) + (d^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/\operatorname{Sqrt}[b*c - a*d]])/(4*b^{(3/2)}*(b*c - a*d)^{(3/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{c+dx}}{(a+bx)^3} dx &= -\frac{\sqrt{c+dx}}{2b(a+bx)^2} + \frac{d \int \frac{1}{(a+bx)^2 \sqrt{c+dx}} dx}{4b} \\ &= -\frac{\sqrt{c+dx}}{2b(a+bx)^2} - \frac{d\sqrt{c+dx}}{4b(bc-ad)(a+bx)} - \frac{d^2 \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{8b(bc-ad)} \\ &= -\frac{\sqrt{c+dx}}{2b(a+bx)^2} - \frac{d\sqrt{c+dx}}{4b(bc-ad)(a+bx)} - \frac{d \operatorname{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{4b(bc-ad)} \\ &= -\frac{\sqrt{c+dx}}{2b(a+bx)^2} - \frac{d\sqrt{c+dx}}{4b(bc-ad)(a+bx)} + \frac{d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4b^{3/2}(bc-ad)^{3/2}} \end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.47

$$\frac{2d^2(c+dx)^{3/2} {}_2F_1\left(\frac{3}{2}, 3; \frac{5}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{3(ad-bc)^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[c + d*x]/(a + b*x)^3, x]
```

```
[Out] (2*d^2*(c + d*x)^(3/2)*Hypergeometric2F1[3/2, 3, 5/2, -((b*(c + d*x))/(-b*c
c) + a*d))]/(3*(-b*c) + a*d)^3)
```

fricas [B] time = 0.46, size = 456, normalized size = 4.15

$$\left[\frac{(b^2 d^2 x^2 + 2 a b d^2 x + a^2 d^2) \sqrt{b^2 c - a b d} \log\left(\frac{b d x + 2 b c - a d - 2 \sqrt{b^2 c - a b d} \sqrt{d x + c}}{b x + a}\right) + 2(2 b^3 c^2 - 3 a b^2 c d + a^2 b d^2 + (b^3 c d - 2 a^2 b^2 c^2 + a^3 b c d^2) x)}{8(a^2 b^4 c^2 - 2 a^3 b^3 c d + a^4 b^2 d^2 + (b^6 c^2 - 2 a b^5 c d + a^2 b^4 d^2) x^2 + 2(a b^5 c^2 - 2 a^2 b^4 c d + a^3 b^3 d^2) x)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^3,x, algorithm="fricas")

[Out] [-1/8*((b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) + 2*(2*b^3*c^2 - 3*a*b^2*c*d + a^2*b*d^2 + (b^3*c*d - a*b^2*d^2)*x)*sqrt(d*x + c))/(a^2*b^4*c^2 - 2*a^3*b^3*c*d + a^4*b^2*d^2 + (b^6*c^2 - 2*a*b^5*c*d + a^2*b^4*d^2)*x^2 + 2*(a*b^5*c^2 - 2*a^2*b^4*c*d + a^3*b^3*d^2)*x), -1/4*((b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) + (2*b^3*c^2 - 3*a*b^2*c*d + a^2*b*d^2 + (b^3*c*d - a*b^2*d^2)*x)*sqrt(d*x + c))/(a^2*b^4*c^2 - 2*a^3*b^3*c*d + a^4*b^2*d^2 + (b^6*c^2 - 2*a*b^5*c*d + a^2*b^4*d^2)*x^2 + 2*(a*b^5*c^2 - 2*a^2*b^4*c*d + a^3*b^3*d^2)*x)]

giac [A] time = 1.33, size = 126, normalized size = 1.15

$$-\frac{d^2 \arctan\left(\frac{\sqrt{d x + c} b}{\sqrt{-b^2 c + a b d}}\right)}{4(b^2 c - a b d) \sqrt{-b^2 c + a b d}} - \frac{(d x + c)^{\frac{3}{2}} b d^2 + \sqrt{d x + c} b c d^2 - \sqrt{d x + c} a d^3}{4(b^2 c - a b d)((d x + c) b - b c + a d)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^3,x, algorithm="giac")

[Out] -1/4*d^2*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/((b^2*c - a*b*d)*sqrt(-b^2*c + a*b*d)) - 1/4*((d*x + c)^(3/2)*b*d^2 + sqrt(d*x + c)*b*c*d^2 - sqrt(d*x + c)*a*d^3)/((b^2*c - a*b*d)*((d*x + c)*b - b*c + a*d)^2)

maple [A] time = 0.01, size = 111, normalized size = 1.01

$$\frac{d^2 \arctan\left(\frac{\sqrt{d x + c} b}{\sqrt{(a d - b c) b}}\right)}{4(a d - b c) \sqrt{(a d - b c) b} b} + \frac{(d x + c)^{\frac{3}{2}} d^2}{4(b d x + a d)^2 (a d - b c)} - \frac{\sqrt{d x + c} d^2}{4(b d x + a d)^2 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a)^3,x)

[Out] $\frac{1}{4}d^2/(b^2d^2+abd)^2/(ad-bc)(d^2+c)^{3/2}-\frac{1}{4}d^2/(b^2d^2+abd)^2/b(d^2+c)^{1/2}+\frac{1}{4}d^2/(ad-bc)/b/((ad-bc)b)^{1/2}\arctan((d^2+c)^{1/2}/((ad-bc)b)^{1/2})$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(1/2)/(b*x+a)^3,x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c positive or negative?

mupad [B] time = 0.30, size = 135, normalized size = 1.23

$$\frac{d^2 \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{4b^{3/2}(ad-bc)^{3/2}} - \frac{\frac{d^2 \sqrt{c+dx}}{4b} - \frac{d^2 (c+dx)^{3/2}}{4(ad-bc)}}{b^2 (c+dx)^2 - (2b^2c - 2abd)(c+dx) + a^2d^2 + b^2c^2 - 2abcd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(1/2)/(a + b*x)^3,x)`

[Out] $\frac{d^2 \operatorname{atan}\left(\frac{b^{1/2}(c+dx)^{1/2}}{(ad-bc)^{1/2}}\right)}{4b^{3/2}(ad-bc)^{3/2}} - \frac{(d^2(c+dx)^{1/2})/(4b) - (d^2(c+dx)^{3/2})/(4(ad-bc))}{b^2(c+dx)^2 - (2b^2c - 2abd)(c+dx) + a^2d^2 + b^2c^2 - 2abcd}$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(1/2)/(b*x+a)**3,x)`

[Out] Timed out

$$3.1384 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^4} dx$$

Optimal. Leaf size=146

$$-\frac{d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8b^{3/2}(bc-ad)^{5/2}} + \frac{d^2\sqrt{c+dx}}{8b(a+bx)(bc-ad)^2} - \frac{d\sqrt{c+dx}}{12b(a+bx)^2(bc-ad)} - \frac{\sqrt{c+dx}}{3b(a+bx)^3}$$

[Out] $-1/8*d^3*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/b^{(3/2)/(-a*d+b*c)^{(5/2)}-1/3*(d*x+c)^{(1/2)/b/(b*x+a)^3-1/12*d*(d*x+c)^{(1/2)/b/(-a*d+b*c)/(b*x+a)^2+1/8*d^2*(d*x+c)^{(1/2)/b/(-a*d+b*c)^2/(b*x+a)}$

Rubi [A] time = 0.10, antiderivative size = 146, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 51, 63, 208}

$$-\frac{d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8b^{3/2}(bc-ad)^{5/2}} + \frac{d^2\sqrt{c+dx}}{8b(a+bx)(bc-ad)^2} - \frac{d\sqrt{c+dx}}{12b(a+bx)^2(bc-ad)} - \frac{\sqrt{c+dx}}{3b(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x)^4, x]

[Out] $-\operatorname{Sqrt}[c + d*x]/(3*b*(a + b*x)^3) - (d*\operatorname{Sqrt}[c + d*x])/(12*b*(b*c - a*d)*(a + b*x)^2) + (d^2*\operatorname{Sqrt}[c + d*x])/(8*b*(b*c - a*d)^2*(a + b*x)) - (d^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/\operatorname{Sqrt}[b*c - a*d]])/(8*b^{(3/2)}*(b*c - a*d)^{(5/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{c+dx}}{(a+bx)^4} dx &= -\frac{\sqrt{c+dx}}{3b(a+bx)^3} + \frac{d \int \frac{1}{(a+bx)^3 \sqrt{c+dx}} dx}{6b} \\
&= -\frac{\sqrt{c+dx}}{3b(a+bx)^3} - \frac{d\sqrt{c+dx}}{12b(bc-ad)(a+bx)^2} - \frac{d^2 \int \frac{1}{(a+bx)^2 \sqrt{c+dx}} dx}{8b(bc-ad)} \\
&= -\frac{\sqrt{c+dx}}{3b(a+bx)^3} - \frac{d\sqrt{c+dx}}{12b(bc-ad)(a+bx)^2} + \frac{d^2\sqrt{c+dx}}{8b(bc-ad)^2(a+bx)} + \frac{d^3 \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{16b(bc-ad)^2} \\
&= -\frac{\sqrt{c+dx}}{3b(a+bx)^3} - \frac{d\sqrt{c+dx}}{12b(bc-ad)(a+bx)^2} + \frac{d^2\sqrt{c+dx}}{8b(bc-ad)^2(a+bx)} + \frac{d^2 \operatorname{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{8b(bc-ad)^2} \\
&= -\frac{\sqrt{c+dx}}{3b(a+bx)^3} - \frac{d\sqrt{c+dx}}{12b(bc-ad)(a+bx)^2} + \frac{d^2\sqrt{c+dx}}{8b(bc-ad)^2(a+bx)} - \frac{d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8b^{3/2}(bc-ad)^{5/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 52, normalized size = 0.36

$$\frac{2d^3(c+dx)^{3/2} {}_2F_1\left(\frac{3}{2}, 4; \frac{5}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{3(ad-bc)^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[c + d*x]/(a + b*x)^4, x]
```

```
[Out] (2*d^3*(c + d*x)^(3/2)*Hypergeometric2F1[3/2, 4, 5/2, -((b*(c + d*x))/(-b*c
+ a*d))]/(3*(-(b*c) + a*d)^4)
```

fricas [B] time = 0.46, size = 785, normalized size = 5.38

$$\frac{3 \left(b^3 d^3 x^3 + 3 a b^2 d^3 x^2 + 3 a^2 b d^3 x + a^3 d^3 \right) \sqrt{b^2 c - a b d} \log \left(\frac{b d x + 2 b c - a d - 2 \sqrt{b^2 c - a b d} \sqrt{d x + c}}{b x + a} \right) - 2 \left(8 b^4 c^3 - 22 a b^3 c^2 d + 17 a^2 b^2 c d^2 - 3 a^3 b d^3 \right)}{48 \left(a^3 b^5 c^3 - 3 a^4 b^4 c^2 d + 3 a^5 b^3 c d^2 - a^6 b^2 d^3 + (b^8 c^3 - 3 a b^7 c^2 d + 3 a^2 b^6 c d^2 - a^3 b^5 d^3) x^3 + 3 (a b^7 c^3 - 3 a^2 b^6 c^2 d + 3 a^3 b^5 c d^2 - a^4 b^4 d^3) x^2 + 3 (a^2 b^6 c^3 - 3 a^3 b^5 c^2 d + 3 a^4 b^4 c d^2 - a^5 b^3 d^3) x + 3 (a^3 b^5 c^3 - 3 a^4 b^4 c^2 d + 3 a^5 b^3 c d^2 - a^6 b^2 d^3) \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^4,x, algorithm="fricas")

[Out] [1/48*(3*(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) - 2*(8*b^4*c^3 - 22*a*b^3*c^2*d + 17*a^2*b^2*c*d^2 - 3*a^3*b*d^3 - 3*(b^4*c*d^2 - a*b^3*d^3)*x^2 + 2*(b^4*c^2*d - 5*a*b^3*c*d^2 + 4*a^2*b^2*d^3)*x)*sqrt(d*x + c)/(a^3*b^5*c^3 - 3*a^4*b^4*c^2*d + 3*a^5*b^3*c*d^2 - a^6*b^2*d^3 + (b^8*c^3 - 3*a*b^7*c^2*d + 3*a^2*b^6*c*d^2 - a^3*b^5*d^3)*x^3 + 3*(a*b^7*c^3 - 3*a^2*b^6*c^2*d + 3*a^3*b^5*c*d^2 - a^4*b^4*d^3)*x^2 + 3*(a^2*b^6*c^3 - 3*a^3*b^5*c^2*d + 3*a^4*b^4*c*d^2 - a^5*b^3*d^3)*x), 1/24*(3*(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) - (8*b^4*c^3 - 22*a*b^3*c^2*d + 17*a^2*b^2*c*d^2 - 3*a^3*b*d^3 - 3*(b^4*c*d^2 - a*b^3*d^3)*x^2 + 2*(b^4*c^2*d - 5*a*b^3*c*d^2 + 4*a^2*b^2*d^3)*x)*sqrt(d*x + c)/(a^3*b^5*c^3 - 3*a^4*b^4*c^2*d + 3*a^5*b^3*c*d^2 - a^6*b^2*d^3 + (b^8*c^3 - 3*a*b^7*c^2*d + 3*a^2*b^6*c*d^2 - a^3*b^5*d^3)*x^3 + 3*(a*b^7*c^3 - 3*a^2*b^6*c^2*d + 3*a^3*b^5*c*d^2 - a^4*b^4*d^3)*x^2 + 3*(a^2*b^6*c^3 - 3*a^3*b^5*c^2*d + 3*a^4*b^4*c*d^2 - a^5*b^3*d^3)*x)]

giac [A] time = 1.35, size = 207, normalized size = 1.42

$$\frac{d^3 \arctan \left(\frac{\sqrt{d x + c} b}{\sqrt{-b^2 c + a b d}} \right)}{8 \left(b^3 c^2 - 2 a b^2 c d + a^2 b d^2 \right) \sqrt{-b^2 c + a b d}} + \frac{3 (d x + c)^{\frac{5}{2}} b^2 d^3 - 8 (d x + c)^{\frac{3}{2}} b^2 c d^3 - 3 \sqrt{d x + c} b^2 c^2 d^3 + 8 (d x + c)^{\frac{3}{2}} a b d^3}{24 \left(b^3 c^2 - 2 a b^2 c d + a^2 b d^2 \right) \left((d x + c) b - b^2 c + a d \right)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^4,x, algorithm="giac")

[Out] 1/8*d^3*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/((b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*sqrt(-b^2*c + a*b*d)) + 1/24*(3*(d*x + c)^(5/2)*b^2*d^3 - 8*(d*x + c)^(3/2)*b^2*c*d^3 - 3*sqrt(d*x + c)*b^2*c^2*d^3 + 8*(d*x + c)^(3/2)*a*b*d^3 + 6*sqrt(d*x + c)*a*b*c*d^4 - 3*sqrt(d*x + c)*a^2*d^5)/((b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*((d*x + c)*b - b*c + a*d)^3)

maple [A] time = 0.02, size = 170, normalized size = 1.16

$$\frac{(dx+c)^{\frac{5}{2}} b d^3}{8(bdx+ad)^3 (a^2 d^2 - 2abcd + b^2 c^2)} + \frac{d^3 \arctan\left(\frac{\sqrt{dx+c} b}{\sqrt{(ad-bc)b}}\right)}{8(a^2 d^2 - 2abcd + b^2 c^2) \sqrt{(ad-bc)b} b} + \frac{(dx+c)^{\frac{3}{2}} d^3}{3(bdx+ad)^3 (ad-bc)} - \frac{\sqrt{dx+c}}{8(bdx+ad)^3 (ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a)^4, x)

[Out] 1/8*d^3/(b*d*x+a*d)^3*b/(a^2*d^2-2*a*b*c*d+b^2*c^2)*(d*x+c)^(5/2)+1/3*d^3/(b*d*x+a*d)^3/(a*d-b*c)*(d*x+c)^(3/2)-1/8*d^3/(b*d*x+a*d)^3/b*(d*x+c)^(1/2)+1/8*d^3/b/(a^2*d^2-2*a*b*c*d+b^2*c^2)/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^4, x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.37, size = 207, normalized size = 1.42

$$\frac{\frac{d^3 (c+dx)^{3/2}}{3(ad-bc)} - \frac{d^3 \sqrt{c+dx}}{8b} + \frac{bd^3 (c+dx)^{5/2}}{8(ad-bc)^2}}{(c+dx) (3a^2 b d^2 - 6a b^2 c d + 3b^3 c^2) + b^3 (c+dx)^3 - (3b^3 c - 3a b^2 d) (c+dx)^2 + a^3 d^3 - b^3 c^3 + 3a b^2 c^2 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/2)/(a + b*x)^4, x)

[Out] ((d^3*(c + d*x)^(3/2))/(3*(a*d - b*c)) - (d^3*(c + d*x)^(1/2))/(8*b) + (b*d^3*(c + d*x)^(5/2))/(8*(a*d - b*c)^2))/((c + d*x)*(3*b^3*c^2 + 3*a^2*b*d^2 - 6*a*b^2*c*d) + b^3*(c + d*x)^3 - (3*b^3*c - 3*a*b^2*d)*(c + d*x)^2 + a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d) + (d^3*atan((b^(1/2)*(c + d*x)^(1/2))/(a*d - b*c)^(1/2)))/(8*b^(3/2)*(a*d - b*c)^(5/2))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(1/2)/(b*x+a)**4,x)
```

```
[Out] Timed out
```

$$3.1385 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^5} dx$$

Optimal. Leaf size=182

$$\frac{5d^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{64b^{3/2}(bc-ad)^{7/2}} - \frac{5d^3\sqrt{c+dx}}{64b(a+bx)(bc-ad)^3} + \frac{5d^2\sqrt{c+dx}}{96b(a+bx)^2(bc-ad)^2} - \frac{d\sqrt{c+dx}}{24b(a+bx)^3(bc-ad)} - \frac{\sqrt{c+dx}}{4b(a+bx)^4}$$

[Out] $5/64*d^4*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/b^{(3/2)/(-a*d+b*c)^{(7/2)}-1/4*(d*x+c)^{(1/2)/b/(b*x+a)^4-1/24*d*(d*x+c)^{(1/2)/b/(-a*d+b*c)/(b*x+a)^3+5/96*d^2*(d*x+c)^{(1/2)/b/(-a*d+b*c)^2/(b*x+a)^2-5/64*d^3*(d*x+c)^{(1/2)/b/(-a*d+b*c)^3/(b*x+a)}$

Rubi [A] time = 0.12, antiderivative size = 182, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 51, 63, 208}

$$\frac{5d^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{64b^{3/2}(bc-ad)^{7/2}} - \frac{5d^3\sqrt{c+dx}}{64b(a+bx)(bc-ad)^3} + \frac{5d^2\sqrt{c+dx}}{96b(a+bx)^2(bc-ad)^2} - \frac{d\sqrt{c+dx}}{24b(a+bx)^3(bc-ad)} - \frac{\sqrt{c+dx}}{4b(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x)^5, x]

[Out] $-\operatorname{Sqrt}[c + d*x]/(4*b*(a + b*x)^4) - (d*\operatorname{Sqrt}[c + d*x])/(24*b*(b*c - a*d)*(a + b*x)^3) + (5*d^2*\operatorname{Sqrt}[c + d*x])/(96*b*(b*c - a*d)^2*(a + b*x)^2) - (5*d^3*\operatorname{Sqrt}[c + d*x])/(64*b*(b*c - a*d)^3*(a + b*x)) + (5*d^4*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/\operatorname{Sqrt}[b*c - a*d]])/(64*b^{(3/2)}*(b*c - a*d)^{(7/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ

`[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && IntLinearQ[a, b, c, d, m, n, x]`

Rule 63

`Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 208

`Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt{c+dx}}{(a+bx)^5} dx &= -\frac{\sqrt{c+dx}}{4b(a+bx)^4} + \frac{d \int \frac{1}{(a+bx)^4 \sqrt{c+dx}} dx}{8b} \\
 &= -\frac{\sqrt{c+dx}}{4b(a+bx)^4} - \frac{d\sqrt{c+dx}}{24b(bc-ad)(a+bx)^3} - \frac{(5d^2) \int \frac{1}{(a+bx)^3 \sqrt{c+dx}} dx}{48b(bc-ad)} \\
 &= -\frac{\sqrt{c+dx}}{4b(a+bx)^4} - \frac{d\sqrt{c+dx}}{24b(bc-ad)(a+bx)^3} + \frac{5d^2\sqrt{c+dx}}{96b(bc-ad)^2(a+bx)^2} + \frac{(5d^3) \int \frac{1}{(a+bx)^2 \sqrt{c+dx}} dx}{64b(bc-ad)^2} \\
 &= -\frac{\sqrt{c+dx}}{4b(a+bx)^4} - \frac{d\sqrt{c+dx}}{24b(bc-ad)(a+bx)^3} + \frac{5d^2\sqrt{c+dx}}{96b(bc-ad)^2(a+bx)^2} - \frac{5d^3\sqrt{c+dx}}{64b(bc-ad)^3(a+bx)} - \frac{(5d^4) \int \frac{1}{(a+bx) \sqrt{c+dx}} dx}{32b(bc-ad)^3} \\
 &= -\frac{\sqrt{c+dx}}{4b(a+bx)^4} - \frac{d\sqrt{c+dx}}{24b(bc-ad)(a+bx)^3} + \frac{5d^2\sqrt{c+dx}}{96b(bc-ad)^2(a+bx)^2} - \frac{5d^3\sqrt{c+dx}}{64b(bc-ad)^3(a+bx)} - \frac{5d^4\sqrt{c+dx}}{32b(bc-ad)^3} \\
 &= -\frac{\sqrt{c+dx}}{4b(a+bx)^4} - \frac{d\sqrt{c+dx}}{24b(bc-ad)(a+bx)^3} + \frac{5d^2\sqrt{c+dx}}{96b(bc-ad)^2(a+bx)^2} - \frac{5d^3\sqrt{c+dx}}{64b(bc-ad)^3(a+bx)} + \frac{5d^4\sqrt{c+dx}}{32b(bc-ad)^3}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.29

$$\frac{2d^4(c+dx)^{3/2} {}_2F_1\left(\frac{3}{2}, 5; \frac{5}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{3(ad-bc)^5}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*x]/(a + b*x)^5,x]

[Out] (2*d^4*(c + d*x)^(3/2)*Hypergeometric2F1[3/2, 5, 5/2, -((b*(c + d*x))/(-(b*c) + a*d))]/(3*(-(b*c) + a*d)^5)

fricas [B] time = 0.48, size = 1176, normalized size = 6.46

$$\left[\frac{15(b^4d^4x^4 + 4ab^3d^4x^3 + 6a^2b^2d^4x^2 + 4a^3bd^4x + a^4d^4)\sqrt{b^2c - abd} \log\left(\frac{bdx+2bc-ad-2\sqrt{b^2c-abd}\sqrt{dx+c}}{bx+a}\right) + 2(4a^4b^6c^4 - 4a^5b^5c^3d + 6a^6b^4c^2d^2 - 4a^7b^3cd^3 + a^8b^2d^4 + (b^{10}c^4 - 4ab^9c^3d + 6a^2b^8c^2d^2 - 4a^3b^7cd^3 + a^4b^6d^4))\sqrt{b^2c - abd}}{384(b^{10}c^4 - 4ab^9c^3d + 6a^2b^8c^2d^2 - 4a^3b^7cd^3 + a^4b^6d^4)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^5,x, algorithm="fricas")

[Out] [-1/384*(15*(b^4*d^4*x^4 + 4*a*b^3*d^4*x^3 + 6*a^2*b^2*d^4*x^2 + 4*a^3*b*d^4*x + a^4*d^4)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) + 2*(48*b^5*c^4 - 184*a*b^4*c^3*d + 254*a^2*b^3*c^2*d^2 - 133*a^3*b^2*c*d^3 + 15*a^4*b*d^4 + 15*(b^5*c*d^3 - a*b^4*d^4)*x^3 - 5*(2*b^5*c^2*d^2 - 13*a*b^4*c*d^3 + 11*a^2*b^3*d^4)*x^2 + (8*b^5*c^3*d - 44*a*b^4*c^2*d^2 + 109*a^2*b^3*c*d^3 - 73*a^3*b^2*d^4)*x)*sqrt(d*x + c))/(a^4*b^6*c^4 - 4*a^5*b^5*c^3*d + 6*a^6*b^4*c^2*d^2 - 4*a^7*b^3*c*d^3 + a^8*b^2*d^4 + (b^10*c^4 - 4*a*b^9*c^3*d + 6*a^2*b^8*c^2*d^2 - 4*a^3*b^7*c*d^3 + a^4*b^6*d^4)*x^4 + 4*(a*b^9*c^4 - 4*a^2*b^8*c^3*d + 6*a^3*b^7*c^2*d^2 - 4*a^4*b^6*c*d^3 + a^5*b^5*d^4)*x^3 + 6*(a^2*b^8*c^4 - 4*a^3*b^7*c^3*d + 6*a^4*b^6*c^2*d^2 - 4*a^5*b^5*c*d^3 + a^6*b^4*d^4)*x^2 + 4*(a^3*b^7*c^4 - 4*a^4*b^6*c^3*d + 6*a^5*b^5*c^2*d^2 - 4*a^6*b^4*c*d^3 + a^7*b^3*d^4)*x), -1/192*(15*(b^4*d^4*x^4 + 4*a*b^3*d^4*x^3 + 6*a^2*b^2*d^4*x^2 + 4*a^3*b*d^4*x + a^4*d^4)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) + (48*b^5*c^4 - 184*a*b^4*c^3*d + 254*a^2*b^3*c^2*d^2 - 133*a^3*b^2*c*d^3 + 15*a^4*b*d^4 + 15*(b^5*c*d^3 - a*b^4*d^4)*x^3 - 5*(2*b^5*c^2*d^2 - 13*a*b^4*c*d^3 + 11*a^2*b^3*d^4)*x^2 + (8*b^5*c^3*d - 44*a*b^4*c^2*d^2 + 109*a^2*b^3*c*d^3 - 73*a^3*b^2*d^4)*x)*sqrt(d*x + c))/(a^4*b^6*c^4 - 4*a^5*b^5*c^3*d + 6*a^6*b^4*c^2*d^2 - 4*a^7*b^3*c*d^3 + a^8*b^2*d^4 + (b^10*c^4 - 4*a*b^9*c^3*d + 6*a^2*b^8*c^2*d^2 - 4*a^3*b^7*c*d^3 + a^4*b^6*d^4)*x^4 + 4*(a*b^9*c^4 - 4*a^2*b^8*c^3*d + 6*a^3*b^7*c^2*d^2 - 4*a^4*b^6*c*d^3 + a^5*b^5*d^4)*x^3 + 6*(a^2*b^8*c^4 - 4*a^3*b^7*c^3*d + 6*a^4*b^6*c^2*d^2 - 4*a^5*b^5*c*d^3 + a^6*b^4*d^4)*x^2 + 4*(a^3*b^7*c^4 - 4*a^4*b^6*c^3*d + 6*a^5*b^5*c^2*d^2 - 4*a^6*b^4*c*d^3 + a^7*b^3*d^4)*x)]

giac [B] time = 1.39, size = 311, normalized size = 1.71

$$\frac{5d^4 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{64(b^4c^3 - 3ab^3c^2d + 3a^2b^2cd^2 - a^3bd^3)\sqrt{-b^2c+abd}} + \frac{15(dx+c)^{\frac{7}{2}}b^3d^4 - 55(dx+c)^{\frac{5}{2}}b^3cd^4 + 73(dx+c)^{\frac{3}{2}}b^3c^2d^4}{64(b^4c^3 - 3ab^3c^2d + 3a^2b^2cd^2 - a^3bd^3)\sqrt{-b^2c+abd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^5,x, algorithm="giac")

[Out]
$$-5/64*d^4*\arctan(\sqrt{d*x+c}*b/\sqrt{-b^2*c+a*b*d})/((b^4*c^3-3*a*b^3*c^2*d+3*a^2*b^2*c*d^2-a^3*b*d^3)*\sqrt{-b^2*c+a*b*d})-1/192*(15*(d*x+c)^{(7/2)}*b^3*d^4-55*(d*x+c)^{(5/2)}*b^3*c*d^4+73*(d*x+c)^{(3/2)}*b^3*c^2*d^4+15*\sqrt{d*x+c}*b^3*c^3*d^4+55*(d*x+c)^{(5/2)}*a*b^2*d^5-14*6*(d*x+c)^{(3/2)}*a*b^2*c*d^5-45*\sqrt{d*x+c}*a*b^2*c^2*d^5+73*(d*x+c)^{(3/2)}*a^2*b*d^6+45*\sqrt{d*x+c}*a^2*b*c*d^6-15*\sqrt{d*x+c}*a^3*d^7)/((b^4*c^3-3*a*b^3*c^2*d+3*a^2*b^2*c*d^2-a^3*b*d^3)*((d*x+c)*b-b*c+a*d)^4)$$

maple [A] time = 0.02, size = 248, normalized size = 1.36

$$\frac{5(dx+c)^{\frac{7}{2}}b^2d^4}{64(bdx+ad)^4(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)} + \frac{55(dx+c)^{\frac{5}{2}}bd^4}{192(bdx+ad)^4(a^2d^2-2abcd+b^2c^2)} + \frac{5d^4a}{64(a^3d^3-3a^2bcd^2-b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a)^5,x)

[Out]
$$5/64*d^4/(b*d*x+a*d)^4*b^2/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)*(d*x+c)^{(7/2)}+55/192*d^4/(b*d*x+a*d)^4*b/(a^2*d^2-2*a*b*c*d+b^2*c^2)*(d*x+c)^{(5/2)}+73/192*d^4/(b*d*x+a*d)^4/(a*d-b*c)*(d*x+c)^{(3/2)}-5/64*d^4/(b*d*x+a*d)^4/b*(d*x+c)^{(1/2)}+5/64*d^4/b/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2})/((a*d-b*c)*b)^{(1/2)}*b)$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^5,x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.22, size = 297, normalized size = 1.63

$$\frac{73d^4(c+dx)^{3/2}}{192(ad-bc)} - \frac{5d^4\sqrt{c+dx}}{64b} + \frac{5b^2d^4(c+dx)^7}{64(ad-bc)^3}$$

$$b^4(c+dx)^4 - (4b^4c - 4ab^3d)(c+dx)^3 - (c+dx)(-4a^3bd^3 + 12a^2b^2cd^2 - 12ab^3c^2d + 4b^4c^3) + a^4d^4 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/2)/(a + b*x)^5,x)

[Out] ((73*d^4*(c + d*x)^(3/2))/(192*(a*d - b*c)) - (5*d^4*(c + d*x)^(1/2))/(64*b) + (5*b^2*d^4*(c + d*x)^(7/2))/(64*(a*d - b*c)^3) + (55*b*d^4*(c + d*x)^(5/2))/(192*(a*d - b*c)^2))/(b^4*(c + d*x)^4 - (4*b^4*c - 4*a*b^3*d)*(c + d*x)^3 - (c + d*x)*(4*b^4*c^3 - 4*a^3*b*d^3 + 12*a^2*b^2*c*d^2 - 12*a*b^3*c^2*d) + a^4*d^4 + b^4*c^4 + (c + d*x)^2*(6*b^4*c^2 + 6*a^2*b^2*d^2 - 12*a*b^3*c*d) + 6*a^2*b^2*c^2*d^2 - 4*a*b^3*c^3*d - 4*a^3*b*c*d^3) + (5*d^4*atan((b^(1/2)*(c + d*x)^(1/2))/(a*d - b*c)^(1/2)))/(64*b^(3/2)*(a*d - b*c)^(7/2))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/2)/(b*x+a)**5,x)

[Out] Timed out

$$3.1386 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^6} dx$$

Optimal. Leaf size=218

$$-\frac{7d^5 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{128b^{3/2}(bc-ad)^{9/2}} + \frac{7d^4\sqrt{c+dx}}{128b(a+bx)(bc-ad)^4} - \frac{7d^3\sqrt{c+dx}}{192b(a+bx)^2(bc-ad)^3} + \frac{7d^2\sqrt{c+dx}}{240b(a+bx)^3(bc-ad)^2} - \frac{d\sqrt{c+dx}}{40b(a+bx)^4}$$

[Out] $-7/128*d^5*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/b^{(3/2)/(-a*d+b*c)^{(9/2)}-1/5*(d*x+c)^{(1/2)/b/(b*x+a)^5-1/40*d*(d*x+c)^{(1/2)/b/(-a*d+b*c)/(b*x+a)^4+7/240*d^2*(d*x+c)^{(1/2)/b/(-a*d+b*c)^2/(b*x+a)^3-7/192*d^3*(d*x+c)^{(1/2)/b/(-a*d+b*c)^3/(b*x+a)^2+7/128*d^4*(d*x+c)^{(1/2)/b/(-a*d+b*c)^4/(b*x+a)}$

Rubi [A] time = 0.15, antiderivative size = 218, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 51, 63, 208}

$$-\frac{7d^5 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{128b^{3/2}(bc-ad)^{9/2}} + \frac{7d^4\sqrt{c+dx}}{128b(a+bx)(bc-ad)^4} - \frac{7d^3\sqrt{c+dx}}{192b(a+bx)^2(bc-ad)^3} + \frac{7d^2\sqrt{c+dx}}{240b(a+bx)^3(bc-ad)^2} - \frac{d\sqrt{c+dx}}{40b(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x)^6, x]

[Out] $-\operatorname{Sqrt}[c + d*x]/(5*b*(a + b*x)^5) - (d*\operatorname{Sqrt}[c + d*x])/(40*b*(b*c - a*d)*(a + b*x)^4) + (7*d^2*\operatorname{Sqrt}[c + d*x])/(240*b*(b*c - a*d)^2*(a + b*x)^3) - (7*d^3*\operatorname{Sqrt}[c + d*x])/(192*b*(b*c - a*d)^3*(a + b*x)^2) + (7*d^4*\operatorname{Sqrt}[c + d*x])/(128*b*(b*c - a*d)^4*(a + b*x)) - (7*d^5*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/\operatorname{Sqrt}[b*c - a*d]])/(128*b^{(3/2)}*(b*c - a*d)^{(9/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(

$m + n + 2) / ((b*c - a*d)*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x], x$
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
 [n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
 ntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] := \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 208

$\text{Int}[(a + b*x)^{-1}, x_Symbol] := \text{Simp}[(\text{Rt}[-(a/b), 2]*\text{ArcTanh}[x/\text{Rt}[-(a/b), 2]])/a, x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{NegQ}[a/b]$

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{c+dx}}{(a+bx)^6} dx &= -\frac{\sqrt{c+dx}}{5b(a+bx)^5} + \frac{d \int \frac{1}{(a+bx)^5 \sqrt{c+dx}} dx}{10b} \\ &= -\frac{\sqrt{c+dx}}{5b(a+bx)^5} - \frac{d\sqrt{c+dx}}{40b(bc-ad)(a+bx)^4} - \frac{(7d^2) \int \frac{1}{(a+bx)^4 \sqrt{c+dx}} dx}{80b(bc-ad)} \\ &= -\frac{\sqrt{c+dx}}{5b(a+bx)^5} - \frac{d\sqrt{c+dx}}{40b(bc-ad)(a+bx)^4} + \frac{7d^2\sqrt{c+dx}}{240b(bc-ad)^2(a+bx)^3} + \frac{(7d^3) \int \frac{1}{(a+bx)^3 \sqrt{c+dx}} dx}{96b(bc-ad)^2} \\ &= -\frac{\sqrt{c+dx}}{5b(a+bx)^5} - \frac{d\sqrt{c+dx}}{40b(bc-ad)(a+bx)^4} + \frac{7d^2\sqrt{c+dx}}{240b(bc-ad)^2(a+bx)^3} - \frac{7d^3\sqrt{c+dx}}{192b(bc-ad)^3(a+bx)^2} \\ &= -\frac{\sqrt{c+dx}}{5b(a+bx)^5} - \frac{d\sqrt{c+dx}}{40b(bc-ad)(a+bx)^4} + \frac{7d^2\sqrt{c+dx}}{240b(bc-ad)^2(a+bx)^3} - \frac{7d^3\sqrt{c+dx}}{192b(bc-ad)^3(a+bx)^2} \\ &= -\frac{\sqrt{c+dx}}{5b(a+bx)^5} - \frac{d\sqrt{c+dx}}{40b(bc-ad)(a+bx)^4} + \frac{7d^2\sqrt{c+dx}}{240b(bc-ad)^2(a+bx)^3} - \frac{7d^3\sqrt{c+dx}}{192b(bc-ad)^3(a+bx)^2} \\ &= -\frac{\sqrt{c+dx}}{5b(a+bx)^5} - \frac{d\sqrt{c+dx}}{40b(bc-ad)(a+bx)^4} + \frac{7d^2\sqrt{c+dx}}{240b(bc-ad)^2(a+bx)^3} - \frac{7d^3\sqrt{c+dx}}{192b(bc-ad)^3(a+bx)^2} \end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.24

$$\frac{2d^5(c+dx)^{3/2} {}_2F_1\left(\frac{3}{2}, 6; \frac{5}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{3(ad-bc)^6}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*x]/(a + b*x)^6, x]

[Out] (2*d^5*(c + d*x)^(3/2)*Hypergeometric2F1[3/2, 6, 5/2, -((b*(c + d*x))/(-(b*c) + a*d)))]/(3*(-(b*c) + a*d)^6)

fricas [B] time = 0.50, size = 1673, normalized size = 7.67

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^6, x, algorithm="fricas")

[Out] [1/3840*(105*(b^5*d^5*x^5 + 5*a*b^4*d^5*x^4 + 10*a^2*b^3*d^5*x^3 + 10*a^3*b^2*d^5*x^2 + 5*a^4*b*d^5*x + a^5*d^5)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) - 2*(384*b^6*c^5 - 1872*a*b^5*c^4*d + 3592*a^2*b^4*c^3*d^2 - 3314*a^3*b^3*c^2*d^3 + 1315*a^4*b^2*c*d^4 - 105*a^5*b*d^5 - 105*(b^6*c*d^4 - a*b^5*d^5)*x^4 + 70*(b^6*c^2*d^3 - 8*a*b^5*c*d^4 + 7*a^2*b^4*d^5)*x^3 - 14*(4*b^6*c^3*d^2 - 27*a*b^5*c^2*d^3 + 87*a^2*b^4*c*d^4 - 64*a^3*b^3*d^5)*x^2 + 2*(24*b^6*c^4*d - 152*a*b^5*c^3*d^2 + 417*a^2*b^4*c^2*d^3 - 684*a^3*b^3*c*d^4 + 395*a^4*b^2*d^5)*x)*sqrt(d*x + c))/(a^5*b^7*c^5 - 5*a^6*b^6*c^4*d + 10*a^7*b^5*c^3*d^2 - 10*a^8*b^4*c^2*d^3 + 5*a^9*b^3*c*d^4 - a^10*b^2*d^5 + (b^12*c^5 - 5*a*b^11*c^4*d + 10*a^2*b^10*c^3*d^2 - 10*a^3*b^9*c^2*d^3 + 5*a^4*b^8*c*d^4 - a^5*b^7*d^5)*x^5 + 5*(a*b^11*c^5 - 5*a^2*b^10*c^4*d + 10*a^3*b^9*c^3*d^2 - 10*a^4*b^8*c^2*d^3 + 5*a^5*b^7*c*d^4 - a^6*b^6*d^5)*x^4 + 10*(a^2*b^10*c^5 - 5*a^3*b^9*c^4*d + 10*a^4*b^8*c^3*d^2 - 10*a^5*b^7*c^2*d^3 + 5*a^6*b^6*c*d^4 - a^7*b^5*d^5)*x^3 + 10*(a^3*b^9*c^5 - 5*a^4*b^8*c^4*d + 10*a^5*b^7*c^3*d^2 - 10*a^6*b^6*c^2*d^3 + 5*a^7*b^5*c*d^4 - a^8*b^4*d^5)*x^2 + 5*(a^4*b^8*c^5 - 5*a^5*b^7*c^4*d + 10*a^6*b^6*c^3*d^2 - 10*a^7*b^5*c^2*d^3 + 5*a^8*b^4*c*d^4 - a^9*b^3*d^5)*x), 1/1920*(105*(b^5*d^5*x^5 + 5*a*b^4*d^5*x^4 + 10*a^2*b^3*d^5*x^3 + 10*a^3*b^2*d^5*x^2 + 5*a^4*b*d^5*x + a^5*d^5)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) - (384*b^6*c^5 - 1872*a*b^5*c^4*d + 3592*a^2*b^4*c^3*d^2 - 3314*a^3*b^3*c^2*d^3 + 1315*a^4*b^2*c*d^4 - 105*a^5*b*d^5 - 105*(b^6*c*d^4 - a*b^5*d^5)*x^4 + 70*(b^6*c^2*d^3 - 8*a*b^5*c*d^4 + 7*a^2*b^4*d^5)*x^3 - 14*(4*b^6*c^3*d^2 - 27*a*b^5*c^2*d^3 + 87*a^2*b^4*c*d^4 - 64*a^3*b^3*d^5)*x^2 + 2*(24*b^6*c^4*d - 152*a*b^5*c^3*d^2 + 417*a^2*b^4*c^2*d^3 - 684*a^3*b^3*c*d^4 + 395*a^4*b^2*d^5)*x)*sqrt(d*x +

c)) / (a^5*b^7*c^5 - 5*a^6*b^6*c^4*d + 10*a^7*b^5*c^3*d^2 - 10*a^8*b^4*c^2*d^3 + 5*a^9*b^3*c*d^4 - a^10*b^2*d^5 + (b^12*c^5 - 5*a*b^11*c^4*d + 10*a^2*b^10*c^3*d^2 - 10*a^3*b^9*c^2*d^3 + 5*a^4*b^8*c*d^4 - a^5*b^7*d^5)*x^5 + 5*(a*b^11*c^5 - 5*a^2*b^10*c^4*d + 10*a^3*b^9*c^3*d^2 - 10*a^4*b^8*c^2*d^3 + 5*a^5*b^7*c*d^4 - a^6*b^6*d^5)*x^4 + 10*(a^2*b^10*c^5 - 5*a^3*b^9*c^4*d + 10*a^4*b^8*c^3*d^2 - 10*a^5*b^7*c^2*d^3 + 5*a^6*b^6*c*d^4 - a^7*b^5*d^5)*x^3 + 10*(a^3*b^9*c^5 - 5*a^4*b^8*c^4*d + 10*a^5*b^7*c^3*d^2 - 10*a^6*b^6*c^2*d^3 + 5*a^7*b^5*c*d^4 - a^8*b^4*d^5)*x^2 + 5*(a^4*b^8*c^5 - 5*a^5*b^7*c^4*d + 10*a^6*b^6*c^3*d^2 - 10*a^7*b^5*c^2*d^3 + 5*a^8*b^4*c*d^4 - a^9*b^3*d^5)*x)]

giac [B] time = 1.47, size = 432, normalized size = 1.98

$$\frac{7d^5 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{128(b^5c^4 - 4ab^4c^3d + 6a^2b^3c^2d^2 - 4a^3b^2cd^3 + a^4bd^4)\sqrt{-b^2c+abd}} + \frac{105(dx+c)^{\frac{9}{2}}b^4d^5 - 490(dx+c)^{\frac{7}{2}}b^4cd^5 + \dots}{128(bdx+ad)^5(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)} + \frac{49(dx+c)^{\frac{7}{2}}b^2d^5}{192(bdx+ad)^5(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - \dots)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^6,x, algorithm="giac")

[Out] 7/128*d^5*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/((b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)*sqrt(-b^2*c + a*b*d)) + 1/1920*(105*(d*x + c)^(9/2)*b^4*d^5 - 490*(d*x + c)^(7/2)*b^4*c*d^5 + 896*(d*x + c)^(5/2)*b^4*c^2*d^5 - 790*(d*x + c)^(3/2)*b^4*c^3*d^5 - 105*sqrt(d*x + c)*b^4*c^4*d^5 + 490*(d*x + c)^(7/2)*a*b^3*d^6 - 1792*(d*x + c)^(5/2)*a*b^3*c*d^6 + 2370*(d*x + c)^(3/2)*a*b^3*c^2*d^6 + 420*sqrt(d*x + c)*a*b^3*c^3*d^6 + 896*(d*x + c)^(5/2)*a^2*b^2*d^7 - 2370*(d*x + c)^(3/2)*a^2*b^2*c*d^7 - 630*sqrt(d*x + c)*a^2*b^2*c^2*d^7 + 790*(d*x + c)^(3/2)*a^3*b*d^8 + 420*sqrt(d*x + c)*a^3*b*c*d^8 - 105*sqrt(d*x + c)*a^4*d^9)/((b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)*((d*x + c)*b - b*c + a*d)^5)

maple [A] time = 0.02, size = 337, normalized size = 1.55

$$\frac{7(dx+c)^{\frac{9}{2}}b^3d^5}{128(bdx+ad)^5(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)} + \frac{49(dx+c)^{\frac{7}{2}}b^2d^5}{192(bdx+ad)^5(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - \dots)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a)^6,x)

[Out] 7/128*d^5/(b*d*x+a*d)^5*b^3/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)*(d*x+c)^(9/2)+49/192*d^5/(b*d*x+a*d)^5*b^2/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)*(d*x+c)^(7/2)+7/15*d^5/(b*d*x+a*d)^5*b/(a^2*

$$d^2 - 2*a*b*c*d + b^2*c^2) * (d*x+c)^{(5/2)} + 79/192*d^5/(b*d*x+a*d)^5/(a*d-b*c) * (d*x+c)^{(3/2)} - 7/128*d^5/(b*d*x+a*d)^5/b*(d*x+c)^{(1/2)} + 7/128*d^5/b/(a^4*d^4 - 4*a^3*b*c*d^3 + 6*a^2*b^2*c^2*d^2 - 4*a*b^3*c^3*d + b^4*c^4)/((a*d-b*c)*b)^{(1/2)} * \arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^6,x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.49, size = 401, normalized size = 1.84

$$\frac{b^5(c+dx)^5 - (c+dx)^2(-10a^3b^2d^3 + 30a^2b^3cd^2 - 30ab^4c^2d + 10b^5c^3) - (5b^5c - 5ab^4d)(c+dx)^4 + a^5d^5}{(a+bx)^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/2)/(a + b*x)^6,x)

[Out] ((79*d^5*(c + d*x)^(3/2))/(192*(a*d - b*c)) - (7*d^5*(c + d*x)^(1/2))/(128*b) + (49*b^2*d^5*(c + d*x)^(7/2))/(192*(a*d - b*c)^3) + (7*b^3*d^5*(c + d*x)^(9/2))/(128*(a*d - b*c)^4) + (7*b*d^5*(c + d*x)^(5/2))/(15*(a*d - b*c)^2) + (b^5*(c + d*x)^5 - (c + d*x)^2*(10*b^5*c^3 - 10*a^3*b^2*d^3 + 30*a^2*b^3*c*d^2 - 30*a*b^4*c^2*d) - (5*b^5*c - 5*a*b^4*d)*(c + d*x)^4 + a^5*d^5 - b^5*c^5 + (c + d*x)^3*(10*b^5*c^2 + 10*a^2*b^3*d^2 - 20*a*b^4*c*d) + (c + d*x)*(5*b^5*c^4 + 5*a^4*b*d^4 - 20*a^3*b^2*c*d^3 + 30*a^2*b^3*c^2*d^2 - 20*a*b^4*c^3*d) - 10*a^2*b^3*c^3*d^2 + 10*a^3*b^2*c^2*d^3 + 5*a*b^4*c^4*d - 5*a^4*b*c*d^4) + (7*d^5*atan((b^(1/2)*(c + d*x)^(1/2))/(a*d - b*c)^(1/2)))/(128*b^(3/2)*(a*d - b*c)^(9/2))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/2)/(b*x+a)**6,x)

[Out] Timed out

3.1387 $\int (a + bx)^5 (c + dx)^{3/2} dx$

Optimal. Leaf size=158

$$\frac{10b^4(c + dx)^{13/2}(bc - ad)}{13d^6} + \frac{20b^3(c + dx)^{11/2}(bc - ad)^2}{11d^6} - \frac{20b^2(c + dx)^{9/2}(bc - ad)^3}{9d^6} + \frac{10b(c + dx)^{7/2}(bc - ad)^4}{7d^6} - \frac{2(c + dx)^{5/2}(bc - ad)^5}{5d^6}$$

[Out] $-2/5*(-a*d+b*c)^5*(d*x+c)^(5/2)/d^6+10/7*b*(-a*d+b*c)^4*(d*x+c)^(7/2)/d^6-20/9*b^2*(-a*d+b*c)^3*(d*x+c)^(9/2)/d^6+20/11*b^3*(-a*d+b*c)^2*(d*x+c)^(11/2)/d^6-10/13*b^4*(-a*d+b*c)*(d*x+c)^(13/2)/d^6+2/15*b^5*(d*x+c)^(15/2)/d^6$

Rubi [A] time = 0.05, antiderivative size = 158, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{10b^4(c + dx)^{13/2}(bc - ad)}{13d^6} + \frac{20b^3(c + dx)^{11/2}(bc - ad)^2}{11d^6} - \frac{20b^2(c + dx)^{9/2}(bc - ad)^3}{9d^6} + \frac{10b(c + dx)^{7/2}(bc - ad)^4}{7d^6} - \frac{2(c + dx)^{5/2}(bc - ad)^5}{5d^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*(c + d*x)^(3/2), x]

[Out] $(-2*(b*c - a*d)^5*(c + d*x)^(5/2))/(5*d^6) + (10*b*(b*c - a*d)^4*(c + d*x)^(7/2))/(7*d^6) - (20*b^2*(b*c - a*d)^3*(c + d*x)^(9/2))/(9*d^6) + (20*b^3*(b*c - a*d)^2*(c + d*x)^(11/2))/(11*d^6) - (10*b^4*(b*c - a*d)*(c + d*x)^(13/2))/(13*d^6) + (2*b^5*(c + d*x)^(15/2))/(15*d^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^5 (c + dx)^{3/2} dx &= \int \left(\frac{(-bc + ad)^5 (c + dx)^{3/2}}{d^5} + \frac{5b(bc - ad)^4 (c + dx)^{5/2}}{d^5} - \frac{10b^2(bc - ad)^3 (c + dx)^{7/2}}{d^5} + \frac{10b^3(bc - ad)^2 (c + dx)^{9/2}}{d^5} - \frac{5b^4(bc - ad) (c + dx)^{11/2}}{d^5} + \frac{b^5 (c + dx)^{13/2}}{d^5} \right) dx \\ &= -\frac{2(bc - ad)^5 (c + dx)^{5/2}}{5d^6} + \frac{10b(bc - ad)^4 (c + dx)^{7/2}}{7d^6} - \frac{20b^2(bc - ad)^3 (c + dx)^{9/2}}{9d^6} + \frac{20b^3(bc - ad)^2 (c + dx)^{11/2}}{11d^6} - \frac{10b^4(bc - ad) (c + dx)^{13/2}}{13d^6} + \frac{2b^5 (c + dx)^{15/2}}{15d^6} \end{aligned}$$

Mathematica [A] time = 0.15, size = 123, normalized size = 0.78

$$\frac{2(c + dx)^{5/2} \left(-17325b^4(c + dx)^4(bc - ad) + 40950b^3(c + dx)^3(bc - ad)^2 - 50050b^2(c + dx)^2(bc - ad)^3 + 32175b(c + dx)(bc - ad)^4 - 2(bc - ad)^5 \right)}{45045d^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*(c + d*x)^(3/2),x]

[Out] $(2*(c + d*x)^{(5/2)}*(-9009*(b*c - a*d)^5 + 32175*b*(b*c - a*d)^4*(c + d*x) - 50050*b^2*(b*c - a*d)^3*(c + d*x)^2 + 40950*b^3*(b*c - a*d)^2*(c + d*x)^3 - 17325*b^4*(b*c - a*d)*(c + d*x)^4 + 3003*b^5*(c + d*x)^5))/(45045*d^6)$

fricas [B] time = 0.44, size = 418, normalized size = 2.65

$$2 \left(3003 b^5 d^7 x^7 - 256 b^5 c^7 + 1920 a b^4 c^6 d - 6240 a^2 b^3 c^5 d^2 + 11440 a^3 b^2 c^4 d^3 - 12870 a^4 b c^3 d^4 + 9009 a^5 c^2 d^5 + 231 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^(3/2),x, algorithm="fricas")

[Out] $2/45045*(3003*b^5*d^7*x^7 - 256*b^5*c^7 + 1920*a*b^4*c^6*d - 6240*a^2*b^3*c^5*d^2 + 11440*a^3*b^2*c^4*d^3 - 12870*a^4*b*c^3*d^4 + 9009*a^5*c^2*d^5 + 231*(16*b^5*c*d^6 + 75*a*b^4*d^7)*x^6 + 63*(b^5*c^2*d^5 + 350*a*b^4*c*d^6 + 650*a^2*b^3*d^7)*x^5 - 35*(2*b^5*c^3*d^4 - 15*a*b^4*c^2*d^5 - 1560*a^2*b^3*c*d^6 - 1430*a^3*b^2*d^7)*x^4 + 5*(16*b^5*c^4*d^3 - 120*a*b^4*c^3*d^4 + 390*a^2*b^3*c^2*d^5 + 14300*a^3*b^2*c*d^6 + 6435*a^4*b*d^7)*x^3 - 3*(32*b^5*c^5*d^2 - 240*a*b^4*c^4*d^3 + 780*a^2*b^3*c^3*d^4 - 1430*a^3*b^2*c^2*d^5 - 17160*a^4*b*c*d^6 - 3003*a^5*d^7)*x^2 + (128*b^5*c^6*d - 960*a*b^4*c^5*d^2 + 3120*a^2*b^3*c^4*d^3 - 5720*a^3*b^2*c^3*d^4 + 6435*a^4*b*c^2*d^5 + 18018*a^5*c*d^6)*x)*sqrt(d*x + c)/d^6$

giac [B] time = 1.53, size = 1084, normalized size = 6.86

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^(3/2),x, algorithm="giac")

[Out] $2/45045*(45045*sqrt(d*x + c)*a^5*c^2 + 30030*((d*x + c)^{(3/2)} - 3*sqrt(d*x + c)*c)*a^5*c + 75075*((d*x + c)^{(3/2)} - 3*sqrt(d*x + c)*c)*a^4*b*c^2/d + 3003*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a^5 + 30030*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a^3*b^2*c^2/d^2 + 30030*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a^4*b*c/d + 12870*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a^2*b^3*c^2/d^3 + 25740*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a^3*b^2*c/d^2 + 6435*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a^4*b/d + 715*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3)*a^5/d$

$$\begin{aligned} & \frac{3}{2}c^3 + 315\sqrt{dx+c}c^4 * a^2 b^4 c^2 / d^4 + 2860(35(dx+c)^{9/2} \\ & - 180(dx+c)^{7/2}c + 378(dx+c)^{5/2}c^2 - 420(dx+c)^{3/2}c^3 \\ & + 315\sqrt{dx+c}c^4) * a^2 b^3 c / d^3 + 1430(35(dx+c)^{9/2} - 180(dx \\ & *x+c)^{7/2}c + 378(dx+c)^{5/2}c^2 - 420(dx+c)^{3/2}c^3 + 315\sqrt{ \\ & dx+c}c^4) * a^3 b^2 / d^2 + 65(63(dx+c)^{11/2} - 385(dx+c)^{9/2} \\ & *c + 990(dx+c)^{7/2}c^2 - 1386(dx+c)^{5/2}c^3 + 1155(dx+c)^{ \\ & (3/2)}c^4 - 693\sqrt{dx+c}c^5) * b^5 c^2 / d^5 + 650(63(dx+c)^{11/2} - \\ & 385(dx+c)^{9/2}c + 990(dx+c)^{7/2}c^2 - 1386(dx+c)^{5/2}c^3 \\ & + 1155(dx+c)^{3/2}c^4 - 693\sqrt{dx+c}c^5) * a^2 b^4 c / d^4 + 650(63 \\ & (dx+c)^{11/2} - 385(dx+c)^{9/2}c + 990(dx+c)^{7/2}c^2 - 1386(dx \\ & *x+c)^{5/2}c^3 + 1155(dx+c)^{3/2}c^4 - 693\sqrt{dx+c}c^5) * a^2 \\ & b^3 / d^3 + 30(231(dx+c)^{13/2} - 1638(dx+c)^{11/2}c + 5005(dx+c) \\ & ^{9/2}c^2 - 8580(dx+c)^{7/2}c^3 + 9009(dx+c)^{5/2}c^4 - 6006(dx \\ & *x+c)^{3/2}c^5 + 3003\sqrt{dx+c}c^6) * b^5 c / d^5 + 75(231(dx+c)^{ \\ & (13/2)} - 1638(dx+c)^{11/2}c + 5005(dx+c)^{9/2}c^2 - 8580(dx+c) \\ &)^{7/2}c^3 + 9009(dx+c)^{5/2}c^4 - 6006(dx+c)^{3/2}c^5 + 3003\sqrt{ \\ & dx+c}c^6) * a^2 b^4 / d^4 + 7(429(dx+c)^{15/2} - 3465(dx+c)^{13/2} \\ &) * c + 12285(dx+c)^{11/2}c^2 - 25025(dx+c)^{9/2}c^3 + 32175(dx+c) \\ & ^{7/2}c^4 - 27027(dx+c)^{5/2}c^5 + 15015(dx+c)^{3/2}c^6 - 643 \\ & 5\sqrt{dx+c}c^7) * b^5 / d^5) / d \end{aligned}$$

maple [B] time = 0.01, size = 273, normalized size = 1.73

$$\frac{2(dx+c)^{\frac{5}{2}} \left(3003b^5x^5d^5 + 17325ab^4d^5x^4 - 2310b^5cd^4x^4 + 40950a^2b^3d^5x^3 - 12600ab^4cd^4x^3 + 1680b^5c^2d^3x^3 + \dots \right)}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5*(d*x+c)^(3/2),x)

[Out] $\frac{2}{45045}(dx+c)^{5/2} * (3003b^5d^5x^5 + 17325ab^4d^5x^4 - 2310b^5cd^4x^4 + 40950a^2b^3d^5x^3 - 12600ab^4cd^4x^3 + 1680b^5c^2d^3x^3 + 50050a^3b^2d^5x^2 - 27300a^2b^3cd^4x^2 + 8400ab^4c^2d^3x^2 - 1120b^5c^3d^2x^2 + 32175a^4b^3d^5x - 28600a^3b^2cd^4x + 15600a^2b^3c^2d^3x - 4800ab^4c^3d^2x + 640b^5c^4d^2x + 9009a^5d^5 - 12870a^4b^3cd^4 + 11440a^3b^2c^2d^3 - 6240a^2b^3c^3d^2 + 1920ab^4c^4d - 256b^5c^5) / d^6$

maxima [A] time = 1.35, size = 259, normalized size = 1.64

$$\frac{2 \left(3003(dx+c)^{\frac{15}{2}}b^5 - 17325(b^5c - ab^4d)(dx+c)^{\frac{13}{2}} + 40950(b^5c^2 - 2ab^4cd + a^2b^3d^2)(dx+c)^{\frac{11}{2}} - 50050(b^5c^3 \dots \right)}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^(3/2),x, algorithm="maxima")

[Out] $\frac{2}{45045} \cdot (3003 \cdot (d \cdot x + c)^{(15/2)} \cdot b^5 - 17325 \cdot (b^5 \cdot c - a \cdot b^4 \cdot d) \cdot (d \cdot x + c)^{(13/2)} + 40950 \cdot (b^5 \cdot c^2 - 2 \cdot a \cdot b^4 \cdot c \cdot d + a^2 \cdot b^3 \cdot d^2) \cdot (d \cdot x + c)^{(11/2)} - 50050 \cdot (b^5 \cdot c^3 - 3 \cdot a \cdot b^4 \cdot c^2 \cdot d + 3 \cdot a^2 \cdot b^3 \cdot c \cdot d^2 - a^3 \cdot b^2 \cdot d^3) \cdot (d \cdot x + c)^{(9/2)} + 32175 \cdot (b^5 \cdot c^4 - 4 \cdot a \cdot b^4 \cdot c^3 \cdot d + 6 \cdot a^2 \cdot b^3 \cdot c^2 \cdot d^2 - 4 \cdot a^3 \cdot b^2 \cdot c \cdot d^3 + a^4 \cdot b \cdot d^4) \cdot (d \cdot x + c)^{(7/2)} - 9009 \cdot (b^5 \cdot c^5 - 5 \cdot a \cdot b^4 \cdot c^4 \cdot d + 10 \cdot a^2 \cdot b^3 \cdot c^3 \cdot d^2 - 10 \cdot a^3 \cdot b^2 \cdot c^2 \cdot d^3 + 5 \cdot a^4 \cdot b \cdot c \cdot d^4 - a^5 \cdot d^5) \cdot (d \cdot x + c)^{(5/2)}) / d^6$

mupad [B] time = 0.24, size = 137, normalized size = 0.87

$$\frac{2b^5(c+dx)^{15/2}}{15d^6} - \frac{(10b^5c - 10ab^4d)(c+dx)^{13/2}}{13d^6} + \frac{2(ad-bc)^5(c+dx)^{5/2}}{5d^6} + \frac{20b^2(ad-bc)^3(c+dx)^{9/2}}{9d^6} + \frac{20b^3}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5*(c + d*x)^(3/2), x)`

[Out] $(2 \cdot b^5 \cdot (c + d \cdot x)^{(15/2)}) / (15 \cdot d^6) - ((10 \cdot b^5 \cdot c - 10 \cdot a \cdot b^4 \cdot d) \cdot (c + d \cdot x)^{(13/2)}) / (13 \cdot d^6) + (2 \cdot (a \cdot d - b \cdot c)^5 \cdot (c + d \cdot x)^{(5/2)}) / (5 \cdot d^6) + (20 \cdot b^2 \cdot (a \cdot d - b \cdot c)^3 \cdot (c + d \cdot x)^{(9/2)}) / (9 \cdot d^6) + (20 \cdot b^3) / d^6 + (10 \cdot b \cdot (a \cdot d - b \cdot c)^4 \cdot (c + d \cdot x)^{(7/2)}) / (7 \cdot d^6)$

sympy [A] time = 26.42, size = 763, normalized size = 4.83

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5*(d*x+c)**(3/2), x)`

[Out] $a^{**5} \cdot c \cdot \text{Piecewise}(\left(\sqrt{c} \cdot x, \text{Eq}(d, 0)\right), (2 \cdot (c + d \cdot x)^{(3/2)} / (3 \cdot d), \text{True})) + 2 \cdot a^{**5} \cdot (-c \cdot (c + d \cdot x)^{(3/2)} / 3 + (c + d \cdot x)^{(5/2)} / 5) / d + 10 \cdot a^{**4} \cdot b \cdot c \cdot (-c \cdot (c + d \cdot x)^{(3/2)} / 3 + (c + d \cdot x)^{(5/2)} / 5) / d^{**2} + 10 \cdot a^{**4} \cdot b \cdot (c^{**2} \cdot (c + d \cdot x)^{(3/2)} / 3 - 2 \cdot c \cdot (c + d \cdot x)^{(5/2)} / 5 + (c + d \cdot x)^{(7/2)} / 7) / d^{**2} + 20 \cdot a^{**3} \cdot b^{**2} \cdot c \cdot (c^{**2} \cdot (c + d \cdot x)^{(3/2)} / 3 - 2 \cdot c \cdot (c + d \cdot x)^{(5/2)} / 5 + (c + d \cdot x)^{(7/2)} / 7) / d^{**3} + 20 \cdot a^{**3} \cdot b^{**2} \cdot (-c^{**3} \cdot (c + d \cdot x)^{(3/2)} / 3 + 3 \cdot c^{**2} \cdot (c + d \cdot x)^{(5/2)} / 5 - 3 \cdot c \cdot (c + d \cdot x)^{(7/2)} / 7 + (c + d \cdot x)^{(9/2)} / 9) / d^{**3} + 20 \cdot a^{**2} \cdot b^{**3} \cdot c \cdot (-c^{**3} \cdot (c + d \cdot x)^{(3/2)} / 3 + 3 \cdot c^{**2} \cdot (c + d \cdot x)^{(5/2)} / 5 - 3 \cdot c \cdot (c + d \cdot x)^{(7/2)} / 7 + (c + d \cdot x)^{(9/2)} / 9) / d^{**4} + 20 \cdot a^{**2} \cdot b^{**3} \cdot (c^{**4} \cdot (c + d \cdot x)^{(3/2)} / 3 - 4 \cdot c^{**3} \cdot (c + d \cdot x)^{(5/2)} / 5 + 6 \cdot c^{**2} \cdot (c + d \cdot x)^{(7/2)} / 7 - 4 \cdot c \cdot (c + d \cdot x)^{(9/2)} / 9 + (c + d \cdot x)^{(11/2)} / 11) / d^{**4} + 10 \cdot a \cdot b^{**4} \cdot c \cdot (c^{**4} \cdot (c + d \cdot x)^{(3/2)} / 3 - 4 \cdot c^{**3} \cdot (c + d \cdot x)^{(5/2)} / 5 + 6 \cdot c^{**2} \cdot (c + d \cdot x)^{(7/2)} / 7 - 4 \cdot c \cdot (c + d \cdot x)^{(9/2)} / 9 + (c + d \cdot x)^{(11/2)} / 11) / d^{**5} + 10 \cdot a \cdot b^{**4} \cdot (-c^{**5} \cdot (c + d \cdot x)^{(3/2)} / 3 + c^{**4} \cdot (c + d \cdot x)^{(5/2)} - 10 \cdot c^{**3} \cdot (c + d \cdot x)^{(7/2)} / 7 + 10 \cdot c^{**2} \cdot (c + d \cdot x)^{(9/2)} / 9 - 5 \cdot c \cdot (c + d \cdot x)^{(11/2)} / 11 + (c + d \cdot x)^{(13/2)} / 13) / d^{**5} + 2 \cdot b^{**5} \cdot c \cdot (-c^{**5} \cdot (c + d \cdot x)^{(3/2)} / 3 + c^{**4} \cdot (c + d \cdot x)^{(5/2)} - 10 \cdot c^{**3} \cdot (c + d \cdot x)^{(7/2)} / 7 + 10 \cdot c^{**2} \cdot (c + d \cdot x)^{(9/2)} / 9 - 5 \cdot c \cdot (c + d \cdot x)^{(11/2)} / 11 + (c + d \cdot x)^{(13/2)} / 13) / d^{**6} + 2 \cdot$

$$b^{*5}(c^{*6}(c + d*x)^{(3/2)}/3 - 6*c^{*5}(c + d*x)^{(5/2)}/5 + 15*c^{*4}(c + d*x)^{(7/2)}/7 - 20*c^{*3}(c + d*x)^{(9/2)}/9 + 15*c^{*2}(c + d*x)^{(11/2)}/11 - 6*c*(c + d*x)^{(13/2)}/13 + (c + d*x)^{(15/2)}/15)/d^{*6}$$

3.1388 $\int (a + bx)^4 (c + dx)^{3/2} dx$

Optimal. Leaf size=129

$$-\frac{8b^3(c+dx)^{11/2}(bc-ad)}{11d^5} + \frac{4b^2(c+dx)^{9/2}(bc-ad)^2}{3d^5} - \frac{8b(c+dx)^{7/2}(bc-ad)^3}{7d^5} + \frac{2(c+dx)^{5/2}(bc-ad)^4}{5d^5} + \frac{2b^4(c+dx)}{13d^5}$$

[Out] $2/5*(-a*d+b*c)^4*(d*x+c)^(5/2)/d^5-8/7*b*(-a*d+b*c)^3*(d*x+c)^(7/2)/d^5+4/3*b^2*(-a*d+b*c)^2*(d*x+c)^(9/2)/d^5-8/11*b^3*(-a*d+b*c)*(d*x+c)^(11/2)/d^5+2/13*b^4*(d*x+c)^(13/2)/d^5$

Rubi [A] time = 0.04, antiderivative size = 129, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{8b^3(c+dx)^{11/2}(bc-ad)}{11d^5} + \frac{4b^2(c+dx)^{9/2}(bc-ad)^2}{3d^5} - \frac{8b(c+dx)^{7/2}(bc-ad)^3}{7d^5} + \frac{2(c+dx)^{5/2}(bc-ad)^4}{5d^5} + \frac{2b^4(c+dx)}{13d^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4*(c + d*x)^(3/2), x]

[Out] $(2*(b*c - a*d)^4*(c + d*x)^(5/2))/(5*d^5) - (8*b*(b*c - a*d)^3*(c + d*x)^(7/2))/(7*d^5) + (4*b^2*(b*c - a*d)^2*(c + d*x)^(9/2))/(3*d^5) - (8*b^3*(b*c - a*d)*(c + d*x)^(11/2))/(11*d^5) + (2*b^4*(c + d*x)^(13/2))/(13*d^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^4 (c + dx)^{3/2} dx &= \int \left(\frac{(-bc + ad)^4 (c + dx)^{3/2}}{d^4} - \frac{4b(bc - ad)^3 (c + dx)^{5/2}}{d^4} + \frac{6b^2(bc - ad)^2 (c + dx)^{7/2}}{d^4} - \frac{4b^3(bc - ad) (c + dx)^{9/2}}{d^4} + \frac{2b^4 (c + dx)^{11/2}}{d^4} \right) dx \\ &= \frac{2(bc - ad)^4 (c + dx)^{5/2}}{5d^5} - \frac{8b(bc - ad)^3 (c + dx)^{7/2}}{7d^5} + \frac{4b^2(bc - ad)^2 (c + dx)^{9/2}}{3d^5} - \frac{8b^3(bc - ad) (c + dx)^{11/2}}{11d^5} + \frac{2b^4 (c + dx)^{13/2}}{13d^5} \end{aligned}$$

Mathematica [A] time = 0.10, size = 101, normalized size = 0.78

$$\frac{2(c+dx)^{5/2}(-5460b^3(c+dx)^3(bc-ad) + 10010b^2(c+dx)^2(bc-ad)^2 - 8580b(c+dx)(bc-ad)^3 + 3003(bc-ad)^4)}{15015d^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4*(c + d*x)^(3/2), x]

[Out] $(2*(c + d*x)^{(5/2)}*(3003*(b*c - a*d)^4 - 8580*b*(b*c - a*d)^3*(c + d*x) + 10010*b^2*(b*c - a*d)^2*(c + d*x)^2 - 5460*b^3*(b*c - a*d)*(c + d*x)^3 + 1155*b^4*(c + d*x)^4)/(15015*d^5)$

fricas [B] time = 0.44, size = 311, normalized size = 2.41

$$2 \left(1155 b^4 d^6 x^6 + 128 b^4 c^6 - 832 a b^3 c^5 d + 2288 a^2 b^2 c^4 d^2 - 3432 a^3 b c^3 d^3 + 3003 a^4 c^2 d^4 + 210 (7 b^4 c d^5 + 26 a b^3 d^6) \right) / (15015 d^5)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^(3/2), x, algorithm="fricas")

[Out] $2/15015*(1155*b^4*d^6*x^6 + 128*b^4*c^6 - 832*a*b^3*c^5*d + 2288*a^2*b^2*c^4*d^2 - 3432*a^3*b*c^3*d^3 + 3003*a^4*c^2*d^4 + 210*(7*b^4*c*d^5 + 26*a*b^3*d^6))*x^5 + 35*(b^4*c^2*d^4 + 208*a*b^3*c*d^5 + 286*a^2*b^2*d^6)*x^4 - 20*(2*b^4*c^3*d^3 - 13*a*b^3*c^2*d^4 - 715*a^2*b^2*c*d^5 - 429*a^3*b*d^6)*x^3 + 3*(16*b^4*c^4*d^2 - 104*a*b^3*c^3*d^3 + 286*a^2*b^2*c^2*d^4 + 4576*a^3*b*c*d^5 + 1001*a^4*d^6)*x^2 - 2*(32*b^4*c^5*d - 208*a*b^3*c^4*d^2 + 572*a^2*b^2*c^3*d^3 - 858*a^3*b*c^2*d^4 - 3003*a^4*c*d^5)*x)*sqrt(d*x + c)/d^5$

giac [B] time = 1.40, size = 807, normalized size = 6.26

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^(3/2), x, algorithm="giac")

[Out] $2/45045*(45045*sqrt(d*x + c)*a^4*c^2 + 30030*((d*x + c)^{(3/2)} - 3*sqrt(d*x + c)*c)*a^4*c + 60060*((d*x + c)^{(3/2)} - 3*sqrt(d*x + c)*c)*a^3*b*c^2/d + 3003*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a^4 + 18018*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a^2*b^2*c^2/d^2 + 24024*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a^3*b*c/d + 5148*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a*b^3*c^2/d^3 + 15444*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a^2*b^2*c/d^2 + 5148*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a^3*b/d + 143*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*sqrt(d*x + c)*c^4)*b^4*c^2/d^4 + 1144*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*sqrt(d*x + c)*c^4)*a*b^3*c/d^3 + 858*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*sqrt(d*x + c)*c^4)*a^4$

$$\begin{aligned} & (7/2)*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*\sqrt{d*x} \\ & + c)*c^4)*a^2*b^2/d^2 + 130*(63*(d*x + c)^{(11/2)} - 385*(d*x + c)^{(9/2)}*c + \\ & 990*(d*x + c)^{(7/2)}*c^2 - 1386*(d*x + c)^{(5/2)}*c^3 + 1155*(d*x + c)^{(3/2)}*c \\ & ^4 - 693*\sqrt{d*x + c}*c^5)*b^4*c/d^4 + 260*(63*(d*x + c)^{(11/2)} - 385*(d*x \\ & + c)^{(9/2)}*c + 990*(d*x + c)^{(7/2)}*c^2 - 1386*(d*x + c)^{(5/2)}*c^3 + 1155*(\\ & d*x + c)^{(3/2)}*c^4 - 693*\sqrt{d*x + c}*c^5)*a*b^3/d^3 + 15*(231*(d*x + c)^{(\\ & 13/2)} - 1638*(d*x + c)^{(11/2)}*c + 5005*(d*x + c)^{(9/2)}*c^2 - 8580*(d*x + c) \\ & ^{(7/2)}*c^3 + 9009*(d*x + c)^{(5/2)}*c^4 - 6006*(d*x + c)^{(3/2)}*c^5 + 3003*\sqrt{ \\ & t(d*x + c)*c^6)*b^4/d^4)/d \end{aligned}$$

maple [A] time = 0.01, size = 186, normalized size = 1.44

$$2(dx + c)^{\frac{5}{2}} \left(1155b^4x^4d^4 + 5460ab^3d^4x^3 - 840b^4cd^3x^3 + 10010a^2b^2d^4x^2 - 3640ab^3cd^3x^2 + 560b^4c^2d^2x^2 + 8580 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4*(d*x+c)^(3/2), x)

[Out] 2/15015*(d*x+c)^(5/2)*(1155*b^4*d^4*x^4+5460*a*b^3*d^4*x^3-840*b^4*c*d^3*x^3+10010*a^2*b^2*d^4*x^2-3640*a*b^3*c*d^3*x^2+560*b^4*c^2*d^2*x^2+8580*a^3*b*d^4*x-5720*a^2*b^2*c*d^3*x+2080*a*b^3*c^2*d^2*x-320*b^4*c^3*d*x+3003*a^4*d^4-3432*a^3*b*c*d^3+2288*a^2*b^2*c^2*d^2-832*a*b^3*c^3*d+128*b^4*c^4)/d^5

maxima [A] time = 1.36, size = 181, normalized size = 1.40

$$2 \left(1155(dx + c)^{\frac{13}{2}}b^4 - 5460(b^4c - ab^3d)(dx + c)^{\frac{11}{2}} + 10010(b^4c^2 - 2ab^3cd + a^2b^2d^2)(dx + c)^{\frac{9}{2}} - 8580(b^4c^3 - 3ab^3cd^2 + a^2b^2c^2d) \right) / 15015d^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^(3/2), x, algorithm="maxima")

[Out] 2/15015*(1155*(d*x + c)^(13/2)*b^4 - 5460*(b^4*c - a*b^3*d)*(d*x + c)^(11/2) + 10010*(b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2)*(d*x + c)^(9/2) - 8580*(b^4*c^3 - 3*a*b^3*c^2*d + 3*a^2*b^2*c*d^2 - a^3*b*d^3)*(d*x + c)^(7/2) + 3003*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*(d*x + c)^(5/2))/d^5

mupad [B] time = 0.24, size = 112, normalized size = 0.87

$$\frac{2b^4(c+dx)^{13/2}}{13d^5} - \frac{(8b^4c - 8ab^3d)(c+dx)^{11/2}}{11d^5} + \frac{2(ad-bc)^4(c+dx)^{5/2}}{5d^5} + \frac{4b^2(ad-bc)^2(c+dx)^{9/2}}{3d^5} + \frac{8b(ad-bc)(c+dx)^{3/2}}{d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^4*(c + d*x)^(3/2), x)`

[Out] $(2*b^4*(c + d*x)^(13/2))/(13*d^5) - ((8*b^4*c - 8*a*b^3*d)*(c + d*x)^(11/2))/(11*d^5) + (2*(a*d - b*c)^4*(c + d*x)^(5/2))/(5*d^5) + (4*b^2*(a*d - b*c)^2*(c + d*x)^(9/2))/(3*d^5) + (8*b*(a*d - b*c)^3*(c + d*x)^(7/2))/(7*d^5)$

sympy [A] time = 20.09, size = 559, normalized size = 4.33

$$a^4 c \left(\begin{cases} \sqrt{c} x & \text{for } d = 0 \\ \frac{2(c+dx)^{\frac{3}{2}}}{3d} & \text{otherwise} \end{cases} \right) + \frac{2a^4 \left(-\frac{c(c+dx)^{\frac{3}{2}}}{3} + \frac{(c+dx)^{\frac{5}{2}}}{5} \right)}{d} + \frac{8a^3 b c \left(-\frac{c(c+dx)^{\frac{3}{2}}}{3} + \frac{(c+dx)^{\frac{5}{2}}}{5} \right)}{d^2} + \frac{8a^3 b \left(\frac{c^2(c+dx)^{\frac{3}{2}}}{3} - \frac{2c(c+dx)^{\frac{5}{2}}}{5} \right)}{d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**4*(d*x+c)**(3/2), x)`

[Out] $a^{**4}*c*\text{Piecewise}(\text{sqrt}(c)*x, \text{Eq}(d, 0)), (2*(c + d*x)**(3/2)/(3*d), \text{True})) + 2*a^{**4}*(-c*(c + d*x)**(3/2)/3 + (c + d*x)**(5/2)/5)/d + 8*a^{**3}*b*c*(-c*(c + d*x)**(3/2)/3 + (c + d*x)**(5/2)/5)/d^{**2} + 8*a^{**3}*b*(c^{**2}*(c + d*x)**(3/2)/3 - 2*c*(c + d*x)**(5/2)/5 + (c + d*x)**(7/2)/7)/d^{**2} + 12*a^{**2}*b^{**2}*c*(c^{**2}*(c + d*x)**(3/2)/3 - 2*c*(c + d*x)**(5/2)/5 + (c + d*x)**(7/2)/7)/d^{**3} + 12*a^{**2}*b^{**2}*(-c^{**3}*(c + d*x)**(3/2)/3 + 3*c^{**2}*(c + d*x)**(5/2)/5 - 3*c*(c + d*x)**(7/2)/7 + (c + d*x)**(9/2)/9)/d^{**3} + 8*a*b^{**3}*c*(-c^{**3}*(c + d*x)**(3/2)/3 + 3*c^{**2}*(c + d*x)**(5/2)/5 - 3*c*(c + d*x)**(7/2)/7 + (c + d*x)**(9/2)/9)/d^{**4} + 8*a*b^{**3}*(c^{**4}*(c + d*x)**(3/2)/3 - 4*c^{**3}*(c + d*x)**(5/2)/5 + 6*c^{**2}*(c + d*x)**(7/2)/7 - 4*c*(c + d*x)**(9/2)/9 + (c + d*x)**(11/2)/11)/d^{**4} + 2*b^{**4}*c*(c^{**4}*(c + d*x)**(3/2)/3 - 4*c^{**3}*(c + d*x)**(5/2)/5 + 6*c^{**2}*(c + d*x)**(7/2)/7 - 4*c*(c + d*x)**(9/2)/9 + (c + d*x)**(11/2)/11)/d^{**5} + 2*b^{**4}*(-c^{**5}*(c + d*x)**(3/2)/3 + c^{**4}*(c + d*x)**(5/2) - 10*c^{**3}*(c + d*x)**(7/2)/7 + 10*c^{**2}*(c + d*x)**(9/2)/9 - 5*c*(c + d*x)**(11/2)/11 + (c + d*x)**(13/2)/13)/d^{**5}$

3.1389 $\int (a + bx)^3 (c + dx)^{3/2} dx$

Optimal. Leaf size=100

$$-\frac{2b^2(c+dx)^{9/2}(bc-ad)}{3d^4} + \frac{6b(c+dx)^{7/2}(bc-ad)^2}{7d^4} - \frac{2(c+dx)^{5/2}(bc-ad)^3}{5d^4} + \frac{2b^3(c+dx)^{11/2}}{11d^4}$$

[Out] $-2/5*(-a*d+b*c)^3*(d*x+c)^(5/2)/d^4+6/7*b*(-a*d+b*c)^2*(d*x+c)^(7/2)/d^4-2/3*b^2*(-a*d+b*c)*(d*x+c)^(9/2)/d^4+2/11*b^3*(d*x+c)^(11/2)/d^4$

Rubi [A] time = 0.03, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{2b^2(c+dx)^{9/2}(bc-ad)}{3d^4} + \frac{6b(c+dx)^{7/2}(bc-ad)^2}{7d^4} - \frac{2(c+dx)^{5/2}(bc-ad)^3}{5d^4} + \frac{2b^3(c+dx)^{11/2}}{11d^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3*(c + d*x)^(3/2), x]

[Out] $(-2*(b*c - a*d)^3*(c + d*x)^(5/2))/(5*d^4) + (6*b*(b*c - a*d)^2*(c + d*x)^(7/2))/(7*d^4) - (2*b^2*(b*c - a*d)*(c + d*x)^(9/2))/(3*d^4) + (2*b^3*(c + d*x)^(11/2))/(11*d^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])]

Rubi steps

$$\begin{aligned} \int (a + bx)^3 (c + dx)^{3/2} dx &= \int \left(\frac{(-bc + ad)^3 (c + dx)^{3/2}}{d^3} + \frac{3b(bc - ad)^2 (c + dx)^{5/2}}{d^3} - \frac{3b^2(bc - ad)(c + dx)^{7/2}}{d^3} + \frac{b^3(c + dx)^{9/2}}{d^3} \right) dx \\ &= -\frac{2(bc - ad)^3 (c + dx)^{5/2}}{5d^4} + \frac{6b(bc - ad)^2 (c + dx)^{7/2}}{7d^4} - \frac{2b^2(bc - ad)(c + dx)^{9/2}}{3d^4} + \frac{2b^3(c + dx)^{11/2}}{11d^4} \end{aligned}$$

Mathematica [A] time = 0.07, size = 79, normalized size = 0.79

$$\frac{2(c+dx)^{5/2}(-385b^2(c+dx)^2(bc-ad) + 495b(c+dx)(bc-ad)^2 - 231(bc-ad)^3 + 105b^3(c+dx)^3)}{1155d^4}$$

$$\frac{\sqrt{d}^2 + 5(63(dx+c)^{11/2} - 385(dx+c)^{9/2}c + 990(dx+c)^{7/2}c^2 - 1386(dx+c)^{5/2}c^3 + 1155(dx+c)^{3/2}c^4 - 693\sqrt{dx+c}c^5)b^3/d^3}{d}$$

maple [A] time = 0.01, size = 116, normalized size = 1.16

$$\frac{2(dx+c)^{5/2}(105b^3x^3d^3 + 385ab^2d^3x^2 - 70b^3cd^2x^2 + 495a^2bd^3x - 220ab^2cd^2x + 40b^3c^2dx + 231a^3d^3 - 198a^2bd^2c)}{1155d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3*(d*x+c)^(3/2),x)

[Out] 2/1155*(d*x+c)^(5/2)*(105*b^3*d^3*x^3+385*a*b^2*d^3*x^2-70*b^3*c*d^2*x^2+495*a^2*b*d^3*x-220*a*b^2*c*d^2*x+40*b^3*c^2*d*x+231*a^3*d^3-198*a^2*b*c*d^2+88*a*b^2*c^2*d-16*b^3*c^3)/d^4

maxima [A] time = 1.36, size = 118, normalized size = 1.18

$$\frac{2\left(105(dx+c)^{11/2}b^3 - 385(b^3c - ab^2d)(dx+c)^{9/2} + 495(b^3c^2 - 2ab^2cd + a^2bd^2)(dx+c)^{7/2} - 231(b^3c^3 - 3ab^2c^2d + 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3)(dx+c)^{5/2}\right)}{1155d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^(3/2),x, algorithm="maxima")

[Out] 2/1155*(105*(d*x + c)^(11/2)*b^3 - 385*(b^3*c - a*b^2*d)*(d*x + c)^(9/2) + 495*(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*(d*x + c)^(7/2) - 231*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b^2*c^2*d - a^3*d^3)*(d*x + c)^(5/2))/d^4

mupad [B] time = 0.25, size = 87, normalized size = 0.87

$$\frac{2b^3(c+dx)^{11/2}}{11d^4} - \frac{(6b^3c - 6ab^2d)(c+dx)^{9/2}}{9d^4} + \frac{2(ad-bc)^3(c+dx)^{5/2}}{5d^4} + \frac{6b(ad-bc)^2(c+dx)^{7/2}}{7d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3*(c + d*x)^(3/2),x)

[Out] (2*b^3*(c + d*x)^(11/2))/(11*d^4) - ((6*b^3*c - 6*a*b^2*d)*(c + d*x)^(9/2))/(9*d^4) + (2*(a*d - b*c)^3*(c + d*x)^(5/2))/(5*d^4) + (6*b*(a*d - b*c)^2*(c + d*x)^(7/2))/(7*d^4)

sympy [A] time = 14.38, size = 386, normalized size = 3.86

$$a^3c \left(\begin{cases} \sqrt{c}x & \text{for } d = 0 \\ \frac{2(c+dx)^{\frac{3}{2}}}{3d} & \text{otherwise} \end{cases} \right) + \frac{2a^3 \left(-\frac{c(c+dx)^{\frac{3}{2}}}{3} + \frac{(c+dx)^{\frac{5}{2}}}{5} \right)}{d} + \frac{6a^2bc \left(-\frac{c(c+dx)^{\frac{3}{2}}}{3} + \frac{(c+dx)^{\frac{5}{2}}}{5} \right)}{d^2} + \frac{6a^2b \left(\frac{c^2(c+dx)^{\frac{3}{2}}}{3} - \frac{2c(c+dx)^{\frac{5}{2}}}{5} \right)}{d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3*(d*x+c)**(3/2),x)

[Out] a**3*c*Piecewise((sqrt(c)*x, Eq(d, 0)), (2*(c + d*x)**(3/2)/(3*d), True)) + 2*a**3*(-c*(c + d*x)**(3/2)/3 + (c + d*x)**(5/2)/5)/d + 6*a**2*b*c*(-c*(c + d*x)**(3/2)/3 + (c + d*x)**(5/2)/5)/d**2 + 6*a**2*b*(c**2*(c + d*x)**(3/2)/3 - 2*c*(c + d*x)**(5/2)/5 + (c + d*x)**(7/2)/7)/d**2 + 6*a*b**2*c*(c**2*(c + d*x)**(3/2)/3 - 2*c*(c + d*x)**(5/2)/5 + (c + d*x)**(7/2)/7)/d**3 + 6*a*b**2*(-c**3*(c + d*x)**(3/2)/3 + 3*c**2*(c + d*x)**(5/2)/5 - 3*c*(c + d*x)**(7/2)/7 + (c + d*x)**(9/2)/9)/d**3 + 2*b**3*c*(-c**3*(c + d*x)**(3/2)/3 + 3*c**2*(c + d*x)**(5/2)/5 - 3*c*(c + d*x)**(7/2)/7 + (c + d*x)**(9/2)/9)/d**4 + 2*b**3*(c**4*(c + d*x)**(3/2)/3 - 4*c**3*(c + d*x)**(5/2)/5 + 6*c**2*(c + d*x)**(7/2)/7 - 4*c*(c + d*x)**(9/2)/9 + (c + d*x)**(11/2)/11)/d**4

3.1390 $\int (a + bx)^2 (c + dx)^{3/2} dx$

Optimal. Leaf size=71

$$-\frac{4b(c + dx)^{7/2}(bc - ad)}{7d^3} + \frac{2(c + dx)^{5/2}(bc - ad)^2}{5d^3} + \frac{2b^2(c + dx)^{9/2}}{9d^3}$$

[Out] $2/5*(-a*d+b*c)^2*(d*x+c)^{(5/2)}/d^3-4/7*b*(-a*d+b*c)*(d*x+c)^{(7/2)}/d^3+2/9*b^2*(d*x+c)^{(9/2)}/d^3$

Rubi [A] time = 0.02, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{4b(c + dx)^{7/2}(bc - ad)}{7d^3} + \frac{2(c + dx)^{5/2}(bc - ad)^2}{5d^3} + \frac{2b^2(c + dx)^{9/2}}{9d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(c + d*x)^(3/2), x]

[Out] $(2*(b*c - a*d)^2*(c + d*x)^{(5/2)})/(5*d^3) - (4*b*(b*c - a*d)*(c + d*x)^{(7/2)})/(7*d^3) + (2*b^2*(c + d*x)^{(9/2)})/(9*d^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2 (c + dx)^{3/2} dx &= \int \left(\frac{(-bc + ad)^2 (c + dx)^{3/2}}{d^2} - \frac{2b(bc - ad)(c + dx)^{5/2}}{d^2} + \frac{b^2(c + dx)^{7/2}}{d^2} \right) dx \\ &= \frac{2(bc - ad)^2 (c + dx)^{5/2}}{5d^3} - \frac{4b(bc - ad)(c + dx)^{7/2}}{7d^3} + \frac{2b^2(c + dx)^{9/2}}{9d^3} \end{aligned}$$

Mathematica [A] time = 0.04, size = 61, normalized size = 0.86

$$\frac{2(c + dx)^{5/2} (63a^2d^2 + 18abd(5dx - 2c) + b^2(8c^2 - 20cdx + 35d^2x^2))}{315d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(c + d*x)^(3/2), x]

[Out] (2*(c + d*x)^(5/2)*(63*a^2*d^2 + 18*a*b*d*(-2*c + 5*d*x) + b^2*(8*c^2 - 20*c*d*x + 35*d^2*x^2)))/(315*d^3)

fricas [B] time = 0.43, size = 137, normalized size = 1.93

$$\frac{2 \left(35 b^2 d^4 x^4 + 8 b^2 c^4 - 36 a b c^3 d + 63 a^2 c^2 d^2 + 10 (5 b^2 c d^3 + 9 a b d^4) x^3 + 3 (b^2 c^2 d^2 + 48 a b c d^3 + 21 a^2 d^4) x^2 - 2 \right)}{315 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^(3/2), x, algorithm="fricas")

[Out] 2/315*(35*b^2*d^4*x^4 + 8*b^2*c^4 - 36*a*b*c^3*d + 63*a^2*c^2*d^2 + 10*(5*b^2*c*d^3 + 9*a*b*d^4)*x^3 + 3*(b^2*c^2*d^2 + 48*a*b*c*d^3 + 21*a^2*d^4)*x^2 - 2*(2*b^2*c^3*d - 9*a*b*c^2*d^2 - 63*a^2*c*d^3)*x)*sqrt(d*x + c)/d^3

giac [B] time = 1.41, size = 360, normalized size = 5.07

$$2 \left(315 \sqrt{dx+c} a^2 c^2 + 210 \left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} c \right) a^2 c + \frac{210 \left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} c \right) a b c^2}{d} + 21 \left(3 (dx+c)^{\frac{5}{2}} - 10 (dx+c) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^(3/2), x, algorithm="giac")

[Out] 2/315*(315*sqrt(d*x + c)*a^2*c^2 + 210*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a^2*c + 210*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a*b*c^2/d + 21*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a^2 + 21*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*b^2*c^2/d^2 + 84*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a*b*c/d + 18*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*b^2*c/d^2 + 18*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*a*b/d + (35*(d*x + c)^(9/2) - 180*(d*x + c)^(7/2)*c + 378*(d*x + c)^(5/2)*c^2 - 420*(d*x + c)^(3/2)*c^3 + 315*sqrt(d*x + c)*c^4)*b^2/d^2)/d

maple [A] time = 0.01, size = 63, normalized size = 0.89

$$\frac{2 (dx + c)^{\frac{5}{2}} \left(35 b^2 x^2 d^2 + 90 a b d^2 x - 20 b^2 c d x + 63 a^2 d^2 - 36 a b c d + 8 b^2 c^2 \right)}{315 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2*(d*x+c)^(3/2),x)`

[Out] $\frac{2}{315}*(d*x+c)^{(5/2)}*(35*b^2*d^2*x^2+90*a*b*d^2*x-20*b^2*c*d*x+63*a^2*d^2-36*a*b*c*d+8*b^2*c^2)/d^3$

maxima [A] time = 1.38, size = 68, normalized size = 0.96

$$\frac{2 \left(35 (dx + c)^{\frac{9}{2}} b^2 - 90 (b^2 c - abd) (dx + c)^{\frac{7}{2}} + 63 (b^2 c^2 - 2 abcd + a^2 d^2) (dx + c)^{\frac{5}{2}} \right)}{315 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2*(d*x+c)^(3/2),x, algorithm="maxima")`

[Out] $\frac{2}{315}*(35*(d*x + c)^{(9/2)}*b^2 - 90*(b^2*c - a*b*d)*(d*x + c)^{(7/2)} + 63*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(d*x + c)^{(5/2)})/d^3$

mupad [B] time = 0.06, size = 68, normalized size = 0.96

$$\frac{2(c+dx)^{5/2} \left(35b^2(c+dx)^2 + 63a^2d^2 + 63b^2c^2 - 90b^2c(c+dx) + 90abd(c+dx) - 126abcd \right)}{315d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2*(c + d*x)^(3/2),x)`

[Out] $\frac{2*(c + d*x)^{(5/2)}*(35*b^2*(c + d*x)^2 + 63*a^2*d^2 + 63*b^2*c^2 - 90*b^2*c*(c + d*x) + 90*a*b*d*(c + d*x) - 126*a*b*c*d)}{(315*d^3)}$

sympy [A] time = 9.61, size = 240, normalized size = 3.38

$$a^2c \left(\left\{ \begin{array}{ll} \sqrt{c} x & \text{for } d = 0 \\ \frac{2(c+dx)^{\frac{3}{2}}}{3d} & \text{otherwise} \end{array} \right. \right) + \frac{2a^2 \left(-\frac{c(c+dx)^{\frac{3}{2}}}{3} + \frac{(c+dx)^{\frac{5}{2}}}{5} \right)}{d} + \frac{4abc \left(-\frac{c(c+dx)^{\frac{3}{2}}}{3} + \frac{(c+dx)^{\frac{5}{2}}}{5} \right)}{d^2} + \frac{4ab \left(\frac{c^2(c+dx)^{\frac{3}{2}}}{3} - \frac{2c(c+dx)^{\frac{5}{2}}}{5} \right)}{d^2} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(d*x+c)**(3/2),x)`

[Out] $a**2*c*Piecewise((sqrt(c)*x, Eq(d, 0)), (2*(c + d*x)**(3/2)/(3*d), True)) + 2*a**2*(-c*(c + d*x)**(3/2)/3 + (c + d*x)**(5/2)/5)/d + 4*a*b*c*(-c*(c + d*x)**(3/2)/3 + (c + d*x)**(5/2)/5)/d**2 + 4*a*b*(c**2*(c + d*x)**(3/2)/3 - 2*c*(c + d*x)**(5/2)/5 + (c + d*x)**(7/2)/7)/d**2 + 2*b**2*c*(c**2*(c + d*x)$

$$\begin{aligned} &)^{3/2}/3 - 2c(c + dx)^{5/2}/5 + (c + dx)^{7/2}/7/d^3 + 2b^2(-c \\ & ^{3/2}(c + dx)^{3/2}/3 + 3c^2(c + dx)^{5/2}/5 - 3c(c + dx)^{7/2}/7 \\ & + (c + dx)^{9/2}/9)/d^3 \end{aligned}$$

3.1391 $\int (a + bx)(c + dx)^{3/2} dx$

Optimal. Leaf size=42

$$\frac{2b(c + dx)^{7/2}}{7d^2} - \frac{2(c + dx)^{5/2}(bc - ad)}{5d^2}$$

[Out] $-2/5*(-a*d+b*c)*(d*x+c)^{(5/2)}/d^2+2/7*b*(d*x+c)^{(7/2)}/d^2$

Rubi [A] time = 0.01, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{2b(c + dx)^{7/2}}{7d^2} - \frac{2(c + dx)^{5/2}(bc - ad)}{5d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(c + d*x)^(3/2), x]

[Out] $(-2*(b*c - a*d)*(c + d*x)^{(5/2)})/(5*d^2) + (2*b*(c + d*x)^{(7/2)})/(7*d^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)(c + dx)^{3/2} dx &= \int \left(\frac{(-bc + ad)(c + dx)^{3/2}}{d} + \frac{b(c + dx)^{5/2}}{d} \right) dx \\ &= -\frac{2(bc - ad)(c + dx)^{5/2}}{5d^2} + \frac{2b(c + dx)^{7/2}}{7d^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 30, normalized size = 0.71

$$\frac{2(c + dx)^{5/2}(7ad - 2bc + 5bdx)}{35d^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(c + d*x)^(3/2), x]

[Out] (2*(c + d*x)^(5/2)*(-2*b*c + 7*a*d + 5*b*d*x))/(35*d^2)

fricas [B] time = 0.44, size = 69, normalized size = 1.64

$$\frac{2(5bd^3x^3 - 2bc^3 + 7ac^2d + (8bcd^2 + 7ad^3)x^2 + (bc^2d + 14acd^2)x)\sqrt{dx + c}}{35d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^(3/2), x, algorithm="fricas")

[Out] 2/35*(5*b*d^3*x^3 - 2*b*c^3 + 7*a*c^2*d + (8*b*c*d^2 + 7*a*d^3)*x^2 + (b*c^2*d + 14*a*c*d^2)*x)*sqrt(d*x + c)/d^2

giac [B] time = 1.23, size = 192, normalized size = 4.57

$$2 \left(105 \sqrt{dx + c} ac^2 + 70 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} c \right) ac + \frac{35 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} c \right) bc^2}{d} + 7 \left(3 (dx + c)^{\frac{5}{2}} - 10 (dx + c)^{\frac{3}{2}} c + \right. \right.$$

105d

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^(3/2), x, algorithm="giac")

[Out] 2/105*(105*sqrt(d*x + c)*a*c^2 + 70*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a*c + 35*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*b*c^2/d + 7*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a + 14*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*b*c/d + 3*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*b/d)/d

maple [A] time = 0.00, size = 27, normalized size = 0.64

$$\frac{2(dx + c)^{\frac{5}{2}}(5bdx + 7ad - 2bc)}{35d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(d*x+c)^(3/2), x)

[Out] 2/35*(d*x+c)^(5/2)*(5*b*d*x+7*a*d-2*b*c)/d^2

maxima [A] time = 1.37, size = 33, normalized size = 0.79

$$\frac{2 \left(5 (dx + c)^{\frac{7}{2}} b - 7 (bc - ad) (dx + c)^{\frac{5}{2}} \right)}{35 d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^(3/2),x, algorithm="maxima")

[Out] $2/35*(5*(d*x + c)^{(7/2)*b - 7*(b*c - a*d)*(d*x + c)^{(5/2)})/d^2$

mupad [B] time = 0.21, size = 29, normalized size = 0.69

$$\frac{2(c+dx)^{5/2}(7ad-7bc+5b(c+dx))}{35d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)*(c + d*x)^(3/2),x)

[Out] $(2*(c + d*x)^{(5/2)*(7*a*d - 7*b*c + 5*b*(c + d*x)))/(35*d^2)$

sympy [A] time = 0.67, size = 146, normalized size = 3.48

$$\begin{cases} \frac{2ac^2\sqrt{c+dx}}{5d} + \frac{4acx\sqrt{c+dx}}{5} + \frac{2adx^2\sqrt{c+dx}}{5} - \frac{4bc^3\sqrt{c+dx}}{35d^2} + \frac{2bc^2x\sqrt{c+dx}}{35d} + \frac{16bcx^2\sqrt{c+dx}}{35} + \frac{2bdx^3\sqrt{c+dx}}{7} & \text{for } d \neq 0 \\ c^{\frac{3}{2}} \left(ax + \frac{bx^2}{2} \right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)**(3/2),x)

[Out] Piecewise(((2*a*c**2*sqrt(c + d*x)/(5*d) + 4*a*c*x*sqrt(c + d*x)/5 + 2*a*d*x**2*sqrt(c + d*x)/5 - 4*b*c**3*sqrt(c + d*x)/(35*d**2) + 2*b*c**2*x*sqrt(c + d*x)/(35*d) + 16*b*c*x**2*sqrt(c + d*x)/35 + 2*b*d*x**3*sqrt(c + d*x)/7, Ne(d, 0)), (c**(3/2)*(a*x + b*x**2/2), True))

$$3.1392 \quad \int (c + dx)^{3/2} dx$$

Optimal. Leaf size=16

$$\frac{2(c + dx)^{5/2}}{5d}$$

[Out] 2/5*(d*x+c)^(5/2)/d

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{2(c + dx)^{5/2}}{5d}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2), x]

[Out] (2*(c + d*x)^(5/2))/(5*d)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (c + dx)^{3/2} dx = \frac{2(c + dx)^{5/2}}{5d}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$\frac{2(c + dx)^{5/2}}{5d}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/2), x]

[Out] (2*(c + d*x)^(5/2))/(5*d)

fricas [B] time = 0.42, size = 28, normalized size = 1.75

$$\frac{2(d^2x^2 + 2cdx + c^2)\sqrt{dx + c}}{5d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2),x, algorithm="fricas")

[Out] 2/5*(d^2*x^2 + 2*c*d*x + c^2)*sqrt(d*x + c)/d

giac [B] time = 1.24, size = 58, normalized size = 3.62

$$\frac{2 \left(3 (dx + c)^{\frac{5}{2}} - 10 (dx + c)^{\frac{3}{2}} c + 30 \sqrt{dx + c} c^2 + 10 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} c \right) c \right)}{15 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2),x, algorithm="giac")

[Out] 2/15*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 30*sqrt(d*x + c)*c^2 + 10*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*c)/d

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{2 (dx + c)^{\frac{5}{2}}}{5 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/2),x)

[Out] 2/5*(d*x+c)^(5/2)/d

maxima [A] time = 1.36, size = 12, normalized size = 0.75

$$\frac{2 (dx + c)^{\frac{5}{2}}}{5 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2),x, algorithm="maxima")

[Out] 2/5*(d*x + c)^(5/2)/d

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{2 (c + d x)^{\frac{5}{2}}}{5 d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(3/2),x)
```

```
[Out] (2*(c + d*x)^(5/2))/(5*d)
```

sympy [A] time = 0.06, size = 12, normalized size = 0.75

$$\frac{2(c + dx)^{\frac{5}{2}}}{5d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(3/2),x)
```

```
[Out] 2*(c + d*x)**(5/2)/(5*d)
```

$$3.1393 \quad \int \frac{(c+dx)^{3/2}}{a+bx} dx$$

Optimal. Leaf size=86

$$-\frac{2(bc-ad)^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{5/2}} + \frac{2\sqrt{c+dx}(bc-ad)}{b^2} + \frac{2(c+dx)^{3/2}}{3b}$$

[Out] $2/3*(d*x+c)^{(3/2)}/b-2*(-a*d+b*c)^{(3/2)}*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})/b^{(5/2)}+2*(-a*d+b*c)*(d*x+c)^{(1/2)}/b^2$

Rubi [A] time = 0.05, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {50, 63, 208}

$$\frac{2\sqrt{c+dx}(bc-ad)}{b^2} - \frac{2(bc-ad)^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{5/2}} + \frac{2(c+dx)^{3/2}}{3b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2)/(a + b*x), x]

[Out] $(2*(b*c - a*d)*\operatorname{Sqrt}[c + d*x])/b^2 + (2*(c + d*x)^{(3/2)})/(3*b) - (2*(b*c - a*d)^{(3/2)}*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/(\operatorname{Sqrt}[b*c - a*d])])/b^{(5/2)}$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

`Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]`

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^{3/2}}{a+bx} dx &= \frac{2(c+dx)^{3/2}}{3b} + \frac{(bc-ad) \int \frac{\sqrt{c+dx}}{a+bx} dx}{b} \\ &= \frac{2(bc-ad)\sqrt{c+dx}}{b^2} + \frac{2(c+dx)^{3/2}}{3b} + \frac{(bc-ad)^2 \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{b^2} \\ &= \frac{2(bc-ad)\sqrt{c+dx}}{b^2} + \frac{2(c+dx)^{3/2}}{3b} + \frac{(2(bc-ad)^2) \text{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{b^2 d} \\ &= \frac{2(bc-ad)\sqrt{c+dx}}{b^2} + \frac{2(c+dx)^{3/2}}{3b} - \frac{2(bc-ad)^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{5/2}} \end{aligned}$$

Mathematica [A] time = 0.07, size = 77, normalized size = 0.90

$$\frac{2\sqrt{c+dx}(-3ad+4bc+bdx)}{3b^2} - \frac{2(bc-ad)^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{5/2}}$$

Antiderivative was successfully verified.

[In] `Integrate[(c + d*x)^(3/2)/(a + b*x), x]`

[Out] `(2*sqrt[c + d*x]*(4*b*c - 3*a*d + b*d*x))/(3*b^2) - (2*(b*c - a*d)^(3/2)*ArcTanh[(sqrt[b]*sqrt[c + d*x])/sqrt[b*c - a*d]])/b^(5/2)`

fricas [A] time = 0.47, size = 188, normalized size = 2.19

$$\left[\frac{3(bc-ad)\sqrt{\frac{bc-ad}{b}} \log\left(\frac{bdx+2bc-ad+2\sqrt{dx+c}b\sqrt{\frac{bc-ad}{b}}}{bx+a}\right) - 2(bdx+4bc-3ad)\sqrt{dx+c}}{3b^2}, - \frac{2\left(3(bc-ad)\sqrt{-\frac{bc-ad}{b}} \arctan\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)\right)}{b^{5/2}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(3/2)/(b*x+a), x, algorithm="fricas")`

[Out] $[-1/3*(3*(b*c - a*d)*\sqrt{(b*c - a*d)/b})*\log((b*d*x + 2*b*c - a*d + 2*\sqrt{d*x + c})*b*\sqrt{(b*c - a*d)/b})/(b*x + a) - 2*(b*d*x + 4*b*c - 3*a*d)*\sqrt{(d*x + c)}/b^2, -2/3*(3*(b*c - a*d)*\sqrt{-(b*c - a*d)/b})*\arctan(-\sqrt{d*x + c})*b*\sqrt{-(b*c - a*d)/b}/(b*c - a*d) - (b*d*x + 4*b*c - 3*a*d)*\sqrt{(d*x + c)}/b^2]$

giac [A] time = 1.29, size = 105, normalized size = 1.22

$$\frac{2(b^2c^2 - 2abcd + a^2d^2) \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{\sqrt{-b^2c+abd}b^2} + \frac{2\left((dx+c)^{\frac{3}{2}}b^2 + 3\sqrt{dx+c}b^2c - 3\sqrt{dx+c}abd\right)}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(3/2)/(b*x+a),x, algorithm="giac")`

[Out] $2*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*\arctan(\sqrt{d*x + c}*b/\sqrt{-b^2*c + a*b*d})/(\sqrt{-b^2*c + a*b*d}*b^2) + 2/3*((d*x + c)^{(3/2)}*b^2 + 3*\sqrt{d*x + c}*b^2*c - 3*\sqrt{d*x + c}*a*b*d)/b^3$

maple [B] time = 0.01, size = 167, normalized size = 1.94

$$\frac{2a^2d^2 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b^2} - \frac{4acd \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b} + \frac{2c^2 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}} - \frac{2\sqrt{dx+c}ad}{b^2} + \frac{2\sqrt{dx+c}c}{b} + \frac{2(dx+c)}{3b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(3/2)/(b*x+a),x)`

[Out] $2/3*(d*x+c)^{(3/2)}/b-2/b^2*a*d*(d*x+c)^{(1/2)}+2/b*(d*x+c)^{(1/2)}*c+2/b^2/((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)*a^2*d^2-4/b/((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)*a*c*d+2/((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)*c^2$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(3/2)/(b*x+a),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.07, size = 93, normalized size = 1.08

$$\frac{2(c+dx)^{3/2}}{3b} - \frac{2(ad-bc)\sqrt{c+dx}}{b^2} + \frac{2\operatorname{atan}\left(\frac{\sqrt{b}(ad-bc)^{3/2}\sqrt{c+dx}}{a^2d^2-2abcd+b^2c^2}\right)(ad-bc)^{3/2}}{b^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(3/2)/(a + b*x), x)`

[Out] `(2*(c + d*x)^(3/2))/(3*b) - (2*(a*d - b*c)*(c + d*x)^(1/2))/b^2 + (2*atan((b^(1/2)*(a*d - b*c)^(3/2)*(c + d*x)^(1/2))/(a^2*d^2 + b^2*c^2 - 2*a*b*c*d))*(a*d - b*c)^(3/2))/b^(5/2)`

sympy [A] time = 14.70, size = 82, normalized size = 0.95

$$\frac{2(c+dx)^{\frac{3}{2}}}{3b} + \frac{\sqrt{c+dx}(-2ad+2bc)}{b^2} + \frac{2(ad-bc)^2 \operatorname{atan}\left(\frac{\sqrt{c+dx}}{\sqrt{\frac{ad-bc}{b}}}\right)}{b^3 \sqrt{\frac{ad-bc}{b}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(3/2)/(b*x+a), x)`

[Out] `2*(c + d*x)**(3/2)/(3*b) + sqrt(c + d*x)*(-2*a*d + 2*b*c)/b**2 + 2*(a*d - b*c)**2*atan(sqrt(c + d*x)/sqrt((a*d - b*c)/b))/(b**3*sqrt((a*d - b*c)/b))`

$$3.1394 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^2} dx$$

Optimal. Leaf size=85

$$-\frac{3d\sqrt{bc-ad} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{5/2}} - \frac{(c+dx)^{3/2}}{b(a+bx)} + \frac{3d\sqrt{c+dx}}{b^2}$$

[Out] $-(d*x+c)^{(3/2)}/b/(b*x+a)-3*d*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})*(-a*d+b*c)^{(1/2)}/b^{(5/2)}+3*d*(d*x+c)^{(1/2)}/b^2$

Rubi [A] time = 0.04, antiderivative size = 85, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 63, 208}

$$-\frac{3d\sqrt{bc-ad} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{5/2}} - \frac{(c+dx)^{3/2}}{b(a+bx)} + \frac{3d\sqrt{c+dx}}{b^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2)/(a + b*x)^2,x]

[Out] $(3*d*\operatorname{Sqrt}[c + d*x])/b^2 - (c + d*x)^{(3/2)}/(b*(a + b*x)) - (3*d*\operatorname{Sqrt}[b*c - a*d]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/(\operatorname{Sqrt}[b*c - a*d])])/b^{(5/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63


```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{3/2}}{(a+bx)^2} dx &= -\frac{(c+dx)^{3/2}}{b(a+bx)} + \frac{(3d) \int \frac{\sqrt{c+dx}}{a+bx} dx}{2b} \\
&= \frac{3d\sqrt{c+dx}}{b^2} - \frac{(c+dx)^{3/2}}{b(a+bx)} + \frac{(3d(bc-ad)) \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{2b^2} \\
&= \frac{3d\sqrt{c+dx}}{b^2} - \frac{(c+dx)^{3/2}}{b(a+bx)} + \frac{(3(bc-ad)) \operatorname{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{b^2} \\
&= \frac{3d\sqrt{c+dx}}{b^2} - \frac{(c+dx)^{3/2}}{b(a+bx)} - \frac{3d\sqrt{bc-ad} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.59

$$\frac{2d(c+dx)^{5/2} {}_2F_1\left(2, \frac{5}{2}; \frac{7}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{5(ad-bc)^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^(3/2)/(a + b*x)^2, x]
```

```
[Out] (2*d*(c + d*x)^(5/2)*Hypergeometric2F1[2, 5/2, 7/2, -((b*(c + d*x))/(-b*c
+ a*d))]/(5*(-(b*c) + a*d)^2)
```

fricas [A] time = 0.47, size = 210, normalized size = 2.47

$$\left[\frac{3(bdx + ad)\sqrt{\frac{bc-ad}{b}} \log\left(\frac{bdx+2bc-ad-2\sqrt{dx+c}b\sqrt{\frac{bc-ad}{b}}}{bx+a}\right) + 2(2bdx - bc + 3ad)\sqrt{dx+c}}{2(b^3x + ab^2)}, - \frac{3(bdx + ad)\sqrt{-\frac{bc-ad}{b}} \arctan\left(\frac{\sqrt{dx+c}b}{b^2}\right)}{2(b^3x + ab^2)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] [1/2*(3*(b*d*x + a*d)*sqrt((b*c - a*d)/b)*log((b*d*x + 2*b*c - a*d - 2*sqrt(d*x + c)*b*sqrt((b*c - a*d)/b))/(b*x + a)) + 2*(2*b*d*x - b*c + 3*a*d)*sqrt(d*x + c)/(b^3*x + a*b^2), -(3*(b*d*x + a*d)*sqrt(-(b*c - a*d)/b)*arctan(-sqrt(d*x + c)*b*sqrt(-(b*c - a*d)/b)/(b*c - a*d)) - (2*b*d*x - b*c + 3*a*d)*sqrt(d*x + c)/(b^3*x + a*b^2)]

giac [A] time = 1.30, size = 113, normalized size = 1.33

$$\frac{2\sqrt{dx+c}d}{b^2} + \frac{3(bcd - ad^2) \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{-b^2c+abd}}\right)}{\sqrt{-b^2c+abd}b^2} - \frac{\sqrt{dx+c}bcd - \sqrt{dx+c}ad^2}{((dx+c)b - bc + ad)b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^2,x, algorithm="giac")

[Out] 2*sqrt(d*x + c)*d/b^2 + 3*(b*c*d - a*d^2)*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/(sqrt(-b^2*c + a*b*d)*b^2) - (sqrt(d*x + c)*b*c*d - sqrt(d*x + c)*a*d^2)/(((d*x + c)*b - b*c + a*d)*b^2)

maple [B] time = 0.01, size = 148, normalized size = 1.74

$$-\frac{3ad^2 \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b^2} + \frac{3cd \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b} + \frac{\sqrt{dx+c}ad^2}{(bdx+ad)b^2} - \frac{\sqrt{dx+c}cd}{(bdx+ad)b} + \frac{2\sqrt{dx+c}d}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/2)/(b*x+a)^2,x)

[Out] 2*d*(d*x+c)^(1/2)/b^2+1/b^2*(d*x+c)^(1/2)/(b*d*x+a*d)*a*d^2-d/b*(d*x+c)^(1/2)/(b*d*x+a*d)*c-3/b^2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)*a*d^2+3*d/b/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)*c

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^2,x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.11, size = 109, normalized size = 1.28

$$\frac{(ad^2 - bcd) \sqrt{c+dx}}{b^3(c+dx) - b^3c + ab^2d} + \frac{2d\sqrt{c+dx}}{b^2} - \frac{3d \operatorname{atan}\left(\frac{\sqrt{b}d\sqrt{ad-bc}\sqrt{c+dx}}{ad^2-bcd}\right) \sqrt{ad-bc}}{b^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(3/2)/(a + b*x)^2,x)

[Out] ((a*d^2 - b*c*d)*(c + d*x)^(1/2))/(b^3*(c + d*x) - b^3*c + a*b^2*d) + (2*d*(c + d*x)^(1/2))/b^2 - (3*d*atan((b^(1/2)*d*(a*d - b*c)^(1/2)*(c + d*x)^(1/2)))/(a*d^2 - b*c*d))*(a*d - b*c)^(1/2))/b^(5/2)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(3/2)/(b*x+a)**2,x)

[Out] Timed out

$$3.1395 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^3} dx$$

Optimal. Leaf size=100

$$-\frac{3d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4b^{5/2}\sqrt{bc-ad}} - \frac{3d\sqrt{c+dx}}{4b^2(a+bx)} - \frac{(c+dx)^{3/2}}{2b(a+bx)^2}$$

[Out] $-1/2*(d*x+c)^{(3/2)}/b/(b*x+a)^2-3/4*d^2*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})/b^{(5/2)}/(-a*d+b*c)^{(1/2)}-3/4*d*(d*x+c)^{(1/2)}/b^2/(b*x+a)$

Rubi [A] time = 0.05, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {47, 63, 208}

$$-\frac{3d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4b^{5/2}\sqrt{bc-ad}} - \frac{3d\sqrt{c+dx}}{4b^2(a+bx)} - \frac{(c+dx)^{3/2}}{2b(a+bx)^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2)/(a + b*x)^3,x]

[Out] $(-3*d*\operatorname{Sqrt}[c + d*x])/(4*b^2*(a + b*x)) - (c + d*x)^{(3/2)}/(2*b*(a + b*x)^2) - (3*d^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/\operatorname{Sqrt}[b*c - a*d]])/(4*b^{(5/2)}*\operatorname{Sqrt}[b*c - a*d])$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208


```
[Out] [1/8*(3*(b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) - 2*(2*b^3*c^2 + a*b^2*c*d - 3*a^2*b*d^2 + 5*(b^3*c*d - a*b^2*d^2)*x)*sqrt(d*x + c))/(a^2*b^4*c - a^3*b^3*d + (b^6*c - a*b^5*d)*x^2 + 2*(a*b^5*c - a^2*b^4*d)*x), 1/4*(3*(b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) - (2*b^3*c^2 + a*b^2*c*d - 3*a^2*b*d^2 + 5*(b^3*c*d - a*b^2*d^2)*x)*sqrt(d*x + c))/(a^2*b^4*c - a^3*b^3*d + (b^6*c - a*b^5*d)*x^2 + 2*(a*b^5*c - a^2*b^4*d)*x)]
```

giac [A] time = 1.36, size = 108, normalized size = 1.08

$$\frac{3d^2 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{4\sqrt{-b^2c+abd}b^2} - \frac{5(dx+c)^{\frac{3}{2}}bd^2 - 3\sqrt{dx+c}bcd^2 + 3\sqrt{dx+c}ad^3}{4((dx+c)b - bc + ad)^2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(3/2)/(b*x+a)^3,x, algorithm="giac")
```

```
[Out] 3/4*d^2*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/(sqrt(-b^2*c + a*b*d)*b^2) - 1/4*(5*(d*x + c)^(3/2)*b*d^2 - 3*sqrt(d*x + c)*b*c*d^2 + 3*sqrt(d*x + c)*a*d^3)/(((d*x + c)*b - b*c + a*d)^2*b^2)
```

maple [A] time = 0.01, size = 121, normalized size = 1.21

$$-\frac{3\sqrt{dx+c}ad^3}{4(bdx+ad)^2b^2} + \frac{3\sqrt{dx+c}cd^2}{4(bdx+ad)^2b} - \frac{5(dx+c)^{\frac{3}{2}}d^2}{4(bdx+ad)^2b} + \frac{3d^2 \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{4\sqrt{(ad-bc)b}b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^(3/2)/(b*x+a)^3,x)
```

```
[Out] -5/4*d^2/(b*d*x+a*d)^2/b*(d*x+c)^(3/2)-3/4*d^3/(b*d*x+a*d)^2/b^2*(d*x+c)^(1/2)*a+3/4*d^2/(b*d*x+a*d)^2/b*(d*x+c)^(1/2)*c+3/4*d^2/b^2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(3/2)/(b*x+a)^3,x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* h
```

elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c positive or negative?

mupad [B] time = 0.28, size = 135, normalized size = 1.35

$$\frac{3d^2 \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{4b^{5/2}\sqrt{ad-bc}} - \frac{\frac{5d^2(c+dx)^{3/2}}{4b} + \frac{3d^2(ad-bc)\sqrt{c+dx}}{4b^2}}{b^2(c+dx)^2 - (2b^2c - 2abd)(c+dx) + a^2d^2 + b^2c^2 - 2abcd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(3/2)/(a + b*x)^3,x)`

[Out] $(3*d^2*\operatorname{atan}((b^{(1/2)}*(c + d*x)^{(1/2)})/(a*d - b*c)^{(1/2)}))/(4*b^{(5/2)}*(a*d - b*c)^{(1/2)}) - ((5*d^2*(c + d*x)^{(3/2)})/(4*b) + (3*d^2*(a*d - b*c)*(c + d*x)^{(1/2)})/(4*b^2))/(b^2*(c + d*x)^2 - (2*b^2*c - 2*a*b*d)*(c + d*x) + a^2*d^2 + b^2*c^2 - 2*a*b*c*d)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(3/2)/(b*x+a)**3,x)`

[Out] Timed out

$$3.1396 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^4} dx$$

Optimal. Leaf size=136

$$\frac{d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8b^{5/2}(bc-ad)^{3/2}} - \frac{d^2\sqrt{c+dx}}{8b^2(a+bx)(bc-ad)} - \frac{d\sqrt{c+dx}}{4b^2(a+bx)^2} - \frac{(c+dx)^{3/2}}{3b(a+bx)^3}$$

[Out] $-1/3*(d*x+c)^{(3/2)}/b/(b*x+a)^3+1/8*d^3*\arctanh(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/b^{(5/2)/(-a*d+b*c)^{(3/2)}-1/4*d*(d*x+c)^{(1/2)}/b^2/(b*x+a)^2-1/8*d^2*(d*x+c)^{(1/2)}/b^2/(-a*d+b*c)/(b*x+a)$

Rubi [A] time = 0.06, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 51, 63, 208}

$$-\frac{d^2\sqrt{c+dx}}{8b^2(a+bx)(bc-ad)} + \frac{d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8b^{5/2}(bc-ad)^{3/2}} - \frac{d\sqrt{c+dx}}{4b^2(a+bx)^2} - \frac{(c+dx)^{3/2}}{3b(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2)/(a + b*x)^4, x]

[Out] $-(d*\text{Sqrt}[c + d*x])/(4*b^2*(a + b*x)^2) - (d^2*\text{Sqrt}[c + d*x])/(8*b^2*(b*c - a*d)*(a + b*x)) - (c + d*x)^{(3/2)}/(3*b*(a + b*x)^3) + (d^3*\text{ArcTanh}[(\text{Sqrt}[b]*\text{Sqrt}[c + d*x])/\text{Sqrt}[b*c - a*d]])/(8*b^{(5/2)}*(b*c - a*d)^{(3/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{3/2}}{(a+bx)^4} dx &= -\frac{(c+dx)^{3/2}}{3b(a+bx)^3} + \frac{d \int \frac{\sqrt{c+dx}}{(a+bx)^3} dx}{2b} \\
&= -\frac{d\sqrt{c+dx}}{4b^2(a+bx)^2} - \frac{(c+dx)^{3/2}}{3b(a+bx)^3} + \frac{d^2 \int \frac{1}{(a+bx)^2\sqrt{c+dx}} dx}{8b^2} \\
&= -\frac{d\sqrt{c+dx}}{4b^2(a+bx)^2} - \frac{d^2\sqrt{c+dx}}{8b^2(bc-ad)(a+bx)} - \frac{(c+dx)^{3/2}}{3b(a+bx)^3} - \frac{d^3 \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{16b^2(bc-ad)} \\
&= -\frac{d\sqrt{c+dx}}{4b^2(a+bx)^2} - \frac{d^2\sqrt{c+dx}}{8b^2(bc-ad)(a+bx)} - \frac{(c+dx)^{3/2}}{3b(a+bx)^3} - \frac{d^2 \operatorname{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{8b^2(bc-ad)} \\
&= -\frac{d\sqrt{c+dx}}{4b^2(a+bx)^2} - \frac{d^2\sqrt{c+dx}}{8b^2(bc-ad)(a+bx)} - \frac{(c+dx)^{3/2}}{3b(a+bx)^3} + \frac{d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8b^{5/2}(bc-ad)^{3/2}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.38

$$\frac{2d^3(c+dx)^{5/2} {}_2F_1\left(\frac{5}{2}, 4; \frac{7}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{5(ad-bc)^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^(3/2)/(a + b*x)^4, x]
```

```
[Out] (2*d^3*(c + d*x)^(5/2)*Hypergeometric2F1[5/2, 4, 7/2, -((b*(c + d*x))/(-b*c
+ a*d))]/(5*(-(b*c) + a*d)^4)
```

fricas [B] time = 0.50, size = 666, normalized size = 4.90

$$\left[\frac{3 \left(b^3 d^3 x^3 + 3 a b^2 d^3 x^2 + 3 a^2 b d^3 x + a^3 d^3 \right) \sqrt{b^2 c - a b d} \log \left(\frac{b d x + 2 b c - a d - 2 \sqrt{b^2 c - a b d} \sqrt{d x + c}}{b x + a} \right) + 2 \left(8 b^4 c^3 - 10 a b^3 c^2 d - 2 a^2 b^2 c d^2 + 3 a^3 b d^3 \right)}{48 \left(a^3 b^5 c^2 - 2 a^4 b^4 c d + a^5 b^3 d^2 + \left(b^8 c^2 - 2 a b^7 c d + a^2 b^6 d^2 \right) x^3 + 3 \left(a b^7 c^2 - 2 a^2 b^6 c d + a^3 b^5 d^2 \right) x^2 + 3 \left(a^2 b^6 c^2 - 2 a^3 b^5 c d + a^4 b^4 d^2 \right) x + 3 \left(a b^5 c^2 - 2 a^2 b^4 c d + a^3 b^3 d^2 \right)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^4,x, algorithm="fricas")

[Out] [-1/48*(3*(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) + 2*(8*b^4*c^3 - 10*a*b^3*c^2*d - a^2*b^2*c*d^2 + 3*a^3*b*d^3 + 3*(b^4*c*d^2 - a*b^3*d^3)*x^2 + 2*(7*b^4*c^2*d - 11*a*b^3*c*d^2 + 4*a^2*b^2*d^3)*x)*sqrt(d*x + c))/(a^3*b^5*c^2 - 2*a^4*b^4*c*d + a^5*b^3*d^2 + (b^8*c^2 - 2*a*b^7*c*d + a^2*b^6*d^2)*x^3 + 3*(a*b^7*c^2 - 2*a^2*b^6*c*d + a^3*b^5*d^2)*x^2 + 3*(a^2*b^6*c^2 - 2*a^3*b^5*c*d + a^4*b^4*d^2)*x), -1/24*(3*(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) + (8*b^4*c^3 - 10*a*b^3*c^2*d - a^2*b^2*c*d^2 + 3*a^3*b*d^3 + 3*(b^4*c*d^2 - a*b^3*d^3)*x^2 + 2*(7*b^4*c^2*d - 11*a*b^3*c*d^2 + 4*a^2*b^2*d^3)*x)*sqrt(d*x + c))/(a^3*b^5*c^2 - 2*a^4*b^4*c*d + a^5*b^3*d^2 + (b^8*c^2 - 2*a*b^7*c*d + a^2*b^6*d^2)*x^3 + 3*(a*b^7*c^2 - 2*a^2*b^6*c*d + a^3*b^5*d^2)*x^2 + 3*(a^2*b^6*c^2 - 2*a^3*b^5*c*d + a^4*b^4*d^2)*x)]

giac [A] time = 1.40, size = 185, normalized size = 1.36

$$\frac{d^3 \arctan \left(\frac{\sqrt{d x + c} b}{\sqrt{-b^2 c + a b d}} \right)}{8 \left(b^3 c - a b^2 d \right) \sqrt{-b^2 c + a b d}} - \frac{3 (d x + c)^{\frac{5}{2}} b^2 d^3 + 8 (d x + c)^{\frac{3}{2}} b^2 c d^3 - 3 \sqrt{d x + c} b^2 c^2 d^3 - 8 (d x + c)^{\frac{3}{2}} a b d^4 + 6 \sqrt{d x + c} a^2 b d^4}{24 \left(b^3 c - a b^2 d \right) \left((d x + c) b - b c + a d \right)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^4,x, algorithm="giac")

[Out] -1/8*d^3*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/((b^3*c - a*b^2*d)*sqrt(-b^2*c + a*b*d)) - 1/24*(3*(d*x + c)^(5/2)*b^2*d^3 + 8*(d*x + c)^(3/2)*b^2*c*d^3 - 3*sqrt(d*x + c)*b^2*c^2*d^3 - 8*(d*x + c)^(3/2)*a*b*d^4 + 6*sqrt(d*x + c)*a*b*c*d^4 - 3*sqrt(d*x + c)*a^2*d^5)/((b^3*c - a*b^2*d)*((d*x + c)*b - b*c + a*d)^3)

maple [A] time = 0.02, size = 163, normalized size = 1.20

$$-\frac{\sqrt{d x + c} a d^4}{8 (b d x + a d)^3 b^2} + \frac{\sqrt{d x + c} c d^3}{8 (b d x + a d)^3 b} + \frac{(d x + c)^{\frac{5}{2}} d^3}{8 (b d x + a d)^3 (a d - b c)} - \frac{(d x + c)^{\frac{3}{2}} d^3}{3 (b d x + a d)^3 b} + \frac{d^3 \arctan \left(\frac{\sqrt{d x + c} b}{\sqrt{(a d - b c) b}} \right)}{8 (a d - b c) \sqrt{(a d - b c) b} b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(3/2)/(b*x+a)^4,x)`

[Out] $\frac{1}{8}d^3/(b*d*x+a*d)^3/(a*d-b*c)*(d*x+c)^{(5/2)} - \frac{1}{3}d^3/(b*d*x+a*d)^3/b*(d*x+c)^{(3/2)} - \frac{1}{8}d^4/(b*d*x+a*d)^3/b^2*(d*x+c)^{(1/2)*a} + \frac{1}{8}d^3/(b*d*x+a*d)^3/b*(d*x+c)^{(1/2)*c} + \frac{1}{8}d^3/(a*d-b*c)/b^2/((a*d-b*c)*b)^{(1/2)*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)*b}}$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(3/2)/(b*x+a)^4,x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.34, size = 209, normalized size = 1.54

$$\frac{d^3 \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{8b^{5/2}(ad-bc)^{3/2}} \frac{\frac{d^3(c+dx)^{3/2}}{3b} - \frac{d^3(c+dx)^{5/2}}{8(ad-bc)} + \frac{d^3(ad-bc)\sqrt{c+dx}}{8b^2}}{(c+dx)\left(3a^2bd^2 - 6ab^2cd + 3b^3c^2\right) + b^3(c+dx)^3 - \left(3b^3c - 3ab^2d\right)(c+dx)^2 + a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(3/2)/(a + b*x)^4,x)`

[Out] $(d^3*\operatorname{atan}((b^{(1/2)}*(c + d*x)^{(1/2)})/(a*d - b*c)^{(1/2)}))/(8*b^{(5/2)}*(a*d - b*c)^{(3/2)}) - ((d^3*(c + d*x)^{(3/2)})/(3*b) - (d^3*(c + d*x)^{(5/2)})/(8*(a*d - b*c))) + (d^3*(a*d - b*c)*(c + d*x)^{(1/2)})/(8*b^2))/((c + d*x)*(3*b^3*c^2 + 3*a^2*b*d^2 - 6*a*b^2*c*d) + b^3*(c + d*x)^3 - (3*b^3*c - 3*a*b^2*d)*(c + d*x)^2 + a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(3/2)/(b*x+a)**4,x)`

[Out] Timed out

$$3.1397 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^5} dx$$

Optimal. Leaf size=172

$$-\frac{3d^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{64b^{5/2}(bc-ad)^{5/2}} + \frac{3d^3\sqrt{c+dx}}{64b^2(a+bx)(bc-ad)^2} - \frac{d^2\sqrt{c+dx}}{32b^2(a+bx)^2(bc-ad)} - \frac{d\sqrt{c+dx}}{8b^2(a+bx)^3} - \frac{(c+dx)^{3/2}}{4b(a+bx)^4}$$

[Out] $-1/4*(d*x+c)^{(3/2)}/b/(b*x+a)^4-3/64*d^4*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})/b^{(5/2)}/(-a*d+b*c)^{(5/2)}-1/8*d*(d*x+c)^{(1/2)}/b^2/(b*x+a)^3-1/32*d^2*(d*x+c)^{(1/2)}/b^2/(-a*d+b*c)/(b*x+a)^2+3/64*d^3*(d*x+c)^{(1/2)}/b^2/(-a*d+b*c)^2/(b*x+a)$

Rubi [A] time = 0.07, antiderivative size = 172, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 51, 63, 208}

$$\frac{3d^3\sqrt{c+dx}}{64b^2(a+bx)(bc-ad)^2} - \frac{d^2\sqrt{c+dx}}{32b^2(a+bx)^2(bc-ad)} - \frac{3d^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{64b^{5/2}(bc-ad)^{5/2}} - \frac{d\sqrt{c+dx}}{8b^2(a+bx)^3} - \frac{(c+dx)^{3/2}}{4b(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2)/(a + b*x)^5, x]

[Out] $-(d*\operatorname{Sqrt}[c + d*x])/(8*b^2*(a + b*x)^3) - (d^2*\operatorname{Sqrt}[c + d*x])/(32*b^2*(b*c - a*d)*(a + b*x)^2) + (3*d^3*\operatorname{Sqrt}[c + d*x])/(64*b^2*(b*c - a*d)^2*(a + b*x)) - (c + d*x)^{(3/2)}/(4*b*(a + b*x)^4) - (3*d^4*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/(\operatorname{Sqrt}[b*c - a*d])]/(64*b^{(5/2)}*(b*c - a*d)^{(5/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ

$[n, -1] \&\& (\text{EqQ}[a, 0] \mid\mid (\text{NeQ}[c, 0] \&\& \text{LtQ}[m - n, 0] \&\& \text{IntegerQ}[n])) \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\text{Int}[\{(a_.) + (b_.)(x_.)\}^{(m_)} \cdot \{(c_.) + (d_.)(x_.)\}^{(n_)}, x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p(m+1)-1)} \cdot (c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /; \text{FreeQ}[\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 208

$\text{Int}[\{(a_.) + (b_.)(x_.)^2\}^{(-1)}, x_Symbol] \rightarrow \text{Simp}[(\text{Rt}[-(a/b), 2] * \text{ArcTanh}[x/\text{Rt}[-(a/b), 2]])/a, x] /; \text{FreeQ}[\{a, b\}, x] \&\& \text{NegQ}[a/b]$

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^{3/2}}{(a+bx)^5} dx &= -\frac{(c+dx)^{3/2}}{4b(a+bx)^4} + \frac{(3d) \int \frac{\sqrt{c+dx}}{(a+bx)^4} dx}{8b} \\ &= -\frac{d\sqrt{c+dx}}{8b^2(a+bx)^3} - \frac{(c+dx)^{3/2}}{4b(a+bx)^4} + \frac{d^2 \int \frac{1}{(a+bx)^3 \sqrt{c+dx}} dx}{16b^2} \\ &= -\frac{d\sqrt{c+dx}}{8b^2(a+bx)^3} - \frac{d^2\sqrt{c+dx}}{32b^2(bc-ad)(a+bx)^2} - \frac{(c+dx)^{3/2}}{4b(a+bx)^4} - \frac{(3d^3) \int \frac{1}{(a+bx)^2 \sqrt{c+dx}} dx}{64b^2(bc-ad)} \\ &= -\frac{d\sqrt{c+dx}}{8b^2(a+bx)^3} - \frac{d^2\sqrt{c+dx}}{32b^2(bc-ad)(a+bx)^2} + \frac{3d^3\sqrt{c+dx}}{64b^2(bc-ad)^2(a+bx)} - \frac{(c+dx)^{3/2}}{4b(a+bx)^4} + \frac{(3d^4) \int \frac{1}{a+bx} dx}{128b^2} \\ &= -\frac{d\sqrt{c+dx}}{8b^2(a+bx)^3} - \frac{d^2\sqrt{c+dx}}{32b^2(bc-ad)(a+bx)^2} + \frac{3d^3\sqrt{c+dx}}{64b^2(bc-ad)^2(a+bx)} - \frac{(c+dx)^{3/2}}{4b(a+bx)^4} + \frac{(3d^3) \text{Su}}{128b^2} \\ &= -\frac{d\sqrt{c+dx}}{8b^2(a+bx)^3} - \frac{d^2\sqrt{c+dx}}{32b^2(bc-ad)(a+bx)^2} + \frac{3d^3\sqrt{c+dx}}{64b^2(bc-ad)^2(a+bx)} - \frac{(c+dx)^{3/2}}{4b(a+bx)^4} - \frac{3d^4 \text{tan}}{64b^5} \end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.30

$$\frac{2d^4(c+dx)^{5/2} {}_2F_1\left(\frac{5}{2}, 5; \frac{7}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{5(ad-bc)^5}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/2)/(a + b*x)^5,x]

[Out] (2*d^4*(c + d*x)^(5/2)*Hypergeometric2F1[5/2, 5, 7/2, -((b*(c + d*x))/(-(b*c) + a*d))]/(5*(-(b*c) + a*d)^5)

fricas [B] time = 0.49, size = 1043, normalized size = 6.06

$$\frac{3 \left(b^4 d^4 x^4 + 4 a b^3 d^4 x^3 + 6 a^2 b^2 d^4 x^2 + 4 a^3 b d^4 x + a^4 d^4 \right) \sqrt{b^2 c - a b d} \log \left(\frac{b d x + 2 b c - a d - 2 \sqrt{b^2 c - a b d} \sqrt{d x + c}}{b x + a} \right) - 2 \left(16 b^5 c^4 - 128 \left(a^4 b^6 c^3 - 3 a^5 b^5 c^2 d + 3 a^6 b^4 c d^2 - a^7 b^3 d^3 + \left(b^{10} c^3 - 3 a b^9 c^2 d + 3 a^2 b^8 c d^2 - a^3 b^7 d^3 \right) \right)}{\right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^5,x, algorithm="fricas")

[Out] [1/128*(3*(b^4*d^4*x^4 + 4*a*b^3*d^4*x^3 + 6*a^2*b^2*d^4*x^2 + 4*a^3*b*d^4*x + a^4*d^4)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) - 2*(16*b^5*c^4 - 40*a*b^4*c^3*d + 26*a^2*b^3*c^2*d^2 + a^3*b^2*c*d^3 - 3*a^4*b*d^4 - 3*(b^5*c*d^3 - a*b^4*d^4)*x^3 + (2*b^5*c^2*d^2 - 13*a*b^4*c*d^3 + 11*a^2*b^3*d^4)*x^2 + (24*b^5*c^3*d - 68*a*b^4*c^2*d^2 + 55*a^2*b^3*c*d^3 - 11*a^3*b^2*d^4)*x)*sqrt(d*x + c))/(a^4*b^6*c^3 - 3*a^5*b^5*c^2*d + 3*a^6*b^4*c*d^2 - a^7*b^3*d^3 + (b^10*c^3 - 3*a*b^9*c^2*d + 3*a^2*b^8*c*d^2 - a^3*b^7*d^3)*x^4 + 4*(a*b^9*c^3 - 3*a^2*b^8*c^2*d + 3*a^3*b^7*c*d^2 - a^4*b^6*d^3)*x^3 + 6*(a^2*b^8*c^3 - 3*a^3*b^7*c^2*d + 3*a^4*b^6*c*d^2 - a^5*b^5*d^3)*x^2 + 4*(a^3*b^7*c^3 - 3*a^4*b^6*c^2*d + 3*a^5*b^5*c*d^2 - a^6*b^4*d^3)*x), 1/64*(3*(b^4*d^4*x^4 + 4*a*b^3*d^4*x^3 + 6*a^2*b^2*d^4*x^2 + 4*a^3*b*d^4*x + a^4*d^4)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) - (16*b^5*c^4 - 40*a*b^4*c^3*d + 26*a^2*b^3*c^2*d^2 + a^3*b^2*c*d^3 - 3*a^4*b*d^4 - 3*(b^5*c*d^3 - a*b^4*d^4)*x^3 + (2*b^5*c^2*d^2 - 13*a*b^4*c*d^3 + 11*a^2*b^3*d^4)*x^2 + (24*b^5*c^3*d - 68*a*b^4*c^2*d^2 + 55*a^2*b^3*c*d^3 - 11*a^3*b^2*d^4)*x)*sqrt(d*x + c))/(a^4*b^6*c^3 - 3*a^5*b^5*c^2*d + 3*a^6*b^4*c*d^2 - a^7*b^3*d^3 + (b^10*c^3 - 3*a*b^9*c^2*d + 3*a^2*b^8*c*d^2 - a^3*b^7*d^3)*x^4 + 4*(a*b^9*c^3 - 3*a^2*b^8*c^2*d + 3*a^3*b^7*c*d^2 - a^4*b^6*d^3)*x^3 + 6*(a^2*b^8*c^3 - 3*a^3*b^7*c^2*d + 3*a^4*b^6*c*d^2 - a^5*b^5*d^3)*x^2 + 4*(a^3*b^7*c^3 - 3*a^4*b^6*c^2*d + 3*a^5*b^5*c*d^2 - a^6*b^4*d^3)*x)]

giac [A] time = 1.47, size = 285, normalized size = 1.66

$$\frac{3 d^4 \arctan \left(\frac{\sqrt{d x + c b}}{\sqrt{-b^2 c + a b d}} \right)}{64 \left(b^4 c^2 - 2 a b^3 c d + a^2 b^2 d^2 \right) \sqrt{-b^2 c + a b d}} + \frac{3 (d x + c)^{\frac{7}{2}} b^3 d^4 - 11 (d x + c)^{\frac{5}{2}} b^3 c d^4 - 11 (d x + c)^{\frac{3}{2}} b^3 c^2 d^4 + 3 \sqrt{d x + c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^5,x, algorithm="giac")

[Out] $\frac{3}{64}d^4 \arctan\left(\frac{\sqrt{d*x+c} * b}{\sqrt{-b^2*c + a*b*d}}\right) / ((b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2) * \sqrt{-b^2*c + a*b*d}) + \frac{1}{64} * (3*(d*x+c)^{(7/2)} * b^3*d^4 - 11*(d*x+c)^{(5/2)} * b^3*c*d^4 - 11*(d*x+c)^{(3/2)} * b^3*c^2*d^4 + 3*\sqrt{d*x+c} * b^3*c^3*d^4 + 11*(d*x+c)^{(5/2)} * a*b^2*d^5 + 22*(d*x+c)^{(3/2)} * a*b^2*c*d^5 - 9*\sqrt{d*x+c} * a*b^2*c^2*d^5 - 11*(d*x+c)^{(3/2)} * a^2*b*d^6 + 9*\sqrt{d*x+c} * a^2*b*c*d^6 - 3*\sqrt{d*x+c} * a^3*d^7) / ((b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2) * ((d*x+c)*b - b*c + a*d)^4)$

maple [A] time = 0.02, size = 222, normalized size = 1.29

$$\frac{3(dx+c)^{\frac{7}{2}} b d^4}{64(bdx+ad)^4(a^2d^2-2abcd+b^2c^2)} - \frac{3\sqrt{dx+c} a d^5}{64(bdx+ad)^4 b^2} + \frac{3\sqrt{dx+c} c d^4}{64(bdx+ad)^4 b} + \frac{11(dx+c)^{\frac{5}{2}} d^4}{64(bdx+ad)^4(ad-bc)} - \frac{11(dx+c)^{\frac{3}{2}} d^4}{64(bdx+ad)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/2)/(b*x+a)^5,x)

[Out] $\frac{3}{64}d^4/(b*d*x+a*d)^4*b/(a^2*d^2-2*a*b*c*d+b^2*c^2)*(d*x+c)^{(7/2)}+11/64*d^4/(b*d*x+a*d)^4/(a*d-b*c)*(d*x+c)^{(5/2)}-11/64*d^4/(b*d*x+a*d)^4/b*(d*x+c)^{(3/2)}-3/64*d^5/(b*d*x+a*d)^4/b^2*(d*x+c)^{(1/2)}*a+3/64*d^4/(b*d*x+a*d)^4/b*(d*x+c)^{(1/2)}*c+3/64*d^4/(a^2*d^2-2*a*b*c*d+b^2*c^2)/b^2/((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^5,x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.37, size = 296, normalized size = 1.72

$$\frac{3d^4 \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{64b^{5/2}(ad-bc)^{5/2}} - \frac{11d^4(c+dx)^{3/2}}{64b} - \frac{11d^4}{64} - \frac{b^4(c+dx)^4 - (4b^4c - 4ab^3d)(c+dx)^3 - (c+dx)(-4a^3bd^3 + 12a^2b^2cd^2 - 12ab^3d^2)}{64b^4(c+dx)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(3/2)/(a + b*x)^5,x)
```

```
[Out] (3*d^4*atan((b^(1/2)*(c + d*x)^(1/2))/(a*d - b*c)^(1/2)))/(64*b^(5/2)*(a*d - b*c)^(5/2)) - ((11*d^4*(c + d*x)^(3/2))/(64*b) - (11*d^4*(c + d*x)^(5/2))/(64*(a*d - b*c)) + (3*d^4*(a*d - b*c)*(c + d*x)^(1/2))/(64*b^2) - (3*b*d^4*(c + d*x)^(7/2))/(64*(a*d - b*c)^2))/(b^4*(c + d*x)^4 - (4*b^4*c - 4*a*b^3*d)*(c + d*x)^3 - (c + d*x)*(4*b^4*c^3 - 4*a^3*b*d^3 + 12*a^2*b^2*c*d^2 - 12*a*b^3*c^2*d) + a^4*d^4 + b^4*c^4 + (c + d*x)^2*(6*b^4*c^2 + 6*a^2*b^2*d^2 - 12*a*b^3*c*d) + 6*a^2*b^2*c^2*d^2 - 4*a*b^3*c^3*d - 4*a^3*b*c*d^3)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(3/2)/(b*x+a)**5,x)
```

```
[Out] Timed out
```


$$3.1398 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^6} dx$$

Optimal. Leaf size=208

$$\frac{3d^5 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{128b^{5/2}(bc-ad)^{7/2}} - \frac{3d^4\sqrt{c+dx}}{128b^2(a+bx)(bc-ad)^3} + \frac{d^3\sqrt{c+dx}}{64b^2(a+bx)^2(bc-ad)^2} - \frac{d^2\sqrt{c+dx}}{80b^2(a+bx)^3(bc-ad)} - \frac{3d\sqrt{c+dx}}{40b^2(a+bx)^4}$$

[Out] $-1/5*(d*x+c)^{(3/2)}/b/(b*x+a)^5+3/128*d^5*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})/b^{(5/2)}/(-a*d+b*c)^{(7/2)}-3/40*d*(d*x+c)^{(1/2)}/b^2/(b*x+a)^4-1/80*d^2*(d*x+c)^{(1/2)}/b^2/(-a*d+b*c)/(b*x+a)^3+1/64*d^3*(d*x+c)^{(1/2)}/b^2/(-a*d+b*c)^2/(b*x+a)^2-3/128*d^4*(d*x+c)^{(1/2)}/b^2/(-a*d+b*c)^3/(b*x+a)$

Rubi [A] time = 0.09, antiderivative size = 208, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 51, 63, 208}

$$-\frac{3d^4\sqrt{c+dx}}{128b^2(a+bx)(bc-ad)^3} + \frac{d^3\sqrt{c+dx}}{64b^2(a+bx)^2(bc-ad)^2} - \frac{d^2\sqrt{c+dx}}{80b^2(a+bx)^3(bc-ad)} + \frac{3d^5 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{128b^{5/2}(bc-ad)^{7/2}} - \frac{3d\sqrt{c+dx}}{40b^2(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2)/(a + b*x)^6, x]

[Out] $(-3*d*\operatorname{Sqrt}[c + d*x])/(40*b^2*(a + b*x)^4) - (d^2*\operatorname{Sqrt}[c + d*x])/(80*b^2*(b*c - a*d)*(a + b*x)^3) + (d^3*\operatorname{Sqrt}[c + d*x])/(64*b^2*(b*c - a*d)^2*(a + b*x)^2) - (3*d^4*\operatorname{Sqrt}[c + d*x])/(128*b^2*(b*c - a*d)^3*(a + b*x)) - (c + d*x)^{(3/2)}/(5*b*(a + b*x)^5) + (3*d^5*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/\operatorname{Sqrt}[b*c - a*d]])/(128*b^{(5/2)}*(b*c - a*d)^{(7/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x]

```
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_)^(m_))*((c_.) + (d_.)*(x_)^(n_)), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{3/2}}{(a+bx)^6} dx &= -\frac{(c+dx)^{3/2}}{5b(a+bx)^5} + \frac{(3d) \int \frac{\sqrt{c+dx}}{(a+bx)^5} dx}{10b} \\
&= -\frac{3d\sqrt{c+dx}}{40b^2(a+bx)^4} - \frac{(c+dx)^{3/2}}{5b(a+bx)^5} + \frac{(3d^2) \int \frac{1}{(a+bx)^4\sqrt{c+dx}} dx}{80b^2} \\
&= -\frac{3d\sqrt{c+dx}}{40b^2(a+bx)^4} - \frac{d^2\sqrt{c+dx}}{80b^2(bc-ad)(a+bx)^3} - \frac{(c+dx)^{3/2}}{5b(a+bx)^5} - \frac{d^3 \int \frac{1}{(a+bx)^3\sqrt{c+dx}} dx}{32b^2(bc-ad)} \\
&= -\frac{3d\sqrt{c+dx}}{40b^2(a+bx)^4} - \frac{d^2\sqrt{c+dx}}{80b^2(bc-ad)(a+bx)^3} + \frac{d^3\sqrt{c+dx}}{64b^2(bc-ad)^2(a+bx)^2} - \frac{(c+dx)^{3/2}}{5b(a+bx)^5} + \frac{(3d^4) \int \frac{1}{(a+bx)^2\sqrt{c+dx}} dx}{128b^2(bc-ad)} \\
&= -\frac{3d\sqrt{c+dx}}{40b^2(a+bx)^4} - \frac{d^2\sqrt{c+dx}}{80b^2(bc-ad)(a+bx)^3} + \frac{d^3\sqrt{c+dx}}{64b^2(bc-ad)^2(a+bx)^2} - \frac{3d^4\sqrt{c+dx}}{128b^2(bc-ad)^3(a+bx)} \\
&= -\frac{3d\sqrt{c+dx}}{40b^2(a+bx)^4} - \frac{d^2\sqrt{c+dx}}{80b^2(bc-ad)(a+bx)^3} + \frac{d^3\sqrt{c+dx}}{64b^2(bc-ad)^2(a+bx)^2} - \frac{3d^4\sqrt{c+dx}}{128b^2(bc-ad)^3(a+bx)} \\
&= -\frac{3d\sqrt{c+dx}}{40b^2(a+bx)^4} - \frac{d^2\sqrt{c+dx}}{80b^2(bc-ad)(a+bx)^3} + \frac{d^3\sqrt{c+dx}}{64b^2(bc-ad)^2(a+bx)^2} - \frac{3d^4\sqrt{c+dx}}{128b^2(bc-ad)^3(a+bx)}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.25

$$\frac{2d^5(c+dx)^{5/2} {}_2F_1\left(\frac{5}{2}, 6; \frac{7}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{5(ad-bc)^6}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/2)/(a + b*x)^6, x]

[Out] (2*d^5*(c + d*x)^(5/2)*Hypergeometric2F1[5/2, 6, 7/2, -(b*(c + d*x))/(-(b*c) + a*d)])/(5*(-(b*c) + a*d)^6)

fricas [B] time = 0.48, size = 1492, normalized size = 7.17

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^6, x, algorithm="fricas")

[Out] [-1/1280*(15*(b^5*d^5*x^5 + 5*a*b^4*d^5*x^4 + 10*a^2*b^3*d^5*x^3 + 10*a^3*b^2*d^5*x^2 + 5*a^4*b*d^5*x + a^5*d^5)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) + 2*(128*b^6*c^5 - 464*a*b^5*c^4*d + 584*a^2*b^4*c^3*d^2 - 258*a^3*b^3*c^2*d^3 - 5*a^4*b^2*c*d^4 + 15*a^5*b*d^5 + 15*(b^6*c*d^4 - a*b^5*d^5)*x^4 - 10*(b^6*c^2*d^3 - 8*a*b^5*c*d^4 + 7*a^2*b^4*d^5)*x^3 + 2*(4*b^6*c^3*d^2 - 27*a*b^5*c^2*d^3 + 87*a^2*b^4*c*d^4 - 64*a^3*b^3*d^5)*x^2 + 2*(88*b^6*c^4*d - 344*a*b^5*c^3*d^2 + 489*a^2*b^4*c^2*d^3 - 268*a^3*b^3*c*d^4 + 35*a^4*b^2*d^5)*x)*sqrt(d*x + c)/(a^5*b^7*c^4 - 4*a^6*b^6*c^3*d + 6*a^7*b^5*c^2*d^2 - 4*a^8*b^4*c*d^3 + a^9*b^3*d^4 + (b^12*c^4 - 4*a*b^11*c^3*d + 6*a^2*b^10*c^2*d^2 - 4*a^3*b^9*c*d^3 + a^4*b^8*d^4)*x^5 + 5*(a*b^11*c^4 - 4*a^2*b^10*c^3*d + 6*a^3*b^9*c^2*d^2 - 4*a^4*b^8*c*d^3 + a^5*b^7*d^4)*x^4 + 10*(a^2*b^10*c^4 - 4*a^3*b^9*c^3*d + 6*a^4*b^8*c^2*d^2 - 4*a^5*b^7*c*d^3 + a^6*b^6*d^4)*x^3 + 10*(a^3*b^9*c^4 - 4*a^4*b^8*c^3*d + 6*a^5*b^7*c^2*d^2 - 4*a^6*b^6*c*d^3 + a^7*b^5*d^4)*x^2 + 5*(a^4*b^8*c^4 - 4*a^5*b^7*c^3*d + 6*a^6*b^6*c^2*d^2 - 4*a^7*b^5*c*d^3 + a^8*b^4*d^4)*x), -1/640*(15*(b^5*d^5*x^5 + 5*a*b^4*d^5*x^4 + 10*a^2*b^3*d^5*x^3 + 10*a^3*b^2*d^5*x^2 + 5*a^4*b*d^5*x + a^5*d^5)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) + (128*b^6*c^5 - 464*a*b^5*c^4*d + 584*a^2*b^4*c^3*d^2 - 258*a^3*b^3*c^2*d^3 - 5*a^4*b^2*c*d^4 + 15*a^5*b*d^5 + 15*(b^6*c*d^4 - a*b^5*d^5)*x^4 - 10*(b^6*c^2*d^3 - 8*a*b^5*c*d^4 + 7*a^2*b^4*d^5)*x^3 + 2*(4*b^6*c^3*d^2 - 27*a*b^5*c^2*d^3 + 87*a^2*b^4*c*d^4 - 64*a^3*b^3*d^5)*x^2 + 2*(88*b^6*c^4*d - 344*a*b^5*c^3*d^2 + 489*a^2*b^4*c^2*d^3 - 268*a^3*b^3*c*d^4 + 35*a^4*b^2*d^5)*x)*sqrt(d*x + c)/(a^5*b^7*c^4 - 4*a^6*b^6*c^3*d + 6*a^7*b^5*c^2*d^2 - 4*a^8*b^4*c*d^3 + a^9*b^3*d^4 + (b^12*c^4 - 4*a*b^11*c^3*d + 6*a^2*b^10*c^2*d^2 - 4*a^3*b^9*c*d^3 + a^4*b^8*d^4)*x^5 + 5*(a*b^11*c^4 - 4*a^2*b^10*c^3*d + 6*a^3*b^9*c^2*d^2 - 4*a^4*b^8*c*d^3 + a^5*b^7*d^4)*x^4 + 10*(a^2*b^10*c^4 - 4*a^3*b^9*c^3*d + 6*a^4*b^8*c^2*d^2 - 4*a^5*b^7*c*d^3 + a^6*b^6*d^4)*x^3 + 10*(a^3*b^9*c^4 - 4*a^4*b^8*c^3*d + 6*a^5*b^7*c^2*d^2 - 4*a^6*b^6*c*d^3 + a^7*b^5*d^4)*x^2 + 5*(a^4*b^8*c^4 - 4*a^5*b^7*c^3*d + 6*a^6*b^6*c^2*d^2 - 4*a^7*b^5*c*d^3 + a^8*b^4*d^4)*x)

$3 + a^4 b^8 d^4) x^5 + 5(a^5 b^{11} c^4 - 4a^2 b^{10} c^3 d + 6a^3 b^9 c^2 d^2 - 4a^4 b^8 c d^3 + a^5 b^7 d^4) x^4 + 10(a^2 b^{10} c^4 - 4a^3 b^9 c^3 d + 6a^4 b^8 c^2 d^2 - 4a^5 b^7 c d^3 + a^6 b^6 d^4) x^3 + 10(a^3 b^9 c^4 - 4a^4 b^8 c^3 d + 6a^5 b^7 c^2 d^2 - 4a^6 b^6 c d^3 + a^7 b^5 d^4) x^2 + 5(a^4 b^8 c^4 - 4a^5 b^7 c^3 d + 6a^6 b^6 c^2 d^2 - 4a^7 b^5 c d^3 + a^8 b^4 d^4) x]$

giac [B] time = 1.39, size = 410, normalized size = 1.97

$$\frac{3d^5 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{128(b^5c^3 - 3ab^4c^2d + 3a^2b^3cd^2 - a^3b^2d^3)\sqrt{-b^2c+abd}} - \frac{15(dx+c)^{\frac{9}{2}}b^4d^5 - 70(dx+c)^{\frac{7}{2}}b^4cd^5 + 128(dx+c)^{\frac{5}{2}}}{128(bdx+ad)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^6,x, algorithm="giac")

[Out] $-3/128*d^5*\arctan(\sqrt{d*x+c}*b/\sqrt{-b^2*c+a*b*d})/((b^5*c^3-3*a*b^4*c^2*d+3*a^2*b^3*c*d^2-a^3*b^2*d^3)*\sqrt{-b^2*c+a*b*d})-1/640*(15*(d*x+c)^{(9/2)}*b^4*d^5-70*(d*x+c)^{(7/2)}*b^4*c*d^5+128*(d*x+c)^{(5/2)}*b^4*c^2*d^5+70*(d*x+c)^{(3/2)}*b^4*c^3*d^5-15*\sqrt{d*x+c}*b^4*c^4*d^5+70*(d*x+c)^{(7/2)}*a*b^3*d^6-256*(d*x+c)^{(5/2)}*a*b^3*c*d^6-210*(d*x+c)^{(3/2)}*a*b^3*c^2*d^6+60*\sqrt{d*x+c}*a*b^3*c^3*d^6+128*(d*x+c)^{(5/2)}*a^2*b^2*d^7+210*(d*x+c)^{(3/2)}*a^2*b^2*c*d^7-90*\sqrt{d*x+c}*a^2*b^2*c^2*d^7-70*(d*x+c)^{(3/2)}*a^3*b*d^8+60*\sqrt{d*x+c}*a^3*b*c*d^8-15*\sqrt{d*x+c}*a^4*d^9)/((b^5*c^3-3*a*b^4*c^2*d+3*a^2*b^3*c*d^2-a^3*b^2*d^3)*((d*x+c)*b-b*c+a*d)^5)$

maple [A] time = 0.02, size = 300, normalized size = 1.44

$$\frac{3(dx+c)^{\frac{9}{2}}b^2d^5}{128(bdx+ad)^5(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)} + \frac{7(dx+c)^{\frac{7}{2}}bd^5}{64(bdx+ad)^5(a^2d^2-2abcd+b^2c^2)} - \frac{3\sqrt{dx+c}ad^6}{128(bdx+ad)^5b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/2)/(b*x+a)^6,x)

[Out] $3/128*d^5/(b*d*x+a*d)^5*b^2/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)*(d*x+c)^{(9/2)}+7/64*d^5/(b*d*x+a*d)^5*b/(a^2*d^2-2*a*b*c*d+b^2*c^2)*(d*x+c)^{(7/2)}+1/5*d^5/(b*d*x+a*d)^5/(a*d-b*c)*(d*x+c)^{(5/2)}-7/64*d^5/(b*d*x+a*d)^5/b*(d*x+c)^{(3/2)}-3/128*d^6/(b*d*x+a*d)^5/b^2*(d*x+c)^{(1/2)}*a+3/128*d^5/(b*d*x+a*d)^5/b*(d*x+c)^{(1/2)}*c+3/128*d^5/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)/b^2/((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(3/2)/(b*x+a)^6,x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.47, size = 398, normalized size = 1.91

$$b^5 (c + dx)^5 - (c + dx)^2 \left(-10 a^3 b^2 d^3 + 30 a^2 b^3 c d^2 - 30 a b^4 c^2 d + 10 b^5 c^3 \right) - \left(5 b^5 c - 5 a b^4 d \right) (c + dx)^4 + a^5$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(3/2)/(a + b*x)^6,x)`

[Out]
$$\begin{aligned} & \left(\frac{d^5 (c + dx)^{5/2}}{5(a*d - b*c)} - \frac{7*d^5 (c + dx)^{3/2}}{64*b} + \left(\frac{3*b^2*d^5 (c + dx)^{9/2}}{128*(a*d - b*c)^3} - \frac{3*d^5 (a*d - b*c)*(c + dx)^{1/2}}{128*b^2} + \frac{7*b*d^5 (c + dx)^{7/2}}{64*(a*d - b*c)^2} \right) / (b^5 (c + dx)^5 - (c + dx)^2 (10*b^5*c^3 - 10*a^3*b^2*d^3 + 30*a^2*b^3*c*d^2 - 30*a*b^4*c^2*d) - (5*b^5*c - 5*a*b^4*d)*(c + dx)^4 + a^5*d^5 - b^5*c^5 + (c + dx)^3 (10*b^5*c^2 + 10*a^2*b^3*d^2 - 20*a*b^4*c*d) + (c + dx)*(5*b^5*c^4 + 5*a^4*b*d^4 - 20*a^3*b^2*c*d^3 + 30*a^2*b^3*c^2*d^2 - 20*a*b^4*c^3*d) - 10*a^2*b^3*c^3*d^2 + 10*a^3*b^2*c^2*d^3 + 5*a*b^4*c^4*d - 5*a^4*b*c*d^4) + \frac{3*d^5 * \operatorname{atan}\left(\frac{b^{1/2}*(c + dx)^{1/2}}{a*d - b*c}\right)}{128*b^{5/2}*(a*d - b*c)^{7/2}} \right) \end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(3/2)/(b*x+a)**6,x)`

[Out] Timed out

3.1399 $\int (a + bx)^5 (c + dx)^{5/2} dx$

Optimal. Leaf size=158

$$\frac{2b^4(c+dx)^{15/2}(bc-ad)}{3d^6} + \frac{20b^3(c+dx)^{13/2}(bc-ad)^2}{13d^6} - \frac{20b^2(c+dx)^{11/2}(bc-ad)^3}{11d^6} + \frac{10b(c+dx)^{9/2}(bc-ad)^4}{9d^6} - \frac{2(c+dx)^{7/2}(bc-ad)^5}{7d^6}$$

[Out] $-2/7*(-a*d+b*c)^5*(d*x+c)^(7/2)/d^6+10/9*b*(-a*d+b*c)^4*(d*x+c)^(9/2)/d^6-20/11*b^2*(-a*d+b*c)^3*(d*x+c)^(11/2)/d^6+20/13*b^3*(-a*d+b*c)^2*(d*x+c)^(13/2)/d^6-2/3*b^4*(-a*d+b*c)*(d*x+c)^(15/2)/d^6+2/17*b^5*(d*x+c)^(17/2)/d^6$

Rubi [A] time = 0.05, antiderivative size = 158, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{2b^4(c+dx)^{15/2}(bc-ad)}{3d^6} + \frac{20b^3(c+dx)^{13/2}(bc-ad)^2}{13d^6} - \frac{20b^2(c+dx)^{11/2}(bc-ad)^3}{11d^6} + \frac{10b(c+dx)^{9/2}(bc-ad)^4}{9d^6} - \frac{2(c+dx)^{7/2}(bc-ad)^5}{7d^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*(c + d*x)^(5/2), x]

[Out] $(-2*(b*c - a*d)^5*(c + d*x)^(7/2))/(7*d^6) + (10*b*(b*c - a*d)^4*(c + d*x)^(9/2))/(9*d^6) - (20*b^2*(b*c - a*d)^3*(c + d*x)^(11/2))/(11*d^6) + (20*b^3*(b*c - a*d)^2*(c + d*x)^(13/2))/(13*d^6) - (2*b^4*(b*c - a*d)*(c + d*x)^(15/2))/(3*d^6) + (2*b^5*(c + d*x)^(17/2))/(17*d^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^5 (c + dx)^{5/2} dx &= \int \left(\frac{(-bc + ad)^5 (c + dx)^{5/2}}{d^5} + \frac{5b(bc - ad)^4 (c + dx)^{7/2}}{d^5} - \frac{10b^2(bc - ad)^3 (c + dx)^{9/2}}{d^5} + \frac{10b^3(bc - ad)^2 (c + dx)^{11/2}}{d^5} - \frac{2b^4(bc - ad) (c + dx)^{13/2}}{d^5} + \frac{2b^5 (c + dx)^{15/2}}{d^5} \right) dx \\ &= -\frac{2(bc - ad)^5 (c + dx)^{7/2}}{7d^6} + \frac{10b(bc - ad)^4 (c + dx)^{9/2}}{9d^6} - \frac{20b^2(bc - ad)^3 (c + dx)^{11/2}}{11d^6} + \frac{20b^3(bc - ad)^2 (c + dx)^{13/2}}{13d^6} - \frac{2b^4(bc - ad) (c + dx)^{15/2}}{3d^6} + \frac{2b^5 (c + dx)^{17/2}}{17d^6} \end{aligned}$$

Mathematica [A] time = 0.11, size = 123, normalized size = 0.78

$$\frac{2(c+dx)^{7/2}(-51051b^4(c+dx)^4(bc-ad) + 117810b^3(c+dx)^3(bc-ad)^2 - 139230b^2(c+dx)^2(bc-ad)^3 + 85085b(c+dx)(bc-ad)^4 - 2b^5(bc-ad)^5)}{153153d^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*(c + d*x)^(5/2),x]

[Out] $(2*(c + d*x)^{(7/2)}*(-21879*(b*c - a*d)^5 + 85085*b*(b*c - a*d)^4*(c + d*x) - 139230*b^2*(b*c - a*d)^3*(c + d*x)^2 + 117810*b^3*(b*c - a*d)^2*(c + d*x)^3 - 51051*b^4*(b*c - a*d)*(c + d*x)^4 + 9009*b^5*(c + d*x)^5)/(153153*d^6)$

fricas [B] time = 0.44, size = 497, normalized size = 3.15

$$2(9009b^5d^8x^8 - 256b^5c^8 + 2176ab^4c^7d - 8160a^2b^3c^6d^2 + 17680a^3b^2c^5d^3 - 24310a^4bc^4d^4 + 21879a^5c^3d^5 + 3003(7b^5c^4d^7 + 17a^2b^4c^3d^8)*x^7 + 231(55b^5c^2d^6 + 527a^2b^4c^2d^7 + 510a^2b^3c^3d^8)*x^6 + 63(b^5c^3d^5 + 1207a^2b^4c^2d^6 + 4590a^2b^3c^2d^7 + 2210a^3b^2c^2d^8)*x^5 - 35(2b^5c^4d^4 - 17a^2b^4c^3d^5 - 5406a^2b^3c^2d^6 - 10166a^3b^2c^2d^7 - 2431a^4b^2c^2d^8)*x^4 + (80b^5c^5d^3 - 680a^2b^4c^4d^4 + 2550a^2b^3c^3d^5 + 249730a^3b^2c^2d^6 + 230945a^4b^2c^2d^7 + 21879a^5d^8)*x^3 - 3(32b^5c^6d^2 - 272a^2b^4c^5d^3 + 1020a^2b^3c^4d^4 - 2210a^3b^2c^3d^5 - 60775a^4b^2c^2d^6 - 21879a^5c^2d^7)*x^2 + (128b^5c^7d - 1088a^2b^4c^6d^2 + 4080a^2b^3c^5d^3 - 8840a^3b^2c^4d^4 + 12155a^4b^2c^3d^5 + 65637a^5c^2d^6)*x)*sqrt(d*x + c)/d^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^(5/2),x, algorithm="fricas")

[Out] $2/153153*(9009*b^5*d^8*x^8 - 256*b^5*c^8 + 2176*a*b^4*c^7*d - 8160*a^2*b^3*c^6*d^2 + 17680*a^3*b^2*c^5*d^3 - 24310*a^4*b*c^4*d^4 + 21879*a^5*c^3*d^5 + 3003*(7*b^5*c^4*d^7 + 17*a^2*b^4*c^3*d^8)*x^7 + 231*(55*b^5*c^2*d^6 + 527*a^2*b^4*c^2*d^7 + 510*a^2*b^3*c^3*d^8)*x^6 + 63*(b^5*c^3*d^5 + 1207*a^2*b^4*c^2*d^6 + 4590*a^2*b^3*c^2*d^7 + 2210*a^3*b^2*c^2*d^8)*x^5 - 35*(2*b^5*c^4*d^4 - 17*a^2*b^4*c^3*d^5 - 5406*a^2*b^3*c^2*d^6 - 10166*a^3*b^2*c^2*d^7 - 2431*a^4*b^2*c^2*d^8)*x^4 + (80*b^5*c^5*d^3 - 680*a^2*b^4*c^4*d^4 + 2550*a^2*b^3*c^3*d^5 + 249730*a^3*b^2*c^2*d^6 + 230945*a^4*b^2*c^2*d^7 + 21879*a^5*d^8)*x^3 - 3*(32*b^5*c^6*d^2 - 272*a^2*b^4*c^5*d^3 + 1020*a^2*b^3*c^4*d^4 - 2210*a^3*b^2*c^3*d^5 - 60775*a^4*b^2*c^2*d^6 - 21879*a^5*c^2*d^7)*x^2 + (128*b^5*c^7*d - 1088*a^2*b^4*c^6*d^2 + 4080*a^2*b^3*c^5*d^3 - 8840*a^3*b^2*c^4*d^4 + 12155*a^4*b^2*c^3*d^5 + 65637*a^5*c^2*d^6)*x)*sqrt(d*x + c)/d^6$

giac [B] time = 1.52, size = 1599, normalized size = 10.12

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(d*x+c)^(5/2),x, algorithm="giac")

[Out] $2/765765*(765765*sqrt(d*x + c)*a^5*c^3 + 765765*((d*x + c)^{(3/2)} - 3*sqrt(d*x + c))*c)*a^5*c^2 + 1276275*((d*x + c)^{(3/2)} - 3*sqrt(d*x + c))*c)*a^4*b*c^3/d + 153153*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c))*c^2)*a^5*c + 510510*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c))*c^2)*a^3*b^2*c^3/d^2 + 765765*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c))*c^2)*a^4*b*c^2/d + 21879*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c))*c^3)*a^5 + 218790*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c))*c^3)*a^5$

```

t(d*x + c)*c^3)*a^2*b^3*c^3/d^3 + 656370*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(
(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*a^3*b^2*c^2/d^2 +
328185*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 -
35*sqrt(d*x + c)*c^3)*a^4*b*c/d + 12155*(35*(d*x + c)^(9/2) - 180*(d*x + c)^(
7/2)*c + 378*(d*x + c)^(5/2)*c^2 - 420*(d*x + c)^(3/2)*c^3 + 315*sqrt(d*x
+ c)*c^4)*a*b^4*c^3/d^4 + 72930*(35*(d*x + c)^(9/2) - 180*(d*x + c)^(7/2)
*c + 378*(d*x + c)^(5/2)*c^2 - 420*(d*x + c)^(3/2)*c^3 + 315*sqrt(d*x + c)*
c^4)*a^2*b^3*c^2/d^3 + 72930*(35*(d*x + c)^(9/2) - 180*(d*x + c)^(7/2)*c +
378*(d*x + c)^(5/2)*c^2 - 420*(d*x + c)^(3/2)*c^3 + 315*sqrt(d*x + c)*c^4)*
a^3*b^2*c/d^2 + 12155*(35*(d*x + c)^(9/2) - 180*(d*x + c)^(7/2)*c + 378*(d*
x + c)^(5/2)*c^2 - 420*(d*x + c)^(3/2)*c^3 + 315*sqrt(d*x + c)*c^4)*a^4*b/d
+ 1105*(63*(d*x + c)^(11/2) - 385*(d*x + c)^(9/2)*c + 990*(d*x + c)^(7/2)*
c^2 - 1386*(d*x + c)^(5/2)*c^3 + 1155*(d*x + c)^(3/2)*c^4 - 693*sqrt(d*x +
c)*c^5)*b^5*c^3/d^5 + 16575*(63*(d*x + c)^(11/2) - 385*(d*x + c)^(9/2)*c +
990*(d*x + c)^(7/2)*c^2 - 1386*(d*x + c)^(5/2)*c^3 + 1155*(d*x + c)^(3/2)*c
^4 - 693*sqrt(d*x + c)*c^5)*a*b^4*c^2/d^4 + 33150*(63*(d*x + c)^(11/2) - 38
5*(d*x + c)^(9/2)*c + 990*(d*x + c)^(7/2)*c^2 - 1386*(d*x + c)^(5/2)*c^3 +
1155*(d*x + c)^(3/2)*c^4 - 693*sqrt(d*x + c)*c^5)*a^2*b^3*c/d^3 + 11050*(63
*(d*x + c)^(11/2) - 385*(d*x + c)^(9/2)*c + 990*(d*x + c)^(7/2)*c^2 - 1386*
(d*x + c)^(5/2)*c^3 + 1155*(d*x + c)^(3/2)*c^4 - 693*sqrt(d*x + c)*c^5)*a^3
*b^2/d^2 + 765*(231*(d*x + c)^(13/2) - 1638*(d*x + c)^(11/2)*c + 5005*(d*x
+ c)^(9/2)*c^2 - 8580*(d*x + c)^(7/2)*c^3 + 9009*(d*x + c)^(5/2)*c^4 - 6006
*(d*x + c)^(3/2)*c^5 + 3003*sqrt(d*x + c)*c^6)*b^5*c^2/d^5 + 3825*(231*(d*x
+ c)^(13/2) - 1638*(d*x + c)^(11/2)*c + 5005*(d*x + c)^(9/2)*c^2 - 8580*(d
*x + c)^(7/2)*c^3 + 9009*(d*x + c)^(5/2)*c^4 - 6006*(d*x + c)^(3/2)*c^5 + 3
003*sqrt(d*x + c)*c^6)*a*b^4*c/d^4 + 2550*(231*(d*x + c)^(13/2) - 1638*(d*x
+ c)^(11/2)*c + 5005*(d*x + c)^(9/2)*c^2 - 8580*(d*x + c)^(7/2)*c^3 + 9009
*(d*x + c)^(5/2)*c^4 - 6006*(d*x + c)^(3/2)*c^5 + 3003*sqrt(d*x + c)*c^6)*a
^2*b^3/d^3 + 357*(429*(d*x + c)^(15/2) - 3465*(d*x + c)^(13/2)*c + 12285*(d
*x + c)^(11/2)*c^2 - 25025*(d*x + c)^(9/2)*c^3 + 32175*(d*x + c)^(7/2)*c^4
- 27027*(d*x + c)^(5/2)*c^5 + 15015*(d*x + c)^(3/2)*c^6 - 6435*sqrt(d*x + c
)*c^7)*b^5*c/d^5 + 595*(429*(d*x + c)^(15/2) - 3465*(d*x + c)^(13/2)*c + 12
285*(d*x + c)^(11/2)*c^2 - 25025*(d*x + c)^(9/2)*c^3 + 32175*(d*x + c)^(7/2
)*c^4 - 27027*(d*x + c)^(5/2)*c^5 + 15015*(d*x + c)^(3/2)*c^6 - 6435*sqrt(d
*x + c)*c^7)*a*b^4/d^4 + 7*(6435*(d*x + c)^(17/2) - 58344*(d*x + c)^(15/2)*
c + 235620*(d*x + c)^(13/2)*c^2 - 556920*(d*x + c)^(11/2)*c^3 + 850850*(d*x
+ c)^(9/2)*c^4 - 875160*(d*x + c)^(7/2)*c^5 + 612612*(d*x + c)^(5/2)*c^6 -
291720*(d*x + c)^(3/2)*c^7 + 109395*sqrt(d*x + c)*c^8)*b^5/d^5)/d

```

maple [B] time = 0.00, size = 273, normalized size = 1.73

$$2(dx+c)^{\frac{7}{2}}(9009b^5x^5d^5 + 51051ab^4d^5x^4 - 6006b^5cd^4x^4 + 117810a^2b^3d^5x^3 - 31416ab^4cd^4x^3 + 3696b^5c^2d^3x^3 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^5*(d*x+c)^(5/2),x)`

[Out] $2/153153*(d*x+c)^{(7/2)}*(9009*b^5*d^5*x^5+51051*a*b^4*d^5*x^4-6006*b^5*c*d^4*x^4+117810*a^2*b^3*d^5*x^3-31416*a*b^4*c*d^4*x^3+3696*b^5*c^2*d^3*x^3+139230*a^3*b^2*d^5*x^2-64260*a^2*b^3*c*d^4*x^2+17136*a*b^4*c^2*d^3*x^2-2016*b^5*c^3*d^2*x^2+85085*a^4*b*d^5*x-61880*a^3*b^2*c*d^4*x+28560*a^2*b^3*c^2*d^3*x-7616*a*b^4*c^3*d^2*x+896*b^5*c^4*d*x+21879*a^5*d^5-24310*a^4*b*c*d^4+17680*a^3*b^2*c^2*d^3-8160*a^2*b^3*c^3*d^2+2176*a*b^4*c^4*d-256*b^5*c^5)/d^6$

maxima [A] time = 1.36, size = 259, normalized size = 1.64

$$2 \left(9009 (dx + c)^{\frac{17}{2}} b^5 - 51051 (b^5 c - ab^4 d) (dx + c)^{\frac{15}{2}} + 117810 (b^5 c^2 - 2 ab^4 cd + a^2 b^3 d^2) (dx + c)^{\frac{13}{2}} - 139230 (b^5 c^3 - 3 a^2 b^4 c^2 d + 3 a^3 b^3 c d^2 - a^4 b^2 d^3) (dx + c)^{\frac{11}{2}} + 85085 (b^5 c^4 - 4 a^2 b^4 c^3 d + 6 a^3 b^3 c^2 d^2 - 4 a^4 b^2 c d^3 + a^5 d^5) (dx + c)^{\frac{9}{2}} - 21879 (b^5 c^5 - 5 a^2 b^4 c^4 d + 10 a^3 b^3 c^3 d^2 - 10 a^4 b^2 c^2 d^3 + 5 a^5 b c d^4 - a^6 d^5) (dx + c)^{\frac{7}{2}} \right) / d^6$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5*(d*x+c)^(5/2),x, algorithm="maxima")`

[Out] $2/153153*(9009*(d*x + c)^{(17/2)}*b^5 - 51051*(b^5*c - a*b^4*d)*(d*x + c)^{(15/2)} + 117810*(b^5*c^2 - 2*a*b^4*c*d + a^2*b^3*d^2)*(d*x + c)^{(13/2)} - 139230*(b^5*c^3 - 3*a*b^4*c^2*d + 3*a^2*b^3*c*d^2 - a^3*b^2*d^3)*(d*x + c)^{(11/2)} + 85085*(b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)*(d*x + c)^{(9/2)} - 21879*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)*(d*x + c)^{(7/2)})/d^6$

mupad [B] time = 0.27, size = 137, normalized size = 0.87

$$\frac{2b^5(c+dx)^{17/2}}{17d^6} - \frac{(10b^5c - 10ab^4d)(c+dx)^{15/2}}{15d^6} + \frac{2(ad-bc)^5(c+dx)^{7/2}}{7d^6} + \frac{20b^2(ad-bc)^3(c+dx)^{11/2}}{11d^6} + \frac{20b^5(ad-bc)(c+dx)^{9/2}}{9d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5*(c + d*x)^(5/2),x)`

[Out] $(2*b^5*(c + d*x)^{(17/2)})/(17*d^6) - ((10*b^5*c - 10*a*b^4*d)*(c + d*x)^{(15/2)})/(15*d^6) + (2*(a*d - b*c)^5*(c + d*x)^{(7/2)})/(7*d^6) + (20*b^2*(a*d - b*c)^3*(c + d*x)^{(11/2)})/(11*d^6) + (20*b^3*(a*d - b*c)^2*(c + d*x)^{(13/2)})/(13*d^6) + (10*b*(a*d - b*c)^4*(c + d*x)^{(9/2)})/(9*d^6)$

sympy [A] time = 43.08, size = 1292, normalized size = 8.18

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5*(d*x+c)**(5/2),x)`

```
[Out] a**5*c**2*Piecewise((sqrt(c)*x, Eq(d, 0)), (2*(c + d*x)**(3/2)/(3*d), True)
) + 4*a**5*c*(-c*(c + d*x)**(3/2)/3 + (c + d*x)**(5/2)/5)/d + 2*a**5*(c**2*
(c + d*x)**(3/2)/3 - 2*c*(c + d*x)**(5/2)/5 + (c + d*x)**(7/2)/7)/d + 10*a*
*4*b*c**2*(-c*(c + d*x)**(3/2)/3 + (c + d*x)**(5/2)/5)/d**2 + 20*a**4*b*c*(
c**2*(c + d*x)**(3/2)/3 - 2*c*(c + d*x)**(5/2)/5 + (c + d*x)**(7/2)/7)/d**2
+ 10*a**4*b*(-c**3*(c + d*x)**(3/2)/3 + 3*c**2*(c + d*x)**(5/2)/5 - 3*c*(c
+ d*x)**(7/2)/7 + (c + d*x)**(9/2)/9)/d**2 + 20*a**3*b**2*c**2*(c**2*(c +
d*x)**(3/2)/3 - 2*c*(c + d*x)**(5/2)/5 + (c + d*x)**(7/2)/7)/d**3 + 40*a**3
*b**2*c*(-c**3*(c + d*x)**(3/2)/3 + 3*c**2*(c + d*x)**(5/2)/5 - 3*c*(c + d*
x)**(7/2)/7 + (c + d*x)**(9/2)/9)/d**3 + 20*a**3*b**2*(c**4*(c + d*x)**(3/2
)/3 - 4*c**3*(c + d*x)**(5/2)/5 + 6*c**2*(c + d*x)**(7/2)/7 - 4*c*(c + d*x)
**9/2)/9 + (c + d*x)**(11/2)/11)/d**3 + 20*a**2*b**3*c**2*(-c**3*(c + d*x)
**3/2)/3 + 3*c**2*(c + d*x)**(5/2)/5 - 3*c*(c + d*x)**(7/2)/7 + (c + d*x)*
*(9/2)/9)/d**4 + 40*a**2*b**3*c*(c**4*(c + d*x)**(3/2)/3 - 4*c**3*(c + d*x)
**5/2)/5 + 6*c**2*(c + d*x)**(7/2)/7 - 4*c*(c + d*x)**(9/2)/9 + (c + d*x)*
*(11/2)/11)/d**4 + 20*a**2*b**3*(-c**5*(c + d*x)**(3/2)/3 + c**4*(c + d*x)*
*(5/2) - 10*c**3*(c + d*x)**(7/2)/7 + 10*c**2*(c + d*x)**(9/2)/9 - 5*c*(c +
d*x)**(11/2)/11 + (c + d*x)**(13/2)/13)/d**4 + 10*a*b**4*c**2*(c**4*(c + d
*x)**(3/2)/3 - 4*c**3*(c + d*x)**(5/2)/5 + 6*c**2*(c + d*x)**(7/2)/7 - 4*c*
(c + d*x)**(9/2)/9 + (c + d*x)**(11/2)/11)/d**5 + 20*a*b**4*c*(-c**5*(c + d
*x)**(3/2)/3 + c**4*(c + d*x)**(5/2) - 10*c**3*(c + d*x)**(7/2)/7 + 10*c**2
*(c + d*x)**(9/2)/9 - 5*c*(c + d*x)**(11/2)/11 + (c + d*x)**(13/2)/13)/d**5
+ 10*a*b**4*(c**6*(c + d*x)**(3/2)/3 - 6*c**5*(c + d*x)**(5/2)/5 + 15*c**4
*(c + d*x)**(7/2)/7 - 20*c**3*(c + d*x)**(9/2)/9 + 15*c**2*(c + d*x)**(11/2
)/11 - 6*c*(c + d*x)**(13/2)/13 + (c + d*x)**(15/2)/15)/d**5 + 2*b**5*c**2*
(-c**5*(c + d*x)**(3/2)/3 + c**4*(c + d*x)**(5/2) - 10*c**3*(c + d*x)**(7/2
)/7 + 10*c**2*(c + d*x)**(9/2)/9 - 5*c*(c + d*x)**(11/2)/11 + (c + d*x)**(1
3/2)/13)/d**6 + 4*b**5*c*(c**6*(c + d*x)**(3/2)/3 - 6*c**5*(c + d*x)**(5/2)
/5 + 15*c**4*(c + d*x)**(7/2)/7 - 20*c**3*(c + d*x)**(9/2)/9 + 15*c**2*(c +
d*x)**(11/2)/11 - 6*c*(c + d*x)**(13/2)/13 + (c + d*x)**(15/2)/15)/d**6 +
2*b**5*(-c**7*(c + d*x)**(3/2)/3 + 7*c**6*(c + d*x)**(5/2)/5 - 3*c**5*(c +
d*x)**(7/2) + 35*c**4*(c + d*x)**(9/2)/9 - 35*c**3*(c + d*x)**(11/2)/11 + 2
1*c**2*(c + d*x)**(13/2)/13 - 7*c*(c + d*x)**(15/2)/15 + (c + d*x)**(17/2)/
17)/d**6
```

3.1400 $\int (a + bx)^4 (c + dx)^{5/2} dx$

Optimal. Leaf size=129

$$-\frac{8b^3(c+dx)^{13/2}(bc-ad)}{13d^5} + \frac{12b^2(c+dx)^{11/2}(bc-ad)^2}{11d^5} - \frac{8b(c+dx)^{9/2}(bc-ad)^3}{9d^5} + \frac{2(c+dx)^{7/2}(bc-ad)^4}{7d^5} + \frac{2b^4(c+dx)^{5/2}}{15d^5}$$

[Out] $2/7*(-a*d+b*c)^4*(d*x+c)^(7/2)/d^5-8/9*b*(-a*d+b*c)^3*(d*x+c)^(9/2)/d^5+12/11*b^2*(-a*d+b*c)^2*(d*x+c)^(11/2)/d^5-8/13*b^3*(-a*d+b*c)*(d*x+c)^(13/2)/d^5+2/15*b^4*(d*x+c)^(15/2)/d^5$

Rubi [A] time = 0.04, antiderivative size = 129, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{8b^3(c+dx)^{13/2}(bc-ad)}{13d^5} + \frac{12b^2(c+dx)^{11/2}(bc-ad)^2}{11d^5} - \frac{8b(c+dx)^{9/2}(bc-ad)^3}{9d^5} + \frac{2(c+dx)^{7/2}(bc-ad)^4}{7d^5} + \frac{2b^4(c+dx)^{5/2}}{15d^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4*(c + d*x)^(5/2), x]

[Out] $(2*(b*c - a*d)^4*(c + d*x)^(7/2))/(7*d^5) - (8*b*(b*c - a*d)^3*(c + d*x)^(9/2))/(9*d^5) + (12*b^2*(b*c - a*d)^2*(c + d*x)^(11/2))/(11*d^5) - (8*b^3*(b*c - a*d)*(c + d*x)^(13/2))/(13*d^5) + (2*b^4*(c + d*x)^(15/2))/(15*d^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^4 (c + dx)^{5/2} dx &= \int \left(\frac{(-bc + ad)^4 (c + dx)^{5/2}}{d^4} - \frac{4b(bc - ad)^3 (c + dx)^{7/2}}{d^4} + \frac{6b^2(bc - ad)^2 (c + dx)^{9/2}}{d^4} - \frac{4b^3(bc - ad) (c + dx)^{11/2}}{d^4} + \frac{2b^4 (c + dx)^{13/2}}{d^4} \right) dx \\ &= \frac{2(bc - ad)^4 (c + dx)^{7/2}}{7d^5} - \frac{8b(bc - ad)^3 (c + dx)^{9/2}}{9d^5} + \frac{12b^2(bc - ad)^2 (c + dx)^{11/2}}{11d^5} - \frac{8b^3(bc - ad) (c + dx)^{13/2}}{13d^5} + \frac{2b^4 (c + dx)^{15/2}}{15d^5} \end{aligned}$$

Mathematica [A] time = 0.11, size = 101, normalized size = 0.78

$$\frac{2(c+dx)^{7/2}(-13860b^3(c+dx)^3(bc-ad) + 24570b^2(c+dx)^2(bc-ad)^2 - 20020b(c+dx)(bc-ad)^3 + 6435(bc-ad)^4)}{45045d^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4*(c + d*x)^(5/2),x]

[Out] (2*(c + d*x)^(7/2)*(6435*(b*c - a*d)^4 - 20020*b*(b*c - a*d)^3*(c + d*x) + 24570*b^2*(b*c - a*d)^2*(c + d*x)^2 - 13860*b^3*(b*c - a*d)*(c + d*x)^3 + 3003*b^4*(c + d*x)^4)/(45045*d^5)

fricas [B] time = 0.45, size = 377, normalized size = 2.92

$$2 \left(3003 b^4 d^7 x^7 + 128 b^4 c^7 - 960 a b^3 c^6 d + 3120 a^2 b^2 c^5 d^2 - 5720 a^3 b c^4 d^3 + 6435 a^4 c^3 d^4 + 231 (31 b^4 c d^6 + 60 a b^3 d^7) \right) / (45045 d^5)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^(5/2),x, algorithm="fricas")

[Out] 2/45045*(3003*b^4*d^7*x^7 + 128*b^4*c^7 - 960*a*b^3*c^6*d + 3120*a^2*b^2*c^5*d^2 - 5720*a^3*b*c^4*d^3 + 6435*a^4*c^3*d^4 + 231*(31*b^4*c*d^6 + 60*a*b^3*d^7))*x^6 + 63*(71*b^4*c^2*d^5 + 540*a*b^3*c*d^6 + 390*a^2*b^2*d^7)*x^5 + 35*(b^4*c^3*d^4 + 636*a*b^3*c^2*d^5 + 1794*a^2*b^2*c*d^6 + 572*a^3*b*d^7)*x^4 - 5*(8*b^4*c^4*d^3 - 60*a*b^3*c^3*d^4 - 8814*a^2*b^2*c^2*d^5 - 10868*a^3*b*c*d^6 - 1287*a^4*d^7)*x^3 + 3*(16*b^4*c^5*d^2 - 120*a*b^3*c^4*d^3 + 390*a^2*b^2*c^3*d^4 + 14300*a^3*b*c^2*d^5 + 6435*a^4*c*d^6)*x^2 - (64*b^4*c^6*d - 480*a*b^3*c^5*d^2 + 1560*a^2*b^2*c^4*d^3 - 2860*a^3*b*c^3*d^4 - 19305*a^4*c^2*d^5)*x)*sqrt(d*x + c)/d^5

giac [B] time = 1.45, size = 1204, normalized size = 9.33

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^(5/2),x, algorithm="giac")

[Out] 2/45045*(45045*sqrt(d*x + c)*a^4*c^3 + 45045*((d*x + c)^(3/2) - 3*sqrt(d*x + c))*c)*a^4*c^2 + 60060*((d*x + c)^(3/2) - 3*sqrt(d*x + c))*c)*a^3*b*c^3/d + 9009*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a^4*c + 18018*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a^2*b^2*c^3/d^2 + 36036*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a^3*b*c^2/d + 1287*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2))*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*a^4 + 5148*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2))*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*a^3*b*c^3/d^3 + 23166*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2))*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*a^2*b^2*c^2/d^2 + 15444*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2))*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*a^3*b*c/d + 143*(35*(d*x + c)^(9/2) - 180*(d*x + c)^(7/2))*c + 378*(d

$$\begin{aligned} & *x + c)^{(5/2)} *c^2 - 420*(d*x + c)^{(3/2)} *c^3 + 315*\text{sqrt}(d*x + c)*c^4)*b^4*c^3/d^4 + 1716*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)} *c + 378*(d*x + c)^{(5/2)} *c^2 - 420*(d*x + c)^{(3/2)} *c^3 + 315*\text{sqrt}(d*x + c)*c^4)*a*b^3*c^2/d^3 + \\ & 2574*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)} *c + 378*(d*x + c)^{(5/2)} *c^2 - 420*(d*x + c)^{(3/2)} *c^3 + 315*\text{sqrt}(d*x + c)*c^4)*a^2*b^2*c/d^2 + 572*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)} *c + 378*(d*x + c)^{(5/2)} *c^2 - 420*(d*x + c)^{(3/2)} *c^3 + 315*\text{sqrt}(d*x + c)*c^4)*a^3*b/d + 195*(63*(d*x + c)^{(11/2)} - 385*(d*x + c)^{(9/2)} *c + 990*(d*x + c)^{(7/2)} *c^2 - 1386*(d*x + c)^{(5/2)} *c^3 + 1155*(d*x + c)^{(3/2)} *c^4 - 693*\text{sqrt}(d*x + c)*c^5)*b^4*c^2/d^4 + 780*(63*(d*x + c)^{(11/2)} - 385*(d*x + c)^{(9/2)} *c + 990*(d*x + c)^{(7/2)} *c^2 - 1386*(d*x + c)^{(5/2)} *c^3 + 1155*(d*x + c)^{(3/2)} *c^4 - 693*\text{sqrt}(d*x + c)*c^5)*a*b^3*c/d^3 + 390*(63*(d*x + c)^{(11/2)} - 385*(d*x + c)^{(9/2)} *c + 990*(d*x + c)^{(7/2)} *c^2 - 1386*(d*x + c)^{(5/2)} *c^3 + 1155*(d*x + c)^{(3/2)} *c^4 - 693*\text{sqrt}(d*x + c)*c^5)*a^2*b^2/d^2 + 45*(231*(d*x + c)^{(13/2)} - 1638*(d*x + c)^{(11/2)} *c + 5005*(d*x + c)^{(9/2)} *c^2 - 8580*(d*x + c)^{(7/2)} *c^3 + 9009*(d*x + c)^{(5/2)} *c^4 - 6006*(d*x + c)^{(3/2)} *c^5 + 3003*\text{sqrt}(d*x + c)*c^6)*b^4*c/d^4 + 60*(231*(d*x + c)^{(13/2)} - 1638*(d*x + c)^{(11/2)} *c + 5005*(d*x + c)^{(9/2)} *c^2 - 8580*(d*x + c)^{(7/2)} *c^3 + 9009*(d*x + c)^{(5/2)} *c^4 - 6006*(d*x + c)^{(3/2)} *c^5 + 3003*\text{sqrt}(d*x + c)*c^6)*a*b^3/d^3 + 7*(429*(d*x + c)^{(15/2)} - 3465*(d*x + c)^{(13/2)} *c + 12285*(d*x + c)^{(11/2)} *c^2 - 25025*(d*x + c)^{(9/2)} *c^3 + 32175*(d*x + c)^{(7/2)} *c^4 - 27027*(d*x + c)^{(5/2)} *c^5 + 15015*(d*x + c)^{(3/2)} *c^6 - 6435*\text{sqrt}(d*x + c)*c^7)*b^4/d^4)/d \end{aligned}$$

maple [A] time = 0.01, size = 186, normalized size = 1.44

$$2(dx + c)^{\frac{7}{2}} \left(3003b^4x^4d^4 + 13860ab^3d^4x^3 - 1848b^4cd^3x^3 + 24570a^2b^2d^4x^2 - 7560ab^3cd^3x^2 + 1008b^4c^2d^2x^2 + \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4*(d*x+c)^(5/2), x)

[Out] $\frac{2}{45045}*(d*x+c)^{(7/2)}*(3003*b^4*d^4*x^4+13860*a*b^3*d^4*x^3-1848*b^4*c*d^3*x^3+24570*a^2*b^2*d^4*x^2-7560*a*b^3*c*d^3*x^2+1008*b^4*c^2*d^2*x^2+20020*a^3*b*d^4*x-10920*a^2*b^2*c*d^3*x+3360*a*b^3*c^2*d^2*x-448*b^4*c^3*d*x+6435*a^4*d^4-5720*a^3*b*c*d^3+3120*a^2*b^2*c^2*d^2-960*a*b^3*c^3*d+128*b^4*c^4)/d^5$

maxima [A] time = 1.33, size = 181, normalized size = 1.40

$$2 \left(3003(dx + c)^{\frac{15}{2}} b^4 - 13860(b^4c - ab^3d)(dx + c)^{\frac{13}{2}} + 24570(b^4c^2 - 2ab^3cd + a^2b^2d^2)(dx + c)^{\frac{11}{2}} - 20020(b^4c^3 - \dots \right)$$

45045

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4*(d*x+c)^(5/2),x, algorithm="maxima")

[Out] $\frac{2}{45045} \cdot (3003 \cdot (d \cdot x + c)^{(15/2)} \cdot b^4 - 13860 \cdot (b^4 \cdot c - a \cdot b^3 \cdot d) \cdot (d \cdot x + c)^{(13/2)} + 24570 \cdot (b^4 \cdot c^2 - 2 \cdot a \cdot b^3 \cdot c \cdot d + a^2 \cdot b^2 \cdot d^2) \cdot (d \cdot x + c)^{(11/2)} - 20020 \cdot (b^4 \cdot c^3 - 3 \cdot a \cdot b^3 \cdot c^2 \cdot d + 3 \cdot a^2 \cdot b^2 \cdot c \cdot d^2 - a^3 \cdot b \cdot d^3) \cdot (d \cdot x + c)^{(9/2)} + 6435 \cdot (b^4 \cdot c^4 - 4 \cdot a \cdot b^3 \cdot c^3 \cdot d + 6 \cdot a^2 \cdot b^2 \cdot c^2 \cdot d^2 - 4 \cdot a^3 \cdot b \cdot c \cdot d^3 + a^4 \cdot d^4) \cdot (d \cdot x + c)^{(7/2)}) / d^5$

mupad [B] time = 0.23, size = 112, normalized size = 0.87

$$\frac{2b^4(c+dx)^{15/2}}{15d^5} - \frac{(8b^4c - 8ab^3d)(c+dx)^{13/2}}{13d^5} + \frac{2(ad-bc)^4(c+dx)^{7/2}}{7d^5} + \frac{12b^2(ad-bc)^2(c+dx)^{11/2}}{11d^5} + \frac{8b(ad-bc)(c+dx)^{5/2}}{5d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^4*(c + d*x)^(5/2),x)

[Out] $(2 \cdot b^4 \cdot (c + d \cdot x)^{(15/2)}) / (15 \cdot d^5) - ((8 \cdot b^4 \cdot c - 8 \cdot a \cdot b^3 \cdot d) \cdot (c + d \cdot x)^{(13/2)}) / (13 \cdot d^5) + (2 \cdot (a \cdot d - b \cdot c)^4 \cdot (c + d \cdot x)^{(7/2)}) / (7 \cdot d^5) + (12 \cdot b^2 \cdot (a \cdot d - b \cdot c)^2 \cdot (c + d \cdot x)^{(11/2)}) / (11 \cdot d^5) + (8 \cdot b \cdot (a \cdot d - b \cdot c) \cdot (c + d \cdot x)^{(9/2)}) / (9 \cdot d^5)$

sympy [A] time = 33.64, size = 960, normalized size = 7.44

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4*(d*x+c)**(5/2),x)

[Out] $a^{**4} \cdot c^{**2} \cdot \text{Piecewise}(\text{sqrt}(c) \cdot x, \text{Eq}(d, 0)), (2 \cdot (c + d \cdot x)^{(3/2)} / (3 \cdot d), \text{True}) + 4 \cdot a^{**4} \cdot c \cdot (-c \cdot (c + d \cdot x)^{(3/2)} / 3 + (c + d \cdot x)^{(5/2)} / 5) / d + 2 \cdot a^{**4} \cdot (c^{**2} \cdot (c + d \cdot x)^{(3/2)} / 3 - 2 \cdot c \cdot (c + d \cdot x)^{(5/2)} / 5 + (c + d \cdot x)^{(7/2)} / 7) / d + 8 \cdot a^{**3} \cdot b \cdot c^{**2} \cdot (-c \cdot (c + d \cdot x)^{(3/2)} / 3 + (c + d \cdot x)^{(5/2)} / 5) / d^{**2} + 16 \cdot a^{**3} \cdot b \cdot c \cdot (c^{**2} \cdot (c + d \cdot x)^{(3/2)} / 3 - 2 \cdot c \cdot (c + d \cdot x)^{(5/2)} / 5 + (c + d \cdot x)^{(7/2)} / 7) / d^{**2} + 8 \cdot a^{**3} \cdot b \cdot (-c^{**3} \cdot (c + d \cdot x)^{(3/2)} / 3 + 3 \cdot c^{**2} \cdot (c + d \cdot x)^{(5/2)} / 5 - 3 \cdot c \cdot (c + d \cdot x)^{(7/2)} / 7 + (c + d \cdot x)^{(9/2)} / 9) / d^{**2} + 12 \cdot a^{**2} \cdot b^{**2} \cdot c^{**2} \cdot (c^{**2} \cdot (c + d \cdot x)^{(3/2)} / 3 - 2 \cdot c \cdot (c + d \cdot x)^{(5/2)} / 5 + (c + d \cdot x)^{(7/2)} / 7) / d^{**3} + 24 \cdot a^{**2} \cdot b^{**2} \cdot c \cdot (-c^{**3} \cdot (c + d \cdot x)^{(3/2)} / 3 + 3 \cdot c^{**2} \cdot (c + d \cdot x)^{(5/2)} / 5 - 3 \cdot c \cdot (c + d \cdot x)^{(7/2)} / 7 + (c + d \cdot x)^{(9/2)} / 9) / d^{**3} + 12 \cdot a^{**2} \cdot b^{**2} \cdot (c^{**4} \cdot (c + d \cdot x)^{(3/2)} / 3 - 4 \cdot c^{**3} \cdot (c + d \cdot x)^{(5/2)} / 5 + 6 \cdot c^{**2} \cdot (c + d \cdot x)^{(7/2)} / 7 - 4 \cdot c \cdot (c + d \cdot x)^{(9/2)} / 9 + (c + d \cdot x)^{(11/2)} / 11) / d^{**3} + 8 \cdot a \cdot b^{**3} \cdot c^{**2} \cdot (-c^{**3} \cdot (c + d \cdot x)^{(3/2)} / 3 + 3 \cdot c^{**2} \cdot (c + d \cdot x)^{(5/2)} / 5 - 3 \cdot c \cdot (c + d \cdot x)^{(7/2)} / 7 + (c + d \cdot x)^{(9/2)} / 9) / d^{**4} + 16 \cdot a \cdot b^{**3} \cdot c \cdot (c^{**4} \cdot (c + d \cdot x)^{(3/2)} / 3 - 4 \cdot c^{**3} \cdot (c + d \cdot x)^{(5/2)} / 5 + 6 \cdot c^{**2} \cdot (c + d \cdot x)^{(7/2)} / 7 - 4 \cdot c \cdot (c + d \cdot x)^{(9/2)} / 9 + (c + d \cdot x)^{(11/2)} / 11) / d^{**4} + 8 \cdot a \cdot b^{**3} \cdot (-c^{**5} \cdot (c + d \cdot x)^{(3/2)} / 3 + c^{**4} \cdot (c + d \cdot x)^{(5/2)} - 10 \cdot c^{**3} \cdot (c + d \cdot x)^{(7/2)} / 7 + 10 \cdot c^{**2} \cdot (c + d \cdot x)^{(9/2)} / 9 - 5 \cdot c \cdot (c + d \cdot x)^{(11/2)}) / d^{**4}$

$$\begin{aligned}
& /11 + (c + d*x)**(13/2)/13)/d**4 + 2*b**4*c**2*(c**4*(c + d*x)**(3/2)/3 - 4 \\
& *c**3*(c + d*x)**(5/2)/5 + 6*c**2*(c + d*x)**(7/2)/7 - 4*c*(c + d*x)**(9/2) \\
& /9 + (c + d*x)**(11/2)/11)/d**5 + 4*b**4*c*(-c**5*(c + d*x)**(3/2)/3 + c**4 \\
& *(c + d*x)**(5/2) - 10*c**3*(c + d*x)**(7/2)/7 + 10*c**2*(c + d*x)**(9/2)/9 \\
& - 5*c*(c + d*x)**(11/2)/11 + (c + d*x)**(13/2)/13)/d**5 + 2*b**4*(c**6*(c \\
& + d*x)**(3/2)/3 - 6*c**5*(c + d*x)**(5/2)/5 + 15*c**4*(c + d*x)**(7/2)/7 - \\
& 20*c**3*(c + d*x)**(9/2)/9 + 15*c**2*(c + d*x)**(11/2)/11 - 6*c*(c + d*x)** \\
& (13/2)/13 + (c + d*x)**(15/2)/15)/d**5
\end{aligned}$$

3.1401 $\int (a + bx)^3 (c + dx)^{5/2} dx$

Optimal. Leaf size=100

$$-\frac{6b^2(c+dx)^{11/2}(bc-ad)}{11d^4} + \frac{2b(c+dx)^{9/2}(bc-ad)^2}{3d^4} - \frac{2(c+dx)^{7/2}(bc-ad)^3}{7d^4} + \frac{2b^3(c+dx)^{13/2}}{13d^4}$$

[Out] $-2/7*(-a*d+b*c)^3*(d*x+c)^(7/2)/d^4+2/3*b*(-a*d+b*c)^2*(d*x+c)^(9/2)/d^4-6/11*b^2*(-a*d+b*c)*(d*x+c)^(11/2)/d^4+2/13*b^3*(d*x+c)^(13/2)/d^4$

Rubi [A] time = 0.03, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{6b^2(c+dx)^{11/2}(bc-ad)}{11d^4} + \frac{2b(c+dx)^{9/2}(bc-ad)^2}{3d^4} - \frac{2(c+dx)^{7/2}(bc-ad)^3}{7d^4} + \frac{2b^3(c+dx)^{13/2}}{13d^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3*(c + d*x)^(5/2), x]

[Out] $(-2*(b*c - a*d)^3*(c + d*x)^(7/2))/(7*d^4) + (2*b*(b*c - a*d)^2*(c + d*x)^(9/2))/(3*d^4) - (6*b^2*(b*c - a*d)*(c + d*x)^(11/2))/(11*d^4) + (2*b^3*(c + d*x)^(13/2))/(13*d^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^3 (c + dx)^{5/2} dx &= \int \left(\frac{(-bc + ad)^3 (c + dx)^{5/2}}{d^3} + \frac{3b(bc - ad)^2 (c + dx)^{7/2}}{d^3} - \frac{3b^2(bc - ad)(c + dx)^{9/2}}{d^3} + \frac{b^3(c + dx)^{11/2}}{d^3} \right) dx \\ &= -\frac{2(bc - ad)^3 (c + dx)^{7/2}}{7d^4} + \frac{2b(bc - ad)^2 (c + dx)^{9/2}}{3d^4} - \frac{6b^2(bc - ad)(c + dx)^{11/2}}{11d^4} + \frac{2b^3(c + dx)^{13/2}}{13d^4} \end{aligned}$$

Mathematica [A] time = 0.07, size = 79, normalized size = 0.79

$$\frac{2(c+dx)^{7/2}(-819b^2(c+dx)^2(bc-ad) + 1001b(c+dx)(bc-ad)^2 - 429(bc-ad)^3 + 231b^3(c+dx)^3)}{3003d^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3*(c + d*x)^(5/2), x]

[Out] $(2*(c + d*x)^{(7/2)}*(-429*(b*c - a*d)^3 + 1001*b*(b*c - a*d)^2*(c + d*x) - 819*b^2*(b*c - a*d)*(c + d*x)^2 + 231*b^3*(c + d*x)^3)/(3003*d^4)$

fricas [B] time = 0.42, size = 268, normalized size = 2.68

$$2 \left(231 b^3 d^6 x^6 - 16 b^3 c^6 + 104 a b^2 c^5 d - 286 a^2 b c^4 d^2 + 429 a^3 c^3 d^3 + 63 (9 b^3 c d^5 + 13 a b^2 d^6) x^5 + 7 (53 b^3 c^2 d^4 + 2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^(5/2), x, algorithm="fricas")

[Out] $2/3003*(231*b^3*d^6*x^6 - 16*b^3*c^6 + 104*a*b^2*c^5*d - 286*a^2*b*c^4*d^2 + 429*a^3*c^3*d^3 + 63*(9*b^3*c*d^5 + 13*a*b^2*d^6)*x^5 + 7*(53*b^3*c^2*d^4 + 299*a*b^2*c*d^5 + 143*a^2*b*d^6)*x^4 + (5*b^3*c^3*d^3 + 1469*a*b^2*c^2*d^4 + 2717*a^2*b*c*d^5 + 429*a^3*d^6)*x^3 - 3*(2*b^3*c^4*d^2 - 13*a*b^2*c^3*d^3 - 715*a^2*b*c^2*d^4 - 429*a^3*c*d^5)*x^2 + (8*b^3*c^5*d - 52*a*b^2*c^4*d^2 + 143*a^2*b*c^3*d^3 + 1287*a^3*c^2*d^4)*x)*sqrt(d*x + c)/d^4$

giac [B] time = 1.58, size = 857, normalized size = 8.57

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^(5/2), x, algorithm="giac")

[Out] $2/15015*(15015*sqrt(d*x + c)*a^3*c^3 + 15015*((d*x + c)^{(3/2)} - 3*sqrt(d*x + c))*c)*a^3*c^2 + 15015*((d*x + c)^{(3/2)} - 3*sqrt(d*x + c))*c)*a^2*b*c^3/d + 3003*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a^3*c + 3003*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a*b^2*c^3/d^2 + 9009*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*sqrt(d*x + c)*c^2)*a^2*b*c^2/d + 429*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a^3 + 429*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*b^3*c^3/d^3 + 3861*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a*b^2*c^2/d^2 + 3861*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 - 35*sqrt(d*x + c)*c^3)*a^2*b*c/d + 143*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*sqrt(d*x + c)*c^4)*b^3*c^2/d^3 + 429*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*sqrt(d*x + c)*c^4)*a*b^2*c/d^2 + 143*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*sqrt(d*x + c)*c^4)*a^2*b*c/d + 143*(35*(d*x + c)^{(9/2)} - 180*(d*x + c)^{(7/2)}*c + 378*(d*x + c)^{(5/2)}*c^2 - 420*(d*x + c)^{(3/2)}*c^3 + 315*sqrt(d*x + c)*c^4)*a^3*c/d$

$$\begin{aligned} & (3/2)*c^3 + 315*\sqrt{d*x + c}*c^4)*a^2*b/d + 65*(63*(d*x + c)^{(11/2)} - 385* \\ & (d*x + c)^{(9/2)}*c + 990*(d*x + c)^{(7/2)}*c^2 - 1386*(d*x + c)^{(5/2)}*c^3 + 11 \\ & 55*(d*x + c)^{(3/2)}*c^4 - 693*\sqrt{d*x + c}*c^5)*b^3*c/d^3 + 65*(63*(d*x + c) \\ &)^{(11/2)} - 385*(d*x + c)^{(9/2)}*c + 990*(d*x + c)^{(7/2)}*c^2 - 1386*(d*x + c) \\ & ^{(5/2)}*c^3 + 1155*(d*x + c)^{(3/2)}*c^4 - 693*\sqrt{d*x + c}*c^5)*a*b^2/d^2 + \\ & 5*(231*(d*x + c)^{(13/2)} - 1638*(d*x + c)^{(11/2)}*c + 5005*(d*x + c)^{(9/2)}*c^2 \\ & - 8580*(d*x + c)^{(7/2)}*c^3 + 9009*(d*x + c)^{(5/2)}*c^4 - 6006*(d*x + c)^{(3 \\ & /2)}*c^5 + 3003*\sqrt{d*x + c}*c^6)*b^3/d^3)/d \end{aligned}$$

maple [A] time = 0.01, size = 116, normalized size = 1.16

$$\frac{2(dx+c)^{\frac{7}{2}}(231b^3x^3d^3+819ab^2d^3x^2-126b^3cd^2x^2+1001a^2bd^3x-364ab^2cd^2x+56b^3c^2dx+429a^3d^3-286a^2d^2)}{3003d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3*(d*x+c)^(5/2),x)

[Out] 2/3003*(d*x+c)^(7/2)*(231*b^3*d^3*x^3+819*a*b^2*d^3*x^2-126*b^3*c*d^2*x^2+1001*a^2*b*d^3*x-364*a*b^2*c*d^2*x+56*b^3*c^2*d*x+429*a^3*d^3-286*a^2*b*c*d^2+104*a*b^2*c^2*d-16*b^3*c^3)/d^4

maxima [A] time = 1.40, size = 118, normalized size = 1.18

$$\frac{2\left(231(dx+c)^{\frac{13}{2}}b^3-819(b^3c-ab^2d)(dx+c)^{\frac{11}{2}}+1001(b^3c^2-2ab^2cd+a^2bd^2)(dx+c)^{\frac{9}{2}}-429(b^3c^3-3ab^2c^2d)\right)}{3003d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^(5/2),x, algorithm="maxima")

[Out] 2/3003*(231*(d*x + c)^(13/2)*b^3 - 819*(b^3*c - a*b^2*d)*(d*x + c)^(11/2) + 1001*(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*(d*x + c)^(9/2) - 429*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*(d*x + c)^(7/2))/d^4

mupad [B] time = 0.08, size = 87, normalized size = 0.87

$$\frac{2b^3(c+dx)^{13/2}}{13d^4} - \frac{(6b^3c-6ab^2d)(c+dx)^{11/2}}{11d^4} + \frac{2(ad-bc)^3(c+dx)^{7/2}}{7d^4} + \frac{2b(ad-bc)^2(c+dx)^{9/2}}{3d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3*(c + d*x)^(5/2),x)

[Out] (2*b^3*(c + d*x)^(13/2))/(13*d^4) - ((6*b^3*c - 6*a*b^2*d)*(c + d*x)^(11/2))/(11*d^4) + (2*(a*d - b*c)^3*(c + d*x)^(7/2))/(7*d^4) + (2*b*(a*d - b*c)^2*(c + d*x)^(9/2))/(3*d^4)

sympy [A] time = 4.61, size = 549, normalized size = 5.49

$$\left\{ \begin{array}{l} \frac{2a^3c^3\sqrt{c+dx}}{7d} + \frac{6a^3c^2x\sqrt{c+dx}}{7} + \frac{6a^3cdx^2\sqrt{c+dx}}{7} + \frac{2a^3d^2x^3\sqrt{c+dx}}{7} - \frac{4a^2bc^4\sqrt{c+dx}}{21d^2} + \frac{2a^2bc^3x\sqrt{c+dx}}{21d} + \frac{10a^2bc^2x^2\sqrt{c+dx}}{7} + \frac{38a^2bcdx^3}{21} \\ c^{\frac{5}{2}} \left(a^3x + \frac{3a^2bx^2}{2} + ab^2x^3 + \frac{b^3x^4}{4} \right) \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3*(d*x+c)**(5/2),x)

[Out] Piecewise((2*a**3*c**3*sqrt(c + d*x)/(7*d) + 6*a**3*c**2*x*sqrt(c + d*x)/7 + 6*a**3*c*d*x**2*sqrt(c + d*x)/7 + 2*a**3*d**2*x**3*sqrt(c + d*x)/7 - 4*a**2*b*c**4*sqrt(c + d*x)/(21*d**2) + 2*a**2*b*c**3*x*sqrt(c + d*x)/(21*d) + 10*a**2*b*c**2*x**2*sqrt(c + d*x)/7 + 38*a**2*b*c*d*x**3*sqrt(c + d*x)/21 + 2*a**2*b*d**2*x**4*sqrt(c + d*x)/3 + 16*a*b**2*c**5*sqrt(c + d*x)/(231*d**3) - 8*a*b**2*c**4*x*sqrt(c + d*x)/(231*d**2) + 2*a*b**2*c**3*x**2*sqrt(c + d*x)/(77*d) + 226*a*b**2*c**2*x**3*sqrt(c + d*x)/231 + 46*a*b**2*c*d*x**4*sqrt(c + d*x)/33 + 6*a*b**2*d**2*x**5*sqrt(c + d*x)/11 - 32*b**3*c**6*sqrt(c + d*x)/(3003*d**4) + 16*b**3*c**5*x*sqrt(c + d*x)/(3003*d**3) - 4*b**3*c**4*x**2*sqrt(c + d*x)/(1001*d**2) + 10*b**3*c**3*x**3*sqrt(c + d*x)/(3003*d) + 106*b**3*c**2*x**4*sqrt(c + d*x)/429 + 54*b**3*c*d*x**5*sqrt(c + d*x)/143 + 2*b**3*d**2*x**6*sqrt(c + d*x)/13, Ne(d, 0)), (c**(5/2)*(a**3*x + 3*a**2*b*x**2/2 + a*b**2*x**3 + b**3*x**4/4), True))

3.1402 $\int (a + bx)^2 (c + dx)^{5/2} dx$

Optimal. Leaf size=71

$$-\frac{4b(c+dx)^{9/2}(bc-ad)}{9d^3} + \frac{2(c+dx)^{7/2}(bc-ad)^2}{7d^3} + \frac{2b^2(c+dx)^{11/2}}{11d^3}$$

[Out] $2/7*(-a*d+b*c)^2*(d*x+c)^(7/2)/d^3-4/9*b*(-a*d+b*c)*(d*x+c)^(9/2)/d^3+2/11*b^2*(d*x+c)^(11/2)/d^3$

Rubi [A] time = 0.02, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{4b(c+dx)^{9/2}(bc-ad)}{9d^3} + \frac{2(c+dx)^{7/2}(bc-ad)^2}{7d^3} + \frac{2b^2(c+dx)^{11/2}}{11d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(c + d*x)^(5/2), x]

[Out] $(2*(b*c - a*d)^2*(c + d*x)^(7/2))/(7*d^3) - (4*b*(b*c - a*d)*(c + d*x)^(9/2))/(9*d^3) + (2*b^2*(c + d*x)^(11/2))/(11*d^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2 (c + dx)^{5/2} dx &= \int \left(\frac{(-bc + ad)^2 (c + dx)^{5/2}}{d^2} - \frac{2b(bc - ad)(c + dx)^{7/2}}{d^2} + \frac{b^2(c + dx)^{9/2}}{d^2} \right) dx \\ &= \frac{2(bc - ad)^2 (c + dx)^{7/2}}{7d^3} - \frac{4b(bc - ad)(c + dx)^{9/2}}{9d^3} + \frac{2b^2(c + dx)^{11/2}}{11d^3} \end{aligned}$$

Mathematica [A] time = 0.05, size = 61, normalized size = 0.86

$$\frac{2(c+dx)^{7/2} (99a^2d^2 + 22abd(7dx - 2c) + b^2(8c^2 - 28cdx + 63d^2x^2))}{693d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(c + d*x)^(5/2), x]

[Out] (2*(c + d*x)^(7/2)*(99*a^2*d^2 + 22*a*b*d*(-2*c + 7*d*x) + b^2*(8*c^2 - 28*c*d*x + 63*d^2*x^2)))/(693*d^3)

fricas [B] time = 0.43, size = 174, normalized size = 2.45

$$\frac{2(63b^2d^5x^5 + 8b^2c^5 - 44abc^4d + 99a^2c^3d^2 + 7(23b^2cd^4 + 22abd^5)x^4 + (113b^2c^2d^3 + 418abcd^4 + 99a^2d^5)x^3)}{693d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^(5/2), x, algorithm="fricas")

[Out] 2/693*(63*b^2*d^5*x^5 + 8*b^2*c^5 - 44*a*b*c^4*d + 99*a^2*c^3*d^2 + 7*(23*b^2*c*d^4 + 22*a*b*d^5)*x^4 + (113*b^2*c^2*d^3 + 418*a*b*c*d^4 + 99*a^2*d^5)*x^3 + 3*(b^2*c^3*d^2 + 110*a*b*c^2*d^3 + 99*a^2*c*d^4)*x^2 - (4*b^2*c^4*d - 22*a*b*c^3*d^2 - 297*a^2*c^2*d^3)*x)*sqrt(d*x + c)/d^3

giac [B] time = 1.76, size = 558, normalized size = 7.86

$$2 \left(3465 \sqrt{dx + c} a^2 c^3 + 3465 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} c \right) a^2 c^2 + \frac{2310 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} c \right) abc^3}{d} + 693 \left(3 (dx + c)^{\frac{5}{2}} - 10 \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^(5/2), x, algorithm="giac")

[Out] 2/3465*(3465*sqrt(d*x + c)*a^2*c^3 + 3465*((d*x + c)^(3/2) - 3*sqrt(d*x + c))*c)*a^2*c^2 + 2310*((d*x + c)^(3/2) - 3*sqrt(d*x + c))*a*b*c^3/d + 693*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2))*c + 15*sqrt(d*x + c)*c^2)*a^2*c + 231*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2))*c + 15*sqrt(d*x + c)*c^2)*b^2*c^3/d^2 + 1386*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2))*c + 15*sqrt(d*x + c)*c^2)*a*b*c^2/d + 99*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2))*c + 35*(d*x + c)^(3/2))*c^2 - 35*sqrt(d*x + c)*c^3)*a^2 + 297*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2))*c + 35*(d*x + c)^(3/2))*c^2 - 35*sqrt(d*x + c)*c^3)*b^2*c^2/d^2 + 594*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2))*c + 35*(d*x + c)^(3/2))*c^2 - 35*sqrt(d*x + c)*c^3)*a*b*c/d + 33*(35*(d*x + c)^(9/2) - 180*(d*x + c)^(7/2))*c + 378*(d*x + c)^(5/2))*c^2 - 420*(d*x + c)^(3/2))*c^3 + 315*sqrt(d*x + c)*c^4)*b^2*c/d^2 + 22*(35*(d*x + c)^(9/2) - 180*(d*x + c)^(7/2))*c + 378*(d*x + c)^(5/2))*c^2 - 420*(d*x + c)^(3/2))*c^3 + 315*sqrt(d*x + c)*c^4)*a*b/d + 5*(63*(d*x + c)^(11/2) - 385*(d*x + c)^(9/2))*c + 990*(d*x + c)^(7/2))*c^2 - 138

$$6*(d*x + c)^{(5/2)}*c^3 + 1155*(d*x + c)^{(3/2)}*c^4 - 693*\sqrt{d*x + c}*c^5)*b^2/d^2)/d$$

maple [A] time = 0.01, size = 63, normalized size = 0.89

$$\frac{2(dx + c)^{\frac{7}{2}}(63b^2x^2d^2 + 154abd^2x - 28b^2cdx + 99a^2d^2 - 44abcd + 8b^2c^2)}{693d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2*(d*x+c)^(5/2), x)

[Out] 2/693*(d*x+c)^(7/2)*(63*b^2*d^2*x^2+154*a*b*d^2*x-28*b^2*c*d*x+99*a^2*d^2-4*a*b*c*d+8*b^2*c^2)/d^3

maxima [A] time = 1.38, size = 68, normalized size = 0.96

$$\frac{2\left(63(dx + c)^{\frac{11}{2}}b^2 - 154(b^2c - abd)(dx + c)^{\frac{9}{2}} + 99(b^2c^2 - 2abcd + a^2d^2)(dx + c)^{\frac{7}{2}}\right)}{693d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^(5/2), x, algorithm="maxima")

[Out] 2/693*(63*(d*x + c)^(11/2)*b^2 - 154*(b^2*c - a*b*d)*(d*x + c)^(9/2) + 99*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(d*x + c)^(7/2))/d^3

mupad [B] time = 0.07, size = 68, normalized size = 0.96

$$\frac{2(c + dx)^{7/2} (63b^2(c + dx)^2 + 99a^2d^2 + 99b^2c^2 - 154b^2c(c + dx) + 154abd(c + dx) - 198abcd)}{693d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2*(c + d*x)^(5/2), x)

[Out] (2*(c + d*x)^(7/2)*(63*b^2*(c + d*x)^2 + 99*a^2*d^2 + 99*b^2*c^2 - 154*b^2*c*(c + d*x) + 154*a*b*d*(c + d*x) - 198*a*b*c*d))/(693*d^3)

sympy [A] time = 3.58, size = 355, normalized size = 5.00

$$\left\{ \begin{array}{l} \frac{2a^2c^3\sqrt{c+dx}}{7d} + \frac{6a^2c^2x\sqrt{c+dx}}{7} + \frac{6a^2cdx^2\sqrt{c+dx}}{7} + \frac{2a^2d^2x^3\sqrt{c+dx}}{7} - \frac{8abc^4\sqrt{c+dx}}{63d^2} + \frac{4abc^3x\sqrt{c+dx}}{63d} + \frac{20abc^2x^2\sqrt{c+dx}}{21} + \frac{76abcdx^3\sqrt{c+dx}}{63} \\ c^{\frac{5}{2}} \left(a^2x + abx^2 + \frac{b^2x^3}{3} \right) \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2*(d*x+c)**(5/2),x)

[Out] Piecewise((2*a**2*c**3*sqrt(c + d*x)/(7*d) + 6*a**2*c**2*x*sqrt(c + d*x)/7 + 6*a**2*c*d*x**2*sqrt(c + d*x)/7 + 2*a**2*d**2*x**3*sqrt(c + d*x)/7 - 8*a*b*c**4*sqrt(c + d*x)/(63*d**2) + 4*a*b*c**3*x*sqrt(c + d*x)/(63*d) + 20*a*b*c**2*x**2*sqrt(c + d*x)/21 + 76*a*b*c*d*x**3*sqrt(c + d*x)/63 + 4*a*b*d**2*x**4*sqrt(c + d*x)/9 + 16*b**2*c**5*sqrt(c + d*x)/(693*d**3) - 8*b**2*c**4*x*sqrt(c + d*x)/(693*d**2) + 2*b**2*c**3*x**2*sqrt(c + d*x)/(231*d) + 226*b**2*c**2*x**3*sqrt(c + d*x)/693 + 46*b**2*c*d*x**4*sqrt(c + d*x)/99 + 2*b**2*d**2*x**5*sqrt(c + d*x)/11, Ne(d, 0)), (c**(5/2)*(a**2*x + a*b*x**2 + b**2*x**3/3), True))

3.1403 $\int (a + bx)(c + dx)^{5/2} dx$

Optimal. Leaf size=42

$$\frac{2b(c + dx)^{9/2}}{9d^2} - \frac{2(c + dx)^{7/2}(bc - ad)}{7d^2}$$

[Out] $-2/7*(-a*d+b*c)*(d*x+c)^{(7/2)}/d^2+2/9*b*(d*x+c)^{(9/2)}/d^2$

Rubi [A] time = 0.01, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{2b(c + dx)^{9/2}}{9d^2} - \frac{2(c + dx)^{7/2}(bc - ad)}{7d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)*(c + d*x)^(5/2), x]

[Out] $(-2*(b*c - a*d)*(c + d*x)^{(7/2)})/(7*d^2) + (2*b*(c + d*x)^{(9/2)})/(9*d^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)(c + dx)^{5/2} dx &= \int \left(\frac{(-bc + ad)(c + dx)^{5/2}}{d} + \frac{b(c + dx)^{7/2}}{d} \right) dx \\ &= -\frac{2(bc - ad)(c + dx)^{7/2}}{7d^2} + \frac{2b(c + dx)^{9/2}}{9d^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 30, normalized size = 0.71

$$\frac{2(c + dx)^{7/2}(9ad - 2bc + 7bdx)}{63d^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(c + d*x)^(5/2), x]

[Out] $(2*(c + d*x)^(7/2)*(-2*b*c + 9*a*d + 7*b*d*x))/(63*d^2)$

fricas [B] time = 0.44, size = 93, normalized size = 2.21

$$\frac{2(7bd^4x^4 - 2bc^4 + 9ac^3d + (19bcd^3 + 9ad^4)x^3 + 3(5bc^2d^2 + 9acd^3)x^2 + (bc^3d + 27ac^2d^2)x)\sqrt{dx+c}}{63d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^(5/2), x, algorithm="fricas")

[Out] $2/63*(7*b*d^4*x^4 - 2*b*c^4 + 9*a*c^3*d + (19*b*c*d^3 + 9*a*d^4)*x^3 + 3*(5*b*c^2*d^2 + 9*a*c*d^3)*x^2 + (b*c^3*d + 27*a*c^2*d^2)*x)*\text{sqrt}(d*x + c)/d^2$

giac [B] time = 1.61, size = 306, normalized size = 7.29

$$2 \left(315 \sqrt{dx+c} ac^3 + 315 \left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} \right) ac^2 + \frac{105 \left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} \right) bc^3}{d} + 63 \left(3(dx+c)^{\frac{5}{2}} - 10(dx+c)^{\frac{3}{2}} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^(5/2), x, algorithm="giac")

[Out] $2/315*(315*\text{sqrt}(d*x + c)*a*c^3 + 315*((d*x + c)^(3/2) - 3*\text{sqrt}(d*x + c))*a*c^2 + 105*((d*x + c)^(3/2) - 3*\text{sqrt}(d*x + c))*b*c^3/d + 63*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*\text{sqrt}(d*x + c)*c^2)*a*c + 63*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*\text{sqrt}(d*x + c)*c^2)*b*c^2/d + 9*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*\text{sqrt}(d*x + c)*c^3)*a + 27*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*\text{sqrt}(d*x + c)*c^3)*b*c/d + (35*(d*x + c)^(9/2) - 180*(d*x + c)^(7/2)*c + 378*(d*x + c)^(5/2)*c^2 - 420*(d*x + c)^(3/2)*c^3 + 315*\text{sqrt}(d*x + c)*c^4)*b/d)/d$

maple [A] time = 0.00, size = 27, normalized size = 0.64

$$\frac{2(dx+c)^{\frac{7}{2}}(7bdx+9ad-2bc)}{63d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(d*x+c)^(5/2), x)

[Out] $2/63*(d*x+c)^(7/2)*(7*b*d*x+9*a*d-2*b*c)/d^2$

maxima [A] time = 1.40, size = 33, normalized size = 0.79

$$\frac{2 \left(7 (dx + c)^{\frac{9}{2}} b - 9 (bc - ad) (dx + c)^{\frac{7}{2}} \right)}{63 d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^(5/2),x, algorithm="maxima")

[Out] 2/63*(7*(d*x + c)^(9/2)*b - 9*(b*c - a*d)*(d*x + c)^(7/2))/d^2

mupad [B] time = 0.05, size = 29, normalized size = 0.69

$$\frac{2 (c + dx)^{7/2} (9 ad - 9 bc + 7 b (c + dx))}{63 d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)*(c + d*x)^(5/2),x)

[Out] (2*(c + d*x)^(7/2)*(9*a*d - 9*b*c + 7*b*(c + d*x)))/(63*d^2)

sympy [A] time = 2.36, size = 194, normalized size = 4.62

$$\left\{ \begin{array}{l} \frac{2ac^3\sqrt{c+dx}}{7d} + \frac{6ac^2x\sqrt{c+dx}}{7} + \frac{6acdx^2\sqrt{c+dx}}{7} + \frac{2ad^2x^3\sqrt{c+dx}}{7} - \frac{4bc^4\sqrt{c+dx}}{63d^2} + \frac{2bc^3x\sqrt{c+dx}}{63d} + \frac{10bc^2x^2\sqrt{c+dx}}{21} + \frac{38bcdx^3\sqrt{c+dx}}{63} + \frac{2bd^4x^4\sqrt{c+dx}}{63} \\ c^{\frac{5}{2}} \left(ax + \frac{bx^2}{2} \right) \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)**(5/2),x)

[Out] Piecewise(((2*a*c**3*sqrt(c + d*x)/(7*d) + 6*a*c**2*x*sqrt(c + d*x)/7 + 6*a*c*d*x**2*sqrt(c + d*x)/7 + 2*a*d**2*x**3*sqrt(c + d*x)/7 - 4*b*c**4*sqrt(c + d*x)/(63*d**2) + 2*b*c**3*x*sqrt(c + d*x)/(63*d) + 10*b*c**2*x**2*sqrt(c + d*x)/21 + 38*b*c*d*x**3*sqrt(c + d*x)/63 + 2*b*d**2*x**4*sqrt(c + d*x)/9, Ne(d, 0)), (c**(5/2)*(a*x + b*x**2/2), True))

3.1404 $\int (c + dx)^{5/2} dx$

Optimal. Leaf size=16

$$\frac{2(c + dx)^{7/2}}{7d}$$

[Out] $2/7*(d*x+c)^{(7/2)}/d$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{2(c + dx)^{7/2}}{7d}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2), x]

[Out] (2*(c + d*x)^(7/2))/(7*d)

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int (c + dx)^{5/2} dx = \frac{2(c + dx)^{7/2}}{7d}$$

Mathematica [A] time = 0.01, size = 16, normalized size = 1.00

$$\frac{2(c + dx)^{7/2}}{7d}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2), x]

[Out] (2*(c + d*x)^(7/2))/(7*d)

fricas [B] time = 0.42, size = 39, normalized size = 2.44

$$\frac{2(d^3x^3 + 3cd^2x^2 + 3c^2dx + c^3)\sqrt{dx + c}}{7d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2),x, algorithm="fricas")

[Out] $2/7*(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3)*\text{sqrt}(d*x + c)/d$

giac [B] time = 1.78, size = 95, normalized size = 5.94

$$\frac{2 \left(5 (dx + c)^{\frac{7}{2}} - 21 (dx + c)^{\frac{5}{2}} c + 35 (dx + c)^{\frac{3}{2}} c^2 + 35 \left((dx + c)^{\frac{3}{2}} - 3 \sqrt{dx + c} c \right) c^2 + 7 \left(3 (dx + c)^{\frac{5}{2}} - 10 (dx + c)^{\frac{3}{2}} c \right) \right)}{35 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2),x, algorithm="giac")

[Out] $2/35*(5*(d*x + c)^{(7/2)} - 21*(d*x + c)^{(5/2)}*c + 35*(d*x + c)^{(3/2)}*c^2 + 3*5*((d*x + c)^{(3/2)} - 3*\text{sqrt}(d*x + c)*c)*c^2 + 7*(3*(d*x + c)^{(5/2)} - 10*(d*x + c)^{(3/2)}*c + 15*\text{sqrt}(d*x + c)*c^2)*c)/d$

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$\frac{2(dx + c)^{\frac{7}{2}}}{7d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2),x)

[Out] $2/7*(d*x+c)^{(7/2)}/d$

maxima [A] time = 1.30, size = 12, normalized size = 0.75

$$\frac{2(dx + c)^{\frac{7}{2}}}{7d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2),x, algorithm="maxima")

[Out] $2/7*(d*x + c)^{(7/2)}/d$

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$\frac{2(c + dx)^{7/2}}{7d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/2),x)
```

```
[Out] (2*(c + d*x)^(7/2))/(7*d)
```

sympy [A] time = 0.06, size = 12, normalized size = 0.75

$$\frac{2(c + dx)^{\frac{7}{2}}}{7d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/2),x)
```

```
[Out] 2*(c + d*x)**(7/2)/(7*d)
```

$$3.1405 \quad \int \frac{(c+dx)^{5/2}}{a+bx} dx$$

Optimal. Leaf size=112

$$-\frac{2(bc-ad)^{5/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{7/2}} + \frac{2\sqrt{c+dx}(bc-ad)^2}{b^3} + \frac{2(c+dx)^{3/2}(bc-ad)}{3b^2} + \frac{2(c+dx)^{5/2}}{5b}$$

[Out] $2/3*(-a*d+b*c)*(d*x+c)^{(3/2)}/b^2+2/5*(d*x+c)^{(5/2)}/b-2*(-a*d+b*c)^{(5/2)}*\text{arc tanh}(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})/b^{(7/2)}+2*(-a*d+b*c)^2*(d*x+c)^{(1/2)}/b^3$

Rubi [A] time = 0.06, antiderivative size = 112, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {50, 63, 208}

$$\frac{2\sqrt{c+dx}(bc-ad)^2}{b^3} + \frac{2(c+dx)^{3/2}(bc-ad)}{3b^2} - \frac{2(bc-ad)^{5/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{7/2}} + \frac{2(c+dx)^{5/2}}{5b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x), x]

[Out] $(2*(b*c - a*d)^2*\text{Sqrt}[c + d*x])/b^3 + (2*(b*c - a*d)*(c + d*x)^{(3/2)})/(3*b^2) + (2*(c + d*x)^{(5/2)})/(5*b) - (2*(b*c - a*d)^{(5/2)}*\text{ArcTanh}[(\text{Sqrt}[b]*\text{Sqrt}[c + d*x])/\text{Sqrt}[b*c - a*d]])/b^{(7/2)}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(c+dx)^{5/2}}{a+bx} dx &= \frac{2(c+dx)^{5/2}}{5b} + \frac{(bc-ad) \int \frac{(c+dx)^{3/2}}{a+bx} dx}{b} \\
 &= \frac{2(bc-ad)(c+dx)^{3/2}}{3b^2} + \frac{2(c+dx)^{5/2}}{5b} + \frac{(bc-ad)^2 \int \frac{\sqrt{c+dx}}{a+bx} dx}{b^2} \\
 &= \frac{2(bc-ad)^2 \sqrt{c+dx}}{b^3} + \frac{2(bc-ad)(c+dx)^{3/2}}{3b^2} + \frac{2(c+dx)^{5/2}}{5b} + \frac{(bc-ad)^3 \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{b^3} \\
 &= \frac{2(bc-ad)^2 \sqrt{c+dx}}{b^3} + \frac{2(bc-ad)(c+dx)^{3/2}}{3b^2} + \frac{2(c+dx)^{5/2}}{5b} + \frac{(2(bc-ad)^3) \text{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{b}{d}x} dx\right)}{b^3 d} \\
 &= \frac{2(bc-ad)^2 \sqrt{c+dx}}{b^3} + \frac{2(bc-ad)(c+dx)^{3/2}}{3b^2} + \frac{2(c+dx)^{5/2}}{5b} - \frac{2(bc-ad)^{5/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{7/2}}
 \end{aligned}$$

Mathematica [A] time = 0.16, size = 105, normalized size = 0.94

$$\frac{2(bc-ad) \left(\sqrt{b}\sqrt{c+dx}(-3ad+4bc+bdx) - 3(bc-ad)^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right) \right)}{3b^{7/2}} + \frac{2(c+dx)^{5/2}}{5b}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x), x]

[Out] (2*(c + d*x)^(5/2))/(5*b) + (2*(b*c - a*d)*(Sqrt[b]*Sqrt[c + d*x]*(4*b*c - 3*a*d + b*d*x) - 3*(b*c - a*d)^(3/2)*ArcTanh[(Sqrt[b]*Sqrt[c + d*x])/Sqrt[b*c - a*d]])/(3*b^(7/2))

fricas [A] time = 0.50, size = 290, normalized size = 2.59

$$\left[\frac{15(b^2c^2 - 2abcd + a^2d^2) \sqrt{\frac{bc-ad}{b}} \log\left(\frac{bdx+2bc-ad-2\sqrt{dx+c}b\sqrt{\frac{bc-ad}{b}}}{bx+a}\right) + 2(3b^2d^2x^2 + 23b^2c^2 - 35abcd + 15a^2d^2 + \dots)}{15b^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a),x, algorithm="fricas")

[Out] [1/15*(15*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*sqrt((b*c - a*d)/b)*log((b*d*x + 2*b*c - a*d - 2*sqrt(d*x + c)*b*sqrt((b*c - a*d)/b))/(b*x + a) + 2*(3*b^2*d^2*x^2 + 23*b^2*c^2 - 35*a*b*c*d + 15*a^2*d^2 + (11*b^2*c*d - 5*a*b*d^2)*x)*sqrt(d*x + c))/b^3, -2/15*(15*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*sqrt(-(b*c - a*d)/b)*arctan(-sqrt(d*x + c)*b*sqrt(-(b*c - a*d)/b)/(b*c - a*d)) - (3*b^2*d^2*x^2 + 23*b^2*c^2 - 35*a*b*c*d + 15*a^2*d^2 + (11*b^2*c*d - 5*a*b*d^2)*x)*sqrt(d*x + c))/b^3]

giac [A] time = 1.60, size = 171, normalized size = 1.53

$$\frac{2(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3) \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{-b^2c+abd}}\right) + 2\left(3(dx+c)^{\frac{5}{2}}b^4 + 5(dx+c)^{\frac{3}{2}}b^4c + 15\sqrt{dx+c}b^4c^2 - 5\sqrt{dx+c}b^4c^3\right)}{\sqrt{-b^2c+abd}b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a),x, algorithm="giac")

[Out] 2*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/(sqrt(-b^2*c + a*b*d)*b^3) + 2/15*(3*(d*x + c)^(5/2)*b^4 + 5*(d*x + c)^(3/2)*b^4*c + 15*sqrt(d*x + c)*b^4*c^2 - 5*(d*x + c)^(3/2)*a*b^3*d - 30*sqrt(d*x + c)*a*b^3*c*d + 15*sqrt(d*x + c)*a^2*b^2*d^2)/b^5

maple [B] time = 0.01, size = 263, normalized size = 2.35

$$-\frac{2a^3d^3 \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b^3} + \frac{6a^2cd^2 \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b^2} - \frac{6ac^2d \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b} + \frac{2c^3 \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}} + \frac{2\sqrt{dx+c}b^4}{\sqrt{(ad-bc)b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a),x)

[Out] 2/5*(d*x+c)^(5/2)/b-2/3/b^2*(d*x+c)^(3/2)*a*d+2/3/b*(d*x+c)^(3/2)*c+2/b^3*a^2*d^2*(d*x+c)^(1/2)-4/b^2*a*c*d*(d*x+c)^(1/2)+2/b*c^2*(d*x+c)^(1/2)-2/b^3/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)*a^3*d^3+6/b^2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)*a^2*c*d^2-6/b/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)*a*c^2*d+2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)*c^3

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.08, size = 130, normalized size = 1.16

$$\frac{2(c+dx)^{5/2}}{5b} - \frac{2(ad-bc)(c+dx)^{3/2}}{3b^2} + \frac{2(ad-bc)^2\sqrt{c+dx}}{b^3} - \frac{2\operatorname{atan}\left(\frac{\sqrt{b(ad-bc)^{5/2}\sqrt{c+dx}}}{a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3}\right)(ad-bc)^{5/2}}{b^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/2)/(a + b*x),x)

[Out] (2*(c + d*x)^(5/2))/(5*b) - (2*(a*d - b*c)*(c + d*x)^(3/2))/(3*b^2) + (2*(a*d - b*c)^2*(c + d*x)^(1/2))/b^3 - (2*atan((b^(1/2)*(a*d - b*c)^(5/2)*(c + d*x)^(1/2))/(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2))*(a*d - b*c)^(5/2))/b^(7/2)

sympy [A] time = 27.01, size = 121, normalized size = 1.08

$$\frac{2(c+dx)^{5/2}}{5b} + \frac{(c+dx)^{3/2}(-2ad+2bc)}{3b^2} + \frac{\sqrt{c+dx}(2a^2d^2-4abcd+2b^2c^2)}{b^3} - \frac{2(ad-bc)^3\operatorname{atan}\left(\frac{\sqrt{c+dx}}{\sqrt{\frac{ad-bc}{b}}}\right)}{b^4\sqrt{\frac{ad-bc}{b}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/2)/(b*x+a),x)

[Out] 2*(c + d*x)**(5/2)/(5*b) + (c + d*x)**(3/2)*(-2*a*d + 2*b*c)/(3*b**2) + sqrt(c + d*x)*(2*a**2*d**2 - 4*a*b*c*d + 2*b**2*c**2)/b**3 - 2*(a*d - b*c)**3*atan(sqrt(c + d*x)/sqrt((a*d - b*c)/b))/(b**4*sqrt((a*d - b*c)/b))

$$3.1406 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^2} dx$$

Optimal. Leaf size=110

$$-\frac{5d(bc-ad)^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{7/2}} + \frac{5d\sqrt{c+dx}(bc-ad)}{b^3} - \frac{(c+dx)^{5/2}}{b(a+bx)} + \frac{5d(c+dx)^{3/2}}{3b^2}$$

[Out] $5/3*d*(d*x+c)^{(3/2)}/b^2-(d*x+c)^{(5/2)}/b/(b*x+a)-5*d*(-a*d+b*c)^{(3/2)}*\arctan$
 $h(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})/b^{(7/2)}+5*d*(-a*d+b*c)*(d*x+c)^{(1$
 $/2)/b^3$

Rubi [A] time = 0.05, antiderivative size = 110, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 63, 208}

$$\frac{5d\sqrt{c+dx}(bc-ad)}{b^3} - \frac{5d(bc-ad)^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{7/2}} - \frac{(c+dx)^{5/2}}{b(a+bx)} + \frac{5d(c+dx)^{3/2}}{3b^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^2, x]

[Out] $(5*d*(b*c - a*d)*\text{Sqrt}[c + d*x])/b^3 + (5*d*(c + d*x)^{(3/2)})/(3*b^2) - (c +$
 $d*x)^{(5/2)}/(b*(a + b*x)) - (5*d*(b*c - a*d)^{(3/2)}*\text{ArcTanh}[(\text{Sqrt}[b]*\text{Sqrt}[c +$
 $d*x])/(\text{Sqrt}[b*c - a*d])]/b^{(7/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
 ((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
 nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
 NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
 rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
 & IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
 ((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
 (b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
 c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
 [m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
 + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/2}}{(a+bx)^2} dx &= -\frac{(c+dx)^{5/2}}{b(a+bx)} + \frac{(5d) \int \frac{(c+dx)^{3/2}}{a+bx} dx}{2b} \\
&= \frac{5d(c+dx)^{3/2}}{3b^2} - \frac{(c+dx)^{5/2}}{b(a+bx)} + \frac{(5d(bc-ad)) \int \frac{\sqrt{c+dx}}{a+bx} dx}{2b^2} \\
&= \frac{5d(bc-ad)\sqrt{c+dx}}{b^3} + \frac{5d(c+dx)^{3/2}}{3b^2} - \frac{(c+dx)^{5/2}}{b(a+bx)} + \frac{(5d(bc-ad)^2) \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{2b^3} \\
&= \frac{5d(bc-ad)\sqrt{c+dx}}{b^3} + \frac{5d(c+dx)^{3/2}}{3b^2} - \frac{(c+dx)^{5/2}}{b(a+bx)} + \frac{(5(bc-ad)^2) \operatorname{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{b^3} \\
&= \frac{5d(bc-ad)\sqrt{c+dx}}{b^3} + \frac{5d(c+dx)^{3/2}}{3b^2} - \frac{(c+dx)^{5/2}}{b(a+bx)} - \frac{5d(bc-ad)^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.45

$$\frac{2d(c+dx)^{7/2} {}_2F_1\left(2, \frac{7}{2}; \frac{9}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{7(ad-bc)^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^2, x]
```

```
[Out] (2*d*(c + d*x)^(7/2)*Hypergeometric2F1[2, 7/2, 9/2, -((b*(c + d*x))/(-b*c)
+ a*d)))/(7*(-b*c) + a*d)^2
```

fricas [A] time = 0.48, size = 330, normalized size = 3.00

$$\left[\frac{15 \left(abcd - a^2 d^2 + (b^2 cd - abd^2)x \right) \sqrt{\frac{bc-ad}{b}} \log \left(\frac{bdx+2bc-ad+2\sqrt{dx+c}b\sqrt{\frac{bc-ad}{b}}}{bx+a} \right) - 2 \left(2b^2 d^2 x^2 - 3b^2 c^2 + 20abcd - 15a^2 d^2 \right)}{6(b^4 x + ab^3)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^2,x, algorithm="fricas")

[Out] [-1/6*(15*(a*b*c*d - a^2*d^2 + (b^2*c*d - a*b*d^2)*x)*sqrt((b*c - a*d)/b)*log((b*d*x + 2*b*c - a*d + 2*sqrt(d*x + c)*b*sqrt((b*c - a*d)/b))/(b*x + a) - 2*(2*b^2*d^2*x^2 - 3*b^2*c^2 + 20*a*b*c*d - 15*a^2*d^2 + 2*(7*b^2*c*d - 5*a*b*d^2)*x)*sqrt(d*x + c))/(b^4*x + a*b^3), -1/3*(15*(a*b*c*d - a^2*d^2 + (b^2*c*d - a*b*d^2)*x)*sqrt(-(b*c - a*d)/b)*arctan(-sqrt(d*x + c)*b*sqrt(-(b*c - a*d)/b)/(b*c - a*d)) - (2*b^2*d^2*x^2 - 3*b^2*c^2 + 20*a*b*c*d - 15*a^2*d^2 + 2*(7*b^2*c*d - 5*a*b*d^2)*x)*sqrt(d*x + c))/(b^4*x + a*b^3)]

giac [A] time = 1.28, size = 181, normalized size = 1.65

$$\frac{5(b^2 c^2 d - 2abcd^2 + a^2 d^3) \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{-b^2c+abd}}\right)}{\sqrt{-b^2c+abd}b^3} - \frac{\sqrt{dx+c}b^2c^2d - 2\sqrt{dx+c}abcd^2 + \sqrt{dx+c}a^2d^3}{((dx+c)b - bc + ad)b^3} + \frac{2((dx+c)^{\frac{3}{2}}b^4)}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^2,x, algorithm="giac")

[Out] 5*(b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3)*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/(sqrt(-b^2*c + a*b*d)*b^3) - (sqrt(d*x + c)*b^2*c^2*d - 2*sqrt(d*x + c)*a*b*c*d^2 + sqrt(d*x + c)*a^2*d^3)/(((d*x + c)*b - b*c + a*d)*b^3) + 2/3*((d*x + c)^(3/2)*b^4*d + 6*sqrt(d*x + c)*b^4*c*d - 6*sqrt(d*x + c)*a*b^3*d^2)/b^6

maple [B] time = 0.01, size = 258, normalized size = 2.35

$$\frac{5a^2d^3 \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b^3} - \frac{10acd^2 \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b^2} + \frac{5c^2d \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}b} - \frac{\sqrt{dx+c}a^2d^3}{(bdx+ad)b^3} + \frac{2\sqrt{dx+c}acd^2}{(bdx+ad)b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^2,x)

```
[Out] 2/3*d*(d*x+c)^(3/2)/b^2-4/b^3*a*d^2*(d*x+c)^(1/2)+4*d/b^2*(d*x+c)^(1/2)*c-1
/b^3*(d*x+c)^(1/2)/(b*d*x+a*d)*a^2*d^3+2/b^2*(d*x+c)^(1/2)/(b*d*x+a*d)*a*c*
d^2-d/b*(d*x+c)^(1/2)/(b*d*x+a*d)*c^2+5/b^3/((a*d-b*c)*b)^(1/2)*arctan((d*x
+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)*a^2*d^3-10/b^2/((a*d-b*c)*b)^(1/2)*arctan(
(d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)*a*c*d^2+5*d/b/((a*d-b*c)*b)^(1/2)*arct
an((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)*c^2
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(5/2)/(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError >> Computation failed since Maxima requested a
dditional constraints; using the 'assume' command before evaluation *may* h
elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more
details)Is a*d-b*c positive or negative?
```

mupad [B] time = 0.12, size = 161, normalized size = 1.46

$$\frac{2d(c+dx)^{3/2}}{3b^2} - \frac{\sqrt{c+dx}(a^2d^3 - 2abcd^2 + b^2c^2d)}{b^4(c+dx) - b^4c + ab^3d} + \frac{5d \operatorname{atan}\left(\frac{\sqrt{b}d(ad-bc)^{3/2}\sqrt{c+dx}}{a^2d^3 - 2abcd^2 + b^2c^2d}\right)(ad-bc)^{3/2}}{b^{7/2}} + \frac{2d(2b^2c - 2ab^2d)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/2)/(a + b*x)^2,x)
```

```
[Out] (2*d*(c + d*x)^(3/2))/(3*b^2) - ((c + d*x)^(1/2)*(a^2*d^3 + b^2*c^2*d - 2*a
*b*c*d^2))/(b^4*(c + d*x) - b^4*c + a*b^3*d) + (5*d*atan((b^(1/2)*d*(a*d -
b*c)^(3/2)*(c + d*x)^(1/2))/(a^2*d^3 + b^2*c^2*d - 2*a*b*c*d^2))*(a*d - b*c
)^(3/2))/b^(7/2) + (2*d*(2*b^2*c - 2*a*b*d)*(c + d*x)^(1/2))/b^4
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/2)/(b*x+a)**2,x)
```

```
[Out] Timed out
```

$$3.1407 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^3} dx$$

Optimal. Leaf size=119

$$-\frac{15d^2\sqrt{bc-ad} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4b^{7/2}} - \frac{5d(c+dx)^{3/2}}{4b^2(a+bx)} - \frac{(c+dx)^{5/2}}{2b(a+bx)^2} + \frac{15d^2\sqrt{c+dx}}{4b^3}$$

[Out] $-5/4*d*(d*x+c)^{(3/2)}/b^2/(b*x+a)-1/2*(d*x+c)^{(5/2)}/b/(b*x+a)^2-15/4*d^2*\text{arc tanh}(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})*(-a*d+b*c)^{(1/2)}/b^{(7/2)}+15/4*d^2*(d*x+c)^{(1/2)}/b^3$

Rubi [A] time = 0.05, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 50, 63, 208}

$$-\frac{15d^2\sqrt{bc-ad} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4b^{7/2}} - \frac{5d(c+dx)^{3/2}}{4b^2(a+bx)} - \frac{(c+dx)^{5/2}}{2b(a+bx)^2} + \frac{15d^2\sqrt{c+dx}}{4b^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^3, x]

[Out] $(15*d^2*\text{Sqrt}[c + d*x])/(4*b^3) - (5*d*(c + d*x)^{(3/2)})/(4*b^2*(a + b*x)) - (c + d*x)^{(5/2)}/(2*b*(a + b*x)^2) - (15*d^2*\text{Sqrt}[b*c - a*d]*\text{ArcTanh}[(\text{Sqrt}[b]*\text{Sqrt}[c + d*x])/\text{Sqrt}[b*c - a*d]])/(4*b^{(7/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/2}}{(a+bx)^3} dx &= -\frac{(c+dx)^{5/2}}{2b(a+bx)^2} + \frac{(5d) \int \frac{(c+dx)^{3/2}}{(a+bx)^2} dx}{4b} \\
&= -\frac{5d(c+dx)^{3/2}}{4b^2(a+bx)} - \frac{(c+dx)^{5/2}}{2b(a+bx)^2} + \frac{(15d^2) \int \frac{\sqrt{c+dx}}{a+bx} dx}{8b^2} \\
&= \frac{15d^2\sqrt{c+dx}}{4b^3} - \frac{5d(c+dx)^{3/2}}{4b^2(a+bx)} - \frac{(c+dx)^{5/2}}{2b(a+bx)^2} + \frac{(15d^2(bc-ad)) \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{8b^3} \\
&= \frac{15d^2\sqrt{c+dx}}{4b^3} - \frac{5d(c+dx)^{3/2}}{4b^2(a+bx)} - \frac{(c+dx)^{5/2}}{2b(a+bx)^2} + \frac{(15d(bc-ad)) \operatorname{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{4b^3} \\
&= \frac{15d^2\sqrt{c+dx}}{4b^3} - \frac{5d(c+dx)^{3/2}}{4b^2(a+bx)} - \frac{(c+dx)^{5/2}}{2b(a+bx)^2} - \frac{15d^2\sqrt{bc-ad} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.44

$$\frac{2d^2(c+dx)^{7/2} {}_2F_1\left(3, \frac{7}{2}; \frac{9}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{7(ad-bc)^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^3, x]
```

```
[Out] (2*d^2*(c + d*x)^(7/2)*Hypergeometric2F1[3, 7/2, 9/2, -((b*(c + d*x))/(-b*c) + a*d))]/(7*(-(b*c) + a*d)^3)
```

fricas [A] time = 0.47, size = 344, normalized size = 2.89

$$\frac{15 \left(b^2 d^2 x^2 + 2 a b d^2 x + a^2 d^2 \right) \sqrt{\frac{bc-ad}{b}} \log \left(\frac{bdx+2bc-ad-2\sqrt{dx+c}b\sqrt{\frac{bc-ad}{b}}}{bx+a} \right) + 2 \left(8 b^2 d^2 x^2 - 2 b^2 c^2 - 5 abcd + 15 a^2 d^2 - \right)}{8 \left(b^5 x^2 + 2 ab^4 x + a^2 b^3 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^3,x, algorithm="fricas")

[Out] [1/8*(15*(b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*sqrt((b*c - a*d)/b)*log((b*d*x + 2*b*c - a*d - 2*sqrt(d*x + c)*b*sqrt((b*c - a*d)/b))/(b*x + a)) + 2*(8*b^2*d^2*x^2 - 2*b^2*c^2 - 5*a*b*c*d + 15*a^2*d^2 - (9*b^2*c*d - 25*a*b*d^2)*x)*sqrt(d*x + c))/(b^5*x^2 + 2*a*b^4*x + a^2*b^3), -1/4*(15*(b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*sqrt(-(b*c - a*d)/b)*arctan(-sqrt(d*x + c)*b*sqrt(-(b*c - a*d)/b)/(b*c - a*d)) - (8*b^2*d^2*x^2 - 2*b^2*c^2 - 5*a*b*c*d + 15*a^2*d^2 - (9*b^2*c*d - 25*a*b*d^2)*x)*sqrt(d*x + c))/(b^5*x^2 + 2*a*b^4*x + a^2*b^3)]

giac [A] time = 1.24, size = 171, normalized size = 1.44

$$\frac{2\sqrt{dx+c}d^2}{b^3} + \frac{15(bcd^2 - ad^3) \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{4\sqrt{-b^2c+abd}b^3} - \frac{9(dx+c)^{\frac{3}{2}}b^2cd^2 - 7\sqrt{dx+c}b^2c^2d^2 - 9(dx+c)^{\frac{3}{2}}abd^3 + 14\sqrt{dx+c}ad^3}{4((dx+c)b - bc + ad)^2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^3,x, algorithm="giac")

[Out] 2*sqrt(d*x + c)*d^2/b^3 + 15/4*(b*c*d^2 - a*d^3)*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/(sqrt(-b^2*c + a*b*d)*b^3) - 1/4*(9*(d*x + c)^(3/2)*b^2*c*d^2 - 7*sqrt(d*x + c)*b^2*c^2*d^2 - 9*(d*x + c)^(3/2)*a*b*d^3 + 14*sqrt(d*x + c)*a*b*c*d^3 - 7*sqrt(d*x + c)*a^2*d^4)/(((d*x + c)*b - b*c + a*d)^2*b^3)

maple [B] time = 0.02, size = 238, normalized size = 2.00

$$\frac{7\sqrt{dx+c}a^2d^4}{4(bdx+ad)^2b^3} - \frac{7\sqrt{dx+c}acd^3}{2(bdx+ad)^2b^2} + \frac{7\sqrt{dx+c}c^2d^2}{4(bdx+ad)^2b} + \frac{9(dx+c)^{\frac{3}{2}}ad^3}{4(bdx+ad)^2b^2} - \frac{15ad^3 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{(ad-bc)b}}\right)}{4\sqrt{(ad-bc)b}b^3} - \frac{9(dx+c)^{\frac{3}{2}}cd^2}{4(bdx+ad)^2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^3,x)


```
[Out] 2*d^2*(d*x+c)^(1/2)/b^3+9/4*d^3/b^2/(b*d*x+a*d)^2*(d*x+c)^(3/2)*a-9/4*d^2/b
/(b*d*x+a*d)^2*(d*x+c)^(3/2)*c+7/4*d^4/b^3/(b*d*x+a*d)^2*(d*x+c)^(1/2)*a^2-
7/2*d^3/b^2/(b*d*x+a*d)^2*(d*x+c)^(1/2)*a*c+7/4*d^2/b/(b*d*x+a*d)^2*(d*x+c)
^(1/2)*c^2-15/4*d^3/b^3/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)
*b)^(1/2)*b)*a+15/4*d^2/b^2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-
b*c)*b)^(1/2)*b)*c
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(5/2)/(b*x+a)^3,x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError >> Computation failed since Maxima requested a
dditional constraints; using the 'assume' command before evaluation *may* h
elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more
details)Is a*d-b*c positive or negative?
```

mupad [B] time = 0.16, size = 199, normalized size = 1.67

$$\frac{2d^2\sqrt{c+dx}}{b^3} - \frac{\left(\frac{9b^2cd^2}{4} - \frac{9abd^3}{4}\right)(c+dx)^{3/2} - \sqrt{c+dx}\left(\frac{7a^2d^4}{4} - \frac{7abcd^3}{2} + \frac{7b^2c^2d^2}{4}\right)}{b^5(c+dx)^2 - (2b^5c - 2ab^4d)(c+dx) + b^5c^2 + a^2b^3d^2 - 2ab^4cd} - \frac{15d^2 \operatorname{atan}\left(\frac{\sqrt{b}d^2\sqrt{ad-bc}}{ad^3-bcd}\right)}{4b^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/2)/(a + b*x)^3,x)
```

```
[Out] (2*d^2*(c + d*x)^(1/2))/b^3 - (((9*b^2*c*d^2)/4 - (9*a*b*d^3)/4)*(c + d*x)^(
3/2) - (c + d*x)^(1/2)*((7*a^2*d^4)/4 + (7*b^2*c^2*d^2)/4 - (7*a*b*c*d^3)/
2))/b^5*(c + d*x)^2 - (2*b^5*c - 2*a*b^4*d)*(c + d*x) + b^5*c^2 + a^2*b^3*
d^2 - 2*a*b^4*c*d) - (15*d^2*atan((b^(1/2)*d^2*(a*d - b*c)^(1/2)*(c + d*x)^(
1/2))/(a*d^3 - b*c*d^2))*(a*d - b*c)^(1/2))/(4*b^(7/2))
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/2)/(b*x+a)**3,x)
```

```
[Out] Timed out
```

$$3.1408 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^4} dx$$

Optimal. Leaf size=126

$$-\frac{5d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8b^{7/2}\sqrt{bc-ad}} - \frac{5d^2\sqrt{c+dx}}{8b^3(a+bx)} - \frac{5d(c+dx)^{3/2}}{12b^2(a+bx)^2} - \frac{(c+dx)^{5/2}}{3b(a+bx)^3}$$

[Out] $-5/12*d*(d*x+c)^{(3/2)}/b^2/(b*x+a)^2-1/3*(d*x+c)^{(5/2)}/b/(b*x+a)^3-5/8*d^3*a$
 $rctanh(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})/b^{(7/2)}/(-a*d+b*c)^{(1/2)}-5/8$
 $*d^2*(d*x+c)^{(1/2)}/b^3/(b*x+a)$

Rubi [A] time = 0.05, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {47, 63, 208}

$$-\frac{5d^2\sqrt{c+dx}}{8b^3(a+bx)} - \frac{5d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8b^{7/2}\sqrt{bc-ad}} - \frac{5d(c+dx)^{3/2}}{12b^2(a+bx)^2} - \frac{(c+dx)^{5/2}}{3b(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^4, x]

[Out] $(-5*d^2*sqrt[c + d*x])/(8*b^3*(a + b*x)) - (5*d*(c + d*x)^{(3/2)})/(12*b^2*(a$
 $+ b*x)^2) - (c + d*x)^{(5/2)}/(3*b*(a + b*x)^3) - (5*d^3*ArcTanh[(sqrt[b]*sqrt[c + d*x])/sqrt[b*c - a*d]])/(8*b^{(7/2)}*sqrt[b*c - a*d])$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 $((a + b*x)^{(m + 1)}*(c + d*x)^n)/(b*(m + 1)), x] - \text{Dist}[(d*n)/(b*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] &&
 NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &&
 & IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
 {p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(c+dx)^{5/2}}{(a+bx)^4} dx &= -\frac{(c+dx)^{5/2}}{3b(a+bx)^3} + \frac{(5d) \int \frac{(c+dx)^{3/2}}{(a+bx)^3} dx}{6b} \\
 &= -\frac{5d(c+dx)^{3/2}}{12b^2(a+bx)^2} - \frac{(c+dx)^{5/2}}{3b(a+bx)^3} + \frac{(5d^2) \int \frac{\sqrt{c+dx}}{(a+bx)^2} dx}{8b^2} \\
 &= -\frac{5d^2\sqrt{c+dx}}{8b^3(a+bx)} - \frac{5d(c+dx)^{3/2}}{12b^2(a+bx)^2} - \frac{(c+dx)^{5/2}}{3b(a+bx)^3} + \frac{(5d^3) \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{16b^3} \\
 &= -\frac{5d^2\sqrt{c+dx}}{8b^3(a+bx)} - \frac{5d(c+dx)^{3/2}}{12b^2(a+bx)^2} - \frac{(c+dx)^{5/2}}{3b(a+bx)^3} + \frac{(5d^2) \text{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{8b^3} \\
 &= -\frac{5d^2\sqrt{c+dx}}{8b^3(a+bx)} - \frac{5d(c+dx)^{3/2}}{12b^2(a+bx)^2} - \frac{(c+dx)^{5/2}}{3b(a+bx)^3} - \frac{5d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8b^{7/2}\sqrt{bc-ad}}
 \end{aligned}$$

Mathematica [A] time = 0.15, size = 119, normalized size = 0.94

$$\frac{5d^3 \tan^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{8b^{7/2}\sqrt{ad-bc}} - \frac{\sqrt{c+dx} (15a^2d^2 + 10abd(c+4dx) + b^2(8c^2 + 26cdx + 33d^2x^2))}{24b^3(a+bx)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^4, x]

[Out] -1/24*(Sqrt[c + d*x]*(15*a^2*d^2 + 10*a*b*d*(c + 4*d*x) + b^2*(8*c^2 + 26*c*d*x + 33*d^2*x^2)))/(b^3*(a + b*x)^3) + (5*d^3*ArcTan[(Sqrt[b]*Sqrt[c + d*x])/Sqrt[-(b*c) + a*d]])/(8*b^(7/2)*Sqrt[-(b*c) + a*d])

fricas [B] time = 0.49, size = 563, normalized size = 4.47

$$\left[\frac{15(b^3d^3x^3 + 3ab^2d^3x^2 + 3a^2bd^3x + a^3d^3)\sqrt{b^2c - abd} \log\left(\frac{bdx + 2bc - ad - 2\sqrt{b^2c - abd}\sqrt{dx+c}}{bx+a}\right) - 2(8b^4c^3 + 2ab^3c^2d + 48(a^3b^5c - a^4b^4d + (b^8c - ab^7d)x^3 + 3(ab^7c - \dots)}{48(a^3b^5c - a^4b^4d + (b^8c - ab^7d)x^3 + 3(ab^7c - \dots)} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^4,x, algorithm="fricas")

[Out] [1/48*(15*(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) - 2*(8*b^4*c^3 + 2*a*b^3*c^2*d + 5*a^2*b^2*c*d^2 - 15*a^3*b*d^3 + 33*(b^4*c*d^2 - a*b^3*d^3)*x^2 + 2*(13*b^4*c^2*d + 7*a*b^3*c*d^2 - 20*a^2*b^2*d^3)*x)*sqrt(d*x + c))/(a^3*b^5*c - a^4*b^4*d + (b^8*c - a*b^7*d)*x^3 + 3*(a*b^7*c - a^2*b^6*d)*x^2 + 3*(a^2*b^6*c - a^3*b^5*d)*x), 1/24*(15*(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) - (8*b^4*c^3 + 2*a*b^3*c^2*d + 5*a^2*b^2*c*d^2 - 15*a^3*b*d^3 + 33*(b^4*c*d^2 - a*b^3*d^3)*x^2 + 2*(13*b^4*c^2*d + 7*a*b^3*c*d^2 - 20*a^2*b^2*d^3)*x)*sqrt(d*x + c))/(a^3*b^5*c - a^4*b^4*d + (b^8*c - a*b^7*d)*x^3 + 3*(a*b^7*c - a^2*b^6*d)*x^2 + 3*(a^2*b^6*c - a^3*b^5*d)*x)]

giac [A] time = 0.98, size = 161, normalized size = 1.28

$$\frac{5d^3 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{8\sqrt{-b^2c+abd}b^3} - \frac{33(dx+c)^5b^2d^3 - 40(dx+c)^3b^2cd^3 + 15\sqrt{dx+c}b^2c^2d^3 + 40(dx+c)^2abd^4 - 30\sqrt{dx+c}abd^3}{24((dx+c)b - bc + ad)^3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^4,x, algorithm="giac")

[Out] 5/8*d^3*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/(sqrt(-b^2*c + a*b*d)*b^3) - 1/24*(33*(d*x + c)^(5/2)*b^2*d^3 - 40*(d*x + c)^(3/2)*b^2*c*d^3 + 15*sqrt(d*x + c)*b^2*c^2*d^3 + 40*(d*x + c)^(3/2)*a*b*d^4 - 30*sqrt(d*x + c)*a*b*c*d^4 + 15*sqrt(d*x + c)*a^2*d^5)/(((d*x + c)*b - b*c + a*d)^3*b^3)

maple [A] time = 0.02, size = 204, normalized size = 1.62

$$-\frac{5\sqrt{dx+c}a^2d^5}{8(bdx+ad)^3b^3} + \frac{5\sqrt{dx+c}acd^4}{4(bdx+ad)^3b^2} - \frac{5\sqrt{dx+c}c^2d^3}{8(bdx+ad)^3b} - \frac{5(dx+c)^{\frac{3}{2}}ad^4}{3(bdx+ad)^3b^2} + \frac{5(dx+c)^{\frac{3}{2}}cd^3}{3(bdx+ad)^3b} - \frac{11(dx+c)^{\frac{5}{2}}d^3}{8(bdx+ad)^3b} + \frac{5d^3 \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{-b^2c+abd}}\right)}{8\sqrt{-b^2c+abd}b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^4,x)

[Out] -11/8*d^3/(b*d*x+a*d)^3/b*(d*x+c)^(5/2)-5/3*d^4/(b*d*x+a*d)^3/b^2*(d*x+c)^(3/2)*a+5/3*d^3/(b*d*x+a*d)^3/b*(d*x+c)^(3/2)*c-5/8*d^5/(b*d*x+a*d)^3/b^3*(d*x+c)^(1/2)*a^2+5/4*d^4/(b*d*x+a*d)^3/b^2*(d*x+c)^(1/2)*a*c-5/8*d^3/(b*d*x+a*d)^3/b*(d*x+c)^(1/2)*c^2+5/8*d^3/b^3/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^4,x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.36, size = 222, normalized size = 1.76

$$\frac{5d^3 \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{8b^{7/2}\sqrt{ad-bc}} - \frac{\frac{11d^3(c+dx)^{5/2}}{8b} + \frac{5d^3\sqrt{c+dx}(a^2d^2-2abcd+b^2c^2)}{8b^3} + \frac{5d^3(ad-bc)(c+dx)}{3b^2}}{(c+dx)(3a^2bd^2-6ab^2cd+3b^3c^2)+b^3(c+dx)^3-(3b^3c-3ab^2d)(c+dx)^2+a^3d^3-b^3c^3+3ab^2c^2d-3a^2b^2cd^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/2)/(a + b*x)^4,x)

[Out] $(5*d^3*\operatorname{atan}((b^{(1/2)}*(c + d*x)^{(1/2)})/(a*d - b*c)^{(1/2)}))/(8*b^{(7/2)}*(a*d - b*c)^{(1/2)}) - ((11*d^3*(c + d*x)^{(5/2)})/(8*b) + (5*d^3*(c + d*x)^{(1/2)}*(a^2*d^2 + b^2*c^2 - 2*a*b*c*d))/(8*b^3) + (5*d^3*(a*d - b*c)*(c + d*x)^{(3/2)})/(3*b^2))/((c + d*x)*(3*b^3*c^2 + 3*a^2*b*d^2 - 6*a*b^2*c*d) + b^3*(c + d*x)^3 - (3*b^3*c - 3*a*b^2*d)*(c + d*x)^2 + a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b^2*c*d^2)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/2)/(b*x+a)**4,x)

[Out] Timed out

$$3.1409 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^5} dx$$

Optimal. Leaf size=162

$$\frac{5d^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{64b^{7/2}(bc-ad)^{3/2}} - \frac{5d^3\sqrt{c+dx}}{64b^3(a+bx)(bc-ad)} - \frac{5d^2\sqrt{c+dx}}{32b^3(a+bx)^2} - \frac{5d(c+dx)^{3/2}}{24b^2(a+bx)^3} - \frac{(c+dx)^{5/2}}{4b(a+bx)^4}$$

[Out] $-5/24*d*(d*x+c)^{(3/2)}/b^2/(b*x+a)^3-1/4*(d*x+c)^{(5/2)}/b/(b*x+a)^4+5/64*d^4*\arctanh(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/b^{(7/2)/(-a*d+b*c)^{(3/2)}-5/32*d^2*(d*x+c)^{(1/2)}/b^3/(b*x+a)^2-5/64*d^3*(d*x+c)^{(1/2)}/b^3/(-a*d+b*c)/(b*x+a)$

Rubi [A] time = 0.07, antiderivative size = 162, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 51, 63, 208}

$$-\frac{5d^3\sqrt{c+dx}}{64b^3(a+bx)(bc-ad)} - \frac{5d^2\sqrt{c+dx}}{32b^3(a+bx)^2} + \frac{5d^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{64b^{7/2}(bc-ad)^{3/2}} - \frac{5d(c+dx)^{3/2}}{24b^2(a+bx)^3} - \frac{(c+dx)^{5/2}}{4b(a+bx)^4}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^5, x]

[Out] $(-5*d^2*\text{Sqrt}[c + d*x])/(32*b^3*(a + b*x)^2) - (5*d^3*\text{Sqrt}[c + d*x])/(64*b^3*(b*c - a*d)*(a + b*x)) - (5*d*(c + d*x)^{(3/2)})/(24*b^2*(a + b*x)^3) - (c + d*x)^{(5/2)}/(4*b*(a + b*x)^4) + (5*d^4*\text{ArcTanh}[(\text{Sqrt}[b]*\text{Sqrt}[c + d*x])/\text{Sqrt}[b*c - a*d]])/(64*b^{(7/2)}*(b*c - a*d)^{(3/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ

[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{(c + dx)^{5/2}}{(a + bx)^5} dx &= -\frac{(c + dx)^{5/2}}{4b(a + bx)^4} + \frac{(5d) \int \frac{(c+dx)^{3/2}}{(a+bx)^4} dx}{8b} \\
 &= -\frac{5d(c + dx)^{3/2}}{24b^2(a + bx)^3} - \frac{(c + dx)^{5/2}}{4b(a + bx)^4} + \frac{(5d^2) \int \frac{\sqrt{c+dx}}{(a+bx)^3} dx}{16b^2} \\
 &= -\frac{5d^2\sqrt{c + dx}}{32b^3(a + bx)^2} - \frac{5d(c + dx)^{3/2}}{24b^2(a + bx)^3} - \frac{(c + dx)^{5/2}}{4b(a + bx)^4} + \frac{(5d^3) \int \frac{1}{(a+bx)^2\sqrt{c+dx}} dx}{64b^3} \\
 &= -\frac{5d^2\sqrt{c + dx}}{32b^3(a + bx)^2} - \frac{5d^3\sqrt{c + dx}}{64b^3(bc - ad)(a + bx)} - \frac{5d(c + dx)^{3/2}}{24b^2(a + bx)^3} - \frac{(c + dx)^{5/2}}{4b(a + bx)^4} - \frac{(5d^4) \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{128b^3(bc - ad)} \\
 &= -\frac{5d^2\sqrt{c + dx}}{32b^3(a + bx)^2} - \frac{5d^3\sqrt{c + dx}}{64b^3(bc - ad)(a + bx)} - \frac{5d(c + dx)^{3/2}}{24b^2(a + bx)^3} - \frac{(c + dx)^{5/2}}{4b(a + bx)^4} - \frac{(5d^3) \operatorname{Subst}\left(\int \frac{1}{a} dx\right)}{64b^3} \\
 &= -\frac{5d^2\sqrt{c + dx}}{32b^3(a + bx)^2} - \frac{5d^3\sqrt{c + dx}}{64b^3(bc - ad)(a + bx)} - \frac{5d(c + dx)^{3/2}}{24b^2(a + bx)^3} - \frac{(c + dx)^{5/2}}{4b(a + bx)^4} + \frac{5d^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc}}\right)}{64b^{7/2}(bc - ad)}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.32

$$\frac{2d^4(c + dx)^{7/2} {}_2F_1\left(\frac{7}{2}, 5; \frac{9}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{7(ad - bc)^5}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^5,x]

[Out] (2*d^4*(c + d*x)^(7/2)*Hypergeometric2F1[7/2, 5, 9/2, -((b*(c + d*x))/(-(b*c) + a*d))])/(7*(-(b*c) + a*d)^5)

fricas [B] time = 0.48, size = 894, normalized size = 5.52

$$\frac{15(b^4 d^4 x^4 + 4 a b^3 d^4 x^3 + 6 a^2 b^2 d^4 x^2 + 4 a^3 b d^4 x + a^4 d^4) \sqrt{b^2 c - a b d} \log\left(\frac{b d x + 2 b c - a d - 2 \sqrt{b^2 c - a b d} \sqrt{d x + c}}{b x + a}\right) + 2(48 b^5 c^3 d - 56 a b^4 c^2 d^2 + 15 a^2 b^3 c d^3 - 5 a^3 b^2 c^2 d^4 + a^4 b c^3 d^5)}{384(a^4 b^6 c^2 - 2 a^5 b^5 c d + a^6 b^4 d^2 + (b^{10} c^2 - 2 a b^9 c d + a^2 b^8 d^2) x^4 + 4(a^3 b^7 c^2 - 2 a^2 b^6 c d + a^4 b^5 d^2) x^3 + 6(a^2 b^8 c^2 - 2 a^3 b^7 c d + a^4 b^6 d^2) x^2 + 4(a^3 b^7 c^2 - 2 a^4 b^6 c d + a^5 b^5 d^2) x), -1/192(15(b^4 d^4 x^4 + 4 a b^3 d^4 x^3 + 6 a^2 b^2 d^4 x^2 + 4 a^3 b d^4 x + a^4 d^4) \sqrt{-b^2 c + a b d} \arctan(\sqrt{-b^2 c + a b d} \sqrt{d x + c} / (b d x + b c))) + (48 b^5 c^4 - 56 a b^4 c^3 d - 2 a^2 b^3 c^2 d^2 - 5 a^3 b^2 c d^3 + 15 a^4 b d^4 + 15 (b^5 c d^3 - a b^4 d^4) x^3 + (118 b^5 c^2 d^2 - 191 a b^4 c d^3 + 73 a^2 b^3 d^4) x^2 + (136 b^5 c^3 d - 172 a b^4 c^2 d^2 - 19 a^2 b^3 c d^3 + 55 a^3 b^2 d^4) x) \sqrt{d x + c}}{(a^4 b^6 c^2 - 2 a^5 b^5 c d + a^6 b^4 d^2 + (b^{10} c^2 - 2 a b^9 c d + a^2 b^8 d^2) x^4 + 4(a^3 b^7 c^2 - 2 a^2 b^6 c d + a^4 b^5 d^2) x^3 + 6(a^2 b^8 c^2 - 2 a^3 b^7 c d + a^4 b^6 d^2) x^2 + 4(a^3 b^7 c^2 - 2 a^4 b^6 c d + a^5 b^5 d^2) x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^5,x, algorithm="fricas")

[Out] [-1/384*(15*(b^4*d^4*x^4 + 4*a*b^3*d^4*x^3 + 6*a^2*b^2*d^4*x^2 + 4*a^3*b*d^4*x + a^4*d^4)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) + 2*(48*b^5*c^4 - 56*a*b^4*c^3*d - 2*a^2*b^3*c^2*d^2 - 5*a^3*b^2*c*d^3 + 15*a^4*b*d^4 + 15*(b^5*c*d^3 - a*b^4*d^4)*x^3 + (118*b^5*c^2*d^2 - 191*a*b^4*c*d^3 + 73*a^2*b^3*d^4)*x^2 + (136*b^5*c^3*d - 172*a*b^4*c^2*d^2 - 19*a^2*b^3*c*d^3 + 55*a^3*b^2*d^4)*x)*sqrt(d*x + c))/(a^4*b^6*c^2 - 2*a^5*b^5*c*d + a^6*b^4*d^2 + (b^10*c^2 - 2*a*b^9*c*d + a^2*b^8*d^2)*x^4 + 4*(a^3*b^7*c^2 - 2*a^2*b^8*c*d + a^4*b^6*d^2)*x^3 + 6*(a^2*b^8*c^2 - 2*a^3*b^7*c*d + a^4*b^6*d^2)*x^2 + 4*(a^3*b^7*c^2 - 2*a^4*b^6*c*d + a^5*b^5*d^2)*x), -1/192*(15*(b^4*d^4*x^4 + 4*a*b^3*d^4*x^3 + 6*a^2*b^2*d^4*x^2 + 4*a^3*b*d^4*x + a^4*d^4)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) + (48*b^5*c^4 - 56*a*b^4*c^3*d - 2*a^2*b^3*c^2*d^2 - 5*a^3*b^2*c*d^3 + 15*a^4*b*d^4 + 15*(b^5*c*d^3 - a*b^4*d^4)*x^3 + (118*b^5*c^2*d^2 - 191*a*b^4*c*d^3 + 73*a^2*b^3*d^4)*x^2 + (136*b^5*c^3*d - 172*a*b^4*c^2*d^2 - 19*a^2*b^3*c*d^3 + 55*a^3*b^2*d^4)*x)*sqrt(d*x + c))/(a^4*b^6*c^2 - 2*a^5*b^5*c*d + a^6*b^4*d^2 + (b^10*c^2 - 2*a*b^9*c*d + a^2*b^8*d^2)*x^4 + 4*(a^3*b^7*c^2 - 2*a^2*b^8*c*d + a^4*b^6*d^2)*x^3 + 6*(a^2*b^8*c^2 - 2*a^3*b^7*c*d + a^4*b^6*d^2)*x^2 + 4*(a^3*b^7*c^2 - 2*a^4*b^6*c*d + a^5*b^5*d^2)*x)]

giac [A] time = 1.09, size = 259, normalized size = 1.60

$$\frac{5 d^4 \arctan\left(\frac{\sqrt{d x+c b}}{\sqrt{-b^2 c+a b d}}\right)}{64\left(b^4 c-a b^3 d\right) \sqrt{-b^2 c+a b d}}-\frac{15(d x+c)^{\frac{7}{2}} b^3 d^4+73(d x+c)^{\frac{5}{2}} b^3 c d^4-55(d x+c)^{\frac{3}{2}} b^3 c^2 d^4+15 \sqrt{d x+c} b^3 c^3 d^4}{64\left(b^4 c-a b^3 d\right) \sqrt{-b^2 c+a b d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^5,x, algorithm="giac")

[Out]
$$-5/64*d^4*\arctan(\sqrt{d*x+c}*b/\sqrt{-b^2*c+a*b*d})/((b^4*c-a*b^3*d)*\sqrt{-b^2*c+a*b*d}) - 1/192*(15*(d*x+c)^{(7/2)}*b^3*d^4 + 73*(d*x+c)^{(5/2)}*b^3*c*d^4 - 55*(d*x+c)^{(3/2)}*b^3*c^2*d^4 + 15*\sqrt{d*x+c}*b^3*c^3*d^4 - 73*(d*x+c)^{(5/2)}*a*b^2*d^5 + 110*(d*x+c)^{(3/2)}*a*b^2*c*d^5 - 45*\sqrt{d*x+c}*a*b^2*c^2*d^5 - 55*(d*x+c)^{(3/2)}*a^2*b*d^6 + 45*\sqrt{d*x+c}*a^2*b*c*d^6 - 15*\sqrt{d*x+c}*a^3*d^7)/((b^4*c-a*b^3*d)*((d*x+c)*b-b*c+a*d)^4)$$

maple [A] time = 0.02, size = 246, normalized size = 1.52

$$-\frac{5\sqrt{dx+c}a^2d^6}{64(bdx+ad)^4b^3} + \frac{5\sqrt{dx+c}acd^5}{32(bdx+ad)^4b^2} - \frac{5\sqrt{dx+c}c^2d^4}{64(bdx+ad)^4b} - \frac{55(dx+c)^{\frac{3}{2}}ad^5}{192(bdx+ad)^4b^2} + \frac{55(dx+c)^{\frac{3}{2}}cd^4}{192(bdx+ad)^4b} + \frac{5(dx+c)^{\frac{3}{2}}}{64(bdx+ad)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^5,x)

[Out]
$$\frac{5}{64}d^4/(b*d*x+a*d)^4/(a*d-b*c)*(d*x+c)^{(7/2)} - \frac{73}{192}d^4/(b*d*x+a*d)^4/b*(d*x+c)^{(5/2)} - \frac{55}{192}d^5/(b*d*x+a*d)^4/b^2*(d*x+c)^{(3/2)}*a + \frac{55}{192}d^4/(b*d*x+a*d)^4/b*(d*x+c)^{(3/2)}*c - \frac{5}{64}d^6/(b*d*x+a*d)^4/b^3*(d*x+c)^{(1/2)}*a^2 + \frac{5}{32}d^5/(b*d*x+a*d)^4/b^2*(d*x+c)^{(1/2)}*a*c - \frac{5}{64}d^4/(b*d*x+a*d)^4/b*(d*x+c)^{(1/2)}*c^2 + \frac{5}{64}d^4/(a*d-b*c)/b^3/((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^5,x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c positive or negative?

mupad [B] time = 0.41, size = 309, normalized size = 1.91

$$\frac{5d^4 \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{64b^{7/2}(ad-bc)^{3/2}} - \frac{\frac{73d^4(c+dx)^{5/2}}{192b} - \frac{5d^4(c+dx)^{7/2}}{64(ad-bc)}}{b^4(c+dx)^4 - (4b^4c - 4ab^3d)(c+dx)^3 - (c+dx)(-4a^3bd^3 + 12a^2b^2cd^2 - 12ab^3d)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/2)/(a + b*x)^5,x)
```

```
[Out] (5*d^4*atan((b^(1/2)*(c + d*x)^(1/2))/(a*d - b*c)^(1/2)))/(64*b^(7/2)*(a*d
- b*c)^(3/2)) - ((73*d^4*(c + d*x)^(5/2))/(192*b) - (5*d^4*(c + d*x)^(7/2))
/(64*(a*d - b*c)) + (5*d^4*(c + d*x)^(1/2)*(a^2*d^2 + b^2*c^2 - 2*a*b*c*d))
/(64*b^3) + (55*d^4*(a*d - b*c)*(c + d*x)^(3/2))/(192*b^2))/(b^4*(c + d*x)^
4 - (4*b^4*c - 4*a*b^3*d)*(c + d*x)^3 - (c + d*x)*(4*b^4*c^3 - 4*a^3*b*d^3
+ 12*a^2*b^2*c*d^2 - 12*a*b^3*c^2*d) + a^4*d^4 + b^4*c^4 + (c + d*x)^2*(6*b
^4*c^2 + 6*a^2*b^2*d^2 - 12*a*b^3*c*d) + 6*a^2*b^2*c^2*d^2 - 4*a*b^3*c^3*d
- 4*a^3*b*c*d^3)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/2)/(b*x+a)**5,x)
```

```
[Out] Timed out
```

$$3.1410 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^6} dx$$

Optimal. Leaf size=198

$$-\frac{3d^5 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{128b^{7/2}(bc-ad)^{5/2}} + \frac{3d^4\sqrt{c+dx}}{128b^3(a+bx)(bc-ad)^2} - \frac{d^3\sqrt{c+dx}}{64b^3(a+bx)^2(bc-ad)} - \frac{d^2\sqrt{c+dx}}{16b^3(a+bx)^3} - \frac{d(c+dx)^{3/2}}{8b^2(a+bx)^4} - \frac{(c+dx)^{5/2}}{5b(a+bx)^5}$$

[Out] $-1/8*d*(d*x+c)^{(3/2)}/b^2/(b*x+a)^4-1/5*(d*x+c)^{(5/2)}/b/(b*x+a)^5-3/128*d^5*\arctanh(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/b^{(7/2)/(-a*d+b*c)^{(5/2)}-1/16*d^2*(d*x+c)^{(1/2)}/b^3/(b*x+a)^3-1/64*d^3*(d*x+c)^{(1/2)}/b^3/(-a*d+b*c)/(b*x+a)^2+3/128*d^4*(d*x+c)^{(1/2)}/b^3/(-a*d+b*c)^2/(b*x+a)$

Rubi [A] time = 0.09, antiderivative size = 198, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {47, 51, 63, 208}

$$\frac{3d^4\sqrt{c+dx}}{128b^3(a+bx)(bc-ad)^2} - \frac{d^3\sqrt{c+dx}}{64b^3(a+bx)^2(bc-ad)} - \frac{d^2\sqrt{c+dx}}{16b^3(a+bx)^3} - \frac{3d^5 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{128b^{7/2}(bc-ad)^{5/2}} - \frac{d(c+dx)^{3/2}}{8b^2(a+bx)^4} - \frac{(c+dx)^{5/2}}{5b(a+bx)^5}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^6, x]

[Out] $-(d^2*\text{Sqrt}[c + d*x])/(16*b^3*(a + b*x)^3) - (d^3*\text{Sqrt}[c + d*x])/(64*b^3*(b*c - a*d)*(a + b*x)^2) + (3*d^4*\text{Sqrt}[c + d*x])/(128*b^3*(b*c - a*d)^2*(a + b*x)) - (d*(c + d*x)^{(3/2)})/(8*b^2*(a + b*x)^4) - (c + d*x)^{(5/2)}/(5*b*(a + b*x)^5) - (3*d^5*\text{ArcTanh}[(\text{Sqrt}[b]*\text{Sqrt}[c + d*x])/\text{Sqrt}[b*c - a*d]])/(128*b^{(7/2)}*(b*c - a*d)^{(5/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x]

```

] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]

```

Rule 63

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 208

```

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/2}}{(a+bx)^6} dx &= -\frac{(c+dx)^{5/2}}{5b(a+bx)^5} + \frac{d \int \frac{(c+dx)^{3/2}}{(a+bx)^5} dx}{2b} \\
&= -\frac{d(c+dx)^{3/2}}{8b^2(a+bx)^4} - \frac{(c+dx)^{5/2}}{5b(a+bx)^5} + \frac{(3d^2) \int \frac{\sqrt{c+dx}}{(a+bx)^4} dx}{16b^2} \\
&= -\frac{d^2\sqrt{c+dx}}{16b^3(a+bx)^3} - \frac{d(c+dx)^{3/2}}{8b^2(a+bx)^4} - \frac{(c+dx)^{5/2}}{5b(a+bx)^5} + \frac{d^3 \int \frac{1}{(a+bx)^3\sqrt{c+dx}} dx}{32b^3} \\
&= -\frac{d^2\sqrt{c+dx}}{16b^3(a+bx)^3} - \frac{d^3\sqrt{c+dx}}{64b^3(bc-ad)(a+bx)^2} - \frac{d(c+dx)^{3/2}}{8b^2(a+bx)^4} - \frac{(c+dx)^{5/2}}{5b(a+bx)^5} - \frac{(3d^4) \int \frac{1}{(a+bx)^2\sqrt{c+dx}} dx}{128b^3(bc-ad)} \\
&= -\frac{d^2\sqrt{c+dx}}{16b^3(a+bx)^3} - \frac{d^3\sqrt{c+dx}}{64b^3(bc-ad)(a+bx)^2} + \frac{3d^4\sqrt{c+dx}}{128b^3(bc-ad)^2(a+bx)} - \frac{d(c+dx)^{3/2}}{8b^2(a+bx)^4} - \frac{(c+dx)^{5/2}}{5b(a+bx)^5} \\
&= -\frac{d^2\sqrt{c+dx}}{16b^3(a+bx)^3} - \frac{d^3\sqrt{c+dx}}{64b^3(bc-ad)(a+bx)^2} + \frac{3d^4\sqrt{c+dx}}{128b^3(bc-ad)^2(a+bx)} - \frac{d(c+dx)^{3/2}}{8b^2(a+bx)^4} - \frac{(c+dx)^{5/2}}{5b(a+bx)^5} \\
&= -\frac{d^2\sqrt{c+dx}}{16b^3(a+bx)^3} - \frac{d^3\sqrt{c+dx}}{64b^3(bc-ad)(a+bx)^2} + \frac{3d^4\sqrt{c+dx}}{128b^3(bc-ad)^2(a+bx)} - \frac{d(c+dx)^{3/2}}{8b^2(a+bx)^4} - \frac{(c+dx)^{5/2}}{5b(a+bx)^5}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.26

$$\frac{2d^5(c+dx)^{7/2} {}_2F_1\left(\frac{7}{2}, 6; \frac{9}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{7(ad-bc)^6}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^6, x]

[Out] (2*d^5*(c + d*x)^(7/2)*Hypergeometric2F1[7/2, 6, 9/2, -(b*(c + d*x))/(-(b*c) + a*d)])/(7*(-(b*c) + a*d)^6)

fricas [B] time = 0.47, size = 1337, normalized size = 6.75

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^6, x, algorithm="fricas")

[Out] [1/1280*(15*(b^5*d^5*x^5 + 5*a*b^4*d^5*x^4 + 10*a^2*b^3*d^5*x^3 + 10*a^3*b^2*d^5*x^2 + 5*a^4*b*d^5*x + a^5*d^5)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) - 2*(128*b^6*c^5 - 304*a*b^5*c^4*d + 184*a^2*b^4*c^3*d^2 + 2*a^3*b^3*c^2*d^3 + 5*a^4*b^2*c*d^4 - 15*a^5*b*d^5 - 15*(b^6*c*d^4 - a*b^5*d^5)*x^4 + 10*(b^6*c^2*d^3 - 8*a*b^5*c*d^4 + 7*a^2*b^4*d^5)*x^3 + 2*(124*b^6*c^3*d^2 - 357*a*b^5*c^2*d^3 + 297*a^2*b^4*c*d^4 - 64*a^3*b^3*d^5)*x^2 + 2*(168*b^6*c^4*d - 424*a*b^5*c^3*d^2 + 279*a^2*b^4*c^2*d^3 + 12*a^3*b^3*c*d^4 - 35*a^4*b^2*d^5)*x)*sqrt(d*x + c))/(a^5*b^7*c^3 - 3*a^6*b^6*c^2*d + 3*a^7*b^5*c*d^2 - a^8*b^4*d^3 + (b^12*c^3 - 3*a*b^11*c^2*d + 3*a^2*b^10*c*d^2 - a^3*b^9*d^3)*x^5 + 5*(a*b^11*c^3 - 3*a^2*b^10*c^2*d + 3*a^3*b^9*c*d^2 - a^4*b^8*d^3)*x^4 + 10*(a^2*b^10*c^3 - 3*a^3*b^9*c^2*d + 3*a^4*b^8*c*d^2 - a^5*b^7*d^3)*x^3 + 10*(a^3*b^9*c^3 - 3*a^4*b^8*c^2*d + 3*a^5*b^7*c*d^2 - a^6*b^6*d^3)*x^2 + 5*(a^4*b^8*c^3 - 3*a^5*b^7*c^2*d + 3*a^6*b^6*c*d^2 - a^7*b^5*d^3)*x), 1/640*(15*(b^5*d^5*x^5 + 5*a*b^4*d^5*x^4 + 10*a^2*b^3*d^5*x^3 + 10*a^3*b^2*d^5*x^2 + 5*a^4*b*d^5*x + a^5*d^5)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) - (128*b^6*c^5 - 304*a*b^5*c^4*d + 184*a^2*b^4*c^3*d^2 + 2*a^3*b^3*c^2*d^3 + 5*a^4*b^2*c*d^4 - 15*a^5*b*d^5 - 15*(b^6*c*d^4 - a*b^5*d^5)*x^4 + 10*(b^6*c^2*d^3 - 8*a*b^5*c*d^4 + 7*a^2*b^4*d^5)*x^3 + 2*(124*b^6*c^3*d^2 - 357*a*b^5*c^2*d^3 + 297*a^2*b^4*c*d^4 - 64*a^3*b^3*d^5)*x^2 + 2*(168*b^6*c^4*d - 424*a*b^5*c^3*d^2 + 279*a^2*b^4*c^2*d^3 + 12*a^3*b^3*c*d^4 - 35*a^4*b^2*d^5)*x)*sqrt(d*x + c))/(a^5*b^7*c^3 - 3*a^6*b^6*c^2*d + 3*a^7*b^5*c*d^2 - a^8*b^4*d^3 + (b^12*c^3 - 3*a*b^11*c^2*d + 3*a^2*b^10*c*d^2 - a^3*b^9*d^3)*x^5 + 5*(a*b^11*c^3 - 3*a^2*b^10*c^2*d + 3*a^3*b^9*c*d^2 - a^4*b^8*d^3)*x^4 + 10*(a^2*b^10*c^3 - 3*a^3*b^9*c^2*d + 3*a^4*b^8*c*d^2 - a^5*b^7*d^3)*x^3 + 10*(a^3*b^9*c^3 - 3*a^4*b^8*c^2*d + 3*a^5*b^7*c*d^2 - a^6*b^6*d^3)*x^2 + 5*(a^4*b^8*c^3 - 3*a^5*b^7*c^2*d + 3*a^6*b^6*c*d^2 - a^7*b^5*d^3)*x)

$d^3)x^3 + 10*(a^3*b^9*c^3 - 3*a^4*b^8*c^2*d + 3*a^5*b^7*c*d^2 - a^6*b^6*d^3)*x^2 + 5*(a^4*b^8*c^3 - 3*a^5*b^7*c^2*d + 3*a^6*b^6*c*d^2 - a^7*b^5*d^3)*x]$

giac [B] time = 1.25, size = 380, normalized size = 1.92

$$\frac{3d^5 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{128(b^5c^2 - 2ab^4cd + a^2b^3d^2)\sqrt{-b^2c+abd}} + \frac{15(dx+c)^{\frac{9}{2}}b^4d^5 - 70(dx+c)^{\frac{7}{2}}b^4cd^5 - 128(dx+c)^{\frac{5}{2}}b^4c^2d^5 + 70(dx+c)^{\frac{3}{2}}b^4c^3d^5 - 15\sqrt{dx+c}b^4c^4d^5 + 70(dx+c)^{\frac{7}{2}}a*b^3*d^6 + 256(dx+c)^{\frac{5}{2}}a*b^3*c*d^6 - 210(dx+c)^{\frac{3}{2}}a*b^3*c^2*d^6 + 60\sqrt{dx+c}a*b^3*c^3*d^6 - 128(dx+c)^{\frac{5}{2}}a^2*b^2*d^7 + 210(dx+c)^{\frac{3}{2}}a^2*b^2*c*d^7 - 90\sqrt{dx+c}a^2*b^2*c^2*d^7 - 70(dx+c)^{\frac{3}{2}}a^3*b*d^8 + 60\sqrt{dx+c}a^3*b*c*d^8 - 15\sqrt{dx+c}a^4*d^9}{128(b^5c^2 - 2ab^4cd + a^2b^3d^2)*((dx+c)*b - b*c + a*d)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^6,x, algorithm="giac")

[Out] $\frac{3}{128}d^5 \arctan\left(\frac{\sqrt{dx+c}b/\sqrt{-b^2c+abd}}{(b^5c^2 - 2ab^4cd + a^2b^3d^2)\sqrt{-b^2c+abd}}\right) + \frac{1}{640}(15(dx+c)^{\frac{9}{2}}b^4d^5 - 70(dx+c)^{\frac{7}{2}}b^4cd^5 - 128(dx+c)^{\frac{5}{2}}b^4c^2d^5 + 70(dx+c)^{\frac{3}{2}}b^4c^3d^5 - 15\sqrt{dx+c}b^4c^4d^5 + 70(dx+c)^{\frac{7}{2}}a*b^3*d^6 + 256(dx+c)^{\frac{5}{2}}a*b^3*c*d^6 - 210(dx+c)^{\frac{3}{2}}a*b^3*c^2*d^6 + 60\sqrt{dx+c}a*b^3*c^3*d^6 - 128(dx+c)^{\frac{5}{2}}a^2*b^2*d^7 + 210(dx+c)^{\frac{3}{2}}a^2*b^2*c*d^7 - 90\sqrt{dx+c}a^2*b^2*c^2*d^7 - 70(dx+c)^{\frac{3}{2}}a^3*b*d^8 + 60\sqrt{dx+c}a^3*b*c*d^8 - 15\sqrt{dx+c}a^4*d^9) / ((b^5c^2 - 2ab^4cd + a^2b^3d^2)*((dx+c)*b - b*c + a*d)^5)$

maple [A] time = 0.02, size = 305, normalized size = 1.54

$$-\frac{3\sqrt{dx+c}a^2d^7}{128(bdx+ad)^5b^3} + \frac{3\sqrt{dx+c}acd^6}{64(bdx+ad)^5b^2} + \frac{3(dx+c)^{\frac{9}{2}}bd^5}{128(bdx+ad)^5(a^2d^2 - 2abcd + b^2c^2)} - \frac{3\sqrt{dx+c}c^2d^5}{128(bdx+ad)^5b} - \frac{7(dx+c)^{\frac{3}{2}}}{64(bdx+ad)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^6,x)

[Out] $\frac{3}{128}d^5/(b*d*x+a*d)^5*b/(a^2*d^2-2*a*b*c*d+b^2*c^2)*(d*x+c)^{\frac{9}{2}}+7/64*d^5/(b*d*x+a*d)^5/(a*d-b*c)*(d*x+c)^{\frac{7}{2}}-1/5*d^5/(b*d*x+a*d)^5/b*(d*x+c)^{\frac{5}{2}}-7/64*d^6/(b*d*x+a*d)^5/b^2*(d*x+c)^{\frac{3}{2}}*a+7/64*d^5/(b*d*x+a*d)^5/b*(d*x+c)^{\frac{3}{2}}*c-3/128*d^7/(b*d*x+a*d)^5/b^3*(d*x+c)^{\frac{1}{2}}*a^2+3/64*d^6/(b*d*x+a*d)^5/b^2*(d*x+c)^{\frac{1}{2}}*a*c-3/128*d^5/(b*d*x+a*d)^5/b*(d*x+c)^{\frac{1}{2}}*c^2+3/128*d^5/b^3/(a^2*d^2-2*a*b*c*d+b^2*c^2)/((a*d-b*c)*b)^{\frac{1}{2}}*\arctan((d*x+c)^{\frac{1}{2}}/((a*d-b*c)*b)^{\frac{1}{2}}*b)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^6,x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.50, size = 411, normalized size = 2.08

$$\frac{3 d^5 \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{128 b^{7/2} (ad-bc)^{5/2} b^5 (c+dx)^5 - (c+dx)^2 \left(-10 a^3 b^2 d^3 + 30 a^2 b^3 c d^2 - 30 a b^4 c^2 d + 10 b^5 c^3\right) - \left(5 b^5 c - \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/2)/(a + b*x)^6,x)

[Out] (3*d^5*atan((b^(1/2)*(c + d*x)^(1/2))/(a*d - b*c)^(1/2)))/(128*b^(7/2)*(a*d - b*c)^(5/2)) - ((d^5*(c + d*x)^(5/2))/(5*b) - (7*d^5*(c + d*x)^(7/2))/(64*(a*d - b*c)) + (3*d^5*(c + d*x)^(1/2)*(a^2*d^2 + b^2*c^2 - 2*a*b*c*d))/(128*b^3) + (7*d^5*(a*d - b*c)*(c + d*x)^(3/2))/(64*b^2) - (3*b*d^5*(c + d*x)^(9/2))/(128*(a*d - b*c)^2)/(b^5*(c + d*x)^5 - (c + d*x)^2*(10*b^5*c^3 - 10*a^3*b^2*d^3 + 30*a^2*b^3*c*d^2 - 30*a*b^4*c^2*d) - (5*b^5*c - 5*a*b^4*d)*(c + d*x)^4 + a^5*d^5 - b^5*c^5 + (c + d*x)^3*(10*b^5*c^2 + 10*a^2*b^3*d^2 - 20*a*b^4*c*d) + (c + d*x)*(5*b^5*c^4 + 5*a^4*b*d^4 - 20*a^3*b^2*c*d^3 + 30*a^2*b^3*c^2*d^2 - 20*a*b^4*c^3*d) - 10*a^2*b^3*c^3*d^2 + 10*a^3*b^2*c^2*d^3 + 5*a*b^4*c^4*d - 5*a^4*b*c*d^4)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/2)/(b*x+a)**6,x)

[Out] Timed out

$$3.1411 \quad \int \frac{\sqrt{-1+x}}{(1+x)^2} dx$$

Optimal. Leaf size=35

$$\frac{\tan^{-1}\left(\frac{\sqrt{x-1}}{\sqrt{2}}\right)}{\sqrt{2}} - \frac{\sqrt{x-1}}{x+1}$$

[Out] 1/2*arctan(1/2*(-1+x)^(1/2)*2^(1/2))*2^(1/2)-(-1+x)^(1/2)/(1+x)

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {47, 63, 203}

$$\frac{\tan^{-1}\left(\frac{\sqrt{x-1}}{\sqrt{2}}\right)}{\sqrt{2}} - \frac{\sqrt{x-1}}{x+1}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[-1 + x]/(1 + x)^2, x]

[Out] -(Sqrt[-1 + x]/(1 + x)) + ArcTan[Sqrt[-1 + x]/Sqrt[2]]/Sqrt[2]

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
```


, 0] || GtQ[b, 0])

Rubi steps

$$\begin{aligned}\int \frac{\sqrt{-1+x}}{(1+x)^2} dx &= -\frac{\sqrt{-1+x}}{1+x} + \frac{1}{2} \int \frac{1}{\sqrt{-1+x}(1+x)} dx \\ &= -\frac{\sqrt{-1+x}}{1+x} + \text{Subst}\left(\int \frac{1}{2+x^2} dx, x, \sqrt{-1+x}\right) \\ &= -\frac{\sqrt{-1+x}}{1+x} + \frac{\tan^{-1}\left(\frac{\sqrt{-1+x}}{\sqrt{2}}\right)}{\sqrt{2}}\end{aligned}$$

Mathematica [A] time = 0.03, size = 51, normalized size = 1.46

$$\frac{-2x - \sqrt{2-2x}(x+1) \tanh^{-1}\left(\frac{\sqrt{1-x}}{\sqrt{2}}\right) + 2}{2\sqrt{x-1}(x+1)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[-1 + x]/(1 + x)^2, x]

[Out] (2 - 2*x - Sqrt[2 - 2*x]*(1 + x)*ArcTanh[Sqrt[1 - x]/Sqrt[2]])/(2*Sqrt[-1 + x]*(1 + x))

fricas [A] time = 0.44, size = 33, normalized size = 0.94

$$\frac{\sqrt{2}(x+1) \arctan\left(\frac{1}{2}\sqrt{2}\sqrt{x-1}\right) - 2\sqrt{x-1}}{2(x+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-1+x)^(1/2)/(1+x)^2, x, algorithm="fricas")

[Out] 1/2*(sqrt(2)*(x + 1)*arctan(1/2*sqrt(2)*sqrt(x - 1)) - 2*sqrt(x - 1))/(x + 1)

giac [A] time = 0.96, size = 29, normalized size = 0.83

$$\frac{1}{2}\sqrt{2} \arctan\left(\frac{1}{2}\sqrt{2}\sqrt{x-1}\right) - \frac{\sqrt{x-1}}{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-1+x)^(1/2)/(1+x)^2,x, algorithm="giac")

[Out] 1/2*sqrt(2)*arctan(1/2*sqrt(2)*sqrt(x - 1)) - sqrt(x - 1)/(x + 1)

maple [A] time = 0.01, size = 30, normalized size = 0.86

$$\frac{\sqrt{2} \arctan\left(\frac{\sqrt{x-1} \sqrt{2}}{2}\right)}{2} - \frac{\sqrt{x-1}}{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x-1)^(1/2)/(x+1)^2,x)

[Out] 1/2*arctan(1/2*(x-1)^(1/2)*2^(1/2))*2^(1/2)-(x-1)^(1/2)/(x+1)

maxima [A] time = 2.97, size = 29, normalized size = 0.83

$$\frac{1}{2} \sqrt{2} \arctan\left(\frac{1}{2} \sqrt{2} \sqrt{x-1}\right) - \frac{\sqrt{x-1}}{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-1+x)^(1/2)/(1+x)^2,x, algorithm="maxima")

[Out] 1/2*sqrt(2)*arctan(1/2*sqrt(2)*sqrt(x - 1)) - sqrt(x - 1)/(x + 1)

mupad [B] time = 0.06, size = 29, normalized size = 0.83

$$\frac{\sqrt{2} \operatorname{atan}\left(\frac{\sqrt{2} \sqrt{x-1}}{2}\right)}{2} - \frac{\sqrt{x-1}}{x+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x - 1)^(1/2)/(x + 1)^2,x)

[Out] (2^(1/2)*atan((2^(1/2)*(x - 1)^(1/2))/2))/2 - (x - 1)^(1/2)/(x + 1)

sympy [A] time = 1.50, size = 104, normalized size = 2.97

$$\left\{ \begin{array}{l} \frac{\sqrt{2} i \operatorname{acosh}\left(\frac{\sqrt{2}}{\sqrt{x+1}}\right)}{2} + \frac{i}{\sqrt{-1+\frac{2}{x+1}} \sqrt{x+1}} - \frac{2i}{\sqrt{-1+\frac{2}{x+1}} (x+1)^{\frac{3}{2}}} \quad \text{for } \frac{2}{|x+1}| > 1 \\ -\frac{\sqrt{1-\frac{2}{x+1}}}{\sqrt{x+1}} - \frac{\sqrt{2} \operatorname{asin}\left(\frac{\sqrt{2}}{\sqrt{x+1}}\right)}{2} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((-1+x)**(1/2)/(1+x)**2,x)
```

```
[Out] Piecewise((sqrt(2)*I*acosh(sqrt(2)/sqrt(x + 1))/2 + I/(sqrt(-1 + 2/(x + 1))  
*sqrt(x + 1)) - 2*I/(sqrt(-1 + 2/(x + 1))*(x + 1)**(3/2)), 2/Abs(x + 1) > 1  
) , (-sqrt(1 - 2/(x + 1))/sqrt(x + 1) - sqrt(2)*asin(sqrt(2)/sqrt(x + 1))/2,  
True))
```

$$3.1412 \quad \int \frac{\sqrt{-1+x}}{(1+x)^3} dx$$

Optimal. Leaf size=56

$$\frac{\sqrt{x-1}}{8(x+1)} - \frac{\sqrt{x-1}}{2(x+1)^2} + \frac{\tan^{-1}\left(\frac{\sqrt{x-1}}{\sqrt{2}}\right)}{8\sqrt{2}}$$

[Out] 1/16*arctan(1/2*(-1+x)^(1/2)*2^(1/2))*2^(1/2)-1/2*(-1+x)^(1/2)/(1+x)^2+1/8*(-1+x)^(1/2)/(1+x)

Rubi [A] time = 0.01, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {47, 51, 63, 203}

$$\frac{\sqrt{x-1}}{8(x+1)} - \frac{\sqrt{x-1}}{2(x+1)^2} + \frac{\tan^{-1}\left(\frac{\sqrt{x-1}}{\sqrt{2}}\right)}{8\sqrt{2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[-1 + x]/(1 + x)^3, x]

[Out] -Sqrt[-1 + x]/(2*(1 + x)^2) + Sqrt[-1 + x]/(8*(1 + x)) + ArcTan[Sqrt[-1 + x]/Sqrt[2]]/(8*Sqrt[2])

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 203

```
Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt
[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a
, 0] || GtQ[b, 0])
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{-1+x}}{(1+x)^3} dx &= -\frac{\sqrt{-1+x}}{2(1+x)^2} + \frac{1}{4} \int \frac{1}{\sqrt{-1+x}(1+x)^2} dx \\
&= -\frac{\sqrt{-1+x}}{2(1+x)^2} + \frac{\sqrt{-1+x}}{8(1+x)} + \frac{1}{16} \int \frac{1}{\sqrt{-1+x}(1+x)} dx \\
&= -\frac{\sqrt{-1+x}}{2(1+x)^2} + \frac{\sqrt{-1+x}}{8(1+x)} + \frac{1}{8} \text{Subst}\left(\int \frac{1}{2+x^2} dx, x, \sqrt{-1+x}\right) \\
&= -\frac{\sqrt{-1+x}}{2(1+x)^2} + \frac{\sqrt{-1+x}}{8(1+x)} + \frac{\tan^{-1}\left(\frac{\sqrt{-1+x}}{\sqrt{2}}\right)}{8\sqrt{2}}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 28, normalized size = 0.50

$$\frac{1}{12}(x-1)^{3/2} {}_2F_1\left(\frac{3}{2}, 3; \frac{5}{2}; \frac{1-x}{2}\right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[-1 + x]/(1 + x)^3, x]

[Out] ((-1 + x)^(3/2)*Hypergeometric2F1[3/2, 3, 5/2, (1 - x)/2])/12

fricas [A] time = 0.47, size = 46, normalized size = 0.82

$$\frac{\sqrt{2}(x^2 + 2x + 1) \arctan\left(\frac{1}{2}\sqrt{2}\sqrt{x-1}\right) + 2\sqrt{x-1}(x-3)}{16(x^2 + 2x + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-1+x)^(1/2)/(1+x)^3,x, algorithm="fricas")

[Out] 1/16*(sqrt(2)*(x^2 + 2*x + 1)*arctan(1/2*sqrt(2)*sqrt(x - 1)) + 2*sqrt(x - 1)*(x - 3))/(x^2 + 2*x + 1)

giac [A] time = 1.04, size = 37, normalized size = 0.66

$$\frac{1}{16} \sqrt{2} \arctan\left(\frac{1}{2} \sqrt{2} \sqrt{x-1}\right) + \frac{(x-1)^{\frac{3}{2}} - 2\sqrt{x-1}}{8(x+1)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-1+x)^(1/2)/(1+x)^3,x, algorithm="giac")

[Out] 1/16*sqrt(2)*arctan(1/2*sqrt(2)*sqrt(x - 1)) + 1/8*((x - 1)^(3/2) - 2*sqrt(x - 1))/(x + 1)^2

maple [A] time = 0.01, size = 40, normalized size = 0.71

$$\frac{\sqrt{2} \arctan\left(\frac{\sqrt{x-1} \sqrt{2}}{2}\right)}{16} + \frac{\frac{(x-1)^{\frac{3}{2}}}{8} - \frac{\sqrt{x-1}}{4}}{(x+1)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x-1)^(1/2)/(x+1)^3,x)

[Out] 2*(1/16*(x-1)^(3/2)-1/8*(x-1)^(1/2))/(x+1)^2+1/16*2^(1/2)*arctan(1/2*(x-1)^(1/2)*2^(1/2))

maxima [A] time = 3.03, size = 43, normalized size = 0.77

$$\frac{1}{16} \sqrt{2} \arctan\left(\frac{1}{2} \sqrt{2} \sqrt{x-1}\right) + \frac{(x-1)^{\frac{3}{2}} - 2\sqrt{x-1}}{8((x-1)^2 + 4x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-1+x)^(1/2)/(1+x)^3,x, algorithm="maxima")

[Out] 1/16*sqrt(2)*arctan(1/2*sqrt(2)*sqrt(x - 1)) + 1/8*((x - 1)^(3/2) - 2*sqrt(x - 1))/((x - 1)^2 + 4*x)

mupad [B] time = 0.04, size = 45, normalized size = 0.80

$$\frac{\sqrt{2} \operatorname{atan}\left(\frac{\sqrt{2} \sqrt{x-1}}{2}\right)}{16} - \frac{\frac{\sqrt{x-1}}{4} - \frac{(x-1)^{3/2}}{8}}{4x + (x-1)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x - 1)^(1/2)/(x + 1)^3,x)`

[Out] $(2^{1/2} \operatorname{atan}((2^{1/2} (x - 1)^{1/2})/2))/16 - ((x - 1)^{1/2}/4 - (x - 1)^{3/2}/8)/(4x + (x - 1)^2)$

sympy [A] time = 2.61, size = 167, normalized size = 2.98

$$\left\{ \begin{array}{l} \frac{\sqrt{2} i \operatorname{acosh}\left(\frac{\sqrt{2}}{\sqrt{x+1}}\right)}{16} - \frac{i}{8\sqrt{-1+\frac{2}{x+1}}\sqrt{x+1}} + \frac{3i}{4\sqrt{-1+\frac{2}{x+1}}(x+1)^{\frac{3}{2}}} - \frac{i}{\sqrt{-1+\frac{2}{x+1}}(x+1)^{\frac{5}{2}}} \quad \text{for } \frac{2}{|x+1|} > 1 \\ -\frac{\sqrt{2} \operatorname{asin}\left(\frac{\sqrt{2}}{\sqrt{x+1}}\right)}{16} + \frac{1}{8\sqrt{1-\frac{2}{x+1}}\sqrt{x+1}} - \frac{3}{4\sqrt{1-\frac{2}{x+1}}(x+1)^{\frac{3}{2}}} + \frac{1}{\sqrt{1-\frac{2}{x+1}}(x+1)^{\frac{5}{2}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-1+x)**(1/2)/(1+x)**3,x)`

[Out] `Piecewise((sqrt(2)*I*acosh(sqrt(2)/sqrt(x + 1))/16 - I/(8*sqrt(-1 + 2/(x + 1))*sqrt(x + 1)) + 3*I/(4*sqrt(-1 + 2/(x + 1))*(x + 1)**(3/2)) - I/(sqrt(-1 + 2/(x + 1))*(x + 1)**(5/2))), 2/Abs(x + 1) > 1, (-sqrt(2)*asin(sqrt(2)/sqrt(x + 1))/16 + 1/(8*sqrt(1 - 2/(x + 1))*sqrt(x + 1)) - 3/(4*sqrt(1 - 2/(x + 1))*(x + 1)**(3/2)) + 1/(sqrt(1 - 2/(x + 1))*(x + 1)**(5/2))), True))`

$$3.1413 \quad \int \frac{(a+bx)^5}{\sqrt{c+dx}} dx$$

Optimal. Leaf size=154

$$-\frac{10b^4(c+dx)^{9/2}(bc-ad)}{9d^6} + \frac{20b^3(c+dx)^{7/2}(bc-ad)^2}{7d^6} - \frac{4b^2(c+dx)^{5/2}(bc-ad)^3}{d^6} + \frac{10b(c+dx)^{3/2}(bc-ad)^4}{3d^6} - \frac{2\sqrt{c+dx}}{d^6}$$

[Out] $10/3*b*(-a*d+b*c)^4*(d*x+c)^(3/2)/d^6-4*b^2*(-a*d+b*c)^3*(d*x+c)^(5/2)/d^6+20/7*b^3*(-a*d+b*c)^2*(d*x+c)^(7/2)/d^6-10/9*b^4*(-a*d+b*c)*(d*x+c)^(9/2)/d^6+2/11*b^5*(d*x+c)^(11/2)/d^6-2*(-a*d+b*c)^5*(d*x+c)^(1/2)/d^6$

Rubi [A] time = 0.05, antiderivative size = 154, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{10b^4(c+dx)^{9/2}(bc-ad)}{9d^6} + \frac{20b^3(c+dx)^{7/2}(bc-ad)^2}{7d^6} - \frac{4b^2(c+dx)^{5/2}(bc-ad)^3}{d^6} + \frac{10b(c+dx)^{3/2}(bc-ad)^4}{3d^6} - \frac{2\sqrt{c+dx}}{d^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/Sqrt[c + d*x], x]

[Out] $(-2*(b*c - a*d)^5*\text{Sqrt}[c + d*x])/d^6 + (10*b*(b*c - a*d)^4*(c + d*x)^(3/2))/(3*d^6) - (4*b^2*(b*c - a*d)^3*(c + d*x)^(5/2))/d^6 + (20*b^3*(b*c - a*d)^2*(c + d*x)^(7/2))/(7*d^6) - (10*b^4*(b*c - a*d)*(c + d*x)^(9/2))/(9*d^6) + (2*b^5*(c + d*x)^(11/2))/(11*d^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{\sqrt{c+dx}} dx &= \int \left(\frac{(-bc+ad)^5}{d^5\sqrt{c+dx}} + \frac{5b(bc-ad)^4\sqrt{c+dx}}{d^5} - \frac{10b^2(bc-ad)^3(c+dx)^{3/2}}{d^5} + \frac{10b^3(bc-ad)^2(c+dx)^{5/2}}{d^5} \right. \\ &= -\frac{2(bc-ad)^5\sqrt{c+dx}}{d^6} + \frac{10b(bc-ad)^4(c+dx)^{3/2}}{3d^6} - \frac{4b^2(bc-ad)^3(c+dx)^{5/2}}{d^6} + \frac{20b^3(bc-ad)^2(c+dx)^{7/2}}{7d^6} \end{aligned}$$

Mathematica [A] time = 0.09, size = 123, normalized size = 0.80

$$\frac{2\sqrt{c+dx} \left(-385b^4(c+dx)^4(bc-ad) + 990b^3(c+dx)^3(bc-ad)^2 - 1386b^2(c+dx)^2(bc-ad)^3 + 1155b(c+dx)(bc-ad)^4 \right)}{693d^6}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/Sqrt[c + d*x], x]

[Out] (2*Sqrt[c + d*x]*(-693*(b*c - a*d)^5 + 1155*b*(b*c - a*d)^4*(c + d*x) - 1386*b^2*(b*c - a*d)^3*(c + d*x)^2 + 990*b^3*(b*c - a*d)^2*(c + d*x)^3 - 385*b^4*(b*c - a*d)*(c + d*x)^4 + 63*b^5*(c + d*x)^5)/(693*d^6)

fricas [A] time = 0.45, size = 261, normalized size = 1.69

$$\frac{2 \left(63 b^5 d^5 x^5 - 256 b^5 c^5 + 1408 a b^4 c^4 d - 3168 a^2 b^3 c^3 d^2 + 3696 a^3 b^2 c^2 d^3 - 2310 a^4 b c d^4 + 693 a^5 d^5 - 35 \left(2 b^5 c d^4 \right) \right)}{693 d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] 2/693*(63*b^5*d^5*x^5 - 256*b^5*c^5 + 1408*a*b^4*c^4*d - 3168*a^2*b^3*c^3*d^2 + 3696*a^3*b^2*c^2*d^3 - 2310*a^4*b*c*d^4 + 693*a^5*d^5 - 35*(2*b^5*c*d^4 - 11*a*b^4*d^5)*x^4 + 10*(8*b^5*c^2*d^3 - 44*a*b^4*c*d^4 + 99*a^2*b^3*d^5)*x^3 - 6*(16*b^5*c^3*d^2 - 88*a*b^4*c^2*d^3 + 198*a^2*b^3*c*d^4 - 231*a^3*b^2*d^5)*x^2 + (128*b^5*c^4*d - 704*a*b^4*c^3*d^2 + 1584*a^2*b^3*c^2*d^3 - 1848*a^3*b^2*c*d^4 + 1155*a^4*b*d^5)*x)*sqrt(d*x + c)/d^6

giac [B] time = 1.07, size = 283, normalized size = 1.84

$$2 \left(693 \sqrt{dx + c} a^5 + \frac{1155 \left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} c \right) a^4 b}{d} + \frac{462 \left(3 (dx+c)^{\frac{5}{2}} - 10 (dx+c)^{\frac{3}{2}} c + 15 \sqrt{dx+c} c^2 \right) a^3 b^2}{d^2} + \frac{198 \left(5 (dx+c)^{\frac{7}{2}} - 21 (dx+c)^{\frac{5}{2}} c + 35 \sqrt{dx+c} c^2 \right) a^2 b^3}{d^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^(1/2), x, algorithm="giac")

[Out] 2/693*(693*sqrt(d*x + c)*a^5 + 1155*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a^4*b/d + 462*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a^3*b^2/d^2 + 198*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*a^2*b^3/d^3 + 11*(35*(d*x + c)^(9/2) - 180*(d*x + c)^(7/2)*c + 378*(d*x + c)^(5/2)*c^2 - 420*(d*x + c)^(3/2)*c^3 + 315*sqrt(d*x + c)*c^4)*a*b^4/d^4 + (63*(d*x + c)^(11/2) - 385*(d*x + c)^(9/2)*c + 1155*(d*x + c)^(7/2)*c^2 - 1386*(d*x + c)^(5/2)*c^3 + 990*(d*x + c)^(3/2)*c^4 - 385*(d*x + c)*c^5)*sqrt(d*x + c)/d^6

$$(9/2)*c + 990*(d*x + c)^{(7/2)}*c^2 - 1386*(d*x + c)^{(5/2)}*c^3 + 1155*(d*x + c)^{(3/2)}*c^4 - 693*\sqrt{d*x + c}*c^5)*b^5/d^5)/d$$

maple [B] time = 0.01, size = 273, normalized size = 1.77

$$2\sqrt{dx+c} \left(63b^5x^5d^5 + 385ab^4d^5x^4 - 70b^5cd^4x^4 + 990a^2b^3d^5x^3 - 440ab^4cd^4x^3 + 80b^5c^2d^3x^3 + 1386a^3b^2d^5x^2 - \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^5/(d*x+c)^(1/2), x)`

[Out] $2/693*(d*x+c)^{(1/2)}*(63*b^5*d^5*x^5+385*a*b^4*d^5*x^4-70*b^5*c*d^4*x^4+990*a^2*b^3*d^5*x^3-440*a*b^4*c*d^4*x^3+80*b^5*c^2*d^3*x^3+1386*a^3*b^2*d^5*x^2-1188*a^2*b^3*c*d^4*x^2+528*a*b^4*c^2*d^3*x^2-96*b^5*c^3*d^2*x^2+1155*a^4*b*d^5*x-1848*a^3*b^2*c*d^4*x+1584*a^2*b^3*c^2*d^3*x-704*a*b^4*c^3*d^2*x+128*b^5*c^4*d*x+693*a^5*d^5-2310*a^4*b*c*d^4+3696*a^3*b^2*c^2*d^3-3168*a^2*b^3*c^3*d^2+1408*a*b^4*c^4*d-256*b^5*c^5)/d^6$

maxima [B] time = 1.38, size = 283, normalized size = 1.84

$$2 \left(693 \sqrt{dx+c} a^5 + \frac{1155 \left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} \right) a^4 b}{d} + \frac{462 \left(3 (dx+c)^{\frac{5}{2}} - 10 (dx+c)^{\frac{3}{2}} c + 15 \sqrt{dx+c} c^2 \right) a^3 b^2}{d^2} + \frac{198 \left(5 (dx+c)^{\frac{7}{2}} - 21 (dx+c)^{\frac{5}{2}} c + 35 (dx+c)^{\frac{3}{2}} c^2 - 35 \sqrt{dx+c} c^3 \right) a^2 b^3}{d^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5/(d*x+c)^(1/2), x, algorithm="maxima")`

[Out] $2/693*(693*\sqrt{d*x+c}*a^5 + 1155*((d*x+c)^{(3/2)} - 3*\sqrt{d*x+c})*c)*a^4*b/d + 462*(3*(d*x+c)^{(5/2)} - 10*(d*x+c)^{(3/2)}*c + 15*\sqrt{d*x+c})*c^2*a^3*b^2/d^2 + 198*(5*(d*x+c)^{(7/2)} - 21*(d*x+c)^{(5/2)}*c + 35*(d*x+c)^{(3/2)}*c^2 - 35*\sqrt{d*x+c})*c^3*a^2*b^3/d^3 + 11*(35*(d*x+c)^{(9/2)} - 180*(d*x+c)^{(7/2)}*c + 378*(d*x+c)^{(5/2)}*c^2 - 420*(d*x+c)^{(3/2)}*c^3 + 315*\sqrt{d*x+c})*c^4*a*b^4/d^4 + (63*(d*x+c)^{(11/2)} - 385*(d*x+c)^{(9/2)}*c + 990*(d*x+c)^{(7/2)}*c^2 - 1386*(d*x+c)^{(5/2)}*c^3 + 1155*(d*x+c)^{(3/2)}*c^4 - 693*\sqrt{d*x+c})*c^5)*b^5/d^5)/d$

mupad [B] time = 0.07, size = 137, normalized size = 0.89

$$\frac{2b^5(c+dx)^{11/2}}{11d^6} - \frac{(10b^5c - 10ab^4d)(c+dx)^{9/2}}{9d^6} + \frac{2(ad-bc)^5\sqrt{c+dx}}{d^6} + \frac{4b^2(ad-bc)^3(c+dx)^{5/2}}{d^6} + \frac{20b^3(ad-bc)^2(c+dx)^{3/2}}{d^6} + \frac{20b^4c(c+dx)^{1/2}}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(c + d*x)^(1/2),x)`

[Out] $(2*b^5*(c + d*x)^(11/2))/(11*d^6) - ((10*b^5*c - 10*a*b^4*d)*(c + d*x)^(9/2))/(9*d^6) + (2*(a*d - b*c)^5*(c + d*x)^(1/2))/d^6 + (4*b^2*(a*d - b*c)^3*(c + d*x)^(5/2))/d^6 + (20*b^3*(a*d - b*c)^2*(c + d*x)^(7/2))/(7*d^6) + (10*b*(a*d - b*c)^4*(c + d*x)^(3/2))/(3*d^6)$

sympy [A] time = 79.91, size = 728, normalized size = 4.73

$$\left\{ \begin{array}{l} \frac{-\frac{2a^5c}{\sqrt{c+dx}} - 2a^5\left(-\frac{c}{\sqrt{c+dx}} - \sqrt{c+dx}\right) - \frac{10a^4bc\left(-\frac{c}{\sqrt{c+dx}} - \sqrt{c+dx}\right)}{d} - \frac{10a^4b\left(\frac{c^2}{\sqrt{c+dx}} + 2c\sqrt{c+dx} - \frac{(c+dx)^{\frac{3}{2}}}{3}\right)}{d} - \frac{20a^3b^2c\left(\frac{c^2}{\sqrt{c+dx}} + 2c\sqrt{c+dx} - \frac{(c+dx)^{\frac{3}{2}}}{3}\right)}{d^2} - \frac{20a^3b^2\left(-\frac{c^3}{\sqrt{c+dx}}\right)}{d^2}}{\sqrt{c}} \\ \left\{ \begin{array}{ll} a^5x & \text{for } b = 0 \\ \frac{(a+bx)^6}{6b} & \text{otherwise} \end{array} \right. \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(d*x+c)**(1/2),x)`

[Out] `Piecewise(((-2*a**5*c/sqrt(c + d*x) - 2*a**5*(-c/sqrt(c + d*x) - sqrt(c + d*x)) - 10*a**4*b*c*(-c/sqrt(c + d*x) - sqrt(c + d*x))/d - 10*a**4*b*(c**2/sqrt(c + d*x) + 2*c*sqrt(c + d*x) - (c + d*x)**(3/2)/3)/d - 20*a**3*b**2*c*(c**2/sqrt(c + d*x) + 2*c*sqrt(c + d*x) - (c + d*x)**(3/2)/3)/d**2 - 20*a**3*b**2*(-c**3/sqrt(c + d*x) - 3*c**2*sqrt(c + d*x) + c*(c + d*x)**(3/2) - (c + d*x)**(5/2)/5)/d**2 - 20*a**2*b**3*c*(-c**3/sqrt(c + d*x) - 3*c**2*sqrt(c + d*x) + c*(c + d*x)**(3/2) - (c + d*x)**(5/2)/5)/d**3 - 20*a**2*b**3*(c**4/sqrt(c + d*x) + 4*c**3*sqrt(c + d*x) - 2*c**2*(c + d*x)**(3/2) + 4*c*(c + d*x)**(5/2)/5 - (c + d*x)**(7/2)/7)/d**3 - 10*a*b**4*c*(c**4/sqrt(c + d*x) + 4*c**3*sqrt(c + d*x) - 2*c**2*(c + d*x)**(3/2) + 4*c*(c + d*x)**(5/2)/5 - (c + d*x)**(7/2)/7)/d**4 - 10*a*b**4*(-c**5/sqrt(c + d*x) - 5*c**4*sqrt(c + d*x) + 10*c**3*(c + d*x)**(3/2)/3 - 2*c**2*(c + d*x)**(5/2) + 5*c*(c + d*x)**(7/2)/7 - (c + d*x)**(9/2)/9)/d**4 - 2*b**5*c*(-c**5/sqrt(c + d*x) - 5*c**4*sqrt(c + d*x) + 10*c**3*(c + d*x)**(3/2)/3 - 2*c**2*(c + d*x)**(5/2) + 5*c*(c + d*x)**(7/2)/7 - (c + d*x)**(9/2)/9)/d**5 - 2*b**5*(c**6/sqrt(c + d*x) + 6*c**5*sqrt(c + d*x) - 5*c**4*(c + d*x)**(3/2) + 4*c**3*(c + d*x)**(5/2) - 15*c**2*(c + d*x)**(7/2)/7 + 2*c*(c + d*x)**(9/2)/3 - (c + d*x)**(11/2)/11)/d**5)/d, Ne(d, 0)), (Piecewise((a**5*x, Eq(b, 0)), ((a + b*x)**6/(6*b), True))/sqrt(c), True))`

$$3.1414 \quad \int \frac{(a+bx)^4}{\sqrt{c+dx}} dx$$

Optimal. Leaf size=127

$$-\frac{8b^3(c+dx)^{7/2}(bc-ad)}{7d^5} + \frac{12b^2(c+dx)^{5/2}(bc-ad)^2}{5d^5} - \frac{8b(c+dx)^{3/2}(bc-ad)^3}{3d^5} + \frac{2\sqrt{c+dx}(bc-ad)^4}{d^5} + \frac{2b^4(c+dx)^{9/2}}{9d^5}$$

[Out] $-8/3*b*(-a*d+b*c)^3*(d*x+c)^{(3/2)}/d^5+12/5*b^2*(-a*d+b*c)^2*(d*x+c)^{(5/2)}/d^5-8/7*b^3*(-a*d+b*c)*(d*x+c)^{(7/2)}/d^5+2/9*b^4*(d*x+c)^{(9/2)}/d^5+2*(-a*d+b*c)^4*(d*x+c)^{(1/2)}/d^5$

Rubi [A] time = 0.04, antiderivative size = 127, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{8b^3(c+dx)^{7/2}(bc-ad)}{7d^5} + \frac{12b^2(c+dx)^{5/2}(bc-ad)^2}{5d^5} - \frac{8b(c+dx)^{3/2}(bc-ad)^3}{3d^5} + \frac{2\sqrt{c+dx}(bc-ad)^4}{d^5} + \frac{2b^4(c+dx)^{9/2}}{9d^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4/Sqrt[c + d*x], x]

[Out] $(2*(b*c - a*d)^4*\text{Sqrt}[c + d*x])/d^5 - (8*b*(b*c - a*d)^3*(c + d*x)^{(3/2)})/(3*d^5) + (12*b^2*(b*c - a*d)^2*(c + d*x)^{(5/2)})/(5*d^5) - (8*b^3*(b*c - a*d)*(c + d*x)^{(7/2)})/(7*d^5) + (2*b^4*(c + d*x)^{(9/2)})/(9*d^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^4}{\sqrt{c+dx}} dx = \int \left(\frac{(-bc+ad)^4}{d^4\sqrt{c+dx}} - \frac{4b(bc-ad)^3\sqrt{c+dx}}{d^4} + \frac{6b^2(bc-ad)^2(c+dx)^{3/2}}{d^4} - \frac{4b^3(bc-ad)(c+dx)^{5/2}}{d^4} + \frac{2b^4(c+dx)^{7/2}}{d^4} \right) dx$$

$$= \frac{2(bc-ad)^4\sqrt{c+dx}}{d^5} - \frac{8b(bc-ad)^3(c+dx)^{3/2}}{3d^5} + \frac{12b^2(bc-ad)^2(c+dx)^{5/2}}{5d^5} - \frac{8b^3(bc-ad)(c+dx)^{7/2}}{7d^5} + \frac{2b^4(c+dx)^{9/2}}{9d^5}$$

Mathematica [A] time = 0.09, size = 101, normalized size = 0.80

$$\frac{2\sqrt{c+dx}(-180b^3(c+dx)^3(bc-ad) + 378b^2(c+dx)^2(bc-ad)^2 - 420b(c+dx)(bc-ad)^3 + 315(bc-ad)^4 + 35b^4d^4)}{315d^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4/Sqrt[c + d*x], x]

[Out] (2*Sqrt[c + d*x]*(315*(b*c - a*d)^4 - 420*b*(b*c - a*d)^3*(c + d*x) + 378*b^2*(b*c - a*d)^2*(c + d*x)^2 - 180*b^3*(b*c - a*d)*(c + d*x)^3 + 35*b^4*(c + d*x)^4))/(315*d^5)

fricas [A] time = 0.43, size = 182, normalized size = 1.43

$$\frac{2 \left(35 b^4 d^4 x^4 + 128 b^4 c^4 - 576 a b^3 c^3 d + 1008 a^2 b^2 c^2 d^2 - 840 a^3 b c d^3 + 315 a^4 d^4 - 20 \left(2 b^4 c d^3 - 9 a b^3 d^4 \right) x^3 + 6 \left(8 b^4 c^2 d^2 - 36 a b^3 c d^3 + 63 a^2 b^2 d^4 \right) x^2 - 4 \left(16 b^4 c^3 d - 7 \right) x + 6 \left(8 b^4 c^2 d^2 - 36 a b^3 c d^3 + 63 a^2 b^2 d^4 \right) \right)}{315 d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] 2/315*(35*b^4*d^4*x^4 + 128*b^4*c^4 - 576*a*b^3*c^3*d + 1008*a^2*b^2*c^2*d^2 - 840*a^3*b*c*d^3 + 315*a^4*d^4 - 20*(2*b^4*c*d^3 - 9*a*b^3*d^4)*x^3 + 6*(8*b^4*c^2*d^2 - 36*a*b^3*c*d^3 + 63*a^2*b^2*d^4)*x^2 - 4*(16*b^4*c^3*d - 7*a*b^3*c^2*d^2 + 126*a^2*b^2*c*d^3 - 105*a^3*b*d^4)*x)*sqrt(d*x + c)/d^5

giac [A] time = 0.96, size = 204, normalized size = 1.61

$$\frac{2 \left(315 \sqrt{d x + c} a^4 + \frac{420 \left((d x + c)^{\frac{3}{2}} - 3 \sqrt{d x + c} \right) a^3 b}{d} + \frac{126 \left(3 (d x + c)^{\frac{5}{2}} - 10 (d x + c)^{\frac{3}{2}} c + 15 \sqrt{d x + c} c^2 \right) a^2 b^2}{d^2} + \frac{36 \left(5 (d x + c)^{\frac{7}{2}} - 21 (d x + c)^{\frac{5}{2}} c + 35 \sqrt{d x + c} c^2 \right) a b^3}{d^3} \right)}{315 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^(1/2), x, algorithm="giac")

[Out] 2/315*(315*sqrt(d*x + c)*a^4 + 420*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a^3*b/d + 126*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a^2*b^2/d^2 + 36*(5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*a*b^3/d^3 + (35*(d*x + c)^(9/2) - 180*(d*x + c)^(7/2)*c + 378*(d*x + c)^(5/2)*c^2 - 420*(d*x + c)^(3/2)*c^3 + 315*sqrt(d*x + c)*c^4)*b^4/d^4)/d

maple [A] time = 0.01, size = 186, normalized size = 1.46

$$\frac{2 \sqrt{d x + c} \left(35 b^4 x^4 d^4 + 180 a b^3 d^4 x^3 - 40 b^4 c d^3 x^3 + 378 a^2 b^2 d^4 x^2 - 216 a b^3 c d^3 x^2 + 48 b^4 c^2 d^2 x^2 + 420 a^3 b d^4 x - 5 \right)}{315 d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^4/(d*x+c)^(1/2),x)`

[Out] $2/315*(d*x+c)^{(1/2)}*(35*b^4*d^4*x^4+180*a*b^3*d^4*x^3-40*b^4*c*d^3*x^3+378*a^2*b^2*d^4*x^2-216*a*b^3*c*d^3*x^2+48*b^4*c^2*d^2*x^2+420*a^3*b*d^4*x-504*a^2*b^2*c*d^3*x+288*a*b^3*c^2*d^2*x-64*b^4*c^3*d*x+315*a^4*d^4-840*a^3*b*c*d^3+1008*a^2*b^2*c^2*d^2-576*a*b^3*c^3*d+128*b^4*c^4)/d^5$

maxima [A] time = 1.38, size = 204, normalized size = 1.61

$$2 \left(315 \sqrt{dx+c} a^4 + \frac{420 \left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} \right) a^3 b}{d} + \frac{126 \left(3 (dx+c)^{\frac{5}{2}} - 10 (dx+c)^{\frac{3}{2}} c + 15 \sqrt{dx+c} c^2 \right) a^2 b^2}{d^2} + \frac{36 \left(5 (dx+c)^{\frac{7}{2}} - 21 (dx+c)^{\frac{5}{2}} c + 35 (dx+c)^{\frac{3}{2}} c^2 \right) a b^3}{d^3} \right) / 315 d$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^4/(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] $2/315*(315*\sqrt{d*x+c}*a^4+420*((d*x+c)^{(3/2)}-3*\sqrt{d*x+c}*c)*a^3*b/d+126*(3*(d*x+c)^{(5/2)}-10*(d*x+c)^{(3/2)}*c+15*\sqrt{d*x+c}*c^2)*a^2*b^2/d^2+36*(5*(d*x+c)^{(7/2)}-21*(d*x+c)^{(5/2)}*c+35*(d*x+c)^{(3/2)}*c^2-35*\sqrt{d*x+c}*c^3)*a*b^3/d^3+(35*(d*x+c)^{(9/2)}-180*(d*x+c)^{(7/2)}*c+378*(d*x+c)^{(5/2)}*c^2-420*(d*x+c)^{(3/2)}*c^3+315*\sqrt{d*x+c}*c^4)*b^4/d^4)/d$

mupad [B] time = 0.24, size = 112, normalized size = 0.88

$$\frac{2b^4(c+dx)^{9/2}}{9d^5} - \frac{(8b^4c-8ab^3d)(c+dx)^{7/2}}{7d^5} + \frac{2(ad-bc)^4\sqrt{c+dx}}{d^5} + \frac{12b^2(ad-bc)^2(c+dx)^{5/2}}{5d^5} + \frac{8b(ad-bc)^2(c+dx)^{3/2}}{3d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*x)^4/(c+d*x)^(1/2),x)`

[Out] $(2*b^4*(c+d*x)^{(9/2)})/(9*d^5) - ((8*b^4*c - 8*a*b^3*d)*(c+d*x)^{(7/2)})/(7*d^5) + (2*(a*d - b*c)^4*(c+d*x)^{(1/2)})/d^5 + (12*b^2*(a*d - b*c)^2*(c+d*x)^{(5/2)})/(5*d^5) + (8*b*(a*d - b*c)^3*(c+d*x)^{(3/2)})/(3*d^5)$

sympy [A] time = 56.90, size = 532, normalized size = 4.19

$$\left\{ \begin{array}{l} \frac{-\frac{2a^4c}{\sqrt{c+dx}} - 2a^4\left(-\frac{c}{\sqrt{c+dx}} - \sqrt{c+dx}\right) - \frac{8a^3bc\left(-\frac{c}{\sqrt{c+dx}} - \sqrt{c+dx}\right)}{d} - \frac{8a^3b\left(\frac{c^2}{\sqrt{c+dx}} + 2c\sqrt{c+dx} - \frac{(c+dx)^{\frac{3}{2}}}{3}\right)}{d} - \frac{12a^2b^2c\left(\frac{c^2}{\sqrt{c+dx}} + 2c\sqrt{c+dx} - \frac{(c+dx)^{\frac{3}{2}}}{3}\right)}{d^2} - \frac{12a^2b^2\left(-\frac{c^3}{\sqrt{c+dx}} - 3c\right)}{d^2}}{\sqrt{c}} \\ \frac{a^4x}{\sqrt{c}} \quad \text{for } b = 0 \\ \frac{(a+bx)^5}{5b} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4/(d*x+c)**(1/2),x)

[Out] Piecewise(((-2*a**4*c/sqrt(c + d*x) - 2*a**4*(-c/sqrt(c + d*x) - sqrt(c + d*x)) - 8*a**3*b*c*(-c/sqrt(c + d*x) - sqrt(c + d*x))/d - 8*a**3*b*(c**2/sqrt(c + d*x) + 2*c*sqrt(c + d*x) - (c + d*x)**(3/2)/3)/d - 12*a**2*b**2*c*(c**2/sqrt(c + d*x) + 2*c*sqrt(c + d*x) - (c + d*x)**(3/2)/3)/d**2 - 12*a**2*b**2*(-c**3/sqrt(c + d*x) - 3*c**2*sqrt(c + d*x) + c*(c + d*x)**(3/2) - (c + d*x)**(5/2)/5)/d**2 - 8*a*b**3*c*(-c**3/sqrt(c + d*x) - 3*c**2*sqrt(c + d*x) + c*(c + d*x)**(3/2) - (c + d*x)**(5/2)/5)/d**3 - 8*a*b**3*(c**4/sqrt(c + d*x) + 4*c**3*sqrt(c + d*x) - 2*c**2*(c + d*x)**(3/2) + 4*c*(c + d*x)**(5/2)/5 - (c + d*x)**(7/2)/7)/d**3 - 2*b**4*c*(c**4/sqrt(c + d*x) + 4*c**3*sqrt(c + d*x) - 2*c**2*(c + d*x)**(3/2) + 4*c*(c + d*x)**(5/2)/5 - (c + d*x)**(7/2)/7)/d**4 - 2*b**4*(-c**5/sqrt(c + d*x) - 5*c**4*sqrt(c + d*x) + 10*c**3*(c + d*x)**(3/2)/3 - 2*c**2*(c + d*x)**(5/2) + 5*c*(c + d*x)**(7/2)/7 - (c + d*x)**(9/2)/9)/d**4)/d, Ne(d, 0)), (Piecewise((a**4*x, Eq(b, 0)), ((a + b*x)**5/(5*b), True))/sqrt(c), True))

$$3.1415 \quad \int \frac{(a+bx)^3}{\sqrt{c+dx}} dx$$

Optimal. Leaf size=96

$$-\frac{6b^2(c+dx)^{5/2}(bc-ad)}{5d^4} + \frac{2b(c+dx)^{3/2}(bc-ad)^2}{d^4} - \frac{2\sqrt{c+dx}(bc-ad)^3}{d^4} + \frac{2b^3(c+dx)^{7/2}}{7d^4}$$

[Out] $2*b*(-a*d+b*c)^2*(d*x+c)^(3/2)/d^4-6/5*b^2*(-a*d+b*c)*(d*x+c)^(5/2)/d^4+2/7*b^3*(d*x+c)^(7/2)/d^4-2*(-a*d+b*c)^3*(d*x+c)^(1/2)/d^4$

Rubi [A] time = 0.03, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{6b^2(c+dx)^{5/2}(bc-ad)}{5d^4} + \frac{2b(c+dx)^{3/2}(bc-ad)^2}{d^4} - \frac{2\sqrt{c+dx}(bc-ad)^3}{d^4} + \frac{2b^3(c+dx)^{7/2}}{7d^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/Sqrt[c + d*x], x]

[Out] $(-2*(b*c - a*d)^3*\text{Sqrt}[c + d*x])/d^4 + (2*b*(b*c - a*d)^2*(c + d*x)^(3/2))/d^4 - (6*b^2*(b*c - a*d)*(c + d*x)^(5/2))/(5*d^4) + (2*b^3*(c + d*x)^(7/2))/(7*d^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^3}{\sqrt{c+dx}} dx = \int \left(\frac{(-bc+ad)^3}{d^3\sqrt{c+dx}} + \frac{3b(bc-ad)^2\sqrt{c+dx}}{d^3} - \frac{3b^2(bc-ad)(c+dx)^{3/2}}{d^3} + \frac{b^3(c+dx)^{5/2}}{d^3} \right) dx$$

$$= -\frac{2(bc-ad)^3\sqrt{c+dx}}{d^4} + \frac{2b(bc-ad)^2(c+dx)^{3/2}}{d^4} - \frac{6b^2(bc-ad)(c+dx)^{5/2}}{5d^4} + \frac{2b^3(c+dx)^{7/2}}{7d^4}$$

Mathematica [A] time = 0.06, size = 79, normalized size = 0.82

$$\frac{2\sqrt{c+dx}(-21b^2(c+dx)^2(bc-ad) + 35b(c+dx)(bc-ad)^2 - 35(bc-ad)^3 + 5b^3(c+dx)^3)}{35d^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/Sqrt[c + d*x], x]

[Out] (2*Sqrt[c + d*x]*(-35*(b*c - a*d)^3 + 35*b*(b*c - a*d)^2*(c + d*x) - 21*b^2*(b*c - a*d)*(c + d*x)^2 + 5*b^3*(c + d*x)^3))/(35*d^4)

fricas [A] time = 0.43, size = 115, normalized size = 1.20

$$\frac{2(5b^3d^3x^3 - 16b^3c^3 + 56ab^2c^2d - 70a^2bcd^2 + 35a^3d^3 - 3(2b^3cd^2 - 7ab^2d^3)x^2 + (8b^3c^2d - 28ab^2cd^2 + 35a^3d^3))}{35d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] 2/35*(5*b^3*d^3*x^3 - 16*b^3*c^3 + 56*a*b^2*c^2*d - 70*a^2*b*c*d^2 + 35*a^3*d^3 - 3*(2*b^3*c*d^2 - 7*a*b^2*d^3)*x^2 + (8*b^3*c^2*d - 28*a*b^2*c*d^2 + 35*a^2*b*d^3)*x)*sqrt(d*x + c)/d^4

giac [A] time = 1.01, size = 137, normalized size = 1.43

$$\frac{2 \left(35 \sqrt{dx+c} a^3 + \frac{35 \left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} c \right) a^2 b}{d} + \frac{7 \left(3 (dx+c)^{\frac{5}{2}} - 10 (dx+c)^{\frac{3}{2}} c + 15 \sqrt{dx+c} c^2 \right) a b^2}{d^2} + \frac{\left(5 (dx+c)^{\frac{7}{2}} - 21 (dx+c)^{\frac{5}{2}} c + 35 (dx+c)^{\frac{3}{2}} c^2 \right) b^3}{d^3} \right)}{35 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^(1/2), x, algorithm="giac")

[Out] 2/35*(35*sqrt(d*x + c)*a^3 + 35*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a^2*b/d + 7*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a*b^2/d^2 + (5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*b^3/d^3)/d

maple [A] time = 0.01, size = 116, normalized size = 1.21

$$\frac{2\sqrt{dx+c} (5b^3x^3d^3 + 21ab^2d^3x^2 - 6b^3cd^2x^2 + 35a^2bd^3x - 28ab^2cd^2x + 8b^3c^2dx + 35a^3d^3 - 70a^2bcd^2 + 56a^3cd^2)}{35d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/(d*x+c)^(1/2), x)

[Out] 2/35*(d*x+c)^(1/2)*(5*b^3*d^3*x^3+21*a*b^2*d^3*x^2-6*b^3*c*d^2*x^2+35*a^2*b*d^3*x-28*a*b^2*c*d^2*x+8*b^3*c^2*d*x+35*a^3*d^3-70*a^2*b*c*d^2+56*a*b^2*c^2*d-16*b^3*c^3)/d^4

maxima [A] time = 1.38, size = 137, normalized size = 1.43

$$2 \left(35 \sqrt{dx+c} a^3 + \frac{35 \left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} c \right) a^2 b}{d} + \frac{7 \left(3 (dx+c)^{\frac{5}{2}} - 10 (dx+c)^{\frac{3}{2}} c + 15 \sqrt{dx+c} c^2 \right) a b^2}{d^2} + \frac{\left(5 (dx+c)^{\frac{7}{2}} - 21 (dx+c)^{\frac{5}{2}} c + 35 (dx+c)^{\frac{3}{2}} c^2 - 35 \sqrt{dx+c} c^3 \right) b^3}{d^3} \right) / 35 d$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] 2/35*(35*sqrt(d*x + c)*a^3 + 35*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a^2*b/d + 7*(3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*a*b^2/d^2 + (5*(d*x + c)^(7/2) - 21*(d*x + c)^(5/2)*c + 35*(d*x + c)^(3/2)*c^2 - 35*sqrt(d*x + c)*c^3)*b^3/d^3)/d

mupad [B] time = 0.26, size = 87, normalized size = 0.91

$$\frac{2 b^3 (c + d x)^{7/2}}{7 d^4} - \frac{(6 b^3 c - 6 a b^2 d) (c + d x)^{5/2}}{5 d^4} + \frac{2 (a d - b c)^3 \sqrt{c + d x}}{d^4} + \frac{2 b (a d - b c)^2 (c + d x)^{3/2}}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3/(c + d*x)^(1/2),x)

[Out] (2*b^3*(c + d*x)^(7/2))/(7*d^4) - ((6*b^3*c - 6*a*b^2*d)*(c + d*x)^(5/2))/(5*d^4) + (2*(a*d - b*c)^3*(c + d*x)^(1/2))/d^4 + (2*b*(a*d - b*c)^2*(c + d*x)^(3/2))/d^4

sympy [A] time = 37.06, size = 366, normalized size = 3.81

$$\left\{ \begin{array}{l} \frac{-\frac{2a^3c}{\sqrt{c+dx}} - 2a^3 \left(-\frac{c}{\sqrt{c+dx}} - \sqrt{c+dx} \right) - \frac{6a^2bc \left(-\frac{c}{\sqrt{c+dx}} - \sqrt{c+dx} \right)}{d} - \frac{6a^2b \left(\frac{c^2}{\sqrt{c+dx}} + 2c\sqrt{c+dx} - \frac{(c+dx)^{\frac{3}{2}}}{3} \right)}{d} - \frac{6ab^2c \left(\frac{c^2}{\sqrt{c+dx}} + 2c\sqrt{c+dx} - \frac{(c+dx)^{\frac{3}{2}}}{3} \right)}{d^2} - \frac{6ab^2 \left(-\frac{c^3}{\sqrt{c+dx}} - 3c^2\sqrt{c+dx} \right)}{d^3}}{\sqrt{c}} \\ \left\{ \begin{array}{ll} a^3 x & \text{for } b = 0 \\ \frac{(a+bx)^4}{4b} & \text{otherwise} \end{array} \right. \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3/(d*x+c)**(1/2),x)

```
[Out] Piecewise((( -2*a**3*c/sqrt(c + d*x) - 2*a**3*(-c/sqrt(c + d*x) - sqrt(c + d
*x)) - 6*a**2*b*c*(-c/sqrt(c + d*x) - sqrt(c + d*x))/d - 6*a**2*b*(c**2/sqr
t(c + d*x) + 2*c*sqrt(c + d*x) - (c + d*x)**(3/2)/3)/d - 6*a*b**2*c*(c**2/s
qrt(c + d*x) + 2*c*sqrt(c + d*x) - (c + d*x)**(3/2)/3)/d**2 - 6*a*b**2*(-c*
*3/sqrt(c + d*x) - 3*c**2*sqrt(c + d*x) + c*(c + d*x)**(3/2) - (c + d*x)**(
5/2)/5)/d**2 - 2*b**3*c*(-c**3/sqrt(c + d*x) - 3*c**2*sqrt(c + d*x) + c*(c
+ d*x)**(3/2) - (c + d*x)**(5/2)/5)/d**3 - 2*b**3*(c**4/sqrt(c + d*x) + 4*c
**3*sqrt(c + d*x) - 2*c**2*(c + d*x)**(3/2) + 4*c*(c + d*x)**(5/2)/5 - (c +
d*x)**(7/2)/7)/d**3)/d, Ne(d, 0)), (Piecewise((a**3*x, Eq(b, 0)), ((a + b*
x)**4/(4*b), True))/sqrt(c), True))
```

$$3.1416 \quad \int \frac{(a+bx)^2}{\sqrt{c+dx}} dx$$

Optimal. Leaf size=69

$$-\frac{4b(c+dx)^{3/2}(bc-ad)}{3d^3} + \frac{2\sqrt{c+dx}(bc-ad)^2}{d^3} + \frac{2b^2(c+dx)^{5/2}}{5d^3}$$

[Out] $-4/3*b*(-a*d+b*c)*(d*x+c)^{(3/2)}/d^3+2/5*b^2*(d*x+c)^{(5/2)}/d^3+2*(-a*d+b*c)^{2*(d*x+c)^{(1/2)}/d^3}$

Rubi [A] time = 0.02, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{4b(c+dx)^{3/2}(bc-ad)}{3d^3} + \frac{2\sqrt{c+dx}(bc-ad)^2}{d^3} + \frac{2b^2(c+dx)^{5/2}}{5d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/Sqrt[c + d*x], x]

[Out] $(2*(b*c - a*d)^2*\text{Sqrt}[c + d*x])/d^3 - (4*b*(b*c - a*d)*(c + d*x)^{(3/2)})/(3*d^3) + (2*b^2*(c + d*x)^{(5/2)})/(5*d^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{\sqrt{c+dx}} dx &= \int \left(\frac{(-bc+ad)^2}{d^2\sqrt{c+dx}} - \frac{2b(bc-ad)\sqrt{c+dx}}{d^2} + \frac{b^2(c+dx)^{3/2}}{d^2} \right) dx \\ &= \frac{2(bc-ad)^2\sqrt{c+dx}}{d^3} - \frac{4b(bc-ad)(c+dx)^{3/2}}{3d^3} + \frac{2b^2(c+dx)^{5/2}}{5d^3} \end{aligned}$$

Mathematica [A] time = 0.04, size = 60, normalized size = 0.87

$$\frac{2\sqrt{c+dx} (15a^2d^2 + 10abd(dx-2c) + b^2(8c^2 - 4cdx + 3d^2x^2))}{15d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/Sqrt[c + d*x], x]

[Out] (2*Sqrt[c + d*x]*(15*a^2*d^2 + 10*a*b*d*(-2*c + d*x) + b^2*(8*c^2 - 4*c*d*x + 3*d^2*x^2)))/(15*d^3)

fricas [A] time = 0.46, size = 64, normalized size = 0.93

$$\frac{2 \left(3 b^2 d^2 x^2 + 8 b^2 c^2 - 20 a b c d + 15 a^2 d^2 - 2 \left(2 b^2 c d - 5 a b d^2 \right) x \right) \sqrt{d x + c}}{15 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] 2/15*(3*b^2*d^2*x^2 + 8*b^2*c^2 - 20*a*b*c*d + 15*a^2*d^2 - 2*(2*b^2*c*d - 5*a*b*d^2)*x)*sqrt(d*x + c)/d^3

giac [A] time = 1.10, size = 82, normalized size = 1.19

$$\frac{2 \left(15 \sqrt{d x + c} a^2 + \frac{10 \left((d x + c)^{\frac{3}{2}} - 3 \sqrt{d x + c} c \right) a b}{d} + \frac{\left(3 (d x + c)^{\frac{5}{2}} - 10 (d x + c)^{\frac{3}{2}} c + 15 \sqrt{d x + c} c^2 \right) b^2}{d^2} \right)}{15 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^(1/2), x, algorithm="giac")

[Out] 2/15*(15*sqrt(d*x + c)*a^2 + 10*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a*b/d + (3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*b^2/d^2)/d

maple [A] time = 0.00, size = 63, normalized size = 0.91

$$\frac{2 \sqrt{d x + c} \left(3 b^2 x^2 d^2 + 10 a b d^2 x - 4 b^2 c d x + 15 a^2 d^2 - 20 a b c d + 8 b^2 c^2 \right)}{15 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(d*x+c)^(1/2), x)

[Out] 2/15*(d*x+c)^(1/2)*(3*b^2*d^2*x^2+10*a*b*d^2*x-4*b^2*c*d*x+15*a^2*d^2-20*a*b*c*d+8*b^2*c^2)/d^3

maxima [A] time = 1.37, size = 82, normalized size = 1.19

$$\frac{2 \left(15 \sqrt{dx+c} a^2 + \frac{10 \left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} \right) ab}{d} + \frac{\left(3 (dx+c)^{\frac{5}{2}} - 10 (dx+c)^{\frac{3}{2}} c + 15 \sqrt{dx+c} c^2 \right) b^2}{d^2} \right)}{15 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] 2/15*(15*sqrt(d*x + c)*a^2 + 10*((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*a*b/d + (3*(d*x + c)^(5/2) - 10*(d*x + c)^(3/2)*c + 15*sqrt(d*x + c)*c^2)*b^2/d^2)/d

mupad [B] time = 0.07, size = 68, normalized size = 0.99

$$\frac{2 \sqrt{c+dx} \left(3 b^2 (c+dx)^2 + 15 a^2 d^2 + 15 b^2 c^2 - 10 b^2 c (c+dx) + 10 a b d (c+dx) - 30 a b c d \right)}{15 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(c + d*x)^(1/2),x)

[Out] (2*(c + d*x)^(1/2)*(3*b^2*(c + d*x)^2 + 15*a^2*d^2 + 15*b^2*c^2 - 10*b^2*c*(c + d*x) + 10*a*b*d*(c + d*x) - 30*a*b*c*d))/(15*d^3)

sympy [A] time = 20.94, size = 231, normalized size = 3.35

$$\left\{ \begin{array}{l} \frac{-\frac{2a^2c}{\sqrt{c+dx}} - 2a^2 \left(-\frac{c}{\sqrt{c+dx}} - \sqrt{c+dx} \right) - \frac{4abc \left(-\frac{c}{\sqrt{c+dx}} - \sqrt{c+dx} \right)}{d} - \frac{4ab \left(\frac{c^2}{\sqrt{c+dx}} + 2c\sqrt{c+dx} - \frac{(c+dx)^{\frac{3}{2}}}{3} \right)}{d} - \frac{2b^2c \left(\frac{c^2}{\sqrt{c+dx}} + 2c\sqrt{c+dx} - \frac{(c+dx)^{\frac{3}{2}}}{3} \right)}{d^2} - \frac{2b^2 \left(-\frac{c^3}{\sqrt{c+dx}} - 3c^2\sqrt{c+dx} + c \right)}{d^2}}{d} \\ \frac{\begin{cases} a^2x & \text{for } b = 0 \\ \frac{(a+bx)^3}{3b} & \text{otherwise} \end{cases}}{\sqrt{c}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(d*x+c)**(1/2),x)

[Out] Piecewise((((-2*a**2*c/sqrt(c + d*x) - 2*a**2*(-c/sqrt(c + d*x) - sqrt(c + d*x)) - 4*a*b*c*(-c/sqrt(c + d*x) - sqrt(c + d*x))/d - 4*a*b*(c**2/sqrt(c +

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d*x) + 2*c*sqrt(c + d*x) - (c + d*x)**(3/2)/3)/d - 2*b**2*c*(c**2/sqrt(c +
d*x) + 2*c*sqrt(c + d*x) - (c + d*x)**(3/2)/3)/d**2 - 2*b**2*(-c**3/sqrt(c
+ d*x) - 3*c**2*sqrt(c + d*x) + c*(c + d*x)**(3/2) - (c + d*x)**(5/2)/5)/d*
*2)/d, Ne(d, 0)), (Piecewise((a**2*x, Eq(b, 0)), ((a + b*x)**3/(3*b), True)
)/sqrt(c), True))

```

$$3.1417 \quad \int \frac{a+bx}{\sqrt{c+dx}} dx$$

Optimal. Leaf size=40

$$\frac{2b(c+dx)^{3/2}}{3d^2} - \frac{2\sqrt{c+dx}(bc-ad)}{d^2}$$

[Out] $2/3*b*(d*x+c)^{(3/2)}/d^2-2*(-a*d+b*c)*(d*x+c)^{(1/2)}/d^2$

Rubi [A] time = 0.01, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{2b(c+dx)^{3/2}}{3d^2} - \frac{2\sqrt{c+dx}(bc-ad)}{d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/Sqrt[c + d*x], x]

[Out] $(-2*(b*c - a*d)*Sqrt[c + d*x])/d^2 + (2*b*(c + d*x)^{(3/2)})/(3*d^2)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{\sqrt{c+dx}} dx &= \int \left(\frac{-bc+ad}{d\sqrt{c+dx}} + \frac{b\sqrt{c+dx}}{d} \right) dx \\ &= -\frac{2(bc-ad)\sqrt{c+dx}}{d^2} + \frac{2b(c+dx)^{3/2}}{3d^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 29, normalized size = 0.72

$$\frac{2\sqrt{c+dx}(3ad-2bc+bdx)}{3d^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/Sqrt[c + d*x],x]

[Out] (2*Sqrt[c + d*x]*(-2*b*c + 3*a*d + b*d*x))/(3*d^2)

fricas [A] time = 0.42, size = 25, normalized size = 0.62

$$\frac{2(bdx - 2bc + 3ad)\sqrt{dx + c}}{3d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)^(1/2),x, algorithm="fricas")

[Out] 2/3*(b*d*x - 2*b*c + 3*a*d)*sqrt(d*x + c)/d^2

giac [A] time = 0.88, size = 39, normalized size = 0.98

$$\frac{2 \left(3 \sqrt{dx + c} a + \frac{\left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} c \right) b}{d} \right)}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)^(1/2),x, algorithm="giac")

[Out] 2/3*(3*sqrt(d*x + c)*a + ((d*x + c)^(3/2) - 3*sqrt(d*x + c)*c)*b/d)/d

maple [A] time = 0.00, size = 26, normalized size = 0.65

$$\frac{2\sqrt{dx + c} (bdx + 3ad - 2bc)}{3d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/(d*x+c)^(1/2),x)

[Out] 2/3*(d*x+c)^(1/2)*(b*d*x+3*a*d-2*b*c)/d^2

maxima [A] time = 1.35, size = 39, normalized size = 0.98

$$\frac{2 \left(3 \sqrt{dx + c} a + \frac{\left((dx+c)^{\frac{3}{2}} - 3 \sqrt{dx+c} c \right) b}{d} \right)}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] $\frac{2}{3} \cdot (3 \cdot \sqrt{d \cdot x + c} \cdot a + ((d \cdot x + c)^{(3/2)} - 3 \cdot \sqrt{d \cdot x + c} \cdot c) \cdot b/d) / d$

mupad [B] time = 0.05, size = 28, normalized size = 0.70

$$\frac{2 \sqrt{c + d x} (3 a d - 3 b c + b (c + d x))}{3 d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(c + d*x)^(1/2),x)

[Out] $(2 \cdot (c + d \cdot x)^{(1/2)} \cdot (3 \cdot a \cdot d - 3 \cdot b \cdot c + b \cdot (c + d \cdot x))) / (3 \cdot d^2)$

sympy [A] time = 4.78, size = 121, normalized size = 3.02

$$\left\{ \begin{array}{ll} \frac{-\frac{2ac}{\sqrt{c+dx}} - 2a \left(-\frac{c}{\sqrt{c+dx}} - \sqrt{c+dx} \right) - \frac{2bc \left(-\frac{c}{\sqrt{c+dx}} - \sqrt{c+dx} \right)}{d} - \frac{2b \left(\frac{c^2}{\sqrt{c+dx}} + 2c\sqrt{c+dx} - \frac{(c+dx)^{3/2}}{3} \right)}{d}}{d} & \text{for } d \neq 0 \\ \frac{ax + \frac{bx^2}{2}}{\sqrt{c}} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)**(1/2),x)

[Out] Piecewise(((−2*a*c/sqrt(c + d*x) − 2*a*(−c/sqrt(c + d*x) − sqrt(c + d*x)) − 2*b*c*(−c/sqrt(c + d*x) − sqrt(c + d*x))/d − 2*b*(c**2/sqrt(c + d*x) + 2*c*sqrt(c + d*x) − (c + d*x)**(3/2)/3)/d)/d, Ne(d, 0)), ((a*x + b*x**2/2)/sqrt(c), True))

$$3.1418 \quad \int \frac{1}{\sqrt{c+dx}} dx$$

Optimal. Leaf size=14

$$\frac{2\sqrt{c+dx}}{d}$$

[Out] 2*(d*x+c)^(1/2)/d

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$\frac{2\sqrt{c+dx}}{d}$$

Antiderivative was successfully verified.

[In] Int[1/Sqrt[c + d*x], x]

[Out] (2*Sqrt[c + d*x])/d

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt{c+dx}} dx = \frac{2\sqrt{c+dx}}{d}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{2\sqrt{c+dx}}{d}$$

Antiderivative was successfully verified.

[In] Integrate[1/Sqrt[c + d*x], x]

[Out] (2*Sqrt[c + d*x])/d

fricas [A] time = 0.43, size = 12, normalized size = 0.86

$$\frac{2\sqrt{dx+c}}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^(1/2),x, algorithm="fricas")

[Out] 2*sqrt(d*x + c)/d

giac [A] time = 0.91, size = 12, normalized size = 0.86

$$\frac{2\sqrt{dx+c}}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^(1/2),x, algorithm="giac")

[Out] 2*sqrt(d*x + c)/d

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{2\sqrt{dx+c}}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^(1/2),x)

[Out] 2*(d*x+c)^(1/2)/d

maxima [A] time = 1.30, size = 12, normalized size = 0.86

$$\frac{2\sqrt{dx+c}}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] 2*sqrt(d*x + c)/d

mupad [B] time = 0.02, size = 12, normalized size = 0.86

$$\frac{2\sqrt{c+dx}}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(c + d*x)^(1/2),x)
```

```
[Out] (2*(c + d*x)^(1/2))/d
```

```
sympy [A] time = 0.06, size = 10, normalized size = 0.71
```

$$\frac{2\sqrt{c + dx}}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(d*x+c)**(1/2),x)
```

```
[Out] 2*sqrt(c + d*x)/d
```

$$3.1419 \quad \int \frac{1}{(a+bx)\sqrt{c+dx}} dx$$

Optimal. Leaf size=47

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{\sqrt{b}\sqrt{bc-ad}}$$

[Out] $-2*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/b^{(1/2)/(-a*d+b*c)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {63, 208}

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{\sqrt{b}\sqrt{bc-ad}}$$

Antiderivative was successfully verified.

[In] `Int[1/((a + b*x)*Sqrt[c + d*x]),x]`

[Out] $(-2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/(\operatorname{Sqrt}[b*c - a*d])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[b*c - a*d]))$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\int \frac{1}{(a+bx)\sqrt{c+dx}} dx = \frac{2 \operatorname{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{d}$$

$$= -\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{\sqrt{b}\sqrt{bc-ad}}$$

Mathematica [A] time = 0.02, size = 47, normalized size = 1.00

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{\sqrt{b}\sqrt{bc-ad}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*Sqrt[c + d*x]),x]

[Out] (-2*ArcTanh[(Sqrt[b]*Sqrt[c + d*x])/Sqrt[b*c - a*d]])/(Sqrt[b]*Sqrt[b*c - a*d])

fricas [A] time = 0.44, size = 119, normalized size = 2.53

$$\left[\frac{\log\left(\frac{bdx+2bc-ad-2\sqrt{b^2c-abd}\sqrt{dx+c}}{bx+a}\right)}{\sqrt{b^2c-abd}}, \frac{2\sqrt{-b^2c+abd}\arctan\left(\frac{\sqrt{-b^2c+abd}\sqrt{dx+c}}{bdx+bc}\right)}{b^2c-abd} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(1/2),x, algorithm="fricas")

[Out] [log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a))/sqrt(b^2*c - a*b*d), 2*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c))/(b^2*c - a*b*d)]

giac [A] time = 0.88, size = 38, normalized size = 0.81

$$\frac{2 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{\sqrt{-b^2c+abd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(1/2),x, algorithm="giac")

[Out] 2*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/sqrt(-b^2*c + a*b*d)

maple [A] time = 0.01, size = 37, normalized size = 0.79

$$\frac{2 \arctan\left(\frac{\sqrt{dx+c} b}{\sqrt{(ad-bc)b}}\right)}{\sqrt{(ad-bc)b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)/(d*x+c)^(1/2),x)

[Out] 2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.27, size = 38, normalized size = 0.81

$$\frac{2 \operatorname{atan}\left(\frac{b \sqrt{c+dx}}{\sqrt{abd-b^2c}}\right)}{\sqrt{abd-b^2c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)*(c + d*x)^(1/2)),x)

[Out] (2*atan((b*(c + d*x)^(1/2))/(a*b*d - b^2*c)^(1/2)))/(a*b*d - b^2*c)^(1/2)

sympy [A] time = 5.41, size = 44, normalized size = 0.94

$$\frac{2 \operatorname{atan}\left(\frac{1}{\sqrt{\frac{b}{ad-bc}} \sqrt{c+dx}}\right)}{\sqrt{\frac{b}{ad-bc}} (ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)/(d*x+c)**(1/2),x)
```

```
[Out] -2*atan(1/(sqrt(b/(a*d - b*c))*sqrt(c + d*x)))/(sqrt(b/(a*d - b*c))*(a*d - b*c))
```

$$3.1420 \quad \int \frac{1}{(a+bx)^2 \sqrt{c+dx}} dx$$

Optimal. Leaf size=76

$$\frac{d \tanh^{-1}\left(\frac{\sqrt{b} \sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{\sqrt{b}(bc-ad)^{3/2}} - \frac{\sqrt{c+dx}}{(a+bx)(bc-ad)}$$

[Out] $d \cdot \operatorname{arctanh}\left(\frac{b^{1/2} \cdot (d \cdot x + c)^{1/2}}{(-a \cdot d + b \cdot c)^{1/2}}\right) / (-a \cdot d + b \cdot c)^{3/2} / b^{1/2} - (d \cdot x + c)^{1/2} / (-a \cdot d + b \cdot c) / (b \cdot x + a)$

Rubi [A] time = 0.03, antiderivative size = 76, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$\frac{d \tanh^{-1}\left(\frac{\sqrt{b} \sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{\sqrt{b}(bc-ad)^{3/2}} - \frac{\sqrt{c+dx}}{(a+bx)(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^2*Sqrt[c + d*x]),x]

[Out] $-(\operatorname{Sqrt}[c + d \cdot x] / ((b \cdot c - a \cdot d) \cdot (a + b \cdot x))) + (d \cdot \operatorname{ArcTanh}[(\operatorname{Sqrt}[b] \cdot \operatorname{Sqrt}[c + d \cdot x]) / \operatorname{Sqrt}[b \cdot c - a \cdot d]]) / (\operatorname{Sqrt}[b] \cdot (b \cdot c - a \cdot d)^{3/2})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^2\sqrt{c+dx}} dx &= -\frac{\sqrt{c+dx}}{(bc-ad)(a+bx)} - \frac{d \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{2(bc-ad)} \\ &= -\frac{\sqrt{c+dx}}{(bc-ad)(a+bx)} - \frac{\text{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{bc-ad} \\ &= -\frac{\sqrt{c+dx}}{(bc-ad)(a+bx)} + \frac{d \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{\sqrt{b}(bc-ad)^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.07, size = 76, normalized size = 1.00

$$\frac{d \tan^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{\sqrt{b}(ad-bc)^{3/2}} - \frac{\sqrt{c+dx}}{(a+bx)(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*Sqrt[c + d*x]), x]

[Out] -(Sqrt[c + d*x]/((b*c - a*d)*(a + b*x))) + (d*ArcTan[(Sqrt[b]*Sqrt[c + d*x])/Sqrt[-(b*c) + a*d]])/(Sqrt[b]*(-(b*c) + a*d)^(3/2))

fricas [B] time = 0.45, size = 280, normalized size = 3.68

$$\left[\frac{\sqrt{b^2c - abd}(bdx + ad) \log\left(\frac{bdx + 2bc - ad - 2\sqrt{b^2c - abd}\sqrt{dx+c}}{bx+a}\right) + 2(b^2c - abd)\sqrt{dx+c}}{2(ab^3c^2 - 2a^2b^2cd + a^3bd^2 + (b^4c^2 - 2ab^3cd + a^2b^2d^2)x)}, -\frac{\sqrt{-b^2c + abd}(bdx + ad) \arctan\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{ab^3c^2 - 2a^2b^2cd + a^3bd^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] [-1/2*(sqrt(b^2*c - a*b*d)*(b*d*x + a*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) + 2*(b^2*c - a*b*d)*sqrt(d*x + c)]

$$\frac{d}{dx} \left(\frac{\sqrt{dx+c} b}{\sqrt{-b^2c+abd}} \right) - \frac{\sqrt{dx+c} d}{((dx+c)b - bc + ad)(bc - ad)}$$

giac [A] time = 1.03, size = 87, normalized size = 1.14

$$\frac{d \arctan\left(\frac{\sqrt{dx+c} b}{\sqrt{-b^2c+abd}}\right)}{\sqrt{-b^2c+abd}(bc-ad)} - \frac{\sqrt{dx+c} d}{((dx+c)b - bc + ad)(bc - ad)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^(1/2),x, algorithm="giac")

[Out] -d*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/(sqrt(-b^2*c + a*b*d)*(b*c - a*d)) - sqrt(d*x + c)*d/(((d*x + c)*b - b*c + a*d)*(b*c - a*d))

maple [A] time = 0.01, size = 77, normalized size = 1.01

$$\frac{d \arctan\left(\frac{\sqrt{dx+c} b}{\sqrt{(ad-bc)b}}\right)}{(ad-bc)\sqrt{(ad-bc)b}} + \frac{\sqrt{dx+c} d}{(ad-bc)(bdx+ad)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/(d*x+c)^(1/2),x)

[Out] d*(d*x+c)^(1/2)/(a*d-b*c)/(b*d*x+a*d)+d/(a*d-b*c)/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.09, size = 74, normalized size = 0.97

$$\frac{d \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{\sqrt{b} (ad-bc)^{3/2}} + \frac{d \sqrt{c+dx}}{(ad-bc)(ad-bc+b(c+dx))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^2*(c + d*x)^(1/2)),x)`

[Out] $(d*\operatorname{atan}((b^{1/2}*(c + d*x)^{1/2})/(a*d - b*c)^{1/2}))/b^{1/2}*(a*d - b*c)^{3/2} + (d*(c + d*x)^{1/2})/((a*d - b*c)*(a*d - b*c + b*(c + d*x)))$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^2 \sqrt{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**2/(d*x+c)**(1/2),x)`

[Out] `Integral(1/((a + b*x)**2*sqrt(c + d*x)), x)`

$$3.1421 \quad \int \frac{1}{(a+bx)^3 \sqrt{c+dx}} dx$$

Optimal. Leaf size=114

$$-\frac{3d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4\sqrt{b}(bc-ad)^{5/2}} + \frac{3d\sqrt{c+dx}}{4(a+bx)(bc-ad)^2} - \frac{\sqrt{c+dx}}{2(a+bx)^2(bc-ad)}$$

[Out] $-3/4*d^2*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})/(-a*d+b*c)^{(5/2)}/b^{(1/2)}-1/2*(d*x+c)^{(1/2)}/(-a*d+b*c)/(b*x+a)^2+3/4*d*(d*x+c)^{(1/2)}/(-a*d+b*c)^2/(b*x+a)$

Rubi [A] time = 0.04, antiderivative size = 114, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$-\frac{3d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4\sqrt{b}(bc-ad)^{5/2}} + \frac{3d\sqrt{c+dx}}{4(a+bx)(bc-ad)^2} - \frac{\sqrt{c+dx}}{2(a+bx)^2(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^3*Sqrt[c + d*x]),x]

[Out] $-\operatorname{Sqrt}[c + d*x]/(2*(b*c - a*d)*(a + b*x)^2) + (3*d*\operatorname{Sqrt}[c + d*x])/(4*(b*c - a*d)^2*(a + b*x)) - (3*d^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/\operatorname{Sqrt}[b*c - a*d]])/(4*\operatorname{Sqrt}[b]*(b*c - a*d)^{(5/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

`Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]`

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^3 \sqrt{c+dx}} dx &= -\frac{\sqrt{c+dx}}{2(bc-ad)(a+bx)^2} - \frac{(3d) \int \frac{1}{(a+bx)^2 \sqrt{c+dx}} dx}{4(bc-ad)} \\
 &= -\frac{\sqrt{c+dx}}{2(bc-ad)(a+bx)^2} + \frac{3d\sqrt{c+dx}}{4(bc-ad)^2(a+bx)} + \frac{(3d^2) \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{8(bc-ad)^2} \\
 &= -\frac{\sqrt{c+dx}}{2(bc-ad)(a+bx)^2} + \frac{3d\sqrt{c+dx}}{4(bc-ad)^2(a+bx)} + \frac{(3d) \text{Subst} \left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx} \right)}{4(bc-ad)^2} \\
 &= -\frac{\sqrt{c+dx}}{2(bc-ad)(a+bx)^2} + \frac{3d\sqrt{c+dx}}{4(bc-ad)^2(a+bx)} - \frac{3d^2 \tanh^{-1} \left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}} \right)}{4\sqrt{b}(bc-ad)^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.44

$$\frac{2d^2 \sqrt{c+dx} {}_2F_1 \left(\frac{1}{2}, 3; \frac{3}{2}; -\frac{b(c+dx)}{ad-bc} \right)}{(ad-bc)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^3*Sqrt[c + d*x]),x]

[Out] (2*d^2*Sqrt[c + d*x]*Hypergeometric2F1[1/2, 3, 3/2, -((b*(c + d*x))/(-(b*c) + a*d))])/(-(b*c) + a*d)^3

fricas [B] time = 0.47, size = 549, normalized size = 4.82

$$\left[\frac{3(b^2d^2x^2 + 2abd^2x + a^2d^2)\sqrt{b^2c - abd} \log\left(\frac{bdx+2bc-ad-2\sqrt{b^2c-abd}\sqrt{dx+c}}{bx+a}\right) - 2(2b^3c^2 - 7ab^2cd + 5a^2bd^2 - 3(b^3c^3 - 3a^3b^3c^2d + 3a^4b^2cd^2 - a^5bd^3 + (b^6c^3 - 3ab^5c^2d + 3a^2b^4cd^2 - a^3b^3d^3))x^2 + 2(ab^5c^3 - 3a^2b^4c^2d + \dots)}{\dots} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^(1/2),x, algorithm="fricas")

[Out] [1/8*(3*(b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) - 2*(2*b^3*c^2 - 7*a*b^2*c*d + 5*a^2*b*d^2 - 3*(b^3*c*d - a*b^2*d^2)*x)*sqrt(d*x + c))/(a^2*b^4*c^3 - 3*a^3*b^3*c^2*d + 3*a^4*b^2*c*d^2 - a^5*b*d^3 + (b^6*c^3 - 3*a*b^5*c^2*d + 3*a^2*b^4*c*d^2 - a^3*b^3*d^3)*x^2 + 2*(a*b^5*c^3 - 3*a^2*b^4*c^2*d + 3*a^3*b^3*c*d^2 - a^4*b^2*d^3)*x), 1/4*(3*(b^2*d^2*x^2 + 2*a*b*d^2*x + a^2*d^2)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) - (2*b^3*c^2 - 7*a*b^2*c*d + 5*a^2*b*d^2 - 3*(b^3*c*d - a*b^2*d^2)*x)*sqrt(d*x + c))/(a^2*b^4*c^3 - 3*a^3*b^3*c^2*d + 3*a^4*b^2*c*d^2 - a^5*b*d^3 + (b^6*c^3 - 3*a*b^5*c^2*d + 3*a^2*b^4*c*d^2 - a^3*b^3*d^3)*x^2 + 2*(a*b^5*c^3 - 3*a^2*b^4*c^2*d + 3*a^3*b^3*c*d^2 - a^4*b^2*d^3)*x)]

giac [A] time = 0.93, size = 148, normalized size = 1.30

$$\frac{3d^2 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{4(b^2c^2 - 2abcd + a^2d^2)\sqrt{-b^2c + abd}} + \frac{3(dx+c)^{\frac{3}{2}}bd^2 - 5\sqrt{dx+c}bcd^2 + 5\sqrt{dx+c}ad^3}{4(b^2c^2 - 2abcd + a^2d^2)((dx+c)b - bc + ad)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^(1/2),x, algorithm="giac")

[Out] 3/4*d^2*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*sqrt(-b^2*c + a*b*d)) + 1/4*(3*(d*x + c)^(3/2)*b*d^2 - 5*sqrt(d*x + c)*b*c*d^2 + 5*sqrt(d*x + c)*a*d^3)/((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*((d*x + c)*b - b*c + a*d)^2)

maple [A] time = 0.01, size = 115, normalized size = 1.01

$$\frac{3d^2 \arctan\left(\frac{\sqrt{dx+c} b}{\sqrt{(ad-bc)b}}\right)}{4(ad-bc)^2 \sqrt{(ad-bc)b}} + \frac{\sqrt{dx+c} d^2}{2(ad-bc)(bdx+ad)^2} + \frac{3\sqrt{dx+c} d^2}{4(ad-bc)^2 (bdx+ad)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^3/(d*x+c)^(1/2),x)

[Out] 1/2*d^2*(d*x+c)^(1/2)/(a*d-b*c)/(b*d*x+a*d)^2+3/4*d^2/(a*d-b*c)^2*(d*x+c)^(1/2)/(b*d*x+a*d)+3/4*d^2/(a*d-b*c)^2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^3/(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details) Is a*d-b*c positive or negative?

mupad [B] time = 0.33, size = 142, normalized size = 1.25

$$\frac{\frac{5d^2\sqrt{c+dx}}{4(ad-bc)} + \frac{3bd^2(c+dx)^{3/2}}{4(ad-bc)^2}}{b^2(c+dx)^2 - (2b^2c - 2abd)(c+dx) + a^2d^2 + b^2c^2 - 2abcd} + \frac{3d^2 \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{4\sqrt{b}(ad-bc)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^3*(c + d*x)^(1/2)),x)`

[Out] $((5*d^2*(c + d*x)^{(1/2)})/(4*(a*d - b*c)) + (3*b*d^2*(c + d*x)^{(3/2)})/(4*(a*d - b*c)^2))/(b^2*(c + d*x)^2 - (2*b^2*c - 2*a*b*d)*(c + d*x) + a^2*d^2 + b^2*c^2 - 2*a*b*c*d) + (3*d^2*\operatorname{atan}((b^{(1/2)}*(c + d*x)^{(1/2)})/(a*d - b*c)^{(1/2)}))/(4*b^{(1/2)}*(a*d - b*c)^{(5/2)})$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**3/(d*x+c)**(1/2),x)`

[Out] Timed out

$$3.1422 \quad \int \frac{1}{(a+bx)^4 \sqrt{c+dx}} dx$$

Optimal. Leaf size=147

$$\frac{5d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8\sqrt{b}(bc-ad)^{7/2}} - \frac{5d^2\sqrt{c+dx}}{8(a+bx)(bc-ad)^3} + \frac{5d\sqrt{c+dx}}{12(a+bx)^2(bc-ad)^2} - \frac{\sqrt{c+dx}}{3(a+bx)^3(bc-ad)}$$

[Out] $5/8*d^3*\arctanh(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/(-a*d+b*c)^{(7/2)}/b^{(1/2)}-1/3*(d*x+c)^{(1/2)/(-a*d+b*c)/(b*x+a)^3+5/12*d*(d*x+c)^{(1/2)/(-a*d+b*c)^2/(b*x+a)^2-5/8*d^2*(d*x+c)^{(1/2)/(-a*d+b*c)^3/(b*x+a)}$

Rubi [A] time = 0.05, antiderivative size = 147, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$-\frac{5d^2\sqrt{c+dx}}{8(a+bx)(bc-ad)^3} + \frac{5d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8\sqrt{b}(bc-ad)^{7/2}} + \frac{5d\sqrt{c+dx}}{12(a+bx)^2(bc-ad)^2} - \frac{\sqrt{c+dx}}{3(a+bx)^3(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^4*Sqrt[c + d*x]),x]

[Out] $-\text{Sqrt}[c + d*x]/(3*(b*c - a*d)*(a + b*x)^3) + (5*d*\text{Sqrt}[c + d*x])/(12*(b*c - a*d)^2*(a + b*x)^2) - (5*d^2*\text{Sqrt}[c + d*x])/(8*(b*c - a*d)^3*(a + b*x)) + (5*d^3*\text{ArcTanh}[(\text{Sqrt}[b]*\text{Sqrt}[c + d*x])/\text{Sqrt}[b*c - a*d]])/(8*\text{Sqrt}[b]*(b*c - a*d)^{(7/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^4 \sqrt{c+dx}} dx &= -\frac{\sqrt{c+dx}}{3(bc-ad)(a+bx)^3} - \frac{(5d) \int \frac{1}{(a+bx)^3 \sqrt{c+dx}} dx}{6(bc-ad)} \\
 &= -\frac{\sqrt{c+dx}}{3(bc-ad)(a+bx)^3} + \frac{5d\sqrt{c+dx}}{12(bc-ad)^2(a+bx)^2} + \frac{(5d^2) \int \frac{1}{(a+bx)^2 \sqrt{c+dx}} dx}{8(bc-ad)^2} \\
 &= -\frac{\sqrt{c+dx}}{3(bc-ad)(a+bx)^3} + \frac{5d\sqrt{c+dx}}{12(bc-ad)^2(a+bx)^2} - \frac{5d^2\sqrt{c+dx}}{8(bc-ad)^3(a+bx)} - \frac{(5d^3) \int \frac{1}{(a+bx)} dx}{16(bc-ad)^3} \\
 &= -\frac{\sqrt{c+dx}}{3(bc-ad)(a+bx)^3} + \frac{5d\sqrt{c+dx}}{12(bc-ad)^2(a+bx)^2} - \frac{5d^2\sqrt{c+dx}}{8(bc-ad)^3(a+bx)} - \frac{(5d^2) \text{Subst}\left(\int \frac{1}{u} du, u, a+bx\right)}{16(bc-ad)^3} \\
 &= -\frac{\sqrt{c+dx}}{3(bc-ad)(a+bx)^3} + \frac{5d\sqrt{c+dx}}{12(bc-ad)^2(a+bx)^2} - \frac{5d^2\sqrt{c+dx}}{8(bc-ad)^3(a+bx)} + \frac{5d^3 \tanh^{-1}\left(\frac{d(a+bx)}{\sqrt{c+dx}}\right)}{8\sqrt{b}(bc-ad)^3}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.34

$$\frac{2d^3\sqrt{c+dx} {}_2F_1\left(\frac{1}{2}, 4; \frac{3}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{(ad-bc)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^4*Sqrt[c + d*x]), x]

[Out] (2*d^3*Sqrt[c + d*x]*Hypergeometric2F1[1/2, 4, 3/2, -((b*(c + d*x))/(-b*c) + a*d)))/(-b*c) + a*d)^4

fricas [B] time = 0.47, size = 884, normalized size = 6.01

$$\left[\frac{15(b^3d^3x^3 + 3ab^2d^3x^2 + 3a^2bd^3x + a^3d^3)\sqrt{b^2c - abd} \log\left(\frac{bdx + 2bc - ad - 2\sqrt{b^2c - abd}\sqrt{dx+c}}{bx+a}\right) + 2(8a^3b^5c^4 - 4a^4b^4c^3d + 6a^5b^3c^2d^2 - 4a^6b^2cd^3 + a^7bd^4 + (b^8c^4 - 4ab^7c^3d + 6a^2b^6c^2d^2 - 4a^3b^5cd^3 + a^4b^4d^4)}{48(a^3b^5c^4 - 4a^4b^4c^3d + 6a^5b^3c^2d^2 - 4a^6b^2cd^3 + a^7bd^4 + (b^8c^4 - 4ab^7c^3d + 6a^2b^6c^2d^2 - 4a^3b^5cd^3 + a^4b^4d^4)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^4/(d*x+c)^(1/2),x, algorithm="fricas")

[Out]
$$\begin{aligned} & [-1/48*(15*(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)*\sqrt{b^2*c - a*b*d})\log((b*d*x + 2*b*c - a*d - 2*\sqrt{b^2*c - a*b*d})*\sqrt{d*x + c})/(b*x + a) + 2*(8*b^4*c^3 - 34*a*b^3*c^2*d + 59*a^2*b^2*c*d^2 - 33*a^3*b*d^3 + 15*(b^4*c*d^2 - a*b^3*d^3)*x^2 - 10*(b^4*c^2*d - 5*a*b^3*c*d^2 + 4*a^2*b^2*d^3)*x)*\sqrt{d*x + c})/(a^3*b^5*c^4 - 4*a^4*b^4*c^3*d + 6*a^5*b^3*c^2*d^2 - 4*a^6*b^2*c*d^3 + a^7*b*d^4 + (b^8*c^4 - 4*a*b^7*c^3*d + 6*a^2*b^6*c^2*d^2 - 4*a^3*b^5*c*d^3 + a^4*b^4*d^4)*x^3 + 3*(a*b^7*c^4 - 4*a^2*b^6*c^3*d + 6*a^3*b^5*c^2*d^2 - 4*a^4*b^4*c*d^3 + a^5*b^3*d^4)*x^2 + 3*(a^2*b^6*c^4 - 4*a^3*b^5*c^3*d + 6*a^4*b^4*c^2*d^2 - 4*a^5*b^3*c*d^3 + a^6*b^2*d^4)*x) \\ & , -1/24*(15*(b^3*d^3*x^3 + 3*a*b^2*d^3*x^2 + 3*a^2*b*d^3*x + a^3*d^3)*\sqrt{-b^2*c + a*b*d})*\arctan(\sqrt{-b^2*c + a*b*d})*\sqrt{d*x + c}/(b*d*x + b*c) + (8*b^4*c^3 - 34*a*b^3*c^2*d + 59*a^2*b^2*c*d^2 - 33*a^3*b*d^3 + 15*(b^4*c*d^2 - a*b^3*d^3)*x^2 - 10*(b^4*c^2*d - 5*a*b^3*c*d^2 + 4*a^2*b^2*d^3)*x)*\sqrt{d*x + c})/(a^3*b^5*c^4 - 4*a^4*b^4*c^3*d + 6*a^5*b^3*c^2*d^2 - 4*a^6*b^2*c*d^3 + a^7*b*d^4 + (b^8*c^4 - 4*a*b^7*c^3*d + 6*a^2*b^6*c^2*d^2 - 4*a^3*b^5*c*d^3 + a^4*b^4*d^4)*x^3 + 3*(a*b^7*c^4 - 4*a^2*b^6*c^3*d + 6*a^3*b^5*c^2*d^2 - 4*a^4*b^4*c*d^3 + a^5*b^3*d^4)*x^2 + 3*(a^2*b^6*c^4 - 4*a^3*b^5*c^3*d + 6*a^4*b^4*c^2*d^2 - 4*a^5*b^3*c*d^3 + a^6*b^2*d^4)*x) \end{aligned}$$

giac [A] time = 1.02, size = 231, normalized size = 1.57

$$\frac{5d^3 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{8(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)\sqrt{-b^2c + abd}} - \frac{15(dx+c)^{\frac{5}{2}}b^2d^3 - 40(dx+c)^{\frac{3}{2}}b^2cd^3 + 33\sqrt{dx+c}b^2c^2d^3}{24(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^4/(d*x+c)^(1/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & -5/8*d^3*\arctan(\sqrt{d*x + c})*b/\sqrt{-b^2*c + a*b*d})/((b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*\sqrt{-b^2*c + a*b*d}) - 1/24*(15*(d*x + c)^{(5/2)}*b^2*d^3 - 40*(d*x + c)^{(3/2)}*b^2*c*d^3 + 33*\sqrt{d*x + c}*b^2*c^2*d^3 + 40*(d*x + c)^{(3/2)}*a*b*d^4 - 66*\sqrt{d*x + c}*a*b*c*d^4 + 33*\sqrt{d*x + c}*a^2*d^5)/((b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*((d*x + c)*b - b*c + a*d)^3) \end{aligned}$$

maple [A] time = 0.01, size = 147, normalized size = 1.00

$$\frac{5d^3 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{(ad-bc)b}}\right)}{8(ad-bc)^3 \sqrt{(ad-bc)b}} + \frac{\sqrt{dx+c} d^3}{3(ad-bc)(bdx+ad)^3} + \frac{5\sqrt{dx+c} d^3}{12(ad-bc)^2 (bdx+ad)^2} + \frac{5\sqrt{dx+c} d^3}{8(ad-bc)^3 (bdx+ad)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^4/(d*x+c)^(1/2),x)`

[Out] $\frac{1}{3}d^3(d*x+c)^{(1/2)}/(a*d-b*c)/(b*d*x+a*d)^3 + \frac{5}{12}d^3/(a*d-b*c)^2*(d*x+c)^{(1/2)}/(b*d*x+a*d)^2 + \frac{5}{8}d^3/(a*d-b*c)^3*(d*x+c)^{(1/2)}/(b*d*x+a*d) + \frac{5}{8}d^3/(a*d-b*c)^3/((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^4/(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.39, size = 218, normalized size = 1.48

$$\frac{\frac{11d^3\sqrt{c+dx}}{8(a-d-bc)} + \frac{5b^2d^3(c+dx)^{5/2}}{8(a-d-bc)^3} + \frac{5bd^3(c+dx)^{3/2}}{3(a-d-bc)^2}}{(c+dx)(3a^2bd^2 - 6ab^2cd + 3b^3c^2) + b^3(c+dx)^3 - (3b^3c - 3ab^2d)(c+dx)^2 + a^3d^3 - b^3c^3 + 3ab^2c^2d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^4*(c + d*x)^(1/2)),x)`

[Out] $((11*d^3*(c + d*x)^{(1/2)})/(8*(a*d - b*c)) + (5*b^2*d^3*(c + d*x)^{(5/2)})/(8*(a*d - b*c)^3) + (5*b*d^3*(c + d*x)^{(3/2)})/(3*(a*d - b*c)^2))/((c + d*x)*(3*b^3*c^2 + 3*a^2*b*d^2 - 6*a*b^2*c*d) + b^3*(c + d*x)^3 - (3*b^3*c - 3*a*b^2*d)*(c + d*x)^2 + a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2) + (5*d^3*\operatorname{atan}((b^{(1/2)}*(c + d*x)^{(1/2)})/(a*d - b*c)^{(1/2)}))/(8*b^{(1/2)}*(a*d - b*c)^{(7/2)})$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**4/(d*x+c)**(1/2),x)`

[Out] Timed out

$$3.1423 \quad \int \frac{1}{(a+bx)^5 \sqrt{c+dx}} dx$$

Optimal. Leaf size=180

$$-\frac{35d^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{64\sqrt{b}(bc-ad)^{9/2}} + \frac{35d^3\sqrt{c+dx}}{64(a+bx)(bc-ad)^4} - \frac{35d^2\sqrt{c+dx}}{96(a+bx)^2(bc-ad)^3} + \frac{7d\sqrt{c+dx}}{24(a+bx)^3(bc-ad)^2} - \frac{\sqrt{c+dx}}{4(a+bx)^4(bc-ad)}$$

[Out] $-35/64*d^4*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)}/(-a*d+b*c)^{(1/2)})/(-a*d+b*c)^{(9/2)}/b^{(1/2)}-1/4*(d*x+c)^{(1/2)}/(-a*d+b*c)/(b*x+a)^4+7/24*d*(d*x+c)^{(1/2)}/(-a*d+b*c)^2/(b*x+a)^3-35/96*d^2*(d*x+c)^{(1/2)}/(-a*d+b*c)^3/(b*x+a)^2+35/64*d^3*(d*x+c)^{(1/2)}/(-a*d+b*c)^4/(b*x+a)$

Rubi [A] time = 0.06, antiderivative size = 180, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$\frac{35d^3\sqrt{c+dx}}{64(a+bx)(bc-ad)^4} - \frac{35d^2\sqrt{c+dx}}{96(a+bx)^2(bc-ad)^3} - \frac{35d^4 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{64\sqrt{b}(bc-ad)^{9/2}} + \frac{7d\sqrt{c+dx}}{24(a+bx)^3(bc-ad)^2} - \frac{\sqrt{c+dx}}{4(a+bx)^4(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^5*Sqrt[c + d*x]),x]

[Out] $-\operatorname{Sqrt}[c + d*x]/(4*(b*c - a*d)*(a + b*x)^4) + (7*d*\operatorname{Sqrt}[c + d*x])/(24*(b*c - a*d)^2*(a + b*x)^3) - (35*d^2*\operatorname{Sqrt}[c + d*x])/(96*(b*c - a*d)^3*(a + b*x)^2) + (35*d^3*\operatorname{Sqrt}[c + d*x])/(64*(b*c - a*d)^4*(a + b*x)) - (35*d^4*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/\operatorname{Sqrt}[b*c - a*d]])/(64*\operatorname{Sqrt}[b]*(b*c - a*d)^{(9/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^5 \sqrt{c+dx}} dx &= -\frac{\sqrt{c+dx}}{4(bc-ad)(a+bx)^4} - \frac{(7d) \int \frac{1}{(a+bx)^4 \sqrt{c+dx}} dx}{8(bc-ad)} \\
 &= -\frac{\sqrt{c+dx}}{4(bc-ad)(a+bx)^4} + \frac{7d\sqrt{c+dx}}{24(bc-ad)^2(a+bx)^3} + \frac{(35d^2) \int \frac{1}{(a+bx)^3 \sqrt{c+dx}} dx}{48(bc-ad)^2} \\
 &= -\frac{\sqrt{c+dx}}{4(bc-ad)(a+bx)^4} + \frac{7d\sqrt{c+dx}}{24(bc-ad)^2(a+bx)^3} - \frac{35d^2\sqrt{c+dx}}{96(bc-ad)^3(a+bx)^2} - \frac{(35d^3) \int \frac{1}{(a+bx)^2 \sqrt{c+dx}} dx}{64(bc-ad)^3} \\
 &= -\frac{\sqrt{c+dx}}{4(bc-ad)(a+bx)^4} + \frac{7d\sqrt{c+dx}}{24(bc-ad)^2(a+bx)^3} - \frac{35d^2\sqrt{c+dx}}{96(bc-ad)^3(a+bx)^2} + \frac{35d^3\sqrt{c+dx}}{64(bc-ad)^3} \\
 &= -\frac{\sqrt{c+dx}}{4(bc-ad)(a+bx)^4} + \frac{7d\sqrt{c+dx}}{24(bc-ad)^2(a+bx)^3} - \frac{35d^2\sqrt{c+dx}}{96(bc-ad)^3(a+bx)^2} + \frac{35d^3\sqrt{c+dx}}{64(bc-ad)^3} \\
 &= -\frac{\sqrt{c+dx}}{4(bc-ad)(a+bx)^4} + \frac{7d\sqrt{c+dx}}{24(bc-ad)^2(a+bx)^3} - \frac{35d^2\sqrt{c+dx}}{96(bc-ad)^3(a+bx)^2} + \frac{35d^3\sqrt{c+dx}}{64(bc-ad)^3}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.28

$$\frac{2d^4\sqrt{c+dx} {}_2F_1\left(\frac{1}{2}, 5; \frac{3}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{(ad-bc)^5}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^5*Sqrt[c + d*x]),x]

[Out] (2*d^4*Sqrt[c + d*x]*Hypergeometric2F1[1/2, 5, 3/2, -((b*(c + d*x))/(-b*c + a*d))])/(-b*c + a*d)^5

fricas [B] time = 0.48, size = 1325, normalized size = 7.36

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^5/(d*x+c)^(1/2),x, algorithm="fricas")

[Out] [1/384*(105*(b^4*d^4*x^4 + 4*a*b^3*d^4*x^3 + 6*a^2*b^2*d^4*x^2 + 4*a^3*b*d^4*x + a^4*d^4)*sqrt(b^2*c - a*b*d)*log((b*d*x + 2*b*c - a*d - 2*sqrt(b^2*c - a*b*d)*sqrt(d*x + c))/(b*x + a)) - 2*(48*b^5*c^4 - 248*a*b^4*c^3*d + 526*a^2*b^3*c^2*d^2 - 605*a^3*b^2*c*d^3 + 279*a^4*b*d^4 - 105*(b^5*c*d^3 - a*b^4*d^4)*x^3 + 35*(2*b^5*c^2*d^2 - 13*a*b^4*c*d^3 + 11*a^2*b^3*d^4)*x^2 - 7*(8*b^5*c^3*d - 44*a*b^4*c^2*d^2 + 109*a^2*b^3*c*d^3 - 73*a^3*b^2*d^4)*x)*sqrt(d*x + c))/(a^4*b^6*c^5 - 5*a^5*b^5*c^4*d + 10*a^6*b^4*c^3*d^2 - 10*a^7*b^3*c^2*d^3 + 5*a^8*b^2*c*d^4 - a^9*b*d^5 + (b^10*c^5 - 5*a*b^9*c^4*d + 10*a^2*b^8*c^3*d^2 - 10*a^3*b^7*c^2*d^3 + 5*a^4*b^6*c*d^4 - a^5*b^5*d^5)*x^4 + 4*(a*b^9*c^5 - 5*a^2*b^8*c^4*d + 10*a^3*b^7*c^3*d^2 - 10*a^4*b^6*c^2*d^3 + 5*a^5*b^5*c*d^4 - a^6*b^4*d^5)*x^3 + 6*(a^2*b^8*c^5 - 5*a^3*b^7*c^4*d + 10*a^4*b^6*c^3*d^2 - 10*a^5*b^5*c^2*d^3 + 5*a^6*b^4*c*d^4 - a^7*b^3*d^5)*x^2 + 4*(a^3*b^7*c^5 - 5*a^4*b^6*c^4*d + 10*a^5*b^5*c^3*d^2 - 10*a^6*b^4*c^2*d^3 + 5*a^7*b^3*c*d^4 - a^8*b^2*d^5)*x), 1/192*(105*(b^4*d^4*x^4 + 4*a*b^3*d^4*x^3 + 6*a^2*b^2*d^4*x^2 + 4*a^3*b*d^4*x + a^4*d^4)*sqrt(-b^2*c + a*b*d)*arctan(sqrt(-b^2*c + a*b*d)*sqrt(d*x + c)/(b*d*x + b*c)) - (48*b^5*c^4 - 248*a*b^4*c^3*d + 526*a^2*b^3*c^2*d^2 - 605*a^3*b^2*c*d^3 + 279*a^4*b*d^4 - 105*(b^5*c*d^3 - a*b^4*d^4)*x^3 + 35*(2*b^5*c^2*d^2 - 13*a*b^4*c*d^3 + 11*a^2*b^3*d^4)*x^2 - 7*(8*b^5*c^3*d - 44*a*b^4*c^2*d^2 + 109*a^2*b^3*c*d^3 - 73*a^3*b^2*d^4)*x)*sqrt(d*x + c))/(a^4*b^6*c^5 - 5*a^5*b^5*c^4*d + 10*a^6*b^4*c^3*d^2 - 10*a^7*b^3*c^2*d^3 + 5*a^8*b^2*c*d^4 - a^9*b*d^5 + (b^10*c^5 - 5*a*b^9*c^4*d + 10*a^2*b^8*c^3*d^2 - 10*a^3*b^7*c^2*d^3 + 5*a^4*b^6*c*d^4 - a^5*b^5*d^5)*x^4 + 4*(a*b^9*c^5 - 5*a^2*b^8*c^4*d + 10*a^3*b^7*c^3*d^2 - 10*a^4*b^6*c^2*d^3 + 5*a^5*b^5*c*d^4 - a^6*b^4*d^5)*x^3 + 6*(a^2*b^8*c^5 - 5*a^3*b^7*c^4*d + 10*a^4*b^6*c^3*d^2 - 10*a^5*b^5*c^2*d^3 + 5*a^6*b^4*c*d^4 - a^7*b^3*d^5)*x^2 + 4*(a^3*b^7*c^5 - 5*a^4*b^6*c^4*d + 10*a^5*b^5*c^3*d^2 - 10*a^6*b^4*c^2*d^3 + 5*a^7*b^3*c*d^4 - a^8*b^2*d^5)*x)]

giac [B] time = 1.13, size = 331, normalized size = 1.84

$$\frac{35 d^4 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{64 (b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4)\sqrt{-b^2c+abd}} + \frac{105(dx+c)^{\frac{7}{2}}b^3d^4 - 385(dx+c)^{\frac{5}{2}}b^3cd^4 + 511}{64 (b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4)\sqrt{-b^2c+abd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^5/(d*x+c)^(1/2),x, algorithm="giac")


```
[Out] 35/64*d^4*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*sqrt(-b^2*c + a*b*d))
+ 1/192*(105*(d*x + c)^(7/2)*b^3*d^4 - 385*(d*x + c)^(5/2)*b^3*c*d^4 + 511*(d*x + c)^(3/2)*b^3*c^2*d^4 - 279*sqrt(d*x + c)*b^3*c^3*d^4 + 385*(d*x + c)^(5/2)*a*b^2*d^5 - 1022*(d*x + c)^(3/2)*a*b^2*c*d^5 + 837*sqrt(d*x + c)*a*b^2*c^2*d^5 + 511*(d*x + c)^(3/2)*a^2*b*d^6 - 837*sqrt(d*x + c)*a^2*b*c*d^6 + 279*sqrt(d*x + c)*a^3*d^7)/((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*((d*x + c)*b - b*c + a*d)^4)
```

maple [A] time = 0.01, size = 179, normalized size = 0.99

$$\frac{35d^4 \arctan\left(\frac{\sqrt{dx+c} b}{\sqrt{(ad-bc)b}}\right)}{64(ad-bc)^4 \sqrt{(ad-bc)b}} + \frac{\sqrt{dx+c} d^4}{4(ad-bc)(bdx+ad)^4} + \frac{7\sqrt{dx+c} d^4}{24(ad-bc)^2(bdx+ad)^3} + \frac{35\sqrt{dx+c} d^4}{96(ad-bc)^3(bdx+ad)^2} + \frac{1}{64(ad-bc)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(b*x+a)^5/(d*x+c)^(1/2),x)
```

```
[Out] 1/4*d^4*(d*x+c)^(1/2)/(a*d-b*c)/(b*d*x+a*d)^4+7/24*d^4/(a*d-b*c)^2*(d*x+c)^(1/2)/(b*d*x+a*d)^3+35/96*d^4/(a*d-b*c)^3*(d*x+c)^(1/2)/(b*d*x+a*d)^2+35/64*d^4/(a*d-b*c)^4*(d*x+c)^(1/2)/(b*d*x+a*d)+35/64*d^4/(a*d-b*c)^4/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)^5/(d*x+c)^(1/2),x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?
```

mupad [B] time = 0.46, size = 307, normalized size = 1.71

$$\frac{93d^4 \sqrt{c+dx}}{64(ad-bc)} + \frac{385b^2 d^4 (c+dx)^{5/2}}{192(ad-bc)^3} + \frac{35b^3 d^4 (c+dx)^{3/2}}{64(ad-bc)} + \frac{b^4 (c+dx)^4 - (4b^4 c - 4ab^3 d)(c+dx)^3 - (c+dx)(-4a^3 b d^3 + 12a^2 b^2 c d^2 - 12ab^3 c^2 d + 4b^4 c^3) + a^4 d^4}{(b^4 c^4 - 4a^3 b^3 c^3 d + 6a^2 b^2 c^2 d^2 - 4a^3 b c d^3 + a^4 d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a + b*x)^5*(c + d*x)^(1/2)),x)
```

```
[Out] ((93*d^4*(c + d*x)^(1/2))/(64*(a*d - b*c)) + (385*b^2*d^4*(c + d*x)^(5/2))/
(192*(a*d - b*c)^3) + (35*b^3*d^4*(c + d*x)^(7/2))/(64*(a*d - b*c)^4) + (51
1*b*d^4*(c + d*x)^(3/2))/(192*(a*d - b*c)^2))/(b^4*(c + d*x)^4 - (4*b^4*c -
4*a*b^3*d)*(c + d*x)^3 - (c + d*x)*(4*b^4*c^3 - 4*a^3*b*d^3 + 12*a^2*b^2*c
*d^2 - 12*a*b^3*c^2*d) + a^4*d^4 + b^4*c^4 + (c + d*x)^2*(6*b^4*c^2 + 6*a^2
*b^2*d^2 - 12*a*b^3*c*d) + 6*a^2*b^2*c^2*d^2 - 4*a*b^3*c^3*d - 4*a^3*b*c*d^
3) + (35*d^4*atan((b^(1/2)*(c + d*x)^(1/2))/(a*d - b*c)^(1/2)))/(64*b^(1/2)
*(a*d - b*c)^(9/2))
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**5/(d*x+c)**(1/2),x)
```

```
[Out] Timed out
```

$$3.1424 \quad \int \frac{(a+bx)^5}{(c+dx)^{3/2}} dx$$

Optimal. Leaf size=152

$$-\frac{10b^4(c+dx)^{7/2}(bc-ad)}{7d^6} + \frac{4b^3(c+dx)^{5/2}(bc-ad)^2}{d^6} - \frac{20b^2(c+dx)^{3/2}(bc-ad)^3}{3d^6} + \frac{10b\sqrt{c+dx}(bc-ad)^4}{d^6} + \frac{2(bc-ad)^5}{d^6\sqrt{c+dx}}$$

[Out] $-20/3*b^2*(-a*d+b*c)^3*(d*x+c)^{(3/2)}/d^6+4*b^3*(-a*d+b*c)^2*(d*x+c)^{(5/2)}/d^6-10/7*b^4*(-a*d+b*c)*(d*x+c)^{(7/2)}/d^6+2/9*b^5*(d*x+c)^{(9/2)}/d^6+2*(-a*d+b*c)^5/d^6/(d*x+c)^{(1/2)}+10*b*(-a*d+b*c)^4*(d*x+c)^{(1/2)}/d^6$

Rubi [A] time = 0.05, antiderivative size = 152, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{10b^4(c+dx)^{7/2}(bc-ad)}{7d^6} + \frac{4b^3(c+dx)^{5/2}(bc-ad)^2}{d^6} - \frac{20b^2(c+dx)^{3/2}(bc-ad)^3}{3d^6} + \frac{10b\sqrt{c+dx}(bc-ad)^4}{d^6} + \frac{2(bc-ad)^5}{d^6\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(c + d*x)^(3/2), x]

[Out] $(2*(b*c - a*d)^5)/(d^6*\text{Sqrt}[c + d*x]) + (10*b*(b*c - a*d)^4*\text{Sqrt}[c + d*x])/d^6 - (20*b^2*(b*c - a*d)^3*(c + d*x)^{(3/2)})/(3*d^6) + (4*b^3*(b*c - a*d)^2*(c + d*x)^{(5/2)})/d^6 - (10*b^4*(b*c - a*d)*(c + d*x)^{(7/2)})/(7*d^6) + (2*b^5*(c + d*x)^{(9/2)})/(9*d^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^5}{(c+dx)^{3/2}} dx = \int \left(\frac{(-bc+ad)^5}{d^5(c+dx)^{3/2}} + \frac{5b(bc-ad)^4}{d^5\sqrt{c+dx}} - \frac{10b^2(bc-ad)^3\sqrt{c+dx}}{d^5} + \frac{10b^3(bc-ad)^2(c+dx)^{3/2}}{d^5} - \frac{5b^4(bc-ad)(c+dx)^{5/2}}{d^5} \right) dx$$

$$= \frac{2(bc-ad)^5}{d^6\sqrt{c+dx}} + \frac{10b(bc-ad)^4\sqrt{c+dx}}{d^6} - \frac{20b^2(bc-ad)^3(c+dx)^{3/2}}{3d^6} + \frac{4b^3(bc-ad)^2(c+dx)^{5/2}}{d^6} - \frac{5b^4(bc-ad)(c+dx)^{7/2}}{7d^6}$$

Mathematica [A] time = 0.12, size = 123, normalized size = 0.81

$$\frac{2\left(-45b^4(c+dx)^4(bc-ad) + 126b^3(c+dx)^3(bc-ad)^2 - 210b^2(c+dx)^2(bc-ad)^3 + 315b(c+dx)(bc-ad)^4 + 63b^5(c+dx)^5\right)}{63d^6\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(c + d*x)^(3/2), x]

[Out] (2*(63*(b*c - a*d)^5 + 315*b*(b*c - a*d)^4*(c + d*x) - 210*b^2*(b*c - a*d)^3*(c + d*x)^2 + 126*b^3*(b*c - a*d)^2*(c + d*x)^3 - 45*b^4*(b*c - a*d)*(c + d*x)^4 + 7*b^5*(c + d*x)^5)/(63*d^6*Sqrt[c + d*x])

fricas [B] time = 0.42, size = 271, normalized size = 1.78

$$\frac{2\left(7b^5d^5x^5 + 256b^5c^5 - 1152ab^4c^4d + 2016a^2b^3c^3d^2 - 1680a^3b^2c^2d^3 + 630a^4bcd^4 - 63a^5d^5 - 5\left(2b^5cd^4 - 9ab^4c^4d\right)\right)}{\sqrt{dx+c}d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^(3/2), x, algorithm="fricas")

[Out] 2/63*(7*b^5*d^5*x^5 + 256*b^5*c^5 - 1152*a*b^4*c^4*d + 2016*a^2*b^3*c^3*d^2 - 1680*a^3*b^2*c^2*d^3 + 630*a^4*b*c*d^4 - 63*a^5*d^5 - 5*(2*b^5*c*d^4 - 9*a*b^4*d^5)*x^4 + 2*(8*b^5*c^2*d^3 - 36*a*b^4*c*d^4 + 63*a^2*b^3*d^5)*x^3 - 2*(16*b^5*c^3*d^2 - 72*a*b^4*c^2*d^3 + 126*a^2*b^3*c*d^4 - 105*a^3*b^2*d^5)*x^2 + (128*b^5*c^4*d - 576*a*b^4*c^3*d^2 + 1008*a^2*b^3*c^2*d^3 - 840*a^3*b^2*c*d^4 + 315*a^4*b*d^5)*x)*sqrt(d*x + c)/(d^7*x + c*d^6)

giac [B] time = 1.01, size = 350, normalized size = 2.30

$$\frac{2\left(b^5c^5 - 5ab^4c^4d + 10a^2b^3c^3d^2 - 10a^3b^2c^2d^3 + 5a^4bcd^4 - a^5d^5\right)}{\sqrt{dx+c}d^6} + \frac{2\left(7(dx+c)^{\frac{9}{2}}b^5d^{48} - 45(dx+c)^{\frac{7}{2}}b^5cd^{48} + 126(dx+c)^{\frac{5}{2}}b^5c^2d^{48} - 210(dx+c)^{\frac{3}{2}}b^5c^3d^{48} + 315\sqrt{dx+c}b^5c^4d^{48} + 45(dx+c)^{\frac{7}{2}}a*b^4*d^{49} - 252(dx+c)^{\frac{5}{2}}a*b^4*c*d^{49} + 630(dx+c)^{\frac{3}{2}}a*b^4*c^2*d^{49} - 1260\sqrt{dx+c}a*b^4*c^3*d^{49} + 126(dx+c)^{\frac{5}{2}}a^2*b^3*d^{50} - 630(dx+c)^{\frac{3}{2}}a^2*b^3*c*d^{50} + 1890\sqrt{dx+c}a^2*b^3*c^2*d^{50} - 1890a^2*b^3*c^3*d^{50} + 1890a^2*b^3*c^4*d^{50} - 1890a^2*b^3*d^{51}\right)}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^(3/2), x, algorithm="giac")

[Out] 2*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)/(sqrt(d*x + c)*d^6) + 2/63*(7*(d*x + c)^(9/2)*b^5*d^48 - 45*(d*x + c)^(7/2)*b^5*c*d^48 + 126*(d*x + c)^(5/2)*b^5*c^2*d^48 - 210*(d*x + c)^(3/2)*b^5*c^3*d^48 + 315*sqrt(d*x + c)*b^5*c^4*d^48 + 45*(d*x + c)^(7/2)*a*b^4*d^49 - 252*(d*x + c)^(5/2)*a*b^4*c*d^49 + 630*(d*x + c)^(3/2)*a*b^4*c^2*d^49 - 1260*sqrt(d*x + c)*a*b^4*c^3*d^49 + 126*(d*x + c)^(5/2)*a^2*b^3*d^50 - 630*(d*x + c)^(3/2)*a^2*b^3*c*d^50 + 1890*sqrt(d*x + c)*a^2*b^3*c^2*d^50 - 1890a^2*b^3*c^3*d^50 + 1890a^2*b^3*c^4*d^50 - 1890a^2*b^3*d^51)


```
[Out] (2*b^5*(c + d*x)^(9/2))/(9*d^6) - ((10*b^5*c - 10*a*b^4*d)*(c + d*x)^(7/2))
/(7*d^6) - (2*a^5*d^5 - 2*b^5*c^5 - 20*a^2*b^3*c^3*d^2 + 20*a^3*b^2*c^2*d^3
+ 10*a*b^4*c^4*d - 10*a^4*b*c*d^4)/(d^6*(c + d*x)^(1/2)) + (20*b^2*(a*d -
b*c)^3*(c + d*x)^(3/2))/(3*d^6) + (4*b^3*(a*d - b*c)^2*(c + d*x)^(5/2))/d^6
+ (10*b*(a*d - b*c)^4*(c + d*x)^(1/2))/d^6
```

sympy [A] time = 47.94, size = 243, normalized size = 1.60

$$\frac{2b^5(c+dx)^{\frac{9}{2}}}{9d^6} + \frac{(c+dx)^{\frac{7}{2}}(10ab^4d-10b^5c)}{7d^6} + \frac{(c+dx)^{\frac{5}{2}}(20a^2b^3d^2-40ab^4cd+20b^5c^2)}{5d^6} + \frac{(c+dx)^{\frac{3}{2}}(20a^3b^2d^3-60a^2b^3cd+10ab^4c^2)}{3d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**5/(d*x+c)**(3/2),x)
```

```
[Out] 2*b**5*(c + d*x)**(9/2)/(9*d**6) + (c + d*x)**(7/2)*(10*a*b**4*d - 10*b**5*
c)/(7*d**6) + (c + d*x)**(5/2)*(20*a**2*b**3*d**2 - 40*a*b**4*c*d + 20*b**5
*c**2)/(5*d**6) + (c + d*x)**(3/2)*(20*a**3*b**2*d**3 - 60*a**2*b**3*c*d**2
+ 60*a*b**4*c**2*d - 20*b**5*c**3)/(3*d**6) + sqrt(c + d*x)*(10*a**4*b*d**
4 - 40*a**3*b**2*c*d**3 + 60*a**2*b**3*c**2*d**2 - 40*a*b**4*c**3*d + 10*b*
*5*c**4)/d**6 - 2*(a*d - b*c)**5/(d**6*sqrt(c + d*x))
```

$$3.1425 \quad \int \frac{(a+bx)^4}{(c+dx)^{3/2}} dx$$

Optimal. Leaf size=123

$$-\frac{8b^3(c+dx)^{5/2}(bc-ad)}{5d^5} + \frac{4b^2(c+dx)^{3/2}(bc-ad)^2}{d^5} - \frac{8b\sqrt{c+dx}(bc-ad)^3}{d^5} - \frac{2(bc-ad)^4}{d^5\sqrt{c+dx}} + \frac{2b^4(c+dx)^{7/2}}{7d^5}$$

[Out] $4*b^2*(-a*d+b*c)^2*(d*x+c)^(3/2)/d^5-8/5*b^3*(-a*d+b*c)*(d*x+c)^(5/2)/d^5+2/7*b^4*(d*x+c)^(7/2)/d^5-2*(-a*d+b*c)^4/d^5/(d*x+c)^(1/2)-8*b*(-a*d+b*c)^3*(d*x+c)^(1/2)/d^5$

Rubi [A] time = 0.04, antiderivative size = 123, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{8b^3(c+dx)^{5/2}(bc-ad)}{5d^5} + \frac{4b^2(c+dx)^{3/2}(bc-ad)^2}{d^5} - \frac{8b\sqrt{c+dx}(bc-ad)^3}{d^5} - \frac{2(bc-ad)^4}{d^5\sqrt{c+dx}} + \frac{2b^4(c+dx)^{7/2}}{7d^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4/(c + d*x)^(3/2), x]

[Out] $(-2*(b*c - a*d)^4)/(d^5*\text{Sqrt}[c + d*x]) - (8*b*(b*c - a*d)^3*\text{Sqrt}[c + d*x])/d^5 + (4*b^2*(b*c - a*d)^2*(c + d*x)^(3/2))/d^5 - (8*b^3*(b*c - a*d)*(c + d*x)^(5/2))/(5*d^5) + (2*b^4*(c + d*x)^(7/2))/(7*d^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^4}{(c+dx)^{3/2}} dx &= \int \left(\frac{(-bc+ad)^4}{d^4(c+dx)^{3/2}} - \frac{4b(bc-ad)^3}{d^4\sqrt{c+dx}} + \frac{6b^2(bc-ad)^2\sqrt{c+dx}}{d^4} - \frac{4b^3(bc-ad)(c+dx)^{3/2}}{d^4} + \frac{b^4(c+dx)^{5/2}}{d^4} \right) dx \\ &= -\frac{2(bc-ad)^4}{d^5\sqrt{c+dx}} - \frac{8b(bc-ad)^3\sqrt{c+dx}}{d^5} + \frac{4b^2(bc-ad)^2(c+dx)^{3/2}}{d^5} - \frac{8b^3(bc-ad)(c+dx)^{5/2}}{5d^5} + \end{aligned}$$

Mathematica [A] time = 0.08, size = 101, normalized size = 0.82

$$\frac{2(-28b^3(c+dx)^3(bc-ad) + 70b^2(c+dx)^2(bc-ad)^2 - 140b(c+dx)(bc-ad)^3 - 35(bc-ad)^4 + 5b^4(c+dx)^4)}{35d^5\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4/(c + d*x)^(3/2), x]

[Out] (2*(-35*(b*c - a*d)^4 - 140*b*(b*c - a*d)^3*(c + d*x) + 70*b^2*(b*c - a*d)^2*(c + d*x)^2 - 28*b^3*(b*c - a*d)*(c + d*x)^3 + 5*b^4*(c + d*x)^4)/(35*d^5*Sqrt[c + d*x])

fricas [A] time = 0.42, size = 192, normalized size = 1.56

$$\frac{2(5b^4d^4x^4 - 128b^4c^4 + 448ab^3c^3d - 560a^2b^2c^2d^2 + 280a^3bcd^3 - 35a^4d^4 - 4(2b^4cd^3 - 7ab^3d^4)x^3 + 2(8b^4c^2d^2 - 28a^2b^2c^2d^2 + 70a^2b^2c^2d^3 - 35a^3b^2d^4)x^2 - 4(16b^4c^3d - 56a^2b^3c^2d^2 + 70a^2b^2c^2d^3 - 35a^3b^2d^4)x)*\sqrt{d*x + c}}{35(d^6x + cd^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^(3/2), x, algorithm="fricas")

[Out] 2/35*(5*b^4*d^4*x^4 - 128*b^4*c^4 + 448*a*b^3*c^3*d - 560*a^2*b^2*c^2*d^2 + 280*a^3*b*c*d^3 - 35*a^4*d^4 - 4*(2*b^4*c*d^3 - 7*a*b^3*d^4)*x^3 + 2*(8*b^4*c^2*d^2 - 28*a*b^3*c*d^3 + 35*a^2*b^2*d^4)*x^2 - 4*(16*b^4*c^3*d - 56*a*b^3*c^2*d^2 + 70*a^2*b^2*c*d^3 - 35*a^3*b*d^4)*x)*sqrt(d*x + c)/(d^6*x + c*d^5)

giac [B] time = 1.08, size = 240, normalized size = 1.95

$$\frac{2(b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4)}{\sqrt{dx + c}d^5} + \frac{2(5(dx+c)^{\frac{7}{2}}b^4d^{30} - 28(dx+c)^{\frac{5}{2}}b^4cd^{30} + 70(dx+c)^{\frac{3}{2}}b^4c^2d^{30} - 28(dx+c)^{\frac{1}{2}}b^4c^3d^{30} + 5b^4c^4d^{30})}{d^{35}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^(3/2), x, algorithm="giac")

[Out] -2*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(sqrt(d*x + c)*d^5) + 2/35*(5*(d*x + c)^(7/2)*b^4*d^30 - 28*(d*x + c)^(5/2)*b^4*c*d^30 + 70*(d*x + c)^(3/2)*b^4*c^2*d^30 - 140*sqrt(d*x + c)*b^4*c^3*d^30 + 28*(d*x + c)^(5/2)*a*b^3*c^2*d^31 - 140*(d*x + c)^(3/2)*a*b^3*c*d^31 + 420*sqrt(d*x + c)*a*b^3*c^2*d^31 + 70*(d*x + c)^(3/2)*a^2*b^2*d^32 - 420*sqrt(d*x + c)*a^2*b^2*c*d^32 + 140*sqrt(d*x + c)*a^3*b*d^33)/d^35

maple [A] time = 0.01, size = 186, normalized size = 1.51

$$\frac{2(-5b^4x^4d^4 - 28ab^3d^4x^3 + 8b^4cd^3x^3 - 70a^2b^2d^4x^2 + 56ab^3cd^3x^2 - 16b^4c^2d^2x^2 - 140a^3bd^4x + 280a^2b^2cd^3x - 35\sqrt{dx+c}d^5)}{35\sqrt{dx+c}d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4/(d*x+c)^(3/2), x)

[Out]
$$\frac{-2/35/(d*x+c)^{(1/2)}*(-5*b^4*d^4*x^4-28*a*b^3*d^4*x^3+8*b^4*c*d^3*x^3-70*a^2*b^2*d^4*x^2+56*a*b^3*c*d^3*x^2-16*b^4*c^2*d^2*x^2-140*a^3*b*d^4*x+280*a^2*b^2*c*d^3*x-224*a*b^3*c^2*d^2*x+64*b^4*c^3*d*x+35*a^4*d^4-280*a^3*b*c*d^3+560*a^2*b^2*c^2*d^2-448*a*b^3*c^3*d+128*b^4*c^4)/d^5}{35\sqrt{dx+c}d^5}$$

maxima [A] time = 1.35, size = 189, normalized size = 1.54

$$\frac{2\left(\frac{5(dx+c)^{\frac{7}{2}}b^4-28(b^4c-ab^3d)(dx+c)^{\frac{5}{2}}+70(b^4c^2-2ab^3cd+a^2b^2d^2)(dx+c)^{\frac{3}{2}}-140(b^4c^3-3ab^3c^2d+3a^2b^2cd^2-a^3bd^3)\sqrt{dx+c}}{d^4}-\frac{35(b^4c^4-4ab^3c^3d+6a^2b^2c^2d^2-4a^3b^2cd^3+a^4d^4)}{35d}\right)}{35d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^(3/2), x, algorithm="maxima")

[Out]
$$\frac{2/35*((5*(d*x+c)^{(7/2)}*b^4-28*(b^4*c-a*b^3*d)*(d*x+c)^{(5/2)}+70*(b^4*c^2-2*a*b^3*c*d+a^2*b^2*d^2)*(d*x+c)^{(3/2)}-140*(b^4*c^3-3*a*b^3*c^2*d+3*a^2*b^2*c*d^2-a^3*b*d^3)*\sqrt{d*x+c}))/d^4-35*(b^4*c^4-4*a*b^3*c^3*d+6*a^2*b^2*c^2*d^2-4*a^3*b^2*c*d^3+a^4*d^4)/(\sqrt{d*x+c}*d^4))/d}{35d}$$

mupad [B] time = 0.06, size = 153, normalized size = 1.24

$$\frac{2b^4(c+dx)^{7/2}}{7d^5} - \frac{(8b^4c-8ab^3d)(c+dx)^{5/2}}{5d^5} - \frac{2a^4d^4-8a^3bcd^3+12a^2b^2c^2d^2-8ab^3c^3d+2b^4c^4}{d^5\sqrt{c+dx}} + \frac{4b^2(a^2d^2-2ab^2cd+b^3c^2)}{d^5\sqrt{c+dx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^4/(c + d*x)^(3/2), x)

[Out]
$$\frac{(2*b^4*(c+d*x)^{(7/2)})/(7*d^5) - ((8*b^4*c - 8*a*b^3*d)*(c+d*x)^{(5/2)})/(5*d^5) - (2*a^4*d^4 + 2*b^4*c^4 + 12*a^2*b^2*c^2*d^2 - 8*a*b^3*c^3*d - 8*a^3*b^2*c*d^3)/(d^5*(c+d*x)^{(1/2)}) + (4*b^2*(a*d - b*c)^2*(c+d*x)^{(3/2)})/d^5 + (8*b*(a*d - b*c)^3*(c+d*x)^{(1/2)})/d^5}{d^5\sqrt{c+dx}}$$

sympy [A] time = 32.87, size = 168, normalized size = 1.37

$$\frac{2b^4(c+dx)^{\frac{7}{2}}}{7d^5} + \frac{(c+dx)^{\frac{5}{2}}(8ab^3d-8b^4c)}{5d^5} + \frac{(c+dx)^{\frac{3}{2}}(12a^2b^2d^2-24ab^3cd+12b^4c^2)}{3d^5} + \frac{\sqrt{c+dx}(8a^3bd^3-24a^2b^2cd+8a^3b^2d^2-8b^4c^2)}{d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4/(d*x+c)**(3/2),x)

[Out] 2*b**4*(c + d*x)**(7/2)/(7*d**5) + (c + d*x)**(5/2)*(8*a*b**3*d - 8*b**4*c)/(5*d**5) + (c + d*x)**(3/2)*(12*a**2*b**2*d**2 - 24*a*b**3*c*d + 12*b**4*c**2)/(3*d**5) + sqrt(c + d*x)*(8*a**3*b*d**3 - 24*a**2*b**2*c*d**2 + 24*a*b**3*c**2*d - 8*b**4*c**3)/d**5 - 2*(a*d - b*c)**4/(d**5*sqrt(c + d*x))

$$3.1426 \quad \int \frac{(a+bx)^3}{(c+dx)^{3/2}} dx$$

Optimal. Leaf size=94

$$-\frac{2b^2(c+dx)^{3/2}(bc-ad)}{d^4} + \frac{6b\sqrt{c+dx}(bc-ad)^2}{d^4} + \frac{2(bc-ad)^3}{d^4\sqrt{c+dx}} + \frac{2b^3(c+dx)^{5/2}}{5d^4}$$

[Out] $-2*b^2*(-a*d+b*c)*(d*x+c)^(3/2)/d^4+2/5*b^3*(d*x+c)^(5/2)/d^4+2*(a*d+b*c)^3/d^4/(d*x+c)^(1/2)+6*b*(-a*d+b*c)^2*(d*x+c)^(1/2)/d^4$

Rubi [A] time = 0.03, antiderivative size = 94, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{2b^2(c+dx)^{3/2}(bc-ad)}{d^4} + \frac{6b\sqrt{c+dx}(bc-ad)^2}{d^4} + \frac{2(bc-ad)^3}{d^4\sqrt{c+dx}} + \frac{2b^3(c+dx)^{5/2}}{5d^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/(c + d*x)^(3/2), x]

[Out] $(2*(b*c - a*d)^3)/(d^4*\text{Sqrt}[c + d*x]) + (6*b*(b*c - a*d)^2*\text{Sqrt}[c + d*x])/d^4 - (2*b^2*(b*c - a*d)*(c + d*x)^(3/2))/d^4 + (2*b^3*(c + d*x)^(5/2))/(5*d^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^3}{(c+dx)^{3/2}} dx = \int \left(\frac{(-bc+ad)^3}{d^3(c+dx)^{3/2}} + \frac{3b(bc-ad)^2}{d^3\sqrt{c+dx}} - \frac{3b^2(bc-ad)\sqrt{c+dx}}{d^3} + \frac{b^3(c+dx)^{3/2}}{d^3} \right) dx$$

$$= \frac{2(bc-ad)^3}{d^4\sqrt{c+dx}} + \frac{6b(bc-ad)^2\sqrt{c+dx}}{d^4} - \frac{2b^2(bc-ad)(c+dx)^{3/2}}{d^4} + \frac{2b^3(c+dx)^{5/2}}{5d^4}$$

Mathematica [A] time = 0.06, size = 78, normalized size = 0.83

$$\frac{2(-5b^2(c+dx)^2(bc-ad) + 15b(c+dx)(bc-ad)^2 + 5(bc-ad)^3 + b^3(c+dx)^3)}{5d^4\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/(c + d*x)^(3/2),x]

[Out] (2*(5*(b*c - a*d)^3 + 15*b*(b*c - a*d)^2*(c + d*x) - 5*b^2*(b*c - a*d)*(c + d*x)^2 + b^3*(c + d*x)^3)/(5*d^4*Sqrt[c + d*x])

fricas [A] time = 0.43, size = 124, normalized size = 1.32

$$\frac{2(b^3 d^3 x^3 + 16 b^3 c^3 - 40 a b^2 c^2 d + 30 a^2 b c d^2 - 5 a^3 d^3 - (2 b^3 c d^2 - 5 a b^2 d^3) x^2 + (8 b^3 c^2 d - 20 a b^2 c d^2 + 15 a^2 b d^3) x)}{5(d^5 x + c d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^(3/2),x, algorithm="fricas")

[Out] 2/5*(b^3*d^3*x^3 + 16*b^3*c^3 - 40*a*b^2*c^2*d + 30*a^2*b*c*d^2 - 5*a^3*d^3 - (2*b^3*c*d^2 - 5*a*b^2*d^3)*x^2 + (8*b^3*c^2*d - 20*a*b^2*c*d^2 + 15*a^2*b*d^3)*x)*sqrt(d*x + c)/(d^5*x + c*d^4)

giac [A] time = 1.05, size = 152, normalized size = 1.62

$$\frac{2(b^3 c^3 - 3 a b^2 c^2 d + 3 a^2 b c d^2 - a^3 d^3)}{\sqrt{d x + c} d^4} + \frac{2\left((d x + c)^{\frac{5}{2}} b^3 d^{16} - 5(d x + c)^{\frac{3}{2}} b^3 c d^{16} + 15 \sqrt{d x + c} b^3 c^2 d^{16} + 5(d x + c)^{\frac{3}{2}} a\right)}{5 d^{20}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^(3/2),x, algorithm="giac")

[Out] 2*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)/(sqrt(d*x + c)*d^4) + 2/5*((d*x + c)^(5/2)*b^3*d^16 - 5*(d*x + c)^(3/2)*b^3*c*d^16 + 15*sqrt(d*x + c)*b^3*c^2*d^16 + 5*(d*x + c)^(3/2)*a*b^2*d^17 - 30*sqrt(d*x + c)*a*b^2*c*d^17 + 15*sqrt(d*x + c)*a^2*b*d^18)/d^20

maple [A] time = 0.01, size = 116, normalized size = 1.23

$$\frac{2(-b^3 x^3 d^3 - 5 a b^2 d^3 x^2 + 2 b^3 c d^2 x^2 - 15 a^2 b d^3 x + 20 a b^2 c d^2 x - 8 b^3 c^2 d x + 5 a^3 d^3 - 30 a^2 b c d^2 + 40 a b^2 c^2 d - 16 b^3 c^3)}{5 \sqrt{d x + c} d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/(d*x+c)^(3/2),x)

[Out] -2/5/(d*x+c)^(1/2)*(-b^3*d^3*x^3-5*a*b^2*d^3*x^2+2*b^3*c*d^2*x^2-15*a^2*b*d^3*x+20*a*b^2*c*d^2*x-8*b^3*c^2*d*x+5*a^3*d^3-30*a^2*b*c*d^2+40*a*b^2*c^2*d-16*b^3*c^3)/d^4

maxima [A] time = 1.38, size = 125, normalized size = 1.33

$$2 \left(\frac{(dx+c)^{\frac{5}{2}} b^3 - 5(b^3 c - ab^2 d)(dx+c)^{\frac{3}{2}} + 15(b^3 c^2 - 2ab^2 cd + a^2 bd^2) \sqrt{dx+c}}{d^3} + \frac{5(b^3 c^3 - 3ab^2 c^2 d + 3a^2 bcd^2 - a^3 d^3)}{\sqrt{dx+c} d^3} \right) \\ \hline 5d$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^(3/2),x, algorithm="maxima")

[Out] 2/5*(((d*x + c)^(5/2)*b^3 - 5*(b^3*c - a*b^2*d)*(d*x + c)^(3/2) + 15*(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*sqrt(d*x + c))/d^3 + 5*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)/(sqrt(d*x + c)*d^3))/d

mupad [B] time = 0.08, size = 114, normalized size = 1.21

$$\frac{2b^3(c+dx)^{5/2}}{5d^4} - \frac{(6b^3c - 6ab^2d)(c+dx)^{3/2}}{3d^4} - \frac{2a^3d^3 - 6a^2bcd^2 + 6ab^2c^2d - 2b^3c^3}{d^4\sqrt{c+dx}} + \frac{6b(ad-bc)^2\sqrt{c+dx}}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3/(c + d*x)^(3/2),x)

[Out] (2*b^3*(c + d*x)^(5/2))/(5*d^4) - ((6*b^3*c - 6*a*b^2*d)*(c + d*x)^(3/2))/(3*d^4) - (2*a^3*d^3 - 2*b^3*c^3 + 6*a*b^2*c^2*d - 6*a^2*b*c*d^2)/(d^4*(c + d*x)^(1/2)) + (6*b*(a*d - b*c)^2*(c + d*x)^(1/2))/d^4

sympy [A] time = 21.51, size = 109, normalized size = 1.16

$$\frac{2b^3(c+dx)^{\frac{5}{2}}}{5d^4} + \frac{(c+dx)^{\frac{3}{2}}(6ab^2d - 6b^3c)}{3d^4} + \frac{\sqrt{c+dx}(6a^2bd^2 - 12ab^2cd + 6b^3c^2)}{d^4} - \frac{2(ad-bc)^3}{d^4\sqrt{c+dx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3/(d*x+c)**(3/2),x)

[Out] 2*b**3*(c + d*x)**(5/2)/(5*d**4) + (c + d*x)**(3/2)*(6*a*b**2*d - 6*b**3*c)/(3*d**4) + sqrt(c + d*x)*(6*a**2*b*d**2 - 12*a*b**2*c*d + 6*b**3*c**2)/d**4 - 2*(a*d - b*c)**3/(d**4*sqrt(c + d*x))

$$3.1427 \quad \int \frac{(a+bx)^2}{(c+dx)^{3/2}} dx$$

Optimal. Leaf size=67

$$-\frac{4b\sqrt{c+dx}(bc-ad)}{d^3} - \frac{2(bc-ad)^2}{d^3\sqrt{c+dx}} + \frac{2b^2(c+dx)^{3/2}}{3d^3}$$

[Out] $2/3*b^2*(d*x+c)^(3/2)/d^3-2*(-a*d+b*c)^2/d^3/(d*x+c)^(1/2)-4*b*(-a*d+b*c)*(d*x+c)^(1/2)/d^3$

Rubi [A] time = 0.02, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{4b\sqrt{c+dx}(bc-ad)}{d^3} - \frac{2(bc-ad)^2}{d^3\sqrt{c+dx}} + \frac{2b^2(c+dx)^{3/2}}{3d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(c + d*x)^(3/2), x]

[Out] $(-2*(b*c - a*d)^2)/(d^3*\text{Sqrt}[c + d*x]) - (4*b*(b*c - a*d)*\text{Sqrt}[c + d*x])/d^3 + (2*b^2*(c + d*x)^(3/2))/(3*d^3)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(c+dx)^{3/2}} dx &= \int \left(\frac{(-bc+ad)^2}{d^2(c+dx)^{3/2}} - \frac{2b(bc-ad)}{d^2\sqrt{c+dx}} + \frac{b^2\sqrt{c+dx}}{d^2} \right) dx \\ &= -\frac{2(bc-ad)^2}{d^3\sqrt{c+dx}} - \frac{4b(bc-ad)\sqrt{c+dx}}{d^3} + \frac{2b^2(c+dx)^{3/2}}{3d^3} \end{aligned}$$

Mathematica [A] time = 0.03, size = 59, normalized size = 0.88

$$\frac{2(-3a^2d^2 + 6abd(2c + dx) + b^2(-8c^2 - 4cdx + d^2x^2))}{3d^3\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(c + d*x)^(3/2), x]

[Out] (2*(-3*a^2*d^2 + 6*a*b*d*(2*c + d*x) + b^2*(-8*c^2 - 4*c*d*x + d^2*x^2)))/(3*d^3*Sqrt[c + d*x])

fricas [A] time = 0.46, size = 73, normalized size = 1.09

$$\frac{2(b^2d^2x^2 - 8b^2c^2 + 12abcd - 3a^2d^2 - 2(2b^2cd - 3abd^2)x)\sqrt{dx+c}}{3(d^4x + cd^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^(3/2), x, algorithm="fricas")

[Out] 2/3*(b^2*d^2*x^2 - 8*b^2*c^2 + 12*a*b*c*d - 3*a^2*d^2 - 2*(2*b^2*c*d - 3*a*b*d^2)*x)*sqrt(d*x + c)/(d^4*x + c*d^3)

giac [A] time = 1.04, size = 84, normalized size = 1.25

$$-\frac{2(b^2c^2 - 2abcd + a^2d^2)}{\sqrt{dx+c}d^3} + \frac{2\left((dx+c)^{\frac{3}{2}}b^2d^6 - 6\sqrt{dx+c}b^2cd^6 + 6\sqrt{dx+c}abd^7\right)}{3d^9}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^(3/2), x, algorithm="giac")

[Out] -2*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)/(sqrt(d*x + c)*d^3) + 2/3*((d*x + c)^(3/2)*b^2*d^6 - 6*sqrt(d*x + c)*b^2*c*d^6 + 6*sqrt(d*x + c)*a*b*d^7)/d^9

maple [A] time = 0.00, size = 63, normalized size = 0.94

$$-\frac{2(-b^2x^2d^2 - 6abd^2x + 4b^2cdx + 3a^2d^2 - 12abcd + 8b^2c^2)}{3\sqrt{dx+c}d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(d*x+c)^(3/2), x)

[Out] -2/3/(d*x+c)^(1/2)*(-b^2*d^2*x^2-6*a*b*d^2*x+4*b^2*c*d*x+3*a^2*d^2-12*a*b*c*d+8*b^2*c^2)/d^3

maxima [A] time = 1.30, size = 75, normalized size = 1.12

$$\frac{2\left(\frac{(dx+c)^{\frac{3}{2}}b^2-6(b^2c-abd)\sqrt{dx+c}}{d^2} - \frac{3(b^2c^2-2abcd+a^2d^2)}{\sqrt{dx+c}d^2}\right)}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^(3/2),x, algorithm="maxima")

[Out] $\frac{2}{3} * \left(\frac{(d*x + c)^{(3/2)} * b^2 - 6 * (b^2 * c - a * b * d) * \sqrt{d*x + c}}{d^2} - 3 * (b^2 * c^2 - 2 * a * b * c * d + a^2 * d^2) / (\sqrt{d*x + c} * d^2) \right) / d$

mupad [B] time = 0.26, size = 67, normalized size = 1.00

$$\frac{\frac{2b^2(c+dx)^2}{3} - 2a^2d^2 - 2b^2c^2 - 4b^2c(c+dx) + 4abd(c+dx) + 4abcd}{d^3\sqrt{c+dx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(c + d*x)^(3/2),x)

[Out] $\left(\frac{2 * b^2 * (c + d * x)^2}{3} - 2 * a^2 * d^2 - 2 * b^2 * c^2 - 4 * b^2 * c * (c + d * x) + 4 * a * b * d * (c + d * x) + 4 * a * b * c * d \right) / (d^3 * (c + d * x)^{(1/2)})$

sympy [A] time = 13.29, size = 65, normalized size = 0.97

$$\frac{2b^2(c+dx)^{\frac{3}{2}}}{3d^3} + \frac{\sqrt{c+dx}(4abd-4b^2c)}{d^3} - \frac{2(ad-bc)^2}{d^3\sqrt{c+dx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(d*x+c)**(3/2),x)

[Out] $2 * b ** 2 * (c + d * x) ** (3/2) / (3 * d ** 3) + \sqrt{c + d * x} * (4 * a * b * d - 4 * b ** 2 * c) / d ** 3 - 2 * (a * d - b * c) ** 2 / (d ** 3 * \sqrt{c + d * x})$

$$3.1428 \quad \int \frac{a+bx}{(c+dx)^{3/2}} dx$$

Optimal. Leaf size=38

$$\frac{2(bc-ad)}{d^2\sqrt{c+dx}} + \frac{2b\sqrt{c+dx}}{d^2}$$

[Out] $2*(-a*d+b*c)/d^2/(d*x+c)^{(1/2)}+2*b*(d*x+c)^{(1/2)}/d^2$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{2(bc-ad)}{d^2\sqrt{c+dx}} + \frac{2b\sqrt{c+dx}}{d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(c + d*x)^(3/2), x]

[Out] $(2*(b*c - a*d))/(d^2*\text{Sqrt}[c + d*x]) + (2*b*\text{Sqrt}[c + d*x])/d^2$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{(c+dx)^{3/2}} dx &= \int \left(\frac{-bc+ad}{d(c+dx)^{3/2}} + \frac{b}{d\sqrt{c+dx}} \right) dx \\ &= \frac{2(bc-ad)}{d^2\sqrt{c+dx}} + \frac{2b\sqrt{c+dx}}{d^2} \end{aligned}$$

Mathematica [A] time = 0.02, size = 27, normalized size = 0.71

$$\frac{2(-ad+2bc+bdx)}{d^2\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(c + d*x)^(3/2), x]

[Out] (2*(2*b*c - a*d + b*d*x))/(d^2*sqrt[c + d*x])

fricas [A] time = 0.43, size = 35, normalized size = 0.92

$$\frac{2(bdx + 2bc - ad)\sqrt{dx + c}}{d^3x + cd^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)^(3/2), x, algorithm="fricas")

[Out] 2*(b*d*x + 2*b*c - a*d)*sqrt(d*x + c)/(d^3*x + c*d^2)

giac [A] time = 1.03, size = 34, normalized size = 0.89

$$\frac{2\sqrt{dx + c}b}{d^2} + \frac{2(bc - ad)}{\sqrt{dx + c}d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)^(3/2), x, algorithm="giac")

[Out] 2*sqrt(d*x + c)*b/d^2 + 2*(b*c - a*d)/(sqrt(d*x + c)*d^2)

maple [A] time = 0.00, size = 26, normalized size = 0.68

$$-\frac{2(-bdx + ad - 2bc)}{\sqrt{dx + c}d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)/(d*x+c)^(3/2), x)

[Out] -2/(d*x+c)^(1/2)*(-b*d*x+a*d-2*b*c)/d^2

maxima [A] time = 1.33, size = 37, normalized size = 0.97

$$\frac{2\left(\frac{\sqrt{dx+cb}}{d} + \frac{bc-ad}{\sqrt{dx+cd}}\right)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)^(3/2), x, algorithm="maxima")

[Out] 2*(sqrt(d*x + c)*b/d + (b*c - a*d)/(sqrt(d*x + c)*d))/d

mupad [B] time = 0.05, size = 25, normalized size = 0.66

$$\frac{4bc - 2ad + 2bdx}{d^2 \sqrt{c + dx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)/(c + d*x)^(3/2), x)

[Out] (4*b*c - 2*a*d + 2*b*d*x)/(d^2*(c + d*x)^(1/2))

sympy [A] time = 0.61, size = 60, normalized size = 1.58

$$\begin{cases} -\frac{2a}{d\sqrt{c+dx}} + \frac{4bc}{d^2\sqrt{c+dx}} + \frac{2bx}{d\sqrt{c+dx}} & \text{for } d \neq 0 \\ \frac{ax + \frac{bx^2}{2}}{c^{\frac{3}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)/(d*x+c)**(3/2), x)

[Out] Piecewise((-2*a/(d*sqrt(c + d*x)) + 4*b*c/(d**2*sqrt(c + d*x)) + 2*b*x/(d*sqrt(c + d*x)), Ne(d, 0)), ((a*x + b*x**2/2)/c**(3/2), True))

$$3.1429 \quad \int \frac{1}{(c+dx)^{3/2}} dx$$

Optimal. Leaf size=14

$$-\frac{2}{d\sqrt{c+dx}}$$

[Out] -2/d/(d*x+c)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$-\frac{2}{d\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(-3/2), x]

[Out] -2/(d*Sqrt[c + d*x])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(c+dx)^{3/2}} dx = -\frac{2}{d\sqrt{c+dx}}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\frac{2}{d\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(-3/2), x]

[Out] -2/(d*Sqrt[c + d*x])

fricas [A] time = 0.45, size = 20, normalized size = 1.43

$$-\frac{2\sqrt{dx+c}}{d^2x+cd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(d*x+c)^(3/2),x, algorithm="fricas")`

[Out] `-2*sqrt(d*x + c)/(d^2*x + c*d)`

giac [A] time = 1.02, size = 12, normalized size = 0.86

$$-\frac{2}{\sqrt{dx + c} d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(d*x+c)^(3/2),x, algorithm="giac")`

[Out] `-2/(sqrt(d*x + c)*d)`

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$-\frac{2}{\sqrt{dx + c} d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(d*x+c)^(3/2),x)`

[Out] `-2/d/(d*x+c)^(1/2)`

maxima [A] time = 1.33, size = 12, normalized size = 0.86

$$-\frac{2}{\sqrt{dx + c} d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(d*x+c)^(3/2),x, algorithm="maxima")`

[Out] `-2/(sqrt(d*x + c)*d)`

mupad [B] time = 0.02, size = 12, normalized size = 0.86

$$-\frac{2}{d\sqrt{c + dx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(c + d*x)^(3/2),x)`

[Out] $-2/(d*(c + d*x)^{(1/2)})$

sympy [A] time = 0.06, size = 12, normalized size = 0.86

$$-\frac{2}{d\sqrt{c + dx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(d*x+c)**(3/2),x)`

[Out] $-2/(d*\text{sqrt}(c + d*x))$

$$3.1430 \quad \int \frac{1}{(a+bx)(c+dx)^{3/2}} dx$$

Optimal. Leaf size=69

$$\frac{2}{\sqrt{c+dx}(bc-ad)} - \frac{2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{3/2}}$$

[Out] $-2*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})*b^{(1/2)/(-a*d+b*c)^{(3/2)}+2/(-a*d+b*c)/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$\frac{2}{\sqrt{c+dx}(bc-ad)} - \frac{2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)*(c + d*x)^(3/2)),x]

[Out] $2/((b*c - a*d)*\operatorname{Sqrt}[c + d*x]) - (2*\operatorname{Sqrt}[b]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/ \operatorname{Sqrt}[b*c - a*d]])/(b*c - a*d)^{(3/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)(c+dx)^{3/2}} dx &= \frac{2}{(bc-ad)\sqrt{c+dx}} + \frac{b \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{bc-ad} \\ &= \frac{2}{(bc-ad)\sqrt{c+dx}} + \frac{(2b) \text{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{d(bc-ad)} \\ &= \frac{2}{(bc-ad)\sqrt{c+dx}} - \frac{2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{3/2}} \end{aligned}$$

Mathematica [C] time = 0.01, size = 46, normalized size = 0.67

$$-\frac{{}_2F_1\left(-\frac{1}{2}, 1; \frac{1}{2}; \frac{b(c+dx)}{bc-ad}\right)}{\sqrt{c+dx}(ad-bc)}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*(c + d*x)^(3/2)), x]

[Out] (-2*Hypergeometric2F1[-1/2, 1, 1/2, (b*(c + d*x))/(b*c - a*d)]/((-b*c) + a*d)*Sqrt[c + d*x])

fricas [A] time = 0.49, size = 214, normalized size = 3.10

$$\left[\frac{(dx+c)\sqrt{\frac{b}{bc-ad}} \log\left(\frac{bdx+2bc-ad+2(bc-ad)\sqrt{dx+c}\sqrt{\frac{b}{bc-ad}}}{bx+a}\right) - 2\sqrt{dx+c}}{bc^2 - acd + (bcd - ad^2)x}, -\frac{2\left((dx+c)\sqrt{-\frac{b}{bc-ad}} \arctan\left(-\frac{(bc-ad)\sqrt{dx+c}}{bdx+bc}\right)\right)}{bc^2 - acd + (bcd - ad^2)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(3/2), x, algorithm="fricas")

[Out] [-(d*x + c)*sqrt(b/(b*c - a*d))*log((b*d*x + 2*b*c - a*d + 2*(b*c - a*d)*sqrt(d*x + c)*sqrt(b/(b*c - a*d)))/(b*x + a)) - 2*sqrt(d*x + c)/(b*c^2 - a*

$c*d + (b*c*d - a*d^2)*x$, $-2*((d*x + c)*\sqrt{-b/(b*c - a*d)}*\arctan(-(b*c - a*d)*\sqrt{d*x + c}*\sqrt{-b/(b*c - a*d)})/(b*d*x + b*c)) - \sqrt{d*x + c})/(b*c^2 - a*c*d + (b*c*d - a*d^2)*x]$

giac [A] time = 0.94, size = 69, normalized size = 1.00

$$\frac{2b \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{-b^2c+abd}}\right)}{\sqrt{-b^2c+abd}(bc-ad)} + \frac{2}{(bc-ad)\sqrt{dx+c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(3/2),x, algorithm="giac")

[Out] $2*b*\arctan(\sqrt{d*x + c}*b/\sqrt{-b^2*c + a*b*d})/(\sqrt{-b^2*c + a*b*d}*(b*c - a*d)) + 2/((b*c - a*d)*\sqrt{d*x + c})$

maple [A] time = 0.01, size = 68, normalized size = 0.99

$$-\frac{2b \arctan\left(\frac{\sqrt{dx+c}b}{\sqrt{(ad-bc)b}}\right)}{(ad-bc)\sqrt{(ad-bc)b}} - \frac{2}{(ad-bc)\sqrt{dx+c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)/(d*x+c)^(3/2),x)

[Out] $-2/(a*d-b*c)/(d*x+c)^(1/2)-2*b/(a*d-b*c)/((a*d-b*c)*b)^(1/2)*\arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.27, size = 57, normalized size = 0.83

$$-\frac{2}{(ad-bc)\sqrt{c+dx}} - \frac{2\sqrt{b} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{ad-bc}}\right)}{(ad-bc)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)*(c + d*x)^(3/2)),x)`

[Out] $-2/((a*d - b*c)*(c + d*x)^{(1/2)}) - (2*b^{(1/2)}*atan((b^{(1/2)}*(c + d*x)^{(1/2)})/(a*d - b*c)^{(1/2)}))/((a*d - b*c)^{(3/2)})$

sympy [A] time = 11.49, size = 60, normalized size = 0.87

$$-\frac{2}{\sqrt{c + dx} (ad - bc)} - \frac{2 \operatorname{atan}\left(\frac{\sqrt{c+dx}}{\sqrt{\frac{ad-bc}{b}}}\right)}{\sqrt{\frac{ad-bc}{b}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/(d*x+c)**(3/2),x)`

[Out] $-2/(\sqrt{c + d*x}*(a*d - b*c)) - 2*atan(\sqrt{c + d*x}/\sqrt{(a*d - b*c)/b})/(\sqrt{(a*d - b*c)/b}*(a*d - b*c))$

$$3.1431 \quad \int \frac{1}{(a+bx)^2(c+dx)^{3/2}} dx$$

Optimal. Leaf size=99

$$-\frac{3d}{\sqrt{c+dx}(bc-ad)^2} - \frac{1}{(a+bx)\sqrt{c+dx}(bc-ad)} + \frac{3\sqrt{b}d \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{5/2}}$$

[Out] $3*d*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})*b^{(1/2)/(-a*d+b*c)^{(5/2)}}-3*d/(-a*d+b*c)^2/(d*x+c)^{(1/2)}-1/(-a*d+b*c)/(b*x+a)/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 99, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$-\frac{3d}{\sqrt{c+dx}(bc-ad)^2} - \frac{1}{(a+bx)\sqrt{c+dx}(bc-ad)} + \frac{3\sqrt{b}d \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^2*(c + d*x)^(3/2)), x]

[Out] $(-3*d)/((b*c - a*d)^2*\operatorname{Sqrt}[c + d*x]) - 1/((b*c - a*d)*(a + b*x)*\operatorname{Sqrt}[c + d*x]) + (3*\operatorname{Sqrt}[b]*d*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/\operatorname{Sqrt}[b*c - a*d]])/(b*c - a*d)^{(5/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^2(c+dx)^{3/2}} dx &= -\frac{1}{(bc-ad)(a+bx)\sqrt{c+dx}} - \frac{(3d) \int \frac{1}{(a+bx)(c+dx)^{3/2}} dx}{2(bc-ad)} \\
 &= -\frac{3d}{(bc-ad)^2\sqrt{c+dx}} - \frac{1}{(bc-ad)(a+bx)\sqrt{c+dx}} - \frac{(3bd) \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{2(bc-ad)^2} \\
 &= -\frac{3d}{(bc-ad)^2\sqrt{c+dx}} - \frac{1}{(bc-ad)(a+bx)\sqrt{c+dx}} - \frac{(3b) \text{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{(bc-ad)^2} \\
 &= -\frac{3d}{(bc-ad)^2\sqrt{c+dx}} - \frac{1}{(bc-ad)(a+bx)\sqrt{c+dx}} + \frac{3\sqrt{b}d \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 48, normalized size = 0.48

$$\frac{2d {}_2F_1\left(-\frac{1}{2}, 2; \frac{1}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{\sqrt{c+dx}(ad-bc)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*(c + d*x)^(3/2)),x]

[Out] (-2*d*Hypergeometric2F1[-1/2, 2, 1/2, -(b*(c + d*x))/(-(b*c) + a*d)]/((-b*c) + a*d)^2*Sqrt[c + d*x])

fricas [B] time = 0.47, size = 423, normalized size = 4.27

$$\left[\frac{3(bd^2x^2 + acd + (bcd + ad^2)x)\sqrt{\frac{b}{bc-ad}} \log\left(\frac{bdx+2bc-ad+2(bc-ad)\sqrt{dx+c}\sqrt{\frac{b}{bc-ad}}}{bx+a}\right) - 2(3bdx + bc + 2ad)\sqrt{dx+c} - 3(bd^2x^2 + acd + (bcd + ad^2)x)}{2(ab^2c^3 - 2a^2bc^2d + a^3cd^2 + (b^3c^2d - 2ab^2cd^2 + a^2bd^3)x^2 + (b^3c^3 - ab^2c^2d - a^2bcd^2 + a^3d^3)x)}, \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^(3/2),x, algorithm="fricas")

```
[Out] [1/2*(3*(b*d^2*x^2 + a*c*d + (b*c*d + a*d^2)*x)*sqrt(b/(b*c - a*d))*log((b*d*x + 2*b*c - a*d + 2*(b*c - a*d)*sqrt(d*x + c)*sqrt(b/(b*c - a*d)))/(b*x + a)) - 2*(3*b*d*x + b*c + 2*a*d)*sqrt(d*x + c))/(a*b^2*c^3 - 2*a^2*b*c^2*d + a^3*c*d^2 + (b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*x^2 + (b^3*c^3 - a*b^2*c^2*d - a^2*b*c*d^2 + a^3*d^3)*x), (3*(b*d^2*x^2 + a*c*d + (b*c*d + a*d^2)*x)*sqrt(-b/(b*c - a*d))*arctan(-(b*c - a*d)*sqrt(d*x + c)*sqrt(-b/(b*c - a*d)))/(b*d*x + b*c)) - (3*b*d*x + b*c + 2*a*d)*sqrt(d*x + c))/(a*b^2*c^3 - 2*a^2*b*c^2*d + a^3*c*d^2 + (b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*x^2 + (b^3*c^3 - a*b^2*c^2*d - a^2*b*c*d^2 + a^3*d^3)*x)]
```

giac [A] time = 1.03, size = 143, normalized size = 1.44

$$\frac{3bd \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{(b^2c^2 - 2abcd + a^2d^2)\sqrt{-b^2c + abd}} - \frac{3(dx+c)bd - 2bcd + 2ad^2}{(b^2c^2 - 2abcd + a^2d^2)\left((dx+c)^{\frac{3}{2}}b - \sqrt{dx+c}bc + \sqrt{dx+c}ad\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)^2/(d*x+c)^(3/2),x, algorithm="giac")
```

```
[Out] -3*b*d*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*sqrt(-b^2*c + a*b*d)) - (3*(d*x + c)*b*d - 2*b*c*d + 2*a*d^2)/((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*((d*x + c)^(3/2)*b - sqrt(d*x + c)*b*c + sqrt(d*x + c)*a*d))
```

maple [A] time = 0.01, size = 101, normalized size = 1.02

$$-\frac{3bd \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{(ad-bc)b}}\right)}{(ad-bc)^2 \sqrt{(ad-bc)b}} - \frac{\sqrt{dx+c}bd}{(ad-bc)^2 (bdx+ad)} - \frac{2d}{(ad-bc)^2 \sqrt{dx+c}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(b*x+a)^2/(d*x+c)^(3/2),x)
```

```
[Out] -2*d/(a*d-b*c)^2/(d*x+c)^(1/2)-d*b/(a*d-b*c)^2*(d*x+c)^(1/2)/(b*d*x+a*d)-3*d*b/(a*d-b*c)^2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)^2/(d*x+c)^(3/2),x, algorithm="maxima")
```

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.19, size = 123, normalized size = 1.24

$$\frac{\frac{2d}{ad-bc} + \frac{3bd(c+dx)}{(ad-bc)^2}}{b(c+dx)^{3/2} + (ad-bc)\sqrt{c+dx}} - \frac{3\sqrt{b}d \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{c+dx}(a^2d^2-2abcd+b^2c^2)}{(ad-bc)^{5/2}}\right)}{(ad-bc)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^2*(c + d*x)^(3/2)),x)

[Out] - ((2*d)/(a*d - b*c) + (3*b*d*(c + d*x))/(a*d - b*c)^2)/(b*(c + d*x)^(3/2)) + (a*d - b*c)*(c + d*x)^(1/2) - (3*b^(1/2)*d*atan((b^(1/2)*(c + d*x)^(1/2)*(a^2*d^2 + b^2*c^2 - 2*a*b*c*d))/(a*d - b*c)^(5/2)))/(a*d - b*c)^(5/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^2 (c + dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2/(d*x+c)**(3/2),x)

[Out] Integral(1/((a + b*x)**2*(c + d*x)**(3/2)), x)

$$3.1432 \quad \int \frac{1}{(a+bx)^3(c+dx)^{3/2}} dx$$

Optimal. Leaf size=140

$$\frac{15d^2}{4\sqrt{c+dx}(bc-ad)^3} - \frac{15\sqrt{b}d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4(bc-ad)^{7/2}} + \frac{5d}{4(a+bx)\sqrt{c+dx}(bc-ad)^2} - \frac{1}{2(a+bx)^2\sqrt{c+dx}(bc-ad)}$$

[Out] $-15/4*d^2*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})*b^{(1/2)/(-a*d+b*c)^{(7/2)}+15/4*d^2/(-a*d+b*c)^3/(d*x+c)^{(1/2)-1/2/(-a*d+b*c)/(b*x+a)^2/(d*x+c)^{(1/2)}+5/4*d/(-a*d+b*c)^2/(b*x+a)/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 140, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$\frac{15d^2}{4\sqrt{c+dx}(bc-ad)^3} - \frac{15\sqrt{b}d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4(bc-ad)^{7/2}} + \frac{5d}{4(a+bx)\sqrt{c+dx}(bc-ad)^2} - \frac{1}{2(a+bx)^2\sqrt{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a+b*x)^3*(c+d*x)^{(3/2)}),x]$

[Out] $(15*d^2)/(4*(b*c-a*d)^3*\operatorname{Sqrt}[c+d*x]) - 1/(2*(b*c-a*d)*(a+b*x)^2*\operatorname{Sqrt}[c+d*x]) + (5*d)/(4*(b*c-a*d)^2*(a+b*x)*\operatorname{Sqrt}[c+d*x]) - (15*\operatorname{Sqrt}[b]*d^2*\operatorname{ArcTanh}[\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c+d*x]]/\operatorname{Sqrt}[b*c-a*d])/(4*(b*c-a*d)^{(7/2)})$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)} / ((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*(m+n+2)) / ((b*c - a*d)*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^n, x] /; \operatorname{FreeQ}\{a, b, c, d, n\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{LtQ}[n, -1] \&\& (\operatorname{EqQ}[a, 0] \mid\mid (\operatorname{NeQ}[c, 0] \&\& \operatorname{LtQ}[m-n, 0] \&\& \operatorname{IntegerQ}[n]))) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /; \operatorname{FreeQ}\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^3(c+dx)^{3/2}} dx &= -\frac{1}{2(bc-ad)(a+bx)^2\sqrt{c+dx}} - \frac{(5d) \int \frac{1}{(a+bx)^2(c+dx)^{3/2}} dx}{4(bc-ad)} \\
 &= -\frac{1}{2(bc-ad)(a+bx)^2\sqrt{c+dx}} + \frac{5d}{4(bc-ad)^2(a+bx)\sqrt{c+dx}} + \frac{(15d^2) \int \frac{1}{(a+bx)(c+dx)^3}}{8(bc-ad)^2} \\
 &= \frac{15d^2}{4(bc-ad)^3\sqrt{c+dx}} - \frac{1}{2(bc-ad)(a+bx)^2\sqrt{c+dx}} + \frac{5d}{4(bc-ad)^2(a+bx)\sqrt{c+dx}} + \\
 &= \frac{15d^2}{4(bc-ad)^3\sqrt{c+dx}} - \frac{1}{2(bc-ad)(a+bx)^2\sqrt{c+dx}} + \frac{5d}{4(bc-ad)^2(a+bx)\sqrt{c+dx}} + \\
 &= \frac{15d^2}{4(bc-ad)^3\sqrt{c+dx}} - \frac{1}{2(bc-ad)(a+bx)^2\sqrt{c+dx}} + \frac{5d}{4(bc-ad)^2(a+bx)\sqrt{c+dx}} -
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.36

$$\frac{2d^2 {}_2F_1\left(-\frac{1}{2}, 3; \frac{1}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{\sqrt{c+dx}(ad-bc)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^3*(c + d*x)^(3/2)), x]

[Out] (-2*d^2*Hypergeometric2F1[-1/2, 3, 1/2, -((b*(c + d*x))/(-(b*c) + a*d))])/((-b*c) + a*d)^3*Sqrt[c + d*x])

fricas [B] time = 0.48, size = 782, normalized size = 5.59

$$\left[\frac{15(b^2d^3x^3 + a^2cd^2 + (b^2cd^2 + 2abd^3)x^2 + (2abcd^2 + a^2d^3)x)\sqrt{\frac{b}{bc-ad}} \log\left(\frac{bdx+2bc-ad+2(bc-ad)\sqrt{dx+c}}{bx+a}\right)}{8(a^2b^3c^4 - 3a^3b^2c^3d + 3a^4bc^2d^2 - a^5cd^3 + (b^5c^3d - 3ab^4c^2d^2 + 3a^2b^3cd^3 - a^3b^2d^4)x^3 + (b^5c^4 - ab^4c^3d - 3a^2b^3c^2d^2 - a^3b^2c^3d^2)x^2 + (2abcd^2 + a^2d^3)x + a^2d^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^(3/2),x, algorithm="fricas")

[Out]
$$\begin{aligned} & [-1/8*(15*(b^2*d^3*x^3 + a^2*c*d^2 + (b^2*c*d^2 + 2*a*b*d^3)*x^2 + (2*a*b*c \\ & *d^2 + a^2*d^3)*x)*\sqrt{b/(b*c - a*d)}*\log((b*d*x + 2*b*c - a*d + 2*(b*c - \\ & a*d)*\sqrt{d*x + c}*\sqrt{b/(b*c - a*d)))/(b*x + a)) - 2*(15*b^2*d^2*x^2 - 2* \\ & b^2*c^2 + 9*a*b*c*d + 8*a^2*d^2 + 5*(b^2*c*d + 5*a*b*d^2)*x)*\sqrt{d*x + c}) \\ & / (a^2*b^3*c^4 - 3*a^3*b^2*c^3*d + 3*a^4*b*c^2*d^2 - a^5*c*d^3 + (b^5*c^3*d \\ & - 3*a*b^4*c^2*d^2 + 3*a^2*b^3*c*d^3 - a^3*b^2*d^4)*x^3 + (b^5*c^4 - a*b^4*c \\ & ^3*d - 3*a^2*b^3*c^2*d^2 + 5*a^3*b^2*c*d^3 - 2*a^4*b*d^4)*x^2 + (2*a*b^4*c^4 \\ & - 5*a^2*b^3*c^3*d + 3*a^3*b^2*c^2*d^2 + a^4*b*c*d^3 - a^5*d^4)*x), -1/4*(\\ & 15*(b^2*d^3*x^3 + a^2*c*d^2 + (b^2*c*d^2 + 2*a*b*d^3)*x^2 + (2*a*b*c*d^2 + \\ & a^2*d^3)*x)*\sqrt{-b/(b*c - a*d)}*\arctan(-(b*c - a*d)*\sqrt{d*x + c}*\sqrt{-b/ \\ & (b*c - a*d)})/(b*d*x + b*c)) - (15*b^2*d^2*x^2 - 2*b^2*c^2 + 9*a*b*c*d + 8*a \\ & ^2*d^2 + 5*(b^2*c*d + 5*a*b*d^2)*x)*\sqrt{d*x + c}) / (a^2*b^3*c^4 - 3*a^3*b^2 \\ & *c^3*d + 3*a^4*b*c^2*d^2 - a^5*c*d^3 + (b^5*c^3*d - 3*a*b^4*c^2*d^2 + 3*a^2 \\ & *b^3*c*d^3 - a^3*b^2*d^4)*x^3 + (b^5*c^4 - a*b^4*c^3*d - 3*a^2*b^3*c^2*d^2 \\ & + 5*a^3*b^2*c*d^3 - 2*a^4*b*d^4)*x^2 + (2*a*b^4*c^4 - 5*a^2*b^3*c^3*d + 3*a \\ & ^3*b^2*c^2*d^2 + a^4*b*c*d^3 - a^5*d^4)*x)] \end{aligned}$$

giac [B] time = 1.03, size = 234, normalized size = 1.67

$$\frac{15bd^2 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{4(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)\sqrt{-b^2c+abd}} + \frac{2d^2}{(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)\sqrt{dx+c}} + \frac{7(dx+c)}{4(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^(3/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & 15/4*b*d^2*\arctan(\sqrt{d*x + c}*b/\sqrt{-b^2*c + a*b*d})/((b^3*c^3 - 3*a*b^2 \\ & *c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*\sqrt{-b^2*c + a*b*d}) + 2*d^2/((b^3*c^3 - \\ & 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*\sqrt{d*x + c}) + 1/4*(7*(d*x + c) \\ & ^{(3/2)}*b^2*d^2 - 9*\sqrt{d*x + c}*b^2*c*d^2 + 9*\sqrt{d*x + c}*a*b*d^3)/((b^3 \\ & *c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*((d*x + c)*b - b*c + a*d)^2 \\ &) \end{aligned}$$

maple [A] time = 0.02, size = 179, normalized size = 1.28

$$\frac{9\sqrt{dx+c}abd^3}{4(ad-bc)^3(bdx+ad)^2} + \frac{9\sqrt{dx+c}b^2cd^2}{4(ad-bc)^3(bdx+ad)^2} - \frac{7(dx+c)^{\frac{3}{2}}b^2d^2}{4(ad-bc)^3(bdx+ad)^2} - \frac{15bd^2 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{(ad-bc)b}}\right)}{4(ad-bc)^3\sqrt{(ad-bc)b}} - \frac{7(dx+c)}{4(ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^3/(d*x+c)^(3/2),x)`

[Out] $-2*d^2/(a*d-b*c)^3/(d*x+c)^{(1/2)}-7/4*d^2*b^2/(a*d-b*c)^3/(b*d*x+a*d)^2*(d*x+c)^{(3/2)}-9/4*d^3*b/(a*d-b*c)^3/(b*d*x+a*d)^2*(d*x+c)^{(1/2)}*a+9/4*d^2*b^2/(a*d-b*c)^3/(b*d*x+a*d)^2*(d*x+c)^{(1/2)}*c-15/4*d^2*b/(a*d-b*c)^3/((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^3/(d*x+c)^(3/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.44, size = 205, normalized size = 1.46

$$\frac{\frac{2d^2}{ad-bc} + \frac{15b^2d^2(c+dx)^2}{4(ad-bc)^3} + \frac{25bd^2(c+dx)}{4(ad-bc)^2}}{b^2(c+dx)^{5/2} - (2b^2c - 2abd)(c+dx)^{3/2} + \sqrt{c+dx}(a^2d^2 - 2abcd + b^2c^2)} - \frac{15\sqrt{b}d^2 \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{c+dx}(a^3d^2 - b^3c^2)}{4(ad-bc)^2}\right)}{4(ad-bc)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a+b*x)^3*(c+d*x)^(3/2)),x)`

[Out] $-\left(\frac{2*d^2}{a*d-b*c} + \frac{15*b^2*d^2*(c+d*x)^2}{4*(a*d-b*c)^3} + \frac{25*b*d^2*(c+d*x)}{4*(a*d-b*c)^2}\right) / (b^2*(c+d*x)^{(5/2)} - (2*b^2*c - 2*a*b*d)*(c+d*x)^{(3/2)} + (c+d*x)^{(1/2)}*(a^2*d^2 + b^2*c^2 - 2*a*b*c*d)) - \left(\frac{15*b^{(1/2)}*d^2*\operatorname{atan}\left(\frac{b^{(1/2)}*(c+d*x)^{(1/2)}*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2)}{(a*d-b*c)^{(7/2)}}\right)}{4*(a*d-b*c)^{(7/2)}}\right)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**3/(d*x+c)**(3/2),x)`

[Out] Timed out

$$3.1433 \quad \int \frac{1}{(a+bx)^4(c+dx)^{3/2}} dx$$

Optimal. Leaf size=173

$$\frac{35d^3}{8\sqrt{c+dx}(bc-ad)^4} + \frac{35\sqrt{b}d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8(bc-ad)^{9/2}} - \frac{35d^2}{24(a+bx)\sqrt{c+dx}(bc-ad)^3} + \frac{7d}{12(a+bx)^2\sqrt{c+dx}(bc-ad)}$$

[Out] $35/8*d^3*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})*b^{(1/2)/(-a*d+b*c)^{(9/2)}-35/8*d^3/(-a*d+b*c)^4/(d*x+c)^{(1/2)}-1/3/(-a*d+b*c)/(b*x+a)^3/(d*x+c)^{(1/2)}+7/12*d/(-a*d+b*c)^2/(b*x+a)^2/(d*x+c)^{(1/2)}-35/24*d^2/(-a*d+b*c)^3/(b*x+a)/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.07, antiderivative size = 173, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$\frac{35d^3}{8\sqrt{c+dx}(bc-ad)^4} - \frac{35d^2}{24(a+bx)\sqrt{c+dx}(bc-ad)^3} + \frac{35\sqrt{b}d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8(bc-ad)^{9/2}} + \frac{7d}{12(a+bx)^2\sqrt{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a+b*x)^4*(c+d*x)^{(3/2))}, x]$

[Out] $(-35*d^3)/(8*(b*c-a*d)^4*\operatorname{Sqrt}[c+d*x]) - 1/(3*(b*c-a*d)*(a+b*x)^3*\operatorname{Sqrt}[c+d*x]) + (7*d)/(12*(b*c-a*d)^2*(a+b*x)^2*\operatorname{Sqrt}[c+d*x]) - (35*d^2)/(24*(b*c-a*d)^3*(a+b*x)*\operatorname{Sqrt}[c+d*x]) + (35*\operatorname{Sqrt}[b]*d^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c+d*x])/(\operatorname{Sqrt}[b*c-a*d])])/(8*(b*c-a*d)^{(9/2)})$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c+d*x)^{(n+1)}/((b*c-a*d)*(m+1)), x] - \operatorname{Dist}[(d*(m+n+2))/((b*c-a*d)*(m+1)), \operatorname{Int}[(a+b*x)^{(m+1)}*(c+d*x)^n, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, n\}, x \ \&\& \ \operatorname{NeQ}[b*c-a*d, 0] \ \&\& \ \operatorname{LtQ}[m, -1] \ \&\& \ !(\operatorname{LtQ}[n, -1] \ \&\& \ (\operatorname{EqQ}[a, 0] \ || \ (\operatorname{NeQ}[c, 0] \ \&\& \ \operatorname{LtQ}[m-n, 0] \ \&\& \ \operatorname{IntegerQ}[n]))) \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c-(a*d)/b+(d*x^p)/b)^n, x], x, (a+b*x)^{(1/p)}], x]] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \ \operatorname{NeQ}[b*c-a*d, 0] \ \&\& \ \operatorname{LtQ}[-1, m, 0] \ \&\& \ \operatorname{LeQ}[-1, n, 0] \ \&\& \ \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]]$

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^4(c+dx)^{3/2}} dx &= -\frac{1}{3(bc-ad)(a+bx)^3\sqrt{c+dx}} - \frac{(7d) \int \frac{1}{(a+bx)^3(c+dx)^{3/2}} dx}{6(bc-ad)} \\
 &= -\frac{1}{3(bc-ad)(a+bx)^3\sqrt{c+dx}} + \frac{7d}{12(bc-ad)^2(a+bx)^2\sqrt{c+dx}} + \frac{(35d^2) \int \frac{1}{(a+bx)^2(c+dx)^{3/2}} dx}{24(bc-ad)} \\
 &= -\frac{1}{3(bc-ad)(a+bx)^3\sqrt{c+dx}} + \frac{7d}{12(bc-ad)^2(a+bx)^2\sqrt{c+dx}} - \frac{35d^2}{24(bc-ad)^3(a+bx)\sqrt{c+dx}} \\
 &= -\frac{35d^3}{8(bc-ad)^4\sqrt{c+dx}} - \frac{1}{3(bc-ad)(a+bx)^3\sqrt{c+dx}} + \frac{7d}{12(bc-ad)^2(a+bx)^2\sqrt{c+dx}} \\
 &= -\frac{35d^3}{8(bc-ad)^4\sqrt{c+dx}} - \frac{1}{3(bc-ad)(a+bx)^3\sqrt{c+dx}} + \frac{7d}{12(bc-ad)^2(a+bx)^2\sqrt{c+dx}} \\
 &= -\frac{35d^3}{8(bc-ad)^4\sqrt{c+dx}} - \frac{1}{3(bc-ad)(a+bx)^3\sqrt{c+dx}} + \frac{7d}{12(bc-ad)^2(a+bx)^2\sqrt{c+dx}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 50, normalized size = 0.29

$$\frac{2d^3 {}_2F_1\left(-\frac{1}{2}, 4; \frac{1}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{\sqrt{c+dx} (ad-bc)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^4*(c + d*x)^(3/2)),x]

[Out] (-2*d^3*Hypergeometric2F1[-1/2, 4, 1/2, -(b*(c + d*x))/(-(b*c) + a*d)]/((-(b*c) + a*d)^4*Sqrt[c + d*x])

[In] integrate(1/(b*x+a)^4/(d*x+c)^(3/2),x, algorithm="giac")

[Out]
$$\frac{-35/8*b*d^3*\arctan(\sqrt{d*x+c}*b/\sqrt{-b^2*c+a*b*d})/((b^4*c^4-4*a*b^3*c^3*d+6*a^2*b^2*c^2*d^2-4*a^3*b*c*d^3+a^4*d^4)*\sqrt{-b^2*c+a*b*d})-2*d^3/((b^4*c^4-4*a*b^3*c^3*d+6*a^2*b^2*c^2*d^2-4*a^3*b*c*d^3+a^4*d^4)*\sqrt{d*x+c})-1/24*(57*(d*x+c)^{(5/2)}*b^3*d^3-136*(d*x+c)^{(3/2)}*b^3*c*d^3+87*\sqrt{d*x+c}*b^3*c^2*d^3+136*(d*x+c)^{(3/2)}*a*b^2*d^4-174*\sqrt{d*x+c}*a*b^2*c*d^4+87*\sqrt{d*x+c}*a^2*b*d^5)/((b^4*c^4-4*a*b^3*c^3*d+6*a^2*b^2*c^2*d^2-4*a^3*b*c*d^3+a^4*d^4)*((d*x+c)*b-b*c+a*d)^3)}$$

maple [B] time = 0.02, size = 292, normalized size = 1.69

$$\frac{29\sqrt{dx+c} a^2 b d^5}{8(ad-bc)^4 (bdx+ad)^3} + \frac{29\sqrt{dx+c} a b^2 c d^4}{4(ad-bc)^4 (bdx+ad)^3} - \frac{29\sqrt{dx+c} b^3 c^2 d^3}{8(ad-bc)^4 (bdx+ad)^3} - \frac{17(dx+c)^{\frac{3}{2}} a b^2 d^4}{3(ad-bc)^4 (bdx+ad)^3} + \frac{17(dx+c)^{\frac{3}{2}} a^2 b c d^3}{3(ad-bc)^4 (bdx+ad)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^4/(d*x+c)^(3/2),x)

[Out]
$$\begin{aligned} & -2*d^3/(a*d-b*c)^4/(d*x+c)^{(1/2)}-19/8*d^3/(a*d-b*c)^4*b^3/(b*d*x+a*d)^3*(d*x+c)^{(5/2)}-17/3*d^4/(a*d-b*c)^4*b^2/(b*d*x+a*d)^3*(d*x+c)^{(3/2)}*a+17/3*d^3/ \\ & (a*d-b*c)^4*b^3/(b*d*x+a*d)^3*(d*x+c)^{(3/2)}*c-29/8*d^5/(a*d-b*c)^4*b/(b*d*x+a*d)^3*(d*x+c)^{(1/2)}*a^2+29/4*d^4/(a*d-b*c)^4*b^2/(b*d*x+a*d)^3*(d*x+c)^{(1/2)}*a*c-29/8*d^3/(a*d-b*c)^4*b^3/(b*d*x+a*d)^3*(d*x+c)^{(1/2)}*c^2-35/8*d^3/(a*d-b*c)^4*b/ \\ & ((a*d-b*c)*b)^{(1/2)}*\arctan((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b) \end{aligned}$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^4/(d*x+c)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.54, size = 294, normalized size = 1.70

$$\frac{\frac{2d^3}{ad-bc} + \frac{35b^2d^3(c+dx)^2}{3(ad-bc)^3} + \frac{35b^3d^3(c+dx)^3}{8(ad-bc)^4} + \frac{77bd^3(c+dx)}{8(ad-bc)^2}}{\sqrt{c+dx} (a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3) + b^3(c+dx)^{7/2} - (3b^3c - 3ab^2d)(c+dx)^{5/2} + (c+dx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^4*(c + d*x)^(3/2)),x)`

[Out]
$$-\left(\frac{2d^3}{(ad - bc)} + \frac{35b^2d^3(c + dx)^2}{3(ad - bc)^3} + \frac{35b^3d^3(c + dx)^3}{8(ad - bc)^4} + \frac{77bd^3(c + dx)}{8(ad - bc)^2}\right) / \left(\frac{(c + dx)^{1/2}(a^3d^3 - b^3c^3 + 3ab^2c^2d - 3a^2b^2cd^2) + b^3(c + dx)^{7/2} - (3b^3c - 3ab^2d)(c + dx)^{5/2} + (c + dx)^{3/2}(3b^3c^2 + 3a^2bd^2 - 6ab^2cd) - (35b^{1/2}d^3 \operatorname{atan}\left(\frac{b^{1/2}(c + dx)^{1/2}(a^4d^4 + b^4c^4 + 6a^2b^2c^2d^2 - 4ab^3c^3d - 4a^3b^2cd^3)}{(ad - bc)^{9/2}}\right))}{8(ad - bc)^{9/2}}\right)$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**4/(d*x+c)**(3/2),x)`

[Out] Timed out

$$3.1434 \quad \int \frac{(a+bx)^5}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=152

$$-\frac{2b^4(c+dx)^{5/2}(bc-ad)}{d^6} + \frac{20b^3(c+dx)^{3/2}(bc-ad)^2}{3d^6} - \frac{20b^2\sqrt{c+dx}(bc-ad)^3}{d^6} - \frac{10b(bc-ad)^4}{d^6\sqrt{c+dx}} + \frac{2(bc-ad)^5}{3d^6(c+dx)^{3/2}} + \frac{2b^5}{d^6}$$

[Out] $2/3*(-a*d+b*c)^5/d^6/(d*x+c)^{(3/2)}+20/3*b^3*(-a*d+b*c)^2*(d*x+c)^{(3/2)}/d^6-2*b^4*(-a*d+b*c)*(d*x+c)^{(5/2)}/d^6+2/7*b^5*(d*x+c)^{(7/2)}/d^6-10*b*(-a*d+b*c)^4/d^6/(d*x+c)^{(1/2)}-20*b^2*(-a*d+b*c)^3*(d*x+c)^{(1/2)}/d^6$

Rubi [A] time = 0.05, antiderivative size = 152, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{2b^4(c+dx)^{5/2}(bc-ad)}{d^6} + \frac{20b^3(c+dx)^{3/2}(bc-ad)^2}{3d^6} - \frac{20b^2\sqrt{c+dx}(bc-ad)^3}{d^6} - \frac{10b(bc-ad)^4}{d^6\sqrt{c+dx}} + \frac{2(bc-ad)^5}{3d^6(c+dx)^{3/2}} + \frac{2b^5}{d^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(c + d*x)^(5/2), x]

[Out] $(2*(b*c - a*d)^5)/(3*d^6*(c + d*x)^{(3/2)}) - (10*b*(b*c - a*d)^4)/(d^6*\text{Sqrt}[c + d*x]) - (20*b^2*(b*c - a*d)^3*\text{Sqrt}[c + d*x])/d^6 + (20*b^3*(b*c - a*d)^2*(c + d*x)^{(3/2)})/(3*d^6) - (2*b^4*(b*c - a*d)*(c + d*x)^{(5/2)})/d^6 + (2*b^5*(c + d*x)^{(7/2)})/(7*d^6)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\int \frac{(a+bx)^5}{(c+dx)^{5/2}} dx = \int \left(\frac{(-bc+ad)^5}{d^5(c+dx)^{5/2}} + \frac{5b(bc-ad)^4}{d^5(c+dx)^{3/2}} - \frac{10b^2(bc-ad)^3}{d^5\sqrt{c+dx}} + \frac{10b^3(bc-ad)^2\sqrt{c+dx}}{d^5} - \frac{5b^4(bc-ad)}{d^5} \right) dx$$

$$= \frac{2(bc-ad)^5}{3d^6(c+dx)^{3/2}} - \frac{10b(bc-ad)^4}{d^6\sqrt{c+dx}} - \frac{20b^2(bc-ad)^3\sqrt{c+dx}}{d^6} + \frac{20b^3(bc-ad)^2(c+dx)^{3/2}}{3d^6} - \frac{2b^4(bc-ad)}{d^6}$$

Mathematica [A] time = 0.12, size = 123, normalized size = 0.81

$$\frac{2(-21b^4(c+dx)^4(bc-ad) + 70b^3(c+dx)^3(bc-ad)^2 - 210b^2(c+dx)^2(bc-ad)^3 - 105b(c+dx)(bc-ad)^4 + 7(b^5c^5 - 256b^5c^5 + 896ab^4c^4d - 1120a^2b^3c^3d^2 + 560a^3b^2c^2d^3 - 70a^4bcd^4 - 7a^5d^5 - 3(2b^5cd^4 - 7ab^4d^5))}{21d^6(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(c + d*x)^(5/2), x]

[Out] (2*(7*(b*c - a*d)^5 - 105*b*(b*c - a*d)^4*(c + d*x) - 210*b^2*(b*c - a*d)^3*(c + d*x)^2 + 70*b^3*(b*c - a*d)^2*(c + d*x)^3 - 21*b^4*(b*c - a*d)*(c + d*x)^4 + 3*b^5*(c + d*x)^5)/(21*d^6*(c + d*x)^(3/2))

fricas [B] time = 0.45, size = 283, normalized size = 1.86

$$\frac{2(3b^5d^5x^5 - 256b^5c^5 + 896ab^4c^4d - 1120a^2b^3c^3d^2 + 560a^3b^2c^2d^3 - 70a^4bcd^4 - 7a^5d^5 - 3(2b^5cd^4 - 7ab^4d^5))}{21d^6(c+dx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^(5/2), x, algorithm="fricas")

[Out] 2/21*(3*b^5*d^5*x^5 - 256*b^5*c^5 + 896*a*b^4*c^4*d - 1120*a^2*b^3*c^3*d^2 + 560*a^3*b^2*c^2*d^3 - 70*a^4*b*c*d^4 - 7*a^5*d^5 - 3*(2*b^5*c*d^4 - 7*a*b^4*d^5)*x^4 + 2*(8*b^5*c^2*d^3 - 28*a*b^4*c*d^4 + 35*a^2*b^3*d^5)*x^3 - 6*(16*b^5*c^3*d^2 - 56*a*b^4*c^2*d^3 + 70*a^2*b^3*c*d^4 - 35*a^3*b^2*d^5)*x^2 - 3*(128*b^5*c^4*d - 448*a*b^4*c^3*d^2 + 560*a^2*b^3*c^2*d^3 - 280*a^3*b^2*c*d^4 + 35*a^4*b*d^5)*x)*sqrt(d*x + c)/(d^8*x^2 + 2*c*d^7*x + c^2*d^6)

giac [B] time = 0.91, size = 335, normalized size = 2.20

$$\frac{2(15(dx+c)b^5c^4 - b^5c^5 - 60(dx+c)ab^4c^3d + 5ab^4c^4d + 90(dx+c)a^2b^3c^2d^2 - 10a^2b^3c^3d^2 - 60(dx+c)a^3b^2c^2d^3 + 10a^3b^2c^2d^3 + 15(dx+c)a^4b^2d^4 - 5a^4b^2c^2d^4 + a^5d^5)/((dx+c)^{3/2}*d^6) + 2/21*(3*(dx+c)^{7/2}*b^5*d^36 - 21*(dx+c)^{5/2}*b^5*c*d^36 + 70*(dx+c)^{3/2}*b^5*c^2*d^36 - 210*sqrt(dx+c)*b^5*c^3*d^36 + 21*(dx+c)^{5/2}*a*b^4*d^37 - 140*(dx+c)^{3/2}*a*b^4*c^3*d^36)}{3(dx+c)^{3/2}d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^(5/2), x, algorithm="giac")

[Out] -2/3*(15*(d*x + c)*b^5*c^4 - b^5*c^5 - 60*(d*x + c)*a*b^4*c^3*d + 5*a*b^4*c^4*d + 90*(d*x + c)*a^2*b^3*c^2*d^2 - 10*a^2*b^3*c^3*d^2 - 60*(d*x + c)*a^3*b^2*c^2*d^3 + 10*a^3*b^2*c^2*d^3 + 15*(d*x + c)*a^4*b^2*d^4 - 5*a^4*b^2*c^2*d^4 + a^5*d^5)/((d*x + c)^(3/2)*d^6) + 2/21*(3*(d*x + c)^(7/2)*b^5*d^36 - 21*(d*x + c)^(5/2)*b^5*c*d^36 + 70*(d*x + c)^(3/2)*b^5*c^2*d^36 - 210*sqrt(d*x + c)*b^5*c^3*d^36 + 21*(d*x + c)^(5/2)*a*b^4*d^37 - 140*(d*x + c)^(3/2)*a*b^4*c^3*d^36)

$$c*d^{37} + 630*\sqrt{d*x + c}*a*b^4*c^2*d^{37} + 70*(d*x + c)^{(3/2)}*a^2*b^3*d^{38} - 630*\sqrt{d*x + c}*a^2*b^3*c*d^{38} + 210*\sqrt{d*x + c}*a^3*b^2*d^{39})/d^{42}$$

maple [B] time = 0.01, size = 273, normalized size = 1.80

$$2 \left(-3b^5x^5d^5 - 21ab^4d^5x^4 + 6b^5cd^4x^4 - 70a^2b^3d^5x^3 + 56ab^4cd^4x^3 - 16b^5c^2d^3x^3 - 210a^3b^2d^5x^2 + 420a^2b^3cd^4x^2 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(d*x+c)^(5/2), x)

[Out]
$$-2/21/(d*x+c)^{(3/2)}*(-3*b^5*d^5*x^5-21*a*b^4*d^5*x^4+6*b^5*c*d^4*x^4-70*a^2*b^3*d^5*x^3+56*a*b^4*c*d^4*x^3-16*b^5*c^2*d^3*x^3-210*a^3*b^2*d^5*x^2+420*a^2*b^3*c*d^4*x^2-336*a*b^4*c^2*d^3*x^2+96*b^5*c^3*d^2*x^2+105*a^4*b*d^5*x-840*a^3*b^2*c*d^4*x+1680*a^2*b^3*c^2*d^3*x-1344*a*b^4*c^3*d^2*x+384*b^5*c^4*d*x+7*a^5*d^5+70*a^4*b*c*d^4-560*a^3*b^2*c^2*d^3+1120*a^2*b^3*c^3*d^2-896*a*b^4*c^4*d+256*b^5*c^5)/d^6$$

maxima [A] time = 1.38, size = 265, normalized size = 1.74

$$2 \left(\frac{3(dx+c)^7 b^5 - 21(b^5c - ab^4d)(dx+c)^5 + 70(b^5c^2 - 2ab^4cd + a^2b^3d^2)(dx+c)^3 - 210(b^5c^3 - 3ab^4c^2d + 3a^2b^3cd^2 - a^3b^2d^3)\sqrt{dx+c}}{d^5} + \frac{7(b^5c^5 - 5ab^4c^4d + 10a^2b^3c^3d^2 - 10a^3b^2c^2d^3 + 5a^4b^2c^2d^4 - a^5d^5 - 15(b^5c^4 - 4a^2b^4c^3d + 6a^2b^3c^2d^2 - 4a^3b^2c^2d^3 + a^4b^2d^4)(d*x + c))}{(d*x + c)^{(3/2)}*d^5} \right) / d$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(d*x+c)^(5/2), x, algorithm="maxima")

[Out]
$$2/21*((3*(d*x + c)^{(7/2)}*b^5 - 21*(b^5*c - a*b^4*d)*(d*x + c)^{(5/2)} + 70*(b^5*c^2 - 2*a*b^4*c*d + a^2*b^3*d^2)*(d*x + c)^{(3/2)} - 210*(b^5*c^3 - 3*a*b^4*c^2*d + 3*a^2*b^3*c*d^2 - a^3*b^2*d^3)*\sqrt{d*x + c}))/d^5 + 7*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c^2*d^4 - a^5*d^5 - 15*(b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c^2*d^3 + a^4*b^2*d^4)*(d*x + c))/((d*x + c)^{(3/2)}*d^5))/d$$

mupad [B] time = 0.08, size = 229, normalized size = 1.51

$$\frac{2b^5(c+dx)^{7/2}}{7d^6} - \frac{(10b^5c - 10ab^4d)(c+dx)^{5/2}}{5d^6} - \frac{\frac{2a^5d^5}{3} - \frac{2b^5c^5}{3}}{3} + (c+dx) \left(10a^4bd^4 - 40a^3b^2cd^3 + 60a^2b^3c^2d^2 - 40a^2b^3c^2d^2 + 60a^2b^3c^2d^2 - 40a^2b^3c^2d^2 + 60a^2b^3c^2d^2 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/(c + d*x)^(5/2), x)

```
[Out] (2*b^5*(c + d*x)^(7/2))/(7*d^6) - ((10*b^5*c - 10*a*b^4*d)*(c + d*x)^(5/2))
/(5*d^6) - ((2*a^5*d^5)/3 - (2*b^5*c^5)/3 + (c + d*x)*(10*b^5*c^4 + 10*a^4*
b*d^4 - 40*a^3*b^2*c*d^3 + 60*a^2*b^3*c^2*d^2 - 40*a*b^4*c^3*d) - (20*a^2*b
^3*c^3*d^2)/3 + (20*a^3*b^2*c^2*d^3)/3 + (10*a*b^4*c^4*d)/3 - (10*a^4*b*c*d
^4)/3)/(d^6*(c + d*x)^(3/2)) + (20*b^2*(a*d - b*c)^3*(c + d*x)^(1/2))/d^6 +
(20*b^3*(a*d - b*c)^2*(c + d*x)^(3/2))/(3*d^6)
```

sympy [A] time = 59.93, size = 196, normalized size = 1.29

$$\frac{2b^5(c+dx)^{\frac{7}{2}}}{7d^6} - \frac{10b(ad-bc)^4}{d^6\sqrt{c+dx}} + \frac{(c+dx)^{\frac{5}{2}}(10ab^4d-10b^5c)}{5d^6} + \frac{(c+dx)^{\frac{3}{2}}(20a^2b^3d^2-40ab^4cd+20b^5c^2)}{3d^6} + \frac{\sqrt{c+dx}}{d^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**5/(d*x+c)**(5/2),x)
```

```
[Out] 2*b**5*(c + d*x)**(7/2)/(7*d**6) - 10*b*(a*d - b*c)**4/(d**6*sqrt(c + d*x))
+ (c + d*x)**(5/2)*(10*a*b**4*d - 10*b**5*c)/(5*d**6) + (c + d*x)**(3/2)*
(20*a**2*b**3*d**2 - 40*a*b**4*c*d + 20*b**5*c**2)/(3*d**6) + sqrt(c + d*x)*
(20*a**3*b**2*d**3 - 60*a**2*b**3*c*d**2 + 60*a*b**4*c**2*d - 20*b**5*c**3)
/d**6 - 2*(a*d - b*c)**5/(3*d**6*(c + d*x)**(3/2))
```

$$3.1435 \quad \int \frac{(a+bx)^4}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=125

$$-\frac{8b^3(c+dx)^{3/2}(bc-ad)}{3d^5} + \frac{12b^2\sqrt{c+dx}(bc-ad)^2}{d^5} + \frac{8b(bc-ad)^3}{d^5\sqrt{c+dx}} - \frac{2(bc-ad)^4}{3d^5(c+dx)^{3/2}} + \frac{2b^4(c+dx)^{5/2}}{5d^5}$$

[Out] $-2/3*(-a*d+b*c)^4/d^5/(d*x+c)^{(3/2)}-8/3*b^3*(-a*d+b*c)*(d*x+c)^{(3/2)}/d^5+2/5*b^4*(d*x+c)^{(5/2)}/d^5+8*b*(-a*d+b*c)^3/d^5/(d*x+c)^{(1/2)}+12*b^2*(-a*d+b*c)^2*(d*x+c)^{(1/2)}/d^5$

Rubi [A] time = 0.04, antiderivative size = 125, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{8b^3(c+dx)^{3/2}(bc-ad)}{3d^5} + \frac{12b^2\sqrt{c+dx}(bc-ad)^2}{d^5} + \frac{8b(bc-ad)^3}{d^5\sqrt{c+dx}} - \frac{2(bc-ad)^4}{3d^5(c+dx)^{3/2}} + \frac{2b^4(c+dx)^{5/2}}{5d^5}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^4/(c + d*x)^(5/2), x]

[Out] $(-2*(b*c - a*d)^4)/(3*d^5*(c + d*x)^{(3/2)}) + (8*b*(b*c - a*d)^3)/(d^5*\text{Sqrt}[c + d*x]) + (12*b^2*(b*c - a*d)^2*\text{Sqrt}[c + d*x])/d^5 - (8*b^3*(b*c - a*d)*(c + d*x)^{(3/2)})/(3*d^5) + (2*b^4*(c + d*x)^{(5/2)})/(5*d^5)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LtQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^4}{(c+dx)^{5/2}} dx &= \int \left(\frac{(-bc+ad)^4}{d^4(c+dx)^{5/2}} - \frac{4b(bc-ad)^3}{d^4(c+dx)^{3/2}} + \frac{6b^2(bc-ad)^2}{d^4\sqrt{c+dx}} - \frac{4b^3(bc-ad)\sqrt{c+dx}}{d^4} + \frac{b^4(c+dx)^{3/2}}{d^4} \right) dx \\ &= -\frac{2(bc-ad)^4}{3d^5(c+dx)^{3/2}} + \frac{8b(bc-ad)^3}{d^5\sqrt{c+dx}} + \frac{12b^2(bc-ad)^2\sqrt{c+dx}}{d^5} - \frac{8b^3(bc-ad)(c+dx)^{3/2}}{3d^5} + \frac{2b^4(c+dx)^{5/2}}{5d^5} \end{aligned}$$

Mathematica [A] time = 0.08, size = 101, normalized size = 0.81

$$\frac{2(-20b^3(c+dx)^3(bc-ad) + 90b^2(c+dx)^2(bc-ad)^2 + 60b(c+dx)(bc-ad)^3 - 5(bc-ad)^4 + 3b^4(c+dx)^4)}{15d^5(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^4/(c + d*x)^(5/2), x]

[Out] (2*(-5*(b*c - a*d)^4 + 60*b*(b*c - a*d)^3*(c + d*x) + 90*b^2*(b*c - a*d)^2*(c + d*x)^2 - 20*b^3*(b*c - a*d)*(c + d*x)^3 + 3*b^4*(c + d*x)^4)/(15*d^5*(c + d*x)^(3/2))

fricas [A] time = 0.45, size = 203, normalized size = 1.62

$$\frac{2(3b^4d^4x^4 + 128b^4c^4 - 320ab^3c^3d + 240a^2b^2c^2d^2 - 40a^3bcd^3 - 5a^4d^4 - 4(2b^4cd^3 - 5ab^3d^4)x^3 + 6(8b^4c^2d^2 - 20a^3b^3c^3d + 15a^2b^2c^2d^4)x^2 + 12(16b^4c^3d - 40a^3b^3c^2d^2 + 30a^2b^2c^3d - 5a^3b^3d^4)x)*\sqrt{d*x + c}}{15(d^7x^2 + 2cd^6x + c^2d^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^(5/2), x, algorithm="fricas")

[Out] 2/15*(3*b^4*d^4*x^4 + 128*b^4*c^4 - 320*a*b^3*c^3*d + 240*a^2*b^2*c^2*d^2 - 40*a^3*b*c*d^3 - 5*a^4*d^4 - 4*(2*b^4*c*d^3 - 5*a*b^3*d^4)*x^3 + 6*(8*b^4*c^2*d^2 - 20*a*b^3*c*d^3 + 15*a^2*b^2*d^4)*x^2 + 12*(16*b^4*c^3*d - 40*a*b^3*c^2*d^2 + 30*a^2*b^2*c*d^3 - 5*a^3*b*d^4)*x)*sqrt(d*x + c)/(d^7*x^2 + 2*c*d^6*x + c^2*d^5)

giac [B] time = 1.02, size = 229, normalized size = 1.83

$$\frac{2(12(dx+c)b^4c^3 - b^4c^4 - 36(dx+c)ab^3c^2d + 4ab^3c^3d + 36(dx+c)a^2b^2cd^2 - 6a^2b^2c^2d^2 - 12(dx+c)a^3bd^3 + 3(dx+c)^{\frac{3}{2}}d^5)}{3(dx+c)^{\frac{3}{2}}d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^(5/2), x, algorithm="giac")

[Out] 2/3*(12*(d*x + c)*b^4*c^3 - b^4*c^4 - 36*(d*x + c)*a*b^3*c^2*d + 4*a*b^3*c^3*d + 36*(d*x + c)*a^2*b^2*c*d^2 - 6*a^2*b^2*c^2*d^2 - 12*(d*x + c)*a^3*b*d^3 + 4*a^3*b*c*d^3 - a^4*d^4)/((d*x + c)^(3/2)*d^5) + 2/15*(3*(d*x + c)^(5/2)*b^4*d^20 - 20*(d*x + c)^(3/2)*b^4*c*d^20 + 90*sqrt(d*x + c)*b^4*c^2*d^20 + 20*(d*x + c)^(3/2)*a*b^3*d^21 - 180*sqrt(d*x + c)*a*b^3*c*d^21 + 90*sqrt(d*x + c)*a^2*b^2*d^22)/d^25

maple [A] time = 0.01, size = 186, normalized size = 1.49

$$\frac{2 \left(-3b^4x^4d^4 - 20ab^3d^4x^3 + 8b^4cd^3x^3 - 90a^2b^2d^4x^2 + 120ab^3cd^3x^2 - 48b^4c^2d^2x^2 + 60a^3bd^4x - 360a^2b^2cd^3x - \right)}{15(dx+c)^{\frac{3}{2}}d^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^4/(d*x+c)^(5/2), x)

[Out] $-\frac{2}{15} \frac{(-3b^4d^4x^4 - 20a^2b^3d^4x^3 + 8b^4cd^3x^3 - 90a^2b^2d^4x^2 + 120ab^3cd^3x^2 - 48b^4c^2d^2x^2 + 60a^3bd^4x - 360a^2b^2cd^3x + 480a^3b^3c^2d^2x - 192b^4c^3d^2x + 5a^4d^4 + 40a^3b^2cd^3 - 240a^2b^2c^2d^2 + 320a^2b^3c^3d - 128b^4c^4)}{d^5}$

maxima [A] time = 1.46, size = 187, normalized size = 1.50

$$2 \left(\frac{3(dx+c)^{\frac{5}{2}}b^4 - 20(b^4c - ab^3d)(dx+c)^{\frac{3}{2}} + 90(b^4c^2 - 2ab^3cd + a^2b^2d^2)\sqrt{dx+c}}{d^4} - \frac{5(b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4 - 12(b^4c^3 - 3ab^3c^2d + 3a^2b^3c^2d + 3a^2b^2c^2d^2 - a^3b^2cd^3)(dx+c))}{(dx+c)^{\frac{3}{2}}d^4} \right) / 15d$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^4/(d*x+c)^(5/2), x, algorithm="maxima")

[Out] $\frac{2}{15} \frac{((3(dx+c)^{\frac{5}{2}}b^4 - 20(b^4c - ab^3d)(dx+c)^{\frac{3}{2}} + 90(b^4c^2 - 2a^2b^3cd + a^2b^2d^2)\sqrt{dx+c})/d^4 - 5(b^4c^4 - 4a^3b^3c^3d + 6a^2b^2c^2d^2 - 4a^3b^2cd^3 + a^4d^4 - 12(b^4c^3 - 3a^2b^3c^2d + 3a^2b^2c^2d^2 - a^3b^2cd^3)(dx+c))}{(dx+c)^{\frac{3}{2}}d^4}}{d}$

mupad [B] time = 0.30, size = 175, normalized size = 1.40

$$\frac{2b^4(c+dx)^{5/2}}{5d^5} - \frac{(8b^4c - 8ab^3d)(c+dx)^{3/2}}{3d^5} + \frac{(c+dx)(-8a^3bd^3 + 24a^2b^2cd^2 - 24ab^3c^2d + 8b^4c^3) - \frac{2a^4d}{3}}{d^5(c+dx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^4/(c + d*x)^(5/2), x)

[Out] $\frac{(2b^4(c+dx)^{\frac{5}{2}})/(5d^5) - ((8b^4c - 8a^2b^3d)(c+dx)^{\frac{3}{2}})/(3d^5) + ((c+dx)(8b^4c^3 - 8a^3b^2cd^3 + 24a^2b^2c^2d^2 - 24a^2b^3cd^2) - (2a^4d^4)/3 - (2b^4c^4)/3 - 4a^2b^2c^2d^2 + (8a^2b^3c^3d)/3 + (8a^3b^2cd^3)/3)/(d^5(c+dx)^{\frac{3}{2}}) + (12b^2(a*d - b*c)^2(c+dx)^{\frac{1}{2}})/d^5}$

sympy [A] time = 43.59, size = 136, normalized size = 1.09

$$\frac{2b^4(c+dx)^{\frac{5}{2}}}{5d^5} - \frac{8b(ad-bc)^3}{d^5\sqrt{c+dx}} + \frac{(c+dx)^{\frac{3}{2}}(8ab^3d-8b^4c)}{3d^5} + \frac{\sqrt{c+dx}(12a^2b^2d^2-24ab^3cd+12b^4c^2)}{d^5} - \frac{2(ad-bc)^4}{3d^5(c+dx)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**4/(d*x+c)**(5/2),x)

[Out] $2*b**4*(c + d*x)**(5/2)/(5*d**5) - 8*b*(a*d - b*c)**3/(d**5*\text{sqrt}(c + d*x))$
 $+ (c + d*x)**(3/2)*(8*a*b**3*d - 8*b**4*c)/(3*d**5) + \text{sqrt}(c + d*x)*(12*a**$
 $2*b**2*d**2 - 24*a*b**3*c*d + 12*b**4*c**2)/d**5 - 2*(a*d - b*c)**4/(3*d**5$
 $*(c + d*x)**(3/2))$

$$3.1436 \quad \int \frac{(a+bx)^3}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=96

$$-\frac{6b^2\sqrt{c+dx}(bc-ad)}{d^4} - \frac{6b(bc-ad)^2}{d^4\sqrt{c+dx}} + \frac{2(bc-ad)^3}{3d^4(c+dx)^{3/2}} + \frac{2b^3(c+dx)^{3/2}}{3d^4}$$

[Out] $2/3*(-a*d+b*c)^3/d^4/(d*x+c)^{(3/2)}+2/3*b^3*(d*x+c)^{(3/2)}/d^4-6*b*(-a*d+b*c)^2/d^4/(d*x+c)^{(1/2)}-6*b^2*(-a*d+b*c)*(d*x+c)^{(1/2)}/d^4$

Rubi [A] time = 0.03, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$-\frac{6b^2\sqrt{c+dx}(bc-ad)}{d^4} - \frac{6b(bc-ad)^2}{d^4\sqrt{c+dx}} + \frac{2(bc-ad)^3}{3d^4(c+dx)^{3/2}} + \frac{2b^3(c+dx)^{3/2}}{3d^4}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3/(c + d*x)^(5/2), x]

[Out] $(2*(b*c - a*d)^3)/(3*d^4*(c + d*x)^{(3/2)}) - (6*b*(b*c - a*d)^2)/(d^4*\text{Sqrt}[c + d*x]) - (6*b^2*(b*c - a*d)*\text{Sqrt}[c + d*x])/d^4 + (2*b^3*(c + d*x)^{(3/2)})/(3*d^4)$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^3}{(c+dx)^{5/2}} dx &= \int \left(\frac{(-bc+ad)^3}{d^3(c+dx)^{5/2}} + \frac{3b(bc-ad)^2}{d^3(c+dx)^{3/2}} - \frac{3b^2(bc-ad)}{d^3\sqrt{c+dx}} + \frac{b^3\sqrt{c+dx}}{d^3} \right) dx \\ &= \frac{2(bc-ad)^3}{3d^4(c+dx)^{3/2}} - \frac{6b(bc-ad)^2}{d^4\sqrt{c+dx}} - \frac{6b^2(bc-ad)\sqrt{c+dx}}{d^4} + \frac{2b^3(c+dx)^{3/2}}{3d^4} \end{aligned}$$

Mathematica [A] time = 0.06, size = 76, normalized size = 0.79

$$\frac{2(-9b^2(c+dx)^2(bc-ad) - 9b(c+dx)(bc-ad)^2 + (bc-ad)^3 + b^3(c+dx)^3)}{3d^4(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3/(c + d*x)^(5/2), x]

[Out] $(2*((b*c - a*d)^3 - 9*b*(b*c - a*d)^2*(c + d*x) - 9*b^2*(b*c - a*d)*(c + d*x)^2 + b^3*(c + d*x)^3))/(3*d^4*(c + d*x)^(3/2))$

fricas [A] time = 0.44, size = 136, normalized size = 1.42

$$\frac{2(b^3 d^3 x^3 - 16 b^3 c^3 + 24 a b^2 c^2 d - 6 a^2 b c d^2 - a^3 d^3 - 3(2 b^3 c d^2 - 3 a b^2 d^3)x^2 - 3(8 b^3 c^2 d - 12 a b^2 c d^2 + 3 a^2 b d^3)x)}{3(d^6 x^2 + 2 c d^5 x + c^2 d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^(5/2), x, algorithm="fricas")

[Out] $2/3*(b^3*d^3*x^3 - 16*b^3*c^3 + 24*a*b^2*c^2*d - 6*a^2*b*c*d^2 - a^3*d^3 - 3*(2*b^3*c*d^2 - 3*a*b^2*d^3)*x^2 - 3*(8*b^3*c^2*d - 12*a*b^2*c*d^2 + 3*a^2*b*d^3)*x)*\text{sqrt}(d*x + c)/(d^6*x^2 + 2*c*d^5*x + c^2*d^4)$

giac [A] time = 1.00, size = 141, normalized size = 1.47

$$\frac{2(9(dx+c)b^3c^2 - b^3c^3 - 18(dx+c)ab^2cd + 3ab^2c^2d + 9(dx+c)a^2bd^2 - 3a^2bcd^2 + a^3d^3)}{3(dx+c)^{\frac{3}{2}}d^4} + \frac{2((dx+c)^{\frac{3}{2}}b^3d^8)}{3(dx+c)^{\frac{3}{2}}d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^(5/2), x, algorithm="giac")

[Out] $-2/3*(9*(d*x + c)*b^3*c^2 - b^3*c^3 - 18*(d*x + c)*a*b^2*c*d + 3*a*b^2*c^2*d + 9*(d*x + c)*a^2*b*d^2 - 3*a^2*b*c*d^2 + a^3*d^3)/((d*x + c)^(3/2)*d^4) + 2/3*((d*x + c)^(3/2)*b^3*d^8 - 9*\text{sqrt}(d*x + c)*b^3*c*d^8 + 9*\text{sqrt}(d*x + c)*a*b^2*d^9)/d^12$

maple [A] time = 0.01, size = 115, normalized size = 1.20

$$\frac{2(-b^3 x^3 d^3 - 9 a b^2 d^3 x^2 + 6 b^3 c d^2 x^2 + 9 a^2 b d^3 x - 36 a b^2 c d^2 x + 24 b^3 c^2 d x + a^3 d^3 + 6 a^2 b c d^2 - 24 a b^2 c^2 d + 16 b^3 c^3)}{3(dx+c)^{\frac{3}{2}}d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^3/(d*x+c)^(5/2), x)

[Out] $-2/3/(d*x+c)^(3/2)*(-b^3*d^3*x^3-9*a*b^2*d^3*x^2+6*b^3*c*d^2*x^2+9*a^2*b*d^3*x-36*a*b^2*c*d^2*x+24*b^3*c^2*d*x+a^3*d^3+6*a^2*b*c*d^2-24*a*b^2*c^2*d+16*b^3*c^3)/d^4$

maxima [A] time = 1.37, size = 122, normalized size = 1.27

$$2 \frac{\left(\frac{(dx+c)^2 b^3 - 9(b^3 c - ab^2 d) \sqrt{dx+c}}{d^3} + \frac{b^3 c^3 - 3ab^2 c^2 d + 3a^2 b c d^2 - a^3 d^3 - 9(b^3 c^2 - 2ab^2 c d + a^2 b d^2)(dx+c)}{(dx+c)^2 d^3} \right)}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] $\frac{2/3 * (((d*x + c)^{(3/2)} * b^3 - 9 * (b^3 * c - a * b^2 * d) * \text{sqrt}(d*x + c)) / d^3 + (b^3 * c^3 - 3 * a * b^2 * c^2 * d + 3 * a^2 * b * c * d^2 - a^3 * d^3 - 9 * (b^3 * c^2 - 2 * a * b^2 * c * d + a^2 * b * d^2) * (d*x + c)) / ((d*x + c)^{(3/2)} * d^3))}{d}$

mupad [B] time = 0.09, size = 128, normalized size = 1.33

$$\frac{2b^3(c+dx)^3 - 2a^3d^3 + 2b^3c^3 - 18b^3c(c+dx)^2 - 18b^3c^2(c+dx) + 18a^2bd(c+dx)^2 - 18a^2bd^2(c+dx)}{3d^4(c+dx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^3/(c + d*x)^(5/2),x)

[Out] $\frac{(2 * b^3 * (c + d * x)^3 - 2 * a^3 * d^3 + 2 * b^3 * c^3 - 18 * b^3 * c * (c + d * x)^2 - 18 * b^3 * c^2 * (c + d * x) + 18 * a^2 * b * d * (c + d * x)^2 - 18 * a^2 * b * d^2 * (c + d * x) + 36 * a^2 * b * c * d * (c + d * x))}{(3 * d^4 * (c + d * x)^{(3/2)})}$

sympy [A] time = 1.44, size = 461, normalized size = 4.80

$$\left\{ \begin{array}{l} \frac{2a^3d^3}{3cd^4\sqrt{c+dx}+3d^5x\sqrt{c+dx}} - \frac{12a^2bcd^2}{3cd^4\sqrt{c+dx}+3d^5x\sqrt{c+dx}} - \frac{18a^2bd^3x}{3cd^4\sqrt{c+dx}+3d^5x\sqrt{c+dx}} + \frac{48ab^2c^2d}{3cd^4\sqrt{c+dx}+3d^5x\sqrt{c+dx}} + \frac{72ab^2cd^2x}{3cd^4\sqrt{c+dx}+3d^5x\sqrt{c+dx}} \\ \frac{a^3x + \frac{3a^2bx^2}{2} + ab^2x^3 + \frac{b^3x^4}{4}}{c^{\frac{5}{2}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**3/(d*x+c)**(5/2),x)

[Out] Piecewise((-2*a**3*d**3/(3*c*d**4*sqrt(c + d*x) + 3*d**5*x*sqrt(c + d*x)) - 12*a**2*b*c*d**2/(3*c*d**4*sqrt(c + d*x) + 3*d**5*x*sqrt(c + d*x)) - 18*a**2*b*d**3*x/(3*c*d**4*sqrt(c + d*x) + 3*d**5*x*sqrt(c + d*x)) + 48*a*b**2*c**2*d/(3*c*d**4*sqrt(c + d*x) + 3*d**5*x*sqrt(c + d*x)) + 72*a*b**2*c*d**2*x/(3*c*d**4*sqrt(c + d*x) + 3*d**5*x*sqrt(c + d*x)) + 18*a*b**2*d**3*x**2/(3*c*d**4*sqrt(c + d*x) + 3*d**5*x*sqrt(c + d*x)) - 32*b**3*c**3/(3*c*d**4*s

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qrt(c + d*x) + 3*d**5*x*sqrt(c + d*x)) - 48*b**3*c**2*d*x/(3*c*d**4*sqrt(c
+ d*x) + 3*d**5*x*sqrt(c + d*x)) - 12*b**3*c*d**2*x**2/(3*c*d**4*sqrt(c + d
*x) + 3*d**5*x*sqrt(c + d*x)) + 2*b**3*d**3*x**3/(3*c*d**4*sqrt(c + d*x) +
3*d**5*x*sqrt(c + d*x)), Ne(d, 0)), ((a**3*x + 3*a**2*b*x**2/2 + a*b**2*x**
3 + b**3*x**4/4)/c**(5/2), True))

```

$$3.1437 \quad \int \frac{(a+bx)^2}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=67

$$\frac{4b(bc-ad)}{d^3\sqrt{c+dx}} - \frac{2(bc-ad)^2}{3d^3(c+dx)^{3/2}} + \frac{2b^2\sqrt{c+dx}}{d^3}$$

[Out] $-2/3*(-a*d+b*c)^2/d^3/(d*x+c)^{(3/2)}+4*b*(-a*d+b*c)/d^3/(d*x+c)^{(1/2)}+2*b^2*(d*x+c)^{(1/2)}/d^3$

Rubi [A] time = 0.02, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {43}

$$\frac{4b(bc-ad)}{d^3\sqrt{c+dx}} - \frac{2(bc-ad)^2}{3d^3(c+dx)^{3/2}} + \frac{2b^2\sqrt{c+dx}}{d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2/(c + d*x)^(5/2), x]

[Out] $(-2*(b*c - a*d)^2)/(3*d^3*(c + d*x)^{(3/2)}) + (4*b*(b*c - a*d))/(d^3*\text{Sqrt}[c + d*x]) + (2*b^2*\text{Sqrt}[c + d*x])/d^3$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^2}{(c+dx)^{5/2}} dx &= \int \left(\frac{(-bc+ad)^2}{d^2(c+dx)^{5/2}} - \frac{2b(bc-ad)}{d^2(c+dx)^{3/2}} + \frac{b^2}{d^2\sqrt{c+dx}} \right) dx \\ &= -\frac{2(bc-ad)^2}{3d^3(c+dx)^{3/2}} + \frac{4b(bc-ad)}{d^3\sqrt{c+dx}} + \frac{2b^2\sqrt{c+dx}}{d^3} \end{aligned}$$

Mathematica [A] time = 0.04, size = 62, normalized size = 0.93

$$\frac{-2a^2d^2 - 4abd(2c + 3dx) + 2b^2(8c^2 + 12cdx + 3d^2x^2)}{3d^3(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2/(c + d*x)^(5/2), x]

[Out] $(-2*a^2*d^2 - 4*a*b*d*(2*c + 3*d*x) + 2*b^2*(8*c^2 + 12*c*d*x + 3*d^2*x^2)) / (3*d^3*(c + d*x)^(3/2))$

fricas [A] time = 0.42, size = 85, normalized size = 1.27

$$\frac{2 \left(3 b^2 d^2 x^2 + 8 b^2 c^2 - 4 a b c d - a^2 d^2 + 6 \left(2 b^2 c d - a b d^2 \right) x \right) \sqrt{d x + c}}{3 \left(d^5 x^2 + 2 c d^4 x + c^2 d^3 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^(5/2), x, algorithm="fricas")

[Out] $2/3*(3*b^2*d^2*x^2 + 8*b^2*c^2 - 4*a*b*c*d - a^2*d^2 + 6*(2*b^2*c*d - a*b*d^2)*x)*sqrt(d*x + c)/(d^5*x^2 + 2*c*d^4*x + c^2*d^3)$

giac [A] time = 1.11, size = 72, normalized size = 1.07

$$\frac{2 \sqrt{d x + c} b^2}{d^3} + \frac{2 \left(6 (d x + c) b^2 c - b^2 c^2 - 6 (d x + c) a b d + 2 a b c d - a^2 d^2 \right)}{3 (d x + c)^{\frac{3}{2}} d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^(5/2), x, algorithm="giac")

[Out] $2*sqrt(d*x + c)*b^2/d^3 + 2/3*(6*(d*x + c)*b^2*c - b^2*c^2 - 6*(d*x + c)*a*b*d + 2*a*b*c*d - a^2*d^2)/((d*x + c)^(3/2)*d^3)$

maple [A] time = 0.01, size = 62, normalized size = 0.93

$$-\frac{2 \left(-3 b^2 x^2 d^2 + 6 a b d^2 x - 12 b^2 c d x + a^2 d^2 + 4 a b c d - 8 b^2 c^2 \right)}{3 (d x + c)^{\frac{3}{2}} d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^2/(d*x+c)^(5/2), x)

[Out] $-2/3/(d*x+c)^(3/2)*(-3*b^2*d^2*x^2+6*a*b*d^2*x-12*b^2*c*d*x+a^2*d^2+4*a*b*c*d-8*b^2*c^2)/d^3$

maxima [A] time = 1.39, size = 72, normalized size = 1.07

$$\frac{2 \left(\frac{3 \sqrt{d x + c} b^2}{d^2} - \frac{b^2 c^2 - 2 a b c d + a^2 d^2 - 6 (b^2 c - a b d) (d x + c)}{(d x + c)^{\frac{3}{2}} d^2} \right)}{3 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] $\frac{2}{3} \cdot \frac{(3\sqrt{d*x+c} \cdot b^2/d^2 - (b^2*c^2 - 2*a*b*c*d + a^2*d^2 - 6*(b^2*c - a*b*d)*(d*x+c))/((d*x+c)^{(3/2)}*d^2))/d}{d}$

mupad [B] time = 0.07, size = 68, normalized size = 1.01

$$\frac{6b^2(c+dx)^2 - 2a^2d^2 - 2b^2c^2 + 12b^2c(c+dx) - 12abd(c+dx) + 4abcd}{3d^3(c+dx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^2/(c + d*x)^(5/2),x)

[Out] $\frac{(6*b^2*(c+d*x)^2 - 2*a^2*d^2 - 2*b^2*c^2 + 12*b^2*c*(c+d*x) - 12*a*b*d*(c+d*x) + 4*a*b*c*d)/(3*d^3*(c+d*x)^{(3/2)})}{c^2}$

sympy [A] time = 1.27, size = 265, normalized size = 3.96

$$\left\{ \begin{array}{l} \frac{2a^2d^2}{3cd^3\sqrt{c+dx}+3d^4x\sqrt{c+dx}} - \frac{8abcd}{3cd^3\sqrt{c+dx}+3d^4x\sqrt{c+dx}} - \frac{12abd^2x}{3cd^3\sqrt{c+dx}+3d^4x\sqrt{c+dx}} + \frac{16b^2c^2}{3cd^3\sqrt{c+dx}+3d^4x\sqrt{c+dx}} + \frac{24b^2cdx}{3cd^3\sqrt{c+dx}+3d^4x\sqrt{c+dx}} \\ \frac{a^2x+abx^2+\frac{b^2x^3}{3}}{c^{\frac{5}{2}}} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**2/(d*x+c)**(5/2),x)

[Out] Piecewise((-2*a**2*d**2/(3*c*d**3*sqrt(c + d*x) + 3*d**4*x*sqrt(c + d*x)) - 8*a*b*c*d/(3*c*d**3*sqrt(c + d*x) + 3*d**4*x*sqrt(c + d*x)) - 12*a*b*d**2*x/(3*c*d**3*sqrt(c + d*x) + 3*d**4*x*sqrt(c + d*x)) + 16*b**2*c**2/(3*c*d**3*sqrt(c + d*x) + 3*d**4*x*sqrt(c + d*x)) + 24*b**2*c*d*x/(3*c*d**3*sqrt(c + d*x) + 3*d**4*x*sqrt(c + d*x)) + 6*b**2*d**2*x**2/(3*c*d**3*sqrt(c + d*x) + 3*d**4*x*sqrt(c + d*x)), Ne(d, 0)), ((a**2*x + a*b*x**2 + b**2*x**3/3)/c**5/2, True))

$$3.1438 \quad \int \frac{a+bx}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=40

$$\frac{2(bc-ad)}{3d^2(c+dx)^{3/2}} - \frac{2b}{d^2\sqrt{c+dx}}$$

[Out] $2/3*(-a*d+b*c)/d^2/(d*x+c)^(3/2)-2*b/d^2/(d*x+c)^(1/2)$

Rubi [A] time = 0.01, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{2(bc-ad)}{3d^2(c+dx)^{3/2}} - \frac{2b}{d^2\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)/(c + d*x)^(5/2), x]

[Out] $(2*(b*c - a*d))/(3*d^2*(c + d*x)^(3/2)) - (2*b)/(d^2*sqrt[c + d*x])$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{a+bx}{(c+dx)^{5/2}} dx &= \int \left(\frac{-bc+ad}{d(c+dx)^{5/2}} + \frac{b}{d(c+dx)^{3/2}} \right) dx \\ &= \frac{2(bc-ad)}{3d^2(c+dx)^{3/2}} - \frac{2b}{d^2\sqrt{c+dx}} \end{aligned}$$

Mathematica [A] time = 0.02, size = 29, normalized size = 0.72

$$-\frac{2(ad+2bc+3bdx)}{3d^2(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)/(c + d*x)^(5/2), x]

[Out] $(-2*(2*b*c + a*d + 3*b*d*x))/(3*d^2*(c + d*x)^{(3/2)})$

fricas [A] time = 0.49, size = 46, normalized size = 1.15

$$\frac{2(3bdx + 2bc + ad)\sqrt{dx + c}}{3(d^4x^2 + 2cd^3x + c^2d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)^(5/2),x, algorithm="fricas")`

[Out] $-2/3*(3*b*d*x + 2*b*c + a*d)*\text{sqrt}(d*x + c)/(d^4*x^2 + 2*c*d^3*x + c^2*d^2)$

giac [A] time = 1.02, size = 28, normalized size = 0.70

$$\frac{2(3(dx + c)b - bc + ad)}{3(dx + c)^{\frac{3}{2}}d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)^(5/2),x, algorithm="giac")`

[Out] $-2/3*(3*(d*x + c)*b - b*c + a*d)/((d*x + c)^{(3/2)}*d^2)$

maple [A] time = 0.00, size = 26, normalized size = 0.65

$$\frac{2(3bdx + ad + 2bc)}{3(dx + c)^{\frac{3}{2}}d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)/(d*x+c)^(5/2),x)`

[Out] $-2/3/(d*x+c)^{(3/2)}*(3*b*d*x+a*d+2*b*c)/d^2$

maxima [A] time = 1.28, size = 28, normalized size = 0.70

$$\frac{2(3(dx + c)b - bc + ad)}{3(dx + c)^{\frac{3}{2}}d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)^(5/2),x, algorithm="maxima")`

[Out] $-2/3*(3*(d*x + c)*b - b*c + a*d)/((d*x + c)^{(3/2)}*d^2)$

mupad [B] time = 0.25, size = 29, normalized size = 0.72

$$-\frac{2ad - 2bc + 6b(c + dx)}{3d^2(c + dx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)/(c + d*x)^(5/2), x)`

[Out] `-(2*a*d - 2*b*c + 6*b*(c + d*x))/(3*d^2*(c + d*x)^(3/2))`

sympy [A] time = 1.12, size = 124, normalized size = 3.10

$$\begin{cases} -\frac{2ad}{3cd^2\sqrt{c+dx}+3d^3x\sqrt{c+dx}} - \frac{4bc}{3cd^2\sqrt{c+dx}+3d^3x\sqrt{c+dx}} - \frac{6bdx}{3cd^2\sqrt{c+dx}+3d^3x\sqrt{c+dx}} & \text{for } d \neq 0 \\ \frac{ax + \frac{bx^2}{2}}{c^{5/2}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)/(d*x+c)**(5/2), x)`

[Out] `Piecewise((-2*a*d/(3*c*d**2*sqrt(c + d*x) + 3*d**3*x*sqrt(c + d*x)) - 4*b*c/(3*c*d**2*sqrt(c + d*x) + 3*d**3*x*sqrt(c + d*x)) - 6*b*d*x/(3*c*d**2*sqrt(c + d*x) + 3*d**3*x*sqrt(c + d*x)), Ne(d, 0)), ((a*x + b*x**2/2)/c**(5/2), True))`

$$3.1439 \quad \int \frac{1}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=16

$$-\frac{2}{3d(c+dx)^{3/2}}$$

[Out] -2/3/d/(d*x+c)^(3/2)

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {32}

$$-\frac{2}{3d(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(-5/2), x]

[Out] -2/(3*d*(c + d*x)^(3/2))

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(c+dx)^{5/2}} dx = -\frac{2}{3d(c+dx)^{3/2}}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$-\frac{2}{3d(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(-5/2), x]

[Out] -2/(3*d*(c + d*x)^(3/2))

fricas [B] time = 0.43, size = 31, normalized size = 1.94

$$-\frac{2\sqrt{dx+c}}{3(d^3x^2+2cd^2x+c^2d)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^(5/2),x, algorithm="fricas")

[Out] -2/3*sqrt(d*x + c)/(d^3*x^2 + 2*c*d^2*x + c^2*d)

giac [A] time = 0.96, size = 12, normalized size = 0.75

$$-\frac{2}{3(dx+c)^{\frac{3}{2}}d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^(5/2),x, algorithm="giac")

[Out] -2/3/((d*x + c)^(3/2)*d)

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$-\frac{2}{3(dx+c)^{\frac{3}{2}}d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^(5/2),x)

[Out] -2/3/d/(d*x+c)^(3/2)

maxima [A] time = 1.36, size = 12, normalized size = 0.75

$$-\frac{2}{3(dx+c)^{\frac{3}{2}}d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] -2/3/((d*x + c)^(3/2)*d)

mupad [B] time = 0.03, size = 12, normalized size = 0.75

$$-\frac{2}{3d(c+dx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(c + d*x)^(5/2),x)

[Out] $-2/(3*d*(c + d*x)^{(3/2)})$

sympy [A] time = 0.07, size = 14, normalized size = 0.88

$$-\frac{2}{3d(c + dx)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(d*x+c)**(5/2),x)`

[Out] $-2/(3*d*(c + d*x)**(3/2))$

$$3.1440 \quad \int \frac{1}{(a+bx)(c+dx)^{5/2}} dx$$

Optimal. Leaf size=93

$$-\frac{2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{5/2}} + \frac{2b}{\sqrt{c+dx}(bc-ad)^2} + \frac{2}{3(c+dx)^{3/2}(bc-ad)}$$

[Out] $2/3/(-a*d+b*c)/(d*x+c)^{(3/2)}-2*b^{(3/2)}*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/(-a*d+b*c)^{(5/2)}+2*b/(-a*d+b*c)^2/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$-\frac{2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{5/2}} + \frac{2b}{\sqrt{c+dx}(bc-ad)^2} + \frac{2}{3(c+dx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)*(c + d*x)^(5/2)),x]

[Out] $2/(3*(b*c - a*d)*(c + d*x)^{(3/2)}) + (2*b)/((b*c - a*d)^2*\operatorname{Sqrt}[c + d*x]) - (2*b^{(3/2)}*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/(\operatorname{Sqrt}[b*c - a*d])])/(b*c - a*d)^{(5/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)(c+dx)^{5/2}} dx &= \frac{2}{3(bc-ad)(c+dx)^{3/2}} + \frac{b \int \frac{1}{(a+bx)(c+dx)^{3/2}} dx}{bc-ad} \\
 &= \frac{2}{3(bc-ad)(c+dx)^{3/2}} + \frac{2b}{(bc-ad)^2 \sqrt{c+dx}} + \frac{b^2 \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{(bc-ad)^2} \\
 &= \frac{2}{3(bc-ad)(c+dx)^{3/2}} + \frac{2b}{(bc-ad)^2 \sqrt{c+dx}} + \frac{(2b^2) \text{Subst}\left(\int \frac{1}{a-\frac{bc}{d}+\frac{bx^2}{d}} dx, x, \sqrt{c+dx}\right)}{d(bc-ad)^2} \\
 &= \frac{2}{3(bc-ad)(c+dx)^{3/2}} + \frac{2b}{(bc-ad)^2 \sqrt{c+dx}} - \frac{2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 48, normalized size = 0.52

$$\frac{{}_2F_1\left(-\frac{3}{2}, 1; -\frac{1}{2}; \frac{b(c+dx)}{bc-ad}\right)}{3(c+dx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*(c + d*x)^(5/2)),x]

[Out] (2*Hypergeometric2F1[-3/2, 1, -1/2, (b*(c + d*x))/(b*c - a*d)]/(3*(b*c - a*d)*(c + d*x)^(3/2))

fricas [B] time = 0.48, size = 398, normalized size = 4.28

$$\left[\frac{3(bd^2x^2 + 2bcdx + bc^2)\sqrt{\frac{b}{bc-ad}} \log\left(\frac{bdx+2bc-ad-2(bc-ad)\sqrt{dx+c}\sqrt{\frac{b}{bc-ad}}}{bx+a}\right) + 2(3bdx + 4bc - ad)\sqrt{dx+c}}{3(b^2c^4 - 2abc^3d + a^2c^2d^2 + (b^2c^2d^2 - 2abcd^3 + a^2d^4)x^2 + 2(b^2c^3d - 2abc^2d^2 + a^2cd^3)x)}, -\frac{2(3(bd^2x^2 + 2bcdx + bc^2)\sqrt{\frac{b}{bc-ad}} \log\left(\frac{bdx+2bc-ad-2(bc-ad)\sqrt{dx+c}\sqrt{\frac{b}{bc-ad}}}{bx+a}\right) + 2(3bdx + 4bc - ad)\sqrt{dx+c}}{3(b^2c^4 - 2abc^3d + a^2c^2d^2 + (b^2c^2d^2 - 2abcd^3 + a^2d^4)x^2 + 2(b^2c^3d - 2abc^2d^2 + a^2cd^3)x)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(5/2),x, algorithm="fricas")

```
[Out] [1/3*(3*(b*d^2*x^2 + 2*b*c*d*x + b*c^2)*sqrt(b/(b*c - a*d))*log((b*d*x + 2*
b*c - a*d - 2*(b*c - a*d)*sqrt(d*x + c)*sqrt(b/(b*c - a*d)))/(b*x + a)) + 2
*(3*b*d*x + 4*b*c - a*d)*sqrt(d*x + c))/(b^2*c^4 - 2*a*b*c^3*d + a^2*c^2*d^
2 + (b^2*c^2*d^2 - 2*a*b*c*d^3 + a^2*d^4)*x^2 + 2*(b^2*c^3*d - 2*a*b*c^2*d^
2 + a^2*c*d^3)*x), -2/3*(3*(b*d^2*x^2 + 2*b*c*d*x + b*c^2)*sqrt(-b/(b*c - a
*d))*arctan(-(b*c - a*d)*sqrt(d*x + c)*sqrt(-b/(b*c - a*d)))/(b*d*x + b*c))
- (3*b*d*x + 4*b*c - a*d)*sqrt(d*x + c))/(b^2*c^4 - 2*a*b*c^3*d + a^2*c^2*d
^2 + (b^2*c^2*d^2 - 2*a*b*c*d^3 + a^2*d^4)*x^2 + 2*(b^2*c^3*d - 2*a*b*c^2*d
^2 + a^2*c*d^3)*x)]
```

giac [A] time = 1.16, size = 113, normalized size = 1.22

$$\frac{2b^2 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{(b^2c^2 - 2abcd + a^2d^2)\sqrt{-b^2c + abd}} + \frac{2(3(dx+c)b + bc - ad)}{3(b^2c^2 - 2abcd + a^2d^2)(dx+c)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)/(d*x+c)^(5/2),x, algorithm="giac")
```

```
[Out] 2*b^2*arctan(sqrt(d*x + c)*b/sqrt(-b^2*c + a*b*d))/((b^2*c^2 - 2*a*b*c*d +
a^2*d^2)*sqrt(-b^2*c + a*b*d)) + 2/3*(3*(d*x + c)*b + b*c - a*d)/((b^2*c^2
- 2*a*b*c*d + a^2*d^2)*(d*x + c)^(3/2))
```

maple [A] time = 0.01, size = 90, normalized size = 0.97

$$\frac{2b^2 \arctan\left(\frac{\sqrt{dx+c} b}{\sqrt{(ad-bc)b}}\right)}{(ad-bc)^2 \sqrt{(ad-bc)b}} + \frac{2b}{(ad-bc)^2 \sqrt{dx+c}} - \frac{2}{3(ad-bc)(dx+c)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(b*x+a)/(d*x+c)^(5/2),x)
```

```
[Out] -2/3/(a*d-b*c)/(d*x+c)^(3/2)+2*b/(a*d-b*c)^2/(d*x+c)^(1/2)+2*b^2/(a*d-b*c)^
2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)/(d*x+c)^(5/2),x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError >> Computation failed since Maxima requested a
dditional constraints; using the 'assume' command before evaluation *may* h
```

elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c positive or negative?

mupad [B] time = 0.33, size = 100, normalized size = 1.08

$$\frac{2b^{3/2} \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{c+dx}(a^2d^2-2abcd+b^2c^2)}{(ad-bc)^{5/2}}\right)}{(ad-bc)^{5/2}} - \frac{\frac{2}{3(ad-bc)} - \frac{2b(c+dx)}{(ad-bc)^2}}{(c+dx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)*(c + d*x)^(5/2)),x)

[Out] (2*b^(3/2)*atan((b^(1/2)*(c + d*x)^(1/2)*(a^2*d^2 + b^2*c^2 - 2*a*b*c*d))/(a*d - b*c)^(5/2)))/(a*d - b*c)^(5/2) - (2/(3*(a*d - b*c)) - (2*b*(c + d*x))/(a*d - b*c)^2)/(c + d*x)^(3/2)

sympy [A] time = 13.58, size = 83, normalized size = 0.89

$$\frac{2b}{\sqrt{c+dx}(ad-bc)^2} + \frac{2b \operatorname{atan}\left(\frac{\sqrt{c+dx}}{\sqrt{\frac{ad-bc}{b}}}\right)}{\sqrt{\frac{ad-bc}{b}}(ad-bc)^2} - \frac{2}{3(c+dx)^{3/2}(ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)**(5/2),x)

[Out] 2*b/(sqrt(c + d*x)*(a*d - b*c)**2) + 2*b*atan(sqrt(c + d*x)/sqrt((a*d - b*c)/b))/(sqrt((a*d - b*c)/b)*(a*d - b*c)**2) - 2/(3*(c + d*x)**(3/2)*(a*d - b*c))

$$3.1441 \quad \int \frac{1}{(a+bx)^2(c+dx)^{5/2}} dx$$

Optimal. Leaf size=124

$$\frac{5b^{3/2}d \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{7/2}} - \frac{5bd}{\sqrt{c+dx}(bc-ad)^3} - \frac{1}{(a+bx)(c+dx)^{3/2}(bc-ad)} - \frac{5d}{3(c+dx)^{3/2}(bc-ad)^2}$$

[Out] $-5/3*d/(-a*d+b*c)^2/(d*x+c)^{(3/2)}-1/(-a*d+b*c)/(b*x+a)/(d*x+c)^{(3/2)}+5*b^{(3/2)}*d*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/(-a*d+b*c)^{(7/2)}-5*b*d/(-a*d+b*c)^3/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 124, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$\frac{5b^{3/2}d \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{(bc-ad)^{7/2}} - \frac{5bd}{\sqrt{c+dx}(bc-ad)^3} - \frac{1}{(a+bx)(c+dx)^{3/2}(bc-ad)} - \frac{5d}{3(c+dx)^{3/2}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^2*(c + d*x)^(5/2)), x]

[Out] $(-5*d)/(3*(b*c - a*d)^2*(c + d*x)^{(3/2)}) - 1/((b*c - a*d)*(a + b*x)*(c + d*x)^{(3/2)}) - (5*b*d)/((b*c - a*d)^3*\operatorname{Sqrt}[c + d*x]) + (5*b^{(3/2)}*d*\operatorname{ArcTanh}[\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/ \operatorname{Sqrt}[b*c - a*d])]/(b*c - a*d)^{(7/2)}$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^2(c+dx)^{5/2}} dx &= -\frac{1}{(bc-ad)(a+bx)(c+dx)^{3/2}} - \frac{(5d) \int \frac{1}{(a+bx)(c+dx)^{5/2}} dx}{2(bc-ad)} \\
 &= -\frac{5d}{3(bc-ad)^2(c+dx)^{3/2}} - \frac{1}{(bc-ad)(a+bx)(c+dx)^{3/2}} - \frac{(5bd) \int \frac{1}{(a+bx)(c+dx)^{3/2}} dx}{2(bc-ad)^2} \\
 &= -\frac{5d}{3(bc-ad)^2(c+dx)^{3/2}} - \frac{1}{(bc-ad)(a+bx)(c+dx)^{3/2}} - \frac{5bd}{(bc-ad)^3\sqrt{c+dx}} - \frac{(5b^2d) \int \frac{1}{(a+bx)\sqrt{c+dx}} dx}{(bc-ad)^2} \\
 &= -\frac{5d}{3(bc-ad)^2(c+dx)^{3/2}} - \frac{1}{(bc-ad)(a+bx)(c+dx)^{3/2}} - \frac{5bd}{(bc-ad)^3\sqrt{c+dx}} - \frac{(5b^2) \int \frac{1}{a+bx} dx}{(bc-ad)^2} \\
 &= -\frac{5d}{3(bc-ad)^2(c+dx)^{3/2}} - \frac{1}{(bc-ad)(a+bx)(c+dx)^{3/2}} - \frac{5bd}{(bc-ad)^3\sqrt{c+dx}} + \frac{5b^3/2 \log\left(\frac{a+bx}{\sqrt{c+dx}}\right)}{(bc-ad)^2}
 \end{aligned}$$

Mathematica [C] time = 0.01, size = 50, normalized size = 0.40

$$-\frac{2d {}_2F_1\left(-\frac{3}{2}, 2; -\frac{1}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{3(c+dx)^{3/2}(ad-bc)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^2*(c + d*x)^(5/2)), x]

[Out] (-2*d*Hypergeometric2F1[-3/2, 2, -1/2, -(b*(c + d*x))/(-(b*c) + a*d)])/(3*(-(b*c) + a*d)^2*(c + d*x)^(3/2))

fricas [B] time = 0.48, size = 782, normalized size = 6.31

$$\left[\frac{15(b^2d^3x^3 + abc^2d + (2b^2cd^2 + abd^3)x^2 + (b^2c^2d + 2abcd^2)x)\sqrt{\frac{b}{bc-ad}} \log\left(\frac{bdx+2bc-ad-2(bc-ad)\sqrt{dx+c}}{bx+a}\sqrt{\frac{b}{bc-ad}}\right)}{6(ab^3c^5 - 3a^2b^2c^4d + 3a^3bc^3d^2 - a^4c^2d^3 + (b^4c^3d^2 - 3ab^3c^2d^3 + 3a^2b^2cd^4 - a^3bd^5)x^3 + (2b^4c^4d - 5ab^3c^3d^2)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^(5/2),x, algorithm="fricas")

[Out]
$$\begin{aligned} & [-1/6*(15*(b^2*d^3*x^3 + a*b*c^2*d + (2*b^2*c*d^2 + a*b*d^3)*x^2 + (b^2*c^2*d + 2*a*b*c*d^2)*x)*\sqrt{b/(b*c - a*d)}*\log((b*d*x + 2*b*c - a*d - 2*(b*c - a*d)*\sqrt{d*x + c})*\sqrt{b/(b*c - a*d)})/(b*x + a) + 2*(15*b^2*d^2*x^2 + 3*b^2*c^2 + 14*a*b*c*d - 2*a^2*d^2 + 10*(2*b^2*c*d + a*b*d^2)*x)*\sqrt{d*x + c}]/(a*b^3*c^5 - 3*a^2*b^2*c^4*d + 3*a^3*b*c^3*d^2 - a^4*c^2*d^3 + (b^4*c^3*d^2 - 3*a*b^3*c^2*d^3 + 3*a^2*b^2*c*d^4 - a^3*b*d^5)*x^3 + (2*b^4*c^4*d - 5*a*b^3*c^3*d^2 + 3*a^2*b^2*c^2*d^3 + a^3*b*c*d^4 - a^4*d^5)*x^2 + (b^4*c^5 - a*b^3*c^4*d - 3*a^2*b^2*c^3*d^2 + 5*a^3*b*c^2*d^3 - 2*a^4*c*d^4)*x), 1/3*(15*(b^2*d^3*x^3 + a*b*c^2*d + (2*b^2*c*d^2 + a*b*d^3)*x^2 + (b^2*c^2*d + 2*a*b*c*d^2)*x)*\sqrt{-b/(b*c - a*d)}*\arctan(-(b*c - a*d)*\sqrt{d*x + c})*\sqrt{-b/(b*c - a*d)}/(b*d*x + b*c)) - (15*b^2*d^2*x^2 + 3*b^2*c^2 + 14*a*b*c*d - 2*a^2*d^2 + 10*(2*b^2*c*d + a*b*d^2)*x)*\sqrt{d*x + c}]/(a*b^3*c^5 - 3*a^2*b^2*c^4*d + 3*a^3*b*c^3*d^2 - a^4*c^2*d^3 + (b^4*c^3*d^2 - 3*a*b^3*c^2*d^3 + 3*a^2*b^2*c*d^4 - a^3*b*d^5)*x^3 + (2*b^4*c^4*d - 5*a*b^3*c^3*d^2 + 3*a^2*b^2*c^2*d^3 + a^3*b*c*d^4 - a^4*d^5)*x^2 + (b^4*c^5 - a*b^3*c^4*d - 3*a^2*b^2*c^3*d^2 + 5*a^3*b*c^2*d^3 - 2*a^4*c*d^4)*x)] \end{aligned}$$

giac [B] time = 1.11, size = 216, normalized size = 1.74

$$\frac{5b^2d \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right) + \sqrt{dx+cb} b^2d}{(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)\sqrt{-b^2c+abd}} - \frac{\sqrt{dx+cb} b^2d}{(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)((dx+c)b - bc + ad)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c)^(5/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & -5*b^2*d*\arctan(\sqrt{d*x + c}*b/\sqrt{-b^2*c + a*b*d})/((b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*\sqrt{-b^2*c + a*b*d}) - \sqrt{d*x + c}*b^2*d/((b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*((d*x + c)*b - b*c + a*d)) - 2/3*(6*(d*x + c)*b*d + b*c*d - a*d^2)/((b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*(d*x + c)^(3/2)) \end{aligned}$$

maple [A] time = 0.02, size = 125, normalized size = 1.01

$$\frac{5b^2d \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{(ad-bc)b}}\right)}{(ad-bc)^3 \sqrt{(ad-bc)b}} + \frac{\sqrt{dx+cb} b^2d}{(ad-bc)^3 (bdx+ad)} + \frac{4bd}{(ad-bc)^3 \sqrt{dx+cb}} - \frac{2d}{3(ad-bc)^2 (dx+c)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/(d*x+c)^(5/2),x)

[Out] $-2/3*d/(a*d-b*c)^2/(d*x+c)^{(3/2)}+4*d/(a*d-b*c)^3*b/(d*x+c)^{(1/2)}+d*b^2/(a*d-b*c)^3*(d*x+c)^{(1/2)}/(b*d*x+a*d)+5*d*b^2/(a*d-b*c)^3/((a*d-b*c)*b)^{(1/2)}*a$
 $\text{rctan}((d*x+c)^{(1/2)}/((a*d-b*c)*b)^{(1/2)}*b)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^2/(d*x+c)^(5/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.38, size = 161, normalized size = 1.30

$$\frac{\frac{10bd(c+dx)}{3(ad-bc)^2} - \frac{2d}{3(ad-bc)} + \frac{5b^2d(c+dx)^2}{(ad-bc)^3}}{b(c+dx)^{5/2} + (ad-bc)(c+dx)^{3/2}} + \frac{5b^{3/2}d \operatorname{atan}\left(\frac{\sqrt{b}\sqrt{c+dx}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}{(ad-bc)^{7/2}}\right)}{(ad-bc)^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^2*(c + d*x)^(5/2)),x)`

[Out] $((10*b*d*(c + d*x))/(3*(a*d - b*c)^2) - (2*d)/(3*(a*d - b*c)) + (5*b^2*d*(c + d*x)^2)/(a*d - b*c)^3)/(b*(c + d*x)^{(5/2)} + (a*d - b*c)*(c + d*x)^{(3/2)})$
 $+ (5*b^{(3/2)}*d*\operatorname{atan}((b^{(1/2)}*(c + d*x)^{(1/2)}*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2))/(a*d - b*c)^{(7/2)}))/((a*d - b*c)^{(7/2)})$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^2 (c + dx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**2/(d*x+c)**(5/2),x)`

[Out] `Integral(1/((a + b*x)**2*(c + d*x)**(5/2)), x)`

$$3.1442 \quad \int \frac{1}{(a+bx)^3(c+dx)^{5/2}} dx$$

Optimal. Leaf size=167

$$-\frac{35b^{3/2}d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4(bc-ad)^{9/2}} + \frac{35bd^2}{4\sqrt{c+dx}(bc-ad)^4} + \frac{35d^2}{12(c+dx)^{3/2}(bc-ad)^3} + \frac{7d}{4(a+bx)(c+dx)^{3/2}(bc-ad)^2} - \frac{1}{2(c+dx)^{3/2}(bc-ad)}$$

[Out] 35/12*d^2/(-a*d+b*c)^3/(d*x+c)^(3/2)-1/2/(-a*d+b*c)/(b*x+a)^2/(d*x+c)^(3/2)+7/4*d/(-a*d+b*c)^2/(b*x+a)/(d*x+c)^(3/2)-35/4*b^(3/2)*d^2*arctanh(b^(1/2)*(d*x+c)^(1/2)/(-a*d+b*c)^(1/2))/(-a*d+b*c)^(9/2)+35/4*b*d^2/(-a*d+b*c)^4/(d*x+c)^(1/2)

Rubi [A] time = 0.06, antiderivative size = 167, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$-\frac{35b^{3/2}d^2 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{4(bc-ad)^{9/2}} + \frac{35bd^2}{4\sqrt{c+dx}(bc-ad)^4} + \frac{35d^2}{12(c+dx)^{3/2}(bc-ad)^3} + \frac{7d}{4(a+bx)(c+dx)^{3/2}(bc-ad)^2} - \frac{1}{2(c+dx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^3*(c + d*x)^(5/2)),x]

[Out] (35*d^2)/(12*(b*c - a*d)^3*(c + d*x)^(3/2)) - 1/(2*(b*c - a*d)*(a + b*x)^2*(c + d*x)^(3/2)) + (7*d)/(4*(b*c - a*d)^2*(a + b*x)*(c + d*x)^(3/2)) + (35*b*d^2)/(4*(b*c - a*d)^4*Sqrt[c + d*x]) - (35*b^(3/2)*d^2*ArcTanh[(Sqrt[b]*Sqrt[c + d*x])/Sqrt[b*c - a*d]])/(4*(b*c - a*d)^(9/2))

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^3(c+dx)^{5/2}} dx &= -\frac{1}{2(bc-ad)(a+bx)^2(c+dx)^{3/2}} - \frac{(7d) \int \frac{1}{(a+bx)^2(c+dx)^{5/2}} dx}{4(bc-ad)} \\
 &= -\frac{1}{2(bc-ad)(a+bx)^2(c+dx)^{3/2}} + \frac{7d}{4(bc-ad)^2(a+bx)(c+dx)^{3/2}} + \frac{(35d^2) \int \frac{1}{(a+bx)(c+dx)^{5/2}} dx}{8(bc-ad)^2} \\
 &= \frac{35d^2}{12(bc-ad)^3(c+dx)^{3/2}} - \frac{1}{2(bc-ad)(a+bx)^2(c+dx)^{3/2}} + \frac{7d}{4(bc-ad)^2(a+bx)(c+dx)^{3/2}} \\
 &= \frac{35d^2}{12(bc-ad)^3(c+dx)^{3/2}} - \frac{1}{2(bc-ad)(a+bx)^2(c+dx)^{3/2}} + \frac{7d}{4(bc-ad)^2(a+bx)(c+dx)^{3/2}} \\
 &= \frac{35d^2}{12(bc-ad)^3(c+dx)^{3/2}} - \frac{1}{2(bc-ad)(a+bx)^2(c+dx)^{3/2}} + \frac{7d}{4(bc-ad)^2(a+bx)(c+dx)^{3/2}} \\
 &= \frac{35d^2}{12(bc-ad)^3(c+dx)^{3/2}} - \frac{1}{2(bc-ad)(a+bx)^2(c+dx)^{3/2}} + \frac{7d}{4(bc-ad)^2(a+bx)(c+dx)^{3/2}} \\
 &= \frac{35d^2}{12(bc-ad)^3(c+dx)^{3/2}} - \frac{1}{2(bc-ad)(a+bx)^2(c+dx)^{3/2}} + \frac{7d}{4(bc-ad)^2(a+bx)(c+dx)^{3/2}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.31

$$-\frac{2d^2 {}_2F_1\left(-\frac{3}{2}, 3; -\frac{1}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{3(c+dx)^{3/2}(ad-bc)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^3*(c + d*x)^(5/2)),x]

[Out] (-2*d^2*Hypergeometric2F1[-3/2, 3, -1/2, -(b*(c + d*x))/(-(b*c) + a*d)])/(3*(-(b*c) + a*d)^3*(c + d*x)^(3/2))

)) + 2/3*(9*(d*x + c)*b*d^2 + b*c*d^2 - a*d^3)/((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*(d*x + c)^(3/2)) + 1/4*(11*(d*x + c)^(3/2)*b^3*d^2 - 13*sqrt(d*x + c)*b^3*c*d^2 + 13*sqrt(d*x + c)*a*b^2*d^3)/((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*((d*x + c)*b - b*c + a*d)^2)

maple [A] time = 0.02, size = 206, normalized size = 1.23

$$\frac{13\sqrt{dx+c} a b^2 d^3}{4(ad-bc)^4 (bdx+ad)^2} - \frac{13\sqrt{dx+c} b^3 c d^2}{4(ad-bc)^4 (bdx+ad)^2} + \frac{11(dx+c)^{\frac{3}{2}} b^3 d^2}{4(ad-bc)^4 (bdx+ad)^2} + \frac{35b^2 d^2 \arctan\left(\frac{\sqrt{dx+c} b}{\sqrt{(ad-bc)b}}\right)}{4(ad-bc)^4 \sqrt{(ad-bc)b}} + \frac{6}{(ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^3/(d*x+c)^(5/2),x)

[Out] -2/3*d^2/(a*d-b*c)^3/(d*x+c)^(3/2)+6*d^2/(a*d-b*c)^4*b/(d*x+c)^(1/2)+11/4*d^2/(a*d-b*c)^4*b^3/(b*d*x+a*d)^2*(d*x+c)^(3/2)+13/4*d^3/(a*d-b*c)^4*b^2/(b*d*x+a*d)^2*(d*x+c)^(1/2)*a-13/4*d^2/(a*d-b*c)^4*b^3/(b*d*x+a*d)^2*(d*x+c)^(1/2)*c+35/4*d^2/(a*d-b*c)^4*b^2/((a*d-b*c)*b)^(1/2)*arctan((d*x+c)^(1/2)/((a*d-b*c)*b)^(1/2)*b)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^3/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.28, size = 243, normalized size = 1.46

$$\frac{\frac{175b^2 d^2 (c+dx)^2}{12(ad-bc)^3} - \frac{2d^2}{3(ad-bc)} + \frac{35b^3 d^2 (c+dx)^3}{4(ad-bc)^4} + \frac{14bd^2 (c+dx)}{3(ad-bc)^2}}{b^2 (c+dx)^{7/2} - (2b^2 c - 2abd) (c+dx)^{5/2} + (c+dx)^{3/2} (a^2 d^2 - 2abcd + b^2 c^2)} + \frac{35b^{3/2} d^2 \operatorname{atan}\left(\frac{\sqrt{b} \sqrt{c+dx}}{a}\right)}{4(ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^3*(c + d*x)^(5/2)),x)

[Out] ((175*b^2*d^2*(c + d*x)^2)/(12*(a*d - b*c)^3) - (2*d^2)/(3*(a*d - b*c))) + (35*b^3*d^2*(c + d*x)^3)/(4*(a*d - b*c)^4) + (14*b*d^2*(c + d*x))/(3*(a*d -

$$\frac{b^2 c^2}{(b^2 (c + dx)^{7/2} - (2b^2 c - 2abd)(c + dx)^{5/2} + (c + dx)^{3/2}(a^2 d^2 + b^2 c^2 - 2abcd))} + \frac{(35b^{3/2} d^2 \operatorname{atan}(b^{1/2} (c + dx)^{1/2} (a^4 d^4 + b^4 c^4 + 6a^2 b^2 c^2 d^2 - 4ab^3 c^3 d - 4a^3 b c d^3)) / (ad - bc))^{9/2}}{4(ad - bc)^{9/2}}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**3/(d*x+c)**(5/2),x)

[Out] Timed out

$$3.1443 \quad \int \frac{1}{(a+bx)^4(c+dx)^{5/2}} dx$$

Optimal. Leaf size=200

$$\frac{105b^{3/2}d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8(bc-ad)^{11/2}} - \frac{105bd^3}{8\sqrt{c+dx}(bc-ad)^5} - \frac{35d^3}{8(c+dx)^{3/2}(bc-ad)^4} - \frac{21d^2}{8(a+bx)(c+dx)^{3/2}(bc-ad)^3} + \frac{1}{4(a+bx)^4(c+dx)^{5/2}}$$

[Out] $-35/8*d^3/(-a*d+b*c)^4/(d*x+c)^{(3/2)}-1/3/(-a*d+b*c)/(b*x+a)^3/(d*x+c)^{(3/2)}+3/4*d/(-a*d+b*c)^2/(b*x+a)^2/(d*x+c)^{(3/2)}-21/8*d^2/(-a*d+b*c)^3/(b*x+a)/(d*x+c)^{(3/2)}+105/8*b^{(3/2)}*d^3*\operatorname{arctanh}(b^{(1/2)}*(d*x+c)^{(1/2)/(-a*d+b*c)^{(1/2)})/(-a*d+b*c)^{(11/2)}-105/8*b*d^3/(-a*d+b*c)^5/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.13, antiderivative size = 200, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {51, 63, 208}

$$\frac{105b^{3/2}d^3 \tanh^{-1}\left(\frac{\sqrt{b}\sqrt{c+dx}}{\sqrt{bc-ad}}\right)}{8(bc-ad)^{11/2}} - \frac{105bd^3}{8\sqrt{c+dx}(bc-ad)^5} - \frac{35d^3}{8(c+dx)^{3/2}(bc-ad)^4} - \frac{21d^2}{8(a+bx)(c+dx)^{3/2}(bc-ad)^3} + \frac{1}{4(a+bx)^4(c+dx)^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^4*(c + d*x)^(5/2)), x]

[Out] $(-35*d^3)/(8*(b*c - a*d)^4*(c + d*x)^{(3/2)}) - 1/(3*(b*c - a*d)*(a + b*x)^3*(c + d*x)^{(3/2)}) + (3*d)/(4*(b*c - a*d)^2*(a + b*x)^2*(c + d*x)^{(3/2)}) - (21*d^2)/(8*(b*c - a*d)^3*(a + b*x)*(c + d*x)^{(3/2)}) - (105*b*d^3)/(8*(b*c - a*d)^5*\operatorname{Sqrt}[c + d*x]) + (105*b^{(3/2)}*d^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])/(\operatorname{Sqrt}[b*c - a*d])])/(8*(b*c - a*d)^{(11/2)})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ

[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] :> Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^4(c+dx)^{5/2}} dx &= -\frac{1}{3(bc-ad)(a+bx)^3(c+dx)^{3/2}} - \frac{(3d) \int \frac{1}{(a+bx)^3(c+dx)^{5/2}} dx}{2(bc-ad)} \\
 &= -\frac{1}{3(bc-ad)(a+bx)^3(c+dx)^{3/2}} + \frac{3d}{4(bc-ad)^2(a+bx)^2(c+dx)^{3/2}} + \frac{(21d^2) \int \frac{1}{(a+bx)^2(c+dx)^{5/2}} dx}{8(bc-ad)^2} \\
 &= -\frac{1}{3(bc-ad)(a+bx)^3(c+dx)^{3/2}} + \frac{3d}{4(bc-ad)^2(a+bx)^2(c+dx)^{3/2}} - \frac{21d^2}{8(bc-ad)^3(a+bx)(c+dx)^{3/2}} \\
 &= -\frac{35d^3}{8(bc-ad)^4(c+dx)^{3/2}} - \frac{1}{3(bc-ad)(a+bx)^3(c+dx)^{3/2}} + \frac{3d}{4(bc-ad)^2(a+bx)^2(c+dx)^{3/2}} \\
 &= -\frac{35d^3}{8(bc-ad)^4(c+dx)^{3/2}} - \frac{1}{3(bc-ad)(a+bx)^3(c+dx)^{3/2}} + \frac{3d}{4(bc-ad)^2(a+bx)^2(c+dx)^{3/2}} \\
 &= -\frac{35d^3}{8(bc-ad)^4(c+dx)^{3/2}} - \frac{1}{3(bc-ad)(a+bx)^3(c+dx)^{3/2}} + \frac{3d}{4(bc-ad)^2(a+bx)^2(c+dx)^{3/2}} \\
 &= -\frac{35d^3}{8(bc-ad)^4(c+dx)^{3/2}} - \frac{1}{3(bc-ad)(a+bx)^3(c+dx)^{3/2}} + \frac{3d}{4(bc-ad)^2(a+bx)^2(c+dx)^{3/2}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 52, normalized size = 0.26

$$-\frac{2d^3 {}_2F_1\left(-\frac{3}{2}, 4; -\frac{1}{2}; -\frac{b(c+dx)}{ad-bc}\right)}{3(c+dx)^{3/2}(ad-bc)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^4*(c + d*x)^(5/2)), x]

[Out] $(-2*d^3*Hypergeometric2F1[-3/2, 4, -1/2, -((b*(c + d*x))/(-(b*c) + a*d))]) / (3*(-(b*c) + a*d)^4*(c + d*x)^{(3/2)})$

fricas [B] time = 0.52, size = 1840, normalized size = 9.20

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^4/(d*x+c)^(5/2),x, algorithm="fricas")`

[Out]
$$\begin{aligned} & [-1/48*(315*(b^4*d^5*x^5 + a^3*b*c^2*d^3 + (2*b^4*c*d^4 + 3*a*b^3*d^5)*x^4 \\ & + (b^4*c^2*d^3 + 6*a*b^3*c*d^4 + 3*a^2*b^2*d^5)*x^3 + (3*a*b^3*c^2*d^3 + 6* \\ & a^2*b^2*c*d^4 + a^3*b*d^5)*x^2 + (3*a^2*b^2*c^2*d^3 + 2*a^3*b*c*d^4)*x)*\text{sqrt} \\ & \text{t}(b/(b*c - a*d))*\log((b*d*x + 2*b*c - a*d - 2*(b*c - a*d)*\text{sqrt}(d*x + c))*\text{sqrt} \\ & \text{t}(b/(b*c - a*d)))/(b*x + a)) + 2*(315*b^4*d^4*x^4 + 8*b^4*c^4 - 50*a*b^3*c^ \\ & 3*d + 165*a^2*b^2*c^2*d^2 + 208*a^3*b*c*d^3 - 16*a^4*d^4 + 420*(b^4*c*d^3 + \\ & 2*a*b^3*d^4)*x^3 + 63*(b^4*c^2*d^2 + 18*a*b^3*c*d^3 + 11*a^2*b^2*d^4)*x^2 \\ & - 18*(b^4*c^3*d - 10*a*b^3*c^2*d^2 - 53*a^2*b^2*c*d^3 - 8*a^3*b*d^4)*x)*\text{sqrt} \\ & \text{t}(d*x + c))/(a^3*b^5*c^7 - 5*a^4*b^4*c^6*d + 10*a^5*b^3*c^5*d^2 - 10*a^6*b^ \\ & 2*c^4*d^3 + 5*a^7*b*c^3*d^4 - a^8*c^2*d^5 + (b^8*c^5*d^2 - 5*a*b^7*c^4*d^3 \\ & + 10*a^2*b^6*c^3*d^4 - 10*a^3*b^5*c^2*d^5 + 5*a^4*b^4*c*d^6 - a^5*b^3*d^7)* \\ & x^5 + (2*b^8*c^6*d - 7*a*b^7*c^5*d^2 + 5*a^2*b^6*c^4*d^3 + 10*a^3*b^5*c^3*d \\ & ^4 - 20*a^4*b^4*c^2*d^5 + 13*a^5*b^3*c*d^6 - 3*a^6*b^2*d^7)*x^4 + (b^8*c^7 \\ & + a*b^7*c^6*d - 17*a^2*b^6*c^5*d^2 + 35*a^3*b^5*c^4*d^3 - 25*a^4*b^4*c^3*d^ \\ & 4 - a^5*b^3*c^2*d^5 + 9*a^6*b^2*c*d^6 - 3*a^7*b*d^7)*x^3 + (3*a*b^7*c^7 - 9 \\ & *a^2*b^6*c^6*d + a^3*b^5*c^5*d^2 + 25*a^4*b^4*c^4*d^3 - 35*a^5*b^3*c^3*d^4 \\ & + 17*a^6*b^2*c^2*d^5 - a^7*b*c*d^6 - a^8*d^7)*x^2 + (3*a^2*b^6*c^7 - 13*a^3 \\ & *b^5*c^6*d + 20*a^4*b^4*c^5*d^2 - 10*a^5*b^3*c^4*d^3 - 5*a^6*b^2*c^3*d^4 + \\ & 7*a^7*b*c^2*d^5 - 2*a^8*c*d^6)*x), 1/24*(315*(b^4*d^5*x^5 + a^3*b*c^2*d^3 + \\ & (2*b^4*c*d^4 + 3*a*b^3*d^5)*x^4 + (b^4*c^2*d^3 + 6*a*b^3*c*d^4 + 3*a^2*b^2 \\ & *d^5)*x^3 + (3*a*b^3*c^2*d^3 + 6*a^2*b^2*c*d^4 + a^3*b*d^5)*x^2 + (3*a^2*b^ \\ & 2*c^2*d^3 + 2*a^3*b*c*d^4)*x)*\text{sqrt}(-b/(b*c - a*d))*\arctan(-(b*c - a*d)*\text{sqrt} \\ & (d*x + c))*\text{sqrt}(-b/(b*c - a*d))/(b*d*x + b*c)) - (315*b^4*d^4*x^4 + 8*b^4*c^ \\ & 4 - 50*a*b^3*c^3*d + 165*a^2*b^2*c^2*d^2 + 208*a^3*b*c*d^3 - 16*a^4*d^4 + 4 \\ & 20*(b^4*c*d^3 + 2*a*b^3*d^4)*x^3 + 63*(b^4*c^2*d^2 + 18*a*b^3*c*d^3 + 11*a^ \\ & 2*b^2*d^4)*x^2 - 18*(b^4*c^3*d - 10*a*b^3*c^2*d^2 - 53*a^2*b^2*c*d^3 - 8*a^ \\ & 3*b*d^4)*x)*\text{sqrt}(d*x + c))/(a^3*b^5*c^7 - 5*a^4*b^4*c^6*d + 10*a^5*b^3*c^5* \\ & d^2 - 10*a^6*b^2*c^4*d^3 + 5*a^7*b*c^3*d^4 - a^8*c^2*d^5 + (b^8*c^5*d^2 - 5 \\ & *a*b^7*c^4*d^3 + 10*a^2*b^6*c^3*d^4 - 10*a^3*b^5*c^2*d^5 + 5*a^4*b^4*c*d^6 \\ & - a^5*b^3*d^7)*x^5 + (2*b^8*c^6*d - 7*a*b^7*c^5*d^2 + 5*a^2*b^6*c^4*d^3 + 1 \\ & 0*a^3*b^5*c^3*d^4 - 20*a^4*b^4*c^2*d^5 + 13*a^5*b^3*c*d^6 - 3*a^6*b^2*d^7)* \\ & x^4 + (b^8*c^7 + a*b^7*c^6*d - 17*a^2*b^6*c^5*d^2 + 35*a^3*b^5*c^4*d^3 - 25 \\ & *a^4*b^4*c^3*d^4 - a^5*b^3*c^2*d^5 + 9*a^6*b^2*c*d^6 - 3*a^7*b*d^7)*x^3 + (\\ & 3*a*b^7*c^7 - 9*a^2*b^6*c^6*d + a^3*b^5*c^5*d^2 + 25*a^4*b^4*c^4*d^3 - 35*a \\ & ^5*b^3*c^3*d^4 + 17*a^6*b^2*c^2*d^5 - a^7*b*c*d^6 - a^8*d^7)*x^2 + (3*a^2*b \end{aligned}$$

$^6*c^7 - 13*a^3*b^5*c^6*d + 20*a^4*b^4*c^5*d^2 - 10*a^5*b^3*c^4*d^3 - 5*a^6*b^2*c^3*d^4 + 7*a^7*b*c^2*d^5 - 2*a^8*c*d^6)*x]$

giac [B] time = 1.20, size = 432, normalized size = 2.16

$$\frac{105 b^2 d^3 \arctan\left(\frac{\sqrt{dx+cb}}{\sqrt{-b^2c+abd}}\right)}{8(b^5 c^5 - 5 ab^4 c^4 d + 10 a^2 b^3 c^3 d^2 - 10 a^3 b^2 c^2 d^3 + 5 a^4 b c d^4 - a^5 d^5) \sqrt{-b^2 c + abd}} - \frac{315 (dx + c)^4 b^4 d^3 - 840 (dx + c)^3 b^4 c d^3 + 693 (dx + c)^2 b^4 c^2 d^3 - 144 (dx + c) b^4 c^3 d^3 - 16 b^4 c^4 d^3 + 840 (dx + c)^3 a b^3 c d^4 - 1386 (dx + c)^2 a b^3 c^2 d^4 + 432 (dx + c) a b^3 c^2 d^4 + 64 a^2 b^3 c^2 d^4 + 693 (dx + c)^2 a^2 b^2 c^2 d^5 - 432 (dx + c) a^2 b^2 c^2 d^5 - 96 a^2 b^2 c^2 d^5 + 144 (dx + c) a^3 b^2 c^2 d^6 + 64 a^3 b^2 c^2 d^6 - 16 a^4 d^7}{(b^5 c^5 - 5 a b^4 c^4 d + 10 a^2 b^3 c^3 d^2 - 10 a^3 b^2 c^2 d^3 + 5 a^4 b c d^4 - a^5 d^5) ((dx + c)^{3/2} b - \sqrt{dx + c} b c + \sqrt{dx + c} a d)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^4/(d*x+c)^(5/2),x, algorithm="giac")

[Out] $-105/8*b^2*d^3*\arctan(\sqrt{d*x+c}*b/\sqrt{-b^2*c+a*b*d})/((b^5*c^5-5*a*b^4*c^4*d+10*a^2*b^3*c^3*d^2-10*a^3*b^2*c^2*d^3+5*a^4*b*c*d^4-a^5*d^5)*\sqrt{-b^2*c+a*b*d})-1/24*(315*(d*x+c)^4*b^4*d^3-840*(d*x+c)^3*b^4*c*d^3+693*(d*x+c)^2*b^4*c^2*d^3-144*(d*x+c)*b^4*c^3*d^3-16*b^4*c^4*d^3+840*(d*x+c)^3*a*b^3*c*d^4-1386*(d*x+c)^2*a*b^3*c^2*d^4+432*(d*x+c)*a*b^3*c^2*d^4+64*a^2*b^3*c^2*d^4+693*(d*x+c)^2*a^2*b^2*c^2*d^5-432*(d*x+c)*a^2*b^2*c^2*d^5-96*a^2*b^2*c^2*d^5+144*(d*x+c)*a^3*b^2*c^2*d^6+64*a^3*b^2*c^2*d^6-16*a^4*d^7)/((b^5*c^5-5*a*b^4*c^4*d+10*a^2*b^3*c^3*d^2-10*a^3*b^2*c^2*d^3+5*a^4*b*c*d^4-a^5*d^5)*((d*x+c)^{3/2}*b-\sqrt{d*x+c}*b*c+\sqrt{d*x+c}*a*d)^3)$

maple [A] time = 0.02, size = 319, normalized size = 1.60

$$\frac{55\sqrt{dx+c} a^2 b^2 d^5}{8(ad-bc)^5 (bdx+ad)^3} - \frac{55\sqrt{dx+c} a b^3 c d^4}{4(ad-bc)^5 (bdx+ad)^3} + \frac{55\sqrt{dx+c} b^4 c^2 d^3}{8(ad-bc)^5 (bdx+ad)^3} + \frac{35(dx+c)^3 a b^3 d^4}{3(ad-bc)^5 (bdx+ad)^3} - \frac{35(dx+c)^2 a^2 b^3 d^4}{3(ad-bc)^5 (bdx+ad)^3} + \frac{35(dx+c) a^3 b^3 d^4}{3(ad-bc)^5 (bdx+ad)^3} - \frac{35 a^4 b^3 d^4}{3(ad-bc)^5 (bdx+ad)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^4/(d*x+c)^(5/2),x)

[Out] $-2/3*d^3/(a*d-b*c)^4/(d*x+c)^{3/2}+8*d^3/(a*d-b*c)^5*b/(d*x+c)^{1/2}+41/8*d^3/(a*d-b*c)^5*b^4/(b*d*x+a*d)^3*(d*x+c)^{5/2}+35/3*d^4/(a*d-b*c)^5*b^3/(b*d*x+a*d)^3*(d*x+c)^{3/2}+a-35/3*d^3/(a*d-b*c)^5*b^4/(b*d*x+a*d)^3*(d*x+c)^{3/2}+c+55/8*d^5/(a*d-b*c)^5*b^2/(b*d*x+a*d)^3*(d*x+c)^{1/2}+a^2-55/4*d^4/(a*d-b*c)^5*b^3/(b*d*x+a*d)^3*(d*x+c)^{1/2}+a*c+55/8*d^3/(a*d-b*c)^5*b^4/(b*d*x+a*d)^3*(d*x+c)^{1/2}+c^2+105/8*d^3/(a*d-b*c)^5*b^2/((a*d-b*c)*b)^{1/2}+a*\arctan((d*x+c)^{1/2}/((a*d-b*c)*b)^{1/2}*b)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^4/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c positive or negative?

mupad [B] time = 0.64, size = 334, normalized size = 1.67

$$\frac{\frac{231b^2d^3(c+dx)^2}{8(ad-bc)^3} - \frac{2d^3}{3(ad-bc)} + \frac{35b^3d^3(c+dx)^3}{(ad-bc)^4} + \frac{105b^4d^3(c+dx)^4}{8(ad-bc)^5} + \frac{6bd^3(c+dx)}{(ad-bc)^2}}{(c+dx)^{3/2} (a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3) + b^3(c+dx)^{9/2} - (3b^3c - 3ab^2d)(c+dx)^{7/2} + (c+dx)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^4*(c + d*x)^(5/2)),x)

[Out] ((231*b^2*d^3*(c + d*x)^2)/(8*(a*d - b*c)^3) - (2*d^3)/(3*(a*d - b*c)) + (3*5*b^3*d^3*(c + d*x)^3)/(a*d - b*c)^4 + (105*b^4*d^3*(c + d*x)^4)/(8*(a*d - b*c)^5) + (6*b*d^3*(c + d*x))/(a*d - b*c)^2)/((c + d*x)^(3/2)*(a^3*d^3 - b^3*c^3 + 3*a*b^2*c^2*d - 3*a^2*b*c*d^2) + b^3*(c + d*x)^(9/2) - (3*b^3*c - 3*a*b^2*d)*(c + d*x)^(7/2) + (c + d*x)^(5/2)*(3*b^3*c^2 + 3*a^2*b*d^2 - 6*a*b^2*c*d)) + (105*b^(3/2)*d^3*atan((b^(1/2)*(c + d*x)^(1/2)*(a^5*d^5 - b^5*c^5 - 10*a^2*b^3*c^3*d^2 + 10*a^3*b^2*c^2*d^3 + 5*a*b^4*c^4*d - 5*a^4*b*c*d^4))/(a*d - b*c)^(11/2)))/(8*(a*d - b*c)^(11/2))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**4/(d*x+c)**(5/2),x)

[Out] Timed out

$$3.1444 \quad \int (a + bx)^5 (ac + bcx)^{3/2} dx$$

Optimal. Leaf size=22

$$\frac{2(ac + bcx)^{15/2}}{15bc^6}$$

[Out] $2/15*(b*c*x+a*c)^{(15/2)}/b/c^6$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$\frac{2(ac + bcx)^{15/2}}{15bc^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*(a*c + b*c*x)^(3/2), x]

[Out] (2*(a*c + b*c*x)^(15/2))/(15*b*c^6)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int (a + bx)^5 (ac + bcx)^{3/2} dx &= \frac{\int (ac + bcx)^{13/2} dx}{c^5} \\ &= \frac{2(ac + bcx)^{15/2}}{15bc^6} \end{aligned}$$

Mathematica [A] time = 0.02, size = 25, normalized size = 1.14

$$\frac{2(a + bx)^6 (c(a + bx))^{3/2}}{15b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*(a*c + b*c*x)^(3/2), x]

[Out] (2*(a + b*x)^6*(c*(a + b*x))^(3/2))/(15*b)

fricas [B] time = 0.42, size = 95, normalized size = 4.32

$$\frac{2(b^7cx^7 + 7ab^6cx^6 + 21a^2b^5cx^5 + 35a^3b^4cx^4 + 35a^4b^3cx^3 + 21a^5b^2cx^2 + 7a^6bcx + a^7c)\sqrt{bcx + ac}}{15b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^(3/2), x, algorithm="fricas")

[Out] 2/15*(b^7*c*x^7 + 7*a*b^6*c*x^6 + 21*a^2*b^5*c*x^5 + 35*a^3*b^4*c*x^4 + 35*a^4*b^3*c*x^3 + 21*a^5*b^2*c*x^2 + 7*a^6*b*c*x + a^7*c)*sqrt(b*c*x + a*c)/b

giac [B] time = 1.26, size = 637, normalized size = 28.95

$$2 \left(6435 \sqrt{bcx + ac} a^7 c - 15015 \left(3 \sqrt{bcx + ac} ac - (bcx + ac)^{\frac{3}{2}} \right) a^6 + \frac{9009 \left(15 \sqrt{bcx + ac} a^2 c^2 - 10 (bcx + ac)^{\frac{3}{2}} ac + 3 (bcx + ac)^{\frac{5}{2}} \right) a^5}{c} \right) -$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^(3/2), x, algorithm="giac")

[Out] 2/6435*(6435*sqrt(b*c*x + a*c)*a^7*c - 15015*(3*sqrt(b*c*x + a*c)*a*c - (b*c*x + a*c)^(3/2))*a^6 + 9009*(15*sqrt(b*c*x + a*c)*a^2*c^2 - 10*(b*c*x + a*c)^(3/2)*a*c + 3*(b*c*x + a*c)^(5/2))*a^5/c - 6435*(35*sqrt(b*c*x + a*c)*a^3*c^3 - 35*(b*c*x + a*c)^(3/2)*a^2*c^2 + 21*(b*c*x + a*c)^(5/2)*a*c - 5*(b*c*x + a*c)^(7/2))*a^4/c^2 + 715*(315*sqrt(b*c*x + a*c)*a^4*c^4 - 420*(b*c*x + a*c)^(3/2)*a^3*c^3 + 378*(b*c*x + a*c)^(5/2)*a^2*c^2 - 180*(b*c*x + a*c)^(7/2)*a*c + 35*(b*c*x + a*c)^(9/2))*a^3/c^3 - 195*(693*sqrt(b*c*x + a*c)*a^5*c^5 - 1155*(b*c*x + a*c)^(3/2)*a^4*c^4 + 1386*(b*c*x + a*c)^(5/2)*a^3*c^3 - 990*(b*c*x + a*c)^(7/2)*a^2*c^2 + 385*(b*c*x + a*c)^(9/2)*a*c - 63*(b*c*x + a*c)^(11/2))*a^2/c^4 + 15*(3003*sqrt(b*c*x + a*c)*a^6*c^6 - 6006*(b*c*x + a*c)^(3/2)*a^5*c^5 + 9009*(b*c*x + a*c)^(5/2)*a^4*c^4 - 8580*(b*c*x + a*c)^(7/2)*a^3*c^3 + 5005*(b*c*x + a*c)^(9/2)*a^2*c^2 - 1638*(b*c*x + a*c)^(11/2)*a*c + 231*(b*c*x + a*c)^(13/2))*a/c^5 - (6435*sqrt(b*c*x + a*c)*a^7*c^7 - 15015*(b*c*x + a*c)^(3/2)*a^6*c^6 + 27027*(b*c*x + a*c)^(5/2)*a^5*c^5 - 32175*(b*c*x + a*c)^(7/2)*a^4*c^4 + 25025*(b*c*x + a*c)^(9/2)*a^3*c^3 - 12285*(b*c*x + a*c)^(11/2)*a^2*c^2 + 3465*(b*c*x + a*c)^(13/2)*a*c - 429*(b*c*x + a*c)^(15/2))/c^6)/b

maple [A] time = 0.00, size = 23, normalized size = 1.05

$$\frac{2(bx + a)^6 (bcx + ac)^{\frac{3}{2}}}{15b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^5*(b*c*x+a*c)^(3/2),x)`

[Out] `2/15*(b*x+a)^6*(b*c*x+a*c)^(3/2)/b`

maxima [A] time = 1.37, size = 18, normalized size = 0.82

$$\frac{2(bc x + ac)^{\frac{15}{2}}}{15bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5*(b*c*x+a*c)^(3/2),x, algorithm="maxima")`

[Out] `2/15*(b*c*x + a*c)^(15/2)/(b*c^6)`

mupad [B] time = 0.05, size = 17, normalized size = 0.77

$$\frac{2(c(a + bx))^{15/2}}{15bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c + b*c*x)^(3/2)*(a + b*x)^5,x)`

[Out] `(2*(c*(a + b*x))^(15/2))/(15*b*c^6)`

sympy [A] time = 1.21, size = 66, normalized size = 3.00

$$\begin{cases} \frac{2b^{\frac{13}{2}}c^{\frac{3}{2}}\left(\frac{a}{b}+x\right)^{\frac{15}{2}}}{15} & \text{for } \left|\frac{a}{b}+x\right| < 1 \\ b^{\frac{13}{2}}c^{\frac{3}{2}}G_{2,2}^{1,1}\left(\frac{1}{\frac{15}{2}}, \frac{\frac{17}{2}}{0}\left|\frac{a}{b}+x\right.\right) + b^{\frac{13}{2}}c^{\frac{3}{2}}G_{2,2}^{0,2}\left(\frac{17}{2}, 1\left|\frac{15}{2}, 0\right.\left|\frac{a}{b}+x\right.\right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5*(b*c*x+a*c)**(3/2),x)`

```
[Out] Piecewise((2*b**(13/2)*c**(3/2)*(a/b + x)**(15/2)/15, Abs(a/b + x) < 1), (b  
**(13/2)*c**(3/2)*meijerg(((1,), (17/2,)), ((15/2,), (0,)), a/b + x) + b**(  
13/2)*c**(3/2)*meijerg(((17/2, 1), ()), ((15/2, 0)), a/b + x), True))
```

$$3.1445 \quad \int (a + bx)^5 \sqrt{ac + bcx} \, dx$$

Optimal. Leaf size=22

$$\frac{2(ac + bcx)^{13/2}}{13bc^6}$$

[Out] 2/13*(b*c*x+a*c)^(13/2)/b/c^6

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$\frac{2(ac + bcx)^{13/2}}{13bc^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5*Sqrt[a*c + b*c*x], x]

[Out] (2*(a*c + b*c*x)^(13/2))/(13*b*c^6)

Rule 21

```
Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
  Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
  && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplifierQ[c + d*x,
  a + b*x])
```

Rule 32

```
Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m +
1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int (a + bx)^5 \sqrt{ac + bcx} \, dx &= \frac{\int (ac + bcx)^{11/2} \, dx}{c^5} \\ &= \frac{2(ac + bcx)^{13/2}}{13bc^6} \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 1.14

$$\frac{2(a + bx)^6 \sqrt{c(a + bx)}}{13b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5*Sqrt[a*c + b*c*x],x]

[Out] (2*(a + b*x)^6*Sqrt[c*(a + b*x)])/(13*b)

fricas [B] time = 0.43, size = 75, normalized size = 3.41

$$\frac{2(b^6x^6 + 6ab^5x^5 + 15a^2b^4x^4 + 20a^3b^3x^3 + 15a^4b^2x^2 + 6a^5bx + a^6)\sqrt{bcx + ac}}{13b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^(1/2),x, algorithm="fricas")

[Out] 2/13*(b^6*x^6 + 6*a*b^5*x^5 + 15*a^2*b^4*x^4 + 20*a^3*b^3*x^3 + 15*a^4*b^2*x^2 + 6*a^5*b*x + a^6)*sqrt(b*c*x + a*c)/b

giac [B] time = 1.27, size = 495, normalized size = 22.50

$$2 \left(3003 \sqrt{bcx + ac} a^6 - \frac{6006 \left(3 \sqrt{bcx + ac} ac - (bcx + ac)^{\frac{3}{2}} \right) a^5}{c} + \frac{3003 \left(15 \sqrt{bcx + ac} a^2 c^2 - 10 (bcx + ac)^{\frac{3}{2}} ac + 3 (bcx + ac)^{\frac{5}{2}} \right) a^4}{c^2} - \frac{1716 \left(35 \sqrt{bcx + ac} \right)}{c^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5*(b*c*x+a*c)^(1/2),x, algorithm="giac")

[Out] 2/3003*(3003*sqrt(b*c*x + a*c)*a^6 - 6006*(3*sqrt(b*c*x + a*c)*a*c - (b*c*x + a*c)^(3/2))*a^5/c + 3003*(15*sqrt(b*c*x + a*c)*a^2*c^2 - 10*(b*c*x + a*c)^(3/2)*a*c + 3*(b*c*x + a*c)^(5/2))*a^4/c^2 - 1716*(35*sqrt(b*c*x + a*c)*a^3*c^3 - 35*(b*c*x + a*c)^(3/2)*a^2*c^2 + 21*(b*c*x + a*c)^(5/2)*a*c - 5*(b*c*x + a*c)^(7/2))*a^3/c^3 + 143*(315*sqrt(b*c*x + a*c)*a^4*c^4 - 420*(b*c*x + a*c)^(3/2)*a^3*c^3 + 378*(b*c*x + a*c)^(5/2)*a^2*c^2 - 180*(b*c*x + a*c)^(7/2)*a*c + 35*(b*c*x + a*c)^(9/2))*a^2/c^4 - 26*(693*sqrt(b*c*x + a*c)*a^5*c^5 - 1155*(b*c*x + a*c)^(3/2)*a^4*c^4 + 1386*(b*c*x + a*c)^(5/2)*a^3*c^3 - 990*(b*c*x + a*c)^(7/2)*a^2*c^2 + 385*(b*c*x + a*c)^(9/2)*a*c - 63*(b*c*x + a*c)^(11/2))*a/c^5 + (3003*sqrt(b*c*x + a*c)*a^6*c^6 - 6006*(b*c*x + a*c)^(3/2)*a^5*c^5 + 9009*(b*c*x + a*c)^(5/2)*a^4*c^4 - 8580*(b*c*x + a*c)^(7/2)*a^3*c^3 + 5005*(b*c*x + a*c)^(9/2)*a^2*c^2 - 1638*(b*c*x + a*c)^(11/2)*a*c + 231*(b*c*x + a*c)^(13/2))/c^6)/b

maple [A] time = 0.00, size = 23, normalized size = 1.05

$$\frac{2(bx + a)^6 \sqrt{bcx + ac}}{13b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^5*(b*c*x+a*c)^(1/2),x)`

[Out] $2/13*(b*x+a)^6*(b*c*x+a*c)^(1/2)/b$

maxima [A] time = 1.36, size = 18, normalized size = 0.82

$$\frac{2(bc x + ac)^{\frac{13}{2}}}{13 b c^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5*(b*c*x+a*c)^(1/2),x, algorithm="maxima")`

[Out] $2/13*(b*c*x + a*c)^(13/2)/(b*c^6)$

mupad [B] time = 0.03, size = 17, normalized size = 0.77

$$\frac{2(c(a + b x))^{13/2}}{13 b c^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a*c + b*c*x)^(1/2)*(a + b*x)^5,x)`

[Out] $(2*(c*(a + b*x))^(13/2))/(13*b*c^6)$

sympy [A] time = 1.06, size = 66, normalized size = 3.00

$$\begin{cases} \frac{2b^{\frac{11}{2}}\sqrt{c}\left(\frac{a}{b}+x\right)^{\frac{13}{2}}}{13} & \text{for } \left|\frac{a}{b}+x\right| < 1 \\ b^{\frac{11}{2}}\sqrt{c}G_{2,2}^{1,1}\left(\begin{matrix} 1 & \frac{15}{2} \\ \frac{13}{2} & 0 \end{matrix} \middle| \frac{a}{b}+x\right) + b^{\frac{11}{2}}\sqrt{c}G_{2,2}^{0,2}\left(\begin{matrix} \frac{15}{2}, 1 \\ \frac{13}{2}, 0 \end{matrix} \middle| \frac{a}{b}+x\right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5*(b*c*x+a*c)**(1/2),x)`

[Out] `Piecewise((2*b**(11/2)*sqrt(c)*(a/b + x)**(13/2)/13, Abs(a/b + x) < 1), (b**
*(11/2)*sqrt(c)*meijerg(((1,), (15/2,)), ((13/2,), (0,)), a/b + x) + b**(11
/2)*sqrt(c)*meijerg(((15/2, 1), ()), (((), (13/2, 0)), a/b + x), True))`

$$3.1446 \quad \int \frac{(a+bx)^5}{\sqrt{ac+bcx}} dx$$

Optimal. Leaf size=22

$$\frac{2(ac + bcx)^{11/2}}{11bc^6}$$

[Out] 2/11*(b*c*x+a*c)^(11/2)/b/c^6

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$\frac{2(ac + bcx)^{11/2}}{11bc^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/Sqrt[a*c + b*c*x], x]

[Out] (2*(a*c + b*c*x)^(11/2))/(11*b*c^6)

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
&& EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a + bx)^5}{\sqrt{ac + bcx}} dx &= \frac{\int (ac + bcx)^{9/2} dx}{c^5} \\ &= \frac{2(ac + bcx)^{11/2}}{11bc^6} \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 1.14

$$\frac{2(a + bx)^6}{11b\sqrt{c(a + bx)}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/Sqrt[a*c + b*c*x], x]

[Out] (2*(a + b*x)^6)/(11*b*Sqrt[c*(a + b*x)])

fricas [B] time = 0.41, size = 67, normalized size = 3.05

$$\frac{2(b^5x^5 + 5ab^4x^4 + 10a^2b^3x^3 + 10a^3b^2x^2 + 5a^4bx + a^5)\sqrt{bcx + ac}}{11bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(1/2), x, algorithm="fricas")

[Out] 2/11*(b^5*x^5 + 5*a*b^4*x^4 + 10*a^2*b^3*x^3 + 10*a^3*b^2*x^2 + 5*a^4*b*x + a^5)*sqrt(b*c*x + a*c)/(b*c)

giac [B] time = 0.97, size = 374, normalized size = 17.00

$$2 \left(693 \sqrt{bcx + ac} a^5 - \frac{1155 \left(3 \sqrt{bcx + ac} ac - (bcx + ac)^{\frac{3}{2}} \right) a^4}{c} + \frac{462 \left(15 \sqrt{bcx + ac} a^2 c^2 - 10 (bcx + ac)^{\frac{3}{2}} ac + 3 (bcx + ac)^{\frac{5}{2}} \right) a^3}{c^2} - \frac{198 \left(35 \sqrt{bcx + ac} a^3 c^3 - 15 (bcx + ac)^{\frac{3}{2}} a^2 c^2 + 10 (bcx + ac)^{\frac{5}{2}} a c - 5 (bcx + ac)^{\frac{7}{2}} \right) a^2}{c^3} + \frac{11 \left(315 \sqrt{bcx + ac} a^4 c^4 - 420 (bcx + ac)^{\frac{3}{2}} a^3 c^3 + 378 (bcx + ac)^{\frac{5}{2}} a^2 c^2 - 180 (bcx + ac)^{\frac{7}{2}} a c + 35 (bcx + ac)^{\frac{9}{2}} \right) a}{c^4} - \frac{693 \sqrt{bcx + ac} a^5 c^5 - 1155 (bcx + ac)^{\frac{3}{2}} a^4 c^4 + 1386 (bcx + ac)^{\frac{5}{2}} a^3 c^3 - 990 (bcx + ac)^{\frac{7}{2}} a^2 c^2 + 385 (bcx + ac)^{\frac{9}{2}} a c - 63 (bcx + ac)^{\frac{11}{2}}}{c^5} \right) / (b*c)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(1/2), x, algorithm="giac")

[Out] 2/693*(693*sqrt(b*c*x + a*c)*a^5 - 1155*(3*sqrt(b*c*x + a*c)*a*c - (b*c*x + a*c)^(3/2))*a^4/c + 462*(15*sqrt(b*c*x + a*c)*a^2*c^2 - 10*(b*c*x + a*c)^(3/2)*a*c + 3*(b*c*x + a*c)^(5/2))*a^3/c^2 - 198*(35*sqrt(b*c*x + a*c)*a^3*c^3 - 35*(b*c*x + a*c)^(3/2)*a^2*c^2 + 21*(b*c*x + a*c)^(5/2)*a*c - 5*(b*c*x + a*c)^(7/2))*a^2/c^3 + 11*(315*sqrt(b*c*x + a*c)*a^4*c^4 - 420*(b*c*x + a*c)^(3/2)*a^3*c^3 + 378*(b*c*x + a*c)^(5/2)*a^2*c^2 - 180*(b*c*x + a*c)^(7/2)*a*c + 35*(b*c*x + a*c)^(9/2))*a/c^4 - (693*sqrt(b*c*x + a*c)*a^5*c^5 - 1155*(b*c*x + a*c)^(3/2)*a^4*c^4 + 1386*(b*c*x + a*c)^(5/2)*a^3*c^3 - 990*(b*c*x + a*c)^(7/2)*a^2*c^2 + 385*(b*c*x + a*c)^(9/2)*a*c - 63*(b*c*x + a*c)^(11/2))/c^5)/(b*c)

maple [A] time = 0.00, size = 23, normalized size = 1.05

$$\frac{2(bx + a)^6}{11\sqrt{bcx + ac} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^5/(b*c*x+a*c)^(1/2),x)`

[Out] $2/11*(b*x+a)^6/b/(b*c*x+a*c)^(1/2)$

maxima [B] time = 1.46, size = 374, normalized size = 17.00

$$2 \left(693 \sqrt{bcx+ac} a^5 - \frac{1155 \left(3 \sqrt{bcx+ac} ac - (bcx+ac)^{\frac{3}{2}} \right) a^4}{c} + \frac{462 \left(15 \sqrt{bcx+ac} a^2 c^2 - 10 (bcx+ac)^{\frac{3}{2}} ac + 3 (bcx+ac)^{\frac{5}{2}} \right) a^3}{c^2} - \frac{198 \left(35 \sqrt{bcx+ac} a^3 c \right)}{c^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5/(b*c*x+a*c)^(1/2),x, algorithm="maxima")`

[Out] $2/693*(693*\sqrt{b*c*x+a*c}*a^5 - 1155*(3*\sqrt{b*c*x+a*c}*a*c - (b*c*x+a*c)^{(3/2}))*a^4/c + 462*(15*\sqrt{b*c*x+a*c}*a^2*c^2 - 10*(b*c*x+a*c)^{(3/2})*a*c + 3*(b*c*x+a*c)^{(5/2}))*a^3/c^2 - 198*(35*\sqrt{b*c*x+a*c}*a^3*c^3 - 35*(b*c*x+a*c)^{(3/2})*a^2*c^2 + 21*(b*c*x+a*c)^{(5/2})*a*c - 5*(b*c*x+a*c)^{(7/2}))*a^2/c^3 + 11*(315*\sqrt{b*c*x+a*c}*a^4*c^4 - 420*(b*c*x+a*c)^{(3/2})*a^3*c^3 + 378*(b*c*x+a*c)^{(5/2})*a^2*c^2 - 180*(b*c*x+a*c)^{(7/2})*a*c + 35*(b*c*x+a*c)^{(9/2}))*a/c^4 - (693*\sqrt{b*c*x+a*c}*a^5*c^5 - 1155*(b*c*x+a*c)^{(3/2})*a^4*c^4 + 1386*(b*c*x+a*c)^{(5/2})*a^3*c^3 - 990*(b*c*x+a*c)^{(7/2})*a^2*c^2 + 385*(b*c*x+a*c)^{(9/2})*a*c - 63*(b*c*x+a*c)^{(11/2}))/c^5)/(b*c)$

mupad [B] time = 0.03, size = 17, normalized size = 0.77

$$\frac{2(c(a+bx))^{11/2}}{11bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*x)^5/(a*c+b*c*x)^(1/2),x)`

[Out] $(2*(c*(a+b*x))^{(11/2)})/(11*b*c^6)$

sympy [A] time = 1.54, size = 73, normalized size = 3.32

$$\begin{cases} \frac{2b^{\frac{9}{2}}\left(\frac{a}{b}+x\right)^{\frac{11}{2}}}{11\sqrt{c}} & \text{for } \left|\frac{a}{b}+x\right| > 1 \vee \left|\frac{a}{b}+x\right| < 1 \\ \frac{b^{\frac{9}{2}}G_{2,2}^{1,1}\left(\begin{matrix} 1 & \frac{13}{2} \\ \frac{11}{2} & 0 \end{matrix} \middle| \frac{a}{b}+x\right)}{\sqrt{c}} + \frac{b^{\frac{9}{2}}G_{2,2}^{0,2}\left(\begin{matrix} \frac{13}{2}, 1 \\ \frac{11}{2}, 0 \end{matrix} \middle| \frac{a}{b}+x\right)}{\sqrt{c}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**5/(b*c*x+a*c)**(1/2),x)
```

```
[Out] Piecewise((2*b**(9/2)*(a/b + x)**(11/2)/(11*sqrt(c)), (Abs(a/b + x) > 1) |  
(Abs(a/b + x) < 1)), (b**(9/2)*meijerg(((1,), (13/2,)), ((11/2,)), (0,)), a/  
b + x)/sqrt(c) + b**(9/2)*meijerg(((13/2, 1), ()), ((11/2, 0)), a/b + x  
) /sqrt(c), True))
```

$$3.1447 \quad \int \frac{(a+bx)^5}{(ac+bcx)^{3/2}} dx$$

Optimal. Leaf size=22

$$\frac{2(ac+bcx)^{9/2}}{9bc^6}$$

[Out] 2/9*(b*c*x+a*c)^(9/2)/b/c^6

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$\frac{2(ac+bcx)^{9/2}}{9bc^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^(3/2), x]

[Out] (2*(a*c + b*c*x)^(9/2))/(9*b*c^6)

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
&& EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^{3/2}} dx &= \frac{\int (ac+bcx)^{7/2} dx}{c^5} \\ &= \frac{2(ac+bcx)^{9/2}}{9bc^6} \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 1.14

$$\frac{2(a+bx)^6}{9b(c(a+bx))^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^(3/2), x]

[Out] (2*(a + b*x)^6)/(9*b*(c*(a + b*x))^(3/2))

fricas [B] time = 0.45, size = 56, normalized size = 2.55

$$\frac{2(b^4x^4 + 4ab^3x^3 + 6a^2b^2x^2 + 4a^3bx + a^4)\sqrt{bcx + ac}}{9bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(3/2), x, algorithm="fricas")

[Out] 2/9*(b^4*x^4 + 4*a*b^3*x^3 + 6*a^2*b^2*x^2 + 4*a^3*b*x + a^4)*sqrt(b*c*x + a*c)/(b*c^2)

giac [B] time = 1.18, size = 266, normalized size = 12.09

$$2 \left(315 \sqrt{bcx + ac} a^4 - \frac{420 \left(3 \sqrt{bcx + ac} ac - (bcx + ac)^{\frac{3}{2}} \right) a^3}{c} + \frac{126 \left(15 \sqrt{bcx + ac} a^2 c^2 - 10 (bcx + ac)^{\frac{3}{2}} ac + 3 (bcx + ac)^{\frac{5}{2}} \right) a^2}{c^2} - \frac{36 \left(35 \sqrt{bcx + ac} a^3 c^3 - 35 (bcx + ac)^{\frac{3}{2}} a^2 c^2 + 21 (bcx + ac)^{\frac{5}{2}} a c - 5 (bcx + ac)^{\frac{7}{2}} \right) a}{c^3} + \frac{(315 \sqrt{bcx + ac} a^4 c^4 - 420 (bcx + ac)^{\frac{3}{2}} a^3 c^3 + 378 (bcx + ac)^{\frac{5}{2}} a^2 c^2 - 180 (bcx + ac)^{\frac{7}{2}} a c + 35 (bcx + ac)^{\frac{9}{2}})}{c^4} \right) / (b*c^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(3/2), x, algorithm="giac")

[Out] 2/315*(315*sqrt(b*c*x + a*c)*a^4 - 420*(3*sqrt(b*c*x + a*c)*a*c - (b*c*x + a*c)^(3/2))*a^3/c + 126*(15*sqrt(b*c*x + a*c)*a^2*c^2 - 10*(b*c*x + a*c)^(3/2)*a*c + 3*(b*c*x + a*c)^(5/2))*a^2/c^2 - 36*(35*sqrt(b*c*x + a*c)*a^3*c^3 - 35*(b*c*x + a*c)^(3/2)*a^2*c^2 + 21*(b*c*x + a*c)^(5/2)*a*c - 5*(b*c*x + a*c)^(7/2))*a/c^3 + (315*sqrt(b*c*x + a*c)*a^4*c^4 - 420*(b*c*x + a*c)^(3/2)*a^3*c^3 + 378*(b*c*x + a*c)^(5/2)*a^2*c^2 - 180*(b*c*x + a*c)^(7/2)*a*c + 35*(b*c*x + a*c)^(9/2))/c^4)/(b*c^2)

maple [A] time = 0.00, size = 23, normalized size = 1.05

$$\frac{2(bx + a)^6}{9(bcx + ac)^{\frac{3}{2}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^(3/2), x)

[Out] 2/9*(b*x+a)^6/b/(b*c*x+a*c)^(3/2)

maxima [A] time = 1.43, size = 18, normalized size = 0.82

$$\frac{2 (bcx + ac)^{\frac{9}{2}}}{9 bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(3/2),x, algorithm="maxima")

[Out] 2/9*(b*c*x + a*c)^(9/2)/(b*c^6)

mupad [B] time = 0.03, size = 17, normalized size = 0.77

$$\frac{2 (c (a + b x))^{\frac{9}{2}}}{9 b c^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/(a*c + b*c*x)^(3/2),x)

[Out] (2*(c*(a + b*x))^(9/2))/(9*b*c^6)

sympy [A] time = 1.65, size = 73, normalized size = 3.32

$$\left\{ \begin{array}{l} \frac{2b^{\frac{7}{2}} \left(\frac{a}{b} + x\right)^{\frac{9}{2}}}{9c^{\frac{3}{2}}} \quad \text{for } \left|\frac{a}{b} + x\right| > 1 \vee \left|\frac{a}{b} + x\right| < 1 \\ \frac{b^{\frac{7}{2}} G_{2,2}^{1,1} \left(\begin{array}{c} 1 \quad \frac{11}{2} \\ \frac{9}{2} \quad 0 \end{array} \middle| \frac{a}{b} + x \right)}{c^{\frac{3}{2}}} + \frac{b^{\frac{7}{2}} G_{2,2}^{0,2} \left(\begin{array}{c} \frac{11}{2}, 1 \\ \frac{9}{2}, 0 \end{array} \middle| \frac{a}{b} + x \right)}{c^{\frac{3}{2}}} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/(b*c*x+a*c)**(3/2),x)

[Out] Piecewise((2*b**(7/2)*(a/b + x)**(9/2)/(9*c**(3/2)), (Abs(a/b + x) > 1) | (Abs(a/b + x) < 1)), (b**(7/2)*meijerg(((1,), (11/2,)), ((9/2,), (0,)), a/b + x)/c**(3/2) + b**(7/2)*meijerg(((11/2, 1), ()), ((), (9/2, 0)), a/b + x)/c**(3/2), True))

$$3.1448 \quad \int \frac{(a+bx)^5}{(ac+bcx)^{5/2}} dx$$

Optimal. Leaf size=22

$$\frac{2(ac + bcx)^{7/2}}{7bc^6}$$

[Out] $2/7*(b*c*x+a*c)^{(7/2)}/b/c^6$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$\frac{2(ac + bcx)^{7/2}}{7bc^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^(5/2), x]

[Out] (2*(a*c + b*c*x)^(7/2))/(7*b*c^6)

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :> Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x] && EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x, a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a + bx)^5}{(ac + bcx)^{5/2}} dx &= \frac{\int (ac + bcx)^{5/2} dx}{c^5} \\ &= \frac{2(ac + bcx)^{7/2}}{7bc^6} \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 1.14

$$\frac{2(a + bx)^6}{7b(c(a + bx))^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^(5/2), x]

[Out] (2*(a + b*x)^6)/(7*b*(c*(a + b*x))^(5/2))

fricas [B] time = 0.41, size = 45, normalized size = 2.05

$$\frac{2(b^3x^3 + 3ab^2x^2 + 3a^2bx + a^3)\sqrt{bcx + ac}}{7bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(5/2), x, algorithm="fricas")

[Out] 2/7*(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3)*sqrt(b*c*x + a*c)/(b*c^3)

giac [B] time = 0.96, size = 178, normalized size = 8.09

$$\frac{2 \left(35 \sqrt{bcx + ac} a^3 - \frac{35 \left(3 \sqrt{bcx + ac} ac - (bcx + ac)^{\frac{3}{2}} \right) a^2}{c} + \frac{7 \left(15 \sqrt{bcx + ac} a^2 c^2 - 10 (bcx + ac)^{\frac{3}{2}} ac + 3 (bcx + ac)^{\frac{5}{2}} \right) a}{c^2} - \frac{35 \sqrt{bcx + ac} a^3 c^3 - 35 (bcx + ac)^{\frac{3}{2}} a^2 c^2}{c^2} \right)}{35 bc^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(5/2), x, algorithm="giac")

[Out] 2/35*(35*sqrt(b*c*x + a*c)*a^3 - 35*(3*sqrt(b*c*x + a*c)*a*c - (b*c*x + a*c)^(3/2))*a^2/c + 7*(15*sqrt(b*c*x + a*c)*a^2*c^2 - 10*(b*c*x + a*c)^(3/2)*a*c + 3*(b*c*x + a*c)^(5/2))*a/c^2 - (35*sqrt(b*c*x + a*c)*a^3*c^3 - 35*(b*c*x + a*c)^(3/2)*a^2*c^2 + 21*(b*c*x + a*c)^(5/2)*a*c - 5*(b*c*x + a*c)^(7/2))/c^3)/(b*c^3)

maple [A] time = 0.00, size = 23, normalized size = 1.05

$$\frac{2(bx + a)^6}{7(bcx + ac)^{\frac{5}{2}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^(5/2), x)

[Out] 2/7*(b*x+a)^6/b/(b*c*x+a*c)^(5/2)

maxima [A] time = 1.38, size = 18, normalized size = 0.82

$$\frac{2(bcx + ac)^{\frac{7}{2}}}{7bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^5/(b*c*x+a*c)^(5/2),x, algorithm="maxima")`

[Out] $2/7*(b*c*x + a*c)^{(7/2)}/(b*c^6)$

mupad [B] time = 0.03, size = 17, normalized size = 0.77

$$\frac{2(c(a+bx))^{7/2}}{7bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(a*c + b*c*x)^(5/2),x)`

[Out] $(2*(c*(a + b*x))^{(7/2)})/(7*b*c^6)$

sympy [A] time = 1.62, size = 73, normalized size = 3.32

$$\begin{cases} \frac{2b^{\frac{5}{2}}\left(\frac{a}{b}+x\right)^{\frac{7}{2}}}{7c^{\frac{5}{2}}} & \text{for } \left|\frac{a}{b}+x\right| > 1 \vee \left|\frac{a}{b}+x\right| < 1 \\ \frac{b^{\frac{5}{2}}G_{2,2}^{1,1}\left(\begin{matrix} 1 & \frac{9}{2} \\ \frac{7}{2} & 0 \end{matrix} \middle| \frac{a}{b}+x\right)}{c^{\frac{5}{2}}} + \frac{b^{\frac{5}{2}}G_{2,2}^{0,2}\left(\begin{matrix} \frac{9}{2}, 1 \\ \frac{7}{2}, 0 \end{matrix} \middle| \frac{a}{b}+x\right)}{c^{\frac{5}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(b*c*x+a*c)**(5/2),x)`

[Out] `Piecewise((2*b**(5/2)*(a/b + x)**(7/2)/(7*c**(5/2)), (Abs(a/b + x) > 1) | (Abs(a/b + x) < 1)), (b**(5/2)*meijerg(((1, (9/2,)), ((7/2,), (0,)), a/b + x)/c**(5/2) + b**(5/2)*meijerg(((9/2, 1), ()), ((), (7/2, 0)), a/b + x)/c**(5/2), True))`

$$3.1449 \quad \int \frac{(a+bx)^5}{(ac+bcx)^{7/2}} dx$$

Optimal. Leaf size=22

$$\frac{2(ac+bcx)^{5/2}}{5bc^6}$$

[Out] 2/5*(b*c*x+a*c)^(5/2)/b/c^6

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$\frac{2(ac+bcx)^{5/2}}{5bc^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^(7/2), x]

[Out] (2*(a*c + b*c*x)^(5/2))/(5*b*c^6)

Rule 21

Int[(u_)*((a_) + (b_)*(v_))^(m_)*((c_) + (d_)*(v_))^(n_), x_Symbol] :>
Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
&& EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
a + b*x])

Rule 32

Int[((a_) + (b_)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^{7/2}} dx &= \frac{\int (ac+bcx)^{3/2} dx}{c^5} \\ &= \frac{2(ac+bcx)^{5/2}}{5bc^6} \end{aligned}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 1.14

$$\frac{2(a+bx)^6}{5b(c(a+bx))^{7/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^(7/2), x]

[Out] (2*(a + b*x)^6)/(5*b*(c*(a + b*x))^(7/2))

fricas [A] time = 0.43, size = 34, normalized size = 1.55

$$\frac{2(b^2x^2 + 2abx + a^2)\sqrt{bcx + ac}}{5bc^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(7/2), x, algorithm="fricas")

[Out] 2/5*(b^2*x^2 + 2*a*b*x + a^2)*sqrt(b*c*x + a*c)/(b*c^4)

giac [B] time = 0.99, size = 106, normalized size = 4.82

$$\frac{2 \left(15 \sqrt{bcx + ac} a^2 - \frac{10 \left(3 \sqrt{bcx + ac} ac - (bcx + ac)^{\frac{3}{2}} \right) a}{c} + \frac{15 \sqrt{bcx + ac} a^2 c^2 - 10 (bcx + ac)^{\frac{3}{2}} ac + 3 (bcx + ac)^{\frac{5}{2}}}{c^2} \right)}{15 bc^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(7/2), x, algorithm="giac")

[Out] 2/15*(15*sqrt(b*c*x + a*c)*a^2 - 10*(3*sqrt(b*c*x + a*c)*a*c - (b*c*x + a*c)^(3/2))*a/c + (15*sqrt(b*c*x + a*c)*a^2*c^2 - 10*(b*c*x + a*c)^(3/2)*a*c + 3*(b*c*x + a*c)^(5/2))/c^2)/(b*c^4)

maple [A] time = 0.00, size = 23, normalized size = 1.05

$$\frac{2(bx + a)^6}{5(bcx + ac)^{\frac{7}{2}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^(7/2), x)

[Out] 2/5*(b*x+a)^6/b/(b*c*x+a*c)^(7/2)

maxima [A] time = 1.41, size = 18, normalized size = 0.82

$$\frac{2(bcx + ac)^{\frac{5}{2}}}{5bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(7/2),x, algorithm="maxima")

[Out] 2/5*(b*c*x + a*c)^(5/2)/(b*c^6)

mupad [B] time = 0.03, size = 17, normalized size = 0.77

$$\frac{2(c(a+bx))^{5/2}}{5bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/(a*c + b*c*x)^(7/2),x)

[Out] (2*(c*(a + b*x))^(5/2))/(5*b*c^6)

sympy [A] time = 4.11, size = 80, normalized size = 3.64

$$\begin{cases} \frac{2a^2\sqrt{ac+bcx}}{5bc^4} + \frac{4ax\sqrt{ac+bcx}}{5c^4} + \frac{2bx^2\sqrt{ac+bcx}}{5c^4} & \text{for } b \neq 0 \\ \frac{a^5x}{(ac)^{7/2}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/(b*c*x+a*c)**(7/2),x)

[Out] Piecewise((2*a**2*sqrt(a*c + b*c*x)/(5*b*c**4) + 4*a*x*sqrt(a*c + b*c*x)/(5*c**4) + 2*b*x**2*sqrt(a*c + b*c*x)/(5*c**4), Ne(b, 0)), (a**5*x/(a*c)**(7/2), True))

$$3.1450 \quad \int \frac{(a+bx)^5}{(ac+bcx)^{9/2}} dx$$

Optimal. Leaf size=22

$$\frac{2(ac+bcx)^{3/2}}{3bc^6}$$

[Out] $2/3*(b*c*x+a*c)^{(3/2)}/b/c^6$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$\frac{2(ac+bcx)^{3/2}}{3bc^6}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^5/(a*c + b*c*x)^{(9/2)}, x]$

[Out] $(2*(a*c + b*c*x)^{(3/2)})/(3*b*c^6)$

Rule 21

$\text{Int}[(u_.)*((a_.) + (b_.)*(v_))^{(m_.)}*((c_.) + (d_.)*(v_))^{(n_.)}, x_Symbol] \rightarrow \text{Dist}[(b/d)^m, \text{Int}[u*(c + d*v)^{(m+n)}, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\& \text{EqQ}[b*c - a*d, 0] \&\& \text{IntegerQ}[m] \&\& (!\text{IntegerQ}[n] || \text{SimplerQ}[c + d*x, a + b*x])$

Rule 32

$\text{Int}[(a_.) + (b_.)*(x_))^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}/(b*(m+1)), x] /; \text{FreeQ}\{a, b, m\}, x] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^{9/2}} dx &= \frac{\int \sqrt{ac+bcx} dx}{c^5} \\ &= \frac{2(ac+bcx)^{3/2}}{3bc^6} \end{aligned}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 1.18

$$\frac{2(a+bx)\sqrt{c(a+bx)}}{3bc^5}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^(9/2), x]

[Out] (2*(a + b*x)*Sqrt[c*(a + b*x)])/(3*b*c^5)

fricas [A] time = 0.44, size = 23, normalized size = 1.05

$$\frac{2\sqrt{bcx+ac}(bx+a)}{3bc^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(9/2), x, algorithm="fricas")

[Out] 2/3*sqrt(b*c*x + a*c)*(b*x + a)/(b*c^5)

giac [B] time = 1.07, size = 54, normalized size = 2.45

$$\frac{2\left(3\sqrt{bcx+ac}a - \frac{3\sqrt{bcx+ac}ac-(bcx+ac)^{\frac{3}{2}}}{c}\right)}{3bc^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(9/2), x, algorithm="giac")

[Out] 2/3*(3*sqrt(b*c*x + a*c)*a - (3*sqrt(b*c*x + a*c)*a*c - (b*c*x + a*c)^(3/2))/c)/(b*c^5)

maple [A] time = 0.00, size = 23, normalized size = 1.05

$$\frac{2(bx+a)^6}{3(bc^2+ac)^{\frac{9}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^(9/2), x)

[Out] 2/3*(b*x+a)^6/b/(b*c*x+a*c)^(9/2)

maxima [A] time = 1.39, size = 18, normalized size = 0.82

$$\frac{2(bc^2+ac)^{\frac{3}{2}}}{3bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(9/2),x, algorithm="maxima")

[Out] $\frac{2}{3}*(b*c*x + a*c)^{(3/2)}/(b*c^6)$

mupad [B] time = 0.03, size = 17, normalized size = 0.77

$$\frac{2(c(a+bx))^{3/2}}{3bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^5/(a*c + b*c*x)^(9/2),x)

[Out] $(2*(c*(a + b*x))^{(3/2)})/(3*b*c^6)$

sympy [A] time = 8.31, size = 53, normalized size = 2.41

$$\begin{cases} \frac{2a\sqrt{ac+bcx}}{3bc^5} + \frac{2x\sqrt{ac+bcx}}{3c^5} & \text{for } b \neq 0 \\ \frac{a^5x}{(ac)^2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**5/(b*c*x+a*c)**(9/2),x)

[Out] Piecewise((2*a*sqrt(a*c + b*c*x)/(3*b*c**5) + 2*x*sqrt(a*c + b*c*x)/(3*c**5), Ne(b, 0)), (a**5*x/(a*c)**(9/2), True))

$$3.1451 \quad \int \frac{(a+bx)^5}{(ac+bcx)^{11/2}} dx$$

Optimal. Leaf size=20

$$\frac{2\sqrt{ac+bcx}}{bc^6}$$

[Out] 2*(b*c*x+a*c)^(1/2)/b/c^6

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$\frac{2\sqrt{ac+bcx}}{bc^6}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^(11/2), x]

[Out] (2*Sqrt[a*c + b*c*x])/(b*c^6)

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :=
Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
&& EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^{11/2}} dx &= \int \frac{1}{\sqrt{ac+bcx}} dx \\ &= \frac{2\sqrt{ac+bcx}}{bc^6} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 1.20

$$\frac{2(a+bx)}{bc^5\sqrt{c(a+bx)}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^(11/2), x]

[Out] (2*(a + b*x))/(b*c^5*Sqrt[c*(a + b*x)])

fricas [A] time = 0.42, size = 18, normalized size = 0.90

$$\frac{2\sqrt{bcx+ac}}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(11/2), x, algorithm="fricas")

[Out] 2*sqrt(b*c*x + a*c)/(b*c^6)

giac [A] time = 1.03, size = 18, normalized size = 0.90

$$\frac{2\sqrt{bcx+ac}}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(11/2), x, algorithm="giac")

[Out] 2*sqrt(b*c*x + a*c)/(b*c^6)

maple [A] time = 0.00, size = 23, normalized size = 1.15

$$\frac{2(bx+a)^6}{(bcx+ac)^{\frac{11}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^(11/2), x)

[Out] 2*(b*x+a)^6/b/(b*c*x+a*c)^(11/2)

maxima [A] time = 1.38, size = 18, normalized size = 0.90

$$\frac{2\sqrt{bcx+ac}}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(11/2), x, algorithm="maxima")

[Out] $2\sqrt{b*c*x + a*c}/(b*c^6)$

mupad [B] time = 0.03, size = 17, normalized size = 0.85

$$\frac{2\sqrt{c(a+bx)}}{bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(a*c + b*c*x)^(11/2), x)`

[Out] $(2*(c*(a + b*x))^{(1/2)})/(b*c^6)$

sympy [A] time = 15.48, size = 29, normalized size = 1.45

$$\begin{cases} \frac{2\sqrt{ac+bcx}}{bc^6} & \text{for } b \neq 0 \\ \frac{a^5x}{(ac)^{\frac{11}{2}}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(b*c*x+a*c)**(11/2), x)`

[Out] `Piecewise((2*sqrt(a*c + b*c*x)/(b*c**6), Ne(b, 0)), (a**5*x/(a*c)**(11/2), True))`

$$3.1452 \quad \int \frac{(a+bx)^5}{(ac+bcx)^{13/2}} dx$$

Optimal. Leaf size=20

$$-\frac{2}{bc^6\sqrt{ac+bcx}}$$

[Out] -2/b/c^6/(b*c*x+a*c)^(1/2)

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {21, 32}

$$-\frac{2}{bc^6\sqrt{ac+bcx}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^5/(a*c + b*c*x)^(13/2), x]

[Out] -2/(b*c^6*Sqrt[a*c + b*c*x])

Rule 21

Int[(u_.)*((a_) + (b_.)*(v_))^(m_.)*((c_) + (d_.)*(v_))^(n_.), x_Symbol] :>
Dist[(b/d)^m, Int[u*(c + d*v)^(m + n), x], x] /; FreeQ[{a, b, c, d, n}, x]
&& EqQ[b*c - a*d, 0] && IntegerQ[m] && (!IntegerQ[n] || SimplerQ[c + d*x,
a + b*x])

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] :> Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^5}{(ac+bcx)^{13/2}} dx &= \int \frac{1}{(ac+bcx)^{3/2}} dx \\ &= -\frac{2}{bc^6\sqrt{ac+bcx}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 24, normalized size = 1.20

$$-\frac{2(a+bx)}{bc^5(c(a+bx))^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^5/(a*c + b*c*x)^(13/2), x]

[Out] (-2*(a + b*x))/(b*c^5*(c*(a + b*x))^(3/2))

fricas [A] time = 0.41, size = 29, normalized size = 1.45

$$-\frac{2\sqrt{bcx+ac}}{b^2c^7x+abc^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(13/2), x, algorithm="fricas")

[Out] -2*sqrt(b*c*x + a*c)/(b^2*c^7*x + a*b*c^7)

giac [A] time = 0.81, size = 18, normalized size = 0.90

$$-\frac{2}{\sqrt{bcx+ac}bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(13/2), x, algorithm="giac")

[Out] -2/(sqrt(b*c*x + a*c)*b*c^6)

maple [A] time = 0.00, size = 23, normalized size = 1.15

$$-\frac{2(bx+a)^6}{(bcx+ac)^{\frac{13}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^5/(b*c*x+a*c)^(13/2), x)

[Out] -2*(b*x+a)^6/b/(b*c*x+a*c)^(13/2)

maxima [A] time = 1.34, size = 18, normalized size = 0.90

$$-\frac{2}{\sqrt{bcx+ac}bc^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^5/(b*c*x+a*c)^(13/2), x, algorithm="maxima")

[Out] $-2/(\sqrt{b*c*x + a*c})*b*c^6$

mupad [B] time = 0.03, size = 17, normalized size = 0.85

$$-\frac{2}{b c^6 \sqrt{c (a + b x)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^5/(a*c + b*c*x)^(13/2), x)`

[Out] $-2/(b*c^6*(c*(a + b*x))^(1/2))$

sympy [A] time = 39.43, size = 48, normalized size = 2.40

$$\begin{cases} -\frac{2\sqrt{ac+bcx}}{abc^7+b^2c^7x} & \text{for } a \neq 0 \\ -\frac{2}{b^{\frac{3}{2}}c^{\frac{13}{2}}\sqrt{x}} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**5/(b*c*x+a*c)**(13/2), x)`

[Out] `Piecewise((-2*sqrt(a*c + b*c*x)/(a*b*c**7 + b**2*c**7*x), Ne(a, 0)), (-2/(b**3/2)*c**(13/2)*sqrt(x)), True)`

$$3.1453 \quad \int \frac{1}{(-2+x)\sqrt{2+x}} dx$$

Optimal. Leaf size=14

$$-\tanh^{-1}\left(\frac{\sqrt{x+2}}{2}\right)$$

[Out] -arctanh(1/2*(2+x)^(1/2))

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {63, 207}

$$-\tanh^{-1}\left(\frac{\sqrt{x+2}}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[1/((-2 + x)*Sqrt[2 + x]),x]

[Out] -ArcTanh[Sqrt[2 + x]/2]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 207

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> -Simp[ArcTanh[(Rt[b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (LtQ[a, 0] || GtQ[b, 0])

Rubi steps

$$\begin{aligned} \int \frac{1}{(-2+x)\sqrt{2+x}} dx &= 2 \text{Subst} \left(\int \frac{1}{-4+x^2} dx, x, \sqrt{2+x} \right) \\ &= -\tanh^{-1}\left(\frac{\sqrt{2+x}}{2}\right) \end{aligned}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$-\tanh^{-1}\left(\frac{\sqrt{x+2}}{2}\right)$$

Antiderivative was successfully verified.

[In] Integrate[1/((-2 + x)*Sqrt[2 + x]),x]

[Out] -ArcTanh[Sqrt[2 + x]/2]

fricas [B] time = 0.43, size = 21, normalized size = 1.50

$$-\frac{1}{2} \log(\sqrt{x+2} + 2) + \frac{1}{2} \log(\sqrt{x+2} - 2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-2+x)/(2+x)^(1/2),x, algorithm="fricas")

[Out] -1/2*log(sqrt(x + 2) + 2) + 1/2*log(sqrt(x + 2) - 2)

giac [B] time = 0.87, size = 22, normalized size = 1.57

$$-\frac{1}{2} \log(\sqrt{x+2} + 2) + \frac{1}{2} \log(|\sqrt{x+2} - 2|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-2+x)/(2+x)^(1/2),x, algorithm="giac")

[Out] -1/2*log(sqrt(x + 2) + 2) + 1/2*log(abs(sqrt(x + 2) - 2))

maple [B] time = 0.01, size = 22, normalized size = 1.57

$$\frac{\ln(\sqrt{x+2} - 2)}{2} - \frac{\ln(\sqrt{x+2} + 2)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x-2)/(x+2)^(1/2),x)

[Out] 1/2*ln((x+2)^(1/2)-2)-1/2*ln((x+2)^(1/2)+2)

maxima [B] time = 1.35, size = 21, normalized size = 1.50

$$-\frac{1}{2} \log(\sqrt{x+2} + 2) + \frac{1}{2} \log(\sqrt{x+2} - 2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-2+x)/(2+x)^(1/2),x, algorithm="maxima")

[Out] -1/2*log(sqrt(x + 2) + 2) + 1/2*log(sqrt(x + 2) - 2)

mupad [B] time = 0.05, size = 10, normalized size = 0.71

$$-\operatorname{atanh}\left(\frac{\sqrt{x+2}}{2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((x - 2)*(x + 2)^(1/2)),x)

[Out] -atanh((x + 2)^(1/2)/2)

sympy [A] time = 0.66, size = 27, normalized size = 1.93

$$\begin{cases} -\operatorname{acoth}\left(\frac{\sqrt{x+2}}{2}\right) & \text{for } \frac{|x+2|}{4} > 1 \\ -\operatorname{atanh}\left(\frac{\sqrt{x+2}}{2}\right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-2+x)/(2+x)**(1/2),x)

[Out] Piecewise((-acoth(sqrt(x + 2)/2), Abs(x + 2)/4 > 1), (-atanh(sqrt(x + 2)/2), True))

$$3.1454 \quad \int \frac{1}{(2+3x)\sqrt{1+5x}} dx$$

Optimal. Leaf size=25

$$\frac{2 \tan^{-1}\left(\sqrt{\frac{3}{7}} \sqrt{5x+1}\right)}{\sqrt{21}}$$

[Out] 2/21*arctan(1/7*21^(1/2)*(1+5*x)^(1/2))*21^(1/2)

Rubi [A] time = 0.01, antiderivative size = 25, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {63, 203}

$$\frac{2 \tan^{-1}\left(\sqrt{\frac{3}{7}} \sqrt{5x+1}\right)}{\sqrt{21}}$$

Antiderivative was successfully verified.

[In] Int[1/((2 + 3*x)*Sqrt[1 + 5*x]),x]

[Out] (2*ArcTan[Sqrt[3/7]*Sqrt[1 + 5*x]])/Sqrt[21]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])

Rubi steps

$$\int \frac{1}{(2+3x)\sqrt{1+5x}} dx = \frac{2}{5} \text{Subst} \left(\int \frac{1}{\frac{7}{5} + \frac{3x^2}{5}} dx, x, \sqrt{1+5x} \right)$$

$$= \frac{2 \tan^{-1} \left(\sqrt{\frac{3}{7}} \sqrt{1+5x} \right)}{\sqrt{21}}$$

Mathematica [A] time = 0.01, size = 25, normalized size = 1.00

$$\frac{2 \tan^{-1} \left(\sqrt{\frac{3}{7}} \sqrt{5x+1} \right)}{\sqrt{21}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((2+3*x)*Sqrt[1+5*x]),x]

[Out] (2*ArcTan[Sqrt[3/7]*Sqrt[1+5*x]])/Sqrt[21]

fricas [A] time = 0.42, size = 18, normalized size = 0.72

$$\frac{2}{21} \sqrt{21} \arctan \left(\frac{1}{7} \sqrt{21} \sqrt{5x+1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(2+3*x)/(1+5*x)^(1/2),x, algorithm="fricas")

[Out] 2/21*sqrt(21)*arctan(1/7*sqrt(21)*sqrt(5*x+1))

giac [A] time = 0.98, size = 18, normalized size = 0.72

$$\frac{2}{21} \sqrt{21} \arctan \left(\frac{1}{7} \sqrt{21} \sqrt{5x+1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(2+3*x)/(1+5*x)^(1/2),x, algorithm="giac")

[Out] 2/21*sqrt(21)*arctan(1/7*sqrt(21)*sqrt(5*x+1))

maple [A] time = 0.01, size = 19, normalized size = 0.76

$$\frac{2\sqrt{21} \arctan \left(\frac{\sqrt{21} \sqrt{5x+1}}{7} \right)}{21}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(3*x+2)/(1+5*x)^(1/2),x)`

[Out] `2/21*arctan(1/7*21^(1/2)*(1+5*x)^(1/2))*21^(1/2)`

maxima [A] time = 3.00, size = 18, normalized size = 0.72

$$\frac{2}{21} \sqrt{21} \arctan\left(\frac{1}{7} \sqrt{21} \sqrt{5x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(2+3*x)/(1+5*x)^(1/2),x, algorithm="maxima")`

[Out] `2/21*sqrt(21)*arctan(1/7*sqrt(21)*sqrt(5*x + 1))`

mupad [B] time = 0.06, size = 15, normalized size = 0.60

$$\frac{2 \sqrt{21} \operatorname{atan}\left(\frac{\sqrt{105x+21}}{7}\right)}{21}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((3*x + 2)*(5*x + 1)^(1/2)),x)`

[Out] `(2*21^(1/2)*atan((105*x + 21)^(1/2)/7))/21`

sympy [A] time = 1.12, size = 61, normalized size = 2.44

$$\left\{ \begin{array}{l} \frac{2\sqrt{21} i \operatorname{acosh}\left(\frac{\sqrt{105}}{15\sqrt{x+\frac{2}{3}}}\right)}{21} \quad \text{for } \frac{7}{15|x+\frac{2}{3}|} > 1 \\ -\frac{2\sqrt{21} \operatorname{asin}\left(\frac{\sqrt{105}}{15\sqrt{x+\frac{2}{3}}}\right)}{21} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(2+3*x)/(1+5*x)**(1/2),x)`

[Out] `Piecewise((2*sqrt(21)*I*acosh(sqrt(105)/(15*sqrt(x + 2/3)))/21, 7/(15*Abs(x + 2/3)) > 1), (-2*sqrt(21)*asin(sqrt(105)/(15*sqrt(x + 2/3)))/21, True))`

$$3.1455 \quad \int \frac{\sqrt[3]{1-x}}{1+x} dx$$

Optimal. Leaf size=84

$$3\sqrt[3]{1-x} + \frac{3 \log(\sqrt[3]{2} - \sqrt[3]{1-x})}{2^{2/3}} - \frac{\log(x+1)}{2^{2/3}} - \sqrt[3]{2} \sqrt{3} \tan^{-1}\left(\frac{2^{2/3}\sqrt[3]{1-x} + 1}{\sqrt{3}}\right)$$

[Out] $3*(1-x)^{(1/3)} + 3/2*\ln(2^{(1/3)} - (1-x)^{(1/3)})*2^{(1/3)} - 1/2*\ln(1+x)*2^{(1/3)} - 2^{(1/3)}*\arctan(1/3*(1+2^{(2/3)}*(1-x)^{(1/3)})*3^{(1/2)})*3^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {50, 57, 617, 204, 31}

$$3\sqrt[3]{1-x} + \frac{3 \log(\sqrt[3]{2} - \sqrt[3]{1-x})}{2^{2/3}} - \frac{\log(x+1)}{2^{2/3}} - \sqrt[3]{2} \sqrt{3} \tan^{-1}\left(\frac{2^{2/3}\sqrt[3]{1-x} + 1}{\sqrt{3}}\right)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(1/3)/(1 + x), x]

[Out] $3*(1-x)^{(1/3)} - 2^{(1/3)}*\text{Sqrt}[3]*\text{ArcTan}[(1+2^{(2/3)}*(1-x)^{(1/3)})/\text{Sqrt}[3]] + (3*\text{Log}[2^{(1/3)} - (1-x)^{(1/3)}])/2^{(2/3)} - \text{Log}[1+x]/2^{(2/3)}$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 57

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2), x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x]

]]) /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt[3]{1-x}}{1+x} dx &= 3\sqrt[3]{1-x} + 2 \int \frac{1}{(1-x)^{2/3}(1+x)} dx \\ &= 3\sqrt[3]{1-x} - \frac{\log(1+x)}{2^{2/3}} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{2-x}} dx, x, \sqrt[3]{1-x}\right)}{2^{2/3}} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{2^{2/3} + \sqrt[3]{2}x+x^2} dx, x, \sqrt[3]{1-x}\right)}{\sqrt[3]{2}} \\ &= 3\sqrt[3]{1-x} + \frac{3 \log(\sqrt[3]{2} - \sqrt[3]{1-x})}{2^{2/3}} - \frac{\log(1+x)}{2^{2/3}} + (3\sqrt[3]{2}) \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + 2^{2/3}\sqrt[3]{1-x}\right) \\ &= 3\sqrt[3]{1-x} - \sqrt[3]{2} \sqrt{3} \tan^{-1}\left(\frac{1 + 2^{2/3}\sqrt[3]{1-x}}{\sqrt{3}}\right) + \frac{3 \log(\sqrt[3]{2} - \sqrt[3]{1-x})}{2^{2/3}} - \frac{\log(1+x)}{2^{2/3}} \end{aligned}$$

Mathematica [A] time = 0.05, size = 104, normalized size = 1.24

$$3\sqrt[3]{1-x} + \sqrt[3]{2} \log(\sqrt[3]{2} - \sqrt[3]{1-x}) - \frac{\log((1-x)^{2/3} + \sqrt[3]{2-2x} + 2^{2/3})}{2^{2/3}} - \sqrt[3]{2} \sqrt{3} \tan^{-1}\left(\frac{2^{2/3}\sqrt[3]{1-x} + 1}{\sqrt{3}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(1/3)/(1 + x), x]

[Out] 3*(1 - x)^(1/3) - 2^(1/3)*Sqrt[3]*ArcTan[(1 + 2^(2/3)*(1 - x)^(1/3))/Sqrt[3]] + 2^(1/3)*Log[2^(1/3) - (1 - x)^(1/3)] - Log[2^(2/3) + (2 - 2*x)^(1/3) + (1 - x)^(2/3)]/2^(2/3)

fricas [A] time = 0.42, size = 86, normalized size = 1.02

$$-\sqrt{3} 2^{\frac{1}{3}} \arctan\left(\frac{1}{3} \sqrt{3} 2^{\frac{2}{3}} (-x+1)^{\frac{1}{3}} + \frac{1}{3} \sqrt{3}\right) - \frac{1}{2} \cdot 2^{\frac{1}{3}} \log\left(2^{\frac{2}{3}} + 2^{\frac{1}{3}} (-x+1)^{\frac{1}{3}} + (-x+1)^{\frac{2}{3}}\right) + 2^{\frac{1}{3}} \log\left(-2^{\frac{1}{3}} + (-x+1)^{\frac{1}{3}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/3)/(1+x),x, algorithm="fricas")

[Out] -sqrt(3)*2^(1/3)*arctan(1/3*sqrt(3)*2^(2/3)*(-x + 1)^(1/3) + 1/3*sqrt(3)) - 1/2*2^(1/3)*log(2^(2/3) + 2^(1/3)*(-x + 1)^(1/3) + (-x + 1)^(2/3)) + 2^(1/3)*log(-2^(1/3) + (-x + 1)^(1/3)) + 3*(-x + 1)^(1/3)

giac [A] time = 1.05, size = 87, normalized size = 1.04

$$-\sqrt{3} 2^{\frac{1}{3}} \arctan\left(\frac{1}{6} \sqrt{3} 2^{\frac{2}{3}} \left(2^{\frac{1}{3}} + 2(-x+1)^{\frac{1}{3}}\right)\right) - \frac{1}{2} \cdot 2^{\frac{1}{3}} \log\left(2^{\frac{2}{3}} + 2^{\frac{1}{3}} (-x+1)^{\frac{1}{3}} + (-x+1)^{\frac{2}{3}}\right) + 2^{\frac{1}{3}} \log\left(\left|-2^{\frac{1}{3}} + (-x+1)^{\frac{1}{3}}\right|\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/3)/(1+x),x, algorithm="giac")

[Out] -sqrt(3)*2^(1/3)*arctan(1/6*sqrt(3)*2^(2/3)*(2^(1/3) + 2*(-x + 1)^(1/3))) - 1/2*2^(1/3)*log(2^(2/3) + 2^(1/3)*(-x + 1)^(1/3) + (-x + 1)^(2/3)) + 2^(1/3)*log(abs(-2^(1/3) + (-x + 1)^(1/3))) + 3*(-x + 1)^(1/3)

maple [A] time = 0.01, size = 84, normalized size = 1.00

$$-2^{\frac{1}{3}} \sqrt{3} \arctan\left(\frac{\left(1 + 2^{\frac{2}{3}} (-x+1)^{\frac{1}{3}}\right) \sqrt{3}}{3}\right) + 2^{\frac{1}{3}} \ln\left((-x+1)^{\frac{1}{3}} - 2^{\frac{1}{3}}\right) - \frac{2^{\frac{1}{3}} \ln\left((-x+1)^{\frac{2}{3}} + 2^{\frac{1}{3}} (-x+1)^{\frac{1}{3}} + 2^{\frac{2}{3}}\right)}{2} + 3(-x+1)^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(1/3)/(x+1),x)

[Out] 3*(-x+1)^(1/3)+2^(1/3)*ln((-x+1)^(1/3)-2^(1/3))-1/2*2^(1/3)*ln((-x+1)^(2/3)+2^(1/3)*(-x+1)^(1/3)+2^(2/3))-2^(1/3)*arctan(1/3*(1+2^(2/3)*(-x+1)^(1/3))*3^(1/2))*3^(1/2)

maxima [A] time = 3.00, size = 86, normalized size = 1.02

$$-\sqrt{3} 2^{\frac{1}{3}} \arctan\left(\frac{1}{6} \sqrt{3} 2^{\frac{2}{3}} \left(2^{\frac{1}{3}} + 2(-x+1)^{\frac{1}{3}}\right)\right) - \frac{1}{2} \cdot 2^{\frac{1}{3}} \log\left(2^{\frac{2}{3}} + 2^{\frac{1}{3}} (-x+1)^{\frac{1}{3}} + (-x+1)^{\frac{2}{3}}\right) + 2^{\frac{1}{3}} \log\left(-2^{\frac{1}{3}} + (-x+1)^{\frac{1}{3}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(1/3)/(1+x),x, algorithm="maxima")

[Out] $-\sqrt{3} \cdot 2^{1/3} \cdot \arctan\left(\frac{1}{6} \sqrt{3} \cdot 2^{2/3} \cdot (2^{1/3} + 2 \cdot (-x + 1)^{1/3})\right) - \frac{1}{2} \cdot 2^{1/3} \cdot \log\left(2^{2/3} + 2^{1/3} \cdot (-x + 1)^{1/3} + (-x + 1)^{2/3}\right) + 2^{1/3} \cdot \log\left(-2^{1/3} + (-x + 1)^{1/3}\right) + 3 \cdot (-x + 1)^{1/3}$

mupad [B] time = 0.07, size = 104, normalized size = 1.24

$$2^{1/3} \ln\left(18(1-x)^{1/3} - 18 \cdot 2^{1/3}\right) + 3(1-x)^{1/3} + \frac{2^{1/3} \ln\left(18(1-x)^{1/3} - 9 \cdot 2^{1/3}(-1 + \sqrt{3} \cdot 1i)\right) (-1 + \sqrt{3} \cdot 1i)}{2} - \frac{2^{1/3} \ln\left(18(1-x)^{1/3} + 9 \cdot 2^{1/3}(-1 + \sqrt{3} \cdot 1i)\right) (-1 + \sqrt{3} \cdot 1i)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1-x)^(1/3)/(x+1),x)

[Out] $2^{1/3} \cdot \log\left(18 \cdot (1-x)^{1/3} - 18 \cdot 2^{1/3}\right) + 3 \cdot (1-x)^{1/3} + \frac{(2^{1/3} \cdot \log\left(18 \cdot (1-x)^{1/3} - 9 \cdot 2^{1/3} \cdot (3^{1/2} \cdot 1i - 1)\right) \cdot (3^{1/2} \cdot 1i - 1))}{2} - \frac{(2^{1/3} \cdot \log\left(18 \cdot (1-x)^{1/3} + 9 \cdot 2^{1/3} \cdot (3^{1/2} \cdot 1i + 1)\right) \cdot (3^{1/2} \cdot 1i + 1))}{2}$

sympy [C] time = 2.26, size = 170, normalized size = 2.02

$$\frac{4 \sqrt[3]{-1} \sqrt[3]{x-1} \Gamma\left(\frac{4}{3}\right)}{\Gamma\left(\frac{7}{3}\right)} + \frac{4 \sqrt[3]{-2} e^{-\frac{i\pi}{3}} \log\left(-\frac{2^{\frac{2}{3}} \sqrt[3]{x-1} e^{\frac{i\pi}{3}}}{2} + 1\right) \Gamma\left(\frac{4}{3}\right)}{3 \Gamma\left(\frac{7}{3}\right)} - \frac{4 \sqrt[3]{-2} \log\left(-\frac{2^{\frac{2}{3}} \sqrt[3]{x-1} e^{i\pi}}{2} + 1\right) \Gamma\left(\frac{4}{3}\right)}{3 \Gamma\left(\frac{7}{3}\right)} + \frac{4 \sqrt[3]{-2} e^{\frac{i\pi}{3}} \log\left(-\frac{2^{\frac{2}{3}} \sqrt[3]{x-1} e^{\frac{i\pi}{3}}}{2} + 1\right) \Gamma\left(\frac{4}{3}\right)}{3 \Gamma\left(\frac{7}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(1/3)/(1+x),x)

[Out] $4 \cdot (-1)^{1/3} \cdot (x-1)^{1/3} \cdot \frac{\Gamma(4/3)}{\Gamma(7/3)} + 4 \cdot (-2)^{1/3} \cdot \exp(-I \cdot \pi/3) \cdot \log(-2^{2/3} \cdot (x-1)^{1/3} \cdot \exp(\text{polar}(I \cdot \pi/3)/2 + 1)) \cdot \frac{\Gamma(4/3)}{3 \cdot \Gamma(7/3)} - 4 \cdot (-2)^{1/3} \cdot \log(-2^{2/3} \cdot (x-1)^{1/3} \cdot \exp(\text{polar}(I \cdot \pi)/2 + 1)) \cdot \frac{\Gamma(4/3)}{3 \cdot \Gamma(7/3)} + 4 \cdot (-2)^{1/3} \cdot \exp(I \cdot \pi/3) \cdot \log(-2^{2/3} \cdot (x-1)^{1/3} \cdot \exp(\text{polar}(5 \cdot I \cdot \pi/3)/2 + 1)) \cdot \frac{\Gamma(4/3)}{3 \cdot \Gamma(7/3)}$

3.1456 $\int \sqrt[3]{3-2x}(7+x) dx$

Optimal. Leaf size=27

$$\frac{3}{28}(3-2x)^{7/3} - \frac{51}{16}(3-2x)^{4/3}$$

[Out] $-51/16*(3-2*x)^{(4/3)}+3/28*(3-2*x)^{(7/3)}$

Rubi [A] time = 0.00, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{3}{28}(3-2x)^{7/3} - \frac{51}{16}(3-2x)^{4/3}$$

Antiderivative was successfully verified.

[In] Int[(3 - 2*x)^(1/3)*(7 + x), x]

[Out] $(-51*(3 - 2*x)^{(4/3)})/16 + (3*(3 - 2*x)^{(7/3)})/28$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \sqrt[3]{3-2x}(7+x) dx &= \int \left(\frac{17}{2} \sqrt[3]{3-2x} - \frac{1}{2}(3-2x)^{4/3} \right) dx \\ &= -\frac{51}{16}(3-2x)^{4/3} + \frac{3}{28}(3-2x)^{7/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 18, normalized size = 0.67

$$-\frac{3}{112}(3-2x)^{4/3}(8x+107)$$

Antiderivative was successfully verified.

[In] Integrate[(3 - 2*x)^(1/3)*(7 + x), x]

[Out] $(-3*(3 - 2*x)^{(4/3)}*(107 + 8*x))/112$

fricas [A] time = 0.42, size = 19, normalized size = 0.70

$$\frac{3}{112} (16x^2 + 190x - 321)(-2x + 3)^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-2*x)^(1/3)*(7+x),x, algorithm="fricas")

[Out] 3/112*(16*x^2 + 190*x - 321)*(-2*x + 3)^(1/3)

giac [A] time = 0.94, size = 26, normalized size = 0.96

$$\frac{3}{28} (2x - 3)^2(-2x + 3)^{\frac{1}{3}} - \frac{51}{16} (-2x + 3)^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-2*x)^(1/3)*(7+x),x, algorithm="giac")

[Out] 3/28*(2*x - 3)^2*(-2*x + 3)^(1/3) - 51/16*(-2*x + 3)^(4/3)

maple [A] time = 0.00, size = 15, normalized size = 0.56

$$\frac{3(8x + 107)(-2x + 3)^{\frac{4}{3}}}{112}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((3-2*x)^(1/3)*(7+x),x)

[Out] -3/112*(8*x+107)*(3-2*x)^(4/3)

maxima [A] time = 1.35, size = 19, normalized size = 0.70

$$\frac{3}{28} (-2x + 3)^{\frac{7}{3}} - \frac{51}{16} (-2x + 3)^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((3-2*x)^(1/3)*(7+x),x, algorithm="maxima")

[Out] 3/28*(-2*x + 3)^(7/3) - 51/16*(-2*x + 3)^(4/3)

mupad [B] time = 0.26, size = 14, normalized size = 0.52

$$\frac{3(3 - 2x)^{\frac{4}{3}}(8x + 107)}{112}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((3 - 2*x)^(1/3)*(x + 7), x)`

[Out] `-(3*(3 - 2*x)^(4/3)*(8*x + 107))/112`

sympy [A] time = 1.09, size = 114, normalized size = 4.22

$$\begin{cases} \frac{3(x+7)^2 \sqrt[3]{2x-3} e^{\frac{i\pi}{3}}}{7} - \frac{51(x+7) \sqrt[3]{2x-3} e^{\frac{i\pi}{3}}}{56} - \frac{2601 \sqrt[3]{2x-3} e^{\frac{i\pi}{3}}}{112} & \text{for } \frac{2|x+7|}{17} > 1 \\ \frac{3 \sqrt[3]{3-2x} (x+7)^2}{7} - \frac{51 \sqrt[3]{3-2x} (x+7)}{56} - \frac{2601 \sqrt[3]{3-2x}}{112} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((3-2*x)**(1/3)*(7+x), x)`

[Out] `Piecewise((3*(x + 7)**2*(2*x - 3)**(1/3)*exp(I*pi/3)/7 - 51*(x + 7)*(2*x - 3)**(1/3)*exp(I*pi/3)/56 - 2601*(2*x - 3)**(1/3)*exp(I*pi/3)/112, 2*Abs(x + 7)/17 > 1), (3*(3 - 2*x)**(1/3)*(x + 7)**2/7 - 51*(3 - 2*x)**(1/3)*(x + 7)/56 - 2601*(3 - 2*x)**(1/3)/112, True))`

$$3.1457 \quad \int \sqrt[3]{1-x} (1+x)^2 dx$$

Optimal. Leaf size=38

$$-\frac{3}{10}(1-x)^{10/3} + \frac{12}{7}(1-x)^{7/3} - 3(1-x)^{4/3}$$

[Out] $-3*(1-x)^{(4/3)}+12/7*(1-x)^{(7/3)}-3/10*(1-x)^{(10/3)}$

Rubi [A] time = 0.01, antiderivative size = 38, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{3}{10}(1-x)^{10/3} + \frac{12}{7}(1-x)^{7/3} - 3(1-x)^{4/3}$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(1/3)*(1 + x)^2,x]

[Out] $-3*(1-x)^{(4/3)} + (12*(1-x)^{(7/3)})/7 - (3*(1-x)^{(10/3)})/10$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int [ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && Le Q[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \sqrt[3]{1-x} (1+x)^2 dx &= \int \left(4\sqrt[3]{1-x} - 4(1-x)^{4/3} + (1-x)^{7/3} \right) dx \\ &= -3(1-x)^{4/3} + \frac{12}{7}(1-x)^{7/3} - \frac{3}{10}(1-x)^{10/3} \end{aligned}$$

Mathematica [A] time = 0.01, size = 23, normalized size = 0.61

$$-\frac{3}{70}(1-x)^{4/3} (7x^2 + 26x + 37)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(1/3)*(1 + x)^2,x]

[Out] $(-3*(1-x)^{4/3}*(37+26*x+7*x^2))/70$

fricas [A] time = 0.45, size = 24, normalized size = 0.63

$$\frac{3}{70} (7x^3 + 19x^2 + 11x - 37)(-x + 1)^{\frac{1}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(1/3)*(1+x)^2,x, algorithm="fricas")`

[Out] $3/70*(7*x^3 + 19*x^2 + 11*x - 37)*(-x + 1)^{1/3}$

giac [A] time = 0.86, size = 38, normalized size = 1.00

$$\frac{3}{10} (x-1)^3(-x+1)^{\frac{1}{3}} + \frac{12}{7} (x-1)^2(-x+1)^{\frac{1}{3}} - 3(-x+1)^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(1/3)*(1+x)^2,x, algorithm="giac")`

[Out] $3/10*(x-1)^3*(-x+1)^{1/3} + 12/7*(x-1)^2*(-x+1)^{1/3} - 3*(-x+1)^{4/3}$

maple [A] time = 0.00, size = 20, normalized size = 0.53

$$\frac{3(7x^2 + 26x + 37)(-x + 1)^{\frac{4}{3}}}{70}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-x+1)^(1/3)*(x+1)^2,x)`

[Out] $-3/70*(7*x^2+26*x+37)*(-x+1)^{4/3}$

maxima [A] time = 1.36, size = 28, normalized size = 0.74

$$-\frac{3}{10} (-x+1)^{\frac{10}{3}} + \frac{12}{7} (-x+1)^{\frac{7}{3}} - 3(-x+1)^{\frac{4}{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^(1/3)*(1+x)^2,x, algorithm="maxima")`

[Out] $-3/10*(-x+1)^{10/3} + 12/7*(-x+1)^{7/3} - 3*(-x+1)^{4/3}$

mupad [B] time = 0.05, size = 21, normalized size = 0.55

$$-\frac{3(1-x)^{4/3}(40x+7(x-1)^2+30)}{70}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((1-x)^(1/3)*(x+1)^2,x)`

[Out] `-(3*(1-x)^(4/3)*(40*x+7*(x-1)^2+30))/70`

sympy [A] time = 1.52, size = 146, normalized size = 3.84

$$\left\{ \begin{array}{ll} -\frac{3\sqrt[3]{x-1}(x+1)^3 e^{-\frac{2i\pi}{3}}}{10} + \frac{3\sqrt[3]{x-1}(x+1)^2 e^{-\frac{2i\pi}{3}}}{35} + \frac{9\sqrt[3]{x-1}(x+1) e^{-\frac{2i\pi}{3}}}{35} + \frac{54\sqrt[3]{x-1} e^{-\frac{2i\pi}{3}}}{35} & \text{for } \frac{|x+1|}{2} > 1 \\ \frac{3\sqrt[3]{1-x}(x+1)^3}{10} - \frac{3\sqrt[3]{1-x}(x+1)^2}{35} - \frac{9\sqrt[3]{1-x}(x+1)}{35} - \frac{54\sqrt[3]{1-x}}{35} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)**(1/3)*(1+x)**2,x)`

[Out] `Piecewise((-3*(x-1)**(1/3)*(x+1)**3*exp(-2*I*pi/3)/10 + 3*(x-1)**(1/3)*(x+1)**2*exp(-2*I*pi/3)/35 + 9*(x-1)**(1/3)*(x+1)*exp(-2*I*pi/3)/35 + 54*(x-1)**(1/3)*exp(-2*I*pi/3)/35, Abs(x+1)/2 > 1), (3*(1-x)**(1/3)*(x+1)**3/10 - 3*(1-x)**(1/3)*(x+1)**2/35 - 9*(1-x)**(1/3)*(x+1)/35 - 54*(1-x)**(1/3)/35, True))`

$$3.1458 \quad \int \frac{1}{(a+bx)\sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=139

$$-\frac{\log(a+bx)}{2b^{2/3}\sqrt[3]{bc-ad}} + \frac{3\log(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx})}{2b^{2/3}\sqrt[3]{bc-ad}} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}+1}{\sqrt[3]{bc-ad}}\right)}{b^{2/3}\sqrt[3]{bc-ad}}$$

[Out] $-1/2*\ln(b*x+a)/b^{(2/3)/(-a*d+b*c)^{(1/3)}+3/2*\ln((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/b^{(2/3)/(-a*d+b*c)^{(1/3)}+\arctan(1/3*(1+2*b^{(1/3)}*(d*x+c)^{(1/3)})/(-a*d+b*c)^{(1/3)})*3^{(1/2)}*3^{(1/2)}/b^{(2/3)/(-a*d+b*c)^{(1/3)}$

Rubi [A] time = 0.11, antiderivative size = 139, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {55, 617, 204, 31}

$$-\frac{\log(a+bx)}{2b^{2/3}\sqrt[3]{bc-ad}} + \frac{3\log(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx})}{2b^{2/3}\sqrt[3]{bc-ad}} + \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}+1}{\sqrt[3]{bc-ad}}\right)}{b^{2/3}\sqrt[3]{bc-ad}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)*(c + d*x)^(1/3)), x]

[Out] (Sqrt[3]*ArcTan[(1 + (2*b^(1/3)*(c + d*x)^(1/3))/(b*c - a*d)^(1/3))/Sqrt[3]])/(b^(2/3)*(b*c - a*d)^(1/3)) - Log[a + b*x]/(2*b^(2/3)*(b*c - a*d)^(1/3)) + (3*Log[(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)])/(2*b^(2/3)*(b*c - a*d)^(1/3))

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 55

Int[1/(((a_.) + (b_.)*(x_))*((c_.) + (d_.)*(x_))^(1/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q), x] + (Dist[3/(2*b), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x])] /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]

Rule 204

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 617

Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)\sqrt[3]{c+dx}} dx &= -\frac{\log(a+bx)}{2b^{2/3}\sqrt[3]{bc-ad}} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{\frac{(bc-ad)^{2/3}}{b^{2/3}} + \frac{\sqrt[3]{bc-ad}x}{\sqrt[3]{b}} + x^2} dx, x, \sqrt[3]{c+dx}\right)}{2b} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{bc-ad}}{\sqrt[3]{b}}} dx, x, 1 + \frac{2\sqrt[3]{b}}{\sqrt[3]{b}}\right)}{2b^{2/3}\sqrt[3]{bc-ad}} \\ &= -\frac{\log(a+bx)}{2b^{2/3}\sqrt[3]{bc-ad}} + \frac{3 \log(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx})}{2b^{2/3}\sqrt[3]{bc-ad}} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2\sqrt[3]{b}}{\sqrt[3]{b}}\right)}{b^{2/3}\sqrt[3]{bc-ad}} \\ &= \frac{\sqrt{3} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}}}{\sqrt{3}}\right)}{b^{2/3}\sqrt[3]{bc-ad}} - \frac{\log(a+bx)}{2b^{2/3}\sqrt[3]{bc-ad}} + \frac{3 \log(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx})}{2b^{2/3}\sqrt[3]{bc-ad}} \end{aligned}$$

Mathematica [A] time = 0.08, size = 106, normalized size = 0.76

$$\frac{3 \log(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}) + 2\sqrt{3} \tan^{-1}\left(\frac{\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}} + 1}{\sqrt{3}}\right) - \log(a+bx)}{2b^{2/3}\sqrt[3]{bc-ad}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*(c + d*x)^(1/3)), x]

[Out] (2*Sqrt[3]*ArcTan[(1 + (2*b^(1/3)*(c + d*x)^(1/3))/(b*c - a*d)^(1/3))/Sqrt[3]] - Log[a + b*x] + 3*Log[(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)])/(2*b^(2/3)*(b*c - a*d)^(1/3))

fricas [B] time = 0.50, size = 570, normalized size = 4.10

$$\sqrt{3}(b^2c - abd) \sqrt{-\frac{(b^3c - ab^2d)^{\frac{1}{3}}}{bc - ad}} \log \left(\frac{2b^2dx + 3b^2c - abd - \sqrt{3} \left((b^3c - ab^2d)^{\frac{1}{3}}(bc - ad) + (b^2c - abd)(dx + c)^{\frac{1}{3}} - 2(b^3c - ab^2d)^{\frac{2}{3}}(dx + c)^{\frac{2}{3}} \right) \sqrt{-\frac{(b^3c - ab^2d)^{\frac{1}{3}}}{bc - ad}}}{bx + a} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] [1/2*(sqrt(3)*(b^2*c - a*b*d)*sqrt(-(b^3*c - a*b^2*d)^(1/3)/(b*c - a*d))*log((2*b^2*d*x + 3*b^2*c - a*b*d - sqrt(3)*((b^3*c - a*b^2*d)^(1/3)*(b*c - a*d) + (b^2*c - a*b*d)*(d*x + c)^(1/3) - 2*(b^3*c - a*b^2*d)^(2/3)*(d*x + c)^(2/3))*sqrt(-(b^3*c - a*b^2*d)^(1/3)/(b*c - a*d)) - 3*(b^3*c - a*b^2*d)^(2/3)*(d*x + c)^(1/3))/(b*x + a) - (b^3*c - a*b^2*d)^(2/3)*log((d*x + c)^(2/3)*b^2 + (b^3*c - a*b^2*d)^(1/3)*(d*x + c)^(1/3)*b + (b^3*c - a*b^2*d)^(2/3)) + 2*(b^3*c - a*b^2*d)^(2/3)*log((d*x + c)^(1/3)*b - (b^3*c - a*b^2*d)^(1/3)))/(b^3*c - a*b^2*d), 1/2*(2*sqrt(3)*(b^2*c - a*b*d)*sqrt((b^3*c - a*b^2*d)^(1/3)/(b*c - a*d))*arctan(1/3*sqrt(3)*(2*(d*x + c)^(1/3)*b + (b^3*c - a*b^2*d)^(1/3))*sqrt((b^3*c - a*b^2*d)^(1/3)/(b*c - a*d))/b - (b^3*c - a*b^2*d)^(2/3)*log((d*x + c)^(2/3)*b^2 + (b^3*c - a*b^2*d)^(1/3)*(d*x + c)^(1/3)*b + (b^3*c - a*b^2*d)^(2/3)) + 2*(b^3*c - a*b^2*d)^(2/3)*log((d*x + c)^(1/3)*b - (b^3*c - a*b^2*d)^(1/3)))/(b^3*c - a*b^2*d)]

giac [A] time = 1.10, size = 196, normalized size = 1.41

$$\frac{3(b^3c - ab^2d)^{\frac{2}{3}} \arctan \left(\frac{\sqrt{3} \left(2(dx+c)^{\frac{1}{3}} + \left(\frac{bc-ad}{b} \right)^{\frac{1}{3}} \right)}{3 \left(\frac{bc-ad}{b} \right)^{\frac{1}{3}}} \right)}{\sqrt{3}b^3c - \sqrt{3}ab^2d} \log \left((dx+c)^{\frac{2}{3}} + (dx+c)^{\frac{1}{3}} \left(\frac{bc-ad}{b} \right)^{\frac{1}{3}} + \left(\frac{bc-ad}{b} \right)^{\frac{2}{3}} \right) \left(\frac{bc-ad}{b} \right)^{\frac{2}{3}} \log \left(\dots \right)}{2(b^3c - ab^2d)^{\frac{1}{3}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] 3*(b^3*c - a*b^2*d)^(2/3)*arctan(1/3*sqrt(3)*(2*(d*x + c)^(1/3) + ((b*c - a*d)/b)^(1/3)))/((b*c - a*d)/b)^(1/3)/(sqrt(3)*b^3*c - sqrt(3)*a*b^2*d) - 1/

$2 \cdot \log((d \cdot x + c)^{2/3} + (d \cdot x + c)^{1/3} \cdot ((b \cdot c - a \cdot d)/b)^{1/3} + ((b \cdot c - a \cdot d)/b)^{2/3}) / (b^3 \cdot c - a \cdot b^2 \cdot d)^{1/3} + ((b \cdot c - a \cdot d)/b)^{2/3} \cdot \log(\text{abs}((d \cdot x + c)^{1/3} - ((b \cdot c - a \cdot d)/b)^{1/3})) / (b \cdot c - a \cdot d)$

maple [A] time = 0.01, size = 161, normalized size = 1.16

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3} \left(\frac{2(dx+c)^{\frac{1}{3}}-1}{\left(\frac{ad-bc}{b}\right)^{\frac{1}{3}}}\right)}{3}\right)}{\left(\frac{ad-bc}{b}\right)^{\frac{1}{3}} b} \ln\left((dx+c)^{\frac{1}{3}} + \left(\frac{ad-bc}{b}\right)^{\frac{1}{3}}\right) \ln\left((dx+c)^{\frac{2}{3}} - \left(\frac{ad-bc}{b}\right)^{\frac{1}{3}} (dx+c)^{\frac{1}{3}} + \left(\frac{ad-bc}{b}\right)^{\frac{2}{3}}\right)}{\left(\frac{ad-bc}{b}\right)^{\frac{1}{3}} b + 2 \left(\frac{ad-bc}{b}\right)^{\frac{1}{3}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)/(d*x+c)^(1/3),x)`

[Out] $-1/b / ((a \cdot d - b \cdot c)/b)^{1/3} \cdot \ln((d \cdot x + c)^{1/3} + ((a \cdot d - b \cdot c)/b)^{1/3}) + 1/2/b / ((a \cdot d - b \cdot c)/b)^{1/3} \cdot \ln((d \cdot x + c)^{2/3} - ((a \cdot d - b \cdot c)/b)^{1/3} \cdot (d \cdot x + c)^{1/3} + ((a \cdot d - b \cdot c)/b)^{2/3}) + 3^{1/2}/b / ((a \cdot d - b \cdot c)/b)^{1/3} \cdot \arctan(1/3 \cdot 3^{1/2} \cdot (2 / ((a \cdot d - b \cdot c)/b)^{1/3} \cdot (d \cdot x + c)^{1/3} - 1))$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)/(d*x+c)^(1/3),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c positive or negative?

mupad [B] time = 0.21, size = 204, normalized size = 1.47

$$\frac{\ln\left(9b(c+dx)^{1/3} - \frac{9b^3c-9ab^2d}{b^{4/3}(bc-ad)^{2/3}}\right)}{b^{2/3}(bc-ad)^{1/3}} + \frac{\ln\left(9b(c+dx)^{1/3} - \frac{(-1+\sqrt{3}i)^2(9b^3c-9ab^2d)}{4b^{4/3}(bc-ad)^{2/3}}\right)(-1+\sqrt{3}i)}{2b^{2/3}(bc-ad)^{1/3}} - \frac{\ln\left(9b(c+dx)^{1/3} - \frac{(-1-\sqrt{3}i)^2(9b^3c-9ab^2d)}{4b^{4/3}(bc-ad)^{2/3}}\right)(-1-\sqrt{3}i)}{2b^{2/3}(bc-ad)^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a+b*x)*(c+d*x)^(1/3)),x)`

```
[Out] log(9*b*(c + d*x)^(1/3) - (9*b^3*c - 9*a*b^2*d)/(b^(4/3)*(b*c - a*d)^(2/3))
)/(b^(2/3)*(b*c - a*d)^(1/3)) + (log(9*b*(c + d*x)^(1/3) - ((3^(1/2)*1i - 1)
)^2*(9*b^3*c - 9*a*b^2*d))/(4*b^(4/3)*(b*c - a*d)^(2/3)))*(3^(1/2)*1i - 1)
/(2*b^(2/3)*(b*c - a*d)^(1/3)) - (log(9*b*(c + d*x)^(1/3) - ((3^(1/2)*1i +
1)^2*(9*b^3*c - 9*a*b^2*d))/(4*b^(4/3)*(b*c - a*d)^(2/3)))*(3^(1/2)*1i + 1)
)/(2*b^(2/3)*(b*c - a*d)^(1/3))
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)\sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)/(d*x+c)**(1/3), x)
```

```
[Out] Integral(1/((a + b*x)*(c + d*x)**(1/3)), x)
```


$$3.1459 \quad \int \frac{1}{(a+bx)(c+dx)^{2/3}} dx$$

Optimal. Leaf size=140

$$-\frac{\log(a+bx)}{2\sqrt[3]{b}(bc-ad)^{2/3}} + \frac{3\log(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx})}{2\sqrt[3]{b}(bc-ad)^{2/3}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}+1}{\sqrt[3]{bc-ad}}\right)}{\sqrt[3]{b}(bc-ad)^{2/3}}$$

[Out] $-1/2*\ln(b*x+a)/b^{(1/3)/(-a*d+b*c)^{(2/3)}+3/2*\ln((-a*d+b*c)^{(1/3)-b^{(1/3)}*(d*x+c)^{(1/3)})/b^{(1/3)/(-a*d+b*c)^{(2/3)}-\arctan(1/3*(1+2*b^{(1/3)}*(d*x+c)^{(1/3)/(-a*d+b*c)^{(1/3)})*3^{(1/2)})*3^{(1/2)}/b^{(1/3)/(-a*d+b*c)^{(2/3)}$

Rubi [A] time = 0.07, antiderivative size = 140, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {57, 617, 204, 31}

$$-\frac{\log(a+bx)}{2\sqrt[3]{b}(bc-ad)^{2/3}} + \frac{3\log(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx})}{2\sqrt[3]{b}(bc-ad)^{2/3}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}+1}{\sqrt[3]{bc-ad}}\right)}{\sqrt[3]{b}(bc-ad)^{2/3}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)*(c + d*x)^(2/3)), x]

[Out] $-((\text{Sqrt}[3]*\text{ArcTan}[(1 + (2*b^{(1/3)}*(c + d*x)^{(1/3)})/(b*c - a*d)^{(1/3)})]/\text{Sqrt}[3]))/(b^{(1/3)}*(b*c - a*d)^{(2/3)}) - \text{Log}[a + b*x]/(2*b^{(1/3)}*(b*c - a*d)^{(2/3)}) + (3*\text{Log}[(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})/(2*b^{(1/3)}*(b*c - a*d)^{(2/3)})$

Rule 31

Int[((a_) + (b_)*(x_))^(n-1), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rule 57

Int[1/(((a_) + (b_)*(x_))*((c_) + (d_)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[(b*c - a*d)/b, 3]}, -Simp[Log[RemoveContent[a + b*x, x]]/(2*b*q^2), x] + (-Dist[3/(2*b*q), Subst[Int[1/(q^2 + q*x + x^2), x], x, (c + d*x)^(1/3)], x] - Dist[3/(2*b*q^2), Subst[Int[1/(q - x), x], x, (c + d*x)^(1/3)], x]) /; FreeQ[{a, b, c, d}, x] && PosQ[(b*c - a*d)/b]

Rule 204

`Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])`

Rule 617

`Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]`

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)(c+dx)^{2/3}} dx &= -\frac{\log(a+bx)}{2\sqrt[3]{b}(bc-ad)^{2/3}} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{\frac{\sqrt[3]{bc-ad}}{\sqrt[3]{b}} - x} dx, x, \sqrt[3]{c+dx}\right)}{2\sqrt[3]{b}(bc-ad)^{2/3}} - \frac{3 \operatorname{Subst}\left(\int \frac{1}{\frac{(bc-ad)^{2/3}}{b^{2/3}} + \frac{\sqrt[3]{bc-ad}}{\sqrt[3]{b}}} dx, x, \sqrt[3]{c+dx}\right)}{2b^{2/3}\sqrt[3]{bc}} \\ &= -\frac{\log(a+bx)}{2\sqrt[3]{b}(bc-ad)^{2/3}} + \frac{3 \log\left(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}\right)}{2\sqrt[3]{b}(bc-ad)^{2/3}} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{-3-x^2} dx, x, 1 + \frac{2c}{b}x\right)}{\sqrt[3]{b}(bc-ad)^{2/3}} \\ &= -\frac{\sqrt{3} \tan^{-1}\left(\frac{1 + \frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}}}{\sqrt{3}}\right)}{\sqrt[3]{b}(bc-ad)^{2/3}} - \frac{\log(a+bx)}{2\sqrt[3]{b}(bc-ad)^{2/3}} + \frac{3 \log\left(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}\right)}{2\sqrt[3]{b}(bc-ad)^{2/3}} \end{aligned}$$

Mathematica [A] time = 0.07, size = 154, normalized size = 1.10

$$\frac{\log\left(\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}\right) - 2 \log\left(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}\right) + 2\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} + \sqrt{3}}\right)}{2\sqrt[3]{b}(bc-ad)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)*(c + d*x)^(2/3)), x]

[Out] -1/2*(2*Sqrt[3]*ArcTan[(1 + (2*b^(1/3)*(c + d*x)^(1/3))/(b*c - a*d)^(1/3))/Sqrt[3]] - 2*Log[(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)] + Log[(b*c -

$$\frac{a*d^{2/3} + b^{1/3}*(b*c - a*d)^{1/3}*(c + d*x)^{1/3} + b^{2/3}*(c + d*x)^{2/3}}{b^{1/3}*(b*c - a*d)^{2/3}}$$

fricas [B] time = 0.50, size = 900, normalized size = 6.43

$$\frac{\sqrt{3}(b^2c - abd)\sqrt{-\frac{(b^3c^2 - 2ab^2cd + a^2bd^2)^{\frac{1}{3}}}{b}} \log\left(\frac{3b^2c^2 - 4abcd + a^2d^2 + 2(b^2cd - abd^2)x + \sqrt{3}\left(2(b^2c - abd)(dx+c)^{\frac{2}{3}} - (b^3c^2 - 2ab^2cd + a^2bd^2)^{\frac{1}{3}}\right)}{2(b^2c - abd)(dx+c)^{\frac{2}{3}} - (b^3c^2 - 2ab^2cd + a^2bd^2)^{\frac{1}{3}}}\right)}{b^{1/3}*(b*c - a*d)^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(2/3),x, algorithm="fricas")

[Out]
$$\begin{aligned} & [-1/2*(\sqrt{3}*(b^2*c - a*b*d)*\sqrt{-(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)}^{1/3}/b)*\log(-(3*b^2*c^2 - 4*a*b*c*d + a^2*d^2 + 2*(b^2*c*d - a*b*d^2)*x + \sqrt{3}*(2*(b^2*c - a*b*d)*(d*x + c)^{2/3} - (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{1/3})*(b*c - a*d) - (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{2/3}*(d*x + c)^{1/3}))*\sqrt{-(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)}^{1/3}/b - 3*(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{1/3}*(b*c - a*d)*(d*x + c)^{1/3})/(b*x + a) + (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{2/3}*\log(-(b^2*c - a*b*d)*(d*x + c)^{2/3} - (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{1/3}*(b*c - a*d) - (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{2/3}*(d*x + c)^{1/3}) - 2*(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{2/3}*\log(-(b^2*c - a*b*d)*(d*x + c)^{1/3} + (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{2/3}))/ (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2), -1/2*(2*\sqrt{3}*(b^2*c - a*b*d)*\sqrt{(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)}^{1/3}/b)*\arctan(1/3*\sqrt{3}*((b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{1/3}*(b*c - a*d) + 2*(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{2/3}*(d*x + c)^{1/3}))*\sqrt{(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)}^{1/3}/b)/(b^2*c^2 - 2*a*b*c*d + a^2*d^2) + (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{2/3}*\log(-(b^2*c - a*b*d)*(d*x + c)^{2/3} - (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{1/3}*(b*c - a*d) - (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{2/3}*(d*x + c)^{1/3}) - 2*(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{2/3}*\log(-(b^2*c - a*b*d)*(d*x + c)^{1/3} + (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)^{2/3}))/ (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)] \end{aligned}$$

giac [A] time = 0.96, size = 207, normalized size = 1.48

$$\frac{3(b^3c - ab^2d)^{\frac{1}{3}} \arctan\left(\frac{\sqrt{3}\left(2(dx+c)^{\frac{1}{3}} + \left(\frac{bc-ad}{b}\right)^{\frac{1}{3}}\right)}{3\left(\frac{bc-ad}{b}\right)^{\frac{1}{3}}}\right)}{\sqrt{3}b^2c - \sqrt{3}abd} + \frac{(b^3c - ab^2d)^{\frac{1}{3}} \log\left((dx+c)^{\frac{2}{3}} + (dx+c)^{\frac{1}{3}}\left(\frac{bc-ad}{b}\right)^{\frac{1}{3}} + \left(\frac{bc-ad}{b}\right)^{\frac{2}{3}}\right)}{2(b^2c - abd)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] $-3*(b^3*c - a*b^2*d)^{(1/3)}*\arctan(1/3*\sqrt{3}*(2*(d*x + c)^{(1/3)} + ((b*c - a*d)/b)^{(1/3)})/((b*c - a*d)/b)^{(1/3)}/(\sqrt{3}*b^2*c - \sqrt{3}*a*b*d) - 1/2*(b^3*c - a*b^2*d)^{(1/3)}*\log((d*x + c)^{(2/3)} + (d*x + c)^{(1/3)}*((b*c - a*d)/b)^{(1/3)} + ((b*c - a*d)/b)^{(2/3)})/(b^2*c - a*b*d) + ((b*c - a*d)/b)^{(1/3)}*\log(\text{abs}((d*x + c)^{(1/3)} - ((b*c - a*d)/b)^{(1/3)})/(b*c - a*d)$

maple [A] time = 0.01, size = 160, normalized size = 1.14

$$\frac{\sqrt{3} \arctan\left(\frac{\sqrt{3}\left(2(dx+c)^{\frac{1}{3}} - 1\right)}{\left(\frac{ad-bc}{b}\right)^{\frac{1}{3}}}\right)}{\left(\frac{ad-bc}{b}\right)^{\frac{2}{3}} b} + \frac{\ln\left((dx+c)^{\frac{1}{3}} + \left(\frac{ad-bc}{b}\right)^{\frac{1}{3}}\right)}{\left(\frac{ad-bc}{b}\right)^{\frac{2}{3}} b} - \frac{\ln\left((dx+c)^{\frac{2}{3}} - \left(\frac{ad-bc}{b}\right)^{\frac{1}{3}}(dx+c)^{\frac{1}{3}} + \left(\frac{ad-bc}{b}\right)^{\frac{2}{3}}\right)}{2\left(\frac{ad-bc}{b}\right)^{\frac{2}{3}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)/(d*x+c)^(2/3),x)

[Out] $1/b/((a*d-b*c)/b)^{(2/3)}*\ln((d*x+c)^{(1/3)}+((a*d-b*c)/b)^{(1/3)})-1/2/b/((a*d-b*c)/b)^{(2/3)}*\ln((d*x+c)^{(2/3)}-((a*d-b*c)/b)^{(1/3)}*(d*x+c)^{(1/3)}+((a*d-b*c)/b)^{(2/3)})+1/b/((a*d-b*c)/b)^{(2/3)}*3^{(1/2)}*\arctan(1/3*3^{(1/2)}*(2/((a*d-b*c)/b)^{(1/3)}*(d*x+c)^{(1/3)}-1))$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c positive or negative?

mupad [B] time = 0.37, size = 206, normalized size = 1.47

$$\frac{\ln\left(9b^2(c+dx)^{1/3} - \frac{9b^3c-9ab^2d}{b^{1/3}(ad-bc)^{2/3}}\right)}{b^{1/3}(ad-bc)^{2/3}} + \frac{\ln\left(9b^2(c+dx)^{1/3} - \frac{(-1+\sqrt{3}i)(9b^3c-9ab^2d)}{2b^{1/3}(ad-bc)^{2/3}}\right)}{2b^{1/3}(ad-bc)^{2/3}} - \frac{(-1+\sqrt{3}i)\ln\left(9b^2(c+dx)^{1/3} - \frac{9b^3c-9ab^2d}{b^{1/3}(ad-bc)^{2/3}}\right)}{2b^{1/3}(ad-bc)^{2/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)*(c + d*x)^(2/3)), x)

[Out] $\log(9b^2(c+dx)^{1/3} - (9b^3c - 9ab^2d)/(b^{1/3}(ad-bc)^{2/3}))/b^{1/3}(ad-bc)^{2/3} + (\log(9b^2(c+dx)^{1/3} - ((3^{1/2})i - 1)(9b^3c - 9ab^2d)/(2b^{1/3}(ad-bc)^{2/3}))) * (3^{1/2})i - 1) / (2b^{1/3}(ad-bc)^{2/3}) - (\log(9b^2(c+dx)^{1/3} + ((3^{1/2})i + 1)(9b^3c - 9ab^2d)/(2b^{1/3}(ad-bc)^{2/3}))) * (3^{1/2})i + 1) / (2b^{1/3}(ad-bc)^{2/3})$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)/(d*x+c)**(2/3), x)

[Out] Integral(1/((a + b*x)*(c + d*x)**(2/3)), x)

3.1460 $\int (a + bx)^{7/2} \sqrt{c + dx} dx$

Optimal. Leaf size=230

$$\frac{7(bc - ad)^5 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{128b^{3/2}d^{9/2}} - \frac{7\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^4}{128bd^4} + \frac{7(a+bx)^{3/2}\sqrt{c+dx}(bc - ad)^3}{192bd^3} - \frac{7(a+bx)^{5/2}\sqrt{c+dx}}{240bd^2}$$

[Out] $7/128*(-a*d+b*c)^5*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(3/2)}/d^{(9/2)}+7/192*(-a*d+b*c)^3*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/b/d^3-7/240*(-a*d+b*c)^2*(b*x+a)^{(5/2)}*(d*x+c)^{(1/2)}/b/d^2+1/40*(-a*d+b*c)*(b*x+a)^{(7/2)}*(d*x+c)^{(1/2)}/b/d+1/5*(b*x+a)^{(9/2)}*(d*x+c)^{(1/2)}/b-7/128*(-a*d+b*c)^4*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b/d^4$

Rubi [A] time = 0.16, antiderivative size = 230, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$\frac{7(bc - ad)^5 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{128b^{3/2}d^{9/2}} - \frac{7\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^4}{128bd^4} + \frac{7(a+bx)^{3/2}\sqrt{c+dx}(bc - ad)^3}{192bd^3} - \frac{7(a+bx)^{5/2}\sqrt{c+dx}}{240bd^2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(7/2)}*\operatorname{Sqrt}[c + d*x], x]$

[Out] $(-7*(b*c - a*d)^4*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(128*b*d^4) + (7*(b*c - a*d)^3*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(192*b*d^3) - (7*(b*c - a*d)^2*(a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x])/(240*b*d^2) + ((b*c - a*d)*(a + b*x)^{(7/2)}*\operatorname{Sqrt}[c + d*x])/(40*b*d) + ((a + b*x)^{(9/2)}*\operatorname{Sqrt}[c + d*x])/(5*b) + (7*(b*c - a*d)^5*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/(128*b^{(3/2)}*d^{(9/2)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{With}[p = \operatorname{Denominator}[m]], \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b +$

$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 206

$\text{Int}[(a_ + (b_)*(x_)^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(1*\text{ArcTanh}[\text{Rt}[-b, 2]*x]/\text{Rt}[a, 2])]/(\text{Rt}[a, 2]*\text{Rt}[-b, 2]), x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{NegQ}[a/b] \&\& (\text{GtQ}[a, 0] \parallel \text{LtQ}[b, 0])$

Rule 217

$\text{Int}[1/\text{Sqrt}[a_ + (b_)*(x_)^2], x_Symbol] \rightarrow \text{Subst}[\text{Int}[1/(1 - b*x^2), x], x, x/\text{Sqrt}[a + b*x^2]] /; \text{FreeQ}\{a, b\}, x] \&\& !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
 \int (a + bx)^{7/2} \sqrt{c + dx} \, dx &= \frac{(a + bx)^{9/2} \sqrt{c + dx}}{5b} + \frac{(bc - ad) \int \frac{(a+bx)^{7/2}}{\sqrt{c+dx}} \, dx}{10b} \\
 &= \frac{(bc - ad)(a + bx)^{7/2} \sqrt{c + dx}}{40bd} + \frac{(a + bx)^{9/2} \sqrt{c + dx}}{5b} - \frac{(7(bc - ad)^2) \int \frac{(a+bx)^{5/2}}{\sqrt{c+dx}} \, dx}{80bd} \\
 &= -\frac{7(bc - ad)^2 (a + bx)^{5/2} \sqrt{c + dx}}{240bd^2} + \frac{(bc - ad)(a + bx)^{7/2} \sqrt{c + dx}}{40bd} + \frac{(a + bx)^{9/2} \sqrt{c + dx}}{5b} \\
 &= \frac{7(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{192bd^3} - \frac{7(bc - ad)^2 (a + bx)^{5/2} \sqrt{c + dx}}{240bd^2} + \frac{(bc - ad)(a + bx)^{7/2} \sqrt{c + dx}}{40bd} \\
 &= -\frac{7(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128bd^4} + \frac{7(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{192bd^3} - \frac{7(bc - ad)^2 (a + bx)^{5/2} \sqrt{c + dx}}{240bd^2} \\
 &= -\frac{7(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128bd^4} + \frac{7(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{192bd^3} - \frac{7(bc - ad)^2 (a + bx)^{5/2} \sqrt{c + dx}}{240bd^2} \\
 &= -\frac{7(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128bd^4} + \frac{7(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{192bd^3} - \frac{7(bc - ad)^2 (a + bx)^{5/2} \sqrt{c + dx}}{240bd^2} \\
 &= -\frac{7(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128bd^4} + \frac{7(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{192bd^3} - \frac{7(bc - ad)^2 (a + bx)^{5/2} \sqrt{c + dx}}{240bd^2}
 \end{aligned}$$

Mathematica [A] time = 1.47, size = 194, normalized size = 0.84

$$\frac{(a + bx)^{9/2} \sqrt{c + dx} \left(\frac{70(bc-ad)^{9/2} \sinh^{-1} \left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{bc-ad}} \right)}{d^{9/2} (a+bx)^{9/2} \sqrt{\frac{b(c+dx)}{bc-ad}}} - \frac{70(bc-ad)^4}{d^4 (a+bx)^4} + \frac{140(bc-ad)^3}{3d^3 (a+bx)^3} - \frac{112(bc-ad)^2}{3d^2 (a+bx)^2} + \frac{32bc-32ad}{ad+bdx} + 256 \right)}{1280b}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/2)*Sqrt[c + d*x], x]

[Out] ((a + b*x)^(9/2)*Sqrt[c + d*x]*(256 - (70*(b*c - a*d)^4)/(d^4*(a + b*x)^4) + (140*(b*c - a*d)^3)/(3*d^3*(a + b*x)^3) - (112*(b*c - a*d)^2)/(3*d^2*(a + b*x)^2) + (32*b*c - 32*a*d)/(a*d + b*d*x) + (70*(b*c - a*d)^(9/2)*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(d^(9/2)*(a + b*x)^(9/2)*Sqrt[(b*c + d*x)/(b*c - a*d)])))/(1280*b)

fricas [A] time = 0.51, size = 702, normalized size = 3.05

$$\frac{105(b^5c^5 - 5ab^4c^4d + 10a^2b^3c^3d^2 - 10a^3b^2c^2d^3 + 5a^4bcd^4 - a^5d^5)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 - \dots)}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)*(d*x+c)^(1/2), x, algorithm="fricas")

[Out] [-1/7680*(105*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 - 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(384*b^5*d^5*x^4 - 105*b^5*c^4*d + 490*a*b^4*c^3*d^2 - 896*a^2*b^3*c^2*d^3 + 790*a^3*b^2*c*d^4 + 105*a^4*b*d^5 + 48*(b^5*c*d^4 + 31*a*b^4*d^5)*x^3 - 8*(7*b^5*c^2*d^3 - 32*a*b^4*c*d^4 - 263*a^2*b^3*d^5)*x^2 + 2*(35*b^5*c^3*d^2 - 161*a*b^4*c^2*d^3 + 289*a^2*b^3*c*d^4 + 605*a^3*b^2*d^5)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*d^5), -1/3840*(105*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x) - 2*(384*b^5*d^5*x^4 - 105*b^5*c^4*d + 490*a*b^4*c^3*d^2 - 896*a^2*b^3*c^2*d^3 + 790*a^3*b^2*c*d^4 + 105*a^4*b*d^5 + 48*(b^5*c*d^4 + 31*a*b^4*d^5)*x^3 - 8*(7*b^5*c^2*d^3 - 32*a*b^4*c*d^4 - 263*a^2*b^3*d^5)*x^2 + 2*(35*b^5*c^3*d^2 - 161*a*b^4*c^2*d^3 + 289*a^2*b^3*c*d^4 + 605*a^3*b^2*d^5)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*d^5)]

giac [B] time = 1.84, size = 1107, normalized size = 4.81

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)*(d*x+c)^(1/2),x, algorithm="giac")

[Out] $\frac{1}{1920} \cdot (480 \cdot (\sqrt{b^2c + (bx+a)bd} - abd) \sqrt{bx+a} (2(bx+a) \cdot (4(bx+a)/b^2 + (b^6cd^3 - 13a^2b^5d^4)/(b^7d^4)) - 3(b^7c^2d^2 + 2ab^6cd^3 - 11a^2b^5d^4)/(b^7d^4)) - 3(b^3c^3 + ab^2c^2d + 3a^2b^2cd^2 - 5a^3d^3) \log(\text{abs}(-\sqrt{bd})\sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd} \cdot b^2) \cdot a^2 \cdot \text{abs}(b) - 1920 \cdot ((b^2c - abd) \log(\text{abs}(-\sqrt{bd})\sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / \sqrt{bd} - \sqrt{b^2c + (bx+a)bd} \sqrt{bx+a}) \cdot a^4 \cdot \text{abs}(b) / b^2 + 40 \cdot (\sqrt{b^2c + (bx+a)bd} \cdot (2(bx+a) \cdot (4(bx+a) \cdot (6(bx+a)/b^3 + (b^{12}cd^5 - 25a^2b^{11}d^6)/(b^{14}d^6)) - (5b^{13}c^2d^4 + 14a^2b^{12}cd^5 - 163a^2b^{11}d^6)/(b^{14}d^6)) + 3(5b^{14}c^3d^3 + 9a^2b^{13}c^2d^4 + 15a^2b^{12}cd^5 - 93a^3b^{11}d^6)/(b^{14}d^6)) \sqrt{bx+a} + 3(5b^4c^4 + 4a^2b^3c^3d + 6a^2b^2c^2d^2 + 20a^3b^2cd^3 - 35a^4d^4) \log(\text{abs}(-\sqrt{bd})\sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd} \cdot b^2d^3) \cdot a \cdot b \cdot \text{abs}(b) + (\sqrt{b^2c + (bx+a)bd} - abd) \cdot (2(4(bx+a) \cdot (6(bx+a) \cdot (8(bx+a)/b^4 + (b^{20}cd^7 - 41a^2b^{19}d^8)/(b^{23}d^8)) - (7b^{21}c^2d^6 + 26a^2b^{20}cd^7 - 513a^2b^{19}d^8)/(b^{23}d^8)) + 5(7b^{22}c^3d^5 + 19a^2b^{21}c^2d^6 + 37a^2b^{20}cd^7 - 447a^3b^{19}d^8)/(b^{23}d^8)) \cdot (bx+a) - 15(7b^{23}c^4d^4 + 12a^2b^{22}c^3d^5 + 18a^2b^{21}c^2d^6 + 28a^3b^{20}cd^7 - 193a^4b^{19}d^8)/(b^{23}d^8)) \sqrt{bx+a} - 15(7b^5c^5 + 5a^2b^4c^4d + 6a^2b^3c^3d^2 + 10a^3b^2c^2d^3 + 35a^4b^2cd^4 - 63a^5d^5) \log(\text{abs}(-\sqrt{bd})\sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd} \cdot b^3d^4) \cdot b^2 \cdot \text{abs}(b) + 1920 \cdot (\sqrt{b^2c + (bx+a)bd} \cdot (2bx + 2a + (bcd - 5ad^2)/d^2) \sqrt{bx+a} + (b^3c^2 + 2a^2b^2cd - 3a^2b^2d^2) \log(\text{abs}(-\sqrt{bd})\sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd} \cdot d)) \cdot a^3 \cdot \text{abs}(b) / b^2) / b$

maple [B] time = 0.01, size = 858, normalized size = 3.73

$$\frac{7\sqrt{(bx+a)(dx+c)} a^5 d \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad+bc)x}\right)}{256\sqrt{dx+c} \sqrt{bx+a} \sqrt{bd} b} + \frac{35\sqrt{(bx+a)(dx+c)} a^4 c \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}}\right)}{256\sqrt{dx+c} \sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/2)*(d*x+c)^(1/2),x)

[Out] $\frac{1}{5}d \cdot (bx+a)^{7/2} \cdot (d*x+c)^{3/2} + \frac{7}{40}d \cdot (bx+a)^{5/2} \cdot (d*x+c)^{3/2} \cdot a + \frac{7}{48}d \cdot (bx+a)^{3/2} \cdot (d*x+c)^{3/2} \cdot a^2 + \frac{7}{64}d \cdot (bx+a)^{1/2} \cdot (d*x+c)^{3/2} \cdot a^3 + \frac{21}{64}d^2 \cdot (bx+a)^{1/2} \cdot (d*x+c)^{3/2} \cdot a^2 \cdot b + \frac{21}{64}d^2 \cdot (bx+a)^{1/2} \cdot (d*x+c)^{3/2} \cdot a \cdot b^2 + \frac{7}{32}d^3 \cdot (bx+a)^{1/2} \cdot (d*x+c)^{3/2} \cdot a^2 \cdot b^2 + \frac{7}{24}d^3 \cdot (bx+a)^{1/2} \cdot (d*x+c)^{3/2} \cdot a \cdot b^3 + \frac{7}{24}d^3 \cdot (bx+a)^{1/2} \cdot (d*x+c)^{3/2} \cdot a^2 \cdot b^3$

```

a*b*c-7/40/d^2*(b*x+a)^(5/2)*(d*x+c)^(3/2)*b*c+7/48/d^3*(b*x+a)^(3/2)*(d*x+
c)^(3/2)*b^2*c^2-7/64/d^4*(b*x+a)^(1/2)*(d*x+c)^(3/2)*b^3*c^3+7/128/b*(d*x+
c)^(1/2)*(b*x+a)^(1/2)*a^4-7/32/d*(d*x+c)^(1/2)*(b*x+a)^(1/2)*a^3*c+7/128/d
^4*(d*x+c)^(1/2)*(b*x+a)^(1/2)*c^4*b^3+35/256*((b*x+a)*(d*x+c))^(1/2)/(d*x+
c)^(1/2)/(b*x+a)^(1/2)*ln((1/2*a*d+1/2*b*c+b*d*x)/(b*d)^(1/2)+(d*x^2*b+(a*d
+b*c)*x+a*c)^(1/2))/(b*d)^(1/2)*a^4*c+35/128/d^2*((b*x+a)*(d*x+c))^(1/2)/(d
*x+c)^(1/2)/(b*x+a)^(1/2)*ln((1/2*a*d+1/2*b*c+b*d*x)/(b*d)^(1/2)+(d*x^2*b+(
a*d+b*c)*x+a*c)^(1/2))/(b*d)^(1/2)*a^2*c^3*b^2-35/256/d^3*((b*x+a)*(d*x+c))
^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((1/2*a*d+1/2*b*c+b*d*x)/(b*d)^(1/2)+(
d*x^2*b+(a*d+b*c)*x+a*c)^(1/2))/(b*d)^(1/2)*a*c^4*b^3-7/256*d/b*((b*x+a)*(d
*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((1/2*a*d+1/2*b*c+b*d*x)/(b*d)^(
1/2)+(d*x^2*b+(a*d+b*c)*x+a*c)^(1/2))/(b*d)^(1/2)*a^5-35/128/d*((b*x+a)*(d*
x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((1/2*a*d+1/2*b*c+b*d*x)/(b*d)^(1
/2)+(d*x^2*b+(a*d+b*c)*x+a*c)^(1/2))/(b*d)^(1/2)*a^3*c^2*b+7/256/d^4*((b*x+
a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((1/2*a*d+1/2*b*c+b*d*x)/(b
*d)^(1/2)+(d*x^2*b+(a*d+b*c)*x+a*c)^(1/2))/(b*d)^(1/2)*c^5*b^4

```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)*(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{7/2} \sqrt{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/2)*(c + d*x)^(1/2),x)

[Out] int((a + b*x)^(7/2)*(c + d*x)^(1/2), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/2)*(d*x+c)**(1/2),x)

[Out] Timed out

3.1461 $\int (a + bx)^{5/2} \sqrt{c + dx} dx$

Optimal. Leaf size=192

$$\frac{5(bc - ad)^4 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{64b^{3/2}d^{7/2}} + \frac{5\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^3}{64bd^3} - \frac{5(a+bx)^{3/2}\sqrt{c+dx}(bc - ad)^2}{96bd^2} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{24b^2}$$

[Out] $-5/64*(-a*d+b*c)^4*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(3/2)}/d^{(7/2)}-5/96*(-a*d+b*c)^2*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/b/d^2+1/24*(-a*d+b*c)*(b*x+a)^{(5/2)}*(d*x+c)^{(1/2)}/b/d+1/4*(b*x+a)^{(7/2)}*(d*x+c)^{(1/2)}/b+5/64*(-a*d+b*c)^3*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b/d^3$

Rubi [A] time = 0.09, antiderivative size = 192, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$\frac{5(bc - ad)^4 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{64b^{3/2}d^{7/2}} + \frac{5\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^3}{64bd^3} - \frac{5(a+bx)^{3/2}\sqrt{c+dx}(bc - ad)^2}{96bd^2} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{24b^2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x], x]$

[Out] $(5*(b*c - a*d)^3*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(64*b*d^3) - (5*(b*c - a*d)^2*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(96*b*d^2) + ((b*c - a*d)*(a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x])/(24*b*d) + ((a + b*x)^{(7/2)}*\operatorname{Sqrt}[c + d*x])/(4*b) - (5*(b*c - a*d)^4*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/(64*b^{(3/2)}*d^{(7/2)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{GtQ}[n, 0] \ \&\& \operatorname{NeQ}[m + n + 1, 0] \ \&\& \operatorname{!(IGtQ}[m, 0] \ \&\& (\operatorname{!IntegerQ}[n] \ \|\ (\operatorname{GtQ}[m, 0] \ \&\& \operatorname{LtQ}[m - n, 0]))) \ \&\& \operatorname{!ILtQ}[m + n + 2, 0] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{LtQ}[-1, m, 0] \ \&\& \operatorname{LeQ}[-1, n, 0] \ \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Den}$

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int (a+bx)^{5/2} \sqrt{c+dx} \, dx &= \frac{(a+bx)^{7/2} \sqrt{c+dx}}{4b} + \frac{(bc-ad) \int \frac{(a+bx)^{5/2}}{\sqrt{c+dx}} \, dx}{8b} \\
 &= \frac{(bc-ad)(a+bx)^{5/2} \sqrt{c+dx}}{24bd} + \frac{(a+bx)^{7/2} \sqrt{c+dx}}{4b} - \frac{(5(bc-ad)^2) \int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} \, dx}{48bd} \\
 &= -\frac{5(bc-ad)^2 (a+bx)^{3/2} \sqrt{c+dx}}{96bd^2} + \frac{(bc-ad)(a+bx)^{5/2} \sqrt{c+dx}}{24bd} + \frac{(a+bx)^{7/2} \sqrt{c+dx}}{4b} \\
 &= \frac{5(bc-ad)^3 \sqrt{a+bx} \sqrt{c+dx}}{64bd^3} - \frac{5(bc-ad)^2 (a+bx)^{3/2} \sqrt{c+dx}}{96bd^2} + \frac{(bc-ad)(a+bx)^{5/2} \sqrt{c+dx}}{24bd} \\
 &= \frac{5(bc-ad)^3 \sqrt{a+bx} \sqrt{c+dx}}{64bd^3} - \frac{5(bc-ad)^2 (a+bx)^{3/2} \sqrt{c+dx}}{96bd^2} + \frac{(bc-ad)(a+bx)^{5/2} \sqrt{c+dx}}{24bd} \\
 &= \frac{5(bc-ad)^3 \sqrt{a+bx} \sqrt{c+dx}}{64bd^3} - \frac{5(bc-ad)^2 (a+bx)^{3/2} \sqrt{c+dx}}{96bd^2} + \frac{(bc-ad)(a+bx)^{5/2} \sqrt{c+dx}}{24bd} \\
 &= \frac{5(bc-ad)^3 \sqrt{a+bx} \sqrt{c+dx}}{64bd^3} - \frac{5(bc-ad)^2 (a+bx)^{3/2} \sqrt{c+dx}}{96bd^2} + \frac{(bc-ad)(a+bx)^{5/2} \sqrt{c+dx}}{24bd}
 \end{aligned}$$

Mathematica [A] time = 0.60, size = 190, normalized size = 0.99

$$\frac{b\sqrt{d}\sqrt{a+bx}(c+dx)(15a^3d^3+a^2bd^2(73c+118dx)+ab^2d(-55c^2+36cdx+136d^2x^2))+b^3(15c^3-10c^2dx+8cd^2x^2)}{192b^2d^{7/2}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)*Sqrt[c + d*x], x]

[Out] (b*Sqrt[d]*Sqrt[a + b*x]*(c + d*x)*(15*a^3*d^3 + a^2*b*d^2*(73*c + 118*d*x) + a*b^2*d*(-55*c^2 + 36*c*d*x + 136*d^2*x^2) + b^3*(15*c^3 - 10*c^2*d*x + 8*c*d^2*x^2 + 48*d^3*x^3)) - 15*(b*c - a*d)^(9/2)*Sqrt[(b*(c + d*x))/(b*c - a*d)]*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]]/(192*b^2*d^(7/2)*Sqrt[c + d*x])

fricas [A] time = 0.49, size = 540, normalized size = 2.81

$$\frac{15(b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 - 4(2bdx + bc + ad))}{192b^2d^{7/2}\sqrt{c+dx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(d*x+c)^(1/2), x, algorithm="fricas")

[Out] [1/768*(15*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 - 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x) + 4*(48*b^4*d^4*x^3 + 15*b^4*c^3*d - 55*a*b^3*c^2*d^2 + 73*a^2*b^2*c*d^3 + 15*a^3*b*d^4 + 8*(b^4*c*d^3 + 17*a*b^3*d^4)*x^2 - 2*(5*b^4*c^2*d^2 - 18*a*b^3*c*d^3 - 59*a^2*b^2*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*d^4), 1/384*(15*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)) + 2*(48*b^4*d^4*x^3 + 15*b^4*c^3*d - 55*a*b^3*c^2*d^2 + 73*a^2*b^2*c*d^3 + 15*a^3*b*d^4 + 8*(b^4*c*d^3 + 17*a*b^3*d^4)*x^2 - 2*(5*b^4*c^2*d^2 - 18*a*b^3*c*d^3 - 59*a^2*b^2*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*d^4)]

giac [B] time = 1.64, size = 726, normalized size = 3.78

$$24 \left(\sqrt{b^2c + (bx+a)bd - abd} \sqrt{bx+a} \left(2(bx+a) \left(\frac{4(bx+a)}{b^2} + \frac{b^6cd^3 - 13ab^5d^4}{b^7d^4} \right) - \frac{3(b^7c^2d^2 + 2ab^6cd^3 - 11a^2b^5d^4)}{b^7d^4} \right) - \frac{3(b^3c^3 + ab^4d^3)}{b^7d^4} \right)$$

$\frac{(d*x+c)^{(1/2)}}{(b*x+a)^{(1/2)}}*\ln\left(\frac{(b*d*x+1/2*a*d+1/2*b*c)}{(b*d)^{(1/2)}+(b*d*x^2+a*c+(a*d+b*c)*x)^{(1/2)}}\right)/(b*d)^{(1/2)}*c^4*b^3$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + b x)^{5/2} \sqrt{c + d x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)*(c + d*x)^(1/2),x)

[Out] int((a + b*x)^(5/2)*(c + d*x)^(1/2), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)*(d*x+c)**(1/2),x)

[Out] Timed out

3.1462 $\int (a + bx)^{3/2} \sqrt{c + dx} dx$

Optimal. Leaf size=154

$$\frac{(bc - ad)^3 \tanh^{-1}\left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{b} \sqrt{c+dx}}\right)}{8b^{3/2}d^{5/2}} - \frac{\sqrt{a+bx} \sqrt{c+dx} (bc - ad)^2}{8bd^2} + \frac{(a + bx)^{3/2} \sqrt{c+dx} (bc - ad)}{12bd} + \frac{(a + bx)^{5/2} \sqrt{c+dx}}{3b}$$

[Out] $1/8*(-a*d+b*c)^3*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(3/2)}/d^{(5/2)}+1/12*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/b/d+1/3*(b*x+a)^{(5/2)}*(d*x+c)^{(1/2)}/b-1/8*(-a*d+b*c)^2*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b/d^2$

Rubi [A] time = 0.07, antiderivative size = 154, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$\frac{(bc - ad)^3 \tanh^{-1}\left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{b} \sqrt{c+dx}}\right)}{8b^{3/2}d^{5/2}} - \frac{\sqrt{a+bx} \sqrt{c+dx} (bc - ad)^2}{8bd^2} + \frac{(a + bx)^{3/2} \sqrt{c+dx} (bc - ad)}{12bd} + \frac{(a + bx)^{5/2} \sqrt{c+dx}}{3b}$$

Antiderivative was successfully verified.

[In] `Int[(a + b*x)^(3/2)*Sqrt[c + d*x], x]`

[Out] $-((b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(8*b*d^2) + ((b*c - a*d)*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(12*b*d) + ((a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x])/(3*b) + ((b*c - a*d)^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/(8*b^{(3/2)}*d^{(5/2)})$

Rule 50

`Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 63

`Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int (a + bx)^{3/2} \sqrt{c + dx} \, dx &= \frac{(a + bx)^{5/2} \sqrt{c + dx}}{3b} + \frac{(bc - ad) \int \frac{(a + bx)^{3/2}}{\sqrt{c + dx}} \, dx}{6b} \\
 &= \frac{(bc - ad)(a + bx)^{3/2} \sqrt{c + dx}}{12bd} + \frac{(a + bx)^{5/2} \sqrt{c + dx}}{3b} - \frac{(bc - ad)^2 \int \frac{\sqrt{a + bx}}{\sqrt{c + dx}} \, dx}{8bd} \\
 &= -\frac{(bc - ad)^2 \sqrt{a + bx} \sqrt{c + dx}}{8bd^2} + \frac{(bc - ad)(a + bx)^{3/2} \sqrt{c + dx}}{12bd} + \frac{(a + bx)^{5/2} \sqrt{c + dx}}{3b} \\
 &= -\frac{(bc - ad)^2 \sqrt{a + bx} \sqrt{c + dx}}{8bd^2} + \frac{(bc - ad)(a + bx)^{3/2} \sqrt{c + dx}}{12bd} + \frac{(a + bx)^{5/2} \sqrt{c + dx}}{3b} \\
 &= -\frac{(bc - ad)^2 \sqrt{a + bx} \sqrt{c + dx}}{8bd^2} + \frac{(bc - ad)(a + bx)^{3/2} \sqrt{c + dx}}{12bd} + \frac{(a + bx)^{5/2} \sqrt{c + dx}}{3b} \\
 &= -\frac{(bc - ad)^2 \sqrt{a + bx} \sqrt{c + dx}}{8bd^2} + \frac{(bc - ad)(a + bx)^{3/2} \sqrt{c + dx}}{12bd} + \frac{(a + bx)^{5/2} \sqrt{c + dx}}{3b}
 \end{aligned}$$

Mathematica [A] time = 0.43, size = 151, normalized size = 0.98

$$\frac{b\sqrt{d} \sqrt{a + bx} (c + dx) (3a^2d^2 + 2abd(4c + 7dx) + b^2(-3c^2 + 2cdx + 8d^2x^2)) + 3(bc - ad)^{7/2} \sqrt{\frac{b(c+dx)}{bc-ad}} \sinh^{-1}\left(\frac{\sqrt{a+bx}}{\sqrt{c+dx}}\right)}{24b^2d^{5/2}\sqrt{c + dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)*Sqrt[c + d*x], x]

$\text{rt}(b^2c + (bx + a)bd - a^2bd)(2bx + 2a + (b^2cd - 5a^2d^2)/d^2)\sqrt{t(bx + a) + (b^3c^2 + 2ab^2cd - 3a^2bd^2)\log(\text{abs}(-\sqrt{bd})\sqrt{t(bx + a) + \sqrt{b^2c + (bx + a)bd - a^2bd}})/(\sqrt{bd}d))}a\text{abs}(b)/b^2)/b$

maple [B] time = 0.01, size = 460, normalized size = 2.99

$$\frac{\sqrt{(bx + a)(dx + c)} a^3 d \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad + bc)x}\right)}{16\sqrt{dx + c} \sqrt{bx + a} \sqrt{bd} b} + \frac{3\sqrt{(bx + a)(dx + c)} a^2 c \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}}\right)}{16\sqrt{dx + c} \sqrt{bx + a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(3/2)*(d*x+c)^(1/2),x)`

[Out] $\frac{1}{3}d(bx+a)^{3/2}(dx+c)^{3/2} + \frac{1}{4}d(bx+a)^{1/2}(dx+c)^{3/2}a - \frac{1}{4}d^2(bx+a)^{1/2}(dx+c)^{3/2}b^2c + \frac{1}{8}b(d^2x+c)^{1/2}(bx+a)^{1/2}a^2 - \frac{1}{4}d(d^2x+c)^{1/2}(bx+a)^{1/2}ac + \frac{1}{8}d^2(d^2x+c)^{1/2}(bx+a)^{1/2}c^2 - \frac{1}{16}d/b((bx+a)(dx+c))^{1/2}/(d^2x+c)^{1/2}/(bx+a)^{1/2}\ln((bd^2x+1/2ad+1/2bc)/(bd)^{1/2}+(bd^2x^2+ac+(ad+bc)x)^{1/2})/(bd)^{1/2}a^3 + \frac{3}{16}((bx+a)(dx+c))^{1/2}/(d^2x+c)^{1/2}/(bx+a)^{1/2}\ln((bd^2x+1/2ad+1/2bc)/(bd)^{1/2}+(bd^2x^2+ac+(ad+bc)x)^{1/2})/(bd)^{1/2}a^2c - \frac{3}{16}d((bx+a)(dx+c))^{1/2}/(d^2x+c)^{1/2}/(bx+a)^{1/2}\ln((bd^2x+1/2ad+1/2bc)/(bd)^{1/2}+(bd^2x^2+ac+(ad+bc)x)^{1/2})/(bd)^{1/2}ac^2b + \frac{1}{16}d^2((bx+a)(dx+c))^{1/2}/(d^2x+c)^{1/2}/(bx+a)^{1/2}\ln((bd^2x+1/2ad+1/2bc)/(bd)^{1/2}+(bd^2x^2+ac+(ad+bc)x)^{1/2})/(bd)^{1/2}c^3b^2$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/2)*(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{3/2} \sqrt{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(3/2)*(c + d*x)^(1/2),x)
```

```
[Out] int((a + b*x)^(3/2)*(c + d*x)^(1/2), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(3/2)*(d*x+c)**(1/2),x)
```

```
[Out] Timed out
```

3.1463 $\int \sqrt{a + bx} \sqrt{c + dx} dx$

Optimal. Leaf size=116

$$-\frac{(bc - ad)^2 \tanh^{-1}\left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{b} \sqrt{c+dx}}\right)}{4b^{3/2}d^{3/2}} + \frac{\sqrt{a + bx} \sqrt{c + dx} (bc - ad)}{4bd} + \frac{(a + bx)^{3/2} \sqrt{c + dx}}{2b}$$

[Out] $-1/4*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(3/2)}/d^{(3/2)}+1/2*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/b+1/4*(-a*d+b*c)*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b/d$

Rubi [A] time = 0.05, antiderivative size = 116, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$-\frac{(bc - ad)^2 \tanh^{-1}\left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{b} \sqrt{c+dx}}\right)}{4b^{3/2}d^{3/2}} + \frac{\sqrt{a + bx} \sqrt{c + dx} (bc - ad)}{4bd} + \frac{(a + bx)^{3/2} \sqrt{c + dx}}{2b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]*Sqrt[c + d*x], x]

[Out] $((b*c - a*d)*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(4*b*d) + ((a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(2*b) - ((b*c - a*d)^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/(4*b^{(3/2)}*d^{(3/2)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \sqrt{a+bx} \sqrt{c+dx} \, dx &= \frac{(a+bx)^{3/2} \sqrt{c+dx}}{2b} + \frac{(bc-ad) \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} \, dx}{4b} \\
 &= \frac{(bc-ad) \sqrt{a+bx} \sqrt{c+dx}}{4bd} + \frac{(a+bx)^{3/2} \sqrt{c+dx}}{2b} - \frac{(bc-ad)^2 \int \frac{1}{\sqrt{a+bx} \sqrt{c+dx}} \, dx}{8bd} \\
 &= \frac{(bc-ad) \sqrt{a+bx} \sqrt{c+dx}}{4bd} + \frac{(a+bx)^{3/2} \sqrt{c+dx}}{2b} - \frac{(bc-ad)^2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{c-\frac{ad}{b} + \frac{dx^2}{b}}} \, dx, \frac{\sqrt{a+bx}}{\sqrt{c+dx}} \right)}{4b^2d} \\
 &= \frac{(bc-ad) \sqrt{a+bx} \sqrt{c+dx}}{4bd} + \frac{(a+bx)^{3/2} \sqrt{c+dx}}{2b} - \frac{(bc-ad)^2 \operatorname{Subst} \left(\int \frac{1}{1-\frac{dx^2}{b}} \, dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}} \right)}{4b^2d} \\
 &= \frac{(bc-ad) \sqrt{a+bx} \sqrt{c+dx}}{4bd} + \frac{(a+bx)^{3/2} \sqrt{c+dx}}{2b} - \frac{(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{b} \sqrt{c+dx}} \right)}{4b^{3/2}d^{3/2}}
 \end{aligned}$$

Mathematica [A] time = 0.28, size = 118, normalized size = 1.02

$$\frac{b\sqrt{d} \sqrt{a+bx} (c+dx)(ad+b(c+2dx)) - (bc-ad)^{5/2} \sqrt{\frac{b(c+dx)}{bc-ad}} \sinh^{-1} \left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{bc-ad}} \right)}{4b^2d^{3/2} \sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]*Sqrt[c + d*x], x]

[Out] (b*Sqrt[d]*Sqrt[a + b*x]*(c + d*x)*(a*d + b*(c + 2*d*x)) - (b*c - a*d)^(5/2)*Sqrt[(b*(c + d*x))/(b*c - a*d)]*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(4*b^2*d^(3/2)*Sqrt[c + d*x])

fricas [A] time = 0.47, size = 300, normalized size = 2.59

$$\left[\frac{(b^2c^2 - 2abcd + a^2d^2)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 - 4(2bdx + bc + ad)\sqrt{bd}\sqrt{bx+a}\sqrt{dx+c} + 16b^2d^2)}{16b^2d^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(1/2),x, algorithm="fricas")

[Out] [1/16*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 - 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x) + 4*(2*b^2*d^2*x + b^2*c*d + a*b*d^2)*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*d^2), 1/8*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)) + 2*(2*b^2*d^2*x + b^2*c*d + a*b*d^2)*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*d^2)]

giac [B] time = 1.25, size = 232, normalized size = 2.00

$$\frac{4 \left(\frac{(b^2c - abd) \log\left(\left| -\sqrt{bd} \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd} \right| \right)}{\sqrt{bd}} - \sqrt{b^2c + (bx+a)bd - abd} \sqrt{bx+a} \right) |a|b}{b^2} - \frac{\left(\sqrt{b^2c + (bx+a)bd - abd} \left(2bx + 2a + \frac{bcd - 5ad^2}{d^2} \right) \sqrt{bx+a} + \frac{(b^3c^2 - 4abd^2)}{b^2} \right)}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(1/2),x, algorithm="giac")

[Out] -1/4*(4*((b^2*c - a*b*d)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/sqrt(b*d) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*sqrt(b*x + a)*a*abs(b)/b^2 - (sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*(2*b*x + 2*a + (b*c*d - 5*a*d^2)/d^2)*sqrt(b*x + a) + (b^3*c^2 + 2*a*b^2*c*d - 3*a^2*b*d^2)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/(sqrt(b*d)*d))*abs(b)/b^2)/b

maple [B] time = 0.01, size = 305, normalized size = 2.63

$$\frac{\sqrt{(bx+a)(dx+c)} a^2 d \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad + bc)x}\right)}{8\sqrt{dx+c}\sqrt{bx+a}\sqrt{bd}b} + \frac{\sqrt{(bx+a)(dx+c)} ac \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad + bc)x}\right)}{4\sqrt{dx+c}\sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)*(d*x+c)^(1/2),x)

```
[Out] 1/2/d*(b*x+a)^(1/2)*(d*x+c)^(3/2)+1/4/b*(d*x+c)^(1/2)*(b*x+a)^(1/2)*a-1/4/d
*(d*x+c)^(1/2)*(b*x+a)^(1/2)*c-1/8*d/b*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2
)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*
c)*x)^(1/2))/(b*d)^(1/2)*a^2+1/4*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x
+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(
1/2))/(b*d)^(1/2)*a*c-1/8/d*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(
1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2
))/(b*d)^(1/2)*c^2*b
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(1/2)*(d*x+c)^(1/2),x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError >> Computation failed since Maxima requested a
dditional constraints; using the 'assume' command before evaluation *may* h
elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more
details)Is a*d-b*c zero or nonzero?
```

mupad [B] time = 0.14, size = 88, normalized size = 0.76

$$\left(\frac{x}{2} + \frac{ad+bc}{4bd}\right) \sqrt{a+bx} \sqrt{c+dx} - \frac{\ln\left(ad+bc+2bdx+2\sqrt{b}\sqrt{d}\sqrt{a+bx}\sqrt{c+dx}\right)(ad-bc)^2}{8b^{3/2}d^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(1/2)*(c + d*x)^(1/2),x)
```

```
[Out] (x/2 + (a*d + b*c)/(4*b*d))*(a + b*x)^(1/2)*(c + d*x)^(1/2) - (log(a*d + b*
c + 2*b*d*x + 2*b^(1/2)*d^(1/2)*(a + b*x)^(1/2)*(c + d*x)^(1/2))*(a*d - b*c
)^2)/(8*b^(3/2)*d^(3/2))
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{a+bx} \sqrt{c+dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(1/2)*(d*x+c)**(1/2),x)
```

```
[Out] Integral(sqrt(a + b*x)*sqrt(c + d*x), x)
```


$$3.1464 \quad \int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=72

$$\frac{(bc - ad) \tanh^{-1} \left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{b} \sqrt{c+dx}} \right)}{b^{3/2} \sqrt{d}} + \frac{\sqrt{a+bx} \sqrt{c+dx}}{b}$$

[Out] $(-a*d+b*c)*\operatorname{arctanh}(d^{1/2}*(b*x+a)^{1/2}/b^{1/2}/(d*x+c)^{1/2})/b^{3/2}/d^{1/2}+(b*x+a)^{1/2}*(d*x+c)^{1/2}/b$

Rubi [A] time = 0.04, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$\frac{(bc - ad) \tanh^{-1} \left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{b} \sqrt{c+dx}} \right)}{b^{3/2} \sqrt{d}} + \frac{\sqrt{a+bx} \sqrt{c+dx}}{b}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/Sqrt[a + b*x], x]

[Out] $(\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/b + ((b*c - a*d)*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/(b^{3/2}*\operatorname{Sqrt}[d])$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx &= \frac{\sqrt{a+bx}\sqrt{c+dx}}{b} + \frac{(bc-ad) \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{2b} \\ &= \frac{\sqrt{a+bx}\sqrt{c+dx}}{b} + \frac{(bc-ad) \operatorname{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \sqrt{a+bx}\right)}{b^2} \\ &= \frac{\sqrt{a+bx}\sqrt{c+dx}}{b} + \frac{(bc-ad) \operatorname{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}}\right)}{b^2} \\ &= \frac{\sqrt{a+bx}\sqrt{c+dx}}{b} + \frac{(bc-ad) \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{3/2}\sqrt{d}} \end{aligned}$$

Mathematica [A] time = 0.10, size = 117, normalized size = 1.62

$$\frac{\sqrt{c+dx} \left(\sqrt{d} \sqrt{a+bx} \sqrt{\frac{b(c+dx)}{bc-ad}} + \sqrt{bc-ad} \sinh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{bc-ad}}\right) \right)}{b\sqrt{d} \sqrt{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[c + d*x]/Sqrt[a + b*x], x]
```

```
[Out] (Sqrt[c + d*x]*(Sqrt[d]*Sqrt[a + b*x]*Sqrt[(b*(c + d*x))/(b*c - a*d)] + Sqr
t[b*c - a*d]*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(b*Sqrt[d]*
Sqrt[(b*(c + d*x))/(b*c - a*d)])
```

fricas [A] time = 0.45, size = 236, normalized size = 3.28

$$\left[\frac{4 \sqrt{bx+a} \sqrt{dx+c} bd - (bc-ad) \sqrt{bd} \log(8 b^2 d^2 x^2 + b^2 c^2 + 6 abcd + a^2 d^2 - 4(2 bdx + bc + ad) \sqrt{bd} \sqrt{bx+a})}{4 b^2 d} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] [1/4*(4*sqrt(b*x + a)*sqrt(d*x + c)*b*d - (b*c - a*d)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 - 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x))/(b^2*d), 1/2*(2*sqrt(b*x + a)*sqrt(d*x + c)*b*d - (b*c - a*d)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)))/(b^2*d)]

giac [A] time = 1.10, size = 93, normalized size = 1.29

$$\frac{\left(\frac{(b^2c-abd) \log\left(\left| -\sqrt{bd} \sqrt{bx+a} + \sqrt{b^2c+(bx+a)bd-abd} \right| \right)}{\sqrt{bd}} - \sqrt{b^2c+(bx+a)bd-abd} \sqrt{bx+a} \right) |b|}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] -((b^2*c - a*b*d)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/sqrt(b*d) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*sqrt(b*x + a))*abs(b)/b^3

maple [A] time = 0.01, size = 107, normalized size = 1.49

$$\frac{(ad-bc) \sqrt{(bx+a)(dx+c)} \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad+bc)x} \right)}{2\sqrt{dx+c} \sqrt{bx+a} \sqrt{bd} b} + \frac{\sqrt{bx+a} \sqrt{dx+c}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a)^(1/2),x)

[Out] (b*x+a)^(1/2)*(d*x+c)^(1/2)/b-1/2*(a*d-b*c)/b*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 4.01, size = 260, normalized size = 3.61

$$\frac{\frac{(2ad+2bc)(\sqrt{a+bx}-\sqrt{a})}{d^2(\sqrt{c+dx}-\sqrt{c})} + \frac{(2ad+2bc)(\sqrt{a+bx}-\sqrt{a})^3}{bd(\sqrt{c+dx}-\sqrt{c})^3} - \frac{8\sqrt{a}\sqrt{c}(\sqrt{a+bx}-\sqrt{a})^2}{d(\sqrt{c+dx}-\sqrt{c})^2}}{\frac{(\sqrt{a+bx}-\sqrt{a})^4}{(\sqrt{c+dx}-\sqrt{c})^4} + \frac{b^2}{d^2} - \frac{2b(\sqrt{a+bx}-\sqrt{a})^2}{d(\sqrt{c+dx}-\sqrt{c})^2}} - \frac{2 \operatorname{atanh}\left(\frac{\sqrt{d}(\sqrt{a+bx}-\sqrt{a})}{\sqrt{b}(\sqrt{c+dx}-\sqrt{c})}\right)(ad-bc)}{b^{3/2}\sqrt{d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/2)/(a + b*x)^(1/2),x)

[Out] (((2*a*d + 2*b*c)*((a + b*x)^(1/2) - a^(1/2)))/(d^2*((c + d*x)^(1/2) - c^(1/2))) + ((2*a*d + 2*b*c)*((a + b*x)^(1/2) - a^(1/2))^3)/(b*d*((c + d*x)^(1/2) - c^(1/2))^3) - (8*a^(1/2)*c^(1/2)*((a + b*x)^(1/2) - a^(1/2))^2)/(d*((c + d*x)^(1/2) - c^(1/2))^2))/(((a + b*x)^(1/2) - a^(1/2))^4/((c + d*x)^(1/2) - c^(1/2))^4 + b^2/d^2 - (2*b*((a + b*x)^(1/2) - a^(1/2))^2)/(d*((c + d*x)^(1/2) - c^(1/2))^2)) - (2*atanh((d^(1/2)*((a + b*x)^(1/2) - a^(1/2)))/(b^(1/2)*((c + d*x)^(1/2) - c^(1/2))))*(a*d - b*c))/(b^(3/2)*d^(1/2))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/2)/(b*x+a)**(1/2),x)

[Out] Integral(sqrt(c + d*x)/sqrt(a + b*x), x)

$$3.1465 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=66

$$\frac{2\sqrt{d} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{3/2}} - \frac{2\sqrt{c+dx}}{b\sqrt{a+bx}}$$

[Out] $2*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})*d^{(1/2)}/b^{(3/2)}-2*(d*x+c)^{(1/2)}/b/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 63, 217, 206}

$$\frac{2\sqrt{d} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{3/2}} - \frac{2\sqrt{c+dx}}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[c + d*x]/(a + b*x)^(3/2), x]`

[Out] $(-2*\operatorname{Sqrt}[c + d*x])/(b*\operatorname{Sqrt}[a + b*x]) + (2*\operatorname{Sqrt}[d]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/b^{(3/2)}$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{c+dx}}{(a+bx)^{3/2}} dx &= -\frac{2\sqrt{c+dx}}{b\sqrt{a+bx}} + \frac{d \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{b} \\ &= -\frac{2\sqrt{c+dx}}{b\sqrt{a+bx}} + \frac{(2d) \operatorname{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \sqrt{a+bx}\right)}{b^2} \\ &= -\frac{2\sqrt{c+dx}}{b\sqrt{a+bx}} + \frac{(2d) \operatorname{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}}\right)}{b^2} \\ &= -\frac{2\sqrt{c+dx}}{b\sqrt{a+bx}} + \frac{2\sqrt{d} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.23, size = 99, normalized size = 1.50

$$\frac{2\left(\sqrt{d}\sqrt{bc-ad}\sqrt{\frac{b(c+dx)}{bc-ad}}\sinh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{bc-ad}}\right)-\frac{b(c+dx)}{\sqrt{a+bx}}\right)}{b^2\sqrt{c+dx}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[c + d*x]/(a + b*x)^(3/2), x]
```

```
[Out] (2*(-((b*(c + d*x))/Sqrt[a + b*x]) + Sqrt[d]*Sqrt[b*c - a*d]*Sqrt[(b*(c + d
*x))/(b*c - a*d)]*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(b^2*S
qrt[c + d*x])
```

fricas [B] time = 0.50, size = 241, normalized size = 3.65

$$\left[\frac{(bx + a)\sqrt{\frac{d}{b}} \log\left(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2b^2dx + b^2c + abd)\sqrt{bx + a}\sqrt{dx + c}\sqrt{\frac{d}{b}} + 8(b^2cd + ab)\right)}{2(b^2x + ab)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] [1/2*((b*x + a)*sqrt(d/b)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b^2*d*x + b^2*c + a*b*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(d/b) + 8*(b^2*c*d + a*b*d^2)*x) - 4*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*x + a*b), -((b*x + a)*sqrt(-d/b)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-d/b)/(b*d^2*x^2 + a*c*d + (b*c*d + a*d^2)*x)) + 2*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*x + a*b)]

giac [B] time = 1.19, size = 131, normalized size = 1.98

$$\frac{\left(\frac{\sqrt{bd} \log\left(\left(\sqrt{bd} \sqrt{bx+a} - \sqrt{b^2c+(bx+a)bd-abd}\right)^2\right)}{b} + \frac{4(\sqrt{bd}bc - \sqrt{bd}ad)}{b^2c-abd - \left(\sqrt{bd} \sqrt{bx+a} - \sqrt{b^2c+(bx+a)bd-abd}\right)^2} \right) |b|}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(3/2),x, algorithm="giac")

[Out] -(sqrt(b*d)*log((sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)/b + 4*(sqrt(b*d)*b*c - sqrt(b*d)*a*d)/(b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2))*abs(b)/b^2

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{dx + c}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a)^(3/2),x)

[Out] int((d*x+c)^(1/2)/(b*x+a)^(3/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{c+dx}}{(a+bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/2)/(a + b*x)^(3/2), x)

[Out] int((c + d*x)^(1/2)/(a + b*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{c+dx}}{(a+bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/2)/(b*x+a)**(3/2),x)

[Out] Integral(sqrt(c + d*x)/(a + b*x)**(3/2), x)

$$3.1466 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=32

$$-\frac{2(c+dx)^{3/2}}{3(a+bx)^{3/2}(bc-ad)}$$

[Out] $-2/3*(d*x+c)^{(3/2)/(-a*d+b*c)/(b*x+a)^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{2(c+dx)^{3/2}}{3(a+bx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x)^(5/2), x]

[Out] $(-2*(c + d*x)^{(3/2)})/(3*(b*c - a*d)*(a + b*x)^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{c+dx}}{(a+bx)^{5/2}} dx = -\frac{2(c+dx)^{3/2}}{3(bc-ad)(a+bx)^{3/2}}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 1.00

$$-\frac{2(c+dx)^{3/2}}{3(a+bx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*x]/(a + b*x)^(5/2), x]

[Out] $(-2*(c + d*x)^{(3/2)})/(3*(b*c - a*d)*(a + b*x)^{(3/2)})$

fricas [B] time = 0.52, size = 65, normalized size = 2.03

$$\frac{2\sqrt{bx+a}(dx+c)^{\frac{3}{2}}}{3(a^2bc - a^3d + (b^3c - ab^2d)x^2 + 2(ab^2c - a^2bd)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(5/2),x, algorithm="fricas")

[Out] -2/3*sqrt(b*x + a)*(d*x + c)^(3/2)/(a^2*b*c - a^3*d + (b^3*c - a*b^2*d)*x^2 + 2*(a*b^2*c - a^2*b*d)*x)

giac [B] time = 1.43, size = 152, normalized size = 4.75

$$\frac{4\left(\sqrt{bd}b^4c^2d - 2\sqrt{bd}ab^3cd^2 + \sqrt{bd}a^2b^2d^3 + 3\sqrt{bd}\left(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}\right)^4d\right)|b|}{3\left(b^2c - abd - \left(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}\right)^2\right)^3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(5/2),x, algorithm="giac")

[Out] -4/3*(sqrt(b*d)*b^4*c^2*d - 2*sqrt(b*d)*a*b^3*c*d^2 + sqrt(b*d)*a^2*b^2*d^3 + 3*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*d)*abs(b)/((b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)^3*b^2)

maple [A] time = 0.00, size = 27, normalized size = 0.84

$$\frac{2(dx+c)^{\frac{3}{2}}}{3(bx+a)^{\frac{3}{2}}(ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a)^(5/2),x)

[Out] 2/3/(b*x+a)^(3/2)*(d*x+c)^(3/2)/(a*d-b*c)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 0.72, size = 27, normalized size = 0.84

$$\frac{2(c + dx)^{3/2}}{(3ad - 3bc)(a + bx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/2)/(a + b*x)^(5/2), x)

[Out] (2*(c + d*x)^(3/2))/((3*a*d - 3*b*c)*(a + b*x)^(3/2))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{c + dx}}{(a + bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/2)/(b*x+a)**(5/2), x)

[Out] Integral(sqrt(c + d*x)/(a + b*x)**(5/2), x)

$$3.1467 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^{7/2}} dx$$

Optimal. Leaf size=66

$$\frac{4d(c+dx)^{3/2}}{15(a+bx)^{3/2}(bc-ad)^2} - \frac{2(c+dx)^{3/2}}{5(a+bx)^{5/2}(bc-ad)}$$

[Out] $-2/5*(d*x+c)^{(3/2)/(-a*d+b*c)/(b*x+a)^{(5/2)+4/15*d*(d*x+c)^{(3/2)/(-a*d+b*c)^2/(b*x+a)^{(3/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{4d(c+dx)^{3/2}}{15(a+bx)^{3/2}(bc-ad)^2} - \frac{2(c+dx)^{3/2}}{5(a+bx)^{5/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x)^(7/2), x]

[Out] $(-2*(c+d*x)^{(3/2))/(5*(b*c-a*d)*(a+b*x)^{(5/2)}) + (4*d*(c+d*x)^{(3/2)})/(15*(b*c-a*d)^2*(a+b*x)^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{\sqrt{c+dx}}{(a+bx)^{7/2}} dx = -\frac{2(c+dx)^{3/2}}{5(bc-ad)(a+bx)^{5/2}} - \frac{(2d) \int \frac{\sqrt{c+dx}}{(a+bx)^{5/2}} dx}{5(bc-ad)}$$

$$= -\frac{2(c+dx)^{3/2}}{5(bc-ad)(a+bx)^{5/2}} + \frac{4d(c+dx)^{3/2}}{15(bc-ad)^2(a+bx)^{3/2}}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.70

$$\frac{2(c+dx)^{3/2}(5ad-3bc+2bdx)}{15(a+bx)^{5/2}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*x]/(a + b*x)^(7/2), x]

[Out] (2*(c + d*x)^(3/2)*(-3*b*c + 5*a*d + 2*b*d*x))/(15*(b*c - a*d)^2*(a + b*x)^(5/2))

fricas [B] time = 0.73, size = 175, normalized size = 2.65

$$\frac{2(2bd^2x^2 - 3bc^2 + 5acd - (bcd - 5ad^2)x)\sqrt{bx+a}\sqrt{dx+c}}{15(a^3b^2c^2 - 2a^4bcd + a^5d^2 + (b^5c^2 - 2ab^4cd + a^2b^3d^2)x^3 + 3(ab^4c^2 - 2a^2b^3cd + a^3b^2d^2)x^2 + 3(a^2b^3c^2 - 2a^3b^2cd + a^4b^2d^2)x + 3a^5c^2 - 2a^4bd^2 + a^3b^2d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(7/2), x, algorithm="fricas")

[Out] 2/15*(2*b*d^2*x^2 - 3*b*c^2 + 5*a*c*d - (b*c*d - 5*a*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^3*b^2*c^2 - 2*a^4*b*c*d + a^5*d^2 + (b^5*c^2 - 2*a*b^4*c*d + a^2*b^3*d^2)*x^3 + 3*(a*b^4*c^2 - 2*a^2*b^3*c*d + a^3*b^2*d^2)*x^2 + 3*(a^2*b^3*c^2 - 2*a^3*b^2*c*d + a^4*b*d^2)*x)

giac [B] time = 1.44, size = 447, normalized size = 6.77

$$\frac{8(\sqrt{bd}b^7c^3d^2 - 3\sqrt{bd}ab^6c^2d^3 + 3\sqrt{bd}a^2b^5cd^4 - \sqrt{bd}a^3b^4d^5 - 5\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c+(bx+a)bd} - ab^2c))}{15(a^3b^2c^2 - 2a^4bcd + a^5d^2 + (b^5c^2 - 2ab^4cd + a^2b^3d^2)x^3 + 3(ab^4c^2 - 2a^2b^3cd + a^3b^2d^2)x^2 + 3(a^2b^3c^2 - 2a^3b^2cd + a^4b^2d^2)x + 3a^5c^2 - 2a^4bd^2 + a^3b^2d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(7/2), x, algorithm="giac")

```
[Out] 8/15*(sqrt(b*d)*b^7*c^3*d^2 - 3*sqrt(b*d)*a*b^6*c^2*d^3 + 3*sqrt(b*d)*a^2*b^5*c*d^4 - sqrt(b*d)*a^3*b^4*d^5 - 5*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*b^5*c^2*d^2 + 10*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a*b^4*c*d^3 - 5*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^2*b^3*d^4 - 5*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*b^3*c*d^2 + 5*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a*b^2*d^3 - 15*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*b*d^2)*abs(b)/((b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)^5*b^2)
```

maple [A] time = 0.01, size = 54, normalized size = 0.82

$$\frac{2(dx+c)^{\frac{3}{2}}(2bdx+5ad-3bc)}{15(bx+a)^{\frac{5}{2}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^(1/2)/(b*x+a)^(7/2),x)
```

```
[Out] 2/15*(d*x+c)^(3/2)*(2*b*d*x+5*a*d-3*b*c)/(b*x+a)^(5/2)/(a^2*d^2-2*a*b*c*d+b^2*c^2)
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(1/2)/(b*x+a)^(7/2),x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?
```

mupad [B] time = 0.82, size = 127, normalized size = 1.92

$$\frac{\sqrt{c+dx} \left(\frac{x(10ad^2-2bcd)}{15b^2(ad-bc)^2} - \frac{6bc^2-10acd}{15b^2(ad-bc)^2} + \frac{4d^2x^2}{15b(ad-bc)^2} \right)}{x^2 \sqrt{a+bx} + \frac{a^2 \sqrt{a+bx}}{b^2} + \frac{2ax \sqrt{a+bx}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(1/2)/(a + b*x)^(7/2),x)`

[Out] $((c + d*x)^{(1/2)}*((x*(10*a*d^2 - 2*b*c*d))/(15*b^2*(a*d - b*c)^2) - (6*b*c^2 - 10*a*c*d)/(15*b^2*(a*d - b*c)^2) + (4*d^2*x^2)/(15*b*(a*d - b*c)^2))/((x^2*(a + b*x)^{(1/2)} + (a^2*(a + b*x)^{(1/2)})/b^2 + (2*a*x*(a + b*x)^{(1/2)})/b)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(1/2)/(b*x+a)**(7/2),x)`

[Out] Timed out

$$3.1468 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^{9/2}} dx$$

Optimal. Leaf size=101

$$-\frac{16d^2(c+dx)^{3/2}}{105(a+bx)^{3/2}(bc-ad)^3} + \frac{8d(c+dx)^{3/2}}{35(a+bx)^{5/2}(bc-ad)^2} - \frac{2(c+dx)^{3/2}}{7(a+bx)^{7/2}(bc-ad)}$$

[Out] $-2/7*(d*x+c)^{(3/2)/(-a*d+b*c)/(b*x+a)^{(7/2)}+8/35*d*(d*x+c)^{(3/2)/(-a*d+b*c)^{(5/2)}-16/105*d^2*(d*x+c)^{(3/2)/(-a*d+b*c)^3/(b*x+a)^{(3/2)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{16d^2(c+dx)^{3/2}}{105(a+bx)^{3/2}(bc-ad)^3} + \frac{8d(c+dx)^{3/2}}{35(a+bx)^{5/2}(bc-ad)^2} - \frac{2(c+dx)^{3/2}}{7(a+bx)^{7/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x)^(9/2), x]

[Out] $(-2*(c+d*x)^{(3/2))/(7*(b*c-a*d)*(a+b*x)^{(7/2)})+(8*d*(c+d*x)^{(3/2)})/(35*(b*c-a*d)^2*(a+b*x)^{(5/2)})-(16*d^2*(c+d*x)^{(3/2)})/(105*(b*c-a*d)^3*(a+b*x)^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{c+dx}}{(a+bx)^{9/2}} dx &= -\frac{2(c+dx)^{3/2}}{7(bc-ad)(a+bx)^{7/2}} - \frac{(4d) \int \frac{\sqrt{c+dx}}{(a+bx)^{7/2}} dx}{7(bc-ad)} \\ &= -\frac{2(c+dx)^{3/2}}{7(bc-ad)(a+bx)^{7/2}} + \frac{8d(c+dx)^{3/2}}{35(bc-ad)^2(a+bx)^{5/2}} + \frac{(8d^2) \int \frac{\sqrt{c+dx}}{(a+bx)^{5/2}} dx}{35(bc-ad)^2} \\ &= -\frac{2(c+dx)^{3/2}}{7(bc-ad)(a+bx)^{7/2}} + \frac{8d(c+dx)^{3/2}}{35(bc-ad)^2(a+bx)^{5/2}} - \frac{16d^2(c+dx)^{3/2}}{105(bc-ad)^3(a+bx)^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.04, size = 77, normalized size = 0.76

$$\frac{2(c+dx)^{3/2} (35a^2d^2 + 14abd(2dx-3c) + b^2(15c^2 - 12cdx + 8d^2x^2))}{105(a+bx)^{7/2}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*x]/(a + b*x)^(9/2), x]

[Out] $(-2*(c + d*x)^{(3/2)}*(35*a^2*d^2 + 14*a*b*d*(-3*c + 2*d*x) + b^2*(15*c^2 - 12*c*d*x + 8*d^2*x^2)))/(105*(b*c - a*d)^3*(a + b*x)^{(7/2)})$

fricas [B] time = 1.26, size = 337, normalized size = 3.34

$$\frac{2(8b^2d^3x^3 + 15b^2c^3 - 42abc^2d + 35a^2cd^2 - 4(b^2cd^2 - 105(a^4b^3c^3 - 3a^5b^2c^2d + 3a^6bcd^2 - a^7d^3 + (b^7c^3 - 3ab^6c^2d + 3a^2b^5cd^2 - a^3b^4d^3))x^4 + 4(ab^6c^3 - 3a^2b^5c^2d + 3a^3b^4c^2d^2 - 3a^4b^3cd^3 - 3a^5b^2c^2d^2 + 3a^6b^2cd^3 - a^7d^4))}{105(a^4b^3c^3 - 3a^5b^2c^2d + 3a^6bcd^2 - a^7d^3 + (b^7c^3 - 3ab^6c^2d + 3a^2b^5cd^2 - a^3b^4d^3))x^4 + 4(ab^6c^3 - 3a^2b^5c^2d + 3a^3b^4c^2d^2 - 3a^4b^3cd^3 - 3a^5b^2c^2d^2 + 3a^6b^2cd^3 - a^7d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(9/2), x, algorithm="fricas")

[Out] $-2/105*(8*b^2*d^3*x^3 + 15*b^2*c^3 - 42*a*b*c^2*d + 35*a^2*c*d^2 - 4*(b^2*c*d^2 - 7*a*b*d^3)*x^2 + (3*b^2*c^2*d - 14*a*b*c*d^2 + 35*a^2*d^3)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^4*b^3*c^3 - 3*a^5*b^2*c^2*d + 3*a^6*b*c*d^2 - a^7*d^3 + (b^7*c^3 - 3*a*b^6*c^2*d + 3*a^2*b^5*c*d^2 - a^3*b^4*d^3)*x^4 + 4*(a*b^6*c^3 - 3*a^2*b^5*c^2*d + 3*a^3*b^4*c*d^2 - a^4*b^3*d^3)*x^3 + 6*(a^2*b^5*c^3 - 3*a^3*b^4*c^2*d + 3*a^4*b^3*c*d^2 - a^5*b^2*d^3)*x^2 + 4*(a^3*b^4*c^3 - 3*a^4*b^3*c^2*d + 3*a^5*b^2*c*d^2 - a^6*b*d^3)*x)$

giac [B] time = 1.58, size = 689, normalized size = 6.82

$$\frac{32(\sqrt{bd}b^{10}c^4d^3 - 4\sqrt{bd}ab^9c^3d^4 + 6\sqrt{bd}a^2b^8c^2d^5 - 4\sqrt{bd}a^3b^7cd^6 + \sqrt{bd}a^4b^6d^7 - 7\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{bd}))}{105(a^4b^3c^3 - 3a^5b^2c^2d + 3a^6bcd^2 - a^7d^3 + (b^7c^3 - 3ab^6c^2d + 3a^2b^5cd^2 - a^3b^4d^3))x^4 + 4(ab^6c^3 - 3a^2b^5c^2d + 3a^3b^4c^2d^2 - 3a^4b^3cd^3 - 3a^5b^2c^2d^2 + 3a^6b^2cd^3 - a^7d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(9/2),x, algorithm="giac")

[Out]
$$\frac{-32/105*(\sqrt{b*d}*b^{10}*c^4*d^3 - 4*\sqrt{b*d}*a*b^9*c^3*d^4 + 6*\sqrt{b*d}*a^2*b^8*c^2*d^5 - 4*\sqrt{b*d}*a^3*b^7*c*d^6 + \sqrt{b*d}*a^4*b^6*d^7 - 7*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*b^8*c^3*d^3 + 21*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a*b^7*c^2*d^4 - 21*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^2*b^6*c*d^5 + 7*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^3*b^5*d^6 + 21*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*b^6*c^2*d^3 - 42*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a*b^5*c*d^4 + 21*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a^2*b^4*d^5 + 35*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*b^4*c*d^3 - 35*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*a*b^3*d^4 + 70*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^8*b^2*d^3)*abs(b)/((b^2*c - a*b*d - (\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d}))^2)^7*b^2}$$

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{2(dx+c)^{\frac{3}{2}}(8b^2x^2d^2+28abd^2x-12b^2cdx+35a^2d^2-42abcd+15b^2c^2)}{105(bx+a)^{\frac{7}{2}}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a)^(9/2),x)

[Out]
$$\frac{2/105*(d*x+c)^{3/2}*(8*b^2*d^2*x^2+28*a*b*d^2*x-12*b^2*c*d*x+35*a^2*d^2-42*a*b*c*d+15*b^2*c^2)/(b*x+a)^{7/2}/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)}$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(9/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 0.97, size = 203, normalized size = 2.01

$$\frac{\sqrt{c+dx} \left(\frac{70a^2cd^2-84abc^2d+30b^2c^3}{105b^3(ad-bc)^3} + \frac{x(70a^2d^3-28abcd^2+6b^2c^2d)}{105b^3(ad-bc)^3} + \frac{16d^3x^3}{105b(ad-bc)^3} + \frac{8d^2x^2(7ad-bc)}{105b^2(ad-bc)^3} \right)}{x^3\sqrt{a+bx} + \frac{a^3\sqrt{a+bx}}{b^3} + \frac{3ax^2\sqrt{a+bx}}{b} + \frac{3a^2x\sqrt{a+bx}}{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(1/2)/(a + b*x)^(9/2), x)`

[Out] `((c + d*x)^(1/2)*((30*b^2*c^3 + 70*a^2*c*d^2 - 84*a*b*c^2*d)/(105*b^3*(a*d - b*c)^3) + (x*(70*a^2*d^3 + 6*b^2*c^2*d - 28*a*b*c*d^2))/(105*b^3*(a*d - b*c)^3) + (16*d^3*x^3)/(105*b*(a*d - b*c)^3) + (8*d^2*x^2*(7*a*d - b*c))/(105*b^2*(a*d - b*c)^3)))/(x^3*(a + b*x)^(1/2) + (a^3*(a + b*x)^(1/2))/b^3 + (3*a*x^2*(a + b*x)^(1/2))/b + (3*a^2*x*(a + b*x)^(1/2))/b^2)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(1/2)/(b*x+a)**(9/2), x)`

[Out] Timed out

$$3.1469 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^{11/2}} dx$$

Optimal. Leaf size=136

$$\frac{32d^3(c+dx)^{3/2}}{315(a+bx)^{3/2}(bc-ad)^4} - \frac{16d^2(c+dx)^{3/2}}{105(a+bx)^{5/2}(bc-ad)^3} + \frac{4d(c+dx)^{3/2}}{21(a+bx)^{7/2}(bc-ad)^2} - \frac{2(c+dx)^{3/2}}{9(a+bx)^{9/2}(bc-ad)}$$

[Out] $-2/9*(d*x+c)^{(3/2)/(-a*d+b*c)/(b*x+a)^{(9/2)+4/21*d*(d*x+c)^{(3/2)/(-a*d+b*c)}^2/(b*x+a)^{(7/2)-16/105*d^2*(d*x+c)^{(3/2)/(-a*d+b*c)^3/(b*x+a)^{(5/2)+32/315*d^3*(d*x+c)^{(3/2)/(-a*d+b*c)^4/(b*x+a)^{(3/2)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{32d^3(c+dx)^{3/2}}{315(a+bx)^{3/2}(bc-ad)^4} - \frac{16d^2(c+dx)^{3/2}}{105(a+bx)^{5/2}(bc-ad)^3} + \frac{4d(c+dx)^{3/2}}{21(a+bx)^{7/2}(bc-ad)^2} - \frac{2(c+dx)^{3/2}}{9(a+bx)^{9/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x)^(11/2), x]

[Out] $(-2*(c+d*x)^{(3/2))/(9*(b*c-a*d)*(a+b*x)^{(9/2)}) + (4*d*(c+d*x)^{(3/2)})/(21*(b*c-a*d)^2*(a+b*x)^{(7/2)}) - (16*d^2*(c+d*x)^{(3/2)})/(105*(b*c-a*d)^3*(a+b*x)^{(5/2)}) + (32*d^3*(c+d*x)^{(3/2)})/(315*(b*c-a*d)^4*(a+b*x)^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{c+dx}}{(a+bx)^{11/2}} dx &= -\frac{2(c+dx)^{3/2}}{9(bc-ad)(a+bx)^{9/2}} - \frac{(2d) \int \frac{\sqrt{c+dx}}{(a+bx)^{9/2}} dx}{3(bc-ad)} \\
&= -\frac{2(c+dx)^{3/2}}{9(bc-ad)(a+bx)^{9/2}} + \frac{4d(c+dx)^{3/2}}{21(bc-ad)^2(a+bx)^{7/2}} + \frac{(8d^2) \int \frac{\sqrt{c+dx}}{(a+bx)^{7/2}} dx}{21(bc-ad)^2} \\
&= -\frac{2(c+dx)^{3/2}}{9(bc-ad)(a+bx)^{9/2}} + \frac{4d(c+dx)^{3/2}}{21(bc-ad)^2(a+bx)^{7/2}} - \frac{16d^2(c+dx)^{3/2}}{105(bc-ad)^3(a+bx)^{5/2}} - \frac{(16d^3) \int \frac{\sqrt{c+dx}}{(a+bx)^{5/2}} dx}{105(bc-ad)^4} \\
&= -\frac{2(c+dx)^{3/2}}{9(bc-ad)(a+bx)^{9/2}} + \frac{4d(c+dx)^{3/2}}{21(bc-ad)^2(a+bx)^{7/2}} - \frac{16d^2(c+dx)^{3/2}}{105(bc-ad)^3(a+bx)^{5/2}} + \frac{32d^3(c+dx)^{3/2}}{315(bc-ad)^4}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 118, normalized size = 0.87

$$\frac{2(c+dx)^{3/2} (105a^3d^3 + 63a^2bd^2(2dx-3c) + 9ab^2d(15c^2-12cdx+8d^2x^2) + b^3(-35c^3+30c^2dx-24cd^2x^2+16d^3x^3))}{315(a+bx)^{9/2}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*x]/(a + b*x)^(11/2), x]

[Out] (2*(c + d*x)^(3/2)*(105*a^3*d^3 + 63*a^2*b*d^2*(-3*c + 2*d*x) + 9*a*b^2*d*(15*c^2 - 12*c*d*x + 8*d^2*x^2) + b^3*(-35*c^3 + 30*c^2*d*x - 24*c*d^2*x^2 + 16*d^3*x^3)))/(315*(b*c - a*d)^4*(a + b*x)^(9/2))

fricas [B] time = 4.38, size = 532, normalized size = 3.91

$$\frac{2(16b^3d^4x^4 - 35b^3c^4 + 135a^2b^2c^3d - 189a^2b^2c^2d^2 + 105a^3cd^3 - 8(b^3cd^3 - 9a^2b^2d^4)x^3 + 6(b^3c^2d^2 - 6a^2b^2cd^3 + 21a^2b^2d^4)x^2 - (5b^3c^3d - 27a^2b^2c^2d^2 + 63a^2b^2cd^3 - 105a^3d^4)x)\sqrt{bx+a}\sqrt{dx+c}}{315(a^5b^4c^4 - 4a^6b^3c^4 + 135a^2b^2c^3d - 189a^2b^2c^2d^2 + 105a^3cd^3 - 8(b^3cd^3 - 9a^2b^2d^4)x^3 + 6(b^3c^2d^2 - 6a^2b^2cd^3 + 21a^2b^2d^4)x^2 - (5b^3c^3d - 27a^2b^2c^2d^2 + 63a^2b^2cd^3 - 105a^3d^4)x)\sqrt{bx+a}\sqrt{dx+c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(11/2), x, algorithm="fricas")

[Out] 2/315*(16*b^3*d^4*x^4 - 35*b^3*c^4 + 135*a*b^2*c^3*d - 189*a^2*b*c^2*d^2 + 105*a^3*c*d^3 - 8*(b^3*c*d^3 - 9*a*b^2*d^4)*x^3 + 6*(b^3*c^2*d^2 - 6*a*b^2*c*d^3 + 21*a^2*b*d^4)*x^2 - (5*b^3*c^3*d - 27*a*b^2*c^2*d^2 + 63*a^2*b*c*d^3 - 105*a^3*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^5*b^4*c^4 - 4*a^6*b^3*c^4 + 135*a^2*b^2*c^3*d - 189*a^2*b^2*c^2*d^2 + 105*a^3*c*d^3 - 8*(b^3*c*d^3 - 9*a*b^2*d^4)*x^3 + 6*(b^3*c^2*d^2 - 6*a*b^2*c*d^3 + 21*a^2*b*d^4)*x^2 - (5*b^3*c^3*d - 27*a*b^2*c^2*d^2 + 63*a^2*b*c*d^3 - 105*a^3*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c)

[In] `int((d*x+c)^(1/2)/(b*x+a)^(11/2),x)`

[Out] $2/315*(d*x+c)^{(3/2)}*(16*b^3*d^3*x^3+72*a*b^2*d^3*x^2-24*b^3*c*d^2*x^2+126*a^2*b*d^3*x-108*a*b^2*c*d^2*x+30*b^3*c^2*d*x+105*a^3*d^3-189*a^2*b*c*d^2+135*a*b^2*c^2*d-35*b^3*c^3)/(b*x+a)^{(9/2)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(1/2)/(b*x+a)^(11/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.18, size = 292, normalized size = 2.15

$$\frac{\sqrt{c+dx} \left(\frac{32d^4x^4}{315b(ad-bc)^4} - \frac{-210a^3cd^3+378a^2bc^2d^2-270ab^2c^3d+70b^3c^4}{315b^4(ad-bc)^4} + \frac{x(210a^3d^4-126a^2bcd^3+54ab^2c^2d^2-10b^3c^3d)}{315b^4(ad-bc)^4} + \frac{16d^3}{315b} \right)}{x^4\sqrt{a+bx} + \frac{a^4\sqrt{a+bx}}{b^4} + \frac{6a^2x^2\sqrt{a+bx}}{b^2} + \frac{4ax^3\sqrt{a+bx}}{b} + \frac{4a^3x\sqrt{a+bx}}{b^3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c+d*x)^(1/2)/(a+b*x)^(11/2),x)`

[Out] $((c+d*x)^{(1/2)}*((32*d^4*x^4)/(315*b*(a*d-b*c)^4) - (70*b^3*c^4 - 210*a^3*c*d^3 + 378*a^2*b*c^2*d^2 - 270*a*b^2*c^3*d)/(315*b^4*(a*d-b*c)^4) + (x*(210*a^3*d^4 - 10*b^3*c^3*d + 54*a*b^2*c^2*d^2 - 126*a^2*b*c*d^3))/(315*b^4*(a*d-b*c)^4) + (16*d^3*x^3*(9*a*d-b*c))/(315*b^2*(a*d-b*c)^4) + (4*d^2*x^2*(21*a^2*d^2 + b^2*c^2 - 6*a*b*c*d)/(105*b^3*(a*d-b*c)^4)))/(x^4*(a+b*x)^{(1/2)} + (a^4*(a+b*x)^{(1/2)})/b^4 + (6*a^2*x^2*(a+b*x)^{(1/2)})/b^2 + (4*a*x^3*(a+b*x)^{(1/2)})/b + (4*a^3*x*(a+b*x)^{(1/2)})/b^3)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(1/2)/(b*x+a)**(11/2),x)`

[Out] Timed out

$$3.1470 \quad \int \frac{\sqrt{c+dx}}{(a+bx)^{13/2}} dx$$

Optimal. Leaf size=171

$$-\frac{256d^4(c+dx)^{3/2}}{3465(a+bx)^{3/2}(bc-ad)^5} + \frac{128d^3(c+dx)^{3/2}}{1155(a+bx)^{5/2}(bc-ad)^4} - \frac{32d^2(c+dx)^{3/2}}{231(a+bx)^{7/2}(bc-ad)^3} + \frac{16d(c+dx)^{3/2}}{99(a+bx)^{9/2}(bc-ad)^2} - \frac{11(a+bx)^{11/2}}{11(a+bx)^{11/2}}$$

[Out] $-2/11*(d*x+c)^{(3/2)/(-a*d+b*c)/(b*x+a)^{(11/2)}+16/99*d*(d*x+c)^{(3/2)/(-a*d+b*c)^2/(b*x+a)^{(9/2)}-32/231*d^2*(d*x+c)^{(3/2)/(-a*d+b*c)^3/(b*x+a)^{(7/2)}+128/1155*d^3*(d*x+c)^{(3/2)/(-a*d+b*c)^4/(b*x+a)^{(5/2)}-256/3465*d^4*(d*x+c)^{(3/2)/(-a*d+b*c)^5/(b*x+a)^{(3/2)}$

Rubi [A] time = 0.04, antiderivative size = 171, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{256d^4(c+dx)^{3/2}}{3465(a+bx)^{3/2}(bc-ad)^5} + \frac{128d^3(c+dx)^{3/2}}{1155(a+bx)^{5/2}(bc-ad)^4} - \frac{32d^2(c+dx)^{3/2}}{231(a+bx)^{7/2}(bc-ad)^3} + \frac{16d(c+dx)^{3/2}}{99(a+bx)^{9/2}(bc-ad)^2} - \frac{11(a+bx)^{11/2}}{11(a+bx)^{11/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[c + d*x]/(a + b*x)^(13/2), x]

[Out] $(-2*(c+d*x)^{(3/2))/(11*(b*c-a*d)*(a+b*x)^{(11/2)}) + (16*d*(c+d*x)^{(3/2))/(99*(b*c-a*d)^2*(a+b*x)^{(9/2)}) - (32*d^2*(c+d*x)^{(3/2))/(231*(b*c-a*d)^3*(a+b*x)^{(7/2)}) + (128*d^3*(c+d*x)^{(3/2))/(1155*(b*c-a*d)^4*(a+b*x)^{(5/2)}) - (256*d^4*(c+d*x)^{(3/2))/(3465*(b*c-a*d)^5*(a+b*x)^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[n] && (LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler

Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt{c+dx}}{(a+bx)^{13/2}} dx &= -\frac{2(c+dx)^{3/2}}{11(bc-ad)(a+bx)^{11/2}} - \frac{(8d) \int \frac{\sqrt{c+dx}}{(a+bx)^{11/2}} dx}{11(bc-ad)} \\
 &= -\frac{2(c+dx)^{3/2}}{11(bc-ad)(a+bx)^{11/2}} + \frac{16d(c+dx)^{3/2}}{99(bc-ad)^2(a+bx)^{9/2}} + \frac{(16d^2) \int \frac{\sqrt{c+dx}}{(a+bx)^{9/2}} dx}{33(bc-ad)^2} \\
 &= -\frac{2(c+dx)^{3/2}}{11(bc-ad)(a+bx)^{11/2}} + \frac{16d(c+dx)^{3/2}}{99(bc-ad)^2(a+bx)^{9/2}} - \frac{32d^2(c+dx)^{3/2}}{231(bc-ad)^3(a+bx)^{7/2}} - \frac{(64d^3) \int \frac{\sqrt{c+dx}}{(a+bx)^{7/2}} dx}{231(bc-ad)^3} \\
 &= -\frac{2(c+dx)^{3/2}}{11(bc-ad)(a+bx)^{11/2}} + \frac{16d(c+dx)^{3/2}}{99(bc-ad)^2(a+bx)^{9/2}} - \frac{32d^2(c+dx)^{3/2}}{231(bc-ad)^3(a+bx)^{7/2}} + \frac{128d^3(c+dx)^{3/2}}{1155(bc-ad)^4(a+bx)^{5/2}} \\
 &= -\frac{2(c+dx)^{3/2}}{11(bc-ad)(a+bx)^{11/2}} + \frac{16d(c+dx)^{3/2}}{99(bc-ad)^2(a+bx)^{9/2}} - \frac{32d^2(c+dx)^{3/2}}{231(bc-ad)^3(a+bx)^{7/2}} + \frac{128d^3(c+dx)^{3/2}}{1155(bc-ad)^4(a+bx)^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.08, size = 170, normalized size = 0.99

$$\frac{2(c+dx)^{3/2} (1155a^4d^4 + 924a^3bd^3(2dx-3c) + 198a^2b^2d^2(15c^2-12cdx+8d^2x^2) + 44ab^3d(-35c^3+30c^2dx-24cd^2x^2+16d^3x^3) + b^4(315c^4-280c^3dx+240c^2d^2x^2-192cd^3x^3+128d^4x^4))}{3465(a+bx)^{11/2}(bc-ad)^5}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[c + d*x]/(a + b*x)^(13/2), x]

[Out] $(-2*(c + d*x)^(3/2)*(1155*a^4*d^4 + 924*a^3*b*d^3*(-3*c + 2*d*x) + 198*a^2*b^2*d^2*(15*c^2 - 12*c*d*x + 8*d^2*x^2) + 44*a*b^3*d*(-35*c^3 + 30*c^2*d*x - 24*c*d^2*x^2 + 16*d^3*x^3) + b^4*(315*c^4 - 280*c^3*d*x + 240*c^2*d^2*x^2 - 192*c*d^3*x^3 + 128*d^4*x^4)))/(3465*(b*c - a*d)^5*(a + b*x)^(11/2))$

fricas [B] time = 9.21, size = 781, normalized size = 4.57

$$\frac{3465 (a^6 b^5 c^5 - 5 a^7 b^4 c^4 d + 10 a^8 b^3 c^3 d^2 - 10 a^9 b^2 c^2 d^3 + 5 a^{10} b c d^4 - a^{11} d^5 + (b^{11} c^5 - 5 a b^{10} c^4 d + 10 a^2 b^9 c^3 d^2 - 10 a^3 b^8 c^2 d^3 + 5 a^4 b^7 c d^4 - a^5 b^6 d^5))}{(b*c - a*d)^5*(a + b*x)^(11/2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(13/2), x, algorithm="fricas")

```
[Out] -2/3465*(128*b^4*d^5*x^5 + 315*b^4*c^5 - 1540*a*b^3*c^4*d + 2970*a^2*b^2*c^3*d^2 - 2772*a^3*b*c^2*d^3 + 1155*a^4*c*d^4 - 64*(b^4*c*d^4 - 11*a*b^3*d^5)*x^4 + 16*(3*b^4*c^2*d^3 - 22*a*b^3*c*d^4 + 99*a^2*b^2*d^5)*x^3 - 8*(5*b^4*c^3*d^2 - 33*a*b^3*c^2*d^3 + 99*a^2*b^2*c*d^4 - 231*a^3*b*d^5)*x^2 + (35*b^4*c^4*d - 220*a*b^3*c^3*d^2 + 594*a^2*b^2*c^2*d^3 - 924*a^3*b*c*d^4 + 1155*a^4*d^5)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^6*b^5*c^5 - 5*a^7*b^4*c^4*d + 10*a^8*b^3*c^3*d^2 - 10*a^9*b^2*c^2*d^3 + 5*a^10*b*c*d^4 - a^11*d^5 + (b^11*c^5 - 5*a*b^10*c^4*d + 10*a^2*b^9*c^3*d^2 - 10*a^3*b^8*c^2*d^3 + 5*a^4*b^7*c*d^4 - a^5*b^6*d^5)*x^6 + 6*(a*b^10*c^5 - 5*a^2*b^9*c^4*d + 10*a^3*b^8*c^3*d^2 - 10*a^4*b^7*c^2*d^3 + 5*a^5*b^6*c*d^4 - a^6*b^5*d^5)*x^5 + 15*(a^2*b^9*c^5 - 5*a^3*b^8*c^4*d + 10*a^4*b^7*c^3*d^2 - 10*a^5*b^6*c^2*d^3 + 5*a^6*b^5*c*d^4 - a^7*b^4*d^5)*x^4 + 20*(a^3*b^8*c^5 - 5*a^4*b^7*c^4*d + 10*a^5*b^6*c^3*d^2 - 10*a^6*b^5*c^2*d^3 + 5*a^7*b^4*c*d^4 - a^8*b^3*d^5)*x^3 + 15*(a^4*b^7*c^5 - 5*a^5*b^6*c^4*d + 10*a^6*b^5*c^3*d^2 - 10*a^7*b^4*c^2*d^3 + 5*a^8*b^3*c*d^4 - a^9*b^2*d^5)*x^2 + 6*(a^5*b^6*c^5 - 5*a^6*b^5*c^4*d + 10*a^7*b^4*c^3*d^2 - 10*a^8*b^3*c^2*d^3 + 5*a^9*b^2*c*d^4 - a^10*b*d^5)*x)
```

giac [B] time = 2.38, size = 1345, normalized size = 7.87

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(1/2)/(b*x+a)^(13/2),x, algorithm="giac")
```

```
[Out] -512/3465*(sqrt(b*d)*b^16*c^6*d^5 - 6*sqrt(b*d)*a*b^15*c^5*d^6 + 15*sqrt(b*d)*a^2*b^14*c^4*d^7 - 20*sqrt(b*d)*a^3*b^13*c^3*d^8 + 15*sqrt(b*d)*a^4*b^12*c^2*d^9 - 6*sqrt(b*d)*a^5*b^11*c*d^10 + sqrt(b*d)*a^6*b^10*d^11 - 11*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*b^14*c^5*d^5 + 55*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a*b^13*c^4*d^6 - 110*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^2*b^12*c^3*d^7 + 110*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^3*b^11*c^2*d^8 - 55*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^4*b^10*c*d^9 + 11*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^5*b^9*d^10 + 55*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*b^12*c^4*d^5 - 220*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a*b^11*c^3*d^6 + 330*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^2*b^10*c^2*d^7 - 220*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^3*b^9*c*d^8 + 55*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^4*b^8*d^9 - 165*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*b^10*c^3*d^5 + 495*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*a*b^9*c^2*d^6 - 495*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^2*b^8*c*d^7 + 165*sqrt(b*d)*
```

$(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^6*a^3*b^7*d^8 + 330*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^8*b^8*c^2*d^5 - 660*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^8*a*b^7*c*d^6 + 330*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^8*a^2*b^6*d^7 + 924*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^10*b^6*c*d^5 - 924*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^10*a*b^5*d^6 + 1386*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^12*b^4*d^5)*\text{abs}(b)/((b^2*c - a*b*d - (\sqrt{b*d})*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^2)^{11}*b^2)$

maple [A] time = 0.01, size = 256, normalized size = 1.50

$$\frac{2(dx+c)^{\frac{3}{2}}(128b^4x^4d^4 + 704ab^3d^4x^3 - 192b^4cd^3x^3 + 1584a^2b^2d^4x^2 - 1056ab^3cd^3x^2 + 240b^4c^2d^2x^2 + 1848a^3bd^4x - 2376a^2b^2cd^3x + 1320a^3b^3c^2d^2x - 280b^4c^3d^3x + 1155a^4d^4 - 772a^3b^2cd^3 + 2970a^2b^2c^2d^2 - 1540a^3b^3cd^3 + 315b^4c^4)}{3465(bx+a)^{\frac{11}{2}}(a^5d^5 - 5a^4bcd^4 + \dots)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/2)/(b*x+a)^(13/2),x)

[Out] 2/3465*(d*x+c)^(3/2)*(128*b^4*d^4*x^4+704*a*b^3*d^4*x^3-192*b^4*c*d^3*x^3+1584*a^2*b^2*d^4*x^2-1056*a*b^3*c*d^3*x^2+240*b^4*c^2*d^2*x^2+1848*a^3*b*d^4*x-2376*a^2*b^2*c*d^3*x+1320*a*b^3*c^2*d^2*x-280*b^4*c^3*d^3*x+1155*a^4*d^4-772*a^3*b^2*c*d^3+2970*a^2*b^2*c^2*d^2-1540*a*b^3*c^3*d+315*b^4*c^4)/(b*x+a)^(11/2)/(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/2)/(b*x+a)^(13/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.43, size = 397, normalized size = 2.32

$$\frac{\sqrt{c+dx} \left(\frac{2310a^4cd^4 - 5544a^3b^2c^2d^3 + 5940a^2b^2c^3d^2 - 3080ab^3c^4d + 630b^4c^5}{3465b^5(ad-bc)^5} + \frac{x(2310a^4d^5 - 1848a^3bcd^4 + 1188a^2b^2c^2d^3 - 440ab^3c^3d^2 - 1056a^2b^2cd^3 + 240b^4c^2d^2x^2 + 1848a^3bd^4x - 2376a^2b^2cd^3x + 1320a^3b^3c^2d^2x - 280b^4c^3d^3x + 1155a^4d^4 - 772a^3b^2cd^3 + 2970a^2b^2c^2d^2 - 1540a^3b^3cd^3 + 315b^4c^4)}{3465b^5(ad-bc)^5} \right)}{x^5\sqrt{a+bx} + \frac{a^5\sqrt{a+bx}}{b^5} + \frac{10a^2x^3\sqrt{a+bx}}{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((c + d*x)^{(1/2)}/(a + b*x)^{(13/2)}, x)$

[Out] $((c + d*x)^{(1/2)}*((630*b^4*c^5 + 2310*a^4*c*d^4 - 5544*a^3*b*c^2*d^3 + 5940*a^2*b^2*c^3*d^2 - 3080*a*b^3*c^4*d)/(3465*b^5*(a*d - b*c)^5) + (x*(2310*a^4*d^5 + 70*b^4*c^4*d - 440*a*b^3*c^3*d^2 + 1188*a^2*b^2*c^2*d^3 - 1848*a^3*b*c*d^4))/(3465*b^5*(a*d - b*c)^5) + (256*d^5*x^5)/(3465*b*(a*d - b*c)^5) + (16*d^2*x^2*(231*a^3*d^3 - 5*b^3*c^3 + 33*a*b^2*c^2*d - 99*a^2*b*c*d^2))/(3465*b^4*(a*d - b*c)^5) + (128*d^4*x^4*(11*a*d - b*c))/(3465*b^2*(a*d - b*c)^5) + (32*d^3*x^3*(99*a^2*d^2 + 3*b^2*c^2 - 22*a*b*c*d))/(3465*b^3*(a*d - b*c)^5))/(x^5*(a + b*x)^{(1/2)} + (a^5*(a + b*x)^{(1/2)})/b^5 + (10*a^2*x^3*(a + b*x)^{(1/2)})/b^2 + (10*a^3*x^2*(a + b*x)^{(1/2)})/b^3 + (5*a*x^4*(a + b*x)^{(1/2)})/b + (5*a^4*x*(a + b*x)^{(1/2)})/b^4)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x+c)**(1/2)/(b*x+a)**(13/2), x)$

[Out] Timed out

3.1471 $\int (a + bx)^{5/2} (c + dx)^{3/2} dx$

Optimal. Leaf size=227

$$-\frac{3(bc - ad)^5 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{128b^{5/2}d^{7/2}} + \frac{3\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^4}{128b^2d^3} - \frac{(a + bx)^{3/2}\sqrt{c+dx}(bc - ad)^3}{64b^2d^2} + \frac{(a + bx)^{5/2}\sqrt{c+dx}}{80b^2d}$$

[Out] $1/5*(b*x+a)^{(7/2)}*(d*x+c)^{(3/2)}/b-3/128*(-a*d+b*c)^5*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(5/2)}/d^{(7/2)}-1/64*(-a*d+b*c)^3*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/b^2/d^2+1/80*(-a*d+b*c)^2*(b*x+a)^{(5/2)}*(d*x+c)^{(1/2)}/b^2/d+3/40*(-a*d+b*c)*(b*x+a)^{(7/2)}*(d*x+c)^{(1/2)}/b^2+3/128*(-a*d+b*c)^4*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b^2/d^3$

Rubi [A] time = 0.13, antiderivative size = 227, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$\frac{3\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^4}{128b^2d^3} - \frac{(a + bx)^{3/2}\sqrt{c+dx}(bc - ad)^3}{64b^2d^2} - \frac{3(bc - ad)^5 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{128b^{5/2}d^{7/2}} + \frac{(a + bx)^{5/2}\sqrt{c+dx}}{80b^2d}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}*(c + d*x)^{(3/2)}, x]$

[Out] $(3*(b*c - a*d)^4*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(128*b^2*d^3) - ((b*c - a*d)^3*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(64*b^2*d^2) + ((b*c - a*d)^2*(a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x])/(80*b^2*d) + (3*(b*c - a*d)*(a + b*x)^{(7/2)}*\operatorname{Sqrt}[c + d*x])/(40*b^2) + ((a + b*x)^{(7/2)}*(c + d*x)^{(3/2)})/(5*b) - (3*(b*c - a*d)^5*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/(128*b^{(5/2)}*d^{(7/2)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{GtQ}[n, 0] \ \&\& \operatorname{NeQ}[m + n + 1, 0] \ \&\& \operatorname{!(IGtQ}[m, 0] \ \&\& (\operatorname{!IntegerQ}[n] \ \|\ (\operatorname{GtQ}[m, 0] \ \&\& \operatorname{LtQ}[m - n, 0])) \ \&\& \operatorname{!ILtQ}[m + 2, 0] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}$

[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int (a + bx)^{5/2} (c + dx)^{3/2} dx &= \frac{(a + bx)^{7/2} (c + dx)^{3/2}}{5b} + \frac{(3(bc - ad)) \int (a + bx)^{5/2} \sqrt{c + dx} dx}{10b} \\
 &= \frac{3(bc - ad)(a + bx)^{7/2} \sqrt{c + dx}}{40b^2} + \frac{(a + bx)^{7/2} (c + dx)^{3/2}}{5b} + \frac{(3(bc - ad)^2) \int \frac{(a + bx)^{5/2}}{\sqrt{c + dx}} dx}{80b^2} \\
 &= \frac{(bc - ad)^2 (a + bx)^{5/2} \sqrt{c + dx}}{80b^2 d} + \frac{3(bc - ad)(a + bx)^{7/2} \sqrt{c + dx}}{40b^2} + \frac{(a + bx)^{7/2} (c + dx)}{5b} \\
 &= -\frac{(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{64b^2 d^2} + \frac{(bc - ad)^2 (a + bx)^{5/2} \sqrt{c + dx}}{80b^2 d} + \frac{3(bc - ad)(a + bx)}{40b^2} \\
 &= \frac{3(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128b^2 d^3} - \frac{(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{64b^2 d^2} + \frac{(bc - ad)^2 (a + bx)^{5/2}}{80b^2 d} \\
 &= \frac{3(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128b^2 d^3} - \frac{(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{64b^2 d^2} + \frac{(bc - ad)^2 (a + bx)^{5/2}}{80b^2 d} \\
 &= \frac{3(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128b^2 d^3} - \frac{(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{64b^2 d^2} + \frac{(bc - ad)^2 (a + bx)^{5/2}}{80b^2 d} \\
 &= \frac{3(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128b^2 d^3} - \frac{(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{64b^2 d^2} + \frac{(bc - ad)^2 (a + bx)^{5/2}}{80b^2 d}
 \end{aligned}$$

Mathematica [A] time = 1.78, size = 187, normalized size = 0.82

$$\frac{(a + bx)^{7/2} \sqrt{c + dx} \left(-\frac{15(bc-ad)^{9/2} \sinh^{-1}\left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{bc-ad}}\right)}{d^{7/2}(a+bx)^{7/2} \sqrt{\frac{b(c+dx)}{bc-ad}}} + \frac{15(bc-ad)^4}{d^3(a+bx)^3} + \frac{10(ad-bc)^3}{d^2(a+bx)^2} + \frac{8(bc-ad)^2}{d(a+bx)} + 48(bc-ad) + 128b(c+dx) \right)}{640b^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)*(c + d*x)^(3/2), x]

[Out] ((a + b*x)^(7/2)*Sqrt[c + d*x]*(48*(b*c - a*d) + (15*(b*c - a*d)^4)/(d^3*(a + b*x)^3) + (10*(-(b*c) + a*d)^3)/(d^2*(a + b*x)^2) + (8*(b*c - a*d)^2)/(d*(a + b*x)) + 128*b*(c + d*x) - (15*(b*c - a*d)^(9/2)*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(d^(7/2)*(a + b*x)^(7/2)*Sqrt[(b*(c + d*x))/(b*c - a*d)])))/(640*b^2)

fricas [A] time = 0.50, size = 702, normalized size = 3.09

$$\frac{15(b^5c^5 - 5ab^4c^4d + 10a^2b^3c^3d^2 - 10a^3b^2c^2d^3 + 5a^4bcd^4 - a^5d^5)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2)}{640b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(d*x+c)^(3/2), x, algorithm="fricas")

[Out] [-1/2560*(15*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(128*b^5*d^5*x^4 + 15*b^5*c^4*d - 70*a*b^4*c^3*d^2 + 128*a^2*b^3*c^2*d^3 + 70*a^3*b^2*c*d^4 - 15*a^4*b*d^5 + 16*(11*b^5*c*d^4 + 21*a*b^4*d^5)*x^3 + 8*(b^5*c^2*d^3 + 64*a*b^4*c*d^4 + 31*a^2*b^3*d^5)*x^2 - 2*(5*b^5*c^3*d^2 - 23*a*b^4*c^2*d^3 - 233*a^2*b^3*c*d^4 - 5*a^3*b^2*d^5)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^3*d^4), 1/1280*(15*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)) + 2*(128*b^5*d^5*x^4 + 15*b^5*c^4*d - 70*a*b^4*c^3*d^2 + 128*a^2*b^3*c^2*d^3 + 70*a^3*b^2*c*d^4 - 15*a^4*b*d^5 + 16*(11*b^5*c*d^4 + 21*a*b^4*d^5)*x^3 + 8*(b^5*c^2*d^3 + 64*a*b^4*c*d^4 + 31*a^2*b^3*d^5)*x^2 - 2*(5*b^5*c^3*d^2 - 23*a*b^4*c^2*d^3 - 233*a^2*b^3*c*d^4 - 5*a^3*b^2*d^5)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^3*d^4)]

giac [B] time = 2.30, size = 1740, normalized size = 7.67

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(d*x+c)^(3/2),x, algorithm="giac")

[Out] $\frac{1}{1920} \cdot (240 \cdot (\sqrt{b^2c + (bx+a)bd} - abd) \sqrt{bx+a} \cdot (2 \cdot (bx+a) \cdot (4 \cdot (bx+a)/b^2 + (b^6cd^3 - 13ab^5d^4)/(b^7d^4)) - 3 \cdot (b^7c^2d^2 + 2ab^6cd^3 - 11a^2b^5d^4)/(b^7d^4)) - 3 \cdot (b^3c^3 + ab^2c^2d + 3a^2b^2cd^2 - 5a^3d^3) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd} - abd)) / (\sqrt{bd} \cdot b^2d^2)) \cdot a^2 \cdot \text{abs}(b) - 1920 \cdot ((b^2c - abd) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd} - abd)) / \sqrt{bd} - \sqrt{b^2c + (bx+a)bd} \cdot \sqrt{bx+a}) \cdot a^3 \cdot \text{abs}(b) / b^2 + 10 \cdot (\sqrt{b^2c + (bx+a)bd} - abd) \cdot (2 \cdot (bx+a) \cdot (4 \cdot (bx+a) \cdot (6 \cdot (bx+a)/b^3 + (b^{12}cd^5 - 25ab^{11}d^6)/(b^{14}d^6)) - (5b^{13}c^2d^4 + 14ab^{12}cd^5 - 163a^2b^{11}d^6)/(b^{14}d^6)) + 3 \cdot (5b^{14}c^3d^3 + 9ab^{13}c^2d^4 + 15a^2b^{12}cd^5 - 93a^3b^{11}d^6)/(b^{14}d^6)) \cdot \sqrt{bx+a} + 3 \cdot (5b^4c^4 + 4ab^3c^3d + 6a^2b^2c^2d^2 + 20a^3b^2cd^3 - 35a^4d^4) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd} - abd)) / (\sqrt{bd} \cdot b^2d^3)) \cdot b \cdot \text{abs}(b) + 30 \cdot (\sqrt{b^2c + (bx+a)bd} - abd) \cdot (2 \cdot (bx+a) \cdot (4 \cdot (bx+a) \cdot (6 \cdot (bx+a)/b^3 + (b^{12}cd^5 - 25ab^{11}d^6)/(b^{14}d^6)) - (5b^{13}c^2d^4 + 14ab^{12}cd^5 - 163a^2b^{11}d^6)/(b^{14}d^6)) + 3 \cdot (5b^{14}c^3d^3 + 9ab^{13}c^2d^4 + 15a^2b^{12}cd^5 - 93a^3b^{11}d^6)/(b^{14}d^6)) \cdot \sqrt{bx+a} + 3 \cdot (5b^4c^4 + 4ab^3c^3d + 6a^2b^2c^2d^2 + 20a^3b^2cd^3 - 35a^4d^4) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd} - abd)) / (\sqrt{bd} \cdot b^2d^3)) \cdot a \cdot d \cdot \text{abs}(b) + 240 \cdot (\sqrt{b^2c + (bx+a)bd} - abd) \cdot \sqrt{bx+a} \cdot (2 \cdot (bx+a) \cdot (4 \cdot (bx+a)/b^2 + (b^6cd^3 - 13ab^5d^4)/(b^7d^4)) - 3 \cdot (b^7c^2d^2 + 2ab^6cd^3 - 11a^2b^5d^4)/(b^7d^4)) - 3 \cdot (b^3c^3 + ab^2c^2d + 3a^2b^2cd^2 - 5a^3d^3) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd} - abd)) / (\sqrt{bd} \cdot b^2d^2)) \cdot a^2 \cdot d \cdot \text{abs}(b) / b + (\sqrt{b^2c + (bx+a)bd} - abd) \cdot (2 \cdot (4 \cdot (bx+a) \cdot (6 \cdot (bx+a) \cdot (8 \cdot (bx+a)/b^4 + (b^{20}cd^7 - 41ab^{19}d^8)/(b^{23}d^8)) - (7b^{21}c^2d^6 + 26ab^{20}cd^7 - 513a^2b^{19}d^8)/(b^{23}d^8)) + 5 \cdot (7b^{22}c^3d^5 + 19ab^{21}c^2d^6 + 37a^2b^{20}cd^7 - 447a^3b^{19}d^8)/(b^{23}d^8)) \cdot (bx+a) - 15 \cdot (7b^{23}c^4d^4 + 12ab^{22}c^3d^5 + 18a^2b^{21}c^2d^6 + 28a^3b^{20}cd^7 - 193a^4b^{19}d^8)/(b^{23}d^8)) \cdot \sqrt{bx+a} - 15 \cdot (7b^5c^5 + 5ab^4c^4d + 6a^2b^3c^3d^2 + 10a^3b^2c^2d^3 + 35a^4b^2cd^4 - 63a^5d^5) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd} - abd)) / (\sqrt{bd} \cdot b^3d^4)) \cdot b \cdot d \cdot \text{abs}(b) + 1440 \cdot (\sqrt{b^2c + (bx+a)bd} - abd) \cdot (2 \cdot bx + 2a + (b^3c^2 + 2ab^2cd - 3a^2bd^2) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd} - abd)) / (\sqrt{bd} \cdot d)) \cdot a^2 \cdot c \cdot \text{abs}(b) / b^2 + 480 \cdot (\sqrt{b^2c + (bx+a)bd} - abd) \cdot (2 \cdot bx + 2a + (b^3c^2 + 2ab^2cd - 3a^2bd^2) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd} - abd)) / (\sqrt{bd} \cdot d)) \cdot a^3 \cdot d \cdot \text{abs}(b) / b^3) / b$

maple [B] time = 0.01, size = 853, normalized size = 3.76

$$\frac{3\sqrt{(bx+a)(dx+c)} a^5 d^2 \ln\left(\frac{bdx+\frac{1}{2}ad+\frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2+ac+(ad+bc)x}\right)}{256\sqrt{dx+c}\sqrt{bx+a}\sqrt{bd}b^2} - \frac{15\sqrt{(bx+a)(dx+c)} a^4 cd \ln\left(\frac{bdx+\frac{1}{2}ad+\frac{1}{2}bc}{\sqrt{bd}}\right)}{256\sqrt{dx+c}\sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)*(d*x+c)^(3/2),x)

[Out] 1/5/d*(b*x+a)^(5/2)*(d*x+c)^(5/2)+1/8/d*(b*x+a)^(3/2)*(d*x+c)^(5/2)*a+1/16/d*(b*x+a)^(1/2)*(d*x+c)^(5/2)*a^2-1/8/d^2*(b*x+a)^(1/2)*(d*x+c)^(5/2)*a*b*c+3/64/d^2*(d*x+c)^(3/2)*(b*x+a)^(1/2)*a*c^2*b+3/32/b*(d*x+c)^(1/2)*(b*x+a)^(1/2)*a^3*c+3/32/d^2*(d*x+c)^(1/2)*(b*x+a)^(1/2)*a*c^3*b-1/8/d^2*(b*x+a)^(3/2)*(d*x+c)^(5/2)*b*c+1/16/d^3*(b*x+a)^(1/2)*(d*x+c)^(5/2)*b^2*c^2+1/64/b*(d*x+c)^(3/2)*(b*x+a)^(1/2)*a^3-3/64/d*(d*x+c)^(3/2)*(b*x+a)^(1/2)*a^2*c-1/64/d^3*(d*x+c)^(3/2)*(b*x+a)^(1/2)*c^3*b^2-3/128*d/b^2*(d*x+c)^(1/2)*(b*x+a)^(1/2)*a^4-9/64/d*(d*x+c)^(1/2)*(b*x+a)^(1/2)*a^2*c^2-3/128/d^3*(d*x+c)^(1/2)*(b*x+a)^(1/2)*c^4*b^2+15/128*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*a^3*c^2+15/256/d^2*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*a*c^4*b^2-15/256*d/b*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*a^4*c+3/256*d^2/b^2*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*a^5-15/128/d*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*a^2*c^3*b-3/256/d^3*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*c^5*b^3

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(d*x+c)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{5/2} (c + dx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)*(c + d*x)^(3/2), x)

[Out] int((a + b*x)^(5/2)*(c + d*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{5}{2}} (c + dx)^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)*(d*x+c)**(3/2), x)

[Out] Integral((a + b*x)**(5/2)*(c + d*x)**(3/2), x)

3.1472 $\int (a + bx)^{3/2} (c + dx)^{3/2} dx$

Optimal. Leaf size=189

$$\frac{3(bc - ad)^4 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{64b^{5/2}d^{5/2}} - \frac{3\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^3}{64b^2d^2} + \frac{(a + bx)^{3/2}\sqrt{c+dx}(bc - ad)^2}{32b^2d} + \frac{(a + bx)^{5/2}\sqrt{c+dx}}{8b^2}$$

[Out] $1/4*(b*x+a)^{(5/2)}*(d*x+c)^{(3/2)}/b+3/64*(-a*d+b*c)^4*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(5/2)}/d^{(5/2)}+1/32*(-a*d+b*c)^2*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/b^2/d+1/8*(-a*d+b*c)*(b*x+a)^{(5/2)}*(d*x+c)^{(1/2)}/b^2-3/64*(-a*d+b*c)^3*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b^2/d^2$

Rubi [A] time = 0.09, antiderivative size = 189, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$-\frac{3\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^3}{64b^2d^2} + \frac{3(bc - ad)^4 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{64b^{5/2}d^{5/2}} + \frac{(a + bx)^{3/2}\sqrt{c+dx}(bc - ad)^2}{32b^2d} + \frac{(a + bx)^{5/2}\sqrt{c+dx}}{8b^2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}*(c + d*x)^{(3/2)}, x]$

[Out] $(-3*(b*c - a*d)^3*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(64*b^2*d^2) + ((b*c - a*d)^2*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(32*b^2*d) + ((b*c - a*d)*(a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x])/(8*b^2) + ((a + b*x)^{(5/2)}*(c + d*x)^{(3/2)})/(4*b) + (3*(b*c - a*d)^4*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/(64*b^{(5/2)}*d^{(5/2)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{GtQ}[n, 0] \ \&\& \operatorname{NeQ}[m + n + 1, 0] \ \&\& \operatorname{!(IGtQ}[m, 0] \ \&\& (\operatorname{!IntegerQ}[n] \ \|\ (\operatorname{GtQ}[m, 0] \ \&\& \operatorname{LtQ}[m - n, 0])) \ \&\& \operatorname{!ILtQ}[m + n + 2, 0] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{LtQ}[-1, m, 0] \ \&\& \operatorname{LeQ}[-1, n, 0] \ \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Den}$

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[Rt[-b, 2]*x]/Rt[a, 2])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int (a + bx)^{3/2} (c + dx)^{3/2} dx &= \frac{(a + bx)^{5/2} (c + dx)^{3/2}}{4b} + \frac{(3(bc - ad)) \int (a + bx)^{3/2} \sqrt{c + dx} dx}{8b} \\
 &= \frac{(bc - ad)(a + bx)^{5/2} \sqrt{c + dx}}{8b^2} + \frac{(a + bx)^{5/2} (c + dx)^{3/2}}{4b} + \frac{(bc - ad)^2 \int \frac{(a + bx)^{3/2}}{\sqrt{c + dx}} dx}{16b^2} \\
 &= \frac{(bc - ad)^2 (a + bx)^{3/2} \sqrt{c + dx}}{32b^2 d} + \frac{(bc - ad)(a + bx)^{5/2} \sqrt{c + dx}}{8b^2} + \frac{(a + bx)^{5/2} (c + dx)^{3/2}}{4b} \\
 &= -\frac{3(bc - ad)^3 \sqrt{a + bx} \sqrt{c + dx}}{64b^2 d^2} + \frac{(bc - ad)^2 (a + bx)^{3/2} \sqrt{c + dx}}{32b^2 d} + \frac{(bc - ad)(a + bx)^{5/2}}{8b^2} \\
 &= -\frac{3(bc - ad)^3 \sqrt{a + bx} \sqrt{c + dx}}{64b^2 d^2} + \frac{(bc - ad)^2 (a + bx)^{3/2} \sqrt{c + dx}}{32b^2 d} + \frac{(bc - ad)(a + bx)^{5/2}}{8b^2} \\
 &= -\frac{3(bc - ad)^3 \sqrt{a + bx} \sqrt{c + dx}}{64b^2 d^2} + \frac{(bc - ad)^2 (a + bx)^{3/2} \sqrt{c + dx}}{32b^2 d} + \frac{(bc - ad)(a + bx)^{5/2}}{8b^2} \\
 &= -\frac{3(bc - ad)^3 \sqrt{a + bx} \sqrt{c + dx}}{64b^2 d^2} + \frac{(bc - ad)^2 (a + bx)^{3/2} \sqrt{c + dx}}{32b^2 d} + \frac{(bc - ad)(a + bx)^{5/2}}{8b^2}
 \end{aligned}$$

Mathematica [A] time = 0.57, size = 193, normalized size = 1.02

$$\frac{3(bc - ad)^{9/2} \sqrt{\frac{b(c+dx)}{bc-ad}} \sinh^{-1}\left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{bc-ad}}\right) - b\sqrt{d} \sqrt{a+bx} (c + dx) (3a^3 d^3 - a^2 b d^2 (11c + 2dx) - ab^2 d (11c^2 + 44cdx))}{64b^3 d^{5/2} \sqrt{c + dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)*(c + d*x)^(3/2),x]

[Out]
$$\begin{aligned} & -(b\sqrt{d}\sqrt{a+bx})(c+dx)(3a^3d^3 - a^2bd^2(11c+2dx) \\ & - ab^2d(11c^2 + 44cdx + 24d^2x^2) + b^3(3c^3 - 2c^2dx - 24cd^2x^2 - 16d^3x^3)) + 3(b^3c - a^3d)^{9/2} \sqrt{\frac{b(c+dx)}{b^3c - a^3d}} \\ &) * \text{ArcSinh}\left[\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b^3c - a^3d}}\right] / (64b^3d^{5/2}\sqrt{c+dx}) \end{aligned}$$

fricas [A] time = 0.49, size = 534, normalized size = 2.83

$$\left[\frac{3(b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + bc + a^2d))}{\dots} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(3/2),x, algorithm="fricas")

[Out]
$$\begin{aligned} & [1/256*(3*(b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4)*\sqrt{bd}*\log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + bc + a^2d)) \\ & * \sqrt{bd}*\sqrt{bx+a}*\sqrt{dx+c} + 8*(b^2cd + ab^2d^2)*x) + 4*(16b^4d^4x^3 - 3b^4c^3d + 11ab^3c^2d^2 + 11a^2b^2c^2d^3 - 3a^3bd^4 + 24*(b^4cd^3 + ab^3d^4)*x^2 + 2*(b^4c^2d^2 + 22ab^3cd^3 + a^2b^2d^4)*x) \\ & *\sqrt{bx+a}*\sqrt{dx+c}) / (b^3d^3), -1/128*(3*(b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4)*\sqrt{-bd}*\arctan(1/2*(2b^2dx + bc + a^2d)*\sqrt{-bd}*\sqrt{bx+a}*\sqrt{dx+c}) \\ & / (b^2d^2x^2 + ab^2cd + (b^2cd + ab^2d^2)*x)) - 2*(16b^4d^4x^3 - 3b^4c^3d + 11ab^3c^2d^2 + 11a^2b^2c^2d^3 - 3a^3bd^4 + 24*(b^4cd^3 + ab^3d^4)*x^2 + 2*(b^4c^2d^2 + 22ab^3cd^3 + a^2b^2d^4)*x) \\ & *\sqrt{bx+a}*\sqrt{dx+c}) / (b^3d^3)] \end{aligned}$$

giac [B] time = 1.89, size = 1071, normalized size = 5.67

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(3/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & 1/192*(8*(\sqrt{b^2c + (bx+a)*bd - a*bd})*\sqrt{bx+a}*(2*(bx+a)*(4 \\ & *(bx+a)/b^2 + (b^6cd^3 - 13ab^5d^4)/(b^7d^4)) - 3*(b^7c^2d^2 + 2 \\ & *ab^6cd^3 - 11a^2b^5d^4)/(b^7d^4)) - 3*(b^3c^3 + ab^2c^2d + 3a^2 \\ & *b^2cd^2 - 5a^3d^3)*\log(\text{abs}(-\sqrt{bd})*\sqrt{bx+a} + \sqrt{b^2c + (bx+a)*bd - a*bd})) / (\sqrt{bd}*b^2d^2)*c*\text{abs}(b) - 192*((b^2c - a*bd)*\log \end{aligned}$$

$$\frac{(\text{abs}(-\sqrt{b*d})\sqrt{b*x+a} + \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})/\sqrt{b*d} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})\sqrt{b*x+a}) * a^2*c*\text{abs}(b)/b^2 + (\sqrt{b^2*c + (b*x+a)*b*d - a*b*d}) * (2*(b*x+a) * (4*(b*x+a) * (6*(b*x+a)/b^3 + (b^{12}*c*d^5 - 25*a*b^{11}*d^6)/(b^{14}*d^6)) - (5*b^{13}*c^2*d^4 + 14*a*b^{12}*c*d^5 - 163*a^2*b^{11}*d^6)/(b^{14}*d^6)) + 3*(5*b^{14}*c^3*d^3 + 9*a*b^{13}*c^2*d^4 + 15*a^2*b^{12}*c*d^5 - 93*a^3*b^{11}*d^6)/(b^{14}*d^6)) * \sqrt{b*x+a} + 3 * (5*b^4*c^4 + 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 + 20*a^3*b*c*d^3 - 35*a^4*d^4) * \log(\text{abs}(-\sqrt{b*d})\sqrt{b*x+a} + \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})) / (\sqrt{b*d} * b^2 * d^3) * d * \text{abs}(b) + 16 * (\sqrt{b^2*c + (b*x+a)*b*d - a*b*d}) * \sqrt{b*x+a} * (2*(b*x+a) * (4*(b*x+a)/b^2 + (b^6*c*d^3 - 13*a*b^5*d^4)/(b^7*d^4)) - 3*(b^7*c^2*d^2 + 2*a*b^6*c*d^3 - 11*a^2*b^5*d^4)/(b^7*d^4)) - 3 * (b^3*c^3 + a*b^2*c^2*d + 3*a^2*b*c*d^2 - 5*a^3*d^3) * \log(\text{abs}(-\sqrt{b*d})\sqrt{b*x+a} + \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})) / (\sqrt{b*d} * b * d^2) * a * d * \text{abs}(b) / b + 96 * (\sqrt{b^2*c + (b*x+a)*b*d - a*b*d}) * (2*b*x + 2*a + (b*c*d - 5*a*d^2)/d^2) * \sqrt{b*x+a} + (b^3*c^2 + 2*a*b^2*c*d - 3*a^2*b*d^2) * \log(\text{abs}(-\sqrt{b*d})\sqrt{b*x+a} + \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})) / (\sqrt{b*d} * d) * a * c * \text{abs}(b) / b^2 + 48 * (\sqrt{b^2*c + (b*x+a)*b*d - a*b*d}) * (2*b*x + 2*a + (b*c*d - 5*a*d^2)/d^2) * \sqrt{b*x+a} + (b^3*c^2 + 2*a*b^2*c*d - 3*a^2*b*d^2) * \log(\text{abs}(-\sqrt{b*d})\sqrt{b*x+a} + \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})) / (\sqrt{b*d} * d) * a^2 * d * \text{abs}(b) / b^3) / b$$

maple [B] time = 0.01, size = 640, normalized size = 3.39

$$\frac{3\sqrt{(bx+a)(dx+c)} a^4 d^2 \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bd} x^2 + ac + (ad+bc)x\right)}{128\sqrt{dx+c} \sqrt{bx+a} \sqrt{bd} b^2} - \frac{3\sqrt{(bx+a)(dx+c)} a^3 cd \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}}\right)}{32\sqrt{dx+c} \sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)*(d*x+c)^(3/2),x)

[Out] 1/4/d*(b*x+a)^(3/2)*(d*x+c)^(5/2)+1/8/d*(b*x+a)^(1/2)*(d*x+c)^(5/2)*a-1/8/d^2*(b*x+a)^(1/2)*(d*x+c)^(5/2)*b*c+1/32/b*(d*x+c)^(3/2)*(b*x+a)^(1/2)*a^2-1/16/d*(d*x+c)^(3/2)*(b*x+a)^(1/2)*a*c+1/32/d^2*(d*x+c)^(3/2)*(b*x+a)^(1/2)*c^2*b-3/64*d/b^2*(d*x+c)^(1/2)*(b*x+a)^(1/2)*a^3+9/64/b*(d*x+c)^(1/2)*(b*x+a)^(1/2)*a^2*c-9/64/d*(d*x+c)^(1/2)*(b*x+a)^(1/2)*a*c^2+3/64/d^2*(d*x+c)^(1/2)*(b*x+a)^(1/2)*c^3*b+3/128*d^2/b^2*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*a^4-3/32*d/b*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*a^3*c+9/64*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*a^2*c^2-3/32/d*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*a*c^3*b+3/128/d^2*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)

$$\frac{\ln\left(\frac{(b*d*x+1/2*a*d+1/2*b*c)}{(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2}}\right)}{(b*d)^{1/2}*c^4*b^2}$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + b x)^{3/2} (c + d x)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)*(c + d*x)^(3/2),x)

[Out] int((a + b*x)^(3/2)*(c + d*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + b x)^{\frac{3}{2}} (c + d x)^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)*(d*x+c)**(3/2),x)

[Out] Integral((a + b*x)**(3/2)*(c + d*x)**(3/2), x)

3.1473 $\int \sqrt{a+bx}(c+dx)^{3/2} dx$

Optimal. Leaf size=151

$$-\frac{(bc-ad)^3 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{8b^{5/2}d^{3/2}} + \frac{\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}{8b^2d} + \frac{(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)}{4b^2} + \frac{(a+bx)^{3/2}(c+dx)^{3/2}}{3b}$$

[Out] $1/3*(b*x+a)^{(3/2)}*(d*x+c)^{(3/2)}/b-1/8*(-a*d+b*c)^3*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(5/2)}/d^{(3/2)}+1/4*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/b^2+1/8*(-a*d+b*c)^2*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b^2/d$

Rubi [A] time = 0.07, antiderivative size = 151, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$-\frac{(bc-ad)^3 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{8b^{5/2}d^{3/2}} + \frac{\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}{8b^2d} + \frac{(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)}{4b^2} + \frac{(a+bx)^{3/2}(c+dx)^{3/2}}{3b}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[a + b*x]*(c + d*x)^(3/2), x]`

[Out] $((b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(8*b^2*d) + ((b*c - a*d)*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(4*b^2) + ((a + b*x)^{(3/2)}*(c + d*x)^{(3/2)})/(3*b) - ((b*c - a*d)^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/(8*b^{(5/2)}*d^{(3/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```


Rule 206

$\text{Int}[(a_ + (b_ .)*(x_)^2)^{-1}, x_Symbol] \text{ :> Simp}[(1*\text{ArcTanh}[\text{Rt}[-b, 2]*x]/\text{Rt}[a, 2]])/(\text{Rt}[a, 2]*\text{Rt}[-b, 2]), x] \text{ /; FreeQ}\{a, b\}, x\} \ \&\& \ \text{NegQ}[a/b] \ \&\& \ (\text{GtQ}[a, 0] \ || \ \text{LtQ}[b, 0])$

Rule 217

$\text{Int}[1/\text{Sqrt}[(a_) + (b_ .)*(x_)^2], x_Symbol] \text{ :> Subst}[\text{Int}[1/(1 - b*x^2), x], x, x/\text{Sqrt}[a + b*x^2]] \text{ /; FreeQ}\{a, b\}, x\} \ \&\& \ !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned} \int \sqrt{a+bx}(c+dx)^{3/2} dx &= \frac{(a+bx)^{3/2}(c+dx)^{3/2}}{3b} + \frac{(bc-ad) \int \sqrt{a+bx} \sqrt{c+dx} dx}{2b} \\ &= \frac{(bc-ad)(a+bx)^{3/2} \sqrt{c+dx}}{4b^2} + \frac{(a+bx)^{3/2}(c+dx)^{3/2}}{3b} + \frac{(bc-ad)^2 \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{8b^2} \\ &= \frac{(bc-ad)^2 \sqrt{a+bx} \sqrt{c+dx}}{8b^2 d} + \frac{(bc-ad)(a+bx)^{3/2} \sqrt{c+dx}}{4b^2} + \frac{(a+bx)^{3/2}(c+dx)^{3/2}}{3b} \\ &= \frac{(bc-ad)^2 \sqrt{a+bx} \sqrt{c+dx}}{8b^2 d} + \frac{(bc-ad)(a+bx)^{3/2} \sqrt{c+dx}}{4b^2} + \frac{(a+bx)^{3/2}(c+dx)^{3/2}}{3b} \\ &= \frac{(bc-ad)^2 \sqrt{a+bx} \sqrt{c+dx}}{8b^2 d} + \frac{(bc-ad)(a+bx)^{3/2} \sqrt{c+dx}}{4b^2} + \frac{(a+bx)^{3/2}(c+dx)^{3/2}}{3b} \\ &= \frac{(bc-ad)^2 \sqrt{a+bx} \sqrt{c+dx}}{8b^2 d} + \frac{(bc-ad)(a+bx)^{3/2} \sqrt{c+dx}}{4b^2} + \frac{(a+bx)^{3/2}(c+dx)^{3/2}}{3b} \end{aligned}$$

Mathematica [A] time = 0.44, size = 152, normalized size = 1.01

$$\frac{-b\sqrt{d} \sqrt{a+bx}(c+dx)(3a^2d^2 - 2abd(4c+dx) - (b^2(3c^2 + 14cdx + 8d^2x^2))) - 3(bc-ad)^{7/2} \sqrt{\frac{b(c+dx)}{bc-ad}} \sinh^{-1}\left(\frac{b(c+dx)}{bc-ad}\right)}{24b^3d^{3/2}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]*(c + d*x)^(3/2), x]

```
[Out] 
$$\frac{-(b\sqrt{d})\sqrt{a+bx}(c+dx)(3a^2d^2 - 2abd(4c+dx) - b^2(3c^2 + 14cdx + 8d^2x^2)) - 3(b^2c - a^2d)^{7/2}\sqrt{(b(c+dx))/(b^2c - a^2d)}}{(24b^3d^{3/2})\sqrt{c+dx}} \operatorname{ArcSinh}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b^2c - a^2d}}\right)$$

```

fricas [A] time = 0.48, size = 410, normalized size = 2.72

$$\frac{3(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + bc + ad)\sqrt{bd}\sqrt{bx+a})}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(1/2)*(d*x+c)^(3/2),x, algorithm="fricas")
```

```
[Out] 
$$\frac{-1/96(3(b^3c^3 - 3a^2b^2cd + 3a^2b^2cd^2 - a^3d^3)\sqrt{bd})\log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + bc + ad)\sqrt{bd}\sqrt{bx+a}) + 8(b^2cd + a^2bd^2)x - 4(8b^3d^3x^2 + 3b^3c^2d + 8a^2b^2cd^2 - 3a^2b^2d^3 + 2(7b^3cd^2 + a^2b^2d^3)x)\sqrt{bd}}{(b^3d^2)} + \frac{1/48(3(b^3c^3 - 3a^2b^2cd + 3a^2b^2cd^2 - a^3d^3)\sqrt{bd})\arctan\left(\frac{1/2(2bdx + bc + ad)\sqrt{bd}}{\sqrt{b^2c + (bx+a)bd - abd}}\right) + 2(8b^3d^3x^2 + 3b^3c^2d + 8a^2b^2cd^2 - 3a^2b^2d^3 + 2(7b^3cd^2 + a^2b^2d^3)x)\sqrt{bd}}{(b^3d^2)}$$

```

giac [B] time = 1.61, size = 576, normalized size = 3.81

$$\frac{24 \left(\frac{(b^2c - abd) \log\left(\frac{-\sqrt{bd}\sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd}}{\sqrt{bd}}\right) - \sqrt{b^2c + (bx+a)bd - abd} \sqrt{bx+a}}{b^2} \right) \operatorname{arctan}\left(\frac{\sqrt{b^2c + (bx+a)bd - abd} \sqrt{bx+a}}{2(bx+a)\left(\frac{4(bx+a)}{b^2} + \frac{b^6cd^3 - 13}{b^7d^4}\right)}\right)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(1/2)*(d*x+c)^(3/2),x, algorithm="giac")
```

```
[Out] 
$$\frac{-1/24(24((b^2c - a^2bd)\log(\operatorname{abs}(-\sqrt{bd})\sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - a^2bd})))/\sqrt{bd} - \sqrt{b^2c + (bx+a)bd - a^2bd}\sqrt{bx+a})\operatorname{arctan}\left(\frac{\sqrt{b^2c + (bx+a)bd - a^2bd}\sqrt{bx+a}}{2(bx+a)\left(\frac{4(bx+a)}{b^2} + \frac{b^6cd^3 - 13}{b^7d^4}\right)}\right) - 3(b^7c^2d^2 + 2a^2b^6cd^3 - 11a^2b^5d^4)/b^7d^4 - 3(b^3c^3 + a^2b^2c^2d + 3a^2b^2cd^2 - 5a^3d^3)\log(\operatorname{abs}(-\sqrt{bd})\sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - a^2bd}))}{(b^3d^2)} + \frac{d\operatorname{abs}(b)/b - 6(\sqrt{b^2c + (bx+a)bd - a^2bd})(2bx + 2a + (b^2cd - 5a^2d^2)/d^2)}{b^2}$$

```

$\sqrt{bx+a} + (b^3c^2 + 2ab^2cd - 3a^2bd^2) \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - ab^2d}) / (\sqrt{bd}d) * c * \text{abs}(b) / b^2 - 6 * (\sqrt{b^2c + (bx+a)bd - ab^2d}) * (2bx + 2a + (b^2cd - 5a^2d^2) / d^2) * \sqrt{bx+a} + (b^3c^2 + 2ab^2cd - 3a^2bd^2) \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - ab^2d}) / (\sqrt{bd}d) * a * d * \text{abs}(b) / b^3 / b$

maple [B] time = 0.01, size = 459, normalized size = 3.04

$$\frac{\sqrt{(bx+a)(dx+c)} a^3 d^2 \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bd}x^2 + ac + (ad+bc)x\right)}{16\sqrt{dx+c} \sqrt{bx+a} \sqrt{bd} b^2} - \frac{3\sqrt{(bx+a)(dx+c)} a^2 cd \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}}\right)}{16\sqrt{dx+c} \sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)*(d*x+c)^(3/2), x)

[Out] $\frac{1}{3}d*(b*x+a)^{(1/2)}*(d*x+c)^{(5/2)} + \frac{1}{12}b*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*a^{-1/12} / d*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*c^{-1/8}d/b^2*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a^2 + \frac{1}{4}b*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a*c^{-1/8} / d*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*c^2 + \frac{1}{16}d^2/b^2*((b*x+a)*(d*x+c))^{(1/2)} / (d*x+c)^{(1/2)} / (b*x+a)^{(1/2)} * \ln((b*d*x + 1/2*a*d + 1/2*b*c) / (b*d)^{(1/2)} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{(1/2)}) / (b*d)^{(1/2)} * a^3 - \frac{3}{16}d/b*((b*x+a)*(d*x+c))^{(1/2)} / (d*x+c)^{(1/2)} / (b*x+a)^{(1/2)} * \ln((b*d*x + 1/2*a*d + 1/2*b*c) / (b*d)^{(1/2)} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{(1/2)}) / (b*d)^{(1/2)} * a^2 * c + \frac{3}{16}*((b*x+a)*(d*x+c))^{(1/2)} / (d*x+c)^{(1/2)} / (b*x+a)^{(1/2)} * \ln((b*d*x + 1/2*a*d + 1/2*b*c) / (b*d)^{(1/2)} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{(1/2)}) / (b*d)^{(1/2)} * a * c^2 - \frac{1}{16}d*((b*x+a)*(d*x+c))^{(1/2)} / (d*x+c)^{(1/2)} / (b*x+a)^{(1/2)} * \ln((b*d*x + 1/2*a*d + 1/2*b*c) / (b*d)^{(1/2)} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{(1/2)}) / (b*d)^{(1/2)} * c^3 * b$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(3/2), x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{a+bx} (c+dx)^{3/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(1/2)*(c + d*x)^(3/2),x)
```

```
[Out] int((a + b*x)^(1/2)*(c + d*x)^(3/2), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(1/2)*(d*x+c)**(3/2),x)
```

```
[Out] Timed out
```

$$3.1474 \quad \int \frac{(c+dx)^{3/2}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=113

$$\frac{3(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{4b^{5/2}\sqrt{d}} + \frac{3\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}{4b^2} + \frac{\sqrt{a+bx}(c+dx)^{3/2}}{2b}$$

[Out] $3/4*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(5/2)}/d^{(1/2)}+1/2*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}/b+3/4*(-a*d+b*c)*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b^2$

Rubi [A] time = 0.05, antiderivative size = 113, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$\frac{3\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}{4b^2} + \frac{3(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{4b^{5/2}\sqrt{d}} + \frac{\sqrt{a+bx}(c+dx)^{3/2}}{2b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2)/Sqrt[a + b*x], x]

[Out] $(3*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(4*b^2) + (\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/2)})/(2*b) + (3*(b*c - a*d)^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/(4*b^{(5/2)}*\operatorname{Sqrt}[d])$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

$\text{Int}[(a_ + (b_ \cdot)(x_)^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(1 \cdot \text{ArcTanh}[\text{Rt}[-b, 2] \cdot x] / \text{Rt}[a, 2]) / (\text{Rt}[a, 2] \cdot \text{Rt}[-b, 2]), x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[a/b] \ \&\& \ (\text{GtQ}[a, 0] \ || \ \text{LtQ}[b, 0])$

Rule 217

$\text{Int}[1/\text{Sqrt}[(a_ + (b_ \cdot)(x_)^2), x_Symbol] \rightarrow \text{Subst}[\text{Int}[1/(1 - b \cdot x^2), x], x, x/\text{Sqrt}[a + b \cdot x^2]] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned} \int \frac{(c + dx)^{3/2}}{\sqrt{a + bx}} dx &= \frac{\sqrt{a + bx} (c + dx)^{3/2}}{2b} + \frac{(3(bc - ad)) \int \frac{\sqrt{c + dx}}{\sqrt{a + bx}} dx}{4b} \\ &= \frac{3(bc - ad)\sqrt{a + bx} \sqrt{c + dx}}{4b^2} + \frac{\sqrt{a + bx} (c + dx)^{3/2}}{2b} + \frac{(3(bc - ad)^2) \int \frac{1}{\sqrt{a + bx} \sqrt{c + dx}} dx}{8b^2} \\ &= \frac{3(bc - ad)\sqrt{a + bx} \sqrt{c + dx}}{4b^2} + \frac{\sqrt{a + bx} (c + dx)^{3/2}}{2b} + \frac{(3(bc - ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{c - \frac{ad}{b} + \frac{dx^2}{b}}} dx, x, \frac{\sqrt{a + bx}}{\sqrt{c + dx}} \right)}{4b^3} \\ &= \frac{3(bc - ad)\sqrt{a + bx} \sqrt{c + dx}}{4b^2} + \frac{\sqrt{a + bx} (c + dx)^{3/2}}{2b} + \frac{(3(bc - ad)^2) \text{Subst} \left(\int \frac{1}{1 - \frac{dx^2}{b}} dx, x, \frac{\sqrt{a + bx}}{\sqrt{c + dx}} \right)}{4b^3} \\ &= \frac{3(bc - ad)\sqrt{a + bx} \sqrt{c + dx}}{4b^2} + \frac{\sqrt{a + bx} (c + dx)^{3/2}}{2b} + \frac{3(bc - ad)^2 \tanh^{-1} \left(\frac{\sqrt{d} \sqrt{a + bx}}{\sqrt{b} \sqrt{c + dx}} \right)}{4b^{5/2} \sqrt{d}} \end{aligned}$$

Mathematica [A] time = 0.29, size = 109, normalized size = 0.96

$$\frac{\sqrt{c + dx} \left(\sqrt{a + bx} (-3ad + 5bc + 2bdx) + \frac{3(bc - ad)^{3/2} \sinh^{-1} \left(\frac{\sqrt{d} \sqrt{a + bx}}{\sqrt{bc - ad}} \right)}{\sqrt{d} \sqrt{\frac{b(c + dx)}{bc - ad}}} \right)}{4b^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/2)/Sqrt[a + b*x], x]

[Out] $(\sqrt{c + dx} * (\sqrt{a + bx} * (5 * b * c - 3 * a * d + 2 * b * d * x) + (3 * (b * c - a * d))^{3/2} * \text{ArcSinh}[(\sqrt{d} * \sqrt{a + bx}) / \sqrt{b * c - a * d}])) / (\sqrt{d} * \sqrt{(b * (c + d * x)) / (b * c - a * d)})) / (4 * b^2)$

fricas [A] time = 0.47, size = 306, normalized size = 2.71

$$\left[\frac{3(b^2c^2 - 2abcd + a^2d^2)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + bc + ad)\sqrt{bd} \sqrt{bx + a} \sqrt{dx + c} + \dots)}{16b^3d} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(3/2)/(b*x+a)^(1/2),x, algorithm="fricas")`

[Out] $[1/16 * (3 * (b^2 * c^2 - 2 * a * b * c * d + a^2 * d^2) * \sqrt{b * d} * \log(8 * b^2 * d^2 * x^2 + b^2 * c^2 + 6 * a * b * c * d + a^2 * d^2 + 4 * (2 * b * d * x + b * c + a * d) * \sqrt{b * d} * \sqrt{b * x + a} * \sqrt{d * x + c} + 8 * (b^2 * c * d + a * b * d^2) * x) + 4 * (2 * b^2 * d^2 * x + 5 * b^2 * c * d - 3 * a * b * d^2) * \sqrt{b * x + a} * \sqrt{d * x + c}) / (b^3 * d), -1/8 * (3 * (b^2 * c^2 - 2 * a * b * c * d + a^2 * d^2) * \sqrt{-b * d} * \arctan(1/2 * (2 * b * d * x + b * c + a * d) * \sqrt{-b * d} * \sqrt{b * x + a} * \sqrt{d * x + c}) / (b^2 * d^2 * x^2 + a * b * c * d + (b^2 * c * d + a * b * d^2) * x)) - 2 * (2 * b^2 * d^2 * x + 5 * b^2 * c * d - 3 * a * b * d^2) * \sqrt{b * x + a} * \sqrt{d * x + c}) / (b^3 * d)]$

giac [B] time = 1.25, size = 233, normalized size = 2.06

$$\frac{4 \left(\frac{(b^2c - abd) \log\left(\left| -\sqrt{bd} \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd} \right| \right)}{\sqrt{bd}} - \sqrt{b^2c + (bx+a)bd - abd} \sqrt{bx+a} \right) c |b|}{b^2} - \frac{\left(\sqrt{b^2c + (bx+a)bd - abd} \left(2bx + 2a + \frac{bcd - 5ad^2}{d^2} \right) \sqrt{bx+a} + \dots \right)}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(3/2)/(b*x+a)^(1/2),x, algorithm="giac")`

[Out] $-1/4 * (4 * ((b^2 * c - a * b * d) * \log(\text{abs}(-\sqrt{b * d} * \sqrt{b * x + a} + \sqrt{b^2 * c + (b * x + a) * b * d - a * b * d})) / \sqrt{b * d} - \sqrt{b^2 * c + (b * x + a) * b * d - a * b * d}) * \sqrt{(b * x + a) * c * \text{abs}(b) / b^2 - (\sqrt{b^2 * c + (b * x + a) * b * d - a * b * d}) * (2 * b * x + 2 * a + (b * c * d - 5 * a * d^2) / d^2) * \sqrt{b * x + a} + (b^3 * c^2 + 2 * a * b^2 * c * d - 3 * a^2 * b * d^2) * \log(\text{abs}(-\sqrt{b * d} * \sqrt{b * x + a} + \sqrt{b^2 * c + (b * x + a) * b * d - a * b * d})) / (\sqrt{b * d} * d)) * d * \text{abs}(b) / b^3) / b$

maple [B] time = 0.01, size = 308, normalized size = 2.73

$$\frac{3\sqrt{(bx+a)(dx+c)} a^2 d^2 \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad + bc)x}\right)}{8\sqrt{dx+c} \sqrt{bx+a} \sqrt{bd} b^2} - \frac{3\sqrt{(bx+a)(dx+c)} acd \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}}\right)}{4\sqrt{dx+c} \sqrt{bx+a}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(3/2)/(b*x+a)^(1/2),x)`

[Out] $\frac{1}{4} \frac{1}{b} \frac{(d^2x^2+c^2)^{3/2} (bx+a)^{1/2}}{(d^2x^2+c^2)^{1/2} (bx+a)^{1/2}} - \frac{3}{4} \frac{1}{b^2} \frac{(d^2x^2+c^2)^{1/2} (bx+a)^{1/2} a^2 d^3}{(d^2x^2+c^2)^{1/2} (bx+a)^{1/2}} + \frac{3}{8} \frac{1}{b^2} \frac{(d^2x^2+c^2)^{1/2} (bx+a)^{1/2} c^3}{(d^2x^2+c^2)^{1/2} (bx+a)^{1/2}} + \frac{1}{b^2} \frac{(d^2x^2+c^2)^{1/2} (bx+a)^{1/2} \ln\left(\frac{bd^2x+1/2ad+1/2b^2c}{(bd)^{1/2}+(bd^2x^2+ac+(ad+bc)x)^{1/2}}\right)}{(bd)^{1/2} a^2 d^2 - 3/4 b^2} + \frac{1}{b^2} \frac{(d^2x^2+c^2)^{1/2} (bx+a)^{1/2} \ln\left(\frac{bd^2x+1/2ad+1/2b^2c}{(bd)^{1/2}+(bd^2x^2+ac+(ad+bc)x)^{1/2}}\right)}{(bd)^{1/2} a^2 d^2 c + 3/8 b^2} + \frac{1}{b^2} \frac{(d^2x^2+c^2)^{1/2} (bx+a)^{1/2} \ln\left(\frac{bd^2x+1/2ad+1/2b^2c}{(bd)^{1/2}+(bd^2x^2+ac+(ad+bc)x)^{1/2}}\right)}{(bd)^{1/2} c^2}$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(3/2)/(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details) Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c+dx)^{3/2}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c+d*x)^(3/2)/(a+b*x)^(1/2),x)`

[Out] `int((c+d*x)^(3/2)/(a+b*x)^(1/2),x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c+dx)^{3/2}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(3/2)/(b*x+a)**(1/2),x)`

[Out] `Integral((c+d*x)**(3/2)/sqrt(a+b*x),x)`

$$3.1475 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=98

$$\frac{3\sqrt{d}(bc-ad)\tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{5/2}} + \frac{3d\sqrt{a+bx}\sqrt{c+dx}}{b^2} - \frac{2(c+dx)^{3/2}}{b\sqrt{a+bx}}$$

[Out] $3*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})*d^{(1/2)}/b^{(5/2)}-2*(d*x+c)^{(3/2)}/b/(b*x+a)^{(1/2)}+3*d*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b^2$

Rubi [A] time = 0.05, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 217, 206}

$$\frac{3d\sqrt{a+bx}\sqrt{c+dx}}{b^2} + \frac{3\sqrt{d}(bc-ad)\tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{5/2}} - \frac{2(c+dx)^{3/2}}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c+dx)^{(3/2)}/(a+bx)^{(3/2)}, x]$

[Out] $(3*d*\operatorname{Sqrt}[a+bx]*\operatorname{Sqrt}[c+dx])/b^2 - (2*(c+dx)^{(3/2)})/(b*\operatorname{Sqrt}[a+bx]) + (3*\operatorname{Sqrt}[d]*(b*c-a*d)*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a+bx])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c+dx])])/b^{(5/2)}$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c+dx)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c+dx)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m+n+2, 0] && (FractionQ[m] || GeQ[2*n+m+1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c+dx)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c+dx)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m+n+1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m-n, 0]))) && !ILtQ[m+n+2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{3/2}}{(a+bx)^{3/2}} dx &= -\frac{2(c+dx)^{3/2}}{b\sqrt{a+bx}} + \frac{(3d) \int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx}{b} \\
&= \frac{3d\sqrt{a+bx}\sqrt{c+dx}}{b^2} - \frac{2(c+dx)^{3/2}}{b\sqrt{a+bx}} + \frac{(3d(bc-ad)) \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{2b^2} \\
&= \frac{3d\sqrt{a+bx}\sqrt{c+dx}}{b^2} - \frac{2(c+dx)^{3/2}}{b\sqrt{a+bx}} + \frac{(3d(bc-ad)) \operatorname{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \sqrt{a+bx}\right)}{b^3} \\
&= \frac{3d\sqrt{a+bx}\sqrt{c+dx}}{b^2} - \frac{2(c+dx)^{3/2}}{b\sqrt{a+bx}} + \frac{(3d(bc-ad)) \operatorname{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}}\right)}{b^3} \\
&= \frac{3d\sqrt{a+bx}\sqrt{c+dx}}{b^2} - \frac{2(c+dx)^{3/2}}{b\sqrt{a+bx}} + \frac{3\sqrt{d}(bc-ad) \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 71, normalized size = 0.72

$$\frac{2(c+dx)^{3/2} {}_2F_1\left(-\frac{3}{2}, -\frac{1}{2}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/2)/(a + b*x)^(3/2), x]

[Out] $(-2*(c + d*x)^{3/2}*\text{Hypergeometric2F1}[-3/2, -1/2, 1/2, (d*(a + b*x))/(-(b*c) + a*d)])/(b*\text{Sqrt}[a + b*x]*((b*(c + d*x))/(b*c - a*d))^{3/2})$

fricas [A] time = 0.51, size = 311, normalized size = 3.17

$$\left[\frac{3(abc - a^2d + (b^2c - abd)x)\sqrt{\frac{d}{b}} \log\left(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 - 4(2b^2dx + b^2c + abd)\sqrt{bx+a}\sqrt{dx-a}\right)}{4(b^3x + ab^2)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(3/2), x, algorithm="fricas")

[Out] $[-1/4*(3*(a*b*c - a^2*d + (b^2*c - a*b*d)*x)*\text{sqrt}(d/b)*\log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 - 4*(2*b^2*d*x + b^2*c + a*b*d)*\text{sqrt}(b*x + a)*\text{sqrt}(d*x + c)*\text{sqrt}(d/b) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(b*d*x - 2*b*c + 3*a*d)*\text{sqrt}(b*x + a)*\text{sqrt}(d*x + c))/(b^3*x + a*b^2), -1/2*(3*(a*b*c - a^2*d + (b^2*c - a*b*d)*x)*\text{sqrt}(-d/b)*\arctan(1/2*(2*b*d*x + b*c + a*d)*\text{sqrt}(b*x + a)*\text{sqrt}(d*x + c)*\text{sqrt}(-d/b)/(b*d^2*x^2 + a*c*d + (b*c*d + a*d^2)*x)) - 2*(b*d*x - 2*b*c + 3*a*d)*\text{sqrt}(b*x + a)*\text{sqrt}(d*x + c))/(b^3*x + a*b^2)]$

giac [B] time = 1.50, size = 204, normalized size = 2.08

$$\frac{\sqrt{b^2c + (bx+a)bd - abd} \sqrt{bx+a} d|b|}{b^4} \frac{3(\sqrt{bd} bc|b| - \sqrt{bd} ad|b|) \log\left(\left(\sqrt{bd} \sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}\right)\right)}{2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(3/2), x, algorithm="giac")

[Out] $\text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)*\text{sqrt}(b*x + a)*d*\text{abs}(b)/b^4 - 3/2*(\text{sqrt}(b*d)*b*c*\text{abs}(b) - \text{sqrt}(b*d)*a*d*\text{abs}(b))*\log((\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}$

$$\frac{(b^2c + (bx + a)bd - ab^2d)^2/b^4 - 4(\sqrt{bd})b^2c^2\sqrt{b} - 2\sqrt{bd}abc\sqrt{b} + \sqrt{bd}a^2d^2\sqrt{b}}{(b^2c - ab^2d - (\sqrt{bd})\sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - ab^2d})^2b^3}$$

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{3}{2}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/2)/(b*x+a)^(3/2),x)

[Out] int((d*x+c)^(3/2)/(b*x+a)^(3/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{3/2}}{(a + bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(3/2)/(a + b*x)^(3/2),x)

[Out] int((c + d*x)^(3/2)/(a + b*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{3}{2}}}{(a + bx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(3/2)/(b*x+a)**(3/2),x)

[Out] Integral((c + d*x)**(3/2)/(a + b*x)**(3/2), x)

$$3.1476 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=92

$$\frac{2d^{3/2} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{5/2}} - \frac{2d\sqrt{c+dx}}{b^2\sqrt{a+bx}} - \frac{2(c+dx)^{3/2}}{3b(a+bx)^{3/2}}$$

[Out] $-2/3*(d*x+c)^{(3/2)}/b/(b*x+a)^{(3/2)}+2*d^{(3/2)}*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)/(d*x+c)^{(1/2)})/b^{(5/2)}-2*d*(d*x+c)^{(1/2)}/b^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 63, 217, 206}

$$\frac{2d^{3/2} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{5/2}} - \frac{2d\sqrt{c+dx}}{b^2\sqrt{a+bx}} - \frac{2(c+dx)^{3/2}}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(3/2)}/(a + b*x)^{(5/2)}, x]$

[Out] $(-2*d*\operatorname{Sqrt}[c + d*x])/(b^2*\operatorname{Sqrt}[a + b*x]) - (2*(c + d*x)^{(3/2)})/(3*b*(a + b*x)^{(3/2)}) + (2*d^{(3/2)}*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/b^{(5/2)}$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{GtQ}[n, 0] \ \&\& \operatorname{LtQ}[m, -1] \ \&\& \operatorname{IntegerQ}[n] \ \&\& \operatorname{IntegerQ}[m] \ \&\& \operatorname{IntegerQ}[m + n + 2, 0] \ \&\& (\operatorname{FractionQ}[m] \ \|\ \operatorname{GeQ}[2*n + m + 1, 0]) \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{LtQ}[-1, m, 0] \ \&\& \operatorname{LeQ}[-1, n, 0] \ \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{3/2}}{(a+bx)^{5/2}} dx &= -\frac{2(c+dx)^{3/2}}{3b(a+bx)^{3/2}} + \frac{d \int \frac{\sqrt{c+dx}}{(a+bx)^{3/2}} dx}{b} \\
&= -\frac{2d\sqrt{c+dx}}{b^2\sqrt{a+bx}} - \frac{2(c+dx)^{3/2}}{3b(a+bx)^{3/2}} + \frac{d^2 \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{b^2} \\
&= -\frac{2d\sqrt{c+dx}}{b^2\sqrt{a+bx}} - \frac{2(c+dx)^{3/2}}{3b(a+bx)^{3/2}} + \frac{(2d^2) \operatorname{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \sqrt{a+bx}\right)}{b^3} \\
&= -\frac{2d\sqrt{c+dx}}{b^2\sqrt{a+bx}} - \frac{2(c+dx)^{3/2}}{3b(a+bx)^{3/2}} + \frac{(2d^2) \operatorname{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}}\right)}{b^3} \\
&= -\frac{2d\sqrt{c+dx}}{b^2\sqrt{a+bx}} - \frac{2(c+dx)^{3/2}}{3b(a+bx)^{3/2}} + \frac{2d^{3/2} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{5/2}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.79

$$-\frac{2(c+dx)^{3/2} {}_2F_1\left(-\frac{3}{2}, -\frac{3}{2}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a+bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad}\right)^{3/2}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^(3/2)/(a + b*x)^(5/2), x]
```

```
[Out] (-2*(c + d*x)^(3/2)*Hypergeometric2F1[-3/2, -3/2, -1/2, (d*(a + b*x))/(-(b*c)
+ a*d)]/(3*b*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(3/2))
```

fricas [B] time = 0.60, size = 325, normalized size = 3.53

$$\frac{3 \left(b^2 dx^2 + 2 abdx + a^2 d \right) \sqrt{\frac{d}{b}} \log \left(8 b^2 d^2 x^2 + b^2 c^2 + 6 abcd + a^2 d^2 + 4 \left(2 b^2 dx + b^2 c + abd \right) \sqrt{bx + a} \sqrt{dx + c} \right)}{6 \left(b^4 x^2 + 2 ab^3 x + a^2 b^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(5/2),x, algorithm="fricas")

[Out] [1/6*(3*(b^2*d*x^2 + 2*a*b*d*x + a^2*d)*sqrt(d/b)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b^2*d*x + b^2*c + a*b*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(d/b) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(4*b*d*x + b*c + 3*a*d)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*x^2 + 2*a*b^3*x + a^2*b^2), -1/3*(3*(b^2*d*x^2 + 2*a*b*d*x + a^2*d)*sqrt(-d/b)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-d/b)/(b*d^2*x^2 + a*c*d + (b*c*d + a*d^2)*x) + 2*(4*b*d*x + b*c + 3*a*d)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*x^2 + 2*a*b^3*x + a^2*b^2)]

giac [B] time = 1.74, size = 455, normalized size = 4.95

$$\frac{\sqrt{bd} d |b| \log \left(\left(\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2 c + (bx + a)bd - abd} \right)^2 \right)}{b^4} 8 \left(2 \sqrt{bd} b^5 c^3 d |b| - 6 \sqrt{bd} ab^4 c^2 d^2 |b| + 6 \sqrt{bd} a^2 b^3 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(5/2),x, algorithm="giac")

[Out] -sqrt(b*d)*d*abs(b)*log((sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)/b^4 - 8/3*(2*sqrt(b*d)*b^5*c^3*d*abs(b) - 6*sqrt(b*d)*a*b^4*c^2*d^2*abs(b) + 6*sqrt(b*d)*a^2*b^3*c*d^3*abs(b) - 2*sqrt(b*d)*a^3*b^2*d^4*abs(b) - 3*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*b^3*c^2*d*abs(b) + 6*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a*b^2*c*d^2*abs(b) - 3*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^2*b*d^3*abs(b) + 3*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*b*c*d*abs(b) - 3*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a*d^2*abs(b))/(b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)^3*b^3)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{3}{2}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/2)/(b*x+a)^(5/2),x)

[Out] int((d*x+c)^(3/2)/(b*x+a)^(5/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{\frac{3}{2}}}{(a + bx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(3/2)/(a + b*x)^(5/2),x)

[Out] int((c + d*x)^(3/2)/(a + b*x)^(5/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{3}{2}}}{(a + bx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(3/2)/(b*x+a)**(5/2),x)

[Out] Integral((c + d*x)**(3/2)/(a + b*x)**(5/2), x)

$$3.1477 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^{7/2}} dx$$

Optimal. Leaf size=32

$$-\frac{2(c+dx)^{5/2}}{5(a+bx)^{5/2}(bc-ad)}$$

[Out] $-2/5*(d*x+c)^(5/2)/(-a*d+b*c)/(b*x+a)^(5/2)$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{2(c+dx)^{5/2}}{5(a+bx)^{5/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^(3/2)/(a + b*x)^(7/2), x]$

[Out] $(-2*(c + d*x)^(5/2))/(5*(b*c - a*d)*(a + b*x)^(5/2))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := \text{Simp}[(a + b*x)^(m + 1)*(c + d*x)^(n + 1)]/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{(c+dx)^{3/2}}{(a+bx)^{7/2}} dx = -\frac{2(c+dx)^{5/2}}{5(bc-ad)(a+bx)^{5/2}}$$

Mathematica [A] time = 0.02, size = 32, normalized size = 1.00

$$-\frac{2(c+dx)^{5/2}}{5(a+bx)^{5/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(c + d*x)^(3/2)/(a + b*x)^(7/2), x]$

[Out] $(-2*(c + d*x)^(5/2))/(5*(b*c - a*d)*(a + b*x)^(5/2))$

fricas [B] time = 0.72, size = 104, normalized size = 3.25

$$\frac{2(d^2x^2 + 2cdx + c^2)\sqrt{bx+a}\sqrt{dx+c}}{5(a^3bc - a^4d + (b^4c - ab^3d)x^3 + 3(ab^3c - a^2b^2d)x^2 + 3(a^2b^2c - a^3bd)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(7/2),x, algorithm="fricas")

[Out] -2/5*(d^2*x^2 + 2*c*d*x + c^2)*sqrt(b*x + a)*sqrt(d*x + c)/(a^3*b*c - a^4*d + (b^4*c - a*b^3*d)*x^3 + 3*(a*b^3*c - a^2*b^2*d)*x^2 + 3*(a^2*b^2*c - a^3*b*d)*x)

giac [B] time = 1.69, size = 374, normalized size = 11.69

$$\frac{4(\sqrt{bd}b^8c^4d^2|b| - 4\sqrt{bd}ab^7c^3d^3|b| + 6\sqrt{bd}a^2b^6c^2d^4|b| - 4\sqrt{bd}a^3b^5cd^5|b| + \sqrt{bd}a^4b^4d^6|b| + 10\sqrt{bd}(\sqrt{bd}\sqrt{bx+a}))}{5(a^3bc - a^4d + (b^4c - ab^3d)x^3 + 3(ab^3c - a^2b^2d)x^2 + 3(a^2b^2c - a^3bd)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(7/2),x, algorithm="giac")

[Out] -4/5*(sqrt(b*d)*b^8*c^4*d^2*abs(b) - 4*sqrt(b*d)*a*b^7*c^3*d^3*abs(b) + 6*sqrt(b*d)*a^2*b^6*c^2*d^4*abs(b) - 4*sqrt(b*d)*a^3*b^5*c*d^5*abs(b) + sqrt(b*d)*a^4*b^4*d^6*abs(b) + 10*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*b^4*c^2*d^2*abs(b) - 20*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a*b^3*c*d^3*abs(b) + 10*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^2*b^2*d^4*abs(b) + 5*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^8*d^2*abs(b))/((b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)^5*b^3)

maple [A] time = 0.00, size = 27, normalized size = 0.84

$$\frac{2(dx+c)^{\frac{5}{2}}}{5(bx+a)^{\frac{5}{2}}(ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/2)/(b*x+a)^(7/2),x)

[Out] 2/5/(b*x+a)^(5/2)*(d*x+c)^(5/2)/(a*d-b*c)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(7/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 0.80, size = 27, normalized size = 0.84

$$\frac{2(c+dx)^{5/2}}{(5ad-5bc)(a+bx)^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(3/2)/(a + b*x)^(7/2),x)

[Out] (2*(c + d*x)^(5/2))/((5*a*d - 5*b*c)*(a + b*x)^(5/2))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(3/2)/(b*x+a)**(7/2),x)

[Out] Timed out

$$3.1478 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^{9/2}} dx$$

Optimal. Leaf size=66

$$\frac{4d(c+dx)^{5/2}}{35(a+bx)^{5/2}(bc-ad)^2} - \frac{2(c+dx)^{5/2}}{7(a+bx)^{7/2}(bc-ad)}$$

[Out] $-2/7*(d*x+c)^{(5/2)/(-a*d+b*c)/(b*x+a)^{(7/2)+4/35*d*(d*x+c)^{(5/2)/(-a*d+b*c)^{2/(b*x+a)^{(5/2)}}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{4d(c+dx)^{5/2}}{35(a+bx)^{5/2}(bc-ad)^2} - \frac{2(c+dx)^{5/2}}{7(a+bx)^{7/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2)/(a + b*x)^(9/2), x]

[Out] $(-2*(c+d*x)^{(5/2))/(7*(b*c-a*d)*(a+b*x)^{(7/2)}) + (4*d*(c+d*x)^{(5/2)})/(35*(b*c-a*d)^2*(a+b*x)^{(5/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{(c+dx)^{3/2}}{(a+bx)^{9/2}} dx = -\frac{2(c+dx)^{5/2}}{7(bc-ad)(a+bx)^{7/2}} - \frac{(2d) \int \frac{(c+dx)^{3/2}}{(a+bx)^{7/2}} dx}{7(bc-ad)}$$

$$= -\frac{2(c+dx)^{5/2}}{7(bc-ad)(a+bx)^{7/2}} + \frac{4d(c+dx)^{5/2}}{35(bc-ad)^2(a+bx)^{5/2}}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.70

$$\frac{2(c+dx)^{5/2}(7ad-5bc+2bdx)}{35(a+bx)^{7/2}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/2)/(a + b*x)^(9/2), x]

[Out] (2*(c + d*x)^(5/2)*(-5*b*c + 7*a*d + 2*b*d*x))/(35*(b*c - a*d)^2*(a + b*x)^(7/2))

fricas [B] time = 1.35, size = 235, normalized size = 3.56

$$\frac{2(2bd^3x^3 - 5bc^3 + 7ac^2d - (bcd^2 - 7ad^3)x^2 - 2(4bc^2d - 7acd^2)x)\sqrt{bx}}{35(a^4b^2c^2 - 2a^5bcd + a^6d^2 + (b^6c^2 - 2ab^5cd + a^2b^4d^2)x^4 + 4(ab^5c^2 - 2a^2b^4cd + a^3b^3d^2)x^3 + 6(a^2b^4c^2 - 2a^3b^3cd + a^4b^2c^2 - 2a^5b^2cd + a^6d^2)x^2 + 4(a^3b^3c^2 - 2a^4b^2cd + a^5b^2d^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(9/2), x, algorithm="fricas")

[Out] 2/35*(2*b*d^3*x^3 - 5*b*c^3 + 7*a*c^2*d - (b*c*d^2 - 7*a*d^3)*x^2 - 2*(4*b*c^2*d - 7*a*c*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^4*b^2*c^2 - 2*a^5*b*c*d + a^6*d^2 + (b^6*c^2 - 2*a*b^5*c*d + a^2*b^4*d^2)*x^4 + 4*(a*b^5*c^2 - 2*a^2*b^4*c*d + a^3*b^3*d^2)*x^3 + 6*(a^2*b^4*c^2 - 2*a^3*b^3*c*d + a^4*b^2*c^2 - 2*a^5*b^2*c*d + a^6*d^2)*x^2 + 4*(a^3*b^3*c^2 - 2*a^4*b^2*c*d + a^5*b^2*d^2)*x)

giac [B] time = 2.12, size = 1024, normalized size = 15.52

$$\frac{8(\sqrt{bd}b^{10}c^5d^3|b| - 5\sqrt{bd}ab^9c^4d^4|b| + 10\sqrt{bd}a^2b^8c^3d^5|b| - 10\sqrt{bd}a^3b^7c^2d^6|b| + 5\sqrt{bd}a^4b^6cd^7|b| - \sqrt{bd}a^5b^5d^8|b|)}{35(a^4b^2c^2 - 2a^5bcd + a^6d^2 + (b^6c^2 - 2ab^5cd + a^2b^4d^2)x^4 + 4(ab^5c^2 - 2a^2b^4cd + a^3b^3d^2)x^3 + 6(a^2b^4c^2 - 2a^3b^3cd + a^4b^2c^2 - 2a^5b^2cd + a^6d^2)x^2 + 4(a^3b^3c^2 - 2a^4b^2cd + a^5b^2d^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(9/2), x, algorithm="giac")

```
[Out] 8/35*(sqrt(b*d)*b^10*c^5*d^3*abs(b) - 5*sqrt(b*d)*a*b^9*c^4*d^4*abs(b) + 10
*sqrt(b*d)*a^2*b^8*c^3*d^5*abs(b) - 10*sqrt(b*d)*a^3*b^7*c^2*d^6*abs(b) + 5
*sqrt(b*d)*a^4*b^6*c*d^7*abs(b) - sqrt(b*d)*a^5*b^5*d^8*abs(b) - 7*sqrt(b*d
)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*b^8*c^4
*d^3*abs(b) + 28*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a
)*b*d - a*b*d))^2*a*b^7*c^3*d^4*abs(b) - 42*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x +
a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^2*b^6*c^2*d^5*abs(b) + 28*sq
rt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a
^3*b^5*c*d^6*abs(b) - 7*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (
b*x + a)*b*d - a*b*d))^2*a^4*b^4*d^7*abs(b) - 14*sqrt(b*d)*(sqrt(b*d)*sqrt(
b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*b^6*c^3*d^3*abs(b) + 42*s
qrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*
a*b^5*c^2*d^4*abs(b) - 42*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c +
(b*x + a)*b*d - a*b*d))^4*a^2*b^4*c*d^5*abs(b) + 14*sqrt(b*d)*(sqrt(b*d)*s
qrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^3*b^3*d^6*abs(b) -
70*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d
))^6*b^4*c^2*d^3*abs(b) + 140*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*
c + (b*x + a)*b*d - a*b*d))^6*a*b^3*c*d^4*abs(b) - 70*sqrt(b*d)*(sqrt(b*d)*
sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^2*b^2*d^5*abs(b) -
35*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d
))^8*b^2*c*d^3*abs(b) + 35*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c
+ (b*x + a)*b*d - a*b*d))^8*a*b*d^4*abs(b) - 35*sqrt(b*d)*(sqrt(b*d)*sqrt(b
*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^10*d^3*abs(b))/((b^2*c - a*b
*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)^7*b
^2)
```

maple [A] time = 0.00, size = 54, normalized size = 0.82

$$\frac{2(dx+c)^{\frac{5}{2}}(2bdx+7ad-5bc)}{35(bx+a)^{\frac{7}{2}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^(3/2)/(b*x+a)^(9/2),x)
```

```
[Out] 2/35*(d*x+c)^(5/2)*(2*b*d*x+7*a*d-5*b*c)/(b*x+a)^(7/2)/(a^2*d^2-2*a*b*c*d+b
^2*c^2)
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(3/2)/(b*x+a)^(9/2),x, algorithm="maxima")
```

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c zero or nonzero?

mupad [B] time = 0.93, size = 178, normalized size = 2.70

$$\frac{\sqrt{c+dx} \left(\frac{4d^3x^3}{35b^2(ad-bc)^2} - \frac{10bc^3-14ac^2d}{35b^3(ad-bc)^2} + \frac{x^2(14ad^3-2bcd^2)}{35b^3(ad-bc)^2} + \frac{4cdx(7ad-4bc)}{35b^3(ad-bc)^2} \right)}{x^3\sqrt{a+bx} + \frac{a^3\sqrt{a+bx}}{b^3} + \frac{3ax^2\sqrt{a+bx}}{b} + \frac{3a^2x\sqrt{a+bx}}{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(3/2)/(a + b*x)^(9/2), x)

[Out] ((c + d*x)^(1/2)*((4*d^3*x^3)/(35*b^2*(a*d - b*c)^2) - (10*b*c^3 - 14*a*c^2*d)/(35*b^3*(a*d - b*c)^2) + (x^2*(14*a*d^3 - 2*b*c*d^2))/(35*b^3*(a*d - b*c)^2) + (4*c*d*x*(7*a*d - 4*b*c))/(35*b^3*(a*d - b*c)^2))/(x^3*(a + b*x)^(1/2) + (a^3*(a + b*x)^(1/2))/b^3 + (3*a*x^2*(a + b*x)^(1/2))/b + (3*a^2*x*(a + b*x)^(1/2))/b^2)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(3/2)/(b*x+a)**(9/2), x)

[Out] Timed out

$$3.1479 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^{11/2}} dx$$

Optimal. Leaf size=101

$$-\frac{16d^2(c+dx)^{5/2}}{315(a+bx)^{5/2}(bc-ad)^3} + \frac{8d(c+dx)^{5/2}}{63(a+bx)^{7/2}(bc-ad)^2} - \frac{2(c+dx)^{5/2}}{9(a+bx)^{9/2}(bc-ad)}$$

[Out] $-2/9*(d*x+c)^{(5/2)/(-a*d+b*c)/(b*x+a)^{(9/2)+8/63*d*(d*x+c)^{(5/2)/(-a*d+b*c)^2/(b*x+a)^{(7/2)-16/315*d^2*(d*x+c)^{(5/2)/(-a*d+b*c)^3/(b*x+a)^{(5/2)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{16d^2(c+dx)^{5/2}}{315(a+bx)^{5/2}(bc-ad)^3} + \frac{8d(c+dx)^{5/2}}{63(a+bx)^{7/2}(bc-ad)^2} - \frac{2(c+dx)^{5/2}}{9(a+bx)^{9/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2)/(a + b*x)^(11/2), x]

[Out] $(-2*(c+d*x)^{(5/2))/(9*(b*c-a*d)*(a+b*x)^{(9/2)}) + (8*d*(c+d*x)^{(5/2)})/(63*(b*c-a*d)^2*(a+b*x)^{(7/2)}) - (16*d^2*(c+d*x)^{(5/2)})/(315*(b*c-a*d)^3*(a+b*x)^{(5/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{3/2}}{(a+bx)^{11/2}} dx &= -\frac{2(c+dx)^{5/2}}{9(bc-ad)(a+bx)^{9/2}} - \frac{(4d) \int \frac{(c+dx)^{3/2}}{(a+bx)^{9/2}} dx}{9(bc-ad)} \\
&= -\frac{2(c+dx)^{5/2}}{9(bc-ad)(a+bx)^{9/2}} + \frac{8d(c+dx)^{5/2}}{63(bc-ad)^2(a+bx)^{7/2}} + \frac{(8d^2) \int \frac{(c+dx)^{3/2}}{(a+bx)^{7/2}} dx}{63(bc-ad)^2} \\
&= -\frac{2(c+dx)^{5/2}}{9(bc-ad)(a+bx)^{9/2}} + \frac{8d(c+dx)^{5/2}}{63(bc-ad)^2(a+bx)^{7/2}} - \frac{16d^2(c+dx)^{5/2}}{315(bc-ad)^3(a+bx)^{5/2}}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 77, normalized size = 0.76

$$\frac{2(c+dx)^{5/2} (63a^2d^2 + 18abd(2dx-5c) + b^2(35c^2 - 20cdx + 8d^2x^2))}{315(a+bx)^{9/2}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/2)/(a + b*x)^(11/2), x]

[Out] (-2*(c + d*x)^(5/2)*(63*a^2*d^2 + 18*a*b*d*(-5*c + 2*d*x) + b^2*(35*c^2 - 20*c*d*x + 8*d^2*x^2)))/(315*(b*c - a*d)^3*(a + b*x)^(9/2))

fricas [B] time = 4.40, size = 426, normalized size = 4.22

$$\frac{2(8b^2d^4x^4 + 35b^2c^4 - 90abc^3d + 63a^2c^2d^2 - 4(b^2cd^3 - 9a^2bd^4)x^3 + 3(b^2c^2d^2 - 6a^2b^2cd^3 + 21a^2d^4)x^2 + 2(25b^2c^3d - 72a^2b^2c^2d^2 + 63a^2c^2d^3)x)\sqrt{b*x+a}\sqrt{d*x+c}}{315(a^5b^3c^3 - 3a^6b^2c^2d + 3a^7bcd^2 - a^8d^3 + (b^3c^3 - 3ab^2c^2d + 3a^2b^6cd^2 - a^3b^5d^3)x^5 + 5(ab^7c^3 - 3a^2b^6c^2d + 3a^5b^3c^3 - 3a^6b^2c^2d + 3a^7bcd^2 - a^8d^3)x^4 + 10(a^2b^6c^3 - 3a^3b^5c^2d + 3a^4b^4c^2d^2 - a^5b^3c^2d^3)x^3 + 10(a^3b^5c^3 - 3a^4b^4c^2d + 3a^5b^3c^2d^2 - a^6b^2c^2d^3)x^2 + 5(a^4b^4c^3 - 3a^5b^3c^2d + 3a^6b^2c^2d^2 - a^7b^2d^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(11/2), x, algorithm="fricas")

[Out] -2/315*(8*b^2*d^4*x^4 + 35*b^2*c^4 - 90*a*b*c^3*d + 63*a^2*c^2*d^2 - 4*(b^2*c*d^3 - 9*a*b*d^4)*x^3 + 3*(b^2*c^2*d^2 - 6*a*b*c*d^3 + 21*a^2*d^4)*x^2 + 2*(25*b^2*c^3*d - 72*a*b*c^2*d^2 + 63*a^2*c^2*d^3)*x)*sqrt(b*x+a)*sqrt(d*x+c)/(a^5*b^3*c^3 - 3*a^6*b^2*c^2*d + 3*a^7*b*c*d^2 - a^8*d^3 + (b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b^6*c*d^2 - a^3*b^5*d^3)*x^5 + 5*(a*b^7*c^3 - 3*a^2*b^6*c^2*d + 3*a^3*b^5*c^2*d^2 - a^4*b^4*d^3)*x^4 + 10*(a^2*b^6*c^3 - 3*a^3*b^5*c^2*d + 3*a^4*b^4*c^2*d^2 - a^5*b^3*d^3)*x^3 + 10*(a^3*b^5*c^3 - 3*a^4*b^4*c^2*d + 3*a^5*b^3*c^2*d^2 - a^6*b^2*d^3)*x^2 + 5*(a^4*b^4*c^3 - 3*a^5*b^3*c^2*d + 3*a^6*b^2*c^2*d^2 - a^7*b^2*d^3)*x)

giac [B] time = 2.94, size = 1394, normalized size = 13.80

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(11/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & -32/315*(\sqrt{b*d})*b^{12}*c^6*d^4*\text{abs}(b) - 6*\sqrt{b*d}*a*b^{11}*c^5*d^5*\text{abs}(b) \\ & + 15*\sqrt{b*d}*a^2*b^{10}*c^4*d^6*\text{abs}(b) - 20*\sqrt{b*d}*a^3*b^9*c^3*d^7*\text{abs}(b) \\ & + 15*\sqrt{b*d}*a^4*b^8*c^2*d^8*\text{abs}(b) - 6*\sqrt{b*d}*a^5*b^7*c*d^9*\text{abs}(b) \\ & + \sqrt{b*d}*a^6*b^6*d^{10}*\text{abs}(b) - 9*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^2*b^{10}*c^5*d^4*\text{abs}(b) \\ & + 45*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^2*a*b^9*c^4*d^5*\text{abs}(b) \\ & - 90*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^2*a^2*b^8*c^3*d^6*\text{abs}(b) \\ & + 90*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^2*a^3*b^7*c^2*d^7*\text{abs}(b) \\ & - 45*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^2*a^4*b^6*c*d^8*\text{abs}(b) \\ & + 9*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^2*a^5*b^5*d^9*\text{abs}(b) \\ & + 36*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^4*b^8*c^4*d^4*\text{abs}(b) \\ & - 144*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^4*a*b^7*c^3*d^5*\text{abs}(b) \\ & + 216*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^4*a^2*b^6*c^2*d^6*\text{abs}(b) \\ & - 144*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^4*a^3*b^5*c*d^7*\text{abs}(b) \\ & + 36*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^4*a^4*b^4*d^8*\text{abs}(b) \\ & + 126*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^6*b^6*c^3*d^4*\text{abs}(b) \\ & - 378*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^6*a*b^5*c^2*d^5*\text{abs}(b) \\ & + 378*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^6*a^2*b^4*c*d^6*\text{abs}(b) \\ & - 126*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^6*a^3*b^3*d^7*\text{abs}(b) \\ & + 441*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^8*b^4*c^2*d^4*\text{abs}(b) \\ & - 882*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^8*a*b^3*c*d^5*\text{abs}(b) \\ & + 441*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^8*a^2*b^2*d^6*\text{abs}(b) \\ & + 315*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^{10}*b^2*c*d^4*\text{abs}(b) \\ & - 315*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^{10}*a*b*d^5*\text{abs}(b) \\ & + 210*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^{12}*d^4*\text{abs}(b)) / ((b^2*c - a*b*d - (\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d-a*b*d})^2)^9*b) \end{aligned}$$

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{2(dx+c)^{\frac{5}{2}}(8b^2x^2d^2+36abd^2x-20b^2cdx+63a^2d^2-90abcd+35b^2c^2)}{315(bx+a)^{\frac{9}{2}}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(3/2)/(b*x+a)^(11/2),x)`

[Out] $2/315*(d*x+c)^{(5/2)}*(8*b^2*d^2*x^2+36*a*b*d^2*x-20*b^2*c*d*x+63*a^2*d^2-90*a*b*c*d+35*b^2*c^2)/(b*x+a)^{(9/2)}/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(3/2)/(b*x+a)^(11/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.11, size = 268, normalized size = 2.65

$$\frac{\sqrt{c+dx} \left(\frac{126a^2c^2d^2-180abc^3d+70b^2c^4}{315b^4(ad-bc)^3} + \frac{x^2(126a^2d^4-36abcd^3+6b^2c^2d^2)}{315b^4(ad-bc)^3} + \frac{16d^4x^4}{315b^2(ad-bc)^3} + \frac{8d^3x^3(9ad-bc)}{315b^3(ad-bc)^3} + \frac{4cdx(63a^2d^2-90abc^2d+b^3c^3)}{315b^4(ad-bc)^3} \right)}{x^4\sqrt{a+bx} + \frac{a^4\sqrt{a+bx}}{b^4} + \frac{6a^2x^2\sqrt{a+bx}}{b^2} + \frac{4ax^3\sqrt{a+bx}}{b} + \frac{4a^3x\sqrt{a+bx}}{b^3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c+d*x)^(3/2)/(a+b*x)^(11/2),x)`

[Out] $((c+d*x)^{(1/2)}*((70*b^2*c^4+126*a^2*c^2*d^2-180*a*b*c^3*d)/(315*b^4*(a*d-b*c)^3)+(x^2*(126*a^2*d^4+6*b^2*c^2*d^2-36*a*b*c*d^3))/(315*b^4*(a*d-b*c)^3)+(16*d^4*x^4)/(315*b^2*(a*d-b*c)^3)+(8*d^3*x^3*(9*a*d-b*c))/(315*b^3*(a*d-b*c)^3)+(4*c*d*x*(63*a^2*d^2+25*b^2*c^2-72*a*b*c*d))/(315*b^4*(a*d-b*c)^3))/(x^4*(a+b*x)^{(1/2)}+(a^4*(a+b*x)^{(1/2)})/b^4+(6*a^2*x^2*(a+b*x)^{(1/2)})/b^2+(4*a*x^3*(a+b*x)^{(1/2)})/b+(4*a^3*x*(a+b*x)^{(1/2)})/b^3)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(3/2)/(b*x+a)**(11/2),x)`

[Out] Timed out

$$3.1480 \quad \int \frac{(c+dx)^{3/2}}{(a+bx)^{13/2}} dx$$

Optimal. Leaf size=136

$$\frac{32d^3(c+dx)^{5/2}}{1155(a+bx)^{5/2}(bc-ad)^4} - \frac{16d^2(c+dx)^{5/2}}{231(a+bx)^{7/2}(bc-ad)^3} + \frac{4d(c+dx)^{5/2}}{33(a+bx)^{9/2}(bc-ad)^2} - \frac{2(c+dx)^{5/2}}{11(a+bx)^{11/2}(bc-ad)}$$

[Out] $-2/11*(d*x+c)^{(5/2)/(-a*d+b*c)/(b*x+a)^{(11/2)+4/33*d*(d*x+c)^{(5/2)/(-a*d+b*c)^2/(b*x+a)^{(9/2)-16/231*d^2*(d*x+c)^{(5/2)/(-a*d+b*c)^3/(b*x+a)^{(7/2)+32/1155*d^3*(d*x+c)^{(5/2)/(-a*d+b*c)^4/(b*x+a)^{(5/2)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{32d^3(c+dx)^{5/2}}{1155(a+bx)^{5/2}(bc-ad)^4} - \frac{16d^2(c+dx)^{5/2}}{231(a+bx)^{7/2}(bc-ad)^3} + \frac{4d(c+dx)^{5/2}}{33(a+bx)^{9/2}(bc-ad)^2} - \frac{2(c+dx)^{5/2}}{11(a+bx)^{11/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(3/2)/(a + b*x)^(13/2), x]

[Out] $(-2*(c+d*x)^{(5/2))/(11*(b*c-a*d)*(a+b*x)^{(11/2)}) + (4*d*(c+d*x)^{(5/2))/(33*(b*c-a*d)^2*(a+b*x)^{(9/2)}) - (16*d^2*(c+d*x)^{(5/2))/(231*(b*c-a*d)^3*(a+b*x)^{(7/2)}) + (32*d^3*(c+d*x)^{(5/2))/(1155*(b*c-a*d)^4*(a+b*x)^{(5/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{3/2}}{(a+bx)^{13/2}} dx &= -\frac{2(c+dx)^{5/2}}{11(bc-ad)(a+bx)^{11/2}} - \frac{(6d) \int \frac{(c+dx)^{3/2}}{(a+bx)^{11/2}} dx}{11(bc-ad)} \\
&= -\frac{2(c+dx)^{5/2}}{11(bc-ad)(a+bx)^{11/2}} + \frac{4d(c+dx)^{5/2}}{33(bc-ad)^2(a+bx)^{9/2}} + \frac{(8d^2) \int \frac{(c+dx)^{3/2}}{(a+bx)^{9/2}} dx}{33(bc-ad)^2} \\
&= -\frac{2(c+dx)^{5/2}}{11(bc-ad)(a+bx)^{11/2}} + \frac{4d(c+dx)^{5/2}}{33(bc-ad)^2(a+bx)^{9/2}} - \frac{16d^2(c+dx)^{5/2}}{231(bc-ad)^3(a+bx)^{7/2}} - \frac{(16d^3) \int \frac{(c+dx)^{3/2}}{(a+bx)^{7/2}} dx}{231(bc-ad)^3} \\
&= -\frac{2(c+dx)^{5/2}}{11(bc-ad)(a+bx)^{11/2}} + \frac{4d(c+dx)^{5/2}}{33(bc-ad)^2(a+bx)^{9/2}} - \frac{16d^2(c+dx)^{5/2}}{231(bc-ad)^3(a+bx)^{7/2}} + \frac{32d^3}{1155(bc-ad)^4}
\end{aligned}$$

Mathematica [A] time = 0.06, size = 118, normalized size = 0.87

$$\frac{2(c+dx)^{5/2} (231a^3d^3 + 99a^2bd^2(2dx-5c) + 11ab^2d(35c^2 - 20cdx + 8d^2x^2) + b^3(-105c^3 + 70c^2dx - 40cd^2x^2 - 16d^3x^3))}{1155(a+bx)^{11/2}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/2)/(a + b*x)^(13/2), x]

[Out] (2*(c + d*x)^(5/2)*(231*a^3*d^3 + 99*a^2*b*d^2*(-5*c + 2*d*x) + 11*a*b^2*d*(35*c^2 - 20*c*d*x + 8*d^2*x^2) + b^3*(-105*c^3 + 70*c^2*d*x - 40*c*d^2*x^2 + 16*d^3*x^3)))/(1155*(b*c - a*d)^4*(a + b*x)^(11/2))

fricas [B] time = 9.76, size = 649, normalized size = 4.77

$$\frac{2(16b^3d^5x^5 - 105b^3c^5 + 385a^2b^2c^4d - 495a^2b^3c^3d^2 + 231a^3c^2d^3 - 8(b^3c^2d^4 - 11a^2b^2d^5)x^4 + 2(3b^3c^2d^3 - 22a^2b^2c^2d^4 + 99a^2b^2d^5)x^3 - (5b^3c^3d^2 - 33a^2b^2c^2d^3 + 99a^2b^2c^2d^4 - 231a^3d^5)x^2 - 2(70b^3c^4d - 275a^2b^2c^3d^2 + 396a^2b^2c^2d^3 - 231a^3c^2d^4)x)\sqrt{b*x+a}\sqrt{d*x+c}}{(a^6b^4c^4 - 4a^7b^3c^3d + 6a^8b^2c^2d^2 - 4a^9bcd^3 + a^{10}d^4 + (b^{10}c^4 - 4ab^9c^3d + 6a^2b^8c^2d^2 - 4a^3b^7cd^3 + a^4b^6d^4))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(13/2), x, algorithm="fricas")

[Out] 2/1155*(16*b^3*d^5*x^5 - 105*b^3*c^5 + 385*a*b^2*c^4*d - 495*a^2*b^3*c^3*d^2 + 231*a^3*c^2*d^3 - 8*(b^3*c^2*d^4 - 11*a^2*b^2*d^5)*x^4 + 2*(3*b^3*c^2*d^3 - 22*a^2*b^2*c^2*d^4 + 99*a^2*b^2*d^5)*x^3 - (5*b^3*c^3*d^2 - 33*a^2*b^2*c^2*d^3 + 99*a^2*b^2*c^2*d^4 - 231*a^3*d^5)*x^2 - 2*(70*b^3*c^4*d - 275*a^2*b^2*c^3*d^2 + 396*a^2*b^2*c^2*d^3 - 231*a^3*c^2*d^4)*x)*sqrt(b*x+a)*sqrt(d*x+c)/(a^6*b^4*c^4 - 4*a^7*b^3*c^3*d + 6*a^8*b^2*c^2*d^2 - 4*a^9*b*c*d^3 + a^10*d^4 + (b^10*c^4 - 4*a*b^9*c^3*d + 6*a^2*b^8*c^2*d^2 - 4*a^3*b^7*c*d^3 + a^4*b^6*d^4)*x^6 + 6*(a*b^9*c^4 - 4*a^2*b^8*c^3*d + 6*a^3*b^7*c^2*d^2 - 4*a^4*b^6*c*d^3 + a^5*b^5*c^2*d^2 - 4*a^6*b^4*c^2*d^3 + a^7*b^3*c^2*d^4 - 4*a^8*b^2*c^2*d^5 + a^9*b*c^2*d^6 + a^10*c^2*d^7))

$$5*b^5*d^4)*x^5 + 15*(a^2*b^8*c^4 - 4*a^3*b^7*c^3*d + 6*a^4*b^6*c^2*d^2 - 4*a^5*b^5*c*d^3 + a^6*b^4*d^4)*x^4 + 20*(a^3*b^7*c^4 - 4*a^4*b^6*c^3*d + 6*a^5*b^5*c^2*d^2 - 4*a^6*b^4*c*d^3 + a^7*b^3*d^4)*x^3 + 15*(a^4*b^6*c^4 - 4*a^5*b^5*c^3*d + 6*a^6*b^4*c^2*d^2 - 4*a^7*b^3*c*d^3 + a^8*b^2*d^4)*x^2 + 6*(a^5*b^5*c^4 - 4*a^6*b^4*c^3*d + 6*a^7*b^3*c^2*d^2 - 4*a^8*b^2*c*d^3 + a^9*b*d^4)*x)$$

giac [B] time = 3.28, size = 1823, normalized size = 13.40

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(13/2),x, algorithm="giac")

[Out] $64/1155*(\sqrt{b*d})*b^{14}*c^7*d^5*\text{abs}(b) - 7*\sqrt{b*d}*a*b^{13}*c^6*d^6*\text{abs}(b) + 21*\sqrt{b*d}*a^2*b^{12}*c^5*d^7*\text{abs}(b) - 35*\sqrt{b*d}*a^3*b^{11}*c^4*d^8*\text{abs}(b) + 35*\sqrt{b*d}*a^4*b^{10}*c^3*d^9*\text{abs}(b) - 21*\sqrt{b*d}*a^5*b^9*c^2*d^{10}*\text{abs}(b) + 7*\sqrt{b*d}*a^6*b^8*c*d^{11}*\text{abs}(b) - \sqrt{b*d}*a^7*b^7*d^{12}*\text{abs}(b) - 11*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*b^{12}*c^6*d^5*\text{abs}(b) + 66*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a*b^{11}*c^5*d^6*\text{abs}(b) - 165*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^2*b^{10}*c^4*d^7*\text{abs}(b) + 220*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^3*b^9*c^3*d^8*\text{abs}(b) - 165*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^4*b^8*c^2*d^9*\text{abs}(b) + 66*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^5*b^7*c*d^{10}*\text{abs}(b) - 11*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^6*b^6*d^{11}*\text{abs}(b) + 55*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*b^{10}*c^5*d^5*\text{abs}(b) - 275*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a*b^9*c^4*d^6*\text{abs}(b) + 550*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a^2*b^8*c^3*d^7*\text{abs}(b) - 550*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a^3*b^7*c^2*d^8*\text{abs}(b) + 275*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a^4*b^6*c*d^9*\text{abs}(b) - 55*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a^5*b^5*d^{10}*\text{abs}(b) - 165*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*b^8*c^4*d^5*\text{abs}(b) + 660*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*a*b^7*c^3*d^6*\text{abs}(b) - 990*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*a^2*b^6*c^2*d^7*\text{abs}(b) + 660*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*a^3*b^5*c*d^8*\text{abs}(b) - 165*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^8*b^6*c^3*d^5*\text{abs}(b) + 2475*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d$

$$\begin{aligned}
& - a*b*d))^{8*a*b^5*c^2*d^6*abs(b) - 2475*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) \\
& - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{8*a^2*b^4*c*d^7*abs(b) + 825*sqrt(b \\
& *d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{8*a^3*b \\
& ^3*d^8*abs(b) - 2541*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x \\
& + a)*b*d - a*b*d))^{10*b^4*c^2*d^5*abs(b) + 5082*sqrt(b*d)*(sqrt(b*d)*sqrt(\\
& b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{10*a*b^3*c*d^6*abs(b) - 254 \\
& 1*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d)) \\
& ^{10*a^2*b^2*d^7*abs(b) - 2079*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2 \\
& *c + (b*x + a)*b*d - a*b*d))^{12*b^2*c*d^5*abs(b) + 2079*sqrt(b*d)*(sqrt(b*d) \\
&)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{12*a*b*d^6*abs(b) - \\
& 1155*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b* \\
& d))^{14*d^5*abs(b))/(b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + \\
& (b*x + a)*b*d - a*b*d))^2)^{11}
\end{aligned}$$

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{2(dx+c)^{\frac{5}{2}}(16b^3x^3d^3+88ab^2d^3x^2-40b^3cd^2x^2+198a^2bd^3x-220ab^2cd^2x+70b^3c^2dx+231a^3d^3-495a^2bc)}{1155(bx+a)^{\frac{11}{2}}(a^4d^4-4a^3bcd^3+6a^2b^2c^2d^2-4ab^3c^3d+b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/2)/(b*x+a)^(13/2),x)

[Out] $2/1155*(d*x+c)^{(5/2)}*(16*b^3*d^3*x^3+88*a*b^2*d^3*x^2-40*b^3*c*d^2*x^2+198*a^2*b*d^3*x-220*a*b^2*c*d^2*x+70*b^3*c^2*d*x+231*a^3*d^3-495*a^2*b*c*d^2+385*a*b^2*c^2*d-105*b^3*c^3)/(b*x+a)^{(11/2)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/2)/(b*x+a)^(13/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.33, size = 376, normalized size = 2.76

$$\frac{\sqrt{c+dx} \left(\frac{x^2(462a^3d^5-198a^2bcd^4+66ab^2c^2d^3-10b^3c^3d^2)}{1155b^5(ad-bc)^4} - \frac{-462a^3c^2d^3+990a^2bc^3d^2-770ab^2c^4d+210b^3c^5}{1155b^5(ad-bc)^4} + \frac{x(924a^3cd^4-1584a^2c^2d^3+564a^2cd^3-1584a^2cd^3+1584a^2cd^3-1584a^2cd^3)}{1155b^5(ad-bc)^4} \right)}{x^5\sqrt{a+bx} + \frac{a^5\sqrt{a+bx}}{b^5} + \frac{10a^2x^3\sqrt{a+bx}}{b^2} + \frac{10a^3x^2\sqrt{a+bx}}{b^3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(3/2)/(a + b*x)^(13/2),x)`

[Out] $((c + d*x)^{(1/2)} * ((x^2 * (462*a^3*d^5 - 10*b^3*c^3*d^2 + 66*a*b^2*c^2*d^3 - 198*a^2*b*c*d^4)) / (1155*b^5*(a*d - b*c)^4) - (210*b^3*c^5 - 462*a^3*c^2*d^3 + 990*a^2*b*c^3*d^2 - 770*a*b^2*c^4*d) / (1155*b^5*(a*d - b*c)^4) + (x*(924*a^3*c*d^4 - 280*b^3*c^4*d + 1100*a*b^2*c^3*d^2 - 1584*a^2*b*c^2*d^3)) / (1155*b^5*(a*d - b*c)^4) + (32*d^5*x^5) / (1155*b^2*(a*d - b*c)^4) + (16*d^4*x^4*(11*a*d - b*c)) / (1155*b^3*(a*d - b*c)^4) + (4*d^3*x^3*(99*a^2*d^2 + 3*b^2*c^2 - 22*a*b*c*d)) / (1155*b^4*(a*d - b*c)^4)) / (x^5*(a + b*x)^{(1/2)} + (a^5*(a + b*x)^{(1/2)})/b^5 + (10*a^2*x^3*(a + b*x)^{(1/2)})/b^2 + (10*a^3*x^2*(a + b*x)^{(1/2)})/b^3 + (5*a*x^4*(a + b*x)^{(1/2)})/b + (5*a^4*x*(a + b*x)^{(1/2)})/b^4)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(3/2)/(b*x+a)**(13/2),x)`

[Out] Timed out

3.1481 $\int (a + bx)^{5/2} (c + dx)^{5/2} dx$

Optimal. Leaf size=262

$$-\frac{5(bc - ad)^6 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{512b^{7/2}d^{7/2}} + \frac{5\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^5}{512b^3d^3} - \frac{5(a+bx)^{3/2}\sqrt{c+dx}(bc - ad)^4}{768b^3d^2} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{192b^3d}$$

[Out] $1/12*(-a*d+b*c)*(b*x+a)^{(7/2)}*(d*x+c)^{(3/2)}/b^2+1/6*(b*x+a)^{(7/2)}*(d*x+c)^{(5/2)}/b-5/512*(-a*d+b*c)^6*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(7/2)}/d^{(7/2)}-5/768*(-a*d+b*c)^4*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/b^3/d^2+1/192*(-a*d+b*c)^3*(b*x+a)^{(5/2)}*(d*x+c)^{(1/2)}/b^3/d+1/32*(-a*d+b*c)^2*(b*x+a)^{(7/2)}*(d*x+c)^{(1/2)}/b^3+5/512*(-a*d+b*c)^5*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b^3/d^3$

Rubi [A] time = 0.15, antiderivative size = 262, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$\frac{5\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^5}{512b^3d^3} - \frac{5(a+bx)^{3/2}\sqrt{c+dx}(bc - ad)^4}{768b^3d^2} - \frac{5(bc - ad)^6 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{512b^{7/2}d^{7/2}} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{192b^3d}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}*(c + d*x)^{(5/2)}, x]$

[Out] $(5*(b*c - a*d)^5*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(512*b^3*d^3) - (5*(b*c - a*d)^4*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(768*b^3*d^2) + ((b*c - a*d)^3*(a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x])/(192*b^3*d) + ((b*c - a*d)^2*(a + b*x)^{(7/2)}*\operatorname{Sqrt}[c + d*x])/(32*b^3) + ((b*c - a*d)*(a + b*x)^{(7/2)}*(c + d*x)^{(3/2)})/(12*b^2) + ((a + b*x)^{(7/2)}*(c + d*x)^{(5/2)})/(6*b) - (5*(b*c - a*d)^6*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/(512*b^{(7/2)}*d^{(7/2)})$

Rule 50

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[n*(b*c - a*d)/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{GtQ}[n, 0] \ \&\& \ \operatorname{NeQ}[m+n+1, 0] \ \&\& \ !(\operatorname{IGtQ}[m, 0] \ \&\& \ (!\operatorname{IntegerQ}[n] \ || \ (\operatorname{GtQ}[m, 0] \ \&\& \ \operatorname{LtQ}[m-n, 0]))) \ \&\& \ !\operatorname{ILtQ}[m+n+2, 0] \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x] := \operatorname{With}[p = \operatorname{Denominator}[m], \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{p*(m+1)-1}*(c - (a*d)/b +$

```
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int (a+bx)^{5/2}(c+dx)^{5/2} dx &= \frac{(a+bx)^{7/2}(c+dx)^{5/2}}{6b} + \frac{(5(bc-ad)) \int (a+bx)^{5/2}(c+dx)^{3/2} dx}{12b} \\
&= \frac{(bc-ad)(a+bx)^{7/2}(c+dx)^{3/2}}{12b^2} + \frac{(a+bx)^{7/2}(c+dx)^{5/2}}{6b} + \frac{(bc-ad)^2 \int (a+bx)^{5/2} \sqrt{c+dx}}{8b^2} \\
&= \frac{(bc-ad)^2(a+bx)^{7/2} \sqrt{c+dx}}{32b^3} + \frac{(bc-ad)(a+bx)^{7/2}(c+dx)^{3/2}}{12b^2} + \frac{(a+bx)^{7/2}(c+dx)^{5/2}}{6b} \\
&= \frac{(bc-ad)^3(a+bx)^{5/2} \sqrt{c+dx}}{192b^3d} + \frac{(bc-ad)^2(a+bx)^{7/2} \sqrt{c+dx}}{32b^3} + \frac{(bc-ad)(a+bx)^{7/2}(c+dx)^{3/2}}{12b^2} \\
&= -\frac{5(bc-ad)^4(a+bx)^{3/2} \sqrt{c+dx}}{768b^3d^2} + \frac{(bc-ad)^3(a+bx)^{5/2} \sqrt{c+dx}}{192b^3d} + \frac{(bc-ad)^2(a+bx)^{7/2}(c+dx)^{3/2}}{32b^2} \\
&= \frac{5(bc-ad)^5 \sqrt{a+bx} \sqrt{c+dx}}{512b^3d^3} - \frac{5(bc-ad)^4(a+bx)^{3/2} \sqrt{c+dx}}{768b^3d^2} + \frac{(bc-ad)^3(a+bx)^{5/2}(c+dx)^{3/2}}{192b^3} \\
&= \frac{5(bc-ad)^5 \sqrt{a+bx} \sqrt{c+dx}}{512b^3d^3} - \frac{5(bc-ad)^4(a+bx)^{3/2} \sqrt{c+dx}}{768b^3d^2} + \frac{(bc-ad)^3(a+bx)^{5/2}(c+dx)^{3/2}}{192b^3} \\
&= \frac{5(bc-ad)^5 \sqrt{a+bx} \sqrt{c+dx}}{512b^3d^3} - \frac{5(bc-ad)^4(a+bx)^{3/2} \sqrt{c+dx}}{768b^3d^2} + \frac{(bc-ad)^3(a+bx)^{5/2}(c+dx)^{3/2}}{192b^3} \\
&= \frac{5(bc-ad)^5 \sqrt{a+bx} \sqrt{c+dx}}{512b^3d^3} - \frac{5(bc-ad)^4(a+bx)^{3/2} \sqrt{c+dx}}{768b^3d^2} + \frac{(bc-ad)^3(a+bx)^{5/2}(c+dx)^{3/2}}{192b^3}
\end{aligned}$$

Mathematica [A] time = 2.53, size = 209, normalized size = 0.80

$$\frac{(a+bx)^{7/2} \sqrt{c+dx} \left(-\frac{15(bc-ad)^{11/2} \sinh^{-1}\left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{bc-ad}}\right)}{d^{7/2}(a+bx)^{7/2} \sqrt{\frac{b(c+dx)}{bc-ad}}} + \frac{15(bc-ad)^5}{d^3(a+bx)^3} - \frac{10(bc-ad)^4}{d^2(a+bx)^2} + \frac{8(bc-ad)^3}{d(a+bx)} + 128b(c+dx)(bc-ad) + 48b^2 \right)}{1536b^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)*(c + d*x)^(5/2), x]

[Out] ((a + b*x)^(7/2)*Sqrt[c + d*x]*(48*(b*c - a*d)^2 + (15*(b*c - a*d)^5)/(d^3*(a + b*x)^3) - (10*(b*c - a*d)^4)/(d^2*(a + b*x)^2) + (8*(b*c - a*d)^3)/(d*(a + b*x)) + 128*b*(b*c - a*d)*(c + d*x) + 256*b^2*(c + d*x)^2 - (15*(b*c -

$$\frac{a*d^{11/2}*\text{ArcSinh}[\text{Sqrt}[d]*\text{Sqrt}[a + b*x]]/\text{Sqrt}[b*c - a*d]}{(d^{7/2}*(a + b*x)^{7/2}*\text{Sqrt}[(b*(c + d*x))/(b*c - a*d)])}/(1536*b^3)$$

fricas [B] time = 0.56, size = 882, normalized size = 3.37

$$\frac{15(b^6c^6 - 6ab^5c^5d + 15a^2b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^4b^2c^2d^4 - 6a^5bcd^5 + a^6d^6)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6a^2d^2x + b^2c^2 + 6a^2d^2)}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(d*x+c)^(5/2),x, algorithm="fricas")

[Out] [1/6144*(15*(b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 - 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x) + 4*(256*b^6*d^6*x^5 + 15*b^6*c^5*d - 85*a*b^5*c^4*d^2 + 198*a^2*b^4*c^3*d^3 + 198*a^3*b^3*c^2*d^4 - 85*a^4*b^2*c*d^5 + 15*a^5*b*d^6 + 640*(b^6*c*d^5 + a*b^5*d^6)*x^4 + 16*(27*b^6*c^2*d^4 + 106*a*b^5*c*d^5 + 27*a^2*b^4*d^6)*x^3 + 8*(b^6*c^3*d^3 + 159*a*b^5*c^2*d^4 + 159*a^2*b^4*c*d^5 + a^3*b^3*d^6)*x^2 - 2*(5*b^6*c^4*d^2 - 28*a*b^5*c^3*d^3 - 594*a^2*b^4*c^2*d^4 - 28*a^3*b^3*c*d^5 + 5*a^4*b^2*d^6)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*d^4), 1/3072*(15*(b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x) + 2*(256*b^6*d^6*x^5 + 15*b^6*c^5*d - 85*a*b^5*c^4*d^2 + 198*a^2*b^4*c^3*d^3 + 198*a^3*b^3*c^2*d^4 - 85*a^4*b^2*c*d^5 + 15*a^5*b*d^6 + 640*(b^6*c*d^5 + a*b^5*d^6)*x^4 + 16*(27*b^6*c^2*d^4 + 106*a*b^5*c*d^5 + 27*a^2*b^4*d^6)*x^3 + 8*(b^6*c^3*d^3 + 159*a*b^5*c^2*d^4 + 159*a^2*b^4*c*d^5 + a^3*b^3*d^6)*x^2 - 2*(5*b^6*c^4*d^2 - 28*a*b^5*c^3*d^3 - 594*a^2*b^4*c^2*d^4 - 28*a^3*b^3*c*d^5 + 5*a^4*b^2*d^6)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*d^4)]

giac [B] time = 3.53, size = 3120, normalized size = 11.91

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(d*x+c)^(5/2),x, algorithm="giac")

[Out] 1/7680*(960*(sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*sqrt(b*x + a)*(2*(b*x + a)*(4*(b*x + a)/b^2 + (b^6*c*d^3 - 13*a*b^5*d^4)/(b^7*d^4)) - 3*(b^7*c^2*d^2 + 2*a*b^6*c*d^3 - 11*a^2*b^5*d^4)/(b^7*d^4)) - 3*(b^3*c^3 + a*b^2*c^2*d + 3*a^2*b*c*d^2 - 5*a^3*d^3)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/sqrt(b^2*c + (b*x + a)*b*d - a*b*d))

$$\begin{aligned}
& b*x + a)*b*d - a*b*d)))/(\text{sqrt}(b*d)*b*d^2)) * a*c^2*abs(b) - 7680*((b^2*c - a* \\
& b*d)*\log(abs(-\text{sqrt}(b*d)*\text{sqrt}(b*x + a) + \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d) \\
&)))/\text{sqrt}(b*d) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)*\text{sqrt}(b*x + a)) * a^3*c^2*a \\
& bs(b)/b^2 + 40*(\text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)*(2*(b*x + a)*(4*(b*x + \\
& a)*(6*(b*x + a)/b^3 + (b^12*c*d^5 - 25*a*b^11*d^6)/(b^14*d^6)) - (5*b^13*c^ \\
& 2*d^4 + 14*a*b^12*c*d^5 - 163*a^2*b^11*d^6)/(b^14*d^6)) + 3*(5*b^14*c^3*d^3 \\
& + 9*a*b^13*c^2*d^4 + 15*a^2*b^12*c*d^5 - 93*a^3*b^11*d^6)/(b^14*d^6))*\text{sqrt} \\
& (b*x + a) + 3*(5*b^4*c^4 + 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 + 20*a^3*b*c*d \\
& ^3 - 35*a^4*d^4)*\log(abs(-\text{sqrt}(b*d)*\text{sqrt}(b*x + a) + \text{sqrt}(b^2*c + (b*x + a)* \\
& b*d - a*b*d)))/(\text{sqrt}(b*d)*b^2*d^3))*b*c^2*abs(b) + 240*(\text{sqrt}(b^2*c + (b*x + \\
& a)*b*d - a*b*d)*(2*(b*x + a)*(4*(b*x + a)*(6*(b*x + a)/b^3 + (b^12*c*d^5 - \\
& 25*a*b^11*d^6)/(b^14*d^6)) - (5*b^13*c^2*d^4 + 14*a*b^12*c*d^5 - 163*a^2*b \\
& ^11*d^6)/(b^14*d^6)) + 3*(5*b^14*c^3*d^3 + 9*a*b^13*c^2*d^4 + 15*a^2*b^12*c \\
& *d^5 - 93*a^3*b^11*d^6)/(b^14*d^6))*\text{sqrt}(b*x + a) + 3*(5*b^4*c^4 + 4*a*b^3*c \\
& ^3*d + 6*a^2*b^2*c^2*d^2 + 20*a^3*b*c*d^3 - 35*a^4*d^4)*\log(abs(-\text{sqrt}(b*d) \\
& *\text{sqrt}(b*x + a) + \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)))/(\text{sqrt}(b*d)*b^2*d^3)) \\
& *a*c*d*abs(b) + 1920*(\text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)*\text{sqrt}(b*x + a)*(2* \\
& (b*x + a)*(4*(b*x + a)/b^2 + (b^6*c*d^3 - 13*a*b^5*d^4)/(b^7*d^4)) - 3*(b^7 \\
& *c^2*d^2 + 2*a*b^6*c*d^3 - 11*a^2*b^5*d^4)/(b^7*d^4)) - 3*(b^3*c^3 + a*b^2*c \\
& ^2*d + 3*a^2*b*c*d^2 - 5*a^3*d^3)*\log(abs(-\text{sqrt}(b*d)*\text{sqrt}(b*x + a) + \text{sqrt}(\\
& b^2*c + (b*x + a)*b*d - a*b*d)))/(\text{sqrt}(b*d)*b*d^2)) * a^2*c*d*abs(b)/b + 8*(s \\
& \text{qrt}(b^2*c + (b*x + a)*b*d - a*b*d)*(2*(4*(b*x + a)*(6*(b*x + a)*(8*(b*x + a) \\
&)/b^4 + (b^20*c*d^7 - 41*a*b^19*d^8)/(b^23*d^8)) - (7*b^21*c^2*d^6 + 26*a*b \\
& ^20*c*d^7 - 513*a^2*b^19*d^8)/(b^23*d^8)) + 5*(7*b^22*c^3*d^5 + 19*a*b^21*c \\
& ^2*d^6 + 37*a^2*b^20*c*d^7 - 447*a^3*b^19*d^8)/(b^23*d^8))*(b*x + a) - 15*(\\
& 7*b^23*c^4*d^4 + 12*a*b^22*c^3*d^5 + 18*a^2*b^21*c^2*d^6 + 28*a^3*b^20*c*d^ \\
& 7 - 193*a^4*b^19*d^8)/(b^23*d^8))*\text{sqrt}(b*x + a) - 15*(7*b^5*c^5 + 5*a*b^4*c \\
& ^4*d + 6*a^2*b^3*c^3*d^2 + 10*a^3*b^2*c^2*d^3 + 35*a^4*b*c*d^4 - 63*a^5*d^5 \\
&)*\log(abs(-\text{sqrt}(b*d)*\text{sqrt}(b*x + a) + \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)))/ \\
& (\text{sqrt}(b*d)*b^3*d^4))*b*c*d*abs(b) + 12*(\text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d) \\
& *(2*(4*(b*x + a)*(6*(b*x + a)*(8*(b*x + a)/b^4 + (b^20*c*d^7 - 41*a*b^19*d^ \\
& 8)/(b^23*d^8)) - (7*b^21*c^2*d^6 + 26*a*b^20*c*d^7 - 513*a^2*b^19*d^8)/(b^2 \\
& 3*d^8)) + 5*(7*b^22*c^3*d^5 + 19*a*b^21*c^2*d^6 + 37*a^2*b^20*c*d^7 - 447*a \\
& ^3*b^19*d^8)/(b^23*d^8))*(b*x + a) - 15*(7*b^23*c^4*d^4 + 12*a*b^22*c^3*d^5 \\
& + 18*a^2*b^21*c^2*d^6 + 28*a^3*b^20*c*d^7 - 193*a^4*b^19*d^8)/(b^23*d^8))* \\
& \text{sqrt}(b*x + a) - 15*(7*b^5*c^5 + 5*a*b^4*c^4*d + 6*a^2*b^3*c^3*d^2 + 10*a^3* \\
& b^2*c^2*d^3 + 35*a^4*b*c*d^4 - 63*a^5*d^5)*\log(abs(-\text{sqrt}(b*d)*\text{sqrt}(b*x + a) \\
& + \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)))/(\text{sqrt}(b*d)*b^3*d^4)) * a*d^2*abs(b) \\
& + 320*(\text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)*\text{sqrt}(b*x + a)*(2*(b*x + a)*(4*(b \\
& *x + a)/b^2 + (b^6*c*d^3 - 13*a*b^5*d^4)/(b^7*d^4)) - 3*(b^7*c^2*d^2 + 2*a* \\
& b^6*c*d^3 - 11*a^2*b^5*d^4)/(b^7*d^4)) - 3*(b^3*c^3 + a*b^2*c^2*d + 3*a^2*b \\
& *c*d^2 - 5*a^3*d^3)*\log(abs(-\text{sqrt}(b*d)*\text{sqrt}(b*x + a) + \text{sqrt}(b^2*c + (b*x + \\
& a)*b*d - a*b*d)))/(\text{sqrt}(b*d)*b*d^2)) * a^3*d^2*abs(b)/b^2 + 120*(\text{sqrt}(b^2*c + \\
& (b*x + a)*b*d - a*b*d)*(2*(b*x + a)*(4*(b*x + a)*(6*(b*x + a)/b^3 + (b^12*c \\
& *d^5 - 25*a*b^11*d^6)/(b^14*d^6)) - (5*b^13*c^2*d^4 + 14*a*b^12*c*d^5 - 16
\end{aligned}$$

$$\begin{aligned}
& 3*a^2*b^{11}*d^6)/(b^{14}*d^6)) + 3*(5*b^{14}*c^3*d^3 + 9*a*b^{13}*c^2*d^4 + 15*a^2 \\
& *b^{12}*c*d^5 - 93*a^3*b^{11}*d^6)/(b^{14}*d^6))*\text{sqrt}(b*x + a) + 3*(5*b^4*c^4 + 4 \\
& *a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 + 20*a^3*b*c*d^3 - 35*a^4*d^4)*\log(\text{abs}(-\text{sqrt} \\
& \text{rt}(b*d))*\text{sqrt}(b*x + a) + \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)))/(\text{sqrt}(b*d)*b^ \\
& 2*d^3))*a^2*d^2*\text{abs}(b)/b + (\text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))*(2*(4*(2*(b \\
& *x + a))*(8*(b*x + a))*(10*(b*x + a)/b^5 + (b^30*c*d^9 - 61*a*b^29*d^10)/(b^3 \\
& 4*d^10)) - 3*(3*b^31*c^2*d^8 + 14*a*b^30*c*d^9 - 417*a^2*b^29*d^10)/(b^34*d \\
& ^10)) + (21*b^32*c^3*d^7 + 77*a*b^31*c^2*d^8 + 183*a^2*b^30*c*d^9 - 3481*a^ \\
& 3*b^29*d^10)/(b^34*d^10))*(b*x + a) - 5*(21*b^33*c^4*d^6 + 56*a*b^32*c^3*d^ \\
& 7 + 106*a^2*b^31*c^2*d^8 + 176*a^3*b^30*c*d^9 - 2279*a^4*b^29*d^10)/(b^34*d \\
& ^10))*(b*x + a) + 15*(21*b^34*c^5*d^5 + 35*a*b^33*c^4*d^6 + 50*a^2*b^32*c^3 \\
& *d^7 + 70*a^3*b^31*c^2*d^8 + 105*a^4*b^30*c*d^9 - 793*a^5*b^29*d^10)/(b^34* \\
& d^10))*\text{sqrt}(b*x + a) + 15*(21*b^6*c^6 + 14*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 \\
& + 20*a^3*b^3*c^3*d^3 + 35*a^4*b^2*c^2*d^4 + 126*a^5*b*c*d^5 - 231*a^6*d^6) \\
& *\log(\text{abs}(-\text{sqrt}(b*d))*\text{sqrt}(b*x + a) + \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)))/ \\
& (\text{sqrt}(b*d)*b^4*d^5))*b*d^2*\text{abs}(b) + 5760*(\text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d \\
&)*(2*b*x + 2*a + (b*c*d - 5*a*d^2)/d^2))*\text{sqrt}(b*x + a) + (b^3*c^2 + 2*a*b^2* \\
& c*d - 3*a^2*b*d^2)*\log(\text{abs}(-\text{sqrt}(b*d))*\text{sqrt}(b*x + a) + \text{sqrt}(b^2*c + (b*x + a \\
&)*b*d - a*b*d)))/(\text{sqrt}(b*d)*d))*a^2*c^2*\text{abs}(b)/b^2 + 3840*(\text{sqrt}(b^2*c + (b* \\
& x + a)*b*d - a*b*d)*(2*b*x + 2*a + (b*c*d - 5*a*d^2)/d^2))*\text{sqrt}(b*x + a) + (\\
& b^3*c^2 + 2*a*b^2*c*d - 3*a^2*b*d^2)*\log(\text{abs}(-\text{sqrt}(b*d))*\text{sqrt}(b*x + a) + \text{sqrt} \\
& \text{rt}(b^2*c + (b*x + a)*b*d - a*b*d)))/(\text{sqrt}(b*d)*d))*a^3*c*d*\text{abs}(b)/b^3)/b
\end{aligned}$$

maple [B] time = 0.01, size = 1089, normalized size = 4.16

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x+a)^{(5/2)}*(d*x+c)^{(5/2)}, x)$

[Out] $1/6/d*(b*x+a)^{(5/2)}*(d*x+c)^{(7/2)}+25/256*((b*x+a)*(d*x+c))^{(1/2)}/(d*x+c)^{(1/2)}/(b*x+a)^{(1/2)}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{(1/2)}+(b*d*x^2+a*c+(a*d+b*c)*x)^{(1/2)})/(b*d)^{(1/2)}*a^3*c^3-1/16/d^2*(b*x+a)^{(1/2)}*(d*x+c)^{(7/2)}*a*b*c+5/192/d^2*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*c^3*b*a+25/512/d^2*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a*c^4*b+1/64/d^2*(d*x+c)^{(5/2)}*(b*x+a)^{(1/2)}*c^2*b*a-25/512*d/b^2*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a^4*c+1/192/b*(d*x+c)^{(5/2)}*(b*x+a)^{(1/2)}*a^3+1/12/d*(b*x+a)^{(3/2)}*(d*x+c)^{(7/2)}*a+1/32/d*(b*x+a)^{(1/2)}*(d*x+c)^{(7/2)}*a^2-1/12/d^2*(b*x+a)^{(3/2)}*(d*x+c)^{(7/2)}*b*c-5/128/d*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*a^2*c^2-25/256/d*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a^2*c^3-5/768/d^3*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*c^4*b^2-1/64/d*(d*x+c)^{(5/2)}*(b*x+a)^{(1/2)}*a^2*c+25/256/b*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a^3*c^2+5/192/b*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*a^3*c+5/512*d^2/b^3*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a^5-5/512/d^3*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*c^5*b^2-1/192/d^3*(d*x+c)^{(5/2)}*(b*x+a)^{(1/2)}*c^3*b^2-5/768*d/b^2*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*a^4+1/32/d^3*(b*x+a)^{(1/2)}*(d*x+c)^{(7/2)}*b^2*c^2-75/1024*d/b*((b*x+a)*(d*x+c))^{(1/2)}/(d*x+c)^{(1/2)}/(b*x+a)^{(1/2)}*1$

```

n((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d
)^(1/2)*a^4*c^2+15/512*d^2/b^2*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*x+a
)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1
/2))/(b*d)^(1/2)*a^5*c+15/512/d^2*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/2)/(b*
x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)
^(1/2))/(b*d)^(1/2)*a*c^5*b^2-75/1024/d*((b*x+a)*(d*x+c))^(1/2)/(d*x+c)^(1/
2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b
*c)*x)^(1/2))/(b*d)^(1/2)*a^2*c^4*b-5/1024/d^3*((b*x+a)*(d*x+c))^(1/2)/(d*x
+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c
+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*c^6*b^3-5/1024*d^3/b^3*((b*x+a)*(d*x+c))^(
1/2)/(d*x+c)^(1/2)/(b*x+a)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*
d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)*a^6

```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(5/2)*(d*x+c)^(5/2),x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError >> Computation failed since Maxima requested a
dditional constraints; using the 'assume' command before evaluation *may* h
elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more
details)Is a*d-b*c zero or nonzero?
```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{5/2} (c + dx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(5/2)*(c + d*x)^(5/2),x)
```

```
[Out] int((a + b*x)^(5/2)*(c + d*x)^(5/2), x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{5}{2}} (c + dx)^{\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(5/2)*(d*x+c)**(5/2),x)
```

```
[Out] Integral((a + b*x)**(5/2)*(c + d*x)**(5/2), x)
```

3.1482 $\int (a + bx)^{3/2}(c + dx)^{5/2} dx$

Optimal. Leaf size=224

$$\frac{3(bc - ad)^5 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{128b^{7/2}d^{5/2}} - \frac{3\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^4}{128b^3d^2} + \frac{(a + bx)^{3/2}\sqrt{c+dx}(bc - ad)^3}{64b^3d} + \frac{(a + bx)^{5/2}\sqrt{c+dx}}{16b^3}$$

[Out] $\frac{1}{8}(-a*d+b*c)*(b*x+a)^{(5/2)}*(d*x+c)^{(3/2)}/b^2+1/5*(b*x+a)^{(5/2)}*(d*x+c)^{(5/2)}/b+3/128*(-a*d+b*c)^5*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(7/2)}/d^{(5/2)}+1/64*(-a*d+b*c)^3*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/b^3/d+1/16*(-a*d+b*c)^2*(b*x+a)^{(5/2)}*(d*x+c)^{(1/2)}/b^3-3/128*(-a*d+b*c)^4*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b^3/d^2$

Rubi [A] time = 0.12, antiderivative size = 224, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$-\frac{3\sqrt{a+bx}\sqrt{c+dx}(bc - ad)^4}{128b^3d^2} + \frac{3(bc - ad)^5 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{128b^{7/2}d^{5/2}} + \frac{(a + bx)^{3/2}\sqrt{c+dx}(bc - ad)^3}{64b^3d} + \frac{(a + bx)^{5/2}\sqrt{c+dx}}{16b^3}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}*(c + d*x)^{(5/2)}, x]$

[Out] $\frac{-3*(b*c - a*d)^4*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x]}{(128*b^3*d^2)} + \frac{((b*c - a*d)^3*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])}{(64*b^3*d)} + \frac{((b*c - a*d)^2*(a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x])}{(16*b^3)} + \frac{((b*c - a*d)*(a + b*x)^{(5/2)}*(c + d*x)^{(3/2)})}{(8*b^2)} + \frac{((a + b*x)^{(5/2)}*(c + d*x)^{(5/2)})}{(5*b)} + \frac{(3*(b*c - a*d)^5*\operatorname{ArcTan}h[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))}{(128*b^{(7/2)}*d^{(5/2)})}$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{NeQ}[m + n + 1, 0] \&\& !(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] || (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m - n, 0]))) \&\& !\operatorname{ILtQ}[m + n + 2, 0] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Den}$

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int (a + bx)^{3/2} (c + dx)^{5/2} dx &= \frac{(a + bx)^{5/2} (c + dx)^{5/2}}{5b} + \frac{(bc - ad) \int (a + bx)^{3/2} (c + dx)^{3/2} dx}{2b} \\
 &= \frac{(bc - ad)(a + bx)^{5/2} (c + dx)^{3/2}}{8b^2} + \frac{(a + bx)^{5/2} (c + dx)^{5/2}}{5b} + \frac{(3(bc - ad)^2) \int (a + bx)^{3/2} (c + dx)^{1/2} dx}{16b^2} \\
 &= \frac{(bc - ad)^2 (a + bx)^{5/2} \sqrt{c + dx}}{16b^3} + \frac{(bc - ad)(a + bx)^{5/2} (c + dx)^{3/2}}{8b^2} + \frac{(a + bx)^{5/2} (c + dx)^{5/2}}{5b} \\
 &= \frac{(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{64b^3 d} + \frac{(bc - ad)^2 (a + bx)^{5/2} \sqrt{c + dx}}{16b^3} + \frac{(bc - ad)(a + bx)^{5/2} (c + dx)^{3/2}}{8b^2} \\
 &= -\frac{3(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128b^3 d^2} + \frac{(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{64b^3 d} + \frac{(bc - ad)^2 (a + bx)^{5/2} (c + dx)^{3/2}}{16b^3} \\
 &= -\frac{3(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128b^3 d^2} + \frac{(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{64b^3 d} + \frac{(bc - ad)^2 (a + bx)^{5/2} (c + dx)^{3/2}}{16b^3} \\
 &= -\frac{3(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128b^3 d^2} + \frac{(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{64b^3 d} + \frac{(bc - ad)^2 (a + bx)^{5/2} (c + dx)^{3/2}}{16b^3} \\
 &= -\frac{3(bc - ad)^4 \sqrt{a + bx} \sqrt{c + dx}}{128b^3 d^2} + \frac{(bc - ad)^3 (a + bx)^{3/2} \sqrt{c + dx}}{64b^3 d} + \frac{(bc - ad)^2 (a + bx)^{5/2} (c + dx)^{3/2}}{16b^3}
 \end{aligned}$$

Mathematica [A] time = 1.47, size = 187, normalized size = 0.83

$$(a + bx)^{5/2} \sqrt{c + dx} \left(\frac{15(bc-ad)^{9/2} \sinh^{-1}\left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{bc-ad}}\right)}{d^{5/2}(a+bx)^{5/2} \sqrt{\frac{b(c+dx)}{bc-ad}}} - \frac{15(bc-ad)^4}{d^2(a+bx)^2} + \frac{10(bc-ad)^3}{d(a+bx)} + 80b(c+dx)(bc-ad) + 40(bc-ad)^2 + 128b^2c^2 \right) / 640b^3$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)*(c + d*x)^(5/2), x]

[Out] ((a + b*x)^(5/2)*Sqrt[c + d*x]*(40*(b*c - a*d)^2 - (15*(b*c - a*d)^4)/(d^2*(a + b*x)^2) + (10*(b*c - a*d)^3)/(d*(a + b*x)) + 80*b*(b*c - a*d)*(c + d*x) + 128*b^2*(c + d*x)^2 + (15*(b*c - a*d)^(9/2)*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(d^(5/2)*(a + b*x)^(5/2)*Sqrt[(b*(c + d*x))/(b*c - a*d)])))/(640*b^3)

fricas [A] time = 0.50, size = 702, normalized size = 3.13

$$\left[\frac{15(b^5c^5 - 5ab^4c^4d + 10a^2b^3c^3d^2 - 10a^3b^2c^2d^3 + 5a^4bcd^4 - a^5d^5)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 - \dots)}{\dots} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(5/2), x, algorithm="fricas")

[Out] [-1/2560*(15*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 - 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(128*b^5*d^5*x^4 - 15*b^5*c^4*d + 70*a*b^4*c^3*d^2 + 128*a^2*b^3*c^2*d^3 - 70*a^3*b^2*c*d^4 + 15*a^4*b*d^5 + 16*(21*b^5*c*d^4 + 11*a*b^4*d^5)*x^3 + 8*(31*b^5*c^2*d^3 + 64*a*b^4*c*d^4 + a^2*b^3*d^5)*x^2 + 2*(5*b^5*c^3*d^2 + 233*a*b^4*c^2*d^3 + 23*a^2*b^3*c*d^4 - 5*a^3*b^2*d^5)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*d^3), -1/1280*(15*(b^5*c^5 - 5*a*b^4*c^4*d + 10*a^2*b^3*c^3*d^2 - 10*a^3*b^2*c^2*d^3 + 5*a^4*b*c*d^4 - a^5*d^5)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)) - 2*(128*b^5*d^5*x^4 - 15*b^5*c^4*d + 70*a*b^4*c^3*d^2 + 128*a^2*b^3*c^2*d^3 - 70*a^3*b^2*c*d^4 + 15*a^4*b*d^5 + 16*(21*b^5*c*d^4 + 11*a*b^4*d^5)*x^3 + 8*(31*b^5*c^2*d^3 + 64*a*b^4*c*d^4 + a^2*b^3*d^5)*x^2 + 2*(5*b^5*c^3*d^2 + 233*a*b^4*c^2*d^3 + 23*a^2*b^3*c*d^4 - 5*a^3*b^2*d^5)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*d^3)]

giac [B] time = 2.33, size = 1962, normalized size = 8.76

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(5/2),x, algorithm="giac")

[Out] $\frac{1}{1920} \cdot (80 \cdot (\sqrt{b^2c + (bx+a)bd - abd}) \sqrt{bx+a} \cdot (2(bx+a) \cdot (4(bx+a)/b^2 + (b^6cd^3 - 13ab^5d^4)/(b^7d^4)) - 3(b^7c^2d^2 + 2ab^6cd^3 - 11a^2b^5d^4)/(b^7d^4)) - 3(b^3c^3 + ab^2c^2d + 3a^2b^3cd^2 - 5a^3d^3) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd}) \cdot b^2 \cdot \text{abs}(b) - 1920 \cdot ((b^2c - abd) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / \sqrt{bd} - \sqrt{b^2c + (bx+a)bd - abd} \cdot \sqrt{bx+a}) \cdot a^2 \cdot c^2 \cdot \text{abs}(b) / b^2 + 20 \cdot (\sqrt{b^2c + (bx+a)bd - abd}) \cdot (2(bx+a) \cdot (4(bx+a) \cdot (6(bx+a)/b^3 + (b^{12}cd^5 - 25ab^{11}d^6)/(b^{14}d^6)) - (5b^{13}c^2d^4 + 14ab^{12}cd^5 - 163a^2b^{11}d^6)/(b^{14}d^6)) + 3 \cdot (5b^{14}c^3d^3 + 9ab^{13}c^2d^4 + 15a^2b^{12}cd^5 - 93a^3b^{11}d^6)/(b^{14}d^6)) \cdot \sqrt{bx+a} + 3 \cdot (5b^4c^4 + 4ab^3c^3d + 6a^2b^2c^2d^2 + 20a^3b^3cd^3 - 35a^4d^4) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd}) \cdot b^2 \cdot d^3 \cdot \text{abs}(b) + 320 \cdot (\sqrt{b^2c + (bx+a)bd - abd}) \cdot \sqrt{bx+a} \cdot (2(bx+a) \cdot (4(bx+a)/b^2 + (b^6cd^3 - 13ab^5d^4)/(b^7d^4)) - 3(b^7c^2d^2 + 2ab^6cd^3 - 11a^2b^5d^4)/(b^7d^4)) - 3(b^3c^3 + ab^2c^2d + 3a^2b^3cd^2 - 5a^3d^3) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd}) \cdot b \cdot d^2 \cdot \text{abs}(b) / b + (\sqrt{b^2c + (bx+a)bd - abd}) \cdot (2 \cdot (4(bx+a) \cdot (6(bx+a) \cdot (8(bx+a)/b^4 + (b^{20}cd^7 - 41ab^{19}d^8)/(b^{23}d^8)) - (7b^{21}c^2d^6 + 26ab^{20}cd^7 - 513a^2b^{19}d^8)/(b^{23}d^8)) + 5 \cdot (7b^{22}c^3d^5 + 19ab^{21}c^2d^6 + 37a^2b^{20}cd^7 - 447a^3b^{19}d^8)/(b^{23}d^8)) \cdot (bx+a) - 15 \cdot (7b^{23}c^4d^4 + 12ab^{22}c^3d^5 + 18a^2b^{21}c^2d^6 + 28a^3b^{20}cd^7 - 193a^4b^{19}d^8)/(b^{23}d^8)) \cdot \sqrt{bx+a} - 15 \cdot (7b^5c^5 + 5ab^4c^4d + 6a^2b^3c^3d^2 + 10a^3b^2c^2d^3 + 35a^4b^3cd^4 - 63a^5d^5) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd}) \cdot b^3 \cdot d^4 \cdot \text{abs}(b) + 80 \cdot (\sqrt{b^2c + (bx+a)bd - abd}) \cdot \sqrt{bx+a} \cdot (2(bx+a) \cdot (4(bx+a)/b^2 + (b^6cd^3 - 13ab^5d^4)/(b^7d^4)) - 3(b^7c^2d^2 + 2ab^6cd^3 - 11a^2b^5d^4)/(b^7d^4)) - 3(b^3c^3 + ab^2c^2d + 3a^2b^3cd^2 - 5a^3d^3) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd}) \cdot b \cdot d^2 \cdot \text{abs}(b) / b^2 + 20 \cdot (\sqrt{b^2c + (bx+a)bd - abd}) \cdot (2(bx+a) \cdot (4(bx+a) \cdot (6(bx+a)/b^3 + (b^{12}cd^5 - 25ab^{11}d^6)/(b^{14}d^6)) - (5b^{13}c^2d^4 + 14ab^{12}cd^5 - 163a^2b^{11}d^6)/(b^{14}d^6)) + 3 \cdot (5b^{14}c^3d^3 + 9ab^{13}c^2d^4 + 15a^2b^{12}cd^5 - 93a^3b^{11}d^6)/(b^{14}d^6)) \cdot \sqrt{bx+a} + 3 \cdot (5b^4c^4 + 4ab^3c^3d + 6a^2b^2c^2d^2 + 20a^3b^3cd^3 - 35a^4d^4) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd}) \cdot b^2 \cdot d^3 \cdot \text{abs}(b) / b + 960 \cdot (\sqrt{b^2c + (bx+a)bd - abd}) \cdot (2bx + 2a + (bcd - 5ad^2)/d^2) \cdot \sqrt{bx+a} + (b^3c^2 + 2ab^2cd - 3a^2bd^2) \cdot \log(\text{abs}(-\sqrt{bd}) \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd})) / (\sqrt{bd}) \cdot d)$

$$*a*c^2*abs(b)/b^2 + 960*(sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*(2*b*x + 2*a + (b*c*d - 5*a*d^2)/d^2)*sqrt(b*x + a) + (b^3*c^2 + 2*a*b^2*c*d - 3*a^2*b*d^2)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/(sqrt(b*d)*d))*a^2*c*d*abs(b)/b^3)/b$$

maple [B] time = 0.01, size = 848, normalized size = 3.79

$$\frac{3\sqrt{(bx+a)(dx+c)} a^5 d^3 \ln\left(\frac{bdx+\frac{1}{2}ad+\frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2+ac+(ad+bc)x}\right)}{256\sqrt{dx+c}\sqrt{bx+a}\sqrt{bd}b^3} + \frac{15\sqrt{(bx+a)(dx+c)} a^4 c d^2 \ln\left(\frac{bdx+\frac{1}{2}ad}{\sqrt{bd}}\right)}{256\sqrt{dx+c}\sqrt{bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)*(d*x+c)^(5/2),x)

[Out] $\frac{1}{5}d*(b*x+a)^{(3/2)}*(d*x+c)^{(7/2)} + \frac{3}{64}b*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*a^2*c - \frac{3}{32}d/b^2*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a^3*c + \frac{9}{64}b*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a^2*c^2 + \frac{3}{40}d*(b*x+a)^{(1/2)}*(d*x+c)^{(7/2)}*a - \frac{1}{64}d/b^2*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*a^3 - \frac{3}{64}d*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*a*c^2 + \frac{1}{64}d^2*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*c^3*b + \frac{3}{128}d^2/b^3*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a^4 - \frac{3}{32}d*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a*c^3 + \frac{3}{128}d^2*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*c^4*b - \frac{3}{40}d^2*(b*x+a)^{(1/2)}*(d*x+c)^{(7/2)}*b*c + \frac{1}{80}b*(d*x+c)^{(5/2)}*(b*x+a)^{(1/2)}*a^2 - \frac{1}{40}d*(d*x+c)^{(5/2)}*(b*x+a)^{(1/2)}*a*c + \frac{1}{80}d^2*(d*x+c)^{(5/2)}*(b*x+a)^{(1/2)}*c^2*b + \frac{15}{128}*((b*x+a)*(d*x+c))^{(1/2)}/(d*x+c)^{(1/2)}/(b*x+a)^{(1/2)}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{(1/2)}+(b*d*x^2+a*c+(a*d+b*c)*x)^{(1/2)})/(b*d)^{(1/2)}*a^2*c^3 + \frac{15}{256}d^2/b^2*((b*x+a)*(d*x+c))^{(1/2)}/(d*x+c)^{(1/2)}/(b*x+a)^{(1/2)}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{(1/2)}+(b*d*x^2+a*c+(a*d+b*c)*x)^{(1/2)})/(b*d)^{(1/2)}*a^4*c - \frac{15}{128}d/b*((b*x+a)*(d*x+c))^{(1/2)}/(d*x+c)^{(1/2)}/(b*x+a)^{(1/2)}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{(1/2)}+(b*d*x^2+a*c+(a*d+b*c)*x)^{(1/2)})/(b*d)^{(1/2)}*a^3*c^2 - \frac{15}{256}d*((b*x+a)*(d*x+c))^{(1/2)}/(d*x+c)^{(1/2)}/(b*x+a)^{(1/2)}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{(1/2)}+(b*d*x^2+a*c+(a*d+b*c)*x)^{(1/2)})/(b*d)^{(1/2)}*a*c^4*b + \frac{3}{256}d^2*((b*x+a)*(d*x+c))^{(1/2)}/(d*x+c)^{(1/2)}/(b*x+a)^{(1/2)}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{(1/2)}+(b*d*x^2+a*c+(a*d+b*c)*x)^{(1/2)})/(b*d)^{(1/2)}*c^5*b^2 - \frac{3}{256}d^3/b^3*((b*x+a)*(d*x+c))^{(1/2)}/(d*x+c)^{(1/2)}/(b*x+a)^{(1/2)}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{(1/2)}+(b*d*x^2+a*c+(a*d+b*c)*x)^{(1/2)})/(b*d)^{(1/2)}*a^5$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* h

elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{3/2} (c + dx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)*(c + d*x)^(5/2), x)

[Out] int((a + b*x)^(3/2)*(c + d*x)^(5/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{3}{2}} (c + dx)^{\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)*(d*x+c)**(5/2), x)

[Out] Integral((a + b*x)**(3/2)*(c + d*x)**(5/2), x)

3.1483 $\int \sqrt{a+bx}(c+dx)^{5/2} dx$

Optimal. Leaf size=186

$$-\frac{5(bc-ad)^4 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{64b^{7/2}d^{3/2}} + \frac{5\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^3}{64b^3d} + \frac{5(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^2}{32b^3} + \frac{5(a+bx)^{3/2}(c+dx)^{5/2}}{24b^2}$$

[Out] $5/24*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(3/2)}/b^2+1/4*(b*x+a)^{(3/2)}*(d*x+c)^{(5/2)}/b-5/64*(-a*d+b*c)^4*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(7/2)}/d^{(3/2)}+5/32*(-a*d+b*c)^2*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/b^3+5/64*(-a*d+b*c)^3*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b^3/d$

Rubi [A] time = 0.09, antiderivative size = 186, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$-\frac{5(bc-ad)^4 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{64b^{7/2}d^{3/2}} + \frac{5\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^3}{64b^3d} + \frac{5(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^2}{32b^3} + \frac{5(a+bx)^{3/2}(c+dx)^{5/2}}{24b^2}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[a + b*x]*(c + d*x)^(5/2), x]`

[Out] $(5*(b*c - a*d)^3*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(64*b^3*d) + (5*(b*c - a*d)^2*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(32*b^3) + (5*(b*c - a*d)*(a + b*x)^{(3/2)}*(c + d*x)^{(3/2)})/(24*b^2) + ((a + b*x)^{(3/2)}*(c + d*x)^{(5/2)})/(4*b) - (5*(b*c - a*d)^4*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/(64*b^{(7/2)}*d^{(3/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
```

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \sqrt{a+bx}(c+dx)^{5/2} dx &= \frac{(a+bx)^{3/2}(c+dx)^{5/2}}{4b} + \frac{(5(bc-ad)) \int \sqrt{a+bx}(c+dx)^{3/2} dx}{8b} \\
 &= \frac{5(bc-ad)(a+bx)^{3/2}(c+dx)^{3/2}}{24b^2} + \frac{(a+bx)^{3/2}(c+dx)^{5/2}}{4b} + \frac{(5(bc-ad)^2) \int \sqrt{a+bx}}{16b^2} \\
 &= \frac{5(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}}{32b^3} + \frac{5(bc-ad)(a+bx)^{3/2}(c+dx)^{3/2}}{24b^2} + \frac{(a+bx)^{3/2}(c+dx)^{5/2}}{4b} \\
 &= \frac{5(bc-ad)^3\sqrt{a+bx}\sqrt{c+dx}}{64b^3d} + \frac{5(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}}{32b^3} + \frac{5(bc-ad)(a+bx)^{3/2}(c+dx)^{3/2}}{24b^2} \\
 &= \frac{5(bc-ad)^3\sqrt{a+bx}\sqrt{c+dx}}{64b^3d} + \frac{5(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}}{32b^3} + \frac{5(bc-ad)(a+bx)^{3/2}(c+dx)^{3/2}}{24b^2} \\
 &= \frac{5(bc-ad)^3\sqrt{a+bx}\sqrt{c+dx}}{64b^3d} + \frac{5(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}}{32b^3} + \frac{5(bc-ad)(a+bx)^{3/2}(c+dx)^{3/2}}{24b^2} \\
 &= \frac{5(bc-ad)^3\sqrt{a+bx}\sqrt{c+dx}}{64b^3d} + \frac{5(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}}{32b^3} + \frac{5(bc-ad)(a+bx)^{3/2}(c+dx)^{3/2}}{24b^2}
 \end{aligned}$$

Mathematica [A] time = 0.58, size = 191, normalized size = 1.03

$$\frac{b\sqrt{d}\sqrt{a+bx}(c+dx)(15a^3d^3 - 5a^2bd^2(11c+2dx) + ab^2d(73c^2 + 36cdx + 8d^2x^2)) + b^3(15c^3 + 118c^2dx + 136cdx^2 + 45d^3x^3)}{192b^4d^{3/2}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]*(c + d*x)^(5/2),x]

[Out] (b*Sqrt[d]*Sqrt[a + b*x]*(c + d*x)*(15*a^3*d^3 - 5*a^2*b*d^2*(11*c + 2*d*x) + a*b^2*d*(73*c^2 + 36*c*d*x + 8*d^2*x^2) + b^3*(15*c^3 + 118*c^2*d*x + 136*c*d^2*x^2 + 48*d^3*x^3)) - 15*(b*c - a*d)^(9/2)*Sqrt[(b*(c + d*x))/(b*c - a*d)]*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]]/(192*b^4*d^(3/2)*Sqrt[c + d*x])

fricas [A] time = 0.50, size = 540, normalized size = 2.90

$$\left[\frac{15(b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 - 4(2bdx + bc + a^2d))}{\dots} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(5/2),x, algorithm="fricas")

[Out] [1/768*(15*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 - 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x) + 4*(48*b^4*d^4*x^3 + 15*b^4*c^3*d + 73*a*b^3*c^2*d^2 - 55*a^2*b^2*c*d^3 + 15*a^3*b*d^4 + 8*(17*b^4*c*d^3 + a*b^3*d^4)*x^2 + 2*(59*b^4*c^2*d^2 + 18*a*b^3*c*d^3 - 5*a^2*b^2*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*d^2), 1/384*(15*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c))/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x) + 2*(48*b^4*d^4*x^3 + 15*b^4*c^3*d + 73*a*b^3*c^2*d^2 - 55*a^2*b^2*c*d^3 + 15*a^3*b*d^4 + 8*(17*b^4*c*d^3 + a*b^3*d^4)*x^2 + 2*(59*b^4*c^2*d^2 + 18*a*b^3*c*d^3 - 5*a^2*b^2*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*d^2)]

giac [B] time = 1.93, size = 1083, normalized size = 5.82

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(5/2),x, algorithm="giac")

[Out] -1/192*(192*((b^2*c - a*b*d)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/sqrt(b*d) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*sqrt(b*x + a))*a*c^2*abs(b)/b^2 - 16*(sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*sqrt(b*x + a)*(2*(b*x + a)*(4*(b*x + a)/b^2 + (b^6*c*d^3 - 13*a*b^5*d^4)/(b^7*d^4)) - 3*(b^7*c^2*d^2 + 2*a*b^6*c*d^3 - 11*a^2*b^5*d^4)/(b^7*d^4)) - 3*(

$$\begin{aligned}
& b^3c^3 + a*b^2*c^2*d + 3*a^2*b*c*d^2 - 5*a^3*d^3) * \log(\text{abs}(-\sqrt{b*d}) * \sqrt{b*x + a} + \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})) / (\sqrt{b*d}) * b*d^2) * c*d * \text{abs}(b) / b - 8 * (\sqrt{b^2*c + (b*x + a)*b*d - a*b*d}) * \sqrt{b*x + a} * (2 * (b*x + a) * (4 * (b*x + a) / b^2 + (b^6*c*d^3 - 13*a*b^5*d^4) / (b^7*d^4)) - 3 * (b^7*c^2*d^2 + 2*a*b^6*c*d^3 - 11*a^2*b^5*d^4) / (b^7*d^4)) - 3 * (b^3*c^3 + a*b^2*c^2*d + 3*a^2*b*c*d^2 - 5*a^3*d^3) * \log(\text{abs}(-\sqrt{b*d}) * \sqrt{b*x + a} + \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})) / (\sqrt{b*d}) * b*d^2) * a*d^2 * \text{abs}(b) / b^2 - (\sqrt{b^2*c + (b*x + a)*b*d - a*b*d}) * (2 * (b*x + a) * (4 * (b*x + a) * (6 * (b*x + a) / b^3 + (b^12*c*d^5 - 25*a*b^11*d^6) / (b^14*d^6)) - (5*b^13*c^2*d^4 + 14*a*b^12*c*d^5 - 163*a^2*b^11*d^6) / (b^14*d^6)) + 3 * (5*b^14*c^3*d^3 + 9*a*b^13*c^2*d^4 + 15*a^2*b^12*c*d^5 - 93*a^3*b^11*d^6) / (b^14*d^6)) * \sqrt{b*x + a} + 3 * (5*b^4*c^4 + 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 + 20*a^3*b*c*d^3 - 35*a^4*d^4) * \log(\text{abs}(-\sqrt{b*d}) * \sqrt{b*x + a} + \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})) / (\sqrt{b*d}) * b^2 * d^3) * d^2 * \text{abs}(b) / b - 48 * (\sqrt{b^2*c + (b*x + a)*b*d - a*b*d}) * (2 * b*x + 2 * a + (b*c*d - 5*a*d^2) / d^2) * \sqrt{b*x + a} + (b^3*c^2 + 2*a*b^2*c*d - 3*a^2*b*d^2) * \log(\text{abs}(-\sqrt{b*d}) * \sqrt{b*x + a} + \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})) / (\sqrt{b*d}) * d) * c^2 * \text{abs}(b) / b^2 - 96 * (\sqrt{b^2*c + (b*x + a)*b*d - a*b*d}) * (2 * b*x + 2 * a + (b*c*d - 5*a*d^2) / d^2) * \sqrt{b*x + a} + (b^3*c^2 + 2*a*b^2*c*d - 3*a^2*b*d^2) * \log(\text{abs}(-\sqrt{b*d}) * \sqrt{b*x + a} + \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})) / (\sqrt{b*d}) * d) * a * c * d * \text{abs}(b) / b^3) / b
\end{aligned}$$

maple [B] time = 0.01, size = 641, normalized size = 3.45

$$\frac{5\sqrt{(bx+a)(dx+c)} a^4 d^3 \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad+bc)x}\right)}{128\sqrt{dx+c} \sqrt{bx+a} \sqrt{bd} b^3} + \frac{5\sqrt{(bx+a)(dx+c)} a^3 c d^2 \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad+bc)x}\right)}{32\sqrt{dx+c} \sqrt{bx+a} b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)*(d*x+c)^(5/2), x)

[Out] $\frac{1}{4}d*(b*x+a)^{(1/2)}*(d*x+c)^{(7/2)} + \frac{1}{24}b*(d*x+c)^{(5/2)}*(b*x+a)^{(1/2)}*a^{-1/24} / d*(d*x+c)^{(5/2)}*(b*x+a)^{(1/2)}*c - \frac{5}{96}d/b^2*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*a^2 + \frac{5}{48}b*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*a*c - \frac{5}{96}d*(d*x+c)^{(3/2)}*(b*x+a)^{(1/2)}*c^2 + \frac{5}{64}d^2/b^3*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a^3 - \frac{15}{64}d/b^2*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a^2*c + \frac{15}{64}b*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*a*c^2 - \frac{5}{64}d*(d*x+c)^{(1/2)}*(b*x+a)^{(1/2)}*c^3 - \frac{5}{128}d^3/b^3*((b*x+a)*(d*x+c))^{(1/2)} / (d*x+c)^{(1/2)} / (b*x+a)^{(1/2)} * \ln((b*d*x + \frac{1}{2}a*d + \frac{1}{2}b*c) / (b*d)^{(1/2)} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{(1/2)}) / (b*d)^{(1/2)} * a^4 + \frac{5}{32}d^2/b^2*((b*x+a)*(d*x+c))^{(1/2)} / (d*x+c)^{(1/2)} / (b*x+a)^{(1/2)} * \ln((b*d*x + \frac{1}{2}a*d + \frac{1}{2}b*c) / (b*d)^{(1/2)} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{(1/2)}) / (b*d)^{(1/2)} * a^3*c - \frac{15}{64}d/b*((b*x+a)*(d*x+c))^{(1/2)} / (d*x+c)^{(1/2)} / (b*x+a)^{(1/2)} * \ln((b*d*x + \frac{1}{2}a*d + \frac{1}{2}b*c) / (b*d)^{(1/2)} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{(1/2)}) / (b*d)^{(1/2)} * a^2*c^2 + \frac{5}{32}*((b*x+a)*(d*x+c))^{(1/2)} / (d*x+c)^{(1/2)} / (b*x+a)^{(1/2)} * \ln((b*d*x + \frac{1}{2}a*d + \frac{1}{2}b*c) / (b*d)^{(1/2)} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{(1/2)}) / (b*d)^{(1/2)} * a*c^3 - \frac{5}{128}d*((b*x+a)*(d*x+c))^{(1/2)} / (d*x+c)^{(1/2)} / (b*x+a)^{(1/2)}$

$$\frac{(b*x+a)^{1/2} * \ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2} + (b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})}{(b*d)^{1/2} * c^4 * b}$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{a+bx} (c+dx)^{5/2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)*(c + d*x)^(5/2),x)

[Out] int((a + b*x)^(1/2)*(c + d*x)^(5/2), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)*(d*x+c)**(5/2),x)

[Out] Timed out

$$3.1484 \quad \int \frac{(c+dx)^{5/2}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=148

$$\frac{5(bc-ad)^3 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{8b^{7/2}\sqrt{d}} + \frac{5\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}{8b^3} + \frac{5\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)}{12b^2} + \frac{\sqrt{a+bx}(c+dx)}{3b}$$

[Out] 5/8*(-a*d+b*c)^3*arctanh(d^(1/2)*(b*x+a)^(1/2)/b^(1/2)/(d*x+c)^(1/2))/b^(7/2)/d^(1/2)+5/12*(-a*d+b*c)*(d*x+c)^(3/2)*(b*x+a)^(1/2)/b^2+1/3*(d*x+c)^(5/2)*(b*x+a)^(1/2)/b+5/8*(-a*d+b*c)^2*(b*x+a)^(1/2)*(d*x+c)^(1/2)/b^3

Rubi [A] time = 0.07, antiderivative size = 148, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$\frac{5\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}{8b^3} + \frac{5\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)}{12b^2} + \frac{5(bc-ad)^3 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{8b^{7/2}\sqrt{d}} + \frac{\sqrt{a+bx}(c+dx)}{3b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/Sqrt[a + b*x], x]

[Out] (5*(b*c - a*d)^2*Sqrt[a + b*x]*Sqrt[c + d*x])/(8*b^3) + (5*(b*c - a*d)*Sqrt[a + b*x]*(c + d*x)^(3/2))/(12*b^2) + (Sqrt[a + b*x]*(c + d*x)^(5/2))/(3*b) + (5*(b*c - a*d)^3*ArcTanh[(Sqrt[d]*Sqrt[a + b*x])/(Sqrt[b]*Sqrt[c + d*x])])/(8*b^(7/2)*Sqrt[d])

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[Rt[-b, 2]*x]/Rt[a, 2])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(c+dx)^{5/2}}{\sqrt{a+bx}} dx &= \frac{\sqrt{a+bx}(c+dx)^{5/2}}{3b} + \frac{(5(bc-ad)) \int \frac{(c+dx)^{3/2}}{\sqrt{a+bx}} dx}{6b} \\
 &= \frac{5(bc-ad)\sqrt{a+bx}(c+dx)^{3/2}}{12b^2} + \frac{\sqrt{a+bx}(c+dx)^{5/2}}{3b} + \frac{(5(bc-ad)^2) \int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx}{8b^2} \\
 &= \frac{5(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8b^3} + \frac{5(bc-ad)\sqrt{a+bx}(c+dx)^{3/2}}{12b^2} + \frac{\sqrt{a+bx}(c+dx)^{5/2}}{3b} + \frac{(5(bc-ad)^2) \int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx}{8b^2} \\
 &= \frac{5(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8b^3} + \frac{5(bc-ad)\sqrt{a+bx}(c+dx)^{3/2}}{12b^2} + \frac{\sqrt{a+bx}(c+dx)^{5/2}}{3b} + \frac{(5(bc-ad)^2) \int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx}{8b^2} \\
 &= \frac{5(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8b^3} + \frac{5(bc-ad)\sqrt{a+bx}(c+dx)^{3/2}}{12b^2} + \frac{\sqrt{a+bx}(c+dx)^{5/2}}{3b} + \frac{(5(bc-ad)^2) \int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx}{8b^2} \\
 &= \frac{5(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8b^3} + \frac{5(bc-ad)\sqrt{a+bx}(c+dx)^{3/2}}{12b^2} + \frac{\sqrt{a+bx}(c+dx)^{5/2}}{3b} + \frac{(5(bc-ad)^2) \int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx}{8b^2}
 \end{aligned}$$

Mathematica [A] time = 0.41, size = 139, normalized size = 0.94

$$\frac{\sqrt{c+dx} \left(\sqrt{a+bx} (15a^2d^2 - 10abd(4c+dx) + b^2(33c^2 + 26cdx + 8d^2x^2)) + \frac{15(bc-ad)^{5/2} \sinh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{bc-ad}}\right)}{\sqrt{d}\sqrt{\frac{b(c+dx)}{bc-ad}}} \right)}{24b^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/Sqrt[a + b*x], x]

[Out] (Sqrt[c + d*x]*(Sqrt[a + b*x]*(15*a^2*d^2 - 10*a*b*d*(4*c + d*x) + b^2*(33*c^2 + 26*c*d*x + 8*d^2*x^2)) + (15*(b*c - a*d)^(5/2)*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(Sqrt[d]*Sqrt[(b*(c + d*x))/(b*c - a*d)])))/(24*b^3)

fricas [A] time = 0.48, size = 412, normalized size = 2.78

$$\left[\frac{15(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 - 4(2bdx + bc + ad)\sqrt{bd}\sqrt{b^2c^2 + 2cdx + d^2x^2})}{b^4} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] [-1/96*(15*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 - 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(8*b^3*d^3*x^2 + 33*b^3*c^2*d - 40*a*b^2*c*d^2 + 15*a^2*b*d^3 + 2*(13*b^3*c*d^2 - 5*a*b^2*d^3)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*d), -1/48*(15*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)) - 2*(8*b^3*d^3*x^2 + 33*b^3*c^2*d - 40*a*b^2*c*d^2 + 15*a^2*b*d^3 + 2*(13*b^3*c*d^2 - 5*a*b^2*d^3)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*d)]

giac [B] time = 1.43, size = 446, normalized size = 3.01

$$\frac{24 \left(\frac{(b^2c - abd) \log \left(\frac{-\sqrt{bd} \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd}}{\sqrt{bd}} \right) - \sqrt{b^2c + (bx+a)bd - abd} \sqrt{bx+a}}{b^2} \right) c^2 |b|}{b^2} - \left(\sqrt{b^2c + (bx+a)bd - abd} \sqrt{bx+a} \left(2(bx+a) \left(\frac{4(bx+a)}{b^2} + \frac{b^6cd^3 - b^2c^2d}{b^7} \right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(1/2), x, algorithm="giac")

[Out] -1/24*(24*((b^2*c - a*b*d)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/sqrt(b*d) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*sqrt(b*x + a))*c^2*abs(b)/b^2 - (sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*sqrt(b*x + a)*(2*(b*x + a)*(4*(b*x + a)/b^2 + (b^6*c*d^3 - 13*a*b^5*d^4)/(b^7*d^4))

$$- 3*(b^7*c^2*d^2 + 2*a*b^6*c*d^3 - 11*a^2*b^5*d^4)/(b^7*d^4) - 3*(b^3*c^3 + a*b^2*c^2*d + 3*a^2*b*c*d^2 - 5*a^3*d^3)*\log(\text{abs}(-\sqrt{b*d})*\sqrt{b*x + a} + \sqrt{b^2*c + (b*x + a)*b*d - a*b*d}))/(\sqrt{b*d}*b*d^2))*d^2*\text{abs}(b)/b^2 - 12*(\sqrt{b^2*c + (b*x + a)*b*d - a*b*d})*(2*b*x + 2*a + (b*c*d - 5*a*d^2)/d^2)*\sqrt{b*x + a} + (b^3*c^2 + 2*a*b^2*c*d - 3*a^2*b*d^2)*\log(\text{abs}(-\sqrt{b*d})*\sqrt{b*x + a} + \sqrt{b^2*c + (b*x + a)*b*d - a*b*d}))/(\sqrt{b*d}*d))*c*d*\text{abs}(b)/b^3)/b$$

maple [B] time = 0.01, size = 465, normalized size = 3.14

$$\frac{5\sqrt{(bx+a)(dx+c)} a^3 d^3 \ln\left(\frac{bdx+\frac{1}{2}ad+\frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2+ac+(ad+bc)x}\right)}{16\sqrt{dx+c} \sqrt{bx+a} \sqrt{bd} b^3} + \frac{15\sqrt{(bx+a)(dx+c)} a^2 c d^2 \ln\left(\frac{bdx+\frac{1}{2}ad}{\sqrt{bd}}\right)}{16\sqrt{dx+c} \sqrt{bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^(1/2),x)

[Out] $\frac{1}{3}(d*x+c)^{5/2}(b*x+a)^{1/2}/b - 5/12/b^2(d*x+c)^{3/2}(b*x+a)^{1/2}*a*d + 5/12/b(d*x+c)^{3/2}(b*x+a)^{1/2}*c + 5/8/b^3(d*x+c)^{1/2}(b*x+a)^{1/2}*a^2*d^2 - 5/4/b^2(d*x+c)^{1/2}(b*x+a)^{1/2}*a*d*c + 5/8/b(d*x+c)^{1/2}(b*x+a)^{1/2}*c^2 - 5/16/b^3((b*x+a)*(d*x+c))^{1/2}/(d*x+c)^{1/2}/(b*x+a)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2}*a^3*d^3 + 15/16/b^2((b*x+a)*(d*x+c))^{1/2}/(d*x+c)^{1/2}/(b*x+a)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2}*a^2*d^2*c - 15/16/b((b*x+a)*(d*x+c))^{1/2}/(d*x+c)^{1/2}/(b*x+a)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2}*a*d*c^2 + 5/16*((b*x+a)*(d*x+c))^{1/2}/(d*x+c)^{1/2}/(b*x+a)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2}*c^3$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c+dx)^{5/2}}{\sqrt{a+bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/2)/(a + b*x)^(1/2), x)
```

```
[Out] int((c + d*x)^(5/2)/(a + b*x)^(1/2), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/2)/(b*x+a)**(1/2), x)
```

```
[Out] Timed out
```

$$3.1485 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=138

$$\frac{15\sqrt{d}(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{4b^{7/2}} + \frac{15d\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}{4b^3} + \frac{5d\sqrt{a+bx}(c+dx)^{3/2}}{2b^2} - \frac{2(c+dx)^{5/2}}{b\sqrt{a+bx}}$$

[Out] 15/4*(-a*d+b*c)^2*arctanh(d^(1/2)*(b*x+a)^(1/2)/b^(1/2)/(d*x+c)^(1/2))*d^(1/2)/b^(7/2)-2*(d*x+c)^(5/2)/b/(b*x+a)^(1/2)+5/2*d*(d*x+c)^(3/2)*(b*x+a)^(1/2)/b^2+15/4*d*(-a*d+b*c)*(b*x+a)^(1/2)*(d*x+c)^(1/2)/b^3

Rubi [A] time = 0.06, antiderivative size = 138, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 217, 206}

$$\frac{5d\sqrt{a+bx}(c+dx)^{3/2}}{2b^2} + \frac{15d\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}{4b^3} + \frac{15\sqrt{d}(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{4b^{7/2}} - \frac{2(c+dx)^{5/2}}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^(3/2), x]

[Out] (15*d*(b*c - a*d)*Sqrt[a + b*x]*Sqrt[c + d*x])/(4*b^3) + (5*d*Sqrt[a + b*x]*(c + d*x)^(3/2))/(2*b^2) - (2*(c + d*x)^(5/2))/(b*Sqrt[a + b*x]) + (15*Sqrt[d]*(b*c - a*d)^2*ArcTanh[(Sqrt[d]*Sqrt[a + b*x])/(Sqrt[b]*Sqrt[c + d*x])])/(4*b^(7/2))

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
```


+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/2}}{(a+bx)^{3/2}} dx &= -\frac{2(c+dx)^{5/2}}{b\sqrt{a+bx}} + \frac{(5d) \int \frac{(c+dx)^{3/2}}{\sqrt{a+bx}} dx}{b} \\
&= \frac{5d\sqrt{a+bx}(c+dx)^{3/2}}{2b^2} - \frac{2(c+dx)^{5/2}}{b\sqrt{a+bx}} + \frac{(15d(bc-ad)) \int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx}{4b^2} \\
&= \frac{15d(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4b^3} + \frac{5d\sqrt{a+bx}(c+dx)^{3/2}}{2b^2} - \frac{2(c+dx)^{5/2}}{b\sqrt{a+bx}} + \frac{(15d(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}} dx}{8b^3} \\
&= \frac{15d(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4b^3} + \frac{5d\sqrt{a+bx}(c+dx)^{3/2}}{2b^2} - \frac{2(c+dx)^{5/2}}{b\sqrt{a+bx}} + \frac{(15d(bc-ad)^2) \operatorname{Sub}}{\dots} \\
&= \frac{15d(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4b^3} + \frac{5d\sqrt{a+bx}(c+dx)^{3/2}}{2b^2} - \frac{2(c+dx)^{5/2}}{b\sqrt{a+bx}} + \frac{(15d(bc-ad)^2) \operatorname{Sub}}{\dots} \\
&= \frac{15d(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4b^3} + \frac{5d\sqrt{a+bx}(c+dx)^{3/2}}{2b^2} - \frac{2(c+dx)^{5/2}}{b\sqrt{a+bx}} + \frac{15\sqrt{d}(bc-ad)^2 \operatorname{tan}}{4b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.07, size = 71, normalized size = 0.51

$$-\frac{2(c+dx)^{5/2} {}_2F_1\left(-\frac{5}{2}, -\frac{1}{2}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^(3/2), x]

[Out] (-2*(c + d*x)^(5/2)*Hypergeometric2F1[-5/2, -1/2, 1/2, (d*(a + b*x))/(-b*c + a*d)]/(b*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(5/2))

fricas [A] time = 0.56, size = 439, normalized size = 3.18

$$\left[\frac{15(ab^2c^2 - 2a^2bcd + a^3d^2 + (b^3c^2 - 2ab^2cd + a^2bd^2)x)\sqrt{\frac{d}{b}} \log\left(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2b^2dx + \dots)\right)}{\dots} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] [1/16*(15*(a*b^2*c^2 - 2*a^2*b*c*d + a^3*d^2 + (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*x)*sqrt(d/b)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b^2*d*x + b^2*c + a*b*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(d/b) + 8*(b^2*c*d + a*b*d^2)*x) + 4*(2*b^2*d^2*x^2 - 8*b^2*c^2 + 25*a*b*c*d - 15*a^2*d^2 + (9*b^2*c*d - 5*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*x + a*b^3), -1/8*(15*(a*b^2*c^2 - 2*a^2*b*c*d + a^3*d^2 + (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*x)*sqrt(-d/b)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-d/b)/(b*d^2*x^2 + a*c*d + (b*c*d + a*d^2)*x)) - 2*(2*b^2*d^2*x^2 - 8*b^2*c^2 + 25*a*b*c*d - 15*a^2*d^2 + (9*b^2*c*d - 5*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^4*x + a*b^3)]

giac [B] time = 2.02, size = 287, normalized size = 2.08

$$\frac{1}{4} \sqrt{b^2c + (bx + a)bd - abd} \sqrt{bx + a} \left(\frac{2(bx + a)d^2|b|}{b^5} + \frac{9(b^{10}cd^3|b| - ab^9d^4|b|)}{b^{14}d^2} \right) - \frac{15(\sqrt{bd}b^2c^2|b| - 2\sqrt{bd}abcd|b|)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(3/2),x, algorithm="giac")

[Out] 1/4*sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*sqrt(b*x + a)*(2*(b*x + a)*d^2*abs(b)/b^5 + 9*(b^10*c*d^3*abs(b) - a*b^9*d^4*abs(b))/(b^14*d^2)) - 15/8*(sqrt(b*d)*b^2*c^2*abs(b) - 2*sqrt(b*d)*a*b*c*d*abs(b) + sqrt(b*d)*a^2*d^2*abs(b))*log((sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)/b^5 - 4*(sqrt(b*d)*b^3*c^3*abs(b) - 3*sqrt(b*d)*a*b^2*c^2*d*abs(b) + 3*sqrt(b*d)*a^2*b*c*d^2*abs(b) - sqrt(b*d)*a^3*d^3*abs(b))/((b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)*b^4)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{2}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^(3/2),x)

[Out] int((d*x+c)^(5/2)/(b*x+a)^(3/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{5/2}}{(a + bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/2)/(a + b*x)^(3/2),x)

[Out] int((c + d*x)^(5/2)/(a + b*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{2}}}{(a + bx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/2)/(b*x+a)**(3/2),x)

[Out] Integral((c + d*x)**(5/2)/(a + b*x)**(3/2), x)

$$3.1486 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=128

$$\frac{5d^{3/2}(bc-ad) \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{7/2}} + \frac{5d^2\sqrt{a+bx}\sqrt{c+dx}}{b^3} - \frac{10d(c+dx)^{3/2}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/2}}{3b(a+bx)^{3/2}}$$

[Out] $-2/3*(d*x+c)^{(5/2)}/b/(b*x+a)^{(3/2)}+5*d^{(3/2)}*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(7/2)}-10/3*d*(d*x+c)^{(3/2)}/b^2/(b*x+a)^{(1/2)}+5*d^2*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/b^3$

Rubi [A] time = 0.06, antiderivative size = 128, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 217, 206}

$$\frac{5d^2\sqrt{a+bx}\sqrt{c+dx}}{b^3} + \frac{5d^{3/2}(bc-ad) \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{7/2}} - \frac{10d(c+dx)^{3/2}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/2}}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^(5/2), x]

[Out] $(5*d^2*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/b^3 - (10*d*(c + d*x)^{(3/2)})/(3*b^2*\operatorname{Sqrt}[a + b*x]) - (2*(c + d*x)^{(5/2)})/(3*b*(a + b*x)^{(3/2)}) + (5*d^{(3/2)}*(b*c - a*d)*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/b^{(7/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/2}}{(a+bx)^{5/2}} dx &= -\frac{2(c+dx)^{5/2}}{3b(a+bx)^{3/2}} + \frac{(5d) \int \frac{(c+dx)^{3/2}}{(a+bx)^{3/2}} dx}{3b} \\
&= -\frac{10d(c+dx)^{3/2}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/2}}{3b(a+bx)^{3/2}} + \frac{(5d^2) \int \frac{\sqrt{c+dx}}{\sqrt{a+bx}} dx}{b^2} \\
&= \frac{5d^2\sqrt{a+bx}\sqrt{c+dx}}{b^3} - \frac{10d(c+dx)^{3/2}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/2}}{3b(a+bx)^{3/2}} + \frac{(5d^2(bc-ad)) \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{2b^3} \\
&= \frac{5d^2\sqrt{a+bx}\sqrt{c+dx}}{b^3} - \frac{10d(c+dx)^{3/2}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/2}}{3b(a+bx)^{3/2}} + \frac{(5d^2(bc-ad)) \text{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x\right)}{b^4} \\
&= \frac{5d^2\sqrt{a+bx}\sqrt{c+dx}}{b^3} - \frac{10d(c+dx)^{3/2}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/2}}{3b(a+bx)^{3/2}} + \frac{(5d^2(bc-ad)) \text{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x\right)}{b^4} \\
&= \frac{5d^2\sqrt{a+bx}\sqrt{c+dx}}{b^3} - \frac{10d(c+dx)^{3/2}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/2}}{3b(a+bx)^{3/2}} + \frac{5d^{3/2}(bc-ad) \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.57

$$\frac{2(c + dx)^{5/2} {}_2F_1\left(-\frac{5}{2}, -\frac{3}{2}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a + bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^(5/2), x]

[Out] (-2*(c + d*x)^(5/2)*Hypergeometric2F1[-5/2, -3/2, -1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(5/2))

fricas [B] time = 0.75, size = 475, normalized size = 3.71

$$\frac{15(a^2bcd - a^3d^2 + (b^3cd - ab^2d^2)x^2 + 2(ab^2cd - a^2bd^2)x)\sqrt{\frac{d}{b}} \log\left(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 - 4(2b^2\right)}{}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] [-1/12*(15*(a^2*b*c*d - a^3*d^2 + (b^3*c*d - a*b^2*d^2)*x^2 + 2*(a*b^2*c*d - a^2*b*d^2)*x)*sqrt(d/b)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 - 4*(2*b^2*d*x + b^2*c + a*b*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(d/b) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(3*b^2*d^2*x^2 - 2*b^2*c^2 - 10*a*b*c*d + 15*a^2*d^2 - 2*(7*b^2*c*d - 10*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^5*x^2 + 2*a*b^4*x + a^2*b^3), -1/6*(15*(a^2*b*c*d - a^3*d^2 + (b^3*c*d - a*b^2*d^2)*x^2 + 2*(a*b^2*c*d - a^2*b*d^2)*x)*sqrt(-d/b)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-d/b)/(b*d^2*x^2 + a*c*d + (b*c*d + a*d^2)*x)) - 2*(3*b^2*d^2*x^2 - 2*b^2*c^2 - 10*a*b*c*d + 15*a^2*d^2 - 2*(7*b^2*c*d - 10*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^5*x^2 + 2*a*b^4*x + a^2*b^3)]

giac [B] time = 2.19, size = 650, normalized size = 5.08

$$\frac{\sqrt{b^2c + (bx + a)bd - abd} \sqrt{bx + a} d^2 |b|}{b^5} - \frac{5(\sqrt{bd} bcd |b| - \sqrt{bd} ad^2 |b|) \log\left(\left(\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - a}\right)}{2b^5}\right)}{2b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(5/2),x, algorithm="giac")

[Out] $\sqrt{b^2c + (bx + a)bd - abd} \sqrt{bx + a} d^2 \text{abs}(b) / b^5 - 5/2 (\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - abd}) \log((\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - abd})^2) / b^5 - 4/3 (7 \sqrt{bd} b^6 c^4 d \text{abs}(b) - 28 \sqrt{bd} a b^5 c^3 d^2 \text{abs}(b) + 42 \sqrt{bd} a^2 b^4 c^2 d^3 a \text{bs}(b) - 28 \sqrt{bd} a^3 b^3 c d^4 \text{abs}(b) + 7 \sqrt{bd} a^4 b^2 d^5 \text{abs}(b) - 12 \sqrt{bd} (\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - abd})^2 b^4 c^3 d \text{abs}(b) + 36 \sqrt{bd} (\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - abd})^2 a b^3 c^2 d^2 \text{abs}(b) - 36 \sqrt{bd} (\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - abd})^2 a^2 b^2 c d^3 \text{abs}(b) + 12 \sqrt{bd} (\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - abd})^2 a^3 b d^4 \text{abs}(b) + 9 \sqrt{bd} (\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - abd})^4 a b c d^2 \text{abs}(b) + 9 \sqrt{bd} (\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - abd})^4 a^2 d^3 \text{abs}(b)) / ((b^2c - abd - (\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2c + (bx + a)bd - abd})^2)^3 b^4)$

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{2}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^(5/2),x)

[Out] int((d*x+c)^(5/2)/(b*x+a)^(5/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{5/2}}{(a + bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/2)/(a + b*x)^(5/2), x)
```

```
[Out] int((c + d*x)^(5/2)/(a + b*x)^(5/2), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/2)/(b*x+a)**(5/2), x)
```

```
[Out] Timed out
```

$$3.1487 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^{7/2}} dx$$

Optimal. Leaf size=120

$$\frac{2d^{5/2} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{7/2}} - \frac{2d^2\sqrt{c+dx}}{b^3\sqrt{a+bx}} - \frac{2d(c+dx)^{3/2}}{3b^2(a+bx)^{3/2}} - \frac{2(c+dx)^{5/2}}{5b(a+bx)^{5/2}}$$

[Out] $-2/3*d*(d*x+c)^{(3/2)}/b^2/(b*x+a)^{(3/2)}-2/5*(d*x+c)^{(5/2)}/b/(b*x+a)^{(5/2)}+2*d^{5/2}*arctanh(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/b^{(7/2)}-2*d^2*(d*x+c)^{(1/2)}/b^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 120, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 63, 217, 206}

$$-\frac{2d^2\sqrt{c+dx}}{b^3\sqrt{a+bx}} + \frac{2d^{5/2} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{b^{7/2}} - \frac{2d(c+dx)^{3/2}}{3b^2(a+bx)^{3/2}} - \frac{2(c+dx)^{5/2}}{5b(a+bx)^{5/2}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^(7/2), x]

[Out] $(-2*d^2*sqrt[c + d*x])/(b^3*sqrt[a + b*x]) - (2*d*(c + d*x)^{(3/2)})/(3*b^2*(a + b*x)^{(3/2)}) - (2*(c + d*x)^{(5/2)})/(5*b*(a + b*x)^{(5/2)}) + (2*d^{(5/2)}*ArcTanh[(sqrt[d]*sqrt[a + b*x])/(sqrt[b]*sqrt[c + d*x])])/b^{(7/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(c+dx)^{5/2}}{(a+bx)^{7/2}} dx &= -\frac{2(c+dx)^{5/2}}{5b(a+bx)^{5/2}} + \frac{d \int \frac{(c+dx)^{3/2}}{(a+bx)^{5/2}} dx}{b} \\
 &= -\frac{2d(c+dx)^{3/2}}{3b^2(a+bx)^{3/2}} - \frac{2(c+dx)^{5/2}}{5b(a+bx)^{5/2}} + \frac{d^2 \int \frac{\sqrt{c+dx}}{(a+bx)^{3/2}} dx}{b^2} \\
 &= -\frac{2d^2\sqrt{c+dx}}{b^3\sqrt{a+bx}} - \frac{2d(c+dx)^{3/2}}{3b^2(a+bx)^{3/2}} - \frac{2(c+dx)^{5/2}}{5b(a+bx)^{5/2}} + \frac{d^3 \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{b^3} \\
 &= -\frac{2d^2\sqrt{c+dx}}{b^3\sqrt{a+bx}} - \frac{2d(c+dx)^{3/2}}{3b^2(a+bx)^{3/2}} - \frac{2(c+dx)^{5/2}}{5b(a+bx)^{5/2}} + \frac{(2d^3) \text{Subst} \left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \sqrt{a+bx} \right)}{b^4} \\
 &= -\frac{2d^2\sqrt{c+dx}}{b^3\sqrt{a+bx}} - \frac{2d(c+dx)^{3/2}}{3b^2(a+bx)^{3/2}} - \frac{2(c+dx)^{5/2}}{5b(a+bx)^{5/2}} + \frac{(2d^3) \text{Subst} \left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}} \right)}{b^4} \\
 &= -\frac{2d^2\sqrt{c+dx}}{b^3\sqrt{a+bx}} - \frac{2d(c+dx)^{3/2}}{3b^2(a+bx)^{3/2}} - \frac{2(c+dx)^{5/2}}{5b(a+bx)^{5/2}} + \frac{2d^{5/2} \tanh^{-1} \left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}} \right)}{b^{7/2}}
 \end{aligned}$$

Mathematica [C] time = 0.07, size = 73, normalized size = 0.61

$$\frac{2(c+dx)^{5/2} {}_2F_1 \left(-\frac{5}{2}, -\frac{5}{2}; -\frac{3}{2}; \frac{d(a+bx)}{ad-bc} \right)}{5b(a+bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^(7/2),x]

[Out] (-2*(c + d*x)^(5/2)*Hypergeometric2F1[-5/2, -5/2, -3/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(5/2))

fricas [B] time = 0.95, size = 463, normalized size = 3.86

$$\frac{15 \left(b^3 d^2 x^3 + 3 a b^2 d^2 x^2 + 3 a^2 b d^2 x + a^3 d^2 \right) \sqrt{\frac{d}{b}} \log \left(8 b^2 d^2 x^2 + b^2 c^2 + 6 a b c d + a^2 d^2 + 4 \left(2 b^2 d x + b^2 c + a b d \right) \sqrt{b} \right)}{30 \left(b^6 x^3 + 3 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(7/2),x, algorithm="fricas")

[Out] [1/30*(15*(b^3*d^2*x^3 + 3*a*b^2*d^2*x^2 + 3*a^2*b*d^2*x + a^3*d^2)*sqrt(d/b)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b^2*d*x + b^2*c + a*b*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(d/b) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(23*b^2*d^2*x^2 + 3*b^2*c^2 + 5*a*b*c*d + 15*a^2*d^2 + (11*b^2*c*d + 35*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^6*x^3 + 3*a*b^5*x^2 + 3*a^2*b^4*x + a^3*b^3), -1/15*(15*(b^3*d^2*x^3 + 3*a*b^2*d^2*x^2 + 3*a^2*b*d^2*x + a^3*d^2)*sqrt(-d/b)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-d/b)/(b*d^2*x^2 + a*c*d + (b*c*d + a*d^2)*x)) + 2*(23*b^2*d^2*x^2 + 3*b^2*c^2 + 5*a*b*c*d + 15*a^2*d^2 + (11*b^2*c*d + 35*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b^6*x^3 + 3*a*b^5*x^2 + 3*a^2*b^4*x + a^3*b^3)]

giac [B] time = 2.48, size = 1025, normalized size = 8.54

$$\frac{\sqrt{bd} d^2 |b| \log \left(\left(\sqrt{bd} \sqrt{bx + a} - \sqrt{b^2 c + (bx + a)bd - abd} \right)^2 \right)}{b^5} - \frac{4 \left(23 \sqrt{bd} b^9 c^5 d^2 |b| - 115 \sqrt{bd} ab^8 c^4 d^3 |b| + 230 \sqrt{bd} \right)}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(7/2),x, algorithm="giac")

[Out] -sqrt(b*d)*d^2*abs(b)*log((sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)/b^5 - 4/15*(23*sqrt(b*d)*b^9*c^5*d^2*abs(b) - 115*sqrt(b*d)*a*b^8*c^4*d^3*abs(b) + 230*sqrt(b*d)*a^2*b^7*c^3*d^4*abs(b) - 230*sqrt(b*d)*a^3*b^6*c^2*d^5*abs(b) + 115*sqrt(b*d)*a^4*b^5*c*d^6*abs(b) - 23*sqrt(b*d)*a^5*b^4*d^7*abs(b) - 70*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*b^7*c^4*d^2*abs(b) + 280*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a*b^6*c^3*d^3*abs(b) - 420*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a

$(b*d))^{2*a^2*b^5*c^2*d^4*abs(b) + 280*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{2*a^3*b^4*c*d^5*abs(b) - 70*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{2*a^4*b^3*d^6*abs(b) + 140*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{4*b^5*c^3*d^2*abs(b) - 420*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{4*a*b^4*c^2*d^3*abs(b) + 420*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{4*a^2*b^3*c*d^4*abs(b) - 140*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{4*a^3*b^2*d^5*abs(b) - 90*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{6*b^3*c^2*d^2*abs(b) + 180*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{6*a*b^2*c*d^3*abs(b) - 90*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{6*a^2*b*d^4*abs(b) + 45*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{8*b*c*d^2*abs(b) - 45*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{8*a*d^3*abs(b)}/((b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^{2})^{5*b^4)}$

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{2}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^(7/2),x)

[Out] int((d*x+c)^(5/2)/(b*x+a)^(7/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(7/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{5/2}}{(a + bx)^{7/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/2)/(a + b*x)^(7/2),x)
```

```
[Out] int((c + d*x)^(5/2)/(a + b*x)^(7/2), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/2)/(b*x+a)**(7/2),x)
```

```
[Out] Timed out
```

$$3.1488 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^{9/2}} dx$$

Optimal. Leaf size=32

$$-\frac{2(c+dx)^{7/2}}{7(a+bx)^{7/2}(bc-ad)}$$

[Out] $-2/7*(d*x+c)^{(7/2)/(-a*d+b*c)/(b*x+a)^{(7/2)}$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{2(c+dx)^{7/2}}{7(a+bx)^{7/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^(9/2), x]

[Out] $(-2*(c + d*x)^{(7/2)})/(7*(b*c - a*d)*(a + b*x)^{(7/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp [((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(c+dx)^{5/2}}{(a+bx)^{9/2}} dx = -\frac{2(c+dx)^{7/2}}{7(bc-ad)(a+bx)^{7/2}}$$

Mathematica [A] time = 0.02, size = 32, normalized size = 1.00

$$-\frac{2(c+dx)^{7/2}}{7(a+bx)^{7/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^(9/2), x]

[Out] $(-2*(c + d*x)^{(7/2)})/(7*(b*c - a*d)*(a + b*x)^{(7/2)})$

fricas [B] time = 1.44, size = 138, normalized size = 4.31

$$\frac{2(d^3x^3 + 3cd^2x^2 + 3c^2dx + c^3)\sqrt{bx+a}\sqrt{dx+c}}{7(a^4bc - a^5d + (b^5c - ab^4d)x^4 + 4(ab^4c - a^2b^3d)x^3 + 6(a^2b^3c - a^3b^2d)x^2 + 4(a^3b^2c - a^4bd)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(9/2),x, algorithm="fricas")

[Out] -2/7*(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3)*sqrt(b*x + a)*sqrt(d*x + c)/
(a^4*b*c - a^5*d + (b^5*c - a*b^4*d)*x^4 + 4*(a*b^4*c - a^2*b^3*d)*x^3 + 6*
(a^2*b^3*c - a^3*b^2*d)*x^2 + 4*(a^3*b^2*c - a^4*b*d)*x)

giac [B] time = 2.54, size = 706, normalized size = 22.06

$$4\left(\sqrt{bd}b^{12}c^6d^3|b| - 6\sqrt{bd}ab^{11}c^5d^4|b| + 15\sqrt{bd}a^2b^{10}c^4d^5|b| - 20\sqrt{bd}a^3b^9c^3d^6|b| + 15\sqrt{bd}a^4b^8c^2d^7|b| - 6\sqrt{bd}a\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(9/2),x, algorithm="giac")

[Out] -4/7*(sqrt(b*d)*b^12*c^6*d^3*abs(b) - 6*sqrt(b*d)*a*b^11*c^5*d^4*abs(b) + 1
5*sqrt(b*d)*a^2*b^10*c^4*d^5*abs(b) - 20*sqrt(b*d)*a^3*b^9*c^3*d^6*abs(b) +
15*sqrt(b*d)*a^4*b^8*c^2*d^7*abs(b) - 6*sqrt(b*d)*a^5*b^7*c*d^8*abs(b) + s
qrt(b*d)*a^6*b^6*d^9*abs(b) + 21*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(
b^2*c + (b*x + a)*b*d - a*b*d))^4*b^8*c^4*d^3*abs(b) - 84*sqrt(b*d)*(sqrt(b
*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a*b^7*c^3*d^4*ab
s(b) + 126*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d
- a*b*d))^4*a^2*b^6*c^2*d^5*abs(b) - 84*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a)
- sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^3*b^5*c*d^6*abs(b) + 21*sqrt(b*d
)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^4*b^4
*d^7*abs(b) + 35*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a
)
*b*d - a*b*d))^8*b^4*c^2*d^3*abs(b) - 70*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a
)
- sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^8*a*b^3*c*d^4*abs(b) + 35*sqrt(b*d
)
(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^8*a^2*b^2
*d^5*abs(b) + 7*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a
)
*b*d - a*b*d))^12*d^3*abs(b))/(b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) -
sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)^7*b^4)

maple [A] time = 0.00, size = 27, normalized size = 0.84

$$\frac{2(dx+c)^{\frac{7}{2}}}{7(bx+a)^{\frac{7}{2}}(ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(5/2)/(b*x+a)^(9/2),x)`

[Out] $2/7/(b*x+a)^{(7/2)}*(d*x+c)^{(7/2)/(a*d-b*c)}$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(5/2)/(b*x+a)^(9/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 0.97, size = 27, normalized size = 0.84

$$\frac{2(c+dx)^{7/2}}{(7ad-7bc)(a+bx)^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c+d*x)^(5/2)/(a+b*x)^(9/2),x)`

[Out] $(2*(c+d*x)^{(7/2)})/((7*a*d-7*b*c)*(a+b*x)^{(7/2)})$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(5/2)/(b*x+a)**(9/2),x)`

[Out] Timed out

$$3.1489 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^{11/2}} dx$$

Optimal. Leaf size=66

$$\frac{4d(c+dx)^{7/2}}{63(a+bx)^{7/2}(bc-ad)^2} - \frac{2(c+dx)^{7/2}}{9(a+bx)^{9/2}(bc-ad)}$$

[Out] $-2/9*(d*x+c)^{(7/2)/(-a*d+b*c)/(b*x+a)^{(9/2)+4/63*d*(d*x+c)^{(7/2)/(-a*d+b*c)^{2/(b*x+a)^{(7/2)}}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{4d(c+dx)^{7/2}}{63(a+bx)^{7/2}(bc-ad)^2} - \frac{2(c+dx)^{7/2}}{9(a+bx)^{9/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^(11/2), x]

[Out] $(-2*(c + d*x)^{(7/2))/(9*(b*c - a*d)*(a + b*x)^{(9/2)}) + (4*d*(c + d*x)^{(7/2)})/(63*(b*c - a*d)^2*(a + b*x)^{(7/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{(c+dx)^{5/2}}{(a+bx)^{11/2}} dx = -\frac{2(c+dx)^{7/2}}{9(bc-ad)(a+bx)^{9/2}} - \frac{(2d) \int \frac{(c+dx)^{5/2}}{(a+bx)^{9/2}} dx}{9(bc-ad)}$$

$$= -\frac{2(c+dx)^{7/2}}{9(bc-ad)(a+bx)^{9/2}} + \frac{4d(c+dx)^{7/2}}{63(bc-ad)^2(a+bx)^{7/2}}$$

Mathematica [A] time = 0.03, size = 46, normalized size = 0.70

$$\frac{2(c+dx)^{7/2}(9ad-7bc+2bdx)}{63(a+bx)^{9/2}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^(11/2), x]

[Out] (2*(c + d*x)^(7/2)*(-7*b*c + 9*a*d + 2*b*d*x))/(63*(b*c - a*d)^2*(a + b*x)^(9/2))

fricas [B] time = 4.71, size = 295, normalized size = 4.47

$$\frac{2(2bd^4x^4 - 7bc^4 + 9ac^3d - (bcd^3 - 9ad^4)x^3 - 3(5bc^2d^2 - 9acd^3))}{63(a^5b^2c^2 - 2a^6bcd + a^7d^2 + (b^7c^2 - 2ab^6cd + a^2b^5d^2)x^5 + 5(ab^6c^2 - 2a^2b^5cd + a^3b^4d^2)x^4 + 10(a^2b^5c^2 - 2a^3b^4cd + a^4b^3d^2)x^3 + 10(a^3b^4c^2 - 2a^4b^3cd + a^5b^2d^2)x^2 + 5(a^4b^3c^2 - 2a^5b^2cd + a^6b^1d^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(11/2), x, algorithm="fricas")

[Out] 2/63*(2*b*d^4*x^4 - 7*b*c^4 + 9*a*c^3*d - (b*c*d^3 - 9*a*d^4)*x^3 - 3*(5*b*c^2*d^2 - 9*a*c*d^3)*x^2 - (19*b*c^3*d - 27*a*c^2*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^5*b^2*c^2 - 2*a^6*b*c*d + a^7*d^2 + (b^7*c^2 - 2*a*b^6*c*d + a^2*b^5*d^2)*x^5 + 5*(a*b^6*c^2 - 2*a^2*b^5*c*d + a^3*b^4*d^2)*x^4 + 10*(a^2*b^5*c^2 - 2*a^3*b^4*c*d + a^4*b^3*d^2)*x^3 + 10*(a^3*b^4*c^2 - 2*a^4*b^3*c*d + a^5*b^2*d^2)*x^2 + 5*(a^4*b^3*c^2 - 2*a^5*b^2*c*d + a^6*b*d^2)*x)

giac [B] time = 3.80, size = 1826, normalized size = 27.67

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(11/2), x, algorithm="giac")

[Out] 8/63*(sqrt(b*d)*b^14*c^7*d^4*abs(b) - 7*sqrt(b*d)*a*b^13*c^6*d^5*abs(b) + 2*1*sqrt(b*d)*a^2*b^12*c^5*d^6*abs(b) - 35*sqrt(b*d)*a^3*b^11*c^4*d^7*abs(b) - 35*sqrt(b*d)*a^4*b^10*c^3*d^8*abs(b) + 35*sqrt(b*d)*a^5*b^9*c^2*d^9*abs(b) - 35*sqrt(b*d)*a^6*b^8*c*d^10*abs(b) + 35*sqrt(b*d)*a^7*b^7*c^2*d^11*abs(b) - 35*sqrt(b*d)*a^8*b^6*c*d^12*abs(b) + 35*sqrt(b*d)*a^9*b^5*c^2*d^13*abs(b) - 35*sqrt(b*d)*a^10*b^4*c*d^14*abs(b) + 35*sqrt(b*d)*a^11*b^3*c^2*d^15*abs(b) - 35*sqrt(b*d)*a^12*b^2*c*d^16*abs(b) + 35*sqrt(b*d)*a^13*b*c^2*d^17*abs(b) - 35*sqrt(b*d)*a^14*b^2*d^18*abs(b) + 35*sqrt(b*d)*a^15*d^19*abs(b))

$$\begin{aligned}
& + 35*\sqrt{b*d}*a^4*b^{10}*c^3*d^8*\text{abs}(b) - 21*\sqrt{b*d}*a^5*b^9*c^2*d^9*\text{abs}(b) \\
& + 7*\sqrt{b*d}*a^6*b^8*c*d^{10}*\text{abs}(b) - \sqrt{b*d}*a^7*b^7*d^{11}*\text{abs}(b) - 9*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*b^{12}*c^6*d^4*\text{abs}(b) + 54*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a*b^{11}*c^5*d^5*\text{abs}(b) - 135*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^2*b^{10}*c^4*d^6*\text{abs}(b) + 180*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^3*b^9*c^3*d^7*\text{abs}(b) - 135*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^4*b^8*c^2*d^8*\text{abs}(b) + 54*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^5*b^7*c*d^9*\text{abs}(b) - 9*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^2*a^6*b^6*d^{10}*\text{abs}(b) - 27*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*b^{10}*c^5*d^4*\text{abs}(b) + 135*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a*b^9*c^4*d^5*\text{abs}(b) - 270*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a^2*b^8*c^3*d^6*\text{abs}(b) + 270*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a^3*b^7*c^2*d^7*\text{abs}(b) - 135*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a^4*b^6*c*d^8*\text{abs}(b) + 27*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^4*a^5*b^5*d^9*\text{abs}(b) - 189*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*b^8*c^4*d^4*\text{abs}(b) + 756*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*a*b^7*c^3*d^5*\text{abs}(b) - 1134*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*a^2*b^6*c^2*d^6*\text{abs}(b) + 756*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*a^3*b^5*c*d^7*\text{abs}(b) - 189*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^6*a^4*b^4*d^8*\text{abs}(b) - 189*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^8*b^6*c^3*d^4*\text{abs}(b) + 567*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^8*a*b^5*c^2*d^5*\text{abs}(b) - 567*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^8*a^2*b^4*c*d^6*\text{abs}(b) + 189*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^8*a^3*b^3*d^7*\text{abs}(b) - 315*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^10*b^4*c^2*d^4*\text{abs}(b) + 630*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^10*a*b^3*c*d^5*\text{abs}(b) - 315*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^10*a^2*b^2*d^6*\text{abs}(b) - 105*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^12*b^2*c*d^4*\text{abs}(b) + 105*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^12*a*b*d^5*\text{abs}(b) - 63*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d})^14*d^4*\text{abs}(b) \\
&)/((b^2*c - a*b*d - (\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c+(b*x+a)*b*d - a*b*d}))^2)^9*b^3)
\end{aligned}$$

maple [A] time = 0.00, size = 54, normalized size = 0.82

$$\frac{2(dx+c)^{\frac{7}{2}}(2bdx+9ad-7bc)}{63(bx+a)^{\frac{9}{2}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^(11/2),x)

[Out] 2/63*(d*x+c)^(7/2)*(2*b*d*x+9*a*d-7*b*c)/(b*x+a)^(9/2)/(a^2*d^2-2*a*b*c*d+b^2*c^2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(11/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.14, size = 229, normalized size = 3.47

$$\frac{\sqrt{c+dx} \left(\frac{4d^4x^4}{63b^3(ad-bc)^2} - \frac{14bc^4-18ac^3d}{63b^4(ad-bc)^2} + \frac{x^3(18ad^4-2bcd^3)}{63b^4(ad-bc)^2} + \frac{2c^2dx(27ad-19bc)}{63b^4(ad-bc)^2} + \frac{2cd^2x^2(9ad-5bc)}{21b^4(ad-bc)^2} \right)}{x^4\sqrt{a+bx} + \frac{a^4\sqrt{a+bx}}{b^4} + \frac{6a^2x^2\sqrt{a+bx}}{b^2} + \frac{4ax^3\sqrt{a+bx}}{b} + \frac{4a^3x\sqrt{a+bx}}{b^3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c+d*x)^(5/2)/(a+b*x)^(11/2),x)

[Out] ((c+d*x)^(1/2)*((4*d^4*x^4)/(63*b^3*(a*d-b*c)^2) - (14*b*c^4 - 18*a*c^3*d)/(63*b^4*(a*d-b*c)^2) + (x^3*(18*a*d^4 - 2*b*c*d^3))/(63*b^4*(a*d-b*c)^2) + (2*c^2*d*x*(27*a*d - 19*b*c))/(63*b^4*(a*d-b*c)^2) + (2*c*d^2*x^2*(9*a*d - 5*b*c))/(21*b^4*(a*d-b*c)^2))/((x^4*(a+b*x)^(1/2) + (a^4*(a+b*x)^(1/2))/b^4 + (6*a^2*x^2*(a+b*x)^(1/2))/b^2 + (4*a*x^3*(a+b*x)^(1/2))/b + (4*a^3*x*(a+b*x)^(1/2))/b^3)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/2)/(b*x+a)**(11/2),x)
```

```
[Out] Timed out
```

$$3.1490 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^{13/2}} dx$$

Optimal. Leaf size=101

$$-\frac{16d^2(c+dx)^{7/2}}{693(a+bx)^{7/2}(bc-ad)^3} + \frac{8d(c+dx)^{7/2}}{99(a+bx)^{9/2}(bc-ad)^2} - \frac{2(c+dx)^{7/2}}{11(a+bx)^{11/2}(bc-ad)}$$

[Out] $-2/11*(d*x+c)^{(7/2)/(-a*d+b*c)/(b*x+a)^{(11/2)+8/99*d*(d*x+c)^{(7/2)/(-a*d+b*c)^2/(b*x+a)^{(9/2)-16/693*d^2*(d*x+c)^{(7/2)/(-a*d+b*c)^3/(b*x+a)^{(7/2)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{16d^2(c+dx)^{7/2}}{693(a+bx)^{7/2}(bc-ad)^3} + \frac{8d(c+dx)^{7/2}}{99(a+bx)^{9/2}(bc-ad)^2} - \frac{2(c+dx)^{7/2}}{11(a+bx)^{11/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^(13/2), x]

[Out] $(-2*(c+d*x)^{(7/2))/(11*(b*c-a*d)*(a+b*x)^{(11/2)} + (8*d*(c+d*x)^{(7/2)})/(99*(b*c-a*d)^2*(a+b*x)^{(9/2)}) - (16*d^2*(c+d*x)^{(7/2)})/(693*(b*c-a*d)^3*(a+b*x)^{(7/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/2}}{(a+bx)^{13/2}} dx &= -\frac{2(c+dx)^{7/2}}{11(bc-ad)(a+bx)^{11/2}} - \frac{(4d) \int \frac{(c+dx)^{5/2}}{(a+bx)^{11/2}} dx}{11(bc-ad)} \\
&= -\frac{2(c+dx)^{7/2}}{11(bc-ad)(a+bx)^{11/2}} + \frac{8d(c+dx)^{7/2}}{99(bc-ad)^2(a+bx)^{9/2}} + \frac{(8d^2) \int \frac{(c+dx)^{5/2}}{(a+bx)^{9/2}} dx}{99(bc-ad)^2} \\
&= -\frac{2(c+dx)^{7/2}}{11(bc-ad)(a+bx)^{11/2}} + \frac{8d(c+dx)^{7/2}}{99(bc-ad)^2(a+bx)^{9/2}} - \frac{16d^2(c+dx)^{7/2}}{693(bc-ad)^3(a+bx)^{7/2}}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 77, normalized size = 0.76

$$-\frac{2(c+dx)^{7/2} (99a^2d^2 + 22abd(2dx-7c) + b^2(63c^2 - 28cdx + 8d^2x^2))}{693(a+bx)^{11/2}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^(13/2), x]

[Out] (-2*(c + d*x)^(7/2)*(99*a^2*d^2 + 22*a*b*d*(-7*c + 2*d*x) + b^2*(63*c^2 - 28*c*d*x + 8*d^2*x^2)))/(693*(b*c - a*d)^3*(a + b*x)^(11/2))

fricas [B] time = 10.68, size = 513, normalized size = 5.08

$$-\frac{2(8b^2d^5x^5 + 63b^2c^5 - 154abc^4d + 99a^2c^3d^2 - 4(b^2cd^4 - 11ab^2d^5)x^4 + (3b^2c^2d^3 - 22ab^2cd^4 + 99a^2d^5)x^3 + (113b^2c^3d^2 - 330ab^2c^2d^3 + 297a^2c^4d)x^2 + (161b^2c^4d - 418ab^2c^3d^2 + 297a^2c^2d^3)x)\sqrt{b*x+a}\sqrt{d*x+c}}{693(a^6b^3c^3 - 3a^7b^2c^2d + 3a^8bcd^2 - a^9d^3 + (b^9c^3 - 3ab^8c^2d + 3a^2b^7cd^2 - a^3b^6d^3)x^6 + 6(ab^8c^3 - 3a^2b^7c^2d + 3a^3b^6c^2d^2 - a^4b^5c^2d^3)x^5 + 15(a^2b^7c^3 - 3a^3b^6c^2d + 3a^4b^5c^2d^2 - a^5b^4d^3)x^4 + 20(a^3b^6c^3 - 3a^4b^5c^2d + 3a^5b^4c^2d^2 - a^6b^3d^3)x^3 + 15(a^4b^5c^3 - 3a^5b^4c^2d + 3a^6b^3c^2d^2 - a^7b^2d^3)x^2 + 6(a^5b^4c^3 - 3a^6b^3c^2d + 3a^7b^2c^2d^2 - a^8b^2d^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(13/2), x, algorithm="fricas")

[Out] -2/693*(8*b^2*d^5*x^5 + 63*b^2*c^5 - 154*a*b*c^4*d + 99*a^2*c^3*d^2 - 4*(b^2*c*d^4 - 11*a*b*d^5)*x^4 + (3*b^2*c^2*d^3 - 22*a*b*c*d^4 + 99*a^2*d^5)*x^3 + (113*b^2*c^3*d^2 - 330*a*b*c^2*d^3 + 297*a^2*c^4*d)*x^2 + (161*b^2*c^4*d - 418*a*b*c^3*d^2 + 297*a^2*c^2*d^3)*x)*sqrt(b*x+a)*sqrt(d*x+c)/(a^6*b^3*c^3 - 3*a^7*b^2*c^2*d + 3*a^8*b*c*d^2 - a^9*d^3 + (b^9*c^3 - 3*a*b^8*c^2*d + 3*a^2*b^7*c*d^2 - a^3*b^6*d^3)*x^6 + 6*(a*b^8*c^3 - 3*a^2*b^7*c^2*d + 3*a^3*b^6*c^2*d^2 - a^4*b^5*c^2*d^3)*x^5 + 15*(a^2*b^7*c^3 - 3*a^3*b^6*c^2*d + 3*a^4*b^5*c^2*d^2 - a^5*b^4*d^3)*x^4 + 20*(a^3*b^6*c^3 - 3*a^4*b^5*c^2*d + 3*a^5*b^4*c^2*d^2 - a^6*b^3*d^3)*x^3 + 15*(a^4*b^5*c^3 - 3*a^5*b^4*c^2*d + 3*a^6*b^3*c^2*d^2 - a^7*b^2*d^3)*x^2 + 6*(a^5*b^4*c^3 - 3*a^6*b^3*c^2*d + 3*a^7*b^2*c^2*d^2 - a^8*b^2*d^3)*x)


```

rt(b^2*c + (b*x + a)*b*d - a*b*d)^8*a^2*b^6*c^2*d^7*abs(b) - 5940*sqrt(b*d
)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^8*a^3*b^5
*c*d^8*abs(b) + 1485*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x
+ a)*b*d - a*b*d))^8*a^4*b^4*d^9*abs(b) + 2079*sqrt(b*d)*(sqrt(b*d)*sqrt(b
*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^10*b^6*c^3*d^5*abs(b) - 6237
*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^
10*a*b^5*c^2*d^6*abs(b) + 6237*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^
2*c + (b*x + a)*b*d - a*b*d))^10*a^2*b^4*c*d^7*abs(b) - 2079*sqrt(b*d)*(sq
rt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^10*a^3*b^3*d^8*
abs(b) + 2541*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b
*d - a*b*d))^12*b^4*c^2*d^5*abs(b) - 5082*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a
) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^12*a*b^3*c*d^6*abs(b) + 2541*sqrt(
b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^12*a^2
*b^2*d^7*abs(b) + 1155*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b
*x + a)*b*d - a*b*d))^14*b^2*c*d^5*abs(b) - 1155*sqrt(b*d)*(sqrt(b*d)*sqrt(
b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^14*a*b*d^6*abs(b) + 462*sq
rt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^16*d
^5*abs(b))/((b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x +
a)*b*d - a*b*d))^2)^11*b^2)

```

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{2(dx+c)^{\frac{7}{2}}(8b^2x^2d^2+44abd^2x-28b^2cdx+99a^2d^2-154abcd+63b^2c^2)}{693(bx+a)^{\frac{11}{2}}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^(5/2)/(b*x+a)^(13/2),x)
```

```
[Out] 2/693*(d*x+c)^(7/2)*(8*b^2*d^2*x^2+44*a*b*d^2*x-28*b^2*c*d*x+99*a^2*d^2-154
*a*b*c*d+63*b^2*c^2)/(b*x+a)^(11/2)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^
3*c^3)
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(5/2)/(b*x+a)^(13/2),x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError >> Computation failed since Maxima requested a
dditional constraints; using the 'assume' command before evaluation *may* h
elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more
details)Is a*d-b*c zero or nonzero?
```

mupad [B] time = 1.35, size = 333, normalized size = 3.30

$$\frac{\sqrt{c+dx} \left(\frac{198a^2c^3d^2 - 308abc^4d + 126b^2c^5}{693b^5(ad-bc)^3} + \frac{x^3(198a^2d^5 - 44abc^4d^4 + 6b^2c^2d^3)}{693b^5(ad-bc)^3} + \frac{16d^5x^5}{693b^3(ad-bc)^3} + \frac{8d^4x^4(11ad-bc)}{693b^4(ad-bc)^3} + \frac{2cd^2x^2(29}{693b^5(ad-bc)^3} \right)}{x^5\sqrt{a+bx} + \frac{a^5\sqrt{a+bx}}{b^5} + \frac{10a^2x^3\sqrt{a+bx}}{b^2} + \frac{10a^3x^2\sqrt{a+bx}}{b^3} + \frac{5ax^4\sqrt{a+bx}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/2)/(a + b*x)^(13/2), x)

[Out] ((c + d*x)^(1/2)*((126*b^2*c^5 + 198*a^2*c^3*d^2 - 308*a*b*c^4*d)/(693*b^5*(a*d - b*c)^3) + (x^3*(198*a^2*d^5 + 6*b^2*c^2*d^3 - 44*a*b*c*d^4))/(693*b^5*(a*d - b*c)^3) + (16*d^5*x^5)/(693*b^3*(a*d - b*c)^3) + (8*d^4*x^4*(11*a*d - b*c))/(693*b^4*(a*d - b*c)^3) + (2*c*d^2*x^2*(297*a^2*d^2 + 113*b^2*c^2 - 330*a*b*c*d))/(693*b^5*(a*d - b*c)^3) + (2*c^2*d*x*(297*a^2*d^2 + 161*b^2*c^2 - 418*a*b*c*d))/(693*b^5*(a*d - b*c)^3)))/(x^5*(a + b*x)^(1/2) + (a^5*(a + b*x)^(1/2))/b^5 + (10*a^2*x^3*(a + b*x)^(1/2))/b^2 + (10*a^3*x^2*(a + b*x)^(1/2))/b^3 + (5*a*x^4*(a + b*x)^(1/2))/b + (5*a^4*x*(a + b*x)^(1/2))/b^4)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/2)/(b*x+a)**(13/2), x)

[Out] Timed out

$$3.1491 \quad \int \frac{(c+dx)^{5/2}}{(a+bx)^{15/2}} dx$$

Optimal. Leaf size=136

$$\frac{32d^3(c+dx)^{7/2}}{3003(a+bx)^{7/2}(bc-ad)^4} - \frac{16d^2(c+dx)^{7/2}}{429(a+bx)^{9/2}(bc-ad)^3} + \frac{12d(c+dx)^{7/2}}{143(a+bx)^{11/2}(bc-ad)^2} - \frac{2(c+dx)^{7/2}}{13(a+bx)^{13/2}(bc-ad)}$$

[Out] $-2/13*(d*x+c)^{(7/2)/(-a*d+b*c)/(b*x+a)^{(13/2)+12/143*d*(d*x+c)^{(7/2)/(-a*d+b*c)^2/(b*x+a)^{(11/2)-16/429*d^2*(d*x+c)^{(7/2)/(-a*d+b*c)^3/(b*x+a)^{(9/2)+2/3003*d^3*(d*x+c)^{(7/2)/(-a*d+b*c)^4/(b*x+a)^{(7/2)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{32d^3(c+dx)^{7/2}}{3003(a+bx)^{7/2}(bc-ad)^4} - \frac{16d^2(c+dx)^{7/2}}{429(a+bx)^{9/2}(bc-ad)^3} + \frac{12d(c+dx)^{7/2}}{143(a+bx)^{11/2}(bc-ad)^2} - \frac{2(c+dx)^{7/2}}{13(a+bx)^{13/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/2)/(a + b*x)^(15/2), x]

[Out] $(-2*(c+d*x)^{(7/2))/(13*(b*c-a*d)*(a+b*x)^{(13/2)}) + (12*d*(c+d*x)^{(7/2))/(143*(b*c-a*d)^2*(a+b*x)^{(11/2)}) - (16*d^2*(c+d*x)^{(7/2))/(429*(b*c-a*d)^3*(a+b*x)^{(9/2)}) + (32*d^3*(c+d*x)^{(7/2))/(3003*(b*c-a*d)^4*(a+b*x)^{(7/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/2}}{(a+bx)^{15/2}} dx &= -\frac{2(c+dx)^{7/2}}{13(bc-ad)(a+bx)^{13/2}} - \frac{(6d) \int \frac{(c+dx)^{5/2}}{(a+bx)^{13/2}} dx}{13(bc-ad)} \\
&= -\frac{2(c+dx)^{7/2}}{13(bc-ad)(a+bx)^{13/2}} + \frac{12d(c+dx)^{7/2}}{143(bc-ad)^2(a+bx)^{11/2}} + \frac{(24d^2) \int \frac{(c+dx)^{5/2}}{(a+bx)^{11/2}} dx}{143(bc-ad)^2} \\
&= -\frac{2(c+dx)^{7/2}}{13(bc-ad)(a+bx)^{13/2}} + \frac{12d(c+dx)^{7/2}}{143(bc-ad)^2(a+bx)^{11/2}} - \frac{16d^2(c+dx)^{7/2}}{429(bc-ad)^3(a+bx)^{9/2}} - \frac{(16d^3)}{429} \int \frac{(c+dx)^{5/2}}{(a+bx)^{9/2}} dx \\
&= -\frac{2(c+dx)^{7/2}}{13(bc-ad)(a+bx)^{13/2}} + \frac{12d(c+dx)^{7/2}}{143(bc-ad)^2(a+bx)^{11/2}} - \frac{16d^2(c+dx)^{7/2}}{429(bc-ad)^3(a+bx)^{9/2}} + \frac{32d^3}{3003(bc-ad)^4} \int \frac{(c+dx)^{5/2}}{(a+bx)^{7/2}} dx
\end{aligned}$$

Mathematica [A] time = 0.07, size = 118, normalized size = 0.87

$$\frac{2(c+dx)^{7/2} (429a^3d^3 + 143a^2bd^2(2dx-7c) + 13abd^2(63c^2 - 28cdx + 8d^2x^2) + b^3(-231c^3 + 126c^2dx - 56cd^2x^2 + 16d^3x^3))}{3003(a+bx)^{13/2}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/2)/(a + b*x)^(15/2), x]

[Out] (2*(c + d*x)^(7/2)*(429*a^3*d^3 + 143*a^2*b*d^2*(-7*c + 2*d*x) + 13*a*b^2*d*(63*c^2 - 28*c*d*x + 8*d^2*x^2) + b^3*(-231*c^3 + 126*c^2*d*x - 56*c*d^2*x^2 + 16*d^3*x^3)))/(3003*(b*c - a*d)^4*(a + b*x)^(13/2))

fricas [B] time = 23.04, size = 765, normalized size = 5.62

$$\frac{2(16b^3d^6x^6 - 231b^3c^6 + 819a*b^2*c^5*d - 1001a^2*b*c^4*d^2 + 429a^3*c^3*d^3 - 8*(b^3*c*d^5 - 13a*b^2*d^6)*x^5 + 2*(3b^3*c^2*d^4 - 26a*b^2*c*d^5 + 143a^2*b*d^6)*x^4 - (5b^3*c^3*d^3 - 39a*b^2*c^2*d^4 + 143a^2*b*c*d^5 - 429a^3*d^6)*x^3 - (371b^3*c^4*d^2 - 1469a*b^2*c^3*d^3 + 2145a^2*b*c^2*d^4 - 1287a^3*c*d^5)*x^2 - (567b^3*c^5*d - 2093a*b^2*c^4*d^2 + 2717a^2*b*c^3*d^3 - 1287a^3*c^2*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c)}{3003(a^7*b^4*c^4 - 4a^8*b^3*c^3*d + 6a^9*b^2*c^2*d^2 - 4a^{10}bcd^3 + a^{11}d^4 + (b^{11}c^4 - 4ab^{10}c^3d + 6a^2b^9c^2d^2 - 4a^3b^8cd^3 + a^4b^7d^4))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(15/2), x, algorithm="fricas")

[Out] 2/3003*(16*b^3*d^6*x^6 - 231*b^3*c^6 + 819*a*b^2*c^5*d - 1001*a^2*b*c^4*d^2 + 429*a^3*c^3*d^3 - 8*(b^3*c*d^5 - 13*a*b^2*d^6)*x^5 + 2*(3*b^3*c^2*d^4 - 26*a*b^2*c*d^5 + 143*a^2*b*d^6)*x^4 - (5*b^3*c^3*d^3 - 39*a*b^2*c^2*d^4 + 143*a^2*b*c*d^5 - 429*a^3*d^6)*x^3 - (371*b^3*c^4*d^2 - 1469*a*b^2*c^3*d^3 + 2145*a^2*b*c^2*d^4 - 1287*a^3*c*d^5)*x^2 - (567*b^3*c^5*d - 2093*a*b^2*c^4*d^2 + 2717*a^2*b*c^3*d^3 - 1287*a^3*c^2*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^7*b^4*c^4 - 4*a^8*b^3*c^3*d + 6*a^9*b^2*c^2*d^2 - 4*a^10*b*c*d^3 + a^11*d^4 + (b^11*c^4 - 4*a*b^10*c^3*d + 6*a^2*b^9*c^2*d^2 - 4*a^3*b^8*c*d^3 + a^4*b^7*d^4))

$$\begin{aligned}
& t(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*b^12*c^6*d^6*abs(b) + 1716*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*a*b^11*c^5*d^7*abs(b) - 4290*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^2*b^10*c^4*d^8*abs(b) + 5720*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^3*b^9*c^3*d^9*abs(b) - 4290*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^4*b^8*c^2*d^10*abs(b) + 1716*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^5*b^7*c*d^11*abs(b) - 286*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^6*b^6*d^12*abs(b) - 2288*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^8*b^10*c^5*d^6*abs(b) + 11440*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^8*a*b^9*c^4*d^7*abs(b) - 22880*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^8*a^2*b^8*c^3*d^8*abs(b) + 22880*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^8*a^3*b^7*c^2*d^9*abs(b) - 11440*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^8*a^4*b^6*c*d^10*abs(b) + 2288*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^8*a^5*b^5*d^11*abs(b) - 10296*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^10*b^8*c^4*d^6*abs(b) + 41184*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^10*a*b^7*c^3*d^7*abs(b) - 61776*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^10*a^2*b^6*c^2*d^8*abs(b) + 41184*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^10*a^3*b^5*c*d^9*abs(b) - 10296*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^10*a^4*b^4*d^10*abs(b) - 16302*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^12*b^6*c^3*d^6*abs(b) + 48906*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^12*a*b^5*c^2*d^7*abs(b) - 48906*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^12*a^2*b^4*c*d^8*abs(b) + 16302*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^12*a^3*b^3*d^9*abs(b) - 18018*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^14*b^4*c^2*d^6*abs(b) + 36036*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^14*a*b^3*c*d^7*abs(b) - 18018*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^14*a^2*b^2*d^8*abs(b) - 9009*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^16*b^2*c*d^6*abs(b) + 9009*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^16*a*b*d^7*abs(b) - 3003*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^18*d^6*abs(b))/((b^2*c - a*b*d - (sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2)^13*b)
\end{aligned}$$

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{2(dx+c)^{\frac{7}{2}}(16b^3x^3d^3+104ab^2d^3x^2-56b^3cd^2x^2+286a^2bd^3x-364ab^2cd^2x+126b^3c^2dx+429a^3d^3-1001a^2b^2d^3)}{3003(bx+a)^{\frac{13}{2}}(a^4d^4-4a^3bcd^3+6a^2b^2c^2d^2-4ab^3c^3d+b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/2)/(b*x+a)^(15/2),x)

[Out] 2/3003*(d*x+c)^(7/2)*(16*b^3*d^3*x^3+104*a*b^2*d^3*x^2-56*b^3*c*d^2*x^2+286*a^2*b*d^3*x-364*a*b^2*c*d^2*x+126*b^3*c^2*d*x+429*a^3*d^3-1001*a^2*b*c*d^2+819*a*b^2*c^2*d-231*b^3*c^3)/(b*x+a)^(13/2)/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/2)/(b*x+a)^(15/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.62, size = 459, normalized size = 3.38

$$\frac{\sqrt{c+dx} \left(\frac{x^2(2574a^3cd^5-4290a^2b^2c^2d^4+2938ab^2c^3d^3-742b^3c^4d^2)}{3003b^6(ad-bc)^4} - \frac{-858a^3c^3d^3+2002a^2b^2c^4d^2-1638ab^2c^5d+462b^3c^6}{3003b^6(ad-bc)^4} + \frac{x^3(858a^3d^6-10b^3c^3d^3+78a^2b^2c^2d^4-286a^2b^2c^2d^5)}{3003b^6(ad-bc)^4} \right)}{x^6\sqrt{a+bx} + \frac{a^6\sqrt{a+bx}}{b^6} + \frac{15a^2x^4}{b^6}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c+d*x)^(5/2)/(a+b*x)^(15/2),x)

[Out] ((c+d*x)^(1/2)*((x^2*(2574*a^3*c*d^5-742*b^3*c^4*d^2+2938*a*b^2*c^3*d^3-4290*a^2*b*c^2*d^4))/(3003*b^6*(a*d-b*c)^4)-(462*b^3*c^6-858*a^3*c^3*d^3+2002*a^2*b*c^4*d^2-1638*a*b^2*c^5*d)/(3003*b^6*(a*d-b*c)^4)+(x^3*(858*a^3*d^6-10*b^3*c^3*d^3+78*a^2*b^2*c^2*d^4-286*a^2*b^2*c^2*d^5))/(3003*b^6*(a*d-b*c)^4)+(32*d^6*x^6)/(3003*b^3*(a*d-b*c)^4)-(x*(1134*b^3*c^5*d-2574*a^3*c^2*d^4-4186*a*b^2*c^4*d^2+5434*a^2*b*c^3*d^3))/(3003*b^6*(a*d-b*c)^4)+(16*d^5*x^5*(13*a*d-b*c))/(3003*b^4*(a*d-b*c)^4))

$$\begin{aligned} &)^4) + (4*d^4*x^4*(143*a^2*d^2 + 3*b^2*c^2 - 26*a*b*c*d))/(3003*b^5*(a*d - \\ &b*c)^4)))/(x^6*(a + b*x)^{1/2} + (a^6*(a + b*x)^{1/2})/b^6 + (15*a^2*x^4*(a \\ &+ b*x)^{1/2})/b^2 + (20*a^3*x^3*(a + b*x)^{1/2})/b^3 + (15*a^4*x^2*(a + b* \\ &x)^{1/2})/b^4 + (6*a*x^5*(a + b*x)^{1/2})/b + (6*a^5*x*(a + b*x)^{1/2})/b^5 \\ &) \end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/2)/(b*x+a)**(15/2),x)

[Out] Timed out

$$3.1492 \quad \int \frac{(a+bx)^{7/2}}{\sqrt{c+dx}} dx$$

Optimal. Leaf size=183

$$\frac{35(bc-ad)^4 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{64\sqrt{b}d^{9/2}} - \frac{35\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^3}{64d^4} + \frac{35(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^2}{96d^3} - \frac{7(a+bx)^{5/2}\sqrt{c+dx}}{24d^2} + \frac{35(bc-ad)^4 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{64\sqrt{b}d^{9/2}}$$

[Out] 35/64*(-a*d+b*c)^4*arctanh(d^(1/2)*(b*x+a)^(1/2)/b^(1/2)/(d*x+c)^(1/2))/d^(9/2)/b^(1/2)+35/96*(-a*d+b*c)^2*(b*x+a)^(3/2)*(d*x+c)^(1/2)/d^3-7/24*(-a*d+b*c)*(b*x+a)^(5/2)*(d*x+c)^(1/2)/d^2+1/4*(b*x+a)^(7/2)*(d*x+c)^(1/2)/d-35/64*(-a*d+b*c)^3*(b*x+a)^(1/2)*(d*x+c)^(1/2)/d^4

Rubi [A] time = 0.10, antiderivative size = 183, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$-\frac{35\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^3}{64d^4} + \frac{35(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^2}{96d^3} - \frac{7(a+bx)^{5/2}\sqrt{c+dx}(bc-ad)}{24d^2} + \frac{35(bc-ad)^4 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{64\sqrt{b}d^{9/2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/2)/Sqrt[c + d*x], x]

[Out] (-35*(b*c - a*d)^3*Sqrt[a + b*x]*Sqrt[c + d*x])/(64*d^4) + (35*(b*c - a*d)^2*(a + b*x)^(3/2)*Sqrt[c + d*x])/(96*d^3) - (7*(b*c - a*d)*(a + b*x)^(5/2)*Sqrt[c + d*x])/(24*d^2) + ((a + b*x)^(7/2)*Sqrt[c + d*x])/(4*d) + (35*(b*c - a*d)^4*ArcTanh[(Sqrt[d]*Sqrt[a + b*x])/(Sqrt[b]*Sqrt[c + d*x])])/(64*Sqrt[b]*d^(9/2))

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ

`[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 206

`Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])`

Rule 217

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]`

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{7/2}}{\sqrt{c+dx}} dx &= \frac{(a+bx)^{7/2}\sqrt{c+dx}}{4d} - \frac{(7(bc-ad)) \int \frac{(a+bx)^{5/2}}{\sqrt{c+dx}} dx}{8d} \\
 &= -\frac{7(bc-ad)(a+bx)^{5/2}\sqrt{c+dx}}{24d^2} + \frac{(a+bx)^{7/2}\sqrt{c+dx}}{4d} + \frac{(35(bc-ad)^2) \int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx}{48d^2} \\
 &= \frac{35(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}}{96d^3} - \frac{7(bc-ad)(a+bx)^{5/2}\sqrt{c+dx}}{24d^2} + \frac{(a+bx)^{7/2}\sqrt{c+dx}}{4d} - \frac{(35(bc-ad)^2) \int \frac{(a+bx)^{1/2}}{\sqrt{c+dx}} dx}{48d^2} \\
 &= -\frac{35(bc-ad)^3\sqrt{a+bx}\sqrt{c+dx}}{64d^4} + \frac{35(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}}{96d^3} - \frac{7(bc-ad)(a+bx)^{5/2}\sqrt{c+dx}}{24d^2} + \frac{(a+bx)^{7/2}\sqrt{c+dx}}{4d} \\
 &= -\frac{35(bc-ad)^3\sqrt{a+bx}\sqrt{c+dx}}{64d^4} + \frac{35(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}}{96d^3} - \frac{7(bc-ad)(a+bx)^{5/2}\sqrt{c+dx}}{24d^2} + \frac{(a+bx)^{7/2}\sqrt{c+dx}}{4d} \\
 &= -\frac{35(bc-ad)^3\sqrt{a+bx}\sqrt{c+dx}}{64d^4} + \frac{35(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}}{96d^3} - \frac{7(bc-ad)(a+bx)^{5/2}\sqrt{c+dx}}{24d^2} + \frac{(a+bx)^{7/2}\sqrt{c+dx}}{4d}
 \end{aligned}$$

Mathematica [A] time = 0.66, size = 189, normalized size = 1.03

$$\frac{\sqrt{d}\sqrt{a+bx}(c+dx)\left(279a^3d^3+a^2bd^2(326dx-511c)+ab^2d(385c^2-252cdx+200d^2x^2)\right)+b^3(-105c^3+70c^2dx)}{192d^{9/2}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/2)/Sqrt[c + d*x], x]

[Out] (Sqrt[d]*Sqrt[a + b*x]*(c + d*x)*(279*a^3*d^3 + a^2*b*d^2*(-511*c + 326*d*x) + a*b^2*d*(385*c^2 - 252*c*d*x + 200*d^2*x^2) + b^3*(-105*c^3 + 70*c^2*d*x - 56*c*d^2*x^2 + 48*d^3*x^3)) + (105*(b*c - a*d)^(9/2)*Sqrt[(b*(c + d*x))/(b*c - a*d)]*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/b/(192*d^(9/2)*Sqrt[c + d*x])

fricas [A] time = 0.54, size = 542, normalized size = 2.96

$$\left[\frac{105(b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + bc + \dots))}{\dots} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] [1/768*(105*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x) + 4*(48*b^4*d^4*x^3 - 105*b^4*c^3*d + 385*a*b^3*c^2*d^2 - 511*a^2*b^2*c*d^3 + 279*a^3*b*d^4 - 8*(7*b^4*c*d^3 - 25*a*b^3*d^4)*x^2 + 2*(35*b^4*c^2*d^2 - 126*a*b^3*c*d^3 + 163*a^2*b^2*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b*d^5), -1/384*(105*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)) - 2*(48*b^4*d^4*x^3 - 105*b^4*c^3*d + 385*a*b^3*c^2*d^2 - 511*a^2*b^2*c*d^3 + 279*a^3*b*d^4 - 8*(7*b^4*c*d^3 - 25*a*b^3*d^4)*x^2 + 2*(35*b^4*c^2*d^2 - 126*a*b^3*c*d^3 + 163*a^2*b^2*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b*d^5)]

giac [A] time = 1.23, size = 268, normalized size = 1.46

$$\frac{\left(\sqrt{b^2c + (bx + a)bd - abd}\left(2(bx + a)\left(4(bx + a)\left(\frac{6(bx+a)}{bd} - \frac{7(bcd^5 - ad^6)}{bd^7}\right) + \frac{35(b^2c^2d^4 - 2abcd^5 + a^2d^6)}{bd^7}\right) - \frac{105(b^3c^3d^3 - 3ab^2c^2d^4)}{bd^7}\right)\right)}{192|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(1/2),x, algorithm="giac")

[Out] $\frac{1}{192} \sqrt{b^2c + (bx+a)bd - abd} (2(bx+a)(4(bx+a)(6(bx+a)/(bd) - 7(b^2cd^5 - ad^6)/(bd^7)) + 35(b^2c^2d^4 - 2ab^2cd^5 + a^2d^6)/(bd^7)) - 105(b^3c^3d^3 - 3ab^2c^2d^4 + 3a^2b^2cd^5 - a^3d^6)/(bd^7)) \sqrt{bx+a} - 105(b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3b^2cd^3 + a^4d^4) \log(\sqrt{-bd} \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd}) / (\sqrt{bd} d^4) * b / \text{abs}(b)$

maple [B] time = 0.01, size = 650, normalized size = 3.55

$$\frac{35\sqrt{(bx+a)(dx+c)} a^4 \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad+bc)x}\right)}{128\sqrt{bx+a} \sqrt{dx+c} \sqrt{bd}} - \frac{35\sqrt{(bx+a)(dx+c)} a^3bc \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}}\right)}{32\sqrt{bx+a} \sqrt{dx+c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/2)/(d*x+c)^(1/2),x)

[Out] $\frac{1}{4} (bx+a)^{7/2} (d*x+c)^{1/2} / d + 7/24 d (bx+a)^{5/2} (d*x+c)^{1/2} a - 7/24 / d^2 (bx+a)^{5/2} (d*x+c)^{1/2} b^2 c + 35/96 d (bx+a)^{3/2} (d*x+c)^{1/2} a^2 - 35/48 d^2 (bx+a)^{3/2} (d*x+c)^{1/2} a b^2 c + 35/96 d^3 (bx+a)^{3/2} (d*x+c)^{1/2} b^2 c^2 + 35/64 d (bx+a)^{1/2} (d*x+c)^{1/2} a^3 - 105/64 d^2 (bx+a)^{1/2} (d*x+c)^{1/2} a^2 b^2 c + 105/64 d^3 (bx+a)^{1/2} (d*x+c)^{1/2} a b^2 c^2 - 35/64 d^4 (bx+a)^{1/2} (d*x+c)^{1/2} b^3 c^3 + 35/128 ((bx+a)(d*x+c))^{1/2} / (bx+a)^{1/2} / (d*x+c)^{1/2} * \ln((b*d*x + 1/2*a*d + 1/2*b*c) / (b*d)^{1/2} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{1/2}) / (b*d)^{1/2} * a^4 - 35/32 d ((bx+a)(d*x+c))^{1/2} / (bx+a)^{1/2} / (d*x+c)^{1/2} * \ln((b*d*x + 1/2*a*d + 1/2*b*c) / (b*d)^{1/2} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{1/2}) / (b*d)^{1/2} * a^3 b^2 c + 105/64 d^2 ((bx+a)(d*x+c))^{1/2} / (bx+a)^{1/2} / (d*x+c)^{1/2} * \ln((b*d*x + 1/2*a*d + 1/2*b*c) / (b*d)^{1/2} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{1/2}) / (b*d)^{1/2} * a^2 b^2 c^2 - 35/32 d^3 ((bx+a)(d*x+c))^{1/2} / (bx+a)^{1/2} / (d*x+c)^{1/2} * \ln((b*d*x + 1/2*a*d + 1/2*b*c) / (b*d)^{1/2} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{1/2}) / (b*d)^{1/2} * a b^3 c^3 + 35/128 d^4 ((bx+a)(d*x+c))^{1/2} / (bx+a)^{1/2} / (d*x+c)^{1/2} * \ln((b*d*x + 1/2*a*d + 1/2*b*c) / (b*d)^{1/2} + (b*d*x^2 + a*c + (a*d + b*c)*x)^{1/2}) / (b*d)^{1/2} * b^4 c^4$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{7/2}}{\sqrt{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/2)/(c + d*x)^(1/2), x)

[Out] int((a + b*x)^(7/2)/(c + d*x)^(1/2), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/2)/(d*x+c)**(1/2), x)

[Out] Timed out

$$3.1493 \quad \int \frac{(a+bx)^{5/2}}{\sqrt{c+dx}} dx$$

Optimal. Leaf size=148

$$\frac{5(bc-ad)^3 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{8\sqrt{b}d^{7/2}} + \frac{5\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}{8d^3} - \frac{5(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)}{12d^2} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{3d}$$

[Out] $-5/8*(-a*d+b*c)^3*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/d^{(7/2)}/b^{(1/2)}-5/12*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/d^2+1/3*(b*x+a)^{(5/2)}*(d*x+c)^{(1/2)}/d+5/8*(-a*d+b*c)^2*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/d^3$

Rubi [A] time = 0.07, antiderivative size = 148, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$\frac{5\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}{8d^3} - \frac{5(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)}{12d^2} - \frac{5(bc-ad)^3 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{8\sqrt{b}d^{7/2}} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{3d}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2)/Sqrt[c + d*x], x]

[Out] $(5*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(8*d^3) - (5*(b*c - a*d)*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(12*d^2) + ((a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x])/(3*d) - (5*(b*c - a*d)^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/(8*\operatorname{Sqrt}[b]*d^{(7/2)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{5/2}}{\sqrt{c+dx}} dx &= \frac{(a+bx)^{5/2}\sqrt{c+dx}}{3d} - \frac{(5(bc-ad)) \int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx}{6d} \\
 &= -\frac{5(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{12d^2} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{3d} + \frac{(5(bc-ad)^2) \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{8d^2} \\
 &= \frac{5(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^3} - \frac{5(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{12d^2} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{3d} - \frac{(5(bc-ad)^2) \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{8d^2} \\
 &= \frac{5(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^3} - \frac{5(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{12d^2} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{3d} - \frac{(5(bc-ad)^2) \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{8d^2} \\
 &= \frac{5(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^3} - \frac{5(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{12d^2} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{3d} - \frac{(5(bc-ad)^2) \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{8d^2} \\
 &= \frac{5(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^3} - \frac{5(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{12d^2} + \frac{(a+bx)^{5/2}\sqrt{c+dx}}{3d} - \frac{5(bc-ad)^2 \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{8d^2}
 \end{aligned}$$

Mathematica [A] time = 0.52, size = 150, normalized size = 1.01

$$\frac{\sqrt{d}\sqrt{a+bx}(c+dx)(33a^2d^2+2abd(13dx-20c)+b^2(15c^2-10cdx+8d^2x^2)) - \frac{15(bc-ad)^{7/2}\sqrt{\frac{b(c+dx)}{bc-ad}}\sinh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{bc-ad}}\right)}{b}}{24d^{7/2}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/Sqrt[c + d*x], x]

[Out] (Sqrt[d]*Sqrt[a + b*x]*(c + d*x)*(33*a^2*d^2 + 2*a*b*d*(-20*c + 13*d*x) + b^2*(15*c^2 - 10*c*d*x + 8*d^2*x^2)) - (15*(b*c - a*d)^(7/2)*Sqrt[(b*(c + d*x))/(b*c - a*d)]*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/b/(24*d^(7/2)*Sqrt[c + d*x])

fricas [A] time = 0.51, size = 412, normalized size = 2.78

$$\frac{15(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)\sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + bc + ad)\sqrt{bd}\sqrt{b^2c + (bx+a)bd - abd})}{24|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] [-1/96*(15*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(8*b^3*d^3*x^2 + 15*b^3*c^2*d - 40*a*b^2*c*d^2 + 33*a^2*b*d^3 - 2*(5*b^3*c*d^2 - 13*a*b^2*d^3)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b*d^4), 1/48*(15*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)) + 2*(8*b^3*d^3*x^2 + 15*b^3*c^2*d - 40*a*b^2*c*d^2 + 33*a^2*b*d^3 - 2*(5*b^3*c*d^2 - 13*a*b^2*d^3)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(b*d^4)]

giac [A] time = 1.27, size = 198, normalized size = 1.34

$$\frac{\left(\sqrt{b^2c + (bx+a)bd - abd} \sqrt{bx+a} \left(2(bx+a) \left(\frac{4(bx+a)}{bd} - \frac{5(bcd^3 - ad^4)}{bd^5}\right) + \frac{15(b^2c^2d^2 - 2abcd^3 + a^2d^4)}{bd^5}\right) + \frac{15(b^3c^3 - 3ab^2c^2d + 3a^2bcd^2 - a^3d^3)}{bd^5}\right)}{24|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(1/2), x, algorithm="giac")

[Out] 1/24*(sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*sqrt(b*x + a)*(2*(b*x + a)*(4*(b*x + a)/(b*d) - 5*(b*c*d^3 - a*d^4)/(b*d^5)) + 15*(b^2*c^2*d^2 - 2*a*b*c*d^3 + a^2*d^4)/(b*d^5)) + 15*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/(sqrt(b*d)*d^3))*b/abs(b)

maple [B] time = 0.01, size = 465, normalized size = 3.14

$$\frac{5\sqrt{(bx+a)(dx+c)} a^3 \ln\left(\frac{bdx+\frac{1}{2}ad+\frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2+ac+(ad+bc)x}\right)}{16\sqrt{bx+a}\sqrt{dx+c}\sqrt{bd}} - \frac{15\sqrt{(bx+a)(dx+c)} a^2bc \ln\left(\frac{bdx+\frac{1}{2}ad+\frac{1}{2}bc}{\sqrt{bd}}\right)}{16\sqrt{bx+a}\sqrt{dx+c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/(d*x+c)^(1/2),x)

[Out] $\frac{1}{3}(b*x+a)^{5/2}(d*x+c)^{1/2}/d+5/12/d*(b*x+a)^{3/2}(d*x+c)^{1/2}*a-5/12/d^2*(b*x+a)^{3/2}(d*x+c)^{1/2}*b*c+5/8/d*(b*x+a)^{1/2}(d*x+c)^{1/2}*a^2-5/4/d^2*(b*x+a)^{1/2}(d*x+c)^{1/2}*a*b*c+5/8/d^3*(b*x+a)^{1/2}(d*x+c)^{1/2}*b^2*c^2+5/16*((b*x+a)*(d*x+c))^{1/2}/(b*x+a)^{1/2}/(d*x+c)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2})*a^3-15/16/d*((b*x+a)*(d*x+c))^{1/2}/(b*x+a)^{1/2}/(d*x+c)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2}*a^2*b*c+15/16/d^2*((b*x+a)*(d*x+c))^{1/2}/(b*x+a)^{1/2}/(d*x+c)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2})*a*b^2*c^2-5/16/d^3*((b*x+a)*(d*x+c))^{1/2}/(b*x+a)^{1/2}/(d*x+c)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2})*b^3*c^3$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a+bx)^{5/2}}{\sqrt{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)/(c + d*x)^(1/2),x)

[Out] int((a + b*x)^(5/2)/(c + d*x)^(1/2), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)/(d*x+c)**(1/2),x)

[Out] Timed out

$$3.1494 \quad \int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx$$

Optimal. Leaf size=113

$$\frac{3(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{4\sqrt{b}d^{5/2}} - \frac{3\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}{4d^2} + \frac{(a+bx)^{3/2}\sqrt{c+dx}}{2d}$$

[Out] $3/4*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/d^{(5/2)}/b^{(1/2)}+1/2*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/d-3/4*(-a*d+b*c)*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/d^2$

Rubi [A] time = 0.05, antiderivative size = 113, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$-\frac{3\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}{4d^2} + \frac{3(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{4\sqrt{b}d^{5/2}} + \frac{(a+bx)^{3/2}\sqrt{c+dx}}{2d}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}/\operatorname{Sqrt}[c + d*x], x]$

[Out] $(-3*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(4*d^2) + ((a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(2*d) + (3*(b*c - a*d)^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/(4*\operatorname{Sqrt}[b]*d^{(5/2)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{NeQ}[m+n+1, 0]$ && $!(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] || (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m-n, 0])))$ && $!\operatorname{ILtQ}[m+n+2, 0]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{LtQ}[-1, m, 0]$ && $\operatorname{LeQ}[-1, n, 0]$ && $\operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx &= \frac{(a+bx)^{3/2}\sqrt{c+dx}}{2d} - \frac{(3(bc-ad)) \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{4d} \\
 &= -\frac{3(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^2} + \frac{(a+bx)^{3/2}\sqrt{c+dx}}{2d} + \frac{(3(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{8d^2} \\
 &= -\frac{3(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^2} + \frac{(a+bx)^{3/2}\sqrt{c+dx}}{2d} + \frac{(3(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}} \right)}{4bd^2} \\
 &= -\frac{3(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^2} + \frac{(a+bx)^{3/2}\sqrt{c+dx}}{2d} + \frac{(3(bc-ad)^2) \text{Subst} \left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}} \right)}{4bd^2} \\
 &= -\frac{3(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^2} + \frac{(a+bx)^{3/2}\sqrt{c+dx}}{2d} + \frac{3(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}} \right)}{4\sqrt{b}d^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.37, size = 119, normalized size = 1.05

$$\frac{\sqrt{d}\sqrt{a+bx}(c+dx)(5ad-3bc+2bdx) + \frac{3(bc-ad)^{5/2}\sqrt{\frac{b(c+dx)}{bc-ad}} \sinh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{bc-ad}}\right)}{b}}{4d^{5/2}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/Sqrt[c + d*x], x]

[Out] $(\sqrt{d} \sqrt{a + bx}) (c + dx) (-3bc + 5ad + 2b^2 dx) + (3(bc - ad)^{5/2} \sqrt{(b(c + dx))/(bc - ad)}) \operatorname{ArcSinh}(\sqrt{d} \sqrt{a + bx}) / \sqrt{t[b(c - ad)]} / b) / (4d^{5/2} \sqrt{c + dx})$

fricas [A] time = 0.47, size = 306, normalized size = 2.71

$$\left[\frac{3(b^2c^2 - 2abcd + a^2d^2) \sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + bc + ad) \sqrt{bd} \sqrt{bx + a} \sqrt{dx + c} + 16bd^3)}{16bd^3} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/2)/(d*x+c)^(1/2),x, algorithm="fricas")`

[Out] $[1/16 * (3(b^2c^2 - 2a*b*c*d + a^2*d^2) * \sqrt{b*d} * \log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d*x + b*c + a*d) * \sqrt{b*d} * \sqrt{b*x + a} * \sqrt{d*x + c} + 8*(b^2*c*d + a*b*d^2)*x) + 4*(2*b^2*d^2*x - 3*b^2*c*d + 5*a*b*d^2) * \sqrt{b*x + a} * \sqrt{d*x + c}) / (b*d^3), -1/8 * (3*(b^2*c^2 - 2*a*b*c*d + a^2*d^2) * \sqrt{-b*d} * \arctan(1/2*(2*b*d*x + b*c + a*d) * \sqrt{-b*d} * \sqrt{b*x + a} * \sqrt{d*x + c}) / (b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)) - 2*(2*b^2*d^2*x - 3*b^2*c*d + 5*a*b*d^2) * \sqrt{b*x + a} * \sqrt{d*x + c}) / (b*d^3)]$

giac [A] time = 0.95, size = 139, normalized size = 1.23

$$\left(\frac{\sqrt{b^2c + (bx + a)bd - abd} \sqrt{bx + a} \left(\frac{2(bx+a)}{bd} - \frac{3(bcd-ad^2)}{bd^3} \right) - \frac{3(b^2c^2 - 2abcd + a^2d^2) \log\left(\left| -\sqrt{bd} \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd} \right| \right)}{\sqrt{bd} d^2}}{4|b|} \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/2)/(d*x+c)^(1/2),x, algorithm="giac")`

[Out] $1/4 * (\sqrt{b^2c + (bx + a)bd - abd} * \sqrt{bx + a} * (2*(bx + a)/(b*d) - 3*(b*c*d - a*d^2)/(b*d^3)) - 3*(b^2*c^2 - 2*a*b*c*d + a^2*d^2) * \log(\operatorname{abs}(-\sqrt{b*d} * \sqrt{b*x + a} + \sqrt{b^2*c + (bx + a)bd - abd})) / (\sqrt{b*d} * d^2)) * b / \operatorname{abs}(b)$

maple [B] time = 0.01, size = 308, normalized size = 2.73

$$\frac{3\sqrt{(bx + a)(dx + c)} a^2 \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad + bc)x}\right)}{8\sqrt{bx + a} \sqrt{dx + c} \sqrt{bd}} - \frac{3\sqrt{(bx + a)(dx + c)} abc \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad + bc)x}\right)}{4\sqrt{bx + a} \sqrt{dx + c} \sqrt{bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(3/2)/(d*x+c)^(1/2),x)`

[Out] $\frac{1}{2}(b*x+a)^{3/2}(d*x+c)^{1/2}/d+3/4/d*(b*x+a)^{1/2}(d*x+c)^{1/2}*a-3/4/d^2*(b*x+a)^{1/2}(d*x+c)^{1/2}*b*c+3/8*((b*x+a)*(d*x+c))^{1/2}/(b*x+a)^{1/2}/(d*x+c)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2}*a^2-3/4/d*((b*x+a)*(d*x+c))^{1/2}/(b*x+a)^{1/2}/(d*x+c)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2}*a*b*c+3/8/d^2*((b*x+a)*(d*x+c))^{1/2}/(b*x+a)^{1/2}/(d*x+c)^{1/2}*\ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^{1/2}+(b*d*x^2+a*c+(a*d+b*c)*x)^{1/2})/(b*d)^{1/2}*b^2*c^2$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/2)/(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*x)^(3/2)/(c+d*x)^(1/2),x)`

[Out] `int((a+b*x)^(3/2)/(c+d*x)^(1/2),x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(3/2)/(d*x+c)**(1/2),x)`

[Out] `Integral((a+b*x)**(3/2)/sqrt(c+d*x),x)`

$$3.1495 \quad \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx$$

Optimal. Leaf size=73

$$\frac{\sqrt{a+bx}\sqrt{c+dx}}{d} - \frac{(bc-ad)\tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{\sqrt{b}d^{3/2}}$$

[Out] $-(-a*d+b*c)*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/d^{(3/2)}/b^{(1/2)}+(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/d$

Rubi [A] time = 0.04, antiderivative size = 73, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 217, 206}

$$\frac{\sqrt{a+bx}\sqrt{c+dx}}{d} - \frac{(bc-ad)\tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{\sqrt{b}d^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/Sqrt[c + d*x], x]

[Out] $(\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/d - ((b*c - a*d)*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/(\operatorname{Sqrt}[b]*d^{(3/2)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206


```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx &= \frac{\sqrt{a+bx}\sqrt{c+dx}}{d} - \frac{(bc-ad) \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{2d} \\ &= \frac{\sqrt{a+bx}\sqrt{c+dx}}{d} - \frac{(bc-ad) \operatorname{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \sqrt{a+bx}\right)}{bd} \\ &= \frac{\sqrt{a+bx}\sqrt{c+dx}}{d} - \frac{(bc-ad) \operatorname{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}}\right)}{bd} \\ &= \frac{\sqrt{a+bx}\sqrt{c+dx}}{d} - \frac{(bc-ad) \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{\sqrt{b}d^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.27, size = 103, normalized size = 1.41

$$\frac{b\sqrt{d}\sqrt{a+bx}(c+dx) - (bc-ad)^{3/2}\sqrt{\frac{b(c+dx)}{bc-ad}} \sinh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{bc-ad}}\right)}{bd^{3/2}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[a + b*x]/Sqrt[c + d*x], x]
```

```
[Out] (b*Sqrt[d]*Sqrt[a + b*x]*(c + d*x) - (b*c - a*d)^(3/2)*Sqrt[(b*(c + d*x))/(
b*c - a*d)]*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(b*d^(3/2)*Sq
rt[c + d*x])
```

fricas [A] time = 0.49, size = 235, normalized size = 3.22

$$\left[\frac{4 \sqrt{bx+a} \sqrt{dx+c} bd - (bc-ad) \sqrt{bd} \log(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + bc + ad) \sqrt{bd} \sqrt{bx+a} \sqrt{dx+c})}{4bd^2} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/2),x, algorithm="fricas")

[Out] [1/4*(4*sqrt(b*x + a)*sqrt(d*x + c)*b*d - (b*c - a*d)*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x))/(b*d^2), 1/2*(2*sqrt(b*x + a)*sqrt(d*x + c)*b*d + (b*c - a*d)*sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x)))/(b*d^2)]

giac [A] time = 1.12, size = 97, normalized size = 1.33

$$\frac{b \left(\frac{(bc-ad) \log\left(\left| -\sqrt{bd} \sqrt{bx+a} + \sqrt{b^2c+(bx+a)bd-abd} \right| \right)}{\sqrt{bd} d} + \frac{\sqrt{b^2c+(bx+a)bd-abd} \sqrt{bx+a}}{bd} \right)}{|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/2),x, algorithm="giac")

[Out] b*((b*c - a*d)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/(sqrt(b*d)*d) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*sqrt(b*x + a)/(b*d))/abs(b)

maple [A] time = 0.01, size = 107, normalized size = 1.47

$$\frac{(-ad + bc) \sqrt{(bx+a)(dx+c)} \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad + bc)x} \right)}{2\sqrt{bx+a} \sqrt{dx+c} \sqrt{bd} d} + \frac{\sqrt{bx+a} \sqrt{dx+c}}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(1/2),x)

[Out] (b*x+a)^(1/2)*(d*x+c)^(1/2)/d-1/2*(-a*d+b*c)/d*((b*x+a)*(d*x+c))^(1/2)/(b*x+a)^(1/2)/(d*x+c)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 3.80, size = 261, normalized size = 3.58

$$\frac{\frac{(2ad+2bc)(\sqrt{a+bx}-\sqrt{a})^3}{d^2(\sqrt{c+dx}-\sqrt{c})^3} + \frac{(2cb^2+2adb)(\sqrt{a+bx}-\sqrt{a})}{d^3(\sqrt{c+dx}-\sqrt{c})} - \frac{8\sqrt{a}b\sqrt{c}(\sqrt{a+bx}-\sqrt{a})^2}{d^2(\sqrt{c+dx}-\sqrt{c})^2}}{\frac{(\sqrt{a+bx}-\sqrt{a})^4}{(\sqrt{c+dx}-\sqrt{c})^4} + \frac{b^2}{d^2} - \frac{2b(\sqrt{a+bx}-\sqrt{a})^2}{d(\sqrt{c+dx}-\sqrt{c})^2}} + \frac{2 \operatorname{atanh}\left(\frac{\sqrt{d}(\sqrt{a+bx}-\sqrt{a})}{\sqrt{b}(\sqrt{c+dx}-\sqrt{c})}\right)(ad-bc)}{\sqrt{b}d^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(1/2),x)

[Out] (((2*a*d + 2*b*c)*((a + b*x)^(1/2) - a^(1/2))^3)/(d^2*((c + d*x)^(1/2) - c^(1/2))^3) + ((2*b^2*c + 2*a*b*d)*((a + b*x)^(1/2) - a^(1/2)))/(d^3*((c + d*x)^(1/2) - c^(1/2))) - (8*a^(1/2)*b*c^(1/2)*((a + b*x)^(1/2) - a^(1/2))^2)/(d^2*((c + d*x)^(1/2) - c^(1/2))^2))/(((a + b*x)^(1/2) - a^(1/2))^4/((c + d*x)^(1/2) - c^(1/2))^4 + b^2/d^2 - (2*b*((a + b*x)^(1/2) - a^(1/2))^2)/(d*((c + d*x)^(1/2) - c^(1/2))^2)) + (2*atanh((d^(1/2)*((a + b*x)^(1/2) - a^(1/2))))/(b^(1/2)*((c + d*x)^(1/2) - c^(1/2))))*(a*d - b*c))/(b^(1/2)*d^(3/2))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(1/2),x)

[Out] Integral(sqrt(a + b*x)/sqrt(c + d*x), x)

$$3.1496 \quad \int \frac{1}{\sqrt{a+bx} \sqrt{c+dx}} dx$$

Optimal. Leaf size=42

$$\frac{2 \tanh^{-1} \left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{b} \sqrt{c+dx}} \right)}{\sqrt{b} \sqrt{d}}$$

[Out] 2*arctanh(d^(1/2)*(b*x+a)^(1/2)/b^(1/2)/(d*x+c)^(1/2))/b^(1/2)/d^(1/2)

Rubi [A] time = 0.03, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {63, 217, 206}

$$\frac{2 \tanh^{-1} \left(\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{b} \sqrt{c+dx}} \right)}{\sqrt{b} \sqrt{d}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*Sqrt[c + d*x]),x]

[Out] (2*ArcTanh[(Sqrt[d]*Sqrt[a + b*x])/(Sqrt[b]*Sqrt[c + d*x])])/(Sqrt[b]*Sqrt[d])

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(1*ArcTanh[Rt[-b, 2]*x]/Rt[a, 2])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx = \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \sqrt{a+bx}\right)}{b}$$

$$= \frac{2 \operatorname{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}}\right)}{b}$$

$$= \frac{2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{\sqrt{b}\sqrt{d}}$$

Mathematica [A] time = 0.07, size = 77, normalized size = 1.83

$$\frac{2\sqrt{c+dx} \sinh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{bc-ad}}\right)}{\sqrt{d}\sqrt{bc-ad} \sqrt{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*Sqrt[c + d*x]),x]

[Out] (2*Sqrt[c + d*x]*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(Sqrt[d]*Sqrt[b*c - a*d]*Sqrt[(b*(c + d*x))/(b*c - a*d)])

fricas [B] time = 0.48, size = 178, normalized size = 4.24

$$\left[\frac{\sqrt{bd} \log\left(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + bc + ad)\sqrt{bd}\sqrt{bx+a}\sqrt{dx+c} + 8(b^2cd + abd^2)x\right)}{2bd}, \dots \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/2),x, algorithm="fricas")

[Out] [1/2*sqrt(b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d*x + b*c + a*d)*sqrt(b*d)*sqrt(b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d + a*b*d^2)*x)/(b*d), -sqrt(-b*d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(-b*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 + a*b*c*d + (b^2*c*d + a*b*d^2)*x))/(b*d)]

giac [A] time = 1.10, size = 50, normalized size = 1.19

$$\frac{2b \log\left(\left|-\sqrt{bd} \sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd}\right|\right)}{\sqrt{bd}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/2),x, algorithm="giac")

[Out] -2*b*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/(sqrt(b*d)*abs(b))

maple [B] time = 0.01, size = 76, normalized size = 1.81

$$\frac{\sqrt{(bx+a)(dx+c)} \ln\left(\frac{bdx + \frac{1}{2}ad + \frac{1}{2}bc}{\sqrt{bd}} + \sqrt{bdx^2 + ac + (ad+bc)x}\right)}{\sqrt{bx+a} \sqrt{dx+c} \sqrt{bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(1/2),x)

[Out] ((b*x+a)*(d*x+c))^(1/2)/(b*x+a)^(1/2)/(d*x+c)^(1/2)*ln((b*d*x+1/2*a*d+1/2*b*c)/(b*d)^(1/2)+(b*d*x^2+a*c+(a*d+b*c)*x)^(1/2))/(b*d)^(1/2)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 0.29, size = 45, normalized size = 1.07

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{c+dx}-\sqrt{c})}{\sqrt{-bd}(\sqrt{a+bx}-\sqrt{a})}\right)}{\sqrt{-bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(1/2)*(c + d*x)^(1/2)),x)`

[Out] $-(4*\operatorname{atan}((b*((c + d*x)^{(1/2)} - c^{(1/2)}))/((-b*d)^{(1/2)*((a + b*x)^{(1/2)} - a^{(1/2)}))))/(-b*d)^{(1/2)}$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a + bx} \sqrt{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/2)/(d*x+c)**(1/2),x)`

[Out] `Integral(1/(sqrt(a + b*x)*sqrt(c + d*x)), x)`

$$3.1497 \quad \int \frac{1}{(a+bx)^{3/2} \sqrt{c+dx}} dx$$

Optimal. Leaf size=30

$$-\frac{2\sqrt{c+dx}}{\sqrt{a+bx}(bc-ad)}$$

[Out] $-2*(d*x+c)^{(1/2)/(-a*d+b*c)/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{2\sqrt{c+dx}}{\sqrt{a+bx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)^{(3/2)*\text{Sqrt}[c + d*x]}), x]$

[Out] $(-2*\text{Sqrt}[c + d*x])/((b*c - a*d)*\text{Sqrt}[a + b*x])$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Simp} [((a + b*x)^{(m + 1)*(c + d*x)^{(n + 1)}})/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{1}{(a+bx)^{3/2} \sqrt{c+dx}} dx = -\frac{2\sqrt{c+dx}}{(bc-ad)\sqrt{a+bx}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$\frac{2\sqrt{c+dx}}{\sqrt{a+bx}(ad-bc)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/((a + b*x)^{(3/2)*\text{Sqrt}[c + d*x]}), x]$

[Out] $(2\sqrt{c + dx})/((-b*c) + a*d)*\sqrt{a + b*x}$

fricas [A] time = 0.44, size = 42, normalized size = 1.40

$$\frac{2\sqrt{bx+a}\sqrt{dx+c}}{abc - a^2d + (b^2c - abd)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/2),x, algorithm="fricas")`

[Out] $-2*\sqrt{b*x + a}*\sqrt{d*x + c}/(a*b*c - a^2*d + (b^2*c - a*b*d)*x)$

giac [B] time = 1.04, size = 66, normalized size = 2.20

$$-\frac{4\sqrt{bd}b}{\left(b^2c - abd - \left(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}\right)^2\right)|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/2),x, algorithm="giac")`

[Out] $-4*\sqrt{b*d}*b/((b^2*c - a*b*d - (\sqrt{b*d}*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d}))^2)*\text{abs}(b)$

maple [A] time = 0.01, size = 27, normalized size = 0.90

$$\frac{2\sqrt{dx+c}}{\sqrt{bx+a}(ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(3/2)/(d*x+c)^(1/2),x)`

[Out] $2/(b*x+a)^(1/2)*(d*x+c)^(1/2)/(a*d-b*c)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* h

elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c zero or nonzero?

mupad [B] time = 0.73, size = 26, normalized size = 0.87

$$\frac{2\sqrt{c+dx}}{(ad-bc)\sqrt{a+bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(1/2)),x)

[Out] (2*(c + d*x)^(1/2))/((a*d - b*c)*(a + b*x)^(1/2))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{3}{2}}\sqrt{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(1/2),x)

[Out] Integral(1/((a + b*x)**(3/2)*sqrt(c + d*x)), x)

$$3.1498 \quad \int \frac{1}{(a+bx)^{5/2} \sqrt{c+dx}} dx$$

Optimal. Leaf size=66

$$\frac{4d\sqrt{c+dx}}{3\sqrt{a+bx}(bc-ad)^2} - \frac{2\sqrt{c+dx}}{3(a+bx)^{3/2}(bc-ad)}$$

[Out] $-2/3*(d*x+c)^{(1/2)/(-a*d+b*c)/(b*x+a)^{(3/2)+4/3*d*(d*x+c)^{(1/2)/(-a*d+b*c)^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{4d\sqrt{c+dx}}{3\sqrt{a+bx}(bc-ad)^2} - \frac{2\sqrt{c+dx}}{3(a+bx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*Sqrt[c + d*x]),x]

[Out] $(-2*\text{Sqrt}[c + d*x])/(3*(b*c - a*d)*(a + b*x)^{(3/2)}) + (4*d*\text{Sqrt}[c + d*x])/(3*(b*c - a*d)^2*\text{Sqrt}[a + b*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{5/2}\sqrt{c+dx}} dx = -\frac{2\sqrt{c+dx}}{3(bc-ad)(a+bx)^{3/2}} - \frac{(2d) \int \frac{1}{(a+bx)^{3/2}\sqrt{c+dx}} dx}{3(bc-ad)}$$

$$= -\frac{2\sqrt{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{4d\sqrt{c+dx}}{3(bc-ad)^2\sqrt{a+bx}}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.70

$$\frac{2\sqrt{c+dx}(3ad-bc+2bdx)}{3(a+bx)^{3/2}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*Sqrt[c + d*x]), x]

[Out] (2*Sqrt[c + d*x]*(-(b*c) + 3*a*d + 2*b*d*x))/(3*(b*c - a*d)^2*(a + b*x)^(3/2))

fricas [B] time = 0.51, size = 118, normalized size = 1.79

$$\frac{2(2bdx - bc + 3ad)\sqrt{bx+a}\sqrt{dx+c}}{3(a^2b^2c^2 - 2a^3bcd + a^4d^2 + (b^4c^2 - 2ab^3cd + a^2b^2d^2)x^2 + 2(ab^3c^2 - 2a^2b^2cd + a^3bd^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] 2/3*(2*b*d*x - b*c + 3*a*d)*sqrt(b*x + a)*sqrt(d*x + c)/(a^2*b^2*c^2 - 2*a^3*b*c*d + a^4*d^2 + (b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2)*x^2 + 2*(a*b^3*c^2 - 2*a^2*b^2*c*d + a^3*b*d^2)*x)

giac [B] time = 1.08, size = 121, normalized size = 1.83

$$\frac{8\left(b^2c - abd - 3\left(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}\right)^2\right)\sqrt{bd}b^2d}{3\left(b^2c - abd - \left(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}\right)^2\right)^3|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/2), x, algorithm="giac")

[Out] $8/3*(b^2*c - a*b*d - 3*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*\sqrt{b*d}*b^2*d/((b^2*c - a*b*d - (\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2)^3*\text{abs}(b)$

maple [A] time = 0.00, size = 54, normalized size = 0.82

$$\frac{2\sqrt{dx + c} (2bdx + 3ad - bc)}{3(bx + a)^{\frac{3}{2}} (a^2d^2 - 2abcd + b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(5/2)/(d*x+c)^(1/2),x)`

[Out] $2/3*(d*x+c)^{(1/2)}*(2*b*d*x+3*a*d-b*c)/(b*x+a)^{(3/2)}/(a^2*d^2-2*a*b*c*d+b^2*c^2)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 0.89, size = 71, normalized size = 1.08

$$\frac{\left(\frac{4dx}{3(ad-bc)^2} + \frac{6ad-2bc}{3b(ad-bc)^2}\right) \sqrt{c+dx}}{x\sqrt{a+bx} + \frac{a\sqrt{a+bx}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(5/2)*(c + d*x)^(1/2)),x)`

[Out] $((4*d*x)/(3*(a*d - b*c)^2) + (6*a*d - 2*b*c)/(3*b*(a*d - b*c)^2))*(c + d*x)^{(1/2)}/(x*(a + b*x)^{(1/2)} + (a*(a + b*x)^{(1/2)})/b)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{5}{2}} \sqrt{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(1/2),x)
```

```
[Out] Integral(1/((a + b*x)**(5/2)*sqrt(c + d*x)), x)
```

$$3.1499 \quad \int \frac{1}{(a+bx)^{7/2} \sqrt{c+dx}} dx$$

Optimal. Leaf size=101

$$-\frac{16d^2\sqrt{c+dx}}{15\sqrt{a+bx}(bc-ad)^3} + \frac{8d\sqrt{c+dx}}{15(a+bx)^{3/2}(bc-ad)^2} - \frac{2\sqrt{c+dx}}{5(a+bx)^{5/2}(bc-ad)}$$

[Out] $-2/5*(d*x+c)^{(1/2)/(-a*d+b*c)/(b*x+a)^{(5/2)}+8/15*d*(d*x+c)^{(1/2)/(-a*d+b*c)}^2/(b*x+a)^{(3/2)}-16/15*d^2*(d*x+c)^{(1/2)/(-a*d+b*c)^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{16d^2\sqrt{c+dx}}{15\sqrt{a+bx}(bc-ad)^3} + \frac{8d\sqrt{c+dx}}{15(a+bx)^{3/2}(bc-ad)^2} - \frac{2\sqrt{c+dx}}{5(a+bx)^{5/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/2)*Sqrt[c + d*x]),x]

[Out] $(-2*\text{Sqrt}[c + d*x])/(5*(b*c - a*d)*(a + b*x)^{(5/2)}) + (8*d*\text{Sqrt}[c + d*x])/(15*(b*c - a*d)^2*(a + b*x)^{(3/2)}) - (16*d^2*\text{Sqrt}[c + d*x])/(15*(b*c - a*d)^3*\text{Sqrt}[a + b*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{7/2}\sqrt{c+dx}} dx &= -\frac{2\sqrt{c+dx}}{5(bc-ad)(a+bx)^{5/2}} - \frac{(4d) \int \frac{1}{(a+bx)^{5/2}\sqrt{c+dx}} dx}{5(bc-ad)} \\
&= -\frac{2\sqrt{c+dx}}{5(bc-ad)(a+bx)^{5/2}} + \frac{8d\sqrt{c+dx}}{15(bc-ad)^2(a+bx)^{3/2}} + \frac{(8d^2) \int \frac{1}{(a+bx)^{3/2}\sqrt{c+dx}} dx}{15(bc-ad)^2} \\
&= -\frac{2\sqrt{c+dx}}{5(bc-ad)(a+bx)^{5/2}} + \frac{8d\sqrt{c+dx}}{15(bc-ad)^2(a+bx)^{3/2}} - \frac{16d^2\sqrt{c+dx}}{15(bc-ad)^3\sqrt{a+bx}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 75, normalized size = 0.74

$$-\frac{2\sqrt{c+dx} (15a^2d^2 - 10abd(c-2dx) + b^2(3c^2 - 4cdx + 8d^2x^2))}{15(a+bx)^{5/2}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/2)*Sqrt[c + d*x]), x]

[Out] (-2*Sqrt[c + d*x]*(15*a^2*d^2 - 10*a*b*d*(c - 2*d*x) + b^2*(3*c^2 - 4*c*d*x + 8*d^2*x^2))/(15*(b*c - a*d)^3*(a + b*x)^(5/2))

fricas [B] time = 0.71, size = 251, normalized size = 2.49

$$-\frac{2(8b^2d^2x^2 + 3b^2c^2 - 10abcd + 15a^2d^2 - 4(b^2cd - 5abd^2)x)}{15(a^3b^3c^3 - 3a^4b^2c^2d + 3a^5bcd^2 - a^6d^3 + (b^6c^3 - 3ab^5c^2d + 3a^2b^4cd^2 - a^3b^3d^3)x^3 + 3(ab^5c^3 - 3a^2b^4c^2d + 3a^3b^3cd^2 - a^4b^2d^3)x^2 + 3(a^2b^4c^3 - 3a^3b^3c^2d + 3a^4b^2c*d^2 - a^5b*d^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/2)/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] -2/15*(8*b^2*d^2*x^2 + 3*b^2*c^2 - 10*a*b*c*d + 15*a^2*d^2 - 4*(b^2*c*d - 5*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^3*b^3*c^3 - 3*a^4*b^2*c^2*d + 3*a^5*b*c*d^2 - a^6*d^3 + (b^6*c^3 - 3*a*b^5*c^2*d + 3*a^2*b^4*c*d^2 - a^3*b^3*d^3)*x^3 + 3*(a*b^5*c^3 - 3*a^2*b^4*c^2*d + 3*a^3*b^3*c*d^2 - a^4*b^2*d^3)*x^2 + 3*(a^2*b^4*c^3 - 3*a^3*b^3*c^2*d + 3*a^4*b^2*c*d^2 - a^5*b*d^3)*x)

giac [B] time = 1.27, size = 227, normalized size = 2.25

$$-\frac{32(b^4c^2 - 2ab^3cd + a^2b^2d^2 - 5(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd})^2 b^2c + 5(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd})^2 b^2c + 5(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd})^2 b^2c)}{15(b^2c - abd - (\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}))^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(7/2)/(d*x+c)^(1/2),x, algorithm="giac")`

[Out]
$$-32/15*(b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2 - 5*(\sqrt{b*d}*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*b^2*c + 5*(\sqrt{b*d}*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*a*b*d + 10*(\sqrt{b*d}*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^4)*\sqrt{b*d}*b^3*d^2/((b^2*c - a*b*d - (\sqrt{b*d}*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2)^5*ab$$

$$s(b))$$

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{2\sqrt{dx+c} \left(8b^2x^2d^2 + 20abd^2x - 4b^2cdx + 15a^2d^2 - 10abcd + 3b^2c^2 \right)}{15(bx+a)^{\frac{5}{2}} \left(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(7/2)/(d*x+c)^(1/2),x)`

[Out]
$$2/15*(d*x+c)^(1/2)*(8*b^2*d^2*x^2+20*a*b*d^2*x-4*b^2*c*d*x+15*a^2*d^2-10*a*b*c*d+3*b^2*c^2)/(b*x+a)^(5/2)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)$$

$$)$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(7/2)/(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.01, size = 133, normalized size = 1.32

$$\frac{\sqrt{c+dx} \left(\frac{16d^2x^2}{15(ad-bc)^3} + \frac{30a^2d^2-20abcd+6b^2c^2}{15b^2(ad-bc)^3} + \frac{8dx(5ad-bc)}{15b(ad-bc)^3} \right)}{x^2\sqrt{a+bx} + \frac{a^2\sqrt{a+bx}}{b^2} + \frac{2ax\sqrt{a+bx}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a+b*x)^(7/2)*(c+d*x)^(1/2)),x)`

```
[Out] ((c + d*x)^(1/2)*((16*d^2*x^2)/(15*(a*d - b*c)^3) + (30*a^2*d^2 + 6*b^2*c^2
- 20*a*b*c*d)/(15*b^2*(a*d - b*c)^3) + (8*d*x*(5*a*d - b*c))/(15*b*(a*d -
b*c)^3)))/(x^2*(a + b*x)^(1/2) + (a^2*(a + b*x)^(1/2))/b^2 + (2*a*x*(a + b*
x)^(1/2))/b)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{7}{2}} \sqrt{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(7/2)/(d*x+c)**(1/2),x)
```

```
[Out] Integral(1/((a + b*x)**(7/2)*sqrt(c + d*x)), x)
```

$$3.1500 \quad \int \frac{1}{(a+bx)^{9/2} \sqrt{c+dx}} dx$$

Optimal. Leaf size=136

$$\frac{32d^3\sqrt{c+dx}}{35\sqrt{a+bx}(bc-ad)^4} - \frac{16d^2\sqrt{c+dx}}{35(a+bx)^{3/2}(bc-ad)^3} + \frac{12d\sqrt{c+dx}}{35(a+bx)^{5/2}(bc-ad)^2} - \frac{2\sqrt{c+dx}}{7(a+bx)^{7/2}(bc-ad)}$$

[Out] $-2/7*(d*x+c)^{(1/2)/(-a*d+b*c)/(b*x+a)^{(7/2)+12/35*d*(d*x+c)^{(1/2)/(-a*d+b*c)^{(5/2)-16/35*d^2*(d*x+c)^{(1/2)/(-a*d+b*c)^3/(b*x+a)^{(3/2)+32/35*d^3*(d*x+c)^{(1/2)/(-a*d+b*c)^4/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{32d^3\sqrt{c+dx}}{35\sqrt{a+bx}(bc-ad)^4} - \frac{16d^2\sqrt{c+dx}}{35(a+bx)^{3/2}(bc-ad)^3} + \frac{12d\sqrt{c+dx}}{35(a+bx)^{5/2}(bc-ad)^2} - \frac{2\sqrt{c+dx}}{7(a+bx)^{7/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(9/2)*Sqrt[c + d*x]),x]

[Out] $(-2*\text{Sqrt}[c + d*x])/(7*(b*c - a*d)*(a + b*x)^{(7/2)}) + (12*d*\text{Sqrt}[c + d*x])/(35*(b*c - a*d)^2*(a + b*x)^{(5/2)}) - (16*d^2*\text{Sqrt}[c + d*x])/(35*(b*c - a*d)^3*(a + b*x)^{(3/2)}) + (32*d^3*\text{Sqrt}[c + d*x])/(35*(b*c - a*d)^4*\text{Sqrt}[a + b*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{9/2}\sqrt{c+dx}} dx &= -\frac{2\sqrt{c+dx}}{7(bc-ad)(a+bx)^{7/2}} - \frac{(6d) \int \frac{1}{(a+bx)^{7/2}\sqrt{c+dx}} dx}{7(bc-ad)} \\
&= -\frac{2\sqrt{c+dx}}{7(bc-ad)(a+bx)^{7/2}} + \frac{12d\sqrt{c+dx}}{35(bc-ad)^2(a+bx)^{5/2}} + \frac{(24d^2) \int \frac{1}{(a+bx)^{5/2}\sqrt{c+dx}} dx}{35(bc-ad)^2} \\
&= -\frac{2\sqrt{c+dx}}{7(bc-ad)(a+bx)^{7/2}} + \frac{12d\sqrt{c+dx}}{35(bc-ad)^2(a+bx)^{5/2}} - \frac{16d^2\sqrt{c+dx}}{35(bc-ad)^3(a+bx)^{3/2}} - \frac{(16d^3)}{35(bc-ad)^4} \\
&= -\frac{2\sqrt{c+dx}}{7(bc-ad)(a+bx)^{7/2}} + \frac{12d\sqrt{c+dx}}{35(bc-ad)^2(a+bx)^{5/2}} - \frac{16d^2\sqrt{c+dx}}{35(bc-ad)^3(a+bx)^{3/2}} + \frac{32d^3}{35(bc-ad)^4}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 116, normalized size = 0.85

$$\frac{2\sqrt{c+dx} (35a^3d^3 - 35a^2bd^2(c-2dx) + 7ab^2d(3c^2 - 4cdx + 8d^2x^2) + b^3(-5c^3 + 6c^2dx - 8cd^2x^2 + 16d^3x^3))}{35(a+bx)^{7/2}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(9/2)*Sqrt[c + d*x]), x]

[Out] (2*Sqrt[c + d*x]*(35*a^3*d^3 - 35*a^2*b*d^2*(c - 2*d*x) + 7*a*b^2*d*(3*c^2 - 4*c*d*x + 8*d^2*x^2) + b^3*(-5*c^3 + 6*c^2*d*x - 8*c*d^2*x^2 + 16*d^3*x^3)))/(35*(b*c - a*d)^4*(a + b*x)^(7/2))

fricas [B] time = 1.22, size = 419, normalized size = 3.08

$$\frac{2(16b^3d^3x^3 - 5b^3c^3 + 21ab^2c^2d)}{35(a^4b^4c^4 - 4a^5b^3c^3d + 6a^6b^2c^2d^2 - 4a^7bcd^3 + a^8d^4 + (b^8c^4 - 4ab^7c^3d + 6a^2b^6c^2d^2 - 4a^3b^5cd^3 + a^4b^4d^4)x^4 + \dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] 2/35*(16*b^3*d^3*x^3 - 5*b^3*c^3 + 21*a*b^2*c^2*d - 35*a^2*b*c*d^2 + 35*a^3*d^3 - 8*(b^3*c*d^2 - 7*a*b^2*d^3)*x^2 + 2*(3*b^3*c^2*d - 14*a*b^2*c*d^2 + 35*a^2*b*d^3)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^4*b^4*c^4 - 4*a^5*b^3*c^3*d + 6*a^6*b^2*c^2*d^2 - 4*a^7*b*c*d^3 + a^8*d^4 + (b^8*c^4 - 4*a*b^7*c^3*d + 6*a^2*b^6*c^2*d^2 - 4*a^3*b^5*c*d^3 + a^4*b^4*d^4)*x^4 + 4*(a*b^7*c^4 - 4*a^2*b^6*c^3*d + 6*a^3*b^5*c^2*d^2 - 4*a^4*b^4*c*d^3 + a^5*b^3*d^4)*x^3 + 6*

$$(a^2b^6c^4 - 4a^3b^5c^3d + 6a^4b^4c^2d^2 - 4a^5b^3cd^3 + a^6b^2d^4)x^2 + 4(a^3b^5c^4 - 4a^4b^4c^3d + 6a^5b^3c^2d^2 - 4a^6b^2cd^3 + a^7b^2d^4)x$$

giac [B] time = 1.47, size = 386, normalized size = 2.84

$$64 \frac{\left(b^6c^3 - 3ab^5c^2d + 3a^2b^4cd^2 - a^3b^3d^3 - 7\left(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}\right)^2 b^4c^2 + 14\left(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}\right)\sqrt{b^2c + (bx+a)bd - abd}\right)}{\left(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}\right)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(d*x+c)^(1/2),x, algorithm="giac")

[Out] $64/35*(b^6*c^3 - 3*a*b^5*c^2*d + 3*a^2*b^4*c*d^2 - a^3*b^3*d^3 - 7*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^2*b^4*c^2 + 14*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^2*a*b^3*c*d - 7*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^2*b^2*d^2 + 21*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^4*b^2*c - 21*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^4*a*b*d - 35*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^6*\text{sqrt}(b*d)*b^4*d^3/((b^2*c - a*b*d - (\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^2)^7*\text{abs}(b))$

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$2\sqrt{dx+c} \frac{\left(16b^3x^3d^3 + 56ab^2d^3x^2 - 8b^3cd^2x^2 + 70a^2bd^3x - 28ab^2cd^2x + 6b^3c^2dx + 35a^3d^3 - 35a^2bcd^2 + 21a^3cd^2 - 35a^2bcd^2 + 21a^3cd^2\right)}{35(bx+a)^{\frac{7}{2}}\left(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(9/2)/(d*x+c)^(1/2),x)

[Out] $2/35*(d*x+c)^{(1/2)}*(16*b^3*d^3*x^3+56*a*b^2*d^3*x^2-8*b^3*c*d^2*x^2+70*a^2*b*d^3*x-28*a*b^2*c*d^2*x+6*b^3*c^2*d*x+35*a^3*d^3-35*a^2*b*c*d^2+21*a*b^2*c^2*d-5*b^3*c^3)/(b*x+a)^{(7/2)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details) Is a*d-b*c zero or nonzero?

mupad [B] time = 1.19, size = 209, normalized size = 1.54

$$\frac{\sqrt{c+dx} \left(\frac{32d^3x^3}{35(ad-bc)^4} + \frac{70a^3d^3-70a^2bcd^2+42ab^2c^2d-10b^3c^3}{35b^3(ad-bc)^4} + \frac{4dx(35a^2d^2-14abcd+3b^2c^2)}{35b^2(ad-bc)^4} + \frac{16d^2x^2(7ad-bc)}{35b(ad-bc)^4} \right)}{x^3\sqrt{a+bx} + \frac{a^3\sqrt{a+bx}}{b^3} + \frac{3ax^2\sqrt{a+bx}}{b} + \frac{3a^2x\sqrt{a+bx}}{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(9/2)*(c + d*x)^(1/2)),x)

[Out] ((c + d*x)^(1/2)*((32*d^3*x^3)/(35*(a*d - b*c)^4) + (70*a^3*d^3 - 10*b^3*c^3 + 42*a*b^2*c^2*d - 70*a^2*b*c*d^2)/(35*b^3*(a*d - b*c)^4) + (4*d*x*(35*a^2*d^2 + 3*b^2*c^2 - 14*a*b*c*d))/(35*b^2*(a*d - b*c)^4) + (16*d^2*x^2*(7*a*d - b*c))/(35*b*(a*d - b*c)^4))/((x^3*(a + b*x)^(1/2) + (a^3*(a + b*x)^(1/2))/b^3 + (3*a*x^2*(a + b*x)^(1/2))/b + (3*a^2*x*(a + b*x)^(1/2))/b^2))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{9}{2}} \sqrt{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(9/2)/(d*x+c)**(1/2),x)

[Out] Integral(1/((a + b*x)**(9/2)*sqrt(c + d*x)), x)

$$3.1501 \quad \int \frac{1}{(a+bx)^{11/2} \sqrt{c+dx}} dx$$

Optimal. Leaf size=171

$$\frac{256d^4\sqrt{c+dx}}{315\sqrt{a+bx}(bc-ad)^5} + \frac{128d^3\sqrt{c+dx}}{315(a+bx)^{3/2}(bc-ad)^4} - \frac{32d^2\sqrt{c+dx}}{105(a+bx)^{5/2}(bc-ad)^3} + \frac{16d\sqrt{c+dx}}{63(a+bx)^{7/2}(bc-ad)^2} - \frac{2\sqrt{c+dx}}{9(a+bx)}$$

[Out] $-2/9*(d*x+c)^{(1/2)/(-a*d+b*c)/(b*x+a)^{(9/2)+16/63*d*(d*x+c)^{(1/2)/(-a*d+b*c)}$
 $)^2/(b*x+a)^{(7/2)-32/105*d^2*(d*x+c)^{(1/2)/(-a*d+b*c)^3/(b*x+a)^{(5/2)+128/3}$
 $15*d^3*(d*x+c)^{(1/2)/(-a*d+b*c)^4/(b*x+a)^{(3/2)-256/315*d^4*(d*x+c)^{(1/2)/(-}$
 $-a*d+b*c)^5/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 171, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{256d^4\sqrt{c+dx}}{315\sqrt{a+bx}(bc-ad)^5} + \frac{128d^3\sqrt{c+dx}}{315(a+bx)^{3/2}(bc-ad)^4} - \frac{32d^2\sqrt{c+dx}}{105(a+bx)^{5/2}(bc-ad)^3} + \frac{16d\sqrt{c+dx}}{63(a+bx)^{7/2}(bc-ad)^2} - \frac{2\sqrt{c+dx}}{9(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(11/2)*Sqrt[c + d*x]), x]

[Out] $(-2*\text{Sqrt}[c + d*x])/((9*(b*c - a*d)*(a + b*x)^{(9/2)} + (16*d*\text{Sqrt}[c + d*x])/(($
 $63*(b*c - a*d)^2*(a + b*x)^{(7/2)} - (32*d^2*\text{Sqrt}[c + d*x])/((105*(b*c - a*d)$
 $^3*(a + b*x)^{(5/2)} + (128*d^3*\text{Sqrt}[c + d*x])/((315*(b*c - a*d)^4*(a + b*x)^$
 $(3/2)) - (256*d^4*\text{Sqrt}[c + d*x])/((315*(b*c - a*d)^5*\text{Sqrt}[a + b*x]))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp
 $[((a + b*x)^{(m + 1)*(c + d*x)^{(n + 1)}}/((b*c - a*d)*(m + 1)), x] /;$ FreeQ[{
 $a, b, c, d, m, n\}, x]$ && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
 1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 $((a + b*x)^{(m + 1)*(c + d*x)^{(n + 1)}}/((b*c - a*d)*(m + 1)), x] - \text{Dist}[(d*\text{S}$
 $\text{implify}[m + n + 2])/((b*c - a*d)*(m + 1)), \text{Int}[(a + b*x)^{\text{Simplify}[m + 1]}*(c$
 $+ d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
 $\text{LtQ}[\text{Simplify}[m + n + 2], 0] \&\& \text{NeQ}[m, -1] \&\& !(\text{LtQ}[m, -1] \&\& \text{LtQ}[n, -1] \&\&$
 $(\text{EqQ}[a, 0] \|\| (\text{NeQ}[c, 0] \&\& \text{LtQ}[m - n, 0] \&\& \text{IntegerQ}[n]))) \&\& (\text{SumSimpler}$
 $\text{Q}[m, 1] \|\| !\text{SumSimplerQ}[n, 1])$

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{11/2}\sqrt{c+dx}} dx &= -\frac{2\sqrt{c+dx}}{9(bc-ad)(a+bx)^{9/2}} - \frac{(8d) \int \frac{1}{(a+bx)^{9/2}\sqrt{c+dx}} dx}{9(bc-ad)} \\
&= -\frac{2\sqrt{c+dx}}{9(bc-ad)(a+bx)^{9/2}} + \frac{16d\sqrt{c+dx}}{63(bc-ad)^2(a+bx)^{7/2}} + \frac{(16d^2) \int \frac{1}{(a+bx)^{7/2}\sqrt{c+dx}} dx}{21(bc-ad)^2} \\
&= -\frac{2\sqrt{c+dx}}{9(bc-ad)(a+bx)^{9/2}} + \frac{16d\sqrt{c+dx}}{63(bc-ad)^2(a+bx)^{7/2}} - \frac{32d^2\sqrt{c+dx}}{105(bc-ad)^3(a+bx)^{5/2}} - \frac{(64d^3) \int \frac{1}{(a+bx)^{5/2}\sqrt{c+dx}} dx}{315(bc-ad)^4} \\
&= -\frac{2\sqrt{c+dx}}{9(bc-ad)(a+bx)^{9/2}} + \frac{16d\sqrt{c+dx}}{63(bc-ad)^2(a+bx)^{7/2}} - \frac{32d^2\sqrt{c+dx}}{105(bc-ad)^3(a+bx)^{5/2}} + \frac{315(64d^3) \int \frac{1}{(a+bx)^{3/2}\sqrt{c+dx}} dx}{315(bc-ad)^4} \\
&= -\frac{2\sqrt{c+dx}}{9(bc-ad)(a+bx)^{9/2}} + \frac{16d\sqrt{c+dx}}{63(bc-ad)^2(a+bx)^{7/2}} - \frac{32d^2\sqrt{c+dx}}{105(bc-ad)^3(a+bx)^{5/2}} + \frac{315(64d^3) \int \frac{1}{(a+bx)^{1/2}\sqrt{c+dx}} dx}{315(bc-ad)^4}
\end{aligned}$$

Mathematica [A] time = 0.07, size = 168, normalized size = 0.98

$$\frac{2\sqrt{c+dx} (315a^4d^4 - 420a^3bd^3(c-2dx) + 126a^2b^2d^2(3c^2 - 4cdx + 8d^2x^2) + 36ab^3d(-5c^3 + 6c^2dx - 8cd^2x^2 + 3d^3x^3) + b^4(35c^4 - 40c^3dx + 48c^2d^2x^2 - 64cd^3x^3 + 128d^4x^4))}{315(a+bx)^{9/2}(bc-ad)^5}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a+b*x)^(11/2)*Sqrt[c+d*x]),x]

[Out] (-2*Sqrt[c+d*x]*(315*a^4*d^4 - 420*a^3*b*d^3*(c-2*d*x) + 126*a^2*b^2*d^2*2*(3*c^2 - 4*c*d*x + 8*d^2*x^2) + 36*a*b^3*d*(-5*c^3 + 6*c^2*d*x - 8*c*d^2*x^2 + 16*d^3*x^3) + b^4*(35*c^4 - 40*c^3*d*x + 48*c^2*d^2*x^2 - 64*c*d^3*x^3 + 128*d^4*x^4)))/(315*(b*c - a*d)^5*(a + b*x)^(9/2))

fricas [B] time = 4.00, size = 638, normalized size = 3.73

$$\frac{315(a^5b^5c^5 - 5a^6b^4c^4d + 10a^7b^3c^3d^2 - 10a^8b^2c^2d^3 + 5a^9bcd^4 - a^{10}d^5 + (b^{10}c^5 - 5ab^9c^4d + 10a^2b^8c^3d^2 - 10a^3b^7c^2d^3 + 5a^4b^6c^2d^4 - 5a^5b^5c^2d^5 + 5a^6b^4c^2d^6 - 5a^7b^3c^2d^7 + 5a^8b^2c^2d^8 - 5a^9b^2c^2d^9 + 5a^{10}c^2d^{10}))}{315(a+bx)^{9/2}(bc-ad)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/2)/(d*x+c)^(1/2),x, algorithm="fricas")

[Out] -2/315*(128*b^4*d^4*x^4 + 35*b^4*c^4 - 180*a*b^3*c^3*d + 378*a^2*b^2*c^2*d^2 - 420*a^3*b*c*d^3 + 315*a^4*d^4 - 64*(b^4*c*d^3 - 9*a*b^3*d^4)*x^3 + 48*(

$$\begin{aligned} & b^4c^2d^2 - 6ab^3cd^3 + 21a^2b^2d^4)x^2 - 8(5b^4c^3d - 27ab^3c^2d^2 + 63a^2b^2cd^3 - 105a^3bd^4)x) \sqrt{bx+a} \sqrt{dx+c} \\ & / (a^5b^5c^5 - 5a^6b^4c^4d + 10a^7b^3c^3d^2 - 10a^8b^2c^2d^3 + 5a^9b^1c^1d^4 - a^{10}d^5 + (b^{10}c^5 - 5a^9b^4c^4d + 10a^8b^3c^3d^2 - 10a^7b^2c^2d^3 + 5a^6b^1c^1d^4 - a^5b^0d^5)x^5 \\ & + 5(a^9b^4c^5 - 5a^8b^3c^4d + 10a^7b^2c^3d^2 - 10a^6b^1c^2d^3 + 5a^5b^0c^1d^4 - a^4b^0c^0d^5)x^4 + 10(a^8b^3c^5 - 5a^7b^2c^4d + 10a^6b^1c^3d^2 - 10a^5b^0c^2d^3 + 5a^4b^0c^1d^4 - a^3b^0c^0d^5)x^3 \\ & + 10(a^7b^2c^5 - 5a^6b^1c^4d + 10a^5b^0c^3d^2 - 10a^4b^0c^2d^3 + 5a^3b^0c^1d^4 - a^2b^0c^0d^5)x^2 + 5(a^6b^1c^5 - 5a^5b^0c^4d + 10a^4b^0c^3d^2 - 10a^3b^0c^2d^3 + 5a^2b^0c^1d^4 - a^1b^0c^0d^5)x) \end{aligned}$$

giac [B] time = 1.57, size = 596, normalized size = 3.49

$$\frac{512 \left(b^8c^4 - 4ab^7c^3d + 6a^2b^6c^2d^2 - 4a^3b^5cd^3 + a^4b^4d^4 - 9 \left(\sqrt{bd} \sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd} \right)^2 b^6c^3 + \dots \right)}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/2)/(d*x+c)^(1/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & -512/315(b^8c^4 - 4a^2b^6c^2d^2 - 4a^3b^5cd^3 + a^4b^4d^4 - 9(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4} \\ & - 9(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^2 b^6c^3 + 27(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4} \\ & - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^2 a^2 b^4 c^2 d - 27(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4} \\ & - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^2 a^2 b^4 c^2 d^2 + 9(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4} \\ & - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^2 a^3 b^3 d^3 + 36(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4} \\ & - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^4 b^4 c^2 - 72(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4} \\ & - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^4 a^2 b^3 c^2 d + 36(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4} \\ & - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^4 a^2 b^2 d^2 - 84(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4} \\ & - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^6 b^2 c + 84(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4} \\ & - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^6 a^2 b^2 d^2 + 126(\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4} \\ & - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^8) \sqrt{bd} b^5 d^4 / ((b^2c - a^2b^4d^4 - (\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2b^4d^4})^2)^9 \text{abs}(b) \end{aligned}$$

maple [A] time = 0.01, size = 256, normalized size = 1.50

$$\frac{2\sqrt{dx+c} (128b^4x^4d^4 + 576ab^3d^4x^3 - 64b^4cd^3x^3 + 1008a^2b^2d^4x^2 - 288ab^3cd^3x^2 + 48b^4c^2d^2x^2 + 840a^3bd^4x - \dots)}{315(bx+a)^{\frac{9}{2}} (a^5d^5 - 5a^4bcd^4 + 10a^3b^2c^2d^3 - \dots)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(11/2)/(d*x+c)^(1/2),x)`

[Out] $2/315*(d*x+c)^(1/2)*(128*b^4*d^4*x^4+576*a*b^3*d^4*x^3-64*b^4*c*d^3*x^3+1008*a^2*b^2*d^4*x^2-288*a*b^3*c*d^3*x^2+48*b^4*c^2*d^2*x^2+840*a^3*b*d^4*x-504*a^2*b^2*c*d^3*x+216*a*b^3*c^2*d^2*x-40*b^4*c^3*d*x+315*a^4*d^4-420*a^3*b*c*d^3+378*a^2*b^2*c^2*d^2-180*a*b^3*c^3*d+35*b^4*c^4)/(b*x+a)^(9/2)/(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(11/2)/(d*x+c)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.37, size = 303, normalized size = 1.77

$$\frac{\sqrt{c+dx} \left(\frac{256d^4x^4}{315(ad-bc)^5} + \frac{630a^4d^4-840a^3bcd^3+756a^2b^2c^2d^2-360ab^3c^3d+70b^4c^4}{315b^4(ad-bc)^5} + \frac{x(1680a^3bd^4-1008a^2b^2cd^3+432ab^3c^2d^2-80b^4c^4)}{315b^4(ad-bc)^5} \right)}{x^4\sqrt{a+bx} + \frac{a^4\sqrt{a+bx}}{b^4} + \frac{6a^2x^2\sqrt{a+bx}}{b^2} + \frac{4ax^3\sqrt{a+bx}}{b} + \frac{4a^3x\sqrt{a+bx}}{b^3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a+b*x)^(11/2)*(c+d*x)^(1/2)),x)`

[Out] $((c+d*x)^(1/2)*((256*d^4*x^4)/(315*(a*d-b*c)^5) + (630*a^4*d^4 + 70*b^4*c^4 + 756*a^2*b^2*c^2*d^2 - 360*a*b^3*c^3*d - 840*a^3*b*c*d^3)/(315*b^4*(a*d-b*c)^5) + (x*(1680*a^3*b*d^4 - 80*b^4*c^3*d + 432*a*b^3*c^2*d^2 - 1008*a^2*b^2*c*d^3))/(315*b^4*(a*d-b*c)^5) + (128*d^3*x^3*(9*a*d-b*c))/(315*b*(a*d-b*c)^5) + (32*d^2*x^2*(21*a^2*d^2 + b^2*c^2 - 6*a*b*c*d))/(105*b^2*(a*d-b*c)^5))/((x^4*(a+b*x)^(1/2) + (a^4*(a+b*x)^(1/2))/b^4 + (6*a^2*x^2*(a+b*x)^(1/2))/b^2 + (4*a*x^3*(a+b*x)^(1/2))/b + (4*a^3*x*(a+b*x)^(1/2))/b^3)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(11/2)/(d*x+c)**(1/2),x)
```

```
[Out] Timed out
```

$$3.1502 \quad \int \frac{(a+bx)^{7/2}}{(c+dx)^{3/2}} dx$$

Optimal. Leaf size=174

$$-\frac{35\sqrt{b}(bc-ad)^3 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{8d^{9/2}} + \frac{35b\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}{8d^4} - \frac{35b(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)}{12d^3} + \frac{7b(a+bx)^{5/2}\sqrt{c+dx}}{3d^2}$$

[Out] $-35/8*(-a*d+b*c)^3*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})*b^{(1/2)}/d^{(9/2)}-2*(b*x+a)^{(7/2)}/d/(d*x+c)^{(1/2)}-35/12*b*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/d^3+7/3*b*(b*x+a)^{(5/2)}*(d*x+c)^{(1/2)}/d^2+35/8*b*(-a*d+b*c)^2*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/d^4$

Rubi [A] time = 0.09, antiderivative size = 174, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 217, 206}

$$\frac{7b(a+bx)^{5/2}\sqrt{c+dx}}{3d^2} - \frac{35b(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)}{12d^3} + \frac{35b\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}{8d^4} - \frac{35\sqrt{b}(bc-ad)^3 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{8d^{9/2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/2)/(c + d*x)^(3/2), x]

[Out] $(-2*(a + b*x)^{(7/2)})/(d*\operatorname{Sqrt}[c + d*x]) + (35*b*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(8*d^4) - (35*b*(b*c - a*d)*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(12*d^3) + (7*b*(a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x])/(3*d^2) - (35*\operatorname{Sqrt}[b]*(b*c - a*d)^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/(8*d^{(9/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,

```
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && ( !IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/2}}{(c+dx)^{3/2}} dx &= -\frac{2(a+bx)^{7/2}}{d\sqrt{c+dx}} + \frac{(7b) \int \frac{(a+bx)^{5/2}}{\sqrt{c+dx}} dx}{d} \\
&= -\frac{2(a+bx)^{7/2}}{d\sqrt{c+dx}} + \frac{7b(a+bx)^{5/2}\sqrt{c+dx}}{3d^2} - \frac{(35b(bc-ad)) \int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx}{6d^2} \\
&= -\frac{2(a+bx)^{7/2}}{d\sqrt{c+dx}} - \frac{35b(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{12d^3} + \frac{7b(a+bx)^{5/2}\sqrt{c+dx}}{3d^2} + \frac{(35b(bc-ad)^2)}{8d^3} \int \frac{(a+bx)^{1/2}}{\sqrt{c+dx}} dx \\
&= -\frac{2(a+bx)^{7/2}}{d\sqrt{c+dx}} + \frac{35b(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^4} - \frac{35b(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{12d^3} + \frac{7b(a+bx)^{5/2}\sqrt{c+dx}}{3d^2} \\
&= -\frac{2(a+bx)^{7/2}}{d\sqrt{c+dx}} + \frac{35b(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^4} - \frac{35b(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{12d^3} + \frac{7b(a+bx)^{5/2}\sqrt{c+dx}}{3d^2} \\
&= -\frac{2(a+bx)^{7/2}}{d\sqrt{c+dx}} + \frac{35b(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^4} - \frac{35b(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{12d^3} + \frac{7b(a+bx)^{5/2}\sqrt{c+dx}}{3d^2} \\
&= -\frac{2(a+bx)^{7/2}}{d\sqrt{c+dx}} + \frac{35b(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^4} - \frac{35b(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{12d^3} + \frac{7b(a+bx)^{5/2}\sqrt{c+dx}}{3d^2}
\end{aligned}$$

Mathematica [C] time = 0.07, size = 73, normalized size = 0.42

$$\frac{2(a+bx)^{9/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/2} {}_2F_1 \left(\frac{3}{2}, \frac{9}{2}; \frac{11}{2}; \frac{d(a+bx)}{ad-bc} \right)}{9b(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/2)/(c + d*x)^(3/2), x]

[Out] (2*(a + b*x)^(9/2)*((b*(c + d*x))/(b*c - a*d))^(3/2)*Hypergeometric2F1[3/2, 9/2, 11/2, (d*(a + b*x))/(-b*c + a*d)])/(9*b*(c + d*x)^(3/2))

fricas [B] time = 0.75, size = 603, normalized size = 3.47

$$\frac{105 \left(b^3 c^4 - 3 a b^2 c^3 d + 3 a^2 b c^2 d^2 - a^3 c d^3 + (b^3 c^3 d - 3 a b^2 c^2 d^2 + 3 a^2 b c d^3 - a^3 d^4) x \right) \sqrt{\frac{b}{d}} \log \left(8 b^2 d^2 x^2 + b^2 c^2 \right)}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(3/2),x, algorithm="fricas")

[Out]
$$\begin{aligned} & [-1/96*(105*(b^3*c^4 - 3*a*b^2*c^3*d + 3*a^2*b*c^2*d^2 - a^3*c*d^3 + (b^3*c^3*d - 3*a*b^2*c^2*d^2 + 3*a^2*b*c*d^3 - a^3*d^4)*x)*\sqrt{b/d}*\log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d^2*x + b*c*d + a*d^2)*\sqrt{(b*x + a)*\sqrt{d*x + c}*\sqrt{b/d}} + 8*(b^2*c*d + a*b*d^2)*x) - 4*(8*b^3*d^3*x^3 + 105*b^3*c^3 - 280*a*b^2*c^2*d + 231*a^2*b*c*d^2 - 48*a^3*d^3 - 2*(7*b^3*c*d^2 - 19*a*b^2*d^3)*x^2 + (35*b^3*c^2*d - 98*a*b^2*c*d^2 + 87*a^2*b*d^3)*x)*\sqrt{(b*x + a)*\sqrt{d*x + c}})/(d^5*x + c*d^4), \\ & 1/48*(105*(b^3*c^4 - 3*a*b^2*c^3*d + 3*a^2*b*c^2*d^2 - a^3*c*d^3 + (b^3*c^3*d - 3*a*b^2*c^2*d^2 + 3*a^2*b*c*d^3 - a^3*d^4)*x)*\sqrt{-b/d}*\arctan(1/2*(2*b*d*x + b*c + a*d)*\sqrt{(b*x + a)*\sqrt{d*x + c}*\sqrt{-b/d}}/(b^2*d*x^2 + a*b*c + (b^2*c + a*b*d)*x) + 2*(8*b^3*d^3*x^3 + 105*b^3*c^3 - 280*a*b^2*c^2*d + 231*a^2*b*c*d^2 - 48*a^3*d^3 - 2*(7*b^3*c*d^2 - 19*a*b^2*d^3)*x^2 + (35*b^3*c^2*d - 98*a*b^2*c*d^2 + 87*a^2*b*d^3)*x)*\sqrt{(b*x + a)*\sqrt{d*x + c}})/(d^5*x + c*d^4)] \end{aligned}$$

giac [B] time = 1.38, size = 279, normalized size = 1.60

$$\frac{\left((bx + a) \left(2(bx + a) \left(\frac{4(bx+a)b^2}{d|b|} - \frac{7(b^3cd^5 - ab^2d^6)}{d^7|b|} \right) + \frac{35(b^4c^2d^4 - 2ab^3cd^5 + a^2b^2d^6)}{d^7|b|} \right) + \frac{105(b^5c^3d^3 - 3ab^4c^2d^4 + 3a^2b^3cd^5 - a^3b^2d^6)}{d^7|b|} \right) \sqrt{b}}{24 \sqrt{b^2c + (bx + a)bd - abd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(3/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & 1/24*((b*x + a)*(2*(b*x + a)*(4*(b*x + a)*b^2/(d*abs(b)) - 7*(b^3*c*d^5 - a*b^2*d^6)/(d^7*abs(b))) + 35*(b^4*c^2*d^4 - 2*a*b^3*c*d^5 + a^2*b^2*d^6)/(d^7*abs(b))) + 105*(b^5*c^3*d^3 - 3*a*b^4*c^2*d^4 + 3*a^2*b^3*c*d^5 - a^3*b^2*d^6)/(d^7*abs(b))*\sqrt{(b*x + a)}/\sqrt{(b^2*c + (b*x + a)*b*d - a*b*d)} + 35/8*(b^5*c^3 - 3*a*b^4*c^2*d + 3*a^2*b^3*c*d^2 - a^3*b^2*d^3)*\log(abs(-\sqrt{(b*d)*\sqrt{(b*x + a) + \sqrt{(b^2*c + (b*x + a)*b*d - a*b*d)}}})))/(\sqrt{(b*d)}*d^4*abs(b)) \end{aligned}$$

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{2}}}{(dx + c)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/2)/(d*x+c)^(3/2),x)

[Out] int((b*x+a)^(7/2)/(d*x+c)^(3/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{7}{2}}}{(c + dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/2)/(c + d*x)^(3/2),x)

[Out] int((a + b*x)^(7/2)/(c + d*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{7}{2}}}{(c + dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/2)/(d*x+c)**(3/2),x)

[Out] Integral((a + b*x)**(7/2)/(c + d*x)**(3/2), x)

$$3.1503 \quad \int \frac{(a+bx)^{5/2}}{(c+dx)^{3/2}} dx$$

Optimal. Leaf size=138

$$\frac{15\sqrt{b}(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{4d^{7/2}} - \frac{15b\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}{4d^3} + \frac{5b(a+bx)^{3/2}\sqrt{c+dx}}{2d^2} - \frac{2(a+bx)^{5/2}}{d\sqrt{c+dx}}$$

[Out] 15/4*(-a*d+b*c)^2*arctanh(d^(1/2)*(b*x+a)^(1/2)/b^(1/2)/(d*x+c)^(1/2))*b^(1/2)/d^(7/2)-2*(b*x+a)^(5/2)/d/(d*x+c)^(1/2)+5/2*b*(b*x+a)^(3/2)*(d*x+c)^(1/2)/d^2-15/4*b*(-a*d+b*c)*(b*x+a)^(1/2)*(d*x+c)^(1/2)/d^3

Rubi [A] time = 0.07, antiderivative size = 138, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 217, 206}

$$\frac{5b(a+bx)^{3/2}\sqrt{c+dx}}{2d^2} - \frac{15b\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}{4d^3} + \frac{15\sqrt{b}(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{4d^{7/2}} - \frac{2(a+bx)^{5/2}}{d\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2)/(c + d*x)^(3/2), x]

[Out] (-2*(a + b*x)^(5/2))/(d*Sqrt[c + d*x]) - (15*b*(b*c - a*d)*Sqrt[a + b*x]*Sqrt[c + d*x])/(4*d^3) + (5*b*(a + b*x)^(3/2)*Sqrt[c + d*x])/(2*d^2) + (15*Sqrt[b]*(b*c - a*d)^2*ArcTanh[(Sqrt[d]*Sqrt[a + b*x])/(Sqrt[b]*Sqrt[c + d*x])])/(4*d^(7/2))

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n

+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_)^(m_))*((c_.) + (d_.)*(x_)^(n_)), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{(c+dx)^{3/2}} dx &= -\frac{2(a+bx)^{5/2}}{d\sqrt{c+dx}} + \frac{(5b) \int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx}{d} \\
&= -\frac{2(a+bx)^{5/2}}{d\sqrt{c+dx}} + \frac{5b(a+bx)^{3/2}\sqrt{c+dx}}{2d^2} - \frac{(15b(bc-ad)) \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{4d^2} \\
&= -\frac{2(a+bx)^{5/2}}{d\sqrt{c+dx}} - \frac{15b(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^3} + \frac{5b(a+bx)^{3/2}\sqrt{c+dx}}{2d^2} + \frac{(15b(bc-ad)^2) \int \frac{1}{\sqrt{c+dx}} dx}{8d^2} \\
&= -\frac{2(a+bx)^{5/2}}{d\sqrt{c+dx}} - \frac{15b(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^3} + \frac{5b(a+bx)^{3/2}\sqrt{c+dx}}{2d^2} + \frac{(15b(bc-ad)^2) \sqrt{c+dx}}{8d^2} \\
&= -\frac{2(a+bx)^{5/2}}{d\sqrt{c+dx}} - \frac{15b(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^3} + \frac{5b(a+bx)^{3/2}\sqrt{c+dx}}{2d^2} + \frac{(15b(bc-ad)^2) \sqrt{c+dx}}{8d^2} \\
&= -\frac{2(a+bx)^{5/2}}{d\sqrt{c+dx}} - \frac{15b(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^3} + \frac{5b(a+bx)^{3/2}\sqrt{c+dx}}{2d^2} + \frac{15\sqrt{b}(bc-ad)^2 \sqrt{c+dx}}{4d^2}
\end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.53

$$\frac{2(a+bx)^{7/2} \left(\frac{b(c+dx)}{bc-ad}\right)^{3/2} {}_2F_1\left(\frac{3}{2}, \frac{7}{2}; \frac{9}{2}; \frac{d(a+bx)}{ad-bc}\right)}{7b(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/(c + d*x)^(3/2), x]

[Out] (2*(a + b*x)^(7/2)*((b*(c + d*x))/(b*c - a*d))^(3/2)*Hypergeometric2F1[3/2, 7/2, 9/2, (d*(a + b*x))/(-b*c + a*d)])/(7*b*(c + d*x)^(3/2))

fricas [A] time = 0.58, size = 441, normalized size = 3.20

$$\left[\frac{15(b^2c^3 - 2abc^2d + a^2cd^2 + (b^2c^2d - 2abcd^2 + a^2d^3)x) \sqrt{\frac{b}{d}} \log\left(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bd^2x + \dots)\right)}{\dots} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(3/2),x, algorithm="fricas")

[Out] [1/16*(15*(b^2*c^3 - 2*a*b*c^2*d + a^2*c*d^2 + (b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3)*x)*sqrt(b/d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d^2*x + b*c*d + a*d^2)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(b/d) + 8*(b^2*c*d + a*b*d^2)*x) + 4*(2*b^2*d^2*x^2 - 15*b^2*c^2 + 25*a*b*c*d - 8*a^2*d^2 - (5*b^2*c*d - 9*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(d^4*x + c*d^3), -1/8*(15*(b^2*c^3 - 2*a*b*c^2*d + a^2*c*d^2 + (b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3)*x)*sqrt(-b/d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-b/d)/(b^2*d*x^2 + a*b*c + (b^2*c + a*b*d)*x)) - 2*(2*b^2*d^2*x^2 - 15*b^2*c^2 + 25*a*b*c*d - 8*a^2*d^2 - (5*b^2*c*d - 9*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(d^4*x + c*d^3)]

giac [A] time = 1.26, size = 201, normalized size = 1.46

$$\frac{\sqrt{bx+a} \left((bx+a) \left(\frac{2(bx+a)b^2}{d|b|} - \frac{5(b^3cd^3-ab^2d^4)}{d^5|b|} \right) - \frac{15(b^4c^2d^2-2ab^3cd^3+a^2b^2d^4)}{d^5|b|} \right)}{4\sqrt{b^2c+(bx+a)bd-abd}} - \frac{15(b^4c^2-2ab^3cd+a^2b^2d^2) \log\left(\left|-\sqrt{bd}\right|\right)}{4\sqrt{bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(3/2),x, algorithm="giac")

[Out] 1/4*sqrt(b*x + a)*((b*x + a)*(2*(b*x + a)*b^2/(d*abs(b)) - 5*(b^3*c*d^3 - a*b^2*d^4)/(d^5*abs(b))) - 15*(b^4*c^2*d^2 - 2*a*b^3*c*d^3 + a^2*b^2*d^4)/(d^5*abs(b)))/sqrt(b^2*c + (b*x + a)*b*d - a*b*d) - 15/4*(b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/(sqrt(b*d)*d^3*abs(b))

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{2}}}{(dx+c)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/(d*x+c)^(3/2),x)

[Out] int((b*x+a)^(5/2)/(d*x+c)^(3/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{5/2}}{(c + dx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)/(c + d*x)^(3/2), x)

[Out] int((a + b*x)^(5/2)/(c + d*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{2}}}{(c + dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)/(d*x+c)**(3/2), x)

[Out] Integral((a + b*x)**(5/2)/(c + d*x)**(3/2), x)

$$3.1504 \quad \int \frac{(a+bx)^{3/2}}{(c+dx)^{3/2}} dx$$

Optimal. Leaf size=98

$$-\frac{3\sqrt{b}(bc-ad)\tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{5/2}} + \frac{3b\sqrt{a+bx}\sqrt{c+dx}}{d^2} - \frac{2(a+bx)^{3/2}}{d\sqrt{c+dx}}$$

[Out] $-3*(-a*d+b*c)*\operatorname{arctanh}(d^{1/2}*(b*x+a)^{1/2}/b^{1/2}/(d*x+c)^{1/2})*b^{1/2}/d^{5/2}-2*(b*x+a)^{3/2}/d/(d*x+c)^{1/2}+3*b*(b*x+a)^{1/2}*(d*x+c)^{1/2}/d^2$

Rubi [A] time = 0.05, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 217, 206}

$$\frac{3b\sqrt{a+bx}\sqrt{c+dx}}{d^2} - \frac{3\sqrt{b}(bc-ad)\tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{5/2}} - \frac{2(a+bx)^{3/2}}{d\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{3/2}/(c + d*x)^{3/2}, x]$

[Out] $(-2*(a + b*x)^{3/2})/(d*\operatorname{Sqrt}[c + d*x]) + (3*b*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/d^2 - (3*\operatorname{Sqrt}[b]*(b*c - a*d)*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/d^{5/2}$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(IntegerQ[n] \&\& !IntegerQ[m]) \&\& !(IntegerQ[m + n + 2, 0] \&\& (FractionQ[m] || GeQ[2*n + m + 1, 0])) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{NeQ}[m + n + 1, 0] \&\& !(IntegerQ[m, 0] \&\& (!IntegerQ[n] || (GtQ[m, 0] \&\& LtQ[m - n, 0]))) \&\& !IntegerQ[m + n + 2, 0] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{(c+dx)^{3/2}} dx &= -\frac{2(a+bx)^{3/2}}{d\sqrt{c+dx}} + \frac{(3b) \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{d} \\
&= -\frac{2(a+bx)^{3/2}}{d\sqrt{c+dx}} + \frac{3b\sqrt{a+bx}\sqrt{c+dx}}{d^2} - \frac{(3b(bc-ad)) \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{2d^2} \\
&= -\frac{2(a+bx)^{3/2}}{d\sqrt{c+dx}} + \frac{3b\sqrt{a+bx}\sqrt{c+dx}}{d^2} - \frac{(3(bc-ad)) \operatorname{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \sqrt{a+bx}\right)}{d^2} \\
&= -\frac{2(a+bx)^{3/2}}{d\sqrt{c+dx}} + \frac{3b\sqrt{a+bx}\sqrt{c+dx}}{d^2} - \frac{(3(bc-ad)) \operatorname{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}}\right)}{d^2} \\
&= -\frac{2(a+bx)^{3/2}}{d\sqrt{c+dx}} + \frac{3b\sqrt{a+bx}\sqrt{c+dx}}{d^2} - \frac{3\sqrt{b}(bc-ad) \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{5/2}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.74

$$\frac{2(a + bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/2} {}_2F_1 \left(\frac{3}{2}, \frac{5}{2}, \frac{7}{2}; \frac{d(a+bx)}{ad-bc} \right)}{5b(c + dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(3/2), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(3/2)*Hypergeometric2F1[3/2, 5/2, 7/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(c + d*x)^(3/2))

fricas [A] time = 0.53, size = 311, normalized size = 3.17

$$\left[\frac{3(bc^2 - acd + (bcd - ad^2)x) \sqrt{\frac{b}{d}} \log \left(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bd^2x + bcd + ad^2) \sqrt{bx + a} \sqrt{dx + c} \right)}{4(d^3x + cd^2)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(3/2), x, algorithm="fricas")

[Out] [-1/4*(3*(b*c^2 - a*c*d + (b*c*d - a*d^2)*x)*sqrt(b/d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d^2*x + b*c*d + a*d^2)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(b/d) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(b*d*x + 3*b*c - 2*a*d)*sqrt(b*x + a)*sqrt(d*x + c))/(d^3*x + c*d^2), 1/2*(3*(b*c^2 - a*c*d + (b*c*d - a*d^2)*x)*sqrt(-b/d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-b/d)/(b^2*d*x^2 + a*b*c + (b^2*c + a*b*d)*x)) + 2*(b*d*x + 3*b*c - 2*a*d)*sqrt(b*x + a)*sqrt(d*x + c))/(d^3*x + c*d^2)]

giac [A] time = 1.27, size = 137, normalized size = 1.40

$$\frac{\sqrt{bx + a} \left(\frac{(bx+a)b^2}{d|b|} + \frac{3(b^3cd - ab^2d^2)}{d^3|b|} \right)}{\sqrt{b^2c + (bx + a)bd - abd}} + \frac{3(b^3c - ab^2d) \log \left(\left| -\sqrt{bd} \sqrt{bx + a} + \sqrt{b^2c + (bx + a)bd - abd} \right| \right)}{\sqrt{bd} d^2 |b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(3/2), x, algorithm="giac")

[Out] sqrt(b*x + a)*((b*x + a)*b^2/(d*abs(b)) + 3*(b^3*c*d - a*b^2*d^2)/(d^3*abs(b)))/sqrt(b^2*c + (b*x + a)*b*d - a*b*d) + 3*(b^3*c - a*b^2*d)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/(sqrt(b*d)*d^2*abs(b))

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(3/2),x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(3/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a+bx)^{\frac{3}{2}}}{(c+dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*x)^(3/2)/(c+d*x)^(3/2),x)

[Out] int((a+b*x)^(3/2)/(c+d*x)^(3/2),x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a+bx)^{\frac{3}{2}}}{(c+dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/(d*x+c)**(3/2),x)

[Out] Integral((a+b*x)**(3/2)/(c+d*x)**(3/2),x)

$$3.1505 \quad \int \frac{\sqrt{a+bx}}{(c+dx)^{3/2}} dx$$

Optimal. Leaf size=66

$$\frac{2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{3/2}} - \frac{2\sqrt{a+bx}}{d\sqrt{c+dx}}$$

[Out] $2*\operatorname{arctanh}(d^{1/2}*(b*x+a)^{1/2}/b^{1/2}/(d*x+c)^{1/2})*b^{1/2}/d^{3/2}-2*(b*x+a)^{1/2}/d/(d*x+c)^{1/2}$

Rubi [A] time = 0.03, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 63, 217, 206}

$$\frac{2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{3/2}} - \frac{2\sqrt{a+bx}}{d\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/(c + d*x)^(3/2), x]

[Out] $(-2*\operatorname{Sqrt}[a + b*x]/(d*\operatorname{Sqrt}[c + d*x]) + (2*\operatorname{Sqrt}[b]*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/d^{3/2}$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{a+bx}}{(c+dx)^{3/2}} dx &= -\frac{2\sqrt{a+bx}}{d\sqrt{c+dx}} + \frac{b \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{d} \\ &= -\frac{2\sqrt{a+bx}}{d\sqrt{c+dx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \sqrt{a+bx}\right)}{d} \\ &= -\frac{2\sqrt{a+bx}}{d\sqrt{c+dx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}}\right)}{d} \\ &= -\frac{2\sqrt{a+bx}}{d\sqrt{c+dx}} + \frac{2\sqrt{b} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{3/2}} \end{aligned}$$

Mathematica [A] time = 0.35, size = 95, normalized size = 1.44

$$\frac{2\sqrt{bc-ad} \sqrt{\frac{b(c+dx)}{bc-ad}} \sinh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{bc-ad}}\right) - 2\sqrt{d}\sqrt{a+bx}}{d^{3/2}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(3/2), x]
```

```
[Out] (-2*Sqrt[d]*Sqrt[a + b*x] + 2*Sqrt[b*c - a*d]*Sqrt[(b*(c + d*x))/(b*c - a*d
) ]*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(d^(3/2)*Sqrt[c + d*x]
)
```

fricas [B] time = 0.50, size = 241, normalized size = 3.65

$$\left[\frac{(dx + c)\sqrt{\frac{b}{d}} \log\left(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bd^2x + bcd + ad^2)\sqrt{bx + a}\sqrt{dx + c}\sqrt{\frac{b}{d}} + 8(b^2cd + abd)\right)}{2(d^2x + cd)} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(3/2),x, algorithm="fricas")

[Out] [1/2*((d*x + c)*sqrt(b/d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d^2*x + b*c*d + a*d^2)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(b/d) + 8*(b^2*c*d + a*b*d^2)*x) - 4*sqrt(b*x + a)*sqrt(d*x + c))/(d^2*x + c*d), -((d*x + c)*sqrt(-b/d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-b/d)/(b^2*d*x^2 + a*b*c + (b^2*c + a*b*d)*x)) + 2*sqrt(b*x + a)*sqrt(d*x + c))/(d^2*x + c*d)]

giac [A] time = 1.22, size = 96, normalized size = 1.45

$$-\frac{2b^2 \log\left(\left|-\sqrt{bd}\sqrt{bx+a} + \sqrt{b^2c+(bx+a)bd-abd}\right|\right)}{\sqrt{bd}d|b|} - \frac{2\sqrt{bx+a}b^2}{\sqrt{b^2c+(bx+a)bd-abd}d|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(3/2),x, algorithm="giac")

[Out] -2*b^2*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/(sqrt(b*d)*d*abs(b)) - 2*sqrt(b*x + a)*b^2/(sqrt(b^2*c + (b*x + a)*b*d - a*b*d)*d*abs(b))

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(3/2),x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(3/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)/(d*x+c)^(3/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/2)/(c + d*x)^(3/2), x)`

[Out] `int((a + b*x)^(1/2)/(c + d*x)^(3/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/2)/(d*x+c)**(3/2),x)`

[Out] `Integral(sqrt(a + b*x)/(c + d*x)**(3/2), x)`

$$3.1506 \quad \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/2}} dx$$

Optimal. Leaf size=30

$$\frac{2\sqrt{a+bx}}{\sqrt{c+dx}(bc-ad)}$$

[Out] $2*(b*x+a)^{(1/2)/(-a*d+b*c)/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{2\sqrt{a+bx}}{\sqrt{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(3/2)),x]

[Out] (2*Sqrt[a + b*x])/((b*c - a*d)*Sqrt[c + d*x])

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{3/2}} dx = \frac{2\sqrt{a+bx}}{(bc-ad)\sqrt{c+dx}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$\frac{2\sqrt{a+bx}}{\sqrt{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(3/2)),x]

[Out] $(2\sqrt{a + bx})/((b*c - a*d)*\sqrt{c + dx})$

fricas [A] time = 0.47, size = 42, normalized size = 1.40

$$\frac{2\sqrt{bx+a}\sqrt{dx+c}}{bc^2 - acd + (bcd - ad^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(1/2)/(d*x+c)^(3/2),x, algorithm="fricas")`

[Out] $2*\sqrt{b*x + a}*\sqrt{d*x + c}/(b*c^2 - a*c*d + (b*c*d - a*d^2)*x)$

giac [A] time = 1.04, size = 47, normalized size = 1.57

$$\frac{2\sqrt{bx+a}b^2}{\sqrt{b^2c + (bx+a)bd - abd}(bc|b| - ad|b|)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(1/2)/(d*x+c)^(3/2),x, algorithm="giac")`

[Out] $2*\sqrt{b*x + a}*b^2/(\sqrt{b^2*c + (b*x + a)*b*d - a*b*d}*(b*c*\text{abs}(b) - a*d*\text{abs}(b)))$

maple [A] time = 0.00, size = 27, normalized size = 0.90

$$\frac{2\sqrt{bx+a}}{\sqrt{dx+c}(ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(1/2)/(d*x+c)^(3/2),x)`

[Out] $-2*(b*x+a)^(1/2)/(d*x+c)^(1/2)/(a*d-b*c)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(1/2)/(d*x+c)^(3/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* h

elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c zero or nonzero?

mupad [B] time = 0.74, size = 26, normalized size = 0.87

$$-\frac{2\sqrt{a+bx}}{(ad-bc)\sqrt{c+dx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/2)*(c + d*x)^(3/2)), x)

[Out] -(2*(a + b*x)^(1/2))/((a*d - b*c)*(c + d*x)^(1/2))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a+bx} (c+dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/2)/(d*x+c)**(3/2), x)

[Out] Integral(1/(sqrt(a + b*x)*(c + d*x)**(3/2)), x)

$$3.1507 \quad \int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/2}} dx$$

Optimal. Leaf size=62

$$-\frac{4d\sqrt{a+bx}}{\sqrt{c+dx}(bc-ad)^2} - \frac{2}{\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}$$

[Out] $-2/(-a*d+b*c)/(b*x+a)^{(1/2)}/(d*x+c)^{(1/2)}-4*d*(b*x+a)^{(1/2)/(-a*d+b*c)^2/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 62, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{4d\sqrt{a+bx}}{\sqrt{c+dx}(bc-ad)^2} - \frac{2}{\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/2)*(c + d*x)^(3/2)), x]

[Out] $-2/((b*c - a*d)*\text{Sqrt}[a + b*x]*\text{Sqrt}[c + d*x]) - (4*d*\text{Sqrt}[a + b*x])/((b*c - a*d)^2*\text{Sqrt}[c + d*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/2}} dx = -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt{c+dx}} - \frac{(2d) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/2}} dx}{bc-ad}$$

$$= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt{c+dx}} - \frac{4d\sqrt{a+bx}}{(bc-ad)^2\sqrt{c+dx}}$$

Mathematica [A] time = 0.02, size = 42, normalized size = 0.68

$$-\frac{2(ad + b(c + 2dx))}{\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(3/2)), x]

[Out] (-2*(a*d + b*(c + 2*d*x)))/((b*c - a*d)^2*Sqrt[a + b*x]*Sqrt[c + d*x])

fricas [B] time = 0.50, size = 125, normalized size = 2.02

$$-\frac{2(2bdx + bc + ad)\sqrt{bx+a}\sqrt{dx+c}}{ab^2c^3 - 2a^2bc^2d + a^3cd^2 + (b^3c^2d - 2ab^2cd^2 + a^2bd^3)x^2 + (b^3c^3 - ab^2c^2d - a^2bcd^2 + a^3d^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(3/2), x, algorithm="fricas")

[Out] -2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)/(a*b^2*c^3 - 2*a^2*b*c^2*d + a^3*c*d^2 + (b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*x^2 + (b^3*c^3 - a*b^2*c^2*d - a^2*b*c*d^2 + a^3*d^3)*x)

giac [B] time = 1.22, size = 142, normalized size = 2.29

$$-\frac{2\sqrt{bx+a}b^2d}{(b^2c^2|b| - 2abcd|b| + a^2d^2|b|)\sqrt{b^2c + (bx+a)bd - abd}} - \frac{4\sqrt{bd}b^2}{(b^2c - abd - (\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(3/2), x, algorithm="giac")

[Out] -2*sqrt(b*x + a)*b^2*d/((b^2*c^2*abs(b) - 2*a*b*c*d*abs(b) + a^2*d^2*abs(b))*sqrt(b^2*c + (b*x + a)*b*d - a*b*d)) - 4*sqrt(b*d)*b^2/((b^2*c - a*b*d -

$(\sqrt{b*d}*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*(b*c*abs(b) - a*d*abs(b))$

maple [A] time = 0.00, size = 52, normalized size = 0.84

$$\frac{2(2bdx + ad + bc)}{\sqrt{bx + a} \sqrt{dx + c} (a^2d^2 - 2abcd + b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(3/2)/(d*x+c)^(3/2),x)`

[Out] `-2*(2*b*d*x+a*d+b*c)/(b*x+a)^(1/2)/(d*x+c)^(1/2)/(a^2*d^2-2*a*b*c*d+b^2*c^2)`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/2)/(d*x+c)^(3/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 0.86, size = 71, normalized size = 1.15

$$\frac{\left(\frac{4bx}{(ad-bc)^2} + \frac{2ad+2bc}{d(ad-bc)^2}\right) \sqrt{c+dx}}{x\sqrt{a+bx} + \frac{c\sqrt{a+bx}}{d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(3/2)*(c + d*x)^(3/2)),x)`

[Out] `-(((4*b*x)/(a*d - b*c)^2 + (2*a*d + 2*b*c)/(d*(a*d - b*c)^2))*(c + d*x)^(1/2))/(x*(a + b*x)^(1/2) + (c*(a + b*x)^(1/2))/d)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} (c + dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(3/2),x)
```

```
[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(3/2)), x)
```

$$3.1508 \quad \int \frac{1}{(a+bx)^{5/2}(c+dx)^{3/2}} dx$$

Optimal. Leaf size=101

$$\frac{16d^2\sqrt{a+bx}}{3\sqrt{c+dx}(bc-ad)^3} + \frac{8d}{3\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2} - \frac{2}{3(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)}$$

[Out] $-2/3/(-a*d+b*c)/(b*x+a)^{(3/2)/(d*x+c)^{(1/2)}+8/3*d/(-a*d+b*c)^2/(b*x+a)^{(1/2)/(d*x+c)^{(1/2)}+16/3*d^2*(b*x+a)^{(1/2)/(-a*d+b*c)^3/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{16d^2\sqrt{a+bx}}{3\sqrt{c+dx}(bc-ad)^3} + \frac{8d}{3\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2} - \frac{2}{3(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*(c + d*x)^(3/2)), x]

[Out] $-2/(3*(b*c - a*d)*(a + b*x)^{(3/2)*\text{Sqrt}[c + d*x]) + (8*d)/(3*(b*c - a*d)^2*\text{Sqrt}[a + b*x]*\text{Sqrt}[c + d*x]) + (16*d^2*\text{Sqrt}[a + b*x])/(3*(b*c - a*d)^3*\text{Sqrt}[c + d*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^{5/2}(c+dx)^{3/2}} dx &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}} - \frac{(4d) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/2}} dx}{3(bc-ad)} \\ &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}} + \frac{8d}{3(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}} + \frac{(8d^2) \int \frac{1}{\sqrt{a+bx}(c+dx)}}{3(bc-ad)} \\ &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}} + \frac{8d}{3(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}} + \frac{16d^2\sqrt{a+bx}}{3(bc-ad)^3\sqrt{c+dx}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 75, normalized size = 0.74

$$\frac{2(3a^2d^2 + 6abd(c + 2dx) + b^2(-c^2 + 4cdx + 8d^2x^2))}{3(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(3/2)), x]

[Out] (2*(3*a^2*d^2 + 6*a*b*d*(c + 2*d*x) + b^2*(-c^2 + 4*c*d*x + 8*d^2*x^2)))/(3*(b*c - a*d)^3*(a + b*x)^(3/2)*Sqrt[c + d*x])

fricas [B] time = 0.65, size = 273, normalized size = 2.70

$$\frac{2(8b^2d^2x^2 - b^2c^2 + 6abcd + 3a^2d^2 + 4(b^2cd + 3a^2b^2d^2 - a^5cd^3 + (b^5c^3d - 3ab^4c^2d^2 + 3a^2b^3cd^3 - a^3b^2d^4)x^3 + (b^5c^4 - ab^4c^3d - 3a^2b^3c^2d^2 + 5a^3b^2c^2d^3 - 2a^4b^2d^4)x^2 + (2a^2b^4c^4 - 5a^2b^3c^3d + 3a^3b^2c^2d^2 + a^4b^2cd^3 - a^5d^4)x)}{3(a^2b^3c^4 - 3a^3b^2c^3d + 3a^4bc^2d^2 - a^5cd^3 + (b^5c^3d - 3ab^4c^2d^2 + 3a^2b^3cd^3 - a^3b^2d^4)x^3 + (b^5c^4 - ab^4c^3d - 3a^2b^3c^2d^2 + 5a^3b^2c^2d^3 - 2a^4b^2d^4)x^2 + (2a^2b^4c^4 - 5a^2b^3c^3d + 3a^3b^2c^2d^2 + a^4b^2cd^3 - a^5d^4)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(3/2), x, algorithm="fricas")

[Out] 2/3*(8*b^2*d^2*x^2 - b^2*c^2 + 6*a*b*c*d + 3*a^2*d^2 + 4*(b^2*c*d + 3*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^2*b^3*c^4 - 3*a^3*b^2*c^3*d + 3*a^4*b*c^2*d^2 - a^5*c*d^3 + (b^5*c^3*d - 3*a*b^4*c^2*d^2 + 3*a^2*b^3*c*d^3 - a^3*b^2*d^4)*x^3 + (b^5*c^4 - a*b^4*c^3*d - 3*a^2*b^3*c^2*d^2 + 5*a^3*b^2*c*d^3 - 2*a^4*b*d^4)*x^2 + (2*a*b^4*c^4 - 5*a^2*b^3*c^3*d + 3*a^3*b^2*c^2*d^2 + a^4*b*c*d^3 - a^5*d^4)*x)

giac [B] time = 1.54, size = 368, normalized size = 3.64

$$\frac{2\sqrt{bx+a}b^2d^2}{(b^3c^3|b| - 3ab^2c^2d|b| + 3a^2bcd^2|b| - a^3d^3|b|)\sqrt{b^2c + (bx+a)bd} - abd} + \frac{4(5\sqrt{bd}b^6c^2d - 10\sqrt{bd}ab^5cd^2 + 5\sqrt{bd}a^4b^4c^2d^3 - 2a^5cd^3)}{3(bc-ad)^3\sqrt{c+dx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(3/2),x, algorithm="giac")

[Out] $2\sqrt{bx+a}b^2d^2/((b^3c^3\text{abs}(b) - 3ab^2c^2d\text{abs}(b) + 3a^2b^2cd^2\text{abs}(b) - a^3d^3\text{abs}(b))\sqrt{b^2c+(bx+a)bd-abd}) + 4/3(5\sqrt{bd}b^6c^2d - 10\sqrt{bd}ab^5cd^2 + 5\sqrt{bd}a^2b^4d^3 - 12\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c+(bx+a)bd-abd}))^2b^4cd + 12\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c+(bx+a)bd-abd})^2ab^3d^2 + 3\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c+(bx+a)bd-abd})^4b^2d)/((b^2c^2\text{abs}(b) - 2ab^2cd\text{abs}(b) + a^2d^2\text{abs}(b))(b^2c-abd-(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c+(bx+a)bd-abd}))^2)^3)$

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{2(8b^2x^2d^2 + 12abd^2x + 4b^2cdx + 3a^2d^2 + 6abcd - b^2c^2)}{3(bx+a)^{\frac{3}{2}}\sqrt{dx+c}(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(3/2),x)

[Out] $-2/3(8b^2d^2x^2+12a*b*d^2*x+4*b^2*c*d*x+3*a^2*d^2+6*a*b*c*d-b^2*c^2)/(b*x+a)^{(3/2)}/(d*x+c)^{(1/2)}/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.06, size = 141, normalized size = 1.40

$$\frac{\sqrt{c+dx}\left(\frac{8x(3ad+bc)}{3(ad-bc)^3} + \frac{16bdx^2}{3(ad-bc)^3} + \frac{6a^2d^2+12abcd-2b^2c^2}{3bd(ad-bc)^3}\right)}{x^2\sqrt{a+bx} + \frac{ac\sqrt{a+bx}}{bd} + \frac{x(ad+bc)\sqrt{a+bx}}{bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a + b*x)^(5/2)*(c + d*x)^(3/2)),x)
```

```
[Out] -((c + d*x)^(1/2)*((8*x*(3*a*d + b*c))/(3*(a*d - b*c)^3) + (16*b*d*x^2)/(3*(a*d - b*c)^3) + (6*a^2*d^2 - 2*b^2*c^2 + 12*a*b*c*d)/(3*b*d*(a*d - b*c)^3))/x^2*(a + b*x)^(1/2) + (a*c*(a + b*x)^(1/2))/(b*d) + (x*(a*d + b*c)*(a + b*x)^(1/2))/(b*d)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{5}{2}} (c + dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(3/2),x)
```

```
[Out] Integral(1/((a + b*x)**(5/2)*(c + d*x)**(3/2)), x)
```


$$3.1509 \quad \int \frac{1}{(a+bx)^{7/2}(c+dx)^{3/2}} dx$$

Optimal. Leaf size=136

$$\frac{32d^3\sqrt{a+bx}}{5\sqrt{c+dx}(bc-ad)^4} - \frac{16d^2}{5\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^3} + \frac{4d}{5(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^2} - \frac{2}{5(a+bx)^{5/2}\sqrt{c+dx}(bc-ad)}$$

[Out] $-2/5/(-a*d+b*c)/(b*x+a)^{(5/2)}/(d*x+c)^{(1/2)}+4/5*d/(-a*d+b*c)^2/(b*x+a)^{(3/2)}/(d*x+c)^{(1/2)}-16/5*d^2/(-a*d+b*c)^3/(b*x+a)^{(1/2)}/(d*x+c)^{(1/2)}-32/5*d^3*(b*x+a)^{(1/2)}/(-a*d+b*c)^4/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{32d^3\sqrt{a+bx}}{5\sqrt{c+dx}(bc-ad)^4} - \frac{16d^2}{5\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^3} + \frac{4d}{5(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^2} - \frac{2}{5(a+bx)^{5/2}\sqrt{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/2)*(c + d*x)^(3/2)), x]

[Out] $-2/(5*(b*c - a*d)*(a + b*x)^{(5/2)*\text{Sqrt}[c + d*x])} + (4*d)/(5*(b*c - a*d)^2*(a + b*x)^{(3/2)*\text{Sqrt}[c + d*x])} - (16*d^2)/(5*(b*c - a*d)^3*\text{Sqrt}[a + b*x]*\text{Sqrt}[c + d*x]) - (32*d^3*\text{Sqrt}[a + b*x])/(5*(b*c - a*d)^4*\text{Sqrt}[c + d*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[n] && !IntegerQ[m] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{7/2}(c+dx)^{3/2}} dx &= -\frac{2}{5(bc-ad)(a+bx)^{5/2}\sqrt{c+dx}} - \frac{(6d) \int \frac{1}{(a+bx)^{5/2}(c+dx)^{3/2}} dx}{5(bc-ad)} \\
&= -\frac{2}{5(bc-ad)(a+bx)^{5/2}\sqrt{c+dx}} + \frac{4d}{5(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}} + \frac{(8d^2) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/2}} dx}{5(bc-ad)^3\sqrt{c+dx}} \\
&= -\frac{2}{5(bc-ad)(a+bx)^{5/2}\sqrt{c+dx}} + \frac{4d}{5(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}} - \frac{16ad^2}{5(bc-ad)^3\sqrt{c+dx}} \\
&= -\frac{2}{5(bc-ad)(a+bx)^{5/2}\sqrt{c+dx}} + \frac{4d}{5(bc-ad)^2(a+bx)^{3/2}\sqrt{c+dx}} - \frac{16ad^2}{5(bc-ad)^3\sqrt{c+dx}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 114, normalized size = 0.84

$$\frac{2(5a^3d^3 + 15a^2bd^2(c + 2dx) + 5ab^2d(-c^2 + 4cdx + 8d^2x^2) + b^3(c^3 - 2c^2dx + 8cd^2x^2 + 16d^3x^3))}{5(a+bx)^{5/2}\sqrt{c+dx}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/2)*(c + d*x)^(3/2)), x]

[Out] (-2*(5*a^3*d^3 + 15*a^2*b*d^2*(c + 2*d*x) + 5*a*b^2*d*(-c^2 + 4*c*d*x + 8*d^2*x^2) + b^3*(c^3 - 2*c^2*d*x + 8*c*d^2*x^2 + 16*d^3*x^3)))/(5*(b*c - a*d)^4*(a + b*x)^(5/2)*Sqrt[c + d*x])

fricas [B] time = 0.98, size = 455, normalized size = 3.35

$$\frac{2(16b^3d^3x^3 + a^3b^4c^5 - 4a^4b^3c^4d + 6a^5b^2c^3d^2 - 4a^6bc^2d^3 + a^7cd^4 + (b^7c^4d - 4ab^6c^3d^2 + 6a^2b^5c^2d^3 - 4a^3b^4cd^4 + a^4b^3d^5))}{5(a+bx)^{5/2}\sqrt{c+dx}(bc-ad)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/2)/(d*x+c)^(3/2), x, algorithm="fricas")

[Out] -2/5*(16*b^3*d^3*x^3 + b^3*c^3 - 5*a*b^2*c^2*d + 15*a^2*b*c*d^2 + 5*a^3*d^3 + 8*(b^3*c*d^2 + 5*a*b^2*d^3)*x^2 - 2*(b^3*c^2*d - 10*a*b^2*c*d^2 - 15*a^2*b*d^3)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^3*b^4*c^5 - 4*a^4*b^3*c^4*d + 6*a^5*b^2*c^3*d^2 - 4*a^6*b*c^2*d^3 + a^7*c*d^4 + (b^7*c^4*d - 4*a*b^6*c^3*d^2 + 6*a^2*b^5*c^2*d^3 - 4*a^3*b^4*c*d^4 + a^4*b^3*d^5)*x^4 + (b^7*c^5 - a*b^6*c^4*d - 6*a^2*b^5*c^3*d^2 + 14*a^3*b^4*c^2*d^3 - 11*a^4*b^3*c*d^4 + 3*a^5*b^2*d^5)*x^3 + 3*(a*b^6*c^5 - 3*a^2*b^5*c^4*d + 2*a^3*b^4*c^3*d^2 + 2*a^4*b^3*c^2*d^3 - 2*a^5*b^2*c*d^4 + a^6*c*d^5))

$$b^3c^2d^3 - 3a^5b^2cd^4 + a^6b^2d^5)x^2 + (3a^2b^5c^5 - 11a^3b^4c^4d + 14a^4b^3c^3d^2 - 6a^5b^2c^2d^3 - a^6b^2cd^4 + a^7d^5)x$$

giac [B] time = 2.46, size = 830, normalized size = 6.10

$$\frac{2\sqrt{bx+a}b^2d^3}{(b^4c^4|b| - 4ab^3c^3d|b| + 6a^2b^2c^2d^2|b| - 4a^3bcd^3|b| + a^4d^4|b|)\sqrt{b^2c + (bx+a)bd - abd}} - \frac{4\left(11\sqrt{bd}b^{10}c^4d^2 - 44\right)}{}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/2)/(d*x+c)^(3/2),x, algorithm="giac")

[Out] $-2\sqrt{bx+a}b^2d^3/((b^4c^4\text{abs}(b) - 4a^2b^3c^3d\text{abs}(b) + 6a^4b^2c^2d^2\text{abs}(b) - 4a^3b^2cd^3\text{abs}(b) + a^4d^4\text{abs}(b))\sqrt{b^2c + (bx+a)bd - a^2bd}) - 4/5(11\sqrt{bd}b^{10}c^4d^2 - 44\sqrt{bd}a^2b^9c^3d^3 + 66\sqrt{bd}a^2b^8c^2d^4 - 44\sqrt{bd}a^3b^7c^2d^5 + 11\sqrt{bd}a^4b^6d^6 - 50\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^2b^8c^3d^2 + 150\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^2a^2b^7c^2d^3 - 150\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^2a^2b^6cd^4 + 50\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^2a^3b^5d^5 + 80\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^4b^6c^2d^2 - 160\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^4a^2b^5cd^3 + 80\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^4a^2b^4d^4 - 30\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^6b^4cd^2 + 30\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^6a^2b^3d^3 + 5\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^8b^2d^2)/((b^3c^3\text{abs}(b) - 3a^2b^2c^2d\text{abs}(b) + 3a^2b^2cd^2\text{abs}(b) - a^3d^3\text{abs}(b))(b^2c - a^2bd - \sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd}))^2)^5$

maple [A] time = 0.01, size = 170, normalized size = 1.25

$$\frac{2(16b^3x^3d^3 + 40ab^2d^3x^2 + 8b^3cd^2x^2 + 30a^2bd^3x + 20ab^2cd^2x - 2b^3c^2dx + 5a^3d^3 + 15a^2bcd^2 - 5ab^2c^2d + b^3c^3)}{5(bx+a)^{\frac{5}{2}}\sqrt{dx+c}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/2)/(d*x+c)^(3/2),x)

[Out] $-2/5(16b^3d^3x^3+40a^2b^2d^3x^2+8b^3cd^2x^2+30a^2b^2d^3x+20a^2b^2cd^2x-2b^3c^2d^2x+5a^3d^3+15a^2b^2cd^2-5a^2b^2c^2d+b^3c^3)/(b$

$(bx+a)^{5/2}/(dx+c)^{1/2}/(a^4d^4-4a^3b^2c^2d^2-4ab^3c^3d+b^4c^4)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/2)/(d*x+c)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.31, size = 227, normalized size = 1.67

$$\frac{\sqrt{c+dx} \left(\frac{16dx^2(5ad+bc)}{5(ad-bc)^4} + \frac{2a^3d^3+6a^2bcd^2-2ab^2c^2d+\frac{2b^3c^3}{5}}{b^2d(ad-bc)^4} + \frac{32bd^2x^3}{5(ad-bc)^4} + \frac{4x(15a^2d^2+10abcd-b^2c^2)}{5b(ad-bc)^4} \right)}{x^3\sqrt{a+bx} + \frac{a^2c\sqrt{a+bx}}{b^2d} + \frac{x^2(2ad+bc)\sqrt{a+bx}}{bd} + \frac{ax(ad+2bc)\sqrt{a+bx}}{b^2d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/2)*(c + d*x)^(3/2)),x)

[Out] $-\left((c + d*x)^{1/2} * \left(\frac{16*d*x^2*(5*a*d + b*c)}{5*(a*d - b*c)^4} + \frac{2*a^3*d^3 + (2*b^3*c^3)/5 - 2*a*b^2*c^2*d + 6*a^2*b*c*d^2}{(b^2*d*(a*d - b*c)^4} + \frac{3*2*b*d^2*x^3}{5*(a*d - b*c)^4} + \frac{4*x*(15*a^2*d^2 - b^2*c^2 + 10*a*b*c*d)}{(5*b*(a*d - b*c)^4)}\right) / (x^3*(a + b*x)^{1/2} + (a^2*c*(a + b*x)^{1/2}) / (b^2*d) + (x^2*(2*a*d + b*c)*(a + b*x)^{1/2}) / (b*d) + (a*x*(a*d + 2*b*c)*(a + b*x)^{1/2}) / (b^2*d))$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{7}{2}}(c+dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/2)/(d*x+c)**(3/2),x)

[Out] Integral(1/((a + b*x)**(7/2)*(c + d*x)**(3/2)), x)

$$3.1510 \quad \int \frac{1}{(a+bx)^{9/2}(c+dx)^{3/2}} dx$$

Optimal. Leaf size=171

$$\frac{256d^4\sqrt{a+bx}}{35\sqrt{c+dx}(bc-ad)^5} + \frac{128d^3}{35\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^4} - \frac{32d^2}{35(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^3} + \frac{16d}{35(a+bx)^{5/2}\sqrt{c+dx}}$$

[Out] $-2/7/(-a*d+b*c)/(b*x+a)^{(7/2)}/(d*x+c)^{(1/2)}+16/35*d/(-a*d+b*c)^2/(b*x+a)^{(5/2)}/(d*x+c)^{(1/2)}-32/35*d^2/(-a*d+b*c)^3/(b*x+a)^{(3/2)}/(d*x+c)^{(1/2)}+128/35*d^3/(-a*d+b*c)^4/(b*x+a)^{(1/2)}/(d*x+c)^{(1/2)}+256/35*d^4*(b*x+a)^{(1/2)}/(-a*d+b*c)^5/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 171, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{256d^4\sqrt{a+bx}}{35\sqrt{c+dx}(bc-ad)^5} + \frac{128d^3}{35\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^4} - \frac{32d^2}{35(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^3} + \frac{16d}{35(a+bx)^{5/2}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(9/2)*(c + d*x)^(3/2)), x]

[Out] $-2/(7*(b*c - a*d)*(a + b*x)^{(7/2)*\text{Sqrt}[c + d*x]) + (16*d)/(35*(b*c - a*d)^2*(a + b*x)^{(5/2)*\text{Sqrt}[c + d*x]) - (32*d^2)/(35*(b*c - a*d)^3*(a + b*x)^{(3/2)*\text{Sqrt}[c + d*x]) + (128*d^3)/(35*(b*c - a*d)^4*\text{Sqrt}[a + b*x]*\text{Sqrt}[c + d*x]) + (256*d^4*\text{Sqrt}[a + b*x])/(35*(b*c - a*d)^5*\text{Sqrt}[c + d*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{9/2}(c+dx)^{3/2}} dx &= -\frac{2}{7(bc-ad)(a+bx)^{7/2}\sqrt{c+dx}} - \frac{(8d) \int \frac{1}{(a+bx)^{7/2}(c+dx)^{3/2}} dx}{7(bc-ad)} \\
&= -\frac{2}{7(bc-ad)(a+bx)^{7/2}\sqrt{c+dx}} + \frac{16d}{35(bc-ad)^2(a+bx)^{5/2}\sqrt{c+dx}} + \frac{(48d^2) \int \frac{1}{(a+bx)^{5/2}(c+dx)^{3/2}} dx}{35(bc-ad)^3} \\
&= -\frac{2}{7(bc-ad)(a+bx)^{7/2}\sqrt{c+dx}} + \frac{16d}{35(bc-ad)^2(a+bx)^{5/2}\sqrt{c+dx}} - \frac{3}{35(bc-ad)^3} \\
&= -\frac{2}{7(bc-ad)(a+bx)^{7/2}\sqrt{c+dx}} + \frac{16d}{35(bc-ad)^2(a+bx)^{5/2}\sqrt{c+dx}} - \frac{3}{35(bc-ad)^3} \\
&= -\frac{2}{7(bc-ad)(a+bx)^{7/2}\sqrt{c+dx}} + \frac{16d}{35(bc-ad)^2(a+bx)^{5/2}\sqrt{c+dx}} - \frac{3}{35(bc-ad)^3}
\end{aligned}$$

Mathematica [A] time = 0.06, size = 166, normalized size = 0.97

$$\frac{2(35a^4d^4 + 140a^3bd^3(c+2dx) + 70a^2b^2d^2(-c^2 + 4cdx + 8d^2x^2)) + 28ab^3d(c^3 - 2c^2dx + 8cd^2x^2 + 16d^3x^3) + b^4}{35(a+bx)^{7/2}\sqrt{c+dx}(bc-ad)^5}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(9/2)*(c + d*x)^(3/2)),x]

[Out] (2*(35*a^4*d^4 + 140*a^3*b*d^3*(c + 2*d*x) + 70*a^2*b^2*d^2*(-c^2 + 4*c*d*x + 8*d^2*x^2) + 28*a*b^3*d*(c^3 - 2*c^2*d*x + 8*c*d^2*x^2 + 16*d^3*x^3) + b^4*(-5*c^4 + 8*c^3*d*x - 16*c^2*d^2*x^2 + 64*c*d^3*x^3 + 128*d^4*x^4))/(35*(b*c - a*d)^5*(a + b*x)^(7/2)*Sqrt[c + d*x])

fricas [B] time = 2.58, size = 689, normalized size = 4.03

$$35(a^4b^5c^6 - 5a^5b^4c^5d + 10a^6b^3c^4d^2 - 10a^7b^2c^3d^3 + 5a^8bc^2d^4 - a^9cd^5 + (b^9c^5d - 5ab^8c^4d^2 + 10a^2b^7c^3d^3 - 10a^3b^6c^2d^4 - 5a^4b^5c^2d^5 + 5a^5b^4c^3d^6 - 5a^6b^3c^4d^7 + 5a^7b^2c^5d^8 - 5a^8b^1c^6d^9))$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(d*x+c)^(3/2),x, algorithm="fricas")

[Out] 2/35*(128*b^4*d^4*x^4 - 5*b^4*c^4 + 28*a*b^3*c^3*d - 70*a^2*b^2*c^2*d^2 + 140*a^3*b*c*d^3 + 35*a^4*d^4 + 64*(b^4*c*d^3 + 7*a*b^3*d^4)*x^3 - 16*(b^4*c^4

$$2*d^2 - 14*a*b^3*c*d^3 - 35*a^2*b^2*d^4)*x^2 + 8*(b^4*c^3*d - 7*a*b^3*c^2*d^2 + 35*a^2*b^2*c*d^3 + 35*a^3*b*d^4)*x)*\sqrt{b*x + a}*\sqrt{d*x + c}/(a^4*b^5*c^6 - 5*a^5*b^4*c^5*d + 10*a^6*b^3*c^4*d^2 - 10*a^7*b^2*c^3*d^3 + 5*a^8*b*c^2*d^4 - a^9*c*d^5 + (b^9*c^5*d - 5*a*b^8*c^4*d^2 + 10*a^2*b^7*c^3*d^3 - 10*a^3*b^6*c^2*d^4 + 5*a^4*b^5*c*d^5 - a^5*b^4*d^6)*x^5 + (b^9*c^6 - a*b^8*c^5*d - 10*a^2*b^7*c^4*d^2 + 30*a^3*b^6*c^3*d^3 - 35*a^4*b^5*c^2*d^4 + 19*a^5*b^4*c*d^5 - 4*a^6*b^3*d^6)*x^4 + 2*(2*a*b^8*c^6 - 7*a^2*b^7*c^5*d + 5*a^3*b^6*c^4*d^2 + 10*a^4*b^5*c^3*d^3 - 20*a^5*b^4*c^2*d^4 + 13*a^6*b^3*c*d^5 - 3*a^7*b^2*d^6)*x^3 + 2*(3*a^2*b^7*c^6 - 13*a^3*b^6*c^5*d + 20*a^4*b^5*c^4*d^2 - 10*a^5*b^4*c^3*d^3 - 5*a^6*b^3*c^2*d^4 + 7*a^7*b^2*c*d^5 - 2*a^8*b*d^6)*x^2 + (4*a^3*b^6*c^6 - 19*a^4*b^5*c^5*d + 35*a^5*b^4*c^4*d^2 - 30*a^6*b^3*c^3*d^3 + 10*a^7*b^2*c^2*d^4 + a^8*b*c*d^5 - a^9*d^6)*x)$$

giac [B] time = 4.77, size = 1518, normalized size = 8.88

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(d*x+c)^(3/2),x, algorithm="giac")

[Out] $2*\sqrt{b*x + a}*b^2*d^4/((b^5*c^5*\text{abs}(b) - 5*a*b^4*c^4*d*\text{abs}(b) + 10*a^2*b^3*c^3*d^2*\text{abs}(b) - 10*a^3*b^2*c^2*d^3*\text{abs}(b) + 5*a^4*b*c*d^4*\text{abs}(b) - a^5*d^5*\text{abs}(b))*\sqrt{b^2*c + (b*x + a)*b*d - a*b*d}) + 4/35*(93*\sqrt{b*d}*b^{14}*c^6*d^3 - 558*\sqrt{b*d}*a*b^{13}*c^5*d^4 + 1395*\sqrt{b*d}*a^2*b^{12}*c^4*d^5 - 1860*\sqrt{b*d}*a^3*b^{11}*c^3*d^6 + 1395*\sqrt{b*d}*a^4*b^{10}*c^2*d^7 - 558*\sqrt{b*d}*a^5*b^9*c*d^8 + 93*\sqrt{b*d}*a^6*b^8*d^9 - 616*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*b^{12}*c^5*d^3 + 3080*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*a*b^{11}*c^4*d^4 - 6160*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*a^2*b^{10}*c^3*d^5 + 6160*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*a^3*b^9*c^2*d^6 - 3080*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*a^4*b^8*c*d^7 + 616*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*a^5*b^7*d^8 + 1673*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^4*b^{10}*c^4*d^3 - 6692*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^4*a*b^9*c^3*d^4 + 10038*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^4*a^2*b^8*c^2*d^5 - 6692*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^4*a^3*b^7*c*d^6 + 1673*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^4*a^4*b^6*d^7 - 2240*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^6*b^8*c^3*d^3 + 6720*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^6*a*b^7*c^2*d^4 - 6720*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^6*a^2*b^6*c*d^5 + 2240*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^6*a^3*b^5*d^6 +$

$$1015\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^8*b^6*c^2*d^3 - 2030*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^8*a*b^5*c*d^4 + 1015*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^8*a^2*b^4*d^5 - 280*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^10*b^4*c*d^3 + 280*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^10*a*b^3*d^4 + 35*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^12*b^2*d^3)/((b^4*c^4*abs(b) - 4*a*b^3*c^3*d*abs(b) + 6*a^2*b^2*c^2*d^2*abs(b) - 4*a^3*b*c*d^3*abs(b) + a^4*d^4*abs(b))*(b^2*c - a*b*d - (\sqrt{b*d}*\sqrt{b*x+a} - \sqrt{b^2*c + (b*x+a)*b*d - a*b*d})^2)^7)$$

maple [A] time = 0.01, size = 256, normalized size = 1.50

$$\frac{2(128b^4x^4d^4 + 448ab^3d^4x^3 + 64b^4cd^3x^3 + 560a^2b^2d^4x^2 + 224ab^3cd^3x^2 - 16b^4c^2d^2x^2 + 280a^3bd^4x + 280a^2b^2d^4)}{35(bx+a)^{\frac{7}{2}}\sqrt{dx+c}(a^5d^5 - 5a^4bcd^4 + 10a^3b^2c^2d^3 - \dots)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(9/2)/(d*x+c)^(3/2),x)

[Out] $-2/35*(128*b^4*d^4*x^4+448*a*b^3*d^4*x^3+64*b^4*c*d^3*x^3+560*a^2*b^2*d^4*x^2+224*a*b^3*c*d^3*x^2-16*b^4*c^2*d^2*x^2+280*a^3*b*d^4*x+280*a^2*b^2*c*d^3*x-56*a*b^3*c^2*d^2*x+8*b^4*c^3*d*x+35*a^4*d^4+140*a^3*b*c*d^3-70*a^2*b^2*c^2*d^2+28*a*b^3*c^3*d-5*b^4*c^4)/(b*x+a)^{(7/2)}/(d*x+c)^{(1/2)}/(a^5*d^5-5*a^4*b*c*d^4+10*a^3*b^2*c^2*d^3-10*a^2*b^3*c^3*d^2+5*a*b^4*c^4*d-b^5*c^5)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(d*x+c)^(3/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.50, size = 337, normalized size = 1.97

$$\frac{\sqrt{c+dx}\left(\frac{256bd^3x^4}{35(ad-bc)^5} + \frac{128d^2x^3(7ad+bc)}{35(ad-bc)^5} + \frac{70a^4d^4+280a^3bcd^3-140a^2b^2c^2d^2+56ab^3c^3d-10b^4c^4}{35b^3d(ad-bc)^5} + \frac{x(560a^3bd^4+560a^2b^2cd^3-10a^3b^2cd^3-10a^2b^3cd^2+5ab^4c^4d-b^5c^5)}{35b^3d(ad-bc)^5}\right)}{x^4\sqrt{a+bx} + \frac{a^3c\sqrt{a+bx}}{b^3d} + \frac{x^3(3ad+bc)\sqrt{a+bx}}{bd} + \frac{3ax^2(ad+bc)\sqrt{a+bx}}{b^2d} + \frac{a^2x(ad+bc)\sqrt{a+bx}}{b^2d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(9/2)*(c + d*x)^(3/2)), x)`

[Out]
$$-\frac{(c + dx)^{1/2} \left(\frac{256bd^3x^4}{35(ad - bc)^5} + (128d^2x^3(7ad + bc)) / (35(ad - bc)^5) + (70a^4d^4 - 10b^4c^4 - 140a^2b^2c^2d^2 + 56a^3c^3d + 280a^3b^2cd^3) / (35b^3d(ad - bc)^5) + (x(560a^3bd^4 + 16b^4c^3d - 112ab^3c^2d^2 + 560a^2b^2cd^3)) / (35b^3d(ad - bc)^5) + (32dx^2(35a^2d^2 - b^2c^2 + 14ab^2cd)) / (35b(ad - bc)^5) \right)}{x^4(a + bx)^{1/2} + a^3c(a + bx)^{1/2}/(b^3d) + (x^3(3ad + bc)(a + bx)^{1/2})/(bd) + (3ax^2(ad + bc)(a + bx)^{1/2})/(b^2d) + (a^2x(ad + 3bc)(a + bx)^{1/2})/(b^3d)}$$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{9}{2}} (c + dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(9/2)/(d*x+c)**(3/2), x)`

[Out] `Integral(1/((a + b*x)**(9/2)*(c + d*x)**(3/2)), x)`

$$3.1511 \quad \int \frac{1}{(a+bx)^{11/2}(c+dx)^{3/2}} dx$$

Optimal. Leaf size=206

$$\frac{512d^5\sqrt{a+bx}}{63\sqrt{c+dx}(bc-ad)^6} - \frac{256d^4}{63\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^5} + \frac{64d^3}{63(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^4} - \frac{32d^2}{63(a+bx)^{5/2}\sqrt{c+dx}}$$

[Out] $-2/9/(-a*d+b*c)/(b*x+a)^{(9/2)}/(d*x+c)^{(1/2)}+20/63*d/(-a*d+b*c)^2/(b*x+a)^{(7/2)}/(d*x+c)^{(1/2)}-32/63*d^2/(-a*d+b*c)^3/(b*x+a)^{(5/2)}/(d*x+c)^{(1/2)}+64/63*d^3/(-a*d+b*c)^4/(b*x+a)^{(3/2)}/(d*x+c)^{(1/2)}-256/63*d^4/(-a*d+b*c)^5/(b*x+a)^{(1/2)}/(d*x+c)^{(1/2)}-512/63*d^5*(b*x+a)^{(1/2)}/(-a*d+b*c)^6/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.06, antiderivative size = 206, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{512d^5\sqrt{a+bx}}{63\sqrt{c+dx}(bc-ad)^6} - \frac{256d^4}{63\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^5} + \frac{64d^3}{63(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^4} - \frac{32d^2}{63(a+bx)^{5/2}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(11/2)*(c + d*x)^(3/2)),x]

[Out] $-2/(9*(b*c - a*d)*(a + b*x)^{(9/2)*Sqrt[c + d*x]) + (20*d)/(63*(b*c - a*d)^2*(a + b*x)^{(7/2)*Sqrt[c + d*x]) - (32*d^2)/(63*(b*c - a*d)^3*(a + b*x)^{(5/2)*Sqrt[c + d*x]) + (64*d^3)/(63*(b*c - a*d)^4*(a + b*x)^{(3/2)*Sqrt[c + d*x]) - (256*d^4)/(63*(b*c - a*d)^5*Sqrt[a + b*x]*Sqrt[c + d*x]) - (512*d^5*Sqrt[a + b*x])/(63*(b*c - a*d)^6*Sqrt[c + d*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler

Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{11/2}(c+dx)^{3/2}} dx &= -\frac{2}{9(bc-ad)(a+bx)^{9/2}\sqrt{c+dx}} - \frac{(10d) \int \frac{1}{(a+bx)^{9/2}(c+dx)^{3/2}} dx}{9(bc-ad)} \\
 &= -\frac{2}{9(bc-ad)(a+bx)^{9/2}\sqrt{c+dx}} + \frac{20d}{63(bc-ad)^2(a+bx)^{7/2}\sqrt{c+dx}} + \frac{(80d^2) \int \frac{1}{(a+bx)^{7/2}(c+dx)^{3/2}} dx}{63(bc-ad)^2} \\
 &= -\frac{2}{9(bc-ad)(a+bx)^{9/2}\sqrt{c+dx}} + \frac{20d}{63(bc-ad)^2(a+bx)^{7/2}\sqrt{c+dx}} - \frac{80d^2}{63(bc-ad)^2} \int \frac{1}{(a+bx)^{5/2}(c+dx)^{3/2}} dx \\
 &= -\frac{2}{9(bc-ad)(a+bx)^{9/2}\sqrt{c+dx}} + \frac{20d}{63(bc-ad)^2(a+bx)^{7/2}\sqrt{c+dx}} - \frac{80d^2}{63(bc-ad)^2} \\
 &= -\frac{2}{9(bc-ad)(a+bx)^{9/2}\sqrt{c+dx}} + \frac{20d}{63(bc-ad)^2(a+bx)^{7/2}\sqrt{c+dx}} - \frac{80d^2}{63(bc-ad)^2} \\
 &= -\frac{2}{9(bc-ad)(a+bx)^{9/2}\sqrt{c+dx}} + \frac{20d}{63(bc-ad)^2(a+bx)^{7/2}\sqrt{c+dx}} - \frac{80d^2}{63(bc-ad)^2} \\
 &= -\frac{2}{9(bc-ad)(a+bx)^{9/2}\sqrt{c+dx}} + \frac{20d}{63(bc-ad)^2(a+bx)^{7/2}\sqrt{c+dx}} - \frac{80d^2}{63(bc-ad)^2}
 \end{aligned}$$

Mathematica [A] time = 0.08, size = 226, normalized size = 1.10

$$\frac{512d^5\sqrt{a+bx}}{63\sqrt{c+dx}(bc-ad)^5(ad-bc)} + \frac{256d^4}{63\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^4(ad-bc)} + \frac{64d^3}{63(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)^4} - \frac{80d^2}{63(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(11/2)*(c + d*x)^(3/2)), x]

[Out] -2/(9*(b*c - a*d)*(a + b*x)^(9/2)*Sqrt[c + d*x]) + (20*d)/(63*(b*c - a*d)^2*(a + b*x)^(7/2)*Sqrt[c + d*x]) - (32*d^2)/(63*(b*c - a*d)^3*(a + b*x)^(5/2)*Sqrt[c + d*x]) + (64*d^3)/(63*(b*c - a*d)^4*(a + b*x)^(3/2)*Sqrt[c + d*x]) + (256*d^4)/(63*(b*c - a*d)^4*(-(b*c) + a*d)*Sqrt[a + b*x]*Sqrt[c + d*x]) + (512*d^5*Sqrt[a + b*x])/(63*(b*c - a*d)^5*(-(b*c) + a*d)*Sqrt[c + d*x])

fricas [B] time = 6.35, size = 955, normalized size = 4.64

$$\frac{63(a^5b^6c^7 - 6a^6b^5c^6d + 15a^7b^4c^5d^2 - 20a^8b^3c^4d^3 + 15a^9b^2c^3d^4 - 6a^{10}bc^2d^5 + a^{11}cd^6 + (b^{11}c^6d - 6ab^{10}c^5d^2)}{63}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/2)/(d*x+c)^(3/2),x, algorithm="fricas")

[Out]
$$-2/63*(256*b^5*d^5*x^5 + 7*b^5*c^5 - 45*a*b^4*c^4*d + 126*a^2*b^3*c^3*d^2 - 210*a^3*b^2*c^2*d^3 + 315*a^4*b*c*d^4 + 63*a^5*d^5 + 128*(b^5*c*d^4 + 9*a*b^4*d^5))*x^4 - 32*(b^5*c^2*d^3 - 18*a*b^4*c*d^4 - 63*a^2*b^3*d^5)*x^3 + 16*(b^5*c^3*d^2 - 9*a*b^4*c^2*d^3 + 63*a^2*b^3*c*d^4 + 105*a^3*b^2*d^5)*x^2 - 2*(5*b^5*c^4*d - 36*a*b^4*c^3*d^2 + 126*a^2*b^3*c^2*d^3 - 420*a^3*b^2*c*d^4 - 315*a^4*b*d^5)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a^5*b^6*c^7 - 6*a^6*b^5*c^6*d + 15*a^7*b^4*c^5*d^2 - 20*a^8*b^3*c^4*d^3 + 15*a^9*b^2*c^3*d^4 - 6*a^10*b*c^2*d^5 + a^11*c*d^6 + (b^11*c^6*d - 6*a*b^10*c^5*d^2 + 15*a^2*b^9*c^4*d^3 - 20*a^3*b^8*c^3*d^4 + 15*a^4*b^7*c^2*d^5 - 6*a^5*b^6*c*d^6 + a^6*b^5*d^7)*x^6 + (b^11*c^7 - a*b^10*c^6*d - 15*a^2*b^9*c^5*d^2 + 55*a^3*b^8*c^4*d^3 - 85*a^4*b^7*c^3*d^4 + 69*a^5*b^6*c^2*d^5 - 29*a^6*b^5*c*d^6 + 5*a^7*b^4*d^7)*x^5 + 5*(a*b^10*c^7 - 4*a^2*b^9*c^6*d + 3*a^3*b^8*c^5*d^2 + 10*a^4*b^7*c^4*d^3 - 25*a^5*b^6*c^3*d^4 + 24*a^6*b^5*c^2*d^5 - 11*a^7*b^4*c*d^6 + 2*a^8*b^3*d^7)*x^4 + 10*(a^2*b^9*c^7 - 5*a^3*b^8*c^6*d + 9*a^4*b^7*c^5*d^2 - 5*a^5*b^6*c^4*d^3 - 5*a^6*b^5*c^3*d^4 + 9*a^7*b^4*c^2*d^5 - 5*a^8*b^3*c*d^6 + a^9*b^2*d^7)*x^3 + 5*(2*a^3*b^8*c^7 - 11*a^4*b^7*c^6*d + 24*a^5*b^6*c^5*d^2 - 25*a^6*b^5*c^4*d^3 + 10*a^7*b^4*c^3*d^4 + 3*a^8*b^3*c^2*d^5 - 4*a^9*b^2*c*d^6 + a^10*b*d^7)*x^2 + (5*a^4*b^7*c^7 - 29*a^5*b^6*c^6*d + 69*a^6*b^5*c^5*d^2 - 85*a^7*b^4*c^4*d^3 + 55*a^8*b^3*c^3*d^4 - 15*a^9*b^2*c^2*d^5 - a^10*b*c*d^6 + a^11*d^7)*x)$$

giac [B] time = 8.71, size = 2438, normalized size = 11.83

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/2)/(d*x+c)^(3/2),x, algorithm="giac")

[Out]
$$-2*sqrt(b*x + a)*b^2*d^5/((b^6*c^6*abs(b) - 6*a*b^5*c^5*d*abs(b) + 15*a^2*b^4*c^4*d^2*abs(b) - 20*a^3*b^3*c^3*d^3*abs(b) + 15*a^4*b^2*c^2*d^4*abs(b) - 6*a^5*b*c*d^5*abs(b) + a^6*d^6*abs(b))*sqrt(b^2*c + (b*x + a)*b*d - a*b*d) - 4/63*(193*sqrt(b*d)*b^18*c^8*d^4 - 1544*sqrt(b*d)*a*b^17*c^7*d^5 + 5404*sqrt(b*d)*a^2*b^16*c^6*d^6 - 10808*sqrt(b*d)*a^3*b^15*c^5*d^7 + 13510*sqrt(b*d)*a^4*b^14*c^4*d^8 - 10808*sqrt(b*d)*a^5*b^13*c^3*d^9 + 5404*sqrt(b*d)*a^6*b^12*c^2*d^10 - 1544*sqrt(b*d)*a^7*b^11*c*d^11 + 193*sqrt(b*d)*a^8*b^10*d^12 - 1674*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*b^16*c^7*d^4 + 11718*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a*b^15*c^6*d^5 - 35154*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^2*b^14*c^5*d^6 + 58590*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sqrt(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^3*b^13*c^4*d^7 - 58590*sqrt(b*d)*(sqrt(b*d)*sqrt(b*x + a) - sq$$

$$\begin{aligned}
& \text{rt}(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^4*b^12*c^3*d^8 + 35154*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^5*b^11*c^2*d^9 - 11718*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^6*b^10*c*d^10 + 1674*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^2*a^7*b^9*d^11 + 6318*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^4*b^14*c^6*d^4 - 37908*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^4*a*b^13*c^5*d^5 + 94770*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^2*b^12*c^4*d^6 - 126360*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^3*b^11*c^3*d^7 + 94770*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^4*b^10*c^2*d^8 - 37908*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^5*b^9*c*d^9 + 6318*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^4*a^6*b^8*d^10 - 13314*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^6*b^12*c^5*d^4 + 66570*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^6*a*b^11*c^4*d^5 - 133140*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^2*b^10*c^3*d^6 + 133140*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^3*b^9*c^2*d^7 - 66570*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^4*b^8*c*d^8 + 13314*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^6*a^5*b^7*d^9 + 16128*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^8*b^10*c^4*d^4 - 64512*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^8*a*b^9*c^3*d^5 + 96768*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^8*a^2*b^8*c^2*d^6 - 64512*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^8*a^3*b^7*c*d^7 + 16128*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^8*a^4*b^6*d^8 - 8190*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^10*b^8*c^3*d^4 + 24570*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^10*a*b^7*c^2*d^5 - 24570*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^10*a^2*b^6*c*d^6 + 8190*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^10*a^3*b^5*d^7 + 2898*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^12*b^6*c^2*d^4 - 5796*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^12*a*b^5*c*d^5 + 2898*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^12*a^2*b^4*d^6 - 630*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^14*b^4*c*d^4 + 630*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^14*a*b^3*d^5 + 63*\text{sqrt}(b*d)*(\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d))^16*b^2*d^4)/((b^5*c^5*abs(b) - 5*a*b^4*c^4*d*abs(b) + 10*a^2*b^3*c^3*d^2*abs(b) - 10*a^3*b^2*c^2*d^3*abs(b) + 5*a^4*b*c*d^4*abs(b) - a^5*d^5*abs(b))*(b^2*c - a*b*d - (\text{sqrt}(b*d)*\text{sqrt}(b*x + a) - \text{sqrt}(b^2*c + (b*x + a)*b*d - a*b*d)))^2)^9)
\end{aligned}$$

maple [B] time = 0.01, size = 356, normalized size = 1.73

$$2 \left(256b^5x^5d^5 + 1152ab^4d^5x^4 + 128b^5cd^4x^4 + 2016a^2b^3d^5x^3 + 576ab^4cd^4x^3 - 32b^5c^2d^3x^3 + 1680a^3b^2d^5x^2 + 1008a^2b^3cd^4x^2 - 144a^4b^2cd^4x - 252a^2b^3c^2d^3x + 72a^4b^2c^3d^2x - 10b^5c^4d^2x + 63a^5d^5 + 315a^4b^2cd^4 - 210a^3b^2c^2d^3 + 126a^2b^3c^3d^2 - 45ab^4c^4d + 7b^5c^5 \right) / (bx+a)^{(11/2)} / (dx+c)^{(3/2)}$$

63 (bx + a)

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(11/2)/(d*x+c)^(3/2), x)

[Out]
$$-2/63 * (256*b^5*d^5*x^5 + 1152*a*b^4*d^5*x^4 + 128*b^5*c*d^4*x^4 + 2016*a^2*b^3*d^5*x^3 + 576*a*b^4*c*d^4*x^3 - 32*b^5*c^2*d^3*x^3 + 1680*a^3*b^2*d^5*x^2 + 1008*a^2*b^3*c*d^4*x^2 - 144*a^4*b^2*c*d^4*x - 252*a^2*b^3*c^2*d^3*x + 72*a^4*b^2*c^3*d^2*x - 10*b^5*c^4*d^2*x + 63*a^5*d^5 + 315*a^4*b^2*c*d^4 - 210*a^3*b^2*c^2*d^3 + 126*a^2*b^3*c^3*d^2 - 45*a*b^4*c^4*d + 7*b^5*c^5) / (b*x+a)^{(9/2)} / (d*x+c)^{(1/2)} / (a^6*d^6 - 6*a^5*b*c*d^5 + 15*a^4*b^2*c^2*d^4 - 20*a^3*b^3*c^3*d^3 + 15*a^2*b^4*c^4*d^2 - 6*a*b^5*c^5*d + b^6*c^6)$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/2)/(d*x+c)^(3/2), x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c zero or nonzero?

mupad [B] time = 1.96, size = 454, normalized size = 2.20

$$\frac{\sqrt{c+dx} \left(\frac{126a^5d^5 + 630a^4bcd^4 - 420a^3b^2c^2d^3 + 252a^2b^3c^3d^2 - 90ab^4c^4d + 14b^5c^5}{63b^4d(ad-bc)^6} + \frac{512bd^4x^5}{63(ad-bc)^6} + \frac{256d^3x^4(9ad+bc)}{63(ad-bc)^6} + \frac{x(1260a^4b^2d^5 - 20b^5c^4d + 144a^4b^2c^3d^2 + 1680a^3b^2cd^4 - 504a^2b^3c^2d^3)}{63b^4d(ad-bc)^6} \right)}{x^5 \sqrt{a+bx} + \frac{a^4c\sqrt{a+bx}}{b^4d} + \frac{x^4(4ad+bc)\sqrt{a+bx}}{bd} + \frac{2ax^3(3a^2d+bc)}{b^2d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(11/2)*(c + d*x)^(3/2)), x)

[Out]
$$-((c + d*x)^{(1/2)} * ((126*a^5*d^5 + 14*b^5*c^5 + 252*a^2*b^3*c^3*d^2 - 420*a^3*b^2*c^2*d^3 - 90*a*b^4*c^4*d + 630*a^4*b^2*c^3*d^4) / (63*b^4*d*(a*d - b*c)^6) + (512*b*d^4*x^5) / (63*(a*d - b*c)^6) + (256*d^3*x^4*(9*a*d + b*c)) / (63*(a*d - b*c)^6) + (x*(1260*a^4*b^2*d^5 - 20*b^5*c^4*d + 144*a^4*b^2*c^3*d^2 + 1680*a^3*b^2*c*d^4 - 504*a^2*b^3*c^2*d^3)) / (63*b^4*d*(a*d - b*c)^6) + (64*d^2*x^3$$

$$\begin{aligned} &*(63*a^2*d^2 - b^2*c^2 + 18*a*b*c*d))/(63*b*(a*d - b*c)^6) + (32*d*x^2*(105 \\ &*a^3*d^3 + b^3*c^3 - 9*a*b^2*c^2*d + 63*a^2*b*c*d^2))/(63*b^2*(a*d - b*c)^6 \\ &)))/(x^5*(a + b*x)^{(1/2)} + (a^4*c*(a + b*x)^{(1/2)})/(b^4*d) + (x^4*(4*a*d + \\ &b*c)*(a + b*x)^{(1/2)})/(b*d) + (2*a*x^3*(3*a*d + 2*b*c)*(a + b*x)^{(1/2)})/(b^ \\ &2*d) + (a^3*x*(a*d + 4*b*c)*(a + b*x)^{(1/2)})/(b^4*d) + (2*a^2*x^2*(2*a*d + \\ &3*b*c)*(a + b*x)^{(1/2)})/(b^3*d)) \end{aligned}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(11/2)/(d*x+c)**(3/2),x)

[Out] Timed out

$$3.1512 \quad \int \frac{(a+bx)^{9/2}}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=204

$$-\frac{105b^{3/2}(bc-ad)^3 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{8d^{11/2}} + \frac{105b^2\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}{8d^5} - \frac{35b^2(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)}{4d^4} + \frac{7b^2}{8d^3}$$

[Out] $-2/3*(b*x+a)^{(9/2)}/d/(d*x+c)^{(3/2)}-105/8*b^{(3/2)}*(-a*d+b*c)^3*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/d^{(11/2)}-6*b*(b*x+a)^{(7/2)}/d^2/(d*x+c)^{(1/2)}-35/4*b^2*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/d^4+7*b^2*(b*x+a)^{(5/2)}*(d*x+c)^{(1/2)}/d^3+105/8*b^2*(-a*d+b*c)^2*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/d^5$

Rubi [A] time = 0.11, antiderivative size = 204, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 217, 206}

$$\frac{7b^2(a+bx)^{5/2}\sqrt{c+dx}}{d^3} - \frac{35b^2(a+bx)^{3/2}\sqrt{c+dx}(bc-ad)}{4d^4} + \frac{105b^2\sqrt{a+bx}\sqrt{c+dx}(bc-ad)^2}{8d^5} - \frac{105b^{3/2}(bc-ad)^3}{8d^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(9/2)/(c + d*x)^(5/2), x]

[Out] $(-2*(a + b*x)^{(9/2)})/(3*d*(c + d*x)^{(3/2)}) - (6*b*(a + b*x)^{(7/2)})/(d^2*\operatorname{Sqrt}[c + d*x]) + (105*b^2*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(8*d^5) - (35*b^2*(b*c - a*d)*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(4*d^4) + (7*b^2*(a + b*x)^{(5/2)}*\operatorname{Sqrt}[c + d*x])/d^3 - (105*b^{(3/2)}*(b*c - a*d)^3*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/(8*d^{(11/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/


```
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && ( !IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{9/2}}{(c+dx)^{5/2}} dx &= -\frac{2(a+bx)^{9/2}}{3d(c+dx)^{3/2}} + \frac{(3b) \int \frac{(a+bx)^{7/2}}{(c+dx)^{3/2}} dx}{d} \\
&= -\frac{2(a+bx)^{9/2}}{3d(c+dx)^{3/2}} - \frac{6b(a+bx)^{7/2}}{d^2\sqrt{c+dx}} + \frac{(21b^2) \int \frac{(a+bx)^{5/2}}{\sqrt{c+dx}} dx}{d^2} \\
&= -\frac{2(a+bx)^{9/2}}{3d(c+dx)^{3/2}} - \frac{6b(a+bx)^{7/2}}{d^2\sqrt{c+dx}} + \frac{7b^2(a+bx)^{5/2}\sqrt{c+dx}}{d^3} - \frac{(35b^2(bc-ad)) \int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx}{2d^3} \\
&= -\frac{2(a+bx)^{9/2}}{3d(c+dx)^{3/2}} - \frac{6b(a+bx)^{7/2}}{d^2\sqrt{c+dx}} - \frac{35b^2(bc-ad)(a+bx)^{3/2}\sqrt{c+dx}}{4d^4} + \frac{7b^2(a+bx)^{5/2}\sqrt{c+dx}}{d^3} \\
&= -\frac{2(a+bx)^{9/2}}{3d(c+dx)^{3/2}} - \frac{6b(a+bx)^{7/2}}{d^2\sqrt{c+dx}} + \frac{105b^2(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^5} - \frac{35b^2(bc-ad)(a+bx)^{3/2}}{4d^4} \\
&= -\frac{2(a+bx)^{9/2}}{3d(c+dx)^{3/2}} - \frac{6b(a+bx)^{7/2}}{d^2\sqrt{c+dx}} + \frac{105b^2(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^5} - \frac{35b^2(bc-ad)(a+bx)^{3/2}}{4d^4} \\
&= -\frac{2(a+bx)^{9/2}}{3d(c+dx)^{3/2}} - \frac{6b(a+bx)^{7/2}}{d^2\sqrt{c+dx}} + \frac{105b^2(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^5} - \frac{35b^2(bc-ad)(a+bx)^{3/2}}{4d^4} \\
&= -\frac{2(a+bx)^{9/2}}{3d(c+dx)^{3/2}} - \frac{6b(a+bx)^{7/2}}{d^2\sqrt{c+dx}} + \frac{105b^2(bc-ad)^2\sqrt{a+bx}\sqrt{c+dx}}{8d^5} - \frac{35b^2(bc-ad)(a+bx)^{3/2}}{4d^4}
\end{aligned}$$

Mathematica [C] time = 0.10, size = 73, normalized size = 0.36

$$\frac{2(a+bx)^{11/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/2} {}_2F_1 \left(\frac{5}{2}, \frac{11}{2}; \frac{13}{2}; \frac{d(a+bx)}{ad-bc} \right)}{11b(c+dx)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(9/2)/(c + d*x)^(5/2), x]

[Out] (2*(a + b*x)^(11/2)*((b*(c + d*x))/(b*c - a*d))^(5/2)*Hypergeometric2F1[5/2, 11/2, 13/2, (d*(a + b*x))/(-b*c + a*d)]/(11*b*(c + d*x)^(5/2))

fricas [B] time = 1.35, size = 879, normalized size = 4.31

$$\frac{315(b^4c^5 - 3ab^3c^4d + 3a^2b^2c^3d^2 - a^3bc^2d^3 + (b^4c^3d^2 - 3ab^3c^2d^3 + 3a^2b^2cd^4 - a^3bd^5)x^2 + 2(b^4c^4d - 3ab^3c^4d^2 - 3a^2b^3c^3d^2 + 3a^2b^2c^2d^3 - a^3b^2c^2d^4)*x)\sqrt{b/d}\log(8b^2d^2x^2 + b^2c^2 + 6a^2b^2cd + a^2d^2 + 4(2b^2d^2x + b^2cd + a^2d^2)\sqrt{bx+a})\sqrt{dx+c})\sqrt{b/d} + 8(b^2cd + a^2bd^2)x - 4(8b^4d^4x^4 + 315b^4c^4 - 840a^2b^3c^3d + 693a^2b^2c^2d^2 - 144a^3b^2c^2d^3 - 16a^4d^4 - 2(9b^4c^3d^3 - 25a^2b^3d^4)x^3 + 3(21b^4c^2d^2 - 60a^2b^3c^2d^3 + 55a^2b^2d^4)x^2 + 2(210b^4c^3d - 567a^2b^3c^2d^2 + 477a^2b^2c^2d^3 - 104a^3b^2d^4)x)\sqrt{bx+a})\sqrt{dx+c})/(d^7x^2 + 2cd^6x + c^2d^5), 1/48(315(b^4c^5 - 3a^2b^2c^3d^2 - a^3b^2c^2d^3 + (b^4c^3d^2 - 3a^2b^3c^2d^3 + 3a^2b^2c^2d^4 - a^3b^2c^2d^4)x)\sqrt{-b/d})\arctan(1/2(2b^2d^2x + b^2cd + a^2d^2)\sqrt{bx+a})\sqrt{dx+c})\sqrt{-b/d}/(b^2d^2x^2 + a^2b^2c + (b^2cd + a^2bd^2)x)) + 2(8b^4d^4x^4 + 315b^4c^4 - 840a^2b^3c^3d + 693a^2b^2c^2d^2 - 144a^3b^2c^2d^3 - 16a^4d^4 - 2(9b^4c^3d^3 - 25a^2b^3d^4)x^3 + 3(21b^4c^2d^2 - 60a^2b^3c^2d^3 + 55a^2b^2d^4)x^2 + 2(210b^4c^3d - 567a^2b^3c^2d^2 + 477a^2b^2c^2d^3 - 104a^3b^2d^4)x)\sqrt{bx+a})\sqrt{dx+c})/(d^7x^2 + 2cd^6x + c^2d^5)]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/(d*x+c)^(5/2),x, algorithm="fricas")

[Out] [-1/96*(315*(b^4*c^5 - 3*a*b^3*c^4*d + 3*a^2*b^2*c^3*d^2 - a^3*b*c^2*d^3 + (b^4*c^3*d^2 - 3*a*b^3*c^2*d^3 + 3*a^2*b^2*c^2*d^4 - a^3*b*d^5)*x^2 + 2*(b^4*c^4*d - 3*a*b^3*c^3*d^2 + 3*a^2*b^2*c^2*d^3 - a^3*b*c^2*d^4)*x)*sqrt(b/d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d^2*x + b*c*d + a*d^2)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(b/d) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(8*b^4*d^4*x^4 + 315*b^4*c^4 - 840*a*b^3*c^3*d + 693*a^2*b^2*c^2*d^2 - 144*a^3*b*c^2*d^3 - 16*a^4*d^4 - 2*(9*b^4*c^3*d^3 - 25*a*b^3*d^4)*x^3 + 3*(21*b^4*c^2*d^2 - 60*a*b^3*c^2*d^3 + 55*a^2*b^2*d^4)*x^2 + 2*(210*b^4*c^3*d - 567*a*b^3*c^2*d^2 + 477*a^2*b^2*c^2*d^3 - 104*a^3*b*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(d^7*x^2 + 2*c*d^6*x + c^2*d^5), 1/48*(315*(b^4*c^5 - 3*a*b^3*c^4*d + 3*a^2*b^2*c^3*d^2 - a^3*b*c^2*d^3 + (b^4*c^3*d^2 - 3*a*b^3*c^2*d^3 + 3*a^2*b^2*c^2*d^4 - a^3*b*d^5)*x^2 + 2*(b^4*c^4*d - 3*a*b^3*c^3*d^2 + 3*a^2*b^2*c^2*d^3 - a^3*b*c^2*d^4)*x)*sqrt(-b/d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-b/d)/(b^2*d*x^2 + a*b*c + (b^2*c + a*b*d)*x)) + 2*(8*b^4*d^4*x^4 + 315*b^4*c^4 - 840*a*b^3*c^3*d + 693*a^2*b^2*c^2*d^2 - 144*a^3*b*c^2*d^3 - 16*a^4*d^4 - 2*(9*b^4*c^3*d^3 - 25*a*b^3*d^4)*x^3 + 3*(21*b^4*c^2*d^2 - 60*a*b^3*c^2*d^3 + 55*a^2*b^2*d^4)*x^2 + 2*(210*b^4*c^3*d - 567*a*b^3*c^2*d^2 + 477*a^2*b^2*c^2*d^3 - 104*a^3*b*d^4)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(d^7*x^2 + 2*c*d^6*x + c^2*d^5)]

giac [B] time = 2.42, size = 500, normalized size = 2.45

$$\frac{\left(\left(\left(2(bx+a)\left(\frac{4(b^6cd^8-ab^5d^9)(bx+a)}{b^2cd^9|b|-abd^{10}|b|} - \frac{9(b^7c^2d^7-2ab^6cd^8+a^2b^5d^9)}{b^2cd^9|b|-abd^{10}|b|}\right) + \frac{63(b^8c^3d^6-3ab^7c^2d^7+3a^2b^6cd^8-a^3b^5d^9)}{b^2cd^9|b|-abd^{10}|b|}\right)(bx+a) + \frac{420(b^9c^4}{24(b^2c + (bx +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/(d*x+c)^(5/2),x, algorithm="giac")

[Out] 1/24*(((2*(b*x + a)*(4*(b^6*c*d^8 - a*b^5*d^9)*(b*x + a)/(b^2*c*d^9*abs(b) - a*b*d^10*abs(b)) - 9*(b^7*c^2*d^7 - 2*a*b^6*c*d^8 + a^2*b^5*d^9)/(b^2*c*d^9*abs(b) - a*b*d^10*abs(b))) + 63*(b^8*c^3*d^6 - 3*a*b^7*c^2*d^7 + 3*a^2*b

$$\frac{(b^6 c d^8 - a^3 b^5 d^9)/(b^2 c d^9 \operatorname{abs}(b) - a b d^{10} \operatorname{abs}(b)) (b x + a) + 420 (b^9 c^4 d^5 - 4 a b^8 c^3 d^6 + 6 a^2 b^7 c^2 d^7 - 4 a^3 b^6 c d^8 + a^4 b^5 d^9)/(b^2 c d^9 \operatorname{abs}(b) - a b d^{10} \operatorname{abs}(b)) (b x + a) + 315 (b^{10} c^5 d^4 - 5 a b^9 c^4 d^5 + 10 a^2 b^8 c^3 d^6 - 10 a^3 b^7 c^2 d^7 + 5 a^4 b^6 c d^8 - a^5 b^5 d^9)/(b^2 c d^9 \operatorname{abs}(b) - a b d^{10} \operatorname{abs}(b)) \sqrt{b x + a}}{(b^2 c + (b x + a) b d - a b d)^{3/2} + 105/8 (b^6 c^3 - 3 a b^5 c^2 d + 3 a^2 b^4 c d^2 - a^3 b^3 d^3) \log(\operatorname{abs}(-\sqrt{b d}) \sqrt{b x + a} + \sqrt{b^2 c + (b x + a) b d - a b d})} / (\sqrt{b d} d^5 \operatorname{abs}(b))$$

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(b x + a)^{\frac{9}{2}}}{(d x + c)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(9/2)/(d*x+c)^(5/2),x)

[Out] int((b*x+a)^(9/2)/(d*x+c)^(5/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(9/2)/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + b x)^{9/2}}{(c + d x)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(9/2)/(c + d*x)^(5/2),x)

[Out] int((a + b*x)^(9/2)/(c + d*x)^(5/2), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(9/2)/(d*x+c)**(5/2),x)
```

```
[Out] Timed out
```

$$3.1513 \quad \int \frac{(a+bx)^{7/2}}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=170

$$\frac{35b^{3/2}(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{4d^{9/2}} - \frac{35b^2\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}{4d^4} + \frac{35b^2(a+bx)^{3/2}\sqrt{c+dx}}{6d^3} - \frac{14b(a+bx)^{5/2}}{3d^2\sqrt{c+dx}}$$

[Out] $-2/3*(b*x+a)^{(7/2)}/d/(d*x+c)^{(3/2)}+35/4*b^{(3/2)}*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/d^{(9/2)}-14/3*b*(b*x+a)^{(5/2)}/d^2/(d*x+c)^{(1/2)}+35/6*b^2*(b*x+a)^{(3/2)}*(d*x+c)^{(1/2)}/d^3-35/4*b^2*(-a*d+b*c)*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/d^4$

Rubi [A] time = 0.08, antiderivative size = 170, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 217, 206}

$$\frac{35b^2(a+bx)^{3/2}\sqrt{c+dx}}{6d^3} - \frac{35b^2\sqrt{a+bx}\sqrt{c+dx}(bc-ad)}{4d^4} + \frac{35b^{3/2}(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{4d^{9/2}} - \frac{14b(a+bx)^{5/2}}{3d^2\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/2)/(c + d*x)^(5/2), x]

[Out] $(-2*(a + b*x)^{(7/2)})/(3*d*(c + d*x)^{(3/2)}) - (14*b*(a + b*x)^{(5/2)})/(3*d^2*\operatorname{Sqrt}[c + d*x]) - (35*b^2*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/(4*d^4) + (35*b^2*(a + b*x)^{(3/2)}*\operatorname{Sqrt}[c + d*x])/(6*d^3) + (35*b^{(3/2)}*(b*c - a*d)^2*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/(4*d^{(9/2)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ

$[m, 0] \&\& (!\text{IntegerQ}[n] \parallel (\text{GtQ}[m, 0] \&\& \text{LtQ}[m - n, 0])) \&\& !\text{ILtQ}[m + n + 2, 0] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\text{Int}[(a_.) + (b_.)(x_)^m)((c_.) + (d_.)(x_)^n], x_Symbol] \text{ :> With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{p(m+1)-1}(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{1/p}], x]] \text{ /; FreeQ}[\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 206

$\text{Int}[(a_) + (b_)(x_)^2]^{-1}, x_Symbol] \text{ :> Simp}[(1*\text{ArcTanh}[\text{Rt}[-b, 2]*x]/\text{Rt}[a, 2])]/(\text{Rt}[a, 2]*\text{Rt}[-b, 2]), x] \text{ /; FreeQ}[\{a, b\}, x] \&\& \text{NegQ}[a/b] \&\& (\text{GtQ}[a, 0] \parallel \text{LtQ}[b, 0])$

Rule 217

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)(x_)^2], x_Symbol] \text{ :> Subst}[\text{Int}[1/(1 - b*x^2), x], x, x/\text{Sqrt}[a + b*x^2]] \text{ /; FreeQ}[\{a, b\}, x] \&\& !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/2}}{(c+dx)^{5/2}} dx &= -\frac{2(a+bx)^{7/2}}{3d(c+dx)^{3/2}} + \frac{(7b) \int \frac{(a+bx)^{5/2}}{(c+dx)^{3/2}} dx}{3d} \\
&= -\frac{2(a+bx)^{7/2}}{3d(c+dx)^{3/2}} - \frac{14b(a+bx)^{5/2}}{3d^2\sqrt{c+dx}} + \frac{(35b^2) \int \frac{(a+bx)^{3/2}}{\sqrt{c+dx}} dx}{3d^2} \\
&= -\frac{2(a+bx)^{7/2}}{3d(c+dx)^{3/2}} - \frac{14b(a+bx)^{5/2}}{3d^2\sqrt{c+dx}} + \frac{35b^2(a+bx)^{3/2}\sqrt{c+dx}}{6d^3} - \frac{(35b^2(bc-ad)) \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{4d^3} \\
&= -\frac{2(a+bx)^{7/2}}{3d(c+dx)^{3/2}} - \frac{14b(a+bx)^{5/2}}{3d^2\sqrt{c+dx}} - \frac{35b^2(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^4} + \frac{35b^2(a+bx)^{3/2}\sqrt{c+dx}}{6d^3} \\
&= -\frac{2(a+bx)^{7/2}}{3d(c+dx)^{3/2}} - \frac{14b(a+bx)^{5/2}}{3d^2\sqrt{c+dx}} - \frac{35b^2(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^4} + \frac{35b^2(a+bx)^{3/2}\sqrt{c+dx}}{6d^3} \\
&= -\frac{2(a+bx)^{7/2}}{3d(c+dx)^{3/2}} - \frac{14b(a+bx)^{5/2}}{3d^2\sqrt{c+dx}} - \frac{35b^2(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^4} + \frac{35b^2(a+bx)^{3/2}\sqrt{c+dx}}{6d^3} \\
&= -\frac{2(a+bx)^{7/2}}{3d(c+dx)^{3/2}} - \frac{14b(a+bx)^{5/2}}{3d^2\sqrt{c+dx}} - \frac{35b^2(bc-ad)\sqrt{a+bx}\sqrt{c+dx}}{4d^4} + \frac{35b^2(a+bx)^{3/2}\sqrt{c+dx}}{6d^3}
\end{aligned}$$

Mathematica [C] time = 0.08, size = 73, normalized size = 0.43

$$\frac{2(a+bx)^{9/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/2} {}_2F_1 \left(\frac{5}{2}, \frac{9}{2}; \frac{11}{2}; \frac{d(a+bx)}{ad-bc} \right)}{9b(c+dx)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/2)/(c + d*x)^(5/2), x]

[Out] (2*(a + b*x)^(9/2)*((b*(c + d*x))/(b*c - a*d))^(5/2)*Hypergeometric2F1[5/2, 9/2, 11/2, (d*(a + b*x))/(-b*c + a*d)])/(9*b*(c + d*x)^(5/2))

fricas [B] time = 0.93, size = 657, normalized size = 3.86

$$\frac{105(b^3c^4 - 2ab^2c^3d + a^2bc^2d^2 + (b^3c^2d^2 - 2ab^2cd^3 + a^2bd^4)x^2 + 2(b^3c^3d - 2ab^2c^2d^2 + a^2bcd^3)x)\sqrt{\frac{b}{d}} \log(8\sqrt{\frac{b}{d}})}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(5/2),x, algorithm="fricas")

[Out] [1/48*(105*(b^3*c^4 - 2*a*b^2*c^3*d + a^2*b*c^2*d^2 + (b^3*c^2*d^2 - 2*a*b^2*c*d^3 + a^2*b*d^4)*x^2 + 2*(b^3*c^3*d - 2*a*b^2*c^2*d^2 + a^2*b*c*d^3)*x)*sqrt(b/d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d^2*x + b*c*d + a*d^2)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(b/d) + 8*(b^2*c*d + a*b*d^2)*x) + 4*(6*b^3*d^3*x^3 - 105*b^3*c^3 + 175*a*b^2*c^2*d - 56*a^2*b*c*d^2 - 8*a^3*d^3 - 3*(7*b^3*c*d^2 - 13*a*b^2*d^3)*x^2 - 2*(70*b^3*c^2*d - 119*a*b^2*c*d^2 + 40*a^2*b*d^3)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(d^6*x^2 + 2*c*d^5*x + c^2*d^4), -1/24*(105*(b^3*c^4 - 2*a*b^2*c^3*d + a^2*b*c^2*d^2 + (b^3*c^2*d^2 - 2*a*b^2*c*d^3 + a^2*b*d^4)*x^2 + 2*(b^3*c^3*d - 2*a*b^2*c^2*d^2 + a^2*b*c*d^3)*x)*sqrt(-b/d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-b/d)/(b^2*d*x^2 + a*b*c + (b^2*c + a*b*d)*x)) - 2*(6*b^3*d^3*x^3 - 105*b^3*c^3 + 175*a*b^2*c^2*d - 56*a^2*b*c*d^2 - 8*a^3*d^3 - 3*(7*b^3*c*d^2 - 13*a*b^2*d^3)*x^2 - 2*(70*b^3*c^2*d - 119*a*b^2*c*d^2 + 40*a^2*b*d^3)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(d^6*x^2 + 2*c*d^5*x + c^2*d^4)]

giac [B] time = 2.14, size = 380, normalized size = 2.24

$$\frac{\left(3(bx + a)\left(\frac{2(b^6cd^6 - ab^5d^7)(bx+a)}{b^2cd^7|b| - abd^8|b|} - \frac{7(b^7c^2d^5 - 2ab^6cd^6 + a^2b^5d^7)}{b^2cd^7|b| - abd^8|b|}\right) - \frac{140(b^8c^3d^4 - 3ab^7c^2d^5 + 3a^2b^6cd^6 - a^3b^5d^7)}{b^2cd^7|b| - abd^8|b|}\right)(bx + a) - \frac{105(b^9c^4d^3 - 4a^8b^8c^3d^4 + 6a^7b^7c^2d^5 - 4a^6b^6c^2d^6 + a^5b^5d^7)}{b^2cd^7|b| - abd^8|b|}}{12(b^2c + (bx + a)bd - abd)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(5/2),x, algorithm="giac")

[Out] 1/12*((3*(b*x + a)*(2*(b^6*c*d^6 - a*b^5*d^7)*(b*x + a)/(b^2*c*d^7*abs(b) - a*b*d^8*abs(b)) - 7*(b^7*c^2*d^5 - 2*a*b^6*c*d^6 + a^2*b^5*d^7)/(b^2*c*d^7*abs(b) - a*b*d^8*abs(b))) - 140*(b^8*c^3*d^4 - 3*a*b^7*c^2*d^5 + 3*a^2*b^6*c*d^6 - a^3*b^5*d^7)/(b^2*c*d^7*abs(b) - a*b*d^8*abs(b)))*(b*x + a) - 105*(b^9*c^4*d^3 - 4*a*b^8*c^3*d^4 + 6*a^2*b^7*c^2*d^5 - 4*a^3*b^6*c*d^6 + a^4*b^5*d^7)/(b^2*c*d^7*abs(b) - a*b*d^8*abs(b))*sqrt(b*x + a)/(b^2*c + (b*x + a)*b*d - a*b*d)^(3/2) - 35/4*(b^5*c^2 - 2*a*b^4*c*d + a^2*b^3*d^2)*log(abs

$(-\sqrt{b*d}*\sqrt{b*x + a} + \sqrt{b^2*c + (b*x + a)*b*d - a*b*d}))/(\sqrt{b*d})*d^4*abs(b))$

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{2}}}{(dx + c)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/2)/(d*x+c)^(5/2),x)

[Out] int((b*x+a)^(7/2)/(d*x+c)^(5/2),x)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{7/2}}{(c + dx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/2)/(c + d*x)^(5/2),x)

[Out] int((a + b*x)^(7/2)/(c + d*x)^(5/2), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/2)/(d*x+c)**(5/2),x)

[Out] Timed out

$$3.1514 \quad \int \frac{(a+bx)^{5/2}}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=128

$$-\frac{5b^{3/2}(bc-ad)\tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{7/2}} + \frac{5b^2\sqrt{a+bx}\sqrt{c+dx}}{d^3} - \frac{10b(a+bx)^{3/2}}{3d^2\sqrt{c+dx}} - \frac{2(a+bx)^{5/2}}{3d(c+dx)^{3/2}}$$

[Out] $-2/3*(b*x+a)^{(5/2)}/d/(d*x+c)^{(3/2)}-5*b^{(3/2)}*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)}/(d*x+c)^{(1/2)})/d^{(7/2)}-10/3*b*(b*x+a)^{(3/2)}/d^2/(d*x+c)^{(1/2)}+5*b^2*(b*x+a)^{(1/2)}*(d*x+c)^{(1/2)}/d^3$

Rubi [A] time = 0.06, antiderivative size = 128, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 217, 206}

$$\frac{5b^2\sqrt{a+bx}\sqrt{c+dx}}{d^3} - \frac{5b^{3/2}(bc-ad)\tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{7/2}} - \frac{10b(a+bx)^{3/2}}{3d^2\sqrt{c+dx}} - \frac{2(a+bx)^{5/2}}{3d(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2)/(c + d*x)^(5/2), x]

[Out] $(-2*(a + b*x)^{(5/2)})/(3*d*(c + d*x)^{(3/2)}) - (10*b*(a + b*x)^{(3/2)})/(3*d^2*\operatorname{Sqrt}[c + d*x]) + (5*b^2*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[c + d*x])/d^3 - (5*b^{(3/2)}*(b*c - a*d)*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x])])/d^{(7/2)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/
Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (Gt
Q[a, 0] || LtQ[b, 0])
```

Rule 217

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x],
x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{(c+dx)^{5/2}} dx &= -\frac{2(a+bx)^{5/2}}{3d(c+dx)^{3/2}} + \frac{(5b) \int \frac{(a+bx)^{3/2}}{(c+dx)^{3/2}} dx}{3d} \\
&= -\frac{2(a+bx)^{5/2}}{3d(c+dx)^{3/2}} - \frac{10b(a+bx)^{3/2}}{3d^2\sqrt{c+dx}} + \frac{(5b^2) \int \frac{\sqrt{a+bx}}{\sqrt{c+dx}} dx}{d^2} \\
&= -\frac{2(a+bx)^{5/2}}{3d(c+dx)^{3/2}} - \frac{10b(a+bx)^{3/2}}{3d^2\sqrt{c+dx}} + \frac{5b^2\sqrt{a+bx}\sqrt{c+dx}}{d^3} - \frac{(5b^2(bc-ad)) \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{2d^3} \\
&= -\frac{2(a+bx)^{5/2}}{3d(c+dx)^{3/2}} - \frac{10b(a+bx)^{3/2}}{3d^2\sqrt{c+dx}} + \frac{5b^2\sqrt{a+bx}\sqrt{c+dx}}{d^3} - \frac{(5b(bc-ad)) \text{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x\right)}{d^3} \\
&= -\frac{2(a+bx)^{5/2}}{3d(c+dx)^{3/2}} - \frac{10b(a+bx)^{3/2}}{3d^2\sqrt{c+dx}} + \frac{5b^2\sqrt{a+bx}\sqrt{c+dx}}{d^3} - \frac{(5b(bc-ad)) \text{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x\right)}{d^3} \\
&= -\frac{2(a+bx)^{5/2}}{3d(c+dx)^{3/2}} - \frac{10b(a+bx)^{3/2}}{3d^2\sqrt{c+dx}} + \frac{5b^2\sqrt{a+bx}\sqrt{c+dx}}{d^3} - \frac{5b^{3/2}(bc-ad) \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.08, size = 73, normalized size = 0.57

$$\frac{2(a+bx)^{7/2} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/2} {}_2F_1\left(\frac{5}{2}, \frac{7}{2}; \frac{9}{2}; \frac{d(a+bx)}{ad-bc}\right)}{7b(c+dx)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/(c + d*x)^(5/2), x]

[Out] (2*(a + b*x)^(7/2)*((b*(c + d*x))/(b*c - a*d))^(5/2)*Hypergeometric2F1[5/2, 7/2, 9/2, (d*(a + b*x))/(-b*c) + a*d])/(7*b*(c + d*x)^(5/2))

fricas [B] time = 0.73, size = 475, normalized size = 3.71

$$\left[\frac{15(b^2c^3 - abc^2d + (b^2cd^2 - abd^3)x^2 + 2(b^2c^2d - abcd^2)x)\sqrt{\frac{b}{d}} \log\left(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bdx + c^2)\sqrt{\frac{b}{d}}\right)}{\dots} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(5/2), x, algorithm="fricas")

[Out] [-1/12*(15*(b^2*c^3 - a*b*c^2*d + (b^2*c*d^2 - a*b*d^3)*x^2 + 2*(b^2*c^2*d - a*b*c*d^2)*x)*sqrt(b/d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d^2*x + b*c*d + a*d^2)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(b/d) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(3*b^2*d^2*x^2 + 15*b^2*c^2 - 10*a*b*c*d - 2*a^2*d^2 + 2*(10*b^2*c*d - 7*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(d^5*x^2 + 2*c*d^4*x + c^2*d^3), 1/6*(15*(b^2*c^3 - a*b*c^2*d + (b^2*c*d^2 - a*b*d^3)*x^2 + 2*(b^2*c^2*d - a*b*c*d^2)*x)*sqrt(-b/d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-b/d)/(b^2*d*x^2 + a*b*c + (b^2*c + a*b*d)*x)) + 2*(3*b^2*d^2*x^2 + 15*b^2*c^2 - 10*a*b*c*d - 2*a^2*d^2 + 2*(10*b^2*c*d - 7*a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c))/(d^5*x^2 + 2*c*d^4*x + c^2*d^3)]

giac [B] time = 1.97, size = 276, normalized size = 2.16

$$\frac{\left((bx+a)\left(\frac{3(b^6cd^4-ab^5d^5)(bx+a)}{b^2cd^5|b|-abd^6|b|} + \frac{20(b^7c^2d^3-2ab^6cd^4+a^2b^5d^5)}{b^2cd^5|b|-abd^6|b|}\right) + \frac{15(b^8c^3d^2-3ab^7c^2d^3+3a^2b^6cd^4-a^3b^5d^5)}{b^2cd^5|b|-abd^6|b|}\right)\sqrt{bx+a}}{3(b^2c+(bx+a)bd-abd)^{\frac{3}{2}}} + \frac{5(b^4c-abd)}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(5/2), x, algorithm="giac")

```
[Out] 1/3*((b*x + a)*(3*(b^6*c*d^4 - a*b^5*d^5)*(b*x + a)/(b^2*c*d^5*abs(b) - a*b*d^6*abs(b)) + 20*(b^7*c^2*d^3 - 2*a*b^6*c*d^4 + a^2*b^5*d^5)/(b^2*c*d^5*abs(b) - a*b*d^6*abs(b))) + 15*(b^8*c^3*d^2 - 3*a*b^7*c^2*d^3 + 3*a^2*b^6*c*d^4 - a^3*b^5*d^5)/(b^2*c*d^5*abs(b) - a*b*d^6*abs(b))*sqrt(b*x + a)/(b^2*c + (b*x + a)*b*d - a*b*d)^(3/2) + 5*(b^4*c - a*b^3*d)*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/(sqrt(b*d)*d^3*abs(b))
```

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((b*x+a)^(5/2)/(d*x+c)^(5/2),x)
```

```
[Out] int((b*x+a)^(5/2)/(d*x+c)^(5/2),x)
```

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(5/2)/(d*x+c)^(5/2),x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?
```

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{5/2}}{(c + dx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(5/2)/(c + d*x)^(5/2),x)
```

```
[Out] int((a + b*x)^(5/2)/(c + d*x)^(5/2), x)
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(5/2)/(d*x+c)**(5/2),x)
```

```
[Out] Timed out
```

$$3.1515 \quad \int \frac{(a+bx)^{3/2}}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=92

$$\frac{2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{5/2}} - \frac{2b\sqrt{a+bx}}{d^2\sqrt{c+dx}} - \frac{2(a+bx)^{3/2}}{3d(c+dx)^{3/2}}$$

[Out] $-2/3*(b*x+a)^{(3/2)}/d/(d*x+c)^{(3/2)}+2*b^{(3/2)}*\operatorname{arctanh}(d^{(1/2)}*(b*x+a)^{(1/2)}/b^{(1/2)/(d*x+c)^{(1/2)})/d^{(5/2)}-2*b*(b*x+a)^{(1/2)}/d^2/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 63, 217, 206}

$$\frac{2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{5/2}} - \frac{2b\sqrt{a+bx}}{d^2\sqrt{c+dx}} - \frac{2(a+bx)^{3/2}}{3d(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] `Int[(a + b*x)^(3/2)/(c + d*x)^(5/2), x]`

[Out] $(-2*(a + b*x)^{(3/2)})/(3*d*(c + d*x)^{(3/2)}) - (2*b*\operatorname{Sqrt}[a + b*x])/(d^2*\operatorname{Sqrt}[c + d*x]) + (2*b^{(3/2)}*\operatorname{ArcTanh}[(\operatorname{Sqrt}[d]*\operatorname{Sqrt}[a + b*x])]/(\operatorname{Sqrt}[b]*\operatorname{Sqrt}[c + d*x]))/d^{(5/2)}$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 206

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(1*ArcTanh[(Rt[-b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && NegQ[a/b] && (GtQ[a, 0] || LtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{3/2}}{(c+dx)^{5/2}} dx &= -\frac{2(a+bx)^{3/2}}{3d(c+dx)^{3/2}} + \frac{b \int \frac{\sqrt{a+bx}}{(c+dx)^{3/2}} dx}{d} \\
 &= -\frac{2(a+bx)^{3/2}}{3d(c+dx)^{3/2}} - \frac{2b\sqrt{a+bx}}{d^2\sqrt{c+dx}} + \frac{b^2 \int \frac{1}{\sqrt{a+bx}\sqrt{c+dx}} dx}{d^2} \\
 &= -\frac{2(a+bx)^{3/2}}{3d(c+dx)^{3/2}} - \frac{2b\sqrt{a+bx}}{d^2\sqrt{c+dx}} + \frac{(2b) \operatorname{Subst}\left(\int \frac{1}{\sqrt{c-\frac{ad}{b}+\frac{dx^2}{b}}} dx, x, \sqrt{a+bx}\right)}{d^2} \\
 &= -\frac{2(a+bx)^{3/2}}{3d(c+dx)^{3/2}} - \frac{2b\sqrt{a+bx}}{d^2\sqrt{c+dx}} + \frac{(2b) \operatorname{Subst}\left(\int \frac{1}{1-\frac{dx^2}{b}} dx, x, \frac{\sqrt{a+bx}}{\sqrt{c+dx}}\right)}{d^2} \\
 &= -\frac{2(a+bx)^{3/2}}{3d(c+dx)^{3/2}} - \frac{2b\sqrt{a+bx}}{d^2\sqrt{c+dx}} + \frac{2b^{3/2} \tanh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{d^{5/2}}
 \end{aligned}$$

Mathematica [A] time = 0.55, size = 111, normalized size = 1.21

$$\frac{6(bc-ad)^{3/2} \left(\frac{b(c+dx)}{bc-ad}\right)^{3/2} \sinh^{-1}\left(\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{bc-ad}}\right) - 2\sqrt{d}\sqrt{a+bx}(ad+3bc+4bdx)}{3d^{5/2}(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(5/2), x]

[Out] (-2*Sqrt[d]*Sqrt[a + b*x]*(3*b*c + a*d + 4*b*d*x) + 6*(b*c - a*d)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(3/2)*ArcSinh[(Sqrt[d]*Sqrt[a + b*x])/Sqrt[b*c - a*d]])/(3*d^(5/2)*(c + d*x)^(3/2))

fricas [B] time = 0.63, size = 325, normalized size = 3.53

$$\frac{3(bd^2x^2 + 2bcdx + bc^2)\sqrt{\frac{b}{d}} \log\left(8b^2d^2x^2 + b^2c^2 + 6abcd + a^2d^2 + 4(2bd^2x + bcd + ad^2)\sqrt{bx+a}\sqrt{dx+c}\sqrt{\frac{b}{d}}\right)}{6(d^4x^2 + 2cd^3x + c^2d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(5/2),x, algorithm="fricas")

[Out] [1/6*(3*(b*d^2*x^2 + 2*b*c*d*x + b*c^2)*sqrt(b/d)*log(8*b^2*d^2*x^2 + b^2*c^2 + 6*a*b*c*d + a^2*d^2 + 4*(2*b*d^2*x + b*c*d + a*d^2)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(b/d) + 8*(b^2*c*d + a*b*d^2)*x) - 4*(4*b*d*x + 3*b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c))/(d^4*x^2 + 2*c*d^3*x + c^2*d^2), -1/3*(3*(b*d^2*x^2 + 2*b*c*d*x + b*c^2)*sqrt(-b/d)*arctan(1/2*(2*b*d*x + b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c)*sqrt(-b/d)/(b^2*d*x^2 + a*b*c + (b^2*c + a*b*d)*x) + 2*(4*b*d*x + 3*b*c + a*d)*sqrt(b*x + a)*sqrt(d*x + c))/(d^4*x^2 + 2*c*d^3*x + c^2*d^2)]

giac [B] time = 1.43, size = 181, normalized size = 1.97

$$\frac{2b^3 \log\left(\left|-\sqrt{bd}\sqrt{bx+a} + \sqrt{b^2c + (bx+a)bd - abd}\right|\right)}{\sqrt{bd}d^2|b|} - \frac{2\sqrt{bx+a}\left(\frac{4(b^5cd^2 - ab^4d^3)(bx+a)}{bcd^3|b| - ad^4|b|} + \frac{3(b^6c^2d - 2ab^5cd^2 + a^2b^4d^3)}{bcd^3|b| - ad^4|b|}\right)}{3(b^2c + (bx+a)bd - abd)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(5/2),x, algorithm="giac")

[Out] -2*b^3*log(abs(-sqrt(b*d)*sqrt(b*x + a) + sqrt(b^2*c + (b*x + a)*b*d - a*b*d)))/(sqrt(b*d)*d^2*abs(b)) - 2/3*sqrt(b*x + a)*(4*(b^5*c*d^2 - a*b^4*d^3)*(b*x + a)/(b*c*d^3*abs(b) - a*d^4*abs(b)) + 3*(b^6*c^2*d - 2*a*b^5*c*d^2 + a^2*b^4*d^3)/(b*c*d^3*abs(b) - a*d^4*abs(b)))/(b^2*c + (b*x + a)*b*d - a*b*d)^(3/2)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(3/2)/(d*x+c)^(5/2),x)`

[Out] `int((b*x+a)^(3/2)/(d*x+c)^(5/2),x)`

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/2)/(d*x+c)^(5/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see 'assume?' for more details)Is a*d-b*c zero or nonzero?

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{3/2}}{(c + dx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(3/2)/(c + d*x)^(5/2),x)`

[Out] `int((a + b*x)^(3/2)/(c + d*x)^(5/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{(c + dx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(3/2)/(d*x+c)**(5/2),x)`

[Out] `Integral((a + b*x)**(3/2)/(c + d*x)**(5/2), x)`

$$3.1516 \quad \int \frac{\sqrt{a+bx}}{(c+dx)^{5/2}} dx$$

Optimal. Leaf size=32

$$\frac{2(a+bx)^{3/2}}{3(c+dx)^{3/2}(bc-ad)}$$

[Out] $2/3*(b*x+a)^{(3/2)/(-a*d+b*c)/(d*x+c)^{(3/2)}$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{2(a+bx)^{3/2}}{3(c+dx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/(c + d*x)^(5/2), x]

[Out] $(2*(a + b*x)^{(3/2)})/(3*(b*c - a*d)*(c + d*x)^{(3/2)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp [((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{5/2}} dx = \frac{2(a+bx)^{3/2}}{3(bc-ad)(c+dx)^{3/2}}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 1.00

$$\frac{2(a+bx)^{3/2}}{3(c+dx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(5/2), x]

[Out] $(2*(a + b*x)^{(3/2)})/(3*(b*c - a*d)*(c + d*x)^{(3/2)})$

fricas [B] time = 0.54, size = 65, normalized size = 2.03

$$\frac{2(bx+a)^{\frac{3}{2}}\sqrt{dx+c}}{3(bc^3-ac^2d+(bcd^2-ad^3)x^2+2(bc^2d-acd^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(5/2),x, algorithm="fricas")

[Out] 2/3*(b*x + a)^(3/2)*sqrt(d*x + c)/(b*c^3 - a*c^2*d + (b*c*d^2 - a*d^3)*x^2 + 2*(b*c^2*d - a*c*d^2)*x)

giac [A] time = 1.15, size = 51, normalized size = 1.59

$$\frac{2(bx+a)^{\frac{3}{2}}b^4d}{3(bcd|b| - ad^2|b|)(b^2c + (bx+a)bd - abd)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(5/2),x, algorithm="giac")

[Out] 2/3*(b*x + a)^(3/2)*b^4*d/((b*c*d*abs(b) - a*d^2*abs(b))*(b^2*c + (b*x + a)*b*d - a*b*d)^(3/2))

maple [A] time = 0.00, size = 27, normalized size = 0.84

$$-\frac{2(bx+a)^{\frac{3}{2}}}{3(dx+c)^{\frac{3}{2}}(ad-bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(5/2),x)

[Out] -2/3*(b*x+a)^(3/2)/(d*x+c)^(3/2)/(a*d-b*c)

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* h

elp (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details) Is a*d-b*c zero or nonzero?

mupad [B] time = 0.56, size = 130, normalized size = 4.06

$$\frac{\left(\frac{2a\sqrt{a+bx}}{3ad^3-3bcd^2} + \frac{2bx\sqrt{a+bx}}{3ad^3-3bcd^2}\right)\sqrt{c+dx}}{x^2 - \frac{3bc^3-3ac^2d}{3ad^3-3bcd^2} + \frac{6cdx(ad-bc)}{3ad^3-3bcd^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(5/2), x)

[Out] -(((2*a*(a + b*x)^(1/2))/(3*a*d^3 - 3*b*c*d^2) + (2*b*x*(a + b*x)^(1/2))/(3*a*d^3 - 3*b*c*d^2))*(c + d*x)^(1/2))/(x^2 - (3*b*c^3 - 3*a*c^2*d)/(3*a*d^3 - 3*b*c*d^2) + (6*c*d*x*(a*d - b*c))/(3*a*d^3 - 3*b*c*d^2))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(5/2), x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(5/2), x)

$$3.1517 \quad \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/2}} dx$$

Optimal. Leaf size=66

$$\frac{4b\sqrt{a+bx}}{3\sqrt{c+dx}(bc-ad)^2} + \frac{2\sqrt{a+bx}}{3(c+dx)^{3/2}(bc-ad)}$$

[Out] $2/3*(b*x+a)^{(1/2)/(-a*d+b*c)/(d*x+c)^{(3/2)+4/3*b*(b*x+a)^{(1/2)/(-a*d+b*c)^2/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{4b\sqrt{a+bx}}{3\sqrt{c+dx}(bc-ad)^2} + \frac{2\sqrt{a+bx}}{3(c+dx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(5/2)),x]

[Out] $(2*\text{Sqrt}[a + b*x])/(3*(b*c - a*d)*(c + d*x)^{(3/2)}) + (4*b*\text{Sqrt}[a + b*x])/(3*(b*c - a*d)^2*\text{Sqrt}[c + d*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{5/2}} dx = \frac{2\sqrt{a+bx}}{3(bc-ad)(c+dx)^{3/2}} + \frac{(2b) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/2}} dx}{3(bc-ad)}$$

$$= \frac{2\sqrt{a+bx}}{3(bc-ad)(c+dx)^{3/2}} + \frac{4b\sqrt{a+bx}}{3(bc-ad)^2\sqrt{c+dx}}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.70

$$\frac{2\sqrt{a+bx}(-ad+3bc+2bdx)}{3(c+dx)^{3/2}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(5/2)),x]

[Out] (2*Sqrt[a + b*x]*(3*b*c - a*d + 2*b*d*x))/(3*(b*c - a*d)^2*(c + d*x)^(3/2))

fricas [B] time = 0.60, size = 118, normalized size = 1.79

$$\frac{2(2bdx + 3bc - ad)\sqrt{bx+a}\sqrt{dx+c}}{3(b^2c^4 - 2abc^3d + a^2c^2d^2 + (b^2c^2d^2 - 2abcd^3 + a^2d^4)x^2 + 2(b^2c^3d - 2abc^2d^2 + a^2cd^3)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(5/2),x, algorithm="fricas")

[Out] 2/3*(2*b*d*x + 3*b*c - a*d)*sqrt(b*x + a)*sqrt(d*x + c)/(b^2*c^4 - 2*a*b*c^3*d + a^2*c^2*d^2 + (b^2*c^2*d^2 - 2*a*b*c*d^3 + a^2*d^4)*x^2 + 2*(b^2*c^3*d - 2*a*b*c^2*d^2 + a^2*c*d^3)*x)

giac [B] time = 1.02, size = 126, normalized size = 1.91

$$\frac{2\left(\frac{2(bx+a)b^4d^2}{b^2c^2d|b|-2abcd^2|b|+a^2d^3|b|} + \frac{3(b^5cd-ab^4d^2)}{b^2c^2d|b|-2abcd^2|b|+a^2d^3|b|}\right)\sqrt{bx+a}}{3\left(b^2c+(bx+a)bd-abd\right)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(5/2),x, algorithm="giac")

[Out] 2/3*(2*(b*x + a)*b^4*d^2/(b^2*c^2*d*abs(b) - 2*a*b*c*d^2*abs(b) + a^2*d^3*a*bs(b)) + 3*(b^5*c*d - a*b^4*d^2)/(b^2*c^2*d*abs(b) - 2*a*b*c*d^2*abs(b) + a^2*d^3*abs(b)))*sqrt(b*x + a)/(b^2*c + (b*x + a)*b*d - a*b*d)^(3/2)

maple [A] time = 0.00, size = 53, normalized size = 0.80

$$\frac{2\sqrt{bx+a}(-2bdx+ad-3bc)}{3(dx+c)^{\frac{3}{2}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(5/2),x)

[Out] $-2/3*(b*x+a)^{(1/2)}*(-2*b*d*x+a*d-3*b*c)/(d*x+c)^{(3/2)}/(a^2*d^2-2*a*b*c*d+b^2*c^2)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 0.90, size = 127, normalized size = 1.92

$$\frac{\sqrt{c+dx} \left(\frac{x(6cb^2+2adb)}{3d^2(ad-bc)^2} - \frac{2a^2d-6abc}{3d^2(ad-bc)^2} + \frac{4b^2x^2}{3d(ad-bc)^2} \right)}{x^2 \sqrt{a+bx} + \frac{c^2 \sqrt{a+bx}}{d^2} + \frac{2cx \sqrt{a+bx}}{d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a+b*x)^(1/2)*(c+d*x)^(5/2)),x)

[Out] $((c+d*x)^{(1/2)}*((x*(6*b^2*c+2*a*b*d))/(3*d^2*(a*d-b*c)^2) - (2*a^2*d-6*a*b*c)/(3*d^2*(a*d-b*c)^2) + (4*b^2*x^2)/(3*d*(a*d-b*c)^2))/(x^2*(a+b*x)^{(1/2)} + (c^2*(a+b*x)^{(1/2)})/d^2 + (2*c*x*(a+b*x)^{(1/2)})/d)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a+bx} (c+dx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(1/2)/(d*x+c)**(5/2),x)
```

```
[Out] Integral(1/(sqrt(a + b*x)*(c + d*x)**(5/2)), x)
```

$$3.1518 \quad \int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/2}} dx$$

Optimal. Leaf size=98

$$-\frac{16bd\sqrt{a+bx}}{3\sqrt{c+dx}(bc-ad)^3} - \frac{8d\sqrt{a+bx}}{3(c+dx)^{3/2}(bc-ad)^2} - \frac{2}{\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)}$$

[Out] $-2/(-a*d+b*c)/(d*x+c)^{(3/2)}/(b*x+a)^{(1/2)}-8/3*d*(b*x+a)^{(1/2)/(-a*d+b*c)^2/(d*x+c)^{(3/2)}-16/3*b*d*(b*x+a)^{(1/2)/(-a*d+b*c)^3/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{16bd\sqrt{a+bx}}{3\sqrt{c+dx}(bc-ad)^3} - \frac{8d\sqrt{a+bx}}{3(c+dx)^{3/2}(bc-ad)^2} - \frac{2}{\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/2)*(c + d*x)^(5/2)), x]

[Out] $-2/((b*c - a*d)*\text{Sqrt}[a + b*x]*(c + d*x)^{(3/2)}) - (8*d*\text{Sqrt}[a + b*x])/(3*(b*c - a*d)^2*(c + d*x)^{(3/2)}) - (16*b*d*\text{Sqrt}[a + b*x])/(3*(b*c - a*d)^3*\text{Sqrt}[c + d*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/2}} dx &= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{3/2}} - \frac{(4d) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/2}} dx}{bc-ad} \\ &= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{3/2}} - \frac{8d\sqrt{a+bx}}{3(bc-ad)^2(c+dx)^{3/2}} - \frac{(8bd) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/2}} dx}{3(bc-ad)^2} \\ &= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{3/2}} - \frac{8d\sqrt{a+bx}}{3(bc-ad)^2(c+dx)^{3/2}} - \frac{16bd\sqrt{a+bx}}{3(bc-ad)^3\sqrt{c+dx}} \end{aligned}$$

Mathematica [A] time = 0.03, size = 78, normalized size = 0.80

$$\frac{2a^2d^2 - 4abd(3c + 2dx) - 2b^2(3c^2 + 12cdx + 8d^2x^2)}{3\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(5/2)), x]

[Out] (2*a^2*d^2 - 4*a*b*d*(3*c + 2*d*x) - 2*b^2*(3*c^2 + 12*c*d*x + 8*d^2*x^2))/
(3*(b*c - a*d)^3*Sqrt[a + b*x]*(c + d*x)^(3/2))

fricas [B] time = 0.82, size = 273, normalized size = 2.79

$$\frac{2(8b^2d^2x^2 + 3b^2c^2 + 6abcd - a^2d^2 + 4(3b^2cd + 3(ab^3c^5 - 3a^2b^2c^4d + 3a^3bc^3d^2 - a^4c^2d^3 + (b^4c^3d^2 - 3ab^3c^2d^3 + 3a^2b^2cd^4 - a^3bd^5)x^3 + (2b^4c^4d - 5ab^3c^3d^2 + 3a^2b^2c^2d^3 + a^3b*c*d^4 - a^4*d^5)*x^2 + (b^4*c^5 - a*b^3*c^4*d - 3*a^2*b^2*c^3*d^2 + 5*a^3*b*c^2*d^3 - 2*a^4*c*d^4)*x))}{3\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(5/2), x, algorithm="fricas")

[Out] -2/3*(8*b^2*d^2*x^2 + 3*b^2*c^2 + 6*a*b*c*d - a^2*d^2 + 4*(3*b^2*c*d + a*b*d^2)*x)*sqrt(b*x + a)*sqrt(d*x + c)/(a*b^3*c^5 - 3*a^2*b^2*c^4*d + 3*a^3*b*c^3*d^2 - a^4*c^2*d^3 + (b^4*c^3*d^2 - 3*a*b^3*c^2*d^3 + 3*a^2*b^2*c*d^4 - a^3*b*d^5)*x^3 + (2*b^4*c^4*d - 5*a*b^3*c^3*d^2 + 3*a^2*b^2*c^2*d^3 + a^3*b*c*d^4 - a^4*d^5)*x^2 + (b^4*c^5 - a*b^3*c^4*d - 3*a^2*b^2*c^3*d^2 + 5*a^3*b*c^2*d^3 - 2*a^4*c*d^4)*x)

giac [B] time = 1.48, size = 373, normalized size = 3.81

$$\frac{4\sqrt{bd}b^3}{(b^2c^2|b| - 2abcd|b| + a^2d^2|b|)\left(b^2c - abd - \left(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - abd}\right)^2\right)} - \frac{2\sqrt{bx+a}\left(\frac{5(b^7c^5d - 5ab^6c^4}{b^7c^5d - 5ab^6c^4}\right)}{3\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(5/2),x, algorithm="giac")

[Out]
$$\frac{-4\sqrt{bd}b^3((b^2c^2\text{abs}(b) - 2ab^2cd\text{abs}(b) + a^2d^2\text{abs}(b))(b^2c - ab^2d - (\sqrt{bd})\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - ab^2d})^2) - 2/3\sqrt{bx+a}(5(b^6c^2d^3\text{abs}(b) - 2ab^5cd^4\text{abs}(b) + a^2b^4d^5\text{abs}(b))(bx+a)/(b^7c^5d - 5ab^6c^4d^2 + 10a^2b^5c^3d^3 - 10a^3b^4c^2d^4 + 5a^4b^3cd^5 - a^5b^2d^6) + 6(b^7c^3d^2\text{abs}(b) - 3ab^6c^2d^3\text{abs}(b) + 3a^2b^5cd^4\text{abs}(b) - a^3b^4d^5\text{abs}(b)))/(b^7c^5d - 5ab^6c^4d^2 + 10a^2b^5c^3d^3 - 10a^3b^4c^2d^4 + 5a^4b^3cd^5 - a^5b^2d^6))/(b^2c + (bx+a)bd - ab^2d)^{3/2}}$$

maple [A] time = 0.01, size = 104, normalized size = 1.06

$$\frac{2(-8b^2x^2d^2 - 4abd^2x - 12b^2cdx + a^2d^2 - 6abcd - 3b^2c^2)}{3\sqrt{bx+a}(dx+c)^{\frac{3}{2}}(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(5/2),x)

[Out]
$$-2/3*(-8b^2d^2x^2-4a^2bd^2x-12b^2cdx+a^2d^2-6abcd-3b^2c^2)/(b*x+a)^{1/2}/(d*x+c)^{3/2}/(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.03, size = 132, normalized size = 1.35

$$\frac{\sqrt{c+dx}\left(\frac{16b^2x^2}{3(ad-bc)^3} + \frac{-2a^2d^2+12abcd+6b^2c^2}{3d^2(ad-bc)^3} + \frac{8bx(ad+3bc)}{3d(ad-bc)^3}\right)}{x^2\sqrt{a+bx} + \frac{c^2\sqrt{a+bx}}{d^2} + \frac{2cx\sqrt{a+bx}}{d}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(5/2)),x)
```

```
[Out] ((c + d*x)^(1/2)*((16*b^2*x^2)/(3*(a*d - b*c)^3) + (6*b^2*c^2 - 2*a^2*d^2 +
  12*a*b*c*d)/(3*d^2*(a*d - b*c)^3) + (8*b*x*(a*d + 3*b*c))/(3*d*(a*d - b*c)
^3)))/(x^2*(a + b*x)^(1/2) + (c^2*(a + b*x)^(1/2))/d^2 + (2*c*x*(a + b*x)^(
1/2))/d)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} (c + dx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(5/2),x)
```

```
[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(5/2)), x)
```

$$3.1519 \quad \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx$$

Optimal. Leaf size=135

$$\frac{32bd^2\sqrt{a+bx}}{3\sqrt{c+dx}(bc-ad)^4} + \frac{16d^2\sqrt{a+bx}}{3(c+dx)^{3/2}(bc-ad)^3} + \frac{4d}{\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)^2} - \frac{2}{3(a+bx)^{3/2}(c+dx)^{3/2}(bc-ad)}$$

[Out] $-2/3/(-a*d+b*c)/(b*x+a)^{(3/2)/(d*x+c)^{(3/2)+4*d/(-a*d+b*c)^2/(d*x+c)^{(3/2)/(b*x+a)^{(1/2)+16/3*d^2*(b*x+a)^{(1/2)/(-a*d+b*c)^3/(d*x+c)^{(3/2)+32/3*b*d^2*(b*x+a)^{(1/2)/(-a*d+b*c)^4/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.03, antiderivative size = 135, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{32bd^2\sqrt{a+bx}}{3\sqrt{c+dx}(bc-ad)^4} + \frac{16d^2\sqrt{a+bx}}{3(c+dx)^{3/2}(bc-ad)^3} + \frac{4d}{\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)^2} - \frac{2}{3(a+bx)^{3/2}(c+dx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*(c + d*x)^(5/2)), x]

[Out] $-2/(3*(b*c - a*d)*(a + b*x)^{(3/2)*(c + d*x)^{(3/2)} + (4*d)/((b*c - a*d)^2*\text{Sqrt}[a + b*x]*(c + d*x)^{(3/2)} + (16*d^2*\text{Sqrt}[a + b*x])/3*(b*c - a*d)^3*(c + d*x)^{(3/2)} + (32*b*d^2*\text{Sqrt}[a + b*x])/3*(b*c - a*d)^4*\text{Sqrt}[c + d*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}(c+dx)^{3/2}} - \frac{(2d) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/2}} dx}{bc-ad} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}(c+dx)^{3/2}} + \frac{4d}{(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/2}} + \frac{(8d^2) \int \frac{1}{\sqrt{a+bx}}}{(bc-ad)^3} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}(c+dx)^{3/2}} + \frac{4d}{(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/2}} + \frac{16d^2 \sqrt{a+bx}}{3(bc-ad)^3 (c+dx)^{3/2}} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}(c+dx)^{3/2}} + \frac{4d}{(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/2}} + \frac{16d^2 \sqrt{a+bx}}{3(bc-ad)^3 (c+dx)^{3/2}}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 118, normalized size = 0.87

$$\frac{-2a^3d^3 + 6a^2bd^2(3c + 2dx) + 6ab^2d(3c^2 + 12cdx + 8d^2x^2) + b^3(-2c^3 + 12c^2dx + 48cd^2x^2 + 32d^3x^3)}{3(a+bx)^{3/2}(c+dx)^{3/2}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(5/2)), x]

[Out] $(-2a^3d^3 + 6a^2bd^2(3c + 2dx) + 6ab^2d(3c^2 + 12cdx + 8d^2x^2) + b^3(-2c^3 + 12c^2dx + 48cd^2x^2 + 32d^3x^3))/(3(bc-ad)^4(a+bx)^{3/2}(c+dx)^{3/2})$

fricas [B] time = 1.08, size = 447, normalized size = 3.31

$$\frac{2(16b^3d^3x^3 - b^3c^3 + 9a^2b^2c^2d + 9a^2b^2c^2d^2 - a^3d^3 + 24(b^3cd^2 + ab^2d^3)x^2 + 6(b^3c^2d + 6a^2b^2cd^2 + a^2b^2d^3)x) \sqrt{bx+a} \sqrt{dx+c}}{3(a^2b^4c^6 - 4a^3b^3c^5d + 6a^4b^2c^4d^2 - 4a^5b^2c^3d^3 + a^6c^2d^4 + (b^6c^4d^2 - 4ab^5c^3d^3 + 6a^2b^4c^2d^4 - 4a^3b^3cd^5 + a^4b^2d^6))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(5/2), x, algorithm="fricas")

[Out] $2/3(16b^3d^3x^3 - b^3c^3 + 9a^2b^2c^2d + 9a^2b^2c^2d^2 - a^3d^3 + 24(b^3cd^2 + ab^2d^3)x^2 + 6(b^3c^2d + 6a^2b^2cd^2 + a^2b^2d^3)x) \sqrt{bx+a} \sqrt{dx+c} / (a^2b^4c^6 - 4a^3b^3c^5d + 6a^4b^2c^4d^2 - 4a^5b^2c^3d^3 + a^6c^2d^4 + (b^6c^4d^2 - 4ab^5c^3d^3 + 6a^2b^4c^2d^4 - 4a^3b^3cd^5 + a^4b^2d^6))$

$$c^2d^4 + a^6d^6)x^2 + 2*(a^5b^5c^6 - 3a^2b^4c^5d + 2a^3b^3c^4d^2 + 2a^4b^2c^3d^3 - 3a^5b^1c^2d^4 + a^6c^1d^5)x$$

giac [B] time = 2.06, size = 670, normalized size = 4.96

$$\frac{2\sqrt{bx+a} \left(\frac{8(b^7c^3d^4|b|-3ab^6c^2d^5|b|+3a^2b^5cd^6|b|-a^3b^4d^7|b|)(bx+a)}{b^9c^7d-7ab^8c^6d^2+21a^2b^7c^5d^3-35a^3b^6c^4d^4+35a^4b^5c^3d^5-21a^5b^4c^2d^6+7a^6b^3cd^7-a^7b^2d^8} + \frac{9(b^8c^4d^3|b|-4ab^7c^3d^4|b|+6a^2b^6c^2d^5|b|-3a^3b^5cd^6|b|-a^4b^4d^7|b|)}{b^9c^7d-7ab^8c^6d^2+21a^2b^7c^5d^3-35a^3b^6c^4d^4+35a^4b^5c^3d^5-21a^5b^4c^2d^6+7a^6b^3cd^7-a^7b^2d^8} \right)}{3(b^2c + (bx+a)bd - abd)^{\frac{3}{2}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(5/2),x, algorithm="giac")

[Out] $\frac{2}{3}\sqrt{bx+a} \cdot (8(b^7c^3d^4|b|-3ab^6c^2d^5|b|+3a^2b^5cd^6|b|-a^3b^4d^7|b|)(bx+a) - 3a^2b^5c^6d^6|b|-a^3b^4c^7d^7|b|) / (b^9c^7d - 7a^8b^8c^6d^2 + 21a^2b^7c^5d^3 - 35a^3b^6c^4d^4 + 35a^4b^5c^3d^5 - 21a^5b^4c^2d^6 + 7a^6b^3cd^7 - a^7b^2d^8) + 9(b^8c^4d^3|b|-4ab^7c^3d^4|b|+6a^2b^6c^2d^5|b|-3a^3b^5cd^6|b|-a^4b^4d^7|b|) / (b^9c^7d - 7a^8b^8c^6d^2 + 21a^2b^7c^5d^3 - 35a^3b^6c^4d^4 + 35a^4b^5c^3d^5 - 21a^5b^4c^2d^6 + 7a^6b^3cd^7 - a^7b^2d^8) / (b^2c + (bx+a)bd - a^2bd)^{3/2} + 8/3(4\sqrt{bd}b^7c^2d - 8\sqrt{bd}a^2b^5d^3 - 9\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd})^{2b^5cd} + 9\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd}))^2 a^4d^2 + 3\sqrt{bd}(\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd}))^4 b^3d) / ((b^3c^3|b|-3ab^2c^2d|b|+3a^2b^1c^1d^2|b|-a^3d^3|b|)(b^2c - a^2bd - (\sqrt{bd}\sqrt{bx+a} - \sqrt{b^2c + (bx+a)bd - a^2bd}))^2)^3$

maple [A] time = 0.01, size = 169, normalized size = 1.25

$$\frac{2(-16b^3x^3d^3 - 24ab^2d^3x^2 - 24b^3cd^2x^2 - 6a^2bd^3x - 36ab^2cd^2x - 6b^3c^2dx + a^3d^3 - 9a^2bcd^2 - 9ab^2c^2d + b^3c^2d)}{3(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{3}{2}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(5/2),x)

[Out] $\frac{-2}{3} \cdot (-16b^3d^3x^3 - 24ab^2d^3x^2 - 24b^3cd^2x^2 - 6a^2bd^3x - 36ab^2cd^2x - 6b^3c^2dx + a^3d^3 - 9a^2bcd^2 - 9ab^2c^2d + b^3c^2d) / (bx+a)^{3/2} / (dx+c)^{3/2} / (a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.29, size = 224, normalized size = 1.66

$$\frac{\sqrt{c+dx} \left(\frac{16bx^2(ad+bc)}{(ad-bc)^4} - \frac{2a^3d^3-18a^2bcd^2-18ab^2c^2d+2b^3c^3}{3bd^2(ad-bc)^4} + \frac{32b^2dx^3}{3(ad-bc)^4} + \frac{4x(a^2d^2+6abcd+b^2c^2)}{d(ad-bc)^4} \right)}{x^3 \sqrt{a+bx} + \frac{ac^2 \sqrt{a+bx}}{bd^2} + \frac{x^2(ad+2bc) \sqrt{a+bx}}{bd} + \frac{cx(2ad+bc) \sqrt{a+bx}}{bd^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/2)*(c + d*x)^(5/2)),x)

[Out] ((c + d*x)^(1/2)*((16*b*x^2*(a*d + b*c))/(a*d - b*c)^4 - (2*a^3*d^3 + 2*b^3*c^3 - 18*a*b^2*c^2*d - 18*a^2*b*c*d^2)/(3*b*d^2*(a*d - b*c)^4) + (32*b^2*d*x^3)/(3*(a*d - b*c)^4) + (4*x*(a^2*d^2 + b^2*c^2 + 6*a*b*c*d))/(d*(a*d - b*c)^4))/((x^3*(a + b*x)^(1/2) + (a*c^2*(a + b*x)^(1/2))/(b*d^2) + (x^2*(a*d + 2*b*c)*(a + b*x)^(1/2))/(b*d) + (c*x*(2*a*d + b*c)*(a + b*x)^(1/2))/(b*d^2)))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{2}}(c+dx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(5/2),x)

[Out] Integral(1/((a + b*x)**(5/2)*(c + d*x)**(5/2)), x)

$$3.1520 \quad \int \frac{1}{(a+bx)^{7/2}(c+dx)^{5/2}} dx$$

Optimal. Leaf size=172

$$\frac{256bd^3\sqrt{a+bx}}{15\sqrt{c+dx}(bc-ad)^5} - \frac{128d^3\sqrt{a+bx}}{15(c+dx)^{3/2}(bc-ad)^4} - \frac{32d^2}{5\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)^3} + \frac{16d}{15(a+bx)^{3/2}(c+dx)^{3/2}(bc-ad)}$$

[Out] $-2/5/(-a*d+b*c)/(b*x+a)^{(5/2)}/(d*x+c)^{(3/2)}+16/15*d/(-a*d+b*c)^2/(b*x+a)^{(3/2)}/(d*x+c)^{(3/2)}-32/5*d^2/(-a*d+b*c)^3/(d*x+c)^{(3/2)}/(b*x+a)^{(1/2)}-128/15*d^3*(b*x+a)^{(1/2)}/(-a*d+b*c)^4/(d*x+c)^{(3/2)}-256/15*b*d^3*(b*x+a)^{(1/2)}/(-a*d+b*c)^5/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.04, antiderivative size = 172, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{256bd^3\sqrt{a+bx}}{15\sqrt{c+dx}(bc-ad)^5} - \frac{128d^3\sqrt{a+bx}}{15(c+dx)^{3/2}(bc-ad)^4} - \frac{32d^2}{5\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)^3} + \frac{16d}{15(a+bx)^{3/2}(c+dx)^{3/2}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/2)*(c + d*x)^(5/2)), x]

[Out] $-2/(5*(b*c - a*d)*(a + b*x)^{(5/2)*(c + d*x)^{(3/2)}) + (16*d)/(15*(b*c - a*d)^2*(a + b*x)^{(3/2)*(c + d*x)^{(3/2)}) - (32*d^2)/(5*(b*c - a*d)^3*\text{Sqrt}[a + b*x]*(c + d*x)^{(3/2)}) - (128*d^3*\text{Sqrt}[a + b*x])/(15*(b*c - a*d)^4*(c + d*x)^{(3/2)}) - (256*b*d^3*\text{Sqrt}[a + b*x])/(15*(b*c - a*d)^5*\text{Sqrt}[c + d*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{7/2}(c+dx)^{5/2}} dx &= -\frac{2}{5(bc-ad)(a+bx)^{5/2}(c+dx)^{3/2}} - \frac{(8d) \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx}{5(bc-ad)} \\
&= -\frac{2}{5(bc-ad)(a+bx)^{5/2}(c+dx)^{3/2}} + \frac{16d}{15(bc-ad)^2(a+bx)^{3/2}(c+dx)^{3/2}} + \frac{(16d^2) \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx}{5(bc-ad)^2} \\
&= -\frac{2}{5(bc-ad)(a+bx)^{5/2}(c+dx)^{3/2}} + \frac{16d}{15(bc-ad)^2(a+bx)^{3/2}(c+dx)^{3/2}} - \frac{16d^2}{5(bc-ad)^2} \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx \\
&= -\frac{2}{5(bc-ad)(a+bx)^{5/2}(c+dx)^{3/2}} + \frac{16d}{15(bc-ad)^2(a+bx)^{3/2}(c+dx)^{3/2}} - \frac{16d^2}{5(bc-ad)^2} \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx \\
&= -\frac{2}{5(bc-ad)(a+bx)^{5/2}(c+dx)^{3/2}} + \frac{16d}{15(bc-ad)^2(a+bx)^{3/2}(c+dx)^{3/2}} - \frac{16d^2}{5(bc-ad)^2} \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx
\end{aligned}$$

Mathematica [A] time = 0.07, size = 170, normalized size = 0.99

$$\frac{2(-5a^4d^4 + 20a^3bd^3(3c + 2dx) + 30a^2b^2d^2(3c^2 + 12cdx + 8d^2x^2) + 20ab^3d(-c^3 + 6c^2dx + 24cd^2x^2 + 16d^3x^3))}{15(a+bx)^{5/2}(c+dx)^{3/2}(bc-ad)^5}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/2)*(c + d*x)^(5/2)), x]

[Out] (-2*(-5*a^4*d^4 + 20*a^3*b*d^3*(3*c + 2*d*x) + 30*a^2*b^2*d^2*(3*c^2 + 12*c*d*x + 8*d^2*x^2) + 20*a*b^3*d*(-c^3 + 6*c^2*d*x + 24*c*d^2*x^2 + 16*d^3*x^3) + b^4*(3*c^4 - 8*c^3*d*x + 48*c^2*d^2*x^2 + 192*c*d^3*x^3 + 128*d^4*x^4))/(15*(b*c - a*d)^5*(a + b*x)^(5/2)*(c + d*x)^(3/2))

fricas [B] time = 3.43, size = 715, normalized size = 4.16

$$\frac{15(a^3b^5c^7 - 5a^4b^4c^6d + 10a^5b^3c^5d^2 - 10a^6b^2c^4d^3 + 5a^7bc^3d^4 - a^8c^2d^5 + (b^8c^5d^2 - 5ab^7c^4d^3 + 10a^2b^6c^3d^4 - 10a^3b^5c^2d^5 + 5a^4b^4c^3d^6 - 5a^5b^3c^4d^7 + 5a^6b^2c^5d^8 - 5a^7b^3c^6d^9 + 5a^8b^4c^7d^{10}))}{15(a+bx)^{5/2}(c+dx)^{3/2}(bc-ad)^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/2)/(d*x+c)^(5/2), x, algorithm="fricas")

[Out] -2/15*(128*b^4*d^4*x^4 + 3*b^4*c^4 - 20*a*b^3*c^3*d + 90*a^2*b^2*c^2*d^2 + 60*a^3*b*c*d^3 - 5*a^4*d^4 + 64*(3*b^4*c*d^3 + 5*a*b^3*d^4)*x^3 + 48*(b^4*c

$$\begin{aligned} &^2*d^2 + 10*a*b^3*c*d^3 + 5*a^2*b^2*d^4)*x^2 - 8*(b^4*c^3*d - 15*a*b^3*c^2* \\ &d^2 - 45*a^2*b^2*c*d^3 - 5*a^3*b*d^4)*x)*\sqrt{b*x + a}*\sqrt{d*x + c}/(a^3*b \\ &^5*c^7 - 5*a^4*b^4*c^6*d + 10*a^5*b^3*c^5*d^2 - 10*a^6*b^2*c^4*d^3 + 5*a^7* \\ &b*c^3*d^4 - a^8*c^2*d^5 + (b^8*c^5*d^2 - 5*a*b^7*c^4*d^3 + 10*a^2*b^6*c^3*d \\ &^4 - 10*a^3*b^5*c^2*d^5 + 5*a^4*b^4*c*d^6 - a^5*b^3*d^7)*x^5 + (2*b^8*c^6*d \\ &- 7*a*b^7*c^5*d^2 + 5*a^2*b^6*c^4*d^3 + 10*a^3*b^5*c^3*d^4 - 20*a^4*b^4*c^ \\ &2*d^5 + 13*a^5*b^3*c*d^6 - 3*a^6*b^2*d^7)*x^4 + (b^8*c^7 + a*b^7*c^6*d - 17 \\ &a^2*b^6*c^5*d^2 + 35*a^3*b^5*c^4*d^3 - 25*a^4*b^4*c^3*d^4 - a^5*b^3*c^2*d^ \\ &5 + 9*a^6*b^2*c*d^6 - 3*a^7*b*d^7)*x^3 + (3*a*b^7*c^7 - 9*a^2*b^6*c^6*d + a \\ &^3*b^5*c^5*d^2 + 25*a^4*b^4*c^4*d^3 - 35*a^5*b^3*c^3*d^4 + 17*a^6*b^2*c^2*d \\ &^5 - a^7*b*c*d^6 - a^8*d^7)*x^2 + (3*a^2*b^6*c^7 - 13*a^3*b^5*c^6*d + 20*a^ \\ &4*b^4*c^5*d^2 - 10*a^5*b^3*c^4*d^3 - 5*a^6*b^2*c^3*d^4 + 7*a^7*b*c^2*d^5 - \\ &2*a^8*c*d^6)*x) \end{aligned}$$

giac [B] time = 3.92, size = 1203, normalized size = 6.99

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/2)/(d*x+c)^(5/2),x, algorithm="giac")

[Out]
$$\begin{aligned} &-2/3*\sqrt{b*x + a}*(11*(b^8*c^4*d^5*abs(b) - 4*a*b^7*c^3*d^6*abs(b) + 6*a^2 \\ &*b^6*c^2*d^7*abs(b) - 4*a^3*b^5*c*d^8*abs(b) + a^4*b^4*d^9*abs(b))*(b*x + a \\ &)/(b^11*c^9*d - 9*a*b^10*c^8*d^2 + 36*a^2*b^9*c^7*d^3 - 84*a^3*b^8*c^6*d^4 \\ &+ 126*a^4*b^7*c^5*d^5 - 126*a^5*b^6*c^4*d^6 + 84*a^6*b^5*c^3*d^7 - 36*a^7*b \\ &^4*c^2*d^8 + 9*a^8*b^3*c*d^9 - a^9*b^2*d^10) + 12*(b^9*c^5*d^4*abs(b) - 5*a \\ &*b^8*c^4*d^5*abs(b) + 10*a^2*b^7*c^3*d^6*abs(b) - 10*a^3*b^6*c^2*d^7*abs(b) \\ &+ 5*a^4*b^5*c*d^8*abs(b) - a^5*b^4*d^9*abs(b))/(b^11*c^9*d - 9*a*b^10*c^8* \\ &d^2 + 36*a^2*b^9*c^7*d^3 - 84*a^3*b^8*c^6*d^4 + 126*a^4*b^7*c^5*d^5 - 126*a \\ &^5*b^6*c^4*d^6 + 84*a^6*b^5*c^3*d^7 - 36*a^7*b^4*c^2*d^8 + 9*a^8*b^3*c*d^9 \\ &- a^9*b^2*d^10))/(b^2*c + (b*x + a)*b*d - a*b*d)^(3/2) - 4/15*(73*\sqrt{b*d} \\ &*b^11*c^4*d^2 - 292*\sqrt{b*d}*a*b^10*c^3*d^3 + 438*\sqrt{b*d}*a^2*b^9*c^2*d^ \\ &4 - 292*\sqrt{b*d}*a^3*b^8*c*d^5 + 73*\sqrt{b*d}*a^4*b^7*d^6 - 320*\sqrt{b*d}* \\ &(\sqrt{b*d}*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*b^9*c^3*d \\ &^2 + 960*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - \\ &a*b*d})^2*a*b^8*c^2*d^3 - 960*\sqrt{b*d}*(\sqrt{b*d}*\sqrt{b*x + a} - \sqrt{b^2 \\ &*c + (b*x + a)*b*d - a*b*d})^2*a^2*b^7*c*d^4 + 320*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{ \\ &t(b*x + a) - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^2*a^3*b^6*d^5 + 490*\sqrt{ \\ &b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^4*b^7* \\ &c^2*d^2 - 980*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b \\ &*d - a*b*d})^4*a*b^6*c*d^3 + 490*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{ \\ &b^2*c + (b*x + a)*b*d - a*b*d})^4*a^2*b^5*d^4 - 240*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{ \\ &rt(b*x + a) - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^6*b^5*c*d^2 + 240*\sqrt{b \\ &*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - a*b*d})^6*a*b^4 \\ &d^3 + 45*\sqrt{b*d}*(\sqrt{b*d})*\sqrt{b*x + a} - \sqrt{b^2*c + (b*x + a)*b*d - \end{aligned}$$


```
)^5) + (x*(80*a^3*b*d^4 - 16*b^4*c^3*d + 240*a*b^3*c^2*d^2 + 720*a^2*b^2*c*d^3))/(15*b^2*d^2*(a*d - b*c)^5) + (128*b*d*x^3*(5*a*d + 3*b*c))/(15*(a*d - b*c)^5)))/(x^4*(a + b*x)^(1/2) + (x^2*(a + b*x)^(1/2)*(a^2*d^2 + b^2*c^2 + 4*a*b*c*d))/(b^2*d^2) + (2*x^3*(a*d + b*c)*(a + b*x)^(1/2))/(b*d) + (a^2*c^2*(a + b*x)^(1/2))/(b^2*d^2) + (2*a*c*x*(a*d + b*c)*(a + b*x)^(1/2))/(b^2*d^2))
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{7}{2}} (c + dx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(7/2)/(d*x+c)**(5/2), x)
```

```
[Out] Integral(1/((a + b*x)**(7/2)*(c + d*x)**(5/2)), x)
```

$$3.1521 \quad \int \frac{1}{(a+bx)^{9/2}(c+dx)^{5/2}} dx$$

Optimal. Leaf size=207

$$\frac{512bd^4\sqrt{a+bx}}{21\sqrt{c+dx}(bc-ad)^6} + \frac{256d^4\sqrt{a+bx}}{21(c+dx)^{3/2}(bc-ad)^5} + \frac{64d^3}{7\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)^4} - \frac{32d^2}{21(a+bx)^{3/2}(c+dx)^{3/2}(bc-ad)^3}$$

[Out] $-2/7/(-a*d+b*c)/(b*x+a)^{(7/2)}/(d*x+c)^{(3/2)}+4/7*d/(-a*d+b*c)^2/(b*x+a)^{(5/2)}/(d*x+c)^{(3/2)}-32/21*d^2/(-a*d+b*c)^3/(b*x+a)^{(3/2)}/(d*x+c)^{(3/2)}+64/7*d^3/(-a*d+b*c)^4/(d*x+c)^{(3/2)}/(b*x+a)^{(1/2)}+256/21*d^4*(b*x+a)^{(1/2)}/(-a*d+b*c)^5/(d*x+c)^{(3/2)}+512/21*b*d^4*(b*x+a)^{(1/2)}/(-a*d+b*c)^6/(d*x+c)^{(1/2)}$

Rubi [A] time = 0.06, antiderivative size = 207, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{512bd^4\sqrt{a+bx}}{21\sqrt{c+dx}(bc-ad)^6} + \frac{256d^4\sqrt{a+bx}}{21(c+dx)^{3/2}(bc-ad)^5} + \frac{64d^3}{7\sqrt{a+bx}(c+dx)^{3/2}(bc-ad)^4} - \frac{32d^2}{21(a+bx)^{3/2}(c+dx)^{3/2}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(9/2)*(c + d*x)^(5/2)), x]

[Out] $-2/(7*(b*c - a*d)*(a + b*x)^{(7/2)*(c + d*x)^{(3/2)}) + (4*d)/(7*(b*c - a*d)^2*(a + b*x)^{(5/2)*(c + d*x)^{(3/2)}) - (32*d^2)/(21*(b*c - a*d)^3*(a + b*x)^{(3/2)*(c + d*x)^{(3/2)}) + (64*d^3)/(7*(b*c - a*d)^4*\text{Sqrt}[a + b*x]*(c + d*x)^{(3/2)}) + (256*d^4*\text{Sqrt}[a + b*x])/(21*(b*c - a*d)^5*(c + d*x)^{(3/2)}) + (512*b*d^4*\text{Sqrt}[a + b*x])/(21*(b*c - a*d)^6*\text{Sqrt}[c + d*x])$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler

Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{9/2}(c+dx)^{5/2}} dx &= -\frac{2}{7(bc-ad)(a+bx)^{7/2}(c+dx)^{3/2}} - \frac{(10d) \int \frac{1}{(a+bx)^{7/2}(c+dx)^{5/2}} dx}{7(bc-ad)} \\
 &= -\frac{2}{7(bc-ad)(a+bx)^{7/2}(c+dx)^{3/2}} + \frac{4d}{7(bc-ad)^2(a+bx)^{5/2}(c+dx)^{3/2}} + \frac{(16d^2) \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx}{7(bc-ad)^2} \\
 &= -\frac{2}{7(bc-ad)(a+bx)^{7/2}(c+dx)^{3/2}} + \frac{4d}{7(bc-ad)^2(a+bx)^{5/2}(c+dx)^{3/2}} - \frac{16d^2}{21(bc-ad)^2} \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx \\
 &= -\frac{2}{7(bc-ad)(a+bx)^{7/2}(c+dx)^{3/2}} + \frac{4d}{7(bc-ad)^2(a+bx)^{5/2}(c+dx)^{3/2}} - \frac{16d^2}{21(bc-ad)^2} \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx \\
 &= -\frac{2}{7(bc-ad)(a+bx)^{7/2}(c+dx)^{3/2}} + \frac{4d}{7(bc-ad)^2(a+bx)^{5/2}(c+dx)^{3/2}} - \frac{16d^2}{21(bc-ad)^2} \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx \\
 &= -\frac{2}{7(bc-ad)(a+bx)^{7/2}(c+dx)^{3/2}} + \frac{4d}{7(bc-ad)^2(a+bx)^{5/2}(c+dx)^{3/2}} - \frac{16d^2}{21(bc-ad)^2} \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/2}} dx
 \end{aligned}$$

Mathematica [A] time = 0.08, size = 233, normalized size = 1.13

$$\frac{2(-7a^5d^5 + 35a^4bd^4(3c + 2dx) + 70a^3b^2d^3(3c^2 + 12cdx + 8d^2x^2) + 70a^2b^3d^2(-c^3 + 6c^2dx + 24cd^2x^2 + 16d^3x^3) + 70ab^4d(-c^4 + 6c^3dx + 24cd^2x^2 + 16d^3x^3) + b^5(-3c^5 + 6c^4dx + 24cd^2x^2 + 16d^3x^3) + 384c^4d^4x^4 + 256d^5x^5)}{21(a+bx)^{7/2}(c+dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(9/2)*(c + d*x)^(5/2)), x]

[Out] (2*(-7*a^5*d^5 + 35*a^4*b*d^4*(3*c + 2*d*x) + 70*a^3*b^2*d^3*(3*c^2 + 12*c*d*x + 8*d^2*x^2) + 70*a^2*b^3*d^2*(-c^3 + 6*c^2*d*x + 24*c*d^2*x^2 + 16*d^3*x^3) + 7*a*b^4*d*(3*c^4 - 8*c^3*d*x + 48*c^2*d^2*x^2 + 192*c*d^3*x^3 + 128*d^4*x^4) + b^5*(-3*c^5 + 6*c^4*d*x - 16*c^3*d^2*x^2 + 96*c^2*d^3*x^3 + 384*c*d^4*x^4 + 256*d^5*x^5))/(21*(b*c - a*d)^6*(a + b*x)^(7/2)*(c + d*x)^(3/2))

fricas [B] time = 7.60, size = 999, normalized size = 4.83

$$\frac{21(a^4b^6c^8 - 6a^5b^5c^7d + 15a^6b^4c^6d^2 - 20a^7b^3c^5d^3 + 15a^8b^2c^4d^4 - 6a^9bc^3d^5 + a^{10}c^2d^6 + (b^{10}c^6d^2 - 6ab^9c^5d^3 - \dots))}{21(a+bx)^{7/2}(c+dx)^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(d*x+c)^(5/2),x, algorithm="fricas")

[Out]
$$\frac{2}{21} \cdot (256b^5d^5x^5 - 3b^5c^5 + 21ab^4c^4d - 70a^2b^3c^3d^2 + 210a^3b^2c^2d^3 + 105a^4b^1c^1d^4 - 7a^5d^5 + 128(3b^5c^4d + 7ab^4c^3d^2 + 32(3b^5c^2d^3 + 42ab^4c^2d^4 + 35a^2b^3d^5)x^3 - 16(b^5c^3d^2 - 21ab^4c^2d^3 - 105a^2b^3c^1d^4 - 35a^3b^2d^5)x^2 + 2(3b^5c^4d - 28ab^4c^3d^2 + 210a^2b^3c^2d^3 + 420a^3b^2c^1d^4 + 35a^4b^1d^5)x) \cdot \sqrt{bx+a} \cdot \sqrt{dx+c} / (a^4b^6c^8 - 6a^5b^5c^7d + 15a^6b^4c^6d^2 - 20a^7b^3c^5d^3 + 15a^8b^2c^4d^4 - 6a^9b^1c^3d^5 + a^{10}c^2d^6 + (b^{10}c^6d^2 - 6a^2b^9c^5d^3 + 15a^3b^8c^4d^4 - 20a^4b^7c^3d^5 + 15a^5b^6c^2d^6 - 6a^6b^5c^1d^7 + a^6b^4d^8)x^6 + 2(b^{10}c^7d - 4a^2b^9c^6d^2 + 3a^3b^8c^5d^3 + 10a^4b^7c^4d^4 - 25a^5b^6c^3d^5 + 24a^6b^5c^2d^6 - 11a^7b^4c^1d^7 + 2a^8b^3d^8)x^5 + (b^{10}c^8 + 2a^2b^9c^7d - 27a^3b^8c^6d^2 + 64a^4b^7c^5d^3 - 55a^5b^6c^4d^4 - 6a^6b^5c^3d^5 + 43a^7b^4c^2d^6 - 28a^8b^3c^1d^7 + 6a^9b^2d^8)x^4 + 4(a^2b^9c^8 - 3a^3b^8c^7d - 2a^4b^7c^6d^2 + 19a^5b^6c^5d^3 - 30a^6b^5c^4d^4 + 19a^7b^4c^3d^5 - 2a^8b^3c^2d^6 - 3a^9b^2c^1d^7 + a^9b^1d^8)x^3 + (6a^2b^8c^8 - 28a^3b^7c^7d + 43a^4b^6c^6d^2 - 6a^5b^5c^5d^3 - 55a^6b^4c^4d^4 + 64a^7b^3c^3d^5 - 27a^8b^2c^2d^6 + 2a^9b^1c^1d^7 + a^{10}d^8)x^2 + 2(2a^3b^7c^8 - 11a^4b^6c^7d + 24a^5b^5c^6d^2 - 25a^6b^4c^5d^3 + 10a^7b^3c^4d^4 + 3a^8b^2c^3d^5 - 4a^9b^1c^2d^6 + a^{10}c^1d^7)x)$$

giac [B] time = 7.76, size = 1964, normalized size = 9.49

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(d*x+c)^(5/2),x, algorithm="giac")

[Out]
$$\frac{2}{3} \cdot \sqrt{bx+a} \cdot (14(b^9c^5d^6 \operatorname{abs}(b) - 5ab^8c^4d^7 \operatorname{abs}(b) + 10a^2b^7c^3d^8 \operatorname{abs}(b) - 10a^3b^6c^2d^9 \operatorname{abs}(b) + 5a^4b^5c^1d^{10} \operatorname{abs}(b) - a^5b^4d^{11} \operatorname{abs}(b)) \cdot (bx+a) / (b^{13}c^{11}d - 11a^2b^{12}c^{10}d^2 + 55a^3b^{11}c^9d^3 - 165a^4b^{10}c^8d^4 + 330a^5b^9c^7d^5 - 462a^6b^8c^6d^6 + 462a^7b^7c^5d^7 - 330a^8b^6c^4d^8 + 165a^9b^5c^3d^9 - 55a^{10}b^4c^2d^{10} + 11a^{11}b^3c^1d^{11} - a^{11}b^2d^{12}) + 15(b^{10}c^6d^5 \operatorname{abs}(b) - 6a^2b^9c^5d^6 \operatorname{abs}(b) + 15a^3b^8c^4d^7 \operatorname{abs}(b) - 20a^4b^7c^3d^8 \operatorname{abs}(b) + 15a^5b^6c^2d^9 \operatorname{abs}(b) - 6a^6b^5c^1d^{10} \operatorname{abs}(b) + a^6b^4d^{11} \operatorname{abs}(b))) / (b^2c + (bx+a) \cdot b \cdot d - a \cdot b \cdot d)^{3/2}$$

$$b^3*c*d^4*x^2-336*a*b^4*c^2*d^3*x^2+16*b^5*c^3*d^2*x^2-70*a^4*b*d^5*x-840*a^3*b^2*c*d^4*x-420*a^2*b^3*c^2*d^3*x+56*a*b^4*c^3*d^2*x-6*b^5*c^4*d*x+7*a^5*d^5-105*a^4*b*c*d^4-210*a^3*b^2*c^2*d^3+70*a^2*b^3*c^3*d^2-21*a*b^4*c^4*d+3*b^5*c^5)/(b*x+a)^{(7/2)}/(d*x+c)^{(3/2)}/(a^6*d^6-6*a^5*b*c*d^5+15*a^4*b^2*c^2*d^4-20*a^3*b^3*c^3*d^3+15*a^2*b^4*c^4*d^2-6*a*b^5*c^5*d+b^6*c^6)$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/2)/(d*x+c)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 1.91, size = 478, normalized size = 2.31

$$\frac{\sqrt{c+dx} \left(\frac{32x^2(35a^3d^3+105a^2bcd^2+21ab^2c^2d-b^3c^3)}{21b(ad-bc)^6} - \frac{14a^5d^5-210a^4bcd^4-420a^3b^2c^2d^3+140a^2b^3c^3d^2-42ab^4c^4d+6b^5c^5}{21b^3d^2(ad-bc)^6} + \frac{64dx^3}{b^2d^2} \right)}{x^5\sqrt{a+bx} + \frac{x^3\sqrt{a+bx}(3a^2d^2+6abcd+b^2c^2)}{b^2d^2} + \frac{x^4(3ad+2bc)\sqrt{a+bx}}{bd} + \dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(9/2)*(c + d*x)^(5/2)),x)

[Out] ((c + d*x)^(1/2)*((32*x^2*(35*a^3*d^3 - b^3*c^3 + 21*a*b^2*c^2*d + 105*a^2*b*c*d^2))/(21*b*(a*d - b*c)^6) - (14*a^5*d^5 + 6*b^5*c^5 + 140*a^2*b^3*c^3*d^2 - 420*a^3*b^2*c^2*d^3 - 42*a*b^4*c^4*d - 210*a^4*b*c*d^4)/(21*b^3*d^2*(a*d - b*c)^6) + (64*d*x^3*(35*a^2*d^2 + 3*b^2*c^2 + 42*a*b*c*d))/(21*(a*d - b*c)^6) + (512*b^2*d^3*x^5)/(21*(a*d - b*c)^6) + (256*b*d^2*x^4*(7*a*d + 3*b*c))/(21*(a*d - b*c)^6) + (x*(140*a^4*b*d^5 + 12*b^5*c^4*d - 112*a*b^4*c^3*d^2 + 1680*a^3*b^2*c*d^4 + 840*a^2*b^3*c^2*d^3))/(21*b^3*d^2*(a*d - b*c)^6)))/(x^5*(a + b*x)^(1/2) + (x^3*(a + b*x)^(1/2)*(3*a^2*d^2 + b^2*c^2 + 6*a*b*c*d))/(b^2*d^2) + (x^4*(3*a*d + 2*b*c)*(a + b*x)^(1/2))/(b*d) + (a^3*c^2*(a + b*x)^(1/2))/(b^3*d^2) + (a*x^2*(a + b*x)^(1/2)*(a^2*d^2 + 3*b^2*c^2 + 6*a*b*c*d))/(b^3*d^2) + (a^2*c*x*(2*a*d + 3*b*c)*(a + b*x)^(1/2))/(b^3*d^2))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(9/2)/(d*x+c)**(5/2),x)
```

```
[Out] Timed out
```

$$3.1522 \quad \int \frac{1}{\sqrt{a+bx} \sqrt{4+a+bx}} dx$$

Optimal. Leaf size=19

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{a+bx}\right)}{b}$$

[Out] 2*arcsinh(1/2*(b*x+a)^(1/2))/b

Rubi [A] time = 0.01, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{a+bx}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*Sqrt[4 + a + b*x]),x]

[Out] (2*ArcSinh[Sqrt[a + b*x]/2])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{a+bx} \sqrt{4+a+bx}} dx &= \frac{2 \text{Subst}\left(\int \frac{1}{\sqrt{4+x^2}} dx, x, \sqrt{a+bx}\right)}{b} \\ &= \frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{a+bx}\right)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 19, normalized size = 1.00

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{a+bx}\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*Sqrt[4 + a + b*x]),x]

[Out] (2*ArcSinh[Sqrt[a + b*x]/2])/b

fricas [B] time = 0.43, size = 31, normalized size = 1.63

$$\frac{\log\left(-bx + \sqrt{bx + a + 4}\sqrt{bx + a} - a - 2\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(b*x+a+4)^(1/2),x, algorithm="fricas")

[Out] -log(-b*x + sqrt(b*x + a + 4)*sqrt(b*x + a) - a - 2)/b

giac [A] time = 1.02, size = 24, normalized size = 1.26

$$\frac{2 \log\left(\sqrt{bx + a + 4} - \sqrt{bx + a}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(b*x+a+4)^(1/2),x, algorithm="giac")

[Out] -2*log(sqrt(b*x + a + 4) - sqrt(b*x + a))/b

maple [B] time = 0.01, size = 86, normalized size = 4.53

$$\frac{\sqrt{(bx+a)(bx+a+4)} \ln\left(\frac{b^2x + \frac{ab}{2} + \frac{(a+4)b}{2}}{\sqrt{b^2}} + \sqrt{b^2x^2 + (a+4)a + (ab + (a+4)b)x}\right)}{\sqrt{bx+a} \sqrt{bx+a+4} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(b*x+a+4)^(1/2),x)

[Out] ((b*x+a)*(b*x+a+4))^(1/2)/(b*x+a)^(1/2)/(b*x+a+4)^(1/2)*ln((1/2*a*b+1/2*b*(a+4)+b^2*x)/(b^2)^(1/2)+(b^2*x^2+(a*b+b*(a+4))*x+a*(a+4))^(1/2))/(b^2)^(1/2)

maxima [B] time = 1.36, size = 48, normalized size = 2.53

$$\frac{\log\left(2b^2x + 2ab + 2\sqrt{b^2x^2 + a^2} + 2(ab + 2b)x + 4ab + 4b\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(b*x+a+4)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*a*b + 2*sqrt(b^2*x^2 + a^2 + 2*(a*b + 2*b)*x + 4*a)*b + 4*b)/b

mupad [B] time = 0.31, size = 50, normalized size = 2.63

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{a+4}-\sqrt{a+bx+4})}{\sqrt{-b^2}(\sqrt{a+bx}-\sqrt{a})}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/2)*(a + b*x + 4)^(1/2)),x)

[Out] (4*atan((b*((a + 4)^(1/2) - (a + b*x + 4)^(1/2)))/((-b^2)^(1/2)*((a + b*x)^(1/2) - a^(1/2)))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a+bx}\sqrt{a+bx+4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/2)/(b*x+a+4)**(1/2),x)

[Out] Integral(1/(sqrt(a + b*x)*sqrt(a + b*x + 4)), x)

$$3.1523 \quad \int \frac{1}{\sqrt{2+bx} \sqrt{6+bx}} dx$$

Optimal. Leaf size=19

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{bx+2}\right)}{b}$$

[Out] 2*arcsinh(1/2*(b*x+2)^(1/2))/b

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{bx+2}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[2 + b*x]*Sqrt[6 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[2 + b*x]/2])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{2+bx} \sqrt{6+bx}} dx &= \frac{2 \text{Subst}\left(\int \frac{1}{\sqrt{4+x^2}} dx, x, \sqrt{2+bx}\right)}{b} \\ &= \frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{2+bx}\right)}{b} \end{aligned}$$

Mathematica [B] time = 0.01, size = 39, normalized size = 2.05

$$\frac{2\sqrt{bx+2} \sin^{-1}\left(\frac{1}{2}\sqrt{-bx-2}\right)}{b\sqrt{-bx-2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[2 + b*x]*Sqrt[6 + b*x]),x]

[Out] (2*Sqrt[2 + b*x]*ArcSin[Sqrt[-2 - b*x]/2])/(b*Sqrt[-2 - b*x])

fricas [A] time = 0.42, size = 27, normalized size = 1.42

$$-\frac{\log(-bx + \sqrt{bx+6}\sqrt{bx+2} - 4)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(1/2)/(b*x+6)^(1/2),x, algorithm="fricas")

[Out] -log(-b*x + sqrt(b*x + 6)*sqrt(b*x + 2) - 4)/b

giac [A] time = 1.05, size = 23, normalized size = 1.21

$$-\frac{2 \log(\sqrt{bx+6} - \sqrt{bx+2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(1/2)/(b*x+6)^(1/2),x, algorithm="giac")

[Out] -2*log(sqrt(b*x + 6) - sqrt(b*x + 2))/b

maple [B] time = 0.01, size = 66, normalized size = 3.47

$$\frac{\sqrt{(bx+2)(bx+6)} \ln\left(\frac{b^2x+4b}{\sqrt{b^2}} + \sqrt{b^2x^2+8bx+12}\right)}{\sqrt{bx+2} \sqrt{bx+6} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+2)^(1/2)/(b*x+6)^(1/2),x)

[Out] ((b*x+2)*(b*x+6))^(1/2)/(b*x+2)^(1/2)/(b*x+6)^(1/2)*ln((b^2*x+4*b)/(b^2)^(1/2)+(b^2*x^2+8*b*x+12)^(1/2))/(b^2)^(1/2)

maxima [B] time = 1.37, size = 33, normalized size = 1.74

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 + 8bx + 12b + 8b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(1/2)/(b*x+6)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 + 8*b*x + 12)*b + 8*b)/b

mupad [B] time = 0.34, size = 47, normalized size = 2.47

$$-\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{6}-\sqrt{bx+6})}{(\sqrt{2}-\sqrt{bx+2})\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x + 2)^(1/2)*(b*x + 6)^(1/2)),x)

[Out] -(4*atan((b*(6^(1/2) - (b*x + 6)^(1/2)))/((2^(1/2) - (b*x + 2)^(1/2))*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+2}\sqrt{bx+6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)**(1/2)/(b*x+6)**(1/2),x)

[Out] Integral(1/(sqrt(b*x + 2)*sqrt(b*x + 6)), x)

$$3.1524 \quad \int \frac{1}{\sqrt{1+bx} \sqrt{5+bx}} dx$$

Optimal. Leaf size=19

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{bx+1}\right)}{b}$$

[Out] 2*arcsinh(1/2*(b*x+1)^(1/2))/b

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{bx+1}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[1 + b*x]*Sqrt[5 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[1 + b*x]/2])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{1+bx} \sqrt{5+bx}} dx &= \frac{2 \text{Subst}\left(\int \frac{1}{\sqrt{4+x^2}} dx, x, \sqrt{1+bx}\right)}{b} \\ &= \frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{1+bx}\right)}{b} \end{aligned}$$

Mathematica [B] time = 0.01, size = 39, normalized size = 2.05

$$\frac{2\sqrt{bx+1} \sin^{-1}\left(\frac{1}{2}\sqrt{-bx-1}\right)}{b\sqrt{-bx-1}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[1 + b*x]*Sqrt[5 + b*x]), x]

[Out] (2*Sqrt[1 + b*x]*ArcSin[Sqrt[-1 - b*x]/2])/(b*Sqrt[-1 - b*x])

fricas [A] time = 0.45, size = 27, normalized size = 1.42

$$-\frac{\log(-bx + \sqrt{bx+5}\sqrt{bx+1} - 3)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+1)^(1/2)/(b*x+5)^(1/2), x, algorithm="fricas")

[Out] -log(-b*x + sqrt(b*x + 5)*sqrt(b*x + 1) - 3)/b

giac [A] time = 0.96, size = 23, normalized size = 1.21

$$-\frac{2 \log(\sqrt{bx+5} - \sqrt{bx+1})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+1)^(1/2)/(b*x+5)^(1/2), x, algorithm="giac")

[Out] -2*log(sqrt(b*x + 5) - sqrt(b*x + 1))/b

maple [B] time = 0.01, size = 66, normalized size = 3.47

$$\frac{\sqrt{(bx+1)(bx+5)} \ln\left(\frac{b^2x+3b}{\sqrt{b^2}} + \sqrt{b^2x^2+6bx+5}\right)}{\sqrt{bx+1} \sqrt{bx+5} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+1)^(1/2)/(b*x+5)^(1/2), x)

[Out] ((b*x+1)*(b*x+5))^(1/2)/(b*x+1)^(1/2)/(b*x+5)^(1/2)*ln((b^2*x+3*b)/(b^2)^(1/2)+(b^2*x^2+6*b*x+5)^(1/2))/(b^2)^(1/2)

maxima [B] time = 1.39, size = 33, normalized size = 1.74

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 + 6bx + 5b + 6b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+1)^(1/2)/(b*x+5)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 + 6*b*x + 5)*b + 6*b)/b

mupad [B] time = 0.33, size = 43, normalized size = 2.26

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{5}-\sqrt{bx+5})}{(\sqrt{bx+1}-1)\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x + 1)^(1/2)*(b*x + 5)^(1/2)),x)

[Out] (4*atan((b*(5^(1/2) - (b*x + 5)^(1/2)))/(((b*x + 1)^(1/2) - 1)*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+1}\sqrt{bx+5}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+1)**(1/2)/(b*x+5)**(1/2),x)

[Out] Integral(1/(sqrt(b*x + 1)*sqrt(b*x + 5)), x)

$$3.1525 \quad \int \frac{1}{\sqrt{bx} \sqrt{4+bx}} dx$$

Optimal. Leaf size=17

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{bx}}{2}\right)}{b}$$

[Out] 2*arcsinh(1/2*(b*x)^(1/2))/b

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{bx}}{2}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[b*x]*Sqrt[4 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[b*x]/2])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{bx} \sqrt{4+bx}} dx &= \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{4+x^2}} dx, x, \sqrt{bx}\right)}{b} \\ &= \frac{2 \sinh^{-1}\left(\frac{\sqrt{bx}}{2}\right)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 34, normalized size = 2.00

$$\frac{2\sqrt{x} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{2}\right)}{\sqrt{b}\sqrt{bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[b*x]*Sqrt[4 + b*x]),x]

[Out] (2*Sqrt[x]*ArcSinh[(Sqrt[b]*Sqrt[x])/2])/(Sqrt[b]*Sqrt[b*x])

fricas [A] time = 0.46, size = 25, normalized size = 1.47

$$-\frac{\log(-bx + \sqrt{bx + 4}\sqrt{bx} - 2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x)^(1/2)/(b*x+4)^(1/2),x, algorithm="fricas")

[Out] -log(-b*x + sqrt(b*x + 4)*sqrt(b*x) - 2)/b

giac [A] time = 0.94, size = 21, normalized size = 1.24

$$-\frac{2 \log(\sqrt{bx + 4} - \sqrt{bx})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x)^(1/2)/(b*x+4)^(1/2),x, algorithm="giac")

[Out] -2*log(sqrt(b*x + 4) - sqrt(b*x))/b

maple [B] time = 0.01, size = 60, normalized size = 3.53

$$\frac{\sqrt{(bx + 4)bx} \ln\left(\frac{b^2x+2b}{\sqrt{b^2}} + \sqrt{b^2x^2 + 4bx}\right)}{\sqrt{bx} \sqrt{bx + 4} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x)^(1/2)/(b*x+4)^(1/2),x)

[Out] (x*b*(b*x+4))^(1/2)/(b*x)^(1/2)/(b*x+4)^(1/2)*ln((b^2*x+2*b)/(b^2)^(1/2)+(b^2*x^2+4*b*x)^(1/2))/(b^2)^(1/2)

maxima [B] time = 1.33, size = 32, normalized size = 1.88

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 + 4bx}b + 4b\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x)^(1/2)/(b*x+4)^(1/2), x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 + 4*b*x)*b + 4*b)/b

mupad [B] time = 0.31, size = 33, normalized size = 1.94

$$-\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{bx+4}-2)}{\sqrt{bx}\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x)^(1/2)*(b*x + 4)^(1/2)), x)

[Out] -(4*atan((b*((b*x + 4)^(1/2) - 2))/((b*x)^(1/2)*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [A] time = 1.27, size = 15, normalized size = 0.88

$$\frac{2 \operatorname{asinh}\left(\frac{\sqrt{b}\sqrt{x}}{2}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x)**(1/2)/(b*x+4)**(1/2), x)

[Out] 2*asinh(sqrt(b)*sqrt(x)/2)/b

$$3.1526 \quad \int \frac{1}{\sqrt{-1+bx} \sqrt{3+bx}} dx$$

Optimal. Leaf size=19

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{bx-1}\right)}{b}$$

[Out] 2*arcsinh(1/2*(b*x-1)^(1/2))/b

Rubi [A] time = 0.01, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{bx-1}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-1 + b*x]*Sqrt[3 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[-1 + b*x]/2])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-1+bx} \sqrt{3+bx}} dx &= \frac{2 \text{Subst}\left(\int \frac{1}{\sqrt{4+x^2}} dx, x, \sqrt{-1+bx}\right)}{b} \\ &= \frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{-1+bx}\right)}{b} \end{aligned}$$

Mathematica [B] time = 0.01, size = 39, normalized size = 2.05

$$\frac{2\sqrt{bx-1} \sin^{-1}\left(\frac{1}{2}\sqrt{1-bx}\right)}{b\sqrt{1-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-1 + b*x]*Sqrt[3 + b*x]),x]

[Out] (2*Sqrt[-1 + b*x]*ArcSin[Sqrt[1 - b*x]/2])/(b*Sqrt[1 - b*x])

fricas [A] time = 0.43, size = 27, normalized size = 1.42

$$-\frac{\log(-bx + \sqrt{bx+3}\sqrt{bx-1} - 1)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-1)^(1/2)/(b*x+3)^(1/2),x, algorithm="fricas")

[Out] -log(-b*x + sqrt(b*x + 3)*sqrt(b*x - 1) - 1)/b

giac [A] time = 1.03, size = 23, normalized size = 1.21

$$-\frac{2 \log(\sqrt{bx+3} - \sqrt{bx-1})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-1)^(1/2)/(b*x+3)^(1/2),x, algorithm="giac")

[Out] -2*log(sqrt(b*x + 3) - sqrt(b*x - 1))/b

maple [B] time = 0.01, size = 64, normalized size = 3.37

$$\frac{\sqrt{(bx-1)(bx+3)} \ln\left(\frac{b^2x+b}{\sqrt{b^2}} + \sqrt{b^2x^2+2bx-3}\right)}{\sqrt{bx-1} \sqrt{bx+3} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x-1)^(1/2)/(b*x+3)^(1/2),x)

[Out] ((b*x-1)*(b*x+3))^(1/2)/(b*x-1)^(1/2)/(b*x+3)^(1/2)*ln((b^2*x+b)/(b^2)^(1/2)+(b^2*x^2+2*b*x-3)^(1/2))/(b^2)^(1/2)

maxima [B] time = 1.32, size = 33, normalized size = 1.74

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 + 2bx - 3b + 2b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-1)^(1/2)/(b*x+3)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 + 2*b*x - 3)*b + 2*b)/b

mupad [B] time = 0.32, size = 44, normalized size = 2.32

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{bx-1}-i)}{(\sqrt{3}-\sqrt{bx+3})\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x - 1)^(1/2)*(b*x + 3)^(1/2)),x)

[Out] (4*atan((b*((b*x - 1)^(1/2) - 1i))/((3^(1/2) - (b*x + 3)^(1/2))*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx-1}\sqrt{bx+3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-1)**(1/2)/(b*x+3)**(1/2),x)

[Out] Integral(1/(sqrt(b*x - 1)*sqrt(b*x + 3)), x)

$$3.1527 \quad \int \frac{1}{\sqrt{-2+bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=11

$$\frac{\cosh^{-1}\left(\frac{bx}{2}\right)}{b}$$

[Out] arccosh(1/2*b*x)/b

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {52}

$$\frac{\cosh^{-1}\left(\frac{bx}{2}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-2 + b*x]*Sqrt[2 + b*x]),x]

[Out] ArcCosh[(b*x)/2]/b

Rule 52

Int[1/(Sqrt[(a_) + (b_.)*(x_)]*Sqrt[(c_) + (d_.)*(x_)]), x_Symbol] := Simp[ArcCosh[(b*x)/a]/b, x] /; FreeQ[{a, b, c, d}, x] && EqQ[a + c, 0] && EqQ[b - d, 0] && GtQ[a, 0]

Rubi steps

$$\int \frac{1}{\sqrt{-2+bx} \sqrt{2+bx}} dx = \frac{\cosh^{-1}\left(\frac{bx}{2}\right)}{b}$$

Mathematica [B] time = 0.00, size = 25, normalized size = 2.27

$$\frac{2 \tanh^{-1}\left(\frac{\sqrt{bx-2}}{\sqrt{bx+2}}\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-2 + b*x]*Sqrt[2 + b*x]),x]

[Out] $(2*\text{ArcTanh}[\text{Sqrt}[-2 + b*x]/\text{Sqrt}[2 + b*x]])/b$

fricas [B] time = 0.44, size = 26, normalized size = 2.36

$$-\frac{\log(-bx + \sqrt{bx+2}\sqrt{bx-2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-2)^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")`

[Out] $-\log(-b*x + \text{sqrt}(b*x + 2)*\text{sqrt}(b*x - 2))/b$

giac [B] time = 1.08, size = 23, normalized size = 2.09

$$-\frac{2 \log(\sqrt{bx+2} - \sqrt{bx-2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-2)^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")`

[Out] $-2*\log(\text{sqrt}(b*x + 2) - \text{sqrt}(b*x - 2))/b$

maple [B] time = 0.01, size = 57, normalized size = 5.18

$$\frac{\sqrt{(bx-2)(bx+2)} \ln\left(\frac{b^2x}{\sqrt{b^2}} + \sqrt{b^2x^2-4}\right)}{\sqrt{bx-2} \sqrt{bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x-2)^(1/2)/(b*x+2)^(1/2),x)`

[Out] $((b*x-2)*(b*x+2))^{(1/2)}/(b*x-2)^{(1/2)}/(b*x+2)^{(1/2)}*\ln(b^2*x/(b^2)^{(1/2)}+(b^2*x^2-4)^{(1/2)})/(b^2)^{(1/2)}$

maxima [B] time = 1.33, size = 26, normalized size = 2.36

$$\frac{\log(2b^2x + 2\sqrt{b^2x^2-4}b)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-2)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $\log(2*b^2*x + 2*\text{sqrt}(b^2*x^2 - 4)*b)/b$

mupad [B] time = 0.30, size = 50, normalized size = 4.55

$$-\frac{4 \operatorname{atan}\left(\frac{b(-\sqrt{bx-2}+\sqrt{2} \operatorname{I}i)}{(\sqrt{2}-\sqrt{bx+2})\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((b*x - 2)^(1/2)*(b*x + 2)^(1/2)),x)`

[Out] $-(4*\operatorname{atan}((b*(2^{1/2})*\operatorname{I}i - (b*x - 2)^{1/2}))/((2^{1/2} - (b*x + 2)^{1/2})*(-b^2)^{1/2}))/(-b^2)^{1/2}$

sympy [C] time = 4.20, size = 75, normalized size = 6.82

$$\frac{G_{6,6}^{6,2}\left(0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1, 0 \mid \frac{4e^{2i\pi}}{b^2x^2}\right)}{4\pi^{\frac{3}{2}}b} + \frac{iG_{6,6}^{2,6}\left(-\frac{1}{2}, -\frac{1}{4}, 0, \frac{1}{4}, \frac{1}{2}, 1 \mid \frac{4}{b^2x^2}\right)}{4\pi^{\frac{3}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-2)**(1/2)/(b*x+2)**(1/2),x)`

[Out] `meijerg(((1/4, 3/4), (1/2, 1/2, 1, 1)), ((0, 1/4, 1/2, 3/4, 1, 0), ()), 4*exp_polar(2*I*pi)/(b**2*x**2))/(4*pi**(3/2)*b) + I*meijerg((-1/2, -1/4, 0, 1/4, 1/2, 1), ((-1/4, 1/4), (-1/2, 0, 0, 0)), 4/(b**2*x**2))/(4*pi**(3/2)*b)`

$$3.1528 \quad \int \frac{1}{\sqrt{-3+bx} \sqrt{1+bx}} dx$$

Optimal. Leaf size=19

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{bx-3}\right)}{b}$$

[Out] 2*arcsinh(1/2*(b*x-3)^(1/2))/b

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{bx-3}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-3 + b*x]*Sqrt[1 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[-3 + b*x]/2])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-3+bx} \sqrt{1+bx}} dx &= \frac{2 \text{Subst}\left(\int \frac{1}{\sqrt{4+x^2}} dx, x, \sqrt{-3+bx}\right)}{b} \\ &= \frac{2 \sinh^{-1}\left(\frac{1}{2}\sqrt{-3+bx}\right)}{b} \end{aligned}$$

Mathematica [B] time = 0.01, size = 39, normalized size = 2.05

$$\frac{2\sqrt{bx-3} \sin^{-1}\left(\frac{1}{2}\sqrt{3-bx}\right)}{b\sqrt{3-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-3 + b*x]*Sqrt[1 + b*x]),x]

[Out] (2*Sqrt[-3 + b*x]*ArcSin[Sqrt[3 - b*x]/2])/(b*Sqrt[3 - b*x])

fricas [A] time = 0.44, size = 27, normalized size = 1.42

$$\frac{\log(-bx + \sqrt{bx+1}\sqrt{bx-3} + 1)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-3)^(1/2)/(b*x+1)^(1/2),x, algorithm="fricas")

[Out] -log(-b*x + sqrt(b*x + 1)*sqrt(b*x - 3) + 1)/b

giac [A] time = 1.00, size = 23, normalized size = 1.21

$$\frac{2 \log(\sqrt{bx+1} - \sqrt{bx-3})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-3)^(1/2)/(b*x+1)^(1/2),x, algorithm="giac")

[Out] -2*log(sqrt(b*x + 1) - sqrt(b*x - 3))/b

maple [B] time = 0.01, size = 66, normalized size = 3.47

$$\frac{\sqrt{(bx-3)(bx+1)} \ln\left(\frac{b^2x-b}{\sqrt{b^2}} + \sqrt{b^2x^2-2bx-3}\right)}{\sqrt{bx-3} \sqrt{bx+1} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x-3)^(1/2)/(b*x+1)^(1/2),x)

[Out] ((b*x-3)*(b*x+1))^(1/2)/(b*x-3)^(1/2)/(b*x+1)^(1/2)*ln((b^2*x-b)/(b^2)^(1/2)+(b^2*x^2-2*b*x-3)^(1/2))/(b^2)^(1/2)

maxima [B] time = 1.38, size = 33, normalized size = 1.74

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 - 2bx - 3b - 2b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-3)^(1/2)/(b*x+1)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 - 2*b*x - 3)*b - 2*b)/b

mupad [B] time = 0.29, size = 46, normalized size = 2.42

$$\frac{4 \operatorname{atan}\left(\frac{b(-\sqrt{bx-3} + \sqrt{3} 1i)}{(\sqrt{bx+1}-1)\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x + 1)^(1/2)*(b*x - 3)^(1/2)),x)

[Out] (4*atan((b*(3^(1/2)*1i - (b*x - 3)^(1/2)))/(((b*x + 1)^(1/2) - 1)*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx-3}\sqrt{bx+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-3)**(1/2)/(b*x+1)**(1/2),x)

[Out] Integral(1/(sqrt(b*x - 3)*sqrt(b*x + 1)), x)

$$3.1529 \quad \int \frac{1}{\sqrt{2+bx} \sqrt{3+bx}} dx$$

Optimal. Leaf size=15

$$\frac{2 \sinh^{-1}(\sqrt{bx+2})}{b}$$

[Out] 2*arcsinh((b*x+2)^(1/2))/b

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1}(\sqrt{bx+2})}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[2 + b*x]*Sqrt[3 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[2 + b*x]])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{2+bx} \sqrt{3+bx}} dx &= \frac{2 \text{Subst}\left(\int \frac{1}{\sqrt{1+x^2}} dx, x, \sqrt{2+bx}\right)}{b} \\ &= \frac{2 \sinh^{-1}(\sqrt{2+bx})}{b} \end{aligned}$$

Mathematica [A] time = 0.00, size = 15, normalized size = 1.00

$$\frac{2 \sinh^{-1}(\sqrt{bx+2})}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[2 + b*x]*Sqrt[3 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[2 + b*x]])/b

fricas [B] time = 0.43, size = 28, normalized size = 1.87

$$\frac{\log(-2bx + 2\sqrt{bx+3}\sqrt{bx+2} - 5)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(1/2)/(b*x+3)^(1/2),x, algorithm="fricas")

[Out] -log(-2*b*x + 2*sqrt(b*x + 3)*sqrt(b*x + 2) - 5)/b

giac [A] time = 1.01, size = 23, normalized size = 1.53

$$\frac{2 \log(\sqrt{bx+3} - \sqrt{bx+2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(1/2)/(b*x+3)^(1/2),x, algorithm="giac")

[Out] -2*log(sqrt(b*x + 3) - sqrt(b*x + 2))/b

maple [B] time = 0.01, size = 66, normalized size = 4.40

$$\frac{\sqrt{(bx+2)(bx+3)} \ln\left(\frac{b^2x+\frac{5}{2}b}{\sqrt{b^2}} + \sqrt{b^2x^2+5bx+6}\right)}{\sqrt{bx+2} \sqrt{bx+3} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+2)^(1/2)/(b*x+3)^(1/2),x)

[Out] ((b*x+2)*(b*x+3))^(1/2)/(b*x+2)^(1/2)/(b*x+3)^(1/2)*ln((5/2*b+b^2*x)/(b^2)^(1/2)+(b^2*x^2+5*b*x+6)^(1/2))/(b^2)^(1/2)

maxima [B] time = 1.38, size = 33, normalized size = 2.20

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 + 5bx + 6b + 5b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)^(1/2)/(b*x+3)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 + 5*b*x + 6)*b + 5*b)/b

mupad [B] time = 0.29, size = 47, normalized size = 3.13

$$-\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{3}-\sqrt{bx+3})}{(\sqrt{2}-\sqrt{bx+2})\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x + 2)^(1/2)*(b*x + 3)^(1/2)),x)

[Out] -(4*atan((b*(3^(1/2) - (b*x + 3)^(1/2)))/((2^(1/2) - (b*x + 2)^(1/2))*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+2}\sqrt{bx+3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2)**(1/2)/(b*x+3)**(1/2),x)

[Out] Integral(1/(sqrt(b*x + 2)*sqrt(b*x + 3)), x)

$$3.1530 \quad \int \frac{1}{2+bx} dx$$

Optimal. Leaf size=10

$$\frac{\log(bx + 2)}{b}$$

[Out] ln(b*x+2)/b

Rubi [A] time = 0.00, antiderivative size = 10, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {31}

$$\frac{\log(bx + 2)}{b}$$

Antiderivative was successfully verified.

[In] Int[(2 + b*x)^(-1), x]

[Out] Log[2 + b*x]/b

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \frac{1}{2+bx} dx = \frac{\log(2+bx)}{b}$$

Mathematica [A] time = 0.00, size = 10, normalized size = 1.00

$$\frac{\log(bx + 2)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[(2 + b*x)^(-1), x]

[Out] Log[2 + b*x]/b

fricas [A] time = 0.41, size = 10, normalized size = 1.00

$$\frac{\log(bx + 2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2),x, algorithm="fricas")

[Out] log(b*x + 2)/b

giac [A] time = 0.95, size = 11, normalized size = 1.10

$$\frac{\log(|bx + 2|)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2),x, algorithm="giac")

[Out] log(abs(b*x + 2))/b

maple [A] time = 0.00, size = 11, normalized size = 1.10

$$\frac{\ln(bx + 2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+2),x)

[Out] ln(b*x+2)/b

maxima [A] time = 1.32, size = 10, normalized size = 1.00

$$\frac{\log(bx + 2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2),x, algorithm="maxima")

[Out] log(b*x + 2)/b

mupad [B] time = 0.26, size = 10, normalized size = 1.00

$$\frac{\ln(bx + 2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x + 2),x)

[Out] log(b*x + 2)/b

sympy [A] time = 0.06, size = 7, normalized size = 0.70

$$\frac{\log (bx + 2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+2),x)

[Out] log(b*x + 2)/b

$$3.1531 \quad \int \frac{1}{\sqrt{1+bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=15

$$\frac{2 \sinh^{-1}(\sqrt{bx+1})}{b}$$

[Out] 2*arcsinh((b*x+1)^(1/2))/b

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1}(\sqrt{bx+1})}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[1 + b*x]*Sqrt[2 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[1 + b*x]])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{1+bx} \sqrt{2+bx}} dx &= \frac{2 \text{Subst}\left(\int \frac{1}{\sqrt{1+x^2}} dx, x, \sqrt{1+bx}\right)}{b} \\ &= \frac{2 \sinh^{-1}(\sqrt{1+bx})}{b} \end{aligned}$$

Mathematica [A] time = 0.00, size = 15, normalized size = 1.00

$$\frac{2 \sinh^{-1}(\sqrt{bx+1})}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[1 + b*x]*Sqrt[2 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[1 + b*x]])/b

fricas [B] time = 0.42, size = 28, normalized size = 1.87

$$\frac{\log(-2bx + 2\sqrt{bx+2}\sqrt{bx+1} - 3)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+1)^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")

[Out] -log(-2*b*x + 2*sqrt(b*x + 2)*sqrt(b*x + 1) - 3)/b

giac [A] time = 0.92, size = 23, normalized size = 1.53

$$\frac{2 \log(\sqrt{bx+2} - \sqrt{bx+1})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+1)^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] -2*log(sqrt(b*x + 2) - sqrt(b*x + 1))/b

maple [B] time = 0.01, size = 66, normalized size = 4.40

$$\frac{\sqrt{(bx+1)(bx+2)} \ln\left(\frac{b^2x+\frac{3}{2}b}{\sqrt{b^2}} + \sqrt{b^2x^2+3bx+2}\right)}{\sqrt{bx+1} \sqrt{bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+1)^(1/2)/(b*x+2)^(1/2),x)

[Out] ((b*x+1)*(b*x+2))^(1/2)/(b*x+1)^(1/2)/(b*x+2)^(1/2)*ln((3/2*b+b^2*x)/(b^2)^(1/2)+(b^2*x^2+3*b*x+2)^(1/2))/(b^2)^(1/2)

maxima [B] time = 1.39, size = 33, normalized size = 2.20

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 + 3bx + 2b + 3b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+1)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 + 3*b*x + 2)*b + 3*b)/b

mupad [B] time = 0.29, size = 43, normalized size = 2.87

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{2}-\sqrt{bx+2})}{(\sqrt{bx+1}-1)\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x + 1)^(1/2)*(b*x + 2)^(1/2)),x)

[Out] (4*atan((b*(2^(1/2) - (b*x + 2)^(1/2)))/(((b*x + 1)^(1/2) - 1)*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+1}\sqrt{bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+1)**(1/2)/(b*x+2)**(1/2),x)

[Out] Integral(1/(sqrt(b*x + 1)*sqrt(b*x + 2)), x)

$$3.1532 \quad \int \frac{1}{\sqrt{bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=19

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{bx}}{\sqrt{2}}\right)}{b}$$

[Out] 2*arcsinh(1/2*(b*x)^(1/2)*2^(1/2))/b

Rubi [A] time = 0.00, antiderivative size = 19, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{bx}}{\sqrt{2}}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[b*x]*Sqrt[2 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[b*x]/Sqrt[2]])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{bx} \sqrt{2+bx}} dx &= \frac{2 \text{Subst}\left(\int \frac{1}{\sqrt{2+x^2}} dx, x, \sqrt{bx}\right)}{b} \\ &= \frac{2 \sinh^{-1}\left(\frac{\sqrt{bx}}{\sqrt{2}}\right)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 36, normalized size = 1.89

$$\frac{2\sqrt{x} \sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}\sqrt{bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[b*x]*Sqrt[2 + b*x]),x]

[Out] (2*Sqrt[x]*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(Sqrt[b]*Sqrt[b*x])

fricas [A] time = 0.44, size = 25, normalized size = 1.32

$$\frac{\log(-bx + \sqrt{bx + 2}\sqrt{bx} - 1)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x)^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")

[Out] -log(-b*x + sqrt(b*x + 2)*sqrt(b*x) - 1)/b

giac [A] time = 1.07, size = 21, normalized size = 1.11

$$\frac{2 \log(\sqrt{bx + 2} - \sqrt{bx})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x)^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] -2*log(sqrt(b*x + 2) - sqrt(b*x))/b

maple [B] time = 0.01, size = 58, normalized size = 3.05

$$\frac{\sqrt{(bx + 2)bx} \ln\left(\frac{b^2x+b}{\sqrt{b^2}} + \sqrt{b^2x^2 + 2bx}\right)}{\sqrt{bx} \sqrt{bx + 2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x)^(1/2)/(b*x+2)^(1/2),x)

[Out] (x*b*(b*x+2))^(1/2)/(b*x)^(1/2)/(b*x+2)^(1/2)*ln((b^2*x+b)/(b^2)^(1/2)+(b^2*x^2+2*b*x)^(1/2))/(b^2)^(1/2)

maxima [A] time = 1.38, size = 32, normalized size = 1.68

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 + 2bx}b + 2b\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 + 2*b*x)*b + 2*b)/b

mupad [B] time = 0.28, size = 37, normalized size = 1.95

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{2}-\sqrt{bx+2})}{\sqrt{bx}\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x)^(1/2)*(b*x + 2)^(1/2)),x)

[Out] (4*atan((b*(2^(1/2) - (b*x + 2)^(1/2)))/((b*x)^(1/2)*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [A] time = 1.35, size = 20, normalized size = 1.05

$$\frac{2 \operatorname{asinh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x)**(1/2)/(b*x+2)**(1/2),x)

[Out] 2*asinh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b

$$3.1533 \quad \int \frac{1}{\sqrt{-1+bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=21

$$\frac{2 \sinh^{-1} \left(\frac{\sqrt{bx-1}}{\sqrt{3}} \right)}{b}$$

[Out] 2*arcsinh(1/3*(b*x-1)^(1/2)*3^(1/2))/b

Rubi [A] time = 0.01, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1} \left(\frac{\sqrt{bx-1}}{\sqrt{3}} \right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-1 + b*x]*Sqrt[2 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[-1 + b*x]/Sqrt[3]])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-1+bx} \sqrt{2+bx}} dx &= \frac{2 \text{Subst} \left(\int \frac{1}{\sqrt{3+x^2}} dx, x, \sqrt{-1+bx} \right)}{b} \\ &= \frac{2 \sinh^{-1} \left(\frac{\sqrt{-1+bx}}{\sqrt{3}} \right)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 41, normalized size = 1.95

$$\frac{2\sqrt{bx-1} \sin^{-1}\left(\frac{\sqrt{1-bx}}{\sqrt{3}}\right)}{b\sqrt{1-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-1 + b*x]*Sqrt[2 + b*x]),x]

[Out] (2*Sqrt[-1 + b*x]*ArcSin[Sqrt[1 - b*x]/Sqrt[3]])/(b*Sqrt[1 - b*x])

fricas [A] time = 0.44, size = 28, normalized size = 1.33

$$\frac{\log\left(-2bx + 2\sqrt{bx+2}\sqrt{bx-1} - 1\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-1)^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")

[Out] -log(-2*b*x + 2*sqrt(b*x + 2)*sqrt(b*x - 1) - 1)/b

giac [A] time = 1.02, size = 23, normalized size = 1.10

$$\frac{2 \log\left(\sqrt{bx+2} - \sqrt{bx-1}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-1)^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] -2*log(sqrt(b*x + 2) - sqrt(b*x - 1))/b

maple [B] time = 0.01, size = 65, normalized size = 3.10

$$\frac{\sqrt{(bx-1)(bx+2)} \ln\left(\frac{b^2x+\frac{1}{2}b}{\sqrt{b^2}} + \sqrt{b^2x^2+bx-2}\right)}{\sqrt{bx-1} \sqrt{bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x-1)^(1/2)/(b*x+2)^(1/2),x)

[Out] ((b*x-1)*(b*x+2))^(1/2)/(b*x-1)^(1/2)/(b*x+2)^(1/2)*ln((1/2*b+b^2*x)/(b^2)^(1/2)+(b^2*x^2+b*x-2)^(1/2))/(b^2)^(1/2)

maxima [A] time = 1.68, size = 30, normalized size = 1.43

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 + bx - 2b + b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-1)^(1/2)/(b*x+2)^(1/2), x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 + b*x - 2)*b + b)/b

mupad [B] time = 0.29, size = 44, normalized size = 2.10

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{bx-1}-i)}{(\sqrt{2}-\sqrt{bx+2})\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x - 1)^(1/2)*(b*x + 2)^(1/2)), x)

[Out] (4*atan((b*((b*x - 1)^(1/2) - 1i))/((2^(1/2) - (b*x + 2)^(1/2))*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx-1}\sqrt{bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-1)**(1/2)/(b*x+2)**(1/2), x)

[Out] Integral(1/(sqrt(b*x - 1)*sqrt(b*x + 2)), x)

$$3.1534 \quad \int \frac{1}{\sqrt{-2+bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=11

$$\frac{\cosh^{-1}\left(\frac{bx}{2}\right)}{b}$$

[Out] arccosh(1/2*b*x)/b

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {52}

$$\frac{\cosh^{-1}\left(\frac{bx}{2}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-2 + b*x]*Sqrt[2 + b*x]),x]

[Out] ArcCosh[(b*x)/2]/b

Rule 52

Int[1/(Sqrt[(a_) + (b_.)*(x_)]*Sqrt[(c_) + (d_.)*(x_)]), x_Symbol] :> Simp[ArcCosh[(b*x)/a]/b, x] /; FreeQ[{a, b, c, d}, x] && EqQ[a + c, 0] && EqQ[b - d, 0] && GtQ[a, 0]

Rubi steps

$$\int \frac{1}{\sqrt{-2+bx} \sqrt{2+bx}} dx = \frac{\cosh^{-1}\left(\frac{bx}{2}\right)}{b}$$

Mathematica [B] time = 0.00, size = 25, normalized size = 2.27

$$\frac{2 \tanh^{-1}\left(\frac{\sqrt{bx-2}}{\sqrt{bx+2}}\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-2 + b*x]*Sqrt[2 + b*x]),x]

[Out] $(2*\text{ArcTanh}[\text{Sqrt}[-2 + b*x]/\text{Sqrt}[2 + b*x]])/b$

fricas [B] time = 0.43, size = 26, normalized size = 2.36

$$-\frac{\log(-bx + \sqrt{bx+2}\sqrt{bx-2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-2)^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")`

[Out] $-\log(-b*x + \text{sqrt}(b*x + 2)*\text{sqrt}(b*x - 2))/b$

giac [B] time = 0.96, size = 23, normalized size = 2.09

$$-\frac{2 \log(\sqrt{bx+2} - \sqrt{bx-2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-2)^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")`

[Out] $-2*\log(\text{sqrt}(b*x + 2) - \text{sqrt}(b*x - 2))/b$

maple [B] time = 0.00, size = 57, normalized size = 5.18

$$\frac{\sqrt{(bx-2)(bx+2)} \ln\left(\frac{b^2x}{\sqrt{b^2}} + \sqrt{b^2x^2-4}\right)}{\sqrt{bx-2} \sqrt{bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x-2)^(1/2)/(b*x+2)^(1/2),x)`

[Out] $((b*x-2)*(b*x+2))^(1/2)/(b*x-2)^(1/2)/(b*x+2)^(1/2)/(b^2)^(1/2)*\ln(1/(b^2)^(1/2)*b^2*x+(b^2*x^2-4)^(1/2))$

maxima [B] time = 1.36, size = 26, normalized size = 2.36

$$\frac{\log(2b^2x + 2\sqrt{b^2x^2-4}b)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-2)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $\log(2*b^2*x + 2*\text{sqrt}(b^2*x^2 - 4)*b)/b$

mupad [B] time = 0.00, size = 50, normalized size = 4.55

$$\frac{4 \operatorname{atan}\left(\frac{b(-\sqrt{bx-2}+\sqrt{2}i)}{(\sqrt{2}-\sqrt{bx+2})\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((b*x - 2)^(1/2)*(b*x + 2)^(1/2)),x)`

[Out] `-(4*atan((b*(2^(1/2)*1i - (b*x - 2)^(1/2)))/((2^(1/2) - (b*x + 2)^(1/2))*(-b^2)^(1/2))))/(-b^2)^(1/2)`

sympy [C] time = 4.28, size = 75, normalized size = 6.82

$$\frac{G_{6,6}^{6,2} \left(\begin{matrix} \frac{1}{4}, \frac{3}{4} \\ 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1, 0 \end{matrix} \middle| \frac{4e^{2i\pi}}{b^2x^2} \right) + iG_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, -\frac{1}{4}, 0, \frac{1}{4}, \frac{1}{2}, 1 \\ -\frac{1}{4}, \frac{1}{4} \end{matrix} \middle| \frac{4}{b^2x^2} \right)}{4\pi^{\frac{3}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-2)**(1/2)/(b*x+2)**(1/2),x)`

[Out] `meijerg(((1/4, 3/4), (1/2, 1/2, 1, 1)), ((0, 1/4, 1/2, 3/4, 1, 0), ()), 4*exp_polar(2*I*pi)/(b**2*x**2))/(4*pi**(3/2)*b) + I*meijerg((-1/2, -1/4, 0, 1/4, 1/2, 1), ()), ((-1/4, 1/4), (-1/2, 0, 0, 0)), 4/(b**2*x**2))/(4*pi**(3/2)*b)`

$$3.1535 \quad \int \frac{1}{\sqrt{-3+bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=21

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{bx-3}}{\sqrt{5}}\right)}{b}$$

[Out] 2*arcsinh(1/5*(b*x-3)^(1/2)*5^(1/2))/b

Rubi [A] time = 0.01, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1}\left(\frac{\sqrt{bx-3}}{\sqrt{5}}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-3 + b*x]*Sqrt[2 + b*x]),x]

[Out] (2*ArcSinh[Sqrt[-3 + b*x]/Sqrt[5]])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-3+bx} \sqrt{2+bx}} dx &= \frac{2 \text{Subst}\left(\int \frac{1}{\sqrt{5+x^2}} dx, x, \sqrt{-3+bx}\right)}{b} \\ &= \frac{2 \sinh^{-1}\left(\frac{\sqrt{-3+bx}}{\sqrt{5}}\right)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 41, normalized size = 1.95

$$\frac{2\sqrt{bx-3} \sin^{-1}\left(\frac{\sqrt{3-bx}}{\sqrt{5}}\right)}{b\sqrt{3-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-3 + b*x]*Sqrt[2 + b*x]),x]

[Out] (2*Sqrt[-3 + b*x]*ArcSin[Sqrt[3 - b*x]/Sqrt[5]])/(b*Sqrt[3 - b*x])

fricas [A] time = 0.43, size = 28, normalized size = 1.33

$$\frac{\log(-2bx + 2\sqrt{bx+2}\sqrt{bx-3} + 1)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-3)^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")

[Out] -log(-2*b*x + 2*sqrt(b*x + 2)*sqrt(b*x - 3) + 1)/b

giac [A] time = 0.96, size = 23, normalized size = 1.10

$$\frac{2 \log(\sqrt{bx+2} - \sqrt{bx-3})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-3)^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] -2*log(sqrt(b*x + 2) - sqrt(b*x - 3))/b

maple [B] time = 0.01, size = 66, normalized size = 3.14

$$\frac{\sqrt{(bx-3)(bx+2)} \ln\left(\frac{b^2x-\frac{1}{2}b}{\sqrt{b^2}} + \sqrt{b^2x^2 - bx - 6}\right)}{\sqrt{bx-3} \sqrt{bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x-3)^(1/2)/(b*x+2)^(1/2),x)

[Out] ((b*x-3)*(b*x+2))^(1/2)/(b*x-3)^(1/2)/(b*x+2)^(1/2)*ln((-1/2*b+b^2*x)/(b^2)^(1/2)+(b^2*x^2-b*x-6)^(1/2))/(b^2)^(1/2)

maxima [A] time = 1.24, size = 33, normalized size = 1.57

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 - bx - 6b - b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-3)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 - b*x - 6)*b - b)/b

mupad [B] time = 0.28, size = 50, normalized size = 2.38

$$-\frac{4 \operatorname{atan}\left(\frac{b(-\sqrt{bx-3} + \sqrt{3}i)}{(\sqrt{2} - \sqrt{bx+2})\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x + 2)^(1/2)*(b*x - 3)^(1/2)),x)

[Out] -(4*atan((b*(3^(1/2)*1i - (b*x - 3)^(1/2)))/((2^(1/2) - (b*x + 2)^(1/2))*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx-3}\sqrt{bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x-3)**(1/2)/(b*x+2)**(1/2),x)

[Out] Integral(1/(sqrt(b*x - 3)*sqrt(b*x + 2)), x)

$$3.1536 \quad \int \frac{1}{\sqrt{3-bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=16

$$-\frac{\sin^{-1}\left(\frac{1}{5}(1-2bx)\right)}{b}$$

[Out] arcsin(2/5*b*x-1/5)/b

Rubi [A] time = 0.01, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {53, 619, 216}

$$-\frac{\sin^{-1}\left(\frac{1}{5}(1-2bx)\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[3 - b*x]*Sqrt[2 + b*x]),x]

[Out] -(ArcSin[(1 - 2*b*x)/5])/b

Rule 53

Int[1/(Sqrt[(a_) + (b_)*(x_)]*Sqrt[(c_) + (d_)*(x_)]), x_Symbol] := Int[1/Sqrt[a*c - b*(a - c)*x - b^2*x^2], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b + d, 0] && GtQ[a + c, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 619

Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(p_), x_Symbol] := Dist[1/(2*c*((-4*c)/(b^2 - 4*a*c))^p), Subst[Int[Simp[1 - x^2/(b^2 - 4*a*c), x]^p, x], x, b + 2*c*x], x] /; FreeQ[{a, b, c, p}, x] && GtQ[4*a - b^2/c, 0]

Rubi steps

$$\int \frac{1}{\sqrt{3-bx}\sqrt{2+bx}} dx = \int \frac{1}{\sqrt{6+bx-b^2x^2}} dx$$

$$= -\frac{\text{Subst}\left(\int \frac{1}{\sqrt{1-\frac{x^2}{25b^2}}} dx, x, b-2b^2x\right)}{5b^2}$$

$$= -\frac{\sin^{-1}\left(\frac{1}{5}(1-2bx)\right)}{b}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 1.38

$$-\frac{2 \sin^{-1}\left(\frac{\sqrt{3-bx}}{\sqrt{5}}\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[3 - b*x]*Sqrt[2 + b*x]),x]

[Out] (-2*ArcSin[Sqrt[3 - b*x]/Sqrt[5]])/b

fricas [B] time = 0.44, size = 44, normalized size = 2.75

$$-\frac{\arctan\left(\frac{(2bx-1)\sqrt{bx+2}\sqrt{-bx+3}}{2(b^2x^2-bx-6)}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+3)^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")

[Out] -arctan(1/2*(2*b*x - 1)*sqrt(b*x + 2)*sqrt(-b*x + 3)/(b^2*x^2 - b*x - 6))/b

giac [A] time = 1.05, size = 18, normalized size = 1.12

$$\frac{2 \arcsin\left(\frac{1}{5}\sqrt{5}\sqrt{bx+2}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+3)^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] $2*\arcsin(1/5*\sqrt{5}*\sqrt{b*x + 2}))/b$

maple [B] time = 0.01, size = 65, normalized size = 4.06

$$\frac{\sqrt{-bx + 3} \sqrt{bx + 2} \arctan\left(\frac{\sqrt{b^2} \left(x - \frac{1}{2b}\right)}{\sqrt{-b^2x^2 + bx + 6}}\right)}{\sqrt{-bx + 3} \sqrt{bx + 2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-b*x+3)^(1/2)/(b*x+2)^(1/2),x)`

[Out] $((-b*x+3)*(b*x+2))^{1/2}/(-b*x+3)^{1/2}/(b*x+2)^{1/2}/(b^2)^{1/2}*\arctan((b^2)^{1/2}*(x-1/2/b)/(-b^2*x^2+b*x+6)^{1/2})$

maxima [A] time = 2.99, size = 21, normalized size = 1.31

$$-\frac{\arcsin\left(-\frac{2b^2x-b}{5b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x+3)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $-\arcsin(-1/5*(2*b^2*x - b)/b)/b$

mupad [B] time = 0.08, size = 44, normalized size = 2.75

$$-\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{3}-\sqrt{3-bx})}{(\sqrt{2}-\sqrt{bx+2})\sqrt{b^2}}\right)}{\sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((b*x + 2)^(1/2)*(3 - b*x)^(1/2)),x)`

[Out] $-(4*\operatorname{atan}((b*(3^{1/2}) - (3 - b*x)^{1/2}))/((2^{1/2}) - (b*x + 2)^{1/2})*(b^2)^{1/2})))/(b^2)^{1/2}$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{-bx + 3} \sqrt{bx + 2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x+3)**(1/2)/(b*x+2)**(1/2),x)`

[Out] `Integral(1/(sqrt(-b*x + 3)*sqrt(b*x + 2)), x)`

$$3.1537 \quad \int \frac{1}{\sqrt{2-bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=11

$$\frac{\sin^{-1}\left(\frac{bx}{2}\right)}{b}$$

[Out] arcsin(1/2*b*x)/b

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {41, 216}

$$\frac{\sin^{-1}\left(\frac{bx}{2}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[2 - b*x]*Sqrt[2 + b*x]),x]

[Out] ArcSin[(b*x)/2]/b

Rule 41

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_))^(m_.), x_Symbol] := Int[(a*c + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[b*c + a*d, 0] && (IntegerQ[m] || (GtQ[a, 0] && GtQ[c, 0]))

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{2-bx} \sqrt{2+bx}} dx &= \int \frac{1}{\sqrt{4-b^2x^2}} dx \\ &= \frac{\sin^{-1}\left(\frac{bx}{2}\right)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 11, normalized size = 1.00

$$\frac{\sin^{-1}\left(\frac{bx}{2}\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[2 - b*x]*Sqrt[2 + b*x]),x]

[Out] ArcSin[(b*x)/2]/b

fricas [B] time = 0.44, size = 31, normalized size = 2.82

$$\frac{2 \arctan\left(\frac{\sqrt{bx+2}\sqrt{-bx+2}-2}{bx}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")

[Out] -2*arctan((sqrt(b*x + 2)*sqrt(-b*x + 2) - 2)/(b*x))/b

giac [A] time = 0.91, size = 15, normalized size = 1.36

$$\frac{2 \arcsin\left(\frac{1}{2}\sqrt{bx+2}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] 2*arcsin(1/2*sqrt(b*x + 2))/b

maple [B] time = 0.01, size = 56, normalized size = 5.09

$$\frac{\sqrt{(-bx+2)(bx+2)} \arctan\left(\frac{\sqrt{b^2} x}{\sqrt{-b^2x^2+4}}\right)}{\sqrt{-bx+2} \sqrt{bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x+2)^(1/2)/(b*x+2)^(1/2),x)

[Out] ((-b*x+2)*(b*x+2))^(1/2)/(-b*x+2)^(1/2)/(b*x+2)^(1/2)/(b^2)^(1/2)*arctan((b^2)^(1/2)*x/(-b^2*x^2+4)^(1/2))

maxima [A] time = 3.03, size = 9, normalized size = 0.82

$$\frac{\arcsin\left(\frac{1}{2}bx\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")

[Out] arcsin(1/2*b*x)/b

mupad [B] time = 0.08, size = 44, normalized size = 4.00

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{2}-\sqrt{2-bx})}{(\sqrt{2}-\sqrt{bx+2})\sqrt{b^2}}\right)}{\sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((2 - b*x)^(1/2)*(b*x + 2)^(1/2)),x)

[Out] -(4*atan((b*(2^(1/2) - (2 - b*x)^(1/2)))/((2^(1/2) - (b*x + 2)^(1/2))*(b^2)^(1/2))))/(b^2)^(1/2)

sympy [C] time = 4.44, size = 76, normalized size = 6.91

$$\frac{iG_{6,6}^{6,2}\left(\begin{matrix} \frac{1}{4}, \frac{3}{4} & \frac{1}{2}, \frac{1}{2}, 1, 1 \\ 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1, 0 \end{matrix} \middle| \frac{4}{b^2x^2}\right)}{4\pi^{\frac{3}{2}}b} + \frac{G_{6,6}^{2,6}\left(\begin{matrix} -\frac{1}{2}, -\frac{1}{4}, 0, \frac{1}{4}, \frac{1}{2}, 1 \\ -\frac{1}{4}, \frac{1}{4} & -\frac{1}{2}, 0, 0, 0 \end{matrix} \middle| \frac{4e^{-2i\pi}}{b^2x^2}\right)}{4\pi^{\frac{3}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)**(1/2)/(b*x+2)**(1/2),x)

[Out] -I*meijerg(((1/4, 3/4), (1/2, 1/2, 1, 1)), ((0, 1/4, 1/2, 3/4, 1, 0), ()), 4/(b**2*x**2))/(4*pi**(3/2)*b) + meijerg(((-1/2, -1/4, 0, 1/4, 1/2, 1), ()), ((-1/4, 1/4), (-1/2, 0, 0, 0)), 4*exp_polar(-2*I*pi)/(b**2*x**2))/(4*pi**(3/2)*b)

$$3.1538 \quad \int \frac{1}{\sqrt{1-bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=16

$$-\frac{\sin^{-1}\left(\frac{1}{3}(-2bx-1)\right)}{b}$$

[Out] arcsin(2/3*b*x+1/3)/b

Rubi [A] time = 0.01, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {53, 619, 216}

$$-\frac{\sin^{-1}\left(\frac{1}{3}(-2bx-1)\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[1 - b*x]*Sqrt[2 + b*x]),x]

[Out] -(ArcSin[(-1 - 2*b*x)/3]/b)

Rule 53

Int[1/(Sqrt[(a_) + (b_)*(x_)]*Sqrt[(c_) + (d_)*(x_)]), x_Symbol] := Int[1/Sqrt[a*c - b*(a - c)*x - b^2*x^2], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b + d, 0] && GtQ[a + c, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 619

Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(p_), x_Symbol] := Dist[1/(2*c*((-4*c)/(b^2 - 4*a*c))^p), Subst[Int[Simp[1 - x^2/(b^2 - 4*a*c), x]^p, x], x, b + 2*c*x], x] /; FreeQ[{a, b, c, p}, x] && GtQ[4*a - b^2/c, 0]

Rubi steps

$$\int \frac{1}{\sqrt{1-bx}\sqrt{2+bx}} dx = \int \frac{1}{\sqrt{2-bx-b^2x^2}} dx$$

$$= -\frac{\text{Subst}\left(\int \frac{1}{\sqrt{1-\frac{x^2}{9b^2}}} dx, x, -b-2b^2x\right)}{3b^2}$$

$$= -\frac{\sin^{-1}\left(\frac{1}{3}(-1-2bx)\right)}{b}$$

Mathematica [A] time = 0.01, size = 22, normalized size = 1.38

$$-\frac{2 \sin^{-1}\left(\frac{\sqrt{1-bx}}{\sqrt{3}}\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[1 - b*x]*Sqrt[2 + b*x]), x]

[Out] (-2*ArcSin[Sqrt[1 - b*x]/Sqrt[3]])/b

fricas [B] time = 0.46, size = 43, normalized size = 2.69

$$-\frac{\arctan\left(\frac{(2bx+1)\sqrt{bx+2}\sqrt{-bx+1}}{2(b^2x^2+bx-2)}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+1)^(1/2)/(b*x+2)^(1/2), x, algorithm="fricas")

[Out] -arctan(1/2*(2*b*x + 1)*sqrt(b*x + 2)*sqrt(-b*x + 1)/(b^2*x^2 + b*x - 2))/b

giac [A] time = 1.05, size = 18, normalized size = 1.12

$$\frac{2 \arcsin\left(\frac{1}{3}\sqrt{3}\sqrt{bx+2}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+1)^(1/2)/(b*x+2)^(1/2), x, algorithm="giac")

[Out] $2 \arcsin(1/3 \sqrt{3} \sqrt{bx + 2})/b$

maple [B] time = 0.01, size = 66, normalized size = 4.12

$$\frac{\sqrt{-bx+1} \sqrt{bx+2} \arctan\left(\frac{\sqrt{b^2}\left(x+\frac{1}{2b}\right)}{\sqrt{-b^2x^2-bx+2}}\right)}{\sqrt{-bx+1} \sqrt{bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-b*x+1)^(1/2)/(b*x+2)^(1/2),x)`

[Out] $((-b*x+1)*(b*x+2))^{(1/2)/(-b*x+1)^{(1/2)/(b*x+2)^{(1/2)/(b^2)^{(1/2)*\arctan((b^2)^{(1/2)*(x+1/2/b)/(-b^2*x^2-b*x+2)^{(1/2))}}$

maxima [A] time = 3.01, size = 19, normalized size = 1.19

$$-\frac{\arcsin\left(-\frac{2b^2x+b}{3b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x+1)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $-\arcsin(-1/3*(2*b^2*x + b)/b)/b$

mupad [B] time = 0.32, size = 40, normalized size = 2.50

$$-\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{2}-\sqrt{bx+2})}{(\sqrt{1-bx}-1)\sqrt{b^2}}\right)}{\sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((1 - b*x)^(1/2)*(b*x + 2)^(1/2)),x)`

[Out] $-(4*\operatorname{atan}((b*(2^{(1/2)} - (b*x + 2)^{(1/2)}))/(((1 - b*x)^{(1/2)} - 1)*(b^2)^{(1/2)})))/((b^2)^{(1/2)}$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{-bx+1} \sqrt{bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x+1)**(1/2)/(b*x+2)**(1/2),x)`

[Out] `Integral(1/(sqrt(-b*x + 1)*sqrt(b*x + 2)), x)`

$$3.1539 \quad \int \frac{1}{\sqrt{-bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=10

$$\frac{\sin^{-1}(bx+1)}{b}$$

[Out] arcsin(b*x+1)/b

Rubi [A] time = 0.01, antiderivative size = 10, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {53, 619, 216}

$$\frac{\sin^{-1}(bx+1)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-(b*x)]*Sqrt[2 + b*x]),x]

[Out] ArcSin[1 + b*x]/b

Rule 53

Int[1/(Sqrt[(a_) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] :> Int[1/Sqrt[a*c - b*(a - c)*x - b^2*x^2], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b + d, 0] && GtQ[a + c, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 619

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] :> Dist[1/(2*c*((-4*c)/(b^2 - 4*a*c))^p), Subst[Int[Simp[1 - x^2/(b^2 - 4*a*c), x]^p, x], x, b + 2*c*x], x] /; FreeQ[{a, b, c, p}, x] && GtQ[4*a - b^2/c, 0]

Rubi steps

$$\int \frac{1}{\sqrt{-bx}\sqrt{2+bx}} dx = \int \frac{1}{\sqrt{-2bx-b^2x^2}} dx$$

$$= \frac{\text{Subst}\left(\int \frac{1}{\sqrt{1-\frac{x^2}{4b^2}}} dx, x, -2b-2b^2x\right)}{2b^2}$$

$$= \frac{\sin^{-1}(1+bx)}{b}$$

Mathematica [B] time = 0.01, size = 51, normalized size = 5.10

$$\frac{2\sqrt{x}\sqrt{bx+2}\sinh^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}\sqrt{-bx}(bx+2)}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-(b*x)]*Sqrt[2 + b*x]),x]

[Out] (2*Sqrt[x]*Sqrt[2 + b*x]*ArcSinh[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(Sqrt[b]*Sqrt[-(b*x*(2 + b*x))])

fricas [B] time = 0.43, size = 26, normalized size = 2.60

$$-\frac{2 \arctan\left(\frac{\sqrt{bx+2}\sqrt{-bx}}{bx}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x)^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")

[Out] -2*arctan(sqrt(b*x + 2)*sqrt(-b*x)/(b*x))/b

giac [A] time = 0.93, size = 18, normalized size = 1.80

$$\frac{2 \arcsin\left(\frac{1}{2}\sqrt{2}\sqrt{bx+2}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x)^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] $2*\arcsin(1/2*\sqrt{2}*\sqrt{b*x + 2})/b$

maple [B] time = 0.00, size = 58, normalized size = 5.80

$$\frac{\sqrt{-(bx+2)bx} \arctan\left(\frac{\sqrt{b^2}\left(x+\frac{1}{b}\right)}{\sqrt{-b^2x^2-2bx}}\right)}{\sqrt{-bx} \sqrt{bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/(-b*x)^{(1/2)}/(b*x+2)^{(1/2)}, x)$

[Out] $(-(b*x+2)*b*x)^{(1/2)}/(-b*x)^{(1/2)}/(b*x+2)^{(1/2)}/(b^2)^{(1/2)}*\arctan((b^2)^{(1/2)}*(x+1/b)/(-b^2*x^2-2*b*x)^{(1/2)})$

maxima [A] time = 3.14, size = 18, normalized size = 1.80

$$-\frac{\arcsin\left(-\frac{b^2x+b}{b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(-b*x)^{(1/2)}/(b*x+2)^{(1/2)}, x, \text{algorithm}="maxima")$

[Out] $-\arcsin(-(b^2*x + b)/b)/b$

mupad [B] time = 0.29, size = 34, normalized size = 3.40

$$-\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{2}-\sqrt{bx+2})}{\sqrt{-bx} \sqrt{b^2}}\right)}{\sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(1/((-b*x)^{(1/2)}*(b*x + 2)^{(1/2)}), x)$

[Out] $-(4*\operatorname{atan}((b*(2^{(1/2)} - (b*x + 2)^{(1/2)}))/((-b*x)^{(1/2)}*(b^2)^{(1/2)})))/(b^2)^{(1/2)}$

sympy [C] time = 1.28, size = 24, normalized size = 2.40

$$-\frac{2i \operatorname{asinh}\left(\frac{\sqrt{2} \sqrt{b} \sqrt{x}}{2}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(-b*x)**(1/2)/(b*x+2)**(1/2), x)$

[Out] $-2*I*\operatorname{asinh}(\sqrt{2}*\sqrt{b}*\sqrt{x}/2)/b$

$$3.1540 \quad \int \frac{1}{\sqrt{-1-bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=11

$$\frac{\sin^{-1}(2bx + 3)}{b}$$

[Out] arcsin(2*b*x+3)/b

Rubi [A] time = 0.01, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {53, 619, 216}

$$\frac{\sin^{-1}(2bx + 3)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-1 - b*x]*Sqrt[2 + b*x]),x]

[Out] ArcSin[3 + 2*b*x]/b

Rule 53

Int[1/(Sqrt[(a_) + (b_)*(x_)]*Sqrt[(c_) + (d_)*(x_)]), x_Symbol] := Int[1/Sqrt[a*c - b*(a - c)*x - b^2*x^2], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b + d, 0] && GtQ[a + c, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 619

Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(p_), x_Symbol] := Dist[1/(2*c*((-4*c)/(b^2 - 4*a*c))^p), Subst[Int[Simp[1 - x^2/(b^2 - 4*a*c), x]^p, x], x, b + 2*c*x], x] /; FreeQ[{a, b, c, p}, x] && GtQ[4*a - b^2/c, 0]

Rubi steps

$$\int \frac{1}{\sqrt{-1-bx}\sqrt{2+bx}} dx = \int \frac{1}{\sqrt{-2-3bx-b^2x^2}} dx$$

$$= \frac{\text{Subst}\left(\int \frac{1}{\sqrt{1-\frac{x^2}{b^2}}} dx, x, -3b-2b^2x\right)}{b^2}$$

$$= \frac{\sin^{-1}(3+2bx)}{b}$$

Mathematica [B] time = 0.01, size = 49, normalized size = 4.45

$$\frac{2\sqrt{bx+1}\sqrt{bx+2}\sinh^{-1}(\sqrt{bx+1})}{b\sqrt{-((bx+1)(bx+2))}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-1 - b*x]*Sqrt[2 + b*x]), x]

[Out] (2*Sqrt[1 + b*x]*Sqrt[2 + b*x]*ArcSinh[Sqrt[1 + b*x]])/(b*Sqrt[-((1 + b*x)*(2 + b*x))])

fricas [B] time = 0.45, size = 44, normalized size = 4.00

$$\frac{\arctan\left(\frac{(2bx+3)\sqrt{bx+2}\sqrt{-bx-1}}{2(b^2x^2+3bx+2)}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-1)^(1/2)/(b*x+2)^(1/2), x, algorithm="fricas")

[Out] -arctan(1/2*(2*b*x + 3)*sqrt(b*x + 2)*sqrt(-b*x - 1)/(b^2*x^2 + 3*b*x + 2))/b

giac [A] time = 1.17, size = 13, normalized size = 1.18

$$\frac{2 \arcsin(\sqrt{bx+2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-1)^(1/2)/(b*x+2)^(1/2), x, algorithm="giac")

[Out] $2*\arcsin(\sqrt{b*x + 2})/b$

maple [B] time = 0.01, size = 66, normalized size = 6.00

$$\frac{\sqrt{(-bx-1)(bx+2)} \arctan\left(\frac{\sqrt{b^2}\left(x+\frac{3}{2b}\right)}{\sqrt{-b^2x^2-3bx-2}}\right)}{\sqrt{-bx-1} \sqrt{bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-b*x-1)^(1/2)/(b*x+2)^(1/2),x)`

[Out] $((-b*x-1)*(b*x+2))^{(1/2)/(-b*x-1)^{(1/2)/(b*x+2)^{(1/2)/(b^2)^{(1/2)*\arctan((b^2)^{(1/2)*(x+3/2/b)/(-b^2*x^2-3*b*x-2)^{(1/2))}}$

maxima [A] time = 3.01, size = 21, normalized size = 1.91

$$\frac{\arcsin\left(-\frac{2b^2x+3b}{b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x-1)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $-\arcsin(-(2*b^2*x + 3*b)/b)/b$

mupad [B] time = 0.30, size = 41, normalized size = 3.73

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{-bx-1}-i)}{(\sqrt{2}-\sqrt{bx+2})\sqrt{b^2}}\right)}{\sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((-b*x-1)^(1/2)*(b*x+2)^(1/2)),x)`

[Out] $(4*\operatorname{atan}((b*((-b*x-1)^{(1/2)}-1i))/((2^{(1/2)}-(b*x+2)^{(1/2)})*(b^2)^{(1/2)})))/((b^2)^{(1/2)})$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{-bx-1} \sqrt{bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x-1)**(1/2)/(b*x+2)**(1/2),x)`

[Out] `Integral(1/(sqrt(-b*x-1)*sqrt(b*x+2)),x)`

$$3.1541 \quad \int \frac{1}{\sqrt{-2-bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=29

$$\frac{\sqrt{bx+2} \log(bx+2)}{b\sqrt{-bx-2}}$$

[Out] $\ln(b*x+2)*(b*x+2)^{(1/2)}/b/(-b*x-2)^{(1/2)}$

Rubi [A] time = 0.00, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {23, 31}

$$\frac{\sqrt{bx+2} \log(bx+2)}{b\sqrt{-bx-2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/(\text{Sqrt}[-2 - b*x]*\text{Sqrt}[2 + b*x]), x]$

[Out] $(\text{Sqrt}[2 + b*x]*\text{Log}[2 + b*x])/(b*\text{Sqrt}[-2 - b*x])$

Rule 23

$\text{Int}[(u_.)*((a_.) + (b_.)*(v_.))^{(m_.)*((c_.) + (d_.)*(v_.))^{(n_.)}, x_Symbol] \rightarrow \text{Dist}[(a + b*v)^m/(c + d*v)^m, \text{Int}[u*(c + d*v)^{(m+n)}, x], x] /;$ $\text{FreeQ}\{a, b, c, d, m, n\}, x\} \ \&\& \ \text{EqQ}[b*c - a*d, 0] \ \&\& \ \text{IntegerQ}[m] \ || \ \text{IntegerQ}[n] \ || \ \text{GtQ}[b/d, 0]$

Rule 31

$\text{Int}[((a_.) + (b_.)*(x_.))^{(-1)}, x_Symbol] \rightarrow \text{Simp}[\text{Log}[\text{RemoveContent}[a + b*x, x]]/b, x] /;$ $\text{FreeQ}\{a, b\}, x\}$

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-2-bx} \sqrt{2+bx}} dx &= \frac{\sqrt{2+bx} \int \frac{1}{2+bx} dx}{\sqrt{-2-bx}} \\ &= \frac{\sqrt{2+bx} \log(2+bx)}{b\sqrt{-2-bx}} \end{aligned}$$

Mathematica [A] time = 0.01, size = 28, normalized size = 0.97

$$\frac{(bx + 2) \log(bx + 2)}{b\sqrt{-(bx + 2)^2}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-2 - b*x]*Sqrt[2 + b*x]),x]

[Out] ((2 + b*x)*Log[2 + b*x])/(b*Sqrt[-(2 + b*x)^2])

fricas [A] time = 0.44, size = 1, normalized size = 0.03

0

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-2)^(1/2)/(b*x+2)^(1/2),x, algorithm="fricas")

[Out] 0

giac [C] time = 0.97, size = 12, normalized size = 0.41

$$-\frac{i \log(|bx + 2|)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-2)^(1/2)/(b*x+2)^(1/2),x, algorithm="giac")

[Out] -I*log(abs(b*x + 2))/b

maple [A] time = 0.00, size = 26, normalized size = 0.90

$$\frac{\sqrt{bx + 2} \ln(bx + 2)}{\sqrt{-bx - 2} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x-2)^(1/2)/(b*x+2)^(1/2),x)

[Out] ln(b*x+2)*(b*x+2)^(1/2)/b/(-b*x-2)^(1/2)

maxima [A] time = 1.35, size = 16, normalized size = 0.55

$$\sqrt{-\frac{1}{b^2}} \log\left(x + \frac{2}{b}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x-2)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")`

[Out] `sqrt(-1/b^2)*log(x + 2/b)`

mupad [B] time = 0.07, size = 47, normalized size = 1.62

$$\frac{4 \operatorname{atan}\left(\frac{b(-\sqrt{-bx-2}+\sqrt{2} \operatorname{I}i)}{(\sqrt{2}-\sqrt{bx+2})\sqrt{b^2}}\right)}{\sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((b*x + 2)^(1/2)*(- b*x - 2)^(1/2)),x)`

[Out] `-(4*atan((b*(2^(1/2)*1i - (- b*x - 2)^(1/2)))/((2^(1/2) - (b*x + 2)^(1/2))* (b^2)^(1/2))))/(b^2)^(1/2)`

sympy [C] time = 1.98, size = 53, normalized size = 1.83

$$\begin{cases} \frac{i \log\left(x + \frac{2}{b}\right)}{b} & \text{for } \left|x + \frac{2}{b}\right| < 1 \\ \frac{i \log\left(\frac{1}{x + \frac{2}{b}}\right)}{b} & \text{for } \frac{1}{\left|x + \frac{2}{b}\right|} < 1 \\ \frac{i G_{2,2}^{2,0}\left(0, 0 \left| x + \frac{2}{b} \right.\right)}{b} - \frac{i G_{2,2}^{0,2}\left(1, 1 \left| x + \frac{2}{b} \right.\right)}{b} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x-2)**(1/2)/(b*x+2)**(1/2),x)`

[Out] `Piecewise((-I*log(x + 2/b)/b, Abs(x + 2/b) < 1), (I*log(1/(x + 2/b))/b, 1/Abs(x + 2/b) < 1), (I*meijerg(((), (1, 1)), ((0, 0), ()), x + 2/b)/b - I*meijerg(((1, 1), ()), (((), (0, 0)), x + 2/b)/b, True))`

$$3.1542 \quad \int \frac{1}{\sqrt{-3-bx} \sqrt{2+bx}} dx$$

Optimal. Leaf size=26

$$-\frac{2 \tan^{-1}\left(\frac{\sqrt{-bx-3}}{\sqrt{bx+2}}\right)}{b}$$

[Out] $-2*\arctan((-b*x-3)^{(1/2)/(b*x+2)^{(1/2)})/b$

Rubi [A] time = 0.01, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {63, 217, 203}

$$-\frac{2 \tan^{-1}\left(\frac{\sqrt{-bx-3}}{\sqrt{bx+2}}\right)}{b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/(\text{Sqrt}[-3 - b*x]*\text{Sqrt}[2 + b*x]),x]$

[Out] $(-2*\text{ArcTan}[\text{Sqrt}[-3 - b*x]/\text{Sqrt}[2 + b*x]])/b$

Rule 63

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_)}*((c_.) + (d_.)*(x_)^{(n_)}), x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 203

$\text{Int}[(a_) + (b_.)*(x_)^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(1*\text{ArcTan}[(\text{Rt}[b, 2]*x)/\text{Rt}[a, 2]])/(\text{Rt}[a, 2]*\text{Rt}[b, 2]), x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a/b] \&\& (\text{GtQ}[a, 0] \parallel \text{GtQ}[b, 0])$

Rule 217

$\text{Int}[1/\text{Sqrt}[(a_) + (b_.)*(x_)^2], x_Symbol] \rightarrow \text{Subst}[\text{Int}[1/(1 - b*x^2), x], x, x/\text{Sqrt}[a + b*x^2]] /; \text{FreeQ}\{a, b\}, x] \&\& !\text{GtQ}[a, 0]$

Rubi steps

$$\int \frac{1}{\sqrt{-3-bx}\sqrt{2+bx}} dx = -\frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{-1-x^2}} dx, x, \sqrt{-3-bx}\right)}{b}$$

$$= -\frac{2 \operatorname{Subst}\left(\int \frac{1}{1+x^2} dx, x, \frac{\sqrt{-3-bx}}{\sqrt{2+bx}}\right)}{b}$$

$$= -\frac{2 \tan^{-1}\left(\frac{\sqrt{-3-bx}}{\sqrt{2+bx}}\right)}{b}$$

Mathematica [B] time = 0.02, size = 53, normalized size = 2.04

$$-\frac{2\sqrt{-bx-3}\sqrt{-bx-2}\sin^{-1}(\sqrt{bx+3})}{b\sqrt{bx+2}\sqrt{bx+3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-3 - b*x]*Sqrt[2 + b*x]), x]

[Out] (-2*Sqrt[-3 - b*x]*Sqrt[-2 - b*x]*ArcSin[Sqrt[3 + b*x]])/(b*Sqrt[2 + b*x]*Sqrt[3 + b*x])

fricas [A] time = 0.45, size = 44, normalized size = 1.69

$$-\frac{\arctan\left(\frac{(2bx+5)\sqrt{bx+2}\sqrt{-bx-3}}{2(b^2x^2+5bx+6)}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-3)^(1/2)/(b*x+2)^(1/2), x, algorithm="fricas")

[Out] -arctan(1/2*(2*b*x + 5)*sqrt(b*x + 2)*sqrt(-b*x - 3)/(b^2*x^2 + 5*b*x + 6))/b

giac [C] time = 1.07, size = 23, normalized size = 0.88

$$\frac{2i \log(\sqrt{bx+3} - \sqrt{bx+2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-3)^(1/2)/(b*x+2)^(1/2), x, algorithm="giac")

[Out] $2*I*\log(\sqrt{b*x + 3} - \sqrt{b*x + 2})/b$

maple [B] time = 0.01, size = 66, normalized size = 2.54

$$\frac{\sqrt{(-bx-3)(bx+2)} \arctan\left(\frac{\sqrt{b^2}\left(x+\frac{5}{2b}\right)}{\sqrt{-b^2x^2-5bx-6}}\right)}{\sqrt{-bx-3} \sqrt{bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-b*x-3)^(1/2)/(b*x+2)^(1/2),x)`

[Out] $((-b*x-3)*(b*x+2))^{(1/2)/(-b*x-3)^{(1/2)/(b*x+2)^{(1/2)/(b^2)^{(1/2)*\arctan((b^2)^{(1/2)*(x+5/2/b)/(-b^2*x^2-5*b*x-6)^{(1/2))}}$

maxima [A] time = 3.01, size = 21, normalized size = 0.81

$$\frac{\arcsin\left(-\frac{2b^2x+5b}{b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x-3)^(1/2)/(b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $-\arcsin(-(2*b^2*x + 5*b)/b)/b$

mupad [B] time = 0.30, size = 47, normalized size = 1.81

$$\frac{4 \operatorname{atan}\left(\frac{b(-\sqrt{-bx-3} + \sqrt{3} \operatorname{I}i)}{(\sqrt{2} - \sqrt{bx+2}) \sqrt{b^2}}\right)}{\sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((b*x + 2)^(1/2)*(- b*x - 3)^(1/2)),x)`

[Out] $-(4*\operatorname{atan}((b*(3^{(1/2)}*1i - (- b*x - 3)^{(1/2)}))/((2^{(1/2)} - (b*x + 2)^{(1/2)})*(b^2)^{(1/2)})))/(b^2)^{(1/2)}$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{-bx-3} \sqrt{bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x-3)**(1/2)/(b*x+2)**(1/2),x)`

[Out] `Integral(1/(sqrt(-b*x - 3)*sqrt(b*x + 2)), x)`

$$3.1543 \quad \int \frac{1}{\sqrt{2-bx} \sqrt{3-bx}} dx$$

Optimal. Leaf size=16

$$-\frac{2 \sinh^{-1}(\sqrt{2-bx})}{b}$$

[Out] -2*arcsinh((-b*x+2)^(1/2))/b

Rubi [A] time = 0.01, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.095$, Rules used = {63, 215}

$$-\frac{2 \sinh^{-1}(\sqrt{2-bx})}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[2 - b*x]*Sqrt[3 - b*x]),x]

[Out] (-2*ArcSinh[Sqrt[2 - b*x]])/b

Rule 63

Int[((a_.) + (b_.)*(x_)^(m_))*((c_.) + (d_.)*(x_)^(n_)), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{2-bx} \sqrt{3-bx}} dx &= -\frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{1+x^2}} dx, x, \sqrt{2-bx}\right)}{b} \\ &= -\frac{2 \sinh^{-1}(\sqrt{2-bx})}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 16, normalized size = 1.00

$$\frac{2 \sinh^{-1}(\sqrt{2-bx})}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[2 - b*x]*Sqrt[3 - b*x]),x]

[Out] (-2*ArcSinh[Sqrt[2 - b*x]])/b

fricas [B] time = 0.45, size = 30, normalized size = 1.88

$$\frac{\log(-2bx + 2\sqrt{-bx+3}\sqrt{-bx+2} + 5)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(1/2)/(-b*x+3)^(1/2),x, algorithm="fricas")

[Out] -log(-2*b*x + 2*sqrt(-b*x + 3)*sqrt(-b*x + 2) + 5)/b

giac [A] time = 1.04, size = 25, normalized size = 1.56

$$\frac{2 \log(\sqrt{-bx+3} - \sqrt{-bx+2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(1/2)/(-b*x+3)^(1/2),x, algorithm="giac")

[Out] 2*log(sqrt(-b*x + 3) - sqrt(-b*x + 2))/b

maple [B] time = 0.01, size = 70, normalized size = 4.38

$$\frac{\sqrt{(-bx+2)(-bx+3)} \ln\left(\frac{b^2x-\frac{5}{2}b}{\sqrt{b^2}} + \sqrt{b^2x^2 - 5bx + 6}\right)}{\sqrt{-bx+2} \sqrt{-bx+3} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x+2)^(1/2)/(-b*x+3)^(1/2),x)

[Out] ((-b*x+2)*(-b*x+3))^(1/2)/(-b*x+2)^(1/2)/(-b*x+3)^(1/2)*ln((-5/2*b+b^2*x)/(b^2)^(1/2)+(b^2*x^2-5*b*x+6)^(1/2))/(b^2)^(1/2)

maxima [B] time = 1.36, size = 33, normalized size = 2.06

$$\frac{\log(2b^2x + 2\sqrt{b^2x^2 - 5bx + 6b - 5b})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)^(1/2)/(-b*x+3)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 - 5*b*x + 6)*b - 5*b)/b

mupad [B] time = 0.31, size = 49, normalized size = 3.06

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{3}-\sqrt{3-bx})}{(\sqrt{2}-\sqrt{2-bx})\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((2 - b*x)^(1/2)*(3 - b*x)^(1/2)),x)

[Out] (4*atan((b*(3^(1/2) - (3 - b*x)^(1/2)))/((2^(1/2) - (2 - b*x)^(1/2))*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{-bx + 2}\sqrt{-bx + 3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2)**(1/2)/(-b*x+3)**(1/2),x)

[Out] Integral(1/(sqrt(-b*x + 2)*sqrt(-b*x + 3)), x)

$$3.1544 \quad \int \frac{1}{2-bx} dx$$

Optimal. Leaf size=12

$$-\frac{\log(2-bx)}{b}$$

[Out] $-\ln(-b*x+2)/b$

Rubi [A] time = 0.00, antiderivative size = 12, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {31}

$$-\frac{\log(2-bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[(2 - b*x)^(-1), x]

[Out] $-(\text{Log}[2 - b*x])/b$

Rule 31

Int[((a_) + (b_.)*(x_))^(n_), x_Symbol] := Simp[Log[RemoveContent[a + b*x, x]]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \frac{1}{2-bx} dx = -\frac{\log(2-bx)}{b}$$

Mathematica [A] time = 0.00, size = 12, normalized size = 1.00

$$-\frac{\log(2-bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[(2 - b*x)^(-1), x]

[Out] $-(\text{Log}[2 - b*x])/b$

fricas [A] time = 0.44, size = 11, normalized size = 0.92

$$-\frac{\log(bx-2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2),x, algorithm="fricas")

[Out] $-\log(b*x - 2)/b$

giac [A] time = 1.10, size = 12, normalized size = 1.00

$$-\frac{\log(|bx - 2|)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2),x, algorithm="giac")

[Out] $-\log(\text{abs}(b*x - 2))/b$

maple [A] time = 0.00, size = 13, normalized size = 1.08

$$-\frac{\ln(-bx + 2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x+2),x)

[Out] $-\ln(-b*x+2)/b$

maxima [A] time = 1.42, size = 11, normalized size = 0.92

$$-\frac{\log(bx - 2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2),x, algorithm="maxima")

[Out] $-\log(b*x - 2)/b$

mupad [B] time = 0.03, size = 11, normalized size = 0.92

$$-\frac{\ln(bx - 2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-1/(b*x - 2),x)

[Out] $-\log(b*x - 2)/b$

sympy [A] time = 0.07, size = 8, normalized size = 0.67

$$-\frac{\log(bx - 2)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+2),x)

[Out] -log(b*x - 2)/b

$$3.1545 \quad \int \frac{1}{\sqrt{1-bx} \sqrt{2-bx}} dx$$

Optimal. Leaf size=16

$$-\frac{2 \sinh^{-1}(\sqrt{1-bx})}{b}$$

[Out] -2*arcsinh((-b*x+1)^(1/2))/b

Rubi [A] time = 0.01, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.095$, Rules used = {63, 215}

$$-\frac{2 \sinh^{-1}(\sqrt{1-bx})}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[1 - b*x]*Sqrt[2 - b*x]),x]

[Out] (-2*ArcSinh[Sqrt[1 - b*x]])/b

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{1-bx} \sqrt{2-bx}} dx &= -\frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{1+x^2}} dx, x, \sqrt{1-bx}\right)}{b} \\ &= -\frac{2 \sinh^{-1}(\sqrt{1-bx})}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 16, normalized size = 1.00

$$\frac{2 \sinh^{-1}(\sqrt{1-bx})}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[1 - b*x]*Sqrt[2 - b*x]),x]

[Out] (-2*ArcSinh[Sqrt[1 - b*x]])/b

fricas [B] time = 0.42, size = 30, normalized size = 1.88

$$\frac{\log(-2bx + 2\sqrt{-bx+2}\sqrt{-bx+1} + 3)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+1)^(1/2)/(-b*x+2)^(1/2),x, algorithm="fricas")

[Out] -log(-2*b*x + 2*sqrt(-b*x + 2)*sqrt(-b*x + 1) + 3)/b

giac [A] time = 0.85, size = 25, normalized size = 1.56

$$\frac{2 \log(\sqrt{-bx+2} - \sqrt{-bx+1})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+1)^(1/2)/(-b*x+2)^(1/2),x, algorithm="giac")

[Out] 2*log(sqrt(-b*x + 2) - sqrt(-b*x + 1))/b

maple [B] time = 0.01, size = 70, normalized size = 4.38

$$\frac{\sqrt{(-bx+1)(-bx+2)} \ln\left(\frac{b^2x-\frac{3}{2}b}{\sqrt{b^2}} + \sqrt{b^2x^2 - 3bx + 2}\right)}{\sqrt{-bx+1} \sqrt{-bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x+1)^(1/2)/(-b*x+2)^(1/2),x)

[Out] ((-b*x+1)*(-b*x+2))^(1/2)/(-b*x+1)^(1/2)/(-b*x+2)^(1/2)*ln((-3/2*b+b^2*x)/(b^2)^(1/2)+(b^2*x^2-3*b*x+2)^(1/2))/(b^2)^(1/2)

maxima [B] time = 1.33, size = 33, normalized size = 2.06

$$\frac{\log(2b^2x + 2\sqrt{b^2x^2 - 3bx + 2b - 3b})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+1)^(1/2)/(-b*x+2)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 - 3*b*x + 2)*b - 3*b)/b

mupad [B] time = 0.31, size = 45, normalized size = 2.81

$$-\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{2}-\sqrt{2-bx})}{(\sqrt{1-bx}-1)\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((1 - b*x)^(1/2)*(2 - b*x)^(1/2)),x)

[Out] -(4*atan((b*(2^(1/2) - (2 - b*x)^(1/2)))/(((1 - b*x)^(1/2) - 1)*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{-bx+1}\sqrt{-bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+1)**(1/2)/(-b*x+2)**(1/2),x)

[Out] Integral(1/(sqrt(-b*x + 1)*sqrt(-b*x + 2)), x)

$$3.1546 \quad \int \frac{1}{\sqrt{-bx} \sqrt{2-bx}} dx$$

Optimal. Leaf size=20

$$-\frac{2 \sinh^{-1}\left(\frac{\sqrt{-bx}}{\sqrt{2}}\right)}{b}$$

[Out] $-2*\operatorname{arcsinh}(1/2*(-b*x)^{(1/2)*2^{(1/2)}})/b$

Rubi [A] time = 0.01, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 215}

$$-\frac{2 \sinh^{-1}\left(\frac{\sqrt{-bx}}{\sqrt{2}}\right)}{b}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/(\operatorname{Sqrt}[-(b*x)]*\operatorname{Sqrt}[2 - b*x]), x]$

[Out] $(-2*\operatorname{ArcSinh}[\operatorname{Sqrt}[-(b*x)]/\operatorname{Sqrt}[2]])/b$

Rule 63

$\operatorname{Int}[(a_.) + (b_.)*(x_)^{(m_)}*((c_.) + (d_.)*(x_)^{(n_)}, x_Symbol] :> \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /; \operatorname{FreeQ}[\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 215

$\operatorname{Int}[1/\operatorname{Sqrt}[(a_) + (b_.)*(x_)^2], x_Symbol] :> \operatorname{Simp}[\operatorname{ArcSinh}[(\operatorname{Rt}[b, 2]*x)/\operatorname{Sqrt}[a]]/\operatorname{Rt}[b, 2], x] /; \operatorname{FreeQ}[\{a, b\}, x] \&\& \operatorname{GtQ}[a, 0] \&\& \operatorname{PosQ}[b]$

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-bx} \sqrt{2-bx}} dx &= -\frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{2+x^2}} dx, x, \sqrt{-bx}\right)}{b} \\ &= -\frac{2 \sinh^{-1}\left(\frac{\sqrt{-bx}}{\sqrt{2}}\right)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 37, normalized size = 1.85

$$\frac{2\sqrt{x} \sin^{-1}\left(\frac{\sqrt{b}\sqrt{x}}{\sqrt{2}}\right)}{\sqrt{b}\sqrt{-bx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-(b*x)]*Sqrt[2 - b*x]), x]

[Out] (2*Sqrt[x]*ArcSin[(Sqrt[b]*Sqrt[x])/Sqrt[2]])/(Sqrt[b]*Sqrt[-(b*x)])

fricas [A] time = 0.44, size = 27, normalized size = 1.35

$$-\frac{\log(-bx + \sqrt{-bx + 2}\sqrt{-bx} + 1)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x)^(1/2)/(-b*x+2)^(1/2), x, algorithm="fricas")

[Out] -log(-b*x + sqrt(-b*x + 2)*sqrt(-b*x) + 1)/b

giac [A] time = 1.03, size = 23, normalized size = 1.15

$$\frac{2 \log(\sqrt{-bx + 2} - \sqrt{-bx})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x)^(1/2)/(-b*x+2)^(1/2), x, algorithm="giac")

[Out] 2*log(sqrt(-b*x + 2) - sqrt(-b*x))/b

maple [B] time = 0.01, size = 64, normalized size = 3.20

$$\frac{\sqrt{-(-bx + 2)bx} \ln\left(\frac{b^2x - b}{\sqrt{b^2}} + \sqrt{b^2x^2 - 2bx}\right)}{\sqrt{-bx} \sqrt{-bx + 2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x)^(1/2)/(-b*x+2)^(1/2), x)

[Out] (-x*b*(-b*x+2))^(1/2)/(-b*x)^(1/2)/(-b*x+2)^(1/2)*ln((b^2*x-b)/(b^2)^(1/2)+(b^2*x^2-2*b*x)^(1/2))/(b^2)^(1/2)

maxima [A] time = 1.36, size = 32, normalized size = 1.60

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 - 2bx}b - 2b\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x)^(1/2)/(-b*x+2)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 - 2*b*x)*b - 2*b)/b

mupad [B] time = 0.28, size = 39, normalized size = 1.95

$$-\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{2}-\sqrt{2-bx})}{\sqrt{-bx}\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((-b*x)^(1/2)*(2 - b*x)^(1/2)),x)

[Out] -(4*atan((b*(2^(1/2) - (2 - b*x)^(1/2)))/((-b*x)^(1/2)*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [A] time = 1.34, size = 53, normalized size = 2.65

$$\left\{ \begin{array}{l} -\frac{2 \operatorname{acosh}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b} \quad \text{for } \frac{|bx|}{2} > 1 \\ -\frac{2i \operatorname{asin}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{x}}{2}\right)}{b} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x)**(1/2)/(-b*x+2)**(1/2),x)

[Out] Piecewise((-2*acosh(sqrt(2)*sqrt(b)*sqrt(x)/2)/b, Abs(b*x)/2 > 1), (-2*I*asin(sqrt(2)*sqrt(b)*sqrt(x)/2)/b, True))

$$3.1547 \quad \int \frac{1}{\sqrt{-1-bx} \sqrt{2-bx}} dx$$

Optimal. Leaf size=22

$$-\frac{2 \sinh^{-1}\left(\frac{\sqrt{-bx-1}}{\sqrt{3}}\right)}{b}$$

[Out] $-2*\operatorname{arcsinh}(1/3*(-b*x-1)^{(1/2)}*3^{(1/2)})/b$

Rubi [A] time = 0.01, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.095$, Rules used = {63, 215}

$$-\frac{2 \sinh^{-1}\left(\frac{\sqrt{-bx-1}}{\sqrt{3}}\right)}{b}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/(\operatorname{Sqrt}[-1 - b*x]*\operatorname{Sqrt}[2 - b*x]), x]$

[Out] $(-2*\operatorname{ArcSinh}[\operatorname{Sqrt}[-1 - b*x]/\operatorname{Sqrt}[3]])/b$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /; \operatorname{FreeQ}\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 215

$\operatorname{Int}[1/\operatorname{Sqrt}[(a_) + (b_.)*(x_)^2], x_Symbol] \rightarrow \operatorname{Simp}[\operatorname{ArcSinh}[(\operatorname{Rt}[b, 2]*x)/\operatorname{Sqrt}[a]]/\operatorname{Rt}[b, 2], x] /; \operatorname{FreeQ}\{a, b\}, x] \&\& \operatorname{GtQ}[a, 0] \&\& \operatorname{PosQ}[b]$

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-1-bx} \sqrt{2-bx}} dx &= -\frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{3+x^2}} dx, x, \sqrt{-1-bx}\right)}{b} \\ &= -\frac{2 \sinh^{-1}\left(\frac{\sqrt{-1-bx}}{\sqrt{3}}\right)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 1.82

$$\frac{2\sqrt{-bx-1} \sin^{-1}\left(\frac{\sqrt{bx+1}}{\sqrt{3}}\right)}{b\sqrt{bx+1}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-1 - b*x]*Sqrt[2 - b*x]),x]

[Out] (-2*Sqrt[-1 - b*x]*ArcSin[Sqrt[1 + b*x]/Sqrt[3]])/(b*Sqrt[1 + b*x])

fricas [A] time = 0.43, size = 30, normalized size = 1.36

$$\frac{\log\left(-2bx + 2\sqrt{-bx+2}\sqrt{-bx-1} + 1\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-1)^(1/2)/(-b*x+2)^(1/2),x, algorithm="fricas")

[Out] -log(-2*b*x + 2*sqrt(-b*x + 2)*sqrt(-b*x - 1) + 1)/b

giac [A] time = 1.10, size = 25, normalized size = 1.14

$$\frac{2 \log\left(\sqrt{-bx+2} - \sqrt{-bx-1}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-1)^(1/2)/(-b*x+2)^(1/2),x, algorithm="giac")

[Out] 2*log(sqrt(-b*x + 2) - sqrt(-b*x - 1))/b

maple [B] time = 0.01, size = 70, normalized size = 3.18

$$\frac{\sqrt{(-bx-1)(-bx+2)} \ln\left(\frac{b^2x-\frac{1}{2}b}{\sqrt{b^2}} + \sqrt{b^2x^2 - bx - 2}\right)}{\sqrt{-bx-1} \sqrt{-bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x-1)^(1/2)/(-b*x+2)^(1/2),x)

[Out] ((-b*x-1)*(-b*x+2))^(1/2)/(-b*x-1)^(1/2)/(-b*x+2)^(1/2)*ln((b^2*x-1/2*b)/(b^2)^(1/2)+(b^2*x^2-b*x-2)^(1/2))/(b^2)^(1/2)

maxima [A] time = 1.38, size = 33, normalized size = 1.50

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 - bx - 2b - b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-1)^(1/2)/(-b*x+2)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 - b*x - 2)*b - b)/b

mupad [B] time = 0.28, size = 46, normalized size = 2.09

$$-\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{-bx-1}-i)}{(\sqrt{2}-\sqrt{2-bx})\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((-b*x-1)^(1/2)*(2-b*x)^(1/2)),x)

[Out] -(4*atan((b*((-b*x-1)^(1/2)-1i))/((2^(1/2)-(2-b*x)^(1/2))*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{-bx-1}\sqrt{-bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-1)**(1/2)/(-b*x+2)**(1/2),x)

[Out] Integral(1/(sqrt(-b*x-1)*sqrt(-b*x+2)), x)

$$3.1548 \quad \int \frac{1}{\sqrt{-2-bx} \sqrt{2-bx}} dx$$

Optimal. Leaf size=12

$$-\frac{\cosh^{-1}\left(-\frac{bx}{2}\right)}{b}$$

[Out] -arccosh(-1/2*b*x)/b

Rubi [A] time = 0.00, antiderivative size = 12, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.048$, Rules used = {52}

$$-\frac{\cosh^{-1}\left(-\frac{bx}{2}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-2 - b*x]*Sqrt[2 - b*x]),x]

[Out] -(ArcCosh[-(b*x)/2])/b

Rule 52

Int[1/(Sqrt[(a_) + (b_.)*(x_)]*Sqrt[(c_) + (d_.)*(x_)]), x_Symbol] :> Simp[ArcCosh[(b*x)/a]/b, x] /; FreeQ[{a, b, c, d}, x] && EqQ[a + c, 0] && EqQ[b - d, 0] && GtQ[a, 0]

Rubi steps

$$\int \frac{1}{\sqrt{-2-bx} \sqrt{2-bx}} dx = -\frac{\cosh^{-1}\left(-\frac{bx}{2}\right)}{b}$$

Mathematica [B] time = 0.00, size = 27, normalized size = 2.25

$$-\frac{2 \tanh^{-1}\left(\frac{\sqrt{-bx-2}}{\sqrt{2-bx}}\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-2 - b*x]*Sqrt[2 - b*x]),x]

[Out] $(-2*\text{ArcTanh}[\text{Sqrt}[-2 - b*x]/\text{Sqrt}[2 - b*x]])/b$

fricas [B] time = 0.43, size = 28, normalized size = 2.33

$$-\frac{\log(-bx + \sqrt{-bx + 2}\sqrt{-bx - 2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x-2)^(1/2)/(-b*x+2)^(1/2),x, algorithm="fricas")`

[Out] $-\log(-b*x + \text{sqrt}(-b*x + 2)*\text{sqrt}(-b*x - 2))/b$

giac [B] time = 1.10, size = 25, normalized size = 2.08

$$\frac{2 \log(\sqrt{-bx + 2} - \sqrt{-bx - 2})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x-2)^(1/2)/(-b*x+2)^(1/2),x, algorithm="giac")`

[Out] $2*\log(\text{sqrt}(-b*x + 2) - \text{sqrt}(-b*x - 2))/b$

maple [B] time = 0.01, size = 61, normalized size = 5.08

$$\frac{\sqrt{(-bx - 2)(-bx + 2)} \ln\left(\frac{b^2x}{\sqrt{b^2}} + \sqrt{b^2x^2 - 4}\right)}{\sqrt{-bx - 2} \sqrt{-bx + 2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(-b*x-2)^(1/2)/(-b*x+2)^(1/2),x)`

[Out] $((-b*x-2)*(-b*x+2))^{(1/2)}/(-b*x-2)^{(1/2)}/(-b*x+2)^{(1/2)}*\ln(1/(b^2)^{(1/2)}*b^2*x+(b^2*x^2-4)^{(1/2)})/(b^2)^{(1/2)}$

maxima [B] time = 1.27, size = 26, normalized size = 2.17

$$\frac{\log(2b^2x + 2\sqrt{b^2x^2 - 4}b)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x-2)^(1/2)/(-b*x+2)^(1/2),x, algorithm="maxima")`

[Out] $\log(2*b^2*x + 2*\text{sqrt}(b^2*x^2 - 4)*b)/b$

mupad [B] time = 0.29, size = 52, normalized size = 4.33

$$\frac{4 \operatorname{atan}\left(\frac{b(-\sqrt{-bx-2} + \sqrt{2} i)}{(\sqrt{2} - \sqrt{2-bx}) \sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((2 - b*x)^(1/2)*(- b*x - 2)^(1/2)),x)`

[Out] `(4*atan((b*(2^(1/2)*1i - (- b*x - 2)^(1/2)))/((2^(1/2) - (2 - b*x)^(1/2))*(-b^2)^(1/2))))/(-b^2)^(1/2)`

sympy [C] time = 4.63, size = 78, normalized size = 6.50

$$\frac{G_{6,6}^{6,2} \left(\begin{matrix} \frac{1}{4}, \frac{3}{4} & \frac{1}{2}, \frac{1}{2}, 1, 1 \\ 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1, 0 \end{matrix} \middle| \frac{4}{b^2 x^2} \right)}{4\pi^{\frac{3}{2}} b} - \frac{i G_{6,6}^{2,6} \left(\begin{matrix} -\frac{1}{2}, -\frac{1}{4}, 0, \frac{1}{4}, \frac{1}{2}, 1 \\ -\frac{1}{4}, \frac{1}{4} & -\frac{1}{2}, 0, 0, 0 \end{matrix} \middle| \frac{4e^{-2i\pi}}{b^2 x^2} \right)}{4\pi^{\frac{3}{2}} b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x-2)**(1/2)/(-b*x+2)**(1/2),x)`

[Out] `-meijerg(((1/4, 3/4), (1/2, 1/2, 1, 1)), ((0, 1/4, 1/2, 3/4, 1, 0), ()), 4/(b**2*x**2))/(4*pi**(3/2)*b) - I*meijerg((-1/2, -1/4, 0, 1/4, 1/2, 1), ((-1/4, 1/4), (-1/2, 0, 0, 0)), 4*exp_polar(-2*I*pi)/(b**2*x**2))/(4*pi**(3/2)*b)`

$$3.1549 \quad \int \frac{1}{\sqrt{-3-bx} \sqrt{2-bx}} dx$$

Optimal. Leaf size=22

$$-\frac{2 \sinh^{-1}\left(\frac{\sqrt{-bx-3}}{\sqrt{5}}\right)}{b}$$

[Out] $-2*\operatorname{arcsinh}(1/5*(-b*x-3)^{(1/2)}*5^{(1/2)})/b$

Rubi [A] time = 0.01, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.095$, Rules used = {63, 215}

$$-\frac{2 \sinh^{-1}\left(\frac{\sqrt{-bx-3}}{\sqrt{5}}\right)}{b}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/(\operatorname{Sqrt}[-3 - b*x]*\operatorname{Sqrt}[2 - b*x]), x]$

[Out] $(-2*\operatorname{ArcSinh}[\operatorname{Sqrt}[-3 - b*x]/\operatorname{Sqrt}[5]])/b$

Rule 63

$\operatorname{Int}[(a_.) + (b_.)*(x_)^m]*((c_.) + (d_.)*(x_)^n), x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /; \operatorname{FreeQ}\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 215

$\operatorname{Int}[1/\operatorname{Sqrt}[(a_) + (b_.)*(x_)^2], x_Symbol] \rightarrow \operatorname{Simp}[\operatorname{ArcSinh}[(\operatorname{Rt}[b, 2]*x)/\operatorname{Sqrt}[a]]/\operatorname{Rt}[b, 2], x] /; \operatorname{FreeQ}\{a, b\}, x] \&\& \operatorname{GtQ}[a, 0] \&\& \operatorname{PosQ}[b]$

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-3-bx} \sqrt{2-bx}} dx &= -\frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{5+x^2}} dx, x, \sqrt{-3-bx}\right)}{b} \\ &= -\frac{2 \sinh^{-1}\left(\frac{\sqrt{-3-bx}}{\sqrt{5}}\right)}{b} \end{aligned}$$

Mathematica [A] time = 0.01, size = 40, normalized size = 1.82

$$\frac{2\sqrt{-bx-3} \sin^{-1}\left(\frac{\sqrt{bx+3}}{\sqrt{5}}\right)}{b\sqrt{bx+3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-3 - b*x]*Sqrt[2 - b*x]),x]

[Out] (-2*Sqrt[-3 - b*x]*ArcSin[Sqrt[3 + b*x]/Sqrt[5]])/(b*Sqrt[3 + b*x])

fricas [A] time = 0.43, size = 30, normalized size = 1.36

$$\frac{\log\left(-2bx + 2\sqrt{-bx+2}\sqrt{-bx-3} - 1\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-3)^(1/2)/(-b*x+2)^(1/2),x, algorithm="fricas")

[Out] -log(-2*b*x + 2*sqrt(-b*x + 2)*sqrt(-b*x - 3) - 1)/b

giac [A] time = 1.28, size = 25, normalized size = 1.14

$$\frac{2 \log\left(\sqrt{-bx+2} - \sqrt{-bx-3}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-3)^(1/2)/(-b*x+2)^(1/2),x, algorithm="giac")

[Out] 2*log(sqrt(-b*x + 2) - sqrt(-b*x - 3))/b

maple [B] time = 0.01, size = 69, normalized size = 3.14

$$\frac{\sqrt{(-bx-3)(-bx+2)} \ln\left(\frac{b^2x+\frac{1}{2}b}{\sqrt{b^2}} + \sqrt{b^2x^2+bx-6}\right)}{\sqrt{-bx-3} \sqrt{-bx+2} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x-3)^(1/2)/(-b*x+2)^(1/2),x)

[Out] ((-b*x-3)*(-b*x+2))^(1/2)/(-b*x-3)^(1/2)/(-b*x+2)^(1/2)*ln((b^2*x+1/2*b)/(b^2)^(1/2)+(b^2*x^2+b*x-6)^(1/2))/(b^2)^(1/2)

maxima [A] time = 1.37, size = 30, normalized size = 1.36

$$\frac{\log\left(2b^2x + 2\sqrt{b^2x^2 + bx - 6b + b}\right)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-3)^(1/2)/(-b*x+2)^(1/2),x, algorithm="maxima")

[Out] log(2*b^2*x + 2*sqrt(b^2*x^2 + b*x - 6)*b + b)/b

mupad [B] time = 0.29, size = 52, normalized size = 2.36

$$\frac{4 \operatorname{atan}\left(\frac{b(-\sqrt{-bx-3} + \sqrt{3}i)}{(\sqrt{2} - \sqrt{2-bx})\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((2 - b*x)^(1/2)*(- b*x - 3)^(1/2)),x)

[Out] (4*atan((b*(3^(1/2)*1i - (- b*x - 3)^(1/2)))/((2^(1/2) - (2 - b*x)^(1/2))*(-b^2)^(1/2))))/(-b^2)^(1/2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{-bx-3}\sqrt{-bx+2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x-3)**(1/2)/(-b*x+2)**(1/2),x)

[Out] Integral(1/(sqrt(-b*x - 3)*sqrt(-b*x + 2)), x)

$$3.1550 \quad \int \frac{1}{\sqrt{-4+bx} \sqrt{4+bx}} dx$$

Optimal. Leaf size=11

$$\frac{\cosh^{-1}\left(\frac{bx}{4}\right)}{b}$$

[Out] arccosh(1/4*b*x)/b

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {52}

$$\frac{\cosh^{-1}\left(\frac{bx}{4}\right)}{b}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-4 + b*x]*Sqrt[4 + b*x]),x]

[Out] ArcCosh[(b*x)/4]/b

Rule 52

Int[1/(Sqrt[(a_) + (b_.)*(x_)]*Sqrt[(c_) + (d_.)*(x_)]), x_Symbol] :> Simp[ArcCosh[(b*x)/a]/b, x] /; FreeQ[{a, b, c, d}, x] && EqQ[a + c, 0] && EqQ[b - d, 0] && GtQ[a, 0]

Rubi steps

$$\int \frac{1}{\sqrt{-4+bx} \sqrt{4+bx}} dx = \frac{\cosh^{-1}\left(\frac{bx}{4}\right)}{b}$$

Mathematica [B] time = 0.00, size = 25, normalized size = 2.27

$$\frac{2 \tanh^{-1}\left(\frac{\sqrt{bx-4}}{\sqrt{bx+4}}\right)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-4 + b*x]*Sqrt[4 + b*x]),x]

[Out] $(2*\text{ArcTanh}[\text{Sqrt}[-4 + b*x]/\text{Sqrt}[4 + b*x]])/b$

fricas [B] time = 0.43, size = 26, normalized size = 2.36

$$-\frac{\log(-bx + \sqrt{bx+4}\sqrt{bx-4})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-4)^(1/2)/(b*x+4)^(1/2),x, algorithm="fricas")`

[Out] $-\log(-b*x + \text{sqrt}(b*x + 4)*\text{sqrt}(b*x - 4))/b$

giac [B] time = 1.04, size = 23, normalized size = 2.09

$$-\frac{2 \log(\sqrt{bx+4} - \sqrt{bx-4})}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-4)^(1/2)/(b*x+4)^(1/2),x, algorithm="giac")`

[Out] $-2*\log(\text{sqrt}(b*x + 4) - \text{sqrt}(b*x - 4))/b$

maple [B] time = 0.01, size = 57, normalized size = 5.18

$$\frac{\sqrt{(bx-4)(bx+4)} \ln\left(\frac{b^2x}{\sqrt{b^2}} + \sqrt{b^2x^2-16}\right)}{\sqrt{bx-4} \sqrt{bx+4} \sqrt{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x-4)^(1/2)/(b*x+4)^(1/2),x)`

[Out] $((b*x-4)*(b*x+4))^(1/2)/(b*x-4)^(1/2)/(b*x+4)^(1/2)*\ln(1/(b^2)^(1/2)*b^2*x+(b^2*x^2-16)^(1/2))/(b^2)^(1/2)$

maxima [B] time = 1.38, size = 26, normalized size = 2.36

$$\frac{\log(2b^2x + 2\sqrt{b^2x^2-16}b)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-4)^(1/2)/(b*x+4)^(1/2),x, algorithm="maxima")`

[Out] $\log(2*b^2*x + 2*\text{sqrt}(b^2*x^2 - 16)*b)/b$

mupad [B] time = 0.32, size = 40, normalized size = 3.64

$$\frac{4 \operatorname{atan}\left(\frac{b(\sqrt{bx-4}-2i)}{(\sqrt{bx+4}-2)\sqrt{-b^2}}\right)}{\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((b*x - 4)^(1/2)*(b*x + 4)^(1/2)),x)`

[Out] $-(4*\operatorname{atan}((b*((b*x - 4)^{(1/2)} - 2i))/((b*x + 4)^{(1/2)} - 2)*(-b^2)^{(1/2)}))/(-b^2)^{(1/2)}$

sympy [C] time = 4.21, size = 75, normalized size = 6.82

$$\frac{G_{6,6}^{6,2}\left(0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1, 0 \left| \frac{16e^{2i\pi}}{b^2x^2} \right. \right)}{4\pi^{\frac{3}{2}}b} + \frac{iG_{6,6}^{2,6}\left(-\frac{1}{2}, -\frac{1}{4}, 0, \frac{1}{4}, \frac{1}{2}, 1 \left| \frac{16}{b^2x^2} \right. \right)}{4\pi^{\frac{3}{2}}b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x-4)**(1/2)/(b*x+4)**(1/2),x)`

[Out] `meijerg(((1/4, 3/4), (1/2, 1/2, 1, 1)), ((0, 1/4, 1/2, 3/4, 1, 0), ()), 16*exp_polar(2*I*pi)/(b**2*x**2))/(4*pi**(3/2)*b) + I*meijerg((-1/2, -1/4, 0, 1/4, 1/2, 1), ()), ((-1/4, 1/4), (-1/2, 0, 0, 0)), 16/(b**2*x**2))/(4*pi**(3/2)*b)`

$$3.1551 \quad \int \frac{1}{\sqrt{\frac{-b+bc}{d}+bx} \sqrt{c+dx}} dx$$

Optimal. Leaf size=43

$$\frac{2 \sinh^{-1} \left(\frac{\sqrt{d} \sqrt{bx - \frac{b(1-c)}{d}}}{\sqrt{b}} \right)}{\sqrt{b} \sqrt{d}}$$

[Out] $2*\operatorname{arcsinh}(d^{(1/2)*(-b*(1-c)/d+b*x)^{(1/2)}/b^{(1/2)})/b^{(1/2)}/d^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 29, $\frac{\text{number of rules}}{\text{integrand size}} = 0.069$, Rules used = {63, 215}

$$\frac{2 \sinh^{-1} \left(\frac{\sqrt{d} \sqrt{bx - \frac{b(1-c)}{d}}}{\sqrt{b}} \right)}{\sqrt{b} \sqrt{d}}$$

Antiderivative was successfully verified.

[In] `Int[1/(Sqrt[(-b + b*c)/d + b*x]*Sqrt[c + d*x]),x]`

[Out] `(2*ArcSinh[(Sqrt[d]*Sqrt[-((b*(1 - c))/d) + b*x])/Sqrt[b]])/(Sqrt[b]*Sqrt[d])`

Rule 63

`Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 215

`Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]`

Rubi steps

$$\int \frac{1}{\sqrt{\frac{-b+bc}{d} + bx} \sqrt{c+dx}} dx = \frac{2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{c - \frac{-b+bc}{b} + \frac{dx^2}{b}}} dx, x, \sqrt{\frac{-b+bc}{d} + bx} \right)}{b}$$

$$= \frac{2 \sinh^{-1} \left(\frac{\sqrt{d} \sqrt{\frac{-b(1-c)}{d} + bx}}{\sqrt{b}} \right)}{\sqrt{b} \sqrt{d}}$$

Mathematica [A] time = 0.03, size = 41, normalized size = 0.95

$$\frac{2\sqrt{c+dx-1} \sinh^{-1}(\sqrt{c+dx-1})}{d\sqrt{\frac{b(c+dx-1)}{d}}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[(-b + b*c)/d + b*x]*Sqrt[c + d*x]), x]

[Out] (2*Sqrt[-1 + c + d*x]*ArcSinh[Sqrt[-1 + c + d*x]])/(d*Sqrt[(b*(-1 + c + d*x))/d])

fricas [B] time = 0.46, size = 175, normalized size = 4.07

$$\left[\frac{\sqrt{bd} \log \left(8bd^2x^2 + 8bc^2 + 8(2bc - b)dx + 4\sqrt{bd}(2dx + 2c - 1)\sqrt{dx + c} \sqrt{\frac{bdx+bc-b}{d}} - 8bc + b \right)}{2bd}, -\frac{\sqrt{-bd} \arctan \left(\frac{\sqrt{bd} \sqrt{\frac{bdx+bc-b}{d}}}{\sqrt{bd}} \right)}{\sqrt{bd}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/((b*c-b)/d+b*x)^(1/2)/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] [1/2*sqrt(b*d)*log(8*b*d^2*x^2 + 8*b*c^2 + 8*(2*b*c - b)*d*x + 4*sqrt(b*d)*(2*d*x + 2*c - 1)*sqrt(d*x + c)*sqrt((b*d*x + b*c - b)/d) - 8*b*c + b)/(b*d), -sqrt(-b*d)*arctan(1/2*sqrt(-b*d)*(2*d*x + 2*c - 1)*sqrt(d*x + c)*sqrt((b*d*x + b*c - b)/d)/(b*d^2*x^2 + b*c^2 + (2*b*c - b)*d*x - b*c))/(b*d)]

giac [A] time = 0.97, size = 57, normalized size = 1.33

$$\frac{2b \log \left(-\sqrt{bd} \sqrt{\frac{bdx+bc-b}{d}} + \sqrt{(bdx+bc-b)b+b^2} \right)}{\sqrt{bd}|b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/((b*c-b)/d+b*x)^(1/2)/(d*x+c)^(1/2),x, algorithm="giac")

[Out] $-2*b*\log(-\sqrt{b*d}*\sqrt{(b*d*x + b*c - b)/d} + \sqrt{(b*d*x + b*c - b)*b + b^2})/(\sqrt{b*d}*abs(b))$

maple [B] time = 0.02, size = 100, normalized size = 2.33

$$\frac{\sqrt{\left(bx + \frac{(c-1)b}{d}\right)}(dx + c) \ln\left(\frac{bdx + \frac{bc}{2} + \frac{(c-1)b}{2}}{\sqrt{bd}} + \sqrt{bdx^2 + \frac{(c-1)bc}{d} + (bc + (c-1)b)x}\right)}{\sqrt{bx + \frac{(c-1)b}{d}} \sqrt{dx + c} \sqrt{bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*c-b)/d+b*x)^(1/2)/(d*x+c)^(1/2),x)

[Out] $((b*x+b*(c-1)/d)*(d*x+c))^(1/2)/(b*x+b*(c-1)/d)^(1/2)/(d*x+c)^(1/2)*\ln((1/2*b*(c-1)+1/2*b*c+b*d*x)/(b*d)^(1/2)+(b*d*x^2+(b*(c-1)+b*c)*x+b*(c-1)/d*c)^(1/2))/(b*d)^(1/2)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/((b*c-b)/d+b*x)^(1/2)/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested additional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(2*c-1>0)', see `assume?` for more details)Is 2*c-1 zero or nonzero?

mupad [B] time = 0.50, size = 66, normalized size = 1.53

$$\frac{4 \operatorname{atan}\left(\frac{d\left(\sqrt{bx - \frac{b-bc}{d}} - \sqrt{-\frac{b-bc}{d}}\right)}{\sqrt{-bd}\left(\sqrt{c+dx} - \sqrt{c}\right)}\right)}{\sqrt{-bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((b*x - (b - b*c)/d)^(1/2)*(c + d*x)^(1/2)),x)

[Out] $(4*\operatorname{atan}(-d*((b*x - (b - b*c)/d)^(1/2) - (-b - b*c)/d)^(1/2)))/((-b*d)^(1/2)*((c + d*x)^(1/2) - c^(1/2)))/(-b*d)^(1/2)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{b\left(\frac{c}{d} + x - \frac{1}{d}\right)} \sqrt{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/((b*c-b)/d+b*x)**(1/2)/(d*x+c)**(1/2), x)

[Out] Integral(1/(sqrt(b*(c/d + x - 1/d))*sqrt(c + d*x)), x)

$$3.1552 \quad \int \frac{1}{\sqrt{x} \sqrt{-3+2x}} dx$$

Optimal. Leaf size=22

$$\sqrt{2} \sinh^{-1} \left(\frac{\sqrt{2x-3}}{\sqrt{3}} \right)$$

[Out] arcsinh(1/3*(-3+2*x)^(1/2)*3^(1/2))*2^(1/2)

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {54, 215}

$$\sqrt{2} \sinh^{-1} \left(\frac{\sqrt{2x-3}}{\sqrt{3}} \right)$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[x]*Sqrt[-3 + 2*x]),x]

[Out] Sqrt[2]*ArcSinh[Sqrt[-3 + 2*x]/Sqrt[3]]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 215

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{x} \sqrt{-3+2x}} dx &= \sqrt{2} \operatorname{Subst} \left(\int \frac{1}{\sqrt{3+x^2}} dx, x, \sqrt{-3+2x} \right) \\ &= \sqrt{2} \sinh^{-1} \left(\frac{\sqrt{-3+2x}}{\sqrt{3}} \right) \end{aligned}$$

Mathematica [A] time = 0.01, size = 31, normalized size = 1.41

$$\frac{\sqrt{4x-6} \sin^{-1}\left(\sqrt{1-\frac{2x}{3}}\right)}{\sqrt{3-2x}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[x]*Sqrt[-3 + 2*x]),x]

[Out] (Sqrt[-6 + 4*x]*ArcSin[Sqrt[1 - (2*x)/3]])/Sqrt[3 - 2*x]

fricas [A] time = 0.44, size = 26, normalized size = 1.18

$$\frac{1}{2} \sqrt{2} \log\left(-2 \sqrt{2} \sqrt{2x-3} \sqrt{x} - 4x + 3\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-3+2*x)^(1/2),x, algorithm="fricas")

[Out] 1/2*sqrt(2)*log(-2*sqrt(2)*sqrt(2*x - 3)*sqrt(x) - 4*x + 3)

giac [A] time = 0.92, size = 23, normalized size = 1.05

$$-\sqrt{2} \log\left(\sqrt{2} \sqrt{x} - \sqrt{2x-3}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-3+2*x)^(1/2),x, algorithm="giac")

[Out] -sqrt(2)*log(sqrt(2)*sqrt(x) - sqrt(2*x - 3))

maple [B] time = 0.01, size = 48, normalized size = 2.18

$$\frac{\sqrt{(2x-3)x} \sqrt{2} \ln\left(\frac{\left(2x-\frac{3}{2}\right)\sqrt{2}}{2} + \sqrt{2x^2-3x}\right)}{2\sqrt{2x-3} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(1/2)/(-3+2*x)^(1/2),x)

[Out] 1/2*(x*(-3+2*x))^(1/2)/x^(1/2)/(-3+2*x)^(1/2)*ln(1/2*(-3/2+2*x)*2^(1/2)+(2*x^2-3*x)^(1/2))*2^(1/2)

maxima [B] time = 2.87, size = 41, normalized size = 1.86

$$-\frac{1}{2}\sqrt{2}\log\left(\frac{\sqrt{2}-\frac{\sqrt{2x-3}}{\sqrt{x}}}{\sqrt{2}+\frac{\sqrt{2x-3}}{\sqrt{x}}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(1/2)/(-3+2*x)^(1/2),x, algorithm="maxima")

[Out] -1/2*sqrt(2)*log(-(sqrt(2) - sqrt(2*x - 3)/sqrt(x))/(sqrt(2) + sqrt(2*x - 3)/sqrt(x)))

mupad [B] time = 0.44, size = 30, normalized size = 1.36

$$-2\sqrt{2}\operatorname{atanh}\left(\frac{\sqrt{2}(-\sqrt{2x-3}+\sqrt{3}i)}{2\sqrt{x}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/2)*(2*x - 3)^(1/2)),x)

[Out] -2*2^(1/2)*atanh((2^(1/2)*(3^(1/2)*1i - (2*x - 3)^(1/2)))/(2*x^(1/2)))

sympy [A] time = 1.03, size = 44, normalized size = 2.00

$$\begin{cases} \sqrt{2}\operatorname{acosh}\left(\frac{\sqrt{6}\sqrt{x}}{3}\right) & \text{for } \frac{2|x|}{3} > 1 \\ -\sqrt{2}i\operatorname{asin}\left(\frac{\sqrt{6}\sqrt{x}}{3}\right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(1/2)/(-3+2*x)**(1/2),x)

[Out] Piecewise((sqrt(2)*acosh(sqrt(6)*sqrt(x)/3), 2*Abs(x)/3 > 1), (-sqrt(2)*I*asin(sqrt(6)*sqrt(x)/3), True))

$$3.1553 \quad \int \frac{1}{\sqrt{-3+2x} \sqrt{2+3x}} dx$$

Optimal. Leaf size=26

$$\sqrt{\frac{2}{3}} \sinh^{-1} \left(\sqrt{\frac{3}{13}} \sqrt{2x-3} \right)$$

[Out] 1/3*arcsinh(1/13*39^(1/2)*(-3+2*x)^(1/2))*6^(1/2)

Rubi [A] time = 0.01, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {54, 215}

$$\sqrt{\frac{2}{3}} \sinh^{-1} \left(\sqrt{\frac{3}{13}} \sqrt{2x-3} \right)$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[-3 + 2*x]*Sqrt[2 + 3*x]),x]

[Out] Sqrt[2/3]*ArcSinh[Sqrt[3/13]*Sqrt[-3 + 2*x]]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 215

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSinh[(Rt[b, 2]*x)/Sqrt[a]]/Rt[b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && PosQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{-3+2x} \sqrt{2+3x}} dx &= \sqrt{2} \text{Subst} \left(\int \frac{1}{\sqrt{13+3x^2}} dx, x, \sqrt{-3+2x} \right) \\ &= \sqrt{\frac{2}{3}} \sinh^{-1} \left(\sqrt{\frac{3}{13}} \sqrt{-3+2x} \right) \end{aligned}$$

Mathematica [A] time = 0.01, size = 26, normalized size = 1.00

$$\sqrt{\frac{2}{3}} \sinh^{-1} \left(\sqrt{\frac{3}{13}} \sqrt{2x-3} \right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[-3 + 2*x]*Sqrt[2 + 3*x]),x]

[Out] Sqrt[2/3]*ArcSinh[Sqrt[3/13]*Sqrt[-3 + 2*x]]

fricas [B] time = 0.45, size = 46, normalized size = 1.77

$$\frac{1}{12} \sqrt{3} \sqrt{2} \log \left(4 \sqrt{3} \sqrt{2} (12x - 5) \sqrt{3x + 2} \sqrt{2x - 3} + 288x^2 - 240x - 119 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-3+2*x)^(1/2)/(2+3*x)^(1/2),x, algorithm="fricas")

[Out] 1/12*sqrt(3)*sqrt(2)*log(4*sqrt(3)*sqrt(2)*(12*x - 5)*sqrt(3*x + 2)*sqrt(2*x - 3) + 288*x^2 - 240*x - 119)

giac [A] time = 1.26, size = 30, normalized size = 1.15

$$-\frac{1}{3} \sqrt{3} \sqrt{2} \log \left(\left| -\sqrt{2} \sqrt{3x+2} + \sqrt{6x-9} \right| \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-3+2*x)^(1/2)/(2+3*x)^(1/2),x, algorithm="giac")

[Out] -1/3*sqrt(3)*sqrt(2)*log(abs(-sqrt(2)*sqrt(3*x + 2) + sqrt(6*x - 9)))

maple [B] time = 0.01, size = 57, normalized size = 2.19

$$\frac{\sqrt{(2x-3)(3x+2)} \sqrt{6} \ln \left(\frac{\left(\frac{6x-5}{2} \right) \sqrt{6}}{6} + \sqrt{6x^2 - 5x - 6} \right)}{6\sqrt{2x-3} \sqrt{3x+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(2*x-3)^(1/2)/(3*x+2)^(1/2),x)

[Out] 1/6*((2*x-3)*(3*x+2))^(1/2)/(2*x-3)^(1/2)/(3*x+2)^(1/2)*ln(1/6*(-5/2+6*x)*6^(1/2)+(6*x^2-5*x-6)^(1/2))*6^(1/2)

maxima [A] time = 3.04, size = 28, normalized size = 1.08

$$\frac{1}{6} \sqrt{6} \log \left(2 \sqrt{6} \sqrt{6x^2 - 5x - 6} + 12x - 5 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-3+2*x)^(1/2)/(2+3*x)^(1/2),x, algorithm="maxima")

[Out] 1/6*sqrt(6)*log(2*sqrt(6)*sqrt(6*x^2 - 5*x - 6) + 12*x - 5)

mupad [B] time = 0.12, size = 43, normalized size = 1.65

$$\frac{2 \sqrt{6} \operatorname{atanh} \left(\frac{\sqrt{6} (-\sqrt{2x-3} + \sqrt{3} i)}{2(\sqrt{2} - \sqrt{3x+2})} \right)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((2*x - 3)^(1/2)*(3*x + 2)^(1/2)),x)

[Out] (2*6^(1/2)*atanh((6^(1/2)*(3^(1/2)*1i - (2*x - 3)^(1/2)))/(2*(2^(1/2) - (3*x + 2)^(1/2)))))/3

sympy [A] time = 1.09, size = 58, normalized size = 2.23

$$\left\{ \begin{array}{l} \frac{\sqrt{6} \operatorname{acosh} \left(\frac{\sqrt{78} \sqrt{x + \frac{2}{3}}}{13} \right)}{3} \quad \text{for } \frac{6|x + \frac{2}{3}|}{13} > 1 \\ -\frac{\sqrt{6} i \operatorname{asin} \left(\frac{\sqrt{78} \sqrt{x + \frac{2}{3}}}{13} \right)}{3} \quad \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-3+2*x)**(1/2)/(2+3*x)**(1/2),x)

[Out] Piecewise((sqrt(6)*acosh(sqrt(78)*sqrt(x + 2/3)/13)/3, 6*Abs(x + 2/3)/13 > 1), (-sqrt(6)*I*asin(sqrt(78)*sqrt(x + 2/3)/13)/3, True))

$$3.1554 \quad \int \frac{1}{\sqrt{\frac{b-bc}{d}+bx} \sqrt{c-dx}} dx$$

Optimal. Leaf size=42

$$\frac{2 \sin^{-1} \left(\frac{\sqrt{d} \sqrt{\frac{b(1-c)}{d}+bx}}{\sqrt{b}} \right)}{\sqrt{b} \sqrt{d}}$$

[Out] $2*\arcsin(d^{(1/2)}*(b*(1-c)/d+b*x)^{(1/2)}/b^{(1/2)})/b^{(1/2)}/d^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 29, $\frac{\text{number of rules}}{\text{integrand size}} = 0.069$, Rules used = {63, 216}

$$\frac{2 \sin^{-1} \left(\frac{\sqrt{d} \sqrt{\frac{b(1-c)}{d}+bx}}{\sqrt{b}} \right)}{\sqrt{b} \sqrt{d}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[(b - b*c)/d + b*x]*Sqrt[c - d*x]),x]

[Out] (2*ArcSin[(Sqrt[d]*Sqrt[(b*(1 - c))/d + b*x])/Sqrt[b]])/(Sqrt[b]*Sqrt[d])

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\int \frac{1}{\sqrt{\frac{b-bc}{d} + bx} \sqrt{c-dx}} dx = \frac{2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{c + \frac{b-bc}{b} - \frac{dx^2}{b}}} dx, x, \sqrt{\frac{b-bc}{d} + bx} \right)}{b}$$

$$= \frac{2 \sin^{-1} \left(\frac{\sqrt{d} \sqrt{\frac{b(1-c)}{d} + bx}}{\sqrt{b}} \right)}{\sqrt{b} \sqrt{d}}$$

Mathematica [A] time = 0.05, size = 67, normalized size = 1.60

$$\frac{2\sqrt{-d} \sqrt{-c+dx+1} \sinh^{-1} \left(\frac{\sqrt{-d} \sqrt{-c-dx}}{\sqrt{d}} \right)}{d^{3/2} \sqrt{\frac{b(-c+dx+1)}{d}}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[(b - b*c)/d + b*x]*Sqrt[c - d*x]),x]

[Out] (2*Sqrt[-d]*Sqrt[1 - c + d*x]*ArcSinh[(Sqrt[-d]*Sqrt[c - d*x])/Sqrt[d]])/(d^(3/2)*Sqrt[(b*(1 - c + d*x))/d])

fricas [B] time = 0.46, size = 176, normalized size = 4.19

$$\left[\frac{\sqrt{-bd} \log \left(8bd^2x^2 + 8bc^2 - 8(2bc - b)dx - 4\sqrt{-bd}(2dx - 2c + 1)\sqrt{-dx + c} \sqrt{\frac{bdx - bc + b}{d}} - 8bc + b \right)}{2bd}, -\frac{\sqrt{bd} \arctan \left(\frac{\sqrt{-bd} \sqrt{\frac{bdx - bc + b}{d}}}{\sqrt{-dx + c}} \right)}{\sqrt{-bd} |b|} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/((-b*c+b)/d+b*x)^(1/2)/(-d*x+c)^(1/2),x, algorithm="fricas")

[Out] [-1/2*sqrt(-b*d)*log(8*b*d^2*x^2 + 8*b*c^2 - 8*(2*b*c - b)*d*x - 4*sqrt(-b*d)*(2*d*x - 2*c + 1)*sqrt(-d*x + c)*sqrt((b*d*x - b*c + b)/d) - 8*b*c + b)/(b*d), -sqrt(b*d)*arctan(1/2*sqrt(b*d)*(2*d*x - 2*c + 1)*sqrt(-d*x + c)*sqrt((b*d*x - b*c + b)/d)/(b*d^2*x^2 + b*c^2 - (2*b*c - b)*d*x - b*c))/(b*d)]

giac [A] time = 1.08, size = 58, normalized size = 1.38

$$\frac{2b \log \left(-\sqrt{-bd} \sqrt{\frac{bdx - bc + b}{d}} + \sqrt{-(bdx - bc + b)b + b^2} \right)}{\sqrt{-bd} |b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/((-b*c+b)/d+b*x)^(1/2)/(-d*x+c)^(1/2),x, algorithm="giac")

[Out] $-2*b*\log(-\sqrt{-b*d}*\sqrt{(b*d*x - b*c + b)/d} + \sqrt{-(b*d*x - b*c + b)*b + b^2})/(\sqrt{-b*d}*abs(b))$

maple [B] time = 0.04, size = 118, normalized size = 2.81

$$\frac{\sqrt{\left(bx + \frac{(-c+1)b}{d}\right)}(-dx + c) \arctan\left(\frac{\sqrt{bd}\left(x - \frac{bc - (-c+1)b}{2bd}\right)}{\sqrt{-bdx^2 + \frac{(-c+1)bc}{d} + (bc - (-c+1)b)x}}\right)}{\sqrt{bx + \frac{(-c+1)b}{d}} \sqrt{-dx + c} \sqrt{bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((-b*c+b)/d+b*x)^(1/2)/(-d*x+c)^(1/2),x)

[Out] $((b*(1-c)/d+b*x)*(-d*x+c))^(1/2)/(b*(1-c)/d+b*x)^(1/2)/(-d*x+c)^(1/2)/(b*d)^(1/2)*\arctan((b*d)^(1/2)*(x-1/2*(-b*(1-c)+b*c)/b/d)/(-b*d*x^2+(-b*(1-c)+b*c)*x+b*(1-c)/d*c)^(1/2))$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/((-b*c+b)/d+b*x)^(1/2)/(-d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(2*c-1>0)', see `assume?` for more details)Is 2*c-1 zero or nonzero?

mupad [B] time = 0.51, size = 63, normalized size = 1.50

$$\frac{4 \operatorname{atan}\left(\frac{d\left(\sqrt{\frac{b-bc}{d}}+bx-\sqrt{\frac{b-bc}{d}}\right)}{\sqrt{bd}\left(\sqrt{c-dx}-\sqrt{c}\right)}\right)}{\sqrt{bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(((b - b*c)/d + b*x)^(1/2)*(c - d*x)^(1/2)),x)

[Out] $-(4*\operatorname{atan}(-d*((b-b*c)/d+b*x)^{(1/2)} - ((b-b*c)/d)^{(1/2)}))/((b*d)^{(1/2)})*((c-d*x)^{(1/2)} - c^{(1/2)}))/((b*d)^{(1/2)})$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{b\left(-\frac{c}{d} + x + \frac{1}{d}\right)}\sqrt{c-dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/((-b*c+b)/d+b*x)**(1/2)/(-d*x+c)**(1/2),x)`

[Out] `Integral(1/(sqrt(b*(-c/d + x + 1/d))*sqrt(c - d*x)), x)`

$$3.1555 \quad \int \frac{1}{\sqrt{4-x} \sqrt{x}} dx$$

Optimal. Leaf size=10

$$-\sin^{-1}\left(1 - \frac{x}{2}\right)$$

[Out] arcsin(-1+1/2*x)

Rubi [A] time = 0.01, antiderivative size = 10, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {53, 619, 216}

$$-\sin^{-1}\left(1 - \frac{x}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[4 - x]*Sqrt[x]),x]

[Out] -ArcSin[1 - x/2]

Rule 53

Int[1/(Sqrt[(a_) + (b_.)*(x_)]*Sqrt[(c_) + (d_.)*(x_)]), x_Symbol] :> Int[1/Sqrt[a*c - b*(a - c)*x - b^2*x^2], x] /; FreeQ[{a, b, c, d}, x] && EqQ[b + d, 0] && GtQ[a + c, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rule 619

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] :> Dist[1/(2*c*((-4*c)/(b^2 - 4*a*c))^(p)), Subst[Int[Simp[1 - x^2/(b^2 - 4*a*c), x]^p, x], x, b + 2*c*x], x] /; FreeQ[{a, b, c, p}, x] && GtQ[4*a - b^2/c, 0]

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt{4-x}\sqrt{x}} dx &= \int \frac{1}{\sqrt{4x-x^2}} dx \\
&= -\left(\frac{1}{4} \text{Subst}\left(\int \frac{1}{\sqrt{1-\frac{x^2}{16}}} dx, x, 4-2x\right)\right) \\
&= -\sin^{-1}\left(1-\frac{x}{2}\right)
\end{aligned}$$

Mathematica [A] time = 0.01, size = 14, normalized size = 1.40

$$-2 \sin^{-1}\left(\sqrt{1-\frac{x}{4}}\right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[4 - x]*Sqrt[x]),x]

[Out] -2*ArcSin[Sqrt[1 - x/4]]

fricas [B] time = 0.43, size = 14, normalized size = 1.40

$$-2 \arctan\left(\frac{\sqrt{-x+4}}{\sqrt{x}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(4-x)^(1/2)/x^(1/2),x, algorithm="fricas")

[Out] -2*arctan(sqrt(-x + 4)/sqrt(x))

giac [A] time = 1.10, size = 8, normalized size = 0.80

$$2 \arcsin\left(\frac{1}{2}\sqrt{x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(4-x)^(1/2)/x^(1/2),x, algorithm="giac")

[Out] 2*arcsin(1/2*sqrt(x))

maple [B] time = 0.00, size = 27, normalized size = 2.70

$$\frac{\sqrt{(-x+4)x} \arcsin\left(\frac{x}{2}-1\right)}{\sqrt{-x+4} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(4-x)^(1/2)/x^(1/2),x)

[Out] ((4-x)*x)^(1/2)/(4-x)^(1/2)/x^(1/2)*arcsin(-1+1/2*x)

maxima [B] time = 2.99, size = 14, normalized size = 1.40

$$-2 \arctan\left(\frac{\sqrt{-x+4}}{\sqrt{x}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(4-x)^(1/2)/x^(1/2),x, algorithm="maxima")

[Out] -2*arctan(sqrt(-x + 4)/sqrt(x))

mupad [B] time = 0.29, size = 16, normalized size = 1.60

$$-4 \operatorname{atan}\left(\frac{\sqrt{4-x}-2}{\sqrt{x}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/2)*(4-x)^(1/2)),x)

[Out] -4*atan(((4-x)^(1/2)-2)/x^(1/2))

sympy [A] time = 0.99, size = 26, normalized size = 2.60

$$\begin{cases} -2i \operatorname{acosh}\left(\frac{\sqrt{x}}{2}\right) & \text{for } \frac{|x|}{4} > 1 \\ 2 \operatorname{asin}\left(\frac{\sqrt{x}}{2}\right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(4-x)**(1/2)/x**(1/2),x)

[Out] Piecewise((-2*I*acosh(sqrt(x)/2), Abs(x)/4 > 1), (2*asin(sqrt(x)/2), True))

$$3.1556 \quad \int \frac{1}{\sqrt{3-2x}\sqrt{x}} dx$$

Optimal. Leaf size=20

$$\sqrt{2} \sin^{-1}\left(\sqrt{\frac{2}{3}}\sqrt{x}\right)$$

[Out] arcsin(1/3*6^(1/2)*x^(1/2))*2^(1/2)

Rubi [A] time = 0.01, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {54, 216}

$$\sqrt{2} \sin^{-1}\left(\sqrt{\frac{2}{3}}\sqrt{x}\right)$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[3 - 2*x]*Sqrt[x]),x]

[Out] Sqrt[2]*ArcSin[Sqrt[2/3]*Sqrt[x]]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_)]*Sqrt[(c_.) + (d_.)*(x_)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{3-2x}\sqrt{x}} dx &= 2 \text{Subst}\left(\int \frac{1}{\sqrt{3-2x^2}} dx, x, \sqrt{x}\right) \\ &= \sqrt{2} \sin^{-1}\left(\sqrt{\frac{2}{3}}\sqrt{x}\right) \end{aligned}$$

Mathematica [A] time = 0.00, size = 20, normalized size = 1.00

$$\sqrt{2} \sin^{-1} \left(\sqrt{\frac{2}{3}} \sqrt{x} \right)$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[3 - 2*x]*Sqrt[x]),x]

[Out] Sqrt[2]*ArcSin[Sqrt[2/3]*Sqrt[x]]

fricas [A] time = 0.43, size = 21, normalized size = 1.05

$$-\sqrt{2} \arctan \left(\frac{\sqrt{2} \sqrt{-2x + 3}}{2 \sqrt{x}} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-2*x)^(1/2)/x^(1/2),x, algorithm="fricas")

[Out] -sqrt(2)*arctan(1/2*sqrt(2)*sqrt(-2*x + 3)/sqrt(x))

giac [A] time = 1.09, size = 13, normalized size = 0.65

$$\sqrt{2} \arcsin \left(\frac{1}{3} \sqrt{6} \sqrt{x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-2*x)^(1/2)/x^(1/2),x, algorithm="giac")

[Out] sqrt(2)*arcsin(1/3*sqrt(6)*sqrt(x))

maple [B] time = 0.01, size = 31, normalized size = 1.55

$$\frac{\sqrt{(-2x + 3)x} \sqrt{2} \arcsin \left(\frac{4x}{3} - 1 \right)}{2\sqrt{-2x + 3} \sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-2*x+3)^(1/2)/x^(1/2),x)

[Out] 1/2*((-2*x+3)*x)^(1/2)/(-2*x+3)^(1/2)/x^(1/2)*2^(1/2)*arcsin(4/3*x-1)

maxima [A] time = 3.12, size = 21, normalized size = 1.05

$$-\sqrt{2} \arctan \left(\frac{\sqrt{2} \sqrt{-2x + 3}}{2 \sqrt{x}} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-2*x)^(1/2)/x^(1/2),x, algorithm="maxima")

[Out] -sqrt(2)*arctan(1/2*sqrt(2)*sqrt(-2*x + 3)/sqrt(x))

mupad [B] time = 0.30, size = 27, normalized size = 1.35

$$2\sqrt{2} \operatorname{atan}\left(\frac{\sqrt{2}(\sqrt{3}-\sqrt{3-2x})}{2\sqrt{x}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(x^(1/2)*(3 - 2*x)^(1/2)),x)

[Out] 2*2^(1/2)*atan((2^(1/2)*(3^(1/2) - (3 - 2*x)^(1/2)))/(2*x^(1/2)))

sympy [A] time = 1.00, size = 44, normalized size = 2.20

$$\begin{cases} -\sqrt{2}i \operatorname{acosh}\left(\frac{\sqrt{6}\sqrt{x}}{3}\right) & \text{for } \frac{2|x|}{3} > 1 \\ \sqrt{2} \operatorname{asin}\left(\frac{\sqrt{6}\sqrt{x}}{3}\right) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-2*x)**(1/2)/x**(1/2),x)

[Out] Piecewise((-sqrt(2)*I*acosh(sqrt(6)*sqrt(x)/3), 2*Abs(x)/3 > 1), (sqrt(2)*asin(sqrt(6)*sqrt(x)/3), True))

$$3.1557 \quad \int \frac{1}{\sqrt{3-2x} \sqrt{3+5x}} dx$$

Optimal. Leaf size=26

$$\sqrt{\frac{2}{5}} \sin^{-1} \left(\sqrt{\frac{2}{21}} \sqrt{5x+3} \right)$$

[Out] 1/5*arcsin(1/21*42^(1/2)*(3+5*x)^(1/2))*10^(1/2)

Rubi [A] time = 0.01, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {54, 216}

$$\sqrt{\frac{2}{5}} \sin^{-1} \left(\sqrt{\frac{2}{21}} \sqrt{5x+3} \right)$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[3 - 2*x]*Sqrt[3 + 5*x]),x]

[Out] Sqrt[2/5]*ArcSin[Sqrt[2/21]*Sqrt[3 + 5*x]]

Rule 54

Int[1/(Sqrt[(a_.) + (b_.)*(x_.)]*Sqrt[(c_.) + (d_.)*(x_.)]), x_Symbol] := Dist[2/Sqrt[b], Subst[Int[1/Sqrt[b*c - a*d + d*x^2], x], x, Sqrt[a + b*x]], x] /; FreeQ[{a, b, c, d}, x] && GtQ[b*c - a*d, 0] && GtQ[b, 0]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{3-2x} \sqrt{3+5x}} dx &= \frac{2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{21-2x^2}} dx, x, \sqrt{3+5x} \right)}{\sqrt{5}} \\ &= \sqrt{\frac{2}{5}} \sin^{-1} \left(\sqrt{\frac{2}{21}} \sqrt{3+5x} \right) \end{aligned}$$

Mathematica [A] time = 0.01, size = 45, normalized size = 1.73

$$\frac{\sqrt{\frac{2}{5}} \sqrt{3-2x} \sinh^{-1}\left(\sqrt{\frac{5}{21}} \sqrt{2x-3}\right)}{\sqrt{2x-3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[3 - 2*x]*Sqrt[3 + 5*x]),x]

[Out] -((Sqrt[2/5]*Sqrt[3 - 2*x]*ArcSinh[Sqrt[5/21]*Sqrt[-3 + 2*x]])/Sqrt[-3 + 2*x])

fricas [B] time = 0.43, size = 44, normalized size = 1.69

$$-\frac{1}{5} \sqrt{5} \sqrt{2} \arctan\left(\frac{\sqrt{5} \sqrt{2} \sqrt{5x+3} \sqrt{-2x+3} - 3 \sqrt{5} \sqrt{2}}{10x}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-2*x)^(1/2)/(3+5*x)^(1/2),x, algorithm="fricas")

[Out] -1/5*sqrt(5)*sqrt(2)*arctan(1/10*(sqrt(5)*sqrt(2)*sqrt(5*x + 3)*sqrt(-2*x + 3) - 3*sqrt(5)*sqrt(2))/x)

giac [A] time = 0.93, size = 21, normalized size = 0.81

$$\frac{1}{5} \sqrt{5} \sqrt{2} \arcsin\left(\frac{1}{21} \sqrt{42} \sqrt{5x+3}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-2*x)^(1/2)/(3+5*x)^(1/2),x, algorithm="giac")

[Out] 1/5*sqrt(5)*sqrt(2)*arcsin(1/21*sqrt(42)*sqrt(5*x + 3))

maple [B] time = 0.01, size = 39, normalized size = 1.50

$$\frac{\sqrt{(-2x+3)(5x+3)} \sqrt{10} \arcsin\left(\frac{20x}{21} - \frac{3}{7}\right)}{10\sqrt{-2x+3} \sqrt{5x+3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((-2*x+3)^(1/2)/(3+5*x)^(1/2)),x)

[Out] 1/10*((-2*x+3)*(3+5*x))^(1/2)/((-2*x+3)^(1/2)/(3+5*x)^(1/2))*10^(1/2)*arcsin(20/21*x-3/7)

maxima [A] time = 3.00, size = 11, normalized size = 0.42

$$-\frac{1}{10} \sqrt{10} \arcsin\left(-\frac{20}{21}x + \frac{3}{7}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-2*x)^(1/2)/(3+5*x)^(1/2),x, algorithm="maxima")

[Out] -1/10*sqrt(10)*arcsin(-20/21*x + 3/7)

mupad [B] time = 0.08, size = 40, normalized size = 1.54

$$-\frac{2\sqrt{10} \operatorname{atan}\left(\frac{\sqrt{10}(\sqrt{3}-\sqrt{3-2x})}{2(\sqrt{3}-\sqrt{5x+3})}\right)}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((3 - 2*x)^(1/2)*(5*x + 3)^(1/2)),x)

[Out] -(2*10^(1/2)*atan((10^(1/2)*(3^(1/2) - (3 - 2*x)^(1/2)))/(2*(3^(1/2) - (5*x + 3)^(1/2)))))/5

sympy [A] time = 1.07, size = 58, normalized size = 2.23

$$\begin{cases} -\frac{\sqrt{10} i \operatorname{acosh}\left(\frac{\sqrt{210} \sqrt{x+\frac{3}{5}}}{21}\right)}{5} & \text{for } \frac{10|x+\frac{3}{5}|}{21} > 1 \\ \frac{\sqrt{10} \operatorname{asin}\left(\frac{\sqrt{210} \sqrt{x+\frac{3}{5}}}{21}\right)}{5} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(3-2*x)**(1/2)/(3+5*x)**(1/2),x)

[Out] Piecewise((-sqrt(10)*I*acosh(sqrt(210)*sqrt(x + 3/5)/21)/5, 10*Abs(x + 3/5)/21 > 1), (sqrt(10)*asin(sqrt(210)*sqrt(x + 3/5)/21)/5, True))

$$3.1558 \quad \int \frac{1}{\sqrt{a-bx} \sqrt{c+dx}} dx$$

Optimal. Leaf size=43

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{d} \sqrt{a-bx}}{\sqrt{b} \sqrt{c+dx}} \right)}{\sqrt{b} \sqrt{d}}$$

[Out] $-2 \arctan(d^{1/2}(-b*x+a)^{1/2}/b^{1/2}/(d*x+c)^{1/2})/b^{1/2}/d^{1/2}$

Rubi [A] time = 0.03, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {63, 217, 203}

$$\frac{2 \tan^{-1} \left(\frac{\sqrt{d} \sqrt{a-bx}}{\sqrt{b} \sqrt{c+dx}} \right)}{\sqrt{b} \sqrt{d}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a - b*x]*Sqrt[c + d*x]),x]

[Out] $(-2 \text{ArcTan}[(\text{Sqrt}[d] \text{Sqrt}[a - b*x]) / (\text{Sqrt}[b] \text{Sqrt}[c + d*x])]) / (\text{Sqrt}[b] \text{Sqrt}[d])$

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 203

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] :> Simp[(1*ArcTan[(Rt[b, 2]*x)/Rt[a, 2]])/(Rt[a, 2]*Rt[b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (GtQ[a, 0] || GtQ[b, 0])

Rule 217

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Subst[Int[1/(1 - b*x^2), x], x, x/Sqrt[a + b*x^2]] /; FreeQ[{a, b}, x] && !GtQ[a, 0]

Rubi steps

$$\int \frac{1}{\sqrt{a-bx}\sqrt{c+dx}} dx = -\frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{c+\frac{ad}{b}-\frac{dx^2}{b}}} dx, x, \sqrt{a-bx}\right)}{b}$$

$$= -\frac{2 \operatorname{Subst}\left(\int \frac{1}{1+\frac{dx^2}{b}} dx, x, \frac{\sqrt{a-bx}}{\sqrt{c+dx}}\right)}{b}$$

$$= -\frac{2 \tan^{-1}\left(\frac{\sqrt{d}\sqrt{a-bx}}{\sqrt{b}\sqrt{c+dx}}\right)}{\sqrt{b}\sqrt{d}}$$

Mathematica [B] time = 0.08, size = 103, normalized size = 2.40

$$\frac{2\sqrt{-b}\sqrt{-ad-bc}\sqrt{\frac{b(c+dx)}{ad+bc}}\sin^{-1}\left(\frac{\sqrt{-b}\sqrt{d}\sqrt{a-bx}}{\sqrt{b}\sqrt{-ad-bc}}\right)}{b^{3/2}\sqrt{d}\sqrt{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a - b*x]*Sqrt[c + d*x]), x]

[Out] (2*Sqrt[-b]*Sqrt[-(b*c) - a*d]*Sqrt[(b*(c + d*x))/(b*c + a*d)]*ArcSin[(Sqrt[-b]*Sqrt[d]*Sqrt[a - b*x])/(Sqrt[b]*Sqrt[-(b*c) - a*d])])/(b^(3/2)*Sqrt[d]*Sqrt[c + d*x])

fricas [B] time = 0.46, size = 185, normalized size = 4.30

$$\left[\frac{\sqrt{-bd} \log\left(8b^2d^2x^2 + b^2c^2 - 6abcd + a^2d^2 - 4(2bdx + bc - ad)\sqrt{-bd}\sqrt{-bx + a}\sqrt{dx + c} + 8(b^2cd - abd^2)x\right)}{2bd} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+a)^(1/2)/(d*x+c)^(1/2), x, algorithm="fricas")

[Out] [-1/2*sqrt(-b*d)*log(8*b^2*d^2*x^2 + b^2*c^2 - 6*a*b*c*d + a^2*d^2 - 4*(2*b*d*x + b*c - a*d)*sqrt(-b*d)*sqrt(-b*x + a)*sqrt(d*x + c) + 8*(b^2*c*d - a*b*d^2)*x)/(b*d), -sqrt(b*d)*arctan(1/2*(2*b*d*x + b*c - a*d)*sqrt(b*d)*sqrt(-b*x + a)*sqrt(d*x + c)/(b^2*d^2*x^2 - a*b*c*d + (b^2*c*d - a*b*d^2)*x))/(b*d)]

giac [A] time = 1.16, size = 54, normalized size = 1.26

$$\frac{2b \log\left(\left|-\sqrt{-bd} \sqrt{-bx+a} + \sqrt{b^2c + (bx-a)bd + abd}\right|\right)}{\sqrt{-bd} |b|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+a)^(1/2)/(d*x+c)^(1/2),x, algorithm="giac")

[Out] 2*b*log(abs(-sqrt(-b*d)*sqrt(-b*x+a) + sqrt(b^2*c + (b*x-a)*b*d + a*b*d)))/sqrt(-b*d)*abs(b)

maple [B] time = 0.01, size = 84, normalized size = 1.95

$$\frac{\sqrt{(-bx+a)(dx+c)} \arctan\left(\frac{\sqrt{bd}\left(x-\frac{ad-bc}{2bd}\right)}{\sqrt{-bdx^2+ac+(ad-bc)x}}\right)}{\sqrt{-bx+a} \sqrt{dx+c} \sqrt{bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-b*x+a)^(1/2)/(d*x+c)^(1/2),x)

[Out] ((-b*x+a)*(d*x+c))^(1/2)/(-b*x+a)^(1/2)/(d*x+c)^(1/2)/(b*d)^(1/2)*arctan((b*d)^(1/2)*(x-1/2*(a*d-b*c)/b/d)/(-b*d*x^2+(a*d-b*c)*x+a*c)^(1/2))

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-b*x+a)^(1/2)/(d*x+c)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError >> Computation failed since Maxima requested a dditional constraints; using the 'assume' command before evaluation *may* help (example of legal syntax is 'assume(a*d-b*c>0)', see `assume?` for more details)Is a*d-b*c zero or nonzero?

mupad [B] time = 0.34, size = 44, normalized size = 1.02

$$\frac{4 \operatorname{atan}\left(\frac{d(\sqrt{a-bx}-\sqrt{a})}{\sqrt{bd}(\sqrt{c+dx}-\sqrt{c})}\right)}{\sqrt{bd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a - b*x)^(1/2)*(c + d*x)^(1/2)),x)`

[Out] $-(4*\operatorname{atan}((d*((a - b*x)^{(1/2)} - a^{(1/2)}))/((b*d)^{(1/2)*((c + d*x)^{(1/2)} - c^{(1/2))}))/((b*d)^{(1/2)}$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a - bx} \sqrt{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(-b*x+a)**(1/2)/(d*x+c)**(1/2),x)`

[Out] `Integral(1/(sqrt(a - b*x)*sqrt(c + d*x)), x)`

3.1559 $\int (a + bx)^{3/2} \sqrt[3]{c + dx} dx$

Optimal. Leaf size=457

$$\frac{108 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} (bc - ad)^3 \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{935 b^{4/3} d^3 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc - ad} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} \right)} \right)}{108 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} (bc - ad)^3 \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{935 b^{4/3} d^3 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc - ad} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} \right)} \right)}$$

[Out] $12/187 * (-a*d+b*c) * (b*x+a)^{(3/2)} * (d*x+c)^{(1/3)} / b/d + 6/17 * (b*x+a)^{(5/2)} * (d*x+c)^{(1/3)} / b - 108/935 * (-a*d+b*c)^2 * (d*x+c)^{(1/3)} * (b*x+a)^{(1/2)} / b/d^2 - 108/935 * 3^{3/4} * (-a*d+b*c)^3 * ((-a*d+b*c)^{(1/3)} - b^{1/3} * (d*x+c)^{(1/3)}) * \operatorname{EllipticF} \left((-b^{1/3} * (d*x+c)^{(1/3)} + (-a*d+b*c)^{(1/3)} * (1+3^{1/2})) / (-b^{1/3} * (d*x+c)^{(1/3)} + (-a*d+b*c)^{(1/3)} * (1-3^{1/2})) \right), 2 * I - I * 3^{1/2} * (((-a*d+b*c)^{(2/3)} + b^{1/3} * (-a*d+b*c)^{(1/3)} * (d*x+c)^{(1/3)} + b^{2/3} * (d*x+c)^{(2/3)}) / (-b^{1/3} * (d*x+c)^{(1/3)} + (-a*d+b*c)^{(1/3)} * (1-3^{1/2}))^2)^{(1/2)} * (1/2 * 6^{1/2} - 1/2 * 2^{1/2}) / b^{4/3} / d^3 / (b*x+a)^{(1/2)} / ((-a*d+b*c)^{(1/3)} * ((-a*d+b*c)^{(1/3)} - b^{1/3} * (d*x+c)^{(1/3)}) / (-b^{1/3} * (d*x+c)^{(1/3)} + (-a*d+b*c)^{(1/3)} * (1-3^{1/2}))^2)^{(1/2)}$

Rubi [A] time = 0.63, antiderivative size = 457, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 219}

$$\frac{108 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} (bc - ad)^3 \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} F \left(\sin^{-1} \left(\frac{(1 + \sqrt{3}) \sqrt[3]{bc - ad} + (1 - \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}}{(1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx}} \right)} \right)}{935 b^{4/3} d^3 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc - ad} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)} * (c + d*x)^{(1/3)}, x]$

[Out] $(-108 * (b*c - a*d)^2 * \operatorname{Sqrt}[a + b*x] * (c + d*x)^{(1/3)}) / (935 * b * d^2) + (12 * (b*c - a*d) * (a + b*x)^{(3/2)} * (c + d*x)^{(1/3)}) / (187 * b * d) + (6 * (a + b*x)^{(5/2)} * (c + d*x)^{(1/3)}) / (17 * b) - (108 * 3^{3/4} * \operatorname{Sqrt}[2 - \operatorname{Sqrt}[3]] * (b*c - a*d)^3 * ((b*c - a*d)^{(1/3)} - b^{1/3} * (c + d*x)^{(1/3)}) * \operatorname{Sqrt}[\left((b*c - a*d)^{(2/3)} + b^{1/3} * (b*c - a*d)^{(1/3)} * (c + d*x)^{(1/3)} + b^{2/3} * (c + d*x)^{(2/3)} \right)] / ((1 - \operatorname{Sqrt}[3]) * (b*c - a*d)^{(1/3)} - b^{1/3} * (c + d*x)^{(1/3)})^2 * \operatorname{EllipticF}[\operatorname{ArcSin}[\left((1 + \operatorname{Sqrt}[3]) * (b*c - a*d)^{(1/3)} - b^{1/3} * (c + d*x)^{(1/3)} \right) / ((1 - \operatorname{Sqrt}[3]) * (b*c - a*d)^{(1/3)} - b^{1/3} * (c + d*x)^{(1/3)})], -7 + 4 * \operatorname{Sqrt}[3]]) / (935 * b^{4/3} * d^3 * \operatorname{Sqrt}[a$

+ b*x]*Sqrt[-(((b*c - a*d)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2))]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 219

Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s + r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2))], x] /; FreeQ[{a, b}, x] && NegQ[a]

Rubi steps

$$\begin{aligned}
\int (a + bx)^{3/2} \sqrt[3]{c + dx} \, dx &= \frac{6(a + bx)^{5/2} \sqrt[3]{c + dx}}{17b} + \frac{(2(bc - ad)) \int \frac{(a+bx)^{3/2}}{(c+dx)^{2/3}} \, dx}{17b} \\
&= \frac{12(bc - ad)(a + bx)^{3/2} \sqrt[3]{c + dx}}{187bd} + \frac{6(a + bx)^{5/2} \sqrt[3]{c + dx}}{17b} - \frac{(18(bc - ad)^2) \int \frac{\sqrt{a+bx}}{(c+dx)^{2/3}} \, dx}{187bd} \\
&= -\frac{108(bc - ad)^2 \sqrt{a + bx} \sqrt[3]{c + dx}}{935bd^2} + \frac{12(bc - ad)(a + bx)^{3/2} \sqrt[3]{c + dx}}{187bd} + \frac{6(a + bx)^{5/2} \sqrt[3]{c + dx}}{17b} \\
&= -\frac{108(bc - ad)^2 \sqrt{a + bx} \sqrt[3]{c + dx}}{935bd^2} + \frac{12(bc - ad)(a + bx)^{3/2} \sqrt[3]{c + dx}}{187bd} + \frac{6(a + bx)^{5/2} \sqrt[3]{c + dx}}{17b} \\
&= -\frac{108(bc - ad)^2 \sqrt{a + bx} \sqrt[3]{c + dx}}{935bd^2} + \frac{12(bc - ad)(a + bx)^{3/2} \sqrt[3]{c + dx}}{187bd} + \frac{6(a + bx)^{5/2} \sqrt[3]{c + dx}}{17b}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.16

$$\frac{2(a + bx)^{5/2} \sqrt[3]{c + dx} {}_2F_1\left(-\frac{1}{3}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc}\right)}{5b \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)*(c + d*x)^(1/3), x]

[Out] (2*(a + b*x)^(5/2)*(c + d*x)^(1/3)*Hypergeometric2F1[-1/3, 5/2, 7/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bx + a\right)^{\frac{3}{2}}(dx + c)^{\frac{1}{3}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(1/3), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)*(d*x + c)^(1/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)*(d*x + c)^(1/3), x)

maple [F] time = 0.15, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)*(d*x+c)^(1/3),x)

[Out] int((b*x+a)^(3/2)*(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)*(d*x + c)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{\frac{3}{2}}(c + dx)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)*(c + d*x)^(1/3),x)

[Out] int((a + b*x)^(3/2)*(c + d*x)^(1/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{3}{2}} \sqrt[3]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)*(d*x+c)**(1/3),x)

[Out] Integral((a + b*x)**(3/2)*(c + d*x)**(1/3), x)

3.1560 $\int \sqrt{a + bx} \sqrt[3]{c + dx} dx$

Optimal. Leaf size=419

$$\frac{12 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} (bc - ad)^2 \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{(1 + \sqrt{3}) \sqrt[3]{bc - ad}}{(1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx}} \right) \right)}{55 b^{4/3} d^2 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc - ad} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}$$

[Out] $6/11*(b*x+a)^{(3/2)}*(d*x+c)^{(1/3)}/b+12/55*(-a*d+b*c)*(d*x+c)^{(1/3)}*(b*x+a)^{(1/2)}/b/d+12/55*3^{(3/4)}*(-a*d+b*c)^2*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*\operatorname{EllipticF}((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})),2*I-I*3^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})))^2)^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})/b^{(4/3)}/d^2/(b*x+a)^{(1/2)}/(-(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.37, antiderivative size = 419, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 219}

$$\frac{12 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} (bc - ad)^2 \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} F \left(\sin^{-1} \left(\frac{(1 + \sqrt{3}) \sqrt[3]{bc - ad}}{(1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx}} \right) \right)}{55 b^{4/3} d^2 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc - ad} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]*(c + d*x)^(1/3),x]

[Out] $(12*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/3)})/(55*b*d) + (6*(a + b*x)^{(3/2)}*(c + d*x)^{(1/3)})/(11*b) + (12*3^{(3/4)}*\operatorname{Sqrt}[2 - \operatorname{Sqrt}[3]]*(b*c - a*d)^2*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})*\operatorname{Sqrt}[\left((b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)} \right)]/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})^2)*\operatorname{EllipticF}[\operatorname{ArcSin}[\left((1 + \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)} \right)/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})], -7 + 4*\operatorname{Sqrt}[3]])/(55*b^{(4/3)}*d^2*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[-\left((b*c - a*d)^{(1/3)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}) \right)]/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})^2))$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2)]), x] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rubi steps

$$\begin{aligned}
\int \sqrt{a+bx} \sqrt[3]{c+dx} dx &= \frac{6(a+bx)^{3/2} \sqrt[3]{c+dx}}{11b} + \frac{(2(bc-ad)) \int \frac{\sqrt{a+bx}}{(c+dx)^{2/3}} dx}{11b} \\
&= \frac{12(bc-ad)\sqrt{a+bx} \sqrt[3]{c+dx}}{55bd} + \frac{6(a+bx)^{3/2} \sqrt[3]{c+dx}}{11b} - \frac{(6(bc-ad)^2) \int \frac{1}{\sqrt{a+bx} (c+dx)^{2/3}} dx}{55bd} \\
&= \frac{12(bc-ad)\sqrt{a+bx} \sqrt[3]{c+dx}}{55bd} + \frac{6(a+bx)^{3/2} \sqrt[3]{c+dx}}{11b} - \frac{(18(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+}} \right)}{55bd^2} \\
&= \frac{12(bc-ad)\sqrt{a+bx} \sqrt[3]{c+dx}}{55bd} + \frac{6(a+bx)^{3/2} \sqrt[3]{c+dx}}{11b} + \frac{12 \cdot 3^{3/4} \sqrt{2-\sqrt{3}} (bc-ad)^2 (\sqrt[3]{b})}{55bd^2}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.17

$$\frac{2(a+bx)^{3/2} \sqrt[3]{c+dx} {}_2F_1\left(-\frac{1}{3}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]*(c + d*x)^(1/3), x]

[Out] (2*(a + b*x)^(3/2)*(c + d*x)^(1/3)*Hypergeometric2F1[-1/3, 3/2, 5/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left(\sqrt{bx+a}(dx+c)^{\frac{1}{3}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(1/3), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)*(d*x+c)^(1/3),x, algorithm="giac")`

[Out] `integrate(sqrt(b*x + a)*(d*x + c)^(1/3), x)`

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \sqrt{bx + a} (dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(1/2)*(d*x+c)^(1/3),x)`

[Out] `int((b*x+a)^(1/2)*(d*x+c)^(1/3),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx + a} (dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)*(d*x+c)^(1/3),x, algorithm="maxima")`

[Out] `integrate(sqrt(b*x + a)*(d*x + c)^(1/3), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \sqrt{a + bx} (c + dx)^{1/3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/2)*(c + d*x)^(1/3),x)`

[Out] `int((a + b*x)^(1/2)*(c + d*x)^(1/3), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{a + bx} \sqrt[3]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/2)*(d*x+c)**(1/3),x)`

[Out] `Integral(sqrt(a + b*x)*(c + d*x)**(1/3), x)`

$$3.1561 \quad \int \frac{\sqrt[3]{c+dx}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=381

$$\frac{6\sqrt{a+bx}\sqrt[3]{c+dx}}{5b} - \frac{4 \cdot 3^{3/4} \sqrt{2-\sqrt{3}} (bc-ad) \left(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx} \right)^2}}}{5b^{4/3}d\sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{bc-ad}\left(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx} \right)^2}}}$$

[Out] $6/5*(d*x+c)^{(1/3)}*(b*x+a)^{(1/2)}/b-4/5*3^{(3/4)}*(-a*d+b*c)*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*EllipticF((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})),2*I-I*3^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})/b^{(4/3)}/d/(b*x+a)^{(1/2)}/(-a*d+b*c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^{(1/2)}$

Rubi [A] time = 0.27, antiderivative size = 381, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 219}

$$\frac{6\sqrt{a+bx}\sqrt[3]{c+dx}}{5b} - \frac{4 \cdot 3^{3/4} \sqrt{2-\sqrt{3}} (bc-ad) \left(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx} \right)^2}}}{5b^{4/3}d\sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{bc-ad}\left(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx} \right)^2}}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/3)/Sqrt[a + b*x],x]

[Out] $(6*\text{Sqrt}[a + b*x]*(c + d*x)^{(1/3)})/(5*b) - (4*3^{(3/4)}*\text{Sqrt}[2 - \text{Sqrt}[3]]*(b*c - a*d)*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})*\text{Sqrt}[\frac{(b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)}]{(1 - \text{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}}^{(1/2)}]*\text{EllipticF}[\text{ArcSin}[\frac{(1 + \text{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}]{(1 - \text{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}}], -7 + 4*\text{Sqrt}[3]])/(5*b^{(4/3)}*d*\text{Sqrt}[a + b*x]*\text{Sqrt}[-\frac{(b*c - a*d)^{(1/3)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})}{(1 - \text{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}}^{(1/2)}])$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2)]), x]] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rubi steps

$$\int \frac{\sqrt[3]{c+dx}}{\sqrt{a+bx}} dx = \frac{6\sqrt{a+bx}\sqrt[3]{c+dx}}{5b} + \frac{(2(bc-ad)) \int \frac{1}{\sqrt{a+bx}(c+dx)^{2/3}} dx}{5b}$$

$$= \frac{6\sqrt{a+bx}\sqrt[3]{c+dx}}{5b} + \frac{(6(bc-ad)) \text{Subst}\left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx}\right)}{5bd}$$

$$= \frac{6\sqrt{a+bx}\sqrt[3]{c+dx}}{5b} - \frac{4 \cdot 3^{3/4} \sqrt{2-\sqrt{3}} (bc-ad) (\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b}\sqrt[3]{bc-ad}}{(1-\sqrt{3})\sqrt[3]{bc-ad}}}}{5b^{4/3}d\sqrt{a+bx} \sqrt{\frac{\sqrt[3]{bc-ad}}{(1-\sqrt{3})}}}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.19

$$\frac{2\sqrt{a+bx}\sqrt[3]{c+dx} {}_2F_1\left(-\frac{1}{3}, \frac{1}{2}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/Sqrt[a + b*x], x]

[Out] (2*Sqrt[a + b*x]*(c + d*x)^(1/3)*Hypergeometric2F1[-1/3, 1/2, 3/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx+c)^{\frac{1}{3}}}{\sqrt{bx+a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] integral((d*x + c)^(1/3)/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{3}}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(1/2), x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/sqrt(b*x + a), x)

maple [F] time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{3}}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(1/2), x)

[Out] int((d*x+c)^(1/3)/(b*x+a)^(1/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/3)/sqrt(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/3}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/3)/(a + b*x)^(1/2),x)

[Out] int((c + d*x)^(1/3)/(a + b*x)^(1/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{c + dx}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/3)/(b*x+a)**(1/2),x)

[Out] Integral((c + d*x)**(1/3)/sqrt(a + b*x), x)

$$3.1562 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=366

$$\frac{4\sqrt{2-\sqrt{3}} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right)}{\sqrt[4]{3} b^{4/3} \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

[Out] $-2*(d*x+c)^{(1/3)}/b/(b*x+a)^{(1/2)}-4/3*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*\operatorname{EllipticF}((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})), 2*I-I*3^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})))^2)^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})*3^{(3/4)}/b^{(4/3)}/(b*x+a)^{(1/2)}/(-(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.26, antiderivative size = 366, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {47, 63, 219}

$$\frac{4\sqrt{2-\sqrt{3}} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right)}{\sqrt[4]{3} b^{4/3} \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(1/3)}/(a + b*x)^{(3/2)}, x]$

[Out] $(-2*(c + d*x)^{(1/3)})/(b*\operatorname{Sqrt}[a + b*x]) - (4*\operatorname{Sqrt}[2 - \operatorname{Sqrt}[3]]*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})*\operatorname{Sqrt}[\left((b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)} \right)]/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})^2]*\operatorname{EllipticF}[\operatorname{ArcSin}[\left((1 + \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)} \right)]/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})], -7 + 4*\operatorname{Sqrt}[3]])/(3^{(1/4)}*b^{(4/3)}*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[-\left((b*c - a*d)^{(1/3)}*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)} \right)]/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})^2])]$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2))], x] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rubi steps

$$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{3/2}} dx = -\frac{2\sqrt[3]{c+dx}}{b\sqrt{a+bx}} + \frac{(2d) \int \frac{1}{\sqrt{a+bx}(c+dx)^{2/3}} dx}{3b}$$

$$= -\frac{2\sqrt[3]{c+dx}}{b\sqrt{a+bx}} + \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx}\right)}{b}$$

$$= -\frac{2\sqrt[3]{c+dx}}{b\sqrt{a+bx}} - \frac{4\sqrt{2-\sqrt{3}}\left(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}\right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b}\sqrt[3]{bc-ad}\sqrt[3]{c+dx} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}}{\sqrt[4]{3}b^{4/3}\sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{bc-ad}\left(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}}$$

Mathematica [C] time = 0.03, size = 71, normalized size = 0.19

$$\frac{2\sqrt[3]{c+dx} {}_2F_1\left(-\frac{1}{2}, -\frac{1}{3}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt{a+bx} \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(3/2), x]

[Out] (-2*(c + d*x)^(1/3)*Hypergeometric2F1[-1/2, -1/3, 1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{1}{3}}}{b^2x^2+2abx+a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(3/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/3)/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{3}}}{(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(3/2), x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(3/2), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{3}}}{(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(3/2), x)

[Out] `int((d*x+c)^(1/3)/(b*x+a)^(3/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(1/3)/(b*x+a)^(3/2),x, algorithm="maxima")`

[Out] `integrate((d*x + c)^(1/3)/(b*x + a)^(3/2), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/3}}{(a + bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(1/3)/(a + b*x)^(3/2),x)`

[Out] `int((c + d*x)^(1/3)/(a + b*x)^(3/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{c + dx}}{(a + bx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(1/3)/(b*x+a)**(3/2),x)`

[Out] `Integral((c + d*x)**(1/3)/(a + b*x)**(3/2), x)`

$$3.1563 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=417

$$4\sqrt{2-\sqrt{3}} d \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \hline 9\sqrt[4]{3} b^{4/3} \sqrt{a+bx} (bc-ad) \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

[Out] $-2/3*(d*x+c)^{(1/3)}/b/(b*x+a)^{(3/2)}-4/9*d*(d*x+c)^{(1/3)}/b/(-a*d+b*c)/(b*x+a)^{(1/2)}+4/27*d*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*\operatorname{EllipticF}((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})),2*I-I*3^{(1/2)}*((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^2)^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})*3^{(3/4)}/b^{(4/3)}/(-a*d+b*c)/(b*x+a)^{(1/2)}/(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.37, antiderivative size = 417, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 51, 63, 219}

$$4\sqrt{2-\sqrt{3}} d \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \hline 9\sqrt[4]{3} b^{4/3} \sqrt{a+bx} (bc-ad) \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/3)/(a + b*x)^(5/2), x]

[Out] $(-2*(c+d*x)^{(1/3)})/(3*b*(a+b*x)^{(3/2)}) - (4*d*(c+d*x)^{(1/3)})/(9*b*(b*c-a*d)*\operatorname{Sqrt}[a+b*x]) + (4*\operatorname{Sqrt}[2-\operatorname{Sqrt}[3]]*d*((b*c-a*d)^{(1/3)}-b^{(1/3)}*(c+d*x)^{(1/3)})*\operatorname{Sqrt}[(b*c-a*d)^{(2/3)}+b^{(1/3)}*(b*c-a*d)^{(1/3)}*(c+d*x)^{(1/3)}+b^{(2/3)}*(c+d*x)^{(2/3)}])/((1-\operatorname{Sqrt}[3])*(b*c-a*d)^{(1/3)}-b^{(1/3)}*(c+d*x)^{(1/3)})^2*\operatorname{EllipticF}[\operatorname{ArcSin}(((1+\operatorname{Sqrt}[3])*(b*c-a*d)^{(1/3)}-b^{(1/3)}*(c+d*x)^{(1/3)})/((1-\operatorname{Sqrt}[3])*(b*c-a*d)^{(1/3)}-b^{(1/3)}*(c+d*x)^{(1/3)}))], -7+4*\operatorname{Sqrt}[3]])/((9*3^{(1/4)}*b^{(4/3)}*(b*c-a*d)*\operatorname{Sqrt}[a+b*x]*\operatorname{Sqrt}[-((b*c-a*d)^{(1/3)}*((b*c-a*d)^{(1/3)}-b^{(1/3)}*(c+d*x)^{(1/3)})/((1-\operatorname{Sqrt}[3])*(b*c-a*d)^{(1/3)}-b^{(1/3)}*(c+d*x)^{(1/3)})^2])]$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*sqrt[2 - sqrt[3]]*(s + r*x)*sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + sqrt[3])*s
+ r*x)/((1 - sqrt[3])*s + r*x)], -7 + 4*sqrt[3]])/(3^(1/4)*r*sqrt[a + b*x^3
]*sqrt[-((s*(s + r*x))/((1 - sqrt[3])*s + r*x)^2)]), x] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{5/2}} dx &= -\frac{2\sqrt[3]{c+dx}}{3b(a+bx)^{3/2}} + \frac{(2d) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{2/3}} dx}{9b} \\
&= -\frac{2\sqrt[3]{c+dx}}{3b(a+bx)^{3/2}} - \frac{4d\sqrt[3]{c+dx}}{9b(bc-ad)\sqrt{a+bx}} - \frac{(2d^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{2/3}} dx}{27b(bc-ad)} \\
&= -\frac{2\sqrt[3]{c+dx}}{3b(a+bx)^{3/2}} - \frac{4d\sqrt[3]{c+dx}}{9b(bc-ad)\sqrt{a+bx}} - \frac{(2d) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx} \right)}{9b(bc-ad)} \\
&= -\frac{2\sqrt[3]{c+dx}}{3b(a+bx)^{3/2}} - \frac{4d\sqrt[3]{c+dx}}{9b(bc-ad)\sqrt{a+bx}} + \frac{4\sqrt{2-\sqrt{3}} d (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{9^{\frac{4}{3}} b^{\frac{4}{3}} (bc-ad)} \sqrt{\frac{(bc-ad)^{2/3} + \dots}{(1-\dots)}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.18

$$-\frac{2\sqrt[3]{c+dx} {}_2F_1\left(-\frac{3}{2}, -\frac{1}{3}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a+bx)^{3/2} \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(5/2), x]

[Out] (-2*(c + d*x)^(1/3)*Hypergeometric2F1[-3/2, -1/3, -1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{1}{3}}}{b^3 x^3 + 3ab^2 x^2 + 3a^2 bx + a^3}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/3)/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(5/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(5/2), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(5/2),x)

[Out] int((d*x+c)^(1/3)/(b*x+a)^(5/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(5/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/3}}{(a + bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/3)/(a + b*x)^(5/2),x)

[Out] int((c + d*x)^(1/3)/(a + b*x)^(5/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{c + dx}}{(a + bx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/3)/(b*x+a)**(5/2),x)

[Out] Integral((c + d*x)**(1/3)/(a + b*x)**(5/2), x)

$$3.1564 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{7/2}} dx$$

Optimal. Leaf size=457

$$\frac{28\sqrt{2-\sqrt{3}} d^2 \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{(1+\sqrt{3})\sqrt[3]{bc-ad}}{(1-\sqrt{3})\sqrt[3]{bc-ad}}\right)\right)}{135\sqrt[4]{3} b^{4/3} \sqrt{a+bx} (bc-ad)^2 \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)}{\left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}}}$$

[Out] $-2/5*(d*x+c)^{(1/3)}/b/(b*x+a)^{(5/2)}-4/45*d*(d*x+c)^{(1/3)}/b/(-a*d+b*c)/(b*x+a)^{(3/2)}+28/135*d^2*(d*x+c)^{(1/3)}/b/(-a*d+b*c)^2/(b*x+a)^{(1/2)}-28/405*d^2*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*\operatorname{EllipticF}((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})),2*I-I*3^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})))^2)^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})*3^{(3/4)}/b^{(4/3)}/(-a*d+b*c)^2/(b*x+a)^{(1/2)}/(-(-a*d+b*c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.45, antiderivative size = 457, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 51, 63, 219}

$$\frac{28\sqrt{2-\sqrt{3}} d^2 \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}} F\left(\sin^{-1}\left(\frac{(1+\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}\right)\right)}{135\sqrt[4]{3} b^{4/3} \sqrt{a+bx} (bc-ad)^2 \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)}{\left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(1/3)}/(a + b*x)^{(7/2)}, x]$

[Out] $(-2*(c + d*x)^{(1/3)})/(5*b*(a + b*x)^{(5/2)}) - (4*d*(c + d*x)^{(1/3)})/(45*b*(b*c - a*d)*(a + b*x)^{(3/2)}) + (28*d^2*(c + d*x)^{(1/3)})/(135*b*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]) - (28*\operatorname{Sqrt}[2 - \operatorname{Sqrt}[3]]*d^2*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})*\operatorname{Sqrt}(((b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)})/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})^2)*\operatorname{EllipticF}[\operatorname{ArcSin}(((1 + \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}))], -7 + 4*\operatorname{Sqrt}[3]])/(135*3^{(1/4)}*b^{(4/3)}*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x])$

] * Sqrt[-(((b*c - a*d)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/
 ((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2)]

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 ((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
 nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
 NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
 rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
 & IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
 m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
 [n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
 ntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
 {p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
 (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
 [b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
 ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 219

Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
 s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
 *x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
 + r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2)]), x]] /; FreeQ[{a, b}, x
] && NegQ[a]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{7/2}} dx &= -\frac{2\sqrt[3]{c+dx}}{5b(a+bx)^{5/2}} + \frac{(2d) \int \frac{1}{(a+bx)^{5/2}(c+dx)^{2/3}} dx}{15b} \\
&= -\frac{2\sqrt[3]{c+dx}}{5b(a+bx)^{5/2}} - \frac{4d\sqrt[3]{c+dx}}{45b(bc-ad)(a+bx)^{3/2}} - \frac{(14d^2) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{2/3}} dx}{135b(bc-ad)} \\
&= -\frac{2\sqrt[3]{c+dx}}{5b(a+bx)^{5/2}} - \frac{4d\sqrt[3]{c+dx}}{45b(bc-ad)(a+bx)^{3/2}} + \frac{28d^2\sqrt[3]{c+dx}}{135b(bc-ad)^2\sqrt{a+bx}} + \frac{(14d^3) \int \frac{1}{\sqrt{a+bx}(c+dx)^2}}{405b(bc-ad)^2} \\
&= -\frac{2\sqrt[3]{c+dx}}{5b(a+bx)^{5/2}} - \frac{4d\sqrt[3]{c+dx}}{45b(bc-ad)(a+bx)^{3/2}} + \frac{28d^2\sqrt[3]{c+dx}}{135b(bc-ad)^2\sqrt{a+bx}} + \frac{(14d^2) \text{Subst} \left(\int \frac{1}{\sqrt{a-}} \right)}{135b(bc-ad)^2} \\
&= -\frac{2\sqrt[3]{c+dx}}{5b(a+bx)^{5/2}} - \frac{4d\sqrt[3]{c+dx}}{45b(bc-ad)(a+bx)^{3/2}} + \frac{28d^2\sqrt[3]{c+dx}}{135b(bc-ad)^2\sqrt{a+bx}} - \frac{28\sqrt{2-\sqrt{3}} d^2 (\sqrt[3]{bc})}{135b(bc-ad)^2}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.16

$$-\frac{2\sqrt[3]{c+dx} {}_2F_1\left(-\frac{5}{2}, -\frac{1}{3}; -\frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{5b(a+bx)^{5/2} \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(7/2), x]

[Out] (-2*(c + d*x)^(1/3)*Hypergeometric2F1[-5/2, -1/3, -3/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{1}{3}}}{b^4 x^4 + 4 ab^3 x^3 + 6 a^2 b^2 x^2 + 4 a^3 bx + a^4}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(7/2), x, algorithm="fricas")

[Out] $\text{integral}(\text{sqrt}(b*x + a)*(d*x + c)^{(1/3)}/(b^4*x^4 + 4*a*b^3*x^3 + 6*a^2*b^2*x^2 + 4*a^3*b*x + a^4), x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x+c)^{(1/3)}/(b*x+a)^{(7/2)},x, \text{algorithm}="giac")$

[Out] $\text{integrate}((d*x + c)^{(1/3)}/(b*x + a)^{(7/2)}, x)$

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((d*x+c)^{(1/3)}/(b*x+a)^{(7/2)},x)$

[Out] $\text{int}((d*x+c)^{(1/3)}/(b*x+a)^{(7/2)},x)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x+c)^{(1/3)}/(b*x+a)^{(7/2)},x, \text{algorithm}="maxima")$

[Out] $\text{integrate}((d*x + c)^{(1/3)}/(b*x + a)^{(7/2)}, x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/3}}{(a + bx)^{7/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((c + d*x)^{(1/3)}/(a + b*x)^{(7/2)},x)$


```
[Out] int((c + d*x)^(1/3)/(a + b*x)^(7/2), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{\sqrt[3]{c + dx}}{(a + bx)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(1/3)/(b*x+a)**(7/2), x)
```

```
[Out] Integral((c + d*x)**(1/3)/(a + b*x)**(7/2), x)
```

$$3.1565 \quad \int \frac{(a+bx)^{3/2}}{\sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=839

$$81\sqrt[4]{3}\sqrt{2+\sqrt{3}}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\sin^{-1}\left(\frac{(1+\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}}{(1-\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)$$

$$91b^{2/3}d^3\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{bc-ad}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left((1-\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

[Out] $6/13*(b*x+a)^{(3/2)}*(d*x+c)^{(2/3)}/d-54/91*(-a*d+b*c)*(d*x+c)^{(2/3)}*(b*x+a)^{(1/2)}/d^2-162/91*(-a*d+b*c)^2*(b*x+a)^{(1/2)}/b^{(2/3)}/d^2/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))-54/91*3^{(3/4)}*(-a*d+b*c)^{(7/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*EllipticF((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})),2*I-I*3^{(1/2)})*2^{(1/2)}*((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^2)^{(1/2)}/b^{(2/3)}/d^3/(b*x+a)^{(1/2)}/(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^2)^{(1/2)}+81/91*3^{(1/4)}*(-a*d+b*c)^{(7/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*EllipticE((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})),2*I-I*3^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^2)^{(1/2)}*(1/2*6^{(1/2)}+1/2*2^{(1/2)})/b^{(2/3)}/d^3/(b*x+a)^{(1/2)}/(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.94, antiderivative size = 839, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {50, 63, 304, 219, 1879}

$$81\sqrt[4]{3}\sqrt{2+\sqrt{3}}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\sin^{-1}\left(\frac{(1+\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}}{(1-\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)$$

$$91b^{2/3}d^3\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{bc-ad}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left((1-\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)/(c + d*x)^(1/3), x]

```
[Out] (-54*(b*c - a*d)*Sqrt[a + b*x]*(c + d*x)^(2/3))/(91*d^2) + (6*(a + b*x)^(3/2)*(c + d*x)^(2/3))/(13*d) - (162*(b*c - a*d)^2*Sqrt[a + b*x])/(91*b^(2/3)*d^2*((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))) + (81*3^(1/4)*Sqrt[2 + Sqrt[3]]*(b*c - a*d)^(7/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2]*EllipticE[ArcSin[((1 + Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))], -7 + 4*Sqrt[3]]]/(91*b^(2/3)*d^3*Sqrt[a + b*x]*Sqrt[-((b*c - a*d)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2)]) - (54*Sqrt[2]*3^(3/4)*(b*c - a*d)^(7/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2]*EllipticF[ArcSin[((1 + Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))], -7 + 4*Sqrt[3]]]/(91*b^(2/3)*d^3*Sqrt[a + b*x]*Sqrt[-((b*c - a*d)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2)])]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]]]/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2))], x]] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rule 304

```
Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
], s = Denom[Rt[b/a, 3]]}, -Dist[(Sqrt[2]*s)/(Sqrt[2] - Sqrt[3])*r), Int[1/S
qrt[a + b*x^3], x], x] + Dist[1/r, Int[((1 + Sqrt[3])*s + r*x)/Sqrt[a + b*x
^3], x], x]] /; FreeQ[{a, b}, x] && NegQ[a]
```

Rule 1879

```
Int[((c_) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = N
umer[Simplify[((1 + Sqrt[3])*d)/c]], s = Denom[Simplify[((1 + Sqrt[3])*d)/c
]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 - Sqrt[3])*s + r*x)), x] + S
imp[(3^(1/4)*Sqrt[2 + Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/(
(1 - Sqrt[3])*s + r*x)^2]*EllipticE[ArcSin[((1 + Sqrt[3])*s + r*x)/((1 - Sq
rt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(r^2*Sqrt[a + b*x^3]*Sqrt[-((s*(s + r*x)
)/((1 - Sqrt[3])*s + r*x)^2))], x]] /; FreeQ[{a, b, c, d}, x] && NegQ[a] &&
EqQ[b*c^3 - 2*(5 + 3*Sqrt[3])*a*d^3, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{\sqrt[3]{c+dx}} dx &= \frac{6(a+bx)^{3/2}(c+dx)^{2/3}}{13d} - \frac{(9(bc-ad)) \int \frac{\sqrt{a+bx}}{\sqrt[3]{c+dx}} dx}{13d} \\
&= -\frac{54(bc-ad)\sqrt{a+bx}(c+dx)^{2/3}}{91d^2} + \frac{6(a+bx)^{3/2}(c+dx)^{2/3}}{13d} + \frac{(27(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}\sqrt[3]{c+dx}} dx}{91d^2} \\
&= -\frac{54(bc-ad)\sqrt{a+bx}(c+dx)^{2/3}}{91d^2} + \frac{6(a+bx)^{3/2}(c+dx)^{2/3}}{13d} + \frac{(81(bc-ad)^2) \text{Subst} \left(\int \frac{x}{\sqrt{a-\frac{bc}{d}+bx}} dx \right)}{91d^3} \\
&= -\frac{54(bc-ad)\sqrt{a+bx}(c+dx)^{2/3}}{91d^2} + \frac{6(a+bx)^{3/2}(c+dx)^{2/3}}{13d} - \frac{(81(bc-ad)^2) \text{Subst} \left(\int \frac{(1+\sqrt{3})\sqrt[3]{bc-ad}}{\sqrt{a-\frac{bc}{d}+bx}} dx \right)}{91\sqrt[3]{bd^2}} \\
&= -\frac{54(bc-ad)\sqrt{a+bx}(c+dx)^{2/3}}{91d^2} + \frac{6(a+bx)^{3/2}(c+dx)^{2/3}}{13d} - \frac{162(bc-ad)^2\sqrt{a+bx}}{91b^{2/3}d^2((1-\sqrt{3})\sqrt[3]{bc-ad}-1)}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.09

$$\frac{2(a+bx)^{5/2} \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{3}, \frac{5}{2}, \frac{7}{2}, \frac{d(a+bx)}{ad-bc}\right)}{5b\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(1/3), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[1/3, 5/2, 7/2, (d*(a + b*x))/(-b*c) + a*d])/(5*b*(c + d*x)^(1/3))

fricas [F] time = 0.59, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{1}{3}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/3), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)/(d*x + c)^(1/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/3), x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(1/3), x)

maple [F] time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(1/3), x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(1/3), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{3/2}}{(c + dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/(c + d*x)^(1/3), x)

[Out] int((a + b*x)^(3/2)/(c + d*x)^(1/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{\sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/(d*x+c)**(1/3),x)

[Out] Integral((a + b*x)**(3/2)/(c + d*x)**(1/3), x)

$$3.1566 \quad \int \frac{\sqrt{a+bx}}{\sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=804

$$\frac{9\sqrt[4]{3} \sqrt{2+\sqrt{3}} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}} E\left(\sin^{-1}\left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}\right)\right)}{7b^{2/3}d^2\sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{bc-ad}\left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}}}$$

[Out] $6/7*(d*x+c)^{(2/3)}*(b*x+a)^{(1/2)}/d+18/7*(-a*d+b*c)*(b*x+a)^{(1/2)}/b^{(2/3)}/d/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))+6/7*3^{(3/4)}*(-a*d+b*c)^{(4/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*EllipticF((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})),2*I-I*3^{(1/2)})*2^{(1/2)}*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^{(1/2)}/b^{(2/3)}/d^2/(b*x+a)^{(1/2)}/(-(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^{(1/2)}-9/7*3^{(1/4)}*(-a*d+b*c)^{(4/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*EllipticE((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})),2*I-I*3^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^{(1/2)}/(1/2)*6^{(1/2)}+1/2*2^{(1/2)}/b^{(2/3)}/d^2/(b*x+a)^{(1/2)}/(-(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^{(1/2)}$

Rubi [A] time = 0.67, antiderivative size = 804, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {50, 63, 304, 219, 1879}

$$\frac{9\sqrt[4]{3} \sqrt{2+\sqrt{3}} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}} E\left(\sin^{-1}\left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}\right)\right)}{7b^{2/3}d^2\sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{bc-ad}\left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/(c + d*x)^(1/3), x]

[Out] $(6*\text{Sqrt}[a + b*x]*(c + d*x)^{(2/3)})/(7*d) + (18*(b*c - a*d)*\text{Sqrt}[a + b*x])/(7*b^{(2/3)}*d*((1 - \text{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})) - ($

$$9 \cdot 3^{1/4} \cdot \sqrt{2 + \sqrt{3}} \cdot (b \cdot c - a \cdot d)^{4/3} \cdot ((b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3}) \cdot \sqrt{((b \cdot c - a \cdot d)^{2/3} + b^{1/3} \cdot (b \cdot c - a \cdot d)^{1/3} \cdot (c + d \cdot x)^{1/3} + b^{2/3} \cdot (c + d \cdot x)^{2/3}) / ((1 - \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3})^2} \cdot \text{EllipticE}[\text{ArcSin}[\frac{(1 + \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3}}{(1 - \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3}}], -7 + 4 \cdot \sqrt{3}]] / (7 \cdot b^{2/3} \cdot d^2 \cdot \sqrt{a + b \cdot x} \cdot \sqrt{-((b \cdot c - a \cdot d)^{1/3} \cdot ((b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3})) / ((1 - \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3})^2)}) + (6 \cdot \sqrt{2} \cdot 3^{3/4} \cdot (b \cdot c - a \cdot d)^{4/3} \cdot ((b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3}) \cdot \sqrt{((b \cdot c - a \cdot d)^{2/3} + b^{1/3} \cdot (b \cdot c - a \cdot d)^{1/3} \cdot (c + d \cdot x)^{1/3} + b^{2/3} \cdot (c + d \cdot x)^{2/3}) / ((1 - \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3})^2} \cdot \text{EllipticF}[\text{ArcSin}[\frac{(1 + \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3}}{(1 - \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3}}], -7 + 4 \cdot \sqrt{3}]] / (7 \cdot b^{2/3} \cdot d^2 \cdot \sqrt{a + b \cdot x} \cdot \sqrt{-((b \cdot c - a \cdot d)^{1/3} \cdot ((b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3})) / ((1 - \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3})^2)})$$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*sqrt[2 - sqrt[3]]*(s + r*x)*sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + sqrt[3])*s
+ r*x)/((1 - sqrt[3])*s + r*x)], -7 + 4*sqrt[3]])/(3^(1/4)*r*sqrt[a + b*x^3
]*sqrt[-((s*(s + r*x))/((1 - sqrt[3])*s + r*x)^2)]), x]] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rule 304

```
Int[(x_)/sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
```


], s = Denom[Rt[b/a, 3]], -Dist[(Sqrt[2]*s)/(Sqrt[2 - Sqrt[3]]*r), Int[1/Sqrt[a + b*x^3], x], x] + Dist[1/r, Int[((1 + Sqrt[3])*s + r*x)/Sqrt[a + b*x^3], x], x] /; FreeQ[{a, b}, x] && NegQ[a]

Rule 1879

Int[((c_) + (d_)*(x_))/Sqrt[(a_) + (b_)*(x_)^3], x_Symbol] := With[{r = Numer[Simplify[((1 + Sqrt[3])*d)/c]], s = Denom[Simplify[((1 + Sqrt[3])*d)/c]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 - Sqrt[3])*s + r*x)), x] + Simp[(3^(1/4)*Sqrt[2 + Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticE[ArcSin[((1 + Sqrt[3])*s + r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(r^2*Sqrt[a + b*x^3]*Sqrt[-((s*(s + r*x))/(1 - Sqrt[3])*s + r*x)^2])], x] /; FreeQ[{a, b, c, d}, x] && NegQ[a] && EqQ[b*c^3 - 2*(5 + 3*Sqrt[3])*a*d^3, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{a+bx}}{\sqrt[3]{c+dx}} dx &= \frac{6\sqrt{a+bx}(c+dx)^{2/3}}{7d} - \frac{(3(bc-ad)) \int \frac{1}{\sqrt{a+bx} \sqrt[3]{c+dx}} dx}{7d} \\ &= \frac{6\sqrt{a+bx}(c+dx)^{2/3}}{7d} - \frac{(9(bc-ad)) \operatorname{Subst} \left(\int \frac{x}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx} \right)}{7d^2} \\ &= \frac{6\sqrt{a+bx}(c+dx)^{2/3}}{7d} + \frac{(9(bc-ad)) \operatorname{Subst} \left(\int \frac{(1+\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}x}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx} \right)}{7\sqrt[3]{b}d^2} - \frac{(9\sqrt{2}(2+))}{9\sqrt[3]{3}\sqrt{2+\sqrt{3}}(bc-ad)} \\ &= \frac{6\sqrt{a+bx}(c+dx)^{2/3}}{7d} + \frac{18(bc-ad)\sqrt{a+bx}}{7b^{2/3}d \left((1-\sqrt{3})\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx} \right)} - \frac{9\sqrt[3]{3}\sqrt{2+\sqrt{3}}(bc-ad)}{9\sqrt[3]{3}\sqrt{2+\sqrt{3}}(bc-ad)} \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.09

$$\frac{2(a+bx)^{3/2} \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(\frac{1}{3}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(1/3),x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[1/3, 3/2, 5/2, (d*(a + b*x))/(-b*c + a*d)])/(3*b*(c + d*x)^(1/3))

fricas [F] time = 0.57, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{3}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)/(d*x + c)^(1/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(1/3), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(1/3),x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(1/3),x)

[Out] int((a + b*x)^(1/2)/(c + d*x)^(1/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a+bx}}{\sqrt[3]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(1/3),x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(1/3), x)

$$3.1567 \quad \int \frac{1}{\sqrt{a+bx} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=762

$$\frac{2\sqrt{2} 3^{3/4} \sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad}}{(1-\sqrt{3}) \sqrt[3]{bc-ad}} \right) \right)}{b^{2/3} d \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

[Out] $-6*(b*x+a)^{(1/2)}/b^{(2/3)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})))-2*3^{(3/4)}*(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*\operatorname{EllipticF}((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})), 2*I-I*3^{(1/2)})*2^{(1/2)}*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^{(2)}^{(1/2)}/b^{(2/3)}/d/(b*x+a)^{(1/2)}/(-(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^{(2)}^{(1/2)}+3*3^{(1/4)}*(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*\operatorname{EllipticE}((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})), 2*I-I*3^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^{(2)}^{(1/2)}*(1/2*6^{(1/2)}+1/2*2^{(1/2))}/b^{(2/3)}/d/(b*x+a)^{(1/2)}/(-(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^{(2)}^{(1/2)}$

Rubi [A] time = 0.58, antiderivative size = 762, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {63, 304, 219, 1879}

$$\frac{6\sqrt{a+bx}}{b^{2/3} \left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)} \frac{2\sqrt{2} 3^{3/4} \sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad}}{(1-\sqrt{3}) \sqrt[3]{bc-ad}} \right) \right)}{b^{2/3} d \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/(\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/3)}), x]$

[Out] $(-6*\operatorname{Sqrt}[a + b*x])/b^{(2/3)}*((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}) + (3*3^{(1/4)}*\operatorname{Sqrt}[2 + \operatorname{Sqrt}[3]]*(b*c - a*d)^{(1/3)}*((b*c - a*d)$

$$\begin{aligned} & \sqrt[3]{b^2(c+dx) - b^2(c+dx)^2} \sqrt{\frac{(b^2c - a^2d)^{2/3} + b^{1/3}(b^2c - a^2d)^{1/3}(c+dx)^{1/3} + b^{2/3}(c+dx)^{2/3}}{(1 - \sqrt{3})(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{(1 + \sqrt{3})(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}}{(1 - \sqrt{3})(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}}\right], -7 + 4\sqrt{3}\right] \\ & - \frac{(b^2c - a^2d)^{1/3}(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}}{(1 - \sqrt{3})(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}} \sqrt{\frac{(b^2c - a^2d)^{2/3} + b^{1/3}(b^2c - a^2d)^{1/3}(c+dx)^{1/3} + b^{2/3}(c+dx)^{2/3}}{(1 - \sqrt{3})(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}}} \\ & - \frac{(b^2c - a^2d)^{1/3}(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}}{(1 - \sqrt{3})(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{(1 + \sqrt{3})(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}}{(1 - \sqrt{3})(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}}\right], -7 + 4\sqrt{3}\right] \\ & - \frac{(b^2c - a^2d)^{1/3}(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}}{(1 - \sqrt{3})(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}} \sqrt{\frac{(b^2c - a^2d)^{2/3} + b^{1/3}(b^2c - a^2d)^{1/3}(c+dx)^{1/3} + b^{2/3}(c+dx)^{2/3}}{(1 - \sqrt{3})(b^2c - a^2d)^{1/3} - b^{1/3}(c+dx)^{1/3}}} \end{aligned}$$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2))], x]] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rule 304

```
Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
], s = Denom[Rt[b/a, 3]]}, -Dist[(Sqrt[2]*s)/(Sqrt[2 - Sqrt[3]]*r), Int[1/S
qrt[a + b*x^3], x], x] + Dist[1/r, Int[((1 + Sqrt[3])*s + r*x)/Sqrt[a + b*x
^3], x], x]] /; FreeQ[{a, b}, x] && NegQ[a]
```

Rule 1879

```
Int[((c_) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = N
umer[Simplify[((1 + Sqrt[3])*d)/c]], s = Denom[Simplify[((1 + Sqrt[3])*d)/c
]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 - Sqrt[3])*s + r*x)), x] + S
imp[(3^(1/4)*Sqrt[2 + Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/(
```

$(1 - \text{Sqrt}[3]) * s + r * x)^2 * \text{EllipticE}[\text{ArcSin}[\frac{(1 + \text{Sqrt}[3]) * s + r * x}{(1 - \text{Sqrt}[3]) * s + r * x}], -7 + 4 * \text{Sqrt}[3]] / (r^2 * \text{Sqrt}[a + b * x^3] * \text{Sqrt}[-((s * (s + r * x)) / ((1 - \text{Sqrt}[3]) * s + r * x)^2)])], x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NegQ}[a] \&\& \text{EqQ}[b * c^3 - 2 * (5 + 3 * \text{Sqrt}[3]) * a * d^3, 0]$

Rubi steps

$$\int \frac{1}{\sqrt{a+bx} \sqrt[3]{c+dx}} dx = \frac{3 \text{Subst} \left(\int \frac{x}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx} \right)}{d}$$

$$= -\frac{3 \text{Subst} \left(\int \frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} x}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx} \right)}{\sqrt[3]{b} d} + \frac{(3\sqrt{2(2+\sqrt{3})} \sqrt[3]{bc-ad}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx} \right)}{\sqrt[3]{b} d}$$

$$= -\frac{6\sqrt{a+bx}}{b^{2/3} \left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)} + \frac{3^4 \sqrt{3} \sqrt{2+\sqrt{3}} \sqrt[3]{bc-ad} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{b^{2/3} \left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.09

$$\frac{2\sqrt{a+bx} \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{3}, \frac{1}{2}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(1/3)), x]

[Out] (2*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[1/3, 1/2, 3/2, (d*(a + b*x))/(-b*c) + a*d])/(b*(c + d*x)^(1/3))

fricas [F] time = 0.56, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{2}{3}}}{bdx^2+ac+(bc+ad)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(2/3)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(1/3)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(1/3),x)

[Out] int(1/(b*x+a)^(1/2)/(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/2)*(c + d*x)^(1/3)),x)

[Out] int(1/((a + b*x)^(1/2)*(c + d*x)^(1/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a+bx} \sqrt[3]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(1/2)/(d*x+c)**(1/3),x)
```

```
[Out] Integral(1/(sqrt(a + b*x)*(c + d*x)**(1/3)), x)
```


$$3.1568 \quad \int \frac{1}{(a+bx)^{3/2} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=796

$$\frac{2\sqrt{a+bx}d}{b^{2/3}(bc-ad)\left((1-\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)} + \frac{\sqrt[4]{3}\sqrt{2+\sqrt{3}}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}}{\left((1-\sqrt{3})\sqrt[3]{b}\right)^2}}}{b^{2/3}(bc-ad)^{2/3}\sqrt{a+bx}}$$

[Out] $-2*(d*x+c)^{(2/3)/(-a*d+b*c)/(b*x+a)^{(1/2)-2*d*(b*x+a)^{(1/2)/b^{(2/3)/(-a*d+b*c)/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2)})})}-2/3*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3))*EllipticF((-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2)})})/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2)})})},2*I-I*3^{(1/2)})*2^{(1/2)*(((-a*d+b*c)^{(2/3)+b^{(1/3)*(-a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)+b^{(2/3)*(d*x+c)^{(2/3)/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2)})})})^2)^{(1/2)*3^{(3/4)/b^{(2/3)/(-a*d+b*c)^{(2/3)/(b*x+a)^{(1/2)/(-a*d+b*c)^{(1/3)*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2)})})})^2)^{(1/2)+3^{(1/4)*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3))*EllipticE((-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2)})})/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2)})})},2*I-I*3^{(1/2)})*(((-a*d+b*c)^{(2/3)+b^{(1/3)*(-a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)+b^{(2/3)*(d*x+c)^{(2/3)/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2)})})})^2)^{(1/2)*(1/2*6^{(1/2)+1/2*2^{(1/2)})/b^{(2/3)/(-a*d+b*c)^{(2/3)/(b*x+a)^{(1/2)/(-a*d+b*c)^{(1/3)*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2)})})})^2)^{(1/2)}}}$

Rubi [A] time = 0.69, antiderivative size = 796, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {51, 63, 304, 219, 1879}

$$\frac{2\sqrt{a+bx}d}{b^{2/3}(bc-ad)\left((1-\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)} + \frac{\sqrt[4]{3}\sqrt{2+\sqrt{3}}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}}{\left((1-\sqrt{3})\sqrt[3]{b}\right)^2}}}{b^{2/3}(bc-ad)^{2/3}\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/2)*(c + d*x)^(1/3)), x]

[Out] $(-2*(c + d*x)^{(2/3)/((b*c - a*d)*Sqrt[a + b*x]) - (2*d*Sqrt[a + b*x])/(b^{(2/3)*(b*c - a*d)*((1 - Sqrt[3])*(b*c - a*d)^{(1/3) - b^{(1/3)*(c + d*x)^{(1/3)}}$

$$\begin{aligned} &)) + (3^{1/4} \sqrt{2 + \sqrt{3}} ((b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3})) \\ &)*\sqrt{((b^*c - a*d)^{2/3} + b^{1/3} (b^*c - a*d)^{1/3} (c + d*x)^{1/3} + b^{2/3} (c + d*x)^{2/3})} / ((1 - \sqrt{3}) (b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3})^2 \\ &)*\text{EllipticE}[\text{ArcSin}[\frac{(1 + \sqrt{3}) (b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3}}{(1 - \sqrt{3}) (b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3}}], \\ &-7 + 4\sqrt{3}]] / (b^{2/3} (b^*c - a*d)^{2/3} \sqrt{a + b*x} \sqrt{-((b^*c - a*d)^{1/3} ((b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3})) / ((1 - \sqrt{3}) (b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3})^2}) - (2\sqrt{2} ((b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3}) \sqrt{((b^*c - a*d)^{2/3} + b^{1/3} (b^*c - a*d)^{1/3} (c + d*x)^{1/3} + b^{2/3} (c + d*x)^{2/3})} / ((1 - \sqrt{3}) (b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3})^2} * \text{EllipticF}[\text{ArcSin}[\frac{(1 + \sqrt{3}) (b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3}}{(1 - \sqrt{3}) (b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3}}], -7 + 4\sqrt{3}]] / (3^{1/4} b^{2/3} (b^*c - a*d)^{2/3} \sqrt{a + b*x} \sqrt{-((b^*c - a*d)^{1/3} ((b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3})) / ((1 - \sqrt{3}) (b^*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3})^2})) \end{aligned}$$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*sqrt[2 - sqrt[3]]*(s + r*x)*sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + sqrt[3])*s
+ r*x)/((1 - sqrt[3])*s + r*x)], -7 + 4*sqrt[3]])/(3^(1/4)*r*sqrt[a + b*x^3
]*sqrt[-((s*(s + r*x))/((1 - sqrt[3])*s + r*x)^2)]), x]] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rule 304

```
Int[(x_)/sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
```

], s = Denom[Rt[b/a, 3]], -Dist[(Sqrt[2]*s)/(Sqrt[2 - Sqrt[3]]*r), Int[1/Sqrt[a + b*x^3], x], x] + Dist[1/r, Int[((1 + Sqrt[3])*s + r*x)/Sqrt[a + b*x^3], x], x] /; FreeQ[{a, b}, x] && NegQ[a]

Rule 1879

Int[((c_) + (d_)*(x_))/Sqrt[(a_) + (b_)*(x_)^3], x_Symbol] := With[{r = Numer[Simplify[((1 + Sqrt[3])*d)/c]], s = Denom[Simplify[((1 + Sqrt[3])*d)/c]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 - Sqrt[3])*s + r*x)), x] + Simp[(3^(1/4)*Sqrt[2 + Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticE[ArcSin[((1 + Sqrt[3])*s + r*x)/((1 - Sqrt[3])*s + r*x)]], -7 + 4*Sqrt[3])]/(r^2*Sqrt[a + b*x^3]*Sqrt[-((s*(s + r*x))/(1 - Sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[a] && EqQ[b*c^3 - 2*(5 + 3*Sqrt[3])*a*d^3, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{3/2} \sqrt[3]{c+dx}} dx &= -\frac{2(c+dx)^{2/3}}{(bc-ad)\sqrt{a+bx}} + \frac{d \int \frac{1}{\sqrt{a+bx} \sqrt[3]{c+dx}} dx}{3(bc-ad)} \\
 &= -\frac{2(c+dx)^{2/3}}{(bc-ad)\sqrt{a+bx}} + \frac{\text{Subst} \left(\int \frac{x}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx} \right)}{bc-ad} \\
 &= -\frac{2(c+dx)^{2/3}}{(bc-ad)\sqrt{a+bx}} - \frac{\text{Subst} \left(\int \frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} x}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx} \right)}{\sqrt[3]{b}(bc-ad)} + \frac{\sqrt{2(2+\sqrt{3})}}{\sqrt[3]{b} \sqrt{2-\sqrt{3}}} \\
 &= -\frac{2(c+dx)^{2/3}}{(bc-ad)\sqrt{a+bx}} - \frac{2d\sqrt{a+bx}}{b^{2/3}(bc-ad) \left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)} + \frac{\sqrt[4]{3} \sqrt{2-\sqrt{3}}}{\sqrt[3]{b} \sqrt{2-\sqrt{3}}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.09

$$\frac{2 \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(-\frac{1}{2}, \frac{1}{3}, \frac{1}{2}, \frac{d(a+bx)}{ad-bc} \right)}{b \sqrt{a+bx} \sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(1/3)),x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[-1/2, 1/3, 1/2, (d*(a + b*x))/(-b*c) + a*d])/(b*sqrt[a + b*x]*(c + d*x)^(1/3))

fricas [F] time = 0.54, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{2}{3}}}{b^2dx^3+a^2c+(b^2c+2abd)x^2+(2abc+a^2d)x},x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(2/3)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(1/3)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(1/3),x)

[Out] int(1/(b*x+a)^(3/2)/(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{3/2} (c + dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(1/3)),x)

[Out] int(1/((a + b*x)^(3/2)*(c + d*x)^(1/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} \sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(1/3),x)

[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(1/3)), x)

$$3.1569 \quad \int \frac{1}{(a+bx)^{5/2} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=842

$$\frac{10\sqrt{a+bx}d^2}{9b^{2/3}(bc-ad)^2\left((1-\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)} - \frac{5\sqrt{2+\sqrt{3}}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}}{\left((1-\sqrt{3})\sqrt[3]{bc-ad}\right)^2}}}{3\cdot 3^{3/4}b^{2/3}(bc-ad)^{5/3}\sqrt{a+bx}}$$

[Out] $-2/3*(d*x+c)^{(2/3)/(-a*d+b*c)/(b*x+a)^{(3/2)+10/9*d*(d*x+c)^{(2/3)/(-a*d+b*c)^2/(b*x+a)^{(1/2)+10/9*d^2*(b*x+a)^{(1/2)/b^{(2/3)/(-a*d+b*c)^2/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2))})+10/27*d*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*EllipticF((-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1+3^{(1/2))})/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2))})},2*I-I*3^{(1/2)})*2^{(1/2)*(((a*d+b*c)^{(2/3)+b^{(1/3)*(a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)+b^{(2/3)*(d*x+c)^{(2/3)/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2))})^2)^{(1/2)*3^{(3/4)/b^{(2/3)/(-a*d+b*c)^{(5/3)/(b*x+a)^{(1/2)/(-a*d+b*c)^{(1/3)*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2))})^2)^{(1/2)-5/9*d*((a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*EllipticE((-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1+3^{(1/2))})/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2))})},2*I-I*3^{(1/2)})*(((a*d+b*c)^{(2/3)+b^{(1/3)*(a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)+b^{(2/3)*(d*x+c)^{(2/3)/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2))})^2)^{(1/2)*(1/2*6^{(1/2)+1/2*2^{(1/2)})*3^{(1/4)/b^{(2/3)/(-a*d+b*c)^{(5/3)/(b*x+a)^{(1/2)/(-a*d+b*c)^{(1/3)*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2))})^2)^{(1/2)}})$

Rubi [A] time = 0.83, antiderivative size = 842, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {51, 63, 304, 219, 1879}

$$\frac{10\sqrt{a+bx}d^2}{9b^{2/3}(bc-ad)^2\left((1-\sqrt{3})\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)} - \frac{5\sqrt{2+\sqrt{3}}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}}{\left((1-\sqrt{3})\sqrt[3]{bc-ad}\right)^2}}}{3\cdot 3^{3/4}b^{2/3}(bc-ad)^{5/3}\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*(c + d*x)^(1/3)),x]

```
[Out] (-2*(c + d*x)^(2/3))/(3*(b*c - a*d)*(a + b*x)^(3/2)) + (10*d*(c + d*x)^(2/3))
)/(9*(b*c - a*d)^2*Sqrt[a + b*x]) + (10*d^2*Sqrt[a + b*x])/(9*b^(2/3)*(b*c
- a*d)^2*((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))) - (5
*Sqrt[2 + Sqrt[3]]*d*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b
*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c +
d*x)^(2/3))]/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2]*
EllipticE[ArcSin[((1 + Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)
)/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))], -7 + 4*Sqrt
[3]])/(3*3^(3/4)*b^(2/3)*(b*c - a*d)^(5/3)*Sqrt[a + b*x]*Sqrt[-((b*c - a*d)
^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))]/((1 - Sqrt[3])*(b*c
- a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2)]) + (10*Sqrt[2]*d*((b*c - a*d)^(
1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*
d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((1 - Sqrt[3])*(b*c - a
*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2]*EllipticF[ArcSin[((1 + Sqrt[3])*(b*
c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))]/((1 - Sqrt[3])*(b*c - a*d)^(1/3)
- b^(1/3)*(c + d*x)^(1/3))], -7 + 4*Sqrt[3]])/(9*3^(1/4)*b^(2/3)*(b*c - a*d)
^(5/3)*Sqrt[a + b*x]*Sqrt[-((b*c - a*d)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)
)*(c + d*x)^(1/3))]/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1
/3))^2)])
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)]/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2))], x]] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rule 304

```
Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
], s = Denom[Rt[b/a, 3]]}, -Dist[(Sqrt[2]*s)/(Sqrt[2 - Sqrt[3]]*r), Int[1/S
qrt[a + b*x^3], x], x] + Dist[1/r, Int[((1 + Sqrt[3])*s + r*x)/Sqrt[a + b*x
^3], x], x]] /; FreeQ[{a, b}, x] && NegQ[a]
```

Rule 1879

```
Int[((c_) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = N
umer[Simplify[((1 + Sqrt[3])*d)/c]], s = Denom[Simplify[((1 + Sqrt[3])*d)/c
]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 - Sqrt[3])*s + r*x)), x] + S
imp[(3^(1/4)*Sqrt[2 + Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/(
(1 - Sqrt[3])*s + r*x)^2]*EllipticE[ArcSin[((1 + Sqrt[3])*s + r*x)/((1 - Sq
rt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(r^2*Sqrt[a + b*x^3]*Sqrt[-((s*(s + r*x)
)/((1 - Sqrt[3])*s + r*x)^2))], x]] /; FreeQ[{a, b, c, d}, x] && NegQ[a] &&
EqQ[b*c^3 - 2*(5 + 3*Sqrt[3])*a*d^3, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/2} \sqrt[3]{c+dx}} dx &= -\frac{2(c+dx)^{2/3}}{3(bc-ad)(a+bx)^{3/2}} - \frac{(5d) \int \frac{1}{(a+bx)^{3/2} \sqrt[3]{c+dx}} dx}{9(bc-ad)} \\
&= -\frac{2(c+dx)^{2/3}}{3(bc-ad)(a+bx)^{3/2}} + \frac{10d(c+dx)^{2/3}}{9(bc-ad)^2 \sqrt{a+bx}} - \frac{(5d^2) \int \frac{1}{\sqrt{a+bx} \sqrt[3]{c+dx}} dx}{27(bc-ad)^2} \\
&= -\frac{2(c+dx)^{2/3}}{3(bc-ad)(a+bx)^{3/2}} + \frac{10d(c+dx)^{2/3}}{9(bc-ad)^2 \sqrt{a+bx}} - \frac{(5d) \operatorname{Subst} \left(\int \frac{x}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx} \right)}{9(bc-ad)^2} \\
&= -\frac{2(c+dx)^{2/3}}{3(bc-ad)(a+bx)^{3/2}} + \frac{10d(c+dx)^{2/3}}{9(bc-ad)^2 \sqrt{a+bx}} + \frac{(5d) \operatorname{Subst} \left(\int \frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{bx}}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx \right)}{9 \sqrt[3]{b} (bc-ad)^2} \\
&= -\frac{2(c+dx)^{2/3}}{3(bc-ad)(a+bx)^{3/2}} + \frac{10d(c+dx)^{2/3}}{9(bc-ad)^2 \sqrt{a+bx}} + \frac{10d^2 \sqrt{a+bx}}{9b^{2/3} (bc-ad)^2 ((1-\sqrt{3}) \sqrt[3]{bc-ad})}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.09

$$\frac{2\sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{3}{2}, \frac{1}{3}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a+bx)^{3/2}\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(1/3)), x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[-3/2, 1/3, -1/2, (d*(a + b*x))/(-b*c + a*d)]/(3*b*(a + b*x)^(3/2)*(c + d*x)^(1/3))

fricas [F] time = 0.55, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{2}{3}}}{b^3dx^4+a^3c+(b^3c+3ab^2d)x^3+3(ab^2c+a^2bd)x^2+(3a^2bc+a^3d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/3), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(2/3)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/3), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(1/3)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(1/3), x)

[Out] int(1/(b*x+a)^(5/2)/(d*x+c)^(1/3), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{5/2}(c+dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/2)*(c + d*x)^(1/3)),x)

[Out] int(1/((a + b*x)^(5/2)*(c + d*x)^(1/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{2}}\sqrt[3]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(1/3),x)

[Out] Integral(1/((a + b*x)**(5/2)*(c + d*x)**(1/3)), x)

$$3.1570 \quad \int \frac{(a+bx)^{3/2}}{(c+dx)^{2/3}} dx$$

Optimal. Leaf size=416

$$54 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} (bc - ad)^2 \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right)$$

$$55 \sqrt[3]{b} d^3 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

[Out] 6/11*(b*x+a)^(3/2)*(d*x+c)^(1/3)/d-54/55*(-a*d+b*c)*(d*x+c)^(1/3)*(b*x+a)^(1/2)/d^2-54/55*3^(3/4)*(-a*d+b*c)^2*((-a*d+b*c)^(1/3)-b^(1/3)*(d*x+c)^(1/3))*EllipticF((-b^(1/3)*(d*x+c)^(1/3)+(-a*d+b*c)^(1/3)*(1+3^(1/2)))/(-b^(1/3)*(d*x+c)^(1/3)+(-a*d+b*c)^(1/3)*(1-3^(1/2))),2*I-I*3^(1/2))*(((a*d+b*c)^(2/3)+b^(1/3)*(-a*d+b*c)^(1/3)*(d*x+c)^(1/3)+b^(2/3)*(d*x+c)^(2/3))/(-b^(1/3)*(d*x+c)^(1/3)+(-a*d+b*c)^(1/3)*(1-3^(1/2)))^2)^(1/2)*(1/2*6^(1/2)-1/2*2^(1/2))/b^(1/3)/d^3/(b*x+a)^(1/2)/((-a*d+b*c)^(1/3)*((-a*d+b*c)^(1/3)-b^(1/3)*(d*x+c)^(1/3))/(-b^(1/3)*(d*x+c)^(1/3)+(-a*d+b*c)^(1/3)*(1-3^(1/2)))^2)^(1/2)

Rubi [A] time = 0.39, antiderivative size = 416, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 219}

$$54 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} (bc - ad)^2 \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right)$$

$$55 \sqrt[3]{b} d^3 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)/(c + d*x)^(2/3), x]

[Out] (-54*(b*c - a*d)*Sqrt[a + b*x]*(c + d*x)^(1/3))/(55*d^2) + (6*(a + b*x)^(3/2)*(c + d*x)^(1/3))/(11*d) - (54*3^(3/4)*Sqrt[2 - Sqrt[3]]*(b*c - a*d)^2*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2*EllipticF[ArcSin[((1 + Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))], -7 + 4*Sqrt[3]]/(55*b^(1/3)*d^3*Sqrt[a + b*x]*Sqrt[-((b*c - a*d)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))]/((1 - Sqrt[3])*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))^2)])

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2)]), x]] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{(c+dx)^{2/3}} dx &= \frac{6(a+bx)^{3/2} \sqrt[3]{c+dx}}{11d} - \frac{(9(bc-ad)) \int \frac{\sqrt{a+bx}}{(c+dx)^{2/3}} dx}{11d} \\
&= -\frac{54(bc-ad)\sqrt{a+bx} \sqrt[3]{c+dx}}{55d^2} + \frac{6(a+bx)^{3/2} \sqrt[3]{c+dx}}{11d} + \frac{(27(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{2/3}} dx}{55d^2} \\
&= -\frac{54(bc-ad)\sqrt{a+bx} \sqrt[3]{c+dx}}{55d^2} + \frac{6(a+bx)^{3/2} \sqrt[3]{c+dx}}{11d} + \frac{(81(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} \right)}{55d^3} \\
&= -\frac{54(bc-ad)\sqrt{a+bx} \sqrt[3]{c+dx}}{55d^2} + \frac{6(a+bx)^{3/2} \sqrt[3]{c+dx}}{11d} - \frac{54 \cdot 3^{3/4} \sqrt{2-\sqrt{3}} (bc-ad)^2 (\sqrt[3]{bc-d})}{55d^3}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.18

$$\frac{2(a+bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{2/3} {}_2F_1 \left(\frac{2}{3}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc} \right)}{5b(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(2/3), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[2/3, 5/2, 7/2, (d*(a + b*x))/(-b*c + a*d)])/(5*b*(c + d*x)^(2/3))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{2}{3}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(2/3), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)/(d*x + c)^(2/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(2/3), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(2/3),x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(2/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{3/2}}{(c + dx)^{2/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/(c + d*x)^(2/3),x)

[Out] int((a + b*x)^(3/2)/(c + d*x)^(2/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{(c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/(d*x+c)**(2/3), x)

[Out] Integral((a + b*x)**(3/2)/(c + d*x)**(2/3), x)

$$3.1571 \quad \int \frac{\sqrt{a+bx}}{(c+dx)^{2/3}} dx$$

Optimal. Leaf size=381

$$6 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} (bc - ad) \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad}}{(1-\sqrt{3}) \sqrt[3]{bc-ad}} \right) \right)$$

$$5 \sqrt[3]{b} d^2 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

[Out] $6/5*(d*x+c)^{(1/3)}*(b*x+a)^{(1/2)}/d+6/5*3^{(3/4)}*(-a*d+b*c)*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*EllipticF((-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2)}))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)})),2*I-I*3^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)))/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^2)^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})/b^{(1/3)}/d^2/(b*x+a)^{(1/2)}/((-a*d+b*c)^{(1/3)}*(-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)}+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.30, antiderivative size = 381, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 219}

$$6 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} (bc - ad) \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad}}{(1-\sqrt{3}) \sqrt[3]{bc-ad}} \right) \right)$$

$$5 \sqrt[3]{b} d^2 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/(c + d*x)^(2/3),x]

[Out] $(6*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/3)})/(5*d) + (6*3^{(3/4)}*\operatorname{Sqrt}[2 - \operatorname{Sqrt}[3]]*(b*c - a*d)*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})*\operatorname{Sqrt}[\left((b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)} \right)]/(1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})^2]*\operatorname{EllipticF}[\operatorname{ArcSin}[\left((1 + \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)} \right)]/\left((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)} \right)], -7 + 4*\operatorname{Sqrt}[3]]/(5*b^{(1/3)}*d^2*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[-\left((b*c - a*d)^{(1/3)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}) \right)]/\left((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)} \right)^2)]$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2)]), x] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rubi steps

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{2/3}} dx = \frac{6\sqrt{a+bx}\sqrt[3]{c+dx}}{5d} - \frac{(3(bc-ad)) \int \frac{1}{\sqrt{a+bx}(c+dx)^{2/3}} dx}{5d}$$

$$= \frac{6\sqrt{a+bx}\sqrt[3]{c+dx}}{5d} - \frac{(9(bc-ad)) \text{Subst}\left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx}\right)}{5d^2}$$

$$= \frac{6\sqrt{a+bx}\sqrt[3]{c+dx}}{5d} + \frac{6 \cdot 3^{3/4} \sqrt{2-\sqrt{3}} (bc-ad) \left(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx}\right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b}\sqrt[3]{bc}}{\left((1-\sqrt{3})\sqrt[3]{bc}\right)}}}{5\sqrt[3]{b}d^2\sqrt{a+bx} \sqrt{\frac{\sqrt[3]{bc}}{\left((1-\sqrt{3})\sqrt[3]{bc}\right)}}}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.19

$$\frac{2(a + bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{2/3} {}_2F_1 \left(\frac{2}{3}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(c + dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(2/3), x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[2/3, 3/2, 5/2, (d*(a + b*x))/(-b*c) + a*d])/(3*b*(c + d*x)^(2/3))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx + a}}{(dx + c)^{\frac{2}{3}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(2/3), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)/(d*x + c)^(2/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx + a}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(2/3), x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(2/3), x)

maple [F] time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx + a}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(2/3), x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(2/3), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(2/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(2/3), x)

[Out] int((a + b*x)^(1/2)/(c + d*x)^(2/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(2/3),x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(2/3), x)

$$3.1572 \quad \int \frac{1}{\sqrt{a+bx} (c+dx)^{2/3}} dx$$

Optimal. Leaf size=345

$$2 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad}}{(1-\sqrt{3}) \sqrt[3]{bc-ad}} \right) \right) \\ \sqrt[3]{b} d \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

[Out] $-2 \cdot 3^{3/4} \cdot ((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot \operatorname{EllipticF}((-b^{1/3} \cdot (d \cdot x + c)^{1/3} + (-a \cdot d + b \cdot c)^{1/3} \cdot (1 + 3^{1/2})) / (-b^{1/3} \cdot (d \cdot x + c)^{1/3} + (-a \cdot d + b \cdot c)^{1/3} \cdot (1 - 3^{1/2})), 2 \cdot I - I \cdot 3^{1/2}) \cdot (((-a \cdot d + b \cdot c)^{2/3} + b^{1/3} \cdot (-a \cdot d + b \cdot c)^{1/3} \cdot (d \cdot x + c)^{1/3} + b^{2/3} \cdot (d \cdot x + c)^{2/3}) / (-b^{1/3} \cdot (d \cdot x + c)^{1/3} + (-a \cdot d + b \cdot c)^{1/3} \cdot (1 - 3^{1/2})))^2)^{1/2} \cdot (1/2 \cdot 6^{1/2} - 1/2 \cdot 2^{1/2}) / b^{1/3} / d / (b \cdot x + a)^{1/2} / (-(-a \cdot d + b \cdot c)^{1/3} \cdot ((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) / (-b^{1/3} \cdot (d \cdot x + c)^{1/3} + (-a \cdot d + b \cdot c)^{1/3} \cdot (1 - 3^{1/2})))^2)^{1/2}$

Rubi [A] time = 0.22, antiderivative size = 345, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 219}

$$2 \cdot 3^{3/4} \sqrt{2 - \sqrt{3}} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \sqrt[3]{b} d \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(2/3)),x]

[Out] $(-2 \cdot 3^{3/4} \cdot \operatorname{Sqrt}[2 - \operatorname{Sqrt}[3]] \cdot ((b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3})) \cdot \operatorname{Sqrt}[\frac{(b \cdot c - a \cdot d)^{2/3} + b^{1/3} \cdot (b \cdot c - a \cdot d)^{1/3} \cdot (c + d \cdot x)^{1/3} + b^{2/3} \cdot (c + d \cdot x)^{2/3}}{((1 - \operatorname{Sqrt}[3]) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3})^2}] \cdot \operatorname{EllipticF}[\operatorname{ArcSin}[\frac{(1 + \operatorname{Sqrt}[3]) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3}}{(1 - \operatorname{Sqrt}[3]) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3}}], -7 + 4 \cdot \operatorname{Sqrt}[3]] / (b^{1/3} \cdot d \cdot \operatorname{Sqrt}[a + b \cdot x] \cdot \operatorname{Sqrt}[-((b \cdot c - a \cdot d)^{1/3} \cdot ((b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3})) / ((1 - \operatorname{Sqrt}[3]) \cdot (b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3})^2])]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2))], x] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rubi steps

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{2/3}} dx = \frac{3 \operatorname{Subst}\left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c+dx}\right)}{d}$$

$$= -\frac{2 \cdot 3^{3/4} \sqrt{2-\sqrt{3}} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{bc-ad} \sqrt[3]{c+dx} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}}}{\sqrt[3]{b} d \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}}}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.21

$$\frac{2\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{2/3} {}_2F_1\left(\frac{1}{2}, \frac{2}{3}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

```
[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(2/3)),x]
```

```
[Out] (2*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[1/2, 2
/3, 3/2, (d*(a + b*x))/(-b*c) + a*d])/(b*(c + d*x)^(2/3))
```

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{1}{3}}}{bdx^2 + ac + (bc+ad)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(2/3),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/3)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a} (dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(2/3)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a} (dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(2/3),x)

[Out] int(1/(b*x+a)^(1/2)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a} (dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(2/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{\sqrt{a+bx} (c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(1/2)*(c + d*x)^(2/3)), x)`

[Out] `int(1/((a + b*x)^(1/2)*(c + d*x)^(2/3)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a + bx} (c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/2)/(d*x+c)**(2/3), x)`

[Out] `Integral(1/(sqrt(a + b*x)*(c + d*x)**(2/3)), x)`

$$3.1573 \quad \int \frac{1}{(a+bx)^{3/2}(c+dx)^{2/3}} dx$$

Optimal. Leaf size=383

$$2\sqrt{2-\sqrt{3}} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \hline \sqrt[4]{3} \sqrt[3]{b} \sqrt{a+bx} (bc-ad) \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

[Out] $-2*(d*x+c)^{(1/3)/(-a*d+b*c)/(b*x+a)^{(1/2)+2/3*((-a*d+b*c)^{(1/3)-b^{(1/3)}*(d*x+c)^{(1/3))}*\operatorname{EllipticF}((-b^{(1/3)}*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)}*(1+3^{(1/2))})/(-b^{(1/3)}*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2))})}, 2*I-I*3^{(1/2)})*(((-a*d+b*c)^{(2/3)+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)+b^{(2/3)}*(d*x+c)^{(2/3)})/(-b^{(1/3)}*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2))})^2)^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})*3^{(3/4)}/b^{(1/3)/(-a*d+b*c)/(b*x+a)^{(1/2)/(-(-a*d+b*c)^{(1/3)}*((-a*d+b*c)^{(1/3)-b^{(1/3)}*(d*x+c)^{(1/3))}/(-b^{(1/3)}*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)}*(1-3^{(1/2))})^2)^{(1/2)}$

Rubi [A] time = 0.29, antiderivative size = 383, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {51, 63, 219}

$$2\sqrt{2-\sqrt{3}} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \hline \sqrt[4]{3} \sqrt[3]{b} \sqrt{a+bx} (bc-ad) \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/2)*(c + d*x)^(2/3)), x]

[Out] $(-2*(c + d*x)^{(1/3)/((b*c - a*d)*\operatorname{Sqrt}[a + b*x])} + (2*\operatorname{Sqrt}[2 - \operatorname{Sqrt}[3]])*((b*c - a*d)^{(1/3) - b^{(1/3)}*(c + d*x)^{(1/3)})*\operatorname{Sqrt}[\left((b*c - a*d)^{(2/3) + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3) + b^{(2/3)}*(c + d*x)^{(2/3)} \right)/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3) - b^{(1/3)}*(c + d*x)^{(1/3)})^2] * \operatorname{EllipticF}[\operatorname{ArcSin}[\left((1 + \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3) - b^{(1/3)}*(c + d*x)^{(1/3)} \right)/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3) - b^{(1/3)}*(c + d*x)^{(1/3)})], -7 + 4*\operatorname{Sqrt}[3]])/(3^{(1/4)}*b^{(1/3)}*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*\operatorname{Sqrt}[-\left((b*c - a*d)^{(1/3)}*((b*c - a*d)^{(1/3) - b^{(1/3)}*(c + d*x)^{(1/3)}) \right)/((1 - \operatorname{Sqrt}[3])*(b*c - a*d)^{(1/3) - b^{(1/3)}*(c + d*x)^{(1/3)})^2])]$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2)]), x] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rubi steps

$$\int \frac{1}{(a + bx)^{3/2}(c + dx)^{2/3}} dx = -\frac{2\sqrt[3]{c + dx}}{(bc - ad)\sqrt{a + bx}} - \frac{d \int \frac{1}{\sqrt{a + bx}(c + dx)^{2/3}} dx}{3(bc - ad)}$$

$$= -\frac{2\sqrt[3]{c + dx}}{(bc - ad)\sqrt{a + bx}} - \frac{\text{Subst}\left(\int \frac{1}{\sqrt{a - \frac{bc}{d} + \frac{bx^3}{d}}} dx, x, \sqrt[3]{c + dx}\right)}{bc - ad}$$

$$= -\frac{2\sqrt[3]{c + dx}}{(bc - ad)\sqrt{a + bx}} + \frac{2\sqrt{2 - \sqrt{3}} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx}\right) \sqrt{\frac{(bc - ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{bc - ad}}{\left((1 - \sqrt{3}) \sqrt[3]{bc - ad}\right)}}}{\sqrt[3]{3} \sqrt[3]{b} (bc - ad) \sqrt{a + bx}}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.19

$$-\frac{2\left(\frac{b(c+dx)}{bc-ad}\right)^{2/3} {}_2F_1\left(-\frac{1}{2}, \frac{2}{3}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt{a+bx}(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(2/3)), x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[-1/2, 2/3, 1/2, (d*(a + b*x))/(-b*c) + a*d])/(b*Sqrt[a + b*x]*(c + d*x)^(2/3))

fricas [F] time = 0.54, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{1}{3}}}{b^2dx^3+a^2c+(b^2c+2abd)x^2+(2abc+a^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(2/3), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/3)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(2/3), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(2/3)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(2/3), x)

[Out] int(1/(b*x+a)^(3/2)/(d*x+c)^(2/3), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(2/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{\frac{3}{2}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(2/3)),x)

[Out] int(1/((a + b*x)^(3/2)*(c + d*x)^(2/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{3}{2}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(2/3),x)

[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(2/3)), x)

$$3.1574 \quad \int \frac{1}{(a+bx)^{5/2}(c+dx)^{2/3}} dx$$

Optimal. Leaf size=421

$$14\sqrt{2-\sqrt{3}} d \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \hline 9\sqrt[4]{3} \sqrt[3]{b} \sqrt{a+bx} (bc-ad)^2 \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

[Out] $-2/3*(d*x+c)^{(1/3)/(-a*d+b*c)/(b*x+a)^{(3/2)+14/9*d*(d*x+c)^{(1/3)/(-a*d+b*c)^2/(b*x+a)^{(1/2)-14/27*d*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)})*EllipticF(((-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1+3^{(1/2))})/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2))})}, 2*I-I*3^{(1/2)})*(((-a*d+b*c)^{(2/3)+b^{(1/3)*(-a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)+b^{(2/3)*(d*x+c)^{(2/3)})/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2))})^2})^{(1/2)*(1/2*6^{(1/2)-1/2*2^{(1/2)})*3^{(3/4)/b^{(1/3)/(-a*d+b*c)^2/(b*x+a)^{(1/2)/(-(-a*d+b*c)^{(1/3)*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)})/(-b^{(1/3)*(d*x+c)^{(1/3)+(-a*d+b*c)^{(1/3)*(1-3^{(1/2))})^2})^{(1/2)}$

Rubi [A] time = 0.37, antiderivative size = 421, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {51, 63, 219}

$$14\sqrt{2-\sqrt{3}} d \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\sin^{-1} \left(\frac{(1+\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{(1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \hline 9\sqrt[4]{3} \sqrt[3]{b} \sqrt{a+bx} (bc-ad)^2 \sqrt{-\frac{\sqrt[3]{bc-ad} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left((1-\sqrt{3}) \sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*(c + d*x)^(2/3)), x]

[Out] $(-2*(c + d*x)^{(1/3)/(3*(b*c - a*d)*(a + b*x)^{(3/2)} + (14*d*(c + d*x)^{(1/3)})/(9*(b*c - a*d)^2*\text{Sqrt}[a + b*x]) - (14*\text{Sqrt}[2 - \text{Sqrt}[3]]*d*((b*c - a*d)^{(1/3) - b^{(1/3)*(c + d*x)^{(1/3)})*\text{Sqrt}[(b*c - a*d)^{(2/3) + b^{(1/3)*(b*c - a*d)^{(1/3)*(c + d*x)^{(1/3) + b^{(2/3)*(c + d*x)^{(2/3)})/((1 - \text{Sqrt}[3])*(b*c - a*d)^{(1/3) - b^{(1/3)*(c + d*x)^{(1/3)})^2})*\text{EllipticF}[\text{ArcSin}[(1 + \text{Sqrt}[3])*(b*c - a*d)^{(1/3) - b^{(1/3)*(c + d*x)^{(1/3)})/(1 - \text{Sqrt}[3])*(b*c - a*d)^{(1/3) - b^{(1/3)*(c + d*x)^{(1/3)})}], -7 + 4*\text{Sqrt}[3]])/(9*3^{(1/4)*b^{(1/3)*(b*c - a*d)^2*\text{Sqrt}[a + b*x]*\text{Sqrt}[-((b*c - a*d)^{(1/3)*((b*c - a*d)^{(1/3) - b^{(1/3)*(c + d*x)^{(1/3)})$

$$\frac{+ d*x)^{(1/3))}{((1 - \text{Sqrt}[3])*(b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})^2}]$$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 219

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 - Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 - Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 + Sqrt[3])*s
+ r*x)/((1 - Sqrt[3])*s + r*x)], -7 + 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[-((s*(s + r*x))/((1 - Sqrt[3])*s + r*x)^2)]), x] /; FreeQ[{a, b}, x
] && NegQ[a]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/2}(c+dx)^{2/3}} dx &= -\frac{2\sqrt[3]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} - \frac{(7d) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{2/3}} dx}{9(bc-ad)} \\
&= -\frac{2\sqrt[3]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{14d\sqrt[3]{c+dx}}{9(bc-ad)^2\sqrt{a+bx}} + \frac{(7d^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{2/3}} dx}{27(bc-ad)^2} \\
&= -\frac{2\sqrt[3]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{14d\sqrt[3]{c+dx}}{9(bc-ad)^2\sqrt{a+bx}} + \frac{(7d) \text{Subst} \left[\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^3}{d}}} dx, x, \sqrt[3]{c} \right]}{9(bc-ad)^2} \\
&= -\frac{2\sqrt[3]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{14d\sqrt[3]{c+dx}}{9(bc-ad)^2\sqrt{a+bx}} - \frac{14\sqrt{2-\sqrt{3}} d (\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c})}{9(bc-ad)^2}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.17

$$-\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{2/3} {}_2F_1 \left(-\frac{3}{2}, \frac{2}{3}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(a+bx)^{3/2}(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(2/3)), x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[-3/2, 2/3, -1/2, (d*(a + b*x))/(-b*c + a*d)]/(3*b*(a + b*x)^(3/2)*(c + d*x)^(2/3))

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a}(dx+c)^{\frac{1}{3}}}{b^3dx^4 + a^3c + (b^3c + 3ab^2d)x^3 + 3(ab^2c + a^2bd)x^2 + (3a^2bc + a^3d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(2/3), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/3)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(2/3)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(2/3),x)

[Out] int(1/(b*x+a)^(5/2)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(2/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{2}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/2)*(c + d*x)^(2/3)),x)

[Out] int(1/((a + b*x)^(5/2)*(c + d*x)^(2/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{2}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(2/3),x)
```

```
[Out] Integral(1/((a + b*x)**(5/2)*(c + d*x)**(2/3)), x)
```


3.1575 $\int (a + bx)^{2/3} \sqrt[3]{c + dx} dx$

Optimal. Leaf size=219

$$\frac{(bc - ad)^2 \log(c + dx)}{18b^{4/3}d^{5/3}} + \frac{(bc - ad)^2 \log\left(\frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}} - 1\right)}{6b^{4/3}d^{5/3}} + \frac{(bc - ad)^2 \tan^{-1}\left(\frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{3\sqrt{3} b^{4/3}d^{5/3}} + \frac{(a + bx)^{2/3} \sqrt[3]{c + dx}}{6bd}$$

[Out] $1/6*(-a*d+b*c)*(b*x+a)^{(2/3)*(d*x+c)^{(1/3)}/b/d+1/2*(b*x+a)^{(5/3)*(d*x+c)^{(1/3)}/b+1/18*(-a*d+b*c)^2*\ln(d*x+c)/b^{(4/3)/d^{(5/3)+1/6*(-a*d+b*c)^2*\ln(-1+d^{(1/3)*(b*x+a)^{(1/3)/b^{(1/3)/(d*x+c)^{(1/3)}/b^{(4/3)/d^{(5/3)+1/9*(-a*d+b*c)^2*\arctan(1/3*3^{(1/2)+2/3*d^{(1/3)*(b*x+a)^{(1/3)/b^{(1/3)/(d*x+c)^{(1/3)*3^{(1/2)}/b^{(4/3)/d^{(5/3)*3^{(1/2)}}$

Rubi [A] time = 0.09, antiderivative size = 219, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {50, 59}

$$\frac{(bc - ad)^2 \log(c + dx)}{18b^{4/3}d^{5/3}} + \frac{(bc - ad)^2 \log\left(\frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}} - 1\right)}{6b^{4/3}d^{5/3}} + \frac{(bc - ad)^2 \tan^{-1}\left(\frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{3\sqrt{3} b^{4/3}d^{5/3}} + \frac{(a + bx)^{2/3} \sqrt[3]{c + dx}}{6bd}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(2/3)*(c + d*x)^(1/3), x]

[Out] $((b*c - a*d)*(a + b*x)^{(2/3)*(c + d*x)^{(1/3)}/(6*b*d) + ((a + b*x)^{(5/3)*(c + d*x)^{(1/3)}/(2*b) + ((b*c - a*d)^2*\text{ArcTan}[1/\text{Sqrt}[3] + (2*d^{(1/3)*(a + b*x)^{(1/3)}/(\text{Sqrt}[3]*b^{(1/3)*(c + d*x)^{(1/3)}/(3*\text{Sqrt}[3]*b^{(4/3)*d^{(5/3) + ((b*c - a*d)^2*\text{Log}[c + d*x]/(18*b^{(4/3)*d^{(5/3) + ((b*c - a*d)^2*\text{Log}[-1 + (d^{(1/3)*(a + b*x)^{(1/3)}/(b^{(1/3)*(c + d*x)^{(1/3)}/(6*b^{(4/3)*d^{(5/3)}}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 59

Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt

[3]*(c + d*x)^(1/3) + 1/Sqrt[3])/d, x] + (-Simp[(3*q*Log[(q*(a + b*x)^(1/3))]/(c + d*x)^(1/3) - 1]/(2*d), x] - Simp[(q*Log[c + d*x]/(2*d), x)]) /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]

Rubi steps

$$\begin{aligned} \int (a + bx)^{2/3} \sqrt[3]{c + dx} \, dx &= \frac{(a + bx)^{5/3} \sqrt[3]{c + dx}}{2b} + \frac{(bc - ad) \int \frac{(a+bx)^{2/3}}{(c+dx)^{2/3}} \, dx}{6b} \\ &= \frac{(bc - ad)(a + bx)^{2/3} \sqrt[3]{c + dx}}{6bd} + \frac{(a + bx)^{5/3} \sqrt[3]{c + dx}}{2b} - \frac{(bc - ad)^2 \int \frac{1}{\sqrt[3]{a+bx} (c+dx)^{2/3}} \, dx}{9bd} \\ &= \frac{(bc - ad)(a + bx)^{2/3} \sqrt[3]{c + dx}}{6bd} + \frac{(a + bx)^{5/3} \sqrt[3]{c + dx}}{2b} + \frac{(bc - ad)^2 \tan^{-1} \left(\frac{1}{\sqrt{3}} + \frac{2 \sqrt[3]{d} \sqrt[3]{a}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c}} \right)}{3\sqrt{3} b^{4/3} d^{5/3}} \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.33

$$\frac{3(a + bx)^{5/3} \sqrt[3]{c + dx} {}_2F_1 \left(-\frac{1}{3}, \frac{5}{3}; \frac{8}{3}; \frac{d(a+bx)}{ad-bc} \right)}{5b \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(2/3)*(c + d*x)^(1/3), x]

[Out] (3*(a + b*x)^(5/3)*(c + d*x)^(1/3)*Hypergeometric2F1[-1/3, 5/3, 8/3, (d*(a + b*x))/(-b*c) + a*d])/(5*b*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [A] time = 0.47, size = 717, normalized size = 3.27

$$\left[\frac{3 \sqrt{\frac{1}{3}} (b^3 c^2 d - 2 a b^2 c d^2 + a^2 b d^3) \sqrt{-\frac{(b d^2)^{\frac{1}{3}}}{b}} \log \left(-3 b d^2 x - 2 b c d - a d^2 + 3 (b d^2)^{\frac{1}{3}} (b x + a)^{\frac{2}{3}} (d x + c)^{\frac{1}{3}} d + 3 \sqrt{\frac{1}{3}} \left(2 \right. \right. \right)}{\left. \left. \left. \right) \right)}{\right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)*(d*x+c)^(1/3),x, algorithm="fricas")

[Out] [1/18*(3*sqrt(1/3)*(b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*sqrt(-(b*d^2)^(1/3)/b)*log(-3*b*d^2*x - 2*b*c*d - a*d^2 + 3*(b*d^2)^(1/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3)*d + 3*sqrt(1/3)*(2*(b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (b*d^2)^(1/3)*(b*d*x + a*d))*sqrt(-(b*d^2)^(1/3)/b)) + 2*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*d^2)^(2/3)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (b*d^2)^(2/3)*(b*x + a))/(b*x + a)) - (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*d^2)^(2/3)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d + (b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) + (b*d^2)^(1/3)*(b*d*x + a*d))/(b*x + a)) + 3*(3*b^2*d^3*x + b^2*c*d^2 + 2*a*b*d^3)*(b*x + a)^(2/3)*(d*x + c)^(1/3))/(b^2*d^3), -1/18*(6*sqrt(1/3)*(b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*sqrt((b*d^2)^(1/3)/b)*arctan(sqrt(1/3)*(2*(b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) + (b*d^2)^(1/3)*(b*d*x + a*d))*sqrt((b*d^2)^(1/3)/b)/(b*d^2*x + a*d^2)) - 2*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*d^2)^(2/3)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (b*d^2)^(2/3)*(b*x + a))/(b*x + a)) + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*d^2)^(2/3)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d + (b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) + (b*d^2)^(1/3)*(b*d*x + a*d))/(b*x + a)) - 3*(3*b^2*d^3*x + b^2*c*d^2 + 2*a*b*d^3)*(b*x + a)^(2/3)*(d*x + c)^(1/3))/(b^2*d^3)]

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{2}{3}}(dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)*(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(2/3)*(d*x + c)^(1/3), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{2}{3}}(dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(2/3)*(d*x+c)^(1/3),x)

[Out] int((b*x+a)^(2/3)*(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{2}{3}}(dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)*(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(2/3)*(d*x + c)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{2/3} (c + dx)^{1/3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(2/3)*(c + d*x)^(1/3),x)

[Out] int((a + b*x)^(2/3)*(c + d*x)^(1/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{2}{3}} \sqrt[3]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(2/3)*(d*x+c)**(1/3),x)

[Out] Integral((a + b*x)**(2/3)*(c + d*x)**(1/3), x)

$$3.1576 \quad \int \frac{\sqrt[3]{c+dx}}{\sqrt[3]{a+bx}} dx$$

Optimal. Leaf size=172

$$\frac{(bc - ad) \log(c + dx)}{6b^{4/3}d^{2/3}} - \frac{(bc - ad) \log\left(\frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}} - 1\right)}{2b^{4/3}d^{2/3}} - \frac{(bc - ad) \tan^{-1}\left(\frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{\sqrt{3} b^{4/3}d^{2/3}} + \frac{(a + bx)^{2/3} \sqrt[3]{c + dx}}{b}$$

[Out] (b*x+a)^(2/3)*(d*x+c)^(1/3)/b-1/6*(-a*d+b*c)*ln(d*x+c)/b^(4/3)/d^(2/3)-1/2*(-a*d+b*c)*ln(-1+d^(1/3)*(b*x+a)^(1/3)/b^(1/3)/(d*x+c)^(1/3))/b^(4/3)/d^(2/3)-1/3*(-a*d+b*c)*arctan(1/3*3^(1/2)+2/3*d^(1/3)*(b*x+a)^(1/3)/b^(1/3)/(d*x+c)^(1/3)*3^(1/2))/b^(4/3)/d^(2/3)*3^(1/2)

Rubi [A] time = 0.05, antiderivative size = 172, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {50, 59}

$$\frac{(bc - ad) \log(c + dx)}{6b^{4/3}d^{2/3}} - \frac{(bc - ad) \log\left(\frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}} - 1\right)}{2b^{4/3}d^{2/3}} - \frac{(bc - ad) \tan^{-1}\left(\frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{\sqrt{3} b^{4/3}d^{2/3}} + \frac{(a + bx)^{2/3} \sqrt[3]{c + dx}}{b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/3)/(a + b*x)^(1/3), x]

[Out] ((a + b*x)^(2/3)*(c + d*x)^(1/3))/b - ((b*c - a*d)*ArcTan[1/Sqrt[3] + (2*d^(1/3)*(a + b*x)^(1/3))/(Sqrt[3]*b^(1/3)*(c + d*x)^(1/3))]/(Sqrt[3]*b^(4/3)*d^(2/3)) - ((b*c - a*d)*Log[c + d*x])/(6*b^(4/3)*d^(2/3)) - ((b*c - a*d)*Log[-1 + (d^(1/3)*(a + b*x)^(1/3))/(b^(1/3)*(c + d*x)^(1/3))]/(2*b^(4/3)*d^(2/3))

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 59

Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt

```
[3]*(c + d*x)^(1/3) + 1/Sqrt[3]]/d, x] + (-Simp[(3*q*Log[(q*(a + b*x)^(1/3))]/(c + d*x)^(1/3) - 1)/(2*d), x] - Simp[(q*Log[c + d*x])/(2*d), x]]) /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]
```

Rubi steps

$$\int \frac{\sqrt[3]{c+dx}}{\sqrt[3]{a+bx}} dx = \frac{(a+bx)^{2/3} \sqrt[3]{c+dx}}{b} + \frac{(bc-ad) \int \frac{1}{\sqrt[3]{a+bx} (c+dx)^{2/3}} dx}{3b}$$

$$= \frac{(a+bx)^{2/3} \sqrt[3]{c+dx}}{b} - \frac{(bc-ad) \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}}\right)}{\sqrt{3} b^{4/3} d^{2/3}} - \frac{(bc-ad) \log(c+dx)}{6b^{4/3} d^{2/3}} - \frac{(bc-ad)}{6b^{4/3} d^{2/3}}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.42

$$\frac{3(a+bx)^{2/3} \sqrt[3]{c+dx} {}_2F_1\left(-\frac{1}{3}, \frac{2}{3}; \frac{5}{3}; \frac{d(a+bx)}{ad-bc}\right)}{2b \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(1/3), x]
```

```
[Out] (3*(a + b*x)^(2/3)*(c + d*x)^(1/3)*Hypergeometric2F1[-1/3, 2/3, 5/3, (d*(a + b*x))/(-(b*c) + a*d)]/(2*b*((b*(c + d*x))/(b*c - a*d))^(1/3))
```

fricas [B] time = 0.51, size = 596, normalized size = 3.47

$$\frac{6(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{1}{3}}bd^2 - 3\sqrt{\frac{1}{3}}(b^2cd - abd^2)\sqrt{-\frac{(bd^2)^{\frac{1}{3}}}{b}} \log\left(-3bd^2x - 2bcd - ad^2 + 3(bd^2)^{\frac{1}{3}}(bx+a)^{\frac{2}{3}}(dx+c)\right)}{1}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(1/3)/(b*x+a)^(1/3), x, algorithm="fricas")
```

```
[Out] [1/6*(6*(b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d^2 - 3*sqrt(1/3)*(b^2*c*d - a*b*d^2)*sqrt(-(b*d^2)^(1/3)/b)*log(-3*b*d^2*x - 2*b*c*d - a*d^2 + 3*(b*d^2)^(1/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3)*d + 3*sqrt(1/3)*(2*(b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (b*d^2)^(1/3)*(b*d*x + a*d))*sqrt(-(b*d^2)^(1/3)/b)) - 2*(b*d^2)^(2/3)*(b*c - a*d)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (b*d^2)^(2/3)*(b*x + a))/(b*x + a)) + (b*d^2)^(2/3)*(b*c - a*d)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d + (b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) + (b*d^2)^(1/3)*(b*d*x + a*d))/(b*x + a)))/(b^2*d^2), 1/6*(6*(b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d^2 + 6*sqrt(1/3)*(b^2*c*d - a*b*d^2)*sqrt((b*d^2)^(1/3)/b)*arctan(sqrt(1/3)*(2*(b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) + (b*d^2)^(1/3)*(b*d*x + a*d))*sqrt((b*d^2)^(1/3)/b)/(b*d^2*x + a*d^2)) - 2*(b*d^2)^(2/3)*(b*c - a*d)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (b*d^2)^(2/3)*(b*x + a))/(b*x + a)) + (b*d^2)^(2/3)*(b*c - a*d)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d + (b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) + (b*d^2)^(1/3)*(b*d*x + a*d))/(b*x + a)))/(b^2*d^2)]
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(1/3)/(b*x+a)^(1/3),x, algorithm="giac")
```

```
[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(1/3), x)
```

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^(1/3)/(b*x+a)^(1/3),x)
```

```
[Out] int((d*x+c)^(1/3)/(b*x+a)^(1/3),x)
```

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(1/3),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{1/3}}{(a + bx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/3)/(a + b*x)^(1/3), x)

[Out] int((c + d*x)^(1/3)/(a + b*x)^(1/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{c + dx}}{\sqrt[3]{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/3)/(b*x+a)**(1/3), x)

[Out] Integral((c + d*x)**(1/3)/(a + b*x)**(1/3), x)

$$3.1577 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{4/3}} dx$$

Optimal. Leaf size=149

$$\frac{3\sqrt[3]{d} \log\left(\frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}} - 1\right)}{2b^{4/3}} - \frac{\sqrt{3} \sqrt[3]{d} \tan^{-1}\left(\frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{b^{4/3}} - \frac{3\sqrt[3]{c+dx}}{b\sqrt[3]{a+bx}} - \frac{\sqrt[3]{d} \log(c+dx)}{2b^{4/3}}$$

[Out] $-3*(d*x+c)^{(1/3)}/b/(b*x+a)^{(1/3)}-1/2*d^{(1/3)}*\ln(d*x+c)/b^{(4/3)}-3/2*d^{(1/3)}*\ln(-1+d^{(1/3)}*(b*x+a)^{(1/3)}/b^{(1/3)}/(d*x+c)^{(1/3)})/b^{(4/3)}-d^{(1/3)}*\arctan(1/3*3^{(1/2)}+2/3*d^{(1/3)}*(b*x+a)^{(1/3)}/b^{(1/3)}/(d*x+c)^{(1/3)}*3^{(1/2)})/b^{(4/3)}$

Rubi [A] time = 0.03, antiderivative size = 149, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {47, 59}

$$\frac{3\sqrt[3]{d} \log\left(\frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}} - 1\right)}{2b^{4/3}} - \frac{\sqrt{3} \sqrt[3]{d} \tan^{-1}\left(\frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{b^{4/3}} - \frac{3\sqrt[3]{c+dx}}{b\sqrt[3]{a+bx}} - \frac{\sqrt[3]{d} \log(c+dx)}{2b^{4/3}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/3)/(a + b*x)^(4/3), x]

[Out] $(-3*(c + d*x)^{(1/3)})/(b*(a + b*x)^{(1/3)}) - (\text{Sqrt}[3]*d^{(1/3)}*\text{ArcTan}[1/\text{Sqrt}[3] + (2*d^{(1/3)}*(a + b*x)^{(1/3)})/(\text{Sqrt}[3]*b^{(1/3)}*(c + d*x)^{(1/3)})])/b^{(4/3)} - (d^{(1/3)}*\text{Log}[c + d*x])/(2*b^{(4/3)}) - (3*d^{(1/3)}*\text{Log}[-1 + (d^{(1/3)}*(a + b*x)^{(1/3)})/b^{(1/3)}*(c + d*x)^{(1/3)}])/b^{(4/3)})/(2*b^{(4/3)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 59

Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt[3]*(c + d*x)^(1/3)) + 1/Sqrt[3]])/d, x] + (-Simp[(3*q*Log[(q*(a + b*x)^(1/3) + 1/Sqrt[3])])]/d, x)]

3))/(c + d*x)^(1/3) - 1)/(2*d), x] - Simp[(q*Log[c + d*x])/(2*d), x]] /;
FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]

Rubi steps

$$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{4/3}} dx = -\frac{3\sqrt[3]{c+dx}}{b\sqrt[3]{a+bx}} + \frac{d \int \frac{1}{\sqrt[3]{a+bx}(c+dx)^{2/3}} dx}{b}$$

$$= -\frac{3\sqrt[3]{c+dx}}{b\sqrt[3]{a+bx}} - \frac{\sqrt{3} \sqrt[3]{d} \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}}\right)}{b^{4/3}} - \frac{\sqrt[3]{d} \log(c+dx)}{2b^{4/3}} - \frac{3\sqrt[3]{d} \log\left(-1 + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}}\right)}{2b^{4/3}}$$

Mathematica [C] time = 0.03, size = 71, normalized size = 0.48

$$\frac{3\sqrt[3]{c+dx} {}_2F_1\left(-\frac{1}{3}, -\frac{1}{3}, \frac{2}{3}, \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[3]{a+bx} \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(4/3), x]

[Out] (-3*(c + d*x)^(1/3)*Hypergeometric2F1[-1/3, -1/3, 2/3, (d*(a + b*x))/(-b*c + a*d)]/(b*(a + b*x)^(1/3)*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [B] time = 0.44, size = 233, normalized size = 1.56

$$\frac{2\sqrt{3}(bx+a)\left(-\frac{d}{b}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{1}{3}}b\left(-\frac{d}{b}\right)^{\frac{2}{3}} + \sqrt{3}(bdx+ad)}{3(bdx+ad)}\right) + (bx+a)\left(-\frac{d}{b}\right)^{\frac{1}{3}} \log\left(\frac{(bx+a)\left(-\frac{d}{b}\right)^{\frac{2}{3}} - (bx+a)^{\frac{2}{3}}(dx+c)^{\frac{1}{3}}}{bx+a}\right)}{2(b^2x+ab)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(4/3), x, algorithm="fricas")

[Out] -1/2*(2*sqrt(3)*(b*x + a)*(-d/b)^(1/3)*arctan(1/3*(2*sqrt(3)*(b*x + a)^(2/3)*(d*x + c)^(1/3)*b*(-d/b)^(2/3) + sqrt(3)*(b*d*x + a*d))/(b*d*x + a*d)) + (b*x + a)*(-d/b)^(1/3)*log(((b*x + a)*(-d/b)^(2/3) - (b*x + a)^(2/3)*(d*x + c)^(1/3)*(-d/b)^(1/3) + (b*x + a)^(1/3)*(d*x + c)^(2/3))/(b*x + a)) - 2*(b

$*x + a)*(-d/b)^{(1/3)}*\log(((b*x + a)*(-d/b)^{(1/3)} + (b*x + a)^{(2/3)}*(d*x + c)^{(1/3)))/(b*x + a)) + 6*(b*x + a)^{(2/3)}*(d*x + c)^{(1/3))/(b^2*x + a*b)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(4/3),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(4/3), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(4/3),x)

[Out] int((d*x+c)^(1/3)/(b*x+a)^(4/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(4/3),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(4/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{1/3}}{(a + bx)^{4/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/3)/(a + b*x)^(4/3),x)

```
[Out] int((c + d*x)^(1/3)/(a + b*x)^(4/3), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{\sqrt[3]{c + dx}}{(a + bx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(1/3)/(b*x+a)**(4/3),x)
```

```
[Out] Integral((c + d*x)**(1/3)/(a + b*x)**(4/3), x)
```

$$3.1578 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{7/3}} dx$$

Optimal. Leaf size=32

$$-\frac{3(c+dx)^{4/3}}{4(a+bx)^{4/3}(bc-ad)}$$

[Out] $-3/4*(d*x+c)^{(4/3)/(-a*d+b*c)/(b*x+a)^{(4/3)}$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{3(c+dx)^{4/3}}{4(a+bx)^{4/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c+d*x)^{(1/3)/(a+b*x)^{(7/3)}, x]$

[Out] $(-3*(c+d*x)^{(4/3))/(4*(b*c-a*d)*(a+b*x)^{(4/3)})$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)]/((b*c - a*d)*(m+1)), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{7/3}} dx = -\frac{3(c+dx)^{4/3}}{4(bc-ad)(a+bx)^{4/3}}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 1.00

$$-\frac{3(c+dx)^{4/3}}{4(a+bx)^{4/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(c+d*x)^{(1/3)/(a+b*x)^{(7/3)}, x]$

[Out] $(-3*(c+d*x)^{(4/3))/(4*(b*c-a*d)*(a+b*x)^{(4/3)})$

fricas [B] time = 0.42, size = 65, normalized size = 2.03

$$\frac{3 (bx + a)^{\frac{2}{3}} (dx + c)^{\frac{4}{3}}}{4 (a^2bc - a^3d + (b^3c - ab^2d)x^2 + 2 (ab^2c - a^2bd)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(7/3),x, algorithm="fricas")

[Out] -3/4*(b*x + a)^(2/3)*(d*x + c)^(4/3)/(a^2*b*c - a^3*d + (b^3*c - a*b^2*d)*x^2 + 2*(a*b^2*c - a^2*b*d)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{7}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(7/3),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(7/3), x)

maple [A] time = 0.00, size = 27, normalized size = 0.84

$$\frac{3 (dx + c)^{\frac{4}{3}}}{4 (bx + a)^{\frac{4}{3}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(7/3),x)

[Out] 3/4/(b*x+a)^(4/3)*(d*x+c)^(4/3)/(a*d-b*c)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{7}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(7/3),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(7/3), x)

mupad [B] time = 0.71, size = 92, normalized size = 2.88

$$\frac{\left(\frac{3c}{4b^2c-4abd} + \frac{3dx}{4b^2c-4abd}\right)(c+dx)^{1/3}}{x(a+bx)^{1/3} - \frac{(4a^2d-4abc)(a+bx)^{1/3}}{4b^2c-4abd}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(1/3)/(a + b*x)^(7/3), x)`

[Out] `-(((3*c)/(4*b^2*c - 4*a*b*d) + (3*d*x)/(4*b^2*c - 4*a*b*d))*(c + d*x)^(1/3))/(x*(a + b*x)^(1/3) - ((4*a^2*d - 4*a*b*c)*(a + b*x)^(1/3))/(4*b^2*c - 4*a*b*d))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{\frac{7}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(1/3)/(b*x+a)**(7/3), x)`

[Out] `Integral((c + d*x)**(1/3)/(a + b*x)**(7/3), x)`

$$3.1579 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{10/3}} dx$$

Optimal. Leaf size=66

$$\frac{9d(c+dx)^{4/3}}{28(a+bx)^{4/3}(bc-ad)^2} - \frac{3(c+dx)^{4/3}}{7(a+bx)^{7/3}(bc-ad)}$$

[Out] $-3/7*(d*x+c)^{(4/3)/(-a*d+b*c)/(b*x+a)^{(7/3)+9/28*d*(d*x+c)^{(4/3)/(-a*d+b*c)^2/(b*x+a)^{(4/3)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{9d(c+dx)^{4/3}}{28(a+bx)^{4/3}(bc-ad)^2} - \frac{3(c+dx)^{4/3}}{7(a+bx)^{7/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/3)/(a + b*x)^(10/3), x]

[Out] $(-3*(c + d*x)^{(4/3))/(7*(b*c - a*d)*(a + b*x)^{(7/3)}) + (9*d*(c + d*x)^{(4/3)})/(28*(b*c - a*d)^2*(a + b*x)^{(4/3)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{10/3}} dx = -\frac{3(c+dx)^{4/3}}{7(bc-ad)(a+bx)^{7/3}} - \frac{(3d) \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{7/3}} dx}{7(bc-ad)}$$

$$= -\frac{3(c+dx)^{4/3}}{7(bc-ad)(a+bx)^{7/3}} + \frac{9d(c+dx)^{4/3}}{28(bc-ad)^2(a+bx)^{4/3}}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.70

$$\frac{3(c+dx)^{4/3}(7ad-4bc+3bdx)}{28(a+bx)^{7/3}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(10/3), x]

[Out] (3*(c + d*x)^(4/3)*(-4*b*c + 7*a*d + 3*b*d*x))/(28*(b*c - a*d)^2*(a + b*x)^(7/3))

fricas [B] time = 0.42, size = 175, normalized size = 2.65

$$\frac{3(3bd^2x^2 - 4bc^2 + 7acd - (bcd - 7ad^2)x)(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{1}{3}}}{28(a^3b^2c^2 - 2a^4bcd + a^5d^2 + (b^5c^2 - 2ab^4cd + a^2b^3d^2)x^3 + 3(ab^4c^2 - 2a^2b^3cd + a^3b^2d^2)x^2 + 3(a^2b^3c^2 - 2a^3b^2cd + a^4b^2d^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(10/3), x, algorithm="fricas")

[Out] 3/28*(3*b*d^2*x^2 - 4*b*c^2 + 7*a*c*d - (b*c*d - 7*a*d^2)*x)*(b*x + a)^(2/3)*(d*x + c)^(1/3)/(a^3*b^2*c^2 - 2*a^4*b*c*d + a^5*d^2 + (b^5*c^2 - 2*a*b^4*c*d + a^2*b^3*d^2)*x^3 + 3*(a*b^4*c^2 - 2*a^2*b^3*c*d + a^3*b^2*d^2)*x^2 + 3*(a^2*b^3*c^2 - 2*a^3*b^2*c*d + a^4*b*d^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{10}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(10/3), x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(10/3), x)

maple [A] time = 0.01, size = 54, normalized size = 0.82

$$\frac{3(dx+c)^{\frac{4}{3}}(3bdx+7ad-4bc)}{28(bx+a)^{\frac{7}{3}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(10/3),x)

[Out] 3/28*(d*x+c)^(4/3)*(3*b*d*x+7*a*d-4*b*c)/(b*x+a)^(7/3)/(a^2*d^2-2*a*b*c*d+b^2*c^2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{3}}}{(bx+a)^{\frac{10}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(10/3),x, algorithm="maxima")

[Out] integrate((d*x+c)^(1/3)/(b*x+a)^(10/3),x)

mupad [B] time = 1.03, size = 127, normalized size = 1.92

$$\frac{(c+dx)^{1/3} \left(\frac{x(21ad^2-3bcd)}{28b^2(ad-bc)^2} - \frac{12bc^2-21acd}{28b^2(ad-bc)^2} + \frac{9d^2x^2}{28b(ad-bc)^2} \right)}{x^2(a+bx)^{1/3} + \frac{a^2(a+bx)^{1/3}}{b^2} + \frac{2ax(a+bx)^{1/3}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c+d*x)^(1/3)/(a+b*x)^(10/3),x)

[Out] ((c+d*x)^(1/3)*((x*(21*a*d^2-3*b*c*d))/(28*b^2*(a*d-b*c)^2)-(12*b*c^2-21*a*c*d)/(28*b^2*(a*d-b*c)^2)+(9*d^2*x^2)/(28*b*(a*d-b*c)^2)))/(x^2*(a+b*x)^(1/3)+(a^2*(a+b*x)^(1/3))/b^2+(2*a*x*(a+b*x)^(1/3))/b)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{\frac{10}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(1/3)/(b*x+a)**(10/3),x)
```

```
[Out] Integral((c + d*x)**(1/3)/(a + b*x)**(10/3), x)
```

$$3.1580 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{13/3}} dx$$

Optimal. Leaf size=101

$$-\frac{27d^2(c+dx)^{4/3}}{140(a+bx)^{4/3}(bc-ad)^3} + \frac{9d(c+dx)^{4/3}}{35(a+bx)^{7/3}(bc-ad)^2} - \frac{3(c+dx)^{4/3}}{10(a+bx)^{10/3}(bc-ad)}$$

[Out] $-3/10*(d*x+c)^{(4/3)/(-a*d+b*c)/(b*x+a)^{(10/3)+9/35*d*(d*x+c)^{(4/3)/(-a*d+b*c)^2/(b*x+a)^{(7/3)-27/140*d^2*(d*x+c)^{(4/3)/(-a*d+b*c)^3/(b*x+a)^{(4/3)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{27d^2(c+dx)^{4/3}}{140(a+bx)^{4/3}(bc-ad)^3} + \frac{9d(c+dx)^{4/3}}{35(a+bx)^{7/3}(bc-ad)^2} - \frac{3(c+dx)^{4/3}}{10(a+bx)^{10/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/3)/(a + b*x)^(13/3), x]

[Out] $(-3*(c+d*x)^{(4/3)}/(10*(b*c-a*d)*(a+b*x)^{(10/3)}) + (9*d*(c+d*x)^{(4/3)})/(35*(b*c-a*d)^2*(a+b*x)^{(7/3)}) - (27*d^2*(c+d*x)^{(4/3)})/(140*(b*c-a*d)^3*(a+b*x)^{(4/3)})$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{13/3}} dx &= -\frac{3(c+dx)^{4/3}}{10(bc-ad)(a+bx)^{10/3}} - \frac{(3d) \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{10/3}} dx}{5(bc-ad)} \\
&= -\frac{3(c+dx)^{4/3}}{10(bc-ad)(a+bx)^{10/3}} + \frac{9d(c+dx)^{4/3}}{35(bc-ad)^2(a+bx)^{7/3}} + \frac{(9d^2) \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{7/3}} dx}{35(bc-ad)^2} \\
&= -\frac{3(c+dx)^{4/3}}{10(bc-ad)(a+bx)^{10/3}} + \frac{9d(c+dx)^{4/3}}{35(bc-ad)^2(a+bx)^{7/3}} - \frac{27d^2(c+dx)^{4/3}}{140(bc-ad)^3(a+bx)^{4/3}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 77, normalized size = 0.76

$$\frac{3(c+dx)^{4/3} (35a^2d^2 + 10abd(3dx-4c) + b^2(14c^2 - 12cdx + 9d^2x^2))}{140(a+bx)^{10/3}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(13/3), x]

[Out] (-3*(c + d*x)^(4/3)*(35*a^2*d^2 + 10*a*b*d*(-4*c + 3*d*x) + b^2*(14*c^2 - 12*c*d*x + 9*d^2*x^2)))/(140*(b*c - a*d)^(3*(a + b*x)^(10/3)))

fricas [B] time = 0.44, size = 337, normalized size = 3.34

$$\frac{3(9b^2d^3x^3 + 14b^2c^3 - 40abc^2d + 35a^2cd^2 - 3(b^2cd^2 - 140(a^4b^3c^3 - 3a^5b^2c^2d + 3a^6bcd^2 - a^7d^3 + (b^7c^3 - 3ab^6c^2d + 3a^2b^5cd^2 - a^3b^4d^3))x^4 + 4(ab^6c^3 - 3a^2b^5c^2d + 3a^3b^4c^2d^2 - 3a^4b^3c^2d^3 + 3a^5b^2c^2d^3 - 3a^6b^2c^2d^3 + 3a^7b^2c^2d^3)x^3 + 6(a^2b^5c^3 - 3a^3b^4c^2d + 3a^4b^3c^2d^2 - a^5b^2c^2d^3)x^2 + 4(a^3b^4c^3 - 3a^4b^3c^2d + 3a^5b^2c^2d^2 - a^6b^2c^2d^3)x)}{140(a^4b^3c^3 - 3a^5b^2c^2d + 3a^6bcd^2 - a^7d^3 + (b^7c^3 - 3ab^6c^2d + 3a^2b^5cd^2 - a^3b^4d^3))x^4 + 4(ab^6c^3 - 3a^2b^5c^2d + 3a^3b^4c^2d^2 - 3a^4b^3c^2d^3 + 3a^5b^2c^2d^3 - 3a^6b^2c^2d^3 + 3a^7b^2c^2d^3)x^3 + 6(a^2b^5c^3 - 3a^3b^4c^2d + 3a^4b^3c^2d^2 - a^5b^2c^2d^3)x^2 + 4(a^3b^4c^3 - 3a^4b^3c^2d + 3a^5b^2c^2d^2 - a^6b^2c^2d^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(13/3), x, algorithm="fricas")

[Out] -3/140*(9*b^2*d^3*x^3 + 14*b^2*c^3 - 40*a*b*c^2*d + 35*a^2*c*d^2 - 3*(b^2*c*d^2 - 10*a*b*d^3)*x^2 + (2*b^2*c^2*d - 10*a*b*c*d^2 + 35*a^2*d^3)*x)*(b*x + a)^(2/3)*(d*x + c)^(1/3)/(a^4*b^3*c^3 - 3*a^5*b^2*c^2*d + 3*a^6*b*c*d^2 - a^7*d^3 + (b^7*c^3 - 3*a*b^6*c^2*d + 3*a^2*b^5*c*d^2 - a^3*b^4*d^3)*x^4 + 4*(a*b^6*c^3 - 3*a^2*b^5*c^2*d + 3*a^3*b^4*c*d^2 - a^4*b^3*d^3)*x^3 + 6*(a^2*b^5*c^3 - 3*a^3*b^4*c^2*d + 3*a^4*b^3*c*d^2 - a^5*b^2*d^3)*x^2 + 4*(a^3*b^4*c^3 - 3*a^4*b^3*c^2*d + 3*a^5*b^2*c*d^2 - a^6*b*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{3}}}{(bx+a)^{\frac{13}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(13/3),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(13/3), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{3(dx+c)^{\frac{4}{3}}(9b^2x^2d^2+30abd^2x-12b^2cdx+35a^2d^2-40abcd+14b^2c^2)}{140(bx+a)^{\frac{10}{3}}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(13/3),x)

[Out] 3/140*(d*x+c)^(4/3)*(9*b^2*d^2*x^2+30*a*b*d^2*x-12*b^2*c*d*x+35*a^2*d^2-40*a*b*c*d+14*b^2*c^2)/(b*x+a)^(10/3)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{3}}}{(bx+a)^{\frac{13}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(13/3),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(13/3), x)

mupad [B] time = 1.02, size = 203, normalized size = 2.01

$$\frac{(c+dx)^{1/3} \left(\frac{105a^2cd^2-120abc^2d+42b^2c^3}{140b^3(ad-bc)^3} + \frac{x(105a^2d^3-30abc^2d+6b^2c^2d)}{140b^3(ad-bc)^3} + \frac{27d^3x^3}{140b(ad-bc)^3} + \frac{9d^2x^2(10ad-bc)}{140b^2(ad-bc)^3} \right)}{x^3(a+bx)^{1/3} + \frac{a^3(a+bx)^{1/3}}{b^3} + \frac{3ax^2(a+bx)^{1/3}}{b} + \frac{3a^2x(a+bx)^{1/3}}{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c+d*x)^(1/3)/(a+b*x)^(13/3),x)

[Out] ((c+d*x)^(1/3)*((42*b^2*c^3+105*a^2*c*d^2-120*a*b*c^2*d)/(140*b^3*(a*d-b*c)^3)+x*(105*a^2*d^3+6*b^2*c^2*d-30*a*b*c*d^2)/(140*b^3*(a*d-b*c)^3)+(27*d^3*x^3)/(140*b*(a*d-b*c)^3)+(9*d^2*x^2*(10*a*d-b*c)/(140*b^2*(a*d-b*c)^3)))/(x^3*(a+b*x)^(1/3)+(a^3*(a+b*x)^(1/3))/b^3+(3*a*x^2*(a+b*x)^(1/3))/b+(3*a^2*x*(a+b*x)^(1/3))/b^2)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/3)/(b*x+a)**(13/3),x)

[Out] Timed out

$$3.1581 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{16/3}} dx$$

Optimal. Leaf size=136

$$\frac{243d^3(c+dx)^{4/3}}{1820(a+bx)^{4/3}(bc-ad)^4} - \frac{81d^2(c+dx)^{4/3}}{455(a+bx)^{7/3}(bc-ad)^3} + \frac{27d(c+dx)^{4/3}}{130(a+bx)^{10/3}(bc-ad)^2} - \frac{3(c+dx)^{4/3}}{13(a+bx)^{13/3}(bc-ad)}$$

[Out] $-3/13*(d*x+c)^{(4/3)/(-a*d+b*c)/(b*x+a)^{(13/3)+27/130*d*(d*x+c)^{(4/3)/(-a*d+b*c)^2/(b*x+a)^{(10/3)-81/455*d^2*(d*x+c)^{(4/3)/(-a*d+b*c)^3/(b*x+a)^{(7/3)+43/1820*d^3*(d*x+c)^{(4/3)/(-a*d+b*c)^4/(b*x+a)^{(4/3)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{243d^3(c+dx)^{4/3}}{1820(a+bx)^{4/3}(bc-ad)^4} - \frac{81d^2(c+dx)^{4/3}}{455(a+bx)^{7/3}(bc-ad)^3} + \frac{27d(c+dx)^{4/3}}{130(a+bx)^{10/3}(bc-ad)^2} - \frac{3(c+dx)^{4/3}}{13(a+bx)^{13/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/3)/(a + b*x)^(16/3), x]

[Out] $(-3*(c+d*x)^{(4/3)/((13*(b*c-a*d)*(a+b*x)^{(13/3))+(27*d*(c+d*x)^{(4/3)/((130*(b*c-a*d)^2*(a+b*x)^{(10/3))-(81*d^2*(c+d*x)^{(4/3)/((455*(b*c-a*d)^3*(a+b*x)^{(7/3))+(243*d^3*(c+d*x)^{(4/3)/((1820*(b*c-a*d)^4*(a+b*x)^{(4/3))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{16/3}} dx &= -\frac{3(c+dx)^{4/3}}{13(bc-ad)(a+bx)^{13/3}} - \frac{(9d) \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{13/3}} dx}{13(bc-ad)} \\
&= -\frac{3(c+dx)^{4/3}}{13(bc-ad)(a+bx)^{13/3}} + \frac{27d(c+dx)^{4/3}}{130(bc-ad)^2(a+bx)^{10/3}} + \frac{(27d^2) \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{10/3}} dx}{65(bc-ad)^2} \\
&= -\frac{3(c+dx)^{4/3}}{13(bc-ad)(a+bx)^{13/3}} + \frac{27d(c+dx)^{4/3}}{130(bc-ad)^2(a+bx)^{10/3}} - \frac{81d^2(c+dx)^{4/3}}{455(bc-ad)^3(a+bx)^{7/3}} - \frac{(81d^3) \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{7/3}} dx}{455(bc-ad)^3} \\
&= -\frac{3(c+dx)^{4/3}}{13(bc-ad)(a+bx)^{13/3}} + \frac{27d(c+dx)^{4/3}}{130(bc-ad)^2(a+bx)^{10/3}} - \frac{81d^2(c+dx)^{4/3}}{455(bc-ad)^3(a+bx)^{7/3}} + \frac{243d^3(c+dx)^{4/3}}{1820(bc-ad)^4}
\end{aligned}$$

Mathematica [A] time = 0.06, size = 118, normalized size = 0.87

$$\frac{3(c+dx)^{4/3} (455a^3d^3 + 195a^2bd^2(3dx-4c) + 39ab^2d(14c^2-12cdx+9d^2x^2) + b^3(-140c^3+126c^2dx-108cd^2x^2+81d^3x^3))}{1820(a+bx)^{13/3}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(16/3), x]

[Out] (3*(c + d*x)^(4/3)*(455*a^3*d^3 + 195*a^2*b*d^2*(-4*c + 3*d*x) + 39*a*b^2*d*(14*c^2 - 12*c*d*x + 9*d^2*x^2) + b^3*(-140*c^3 + 126*c^2*d*x - 108*c*d^2*x^2 + 81*d^3*x^3)))/(1820*(b*c - a*d)^4*(a + b*x)^(13/3))

fricas [B] time = 0.44, size = 533, normalized size = 3.92

$$\frac{3(81b^3d^4x^4 - 140b^3c^4 + 546ab^2c^3d - 780a^2b^2c^2d^2 + 455a^3c^2d^3 - 27(b^3c^2d^3 - 13a^2b^2d^4)x^3 + 9(2b^3c^2d^2 - 13a^2b^2c^2d^3 + 65a^2b^2d^4)x^2 - (14b^3c^3d - 78a^2b^2c^2d^2 + 195a^2b^2c^2d^3 - 455a^3d^4)x)(b^3x^2 + a^2x + a^2)(d^2x + c)^{1/3}}{1820(a^5b^4c^4 - 4a^6b^3c^3d + 6a^7b^2c^2d^2 - 4a^8bcd^3 + a^9d^4 + (b^9c^4 - 4ab^8c^3d + 6a^2b^7c^2d^2 - 4a^3b^6cd^3 + a^4b^5d^4)x^2 + 5a^4b^5d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(16/3), x, algorithm="fricas")

[Out] 3/1820*(81*b^3*d^4*x^4 - 140*b^3*c^4 + 546*a*b^2*c^3*d - 780*a^2*b^2*c^2*d^2 + 455*a^3*c^2*d^3 - 27*(b^3*c^2*d^3 - 13*a^2*b^2*d^4)*x^3 + 9*(2*b^3*c^2*d^2 - 13*a^2*b^2*c^2*d^3 + 65*a^2*b^2*d^4)*x^2 - (14*b^3*c^3*d - 78*a^2*b^2*c^2*d^2 + 195*a^2*b^2*c^2*d^3 - 455*a^3*d^4)*x)*(b*x + a)^(2/3)*(d*x + c)^(1/3)/(a^5*b^4*c^4 - 4*a^6*b^3*c^3*d + 6*a^7*b^2*c^2*d^2 - 4*a^8*b*c*d^3 + a^9*d^4 + (b^9*c^4 - 4*a*b^8*c^3*d + 6*a^2*b^7*c^2*d^2 - 4*a^3*b^6*c*d^3 + a^4*b^5*d^4)*x^2 + 5*a^4*b^5*d^4)

$(a^5 b^8 c^4 - 4 a^2 b^7 c^3 d + 6 a^3 b^6 c^2 d^2 - 4 a^4 b^5 c d^3 + a^5 b^4 d^4) x^4 + 10 (a^2 b^7 c^4 - 4 a^3 b^6 c^3 d + 6 a^4 b^5 c^2 d^2 - 4 a^5 b^4 c d^3 + a^6 b^3 d^4) x^3 + 10 (a^3 b^6 c^4 - 4 a^4 b^5 c^3 d + 6 a^5 b^4 c^2 d^2 - 4 a^6 b^3 c d^3 + a^7 b^2 d^4) x^2 + 5 (a^4 b^5 c^4 - 4 a^5 b^4 c^3 d + 6 a^6 b^3 c^2 d^2 - 4 a^7 b^2 c d^3 + a^8 b d^4) x$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{16}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(16/3),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(16/3), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{3(dx + c)^{\frac{4}{3}} (81b^3 d^3 x^3 + 351a b^2 d^3 x^2 - 108b^3 c d^2 x^2 + 585a^2 b d^3 x - 468a b^2 c d^2 x + 126b^3 c^2 dx + 455a^3 d^3 - 780a^2 b^2 d^3)}{1820(bx + a)^{\frac{13}{3}} (a^4 d^4 - 4a^3 b c d^3 + 6a^2 b^2 c^2 d^2 - 4a b^3 c^3 d + b^4 c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(16/3),x)

[Out] 3/1820*(d*x+c)^(4/3)*(81*b^3*d^3*x^3+351*a*b^2*d^3*x^2-108*b^3*c*d^2*x^2+585*a^2*b*d^3*x-468*a*b^2*c*d^2*x+126*b^3*c^2*d*x+455*a^3*d^3-780*a^2*b*c*d^2+546*a*b^2*c^2*d-140*b^3*c^3)/(b*x+a)^(13/3)/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{16}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(16/3),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(16/3), x)

mupad [B] time = 1.15, size = 293, normalized size = 2.15

$$(c + dx)^{1/3} \left(\frac{243d^4x^4}{1820b(ad-bc)^4} - \frac{-1365a^3cd^3+2340a^2bc^2d^2-1638ab^2c^3d+420b^3c^4}{1820b^4(ad-bc)^4} + \frac{x(1365a^3d^4-585a^2bcd^3+234ab^2c^2d^2-42b^3c^3d)}{1820b^4(ad-bc)^4} \right)$$

$$x^4(a+bx)^{1/3} + \frac{a^4(a+bx)^{1/3}}{b^4} + \frac{6a^2x^2(a+bx)^{1/3}}{b^2} + \frac{4ax^3(a+bx)^{1/3}}{b} + \frac{4a^3x(a+bx)^{1/3}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/3)/(a + b*x)^(16/3), x)

[Out] ((c + d*x)^(1/3)*((243*d^4*x^4)/(1820*b*(a*d - b*c)^4) - (420*b^3*c^4 - 1365*a^3*c*d^3 + 2340*a^2*b*c^2*d^2 - 1638*a*b^2*c^3*d)/(1820*b^4*(a*d - b*c)^4) + (x*(1365*a^3*d^4 - 42*b^3*c^3*d + 234*a*b^2*c^2*d^2 - 585*a^2*b*c*d^3))/(1820*b^4*(a*d - b*c)^4) + (81*d^3*x^3*(13*a*d - b*c))/(1820*b^2*(a*d - b*c)^4) + (27*d^2*x^2*(65*a^2*d^2 + 2*b^2*c^2 - 13*a*b*c*d))/(1820*b^3*(a*d - b*c)^4))/((x^4*(a + b*x)^(1/3) + (a^4*(a + b*x)^(1/3))/b^4 + (6*a^2*x^2*(a + b*x)^(1/3))/b^2 + (4*a*x^3*(a + b*x)^(1/3))/b + (4*a^3*x*(a + b*x)^(1/3))/b^3))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/3)/(b*x+a)**(16/3), x)

[Out] Timed out

3.1582 $\int (a + bx)^{4/3} \sqrt[3]{c + dx} dx$

Optimal. Leaf size=655

$$3^{3/4} \sqrt{2 + \sqrt{3}} (bc - ad)^3 ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\dots}$$

$$10 \cdot 2^{2/3} b^{4/3} d^{7/3} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx)$$

[Out] $-3/20 * (-a*d+b*c)^2 * (b*x+a)^{(1/3)} * (d*x+c)^{(1/3)} / b/d^2 + 3/40 * (-a*d+b*c) * (b*x+a)^{(4/3)} * (d*x+c)^{(1/3)} / b/d + 3/8 * (b*x+a)^{(7/3)} * (d*x+c)^{(1/3)} / b + 1/20 * 3^{(3/4)} * (-a*d+b*c)^3 * ((b*x+a) * (d*x+c))^{(2/3)} * ((-a*d+b*c)^{(2/3)} + 2^{(2/3)} * b^{(1/3)} * d^{(1/3)}) * ((b*x+a) * (d*x+c))^{(1/3)} * \text{EllipticF}((2^{(2/3)} * b^{(1/3)} * d^{(1/3)} * ((b*x+a) * (d*x+c))^{(1/3)} + (-a*d+b*c)^{(2/3)} * (1-3^{(1/2)})) / (2^{(2/3)} * b^{(1/3)} * d^{(1/3)} * ((b*x+a) * (d*x+c))^{(1/3)} + (-a*d+b*c)^{(2/3)} * (1+3^{(1/2)})), I * 3^{(1/2)} + 2 * I) * ((2 * b * d * x + a * d + b * c)^2)^{(1/2)} * (1/2 * 6^{(1/2)} + 1/2 * 2^{(1/2)}) * (((-a*d+b*c)^{(4/3)} - 2^{(2/3)} * b^{(1/3)} * d^{(1/3)} * (-a*d+b*c)^{(2/3)} * ((b*x+a) * (d*x+c))^{(1/3)} + 2 * 2^{(1/3)} * b^{(2/3)} * d^{(2/3)} * ((b*x+a) * (d*x+c))^{(2/3)}) / (2^{(2/3)} * b^{(1/3)} * d^{(1/3)} * ((b*x+a) * (d*x+c))^{(1/3)} + (-a*d+b*c)^{(2/3)} * (1+3^{(1/2)}))^{(1/2)} * 2^{(1/3)} / b^{(4/3)} / d^{(7/3)} / (b*x+a)^{(2/3)} / (d*x+c)^{(2/3)} / (2 * b * d * x + a * d + b * c) / ((a*d+b*(2*d*x+c))^2)^{(1/2)} / ((-a*d+b*c)^{(2/3)} * ((-a*d+b*c)^{(2/3)} + 2^{(2/3)} * b^{(1/3)} * d^{(1/3)} * ((b*x+a) * (d*x+c))^{(1/3)}) / (2^{(2/3)} * b^{(1/3)} * d^{(1/3)} * ((b*x+a) * (d*x+c))^{(1/3)} + (-a*d+b*c)^{(2/3)} * (1+3^{(1/2)}))^{(1/2)}$

Rubi [A] time = 1.42, antiderivative size = 655, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 218}

$$3^{3/4} \sqrt{2 + \sqrt{3}} (bc - ad)^3 ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\dots}$$

$$10 \cdot 2^{2/3} b^{4/3} d^{7/3} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(4/3)} * (c + d*x)^{(1/3)}, x]$

[Out] $(-3 * (b*c - a*d)^2 * (a + b*x)^{(1/3)} * (c + d*x)^{(1/3)}) / (20 * b * d^2) + (3 * (b*c - a*d) * (a + b*x)^{(4/3)} * (c + d*x)^{(1/3)}) / (40 * b * d) + (3 * (a + b*x)^{(7/3)} * (c + d*x)^{(1/3)}) / (8 * b) + (3^{(3/4)} * \text{Sqrt}[2 + \text{Sqrt}[3]] * (b*c - a*d)^3 * ((a + b*x) * (c + d*x))^{(2/3)} * \text{Sqrt}[(b*c + a*d + 2 * b * d * x)^2] * ((b*c - a*d)^{(2/3)} + 2^{(2/3)} * b^{(1/3)} * d^{(1/3)} * ((a + b*x) * (c + d*x))^{(1/3)})) / (2 * 2^{(2/3)} * b^{(1/3)} * d^{(1/3)} * ((a + b*x) * (c + d*x))^{(1/3)} + (-a*d+b*c)^{(2/3)} * (1+3^{(1/2)}))^{(1/2)}$

$$3)d^{1/3}((a+bx)(c+dx))^{1/3} \sqrt{((b^3c - a^3d)^{4/3} - 2^{2/3}b^{1/3}d^{1/3}(b^3c - a^3d)^{2/3}((a+bx)(c+dx))^{1/3} + 2^{2/3}b^{2/3}d^{2/3}((a+bx)(c+dx))^{2/3}) / ((1 + \sqrt{3})(b^3c - a^3d)^{2/3} + 2^{2/3}b^{1/3}d^{1/3}((a+bx)(c+dx))^{1/3})^2} \text{EllipticF}[\text{ArcSin}[\frac{((1 - \sqrt{3})(b^3c - a^3d)^{2/3} + 2^{2/3}b^{1/3}d^{1/3}((a+bx)(c+dx))^{1/3})}{(1 + \sqrt{3})(b^3c - a^3d)^{2/3} + 2^{2/3}b^{1/3}d^{1/3}((a+bx)(c+dx))^{1/3}}], -7 - 4\sqrt{3}]] / (10 \cdot 2^{2/3}b^{4/3}d^{7/3}(a+bx)^{2/3}(c+dx)^{2/3}(b^3c + a^3d + 2b^2dx) \sqrt{((b^3c - a^3d)^{2/3} + 2^{2/3}b^{1/3}d^{1/3}((a+bx)(c+dx))^{1/3})} / ((1 + \sqrt{3})(b^3c - a^3d)^{2/3} + 2^{2/3}b^{1/3}d^{1/3}((a+bx)(c+dx))^{1/3})^2} \sqrt{(a^3d + b^3(c + 2dx))^2}$$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)]], -7 - 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x*d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int (a+bx)^{4/3} \sqrt[3]{c+dx} \, dx &= \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8b} + \frac{(bc-ad) \int \frac{(a+bx)^{4/3}}{(c+dx)^{2/3}} \, dx}{8b} \\
&= \frac{3(bc-ad)(a+bx)^{4/3} \sqrt[3]{c+dx}}{40bd} + \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8b} - \frac{(bc-ad)^2 \int \frac{\sqrt[3]{a+bx}}{(c+dx)^{2/3}} \, dx}{10bd} \\
&= -\frac{3(bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{20bd^2} + \frac{3(bc-ad)(a+bx)^{4/3} \sqrt[3]{c+dx}}{40bd} + \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8b} \\
&= -\frac{3(bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{20bd^2} + \frac{3(bc-ad)(a+bx)^{4/3} \sqrt[3]{c+dx}}{40bd} + \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8b} \\
&= -\frac{3(bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{20bd^2} + \frac{3(bc-ad)(a+bx)^{4/3} \sqrt[3]{c+dx}}{40bd} + \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8b} \\
&= -\frac{3(bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{20bd^2} + \frac{3(bc-ad)(a+bx)^{4/3} \sqrt[3]{c+dx}}{40bd} + \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8b}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.11

$$\frac{3(a+bx)^{7/3} \sqrt[3]{c+dx} {}_2F_1\left(-\frac{1}{3}, \frac{7}{3}; \frac{10}{3}; \frac{d(a+bx)}{ad-bc}\right)}{7b \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(4/3)*(c + d*x)^(1/3), x]

[Out] (3*(a + b*x)^(7/3)*(c + d*x)^(1/3)*Hypergeometric2F1[-1/3, 7/3, 10/3, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(\frac{bx+a}{3}\right)^{\frac{4}{3}}\left(\frac{dx+c}{3}\right)^{\frac{1}{3}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)*(d*x+c)^(1/3), x, algorithm="fricas")

[Out] `integral((b*x + a)^(4/3)*(d*x + c)^(1/3), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{4}{3}} (dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(4/3)*(d*x+c)^(1/3),x, algorithm="giac")`

[Out] `integrate((b*x + a)^(4/3)*(d*x + c)^(1/3), x)`

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{4}{3}} (dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(4/3)*(d*x+c)^(1/3),x)`

[Out] `int((b*x+a)^(4/3)*(d*x+c)^(1/3),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{4}{3}} (dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(4/3)*(d*x+c)^(1/3),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(4/3)*(d*x + c)^(1/3), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{\frac{4}{3}} (c + dx)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(4/3)*(c + d*x)^(1/3),x)`

[Out] `int((a + b*x)^(4/3)*(c + d*x)^(1/3), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{4}{3}} \sqrt[3]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(4/3)*(d*x+c)**(1/3),x)
```

```
[Out] Integral((a + b*x)**(4/3)*(c + d*x)**(1/3), x)
```


3.1583 $\int \sqrt[3]{a + bx} \sqrt[3]{c + dx} dx$

Optimal. Leaf size=617

$$3^{3/4} \sqrt{2 + \sqrt{3}} (bc - ad)^2 ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right)$$

$$5 \cdot 2^{2/3} b^{4/3} d^{4/3} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx)^{1/2}$$

[Out] $\frac{3}{10}(-a*d+b*c)*(b*x+a)^{(1/3)}*(d*x+c)^{(1/3)}/b/d+3/5*(b*x+a)^{(4/3)}*(d*x+c)^{(1/3)}/b-1/10*3^{(3/4)}*(-a*d+b*c)^2*((b*x+a)*(d*x+c))^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}+1/2*2^{(1/2)})*(((a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*2^{(1/3)}/b^{(4/3)}/d^{(4/3)}/(b*x+a)^{(2/3)}/(d*x+c)^{(2/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.85, antiderivative size = 617, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 218}

$$3^{3/4} \sqrt{2 + \sqrt{3}} (bc - ad)^2 ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right)$$

$$5 \cdot 2^{2/3} b^{4/3} d^{4/3} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx)^{1/2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/3)*(c + d*x)^(1/3), x]

[Out] $\frac{3*(b*c - a*d)*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)}}{(10*b*d)} + \frac{3*(a + b*x)^{(4/3)}*(c + d*x)^{(1/3)}}{(5*b)} - \frac{3^{(3/4)}*\text{Sqrt}[2 + \text{Sqrt}[3]]*(b*c - a*d)^2*((a + b*x)*(c + d*x))^{(2/3)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*\text{Sqrt}[(b*c - a*d)^{(4/3)} - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2$

$$\frac{2^{1/3} b^{2/3} d^{2/3} ((a + b x)(c + d x))^{2/3}}{((1 + \sqrt{3})(b c - a d))^{2/3} + 2^{2/3} b^{1/3} d^{1/3} ((a + b x)(c + d x))^{1/3}} \frac{\text{EllipticF}\left[\text{ArcSin}\left[\frac{(1 - \sqrt{3})(b c - a d)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} ((a + b x)(c + d x))^{1/3}}{(1 + \sqrt{3})(b c - a d)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} ((a + b x)(c + d x))^{1/3}}\right], -7 - 4\sqrt{3}\right]}{(5 \cdot 2^{2/3} b^{4/3} d^{4/3} (a + b x)^{2/3} (c + d x)^{2/3} (b c + a d + 2 b d x) \sqrt{(b c - a d)^{2/3} ((b c - a d)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} ((a + b x)(c + d x))^{1/3})})}{((1 + \sqrt{3})(b c - a d))^{2/3} + 2^{2/3} b^{1/3} d^{1/3} ((a + b x)(c + d x))^{1/3}} \sqrt{(a d + b(c + 2 d x))^2}$$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x*d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \sqrt[3]{a+bx} \sqrt[3]{c+dx} dx &= \frac{3(a+bx)^{4/3} \sqrt[3]{c+dx}}{5b} + \frac{(bc-ad) \int \frac{\sqrt[3]{a+bx}}{(c+dx)^{2/3}} dx}{5b} \\
&= \frac{3(bc-ad) \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{10bd} + \frac{3(a+bx)^{4/3} \sqrt[3]{c+dx}}{5b} - \frac{(bc-ad)^2 \int \frac{1}{(a+bx)^{2/3} (c+dx)^{2/3}} dx}{10bd} \\
&= \frac{3(bc-ad) \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{10bd} + \frac{3(a+bx)^{4/3} \sqrt[3]{c+dx}}{5b} - \frac{((bc-ad)^2 ((a+bx)(c+dx))^{2/3}}{10bd(a+bx)^{2/3}} \\
&= \frac{3(bc-ad) \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{10bd} + \frac{3(a+bx)^{4/3} \sqrt[3]{c+dx}}{5b} - \frac{(3(bc-ad)^2 ((a+bx)(c+dx))^2}{10bd(a+bx)^{2/3}} \\
&= \frac{3(bc-ad) \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{10bd} + \frac{3(a+bx)^{4/3} \sqrt[3]{c+dx}}{5b} - \frac{3^{3/4} \sqrt{2+\sqrt{3}} (bc-ad)^2 ((a+bx)(c+dx))^{2/3}}{10bd(a+bx)^{2/3}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.12

$$\frac{3(a+bx)^{4/3} \sqrt[3]{c+dx} {}_2F_1\left(-\frac{1}{3}, \frac{4}{3}; \frac{7}{3}; \frac{d(a+bx)}{ad-bc}\right)}{4b \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/3)*(c + d*x)^(1/3), x]

[Out] (3*(a + b*x)^(4/3)*(c + d*x)^(1/3)*Hypergeometric2F1[-1/3, 4/3, 7/3, (d*(a + b*x))/(-(b*c) + a*d)]/(4*b*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bx+a\right)^{\frac{1}{3}}\left(dx+c\right)^{\frac{1}{3}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)*(d*x+c)^(1/3), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/3)*(d*x + c)^(1/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{3}}(dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)*(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/3)*(d*x + c)^(1/3), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{3}}(dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/3)*(d*x+c)^(1/3),x)

[Out] int((b*x+a)^(1/3)*(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{3}}(dx + c)^{\frac{1}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)*(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/3)*(d*x + c)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{1/3} (c + dx)^{1/3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/3)*(c + d*x)^(1/3),x)

[Out] int((a + b*x)^(1/3)*(c + d*x)^(1/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt[3]{a + bx} \sqrt[3]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/3)*(d*x+c)**(1/3),x)

[Out] Integral((a + b*x)**(1/3)*(c + d*x)**(1/3), x)

$$3.1584 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{2/3}} dx$$

Optimal. Leaf size=576

$$3^{3/4} \sqrt{2 + \sqrt{3}} (bc - ad)((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\dots}$$

$$2^{2/3} b^{4/3} \sqrt[3]{d} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx)$$

[Out] $3/2*(b*x+a)^{(1/3)}*(d*x+c)^{(1/3)}/b+1/2*3^{(3/4)}*(-a*d+b*c)*((b*x+a)*(d*x+c))^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)}))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}+1/2*2^{(1/2)})*(((a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)}))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))^{(2/3)}*2^{(1/3)}/b^{(4/3)}/d^{(1/3)}/(b*x+a)^{(2/3)}/(d*x+c)^{(2/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*c*(2*d*x+c))^{(2/3)})/((-a*d+b*c)^{(2/3)}*((a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))^{(2/3)}*2^{(1/2)}$

Rubi [A] time = 0.56, antiderivative size = 576, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 218}

$$3^{3/4} \sqrt{2 + \sqrt{3}} (bc - ad)((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\dots}$$

$$2^{2/3} b^{4/3} \sqrt[3]{d} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx)$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/3)/(a + b*x)^(2/3), x]

[Out] $(3*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)})/(2*b) + (3^{(3/4)}*\text{Sqrt}[2 + \text{Sqrt}[3]])*(b*c - a*d)*((a + b*x)*(c + d*x))^{(2/3)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*\text{Sqrt}[(b*c - a*d)^{(4/3)} - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)}]/((1 + S$

$$\sqrt[3]{3} \cdot (b \cdot c - a \cdot d)^{2/3} + 2^{2/3} \cdot b^{1/3} \cdot d^{1/3} \cdot ((a + b \cdot x) \cdot (c + d \cdot x))^{1/3} \cdot \text{EllipticF}\left[\text{ArcSin}\left[\frac{(1 - \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{2/3} + 2^{2/3} \cdot b^{1/3} \cdot d^{1/3} \cdot ((a + b \cdot x) \cdot (c + d \cdot x))^{1/3}}{(1 + \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{2/3} + 2^{2/3} \cdot b^{1/3} \cdot d^{1/3} \cdot ((a + b \cdot x) \cdot (c + d \cdot x))^{1/3}}\right], -7 - 4\sqrt{3}\right] / (2^{2/3} \cdot b^{4/3} \cdot d^{1/3} \cdot (a + b \cdot x)^{2/3} \cdot (c + d \cdot x)^{2/3} \cdot (b \cdot c + a \cdot d + 2 \cdot b \cdot d \cdot x) \cdot \sqrt{((b \cdot c - a \cdot d)^{2/3} \cdot ((b \cdot c - a \cdot d)^{2/3} + 2^{2/3} \cdot b^{1/3} \cdot d^{1/3} \cdot ((a + b \cdot x) \cdot (c + d \cdot x))^{1/3})) / ((1 + \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{2/3} + 2^{2/3} \cdot b^{1/3} \cdot d^{1/3} \cdot ((a + b \cdot x) \cdot (c + d \cdot x))^{1/3})^2} \cdot \sqrt{(a \cdot d + b \cdot (c + 2 \cdot d \cdot x))^2}$$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*sqrt[2 + sqrt[3]]*(s + r*x)*sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - sqrt[3])*s
+ r*x)/((1 + sqrt[3])*s + r*x)], -7 - 4*sqrt[3]])/(3^(1/4)*r*sqrt[a + b*x^3
]*sqrt[(s*(s + r*x))/((1 + sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/sqrt[b^2 - 4*a*c + 4*c*x*d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{2/3}} dx &= \frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx}}{2b} + \frac{(bc-ad) \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{2b} \\
&= \frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx}}{2b} + \frac{\left((bc-ad)((a+bx)(c+dx))^{2/3}\right) \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{2/3}} dx}{2b(a+bx)^{2/3}(c+dx)^{2/3}} \\
&= \frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx}}{2b} + \frac{\left(3(bc-ad)((a+bx)(c+dx))^{2/3}\sqrt{(bc+ad+2bdx)^2}\right) \text{Subst}\left(\int \frac{1}{\sqrt{-4abcd}}\right)}{2b(a+bx)^{2/3}(c+dx)^{2/3}(bc+ad+2bdx)} \\
&= \frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx}}{2b} + \frac{3^{3/4}\sqrt{2+\sqrt{3}}(bc-ad)((a+bx)(c+dx))^{2/3}\sqrt{(bc+ad+2bdx)^2}}{2b(a+bx)^{2/3}(c+dx)^{2/3}(bc+ad+2bdx)}
\end{aligned}$$

 $2^{2/3}b^{4/3} \dots$

Mathematica [C] time = 0.03, size = 71, normalized size = 0.12

$$\frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx} {}_2F_1\left(-\frac{1}{3}, \frac{1}{3}; \frac{4}{3}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(2/3), x]

[Out] (3*(a + b*x)^(1/3)*(c + d*x)^(1/3)*Hypergeometric2F1[-1/3, 1/3, 4/3, (d*(a + b*x))/(-(b*c) + a*d)]/(b*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx+c)^{\frac{1}{3}}}{(bx+a)^{\frac{2}{3}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(2/3), x, algorithm="fricas")

[Out] integral((d*x + c)^(1/3)/(b*x + a)^(2/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(2/3),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(2/3), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(2/3),x)

[Out] int((d*x+c)^(1/3)/(b*x+a)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(2/3),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(2/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/3}}{(a + bx)^{2/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/3)/(a + b*x)^(2/3),x)

[Out] int((c + d*x)^(1/3)/(a + b*x)^(2/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{c + dx}}{(a + bx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/3)/(b*x+a)**(2/3), x)

[Out] Integral((c + d*x)**(1/3)/(a + b*x)**(2/3), x)

$$3.1585 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{5/3}} dx$$

Optimal. Leaf size=568

$$3^{3/4} \sqrt{2 + \sqrt{3}} d^{2/3} ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\frac{2 \sqrt[3]{2} b^{2/3}}{}}$$

$$\frac{2^{2/3} b^{4/3} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx)}{\sqrt{\frac{2 \sqrt[3]{2} b^{2/3}}{}}}$$

[Out] $-3/2*(d*x+c)^{(1/3)}/b/(b*x+a)^{(2/3)}+1/2*3^{(3/4)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)}))/((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}+1/2*2^{(1/2)})*(((a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*2^{(1/3)}/b^{(4/3)}/(b*x+a)^{(2/3)}/(d*x+c)^{(2/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.59, antiderivative size = 568, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 62, 623, 218}

$$3^{3/4} \sqrt{2 + \sqrt{3}} d^{2/3} ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\frac{2 \sqrt[3]{2} b^{2/3}}{}}$$

$$\frac{2^{2/3} b^{4/3} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx)}{\sqrt{\frac{(bc-ad)}{(2^{2/3} \sqrt[3]{2} b^{2/3})}}}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/3)/(a + b*x)^(5/3), x]

[Out] $(-3*(c + d*x)^{(1/3)})/(2*b*(a + b*x)^{(2/3)}) + (3^{(3/4)}*\text{Sqrt}[2 + \text{Sqrt}[3]])*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*\text{Sqrt}[(b*c - a*d)^{(4/3)} - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)})/((1 + \text{Sqrt}[3])^{(1/2)})$

$$\begin{aligned} & [3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)} \\ &)^2*EllipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d \\ & ^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})/((1 + Sqrt[3])*(b*c - a*d)^{(2/3)} + 2^{(2 \\ & /3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})], -7 - 4*Sqrt[3]]/(2^{(2/3)} \\ &)*b^{(4/3)}*(a + b*x)^{(2/3)}*(c + d*x)^{(2/3)}*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c \\ & - a*d)^{(2/3)}*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d \\ & *x))^{(1/3)})/((1 + Sqrt[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a \\ & + b*x)*(c + d*x))^{(1/3)})^2]*Sqrt[(a*d + b*(c + 2*d*x))^2] \end{aligned}$$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[3]{c+dx}}{(a+bx)^{5/3}} dx &= -\frac{3\sqrt[3]{c+dx}}{2b(a+bx)^{2/3}} + \frac{d \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{2b} \\
&= -\frac{3\sqrt[3]{c+dx}}{2b(a+bx)^{2/3}} + \frac{(d((a+bx)(c+dx))^{2/3}) \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{2/3}} dx}{2b(a+bx)^{2/3}(c+dx)^{2/3}} \\
&= -\frac{3\sqrt[3]{c+dx}}{2b(a+bx)^{2/3}} + \frac{(3d((a+bx)(c+dx))^{2/3} \sqrt{(bc+ad+2bdx)^2}) \text{Subst} \left(\int \frac{1}{\sqrt{-4abcd+(bc+ad)^2+4bdx^3}} \right)}{2b(a+bx)^{2/3}(c+dx)^{2/3}(bc+ad+2bdx)} \\
&= -\frac{3\sqrt[3]{c+dx}}{2b(a+bx)^{2/3}} + \frac{3^{3/4} \sqrt{2+\sqrt{3}} d^{2/3} ((a+bx)(c+dx))^{2/3} \sqrt{(bc+ad+2bdx)^2} ((bc-ad)^{2/3} + 2^{2/3} b^{4/3} (a+bx))}{2b(a+bx)^{2/3}(c+dx)^{2/3}(bc+ad+2bdx)}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.13

$$\frac{3\sqrt[3]{c+dx} {}_2F_1\left(-\frac{2}{3}, -\frac{1}{3}; \frac{1}{3}; \frac{d(a+bx)}{ad-bc}\right)}{2b(a+bx)^{2/3} \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(5/3), x]

[Out] (-3*(c + d*x)^(1/3)*Hypergeometric2F1[-2/3, -1/3, 1/3, (d*(a + b*x))/(-(b*c) + a*d)]/(2*b*(a + b*x)^(2/3)*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{1}{3}}}{b^2x^2+2abx+a^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(5/3), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/3)*(d*x + c)^(1/3)/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{5}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(5/3),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(5/3), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{5}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(5/3),x)

[Out] int((d*x+c)^(1/3)/(b*x+a)^(5/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{5}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(5/3),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(5/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/3}}{(a + bx)^{5/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/3)/(a + b*x)^(5/3),x)

[Out] int((c + d*x)^(1/3)/(a + b*x)^(5/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{c + dx}}{(a + bx)^{\frac{5}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/3)/(b*x+a)**(5/3),x)

[Out] Integral((c + d*x)**(1/3)/(a + b*x)**(5/3), x)

$$3.1586 \quad \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{8/3}} dx$$

Optimal. Leaf size=617

$$3^{3/4} \sqrt{2 + \sqrt{3}} d^{5/3} ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\frac{2\sqrt[3]{2}}{\sqrt[3]{2}}}$$

$$5 \cdot 2^{2/3} b^{4/3} (a + bx)^{2/3} (c + dx)^{2/3} (bc - ad) (ad + bc + 2bdx)$$

[Out] $-3/5*(d*x+c)^{(1/3)}/b/(b*x+a)^{(5/3)}-3/10*d*(d*x+c)^{(1/3)}/b/(-a*d+b*c)/(b*x+a)^{(2/3)}-1/10*3^{(3/4)}*d^{(5/3)}*((b*x+a)*(d*x+c))^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)}))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}+1/2*2^{(1/2)})*(((-a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*2^{(1/3)}/b^{(4/3)}/(-a*d+b*c)/(b*x+a)^{(2/3)}/(d*x+c)^{(2/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.84, antiderivative size = 617, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 51, 62, 623, 218}

$$3^{3/4} \sqrt{2 + \sqrt{3}} d^{5/3} ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\frac{2\sqrt[3]{2}}{\sqrt[3]{2}}}$$

$$5 \cdot 2^{2/3} b^{4/3} (a + bx)^{2/3} (c + dx)^{2/3} (bc - ad) (ad + bc + 2bdx)$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/3)/(a + b*x)^(8/3), x]

[Out] $(-3*(c + d*x)^{(1/3)})/(5*b*(a + b*x)^{(5/3)}) - (3*d*(c + d*x)^{(1/3)})/(10*b*(b*c - a*d)*(a + b*x)^{(2/3)}) - (3^{(3/4)}*Sqrt[2 + Sqrt[3]]*d^{(5/3)}*((a + b*x)*(c + d*x))^{(2/3)}*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*Sqrt[((b*c - a*d)^{(4/3)} - 2^{(2/3)}*b^{(2/3)}*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

$$\frac{2}{3}b^{1/3}d^{1/3}(b^2c - a^2d)^{2/3}((a + bx)(c + dx))^{1/3} + 2 \cdot 2^{1/3}b^{2/3}d^{2/3}((a + bx)(c + dx))^{2/3} / ((1 + \sqrt{3})(b^2c - a^2d)^{2/3} + 2^{2/3}b^{1/3}d^{1/3}((a + bx)(c + dx))^{1/3})^2 \cdot \text{EllipticF}[\text{ArcSin}[\frac{((1 - \sqrt{3})(b^2c - a^2d)^{2/3} + 2^{2/3}b^{1/3}d^{1/3}((a + bx)(c + dx))^{1/3})}{(1 + \sqrt{3})(b^2c - a^2d)^{2/3} + 2^{2/3}b^{1/3}d^{1/3}((a + bx)(c + dx))^{1/3}}], -7 - 4\sqrt{3}]] / (5 \cdot 2^{2/3}b^{4/3}(b^2c - a^2d)(a + bx)^{2/3}(c + dx)^{2/3}(b^2c + a^2d + 2b^2dx)\sqrt{((b^2c - a^2d)^{2/3}((b^2c - a^2d)^{2/3} + 2^{2/3}b^{1/3}d^{1/3}((a + bx)(c + dx))^{1/3})) / ((1 + \sqrt{3})(b^2c - a^2d)^{2/3} + 2^{2/3}b^{1/3}d^{1/3}((a + bx)(c + dx))^{1/3})^2} \sqrt{(a^2d + b^2(c + 2dx))^2}]$$
Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)]^2)*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]]/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] &
& PosQ[a]
```


Rule 623

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] :> With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt[3]{c+dx}}{(a+bx)^{8/3}} dx &= -\frac{3\sqrt[3]{c+dx}}{5b(a+bx)^{5/3}} + \frac{d \int \frac{1}{(a+bx)^{5/3}(c+dx)^{2/3}} dx}{5b} \\
 &= -\frac{3\sqrt[3]{c+dx}}{5b(a+bx)^{5/3}} - \frac{3d\sqrt[3]{c+dx}}{10b(bc-ad)(a+bx)^{2/3}} - \frac{d^2 \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{10b(bc-ad)} \\
 &= -\frac{3\sqrt[3]{c+dx}}{5b(a+bx)^{5/3}} - \frac{3d\sqrt[3]{c+dx}}{10b(bc-ad)(a+bx)^{2/3}} - \frac{(d^2((a+bx)(c+dx))^{2/3}) \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{2/3}} dx}{10b(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}} \\
 &= -\frac{3\sqrt[3]{c+dx}}{5b(a+bx)^{5/3}} - \frac{3d\sqrt[3]{c+dx}}{10b(bc-ad)(a+bx)^{2/3}} - \frac{(3d^2((a+bx)(c+dx))^{2/3} \sqrt{(bc+ad+2bdx)^2}) \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{2/3}} dx}{10b(bc-ad)(a+bx)^{2/3}} \\
 &= -\frac{3\sqrt[3]{c+dx}}{5b(a+bx)^{5/3}} - \frac{3d\sqrt[3]{c+dx}}{10b(bc-ad)(a+bx)^{2/3}} - \frac{3^{3/4} \sqrt{2+\sqrt{3}} d^{5/3} ((a+bx)(c+dx))^{2/3} \sqrt{(bc+ad+2bdx)^2}}{10b(bc-ad)(a+bx)^{2/3}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.12

$$\frac{3\sqrt[3]{c+dx} {}_2F_1\left(-\frac{5}{3}, -\frac{1}{3}; -\frac{2}{3}; \frac{d(a+bx)}{ad-bc}\right)}{5b(a+bx)^{5/3} \sqrt[3]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/3)/(a + b*x)^(8/3), x]

[Out] (-3*(c + d*x)^(1/3)*Hypergeometric2F1[-5/3, -1/3, -2/3, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(a + b*x)^(5/3)*((b*(c + d*x))/(b*c - a*d))^(1/3))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{1}{3}}}{b^3x^3+3ab^2x^2+3a^2bx+a^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(8/3),x, algorithm="fricas")

[Out] integral((b*x + a)^(1/3)*(d*x + c)^(1/3)/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{3}}}{(bx+a)^{\frac{8}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(8/3),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(8/3), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{3}}}{(bx+a)^{\frac{8}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/3)/(b*x+a)^(8/3),x)

[Out] int((d*x+c)^(1/3)/(b*x+a)^(8/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{3}}}{(bx+a)^{\frac{8}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/3)/(b*x+a)^(8/3),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/3)/(b*x + a)^(8/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/3}}{(a + bx)^{8/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/3)/(a + b*x)^(8/3), x)

[Out] int((c + d*x)^(1/3)/(a + b*x)^(8/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{c + dx}}{(a + bx)^{8/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/3)/(b*x+a)**(8/3), x)

[Out] Integral((c + d*x)**(1/3)/(a + b*x)**(8/3), x)

$$3.1587 \quad \int \frac{(a+bx)^{4/3}}{\sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=216

$$\frac{(bc-ad)^2 \log(a+bx)}{9b^{2/3}d^{7/3}} - \frac{(bc-ad)^2 \log\left(\frac{\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{d}\sqrt[3]{a+bx}} - 1\right)}{3b^{2/3}d^{7/3}} - \frac{2(bc-ad)^2 \tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt{3}\sqrt[3]{d}\sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{3\sqrt{3}b^{2/3}d^{7/3}} - \frac{2\sqrt[3]{a+bx}(c+dx)}{3d^2}$$

[Out] $-2/3*(-a*d+b*c)*(b*x+a)^{(1/3)}*(d*x+c)^{(2/3)}/d^2+1/2*(b*x+a)^{(4/3)}*(d*x+c)^{(2/3)}/d-1/9*(-a*d+b*c)^2*\ln(b*x+a)/b^{(2/3)}/d^{(7/3)}-1/3*(-a*d+b*c)^2*\ln(-1+b^{(1/3)}*(d*x+c)^{(1/3)}/d^{(1/3)})/(b*x+a)^{(1/3)}/b^{(2/3)}/d^{(7/3)}-2/9*(-a*d+b*c)^2*\arctan(1/3*3^{(1/2)}+2/3*b^{(1/3)}*(d*x+c)^{(1/3)}/d^{(1/3)})/(b*x+a)^{(1/3)}*3^{(1/2)}/b^{(2/3)}/d^{(7/3)}*3^{(1/2)}$

Rubi [A] time = 0.09, antiderivative size = 216, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {50, 59}

$$\frac{(bc-ad)^2 \log(a+bx)}{9b^{2/3}d^{7/3}} - \frac{(bc-ad)^2 \log\left(\frac{\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{d}\sqrt[3]{a+bx}} - 1\right)}{3b^{2/3}d^{7/3}} - \frac{2(bc-ad)^2 \tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt{3}\sqrt[3]{d}\sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{3\sqrt{3}b^{2/3}d^{7/3}} - \frac{2\sqrt[3]{a+bx}(c+dx)}{3d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(4/3)/(c + d*x)^(1/3), x]

[Out] $(-2*(b*c - a*d)*(a + b*x)^{(1/3)}*(c + d*x)^{(2/3)})/(3*d^2) + ((a + b*x)^{(4/3)}*(c + d*x)^{(2/3)})/(2*d) - (2*(b*c - a*d)^2*\text{ArcTan}[1/\text{Sqrt}[3] + (2*b^{(1/3)}*(c + d*x)^{(1/3)})/(\text{Sqrt}[3]*d^{(1/3)}*(a + b*x)^{(1/3)})])/(3*\text{Sqrt}[3]*b^{(2/3)}*d^{(7/3)}) - ((b*c - a*d)^2*\text{Log}[a + b*x])/(9*b^{(2/3)}*d^{(7/3)}) - ((b*c - a*d)^2*\text{Log}[-1 + (b^{(1/3)}*(c + d*x)^{(1/3)})/(d^{(1/3)}*(a + b*x)^{(1/3)})])/(3*b^{(2/3)}*d^{(7/3)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 59

```
Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] :=
  With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt
  [3]*(c + d*x)^(1/3)) + 1/Sqrt[3]])/d, x] + (-Simp[(3*q*Log[(q*(a + b*x)^(1/
  3)))/(c + d*x)^(1/3) - 1])/(2*d), x] - Simp[(q*Log[c + d*x])/(2*d), x])] /;
  FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]
```

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^{4/3}}{\sqrt[3]{c+dx}} dx &= \frac{(a+bx)^{4/3}(c+dx)^{2/3}}{2d} - \frac{(2(bc-ad)) \int \frac{\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} dx}{3d} \\ &= -\frac{2(bc-ad)\sqrt[3]{a+bx}(c+dx)^{2/3}}{3d^2} + \frac{(a+bx)^{4/3}(c+dx)^{2/3}}{2d} + \frac{(2(bc-ad)^2) \int \frac{1}{(a+bx)^{2/3}\sqrt[3]{c+dx}} dx}{9d^2} \\ &= -\frac{2(bc-ad)\sqrt[3]{a+bx}(c+dx)^{2/3}}{3d^2} + \frac{(a+bx)^{4/3}(c+dx)^{2/3}}{2d} - \frac{2(bc-ad)^2 \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt{3}\sqrt[3]{d}\sqrt[3]{a}}\right)}{3\sqrt{3}b^{2/3}d^{7/3}} \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.34

$$\frac{3(a+bx)^{7/3} \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{3}, \frac{7}{3}; \frac{10}{3}; \frac{d(a+bx)}{ad-bc}\right)}{7b\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(4/3)/(c + d*x)^(1/3), x]

[Out] (3*(a + b*x)^(7/3)*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[1/3, 7/3, 10/3, (d*(a + b*x))/(-b*c) + a*d])/(7*b*(c + d*x)^(1/3))

fricas [B] time = 0.48, size = 740, normalized size = 3.43

$$\left[\frac{6\sqrt{\frac{1}{3}}(b^3c^2d - 2ab^2cd^2 + a^2bd^3)\sqrt{\frac{(-b^2d)^{\frac{1}{3}}}{d}} \log\left(3b^2dx + b^2c + 2abd + 3(-b^2d)^{\frac{1}{3}}(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}b + 3\sqrt{\frac{1}{3}}\right)}{\right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] [1/18*(6*sqrt(1/3)*(b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*sqrt((-b^2*d)^(1/3)/d)*log(3*b^2*d*x + b^2*c + 2*a*b*d + 3*(-b^2*d)^(1/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3)*b + 3*sqrt(1/3)*(2*(b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) + (-b^2*d)^(1/3)*(b*d*x + b*c)))*sqrt((-b^2*d)^(1/3)/d) + 2*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(-b^2*d)^(2/3)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d + (-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) - (-b^2*d)^(1/3)*(b*d*x + b*c))/(d*x + c)) - 4*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(-b^2*d)^(2/3)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (-b^2*d)^(2/3)*(d*x + c))/(d*x + c)) + 3*(3*b^3*d^2*x - 4*b^3*c*d + 7*a*b^2*d^2)*(b*x + a)^(1/3)*(d*x + c)^(2/3))/(b^2*d^3), 1/18*(12*sqrt(1/3)*(b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*sqrt(-(-b^2*d)^(1/3)/d)*arctan(sqrt(1/3)*(2*(-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) - (-b^2*d)^(1/3)*(b*d*x + b*c)))*sqrt(-(-b^2*d)^(1/3)/d)/(b^2*d*x + b^2*c)) + 2*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(-b^2*d)^(2/3)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d + (-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) - (-b^2*d)^(1/3)*(b*d*x + b*c))/(d*x + c)) - 4*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(-b^2*d)^(2/3)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (-b^2*d)^(2/3)*(d*x + c))/(d*x + c)) + 3*(3*b^3*d^2*x - 4*b^3*c*d + 7*a*b^2*d^2)*(b*x + a)^(1/3)*(d*x + c)^(2/3))/(b^2*d^3)]

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{4}{3}}}{(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(4/3)/(d*x + c)^(1/3), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{4}{3}}}{(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(4/3)/(d*x+c)^(1/3),x)

[Out] int((b*x+a)^(4/3)/(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{4}{3}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(4/3)/(d*x + c)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{4/3}}{(c + dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(4/3)/(c + d*x)^(1/3),x)

[Out] int((a + b*x)^(4/3)/(c + d*x)^(1/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{4}{3}}}{\sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(4/3)/(d*x+c)**(1/3),x)

[Out] Integral((a + b*x)**(4/3)/(c + d*x)**(1/3), x)

$$3.1588 \quad \int \frac{\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=171

$$\frac{(bc-ad)\log(a+bx)}{6b^{2/3}d^{4/3}} + \frac{(bc-ad)\log\left(\frac{\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{d}\sqrt[3]{a+bx}} - 1\right)}{2b^{2/3}d^{4/3}} + \frac{(bc-ad)\tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt{3}\sqrt[3]{d}\sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{\sqrt{3}b^{2/3}d^{4/3}} + \frac{\sqrt[3]{a+bx}(c+dx)^{2/3}}{d}$$

[Out] (b*x+a)^(1/3)*(d*x+c)^(2/3)/d+1/6*(-a*d+b*c)*ln(b*x+a)/b^(2/3)/d^(4/3)+1/2*(-a*d+b*c)*ln(-1+b^(1/3)*(d*x+c)^(1/3)/d^(1/3)/(b*x+a)^(1/3))/b^(2/3)/d^(4/3)+1/3*(-a*d+b*c)*arctan(1/3*3^(1/2)+2/3*b^(1/3)*(d*x+c)^(1/3)/d^(1/3)/(b*x+a)^(1/3)*3^(1/2))/b^(2/3)/d^(4/3)*3^(1/2)

Rubi [A] time = 0.04, antiderivative size = 171, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {50, 59}

$$\frac{(bc-ad)\log(a+bx)}{6b^{2/3}d^{4/3}} + \frac{(bc-ad)\log\left(\frac{\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{d}\sqrt[3]{a+bx}} - 1\right)}{2b^{2/3}d^{4/3}} + \frac{(bc-ad)\tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt{3}\sqrt[3]{d}\sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{\sqrt{3}b^{2/3}d^{4/3}} + \frac{\sqrt[3]{a+bx}(c+dx)^{2/3}}{d}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/3)/(c + d*x)^(1/3), x]

[Out] ((a + b*x)^(1/3)*(c + d*x)^(2/3))/d + ((b*c - a*d)*ArcTan[1/Sqrt[3] + (2*b^(1/3)*(c + d*x)^(1/3))/(Sqrt[3]*d^(1/3)*(a + b*x)^(1/3))]/(Sqrt[3]*b^(2/3)*d^(4/3)) + ((b*c - a*d)*Log[a + b*x]/(6*b^(2/3)*d^(4/3)) + ((b*c - a*d)*Log[-1 + (b^(1/3)*(c + d*x)^(1/3))/(d^(1/3)*(a + b*x)^(1/3))]/(2*b^(2/3)*d^(4/3)))

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 59

```
Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] :=
With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt
```


$[3]*(c + d*x)^{(1/3)} + 1/\text{Sqrt}[3]]/d, x] + (-\text{Simp}[(3*q*\text{Log}[(q*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - 1])/(2*d), x] - \text{Simp}[(q*\text{Log}[c + d*x])/(2*d), x]) /;$
 $\text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{PosQ}[d/b]$

Rubi steps

$$\int \frac{\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} dx = \frac{\sqrt[3]{a+bx}(c+dx)^{2/3}}{d} - \frac{(bc-ad) \int \frac{1}{(a+bx)^{2/3} \sqrt[3]{c+dx}} dx}{3d}$$

$$= \frac{\sqrt[3]{a+bx}(c+dx)^{2/3}}{d} + \frac{(bc-ad) \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt{3}\sqrt[3]{d}\sqrt[3]{a+bx}}\right)}{\sqrt{3}b^{2/3}d^{4/3}} + \frac{(bc-ad) \log(a+bx)}{6b^{2/3}d^{4/3}} + \frac{(bc-ad)}{6b^{2/3}d^{4/3}}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.43

$$\frac{3(a+bx)^{4/3} \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{3}, \frac{4}{3}; \frac{7}{3}; \frac{d(a+bx)}{ad-bc}\right)}{4b\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/3)/(c + d*x)^(1/3), x]

[Out] (3*(a + b*x)^(4/3)*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[1/3, 4/3, 7/3, (d*(a + b*x))/(-b*c + a*d)]/(4*b*(c + d*x)^(1/3))

fricas [B] time = 0.47, size = 618, normalized size = 3.61

$$\left[\frac{6(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}b^2d - 3\sqrt{\frac{1}{3}}(b^2cd - abd^2)\sqrt{\frac{(-b^2d)^{\frac{1}{3}}}{d}} \log\left(3b^2dx + b^2c + 2abd + 3(-b^2d)^{\frac{1}{3}}(bx+a)^{\frac{1}{3}}(dx+c)\right)}{4b\sqrt[3]{c+dx}} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/(d*x+c)^(1/3), x, algorithm="fricas")

```
[Out] [1/6*(6*(b*x + a)^(1/3)*(d*x + c)^(2/3)*b^2*d - 3*sqrt(1/3)*(b^2*c*d - a*b*d^2)*sqrt((-b^2*d)^(1/3)/d)*log(3*b^2*d*x + b^2*c + 2*a*b*d + 3*(-b^2*d)^(1/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3)*b + 3*sqrt(1/3)*(2*(b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) + (-b^2*d)^(1/3)*(b*d*x + b*c))*sqrt((-b^2*d)^(1/3)/d)) - (-b^2*d)^(2/3)*(b*c - a*d)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d + (-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) - (-b^2*d)^(1/3)*(b*d*x + b*c))/(d*x + c)) + 2*(-b^2*d)^(2/3)*(b*c - a*d)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (-b^2*d)^(2/3)*(d*x + c))/(d*x + c)))/(b^2*d^2), 1/6*(6*(b*x + a)^(1/3)*(d*x + c)^(2/3)*b^2*d - 6*sqrt(1/3)*(b^2*c*d - a*b*d^2)*sqrt(-(-b^2*d)^(1/3)/d)*arctan(sqrt(1/3)*(2*(-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) - (-b^2*d)^(1/3)*(b*d*x + b*c))*sqrt(-(-b^2*d)^(1/3)/d)/(b^2*d*x + b^2*c)) - (-b^2*d)^(2/3)*(b*c - a*d)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d + (-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) - (-b^2*d)^(1/3)*(b*d*x + b*c))/(d*x + c)) + 2*(-b^2*d)^(2/3)*(b*c - a*d)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (-b^2*d)^(2/3)*(d*x + c))/(d*x + c)))/(b^2*d^2)]
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{3}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(1/3)/(d*x+c)^(1/3),x, algorithm="giac")
```

```
[Out] integrate((b*x + a)^(1/3)/(d*x + c)^(1/3), x)
```

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{3}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((b*x+a)^(1/3)/(d*x+c)^(1/3),x)
```

```
[Out] int((b*x+a)^(1/3)/(d*x+c)^(1/3),x)
```

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{3}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/3)/(d*x + c)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{1/3}}{(c + dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/3)/(c + d*x)^(1/3), x)

[Out] int((a + b*x)^(1/3)/(c + d*x)^(1/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{a + bx}}{\sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/3)/(d*x+c)**(1/3), x)

[Out] Integral((a + b*x)**(1/3)/(c + d*x)**(1/3), x)

$$3.1589 \quad \int \frac{1}{(a+bx)^{2/3} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=126

$$-\frac{3 \log\left(\frac{\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{d} \sqrt[3]{a+bx}} - 1\right)}{2b^{2/3} \sqrt[3]{d}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt{3} \sqrt[3]{d} \sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{b^{2/3} \sqrt[3]{d}} - \frac{\log(a+bx)}{2b^{2/3} \sqrt[3]{d}}$$

[Out] $-1/2*\ln(b*x+a)/b^(2/3)/d^(1/3)-3/2*\ln(-1+b^(1/3)*(d*x+c)^(1/3)/d^(1/3)/(b*x+a)^(1/3))/b^(2/3)/d^(1/3)-\arctan(1/3*3^(1/2)+2/3*b^(1/3)*(d*x+c)^(1/3)/d^(1/3)/(b*x+a)^(1/3)*3^(1/2))*3^(1/2)/b^(2/3)/d^(1/3)$

Rubi [A] time = 0.01, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {59}

$$-\frac{3 \log\left(\frac{\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{d} \sqrt[3]{a+bx}} - 1\right)}{2b^{2/3} \sqrt[3]{d}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt{3} \sqrt[3]{d} \sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{b^{2/3} \sqrt[3]{d}} - \frac{\log(a+bx)}{2b^{2/3} \sqrt[3]{d}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(2/3)*(c + d*x)^(1/3)),x]

[Out] $-\left(\frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt{3} \sqrt[3]{d} \sqrt[3]{a+bx}}\right]}{\sqrt{3} \sqrt[3]{d} \sqrt[3]{a+bx}}\right) - \frac{\log(a+bx)}{2b^{2/3} \sqrt[3]{d}} - \frac{3 \operatorname{Log}\left[-1 + \frac{b^{1/3} (c+d*x)^{1/3}}{d^{1/3} (a+b*x)^{1/3}}\right]}{2b^{2/3} \sqrt[3]{d}}$

Rule 59

Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] :=
 With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt[3]*(c + d*x)^(1/3) + 1/Sqrt[3]])]/d, x] + (-Simp[(3*q*Log[(q*(a + b*x)^(1/3))/(c + d*x)^(1/3) - 1])]/(2*d), x] - Simp[(q*Log[c + d*x])/(2*d), x]) /;
 FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]

Rubi steps

$$\int \frac{1}{(a+bx)^{2/3} \sqrt[3]{c+dx}} dx = -\frac{\sqrt{3} \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt{3} \sqrt[3]{d} \sqrt[3]{a+bx}}\right)}{b^{2/3} \sqrt[3]{d}} - \frac{\log(a+bx)}{2b^{2/3} \sqrt[3]{d}} - \frac{3 \log\left(-1 + \frac{\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{d} \sqrt[3]{a+bx}}\right)}{2b^{2/3} \sqrt[3]{d}}$$

Mathematica [C] time = 0.03, size = 71, normalized size = 0.56

$$\frac{3\sqrt[3]{a+bx}\sqrt[3]{\frac{b(c+dx)}{bc-ad}}{}_2F_1\left(\frac{1}{3}, \frac{1}{3}; \frac{4}{3}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(2/3)*(c + d*x)^(1/3)),x]

[Out] (3*(a + b*x)^(1/3)*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[1/3, 1/3, 4/3, (d*(a + b*x))/(-b*c) + a*d])/(b*(c + d*x)^(1/3))

fricas [B] time = 0.47, size = 519, normalized size = 4.12

$$\sqrt{3}bd\sqrt{\frac{(-b^2d)^{\frac{1}{3}}}{d}}\log\left(3b^2dx + b^2c + 2abd + 3(-b^2d)^{\frac{1}{3}}(bx + a)^{\frac{1}{3}}(dx + c)^{\frac{2}{3}}b + \sqrt{3}\left(2(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{1}{3}}bd - (-b^2d)^{\frac{1}{3}}(bx + a)^{\frac{1}{3}}(dx + c)^{\frac{2}{3}}b\right)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(2/3)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] [1/2*(sqrt(3)*b*d*sqrt((-b^2*d)^(1/3)/d)*log(3*b^2*d*x + b^2*c + 2*a*b*d + 3*(-b^2*d)^(1/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3)*b + sqrt(3)*(2*(b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) + (-b^2*d)^(1/3)*(b*d*x + b*c))*sqrt((-b^2*d)^(1/3)/d) + (-b^2*d)^(2/3)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d + (-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) - (-b^2*d)^(1/3)*(b*d*x + b*c))/(d*x + c)) - 2*(-b^2*d)^(2/3)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (-b^2*d)^(2/3)*(d*x + c))/(d*x + c)))/(b^2*d), 1/2*(2*sqrt(3)*b*d*sqrt(-(-b^2*d)^(1/3)/d)*arctan(1/3*sqrt(3)*(2*(-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) - (-b^2*d)^(1/3)*(b*d*x + b*c))*sqrt(-(-b^2*d)^(1/3)/d)/(b^2*d*x + b^2*c)) + (-b^2*d)^(2/3)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d + (-b^2*d)^(2/3)*(b*x + a)^(1/3)*(d*x + c)^(2/3) - (-b^2*d)^(1/3)*(b*d*x + b*c))/(d*x + c)) - 2*(-b^2*d)^(2/3)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (-b^2*d)^(2/3)*(d*x + c))/(d*x + c)))/(b^2*d)]

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(2/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(2/3)*(d*x + c)^(1/3)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(2/3)/(d*x+c)^(1/3),x)

[Out] int(1/(b*x+a)^(2/3)/(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(2/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(2/3)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{\frac{2}{3}}(c+dx)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(2/3)*(c + d*x)^(1/3)),x)

[Out] int(1/((a + b*x)^(2/3)*(c + d*x)^(1/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{2}{3}}\sqrt[3]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(2/3)/(d*x+c)**(1/3),x)
```

```
[Out] Integral(1/((a + b*x)**(2/3)*(c + d*x)**(1/3)), x)
```

$$3.1590 \quad \int \frac{1}{(a+bx)^{5/3} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=32

$$-\frac{3(c+dx)^{2/3}}{2(a+bx)^{2/3}(bc-ad)}$$

[Out] $-3/2*(d*x+c)^{(2/3)/(-a*d+b*c)/(b*x+a)^{(2/3)}$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{3(c+dx)^{2/3}}{2(a+bx)^{2/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)^{(5/3)*(c + d*x)^{(1/3))}, x]$

[Out] $(-3*(c + d*x)^{(2/3))/(2*(b*c - a*d)*(a + b*x)^{(2/3)})$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_. + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Simp} [((a + b*x)^{(m + 1)*(c + d*x)^{(n + 1))}/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{1}{(a+bx)^{5/3} \sqrt[3]{c+dx}} dx = -\frac{3(c+dx)^{2/3}}{2(bc-ad)(a+bx)^{2/3}}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 1.00

$$-\frac{3(c+dx)^{2/3}}{2(a+bx)^{2/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/((a + b*x)^{(5/3)*(c + d*x)^{(1/3))}, x]$

[Out] $(-3*(c + d*x)^{(2/3))/(2*(b*c - a*d)*(a + b*x)^{(2/3)})$

fricas [A] time = 0.46, size = 42, normalized size = 1.31

$$\frac{3 (bx + a)^{\frac{1}{3}} (dx + c)^{\frac{2}{3}}}{2 (abc - a^2d + (b^2c - abd)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/3)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] -3/2*(b*x + a)^(1/3)*(d*x + c)^(2/3)/(a*b*c - a^2*d + (b^2*c - a*b*d)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{3}}(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/3)*(d*x + c)^(1/3)), x)

maple [A] time = 0.01, size = 27, normalized size = 0.84

$$\frac{3 (dx + c)^{\frac{2}{3}}}{2 (bx + a)^{\frac{2}{3}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/3)/(d*x+c)^(1/3),x)

[Out] 3/2/(b*x+a)^(2/3)*(d*x+c)^(2/3)/(a*d-b*c)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{3}}(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/3)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{1}{(a + bx)^{5/3} (c + dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(5/3)*(c + d*x)^(1/3)), x)`

[Out] `int(1/((a + b*x)^(5/3)*(c + d*x)^(1/3)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{5}{3}} \sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/3)/(d*x+c)**(1/3), x)`

[Out] `Integral(1/((a + b*x)**(5/3)*(c + d*x)**(1/3)), x)`

$$3.1591 \quad \int \frac{1}{(a+bx)^{8/3} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=66

$$\frac{9d(c+dx)^{2/3}}{10(a+bx)^{2/3}(bc-ad)^2} - \frac{3(c+dx)^{2/3}}{5(a+bx)^{5/3}(bc-ad)}$$

[Out] $-3/5*(d*x+c)^{(2/3)/(-a*d+b*c)/(b*x+a)^{(5/3)+9/10*d*(d*x+c)^{(2/3)/(-a*d+b*c)^{2/3}/(b*x+a)^{(2/3)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{9d(c+dx)^{2/3}}{10(a+bx)^{2/3}(bc-ad)^2} - \frac{3(c+dx)^{2/3}}{5(a+bx)^{5/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(8/3)*(c + d*x)^(1/3)), x]

[Out] $(-3*(c + d*x)^{(2/3))/(5*(b*c - a*d)*(a + b*x)^{(5/3)}) + (9*d*(c + d*x)^{(2/3))/(10*(b*c - a*d)^2*(a + b*x)^{(2/3)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[n] && !LtQ[m, -1] && !LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{8/3} \sqrt[3]{c+dx}} dx = -\frac{3(c+dx)^{2/3}}{5(bc-ad)(a+bx)^{5/3}} - \frac{(3d) \int \frac{1}{(a+bx)^{5/3} \sqrt[3]{c+dx}} dx}{5(bc-ad)}$$

$$= -\frac{3(c+dx)^{2/3}}{5(bc-ad)(a+bx)^{5/3}} + \frac{9d(c+dx)^{2/3}}{10(bc-ad)^2(a+bx)^{2/3}}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.70

$$\frac{3(c+dx)^{2/3}(5ad-2bc+3bdx)}{10(a+bx)^{5/3}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a+b*x)^(8/3)*(c+d*x)^(1/3)),x]

[Out] (3*(c+d*x)^(2/3)*(-2*b*c+5*a*d+3*b*d*x))/(10*(b*c-a*d)^2*(a+b*x)^(5/3))

fricas [B] time = 0.44, size = 118, normalized size = 1.79

$$\frac{3(3bdx-2bc+5ad)(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}}{10(a^2b^2c^2-2a^3bcd+a^4d^2+(b^4c^2-2ab^3cd+a^2b^2d^2)x^2+2(ab^3c^2-2a^2b^2cd+a^3bd^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(8/3)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] 3/10*(3*b*d*x-2*b*c+5*a*d)*(b*x+a)^(1/3)*(d*x+c)^(2/3)/(a^2*b^2*c^2-2*a^3*b*c*d+a^4*d^2+(b^4*c^2-2*a*b^3*c*d+a^2*b^2*d^2)*x^2+2*(a*b^3*c^2-2*a^2*b^2*c*d+a^3*b*d^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{8}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(8/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(1/((b*x+a)^(8/3)*(d*x+c)^(1/3)), x)

maple [A] time = 0.00, size = 54, normalized size = 0.82

$$\frac{3(dx+c)^{\frac{2}{3}}(3bdx+5ad-2bc)}{10(bx+a)^{\frac{5}{3}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(8/3)/(d*x+c)^(1/3),x)

[Out] 3/10*(d*x+c)^(2/3)*(3*b*d*x+5*a*d-2*b*c)/(b*x+a)^(5/3)/(a^2*d^2-2*a*b*c*d+b^2*c^2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{8}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(8/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(8/3)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{1}{(a+bx)^{\frac{8}{3}}(c+dx)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(8/3)*(c + d*x)^(1/3)),x)

[Out] int(1/((a + b*x)^(8/3)*(c + d*x)^(1/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{8}{3}}\sqrt[3]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(8/3)/(d*x+c)**(1/3),x)

[Out] Integral(1/((a + b*x)**(8/3)*(c + d*x)**(1/3)), x)

$$3.1592 \quad \int \frac{1}{(a+bx)^{11/3} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=101

$$-\frac{27d^2(c+dx)^{2/3}}{40(a+bx)^{2/3}(bc-ad)^3} + \frac{9d(c+dx)^{2/3}}{20(a+bx)^{5/3}(bc-ad)^2} - \frac{3(c+dx)^{2/3}}{8(a+bx)^{8/3}(bc-ad)}$$

[Out] $-3/8*(d*x+c)^{(2/3)/(-a*d+b*c)/(b*x+a)^{(8/3)+9/20*d*(d*x+c)^{(2/3)/(-a*d+b*c)^{2/3}/(b*x+a)^{(5/3)-27/40*d^2*(d*x+c)^{(2/3)/(-a*d+b*c)^3/(b*x+a)^{(2/3)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{27d^2(c+dx)^{2/3}}{40(a+bx)^{2/3}(bc-ad)^3} + \frac{9d(c+dx)^{2/3}}{20(a+bx)^{5/3}(bc-ad)^2} - \frac{3(c+dx)^{2/3}}{8(a+bx)^{8/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(11/3)*(c + d*x)^(1/3)),x]

[Out] $(-3*(c+d*x)^{(2/3))/(8*(b*c-a*d)*(a+b*x)^{(8/3)}) + (9*d*(c+d*x)^{(2/3)})/(20*(b*c-a*d)^2*(a+b*x)^{(5/3)}) - (27*d^2*(c+d*x)^{(2/3)})/(40*(b*c-a*d)^3*(a+b*x)^{(2/3)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{11/3} \sqrt[3]{c+dx}} dx &= -\frac{3(c+dx)^{2/3}}{8(bc-ad)(a+bx)^{8/3}} - \frac{(3d) \int \frac{1}{(a+bx)^{8/3} \sqrt[3]{c+dx}} dx}{4(bc-ad)} \\
&= -\frac{3(c+dx)^{2/3}}{8(bc-ad)(a+bx)^{8/3}} + \frac{9d(c+dx)^{2/3}}{20(bc-ad)^2(a+bx)^{5/3}} + \frac{(9d^2) \int \frac{1}{(a+bx)^{5/3} \sqrt[3]{c+dx}} dx}{20(bc-ad)^2} \\
&= -\frac{3(c+dx)^{2/3}}{8(bc-ad)(a+bx)^{8/3}} + \frac{9d(c+dx)^{2/3}}{20(bc-ad)^2(a+bx)^{5/3}} - \frac{27d^2(c+dx)^{2/3}}{40(bc-ad)^3(a+bx)^{2/3}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 77, normalized size = 0.76

$$-\frac{3(c+dx)^{2/3} (20a^2d^2 + 8abd(3dx - 2c) + b^2(5c^2 - 6cdx + 9d^2x^2))}{40(a+bx)^{8/3}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(11/3)*(c + d*x)^(1/3)),x]

[Out] (-3*(c + d*x)^(2/3)*(20*a^2*d^2 + 8*a*b*d*(-2*c + 3*d*x) + b^2*(5*c^2 - 6*c*d*x + 9*d^2*x^2)))/(40*(b*c - a*d)^3*(a + b*x)^(8/3))

fricas [B] time = 0.51, size = 251, normalized size = 2.49

$$\frac{3(9b^2d^2x^2 + 5b^2c^2 - 16abcd + 20a^2d^2 - 6(b^2cd - 4abd^2)x)}{40(a^3b^3c^3 - 3a^4b^2c^2d + 3a^5bcd^2 - a^6d^3 + (b^6c^3 - 3ab^5c^2d + 3a^2b^4cd^2 - a^3b^3d^3)x^3 + 3(ab^5c^3 - 3a^2b^4c^2d + \dots)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/3)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] -3/40*(9*b^2*d^2*x^2 + 5*b^2*c^2 - 16*a*b*c*d + 20*a^2*d^2 - 6*(b^2*c*d - 4*a*b*d^2)*x)*(b*x + a)^(1/3)*(d*x + c)^(2/3)/(a^3*b^3*c^3 - 3*a^4*b^2*c^2*d + 3*a^5*b*c*d^2 - a^6*d^3 + (b^6*c^3 - 3*a*b^5*c^2*d + 3*a^2*b^4*c*d^2 - a^3*b^3*d^3)*x^3 + 3*(a*b^5*c^3 - 3*a^2*b^4*c^2*d + 3*a^3*b^3*c*d^2 - a^4*b^2*d^3)*x^2 + 3*(a^2*b^4*c^3 - 3*a^3*b^3*c^2*d + 3*a^4*b^2*c*d^2 - a^5*b*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{11}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(11/3)*(d*x + c)^(1/3)), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{3(dx+c)^{\frac{2}{3}}(9b^2x^2d^2+24abd^2x-6b^2cdx+20a^2d^2-16abcd+5b^2c^2)}{40(bx+a)^{\frac{8}{3}}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(11/3)/(d*x+c)^(1/3),x)

[Out] 3/40*(d*x+c)^(2/3)*(9*b^2*d^2*x^2+24*a*b*d^2*x-6*b^2*c*d*x+20*a^2*d^2-16*a*b*c*d+5*b^2*c^2)/(b*x+a)^(8/3)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{11}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(11/3)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{\frac{11}{3}}(c+dx)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(11/3)*(c + d*x)^(1/3)),x)

[Out] int(1/((a + b*x)^(11/3)*(c + d*x)^(1/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{11}{3}}\sqrt[3]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(11/3)/(d*x+c)**(1/3),x)
```

```
[Out] Integral(1/((a + b*x)**(11/3)*(c + d*x)**(1/3)), x)
```

$$3.1593 \quad \int \frac{1}{(a+bx)^{14/3} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=136

$$\frac{243d^3(c+dx)^{2/3}}{440(a+bx)^{2/3}(bc-ad)^4} - \frac{81d^2(c+dx)^{2/3}}{220(a+bx)^{5/3}(bc-ad)^3} + \frac{27d(c+dx)^{2/3}}{88(a+bx)^{8/3}(bc-ad)^2} - \frac{3(c+dx)^{2/3}}{11(a+bx)^{11/3}(bc-ad)}$$

[Out] $-3/11*(d*x+c)^{(2/3)/(-a*d+b*c)/(b*x+a)^{(11/3)+27/88*d*(d*x+c)^{(2/3)/(-a*d+b*c)^2/(b*x+a)^{(8/3)-81/220*d^2*(d*x+c)^{(2/3)/(-a*d+b*c)^3/(b*x+a)^{(5/3)+243/440*d^3*(d*x+c)^{(2/3)/(-a*d+b*c)^4/(b*x+a)^{(2/3)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{243d^3(c+dx)^{2/3}}{440(a+bx)^{2/3}(bc-ad)^4} - \frac{81d^2(c+dx)^{2/3}}{220(a+bx)^{5/3}(bc-ad)^3} + \frac{27d(c+dx)^{2/3}}{88(a+bx)^{8/3}(bc-ad)^2} - \frac{3(c+dx)^{2/3}}{11(a+bx)^{11/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(14/3)*(c + d*x)^(1/3)),x]

[Out] $(-3*(c+d*x)^{(2/3))/(11*(b*c-a*d)*(a+b*x)^{(11/3)}+(27*d*(c+d*x)^{(2/3))/(88*(b*c-a*d)^2*(a+b*x)^{(8/3)}-(81*d^2*(c+d*x)^{(2/3))/(220*(b*c-a*d)^3*(a+b*x)^{(5/3)}+(243*d^3*(c+d*x)^{(2/3))/(440*(b*c-a*d)^4*(a+b*x)^{(2/3)}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{14/3} \sqrt[3]{c+dx}} dx &= -\frac{3(c+dx)^{2/3}}{11(bc-ad)(a+bx)^{11/3}} - \frac{(9d) \int \frac{1}{(a+bx)^{11/3} \sqrt[3]{c+dx}} dx}{11(bc-ad)} \\
&= -\frac{3(c+dx)^{2/3}}{11(bc-ad)(a+bx)^{11/3}} + \frac{27d(c+dx)^{2/3}}{88(bc-ad)^2(a+bx)^{8/3}} + \frac{(27d^2) \int \frac{1}{(a+bx)^{8/3} \sqrt[3]{c+dx}} dx}{44(bc-ad)^2} \\
&= -\frac{3(c+dx)^{2/3}}{11(bc-ad)(a+bx)^{11/3}} + \frac{27d(c+dx)^{2/3}}{88(bc-ad)^2(a+bx)^{8/3}} - \frac{81d^2(c+dx)^{2/3}}{220(bc-ad)^3(a+bx)^{5/3}} - \dots \\
&= -\frac{3(c+dx)^{2/3}}{11(bc-ad)(a+bx)^{11/3}} + \frac{27d(c+dx)^{2/3}}{88(bc-ad)^2(a+bx)^{8/3}} - \frac{81d^2(c+dx)^{2/3}}{220(bc-ad)^3(a+bx)^{5/3}} + \dots
\end{aligned}$$

Mathematica [A] time = 0.05, size = 118, normalized size = 0.87

$$\frac{3(c+dx)^{2/3} (220a^3d^3 + 132a^2bd^2(3dx-2c) + 33ab^2d(5c^2-6cdx+9d^2x^2) + b^3(-40c^3+45c^2dx-54cd^2x^2+81d^3x^3))}{440(a+bx)^{11/3}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a+b*x)^(14/3)*(c+d*x)^(1/3)),x]

[Out] (3*(c+d*x)^(2/3)*(220*a^3*d^3+132*a^2*b*d^2*(-2*c+3*d*x)+33*a*b^2*d*(5*c^2-6*c*d*x+9*d^2*x^2)+b^3*(-40*c^3+45*c^2*d*x-54*c*d^2*x^2+81*d^3*x^3)))/(440*(b*c-a*d)^4*(a+b*x)^(11/3))

fricas [B] time = 0.55, size = 420, normalized size = 3.09

$$\frac{3(81b^3d^3x^3-40b^3c^3+165ab^2c^2d-264a^2b^3cd^2+220a^3d^3-27(2b^3cd^2-11a^2b^2d^3)x^2+9(5b^3c^2d-22a^2b^2cd^2+44a^2bd^3)x)(b*x+a)^{1/3}(d*x+c)^{2/3}}{440(a^4b^4c^4-4a^5b^3c^3d+6a^6b^2c^2d^2-4a^7bcd^3+a^8d^4+(b^8c^4-4ab^7c^3d+6a^2b^6c^2d^2-4a^3b^5cd^3+a^4b^4d^4)x^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(14/3)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] 3/440*(81*b^3*d^3*x^3-40*b^3*c^3+165*a*b^2*c^2*d-264*a^2*b^3*c*d^2+220*a^3*d^3-27*(2*b^3*c*d^2-11*a^2*b^2*d^3)*x^2+9*(5*b^3*c^2*d-22*a^2*b^2*c*d^2+44*a^2*b*d^3)*x)*(b*x+a)^(1/3)*(d*x+c)^(2/3)/(a^4*b^4*c^4-4*a^5*b^3*c^3*d+6*a^6*b^2*c^2*d^2-4*a^7*b*c*d^3+a^8*d^4+(b^8*c^4-4*a*b^7*c^3*d+6*a^2*b^6*c^2*d^2-4*a^3*b^5*c^2*d^2-4*a^4*b^4*c*d^3+a^5*b^3*d^4)*x^3+6*(a^2*b^6*c^4-4*a^3*b^5*c^3*d+6*a^4*b^4*c^2*d^2-4*a^5*b^3*d^4)*x^2+6*(a^2*b^6*c^4-4*a^3*b^5*c^3*d+6*a^4*b^4*c^2*d^2-4*a^5*b^3*d^4)*x+6*(a^2*b^6*c^4-4*a^3*b^5*c^3*d+6*a^4*b^4*c^2*d^2-4*a^5*b^3*d^4))

$*c*d^3 + a^6*b^2*d^4)*x^2 + 4*(a^3*b^5*c^4 - 4*a^4*b^4*c^3*d + 6*a^5*b^3*c^2*d^2 - 4*a^6*b^2*c*d^3 + a^7*b*d^4)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{14}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(14/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(14/3)*(d*x + c)^(1/3)), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{3(dx+c)^{\frac{2}{3}}(81b^3d^3x^3 + 297ab^2d^3x^2 - 54b^3cd^2x^2 + 396a^2bd^3x - 198ab^2cd^2x + 45b^3c^2dx + 220a^3d^3 - 264a^2bcd)}{440(bx+a)^{\frac{11}{3}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(14/3)/(d*x+c)^(1/3),x)

[Out] $3/440*(d*x+c)^{(2/3)}*(81*b^3*d^3*x^3+297*a*b^2*d^3*x^2-54*b^3*c*d^2*x^2+396*a^2*b*d^3*x-198*a*b^2*c*d^2*x+45*b^3*c^2*d*x+220*a^3*d^3-264*a^2*b*c*d^2+16*5*a*b^2*c^2*d-40*b^3*c^3)/(b*x+a)^{(11/3)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{14}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(14/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(14/3)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{14/3}(c+dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a + b*x)^(14/3)*(c + d*x)^(1/3)),x)
```

```
[Out] int(1/((a + b*x)^(14/3)*(c + d*x)^(1/3)), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(14/3)/(d*x+c)**(1/3),x)
```

```
[Out] Timed out
```

$$3.1594 \quad \int \frac{(a+bx)^{8/3}}{\sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=1365

$$3\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{\frac{(bc-ad)^{4/3}-2^2}{(bc-ad)^{4/3}-2^2}}$$

$$7\sqrt[3]{2}b^{2/3}d^{11/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)$$

[Out] $\frac{3}{7}(-a*d+b*c)^2*(b*x+a)^{(2/3)}*(d*x+c)^{(2/3)}/d^3-12/35*(-a*d+b*c)*(b*x+a)^{(5/3)}*(d*x+c)^{(2/3)}/d^2+3/10*(b*x+a)^{(8/3)}*(d*x+c)^{(2/3)}/d-3/7*2^{(2/3)}*(-a*d+b*c)^3*((b*x+a)*(d*x+c))^{(1/3)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}/b^{(2/3)}/d^{(11/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))-2/7*2^{(1/6)}*3^{(3/4)}*(-a*d+b*c)^{(11/3)}*((b*x+a)*(d*x+c))^{(1/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)})))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((-a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/b^{(2/3)}/d^{(11/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*(-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}+3/14*3^{(1/4)}*(-a*d+b*c)^{(11/3)}*((b*x+a)*(d*x+c))^{(1/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticE((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)})))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})*((-a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*2^{(2/3)}/b^{(2/3)}/d^{(11/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*(-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 2.80, antiderivative size = 1365, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {50, 62, 623, 303, 218, 1877}

$$3\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{(bc-ad)^{4/3}}$$

$$7\sqrt[3]{2}b^{2/3}d^{11/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(8/3)/(c + d*x)^(1/3), x]

[Out] (3*(b*c - a*d)^2*(a + b*x)^(2/3)*(c + d*x)^(2/3))/(7*d^3) - (12*(b*c - a*d)*(a + b*x)^(5/3)*(c + d*x)^(2/3))/(35*d^2) + (3*(a + b*x)^(8/3)*(c + d*x)^(2/3))/(10*d) - (3*2^(2/3)*(b*c - a*d)^3*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/(7*b^(2/3)*d^(11/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))) + (3*3^(1/4)*Sqrt[2 - Sqrt[3]]*(b*c - a*d)^(11/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2*EllipticE[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(7*2^(1/3)*b^(2/3)*d^(11/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2]) - (2*2^(1/6)*3^(3/4)*(b*c - a*d)^(11/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*EllipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(7*b^(2/3)*d^(11/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 303

```
Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
], s = Denom[Rt[b/a, 3]]}, Dist[(Sqrt[2]*s)/(Sqrt[2 + Sqrt[3]]*r), Int[1/Sq
rt[a + b*x^3], x], x] + Dist[1/r, Int[((1 - Sqrt[3])*s + r*x)/Sqrt[a + b*x^
3], x], x] /; FreeQ[{a, b}, x] && PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rule 1877

```
Int[((c_.) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = N
umer[Simplify[((1 - Sqrt[3])*d)/c]], s = Denom[Simplify[((1 - Sqrt[3])*d)/c
]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 + Sqrt[3])*s + r*x)), x] - S
imp[(3^(1/4)*Sqrt[2 - Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/
(1 + Sqrt[3])*s + r*x]^2]*EllipticE[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + S
qrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(r^2*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/
```


((1 + Sqrt[3])*s + r*x)^2)), x]] /; FreeQ[{a, b, c, d}, x] && PosQ[a] && EqQ[b*c^3 - 2*(5 - 3*Sqrt[3])*a*d^3, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{8/3}}{\sqrt[3]{c+dx}} dx &= \frac{3(a+bx)^{8/3}(c+dx)^{2/3}}{10d} - \frac{(4(bc-ad)) \int \frac{(a+bx)^{5/3}}{\sqrt[3]{c+dx}} dx}{5d} \\
 &= -\frac{12(bc-ad)(a+bx)^{5/3}(c+dx)^{2/3}}{35d^2} + \frac{3(a+bx)^{8/3}(c+dx)^{2/3}}{10d} + \frac{(4(bc-ad)^2) \int \frac{(a+bx)^{2/3}}{\sqrt[3]{c+dx}} dx}{7d^2} \\
 &= \frac{3(bc-ad)^2(a+bx)^{2/3}(c+dx)^{2/3}}{7d^3} - \frac{12(bc-ad)(a+bx)^{5/3}(c+dx)^{2/3}}{35d^2} + \frac{3(a+bx)^{8/3}(c+dx)^2}{10d} \\
 &= \frac{3(bc-ad)^2(a+bx)^{2/3}(c+dx)^{2/3}}{7d^3} - \frac{12(bc-ad)(a+bx)^{5/3}(c+dx)^{2/3}}{35d^2} + \frac{3(a+bx)^{8/3}(c+dx)^2}{10d} \\
 &= \frac{3(bc-ad)^2(a+bx)^{2/3}(c+dx)^{2/3}}{7d^3} - \frac{12(bc-ad)(a+bx)^{5/3}(c+dx)^{2/3}}{35d^2} + \frac{3(a+bx)^{8/3}(c+dx)^2}{10d} \\
 &= \frac{3(bc-ad)^2(a+bx)^{2/3}(c+dx)^{2/3}}{7d^3} - \frac{12(bc-ad)(a+bx)^{5/3}(c+dx)^{2/3}}{35d^2} + \frac{3(a+bx)^{8/3}(c+dx)^2}{10d} \\
 &= \frac{3(bc-ad)^2(a+bx)^{2/3}(c+dx)^{2/3}}{7d^3} - \frac{12(bc-ad)(a+bx)^{5/3}(c+dx)^{2/3}}{35d^2} + \frac{3(a+bx)^{8/3}(c+dx)^2}{10d}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.05

$$\frac{3(a+bx)^{11/3} \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{3}, \frac{11}{3}; \frac{14}{3}; \frac{d(a+bx)}{ad-bc}\right)}{11b\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(8/3)/(c + d*x)^(1/3), x]

[Out] $(3*(a + b*x)^{(11/3)*((b*(c + d*x))/(b*c - a*d))^{(1/3)}*Hypergeometric2F1[1/3, 11/3, 14/3, (d*(a + b*x))/(-(b*c) + a*d)])/(11*b*(c + d*x)^{(1/3)})$

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(b^2x^2 + 2abx + a^2)(bx + a)^{\frac{2}{3}}}{(dx + c)^{\frac{1}{3}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(8/3)/(d*x+c)^(1/3),x, algorithm="fricas")`

[Out] `integral((b^2*x^2 + 2*a*b*x + a^2)*(b*x + a)^(2/3)/(d*x + c)^(1/3), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{8}{3}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(8/3)/(d*x+c)^(1/3),x, algorithm="giac")`

[Out] `integrate((b*x + a)^(8/3)/(d*x + c)^(1/3), x)`

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{8}{3}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(8/3)/(d*x+c)^(1/3),x)`

[Out] `int((b*x+a)^(8/3)/(d*x+c)^(1/3),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{8}{3}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(8/3)/(d*x+c)^(1/3),x, algorithm="maxima")`

[Out] integrate((b*x + a)^(8/3)/(d*x + c)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{8/3}}{(c + dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(8/3)/(c + d*x)^(1/3), x)

[Out] int((a + b*x)^(8/3)/(c + d*x)^(1/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{8}{3}}}{\sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(8/3)/(d*x+c)**(1/3), x)

[Out] Integral((a + b*x)**(8/3)/(c + d*x)**(1/3), x)

= 0.316, Rules used = {50, 62, 623, 303, 218, 1877}

$$15\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{\frac{(bc-ad)^4}{(bc+ad+2bdx)^2}}$$

$$28\sqrt[3]{2}b^{2/3}d^{8/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/3)/(c + d*x)^(1/3), x]

[Out] (-15*(b*c - a*d)*(a + b*x)^(2/3)*(c + d*x)^(2/3))/(28*d^2) + (3*(a + b*x)^(5/3)*(c + d*x)^(2/3))/(7*d) + (15*(b*c - a*d)^2*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/((14*2^(1/3)*b^(2/3)*d^(8/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))) - (15*3^(1/4)*Sqrt[2 - Sqrt[3]]*(b*c - a*d)^(8/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2)*EllipticE[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(28*2^(1/3)*b^(2/3)*d^(8/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3)))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2]) + (5*3^(3/4)*(b*c - a*d)^(8/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2)*EllipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(7*2^(5/6)*b^(2/3)*d^(8/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3)))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[

```
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 303

```
Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
], s = Denom[Rt[b/a, 3]]}, Dist[(Sqrt[2]*s)/(Sqrt[2 + Sqrt[3]]*r), Int[1/Sq
rt[a + b*x^3], x], x] + Dist[1/r, Int[((1 - Sqrt[3])*s + r*x)/Sqrt[a + b*x^
3], x], x]] /; FreeQ[{a, b}, x] && PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rule 1877

```
Int[((c_) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = N
umer[Simplify[((1 - Sqrt[3])*d)/c]], s = Denom[Simplify[((1 - Sqrt[3])*d)/c
]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 + Sqrt[3])*s + r*x)), x] - S
imp[(3^(1/4)*Sqrt[2 - Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/(
(1 + Sqrt[3])*s + r*x)^2]*EllipticE[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + Sq
rt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(r^2*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/
((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b, c, d}, x] && PosQ[a] && Eq
```

Q[$b*c^3 - 2*(5 - 3*\text{Sqrt}[3])*a*d^3, 0]$

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{5/3}}{\sqrt[3]{c+dx}} dx &= \frac{3(a+bx)^{5/3}(c+dx)^{2/3}}{7d} - \frac{(5(bc-ad)) \int \frac{(a+bx)^{2/3}}{\sqrt[3]{c+dx}} dx}{7d} \\
 &= -\frac{15(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}{28d^2} + \frac{3(a+bx)^{5/3}(c+dx)^{2/3}}{7d} + \frac{(5(bc-ad)^2) \int \frac{1}{\sqrt[3]{a+bx}\sqrt[3]{c+dx}} dx}{14d^2} \\
 &= -\frac{15(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}{28d^2} + \frac{3(a+bx)^{5/3}(c+dx)^{2/3}}{7d} + \frac{(5(bc-ad)^2 \sqrt[3]{(a+bx)(c+dx)})}{14d^2 \sqrt[3]{a+bx}} \\
 &= -\frac{15(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}{28d^2} + \frac{3(a+bx)^{5/3}(c+dx)^{2/3}}{7d} + \frac{(15(bc-ad)^2 \sqrt[3]{(a+bx)(c+dx)})}{14d^2 \sqrt[3]{a+bx}} \\
 &= -\frac{15(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}{28d^2} + \frac{3(a+bx)^{5/3}(c+dx)^{2/3}}{7d} + \frac{(15(bc-ad)^2 \sqrt[3]{(a+bx)(c+dx)})}{14d^2 \sqrt[3]{a+bx}} \\
 &= -\frac{15(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}{28d^2} + \frac{3(a+bx)^{5/3}(c+dx)^{2/3}}{7d} + \frac{15(bc-ad)^2 \sqrt[3]{(a+bx)(c+dx)}}{14\sqrt[3]{2} b^{2/3} d^{8/3} \sqrt[3]{a+bx} \sqrt[3]{c+dx}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.05

$$\frac{3(a+bx)^{8/3} \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{3}, \frac{8}{3}; \frac{11}{3}; \frac{d(a+bx)}{ad-bc}\right)}{8b\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/3)/(c + d*x)^(1/3), x]

[Out] (3*(a + b*x)^(8/3)*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[1/3, 8/3, 11/3, (d*(a + b*x))/(-b*c + a*d)]/(8*b*(c + d*x)^(1/3))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{5}{3}}}{(dx+c)^{\frac{1}{3}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/3)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] integral((b*x + a)^(5/3)/(d*x + c)^(1/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{3}}}{(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/3)/(d*x + c)^(1/3), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{3}}}{(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/3)/(d*x+c)^(1/3),x)

[Out] int((b*x+a)^(5/3)/(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{3}}}{(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/3)/(d*x + c)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{5/3}}{(c + dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/3)/(c + d*x)^(1/3), x)

[Out] int((a + b*x)^(5/3)/(c + d*x)^(1/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{5/3}}{\sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/3)/(d*x+c)**(1/3), x)

[Out] Integral((a + b*x)**(5/3)/(c + d*x)**(1/3), x)

$$3.1596 \quad \int \frac{(a+bx)^{2/3}}{\sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=1293

$$3\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{\frac{(bc-ad)^{4/3}-2^2}{(bc-ad)^{4/3}-2^2}}$$

$$4\sqrt[3]{2}b^{2/3}d^{5/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)\sqrt{\frac{(bc-ad)^{4/3}-2^2}{(bc-ad)^{4/3}-2^2}}$$

[Out] $\frac{3}{4}(bx+a)^{2/3}(dx+c)^{2/3}/d-3/4(-ad+bc)*((bx+a)*(dx+c))^{1/3}*((2*b*d*x+a*d+b*c)^2)^{1/2}*((a*d+b*(2*d*x+c))^2)^{1/2}*2^{2/3}/b^{2/3}/d^{5/3}/(bx+a)^{1/3}/(dx+c)^{1/3}/(2*b*d*x+a*d+b*c)/(2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}+(-a*d+b*c)^{2/3}*(1+3^{1/2})))-1/2*3^{3/4}*(-a*d+b*c)^{5/3}*((bx+a)*(dx+c))^{1/3}*(-a*d+b*c)^{2/3}+2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}*EllipticF((2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}+(-a*d+b*c)^{2/3}*(1-3^{1/2}))/((2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}+(-a*d+b*c)^{2/3}*(1+3^{1/2}))), I*3^{1/2}+2*I)*((2*b*d*x+a*d+b*c)^2)^{1/2}*((-a*d+b*c)^{4/3}-2^{2/3}*b^{1/3}*d^{1/3}*(-a*d+b*c)^{2/3}*((bx+a)*(dx+c))^{1/3}+2*2^{1/3}*b^{2/3}*d^{2/3}*((bx+a)*(dx+c))^{2/3}))/((2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}+(-a*d+b*c)^{2/3}*(1+3^{1/2}))^2)^{1/2}*2^{1/6}/b^{2/3}/d^{5/3}/(bx+a)^{1/3}/(dx+c)^{1/3}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{1/2}/((-a*d+b*c)^{2/3}*((-a*d+b*c)^{2/3}+2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}))/((2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}+(-a*d+b*c)^{2/3}*(1+3^{1/2}))^2)^{1/2}+3/8*3^{1/4}*(-a*d+b*c)^{5/3}*((bx+a)*(dx+c))^{1/3}*(-a*d+b*c)^{2/3}+2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}*EllipticE((2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}+(-a*d+b*c)^{2/3}*(1-3^{1/2}))/((2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}+(-a*d+b*c)^{2/3}*(1+3^{1/2}))), I*3^{1/2}+2*I)*((2*b*d*x+a*d+b*c)^2)^{1/2}*(1/2*6^{1/2}-1/2*2^{1/2})*(((-a*d+b*c)^{4/3}-2^{2/3}*b^{1/3}*d^{1/3}*(-a*d+b*c)^{2/3}*((bx+a)*(dx+c))^{1/3}+2*2^{1/3}*b^{2/3}*d^{2/3}*((bx+a)*(dx+c))^{2/3}))/((2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}+(-a*d+b*c)^{2/3}*(1+3^{1/2}))^2)^{1/2}*2^{2/3}/b^{2/3}/d^{5/3}/(bx+a)^{1/3}/(dx+c)^{1/3}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{1/2}/((-a*d+b*c)^{2/3}*((-a*d+b*c)^{2/3}+2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}))/((2^{2/3}*b^{1/3}*d^{1/3}*((bx+a)*(dx+c))^{1/3}+(-a*d+b*c)^{2/3}*(1+3^{1/2}))^2)^{1/2}$

Rubi [A] time = 1.56, antiderivative size = 1293, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {50, 62, 623, 303, 218, 1877}

$$3\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{(bc-ad)^{4/3}-}$$

$$4\sqrt[3]{2}b^{2/3}d^{5/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(2/3)/(c + d*x)^(1/3), x]

[Out] (3*(a + b*x)^(2/3)*(c + d*x)^(2/3))/(4*d) - (3*(b*c - a*d)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/(2*2^(1/3)*b^(2/3)*d^(5/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))) + (3*3^(1/4)*Sqrt[2 - Sqrt[3]]*(b*c - a*d)^(5/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2*EllipticE[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(4*2^(1/3)*b^(2/3)*d^(5/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^(1/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2*Sqrt[(a*d + b*(c + 2*d*x))^2] - (3^(3/4)*(b*c - a*d)^(5/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2*EllipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(2^(5/6)*b^(2/3)*d^(5/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2*Sqrt[(a*d + b*(c + 2*d*x))^2])

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/

```
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]]/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 303

```
Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
], s = Denom[Rt[b/a, 3]]}, Dist[(Sqrt[2]*s)/(Sqrt[2 + Sqrt[3]]*r), Int[1/Sq
rt[a + b*x^3], x], x] + Dist[1/r, Int[((1 - Sqrt[3])*s + r*x)/Sqrt[a + b*x^
3], x], x]] /; FreeQ[{a, b}, x] && PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rule 1877

```
Int[((c_) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = N
umer[Simplify[((1 - Sqrt[3])*d)/c]], s = Denom[Simplify[((1 - Sqrt[3])*d)/c
]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 + Sqrt[3])*s + r*x)), x] - S
imp[(3^(1/4)*Sqrt[2 - Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/
(1 + Sqrt[3])*s + r*x]^2]*EllipticE[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + S
qrt[3])*s + r*x)], -7 - 4*Sqrt[3]]/(r^2*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/
((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b, c, d}, x] && PosQ[a] && Eq
```

Q[b*c^3 - 2*(5 - 3*sqrt[3])*a*d^3, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{2/3}}{\sqrt[3]{c+dx}} dx &= \frac{3(a+bx)^{2/3}(c+dx)^{2/3}}{4d} - \frac{(bc-ad) \int \frac{1}{\sqrt[3]{a+bx} \sqrt[3]{c+dx}} dx}{2d} \\
 &= \frac{3(a+bx)^{2/3}(c+dx)^{2/3}}{4d} - \frac{\left((bc-ad) \sqrt[3]{(a+bx)(c+dx)}\right) \int \frac{1}{\sqrt[3]{ac+(bc+ad)x+bdx^2}} dx}{2d \sqrt[3]{a+bx} \sqrt[3]{c+dx}} \\
 &= \frac{3(a+bx)^{2/3}(c+dx)^{2/3}}{4d} - \frac{\left(3(bc-ad) \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}\right) \text{Subst}\left(\int \frac{\sqrt{-4ab}}{\sqrt{-4ab}}\right)}{2d \sqrt[3]{a+bx} \sqrt[3]{c+dx} (bc+ad+2bdx)} \\
 &= \frac{3(a+bx)^{2/3}(c+dx)^{2/3}}{4d} - \frac{\left(3(bc-ad) \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}\right) \text{Subst}\left(\int \frac{(1-\sqrt{3})}{\sqrt{-4}}\right)}{2 \cdot 2^{2/3} \sqrt[3]{b} d^{4/3} \sqrt[3]{a+bx} \sqrt[3]{c+dx} (bc+ad+2bdx)} \\
 &= \frac{3(a+bx)^{2/3}(c+dx)^{2/3}}{4d} - \frac{3(bc-ad) \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}}{2 \sqrt[3]{2} b^{2/3} d^{5/3} \sqrt[3]{a+bx} \sqrt[3]{c+dx} (bc+ad+2bdx) \left((1+\sqrt{3})(bc-ad)\right)}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.06

$$\frac{3(a+bx)^{5/3} \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{3}, \frac{5}{3}, \frac{8}{3}, \frac{d(a+bx)}{ad-bc}\right)}{5b \sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(2/3)/(c + d*x)^(1/3), x]

[Out] (3*(a + b*x)^(5/3)*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[1/3, 5/3, 8/3, (d*(a + b*x))/(-b*c) + a*d])/(5*b*(c + d*x)^(1/3))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{2}{3}}}{(dx+c)^{\frac{1}{3}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] integral((b*x + a)^(2/3)/(d*x + c)^(1/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{2}{3}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(2/3)/(d*x + c)^(1/3), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{2}{3}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(2/3)/(d*x+c)^(1/3),x)

[Out] int((b*x+a)^(2/3)/(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{2}{3}}}{(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(2/3)/(d*x + c)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{\frac{2}{3}}}{(c + dx)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(2/3)/(c + d*x)^(1/3), x)
```

```
[Out] int((a + b*x)^(2/3)/(c + d*x)^(1/3), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(a + bx)^{\frac{2}{3}}}{\sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(2/3)/(d*x+c)**(1/3), x)
```

```
[Out] Integral((a + b*x)**(2/3)/(c + d*x)**(1/3), x)
```

$$3.1597 \quad \int \frac{1}{\sqrt[3]{a+bx} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=1257

$$3\sqrt[4]{3} \sqrt{2 - \sqrt{3}} (bc - ad)^{2/3} \sqrt[3]{(a + bx)(c + dx)} \sqrt{(bc + ad + 2bdx)^2} \left((bc - ad)^{2/3} + 2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} \right)$$

$$2\sqrt[3]{2} b^{2/3} d^{2/3} \sqrt[3]{a + bx} \sqrt[3]{c + dx} (bc + ad + 2bdx)$$

[Out] $\frac{3}{2} \cdot ((b*x+a)*(d*x+c))^{1/3} \cdot ((2*b*d*x+a*d+b*c)^2)^{1/2} \cdot ((a*d+b*(2*d*x+c))^2)^{1/2} \cdot 2^{2/3} / b^{2/3} / d^{2/3} / (b*x+a)^{1/3} / (d*x+c)^{1/3} / (2*b*d*x+a*d+b*c) / (2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1+3^{1/2})) + 2^{1/6} * 3^{3/4} * (-a*d+b*c)^{2/3} * ((b*x+a)*(d*x+c))^{1/3} * ((-a*d+b*c)^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3}) * \text{EllipticF}((2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1-3^{1/2})) / (2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1+3^{1/2}))), I * 3^{1/2} + 2 * I) \cdot ((2*b*d*x+a*d+b*c)^2)^{1/2} \cdot (((-a*d+b*c)^{4/3} - 2^{2/3} * b^{1/3} * d^{1/3} * (-a*d+b*c)^{2/3} * ((b*x+a)*(d*x+c))^{1/3} + 2 * 2^{1/3} * b^{2/3} * d^{2/3} * ((b*x+a)*(d*x+c))^{2/3}) / (2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1+3^{1/2})))^2)^{1/2} / b^{2/3} / d^{2/3} / (b*x+a)^{1/3} / (d*x+c)^{1/3} / (2*b*d*x+a*d+b*c) / ((a*d+b*(2*d*x+c))^2)^{1/2} / ((-a*d+b*c)^{2/3} * (-a*d+b*c)^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3}) / (2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1+3^{1/2})))^2)^{1/2} - 3/4 * 3^{1/4} * (-a*d+b*c)^{2/3} * ((b*x+a)*(d*x+c))^{1/3} * ((-a*d+b*c)^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3}) * \text{EllipticE}((2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1-3^{1/2})) / (2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1+3^{1/2}))), I * 3^{1/2} + 2 * I) \cdot ((2*b*d*x+a*d+b*c)^2)^{1/2} \cdot (1/2 * 6^{1/2} - 1/2 * 2^{1/2}) * (((-a*d+b*c)^{4/3} - 2^{2/3} * b^{1/3} * d^{1/3} * (-a*d+b*c)^{2/3} * ((b*x+a)*(d*x+c))^{1/3} + 2 * 2^{1/3} * b^{2/3} * d^{2/3} * ((b*x+a)*(d*x+c))^{2/3}) / (2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1+3^{1/2})))^2)^{1/2} * 2^{2/3} / b^{2/3} / d^{2/3} / (b*x+a)^{1/3} / (d*x+c)^{1/3} / (2*b*d*x+a*d+b*c) / ((a*d+b*(2*d*x+c))^2)^{1/2} / (((-a*d+b*c)^{2/3} * ((-a*d+b*c)^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3}) / (2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1+3^{1/2})))^2)^{1/2}$

Rubi [A] time = 1.18, antiderivative size = 1257, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {62, 623, 303, 218, 1877}

$$3\sqrt[4]{3} \sqrt{2 - \sqrt{3}} (bc - ad)^{2/3} \sqrt[3]{(a + bx)(c + dx)} \sqrt{(bc + ad + 2bdx)^2} \left((bc - ad)^{2/3} + 2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} \right)$$

$$2\sqrt[3]{2} b^{2/3} d^{2/3} \sqrt[3]{a + bx} \sqrt[3]{c + dx} (bc + ad + 2bdx)$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/3)*(c + d*x)^(1/3)),x]

[Out] (3*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/(2^(1/3)*b^(2/3)*d^(2/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))) - (3*3^(1/4)*Sqrt[2 - Sqrt[3]]*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2)*EllipticE[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(2*2^(1/3)*b^(2/3)*d^(2/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2]) + (2^(1/6)*3^(3/4)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2)*EllipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(b^(2/3)*d^(2/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])

Rule 62

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(a + b*x)^m*(c + d*x)^m]/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x

+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[3, Denominator[m], 4]

Rule 218

Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + Sqrt[3])*s + r*x)]], -7 - 4*Sqrt[3])]/(3^(1/4)*r*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b}, x] && PosQ[a]

Rule 303

Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Dist[(Sqrt[2]*s)/(Sqrt[2 + Sqrt[3]]*r), Int[1/Sqrt[a + b*x^3], x], x] + Dist[1/r, Int[((1 - Sqrt[3])*s + r*x)/Sqrt[a + b*x^3], x], x] /; FreeQ[{a, b}, x] && PosQ[a]

Rule 623

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rule 1877

Int[((c_) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Simplify[((1 - Sqrt[3])*d)/c]], s = Denom[Simplify[((1 - Sqrt[3])*d)/c]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 + Sqrt[3])*s + r*x)), x] - Simp[(3^(1/4)*Sqrt[2 - Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticE[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + Sqrt[3])*s + r*x)]], -7 - 4*Sqrt[3])]/(r^2*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b, c, d}, x] && PosQ[a] && EqQ[b*c^3 - 2*(5 - 3*Sqrt[3])*a*d^3, 0]

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt[3]{a+bx}\sqrt[3]{c+dx}} dx &= \frac{\sqrt[3]{(a+bx)(c+dx)} \int \frac{1}{\sqrt[3]{ac+(bc+ad)x+bdx^2}} dx}{\sqrt[3]{a+bx}\sqrt[3]{c+dx}} \\
&= \frac{(3\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}) \operatorname{Subst}\left(\int \frac{x}{\sqrt{-4abcd+(bc+ad)^2+4bdx^3}} dx, x, \sqrt[3]{a+bx}\right)}{\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)} \\
&= \frac{(3\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}) \operatorname{Subst}\left(\int \frac{(1-\sqrt{3})(bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}x}{\sqrt{-4abcd+(bc+ad)^2+4bdx^3}} dx, x, \sqrt[3]{a+bx}\right)}{2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)} \\
&= \frac{3\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\sqrt{(ad+b(c+2dx))^2}}{\sqrt[3]{2}b^{2/3}d^{2/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)\left((1+\sqrt{3})(bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{a+bx}\right)}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.06

$$\frac{3(a+bx)^{2/3}\sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{3}, \frac{2}{3}, \frac{5}{3}, \frac{d(a+bx)}{ad-bc}\right)}{2b\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/3)*(c + d*x)^(1/3)), x]

[Out] (3*(a + b*x)^(2/3)*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[1/3, 2/3, 5/3, (d*(a + b*x))/(-b*c + a*d)]/(2*b*(c + d*x)^(1/3))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\operatorname{integral}\left(\frac{(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{2}{3}}}{bdx^2+ac+(bc+ad)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3)/(d*x+c)^(1/3), x, algorithm="fricas")

[Out] integral((b*x + a)^(2/3)*(d*x + c)^(2/3)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{3}}(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/3)*(d*x + c)^(1/3)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{3}}(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/3)/(d*x+c)^(1/3),x)

[Out] int(1/(b*x+a)^(1/3)/(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{3}}(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/3)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{\frac{1}{3}}(c + dx)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/3)*(c + d*x)^(1/3)),x)

[Out] int(1/((a + b*x)^(1/3)*(c + d*x)^(1/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[3]{a + bx} \sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(1/3)/(d*x+c)**(1/3),x)
```

```
[Out] Integral(1/((a + b*x)**(1/3)*(c + d*x)**(1/3)), x)
```


= 0.316, Rules used = {51, 62, 623, 303, 218, 1877}

$$3\sqrt[4]{3} \sqrt{2 - \sqrt{3}} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} \sqrt{(bc + ad + 2bdx)^2} \left((bc - ad)^{2/3} + 2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} \right) \sqrt{\frac{(bc - ad)^2}{(bc - ad)^2 + 2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)}}}$$

$$2\sqrt[3]{2} b^{2/3} \sqrt[3]{bc - ad} \sqrt[3]{a + bx} \sqrt[3]{c + dx} (bc + ad + 2bdx)$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(4/3)*(c + d*x)^(1/3)), x]

[Out] (-3*(c + d*x)^(2/3))/((b*c - a*d)*(a + b*x)^(1/3)) + (3*d^(1/3)*((a + b*x)*(c + d*x)^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/((2^(1/3)*b^(2/3)*(b*c - a*d)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))) - (3*3^(1/4)*Sqrt[2 - Sqrt[3]]*d^(1/3)*((a + b*x)*(c + d*x)^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2)*EllipticE[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(2*2^(1/3)*b^(2/3)*(b*c - a*d)^(1/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3)))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2]) + (2^(1/6)*3^(3/4)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2)*EllipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(b^(2/3)*(b*c - a*d)^(1/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3)))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[

$((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] - \text{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[m, -1] \&\& !(\text{LtQ}[n, -1] \&\& (\text{EqQ}[a, 0] \mid\mid (\text{NeQ}[c, 0] \&\& \text{LtQ}[m - n, 0] \&\& \text{IntegerQ}[n]))) \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 62

$\text{Int}[(a + b*x)^m*(c + d*x)^m, x_Symbol] := \text{Dist}[(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, \text{Int}[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[3, \text{Denominator}[m], 4]$

Rule 218

$\text{Int}[1/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(2*\text{Sqrt}[2 + \text{Sqrt}[3]]*(s + r*x)*\text{Sqrt}[(s^2 - r*s*x + r^2*x^2)/((1 + \text{Sqrt}[3])*s + r*x)^2]*\text{EllipticF}[\text{ArcSin}[(1 - \text{Sqrt}[3])*s + r*x]/((1 + \text{Sqrt}[3])*s + r*x)], -7 - 4*\text{Sqrt}[3]]/(3^{1/4}*r*\text{Sqrt}[a + b*x^3]*\text{Sqrt}[(s*(s + r*x))/((1 + \text{Sqrt}[3])*s + r*x)^2]), x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a]$

Rule 303

$\text{Int}[x/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[2]*s)/(\text{Sqrt}[2 + \text{Sqrt}[3]]*r), \text{Int}[1/\text{Sqrt}[a + b*x^3], x], x] + \text{Dist}[1/r, \text{Int}[(1 - \text{Sqrt}[3])*s + r*x]/\text{Sqrt}[a + b*x^3], x], x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a]$

Rule 623

$\text{Int}[(a + b*x + c*x^2)^p, x_Symbol] := \text{With}\{d = \text{Denominator}[p]\}, \text{Dist}[(d*\text{Sqrt}[(b + 2*c*x)^2])/(b + 2*c*x), \text{Subst}[\text{Int}[x^{d*(p + 1) - 1}/\text{Sqrt}[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^{(1/d)}, x] /; 3 \leq d \leq 4] /; \text{FreeQ}\{a, b, c\}, x] \&\& \text{NeQ}[b^2 - 4*a*c, 0] \&\& \text{RationalQ}[p]$

Rule 1877

$\text{Int}[(c + d*x)/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}\{r = \text{Numer}[\text{Simplify}[(1 - \text{Sqrt}[3])*d]/c], s = \text{Denom}[\text{Simplify}[(1 - \text{Sqrt}[3])*d]/c]\}, \text{Simp}[(2*d*s^3*\text{Sqrt}[a + b*x^3])/(a*r^2*((1 + \text{Sqrt}[3])*s + r*x)), x] - \text{Simp}[(3^{1/4}*\text{Sqrt}[2 - \text{Sqrt}[3]]*d*s*(s + r*x)*\text{Sqrt}[(s^2 - r*s*x + r^2*x^2)/((1 + \text{Sqrt}[3])*s + r*x)^2]*\text{EllipticE}[\text{ArcSin}[(1 - \text{Sqrt}[3])*s + r*x]/((1 + \text{Sqrt}[3])*s + r*x)], -7 - 4*\text{Sqrt}[3]]/(r^2*\text{Sqrt}[a + b*x^3]*\text{Sqrt}[(s*(s + r*x))/((1 + \text{Sqrt}[3])*s + r*x)^2]), x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{PosQ}[a] \&\& \text{Eq}$

Q[$b^3c^3 - 2(5 - 3\sqrt{3})a^3d^3, 0]$

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{4/3} \sqrt[3]{c+dx}} dx &= -\frac{3(c+dx)^{2/3}}{(bc-ad)\sqrt[3]{a+bx}} + \frac{d \int \frac{1}{\sqrt[3]{a+bx} \sqrt[3]{c+dx}} dx}{bc-ad} \\
 &= -\frac{3(c+dx)^{2/3}}{(bc-ad)\sqrt[3]{a+bx}} + \frac{(d\sqrt[3]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[3]{ac+(bc+ad)x+bdx^2}} dx}{(bc-ad)\sqrt[3]{a+bx} \sqrt[3]{c+dx}} \\
 &= -\frac{3(c+dx)^{2/3}}{(bc-ad)\sqrt[3]{a+bx}} + \frac{(3d\sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}) \text{Subst}\left(\int \frac{1}{\sqrt{-4abcd}}\right)}{(bc-ad)\sqrt[3]{a+bx} \sqrt[3]{c+dx} (bc+ad+2bdx)} \\
 &= -\frac{3(c+dx)^{2/3}}{(bc-ad)\sqrt[3]{a+bx}} + \frac{(3d^{2/3} \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}) \text{Subst}\left(\int \frac{(1-\sqrt{-4abcd})}{\sqrt{-4abcd}}\right)}{2^{2/3} \sqrt[3]{b} (bc-ad)\sqrt[3]{a+bx} \sqrt[3]{c+dx} (bc+ad+2bdx)} \\
 &= -\frac{3(c+dx)^{2/3}}{(bc-ad)\sqrt[3]{a+bx}} + \frac{3\sqrt[3]{d} \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}}{\sqrt[3]{2} b^{2/3} (bc-ad)\sqrt[3]{a+bx} \sqrt[3]{c+dx} (bc+ad+2bdx) \left((1+\sqrt{3})\right)}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.05

$$\frac{3\sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{3}, \frac{1}{3}, \frac{2}{3}, \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[3]{a+bx} \sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(4/3)*(c + d*x)^(1/3)), x]

[Out] (-3*((b*(c + d*x))/(b*c - a*d))^(1/3)*Hypergeometric2F1[-1/3, 1/3, 2/3, (d*(a + b*x))/(-b*c) + a*d])/(b*(a + b*x)^(1/3)*(c + d*x)^(1/3))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{2}{3}}}{b^2dx^3+a^2c+(b^2c+2abd)x^2+(2abc+a^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(4/3)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] integral((b*x + a)^(2/3)*(d*x + c)^(2/3)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{4}{3}}(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(4/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(4/3)*(d*x + c)^(1/3)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{4}{3}}(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(4/3)/(d*x+c)^(1/3),x)

[Out] int(1/(b*x+a)^(4/3)/(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{4}{3}}(dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(4/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(4/3)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{\frac{4}{3}}(c + dx)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(4/3)*(c + d*x)^(1/3)), x)`

[Out] `int(1/((a + b*x)^(4/3)*(c + d*x)^(1/3)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{4}{3}} \sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(4/3)/(d*x+c)**(1/3), x)`

[Out] `Integral(1/((a + b*x)**(4/3)*(c + d*x)**(1/3)), x)`

$$3.1599 \quad \int \frac{1}{(a+bx)^{7/3} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=1335

$$3\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{(bc-ad)^{4/3}-2^2}$$

$$4\sqrt[3]{2}b^{2/3}(bc-ad)^{4/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)\sqrt{\quad}$$

[Out]
$$\begin{aligned} & -3/4*(d*x+c)^{(2/3)/(-a*d+b*c)/(b*x+a)^{(4/3)+3/2*d*(d*x+c)^{(2/3)/(-a*d+b*c)} \\ & 2/(b*x+a)^{(1/3)-3/4*d^{(4/3)*((b*x+a)*(d*x+c))^{(1/3)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*((a*d+b*(2*d*x+c))^2)^{(1/2)*2^{(2/3)/b^{(2/3)/(-a*d+b*c)} \\ & 2/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))}} \\ & -1/2*3^{(3/4)*d^{(4/3)*((b*x+a)*(d*x+c))^{(1/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3))*E1 \\ & lipticF((2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1-3^{(1/2))}} \\ &)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))}} \\ &),I*3^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*(((a*d+b*c)^{(4/3)-2^{(2/3)*b^{(1/3)*d^{(1/3)*(-a*d+b*c)^{(2/3)*((b*x+a)*(d*x+c))^{(1/3)+2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((b*x+a)*(d*x+c))^{(2/3))} \\ &)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))}} \\ &)^2)^{(1/2)*2^{(1/6)/b^{(2/3)/(-a*d+b*c)^{(4/3)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3))} \\ &)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))}} \\ &)^2)^{(1/2)+3/8*3^{(1/4)*d^{(4/3)*((b*x+a)*(d*x+c))^{(1/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3))*E1 \\ & lipticE((2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1-3^{(1/2))}} \\ &)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))}} \\ &),I*3^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*(1/2*6^{(1/2)-1/2*2^{(1/2)*(((-a*d+b*c)^{(4/3)-2^{(2/3)*b^{(1/3)*d^{(1/3)*(-a*d+b*c)^{(2/3)*((b*x+a)*(d*x+c))^{(1/3)+2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((b*x+a)*(d*x+c))^{(2/3))} \\ &)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))}} \\ &)^2)^{(1/2)*2^{(2/3)/b^{(2/3)/(-a*d+b*c)^{(4/3)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3))} \\ &)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))}} \\ &)^2)^{(1/2)} \end{aligned}$$

Rubi [A] time = 2.01, antiderivative size = 1335, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {51, 62, 623, 303, 218, 1877}

$$3\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{(bc-ad)^{4/3}}$$

$$4\sqrt[3]{2}b^{2/3}(bc-ad)^{4/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/3)*(c + d*x)^(1/3)), x]

[Out]
$$\begin{aligned} & (-3*(c + d*x)^{(2/3)})/(4*(b*c - a*d)*(a + b*x)^{(4/3)}) + (3*d*(c + d*x)^{(2/3)}) \\ &)/(2*(b*c - a*d)^2*(a + b*x)^{(1/3)}) - (3*d^{(4/3)}*((a + b*x)*(c + d*x))^{(1/3)} \\ &)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2]/(2*2^{(1/3)}*b \\ & ^{(2/3)}*(b*c - a*d)^2*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)}*(b*c + a*d + 2*b*d*x)* \\ & ((1 + Sqrt[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + \\ & d*x))^{(1/3)})) + (3*3^{(1/4)}*Sqrt[2 - Sqrt[3]]*d^{(4/3)}*((a + b*x)*(c + d*x))^{(1/3)} \\ &)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)} \\ &)*((a + b*x)*(c + d*x))^{(1/3)})*Sqrt[((b*c - a*d)^{(4/3)} - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)} \\ &)*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)}*b^{(2/3)} \\ & *d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)})/((1 + Sqrt[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)} \\ &)*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2*EllipticE[ArcSin[((1 - Sqrt[3]) \\ &)*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}) \\ &]^{(1/3)}/((1 + Sqrt[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b \\ & *x)*(c + d*x))^{(1/3)}), -7 - 4*Sqrt[3]]]/(4*2^{(1/3)}*b^{(2/3)}*(b*c - a*d)^{(4/3)} \\ &)*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)}*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^{(2/3)} \\ &)*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}) \\ &]/((1 + Sqrt[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x) \\ &)*(c + d*x))^{(1/3)})^2*Sqrt[(a*d + b*(c + 2*d*x))^2] - (3^{(3/4)}*d^{(4/3)}*((a \\ & + b*x)*(c + d*x))^{(1/3)}*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + \\ & 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*Sqrt[((b*c - a*d)^{(4/3)} \\ &) - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} \\ & + 2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)})/((1 + Sqrt[3])*(b*c \\ & - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2*El \\ & lipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(\\ & (a + b*x)*(c + d*x))^{(1/3)})/((1 + Sqrt[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)} \\ &)*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})], -7 - 4*Sqrt[3]]]/(2^{(5/6)}*b^{(2/3)} \\ &)*(b*c - a*d)^{(4/3)}*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)}*(b*c + a*d + 2*b*d*x)*S \\ & qrt[((b*c - a*d)^{(2/3)}*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b \\ & *x)*(c + d*x))^{(1/3)})/((1 + Sqrt[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d \\ & ^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2]*Sqrt[(a*d + b*(c + 2*d*x))^2] \end{aligned}$$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[

$((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] - \text{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[m, -1] \&\& !(\text{LtQ}[n, -1] \&\& (\text{EqQ}[a, 0] \mid\mid (\text{NeQ}[c, 0] \&\& \text{LtQ}[m - n, 0] \&\& \text{IntegerQ}[n]))) \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 62

$\text{Int}[(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, \text{Int}[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[3, \text{Denominator}[m], 4]$

Rule 218

$\text{Int}[1/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(2*\text{Sqrt}[2 + \text{Sqrt}[3]]*(s + r*x)*\text{Sqrt}[(s^2 - r*s*x + r^2*x^2)/((1 + \text{Sqrt}[3])*s + r*x)^2]*\text{EllipticF}[\text{ArcSin}[(1 - \text{Sqrt}[3])*s + r*x]/((1 + \text{Sqrt}[3])*s + r*x)], -7 - 4*\text{Sqrt}[3]])/(3^{1/4}*r*\text{Sqrt}[a + b*x^3]*\text{Sqrt}[(s*(s + r*x))/((1 + \text{Sqrt}[3])*s + r*x)^2]), x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a]$

Rule 303

$\text{Int}[x/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[2]*s)/(\text{Sqrt}[2 + \text{Sqrt}[3]]*r), \text{Int}[1/\text{Sqrt}[a + b*x^3], x], x] + \text{Dist}[1/r, \text{Int}[(1 - \text{Sqrt}[3])*s + r*x]/\text{Sqrt}[a + b*x^3], x], x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a]$

Rule 623

$\text{Int}[(a + b*x + c*x^2)^p, x_Symbol] := \text{With}[\{d = \text{Denominator}[p]\}, \text{Dist}[(d*\text{Sqrt}[(b + 2*c*x)^2])/(b + 2*c*x), \text{Subst}[\text{Int}[x^{d*(p + 1) - 1}/\text{Sqrt}[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^{(1/d)}, x] /; 3 \leq d \leq 4] /; \text{FreeQ}\{a, b, c\}, x] \&\& \text{NeQ}[b^2 - 4*a*c, 0] \&\& \text{RationalQ}[p]$

Rule 1877

$\text{Int}[(c + d*x)/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}[\{r = \text{Numer}[\text{Simplify}[(1 - \text{Sqrt}[3])*d]/c], s = \text{Denom}[\text{Simplify}[(1 - \text{Sqrt}[3])*d]/c]\}, \text{Simp}[(2*d*s^3*\text{Sqrt}[a + b*x^3])/(a*r^2*((1 + \text{Sqrt}[3])*s + r*x)), x] - \text{Simp}[(3^{1/4}*\text{Sqrt}[2 - \text{Sqrt}[3]]*d*s*(s + r*x)*\text{Sqrt}[(s^2 - r*s*x + r^2*x^2)/((1 + \text{Sqrt}[3])*s + r*x)^2]*\text{EllipticE}[\text{ArcSin}[(1 - \text{Sqrt}[3])*s + r*x]/((1 + \text{Sqrt}[3])*s + r*x)], -7 - 4*\text{Sqrt}[3]])/(r^2*\text{Sqrt}[a + b*x^3]*\text{Sqrt}[(s*(s + r*x))/((1 + \text{Sqrt}[3])*s + r*x)^2]), x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{PosQ}[a] \&\& \text{Eq}$

Q[$b^3 c^3 - 2(5 - 3\sqrt{3}) a d^3, 0]$

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{7/3} \sqrt[3]{c+dx}} dx &= -\frac{3(c+dx)^{2/3}}{4(bc-ad)(a+bx)^{4/3}} - \frac{d \int \frac{1}{(a+bx)^{4/3} \sqrt[3]{c+dx}} dx}{2(bc-ad)} \\
 &= -\frac{3(c+dx)^{2/3}}{4(bc-ad)(a+bx)^{4/3}} + \frac{3d(c+dx)^{2/3}}{2(bc-ad)^2 \sqrt[3]{a+bx}} - \frac{d^2 \int \frac{1}{\sqrt[3]{a+bx} \sqrt[3]{c+dx}} dx}{2(bc-ad)^2} \\
 &= -\frac{3(c+dx)^{2/3}}{4(bc-ad)(a+bx)^{4/3}} + \frac{3d(c+dx)^{2/3}}{2(bc-ad)^2 \sqrt[3]{a+bx}} - \frac{(d^2 \sqrt[3]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[3]{ac+(bc+ad)x}} dx}{2(bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}} \\
 &= -\frac{3(c+dx)^{2/3}}{4(bc-ad)(a+bx)^{4/3}} + \frac{3d(c+dx)^{2/3}}{2(bc-ad)^2 \sqrt[3]{a+bx}} - \frac{(3d^2 \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad-x)}) \int \frac{1}{\sqrt[3]{ac+(bc+ad)x}} dx}{2(bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}} \\
 &= -\frac{3(c+dx)^{2/3}}{4(bc-ad)(a+bx)^{4/3}} + \frac{3d(c+dx)^{2/3}}{2(bc-ad)^2 \sqrt[3]{a+bx}} - \frac{(3d^{5/3} \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad-x)}) \int \frac{1}{\sqrt[3]{ac+(bc+ad)x}} dx}{2 \cdot 2^{2/3} \sqrt[3]{a+bx} \sqrt[3]{c+dx}} \\
 &= -\frac{3(c+dx)^{2/3}}{4(bc-ad)(a+bx)^{4/3}} + \frac{3d(c+dx)^{2/3}}{2(bc-ad)^2 \sqrt[3]{a+bx}} - \frac{3d^{4/3} \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad-x)} \int \frac{1}{\sqrt[3]{ac+(bc+ad)x}} dx}{2 \sqrt[3]{2} b^{2/3} (bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.05

$$\frac{3 \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{4}{3}, \frac{1}{3}; -\frac{1}{3}; \frac{d(a+bx)}{ad-bc}\right)}{4b(a+bx)^{4/3} \sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/3)*(c + d*x)^(1/3)),x]

[Out] $(-3*((b*(c + d*x))/(b*c - a*d))^(1/3)*\text{Hypergeometric2F1}[-4/3, 1/3, -1/3, (d*(a + b*x))/(-b*c + a*d)])/(4*b*(a + b*x)^(4/3)*(c + d*x)^(1/3))$

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{2}{3}}}{b^3dx^4+a^3c+(b^3c+3ab^2d)x^3+3(ab^2c+a^2bd)x^2+(3a^2bc+a^3d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/3)/(d*x+c)^(1/3),x, algorithm="fricas")

[Out] integral((b*x + a)^(2/3)*(d*x + c)^(2/3)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/3)/(d*x+c)^(1/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/3)*(d*x + c)^(1/3)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/3)/(d*x+c)^(1/3),x)

[Out] int(1/(b*x+a)^(7/3)/(d*x+c)^(1/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{3}}(dx+c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/3)/(d*x+c)^(1/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(7/3)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{7/3} (c + dx)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/3)*(c + d*x)^(1/3)), x)

[Out] int(1/((a + b*x)^(7/3)*(c + d*x)^(1/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{7}{3}} \sqrt[3]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/3)/(d*x+c)**(1/3), x)

[Out] Integral(1/((a + b*x)**(7/3)*(c + d*x)**(1/3)), x)

$$3.1600 \quad \int \frac{1}{(a+bx)^{10/3} \sqrt[3]{c+dx}} dx$$

Optimal. Leaf size=1372

$$15\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{(bc-ad)^{4/3}}$$

$$28\sqrt[3]{2}b^{2/3}(bc-ad)^{7/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)$$

[Out] $-3/7*(d*x+c)^{(2/3)/(-a*d+b*c)/(b*x+a)^{(7/3)+15/28*d*(d*x+c)^{(2/3)/(-a*d+b*c)}$
 $)^{2/(b*x+a)^{(4/3)-15/14*d^2*(d*x+c)^{(2/3)/(-a*d+b*c)^3/(b*x+a)^{(1/3)+15/28*$
 $d^{(7/3)*((b*x+a)*(d*x+c))^{(1/3)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*((a*d+b*(2*d*x+$
 $c))^2)^{(1/2)*2^{(2/3)/b^{(2/3)/(-a*d+b*c)^3/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*$
 $d*x+a*d+b*c)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2$
 $/3)*(1+3^{(1/2)))+5/14*3^{(3/4)*d^{(7/3)*((b*x+a)*(d*x+c))^{(1/3)*((-a*d+b*c)^{($
 $2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3))*EllipticF((2^{(2/3)*b^{$
 $(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1-3^{(1/2)))/(2^{(2/3}$
 $)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))}, I*3$
 $^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*((-a*d+b*c)^{(4/3)-2^{(2/3)*b^{(1/3)*$
 $d^{(1/3)*(-a*d+b*c)^{(2/3)*((b*x+a)*(d*x+c))^{(1/3)+2*2^{(1/3)*b^{(2/3)*d^{(2/3)*$
 $((b*x+a)*(d*x+c))^{(2/3)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-$
 $a*d+b*c)^{(2/3)*(1+3^{(1/2))})^2)^{(1/2)*2^{(1/6)/b^{(2/3)/(-a*d+b*c)^{(7/3)/(b*x$
 $+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)/((-a*$
 $d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1$
 $/3)))/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3$
 $^{(1/2))})^2)^{(1/2)-15/56*3^{(1/4)*d^{(7/3)*((b*x+a)*(d*x+c))^{(1/3)*((-a*d+b*c)$
 $^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3))*EllipticE((2^{(2/3)*$
 $b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1-3^{(1/2)))/(2^{(2$
 $/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))}, I$
 $*3^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*(1/2*6^{(1/2)-1/2*2^{(1/2)))*((-a*d$
 $+b*c)^{(4/3)-2^{(2/3)*b^{(1/3)*d^{(1/3)*(-a*d+b*c)^{(2/3)*((b*x+a)*(d*x+c))^{(1/3}$
 $)+2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((b*x+a)*(d*x+c))^{(2/3)/(2^{(2/3)*b^{(1/3)*d^{(1/$
 $3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^2)^{(1/2)*2^{(2/3)/b$
 $^{(2/3)/(-a*d+b*c)^{(7/3)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/((a*d$
 $+b*(2*d*x+c))^2)^{(1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*$
 $d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))$
 $^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^2)^{(1/2)}$

Rubi [A] time = 2.44, antiderivative size = 1372, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {51, 62, 623, 303, 218, 1877}

$$15\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{\frac{(bc-ad)^4}{(bc-ad)^4}}$$

$$28\sqrt[3]{2}b^{2/3}(bc-ad)^{7/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(10/3)*(c + d*x)^(1/3)), x]

[Out]
$$\begin{aligned} & \frac{-3(c + d*x)^{(2/3)}}{(7*(b*c - a*d)*(a + b*x)^{(7/3))} + (15*d*(c + d*x)^{(2/3)})} \\ & \frac{)}{(28*(b*c - a*d)^2*(a + b*x)^{(4/3))} - (15*d^2*(c + d*x)^{(2/3)})}{(14*(b*c - a*d)^3*(a + b*x)^{(1/3))} + (15*d^{(7/3)}*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]}/(14*2^{(1/3)}*b^{(2/3)}*(b*c - a*d)^3*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)}*(b*c + a*d + 2*b*d*x)*((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})) - (15*3^{(1/4)}*\text{Sqrt}[2 - \text{Sqrt}[3]]*d^{(7/3)}*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*\text{Sqrt}[(b*c - a*d)^{(4/3)} - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)})}/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2*\text{EllipticE}[\text{ArcSin}[\frac{(1 - \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}}{(1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}}], -7 - 4*\text{Sqrt}[3]])/(28*2^{(1/3)}*b^{(2/3)}*(b*c - a*d)^{(7/3)}*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(b*c - a*d)^{(2/3)}*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})]/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2] + (5*3^{(3/4)}*d^{(7/3)}*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*\text{Sqrt}[(b*c - a*d)^{(4/3)} - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)})}/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2*\text{EllipticF}[\text{ArcSin}[\frac{(1 - \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}}{(1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}}], -7 - 4*\text{Sqrt}[3]])/(7*2^{(5/6)}*b^{(2/3)}*(b*c - a*d)^{(7/3)}*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(b*c - a*d)^{(2/3)}*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})]/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]$$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)]/((1 + Sqrt[3])*s + r*x)^2*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]]]/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 303

```
Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
], s = Denom[Rt[b/a, 3]]}, Dist[(Sqrt[2]*s)/(Sqrt[2 + Sqrt[3]]*r), Int[1/Sq
rt[a + b*x^3], x], x] + Dist[1/r, Int[((1 - Sqrt[3])*s + r*x)/Sqrt[a + b*x^
3], x], x]] /; FreeQ[{a, b}, x] && PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rule 1877

```
Int[((c_.) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = N
umer[Simplify[((1 - Sqrt[3])*d)/c]], s = Denom[Simplify[((1 - Sqrt[3])*d)/c
]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 + Sqrt[3])*s + r*x)), x] - S
imp[(3^(1/4)*Sqrt[2 - Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)]/
((1 + Sqrt[3])*s + r*x)^2*EllipticE[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + S
qrt[3])*s + r*x)], -7 - 4*Sqrt[3]]]/(r^2*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/
```

((1 + Sqrt[3])*s + r*x)^2)), x]] /; FreeQ[{a, b, c, d}, x] && PosQ[a] && EqQ[b*c^3 - 2*(5 - 3*Sqrt[3])*a*d^3, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{10/3} \sqrt[3]{c+dx}} dx &= -\frac{3(c+dx)^{2/3}}{7(bc-ad)(a+bx)^{7/3}} - \frac{(5d) \int \frac{1}{(a+bx)^{7/3} \sqrt[3]{c+dx}} dx}{7(bc-ad)} \\
 &= -\frac{3(c+dx)^{2/3}}{7(bc-ad)(a+bx)^{7/3}} + \frac{15d(c+dx)^{2/3}}{28(bc-ad)^2(a+bx)^{4/3}} + \frac{(5d^2) \int \frac{1}{(a+bx)^{4/3} \sqrt[3]{c+dx}} dx}{14(bc-ad)^2} \\
 &= -\frac{3(c+dx)^{2/3}}{7(bc-ad)(a+bx)^{7/3}} + \frac{15d(c+dx)^{2/3}}{28(bc-ad)^2(a+bx)^{4/3}} - \frac{15d^2(c+dx)^{2/3}}{14(bc-ad)^3 \sqrt[3]{a+bx}} + \frac{(5d^3) \int \frac{1}{(a+bx)^{1/3} \sqrt[3]{c+dx}} dx}{14(bc-ad)^3} \\
 &= -\frac{3(c+dx)^{2/3}}{7(bc-ad)(a+bx)^{7/3}} + \frac{15d(c+dx)^{2/3}}{28(bc-ad)^2(a+bx)^{4/3}} - \frac{15d^2(c+dx)^{2/3}}{14(bc-ad)^3 \sqrt[3]{a+bx}} + \frac{(5d^3) \sqrt[3]{c+dx}}{14(bc-ad)^3} \\
 &= -\frac{3(c+dx)^{2/3}}{7(bc-ad)(a+bx)^{7/3}} + \frac{15d(c+dx)^{2/3}}{28(bc-ad)^2(a+bx)^{4/3}} - \frac{15d^2(c+dx)^{2/3}}{14(bc-ad)^3 \sqrt[3]{a+bx}} + \frac{(15d^3) \sqrt[3]{c+dx}}{14(bc-ad)^3} \\
 &= -\frac{3(c+dx)^{2/3}}{7(bc-ad)(a+bx)^{7/3}} + \frac{15d(c+dx)^{2/3}}{28(bc-ad)^2(a+bx)^{4/3}} - \frac{15d^2(c+dx)^{2/3}}{14(bc-ad)^3 \sqrt[3]{a+bx}} + \frac{(15d^8) \sqrt[3]{c+dx}}{14(bc-ad)^3} \\
 &= -\frac{3(c+dx)^{2/3}}{7(bc-ad)(a+bx)^{7/3}} + \frac{15d(c+dx)^{2/3}}{28(bc-ad)^2(a+bx)^{4/3}} - \frac{15d^2(c+dx)^{2/3}}{14(bc-ad)^3 \sqrt[3]{a+bx}} + \frac{(15d^8) \sqrt[3]{c+dx}}{14 \sqrt[3]{2}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.05

$$\frac{3 \sqrt[3]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{7}{3}, \frac{1}{3}; -\frac{4}{3}; \frac{d(a+bx)}{ad-bc}\right)}{7b(a+bx)^{7/3} \sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(10/3)*(c + d*x)^(1/3)),x]

[Out] $(-3*((b*(c + d*x))/(b*c - a*d))^{1/3} * \text{Hypergeometric2F1}[-7/3, 1/3, -4/3, (d*(a + b*x))/(-(b*c) + a*d)]) / (7*b*(a + b*x)^{7/3} * (c + d*x)^{1/3})$

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^{\frac{2}{3}} (dx + c)^{\frac{2}{3}}}{b^4 dx^5 + a^4 c + (b^4 c + 4 ab^3 d)x^4 + 2(2 ab^3 c + 3 a^2 b^2 d)x^3 + 2(3 a^2 b^2 c + 2 a^3 b d)x^2 + (4 a^3 b c + a^4 d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(10/3)/(d*x+c)^(1/3),x, algorithm="fricas")`

[Out] `integral((b*x + a)^(2/3)*(d*x + c)^(2/3)/(b^4*d*x^5 + a^4*c + (b^4*c + 4*a*b^3*d)*x^4 + 2*(2*a*b^3*c + 3*a^2*b^2*d)*x^3 + 2*(3*a^2*b^2*c + 2*a^3*b*d)*x^2 + (4*a^3*b*c + a^4*d)*x), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{10}{3}} (dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(10/3)/(d*x+c)^(1/3),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(10/3)*(d*x + c)^(1/3)), x)`

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{10}{3}} (dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(10/3)/(d*x+c)^(1/3),x)`

[Out] `int(1/(b*x+a)^(10/3)/(d*x+c)^(1/3),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{10}{3}} (dx + c)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(10/3)/(d*x+c)^(1/3),x, algorithm="maxima")`

[Out] integrate(1/((b*x + a)^(10/3)*(d*x + c)^(1/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + b x)^{10/3} (c + d x)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(10/3)*(c + d*x)^(1/3)), x)

[Out] int(1/((a + b*x)^(10/3)*(c + d*x)^(1/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + b x)^{10/3} \sqrt[3]{c + d x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(10/3)/(d*x+c)**(1/3), x)

[Out] Integral(1/((a + b*x)**(10/3)*(c + d*x)**(1/3)), x)

$$3.1601 \quad \int \frac{(a+bx)^{5/3}}{(c+dx)^{2/3}} dx$$

Optimal. Leaf size=216

$$\frac{5(bc-ad)^2 \log(c+dx)}{18\sqrt[3]{b}d^{8/3}} - \frac{5(bc-ad)^2 \log\left(\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{b}\sqrt[3]{c+dx}} - 1\right)}{6\sqrt[3]{b}d^{8/3}} - \frac{5(bc-ad)^2 \tan^{-1}\left(\frac{2\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt{3}\sqrt[3]{b}\sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{3\sqrt{3}\sqrt[3]{b}d^{8/3}} - \frac{5(a+bx)^{2/3}\sqrt[3]{c+dx}}{6d^2}$$

[Out] $-5/6*(-a*d+b*c)*(b*x+a)^{(2/3)}*(d*x+c)^{(1/3)}/d^{2+1/2}*(b*x+a)^{(5/3)}*(d*x+c)^{(1/3)}/d-5/18*(-a*d+b*c)^2*\ln(d*x+c)/b^{(1/3)}/d^{(8/3)}-5/6*(-a*d+b*c)^2*\ln(-1+d^{(1/3)}*(b*x+a)^{(1/3)}/b^{(1/3)}/(d*x+c)^{(1/3)})/b^{(1/3)}/d^{(8/3)}-5/9*(-a*d+b*c)^2*\arctan(1/3*3^{(1/2)}+2/3*d^{(1/3)}*(b*x+a)^{(1/3)}/b^{(1/3)}/(d*x+c)^{(1/3)}*3^{(1/2)})/b^{(1/3)}/d^{(8/3)}*3^{(1/2)}$

Rubi [A] time = 0.08, antiderivative size = 216, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {50, 59}

$$\frac{5(a+bx)^{2/3}\sqrt[3]{c+dx}(bc-ad)}{6d^2} - \frac{5(bc-ad)^2 \log(c+dx)}{18\sqrt[3]{b}d^{8/3}} - \frac{5(bc-ad)^2 \log\left(\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{b}\sqrt[3]{c+dx}} - 1\right)}{6\sqrt[3]{b}d^{8/3}} - \frac{5(bc-ad)^2 \tan^{-1}\left(\frac{2\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt{3}\sqrt[3]{b}\sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{3\sqrt{3}\sqrt[3]{b}d^{8/3}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(5/3)}/(c + d*x)^{(2/3)}, x]$

[Out] $(-5*(b*c - a*d)*(a + b*x)^{(2/3)}*(c + d*x)^{(1/3)})/(6*d^2) + ((a + b*x)^{(5/3)}*(c + d*x)^{(1/3)})/(2*d) - (5*(b*c - a*d)^2*\text{ArcTan}[1/\text{Sqrt}[3] + (2*d^{(1/3)}*(a + b*x)^{(1/3)})/(\text{Sqrt}[3]*b^{(1/3)}*(c + d*x)^{(1/3)})]/(3*\text{Sqrt}[3]*b^{(1/3)}*d^{(8/3)}) - (5*(b*c - a*d)^2*\text{Log}[c + d*x]/(18*b^{(1/3)}*d^{(8/3)}) - (5*(b*c - a*d)^2*\text{Log}[-1 + (d^{(1/3)}*(a + b*x)^{(1/3)})/(b^{(1/3)}*(c + d*x)^{(1/3)})]/(6*b^{(1/3)}*d^{(8/3)}))$

Rule 50

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 59


```
Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] :=
  With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt
  [3]*(c + d*x)^(1/3)) + 1/Sqrt[3]])/d, x] + (-Simp[(3*q*Log[(q*(a + b*x)^(1/
  3))]/(c + d*x)^(1/3) - 1])/(2*d), x] - Simp[(q*Log[c + d*x])/(2*d), x]] /;
  FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]
```

Rubi steps

$$\begin{aligned} \int \frac{(a + bx)^{5/3}}{(c + dx)^{2/3}} dx &= \frac{(a + bx)^{5/3} \sqrt[3]{c + dx}}{2d} - \frac{(5(bc - ad)) \int \frac{(a+bx)^{2/3}}{(c+dx)^{2/3}} dx}{6d} \\ &= -\frac{5(bc - ad)(a + bx)^{2/3} \sqrt[3]{c + dx}}{6d^2} + \frac{(a + bx)^{5/3} \sqrt[3]{c + dx}}{2d} + \frac{(5(bc - ad)^2) \int \frac{1}{\sqrt[3]{a+bx}(c+dx)^{2/3}} dx}{9d^2} \\ &= -\frac{5(bc - ad)(a + bx)^{2/3} \sqrt[3]{c + dx}}{6d^2} + \frac{(a + bx)^{5/3} \sqrt[3]{c + dx}}{2d} - \frac{5(bc - ad)^2 \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}}\right)}{3\sqrt{3} \sqrt[3]{b} d^{8/3}} \end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.34

$$\frac{3(a + bx)^{8/3} \left(\frac{b(c+dx)}{bc-ad}\right)^{2/3} {}_2F_1\left(\frac{2}{3}, \frac{8}{3}; \frac{11}{3}; \frac{d(a+bx)}{ad-bc}\right)}{8b(c + dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/3)/(c + d*x)^(2/3), x]

[Out] (3*(a + b*x)^(8/3)*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[2/3, 8/3, 11/3, (d*(a + b*x))/(-b*c) + a*d])/(8*b*(c + d*x)^(2/3))

fricas [B] time = 0.47, size = 741, normalized size = 3.43

$$\left[\frac{15 \sqrt{\frac{1}{3}} (b^3 c^2 d - 2 a b^2 c d^2 + a^2 b d^3) \sqrt{\frac{(-b d^2)^{\frac{1}{3}}}{b}} \log \left(-3 b d^2 x - 2 b c d - a d^2 - 3 (-b d^2)^{\frac{1}{3}} (b x + a)^{\frac{2}{3}} (d x + c)^{\frac{1}{3}} d - 3 \sqrt{\dots} \right)}{\dots} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/3)/(d*x+c)^(2/3),x, algorithm="fricas")

[Out] [1/18*(15*sqrt(1/3)*(b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*sqrt((-b*d^2)^(1/3)/b)*log(-3*b*d^2*x - 2*b*c*d - a*d^2 - 3*(-b*d^2)^(1/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3)*d - 3*sqrt(1/3)*(2*(b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) + (-b*d^2)^(1/3)*(b*d*x + a*d)))*sqrt((-b*d^2)^(1/3)/b) - 10*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(-b*d^2)^(2/3)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (-b*d^2)^(2/3)*(b*x + a))/(b*x + a)) + 5*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(-b*d^2)^(2/3)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d + (-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (-b*d^2)^(1/3)*(b*d*x + a*d))/(b*x + a)) + 3*(3*b^2*d^3*x - 5*b^2*c*d^2 + 8*a*b*d^3)*(b*x + a)^(2/3)*(d*x + c)^(1/3))/(b*d^4), 1/18*(30*sqrt(1/3)*(b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*sqrt(-(-b*d^2)^(1/3)/b)*arctan(sqrt(1/3)*(2*(-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (-b*d^2)^(1/3)*(b*d*x + a*d)))*sqrt(-(-b*d^2)^(1/3)/b)/(b*d^2*x + a*d^2)) - 10*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(-b*d^2)^(2/3)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (-b*d^2)^(2/3)*(b*x + a))/(b*x + a)) + 5*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(-b*d^2)^(2/3)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d + (-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (-b*d^2)^(1/3)*(b*d*x + a*d))/(b*x + a)) + 3*(3*b^2*d^3*x - 5*b^2*c*d^2 + 8*a*b*d^3)*(b*x + a)^(2/3)*(d*x + c)^(1/3))/(b*d^4)]

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/3)/(d*x + c)^(2/3), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/3)/(d*x+c)^(2/3),x)

[Out] int((b*x+a)^(5/3)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/3)/(d*x + c)^(2/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{\frac{5}{3}}}{(c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/3)/(c + d*x)^(2/3), x)

[Out] int((a + b*x)^(5/3)/(c + d*x)^(2/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{3}}}{(c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/3)/(d*x+c)**(2/3), x)

[Out] Integral((a + b*x)**(5/3)/(c + d*x)**(2/3), x)

$$3.1602 \quad \int \frac{(a+bx)^{2/3}}{(c+dx)^{2/3}} dx$$

Optimal. Leaf size=169

$$\frac{(bc-ad)\log(c+dx)}{3\sqrt[3]{b}d^{5/3}} + \frac{(bc-ad)\log\left(\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{b}\sqrt[3]{c+dx}} - 1\right)}{\sqrt[3]{b}d^{5/3}} + \frac{2(bc-ad)\tan^{-1}\left(\frac{2\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt{3}\sqrt[3]{b}\sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{\sqrt{3}\sqrt[3]{b}d^{5/3}} + \frac{(a+bx)^{2/3}\sqrt[3]{c+dx}}{d}$$

[Out] (b*x+a)^(2/3)*(d*x+c)^(1/3)/d+1/3*(-a*d+b*c)*ln(d*x+c)/b^(1/3)/d^(5/3)+(-a*d+b*c)*ln(-1+d^(1/3)*(b*x+a)^(1/3)/b^(1/3)/(d*x+c)^(1/3))/b^(1/3)/d^(5/3)+2/3*(-a*d+b*c)*arctan(1/3*3^(1/2)+2/3*d^(1/3)*(b*x+a)^(1/3)/b^(1/3)/(d*x+c)^(1/3)*3^(1/2))/b^(1/3)/d^(5/3)*3^(1/2)

Rubi [A] time = 0.04, antiderivative size = 169, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {50, 59}

$$\frac{(bc-ad)\log(c+dx)}{3\sqrt[3]{b}d^{5/3}} + \frac{(bc-ad)\log\left(\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{b}\sqrt[3]{c+dx}} - 1\right)}{\sqrt[3]{b}d^{5/3}} + \frac{2(bc-ad)\tan^{-1}\left(\frac{2\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt{3}\sqrt[3]{b}\sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{\sqrt{3}\sqrt[3]{b}d^{5/3}} + \frac{(a+bx)^{2/3}\sqrt[3]{c+dx}}{d}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(2/3)/(c + d*x)^(2/3), x]

[Out] ((a + b*x)^(2/3)*(c + d*x)^(1/3))/d + (2*(b*c - a*d)*ArcTan[1/Sqrt[3] + (2*d^(1/3)*(a + b*x)^(1/3))/(Sqrt[3]*b^(1/3)*(c + d*x)^(1/3))]/(Sqrt[3]*b^(1/3)*d^(5/3)) + ((b*c - a*d)*Log[c + d*x])/(3*b^(1/3)*d^(5/3)) + ((b*c - a*d)*Log[-1 + (d^(1/3)*(a + b*x)^(1/3))/(b^(1/3)*(c + d*x)^(1/3))])/(b^(1/3)*d^(5/3))

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 59

```
Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] :=
With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt
```

$[3]*(c + d*x)^{(1/3)} + 1/\text{Sqrt}[3]]/d, x] + (-\text{Simp}[(3*q*\text{Log}[(q*(a + b*x))^{(1/3)}]/(c + d*x)^{(1/3)} - 1])/(2*d), x] - \text{Simp}[(q*\text{Log}[c + d*x])/(2*d), x]) /;$
 $\text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{PosQ}[d/b]$

Rubi steps

$$\int \frac{(a + bx)^{2/3}}{(c + dx)^{2/3}} dx = \frac{(a + bx)^{2/3} \sqrt[3]{c + dx}}{d} - \frac{(2(bc - ad)) \int \frac{1}{\sqrt[3]{a+bx}(c+dx)^{2/3}} dx}{3d}$$

$$= \frac{(a + bx)^{2/3} \sqrt[3]{c + dx}}{d} + \frac{2(bc - ad) \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}}\right)}{\sqrt{3} \sqrt[3]{b} d^{5/3}} + \frac{(bc - ad) \log(c + dx)}{3\sqrt[3]{b} d^{5/3}} + \frac{(bc - ad)}{3\sqrt[3]{b} d^{5/3}}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.43

$$\frac{3(a + bx)^{5/3} \left(\frac{b(c+dx)}{bc-ad}\right)^{2/3} {}_2F_1\left(\frac{2}{3}, \frac{5}{3}; \frac{8}{3}; \frac{d(a+bx)}{ad-bc}\right)}{5b(c + dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(2/3)/(c + d*x)^(2/3), x]

[Out] (3*(a + b*x)^(5/3)*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[2/3, 5/3, 8/3, (d*(a + b*x))/(-b*c) + a*d])/(5*b*(c + d*x)^(2/3))

fricas [B] time = 0.47, size = 619, normalized size = 3.66

$$\left[\frac{3(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{1}{3}}bd^2 - 3\sqrt{\frac{1}{3}}(b^2cd - abd^2)\sqrt{\frac{(-bd^2)^{\frac{1}{3}}}{b}} \log\left(-3bd^2x - 2bcd - ad^2 - 3(-bd^2)^{\frac{1}{3}}(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{1}{3}}\right)}{5b(c + dx)^{\frac{2}{3}}}\right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/(d*x+c)^(2/3), x, algorithm="fricas")

```
[Out] [1/3*(3*(b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d^2 - 3*sqrt(1/3)*(b^2*c*d - a*b*d^2)*sqrt((-b*d^2)^(1/3)/b)*log(-3*b*d^2*x - 2*b*c*d - a*d^2 - 3*(-b*d^2)^(1/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3)*d - 3*sqrt(1/3)*(2*(b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) + (-b*d^2)^(1/3)*(b*d*x + a*d))*sqrt((-b*d^2)^(1/3)/b)) + 2*(-b*d^2)^(2/3)*(b*c - a*d)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (-b*d^2)^(2/3)*(b*x + a))/(b*x + a)) - (-b*d^2)^(2/3)*(b*c - a*d)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d + (-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (-b*d^2)^(1/3)*(b*d*x + a*d))/(b*x + a)))/(b*d^3), 1/3*(3*(b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d^2 - 6*sqrt(1/3)*(b^2*c*d - a*b*d^2)*sqrt(-(-b*d^2)^(1/3)/b)*arctan(sqrt(1/3)*(2*(-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (-b*d^2)^(1/3)*(b*d*x + a*d))*sqrt(-(-b*d^2)^(1/3)/b)/(b*d^2*x + a*d^2)) + 2*(-b*d^2)^(2/3)*(b*c - a*d)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (-b*d^2)^(2/3)*(b*x + a))/(b*x + a)) - (-b*d^2)^(2/3)*(b*c - a*d)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d + (-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (-b*d^2)^(1/3)*(b*d*x + a*d))/(b*x + a)))/(b*d^3)]
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{2}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(2/3)/(d*x+c)^(2/3),x, algorithm="giac")
```

```
[Out] integrate((b*x + a)^(2/3)/(d*x + c)^(2/3), x)
```

maple [F] time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{2}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((b*x+a)^(2/3)/(d*x+c)^(2/3),x)
```

```
[Out] int((b*x+a)^(2/3)/(d*x+c)^(2/3),x)
```

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{2}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(2/3)/(d*x + c)^(2/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{2/3}}{(c + dx)^{2/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(2/3)/(c + d*x)^(2/3), x)

[Out] int((a + b*x)^(2/3)/(c + d*x)^(2/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{2}{3}}}{(c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(2/3)/(d*x+c)**(2/3), x)

[Out] Integral((a + b*x)**(2/3)/(c + d*x)**(2/3), x)

$$3.1603 \quad \int \frac{1}{\sqrt[3]{a+bx} (c+dx)^{2/3}} dx$$

Optimal. Leaf size=126

$$-\frac{3 \log\left(\frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}} - 1\right)}{2\sqrt[3]{b} d^{2/3}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{\sqrt[3]{b} d^{2/3}} - \frac{\log(c+dx)}{2\sqrt[3]{b} d^{2/3}}$$

[Out] $-1/2*\ln(d*x+c)/b^{(1/3)}/d^{(2/3)}-3/2*\ln(-1+d^{(1/3)}*(b*x+a)^{(1/3)}/b^{(1/3)}/(d*x+c)^{(1/3)})/b^{(1/3)}/d^{(2/3)}-\arctan(1/3*3^{(1/2)}+2/3*d^{(1/3)}*(b*x+a)^{(1/3)}/b^{(1/3)}/(d*x+c)^{(1/3)}*3^{(1/2)})*3^{(1/2)}/b^{(1/3)}/d^{(2/3)}$

Rubi [A] time = 0.02, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {59}

$$-\frac{3 \log\left(\frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}} - 1\right)}{2\sqrt[3]{b} d^{2/3}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}} + \frac{1}{\sqrt{3}}\right)}{\sqrt[3]{b} d^{2/3}} - \frac{\log(c+dx)}{2\sqrt[3]{b} d^{2/3}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/3)*(c + d*x)^(2/3)), x]

[Out] $-\left(\frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}}\right]}{\sqrt{3} \sqrt[3]{b} d^{2/3}} + \frac{\log(c+dx)}{2\sqrt[3]{b} d^{2/3}}\right) - \frac{3 \log\left(-1 + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}}\right)}{2\sqrt[3]{b} d^{2/3}}$

Rule 59

Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] :=
 With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt[3]*(c + d*x)^(1/3) + 1/Sqrt[3]])]/d, x] + (-Simp[(3*q*Log[(q*(a + b*x)^(1/3))/(c + d*x)^(1/3) - 1])]/(2*d), x] - Simp[(q*Log[c + d*x])/(2*d), x])] /;
 FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]

Rubi steps

$$\int \frac{1}{\sqrt[3]{a+bx} (c+dx)^{2/3}} dx = -\frac{\sqrt{3} \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt{3} \sqrt[3]{b} \sqrt[3]{c+dx}}\right)}{\sqrt[3]{b} d^{2/3}} - \frac{\log(c+dx)}{2\sqrt[3]{b} d^{2/3}} - \frac{3 \log\left(-1 + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{b} \sqrt[3]{c+dx}}\right)}{2\sqrt[3]{b} d^{2/3}}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.58

$$\frac{3(a + bx)^{2/3} \left(\frac{b(c+dx)}{bc-ad}\right)^{2/3} {}_2F_1\left(\frac{2}{3}, \frac{2}{3}; \frac{5}{3}; \frac{d(a+bx)}{ad-bc}\right)}{2b(c + dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/3)*(c + d*x)^(2/3)),x]

[Out] (3*(a + b*x)^(2/3)*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[2/3, 2/3, 5/3, (d*(a + b*x))/(-b*c) + a*d])/(2*b*(c + d*x)^(2/3))

fricas [B] time = 0.48, size = 521, normalized size = 4.13

$$\sqrt{3}bd\sqrt{\frac{(-bd^2)^{1/3}}{b}} \log\left(-3bd^2x - 2bcd - ad^2 - 3(-bd^2)^{1/3}(bx + a)^{2/3}(dx + c)^{1/3}d - \sqrt{3}\left(2(bx + a)^{1/3}(dx + c)^{2/3}bd - \dots\right)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3)/(d*x+c)^(2/3),x, algorithm="fricas")

[Out] [1/2*(sqrt(3)*b*d*sqrt((-b*d^2)^(1/3)/b)*log(-3*b*d^2*x - 2*b*c*d - a*d^2 - 3*(-b*d^2)^(1/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3)*d - sqrt(3)*(2*(b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d - (-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) + (-b*d^2)^(1/3)*(b*d*x + a*d))*sqrt((-b*d^2)^(1/3)/b)) - 2*(-b*d^2)^(2/3)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (-b*d^2)^(2/3)*(b*x + a))/(b*x + a)) + (-b*d^2)^(2/3)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d + (-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (-b*d^2)^(1/3)*(b*d*x + a*d))/(b*x + a)))/b*d^2, 1/2*(2*sqrt(3)*b*d*sqrt(-(-b*d^2)^(1/3)/b)*arctan(1/3*sqrt(3)*(2*(-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (-b*d^2)^(1/3)*(b*d*x + a*d))*sqrt(-(-b*d^2)^(1/3)/b)/(b*d^2*x + a*d^2)) - 2*(-b*d^2)^(2/3)*log(((b*x + a)^(2/3)*(d*x + c)^(1/3)*b*d - (-b*d^2)^(2/3)*(b*x + a))/(b*x + a)) + (-b*d^2)^(2/3)*log(((b*x + a)^(1/3)*(d*x + c)^(2/3)*b*d + (-b*d^2)^(2/3)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - (-b*d^2)^(1/3)*(b*d*x + a*d))/(b*x + a)))/b*d^2]

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/3)*(d*x + c)^(2/3)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/3)/(d*x+c)^(2/3),x)

[Out] int(1/(b*x+a)^(1/3)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/3)*(d*x + c)^(2/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{\frac{1}{3}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/3)*(c + d*x)^(2/3)),x)

[Out] int(1/((a + b*x)^(1/3)*(c + d*x)^(2/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[3]{a+bx} (c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(1/3)/(d*x+c)**(2/3),x)
```

```
[Out] Integral(1/((a + b*x)**(1/3)*(c + d*x)**(2/3)), x)
```

$$3.1604 \quad \int \frac{1}{(a+bx)^{4/3}(c+dx)^{2/3}} dx$$

Optimal. Leaf size=30

$$-\frac{3\sqrt[3]{c+dx}}{\sqrt[3]{a+bx}(bc-ad)}$$

[Out] $-3*(d*x+c)^{(1/3)/(-a*d+b*c)/(b*x+a)^{(1/3)}$

Rubi [A] time = 0.00, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{3\sqrt[3]{c+dx}}{\sqrt[3]{a+bx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)^{(4/3})*(c + d*x)^{(2/3})), x]$

[Out] $(-3*(c + d*x)^{(1/3}))/((b*c - a*d)*(a + b*x)^{(1/3})))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Simp} [((a + b*x)^{(m + 1})*(c + d*x)^{(n + 1}))/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}[\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{1}{(a+bx)^{4/3}(c+dx)^{2/3}} dx = -\frac{3\sqrt[3]{c+dx}}{(bc-ad)\sqrt[3]{a+bx}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$\frac{3\sqrt[3]{c+dx}}{\sqrt[3]{a+bx}(ad-bc)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/((a + b*x)^{(4/3})*(c + d*x)^{(2/3})), x]$

[Out] $(3*(c + d*x)^{(1/3)})/((-b*c) + a*d)*(a + b*x)^{(1/3)}$

fricas [A] time = 0.42, size = 42, normalized size = 1.40

$$\frac{3(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{1}{3}}}{abc - a^2d + (b^2c - abd)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(4/3)/(d*x+c)^(2/3),x, algorithm="fricas")`

[Out] $-3*(b*x + a)^{(2/3)}*(d*x + c)^{(1/3)}/(a*b*c - a^2*d + (b^2*c - a*b*d)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{4}{3}}(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(4/3)/(d*x+c)^(2/3),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(4/3)*(d*x + c)^(2/3)), x)`

maple [A] time = 0.00, size = 27, normalized size = 0.90

$$\frac{3(dx + c)^{\frac{1}{3}}}{(bx + a)^{\frac{1}{3}}(ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(4/3)/(d*x+c)^(2/3),x)`

[Out] $3/(b*x+a)^{(1/3)}*(d*x+c)^{(1/3)}/(a*d-b*c)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{4}{3}}(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(4/3)/(d*x+c)^(2/3),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(4/3)*(d*x + c)^(2/3)), x)`

mupad [B] time = 0.83, size = 26, normalized size = 0.87

$$\frac{3(c + dx)^{1/3}}{(ad - bc)(a + bx)^{1/3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(4/3)*(c + d*x)^(2/3)),x)`

[Out] `(3*(c + d*x)^(1/3))/((a*d - b*c)*(a + b*x)^(1/3))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{4}{3}}(c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(4/3)/(d*x+c)**(2/3),x)`

[Out] `Integral(1/((a + b*x)**(4/3)*(c + d*x)**(2/3)), x)`

$$3.1605 \quad \int \frac{1}{(a+bx)^{7/3}(c+dx)^{2/3}} dx$$

Optimal. Leaf size=66

$$\frac{9d\sqrt[3]{c+dx}}{4\sqrt[3]{a+bx}(bc-ad)^2} - \frac{3\sqrt[3]{c+dx}}{4(a+bx)^{4/3}(bc-ad)}$$

[Out] $-3/4*(d*x+c)^{(1/3)/(-a*d+b*c)/(b*x+a)^{(4/3)+9/4*d*(d*x+c)^{(1/3)/(-a*d+b*c)^2/(b*x+a)^{(1/3)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{9d\sqrt[3]{c+dx}}{4\sqrt[3]{a+bx}(bc-ad)^2} - \frac{3\sqrt[3]{c+dx}}{4(a+bx)^{4/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/3)*(c + d*x)^(2/3)), x]

[Out] $(-3*(c + d*x)^{(1/3)})/(4*(b*c - a*d)*(a + b*x)^{(4/3)} + (9*d*(c + d*x)^{(1/3)})/(4*(b*c - a*d)^2*(a + b*x)^{(1/3)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{7/3}(c+dx)^{2/3}} dx = -\frac{3\sqrt[3]{c+dx}}{4(bc-ad)(a+bx)^{4/3}} - \frac{(3d) \int \frac{1}{(a+bx)^{4/3}(c+dx)^{2/3}} dx}{4(bc-ad)}$$

$$= -\frac{3\sqrt[3]{c+dx}}{4(bc-ad)(a+bx)^{4/3}} + \frac{9d\sqrt[3]{c+dx}}{4(bc-ad)^2\sqrt[3]{a+bx}}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.70

$$\frac{3\sqrt[3]{c+dx}(4ad-bc+3bdx)}{4(a+bx)^{4/3}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/3)*(c + d*x)^(2/3)), x]

[Out] (3*(c + d*x)^(1/3)*(-(b*c) + 4*a*d + 3*b*d*x))/(4*(b*c - a*d)^2*(a + b*x)^(4/3))

fricas [B] time = 0.43, size = 118, normalized size = 1.79

$$\frac{3(3bdx - bc + 4ad)(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{1}{3}}}{4(a^2b^2c^2 - 2a^3bcd + a^4d^2 + (b^4c^2 - 2ab^3cd + a^2b^2d^2)x^2 + 2(ab^3c^2 - 2a^2b^2cd + a^3bd^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/3)/(d*x+c)^(2/3), x, algorithm="fricas")

[Out] 3/4*(3*b*d*x - b*c + 4*a*d)*(b*x + a)^(2/3)*(d*x + c)^(1/3)/(a^2*b^2*c^2 - 2*a^3*b*c*d + a^4*d^2 + (b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2)*x^2 + 2*(a*b^3*c^2 - 2*a^2*b^2*c*d + a^3*b*d^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/3)/(d*x+c)^(2/3), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/3)*(d*x + c)^(2/3)), x)

maple [A] time = 0.00, size = 54, normalized size = 0.82

$$\frac{3(dx+c)^{\frac{1}{3}}(3bdx+4ad-bc)}{4(bx+a)^{\frac{4}{3}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(7/3)/(d*x+c)^(2/3),x)`

[Out] `3/4*(d*x+c)^(1/3)*(3*b*d*x+4*a*d-b*c)/(b*x+a)^(4/3)/(a^2*d^2-2*a*b*c*d+b^2*c^2)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(7/3)/(d*x+c)^(2/3),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(7/3)*(d*x + c)^(2/3)), x)`

mupad [B] time = 0.98, size = 71, normalized size = 1.08

$$\frac{\left(\frac{9dx}{4(ad-bc)^2} + \frac{12ad-3bc}{4b(ad-bc)^2}\right)(c+dx)^{1/3}}{x(a+bx)^{1/3} + \frac{a(a+bx)^{1/3}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(7/3)*(c + d*x)^(2/3)),x)`

[Out] `((9*d*x)/(4*(a*d - b*c)^2) + (12*a*d - 3*b*c)/(4*b*(a*d - b*c)^2))*(c + d*x)^(1/3)/(x*(a + b*x)^(1/3) + (a*(a + b*x)^(1/3))/b)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{7}{3}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(7/3)/(d*x+c)**(2/3),x)`

[Out] `Integral(1/((a + b*x)**(7/3)*(c + d*x)**(2/3)), x)`

$$3.1606 \quad \int \frac{1}{(a+bx)^{10/3}(c+dx)^{2/3}} dx$$

Optimal. Leaf size=101

$$-\frac{27d^2\sqrt[3]{c+dx}}{14\sqrt[3]{a+bx}(bc-ad)^3} + \frac{9d\sqrt[3]{c+dx}}{14(a+bx)^{4/3}(bc-ad)^2} - \frac{3\sqrt[3]{c+dx}}{7(a+bx)^{7/3}(bc-ad)}$$

[Out] $-3/7*(d*x+c)^{(1/3)/(-a*d+b*c)/(b*x+a)^{(7/3)+9/14*d*(d*x+c)^{(1/3)/(-a*d+b*c)}$
 $^2/(b*x+a)^{(4/3)-27/14*d^2*(d*x+c)^{(1/3)/(-a*d+b*c)^3/(b*x+a)^{(1/3)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.105, Rules used = {45, 37}

$$-\frac{27d^2\sqrt[3]{c+dx}}{14\sqrt[3]{a+bx}(bc-ad)^3} + \frac{9d\sqrt[3]{c+dx}}{14(a+bx)^{4/3}(bc-ad)^2} - \frac{3\sqrt[3]{c+dx}}{7(a+bx)^{7/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(10/3)*(c + d*x)^(2/3)),x]

[Out] $(-3*(c + d*x)^{(1/3))/(7*(b*c - a*d)*(a + b*x)^{(7/3)} + (9*d*(c + d*x)^{(1/3)})/(14*(b*c - a*d)^2*(a + b*x)^{(4/3)} - (27*d^2*(c + d*x)^{(1/3))/(14*(b*c - a*d)^3*(a + b*x)^{(1/3)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{10/3}(c+dx)^{2/3}} dx &= -\frac{3\sqrt[3]{c+dx}}{7(bc-ad)(a+bx)^{7/3}} - \frac{(6d) \int \frac{1}{(a+bx)^{7/3}(c+dx)^{2/3}} dx}{7(bc-ad)} \\
&= -\frac{3\sqrt[3]{c+dx}}{7(bc-ad)(a+bx)^{7/3}} + \frac{9d\sqrt[3]{c+dx}}{14(bc-ad)^2(a+bx)^{4/3}} + \frac{(9d^2) \int \frac{1}{(a+bx)^{4/3}(c+dx)^{2/3}} dx}{14(bc-ad)^2} \\
&= -\frac{3\sqrt[3]{c+dx}}{7(bc-ad)(a+bx)^{7/3}} + \frac{9d\sqrt[3]{c+dx}}{14(bc-ad)^2(a+bx)^{4/3}} - \frac{27d^2\sqrt[3]{c+dx}}{14(bc-ad)^3\sqrt[3]{a+bx}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 75, normalized size = 0.74

$$-\frac{3\sqrt[3]{c+dx} (14a^2d^2 - 7abd(c-3dx) + b^2(2c^2 - 3cdx + 9d^2x^2))}{14(a+bx)^{7/3}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(10/3)*(c + d*x)^(2/3)), x]

[Out] (-3*(c + d*x)^(1/3)*(14*a^2*d^2 - 7*a*b*d*(c - 3*d*x) + b^2*(2*c^2 - 3*c*d*x + 9*d^2*x^2)))/(14*(b*c - a*d)^3*(a + b*x)^(7/3))

fricas [B] time = 0.42, size = 251, normalized size = 2.49

$$\frac{3(9b^2d^2x^2 + 2b^2c^2 - 7abcd + 14a^2d^2 - 3(b^2cd - 7abd^2)x)}{14(a^3b^3c^3 - 3a^4b^2c^2d + 3a^5bcd^2 - a^6d^3 + (b^6c^3 - 3ab^5c^2d + 3a^2b^4cd^2 - a^3b^3d^3)x^3 + 3(ab^5c^3 - 3a^2b^4c^2d + 3a^3b^3cd^2 - a^4b^2c^2d^2 + 3a^5bcd^3 - a^6d^4)x^2 + 3(a^2b^4c^3 - 3a^3b^3c^2d + 3a^4b^2cd^2 - a^5bd^3)x + 3(a^3b^3c^3 - 3a^4b^2c^2d + 3a^5bcd^2 - a^6d^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(10/3)/(d*x+c)^(2/3), x, algorithm="fricas")

[Out] -3/14*(9*b^2*d^2*x^2 + 2*b^2*c^2 - 7*a*b*c*d + 14*a^2*d^2 - 3*(b^2*c*d - 7*a*b*d^2)*x)*(b*x + a)^(2/3)*(d*x + c)^(1/3)/(a^3*b^3*c^3 - 3*a^4*b^2*c^2*d + 3*a^5*b*c*d^2 - a^6*d^3 + (b^6*c^3 - 3*a*b^5*c^2*d + 3*a^2*b^4*c*d^2 - a^3*b^3*d^3)*x^3 + 3*(a*b^5*c^3 - 3*a^2*b^4*c^2*d + 3*a^3*b^3*c*d^2 - a^4*b^2*d^3)*x^2 + 3*(a^2*b^4*c^3 - 3*a^3*b^3*c^2*d + 3*a^4*b^2*c*d^2 - a^5*b*d^3)*x + 3*(a^3*b^3*c^3 - 3*a^4*b^2*c^2*d + 3*a^5*b*c*d^2 - a^6*d^3))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{10}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(10/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(10/3)*(d*x + c)^(2/3)), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{3(dx+c)^{\frac{1}{3}}(9b^2x^2d^2+21abd^2x-3b^2cdx+14a^2d^2-7abcd+2b^2c^2)}{14(bx+a)^{\frac{7}{3}}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(10/3)/(d*x+c)^(2/3),x)

[Out] 3/14*(d*x+c)^(1/3)*(9*b^2*d^2*x^2+21*a*b*d^2*x-3*b^2*c*d*x+14*a^2*d^2-7*a*b*c*d+2*b^2*c^2)/(b*x+a)^(7/3)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{10}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(10/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(10/3)*(d*x + c)^(2/3)), x)

mupad [B] time = 1.51, size = 133, normalized size = 1.32

$$\frac{(c+dx)^{1/3} \left(\frac{27d^2x^2}{14(ad-bc)^3} + \frac{42a^2d^2-21abcd+6b^2c^2}{14b^2(ad-bc)^3} + \frac{9dx(7ad-bc)}{14b(ad-bc)^3} \right)}{x^2(a+bx)^{1/3} + \frac{a^2(a+bx)^{1/3}}{b^2} + \frac{2ax(a+bx)^{1/3}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(10/3)*(c + d*x)^(2/3)),x)

[Out] ((c + d*x)^(1/3)*((27*d^2*x^2)/(14*(a*d - b*c)^3) + (42*a^2*d^2 + 6*b^2*c^2 - 21*a*b*c*d)/(14*b^2*(a*d - b*c)^3) + (9*d*x*(7*a*d - b*c))/(14*b*(a*d - b*c)^3))/((x^2*(a + b*x)^(1/3) + (a^2*(a + b*x)^(1/3))/b^2 + (2*a*x*(a + b*x)^(1/3))/b)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{10}{3}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(10/3)/(d*x+c)**(2/3),x)
```

```
[Out] Integral(1/((a + b*x)**(10/3)*(c + d*x)**(2/3)), x)
```

$$3.1607 \quad \int \frac{1}{(a+bx)^{13/3}(c+dx)^{2/3}} dx$$

Optimal. Leaf size=136

$$\frac{243d^3\sqrt[3]{c+dx}}{140\sqrt[3]{a+bx}(bc-ad)^4} - \frac{81d^2\sqrt[3]{c+dx}}{140(a+bx)^{4/3}(bc-ad)^3} + \frac{27d\sqrt[3]{c+dx}}{70(a+bx)^{7/3}(bc-ad)^2} - \frac{3\sqrt[3]{c+dx}}{10(a+bx)^{10/3}(bc-ad)}$$

[Out] $-3/10*(d*x+c)^{(1/3)/(-a*d+b*c)/(b*x+a)^{(10/3)+27/70*d*(d*x+c)^{(1/3)/(-a*d+b*c)^2/(b*x+a)^{(7/3)-81/140*d^2*(d*x+c)^{(1/3)/(-a*d+b*c)^3/(b*x+a)^{(4/3)+243/140*d^3*(d*x+c)^{(1/3)/(-a*d+b*c)^4/(b*x+a)^{(1/3)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{243d^3\sqrt[3]{c+dx}}{140\sqrt[3]{a+bx}(bc-ad)^4} - \frac{81d^2\sqrt[3]{c+dx}}{140(a+bx)^{4/3}(bc-ad)^3} + \frac{27d\sqrt[3]{c+dx}}{70(a+bx)^{7/3}(bc-ad)^2} - \frac{3\sqrt[3]{c+dx}}{10(a+bx)^{10/3}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(13/3)*(c + d*x)^(2/3)), x]

[Out] $(-3*(c + d*x)^{(1/3))/(10*(b*c - a*d)*(a + b*x)^{(10/3)} + (27*d*(c + d*x)^{(1/3))/(70*(b*c - a*d)^2*(a + b*x)^{(7/3)} - (81*d^2*(c + d*x)^{(1/3))/(140*(b*c - a*d)^3*(a + b*x)^{(4/3)} + (243*d^3*(c + d*x)^{(1/3))/(140*(b*c - a*d)^4*(a + b*x)^{(1/3)}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{13/3}(c+dx)^{2/3}} dx &= -\frac{3\sqrt[3]{c+dx}}{10(bc-ad)(a+bx)^{10/3}} - \frac{(9d) \int \frac{1}{(a+bx)^{10/3}(c+dx)^{2/3}} dx}{10(bc-ad)} \\
&= -\frac{3\sqrt[3]{c+dx}}{10(bc-ad)(a+bx)^{10/3}} + \frac{27d\sqrt[3]{c+dx}}{70(bc-ad)^2(a+bx)^{7/3}} + \frac{(27d^2) \int \frac{1}{(a+bx)^{7/3}(c+dx)^{2/3}} dx}{35(bc-ad)^2} \\
&= -\frac{3\sqrt[3]{c+dx}}{10(bc-ad)(a+bx)^{10/3}} + \frac{27d\sqrt[3]{c+dx}}{70(bc-ad)^2(a+bx)^{7/3}} - \frac{81d^2\sqrt[3]{c+dx}}{140(bc-ad)^3(a+bx)^{4/3}} \\
&= -\frac{3\sqrt[3]{c+dx}}{10(bc-ad)(a+bx)^{10/3}} + \frac{27d\sqrt[3]{c+dx}}{70(bc-ad)^2(a+bx)^{7/3}} - \frac{81d^2\sqrt[3]{c+dx}}{140(bc-ad)^3(a+bx)^{4/3}} +
\end{aligned}$$

Mathematica [A] time = 0.05, size = 116, normalized size = 0.85

$$\frac{3\sqrt[3]{c+dx} (140a^3d^3 - 105a^2bd^2(c-3dx) + 30ab^2d(2c^2 - 3cdx + 9d^2x^2) + b^3(-14c^3 + 18c^2dx - 27cd^2x^2 + 81d^3x^3))}{140(a+bx)^{10/3}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(13/3)*(c + d*x)^(2/3)),x]

[Out] (3*(c + d*x)^(1/3)*(140*a^3*d^3 - 105*a^2*b*d^2*(c - 3*d*x) + 30*a*b^2*d*(2*c^2 - 3*c*d*x + 9*d^2*x^2) + b^3*(-14*c^3 + 18*c^2*d*x - 27*c*d^2*x^2 + 81*d^3*x^3)))/(140*(b*c - a*d)^4*(a + b*x)^(10/3))

fricas [B] time = 0.45, size = 419, normalized size = 3.08

$$\frac{3(81b^3d^3x^3 - 14b^3c^3 + 60ab^2c^2d - 140(a^4b^4c^4 - 4a^5b^3c^3d + 6a^6b^2c^2d^2 - 4a^7bcd^3 + a^8d^4 + (b^8c^4 - 4ab^7c^3d + 6a^2b^6c^2d^2 - 4a^3b^5cd^3 + a^4b^4d^4)x^4)}{140(a+bx)^{10/3}(bc-ad)^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(13/3)/(d*x+c)^(2/3),x, algorithm="fricas")

[Out] 3/140*(81*b^3*d^3*x^3 - 14*b^3*c^3 + 60*a*b^2*c^2*d - 105*a^2*b*c*d^2 + 140*a^3*d^3 - 27*(b^3*c*d^2 - 10*a*b^2*d^3)*x^2 + 9*(2*b^3*c^2*d - 10*a*b^2*c*d^2 + 35*a^2*b*d^3)*x)*(b*x + a)^(2/3)*(d*x + c)^(1/3)/(a^4*b^4*c^4 - 4*a^5*b^3*c^3*d + 6*a^6*b^2*c^2*d^2 - 4*a^7*b*c*d^3 + a^8*d^4 + (b^8*c^4 - 4*a*b^7*c^3*d + 6*a^2*b^6*c^2*d^2 - 4*a^3*b^5*c*d^3 + a^4*b^4*d^4)*x^4 + 4*(a*b^7*c^4 - 4*a^2*b^6*c^3*d + 6*a^3*b^5*c^2*d^2 - 4*a^4*b^4*c*d^3 + a^5*b^3*d^4

) $x^3 + 6(a^2b^6c^4 - 4a^3b^5c^3d + 6a^4b^4c^2d^2 - 4a^5b^3c^2d^3 + a^6b^2d^4)x^2 + 4(a^3b^5c^4 - 4a^4b^4c^3d + 6a^5b^3c^2d^2 - 4a^6b^2c^2d^3 + a^7b^2d^4)x$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{13}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(13/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(13/3)*(d*x + c)^(2/3)), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{3(dx+c)^{\frac{1}{3}}(81b^3d^3x^3 + 270ab^2d^3x^2 - 27b^3cd^2x^2 + 315a^2bd^3x - 90ab^2cd^2x + 18b^3c^2dx + 140a^3d^3 - 105a^2bcd^2)}{140(bx+a)^{\frac{10}{3}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(13/3)/(d*x+c)^(2/3),x)

[Out] $\frac{3}{140}(d*x+c)^{\frac{1}{3}}(81*b^3*d^3*x^3+270*a*b^2*d^3*x^2-27*b^3*c*d^2*x^2+315*a^2*b*d^3*x-90*a*b^2*c*d^2*x+18*b^3*c^2*d*x+140*a^3*d^3-105*a^2*b*c*d^2+60*a*b^2*c^2*d-14*b^3*c^3)/(b*x+a)^{\frac{10}{3}}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{13}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(13/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(13/3)*(d*x + c)^(2/3)), x)

mupad [B] time = 1.27, size = 209, normalized size = 1.54

$$\frac{(c+dx)^{\frac{1}{3}}\left(\frac{243d^3x^3}{140(ad-bc)^4} + \frac{420a^3d^3-315a^2bcd^2+180ab^2c^2d-42b^3c^3}{140b^3(ad-bc)^4} + \frac{27dx(35a^2d^2-10abcd+2b^2c^2)}{140b^2(ad-bc)^4} + \frac{81d^2x^2(10ad-bc)}{140b(ad-bc)^4}\right)}{x^3(a+bx)^{\frac{1}{3}} + \frac{a^3(a+bx)^{\frac{1}{3}}}{b^3} + \frac{3ax^2(a+bx)^{\frac{1}{3}}}{b} + \frac{3a^2x(a+bx)^{\frac{1}{3}}}{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a + b*x)^(13/3)*(c + d*x)^(2/3)),x)
```

```
[Out] ((c + d*x)^(1/3)*((243*d^3*x^3)/(140*(a*d - b*c)^4) + (420*a^3*d^3 - 42*b^3*c^3 + 180*a*b^2*c^2*d - 315*a^2*b*c*d^2)/(140*b^3*(a*d - b*c)^4) + (27*d*x*(35*a^2*d^2 + 2*b^2*c^2 - 10*a*b*c*d))/(140*b^2*(a*d - b*c)^4) + (81*d^2*x^2*(10*a*d - b*c))/(140*b*(a*d - b*c)^4))/(x^3*(a + b*x)^(1/3) + (a^3*(a + b*x)^(1/3))/b^3 + (3*a*x^2*(a + b*x)^(1/3))/b + (3*a^2*x*(a + b*x)^(1/3))/b^2)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(13/3)/(d*x+c)**(2/3),x)
```

```
[Out] Timed out
```

$$3.1608 \quad \int \frac{(a+bx)^{7/3}}{(c+dx)^{2/3}} dx$$

Optimal. Leaf size=649

$$7 \cdot 3^{3/4} \sqrt{2 + \sqrt{3}} (bc - ad)^3 ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right)$$

$$10 \cdot 2^{2/3} \sqrt[3]{b} d^{10/3} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx)^{2/3}$$

[Out] $21/20*(-a*d+b*c)^2*(b*x+a)^{(1/3)}*(d*x+c)^{(1/3)}/d^3-21/40*(-a*d+b*c)*(b*x+a)^{(4/3)}*(d*x+c)^{(1/3)}/d^2+3/8*(b*x+a)^{(7/3)}*(d*x+c)^{(1/3)}/d-7/20*3^{(3/4)}*(-a*d+b*c)^3*((b*x+a)*(d*x+c))^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)}))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}+1/2*2^{(1/2)})*((-a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))^2)^{(1/2)}*2^{(1/3)}/b^{(1/3)}/d^{(10/3)}/(b*x+a)^{(2/3)}/(d*x+c)^{(2/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 1.12, antiderivative size = 649, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 218}

$$7 \cdot 3^{3/4} \sqrt{2 + \sqrt{3}} (bc - ad)^3 ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right)$$

$$10 \cdot 2^{2/3} \sqrt[3]{b} d^{10/3} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx)^{2/3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/3)/(c + d*x)^(2/3), x]

[Out] $(21*(b*c - a*d)^2*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)})/(20*d^3) - (21*(b*c - a*d)*(a + b*x)^{(4/3)}*(c + d*x)^{(1/3)})/(40*d^2) + (3*(a + b*x)^{(7/3)}*(c + d*x)^{(1/3)})/(8*d) - (7*3^{(3/4)}*Sqrt[2 + Sqrt[3]]*(b*c - a*d)^3*((a + b*x)*(c + d*x))^{(2/3)}*Sqrt[(ad + bc + 2bdx)^2] * (2^{(2/3)} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3}))$

$$d*x))^{2/3}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{2/3} + 2^{2/3}*b^{1/3}*d^{1/3}*(a + b*x)*(c + d*x))^{1/3})*\text{Sqrt}[(b*c - a*d)^{4/3} - 2^{2/3}*b^{1/3}*d^{1/3}*(b*c - a*d)^{2/3}*((a + b*x)*(c + d*x))^{1/3} + 2*2^{1/3}*b^{2/3}*d^{2/3}*((a + b*x)*(c + d*x))^{2/3}]/((1 + \text{Sqrt}[3])*(b*c - a*d)^{2/3} + 2^{2/3}*b^{1/3}*d^{1/3}*(a + b*x)*(c + d*x))^{1/3})^2]*\text{EllipticF}[\text{ArcSin}[\frac{((1 - \text{Sqrt}[3])*(b*c - a*d)^{2/3} + 2^{2/3}*b^{1/3}*d^{1/3}*(a + b*x)*(c + d*x))^{1/3}}{(1 + \text{Sqrt}[3])*(b*c - a*d)^{2/3} + 2^{2/3}*b^{1/3}*d^{1/3}*(a + b*x)*(c + d*x))^{1/3}}], -7 - 4*\text{Sqrt}[3]]]/(10*2^{2/3}*b^{1/3}*d^{10/3}*(a + b*x)^{2/3}*(c + d*x)^{2/3}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(b*c - a*d)^{2/3}*((b*c - a*d)^{2/3} + 2^{2/3}*b^{1/3}*d^{1/3}*(a + b*x)*(c + d*x))^{1/3}])]/((1 + \text{Sqrt}[3])*(b*c - a*d)^{2/3} + 2^{2/3}*b^{1/3}*d^{1/3}*(a + b*x)*(c + d*x))^{1/3})^2]*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]$$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
((a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/\text{Sqrt}[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*\text{Sqrt}[2 + \text{Sqrt}[3]]*(s + r*x)*\text{Sqrt}[(s^2 - r*s
*x + r^2*x^2)/((1 + \text{Sqrt}[3])*s + r*x)^2]*\text{EllipticF}[\text{ArcSin}[\frac{(1 - \text{Sqrt}[3])*s
+ r*x}{(1 + \text{Sqrt}[3])*s + r*x}], -7 - 4*\text{Sqrt}[3]]]/(3^{1/4}*r*\text{Sqrt}[a + b*x^3
]*\text{Sqrt}[(s*(s + r*x))/((1 + \text{Sqrt}[3])*s + r*x)^2]), x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*\text{Sqrt}[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/\text{Sqrt}[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/3}}{(c+dx)^{2/3}} dx &= \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8d} - \frac{(7(bc-ad)) \int \frac{(a+bx)^{4/3}}{(c+dx)^{2/3}} dx}{8d} \\
&= -\frac{21(bc-ad)(a+bx)^{4/3} \sqrt[3]{c+dx}}{40d^2} + \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8d} + \frac{(7(bc-ad)^2) \int \frac{\sqrt[3]{a+bx}}{(c+dx)^{2/3}} dx}{10d^2} \\
&= \frac{21(bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{20d^3} - \frac{21(bc-ad)(a+bx)^{4/3} \sqrt[3]{c+dx}}{40d^2} + \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8d} \\
&= \frac{21(bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{20d^3} - \frac{21(bc-ad)(a+bx)^{4/3} \sqrt[3]{c+dx}}{40d^2} + \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8d} \\
&= \frac{21(bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{20d^3} - \frac{21(bc-ad)(a+bx)^{4/3} \sqrt[3]{c+dx}}{40d^2} + \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8d} \\
&= \frac{21(bc-ad)^2 \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{20d^3} - \frac{21(bc-ad)(a+bx)^{4/3} \sqrt[3]{c+dx}}{40d^2} + \frac{3(a+bx)^{7/3} \sqrt[3]{c+dx}}{8d}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.11

$$\frac{3(a+bx)^{10/3} \left(\frac{b(c+dx)}{bc-ad} \right)^{2/3} {}_2F_1 \left(\frac{2}{3}, \frac{10}{3}; \frac{13}{3}; \frac{d(a+bx)}{ad-bc} \right)}{10b(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/3)/(c + d*x)^(2/3), x]

[Out] (3*(a + b*x)^(10/3)*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[2/3, 10/3, 13/3, (d*(a + b*x))/(-b*c + a*d)]/(10*b*(c + d*x)^(2/3))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(b^2x^2 + 2abx + a^2)(bx + a)^{\frac{1}{3}}}{(dx + c)^{\frac{2}{3}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/3)/(d*x+c)^(2/3),x, algorithm="fricas")

[Out] integral((b^2*x^2 + 2*a*b*x + a^2)*(b*x + a)^(1/3)/(d*x + c)^(2/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(7/3)/(d*x + c)^(2/3), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/3)/(d*x+c)^(2/3),x)

[Out] int((b*x+a)^(7/3)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/3)/(d*x + c)^(2/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{7/3}}{(c + dx)^{2/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(7/3)/(c + d*x)^(2/3),x)
```

```
[Out] int((a + b*x)^(7/3)/(c + d*x)^(2/3), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(a + bx)^{\frac{7}{3}}}{(c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(7/3)/(d*x+c)**(2/3),x)
```

```
[Out] Integral((a + b*x)**(7/3)/(c + d*x)**(2/3), x)
```

$$3.1609 \quad \int \frac{(a+bx)^{4/3}}{(c+dx)^{2/3}} dx$$

Optimal. Leaf size=614

$$2\sqrt[3]{2}3^{3/4}\sqrt{2+\sqrt{3}}(bc-ad)^2((a+bx)(c+dx))^{2/3}\sqrt{(ad+bc+2bdx)^2}\left(2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}+(bc-ad)\right)$$

$$5\sqrt[3]{b}d^{7/3}(a+bx)^{2/3}(c+dx)^{2/3}(ad+bc+2bdx)$$

[Out] $-6/5*(-a*d+b*c)*(b*x+a)^{(1/3)}*(d*x+c)^{(1/3)}/d^2+3/5*(b*x+a)^{(4/3)}*(d*x+c)^{(1/3)}/d+2/5*2^{(1/3)}*3^{(3/4)}*(-a*d+b*c)^2*((b*x+a)*(d*x+c))^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)}))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})),I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}+1/2*2^{(1/2)})*(((-a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/b^{(1/3)}/d^{(7/3)}/(b*x+a)^{(2/3)}/(d*x+c)^{(2/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.82, antiderivative size = 614, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 218}

$$2\sqrt[3]{2}3^{3/4}\sqrt{2+\sqrt{3}}(bc-ad)^2((a+bx)(c+dx))^{2/3}\sqrt{(ad+bc+2bdx)^2}\left(2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}+(bc-ad)\right)$$

$$5\sqrt[3]{b}d^{7/3}(a+bx)^{2/3}(c+dx)^{2/3}(ad+bc+2bdx)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(4/3)/(c + d*x)^(2/3), x]

[Out] $(-6*(b*c - a*d)*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)})/(5*d^2) + (3*(a + b*x)^{(4/3)}*(c + d*x)^{(1/3)})/(5*d) + (2*2^{(1/3)}*3^{(3/4)}*\text{Sqrt}[2 + \text{Sqrt}[3]]*(b*c - a*d)^2*((a + b*x)*(c + d*x))^{(2/3)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*\text{Sqrt}[(b*c - a$

$$\begin{aligned} & *d)^{4/3} - 2^{2/3} * b^{1/3} * d^{1/3} * (b*c - a*d)^{2/3} * ((a + b*x)*(c + d*x)) \\ & ^{1/3} + 2 * 2^{1/3} * b^{2/3} * d^{2/3} * ((a + b*x)*(c + d*x))^{2/3} / ((1 + \text{Sqrt}[\\ & 3]) * (b*c - a*d)^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((a + b*x)*(c + d*x))^{1/3} \\ &)^2 * \text{EllipticF}[\text{ArcSin}[(1 - \text{Sqrt}[3]) * (b*c - a*d)^{2/3} + 2^{2/3} * b^{1/3} * d^{ \\ & 1/3} * ((a + b*x)*(c + d*x))^{1/3}] / ((1 + \text{Sqrt}[3]) * (b*c - a*d)^{2/3} + 2^{2/ \\ & 3} * b^{1/3} * d^{1/3} * ((a + b*x)*(c + d*x))^{1/3})], -7 - 4 * \text{Sqrt}[3]] / (5 * b^{1/ \\ & 3} * d^{7/3} * (a + b*x)^{2/3} * (c + d*x)^{2/3} * (b*c + a*d + 2 * b*d*x) * \text{Sqrt}[(b*c \\ & - a*d)^{2/3} * ((b*c - a*d)^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((a + b*x)*(c + \\ & d*x))^{1/3})] / ((1 + \text{Sqrt}[3]) * (b*c - a*d)^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((\\ & a + b*x)*(c + d*x))^{1/3})^2 * \text{Sqrt}[(a*d + b*(c + 2*d*x))^2] \end{aligned}$$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x*d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{4/3}}{(c+dx)^{2/3}} dx &= \frac{3(a+bx)^{4/3} \sqrt[3]{c+dx}}{5d} - \frac{(4(bc-ad)) \int \frac{\sqrt[3]{a+bx}}{(c+dx)^{2/3}} dx}{5d} \\
&= -\frac{6(bc-ad) \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{5d^2} + \frac{3(a+bx)^{4/3} \sqrt[3]{c+dx}}{5d} + \frac{(2(bc-ad)^2) \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{5d^2} \\
&= -\frac{6(bc-ad) \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{5d^2} + \frac{3(a+bx)^{4/3} \sqrt[3]{c+dx}}{5d} + \frac{(2(bc-ad)^2((a+bx)(c+dx))^{2/3}) \int}{5d^2(a+bx)^{2/3}(c+dx)} \\
&= -\frac{6(bc-ad) \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{5d^2} + \frac{3(a+bx)^{4/3} \sqrt[3]{c+dx}}{5d} + \frac{(6(bc-ad)^2((a+bx)(c+dx))^{2/3} \sqrt{c+dx})}{5} \\
&= -\frac{6(bc-ad) \sqrt[3]{a+bx} \sqrt[3]{c+dx}}{5d^2} + \frac{3(a+bx)^{4/3} \sqrt[3]{c+dx}}{5d} + \frac{2\sqrt[3]{2} 3^{3/4} \sqrt{2+\sqrt{3}} (bc-ad)^2 ((a+bx)(c+dx))^{2/3}}{5}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.12

$$\frac{3(a+bx)^{7/3} \left(\frac{b(c+dx)}{bc-ad}\right)^{2/3} {}_2F_1\left(\frac{2}{3}, \frac{7}{3}; \frac{10}{3}; \frac{d(a+bx)}{ad-bc}\right)}{7b(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(4/3)/(c + d*x)^(2/3), x]

[Out] (3*(a + b*x)^(7/3)*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[2/3, 7/3, 10/3, (d*(a + b*x))/(-b*c) + a*d])/(7*b*(c + d*x)^(2/3))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{4/3}}{(dx+c)^{2/3}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/(d*x+c)^(2/3), x, algorithm="fricas")

[Out] integral((b*x + a)^(4/3)/(d*x + c)^(2/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{4}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(4/3)/(d*x + c)^(2/3), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{4}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(4/3)/(d*x+c)^(2/3),x)

[Out] int((b*x+a)^(4/3)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{4}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(4/3)/(d*x + c)^(2/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{\frac{4}{3}}}{(c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(4/3)/(c + d*x)^(2/3),x)

[Out] int((a + b*x)^(4/3)/(c + d*x)^(2/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{4}{3}}}{(c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(4/3)/(d*x+c)**(2/3), x)

[Out] Integral((a + b*x)**(4/3)/(c + d*x)**(2/3), x)

$$3.1610 \quad \int \frac{\sqrt[3]{a+bx}}{(c+dx)^{2/3}} dx$$

Optimal. Leaf size=577

$$\frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx}}{2d} - \frac{3^{3/4}\sqrt{2+\sqrt{3}}(bc-ad)((a+bx)(c+dx))^{2/3}\sqrt{(ad+bc+2bdx)^2}(2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)})}{2^{2/3}\sqrt[3]{b}d^{4/3}(a+bx)^{2/3}(c+dx)^{2/3}}$$

[Out] $3/2*(b*x+a)^{(1/3)}*(d*x+c)^{(1/3)}/d-1/2*3^{(3/4)}*(-a*d+b*c)*((b*x+a)*(d*x+c))^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)}))/((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})),I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}+1/2*2^{(1/2)})*(((a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))^{(2/3)})^{(1/2)}*2^{(1/3)}/b^{(1/3)}/d^{(4/3)}/(b*x+a)^{(2/3)}/(d*x+c)^{(2/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))^{(2/3)})^{(1/2)}$

Rubi [A] time = 0.55, antiderivative size = 577, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 218}

$$\frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx}}{2d} - \frac{3^{3/4}\sqrt{2+\sqrt{3}}(bc-ad)((a+bx)(c+dx))^{2/3}\sqrt{(ad+bc+2bdx)^2}(2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)})}{2^{2/3}\sqrt[3]{b}d^{4/3}(a+bx)^{2/3}(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/3)/(c + d*x)^(2/3), x]

[Out] $(3*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)})/(2*d) - (3^{(3/4)}*\text{Sqrt}[2 + \text{Sqrt}[3]]*(b*c - a*d)*((a + b*x)*(c + d*x))^{(2/3)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*\text{Sqrt}[(b*c - a*d)^{(4/3)} - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)})/(1 + S$

```

qrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(
1/3))^2*EllipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)
)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3)]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2
^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]]/(2^(
2/3)*b^(1/3)*d^(4/3)*(a + b*x)^(2/3)*(c + d*x)^(2/3)*(b*c + a*d + 2*b*d*x)*
Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a +
b*x)*(c + d*x))^(1/3)))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*
d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2]

```

Rule 50

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 62

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]

```

Rule 218

```

Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)]/((1 + Sqrt[3])*s + r*x)^2)*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]]/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] &
& PosQ[a]

```

Rule 623

```

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[3]{a+bx}}{(c+dx)^{2/3}} dx &= \frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx}}{2d} - \frac{(bc-ad) \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{2d} \\
&= \frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx}}{2d} - \frac{((bc-ad)((a+bx)(c+dx))^{2/3}) \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{2/3}} dx}{2d(a+bx)^{2/3}(c+dx)^{2/3}} \\
&= \frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx}}{2d} - \frac{(3(bc-ad)((a+bx)(c+dx))^{2/3} \sqrt{(bc+ad+2bdx)^2}) \text{Subst} \left(\int \frac{1}{\sqrt{-4abcd+}} \right)}{2d(a+bx)^{2/3}(c+dx)^{2/3}(bc+ad+2bdx)} \\
&= \frac{3\sqrt[3]{a+bx}\sqrt[3]{c+dx}}{2d} - \frac{3^{3/4} \sqrt{2+\sqrt{3}} (bc-ad)((a+bx)(c+dx))^{2/3} \sqrt{(bc+ad+2bdx)^2} ((bc-ad) \int \frac{1}{\sqrt{-4abcd+}})}{2d(a+bx)^{2/3}(c+dx)^{2/3}(bc+ad+2bdx)}
\end{aligned}$$

 $2^{2/3} \sqrt[3]{b} d^{4/3}$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.13

$$\frac{3(a+bx)^{4/3} \left(\frac{b(c+dx)}{bc-ad} \right)^{2/3} {}_2F_1 \left(\frac{2}{3}, \frac{4}{3}; \frac{7}{3}; \frac{d(a+bx)}{ad-bc} \right)}{4b(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/3)/(c + d*x)^(2/3), x]

[Out] (3*(a + b*x)^(4/3)*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[2/3, 4/3, 7/3, (d*(a + b*x))/(-b*c) + a*d])/(4*b*(c + d*x)^(2/3))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{1}{3}}}{(dx+c)^{\frac{2}{3}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/(d*x+c)^(2/3), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/3)/(d*x + c)^(2/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{3}}}{(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/3)/(d*x + c)^(2/3), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/3)/(d*x+c)^(2/3),x)

[Out] int((b*x+a)^(1/3)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{3}}}{(dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/3)/(d*x + c)^(2/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{1/3}}{(c + dx)^{2/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/3)/(c + d*x)^(2/3),x)

[Out] int((a + b*x)^(1/3)/(c + d*x)^(2/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{a + bx}}{(c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/3)/(d*x+c)**(2/3),x)

[Out] Integral((a + b*x)**(1/3)/(c + d*x)**(2/3), x)

$$3.1611 \quad \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx$$

Optimal. Leaf size=542

$$\sqrt[3]{2} 3^{3/4} \sqrt{2 + \sqrt{3}} ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\frac{2 \sqrt[3]{2} b^{2/3}}{}}$$

$$\sqrt[3]{b} \sqrt[3]{d} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx) \sqrt{\frac{(bc - ad)^{2/3}}{(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3})}}$$

[Out] $2^{1/3} * 3^{3/4} * ((b*x+a)*(d*x+c))^{2/3} * ((-a*d+b*c))^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} * ((b*x+a)*(d*x+c))^{1/3} * \text{EllipticF}((2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1-3^{1/2}))/ (2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1+3^{1/2})), I * 3^{1/2} + 2 * I) * ((2 * b * d * x + a * d + b * c)^2)^{1/2} * (1/2 * 6^{1/2} + 1/2 * 2^{1/2}) * (((-a*d+b*c))^{4/3} - 2^{2/3} * b^{1/3} * d^{1/3} * (-a*d+b*c)^{2/3} * ((b*x+a)*(d*x+c))^{1/3} + 2 * 2^{1/3} * b^{2/3} * d^{2/3} * ((b*x+a)*(d*x+c))^{2/3}) / (2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1+3^{1/2}))^2)^{1/2} / b^{1/3} / d^{1/3} / (b*x+a)^{2/3} / (d*x+c)^{2/3} / (2 * b * d * x + a * d + b * c) / ((a*d+b*(2*d*x+c))^2)^{1/2} / ((-a*d+b*c))^{2/3} * ((-a*d+b*c))^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3}) / (2^{2/3} * b^{1/3} * d^{1/3} * ((b*x+a)*(d*x+c))^{1/3} + (-a*d+b*c)^{2/3} * (1+3^{1/2}))^2)^{1/2}$

Rubi [A] time = 0.43, antiderivative size = 542, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {62, 623, 218}

$$\sqrt[3]{2} 3^{3/4} \sqrt{2 + \sqrt{3}} ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\frac{2 \sqrt[3]{2} b^{2/3}}{}}$$

$$\sqrt[3]{b} \sqrt[3]{d} (a + bx)^{2/3} (c + dx)^{2/3} (ad + bc + 2bdx) \sqrt{\frac{(bc - ad)^{2/3}}{(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3})}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(2/3)*(c + d*x)^(2/3)), x]

[Out] $(2^{1/3} * 3^{3/4} * \text{Sqrt}[2 + \text{Sqrt}[3]]) * ((a + b*x)*(c + d*x))^{2/3} * \text{Sqrt}[(b*c + a*d + 2*b*d*x)^2] * ((b*c - a*d)^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((a + b*x)*(c + d*x))^{1/3}) * \text{Sqrt}[(b*c - a*d)^{4/3} - 2^{2/3} * b^{1/3} * d^{1/3} * (b*c - a*d)^{2/3} * ((a + b*x)*(c + d*x))^{1/3} + 2 * 2^{1/3} * b^{2/3} * d^{2/3} * ((a + b*x)*(c + d*x))^{2/3}] / ((1 + \text{Sqrt}[3]) * (b*c - a*d)^{2/3} + 2^{2/3} * b^{1/3} * d^{1/3} * ((a + b*x)*(c + d*x))^{1/3})$

$$\frac{1}{3} \left((a + bx)(c + dx) \right)^{1/3} \left((1 - \sqrt{3})(bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} \left((a + bx)(c + dx) \right)^{1/3} \right) / \left((1 + \sqrt{3})(bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} \left((a + bx)(c + dx) \right)^{1/3} \right)$$

$$\text{EllipticF} \left[\text{ArcSin} \left[\frac{(1 - \sqrt{3})(bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} \left((a + bx)(c + dx) \right)^{1/3}}{(1 + \sqrt{3})(bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} \left((a + bx)(c + dx) \right)^{1/3}} \right], -7 - 4\sqrt{3} \right] / \left(b^{1/3} d^{1/3} (a + bx)^{2/3} (c + dx)^{2/3} (bc + ad + 2bdx) \sqrt{\left((bc - ad)^{2/3} \left((bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} \left((a + bx)(c + dx) \right)^{1/3} \right) \right) / \left((1 + \sqrt{3})(bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} \left((a + bx)(c + dx) \right)^{1/3} \right)^2} \right) \sqrt{(ad + b(c + 2dx))^2}$$

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)]/((1 + Sqrt[3])*s + r*x)^2)*EllipticF[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]]/(3^(1/4)*r*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] && PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx &= \frac{((a+bx)(c+dx))^{2/3} \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{2/3}} dx}{(a+bx)^{2/3}(c+dx)^{2/3}} \\
&= \frac{(3((a+bx)(c+dx))^{2/3} \sqrt{(bc+ad+2bdx)^2}) \text{Subst} \left(\int \frac{1}{\sqrt{-4abcd+(bc+ad)^2+4bdx^3}} dx, x, \sqrt[3]{\frac{a+bx}{c+dx}} \right)}{(a+bx)^{2/3}(c+dx)^{2/3}(bc+ad+2bdx)} \\
&= \frac{\sqrt[3]{2} 3^{3/4} \sqrt{2+\sqrt{3}} ((a+bx)(c+dx))^{2/3} \sqrt{(bc+ad+2bdx)^2} \left((bc-ad)^{2/3} + 2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \right)}{\sqrt[3]{b} \sqrt[3]{d} (a+bx)^{2/3} (c+dx)^{2/3}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.13

$$\frac{3 \sqrt[3]{a+bx} \left(\frac{b(c+dx)}{bc-ad} \right)^{2/3} {}_2F_1 \left(\frac{1}{3}, \frac{2}{3}; \frac{4}{3}; \frac{d(a+bx)}{ad-bc} \right)}{b(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a+b*x)^(2/3)*(c+d*x)^(2/3)),x]

[Out] (3*(a+b*x)^(1/3)*((b*(c+d*x))/(b*c-a*d))^(2/3)*Hypergeometric2F1[1/3, 2/3, 4/3, (d*(a+b*x))/(-(b*c)+a*d)]/(b*(c+d*x)^(2/3))

fricas [F] time = 0.43, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{1/3}(dx+c)^{1/3}}{bdx^2+ac+(bc+ad)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(2/3)/(d*x+c)^(2/3),x, algorithm="fricas")

[Out] integral((b*x+a)^(1/3)*(d*x+c)^(1/3)/(b*d*x^2+a*c+(b*c+a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{2/3}(dx+c)^{2/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(2/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(2/3)*(d*x + c)^(2/3)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{2}{3}} (dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(2/3)/(d*x+c)^(2/3),x)

[Out] int(1/(b*x+a)^(2/3)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{2}{3}} (dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(2/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(2/3)*(d*x + c)^(2/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{\frac{2}{3}} (c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(2/3)*(c + d*x)^(2/3)),x)

[Out] int(1/((a + b*x)^(2/3)*(c + d*x)^(2/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{2}{3}} (c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(2/3)/(d*x+c)**(2/3),x)

[Out] Integral(1/((a + b*x)**(2/3)*(c + d*x)**(2/3)), x)

$$3.1612 \quad \int \frac{1}{(a+bx)^{5/3}(c+dx)^{2/3}} dx$$

Optimal. Leaf size=586

$$3^{3/4} \sqrt{2 + \sqrt{3}} d^{2/3} ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\frac{2\sqrt[3]{2b}}{\dots}}$$

$$2^{2/3} \sqrt[3]{b} (a + bx)^{2/3} (c + dx)^{2/3} (bc - ad)(ad + bc + 2bdx)$$

[Out] $-3/2*(d*x+c)^{(1/3)/(-a*d+b*c)/(b*x+a)^{(2/3)}-1/2*3^{(3/4)*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)}*((-a*d+b*c)^{(2/3)+2^{(2/3)}*b^{(1/3)*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2))})/(2^{(2/3)}*b^{(1/3)*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2))})}, I*3^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)+1/2*2^{(1/2)})*(((a*d+b*c)^{(4/3)}-2^{(2/3)*b^{(1/3)*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)*b^{(2/3)*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)*b^{(1/3)*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2))})^2)^{(1/2)}*2^{(1/3)/b^{(1/3)/(-a*d+b*c)/(b*x+a)^{(2/3)/(d*x+c)^{(2/3)/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)*b^{(1/3)*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2))})^2)^{(1/2)}$

Rubi [A] time = 0.55, antiderivative size = 586, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {51, 62, 623, 218}

$$3^{3/4} \sqrt{2 + \sqrt{3}} d^{2/3} ((a + bx)(c + dx))^{2/3} \sqrt{(ad + bc + 2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} + (bc - ad)^{2/3} \right) \sqrt{\frac{2\sqrt[3]{2b}}{\dots}}$$

$$2^{2/3} \sqrt[3]{b} (a + bx)^{2/3} (c + dx)^{2/3} (bc - ad)(ad + bc + 2bdx)$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/3)*(c + d*x)^(2/3)), x]

[Out] $(-3*(c + d*x)^{(1/3))/(2*(b*c - a*d)*(a + b*x)^{(2/3)}) - (3^{(3/4)}*Sqrt[2 + Sqrt[3]]*d^{(2/3)*((a + b*x)*(c + d*x))^{(2/3)}*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}*Sqrt[((b*c - a*d)^{(4/3)} - 2^{(2/3)*b^{(1/3)*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)*b^{(2/3)*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)})/$

$$\left((1 + \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{2/3} + 2^{2/3} \cdot b^{1/3} \cdot d^{1/3} \cdot ((a + b \cdot x) \cdot (c + d \cdot x))^{1/3} \right)^2 \cdot \text{EllipticF}\left[\text{ArcSin}\left[\frac{(1 - \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{2/3} + 2^{2/3} \cdot b^{1/3} \cdot d^{1/3} \cdot ((a + b \cdot x) \cdot (c + d \cdot x))^{1/3}}{(1 + \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{2/3} + 2^{2/3} \cdot b^{1/3} \cdot d^{1/3} \cdot ((a + b \cdot x) \cdot (c + d \cdot x))^{1/3}}\right], -7 - 4\sqrt{3}\right] \Big/ \left(2^{2/3} \cdot b^{1/3} \cdot (b \cdot c - a \cdot d) \cdot (a + b \cdot x)^{2/3} \cdot (c + d \cdot x)^{2/3} \cdot (b \cdot c + a \cdot d + 2 \cdot b \cdot d \cdot x) \cdot \sqrt{\left((b \cdot c - a \cdot d)^{2/3} \cdot \left((b \cdot c - a \cdot d)^{2/3} + 2^{2/3} \cdot b^{1/3} \cdot d^{1/3} \cdot ((a + b \cdot x) \cdot (c + d \cdot x))^{1/3} \right) \right)} \Big/ \left((1 + \sqrt{3}) \cdot (b \cdot c - a \cdot d)^{2/3} + 2^{2/3} \cdot b^{1/3} \cdot d^{1/3} \cdot ((a + b \cdot x) \cdot (c + d \cdot x))^{1/3} \right)^2 \cdot \sqrt{(a \cdot d + b \cdot (c + 2 \cdot d \cdot x))^2} \right)$$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)]/((1 + Sqrt[3])*s + r*x)^2)*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]]/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/3}(c+dx)^{2/3}} dx &= -\frac{3\sqrt[3]{c+dx}}{2(bc-ad)(a+bx)^{2/3}} - \frac{d \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{2(bc-ad)} \\
&= -\frac{3\sqrt[3]{c+dx}}{2(bc-ad)(a+bx)^{2/3}} - \frac{(d((a+bx)(c+dx))^{2/3}) \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{2/3}} dx}{2(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}} \\
&= -\frac{3\sqrt[3]{c+dx}}{2(bc-ad)(a+bx)^{2/3}} - \frac{(3d((a+bx)(c+dx))^{2/3} \sqrt{(bc+ad+2bdx)^2}) \text{Subst} \left(\int \frac{1}{\sqrt{-}} \right)}{2(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}} \\
&= -\frac{3\sqrt[3]{c+dx}}{2(bc-ad)(a+bx)^{2/3}} - \frac{3^{3/4} \sqrt{2+\sqrt{3}} d^{2/3} ((a+bx)(c+dx))^{2/3} \sqrt{(bc+ad+2bdx)^2}}{2(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.12

$$-\frac{3 \left(\frac{b(c+dx)}{bc-ad} \right)^{2/3} {}_2F_1 \left(-\frac{2}{3}, \frac{2}{3}; \frac{1}{3}; \frac{d(a+bx)}{ad-bc} \right)}{2b(a+bx)^{2/3}(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/3)*(c + d*x)^(2/3)), x]

[Out] (-3*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[-2/3, 2/3, 1/3, (d*(a + b*x))/(-(b*c) + a*d)]/(2*b*(a + b*x)^(2/3)*(c + d*x)^(2/3))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{1/3}(dx+c)^{1/3}}{b^2dx^3 + a^2c + (b^2c + 2abd)x^2 + (2abc + a^2d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/3)/(d*x+c)^(2/3), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/3)*(d*x + c)^(1/3)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/3)*(d*x + c)^(2/3)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/3)/(d*x+c)^(2/3),x)

[Out] int(1/(b*x+a)^(5/3)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/3)*(d*x + c)^(2/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{3}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/3)*(c + d*x)^(2/3)),x)

[Out] int(1/((a + b*x)^(5/3)*(c + d*x)^(2/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{3}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(5/3)/(d*x+c)**(2/3),x)
```

```
[Out] Integral(1/((a + b*x)**(5/3)*(c + d*x)**(2/3)), x)
```


$$- a*d)^{(4/3)} - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)}/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2*\text{EllipticF}[\text{ArcSin}[(1 - \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}]/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})], -7 - 4*\text{Sqrt}[3]]/(5*b^{(1/3)}*(b*c - a*d)^2*(a + b*x)^{(2/3)}*(c + d*x)^{(2/3)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(b*c - a*d)^{(2/3)}*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})]/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]$$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]]/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{8/3}(c+dx)^{2/3}} dx &= -\frac{3\sqrt[3]{c+dx}}{5(bc-ad)(a+bx)^{5/3}} - \frac{(4d) \int \frac{1}{(a+bx)^{5/3}(c+dx)^{2/3}} dx}{5(bc-ad)} \\
&= -\frac{3\sqrt[3]{c+dx}}{5(bc-ad)(a+bx)^{5/3}} + \frac{6d\sqrt[3]{c+dx}}{5(bc-ad)^2(a+bx)^{2/3}} + \frac{(2d^2) \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{5(bc-ad)^2} \\
&= -\frac{3\sqrt[3]{c+dx}}{5(bc-ad)(a+bx)^{5/3}} + \frac{6d\sqrt[3]{c+dx}}{5(bc-ad)^2(a+bx)^{2/3}} + \frac{(2d^2((a+bx)(c+dx))^{2/3}) \int \frac{1}{(a+bx)(c+dx)} dx}{5(bc-ad)^2(a+bx)^{2/3}} \\
&= -\frac{3\sqrt[3]{c+dx}}{5(bc-ad)(a+bx)^{5/3}} + \frac{6d\sqrt[3]{c+dx}}{5(bc-ad)^2(a+bx)^{2/3}} + \frac{(6d^2((a+bx)(c+dx))^{2/3}\sqrt{(bc-ad)}) \int \frac{1}{(a+bx)(c+dx)} dx}{5(bc-ad)^2(a+bx)^{2/3}} \\
&= -\frac{3\sqrt[3]{c+dx}}{5(bc-ad)(a+bx)^{5/3}} + \frac{6d\sqrt[3]{c+dx}}{5(bc-ad)^2(a+bx)^{2/3}} + \frac{2^3\sqrt{2}3^{3/4}\sqrt{2+\sqrt{3}}d^{5/3}((a+bx)(c+dx))^{2/3}}{5(bc-ad)^2(a+bx)^{2/3}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.12

$$\frac{3 \left(\frac{b(c+dx)}{bc-ad} \right)^{2/3} {}_2F_1 \left(-\frac{5}{3}, \frac{2}{3}; -\frac{2}{3}; \frac{d(a+bx)}{ad-bc} \right)}{5b(a+bx)^{5/3}(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(8/3)*(c + d*x)^(2/3)),x]

[Out] (-3*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[-5/3, 2/3, -2/3, (d*(a + b*x))/(-b*c + a*d)]/(5*b*(a + b*x)^(5/3)*(c + d*x)^(2/3))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{1/3}(dx+c)^{1/3}}{b^3dx^4 + a^3c + (b^3c + 3ab^2d)x^3 + 3(ab^2c + a^2bd)x^2 + (3a^2bc + a^3d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(8/3)/(d*x+c)^(2/3),x, algorithm="fricas")

[Out] integral((b*x + a)^(1/3)*(d*x + c)^(1/3)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{8}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(8/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(8/3)*(d*x + c)^(2/3)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{8}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(8/3)/(d*x+c)^(2/3),x)

[Out] int(1/(b*x+a)^(8/3)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{8}{3}}(dx+c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(8/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(8/3)*(d*x + c)^(2/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{\frac{8}{3}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(8/3)*(c + d*x)^(2/3)),x)

[Out] int(1/((a + b*x)^(8/3)*(c + d*x)^(2/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{8}{3}}(c+dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(8/3)/(d*x+c)**(2/3),x)
```

```
[Out] Integral(1/((a + b*x)**(8/3)*(c + d*x)**(2/3)), x)
```

$$3.1614 \quad \int \frac{1}{(a+bx)^{11/3}(c+dx)^{2/3}} dx$$

Optimal. Leaf size=656

$$7 \cdot 3^{3/4} \sqrt{2 + \sqrt{3}} d^{8/3} ((a+bx)(c+dx))^{2/3} \sqrt{(ad+bc+2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a+bx)(c+dx)} + (bc-ad)^{2/3} \right) \sqrt{\frac{2 \sqrt[3]{b}}{\sqrt[3]{d}}}$$

$$10 \cdot 2^{2/3} \sqrt[3]{b} (a+bx)^{2/3} (c+dx)^{2/3} (bc-ad)^3 (ad+bc+2bdx)^{2/3}$$

[Out] $-3/8*(d*x+c)^{(1/3)/(-a*d+b*c)/(b*x+a)^{(8/3)+21/40*d*(d*x+c)^{(1/3)/(-a*d+b*c)^{(2/2/3)}(b*x+a)^{(5/3)-21/20*d^2*(d*x+c)^{(1/3)/(-a*d+b*c)^3/(b*x+a)^{(2/3)-7/20*3^{3/4}*d^{8/3}*((b*x+a)*(d*x+c))^{2/3}*((-a*d+b*c)^{(2/3)+2^{2/3}*b^{1/3}*d^{1/3}*((b*x+a)*(d*x+c))^{1/3}*EllipticF((2^{2/3}*b^{1/3}*d^{1/3}*((b*x+a)*(d*x+c))^{1/3)+(-a*d+b*c)^{(2/3)*(1-3^{1/2})))/(2^{2/3}*b^{1/3}*d^{1/3}*((b*x+a)*(d*x+c))^{1/3)+(-a*d+b*c)^{(2/3)*(1+3^{1/2}))}, I*3^{1/2}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*(1/2*6^{1/2}+1/2*2^{1/2}))*((-a*d+b*c)^{(4/3)-2^{2/3}*b^{1/3}*d^{1/3}*((b*x+a)*(d*x+c))^{1/3)+2*2^{1/3}*b^{2/3}*d^{2/3}*((b*x+a)*(d*x+c))^{2/3})/(2^{2/3}*b^{1/3}*d^{1/3}*((b*x+a)*(d*x+c))^{1/3}+(-a*d+b*c)^{(2/3)*(1+3^{1/2}))^2)^{(1/2)*2^{1/3}/b^{1/3}/(-a*d+b*c)^3/(b*x+a)^{(2/3)/(d*x+c)^{(2/3)/(2*b*d*x+a*d+b*c)/((a*d+b*c*(2*d*x+c))^2)^{(1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{2/3}*b^{1/3}*d^{1/3}*((b*x+a)*(d*x+c))^{1/3})/(2^{2/3}*b^{1/3}*d^{1/3}*((b*x+a)*(d*x+c))^{1/3)+(-a*d+b*c)^{(2/3)*(1+3^{1/2}))^2)^{(1/2)}$

Rubi [A] time = 1.09, antiderivative size = 656, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {51, 62, 623, 218}

$$7 \cdot 3^{3/4} \sqrt{2 + \sqrt{3}} d^{8/3} ((a+bx)(c+dx))^{2/3} \sqrt{(ad+bc+2bdx)^2} \left(2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a+bx)(c+dx)} + (bc-ad)^{2/3} \right) \sqrt{\frac{2 \sqrt[3]{b}}{\sqrt[3]{d}}}$$

$$10 \cdot 2^{2/3} \sqrt[3]{b} (a+bx)^{2/3} (c+dx)^{2/3} (bc-ad)^3 (ad+bc+2bdx)^{2/3}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(11/3)*(c + d*x)^(2/3)), x]

[Out] $(-3*(c + d*x)^{(1/3)/(8*(b*c - a*d)*(a + b*x)^{(8/3))} + (21*d*(c + d*x)^{(1/3)/(40*(b*c - a*d)^2*(a + b*x)^{(5/3))} - (21*d^2*(c + d*x)^{(1/3)/(20*(b*c - a*d)^3*(a + b*x)^{(2/3))} - (7*3^{3/4}*Sqrt[2 + Sqrt[3]])*d^{8/3}*((a + b*x)*$

$$(c + dx)^{2/3} \sqrt{(bc + ad + 2b^2 dx)^2} ((bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} (a + bx)(c + dx)^{1/3}) \sqrt{((bc - ad)^{4/3} - 2^{2/3} b^{1/3} d^{1/3} (bc - ad)^{2/3} ((a + bx)(c + dx)^{1/3} + 2^{2/3} b^{2/3} d^{2/3} ((a + bx)(c + dx)^{2/3})) / ((1 + \sqrt{3})(bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} ((a + bx)(c + dx)^{1/3}))^2} \text{EllipticF}[\text{ArcSin}[\frac{((1 - \sqrt{3})(bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} (a + bx)(c + dx)^{1/3})}{(1 + \sqrt{3})(bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} ((a + bx)(c + dx)^{1/3})}], -7 - 4\sqrt{3}]] / (10 \cdot 2^{2/3} b^{1/3} (bc - ad)^3 (a + bx)^{2/3} (c + dx)^{2/3} (bc + ad + 2b^2 dx) \sqrt{((bc - ad)^{2/3} ((bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} ((a + bx)(c + dx)^{1/3})) / ((1 + \sqrt{3})(bc - ad)^{2/3} + 2^{2/3} b^{1/3} d^{1/3} ((a + bx)(c + dx)^{1/3}))^2} \sqrt{(ad + b(c + 2dx))^2})$$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
((a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*sqrt[2 + sqrt[3]]*(s + r*x)*sqrt[(s^2 - r*s
*x + r^2*x^2)]/((1 + sqrt[3])*s + r*x)^2)*EllipticF[ArcSin[(((1 - sqrt[3])*s
+ r*x)/((1 + sqrt[3])*s + r*x))], -7 - 4*sqrt[3]]]/(3^(1/4)*r*sqrt[a + b*x^3
]*sqrt[(s*(s + r*x))/((1 + sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{11/3}(c+dx)^{2/3}} dx &= -\frac{3\sqrt[3]{c+dx}}{8(bc-ad)(a+bx)^{8/3}} - \frac{(7d) \int \frac{1}{(a+bx)^{8/3}(c+dx)^{2/3}} dx}{8(bc-ad)} \\
&= -\frac{3\sqrt[3]{c+dx}}{8(bc-ad)(a+bx)^{8/3}} + \frac{21d\sqrt[3]{c+dx}}{40(bc-ad)^2(a+bx)^{5/3}} + \frac{(7d^2) \int \frac{1}{(a+bx)^{5/3}(c+dx)^{2/3}} dx}{10(bc-ad)^2} \\
&= -\frac{3\sqrt[3]{c+dx}}{8(bc-ad)(a+bx)^{8/3}} + \frac{21d\sqrt[3]{c+dx}}{40(bc-ad)^2(a+bx)^{5/3}} - \frac{21d^2\sqrt[3]{c+dx}}{20(bc-ad)^3(a+bx)^{2/3}} - \frac{(7d^3) \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{10(bc-ad)^3} \\
&= -\frac{3\sqrt[3]{c+dx}}{8(bc-ad)(a+bx)^{8/3}} + \frac{21d\sqrt[3]{c+dx}}{40(bc-ad)^2(a+bx)^{5/3}} - \frac{21d^2\sqrt[3]{c+dx}}{20(bc-ad)^3(a+bx)^{2/3}} - \frac{(7d^3) \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{10(bc-ad)^3} \\
&= -\frac{3\sqrt[3]{c+dx}}{8(bc-ad)(a+bx)^{8/3}} + \frac{21d\sqrt[3]{c+dx}}{40(bc-ad)^2(a+bx)^{5/3}} - \frac{21d^2\sqrt[3]{c+dx}}{20(bc-ad)^3(a+bx)^{2/3}} - \frac{(21d^3) \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{10(bc-ad)^3} \\
&= -\frac{3\sqrt[3]{c+dx}}{8(bc-ad)(a+bx)^{8/3}} + \frac{21d\sqrt[3]{c+dx}}{40(bc-ad)^2(a+bx)^{5/3}} - \frac{21d^2\sqrt[3]{c+dx}}{20(bc-ad)^3(a+bx)^{2/3}} - \frac{7d^3 \int \frac{1}{(a+bx)^{2/3}(c+dx)^{2/3}} dx}{10(bc-ad)^3}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.11

$$-\frac{3 \left(\frac{b(c+dx)}{bc-ad} \right)^{2/3} {}_2F_1 \left(-\frac{8}{3}, \frac{2}{3}; -\frac{5}{3}; \frac{d(a+bx)}{ad-bc} \right)}{8b(a+bx)^{8/3}(c+dx)^{2/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(11/3)*(c + d*x)^(2/3)), x]

[Out] (-3*((b*(c + d*x))/(b*c - a*d))^(2/3)*Hypergeometric2F1[-8/3, 2/3, -5/3, (d*(a + b*x))/(-(b*c) + a*d)])/(8*b*(a + b*x)^(8/3)*(c + d*x)^(2/3))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{1}{3}}}{b^4 dx^5 + a^4 c + (b^4 c + 4 ab^3 d)x^4 + 2(2 ab^3 c + 3 a^2 b^2 d)x^3 + 2(3 a^2 b^2 c + 2 a^3 b d)x^2 + (4 a^3 b c + a^4 d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/3)/(d*x+c)^(2/3),x, algorithm="fricas")

[Out] integral((b*x + a)^(1/3)*(d*x + c)^(1/3)/(b^4*d*x^5 + a^4*c + (b^4*c + 4*a*b^3*d)*x^4 + 2*(2*a*b^3*c + 3*a^2*b^2*d)*x^3 + 2*(3*a^2*b^2*c + 2*a^3*b*d)*x^2 + (4*a^3*b*c + a^4*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{11}{3}} (dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/3)/(d*x+c)^(2/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(11/3)*(d*x + c)^(2/3)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{11}{3}} (dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(11/3)/(d*x+c)^(2/3),x)

[Out] int(1/(b*x+a)^(11/3)/(d*x+c)^(2/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{11}{3}} (dx + c)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/3)/(d*x+c)^(2/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(11/3)*(d*x + c)^(2/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{11/3} (c + dx)^{2/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(11/3)*(c + d*x)^(2/3)),x)

[Out] `int(1/((a + b*x)^(11/3)*(c + d*x)^(2/3)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{11}{3}} (c + dx)^{\frac{2}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(11/3)/(d*x+c)**(2/3), x)`

[Out] `Integral(1/((a + b*x)**(11/3)*(c + d*x)**(2/3)), x)`

$$3.1615 \quad \int \frac{(a+bx)^{7/3}}{(c+dx)^{4/3}} dx$$

Optimal. Leaf size=241

$$\frac{7\sqrt[3]{b}(bc-ad)^2 \log(a+bx)}{9d^{10/3}} - \frac{7\sqrt[3]{b}(bc-ad)^2 \log\left(\frac{\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{d}\sqrt[3]{a+bx}} - 1\right)}{3d^{10/3}} - \frac{14\sqrt[3]{b}(bc-ad)^2 \tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt{3}\sqrt[3]{d}\sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{3\sqrt{3}d^{10/3}}$$

[Out] $-3*(b*x+a)^{(7/3)}/d/(d*x+c)^{(1/3)}-14/3*b*(-a*d+b*c)*(b*x+a)^{(1/3)}*(d*x+c)^{(2/3)}/d^3+7/2*b*(b*x+a)^{(4/3)}*(d*x+c)^{(2/3)}/d^2-7/9*b^{(1/3)}*(-a*d+b*c)^2*\ln(b*x+a)/d^{(10/3)}-7/3*b^{(1/3)}*(-a*d+b*c)^2*\ln(-1+b^{(1/3)}*(d*x+c)^{(1/3)}/d^{(1/3)})/(b*x+a)^{(1/3)}/d^{(10/3)}-14/9*b^{(1/3)}*(-a*d+b*c)^2*\arctan(1/3*3^{(1/2)}+2/3*b^{(1/3)}*(d*x+c)^{(1/3)}/d^{(1/3)})/(b*x+a)^{(1/3)*3^{(1/2)}/d^{(10/3)*3^{(1/2)}}$

Rubi [A] time = 0.11, antiderivative size = 241, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {47, 50, 59}

$$\frac{7b(a+bx)^{4/3}(c+dx)^{2/3}}{2d^2} - \frac{14b\sqrt[3]{a+bx}(c+dx)^{2/3}(bc-ad)}{3d^3} - \frac{7\sqrt[3]{b}(bc-ad)^2 \log(a+bx)}{9d^{10/3}} - \frac{7\sqrt[3]{b}(bc-ad)^2 \log\left(\frac{\sqrt[3]{b}}{\sqrt[3]{d}}\right)}{3d^{10/3}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/3)/(c + d*x)^(4/3), x]

[Out] $(-3*(a+b*x)^{(7/3)})/(d*(c+d*x)^{(1/3)}) - (14*b*(b*c-a*d)*(a+b*x)^{(1/3)}*(c+d*x)^{(2/3)})/(3*d^3) + (7*b*(a+b*x)^{(4/3)}*(c+d*x)^{(2/3)})/(2*d^2) - (14*b^{(1/3)}*(b*c-a*d)^2*\text{ArcTan}[1/\text{Sqrt}[3] + (2*b^{(1/3)}*(c+d*x)^{(1/3)})/(\text{Sqrt}[3]*d^{(1/3)}*(a+b*x)^{(1/3)})]/(3*\text{Sqrt}[3]*d^{(10/3)}) - (7*b^{(1/3)}*(b*c-a*d)^2*\text{Log}[a+b*x])/ (9*d^{(10/3)}) - (7*b^{(1/3)}*(b*c-a*d)^2*\text{Log}[-1+(b^{(1/3)}*(c+d*x)^{(1/3)})/d^{(1/3)}*(a+b*x)^{(1/3)})]/(3*d^{(10/3)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 59

```
Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] :=
With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt
[3]*(c + d*x)^(1/3)) + 1/Sqrt[3]])/d, x] + (-Simp[(3*q*Log[q*(a + b*x)^(1/
3))]/(c + d*x)^(1/3) - 1]/(2*d), x] - Simp[(q*Log[c + d*x])/(2*d), x]] /;
FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]
```

Rubi steps

$$\begin{aligned} \int \frac{(a + bx)^{7/3}}{(c + dx)^{4/3}} dx &= -\frac{3(a + bx)^{7/3}}{d\sqrt[3]{c + dx}} + \frac{(7b) \int \frac{(a+bx)^{4/3}}{\sqrt[3]{c+dx}} dx}{d} \\ &= -\frac{3(a + bx)^{7/3}}{d\sqrt[3]{c + dx}} + \frac{7b(a + bx)^{4/3}(c + dx)^{2/3}}{2d^2} - \frac{(14b(bc - ad)) \int \frac{\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} dx}{3d^2} \\ &= -\frac{3(a + bx)^{7/3}}{d\sqrt[3]{c + dx}} - \frac{14b(bc - ad)\sqrt[3]{a + bx}(c + dx)^{2/3}}{3d^3} + \frac{7b(a + bx)^{4/3}(c + dx)^{2/3}}{2d^2} + \frac{(14b(bc - ad)^2)}{3d^2} \\ &= -\frac{3(a + bx)^{7/3}}{d\sqrt[3]{c + dx}} - \frac{14b(bc - ad)\sqrt[3]{a + bx}(c + dx)^{2/3}}{3d^3} + \frac{7b(a + bx)^{4/3}(c + dx)^{2/3}}{2d^2} - \frac{14\sqrt[3]{b}(bc - ad)^2}{3d^2} \end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.30

$$\frac{3(a + bx)^{10/3} \left(\frac{b(c+dx)}{bc-ad} \right)^{4/3} {}_2F_1 \left(\frac{4}{3}, \frac{10}{3}; \frac{13}{3}; \frac{d(a+bx)}{ad-bc} \right)}{10b(c + dx)^{4/3}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*x)^(7/3)/(c + d*x)^(4/3), x]
```

```
[Out] (3*(a + b*x)^(10/3)*((b*(c + d*x))/(b*c - a*d))^(4/3)*Hypergeometric2F1[4/3,
10/3, 13/3, (d*(a + b*x))/(-b*c + a*d)]/(10*b*(c + d*x)^(4/3))
```

fricas [B] time = 0.45, size = 423, normalized size = 1.76

$$28\sqrt{3}\left(b^2c^3 - 2abc^2d + a^2cd^2 + (b^2c^2d - 2abcd^2 + a^2d^3)x\right)\left(-\frac{b}{d}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}d\left(-\frac{b}{d}\right)^{\frac{2}{3}} + \sqrt{3}(bdx+bc)}{3(bdx+bc)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/3)/(d*x+c)^(4/3),x, algorithm="fricas")

[Out]
$$-1/18*(28*\sqrt{3}*(b^2*c^3 - 2*a*b*c^2*d + a^2*c*d^2 + (b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3)*x)*(-b/d)^{(1/3)}*\arctan(1/3*(2*\sqrt{3}*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)}*d*(-b/d)^{(2/3)} + \sqrt{3}*(b*d*x + b*c))/(b*d*x + b*c)) + 14*(b^2*c^3 - 2*a*b*c^2*d + a^2*c*d^2 + (b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3)*x)*(-b/d)^{(1/3)}*\log(((d*x + c)*(-b/d)^{(2/3)} - (b*x + a)^{(1/3)}*(d*x + c)^{(2/3)}*(-b/d)^{(1/3)} + (b*x + a)^{(2/3)}*(d*x + c)^{(1/3)))/(d*x + c)) - 28*(b^2*c^3 - 2*a*b*c^2*d + a^2*c*d^2 + (b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3)*x)*(-b/d)^{(1/3)}*\log(((d*x + c)*(-b/d)^{(1/3)} + (b*x + a)^{(1/3)}*(d*x + c)^{(2/3)))/(d*x + c)) - 3*(3*b^2*d^2*x^2 - 28*b^2*c^2 + 49*a*b*c*d - 18*a^2*d^2 - (7*b^2*c*d - 13*a*b*d^2)*x)*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)))/(d^4*x + c*d^3)$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{7}{3}}}{(dx+c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/3)/(d*x+c)^(4/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(7/3)/(d*x + c)^(4/3), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{7}{3}}}{(dx+c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/3)/(d*x+c)^(4/3),x)

[Out] int((b*x+a)^(7/3)/(d*x+c)^(4/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/3)/(d*x+c)^(4/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/3)/(d*x + c)^(4/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{\frac{7}{3}}}{(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/3)/(c + d*x)^(4/3), x)

[Out] int((a + b*x)^(7/3)/(c + d*x)^(4/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{7}{3}}}{(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/3)/(d*x+c)**(4/3), x)

[Out] Integral((a + b*x)**(7/3)/(c + d*x)**(4/3), x)

$$3.1616 \quad \int \frac{(a+bx)^{4/3}}{(c+dx)^{4/3}} dx$$

Optimal. Leaf size=195

$$\frac{2\sqrt[3]{b}(bc-ad)\log(a+bx)}{3d^{7/3}} + \frac{2\sqrt[3]{b}(bc-ad)\log\left(\frac{\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{d}\sqrt[3]{a+bx}} - 1\right)}{d^{7/3}} + \frac{4\sqrt[3]{b}(bc-ad)\tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt{3}\sqrt[3]{d}\sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{\sqrt{3}d^{7/3}} + \frac{4b\sqrt[3]{a}}{d^{7/3}}$$

[Out] $-3*(b*x+a)^{(4/3)}/d/(d*x+c)^{(1/3)}+4*b*(b*x+a)^{(1/3)}*(d*x+c)^{(2/3)}/d^2+2/3*b^{(1/3)}*(-a*d+b*c)*\ln(b*x+a)/d^{(7/3)}+2*b^{(1/3)}*(-a*d+b*c)*\ln(-1+b^{(1/3)}*(d*x+c)^{(1/3)}/d^{(1/3)}/(b*x+a)^{(1/3)})/d^{(7/3)}+4/3*b^{(1/3)}*(-a*d+b*c)*\arctan(1/3*3^{(1/2)}+2/3*b^{(1/3)}*(d*x+c)^{(1/3)}/d^{(1/3)}/(b*x+a)^{(1/3)}*3^{(1/2)})/d^{(7/3)}*3^{(1/2)}$

Rubi [A] time = 0.07, antiderivative size = 195, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {47, 50, 59}

$$\frac{4b\sqrt[3]{a+bx}(c+dx)^{2/3}}{d^2} + \frac{2\sqrt[3]{b}(bc-ad)\log(a+bx)}{3d^{7/3}} + \frac{2\sqrt[3]{b}(bc-ad)\log\left(\frac{\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{d}\sqrt[3]{a+bx}} - 1\right)}{d^{7/3}} + \frac{4\sqrt[3]{b}(bc-ad)\tan^{-1}\left(\frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt{3}\sqrt[3]{d}\sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{\sqrt{3}d^{7/3}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(4/3)/(c + d*x)^(4/3), x]

[Out] $(-3*(a+b*x)^{(4/3)})/(d*(c+d*x)^{(1/3)})+(4*b*(a+b*x)^{(1/3)}*(c+d*x)^{(2/3)})/d^2+(4*b^{(1/3)}*(b*c-a*d)*\text{ArcTan}[1/\text{Sqrt}[3]+(2*b^{(1/3)}*(c+d*x)^{(1/3)})/(\text{Sqrt}[3]*d^{(1/3)}*(a+b*x)^{(1/3)})]/(\text{Sqrt}[3]*d^{(7/3)})+(2*b^{(1/3)}*(b*c-a*d)*\text{Log}[a+b*x])/ (3*d^{(7/3)})+(2*b^{(1/3)}*(b*c-a*d)*\text{Log}[-1+(b^{(1/3)}*(c+d*x)^{(1/3)})/(d^{(1/3)}*(a+b*x)^{(1/3)})]/d^{(7/3)}$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/

```
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 59

```
Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] :>
With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt
[3]*(c + d*x)^(1/3)) + 1/Sqrt[3]])/d, x] + (-Simp[(3*q*Log[(q*(a + b*x)^(1/
3)))/(c + d*x)^(1/3) - 1])/(2*d), x] - Simp[(q*Log[c + d*x])/(2*d), x]] /;
FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]
```

Rubi steps

$$\begin{aligned} \int \frac{(a + bx)^{4/3}}{(c + dx)^{4/3}} dx &= -\frac{3(a + bx)^{4/3}}{d\sqrt[3]{c + dx}} + \frac{(4b) \int \frac{\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} dx}{d} \\ &= -\frac{3(a + bx)^{4/3}}{d\sqrt[3]{c + dx}} + \frac{4b\sqrt[3]{a + bx}(c + dx)^{2/3}}{d^2} - \frac{(4b(bc - ad)) \int \frac{1}{(a+bx)^{2/3}\sqrt[3]{c+dx}} dx}{3d^2} \\ &= -\frac{3(a + bx)^{4/3}}{d\sqrt[3]{c + dx}} + \frac{4b\sqrt[3]{a + bx}(c + dx)^{2/3}}{d^2} + \frac{4\sqrt[3]{b}(bc - ad) \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt{3}\sqrt[3]{d}\sqrt[3]{a+bx}}\right)}{\sqrt{3}d^{7/3}} + \frac{2\sqrt[3]{b}(bc - ad)}{3d^2} \end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.37

$$\frac{3(a + bx)^{7/3} \left(\frac{b(c+dx)}{bc-ad}\right)^{4/3} {}_2F_1\left(\frac{4}{3}, \frac{7}{3}; \frac{10}{3}; \frac{d(a+bx)}{ad-bc}\right)}{7b(c + dx)^{4/3}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*x)^(4/3)/(c + d*x)^(4/3), x]
```

```
[Out] (3*(a + b*x)^(7/3)*((b*(c + d*x))/(b*c - a*d))^(4/3)*Hypergeometric2F1[4/3,
7/3, 10/3, (d*(a + b*x))/(-b*c + a*d)]/(7*b*(c + d*x)^(4/3))
```


fricas [A] time = 0.48, size = 306, normalized size = 1.57

$$4\sqrt{3}\left(bc^2 - acd + (bcd - ad^2)x\right)\left(-\frac{b}{d}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}d\left(-\frac{b}{d}\right)^{\frac{2}{3}} + \sqrt{3}(bdx+bc)}{3(bdx+bc)}\right) + 2\left(bc^2 - acd + (bcd - ad^2)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/(d*x+c)^(4/3),x, algorithm="fricas")

[Out] 1/3*(4*sqrt(3)*(b*c^2 - a*c*d + (b*c*d - a*d^2)*x)*(-b/d)^(1/3)*arctan(1/3*(2*sqrt(3)*(b*x + a)^(1/3)*(d*x + c)^(2/3)*d*(-b/d)^(2/3) + sqrt(3)*(b*d*x + b*c))/(b*d*x + b*c)) + 2*(b*c^2 - a*c*d + (b*c*d - a*d^2)*x)*(-b/d)^(1/3)*log(((d*x + c)*(-b/d)^(2/3) - (b*x + a)^(1/3)*(d*x + c)^(2/3)*(-b/d)^(1/3) + (b*x + a)^(2/3)*(d*x + c)^(1/3))/(d*x + c)) - 4*(b*c^2 - a*c*d + (b*c*d - a*d^2)*x)*(-b/d)^(1/3)*log(((d*x + c)*(-b/d)^(1/3) + (b*x + a)^(1/3)*(d*x + c)^(2/3))/(d*x + c)) + 3*(b*d*x + 4*b*c - 3*a*d)*(b*x + a)^(1/3)*(d*x + c)^(2/3))/(d^3*x + c*d^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{4}{3}}}{(dx+c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/(d*x+c)^(4/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(4/3)/(d*x + c)^(4/3), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{4}{3}}}{(dx+c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(4/3)/(d*x+c)^(4/3),x)

[Out] int((b*x+a)^(4/3)/(d*x+c)^(4/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{4}{3}}}{(dx+c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(4/3)/(d*x+c)^(4/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(4/3)/(d*x + c)^(4/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{4/3}}{(c + dx)^{4/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(4/3)/(c + d*x)^(4/3),x)

[Out] int((a + b*x)^(4/3)/(c + d*x)^(4/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{4}{3}}}{(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(4/3)/(d*x+c)**(4/3),x)

[Out] Integral((a + b*x)**(4/3)/(c + d*x)**(4/3), x)

$$3.1617 \quad \int \frac{\sqrt[3]{a+bx}}{(c+dx)^{4/3}} dx$$

Optimal. Leaf size=149

$$\frac{3\sqrt[3]{b} \log\left(\frac{\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{d} \sqrt[3]{a+bx}} - 1\right)}{2d^{4/3}} - \frac{\sqrt{3} \sqrt[3]{b} \tan^{-1}\left(\frac{2\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt{3} \sqrt[3]{d} \sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{d^{4/3}} - \frac{3\sqrt[3]{a+bx}}{d\sqrt[3]{c+dx}} - \frac{\sqrt[3]{b} \log(a+bx)}{2d^{4/3}}$$

[Out] $-3*(b*x+a)^{(1/3)}/d/(d*x+c)^{(1/3)}-1/2*b^{(1/3)}*\ln(b*x+a)/d^{(4/3)}-3/2*b^{(1/3)}*\ln(-1+b^{(1/3)}*(d*x+c)^{(1/3)}/d^{(1/3)}/(b*x+a)^{(1/3)})/d^{(4/3)}-b^{(1/3)}*\arctan(1/3*3^{(1/2)}+2/3*b^{(1/3)}*(d*x+c)^{(1/3)}/d^{(1/3)}/(b*x+a)^{(1/3)}*3^{(1/2)})/d^{(4/3)}$

Rubi [A] time = 0.03, antiderivative size = 149, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {47, 59}

$$\frac{3\sqrt[3]{b} \log\left(\frac{\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{d} \sqrt[3]{a+bx}} - 1\right)}{2d^{4/3}} - \frac{\sqrt{3} \sqrt[3]{b} \tan^{-1}\left(\frac{2\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt{3} \sqrt[3]{d} \sqrt[3]{a+bx}} + \frac{1}{\sqrt{3}}\right)}{d^{4/3}} - \frac{3\sqrt[3]{a+bx}}{d\sqrt[3]{c+dx}} - \frac{\sqrt[3]{b} \log(a+bx)}{2d^{4/3}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/3)/(c + d*x)^(4/3), x]

[Out] $(-3*(a + b*x)^{(1/3)})/(d*(c + d*x)^{(1/3)}) - (\text{Sqrt}[3]*b^{(1/3)}*\text{ArcTan}[1/\text{Sqrt}[3] + (2*b^{(1/3)}*(c + d*x)^{(1/3)})/(\text{Sqrt}[3]*d^{(1/3)}*(a + b*x)^{(1/3)})])/d^{(4/3)} - (b^{(1/3)}*\text{Log}[a + b*x])/(2*d^{(4/3)}) - (3*b^{(1/3)}*\text{Log}[-1 + (b^{(1/3)}*(c + d*x)^{(1/3)})/d^{(1/3)}*(a + b*x)^{(1/3)}])/d^{(4/3)})/(2*d^{(4/3)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 59

Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] := With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt[3]*(c + d*x)^(1/3)) + 1/Sqrt[3]])/d, x] + (-Simp[(3*q*Log[(q*(a + b*x)^(1/3)/

3))/(c + d*x)^(1/3) - 1)/(2*d), x] - Simp[(q*Log[c + d*x])/(2*d), x]] /;
 FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]

Rubi steps

$$\int \frac{\sqrt[3]{a+bx}}{(c+dx)^{4/3}} dx = -\frac{3\sqrt[3]{a+bx}}{d\sqrt[3]{c+dx}} + \frac{b \int \frac{1}{(a+bx)^{2/3} \sqrt[3]{c+dx}} dx}{d}$$

$$= -\frac{3\sqrt[3]{a+bx}}{d\sqrt[3]{c+dx}} - \frac{\sqrt{3} \sqrt[3]{b} \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt{3} \sqrt[3]{d} \sqrt[3]{a+bx}}\right)}{d^{4/3}} - \frac{\sqrt[3]{b} \log(a+bx)}{2d^{4/3}} - \frac{3\sqrt[3]{b} \log\left(-1 + \frac{\sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{d} \sqrt[3]{a+bx}}\right)}{2d^{4/3}}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.49

$$\frac{3(a+bx)^{4/3} \left(\frac{b(c+dx)}{bc-ad}\right)^{4/3} {}_2F_1\left(\frac{4}{3}, \frac{4}{3}, \frac{7}{3}, \frac{d(a+bx)}{ad-bc}\right)}{4b(c+dx)^{4/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/3)/(c + d*x)^(4/3), x]

[Out] (3*(a + b*x)^(4/3)*((b*(c + d*x))/(b*c - a*d))^(4/3)*Hypergeometric2F1[4/3, 4/3, 7/3, (d*(a + b*x))/(-b*c + a*d)]/(4*b*(c + d*x)^(4/3))

fricas [B] time = 0.45, size = 233, normalized size = 1.56

$$2\sqrt{3}(dx+c)\left(-\frac{b}{d}\right)^{\frac{1}{3}} \arctan\left(\frac{2\sqrt{3}(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}d\left(-\frac{b}{d}\right)^{\frac{2}{3}}+\sqrt{3}(bdx+bc)}{3(bdx+bc)}\right) + (dx+c)\left(-\frac{b}{d}\right)^{\frac{1}{3}} \log\left(\frac{(dx+c)\left(-\frac{b}{d}\right)^{\frac{2}{3}}-(bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}}{dx+c}\right)$$

$$2(d^2x + cd)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/(d*x+c)^(4/3), x, algorithm="fricas")

[Out] -1/2*(2*sqrt(3)*(d*x + c)*(-b/d)^(1/3)*arctan(1/3*(2*sqrt(3)*(b*x + a)^(1/3)*(d*x + c)^(2/3)*d*(-b/d)^(2/3) + sqrt(3)*(b*d*x + b*c))/(b*d*x + b*c)) + (d*x + c)*(-b/d)^(1/3)*log(((d*x + c)*(-b/d)^(2/3) - (b*x + a)^(1/3)*(d*x + c)^(2/3)*(-b/d)^(1/3) + (b*x + a)^(2/3)*(d*x + c)^(1/3))/(d*x + c)) - 2*(d*x + c)*(-b/d)^(1/3)*log(((d*x + c)*(-b/d)^(1/3) + (b*x + a)^(1/3)*(d*x + c)^(2/3))/(d*x + c)) + 6*(b*x + a)^(1/3)*(d*x + c)^(2/3)/(d^2*x + c*d)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/(d*x+c)^(4/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/3)/(d*x + c)^(4/3), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/3)/(d*x+c)^(4/3),x)

[Out] int((b*x+a)^(1/3)/(d*x+c)^(4/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/3)/(d*x+c)^(4/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/3)/(d*x + c)^(4/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{1/3}}{(c + dx)^{4/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/3)/(c + d*x)^(4/3),x)

[Out] int((a + b*x)^(1/3)/(c + d*x)^(4/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[3]{a+bx}}{(c+dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/3)/(d*x+c)**(4/3),x)

[Out] Integral((a + b*x)**(1/3)/(c + d*x)**(4/3), x)

$$3.1618 \quad \int \frac{1}{(a+bx)^{2/3}(c+dx)^{4/3}} dx$$

Optimal. Leaf size=30

$$\frac{3\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}(bc-ad)}$$

[Out] $3*(b*x+a)^{(1/3)/(-a*d+b*c)/(d*x+c)^{(1/3)}$

Rubi [A] time = 0.00, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{3\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)^{(2/3})*(c + d*x)^{(4/3})), x]$

[Out] $(3*(a + b*x)^{(1/3}))/((b*c - a*d)*(c + d*x)^{(1/3}))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp} [((a + b*x)^{(m + 1})*(c + d*x)^{(n + 1}))/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{1}{(a+bx)^{2/3}(c+dx)^{4/3}} dx = \frac{3\sqrt[3]{a+bx}}{(bc-ad)\sqrt[3]{c+dx}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$\frac{3\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/((a + b*x)^{(2/3})*(c + d*x)^{(4/3})), x]$

[Out] $(3*(a + b*x)^{(1/3)})/((b*c - a*d)*(c + d*x)^{(1/3}))$

fricas [A] time = 0.46, size = 42, normalized size = 1.40

$$\frac{3 (bx + a)^{\frac{1}{3}} (dx + c)^{\frac{2}{3}}}{bc^2 - acd + (bcd - ad^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(2/3)/(d*x+c)^(4/3),x, algorithm="fricas")`

[Out] $3*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)}/(b*c^2 - a*c*d + (b*c*d - a*d^2)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(2/3)/(d*x+c)^(4/3),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(2/3)*(d*x + c)^(4/3)), x)`

maple [A] time = 0.00, size = 27, normalized size = 0.90

$$-\frac{3 (bx + a)^{\frac{1}{3}}}{(dx + c)^{\frac{1}{3}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(2/3)/(d*x+c)^(4/3),x)`

[Out] $-3*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(a*d-b*c)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(2/3)/(d*x+c)^(4/3),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(2/3)*(d*x + c)^(4/3)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{1}{(a + bx)^{2/3} (c + dx)^{4/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(2/3)*(c + d*x)^(4/3)), x)

[Out] int(1/((a + b*x)^(2/3)*(c + d*x)^(4/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{2}{3}} (c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(2/3)/(d*x+c)**(4/3), x)

[Out] Integral(1/((a + b*x)**(2/3)*(c + d*x)**(4/3)), x)

$$3.1619 \quad \int \frac{1}{(a+bx)^{5/3}(c+dx)^{4/3}} dx$$

Optimal. Leaf size=66

$$-\frac{9d\sqrt[3]{a+bx}}{2\sqrt[3]{c+dx}(bc-ad)^2} - \frac{3}{2(a+bx)^{2/3}\sqrt[3]{c+dx}(bc-ad)}$$

[Out] $-3/2/(-a*d+b*c)/(b*x+a)^{(2/3)}/(d*x+c)^{(1/3)}-9/2*d*(b*x+a)^{(1/3)/(-a*d+b*c)^{2/(d*x+c)^{(1/3)}}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{9d\sqrt[3]{a+bx}}{2\sqrt[3]{c+dx}(bc-ad)^2} - \frac{3}{2(a+bx)^{2/3}\sqrt[3]{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/3)*(c + d*x)^(4/3)),x]

[Out] $-3/(2*(b*c - a*d)*(a + b*x)^{(2/3)*(c + d*x)^{(1/3)}) - (9*d*(a + b*x)^{(1/3)})/(2*(b*c - a*d)^{2*(c + d*x)^{(1/3)}}$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  (((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{(a+bx)^{5/3}(c+dx)^{4/3}} dx = -\frac{3}{2(bc-ad)(a+bx)^{2/3}\sqrt[3]{c+dx}} - \frac{(3d) \int \frac{1}{(a+bx)^{2/3}(c+dx)^{4/3}} dx}{2(bc-ad)}$$

$$= -\frac{3}{2(bc-ad)(a+bx)^{2/3}\sqrt[3]{c+dx}} - \frac{9d\sqrt[3]{a+bx}}{2(bc-ad)^2\sqrt[3]{c+dx}}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 0.68

$$-\frac{3(2ad + b(c + 3dx))}{2(a + bx)^{2/3}\sqrt[3]{c + dx}(bc - ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/3)*(c + d*x)^(4/3)), x]

[Out] (-3*(2*a*d + b*(c + 3*d*x)))/(2*(b*c - a*d)^2*(a + b*x)^(2/3)*(c + d*x)^(1/3))

fricas [B] time = 0.42, size = 126, normalized size = 1.91

$$\frac{3(3bdx + bc + 2ad)(bx + a)^{\frac{1}{3}}(dx + c)^{\frac{2}{3}}}{2(ab^2c^3 - 2a^2bc^2d + a^3cd^2 + (b^3c^2d - 2ab^2cd^2 + a^2bd^3)x^2 + (b^3c^3 - ab^2c^2d - a^2bcd^2 + a^3d^3)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/3)/(d*x+c)^(4/3), x, algorithm="fricas")

[Out] -3/2*(3*b*d*x + b*c + 2*a*d)*(b*x + a)^(1/3)*(d*x + c)^(2/3)/(a*b^2*c^3 - 2*a^2*b*c^2*d + a^3*c*d^2 + (b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*x^2 + (b^3*c^3 - a*b^2*c^2*d - a^2*b*c*d^2 + a^3*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{3}}(dx+c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/3)/(d*x+c)^(4/3), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/3)*(d*x + c)^(4/3)), x)

maple [A] time = 0.00, size = 53, normalized size = 0.80

$$\frac{3(3bdx + 2ad + bc)}{2(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{1}{3}}(a^2d^2 - 2abcd + b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(5/3)/(d*x+c)^(4/3),x)`

[Out] `-3/2*(3*b*d*x+2*a*d+b*c)/(b*x+a)^(2/3)/(d*x+c)^(1/3)/(a^2*d^2-2*a*b*c*d+b^2*c^2)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{3}}(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/3)/(d*x+c)^(4/3),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(5/3)*(d*x + c)^(4/3)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{1}{(a + bx)^{\frac{5}{3}}(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(5/3)*(c + d*x)^(4/3)),x)`

[Out] `int(1/((a + b*x)^(5/3)*(c + d*x)^(4/3)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{5}{3}}(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/3)/(d*x+c)**(4/3),x)`

[Out] `Integral(1/((a + b*x)**(5/3)*(c + d*x)**(4/3)), x)`

$$3.1620 \quad \int \frac{1}{(a+bx)^{8/3}(c+dx)^{4/3}} dx$$

Optimal. Leaf size=101

$$\frac{27d^2\sqrt[3]{a+bx}}{5\sqrt[3]{c+dx}(bc-ad)^3} + \frac{9d}{5(a+bx)^{2/3}\sqrt[3]{c+dx}(bc-ad)^2} - \frac{3}{5(a+bx)^{5/3}\sqrt[3]{c+dx}(bc-ad)}$$

[Out] $-3/5/(-a*d+b*c)/(b*x+a)^{(5/3)/(d*x+c)^{(1/3)}+9/5*d/(-a*d+b*c)^2/(b*x+a)^{(2/3)/(d*x+c)^{(1/3)}+27/5*d^2*(b*x+a)^{(1/3)/(-a*d+b*c)^3/(d*x+c)^{(1/3)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{27d^2\sqrt[3]{a+bx}}{5\sqrt[3]{c+dx}(bc-ad)^3} + \frac{9d}{5(a+bx)^{2/3}\sqrt[3]{c+dx}(bc-ad)^2} - \frac{3}{5(a+bx)^{5/3}\sqrt[3]{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(8/3)*(c + d*x)^(4/3)), x]

[Out] $-3/(5*(b*c - a*d)*(a + b*x)^{(5/3)*(c + d*x)^{(1/3)}) + (9*d)/(5*(b*c - a*d)^2*(a + b*x)^{(2/3)*(c + d*x)^{(1/3)}) + (27*d^2*(a + b*x)^{(1/3)})/(5*(b*c - a*d)^3*(c + d*x)^{(1/3)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{8/3}(c+dx)^{4/3}} dx &= -\frac{3}{5(bc-ad)(a+bx)^{5/3}\sqrt[3]{c+dx}} - \frac{(6d) \int \frac{1}{(a+bx)^{5/3}(c+dx)^{4/3}} dx}{5(bc-ad)} \\
&= -\frac{3}{5(bc-ad)(a+bx)^{5/3}\sqrt[3]{c+dx}} + \frac{9d}{5(bc-ad)^2(a+bx)^{2/3}\sqrt[3]{c+dx}} + \frac{(9d^2) \int \frac{1}{(a+bx)^{2/3}(c+dx)^{4/3}} dx}{5(bc-ad)^3\sqrt[3]{c+dx}} \\
&= -\frac{3}{5(bc-ad)(a+bx)^{5/3}\sqrt[3]{c+dx}} + \frac{9d}{5(bc-ad)^2(a+bx)^{2/3}\sqrt[3]{c+dx}} + \frac{27d^2\sqrt[3]{a+bx}}{5(bc-ad)^3\sqrt[3]{c+dx}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 75, normalized size = 0.74

$$\frac{3(5a^2d^2 + 5abd(c + 3dx) + b^2(-c^2 + 3cdx + 9d^2x^2))}{5(a+bx)^{5/3}\sqrt[3]{c+dx}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(8/3)*(c + d*x)^(4/3)), x]

[Out] (3*(5*a^2*d^2 + 5*a*b*d*(c + 3*d*x) + b^2*(-c^2 + 3*c*d*x + 9*d^2*x^2)))/(5*(b*c - a*d)^3*(a + b*x)^(5/3)*(c + d*x)^(1/3))

fricas [B] time = 0.45, size = 273, normalized size = 2.70

$$\frac{3(9b^2d^2x^2 - b^2c^2 + 5abcd + 5a^2d^2 + 3(b^2cd + 5abd^2))}{5(a^2b^3c^4 - 3a^3b^2c^3d + 3a^4bc^2d^2 - a^5cd^3 + (b^5c^3d - 3ab^4c^2d^2 + 3a^2b^3cd^3 - a^3b^2d^4)x^3 + (b^5c^4 - ab^4c^3d - 3a^2b^3c^2d^2 + 5a^3b^2c*d^3 - 2a^4*b*d^4)*x^2 + (2*a*b^4*c^4 - 5*a^2*b^3*c^3*d + 3*a^3*b^2*c^2*d^2 + a^4*b*c*d^3 - a^5*d^4)*x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(8/3)/(d*x+c)^(4/3), x, algorithm="fricas")

[Out] 3/5*(9*b^2*d^2*x^2 - b^2*c^2 + 5*a*b*c*d + 5*a^2*d^2 + 3*(b^2*c*d + 5*a*b*d^2)*x)*(b*x + a)^(1/3)*(d*x + c)^(2/3)/(a^2*b^3*c^4 - 3*a^3*b^2*c^3*d + 3*a^4*b*c^2*d^2 - a^5*c*d^3 + (b^5*c^3*d - 3*a*b^4*c^2*d^2 + 3*a^2*b^3*c*d^3 - a^3*b^2*d^4)*x^3 + (b^5*c^4 - a*b^4*c^3*d - 3*a^2*b^3*c^2*d^2 + 5*a^3*b^2*c*d^3 - 2*a^4*b*d^4)*x^2 + (2*a*b^4*c^4 - 5*a^2*b^3*c^3*d + 3*a^3*b^2*c^2*d^2 + a^4*b*c*d^3 - a^5*d^4)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{8}{3}}(dx+c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(8/3)/(d*x+c)^(4/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(8/3)*(d*x + c)^(4/3)), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{3(9b^2x^2d^2 + 15abd^2x + 3b^2cdx + 5a^2d^2 + 5abcd - b^2c^2)}{5(bx + a)^{\frac{5}{3}}(dx + c)^{\frac{1}{3}}(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(8/3)/(d*x+c)^(4/3),x)

[Out] -3/5*(9*b^2*d^2*x^2+15*a*b*d^2*x+3*b^2*c*d*x+5*a^2*d^2+5*a*b*c*d-b^2*c^2)/(b*x+a)^(5/3)/(d*x+c)^(1/3)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{8}{3}}(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(8/3)/(d*x+c)^(4/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(8/3)*(d*x + c)^(4/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{\frac{8}{3}}(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(8/3)*(c + d*x)^(4/3)),x)

[Out] int(1/((a + b*x)^(8/3)*(c + d*x)^(4/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{8}{3}}(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(8/3)/(d*x+c)**(4/3),x)

[Out] Integral(1/((a + b*x)**(8/3)*(c + d*x)**(4/3)), x)

$$3.1621 \quad \int \frac{1}{(a+bx)^{11/3}(c+dx)^{4/3}} dx$$

Optimal. Leaf size=136

$$\frac{243d^3\sqrt[3]{a+bx}}{40\sqrt[3]{c+dx}(bc-ad)^4} - \frac{81d^2}{40(a+bx)^{2/3}\sqrt[3]{c+dx}(bc-ad)^3} + \frac{27d}{40(a+bx)^{5/3}\sqrt[3]{c+dx}(bc-ad)^2} - \frac{3}{8(a+bx)^{8/3}\sqrt[3]{c+dx}}$$

[Out] $-3/8/(-a*d+b*c)/(b*x+a)^{(8/3)}/(d*x+c)^{(1/3)}+27/40*d/(-a*d+b*c)^2/(b*x+a)^{(5/3)}/(d*x+c)^{(1/3)}-81/40*d^2/(-a*d+b*c)^3/(b*x+a)^{(2/3)}/(d*x+c)^{(1/3)}-243/40*d^3*(b*x+a)^{(1/3)}/(-a*d+b*c)^4/(d*x+c)^{(1/3)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{243d^3\sqrt[3]{a+bx}}{40\sqrt[3]{c+dx}(bc-ad)^4} - \frac{81d^2}{40(a+bx)^{2/3}\sqrt[3]{c+dx}(bc-ad)^3} + \frac{27d}{40(a+bx)^{5/3}\sqrt[3]{c+dx}(bc-ad)^2} - \frac{3}{8(a+bx)^{8/3}\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(11/3)*(c + d*x)^(4/3)),x]

[Out] $-3/(8*(b*c - a*d)*(a + b*x)^{(8/3)*(c + d*x)^{(1/3)}) + (27*d)/(40*(b*c - a*d)^2*(a + b*x)^{(5/3)*(c + d*x)^{(1/3)}) - (81*d^2)/(40*(b*c - a*d)^3*(a + b*x)^{(2/3)*(c + d*x)^{(1/3)}) - (243*d^3*(a + b*x)^{(1/3)})/(40*(b*c - a*d)^4*(c + d*x)^{(1/3)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{11/3}(c+dx)^{4/3}} dx &= -\frac{3}{8(bc-ad)(a+bx)^{8/3}\sqrt[3]{c+dx}} - \frac{(9d) \int \frac{1}{(a+bx)^{8/3}(c+dx)^{4/3}} dx}{8(bc-ad)} \\
&= -\frac{3}{8(bc-ad)(a+bx)^{8/3}\sqrt[3]{c+dx}} + \frac{27d}{40(bc-ad)^2(a+bx)^{5/3}\sqrt[3]{c+dx}} + \frac{(27d^2) \int \frac{1}{(a+bx)^{5/3}(c+dx)^{4/3}} dx}{20(bc-ad)^2} \\
&= -\frac{3}{8(bc-ad)(a+bx)^{8/3}\sqrt[3]{c+dx}} + \frac{27d}{40(bc-ad)^2(a+bx)^{5/3}\sqrt[3]{c+dx}} - \frac{27d^2}{40(bc-ad)^3} \\
&= -\frac{3}{8(bc-ad)(a+bx)^{8/3}\sqrt[3]{c+dx}} + \frac{27d}{40(bc-ad)^2(a+bx)^{5/3}\sqrt[3]{c+dx}} - \frac{27d^2}{40(bc-ad)^3}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 116, normalized size = 0.85

$$\frac{3(40a^3d^3 + 60a^2bd^2(c+3dx) + 24ab^2d(-c^2 + 3cdx + 9d^2x^2) + b^3(5c^3 - 9c^2dx + 27cd^2x^2 + 81d^3x^3))}{40(a+bx)^{8/3}\sqrt[3]{c+dx}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(11/3)*(c + d*x)^(4/3)), x]

[Out] (-3*(40*a^3*d^3 + 60*a^2*b*d^2*(c + 3*d*x) + 24*a*b^2*d*(-c^2 + 3*c*d*x + 9*d^2*x^2) + b^3*(5*c^3 - 9*c^2*d*x + 27*c*d^2*x^2 + 81*d^3*x^3)))/(40*(b*c - a*d)^4*(a + b*x)^(8/3)*(c + d*x)^(1/3))

fricas [B] time = 0.53, size = 456, normalized size = 3.35

$$\frac{3(81b^3d^3x^3 + 5b^3c^3 - 24a^2b^2c^2d + 60a^2b^2cd^2 + 40a^3d^3 + 27(b^3cd^2 + 8a^2b^2d^3)x^2 - 9(b^3c^2d - 8a^2b^2cd^2 - 20a^2b^2d^3)x)(b^3x + a)^{1/3}(d^2x + c)^{2/3}}{40(a^3b^4c^5 - 4a^4b^3c^4d + 6a^5b^2c^3d^2 - 4a^6bc^2d^3 + a^7cd^4 + (b^7c^4d - 4ab^6c^3d^2 + 6a^2b^5c^2d^3 - 4a^3b^4cd^4 + a^4b^3c^3d^5 - 4a^5b^2c^2d^4 + 4a^6b^2cd^3 - 4a^7b^2d^2 + 6a^8b^2d^2 - 4a^9b^2d^2 + a^{10}b^2d^2)x^4 + (b^7c^4d - 4ab^6c^3d^2 + 6a^2b^5c^2d^3 - 4a^3b^4cd^4 + a^4b^3c^3d^5 - 4a^5b^2c^2d^4 + 4a^6b^2cd^3 - 4a^7b^2d^2 + 6a^8b^2d^2 - 4a^9b^2d^2 + a^{10}b^2d^2)x^3 + (b^7c^4d - 4ab^6c^3d^2 + 6a^2b^5c^2d^3 - 4a^3b^4cd^4 + a^4b^3c^3d^5 - 4a^5b^2c^2d^4 + 4a^6b^2cd^3 - 4a^7b^2d^2 + 6a^8b^2d^2 - 4a^9b^2d^2 + a^{10}b^2d^2)x^2 + (b^7c^4d - 4ab^6c^3d^2 + 6a^2b^5c^2d^3 - 4a^3b^4cd^4 + a^4b^3c^3d^5 - 4a^5b^2c^2d^4 + 4a^6b^2cd^3 - 4a^7b^2d^2 + 6a^8b^2d^2 - 4a^9b^2d^2 + a^{10}b^2d^2)x + (b^7c^4d - 4ab^6c^3d^2 + 6a^2b^5c^2d^3 - 4a^3b^4cd^4 + a^4b^3c^3d^5 - 4a^5b^2c^2d^4 + 4a^6b^2cd^3 - 4a^7b^2d^2 + 6a^8b^2d^2 - 4a^9b^2d^2 + a^{10}b^2d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/3)/(d*x+c)^(4/3), x, algorithm="fricas")

[Out] -3/40*(81*b^3*d^3*x^3 + 5*b^3*c^3 - 24*a*b^2*c^2*d + 60*a^2*b*c*d^2 + 40*a^3*d^3 + 27*(b^3*c*d^2 + 8*a*b^2*d^3)*x^2 - 9*(b^3*c^2*d - 8*a*b^2*c*d^2 - 20*a^2*b*d^3)*x)*(b*x + a)^(1/3)*(d*x + c)^(2/3)/(a^3*b^4*c^5 - 4*a^4*b^3*c^4*d + 6*a^5*b^2*c^3*d^2 - 4*a^6*b*c^2*d^3 + a^7*c*d^4 + (b^7*c^4*d - 4*a*b^6*c^3*d^2 + 6*a^2*b^5*c^2*d^3 - 4*a^3*b^4*c*d^4 + a^4*b^3*c^3*d^5 - 4*a^5*b^2*c^2*d^4 + 4*a^6*b^2*c*d^3 - 4*a^7*b^2*d^2 + 6*a^8*b^2*d^2 - 4*a^9*b^2*d^2 + a^10*b^2*d^2)*x^4 + (b^7*c^4*d - 4*a*b^6*c^3*d^2 + 6*a^2*b^5*c^2*d^3 - 4*a^3*b^4*c*d^4 + a^4*b^3*c^3*d^5 - 4*a^5*b^2*c^2*d^4 + 4*a^6*b^2*c*d^3 - 4*a^7*b^2*d^2 + 6*a^8*b^2*d^2 - 4*a^9*b^2*d^2 + a^10*b^2*d^2)*x^3 + (b^7*c^4*d - 4*a*b^6*c^3*d^2 + 6*a^2*b^5*c^2*d^3 - 4*a^3*b^4*c*d^4 + a^4*b^3*c^3*d^5 - 4*a^5*b^2*c^2*d^4 + 4*a^6*b^2*c*d^3 - 4*a^7*b^2*d^2 + 6*a^8*b^2*d^2 - 4*a^9*b^2*d^2 + a^10*b^2*d^2)*x^2 + (b^7*c^4*d - 4*a*b^6*c^3*d^2 + 6*a^2*b^5*c^2*d^3 - 4*a^3*b^4*c*d^4 + a^4*b^3*c^3*d^5 - 4*a^5*b^2*c^2*d^4 + 4*a^6*b^2*c*d^3 - 4*a^7*b^2*d^2 + 6*a^8*b^2*d^2 - 4*a^9*b^2*d^2 + a^10*b^2*d^2)*x + (b^7*c^4*d - 4*a*b^6*c^3*d^2 + 6*a^2*b^5*c^2*d^3 - 4*a^3*b^4*c*d^4 + a^4*b^3*c^3*d^5 - 4*a^5*b^2*c^2*d^4 + 4*a^6*b^2*c*d^3 - 4*a^7*b^2*d^2 + 6*a^8*b^2*d^2 - 4*a^9*b^2*d^2 + a^10*b^2*d^2)

$$\begin{aligned} &^5 - a*b^6*c^4*d - 6*a^2*b^5*c^3*d^2 + 14*a^3*b^4*c^2*d^3 - 11*a^4*b^3*c*d^4 \\ &+ 3*a^5*b^2*d^5)*x^3 + 3*(a*b^6*c^5 - 3*a^2*b^5*c^4*d + 2*a^3*b^4*c^3*d^2 \\ &+ 2*a^4*b^3*c^2*d^3 - 3*a^5*b^2*c*d^4 + a^6*b*d^5)*x^2 + (3*a^2*b^5*c^5 - \\ &11*a^3*b^4*c^4*d + 14*a^4*b^3*c^3*d^2 - 6*a^5*b^2*c^2*d^3 - a^6*b*c*d^4 + a \\ &^7*d^5)*x) \end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{11}{3}}(dx+c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/3)/(d*x+c)^(4/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(11/3)*(d*x + c)^(4/3)), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{3(81b^3d^3x^3 + 216ab^2d^3x^2 + 27b^3cd^2x^2 + 180a^2bd^3x + 72ab^2cd^2x - 9b^3c^2dx + 40a^3d^3 + 60a^2bcd^2 - 24ab^2c^2d - 4a^3b^2cd + b^4c^4)}{40(bx+a)^{\frac{8}{3}}(dx+c)^{\frac{1}{3}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(11/3)/(d*x+c)^(4/3),x)

[Out] -3/40*(81*b^3*d^3*x^3+216*a*b^2*d^3*x^2+27*b^3*c*d^2*x^2+180*a^2*b*d^3*x+72*a*b^2*c*d^2*x-9*b^3*c^2*d*x+40*a^3*d^3+60*a^2*b*c*d^2-24*a*b^2*c^2*d+5*b^3*c^3)/(b*x+a)^(8/3)/(d*x+c)^(1/3)/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{11}{3}}(dx+c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/3)/(d*x+c)^(4/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(11/3)*(d*x + c)^(4/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{11/3}(c+dx)^{4/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(11/3)*(c + d*x)^(4/3)), x)`

[Out] `int(1/((a + b*x)^(11/3)*(c + d*x)^(4/3)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{11}{3}} (c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(11/3)/(d*x+c)**(4/3), x)`

[Out] `Integral(1/((a + b*x)**(11/3)*(c + d*x)**(4/3)), x)`

$$3.1622 \quad \int \frac{(a+bx)^{8/3}}{(c+dx)^{4/3}} dx$$

Optimal. Leaf size=1355

$$15 \cdot 2^{2/3} \sqrt[4]{3} \sqrt{2 - \sqrt{3}} \sqrt[3]{b} \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2} \left((bc-ad)^{2/3} + 2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a+bx)(c+dx)} \right) \sqrt[3]{7d^{11/3} \sqrt[3]{a+bx} \sqrt[3]{c+dx} (bc+ad+2bdx)}$$

[Out] $-3*(b*x+a)^{(8/3)}/d/(d*x+c)^{(1/3)}-30/7*b*(-a*d+b*c)*(b*x+a)^{(2/3)*(d*x+c)^{(2/3)}/d^3+24/7*b*(b*x+a)^{(5/3)*(d*x+c)^{(2/3)}/d^2+30/7*2^{(2/3)*b^{(1/3)*(-a*d+b*c)^2*((b*x+a)*(d*x+c))^{(1/3)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*((a*d+b*(2*d*x+c))^2)^{(1/2)}/d^{(11/3)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})+20/7*2^{(1/6)*3^{(3/4)*b^{(1/3)*(-a*d+b*c)^{(8/3)*((b*x+a)*(d*x+c))^{(1/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)*EllipticF((2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1-3^{(1/2))})/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})}, I*3^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*(((a*d+b*c)^{(4/3)-2^{(2/3)*b^{(1/3)*d^{(1/3)*(-a*d+b*c)^{(2/3)*((b*x+a)*(d*x+c))^{(1/3)+2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((b*x+a)*(d*x+c))^{(2/3)}/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^2)^{(1/2)}/d^{(11/3)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)}/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^2)^{(1/2)-15/7*2^{(2/3)*3^{(1/4)*b^{(1/3)*(-a*d+b*c)^{(8/3)*((b*x+a)*(d*x+c))^{(1/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)*EllipticE((2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1-3^{(1/2))})/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})}, I*3^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*(1/2*6^{(1/2)-1/2*2^{(1/2)))*(((a*d+b*c)^{(4/3)-2^{(2/3)*b^{(1/3)*d^{(1/3)*(-a*d+b*c)^{(2/3)*((b*x+a)*(d*x+c))^{(1/3)+2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((b*x+a)*(d*x+c))^{(2/3)}/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^2)^{(1/2)}/d^{(11/3)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^2)^{(1/2)}}$

Rubi [A] time = 2.51, antiderivative size = 1355, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 7, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.368, Rules used = {47, 50, 62, 623, 303, 218, 1877}

$$15 \cdot 2^{2/3} \sqrt[4]{3} \sqrt{2 - \sqrt{3}} \sqrt[3]{b} \sqrt[3]{(a + bx)(c + dx)} \sqrt{(bc + ad + 2bdx)^2} \left((bc - ad)^{2/3} + 2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} \right)$$

$$7d^{11/3} \sqrt[3]{a + bx} \sqrt[3]{c + dx} (bc + ad + 2bdx)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(8/3)/(c + d*x)^(4/3), x]

[Out]
$$\begin{aligned} & (-3*(a + b*x)^{(8/3)})/(d*(c + d*x)^{(1/3)}) - (30*b*(b*c - a*d)*(a + b*x)^{(2/3)} \\ & *(c + d*x)^{(2/3)})/(7*d^3) + (24*b*(a + b*x)^{(5/3)*(c + d*x)^{(2/3)})/(7*d^2) \\ & + (30*2^{(2/3)*b^{(1/3)}*(b*c - a*d)^2*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c \\ & + a*d + 2*b*d*x)^2]*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]}/(7*d^{(11/3)*(a + b*x)^{(1/3)} \\ & *(c + d*x)^{(1/3)*(b*c + a*d + 2*b*d*x)*((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} \\ & + 2^{(2/3)*b^{(1/3)*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})}) - (15*2^{(2/3)*3^{(1/4)} \\ & *\text{Sqrt}[2 - \text{Sqrt}[3]]*b^{(1/3)*(b*c - a*d)^{(8/3)*((a + b*x)*(c + d*x))^{(1/3)* \\ & \text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)* \\ & ((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c - a*d)^{(4/3)} - 2^{(2/3)*b^{(1/3)*d^{(1/3)* \\ & (1/3)*(b*c - a*d)^{(2/3)*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)*b^{(2/3)*d^{(2/3)} \\ & *((a + b*x)*(c + d*x))^{(2/3)})}/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)* \\ & b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})^2}*\text{EllipticE}[\text{ArcSin}[(1 - \text{Sqrt} \\ & [3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)} \\ &)}/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c \\ & + d*x))^{(1/3)})}], -7 - 4*\text{Sqrt}[3])]/(7*d^{(11/3)*(a + b*x)^{(1/3)*(c + d*x)^{(1/3)} \\ & *(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(b*c - a*d)^{(2/3)*((b*c - a*d)^{(2/3)} + 2^{(2/3)* \\ & b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})})}/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} \\ & + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})^2}*\text{Sqrt}[(a*d \\ & + b*(c + 2*d*x))^2]) + (20*2^{(1/6)*3^{(3/4)*b^{(1/3)*(b*c - a*d)^{(8/3)*((a + \\ & b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2 \\ & ^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c - a*d)^{(4/3)} \\ & - 2^{(2/3)*b^{(1/3)*d^{(1/3)*(b*c - a*d)^{(2/3)*((a + b*x)*(c + d*x))^{(1/3)} + \\ & 2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((a + b*x)*(c + d*x))^{(2/3)})}/((1 + \text{Sqrt}[3])*(b*c \\ & - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})^2}*\text{EllipticF} \\ & [\text{ArcSin}[(1 - \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a \\ & + b*x)*(c + d*x))^{(1/3)})}/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)* \\ &)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})}], -7 - 4*\text{Sqrt}[3])]/(7*d^{(11/3)*(a + \\ & b*x)^{(1/3)*(c + d*x)^{(1/3)*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(b*c - a*d)^{(2/3)*((\\ & b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})})}/((\\ & 1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d* \\ & x))^{(1/3)})^2}*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]) \end{aligned}$$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 303

```
Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
], s = Denom[Rt[b/a, 3]]}, Dist[(Sqrt[2]*s)/(Sqrt[2 + Sqrt[3]]*r), Int[1/Sq
rt[a + b*x^3], x], x] + Dist[1/r, Int[((1 - Sqrt[3])*s + r*x)/Sqrt[a + b*x^
3], x], x]] /; FreeQ[{a, b}, x] && PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
```

$\leq d \leq 4$ /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rule 1877

Int[((c_) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Simplify[((1 - Sqrt[3])*d)/c]], s = Denom[Simplify[((1 - Sqrt[3])*d)/c]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 + Sqrt[3])*s + r*x)), x] - Simp[(3^(1/4)*Sqrt[2 - Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticE[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(r^2*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b, c, d}, x] && PosQ[a] && EqQ[b*c^3 - 2*(5 - 3*Sqrt[3])*a*d^3, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{8/3}}{(c+dx)^{4/3}} dx &= -\frac{3(a+bx)^{8/3}}{d\sqrt[3]{c+dx}} + \frac{(8b) \int \frac{(a+bx)^{5/3}}{\sqrt[3]{c+dx}} dx}{d} \\
 &= -\frac{3(a+bx)^{8/3}}{d\sqrt[3]{c+dx}} + \frac{24b(a+bx)^{5/3}(c+dx)^{2/3}}{7d^2} - \frac{(40b(bc-ad)) \int \frac{(a+bx)^{2/3}}{\sqrt[3]{c+dx}} dx}{7d^2} \\
 &= -\frac{3(a+bx)^{8/3}}{d\sqrt[3]{c+dx}} - \frac{30b(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}{7d^3} + \frac{24b(a+bx)^{5/3}(c+dx)^{2/3}}{7d^2} + \frac{(20b(bc-ad)) \int \frac{(a+bx)^{-1/3}}{\sqrt[3]{c+dx}} dx}{7d^2} \\
 &= -\frac{3(a+bx)^{8/3}}{d\sqrt[3]{c+dx}} - \frac{30b(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}{7d^3} + \frac{24b(a+bx)^{5/3}(c+dx)^{2/3}}{7d^2} + \frac{(20b(bc-ad)) \int \frac{(a+bx)^{-1/3}}{\sqrt[3]{c+dx}} dx}{7d^2} \\
 &= -\frac{3(a+bx)^{8/3}}{d\sqrt[3]{c+dx}} - \frac{30b(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}{7d^3} + \frac{24b(a+bx)^{5/3}(c+dx)^{2/3}}{7d^2} + \frac{(60b(bc-ad)) \int \frac{(a+bx)^{-1/3}}{\sqrt[3]{c+dx}} dx}{7d^2} \\
 &= -\frac{3(a+bx)^{8/3}}{d\sqrt[3]{c+dx}} - \frac{30b(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}{7d^3} + \frac{24b(a+bx)^{5/3}(c+dx)^{2/3}}{7d^2} + \frac{(30\sqrt[3]{2}b^{2/3}) \int \frac{(a+bx)^{-1/3}}{\sqrt[3]{c+dx}} dx}{7d^2} \\
 &= -\frac{3(a+bx)^{8/3}}{d\sqrt[3]{c+dx}} - \frac{30b(bc-ad)(a+bx)^{2/3}(c+dx)^{2/3}}{7d^3} + \frac{24b(a+bx)^{5/3}(c+dx)^{2/3}}{7d^2} + \frac{30\sqrt[3]{2}b^{2/3}(a+bx)^{2/3}(c+dx)^{2/3}}{7d^{11/3}\sqrt[3]{a+bx}}
 \end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.05

$$\frac{3(a + bx)^{11/3} \left(\frac{b(c+dx)}{bc-ad}\right)^{4/3} {}_2F_1\left(\frac{4}{3}, \frac{11}{3}; \frac{14}{3}; \frac{d(a+bx)}{ad-bc}\right)}{11b(c + dx)^{4/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(8/3)/(c + d*x)^(4/3), x]

[Out] (3*(a + b*x)^(11/3)*((b*(c + d*x))/(b*c - a*d))^(4/3)*Hypergeometric2F1[4/3, 11/3, 14/3, (d*(a + b*x))/(-b*c) + a*d])/(11*b*(c + d*x)^(4/3))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(b^2x^2 + 2abx + a^2)(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{2}{3}}}{d^2x^2 + 2cdx + c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(8/3)/(d*x+c)^(4/3), x, algorithm="fricas")

[Out] integral((b^2*x^2 + 2*a*b*x + a^2)*(b*x + a)^(2/3)*(d*x + c)^(2/3)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{8}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(8/3)/(d*x+c)^(4/3), x, algorithm="giac")

[Out] integrate((b*x + a)^(8/3)/(d*x + c)^(4/3), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{8}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(8/3)/(d*x+c)^(4/3), x)

[Out] $\text{int}((b*x+a)^{(8/3)}/(d*x+c)^{(4/3)}, x)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{8}{3}}}{(dx+c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)^{(8/3)}/(d*x+c)^{(4/3)}, x, \text{algorithm}="maxima")$

[Out] $\text{integrate}((b*x + a)^{(8/3)}/(d*x + c)^{(4/3)}, x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a+bx)^{8/3}}{(c+dx)^{4/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^{(8/3)}/(c + d*x)^{(4/3)}, x)$

[Out] $\text{int}((a + b*x)^{(8/3)}/(c + d*x)^{(4/3)}, x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a+bx)^{\frac{8}{3}}}{(c+dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)**(8/3)/(d*x+c)**(4/3), x)$

[Out] $\text{Integral}((a + b*x)**(8/3)/(c + d*x)**(4/3), x)$

$$3.1623 \quad \int \frac{(a+bx)^{5/3}}{(c+dx)^{4/3}} dx$$

Optimal. Leaf size=1317

$$15\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{b}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{(bc-ad)}$$

$$4\sqrt[3]{2}d^{8/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)$$

[Out] $-3*(b*x+a)^{(5/3)}/d/(d*x+c)^{(1/3)}+15/4*b*(b*x+a)^{(2/3)}*(d*x+c)^{(2/3)}/d^2-15/4*b^{(1/3)}*(-a*d+b*c)*((b*x+a)*(d*x+c))^{(1/3)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}*2^{(2/3)}/d^{(8/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))-5/2*3^{(3/4)}*b^{(1/3)}*(-a*d+b*c)^{(5/3)}*((b*x+a)*(d*x+c))^{(1/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)}))/((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(((a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*2^{(1/6)}/d^{(8/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}))/((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}+15/8*3^{(1/4)}*b^{(1/3)}*(-a*d+b*c)^{(5/3)}*((b*x+a)*(d*x+c))^{(1/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticE((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)}))/((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})*(((a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*2^{(2/3)}/d^{(8/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}))/((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 2.00, antiderivative size = 1317, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 7, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.368, Rules used = {47, 50, 62, 623, 303, 218, 1877}

$$15\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{b}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{(bc-ad)}$$

$$4\sqrt[3]{2}d^{8/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/3)/(c + d*x)^(4/3), x]

[Out]
$$\begin{aligned} & (-3*(a + b*x)^{(5/3)})/(d*(c + d*x)^{(1/3)}) + (15*b*(a + b*x)^{(2/3)}*(c + d*x)^{(2/3)})/(4*d^2) - (15*b^{(1/3)}*(b*c - a*d)*((a + b*x)*(c + d*x))^{(1/3)}*\sqrt{[(b*c + a*d + 2*b*d*x)^2]*\sqrt{(a*d + b*(c + 2*d*x))^2}})/(2*2^{(1/3)}*d^{(8/3)}*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)}*(b*c + a*d + 2*b*d*x)*((1 + \sqrt{3})*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})) + (15*3^{(1/4)}*\sqrt{2 - \sqrt{3}}*b^{(1/3)}*(b*c - a*d)^{(5/3)}*((a + b*x)*(c + d*x))^{(1/3)}*\sqrt{(b*c + a*d + 2*b*d*x)^2}*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*\sqrt{((b*c - a*d)^{(4/3)} - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)})}/((1 + \sqrt{3})*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2)*\text{EllipticE}[\text{ArcSin}[\frac{(1 - \sqrt{3})*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}}{(1 + \sqrt{3})*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}}], -7 - 4*\sqrt{3}]]/(4*2^{(1/3)}*d^{(8/3)}*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)}*(b*c + a*d + 2*b*d*x)*\sqrt{((b*c - a*d)^{(2/3)}*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}))}/((1 + \sqrt{3})*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2)*\sqrt{(a*d + b*(c + 2*d*x))^2}) - (5*3^{(3/4)}*b^{(1/3)}*(b*c - a*d)^{(5/3)}*((a + b*x)*(c + d*x))^{(1/3)}*\sqrt{(b*c + a*d + 2*b*d*x)^2}*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})*\sqrt{((b*c - a*d)^{(4/3)} - 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(b*c - a*d)^{(2/3)}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((a + b*x)*(c + d*x))^{(2/3)})}/((1 + \sqrt{3})*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2)*\text{EllipticF}[\text{ArcSin}[\frac{(1 - \sqrt{3})*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}}{(1 + \sqrt{3})*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}}], -7 - 4*\sqrt{3}]]/(2^{(5/6)}*d^{(8/3)}*(a + b*x)^{(1/3)}*(c + d*x)^{(1/3)}*(b*c + a*d + 2*b*d*x)*\sqrt{((b*c - a*d)^{(2/3)}*((b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)}))}/((1 + \sqrt{3})*(b*c - a*d)^{(2/3)} + 2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((a + b*x)*(c + d*x))^{(1/3)})^2)*\sqrt{(a*d + b*(c + 2*d*x))^2}) \end{aligned}$$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[

```
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + Sqrt[3])*s + r*x)]], -7 - 4*Sqrt[3])]/(3^(1/4)*r*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] && PosQ[a]
```

Rule 303

```
Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Dist[(Sqrt[2]*s)/(Sqrt[2 + Sqrt[3]]*r), Int[1/Sqrt[a + b*x^3], x], x] + Dist[1/r, Int[((1 - Sqrt[3])*s + r*x)/Sqrt[a + b*x^3], x], x]] /; FreeQ[{a, b}, x] && PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rule 1877

```
Int[((c_) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Simplify[((1 - Sqrt[3])*d)/c]], s = Denom[Simplify[((1 - Sqrt[3])*d)/c]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 + Sqrt[3])*s + r*x)), x] - Simp[(3^(1/4)*Sqrt[2 - Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticE[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(r^2*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x] /; FreeQ[{a, b, c, d}, x] && PosQ[a] && EqQ[b*c^3 - 2*(5 - 3*Sqrt[3])*a*d^3, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/3}}{(c+dx)^{4/3}} dx &= -\frac{3(a+bx)^{5/3}}{d\sqrt[3]{c+dx}} + \frac{(5b) \int \frac{(a+bx)^{2/3}}{\sqrt[3]{c+dx}} dx}{d} \\
&= -\frac{3(a+bx)^{5/3}}{d\sqrt[3]{c+dx}} + \frac{15b(a+bx)^{2/3}(c+dx)^{2/3}}{4d^2} - \frac{(5b(bc-ad)) \int \frac{1}{\sqrt[3]{a+bx}\sqrt[3]{c+dx}} dx}{2d^2} \\
&= -\frac{3(a+bx)^{5/3}}{d\sqrt[3]{c+dx}} + \frac{15b(a+bx)^{2/3}(c+dx)^{2/3}}{4d^2} - \frac{(5b(bc-ad)\sqrt[3]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[3]{ac+(bc+ad)x+bd}}} \\
&= -\frac{3(a+bx)^{5/3}}{d\sqrt[3]{c+dx}} + \frac{15b(a+bx)^{2/3}(c+dx)^{2/3}}{4d^2} - \frac{(15b(bc-ad)\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)})}{2d^2\sqrt[3]{a+bx}} \\
&= -\frac{3(a+bx)^{5/3}}{d\sqrt[3]{c+dx}} + \frac{15b(a+bx)^{2/3}(c+dx)^{2/3}}{4d^2} - \frac{(15b^{2/3}(bc-ad)\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)})}{2\sqrt[3]{2}d^{8/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}} \\
&= -\frac{3(a+bx)^{5/3}}{d\sqrt[3]{c+dx}} + \frac{15b(a+bx)^{2/3}(c+dx)^{2/3}}{4d^2} - \frac{15\sqrt[3]{b}(bc-ad)\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)}}{2\sqrt[3]{2}d^{8/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)} \left((1 - \dots) \right)
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.06

$$\frac{3(a+bx)^{8/3} \left(\frac{b(c+dx)}{bc-ad} \right)^{4/3} {}_2F_1 \left(\frac{4}{3}, \frac{8}{3}; \frac{11}{3}; \frac{d(a+bx)}{ad-bc} \right)}{8b(c+dx)^{4/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/3)/(c + d*x)^(4/3), x]

[Out] (3*(a + b*x)^(8/3)*((b*(c + d*x))/(b*c - a*d))^(4/3)*Hypergeometric2F1[4/3, 8/3, 11/3, (d*(a + b*x))/(-b*c + a*d)])/(8*b*(c + d*x)^(4/3))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^{\frac{5}{3}}(dx + c)^{\frac{2}{3}}}{d^2x^2 + 2cdx + c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/3)/(d*x+c)^(4/3), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/3)*(d*x + c)^(2/3)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/3)/(d*x+c)^(4/3), x, algorithm="giac")

[Out] integrate((b*x + a)^(5/3)/(d*x + c)^(4/3), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/3)/(d*x+c)^(4/3), x)

[Out] int((b*x+a)^(5/3)/(d*x+c)^(4/3), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/3)/(d*x+c)^(4/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/3)/(d*x + c)^(4/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{5/3}}{(c + dx)^{4/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/3)/(c + d*x)^(4/3),x)

[Out] int((a + b*x)^(5/3)/(c + d*x)^(4/3), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{3}}}{(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/3)/(d*x+c)**(4/3),x)

[Out] Integral((a + b*x)**(5/3)/(c + d*x)**(4/3), x)

$$3.1624 \quad \int \frac{(a+bx)^{2/3}}{(c+dx)^{4/3}} dx$$

Optimal. Leaf size=1279

$$3\sqrt[4]{3} \sqrt{2 - \sqrt{3}} \sqrt[3]{b} (bc - ad)^{2/3} \sqrt[3]{(a + bx)(c + dx)} \sqrt{(bc + ad + 2bdx)^2} \left((bc - ad)^{2/3} + 2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a + bx)(c + dx)} \right)$$

$$\sqrt[3]{2} d^{5/3} \sqrt[3]{a + bx} \sqrt[3]{c + dx} (bc + ad + 2bdx)$$

[Out] $-3*(b*x+a)^{(2/3)}/d/(d*x+c)^{(1/3)}+3*2^{(2/3)}*b^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}/d^{(5/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)}))+2*2^{(1/6)}*3^{(3/4)}*b^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)}))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(((a*d+b*(2*d*x+c))^2)^{(1/2)}*((-a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/d^{(5/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}-3/2*3^{(1/4)}*b^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticE((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)}))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})), I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})*(((a*d+b*(2*d*x+c))^2)^{(1/2)}*((-a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*2^{(2/3)}/d^{(5/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 1.54, antiderivative size = 1279, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {47, 62, 623, 303, 218, 1877}

$$3\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{b}(bc-ad)^{2/3}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)$$

$$\sqrt[3]{2}d^{5/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(2/3)/(c + d*x)^(4/3), x]

[Out] (-3*(a + b*x)^(2/3))/(d*(c + d*x)^(1/3)) + (3*2^(2/3)*b^(1/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/(d^(5/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))) - (3*3^(1/4)*Sqrt[2 - Sqrt[3]]*b^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*EllipticE[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(2^(1/3)*d^(5/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3)))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2]) + (2*2^(1/6)*3^(3/4)*b^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[(b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3)]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*EllipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(d^(5/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[(b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3)))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I

```

nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
  NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) &&
  !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]

```

Rule 62

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]

```

Rule 218

```

Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)/((1 + Sqrt[3])*s + r*x)^2]*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] &
& PosQ[a]

```

Rule 303

```

Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
], s = Denom[Rt[b/a, 3]]}, Dist[(Sqrt[2]*s)/(Sqrt[2 + Sqrt[3]]*r), Int[1/Sq
rt[a + b*x^3], x], x] + Dist[1/r, Int[((1 - Sqrt[3])*s + r*x)/Sqrt[a + b*x^
3], x], x]] /; FreeQ[{a, b}, x] && PosQ[a]

```

Rule 623

```

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

```

Rule 1877

```

Int[((c_) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = N
umer[Simplify[((1 - Sqrt[3])*d)/c]], s = Denom[Simplify[((1 - Sqrt[3])*d)/c
]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 + Sqrt[3])*s + r*x)), x] - S
imp[(3^(1/4)*Sqrt[2 - Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)/
(1 + Sqrt[3])*s + r*x]^2]*EllipticE[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + S
qrt[3])*s + r*x)], -7 - 4*Sqrt[3]])/(r^2*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/
((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b, c, d}, x] && PosQ[a] && Eq

```

Q[b*c^3 - 2*(5 - 3*sqrt[3])*a*d^3, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{2/3}}{(c+dx)^{4/3}} dx &= -\frac{3(a+bx)^{2/3}}{d\sqrt[3]{c+dx}} + \frac{(2b) \int \frac{1}{\sqrt[3]{a+bx} \sqrt[3]{c+dx}} dx}{d} \\
 &= -\frac{3(a+bx)^{2/3}}{d\sqrt[3]{c+dx}} + \frac{(2b\sqrt[3]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[3]{ac+(bc+ad)x+bdx^2}} dx}{d\sqrt[3]{a+bx} \sqrt[3]{c+dx}} \\
 &= -\frac{3(a+bx)^{2/3}}{d\sqrt[3]{c+dx}} + \frac{(6b\sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}) \operatorname{Subst}\left(\int \frac{x}{\sqrt{-4abcd+(bc+ad)^2+4bdx^3}} dx\right)}{d\sqrt[3]{a+bx} \sqrt[3]{c+dx} (bc+ad+2bdx)} \\
 &= -\frac{3(a+bx)^{2/3}}{d\sqrt[3]{c+dx}} + \frac{(3\sqrt[3]{2} b^{2/3} \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}) \operatorname{Subst}\left(\int \frac{(1-\sqrt{3})(bc-ad)^{2/3}+2\sqrt{3}bdx}{\sqrt{-4abcd+(bc+ad)^2+4bdx^3}} dx\right)}{d^{4/3} \sqrt[3]{a+bx} \sqrt[3]{c+dx} (bc+ad+2bdx)} \\
 &= -\frac{3(a+bx)^{2/3}}{d\sqrt[3]{c+dx}} + \frac{3 \cdot 2^{2/3} \sqrt[3]{b} \sqrt[3]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2} \sqrt{(ad+b(c+dx))}}{d^{5/3} \sqrt[3]{a+bx} \sqrt[3]{c+dx} (bc+ad+2bdx) \left((1+\sqrt{3})(bc-ad)^{2/3} + 2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \right)}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.06

$$\frac{3(a+bx)^{5/3} \left(\frac{b(c+dx)}{bc-ad} \right)^{4/3} {}_2F_1\left(\frac{4}{3}, \frac{5}{3}; \frac{8}{3}; \frac{d(a+bx)}{ad-bc} \right)}{5b(c+dx)^{4/3}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(2/3)/(c + d*x)^(4/3), x]

[Out] (3*(a + b*x)^(5/3)*((b*(c + d*x))/(b*c - a*d))^(4/3)*Hypergeometric2F1[4/3, 5/3, 8/3, (d*(a + b*x))/(-b*c) + a*d])/(5*b*(c + d*x)^(4/3))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\operatorname{integral}\left(\frac{(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{2}{3}}}{d^2x^2+2cdx+c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/(d*x+c)^(4/3),x, algorithm="fricas")

[Out] integral((b*x + a)^(2/3)*(d*x + c)^(2/3)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{2}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/(d*x+c)^(4/3),x, algorithm="giac")

[Out] integrate((b*x + a)^(2/3)/(d*x + c)^(4/3), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{2}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(2/3)/(d*x+c)^(4/3),x)

[Out] int((b*x+a)^(2/3)/(d*x+c)^(4/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{2}{3}}}{(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2/3)/(d*x+c)^(4/3),x, algorithm="maxima")

[Out] integrate((b*x + a)^(2/3)/(d*x + c)^(4/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{\frac{2}{3}}}{(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(2/3)/(c + d*x)^(4/3), x)
```

```
[Out] int((a + b*x)^(2/3)/(c + d*x)^(4/3), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(a + bx)^{\frac{2}{3}}}{(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(2/3)/(d*x+c)**(4/3), x)
```

```
[Out] Integral((a + b*x)**(2/3)/(c + d*x)**(4/3), x)
```

$$3.1625 \quad \int \frac{1}{\sqrt[3]{a+bx} (c+dx)^{4/3}} dx$$

Optimal. Leaf size=1298

$$3\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{b}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)})}\sqrt{\frac{(bc-ad)^4}{(bc+ad+2bdx)^2}}$$

$$2\sqrt[3]{2}d^{2/3}\sqrt[3]{bc-ad}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)\sqrt{\frac{(bc+ad+2bdx)^2}{(bc-ad)^4}}$$

[Out] $3*(b*x+a)^{(2/3)/(-a*d+b*c)/(d*x+c)^{(1/3)}-3/2*b^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)}}*((2*b*d*x+a*d+b*c)^2)^{(1/2)*((a*d+b*(2*d*x+c))^2)^{(1/2)*2^{(2/3)/d^{(2/3)/(-a*d+b*c)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^{-2^{(1/6)*3^{(3/4)*b^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)*EllipticF((2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1-3^{(1/2))})/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})}, I*3^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*(((a*d+b*c)^{(4/3)-2^{(2/3)*b^{(1/3)*d^{(1/3)*(-a*d+b*c)^{(2/3)*((b*x+a)*(d*x+c))^{(1/3)+2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^{-2^{(1/2)/d^{(2/3)/(-a*d+b*c)^{(1/3)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^{-2^{(1/2)+3/4*3^{(1/4)*b^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)*EllipticE((2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1-3^{(1/2))})/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})}, I*3^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*(1/2*6^{(1/2)-1/2*2^{(1/2)})*(((a*d+b*c)^{(4/3)-2^{(2/3)*b^{(1/3)*d^{(1/3)*(-a*d+b*c)^{(2/3)*((b*x+a)*(d*x+c))^{(1/3)+2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^{-2^{(1/2)*2^{(2/3)/d^{(2/3)/(-a*d+b*c)^{(1/3)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^{-2^{(1/2)}}}}$

Rubi [A] time = 1.52, antiderivative size = 1298, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {51, 62, 623, 303, 218, 1877}

$$3\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{b}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)\sqrt{\frac{(bc-ad)}{bc+ad+2bdx}}$$

$$2\sqrt[3]{2}d^{2/3}\sqrt[3]{bc-ad}\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)\sqrt{\frac{(bc-ad)}{bc+ad+2bdx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/3)*(c + d*x)^(4/3)),x]

[Out] (3*(a + b*x)^(2/3))/((b*c - a*d)*(c + d*x)^(1/3)) - (3*b^(1/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/((2^(1/3)*d^(2/3)*(b*c - a*d)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))) + (3*3^(1/4)*Sqrt[2 - Sqrt[3]]*b^(1/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*EllipticE[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(2*2^(1/3)*d^(2/3)*(b*c - a*d)^(1/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3)))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2]) - (2^(1/6)*3^(3/4)*b^(1/3)*((a + b*x)*(c + d*x))^(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))*Sqrt[((b*c - a*d)^(4/3) - 2^(2/3)*b^(1/3)*d^(1/3)*(b*c - a*d)^(2/3)*((a + b*x)*(c + d*x))^(1/3) + 2*2^(1/3)*b^(2/3)*d^(2/3)*((a + b*x)*(c + d*x))^(2/3))]/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*EllipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))], -7 - 4*Sqrt[3]])/(d^(2/3)*(b*c - a*d)^(1/3)*(a + b*x)^(1/3)*(c + d*x)^(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[((b*c - a*d)^(2/3)*((b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3)))/((1 + Sqrt[3])*(b*c - a*d)^(2/3) + 2^(2/3)*b^(1/3)*d^(1/3)*((a + b*x)*(c + d*x))^(1/3))^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[

$((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] - \text{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[m, -1] \&\& !(\text{LtQ}[n, -1] \&\& (\text{EqQ}[a, 0] \mid\mid (\text{NeQ}[c, 0] \&\& \text{LtQ}[m - n, 0] \&\& \text{IntegerQ}[n]))) \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 62

$\text{Int}[(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, \text{Int}[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[3, \text{Denominator}[m], 4]$

Rule 218

$\text{Int}[1/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(2*\text{Sqrt}[2 + \text{Sqrt}[3]]*(s + r*x)*\text{Sqrt}[(s^2 - r*s*x + r^2*x^2)/((1 + \text{Sqrt}[3])*s + r*x)^2]*\text{EllipticF}[\text{ArcSin}[(1 - \text{Sqrt}[3])*s + r*x]/((1 + \text{Sqrt}[3])*s + r*x)], -7 - 4*\text{Sqrt}[3]]/(3^{1/4}*r*\text{Sqrt}[a + b*x^3]*\text{Sqrt}[(s*(s + r*x))/((1 + \text{Sqrt}[3])*s + r*x)^2]), x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a]$

Rule 303

$\text{Int}[x/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[2]*s)/(\text{Sqrt}[2 + \text{Sqrt}[3]]*r), \text{Int}[1/\text{Sqrt}[a + b*x^3], x], x] + \text{Dist}[1/r, \text{Int}[(1 - \text{Sqrt}[3])*s + r*x]/\text{Sqrt}[a + b*x^3], x], x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a]$

Rule 623

$\text{Int}[(a + b*x + c*x^2)^p, x_Symbol] := \text{With}\{d = \text{Denominator}[p]\}, \text{Dist}[(d*\text{Sqrt}[(b + 2*c*x)^2])/(b + 2*c*x), \text{Subst}[\text{Int}[x^{d*(p + 1) - 1}/\text{Sqrt}[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^{(1/d)}, x] /; 3 \leq d \leq 4] /; \text{FreeQ}\{a, b, c\}, x] \&\& \text{NeQ}[b^2 - 4*a*c, 0] \&\& \text{RationalQ}[p]$

Rule 1877

$\text{Int}[(c + d*x)/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}\{r = \text{Numer}[\text{Simplify}[(1 - \text{Sqrt}[3])*d/c]], s = \text{Denom}[\text{Simplify}[(1 - \text{Sqrt}[3])*d/c]]\}, \text{Simp}[(2*d*s^3*\text{Sqrt}[a + b*x^3])/(a*r^2*((1 + \text{Sqrt}[3])*s + r*x)), x] - \text{Simp}[(3^{1/4}*\text{Sqrt}[2 - \text{Sqrt}[3]]*d*s*(s + r*x)*\text{Sqrt}[(s^2 - r*s*x + r^2*x^2)/((1 + \text{Sqrt}[3])*s + r*x)^2]*\text{EllipticE}[\text{ArcSin}[(1 - \text{Sqrt}[3])*s + r*x]/((1 + \text{Sqrt}[3])*s + r*x)], -7 - 4*\text{Sqrt}[3]]/(r^2*\text{Sqrt}[a + b*x^3]*\text{Sqrt}[(s*(s + r*x))/((1 + \text{Sqrt}[3])*s + r*x)^2]), x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{PosQ}[a] \&\& \text{Eq}$

Q[b*c^3 - 2*(5 - 3*sqrt[3])*a*d^3, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{\sqrt[3]{a+bx}(c+dx)^{4/3}} dx &= \frac{3(a+bx)^{2/3}}{(bc-ad)\sqrt[3]{c+dx}} - \frac{b \int \frac{1}{\sqrt[3]{a+bx}\sqrt[3]{c+dx}} dx}{bc-ad} \\
 &= \frac{3(a+bx)^{2/3}}{(bc-ad)\sqrt[3]{c+dx}} - \frac{(b\sqrt[3]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[3]{ac+(bc+ad)x+bdx^2}} dx}{(bc-ad)\sqrt[3]{a+bx}\sqrt[3]{c+dx}} \\
 &= \frac{3(a+bx)^{2/3}}{(bc-ad)\sqrt[3]{c+dx}} - \frac{(3b\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}) \operatorname{Subst}\left(\int \frac{1}{\sqrt{-4abcd+(bc+ad)^2+4bdx^2}} dx\right)}{(bc-ad)\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)} \\
 &= \frac{3(a+bx)^{2/3}}{(bc-ad)\sqrt[3]{c+dx}} - \frac{(3b^{2/3}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}) \operatorname{Subst}\left(\int \frac{(1-\sqrt{3})}{\sqrt{-4abcd+(bc+ad)^2+4bdx^2}} dx\right)}{2^{2/3}\sqrt[3]{d}(bc-ad)\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)} \\
 &= \frac{3(a+bx)^{2/3}}{(bc-ad)\sqrt[3]{c+dx}} - \frac{3\sqrt[3]{b}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}}{\sqrt[3]{2}d^{2/3}(bc-ad)\sqrt[3]{a+bx}\sqrt[3]{c+dx}(bc+ad+2bdx)((1+\sqrt{3}))}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.06

$$\frac{3(a+bx)^{2/3} \left(\frac{b(c+dx)}{bc-ad}\right)^{4/3} {}_2F_1\left(\frac{2}{3}, \frac{4}{3}; \frac{5}{3}; \frac{d(a+bx)}{ad-bc}\right)}{2b(c+dx)^{4/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/3)*(c + d*x)^(4/3)), x]

[Out] (3*(a + b*x)^(2/3)*((b*(c + d*x))/(b*c - a*d))^(4/3)*Hypergeometric2F1[2/3, 4/3, 5/3, (d*(a + b*x))/(-b*c) + a*d])/(2*b*(c + d*x)^(4/3))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\operatorname{integral}\left(\frac{(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{2}{3}}}{bd^2x^3+ac^2+(2bcd+ad^2)x^2+(bc^2+2acd)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3)/(d*x+c)^(4/3),x, algorithm="fricas")

[Out] integral((b*x + a)^(2/3)*(d*x + c)^(2/3)/(b*d^2*x^3 + a*c^2 + (2*b*c*d + a*d^2)*x^2 + (b*c^2 + 2*a*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{3}}(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3)/(d*x+c)^(4/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/3)*(d*x + c)^(4/3)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{3}}(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/3)/(d*x+c)^(4/3),x)

[Out] int(1/(b*x+a)^(1/3)/(d*x+c)^(4/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{3}}(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/3)/(d*x+c)^(4/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/3)*(d*x + c)^(4/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{\frac{1}{3}}(c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(1/3)*(c + d*x)^(4/3)), x)`

[Out] `int(1/((a + b*x)^(1/3)*(c + d*x)^(4/3)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[3]{a + bx} (c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/3)/(d*x+c)**(4/3), x)`

[Out] `Integral(1/((a + b*x)**(1/3)*(c + d*x)**(4/3)), x)`

$$3.1626 \quad \int \frac{1}{(a+bx)^{4/3}(c+dx)^{4/3}} dx$$

Optimal. Leaf size=1327

$$\frac{6(a+bx)^{2/3}d}{(bc-ad)^2\sqrt[3]{c+dx}} \frac{3\sqrt[3]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{b}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)})}{\sqrt[3]{2}(bc-ad)^{4/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}}$$

[Out]
$$\begin{aligned} & -3/(-a*d+b*c)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)}-6*d*(b*x+a)^{(2/3)/(-a*d+b*c)^{(2/3)/(d} \\ & *x+c)^{(1/3)+3*2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)*((2*b*d*x+a*d} \\ & +b*c)^2)^{(1/2)*((a*d+b*(2*d*x+c))^2)^{(1/2)/(-a*d+b*c)^{(2/3)/(b*x+a)^{(1/3)/(d*x+} \\ & c)^{(1/3)/(2*b*d*x+a*d+b*c)/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)} \\ & +(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})+2*2^{(1/6)*3^{(3/4)*b^{(1/3)*d^{(1/3)*((b*x+a)*(} \\ & d*x+c)^{(1/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(} \\ & 1/3))*EllipticF((2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)} \\ & ^{(2/3)*(1-3^{(1/2))})/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+} \\ & b*c)^{(2/3)*(1+3^{(1/2))}), I*3^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*(((a*d+} \\ & b*c)^{(4/3)-2^{(2/3)*b^{(1/3)*d^{(1/3)*(-a*d+b*c)^{(2/3)*((b*x+a)*(d*x+c))^{(1/3)} \\ & +2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((b*x+a)*(d*x+c))^{(2/3)))/(2^{(2/3)*b^{(1/3)*d^{(1/3)} \\ &)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^2)^{(1/2)/(-a*d+b*c} \\ & ^{(4/3)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(} \\ & 1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*} \\ & (d*x+c))^{(1/3)))/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)} \\ & ^{(2/3)*(1+3^{(1/2))})^2)^{(1/2)-3/2*3^{(1/4)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(} \\ & 1/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3))*El} \\ & lipticE((2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(} \\ & 1-3^{(1/2))})/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/} \\ & 3)*(1+3^{(1/2))}), I*3^{(1/2)+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*(1/2*6^{(1/2)-1/2} \\ & *2^{(1/2)*(((-a*d+b*c)^{(4/3)-2^{(2/3)*b^{(1/3)*d^{(1/3)*(-a*d+b*c)^{(2/3)*((b*x} \\ & +a)*(d*x+c))^{(1/3)+2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((b*x+a)*(d*x+c))^{(2/3)))/(2^{(2} \\ & /3)*b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^2} \\ &)^2)^{(1/2)*2^{(2/3)/(-a*d+b*c)^{(4/3)/(b*x+a)^{(1/3)/(d*x+c)^{(1/3)/(2*b*d*x+a*d+b} \\ & *c)/((a*d+b*(2*d*x+c))^2)^{(1/2)/((-a*d+b*c)^{(2/3)*((-a*d+b*c)^{(2/3)+2^{(2/3)} \\ & *b^{(1/3)*d^{(1/3)*((b*x+a)*(d*x+c))^{(1/3)))/(2^{(2/3)*b^{(1/3)*d^{(1/3)*((b*x+a)} \\ & *(d*x+c))^{(1/3)+(-a*d+b*c)^{(2/3)*(1+3^{(1/2))})^2)^{(1/2)} \end{aligned}$$

Rubi [A] time = 1.96, antiderivative size = 1327, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {51, 62, 623, 303, 218, 1877}

$$\frac{6(a+bx)^{2/3}d}{(bc-ad)^2\sqrt[3]{c+dx}} \cdot \frac{3\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{b}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)}{\sqrt[3]{2}(bc-ad)^{4/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(4/3)*(c + d*x)^(4/3)), x]

[Out]
$$\begin{aligned} & -3/((b*c - a*d)*(a + b*x)^{(1/3)*(c + d*x)^{(1/3)}) - (6*d*(a + b*x)^{(2/3))}/((\\ & b*c - a*d)^{2*(c + d*x)^{(1/3)}) + (3*2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + \\ & d*x))^{(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^{(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]} \\ & b*c - a*d)^{2*(a + b*x)^{(1/3)*(c + d*x)^{(1/3)*(b*c + a*d + 2*b*d*x)*((1 + Sqrt[3])*(b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3)) - (3*3^{(1/4)*Sqrt[2 - Sqrt[3]]*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]}*((b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3)*((a + b*x)*(c + d*x))^{(1/3)*Sqrt[((b*c - a*d)^{(4/3) - 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]}*((b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3)*((a + b*x)*(c + d*x))^{(2/3))}/((1 + Sqrt[3])*(b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3)*((1 - Sqrt[3])*(b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3))/((1 + Sqrt[3])*(b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3)), -7 - 4*Sqrt[3]))/(2^{(1/3)*(b*c - a*d)^{(4/3)*(a + b*x)^{(1/3)*(c + d*x)^{(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[(b*c - a*d)^{(2/3)*((b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3)))/((1 + Sqrt[3])*(b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3))^{(1/3)})^2]*Sqrt[(a*d + b*(c + 2*d*x))^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]}*((b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3)*((a + b*x)*(c + d*x))^{(1/3)*Sqrt[(b*c - a*d)^{(4/3) - 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]}*((b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3)*((a + b*x)*(c + d*x))^{(2/3))}/((1 + Sqrt[3])*(b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3))^{(1/3)})^2]*EllipticF[ArcSin[((1 - Sqrt[3])*(b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3)*((a + b*x)*(c + d*x))^{(1/3))}/((1 + Sqrt[3])*(b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3))], -7 - 4*Sqrt[3]))/(b*c - a*d)^{(4/3)*(a + b*x)^{(1/3)*(c + d*x)^{(1/3)*(b*c + a*d + 2*b*d*x)*Sqrt[(b*c - a*d)^{(2/3)*((b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3)))/((1 + Sqrt[3])*(b*c - a*d)^{(2/3) + 2^{(2/3)*b^{(1/3)*d^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)})} \\ & /3))^{(1/3)})^2]*Sqrt[(a*d + b*(c + 2*d*x))^{(1/3)*((a + b*x)*(c + d*x))^{(1/3)*Sqrt[(b*c + a*d + 2*b*d*x)^2]} \\ & /3)) \end{aligned}$$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[

$((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] - \text{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x] /; \text{FreeQ}\{a, b, c, d, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[m, -1] \&\& !(\text{LtQ}[n, -1] \&\& (\text{EqQ}[a, 0] \mid\mid (\text{NeQ}[c, 0] \&\& \text{LtQ}[m - n, 0] \&\& \text{IntegerQ}[n]))) \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 62

$\text{Int}[(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, \text{Int}[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[3, \text{Denominator}[m], 4]$

Rule 218

$\text{Int}[1/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(2*\text{Sqrt}[2 + \text{Sqrt}[3]]*(s + r*x)*\text{Sqrt}[(s^2 - r*s*x + r^2*x^2)/((1 + \text{Sqrt}[3])*s + r*x)^2]*\text{EllipticF}[\text{ArcSin}[(1 - \text{Sqrt}[3])*s + r*x]/((1 + \text{Sqrt}[3])*s + r*x)], -7 - 4*\text{Sqrt}[3]]/(3^{1/4}*r*\text{Sqrt}[a + b*x^3]*\text{Sqrt}[(s*(s + r*x))/((1 + \text{Sqrt}[3])*s + r*x)^2]), x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a]$

Rule 303

$\text{Int}[x/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[2]*s)/(\text{Sqrt}[2 + \text{Sqrt}[3]]*r), \text{Int}[1/\text{Sqrt}[a + b*x^3], x], x] + \text{Dist}[1/r, \text{Int}[(1 - \text{Sqrt}[3])*s + r*x]/\text{Sqrt}[a + b*x^3], x], x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a]$

Rule 623

$\text{Int}[(a + b*x + c*x^2)^p, x_Symbol] := \text{With}\{d = \text{Denominator}[p]\}, \text{Dist}[(d*\text{Sqrt}[(b + 2*c*x)^2])/(b + 2*c*x), \text{Subst}[\text{Int}[x^{d*(p + 1) - 1}/\text{Sqrt}[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^{(1/d)}, x] /; 3 \leq d \leq 4] /; \text{FreeQ}\{a, b, c\}, x] \&\& \text{NeQ}[b^2 - 4*a*c, 0] \&\& \text{RationalQ}[p]$

Rule 1877

$\text{Int}[(c + d*x)/\text{Sqrt}[(a + b*x)^3], x_Symbol] := \text{With}\{r = \text{Numer}[\text{Simplify}[(1 - \text{Sqrt}[3])*d/c]], s = \text{Denom}[\text{Simplify}[(1 - \text{Sqrt}[3])*d/c]]\}, \text{Simp}[(2*d*s^3*\text{Sqrt}[a + b*x^3])/(a*r^2*((1 + \text{Sqrt}[3])*s + r*x)), x] - \text{Simp}[(3^{1/4}*\text{Sqrt}[2 - \text{Sqrt}[3]]*d*s*(s + r*x)*\text{Sqrt}[(s^2 - r*s*x + r^2*x^2)/((1 + \text{Sqrt}[3])*s + r*x)^2]*\text{EllipticE}[\text{ArcSin}[(1 - \text{Sqrt}[3])*s + r*x]/((1 + \text{Sqrt}[3])*s + r*x)], -7 - 4*\text{Sqrt}[3]]/(r^2*\text{Sqrt}[a + b*x^3]*\text{Sqrt}[(s*(s + r*x))/((1 + \text{Sqrt}[3])*s + r*x)^2]), x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{PosQ}[a] \&\& \text{Eq}$

Q[$b*c^3 - 2*(5 - 3*\text{Sqrt}[3])*a*d^3, 0]$

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{4/3}(c+dx)^{4/3}} dx &= -\frac{3}{(bc-ad)\sqrt[3]{a+bx}\sqrt[3]{c+dx}} - \frac{(2d) \int \frac{1}{\sqrt[3]{a+bx}(c+dx)^{4/3}} dx}{bc-ad} \\
 &= -\frac{3}{(bc-ad)\sqrt[3]{a+bx}\sqrt[3]{c+dx}} - \frac{6d(a+bx)^{2/3}}{(bc-ad)^2\sqrt[3]{c+dx}} + \frac{(2bd) \int \frac{1}{\sqrt[3]{a+bx}\sqrt[3]{c+dx}} dx}{(bc-ad)^2} \\
 &= -\frac{3}{(bc-ad)\sqrt[3]{a+bx}\sqrt[3]{c+dx}} - \frac{6d(a+bx)^{2/3}}{(bc-ad)^2\sqrt[3]{c+dx}} + \frac{(2bd\sqrt[3]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[3]{a+bx}\sqrt[3]{c+dx}} dx}{(bc-ad)^2\sqrt[3]{a+bx}} \\
 &= -\frac{3}{(bc-ad)\sqrt[3]{a+bx}\sqrt[3]{c+dx}} - \frac{6d(a+bx)^{2/3}}{(bc-ad)^2\sqrt[3]{c+dx}} + \frac{(6bd\sqrt[3]{(a+bx)(c+dx)})\sqrt{(bc-ad)}}{(bc-ad)^2\sqrt[3]{a+bx}} \\
 &= -\frac{3}{(bc-ad)\sqrt[3]{a+bx}\sqrt[3]{c+dx}} - \frac{6d(a+bx)^{2/3}}{(bc-ad)^2\sqrt[3]{c+dx}} + \frac{(3\sqrt[3]{2}b^{2/3}d^{2/3}\sqrt[3]{(a+bx)(c+dx)})\sqrt{(bc-ad)}}{(bc-ad)^2\sqrt[3]{a+bx}} \\
 &= -\frac{3}{(bc-ad)\sqrt[3]{a+bx}\sqrt[3]{c+dx}} - \frac{6d(a+bx)^{2/3}}{(bc-ad)^2\sqrt[3]{c+dx}} + \frac{3 \cdot 2^{2/3} \sqrt[3]{b} \sqrt[3]{d} \sqrt[3]{(a+bx)(c+dx)}}{(bc-ad)^2\sqrt[3]{a+bx}\sqrt[3]{c+dx}}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.05

$$\frac{3 \left(\frac{b(c+dx)}{bc-ad} \right)^{4/3} {}_2F_1 \left(-\frac{1}{3}, \frac{4}{3}; \frac{2}{3}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt[3]{a+bx}(c+dx)^{4/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(4/3)*(c + d*x)^(4/3)),x]

[Out] (-3*((b*(c + d*x))/(b*c - a*d))^(4/3)*Hypergeometric2F1[-1/3, 4/3, 2/3, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(a + b*x)^(1/3)*(c + d*x)^(4/3))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^{\frac{2}{3}}(dx + c)^{\frac{2}{3}}}{b^2d^2x^4 + a^2c^2 + 2(b^2cd + abd^2)x^3 + (b^2c^2 + 4abcd + a^2d^2)x^2 + 2(abc^2 + a^2cd)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(4/3)/(d*x+c)^(4/3),x, algorithm="fricas")

[Out] integral((b*x + a)^(2/3)*(d*x + c)^(2/3)/(b^2*d^2*x^4 + a^2*c^2 + 2*(b^2*c*d + a*b*d^2)*x^3 + (b^2*c^2 + 4*a*b*c*d + a^2*d^2)*x^2 + 2*(a*b*c^2 + a^2*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{4}{3}}(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(4/3)/(d*x+c)^(4/3),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(4/3)*(d*x + c)^(4/3)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{4}{3}}(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(4/3)/(d*x+c)^(4/3),x)

[Out] int(1/(b*x+a)^(4/3)/(d*x+c)^(4/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{4}{3}}(dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(4/3)/(d*x+c)^(4/3),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(4/3)*(d*x + c)^(4/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{4/3} (c + dx)^{4/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(4/3)*(c + d*x)^(4/3)), x)

[Out] int(1/((a + b*x)^(4/3)*(c + d*x)^(4/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{4}{3}} (c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(4/3)/(d*x+c)**(4/3), x)

[Out] Integral(1/((a + b*x)**(4/3)*(c + d*x)**(4/3)), x)

$$3.1627 \quad \int \frac{1}{(a+bx)^{7/3}(c+dx)^{4/3}} dx$$

Optimal. Leaf size=1370

$$\frac{15(a+bx)^{2/3}d^2}{2(bc-ad)^3\sqrt[3]{c+dx}} + \frac{15\sqrt[4]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{b}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)}{4\sqrt[3]{2}(bc-ad)^{7/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}}$$

[Out]
$$\begin{aligned} & -3/4/(-a*d+b*c)/(b*x+a)^{(4/3)}/(d*x+c)^{(1/3)}+15/4*d/(-a*d+b*c)^2/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+15/2*d^2*(b*x+a)^{(2/3)}/(-a*d+b*c)^3/(d*x+c)^{(1/3)}-15/4*b^{(1/3)}*d^{(4/3)}*((b*x+a)*(d*x+c))^{(1/3)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}*2^{(2/3)}/(-a*d+b*c)^3/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))-5/2*3^{(3/4)}*b^{(1/3)}*d^{(4/3)}*((b*x+a)*(d*x+c))^{(1/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticF((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)})))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})) , I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(((-a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*2^{(1/6)}/(-a*d+b*c)^{(7/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}+15/8*3^{(1/4)}*b^{(1/3)}*d^{(4/3)}*((b*x+a)*(d*x+c))^{(1/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})*EllipticE((2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1-3^{(1/2)})))/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})) , I*3^{(1/2)}+2*I)*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*(1/2*6^{(1/2)}-1/2*2^{(1/2)})*(((-a*d+b*c)^{(4/3)}-2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*(-a*d+b*c)^{(2/3)}*((b*x+a)*(d*x+c))^{(1/3)}+2*2^{(1/3)}*b^{(2/3)}*d^{(2/3)}*((b*x+a)*(d*x+c))^{(2/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*2^{(2/3)}/(-a*d+b*c)^{(7/3)}/(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}/((-a*d+b*c)^{(2/3)}*((-a*d+b*c)^{(2/3)}+2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)})/(2^{(2/3)}*b^{(1/3)}*d^{(1/3)}*((b*x+a)*(d*x+c))^{(1/3)}+(-a*d+b*c)^{(2/3)}*(1+3^{(1/2)})))^2)^{(1/2)} \end{aligned}$$

Rubi [A] time = 2.42, antiderivative size = 1370, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {51, 62, 623, 303, 218, 1877}

$$\frac{15(a+bx)^{2/3}d^2}{2(bc-ad)^3\sqrt[3]{c+dx}} + \frac{15^4\sqrt[3]{3}\sqrt{2-\sqrt{3}}\sqrt[3]{b}\sqrt[3]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\left((bc-ad)^{2/3}+2^{2/3}\sqrt[3]{b}\sqrt[3]{d}\sqrt[3]{(a+bx)(c+dx)}\right)}{4\sqrt[3]{2}(bc-ad)^{7/3}\sqrt[3]{a+bx}\sqrt[3]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/3)*(c + d*x)^(4/3)), x]

[Out]
$$\begin{aligned} & -3/(4*(b*c - a*d)*(a + b*x)^{(4/3)*(c + d*x)^{(1/3)}) + (15*d)/(4*(b*c - a*d)^2*(a + b*x)^{(1/3)*(c + d*x)^{(1/3)}) + (15*d^2*(a + b*x)^{(2/3)})/(2*(b*c - a*d)^3*(c + d*x)^{(1/3)}) - (15*b^{(1/3)*d^{(4/3)}}*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]}/(2*2^{(1/3)*(b*c - a*d)^3*(a + b*x)^{(1/3)*(c + d*x)^{(1/3)*(b*c + a*d + 2*b*d*x)*((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})} + (15*3^{(1/4)*\text{Sqrt}[2 - \text{Sqrt}[3]]*b^{(1/3)*d^{(4/3)}}*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c - a*d)^{(4/3)} - 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c - a*d)^{(2/3)*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((a + b*x)*(c + d*x))^{(2/3)}}}/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})^2]*\text{EllipticE}[\text{ArcSin}[(1 - \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})]/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})], -7 - 4*\text{Sqrt}[3]])/(4*2^{(1/3)*(b*c - a*d)^{(7/3)*(a + b*x)^{(1/3)*(c + d*x)^{(1/3)*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(b*c - a*d)^{(2/3)*((b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})}]/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})^2]*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]) - (5*3^{(3/4)*b^{(1/3)*d^{(4/3)}}*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*((b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)*\text{Sqrt}[(b*c - a*d)^{(4/3)} - 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)} + 2*2^{(1/3)*b^{(2/3)*d^{(2/3)*((a + b*x)*(c + d*x))^{(2/3)}}}/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})^2]*\text{EllipticF}[\text{ArcSin}[(1 - \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})]/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})], -7 - 4*\text{Sqrt}[3]])/(2^{(5/6)*(b*c - a*d)^{(7/3)*(a + b*x)^{(1/3)*(c + d*x)^{(1/3)*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(b*c - a*d)^{(2/3)*((b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})}]/((1 + \text{Sqrt}[3])*(b*c - a*d)^{(2/3)} + 2^{(2/3)*b^{(1/3)*d^{(1/3)}}*((a + b*x)*(c + d*x))^{(1/3)})^2]*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2] \end{aligned}$$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 218

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(2*Sqrt[2 + Sqrt[3]]*(s + r*x)*Sqrt[(s^2 - r*s
*x + r^2*x^2)]/((1 + Sqrt[3])*s + r*x)^2*EllipticF[ArcSin[((1 - Sqrt[3])*s
+ r*x)/((1 + Sqrt[3])*s + r*x)], -7 - 4*Sqrt[3]]]/(3^(1/4)*r*Sqrt[a + b*x^3
]*Sqrt[(s*(s + r*x))/((1 + Sqrt[3])*s + r*x)^2]), x]] /; FreeQ[{a, b}, x] &
& PosQ[a]
```

Rule 303

```
Int[(x_)/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = Numer[Rt[b/a, 3]
], s = Denom[Rt[b/a, 3]]}, Dist[(Sqrt[2]*s)/(Sqrt[2 + Sqrt[3]]*r), Int[1/Sq
rt[a + b*x^3], x], x] + Dist[1/r, Int[((1 - Sqrt[3])*s + r*x)/Sqrt[a + b*x^
3], x], x]] /; FreeQ[{a, b}, x] && PosQ[a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rule 1877

```
Int[((c_.) + (d_.)*(x_))/Sqrt[(a_) + (b_.)*(x_)^3], x_Symbol] := With[{r = N
umer[Simplify[((1 - Sqrt[3])*d)/c]], s = Denom[Simplify[((1 - Sqrt[3])*d)/c
]]}, Simp[(2*d*s^3*Sqrt[a + b*x^3])/(a*r^2*((1 + Sqrt[3])*s + r*x)), x] - S
imp[(3^(1/4)*Sqrt[2 - Sqrt[3]]*d*s*(s + r*x)*Sqrt[(s^2 - r*s*x + r^2*x^2)]/
((1 + Sqrt[3])*s + r*x)^2*EllipticE[ArcSin[((1 - Sqrt[3])*s + r*x)/((1 + S
qrt[3])*s + r*x)], -7 - 4*Sqrt[3]]]/(r^2*Sqrt[a + b*x^3]*Sqrt[(s*(s + r*x))/
```

((1 + Sqrt[3])*s + r*x)^2), x]] /; FreeQ[{a, b, c, d}, x] && PosQ[a] && EqQ[b*c^3 - 2*(5 - 3*Sqrt[3])*a*d^3, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{7/3}(c+dx)^{4/3}} dx &= -\frac{3}{4(bc-ad)(a+bx)^{4/3}\sqrt[3]{c+dx}} - \frac{(5d) \int \frac{1}{(a+bx)^{4/3}(c+dx)^{4/3}} dx}{4(bc-ad)} \\
 &= -\frac{3}{4(bc-ad)(a+bx)^{4/3}\sqrt[3]{c+dx}} + \frac{15d}{4(bc-ad)^2\sqrt[3]{a+bx}\sqrt[3]{c+dx}} + \frac{(5d^2) \int \frac{1}{\sqrt[3]{a+bx}(c+dx)^{4/3}} dx}{2(bc-ad)} \\
 &= -\frac{3}{4(bc-ad)(a+bx)^{4/3}\sqrt[3]{c+dx}} + \frac{15d}{4(bc-ad)^2\sqrt[3]{a+bx}\sqrt[3]{c+dx}} + \frac{15d^2(a+bx)}{2(bc-ad)^3\sqrt[3]{c}} \\
 &= -\frac{3}{4(bc-ad)(a+bx)^{4/3}\sqrt[3]{c+dx}} + \frac{15d}{4(bc-ad)^2\sqrt[3]{a+bx}\sqrt[3]{c+dx}} + \frac{15d^2(a+bx)}{2(bc-ad)^3\sqrt[3]{c}} \\
 &= -\frac{3}{4(bc-ad)(a+bx)^{4/3}\sqrt[3]{c+dx}} + \frac{15d}{4(bc-ad)^2\sqrt[3]{a+bx}\sqrt[3]{c+dx}} + \frac{15d^2(a+bx)}{2(bc-ad)^3\sqrt[3]{c}} \\
 &= -\frac{3}{4(bc-ad)(a+bx)^{4/3}\sqrt[3]{c+dx}} + \frac{15d}{4(bc-ad)^2\sqrt[3]{a+bx}\sqrt[3]{c+dx}} + \frac{15d^2(a+bx)}{2(bc-ad)^3\sqrt[3]{c}} \\
 &= -\frac{3}{4(bc-ad)(a+bx)^{4/3}\sqrt[3]{c+dx}} + \frac{15d}{4(bc-ad)^2\sqrt[3]{a+bx}\sqrt[3]{c+dx}} + \frac{15d^2(a+bx)}{2(bc-ad)^3\sqrt[3]{c}} \\
 &= -\frac{3}{4(bc-ad)(a+bx)^{4/3}\sqrt[3]{c+dx}} + \frac{15d}{4(bc-ad)^2\sqrt[3]{a+bx}\sqrt[3]{c+dx}} + \frac{15d^2(a+bx)}{2(bc-ad)^3\sqrt[3]{c}}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.05

$$\frac{3 \left(\frac{b(c+dx)}{bc-ad} \right)^{4/3} {}_2F_1 \left(-\frac{4}{3}, \frac{4}{3}; -\frac{1}{3}; \frac{d(a+bx)}{ad-bc} \right)}{4b(a+bx)^{4/3}(c+dx)^{4/3}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/3)*(c + d*x)^(4/3)),x]

[Out] $(-3*((b*(c + d*x))/(b*c - a*d))^{4/3} * \text{Hypergeometric2F1}[-4/3, 4/3, -1/3, (d*(a + b*x))/(-(b*c) + a*d)]) / (4*b*(a + b*x)^{4/3} * (c + d*x)^{4/3})$

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^{\frac{2}{3}} (dx + c)^{\frac{2}{3}}}{b^3 d^2 x^5 + a^3 c^2 + (2 b^3 cd + 3 ab^2 d^2) x^4 + (b^3 c^2 + 6 ab^2 cd + 3 a^2 b d^2) x^3 + (3 ab^2 c^2 + 6 a^2 bcd + a^3 d^2) x^2 + \dots} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(7/3)/(d*x+c)^(4/3),x, algorithm="fricas")`

[Out] `integral((b*x + a)^(2/3)*(d*x + c)^(2/3)/(b^3*d^2*x^5 + a^3*c^2 + (2*b^3*c*d + 3*a*b^2*d^2)*x^4 + (b^3*c^2 + 6*a*b^2*c*d + 3*a^2*b*d^2)*x^3 + (3*a*b^2*c^2 + 6*a^2*b*c*d + a^3*d^2)*x^2 + (3*a^2*b*c^2 + 2*a^3*c*d)*x), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{3}} (dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(7/3)/(d*x+c)^(4/3),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(7/3)*(d*x + c)^(4/3)), x)`

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{3}} (dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(7/3)/(d*x+c)^(4/3),x)`

[Out] `int(1/(b*x+a)^(7/3)/(d*x+c)^(4/3),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{3}} (dx + c)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(7/3)/(d*x+c)^(4/3),x, algorithm="maxima")`

[Out] integrate(1/((b*x + a)^(7/3)*(d*x + c)^(4/3)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{7/3} (c + dx)^{4/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/3)*(c + d*x)^(4/3)), x)

[Out] int(1/((a + b*x)^(7/3)*(c + d*x)^(4/3)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{7}{3}} (c + dx)^{\frac{4}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/3)/(d*x+c)**(4/3), x)

[Out] Integral(1/((a + b*x)**(7/3)*(c + d*x)**(4/3)), x)

$$3.1628 \quad \int \frac{\sqrt[3]{-1+x}}{\sqrt[3]{1+x}} dx$$

Optimal. Leaf size=77

$$\sqrt[3]{x-1}(x+1)^{2/3} + \frac{1}{3} \log(x-1) + \log\left(\frac{\sqrt[3]{x+1}}{\sqrt[3]{x-1}} - 1\right) + \frac{2 \tan^{-1}\left(\frac{2\sqrt[3]{x+1}}{\sqrt{3}\sqrt[3]{x-1}} + \frac{1}{\sqrt{3}}\right)}{\sqrt{3}}$$

[Out] $(-1+x)^{(1/3)}*(1+x)^{(2/3)}+1/3*\ln(-1+x)+\ln(-1+(1+x)^{(1/3)})/(-1+x)^{(1/3)}+2/3*\arctan(1/3*3^{(1/2)}+2/3*(1+x)^{(1/3)})/(-1+x)^{(1/3)}*3^{(1/2)})*3^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 77, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {50, 59}

$$\sqrt[3]{x-1}(x+1)^{2/3} + \frac{1}{3} \log(x-1) + \log\left(\frac{\sqrt[3]{x+1}}{\sqrt[3]{x-1}} - 1\right) + \frac{2 \tan^{-1}\left(\frac{2\sqrt[3]{x+1}}{\sqrt{3}\sqrt[3]{x-1}} + \frac{1}{\sqrt{3}}\right)}{\sqrt{3}}$$

Antiderivative was successfully verified.

[In] Int[(-1 + x)^(1/3)/(1 + x)^(1/3), x]

[Out] $(-1 + x)^{(1/3)}*(1 + x)^{(2/3)} + (2*\text{ArcTan}[1/\text{Sqrt}[3] + (2*(1 + x)^{(1/3)})/(\text{Sqrt}[3]*(-1 + x)^{(1/3)})])/\text{Sqrt}[3] + \text{Log}[-1 + x]/3 + \text{Log}[-1 + (1 + x)^{(1/3)}/(-1 + x)^{(1/3)]}$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 59

```
Int[1/(((a_.) + (b_.)*(x_))^(1/3)*((c_.) + (d_.)*(x_))^(2/3)), x_Symbol] :=
With[{q = Rt[d/b, 3]}, -Simp[(Sqrt[3]*q*ArcTan[(2*q*(a + b*x)^(1/3))/(Sqrt
[3]*(c + d*x)^(1/3)) + 1/Sqrt[3]])/d, x] + (-Simp[(3*q*Log[(q*(a + b*x)^(1/
3))]/(c + d*x)^(1/3) - 1])/(2*d), x] - Simp[(q*Log[c + d*x])/(2*d), x]) /;
FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && PosQ[d/b]
```


Rubi steps

$$\int \frac{\sqrt[3]{-1+x}}{\sqrt[3]{1+x}} dx = \sqrt[3]{-1+x}(1+x)^{2/3} - \frac{2}{3} \int \frac{1}{(-1+x)^{2/3} \sqrt[3]{1+x}} dx$$

$$= \sqrt[3]{-1+x}(1+x)^{2/3} + \frac{2 \tan^{-1}\left(\frac{1}{\sqrt{3}} + \frac{2\sqrt[3]{1+x}}{\sqrt{3}\sqrt[3]{-1+x}}\right)}{\sqrt{3}} + \frac{1}{3} \log(-1+x) + \log\left(-1 + \frac{\sqrt[3]{1+x}}{\sqrt[3]{-1+x}}\right)$$

Mathematica [C] time = 0.02, size = 48, normalized size = 0.62

$$\frac{3 \left(\frac{x-1}{x+1}\right)^{4/3} (x+1)^{4/3} {}_2F_1\left(\frac{1}{3}, \frac{4}{3}, \frac{7}{3}, \frac{1-x}{2}\right)}{4\sqrt[3]{2}}$$

Antiderivative was successfully verified.

[In] Integrate[(-1 + x)^(1/3)/(1 + x)^(1/3), x]

[Out] (3*((-1 + x)/(1 + x))^(4/3)*(1 + x)^(4/3)*Hypergeometric2F1[1/3, 4/3, 7/3, (1 - x)/2])/(4*2^(1/3))

fricas [A] time = 0.45, size = 107, normalized size = 1.39

$$-\frac{2}{3} \sqrt{3} \arctan\left(\frac{\sqrt{3}(x+1) + 2\sqrt{3}(x+1)^{2/3}(x-1)^{1/3}}{3(x+1)}\right) + (x+1)^{2/3}(x-1)^{1/3} - \frac{1}{3} \log\left(\frac{(x+1)^{2/3}(x-1)^{1/3} + (x+1)^{1/3}(x-1)^{2/3}}{x+1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-1+x)^(1/3)/(1+x)^(1/3), x, algorithm="fricas")

[Out] -2/3*sqrt(3)*arctan(1/3*(sqrt(3)*(x + 1) + 2*sqrt(3)*(x + 1)^(2/3)*(x - 1)^(1/3))/(x + 1)) + (x + 1)^(2/3)*(x - 1)^(1/3) - 1/3*log(((x + 1)^(2/3)*(x - 1)^(1/3) + (x + 1)^(1/3)*(x - 1)^(2/3) + x + 1)/(x + 1)) + 2/3*log(((x + 1)^(2/3)*(x - 1)^(1/3) - x - 1)/(x + 1))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(x-1)^{\frac{1}{3}}}{(x+1)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-1+x)^(1/3)/(1+x)^(1/3),x, algorithm="giac")

[Out] integrate((x - 1)^(1/3)/(x + 1)^(1/3), x)

maple [C] time = 0.38, size = 573, normalized size = 7.44

$$(x-1)^{\frac{1}{3}}(x+1)^{\frac{2}{3}} + \frac{2 \operatorname{RootOf}(_Z^2 + _Z + 1) \ln \left(\frac{-2x^2 \operatorname{RootOf}(_Z^2 + _Z + 1)^2 + x^2 \operatorname{RootOf}(_Z^2 + _Z + 1) + 2x \operatorname{RootOf}(_Z^2 + _Z + 1)^2 + x^2 + 3(x^3 - x^2 - x + 1)^{\frac{1}{3}} x \operatorname{RootOf}(_Z^2 + _Z + 1)}{\dots} \right)}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x-1)^(1/3)/(x+1)^(1/3),x)

[Out] (x-1)^(1/3)*(x+1)^(2/3)+(2/3*RootOf(_Z^2+_Z+1)*ln(-(2*RootOf(_Z^2+_Z+1)^2*x^2+3*RootOf(_Z^2+_Z+1)*(x^3-x^2-x+1)^(2/3)+3*RootOf(_Z^2+_Z+1)*(x^3-x^2-x+1)^(1/3)*x-2*RootOf(_Z^2+_Z+1)^2*x+5*RootOf(_Z^2+_Z+1)*x^2-3*RootOf(_Z^2+_Z+1)*(x^3-x^2-x+1)^(1/3)-4*RootOf(_Z^2+_Z+1)*x+2*x^2-RootOf(_Z^2+_Z+1)-2)/(x-1))-2/3*ln((-2*RootOf(_Z^2+_Z+1)^2*x^2+3*RootOf(_Z^2+_Z+1)*(x^3-x^2-x+1)^(2/3)+3*RootOf(_Z^2+_Z+1)*(x^3-x^2-x+1)^(1/3)*x+2*RootOf(_Z^2+_Z+1)^2*x+RootOf(_Z^2+_Z+1)*x^2+3*(x^3-x^2-x+1)^(2/3)-3*RootOf(_Z^2+_Z+1)*(x^3-x^2-x+1)^(1/3)+3*(x^3-x^2-x+1)^(1/3)*x+x^2-3*(x^3-x^2-x+1)^(1/3)-RootOf(_Z^2+_Z+1)-2*x+1)/(x-1))*RootOf(_Z^2+_Z+1)-2/3*ln((-2*RootOf(_Z^2+_Z+1)^2*x^2+3*RootOf(_Z^2+_Z+1)*(x^3-x^2-x+1)^(2/3)+3*RootOf(_Z^2+_Z+1)*(x^3-x^2-x+1)^(1/3)*x+2*RootOf(_Z^2+_Z+1)^2*x+RootOf(_Z^2+_Z+1)*x^2+3*(x^3-x^2-x+1)^(2/3)-3*RootOf(_Z^2+_Z+1)*(x^3-x^2-x+1)^(1/3)+3*(x^3-x^2-x+1)^(1/3)*x+x^2-3*(x^3-x^2-x+1)^(1/3)-RootOf(_Z^2+_Z+1)-2*x+1)/(x-1)))/(x-1)^(2/3)*((x-1)^2*(x+1))^(1/3)/(x+1)^(1/3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(x-1)^{\frac{1}{3}}}{(x+1)^{\frac{1}{3}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-1+x)^(1/3)/(1+x)^(1/3),x, algorithm="maxima")

[Out] integrate((x - 1)^(1/3)/(x + 1)^(1/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(x-1)^{1/3}}{(x+1)^{1/3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x - 1)^(1/3)/(x + 1)^(1/3), x)`

[Out] `int((x - 1)^(1/3)/(x + 1)^(1/3), x)`

sympy [C] time = 2.55, size = 39, normalized size = 0.51

$$\frac{2^{\frac{2}{3}} (x-1)^{\frac{4}{3}} \Gamma\left(\frac{4}{3}\right) {}_2F_1\left(\frac{1}{3}, \frac{4}{3} \middle| \frac{7}{3} \middle| \frac{(x-1)e^{i\pi}}{2}\right)}{2\Gamma\left(\frac{7}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((-1+x)**(1/3)/(1+x)**(1/3), x)`

[Out] `2**(2/3)*(x - 1)**(4/3)*gamma(4/3)*hyper((1/3, 4/3), (7/3,), (x - 1)*exp_polar(I*pi)/2)/(2*gamma(7/3))`

3.1629 $\int (a + bx)^{3/2} \sqrt[4]{c + dx} dx$

Optimal. Leaf size=185

$$\frac{16(bc - ad)^{13/4} \sqrt{-\frac{d(ax+b)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{77b^{5/4}d^3\sqrt{a+bx}} - \frac{8\sqrt{a+bx} \sqrt[4]{c+dx} (bc - ad)^2}{77bd^2} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx} (bc - ad)}{77bd}$$

[Out] $\frac{4}{77}(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(1/4)}/b/d+4/11*(b*x+a)^{(5/2)}*(d*x+c)^{(1/4)}/b-8/77*(-a*d+b*c)^2*(d*x+c)^{(1/4)}*(b*x+a)^{(1/2)}/b/d^2+16/77*(-a*d+b*c)^{(13/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(5/4)}/d^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.21, antiderivative size = 185, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 224, 221}

$$\frac{16(bc - ad)^{13/4} \sqrt{-\frac{d(ax+b)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{77b^{5/4}d^3\sqrt{a+bx}} - \frac{8\sqrt{a+bx} \sqrt[4]{c+dx} (bc - ad)^2}{77bd^2} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx} (bc - ad)}{77bd}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}*(c + d*x)^{(1/4)}, x]$

[Out] $(-8*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/4)})/(77*b*d^2) + (4*(b*c - a*d)*(a + b*x)^{(3/2)}*(c + d*x)^{(1/4)})/(77*b*d) + (4*(a + b*x)^{(5/2)}*(c + d*x)^{(1/4)})/(11*b) + (16*(b*c - a*d)^{(13/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(77*b^{(5/4)}*d^3*\operatorname{Sqrt}[a + b*x])$

Rule 50

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x] \rightarrow \operatorname{Simp}[(a + b*x)^{m+1}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{n-1}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m+n+1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m-n, 0]))) && !ILtQ[m+n+2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{p*(m+1)-1}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ

[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] :> Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] :> Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int (a + bx)^{3/2} \sqrt[4]{c + dx} \, dx &= \frac{4(a + bx)^{5/2} \sqrt[4]{c + dx}}{11b} + \frac{(bc - ad) \int \frac{(a+bx)^{3/2}}{(c+dx)^{3/4}} \, dx}{11b} \\
 &= \frac{4(bc - ad)(a + bx)^{3/2} \sqrt[4]{c + dx}}{77bd} + \frac{4(a + bx)^{5/2} \sqrt[4]{c + dx}}{11b} - \frac{(6(bc - ad)^2) \int \frac{\sqrt{a+bx}}{(c+dx)^{3/4}} \, dx}{77bd} \\
 &= -\frac{8(bc - ad)^2 \sqrt{a + bx} \sqrt[4]{c + dx}}{77bd^2} + \frac{4(bc - ad)(a + bx)^{3/2} \sqrt[4]{c + dx}}{77bd} + \frac{4(a + bx)^{5/2} \sqrt[4]{c + dx}}{11b} \\
 &= -\frac{8(bc - ad)^2 \sqrt{a + bx} \sqrt[4]{c + dx}}{77bd^2} + \frac{4(bc - ad)(a + bx)^{3/2} \sqrt[4]{c + dx}}{77bd} + \frac{4(a + bx)^{5/2} \sqrt[4]{c + dx}}{11b} \\
 &= -\frac{8(bc - ad)^2 \sqrt{a + bx} \sqrt[4]{c + dx}}{77bd^2} + \frac{4(bc - ad)(a + bx)^{3/2} \sqrt[4]{c + dx}}{77bd} + \frac{4(a + bx)^{5/2} \sqrt[4]{c + dx}}{11b} \\
 &= -\frac{8(bc - ad)^2 \sqrt{a + bx} \sqrt[4]{c + dx}}{77bd^2} + \frac{4(bc - ad)(a + bx)^{3/2} \sqrt[4]{c + dx}}{77bd} + \frac{4(a + bx)^{5/2} \sqrt[4]{c + dx}}{11b}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.39

$$\frac{2(a + bx)^{5/2} \sqrt[4]{c + dx} {}_2F_1\left(-\frac{1}{4}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc}\right)}{5b \sqrt[4]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)*(c + d*x)^(1/4), x]

[Out] (2*(a + b*x)^(5/2)*(c + d*x)^(1/4)*Hypergeometric2F1[-1/4, 5/2, 7/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*((b*(c + d*x))/(b*c - a*d))^(1/4))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bx + a\right)^{\frac{3}{2}}\left(dx + c\right)^{\frac{1}{4}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(1/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)*(d*x + c)^(1/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}} (dx + c)^{\frac{1}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(1/4), x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)*(d*x + c)^(1/4), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}} (dx + c)^{\frac{1}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)*(d*x+c)^(1/4), x)

[Out] int((b*x+a)^(3/2)*(d*x+c)^(1/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}} (dx + c)^{\frac{1}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)*(d*x + c)^(1/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{3/2} (c + dx)^{1/4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)*(c + d*x)^(1/4),x)

[Out] int((a + b*x)^(3/2)*(c + d*x)^(1/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{3}{2}} \sqrt[4]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)*(d*x+c)**(1/4),x)

[Out] Integral((a + b*x)**(3/2)*(c + d*x)**(1/4), x)

3.1630 $\int \sqrt{a+bx} \sqrt[4]{c+dx} dx$

Optimal. Leaf size=147

$$\frac{8(bc-ad)^{9/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{21b^{5/4}d^2\sqrt{a+bx}} + \frac{4\sqrt{a+bx} \sqrt[4]{c+dx} (bc-ad)}{21bd} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7b}$$

[Out] $4/7*(b*x+a)^{(3/2)}*(d*x+c)^{(1/4)}/b+4/21*(-a*d+b*c)*(d*x+c)^{(1/4)}*(b*x+a)^{(1/2)}/b/d-8/21*(-a*d+b*c)^{(9/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(5/4)}/d^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.09, antiderivative size = 147, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 224, 221}

$$\frac{8(bc-ad)^{9/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{21b^{5/4}d^2\sqrt{a+bx}} + \frac{4\sqrt{a+bx} \sqrt[4]{c+dx} (bc-ad)}{21bd} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7b}$$

Antiderivative was successfully verified.

[In] `Int[Sqrt[a + b*x]*(c + d*x)^(1/4), x]`

[Out] $(4*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/4)})/(21*b*d) + (4*(a + b*x)^{(3/2)}*(c + d*x)^{(1/4)})/(7*b) - (8*(b*c - a*d)^{(9/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(21*b^{(5/4)}*d^2*\operatorname{Sqrt}[a + b*x])$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```


Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \sqrt{a+bx} \sqrt[4]{c+dx} \, dx &= \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7b} + \frac{(bc-ad) \int \frac{\sqrt{a+bx}}{(c+dx)^{3/4}} \, dx}{7b} \\
 &= \frac{4(bc-ad)\sqrt{a+bx} \sqrt[4]{c+dx}}{21bd} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7b} - \frac{(2(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} \, dx}{21bd} \\
 &= \frac{4(bc-ad)\sqrt{a+bx} \sqrt[4]{c+dx}}{21bd} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7b} - \frac{(8(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+}} \right)}{21bd^2} \\
 &= \frac{4(bc-ad)\sqrt{a+bx} \sqrt[4]{c+dx}}{21bd} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7b} - \frac{(8(bc-ad)^2 \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+}} \right)}{21bd^2 \sqrt{a+bx}} \\
 &= \frac{4(bc-ad)\sqrt{a+bx} \sqrt[4]{c+dx}}{21bd} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7b} - \frac{8(bc-ad)^{9/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt{a+bx} \sqrt[4]{c+dx}}{\sqrt{a+bx}} \right) \right)}{21b^{5/4} d^2 \sqrt{a+bx}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.50

$$\frac{2(a+bx)^{3/2} \sqrt[4]{c+dx} {}_2F_1 \left(-\frac{1}{4}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b \sqrt[4]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]*(c + d*x)^(1/4),x]

[Out] $(2*(a + b*x)^{(3/2)}*(c + d*x)^{(1/4)}*Hypergeometric2F1[-1/4, 3/2, 5/2, (d*(a + b*x))/(-(b*c) + a*d)])/(3*b*((b*(c + d*x))/(b*c - a*d))^{(1/4)})$

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\sqrt{bx+a}(dx+c)^{\frac{1}{4}},x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(1/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{1}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)*(d*x + c)^(1/4), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{1}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)*(d*x+c)^(1/4),x)

[Out] int((b*x+a)^(1/2)*(d*x+c)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{1}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)*(d*x + c)^(1/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{a + bx} (c + dx)^{1/4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)*(c + d*x)^(1/4), x)

[Out] int((a + b*x)^(1/2)*(c + d*x)^(1/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{a + bx} \sqrt[4]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)*(d*x+c)**(1/4), x)

[Out] Integral(sqrt(a + b*x)*(c + d*x)**(1/4), x)

$$3.1631 \quad \int \frac{\sqrt[4]{c+dx}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=111

$$\frac{4(bc-ad)^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{3b^{5/4} d \sqrt{a+bx}} + \frac{4\sqrt{a+bx} \sqrt[4]{c+dx}}{3b}$$

[Out] $4/3*(d*x+c)^{(1/4)}*(b*x+a)^{(1/2)}/b+4/3*(-a*d+b*c)^{(5/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(5/4)}/d/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.07, antiderivative size = 111, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 224, 221}

$$\frac{4(bc-ad)^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{3b^{5/4} d \sqrt{a+bx}} + \frac{4\sqrt{a+bx} \sqrt[4]{c+dx}}{3b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/4)/Sqrt[a + b*x], x]

[Out] $(4*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/4)})/(3*b) + (4*(b*c - a*d)^{(5/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1)/(3*b^{(5/4)}*d*\operatorname{Sqrt}[a + b*x])$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[4]{c+dx}}{\sqrt{a+bx}} dx &= \frac{4\sqrt{a+bx}\sqrt[4]{c+dx}}{3b} + \frac{(bc-ad) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{3b} \\
&= \frac{4\sqrt{a+bx}\sqrt[4]{c+dx}}{3b} + \frac{(4(bc-ad)) \operatorname{Subst}\left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx}\right)}{3bd} \\
&= \frac{4\sqrt{a+bx}\sqrt[4]{c+dx}}{3b} + \frac{\left(4(bc-ad)\sqrt{\frac{d(a+bx)}{-bc+ad}}\right) \operatorname{Subst}\left(\int \frac{1}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)d}}} dx, x, \sqrt[4]{c+dx}\right)}{3bd\sqrt{a+bx}} \\
&= \frac{4\sqrt{a+bx}\sqrt[4]{c+dx}}{3b} + \frac{4(bc-ad)^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{3b^{5/4}d\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.64

$$\frac{2\sqrt{a+bx}\sqrt[4]{c+dx} {}_2F_1\left(-\frac{1}{4}, \frac{1}{2}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b^4 \sqrt{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^(1/4)/Sqrt[a + b*x], x]
```

[Out] $(2\sqrt{a + b*x}*(c + d*x)^{1/4}*\text{Hypergeometric2F1}[-1/4, 1/2, 3/2, (d*(a + b*x))/(-(b*c) + a*d)])/(b*((b*(c + d*x))/(b*c - a*d))^{1/4})$

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx + c)^{\frac{1}{4}}}{\sqrt{bx + a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(1/4)/(b*x+a)^(1/2),x, algorithm="fricas")`

[Out] `integral((d*x + c)^(1/4)/sqrt(b*x + a), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{4}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(1/4)/(b*x+a)^(1/2),x, algorithm="giac")`

[Out] `integrate((d*x + c)^(1/4)/sqrt(b*x + a), x)`

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{4}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(1/4)/(b*x+a)^(1/2),x)`

[Out] `int((d*x+c)^(1/4)/(b*x+a)^(1/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{4}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(1/4)/(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] `integrate((d*x + c)^(1/4)/sqrt(b*x + a), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{1/4}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/4)/(a + b*x)^(1/2), x)

[Out] int((c + d*x)^(1/4)/(a + b*x)^(1/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[4]{c + dx}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/4)/(b*x+a)**(1/2), x)

[Out] Integral((c + d*x)**(1/4)/sqrt(a + b*x), x)

$$3.1632 \quad \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=104

$$\frac{2\sqrt[4]{bc-ad} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{b^{5/4} \sqrt{a+bx}} - \frac{2\sqrt[4]{c+dx}}{b\sqrt{a+bx}}$$

[Out] $-2*(d*x+c)^{(1/4)}/b/(b*x+a)^{(1/2)}+2*(-a*d+b*c)^{(1/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(5/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.06, antiderivative size = 104, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 63, 224, 221}

$$\frac{2\sqrt[4]{bc-ad} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{b^{5/4} \sqrt{a+bx}} - \frac{2\sqrt[4]{c+dx}}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(1/4)}/(a + b*x)^{(3/2)}, x]$

[Out] $(-2*(c + d*x)^{(1/4)}/(b*\operatorname{Sqrt}[a + b*x]) + (2*(b*c - a*d)^{(1/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/ (b^{(5/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IntegerQ[m+n+2], 0] && (FractionQ[m] || GeQ[2*n+m+1, 0]) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

`Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]`

Rule 224

`Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]`

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{3/2}} dx &= -\frac{2\sqrt[4]{c+dx}}{b\sqrt{a+bx}} + \frac{d \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{2b} \\
 &= -\frac{2\sqrt[4]{c+dx}}{b\sqrt{a+bx}} + \frac{2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{b} \\
 &= -\frac{2\sqrt[4]{c+dx}}{b\sqrt{a+bx}} + \frac{\left(2\sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)^d}}} dx, x, \sqrt[4]{c+dx} \right)}{b\sqrt{a+bx}} \\
 &= -\frac{2\sqrt[4]{c+dx}}{b\sqrt{a+bx}} + \frac{2\sqrt[4]{bc-ad} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{5/4} \sqrt{a+bx}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.68

$$-\frac{2\sqrt[4]{c+dx} {}_2F_1 \left(-\frac{1}{2}, -\frac{1}{4}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt{a+bx} \sqrt[4]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/4)/(a + b*x)^(3/2), x]

[Out] $(-2*(c + d*x)^{(1/4)}*Hypergeometric2F1[-1/2, -1/4, 1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*\text{Sqrt}[a + b*x]*((b*(c + d*x))/(b*c - a*d))^{(1/4)})$

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{1}{4}}}{b^2x^2+2abx+a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(1/4)/(b*x+a)^(3/2),x, algorithm="fricas")`

[Out] `integral(sqrt(b*x + a)*(d*x + c)^(1/4)/(b^2*x^2 + 2*a*b*x + a^2), x)`

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(1/4)/(b*x+a)^(3/2),x, algorithm="giac")`

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
UT:sage2:=int(sage0,x);OUTPUT:

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{4}}}{(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(1/4)/(b*x+a)^(3/2),x)`

[Out] `int((d*x+c)^(1/4)/(b*x+a)^(3/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{4}}}{(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(1/4)/(b*x+a)^(3/2),x, algorithm="maxima")`

[Out] `integrate((d*x + c)^(1/4)/(b*x + a)^(3/2), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{1/4}}{(a + bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/4)/(a + b*x)^(3/2), x)

[Out] int((c + d*x)^(1/4)/(a + b*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[4]{c + dx}}{(a + bx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/4)/(b*x+a)**(3/2), x)

[Out] Integral((c + d*x)**(1/4)/(a + b*x)**(3/2), x)

$$3.1633 \quad \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=145

$$\frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{3b^{5/4}\sqrt{a+bx}(bc-ad)^{3/4}} - \frac{d\sqrt[4]{c+dx}}{3b\sqrt{a+bx}(bc-ad)} - \frac{2\sqrt[4]{c+dx}}{3b(a+bx)^{3/2}}$$

[Out] $-2/3*(d*x+c)^{(1/4)}/b/(b*x+a)^{(3/2)}-1/3*d*(d*x+c)^{(1/4)}/b/(-a*d+b*c)/(b*x+a)^{(1/2)}-1/3*d*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a))/(-a*d+b*c)^{(1/2)}/b^{(5/4)}/(-a*d+b*c)^{(3/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.09, antiderivative size = 145, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 51, 63, 224, 221}

$$\frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{3b^{5/4}\sqrt{a+bx}(bc-ad)^{3/4}} - \frac{d\sqrt[4]{c+dx}}{3b\sqrt{a+bx}(bc-ad)} - \frac{2\sqrt[4]{c+dx}}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(1/4)}/(a + b*x)^{(5/2)}, x]$

[Out] $(-2*(c + d*x)^{(1/4)})/(3*b*(a + b*x)^{(3/2)}) - (d*(c + d*x)^{(1/4)})/(3*b*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]) - (d*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1)/(3*b^{(5/4)}*(b*c - a*d)^{(3/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(IntegerQ[n] \&\& !IntegerQ[m]) \&\& !(IntegerQ[m + n + 2, 0] \&\& (FractionQ[m] || GeQ[2*n + m + 1, 0])) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}]/((b*c - a*d)*(m + 1)), x] - \operatorname{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, n\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(LtQ$

```
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
  {p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
  (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
  b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
  4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
  b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[
  a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
  b/a] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[4]{c+dx}}{(a+bx)^{5/2}} dx &= -\frac{2\sqrt[4]{c+dx}}{3b(a+bx)^{3/2}} + \frac{d \int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/4}} dx}{6b} \\
&= -\frac{2\sqrt[4]{c+dx}}{3b(a+bx)^{3/2}} - \frac{d\sqrt[4]{c+dx}}{3b(bc-ad)\sqrt{a+bx}} - \frac{d^2 \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{12b(bc-ad)} \\
&= -\frac{2\sqrt[4]{c+dx}}{3b(a+bx)^{3/2}} - \frac{d\sqrt[4]{c+dx}}{3b(bc-ad)\sqrt{a+bx}} - \frac{d \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{3b(bc-ad)} \\
&= -\frac{2\sqrt[4]{c+dx}}{3b(a+bx)^{3/2}} - \frac{d\sqrt[4]{c+dx}}{3b(bc-ad)\sqrt{a+bx}} - \frac{\left(d\sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)d}}} dx, x, \sqrt[4]{c+dx} \right)}{3b(bc-ad)\sqrt{a+bx}} \\
&= -\frac{2\sqrt[4]{c+dx}}{3b(a+bx)^{3/2}} - \frac{d\sqrt[4]{c+dx}}{3b(bc-ad)\sqrt{a+bx}} - \frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right) - 1}{3b^{5/4}(bc-ad)^{3/4}\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.50

$$-\frac{2\sqrt[4]{c+dx} {}_2F_1 \left(-\frac{3}{2}, -\frac{1}{4}, -\frac{1}{2}, \frac{d(a+bx)}{ad-bc} \right)}{3b(a+bx)^{3/2} \sqrt[4]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/4)/(a + b*x)^(5/2), x]

[Out] (-2*(c + d*x)^(1/4)*Hypergeometric2F1[-3/2, -1/4, -1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(1/4))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\operatorname{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{1}{4}}}{b^3 x^3 + 3ab^2 x^2 + 3a^2 bx + a^3}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/4)/(b*x+a)^(5/2), x, algorithm="fricas")

```
[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/4)/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)
```

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(1/4)/(b*x+a)^(5/2),x, algorithm="giac")
```

```
[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP
UT:sage2:=int(sage0,x):;OUTPUT:
```

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{4}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^(1/4)/(b*x+a)^(5/2),x)
```

```
[Out] int((d*x+c)^(1/4)/(b*x+a)^(5/2),x)
```

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{4}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(1/4)/(b*x+a)^(5/2),x, algorithm="maxima")
```

```
[Out] integrate((d*x + c)^(1/4)/(b*x + a)^(5/2), x)
```

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{1/4}}{(a + bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(1/4)/(a + b*x)^(5/2),x)
```

```
[Out] int((c + d*x)^(1/4)/(a + b*x)^(5/2), x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[4]{c + dx}}{(a + bx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/4)/(b*x+a)**(5/2),x)

[Out] Integral((c + d*x)**(1/4)/(a + b*x)**(5/2), x)

$$3.1634 \quad \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{7/2}} dx$$

Optimal. Leaf size=185

$$\frac{d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{6b^{5/4} \sqrt{a+bx} (bc-ad)^{7/4}} + \frac{d^2 \sqrt[4]{c+dx}}{6b \sqrt{a+bx} (bc-ad)^2} - \frac{d \sqrt[4]{c+dx}}{15b(a+bx)^{3/2}(bc-ad)} - \frac{2 \sqrt[4]{c+dx}}{5b(a+bx)^{5/2}}$$

[Out] $-2/5*(d*x+c)^{(1/4)}/b/(b*x+a)^{(5/2)}-1/15*d*(d*x+c)^{(1/4)}/b/(-a*d+b*c)/(b*x+a)^{(3/2)}+1/6*d^2*(d*x+c)^{(1/4)}/b/(-a*d+b*c)^2/(b*x+a)^{(1/2)}+1/6*d^2*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(5/4)}/(-a*d+b*c)^{(7/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.13, antiderivative size = 185, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 51, 63, 224, 221}

$$\frac{d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{6b^{5/4} \sqrt{a+bx} (bc-ad)^{7/4}} + \frac{d^2 \sqrt[4]{c+dx}}{6b \sqrt{a+bx} (bc-ad)^2} - \frac{d \sqrt[4]{c+dx}}{15b(a+bx)^{3/2}(bc-ad)} - \frac{2 \sqrt[4]{c+dx}}{5b(a+bx)^{5/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(1/4)}/(a + b*x)^{(7/2)}, x]$

[Out] $(-2*(c + d*x)^{(1/4)})/(5*b*(a + b*x)^{(5/2)}) - (d*(c + d*x)^{(1/4)})/(15*b*(b*c - a*d)*(a + b*x)^{(3/2)}) + (d^2*(c + d*x)^{(1/4)})/(6*b*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]) + (d^2*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(6*b^{(5/4)}*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}/((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*($

```

m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]

```

Rule 63

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 221

```

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]

```

Rule 224

```

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]

```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[4]{c+dx}}{(a+bx)^{7/2}} dx &= -\frac{2\sqrt[4]{c+dx}}{5b(a+bx)^{5/2}} + \frac{d \int \frac{1}{(a+bx)^{5/2}(c+dx)^{3/4}} dx}{10b} \\
&= -\frac{2\sqrt[4]{c+dx}}{5b(a+bx)^{5/2}} - \frac{d\sqrt[4]{c+dx}}{15b(bc-ad)(a+bx)^{3/2}} - \frac{d^2 \int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/4}} dx}{12b(bc-ad)} \\
&= -\frac{2\sqrt[4]{c+dx}}{5b(a+bx)^{5/2}} - \frac{d\sqrt[4]{c+dx}}{15b(bc-ad)(a+bx)^{3/2}} + \frac{d^2\sqrt[4]{c+dx}}{6b(bc-ad)^2\sqrt{a+bx}} + \frac{d^3 \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{24b(bc-ad)^2} \\
&= -\frac{2\sqrt[4]{c+dx}}{5b(a+bx)^{5/2}} - \frac{d\sqrt[4]{c+dx}}{15b(bc-ad)(a+bx)^{3/2}} + \frac{d^2\sqrt[4]{c+dx}}{6b(bc-ad)^2\sqrt{a+bx}} + \frac{d^2 \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx \right)}{6b(bc-ad)} \\
&= -\frac{2\sqrt[4]{c+dx}}{5b(a+bx)^{5/2}} - \frac{d\sqrt[4]{c+dx}}{15b(bc-ad)(a+bx)^{3/2}} + \frac{d^2\sqrt[4]{c+dx}}{6b(bc-ad)^2\sqrt{a+bx}} + \frac{\left(d^2\sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx \right)}{6b(bc-ad)} \\
&= -\frac{2\sqrt[4]{c+dx}}{5b(a+bx)^{5/2}} - \frac{d\sqrt[4]{c+dx}}{15b(bc-ad)(a+bx)^{3/2}} + \frac{d^2\sqrt[4]{c+dx}}{6b(bc-ad)^2\sqrt{a+bx}} + \frac{d^2\sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{d\sqrt{a+bx}}{\sqrt{bc-ad}} \right) \right)}{6b^{5/4}(bc-ad)^{7/4}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.39

$$-\frac{2\sqrt[4]{c+dx} {}_2F_1\left(-\frac{5}{2}, -\frac{1}{4}; -\frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{5b(a+bx)^{5/2} \sqrt[4]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/4)/(a + b*x)^(7/2), x]

[Out] (-2*(c + d*x)^(1/4)*Hypergeometric2F1[-5/2, -1/4, -3/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(1/4))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{1}{4}}}{b^4x^4 + 4ab^3x^3 + 6a^2b^2x^2 + 4a^3bx + a^4}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/4)/(b*x+a)^(7/2),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/4)/(b^4*x^4 + 4*a*b^3*x^3 + 6*a^2*b^2*x^2 + 4*a^3*b*x + a^4), x)

giac [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/4)/(b*x+a)^(7/2),x, algorithm="giac")

[Out] Exception raised: TypeError >> An error occurred running a Giac command:INP UT:sage2:=int(sage0,x);;OUTPUT:

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{4}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/4)/(b*x+a)^(7/2),x)

[Out] int((d*x+c)^(1/4)/(b*x+a)^(7/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{4}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/4)/(b*x+a)^(7/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/4)/(b*x + a)^(7/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{1/4}}{(a + bx)^{7/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(1/4)/(a + b*x)^(7/2), x)
```

```
[Out] int((c + d*x)^(1/4)/(a + b*x)^(7/2), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{\sqrt[4]{c + dx}}{(a + bx)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(1/4)/(b*x+a)**(7/2), x)
```

```
[Out] Integral((c + d*x)**(1/4)/(a + b*x)**(7/2), x)
```

3.1635 $\int (a + bx)^{3/2}(c + dx)^{3/4} dx$

Optimal. Leaf size=270

$$\frac{16(bc - ad)^{15/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{65b^{7/4}d^3\sqrt{a+bx}} + \frac{16(bc - ad)^{15/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{65b^{7/4}d^3\sqrt{a+bx}}$$

[Out] $4/39*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(3/4)}/b/d+4/13*(b*x+a)^{(5/2)}*(d*x+c)^{(3/4)}/b-8/65*(-a*d+b*c)^2*(d*x+c)^{(3/4)}*(b*x+a)^{(1/2)}/b/d^2+16/65*(-a*d+b*c)^{(15/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/d^3/(b*x+a)^{(1/2)}-16/65*(-a*d+b*c)^{(15/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/d^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.36, antiderivative size = 270, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {50, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{16(bc - ad)^{15/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{65b^{7/4}d^3\sqrt{a+bx}} + \frac{16(bc - ad)^{15/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{65b^{7/4}d^3\sqrt{a+bx}} - \frac{8\sqrt{a}}{d^3}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}*(c + d*x)^{(3/4)}, x]$

[Out] $(-8*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)})/(65*b*d^2) + (4*(b*c - a*d)*(a + b*x)^{(3/2)}*(c + d*x)^{(3/4)})/(39*b*d) + (4*(a + b*x)^{(5/2)}*(c + d*x)^{(3/4)})/(13*b) + (16*(b*c - a*d)^{(15/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1])/(65*b^{(7/4)}*d^3*\operatorname{Sqrt}[a + b*x]) - (16*(b*c - a*d)^{(15/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1])/(65*b^{(7/4)}*d^3*\operatorname{Sqrt}[a + b*x])$

Rule 50

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x] \rightarrow \operatorname{Simp}[(a + b*x)^{m+1}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[n*(b*c - a*d)/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{n-1}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m+n+1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m-n, 0]))) && !ILtQ[m+n+2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt
[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x
] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[
a, 0]
```

Rubi steps

$$\begin{aligned}
\int (a + bx)^{3/2}(c + dx)^{3/4} dx &= \frac{4(a + bx)^{5/2}(c + dx)^{3/4}}{13b} + \frac{(3(bc - ad)) \int \frac{(a+bx)^{3/2}}{\sqrt[4]{c+dx}} dx}{13b} \\
&= \frac{4(bc - ad)(a + bx)^{3/2}(c + dx)^{3/4}}{39bd} + \frac{4(a + bx)^{5/2}(c + dx)^{3/4}}{13b} - \frac{(2(bc - ad)^2) \int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx}{13bd} \\
&= -\frac{8(bc - ad)^2 \sqrt{a + bx} (c + dx)^{3/4}}{65bd^2} + \frac{4(bc - ad)(a + bx)^{3/2}(c + dx)^{3/4}}{39bd} + \frac{4(a + bx)^{5/2}(c + dx)^{3/4}}{13b} \\
&= -\frac{8(bc - ad)^2 \sqrt{a + bx} (c + dx)^{3/4}}{65bd^2} + \frac{4(bc - ad)(a + bx)^{3/2}(c + dx)^{3/4}}{39bd} + \frac{4(a + bx)^{5/2}(c + dx)^{3/4}}{13b} \\
&= -\frac{8(bc - ad)^2 \sqrt{a + bx} (c + dx)^{3/4}}{65bd^2} + \frac{4(bc - ad)(a + bx)^{3/2}(c + dx)^{3/4}}{39bd} + \frac{4(a + bx)^{5/2}(c + dx)^{3/4}}{13b} \\
&= -\frac{8(bc - ad)^2 \sqrt{a + bx} (c + dx)^{3/4}}{65bd^2} + \frac{4(bc - ad)(a + bx)^{3/2}(c + dx)^{3/4}}{39bd} + \frac{4(a + bx)^{5/2}(c + dx)^{3/4}}{13b} \\
&= -\frac{8(bc - ad)^2 \sqrt{a + bx} (c + dx)^{3/4}}{65bd^2} + \frac{4(bc - ad)(a + bx)^{3/2}(c + dx)^{3/4}}{39bd} + \frac{4(a + bx)^{5/2}(c + dx)^{3/4}}{13b} \\
&= -\frac{8(bc - ad)^2 \sqrt{a + bx} (c + dx)^{3/4}}{65bd^2} + \frac{4(bc - ad)(a + bx)^{3/2}(c + dx)^{3/4}}{39bd} + \frac{4(a + bx)^{5/2}(c + dx)^{3/4}}{13b}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.27

$$\frac{2(a + bx)^{5/2}(c + dx)^{3/4} {}_2F_1\left(-\frac{3}{4}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc}\right)}{5b \left(\frac{b(c+dx)}{bc-ad}\right)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)*(c + d*x)^(3/4), x]

[Out] $(2*(a + b*x)^{(5/2)}*(c + d*x)^{(3/4)}*\text{Hypergeometric2F1}[-3/4, 5/2, 7/2, (d*(a + b*x))/(-(b*c) + a*d)])/(5*b*((b*(c + d*x))/(b*c - a*d))^{(3/4)})$

fricas [F] time = 0.51, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bx + a\right)^{\frac{3}{2}}\left(dx + c\right)^{\frac{3}{4}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/2)*(d*x+c)^(3/4),x, algorithm="fricas")`

[Out] `integral((b*x + a)^(3/2)*(d*x + c)^(3/4), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{3}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/2)*(d*x+c)^(3/4),x, algorithm="giac")`

[Out] `integrate((b*x + a)^(3/2)*(d*x + c)^(3/4), x)`

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{3}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(3/2)*(d*x+c)^(3/4),x)`

[Out] `int((b*x+a)^(3/2)*(d*x+c)^(3/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{3}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/2)*(d*x+c)^(3/4),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(3/2)*(d*x + c)^(3/4), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + b x)^{3/2} (c + d x)^{3/4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(3/2)*(c + d*x)^(3/4), x)
```

```
[Out] int((a + b*x)^(3/2)*(c + d*x)^(3/4), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int (a + bx)^{\frac{3}{2}} (c + dx)^{\frac{3}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(3/2)*(d*x+c)**(3/4), x)
```

```
[Out] Integral((a + b*x)**(3/2)*(c + d*x)**(3/4), x)
```

3.1636 $\int \sqrt{a + bx} (c + dx)^{3/4} dx$

Optimal. Leaf size=232

$$\frac{8(bc - ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{15b^{7/4}d^2\sqrt{a+bx}} - \frac{8(bc - ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{15b^{7/4}d^2\sqrt{a+bx}} +$$

[Out] $4/9*(b*x+a)^{(3/2)}*(d*x+c)^{(3/4)}/b+4/15*(-a*d+b*c)*(d*x+c)^{(3/4)}*(b*x+a)^{(1/2)}/b/d-8/15*(-a*d+b*c)^{(11/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/d^2/(b*x+a)^{(1/2)}+8/15*(-a*d+b*c)^{(11/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/d^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.25, antiderivative size = 232, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {50, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{8(bc - ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{15b^{7/4}d^2\sqrt{a+bx}} - \frac{8(bc - ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{15b^{7/4}d^2\sqrt{a+bx}} + \frac{4\sqrt{a+bx}}{d}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)}, x]$

[Out] $(4*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)})/(15*b*d) + (4*(a + b*x)^{(3/2)}*(c + d*x)^{(3/4)})/(9*b) - (8*(b*c - a*d)^{(11/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(15*b^{(7/4)}*d^2*\operatorname{Sqrt}[a + b*x]) + (8*(b*c - a*d)^{(11/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(15*b^{(7/4)}*d^2*\operatorname{Sqrt}[a + b*x])$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{GtQ}[n, 0] \ \&\& \operatorname{NeQ}[m + n + 1, 0] \ \&\& !(\operatorname{IGtQ}[m, 0] \ \&\& (!\operatorname{IntegerQ}[n] || (\operatorname{GtQ}[m, 0] \ \&\& \operatorname{LtQ}[m - n, 0]))) \ \&\& !\operatorname{ILtQ}[m + n + 2, 0] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d))/b +$

$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{ :> } \text{Simp}[\text{EllipticF}[\text{ArcSin}[\text{Rt}[-b, 4]*x]/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{GtQ}[a, 0]$

Rule 224

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{ :> } \text{Dist}[\text{Sqrt}[1 + (b*x^4)/a]/\text{Sqrt}[a + b*x^4], \text{Int}[1/\text{Sqrt}[1 + (b*x^4)/a], x], x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{!GtQ}[a, 0]$

Rule 307

$\text{Int}[(x_)^2/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{ :> } \text{With}[\{q = \text{Rt}[-(b/a), 2]\}, -\text{Dist}[q^{(-1)}, \text{Int}[1/\text{Sqrt}[a + b*x^4], x], x] + \text{Dist}[1/q, \text{Int}[(1 + q*x^2)/\text{Sqrt}[a + b*x^4], x], x]] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a]$

Rule 424

$\text{Int}[\text{Sqrt}[(a_) + (b_)*(x_)^2]/\text{Sqrt}[(c_) + (d_)*(x_)^2], x_Symbol] \text{ :> } \text{Simp}[(\text{Sqrt}[a]*\text{EllipticE}[\text{ArcSin}[\text{Rt}[-(d/c), 2]*x], (b*c)/(a*d)])/(\text{Sqrt}[c]*\text{Rt}[-(d/c), 2]), x] /; \text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NegQ}[d/c] \ \&\& \ \text{GtQ}[c, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1199

$\text{Int}[(d_) + (e_)*(x_)^2/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \text{ :> } \text{Dist}[d/\text{Sqrt}[a], \text{Int}[\text{Sqrt}[1 + (e*x^2)/d]/\text{Sqrt}[1 - (e*x^2)/d], x], x] /; \text{FreeQ}[\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1200

$\text{Int}[(d_) + (e_)*(x_)^2/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \text{ :> } \text{Dist}[\text{Sqrt}[1 + (c*x^4)/a]/\text{Sqrt}[a + c*x^4], \text{Int}[(d + e*x^2)/\text{Sqrt}[1 + (c*x^4)/a], x], x] /; \text{FreeQ}[\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{!GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \sqrt{a+bx}(c+dx)^{3/4} dx &= \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9b} + \frac{(bc-ad) \int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx}{3b} \\
&= \frac{4(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15bd} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9b} - \frac{(2(bc-ad)^2) \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{15bd} \\
&= \frac{4(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15bd} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9b} - \frac{(8(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{u} \sqrt[4]{c+dx}} du \right)}{15bd} \\
&= \frac{4(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15bd} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9b} + \frac{(8(bc-ad)^{5/2}) \text{Subst} \left(\int \frac{1}{\sqrt{u} \sqrt[4]{c+dx}} du \right)}{15bd} \\
&= \frac{4(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15bd} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9b} + \frac{(8(bc-ad)^{5/2} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{u} \sqrt[4]{c+dx}} du \right)}{15bd} \\
&= \frac{4(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15bd} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9b} + \frac{8(bc-ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \text{Erfi} \left(\sqrt{\frac{d(a+bx)}{bc-ad}} \sqrt{c+dx} \right)}{15b^{7/4} d^2} \\
&= \frac{4(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15bd} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9b} - \frac{8(bc-ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \text{Erfi} \left(\sqrt{\frac{d(a+bx)}{bc-ad}} \sqrt{c+dx} \right)}{15b^{7/4} d^2}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.31

$$\frac{2(a+bx)^{3/2}(c+dx)^{3/4} {}_2F_1 \left(-\frac{3}{4}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]*(c + d*x)^(3/4), x]

[Out] (2*(a + b*x)^(3/2)*(c + d*x)^(3/4)*Hypergeometric2F1[-3/4, 3/2, 5/2, (d*(a + b*x))/(-b*c + a*d)])/(3*b*((b*(c + d*x))/(b*c - a*d))^(3/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\sqrt{bx+a}(dx+c)^{\frac{3}{4}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(3/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{3}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(3/4),x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)*(d*x + c)^(3/4), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{3}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)*(d*x+c)^(3/4),x)

[Out] int((b*x+a)^(1/2)*(d*x+c)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{3}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)*(d*x + c)^(3/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \sqrt{a+bx}(c+dx)^{\frac{3}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(1/2)*(c + d*x)^(3/4), x)
```

```
[Out] int((a + b*x)^(1/2)*(c + d*x)^(3/4), x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{a + bx} (c + dx)^{\frac{3}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(1/2)*(d*x+c)**(3/4), x)
```

```
[Out] Integral(sqrt(a + b*x)*(c + d*x)**(3/4), x)
```

$$3.1637 \quad \int \frac{(c+dx)^{3/4}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=196

$$\frac{12(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{5b^{7/4} d \sqrt{a+bx}} + \frac{12(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5b^{7/4} d \sqrt{a+bx}}$$

[Out] $4/5*(d*x+c)^{(3/4)}*(b*x+a)^{(1/2)}/b+12/5*(-a*d+b*c)^{(7/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/d/(b*x+a)^{(1/2)}-12/5*(-a*d+b*c)^{(7/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/d/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.22, antiderivative size = 196, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {50, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{12(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5b^{7/4} d \sqrt{a+bx}} + \frac{12(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5b^{7/4} d \sqrt{a+bx}} + 4\sqrt{a+bx}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(3/4)}/\operatorname{Sqrt}[a + b*x], x]$

[Out] $(4*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)})/(5*b) + (12*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(5*b^{(7/4)}*d*\operatorname{Sqrt}[a + b*x]) - (12*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(5*b^{(7/4)}*d*\operatorname{Sqrt}[a + b*x])$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[p = \operatorname{Denominator}[m]], \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b +$

$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{Simp}[\text{EllipticF}[\text{ArcSin}[(\text{Rt}[-b, 4]*x)/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{NegQ}[b/a] \&\& \text{GtQ}[a, 0]$

Rule 224

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[\text{Sqrt}[1 + (b*x^4)/a]/\text{Sqrt}[a + b*x^4], \text{Int}[1/\text{Sqrt}[1 + (b*x^4)/a], x], x] /; \text{FreeQ}\{a, b\}, x] \&\& \text{NegQ}[b/a] \&\& \text{!GtQ}[a, 0]$

Rule 307

$\text{Int}[(x_)^2/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{With}\{q = \text{Rt}[-(b/a), 2]\}, -\text{Dist}[q^{-1}, \text{Int}[1/\text{Sqrt}[a + b*x^4], x], x] + \text{Dist}[1/q, \text{Int}[(1 + q*x^2)/\text{Sqrt}[a + b*x^4], x], x]] /; \text{FreeQ}\{a, b\}, x] \&\& \text{NegQ}[b/a]$

Rule 424

$\text{Int}[\text{Sqrt}[(a_) + (b_)*(x_)^2]/\text{Sqrt}[(c_) + (d_)*(x_)^2], x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[a]*\text{EllipticE}[\text{ArcSin}[\text{Rt}[-(d/c), 2]*x], (b*c)/(a*d)])/(\text{Sqrt}[c]*\text{Rt}[-(d/c), 2]), x] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NegQ}[d/c] \&\& \text{GtQ}[c, 0] \&\& \text{GtQ}[a, 0]$

Rule 1199

$\text{Int}[(d_) + (e_)*(x_)^2]/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[d/\text{Sqrt}[a], \text{Int}[\text{Sqrt}[1 + (e*x^2)/d]/\text{Sqrt}[1 - (e*x^2)/d], x], x] /; \text{FreeQ}\{a, c, d, e\}, x] \&\& \text{NegQ}[c/a] \&\& \text{EqQ}[c*d^2 + a*e^2, 0] \&\& \text{GtQ}[a, 0]$

Rule 1200

$\text{Int}[(d_) + (e_)*(x_)^2]/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[\text{Sqrt}[1 + (c*x^4)/a]/\text{Sqrt}[a + c*x^4], \text{Int}[(d + e*x^2)/\text{Sqrt}[1 + (c*x^4)/a], x], x] /; \text{FreeQ}\{a, c, d, e\}, x] \&\& \text{NegQ}[c/a] \&\& \text{EqQ}[c*d^2 + a*e^2, 0] \&\& \text{!GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{3/4}}{\sqrt{a+bx}} dx &= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5b} + \frac{(3(bc-ad)) \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{5b} \\
&= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5b} + \frac{(12(bc-ad)) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5bd} \\
&= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5b} - \frac{(12(bc-ad)^{3/2}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5b^{3/2}d} + \frac{(12(bc-ad)^{3/2})}{5b^{3/2}d} \\
&= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5b} - \frac{(12(bc-ad)^{3/2} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{5b^{3/2}d\sqrt{a+bx}} + \frac{(12(bc-ad)^{3/2})}{5b^{3/2}d} \\
&= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5b} - \frac{12(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{5b^{7/4}d\sqrt{a+bx}} + \frac{(12(bc-ad)^{3/2})}{5b^{3/2}d} \\
&= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5b} + \frac{12(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{5b^{7/4}d\sqrt{a+bx}} - \frac{12(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}}}{5b^{7/4}d\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.36

$$\frac{2\sqrt{a+bx}(c+dx)^{3/4} {}_2F_1 \left(-\frac{3}{4}, \frac{1}{2}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/4)/Sqrt[a + b*x], x]

[Out] (2*Sqrt[a + b*x]*(c + d*x)^(3/4)*Hypergeometric2F1[-3/4, 1/2, 3/2, (d*(a + b*x))/(-b*c) + a*d])/(b*((b*(c + d*x))/(b*c - a*d))^(3/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx+c)^{\frac{3}{4}}}{\sqrt{bx+a}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(1/2),x, algorithm="fricas")

[Out] integral((d*x + c)^(3/4)/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(3/4)/sqrt(b*x + a), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/4)/(b*x+a)^(1/2),x)

[Out] int((d*x+c)^(3/4)/(b*x+a)^(1/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(3/4)/sqrt(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{3/4}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(3/4)/(a + b*x)^(1/2), x)

[Out] int((c + d*x)^(3/4)/(a + b*x)^(1/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{3/4}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(3/4)/(b*x+a)**(1/2), x)

[Out] Integral((c + d*x)**(3/4)/sqrt(a + b*x), x)

$$3.1638 \quad \int \frac{(c+dx)^{3/4}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=184

$$\frac{6(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{b^{7/4} \sqrt{a+bx}} + \frac{6(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{b^{7/4} \sqrt{a+bx}}$$

[Out] $-2*(d*x+c)^{(3/4)}/b/(b*x+a)^{(1/2)}+6*(-a*d+b*c)^{(3/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/(b*x+a)^{(1/2)}-6*(-a*d+b*c)^{(3/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.21, antiderivative size = 184, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {47, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{6(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{b^{7/4} \sqrt{a+bx}} + \frac{6(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{b^{7/4} \sqrt{a+bx}} + \frac{2(c+dx)}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(3/4)}/(a + b*x)^{(3/2)}, x]$

[Out] $(-2*(c + d*x)^{(3/4)})/(b*\operatorname{Sqrt}[a + b*x]) + (6*(b*c - a*d)^{(3/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/(b^{(7/4)}*\operatorname{Sqrt}[a + b*x]) - (6*(b*c - a*d)^{(3/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/(b^{(7/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b +$

$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{ :> } \text{Simp}[\text{EllipticF}[\text{ArcSin}[\text{Rt}[-b, 4]*x]/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{GtQ}[a, 0]$

Rule 224

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{ :> } \text{Dist}[\text{Sqrt}[1 + (b*x^4)/a]/\text{Sqrt}[a + b*x^4], \text{Int}[1/\text{Sqrt}[1 + (b*x^4)/a], x], x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{!GtQ}[a, 0]$

Rule 307

$\text{Int}[(x_)^2/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{ :> } \text{With}[\{q = \text{Rt}[-(b/a), 2]\}, -\text{Dist}[q^{(-1)}, \text{Int}[1/\text{Sqrt}[a + b*x^4], x], x] + \text{Dist}[1/q, \text{Int}[(1 + q*x^2)/\text{Sqrt}[a + b*x^4], x], x]] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a]$

Rule 424

$\text{Int}[\text{Sqrt}[(a_) + (b_)*(x_)^2]/\text{Sqrt}[(c_) + (d_)*(x_)^2], x_Symbol] \text{ :> } \text{Simp}[(\text{Sqrt}[a]*\text{EllipticE}[\text{ArcSin}[\text{Rt}[-(d/c), 2]*x], (b*c)/(a*d)])/(\text{Sqrt}[c]*\text{Rt}[-(d/c), 2]), x] /; \text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NegQ}[d/c] \ \&\& \ \text{GtQ}[c, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1199

$\text{Int}[(d_) + (e_)*(x_)^2/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \text{ :> } \text{Dist}[d/\text{Sqrt}[a], \text{Int}[\text{Sqrt}[1 + (e*x^2)/d]/\text{Sqrt}[1 - (e*x^2)/d], x], x] /; \text{FreeQ}[\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1200

$\text{Int}[(d_) + (e_)*(x_)^2/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \text{ :> } \text{Dist}[\text{Sqrt}[1 + (c*x^4)/a]/\text{Sqrt}[a + c*x^4], \text{Int}[(d + e*x^2)/\text{Sqrt}[1 + (c*x^4)/a], x], x] /; \text{FreeQ}[\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{!GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{3/4}}{(a+bx)^{3/2}} dx &= -\frac{2(c+dx)^{3/4}}{b\sqrt{a+bx}} + \frac{(3d) \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{2b} \\
&= -\frac{2(c+dx)^{3/4}}{b\sqrt{a+bx}} + \frac{6 \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{b} \\
&= -\frac{2(c+dx)^{3/4}}{b\sqrt{a+bx}} - \frac{(6\sqrt{bc-ad}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{b^{3/2}} + \frac{(6\sqrt{bc-ad}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{b^{3/2}} \\
&= -\frac{2(c+dx)^{3/4}}{b\sqrt{a+bx}} - \frac{(6\sqrt{bc-ad} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})^d}}} dx, x, \sqrt[4]{c+dx} \right)}{b^{3/2}\sqrt{a+bx}} + \frac{(6\sqrt{bc-ad} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})^d}}} dx, x, \sqrt[4]{c+dx} \right)}{b^{3/2}\sqrt{a+bx}} \\
&= -\frac{2(c+dx)^{3/4}}{b\sqrt{a+bx}} - \frac{6(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{7/4}\sqrt{a+bx}} + \frac{6(bc-ad)^{3/4} \sqrt{\frac{d(a+bx)}{-bc+ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{7/4}\sqrt{a+bx}} \\
&= -\frac{2(c+dx)^{3/4}}{b\sqrt{a+bx}} + \frac{6(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{7/4}\sqrt{a+bx}} - \frac{6(bc-ad)^{3/4} \sqrt{\frac{d(a+bx)}{-bc+ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{7/4}\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.39

$$-\frac{2(c+dx)^{3/4} {}_2F_1 \left(-\frac{3}{4}, -\frac{1}{2}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/4)/(a + b*x)^(3/2), x]

[Out] (-2*(c + d*x)^(3/4)*Hypergeometric2F1[-3/4, -1/2, 1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(3/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{3}{4}}}{b^2x^2 + 2abx + a^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(3/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(3/4)/(b*x + a)^(3/2), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/4)/(b*x+a)^(3/2),x)

[Out] int((d*x+c)^(3/4)/(b*x+a)^(3/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(3/4)/(b*x + a)^(3/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{3/4}}{(a + bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(3/4)/(a + b*x)^(3/2), x)

[Out] int((c + d*x)^(3/4)/(a + b*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{3}{4}}}{(a + bx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(3/4)/(b*x+a)**(3/2), x)

[Out] Integral((c + d*x)**(3/4)/(a + b*x)**(3/2), x)

$$3.1639 \quad \int \frac{(c+dx)^{3/4}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=221

$$\frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{b^{7/4}\sqrt{a+bx}\sqrt[4]{bc-ad}} + \frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{b^{7/4}\sqrt{a+bx}\sqrt[4]{bc-ad}} - \frac{d(c+dx)^{3/4}}{b\sqrt{a+bx}(bc-ad)} - \frac{2(c+dx)^{3/4}}{3b(a+bx)^{3/2}}$$

[Out] $-2/3*(d*x+c)^{(3/4)}/b/(b*x+a)^{(3/2)}-d*(d*x+c)^{(3/4)}/b/(-a*d+b*c)/(b*x+a)^{(1/2)}+d*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/(-a*d+b*c)^{(1/4)}/(b*x+a)^{(1/2)}-d*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/(-a*d+b*c)^{(1/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.24, antiderivative size = 221, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{b^{7/4}\sqrt{a+bx}\sqrt[4]{bc-ad}} + \frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{b^{7/4}\sqrt{a+bx}\sqrt[4]{bc-ad}} - \frac{d(c+dx)^{3/4}}{b\sqrt{a+bx}(bc-ad)} - \frac{2(c+dx)^{3/4}}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(3/4)}/(a + b*x)^{(5/2)}, x]$

[Out] $(-2*(c + d*x)^{(3/4)})/(3*b*(a + b*x)^{(3/2)}) - (d*(c + d*x)^{(3/4)})/(b*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]) + (d*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(b^{(7/4)}*(b*c - a*d)^{(1/4)}*\operatorname{Sqrt}[a + b*x]) - (d*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(b^{(7/4)}*(b*c - a*d)^{(1/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{GtQ}[n, 0] \ \&\& \ \operatorname{LtQ}[m, -1] \ \&\& \ !(\operatorname{IntegerQ}[n] \ \&\& \ !\operatorname{IntegerQ}[m]) \ \&\& \ !(I\operatorname{LeQ}[m + n + 2, 0] \ \&\& \ (\operatorname{FractionQ}[m] \ || \ \operatorname{GeQ}[2*n + m + 1, 0])) \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] :> Dist[Sqrt[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(c + dx)^{3/4}}{(a + bx)^{5/2}} dx &= -\frac{2(c + dx)^{3/4}}{3b(a + bx)^{3/2}} + \frac{d \int \frac{1}{(a+bx)^{3/2} \sqrt[4]{c+dx}} dx}{2b} \\
 &= -\frac{2(c + dx)^{3/4}}{3b(a + bx)^{3/2}} - \frac{d(c + dx)^{3/4}}{b(bc - ad)\sqrt{a + bx}} + \frac{d^2 \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{4b(bc - ad)} \\
 &= -\frac{2(c + dx)^{3/4}}{3b(a + bx)^{3/2}} - \frac{d(c + dx)^{3/4}}{b(bc - ad)\sqrt{a + bx}} + \frac{d \operatorname{Subst} \left(\int \frac{x^2}{\sqrt{a - \frac{bc}{d} + \frac{bx^4}{d}}} dx, x, \sqrt[4]{c + dx} \right)}{b(bc - ad)} \\
 &= -\frac{2(c + dx)^{3/4}}{3b(a + bx)^{3/2}} - \frac{d(c + dx)^{3/4}}{b(bc - ad)\sqrt{a + bx}} - \frac{d \operatorname{Subst} \left(\int \frac{1}{\sqrt{a - \frac{bc}{d} + \frac{bx^4}{d}}} dx, x, \sqrt[4]{c + dx} \right)}{b^{3/2} \sqrt{bc - ad}} + \frac{d \operatorname{Subst} \left(\int \frac{1}{\sqrt{a - \frac{bc}{d} + \frac{bx^4}{d}}} dx, x, \sqrt[4]{c + dx} \right)}{b^{3/2} \sqrt{bc - ad}} \\
 &= -\frac{2(c + dx)^{3/4}}{3b(a + bx)^{3/2}} - \frac{d(c + dx)^{3/4}}{b(bc - ad)\sqrt{a + bx}} - \frac{\left(d \sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1 + \frac{bx^4}{\left(\frac{a-bc}{d}\right)^d}}} dx, x, \sqrt[4]{c + dx} \right)}{b^{3/2} \sqrt{bc - ad} \sqrt{a + bx}} + \frac{\left(d \sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1 + \frac{bx^4}{\left(\frac{a-bc}{d}\right)^d}}} dx, x, \sqrt[4]{c + dx} \right)}{b^{3/2} \sqrt{bc - ad} \sqrt{a + bx}} \\
 &= -\frac{2(c + dx)^{3/4}}{3b(a + bx)^{3/2}} - \frac{d(c + dx)^{3/4}}{b(bc - ad)\sqrt{a + bx}} - \frac{d \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{7/4} \sqrt[4]{bc - ad} \sqrt{a + bx}} + \frac{\left(d \sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1 + \frac{bx^4}{\left(\frac{a-bc}{d}\right)^d}}} dx, x, \sqrt[4]{c + dx} \right)}{b^{3/2} \sqrt{bc - ad} \sqrt{a + bx}} \\
 &= -\frac{2(c + dx)^{3/4}}{3b(a + bx)^{3/2}} - \frac{d(c + dx)^{3/4}}{b(bc - ad)\sqrt{a + bx}} + \frac{d \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{7/4} \sqrt[4]{bc - ad} \sqrt{a + bx}} - \frac{d \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{7/4} \sqrt[4]{bc - ad} \sqrt{a + bx}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.33

$$\frac{2(c + dx)^{3/4} {}_2F_1\left(-\frac{3}{2}, -\frac{3}{4}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a + bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad}\right)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/4)/(a + b*x)^(5/2), x]

[Out] (-2*(c + d*x)^(3/4)*Hypergeometric2F1[-3/2, -3/4, -1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(3/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}}{b^3x^3+3ab^2x^2+3a^2bx+a^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{(bx+a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(5/2), x, algorithm="giac")

[Out] integrate((d*x + c)^(3/4)/(b*x + a)^(5/2), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{(bx+a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/4)/(b*x+a)^(5/2), x)

[Out] `int((d*x+c)^(3/4)/(b*x+a)^(5/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{3}{4}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(3/4)/(b*x+a)^(5/2),x, algorithm="maxima")`

[Out] `integrate((d*x + c)^(3/4)/(b*x + a)^(5/2), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{3/4}}{(a + bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(3/4)/(a + b*x)^(5/2),x)`

[Out] `int((c + d*x)^(3/4)/(a + b*x)^(5/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{3}{4}}}{(a + bx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(3/4)/(b*x+a)**(5/2),x)`

[Out] `Integral((c + d*x)**(3/4)/(a + b*x)**(5/2), x)`

$$3.1640 \quad \int \frac{(c+dx)^{3/4}}{(a+bx)^{7/2}} dx$$

Optimal. Leaf size=270

$$\frac{3d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{10b^{7/4} \sqrt{a+bx} (bc-ad)^{5/4}} - \frac{3d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{10b^{7/4} \sqrt{a+bx} (bc-ad)^{5/4}} + \frac{3d^2 (c+dx)^{3/4}}{10b \sqrt{a+bx} (bc-ad)}$$

[Out] $-2/5*(d*x+c)^{(3/4)}/b/(b*x+a)^{(5/2)}-1/5*d*(d*x+c)^{(3/4)}/b/(-a*d+b*c)/(b*x+a)^{(3/2)}+3/10*d^2*(d*x+c)^{(3/4)}/b/(-a*d+b*c)^2/(b*x+a)^{(1/2)}-3/10*d^2*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/(-a*d+b*c)^{(5/4)}/(b*x+a)^{(1/2)}+3/10*d^2*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(7/4)}/(-a*d+b*c)^{(5/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.28, antiderivative size = 270, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{3d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{10b^{7/4} \sqrt{a+bx} (bc-ad)^{5/4}} - \frac{3d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{10b^{7/4} \sqrt{a+bx} (bc-ad)^{5/4}} + \frac{3d^2 (c+dx)^{3/4}}{10b \sqrt{a+bx} (bc-ad)^2} - \frac{5b}{10b \sqrt{a+bx} (bc-ad)^2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(3/4)}/(a + b*x)^{(7/2)}, x]$

[Out] $(-2*(c + d*x)^{(3/4)})/(5*b*(a + b*x)^{(5/2)}) - (d*(c + d*x)^{(3/4)})/(5*b*(b*c - a*d)*(a + b*x)^{(3/2)}) + (3*d^2*(c + d*x)^{(3/4)})/(10*b*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]) - (3*d^2*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1])/(10*b^{(7/4)}*(b*c - a*d)^{(5/4)}*\operatorname{Sqrt}[a + b*x]) + (3*d^2*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1])/(10*b^{(7/4)}*(b*c - a*d)^{(5/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{IntegerQ}[n] \&\& !\operatorname{IntegerQ}[m]) \&\& !(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid \mid \operatorname{GeQ}[2*n + m + 1, 0])) \& \& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
```


$d, e\}, x] \&\& \text{NegQ}[c/a] \&\& \text{EqQ}[c*d^2 + a*e^2, 0] \&\& \text{GtQ}[a, 0]$

Rule 1200

$\text{Int}[\frac{(d_.) + (e_.)(x_)^2}{\text{Sqrt}[(a_) + (c_.)(x_)^4]}, x_Symbol] \rightarrow \text{Dist}[\text{Sqrt}[1 + (c*x^4)/a]/\text{Sqrt}[a + c*x^4], \text{Int}[(d + e*x^2)/\text{Sqrt}[1 + (c*x^4)/a], x], x]$ /; $\text{FreeQ}[\{a, c, d, e\}, x] \&\& \text{NegQ}[c/a] \&\& \text{EqQ}[c*d^2 + a*e^2, 0] \&\& \text{!GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{3/4}}{(a+bx)^{7/2}} dx &= -\frac{2(c+dx)^{3/4}}{5b(a+bx)^{5/2}} + \frac{(3d) \int \frac{1}{(a+bx)^{5/2} \sqrt[4]{c+dx}} dx}{10b} \\
&= -\frac{2(c+dx)^{3/4}}{5b(a+bx)^{5/2}} - \frac{d(c+dx)^{3/4}}{5b(bc-ad)(a+bx)^{3/2}} - \frac{(3d^2) \int \frac{1}{(a+bx)^{3/2} \sqrt[4]{c+dx}} dx}{20b(bc-ad)} \\
&= -\frac{2(c+dx)^{3/4}}{5b(a+bx)^{5/2}} - \frac{d(c+dx)^{3/4}}{5b(bc-ad)(a+bx)^{3/2}} + \frac{3d^2(c+dx)^{3/4}}{10b(bc-ad)^2 \sqrt{a+bx}} - \frac{(3d^3) \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{40b(bc-ad)^2} \\
&= -\frac{2(c+dx)^{3/4}}{5b(a+bx)^{5/2}} - \frac{d(c+dx)^{3/4}}{5b(bc-ad)(a+bx)^{3/2}} + \frac{3d^2(c+dx)^{3/4}}{10b(bc-ad)^2 \sqrt{a+bx}} - \frac{(3d^2) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d} + \frac{bx^4}{d}}} dx \right)}{10b(bc-ad)^2} \\
&= -\frac{2(c+dx)^{3/4}}{5b(a+bx)^{5/2}} - \frac{d(c+dx)^{3/4}}{5b(bc-ad)(a+bx)^{3/2}} + \frac{3d^2(c+dx)^{3/4}}{10b(bc-ad)^2 \sqrt{a+bx}} + \frac{(3d^2) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d} + \frac{bx^4}{d}}} dx \right)}{10b^{3/2}(bc-ad)} \\
&= -\frac{2(c+dx)^{3/4}}{5b(a+bx)^{5/2}} - \frac{d(c+dx)^{3/4}}{5b(bc-ad)(a+bx)^{3/2}} + \frac{3d^2(c+dx)^{3/4}}{10b(bc-ad)^2 \sqrt{a+bx}} + \frac{(3d^2 \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d} + \frac{bx^4}{d}}} dx \right)}{10b^{3/2}(bc-ad)} \\
&= -\frac{2(c+dx)^{3/4}}{5b(a+bx)^{5/2}} - \frac{d(c+dx)^{3/4}}{5b(bc-ad)(a+bx)^{3/2}} + \frac{3d^2(c+dx)^{3/4}}{10b(bc-ad)^2 \sqrt{a+bx}} + \frac{3d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt{a+bx}}{\sqrt{a-\frac{bc}{d} + \frac{bx^4}{d}}} \right) \right)}{10b^{7/4}(bc-ad)^{5/4}} \\
&= -\frac{2(c+dx)^{3/4}}{5b(a+bx)^{5/2}} - \frac{d(c+dx)^{3/4}}{5b(bc-ad)(a+bx)^{3/2}} + \frac{3d^2(c+dx)^{3/4}}{10b(bc-ad)^2 \sqrt{a+bx}} - \frac{3d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt{a+bx}}{\sqrt{a-\frac{bc}{d} + \frac{bx^4}{d}}} \right) \right)}{10b^{7/4}(bc-ad)^{5/4}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.27

$$-\frac{2(c+dx)^{3/4} {}_2F_1 \left(-\frac{5}{2}, -\frac{3}{4}; -\frac{3}{2}; \frac{d(a+bx)}{ad-bc} \right)}{5b(a+bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(3/4)/(a + b*x)^(7/2), x]

[Out] $(-2*(c + d*x)^{3/4}*\text{Hypergeometric2F1}[-5/2, -3/4, -3/2, (d*(a + b*x))/(-(b*c) + a*d)])/(5*b*(a + b*x)^{5/2}*((b*(c + d*x))/(b*c - a*d))^{3/4})$

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}}{b^4x^4+4ab^3x^3+6a^2b^2x^2+4a^3bx+a^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(7/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(b^4*x^4 + 4*a*b^3*x^3 + 6*a^2*b^2*x^2 + 4*a^3*b*x + a^4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{(bx+a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(7/2), x, algorithm="giac")

[Out] integrate((d*x + c)^(3/4)/(b*x + a)^(7/2), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{(bx+a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(3/4)/(b*x+a)^(7/2), x)

[Out] int((d*x+c)^(3/4)/(b*x+a)^(7/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{3}{4}}}{(bx+a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(3/4)/(b*x+a)^(7/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(3/4)/(b*x + a)^(7/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{3/4}}{(a + bx)^{7/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(3/4)/(a + b*x)^(7/2), x)

[Out] int((c + d*x)^(3/4)/(a + b*x)^(7/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{3}{4}}}{(a + bx)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(3/4)/(b*x+a)**(7/2),x)

[Out] Integral((c + d*x)**(3/4)/(a + b*x)**(7/2), x)

3.1641 $\int (a + bx)^{3/2}(c + dx)^{5/4} dx$

Optimal. Leaf size=220

$$\frac{16(bc - ad)^{17/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{231b^{9/4}d^3\sqrt{a+bx}} - \frac{8\sqrt{a+bx} \sqrt[4]{c+dx} (bc - ad)^3}{231b^2d^2} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{231b^2d}$$

[Out] $4/231*(-a*d+b*c)^2*(b*x+a)^{(3/2)}*(d*x+c)^{(1/4)}/b^2/d+4/33*(-a*d+b*c)*(b*x+a)^{(5/2)}*(d*x+c)^{(1/4)}/b^2+4/15*(b*x+a)^{(5/2)}*(d*x+c)^{(5/4)}/b-8/231*(-a*d+b*c)^3*(d*x+c)^{(1/4)}*(b*x+a)^{(1/2)}/b^2/d^2+16/231*(-a*d+b*c)^{(17/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(9/4)}/d^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.17, antiderivative size = 220, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 224, 221}

$$-\frac{8\sqrt{a+bx} \sqrt[4]{c+dx} (bc - ad)^3}{231b^2d^2} + \frac{16(bc - ad)^{17/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{231b^{9/4}d^3\sqrt{a+bx}} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx} (bc - ad)}{231b^2d}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}*(c + d*x)^{(5/4)}, x]$

[Out] $(-8*(b*c - a*d)^3*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/4)})/(231*b^2*d^2) + (4*(b*c - a*d)^2*(a + b*x)^{(3/2)}*(c + d*x)^{(1/4)})/(231*b^2*d) + (4*(b*c - a*d)*(a + b*x)^{(5/2)}*(c + d*x)^{(1/4)})/(33*b^2) + (4*(a + b*x)^{(5/2)}*(c + d*x)^{(5/4)})/(15*b) + (16*(b*c - a*d)^{(17/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1])/(231*b^{(9/4)}*d^3*\operatorname{Sqrt}[a + b*x])$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[n*(b*c - a*d)/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{NeQ}[m + n + 1, 0] \&\& !(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] || (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m - n, 0]))) \&\& !\operatorname{ILtQ}[m + n + 2, 0] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{With}[p = \operatorname{Denominator}[m], \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b +$

$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{:>} \text{Simp}[\text{EllipticF}[\text{ArcSin}[(\text{Rt}[-b, 4]*x)/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{GtQ}[a, 0]$

Rule 224

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{:>} \text{Dist}[\text{Sqrt}[1 + (b*x^4)/a]/\text{Sqrt}[a + b*x^4], \text{Int}[1/\text{Sqrt}[1 + (b*x^4)/a], x], x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{!GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
 \int (a + bx)^{3/2} (c + dx)^{5/4} dx &= \frac{4(a + bx)^{5/2} (c + dx)^{5/4}}{15b} + \frac{(bc - ad) \int (a + bx)^{3/2} \sqrt[4]{c + dx} dx}{3b} \\
 &= \frac{4(bc - ad)(a + bx)^{5/2} \sqrt[4]{c + dx}}{33b^2} + \frac{4(a + bx)^{5/2} (c + dx)^{5/4}}{15b} + \frac{(bc - ad)^2 \int \frac{(a + bx)^{3/2}}{(c + dx)^{3/4}} dx}{33b^2} \\
 &= \frac{4(bc - ad)^2 (a + bx)^{3/2} \sqrt[4]{c + dx}}{231b^2 d} + \frac{4(bc - ad)(a + bx)^{5/2} \sqrt[4]{c + dx}}{33b^2} + \frac{4(a + bx)^{5/2} (c + dx)^{5/4}}{15b} \\
 &= -\frac{8(bc - ad)^3 \sqrt{a + bx} \sqrt[4]{c + dx}}{231b^2 d^2} + \frac{4(bc - ad)^2 (a + bx)^{3/2} \sqrt[4]{c + dx}}{231b^2 d} + \frac{4(bc - ad)(a + bx)^{5/2} (c + dx)^{5/4}}{33b^2} \\
 &= -\frac{8(bc - ad)^3 \sqrt{a + bx} \sqrt[4]{c + dx}}{231b^2 d^2} + \frac{4(bc - ad)^2 (a + bx)^{3/2} \sqrt[4]{c + dx}}{231b^2 d} + \frac{4(bc - ad)(a + bx)^{5/2} (c + dx)^{5/4}}{33b^2} \\
 &= -\frac{8(bc - ad)^3 \sqrt{a + bx} \sqrt[4]{c + dx}}{231b^2 d^2} + \frac{4(bc - ad)^2 (a + bx)^{3/2} \sqrt[4]{c + dx}}{231b^2 d} + \frac{4(bc - ad)(a + bx)^{5/2} (c + dx)^{5/4}}{33b^2} \\
 &= -\frac{8(bc - ad)^3 \sqrt{a + bx} \sqrt[4]{c + dx}}{231b^2 d^2} + \frac{4(bc - ad)^2 (a + bx)^{3/2} \sqrt[4]{c + dx}}{231b^2 d} + \frac{4(bc - ad)(a + bx)^{5/2} (c + dx)^{5/4}}{33b^2}
 \end{aligned}$$

Mathematica [C] time = 0.07, size = 73, normalized size = 0.33

$$\frac{2(a + bx)^{5/2}(c + dx)^{5/4} {}_2F_1\left(-\frac{5}{4}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc}\right)}{5b\left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)*(c + d*x)^(5/4), x]

[Out] (2*(a + b*x)^(5/2)*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, 5/2, 7/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bdx^2 + ac + (bc + ad)x\right)\sqrt{bx + a}(dx + c)^{\frac{1}{4}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(5/4), x, algorithm="fricas")

[Out] integral((b*d*x^2 + a*c + (b*c + a*d)*x)*sqrt(b*x + a)*(d*x + c)^(1/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(5/4), x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)*(d*x + c)^(5/4), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)*(d*x+c)^(5/4), x)

[Out] int((b*x+a)^(3/2)*(d*x+c)^(5/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)*(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{3/2} (c + dx)^{5/4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)*(c + d*x)^(5/4),x)

[Out] int((a + b*x)^(3/2)*(c + d*x)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{3}{2}} (c + dx)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)*(d*x+c)**(5/4),x)

[Out] Integral((a + b*x)**(3/2)*(c + d*x)**(5/4), x)

3.1642 $\int \sqrt{a + bx} (c + dx)^{5/4} dx$

Optimal. Leaf size=182

$$\frac{40(bc - ad)^{13/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{231b^{9/4}d^2\sqrt{a+bx}} + \frac{20\sqrt{a+bx} \sqrt[4]{c+dx} (bc - ad)^2}{231b^2d} + \frac{20(a+bx)^{3/2} \sqrt[4]{c+dx}}{77b^2}$$

[Out] $20/77*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(1/4)}/b^2+4/11*(b*x+a)^{(3/2)}*(d*x+c)^{(5/4)}/b+20/231*(-a*d+b*c)^2*(d*x+c)^{(1/4)}*(b*x+a)^{(1/2)}/b^2/d-40/231*(-a*d+b*c)^{(13/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a))/(-a*d+b*c)^{(1/2)}/b^{(9/4)}/d^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.10, antiderivative size = 182, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 224, 221}

$$\frac{40(bc - ad)^{13/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{231b^{9/4}d^2\sqrt{a+bx}} + \frac{20\sqrt{a+bx} \sqrt[4]{c+dx} (bc - ad)^2}{231b^2d} + \frac{20(a+bx)^{3/2} \sqrt[4]{c+dx} (bc - ad)}{77b^2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(5/4)}, x]$

[Out] $(20*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/4)})/(231*b^2*d) + (20*(b*c - a*d)*(a + b*x)^{(3/2)}*(c + d*x)^{(1/4)})/(77*b^2) + (4*(a + b*x)^{(3/2)}*(c + d*x)^{(5/4)})/(11*b) - (40*(b*c - a*d)^{(13/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(231*b^{(9/4)}*d^2*\operatorname{Sqrt}[a + b*x])$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{GtQ}[n, 0] \ \&\& \ \operatorname{NeQ}[m + n + 1, 0] \ \&\& \ !(\operatorname{IGtQ}[m, 0] \ \&\& \ (!\operatorname{IntegerQ}[n] \ || \ (\operatorname{GtQ}[m, 0] \ \&\& \ \operatorname{LtQ}[m - n, 0]))) \ \&\& \ !\operatorname{ILtQ}[m + 2, 0] \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[p = \operatorname{Denominator}[m], \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{NeQ}$

`[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 221

`Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]`

Rule 224

`Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]`

Rubi steps

$$\begin{aligned}
 \int \sqrt{a+bx} (c+dx)^{5/4} dx &= \frac{4(a+bx)^{3/2}(c+dx)^{5/4}}{11b} + \frac{(5(bc-ad)) \int \sqrt{a+bx} \sqrt[4]{c+dx} dx}{11b} \\
 &= \frac{20(bc-ad)(a+bx)^{3/2} \sqrt[4]{c+dx}}{77b^2} + \frac{4(a+bx)^{3/2}(c+dx)^{5/4}}{11b} + \frac{(5(bc-ad)^2) \int \frac{\sqrt{a+bx}}{(c+dx)^{3/4}} dx}{77b^2} \\
 &= \frac{20(bc-ad)^2 \sqrt{a+bx} \sqrt[4]{c+dx}}{231b^2d} + \frac{20(bc-ad)(a+bx)^{3/2} \sqrt[4]{c+dx}}{77b^2} + \frac{4(a+bx)^{3/2}(c+dx)^{5/4}}{11b} \\
 &= \frac{20(bc-ad)^2 \sqrt{a+bx} \sqrt[4]{c+dx}}{231b^2d} + \frac{20(bc-ad)(a+bx)^{3/2} \sqrt[4]{c+dx}}{77b^2} + \frac{4(a+bx)^{3/2}(c+dx)^{5/4}}{11b} \\
 &= \frac{20(bc-ad)^2 \sqrt{a+bx} \sqrt[4]{c+dx}}{231b^2d} + \frac{20(bc-ad)(a+bx)^{3/2} \sqrt[4]{c+dx}}{77b^2} + \frac{4(a+bx)^{3/2}(c+dx)^{5/4}}{11b} \\
 &= \frac{20(bc-ad)^2 \sqrt{a+bx} \sqrt[4]{c+dx}}{231b^2d} + \frac{20(bc-ad)(a+bx)^{3/2} \sqrt[4]{c+dx}}{77b^2} + \frac{4(a+bx)^{3/2}(c+dx)^{5/4}}{11b}
 \end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.40

$$\frac{2(a+bx)^{3/2}(c+dx)^{5/4} {}_2F_1\left(-\frac{5}{4}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b\left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]*(c + d*x)^(5/4), x]

[Out] (2*(a + b*x)^(3/2)*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, 3/2, 5/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\sqrt{bx+a}(dx+c)^{\frac{5}{4}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(5/4), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(5/4), x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)*(d*x + c)^(5/4), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)*(d*x+c)^(5/4), x)

[Out] int((b*x+a)^(1/2)*(d*x+c)^(5/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)*(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sqrt{a + bx} (c + dx)^{5/4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)*(c + d*x)^(5/4),x)

[Out] int((a + b*x)^(1/2)*(c + d*x)^(5/4), x)

sympy [A] time = 14.77, size = 218, normalized size = 1.20

$$\frac{2ad(a+bx)^{\frac{3}{2}} {}_2F_1\left(\begin{matrix} -\frac{1}{4}, \frac{3}{2} \\ \frac{5}{2} \end{matrix} \middle| \frac{ade^{i\pi}}{b \operatorname{polar_lift}\left(-\frac{ad}{b} + c\right)} + \frac{dxe^{i\pi}}{\operatorname{polar_lift}\left(-\frac{ad}{b} + c\right)}\right) \sqrt[4]{\operatorname{polar_lift}\left(-\frac{ad}{b} + c\right)} + 2c(a+bx)^{\frac{3}{2}} {}_2F_1\left(\begin{matrix} -\frac{1}{4}, \frac{3}{2} \\ \frac{5}{2} \end{matrix} \middle| \frac{bpe^{i\pi}}{\operatorname{polar_lift}\left(-\frac{ad}{b} + c\right)} + \frac{dxe^{i\pi}}{\operatorname{polar_lift}\left(-\frac{ad}{b} + c\right)}\right) \sqrt[4]{\operatorname{polar_lift}\left(-\frac{ad}{b} + c\right)}}{3b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)*(d*x+c)**(5/4),x)

[Out] -2*a*d*(a + b*x)**(3/2)*hyper((-1/4, 3/2), (5/2,), a*d*exp_polar(I*pi)/(b*polar_lift(-a*d/b + c)) + d*x*exp_polar(I*pi)/polar_lift(-a*d/b + c))*polar_lift(-a*d/b + c)**(1/4)/(3*b**2) + 2*c*(a + b*x)**(3/2)*hyper((-1/4, 3/2), (5/2,), a*d*exp_polar(I*pi)/(b*polar_lift(-a*d/b + c)) + d*x*exp_polar(I*pi)/polar_lift(-a*d/b + c))*polar_lift(-a*d/b + c)**(1/4)/(3*b) + 2*d*(a + b*x)**(5/2)*hyper((-1/4, 5/2), (7/2,), a*d*exp_polar(I*pi)/(b*polar_lift(-a*d/b + c)) + d*x*exp_polar(I*pi)/polar_lift(-a*d/b + c))*polar_lift(-a*d/b + c)**(1/4)/(5*b**2)

$$3.1643 \quad \int \frac{(c+dx)^{5/4}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=144

$$\frac{20(bc-ad)^{9/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{21b^{9/4}d\sqrt{a+bx}} + \frac{20\sqrt{a+bx} \sqrt[4]{c+dx} (bc-ad)}{21b^2} + \frac{4\sqrt{a+bx} (c+dx)^{5/4}}{7b}$$

[Out] 20/21*(-a*d+b*c)*(d*x+c)^(1/4)*(b*x+a)^(1/2)/b^2+4/7*(d*x+c)^(5/4)*(b*x+a)^(1/2)/b+20/21*(-a*d+b*c)^(9/4)*EllipticF(b^(1/4)*(d*x+c)^(1/4)/(-a*d+b*c)^(1/4),I)*(-d*(b*x+a)/(-a*d+b*c))^(1/2)/b^(9/4)/d/(b*x+a)^(1/2)

Rubi [A] time = 0.08, antiderivative size = 144, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 224, 221}

$$\frac{20\sqrt{a+bx} \sqrt[4]{c+dx} (bc-ad)}{21b^2} + \frac{20(bc-ad)^{9/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{21b^{9/4}d\sqrt{a+bx}} + \frac{4\sqrt{a+bx} (c+dx)^{5/4}}{7b}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/4)/Sqrt[a + b*x], x]

[Out] (20*(b*c - a*d)*Sqrt[a + b*x]*(c + d*x)^(1/4))/(21*b^2) + (4*Sqrt[a + b*x]*(c + d*x)^(5/4))/(7*b) + (20*(b*c - a*d)^(9/4)*Sqrt[-((d*(a + b*x))/(b*c - a*d))]*EllipticF[ArcSin[(b^(1/4)*(c + d*x)^(1/4))/(b*c - a*d)^(1/4)], -1])/(21*b^(9/4)*d*Sqrt[a + b*x])

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(c+dx)^{5/4}}{\sqrt{a+bx}} dx &= \frac{4\sqrt{a+bx}(c+dx)^{5/4}}{7b} + \frac{(5(bc-ad)) \int \frac{\sqrt[4]{c+dx}}{\sqrt{a+bx}} dx}{7b} \\
 &= \frac{20(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}}{21b^2} + \frac{4\sqrt{a+bx}(c+dx)^{5/4}}{7b} + \frac{(5(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{21b^2} \\
 &= \frac{20(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}}{21b^2} + \frac{4\sqrt{a+bx}(c+dx)^{5/4}}{7b} + \frac{(20(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx \right)}{21b^2 d} \\
 &= \frac{20(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}}{21b^2} + \frac{4\sqrt{a+bx}(c+dx)^{5/4}}{7b} + \frac{(20(bc-ad)^2 \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1-\frac{bx^4}{d(a+bx)}}} dx \right)}{21b^2 d \sqrt{a+bx}} \\
 &= \frac{20(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}}{21b^2} + \frac{4\sqrt{a+bx}(c+dx)^{5/4}}{7b} + \frac{20(bc-ad)^{9/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b}}{\sqrt[4]{d}} \right) \right)}{21b^{9/4} d \sqrt{a+bx}}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.49

$$\frac{2\sqrt{a+bx}(c+dx)^{5/4} {}_2F_1 \left(-\frac{5}{4}, \frac{1}{2}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/Sqrt[a + b*x], x]

[Out] (2*Sqrt[a + b*x]*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, 1/2, 3/2, (d*(a + b*x))/(-(b*c) + a*d)])/(b*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(dx + c)^{\frac{5}{4}}}{\sqrt{bx + a}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] integral((d*x + c)^(5/4)/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(1/2), x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/sqrt(b*x + a), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(1/2), x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(1/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/sqrt(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{5/4}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(1/2),x)

[Out] int((c + d*x)^(5/4)/(a + b*x)^(1/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{5/4}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/4)/(b*x+a)**(1/2),x)

[Out] Integral((c + d*x)**(5/4)/sqrt(a + b*x), x)

$$3.1644 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=132

$$\frac{10(bc-ad)^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{3b^{9/4} \sqrt{a+bx}} + \frac{10d\sqrt{a+bx} \sqrt[4]{c+dx}}{3b^2} - \frac{2(c+dx)^{5/4}}{b\sqrt{a+bx}}$$

[Out] $-2*(d*x+c)^{(5/4)}/b/(b*x+a)^{(1/2)}+10/3*d*(d*x+c)^{(1/4)}*(b*x+a)^{(1/2)}/b^2+10/3*(-a*d+b*c)^{(5/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(9/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.08, antiderivative size = 132, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 224, 221}

$$\frac{10d\sqrt{a+bx} \sqrt[4]{c+dx}}{3b^2} + \frac{10(bc-ad)^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{3b^{9/4} \sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{b\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c+d*x)^{(5/4)}/(a+b*x)^{(3/2)}, x]$

[Out] $(10*d*\operatorname{Sqrt}[a+b*x]*(c+d*x)^{(1/4)})/(3*b^2) - (2*(c+d*x)^{(5/4)})/(b*\operatorname{Sqrt}[a+b*x]) + (10*(b*c-a*d)^{(5/4)}*\operatorname{Sqrt}[-(d*(a+b*x))/(b*c-a*d)]*\operatorname{EllipticF}[\operatorname{ArcSin}[b^{(1/4)}*(c+d*x)^{(1/4)}/(b*c-a*d)^{(1/4)}], -1])/(3*b^{(9/4)}*\operatorname{Sqrt}[a+b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m+n+2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n+m+1, 0]))$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{NeQ}[m+n+1, 0]$ && $!(\operatorname{IGtQ}$

```
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0])) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{3/2}} dx &= -\frac{2(c+dx)^{5/4}}{b\sqrt{a+bx}} + \frac{(5d) \int \frac{\sqrt[4]{c+dx}}{\sqrt{a+bx}} dx}{2b} \\
&= \frac{10d\sqrt{a+bx} \sqrt[4]{c+dx}}{3b^2} - \frac{2(c+dx)^{5/4}}{b\sqrt{a+bx}} + \frac{(5d(bc-ad)) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{6b^2} \\
&= \frac{10d\sqrt{a+bx} \sqrt[4]{c+dx}}{3b^2} - \frac{2(c+dx)^{5/4}}{b\sqrt{a+bx}} + \frac{(10(bc-ad)) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{3b^2} \\
&= \frac{10d\sqrt{a+bx} \sqrt[4]{c+dx}}{3b^2} - \frac{2(c+dx)^{5/4}}{b\sqrt{a+bx}} + \frac{(10(bc-ad)\sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{3b^2\sqrt{a+bx}} \\
&= \frac{10d\sqrt{a+bx} \sqrt[4]{c+dx}}{3b^2} - \frac{2(c+dx)^{5/4}}{b\sqrt{a+bx}} + \frac{10(bc-ad)^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right) - 1}{3b^{9/4}\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.54

$$\frac{2(c+dx)^{5/4} {}_2F_1 \left(-\frac{5}{4}, -\frac{1}{2}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(3/2), x]

[Out] (-2*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, -1/2, 1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{5}{4}}}{b^2x^2 + 2abx + a^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(3/2),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/4)/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(3/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(3/2), x)

maple [F] time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(3/2),x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(3/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(3/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{5/4}}{(a + bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(3/2),x)

```
[Out] int((c + d*x)^(5/4)/(a + b*x)^(3/2), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/4)/(b*x+a)**(3/2), x)
```

```
[Out] Integral((c + d*x)**(5/4)/(a + b*x)**(3/2), x)
```

$$3.1645 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=135

$$\frac{5d\sqrt[4]{bc-ad}\sqrt{-\frac{d(a+bx)}{bc-ad}}\operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{3b^{9/4}\sqrt{a+bx}} - \frac{5d\sqrt[4]{c+dx}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{3b(a+bx)^{3/2}}$$

[Out] $-2/3*(d*x+c)^{(5/4)}/b/(b*x+a)^{(3/2)}-5/3*d*(d*x+c)^{(1/4)}/b^2/(b*x+a)^{(1/2)}+5/3*d*(-a*d+b*c)^{(1/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(9/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.08, antiderivative size = 135, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 63, 224, 221}

$$-\frac{5d\sqrt[4]{c+dx}}{3b^2\sqrt{a+bx}} + \frac{5d\sqrt[4]{bc-ad}\sqrt{-\frac{d(a+bx)}{bc-ad}}F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)-1}{3b^{9/4}\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{3b(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(5/4)}/(a + b*x)^{(5/2)}, x]$

[Out] $(-5*d*(c + d*x)^{(1/4)}/(3*b^2*\operatorname{Sqrt}[a + b*x]) - (2*(c + d*x)^{(5/4)}/(3*b*(a + b*x)^{(3/2)})) + (5*d*(b*c - a*d)^{(1/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1])/(3*b^{(9/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\}$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{IntegerQ}[m + n + 2, 0])$ && $(\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0])$ && $\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\}$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{LtQ}[-1, m, 0]$ && $\operatorname{LeQ}[-1, n, 0]$ && $\operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]]$

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(c+dx)^{5/4}}{(a+bx)^{5/2}} dx &= -\frac{2(c+dx)^{5/4}}{3b(a+bx)^{3/2}} + \frac{(5d) \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{3/2}} dx}{6b} \\
 &= -\frac{5d\sqrt[4]{c+dx}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{3b(a+bx)^{3/2}} + \frac{(5d^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{12b^2} \\
 &= -\frac{5d\sqrt[4]{c+dx}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{3b(a+bx)^{3/2}} + \frac{(5d) \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{3b^2} \\
 &= -\frac{5d\sqrt[4]{c+dx}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{3b(a+bx)^{3/2}} + \frac{(5d\sqrt{\frac{d(a+bx)}{-bc+ad}}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{3b^2\sqrt{a+bx}} \\
 &= -\frac{5d\sqrt[4]{c+dx}}{3b^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{3b(a+bx)^{3/2}} + \frac{5d\sqrt[4]{bc-ad} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right) - 1}{3b^{9/4}\sqrt{a+bx}}
 \end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.54

$$\frac{2(c+dx)^{5/4} {}_2F_1 \left(-\frac{3}{2}, -\frac{5}{4}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(a+bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(5/2), x]

[Out] (-2*(c + d*x)^(5/4)*Hypergeometric2F1[-3/2, -5/4, -1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{5}{4}}}{b^3x^3+3ab^2x^2+3a^2bx+a^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/4)/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(5/2), x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(5/2), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(5/2), x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(5/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(5/4)/(b*x+a)^(5/2),x, algorithm="maxima")`

[Out] `integrate((d*x + c)^(5/4)/(b*x + a)^(5/2), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{5/4}}{(a + bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(5/4)/(a + b*x)^(5/2),x)`

[Out] `int((c + d*x)^(5/4)/(a + b*x)^(5/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(5/4)/(b*x+a)**(5/2),x)`

[Out] `Integral((c + d*x)**(5/4)/(a + b*x)**(5/2), x)`

$$3.1646 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{7/2}} dx$$

Optimal. Leaf size=175

$$\frac{d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{6b^{9/4} \sqrt{a+bx} (bc-ad)^{3/4}} - \frac{d^2 \sqrt[4]{c+dx}}{6b^2 \sqrt{a+bx} (bc-ad)} - \frac{d \sqrt[4]{c+dx}}{3b^2 (a+bx)^{3/2}} - \frac{2(c+dx)^{5/4}}{5b(a+bx)^{5/2}}$$

[Out] $-1/3*d*(d*x+c)^{(1/4)}/b^2/(b*x+a)^{(3/2)}-2/5*(d*x+c)^{(5/4)}/b/(b*x+a)^{(5/2)}-1/6*d^2*(d*x+c)^{(1/4)}/b^2/(-a*d+b*c)/(b*x+a)^{(1/2)}-1/6*d^2*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(9/4)}/(-a*d+b*c)^{(3/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.10, antiderivative size = 175, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 51, 63, 224, 221}

$$\frac{d^2 \sqrt[4]{c+dx}}{6b^2 \sqrt{a+bx} (bc-ad)} - \frac{d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{6b^{9/4} \sqrt{a+bx} (bc-ad)^{3/4}} - \frac{d \sqrt[4]{c+dx}}{3b^2 (a+bx)^{3/2}} - \frac{2(c+dx)^{5/4}}{5b(a+bx)^{5/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(5/4)}/(a + b*x)^{(7/2)}, x]$

[Out] $-(d*(c + d*x)^{(1/4)})/(3*b^2*(a + b*x)^{(3/2)}) - (d^2*(c + d*x)^{(1/4)})/(6*b^2*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]) - (2*(c + d*x)^{(5/4)})/(5*b*(a + b*x)^{(5/2)}) - (d^2*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/(6*b^{(9/4)}*(b*c - a*d)^{(3/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{IntegerQ}[n] \&\& !\operatorname{IntegerQ}[m]) \&\& !(I\operatorname{LeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0])) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*(m + n + 2)]/((b*c - a*d)*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^n, x], x$

```
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{7/2}} dx &= -\frac{2(c+dx)^{5/4}}{5b(a+bx)^{5/2}} + \frac{d \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{5/2}} dx}{2b} \\
&= -\frac{d\sqrt[4]{c+dx}}{3b^2(a+bx)^{3/2}} - \frac{2(c+dx)^{5/4}}{5b(a+bx)^{5/2}} + \frac{d^2 \int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/4}} dx}{12b^2} \\
&= -\frac{d\sqrt[4]{c+dx}}{3b^2(a+bx)^{3/2}} - \frac{d^2\sqrt[4]{c+dx}}{6b^2(bc-ad)\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{5b(a+bx)^{5/2}} - \frac{d^3 \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{24b^2(bc-ad)} \\
&= -\frac{d\sqrt[4]{c+dx}}{3b^2(a+bx)^{3/2}} - \frac{d^2\sqrt[4]{c+dx}}{6b^2(bc-ad)\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{5b(a+bx)^{5/2}} - \frac{d^2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{6b^2(bc-ad)} \\
&= -\frac{d\sqrt[4]{c+dx}}{3b^2(a+bx)^{3/2}} - \frac{d^2\sqrt[4]{c+dx}}{6b^2(bc-ad)\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{5b(a+bx)^{5/2}} - \frac{\left(d^2 \sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)d}}} dx, x, \sqrt[4]{c+dx} \right)}{6b^2(bc-ad)\sqrt{a+bx}} \\
&= -\frac{d\sqrt[4]{c+dx}}{3b^2(a+bx)^{3/2}} - \frac{d^2\sqrt[4]{c+dx}}{6b^2(bc-ad)\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{5b(a+bx)^{5/2}} - \frac{d^2 \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right)}{6b^{9/4}(bc-ad)^{3/4}\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.42

$$\frac{2(c+dx)^{5/4} {}_2F_1 \left(-\frac{5}{2}, -\frac{5}{4}; -\frac{3}{2}; \frac{d(a+bx)}{ad-bc} \right)}{5b(a+bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(7/2), x]

[Out] (-2*(c + d*x)^(5/4)*Hypergeometric2F1[-5/2, -5/4, -3/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.52, size = 0, normalized size = 0.00

$$\operatorname{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{5/4}}{b^4x^4 + 4ab^3x^3 + 6a^2b^2x^2 + 4a^3bx + a^4}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(7/2),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/4)/(b^4*x^4 + 4*a*b^3*x^3 + 6*a^2*b^2*x^2 + 4*a^3*b*x + a^4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(7/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(7/2), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(7/2),x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(7/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(7/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(7/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/4)/(a + b*x)^(7/2), x)
```

```
[Out] int((c + d*x)^(5/4)/(a + b*x)^(7/2), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/4)/(b*x+a)**(7/2), x)
```

```
[Out] Integral((c + d*x)**(5/4)/(a + b*x)**(7/2), x)
```

$$3.1647 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{9/2}} dx$$

Optimal. Leaf size=213

$$\frac{5d^3 \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{84b^{9/4} \sqrt{a+bx} (bc-ad)^{7/4}} + \frac{5d^3 \sqrt[4]{c+dx}}{84b^2 \sqrt{a+bx} (bc-ad)^2} - \frac{d^2 \sqrt[4]{c+dx}}{42b^2 (a+bx)^{3/2} (bc-ad)} - \frac{d \sqrt[4]{c+dx}}{7b^2 (a+bx)^{5/2}} - \frac{2}{7b^2}$$

[Out] $-1/7*d*(d*x+c)^{(1/4)}/b^2/(b*x+a)^{(5/2)}-1/42*d^2*(d*x+c)^{(1/4)}/b^2/(-a*d+b*c)/(b*x+a)^{(3/2)}-2/7*(d*x+c)^{(5/4)}/b/(b*x+a)^{(7/2)}+5/84*d^3*(d*x+c)^{(1/4)}/b^2/(-a*d+b*c)^2/(b*x+a)^{(1/2)}+5/84*d^3*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(9/4)}/(-a*d+b*c)^{(7/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.12, antiderivative size = 213, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 51, 63, 224, 221}

$$\frac{5d^3 \sqrt[4]{c+dx}}{84b^2 \sqrt{a+bx} (bc-ad)^2} - \frac{d^2 \sqrt[4]{c+dx}}{42b^2 (a+bx)^{3/2} (bc-ad)} + \frac{5d^3 \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{84b^{9/4} \sqrt{a+bx} (bc-ad)^{7/4}} - \frac{d \sqrt[4]{c+dx}}{7b^2 (a+bx)^{5/2}} - \frac{2}{7b^2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(5/4)}/(a + b*x)^{(9/2)}, x]$

[Out] $-(d*(c + d*x)^{(1/4)})/(7*b^2*(a + b*x)^{(5/2)}) - (d^2*(c + d*x)^{(1/4)})/(42*b^2*(b*c - a*d)*(a + b*x)^{(3/2)}) + (5*d^3*(c + d*x)^{(1/4)})/(84*b^2*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]) - (2*(c + d*x)^{(5/4)})/(7*b*(a + b*x)^{(7/2)}) + (5*d^3*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(84*b^{(9/4)}*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\}$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}]/((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*($

```

m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]

```

Rule 63

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 221

```

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] :> Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]

```

Rule 224

```

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] :> Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]

```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{9/2}} dx &= -\frac{2(c+dx)^{5/4}}{7b(a+bx)^{7/2}} + \frac{(5d) \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{7/2}} dx}{14b} \\
&= -\frac{d\sqrt[4]{c+dx}}{7b^2(a+bx)^{5/2}} - \frac{2(c+dx)^{5/4}}{7b(a+bx)^{7/2}} + \frac{d^2 \int \frac{1}{(a+bx)^{5/2}(c+dx)^{3/4}} dx}{28b^2} \\
&= -\frac{d\sqrt[4]{c+dx}}{7b^2(a+bx)^{5/2}} - \frac{d^2\sqrt[4]{c+dx}}{42b^2(bc-ad)(a+bx)^{3/2}} - \frac{2(c+dx)^{5/4}}{7b(a+bx)^{7/2}} - \frac{(5d^3) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/4}} dx}{168b^2(bc-ad)} \\
&= -\frac{d\sqrt[4]{c+dx}}{7b^2(a+bx)^{5/2}} - \frac{d^2\sqrt[4]{c+dx}}{42b^2(bc-ad)(a+bx)^{3/2}} + \frac{5d^3\sqrt[4]{c+dx}}{84b^2(bc-ad)^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{7b(a+bx)^{7/2}} + \dots \\
&= -\frac{d\sqrt[4]{c+dx}}{7b^2(a+bx)^{5/2}} - \frac{d^2\sqrt[4]{c+dx}}{42b^2(bc-ad)(a+bx)^{3/2}} + \frac{5d^3\sqrt[4]{c+dx}}{84b^2(bc-ad)^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{7b(a+bx)^{7/2}} + \dots \\
&= -\frac{d\sqrt[4]{c+dx}}{7b^2(a+bx)^{5/2}} - \frac{d^2\sqrt[4]{c+dx}}{42b^2(bc-ad)(a+bx)^{3/2}} + \frac{5d^3\sqrt[4]{c+dx}}{84b^2(bc-ad)^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{7b(a+bx)^{7/2}} + \dots \\
&= -\frac{d\sqrt[4]{c+dx}}{7b^2(a+bx)^{5/2}} - \frac{d^2\sqrt[4]{c+dx}}{42b^2(bc-ad)(a+bx)^{3/2}} + \frac{5d^3\sqrt[4]{c+dx}}{84b^2(bc-ad)^2\sqrt{a+bx}} - \frac{2(c+dx)^{5/4}}{7b(a+bx)^{7/2}} + \dots
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.34

$$\frac{2(c+dx)^{5/4} {}_2F_1\left(-\frac{7}{2}, -\frac{5}{4}; -\frac{5}{2}; \frac{d(a+bx)}{ad-bc}\right)}{7b(a+bx)^{7/2} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(9/2), x]

[Out] (-2*(c + d*x)^(5/4)*Hypergeometric2F1[-7/2, -5/4, -5/2, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*(a + b*x)^(7/2)*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.56, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{5}{4}}}{b^5x^5+5ab^4x^4+10a^2b^3x^3+10a^3b^2x^2+5a^4bx+a^5}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(9/2),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/4)/(b^5*x^5 + 5*a*b^4*x^4 + 10*a^2*b^3*x^3 + 10*a^3*b^2*x^2 + 5*a^4*b*x + a^5), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{9}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(9/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(9/2), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{9}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(9/2),x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(9/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{9}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(9/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(9/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{5/4}}{(a + bx)^{9/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(5/4)/(a + b*x)^(9/2), x)`

[Out] `int((c + d*x)^(5/4)/(a + b*x)^(9/2), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(5/4)/(b*x+a)**(9/2), x)`

[Out] Timed out

$$3.1648 \quad \int \frac{(a+bx)^{5/2}}{\sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=264

$$\frac{32(bc-ad)^{15/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{39b^{3/4}d^4\sqrt{a+bx}} - \frac{32(bc-ad)^{15/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{39b^{3/4}d^4\sqrt{a+bx}}$$

[Out] $-40/117*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(3/4)}/d^2+4/13*(b*x+a)^{(5/2)}*(d*x+c)^{(3/4)}/d+16/39*(-a*d+b*c)^2*(d*x+c)^{(3/4)}*(b*x+a)^{(1/2)}/d^3-32/39*(-a*d+b*c)^{(15/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(3/4)}/d^4/(b*x+a)^{(1/2)}+32/39*(-a*d+b*c)^{(15/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(3/4)}/d^4/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.30, antiderivative size = 264, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {50, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{32(bc-ad)^{15/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{39b^{3/4}d^4\sqrt{a+bx}} - \frac{32(bc-ad)^{15/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{39b^{3/4}d^4\sqrt{a+bx}} + \frac{16\sqrt{a+bx}}{39b^{3/4}d^4}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}/(c + d*x)^{(1/4)}, x]$

[Out] $(16*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)})/(39*d^3) - (40*(b*c - a*d)*(a + b*x)^{(3/2)}*(c + d*x)^{(3/4)})/(117*d^2) + (4*(a + b*x)^{(5/2)}*(c + d*x)^{(3/4)})/(13*d) - (32*(b*c - a*d)^{(15/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(39*b^{(3/4)}*d^4*\operatorname{Sqrt}[a + b*x]) + (32*(b*c - a*d)^{(15/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(39*b^{(3/4)}*d^4*\operatorname{Sqrt}[a + b*x])$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)], \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /; \operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{GtQ}[n, 0] \ \&\& \operatorname{NeQ}[m+n+1, 0] \ \&\& \operatorname{!(IGtQ}[m, 0] \ \&\& \operatorname{!(IntegerQ}[n] \ \|\ (\operatorname{GtQ}[m, 0] \ \&\& \operatorname{LtQ}[m-n, 0])) \ \&\& \operatorname{!ILtQ}[m+n+2, 0] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt
[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x
] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[
a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{\sqrt[4]{c+dx}} dx &= \frac{4(a+bx)^{5/2}(c+dx)^{3/4}}{13d} - \frac{(10(bc-ad)) \int \frac{(a+bx)^{3/2}}{\sqrt[4]{c+dx}} dx}{13d} \\
&= -\frac{40(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}}{117d^2} + \frac{4(a+bx)^{5/2}(c+dx)^{3/4}}{13d} + \frac{(20(bc-ad)^2) \int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx}{39d^2} \\
&= \frac{16(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}}{39d^3} - \frac{40(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}}{117d^2} + \frac{4(a+bx)^{5/2}(c+dx)^{3/4}}{13d} \\
&= \frac{16(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}}{39d^3} - \frac{40(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}}{117d^2} + \frac{4(a+bx)^{5/2}(c+dx)^{3/4}}{13d} \\
&= \frac{16(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}}{39d^3} - \frac{40(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}}{117d^2} + \frac{4(a+bx)^{5/2}(c+dx)^{3/4}}{13d} \\
&= \frac{16(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}}{39d^3} - \frac{40(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}}{117d^2} + \frac{4(a+bx)^{5/2}(c+dx)^{3/4}}{13d} \\
&= \frac{16(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}}{39d^3} - \frac{40(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}}{117d^2} + \frac{4(a+bx)^{5/2}(c+dx)^{3/4}}{13d} \\
&= \frac{16(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}}{39d^3} - \frac{40(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}}{117d^2} + \frac{4(a+bx)^{5/2}(c+dx)^{3/4}}{13d} \\
&= \frac{16(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}}{39d^3} - \frac{40(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}}{117d^2} + \frac{4(a+bx)^{5/2}(c+dx)^{3/4}}{13d}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.28

$$\frac{2(a+bx)^{7/2} \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{4}, \frac{7}{2}; \frac{9}{2}; \frac{d(a+bx)}{ad-bc}\right)}{7b \sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/(c + d*x)^(1/4), x]

[Out] (2*(a + b*x)^(7/2)*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[1/4, 7/2, 9/2, (d*(a + b*x))/(-(b*c) + a*d)])/(7*b*(c + d*x)^(1/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(b^2x^2 + 2abx + a^2)\sqrt{bx + a}}{(dx + c)^{\frac{1}{4}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(1/4), x, algorithm="fricas")

[Out] integral((b^2*x^2 + 2*a*b*x + a^2)*sqrt(b*x + a)/(d*x + c)^(1/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(1/4), x, algorithm="giac")

[Out] integrate((b*x + a)^(5/2)/(d*x + c)^(1/4), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/(d*x+c)^(1/4), x)

[Out] int((b*x+a)^(5/2)/(d*x+c)^(1/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/2)/(d*x + c)^(1/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{5/2}}{(c + dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)/(c + d*x)^(1/4),x)

[Out] int((a + b*x)^(5/2)/(c + d*x)^(1/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{5/2}}{\sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)/(d*x+c)**(1/4),x)

[Out] Integral((a + b*x)**(5/2)/(c + d*x)**(1/4), x)

$$3.1649 \quad \int \frac{(a+bx)^{3/2}}{\sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=229

$$\frac{16(bc-ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{15b^{3/4}d^3 \sqrt{a+bx}} + \frac{16(bc-ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{15b^{3/4}d^3 \sqrt{a+bx}}$$

[Out] $4/9*(b*x+a)^{(3/2)}*(d*x+c)^{(3/4)}/d-8/15*(-a*d+b*c)*(d*x+c)^{(3/4)}*(b*x+a)^{(1/2)}/d^2+16/15*(-a*d+b*c)^{(11/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(3/4)}/d^3/(b*x+a)^{(1/2)}-16/15*(-a*d+b*c)^{(11/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(3/4)}/d^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.24, antiderivative size = 229, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {50, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{16(bc-ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{15b^{3/4}d^3 \sqrt{a+bx}} + \frac{16(bc-ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{15b^{3/4}d^3 \sqrt{a+bx}} - 8\sqrt{a}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}/(c + d*x)^{(1/4)}, x]$

[Out] $(-8*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)})/(15*d^2) + (4*(a + b*x)^{(3/2)}*(c + d*x)^{(3/4)})/(9*d) + (16*(b*c - a*d)^{(11/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(15*b^{(3/4)}*d^3*\operatorname{Sqrt}[a + b*x]) - (16*(b*c - a*d)^{(11/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(15*b^{(3/4)}*d^3*\operatorname{Sqrt}[a + b*x])$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{GtQ}[n, 0] \ \&\& \operatorname{NeQ}[m + n + 1, 0] \ \&\& \operatorname{!(IGtQ}[m, 0] \ \&\& \operatorname{!(IntegerQ}[n] \ \|\ (\operatorname{GtQ}[m, 0] \ \&\& \operatorname{LtQ}[m - n, 0])) \ \&\& \operatorname{!ILtQ}[m + n + 2, 0] \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)]/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt
[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x
] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[
a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{\sqrt[4]{c+dx}} dx &= \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9d} - \frac{(2(bc-ad)) \int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx}{3d} \\
&= -\frac{8(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^2} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9d} + \frac{(4(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}\sqrt[4]{c+dx}} dx}{15d^2} \\
&= -\frac{8(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^2} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9d} + \frac{(16(bc-ad)^2) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+x}} \right)}{15d^3} \\
&= -\frac{8(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^2} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9d} - \frac{(16(bc-ad)^{5/2}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}}} \right)}{15\sqrt{b}d^3} \\
&= -\frac{8(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^2} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9d} - \frac{(16(bc-ad)^{5/2} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}}} \right)}{15\sqrt{b}d^3} \\
&= -\frac{8(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^2} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9d} - \frac{16(bc-ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt{a+bx}}{\sqrt{a-\frac{bc}{d}}} \right) \right)}{15b^{3/4}d^3\sqrt{a+bx}} \\
&= -\frac{8(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^2} + \frac{4(a+bx)^{3/2}(c+dx)^{3/4}}{9d} + \frac{16(bc-ad)^{11/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt{a+bx}}{\sqrt{a-\frac{bc}{d}}} \right) \right)}{15b^{3/4}d^3\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.32

$$\frac{2(a+bx)^{5/2} \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(\frac{1}{4}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc} \right)}{5b\sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(1/4), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[1/4, 5/2, 7/2, (d*(a + b*x))/(-b*c + a*d)]/(5*b*(c + d*x)^(1/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{1}{4}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)/(d*x + c)^(1/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(1/4), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(1/4),x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(1/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{3/2}}{(c + dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/(c + d*x)^(1/4), x)

[Out] int((a + b*x)^(3/2)/(c + d*x)^(1/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{\sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/(d*x+c)**(1/4), x)

[Out] Integral((a + b*x)**(3/2)/(c + d*x)**(1/4), x)

$$3.1650 \quad \int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=196

$$\frac{8(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{5b^{3/4}d^2\sqrt{a+bx}} - \frac{8(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{5b^{3/4}d^2\sqrt{a+bx}} + \frac{4\sqrt{a+bx}}{5a}$$

[Out] $4/5*(d*x+c)^{(3/4)}*(b*x+a)^{(1/2)}/d-8/5*(-a*d+b*c)^{(7/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(3/4)}/d^2/(b*x+a)^{(1/2)}+8/5*(-a*d+b*c)^{(7/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(3/4)}/d^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.22, antiderivative size = 196, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {50, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{8(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{5b^{3/4}d^2\sqrt{a+bx}} - \frac{8(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{5b^{3/4}d^2\sqrt{a+bx}} + \frac{4\sqrt{a+bx}}{5a}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[\operatorname{Sqrt}[a + b*x]/(c + d*x)^{(1/4)}, x]$

[Out] $(4*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)})/(5*d) - (8*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1)/(5*b^{(3/4)}*d^2*\operatorname{Sqrt}[a + b*x]) + (8*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1)/(5*b^{(3/4)}*d^2*\operatorname{Sqrt}[a + b*x])$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{NeQ}[m + n + 1, 0]$ && $!(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] \mid\mid (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m - n, 0])))$ && $!\operatorname{ILtQ}[m + n + 2, 0]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b +$

$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{Simp}[\text{EllipticF}[\text{ArcSin}[(\text{Rt}[-b, 4]*x)/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{GtQ}[a, 0]$

Rule 224

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[\text{Sqrt}[1 + (b*x^4)/a]/\text{Sqrt}[a + b*x^4], \text{Int}[1/\text{Sqrt}[1 + (b*x^4)/a], x], x] /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{!GtQ}[a, 0]$

Rule 307

$\text{Int}[(x_)^2/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{With}\{q = \text{Rt}[-(b/a), 2]\}, -\text{Dist}[q^{-1}, \text{Int}[1/\text{Sqrt}[a + b*x^4], x], x] + \text{Dist}[1/q, \text{Int}[(1 + q*x^2)/\text{Sqrt}[a + b*x^4], x], x]] /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a]$

Rule 424

$\text{Int}[\text{Sqrt}[(a_) + (b_)*(x_)^2]/\text{Sqrt}[(c_) + (d_)*(x_)^2], x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[a]*\text{EllipticE}[\text{ArcSin}[\text{Rt}[-(d/c), 2]*x], (b*c)/(a*d)])/(\text{Sqrt}[c]*\text{Rt}[-(d/c), 2]), x] /; \text{FreeQ}\{a, b, c, d\}, x] \ \&\& \ \text{NegQ}[d/c] \ \&\& \ \text{GtQ}[c, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1199

$\text{Int}[(d_) + (e_)*(x_)^2]/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[d/\text{Sqrt}[a], \text{Int}[\text{Sqrt}[1 + (e*x^2)/d]/\text{Sqrt}[1 - (e*x^2)/d], x], x] /; \text{FreeQ}\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1200

$\text{Int}[(d_) + (e_)*(x_)^2]/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[\text{Sqrt}[1 + (c*x^4)/a]/\text{Sqrt}[a + c*x^4], \text{Int}[(d + e*x^2)/\text{Sqrt}[1 + (c*x^4)/a], x], x] /; \text{FreeQ}\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{!GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx &= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5d} - \frac{(2(bc-ad)) \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{5d} \\
&= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5d} - \frac{(8(bc-ad)) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d^2} \\
&= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5d} + \frac{(8(bc-ad)^{3/2}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5\sqrt{b}d^2} - \frac{(8(bc-ad)^{3/2}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5\sqrt{b}d^2} \\
&= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5d} + \frac{(8(bc-ad)^{3/2} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{5\sqrt{b}d^2\sqrt{a+bx}} - \frac{(8(bc-ad)^{3/2} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{5\sqrt{b}d^2\sqrt{a+bx}} \\
&= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5d} + \frac{8(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{5b^{3/4}d^2\sqrt{a+bx}} - \frac{(8(bc-ad)^{3/2} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{5\sqrt{b}d^2\sqrt{a+bx}} \\
&= \frac{4\sqrt{a+bx}(c+dx)^{3/4}}{5d} - \frac{8(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{5b^{3/4}d^2\sqrt{a+bx}} + \frac{8(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{5b^{3/4}d^2\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.37

$$\frac{2(a+bx)^{3/2} \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(\frac{1}{4}, \frac{3}{2}, \frac{5}{2}, \frac{d(a+bx)}{ad-bc} \right)}{3b \sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(1/4), x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[1/4, 3/2, 5/2, (d*(a + b*x))/(-b*c + a*d)]/(3*b*(c + d*x)^(1/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{4}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)/(d*x + c)^(1/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(1/4), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(1/4),x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(1/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(1/2)/(c + d*x)^(1/4),x)
```

```
[Out] int((a + b*x)^(1/2)/(c + d*x)^(1/4), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{\sqrt{a + bx}}{\sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(1/2)/(d*x+c)**(1/4),x)
```

```
[Out] Integral(sqrt(a + b*x)/(c + d*x)**(1/4), x)
```

$$3.1651 \quad \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=167

$$\frac{4(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{b^{3/4} d \sqrt{a+bx}} - \frac{4(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \text{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{b^{3/4} d \sqrt{a+bx}}$$

[Out] 4*(-a*d+b*c)^(3/4)*EllipticE(b^(1/4)*(d*x+c)^(1/4)/(-a*d+b*c)^(1/4),I)*(-d*(b*x+a)/(-a*d+b*c))^(1/2)/b^(3/4)/d/(b*x+a)^(1/2)-4*(-a*d+b*c)^(3/4)*EllipticF(b^(1/4)*(d*x+c)^(1/4)/(-a*d+b*c)^(1/4),I)*(-d*(b*x+a)/(-a*d+b*c))^(1/2)/b^(3/4)/d/(b*x+a)^(1/2)

Rubi [A] time = 0.19, antiderivative size = 167, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 7, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.368$, Rules used = {63, 307, 224, 221, 1200, 1199, 424}

$$\frac{4(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{b^{3/4} d \sqrt{a+bx}} - \frac{4(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{b^{3/4} d \sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(1/4)),x]

[Out] (4*(b*c - a*d)^(3/4)*Sqrt[-((d*(a + b*x))/(b*c - a*d))]*EllipticE[ArcSin[(b^(1/4)*(c + d*x)^(1/4))/(b*c - a*d)^(1/4)], -1])/(b^(3/4)*d*Sqrt[a + b*x]) - (4*(b*c - a*d)^(3/4)*Sqrt[-((d*(a + b*x))/(b*c - a*d))]*EllipticF[ArcSin[(b^(1/4)*(c + d*x)^(1/4))/(b*c - a*d)^(1/4)], -1])/(b^(3/4)*d*Sqrt[a + b*x])

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)]/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt
[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x
] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[
a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx &= \frac{4 \operatorname{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{d} \\
&= -\frac{(4\sqrt{bc-ad}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b}d} + \frac{(4\sqrt{bc-ad}) \operatorname{Subst} \left(\int \frac{1+\frac{\sqrt{b}x}{\sqrt{bc-d}}}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b}d} \\
&= -\frac{(4\sqrt{bc-ad} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b}d\sqrt{a+bx}} + \frac{(4\sqrt{bc-ad} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \operatorname{Subst} \left(\int \frac{1+\frac{\sqrt{b}x}{\sqrt{bc-d}}}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b}d\sqrt{a+bx}} \\
&= -\frac{4(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{3/4}d\sqrt{a+bx}} + \frac{(4\sqrt{bc-ad} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \operatorname{Subst} \left(\int \frac{1+\frac{\sqrt{b}x}{\sqrt{bc-d}}}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b}d\sqrt{a+bx}} \\
&= \frac{4(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{3/4}d\sqrt{a+bx}} - \frac{4(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{b^{3/4}d\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.43

$$\frac{2\sqrt{a+bx} \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(\frac{1}{4}, \frac{1}{2}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b^4 \sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(1/4)), x]

[Out] (2*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[1/4, 1/2, 3/2, (d*(a + b*x))/(-b*c + a*d)]/(b*(c + d*x)^(1/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\operatorname{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{3}{4}}}{bdx^2+ac+(bc+ad)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(1/4)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(1/4),x)

[Out] int(1/(b*x+a)^(1/2)/(d*x+c)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/2)*(c + d*x)^(1/4)),x)

```
[Out] int(1/((a + b*x)^(1/2)*(c + d*x)^(1/4)), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{1}{\sqrt{a + bx} \sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(1/2)/(d*x+c)**(1/4), x)
```

```
[Out] Integral(1/(sqrt(a + b*x)*(c + d*x)**(1/4)), x)
```

$$3.1652 \quad \int \frac{1}{(a+bx)^{3/2} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=191

$$\frac{2\sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{b^{3/4}\sqrt{a+bx}\sqrt[4]{bc-ad}} + \frac{2\sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{b^{3/4}\sqrt{a+bx}\sqrt[4]{bc-ad}} - \frac{2(c+dx)^{3/4}}{\sqrt{a+bx}(bc-ad)}$$

[Out] $-2*(d*x+c)^{(3/4)/(-a*d+b*c)/(b*x+a)^{(1/2)+2*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(3/4)/(-a*d+b*c)^{(1/4)}/(b*x+a)^{(1/2)-2*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(3/4)/(-a*d+b*c)^{(1/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.22, antiderivative size = 191, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{2\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{b^{3/4}\sqrt{a+bx}\sqrt[4]{bc-ad}} + \frac{2\sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{b^{3/4}\sqrt{a+bx}\sqrt[4]{bc-ad}} - \frac{2(c+dx)^{3/4}}{\sqrt{a+bx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a + b*x)^{(3/2)}*(c + d*x)^{(1/4))}, x]$

[Out] $(-2*(c + d*x)^{(3/4))/((b*c - a*d)*\operatorname{Sqrt}[a + b*x]) + (2*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/ (b^{(3/4)}*(b*c - a*d)^{(1/4)}*\operatorname{Sqrt}[a + b*x]) - (2*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/ (b^{(3/4)}*(b*c - a*d)^{(1/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] :> \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}]/((b*c - a*d)*(m + 1)), x] - \operatorname{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x], x] /; \operatorname{FreeQ}\{a, b, c, d, n\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{LtQ}[n, -1] \&\& (\operatorname{EqQ}[a, 0] \mid\mid (\operatorname{NeQ}[c, 0] \&\& \operatorname{LtQ}[m - n, 0] \&\& \operatorname{IntegerQ}[n]))) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] :> \operatorname{With}[p = \operatorname{Denominator}[m]], \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b +$

$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{Simp}[\text{EllipticF}[\text{ArcSin}[(\text{Rt}[-b, 4]*x)/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{GtQ}[a, 0]$

Rule 224

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[\text{Sqrt}[1 + (b*x^4)/a]/\text{Sqrt}[a + b*x^4], \text{Int}[1/\text{Sqrt}[1 + (b*x^4)/a], x], x] /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ !\text{GtQ}[a, 0]$

Rule 307

$\text{Int}[(x_)^2/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{With}\{q = \text{Rt}[-(b/a), 2]\}, -\text{Dist}[q^{-1}, \text{Int}[1/\text{Sqrt}[a + b*x^4], x], x] + \text{Dist}[1/q, \text{Int}[(1 + q*x^2)/\text{Sqrt}[a + b*x^4], x], x]] /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a]$

Rule 424

$\text{Int}[\text{Sqrt}[(a_) + (b_)*(x_)^2]/\text{Sqrt}[(c_) + (d_)*(x_)^2], x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[a]*\text{EllipticE}[\text{ArcSin}[\text{Rt}[-(d/c), 2]*x], (b*c)/(a*d)])/(\text{Sqrt}[c]*\text{Rt}[-(d/c), 2]), x] /; \text{FreeQ}\{a, b, c, d\}, x] \ \&\& \ \text{NegQ}[d/c] \ \&\& \ \text{GtQ}[c, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1199

$\text{Int}[(d_) + (e_)*(x_)^2]/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[d/\text{Sqrt}[a], \text{Int}[\text{Sqrt}[1 + (e*x^2)/d]/\text{Sqrt}[1 - (e*x^2)/d], x], x] /; \text{FreeQ}\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1200

$\text{Int}[(d_) + (e_)*(x_)^2]/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[\text{Sqrt}[1 + (c*x^4)/a]/\text{Sqrt}[a + c*x^4], \text{Int}[(d + e*x^2)/\text{Sqrt}[1 + (c*x^4)/a], x], x] /; \text{FreeQ}\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{3/2} \sqrt[4]{c+dx}} dx &= -\frac{2(c+dx)^{3/4}}{(bc-ad)\sqrt{a+bx}} + \frac{d \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{2(bc-ad)} \\
&= -\frac{2(c+dx)^{3/4}}{(bc-ad)\sqrt{a+bx}} + \frac{2 \operatorname{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{bc-ad} \\
&= -\frac{2(c+dx)^{3/4}}{(bc-ad)\sqrt{a+bx}} - \frac{2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b} \sqrt{bc-ad}} + \frac{2 \operatorname{Subst} \left(\int \frac{1+\frac{\sqrt{b}x^2}{\sqrt{bc-ad}}}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b} \sqrt{bc-ad}} \\
&= -\frac{2(c+dx)^{3/4}}{(bc-ad)\sqrt{a+bx}} - \frac{\left(2\sqrt{\frac{d(a+bx)}{-bc+ad}}\right) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)^d}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b} \sqrt{bc-ad} \sqrt{a+bx}} + \frac{\left(2\sqrt{\frac{d(a+bx)}{-bc+ad}}\right) \operatorname{Subst} \left(\int \frac{1+\frac{\sqrt{b}x^2}{\sqrt{bc-ad}}}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)^d}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b} \sqrt{bc-ad} \sqrt{a+bx}} \\
&= -\frac{2(c+dx)^{3/4}}{(bc-ad)\sqrt{a+bx}} - \frac{2\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{b^{3/4} \sqrt[4]{bc-ad} \sqrt{a+bx}} + \frac{\left(2\sqrt{\frac{d(a+bx)}{-bc+ad}}\right) \operatorname{Subst} \left(\int \frac{1+\frac{\sqrt{b}x^2}{\sqrt{bc-ad}}}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)^d}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b} \sqrt{bc-ad} \sqrt{a+bx}} \\
&= -\frac{2(c+dx)^{3/4}}{(bc-ad)\sqrt{a+bx}} + \frac{2\sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{b^{3/4} \sqrt[4]{bc-ad} \sqrt{a+bx}} - \frac{2\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{b^{3/4} \sqrt[4]{bc-ad}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.37

$$-\frac{2\sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{2}, \frac{1}{4}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt{a+bx} \sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(1/4)), x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[-1/2, 1/4, 1/2, (d*(a + b*x))/(-b*c + a*d)]/(b*Sqrt[a + b*x]*(c + d*x)^(1/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}}{b^2dx^3+a^2c+(b^2c+2abd)x^2+(2abc+a^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(1/4)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(1/4),x)

[Out] int(1/(b*x+a)^(3/2)/(d*x+c)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{3/2} (c + dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(3/2)*(c + d*x)^(1/4)), x)`

[Out] `int(1/((a + b*x)^(3/2)*(c + d*x)^(1/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} \sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(3/2)/(d*x+c)**(1/4), x)`

[Out] `Integral(1/((a + b*x)**(3/2)*(c + d*x)**(1/4)), x)`

$$3.1653 \quad \int \frac{1}{(a+bx)^{5/2} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=224

$$\frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{b^{3/4}\sqrt{a+bx}(bc-ad)^{5/4}} - \frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{b^{3/4}\sqrt{a+bx}(bc-ad)^{5/4}} + \frac{d(c+dx)^{3/4}}{\sqrt{a+bx}(bc-ad)^2} - \frac{2(c+dx)}{3(a+bx)^{3/2}}$$

[Out] $-2/3*(d*x+c)^{(3/4)/(-a*d+b*c)/(b*x+a)^{(3/2)+d*(d*x+c)^{(3/4)/(-a*d+b*c)^2/(b*x+a)^{(1/2)-d*EllipticE(b^{(1/4)*(d*x+c)^{(1/4)/(-a*d+b*c)^{(1/4)},I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)/b^{(3/4)/(-a*d+b*c)^{(5/4)/(b*x+a)^{(1/2)+d*EllipticF(b^{(1/4)*(d*x+c)^{(1/4)/(-a*d+b*c)^{(1/4)},I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)/b^{(3/4)/(-a*d+b*c)^{(5/4)/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.26, antiderivative size = 224, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{b^{3/4}\sqrt{a+bx}(bc-ad)^{5/4}} - \frac{d\sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{b^{3/4}\sqrt{a+bx}(bc-ad)^{5/4}} + \frac{d(c+dx)^{3/4}}{\sqrt{a+bx}(bc-ad)^2} - \frac{2(c+dx)}{3(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*(c + d*x)^(1/4)), x]

[Out] $(-2*(c+d*x)^{(3/4))/(3*(b*c-a*d)*(a+b*x)^{(3/2)}) + (d*(c+d*x)^{(3/4)})/((b*c-a*d)^2*\sqrt{a+b*x}) - (d*\sqrt{-((d*(a+b*x))/(b*c-a*d))})*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)*(c+d*x)^{(1/4)})/(b*c-a*d)^{(1/4)}], -1]/(b^{(3/4)*(b*c-a*d)^{(5/4)*\sqrt{a+b*x}}) + (d*\sqrt{-((d*(a+b*x))/(b*c-a*d))})*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)*(c+d*x)^{(1/4)})/(b*c-a*d)^{(1/4)}], -1]/(b^{(3/4)*(b*c-a*d)^{(5/4)*\sqrt{a+b*x}})$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt
[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x
] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[
a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/2} \sqrt[4]{c+dx}} dx &= -\frac{2(c+dx)^{3/4}}{3(bc-ad)(a+bx)^{3/2}} - \frac{d \int \frac{1}{(a+bx)^{3/2} \sqrt[4]{c+dx}} dx}{2(bc-ad)} \\
&= -\frac{2(c+dx)^{3/4}}{3(bc-ad)(a+bx)^{3/2}} + \frac{d(c+dx)^{3/4}}{(bc-ad)^2 \sqrt{a+bx}} - \frac{d^2 \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{4(bc-ad)^2} \\
&= -\frac{2(c+dx)^{3/4}}{3(bc-ad)(a+bx)^{3/2}} + \frac{d(c+dx)^{3/4}}{(bc-ad)^2 \sqrt{a+bx}} - \frac{d \operatorname{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{(bc-ad)^2} \\
&= -\frac{2(c+dx)^{3/4}}{3(bc-ad)(a+bx)^{3/2}} + \frac{d(c+dx)^{3/4}}{(bc-ad)^2 \sqrt{a+bx}} + \frac{d \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{\sqrt{b}(bc-ad)^{3/2}} \\
&= -\frac{2(c+dx)^{3/4}}{3(bc-ad)(a+bx)^{3/2}} + \frac{d(c+dx)^{3/4}}{(bc-ad)^2 \sqrt{a+bx}} + \frac{\left(d \sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)^d}} dx \right)}{\sqrt{b}(bc-ad)^{3/2} \sqrt{a+bx}} \\
&= -\frac{2(c+dx)^{3/4}}{3(bc-ad)(a+bx)^{3/2}} + \frac{d(c+dx)^{3/4}}{(bc-ad)^2 \sqrt{a+bx}} + \frac{d \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right)}{b^{3/4}(bc-ad)^{5/4} \sqrt{a+bx}} \\
&= -\frac{2(c+dx)^{3/4}}{3(bc-ad)(a+bx)^{3/2}} + \frac{d(c+dx)^{3/4}}{(bc-ad)^2 \sqrt{a+bx}} - \frac{d \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right)}{b^{3/4}(bc-ad)^{5/4} \sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.33

$$-\frac{2 \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(-\frac{3}{2}, \frac{1}{4}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(a+bx)^{3/2} \sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(1/4)),x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[-3/2, 1/4, -1/2, (d*(a + b*x))/(-b*c + a*d)]/(3*b*(a + b*x)^(3/2)*(c + d*x)^(1/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}}{b^3dx^4+a^3c+(b^3c+3ab^2d)x^3+3(ab^2c+a^2bd)x^2+(3a^2bc+a^3d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(1/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(1/4),x)

[Out] int(1/(b*x+a)^(5/2)/(d*x+c)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{5/2} (c + dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/2)*(c + d*x)^(1/4)), x)

[Out] int(1/((a + b*x)^(5/2)*(c + d*x)^(1/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{5}{2}} \sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(1/4), x)

[Out] Integral(1/((a + b*x)**(5/2)*(c + d*x)**(1/4)), x)

$$3.1654 \quad \int \frac{(a+bx)^{3/2}}{(c+dx)^{3/4}} dx$$

Optimal. Leaf size=144

$$\frac{16(bc-ad)^{9/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{7\sqrt[4]{b} d^3 \sqrt{a+bx}} - \frac{8\sqrt{a+bx} \sqrt[4]{c+dx} (bc-ad)}{7d^2} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7d}$$

[Out] $4/7*(b*x+a)^{(3/2)}*(d*x+c)^{(1/4)}/d-8/7*(-a*d+b*c)*(d*x+c)^{(1/4)}*(b*x+a)^{(1/2)}/d^2+16/7*(-a*d+b*c)^{(9/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(1/4)}/d^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.08, antiderivative size = 144, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 224, 221}

$$-\frac{8\sqrt{a+bx} \sqrt[4]{c+dx} (bc-ad)}{7d^2} + \frac{16(bc-ad)^{9/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{7\sqrt[4]{b} d^3 \sqrt{a+bx}} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7d}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}/(c + d*x)^{(3/4)}, x]$

[Out] $(-8*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/4)})/(7*d^2) + (4*(a + b*x)^{(3/2)}*(c + d*x)^{(1/4)})/(7*d) + (16*(b*c - a*d)^{(9/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1)]/(7*b^{(1/4)}*d^3*\operatorname{Sqrt}[a + b*x])$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{NeQ}[m+n+1, 0]$ && $!(\operatorname{IGtQ}[m, 0] \&\& (!\operatorname{IntegerQ}[n] \mid\mid (\operatorname{GtQ}[m, 0] \&\& \operatorname{LtQ}[m-n, 0])))$ && $!\operatorname{ILtQ}[m+n+2, 0]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{LtQ}[-1, m, 0]$ && $\operatorname{LeQ}[-1, n, 0]$ && $\operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Den}$

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^{3/2}}{(c+dx)^{3/4}} dx &= \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7d} - \frac{(6(bc-ad)) \int \frac{\sqrt{a+bx}}{(c+dx)^{3/4}} dx}{7d} \\ &= -\frac{8(bc-ad)\sqrt{a+bx} \sqrt[4]{c+dx}}{7d^2} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7d} + \frac{(4(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{7d^2} \\ &= -\frac{8(bc-ad)\sqrt{a+bx} \sqrt[4]{c+dx}}{7d^2} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7d} + \frac{(16(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx \right)}{7d^3} \\ &= -\frac{8(bc-ad)\sqrt{a+bx} \sqrt[4]{c+dx}}{7d^2} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7d} + \frac{(16(bc-ad)^2 \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{a+bx}} dx \right)}{7d^3 \sqrt{a+bx}} \\ &= -\frac{8(bc-ad)\sqrt{a+bx} \sqrt[4]{c+dx}}{7d^2} + \frac{4(a+bx)^{3/2} \sqrt[4]{c+dx}}{7d} + \frac{16(bc-ad)^{9/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt{a+bx}}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} \right) \right)}{7 \sqrt[4]{b} d^3 \sqrt{a+bx}} \end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.51

$$\frac{2(a+bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4} {}_2F_1 \left(\frac{3}{4}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc} \right)}{5b(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(3/4), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[3/4, 5/2, 7/2, (d*(a + b*x))/(-b*c + a*d)]/(5*b*(c + d*x)^(3/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{3}{4}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(3/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)/(d*x + c)^(3/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(3/4), x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(3/4), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(3/4), x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(3/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/2)/(d*x+c)^(3/4),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(3/2)/(d*x + c)^(3/4), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{3/2}}{(c + dx)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(3/2)/(c + d*x)^(3/4),x)`

[Out] `int((a + b*x)^(3/2)/(c + d*x)^(3/4), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{(c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(3/2)/(d*x+c)**(3/4),x)`

[Out] `Integral((a + b*x)**(3/2)/(c + d*x)**(3/4), x)`

$$3.1655 \quad \int \frac{\sqrt{a+bx}}{(c+dx)^{3/4}} dx$$

Optimal. Leaf size=111

$$\frac{4\sqrt{a+bx}\sqrt[4]{c+dx}}{3d} - \frac{8(bc-ad)^{5/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}\text{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{3\sqrt[4]{b}d^2\sqrt{a+bx}}$$

[Out] $4/3*(d*x+c)^{(1/4)}*(b*x+a)^{(1/2)}/d-8/3*(-a*d+b*c)^{(5/4)}*\text{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(1/4)}/d^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.07, antiderivative size = 111, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 63, 224, 221}

$$\frac{4\sqrt{a+bx}\sqrt[4]{c+dx}}{3d} - \frac{8(bc-ad)^{5/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\middle| -1\right)}{3\sqrt[4]{b}d^2\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/(c + d*x)^(3/4), x]

[Out] $(4*\text{Sqrt}[a + b*x]*(c + d*x)^{(1/4)})/(3*d) - (8*(b*c - a*d)^{(5/4)}*\text{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\text{EllipticF}[\text{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(3*b^{(1/4)}*d^2*\text{Sqrt}[a + b*x])$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt{a+bx}}{(c+dx)^{3/4}} dx &= \frac{4\sqrt{a+bx} \sqrt[4]{c+dx}}{3d} - \frac{(2(bc-ad)) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{3d} \\ &= \frac{4\sqrt{a+bx} \sqrt[4]{c+dx}}{3d} - \frac{(8(bc-ad)) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{3d^2} \\ &= \frac{4\sqrt{a+bx} \sqrt[4]{c+dx}}{3d} - \frac{\left(8(bc-ad) \sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)^d}}} dx, x, \sqrt[4]{c+dx} \right)}{3d^2 \sqrt{a+bx}} \\ &= \frac{4\sqrt{a+bx} \sqrt[4]{c+dx}}{3d} - \frac{8(bc-ad)^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{3 \sqrt[4]{b} d^2 \sqrt{a+bx}} \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.66

$$\frac{2(a+bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4} {}_2F_1 \left(\frac{3}{4}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(3/4), x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[3/4, 3/2, 5/2, (d*(a + b*x))/(-b*c) + a*d])/(3*b*(c + d*x)^(3/4))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}}{(dx+c)^{\frac{3}{4}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(3/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)/(d*x + c)^(3/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(3/4),x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(3/4), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(3/4),x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(3/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\sqrt{a + bx}}{(c + dx)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(3/4), x)

[Out] int((a + b*x)^(1/2)/(c + d*x)^(3/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a + bx}}{(c + dx)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(3/4), x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(3/4), x)

$$3.1656 \quad \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx$$

Optimal. Leaf size=83

$$\frac{4\sqrt[4]{bc-ad} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{\sqrt[4]{b} d \sqrt{a+bx}}$$

[Out] $4*(-a*d+b*c)^{(1/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)} / (-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a) / (-a*d+b*c))^{(1/2)} / b^{(1/4)} / d / (b*x+a)^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 83, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {63, 224, 221}

$$\frac{4\sqrt[4]{bc-ad} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{\sqrt[4]{b} d \sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(3/4)),x]

[Out] $(4*(b*c - a*d)^{(1/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)}) / (b*c - a*d)^{(1/4)}], -1]) / (b^{(1/4)}*d*\operatorname{Sqrt}[a + b*x])$

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[

b/a] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx &= \frac{4 \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{d} \\ &= \frac{\left(4\sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)d}}} dx, x, \sqrt[4]{c+dx} \right)}{d\sqrt{a+bx}} \\ &= \frac{4\sqrt[4]{bc-ad} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{\sqrt[4]{b} d \sqrt{a+bx}} \end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.86

$$\frac{2\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4} {}_2F_1 \left(\frac{1}{2}, \frac{3}{4}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(3/4)), x]

[Out] (2*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[1/2, 3/4, 3/2, (d*(a + b*x))/(-b*c + a*d)])/(b*(c + d*x)^(3/4))

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\operatorname{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{1}{4}}}{bdx^2+ac+(bc+ad)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(3/4), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/4)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(3/4),x, algorithm="giac")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(3/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(3/4),x)

[Out] int(1/(b*x+a)^(1/2)/(d*x+c)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/2)*(c + d*x)^(3/4)),x)

[Out] int(1/((a + b*x)^(1/2)*(c + d*x)^(3/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(1/2)/(d*x+c)**(3/4),x)
```

```
[Out] Integral(1/(sqrt(a + b*x)*(c + d*x)**(3/4)), x)
```

$$3.1657 \quad \int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/4}} dx$$

Optimal. Leaf size=111

$$-\frac{2\sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{\sqrt[4]{b}\sqrt{a+bx}(bc-ad)^{3/4}} - \frac{2\sqrt[4]{c+dx}}{\sqrt{a+bx}(bc-ad)}$$

[Out] $-2*(d*x+c)^{(1/4)/(-a*d+b*c)/(b*x+a)^{(1/2)}-2*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/b^{(1/4)}/(-a*d+b*c)^{(3/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.06, antiderivative size = 111, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {51, 63, 224, 221}

$$-\frac{2\sqrt[4]{c+dx}}{\sqrt{a+bx}(bc-ad)} - \frac{2\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{\sqrt[4]{b}\sqrt{a+bx}(bc-ad)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a + b*x)^{(3/2)}*(c + d*x)^{(3/4))}, x]$

[Out] $(-2*(c + d*x)^{(1/4)})/((b*c - a*d)*\operatorname{Sqrt}[a + b*x]) - (2*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))] * \operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(b^{(1/4)}*(b*c - a*d)^{(3/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}]/((b*c - a*d)*(m + 1)), x] - \operatorname{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, n\}, x] \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{LtQ}[m, -1] \ \&\& \ !(\operatorname{LtQ}[n, -1] \ \&\& \ (\operatorname{EqQ}[a, 0] \ || \ (\operatorname{NeQ}[c, 0] \ \&\& \ \operatorname{LtQ}[m - n, 0] \ \&\& \ \operatorname{IntegerQ}[n]))) \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x] \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{LtQ}[-1, m, 0] \ \&\& \ \operatorname{LeQ}[-1, n, 0] \ \&\& \ \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
  4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/4}} dx &= -\frac{2\sqrt[4]{c+dx}}{(bc-ad)\sqrt{a+bx}} - \frac{d \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{2(bc-ad)} \\
&= -\frac{2\sqrt[4]{c+dx}}{(bc-ad)\sqrt{a+bx}} - \frac{2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{bc-ad} \\
&= -\frac{2\sqrt[4]{c+dx}}{(bc-ad)\sqrt{a+bx}} - \frac{\left(2\sqrt{\frac{d(a+bx)}{-bc+ad}} \right) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)d}}} dx, x, \sqrt[4]{c+dx} \right)}{(bc-ad)\sqrt{a+bx}} \\
&= -\frac{2\sqrt[4]{c+dx}}{(bc-ad)\sqrt{a+bx}} - \frac{2\sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right) - 1}{\sqrt[4]{b}(bc-ad)^{3/4}\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.64

$$-\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4} {}_2F_1 \left(-\frac{1}{2}, \frac{3}{4}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt{a+bx}(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(3/4)), x]

[Out] $(-2*((b*(c + d*x))/(b*c - a*d))^{3/4} * \text{Hypergeometric2F1}[-1/2, 3/4, 1/2, (d*(a + b*x))/(-(b*c) + a*d)]) / (b*\text{Sqrt}[a + b*x]*(c + d*x)^{3/4})$

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{1}{4}}}{b^2dx^3+a^2c+(b^2c+2abd)x^2+(2abc+a^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/2)/(d*x+c)^(3/4),x, algorithm="fricas")`

[Out] `integral(sqrt(b*x + a)*(d*x + c)^(1/4)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/2)/(d*x+c)^(3/4),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(3/2)*(d*x + c)^(3/4)), x)`

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(3/2)/(d*x+c)^(3/4),x)`

[Out] `int(1/(b*x+a)^(3/2)/(d*x+c)^(3/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/2)/(d*x+c)^(3/4),x, algorithm="maxima")`

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{3/2} (c + dx)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(3/4)), x)

[Out] int(1/((a + b*x)^(3/2)*(c + d*x)^(3/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} (c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(3/4), x)

[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(3/4)), x)

$$3.1658 \quad \int \frac{1}{(a+bx)^{5/2}(c+dx)^{3/4}} dx$$

Optimal. Leaf size=149

$$\frac{5d\sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{3\sqrt[4]{b}\sqrt{a+bx}(bc-ad)^{7/4}} + \frac{5d\sqrt[4]{c+dx}}{3\sqrt{a+bx}(bc-ad)^2} - \frac{2\sqrt[4]{c+dx}}{3(a+bx)^{3/2}(bc-ad)}$$

[Out] $-2/3*(d*x+c)^{(1/4)/(-a*d+b*c)/(b*x+a)^{(3/2)+5/3*d*(d*x+c)^{(1/4)/(-a*d+b*c)}^2/(b*x+a)^{(1/2)+5/3*d*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)/(-a*d+b*c)}^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)/b^{(1/4)/(-a*d+b*c)}^{(7/4)/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.07, antiderivative size = 149, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {51, 63, 224, 221}

$$\frac{5d\sqrt[4]{c+dx}}{3\sqrt{a+bx}(bc-ad)^2} - \frac{2\sqrt[4]{c+dx}}{3(a+bx)^{3/2}(bc-ad)} + \frac{5d\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{3\sqrt[4]{b}\sqrt{a+bx}(bc-ad)^{7/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a+b*x)^{(5/2)}*(c+d*x)^{(3/4)}), x]$

[Out] $(-2*(c+d*x)^{(1/4))/(3*(b*c-a*d)*(a+b*x)^{(3/2)}) + (5*d*(c+d*x)^{(1/4)})/(3*(b*c-a*d)^2*\operatorname{Sqrt}[a+b*x]) + (5*d*\operatorname{Sqrt}[-(d*(a+b*x))/(b*c-a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c+d*x)^{(1/4)})/(b*c-a*d)^{(1/4)}], -1]/(3*b^{(1/4)}*(b*c-a*d)^{(7/4)}*\operatorname{Sqrt}[a+b*x])$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)]/((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*(m+n+2)]/((b*c - a*d)*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^n, x], x] /;$ FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{5/2}(c+dx)^{3/4}} dx &= -\frac{2\sqrt[4]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} - \frac{(5d) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{3/4}} dx}{6(bc-ad)} \\
 &= -\frac{2\sqrt[4]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{5d\sqrt[4]{c+dx}}{3(bc-ad)^2\sqrt{a+bx}} + \frac{(5d^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{12(bc-ad)^2} \\
 &= -\frac{2\sqrt[4]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{5d\sqrt[4]{c+dx}}{3(bc-ad)^2\sqrt{a+bx}} + \frac{(5d) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{3(bc-ad)^2} \\
 &= -\frac{2\sqrt[4]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{5d\sqrt[4]{c+dx}}{3(bc-ad)^2\sqrt{a+bx}} + \frac{(5d\sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})}}} dx, x, \sqrt[4]{c+dx} \right)}{3(bc-ad)^2\sqrt{a+bx}} \\
 &= -\frac{2\sqrt[4]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{5d\sqrt[4]{c+dx}}{3(bc-ad)^2\sqrt{a+bx}} + \frac{5d\sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right)}{3\sqrt[4]{b}(bc-ad)^{7/4}\sqrt{a+bx}}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.49

$$-\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4} {}_2F_1 \left(-\frac{3}{2}, \frac{3}{4}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(a+bx)^{3/2}(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(3/4)), x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[-3/2, 3/4, -1/2, (d*(a + b*x))/(-(b*c) + a*d)])/(3*b*(a + b*x)^(3/2)*(c + d*x)^(3/4))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{1}{4}}}{b^3 dx^4 + a^3 c + (b^3 c + 3 ab^2 d)x^3 + 3(ab^2 c + a^2 bd)x^2 + (3 a^2 bc + a^3 d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(3/4), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/4)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(3/4), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(3/4)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(3/4), x)

[Out] int(1/(b*x+a)^(5/2)/(d*x+c)^(3/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{5/2} (c + dx)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/2)*(c + d*x)^(3/4)),x)

[Out] int(1/((a + b*x)^(5/2)*(c + d*x)^(3/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{5}{2}} (c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(3/4),x)

[Out] Integral(1/((a + b*x)**(5/2)*(c + d*x)**(3/4)), x)

$$3.1659 \quad \int \frac{(a+bx)^{5/2}}{(c+dx)^{5/4}} dx$$

Optimal. Leaf size=254

$$\frac{32\sqrt[4]{b}(bc-ad)^{11/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}\operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right),-1\right)}{3d^4\sqrt{a+bx}} + \frac{32\sqrt[4]{b}(bc-ad)^{11/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{3d^4\sqrt{a+bx}}$$

[Out] $-4*(b*x+a)^{(5/2)}/d/(d*x+c)^{(1/4)}+40/9*b*(b*x+a)^{(3/2)}*(d*x+c)^{(3/4)}/d^2-16/3*b*(-a*d+b*c)*(d*x+c)^{(3/4)}*(b*x+a)^{(1/2)}/d^3+32/3*b^{(1/4)}*(-a*d+b*c)^{(11/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)},I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^4/(b*x+a)^{(1/2)}-32/3*b^{(1/4)}*(-a*d+b*c)^{(11/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)},I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^4/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.26, antiderivative size = 254, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 50, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{16b\sqrt{a+bx}(c+dx)^{3/4}(bc-ad)}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} - \frac{32\sqrt[4]{b}(bc-ad)^{11/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{3d^4\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}/(c + d*x)^{(5/4)}, x]$

[Out] $(-4*(a + b*x)^{(5/2)})/(d*(c + d*x)^{(1/4)}) - (16*b*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)})/(3*d^3) + (40*b*(a + b*x)^{(3/2)}*(c + d*x)^{(3/4)})/(9*d^2) + (32*b^{(1/4)}*(b*c - a*d)^{(11/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/(3*d^4*\operatorname{Sqrt}[a + b*x]) - (32*b^{(1/4)}*(b*c - a*d)^{(11/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/(3*d^4*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_.)}*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{IntegerQ}[n] \&\& !\operatorname{IntegerQ}[m]) \&\& !(I\operatorname{LeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0])) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
```

$d, e\}, x] \ \&\& \text{NegQ}[c/a] \ \&\& \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \text{GtQ}[a, 0]$

Rule 1200

$\text{Int}[(d_ + (e_.)*(x_)^2)/\text{Sqrt}[(a_ + (c_.)*(x_)^4], x_Symbol] \ :> \text{Dist}[\text{Sqrt}[1 + (c*x^4)/a]/\text{Sqrt}[a + c*x^4], \text{Int}[(d + e*x^2)/\text{Sqrt}[1 + (c*x^4)/a], x], x] \ /; \text{FreeQ}\{a, c, d, e\}, x] \ \&\& \text{NegQ}[c/a] \ \&\& \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{(c+dx)^{5/4}} dx &= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} + \frac{(10b) \int \frac{(a+bx)^{3/2}}{\sqrt[4]{c+dx}} dx}{d} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} - \frac{(20b(bc-ad)) \int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx}{3d^2} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} - \frac{16b(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} + \frac{(8b(bc-ad))}{9d^2} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} - \frac{16b(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} + \frac{(32b(bc-ad))}{9d^2} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} - \frac{16b(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} + \frac{(32\sqrt{b}(bc-ad))}{9d^2} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} - \frac{16b(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} - \frac{(32\sqrt{b}(bc-ad))}{9d^2} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} - \frac{16b(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} - \frac{(32\sqrt{b}(bc-ad))}{9d^2} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} - \frac{16b(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} - \frac{(32\sqrt{b}(bc-ad))}{9d^2} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} - \frac{16b(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} - \frac{(32\sqrt{b}(bc-ad))}{9d^2} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} - \frac{16b(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} - \frac{(32\sqrt{b}(bc-ad))}{9d^2} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} - \frac{16b(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} - \frac{(32\sqrt{b}(bc-ad))}{9d^2} \\
&= -\frac{4(a+bx)^{5/2}}{d\sqrt[4]{c+dx}} - \frac{16b(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{3d^3} + \frac{40b(a+bx)^{3/2}(c+dx)^{3/4}}{9d^2} - \frac{(32\sqrt{b}(bc-ad))}{9d^2}
\end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.29

$$\frac{2(a+bx)^{7/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(\frac{5}{4}, \frac{7}{2}; \frac{9}{2}; \frac{d(a+bx)}{ad-bc} \right)}{7b(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/(c + d*x)^(5/4),x]

[Out] $(2*(a + b*x)^{(7/2)}*((b*(c + d*x))/(b*c - a*d))^{(5/4)}*Hypergeometric2F1[5/4, 7/2, 9/2, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*(c + d*x)^{(5/4)})$

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(b^2x^2 + 2abx + a^2)\sqrt{bx + a}(dx + c)^{\frac{3}{4}}}{d^2x^2 + 2cdx + c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] integral((b^2*x^2 + 2*a*b*x + a^2)*sqrt(b*x + a)*(d*x + c)^(3/4)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/2)/(d*x + c)^(5/4), x)

maple [F] time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/(d*x+c)^(5/4),x)

[Out] int((b*x+a)^(5/2)/(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/2)/(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{5/2}}{(c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)/(c + d*x)^(5/4), x)

[Out] int((a + b*x)^(5/2)/(c + d*x)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{2}}}{(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)/(d*x+c)**(5/4), x)

[Out] Integral((a + b*x)**(5/2)/(c + d*x)**(5/4), x)

$$3.1660 \quad \int \frac{(a+bx)^{3/2}}{(c+dx)^{5/4}} dx$$

Optimal. Leaf size=220

$$\frac{48\sqrt[4]{b}(bc-ad)^{7/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}\operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{5d^3\sqrt{a+bx}} - \frac{48\sqrt[4]{b}(bc-ad)^{7/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{5d^3\sqrt{a+bx}}$$

[Out] $-4*(b*x+a)^{(3/2)}/d/(d*x+c)^{(1/4)}+24/5*b*(d*x+c)^{(3/4)}*(b*x+a)^{(1/2)}/d^2-48/5*b^{(1/4)}*(-a*d+b*c)^{(7/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^3/(b*x+a)^{(1/2)}+48/5*b^{(1/4)}*(-a*d+b*c)^{(7/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.23, antiderivative size = 220, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 50, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{24b\sqrt{a+bx}(c+dx)^{3/4}}{5d^2} + \frac{48\sqrt[4]{b}(bc-ad)^{7/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)-1}{5d^3\sqrt{a+bx}} - \frac{48\sqrt[4]{b}(bc-ad)^{7/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{5d^3\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}/(c + d*x)^{(5/4)}, x]$

[Out] $(-4*(a + b*x)^{(3/2)})/(d*(c + d*x)^{(1/4)}) + (24*b*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)})/(5*d^2) - (48*b^{(1/4)}*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(5*d^3*\operatorname{Sqrt}[a + b*x]) + (48*b^{(1/4)}*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(5*d^3*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\}$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ && $\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{3/2}}{(c+dx)^{5/4}} dx &= -\frac{4(a+bx)^{3/2}}{d\sqrt[4]{c+dx}} + \frac{(6b) \int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx}{d} \\
 &= -\frac{4(a+bx)^{3/2}}{d\sqrt[4]{c+dx}} + \frac{24b\sqrt{a+bx}(c+dx)^{3/4}}{5d^2} - \frac{(12b(bc-ad)) \int \frac{1}{\sqrt{a+bx}\sqrt[4]{c+dx}} dx}{5d^2} \\
 &= -\frac{4(a+bx)^{3/2}}{d\sqrt[4]{c+dx}} + \frac{24b\sqrt{a+bx}(c+dx)^{3/4}}{5d^2} - \frac{(48b(bc-ad)) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d^3} \\
 &= -\frac{4(a+bx)^{3/2}}{d\sqrt[4]{c+dx}} + \frac{24b\sqrt{a+bx}(c+dx)^{3/4}}{5d^2} + \frac{(48\sqrt{b}(bc-ad)^{3/2}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d^3} \\
 &= -\frac{4(a+bx)^{3/2}}{d\sqrt[4]{c+dx}} + \frac{24b\sqrt{a+bx}(c+dx)^{3/4}}{5d^2} + \frac{(48\sqrt{b}(bc-ad)^{3/2} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d^3\sqrt{a+bx}} \\
 &= -\frac{4(a+bx)^{3/2}}{d\sqrt[4]{c+dx}} + \frac{24b\sqrt{a+bx}(c+dx)^{3/4}}{5d^2} + \frac{48\sqrt[4]{b}(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right)}{5d^3\sqrt{a+bx}} \\
 &= -\frac{4(a+bx)^{3/2}}{d\sqrt[4]{c+dx}} + \frac{24b\sqrt{a+bx}(c+dx)^{3/4}}{5d^2} - \frac{48\sqrt[4]{b}(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right)}{5d^3\sqrt{a+bx}}
 \end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.33

$$\frac{2(a + bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(\frac{5}{4}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc} \right)}{5b(c + dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(5/4), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[5/4, 5/2, 7/2, (d*(a + b*x))/(-b*c) + a*d])/(5*b*(c + d*x)^(5/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^{\frac{3}{2}}(dx + c)^{\frac{3}{4}}}{d^2x^2 + 2cdx + c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(5/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)*(d*x + c)^(3/4)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(5/4), x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(5/4), x)

maple [F] time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(5/4), x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(5/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{3/2}}{(c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/(c + d*x)^(5/4),x)

[Out] int((a + b*x)^(3/2)/(c + d*x)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/(d*x+c)**(5/4),x)

[Out] Integral((a + b*x)**(3/2)/(c + d*x)**(5/4), x)

$$3.1661 \quad \int \frac{\sqrt{a+bx}}{(c+dx)^{5/4}} dx$$

Optimal. Leaf size=190

$$\frac{8\sqrt[4]{b}(bc-ad)^{3/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}\operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right),-1\right)}{d^2\sqrt{a+bx}} + \frac{8\sqrt[4]{b}(bc-ad)^{3/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{d^2\sqrt{a+bx}}$$

[Out] $-4*(b*x+a)^{(1/2)}/d/(d*x+c)^{(1/4)}+8*b^{(1/4)}*(-a*d+b*c)^{(3/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)},I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^2/(b*x+a)^{(1/2)}-8*b^{(1/4)}*(-a*d+b*c)^{(3/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)},I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.21, antiderivative size = 190, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {47, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{8\sqrt[4]{b}(bc-ad)^{3/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)-1}{d^2\sqrt{a+bx}} + \frac{8\sqrt[4]{b}(bc-ad)^{3/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)-1}{d^2\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[\operatorname{Sqrt}[a + b*x]/(c + d*x)^{(5/4)}, x]$

[Out] $(-4*\operatorname{Sqrt}[a + b*x])/(d*(c + d*x)^{(1/4)}) + (8*b^{(1/4)}*(b*c - a*d)^{(3/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1])/(d^2*\operatorname{Sqrt}[a + b*x]) - (8*b^{(1/4)}*(b*c - a*d)^{(3/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1])/(d^2*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{IntegerQ}[n] \&\& !\operatorname{IntegerQ}[m]) \&\& !(I\operatorname{LeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0])) \& \& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b +$

$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{ :> } \text{Simp}[\text{EllipticF}[\text{ArcSin}[\text{Rt}[-b, 4]*x]/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{GtQ}[a, 0]$

Rule 224

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{ :> } \text{Dist}[\text{Sqrt}[1 + (b*x^4)/a]/\text{Sqrt}[a + b*x^4], \text{Int}[1/\text{Sqrt}[1 + (b*x^4)/a], x], x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{!GtQ}[a, 0]$

Rule 307

$\text{Int}[(x_)^2/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \text{ :> } \text{With}[\{q = \text{Rt}[-(b/a), 2]\}, -\text{Dist}[q^{(-1)}, \text{Int}[1/\text{Sqrt}[a + b*x^4], x], x] + \text{Dist}[1/q, \text{Int}[(1 + q*x^2)/\text{Sqrt}[a + b*x^4], x], x]] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a]$

Rule 424

$\text{Int}[\text{Sqrt}[(a_) + (b_)*(x_)^2]/\text{Sqrt}[(c_) + (d_)*(x_)^2], x_Symbol] \text{ :> } \text{Simp}[(\text{Sqrt}[a]*\text{EllipticE}[\text{ArcSin}[\text{Rt}[-(d/c), 2]*x], (b*c)/(a*d)])/(\text{Sqrt}[c]*\text{Rt}[-(d/c), 2]), x] /; \text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NegQ}[d/c] \ \&\& \ \text{GtQ}[c, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1199

$\text{Int}[(d_) + (e_)*(x_)^2/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \text{ :> } \text{Dist}[d/\text{Sqrt}[a], \text{Int}[\text{Sqrt}[1 + (e*x^2)/d]/\text{Sqrt}[1 - (e*x^2)/d], x], x] /; \text{FreeQ}[\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1200

$\text{Int}[(d_) + (e_)*(x_)^2/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \text{ :> } \text{Dist}[\text{Sqrt}[1 + (c*x^4)/a]/\text{Sqrt}[a + c*x^4], \text{Int}[(d + e*x^2)/\text{Sqrt}[1 + (c*x^4)/a], x], x] /; \text{FreeQ}[\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{!GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{a+bx}}{(c+dx)^{5/4}} dx &= -\frac{4\sqrt{a+bx}}{d\sqrt[4]{c+dx}} + \frac{(2b) \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{d} \\
&= -\frac{4\sqrt{a+bx}}{d\sqrt[4]{c+dx}} + \frac{(8b) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{d^2} \\
&= -\frac{4\sqrt{a+bx}}{d\sqrt[4]{c+dx}} - \frac{(8\sqrt{b} \sqrt{bc-ad}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{d^2} + \frac{(8\sqrt{b} \sqrt{bc-ad}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{d^2} \\
&= -\frac{4\sqrt{a+bx}}{d\sqrt[4]{c+dx}} - \frac{(8\sqrt{b} \sqrt{bc-ad} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{d^2 \sqrt{a+bx}} + \frac{(8\sqrt{b} \sqrt{bc-ad} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{d^2 \sqrt{a+bx}} \\
&= -\frac{4\sqrt{a+bx}}{d\sqrt[4]{c+dx}} - \frac{8\sqrt[4]{b} (bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{d^2 \sqrt{a+bx}} + \frac{(8\sqrt{b} \sqrt{bc-ad} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{d^2 \sqrt{a+bx}} \\
&= -\frac{4\sqrt{a+bx}}{d\sqrt[4]{c+dx}} + \frac{8\sqrt[4]{b} (bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{d^2 \sqrt{a+bx}} - \frac{8\sqrt[4]{b} (bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{d^2 \sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.38

$$\frac{2(a+bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(\frac{5}{4}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(5/4), x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[5/4, 3/2, 5/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(c + d*x)^(5/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}}{d^2x^2+2cdx+c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(5/4), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(5/4),x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\sqrt{a + bx}}{(c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(5/4), x)

[Out] int((a + b*x)^(1/2)/(c + d*x)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a + bx}}{(c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(5/4), x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(5/4), x)

$$3.1662 \quad \int \frac{1}{\sqrt{a+bx} (c+dx)^{5/4}} dx$$

Optimal. Leaf size=197

$$\frac{4\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{d\sqrt{a+bx} \sqrt[4]{bc-ad}} + \frac{4\sqrt{a+bx}}{\sqrt[4]{c+dx} (bc-ad)} - \frac{4\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{d\sqrt{a+bx} \sqrt[4]{bc-ad}}$$

[Out] $4*(b*x+a)^{(1/2)/(-a*d+b*c)/(d*x+c)^{(1/4)}-4*b^{(1/4)*\operatorname{EllipticE}(b^{(1/4)*(d*x+c)^{(1/4)/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)/d/(-a*d+b*c)^{(1/4)/(b*x+a)^{(1/2)+4*b^{(1/4)*\operatorname{EllipticF}(b^{(1/4)*(d*x+c)^{(1/4)/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)/d/(-a*d+b*c)^{(1/4)/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.21, antiderivative size = 197, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{4\sqrt{a+bx}}{\sqrt[4]{c+dx} (bc-ad)} + \frac{4\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{d\sqrt{a+bx} \sqrt[4]{bc-ad}} - \frac{4\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{d\sqrt{a+bx} \sqrt[4]{bc-ad}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(5/4)),x]

[Out] $(4*\operatorname{Sqrt}[a + b*x])/((b*c - a*d)*(c + d*x)^{(1/4)}) - (4*b^{(1/4)*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/((d*(b*c - a*d)^{(1/4)*\operatorname{Sqrt}[a + b*x]) + (4*b^{(1/4)*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/((d*(b*c - a*d)^{(1/4)*\operatorname{Sqrt}[a + b*x])$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +

$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{Simp}[\text{EllipticF}[\text{ArcSin}[(\text{Rt}[-b, 4]*x)/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{GtQ}[a, 0]$

Rule 224

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[\text{Sqrt}[1 + (b*x^4)/a]/\text{Sqrt}[a + b*x^4], \text{Int}[1/\text{Sqrt}[1 + (b*x^4)/a], x], x] /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{!GtQ}[a, 0]$

Rule 307

$\text{Int}[(x_)^2/\text{Sqrt}[(a_) + (b_)*(x_)^4], x_Symbol] \rightarrow \text{With}\{q = \text{Rt}[-(b/a), 2]\}, -\text{Dist}[q^{-1}, \text{Int}[1/\text{Sqrt}[a + b*x^4], x], x] + \text{Dist}[1/q, \text{Int}[(1 + q*x^2)/\text{Sqrt}[a + b*x^4], x], x]] /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a]$

Rule 424

$\text{Int}[\text{Sqrt}[(a_) + (b_)*(x_)^2]/\text{Sqrt}[(c_) + (d_)*(x_)^2], x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[a]*\text{EllipticE}[\text{ArcSin}[\text{Rt}[-(d/c), 2]*x], (b*c)/(a*d)])/(\text{Sqrt}[c]*\text{Rt}[-(d/c), 2]), x] /; \text{FreeQ}\{a, b, c, d\}, x] \ \&\& \ \text{NegQ}[d/c] \ \&\& \ \text{GtQ}[c, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1199

$\text{Int}[(d_) + (e_)*(x_)^2]/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[d/\text{Sqrt}[a], \text{Int}[\text{Sqrt}[1 + (e*x^2)/d]/\text{Sqrt}[1 - (e*x^2)/d], x], x] /; \text{FreeQ}\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{GtQ}[a, 0]$

Rule 1200

$\text{Int}[(d_) + (e_)*(x_)^2]/\text{Sqrt}[(a_) + (c_)*(x_)^4], x_Symbol] \rightarrow \text{Dist}[\text{Sqrt}[1 + (c*x^4)/a]/\text{Sqrt}[a + c*x^4], \text{Int}[(d + e*x^2)/\text{Sqrt}[1 + (c*x^4)/a], x], x] /; \text{FreeQ}\{a, c, d, e\}, x] \ \&\& \ \text{NegQ}[c/a] \ \&\& \ \text{EqQ}[c*d^2 + a*e^2, 0] \ \&\& \ \text{!GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt{a+bx}(c+dx)^{5/4}} dx &= \frac{4\sqrt{a+bx}}{(bc-ad)\sqrt[4]{c+dx}} - \frac{b \int \frac{1}{\sqrt{a+bx}\sqrt[4]{c+dx}} dx}{bc-ad} \\
&= \frac{4\sqrt{a+bx}}{(bc-ad)\sqrt[4]{c+dx}} - \frac{(4b) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{d(bc-ad)} \\
&= \frac{4\sqrt{a+bx}}{(bc-ad)\sqrt[4]{c+dx}} + \frac{(4\sqrt{b}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{d\sqrt{bc-ad}} - \frac{(4\sqrt{b}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{d\sqrt{bc-ad}} \\
&= \frac{4\sqrt{a+bx}}{(bc-ad)\sqrt[4]{c+dx}} + \frac{(4\sqrt{b} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{d\sqrt{bc-ad} \sqrt{a+bx}} - \frac{(4\sqrt{b} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{d\sqrt{bc-ad} \sqrt{a+bx}} \\
&= \frac{4\sqrt{a+bx}}{(bc-ad)\sqrt[4]{c+dx}} + \frac{4\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{d\sqrt[4]{bc-ad} \sqrt{a+bx}} - \frac{(4\sqrt[4]{b} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{d\sqrt[4]{bc-ad} \sqrt{a+bx}} \\
&= \frac{4\sqrt{a+bx}}{(bc-ad)\sqrt[4]{c+dx}} - \frac{4\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{d\sqrt[4]{bc-ad} \sqrt{a+bx}} + \frac{4\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{d\sqrt[4]{bc-ad} \sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.36

$$\frac{2\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(\frac{1}{2}, \frac{5}{4}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(5/4)), x]

[Out] (2*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[1/2, 5/4, 3/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(c + d*x)^(5/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}}{bd^2x^3+ac^2+(2bcd+ad^2)x^2+(bc^2+2acd)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(b*d^2*x^3 + a*c^2 + (2*b*c*d + a*d^2)*x^2 + (b*c^2 + 2*a*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(5/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(5/4),x)

[Out] int(1/(b*x+a)^(1/2)/(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(5/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{\sqrt{a+bx} (c+dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(1/2)*(c + d*x)^(5/4)), x)`

[Out] `int(1/((a + b*x)^(1/2)*(c + d*x)^(5/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a+bx} (c+dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/2)/(d*x+c)**(5/4), x)`

[Out] `Integral(1/(sqrt(a + b*x)*(c + d*x)**(5/4)), x)`

$$3.1663 \quad \int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/4}} dx$$

Optimal. Leaf size=222

$$\frac{6\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{\sqrt{a+bx} (bc-ad)^{5/4}} - \frac{6d\sqrt{a+bx}}{\sqrt[4]{c+dx} (bc-ad)^2} - \frac{2}{\sqrt{a+bx} \sqrt[4]{c+dx} (bc-ad)} + \frac{6\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}}}{\sqrt{a+bx}}$$

[Out] $-2/(-a*d+b*c)/(d*x+c)^{(1/4)}/(b*x+a)^{(1/2)}-6*d*(b*x+a)^{(1/2)}/(-a*d+b*c)^2/(d*x+c)^{(1/4)}+6*b^{(1/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/(-a*d+b*c)^{(5/4)}/(b*x+a)^{(1/2)}-6*b^{(1/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/(-a*d+b*c)^{(5/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.23, antiderivative size = 222, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{6d\sqrt{a+bx}}{\sqrt[4]{c+dx} (bc-ad)^2} - \frac{2}{\sqrt{a+bx} \sqrt[4]{c+dx} (bc-ad)} - \frac{6\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{\sqrt{a+bx} (bc-ad)^{5/4}} + \frac{6\sqrt[4]{b} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/2)*(c + d*x)^(5/4)), x]

[Out] $-2/((b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/4)}) - (6*d*\operatorname{Sqrt}[a + b*x])/((b*c - a*d)^2*(c + d*x)^{(1/4)}) + (6*b^{(1/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/((b*c - a*d)^{(5/4)}*\operatorname{Sqrt}[a + b*x]) - (6*b^{(1/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/((b*c - a*d)^{(5/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt
[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x
] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[
a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/4}} dx &= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}} - \frac{(3d) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/4}} dx}{2(bc-ad)} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}} - \frac{6d\sqrt{a+bx}}{(bc-ad)^2\sqrt[4]{c+dx}} + \frac{(3bd) \int \frac{1}{\sqrt{a+bx}\sqrt[4]{c+dx}} dx}{2(bc-ad)^2} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}} - \frac{6d\sqrt{a+bx}}{(bc-ad)^2\sqrt[4]{c+dx}} + \frac{(6b) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, \right)}{(bc-ad)^2} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}} - \frac{6d\sqrt{a+bx}}{(bc-ad)^2\sqrt[4]{c+dx}} - \frac{(6\sqrt{b}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, \right)}{(bc-ad)^{3/2}} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}} - \frac{6d\sqrt{a+bx}}{(bc-ad)^2\sqrt[4]{c+dx}} - \frac{(6\sqrt{b}\sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, \right)}{(bc-ad)^{3/2}} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}} - \frac{6d\sqrt{a+bx}}{(bc-ad)^2\sqrt[4]{c+dx}} - \frac{6\sqrt[4]{b}\sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b}}{\sqrt[4]{a+bx}} \right) \right)}{(bc-ad)^{5/4}\sqrt{a+bx}} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[4]{c+dx}} - \frac{6d\sqrt{a+bx}}{(bc-ad)^2\sqrt[4]{c+dx}} + \frac{6\sqrt[4]{b}\sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b}}{\sqrt[4]{a+bx}} \right) \right)}{(bc-ad)^{5/4}\sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.32

$$-\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(-\frac{1}{2}, \frac{5}{4}, \frac{1}{2}, \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt{a+bx}(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(5/4)),x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[-1/2, 5/4, 1/2, (d*(a + b*x))/(-b*c + a*d)])/(b*Sqrt[a + b*x]*(c + d*x)^(5/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{3}{4}}}{b^2 d^2 x^4 + a^2 c^2 + 2(b^2 cd + abd^2)x^3 + (b^2 c^2 + 4abcd + a^2 d^2)x^2 + 2(abc^2 + a^2 cd)x', x} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(b^2*d^2*x^4 + a^2*c^2 + 2*(b^2*c*d + a*b*d^2)*x^3 + (b^2*c^2 + 4*a*b*c*d + a^2*d^2)*x^2 + 2*(a*b*c^2 + a^2*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(5/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(5/4),x)

[Out] int(1/(b*x+a)^(3/2)/(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(5/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{3/2} (c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(5/4)), x)

[Out] int(1/((a + b*x)^(3/2)*(c + d*x)^(5/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} (c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(5/4), x)

[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(5/4)), x)

$$3.1664 \quad \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/4}} dx$$

Optimal. Leaf size=261

$$\frac{7\sqrt[4]{b}d\sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{\sqrt{a+bx}(bc-ad)^{9/4}} + \frac{7d^2\sqrt{a+bx}}{\sqrt[4]{c+dx}(bc-ad)^3} + \frac{7d}{3\sqrt{a+bx}\sqrt[4]{c+dx}(bc-ad)^2} - \frac{1}{3(a+bx)}$$

[Out] $-2/3/(-a*d+b*c)/(b*x+a)^{(3/2)}/(d*x+c)^{(1/4)}+7/3*d/(-a*d+b*c)^2/(d*x+c)^{(1/4)}/(b*x+a)^{(1/2)}+7*d^2*(b*x+a)^{(1/2)}/(-a*d+b*c)^3/(d*x+c)^{(1/4)}-7*b^{(1/4)}*d*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/(-a*d+b*c)^{(9/4)}/(b*x+a)^{(1/2)}+7*b^{(1/4)}*d*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/(-a*d+b*c)^{(9/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.26, antiderivative size = 261, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{7d^2\sqrt{a+bx}}{\sqrt[4]{c+dx}(bc-ad)^3} + \frac{7d}{3\sqrt{a+bx}\sqrt[4]{c+dx}(bc-ad)^2} - \frac{2}{3(a+bx)^{3/2}\sqrt[4]{c+dx}(bc-ad)} + \frac{7\sqrt[4]{b}d\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}}{\sqrt[4]{bc-ad}}\right)\right)}{\sqrt{a+bx}(bc-ad)^{9/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a + b*x)^{(5/2)}*(c + d*x)^{(5/4))}, x]$

[Out] $-2/(3*(b*c - a*d)*(a + b*x)^{(3/2)}*(c + d*x)^{(1/4)}) + (7*d)/(3*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/4)}) + (7*d^2*\operatorname{Sqrt}[a + b*x])/((b*c - a*d)^3*(c + d*x)^{(1/4)}) - (7*b^{(1/4)}*d*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/((b*c - a*d)^{(9/4)}*\operatorname{Sqrt}[a + b*x]) + (7*b^{(1/4)}*d*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/((b*c - a*d)^{(9/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}]/((b*c - a*d)*(m + 1)), x] - \operatorname{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, n\}, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{LtQ}[m, -1] \ \&\& \ !(\operatorname{LtQ}[n, -1] \ \&\& \ (\operatorname{EqQ}[a, 0] \ || \ (\operatorname{NeQ}[c, 0] \ \&\& \ \operatorname{LtQ}[m - n, 0] \ \&\& \ \operatorname{IntegerQ}[n]))) \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt
[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x
] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[
a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/4}} dx &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[4]{c+dx}} - \frac{(7d) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/4}} dx}{6(bc-ad)} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[4]{c+dx}} + \frac{7d}{3(bc-ad)^2\sqrt{a+bx}\sqrt[4]{c+dx}} + \frac{(7d^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/4}} dx}{4(bc-ad)} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[4]{c+dx}} + \frac{7d}{3(bc-ad)^2\sqrt{a+bx}\sqrt[4]{c+dx}} + \frac{7d^2\sqrt{a+bx}}{(bc-ad)^3\sqrt[4]{c+dx}} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[4]{c+dx}} + \frac{7d}{3(bc-ad)^2\sqrt{a+bx}\sqrt[4]{c+dx}} + \frac{7d^2\sqrt{a+bx}}{(bc-ad)^3\sqrt[4]{c+dx}} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[4]{c+dx}} + \frac{7d}{3(bc-ad)^2\sqrt{a+bx}\sqrt[4]{c+dx}} + \frac{7d^2\sqrt{a+bx}}{(bc-ad)^3\sqrt[4]{c+dx}} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[4]{c+dx}} + \frac{7d}{3(bc-ad)^2\sqrt{a+bx}\sqrt[4]{c+dx}} + \frac{7d^2\sqrt{a+bx}}{(bc-ad)^3\sqrt[4]{c+dx}} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[4]{c+dx}} + \frac{7d}{3(bc-ad)^2\sqrt{a+bx}\sqrt[4]{c+dx}} + \frac{7d^2\sqrt{a+bx}}{(bc-ad)^3\sqrt[4]{c+dx}} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[4]{c+dx}} + \frac{7d}{3(bc-ad)^2\sqrt{a+bx}\sqrt[4]{c+dx}} + \frac{7d^2\sqrt{a+bx}}{(bc-ad)^3\sqrt[4]{c+dx}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.28

$$\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(-\frac{3}{2}, \frac{5}{4}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(a+bx)^{3/2}(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(5/4)),x]

[Out] $(-2*((b*(c + d*x))/(b*c - a*d))^(5/4)*\text{Hypergeometric2F1}[-3/2, 5/4, -1/2, (d*(a + b*x))/(-(b*c) + a*d)])/(3*b*(a + b*x)^(3/2)*(c + d*x)^(5/4))$

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{3}{4}}}{b^3 d^2 x^5 + a^3 c^2 + (2 b^3 c d + 3 a b^2 d^2) x^4 + (b^3 c^2 + 6 a b^2 c d + 3 a^2 b d^2) x^3 + (3 a b^2 c^2 + 6 a^2 b c d + a^3 d^2) x^2 + \dots} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] $\text{integral}(\text{sqrt}(b*x + a)*(d*x + c)^{(3/4)}/(b^3*d^2*x^5 + a^3*c^2 + (2*b^3*c*d + 3*a*b^2*d^2)*x^4 + (b^3*c^2 + 6*a*b^2*c*d + 3*a^2*b*d^2)*x^3 + (3*a*b^2*c^2 + 6*a^2*b*c*d + a^3*d^2)*x^2 + (3*a^2*b*c^2 + 2*a^3*c*d)*x), x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(5/4)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(5/4),x)

[Out] int(1/(b*x+a)^(5/2)/(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(5/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{5/2} (c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/2)*(c + d*x)^(5/4)),x)

[Out] int(1/((a + b*x)^(5/2)*(c + d*x)^(5/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{5}{2}} (c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(5/4),x)

[Out] Integral(1/((a + b*x)**(5/2)*(c + d*x)**(5/4)), x)

$$3.1665 \quad \int \frac{(a+bx)^{7/2}}{(c+dx)^{7/4}} dx$$

Optimal. Leaf size=207

$$\frac{320b^{3/4}(bc-ad)^{13/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{33d^5 \sqrt{a+bx}} + \frac{160b \sqrt{a+bx} \sqrt[4]{c+dx} (bc-ad)^2}{33d^4} - \frac{80b(a+bx)^{3/2} \sqrt[4]{c+dx}}{33d^3}$$

[Out] $-4/3*(b*x+a)^{(7/2)}/d/(d*x+c)^{(3/4)}-80/33*b*(-a*d+b*c)*(b*x+a)^{(3/2)*(d*x+c)^{(1/4)}/d^3+56/33*b*(b*x+a)^{(5/2)*(d*x+c)^{(1/4)}/d^2+160/33*b*(-a*d+b*c)^2*(d*x+c)^{(1/4)*(b*x+a)^{(1/2)}/d^4-320/33*b^{(3/4)*(-a*d+b*c)^{(13/4)*\operatorname{EllipticF}(b^{(1/4)*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^5/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.14, antiderivative size = 207, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 224, 221}

$$\frac{320b^{3/4}(bc-ad)^{13/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{33d^5 \sqrt{a+bx}} + \frac{56b(a+bx)^{5/2} \sqrt[4]{c+dx}}{33d^2} - \frac{80b(a+bx)^{3/2} \sqrt[4]{c+dx} (bc-ad)}{33d^3}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(7/2)}/(c + d*x)^{(7/4)}, x]$

[Out] $(-4*(a + b*x)^{(7/2)})/(3*d*(c + d*x)^{(3/4)}) + (160*b*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/4)})/(33*d^4) - (80*b*(b*c - a*d)*(a + b*x)^{(3/2)*(c + d*x)^{(1/4)})/(33*d^3) + (56*b*(a + b*x)^{(5/2)*(c + d*x)^{(1/4)})/(33*d^2) - (320*b^{(3/4)*(b*c - a*d)^{(13/4)*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1)]/(33*d^5*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)*((c_. + (d_.)*(x_))^{(n_)}), x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m+1)*(c + d*x)^n}/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)*(c + d*x)^{(n-1)}}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{IntegerQ}[n] \&\& !\operatorname{IntegerQ}[m]) \&\& !(I\operatorname{LeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] || \operatorname{GeQ}[2*n + m + 1, 0])) \& \& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/2}}{(c+dx)^{7/4}} dx &= -\frac{4(a+bx)^{7/2}}{3d(c+dx)^{3/4}} + \frac{(14b) \int \frac{(a+bx)^{5/2}}{(c+dx)^{3/4}} dx}{3d} \\
&= -\frac{4(a+bx)^{7/2}}{3d(c+dx)^{3/4}} + \frac{56b(a+bx)^{5/2} \sqrt[4]{c+dx}}{33d^2} - \frac{(140b(bc-ad)) \int \frac{(a+bx)^{3/2}}{(c+dx)^{3/4}} dx}{33d^2} \\
&= -\frac{4(a+bx)^{7/2}}{3d(c+dx)^{3/4}} - \frac{80b(bc-ad)(a+bx)^{3/2} \sqrt[4]{c+dx}}{33d^3} + \frac{56b(a+bx)^{5/2} \sqrt[4]{c+dx}}{33d^2} + \frac{(40b(bc-ad)) \int \frac{(a+bx)^{1/2}}{(c+dx)^{3/4}} dx}{33d^2} \\
&= -\frac{4(a+bx)^{7/2}}{3d(c+dx)^{3/4}} + \frac{160b(bc-ad)^2 \sqrt{a+bx} \sqrt[4]{c+dx}}{33d^4} - \frac{80b(bc-ad)(a+bx)^{3/2} \sqrt[4]{c+dx}}{33d^3} + \frac{56b(a+bx)^{5/2} \sqrt[4]{c+dx}}{33d^2} \\
&= -\frac{4(a+bx)^{7/2}}{3d(c+dx)^{3/4}} + \frac{160b(bc-ad)^2 \sqrt{a+bx} \sqrt[4]{c+dx}}{33d^4} - \frac{80b(bc-ad)(a+bx)^{3/2} \sqrt[4]{c+dx}}{33d^3} + \frac{56b(a+bx)^{5/2} \sqrt[4]{c+dx}}{33d^2} \\
&= -\frac{4(a+bx)^{7/2}}{3d(c+dx)^{3/4}} + \frac{160b(bc-ad)^2 \sqrt{a+bx} \sqrt[4]{c+dx}}{33d^4} - \frac{80b(bc-ad)(a+bx)^{3/2} \sqrt[4]{c+dx}}{33d^3} + \frac{56b(a+bx)^{5/2} \sqrt[4]{c+dx}}{33d^2} \\
&= -\frac{4(a+bx)^{7/2}}{3d(c+dx)^{3/4}} + \frac{160b(bc-ad)^2 \sqrt{a+bx} \sqrt[4]{c+dx}}{33d^4} - \frac{80b(bc-ad)(a+bx)^{3/2} \sqrt[4]{c+dx}}{33d^3} + \frac{56b(a+bx)^{5/2} \sqrt[4]{c+dx}}{33d^2}
\end{aligned}$$

Mathematica [C] time = 0.08, size = 73, normalized size = 0.35

$$\frac{2(a+bx)^{9/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{7/4} {}_2F_1 \left(\frac{7}{4}, \frac{9}{2}; \frac{11}{2}; \frac{d(a+bx)}{ad-bc} \right)}{9b(c+dx)^{7/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/2)/(c + d*x)^(7/4), x]

[Out] (2*(a + b*x)^(9/2)*((b*(c + d*x))/(b*c - a*d))^(7/4)*Hypergeometric2F1[7/4, 9/2, 11/2, (d*(a + b*x))/(-(b*c) + a*d)]/(9*b*(c + d*x)^(7/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(b^3x^3 + 3ab^2x^2 + 3a^2bx + a^3)\sqrt{bx+a}(dx+c)^{\frac{1}{4}}}{d^2x^2 + 2cdx + c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(7/4),x, algorithm="fricas")

[Out] integral((b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3)*sqrt(b*x + a)*(d*x + c)^(1/4)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{2}}}{(dx + c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(7/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(7/2)/(d*x + c)^(7/4), x)

maple [F] time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{2}}}{(dx + c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/2)/(d*x+c)^(7/4),x)

[Out] int((b*x+a)^(7/2)/(d*x+c)^(7/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{2}}}{(dx + c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(7/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/2)/(d*x + c)^(7/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{7/2}}{(c + dx)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(7/2)/(c + d*x)^(7/4), x)`

[Out] `int((a + b*x)^(7/2)/(c + d*x)^(7/4), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{7}{2}}}{(c + dx)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(7/2)/(d*x+c)**(7/4), x)`

[Out] `Integral((a + b*x)**(7/2)/(c + d*x)**(7/4), x)`

$$3.1666 \quad \int \frac{(a+bx)^{3/2}}{(c+dx)^{7/4}} dx$$

Optimal. Leaf size=137

$$\frac{16b^{3/4}(bc-ad)^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{3d^3 \sqrt{a+bx}} + \frac{8b\sqrt{a+bx} \sqrt[4]{c+dx}}{3d^2} - \frac{4(a+bx)^{3/2}}{3d(c+dx)^{3/4}}$$

[Out] $-4/3*(b*x+a)^{(3/2)}/d/(d*x+c)^{(3/4)}+8/3*b*(d*x+c)^{(1/4)}*(b*x+a)^{(1/2)}/d^2-16/3*b^{(3/4)}*(-a*d+b*c)^{(5/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.08, antiderivative size = 137, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 63, 224, 221}

$$\frac{16b^{3/4}(bc-ad)^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{3d^3 \sqrt{a+bx}} + \frac{8b\sqrt{a+bx} \sqrt[4]{c+dx}}{3d^2} - \frac{4(a+bx)^{3/2}}{3d(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}/(c + d*x)^{(7/4)}, x]$

[Out] $(-4*(a + b*x)^{(3/2)})/(3*d*(c + d*x)^{(3/4)}) + (8*b*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/4)})/(3*d^2) - (16*b^{(3/4)}*(b*c - a*d)^{(5/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)]*\operatorname{EllipticF}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1])/(3*d^3*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{GtQ}[n, 0] \ \&\& \ \operatorname{LtQ}[m, -1] \ \&\& \ !(\operatorname{IntegerQ}[n] \ \&\& \ !\operatorname{IntegerQ}[m]) \ \&\& \ !(\operatorname{ILeQ}[m + n + 2, 0] \ \&\& \ (\operatorname{FractionQ}[m] \ || \ \operatorname{GeQ}[2*n + m + 1, 0])) \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{GtQ}[n, 0] \ \&\& \ \operatorname{NeQ}[m + n + 1, 0] \ \&\& \ !(\operatorname{IGtQ}$

$[m, 0] \&\& (!\text{IntegerQ}[n] \ || \ (\text{GtQ}[m, 0] \ \&\& \ \text{LtQ}[m - n, 0])) \ \&\& \ !\text{ILtQ}[m + n + 2, 0] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\text{Int}[(a_.) + (b_.)(x_)^m)((c_.) + (d_.)(x_)^n), x_Symbol] \text{ :> With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{p(m+1)-1}(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{1/p}], x]] \ /; \text{FreeQ}\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

$\text{Int}[1/\text{Sqrt}[(a_) + (b_.)(x_)^4], x_Symbol] \text{ :> Simp}[\text{EllipticF}[\text{ArcSin}[(\text{Rt}[-b, 4]*x)/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] \ /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{GtQ}[a, 0]$

Rule 224

$\text{Int}[1/\text{Sqrt}[(a_) + (b_.)(x_)^4], x_Symbol] \text{ :> Dist}[\text{Sqrt}[1 + (b*x^4)/a]/\text{Sqrt}[a + b*x^4], \text{Int}[1/\text{Sqrt}[1 + (b*x^4)/a], x], x] \ /; \text{FreeQ}\{a, b\}, x] \ \&\& \ \text{NegQ}[b/a] \ \&\& \ !\text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{(c+dx)^{7/4}} dx &= -\frac{4(a+bx)^{3/2}}{3d(c+dx)^{3/4}} + \frac{(2b) \int \frac{\sqrt{a+bx}}{(c+dx)^{3/4}} dx}{d} \\
&= -\frac{4(a+bx)^{3/2}}{3d(c+dx)^{3/4}} + \frac{8b\sqrt{a+bx} \sqrt[4]{c+dx}}{3d^2} - \frac{(4b(bc-ad)) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{3d^2} \\
&= -\frac{4(a+bx)^{3/2}}{3d(c+dx)^{3/4}} + \frac{8b\sqrt{a+bx} \sqrt[4]{c+dx}}{3d^2} - \frac{(16b(bc-ad)) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{3d^3} \\
&= -\frac{4(a+bx)^{3/2}}{3d(c+dx)^{3/4}} + \frac{8b\sqrt{a+bx} \sqrt[4]{c+dx}}{3d^2} - \frac{(16b(bc-ad)\sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{3d^3\sqrt{a+bx}} \\
&= -\frac{4(a+bx)^{3/2}}{3d(c+dx)^{3/4}} + \frac{8b\sqrt{a+bx} \sqrt[4]{c+dx}}{3d^2} - \frac{16b^{3/4}(bc-ad)^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right)}{3d^3\sqrt{a+bx}} - 1
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.53

$$\frac{2(a+bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{7/4} {}_2F_1 \left(\frac{7}{4}, \frac{5}{2}, \frac{7}{2}, \frac{d(a+bx)}{ad-bc} \right)}{5b(c+dx)^{7/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(7/4), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(7/4)*Hypergeometric2F1[7/4, 5/2, 7/2, (d*(a + b*x))/(-b*c) + a*d])/(5*b*(c + d*x)^(7/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{1}{4}}}{d^2x^2+2cdx+c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(7/4), x, algorithm="fricas")

[Out] $\text{integral}((b*x + a)^{(3/2)}*(d*x + c)^{(1/4)} / (d^2*x^2 + 2*c*d*x + c^2), x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)^{(3/2)} / (d*x+c)^{(7/4)}, x, \text{algorithm}="giac")$

[Out] $\text{integrate}((b*x + a)^{(3/2)} / (d*x + c)^{(7/4)}, x)$

maple [F] time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x+a)^{(3/2)} / (d*x+c)^{(7/4)}, x)$

[Out] $\text{int}((b*x+a)^{(3/2)} / (d*x+c)^{(7/4)}, x)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)^{(3/2)} / (d*x+c)^{(7/4)}, x, \text{algorithm}="maxima")$

[Out] $\text{integrate}((b*x + a)^{(3/2)} / (d*x + c)^{(7/4)}, x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{3/2}}{(c + dx)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^{(3/2)} / (c + d*x)^{(7/4)}, x)$

[Out] $\text{int}((a + b*x)^{(3/2)} / (c + d*x)^{(7/4)}, x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{(c + dx)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/(d*x+c)**(7/4),x)

[Out] Integral((a + b*x)**(3/2)/(c + d*x)**(7/4), x)

$$3.1667 \quad \int \frac{\sqrt{a+bx}}{(c+dx)^{7/4}} dx$$

Optimal. Leaf size=111

$$\frac{8b^{3/4} \sqrt[4]{bc-ad} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{3d^2 \sqrt{a+bx}} - \frac{4\sqrt{a+bx}}{3d(c+dx)^{3/4}}$$

[Out] $-4/3*(b*x+a)^{(1/2)}/d/(d*x+c)^{(3/4)}+8/3*b^{(3/4)}*(-a*d+b*c)^{(1/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^2/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.06, antiderivative size = 111, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 63, 224, 221}

$$\frac{8b^{3/4} \sqrt[4]{bc-ad} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{3d^2 \sqrt{a+bx}} - \frac{4\sqrt{a+bx}}{3d(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[\operatorname{Sqrt}[a + b*x]/(c + d*x)^{(7/4)}, x]$

[Out] $(-4*\operatorname{Sqrt}[a + b*x])/(3*d*(c + d*x)^{(3/4)}) + (8*b^{(3/4)}*(b*c - a*d)^{(1/4)}*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(3*d^2*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{LtQ}[-1, m, 0]$ && $\operatorname{LeQ}[-1, n, 0]$ && $\operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]]$ && $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

`Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]`

Rule 224

`Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]`

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt{a+bx}}{(c+dx)^{7/4}} dx &= -\frac{4\sqrt{a+bx}}{3d(c+dx)^{3/4}} + \frac{(2b) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{3d} \\
 &= -\frac{4\sqrt{a+bx}}{3d(c+dx)^{3/4}} + \frac{(8b) \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{3d^2} \\
 &= -\frac{4\sqrt{a+bx}}{3d(c+dx)^{3/4}} + \frac{(8b\sqrt{\frac{d(a+bx)}{-bc+ad}}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{3d^2\sqrt{a+bx}} \\
 &= -\frac{4\sqrt{a+bx}}{3d(c+dx)^{3/4}} + \frac{8b^{3/4}\sqrt[4]{bc-ad} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{3d^2\sqrt{a+bx}}
 \end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.66

$$\frac{2(a+bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{7/4} {}_2F_1 \left(\frac{3}{2}, \frac{7}{4}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(c+dx)^{7/4}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(7/4), x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(7/4)*Hypergeometric2F1[3/2, 7/4, 5/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(c + d*x)^(7/4))

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{1}{4}}}{d^2x^2+2cdx+c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(7/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/4)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(7/4),x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(7/4), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(7/4),x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(7/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(7/4),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(7/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(7/4), x)

[Out] int((a + b*x)^(1/2)/(c + d*x)^(7/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(7/4), x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(7/4), x)

$$3.1668 \quad \int \frac{1}{\sqrt{a+bx} (c+dx)^{7/4}} dx$$

Optimal. Leaf size=118

$$\frac{4b^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{3d\sqrt{a+bx} (bc-ad)^{3/4}} + \frac{4\sqrt{a+bx}}{3(c+dx)^{3/4}(bc-ad)}$$

[Out] $4/3*(b*x+a)^{(1/2)/(-a*d+b*c)/(d*x+c)^{(3/4)}+4/3*b^{(3/4)*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)/d/(-a*d+b*c)^{(3/4)/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.07, antiderivative size = 118, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {51, 63, 224, 221}

$$\frac{4b^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{3d\sqrt{a+bx} (bc-ad)^{3/4}} + \frac{4\sqrt{a+bx}}{3(c+dx)^{3/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/(\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(7/4)}), x]$

[Out] $(4*\operatorname{Sqrt}[a + b*x])/(3*(b*c - a*d)*(c + d*x)^{(3/4)}) + (4*b^{(3/4)*\operatorname{Sqrt}[-((d*(a + b*x))/(b*c - a*d))] * \operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(3*d*(b*c - a*d)^{(3/4)*\operatorname{Sqrt}[a + b*x])$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}/((b*c - a*d)*(m + 1)), x] - \operatorname{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x] /; \operatorname{FreeQ}\{a, b, c, d, n\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{LtQ}[n, -1] \&\& (\operatorname{EqQ}[a, 0] \mid\mid (\operatorname{NeQ}[c, 0] \&\& \operatorname{LtQ}[m - n, 0] \&\& \operatorname{IntegerQ}[n]))) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /; \operatorname{FreeQ}\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{a+bx}(c+dx)^{7/4}} dx &= \frac{4\sqrt{a+bx}}{3(bc-ad)(c+dx)^{3/4}} + \frac{b \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{3(bc-ad)} \\ &= \frac{4\sqrt{a+bx}}{3(bc-ad)(c+dx)^{3/4}} + \frac{(4b) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{3d(bc-ad)} \\ &= \frac{4\sqrt{a+bx}}{3(bc-ad)(c+dx)^{3/4}} + \frac{\left(4b\sqrt{\frac{d(a+bx)}{-bc+ad}}\right) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{\left(a-\frac{bc}{d}\right)d}}} dx, x, \sqrt[4]{c+dx} \right)}{3d(bc-ad)\sqrt{a+bx}} \\ &= \frac{4\sqrt{a+bx}}{3(bc-ad)(c+dx)^{3/4}} + \frac{4b^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{3d(bc-ad)^{3/4} \sqrt{a+bx}} \end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.60

$$\frac{2\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{7/4} {}_2F_1\left(\frac{1}{2}, \frac{7}{4}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b(c+dx)^{7/4}}$$

Antiderivative was successfully verified.

```
[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(7/4)), x]
```

[Out] $(2\sqrt{a + bx} * ((b(c + dx)) / (b*c - a*d))^{7/4} * \text{Hypergeometric2F1}[1/2, 7/4, 3/2, (d(a + bx)) / (-(b*c) + a*d)]) / (b(c + dx))^{7/4}$

fricas [F] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx + a} (dx + c)^{\frac{1}{4}}}{bd^2x^3 + ac^2 + (2bcd + ad^2)x^2 + (bc^2 + 2acd)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(1/2)/(d*x+c)^(7/4),x, algorithm="fricas")`

[Out] `integral(sqrt(b*x + a)*(d*x + c)^(1/4)/(b*d^2*x^3 + a*c^2 + (2*b*c*d + a*d^2)*x^2 + (b*c^2 + 2*a*c*d)*x), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx + a} (dx + c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(1/2)/(d*x+c)^(7/4),x, algorithm="giac")`

[Out] `integrate(1/(sqrt(b*x + a)*(d*x + c)^(7/4)), x)`

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx + a} (dx + c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(1/2)/(d*x+c)^(7/4),x)`

[Out] `int(1/(b*x+a)^(1/2)/(d*x+c)^(7/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx + a} (dx + c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(1/2)/(d*x+c)^(7/4),x, algorithm="maxima")`

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(7/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{\sqrt{a + bx} (c + dx)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/2)*(c + d*x)^(7/4)), x)

[Out] int(1/((a + b*x)^(1/2)*(c + d*x)^(7/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a + bx} (c + dx)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/2)/(d*x+c)**(7/4), x)

[Out] Integral(1/(sqrt(a + b*x)*(c + d*x)**(7/4)), x)

$$3.1669 \quad \int \frac{1}{(a+bx)^{3/2}(c+dx)^{7/4}} dx$$

Optimal. Leaf size=146

$$\frac{10b^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{3\sqrt{a+bx}(bc-ad)^{7/4}} - \frac{10d\sqrt{a+bx}}{3(c+dx)^{3/4}(bc-ad)^2} - \frac{2}{\sqrt{a+bx}(c+dx)^{3/4}(bc-ad)}$$

[Out] $-2/(-a*d+b*c)/(d*x+c)^{(3/4)}/(b*x+a)^{(1/2)}-10/3*d*(b*x+a)^{(1/2)}/(-a*d+b*c)^2/(d*x+c)^{(3/4)}-10/3*b^{(3/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/(-a*d+b*c)^{(7/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.08, antiderivative size = 146, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {51, 63, 224, 221}

$$\frac{10b^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{3\sqrt{a+bx}(bc-ad)^{7/4}} - \frac{10d\sqrt{a+bx}}{3(c+dx)^{3/4}(bc-ad)^2} - \frac{2}{\sqrt{a+bx}(c+dx)^{3/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a + b*x)^{(3/2)}*(c + d*x)^{(7/4))}, x]$

[Out] $-2/((b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)}) - (10*d*\operatorname{Sqrt}[a + b*x])/(3*(b*c - a*d)^2*(c + d*x)^{(3/4)}) - (10*b^{(3/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/(3*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^{(n+1)}/((b*c - a*d)*(m+1)), x] - \operatorname{Dist}[(d*(m+n+2))/((b*c - a*d)*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^n, x] /; \operatorname{FreeQ}\{a, b, c, d, n\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{LtQ}[n, -1] \&\& (\operatorname{EqQ}[a, 0] \mid\mid (\operatorname{NeQ}[c, 0] \&\& \operatorname{LtQ}[m - n, 0] \&\& \operatorname{IntegerQ}[n]))) \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /; \operatorname{FreeQ}\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Den}$

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{3/2}(c+dx)^{7/4}} dx &= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}} - \frac{(5d) \int \frac{1}{\sqrt{a+bx}(c+dx)^{7/4}} dx}{2(bc-ad)} \\
 &= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}} - \frac{10d\sqrt{a+bx}}{3(bc-ad)^2(c+dx)^{3/4}} - \frac{(5bd) \int \frac{1}{\sqrt{a+bx}(c+dx)^{3/4}} dx}{6(bc-ad)^2} \\
 &= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}} - \frac{10d\sqrt{a+bx}}{3(bc-ad)^2(c+dx)^{3/4}} - \frac{(10b) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx \right)}{3(bc-ad)} \\
 &= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}} - \frac{10d\sqrt{a+bx}}{3(bc-ad)^2(c+dx)^{3/4}} - \frac{(10b\sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx \right)}{3(bc-ad)} \\
 &= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}} - \frac{10d\sqrt{a+bx}}{3(bc-ad)^2(c+dx)^{3/4}} - \frac{10b^{3/4} \sqrt{\frac{d(a+bx)}{-bc-ad}} F \left(\sin^{-1} \right)}{3(bc-ad)^{7/4} \sqrt{a+bx}}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.49

$$-\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{7/4} {}_2F_1 \left(-\frac{1}{2}, \frac{7}{4}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt{a+bx}(c+dx)^{7/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(7/4)),x]

[Out] $(-2*((b*(c + d*x))/(b*c - a*d))^(7/4)*\text{Hypergeometric2F1}[-1/2, 7/4, 1/2, (d*(a + b*x))/(-(b*c) + a*d)])/(b*\text{Sqrt}[a + b*x]*(c + d*x)^(7/4))$

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{1}{4}}}{b^2d^2x^4+a^2c^2+2(b^2cd+abd^2)x^3+(b^2c^2+4abcd+a^2d^2)x^2+2(abc^2+a^2cd)x},x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(7/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/4)/(b^2*d^2*x^4 + a^2*c^2 + 2*(b^2*c*d + a*b*d^2)*x^3 + (b^2*c^2 + 4*a*b*c*d + a^2*d^2)*x^2 + 2*(a*b*c^2 + a^2*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(7/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(7/4)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(7/4),x)

[Out] int(1/(b*x+a)^(3/2)/(d*x+c)^(7/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(7/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(7/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{3/2} (c + dx)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(7/4)),x)

[Out] int(1/((a + b*x)^(3/2)*(c + d*x)^(7/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} (c + dx)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(7/4),x)

[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(7/4)), x)

$$3.1670 \quad \int \frac{1}{(a+bx)^{5/2}(c+dx)^{7/4}} dx$$

Optimal. Leaf size=178

$$\frac{5b^{3/4}d\sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{\sqrt{a+bx}(bc-ad)^{11/4}} + \frac{5d^2\sqrt{a+bx}}{(c+dx)^{3/4}(bc-ad)^3} + \frac{3d}{\sqrt{a+bx}(c+dx)^{3/4}(bc-ad)^2} - \frac{1}{3(a+bx)^{3/2}}$$

[Out] $-2/3/(-a*d+b*c)/(b*x+a)^{(3/2)}/(d*x+c)^{(3/4)}+3*d/(-a*d+b*c)^2/(d*x+c)^{(3/4)}/(b*x+a)^{(1/2)}+5*d^2*(b*x+a)^{(1/2)}/(-a*d+b*c)^3/(d*x+c)^{(3/4)}+5*b^{(3/4)}*d*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/(-a*d+b*c)^{(11/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.10, antiderivative size = 178, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {51, 63, 224, 221}

$$\frac{5b^{3/4}d\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{\sqrt{a+bx}(bc-ad)^{11/4}} + \frac{5d^2\sqrt{a+bx}}{(c+dx)^{3/4}(bc-ad)^3} + \frac{3d}{\sqrt{a+bx}(c+dx)^{3/4}(bc-ad)^2} - \frac{1}{3(a+bx)^{3/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a + b*x)^{(5/2)}*(c + d*x)^{(7/4))}, x]$

[Out] $-2/(3*(b*c - a*d)*(a + b*x)^{(3/2)}*(c + d*x)^{(3/4)}) + (3*d)/((b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)}) + (5*d^2*\operatorname{Sqrt}[a + b*x])/((b*c - a*d)^3*(c + d*x)^{(3/4)}) + (5*b^{(3/4)}*d*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/((b*c - a*d)^{(11/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}/((b*c - a*d)*(m + 1)), x] - \operatorname{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, n\}, x\} \ \&\& \ \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \ \operatorname{LtQ}[m, -1] \ \&\& \ !(\operatorname{LtQ}[n, -1] \ \&\& \ (\operatorname{EqQ}[a, 0] \ || \ (\operatorname{NeQ}[c, 0] \ \&\& \ \operatorname{LtQ}[m - n, 0] \ \&\& \ \operatorname{IntegerQ}[n]))) \ \&\& \ \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x\} \ \&\& \ \operatorname{NeQ}$

`[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 221

`Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]`

Rule 224

`Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]`

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{5/2}(c+dx)^{7/4}} dx &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}} - \frac{(3d) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{7/4}} dx}{2(bc-ad)} \\
 &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}} + \frac{3d}{(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}} + \frac{(15d^2) \int \frac{1}{\sqrt{a+bx}}}{4(bc-ad)} \\
 &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}} + \frac{3d}{(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}} + \frac{5d^2 \sqrt{a+bx}}{(bc-ad)^3 (c+dx)} \\
 &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}} + \frac{3d}{(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}} + \frac{5d^2 \sqrt{a+bx}}{(bc-ad)^3 (c+dx)} \\
 &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}} + \frac{3d}{(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}} + \frac{5d^2 \sqrt{a+bx}}{(bc-ad)^3 (c+dx)} \\
 &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}(c+dx)^{3/4}} + \frac{3d}{(bc-ad)^2 \sqrt{a+bx} (c+dx)^{3/4}} + \frac{5d^2 \sqrt{a+bx}}{(bc-ad)^3 (c+dx)}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.41

$$\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{7/4} {}_2F_1 \left(-\frac{3}{2}, \frac{7}{4}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(a+bx)^{3/2}(c+dx)^{7/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(7/4)), x]

[Out] $(-2*((b*(c + d*x))/(b*c - a*d))^(7/4)*\text{Hypergeometric2F1}[-3/2, 7/4, -1/2, (d*(a + b*x))/(-(b*c) + a*d)])/(3*b*(a + b*x)^(3/2)*(c + d*x)^(7/4))$

fricas [F] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a}(dx+c)^{\frac{1}{4}}}{b^3d^2x^5 + a^3c^2 + (2b^3cd + 3ab^2d^2)x^4 + (b^3c^2 + 6ab^2cd + 3a^2bd^2)x^3 + (3ab^2c^2 + 6a^2bcd + a^3d^2)x^2 + \dots} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(7/4), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/4)/(b^3*d^2*x^5 + a^3*c^2 + (2*b^3*c*d + 3*a*b^2*d^2)*x^4 + (b^3*c^2 + 6*a*b^2*c*d + 3*a^2*b*d^2)*x^3 + (3*a*b^2*c^2 + 6*a^2*b*c*d + a^3*d^2)*x^2 + (3*a^2*b*c^2 + 2*a^3*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(7/4), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(7/4)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(7/4), x)

[Out] `int(1/(b*x+a)^(5/2)/(d*x+c)^(7/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/2)/(d*x+c)^(7/4),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(5/2)*(d*x + c)^(7/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{5/2}(c+dx)^{7/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(5/2)*(c + d*x)^(7/4)),x)`

[Out] `int(1/((a + b*x)^(5/2)*(c + d*x)^(7/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{2}}(c+dx)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/2)/(d*x+c)**(7/4),x)`

[Out] `Integral(1/((a + b*x)**(5/2)*(c + d*x)**(7/4)), x)`

$$3.1671 \quad \int \frac{(a+bx)^{7/2}}{(c+dx)^{9/4}} dx$$

Optimal. Leaf size=286

$$\frac{448b^{5/4}(bc-ad)^{11/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}\operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right),-1\right)}{15d^5\sqrt{a+bx}} + \frac{448b^{5/4}(bc-ad)^{11/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{15d^5\sqrt{a+bx}}$$

[Out] $-4/5*(b*x+a)^{(7/2)}/d/(d*x+c)^{(5/4)}-56/5*b*(b*x+a)^{(5/2)}/d^2/(d*x+c)^{(1/4)}+12/9*b^2*(b*x+a)^{(3/2)}*(d*x+c)^{(3/4)}/d^3-224/15*b^2*(-a*d+b*c)*(d*x+c)^{(3/4)}*(b*x+a)^{(1/2)}/d^4+448/15*b^{(5/4)}*(-a*d+b*c)^{(11/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)},I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^5/(b*x+a)^{(1/2)}-448/15*b^{(5/4)}*(-a*d+b*c)^{(11/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)},I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^5/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.30, antiderivative size = 286, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 50, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{112b^2(a+bx)^{3/2}(c+dx)^{3/4}}{9d^3} - \frac{224b^2\sqrt{a+bx}(c+dx)^{3/4}(bc-ad)}{15d^4} - \frac{448b^{5/4}(bc-ad)^{11/4}\sqrt{-\frac{d(a+bx)}{bc-ad}}F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{15d^5\sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a+b*x)^{(7/2)}/(c+d*x)^{(9/4)},x]$

[Out] $(-4*(a+b*x)^{(7/2)})/(5*d*(c+d*x)^{(5/4)}) - (56*b*(a+b*x)^{(5/2)})/(5*d^2*(c+d*x)^{(1/4)}) - (224*b^2*(b*c-a*d)*\operatorname{Sqrt}[a+b*x]*(c+d*x)^{(3/4)})/(15*d^4) + (112*b^2*(a+b*x)^{(3/2)}*(c+d*x)^{(3/4)})/(9*d^3) + (448*b^{(5/4)}*(b*c-a*d)^{(11/4)}*\operatorname{Sqrt}[-((d*(a+b*x))/(b*c-a*d))]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c+d*x)^{(1/4)})/(b*c-a*d)^{(1/4)}],-1])/(15*d^5*\operatorname{Sqrt}[a+b*x]) - (448*b^{(5/4)}*(b*c-a*d)^{(11/4)}*\operatorname{Sqrt}[-((d*(a+b*x))/(b*c-a*d))]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c+d*x)^{(1/4)})/(b*c-a*d)^{(1/4)}],-1])/(15*d^5*\operatorname{Sqrt}[a+b*x])$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ & $\operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
```


$d, e\}, x] \&\& \text{NegQ}[c/a] \&\& \text{EqQ}[c*d^2 + a*e^2, 0] \&\& \text{GtQ}[a, 0]$

Rule 1200

$\text{Int}[\frac{(d_.) + (e_.)*(x_)^2}{\text{Sqrt}[(a_) + (c_.)*(x_)^4]}, x_Symbol] \rightarrow \text{Dist}[\text{Sqrt}[1 + (c*x^4)/a]/\text{Sqrt}[a + c*x^4], \text{Int}[(d + e*x^2)/\text{Sqrt}[1 + (c*x^4)/a], x], x]$ /; $\text{FreeQ}[\{a, c, d, e\}, x] \&\& \text{NegQ}[c/a] \&\& \text{EqQ}[c*d^2 + a*e^2, 0] \&\& \text{!GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/2}}{(c+dx)^{9/4}} dx &= -\frac{4(a+bx)^{7/2}}{5d(c+dx)^{5/4}} + \frac{(14b) \int \frac{(a+bx)^{5/2}}{(c+dx)^{5/4}} dx}{5d} \\
&= -\frac{4(a+bx)^{7/2}}{5d(c+dx)^{5/4}} - \frac{56b(a+bx)^{5/2}}{5d^2\sqrt[4]{c+dx}} + \frac{(28b^2) \int \frac{(a+bx)^{3/2}}{\sqrt[4]{c+dx}} dx}{d^2} \\
&= -\frac{4(a+bx)^{7/2}}{5d(c+dx)^{5/4}} - \frac{56b(a+bx)^{5/2}}{5d^2\sqrt[4]{c+dx}} + \frac{112b^2(a+bx)^{3/2}(c+dx)^{3/4}}{9d^3} - \frac{(56b^2(bc-ad)) \int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx}{3d^3} \\
&= -\frac{4(a+bx)^{7/2}}{5d(c+dx)^{5/4}} - \frac{56b(a+bx)^{5/2}}{5d^2\sqrt[4]{c+dx}} - \frac{224b^2(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^4} + \frac{112b^2(a+bx)^{3/2}(c+dx)^{3/4}}{9d^3} \\
&= -\frac{4(a+bx)^{7/2}}{5d(c+dx)^{5/4}} - \frac{56b(a+bx)^{5/2}}{5d^2\sqrt[4]{c+dx}} - \frac{224b^2(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^4} + \frac{112b^2(a+bx)^{3/2}(c+dx)^{3/4}}{9d^3} \\
&= -\frac{4(a+bx)^{7/2}}{5d(c+dx)^{5/4}} - \frac{56b(a+bx)^{5/2}}{5d^2\sqrt[4]{c+dx}} - \frac{224b^2(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^4} + \frac{112b^2(a+bx)^{3/2}(c+dx)^{3/4}}{9d^3} \\
&= -\frac{4(a+bx)^{7/2}}{5d(c+dx)^{5/4}} - \frac{56b(a+bx)^{5/2}}{5d^2\sqrt[4]{c+dx}} - \frac{224b^2(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^4} + \frac{112b^2(a+bx)^{3/2}(c+dx)^{3/4}}{9d^3} \\
&= -\frac{4(a+bx)^{7/2}}{5d(c+dx)^{5/4}} - \frac{56b(a+bx)^{5/2}}{5d^2\sqrt[4]{c+dx}} - \frac{224b^2(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^4} + \frac{112b^2(a+bx)^{3/2}(c+dx)^{3/4}}{9d^3} \\
&= -\frac{4(a+bx)^{7/2}}{5d(c+dx)^{5/4}} - \frac{56b(a+bx)^{5/2}}{5d^2\sqrt[4]{c+dx}} - \frac{224b^2(bc-ad)\sqrt{a+bx}(c+dx)^{3/4}}{15d^4} + \frac{112b^2(a+bx)^{3/2}(c+dx)^{3/4}}{9d^3}
\end{aligned}$$

Mathematica [C] time = 0.09, size = 73, normalized size = 0.26

$$\frac{2(a+bx)^{9/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{9/4} {}_2F_1 \left(\frac{9}{4}, \frac{9}{2}; \frac{11}{2}; \frac{d(a+bx)}{ad-bc} \right)}{9b(c+dx)^{9/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/2)/(c + d*x)^(9/4), x]

[Out] (2*(a + b*x)^(9/2)*((b*(c + d*x))/(b*c - a*d))^(9/4)*Hypergeometric2F1[9/4, 9/2, 11/2, (d*(a + b*x))/(-b*c + a*d)])/(9*b*(c + d*x)^(9/4))

fricas [F] time = 0.53, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(b^3 x^3 + 3 a b^2 x^2 + 3 a^2 b x + a^3) \sqrt{b x + a} (d x + c)^{\frac{3}{4}}}{d^3 x^3 + 3 c d^2 x^2 + 3 c^2 d x + c^3}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(9/4), x, algorithm="fricas")

[Out] integral((b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3)*sqrt(b*x + a)*(d*x + c)^(3/4)/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(b x + a)^{\frac{7}{2}}}{(d x + c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/2)/(d*x+c)^(9/4), x, algorithm="giac")

[Out] integrate((b*x + a)^(7/2)/(d*x + c)^(9/4), x)

maple [F] time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{(b x + a)^{\frac{7}{2}}}{(d x + c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/2)/(d*x+c)^(9/4), x)

[Out] int((b*x+a)^(7/2)/(d*x+c)^(9/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(b x + a)^{\frac{7}{2}}}{(d x + c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(7/2)/(d*x+c)^(9/4),x, algorithm="maxima")
```

```
[Out] integrate((b*x + a)^(7/2)/(d*x + c)^(9/4), x)
```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + b x)^{7/2}}{(c + d x)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(7/2)/(c + d*x)^(9/4),x)
```

```
[Out] int((a + b*x)^(7/2)/(c + d*x)^(9/4), x)
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(7/2)/(d*x+c)**(9/4),x)
```

```
[Out] Timed out
```

$$3.1672 \quad \int \frac{(a+bx)^{5/2}}{(c+dx)^{9/4}} dx$$

Optimal. Leaf size=248

$$\frac{96b^{5/4}(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{5d^4 \sqrt{a+bx}} - \frac{96b^{5/4}(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{5d^4 \sqrt{a+bx}}$$

[Out] $-4/5*(b*x+a)^{(5/2)}/d/(d*x+c)^{(5/4)}-8*b*(b*x+a)^{(3/2)}/d^2/(d*x+c)^{(1/4)}+48/5*b^2*(d*x+c)^{(3/4)}*(b*x+a)^{(1/2)}/d^3-96/5*b^{(5/4)}*(-a*d+b*c)^{(7/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^4/(b*x+a)^{(1/2)}+96/5*b^{(5/4)}*(-a*d+b*c)^{(7/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^4/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.26, antiderivative size = 248, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 50, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{48b^2 \sqrt{a+bx} (c+dx)^{3/4}}{5d^3} + \frac{96b^{5/4}(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5d^4 \sqrt{a+bx}} - \frac{96b^{5/4}(bc-ad)^{7/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{5d^4 \sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}/(c + d*x)^{(9/4)}, x]$

[Out] $(-4*(a + b*x)^{(5/2)})/(5*d*(c + d*x)^{(5/4)}) - (8*b*(a + b*x)^{(3/2)})/(d^2*(c + d*x)^{(1/4)}) + (48*b^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(3/4)})/(5*d^3) - (96*b^{(5/4)}*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1)]/(5*d^4*\operatorname{Sqrt}[a + b*x]) + (96*b^{(5/4)}*(b*c - a*d)^{(7/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1)]/(5*d^4*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x] := \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^{(m+1)}*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\} \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& !(\operatorname{IntegerQ}[n] \&\& !\operatorname{IntegerQ}[m]) \&\& !(I\operatorname{LeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0])) \& \& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]},
-Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{5/2}}{(c+dx)^{9/4}} dx &= -\frac{4(a+bx)^{5/2}}{5d(c+dx)^{5/4}} + \frac{(2b) \int \frac{(a+bx)^{3/2}}{(c+dx)^{5/4}} dx}{d} \\
 &= -\frac{4(a+bx)^{5/2}}{5d(c+dx)^{5/4}} - \frac{8b(a+bx)^{3/2}}{d^2 \sqrt[4]{c+dx}} + \frac{(12b^2) \int \frac{\sqrt{a+bx}}{\sqrt[4]{c+dx}} dx}{d^2} \\
 &= -\frac{4(a+bx)^{5/2}}{5d(c+dx)^{5/4}} - \frac{8b(a+bx)^{3/2}}{d^2 \sqrt[4]{c+dx}} + \frac{48b^2 \sqrt{a+bx} (c+dx)^{3/4}}{5d^3} - \frac{(24b^2(bc-ad)) \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{5d^3} \\
 &= -\frac{4(a+bx)^{5/2}}{5d(c+dx)^{5/4}} - \frac{8b(a+bx)^{3/2}}{d^2 \sqrt[4]{c+dx}} + \frac{48b^2 \sqrt{a+bx} (c+dx)^{3/4}}{5d^3} - \frac{(96b^2(bc-ad)) \text{Subst} \left(\int \frac{x}{\sqrt{a-\frac{b}{c}x^2}} dx \right)}{5d^4} \\
 &= -\frac{4(a+bx)^{5/2}}{5d(c+dx)^{5/4}} - \frac{8b(a+bx)^{3/2}}{d^2 \sqrt[4]{c+dx}} + \frac{48b^2 \sqrt{a+bx} (c+dx)^{3/4}}{5d^3} + \frac{(96b^{3/2}(bc-ad)^{3/2}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{b}{c}x^2}} dx \right)}{5d^4} \\
 &= -\frac{4(a+bx)^{5/2}}{5d(c+dx)^{5/4}} - \frac{8b(a+bx)^{3/2}}{d^2 \sqrt[4]{c+dx}} + \frac{48b^2 \sqrt{a+bx} (c+dx)^{3/4}}{5d^3} + \frac{(96b^{3/2}(bc-ad)^{3/2} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{b}{c}x^2}} dx \right)}{5d^4} \\
 &= -\frac{4(a+bx)^{5/2}}{5d(c+dx)^{5/4}} - \frac{8b(a+bx)^{3/2}}{d^2 \sqrt[4]{c+dx}} + \frac{48b^2 \sqrt{a+bx} (c+dx)^{3/4}}{5d^3} + \frac{96b^{5/4}(bc-ad)^{7/4} \sqrt{\frac{d(a+bx)}{bc-ad}} F \left(\int \frac{1}{\sqrt{a-\frac{b}{c}x^2}} dx \right)}{5d^4 \sqrt{a+bx}} \\
 &= -\frac{4(a+bx)^{5/2}}{5d(c+dx)^{5/4}} - \frac{8b(a+bx)^{3/2}}{d^2 \sqrt[4]{c+dx}} + \frac{48b^2 \sqrt{a+bx} (c+dx)^{3/4}}{5d^3} - \frac{96b^{5/4}(bc-ad)^{7/4} \sqrt{\frac{d(a+bx)}{bc-ad}} E \left(\int \frac{1}{\sqrt{a-\frac{b}{c}x^2}} dx \right)}{5d^4 \sqrt{a+bx}}
 \end{aligned}$$

Mathematica [C] time = 0.07, size = 73, normalized size = 0.29

$$\frac{2(a + bx)^{7/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{9/4} {}_2F_1 \left(\frac{9}{4}, \frac{7}{2}; \frac{9}{2}; \frac{d(a+bx)}{ad-bc} \right)}{7b(c + dx)^{9/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/(c + d*x)^(9/4), x]

[Out] (2*(a + b*x)^(7/2)*((b*(c + d*x))/(b*c - a*d))^(9/4)*Hypergeometric2F1[9/4, 7/2, 9/2, (d*(a + b*x))/(-b*c) + a*d])/(7*b*(c + d*x)^(9/4))

fricas [F] time = 0.53, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(b^2x^2 + 2abx + a^2)\sqrt{bx + a}(dx + c)^{\frac{3}{4}}}{d^3x^3 + 3cd^2x^2 + 3c^2dx + c^3}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(9/4), x, algorithm="fricas")

[Out] integral((b^2*x^2 + 2*a*b*x + a^2)*sqrt(b*x + a)*(d*x + c)^(3/4)/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(9/4), x, algorithm="giac")

[Out] integrate((b*x + a)^(5/2)/(d*x + c)^(9/4), x)

maple [F] time = 0.14, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/(d*x+c)^(9/4), x)

[Out] `int((b*x+a)^(5/2)/(d*x+c)^(9/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{2}}}{(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(5/2)/(d*x+c)^(9/4),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(5/2)/(d*x + c)^(9/4), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a+bx)^{5/2}}{(c+dx)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(5/2)/(c + d*x)^(9/4),x)`

[Out] `int((a + b*x)^(5/2)/(c + d*x)^(9/4), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(5/2)/(d*x+c)**(9/4),x)`

[Out] Timed out

$$3.1673 \quad \int \frac{(a+bx)^{3/2}}{(c+dx)^{9/4}} dx$$

Optimal. Leaf size=222

$$\frac{48b^{5/4}(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{5d^3 \sqrt{a+bx}} + \frac{48b^{5/4}(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right)}{5d^3 \sqrt{a+bx}}$$

[Out] $-4/5*(b*x+a)^{(3/2)}/d/(d*x+c)^{(5/4)}-24/5*b*(b*x+a)^{(1/2)}/d^2/(d*x+c)^{(1/4)}+8/5*b^{(5/4)*(-a*d+b*c)^{(3/4)}*EllipticE(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^3/(b*x+a)^{(1/2)}-48/5*b^{(5/4)*(-a*d+b*c)^{(3/4)}*EllipticF(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^3/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.23, antiderivative size = 222, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {47, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{48b^{5/4}(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5d^3 \sqrt{a+bx}} + \frac{48b^{5/4}(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5d^3 \sqrt{a+bx}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}/(c + d*x)^{(9/4)}, x]$

[Out] $(-4*(a + b*x)^{(3/2)})/(5*d*(c + d*x)^{(5/4)}) - (24*b*\operatorname{Sqrt}[a + b*x])/(5*d^2*(c + d*x)^{(1/4)}) + (48*b^{(5/4)}*(b*c - a*d)^{(3/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*EllipticE[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(5*d^3*\operatorname{Sqrt}[a + b*x]) - (48*b^{(5/4)}*(b*c - a*d)^{(3/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*EllipticF[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(5*d^3*\operatorname{Sqrt}[a + b*x])$

Rule 47

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+1)), x] - \operatorname{Dist}[(d*n)/(b*(m+1)), \operatorname{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, x\}$ && $\operatorname{NeQ}[b*c - a*d, 0]$ && $\operatorname{GtQ}[n, 0]$ && $\operatorname{LtQ}[m, -1]$ && $!(\operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m])$ && $!(\operatorname{ILeQ}[m + n + 2, 0] \&\& (\operatorname{FractionQ}[m] \mid\mid \operatorname{GeQ}[2*n + m + 1, 0]))$ && $\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt
[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x
] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[
a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{(c+dx)^{9/4}} dx &= -\frac{4(a+bx)^{3/2}}{5d(c+dx)^{5/4}} + \frac{(6b) \int \frac{\sqrt{a+bx}}{(c+dx)^{5/4}} dx}{5d} \\
&= -\frac{4(a+bx)^{3/2}}{5d(c+dx)^{5/4}} - \frac{24b\sqrt{a+bx}}{5d^2\sqrt[4]{c+dx}} + \frac{(12b^2) \int \frac{1}{\sqrt{a+bx}\sqrt[4]{c+dx}} dx}{5d^2} \\
&= -\frac{4(a+bx)^{3/2}}{5d(c+dx)^{5/4}} - \frac{24b\sqrt{a+bx}}{5d^2\sqrt[4]{c+dx}} + \frac{(48b^2) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d^3} \\
&= -\frac{4(a+bx)^{3/2}}{5d(c+dx)^{5/4}} - \frac{24b\sqrt{a+bx}}{5d^2\sqrt[4]{c+dx}} - \frac{(48b^{3/2}\sqrt{bc-ad}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d^3} + \dots \\
&= -\frac{4(a+bx)^{3/2}}{5d(c+dx)^{5/4}} - \frac{24b\sqrt{a+bx}}{5d^2\sqrt[4]{c+dx}} - \frac{(48b^{3/2}\sqrt{bc-ad} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d^3\sqrt{a+bx}} \\
&= -\frac{4(a+bx)^{3/2}}{5d(c+dx)^{5/4}} - \frac{24b\sqrt{a+bx}}{5d^2\sqrt[4]{c+dx}} - \frac{48b^{5/4}(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{5d^3\sqrt{a+bx}} + \dots \\
&= -\frac{4(a+bx)^{3/2}}{5d(c+dx)^{5/4}} - \frac{24b\sqrt{a+bx}}{5d^2\sqrt[4]{c+dx}} + \frac{48b^{5/4}(bc-ad)^{3/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{5d^3\sqrt{a+bx}} - \dots
\end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.33

$$\frac{2(a+bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{9/4} {}_2F_1 \left(\frac{9}{4}, \frac{5}{2}, \frac{7}{2}, \frac{d(a+bx)}{ad-bc} \right)}{5b(c+dx)^{9/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(9/4), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(9/4)*Hypergeometric2F1[9/4, 5/2, 7/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(c + d*x)^(9/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{3}{4}}}{d^3x^3+3cd^2x^2+3c^2dx+c^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(9/4),x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)*(d*x + c)^(3/4)/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(9/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(9/4), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(9/4),x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(9/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(9/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(9/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{3/2}}{(c + dx)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/(c + d*x)^(9/4), x)

[Out] int((a + b*x)^(3/2)/(c + d*x)^(9/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{(c + dx)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/(d*x+c)**(9/4), x)

[Out] Integral((a + b*x)**(3/2)/(c + d*x)**(9/4), x)

$$3.1674 \quad \int \frac{\sqrt{a+bx}}{(c+dx)^{9/4}} dx$$

Optimal. Leaf size=232

$$\frac{8b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{5d^2 \sqrt{a+bx} \sqrt[4]{bc-ad}} - \frac{8b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5d^2 \sqrt{a+bx} \sqrt[4]{bc-ad}} + \frac{8b\sqrt{a+bx}}{5d\sqrt[4]{c+dx}(bc-dx)}$$

[Out] $-4/5*(b*x+a)^{(1/2)}/d/(d*x+c)^{(5/4)}+8/5*b*(b*x+a)^{(1/2)}/d/(-a*d+b*c)/(d*x+c)^{(1/4)}-8/5*b^{(5/4)}*EllipticE(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^2/(-a*d+b*c)^{(1/4)}/(b*x+a)^{(1/2)}+8/5*b^{(5/4)}*EllipticF(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/d^2/(-a*d+b*c)^{(1/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.23, antiderivative size = 232, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{8b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5d^2 \sqrt{a+bx} \sqrt[4]{bc-ad}} - \frac{8b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5d^2 \sqrt{a+bx} \sqrt[4]{bc-ad}} + \frac{8b\sqrt{a+bx}}{5d\sqrt[4]{c+dx}(bc-dx)} - \frac{4}{5d}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/(c + d*x)^(9/4), x]

[Out] $(-4*\operatorname{Sqrt}[a + b*x])/(5*d*(c + d*x)^{(5/4)}) + (8*b*\operatorname{Sqrt}[a + b*x])/(5*d*(b*c - a*d)*(c + d*x)^{(1/4)}) - (8*b^{(5/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*EllipticE[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/(5*d^2*(b*c - a*d)^{(1/4)}*\operatorname{Sqrt}[a + b*x]) + (8*b^{(5/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*EllipticF[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/(5*d^2*(b*c - a*d)^{(1/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]},
-Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)]/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```


Rule 1200

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{\sqrt{a+bx}}{(c+dx)^{9/4}} dx &= -\frac{4\sqrt{a+bx}}{5d(c+dx)^{5/4}} + \frac{(2b) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/4}} dx}{5d} \\
 &= -\frac{4\sqrt{a+bx}}{5d(c+dx)^{5/4}} + \frac{8b\sqrt{a+bx}}{5d(bc-ad)\sqrt[4]{c+dx}} - \frac{(2b^2) \int \frac{1}{\sqrt{a+bx}\sqrt[4]{c+dx}} dx}{5d(bc-ad)} \\
 &= -\frac{4\sqrt{a+bx}}{5d(c+dx)^{5/4}} + \frac{8b\sqrt{a+bx}}{5d(bc-ad)\sqrt[4]{c+dx}} - \frac{(8b^2) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d^2(bc-ad)} \\
 &= -\frac{4\sqrt{a+bx}}{5d(c+dx)^{5/4}} + \frac{8b\sqrt{a+bx}}{5d(bc-ad)\sqrt[4]{c+dx}} + \frac{(8b^{3/2}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d^2\sqrt{bc-ad}} - \dots \\
 &= -\frac{4\sqrt{a+bx}}{5d(c+dx)^{5/4}} + \frac{8b\sqrt{a+bx}}{5d(bc-ad)\sqrt[4]{c+dx}} + \frac{(8b^{3/2}\sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})^d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d^2\sqrt{bc-ad}\sqrt{a+bx}} \\
 &= -\frac{4\sqrt{a+bx}}{5d(c+dx)^{5/4}} + \frac{8b\sqrt{a+bx}}{5d(bc-ad)\sqrt[4]{c+dx}} + \frac{8b^{5/4}\sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{5d^2\sqrt[4]{bc-ad}\sqrt{a+bx}} - \dots \\
 &= -\frac{4\sqrt{a+bx}}{5d(c+dx)^{5/4}} + \frac{8b\sqrt{a+bx}}{5d(bc-ad)\sqrt[4]{c+dx}} - \frac{8b^{5/4}\sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \middle| -1 \right)}{5d^2\sqrt[4]{bc-ad}\sqrt{a+bx}} + \dots
 \end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.31

$$\frac{2(a + bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{9/4} {}_2F_1 \left(\frac{3}{2}, \frac{9}{4}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(c + dx)^{9/4}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(9/4), x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(9/4)*Hypergeometric2F1[3/2, 9/4, 5/2, (d*(a + b*x))/(-b*c) + a*d])/(3*b*(c + d*x)^(9/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx + a} (dx + c)^{\frac{3}{4}}}{d^3 x^3 + 3cd^2 x^2 + 3c^2 dx + c^3}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(9/4), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx + a}}{(dx + c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(9/4), x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(9/4), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx + a}}{(dx + c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(9/4), x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(9/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(9/4),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(9/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(9/4), x)

[Out] int((a + b*x)^(1/2)/(c + d*x)^(9/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(9/4), x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(9/4), x)

$$3.1675 \quad \int \frac{1}{\sqrt{a+bx} (c+dx)^{9/4}} dx$$

Optimal. Leaf size=236

$$\frac{12b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{5d\sqrt{a+bx} (bc-ad)^{5/4}} - \frac{12b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5d\sqrt{a+bx} (bc-ad)^{5/4}} + \frac{12b\sqrt{a+bx}}{5\sqrt[4]{c+dx} (bc-ad)}$$

[Out] $4/5*(b*x+a)^{(1/2)/(-a*d+b*c)/(d*x+c)^{(5/4)}+12/5*b*(b*x+a)^{(1/2)/(-a*d+b*c)^2/(d*x+c)^{(1/4)}-12/5*b^{(5/4)*\operatorname{EllipticE}(b^{(1/4)*(d*x+c)^{(1/4)/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)/d/(-a*d+b*c)^{(5/4)/(b*x+a)^{(1/2)}+12/5*b^{(5/4)*\operatorname{EllipticF}(b^{(1/4)*(d*x+c)^{(1/4)/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)/d/(-a*d+b*c)^{(5/4)/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.24, antiderivative size = 236, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{12b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5d\sqrt{a+bx} (bc-ad)^{5/4}} - \frac{12b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5d\sqrt{a+bx} (bc-ad)^{5/4}} + \frac{12b\sqrt{a+bx}}{5\sqrt[4]{c+dx} (bc-ad)^2} + 5d$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(9/4)),x]

[Out] $(4*\operatorname{Sqrt}[a + b*x])/(5*(b*c - a*d)*(c + d*x)^{(5/4)} + (12*b*\operatorname{Sqrt}[a + b*x])/(5*(b*c - a*d)^2*(c + d*x)^{(1/4)}) - (12*b^{(5/4)*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)]*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(5*d*(b*c - a*d)^{(5/4)*\operatorname{Sqrt}[a + b*x]) + (12*b^{(5/4)*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)]*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1])/(5*d*(b*c - a*d)^{(5/4)*\operatorname{Sqrt}[a + b*x])$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt
[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x
] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[
a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt{a+bx}(c+dx)^{9/4}} dx &= \frac{4\sqrt{a+bx}}{5(bc-ad)(c+dx)^{5/4}} + \frac{(3b) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/4}} dx}{5(bc-ad)} \\
&= \frac{4\sqrt{a+bx}}{5(bc-ad)(c+dx)^{5/4}} + \frac{12b\sqrt{a+bx}}{5(bc-ad)^2 \sqrt[4]{c+dx}} - \frac{(3b^2) \int \frac{1}{\sqrt{a+bx} \sqrt[4]{c+dx}} dx}{5(bc-ad)^2} \\
&= \frac{4\sqrt{a+bx}}{5(bc-ad)(c+dx)^{5/4}} + \frac{12b\sqrt{a+bx}}{5(bc-ad)^2 \sqrt[4]{c+dx}} - \frac{(12b^2) \text{Subst} \left(\int \frac{x^2}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d(bc-ad)^2} \\
&= \frac{4\sqrt{a+bx}}{5(bc-ad)(c+dx)^{5/4}} + \frac{12b\sqrt{a+bx}}{5(bc-ad)^2 \sqrt[4]{c+dx}} + \frac{(12b^{3/2}) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^4}{d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d(bc-ad)^{3/2}} \\
&= \frac{4\sqrt{a+bx}}{5(bc-ad)(c+dx)^{5/4}} + \frac{12b\sqrt{a+bx}}{5(bc-ad)^2 \sqrt[4]{c+dx}} + \frac{(12b^{3/2} \sqrt{\frac{d(a+bx)}{-bc+ad}}) \text{Subst} \left(\int \frac{1}{\sqrt{1+\frac{bx^4}{(a-\frac{bc}{d})d}}} dx, x, \sqrt[4]{c+dx} \right)}{5d(bc-ad)^{3/2} \sqrt{a+bx}} \\
&= \frac{4\sqrt{a+bx}}{5(bc-ad)(c+dx)^{5/4}} + \frac{12b\sqrt{a+bx}}{5(bc-ad)^2 \sqrt[4]{c+dx}} + \frac{12b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right)}{5d(bc-ad)^{5/4} \sqrt{a+bx}} \\
&= \frac{4\sqrt{a+bx}}{5(bc-ad)(c+dx)^{5/4}} + \frac{12b\sqrt{a+bx}}{5(bc-ad)^2 \sqrt[4]{c+dx}} - \frac{12b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E \left(\sin^{-1} \left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}} \right) \right)}{5d(bc-ad)^{5/4} \sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.30

$$\frac{2\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad} \right)^{9/4} {}_2F_1 \left(\frac{1}{2}, \frac{9}{4}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b(c+dx)^{9/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(9/4)), x]

[Out] (2*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(9/4)*Hypergeometric2F1[1/2, 9/4, 3/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(c + d*x)^(9/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}}{bd^3x^4+ac^3+(3bcd^2+ad^3)x^3+3(bc^2d+acd^2)x^2+(bc^3+3ac^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(9/4),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(3/4)/(b*d^3*x^4 + a*c^3 + (3*b*c*d^2 + a*d^3)*x^3 + 3*(b*c^2*d + a*c*d^2)*x^2 + (b*c^3 + 3*a*c^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(9/4),x, algorithm="giac")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(9/4)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(9/4),x)

[Out] int(1/(b*x+a)^(1/2)/(d*x+c)^(9/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(9/4),x, algorithm="maxima")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(9/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{\sqrt{a+bx} (c+dx)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/2)*(c + d*x)^(9/4)), x)

[Out] int(1/((a + b*x)^(1/2)*(c + d*x)^(9/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a+bx} (c+dx)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/2)/(d*x+c)**(9/4), x)

[Out] Integral(1/(sqrt(a + b*x)*(c + d*x)**(9/4)), x)

$$3.1676 \quad \int \frac{1}{(a+bx)^{3/2}(c+dx)^{9/4}} dx$$

Optimal. Leaf size=262

$$\frac{42b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{5\sqrt{a+bx}(bc-ad)^{9/4}} + \frac{42b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5\sqrt{a+bx}(bc-ad)^{9/4}} - \frac{42bd\sqrt{a+bx}}{5\sqrt[4]{c+dx}(bc-ad)^3}$$

[Out] $-2/(-a*d+b*c)/(d*x+c)^{(5/4)}/(b*x+a)^{(1/2)}-14/5*d*(b*x+a)^{(1/2)}/(-a*d+b*c)^2/(d*x+c)^{(5/4)}-42/5*b*d*(b*x+a)^{(1/2)}/(-a*d+b*c)^3/(d*x+c)^{(1/4)}+42/5*b^{(5/4)}*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/(-a*d+b*c)^{(9/4)}/(b*x+a)^{(1/2)}-42/5*b^{(5/4)}*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/(-a*d+b*c)^{(9/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.26, antiderivative size = 262, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{42b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5\sqrt{a+bx}(bc-ad)^{9/4}} + \frac{42b^{5/4} \sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b} \sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right) \middle| -1\right)}{5\sqrt{a+bx}(bc-ad)^{9/4}} - \frac{42bd\sqrt{a+bx}}{5\sqrt[4]{c+dx}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a + b*x)^{(3/2)}*(c + d*x)^{(9/4)}), x]$

[Out] $-2/((b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(5/4)}) - (14*d*\operatorname{Sqrt}[a + b*x])/(5*(b*c - a*d)^2*(c + d*x)^{(5/4)}) - (42*b*d*\operatorname{Sqrt}[a + b*x])/(5*(b*c - a*d)^3*(c + d*x)^{(1/4)}) + (42*b^{(5/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticE}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/(5*(b*c - a*d)^{(9/4)}*\operatorname{Sqrt}[a + b*x]) - (42*b^{(5/4)}*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[(b^{(1/4)}*(c + d*x)^{(1/4)})/(b*c - a*d)^{(1/4)}], -1]/(5*(b*c - a*d)^{(9/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 51

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}/((b*c - a*d)*(m + 1)), x] - \operatorname{Dist}[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^n, x], x] /; \operatorname{FreeQ}\{a, b, c, d, n\}, x \ \&\& \operatorname{NeQ}[b*c - a*d, 0] \ \&\& \operatorname{LtQ}[m, -1] \ \&\& !(\operatorname{LtQ}[n, -1] \ \&\& (\operatorname{EqQ}[a, 0] \ \|\ (\operatorname{NeQ}[c, 0] \ \&\& \operatorname{LtQ}[m - n, 0] \ \&\& \operatorname{IntegerQ}[n]))) \ \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 224

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt
[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && !GtQ[a, 0]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)]/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 1200

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt
[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x
] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[
a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{3/2}(c+dx)^{9/4}} dx &= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{5/4}} - \frac{(7d) \int \frac{1}{\sqrt{a+bx}(c+dx)^{9/4}} dx}{2(bc-ad)} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{5/4}} - \frac{14d\sqrt{a+bx}}{5(bc-ad)^2(c+dx)^{5/4}} - \frac{(21bd) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/4}} dx}{10(bc-ad)^2} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{5/4}} - \frac{14d\sqrt{a+bx}}{5(bc-ad)^2(c+dx)^{5/4}} - \frac{42bd\sqrt{a+bx}}{5(bc-ad)^3\sqrt[4]{c+dx}} + \dots \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{5/4}} - \frac{14d\sqrt{a+bx}}{5(bc-ad)^2(c+dx)^{5/4}} - \frac{42bd\sqrt{a+bx}}{5(bc-ad)^3\sqrt[4]{c+dx}} + \dots \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{5/4}} - \frac{14d\sqrt{a+bx}}{5(bc-ad)^2(c+dx)^{5/4}} - \frac{42bd\sqrt{a+bx}}{5(bc-ad)^3\sqrt[4]{c+dx}} - \dots \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{5/4}} - \frac{14d\sqrt{a+bx}}{5(bc-ad)^2(c+dx)^{5/4}} - \frac{42bd\sqrt{a+bx}}{5(bc-ad)^3\sqrt[4]{c+dx}} - \dots \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{5/4}} - \frac{14d\sqrt{a+bx}}{5(bc-ad)^2(c+dx)^{5/4}} - \frac{42bd\sqrt{a+bx}}{5(bc-ad)^3\sqrt[4]{c+dx}} - \dots \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}(c+dx)^{5/4}} - \frac{14d\sqrt{a+bx}}{5(bc-ad)^2(c+dx)^{5/4}} - \frac{42bd\sqrt{a+bx}}{5(bc-ad)^3\sqrt[4]{c+dx}} + \dots
\end{aligned}$$

Mathematica [C] time = 0.05, size = 71, normalized size = 0.27

$$-\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{9/4} {}_2F_1 \left(-\frac{1}{2}, \frac{9}{4}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt{a+bx}(c+dx)^{9/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(9/4)),x]

[Out] $(-2*((b*(c + d*x))/(b*c - a*d))^(9/4)*\text{Hypergeometric2F1}[-1/2, 9/4, 1/2, (d*(a + b*x))/(-b*c + a*d)])/(b*\text{Sqrt}[a + b*x]*(c + d*x)^(9/4))$

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{3}{4}}}{b^2d^3x^5 + a^2c^3 + (3b^2cd^2 + 2abd^3)x^4 + (3b^2c^2d + 6abcd^2 + a^2d^3)x^3 + (b^2c^3 + 6abc^2d + 3a^2cd^2)x^2 + \dots}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(9/4),x, algorithm="fricas")

[Out] $\text{integral}(\text{sqrt}(b*x + a)*(d*x + c)^(3/4)/(b^2*d^3*x^5 + a^2*c^3 + (3*b^2*c*d^2 + 2*a*b*d^3)*x^4 + (3*b^2*c^2*d + 6*a*b*c*d^2 + a^2*d^3)*x^3 + (b^2*c^3 + 6*a*b*c^2*d + 3*a^2*c*d^2)*x^2 + (2*a*b*c^3 + 3*a^2*c^2*d)*x), x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(9/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(9/4)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(9/4),x)

[Out] int(1/(b*x+a)^(3/2)/(d*x+c)^(9/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(9/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(9/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{3/2} (c + dx)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(9/4)),x)

[Out] int(1/((a + b*x)^(3/2)*(c + d*x)^(9/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} (c + dx)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(9/4),x)

[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(9/4)), x)

$$3.1677 \quad \int \frac{1}{(a+bx)^{5/2}(c+dx)^{9/4}} dx$$

Optimal. Leaf size=303

$$\frac{77b^{5/4}d\sqrt{-\frac{d(a+bx)}{bc-ad}} \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right), -1\right)}{5\sqrt{a+bx}(bc-ad)^{13/4}} - \frac{77b^{5/4}d\sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{5\sqrt{a+bx}(bc-ad)^{13/4}} + \frac{77bd^2\sqrt{a+bx}}{5\sqrt[4]{c+dx}(bc-ad)^4}$$

[Out] $-2/3/(-a*d+b*c)/(b*x+a)^{(3/2)}/(d*x+c)^{(5/4)}+11/3*d/(-a*d+b*c)^2/(d*x+c)^{(5/4)}/(b*x+a)^{(1/2)}+77/15*d^2*(b*x+a)^{(1/2)}/(-a*d+b*c)^3/(d*x+c)^{(5/4)}+77/5*b*d^2*(b*x+a)^{(1/2)}/(-a*d+b*c)^4/(d*x+c)^{(1/4)}-77/5*b^{(5/4)}*d*\operatorname{EllipticE}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/(-a*d+b*c)^{(13/4)}/(b*x+a)^{(1/2)}+77/5*b^{(5/4)}*d*\operatorname{EllipticF}(b^{(1/4)}*(d*x+c)^{(1/4)}/(-a*d+b*c)^{(1/4)}, I)*(-d*(b*x+a)/(-a*d+b*c))^{(1/2)}/(-a*d+b*c)^{(13/4)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.29, antiderivative size = 303, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {51, 63, 307, 224, 221, 1200, 1199, 424}

$$\frac{77b^{5/4}d\sqrt{-\frac{d(a+bx)}{bc-ad}} F\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{5\sqrt{a+bx}(bc-ad)^{13/4}} - \frac{77b^{5/4}d\sqrt{-\frac{d(a+bx)}{bc-ad}} E\left(\sin^{-1}\left(\frac{\sqrt[4]{b}\sqrt[4]{c+dx}}{\sqrt[4]{bc-ad}}\right)\right) - 1}{5\sqrt{a+bx}(bc-ad)^{13/4}} + \frac{77bd^2\sqrt{a+bx}}{5\sqrt[4]{c+dx}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*(c + d*x)^(9/4)), x]

[Out] $-2/(3*(b*c - a*d)*(a + b*x)^{(3/2)}*(c + d*x)^{(5/4)}) + (11*d)/(3*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(5/4)}) + (77*d^2*\operatorname{Sqrt}[a + b*x])/(15*(b*c - a*d)^3*(c + d*x)^{(5/4)}) + (77*b*d^2*\operatorname{Sqrt}[a + b*x])/(5*(b*c - a*d)^4*(c + d*x)^{(1/4)}) - (77*b^{(5/4)}*d*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticE}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1]/(5*(b*c - a*d)^{(13/4)}*\operatorname{Sqrt}[a + b*x]) + (77*b^{(5/4)}*d*\operatorname{Sqrt}[-(d*(a + b*x))/(b*c - a*d)])*\operatorname{EllipticF}[\operatorname{ArcSin}[b^{(1/4)}*(c + d*x)^{(1/4)}/(b*c - a*d)^{(1/4)}], -1]/(5*(b*c - a*d)^{(13/4)}*\operatorname{Sqrt}[a + b*x])$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I

ntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 224

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (b*x^4)/a]/Sqrt[a + b*x^4], Int[1/Sqrt[1 + (b*x^4)/a], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a] && !GtQ[a, 0]

Rule 307

Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/Sqrt[a + b*x^4], x], x] /; FreeQ[{a, b}, x] && NegQ[b/a]

Rule 424

Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]

Rule 1199

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sqrt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]

Rule 1200

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[Sqrt[1 + (c*x^4)/a]/Sqrt[a + c*x^4], Int[(d + e*x^2)/Sqrt[1 + (c*x^4)/a], x], x] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && !GtQ[a, 0]

Mathematica [C] time = 0.05, size = 73, normalized size = 0.24

$$\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{9/4} {}_2F_1 \left(-\frac{3}{2}, \frac{9}{4}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(a+bx)^{3/2}(c+dx)^{9/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(9/4)), x]

[Out] $(-2*((b*(c + d*x))/(b*c - a*d))^(9/4)*\text{Hypergeometric2F1}[-3/2, 9/4, -1/2, (d*(a + b*x))/(-b*c) + a*d])/(3*b*(a + b*x)^(3/2)*(c + d*x)^(9/4))$

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{3}{4}}}{b^3 d^3 x^6 + a^3 c^3 + 3(b^3 c d^2 + a b^2 d^3) x^5 + 3(b^3 c^2 d + 3 a b^2 c d^2 + a^2 b d^3) x^4 + (b^3 c^3 + 9 a b^2 c^2 d + 9 a^2 b c d^2 - \dots)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(9/4), x, algorithm="fricas")

[Out] $\text{integral}(\text{sqrt}(b*x + a)*(d*x + c)^{(3/4)}/(b^3*d^3*x^6 + a^3*c^3 + 3*(b^3*c*d^2 + a*b^2*d^3)*x^5 + 3*(b^3*c^2*d + 3*a*b^2*c*d^2 + a^2*b*d^3)*x^4 + (b^3*c^3 + 9*a*b^2*c^2*d + 9*a^2*b*c*d^2 + a^3*d^3)*x^3 + 3*(a*b^2*c^3 + 3*a^2*b*c^2*d + a^3*c*d^2)*x^2 + 3*(a^2*b*c^3 + a^3*c^2*d)*x), x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(9/4), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(9/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(9/4), x)

[Out] `int(1/(b*x+a)^(5/2)/(d*x+c)^(9/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/2)/(d*x+c)^(9/4),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(5/2)*(d*x + c)^(9/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{2}}(c+dx)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(5/2)*(c + d*x)^(9/4)),x)`

[Out] `int(1/((a + b*x)^(5/2)*(c + d*x)^(9/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{2}}(c+dx)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/2)/(d*x+c)**(9/4),x)`

[Out] `Integral(1/((a + b*x)**(5/2)*(c + d*x)**(9/4)), x)`

3.1678 $\int (a + bx)^{3/4} (c + dx)^{5/4} dx$

Optimal. Leaf size=205

$$\frac{5(bc - ad)^3 \tan^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{64b^{9/4}d^{7/4}} - \frac{5(bc - ad)^3 \tanh^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{64b^{9/4}d^{7/4}} + \frac{5(a + bx)^{3/4} \sqrt[4]{c + dx} (bc - ad)^2}{96b^2d} + \frac{5(a + bx)^{7/4} \sqrt[4]{c}}{24b^2d}$$

[Out] $5/96*(-a*d+b*c)^2*(b*x+a)^{(3/4)}*(d*x+c)^{(1/4)}/b^2/d+5/24*(-a*d+b*c)*(b*x+a)^{(7/4)}*(d*x+c)^{(1/4)}/b^2+1/3*(b*x+a)^{(7/4)}*(d*x+c)^{(5/4)}/b+5/64*(-a*d+b*c)^3*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(9/4)}/d^{(7/4)}-5/64*(-a*d+b*c)^3*\operatorname{arctanh}(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(9/4)}/d^{(7/4)}$

Rubi [A] time = 0.14, antiderivative size = 205, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {50, 63, 331, 298, 205, 208}

$$\frac{5(bc - ad)^3 \tan^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{64b^{9/4}d^{7/4}} - \frac{5(bc - ad)^3 \tanh^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{64b^{9/4}d^{7/4}} + \frac{5(a + bx)^{3/4} \sqrt[4]{c + dx} (bc - ad)^2}{96b^2d} + \frac{5(a + bx)^{7/4} \sqrt[4]{c}}{24b^2d}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(3/4)}*(c + d*x)^{(5/4)}, x]$

[Out] $(5*(b*c - a*d)^2*(a + b*x)^{(3/4)}*(c + d*x)^{(1/4)})/(96*b^2*d) + (5*(b*c - a*d)*(a + b*x)^{(7/4)}*(c + d*x)^{(1/4)})/(24*b^2) + ((a + b*x)^{(7/4)}*(c + d*x)^{(5/4)})/(3*b) + (5*(b*c - a*d)^3*\text{ArcTan}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(64*b^{(9/4)}*d^{(7/4)}) - (5*(b*c - a*d)^3*\text{ArcTanh}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(64*b^{(9/4)}*d^{(7/4)})$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ

$[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 205

$\text{Int}[\frac{(a_ + (b_.) * (x_)^2)^{-1}}{a, x}] \rightarrow \text{Simp}[\frac{\text{Rt}[a/b, 2] * \text{ArcTan}[x/\text{Rt}[a/b, 2]]}{a, x}] \text{ ; FreeQ}\{a, b\}, x\} \&\& \text{PosQ}[a/b]$

Rule 208

$\text{Int}[\frac{(a_ + (b_.) * (x_)^2)^{-1}}{\text{Rt}[-(a/b), 2]}, x] \rightarrow \text{Simp}[\frac{\text{Rt}[-(a/b), 2] * \text{ArcTanh}[x/\text{Rt}[-(a/b), 2]]}{a, x}] \text{ ; FreeQ}\{a, b\}, x\} \&\& \text{NegQ}[a/b]$

Rule 298

$\text{Int}[\frac{(x_)^2}{(a_ + (b_.) * (x_)^4)}, x_Symbol] \rightarrow \text{With}\{r = \text{Numerator}[\text{Rt}[-(a/b), 2]], s = \text{Denominator}[\text{Rt}[-(a/b), 2]]\}, \text{Dist}[s/(2*b), \text{Int}[1/(r + s*x^2), x], x] - \text{Dist}[s/(2*b), \text{Int}[1/(r - s*x^2), x], x]\} \text{ ; FreeQ}\{a, b\}, x\} \&\& !\text{GtQ}[a/b, 0]$

Rule 331

$\text{Int}[(x_)^{(m_)} * ((a_ + (b_.) * (x_)^n)^{p_}), x_Symbol] \rightarrow \text{Dist}[a^{(p + (m + 1)/n)}, \text{Subst}[\text{Int}[x^m / (1 - b*x^n)^{(p + (m + 1)/n + 1)}, x], x, x/(a + b*x^n)^{(1/n)}], x] \text{ ; FreeQ}\{a, b\}, x\} \&\& \text{IGtQ}[n, 0] \&\& \text{LtQ}[-1, p, 0] \&\& \text{NeQ}[p, -2^{(-1)}] \&\& \text{IntegersQ}[m, p + (m + 1)/n]$

Rubi steps

$$\begin{aligned}
\int (a + bx)^{3/4} (c + dx)^{5/4} dx &= \frac{(a + bx)^{7/4} (c + dx)^{5/4}}{3b} + \frac{(5(bc - ad)) \int (a + bx)^{3/4} \sqrt[4]{c + dx} dx}{12b} \\
&= \frac{5(bc - ad)(a + bx)^{7/4} \sqrt[4]{c + dx}}{24b^2} + \frac{(a + bx)^{7/4} (c + dx)^{5/4}}{3b} + \frac{(5(bc - ad)^2) \int \frac{(a+bx)^{3/4}}{(c+dx)^{3/4}} dx}{96b^2} \\
&= \frac{5(bc - ad)^2 (a + bx)^{3/4} \sqrt[4]{c + dx}}{96b^2 d} + \frac{5(bc - ad)(a + bx)^{7/4} \sqrt[4]{c + dx}}{24b^2} + \frac{(a + bx)^{7/4} (c + dx)^{5/4}}{3b} \\
&= \frac{5(bc - ad)^2 (a + bx)^{3/4} \sqrt[4]{c + dx}}{96b^2 d} + \frac{5(bc - ad)(a + bx)^{7/4} \sqrt[4]{c + dx}}{24b^2} + \frac{(a + bx)^{7/4} (c + dx)^{5/4}}{3b} \\
&= \frac{5(bc - ad)^2 (a + bx)^{3/4} \sqrt[4]{c + dx}}{96b^2 d} + \frac{5(bc - ad)(a + bx)^{7/4} \sqrt[4]{c + dx}}{24b^2} + \frac{(a + bx)^{7/4} (c + dx)^{5/4}}{3b} \\
&= \frac{5(bc - ad)^2 (a + bx)^{3/4} \sqrt[4]{c + dx}}{96b^2 d} + \frac{5(bc - ad)(a + bx)^{7/4} \sqrt[4]{c + dx}}{24b^2} + \frac{(a + bx)^{7/4} (c + dx)^{5/4}}{3b} \\
&= \frac{5(bc - ad)^2 (a + bx)^{3/4} \sqrt[4]{c + dx}}{96b^2 d} + \frac{5(bc - ad)(a + bx)^{7/4} \sqrt[4]{c + dx}}{24b^2} + \frac{(a + bx)^{7/4} (c + dx)^{5/4}}{3b}
\end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.36

$$\frac{4(a + bx)^{7/4} (c + dx)^{5/4} {}_2F_1\left(-\frac{5}{4}, \frac{7}{4}; \frac{11}{4}; \frac{d(a+bx)}{ad-bc}\right)}{7b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/4)*(c + d*x)^(5/4), x]

[Out] (4*(a + b*x)^(7/4)*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, 7/4, 11/4, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [B] time = 0.63, size = 2151, normalized size = 10.49

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)*(d*x+c)^(5/4),x, algorithm="fricas")

[Out]
$$-1/384*(60*b^2*d*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^9*d^7))^{1/4}*\arctan(((b^{10}c^3*d^5 - 3*a*b^9c^2*d^6 + 3*a^2*b^8c*d^7 - a^3*b^7*d^8)*(b*x + a)^{3/4}*(d*x + c)^{1/4}*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^9*d^7)))^{3/4} + (b^8*d^5*x + a*b^7*d^5)*\sqrt{((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)*\sqrt{b*x + a}*\sqrt{d*x + c} + (b^5*d^4*x + a*b^4*d^4)*\sqrt{((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^9*d^7)))/(b*x + a))*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^9*d^7))^{3/4})/(a*b^{12}c^{12} - 12*a^2*b^{11}c^{11}d + 66*a^3*b^{10}c^{10}d^2 - 220*a^4*b^9c^9d^3 + 495*a^5*b^8c^8d^4 - 792*a^6*b^7c^7d^5 + 924*a^7*b^6c^6d^6 - 792*a^8*b^5c^5d^7 + 495*a^9*b^4c^4d^8 - 220*a^{10}b^3c^3d^9 + 66*a^{11}b^2c^2d^{10} - 12*a^{12}b*c*d^{11} + a^{13}d^{12} + (b^{13}c^{12} - 12*a*b^{12}c^{11}d + 66*a^2*b^{11}c^{10}d^2 - 220*a^3*b^{10}c^9d^3 + 495*a^4*b^9c^8d^4 - 792*a^5*b^8c^7d^5 + 924*a^6*b^7c^6d^6 - 792*a^7*b^6c^5d^7 + 495*a^8*b^5c^4d^8 - 220*a^9*b^4c^3d^9 + 66*a^{10}b^3c^2d^{10} - 12*a^{11}b^2c*d^{11} + a^{12}b*d^{12})*x)) + 15*b^2*d*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^9*d^7))^{1/4}*\log(-5*((b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*(b*x + a)^{3/4}*(d*x + c)^{1/4} + (b^3*d^2*x + a*b^2*d^2))*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^9*d^7))^{1/4})/(b*x + a) - 15*b^2*d*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^9*d^7))^{1/4}*\log(-5*((b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*(b*x + a)^{3/4}*(d*x + c)^{1/4}) - (b^3*d^2*x + a*b^2*d^2))*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 +$$

$924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^9*d^7)^{(1/4))/(b*x + a)) - 4*(32*b^2*d^2*x^2 + 5*b^2*c^2 + 42*a*b*c*d - 15*a^2*d^2 + 4*(13*b^2*c*d + 3*a*b*d^2)*x)*(b*x + a)^{(3/4)*(d*x + c)^{(1/4)))/(b^2*d)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{4}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)*(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/4)*(d*x + c)^(5/4), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{4}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/4)*(d*x+c)^(5/4),x)

[Out] int((b*x+a)^(3/4)*(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{4}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)*(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/4)*(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{3/4} (c + dx)^{5/4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/4)*(c + d*x)^(5/4),x)

[Out] int((a + b*x)^(3/4)*(c + d*x)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{3}{4}} (c + dx)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/4)*(d*x+c)**(5/4),x)

[Out] Integral((a + b*x)**(3/4)*(c + d*x)**(5/4), x)

$$3.1679 \quad \int \frac{(c+dx)^{5/4}}{\sqrt[4]{a+bx}} dx$$

Optimal. Leaf size=167

$$\frac{5(bc-ad)^2 \tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16b^{9/4}d^{3/4}} + \frac{5(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16b^{9/4}d^{3/4}} + \frac{5(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)}{8b^2} + \frac{(a+bx)^{3/4}(c+dx)}{2b}$$

[Out] $5/8*(-a*d+b*c)*(b*x+a)^{(3/4)}*(d*x+c)^{(1/4)}/b^2+1/2*(b*x+a)^{(3/4)}*(d*x+c)^{(5/4)}/b-5/16*(-a*d+b*c)^2*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(9/4)}/d^{(3/4)}+5/16*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(9/4)}/d^{(3/4)}$

Rubi [A] time = 0.10, antiderivative size = 167, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {50, 63, 331, 298, 205, 208}

$$\frac{5(bc-ad)^2 \tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16b^{9/4}d^{3/4}} + \frac{5(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16b^{9/4}d^{3/4}} + \frac{5(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)}{8b^2} + \frac{(a+bx)^{3/4}(c+dx)}{2b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^{(5/4)}/(a + b*x)^{(1/4)}, x]$

[Out] $(5*(b*c - a*d)*(a + b*x)^{(3/4)}*(c + d*x)^{(1/4)})/(8*b^2) + ((a + b*x)^{(3/4)}*(c + d*x)^{(5/4)})/(2*b) - (5*(b*c - a*d)^2*\text{ArcTan}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(16*b^{(9/4)}*d^{(3/4)}) + (5*(b*c - a*d)^2*\text{ArcTanh}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(16*b^{(9/4)}*d^{(3/4)})$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m+n+1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m-n, 0]))) && !ILtQ[m+n+2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\text{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rule 298

Int[(x_)^2/((a_) + (b_.)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[-(a/b), 2]], s = Denominator[Rt[-(a/b), 2]]}, Dist[s/(2*b), Int[1/(r + s*x^2), x], x] - Dist[s/(2*b), Int[1/(r - s*x^2), x], x]] /; FreeQ[{a, b}, x] && !GtQ[a/b, 0]

Rule 331

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{\sqrt[4]{a+bx}} dx &= \frac{(a+bx)^{3/4}(c+dx)^{5/4}}{2b} + \frac{(5(bc-ad)) \int \frac{\sqrt[4]{c+dx}}{\sqrt[4]{a+bx}} dx}{8b} \\
&= \frac{5(bc-ad)(a+bx)^{3/4}\sqrt[4]{c+dx}}{8b^2} + \frac{(a+bx)^{3/4}(c+dx)^{5/4}}{2b} + \frac{(5(bc-ad)^2) \int \frac{1}{\sqrt[4]{a+bx}(c+dx)^{3/4}} dx}{32b^2} \\
&= \frac{5(bc-ad)(a+bx)^{3/4}\sqrt[4]{c+dx}}{8b^2} + \frac{(a+bx)^{3/4}(c+dx)^{5/4}}{2b} + \frac{(5(bc-ad)^2) \text{Subst} \left(\int \frac{x^2}{\left(\frac{c-ad}{b} + \frac{dx^4}{b}\right)^{3/4}} dx, x \right)}{8b^3} \\
&= \frac{5(bc-ad)(a+bx)^{3/4}\sqrt[4]{c+dx}}{8b^2} + \frac{(a+bx)^{3/4}(c+dx)^{5/4}}{2b} + \frac{(5(bc-ad)^2) \text{Subst} \left(\int \frac{x^2}{1-\frac{dx^4}{b}} dx, x \right)}{8b^3} \\
&= \frac{5(bc-ad)(a+bx)^{3/4}\sqrt[4]{c+dx}}{8b^2} + \frac{(a+bx)^{3/4}(c+dx)^{5/4}}{2b} + \frac{(5(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{b}-\sqrt{d}x^2} dx \right)}{16b^2\sqrt{d}} \\
&= \frac{5(bc-ad)(a+bx)^{3/4}\sqrt[4]{c+dx}}{8b^2} + \frac{(a+bx)^{3/4}(c+dx)^{5/4}}{2b} - \frac{5(bc-ad)^2 \tan^{-1} \left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}} \right)}{16b^{9/4}d^{3/4}} + \dots
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.44

$$\frac{4(a+bx)^{3/4}(c+dx)^{5/4} {}_2F_1\left(-\frac{5}{4}, \frac{3}{4}; \frac{7}{4}; \frac{d(a+bx)}{ad-bc}\right)}{3b\left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(1/4), x]

[Out] (4*(a + b*x)^(3/4)*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, 3/4, 7/4, (d*(a + b*x))/(-b*c + a*d)]/(3*b*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [B] time = 0.59, size = 1468, normalized size = 8.79

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(1/4), x, algorithm="fricas")

```
[Out] -1/32*(20*b^2*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^9*d^3))^(1/4)*arctan(-((b^9*c^2*d^2 - 2*a*b^8*c*d^3 + a^2*b^7*d^4)*(b*x + a)^(3/4)*(d*x + c)^(1/4))*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^9*d^3))^(3/4) - (b^8*d^2*x + a*b^7*d^2)*sqrt(((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*sqrt(b*x + a)*sqrt(d*x + c) + (b^5*d^2*x + a*b^4*d^2)*sqrt((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^9*d^3)))/(b*x + a))*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^9*d^3))^(3/4))/(a*b^8*c^8 - 8*a^2*b^7*c^7*d + 28*a^3*b^6*c^6*d^2 - 56*a^4*b^5*c^5*d^3 + 70*a^5*b^4*c^4*d^4 - 56*a^6*b^3*c^3*d^5 + 28*a^7*b^2*c^2*d^6 - 8*a^8*b*c*d^7 + a^9*d^8 + (b^9*c^8 - 8*a*b^8*c^7*d + 28*a^2*b^7*c^6*d^2 - 56*a^3*b^6*c^5*d^3 + 70*a^4*b^5*c^4*d^4 - 56*a^5*b^4*c^3*d^5 + 28*a^6*b^3*c^2*d^6 - 8*a^7*b^2*c*d^7 + a^8*b*d^8)*x)) - 5*b^2*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^9*d^3))^(1/4)*log(5*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^(3/4)*(d*x + c)^(1/4) + (b^3*d*x + a*b^2*d)*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^9*d^3))^(1/4)))/(b*x + a)) + 5*b^2*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^9*d^3))^(1/4)*log(5*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^(3/4)*(d*x + c)^(1/4) - (b^3*d*x + a*b^2*d)*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^9*d^3))^(1/4)))/(b*x + a)) - 4*(4*b*d*x + 9*b*c - 5*a*d)*(b*x + a)^(3/4)*(d*x + c)^(1/4))/b^2
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^(5/4)/(b*x+a)^(1/4),x, algorithm="giac")
```

```
[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(1/4), x)
```

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(1/4),x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(1/4),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(1/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{5/4}}{(a + bx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(1/4),x)

[Out] int((c + d*x)^(5/4)/(a + b*x)^(1/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{4}}}{\sqrt[4]{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/4)/(b*x+a)**(1/4),x)

[Out] Integral((c + d*x)**(5/4)/(a + b*x)**(1/4), x)

$$3.1680 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{5/4}} dx$$

Optimal. Leaf size=152

$$-\frac{5\sqrt[4]{d}(bc-ad)\tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2b^{9/4}} + \frac{5\sqrt[4]{d}(bc-ad)\tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2b^{9/4}} + \frac{5d(a+bx)^{3/4}\sqrt[4]{c+dx}}{b^2} - \frac{4(c+dx)^{5/4}}{b\sqrt[4]{a+bx}}$$

[Out] $5*d*(b*x+a)^{(3/4)}*(d*x+c)^{(1/4)}/b^2-4*(d*x+c)^{(5/4)}/b/(b*x+a)^{(1/4)}-5/2*d^{(1/4)}*(-a*d+b*c)*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(9/4)}+5/2*d^{(1/4)}*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(9/4)}$

Rubi [A] time = 0.10, antiderivative size = 152, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 7, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.368$, Rules used = {47, 50, 63, 331, 298, 205, 208}

$$\frac{5d(a+bx)^{3/4}\sqrt[4]{c+dx}}{b^2} - \frac{5\sqrt[4]{d}(bc-ad)\tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2b^{9/4}} + \frac{5\sqrt[4]{d}(bc-ad)\tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2b^{9/4}} - \frac{4(c+dx)^{5/4}}{b\sqrt[4]{a+bx}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^{(5/4)}/(a + b*x)^{(5/4)}, x]$

[Out] $(5*d*(a + b*x)^{(3/4)}*(c + d*x)^{(1/4)})/b^2 - (4*(c + d*x)^{(5/4)})/(b*(a + b*x)^{(1/4)}) - (5*d^{(1/4)}*(b*c - a*d)*\text{ArcTan}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(2*b^{(9/4)}) + (5*d^{(1/4)}*(b*c - a*d)*\text{ArcTanh}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(2*b^{(9/4)})$

Rule 47

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \text{Dist}[(d*n)/(b*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\text{FreeQ}\{a, b, c, d\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{GtQ}[n, 0] \&\& \text{LtQ}[m, -1] \&\& !(IntegerQ[n] \&\& !IntegerQ[m]) \&\& !(IntegerQ[m + n + 2], 0) \&\& (\text{FractionQ}[m] || \text{GeQ}[2*n + m + 1, 0]) \&\& \& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ $\text{FreeQ}\{a, b,$

$c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{GtQ}[n, 0] \&\& \text{NeQ}[m + n + 1, 0] \&\& \text{!(IGtQ}[m, 0] \&\& (\text{!IntegerQ}[n] \mid\mid (\text{GtQ}[m, 0] \&\& \text{LtQ}[m - n, 0]))) \&\& \text{!ILtQ}[m + n + 2, 0] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\text{Int}[(a_.) + (b_.)*(x_)^m]*((c_.) + (d_.)*(x_)^n), x_Symbol] \text{ :> With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{p*(m+1)-1}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{1/p}], x]] \text{ /; FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 205

$\text{Int}[(a_.) + (b_.)*(x_)^2]^{-1}, x_Symbol] \text{ :> Simp}[(\text{Rt}[a/b, 2]*\text{ArcTan}[x/\text{Rt}[a/b, 2]])/a, x] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a/b]$

Rule 208

$\text{Int}[(a_.) + (b_.)*(x_)^2]^{-1}, x_Symbol] \text{ :> Simp}[(\text{Rt}[-(a/b), 2]*\text{ArcTanh}[x/\text{Rt}[-(a/b), 2]])/a, x] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{NegQ}[a/b]$

Rule 298

$\text{Int}[x_]^2/((a_) + (b_.)*(x_)^4), x_Symbol] \text{ :> With}\{r = \text{Numerator}[\text{Rt}[-(a/b), 2]], s = \text{Denominator}[\text{Rt}[-(a/b), 2]]\}, \text{Dist}[s/(2*b), \text{Int}[1/(r + s*x^2), x], x] - \text{Dist}[s/(2*b), \text{Int}[1/(r - s*x^2), x], x]] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{!GtQ}[a/b, 0]$

Rule 331

$\text{Int}[x_]^{m_.}*((a_) + (b_.)*(x_)^{n_.})^{p_.}, x_Symbol] \text{ :> Dist}[a^{(p + (m + 1)/n)}, \text{Subst}[\text{Int}[x^m/(1 - b*x^n)^{p + (m + 1)/n + 1}], x], x, x/(a + b*x^n)^{1/n}], x] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{IGtQ}[n, 0] \&\& \text{LtQ}[-1, p, 0] \&\& \text{NeQ}[p, -2^{-1}] \&\& \text{IntegersQ}[m, p + (m + 1)/n]$

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{5/4}} dx &= -\frac{4(c+dx)^{5/4}}{b^4\sqrt[4]{a+bx}} + \frac{(5d) \int \frac{\sqrt[4]{c+dx}}{\sqrt[4]{a+bx}} dx}{b} \\
&= \frac{5d(a+bx)^{3/4}\sqrt[4]{c+dx}}{b^2} - \frac{4(c+dx)^{5/4}}{b^4\sqrt[4]{a+bx}} + \frac{(5d(bc-ad)) \int \frac{1}{\sqrt[4]{a+bx}(c+dx)^{3/4}} dx}{4b^2} \\
&= \frac{5d(a+bx)^{3/4}\sqrt[4]{c+dx}}{b^2} - \frac{4(c+dx)^{5/4}}{b^4\sqrt[4]{a+bx}} + \frac{(5d(bc-ad)) \text{Subst} \left(\int \frac{x^2}{\left(c-\frac{ad}{b}+\frac{dx^4}{b}\right)^{3/4}} dx, x, \sqrt[4]{a+bx} \right)}{b^3} \\
&= \frac{5d(a+bx)^{3/4}\sqrt[4]{c+dx}}{b^2} - \frac{4(c+dx)^{5/4}}{b^4\sqrt[4]{a+bx}} + \frac{(5d(bc-ad)) \text{Subst} \left(\int \frac{x^2}{1-\frac{dx^4}{b}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{b^3} \\
&= \frac{5d(a+bx)^{3/4}\sqrt[4]{c+dx}}{b^2} - \frac{4(c+dx)^{5/4}}{b^4\sqrt[4]{a+bx}} + \frac{(5\sqrt{d}(bc-ad)) \text{Subst} \left(\int \frac{1}{\sqrt{b}-\sqrt{d}x^2} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{2b^2} \\
&= \frac{5d(a+bx)^{3/4}\sqrt[4]{c+dx}}{b^2} - \frac{4(c+dx)^{5/4}}{b^4\sqrt[4]{a+bx}} - \frac{5\sqrt[4]{d}(bc-ad) \tan^{-1} \left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}} \right)}{2b^{9/4}} + \frac{5\sqrt[4]{d}(bc-ad) \tan^{-1} \left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}} \right)}{2b^{9/4}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 71, normalized size = 0.47

$$-\frac{4(c+dx)^{5/4} {}_2F_1\left(-\frac{5}{4}, -\frac{1}{4}; \frac{3}{4}; \frac{d(a+bx)}{ad-bc}\right)}{b^4\sqrt[4]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(5/4), x]

[Out] (-4*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, -1/4, 3/4, (d*(a + b*x))/(-b*c + a*d)]/(b*(a + b*x)^(1/4)*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [B] time = 0.53, size = 857, normalized size = 5.64

$$20 (b^3x + ab^2) \left(\frac{b^4c^4d - 4ab^3c^3d^2 + 6a^2b^2c^2d^3 - 4a^3bcd^4 + a^4d^5}{b^9} \right)^{\frac{1}{4}} \arctan \left(\frac{(b^8c - ab^7d)(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{1}{4}} \left(\frac{b^4c^4d - 4ab^3c^3d^2 + 6a^2b^2c^2d^3 - 4a^3bcd^4 + a^4d^5}{b^9} \right)^{\frac{1}{4}}}{ab^4c^4d - 4a^4b^4d^5} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(5/4),x, algorithm="fricas")

[Out] 1/4*(20*(b^3*x + a*b^2)*((b^4*c^4*d - 4*a*b^3*c^3*d^2 + 6*a^2*b^2*c^2*d^3 - 4*a^3*b*c*d^4 + a^4*d^5)/b^9)^(1/4)*arctan(((b^8*c - a*b^7*d)*(b*x + a)^(3/4)*(d*x + c)^(1/4)*((b^4*c^4*d - 4*a*b^3*c^3*d^2 + 6*a^2*b^2*c^2*d^3 - 4*a^3*b*c*d^4 + a^4*d^5)/b^9)^(3/4) + (b^8*x + a*b^7)*sqrt(((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*sqrt(b*x + a)*sqrt(d*x + c) + (b^5*x + a*b^4)*sqrt((b^4*c^4*d - 4*a*b^3*c^3*d^2 + 6*a^2*b^2*c^2*d^3 - 4*a^3*b*c*d^4 + a^4*d^5)/b^9)))/(b*x + a))*((b^4*c^4*d - 4*a*b^3*c^3*d^2 + 6*a^2*b^2*c^2*d^3 - 4*a^3*b*c*d^4 + a^4*d^5)/b^9)^(3/4))/(a*b^4*c^4*d - 4*a^2*b^3*c^3*d^2 + 6*a^3*b^2*c^2*d^3 - 4*a^4*b*c*d^4 + a^5*d^5 + (b^5*c^4*d - 4*a*b^4*c^3*d^2 + 6*a^2*b^3*c^2*d^3 - 4*a^3*b^2*c*d^4 + a^4*b*d^5)*x)) + 5*(b^3*x + a*b^2)*((b^4*c^4*d - 4*a*b^3*c^3*d^2 + 6*a^2*b^2*c^2*d^3 - 4*a^3*b*c*d^4 + a^4*d^5)/b^9)^(1/4)*log(-5*((b*c - a*d)*(b*x + a)^(3/4)*(d*x + c)^(1/4) + (b^3*x + a*b^2)*((b^4*c^4*d - 4*a*b^3*c^3*d^2 + 6*a^2*b^2*c^2*d^3 - 4*a^3*b*c*d^4 + a^4*d^5)/b^9)^(1/4)))/(b*x + a)) - 5*(b^3*x + a*b^2)*((b^4*c^4*d - 4*a*b^3*c^3*d^2 + 6*a^2*b^2*c^2*d^3 - 4*a^3*b*c*d^4 + a^4*d^5)/b^9)^(1/4)*log(-5*((b*c - a*d)*(b*x + a)^(3/4)*(d*x + c)^(1/4) - (b^3*x + a*b^2)*((b^4*c^4*d - 4*a*b^3*c^3*d^2 + 6*a^2*b^2*c^2*d^3 - 4*a^3*b*c*d^4 + a^4*d^5)/b^9)^(1/4)))/(b*x + a)) + 4*(b*d*x - 4*b*c + 5*a*d)*(b*x + a)^(3/4)*(d*x + c)^(1/4))/(b^3*x + a*b^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(5/4),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(5/4), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(5/4), x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(5/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(5/4), x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(5/4), x)

[Out] int((c + d*x)^(5/4)/(a + b*x)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/4)/(b*x+a)**(5/4), x)

[Out] Integral((c + d*x)**(5/4)/(a + b*x)**(5/4), x)

$$3.1681 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{9/4}} dx$$

Optimal. Leaf size=134

$$-\frac{2d^{5/4} \tan^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{b^{9/4}} + \frac{2d^{5/4} \tanh^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{b^{9/4}} - \frac{4d\sqrt[4]{c+dx}}{b^2\sqrt[4]{a+bx}} - \frac{4(c+dx)^{5/4}}{5b(a+bx)^{5/4}}$$

[Out] $-4*d*(d*x+c)^{(1/4)}/b^2/(b*x+a)^{(1/4)}-4/5*(d*x+c)^{(5/4)}/b/(b*x+a)^{(5/4)}-2*d^{(5/4)}*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(9/4)}+2*d^{(5/4)}*\operatorname{arctanh}(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(9/4)}$

Rubi [A] time = 0.09, antiderivative size = 134, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {47, 63, 331, 298, 205, 208}

$$-\frac{2d^{5/4} \tan^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{b^{9/4}} + \frac{2d^{5/4} \tanh^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{b^{9/4}} - \frac{4d\sqrt[4]{c+dx}}{b^2\sqrt[4]{a+bx}} - \frac{4(c+dx)^{5/4}}{5b(a+bx)^{5/4}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^{(5/4)}/(a + b*x)^{(9/4)}, x]$

[Out] $(-4*d*(c + d*x)^{(1/4)})/(b^2*(a + b*x)^{(1/4)}) - (4*(c + d*x)^{(5/4)})/(5*b*(a + b*x)^{(5/4)}) - (2*d^{(5/4)}*ArcTan[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/b^{(9/4)} + (2*d^{(5/4)}*ArcTanh[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/b^{(9/4)}$

Rule 47

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \text{Dist}[(d*n)/(b*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rule 298

Int[(x_)^2/((a_) + (b_.)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[-(a/b), 2]], s = Denominator[Rt[-(a/b), 2]]}, Dist[s/(2*b), Int[1/(r + s*x^2), x], x] - Dist[s/(2*b), Int[1/(r - s*x^2), x], x]] /; FreeQ[{a, b}, x] && !GtQ[a/b, 0]

Rule 331

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{9/4}} dx &= -\frac{4(c+dx)^{5/4}}{5b(a+bx)^{5/4}} + \frac{d \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{5/4}} dx}{b} \\
&= -\frac{4d\sqrt[4]{c+dx}}{b^2\sqrt[4]{a+bx}} - \frac{4(c+dx)^{5/4}}{5b(a+bx)^{5/4}} + \frac{d^2 \int \frac{1}{\sqrt[4]{a+bx}(c+dx)^{3/4}} dx}{b^2} \\
&= -\frac{4d\sqrt[4]{c+dx}}{b^2\sqrt[4]{a+bx}} - \frac{4(c+dx)^{5/4}}{5b(a+bx)^{5/4}} + \frac{(4d^2) \operatorname{Subst} \left(\int \frac{x^2}{\left(c - \frac{ad}{b} + \frac{dx^4}{b}\right)^{3/4}} dx, x, \sqrt[4]{a+bx} \right)}{b^3} \\
&= -\frac{4d\sqrt[4]{c+dx}}{b^2\sqrt[4]{a+bx}} - \frac{4(c+dx)^{5/4}}{5b(a+bx)^{5/4}} + \frac{(4d^2) \operatorname{Subst} \left(\int \frac{x^2}{1 - \frac{dx^4}{b}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{b^3} \\
&= -\frac{4d\sqrt[4]{c+dx}}{b^2\sqrt[4]{a+bx}} - \frac{4(c+dx)^{5/4}}{5b(a+bx)^{5/4}} + \frac{(2d^{3/2}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{b - \sqrt{d}x^2}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{b^2} - \frac{(2d^{3/2}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{b - \sqrt{d}x^2}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{b^2} \\
&= -\frac{4d\sqrt[4]{c+dx}}{b^2\sqrt[4]{a+bx}} - \frac{4(c+dx)^{5/4}}{5b(a+bx)^{5/4}} - \frac{2d^{5/4} \tan^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{b^{9/4}} + \frac{2d^{5/4} \tanh^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{b^{9/4}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.54

$$\frac{4(c+dx)^{5/4} {}_2F_1 \left(-\frac{5}{4}, -\frac{5}{4}; -\frac{1}{4}; \frac{d(a+bx)}{ad-bc} \right)}{5b(a+bx)^{5/4} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(9/4), x]

[Out] (-4*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, -5/4, -1/4, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(a + b*x)^(5/4)*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [B] time = 0.48, size = 368, normalized size = 2.75

$$20(b^4x^2 + 2ab^3x + a^2b^2)\left(\frac{d^5}{b^9}\right)^{\frac{1}{4}} \arctan\left(\frac{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{1}{4}}b^7d\left(\frac{d^5}{b^9}\right)^{\frac{3}{4}} - (b^8x+ab^7)\sqrt{\frac{\sqrt{bx+a}\sqrt{dx+c}d^2+(b^5x+ab^4)\sqrt{\frac{d^5}{b^9}}}{bx+a}}}{bd^5x+ad^5}\right) - 5(b^4x^2 + 2ab^3x + a^2b^2)\left(\frac{d^5}{b^9}\right)^{\frac{1}{4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(9/4),x, algorithm="fricas")

[Out] -1/5*(20*(b^4*x^2 + 2*a*b^3*x + a^2*b^2)*(d^5/b^9)^(1/4)*arctan(-((b*x + a)^(3/4)*(d*x + c)^(1/4)*b^7*d*(d^5/b^9)^(3/4) - (b^8*x + a*b^7)*sqrt((sqrt(b*x + a)*sqrt(d*x + c)*d^2 + (b^5*x + a*b^4)*sqrt(d^5/b^9))/(b*x + a))*(d^5/b^9)^(3/4))/(b*d^5*x + a*d^5)) - 5*(b^4*x^2 + 2*a*b^3*x + a^2*b^2)*(d^5/b^9)^(1/4)*log(((b*x + a)^(3/4)*(d*x + c)^(1/4)*d + (b^3*x + a*b^2)*(d^5/b^9)^(1/4))/(b*x + a)) + 5*(b^4*x^2 + 2*a*b^3*x + a^2*b^2)*(d^5/b^9)^(1/4)*log(((b*x + a)^(3/4)*(d*x + c)^(1/4)*d - (b^3*x + a*b^2)*(d^5/b^9)^(1/4))/(b*x + a)) + 4*(6*b*d*x + b*c + 5*a*d)*(b*x + a)^(3/4)*(d*x + c)^(1/4))/(b^4*x^2 + 2*a*b^3*x + a^2*b^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(9/4),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(9/4), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(9/4),x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(9/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(9/4),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(9/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{5/4}}{(a + bx)^{9/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(9/4),x)

[Out] int((c + d*x)^(5/4)/(a + b*x)^(9/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{9}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/4)/(b*x+a)**(9/4),x)

[Out] Integral((c + d*x)**(5/4)/(a + b*x)**(9/4), x)

$$3.1682 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{13/4}} dx$$

Optimal. Leaf size=32

$$-\frac{4(c+dx)^{9/4}}{9(a+bx)^{9/4}(bc-ad)}$$

[Out] $-4/9*(d*x+c)^{(9/4)/(-a*d+b*c)/(b*x+a)^{(9/4)}$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{4(c+dx)^{9/4}}{9(a+bx)^{9/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^{(5/4)/(a + b*x)^{(13/4)}, x]$

[Out] $(-4*(c + d*x)^{(9/4))/(9*(b*c - a*d)*(a + b*x)^{(9/4)})$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Simp}[(a + b*x)^{(m + 1)*(c + d*x)^{(n + 1)}]/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{EqQ}[m + n + 2, 0] \&\& \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{(c+dx)^{5/4}}{(a+bx)^{13/4}} dx = -\frac{4(c+dx)^{9/4}}{9(bc-ad)(a+bx)^{9/4}}$$

Mathematica [A] time = 0.02, size = 32, normalized size = 1.00

$$-\frac{4(c+dx)^{9/4}}{9(a+bx)^{9/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(c + d*x)^{(5/4)/(a + b*x)^{(13/4)}, x]$

[Out] $(-4*(c + d*x)^{(9/4))/(9*(b*c - a*d)*(a + b*x)^{(9/4)})$

fricas [B] time = 0.47, size = 104, normalized size = 3.25

$$\frac{4(d^2x^2 + 2cdx + c^2)(bx + a)^{\frac{3}{4}}(dx + c)^{\frac{1}{4}}}{9(a^3bc - a^4d + (b^4c - ab^3d)x^3 + 3(ab^3c - a^2b^2d)x^2 + 3(a^2b^2c - a^3bd)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(13/4),x, algorithm="fricas")

[Out] $-4/9*(d^2*x^2 + 2*c*d*x + c^2)*(b*x + a)^{(3/4)}*(d*x + c)^{(1/4)}/(a^3*b*c - a^4*d + (b^4*c - a*b^3*d)*x^3 + 3*(a*b^3*c - a^2*b^2*d)*x^2 + 3*(a^2*b^2*c - a^3*b*d)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{13}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(13/4),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(13/4), x)

maple [A] time = 0.00, size = 27, normalized size = 0.84

$$\frac{4(dx + c)^{\frac{9}{4}}}{9(bx + a)^{\frac{9}{4}}(ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(13/4),x)

[Out] $4/9/(b*x+a)^{(9/4)}*(d*x+c)^{(9/4)}/(a*d-b*c)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{13}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(13/4),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(13/4), x)

mupad [B] time = 0.81, size = 99, normalized size = 3.09

$$\frac{4c^2(c+dx)^{1/4} + 4d^2x^2(c+dx)^{1/4} + 8cdx(c+dx)^{1/4}}{(a+bx)^{1/4}(9da^3 + 18da^2bx - 9ca^2b + 9dab^2x^2 - 18cab^2x - 9cb^3x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(13/4), x)

[Out] (4*c^2*(c + d*x)^(1/4) + 4*d^2*x^2*(c + d*x)^(1/4) + 8*c*d*x*(c + d*x)^(1/4)) / ((a + b*x)^(1/4) * (9*a^3*d - 9*b^3*c*x^2 - 9*a^2*b*c - 18*a*b^2*c*x + 18*a^2*b*d*x + 9*a*b^2*d*x^2))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/4)/(b*x+a)**(13/4), x)

[Out] Timed out

$$3.1683 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{17/4}} dx$$

Optimal. Leaf size=66

$$\frac{16d(c+dx)^{9/4}}{117(a+bx)^{9/4}(bc-ad)^2} - \frac{4(c+dx)^{9/4}}{13(a+bx)^{13/4}(bc-ad)}$$

[Out] $-4/13*(d*x+c)^{(9/4)/(-a*d+b*c)/(b*x+a)^{(13/4)+16/117*d*(d*x+c)^{(9/4)/(-a*d+b*c)^2/(b*x+a)^{(9/4)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{16d(c+dx)^{9/4}}{117(a+bx)^{9/4}(bc-ad)^2} - \frac{4(c+dx)^{9/4}}{13(a+bx)^{13/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/4)/(a + b*x)^(17/4), x]

[Out] $(-4*(c + d*x)^{(9/4))/(13*(b*c - a*d)*(a + b*x)^{(13/4)}) + (16*d*(c + d*x)^{(9/4))/(117*(b*c - a*d)^2*(a + b*x)^{(9/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[m] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{(c+dx)^{5/4}}{(a+bx)^{17/4}} dx = -\frac{4(c+dx)^{9/4}}{13(bc-ad)(a+bx)^{13/4}} - \frac{(4d) \int \frac{(c+dx)^{5/4}}{(a+bx)^{13/4}} dx}{13(bc-ad)}$$

$$= -\frac{4(c+dx)^{9/4}}{13(bc-ad)(a+bx)^{13/4}} + \frac{16d(c+dx)^{9/4}}{117(bc-ad)^2(a+bx)^{9/4}}$$

Mathematica [A] time = 0.03, size = 46, normalized size = 0.70

$$\frac{4(c+dx)^{9/4}(13ad-9bc+4bdx)}{117(a+bx)^{13/4}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(17/4), x]

[Out] (4*(c + d*x)^(9/4)*(-9*b*c + 13*a*d + 4*b*d*x))/(117*(b*c - a*d)^2*(a + b*x)^(13/4))

fricas [B] time = 0.51, size = 235, normalized size = 3.56

$$\frac{4(4bd^3x^3 - 9bc^3 + 13ac^2d - (bcd^2 - 13ad^3)x^2 - 2(7bc^2d - 13acd^2)x)(bx - a)}{117(a^4b^2c^2 - 2a^5bcd + a^6d^2 + (b^6c^2 - 2ab^5cd + a^2b^4d^2)x^4 + 4(ab^5c^2 - 2a^2b^4cd + a^3b^3d^2)x^3 + 6(a^2b^4c^2 - 2a^3b^3cd + a^4b^2d^2)x^2 + 4(a^3b^3c^2 - 2a^4b^2cd + a^5b^2d^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(17/4), x, algorithm="fricas")

[Out] 4/117*(4*b*d^3*x^3 - 9*b*c^3 + 13*a*c^2*d - (b*c*d^2 - 13*a*d^3)*x^2 - 2*(7*b*c^2*d - 13*a*c*d^2)*x)*(b*x + a)^(3/4)*(d*x + c)^(1/4)/(a^4*b^2*c^2 - 2*a^5*b*c*d + a^6*d^2 + (b^6*c^2 - 2*a*b^5*c*d + a^2*b^4*d^2)*x^4 + 4*(a*b^5*c^2 - 2*a^2*b^4*c*d + a^3*b^3*d^2)*x^3 + 6*(a^2*b^4*c^2 - 2*a^3*b^3*c*d + a^4*b^2*d^2)*x^2 + 4*(a^3*b^3*c^2 - 2*a^4*b^2*c*d + a^5*b*d^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{17}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(17/4), x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(17/4), x)

maple [A] time = 0.01, size = 54, normalized size = 0.82

$$\frac{4(dx+c)^{\frac{9}{4}}(4bdx+13ad-9bc)}{117(bx+a)^{\frac{13}{4}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(17/4), x)

[Out] 4/117*(d*x+c)^(9/4)*(4*b*d*x+13*a*d-9*b*c)/(b*x+a)^(13/4)/(a^2*d^2-2*a*b*c*d+b^2*c^2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{17}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(17/4), x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(17/4), x)

mupad [B] time = 0.95, size = 178, normalized size = 2.70

$$\frac{(c+dx)^{1/4} \left(\frac{16d^3x^3}{117b^2(ad-bc)^2} - \frac{36bc^3-52ac^2d}{117b^3(ad-bc)^2} + \frac{x^2(52ad^3-4bcd^2)}{117b^3(ad-bc)^2} + \frac{8cdx(13ad-7bc)}{117b^3(ad-bc)^2} \right)}{x^3(a+bx)^{1/4} + \frac{a^3(a+bx)^{1/4}}{b^3} + \frac{3ax^2(a+bx)^{1/4}}{b} + \frac{3a^2x(a+bx)^{1/4}}{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(17/4), x)

[Out] ((c + d*x)^(1/4)*((16*d^3*x^3)/(117*b^2*(a*d - b*c)^2) - (36*b*c^3 - 52*a*c^2*d)/(117*b^3*(a*d - b*c)^2) + (x^2*(52*a*d^3 - 4*b*c*d^2))/(117*b^3*(a*d - b*c)^2) + (8*c*d*x*(13*a*d - 7*b*c))/(117*b^3*(a*d - b*c)^2))/(x^3*(a + b*x)^(1/4) + (a^3*(a + b*x)^(1/4))/b^3 + (3*a*x^2*(a + b*x)^(1/4))/b + (3*a^2*x*(a + b*x)^(1/4))/b^2)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/4)/(b*x+a)**(17/4),x)
```

```
[Out] Timed out
```

$$3.1684 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{21/4}} dx$$

Optimal. Leaf size=101

$$-\frac{128d^2(c+dx)^{9/4}}{1989(a+bx)^{9/4}(bc-ad)^3} + \frac{32d(c+dx)^{9/4}}{221(a+bx)^{13/4}(bc-ad)^2} - \frac{4(c+dx)^{9/4}}{17(a+bx)^{17/4}(bc-ad)}$$

[Out] $-4/17*(d*x+c)^{(9/4)/(-a*d+b*c)/(b*x+a)^{(17/4)+32/221*d*(d*x+c)^{(9/4)/(-a*d+b*c)^2/(b*x+a)^{(13/4)-128/1989*d^2*(d*x+c)^{(9/4)/(-a*d+b*c)^3/(b*x+a)^{(9/4)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{128d^2(c+dx)^{9/4}}{1989(a+bx)^{9/4}(bc-ad)^3} + \frac{32d(c+dx)^{9/4}}{221(a+bx)^{13/4}(bc-ad)^2} - \frac{4(c+dx)^{9/4}}{17(a+bx)^{17/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/4)/(a + b*x)^(21/4), x]

[Out] $(-4*(c + d*x)^{(9/4))/(17*(b*c - a*d)*(a + b*x)^{(17/4))} + (32*d*(c + d*x)^{(9/4))/(221*(b*c - a*d)^2*(a + b*x)^{(13/4))} - (128*d^2*(c + d*x)^{(9/4))/(1989*(b*c - a*d)^3*(a + b*x)^{(9/4))}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{21/4}} dx &= -\frac{4(c+dx)^{9/4}}{17(bc-ad)(a+bx)^{17/4}} - \frac{(8d) \int \frac{(c+dx)^{5/4}}{(a+bx)^{17/4}} dx}{17(bc-ad)} \\
&= -\frac{4(c+dx)^{9/4}}{17(bc-ad)(a+bx)^{17/4}} + \frac{32d(c+dx)^{9/4}}{221(bc-ad)^2(a+bx)^{13/4}} + \frac{(32d^2) \int \frac{(c+dx)^{5/4}}{(a+bx)^{13/4}} dx}{221(bc-ad)^2} \\
&= -\frac{4(c+dx)^{9/4}}{17(bc-ad)(a+bx)^{17/4}} + \frac{32d(c+dx)^{9/4}}{221(bc-ad)^2(a+bx)^{13/4}} - \frac{128d^2(c+dx)^{9/4}}{1989(bc-ad)^3(a+bx)^{9/4}}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 77, normalized size = 0.76

$$-\frac{4(c+dx)^{9/4} \left(221a^2d^2 + 34abd(4dx-9c) + b^2(117c^2 - 72cdx + 32d^2x^2) \right)}{1989(a+bx)^{17/4}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(21/4), x]

[Out] (-4*(c + d*x)^(9/4)*(221*a^2*d^2 + 34*a*b*d*(-9*c + 4*d*x) + b^2*(117*c^2 - 72*c*d*x + 32*d^2*x^2)))/(1989*(b*c - a*d)^3*(a + b*x)^(17/4))

fricas [B] time = 0.57, size = 426, normalized size = 4.22

$$\frac{4 \left(32b^2d^4x^4 + 117b^2c^4 - 306abc^3d + 221a^2c^2d^2 - 8(b^2c^3 - 17ab^2cd^3 - 17a^2b^3c^3 - 3a^6b^2c^2d + 3a^7bcd^2 - a^8d^3 + (b^8c^3 - 3ab^7c^2d + 3a^2b^6cd^2 - a^3b^5d^3)x^5 + 5(ab^7c^3 - 3a^2b^6c^2d + 5ab^6c^3d - 17a^5b^3c^3 - 3a^6b^2c^2d + 3a^7bcd^2 - a^8d^3) \right)}{1989(a+bx)^{17/4}(bc-ad)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(21/4), x, algorithm="fricas")

[Out] -4/1989*(32*b^2*d^4*x^4 + 117*b^2*c^4 - 306*a*b*c^3*d + 221*a^2*c^2*d^2 - 8*(b^2*c^3*d^3 - 17*a*b*d^4)*x^3 + (5*b^2*c^2*d^2 - 34*a*b*c*d^3 + 221*a^2*d^4)*x^2 + 2*(81*b^2*c^3*d - 238*a*b*c^2*d^2 + 221*a^2*c*d^3)*x*(b*x + a)^(3/4)*(d*x + c)^(1/4)/(a^5*b^3*c^3 - 3*a^6*b^2*c^2*d + 3*a^7*b*c*d^2 - a^8*d^3 + (b^8*c^3 - 3*a*b^7*c^2*d + 3*a^2*b^6*c*d^2 - a^3*b^5*d^3)*x^5 + 5*(a*b^7*c^3 - 3*a^2*b^6*c^2*d + 3*a^3*b^5*c*d^2 - a^4*b^4*d^3)*x^4 + 10*(a^2*b^6*c^3 - 3*a^3*b^5*c^2*d + 3*a^4*b^4*c*d^2 - a^5*b^3*d^3)*x^3 + 10*(a^3*b^5*c^3 - 3*a^4*b^4*c^2*d + 3*a^5*b^3*c*d^2 - a^6*b^2*d^3)*x^2 + 5*(a^4*b^4*c^3 - 3*a^5*b^3*c^2*d + 3*a^6*b^2*c*d^2 - a^7*b*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{21}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(21/4),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(21/4), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{4(dx+c)^{\frac{9}{4}}(32b^2x^2d^2+136abd^2x-72b^2cdx+221a^2d^2-306abcd+117b^2c^2)}{1989(bx+a)^{\frac{17}{4}}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(21/4),x)

[Out] 4/1989*(d*x+c)^(9/4)*(32*b^2*d^2*x^2+136*a*b*d^2*x-72*b^2*c*d*x+221*a^2*d^2-306*a*b*c*d+117*b^2*c^2)/(b*x+a)^(17/4)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{21}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(21/4),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(21/4), x)

mupad [B] time = 1.13, size = 268, normalized size = 2.65

$$\frac{(c+dx)^{1/4} \left(\frac{884a^2c^2d^2-1224abc^3d+468b^2c^4}{1989b^4(ad-bc)^3} + \frac{x^2(884a^2d^4-136abcd^3+20b^2c^2d^2)}{1989b^4(ad-bc)^3} + \frac{128d^4x^4}{1989b^2(ad-bc)^3} + \frac{32d^3x^3(17ad-bc)}{1989b^3(ad-bc)^3} + \frac{8cd^2x^2}{1989b^4(ad-bc)^3} \right)}{x^4(a+bx)^{1/4} + \frac{a^4(a+bx)^{1/4}}{b^4} + \frac{6a^2x^2(a+bx)^{1/4}}{b^2} + \frac{4ax^3(a+bx)^{1/4}}{b} + \frac{4a^3x(a+bx)^{1/4}}{b^3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c+d*x)^(5/4)/(a+b*x)^(21/4),x)

[Out] ((c+d*x)^(1/4)*((468*b^2*c^4+884*a^2*c^2*d^2-1224*a*b*c^3*d)/(1989*b^4*(a*d-b*c)^3)+(x^2*(884*a^2*d^4+20*b^2*c^2*d^2-136*a*b*c*d^3))/(1989*b^4*(a*d-b*c)^3)+(128*d^4*x^4)/(1989*b^2*(a*d-b*c)^3)+(32*d^3*x^3*(17*a*d-b*c))/(1989*b^3*(a*d-b*c)^3)+(8*c*d*x*(221*a^2*d^2+81*b^2*c^2))/(1989*b^4*(a*d-b*c)^3))

$$\frac{c^2 - 238abcd}{1989b^4(ad - bc^3)} \left(\frac{1}{x^4(a + bx)^{1/4} + a^4(a + bx)^{1/4}} \right) \frac{1}{b^4} + \frac{6a^2x^2(a + bx)^{1/4}}{b^2} + \frac{4ax^3(a + bx)^{1/4}}{b} + \frac{4a^3x(a + bx)^{1/4}}{b^3}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/4)/(b*x+a)**(21/4),x)

[Out] Timed out

$$3.1685 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{25/4}} dx$$

Optimal. Leaf size=136

$$\frac{512d^3(c+dx)^{9/4}}{13923(a+bx)^{9/4}(bc-ad)^4} - \frac{128d^2(c+dx)^{9/4}}{1547(a+bx)^{13/4}(bc-ad)^3} + \frac{16d(c+dx)^{9/4}}{119(a+bx)^{17/4}(bc-ad)^2} - \frac{4(c+dx)^{9/4}}{21(a+bx)^{21/4}(bc-ad)}$$

[Out] $-4/21*(d*x+c)^{(9/4)/(-a*d+b*c)/(b*x+a)^{(21/4)+16/119*d*(d*x+c)^{(9/4)/(-a*d+b*c)^2/(b*x+a)^{(17/4)-128/1547*d^2*(d*x+c)^{(9/4)/(-a*d+b*c)^3/(b*x+a)^{(13/4)+512/13923*d^3*(d*x+c)^{(9/4)/(-a*d+b*c)^4/(b*x+a)^{(9/4)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{512d^3(c+dx)^{9/4}}{13923(a+bx)^{9/4}(bc-ad)^4} - \frac{128d^2(c+dx)^{9/4}}{1547(a+bx)^{13/4}(bc-ad)^3} + \frac{16d(c+dx)^{9/4}}{119(a+bx)^{17/4}(bc-ad)^2} - \frac{4(c+dx)^{9/4}}{21(a+bx)^{21/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/4)/(a + b*x)^(25/4), x]

[Out] $(-4*(c + d*x)^{(9/4))/(21*(b*c - a*d)*(a + b*x)^{(21/4)} + (16*d*(c + d*x)^{(9/4))/(119*(b*c - a*d)^2*(a + b*x)^{(17/4)} - (128*d^2*(c + d*x)^{(9/4))/(1547*(b*c - a*d)^3*(a + b*x)^{(13/4)} + (512*d^3*(c + d*x)^{(9/4))/(13923*(b*c - a*d)^4*(a + b*x)^{(9/4))}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{25/4}} dx &= -\frac{4(c+dx)^{9/4}}{21(bc-ad)(a+bx)^{21/4}} - \frac{(4d) \int \frac{(c+dx)^{5/4}}{(a+bx)^{21/4}} dx}{7(bc-ad)} \\
&= -\frac{4(c+dx)^{9/4}}{21(bc-ad)(a+bx)^{21/4}} + \frac{16d(c+dx)^{9/4}}{119(bc-ad)^2(a+bx)^{17/4}} + \frac{(32d^2) \int \frac{(c+dx)^{5/4}}{(a+bx)^{17/4}} dx}{119(bc-ad)^2} \\
&= -\frac{4(c+dx)^{9/4}}{21(bc-ad)(a+bx)^{21/4}} + \frac{16d(c+dx)^{9/4}}{119(bc-ad)^2(a+bx)^{17/4}} - \frac{128d^2(c+dx)^{9/4}}{1547(bc-ad)^3(a+bx)^{13/4}} - \frac{(128d^3)}{1547} \\
&= -\frac{4(c+dx)^{9/4}}{21(bc-ad)(a+bx)^{21/4}} + \frac{16d(c+dx)^{9/4}}{119(bc-ad)^2(a+bx)^{17/4}} - \frac{128d^2(c+dx)^{9/4}}{1547(bc-ad)^3(a+bx)^{13/4}} + \frac{51}{13923}
\end{aligned}$$

Mathematica [A] time = 0.07, size = 118, normalized size = 0.87

$$\frac{4(c+dx)^{9/4} (1547a^3d^3 + 357a^2bd^2(4dx-9c) + 21ab^2d(117c^2 - 72cdx + 32d^2x^2) + b^3(-663c^3 + 468c^2dx - 288cd^2x^2 + 128d^3x^3))}{13923(a+bx)^{21/4}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(25/4), x]

[Out] (4*(c + d*x)^(9/4)*(1547*a^3*d^3 + 357*a^2*b*d^2*(-9*c + 4*d*x) + 21*a*b^2*d*(117*c^2 - 72*c*d*x + 32*d^2*x^2) + b^3*(-663*c^3 + 468*c^2*d*x - 288*c*d^2*x^2 + 128*d^3*x^3)))/(13923*(b*c - a*d)^4*(a + b*x)^(21/4))

fricas [B] time = 0.68, size = 649, normalized size = 4.77

$$\frac{4(128b^3d^5x^5 - 663b^3c^5 + 2457ab^2c^4d^2 + 1547a^3c^2d^3 - 32(b^3cd^4 - 21a*b^2*d^5)*x^4 + 4(5b^3c^2d^3 - 42a*b^2*c*d^4 + 357a^2*b*d^5)*x^3 - (15b^3c^3d^2 - 105a*b^2*c^2*d^3 + 357a^2*b*c*d^4 - 1547a^3*d^5)*x^2 - 2(429b^3c^4d - 1701a*b^2*c^3*d^2 + 2499a^2*b*c^2*d^3 - 1547a^3*c*d^4)*x*(b*x + a)^(3/4)*(d*x + c)^(1/4)/(a^6*b^4*c^4 - 4a^7*b^3*c^3*d + 6a^8*b^2*c^2*d^2 - 4a^9*bcd^3 + a^{10}d^4 + (b^{10}c^4 - 4ab^9c^3d + 6a^2b^8c^2d^2 - 4a^3b^7cd^3 + a^4b^6d^4))}{13923}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(25/4), x, algorithm="fricas")

[Out] 4/13923*(128*b^3*d^5*x^5 - 663*b^3*c^5 + 2457*a*b^2*c^4*d - 3213*a^2*b*c^3*d^2 + 1547*a^3*c^2*d^3 - 32*(b^3*c*d^4 - 21*a*b^2*d^5)*x^4 + 4*(5*b^3*c^2*d^3 - 42*a*b^2*c*d^4 + 357*a^2*b*d^5)*x^3 - (15*b^3*c^3*d^2 - 105*a*b^2*c^2*d^3 + 357*a^2*b*c*d^4 - 1547*a^3*d^5)*x^2 - 2*(429*b^3*c^4*d - 1701*a*b^2*c^3*d^2 + 2499*a^2*b*c^2*d^3 - 1547*a^3*c*d^4)*x*(b*x + a)^(3/4)*(d*x + c)^(1/4)/(a^6*b^4*c^4 - 4*a^7*b^3*c^3*d + 6*a^8*b^2*c^2*d^2 - 4*a^9*b*c*d^3 + a^10*d^4 + (b^10*c^4 - 4*a*b^9*c^3*d + 6*a^2*b^8*c^2*d^2 - 4*a^3*b^7*c*d^3 + a^4*b^6*d^4)*x^6 + 6*(a*b^9*c^4 - 4*a^2*b^8*c^3*d + 6*a^3*b^7*c^2*d^2 - 4

$*a^4*b^6*c*d^3 + a^5*b^5*d^4)*x^5 + 15*(a^2*b^8*c^4 - 4*a^3*b^7*c^3*d + 6*a^4*b^6*c^2*d^2 - 4*a^5*b^5*c*d^3 + a^6*b^4*d^4)*x^4 + 20*(a^3*b^7*c^4 - 4*a^4*b^6*c^3*d + 6*a^5*b^5*c^2*d^2 - 4*a^6*b^4*c*d^3 + a^7*b^3*d^4)*x^3 + 15*(a^4*b^6*c^4 - 4*a^5*b^5*c^3*d + 6*a^6*b^4*c^2*d^2 - 4*a^7*b^3*c*d^3 + a^8*b^2*d^4)*x^2 + 6*(a^5*b^5*c^4 - 4*a^6*b^4*c^3*d + 6*a^7*b^3*c^2*d^2 - 4*a^8*b^2*c*d^3 + a^9*b*d^4)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{25}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(25/4),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(25/4), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{4(dx + c)^{\frac{9}{4}} (128b^3d^3x^3 + 672ab^2d^3x^2 - 288b^3cd^2x^2 + 1428a^2bd^3x - 1512ab^2cd^2x + 468b^3c^2dx + 1547a^3d^3 - 13923(bx + a)^{\frac{21}{4}} (a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4))}{13923(bx + a)^{\frac{21}{4}} (a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(25/4),x)

[Out] $4/13923*(d*x+c)^{(9/4)}*(128*b^3*d^3*x^3+672*a*b^2*d^3*x^2-288*b^3*c*d^2*x^2+1428*a^2*b*d^3*x-1512*a*b^2*c*d^2*x+468*b^3*c^2*d*x+1547*a^3*d^3-3213*a^2*b*c*d^2+2457*a*b^2*c^2*d-663*b^3*c^3)/(b*x+a)^{(21/4)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{25}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(25/4),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(25/4), x)

mupad [B] time = 1.36, size = 376, normalized size = 2.76

$$(c + dx)^{1/4} \left(\frac{x^2 (6188 a^3 d^5 - 1428 a^2 b c d^4 + 420 a b^2 c^2 d^3 - 60 b^3 c^3 d^2)}{13923 b^5 (a d - b c)^4} - \frac{-6188 a^3 c^2 d^3 + 12852 a^2 b c^3 d^2 - 9828 a b^2 c^4 d + 2652 b^3 c^5}{13923 b^5 (a d - b c)^4} + \frac{x (12376 a^3 d^4 - 3432 b^3 c^4 d + 13608 a^2 b^2 c^3 d^2 - 19992 a^2 b c^2 d^3)}{13923 b^5 (a d - b c)^4} + \frac{512 d^5 x^5}{13923 b^2 (a d - b c)^4} + \frac{128 d^4 x^4 (21 a d - b c)}{13923 b^3 (a d - b c)^4} + \frac{16 d^3 x^3 (357 a^2 d^2 + 5 b^2 c^2 - 42 a b c d)}{13923 b^4 (a d - b c)^4} \right) / (x^5 (a + b x)^{1/4} + \frac{a^5 (a + b x)^{1/4}}{b^5} + \frac{10 a^2 x^3 (a + b x)^{1/4}}{b^2} + \frac{10 a^3 x^2 (a + b x)^{1/4}}{b^3} + \frac{5 a x^4 (a + b x)^{1/4}}{b} + \frac{5 a^4 x (a + b x)^{1/4}}{b^4})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(25/4), x)

[Out] ((c + d*x)^(1/4)*((x^2*(6188*a^3*d^5 - 60*b^3*c^3*d^2 + 420*a*b^2*c^2*d^3 - 1428*a^2*b*c*d^4))/(13923*b^5*(a*d - b*c)^4) - (2652*b^3*c^5 - 6188*a^3*c^2*d^3 + 12852*a^2*b*c^3*d^2 - 9828*a*b^2*c^4*d)/(13923*b^5*(a*d - b*c)^4) + (x*(12376*a^3*c*d^4 - 3432*b^3*c^4*d + 13608*a*b^2*c^3*d^2 - 19992*a^2*b*c^2*d^3))/(13923*b^5*(a*d - b*c)^4) + (512*d^5*x^5)/(13923*b^2*(a*d - b*c)^4) + (128*d^4*x^4*(21*a*d - b*c))/(13923*b^3*(a*d - b*c)^4) + (16*d^3*x^3*(357*a^2*d^2 + 5*b^2*c^2 - 42*a*b*c*d))/(13923*b^4*(a*d - b*c)^4)))/(x^5*(a + b*x)^(1/4) + (a^5*(a + b*x)^(1/4))/b^5 + (10*a^2*x^3*(a + b*x)^(1/4))/b^2 + (10*a^3*x^2*(a + b*x)^(1/4))/b^3 + (5*a*x^4*(a + b*x)^(1/4))/b + (5*a^4*x*(a + b*x)^(1/4))/b^4)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/4)/(b*x+a)**(25/4), x)

[Out] Timed out

3.1686 $\int (a + bx)^{5/4} (c + dx)^{5/4} dx$

Optimal. Leaf size=408

$$\frac{5(bc - ad)^{9/2}((a + bx)(c + dx))^{3/4} \sqrt{(ad + bc + 2bdx)^2} \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{168\sqrt{2} b^{9/4} d^{9/4} (a + bx)^{3/4} (c + dx)^{3/4} (ad + bc + 2bdx) \sqrt{(ad + b(c + 2dx))}}$$

[Out] $-5/84*(-a*d+b*c)^3*(b*x+a)^{(1/4)}*(d*x+c)^{(1/4)}/b^2/d^2+1/42*(-a*d+b*c)^2*(b*x+a)^{(5/4)}*(d*x+c)^{(1/4)}/b^2/d+1/7*(-a*d+b*c)*(b*x+a)^{(9/4)}*(d*x+c)^{(1/4)}/b^2+2/7*(b*x+a)^{(9/4)}*(d*x+c)^{(5/4)}/b+5/336*(-a*d+b*c)^{(9/2)}*((b*x+a)*(d*x+c))^{(3/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/b^{(9/4)}/d^{(9/4)}/(b*x+a)^{(3/4)}/(d*x+c)^{(3/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.59, antiderivative size = 408, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 220}

$$\frac{5\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc-ad)^3}{84b^2d^2} + \frac{5(bc-ad)^{9/2}((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)}{168\sqrt{2} b^{9/4} d^{9/4} (a+bx)^{3/4} (c+dx)^{3/4} (ad+b(c+2dx))}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/4)*(c + d*x)^(5/4), x]

[Out] $(-5*(b*c - a*d)^3*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)})/(84*b^2*d^2) + ((b*c - a*d)^2*(a + b*x)^{(5/4)}*(c + d*x)^{(1/4)})/(42*b^2*d) + ((b*c - a*d)*(a + b*x)^{(9/4)}*(c + d*x)^{(1/4)})/(7*b^2) + (2*(a + b*x)^{(9/4)}*(c + d*x)^{(5/4)})/(7*b) + (5*(b*c - a*d)^{(9/2)}*((a + b*x)*(c + d*x))^{(3/4)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)]))/(b*c - a*d))*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2/((b*c - a*d)^2*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)]))/(b*c - a*d))^2]*\text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)})/\text{Sqrt}[b*c - a*d]], 1/2]/(168*\text{Sqrt}[2]*b^{(9/4)}*d^{(9/4)}*(a + b*x)^{(3/4)}*(c + d*x)^{(3/4)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[(
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x
, 1/2]]/(2*q*Sqrt[a + b*x^4]), x]] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x*d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int (a + bx)^{5/4}(c + dx)^{5/4} dx &= \frac{2(a + bx)^{9/4}(c + dx)^{5/4}}{7b} + \frac{(5(bc - ad)) \int (a + bx)^{5/4} \sqrt[4]{c + dx} dx}{14b} \\
&= \frac{(bc - ad)(a + bx)^{9/4} \sqrt[4]{c + dx}}{7b^2} + \frac{2(a + bx)^{9/4}(c + dx)^{5/4}}{7b} + \frac{(bc - ad)^2 \int \frac{(a+bx)^{5/4}}{(c+dx)^{3/4}} dx}{28b^2} \\
&= \frac{(bc - ad)^2(a + bx)^{5/4} \sqrt[4]{c + dx}}{42b^2d} + \frac{(bc - ad)(a + bx)^{9/4} \sqrt[4]{c + dx}}{7b^2} + \frac{2(a + bx)^{9/4}(c + dx)^{5/4}}{7b} \\
&= -\frac{5(bc - ad)^3 \sqrt[4]{a + bx} \sqrt[4]{c + dx}}{84b^2d^2} + \frac{(bc - ad)^2(a + bx)^{5/4} \sqrt[4]{c + dx}}{42b^2d} + \frac{(bc - ad)(a + bx)^{9/4}(c + dx)^{5/4}}{7b^2} \\
&= -\frac{5(bc - ad)^3 \sqrt[4]{a + bx} \sqrt[4]{c + dx}}{84b^2d^2} + \frac{(bc - ad)^2(a + bx)^{5/4} \sqrt[4]{c + dx}}{42b^2d} + \frac{(bc - ad)(a + bx)^{9/4}(c + dx)^{5/4}}{7b^2} \\
&= -\frac{5(bc - ad)^3 \sqrt[4]{a + bx} \sqrt[4]{c + dx}}{84b^2d^2} + \frac{(bc - ad)^2(a + bx)^{5/4} \sqrt[4]{c + dx}}{42b^2d} + \frac{(bc - ad)(a + bx)^{9/4}(c + dx)^{5/4}}{7b^2} \\
&= -\frac{5(bc - ad)^3 \sqrt[4]{a + bx} \sqrt[4]{c + dx}}{84b^2d^2} + \frac{(bc - ad)^2(a + bx)^{5/4} \sqrt[4]{c + dx}}{42b^2d} + \frac{(bc - ad)(a + bx)^{9/4}(c + dx)^{5/4}}{7b^2}
\end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.18

$$\frac{4(a + bx)^{9/4}(c + dx)^{5/4} {}_2F_1\left(-\frac{5}{4}, \frac{9}{4}, \frac{13}{4}, \frac{d(a+bx)}{ad-bc}\right)}{9b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/4)*(c + d*x)^(5/4), x]

[Out] (4*(a + b*x)^(9/4)*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, 9/4, 13/4, (d*(a + b*x))/(-(b*c) + a*d)]/(9*b*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bdx^2 + ac + (bc + ad)x\right)(bx + a)^{\frac{1}{4}}(dx + c)^{\frac{1}{4}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)*(d*x+c)^(5/4),x, algorithm="fricas")

[Out] integral((b*d*x^2 + a*c + (b*c + a*d)*x)*(b*x + a)^(1/4)*(d*x + c)^(1/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{4}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)*(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/4)*(d*x + c)^(5/4), x)

maple [F] time = 0.11, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{4}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/4)*(d*x+c)^(5/4),x)

[Out] int((b*x+a)^(5/4)*(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{4}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)*(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/4)*(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{5/4}(c + dx)^{5/4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/4)*(c + d*x)^(5/4),x)

[Out] int((a + b*x)^(5/4)*(c + d*x)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{5}{4}} (c + dx)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/4)*(d*x+c)**(5/4), x)

[Out] Integral((a + b*x)**(5/4)*(c + d*x)**(5/4), x)

$$3.1687 \quad \int \sqrt[4]{a + bx} (c + dx)^{5/4} dx$$

Optimal. Leaf size=370

$$\frac{(bc - ad)^{7/2}((a + bx)(c + dx))^{3/4} \sqrt{(ad + bc + 2bdx)^2} \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{12\sqrt{2} b^{9/4} d^{5/4} (a + bx)^{3/4} (c + dx)^{3/4} (ad + bc + 2bdx) \sqrt{(ad + b(c + 2dx))}} \text{EllipticF}$$

[Out] $\frac{1}{6}(-a*d+b*c)^2*(b*x+a)^{(1/4)}*(d*x+c)^{(1/4)}/b^2/d+1/3*(-a*d+b*c)*(b*x+a)^{(5/4)}*(d*x+c)^{(1/4)}/b^2+2/5*(b*x+a)^{(5/4)}*(d*x+c)^{(5/4)}/b-1/24*(-a*d+b*c)^{(7/2)}*((b*x+a)*(d*x+c))^{(3/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})), 1/2*2^{(1/2)})*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/b^{(9/4)}/d^{(5/4)}/(b*x+a)^{(3/4)}/(d*x+c)^{(3/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.38, antiderivative size = 370, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 220}

$$\frac{(bc - ad)^{7/2}((a + bx)(c + dx))^{3/4} \sqrt{(ad + bc + 2bdx)^2} \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}{12\sqrt{2} b^{9/4} d^{5/4} (a + bx)^{3/4} (c + dx)^{3/4} (ad + bc + 2bdx) \sqrt{(ad + b(c + 2dx))}} F\left(2\right)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/4)*(c + d*x)^(5/4), x]

[Out] $((b*c - a*d)^2*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)})/(6*b^2*d) + ((b*c - a*d)*(a + b*x)^{(5/4)}*(c + d*x)^{(1/4)})/(3*b^2) + (2*(a + b*x)^{(5/4)}*(c + d*x)^{(5/4)})/(5*b) - ((b*c - a*d)^{(7/2)}*((a + b*x)*(c + d*x))^{(3/4)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2/((b*c - a*d)^2*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))^2]*\text{EllipticF}[2*\text{ArcTan}[\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)}/\text{Sqrt}[b*c - a*d]], 1/2)]/(12*\text{Sqrt}[2]*b^{(9/4)}*d^{(5/4)}*(a + b*x)^{(3/4)}*(c + d*x)^{(3/4)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2])$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x],
1/2]]/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \sqrt[4]{a+bx} (c+dx)^{5/4} dx &= \frac{2(a+bx)^{5/4}(c+dx)^{5/4}}{5b} + \frac{(bc-ad) \int \sqrt[4]{a+bx} \sqrt[4]{c+dx} dx}{2b} \\
&= \frac{(bc-ad)(a+bx)^{5/4} \sqrt[4]{c+dx}}{3b^2} + \frac{2(a+bx)^{5/4}(c+dx)^{5/4}}{5b} + \frac{(bc-ad)^2 \int \frac{\sqrt[4]{a+bx}}{(c+dx)^{3/4}} dx}{12b^2} \\
&= \frac{(bc-ad)^2 \sqrt[4]{a+bx} \sqrt[4]{c+dx}}{6b^2d} + \frac{(bc-ad)(a+bx)^{5/4} \sqrt[4]{c+dx}}{3b^2} + \frac{2(a+bx)^{5/4}(c+dx)^{5/4}}{5b} \\
&= \frac{(bc-ad)^2 \sqrt[4]{a+bx} \sqrt[4]{c+dx}}{6b^2d} + \frac{(bc-ad)(a+bx)^{5/4} \sqrt[4]{c+dx}}{3b^2} + \frac{2(a+bx)^{5/4}(c+dx)^{5/4}}{5b} \\
&= \frac{(bc-ad)^2 \sqrt[4]{a+bx} \sqrt[4]{c+dx}}{6b^2d} + \frac{(bc-ad)(a+bx)^{5/4} \sqrt[4]{c+dx}}{3b^2} + \frac{2(a+bx)^{5/4}(c+dx)^{5/4}}{5b} \\
&= \frac{(bc-ad)^2 \sqrt[4]{a+bx} \sqrt[4]{c+dx}}{6b^2d} + \frac{(bc-ad)(a+bx)^{5/4} \sqrt[4]{c+dx}}{3b^2} + \frac{2(a+bx)^{5/4}(c+dx)^{5/4}}{5b}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.20

$$\frac{4(a+bx)^{5/4}(c+dx)^{5/4} {}_2F_1\left(-\frac{5}{4}, \frac{5}{4}, \frac{9}{4}, \frac{d(a+bx)}{ad-bc}\right)}{5b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/4)*(c + d*x)^(5/4), x]

[Out] (4*(a + b*x)^(5/4)*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, 5/4, 9/4, (d*(a + b*x))/(-b*c + a*d)]/(5*b*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bx+a\right)^{\frac{1}{4}}(dx+c)^{\frac{5}{4}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)*(d*x+c)^(5/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/4)*(d*x + c)^(5/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{4}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)*(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/4)*(d*x + c)^(5/4), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{4}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/4)*(d*x+c)^(5/4),x)

[Out] int((b*x+a)^(1/4)*(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{4}}(dx + c)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)*(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/4)*(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{1/4} (c + dx)^{5/4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/4)*(c + d*x)^(5/4),x)

[Out] int((a + b*x)^(1/4)*(c + d*x)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt[4]{a + bx} (c + dx)^{\frac{5}{4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/4)*(d*x+c)**(5/4),x)

[Out] Integral((a + b*x)**(1/4)*(c + d*x)**(5/4), x)

$$3.1688 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{3/4}} dx$$

Optimal. Leaf size=332

$$5(bc - ad)^{5/2}((a + bx)(c + dx))^{3/4} \sqrt{(ad + bc + 2bdx)^2 \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} \text{EllipticF}$$

$$6\sqrt{2} b^{9/4} \sqrt[4]{d} (a + bx)^{3/4} (c + dx)^{3/4} (ad + bc + 2bdx) \sqrt{(ad + b(c + 2dx))^2}$$

[Out] $5/3*(-a*d+b*c)*(b*x+a)^{(1/4)}*(d*x+c)^{(1/4)}/b^2+2/3*(b*x+a)^{(1/4)}*(d*x+c)^{(5/4)}/b+5/12*(-a*d+b*c)^{(5/2)}*((b*x+a)*(d*x+c))^{(3/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})), 1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c)))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/b^{(9/4)}/d^{(1/4)}/(b*x+a)^{(3/4)}/(d*x+c)^{(3/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.29, antiderivative size = 332, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 220}

$$\frac{5\sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc-ad)}{3b^2} + \frac{5(bc-ad)^{5/2}((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{6\sqrt{2} b^{9/4} \sqrt[4]{d} (a+bx)^{3/4} (c+dx)^{3/4} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/4)/(a + b*x)^(3/4), x]

[Out] $(5*(b*c - a*d)*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)})/(3*b^2) + (2*(a + b*x)^{(1/4)}*(c + d*x)^{(5/4)})/(3*b) + (5*(b*c - a*d)^{(5/2)}*((a + b*x)*(c + d*x))^{(3/4)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)]))/(b*c - a*d)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)]))/(b*c - a*d)^2))*\text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)})/\text{Sqrt}[b*c - a*d]], 1/2)]/(6*\text{Sqrt}[2]*b^{(9/4)}*d^{(1/4)}*(a + b*x)^{(3/4)}*(c + d*x)^{(3/4)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2])$

Rule 50


```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x],
1/2]]/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{3/4}} dx &= \frac{2\sqrt[4]{a+bx}(c+dx)^{5/4}}{3b} + \frac{(5(bc-ad)) \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{3/4}} dx}{6b} \\
&= \frac{5(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{3b^2} + \frac{2\sqrt[4]{a+bx}(c+dx)^{5/4}}{3b} + \frac{(5(bc-ad)^2) \int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx}{12b^2} \\
&= \frac{5(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{3b^2} + \frac{2\sqrt[4]{a+bx}(c+dx)^{5/4}}{3b} + \frac{(5(bc-ad)^2((a+bx)(c+dx))^{3/4}) \int \frac{1}{(a+bx)(c+dx)} dx}{12b^2(a+bx)^{3/4}(c+dx)^{3/4}} \\
&= \frac{5(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{3b^2} + \frac{2\sqrt[4]{a+bx}(c+dx)^{5/4}}{3b} + \frac{(5(bc-ad)^2((a+bx)(c+dx))^{3/4}\sqrt{(bc-ad)}) \int \frac{1}{(a+bx)(c+dx)} dx}{3b^2} \\
&= \frac{5(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{3b^2} + \frac{2\sqrt[4]{a+bx}(c+dx)^{5/4}}{3b} + \frac{5(bc-ad)^{5/2}((a+bx)(c+dx))^{3/4}\sqrt{(bc-ad)} \int \frac{1}{(a+bx)(c+dx)} dx}{3b^2}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 71, normalized size = 0.21

$$\frac{4\sqrt[4]{a+bx}(c+dx)^{5/4} {}_2F_1\left(-\frac{5}{4}, \frac{1}{4}; \frac{5}{4}; \frac{d(a+bx)}{ad-bc}\right)}{b\left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(3/4), x]

[Out] (4*(a + b*x)^(1/4)*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, 1/4, 5/4, (d*(a + b*x))/(-(b*c) + a*d)]/(b*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx+c)^{\frac{5}{4}}}{(bx+a)^{\frac{3}{4}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(3/4), x, algorithm="fricas")

[Out] integral((d*x + c)^(5/4)/(b*x + a)^(3/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(3/4),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(3/4), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(3/4),x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(3/4),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(3/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{5/4}}{(a + bx)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(3/4),x)

[Out] int((c + d*x)^(5/4)/(a + b*x)^(3/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/4)/(b*x+a)**(3/4),x)

[Out] Integral((c + d*x)**(5/4)/(a + b*x)**(3/4), x)

$$3.1689 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{7/4}} dx$$

Optimal. Leaf size=325

$$\frac{5d^{3/4}(bc-ad)^{3/2}((a+bx)(c+dx))^{3/4}\sqrt{(ad+bc+2bdx)^2}\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)\sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)^2}}}{3\sqrt{2}b^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^2}}$$

[Out] $10/3*d*(b*x+a)^{(1/4)}*(d*x+c)^{(1/4)}/b^{2-4/3}*(d*x+c)^{(5/4)}/b/(b*x+a)^{(3/4)}+5/6*d^{(3/4)}*(-a*d+b*c)^{(3/2)}*((b*x+a)*(d*x+c))^{(3/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c)))*((2*b*d*x+a*d+b*c)^{(1/2)}*((a*d+b*(2*d*x+c))^{(1/2)}/(-a*d+b*c)^{(1/2)}/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^{(1/2)})/b^{(9/4)}/(b*x+a)^{(3/4)}/(d*x+c)^{(3/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^{(1/2)})$

Rubi [A] time = 0.28, antiderivative size = 325, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 50, 62, 623, 220}

$$\frac{5d^{3/4}(bc-ad)^{3/2}((a+bx)(c+dx))^{3/4}\sqrt{(ad+bc+2bdx)^2}\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)\sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)^2}}}{3\sqrt{2}b^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^2}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/4)/(a + b*x)^(7/4), x]

[Out] $(10*d*(a+b*x)^{(1/4)}*(c+d*x)^{(1/4)})/(3*b^2) - (4*(c+d*x)^{(5/4)})/(3*b*(a+b*x)^{(3/4)}) + (5*d^{(3/4)}*(b*c-a*d)^{(3/2)}*((a+b*x)*(c+d*x))^{(3/4)}*\text{Sqrt}[(b*c+a*d+2*b*d*x)^2]*(1+(2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a+b*x)*(c+d*x)]))/(b*c-a*d))*\text{Sqrt}[(a*d+b*(c+2*d*x))^{(1/2)}/((b*c-a*d)^2*(1+(2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a+b*x)*(c+d*x)]))/(b*c-a*d)^2)]*\text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a+b*x)*(c+d*x))^{(1/4)})/\text{Sqrt}[b*c-a*d]],1/2]/(3*\text{Sqrt}[2]*b^{(9/4)}*(a+b*x)^{(3/4)}*(c+d*x)^{(3/4)}*(b*c+a*d+2*b*d*x)*\text{Sqrt}[(a*d+b*(c+2*d*x))^{(1/2)}])$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I

```

nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
  NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) &&
  !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &&
  & IntLinearQ[a, b, c, d, m, n, x]

```

Rule 50

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && ( !IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 62

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] :> Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]

```

Rule 220

```

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] :> With[{q = Rt[b/a, 4]}, Simp[(
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x]
, 1/2])/(2*q*Sqrt[a + b*x^4]), x]] /; FreeQ[{a, b}, x] && PosQ[b/a]

```

Rule 623

```

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] :> With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{7/4}} dx &= -\frac{4(c+dx)^{5/4}}{3b(a+bx)^{3/4}} + \frac{(5d) \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{3/4}} dx}{3b} \\
&= \frac{10d\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{3b^2} - \frac{4(c+dx)^{5/4}}{3b(a+bx)^{3/4}} + \frac{(5d(bc-ad)) \int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx}{6b^2} \\
&= \frac{10d\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{3b^2} - \frac{4(c+dx)^{5/4}}{3b(a+bx)^{3/4}} + \frac{(5d(bc-ad)((a+bx)(c+dx))^{3/4}) \int \frac{1}{(ac+(bc+ad)x+bdx^2)}}{6b^2(a+bx)^{3/4}(c+dx)^{3/4}} \\
&= \frac{10d\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{3b^2} - \frac{4(c+dx)^{5/4}}{3b(a+bx)^{3/4}} + \frac{(10d(bc-ad)((a+bx)(c+dx))^{3/4}\sqrt{(bc+ad+2bdx)}}{3b^2(a+bx)^{3/4}(c+dx)^{3/4}} \\
&= \frac{10d\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{3b^2} - \frac{4(c+dx)^{5/4}}{3b(a+bx)^{3/4}} + \frac{5d^{3/4}(bc-ad)^{3/2}((a+bx)(c+dx))^{3/4}\sqrt{(bc+ad+2bdx)}}{3\sqrt{2}b^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.22

$$\frac{4(c+dx)^{5/4} {}_2F_1\left(-\frac{5}{4}, -\frac{3}{4}; \frac{1}{4}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a+bx)^{3/4} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(7/4), x]

[Out] (-4*(c + d*x)^(5/4)*Hypergeometric2F1[-5/4, -3/4, 1/4, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(a + b*x)^(3/4)*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.44, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{5}{4}}}{b^2x^2+2abx+a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(7/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/4)*(d*x + c)^(5/4)/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(7/4),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(7/4), x)

maple [F] time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(7/4),x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(7/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(7/4),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(7/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(7/4),x)

[Out] int((c + d*x)^(5/4)/(a + b*x)^(7/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{7}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/4)/(b*x+a)**(7/4), x)

[Out] Integral((c + d*x)**(5/4)/(a + b*x)**(7/4), x)

$$3.1690 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{11/4}} dx$$

Optimal. Leaf size=325

$$\frac{5\sqrt{2} d^{7/4} \sqrt{bc-ad} ((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{21b^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^2}}$$

[Out] $-20/21*d*(d*x+c)^{(1/4)}/b^2/(b*x+a)^{(3/4)}-4/7*(d*x+c)^{(5/4)}/b/(b*x+a)^{(7/4)}+5/21*d^{(7/4)}*((b*x+a)*(d*x+c))^{(3/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)})*2^{(1/2)}*(-a*d+b*c)^{(1/2)}*(1+2*b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/b^{(9/4)}/(b*x+a)^{(3/4)}/(d*x+c)^{(3/4)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.30, antiderivative size = 325, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 62, 623, 220}

$$\frac{5\sqrt{2} d^{7/4} \sqrt{bc-ad} ((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{21b^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^2}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/4)/(a + b*x)^(11/4), x]

[Out] $(-20*d*(c+d*x)^{(1/4)})/(21*b^2*(a+b*x)^{(3/4)}) - (4*(c+d*x)^{(5/4)})/(7*b*(a+b*x)^{(7/4)}) + (5*\text{Sqrt}[2]*d^{(7/4)}*\text{Sqrt}[b*c-a*d]*((a+b*x)*(c+d*x))^{(3/4)}*\text{Sqrt}[(b*c+a*d+2*b*d*x)^2]*(1+(2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a+b*x)*(c+d*x]))/(b*c-a*d))*\text{Sqrt}[(a*d+b*(c+2*d*x))^2/((b*c-a*d)^2*(1+(2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a+b*x)*(c+d*x]))/(b*c-a*d))^2])*\text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a+b*x)*(c+d*x))^{(1/4)})/\text{Sqrt}[b*c-a*d]],1/2)]/(21*b^{(9/4)}*(a+b*x)^{(3/4)}*(c+d*x)^{(3/4)}*(b*c+a*d+2*b*d*x)*\text{Sqrt}[(a*d+b*(c+2*d*x))^2])$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x]
, 1/2]]/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{11/4}} dx &= -\frac{4(c+dx)^{5/4}}{7b(a+bx)^{7/4}} + \frac{(5d) \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{7/4}} dx}{7b} \\
&= -\frac{20d\sqrt[4]{c+dx}}{21b^2(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{7b(a+bx)^{7/4}} + \frac{(5d^2) \int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx}{21b^2} \\
&= -\frac{20d\sqrt[4]{c+dx}}{21b^2(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{7b(a+bx)^{7/4}} + \frac{(5d^2((a+bx)(c+dx))^{3/4}) \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{3/4}} dx}{21b^2(a+bx)^{3/4}(c+dx)^{3/4}} \\
&= -\frac{20d\sqrt[4]{c+dx}}{21b^2(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{7b(a+bx)^{7/4}} + \frac{(20d^2((a+bx)(c+dx))^{3/4} \sqrt{(bc+ad+2bdx)^2}) \text{Subst} \left(\int \frac{1}{\sqrt{bc-ad+2bdx}} dx \right)}{21b^2(a+bx)^{3/4}(c+dx)^{3/4}} \\
&= -\frac{20d\sqrt[4]{c+dx}}{21b^2(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{7b(a+bx)^{7/4}} + \frac{5\sqrt{2}d^{7/4}\sqrt{bc-ad}((a+bx)(c+dx))^{3/4}\sqrt{(bc+ad+2bdx)^2}}{21b^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.22

$$\frac{4(c+dx)^{5/4} {}_2F_1\left(-\frac{7}{4}, -\frac{5}{4}; -\frac{3}{4}; \frac{d(a+bx)}{ad-bc}\right)}{7b(a+bx)^{7/4} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(11/4), x]

[Out] (-4*(c + d*x)^(5/4)*Hypergeometric2F1[-7/4, -5/4, -3/4, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*(a + b*x)^(7/4)*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{1/4}(dx+c)^{5/4}}{b^3x^3+3ab^2x^2+3a^2bx+a^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(11/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/4)*(d*x + c)^(5/4)/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(11/4),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(11/4), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(11/4),x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(11/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(11/4),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(11/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{5/4}}{(a + bx)^{11/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/4)/(a + b*x)^(11/4),x)

[Out] int((c + d*x)^(5/4)/(a + b*x)^(11/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{11}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/4)/(b*x+a)**(11/4),x)

[Out] Integral((c + d*x)**(5/4)/(a + b*x)**(11/4), x)

$$3.1691 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{15/4}} dx$$

Optimal. Leaf size=363

$$10\sqrt{2} d^{11/4} ((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} \text{EllipticF}$$

$$231b^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}\sqrt{bc-ad}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^{3/4}}$$

[Out] $-20/77*d*(d*x+c)^{(1/4)}/b^2/(b*x+a)^{(7/4)}-20/231*d^2*(d*x+c)^{(1/4)}/b^2/(-a*d+b*c)/(b*x+a)^{(3/4)}-4/11*(d*x+c)^{(5/4)}/b/(b*x+a)^{(11/4)}-10/231*d^{(11/4)}*((b*x+a)*(d*x+c))^{(3/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)})*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/b^{(9/4)}/(b*x+a)^{(3/4)}/(d*x+c)^{(3/4)}/(2*b*d*x+a*d+b*c)/(-a*d+b*c)^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.35, antiderivative size = 363, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 51, 62, 623, 220}

$$\frac{20d^2\sqrt[4]{c+dx}}{231b^2(a+bx)^{3/4}(bc-ad)} \frac{10\sqrt{2} d^{11/4} ((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)}{231b^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}\sqrt{bc-ad}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^{3/4}}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/4)/(a + b*x)^(15/4), x]

[Out] $(-20*d*(c+d*x)^{(1/4)})/(77*b^2*(a+b*x)^{(7/4)}) - (20*d^2*(c+d*x)^{(1/4)})/(231*b^2*(b*c-a*d)*(a+b*x)^{(3/4)}) - (4*(c+d*x)^{(5/4)})/(11*b*(a+b*x)^{(11/4)}) - (10*\text{Sqrt}[2]*d^{(11/4)}*((a+b*x)*(c+d*x))^{(3/4)}*\text{Sqrt}[(b*c+a*d+2*b*d*x)^2]*(1+(2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a+b*x)*(c+d*x)]))/(b*c-a*d))*\text{Sqrt}[(a*d+b*(c+2*d*x))^2/((b*c-a*d)^2*(1+(2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a+b*x)*(c+d*x)]))/(b*c-a*d))^2]*\text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a+b*x)*(c+d*x))^{(1/4)})/\text{Sqrt}[b*c-a*d]],1/2)]/(231*b^{(9/4)}*\text{Sqrt}[b*c-a*d]*(a+b*x)^{(3/4)}*(c+d*x)^{(3/4)}*(b*c+a*d+2*b*d*x)*\text{Sqrt}[(a*d+b*(c+2*d*x))^2])$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(IleQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[(
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2]]*EllipticF[2*ArcTan[q*x]
, 1/2])/(2*q*Sqrt[a + b*x^4]), x]] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{15/4}} dx &= -\frac{4(c+dx)^{5/4}}{11b(a+bx)^{11/4}} + \frac{(5d) \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{11/4}} dx}{11b} \\
&= -\frac{20d\sqrt[4]{c+dx}}{77b^2(a+bx)^{7/4}} - \frac{4(c+dx)^{5/4}}{11b(a+bx)^{11/4}} + \frac{(5d^2) \int \frac{1}{(a+bx)^{7/4}(c+dx)^{3/4}} dx}{77b^2} \\
&= -\frac{20d\sqrt[4]{c+dx}}{77b^2(a+bx)^{7/4}} - \frac{20d^2\sqrt[4]{c+dx}}{231b^2(bc-ad)(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{11b(a+bx)^{11/4}} - \frac{(10d^3) \int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx}{231b^2(bc-ad)} \\
&= -\frac{20d\sqrt[4]{c+dx}}{77b^2(a+bx)^{7/4}} - \frac{20d^2\sqrt[4]{c+dx}}{231b^2(bc-ad)(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{11b(a+bx)^{11/4}} - \frac{(10d^3((a+bx)(c+dx))^3)}{231b^2(bc-ad)(a+bx)^{3/4}} \\
&= -\frac{20d\sqrt[4]{c+dx}}{77b^2(a+bx)^{7/4}} - \frac{20d^2\sqrt[4]{c+dx}}{231b^2(bc-ad)(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{11b(a+bx)^{11/4}} - \frac{(40d^3((a+bx)(c+dx))^3)}{10\sqrt{2}d^{11/4}((a+bx)(c+dx))^{3/4}} \\
&= -\frac{20d\sqrt[4]{c+dx}}{77b^2(a+bx)^{7/4}} - \frac{20d^2\sqrt[4]{c+dx}}{231b^2(bc-ad)(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{11b(a+bx)^{11/4}} - \frac{10\sqrt{2}d^{11/4}((a+bx)(c+dx))^{3/4}}{10\sqrt{2}d^{11/4}((a+bx)(c+dx))^{3/4}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.20

$$-\frac{4(c+dx)^{5/4} {}_2F_1\left(-\frac{11}{4}, -\frac{5}{4}; -\frac{7}{4}; \frac{d(a+bx)}{ad-bc}\right)}{11b(a+bx)^{11/4} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(15/4), x]

[Out] (-4*(c + d*x)^(5/4)*Hypergeometric2F1[-11/4, -5/4, -7/4, (d*(a + b*x))/(-(b*c) + a*d)]/(11*b*(a + b*x)^(11/4)*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.50, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{5}{4}}}{b^4x^4+4ab^3x^3+6a^2b^2x^2+4a^3bx+a^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(15/4), x, algorithm="fricas")

[Out] $\text{integral}((b*x + a)^{(1/4)}*(d*x + c)^{(5/4)}/(b^4*x^4 + 4*a*b^3*x^3 + 6*a^2*b^2*x^2 + 4*a^3*b*x + a^4), x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{15}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x+c)^{(5/4)}/(b*x+a)^{(15/4)},x, \text{algorithm}="giac")$

[Out] $\text{integrate}((d*x + c)^{(5/4)}/(b*x + a)^{(15/4)}, x)$

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{15}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((d*x+c)^{(5/4)}/(b*x+a)^{(15/4)},x)$

[Out] $\text{int}((d*x+c)^{(5/4)}/(b*x+a)^{(15/4)},x)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{15}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x+c)^{(5/4)}/(b*x+a)^{(15/4)},x, \text{algorithm}="maxima")$

[Out] $\text{integrate}((d*x + c)^{(5/4)}/(b*x + a)^{(15/4)}, x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{5/4}}{(a + bx)^{15/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((c + d*x)^{(5/4)}/(a + b*x)^{(15/4)},x)$

```
[Out] int((c + d*x)^(5/4)/(a + b*x)^(15/4), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/4)/(b*x+a)**(15/4), x)
```

```
[Out] Timed out
```

$$3.1692 \quad \int \frac{(c+dx)^{5/4}}{(a+bx)^{19/4}} dx$$

Optimal. Leaf size=401

$$4\sqrt{2} d^{15/4} ((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} \text{EllipticF} \\ \frac{231b^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}(bc-ad)^{3/2}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))}}{}$$

[Out] $-4/33*d*(d*x+c)^{(1/4)}/b^2/(b*x+a)^{(11/4)}-4/231*d^2*(d*x+c)^{(1/4)}/b^2/(-a*d+b*c)/(b*x+a)^{(7/4)}+8/231*d^3*(d*x+c)^{(1/4)}/b^2/(-a*d+b*c)^2/(b*x+a)^{(3/4)}-4/15*(d*x+c)^{(5/4)}/b/(b*x+a)^{(15/4)}+4/231*d^{(15/4)}*((b*x+a)*(d*x+c))^{(3/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)})*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/b^{(9/4)}/(-a*d+b*c)^{(3/2)}/(b*x+a)^{(3/4)}/(d*x+c)^{(3/4)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.43, antiderivative size = 401, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {47, 51, 62, 623, 220}

$$\frac{8d^3\sqrt[4]{c+dx}}{231b^2(a+bx)^{3/4}(bc-ad)^2} - \frac{4d^2\sqrt[4]{c+dx}}{231b^2(a+bx)^{7/4}(bc-ad)} + \frac{4\sqrt{2}d^{15/4}((a+bx)(c+dx))^{3/4}\sqrt{(ad+bc+2bdx)^2}\left(\frac{2\sqrt{b}\sqrt{d}}{bc-ad}+1\right)}{231b^{9/4}(a+bx)^{3/4}(c+dx)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/4)/(a + b*x)^(19/4), x]

[Out] $(-4*d*(c+d*x)^{(1/4)})/(33*b^2*(a+b*x)^{(11/4)}) - (4*d^2*(c+d*x)^{(1/4)})/(231*b^2*(b*c-a*d)*(a+b*x)^{(7/4)}) + (8*d^3*(c+d*x)^{(1/4)})/(231*b^2*(b*c-a*d)^2*(a+b*x)^{(3/4)}) - (4*(c+d*x)^{(5/4)})/(15*b*(a+b*x)^{(15/4)}) + (4*\text{Sqrt}[2]*d^{(15/4)}*((a+b*x)*(c+d*x))^{(3/4)}*\text{Sqrt}[(b*c+a*d+2*b*d*x)^2]*(1+(2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a+b*x)*(c+d*x)]))/(b*c-a*d))*\text{Sqrt}[(a*d+b*(c+2*d*x))^2/((b*c-a*d)^2*(1+(2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a+b*x)*(c+d*x)]))/(b*c-a*d)^2)]*\text{EllipticF}[2*\text{ArcTan}[\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a+b*x)*(c+d*x))^{(1/4)}/\text{Sqrt}[b*c-a*d]],1/2)]/(231*b^{(9/4)}*(b*c-a*d)^{(3/2)}*(a+b*x)^{(3/4)}*(c+d*x)^{(3/4)}*(b*c+a*d+2*b*d*x)*\text{Sqrt}[(a*d+b*(c+2*d*x))^2])$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
((a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
((1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2])*EllipticF[2*ArcTan[q*x],
1/2])/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/4}}{(a+bx)^{19/4}} dx &= -\frac{4(c+dx)^{5/4}}{15b(a+bx)^{15/4}} + \frac{d \int \frac{\sqrt[4]{c+dx}}{(a+bx)^{15/4}} dx}{3b} \\
&= -\frac{4d\sqrt[4]{c+dx}}{33b^2(a+bx)^{11/4}} - \frac{4(c+dx)^{5/4}}{15b(a+bx)^{15/4}} + \frac{d^2 \int \frac{1}{(a+bx)^{11/4}(c+dx)^{3/4}} dx}{33b^2} \\
&= -\frac{4d\sqrt[4]{c+dx}}{33b^2(a+bx)^{11/4}} - \frac{4d^2\sqrt[4]{c+dx}}{231b^2(bc-ad)(a+bx)^{7/4}} - \frac{4(c+dx)^{5/4}}{15b(a+bx)^{15/4}} - \frac{(2d^3) \int \frac{1}{(a+bx)^{7/4}(c+dx)^{3/4}} dx}{77b^2(bc-ad)} \\
&= -\frac{4d\sqrt[4]{c+dx}}{33b^2(a+bx)^{11/4}} - \frac{4d^2\sqrt[4]{c+dx}}{231b^2(bc-ad)(a+bx)^{7/4}} + \frac{8d^3\sqrt[4]{c+dx}}{231b^2(bc-ad)^2(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{15b(a+bx)^{15/4}} \\
&= -\frac{4d\sqrt[4]{c+dx}}{33b^2(a+bx)^{11/4}} - \frac{4d^2\sqrt[4]{c+dx}}{231b^2(bc-ad)(a+bx)^{7/4}} + \frac{8d^3\sqrt[4]{c+dx}}{231b^2(bc-ad)^2(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{15b(a+bx)^{15/4}} \\
&= -\frac{4d\sqrt[4]{c+dx}}{33b^2(a+bx)^{11/4}} - \frac{4d^2\sqrt[4]{c+dx}}{231b^2(bc-ad)(a+bx)^{7/4}} + \frac{8d^3\sqrt[4]{c+dx}}{231b^2(bc-ad)^2(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{15b(a+bx)^{15/4}} \\
&= -\frac{4d\sqrt[4]{c+dx}}{33b^2(a+bx)^{11/4}} - \frac{4d^2\sqrt[4]{c+dx}}{231b^2(bc-ad)(a+bx)^{7/4}} + \frac{8d^3\sqrt[4]{c+dx}}{231b^2(bc-ad)^2(a+bx)^{3/4}} - \frac{4(c+dx)^{5/4}}{15b(a+bx)^{15/4}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.18

$$-\frac{4(c+dx)^{5/4} {}_2F_1\left(-\frac{15}{4}, -\frac{5}{4}; -\frac{11}{4}; \frac{d(a+bx)}{ad-bc}\right)}{15b(a+bx)^{15/4} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/4)/(a + b*x)^(19/4), x]

[Out] (-4*(c + d*x)^(5/4)*Hypergeometric2F1[-15/4, -5/4, -11/4, (d*(a + b*x))/(-(b*c) + a*d)]/(15*b*(a + b*x)^(15/4)*((b*(c + d*x))/(b*c - a*d))^(5/4))

fricas [F] time = 0.58, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{5}{4}}}{b^5x^5+5ab^4x^4+10a^2b^3x^3+10a^3b^2x^2+5a^4bx+a^5}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(19/4),x, algorithm="fricas")

[Out] integral((b*x + a)^(1/4)*(d*x + c)^(5/4)/(b^5*x^5 + 5*a*b^4*x^4 + 10*a^2*b^3*x^3 + 10*a^3*b^2*x^2 + 5*a^4*b*x + a^5), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{19}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(19/4),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(19/4), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{19}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/4)/(b*x+a)^(19/4),x)

[Out] int((d*x+c)^(5/4)/(b*x+a)^(19/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{4}}}{(bx + a)^{\frac{19}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/4)/(b*x+a)^(19/4),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/4)/(b*x + a)^(19/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{\frac{5}{4}}}{(a + bx)^{\frac{19}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/4)/(a + b*x)^(19/4),x)
```

```
[Out] int((c + d*x)^(5/4)/(a + b*x)^(19/4), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/4)/(b*x+a)**(19/4),x)
```

```
[Out] Timed out
```


$$3.1693 \quad \int \frac{(a+bx)^{5/4}}{\sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=167

$$\frac{5(bc-ad)^2 \tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16b^{3/4}d^{9/4}} + \frac{5(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16b^{3/4}d^{9/4}} - \frac{5\sqrt[4]{a+bx}(c+dx)^{3/4}(bc-ad)}{8d^2} + \frac{(a+bx)^{5/4}(c+dx)^{3/4}}{2d}$$

[Out] $-5/8*(-a*d+b*c)*(b*x+a)^{(1/4)}*(d*x+c)^{(3/4)}/d^2+1/2*(b*x+a)^{(5/4)}*(d*x+c)^{(3/4)}/d+5/16*(-a*d+b*c)^2*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}*(d*x+c)^{(1/4)})/b^{(3/4)}/d^{(9/4)}+5/16*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}*(d*x+c)^{(1/4)})/b^{(3/4)}/d^{(9/4)}$

Rubi [A] time = 0.10, antiderivative size = 167, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {50, 63, 240, 212, 208, 205}

$$\frac{5(bc-ad)^2 \tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16b^{3/4}d^{9/4}} + \frac{5(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16b^{3/4}d^{9/4}} - \frac{5\sqrt[4]{a+bx}(c+dx)^{3/4}(bc-ad)}{8d^2} + \frac{(a+bx)^{5/4}(c+dx)^{3/4}}{2d}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/4)/(c + d*x)^(1/4), x]

[Out] $(-5*(b*c - a*d)*(a + b*x)^{(1/4)}*(c + d*x)^{(3/4)})/(8*d^2) + ((a + b*x)^{(5/4)}*(c + d*x)^{(3/4)})/(2*d) + (5*(b*c - a*d)^2*\operatorname{ArcTan}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(16*b^{(3/4)}*d^{(9/4)}) + (5*(b*c - a*d)^2*\operatorname{ArcTanh}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(16*b^{(3/4)}*d^{(9/4)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ

$[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 205

$\text{Int}[(a_ + (b_.)*(x_)^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(\text{Rt}[a/b, 2]*\text{ArcTan}[x/\text{Rt}[a/b, 2]])/a, x] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a/b]$

Rule 208

$\text{Int}[(a_ + (b_.)*(x_)^2)^{-1}, x_Symbol] \rightarrow \text{Simp}[(\text{Rt}[-(a/b), 2]*\text{ArcTanh}[x/\text{Rt}[-(a/b), 2]])/a, x] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{NegQ}[a/b]$

Rule 212

$\text{Int}[(a_ + (b_.)*(x_)^4)^{-1}, x_Symbol] \rightarrow \text{With}\{r = \text{Numerator}[\text{Rt}[-(a/b), 2]], s = \text{Denominator}[\text{Rt}[-(a/b), 2]]\}, \text{Dist}[r/(2*a), \text{Int}[1/(r - s*x^2), x], x] + \text{Dist}[r/(2*a), \text{Int}[1/(r + s*x^2), x], x]] \text{ /; FreeQ}\{a, b\}, x] \&\& !\text{GtQ}[a/b, 0]$

Rule 240

$\text{Int}[(a_ + (b_.)*(x_)^{(n_)})^{(p_)}, x_Symbol] \rightarrow \text{Dist}[a^{(p + 1/n)}, \text{Subst}[\text{Int}[1/(1 - b*x^n)^{(p + 1/n + 1)}, x], x, x/(a + b*x^n)^{(1/n)}], x] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{IGtQ}[n, 0] \&\& \text{LtQ}[-1, p, 0] \&\& \text{NeQ}[p, -2^{(-1)}] \&\& \text{IntegerQ}[p + 1/n]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/4}}{\sqrt[4]{c+dx}} dx &= \frac{(a+bx)^{5/4}(c+dx)^{3/4}}{2d} - \frac{(5(bc-ad)) \int \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} dx}{8d} \\
&= -\frac{5(bc-ad)\sqrt[4]{a+bx}(c+dx)^{3/4}}{8d^2} + \frac{(a+bx)^{5/4}(c+dx)^{3/4}}{2d} + \frac{(5(bc-ad)^2) \int \frac{1}{(a+bx)^{3/4}\sqrt[4]{c+dx}} dx}{32d^2} \\
&= -\frac{5(bc-ad)\sqrt[4]{a+bx}(c+dx)^{3/4}}{8d^2} + \frac{(a+bx)^{5/4}(c+dx)^{3/4}}{2d} + \frac{(5(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt[4]{c-\frac{ad}{b}+\frac{dx^4}{b}}} dx, \frac{dx}{\sqrt[4]{b}} \right)}{8bd^2} \\
&= -\frac{5(bc-ad)\sqrt[4]{a+bx}(c+dx)^{3/4}}{8d^2} + \frac{(a+bx)^{5/4}(c+dx)^{3/4}}{2d} + \frac{(5(bc-ad)^2) \text{Subst} \left(\int \frac{1}{1-\frac{dx^4}{b}} dx, \frac{dx}{\sqrt[4]{b}} \right)}{8bd^2} \\
&= -\frac{5(bc-ad)\sqrt[4]{a+bx}(c+dx)^{3/4}}{8d^2} + \frac{(a+bx)^{5/4}(c+dx)^{3/4}}{2d} + \frac{(5(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{b}-\sqrt{d}x^2} dx, \frac{dx}{\sqrt[4]{b}} \right)}{16\sqrt{b}d^2} \\
&= -\frac{5(bc-ad)\sqrt[4]{a+bx}(c+dx)^{3/4}}{8d^2} + \frac{(a+bx)^{5/4}(c+dx)^{3/4}}{2d} + \frac{5(bc-ad)^2 \tan^{-1} \left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}} \right)}{16b^{3/4}d^{9/4}} + \dots
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.44

$$\frac{4(a+bx)^{9/4} \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(\frac{1}{4}, \frac{9}{4}; \frac{13}{4}; \frac{d(a+bx)}{ad-bc} \right)}{9b\sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/4)/(c + d*x)^(1/4), x]

[Out] (4*(a + b*x)^(9/4)*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[1/4, 9/4, 13/4, (d*(a + b*x))/(-(b*c) + a*d)]/(9*b*(c + d*x)^(1/4))

fricas [B] time = 0.59, size = 1468, normalized size = 8.79

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)/(d*x+c)^(1/4), x, algorithm="fricas")

```
[Out] -1/32*(20*d^2*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^3*d^9))^(1/4)*arctan(-((b^4*c^2*d^7 - 2*a*b^3*c*d^8 + a^2*b^2*d^9)*(b*x + a)^(1/4)*(d*x + c)^(3/4))*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^3*d^9))^(3/4) - (b^2*d^8*x + b^2*c*d^7)*sqrt(((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*sqrt(b*x + a)*sqrt(d*x + c) + (b^2*d^5*x + b^2*c*d^4)*sqrt((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^3*d^9))))/(d*x + c))*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^3*d^9))^(3/4))/(b^8*c^9 - 8*a*b^7*c^8*d + 28*a^2*b^6*c^7*d^2 - 56*a^3*b^5*c^6*d^3 + 70*a^4*b^4*c^5*d^4 - 56*a^5*b^3*c^4*d^5 + 28*a^6*b^2*c^3*d^6 - 8*a^7*b*c^2*d^7 + a^8*c*d^8 + (b^8*c^8*d - 8*a*b^7*c^7*d^2 + 28*a^2*b^6*c^6*d^3 - 56*a^3*b^5*c^5*d^4 + 70*a^4*b^4*c^4*d^5 - 56*a^5*b^3*c^3*d^6 + 28*a^6*b^2*c^2*d^7 - 8*a^7*b*c*d^8 + a^8*d^9)*x)) - 5*d^2*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^3*d^9))^(1/4)*log(5*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^(1/4)*(d*x + c)^(3/4) + (b*d^3*x + b*c*d^2))*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^3*d^9))^(1/4))/(d*x + c)) + 5*d^2*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^3*d^9))^(1/4)*log(5*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^(1/4)*(d*x + c)^(3/4) - (b*d^3*x + b*c*d^2))*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b^3*d^9))^(1/4))/(d*x + c)) - 4*(4*b*d*x - 5*b*c + 9*a*d)*(b*x + a)^(1/4)*(d*x + c)^(3/4))/d^2
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{4}}}{(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(5/4)/(d*x+c)^(1/4),x, algorithm="giac")
```

```
[Out] integrate((b*x + a)^(5/4)/(d*x + c)^(1/4), x)
```

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{4}}}{(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/4)/(d*x+c)^(1/4), x)

[Out] int((b*x+a)^(5/4)/(d*x+c)^(1/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{4}}}{(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)/(d*x+c)^(1/4), x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/4)/(d*x + c)^(1/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{5}{4}}}{(c + dx)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/4)/(c + d*x)^(1/4), x)

[Out] int((a + b*x)^(5/4)/(c + d*x)^(1/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{4}}}{\sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/4)/(d*x+c)**(1/4), x)

[Out] Integral((a + b*x)**(5/4)/(c + d*x)**(1/4), x)

$$3.1694 \quad \int \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=127

$$-\frac{(bc-ad)\tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2b^{3/4}d^{5/4}} - \frac{(bc-ad)\tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2b^{3/4}d^{5/4}} + \frac{\sqrt[4]{a+bx}(c+dx)^{3/4}}{d}$$

[Out] $(b*x+a)^{(1/4)}*(d*x+c)^{(3/4)}/d-1/2*(-a*d+b*c)*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(3/4)}/d^{(5/4)}-1/2*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(3/4)}/d^{(5/4)}$

Rubi [A] time = 0.07, antiderivative size = 127, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {50, 63, 240, 212, 208, 205}

$$-\frac{(bc-ad)\tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2b^{3/4}d^{5/4}} - \frac{(bc-ad)\tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2b^{3/4}d^{5/4}} + \frac{\sqrt[4]{a+bx}(c+dx)^{3/4}}{d}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(1/4)}/(c + d*x)^{(1/4)}, x]$

[Out] $((a + b*x)^{(1/4)}*(c + d*x)^{(3/4)})/d - ((b*c - a*d)*\text{ArcTan}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(2*b^{(3/4)}*d^{(5/4)}) - ((b*c - a*d)*\text{ArcTanh}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(2*b^{(3/4)}*d^{(5/4)})$

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n-1)}, x], x] /; \text{FreeQ}\{a, b, c, d\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{NeQ}[m+n+1, 0] \ \&\& \ !(\text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{GtQ}[m, 0] \ \&\& \ \text{LtQ}[m-n, 0]))) \ \&\& \ !\text{ILtQ}[m+n+2, 0] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] /; \text{FreeQ}\{a, b, c, d\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]]$

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rule 212

Int[((a_) + (b_.)*(x_)^4)^(-1), x_Symbol] := With[{r = Numerator[Rt[-(a/b), 2]], s = Denominator[Rt[-(a/b), 2]]}, Dist[r/(2*a), Int[1/(r - s*x^2), x], x] + Dist[r/(2*a), Int[1/(r + s*x^2), x], x]] /; FreeQ[{a, b}, x] && !GtQ[a/b, 0]

Rule 240

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/n]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} dx &= \frac{\sqrt[4]{a+bx}(c+dx)^{3/4}}{d} - \frac{(bc-ad) \int \frac{1}{(a+bx)^{3/4} \sqrt[4]{c+dx}} dx}{4d} \\
&= \frac{\sqrt[4]{a+bx}(c+dx)^{3/4}}{d} - \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{1}{\sqrt[4]{c-\frac{ad}{b}+\frac{dx^4}{b}}} dx, x, \sqrt[4]{a+bx} \right)}{bd} \\
&= \frac{\sqrt[4]{a+bx}(c+dx)^{3/4}}{d} - \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{1}{1-\frac{dx^4}{b}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{bd} \\
&= \frac{\sqrt[4]{a+bx}(c+dx)^{3/4}}{d} - \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{1}{\sqrt{b-\sqrt{d}x^2}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{2\sqrt{b}d} - \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{1}{\sqrt{b+\sqrt{d}x^2}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{2\sqrt{b}d} \\
&= \frac{\sqrt[4]{a+bx}(c+dx)^{3/4}}{d} - \frac{(bc-ad) \tan^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{2b^{3/4}d^{5/4}} - \frac{(bc-ad) \tanh^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{2b^{3/4}d^{5/4}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.57

$$\frac{4(a+bx)^{5/4} \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(\frac{1}{4}, \frac{5}{4}, \frac{9}{4}, \frac{d(a+bx)}{ad-bc} \right)}{5b \sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/4)/(c + d*x)^(1/4), x]

[Out] (4*(a + b*x)^(5/4)*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[1/4, 5/4, 9/4, (d*(a + b*x))/(-b*c) + a*d])/(5*b*(c + d*x)^(1/4))

fricas [B] time = 0.49, size = 814, normalized size = 6.41

$$4d \left(\frac{b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4}{b^3d^5} \right)^{\frac{1}{4}} \arctan \left(\frac{(b^3cd^4 - ab^2d^5)(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{3}{4}} \left(\frac{b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4}{b^3d^5} \right)^{\frac{3}{4}} + (b^2d^5x + b^4c^5 - 4ab^3c^4d + 6a^2b^2c^3d^2 - 4a^3bcd^3 + a^4d^4)^{\frac{3}{4}}}{b^4c^5 - 4ab^3c^4d + 6a^2b^2c^3d^2 - 4a^3bcd^3 + a^4d^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out]
$$-1/4*(4*d*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b^3*d^5))^{1/4}*\arctan(((b^3*c*d^4 - a*b^2*d^5)*(b*x + a)^{1/4}*(d*x + c)^{3/4}*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b^3*d^5))^{3/4} + (b^2*d^5*x + b^2*c*d^4)*\sqrt{((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*\sqrt{b*x + a}*\sqrt{d*x + c} + (b^2*d^3*x + b^2*c*d^2)*\sqrt{((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b^3*d^5))})/(d*x + c))*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b^3*d^5))^{3/4})/(b^4*c^5 - 4*a*b^3*c^4*d + 6*a^2*b^2*c^3*d^2 - 4*a^3*b*c^2*d^3 + a^4*c*d^4 + (b^4*c^4*d - 4*a*b^3*c^3*d^2 + 6*a^2*b^2*c^2*d^3 - 4*a^3*b*c*d^4 + a^4*d^5)*x)) + d*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b^3*d^5))^{1/4}*\log(-((b*c - a*d)*(b*x + a)^{1/4}*(d*x + c)^{3/4} + (b*d^2*x + b*c*d)*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b^3*d^5))^{1/4}))/ (d*x + c)) - d*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b^3*d^5))^{1/4}*\log(-((b*c - a*d)*(b*x + a)^{1/4}*(d*x + c)^{3/4} - (b*d^2*x + b*c*d)*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b^3*d^5))^{1/4}))/ (d*x + c)) - 4*(b*x + a)^{1/4}*(d*x + c)^{3/4})/d$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{4}}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/4)/(d*x + c)^(1/4), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{4}}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/4)/(d*x+c)^(1/4),x)

[Out] int((b*x+a)^(1/4)/(d*x+c)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{4}}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/4)/(d*x + c)^(1/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + b x)^{1/4}}{(c + d x)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/4)/(c + d*x)^(1/4),x)

[Out] int((a + b*x)^(1/4)/(c + d*x)^(1/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[4]{a + b x}}{\sqrt[4]{c + d x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/4)/(d*x+c)**(1/4),x)

[Out] Integral((a + b*x)**(1/4)/(c + d*x)**(1/4), x)

$$3.1695 \quad \int \frac{1}{(a+bx)^{3/4} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=85

$$\frac{2 \tan^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{b^{3/4} \sqrt[4]{d}} + \frac{2 \tanh^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{b^{3/4} \sqrt[4]{d}}$$

[Out] $2 \arctan(d^{1/4} (b x + a)^{1/4} / b^{1/4} / (d x + c)^{1/4}) / b^{3/4} / d^{1/4} + 2 \operatorname{arctanh}(d^{1/4} (b x + a)^{1/4} / b^{1/4} / (d x + c)^{1/4}) / b^{3/4} / d^{1/4}$

Rubi [A] time = 0.06, antiderivative size = 85, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {63, 240, 212, 208, 205}

$$\frac{2 \tan^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{b^{3/4} \sqrt[4]{d}} + \frac{2 \tanh^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{b^{3/4} \sqrt[4]{d}}$$

Antiderivative was successfully verified.

[In] `Int[1/((a + b*x)^(3/4)*(c + d*x)^(1/4)),x]`

[Out] $(2 \operatorname{ArcTan}[(d^{1/4} (a + b x)^{1/4}) / (b^{1/4} (c + d x)^{1/4})]) / (b^{3/4} d^{1/4}) + (2 \operatorname{ArcTanh}[(d^{1/4} (a + b x)^{1/4}) / (b^{1/4} (c + d x)^{1/4})]) / (b^{3/4} d^{1/4})$

Rule 63

`Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]`

Rule 205

`Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]`

Rule 208

`Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]`

Rule 212

```
Int[((a_) + (b_.)*(x_)^4)^(-1), x_Symbol] := With[{r = Numerator[Rt[-(a/b),
2]], s = Denominator[Rt[-(a/b), 2]]}, Dist[r/(2*a), Int[1/(r - s*x^2), x],
x] + Dist[r/(2*a), Int[1/(r + s*x^2), x], x]] /; FreeQ[{a, b}, x] && !GtQ
[a/b, 0]
```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int
[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a,
b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/
n]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{3/4} \sqrt[4]{c+dx}} dx &= \frac{4 \operatorname{Subst} \left(\int \frac{1}{\sqrt[4]{c-\frac{ad}{b}+\frac{dx^4}{b}}} dx, x, \sqrt[4]{a+bx} \right)}{b} \\
&= \frac{4 \operatorname{Subst} \left(\int \frac{1}{1-\frac{dx^4}{b}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{b} \\
&= \frac{2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{b}-\sqrt{d}x^2} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{\sqrt{b}} + \frac{2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{b}+\sqrt{d}x^2} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{\sqrt{b}} \\
&= \frac{2 \tan^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{b^{3/4} \sqrt[4]{d}} + \frac{2 \tanh^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{b^{3/4} \sqrt[4]{d}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 71, normalized size = 0.84

$$\frac{4 \sqrt[4]{a+bx} \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(\frac{1}{4}, \frac{1}{4}; \frac{5}{4}; \frac{d(a+bx)}{ad-bc} \right)}{b \sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

```
[In] Integrate[1/((a + b*x)^(3/4)*(c + d*x)^(1/4)),x]
```

[Out] $(4*(a + b*x)^{(1/4)*((b*(c + d*x))/(b*c - a*d))^{(1/4)*Hypergeometric2F1[1/4, 1/4, 5/4, (d*(a + b*x))/(-b*c) + a*d]})/(b*(c + d*x)^{(1/4)})$

fricas [B] time = 0.45, size = 234, normalized size = 2.75

$$-4 \left(\frac{1}{b^3 d} \right)^{\frac{1}{4}} \arctan \left(\frac{(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{3}{4}} b^2 d \left(\frac{1}{b^3 d} \right)^{\frac{3}{4}} - (b^2 d^2 x + b^2 c d) \sqrt{\frac{(b^2 dx + b^2 c) \sqrt{\frac{1}{b^3 d} + \sqrt{bx+a} \sqrt{dx+c}}}{dx+c}} \left(\frac{1}{b^3 d} \right)^{\frac{3}{4}}}{dx+c} \right) + \left(\frac{1}{b^3 d} \right)^{\frac{1}{4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/4)/(d*x+c)^(1/4),x, algorithm="fricas")`

[Out] $-4*(1/(b^3*d))^{(1/4)*\arctan(-((b*x + a)^{(1/4)*(d*x + c)^{(3/4)*b^2*d*(1/(b^3*d))^{(3/4)} - (b^2*d^2*x + b^2*c*d)*\sqrt{((b^2*d*x + b^2*c)*\sqrt{1/(b^3*d)) + \sqrt{b*x + a}*\sqrt{d*x + c}})/(d*x + c))*(1/(b^3*d))^{(3/4))/(d*x + c)) + (1/(b^3*d))^{(1/4)*\log(((b*d*x + b*c)*(1/(b^3*d))^{(1/4)} + (b*x + a)^{(1/4)*(d*x + c)^{(3/4))/(d*x + c)) - (1/(b^3*d))^{(1/4)*\log(-((b*d*x + b*c)*(1/(b^3*d))^{(1/4)} - (b*x + a)^{(1/4)*(d*x + c)^{(3/4))/(d*x + c))}$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/4)/(d*x+c)^(1/4),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(3/4)*(d*x + c)^(1/4)), x)`

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(3/4)/(d*x+c)^(1/4),x)`

[Out] `int(1/(b*x+a)^(3/4)/(d*x+c)^(1/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/4)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/4)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{3/4} (c + dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/4)*(c + d*x)^(1/4)),x)

[Out] int(1/((a + b*x)^(3/4)*(c + d*x)^(1/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{4}} \sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/4)/(d*x+c)**(1/4),x)

[Out] Integral(1/((a + b*x)**(3/4)*(c + d*x)**(1/4)), x)

$$3.1696 \quad \int \frac{1}{(a+bx)^{7/4} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=32

$$-\frac{4(c+dx)^{3/4}}{3(a+bx)^{3/4}(bc-ad)}$$

[Out] $-4/3*(d*x+c)^{(3/4)/(-a*d+b*c)/(b*x+a)^{(3/4)}$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{4(c+dx)^{3/4}}{3(a+bx)^{3/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)^{(7/4)}*(c + d*x)^{(1/4))}, x]$

[Out] $(-4*(c + d*x)^{(3/4)})/(3*(b*c - a*d)*(a + b*x)^{(3/4)})$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}]/((b*c - a*d)*(m + 1)), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^{7/4} \sqrt[4]{c+dx}} dx = -\frac{4(c+dx)^{3/4}}{3(bc-ad)(a+bx)^{3/4}}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 1.00

$$-\frac{4(c+dx)^{3/4}}{3(a+bx)^{3/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/((a + b*x)^{(7/4)}*(c + d*x)^{(1/4))}, x]$

[Out] $(-4*(c + d*x)^{(3/4)})/(3*(b*c - a*d)*(a + b*x)^{(3/4)})$

fricas [A] time = 0.43, size = 42, normalized size = 1.31

$$\frac{4 (bx + a)^{\frac{1}{4}} (dx + c)^{\frac{3}{4}}}{3 (abc - a^2d + (b^2c - abd)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/4)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out] -4/3*(b*x + a)^(1/4)*(d*x + c)^(3/4)/(a*b*c - a^2*d + (b^2*c - a*b*d)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{4}}(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/4)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/4)*(d*x + c)^(1/4)), x)

maple [A] time = 0.00, size = 27, normalized size = 0.84

$$\frac{4 (dx + c)^{\frac{3}{4}}}{3 (bx + a)^{\frac{3}{4}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/4)/(d*x+c)^(1/4),x)

[Out] 4/3/(b*x+a)^(3/4)*(d*x+c)^(3/4)/(a*d-b*c)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{4}}(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/4)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(7/4)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{1}{(a + bx)^{7/4} (c + dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/4)*(c + d*x)^(1/4)), x)

[Out] int(1/((a + b*x)^(7/4)*(c + d*x)^(1/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{7}{4}} \sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/4)/(d*x+c)**(1/4), x)

[Out] Integral(1/((a + b*x)**(7/4)*(c + d*x)**(1/4)), x)

$$3.1697 \quad \int \frac{1}{(a+bx)^{11/4} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=66

$$\frac{16d(c+dx)^{3/4}}{21(a+bx)^{3/4}(bc-ad)^2} - \frac{4(c+dx)^{3/4}}{7(a+bx)^{7/4}(bc-ad)}$$

[Out] $-4/7*(d*x+c)^{(3/4)/(-a*d+b*c)/(b*x+a)^{(7/4)+16/21*d*(d*x+c)^{(3/4)/(-a*d+b*c)^{2/(b*x+a)^{(3/4)}}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{16d(c+dx)^{3/4}}{21(a+bx)^{3/4}(bc-ad)^2} - \frac{4(c+dx)^{3/4}}{7(a+bx)^{7/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(11/4)*(c + d*x)^(1/4)),x]

[Out] $(-4*(c+d*x)^{(3/4))/(7*(b*c-a*d)*(a+b*x)^{(7/4)}) + (16*d*(c+d*x)^{(3/4)})/(21*(b*c-a*d)^2*(a+b*x)^{(3/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{11/4} \sqrt[4]{c+dx}} dx = -\frac{4(c+dx)^{3/4}}{7(bc-ad)(a+bx)^{7/4}} - \frac{(4d) \int \frac{1}{(a+bx)^{7/4} \sqrt[4]{c+dx}} dx}{7(bc-ad)}$$

$$= -\frac{4(c+dx)^{3/4}}{7(bc-ad)(a+bx)^{7/4}} + \frac{16d(c+dx)^{3/4}}{21(bc-ad)^2(a+bx)^{3/4}}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.70

$$\frac{4(c+dx)^{3/4}(7ad-3bc+4bdx)}{21(a+bx)^{7/4}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(11/4)*(c + d*x)^(1/4)), x]

[Out] (4*(c + d*x)^(3/4)*(-3*b*c + 7*a*d + 4*b*d*x))/(21*(b*c - a*d)^2*(a + b*x)^(7/4))

fricas [B] time = 0.59, size = 118, normalized size = 1.79

$$\frac{4(4bdx - 3bc + 7ad)(bx + a)^{\frac{1}{4}}(dx + c)^{\frac{3}{4}}}{21(a^2b^2c^2 - 2a^3bcd + a^4d^2 + (b^4c^2 - 2ab^3cd + a^2b^2d^2)x^2 + 2(ab^3c^2 - 2a^2b^2cd + a^3bd^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/4)/(d*x+c)^(1/4), x, algorithm="fricas")

[Out] 4/21*(4*b*d*x - 3*b*c + 7*a*d)*(b*x + a)^(1/4)*(d*x + c)^(3/4)/(a^2*b^2*c^2 - 2*a^3*b*c*d + a^4*d^2 + (b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2)*x^2 + 2*(a*b^3*c^2 - 2*a^2*b^2*c*d + a^3*b*d^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{11}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/4)/(d*x+c)^(1/4), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(11/4)*(d*x + c)^(1/4)), x)

maple [A] time = 0.00, size = 54, normalized size = 0.82

$$\frac{4(dx+c)^{\frac{3}{4}}(4bdx+7ad-3bc)}{21(bx+a)^{\frac{7}{4}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(11/4)/(d*x+c)^(1/4),x)

[Out] 4/21*(d*x+c)^(3/4)*(4*b*d*x+7*a*d-3*b*c)/(b*x+a)^(7/4)/(a^2*d^2-2*a*b*c*d+b^2*c^2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{11}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/4)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(11/4)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{1}{(a+bx)^{\frac{11}{4}}(c+dx)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(11/4)*(c + d*x)^(1/4)),x)

[Out] int(1/((a + b*x)^(11/4)*(c + d*x)^(1/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{11}{4}}\sqrt[4]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(11/4)/(d*x+c)**(1/4),x)

[Out] Integral(1/((a + b*x)**(11/4)*(c + d*x)**(1/4)), x)

$$3.1698 \quad \int \frac{1}{(a+bx)^{15/4} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=101

$$-\frac{128d^2(c+dx)^{3/4}}{231(a+bx)^{3/4}(bc-ad)^3} + \frac{32d(c+dx)^{3/4}}{77(a+bx)^{7/4}(bc-ad)^2} - \frac{4(c+dx)^{3/4}}{11(a+bx)^{11/4}(bc-ad)}$$

[Out] $-4/11*(d*x+c)^{(3/4)/(-a*d+b*c)/(b*x+a)^{(11/4)+32/77*d*(d*x+c)^{(3/4)/(-a*d+b*c)^2/(b*x+a)^{(7/4)-128/231*d^2*(d*x+c)^{(3/4)/(-a*d+b*c)^3/(b*x+a)^{(3/4)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{128d^2(c+dx)^{3/4}}{231(a+bx)^{3/4}(bc-ad)^3} + \frac{32d(c+dx)^{3/4}}{77(a+bx)^{7/4}(bc-ad)^2} - \frac{4(c+dx)^{3/4}}{11(a+bx)^{11/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(15/4)*(c + d*x)^(1/4)), x]

[Out] $(-4*(c + d*x)^{(3/4))/(11*(b*c - a*d)*(a + b*x)^{(11/4)} + (32*d*(c + d*x)^{(3/4))/(77*(b*c - a*d)^2*(a + b*x)^{(7/4)} - (128*d^2*(c + d*x)^{(3/4))/(231*(b*c - a*d)^3*(a + b*x)^{(3/4)}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{15/4} \sqrt[4]{c+dx}} dx &= -\frac{4(c+dx)^{3/4}}{11(bc-ad)(a+bx)^{11/4}} - \frac{(8d) \int \frac{1}{(a+bx)^{11/4} \sqrt[4]{c+dx}} dx}{11(bc-ad)} \\
&= -\frac{4(c+dx)^{3/4}}{11(bc-ad)(a+bx)^{11/4}} + \frac{32d(c+dx)^{3/4}}{77(bc-ad)^2(a+bx)^{7/4}} + \frac{(32d^2) \int \frac{1}{(a+bx)^{7/4} \sqrt[4]{c+dx}} dx}{77(bc-ad)^2} \\
&= -\frac{4(c+dx)^{3/4}}{11(bc-ad)(a+bx)^{11/4}} + \frac{32d(c+dx)^{3/4}}{77(bc-ad)^2(a+bx)^{7/4}} - \frac{128d^2(c+dx)^{3/4}}{231(bc-ad)^3(a+bx)^{3/4}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 77, normalized size = 0.76

$$-\frac{4(c+dx)^{3/4} (77a^2d^2 + 22abd(4dx-3c) + b^2(21c^2 - 24cdx + 32d^2x^2))}{231(a+bx)^{11/4}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(15/4)*(c + d*x)^(1/4)), x]

[Out] (-4*(c + d*x)^(3/4)*(77*a^2*d^2 + 22*a*b*d*(-3*c + 4*d*x) + b^2*(21*c^2 - 24*c*d*x + 32*d^2*x^2))/(231*(b*c - a*d)^3*(a + b*x)^(11/4))

fricas [B] time = 1.03, size = 252, normalized size = 2.50

$$-\frac{4(32b^2d^2x^2 + 21b^2c^2 - 66abcd + 77a^2d^2 - 8(3b^2cd - 11abd^2))}{231(a^3b^3c^3 - 3a^4b^2c^2d + 3a^5bcd^2 - a^6d^3 + (b^6c^3 - 3ab^5c^2d + 3a^2b^4cd^2 - a^3b^3d^3)x^3 + 3(ab^5c^3 - 3a^2b^4c^2d + 3a^3b^3cd^2 - a^4b^2d^3)x^2 + 3(a^2b^4c^3 - 3a^3b^3c^2d + 3a^4b^2c*d^2 - a^5b*d^3)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(15/4)/(d*x+c)^(1/4), x, algorithm="fricas")

[Out] -4/231*(32*b^2*d^2*x^2 + 21*b^2*c^2 - 66*a*b*c*d + 77*a^2*d^2 - 8*(3*b^2*c*d - 11*a*b*d^2)*x)*(b*x + a)^(1/4)*(d*x + c)^(3/4)/(a^3*b^3*c^3 - 3*a^4*b^2*c^2*d + 3*a^5*b*c*d^2 - a^6*d^3 + (b^6*c^3 - 3*a*b^5*c^2*d + 3*a^2*b^4*c*d^2 - a^3*b^3*d^3)*x^3 + 3*(a*b^5*c^3 - 3*a^2*b^4*c^2*d + 3*a^3*b^3*c*d^2 - a^4*b^2*d^3)*x^2 + 3*(a^2*b^4*c^3 - 3*a^3*b^3*c^2*d + 3*a^4*b^2*c*d^2 - a^5*b*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{15}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(15/4)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(15/4)*(d*x + c)^(1/4)), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{4(dx+c)^{\frac{3}{4}}(32b^2x^2d^2+88abd^2x-24b^2cdx+77a^2d^2-66abcd+21b^2c^2)}{231(bx+a)^{\frac{11}{4}}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(15/4)/(d*x+c)^(1/4),x)

[Out] 4/231*(d*x+c)^(3/4)*(32*b^2*d^2*x^2+88*a*b*d^2*x-24*b^2*c*d*x+77*a^2*d^2-66*a*b*c*d+21*b^2*c^2)/(b*x+a)^(11/4)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{15}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(15/4)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(15/4)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{15/4}(c+dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(15/4)*(c + d*x)^(1/4)),x)

[Out] int(1/((a + b*x)^(15/4)*(c + d*x)^(1/4)), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(15/4)/(d*x+c)**(1/4),x)

[Out] Timed out

$$3.1699 \quad \int \frac{1}{(a+bx)^{19/4} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=136

$$\frac{512d^3(c+dx)^{3/4}}{1155(a+bx)^{3/4}(bc-ad)^4} - \frac{128d^2(c+dx)^{3/4}}{385(a+bx)^{7/4}(bc-ad)^3} + \frac{16d(c+dx)^{3/4}}{55(a+bx)^{11/4}(bc-ad)^2} - \frac{4(c+dx)^{3/4}}{15(a+bx)^{15/4}(bc-ad)}$$

[Out] $-4/15*(d*x+c)^{(3/4)/(-a*d+b*c)/(b*x+a)^{(15/4)}+16/55*d*(d*x+c)^{(3/4)/(-a*d+b*c)^2/(b*x+a)^{(11/4)}-128/385*d^2*(d*x+c)^{(3/4)/(-a*d+b*c)^3/(b*x+a)^{(7/4)}+12/1155*d^3*(d*x+c)^{(3/4)/(-a*d+b*c)^4/(b*x+a)^{(3/4)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{512d^3(c+dx)^{3/4}}{1155(a+bx)^{3/4}(bc-ad)^4} - \frac{128d^2(c+dx)^{3/4}}{385(a+bx)^{7/4}(bc-ad)^3} + \frac{16d(c+dx)^{3/4}}{55(a+bx)^{11/4}(bc-ad)^2} - \frac{4(c+dx)^{3/4}}{15(a+bx)^{15/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(19/4)*(c + d*x)^(1/4)), x]

[Out] $(-4*(c + d*x)^{(3/4))/(15*(b*c - a*d)*(a + b*x)^{(15/4)}) + (16*d*(c + d*x)^{(3/4))/(55*(b*c - a*d)^2*(a + b*x)^{(11/4)}) - (128*d^2*(c + d*x)^{(3/4))/(385*(b*c - a*d)^3*(a + b*x)^{(7/4)}) + (512*d^3*(c + d*x)^{(3/4))/(1155*(b*c - a*d)^4*(a + b*x)^{(3/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{19/4} \sqrt[4]{c+dx}} dx &= -\frac{4(c+dx)^{3/4}}{15(bc-ad)(a+bx)^{15/4}} - \frac{(4d) \int \frac{1}{(a+bx)^{15/4} \sqrt[4]{c+dx}} dx}{5(bc-ad)} \\
&= -\frac{4(c+dx)^{3/4}}{15(bc-ad)(a+bx)^{15/4}} + \frac{16d(c+dx)^{3/4}}{55(bc-ad)^2(a+bx)^{11/4}} + \frac{(32d^2) \int \frac{1}{(a+bx)^{11/4} \sqrt[4]{c+dx}} dx}{55(bc-ad)^2} \\
&= -\frac{4(c+dx)^{3/4}}{15(bc-ad)(a+bx)^{15/4}} + \frac{16d(c+dx)^{3/4}}{55(bc-ad)^2(a+bx)^{11/4}} - \frac{128d^2(c+dx)^{3/4}}{385(bc-ad)^3(a+bx)^{7/4}} \\
&= -\frac{4(c+dx)^{3/4}}{15(bc-ad)(a+bx)^{15/4}} + \frac{16d(c+dx)^{3/4}}{55(bc-ad)^2(a+bx)^{11/4}} - \frac{128d^2(c+dx)^{3/4}}{385(bc-ad)^3(a+bx)^{7/4}} + \dots
\end{aligned}$$

Mathematica [A] time = 0.05, size = 118, normalized size = 0.87

$$\frac{4(c+dx)^{3/4} (385a^3d^3 + 165a^2bd^2(4dx-3c) + 15ab^2d(21c^2 - 24cdx + 32d^2x^2) + b^3(-77c^3 + 84c^2dx - 96cd^2x^2 + 128d^3x^3))}{1155(a+bx)^{15/4}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(19/4)*(c + d*x)^(1/4)),x]

[Out] (4*(c + d*x)^(3/4)*(385*a^3*d^3 + 165*a^2*b*d^2*(-3*c + 4*d*x) + 15*a*b^2*d*(21*c^2 - 24*c*d*x + 32*d^2*x^2) + b^3*(-77*c^3 + 84*c^2*d*x - 96*c*d^2*x^2 + 128*d^3*x^3)))/(1155*(b*c - a*d)^4*(a + b*x)^(15/4))

fricas [B] time = 2.12, size = 419, normalized size = 3.08

$$\frac{4(128b^3d^3x^3 - 77b^3c^3 + 315ab^2c^2d)}{1155(a^4b^4c^4 - 4a^5b^3c^3d + 6a^6b^2c^2d^2 - 4a^7bcd^3 + a^8d^4 + (b^8c^4 - 4ab^7c^3d + 6a^2b^6c^2d^2 - 4a^3b^5cd^3 + a^4b^4d^4)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(19/4)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out] 4/1155*(128*b^3*d^3*x^3 - 77*b^3*c^3 + 315*a*b^2*c^2*d - 495*a^2*b*c*d^2 + 385*a^3*d^3 - 96*(b^3*c*d^2 - 5*a*b^2*d^3)*x^2 + 12*(7*b^3*c^2*d - 30*a*b^2*c*d^2 + 55*a^2*b*d^3)*x)*(b*x + a)^(1/4)*(d*x + c)^(3/4)/(a^4*b^4*c^4 - 4*a^5*b^3*c^3*d + 6*a^6*b^2*c^2*d^2 - 4*a^7*b*c*d^3 + a^8*d^4 + (b^8*c^4 - 4*a*b^7*c^3*d + 6*a^2*b^6*c^2*d^2 - 4*a^3*b^5*c*d^3 + a^4*b^4*d^4)*x^4 + 4*(a*b^7*c^4 - 4*a^2*b^6*c^3*d + 6*a^3*b^5*c^2*d^2 - 4*a^4*b^4*c*d^3 + a^5*b^3*d^4)*x^3 + 6*(a^2*b^6*c^4 - 4*a^3*b^5*c^3*d + 6*a^4*b^4*c^2*d^2 - 4*a^5*b^3*d^4)*x^2 + 4*(a^6*b^2*c^4 - 4*a^7*b*c^3*d + 6*a^8*d^4)*x + 4*(b^8*c^4 - 4*a*b^7*c^3*d + 6*a^2*b^6*c^2*d^2 - 4*a^3*b^5*c*d^3 + a^4*b^4*d^4))

$*c*d^3 + a^6*b^2*d^4)*x^2 + 4*(a^3*b^5*c^4 - 4*a^4*b^4*c^3*d + 6*a^5*b^3*c^2*d^2 - 4*a^6*b^2*c*d^3 + a^7*b*d^4)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{19}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(19/4)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(19/4)*(d*x + c)^(1/4)), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{4(dx+c)^{\frac{3}{4}}(128b^3d^3x^3 + 480ab^2d^3x^2 - 96b^3cd^2x^2 + 660a^2bd^3x - 360ab^2cd^2x + 84b^3c^2dx + 385a^3d^3 - 495a^2bd^3 - 315ab^2c^2d - 77b^3c^3)}{1155(bx+a)^{\frac{15}{4}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(19/4)/(d*x+c)^(1/4),x)

[Out] $4/1155*(d*x+c)^{(3/4)}*(128*b^3*d^3*x^3+480*a*b^2*d^3*x^2-96*b^3*c*d^2*x^2+660*a^2*b*d^3*x-360*a*b^2*c*d^2*x+84*b^3*c^2*d*x+385*a^3*d^3-495*a^2*b*c*d^2+315*a*b^2*c^2*d-77*b^3*c^3)/(b*x+a)^{(15/4)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{19}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(19/4)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(19/4)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{19/4}(c+dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a + b*x)^(19/4)*(c + d*x)^(1/4)),x)
```

```
[Out] int(1/((a + b*x)^(19/4)*(c + d*x)^(1/4)), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(19/4)/(d*x+c)**(1/4),x)
```

```
[Out] Timed out
```

$$3.1700 \quad \int \frac{(a+bx)^{7/4}}{\sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=751

$$\frac{7(bc-ad)^{7/2} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{20\sqrt{2} b^{3/4} d^{11/4} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}} \text{EllipticF}$$

[Out] $-7/15*(-a*d+b*c)*(b*x+a)^{(3/4)}*(d*x+c)^{(3/4)}/d^2+2/5*(b*x+a)^{(7/4)}*(d*x+c)^{(3/4)}/d+7/10*(-a*d+b*c)*((b*x+a)*(d*x+c))^{(1/2)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}/d^{(5/2)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/b^{(1/2)}/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))-7/20*(-a*d+b*c)^{(7/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*(b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c))^{(1/2)})^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*(b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c))^{(1/2)})^2*\text{EllipticE}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*(b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c))^{(1/2)}), 1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^{(1/2)}/b^{(3/4)}/d^{(11/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}+7/40*(-a*d+b*c)^{(7/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*(b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c))^{(1/2)})^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*(b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c))^{(1/2)})^2*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*(b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c))^{(1/2)}), 1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^{(1/2)}/b^{(3/4)}/d^{(11/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}/(1/2)$

Rubi [A] time = 0.79, antiderivative size = 751, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {50, 62, 623, 305, 220, 1196}

$$\frac{7(bc-ad)^{7/2} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{20\sqrt{2} b^{3/4} d^{11/4} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}} F\left(2 \arctan\left(\frac{b^{1/4} d^{1/4} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1\right), \frac{1}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/4)/(c + d*x)^(1/4), x]

[Out]
$$\begin{aligned} & (-7*(b*c - a*d)*(a + b*x)^{(3/4)}*(c + d*x)^{(3/4)})/(15*d^2) + (2*(a + b*x)^{(7/4)}*(c + d*x)^{(3/4)})/(5*d) + (7*(b*c - a*d)*\text{Sqrt}[(a + b*x)*(c + d*x)]*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2])/(10*\text{Sqrt}[b]*d^{(5/2)}) \\ & *(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)}*(b*c + a*d + 2*b*d*x)*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))) - (7*(b*c - a*d)^{(7/2)}*((a + b*x)*(c + d*x))^{(1/4)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))^2) \\ &]*\text{EllipticE}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)})/\text{Sqrt}[b*c - a*d]], 1/2)]/(10*\text{Sqrt}[2]*b^{(3/4)}*d^{(11/4)}*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]) + (7*(b*c - a*d)^{(7/2)}*((a + b*x)*(c + d*x))^{(1/4)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))^2) \\ &]*\text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)})/\text{Sqrt}[b*c - a*d]], 1/2)]/(20*\text{Sqrt}[2]*b^{(3/4)}*d^{(11/4)}*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]) \end{aligned}$$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 62

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[((a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[3, Denominator[m], 4]

Rule 220

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x], 1/2]]/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]

Rule 305

Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 2]}, D

`ist[1/q, Int[1/Sqrt[a + b*x^4], x], x] - Dist[1/q, Int[(1 - q*x^2)/Sqrt[a + b*x^4], x], x] /; FreeQ[{a, b}, x] && PosQ[b/a]`

Rule 623

`Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]`

Rule 1196

`Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := With[{q = Rt[c/a, 4]}, -Simp[(d*x*Sqrt[a + c*x^4])/(a*(1 + q^2*x^2)), x] + Simp[(d*(1 + q^2*x^2)*Sqrt[(a + c*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticE[2*ArcTan[q*x], 1/2])/(q*Sqrt[a + c*x^4]), x] /; EqQ[e + d*q^2, 0]] /; FreeQ[{a, c, d, e}, x] && PosQ[c/a]`

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{7/4}}{\sqrt[4]{c+dx}} dx &= \frac{2(a+bx)^{7/4}(c+dx)^{3/4}}{5d} - \frac{(7(bc-ad)) \int \frac{(a+bx)^{3/4}}{\sqrt[4]{c+dx}} dx}{10d} \\
 &= -\frac{7(bc-ad)(a+bx)^{3/4}(c+dx)^{3/4}}{15d^2} + \frac{2(a+bx)^{7/4}(c+dx)^{3/4}}{5d} + \frac{(7(bc-ad)^2) \int \frac{1}{\sqrt[4]{a+bx} \sqrt[4]{c+dx}} dx}{20d^2} \\
 &= -\frac{7(bc-ad)(a+bx)^{3/4}(c+dx)^{3/4}}{15d^2} + \frac{2(a+bx)^{7/4}(c+dx)^{3/4}}{5d} + \frac{(7(bc-ad)^2 \sqrt[4]{(a+bx)(c+dx)})}{20d^2 \sqrt[4]{a+bx} \sqrt[4]{c+dx}} \\
 &= -\frac{7(bc-ad)(a+bx)^{3/4}(c+dx)^{3/4}}{15d^2} + \frac{2(a+bx)^{7/4}(c+dx)^{3/4}}{5d} + \frac{(7(bc-ad)^2 \sqrt[4]{(a+bx)(c+dx)}) \sqrt[4]{(a+bx)(c+dx)}}{10\sqrt{b} d^{5/2} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+)} \\
 &= -\frac{7(bc-ad)(a+bx)^{3/4}(c+dx)^{3/4}}{15d^2} + \frac{2(a+bx)^{7/4}(c+dx)^{3/4}}{5d} + \frac{(7(bc-ad)^3 \sqrt[4]{(a+bx)(c+dx)}) \sqrt[4]{(a+bx)(c+dx)}}{10\sqrt{b} d^{5/2} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+)}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.10

$$\frac{4(a + bx)^{11/4} \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{4}, \frac{11}{4}; \frac{15}{4}; \frac{d(a+bx)}{ad-bc}\right)}{11b\sqrt[4]{c + dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/4)/(c + d*x)^(1/4), x]

[Out] (4*(a + b*x)^(11/4)*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[1/4, 11/4, 15/4, (d*(a + b*x))/(-(b*c) + a*d)]/(11*b*(c + d*x)^(1/4))

fricas [F] time = 0.51, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^{\frac{7}{4}}}{(dx + c)^{\frac{1}{4}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/4)/(d*x+c)^(1/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(7/4)/(d*x + c)^(1/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{4}}}{(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/4)/(d*x+c)^(1/4), x, algorithm="giac")

[Out] integrate((b*x + a)^(7/4)/(d*x + c)^(1/4), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{4}}}{(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/4)/(d*x+c)^(1/4), x)

[Out] int((b*x+a)^(7/4)/(d*x+c)^(1/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{4}}}{(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/4)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/4)/(d*x + c)^(1/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{7/4}}{(c + dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/4)/(c + d*x)^(1/4),x)

[Out] int((a + b*x)^(7/4)/(c + d*x)^(1/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{7}{4}}}{\sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/4)/(d*x+c)**(1/4),x)

[Out] Integral((a + b*x)**(7/4)/(c + d*x)**(1/4), x)

3.1701 $\int \frac{(a+bx)^{3/4}}{\sqrt[4]{c+dx}} dx$

Optimal. Leaf size=705

$$(bc - ad)^{5/2} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}$$

$$2\sqrt{2} b^{3/4} d^{7/4} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}$$

[Out] $\frac{2}{3}(b*x+a)^{(3/4)}*(d*x+c)^{(3/4)}/d - ((b*x+a)*(d*x+c))^{(1/2)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}/d^{(3/2)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/b^{(1/2)}/(1+2*b^{(1/2)*d^{(1/2)}}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}/(-a*d+b*c)^{(5/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^{(1/2)})^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})))*EllipticE(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})), 1/2*2^{(1/2)}*(1+2*b^{(1/2)*d^{(1/2)}}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)/(-a*d+b*c)^2/(1+2*b^{(1/2)*d^{(1/2)}}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)/b^{(3/4)}/d^{(7/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)} - 1/4*(-a*d+b*c)^{(5/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^{(1/2)})^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})))*EllipticF(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})), 1/2*2^{(1/2)}*(1+2*b^{(1/2)*d^{(1/2)}}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)/(-a*d+b*c)^2/(1+2*b^{(1/2)*d^{(1/2)}}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)/b^{(3/4)}/d^{(7/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.62, antiderivative size = 705, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {50, 62, 623, 305, 220, 1196}

$$(bc - ad)^{5/2} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} F\left(2\sqrt{2} b^{3/4} d^{7/4} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}\right)$$

$$2\sqrt{2} b^{3/4} d^{7/4} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(3/4)}/(c + d*x)^{(1/4)}, x]$

```
[Out] (2*(a + b*x)^(3/4)*(c + d*x)^(3/4))/(3*d) - (Sqrt[(a + b*x)*(c + d*x)]*Sqrt
[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/(Sqrt[b]*d^(3/2)*(
a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*(1 + (2*Sqrt[b]*Sqrt[d]
)*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))) + ((b*c - a*d)^(5/2)*((a + b*x)*
(c + d*x))^(1/4)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt
[(a + b*x)*(c + d*x)])/(b*c - a*d))*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*
d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))^2)]*El
lipticE[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt
[b*c - a*d]], 1/2])/(Sqrt[2]*b^(3/4)*d^(7/4)*(a + b*x)^(1/4)*(c + d*x)^(1/4)
)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2]) - ((b*c - a*d)^(5/2)
*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*
Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))*Sqrt[(a*d + b*(c + 2*d*x))^
2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c -
a*d))^2)]*EllipticF[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))
^(1/4))/Sqrt[b*c - a*d]], 1/2])/(2*Sqrt[2]*b^(3/4)*d^(7/4)*(a + b*x)^(1/4)*
(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2])
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x],
1/2])/(2*q*Sqrt[a + b*x^4]), x]] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 305

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 2]}, D
ist[1/q, Int[1/Sqrt[a + b*x^4], x], x] - Dist[1/q, Int[(1 - q*x^2)/Sqrt[a +
b*x^4], x], x]] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rule 1196

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := With[{q = Rt[c/a, 4]}, -Simp[(d*x*Sqrt[a + c*x^4])/(a*(1 + q^2*x^2)), x] + Simp[(d*(1 + q^2*x^2)*Sqrt[(a + c*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticE[2*ArcTan[q*x], 1/2])/(q*Sqrt[a + c*x^4]), x] /; EqQ[e + d*q^2, 0] /; FreeQ[{a, c, d, e}, x] && PosQ[c/a]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{3/4}}{\sqrt[4]{c+dx}} dx &= \frac{2(a+bx)^{3/4}(c+dx)^{3/4}}{3d} - \frac{(bc-ad) \int \frac{1}{\sqrt[4]{a+bx} \sqrt[4]{c+dx}} dx}{2d} \\
 &= \frac{2(a+bx)^{3/4}(c+dx)^{3/4}}{3d} - \frac{\left((bc-ad)\sqrt[4]{(a+bx)(c+dx)}\right) \int \frac{1}{\sqrt[4]{ac+(bc+ad)x+bdx^2}} dx}{2d\sqrt[4]{a+bx} \sqrt[4]{c+dx}} \\
 &= \frac{2(a+bx)^{3/4}(c+dx)^{3/4}}{3d} - \frac{\left(2(bc-ad)\sqrt[4]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}\right) \text{Subst}\left(\int \frac{1}{\sqrt{-4abx^2+4ac+(bc+ad)x+bdx^2}} dx\right)}{d\sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+ad+2bdx)} \\
 &= \frac{2(a+bx)^{3/4}(c+dx)^{3/4}}{3d} - \frac{\left((bc-ad)^2\sqrt[4]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}\right) \text{Subst}\left(\int \frac{1}{\sqrt{-4abx^2+4ac+(bc+ad)x+bdx^2}} dx\right)}{\sqrt{b} d^{3/2} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+ad+2bdx)} \\
 &= \frac{2(a+bx)^{3/4}(c+dx)^{3/4}}{3d} - \frac{\sqrt{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2} \sqrt{(ad+b(c+2dx))^2}}{\sqrt{b} d^{3/2} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+ad+2bdx) \left(1 + \frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad}\right)}
 \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.10

$$\frac{4(a+bx)^{7/4} \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{4}, \frac{7}{4}; \frac{11}{4}; \frac{d(a+bx)}{ad-bc}\right)}{7b\sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/4)/(c + d*x)^(1/4),x]

[Out] (4*(a + b*x)^(7/4)*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[1/4, 7/4, 11/4, (d*(a + b*x))/(-b*c + a*d)])/(7*b*(c + d*x)^(1/4))

fricas [F] time = 0.55, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{3}{4}}}{(dx+c)^{\frac{1}{4}}},x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out] integral((b*x + a)^(3/4)/(d*x + c)^(1/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{4}}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/4)/(d*x + c)^(1/4), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{4}}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/4)/(d*x+c)^(1/4),x)

[Out] int((b*x+a)^(3/4)/(d*x+c)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{4}}}{(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(3/4)/(d*x+c)^(1/4),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(3/4)/(d*x + c)^(1/4), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{3/4}}{(c + dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(3/4)/(c + d*x)^(1/4),x)`

[Out] `int((a + b*x)^(3/4)/(c + d*x)^(1/4), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{4}}}{\sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(3/4)/(d*x+c)**(1/4),x)`

[Out] `Integral((a + b*x)**(3/4)/(c + d*x)**(1/4), x)`

$$3.1702 \quad \int \frac{1}{\sqrt[4]{a+bx} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=688

$$\frac{(bc-ad)^{3/2} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{\sqrt{2} b^{3/4} d^{3/4} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}} \text{EllipticF}$$

[Out] $2*((b*x+a)*(d*x+c))^{(1/2)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^{(1/2)})^{(1/2)}/(-a*d+b*c)/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/b^{(1/2)}/d^{(1/2)}/(1+2*b^{(1/2)*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^{(1/2)}+1/2*(-a*d+b*c)^{(3/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^{(1/2)}*EllipticF(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)}*(1+2*b^{(1/2)*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^{(1/2)}/(-a*d+b*c)^2/(1+2*b^{(1/2)*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c)}))^{(1/2)}/b^{(3/4)}/d^{(3/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^{(1/2)}-(-a*d+b*c)^{(3/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^{(1/2)}*EllipticE(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)}*2^{(1/2)}*(1+2*b^{(1/2)*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^{(1/2)}/(-a*d+b*c)^2/(1+2*b^{(1/2)*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c)}))^{(1/2)}/b^{(3/4)}/d^{(3/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^{(1/2)})^{(1/2)}$

Rubi [A] time = 0.50, antiderivative size = 688, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {62, 623, 305, 220, 1196}

$$\frac{(bc-ad)^{3/2} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{\sqrt{2} b^{3/4} d^{3/4} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}} F\left(2 \tan^{-1}\left(\frac{\sqrt[4]{a+bx} \sqrt[4]{c+dx}}{\sqrt{2} b^{3/4} d^{3/4}}\right), x\right)$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/4)*(c + d*x)^(1/4)), x]

```
[Out] (2*Sqrt[(a + b*x)*(c + d*x)]*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/(Sqrt[b]*Sqrt[d]*(b*c - a*d)*(a + b*x)^(1/4)*(c + d*x)^(1/4)
*(b*c + a*d + 2*b*d*x)*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))) - (Sqrt[2]*(b*c - a*d)^(3/2)*((a + b*x)*(c + d*x))^(1/4)*Sqrt[
(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*S
qrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))^2]*EllipticE[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2])/(b
^(3/4)*d^(3/4)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2]) + ((b*c - a*d)^(3/2)*((a + b*x)*(c + d*x))^(1/4)*S
qrt[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[
b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))^2]*EllipticF[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2]
)/(Sqrt[2]*b^(3/4)*d^(3/4)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2])
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(a + b*x)^(m)*(c + d*x)^(m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x], 1/2])/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 305

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 2]}, Dist[1/q, Int[1/Sqrt[a + b*x^4], x], x] - Dist[1/q, Int[(1 - q*x^2)/Sqrt[a + b*x^4], x], x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rule 1196

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := With[{q =
```

Rt[c/a, 4]}, -Simp[(d*x*Sqrt[a + c*x^4])/(a*(1 + q^2*x^2)), x] + Simp[(d*(1 + q^2*x^2)*Sqrt[(a + c*x^4)/(a*(1 + q^2*x^2)^2])*EllipticE[2*ArcTan[q*x], 1/2])/(q*Sqrt[a + c*x^4]), x] /; EqQ[e + d*q^2, 0] /; FreeQ[{a, c, d, e}, x] && PosQ[c/a]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt[4]{a+bx} \sqrt[4]{c+dx}} dx &= \frac{\sqrt[4]{(a+bx)(c+dx)} \int \frac{1}{\sqrt[4]{ac+(bc+ad)x+bdx^2}} dx}{\sqrt[4]{a+bx} \sqrt[4]{c+dx}} \\ &= \frac{(4\sqrt[4]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}) \text{Subst}\left(\int \frac{x^2}{\sqrt{-4abcd+(bc+ad)^2+4bdx^4}} dx, x, \sqrt[4]{(a+bx)(c+dx)}\right)}{\sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+ad+2bdx)} \\ &= \frac{(2(bc-ad)\sqrt[4]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}) \text{Subst}\left(\int \frac{1}{\sqrt{-4abcd+(bc+ad)^2+4bdx^4}} dx, x, \sqrt[4]{(a+bx)(c+dx)}\right)}{\sqrt{b} \sqrt{d} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+ad+2bdx)} \\ &= \frac{2\sqrt{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2} \sqrt{(ad+b(c+2dx))^2}}{\sqrt{b} \sqrt{d} (bc-ad) \sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+ad+2bdx) \left(1 + \frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad}\right)} - \frac{\sqrt{2} (bc-ad)}{\sqrt{b} \sqrt{d} (bc-ad) \sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+ad+2bdx)} \end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.11

$$\frac{4(a+bx)^{3/4} \sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{4}, \frac{3}{4}; \frac{7}{4}; \frac{d(a+bx)}{ad-bc}\right)}{3b \sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/4)*(c + d*x)^(1/4)), x]

[Out] (4*(a + b*x)^(3/4)*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[1/4, 3/4, 7/4, (d*(a + b*x))/(-b*c + a*d)]/(3*b*(c + d*x)^(1/4))

fricas [F] time = 0.51, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{3}{4}}}{bdx^2+ac+(bc+ad)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/4)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out] integral((b*x + a)^(3/4)*(d*x + c)^(3/4)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{4}}(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/4)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/4)*(d*x + c)^(1/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{4}}(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/4)/(d*x+c)^(1/4),x)

[Out] int(1/(b*x+a)^(1/4)/(d*x+c)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{4}}(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/4)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/4)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{1/4}(c + dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/4)*(c + d*x)^(1/4)),x)

```
[Out] int(1/((a + b*x)^(1/4)*(c + d*x)^(1/4)), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{1}{\sqrt[4]{a+bx}\sqrt[4]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(1/4)/(d*x+c)**(1/4),x)
```

```
[Out] Integral(1/((a + b*x)**(1/4)*(c + d*x)**(1/4)), x)
```

$$3.1703 \quad \int \frac{1}{(a+bx)^{5/4} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=718

$$\frac{\sqrt{2} \sqrt[4]{d} \sqrt{bc-ad} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{b^{3/4} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}}$$

[Out] $-4*(d*x+c)^{(3/4)} / (-a*d+b*c) / (b*x+a)^{(1/4)} + 4*d^{(1/2)} * ((b*x+a)*(d*x+c))^{(1/2)}$
 $* ((2*b*d*x+a*d+b*c)^2)^{(1/2)} * ((a*d+b*(2*d*x+c))^2)^{(1/2)} / (-a*d+b*c)^2 / (b*x+a)^{(1/4)}$
 $/ (d*x+c)^{(1/4)} / (2*b*d*x+a*d+b*c) / b^{(1/2)} / (1+2*b^{(1/2)}*d^{(1/2)} * ((b*x+a)*(d*x+c))^{(1/2)})$
 $/ (-a*d+b*c) - 2*d^{(1/4)} * ((b*x+a)*(d*x+c))^{(1/4)} * (\cos(2*\arctan(b^{(1/4)}*d^{(1/4)} * ((b*x+a)*(d*x+c))^{(1/4)} * 2^{(1/2)} / (-a*d+b*c)^{(1/2)}))^{(1/2)}$
 $/ \cos(2*\arctan(b^{(1/4)}*d^{(1/4)} * ((b*x+a)*(d*x+c))^{(1/4)} * 2^{(1/2)} / (-a*d+b*c)^{(1/2)})) * \text{EllipticE}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)} * ((b*x+a)*(d*x+c))^{(1/4)} * 2^{(1/2)} / (-a*d+b*c)^{(1/2)}))$
 $, 1/2 * 2^{(1/2)} * 2^{(1/2)} * (-a*d+b*c)^{(1/2)} * (1+2*b^{(1/2)}*d^{(1/2)} * ((b*x+a)*(d*x+c))^{(1/2)}) / (-a*d+b*c) * ((2*b*d*x+a*d+b*c)^2)^{(1/2)} * ((a*d+b*(2*d*x+c))^2 / (-a*d+b*c)^2 / (1+2*b^{(1/2)}*d^{(1/2)} * ((b*x+a)*(d*x+c))^{(1/2)}) / (-a*d+b*c))^{(1/2)} / b^{(3/4)} / (b*x+a)^{(1/4)} / (d*x+c)^{(1/4)} / (2*b*d*x+a*d+b*c) / ((a*d+b*(2*d*x+c))^2)^{(1/2)} + d^{(1/4)} * ((b*x+a)*(d*x+c))^{(1/4)} * (\cos(2*\arctan(b^{(1/4)}*d^{(1/4)} * ((b*x+a)*(d*x+c))^{(1/4)} * 2^{(1/2)} / (-a*d+b*c)^{(1/2)}))^{(1/2)} / \cos(2*\arctan(b^{(1/4)}*d^{(1/4)} * ((b*x+a)*(d*x+c))^{(1/4)} * 2^{(1/2)} / (-a*d+b*c)^{(1/2)})) * \text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)} * ((b*x+a)*(d*x+c))^{(1/4)} * 2^{(1/2)} / (-a*d+b*c)^{(1/2)}))$
 $, 1/2 * 2^{(1/2)} * 2^{(1/2)} * (-a*d+b*c)^{(1/2)} * (1+2*b^{(1/2)}*d^{(1/2)} * ((b*x+a)*(d*x+c))^{(1/2)}) / (-a*d+b*c) * ((2*b*d*x+a*d+b*c)^2)^{(1/2)} * ((a*d+b*(2*d*x+c))^2 / (-a*d+b*c)^2 / (1+2*b^{(1/2)}*d^{(1/2)} * ((b*x+a)*(d*x+c))^{(1/2)}) / (-a*d+b*c))^{(1/2)} / b^{(3/4)} / (b*x+a)^{(1/4)} / (d*x+c)^{(1/4)} / (2*b*d*x+a*d+b*c) / ((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.61, antiderivative size = 718, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {51, 62, 623, 305, 220, 1196}

$$\frac{\sqrt{2} \sqrt[4]{d} \sqrt{bc-ad} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}}}{b^{3/4} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/4)*(c + d*x)^(1/4)), x]

```
[Out] (-4*(c + d*x)^(3/4))/((b*c - a*d)*(a + b*x)^(1/4)) + (4*Sqrt[d]*Sqrt[(a + b
*x)*(c + d*x)]*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])
/(Sqrt[b]*(b*c - a*d)^2*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*
x)*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))) - (2*Sq
rt[2]*d^(1/4)*Sqrt[b*c - a*d]*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b*c + a*d +
2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d)
)*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[
(a + b*x)*(c + d*x)])/(b*c - a*d))^2)]*EllipticE[2*ArcTan[(Sqrt[2]*b^(1/4)*
d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2)]/(b^(3/4)*(a +
b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))
^2]) + (Sqrt[2]*d^(1/4)*Sqrt[b*c - a*d]*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b
*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(
b*c - a*d))*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqr
t[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))^2)]*EllipticF[2*ArcTan[(Sqrt[2
]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2)]/(b^(
3/4)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c
+ 2*d*x))^2])
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x],
1/2]]/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 305

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 2]}, D
ist[1/q, Int[1/Sqrt[a + b*x^4], x], x] - Dist[1/q, Int[(1 - q*x^2)/Sqrt[a +
b*x^4], x], x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rule 1196

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := With[{q = Rt[c/a, 4]}, -Simp[(d*x*Sqrt[a + c*x^4])/(a*(1 + q^2*x^2)), x] + Simp[(d*(1 + q^2*x^2)*Sqrt[(a + c*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticE[2*ArcTan[q*x], 1/2])/(q*Sqrt[a + c*x^4]), x] /; EqQ[e + d*q^2, 0] /; FreeQ[{a, c, d, e}, x] && PosQ[c/a]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{5/4} \sqrt[4]{c+dx}} dx &= -\frac{4(c+dx)^{3/4}}{(bc-ad)\sqrt[4]{a+bx}} + \frac{(2d) \int \frac{1}{\sqrt[4]{a+bx} \sqrt[4]{c+dx}} dx}{bc-ad} \\
 &= -\frac{4(c+dx)^{3/4}}{(bc-ad)\sqrt[4]{a+bx}} + \frac{(2d \sqrt[4]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[4]{ac+(bc+ad)x+bdx^2}}} dx}{(bc-ad)\sqrt[4]{a+bx} \sqrt[4]{c+dx}} \\
 &= -\frac{4(c+dx)^{3/4}}{(bc-ad)\sqrt[4]{a+bx}} + \frac{(8d \sqrt[4]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}) \text{Subst} \left(\int \frac{1}{\sqrt{-4abcd}} \right)}{(bc-ad)\sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+ad+2bdx)} \\
 &= -\frac{4(c+dx)^{3/4}}{(bc-ad)\sqrt[4]{a+bx}} + \frac{(4\sqrt{d} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2}) \text{Subst} \left(\int \frac{1}{\sqrt{-4abcd}} \right)}{\sqrt{b} \sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+ad+2bdx)} \\
 &= -\frac{4(c+dx)^{3/4}}{(bc-ad)\sqrt[4]{a+bx}} + \frac{4\sqrt{d} \sqrt{(a+bx)(c+dx)} \sqrt{(bc+ad+2bdx)^2} \sqrt{(ad+b(c+dx))}}{\sqrt{b} (bc-ad)^2 \sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc+ad+2bdx) \left(1 + \frac{2\sqrt{b}\sqrt{d}}{\sqrt{bc-ad}}\right)}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.10

$$-\frac{4\sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{4}, \frac{1}{4}; \frac{3}{4}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[4]{a+bx} \sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/4)*(c + d*x)^(1/4)),x]

[Out] (-4*((b*(c + d*x))/(b*c - a*d))^(1/4)*Hypergeometric2F1[-1/4, 1/4, 3/4, (d*(a + b*x))/(-b*c) + a*d])/(b*(a + b*x)^(1/4)*(c + d*x)^(1/4))

fricas [F] time = 0.52, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^{\frac{3}{4}}(dx + c)^{\frac{3}{4}}}{b^2dx^3 + a^2c + (b^2c + 2abd)x^2 + (2abc + a^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/4)/(d*x+c)^(1/4),x, algorithm="fricas")

[Out] integral((b*x + a)^(3/4)*(d*x + c)^(3/4)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{4}}(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/4)/(d*x+c)^(1/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/4)*(d*x + c)^(1/4)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{4}}(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/4)/(d*x+c)^(1/4),x)

[Out] int(1/(b*x+a)^(5/4)/(d*x+c)^(1/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{4}}(dx + c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/4)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/4)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{5/4} (c + dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/4)*(c + d*x)^(1/4)),x)

[Out] int(1/((a + b*x)^(5/4)*(c + d*x)^(1/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{5/4} \sqrt[4]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/4)/(d*x+c)**(1/4),x)

[Out] Integral(1/((a + b*x)**(5/4)*(c + d*x)**(1/4)), x)

$$3.1704 \quad \int \frac{1}{(a+bx)^{9/4} \sqrt[4]{c+dx}} dx$$

Optimal. Leaf size=760

$$2\sqrt{2} d^{5/4} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} \text{EllipticF}$$

$$\frac{5b^{3/4} \sqrt[4]{a+bx} \sqrt[4]{c+dx} \sqrt{bc-ad} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}}{2\sqrt{2} d^{5/4} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)}} \text{EllipticF}$$

[Out] $-4/5*(d*x+c)^{(3/4)/(-a*d+b*c)/(b*x+a)^{(5/4)+8/5*d*(d*x+c)^{(3/4)/(-a*d+b*c)^2/(b*x+a)^{(1/4)-8/5*d^{(3/2)*((b*x+a)*(d*x+c))^{(1/2)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*((a*d+b*(2*d*x+c))^2)^{(1/2)/(-a*d+b*c)^3/(b*x+a)^{(1/4)/(d*x+c)^{(1/4)/(2*b*d*x+a*d+b*c)/b^{(1/2)/(1+2*b^{(1/2)*d^{(1/2)*((b*x+a)*(d*x+c))^{(1/2)/(-a*d+b*c))}+4/5*d^{(5/4)*((b*x+a)*(d*x+c))^{(1/4)*(cos(2*arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)/(-a*d+b*c)^{(1/2))})^2)^{(1/2)/cos(2*arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)/(-a*d+b*c)^{(1/2))})})*EllipticE(sin(2*arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)/(-a*d+b*c)^{(1/2))})})}, 1/2*2^{(1/2)})*2^{(1/2)*(1+2*b^{(1/2)*d^{(1/2)*((b*x+a)*(d*x+c))^{(1/2)/(-a*d+b*c)})})*((2*b*d*x+a*d+b*c)^2)^{(1/2)*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/2)*d^{(1/2)*((b*x+a)*(d*x+c))^{(1/2)/(-a*d+b*c)})^2)^{(1/2)/b^{(3/4)/(b*x+a)^{(1/4)/(d*x+c)^{(1/4)/(2*b*d*x+a*d+b*c)/(-a*d+b*c)^{(1/2)/((a*d+b*(2*d*x+c))^2)^{(1/2)-2/5*d^{(5/4)*((b*x+a)*(d*x+c))^{(1/4)*(cos(2*arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)/(-a*d+b*c)^{(1/2))})^2)^{(1/2)/cos(2*arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)/(-a*d+b*c)^{(1/2))})})*EllipticF(sin(2*arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)/(-a*d+b*c)^{(1/2))})})}, 1/2*2^{(1/2)})*2^{(1/2)*(1+2*b^{(1/2)*d^{(1/2)*((b*x+a)*(d*x+c))^{(1/2)/(-a*d+b*c)})})*((2*b*d*x+a*d+b*c)^2)^{(1/2)*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/2)*d^{(1/2)*((b*x+a)*(d*x+c))^{(1/2)/(-a*d+b*c)})^2)^{(1/2)/b^{(3/4)/(b*x+a)^{(1/4)/(d*x+c)^{(1/4)/(2*b*d*x+a*d+b*c)/(-a*d+b*c)^{(1/2)/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.73, antiderivative size = 760, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {51, 62, 623, 305, 220, 1196}

$$2\sqrt{2} d^{5/4} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} F\left(2 \tan^{-1} \frac{\sqrt{bc-ad} \sqrt{(ad+b(c+2dx))^2}}{2\sqrt{2} d^{5/4} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)}}\right)$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(9/4)*(c + d*x)^(1/4)),x]

[Out]
$$\begin{aligned} & (-4*(c + d*x)^{(3/4)})/(5*(b*c - a*d)*(a + b*x)^{(5/4)}) + (8*d*(c + d*x)^{(3/4)})/(5*(b*c - a*d)^2*(a + b*x)^{(1/4)}) - (8*d^{(3/2)}*\text{Sqrt}[(a + b*x)*(c + d*x)]* \\ & \text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2])/(5*\text{Sqrt}[b]*(b*c - a*d)^3*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)}*(b*c + a*d + 2*b*d*x)*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))) + (4*\text{Sqrt}[2]*d^{(5/4)} \\ & *((a + b*x)*(c + d*x))^{(1/4)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))^2)]* \\ & \text{EllipticE}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)})/\text{Sqrt}[b*c - a*d]], 1/2)]/(5*b^{(3/4)}*\text{Sqrt}[b*c - a*d]*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]) - (2*\text{Sqrt}[2]*d^{(5/4)}*((a + b*x)*(c + d*x))^{(1/4)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))^2)]* \\ & \text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)})/\text{Sqrt}[b*c - a*d]], 1/2)]/(5*b^{(3/4)}*\text{Sqrt}[b*c - a*d]*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2]) \end{aligned}$$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 62

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[((a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[3, Denominator[m], 4]

Rule 220

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[((1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2])*EllipticF[2*ArcTan[q*x], 1/2])/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]

Rule 305

Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 2]}, D

`Int[1/q, Int[1/Sqrt[a + b*x^4], x], x] - Dist[1/q, Int[(1 - q*x^2)/Sqrt[a + b*x^4], x], x] /; FreeQ[{a, b}, x] && PosQ[b/a]`

Rule 623

`Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]`

Rule 1196

`Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := With[{q = Rt[c/a, 4]}, -Simp[(d*x*Sqrt[a + c*x^4])/(a*(1 + q^2*x^2)), x] + Simp[(d*(1 + q^2*x^2)*Sqrt[(a + c*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticE[2*ArcTan[q*x], 1/2])/(q*Sqrt[a + c*x^4]), x] /; EqQ[e + d*q^2, 0]] /; FreeQ[{a, c, d, e}, x] && PosQ[c/a]`

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{9/4} \sqrt[4]{c+dx}} dx &= -\frac{4(c+dx)^{3/4}}{5(bc-ad)(a+bx)^{5/4}} - \frac{(2d) \int \frac{1}{(a+bx)^{5/4} \sqrt[4]{c+dx}} dx}{5(bc-ad)} \\
 &= -\frac{4(c+dx)^{3/4}}{5(bc-ad)(a+bx)^{5/4}} + \frac{8d(c+dx)^{3/4}}{5(bc-ad)^2 \sqrt[4]{a+bx}} - \frac{(4d^2) \int \frac{1}{\sqrt[4]{a+bx} \sqrt[4]{c+dx}} dx}{5(bc-ad)^2} \\
 &= -\frac{4(c+dx)^{3/4}}{5(bc-ad)(a+bx)^{5/4}} + \frac{8d(c+dx)^{3/4}}{5(bc-ad)^2 \sqrt[4]{a+bx}} - \frac{(4d^2 \sqrt[4]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[4]{ac+(bc+ad)x}} dx}{5(bc-ad)^2 \sqrt[4]{a+bx} \sqrt[4]{c+dx}} \\
 &= -\frac{4(c+dx)^{3/4}}{5(bc-ad)(a+bx)^{5/4}} + \frac{8d(c+dx)^{3/4}}{5(bc-ad)^2 \sqrt[4]{a+bx}} - \frac{(16d^2 \sqrt[4]{(a+bx)(c+dx)} \sqrt{(bc+ad)})}{5(bc-ad)^2} \\
 &= -\frac{4(c+dx)^{3/4}}{5(bc-ad)(a+bx)^{5/4}} + \frac{8d(c+dx)^{3/4}}{5(bc-ad)^2 \sqrt[4]{a+bx}} - \frac{(8d^{3/2} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(bc+ad)})}{5\sqrt{b}(bc-ad)} \\
 &= -\frac{4(c+dx)^{3/4}}{5(bc-ad)(a+bx)^{5/4}} + \frac{8d(c+dx)^{3/4}}{5(bc-ad)^2 \sqrt[4]{a+bx}} - \frac{8d^{3/2} \sqrt{(a+bx)(c+dx)} \sqrt{(bc+ad)}}{5\sqrt{b}(bc-ad)^3 \sqrt[4]{a+bx} \sqrt[4]{c+dx}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.10

$$\frac{4\sqrt[4]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{5}{4}, \frac{1}{4}; -\frac{1}{4}; \frac{d(a+bx)}{ad-bc}\right)}{5b(a+bx)^{5/4}\sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(9/4)*(c + d*x)^(1/4)), x]

[Out] $(-4*((b*(c + d*x))/(b*c - a*d))^(1/4)*\text{Hypergeometric2F1}[-5/4, 1/4, -1/4, (d*(a + b*x))/(-b*c + a*d)])/(5*b*(a + b*x)^(5/4)*(c + d*x)^(1/4))$

fricas [F] time = 0.55, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{3}{4}}}{b^3dx^4+a^3c+(b^3c+3ab^2d)x^3+3(ab^2c+a^2bd)x^2+(3a^2bc+a^3d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/4)/(d*x+c)^(1/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/4)*(d*x + c)^(3/4)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{9}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/4)/(d*x+c)^(1/4), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(9/4)*(d*x + c)^(1/4)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{9}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(9/4)/(d*x+c)^(1/4), x)

[Out] int(1/(b*x+a)^(9/4)/(d*x+c)^(1/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{9}{4}}(dx+c)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/4)/(d*x+c)^(1/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(9/4)*(d*x + c)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{9/4}(c+dx)^{1/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(9/4)*(c + d*x)^(1/4)),x)

[Out] int(1/((a + b*x)^(9/4)*(c + d*x)^(1/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{9}{4}}\sqrt[4]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(9/4)/(d*x+c)**(1/4),x)

[Out] Integral(1/((a + b*x)**(9/4)*(c + d*x)**(1/4)), x)

$$3.1705 \quad \int \frac{(a+bx)^{7/4}}{(c+dx)^{3/4}} dx$$

Optimal. Leaf size=167

$$-\frac{21(bc-ad)^2 \tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16\sqrt[4]{b}d^{11/4}} + \frac{21(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16\sqrt[4]{b}d^{11/4}} - \frac{7(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)}{8d^2} + \frac{(a+bx)^{7/4}\sqrt[4]{c+dx}}{2d}$$

[Out] $-7/8*(-a*d+b*c)*(b*x+a)^{(3/4)}*(d*x+c)^{(1/4)}/d^2+1/2*(b*x+a)^{(7/4)}*(d*x+c)^{(1/4)}/d-21/16*(-a*d+b*c)^2*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(1/4)}/d^{(11/4)}+21/16*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(1/4)}/d^{(11/4)}$

Rubi [A] time = 0.11, antiderivative size = 167, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {50, 63, 331, 298, 205, 208}

$$\frac{7(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)}{8d^2} - \frac{21(bc-ad)^2 \tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16\sqrt[4]{b}d^{11/4}} + \frac{21(bc-ad)^2 \tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{16\sqrt[4]{b}d^{11/4}} + \frac{(a+bx)^{7/4}\sqrt[4]{c+dx}}{2d}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(7/4)}/(c + d*x)^{(3/4)}, x]$

[Out] $(-7*(b*c - a*d)*(a + b*x)^{(3/4)}*(c + d*x)^{(1/4)})/(8*d^2) + ((a + b*x)^{(7/4)}*(c + d*x)^{(1/4)})/(2*d) - (21*(b*c - a*d)^2*\text{ArcTan}[d^{(1/4)}*(a + b*x)^{(1/4)}/(b^{(1/4)}*(c + d*x)^{(1/4)})]/(16*b^{(1/4)}*d^{(11/4)}) + (21*(b*c - a*d)^2*\text{ArcTanh}[d^{(1/4)}*(a + b*x)^{(1/4)}/(b^{(1/4)}*(c + d*x)^{(1/4)})]/(16*b^{(1/4)}*d^{(11/4)})$

Rule 50

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x] \rightarrow \text{Simp}[(a + b*x)^{m+1}*(c + d*x)^n/(b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m+n+1)), \text{Int}[(a + b*x)^m*(c + d*x)^{n-1}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x] \rightarrow \text{With}[p = \text{Denominator}[m], \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{p*(m+1)-1}*(c - (a*d)/b +$

$(d*x^p)/b)^n, x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 205

$\text{Int}[(a_ + (b_.)*(x_)^2)^{-1}, x_Symbol] \ :> \ \text{Simp}[(\text{Rt}[a/b, 2]*\text{ArcTan}[x/\text{Rt}[a/b, 2]])/a, x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{PosQ}[a/b]$

Rule 208

$\text{Int}[(a_ + (b_.)*(x_)^2)^{-1}, x_Symbol] \ :> \ \text{Simp}[(\text{Rt}[-(a/b), 2]*\text{ArcTanh}[x/\text{Rt}[-(a/b), 2]])/a, x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{NegQ}[a/b]$

Rule 298

$\text{Int}[(x_)^2/((a_ + (b_.)*(x_)^4), x_Symbol] \ :> \ \text{With}[\{r = \text{Numerator}[\text{Rt}[-(a/b), 2]], s = \text{Denominator}[\text{Rt}[-(a/b), 2]]\}, \text{Dist}[s/(2*b), \text{Int}[1/(r + s*x^2), x], x] - \text{Dist}[s/(2*b), \text{Int}[1/(r - s*x^2), x], x]] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{!GtQ}[a/b, 0]$

Rule 331

$\text{Int}[(x_)^{(m_)}*((a_ + (b_.)*(x_)^{(n_)})^{(p_)}, x_Symbol] \ :> \ \text{Dist}[a^{(p + (m + 1)/n)}, \text{Subst}[\text{Int}[x^m/(1 - b*x^n)^{(p + (m + 1)/n + 1)}, x], x, x/(a + b*x^n)^{(1/n)}], x] /; \text{FreeQ}[\{a, b\}, x] \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{LtQ}[-1, p, 0] \ \&\& \ \text{NeQ}[p, -2^{(-1)}] \ \&\& \ \text{IntegersQ}[m, p + (m + 1)/n]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/4}}{(c+dx)^{3/4}} dx &= \frac{(a+bx)^{7/4} \sqrt[4]{c+dx}}{2d} - \frac{(7(bc-ad)) \int \frac{(a+bx)^{3/4}}{(c+dx)^{3/4}} dx}{8d} \\
&= -\frac{7(bc-ad)(a+bx)^{3/4} \sqrt[4]{c+dx}}{8d^2} + \frac{(a+bx)^{7/4} \sqrt[4]{c+dx}}{2d} + \frac{(21(bc-ad)^2) \int \frac{1}{\sqrt[4]{a+bx} (c+dx)^{3/4}} dx}{32d^2} \\
&= -\frac{7(bc-ad)(a+bx)^{3/4} \sqrt[4]{c+dx}}{8d^2} + \frac{(a+bx)^{7/4} \sqrt[4]{c+dx}}{2d} + \frac{(21(bc-ad)^2) \text{Subst} \left(\int \frac{x^2}{\left(c-\frac{ad}{b} + \frac{dx^4}{b}\right)^3} dx, x \right)}{8bd^2} \\
&= -\frac{7(bc-ad)(a+bx)^{3/4} \sqrt[4]{c+dx}}{8d^2} + \frac{(a+bx)^{7/4} \sqrt[4]{c+dx}}{2d} + \frac{(21(bc-ad)^2) \text{Subst} \left(\int \frac{x^2}{1-\frac{dx^4}{b}} dx, x \right)}{8bd^2} \\
&= -\frac{7(bc-ad)(a+bx)^{3/4} \sqrt[4]{c+dx}}{8d^2} + \frac{(a+bx)^{7/4} \sqrt[4]{c+dx}}{2d} + \frac{(21(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{b}-\sqrt{d}x^2} dx, x \right)}{16d^{5/2}} \\
&= -\frac{7(bc-ad)(a+bx)^{3/4} \sqrt[4]{c+dx}}{8d^2} + \frac{(a+bx)^{7/4} \sqrt[4]{c+dx}}{2d} - \frac{21(bc-ad)^2 \tan^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{16\sqrt[4]{b} d^{11/4}} + \dots
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.44

$$\frac{4(a+bx)^{11/4} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4} {}_2F_1 \left(\frac{3}{4}, \frac{11}{4}; \frac{15}{4}; \frac{d(a+bx)}{ad-bc} \right)}{11b(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/4)/(c + d*x)^(3/4), x]

[Out] (4*(a + b*x)^(11/4)*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[3/4, 11/4, 15/4, (d*(a + b*x))/(-b*c) + a*d])/(11*b*(c + d*x)^(3/4))

fricas [B] time = 0.58, size = 1457, normalized size = 8.72

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/4)/(d*x+c)^(3/4), x, algorithm="fricas")

```
[Out] -1/32*(84*d^2*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b*d^11))^(1/4)*arctan(-((b^3*c^2*d^8 - 2*a*b^2*c*d^9 + a^2*b*d^10)*(b*x + a)^(3/4)*(d*x + c)^(1/4))*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b*d^11))^(3/4) - (b^2*d^8*x + a*b*d^8)*sqrt(((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*sqrt(b*x + a)*sqrt(d*x + c) + (b*d^6*x + a*d^6)*sqrt((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b*d^11))))/(b*x + a))*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b*d^11))^(3/4))/(a*b^8*c^8 - 8*a^2*b^7*c^7*d + 28*a^3*b^6*c^6*d^2 - 56*a^4*b^5*c^5*d^3 + 70*a^5*b^4*c^4*d^4 - 56*a^6*b^3*c^3*d^5 + 28*a^7*b^2*c^2*d^6 - 8*a^8*b*c*d^7 + a^9*d^8 + (b^9*c^8 - 8*a*b^8*c^7*d + 28*a^2*b^7*c^6*d^2 - 56*a^3*b^6*c^5*d^3 + 70*a^4*b^5*c^4*d^4 - 56*a^5*b^4*c^3*d^5 + 28*a^6*b^3*c^2*d^6 - 8*a^7*b^2*c*d^7 + a^8*b*d^8)*x)) - 21*d^2*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b*d^11))^(1/4)*log(21*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^(3/4)*(d*x + c)^(1/4) + (b*d^3*x + a*d^3))*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b*d^11))^(1/4))/(b*x + a)) + 21*d^2*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b*d^11))^(1/4)*log(21*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^(3/4)*(d*x + c)^(1/4) - (b*d^3*x + a*d^3))*((b^8*c^8 - 8*a*b^7*c^7*d + 28*a^2*b^6*c^6*d^2 - 56*a^3*b^5*c^5*d^3 + 70*a^4*b^4*c^4*d^4 - 56*a^5*b^3*c^3*d^5 + 28*a^6*b^2*c^2*d^6 - 8*a^7*b*c*d^7 + a^8*d^8)/(b*d^11))^(1/4))/(b*x + a)) - 4*(4*b*d*x - 7*b*c + 11*a*d)*(b*x + a)^(3/4)*(d*x + c)^(1/4))/d^2
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(7/4)/(d*x+c)^(3/4),x, algorithm="giac")
```

```
[Out] integrate((b*x + a)^(7/4)/(d*x + c)^(3/4), x)
```


maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/4)/(d*x+c)^(3/4), x)

[Out] int((b*x+a)^(7/4)/(d*x+c)^(3/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/4)/(d*x+c)^(3/4), x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/4)/(d*x + c)^(3/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{7}{4}}}{(c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/4)/(c + d*x)^(3/4), x)

[Out] int((a + b*x)^(7/4)/(c + d*x)^(3/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{7}{4}}}{(c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/4)/(d*x+c)**(3/4), x)

[Out] Integral((a + b*x)**(7/4)/(c + d*x)**(3/4), x)

$$3.1706 \quad \int \frac{(a+bx)^{3/4}}{(c+dx)^{3/4}} dx$$

Optimal. Leaf size=127

$$\frac{3(bc-ad)\tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2\sqrt[4]{b}d^{7/4}} - \frac{3(bc-ad)\tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2\sqrt[4]{b}d^{7/4}} + \frac{(a+bx)^{3/4}\sqrt[4]{c+dx}}{d}$$

[Out] $(b*x+a)^{(3/4)}*(d*x+c)^{(1/4)}/d+3/2*(-a*d+b*c)*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(1/4)}/d^{(7/4)}-3/2*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(1/4)}/d^{(7/4)}$

Rubi [A] time = 0.08, antiderivative size = 127, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {50, 63, 331, 298, 205, 208}

$$\frac{3(bc-ad)\tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2\sqrt[4]{b}d^{7/4}} - \frac{3(bc-ad)\tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2\sqrt[4]{b}d^{7/4}} + \frac{(a+bx)^{3/4}\sqrt[4]{c+dx}}{d}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/4)/(c + d*x)^(3/4), x]

[Out] $((a + b*x)^{(3/4)}*(c + d*x)^{(1/4)})/d + (3*(b*c - a*d)*\operatorname{ArcTan}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(2*b^{(1/4)}*d^{(7/4)}) - (3*(b*c - a*d)*\operatorname{ArcTanh}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(2*b^{(1/4)}*d^{(7/4)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 205

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[a/b, 2]*ArcTan[x/Rt[a/b, 2]])/a, x] /; FreeQ[{a, b}, x] && PosQ[a/b]

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rule 298

Int[(x_)^2/((a_) + (b_.)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[-(a/b), 2]], s = Denominator[Rt[-(a/b), 2]]}, Dist[s/(2*b), Int[1/(r + s*x^2), x], x] - Dist[s/(2*b), Int[1/(r - s*x^2), x], x]] /; FreeQ[{a, b}, x] && !GtQ[a/b, 0]

Rule 331

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/4}}{(c+dx)^{3/4}} dx &= \frac{(a+bx)^{3/4} \sqrt[4]{c+dx}}{d} - \frac{(3(bc-ad)) \int \frac{1}{\sqrt[4]{a+bx} (c+dx)^{3/4}} dx}{4d} \\
&= \frac{(a+bx)^{3/4} \sqrt[4]{c+dx}}{d} - \frac{(3(bc-ad)) \operatorname{Subst} \left(\int \frac{x^2}{\left(c - \frac{ad}{b} + \frac{dx^4}{b}\right)^{3/4}} dx, x, \sqrt[4]{a+bx} \right)}{bd} \\
&= \frac{(a+bx)^{3/4} \sqrt[4]{c+dx}}{d} - \frac{(3(bc-ad)) \operatorname{Subst} \left(\int \frac{x^2}{1 - \frac{dx^4}{b}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{bd} \\
&= \frac{(a+bx)^{3/4} \sqrt[4]{c+dx}}{d} - \frac{(3(bc-ad)) \operatorname{Subst} \left(\int \frac{1}{\sqrt{b-\sqrt{d}} x^2} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{2d^{3/2}} + \frac{(3(bc-ad)) \operatorname{Subst} \left(\int \frac{1}{\sqrt{b-\sqrt{d}} x^2} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{2d^{3/2}} \\
&= \frac{(a+bx)^{3/4} \sqrt[4]{c+dx}}{d} + \frac{3(bc-ad) \tan^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{2\sqrt[4]{b} d^{7/4}} - \frac{3(bc-ad) \tanh^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{2\sqrt[4]{b} d^{7/4}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.57

$$\frac{4(a+bx)^{7/4} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4} {}_2F_1 \left(\frac{3}{4}, \frac{7}{4}; \frac{11}{4}; \frac{d(a+bx)}{ad-bc} \right)}{7b(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/4)/(c + d*x)^(3/4), x]

[Out] (4*(a + b*x)^(7/4)*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[3/4, 7/4, 11/4, (d*(a + b*x))/(-b*c) + a*d])/(7*b*(c + d*x)^(3/4))

fricas [B] time = 0.53, size = 808, normalized size = 6.36

$$12d \left(\frac{b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4}{bd^7} \right)^{\frac{1}{4}} \arctan \left(\frac{(b^2cd^5 - abd^6)(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{1}{4}} \left(\frac{b^4c^4 - 4ab^3c^3d + 6a^2b^2c^2d^2 - 4a^3bcd^3 + a^4d^4}{bd^7} \right)^{\frac{3}{4}} + (b^2d^5x + a^3b^2)}{ab^4c^4 - 4a^2b^3c^3d + 6a^3b^2c^2d^2 - 4a^4b^2cd^3 + a^5d^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)/(d*x+c)^(3/4),x, algorithm="fricas")

[Out]
$$-1/4*(12*d*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b*d^7))^(1/4)*\arctan(((b^2*c*d^5 - a*b*d^6)*(b*x + a)^(3/4)*(d*x + c)^(1/4))*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b*d^7))^(3/4) + (b^2*d^5*x + a*b*d^5)*\sqrt{((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*\sqrt{b*x + a}*\sqrt{d*x + c} + (b*d^4*x + a*d^4)*\sqrt{(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b*d^7))})/(b*x + a))*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b*d^7))^(3/4))/(a*b^4*c^4 - 4*a^2*b^3*c^3*d + 6*a^3*b^2*c^2*d^2 - 4*a^4*b*c*d^3 + a^5*d^4 + (b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)*x) + 3*d*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b*d^7))^(1/4)*\log(-3*((b*c - a*d)*(b*x + a)^(3/4)*(d*x + c)^(1/4) + (b*d^2*x + a*d^2))*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b*d^7))^(1/4))/(b*x + a)) - 3*d*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b*d^7))^(1/4)*\log(-3*((b*c - a*d)*(b*x + a)^(3/4)*(d*x + c)^(1/4) - (b*d^2*x + a*d^2))*((b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)/(b*d^7))^(1/4))/(b*x + a)) - 4*(b*x + a)^(3/4)*(d*x + c)^(1/4))/d$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)/(d*x+c)^(3/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/4)/(d*x + c)^(3/4), x)

maple [F] time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/4)/(d*x+c)^(3/4),x)

[Out] int((b*x+a)^(3/4)/(d*x+c)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/4)/(d*x + c)^(3/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{3/4}}{(c + dx)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/4)/(c + d*x)^(3/4),x)

[Out] int((a + b*x)^(3/4)/(c + d*x)^(3/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{4}}}{(c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/4)/(d*x+c)**(3/4),x)

[Out] Integral((a + b*x)**(3/4)/(c + d*x)**(3/4), x)

$$3.1707 \quad \int \frac{1}{\sqrt[4]{a+bx} (c+dx)^{3/4}} dx$$

Optimal. Leaf size=85

$$\frac{2 \tanh^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{\sqrt[4]{b} d^{3/4}} - \frac{2 \tan^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{\sqrt[4]{b} d^{3/4}}$$

[Out] $-2*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(1/4)}/d^{(3/4)}+2*\arctanh(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/b^{(1/4)}/d^{(3/4)}$

Rubi [A] time = 0.07, antiderivative size = 85, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {63, 331, 298, 205, 208}

$$\frac{2 \tanh^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{\sqrt[4]{b} d^{3/4}} - \frac{2 \tan^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{\sqrt[4]{b} d^{3/4}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)^{(1/4)}*(c + d*x)^{(3/4))}, x]$

[Out] $(-2*\text{ArcTan}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(b^{(1/4)}*d^{(3/4)}) + (2*\text{ArcTanh}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(b^{(1/4)}*d^{(3/4)})$

Rule 63

$\text{Int}(((a_.) + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol) \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}\{a, b, c, d, x\} \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 205

$\text{Int}(((a_.) + (b_.)*(x_.)^2)^{-1}, x_Symbol) \rightarrow \text{Simp}[(\text{Rt}[a/b, 2]*\text{ArcTan}[x/\text{Rt}[a/b, 2]])/a, x] /; \text{FreeQ}\{a, b, x\} \&\& \text{PosQ}[a/b]$

Rule 208

$\text{Int}(((a_.) + (b_.)*(x_.)^2)^{-1}, x_Symbol) \rightarrow \text{Simp}[(\text{Rt}[-(a/b), 2]*\text{ArcTanh}[x/\text{Rt}[-(a/b), 2]])/a, x] /; \text{FreeQ}\{a, b, x\} \&\& \text{NegQ}[a/b]$

Rule 298

```
Int[(x_)^2/((a_) + (b_)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[-(a/b), 2]], s = Denominator[Rt[-(a/b), 2]]}, Dist[s/(2*b), Int[1/(r + s*x^2), x], x] - Dist[s/(2*b), Int[1/(r - s*x^2), x], x]] /; FreeQ[{a, b}, x] && !GtQ[a/b, 0]
```

Rule 331

```
Int[(x_)^(m_)*((a_) + (b_)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]
```

Rubi steps

$$\int \frac{1}{\sqrt[4]{a+bx}(c+dx)^{3/4}} dx = \frac{4 \operatorname{Subst}\left(\int \frac{x^2}{\left(c-\frac{ad}{b}+\frac{dx^4}{b}\right)^{3/4}} dx, x, \sqrt[4]{a+bx}\right)}{b}$$

$$= \frac{4 \operatorname{Subst}\left(\int \frac{x^2}{1-\frac{dx^4}{b}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}}\right)}{b}$$

$$= \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{b}-\sqrt{d}x^2} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}}\right)}{\sqrt{d}} - \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt{b}+\sqrt{d}x^2} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}}\right)}{\sqrt{d}}$$

$$= -\frac{2 \tan^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{\sqrt[4]{b} d^{3/4}} + \frac{2 \tanh^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{\sqrt[4]{b} d^{3/4}}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.86

$$\frac{4(a+bx)^{3/4} \left(\frac{b(c+dx)}{bc-ad}\right)^{3/4} {}_2F_1\left(\frac{3}{4}, \frac{3}{4}; \frac{7}{4}; \frac{d(a+bx)}{ad-bc}\right)}{3b(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/4)*(c + d*x)^(3/4)), x]

[Out] $(4*(a + b*x)^{(3/4)*((b*(c + d*x))/(b*c - a*d))^{(3/4)*Hypergeometric2F1[3/4, 3/4, 7/4, (d*(a + b*x))/(-(b*c) + a*d)]})/(3*b*(c + d*x)^{(3/4)})$

fricas [B] time = 0.46, size = 234, normalized size = 2.75

$$-4 \left(\frac{1}{bd^3} \right)^{\frac{1}{4}} \arctan \left(\frac{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{1}{4}}bd^2 \left(\frac{1}{bd^3} \right)^{\frac{3}{4}} - (b^2d^2x + abd^2) \sqrt{\frac{(bd^2x+ad^2) \sqrt{\frac{1}{bd^3} + \sqrt{bx+a} \sqrt{dx+c}}}{bx+a}} \left(\frac{1}{bd^3} \right)^{\frac{3}{4}}}{bx+a} \right) + \left(\frac{1}{bd} \right)^{\frac{1}{4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(1/4)/(d*x+c)^(3/4),x, algorithm="fricas")`

[Out] $-4*(1/(b*d^3))^{(1/4)*\arctan(-((b*x + a)^{(3/4)*(d*x + c)^{(1/4)*b*d^2*(1/(b*d^3))^{(3/4)} - (b^2*d^2*x + a*b*d^2)*\sqrt{((b*d^2*x + a*d^2)*\sqrt{1/(b*d^3)) + \sqrt{b*x + a}*\sqrt{d*x + c}})/(b*x + a))*(1/(b*d^3))^{(3/4)})/(b*x + a)) + (1/(b*d^3))^{(1/4)*\log(((b*d*x + a*d)*(1/(b*d^3))^{(1/4)} + (b*x + a)^{(3/4)*(d*x + c)^{(1/4)})/(b*x + a)) - (1/(b*d^3))^{(1/4)*\log(-((b*d*x + a*d)*(1/(b*d^3))^{(1/4)} - (b*x + a)^{(3/4)*(d*x + c)^{(1/4)})/(b*x + a))}$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(1/4)/(d*x+c)^(3/4),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(1/4)*(d*x + c)^(3/4)), x)`

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(1/4)/(d*x+c)^(3/4),x)`

[Out] `int(1/(b*x+a)^(1/4)/(d*x+c)^(3/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/4)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/4)*(d*x + c)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{1/4} (c + dx)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/4)*(c + d*x)^(3/4)),x)

[Out] int(1/((a + b*x)^(1/4)*(c + d*x)^(3/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[4]{a + bx} (c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/4)/(d*x+c)**(3/4),x)

[Out] Integral(1/((a + b*x)**(1/4)*(c + d*x)**(3/4)), x)

$$3.1708 \quad \int \frac{1}{(a+bx)^{5/4}(c+dx)^{3/4}} dx$$

Optimal. Leaf size=30

$$-\frac{4\sqrt[4]{c+dx}}{\sqrt[4]{a+bx}(bc-ad)}$$

[Out] $-4*(d*x+c)^{(1/4)} / (-a*d+b*c) / (b*x+a)^{(1/4)}$

Rubi [A] time = 0.00, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{4\sqrt[4]{c+dx}}{\sqrt[4]{a+bx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/4)*(c + d*x)^(3/4)), x]

[Out] $(-4*(c + d*x)^{(1/4)}) / ((b*c - a*d)*(a + b*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{(a+bx)^{5/4}(c+dx)^{3/4}} dx = -\frac{4\sqrt[4]{c+dx}}{(bc-ad)\sqrt[4]{a+bx}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$\frac{4\sqrt[4]{c+dx}}{\sqrt[4]{a+bx}(ad-bc)}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/4)*(c + d*x)^(3/4)), x]

[Out] $(4*(c + d*x)^{(1/4)})/((-b*c) + a*d)*(a + b*x)^{(1/4)}$

fricas [A] time = 0.50, size = 42, normalized size = 1.40

$$\frac{4 (bx + a)^{\frac{3}{4}} (dx + c)^{\frac{1}{4}}}{abc - a^2d + (b^2c - abd)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/4)/(d*x+c)^(3/4),x, algorithm="fricas")`

[Out] $-4*(b*x + a)^{(3/4)}*(d*x + c)^{(1/4)}/(a*b*c - a^2*d + (b^2*c - a*b*d)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{4}}(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/4)/(d*x+c)^(3/4),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(5/4)*(d*x + c)^(3/4)), x)`

maple [A] time = 0.00, size = 27, normalized size = 0.90

$$\frac{4 (dx + c)^{\frac{1}{4}}}{(bx + a)^{\frac{1}{4}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(5/4)/(d*x+c)^(3/4),x)`

[Out] $4/(b*x+a)^{(1/4)}*(d*x+c)^{(1/4)}/(a*d-b*c)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{4}}(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/4)/(d*x+c)^(3/4),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(5/4)*(d*x + c)^(3/4)), x)`

mupad [B] time = 0.71, size = 26, normalized size = 0.87

$$\frac{4(c + dx)^{1/4}}{(ad - bc)(a + bx)^{1/4}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(5/4)*(c + d*x)^(3/4)), x)`

[Out] `(4*(c + d*x)^(1/4))/((a*d - b*c)*(a + b*x)^(1/4))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{5}{4}} (c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/4)/(d*x+c)**(3/4), x)`

[Out] `Integral(1/((a + b*x)**(5/4)*(c + d*x)**(3/4)), x)`

$$3.1709 \quad \int \frac{1}{(a+bx)^{9/4}(c+dx)^{3/4}} dx$$

Optimal. Leaf size=66

$$\frac{16d\sqrt[4]{c+dx}}{5\sqrt[4]{a+bx}(bc-ad)^2} - \frac{4\sqrt[4]{c+dx}}{5(a+bx)^{5/4}(bc-ad)}$$

[Out] $-4/5*(d*x+c)^{(1/4)/(-a*d+b*c)/(b*x+a)^{(5/4)+16/5*d*(d*x+c)^{(1/4)/(-a*d+b*c)^{2/(b*x+a)^{(1/4)}}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{16d\sqrt[4]{c+dx}}{5\sqrt[4]{a+bx}(bc-ad)^2} - \frac{4\sqrt[4]{c+dx}}{5(a+bx)^{5/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(9/4)*(c + d*x)^(3/4)),x]

[Out] $(-4*(c + d*x)^{(1/4))/(5*(b*c - a*d)*(a + b*x)^{(5/4)} + (16*d*(c + d*x)^{(1/4)})/(5*(b*c - a*d)^2*(a + b*x)^{(1/4))}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{9/4}(c+dx)^{3/4}} dx = -\frac{4\sqrt[4]{c+dx}}{5(bc-ad)(a+bx)^{5/4}} - \frac{(4d) \int \frac{1}{(a+bx)^{5/4}(c+dx)^{3/4}} dx}{5(bc-ad)}$$

$$= -\frac{4\sqrt[4]{c+dx}}{5(bc-ad)(a+bx)^{5/4}} + \frac{16d\sqrt[4]{c+dx}}{5(bc-ad)^2\sqrt[4]{a+bx}}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.70

$$\frac{4\sqrt[4]{c+dx}(5ad-bc+4bdx)}{5(a+bx)^{5/4}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(9/4)*(c + d*x)^(3/4)), x]

[Out] (4*(c + d*x)^(1/4)*(-(b*c) + 5*a*d + 4*b*d*x))/(5*(b*c - a*d)^2*(a + b*x)^(5/4))

fricas [B] time = 0.86, size = 118, normalized size = 1.79

$$\frac{4(4bdx - bc + 5ad)(bx + a)^{\frac{3}{4}}(dx + c)^{\frac{1}{4}}}{5(a^2b^2c^2 - 2a^3bcd + a^4d^2 + (b^4c^2 - 2ab^3cd + a^2b^2d^2)x^2 + 2(ab^3c^2 - 2a^2b^2cd + a^3bd^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/4)/(d*x+c)^(3/4), x, algorithm="fricas")

[Out] 4/5*(4*b*d*x - b*c + 5*a*d)*(b*x + a)^(3/4)*(d*x + c)^(1/4)/(a^2*b^2*c^2 - 2*a^3*b*c*d + a^4*d^2 + (b^4*c^2 - 2*a*b^3*c*d + a^2*b^2*d^2)*x^2 + 2*(a*b^3*c^2 - 2*a^2*b^2*c*d + a^3*b*d^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{9}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/4)/(d*x+c)^(3/4), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(9/4)*(d*x + c)^(3/4)), x)

maple [A] time = 0.00, size = 54, normalized size = 0.82

$$\frac{4(dx+c)^{\frac{1}{4}}(4bdx+5ad-bc)}{5(bx+a)^{\frac{5}{4}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(9/4)/(d*x+c)^(3/4),x)`

[Out] `4/5*(d*x+c)^(1/4)*(4*b*d*x+5*a*d-b*c)/(b*x+a)^(5/4)/(a^2*d^2-2*a*b*c*d+b^2*c^2)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{9}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(9/4)/(d*x+c)^(3/4),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(9/4)*(d*x + c)^(3/4)), x)`

mupad [B] time = 0.87, size = 71, normalized size = 1.08

$$\frac{\left(\frac{16dx}{5(ad-bc)^2} + \frac{20ad-4bc}{5b(ad-bc)^2}\right)(c+dx)^{1/4}}{x(a+bx)^{1/4} + \frac{a(a+bx)^{1/4}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(9/4)*(c + d*x)^(3/4)),x)`

[Out] `((((16*d*x)/(5*(a*d - b*c)^2) + (20*a*d - 4*b*c)/(5*b*(a*d - b*c)^2))*(c + d*x)^(1/4))/(x*(a + b*x)^(1/4) + (a*(a + b*x)^(1/4))/b)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{9}{4}}(c+dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(9/4)/(d*x+c)**(3/4),x)`

[Out] `Integral(1/((a + b*x)**(9/4)*(c + d*x)**(3/4)), x)`

$$3.1710 \quad \int \frac{1}{(a+bx)^{13/4}(c+dx)^{3/4}} dx$$

Optimal. Leaf size=101

$$-\frac{128d^2\sqrt[4]{c+dx}}{45\sqrt[4]{a+bx}(bc-ad)^3} + \frac{32d\sqrt[4]{c+dx}}{45(a+bx)^{5/4}(bc-ad)^2} - \frac{4\sqrt[4]{c+dx}}{9(a+bx)^{9/4}(bc-ad)}$$

[Out] $-4/9*(d*x+c)^{(1/4)/(-a*d+b*c)/(b*x+a)^{(9/4)+32/45*d*(d*x+c)^{(1/4)/(-a*d+b*c)^2/(b*x+a)^{(5/4)-128/45*d^2*(d*x+c)^{(1/4)/(-a*d+b*c)^3/(b*x+a)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{128d^2\sqrt[4]{c+dx}}{45\sqrt[4]{a+bx}(bc-ad)^3} + \frac{32d\sqrt[4]{c+dx}}{45(a+bx)^{5/4}(bc-ad)^2} - \frac{4\sqrt[4]{c+dx}}{9(a+bx)^{9/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(13/4)*(c + d*x)^(3/4)), x]

[Out] $(-4*(c + d*x)^{(1/4))/(9*(b*c - a*d)*(a + b*x)^{(9/4)} + (32*d*(c + d*x)^{(1/4)})/(45*(b*c - a*d)^2*(a + b*x)^{(5/4)} - (128*d^2*(c + d*x)^{(1/4)})/(45*(b*c - a*d)^3*(a + b*x)^{(1/4))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{13/4}(c+dx)^{3/4}} dx &= -\frac{4\sqrt[4]{c+dx}}{9(bc-ad)(a+bx)^{9/4}} - \frac{(8d) \int \frac{1}{(a+bx)^{9/4}(c+dx)^{3/4}} dx}{9(bc-ad)} \\
&= -\frac{4\sqrt[4]{c+dx}}{9(bc-ad)(a+bx)^{9/4}} + \frac{32d\sqrt[4]{c+dx}}{45(bc-ad)^2(a+bx)^{5/4}} + \frac{(32d^2) \int \frac{1}{(a+bx)^{5/4}(c+dx)^{3/4}} dx}{45(bc-ad)^2} \\
&= -\frac{4\sqrt[4]{c+dx}}{9(bc-ad)(a+bx)^{9/4}} + \frac{32d\sqrt[4]{c+dx}}{45(bc-ad)^2(a+bx)^{5/4}} - \frac{128d^2\sqrt[4]{c+dx}}{45(bc-ad)^3\sqrt[4]{a+bx}}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 75, normalized size = 0.74

$$-\frac{4\sqrt[4]{c+dx} (45a^2d^2 - 18abd(c-4dx) + b^2(5c^2 - 8cdx + 32d^2x^2))}{45(a+bx)^{9/4}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(13/4)*(c + d*x)^(3/4)), x]

[Out] (-4*(c + d*x)^(1/4)*(45*a^2*d^2 - 18*a*b*d*(c - 4*d*x) + b^2*(5*c^2 - 8*c*d*x + 32*d^2*x^2)))/(45*(b*c - a*d)^3*(a + b*x)^(9/4))

fricas [B] time = 0.69, size = 251, normalized size = 2.49

$$\frac{4(32b^2d^2x^2 + 5b^2c^2 - 18abcd + 45a^2d^2 - 8(b^2cd - 9abd^2)x)}{45(a^3b^3c^3 - 3a^4b^2c^2d + 3a^5bcd^2 - a^6d^3 + (b^6c^3 - 3ab^5c^2d + 3a^2b^4cd^2 - a^3b^3d^3)x^3 + 3(ab^5c^3 - 3a^2b^4c^2d + 3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(13/4)/(d*x+c)^(3/4), x, algorithm="fricas")

[Out] -4/45*(32*b^2*d^2*x^2 + 5*b^2*c^2 - 18*a*b*c*d + 45*a^2*d^2 - 8*(b^2*c*d - 9*a*b*d^2)*x)*(b*x + a)^(3/4)*(d*x + c)^(1/4)/(a^3*b^3*c^3 - 3*a^4*b^2*c^2*d + 3*a^5*b*c*d^2 - a^6*d^3 + (b^6*c^3 - 3*a*b^5*c^2*d + 3*a^2*b^4*c*d^2 - a^3*b^3*d^3)*x^3 + 3*(a*b^5*c^3 - 3*a^2*b^4*c^2*d + 3*a^3*b^3*c*d^2 - a^4*b^2*d^3)*x^2 + 3*(a^2*b^4*c^3 - 3*a^3*b^3*c^2*d + 3*a^4*b^2*c*d^2 - a^5*b*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{13}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(13/4)/(d*x+c)^(3/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(13/4)*(d*x + c)^(3/4)), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{4(dx+c)^{\frac{1}{4}}(32b^2x^2d^2+72abd^2x-8b^2cdx+45a^2d^2-18abcd+5b^2c^2)}{45(bx+a)^{\frac{9}{4}}(a^3d^3-3a^2bcd^2+3ab^2c^2d-b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(13/4)/(d*x+c)^(3/4),x)

[Out] 4/45*(d*x+c)^(1/4)*(32*b^2*d^2*x^2+72*a*b*d^2*x-8*b^2*c*d*x+45*a^2*d^2-18*a*b*c*d+5*b^2*c^2)/(b*x+a)^(9/4)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{13}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(13/4)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(13/4)*(d*x + c)^(3/4)), x)

mupad [B] time = 1.02, size = 133, normalized size = 1.32

$$\frac{(c+dx)^{1/4} \left(\frac{128d^2x^2}{45(ad-bc)^3} + \frac{180a^2d^2-72abcd+20b^2c^2}{45b^2(ad-bc)^3} + \frac{32dx(9ad-bc)}{45b(ad-bc)^3} \right)}{x^2(a+bx)^{1/4} + \frac{a^2(a+bx)^{1/4}}{b^2} + \frac{2ax(a+bx)^{1/4}}{b}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a+b*x)^(13/4)*(c+d*x)^(3/4)),x)

[Out] ((c+d*x)^(1/4)*((128*d^2*x^2)/(45*(a*d-b*c)^3)+(180*a^2*d^2+20*b^2*c^2-72*a*b*c*d)/(45*b^2*(a*d-b*c)^3)+(32*d*x*(9*a*d-b*c))/(45*b*(a*d-b*c)^3))/(x^2*(a+b*x)^(1/4)+(a^2*(a+b*x)^(1/4))/b^2+(2*a*x*(a+b*x)^(1/4))/b)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(13/4)/(d*x+c)**(3/4),x)

[Out] Timed out

$$3.1711 \quad \int \frac{1}{(a+bx)^{17/4}(c+dx)^{3/4}} dx$$

Optimal. Leaf size=136

$$\frac{512d^3\sqrt[4]{c+dx}}{195\sqrt[4]{a+bx}(bc-ad)^4} - \frac{128d^2\sqrt[4]{c+dx}}{195(a+bx)^{5/4}(bc-ad)^3} + \frac{16d\sqrt[4]{c+dx}}{39(a+bx)^{9/4}(bc-ad)^2} - \frac{4\sqrt[4]{c+dx}}{13(a+bx)^{13/4}(bc-ad)}$$

[Out] $-4/13*(d*x+c)^{(1/4)/(-a*d+b*c)/(b*x+a)^{(13/4)+16/39*d*(d*x+c)^{(1/4)/(-a*d+b*c)^2/(b*x+a)^{(9/4)-128/195*d^2*(d*x+c)^{(1/4)/(-a*d+b*c)^3/(b*x+a)^{(5/4)+512/195*d^3*(d*x+c)^{(1/4)/(-a*d+b*c)^4/(b*x+a)^{(1/4)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{512d^3\sqrt[4]{c+dx}}{195\sqrt[4]{a+bx}(bc-ad)^4} - \frac{128d^2\sqrt[4]{c+dx}}{195(a+bx)^{5/4}(bc-ad)^3} + \frac{16d\sqrt[4]{c+dx}}{39(a+bx)^{9/4}(bc-ad)^2} - \frac{4\sqrt[4]{c+dx}}{13(a+bx)^{13/4}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(17/4)*(c + d*x)^(3/4)), x]

[Out] $(-4*(c + d*x)^{(1/4))/(13*(b*c - a*d)*(a + b*x)^{(13/4)} + (16*d*(c + d*x)^{(1/4))/(39*(b*c - a*d)^2*(a + b*x)^{(9/4)} - (128*d^2*(c + d*x)^{(1/4))/(195*(b*c - a*d)^3*(a + b*x)^{(5/4)} + (512*d^3*(c + d*x)^{(1/4))/(195*(b*c - a*d)^4*(a + b*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[n] && !IntegerQ[m] && !IntegerQ[m + n + 2] && !IntegerQ[m + n + 1] && !IntegerQ[m + n]

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{17/4}(c+dx)^{3/4}} dx &= -\frac{4\sqrt[4]{c+dx}}{13(bc-ad)(a+bx)^{13/4}} - \frac{(12d) \int \frac{1}{(a+bx)^{13/4}(c+dx)^{3/4}} dx}{13(bc-ad)} \\
&= -\frac{4\sqrt[4]{c+dx}}{13(bc-ad)(a+bx)^{13/4}} + \frac{16d\sqrt[4]{c+dx}}{39(bc-ad)^2(a+bx)^{9/4}} + \frac{(32d^2) \int \frac{1}{(a+bx)^{9/4}(c+dx)^{3/4}} dx}{39(bc-ad)^2} \\
&= -\frac{4\sqrt[4]{c+dx}}{13(bc-ad)(a+bx)^{13/4}} + \frac{16d\sqrt[4]{c+dx}}{39(bc-ad)^2(a+bx)^{9/4}} - \frac{128d^2\sqrt[4]{c+dx}}{195(bc-ad)^3(a+bx)^{5/4}} - \frac{(128d^3) \int \frac{1}{(a+bx)^{5/4}(c+dx)^{3/4}} dx}{195(bc-ad)^3} \\
&= -\frac{4\sqrt[4]{c+dx}}{13(bc-ad)(a+bx)^{13/4}} + \frac{16d\sqrt[4]{c+dx}}{39(bc-ad)^2(a+bx)^{9/4}} - \frac{128d^2\sqrt[4]{c+dx}}{195(bc-ad)^3(a+bx)^{5/4}} + \frac{128d^3}{195(bc-ad)^3} \int \frac{1}{(a+bx)^{5/4}(c+dx)^{3/4}} dx
\end{aligned}$$

Mathematica [A] time = 0.05, size = 116, normalized size = 0.85

$$\frac{4\sqrt[4]{c+dx} (195a^3d^3 - 117a^2bd^2(c-4dx) + 13ab^2d(5c^2 - 8cdx + 32d^2x^2) + b^3(-15c^3 + 20c^2dx - 32cd^2x^2 + 128d^3x^3))}{195(a+bx)^{13/4}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(17/4)*(c + d*x)^(3/4)), x]

[Out] (4*(c + d*x)^(1/4)*(195*a^3*d^3 - 117*a^2*b*d^2*(c - 4*d*x) + 13*a*b^2*d*(5*c^2 - 8*c*d*x + 32*d^2*x^2) + b^3*(-15*c^3 + 20*c^2*d*x - 32*c*d^2*x^2 + 128*d^3*x^3)))/(195*(b*c - a*d)^4*(a + b*x)^(13/4))

fricas [B] time = 0.77, size = 419, normalized size = 3.08

$$\frac{4(128b^3d^3x^3 - 15b^3c^3 + 65ab^2c^2d - 117a^2b^3cd^2 + 195a^3d^3 - 32(b^3cd^2 - 13a^2b^2d^3)x^2 + 4(5b^3c^2d - 26a^2b^2cd^2 + 117a^2b^3d^3)x)(b*x + a)^{3/4}(d*x + c)^{1/4}}{195(a^4b^4c^4 - 4a^5b^3c^3d + 6a^6b^2c^2d^2 - 4a^7bcd^3 + a^8d^4 + (b^8c^4 - 4ab^7c^3d + 6a^2b^6c^2d^2 - 4a^3b^5cd^3 + a^4b^4d^4)x^4 + \dots)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(17/4)/(d*x+c)^(3/4), x, algorithm="fricas")

[Out] 4/195*(128*b^3*d^3*x^3 - 15*b^3*c^3 + 65*a*b^2*c^2*d - 117*a^2*b*c*d^2 + 195*a^3*d^3 - 32*(b^3*c*d^2 - 13*a*b^2*d^3)*x^2 + 4*(5*b^3*c^2*d - 26*a*b^2*c*d^2 + 117*a^2*b*d^3)*x)*(b*x + a)^(3/4)*(d*x + c)^(1/4)/(a^4*b^4*c^4 - 4*a^5*b^3*c^3*d + 6*a^6*b^2*c^2*d^2 - 4*a^7*b*c*d^3 + a^8*d^4 + (b^8*c^4 - 4*a*b^7*c^3*d + 6*a^2*b^6*c^2*d^2 - 4*a^3*b^5*c*d^3 + a^4*b^4*d^4)*x^4 + 4*(a*b^7*c^4 - 4*a^2*b^6*c^3*d + 6*a^3*b^5*c^2*d^2 - 4*a^4*b^4*c*d^3 + a^5*b^3*d^4 - 4*a^6*b^2*c^2*d^2 + 4*a^7*b*c*d^3 - a^8*d^4))

$$\begin{aligned} &^4)*x^3 + 6*(a^2*b^6*c^4 - 4*a^3*b^5*c^3*d + 6*a^4*b^4*c^2*d^2 - 4*a^5*b^3*c*d^3 + a^6*b^2*d^4)*x^2 + 4*(a^3*b^5*c^4 - 4*a^4*b^4*c^3*d + 6*a^5*b^3*c^2*d^2 - 4*a^6*b^2*c*d^3 + a^7*b*d^4)*x \end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{17}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(17/4)/(d*x+c)^(3/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(17/4)*(d*x + c)^(3/4)), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{4(dx+c)^{\frac{1}{4}}(128b^3d^3x^3 + 416ab^2d^3x^2 - 32b^3cd^2x^2 + 468a^2bd^3x - 104ab^2cd^2x + 20b^3c^2dx + 195a^3d^3 - 117a^2b^2d^2 - 4a^3b^2c^2d^2 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}{195(bx+a)^{\frac{13}{4}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(17/4)/(d*x+c)^(3/4),x)

[Out] $4/195*(d*x+c)^{(1/4)}*(128*b^3*d^3*x^3+416*a*b^2*d^3*x^2-32*b^3*c*d^2*x^2+468*a^2*b*d^3*x-104*a*b^2*c*d^2*x+20*b^3*c^2*d*x+195*a^3*d^3-117*a^2*b*c*d^2+6*5*a*b^2*c^2*d-15*b^3*c^3)/(b*x+a)^{(13/4)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{17}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(17/4)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(17/4)*(d*x + c)^(3/4)), x)

mupad [B] time = 1.26, size = 209, normalized size = 1.54

$$\frac{(c+dx)^{1/4} \left(\frac{512d^3x^3}{195(ad-bc)^4} + \frac{780a^3d^3-468a^2bcd^2+260ab^2c^2d-60b^3c^3}{195b^3(ad-bc)^4} + \frac{16dx(117a^2d^2-26abcd+5b^2c^2)}{195b^2(ad-bc)^4} + \frac{128d^2x^2(13ad-bc)}{195b(ad-bc)^4} \right)}{x^3(a+bx)^{1/4} + \frac{a^3(a+bx)^{1/4}}{b^3} + \frac{3ax^2(a+bx)^{1/4}}{b} + \frac{3a^2x(a+bx)^{1/4}}{b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a + b*x)^(17/4)*(c + d*x)^(3/4)),x)
```

```
[Out] ((c + d*x)^(1/4)*((512*d^3*x^3)/(195*(a*d - b*c)^4) + (780*a^3*d^3 - 60*b^3*c^3 + 260*a*b^2*c^2*d - 468*a^2*b*c*d^2)/(195*b^3*(a*d - b*c)^4) + (16*d*x*(117*a^2*d^2 + 5*b^2*c^2 - 26*a*b*c*d))/(195*b^2*(a*d - b*c)^4) + (128*d^2*x^2*(13*a*d - b*c))/(195*b*(a*d - b*c)^4)))/(x^3*(a + b*x)^(1/4) + (a^3*(a + b*x)^(1/4))/b^3 + (3*a*x^2*(a + b*x)^(1/4))/b + (3*a^2*x*(a + b*x)^(1/4))/b^2)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(17/4)/(d*x+c)**(3/4),x)
```

```
[Out] Timed out
```


$$3.1712 \quad \int \frac{(a+bx)^{5/4}}{(c+dx)^{3/4}} dx$$

Optimal. Leaf size=332

$$\frac{5(bc-ad)^{5/2}((a+bx)(c+dx))^{3/4}\sqrt{(ad+bc+2bdx)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)}}{\sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)^2}}}} \text{EllipticF}\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1, \frac{1}{2}\right)$$

$$6\sqrt{2}\sqrt[4]{b}d^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))}$$

[Out] $-5/3*(-a*d+b*c)*(b*x+a)^{(1/4)}*(d*x+c)^{(1/4)}/d^2+2/3*(b*x+a)^{(5/4)}*(d*x+c)^{(1/4)}/d+5/12*(-a*d+b*c)^{(5/2)}*((b*x+a)*(d*x+c))^{(3/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})), 1/2*2^{(1/2)})*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^{(1/2)}*((2*b*d*x+a*d+b*c)^{(1/2)}*((a*d+b*(2*d*x+c))^{(1/2)}/(-a*d+b*c)^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^{(1/2)})/b^{(1/4)}/d^{(9/4)})/(b*x+a)^{(3/4)}/(d*x+c)^{(3/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^{(1/2)})^{(1/2)}$

Rubi [A] time = 0.29, antiderivative size = 332, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 220}

$$\frac{5(bc-ad)^{5/2}((a+bx)(c+dx))^{3/4}\sqrt{(ad+bc+2bdx)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)}}{3d^2} + \frac{6\sqrt{2}\sqrt[4]{b}d^{9/4}(a+bx)^{3/4}(c+dx)^{3/4}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))}}{\sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)^2}}}} \text{EllipticF}\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1, \frac{1}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/4)/(c + d*x)^(3/4), x]

[Out] $(-5*(b*c - a*d)*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)})/(3*d^2) + (2*(a + b*x)^{(5/4)}*(c + d*x)^{(1/4)})/(3*d) + (5*(b*c - a*d)^{(5/2)}*((a + b*x)*(c + d*x))^{(3/4)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))*\text{Sqrt}[(a*d + b*(c + 2*d*x))^{(1/2)}/((b*c - a*d)^{(1/2)}*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)])/(b*c - a*d))^{(1/2)})]*\text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)})/\text{Sqrt}[b*c - a*d]], 1/2)]/(6*\text{Sqrt}[2]*b^{(1/4)}*d^{(9/4)}*(a + b*x)^{(3/4)}*(c + d*x)^{(3/4)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^{(1/2)}])$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[(
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x]
, 1/2])/(2*q*Sqrt[a + b*x^4]), x]] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/4}}{(c+dx)^{3/4}} dx &= \frac{2(a+bx)^{5/4} \sqrt[4]{c+dx}}{3d} - \frac{(5(bc-ad)) \int \frac{\sqrt[4]{a+bx}}{(c+dx)^{3/4}} dx}{6d} \\
&= -\frac{5(bc-ad) \sqrt[4]{a+bx} \sqrt[4]{c+dx}}{3d^2} + \frac{2(a+bx)^{5/4} \sqrt[4]{c+dx}}{3d} + \frac{(5(bc-ad)^2) \int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx}{12d^2} \\
&= -\frac{5(bc-ad) \sqrt[4]{a+bx} \sqrt[4]{c+dx}}{3d^2} + \frac{2(a+bx)^{5/4} \sqrt[4]{c+dx}}{3d} + \frac{(5(bc-ad)^2((a+bx)(c+dx))^{3/4}) \int}{12d^2(a+bx)^{3/4}(c+dx)^{3/4}} \\
&= -\frac{5(bc-ad) \sqrt[4]{a+bx} \sqrt[4]{c+dx}}{3d^2} + \frac{2(a+bx)^{5/4} \sqrt[4]{c+dx}}{3d} + \frac{(5(bc-ad)^2((a+bx)(c+dx))^{3/4} \sqrt{(a+bx)(c+dx)})}{12d^2(a+bx)^{3/4}(c+dx)^{3/4}} \\
&= -\frac{5(bc-ad) \sqrt[4]{a+bx} \sqrt[4]{c+dx}}{3d^2} + \frac{2(a+bx)^{5/4} \sqrt[4]{c+dx}}{3d} + \frac{5(bc-ad)^{5/2}((a+bx)(c+dx))^{3/4} \sqrt{(a+bx)(c+dx)}}{12d^2(a+bx)^{3/4}(c+dx)^{3/4}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.22

$$\frac{4(a+bx)^{9/4} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4} {}_2F_1 \left(\frac{3}{4}, \frac{9}{4}; \frac{13}{4}; \frac{d(a+bx)}{ad-bc} \right)}{9b(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/4)/(c + d*x)^(3/4), x]

[Out] (4*(a + b*x)^(9/4)*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[3/4, 9/4, 13/4, (d*(a + b*x))/(-(b*c) + a*d)]/(9*b*(c + d*x)^(3/4))

fricas [F] time = 0.68, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{5}{4}}}{(dx+c)^{\frac{3}{4}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)/(d*x+c)^(3/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/4)/(d*x + c)^(3/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)/(d*x+c)^(3/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/4)/(d*x + c)^(3/4), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/4)/(d*x+c)^(3/4),x)

[Out] int((b*x+a)^(5/4)/(d*x+c)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/4)/(d*x + c)^(3/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{\frac{5}{4}}}{(c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/4)/(c + d*x)^(3/4),x)

[Out] int((a + b*x)^(5/4)/(c + d*x)^(3/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{4}}}{(c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/4)/(d*x+c)**(3/4), x)

[Out] Integral((a + b*x)**(5/4)/(c + d*x)**(3/4), x)

$$3.1713 \quad \int \frac{\sqrt[4]{a+bx}}{(c+dx)^{3/4}} dx$$

Optimal. Leaf size=295

$$\frac{2\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{d} \frac{(bc-ad)^{3/2}((a+bx)(c+dx))^{3/4}\sqrt{(ad+bc+2bdx)^2}\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)}{\sqrt{2}\sqrt[4]{b}d^{5/4}(a+bx)^{3/4}(c+dx)^{3/4}(ad+bc+2bdx)\sqrt{(bc-ad)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)}}$$

[Out] $2*(b*x+a)^{(1/4)}*(d*x+c)^{(1/4)}/d-1/2*(-a*d+b*c)^{(3/2)}*((b*x+a)*(d*x+c))^{(3/4)}$
 $)*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2))))^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2))})$
 $*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))$
 $*(2*b*d*x+a*d+b*c)^{(1/2)}*((a*d+b*(2*d*x+c))^{(1/2)}/(-a*d+b*c)^{(1/2)}/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))$
 $^{(1/2)}/b^{(1/4)}/d^{(5/4)}/(b*x+a)^{(3/4)}/(d*x+c)^{(3/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^{(1/2)})^{(1/2)}$

Rubi [A] time = 0.22, antiderivative size = 295, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {50, 62, 623, 220}

$$\frac{2\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{d} \frac{(bc-ad)^{3/2}((a+bx)(c+dx))^{3/4}\sqrt{(ad+bc+2bdx)^2}\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)}{\sqrt{2}\sqrt[4]{b}d^{5/4}(a+bx)^{3/4}(c+dx)^{3/4}(ad+bc+2bdx)\sqrt{(bc-ad)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/4)/(c + d*x)^(3/4), x]

[Out] $(2*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)})/d - ((b*c - a*d)^{(3/2)}*((a + b*x)*(c + d*x))^{(3/4)}*\text{Sqrt}[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)]))/(b*c - a*d))$
 $*\text{Sqrt}[(a*d + b*(c + 2*d*x))^{(1/2)}/((b*c - a*d)^{(1/2)}*(1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)]))/(b*c - a*d)^{(1/2)})$
 $*\text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)})/\text{Sqrt}[b*c - a*d]], 1/2)]/(\text{Sqrt}[2]*b^{(1/4)}*d^{(5/4)}*(a + b*x)^{(3/4)}*(c + d*x)^{(3/4)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^{(1/2)})]$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
 $((a + b*x)^{(m+1)}*(c + d*x)^n)/(b*(m+n+1)), x] + \text{Dist}[(n*(b*c - a*d))/$

$(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 62

$\text{Int}[(a_.) + (b_.)*(x_.))^{(m_)}*((c_.) + (d_.)*(x_.))^{(n_)}, x_Symbol] := \text{Dist}[(a + b*x)^m*(c + d*x)^n/((a + b*x)*(c + d*x))^m, \text{Int}[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[3, Denominator[m], 4]

Rule 220

$\text{Int}[1/\text{Sqrt}[(a_.) + (b_.)*(x_.)^4], x_Symbol] := \text{With}[\{q = \text{Rt}[b/a, 4]\}, \text{Simp}[(1 + q^2*x^2)*\text{Sqrt}[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*\text{EllipticF}[2*\text{ArcTan}[q*x], 1/2)]/(2*q*\text{Sqrt}[a + b*x^4]), x] /;$ FreeQ[{a, b}, x] && PosQ[b/a]

Rule 623

$\text{Int}[(a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2]^{(p_)}, x_Symbol] := \text{With}[\{d = \text{Denominator}[p]\}, \text{Dist}[(d*\text{Sqrt}[(b + 2*c*x)^2])/(b + 2*c*x), \text{Subst}[\text{Int}[x^{(d*(p + 1) - 1)}/\text{Sqrt}[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^{(1/d)}], x] /;$ 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rubi steps

$$\begin{aligned} \int \frac{\sqrt[4]{a+bx}}{(c+dx)^{3/4}} dx &= \frac{2\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{d} - \frac{(bc-ad) \int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx}{2d} \\ &= \frac{2\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{d} - \frac{((bc-ad)((a+bx)(c+dx))^{3/4}) \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{3/4}} dx}{2d(a+bx)^{3/4}(c+dx)^{3/4}} \\ &= \frac{2\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{d} - \frac{(2(bc-ad)((a+bx)(c+dx))^{3/4}\sqrt{(bc+ad+2bdx)^2}) \text{Subst}\left(\int \frac{1}{\sqrt{-4abcd}}\right)}{d(a+bx)^{3/4}(c+dx)^{3/4}(bc+ad+2bdx)} \\ &= \frac{2\sqrt[4]{a+bx}\sqrt[4]{c+dx}}{d} - \frac{(bc-ad)^{3/2}((a+bx)(c+dx))^{3/4}\sqrt{(bc+ad+2bdx)^2} \left(1 + \frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)}}{bc-ad}\right)}{\sqrt{2}\sqrt[4]{b}d^{5/4}(a+bx)^{3/4}(c+dx)^{3/4}} \end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.25

$$\frac{4(a + bx)^{5/4} \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4} {}_2F_1 \left(\frac{3}{4}, \frac{5}{4}; \frac{9}{4}; \frac{d(a+bx)}{ad-bc} \right)}{5b(c + dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/4)/(c + d*x)^(3/4), x]

[Out] (4*(a + b*x)^(5/4)*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[3/4, 5/4, 9/4, (d*(a + b*x))/(-b*c) + a*d])/(5*b*(c + d*x)^(3/4))

fricas [F] time = 0.62, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^{\frac{1}{4}}}{(dx + c)^{\frac{3}{4}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)/(d*x+c)^(3/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/4)/(d*x + c)^(3/4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)/(d*x+c)^(3/4), x, algorithm="giac")

[Out] integrate((b*x + a)^(1/4)/(d*x + c)^(3/4), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/4)/(d*x+c)^(3/4), x)

[Out] int((b*x+a)^(1/4)/(d*x+c)^(3/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{4}}}{(dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/4)/(d*x + c)^(3/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{1/4}}{(c + dx)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/4)/(c + d*x)^(3/4),x)

[Out] int((a + b*x)^(1/4)/(c + d*x)^(3/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[4]{a + bx}}{(c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/4)/(d*x+c)**(3/4),x)

[Out] Integral((a + b*x)**(1/4)/(c + d*x)**(3/4), x)

$$3.1714 \quad \int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx$$

Optimal. Leaf size=270

$$\frac{\sqrt{2} \sqrt{bc-ad} ((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)}{\sqrt{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} \text{EllipticF} \left(\frac{\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}, \frac{1}{2} \right) \sqrt{(ad+b(c+2dx))^2}$$

[Out] $((b*x+a)*(d*x+c))^{3/4} * (\cos(2*\arctan(b^{1/4}*d^{1/4})*((b*x+a)*(d*x+c))^{1/4}) * 2^{1/2} / (-a*d+b*c)^{1/2})^{1/2} / \cos(2*\arctan(b^{1/4}*d^{1/4})*((b*x+a)*(d*x+c))^{1/4}) * 2^{1/2} / (-a*d+b*c)^{1/2}) * \text{EllipticF}(\sin(2*\arctan(b^{1/4}*d^{1/4})*((b*x+a)*(d*x+c))^{1/4}) * 2^{1/2} / (-a*d+b*c)^{1/2}), 1/2 * 2^{1/2}) * 2^{1/2} * (-a*d+b*c)^{1/2} * (1+2*b^{1/2}*d^{1/2}) * ((b*x+a)*(d*x+c))^{1/2} / (-a*d+b*c) * ((2*b*d*x+a*d+b*c)^2)^{1/2} * ((a*d+b*(2*d*x+c))^2 / (-a*d+b*c)^2 / (1+2*b^{1/2}*d^{1/2}) * d^{1/2} * ((b*x+a)*(d*x+c))^{1/2} / (-a*d+b*c))^{1/2} / b^{1/4} / d^{1/4} / (b*x+a)^{3/4} / (d*x+c)^{3/4} / (2*b*d*x+a*d+b*c) / ((a*d+b*(2*d*x+c))^2)^{1/2}$

Rubi [A] time = 0.18, antiderivative size = 270, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {62, 623, 220}

$$\frac{\sqrt{2} \sqrt{bc-ad} ((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)}{\sqrt{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} F \left(\frac{\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}, \frac{1}{2} \right) \sqrt{(ad+b(c+2dx))^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/4)*(c + d*x)^(3/4)), x]

[Out] $(\text{Sqrt}[2] * \text{Sqrt}[b*c - a*d] * ((a + b*x)*(c + d*x))^{3/4} * \text{Sqrt}[(b*c + a*d + 2*b*d*x)^2] * (1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)]) / (b*c - a*d)) * \text{Sqrt}[(a*d + b*(c + 2*d*x))^2 / ((b*c - a*d)^2 * (1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)]) / (b*c - a*d))^2]) * \text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{1/4}*d^{1/4}) * ((a + b*x)*(c + d*x))^{1/4}) / \text{Sqrt}[b*c - a*d]], 1/2]) / (b^{1/4}*d^{1/4} * (a + b*x)^{3/4} * (c + d*x)^{3/4} * (b*c + a*d + 2*b*d*x) * \text{Sqrt}[(a*d + b*(c + 2*d*x))^2])$

Rule 62

Int[((a_.) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] :> Dist[(a + b*x)^m*(c + d*x)^m]/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[

-1, m, 0] && LeQ[3, Denominator[m], 4]

Rule 220

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x], 1/2]]/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]

Rule 623

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx &= \frac{((a+bx)(c+dx))^{3/4} \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{3/4}} dx}{(a+bx)^{3/4}(c+dx)^{3/4}} \\ &= \frac{(4((a+bx)(c+dx))^{3/4} \sqrt{(bc+ad+2bdx)^2}) \operatorname{Subst}\left(\int \frac{1}{\sqrt{-4abcd+(bc+ad)^2+4bdx^4}} dx, x, \right)}{(a+bx)^{3/4}(c+dx)^{3/4}(bc+ad+2bdx)} \\ &= \frac{\sqrt{2} \sqrt{bc-ad} ((a+bx)(c+dx))^{3/4} \sqrt{(bc+ad+2bdx)^2} \left(1 + \frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad}\right)}{\sqrt[4]{b} \sqrt[4]{d} (a+bx)^{3/4}(c+dx)^{3/4}(bc+ad+2bdx)} \end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.26

$$\frac{4\sqrt[4]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{3/4} {}_2F_1\left(\frac{1}{4}, \frac{3}{4}; \frac{5}{4}; \frac{d(a+bx)}{ad-bc}\right)}{b(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/4)*(c + d*x)^(3/4)), x]

[Out] (4*(a + b*x)^(1/4)*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[1/4, 3/4, 5/4, (d*(a + b*x))/(-b*c) + a*d])/(b*(c + d*x)^(3/4))

fricas [F] time = 0.63, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{1}{4}}}{bdx^2+ac+(bc+ad)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/4)/(d*x+c)^(3/4),x, algorithm="fricas")

[Out] integral((b*x + a)^(1/4)*(d*x + c)^(1/4)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/4)/(d*x+c)^(3/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/4)*(d*x + c)^(3/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/4)/(d*x+c)^(3/4),x)

[Out] int(1/(b*x+a)^(3/4)/(d*x+c)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/4)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/4)*(d*x + c)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{3/4} (c + dx)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/4)*(c + d*x)^(3/4)), x)

[Out] int(1/((a + b*x)^(3/4)*(c + d*x)^(3/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{4}} (c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/4)/(d*x+c)**(3/4), x)

[Out] Integral(1/((a + b*x)**(3/4)*(c + d*x)**(3/4)), x)

$$3.1715 \quad \int \frac{1}{(a+bx)^{7/4}(c+dx)^{3/4}} dx$$

Optimal. Leaf size=306

$$2\sqrt{2} d^{3/4} ((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} \text{EllipticF} \\ \frac{3\sqrt[4]{b}(a+bx)^{3/4}(c+dx)^{3/4}\sqrt{bc-ad}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^2}}$$

[Out] $-4/3*(d*x+c)^{(1/4)} / (-a*d+b*c) / (b*x+a)^{(3/4)} - 2/3*d^{(3/4)} * ((b*x+a)*(d*x+c))^{(3/4)} * (\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)} / (-a*d+b*c)^{(1/2)}))^{(1/2)} / \cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)} / (-a*d+b*c)^{(1/2)})) * \text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)} / (-a*d+b*c)^{(1/2)})), 1/2*2^{(1/2)})*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)} / (-a*d+b*c)) * ((2*b*d*x+a*d+b*c)^2)^{(1/2)} * ((a*d+b*(2*d*x+c))^2 / (-a*d+b*c)^2 / (1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)} / (-a*d+b*c))^{(1/2)} / b^{(1/4)} / (b*x+a)^{(3/4)} / (d*x+c)^{(3/4)} / (2*b*d*x+a*d+b*c) / (-a*d+b*c)^{(1/2)} / ((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.22, antiderivative size = 306, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {51, 62, 623, 220}

$$2\sqrt{2} d^{3/4} ((a+bx)(c+dx))^{3/4} \sqrt{(ad+bc+2bdx)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)} \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} F \left(2 \arctan \left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \right) \\ \frac{3\sqrt[4]{b}(a+bx)^{3/4}(c+dx)^{3/4}\sqrt{bc-ad}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^2}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/4)*(c + d*x)^(3/4)), x]

[Out] $(-4*(c + d*x)^{(1/4)}) / (3*(b*c - a*d)*(a + b*x)^{(3/4)}) - (2*\text{Sqrt}[2]*d^{(3/4)} * ((a + b*x)*(c + d*x))^{(3/4)} * \text{Sqrt}[(b*c + a*d + 2*b*d*x)^2] * (1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)]) / (b*c - a*d)) * \text{Sqrt}[(a*d + b*(c + 2*d*x))^2 / ((b*c - a*d)^2 * (1 + (2*\text{Sqrt}[b]*\text{Sqrt}[d]*\text{Sqrt}[(a + b*x)*(c + d*x)]) / (b*c - a*d))^2]) * \text{EllipticF}[2*\text{ArcTan}[(\text{Sqrt}[2]*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)}) / \text{Sqrt}[b*c - a*d]], 1/2]) / (3*b^{(1/4)}*\text{Sqrt}[b*c - a*d]*(a + b*x)^{(3/4)}*(c + d*x)^{(3/4)}*(b*c + a*d + 2*b*d*x)*\text{Sqrt}[(a*d + b*(c + 2*d*x))^2])$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1)) / ((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2)) / ((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x

] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 62

Int[((a_.) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(m_), x_Symbol] := Dist[(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[3, Denominator[m], 4]

Rule 220

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x], 1/2]]/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]

Rule 623

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a + bx)^{7/4}(c + dx)^{3/4}} dx &= -\frac{4\sqrt[4]{c + dx}}{3(bc - ad)(a + bx)^{3/4}} - \frac{(2d) \int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx}{3(bc - ad)} \\
 &= -\frac{4\sqrt[4]{c + dx}}{3(bc - ad)(a + bx)^{3/4}} - \frac{(2d((a + bx)(c + dx))^{3/4}) \int \frac{1}{(ac+(bc+ad)x+bdx^2)^{3/4}} dx}{3(bc - ad)(a + bx)^{3/4}(c + dx)^{3/4}} \\
 &= -\frac{4\sqrt[4]{c + dx}}{3(bc - ad)(a + bx)^{3/4}} - \frac{(8d((a + bx)(c + dx))^{3/4}\sqrt{(bc + ad + 2bdx)^2}) \text{Subst}\left(\int \frac{1}{\sqrt{bc + ad + 2bdx}} dx\right)}{3(bc - ad)(a + bx)^{3/4}(c + dx)^{3/4}} \\
 &= -\frac{4\sqrt[4]{c + dx}}{3(bc - ad)(a + bx)^{3/4}} - \frac{2\sqrt{2} d^{3/4}((a + bx)(c + dx))^{3/4}\sqrt{(bc + ad + 2bdx)^2} \left(1 + \frac{2}{\sqrt{bc + ad + 2bdx}}\right)}{3\sqrt[4]{b} \sqrt{bc - ad} (a + bx)^{3/4}(c + dx)^{3/4}}
 \end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.24

$$-\frac{4\left(\frac{b(c+dx)}{bc-ad}\right)^{3/4} {}_2F_1\left(-\frac{3}{4}, \frac{3}{4}; \frac{1}{4}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a+bx)^{3/4}(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/4)*(c + d*x)^(3/4)), x]

[Out] (-4*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[-3/4, 3/4, 1/4, (d*(a + b*x))/(-b*c + a*d)]/(3*b*(a + b*x)^(3/4)*(c + d*x)^(3/4))

fricas [F] time = 0.63, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{1}{4}}}{b^2dx^3+a^2c+(b^2c+2abd)x^2+(2abc+a^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/4)/(d*x+c)^(3/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/4)*(d*x + c)^(1/4)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/4)/(d*x+c)^(3/4), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/4)*(d*x + c)^(3/4)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/4)/(d*x+c)^(3/4), x)

[Out] int(1/(b*x+a)^(7/4)/(d*x+c)^(3/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{4}}(dx+c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/4)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(7/4)*(d*x + c)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{\frac{7}{4}}(c+dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/4)*(c + d*x)^(3/4)), x)

[Out] int(1/((a + b*x)^(7/4)*(c + d*x)^(3/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{7}{4}}(c+dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/4)/(d*x+c)**(3/4), x)

[Out] Integral(1/((a + b*x)**(7/4)*(c + d*x)**(3/4)), x)


```

m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]

```

Rule 62

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]

```

Rule 220

```

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x]
, 1/2]]/(2*q*Sqrt[a + b*x^4]), x]] /; FreeQ[{a, b}, x] && PosQ[b/a]

```

Rule 623

```

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{11/4}(c+dx)^{3/4}} dx &= -\frac{4\sqrt[4]{c+dx}}{7(bc-ad)(a+bx)^{7/4}} - \frac{(6d) \int \frac{1}{(a+bx)^{7/4}(c+dx)^{3/4}} dx}{7(bc-ad)} \\
&= -\frac{4\sqrt[4]{c+dx}}{7(bc-ad)(a+bx)^{7/4}} + \frac{8d\sqrt[4]{c+dx}}{7(bc-ad)^2(a+bx)^{3/4}} + \frac{(4d^2) \int \frac{1}{(a+bx)^{3/4}(c+dx)^{3/4}} dx}{7(bc-ad)^2} \\
&= -\frac{4\sqrt[4]{c+dx}}{7(bc-ad)(a+bx)^{7/4}} + \frac{8d\sqrt[4]{c+dx}}{7(bc-ad)^2(a+bx)^{3/4}} + \frac{(4d^2((a+bx)(c+dx))^{3/4}) \int \frac{1}{(ac+bx^2+dx^2)} dx}{7(bc-ad)^2(a+bx)^{3/4}} \\
&= -\frac{4\sqrt[4]{c+dx}}{7(bc-ad)(a+bx)^{7/4}} + \frac{8d\sqrt[4]{c+dx}}{7(bc-ad)^2(a+bx)^{3/4}} + \frac{(16d^2((a+bx)(c+dx))^{3/4} \sqrt{(bc+bx^2+dx^2)}) \int \frac{1}{(ac+bx^2+dx^2)} dx}{7(bc-ad)^2(a+bx)^{3/4}} \\
&= -\frac{4\sqrt[4]{c+dx}}{7(bc-ad)(a+bx)^{7/4}} + \frac{8d\sqrt[4]{c+dx}}{7(bc-ad)^2(a+bx)^{3/4}} + \frac{4\sqrt{2} d^{7/4} ((a+bx)(c+dx))^{3/4} \sqrt{(bc+bx^2+dx^2)} \int \frac{1}{(ac+bx^2+dx^2)} dx}{7(bc-ad)^2(a+bx)^{3/4}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.22

$$-\frac{4 \left(\frac{b(c+dx)}{bc-ad} \right)^{3/4} {}_2F_1 \left(-\frac{7}{4}, \frac{3}{4}; -\frac{3}{4}; \frac{d(a+bx)}{ad-bc} \right)}{7b(a+bx)^{7/4}(c+dx)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(11/4)*(c + d*x)^(3/4)), x]

[Out] (-4*((b*(c + d*x))/(b*c - a*d))^(3/4)*Hypergeometric2F1[-7/4, 3/4, -3/4, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*(a + b*x)^(7/4)*(c + d*x)^(3/4))

fricas [F] time = 0.86, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{1}{4}}}{b^3 dx^4 + a^3 c + (b^3 c + 3 ab^2 d)x^3 + 3(ab^2 c + a^2 bd)x^2 + (3 a^2 bc + a^3 d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/4)/(d*x+c)^(3/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/4)*(d*x + c)^(1/4)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{11}{4}} (dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/4)/(d*x+c)^(3/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(11/4)*(d*x + c)^(3/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{11}{4}} (dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(11/4)/(d*x+c)^(3/4),x)

[Out] int(1/(b*x+a)^(11/4)/(d*x+c)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{11}{4}} (dx + c)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/4)/(d*x+c)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(11/4)*(d*x + c)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{\frac{11}{4}} (c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(11/4)*(c + d*x)^(3/4)),x)

[Out] int(1/((a + b*x)^(11/4)*(c + d*x)^(3/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{11}{4}} (c + dx)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(11/4)/(d*x+c)**(3/4),x)
```

```
[Out] Integral(1/((a + b*x)**(11/4)*(c + d*x)**(3/4)), x)
```

$$3.1717 \quad \int \frac{(a+bx)^{5/4}}{(c+dx)^{5/4}} dx$$

Optimal. Leaf size=152

$$\frac{5\sqrt[4]{b}(bc-ad)\tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2d^{9/4}} - \frac{5\sqrt[4]{b}(bc-ad)\tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2d^{9/4}} + \frac{5b\sqrt[4]{a+bx}(c+dx)^{3/4}}{d^2} - \frac{4(a+bx)^{5/4}}{d\sqrt[4]{c+dx}}$$

[Out] $-4*(b*x+a)^{(5/4)}/d/(d*x+c)^{(1/4)}+5*b*(b*x+a)^{(1/4)}*(d*x+c)^{(3/4)}/d^2-5/2*b^{(1/4)}*(-a*d+b*c)*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/d^{(9/4)}$
 $-5/2*b^{(1/4)}*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/d^{(9/4)}$

Rubi [A] time = 0.09, antiderivative size = 152, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 7, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.368$, Rules used = {47, 50, 63, 240, 212, 208, 205}

$$\frac{5b\sqrt[4]{a+bx}(c+dx)^{3/4}}{d^2} - \frac{5\sqrt[4]{b}(bc-ad)\tan^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2d^{9/4}} - \frac{5\sqrt[4]{b}(bc-ad)\tanh^{-1}\left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}}\right)}{2d^{9/4}} - \frac{4(a+bx)^{5/4}}{d\sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(5/4)}/(c + d*x)^{(5/4)}, x]$

[Out] $(-4*(a + b*x)^{(5/4)})/(d*(c + d*x)^{(1/4)}) + (5*b*(a + b*x)^{(1/4)}*(c + d*x)^{(3/4)})/d^2 - (5*b^{(1/4)}*(b*c - a*d)*\text{ArcTan}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(2*d^{(9/4)}) - (5*b^{(1/4)}*(b*c - a*d)*\text{ArcTanh}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/(2*d^{(9/4)})$

Rule 47

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \text{Dist}[(d*n)/(b*(m + 1)), \text{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 50

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b,

$c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{GtQ}[n, 0] \&\& \text{NeQ}[m + n + 1, 0] \&\& \text{!(IGtQ}[m, 0] \&\& (\text{!IntegerQ}[n] \mid\mid (\text{GtQ}[m, 0] \&\& \text{LtQ}[m - n, 0]))) \&\& \text{!ILtQ}[m + n + 2, 0] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\text{Int}[(a_.) + (b_.)*(x_)^{(m_)}*((c_.) + (d_.)*(x_)^{(n_)}, x_Symbol] \text{:> With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] \text{/; FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 205

$\text{Int}[(a_) + (b_.)*(x_)^2)^{-1}, x_Symbol] \text{:> Simp}[(\text{Rt}[a/b, 2]*\text{ArcTan}[x/\text{Rt}[a/b, 2]])/a, x] \text{/; FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a/b]$

Rule 208

$\text{Int}[(a_) + (b_.)*(x_)^2)^{-1}, x_Symbol] \text{:> Simp}[(\text{Rt}[-(a/b), 2]*\text{ArcTanh}[x/\text{Rt}[-(a/b), 2]])/a, x] \text{/; FreeQ}\{a, b\}, x] \&\& \text{NegQ}[a/b]$

Rule 212

$\text{Int}[(a_) + (b_.)*(x_)^4)^{-1}, x_Symbol] \text{:> With}\{r = \text{Numerator}[\text{Rt}[-(a/b), 2]], s = \text{Denominator}[\text{Rt}[-(a/b), 2]]\}, \text{Dist}[r/(2*a), \text{Int}[1/(r - s*x^2), x], x] + \text{Dist}[r/(2*a), \text{Int}[1/(r + s*x^2), x], x]] \text{/; FreeQ}\{a, b\}, x] \&\& \text{!GtQ}[a/b, 0]$

Rule 240

$\text{Int}[(a_) + (b_.)*(x_)^{(n_)}]^{(p_)}, x_Symbol] \text{:> Dist}[a^{(p + 1/n)}, \text{Subst}[\text{Int}[1/(1 - b*x^n)^{(p + 1/n + 1)}, x], x, x/(a + b*x^n)^{(1/n)}], x] \text{/; FreeQ}\{a, b\}, x] \&\& \text{IGtQ}[n, 0] \&\& \text{LtQ}[-1, p, 0] \&\& \text{NeQ}[p, -2^{(-1)}] \&\& \text{IntegerQ}[p + 1/n]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/4}}{(c+dx)^{5/4}} dx &= -\frac{4(a+bx)^{5/4}}{d\sqrt[4]{c+dx}} + \frac{(5b) \int \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} dx}{d} \\
&= -\frac{4(a+bx)^{5/4}}{d\sqrt[4]{c+dx}} + \frac{5b\sqrt[4]{a+bx}(c+dx)^{3/4}}{d^2} - \frac{(5b(bc-ad)) \int \frac{1}{(a+bx)^{3/4}\sqrt[4]{c+dx}} dx}{4d^2} \\
&= -\frac{4(a+bx)^{5/4}}{d\sqrt[4]{c+dx}} + \frac{5b\sqrt[4]{a+bx}(c+dx)^{3/4}}{d^2} - \frac{(5(bc-ad)) \text{Subst} \left(\int \frac{1}{\sqrt[4]{c-\frac{ad}{b}+\frac{dx^4}{b}}} dx, x, \sqrt[4]{a+bx} \right)}{d^2} \\
&= -\frac{4(a+bx)^{5/4}}{d\sqrt[4]{c+dx}} + \frac{5b\sqrt[4]{a+bx}(c+dx)^{3/4}}{d^2} - \frac{(5(bc-ad)) \text{Subst} \left(\int \frac{1}{1-\frac{dx^4}{b}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{d^2} \\
&= -\frac{4(a+bx)^{5/4}}{d\sqrt[4]{c+dx}} + \frac{5b\sqrt[4]{a+bx}(c+dx)^{3/4}}{d^2} - \frac{(5\sqrt{b}(bc-ad)) \text{Subst} \left(\int \frac{1}{\sqrt{b}-\sqrt{d}x^2} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{2d^2} \\
&= -\frac{4(a+bx)^{5/4}}{d\sqrt[4]{c+dx}} + \frac{5b\sqrt[4]{a+bx}(c+dx)^{3/4}}{d^2} - \frac{5\sqrt[4]{b}(bc-ad) \tan^{-1} \left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}} \right)}{2d^{9/4}} - \frac{5\sqrt[4]{b}(bc-ad) \tan^{-1} \left(\frac{\sqrt[4]{d}\sqrt[4]{a+bx}}{\sqrt[4]{b}\sqrt[4]{c+dx}} \right)}{2d^{9/4}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.48

$$\frac{4(a+bx)^{9/4} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(\frac{5}{4}, \frac{9}{4}, \frac{13}{4}, \frac{d(a+bx)}{ad-bc} \right)}{9b(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/4)/(c + d*x)^(5/4), x]

[Out] (4*(a + b*x)^(9/4)*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[5/4, 9/4, 13/4, (d*(a + b*x))/(-(b*c) + a*d)]/(9*b*(c + d*x)^(5/4))

fricas [B] time = 0.84, size = 857, normalized size = 5.64

$$20(d^3x + cd^2) \left(\frac{b^5c^4 - 4ab^4c^3d + 6a^2b^3c^2d^2 - 4a^3b^2cd^3 + a^4bd^4}{d^9} \right)^{\frac{1}{4}} \arctan \left(\frac{(bcd^7 - ad^8)(bx+a)^{\frac{1}{4}}(dx+c)^{\frac{3}{4}} \left(\frac{b^5c^4 - 4ab^4c^3d + 6a^2b^3c^2d^2 - 4a^3b^2cd^3 + a^4bd^4}{d^9} \right)}{b^5c^5 - 4ab^4c^4d + 6a^2b^3c^3d^2 - 4a^3b^2c^2d^3 + a^4bd^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out]
$$-1/4*(20*(d^3*x + c*d^2)*((b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)/d^9)^{(1/4)}*\arctan(((b*c*d^7 - a*d^8)*(b*x + a)^{(1/4)}*(d*x + c)^{(3/4)}*((b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)/d^9)^{(3/4)} + (d^8*x + c*d^7)*\sqrt{((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*\sqrt{b*x + a}*\sqrt{d*x + c} + (d^5*x + c*d^4)*\sqrt{(b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)/d^9}})/(d*x + c))*((b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)/d^9)^{(3/4)})/(b^5*c^5 - 4*a*b^4*c^4*d + 6*a^2*b^3*c^3*d^2 - 4*a^3*b^2*c^2*d^3 + a^4*b*c*d^4 + (b^5*c^4*d - 4*a*b^4*c^3*d^2 + 6*a^2*b^3*c^2*d^3 - 4*a^3*b^2*c*d^4 + a^4*b*d^5)*x)) + 5*(d^3*x + c*d^2)*((b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)/d^9)^{(1/4)}*\log(-5*((b*c - a*d)*(b*x + a)^{(1/4)}*(d*x + c)^{(3/4)} + (d^3*x + c*d^2)*((b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)/d^9)^{(1/4)}))/(d*x + c)) - 5*(d^3*x + c*d^2)*((b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)/d^9)^{(1/4)}*\log(-5*((b*c - a*d)*(b*x + a)^{(1/4)}*(d*x + c)^{(3/4)} - (d^3*x + c*d^2)*((b^5*c^4 - 4*a*b^4*c^3*d + 6*a^2*b^3*c^2*d^2 - 4*a^3*b^2*c*d^3 + a^4*b*d^4)/d^9)^{(1/4)}))/(d*x + c)) - 4*(b*d*x + 5*b*c - 4*a*d)*(b*x + a)^{(1/4)}*(d*x + c)^{(3/4)})/(d^3*x + c*d^2)$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{4}}}{(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/4)/(d*x + c)^(5/4), x)

maple [F] time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/4)/(d*x+c)^(5/4), x)

[Out] int((b*x+a)^(5/4)/(d*x+c)^(5/4), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/4)/(d*x+c)^(5/4), x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/4)/(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{5}{4}}}{(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/4)/(c + d*x)^(5/4), x)

[Out] int((a + b*x)^(5/4)/(c + d*x)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{4}}}{(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/4)/(d*x+c)**(5/4), x)

[Out] Integral((a + b*x)**(5/4)/(c + d*x)**(5/4), x)

$$3.1718 \quad \int \frac{\sqrt[4]{a+bx}}{(c+dx)^{5/4}} dx$$

Optimal. Leaf size=108

$$\frac{2\sqrt[4]{b} \tan^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{d^{5/4}} + \frac{2\sqrt[4]{b} \tanh^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{d^{5/4}} - \frac{4\sqrt[4]{a+bx}}{d\sqrt[4]{c+dx}}$$

[Out] $-4*(b*x+a)^{(1/4)}/d/(d*x+c)^{(1/4)}+2*b^{(1/4)}*\arctan(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/d^{(5/4)}+2*b^{(1/4)}*\operatorname{arctanh}(d^{(1/4)}*(b*x+a)^{(1/4)}/b^{(1/4)}/(d*x+c)^{(1/4)})/d^{(5/4)}$

Rubi [A] time = 0.07, antiderivative size = 108, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {47, 63, 240, 212, 208, 205}

$$\frac{2\sqrt[4]{b} \tan^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{d^{5/4}} + \frac{2\sqrt[4]{b} \tanh^{-1}\left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}}\right)}{d^{5/4}} - \frac{4\sqrt[4]{a+bx}}{d\sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(1/4)}/(c + d*x)^{(5/4)}, x]$

[Out] $(-4*(a + b*x)^{(1/4)}/(d*(c + d*x)^{(1/4)}) + (2*b^{(1/4)}*\text{ArcTan}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/d^{(5/4)} + (2*b^{(1/4)}*\text{ArcTanh}[(d^{(1/4)}*(a + b*x)^{(1/4)})/(b^{(1/4)}*(c + d*x)^{(1/4)})])/d^{(5/4)}$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 205

$\text{Int}[\frac{((a_) + (b_.) * (x_)^2)^{-1}}{a}, x] \text{ ; FreeQ}\{a, b\}, x \ \&\& \ \text{PosQ}[a/b]$
 $\text{:=> Simp}[(\text{Rt}[a/b, 2] * \text{ArcTan}[x/\text{Rt}[a/b, 2]])/a, x]$

Rule 208

$\text{Int}[\frac{((a_) + (b_.) * (x_)^2)^{-1}}{a}, x] \text{ ; FreeQ}\{a, b\}, x \ \&\& \ \text{NegQ}[a/b]$
 $\text{:=> Simp}[(\text{Rt}[-(a/b), 2] * \text{ArcTanh}[x/\text{Rt}[-(a/b), 2]])/a, x]$

Rule 212

$\text{Int}[\frac{((a_) + (b_.) * (x_)^4)^{-1}}{a}, x] \text{ ; FreeQ}\{a, b\}, x \ \&\& \ \text{!GtQ}[a/b, 0]$
 $\text{:=> With}\{r = \text{Numerator}[\text{Rt}[-(a/b), 2]], s = \text{Denominator}[\text{Rt}[-(a/b), 2]]\}, \text{Dist}[r/(2*a), \text{Int}[1/(r - s*x^2), x], x] + \text{Dist}[r/(2*a), \text{Int}[1/(r + s*x^2), x], x]$

Rule 240

$\text{Int}[\frac{((a_) + (b_.) * (x_)^{(n_)})^{(p_)}}{a}, x] \text{ ; FreeQ}\{a, b\}, x \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{LtQ}[-1, p, 0] \ \&\& \ \text{NeQ}[p, -2^{(-1)}] \ \&\& \ \text{IntegerQ}[p + 1/n]$
 $\text{:=> Dist}[a^{(p + 1/n)}, \text{Subst}[\text{Int}[1/(1 - b*x^n)^{(p + 1/n + 1)}, x], x, x/(a + b*x^n)^{(1/n)}, x]$

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[4]{a+bx}}{(c+dx)^{5/4}} dx &= -\frac{4\sqrt[4]{a+bx}}{d\sqrt[4]{c+dx}} + \frac{b \int \frac{1}{(a+bx)^{3/4} \sqrt[4]{c+dx}} dx}{d} \\
&= -\frac{4\sqrt[4]{a+bx}}{d\sqrt[4]{c+dx}} + \frac{4 \operatorname{Subst} \left(\int \frac{1}{\sqrt[4]{c-\frac{ad}{b} + \frac{dx^4}{b}}} dx, x, \sqrt[4]{a+bx} \right)}{d} \\
&= -\frac{4\sqrt[4]{a+bx}}{d\sqrt[4]{c+dx}} + \frac{4 \operatorname{Subst} \left(\int \frac{1}{1-\frac{dx^4}{b}} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{d} \\
&= -\frac{4\sqrt[4]{a+bx}}{d\sqrt[4]{c+dx}} + \frac{(2\sqrt{b}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{b}-\sqrt{d}x^2} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{d} + \frac{(2\sqrt{b}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{b}+\sqrt{d}x^2} dx, x, \frac{\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}} \right)}{d} \\
&= -\frac{4\sqrt[4]{a+bx}}{d\sqrt[4]{c+dx}} + \frac{2\sqrt[4]{b} \tan^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{d^{5/4}} + \frac{2\sqrt[4]{b} \tanh^{-1} \left(\frac{\sqrt[4]{d} \sqrt[4]{a+bx}}{\sqrt[4]{b} \sqrt[4]{c+dx}} \right)}{d^{5/4}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.68

$$\frac{4(a+bx)^{5/4} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(\frac{5}{4}, \frac{5}{4}; \frac{9}{4}; \frac{d(a+bx)}{ad-bc} \right)}{5b(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/4)/(c + d*x)^(5/4), x]

[Out] (4*(a + b*x)^(5/4)*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[5/4, 5/4, 9/4, (d*(a + b*x))/(-b*c) + a*d])/(5*b*(c + d*x)^(5/4))

fricas [B] time = 0.59, size = 273, normalized size = 2.53

$$4(d^2x + cd) \left(\frac{b}{d^5} \right)^{1/4} \arctan \left(\frac{(bx+a)^{1/4} (dx+c)^{3/4} d^4 \left(\frac{b}{d^5} \right)^{3/4} - (d^5x+cd^4) \sqrt{\frac{(d^3x+cd^2) \sqrt{\frac{b}{d^5} + \sqrt{bx+a} \sqrt{dx+c}}}{dx+c}} \left(\frac{b}{d^5} \right)^{3/4}}{bdx+bc} \right) - (d^2x + cd) \left(\frac{b}{d^5} \right)^{1/4} \log \left(\dots \right)$$

$d^2x + cd$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] $-(4*(d^2*x + c*d)*(b/d^5)^{1/4}*\arctan(-((b*x + a)^{1/4}*(d*x + c)^{3/4}*d^4*(b/d^5)^{3/4} - (d^5*x + c*d^4)*\sqrt{((d^3*x + c*d^2)*\sqrt{b/d^5} + \sqrt{b*x + a}*\sqrt{d*x + c})/(d*x + c)}*(b/d^5)^{3/4})/(b*d*x + b*c)) - (d^2*x + c*d)*(b/d^5)^{1/4}*\log(((d^2*x + c*d)*(b/d^5)^{1/4} + (b*x + a)^{1/4}*(d*x + c)^{3/4})/(d*x + c)) + (d^2*x + c*d)*(b/d^5)^{1/4}*\log(-((d^2*x + c*d)*(b/d^5)^{1/4} - (b*x + a)^{1/4}*(d*x + c)^{3/4})/(d*x + c)) + 4*(b*x + a)^{1/4}*(d*x + c)^{3/4})/(d^2*x + c*d)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/4)/(d*x + c)^(5/4), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/4)/(d*x+c)^(5/4),x)

[Out] int((b*x+a)^(1/4)/(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/4)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/4)/(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{1/4}}{(c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(1/4)/(c + d*x)^(5/4), x)
```

```
[Out] int((a + b*x)^(1/4)/(c + d*x)^(5/4), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{\sqrt[4]{a + bx}}{(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(1/4)/(d*x+c)**(5/4), x)
```

```
[Out] Integral((a + b*x)**(1/4)/(c + d*x)**(5/4), x)
```


$$3.1719 \quad \int \frac{1}{(a+bx)^{3/4}(c+dx)^{5/4}} dx$$

Optimal. Leaf size=30

$$\frac{4\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}(bc-ad)}$$

[Out] $4*(b*x+a)^{(1/4)/(-a*d+b*c)/(d*x+c)^{(1/4)}$

Rubi [A] time = 0.00, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{4\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)^{(3/4})*(c + d*x)^{(5/4})), x]$

[Out] $(4*(a + b*x)^{(1/4}))/((b*c - a*d)*(c + d*x)^{(1/4}))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp} [((a + b*x)^{(m + 1})*(c + d*x)^{(n + 1}))/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}[\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{EqQ}[m + n + 2, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{1}{(a+bx)^{3/4}(c+dx)^{5/4}} dx = \frac{4\sqrt[4]{a+bx}}{(bc-ad)\sqrt[4]{c+dx}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$\frac{4\sqrt[4]{a+bx}}{\sqrt[4]{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/((a + b*x)^{(3/4})*(c + d*x)^{(5/4})), x]$

[Out] $(4*(a + b*x)^{(1/4)})/((b*c - a*d)*(c + d*x)^{(1/4)})$

fricas [A] time = 0.65, size = 42, normalized size = 1.40

$$\frac{4 (bx + a)^{\frac{1}{4}} (dx + c)^{\frac{3}{4}}}{bc^2 - acd + (bcd - ad^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/4)/(d*x+c)^(5/4),x, algorithm="fricas")`

[Out] $4*(b*x + a)^{(1/4)}*(d*x + c)^{(3/4)}/(b*c^2 - a*c*d + (b*c*d - a*d^2)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{3}{4}}(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/4)/(d*x+c)^(5/4),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(3/4)*(d*x + c)^(5/4)), x)`

maple [A] time = 0.00, size = 27, normalized size = 0.90

$$-\frac{4 (bx + a)^{\frac{1}{4}}}{(dx + c)^{\frac{1}{4}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(3/4)/(d*x+c)^(5/4),x)`

[Out] $-4*(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(a*d-b*c)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{3}{4}}(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(3/4)/(d*x+c)^(5/4),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(3/4)*(d*x + c)^(5/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{1}{(a + bx)^{3/4} (c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/4)*(c + d*x)^(5/4)), x)

[Out] int(1/((a + b*x)^(3/4)*(c + d*x)^(5/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{4}} (c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/4)/(d*x+c)**(5/4), x)

[Out] Integral(1/((a + b*x)**(3/4)*(c + d*x)**(5/4)), x)

$$3.1720 \quad \int \frac{1}{(a+bx)^{7/4}(c+dx)^{5/4}} dx$$

Optimal. Leaf size=66

$$-\frac{16d\sqrt[4]{a+bx}}{3\sqrt[4]{c+dx}(bc-ad)^2} - \frac{4}{3(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)}$$

[Out] $-4/3/(-a*d+b*c)/(b*x+a)^{(3/4)}/(d*x+c)^{(1/4)}-16/3*d*(b*x+a)^{(1/4)}/(-a*d+b*c)^2/(d*x+c)^{(1/4)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{16d\sqrt[4]{a+bx}}{3\sqrt[4]{c+dx}(bc-ad)^2} - \frac{4}{3(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/4)*(c + d*x)^(5/4)), x]

[Out] $-4/(3*(b*c - a*d)*(a + b*x)^{(3/4)*(c + d*x)^{(1/4)}) - (16*d*(a + b*x)^{(1/4)})/(3*(b*c - a*d)^2*(c + d*x)^{(1/4)})$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  (((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int \frac{1}{(a+bx)^{7/4}(c+dx)^{5/4}} dx = -\frac{4}{3(bc-ad)(a+bx)^{3/4}\sqrt[4]{c+dx}} - \frac{(4d) \int \frac{1}{(a+bx)^{3/4}(c+dx)^{5/4}} dx}{3(bc-ad)}$$

$$= -\frac{4}{3(bc-ad)(a+bx)^{3/4}\sqrt[4]{c+dx}} - \frac{16d\sqrt[4]{a+bx}}{3(bc-ad)^2\sqrt[4]{c+dx}}$$

Mathematica [A] time = 0.02, size = 45, normalized size = 0.68

$$-\frac{4(3ad + b(c + 4dx))}{3(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/4)*(c + d*x)^(5/4)), x]

[Out] (-4*(3*a*d + b*(c + 4*d*x)))/(3*(b*c - a*d)^2*(a + b*x)^(3/4)*(c + d*x)^(1/4))

fricas [B] time = 0.59, size = 126, normalized size = 1.91

$$\frac{4(4bdx + bc + 3ad)(bx + a)^{\frac{1}{4}}(dx + c)^{\frac{3}{4}}}{3(ab^2c^3 - 2a^2bc^2d + a^3cd^2 + (b^3c^2d - 2ab^2cd^2 + a^2bd^3)x^2 + (b^3c^3 - ab^2c^2d - a^2bcd^2 + a^3d^3)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/4)/(d*x+c)^(5/4), x, algorithm="fricas")

[Out] -4/3*(4*b*d*x + b*c + 3*a*d)*(b*x + a)^(1/4)*(d*x + c)^(3/4)/(a*b^2*c^3 - 2*a^2*b*c^2*d + a^3*c*d^2 + (b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*x^2 + (b^3*c^3 - a*b^2*c^2*d - a^2*b*c*d^2 + a^3*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{4}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/4)/(d*x+c)^(5/4), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/4)*(d*x + c)^(5/4)), x)

maple [A] time = 0.01, size = 53, normalized size = 0.80

$$\frac{4(4bdx + 3ad + bc)}{3(bx + a)^{\frac{3}{4}}(dx + c)^{\frac{1}{4}}(a^2d^2 - 2abcd + b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(7/4)/(d*x+c)^(5/4),x)`

[Out] `-4/3*(4*b*d*x+3*a*d+b*c)/(b*x+a)^(3/4)/(d*x+c)^(1/4)/(a^2*d^2-2*a*b*c*d+b^2*c^2)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{4}}(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(7/4)/(d*x+c)^(5/4),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(7/4)*(d*x + c)^(5/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{1}{(a + bx)^{\frac{7}{4}}(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(7/4)*(c + d*x)^(5/4)),x)`

[Out] `int(1/((a + b*x)^(7/4)*(c + d*x)^(5/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{7}{4}}(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(7/4)/(d*x+c)**(5/4),x)`

[Out] `Integral(1/((a + b*x)**(7/4)*(c + d*x)**(5/4)), x)`

$$3.1721 \quad \int \frac{1}{(a+bx)^{11/4}(c+dx)^{5/4}} dx$$

Optimal. Leaf size=101

$$\frac{128d^2\sqrt[4]{a+bx}}{21\sqrt[4]{c+dx}(bc-ad)^3} + \frac{32d}{21(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)^2} - \frac{4}{7(a+bx)^{7/4}\sqrt[4]{c+dx}(bc-ad)}$$

[Out] $-4/7/(-a*d+b*c)/(b*x+a)^{(7/4)}/(d*x+c)^{(1/4)}+32/21*d/(-a*d+b*c)^2/(b*x+a)^{(3/4)}/(d*x+c)^{(1/4)}+128/21*d^2*(b*x+a)^{(1/4)}/(-a*d+b*c)^3/(d*x+c)^{(1/4)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{128d^2\sqrt[4]{a+bx}}{21\sqrt[4]{c+dx}(bc-ad)^3} + \frac{32d}{21(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)^2} - \frac{4}{7(a+bx)^{7/4}\sqrt[4]{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(11/4)*(c + d*x)^(5/4)), x]

[Out] $-4/(7*(b*c - a*d)*(a + b*x)^{(7/4)*(c + d*x)^{(1/4)}) + (32*d)/(21*(b*c - a*d)^2*(a + b*x)^{(3/4)*(c + d*x)^{(1/4)}) + (128*d^2*(a + b*x)^{(1/4)})/(21*(b*c - a*d)^3*(c + d*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{11/4}(c+dx)^{5/4}} dx &= -\frac{4}{7(bc-ad)(a+bx)^{7/4}\sqrt[4]{c+dx}} - \frac{(8d) \int \frac{1}{(a+bx)^{7/4}(c+dx)^{5/4}} dx}{7(bc-ad)} \\
&= -\frac{4}{7(bc-ad)(a+bx)^{7/4}\sqrt[4]{c+dx}} + \frac{32d}{21(bc-ad)^2(a+bx)^{3/4}\sqrt[4]{c+dx}} + \frac{(32d^2) \int \frac{1}{(a+bx)^{5/4}(c+dx)^{5/4}} dx}{21(bc-ad)^3} \\
&= -\frac{4}{7(bc-ad)(a+bx)^{7/4}\sqrt[4]{c+dx}} + \frac{32d}{21(bc-ad)^2(a+bx)^{3/4}\sqrt[4]{c+dx}} + \frac{128d^2\sqrt[4]{a}}{21(bc-ad)^3}
\end{aligned}$$

Mathematica [A] time = 0.03, size = 76, normalized size = 0.75

$$\frac{84a^2d^2 + 56abd(c + 4dx) + 4b^2(-3c^2 + 8cdx + 32d^2x^2)}{21(a+bx)^{7/4}\sqrt[4]{c+dx}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(11/4)*(c + d*x)^(5/4)), x]

[Out] (84*a^2*d^2 + 56*a*b*d*(c + 4*d*x) + 4*b^2*(-3*c^2 + 8*c*d*x + 32*d^2*x^2)) / (21*(b*c - a*d)^3*(a + b*x)^(7/4)*(c + d*x)^(1/4))

fricas [B] time = 0.84, size = 273, normalized size = 2.70

$$\frac{4(32b^2d^2x^2 - 3b^2c^2 + 14abcd + 21a^2d^2 + 8(b^2cd + 7a^2b^2d^2))}{21(a^2b^3c^4 - 3a^3b^2c^3d + 3a^4bc^2d^2 - a^5cd^3 + (b^5c^3d - 3ab^4c^2d^2 + 3a^2b^3cd^3 - a^3b^2d^4)x^3 + (b^5c^4 - ab^4c^3d - 3a^2b^3c^2d^2 + 5a^3b^2c^2d^2 + a^4b^2cd^3 - a^5d^4)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(11/4)/(d*x+c)^(5/4), x, algorithm="fricas")

[Out] 4/21*(32*b^2*d^2*x^2 - 3*b^2*c^2 + 14*a*b*c*d + 21*a^2*d^2 + 8*(b^2*c*d + 7*a*b*d^2)*x)*(b*x + a)^(1/4)*(d*x + c)^(3/4)/(a^2*b^3*c^4 - 3*a^3*b^2*c^3*d + 3*a^4*b*c^2*d^2 - a^5*c*d^3 + (b^5*c^3*d - 3*a*b^4*c^2*d^2 + 3*a^2*b^3*c*d^3 - a^3*b^2*d^4)*x^3 + (b^5*c^4 - a*b^4*c^3*d - 3*a^2*b^3*c^2*d^2 + 5*a^3*b^2*c*d^3 - 2*a^4*b*d^4)*x^2 + (2*a*b^4*c^4 - 5*a^2*b^3*c^3*d + 3*a^3*b^2*c^2*d^2 + a^4*b*c*d^3 - a^5*d^4)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{11}{4}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(11/4)/(d*x+c)^(5/4),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(11/4)*(d*x + c)^(5/4)), x)`

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{4(32b^2x^2d^2 + 56abd^2x + 8b^2cdx + 21a^2d^2 + 14abcd - 3b^2c^2)}{21(bx + a)^{\frac{7}{4}}(dx + c)^{\frac{1}{4}}(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(11/4)/(d*x+c)^(5/4),x)`

[Out] `-4/21*(32*b^2*d^2*x^2+56*a*b*d^2*x+8*b^2*c*d*x+21*a^2*d^2+14*a*b*c*d-3*b^2*c^2)/(b*x+a)^(7/4)/(d*x+c)^(1/4)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{11}{4}}(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(11/4)/(d*x+c)^(5/4),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(11/4)*(d*x + c)^(5/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{\frac{11}{4}}(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(11/4)*(c + d*x)^(5/4)),x)`

[Out] `int(1/((a + b*x)^(11/4)*(c + d*x)^(5/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{11}{4}}(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(11/4)/(d*x+c)**(5/4),x)
```

```
[Out] Integral(1/((a + b*x)**(11/4)*(c + d*x)**(5/4)), x)
```

$$3.1722 \quad \int \frac{1}{(a+bx)^{15/4}(c+dx)^{5/4}} dx$$

Optimal. Leaf size=136

$$\frac{512d^3\sqrt[4]{a+bx}}{77\sqrt[4]{c+dx}(bc-ad)^4} - \frac{128d^2}{77(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)^3} + \frac{48d}{77(a+bx)^{7/4}\sqrt[4]{c+dx}(bc-ad)^2} - \frac{4}{11(a+bx)^{11/4}\sqrt[4]{c+dx}}$$

[Out] $-4/11/(-a*d+b*c)/(b*x+a)^{(11/4)}/(d*x+c)^{(1/4)}+48/77*d/(-a*d+b*c)^2/(b*x+a)^{(7/4)}/(d*x+c)^{(1/4)}-128/77*d^2/(-a*d+b*c)^3/(b*x+a)^{(3/4)}/(d*x+c)^{(1/4)}-512/77*d^3*(b*x+a)^{(1/4)}/(-a*d+b*c)^4/(d*x+c)^{(1/4)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{512d^3\sqrt[4]{a+bx}}{77\sqrt[4]{c+dx}(bc-ad)^4} - \frac{128d^2}{77(a+bx)^{3/4}\sqrt[4]{c+dx}(bc-ad)^3} + \frac{48d}{77(a+bx)^{7/4}\sqrt[4]{c+dx}(bc-ad)^2} - \frac{4}{11(a+bx)^{11/4}\sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(15/4)*(c + d*x)^(5/4)), x]

[Out] $-4/(11*(b*c - a*d)*(a + b*x)^{(11/4)*(c + d*x)^{(1/4)}) + (48*d)/(77*(b*c - a*d)^2*(a + b*x)^{(7/4)*(c + d*x)^{(1/4)}) - (128*d^2)/(77*(b*c - a*d)^3*(a + b*x)^{(3/4)*(c + d*x)^{(1/4)}) - (512*d^3*(a + b*x)^{(1/4)})/(77*(b*c - a*d)^4*(c + d*x)^{(1/4)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{15/4}(c+dx)^{5/4}} dx &= -\frac{4}{11(bc-ad)(a+bx)^{11/4}\sqrt[4]{c+dx}} - \frac{(12d) \int \frac{1}{(a+bx)^{11/4}(c+dx)^{5/4}} dx}{11(bc-ad)} \\
&= -\frac{4}{11(bc-ad)(a+bx)^{11/4}\sqrt[4]{c+dx}} + \frac{48d}{77(bc-ad)^2(a+bx)^{7/4}\sqrt[4]{c+dx}} + \frac{(96d^2) \int \frac{1}{(a+bx)^{7/4}(c+dx)^{5/4}} dx}{77(bc-ad)^2} \\
&= -\frac{4}{11(bc-ad)(a+bx)^{11/4}\sqrt[4]{c+dx}} + \frac{48d}{77(bc-ad)^2(a+bx)^{7/4}\sqrt[4]{c+dx}} - \frac{96d^2}{77(bc-ad)^2} \\
&= -\frac{4}{11(bc-ad)(a+bx)^{11/4}\sqrt[4]{c+dx}} + \frac{48d}{77(bc-ad)^2(a+bx)^{7/4}\sqrt[4]{c+dx}} - \frac{96d^2}{77(bc-ad)^2}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 116, normalized size = 0.85

$$\frac{4(77a^3d^3 + 77a^2bd^2(c+4dx) + 11ab^2d(-3c^2 + 8cdx + 32d^2x^2) + b^3(7c^3 - 12c^2dx + 32cd^2x^2 + 128d^3x^3))}{77(a+bx)^{11/4}\sqrt[4]{c+dx}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(15/4)*(c + d*x)^(5/4)), x]

[Out] (-4*(77*a^3*d^3 + 77*a^2*b*d^2*(c + 4*d*x) + 11*a*b^2*d*(-3*c^2 + 8*c*d*x + 32*d^2*x^2) + b^3*(7*c^3 - 12*c^2*d*x + 32*c*d^2*x^2 + 128*d^3*x^3))/(77*(b*c - a*d)^4*(a + b*x)^(11/4)*(c + d*x)^(1/4))

fricas [B] time = 1.54, size = 457, normalized size = 3.36

$$\frac{4(128b^3d^3x^3 + 77a^3d^3 + 77a^2bd^2(c+4dx) + 11ab^2d(-3c^2 + 8cdx + 32d^2x^2) + b^3(7c^3 - 12c^2dx + 32cd^2x^2 + 128d^3x^3))}{77(a^3b^4c^5 - 4a^4b^3c^4d + 6a^5b^2c^3d^2 - 4a^6bc^2d^3 + a^7cd^4 + (b^7c^4d - 4ab^6c^3d^2 + 6a^2b^5c^2d^3 - 4a^3b^4cd^4 + a^4b^3d^5))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(15/4)/(d*x+c)^(5/4), x, algorithm="fricas")

[Out] -4/77*(128*b^3*d^3*x^3 + 7*b^3*c^3 - 33*a*b^2*c^2*d + 77*a^2*b*c*d^2 + 77*a^3*d^3 + 32*(b^3*c*d^2 + 11*a*b^2*d^3)*x^2 - 4*(3*b^3*c^2*d - 22*a*b^2*c*d^2 - 77*a^2*b*d^3)*x)*(b*x + a)^(1/4)*(d*x + c)^(3/4)/(a^3*b^4*c^5 - 4*a^4*b^3*c^4*d + 6*a^5*b^2*c^3*d^2 - 4*a^6*b*c^2*d^3 + a^7*c*d^4 + (b^7*c^4*d - 4*a*b^6*c^3*d^2 + 6*a^2*b^5*c^2*d^3 - 4*a^3*b^4*c*d^4 + a^4*b^3*d^5)*x^4 + (

$$b^7c^5 - a^6b^5c^4d - 6a^2b^5c^3d^2 + 14a^3b^4c^2d^3 - 11a^4b^3c^2d^4 + 3a^5b^2d^5)x^3 + 3(a^6b^5c^4d - 3a^2b^5c^4d + 2a^3b^4c^3d^2 + 2a^4b^3c^2d^3 - 3a^5b^2c^2d^4 + a^6b^2d^5)x^2 + (3a^2b^5c^5 - 11a^3b^4c^4d + 14a^4b^3c^3d^2 - 6a^5b^2c^2d^3 - a^6b^2c^2d^4 + a^7d^5)x$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{15}{4}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(15/4)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(15/4)*(d*x + c)^(5/4)), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{4(128b^3d^3x^3 + 352ab^2d^3x^2 + 32b^3cd^2x^2 + 308a^2bd^3x + 88ab^2cd^2x - 12b^3c^2dx + 77a^3d^3 + 77a^2bcd^2 - 33a^3c^2d^2 + 77a^2b^2cd^2 - 4ab^3c^3d + b^4c^4)}{77(bx+a)^{\frac{11}{4}}(dx+c)^{\frac{1}{4}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(15/4)/(d*x+c)^(5/4),x)

[Out] $-4/77*(128*b^3*d^3*x^3+352*a*b^2*d^3*x^2+32*b^3*c*d^2*x^2+308*a^2*b*d^3*x+88*a*b^2*c*d^2*x-12*b^3*c^2*d*x+77*a^3*d^3+77*a^2*b*c*d^2-33*a*b^2*c^2*d+7*b^3*c^3)/(b*x+a)^{(11/4)}/(d*x+c)^{(1/4)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{15}{4}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(15/4)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(15/4)*(d*x + c)^(5/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{15/4}(c+dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/((a + b*x)^(15/4)*(c + d*x)^(5/4)),x)
```

```
[Out] int(1/((a + b*x)^(15/4)*(c + d*x)^(5/4)), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(15/4)/(d*x+c)**(5/4),x)
```

```
[Out] Timed out
```

$$3.1723 \quad \int \frac{(a+bx)^{11/4}}{(c+dx)^{5/4}} dx$$

Optimal. Leaf size=776

$$\frac{77\sqrt[4]{b}(bc-ad)^{7/2}\sqrt[4]{(a+bx)(c+dx)}\sqrt{(ad+bc+2bdx)^2}\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)\sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)^2}}}{20\sqrt{2}d^{15/4}\sqrt[4]{a+bx}\sqrt[4]{c+dx}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^2}}$$

[Out] $-4*(b*x+a)^{(11/4)}/d/(d*x+c)^{(1/4)}-77/15*b*(-a*d+b*c)*(b*x+a)^{(3/4)}*(d*x+c)^{(3/4)}/d^3+22/5*b*(b*x+a)^{(7/4)}*(d*x+c)^{(3/4)}/d^2+77/10*(-a*d+b*c)*b^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}/d^{(7/2)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))-77/20*b^{(1/4)}*(-a*d+b*c)^{(7/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticE}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/d^{(15/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}+77/40*b^{(1/4)}*(-a*d+b*c)^{(7/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/d^{(15/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.88, antiderivative size = 776, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 7, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.368$, Rules used = {47, 50, 62, 623, 305, 220, 1196}

$$\frac{77b(a+bx)^{3/4}(c+dx)^{3/4}(bc-ad)}{15d^3} + \frac{77\sqrt{b}(bc-ad)\sqrt{(a+bx)(c+dx)}\sqrt{(ad+bc+2bdx)^2}\sqrt{(ad+b(c+2dx))^2}}{10d^{7/2}\sqrt[4]{a+bx}\sqrt[4]{c+dx}(ad+bc+2bdx)\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(11/4)/(c + d*x)^(5/4),x]

[Out]
$$\begin{aligned} & (-4*(a + b*x)^{(11/4)})/(d*(c + d*x)^{(1/4)}) - (77*b*(b*c - a*d)*(a + b*x)^{(3/4)} \\ & (c + d*x)^{(3/4)})/(15*d^3) + (22*b*(a + b*x)^{(7/4)}*(c + d*x)^{(3/4)})/(5*d^2) \\ & + (77*\sqrt{b}*(b*c - a*d)*\sqrt{(a + b*x)*(c + d*x)}*\sqrt{(b*c + a*d + 2*b*d*x)^2} \\ & *\sqrt{(a*d + b*(c + 2*d*x))^2})/(10*d^{(7/2)}*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)} \\ & *(b*c + a*d + 2*b*d*x)*(1 + (2*\sqrt{b}*\sqrt{d}*\sqrt{(a + b*x)*(c + d*x)})) \\ & /((b*c - a*d))) - (77*b^{(1/4)}*(b*c - a*d)^{(7/2)}*((a + b*x)*(c + d*x))^{(1/4)} \\ & *\sqrt{(b*c + a*d + 2*b*d*x)^2}*(1 + (2*\sqrt{b}*\sqrt{d}*\sqrt{(a + b*x)*(c + d*x)})) \\ & /((b*c - a*d))*\sqrt{(a*d + b*(c + 2*d*x))^2}/((b*c - a*d)^2*(1 + (2*\sqrt{b}*\sqrt{d} \\ & *\sqrt{(a + b*x)*(c + d*x)})))/(b*c - a*d)^2]*\text{EllipticE}[2*\text{ArcTan}[(\sqrt{2}*b^{(1/4)} \\ & *d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)})/\sqrt{b*c - a*d}], 1/2)]/(10*\sqrt{2}*d^{(15/4)} \\ & *(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)}*(b*c + a*d + 2*b*d*x)*\sqrt{(a*d + b*(c + 2*d*x))^2} \\ &) + (77*b^{(1/4)}*(b*c - a*d)^{(7/2)}*((a + b*x)*(c + d*x))^{(1/4)}*\sqrt{(b*c + a*d + 2*b*d*x)^2} \\ & *(1 + (2*\sqrt{b}*\sqrt{d}*\sqrt{(a + b*x)*(c + d*x)})))/(b*c - a*d)*\sqrt{(a*d + b*(c + 2*d*x))^2} \\ & /((b*c - a*d)^2*(1 + (2*\sqrt{b}*\sqrt{d}*\sqrt{(a + b*x)*(c + d*x)})))/(b*c - a*d)^2 \\ &)]*\text{EllipticF}[2*\text{ArcTan}[(\sqrt{2}*b^{(1/4)}*d^{(1/4)}*((a + b*x)*(c + d*x))^{(1/4)})/\sqrt{b*c - a*d}], 1/2)] \\ & /((20*\sqrt{2}*d^{(15/4)}*(a + b*x)^{(1/4)}*(c + d*x)^{(1/4)}*(b*c + a*d + 2*b*d*x)*\sqrt{(a*d + b*(c + 2*d*x))^2}) \end{aligned}$$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)),
Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) &&
!(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &&
& IntLinearQ[a, b, c, d, m, n, x]

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] &&
(!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] &&
IntLinearQ[a, b, c, d, m, n, x]

Rule 62

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] :> Dist[
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] &&
LeQ[3, Denominator[m], 4]

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[(
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x]
, 1/2])/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 305

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 2]}, D
ist[1/q, Int[1/Sqrt[a + b*x^4], x], x] - Dist[1/q, Int[(1 - q*x^2)/Sqrt[a +
b*x^4], x], x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rule 1196

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := With[{q =
Rt[c/a, 4]}, -Simp[(d*x*Sqrt[a + c*x^4])/(a*(1 + q^2*x^2)), x] + Simp[(d*(
1 + q^2*x^2)*Sqrt[(a + c*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticE[2*ArcTan[q*x],
1/2])/(q*Sqrt[a + c*x^4]), x] /; EqQ[e + d*q^2, 0] /; FreeQ[{a, c, d, e},
x] && PosQ[c/a]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{11/4}}{(c+dx)^{5/4}} dx &= -\frac{4(a+bx)^{11/4}}{d\sqrt[4]{c+dx}} + \frac{(11b) \int \frac{(a+bx)^{7/4}}{\sqrt[4]{c+dx}} dx}{d} \\
&= -\frac{4(a+bx)^{11/4}}{d\sqrt[4]{c+dx}} + \frac{22b(a+bx)^{7/4}(c+dx)^{3/4}}{5d^2} - \frac{(77b(bc-ad)) \int \frac{(a+bx)^{3/4}}{\sqrt[4]{c+dx}} dx}{10d^2} \\
&= -\frac{4(a+bx)^{11/4}}{d\sqrt[4]{c+dx}} - \frac{77b(bc-ad)(a+bx)^{3/4}(c+dx)^{3/4}}{15d^3} + \frac{22b(a+bx)^{7/4}(c+dx)^{3/4}}{5d^2} + \frac{(77b(bc-ad)) \int \frac{(a+bx)^{-1/4}}{\sqrt[4]{c+dx}} dx}{10d^2} \\
&= -\frac{4(a+bx)^{11/4}}{d\sqrt[4]{c+dx}} - \frac{77b(bc-ad)(a+bx)^{3/4}(c+dx)^{3/4}}{15d^3} + \frac{22b(a+bx)^{7/4}(c+dx)^{3/4}}{5d^2} + \frac{(77b(bc-ad)) \int \frac{(a+bx)^{-1/4}}{\sqrt[4]{c+dx}} dx}{10d^2} \\
&= -\frac{4(a+bx)^{11/4}}{d\sqrt[4]{c+dx}} - \frac{77b(bc-ad)(a+bx)^{3/4}(c+dx)^{3/4}}{15d^3} + \frac{22b(a+bx)^{7/4}(c+dx)^{3/4}}{5d^2} + \frac{(77b(bc-ad)) \int \frac{(a+bx)^{-1/4}}{\sqrt[4]{c+dx}} dx}{10d^2} \\
&= -\frac{4(a+bx)^{11/4}}{d\sqrt[4]{c+dx}} - \frac{77b(bc-ad)(a+bx)^{3/4}(c+dx)^{3/4}}{15d^3} + \frac{22b(a+bx)^{7/4}(c+dx)^{3/4}}{5d^2} + \frac{(77\sqrt{b}(bc-ad)) \int \frac{(a+bx)^{-1/4}}{\sqrt[4]{c+dx}} dx}{10d^{7/2}}
\end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.09

$$\frac{4(a+bx)^{15/4} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(\frac{5}{4}, \frac{15}{4}; \frac{19}{4}; \frac{d(a+bx)}{ad-bc} \right)}{15b(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(11/4)/(c + d*x)^(5/4), x]

[Out] (4*(a + b*x)^(15/4)*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[5/4, 15/4, 19/4, (d*(a + b*x))/(-b*c + a*d)]/(15*b*(c + d*x)^(5/4))

fricas [F] time = 1.12, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(b^2x^2 + 2abx + a^2)(bx + a)^{\frac{3}{4}}(dx + c)^{\frac{3}{4}}}{d^2x^2 + 2cdx + c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(11/4)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] integral((b^2*x^2 + 2*a*b*x + a^2)*(b*x + a)^(3/4)*(d*x + c)^(3/4)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{11}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(11/4)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(11/4)/(d*x + c)^(5/4), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{11}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(11/4)/(d*x+c)^(5/4),x)

[Out] int((b*x+a)^(11/4)/(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{11}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(11/4)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(11/4)/(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{11/4}}{(c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(11/4)/(c + d*x)^(5/4),x)
```

```
[Out] int((a + b*x)^(11/4)/(c + d*x)^(5/4), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(11/4)/(d*x+c)**(5/4),x)
```

```
[Out] Timed out
```

$$3.1724 \quad \int \frac{(a+bx)^{7/4}}{(c+dx)^{5/4}} dx$$

Optimal. Leaf size=730

$$\frac{7\sqrt[4]{b}(bc-ad)^{5/2}\sqrt[4]{(a+bx)(c+dx)}\sqrt{(ad+bc+2bdx)^2}\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)\sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)^2}}}{2\sqrt{2}d^{11/4}\sqrt[4]{a+bx}\sqrt[4]{c+dx}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^2}}$$

[Out] $-4*(b*x+a)^{(7/4)}/d/(d*x+c)^{(1/4)}+14/3*b*(b*x+a)^{(3/4)}*(d*x+c)^{(3/4)}/d^2-7*b^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}/d^{(5/2)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))+7/2*b^{(1/4)}*(-a*d+b*c)^{(5/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticE}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/d^{(11/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}-7/4*b^{(1/4)}*(-a*d+b*c)^{(5/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/d^{(11/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.73, antiderivative size = 730, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 7, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.368$, Rules used = {47, 50, 62, 623, 305, 220, 1196}

$$\frac{14b(a+bx)^{3/4}(c+dx)^{3/4}}{3d^2} - \frac{7\sqrt{b}\sqrt{(a+bx)(c+dx)}\sqrt{(ad+bc+2bdx)^2}\sqrt{(ad+b(c+2dx))^2}}{d^{5/2}\sqrt[4]{a+bx}\sqrt[4]{c+dx}(ad+bc+2bdx)\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/4)/(c + d*x)^(5/4), x]

```
[Out] (-4*(a + b*x)^(7/4))/(d*(c + d*x)^(1/4)) + (14*b*(a + b*x)^(3/4)*(c + d*x)^(3/4))/(3*d^2) - (7*Sqrt[b]*Sqrt[(a + b*x)*(c + d*x)]*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/(d^(5/2)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])))/(b*c - a*d)) + (7*b^(1/4)*(b*c - a*d)^(5/2)*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])))/(b*c - a*d)*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])))/(b*c - a*d)^2]*EllipticE[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2])/(Sqrt[2]*d^(11/4)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2]) - (7*b^(1/4)*(b*c - a*d)^(5/2)*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])))/(b*c - a*d)*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])))/(b*c - a*d)^2]*EllipticF[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2])/(2*Sqrt[2]*d^(11/4)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2])
```

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
((a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
```

$(1 + q^2 x^2) \sqrt{(a + b x^4)/(a(1 + q^2 x^2)^2)} \text{EllipticF}[2 \text{ArcTan}[q x], 1/2] / (2 q \sqrt{a + b x^4}), x] /; \text{FreeQ}\{a, b\}, x\} \ \&\& \ \text{PosQ}[b/a]$

Rule 305

$\text{Int}[(x_)^2/\sqrt{(a_) + (b_.)(x_)^4}, x_Symbol] \text{ :> With}\{q = \text{Rt}[b/a, 2]\}, \text{Dist}[1/q, \text{Int}[1/\sqrt{a + b x^4}, x], x] - \text{Dist}[1/q, \text{Int}[(1 - q x^2)/\sqrt{a + b x^4}, x], x] /; \text{FreeQ}\{a, b\}, x\} \ \&\& \ \text{PosQ}[b/a]$

Rule 623

$\text{Int}[(a_.) + (b_.)(x_) + (c_.)(x_)^2]^{(p_)}, x_Symbol] \text{ :> With}\{d = \text{Denominator}[p]\}, \text{Dist}[(d \sqrt{(b + 2 c x)^2})/(b + 2 c x), \text{Subst}[\text{Int}[x^{(d(p + 1) - 1)}/\sqrt{b^2 - 4 a c + 4 c x^d}], x], x, (a + b x + c x^2)^{(1/d)}], x] /; 3 \leq d \leq 4 /; \text{FreeQ}\{a, b, c\}, x\} \ \&\& \ \text{NeQ}[b^2 - 4 a c, 0] \ \&\& \ \text{RationalQ}[p]$

Rule 1196

$\text{Int}[(d_) + (e_.)(x_)^2]/\sqrt{(a_) + (c_.)(x_)^4}, x_Symbol] \text{ :> With}\{q = \text{Rt}[c/a, 4]\}, -\text{Simp}[(d x \sqrt{a + c x^4})/(a(1 + q^2 x^2)), x] + \text{Simp}[(d(1 + q^2 x^2) \sqrt{(a + c x^4)/(a(1 + q^2 x^2)^2)} \text{EllipticE}[2 \text{ArcTan}[q x], 1/2])/(q \sqrt{a + c x^4}), x] /; \text{EqQ}[e + d q^2, 0] /; \text{FreeQ}\{a, c, d, e\}, x\} \ \&\& \ \text{PosQ}[c/a]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/4}}{(c+dx)^{5/4}} dx &= -\frac{4(a+bx)^{7/4}}{d\sqrt[4]{c+dx}} + \frac{(7b) \int \frac{(a+bx)^{3/4}}{\sqrt[4]{c+dx}} dx}{d} \\
&= -\frac{4(a+bx)^{7/4}}{d\sqrt[4]{c+dx}} + \frac{14b(a+bx)^{3/4}(c+dx)^{3/4}}{3d^2} - \frac{(7b(bc-ad)) \int \frac{1}{\sqrt[4]{a+bx}\sqrt[4]{c+dx}} dx}{2d^2} \\
&= -\frac{4(a+bx)^{7/4}}{d\sqrt[4]{c+dx}} + \frac{14b(a+bx)^{3/4}(c+dx)^{3/4}}{3d^2} - \frac{(7b(bc-ad)\sqrt[4]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[4]{ac+(bc+ad)x+bd}}} \\
&= -\frac{4(a+bx)^{7/4}}{d\sqrt[4]{c+dx}} + \frac{14b(a+bx)^{3/4}(c+dx)^{3/4}}{3d^2} - \frac{(14b(bc-ad)\sqrt[4]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)})}{d^2\sqrt[4]{a+bx}\sqrt[4]{c+dx}} \\
&= -\frac{4(a+bx)^{7/4}}{d\sqrt[4]{c+dx}} + \frac{14b(a+bx)^{3/4}(c+dx)^{3/4}}{3d^2} - \frac{(7\sqrt{b}(bc-ad)^2\sqrt[4]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)})}{d^{5/2}\sqrt[4]{a+bx}\sqrt[4]{c+dx}} \\
&= -\frac{4(a+bx)^{7/4}}{d\sqrt[4]{c+dx}} + \frac{14b(a+bx)^{3/4}(c+dx)^{3/4}}{3d^2} - \frac{7\sqrt{b}\sqrt{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\sqrt{(ad)}}{d^{5/2}\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad+2bdx)} \left(1 + \frac{2\sqrt{b}\sqrt{(a+bx)(c+dx)}}{bc+ad+2bdx}\right)
\end{aligned}$$

Mathematica [C] time = 0.07, size = 73, normalized size = 0.10

$$\frac{4(a+bx)^{11/4} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4} {}_2F_1\left(\frac{5}{4}, \frac{11}{4}; \frac{15}{4}; \frac{d(a+bx)}{ad-bc}\right)}{11b(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/4)/(c + d*x)^(5/4), x]

[Out] (4*(a + b*x)^(11/4)*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[5/4, 11/4, 15/4, (d*(a + b*x))/(-(b*c) + a*d)]/(11*b*(c + d*x)^(5/4))

fricas [F] time = 0.73, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{7}{4}}(dx+c)^{\frac{3}{4}}}{d^2x^2+2cdx+c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/4)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] integral((b*x + a)^(7/4)*(d*x + c)^(3/4)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/4)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(7/4)/(d*x + c)^(5/4), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/4)/(d*x+c)^(5/4),x)

[Out] int((b*x+a)^(7/4)/(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/4)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/4)/(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{7/4}}{(c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/4)/(c + d*x)^(5/4),x)

[Out] `int((a + b*x)^(7/4)/(c + d*x)^(5/4), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{7}{4}}}{(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(7/4)/(d*x+c)**(5/4), x)`

[Out] `Integral((a + b*x)**(7/4)/(c + d*x)**(5/4), x)`

$$3.1725 \quad \int \frac{(a+bx)^{3/4}}{(c+dx)^{5/4}} dx$$

Optimal. Leaf size=712

$$\frac{3\sqrt[4]{b}(bc-ad)^{3/2}\sqrt[4]{(a+bx)(c+dx)}\sqrt{(ad+bc+2bdx)^2}\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)\sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)^2}}}{\sqrt{2}d^{7/4}\sqrt[4]{a+bx}\sqrt[4]{c+dx}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^2}}$$

[Out] $-4*(b*x+a)^{(3/4)}/d/(d*x+c)^{(1/4)}+6*b^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}/d^{(3/2)}/(-a*d+b*c)/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))+3/2*b^{(1/4)}*(-a*d+b*c)^{(3/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/d^{(7/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)*2^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}-3*b^{(1/4)}*(-a*d+b*c)^{(3/2)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticE}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)})*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/d^{(7/4)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.61, antiderivative size = 712, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {47, 62, 623, 305, 220, 1196}

$$\frac{6\sqrt{b}\sqrt{(a+bx)(c+dx)}\sqrt{(ad+bc+2bdx)^2}\sqrt{(ad+b(c+2dx))^2}}{d^{3/2}\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc-ad)(ad+bc+2bdx)\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)} + \frac{3\sqrt[4]{b}(bc-ad)^{3/2}\sqrt[4]{(a+bx)(c+dx)}\sqrt{(ad+b(c+2dx))^2}}{\sqrt{2}d^{7/4}\sqrt[4]{a+bx}\sqrt[4]{c+dx}(ad+bc+2bdx)\sqrt{(ad+b(c+2dx))^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/4)/(c + d*x)^(5/4), x]

```
[Out] (-4*(a + b*x)^(3/4))/(d*(c + d*x)^(1/4)) + (6*Sqrt[b]*Sqrt[(a + b*x)*(c + d*x)]*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/(d^(3/2)*(b*c - a*d)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x])]/(b*c - a*d))) - (3*Sqrt[2]*b^(1/4)*(b*c - a*d)^(3/2)*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x])]/(b*c - a*d))*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x])]/(b*c - a*d))^2)]*EllipticE[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2])/(d^(7/4)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2]) + (3*b^(1/4)*(b*c - a*d)^(3/2)*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x])]/(b*c - a*d))*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x])]/(b*c - a*d))^2)]*EllipticF[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2])/(Sqrt[2]*d^(7/4)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2])
```

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)),
Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) &&
!(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &&
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x],
1/2])/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 305

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 2]}, D
ist[1/q, Int[1/Sqrt[a + b*x^4], x], x] - Dist[1/q, Int[(1 - q*x^2)/Sqrt[a +
b*x^4], x], x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rule 1196

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := With[{q = Rt[c/a, 4]}, -Simp[(d*x*Sqrt[a + c*x^4])/(a*(1 + q^2*x^2)), x] + Simp[(d*(1 + q^2*x^2)*Sqrt[(a + c*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticE[2*ArcTan[q*x], 1/2])/(q*Sqrt[a + c*x^4]), x] /; EqQ[e + d*q^2, 0] /; FreeQ[{a, c, d, e}, x] && PosQ[c/a]

Rubi steps

$$\begin{aligned}
 \int \frac{(a+bx)^{3/4}}{(c+dx)^{5/4}} dx &= -\frac{4(a+bx)^{3/4}}{d\sqrt[4]{c+dx}} + \frac{(3b) \int \frac{1}{\sqrt[4]{a+bx}\sqrt[4]{c+dx}} dx}{d} \\
 &= -\frac{4(a+bx)^{3/4}}{d\sqrt[4]{c+dx}} + \frac{(3b\sqrt[4]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[4]{ac+(bc+ad)x+bdx^2}} dx}{d\sqrt[4]{a+bx}\sqrt[4]{c+dx}} \\
 &= -\frac{4(a+bx)^{3/4}}{d\sqrt[4]{c+dx}} + \frac{(12b\sqrt[4]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}) \text{Subst}\left(\int \frac{x^2}{\sqrt{-4abcd+(bc+ad)^2+4bdx^4}}\right)}{d\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad+2bdx)} \\
 &= -\frac{4(a+bx)^{3/4}}{d\sqrt[4]{c+dx}} + \frac{(6\sqrt{b}(bc-ad)\sqrt[4]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}) \text{Subst}\left(\int \frac{1}{\sqrt{-4abcd+(bc+ad)^2+4bdx^4}}\right)}{d^{3/2}\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad+2bdx)} \\
 &= -\frac{4(a+bx)^{3/4}}{d\sqrt[4]{c+dx}} + \frac{6\sqrt{b}\sqrt{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\sqrt{(ad+b(c+2dx))^2}}{d^{3/2}(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad+2bdx)\left(1+\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}\right)}
 \end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.10

$$\frac{4(a+bx)^{7/4} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4} {}_2F_1\left(\frac{5}{4}, \frac{7}{4}, \frac{11}{4}, \frac{d(a+bx)}{ad-bc}\right)}{7b(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/4)/(c + d*x)^(5/4),x]

[Out] (4*(a + b*x)^(7/4)*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[5/4, 7/4, 11/4, (d*(a + b*x))/(-b*c + a*d)]/(7*b*(c + d*x)^(5/4))

fricas [F] time = 0.63, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^{\frac{3}{4}}(dx + c)^{\frac{3}{4}}}{d^2x^2 + 2cdx + c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] integral((b*x + a)^(3/4)*(d*x + c)^(3/4)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/4)/(d*x + c)^(5/4), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/4)/(d*x+c)^(5/4),x)

[Out] int((b*x+a)^(3/4)/(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{4}}}{(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/4)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/4)/(d*x + c)^(5/4), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{3/4}}{(c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/4)/(c + d*x)^(5/4),x)

[Out] int((a + b*x)^(3/4)/(c + d*x)^(5/4), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{4}}}{(c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/4)/(d*x+c)**(5/4),x)

[Out] Integral((a + b*x)**(3/4)/(c + d*x)**(5/4), x)


```
[Out] (4*(a + b*x)^(3/4))/((b*c - a*d)*(c + d*x)^(1/4)) - (4*Sqrt[b]*Sqrt[(a + b*x)*(c + d*x)]*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/
(Sqrt[d]*(b*c - a*d)^2*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)^(1/4)*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))) + (2*Sqrt[2]*b^(1/4)*Sqrt[b*c - a*d]*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))
*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))^2)*EllipticE[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2)]/(d^(3/4)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2]) - (Sqrt[2]*b^(1/4)*Sqrt[b*c - a*d]*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))*Sqrt[(a*d + b*(c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))^2)*EllipticF[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2)]/(d^(3/4)*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2])
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x],
1/2]]/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 305

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 2]}, D
ist[1/q, Int[1/Sqrt[a + b*x^4], x], x] - Dist[1/q, Int[(1 - q*x^2)/Sqrt[a +
b*x^4], x], x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rule 1196

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := With[{q = Rt[c/a, 4]}, -Simp[(d*x*Sqrt[a + c*x^4])/(a*(1 + q^2*x^2)), x] + Simp[(d*(1 + q^2*x^2)*Sqrt[(a + c*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticE[2*ArcTan[q*x], 1/2])/(q*Sqrt[a + c*x^4]), x] /; EqQ[e + d*q^2, 0]] /; FreeQ[{a, c, d, e}, x] && PosQ[c/a]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{\sqrt[4]{a+bx}(c+dx)^{5/4}} dx &= \frac{4(a+bx)^{3/4}}{(bc-ad)\sqrt[4]{c+dx}} - \frac{(2b) \int \frac{1}{\sqrt[4]{a+bx}\sqrt[4]{c+dx}} dx}{bc-ad} \\
 &= \frac{4(a+bx)^{3/4}}{(bc-ad)\sqrt[4]{c+dx}} - \frac{(2b\sqrt[4]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[4]{ac+(bc+ad)x+bdx^2}} dx}{(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}} \\
 &= \frac{4(a+bx)^{3/4}}{(bc-ad)\sqrt[4]{c+dx}} - \frac{(8b\sqrt[4]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}) \text{Subst}\left(\int \frac{x}{\sqrt{-4abcd+(bc+ad)x^2}} dx\right)}{(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad)} \\
 &= \frac{4(a+bx)^{3/4}}{(bc-ad)\sqrt[4]{c+dx}} - \frac{(4\sqrt{b}\sqrt[4]{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}) \text{Subst}\left(\int \frac{x}{\sqrt{-4abcd+(bc+ad)x^2}} dx\right)}{\sqrt{d}\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad)} \\
 &= \frac{4(a+bx)^{3/4}}{(bc-ad)\sqrt[4]{c+dx}} - \frac{4\sqrt{b}\sqrt{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\sqrt{(ad+b(c+2dx))}}{\sqrt{d}(bc-ad)^2\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad+2bdx)} \left(1 + \frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)}}{bc-ad}\right)
 \end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.10

$$\frac{4(a+bx)^{3/4} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/4} {}_2F_1\left(\frac{3}{4}, \frac{5}{4}; \frac{7}{4}; \frac{d(a+bx)}{ad-bc}\right)}{3b(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/4)*(c + d*x)^(5/4)),x]

[Out] $(4*(a + b*x)^{(3/4)}*((b*(c + d*x))/(b*c - a*d))^{(5/4)}*Hypergeometric2F1[3/4, 5/4, 7/4, (d*(a + b*x))/(-b*c + a*d)]/(3*b*(c + d*x)^{(5/4)})$

fricas [F] time = 0.93, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^{\frac{3}{4}}(dx + c)^{\frac{3}{4}}}{bd^2x^3 + ac^2 + (2bcd + ad^2)x^2 + (bc^2 + 2acd)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/4)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] $\text{integral}((b*x + a)^{(3/4)}*(d*x + c)^{(3/4)}/(b*d^2*x^3 + a*c^2 + (2*b*c*d + a*d^2)*x^2 + (b*c^2 + 2*a*c*d)*x), x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{4}}(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/4)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] $\text{integrate}(1/((b*x + a)^{(1/4)}*(d*x + c)^{(5/4)}), x)$

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{4}}(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/4)/(d*x+c)^(5/4),x)

[Out] $\text{int}(1/(b*x+a)^{(1/4)}/(d*x+c)^{(5/4)},x)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{4}}(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/4)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/4)*(d*x + c)^(5/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{1/4} (c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/4)*(c + d*x)^(5/4)),x)

[Out] int(1/((a + b*x)^(1/4)*(c + d*x)^(5/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[4]{a + bx} (c + dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/4)/(d*x+c)**(5/4),x)

[Out] Integral(1/((a + b*x)**(1/4)*(c + d*x)**(5/4)), x)

$$3.1727 \quad \int \frac{1}{(a+bx)^{5/4}(c+dx)^{5/4}} dx$$

Optimal. Leaf size=750

$$2\sqrt{2} \sqrt[4]{b} \sqrt[4]{d} \sqrt[4]{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2} \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right) \sqrt{\frac{(ad+b(c+2dx))^2}{(bc-ad)^2 \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)^2}} \text{Ellip}$$

$$\sqrt[4]{a+bx} \sqrt[4]{c+dx} \sqrt{bc-ad} (ad+bc+2bdx) \sqrt{(ad+b(c+2dx))^2}$$

[Out] $-4/(-a*d+b*c)/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}-8*d*(b*x+a)^{(3/4)}/(-a*d+b*c)^{2/(d*x+c)^{(1/4)}+8*b^{(1/2)*d^{(1/2)*((b*x+a)*(d*x+c))^{(1/2)*((2*b*d*x+a*d+b*c)^2)^{(1/2)*((a*d+b*(2*d*x+c))^2)^{(1/2)}/(-a*d+b*c)^3/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/(1+2*b^{(1/2)*d^{(1/2)*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))}-4*b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*(\cos(2*\arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/(-a*d+b*c)^{(1/2))}*\text{EllipticE}(\sin(2*\arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/(-a*d+b*c)^{(1/2))}), 1/2*2^{(1/2)})^2)^{(1/2)}/(-a*d+b*c)^{(1/2))}*(1+2*b^{(1/2)*d^{(1/2)*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/(-a*d+b*c)^{(1/2)}/(2*b*d*x+a*d+b*c)/(-a*d+b*c)^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)+2*b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*(\cos(2*\arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/(-a*d+b*c)^{(1/2))}*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)*d^{(1/4)*((b*x+a)*(d*x+c))^{(1/4)*2^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/(-a*d+b*c)^{(1/2))}), 1/2*2^{(1/2)})^2)^{(1/2)}/(-a*d+b*c)^{(1/2))}*(1+2*b^{(1/2)*d^{(1/2)*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c)^{(1/2))})^2)^{(1/2)}/(-a*d+b*c)^{(1/2)}/(2*b*d*x+a*d+b*c)/(-a*d+b*c)^{(1/2)}/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.74, antiderivative size = 750, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {51, 62, 623, 305, 220, 1196}

$$-\frac{8d(a+bx)^{3/4}}{\sqrt[4]{c+dx}(bc-ad)^2} + \frac{8\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)} \sqrt{(ad+bc+2bdx)^2} \sqrt{(ad+b(c+2dx))^2}}{\sqrt[4]{a+bx} \sqrt[4]{c+dx} (bc-ad)^3 (ad+bc+2bdx) \left(\frac{2\sqrt{b} \sqrt{d} \sqrt{(a+bx)(c+dx)}}{bc-ad} + 1 \right)} - \frac{4}{\sqrt[4]{a+bx} \sqrt[4]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/4)*(c + d*x)^(5/4)), x]

```
[Out] -4/((b*c - a*d)*(a + b*x)^(1/4)*(c + d*x)^(1/4)) - (8*d*(a + b*x)^(3/4))/((
b*c - a*d)^2*(c + d*x)^(1/4)) + (8*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)
]*Sqrt[(b*c + a*d + 2*b*d*x)^2]*Sqrt[(a*d + b*(c + 2*d*x))^2])/((b*c - a*d)
^3*(a + b*x)^(1/4)*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*(1 + (2*Sqrt[b]*Sqr
t[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))) - (4*Sqrt[2]*b^(1/4)*d^(1/4)
*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*(1 + (2*Sqrt[b]*
Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))*Sqrt[(a*d + b*(c + 2*d*x))^
2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c -
a*d))^2)]*EllipticE[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)*(c + d*x))
^(1/4))/Sqrt[b*c - a*d]], 1/2)]/(Sqrt[b*c - a*d]*(a + b*x)^(1/4)*(c + d*x)^
(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2]) + (2*Sqrt[2]*b^(
1/4)*d^(1/4)*((a + b*x)*(c + d*x))^(1/4)*Sqrt[(b*c + a*d + 2*b*d*x)^2]*(1 +
(2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*x)])/(b*c - a*d))*Sqrt[(a*d + b*(
c + 2*d*x))^2]/((b*c - a*d)^2*(1 + (2*Sqrt[b]*Sqrt[d]*Sqrt[(a + b*x)*(c + d*
x)])/(b*c - a*d))^2)]*EllipticF[2*ArcTan[(Sqrt[2]*b^(1/4)*d^(1/4)*((a + b*x)
*(c + d*x))^(1/4))/Sqrt[b*c - a*d]], 1/2)]/(Sqrt[b*c - a*d]*(a + b*x)^(1/4)
*(c + d*x)^(1/4)*(b*c + a*d + 2*b*d*x)*Sqrt[(a*d + b*(c + 2*d*x))^2])
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 62

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[
(a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x
+ b*d*x^2)^m, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[
-1, m, 0] && LeQ[3, Denominator[m], 4]
```

Rule 220

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[
(1 + q^2*x^2)*Sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticF[2*ArcTan[q*x],
1/2]]/(2*q*Sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 305

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 2]}, D
ist[1/q, Int[1/Sqrt[a + b*x^4], x], x] - Dist[1/q, Int[(1 - q*x^2)/Sqrt[a +
b*x^4], x], x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denominator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1) - 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3 <= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]

Rule 1196

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := With[{q = Rt[c/a, 4]}, -Simp[(d*x*Sqrt[a + c*x^4])/(a*(1 + q^2*x^2)), x] + Simp[(d*(1 + q^2*x^2)*Sqrt[(a + c*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticE[2*ArcTan[q*x], 1/2])/(q*Sqrt[a + c*x^4]), x] /; EqQ[e + d*q^2, 0] /; FreeQ[{a, c, d, e}, x] && PosQ[c/a]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{5/4}(c+dx)^{5/4}} dx &= -\frac{4}{(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}} - \frac{(2d) \int \frac{1}{\sqrt[4]{a+bx}(c+dx)^{5/4}} dx}{bc-ad} \\
 &= -\frac{4}{(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}} - \frac{8d(a+bx)^{3/4}}{(bc-ad)^2\sqrt[4]{c+dx}} + \frac{(4bd) \int \frac{1}{\sqrt[4]{a+bx}\sqrt[4]{c+dx}} dx}{(bc-ad)^2} \\
 &= -\frac{4}{(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}} - \frac{8d(a+bx)^{3/4}}{(bc-ad)^2\sqrt[4]{c+dx}} + \frac{(4bd\sqrt[4]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[4]{a+bx}\sqrt[4]{c+dx}} dx}{(bc-ad)^2\sqrt[4]{a+bx}} \\
 &= -\frac{4}{(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}} - \frac{8d(a+bx)^{3/4}}{(bc-ad)^2\sqrt[4]{c+dx}} + \frac{(16bd\sqrt[4]{(a+bx)(c+dx)}\sqrt{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[4]{a+bx}\sqrt[4]{c+dx}} dx}{(bc-ad)^2\sqrt[4]{a+bx}} \\
 &= -\frac{4}{(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}} - \frac{8d(a+bx)^{3/4}}{(bc-ad)^2\sqrt[4]{c+dx}} + \frac{(8\sqrt{b}\sqrt{d}\sqrt[4]{(a+bx)(c+dx)}) \int \frac{1}{\sqrt[4]{a+bx}\sqrt[4]{c+dx}} dx}{(bc-ad)^2\sqrt[4]{a+bx}} \\
 &= -\frac{4}{(bc-ad)\sqrt[4]{a+bx}\sqrt[4]{c+dx}} - \frac{8d(a+bx)^{3/4}}{(bc-ad)^2\sqrt[4]{c+dx}} + \frac{8\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)} \int \frac{1}{\sqrt[4]{a+bx}\sqrt[4]{c+dx}} dx}{(bc-ad)^3\sqrt[4]{a+bx}\sqrt[4]{c+dx}}
 \end{aligned}$$

Mathematica [C] time = 0.05, size = 71, normalized size = 0.09

$$-\frac{4 \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(-\frac{1}{4}, \frac{5}{4}; \frac{3}{4}; \frac{d(a+bx)}{ad-bc} \right)}{b \sqrt[4]{a+bx} (c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/4)*(c + d*x)^(5/4)), x]

[Out] (-4*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[-1/4, 5/4, 3/4, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(a + b*x)^(1/4)*(c + d*x)^(5/4))

fricas [F] time = 1.23, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^{\frac{3}{4}}(dx + c)^{\frac{3}{4}}}{b^2 d^2 x^4 + a^2 c^2 + 2(b^2 cd + abd^2)x^3 + (b^2 c^2 + 4abcd + a^2 d^2)x^2 + 2(abc^2 + a^2 cd)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/4)/(d*x+c)^(5/4), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/4)*(d*x + c)^(3/4)/(b^2*d^2*x^4 + a^2*c^2 + 2*(b^2*c*d + a*b*d^2)*x^3 + (b^2*c^2 + 4*a*b*c*d + a^2*d^2)*x^2 + 2*(a*b*c^2 + a^2*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{4}}(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/4)/(d*x+c)^(5/4), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/4)*(d*x + c)^(5/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{4}}(dx + c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/4)/(d*x+c)^(5/4), x)

[Out] `int(1/(b*x+a)^(5/4)/(d*x+c)^(5/4),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{4}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/4)/(d*x+c)^(5/4),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(5/4)*(d*x + c)^(5/4)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{4}}(c+dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(5/4)*(c + d*x)^(5/4)),x)`

[Out] `int(1/((a + b*x)^(5/4)*(c + d*x)^(5/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{4}}(c+dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/4)/(d*x+c)**(5/4),x)`

[Out] `Integral(1/((a + b*x)**(5/4)*(c + d*x)**(5/4)), x)`

$$3.1728 \quad \int \frac{1}{(a+bx)^{9/4}(c+dx)^{5/4}} dx$$

Optimal. Leaf size=795

$$\frac{48(a+bx)^{3/4}d^2}{5(bc-ad)^3\sqrt[4]{c+dx}} - \frac{48\sqrt{b}\sqrt{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\sqrt{(ad+b(c+2dx))^2}d^{3/2}}{5(bc-ad)^4\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad+2bdx)\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)} + \frac{24\sqrt{2}\sqrt[4]{b}\sqrt[4]{(a+bx)}}{5(bc-ad)^4\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad+2bdx)\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)}$$

[Out] $-4/5/(-a*d+b*c)/(b*x+a)^{(5/4)}/(d*x+c)^{(1/4)}+24/5*d/(-a*d+b*c)^2/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}+48/5*d^2*(b*x+a)^{(3/4)}/(-a*d+b*c)^3/(d*x+c)^{(1/4)}-48/5*d^{(3/2)}*b^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2)^{(1/2)}/(-a*d+b*c)^4/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))+24/5*b^{(1/4)}*d^{(5/4)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticE}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)})*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/(-a*d+b*c)^{(3/2)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}-12/5*b^{(1/4)}*d^{(5/4)}*((b*x+a)*(d*x+c))^{(1/4)}*(\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))^2)^{(1/2)}/\cos(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)}))*\text{EllipticF}(\sin(2*\arctan(b^{(1/4)}*d^{(1/4)}*((b*x+a)*(d*x+c))^{(1/4)}*2^{(1/2)}/(-a*d+b*c)^{(1/2)})),1/2*2^{(1/2)})*2^{(1/2)}*(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))*((2*b*d*x+a*d+b*c)^2)^{(1/2)}*((a*d+b*(2*d*x+c))^2/(-a*d+b*c)^2/(1+2*b^{(1/2)}*d^{(1/2)}*((b*x+a)*(d*x+c))^{(1/2)}/(-a*d+b*c))^2)^{(1/2)}/(-a*d+b*c)^{(3/2)}/(b*x+a)^{(1/4)}/(d*x+c)^{(1/4)}/(2*b*d*x+a*d+b*c)/((a*d+b*(2*d*x+c))^2)^{(1/2)}$

Rubi [A] time = 0.86, antiderivative size = 795, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {51, 62, 623, 305, 220, 1196}

$$\frac{48(a+bx)^{3/4}d^2}{5(bc-ad)^3\sqrt[4]{c+dx}} - \frac{48\sqrt{b}\sqrt{(a+bx)(c+dx)}\sqrt{(bc+ad+2bdx)^2}\sqrt{(ad+b(c+2dx))^2}d^{3/2}}{5(bc-ad)^4\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad+2bdx)\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)} + \frac{24\sqrt{2}\sqrt[4]{b}\sqrt[4]{(a+bx)}}{5(bc-ad)^4\sqrt[4]{a+bx}\sqrt[4]{c+dx}(bc+ad+2bdx)\left(\frac{2\sqrt{b}\sqrt{d}\sqrt{(a+bx)(c+dx)}}{bc-ad}+1\right)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(9/4)*(c + d*x)^(5/4)),x]

[Out]
$$-4/(5*(b*c - a*d)*(a + b*x)^{5/4}*(c + d*x)^{1/4}) + (24*d)/(5*(b*c - a*d)^2*(a + b*x)^{1/4}*(c + d*x)^{1/4}) + (48*d^2*(a + b*x)^{3/4})/(5*(b*c - a*d)^3*(c + d*x)^{1/4}) - (48*\sqrt{b}*d^{3/2}*\sqrt{(a + b*x)*(c + d*x)}*\sqrt{(b*c + a*d + 2*b*d*x)^2}*\sqrt{(a*d + b*(c + 2*d*x))^2})/(5*(b*c - a*d)^4*(a + b*x)^{1/4}*(c + d*x)^{1/4}*(b*c + a*d + 2*b*d*x)*(1 + (2*\sqrt{b}*\sqrt{d}*\sqrt{(a + b*x)*(c + d*x)}))/(b*c - a*d)) + (24*\sqrt{2}*b^{1/4}*d^{5/4}*((a + b*x)*(c + d*x))^{1/4}*\sqrt{(b*c + a*d + 2*b*d*x)^2}*(1 + (2*\sqrt{b}*\sqrt{d}*\sqrt{(a + b*x)*(c + d*x)}))/(b*c - a*d))*\sqrt{(a*d + b*(c + 2*d*x))^2}/((b*c - a*d)^2*(1 + (2*\sqrt{b}*\sqrt{d}*\sqrt{(a + b*x)*(c + d*x)}))/(b*c - a*d))^2]*\text{EllipticE}[2*\text{ArcTan}[\sqrt{2}*b^{1/4}*d^{1/4}*((a + b*x)*(c + d*x))^{1/4}]/\sqrt{b*c - a*d}], 1/2)]/(5*(b*c - a*d)^{3/2}*(a + b*x)^{1/4}*(c + d*x)^{1/4}*(b*c + a*d + 2*b*d*x)*\sqrt{(a*d + b*(c + 2*d*x))^2}) - (12*\sqrt{2}*b^{1/4}*d^{5/4}*((a + b*x)*(c + d*x))^{1/4}*\sqrt{(b*c + a*d + 2*b*d*x)^2}*(1 + (2*\sqrt{b}*\sqrt{d}*\sqrt{(a + b*x)*(c + d*x)}))/(b*c - a*d))*\sqrt{(a*d + b*(c + 2*d*x))^2}/((b*c - a*d)^2*(1 + (2*\sqrt{b}*\sqrt{d}*\sqrt{(a + b*x)*(c + d*x)}))/(b*c - a*d))^2]*\text{EllipticF}[2*\text{ArcTan}[\sqrt{2}*b^{1/4}*d^{1/4}*((a + b*x)*(c + d*x))^{1/4}]/\sqrt{b*c - a*d}], 1/2)]/(5*(b*c - a*d)^{3/2}*(a + b*x)^{1/4}*(c + d*x)^{1/4}*(b*c + a*d + 2*b*d*x)*\sqrt{(a*d + b*(c + 2*d*x))^2})$$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 62

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := Dist[((a + b*x)^m*(c + d*x)^m)/((a + b*x)*(c + d*x))^m, Int[(a*c + (b*c + a*d)*x + b*d*x^2)^m, x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[3, Denominator[m], 4]

Rule 220

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 4]}, Simp[((1 + q^2*x^2)*sqrt[(a + b*x^4)/(a*(1 + q^2*x^2)^2])*EllipticF[2*ArcTan[q*x], 1/2])/(2*q*sqrt[a + b*x^4]), x] /; FreeQ[{a, b}, x] && PosQ[b/a]

Rule 305

Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[b/a, 2]}, D

```
ist[1/q, Int[1/Sqrt[a + b*x^4], x], x] - Dist[1/q, Int[(1 - q*x^2)/Sqrt[a +
b*x^4], x], x] /; FreeQ[{a, b}, x] && PosQ[b/a]
```

Rule 623

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(p_), x_Symbol] := With[{d = Denomi
nator[p]}, Dist[(d*Sqrt[(b + 2*c*x)^2])/(b + 2*c*x), Subst[Int[x^(d*(p + 1)
- 1)/Sqrt[b^2 - 4*a*c + 4*c*x^d], x], x, (a + b*x + c*x^2)^(1/d)], x] /; 3
<= d <= 4] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0] && RationalQ[p]
```

Rule 1196

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := With[{q =
Rt[c/a, 4]}, -Simp[(d*x*Sqrt[a + c*x^4])/(a*(1 + q^2*x^2)), x] + Simp[(d*(
1 + q^2*x^2)*Sqrt[(a + c*x^4)/(a*(1 + q^2*x^2)^2)]*EllipticE[2*ArcTan[q*x],
1/2])/(q*Sqrt[a + c*x^4]), x] /; EqQ[e + d*q^2, 0]] /; FreeQ[{a, c, d, e},
x] && PosQ[c/a]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{9/4}(c+dx)^{5/4}} dx &= -\frac{4}{5(bc-ad)(a+bx)^{5/4}\sqrt[4]{c+dx}} - \frac{(6d) \int \frac{1}{(a+bx)^{5/4}(c+dx)^{5/4}} dx}{5(bc-ad)} \\
&= -\frac{4}{5(bc-ad)(a+bx)^{5/4}\sqrt[4]{c+dx}} + \frac{24d}{5(bc-ad)^2\sqrt[4]{a+bx}\sqrt[4]{c+dx}} + \frac{(12d^2) \int \frac{1}{\sqrt[4]{a+bx}}}{5(bc-ad)} \\
&= -\frac{4}{5(bc-ad)(a+bx)^{5/4}\sqrt[4]{c+dx}} + \frac{24d}{5(bc-ad)^2\sqrt[4]{a+bx}\sqrt[4]{c+dx}} + \frac{48d^2(a+bx)}{5(bc-ad)^3\sqrt[4]{c}} \\
&= -\frac{4}{5(bc-ad)(a+bx)^{5/4}\sqrt[4]{c+dx}} + \frac{24d}{5(bc-ad)^2\sqrt[4]{a+bx}\sqrt[4]{c+dx}} + \frac{48d^2(a+bx)}{5(bc-ad)^3\sqrt[4]{c}} \\
&= -\frac{4}{5(bc-ad)(a+bx)^{5/4}\sqrt[4]{c+dx}} + \frac{24d}{5(bc-ad)^2\sqrt[4]{a+bx}\sqrt[4]{c+dx}} + \frac{48d^2(a+bx)}{5(bc-ad)^3\sqrt[4]{c}} \\
&= -\frac{4}{5(bc-ad)(a+bx)^{5/4}\sqrt[4]{c+dx}} + \frac{24d}{5(bc-ad)^2\sqrt[4]{a+bx}\sqrt[4]{c+dx}} + \frac{48d^2(a+bx)}{5(bc-ad)^3\sqrt[4]{c}} \\
&= -\frac{4}{5(bc-ad)(a+bx)^{5/4}\sqrt[4]{c+dx}} + \frac{24d}{5(bc-ad)^2\sqrt[4]{a+bx}\sqrt[4]{c+dx}} + \frac{48d^2(a+bx)}{5(bc-ad)^3\sqrt[4]{c}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.09

$$-\frac{4 \left(\frac{b(c+dx)}{bc-ad} \right)^{5/4} {}_2F_1 \left(-\frac{5}{4}, \frac{5}{4}; -\frac{1}{4}; \frac{d(a+bx)}{ad-bc} \right)}{5b(a+bx)^{5/4}(c+dx)^{5/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(9/4)*(c + d*x)^(5/4)), x]

[Out] (-4*((b*(c + d*x))/(b*c - a*d))^(5/4)*Hypergeometric2F1[-5/4, 5/4, -1/4, (d*(a + b*x))/(-b*c + a*d)])/(5*b*(a + b*x)^(5/4)*(c + d*x)^(5/4))

fricas [F] time = 0.86, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{3}{4}}(dx+c)^{\frac{3}{4}}}{b^3d^2x^5 + a^3c^2 + (2b^3cd + 3ab^2d^2)x^4 + (b^3c^2 + 6ab^2cd + 3a^2bd^2)x^3 + (3ab^2c^2 + 6a^2bcd + a^3d^2)x^2 + \dots} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/4)/(d*x+c)^(5/4),x, algorithm="fricas")

[Out] integral((b*x + a)^(3/4)*(d*x + c)^(3/4)/(b^3*d^2*x^5 + a^3*c^2 + (2*b^3*c*d + 3*a*b^2*d^2)*x^4 + (b^3*c^2 + 6*a*b^2*c*d + 3*a^2*b*d^2)*x^3 + (3*a*b^2*c^2 + 6*a^2*b*c*d + a^3*d^2)*x^2 + (3*a^2*b*c^2 + 2*a^3*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{9}{4}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/4)/(d*x+c)^(5/4),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(9/4)*(d*x + c)^(5/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{9}{4}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(9/4)/(d*x+c)^(5/4),x)

[Out] int(1/(b*x+a)^(9/4)/(d*x+c)^(5/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{9}{4}}(dx+c)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(9/4)/(d*x+c)^(5/4),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(9/4)*(d*x + c)^(5/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{9/4}(c+dx)^{5/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(9/4)*(c + d*x)^(5/4)), x)`

[Out] `int(1/((a + b*x)^(9/4)*(c + d*x)^(5/4)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{9}{4}} (c + dx)^{\frac{5}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(9/4)/(d*x+c)**(5/4), x)`

[Out] `Integral(1/((a + b*x)**(9/4)*(c + d*x)**(5/4)), x)`

$$3.1729 \quad \int \frac{1}{\sqrt[4]{1-ax} (1+bx)^{3/4}} dx$$

Optimal. Leaf size=279

$$\frac{\log\left(-\frac{\sqrt{2} \sqrt[4]{a} \sqrt[4]{b} \sqrt[4]{1-ax}}{\sqrt[4]{bx+1}} + \frac{\sqrt{b} \sqrt{1-ax}}{\sqrt{bx+1}} + \sqrt{a}\right)}{\sqrt{2} \sqrt[4]{a} b^{3/4}} + \frac{\log\left(\frac{\sqrt{2} \sqrt[4]{a} \sqrt[4]{b} \sqrt[4]{1-ax}}{\sqrt[4]{bx+1}} + \frac{\sqrt{b} \sqrt{1-ax}}{\sqrt{bx+1}} + \sqrt{a}\right)}{\sqrt{2} \sqrt[4]{a} b^{3/4}} + \frac{\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{b} \sqrt[4]{1-ax}}{\sqrt[4]{a} \sqrt[4]{bx+1}}\right)}{\sqrt[4]{a} b^{3/4}}$$

[Out] $-1/2*\ln(-a^{(1/4)}*b^{(1/4)}*(-a*x+1)^{(1/4)}*2^{(1/2)}/(b*x+1)^{(1/4)}+a^{(1/2)}+b^{(1/2)}*(-a*x+1)^{(1/2)}/(b*x+1)^{(1/2)})/a^{(1/4)}/b^{(3/4)}*2^{(1/2)}+1/2*\ln(a^{(1/4)}*b^{(1/4)}*(-a*x+1)^{(1/4)}*2^{(1/2)}/(b*x+1)^{(1/4)}+a^{(1/2)}+b^{(1/2)}*(-a*x+1)^{(1/2)}/(b*x+1)^{(1/2)})/a^{(1/4)}/b^{(3/4)}*2^{(1/2)}+\arctan(1-b^{(1/4)}*(-a*x+1)^{(1/4)}*2^{(1/2)})/a^{(1/4)}/(b*x+1)^{(1/4)}*2^{(1/2)}/a^{(1/4)}/b^{(3/4)}-\arctan(1+b^{(1/4)}*(-a*x+1)^{(1/4)}*2^{(1/2)})/a^{(1/4)}/(b*x+1)^{(1/4)}*2^{(1/2)}/a^{(1/4)}/b^{(3/4)}$

Rubi [A] time = 0.30, antiderivative size = 279, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 8, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.400$, Rules used = {63, 331, 297, 1162, 617, 204, 1165, 628}

$$\frac{\log\left(-\frac{\sqrt{2} \sqrt[4]{a} \sqrt[4]{b} \sqrt[4]{1-ax}}{\sqrt[4]{bx+1}} + \frac{\sqrt{b} \sqrt{1-ax}}{\sqrt{bx+1}} + \sqrt{a}\right)}{\sqrt{2} \sqrt[4]{a} b^{3/4}} + \frac{\log\left(\frac{\sqrt{2} \sqrt[4]{a} \sqrt[4]{b} \sqrt[4]{1-ax}}{\sqrt[4]{bx+1}} + \frac{\sqrt{b} \sqrt{1-ax}}{\sqrt{bx+1}} + \sqrt{a}\right)}{\sqrt{2} \sqrt[4]{a} b^{3/4}} + \frac{\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{b} \sqrt[4]{1-ax}}{\sqrt[4]{a} \sqrt[4]{bx+1}}\right)}{\sqrt[4]{a} b^{3/4}}$$

Antiderivative was successfully verified.

[In] Int[1/((1 - a*x)^(1/4)*(1 + b*x)^(3/4)),x]

[Out] $(\text{Sqrt}[2]*\text{ArcTan}[1 - (\text{Sqrt}[2]*b^{(1/4)}*(1 - a*x)^{(1/4)})/(a^{(1/4)}*(1 + b*x)^{(1/4)})])/(a^{(1/4)}*b^{(3/4)}) - (\text{Sqrt}[2]*\text{ArcTan}[1 + (\text{Sqrt}[2]*b^{(1/4)}*(1 - a*x)^{(1/4)})/(a^{(1/4)}*(1 + b*x)^{(1/4)})])/(a^{(1/4)}*b^{(3/4)}) - \text{Log}[\text{Sqrt}[a] + (\text{Sqrt}[b]*\text{Sqrt}[1 - a*x])/(\text{Sqrt}[1 + b*x]) - (\text{Sqrt}[2]*a^{(1/4)}*b^{(1/4)}*(1 - a*x)^{(1/4)})/(1 + b*x)^{(1/4)}]/(\text{Sqrt}[2]*a^{(1/4)}*b^{(3/4)}) + \text{Log}[\text{Sqrt}[a] + (\text{Sqrt}[b]*\text{Sqrt}[1 - a*x])/(\text{Sqrt}[1 + b*x]) + (\text{Sqrt}[2]*a^{(1/4)}*b^{(1/4)}*(1 - a*x)^{(1/4)})/(1 + b*x)^{(1/4)}]/(\text{Sqrt}[2]*a^{(1/4)}*b^{(3/4)})]$

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 204


```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])
```

Rule 297

```
Int[(x_)^2/((a_) + (b_.)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[a/b, 2]], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*s), Int[(r + s*x^2)/(a + b*x^4), x], x] - Dist[1/(2*s), Int[(r - s*x^2)/(a + b*x^4), x], x] /; FreeQ[{a, b}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] & AtomQ[SplitProduct[SumBaseQ, b]]))
```

Rule 331

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*Simplify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c]) /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 1162

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x], x] + Dist[e/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x] /; FreeQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]
```

Rule 1165

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x], x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x] /; Fre
```

eQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{\sqrt[4]{1-ax}(1+bx)^{3/4}} dx &= -\frac{4 \operatorname{Subst}\left(\int \frac{x^2}{\left(1+\frac{b}{a}-\frac{bx^4}{a}\right)^{3/4}} dx, x, \sqrt[4]{1-ax}\right)}{a} \\
 &= -\frac{4 \operatorname{Subst}\left(\int \frac{x^2}{1+\frac{bx^4}{a}} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+bx}}\right)}{a} \\
 &= \frac{2 \operatorname{Subst}\left(\int \frac{\sqrt{a}-\sqrt{b}x^2}{1+\frac{bx^4}{a}} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+bx}}\right)}{a\sqrt{b}} - \frac{2 \operatorname{Subst}\left(\int \frac{\sqrt{a}+\sqrt{b}x^2}{1+\frac{bx^4}{a}} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+bx}}\right)}{a\sqrt{b}} \\
 &= -\frac{\operatorname{Subst}\left(\int \frac{1}{\frac{\sqrt{a}}{\sqrt{b}}-\frac{\sqrt{2}}{\sqrt[4]{b}}\frac{\sqrt[4]{ax}}{+x^2}} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+bx}}\right)}{b} - \frac{\operatorname{Subst}\left(\int \frac{1}{\frac{\sqrt{a}}{\sqrt{b}}+\frac{\sqrt{2}}{\sqrt[4]{b}}\frac{\sqrt[4]{ax}}{+x^2}} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+bx}}\right)}{b} \\
 &= -\frac{\log\left(\sqrt{a} + \frac{\sqrt{b}\sqrt{1-ax}}{\sqrt{1+bx}} - \frac{\sqrt{2}\sqrt[4]{a}\sqrt[4]{b}\sqrt[4]{1-ax}}{\sqrt[4]{1+bx}}\right)}{\sqrt{2}\sqrt[4]{a}b^{3/4}} + \frac{\log\left(\sqrt{a} + \frac{\sqrt{b}\sqrt{1-ax}}{\sqrt{1+bx}} + \frac{\sqrt{2}\sqrt[4]{a}\sqrt[4]{b}\sqrt[4]{1-ax}}{\sqrt[4]{1+bx}}\right)}{\sqrt{2}\sqrt[4]{a}b^{3/4}} \\
 &= \frac{\sqrt{2}\tan^{-1}\left(1 - \frac{\sqrt{2}\sqrt[4]{b}\sqrt[4]{1-ax}}{\sqrt[4]{a}\sqrt[4]{1+bx}}\right)}{\sqrt[4]{a}b^{3/4}} - \frac{\sqrt{2}\tan^{-1}\left(1 + \frac{\sqrt{2}\sqrt[4]{b}\sqrt[4]{1-ax}}{\sqrt[4]{a}\sqrt[4]{1+bx}}\right)}{\sqrt[4]{a}b^{3/4}} - \frac{\log\left(\sqrt{a} + \frac{\sqrt{b}\sqrt{1-ax}}{\sqrt{1+bx}}\right)}{\sqrt{2}\sqrt[4]{a}b^{3/4}}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 65, normalized size = 0.23

$$\frac{4(1-ax)^{3/4}\left(\frac{abx+a}{a+b}\right)^{3/4} {}_2F_1\left(\frac{3}{4}, \frac{3}{4}; \frac{7}{4}; \frac{b-abx}{a+b}\right)}{3a(bx+1)^{3/4}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1 - a*x)^(1/4)*(1 + b*x)^(3/4)), x]

[Out] (-4*(1 - a*x)^(3/4)*((a + a*b*x)/(a + b))^(3/4)*Hypergeometric2F1[3/4, 3/4, 7/4, (b - a*b*x)/(a + b)])/(3*a*(1 + b*x)^(3/4))

fricas [A] time = 0.79, size = 247, normalized size = 0.89

$$-4 \left(-\frac{1}{ab^3} \right)^{\frac{1}{4}} \arctan \left(\frac{(-ax+1)^{\frac{3}{4}}(bx+1)^{\frac{1}{4}}ab^2 \left(-\frac{1}{ab^3} \right)^{\frac{3}{4}} - (a^2b^2x - ab^2) \sqrt{\frac{(ab^2x-b^2) \sqrt{-\frac{1}{ab^3}} - \sqrt{-ax+1} \sqrt{bx+1}}{ax-1}}}{ax-1} \left(-\frac{1}{ab^3} \right)^{\frac{3}{4}} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-a*x+1)^(1/4)/(b*x+1)^(3/4),x, algorithm="fricas")

[Out] $-4 * (-1/(a*b^3))^{1/4} * \arctan(-((-a*x + 1)^{3/4} * (b*x + 1)^{1/4} * a*b^2 * (-1/(a*b^3))^{3/4} - (a^2*b^2*x - a*b^2) * \sqrt{((a*b^2*x - b^2) * \sqrt{-1/(a*b^3)}) - \sqrt{-a*x + 1} * \sqrt{b*x + 1}} / (a*x - 1)) * (-1/(a*b^3))^{3/4} / (a*x - 1)) - (-1/(a*b^3))^{1/4} * \log(((a*b*x - b) * (-1/(a*b^3))^{1/4} + (-a*x + 1)^{3/4} * (b*x + 1)^{1/4}) / (a*x - 1)) + (-1/(a*b^3))^{1/4} * \log(-((a*b*x - b) * (-1/(a*b^3))^{1/4} - (-a*x + 1)^{3/4} * (b*x + 1)^{1/4}) / (a*x - 1))$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(-ax+1)^{\frac{1}{4}}(bx+1)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-a*x+1)^(1/4)/(b*x+1)^(3/4),x, algorithm="giac")

[Out] integrate(1/((-a*x + 1)^(1/4)*(b*x + 1)^(3/4)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(-ax+1)^{\frac{1}{4}}(bx+1)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-a*x+1)^(1/4)/(b*x+1)^(3/4),x)

[Out] int(1/(-a*x+1)^(1/4)/(b*x+1)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(-ax+1)^{\frac{1}{4}}(bx+1)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-a*x+1)^(1/4)/(b*x+1)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((-a*x + 1)^(1/4)*(b*x + 1)^(3/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(1 - ax)^{1/4} (bx + 1)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((1 - a*x)^(1/4)*(b*x + 1)^(3/4)),x)

[Out] int(1/((1 - a*x)^(1/4)*(b*x + 1)^(3/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[4]{-ax + 1} (bx + 1)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-a*x+1)**(1/4)/(b*x+1)**(3/4),x)

[Out] Integral(1/((-a*x + 1)**(1/4)*(b*x + 1)**(3/4)), x)

$$3.1730 \quad \int \frac{1}{\sqrt[4]{1-ax} (1+ax)^{3/4}} dx$$

Optimal. Leaf size=193

$$\frac{\log\left(\frac{\sqrt{1-ax}}{\sqrt{ax+1}} - \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{ax+1}} + 1\right)}{\sqrt{2} a} + \frac{\log\left(\frac{\sqrt{1-ax}}{\sqrt{ax+1}} + \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{ax+1}} + 1\right)}{\sqrt{2} a} + \frac{\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{ax+1}}\right)}{a} - \frac{\sqrt{2} \tan^{-1}\left(\frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{ax+1}}\right)}{a} +$$

[Out] $-1/2*\ln(1-(-a*x+1)^{(1/4)}*2^{(1/2)}/(a*x+1)^{(1/4)}+(-a*x+1)^{(1/2)}/(a*x+1)^{(1/2)})/a*2^{(1/2)}+1/2*\ln(1+(-a*x+1)^{(1/4)}*2^{(1/2)}/(a*x+1)^{(1/4)}+(-a*x+1)^{(1/2)}/(a*x+1)^{(1/2)})/a*2^{(1/2)}-\arctan(-1+(-a*x+1)^{(1/4)}*2^{(1/2)}/(a*x+1)^{(1/4)})*2^{(1/2)}/a-\arctan(1+(-a*x+1)^{(1/4)}*2^{(1/2)}/(a*x+1)^{(1/4)})*2^{(1/2)}/a$

Rubi [A] time = 0.14, antiderivative size = 193, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 8, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.400$, Rules used = {63, 331, 297, 1162, 617, 204, 1165, 628}

$$\frac{\log\left(\frac{\sqrt{1-ax}}{\sqrt{ax+1}} - \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{ax+1}} + 1\right)}{\sqrt{2} a} + \frac{\log\left(\frac{\sqrt{1-ax}}{\sqrt{ax+1}} + \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{ax+1}} + 1\right)}{\sqrt{2} a} + \frac{\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{ax+1}}\right)}{a} - \frac{\sqrt{2} \tan^{-1}\left(\frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{ax+1}}\right)}{a} +$$

Antiderivative was successfully verified.

[In] Int[1/((1 - a*x)^(1/4)*(1 + a*x)^(3/4)), x]

[Out] (Sqrt[2]*ArcTan[1 - (Sqrt[2]*(1 - a*x)^(1/4))/(1 + a*x)^(1/4)])/a - (Sqrt[2]*ArcTan[1 + (Sqrt[2]*(1 - a*x)^(1/4))/(1 + a*x)^(1/4)])/a - Log[1 + Sqrt[1 - a*x]/Sqrt[1 + a*x] - (Sqrt[2]*(1 - a*x)^(1/4))/(1 + a*x)^(1/4)]/(Sqrt[2]*a) + Log[1 + Sqrt[1 - a*x]/Sqrt[1 + a*x] + (Sqrt[2]*(1 - a*x)^(1/4))/(1 + a*x)^(1/4)]/(Sqrt[2]*a)

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 204

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 297

```
Int[(x_)^2/((a_) + (b_.)*(x_)^4), x_Symbol] := With[{r = Numerator[Rt[a/b,
2]], s = Denominator[Rt[a/b, 2]]}, Dist[1/(2*s), Int[(r + s*x^2)/(a + b*x^4
), x], x] - Dist[1/(2*s), Int[(r - s*x^2)/(a + b*x^4), x], x]] /; FreeQ[{a,
b}, x] && (GtQ[a/b, 0] || (PosQ[a/b] && AtomQ[SplitProduct[SumBaseQ, a]] &
& AtomQ[SplitProduct[SumBaseQ, b]]))
```

Rule 331

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m +
1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)
^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2
^(-1)] && IntegersQ[m, p + (m + 1)/n]
```

Rule 617

```
Int[((a_) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := With[{q = 1 - 4*S
implify[(a*c)/b^2]}, Dist[-2/b, Subst[Int[1/(q - x^2), x], x, 1 + (2*c*x)/b
], x] /; RationalQ[q] && (EqQ[q^2, 1] || !RationalQ[b^2 - 4*a*c])] /; Free
Q[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 1162

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
(2*d)/e, 2]}, Dist[e/(2*c), Int[1/Simp[d/e + q*x + x^2, x], x] + Dist[e
/(2*c), Int[1/Simp[d/e - q*x + x^2, x], x], x]] /; FreeQ[{a, c, d, e}, x] &
& EqQ[c*d^2 - a*e^2, 0] && PosQ[d*e]
```

Rule 1165

```
Int[((d_) + (e_.)*(x_)^2)/((a_) + (c_.)*(x_)^4), x_Symbol] := With[{q = Rt[
(-2*d)/e, 2]}, Dist[e/(2*c*q), Int[(q - 2*x)/Simp[d/e + q*x - x^2, x], x],
x] + Dist[e/(2*c*q), Int[(q + 2*x)/Simp[d/e - q*x - x^2, x], x], x]] /; Fre
eQ[{a, c, d, e}, x] && EqQ[c*d^2 - a*e^2, 0] && NegQ[d*e]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt[4]{1-ax}(1+ax)^{3/4}} dx &= \frac{4 \operatorname{Subst}\left(\int \frac{x^2}{(2-x^4)^{3/4}} dx, x, \sqrt[4]{1-ax}\right)}{a} \\
&= \frac{4 \operatorname{Subst}\left(\int \frac{x^2}{1+x^4} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{a} \\
&= \frac{2 \operatorname{Subst}\left(\int \frac{1-x^2}{1+x^4} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{a} - \frac{2 \operatorname{Subst}\left(\int \frac{1+x^2}{1+x^4} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{a} \\
&= \frac{\operatorname{Subst}\left(\int \frac{1}{1-\sqrt{2}x+x^2} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{a} - \frac{\operatorname{Subst}\left(\int \frac{1}{1+\sqrt{2}x+x^2} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{a} - \frac{\operatorname{Subst}\left(\int \frac{1}{-1-x^2} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{a} \\
&= \frac{\log\left(1 + \frac{\sqrt{1-ax}}{\sqrt{1+ax}} - \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{\sqrt{2}a} + \frac{\log\left(1 + \frac{\sqrt{1-ax}}{\sqrt{1+ax}} + \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{\sqrt{2}a} - \frac{\sqrt{2} \operatorname{Subst}\left(\int \frac{1}{-1-x^2} dx, x, \frac{\sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{a} \\
&= \frac{\sqrt{2} \tan^{-1}\left(1 - \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{a} - \frac{\sqrt{2} \tan^{-1}\left(1 + \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{a} - \frac{\log\left(1 + \frac{\sqrt{1-ax}}{\sqrt{1+ax}} - \frac{\sqrt{2} \sqrt[4]{1-ax}}{\sqrt[4]{1+ax}}\right)}{\sqrt{2}a}
\end{aligned}$$

Mathematica [C] time = 0.01, size = 42, normalized size = 0.22

$$\frac{2\sqrt[4]{2}(1-ax)^{3/4} {}_2F_1\left(\frac{3}{4}, \frac{3}{4}; \frac{7}{4}; \frac{1}{2}(1-ax)\right)}{3a}$$

Antiderivative was successfully verified.

[In] Integrate[1/((1 - a*x)^(1/4)*(1 + a*x)^(3/4)), x]

[Out] (-2*2^(1/4)*(1 - a*x)^(3/4)*Hypergeometric2F1[3/4, 3/4, 7/4, (1 - a*x)/2])/ (3*a)

fricas [B] time = 0.65, size = 448, normalized size = 2.32

$$2\sqrt{2} \frac{1}{a^4} \arctan \left(\frac{\sqrt{2}(ax+1)^{\frac{1}{4}}(-ax+1)^{\frac{3}{4}} a^{\frac{3}{4}} - \sqrt{2}(a^4x - a^3) \sqrt{\frac{\sqrt{2}(ax+1)^{\frac{1}{4}}(-ax+1)^{\frac{3}{4}} a^{\frac{1}{4}} + (a^3x - a^2) \sqrt{\frac{1}{a^4} - \sqrt{ax+1}}}}{ax-1}} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-a*x+1)^(1/4)/(a*x+1)^(3/4),x, algorithm="fricas")

[Out] 2*sqrt(2)*(a^(-4))^(1/4)*arctan(-(sqrt(2)*(a*x + 1)^(1/4)*(-a*x + 1)^(3/4)*a^3*(a^(-4))^(3/4) - sqrt(2)*(a^4*x - a^3)*sqrt((sqrt(2)*(a*x + 1)^(1/4)*(-a*x + 1)^(3/4)*a*(a^(-4))^(1/4) + (a^3*x - a^2)*sqrt(a^(-4)) - sqrt(a*x + 1)*sqrt(-a*x + 1)))/(a*x - 1))*(a^(-4))^(3/4) + a*x - 1)/(a*x - 1) + 2*sqrt(2)*(a^(-4))^(1/4)*arctan(-(sqrt(2)*(a*x + 1)^(1/4)*(-a*x + 1)^(3/4)*a^3*(a^(-4))^(3/4) - sqrt(2)*(a^4*x - a^3)*sqrt(-(sqrt(2)*(a*x + 1)^(1/4)*(-a*x + 1)^(3/4)*a*(a^(-4))^(1/4) - (a^3*x - a^2)*sqrt(a^(-4)) + sqrt(a*x + 1)*sqrt(-a*x + 1)))/(a*x - 1))*(a^(-4))^(3/4) - a*x + 1)/(a*x - 1) - 1/2*sqrt(2)*(a^(-4))^(1/4)*log((sqrt(2)*(a*x + 1)^(1/4)*(-a*x + 1)^(3/4)*a*(a^(-4))^(1/4) + (a^3*x - a^2)*sqrt(a^(-4)) - sqrt(a*x + 1)*sqrt(-a*x + 1)))/(a*x - 1) + 1/2*sqrt(2)*(a^(-4))^(1/4)*log(-(sqrt(2)*(a*x + 1)^(1/4)*(-a*x + 1)^(3/4)*a*(a^(-4))^(1/4) - (a^3*x - a^2)*sqrt(a^(-4)) + sqrt(a*x + 1)*sqrt(-a*x + 1)))/(a*x - 1))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ax+1)^{\frac{3}{4}}(-ax+1)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-a*x+1)^(1/4)/(a*x+1)^(3/4),x, algorithm="giac")

[Out] integrate(1/((a*x + 1)^(3/4)*(-a*x + 1)^(1/4)), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{1}{(-ax+1)^{\frac{1}{4}}(ax+1)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(-a*x+1)^(1/4)/(a*x+1)^(3/4),x)

[Out] int(1/(-a*x+1)^(1/4)/(a*x+1)^(3/4),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(ax+1)^{\frac{3}{4}}(-ax+1)^{\frac{1}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-a*x+1)^(1/4)/(a*x+1)^(3/4),x, algorithm="maxima")

[Out] integrate(1/((a*x + 1)^(3/4)*(-a*x + 1)^(1/4)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(1 - ax)^{1/4} (ax + 1)^{3/4}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((1 - a*x)^(1/4)*(a*x + 1)^(3/4)),x)

[Out] int(1/((1 - a*x)^(1/4)*(a*x + 1)^(3/4)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[4]{-ax + 1} (ax + 1)^{\frac{3}{4}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(-a*x+1)**(1/4)/(a*x+1)**(3/4),x)

[Out] Integral(1/((-a*x + 1)**(1/4)*(a*x + 1)**(3/4)), x)

$$3.1731 \quad \int \frac{(a+bx)^{3/2}}{\sqrt[5]{c+dx}} dx$$

Optimal. Leaf size=74

$$\frac{2(a+bx)^{5/2} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{5}{2}; \frac{7}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{5b\sqrt[5]{c+dx}}$$

[Out] 2/5*(b*x+a)^(5/2)*(b*(d*x+c)/(-a*d+b*c))^(1/5)*hypergeom([1/5, 5/2], [7/2], -d*(b*x+a)/(-a*d+b*c))/b/(d*x+c)^(1/5)

Rubi [A] time = 0.03, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{2(a+bx)^{5/2} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{5}{2}; \frac{7}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{5b\sqrt[5]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)/(c + d*x)^(1/5), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(1/5)*Hypergeometric2F1[1/5, 5/2, 7/2, -((d*(a + b*x))/(b*c - a*d))]/(5*b*(c + d*x)^(1/5))

Rule 69

```
Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))
```

Rule 70

```
Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])
```

Rubi steps

$$\int \frac{(a+bx)^{3/2}}{\sqrt[5]{c+dx}} dx = \frac{\sqrt[5]{\frac{b(c+dx)}{bc-ad}} \int \frac{(a+bx)^{3/2}}{\sqrt[5]{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}}} dx}{\sqrt[5]{c+dx}}$$

$$= \frac{2(a+bx)^{5/2} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{5}{2}; \frac{7}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{5b\sqrt[5]{c+dx}}$$

Mathematica [A] time = 0.03, size = 73, normalized size = 0.99

$$\frac{2(a+bx)^{5/2} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc}\right)}{5b\sqrt[5]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(1/5), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(1/5)*Hypergeometric2F1[1/5, 5/2, 7/2, (d*(a + b*x))/(-b*c + a*d)])/(5*b*(c + d*x)^(1/5))

fricas [F] time = 4.08, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{1}{5}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/5), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)/(d*x + c)^(1/5), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/5), x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(1/5), x)

maple [F] time = 0.19, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(1/5), x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(1/5), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/5), x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(1/5), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{3}{2}}}{(c + dx)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/(c + d*x)^(1/5), x)

[Out] int((a + b*x)^(3/2)/(c + d*x)^(1/5), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{\sqrt[5]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/(d*x+c)**(1/5), x)

[Out] Integral((a + b*x)**(3/2)/(c + d*x)**(1/5), x)

$$3.1732 \quad \int \frac{\sqrt{a+bx}}{\sqrt[5]{c+dx}} dx$$

Optimal. Leaf size=74

$$\frac{2(a+bx)^{3/2} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{3}{2}; \frac{5}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{3b\sqrt[5]{c+dx}}$$

[Out] $2/3*(b*x+a)^{(3/2)}*(b*(d*x+c)/(-a*d+b*c))^{(1/5)}*\text{hypergeom}([1/5, 3/2], [5/2], -d*(b*x+a)/(-a*d+b*c))/b/(d*x+c)^{(1/5)}$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{2(a+bx)^{3/2} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{3}{2}; \frac{5}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{3b\sqrt[5]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/(c + d*x)^(1/5), x]

[Out] $(2*(a + b*x)^{(3/2)}*((b*(c + d*x))/(b*c - a*d))^{(1/5)}*\text{Hypergeometric2F1}[1/5, 3/2, 5/2, -((d*(a + b*x))/(b*c - a*d))]/(3*b*(c + d*x)^{(1/5)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{\sqrt{a+bx}}{\sqrt[5]{c+dx}} dx = \frac{\sqrt[5]{\frac{b(c+dx)}{bc-ad}} \int \frac{\sqrt{a+bx}}{\sqrt[5]{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}}} dx}{\sqrt[5]{c+dx}}$$

$$= \frac{2(a+bx)^{3/2} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{3}{2}; \frac{5}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{3b\sqrt[5]{c+dx}}$$

Mathematica [A] time = 0.03, size = 73, normalized size = 0.99

$$\frac{2(a+bx)^{3/2} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b\sqrt[5]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(1/5), x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(1/5)*Hypergeometric2F1[1/5, 3/2, 5/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(c + d*x)^(1/5))

fricas [F] time = 4.41, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{5}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/5), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)/(d*x + c)^(1/5), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/5), x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(1/5), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(1/5), x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(1/5), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/5), x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(1/5), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{1/5}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(1/5), x)

[Out] int((a + b*x)^(1/2)/(c + d*x)^(1/5), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a+bx}}{\sqrt[5]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(1/5), x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(1/5), x)

$$3.1733 \quad \int \frac{1}{\sqrt{a+bx} \sqrt[5]{c+dx}} dx$$

Optimal. Leaf size=72

$$\frac{2\sqrt{a+bx} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{1}{2}; \frac{3}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[5]{c+dx}}$$

[Out] $2*(b*(d*x+c)/(-a*d+b*c))^{(1/5)}*\text{hypergeom}([1/5, 1/2], [3/2], -d*(b*x+a)/(-a*d+b*c))*(b*x+a)^{(1/2)}/b/(d*x+c)^{(1/5)}$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{2\sqrt{a+bx} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{1}{2}; \frac{3}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[5]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(1/5)),x]

[Out] $(2*\text{Sqrt}[a + b*x]*((b*(c + d*x))/(b*c - a*d))^{(1/5)}*\text{Hypergeometric2F1}[1/5, 1/2, 3/2, -((d*(a + b*x))/(b*c - a*d))]/(b*(c + d*x)^{(1/5)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{\sqrt{a+bx} \sqrt[5]{c+dx}} dx = \frac{\sqrt[5]{\frac{b(c+dx)}{bc-ad}} \int \frac{1}{\sqrt{a+bx} \sqrt[5]{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}}} dx}{\sqrt[5]{c+dx}}$$

$$= \frac{2\sqrt{a+bx} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{1}{2}; \frac{3}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[5]{c+dx}}$$

Mathematica [A] time = 0.02, size = 71, normalized size = 0.99

$$\frac{2\sqrt{a+bx} \sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{5}, \frac{1}{2}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[5]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(1/5)),x]

[Out] (2*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(1/5)*Hypergeometric2F1[1/5, 1/2, 3/2, (d*(a + b*x))/(-(b*c) + a*d)])/(b*(c + d*x)^(1/5))

fricas [F] time = 5.56, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{4}{5}}}{bdx^2+ac+(bc+ad)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/5),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(4/5)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/5),x, algorithm="giac")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(1/5)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a} (dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(1/5),x)

[Out] int(1/(b*x+a)^(1/2)/(d*x+c)^(1/5),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a} (dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/5),x, algorithm="maxima")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(1/5)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{\sqrt{a+bx} (c+dx)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/2)*(c + d*x)^(1/5)),x)

[Out] int(1/((a + b*x)^(1/2)*(c + d*x)^(1/5)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a+bx} \sqrt[5]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/2)/(d*x+c)**(1/5),x)

[Out] Integral(1/(sqrt(a + b*x)*(c + d*x)**(1/5)), x)

$$3.1734 \quad \int \frac{1}{(a+bx)^{3/2} \sqrt[5]{c+dx}} dx$$

Optimal. Leaf size=72

$$\frac{2\sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{2}, \frac{1}{5}; \frac{1}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt{a+bx} \sqrt[5]{c+dx}}$$

[Out] $-2*(b*(d*x+c)/(-a*d+b*c))^{(1/5)}*\text{hypergeom}([-1/2, 1/5], [1/2], -d*(b*x+a)/(-a*d+b*c))/b/(d*x+c)^{(1/5)}/(b*x+a)^{(1/2)}$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{2\sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{2}, \frac{1}{5}; \frac{1}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt{a+bx} \sqrt[5]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/2)*(c + d*x)^(1/5)), x]

[Out] $(-2*((b*(c + d*x))/(b*c - a*d))^{(1/5)}*\text{Hypergeometric2F1}[-1/2, 1/5, 1/2, -((d*(a + b*x))/(b*c - a*d))]/(b*\text{Sqrt}[a + b*x]*(c + d*x)^{(1/5)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{3/2} \sqrt[5]{c+dx}} dx = \frac{\sqrt[5]{\frac{b(c+dx)}{bc-ad}} \int \frac{1}{(a+bx)^{3/2} \sqrt[5]{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}}} dx}{\sqrt[5]{c+dx}}$$

$$= -\frac{2\sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{2}, \frac{1}{5}, \frac{1}{2}, -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt{a+bx} \sqrt[5]{c+dx}}$$

Mathematica [A] time = 0.02, size = 71, normalized size = 0.99

$$-\frac{2\sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{2}, \frac{1}{5}, \frac{1}{2}, \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt{a+bx} \sqrt[5]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(1/5)), x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(1/5)*Hypergeometric2F1[-1/2, 1/5, 1/2, (d*(a + b*x))/(-b*c + a*d)]/(b*Sqrt[a + b*x]*(c + d*x)^(1/5))

fricas [F] time = 4.86, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{4}{5}}}{b^2dx^3+a^2c+(b^2c+2abd)x^2+(2abc+a^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/5), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(4/5)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/5), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(1/5)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(1/5),x)

[Out] int(1/(b*x+a)^(3/2)/(d*x+c)^(1/5),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/5),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(1/5)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{\frac{3}{2}}(c+dx)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(1/5)),x)

[Out] int(1/((a + b*x)^(3/2)*(c + d*x)^(1/5)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{3}{2}}\sqrt[5]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(1/5),x)

[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(1/5)), x)

$$3.1735 \quad \int \frac{1}{(a+bx)^{5/2} \sqrt[5]{c+dx}} dx$$

Optimal. Leaf size=74

$$\frac{2\sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{3}{2}, \frac{1}{5}; -\frac{1}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{3b(a+bx)^{3/2}\sqrt[5]{c+dx}}$$

[Out] $-2/3*(b*(d*x+c)/(-a*d+b*c))^{(1/5)*\text{hypergeom}([-3/2, 1/5], [-1/2], -d*(b*x+a)/(-a*d+b*c))/b/(b*x+a)^{(3/2)/(d*x+c)^{(1/5)}$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{2\sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{3}{2}, \frac{1}{5}; -\frac{1}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{3b(a+bx)^{3/2}\sqrt[5]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*(c + d*x)^(1/5)),x]

[Out] $(-2*((b*(c + d*x))/(b*c - a*d))^{(1/5)*\text{Hypergeometric2F1}[-3/2, 1/5, -1/2, -(d*(a + b*x))/(b*c - a*d)]})/(3*b*(a + b*x)^{(3/2)*(c + d*x)^{(1/5)}$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{5/2} \sqrt[5]{c+dx}} dx = \frac{\sqrt[5]{\frac{b(c+dx)}{bc-ad}} \int \frac{1}{(a+bx)^{5/2} \sqrt[5]{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}}} dx}{\sqrt[5]{c+dx}}$$

$$= -\frac{2\sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{3}{2}, \frac{1}{5}; -\frac{1}{2}; -\frac{d(a+bx)}{bc-ad}\right)}{3b(a+bx)^{3/2} \sqrt[5]{c+dx}}$$

Mathematica [A] time = 0.02, size = 73, normalized size = 0.99

$$-\frac{2\sqrt[5]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{3}{2}, \frac{1}{5}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a+bx)^{3/2} \sqrt[5]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(1/5)), x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(1/5)*Hypergeometric2F1[-3/2, 1/5, -1/2, (d*(a + b*x))/(-b*c + a*d)])/(3*b*(a + b*x)^(3/2)*(c + d*x)^(1/5))

fricas [F] time = 5.75, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{4}{5}}}{b^3dx^4 + a^3c + (b^3c + 3ab^2d)x^3 + 3(ab^2c + a^2bd)x^2 + (3a^2bc + a^3d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/5), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(4/5)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/5), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(1/5)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(1/5),x)

[Out] int(1/(b*x+a)^(5/2)/(d*x+c)^(1/5),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{1}{5}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/5),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(1/5)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{5/2}(c+dx)^{1/5}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/2)*(c + d*x)^(1/5)),x)

[Out] int(1/((a + b*x)^(5/2)*(c + d*x)^(1/5)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{2}}\sqrt[5]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(1/5),x)

[Out] Integral(1/((a + b*x)**(5/2)*(c + d*x)**(1/5)), x)

3.1736 $\int (a + bx)^{5/2} \sqrt[6]{c + dx} dx$

Optimal. Leaf size=487

$$\frac{81 \cdot 3^{3/4} \sqrt[6]{c + dx} (bc - ad)^{11/3} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} \operatorname{EllipticF} \left(\cos^{-1} \left(\frac{\sqrt[3]{bc - ad}}{\sqrt[3]{bc - ad}} \right) \right)}{2816bd^4 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}$$

[Out] $-9/352(-a*d+b*c)^2*(b*x+a)^{(3/2)}*(d*x+c)^{(1/6)}/b/d^2+3/176*(-a*d+b*c)*(b*x+a)^{(5/2)}*(d*x+c)^{(1/6)}/b/d+3/11*(b*x+a)^{(7/2)}*(d*x+c)^{(1/6)}/b+81/1408*(-a*d+b*c)^3*(d*x+c)^{(1/6)}*(b*x+a)^{(1/2)}/b/d^3-81/2816*3^{(3/4)}*(-a*d+b*c)^{(11/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*\operatorname{EllipticF}((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/b/d^4/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.52, antiderivative size = 487, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 225}

$$\frac{81 \cdot 3^{3/4} \sqrt[6]{c + dx} (bc - ad)^{11/3} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} F \left(\cos^{-1} \left(\frac{\sqrt[3]{bc - ad}}{\sqrt[3]{bc - ad}} \right) \right)}{2816bd^4 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}*(c + d*x)^{(1/6)}, x]$

[Out] $(81*(b*c - a*d)^3*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/6)})/(1408*b*d^3) - (9*(b*c - a*d)^2*(a + b*x)^{(3/2)}*(c + d*x)^{(1/6)})/(352*b*d^2) + (3*(b*c - a*d)*(a + b*x)^{(5/2)}*(c + d*x)^{(1/6)})/(176*b*d) + (3*(a + b*x)^{(7/2)}*(c + d*x)^{(1/6)})/(11*b) - (81*3^{(3/4)}*(b*c - a*d)^{(11/3)}*(c + d*x)^{(1/6)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})*\operatorname{Sqrt}(((b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}))$

$$3)(c + dx)^{1/3} + b^{2/3}(c + dx)^{2/3})/((b^3c - a^3d)^{1/3} - (1 + \sqrt{3})b^{1/3}(c + dx)^{1/3})^2 * \text{EllipticF}[\text{ArcCos}[\frac{(b^3c - a^3d)^{1/3} - (1 + \sqrt{3})b^{1/3}(c + dx)^{1/3}}{(b^3c - a^3d)^{1/3} - (1 + \sqrt{3})b^{1/3}(c + dx)^{1/3}}}], \frac{2 + \sqrt{3}}{4}]/(2816b^4d^4\sqrt{a + bx}\sqrt{-(b^{1/3}(c + dx)^{1/3}((b^3c - a^3d)^{1/3} - b^{1/3}(c + dx)^{1/3}))/((b^3c - a^3d)^{1/3} - (1 + \sqrt{3})b^{1/3}(c + dx)^{1/3})^2})]$$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])]/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rubi steps

$$\begin{aligned}
\int (a+bx)^{5/2} \sqrt[6]{c+dx} \, dx &= \frac{3(a+bx)^{7/2} \sqrt[6]{c+dx}}{11b} + \frac{(bc-ad) \int \frac{(a+bx)^{5/2}}{(c+dx)^{5/6}} \, dx}{22b} \\
&= \frac{3(bc-ad)(a+bx)^{5/2} \sqrt[6]{c+dx}}{176bd} + \frac{3(a+bx)^{7/2} \sqrt[6]{c+dx}}{11b} - \frac{(15(bc-ad)^2) \int \frac{(a+bx)^{3/2}}{(c+dx)^{5/6}} \, dx}{352bd} \\
&= -\frac{9(bc-ad)^2(a+bx)^{3/2} \sqrt[6]{c+dx}}{352bd^2} + \frac{3(bc-ad)(a+bx)^{5/2} \sqrt[6]{c+dx}}{176bd} + \frac{3(a+bx)^{7/2} \sqrt[6]{c+dx}}{11b} \\
&= \frac{81(bc-ad)^3 \sqrt{a+bx} \sqrt[6]{c+dx}}{1408bd^3} - \frac{9(bc-ad)^2(a+bx)^{3/2} \sqrt[6]{c+dx}}{352bd^2} + \frac{3(bc-ad)(a+bx)^{5/2} \sqrt[6]{c+dx}}{176bd} \\
&= \frac{81(bc-ad)^3 \sqrt{a+bx} \sqrt[6]{c+dx}}{1408bd^3} - \frac{9(bc-ad)^2(a+bx)^{3/2} \sqrt[6]{c+dx}}{352bd^2} + \frac{3(bc-ad)(a+bx)^{5/2} \sqrt[6]{c+dx}}{176bd} \\
&= \frac{81(bc-ad)^3 \sqrt{a+bx} \sqrt[6]{c+dx}}{1408bd^3} - \frac{9(bc-ad)^2(a+bx)^{3/2} \sqrt[6]{c+dx}}{352bd^2} + \frac{3(bc-ad)(a+bx)^{5/2} \sqrt[6]{c+dx}}{176bd}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.15

$$\frac{2(a+bx)^{7/2} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{7}{2}; \frac{9}{2}; \frac{d(a+bx)}{ad-bc}\right)}{7b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)*(c + d*x)^(1/6), x]

[Out] (2*(a + b*x)^(7/2)*(c + d*x)^(1/6)*Hypergeometric2F1[-1/6, 7/2, 9/2, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [F] time = 1.22, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(b^2x^2 + 2abx + a^2\right)\sqrt{bx+a}(dx+c)^{\frac{1}{6}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(d*x+c)^(1/6),x, algorithm="fricas")

[Out] integral((b^2*x^2 + 2*a*b*x + a^2)*sqrt(b*x + a)*(d*x + c)^(1/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{2}}(dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(d*x+c)^(1/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/2)*(d*x + c)^(1/6), x)

maple [F] time = 0.15, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{2}}(dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)*(d*x+c)^(1/6),x)

[Out] int((b*x+a)^(5/2)*(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{2}}(dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)*(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/2)*(d*x + c)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{5/2} (c + dx)^{1/6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/2)*(c + d*x)^(1/6),x)

[Out] int((a + b*x)^(5/2)*(c + d*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{5}{2}} \sqrt[6]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(5/2)*(d*x+c)**(1/6),x)
```

```
[Out] Integral((a + b*x)**(5/2)*(c + d*x)**(1/6), x)
```

3.1737 $\int (a + bx)^{3/2} \sqrt[6]{c + dx} dx$

Optimal. Leaf size=449

$$\frac{27 \cdot 3^{3/4} \sqrt[6]{c + dx} (bc - ad)^{8/3} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} \operatorname{EllipticF} \left(\cos^{-1} \left(\frac{\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}}{\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}} \right) \right)}{640bd^3 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}$$

[Out] $\frac{3}{80}(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(1/6)}/b/d+3/8*(b*x+a)^{(5/2)}*(d*x+c)^{(1/6)}/b-27/320*(-a*d+b*c)^2*(d*x+c)^{(1/6)}*(b*x+a)^{(1/2)}/b/d^2+27/640*3^{(3/4)}*(-a*d+b*c)^{(8/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*\operatorname{EllipticF}((1-(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)))/(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/b/d^3/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.34, antiderivative size = 449, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 225}

$$\frac{27 \cdot 3^{3/4} \sqrt[6]{c + dx} (bc - ad)^{8/3} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} F \left(\cos^{-1} \left(\frac{\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}}{\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}} \right) \right)}{640bd^3 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(3/2)}*(c + d*x)^{(1/6)}, x]$

[Out] $(-27*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/6)})/(320*b*d^2) + (3*(b*c - a*d)*(a + b*x)^{(3/2)}*(c + d*x)^{(1/6)})/(80*b*d) + (3*(a + b*x)^{(5/2)}*(c + d*x)^{(1/6)})/(8*b) + (27*3^{(3/4)}*(b*c - a*d)^{(8/3)}*(c + d*x)^{(1/6)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})*\operatorname{Sqrt}[\left((b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)} \right) / \left((b*c - a*d)^{(1/3)} - (1 + \operatorname{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)} \right)^2]*\operatorname{EllipticF}[\operatorname{ArcCos}[\left((b*c - a*d)^{(1/3)} - (1 + \operatorname{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)} \right) / \left((b*c - a*d)^{(1/3)} - (1 + \operatorname{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)} \right)]]$

3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3)), (2 + Sqrt[3])/4]/(640*b*d^3*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)])

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 225

Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x] /; FreeQ[{a, b}, x]

Rubi steps

$$\begin{aligned}
\int (a + bx)^{3/2} \sqrt[6]{c + dx} \, dx &= \frac{3(a + bx)^{5/2} \sqrt[6]{c + dx}}{8b} + \frac{(bc - ad) \int \frac{(a+bx)^{3/2}}{(c+dx)^{5/6}} \, dx}{16b} \\
&= \frac{3(bc - ad)(a + bx)^{3/2} \sqrt[6]{c + dx}}{80bd} + \frac{3(a + bx)^{5/2} \sqrt[6]{c + dx}}{8b} - \frac{(9(bc - ad)^2) \int \frac{\sqrt{a+bx}}{(c+dx)^{5/6}} \, dx}{160bd} \\
&= -\frac{27(bc - ad)^2 \sqrt{a + bx} \sqrt[6]{c + dx}}{320bd^2} + \frac{3(bc - ad)(a + bx)^{3/2} \sqrt[6]{c + dx}}{80bd} + \frac{3(a + bx)^{5/2} \sqrt[6]{c + dx}}{8b} \\
&= -\frac{27(bc - ad)^2 \sqrt{a + bx} \sqrt[6]{c + dx}}{320bd^2} + \frac{3(bc - ad)(a + bx)^{3/2} \sqrt[6]{c + dx}}{80bd} + \frac{3(a + bx)^{5/2} \sqrt[6]{c + dx}}{8b} \\
&= -\frac{27(bc - ad)^2 \sqrt{a + bx} \sqrt[6]{c + dx}}{320bd^2} + \frac{3(bc - ad)(a + bx)^{3/2} \sqrt[6]{c + dx}}{80bd} + \frac{3(a + bx)^{5/2} \sqrt[6]{c + dx}}{8b}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.16

$$\frac{2(a + bx)^{5/2} \sqrt[6]{c + dx} {}_2F_1\left(-\frac{1}{6}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc}\right)}{5b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)*(c + d*x)^(1/6), x]

[Out] (2*(a + b*x)^(5/2)*(c + d*x)^(1/6)*Hypergeometric2F1[-1/6, 5/2, 7/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [F] time = 0.75, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bx + a\right)^{\frac{3}{2}}(dx + c)^{\frac{1}{6}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(1/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)*(d*x + c)^(1/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(1/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)*(d*x + c)^(1/6), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)*(d*x+c)^(1/6),x)

[Out] int((b*x+a)^(3/2)*(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}}(dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)*(d*x + c)^(1/6), x)

mpad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{3/2} (c + dx)^{1/6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)*(c + d*x)^(1/6),x)

[Out] int((a + b*x)^(3/2)*(c + d*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{3}{2}} \sqrt[6]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)*(d*x+c)**(1/6),x)

[Out] Integral((a + b*x)**(3/2)*(c + d*x)**(1/6), x)

3.1738 $\int \sqrt{a + bx} \sqrt[6]{c + dx} dx$

Optimal. Leaf size=411

$$\frac{3 \cdot 3^{3/4} \sqrt[6]{c + dx} (bc - ad)^{5/3} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} \operatorname{EllipticF} \left(\cos^{-1} \left(\frac{\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}}{\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}} \right)} \right)}{40bd^2 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}$$

[Out] $\frac{3}{5} (b*x+a)^{(3/2)} (d*x+c)^{(1/6)} / b + 3/20 * (-a*d+b*c) * (d*x+c)^{(1/6)} * (b*x+a)^{(1/2)} / b/d - 3/40 * 3^{(3/4)} * (-a*d+b*c)^{(5/3)} * (d*x+c)^{(1/6)} * ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)}) * (((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1 - 3^{(1/2)}))^{(2)} / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1 + 3^{(1/2)}))^{(2)})^{(1/2)} / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1 - 3^{(1/2)})) * ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1 + 3^{(1/2)})) * \operatorname{EllipticF}((1 - ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1 - 3^{(1/2)}))^{(2)} / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1 + 3^{(1/2)}))^{(2)})^{(1/2)}, 1/4 * 6^{(1/2)} + 1/4 * 2^{(1/2)}) * (((-a*d+b*c)^{(2/3)} + b^{(1/3)} * (-a*d+b*c)^{(1/3)} * (d*x+c)^{(1/3)} + b^{(2/3)} * (d*x+c)^{(2/3)}) / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1 + 3^{(1/2)}))^{(2)})^{(1/2)} / b/d^2 / (b*x+a)^{(1/2)} / (-b^{(1/3)} * (d*x+c)^{(1/3)} * ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)}) / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1 + 3^{(1/2)}))^{(2)})^{(1/2)}$

Rubi [A] time = 0.28, antiderivative size = 411, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 225}

$$\frac{3 \cdot 3^{3/4} \sqrt[6]{c + dx} (bc - ad)^{5/3} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + (bc - ad)^{2/3} + b^{2/3} (c + dx)^{2/3}}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} F \left(\cos^{-1} \left(\frac{\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}}{\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}} \right)} \right)}{40bd^2 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]*(c + d*x)^(1/6), x]

[Out] $(3*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/6)}) / (20*b*d) + (3*(a + b*x)^{(3/2)} * (c + d*x)^{(1/6)}) / (5*b) - (3*3^{(3/4)} * (b*c - a*d)^{(5/3)} * (c + d*x)^{(1/6)} * ((b*c - a*d)^{(1/3)} - b^{(1/3)} * (c + d*x)^{(1/3)}) * \operatorname{Sqrt}[\left((b*c - a*d)^{(2/3)} + b^{(1/3)} * (b*c - a*d)^{(1/3)} * (c + d*x)^{(1/3)} + b^{(2/3)} * (c + d*x)^{(2/3)} \right) / \left((b*c - a*d)^{(1/3)} - (1 + \operatorname{Sqrt}[3]) * b^{(1/3)} * (c + d*x)^{(1/3)} \right)^2] * \operatorname{EllipticF}[\operatorname{ArcCos}[\left((b*c - a*d)^{(1/3)} - (1 - \operatorname{Sqrt}[3]) * b^{(1/3)} * (c + d*x)^{(1/3)} \right) / \left((b*c - a*d)^{(1/3)} - (1 + \operatorname{Sqrt}[3]) * b^{(1/3)} * (c + d*x)^{(1/3)} \right)^2]])$

$$+ \text{Sqrt}[3]) * b^{(1/3)} * (c + d * x)^{(1/3)}], (2 + \text{Sqrt}[3])/4]/(40 * b * d^2 * \text{Sqrt}[a + b * x] * \text{Sqrt}[-((b^{(1/3)} * (c + d * x)^{(1/3)} * ((b * c - a * d)^{(1/3)} - b^{(1/3)} * (c + d * x)^{(1/3)})) / ((b * c - a * d)^{(1/3)} - (1 + \text{Sqrt}[3]) * b^{(1/3)} * (c + d * x)^{(1/3)})^2)])$$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])]/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rubi steps

$$\begin{aligned}
\int \sqrt{a+bx} \sqrt[6]{c+dx} dx &= \frac{3(a+bx)^{3/2} \sqrt[6]{c+dx}}{5b} + \frac{(bc-ad) \int \frac{\sqrt{a+bx}}{(c+dx)^{5/6}} dx}{10b} \\
&= \frac{3(bc-ad)\sqrt{a+bx} \sqrt[6]{c+dx}}{20bd} + \frac{3(a+bx)^{3/2} \sqrt[6]{c+dx}}{5b} - \frac{(3(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/6}} dx}{40bd} \\
&= \frac{3(bc-ad)\sqrt{a+bx} \sqrt[6]{c+dx}}{20bd} + \frac{3(a+bx)^{3/2} \sqrt[6]{c+dx}}{5b} - \frac{(9(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx}{d}}} \right)}{20bd^2} \\
&= \frac{3(bc-ad)\sqrt{a+bx} \sqrt[6]{c+dx}}{20bd} + \frac{3(a+bx)^{3/2} \sqrt[6]{c+dx}}{5b} - \frac{3 \cdot 3^{3/4} (bc-ad)^{5/3} \sqrt[6]{c+dx} \left(\sqrt[3]{bc-d} \right)}{20bd^2}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.18

$$\frac{2(a+bx)^{3/2} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]*(c + d*x)^(1/6), x]

[Out] (2*(a + b*x)^(3/2)*(c + d*x)^(1/6)*Hypergeometric2F1[-1/6, 3/2, 5/2, (d*(a + b*x))/(-(b*c) + a*d)])/(3*b*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [F] time = 0.64, size = 0, normalized size = 0.00

$$\text{integral}\left(\sqrt{bx+a}(dx+c)^{\frac{1}{6}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(1/6), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx+a}(dx+c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)*(d*x+c)^(1/6),x, algorithm="giac")`

[Out] `integrate(sqrt(b*x + a)*(d*x + c)^(1/6), x)`

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \sqrt{bx + a} (dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(1/2)*(d*x+c)^(1/6),x)`

[Out] `int((b*x+a)^(1/2)*(d*x+c)^(1/6),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx + a} (dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)*(d*x+c)^(1/6),x, algorithm="maxima")`

[Out] `integrate(sqrt(b*x + a)*(d*x + c)^(1/6), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \sqrt{a + bx} (c + dx)^{1/6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/2)*(c + d*x)^(1/6),x)`

[Out] `int((a + b*x)^(1/2)*(c + d*x)^(1/6), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{a + bx} \sqrt[6]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/2)*(d*x+c)**(1/6),x)`

[Out] `Integral(sqrt(a + b*x)*(c + d*x)**(1/6), x)`

$$*d*\text{Sqrt}[a + b*x]*\text{Sqrt}[-(b^{1/3}*(c + d*x)^{1/3}*((b*c - a*d)^{1/3} - b^{1/3}*(c + d*x)^{1/3}))/((b*c - a*d)^{1/3} - (1 + \text{Sqrt}[3])*b^{1/3}*(c + d*x)^{1/3})^2]]$$

Rule 50

$$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + n + 1)), x] + \text{Dist}[(n*(b*c - a*d))/(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$$

$$\text{FreeQ}\{a, b, c, d\}, x\} \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{NeQ}[m + n + 1, 0] \ \&\& \ !(\text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{GtQ}[m, 0] \ \&\& \ \text{LtQ}[m - n, 0]))) \ \&\& \ !\text{ILtQ}[m + n + 2, 0] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$$

Rule 63

$$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /;$$

$$\text{FreeQ}\{a, b, c, d\}, x\} \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[-1, m, 0] \ \&\& \ \text{LeQ}[-1, n, 0] \ \&\& \ \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \ \text{IntLinearQ}[a, b, c, d, m, n, x]$$

Rule 225

$$\text{Int}[1/\text{Sqrt}[(a_.) + (b_.)*(x_.)^6], x_Symbol] \rightarrow \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticF}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])]/(2*3^{1/4}*s*\text{Sqrt}[a + b*x^6]*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]), x]] /;$$

$$\text{FreeQ}\{a, b\}, x]$$

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[6]{c+dx}}{\sqrt{a+bx}} dx &= \frac{3\sqrt{a+bx} \sqrt[6]{c+dx}}{2b} + \frac{(bc-ad) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/6}} dx}{4b} \\
&= \frac{3\sqrt{a+bx} \sqrt[6]{c+dx}}{2b} + \frac{(3(bc-ad)) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{2bd} \\
&= \frac{3\sqrt{a+bx} \sqrt[6]{c+dx}}{2b} + \frac{3^{3/4}(bc-ad)^{2/3} \sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{bc-ad}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt[3]{b}) \sqrt[3]{c+dx} \right)}}}{4bd\sqrt{a+bx} \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt[3]{b}) \sqrt[3]{c+dx} \right)}}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.19

$$\frac{2\sqrt{a+bx} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{1}{2}, \frac{3}{2}, \frac{d(a+bx)}{ad-bc}\right)}{b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/6)/Sqrt[a + b*x], x]

[Out] (2*Sqrt[a + b*x]*(c + d*x)^(1/6)*Hypergeometric2F1[-1/6, 1/2, 3/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [F] time = 0.81, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(dx+c)^{\frac{1}{6}}}{\sqrt{bx+a}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] integral((d*x + c)^(1/6)/sqrt(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{6}}}{\sqrt{bx+a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(1/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/6)/sqrt(b*x + a), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/6)/(b*x+a)^(1/2),x)

[Out] int((d*x+c)^(1/6)/(b*x+a)^(1/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(1/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/6)/sqrt(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/6}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/6)/(a + b*x)^(1/2),x)

[Out] int((c + d*x)^(1/6)/(a + b*x)^(1/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{c + dx}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/6)/(b*x+a)**(1/2),x)

[Out] Integral((c + d*x)**(1/6)/sqrt(a + b*x), x)

$$3.1740 \quad \int \frac{\sqrt[6]{c+dx}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=367

$$\frac{\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right)}{\sqrt[4]{3} b \sqrt{a+bx} \sqrt[3]{bc-ad} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

[Out] $-2*(d*x+c)^{(1/6)}/b/(b*x+a)^{(1/2)}+1/3*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)})*(d*x+c)^{(1/3)}*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*\operatorname{EllipticF}((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3))}/(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}*3^{(3/4)}/b/(-a*d+b*c)^{(1/3)}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3))}/(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.23, antiderivative size = 367, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {47, 63, 225}

$$\frac{\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \frac{1}{4} \left(2 \right)}{\sqrt[4]{3} b \sqrt{a+bx} \sqrt[3]{bc-ad} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(1/6)}/(a + b*x)^{(3/2)}, x]$

[Out] $(-2*(c + d*x)^{(1/6)}/(b*\operatorname{Sqrt}[a + b*x]) + ((c + d*x)^{(1/6)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})*\operatorname{Sqrt}(((b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3))}/((b*c - a*d)^{(1/3)} - (1 + \operatorname{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2)*\operatorname{EllipticF}[\operatorname{ArcCos}(((b*c - a*d)^{(1/3)} - (1 - \operatorname{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3))}/((b*c - a*d)^{(1/3)} - (1 + \operatorname{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})), (2 + \operatorname{Sqrt}[3])/4])/((3^{(1/4)}*b*(b*c - a*d)^{(1/3)}*\operatorname{Sqrt}[a + b*x])$

```
rt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c
+ d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))
^2)])
```

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x] /; FreeQ[{a, b}, x
]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[6]{c+dx}}{(a+bx)^{3/2}} dx &= -\frac{2\sqrt[6]{c+dx}}{b\sqrt{a+bx}} + \frac{d \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/6}} dx}{3b} \\
&= -\frac{2\sqrt[6]{c+dx}}{b\sqrt{a+bx}} + \frac{2 \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{b} \\
&= -\frac{2\sqrt[6]{c+dx}}{b\sqrt{a+bx}} + \frac{\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{bc-ad} \sqrt[3]{c+dx} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F\left(c\right)}{\sqrt[4]{3} b \sqrt[3]{bc-ad} \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 71, normalized size = 0.19

$$-\frac{2\sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{2}, -\frac{1}{6}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt{a+bx} \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/6)/(a + b*x)^(3/2), x]

[Out] (-2*(c + d*x)^(1/6)*Hypergeometric2F1[-1/2, -1/6, 1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [F] time = 0.65, size = 0, normalized size = 0.00

$$\operatorname{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{1}{6}}}{b^2x^2 + 2abx + a^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(3/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/6)/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{6}}}{(bx+a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(3/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/6)/(b*x + a)^(3/2), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/6)/(b*x+a)^(3/2),x)

[Out] int((d*x+c)^(1/6)/(b*x+a)^(3/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(3/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/6)/(b*x + a)^(3/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/6}}{(a + bx)^{3/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/6)/(a + b*x)^(3/2),x)

[Out] int((c + d*x)^(1/6)/(a + b*x)^(3/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{c + dx}}{(a + bx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/6)/(b*x+a)**(3/2),x)

[Out] Integral((c + d*x)**(1/6)/(a + b*x)**(3/2), x)

$$3.1741 \quad \int \frac{\sqrt[6]{c+dx}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=409

$$\frac{2d\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right)} \right)}{9\sqrt[4]{3} b \sqrt{a+bx} (bc-ad)^{4/3} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

[Out] $-2/3*(d*x+c)^{(1/6)}/b/(b*x+a)^{(3/2)}-2/9*d*(d*x+c)^{(1/6)}/b/(-a*d+b*c)/(b*x+a)^{(1/2)}-2/27*d*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2*\operatorname{EllipticF}((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}*3^{(3/4)}/b/(-a*d+b*c)^{(4/3)}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.28, antiderivative size = 409, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {47, 51, 63, 225}

$$\frac{2d\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right)} \right)}{9\sqrt[4]{3} b \sqrt{a+bx} (bc-ad)^{4/3} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(1/6)}/(a + b*x)^{(5/2)}, x]$

[Out] $(-2*(c + d*x)^{(1/6)})/(3*b*(a + b*x)^{(3/2)}) - (2*d*(c + d*x)^{(1/6)})/(9*b*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]) - (2*d*(c + d*x)^{(1/6)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})*\operatorname{Sqrt}[(b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)})/((b*c - a*d)^{(1/3)} - (1 + \operatorname{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2]*\operatorname{EllipticF}[\operatorname{ArcCos}[(b*c - a*d)^{(1/3)} - (1 - \operatorname{Sqrt}[3]$

```

])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c +
d*x)^(1/3)), (2 + Sqrt[3])/4)]/(9*3^(1/4)*b*(b*c - a*d)^(4/3)*Sqrt[a + b*
x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(
1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)])

```

Rule 47

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]

```

Rule 51

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]

```

Rule 63

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 225

```

Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4)]/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x] /; FreeQ[{a, b}, x
]

```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[6]{c+dx}}{(a+bx)^{5/2}} dx &= -\frac{2\sqrt[6]{c+dx}}{3b(a+bx)^{3/2}} + \frac{d \int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/6}} dx}{9b} \\
&= -\frac{2\sqrt[6]{c+dx}}{3b(a+bx)^{3/2}} - \frac{2d\sqrt[6]{c+dx}}{9b(bc-ad)\sqrt{a+bx}} - \frac{(2d^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/6}} dx}{27b(bc-ad)} \\
&= -\frac{2\sqrt[6]{c+dx}}{3b(a+bx)^{3/2}} - \frac{2d\sqrt[6]{c+dx}}{9b(bc-ad)\sqrt{a+bx}} - \frac{(4d) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{9b(bc-ad)} \\
&= -\frac{2\sqrt[6]{c+dx}}{3b(a+bx)^{3/2}} - \frac{2d\sqrt[6]{c+dx}}{9b(bc-ad)\sqrt{a+bx}} - \frac{2d\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b}}{\sqrt[3]{bc-ad}}}}{9^4 \sqrt[3]{b} (bc-ad)^{4/3} \sqrt{\dots}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.18

$$-\frac{2\sqrt[6]{c+dx} {}_2F_1\left(-\frac{3}{2}, -\frac{1}{6}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a+bx)^{3/2} \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/6)/(a + b*x)^(5/2), x]

[Out] (-2*(c + d*x)^(1/6)*Hypergeometric2F1[-3/2, -1/6, -1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [F] time = 0.85, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{1}{6}}}{b^3 x^3 + 3ab^2 x^2 + 3a^2 bx + a^3}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(5/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/6)/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(5/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/6)/(b*x + a)^(5/2), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/6)/(b*x+a)^(5/2),x)

[Out] int((d*x+c)^(1/6)/(b*x+a)^(5/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/6)/(b*x + a)^(5/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/6}}{(a + bx)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/6)/(a + b*x)^(5/2),x)

[Out] int((c + d*x)^(1/6)/(a + b*x)^(5/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{c + dx}}{(a + bx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/6)/(b*x+a)**(5/2),x)

[Out] Integral((c + d*x)**(1/6)/(a + b*x)**(5/2), x)

3.1742 $\int (a + bx)^{3/2} (c + dx)^{5/6} dx$

Optimal. Leaf size=896

$$\frac{81 \sqrt[4]{3} \sqrt[6]{c + dx} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{(bc - ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{c + dx} \sqrt[3]{bc - ad} + b^{2/3} (c + dx)^{2/3}}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}} E \left(\cos^{-1} \left(\frac{\sqrt[3]{bc - ad} - (1 - \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}}{\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx}} \right) \right)}{448 b^{5/3} d^3 \sqrt{a + bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c + dx} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right)}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}$$

[Out] $\frac{3}{28} (-a*d+b*c) * (b*x+a)^{(3/2)} * (d*x+c)^{(5/6)} / b/d + \frac{3}{10} (b*x+a)^{(5/2)} * (d*x+c)^{(5/6)} / b - \frac{27}{224} (-a*d+b*c)^2 * (d*x+c)^{(5/6)} * (b*x+a)^{(1/2)} / b/d^2 - \frac{81}{448} (-a*d+b*c)^3 * (d*x+c)^{(1/6)} * (1+3^{(1/2)}) * (b*x+a)^{(1/2)} / b^{(5/3)} / d^2 / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)})) - \frac{81}{448} 3^{(1/4)} * (-a*d+b*c)^{(10/3)} * (d*x+c)^{(1/6)} * ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)}) * (((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1-3^{(1/2)}))^{-2} / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)}))^{-2})^{(1/2)} / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1-3^{(1/2)})) * ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)})) * \text{EllipticE}((1 - ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1-3^{(1/2)}))^{-2} / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)}))^{-2})^{(1/2)}, 1/4 * 6^{(1/2)} + 1/4 * 2^{(1/2)}) * (((-a*d+b*c)^{(2/3)} + b^{(1/3)} * (-a*d+b*c)^{(1/3)} * (d*x+c)^{(1/3)} + b^{(2/3)} * (d*x+c)^{(2/3)}) / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)}))^{-2})^{(1/2)} / b^{(5/3)} / d^3 / (b*x+a)^{(1/2)} / (-b^{(1/3)} * (d*x+c)^{(1/3)} * ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)}) / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)}))^{-2})^{(1/2)} - \frac{27}{896} 3^{(3/4)} * (-a*d+b*c)^{(10/3)} * (d*x+c)^{(1/6)} * ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)}) * (((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1-3^{(1/2)}))^{-2} / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)}))^{-2})^{(1/2)} / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1-3^{(1/2)})) * ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)})) * \text{EllipticF}((1 - ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1-3^{(1/2)}))^{-2} / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)}))^{-2})^{(1/2)}, 1/4 * 6^{(1/2)} + 1/4 * 2^{(1/2)}) * (1-3^{(1/2)}) * (((-a*d+b*c)^{(2/3)} + b^{(1/3)} * (-a*d+b*c)^{(1/3)} * (d*x+c)^{(1/3)} + b^{(2/3)} * (d*x+c)^{(2/3)}) / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)}))^{-2})^{(1/2)} / b^{(5/3)} / d^3 / (b*x+a)^{(1/2)} / (-b^{(1/3)} * (d*x+c)^{(1/3)} * ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)}) / ((-a*d+b*c)^{(1/3)} - b^{(1/3)} * (d*x+c)^{(1/3)} * (1+3^{(1/2)}))^{-2})^{(1/2)}$

Rubi [A] time = 1.08, antiderivative size = 896, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {50, 63, 308, 225, 1881}

$$81\sqrt[4]{3}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad}-(1-\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)$$

$$448b^{5/3}d^3\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)*(c + d*x)^(5/6), x]

[Out] (-27*(b*c - a*d)^2*Sqrt[a + b*x]*(c + d*x)^(5/6))/(224*b*d^2) + (3*(b*c - a*d)*(a + b*x)^(3/2)*(c + d*x)^(5/6))/(28*b*d) + (3*(a + b*x)^(5/2)*(c + d*x)^(5/6))/(10*b) - (81*(1 + Sqrt[3])*(b*c - a*d)^3*Sqrt[a + b*x]*(c + d*x)^(1/6))/(448*b^(5/3)*d^2*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) - (81*3^(1/4)*(b*c - a*d)^(10/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(448*b^(5/3)*d^3*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)] - (27*3^(3/4)*(1 - Sqrt[3])*(b*c - a*d)^(10/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(896*b^(5/3)*d^3*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
```

$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 225

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^6], x_Symbol] :> \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticF}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*3^{(1/4)}*s*\text{Sqrt}[a + b*x^6]*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]), x]] /; \text{FreeQ}\{a, b\}, x]$

Rule 308

$\text{Int}[(x_)^4/\text{Sqrt}[(a_) + (b_)*(x_)^6], x_Symbol] :> \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[3] - 1)*s^2/(2*r^2), \text{Int}[1/\text{Sqrt}[a + b*x^6], x], x] - \text{Dist}[1/(2*r^2), \text{Int}[(\text{Sqrt}[3] - 1)*s^2 - 2*r^2*x^4]/\text{Sqrt}[a + b*x^6], x], x]] /; \text{FreeQ}\{a, b\}, x]$

Rule 1881

$\text{Int}[(c_) + (d_)*(x_)^4/\text{Sqrt}[(a_) + (b_)*(x_)^6], x_Symbol] :> \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(1 + \text{Sqrt}[3])*d*s^3*x*\text{Sqrt}[a + b*x^6]/(2*a*r^2*(s + (1 + \text{Sqrt}[3])*r*x^2)), x] - \text{Simp}[(3^{(1/4)}*d*s*x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticE}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*r^2*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{Sqrt}[a + b*x^6]), x]] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{EqQ}[2*\text{Rt}[b/a, 3]^2*c - (1 - \text{Sqrt}[3])*d, 0]$

Rubi steps

$$\begin{aligned}
\int (a + bx)^{3/2} (c + dx)^{5/6} dx &= \frac{3(a + bx)^{5/2} (c + dx)^{5/6}}{10b} + \frac{(bc - ad) \int \frac{(a+bx)^{3/2}}{\sqrt[6]{c+dx}} dx}{4b} \\
&= \frac{3(bc - ad)(a + bx)^{3/2} (c + dx)^{5/6}}{28bd} + \frac{3(a + bx)^{5/2} (c + dx)^{5/6}}{10b} - \frac{(9(bc - ad)^2) \int \frac{\sqrt{a+bx}}{\sqrt[6]{c+dx}} dx}{56bd} \\
&= -\frac{27(bc - ad)^2 \sqrt{a + bx} (c + dx)^{5/6}}{224bd^2} + \frac{3(bc - ad)(a + bx)^{3/2} (c + dx)^{5/6}}{28bd} + \frac{3(a + bx)^{5/2} (c + dx)^{5/6}}{10b} \\
&= -\frac{27(bc - ad)^2 \sqrt{a + bx} (c + dx)^{5/6}}{224bd^2} + \frac{3(bc - ad)(a + bx)^{3/2} (c + dx)^{5/6}}{28bd} + \frac{3(a + bx)^{5/2} (c + dx)^{5/6}}{10b} \\
&= -\frac{27(bc - ad)^2 \sqrt{a + bx} (c + dx)^{5/6}}{224bd^2} + \frac{3(bc - ad)(a + bx)^{3/2} (c + dx)^{5/6}}{28bd} + \frac{3(a + bx)^{5/2} (c + dx)^{5/6}}{10b} \\
&= -\frac{27(bc - ad)^2 \sqrt{a + bx} (c + dx)^{5/6}}{224bd^2} + \frac{3(bc - ad)(a + bx)^{3/2} (c + dx)^{5/6}}{28bd} + \frac{3(a + bx)^{5/2} (c + dx)^{5/6}}{10b}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.08

$$\frac{2(a + bx)^{5/2} (c + dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, \frac{5}{2}, \frac{7}{2}, \frac{d(a+bx)}{ad-bc}\right)}{5b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)*(c + d*x)^(5/6), x]

[Out] (2*(a + b*x)^(5/2)*(c + d*x)^(5/6)*Hypergeometric2F1[-5/6, 5/2, 7/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*((b*(c + d*x))/(b*c - a*d))^(5/6))

fricas [F] time = 1.04, size = 0, normalized size = 0.00

$$\text{integral}\left((bx + a)^{\frac{3}{2}}(dx + c)^{\frac{5}{6}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(5/6),x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)*(d*x + c)^(5/6), x)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(5/6),x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}} (dx + c)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)*(d*x+c)^(5/6),x)

[Out] int((b*x+a)^(3/2)*(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{3}{2}} (dx + c)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)*(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)*(d*x + c)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{3/2} (c + dx)^{5/6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)*(c + d*x)^(5/6),x)

[Out] int((a + b*x)^(3/2)*(c + d*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{3}{2}} (c + dx)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)*(d*x+c)**(5/6),x)

[Out] Integral((a + b*x)**(3/2)*(c + d*x)**(5/6), x)

3.1743 $\int \sqrt{a + bx} (c + dx)^{5/6} dx$

Optimal. Leaf size=858

$$\frac{45 \sqrt[4]{3} \sqrt[6]{c + dx} (\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx}) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + b^{2/3} (c+dx)^{2/3}}{(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})^2}} E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}\right)\right)}{112b^{5/3}d^2\sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})^2}}}$$

[Out] $\frac{3}{7} (b*x+a)^{3/2} (d*x+c)^{5/6} / b + 15/56 (-a*d+b*c) (d*x+c)^{5/6} (b*x+a)^{1/2} / (b/d + 45/112 (-a*d+b*c)^2 (d*x+c)^{1/6} (1+3^{1/2}) (b*x+a)^{1/2} / b^{5/3} / d / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2}))) + 45/112 3^{1/4} (-a*d+b*c)^{7/3} (d*x+c)^{1/6} ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) (((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1-3^{1/2})))^2 / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2}))^2)^{1/2} / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1-3^{1/2})) * ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2})) * \text{EllipticE}((1 - ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1-3^{1/2})))^2 / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2})))^2)^{1/2}, 1/4 * 6^{1/2} + 1/4 * 2^{1/2}) * (((-a*d+b*c)^{2/3} + b^{1/3} (-a*d+b*c)^{1/3} (d*x+c)^{1/3} + b^{2/3} (d*x+c)^{2/3})) / (((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2}))^2)^{1/2} / b^{5/3} / d^2 / (b*x+a)^{1/2} / (-b^{1/3} (d*x+c)^{1/3} ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3})) / (((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2}))^2)^{1/2} + 15/224 * 3^{3/4} (-a*d+b*c)^{7/3} (d*x+c)^{1/6} ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) * (((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1-3^{1/2})))^2 / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2}))^2)^{1/2} / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1-3^{1/2})) * ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2})) * \text{EllipticF}((1 - ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1-3^{1/2})))^2 / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2}))^2)^{1/2}, 1/4 * 6^{1/2} + 1/4 * 2^{1/2}) * (1-3^{1/2}) * (((-a*d+b*c)^{2/3} + b^{1/3} (-a*d+b*c)^{1/3} (d*x+c)^{1/3} + b^{2/3} (d*x+c)^{2/3})) / (((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2}))^2)^{1/2} / b^{5/3} / d^2 / (b*x+a)^{1/2} / (-b^{1/3} (d*x+c)^{1/3} ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3})) / (((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3} (1+3^{1/2}))^2)^{1/2}$

Rubi [A] time = 0.82, antiderivative size = 858, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {50, 63, 308, 225, 1881}

$$\frac{45\sqrt[4]{3}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad}-(1-\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)}{112b^{5/3}d^2\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]*(c + d*x)^(5/6), x]

[Out] (15*(b*c - a*d)*Sqrt[a + b*x]*(c + d*x)^(5/6))/(56*b*d) + (3*(a + b*x)^(3/2)*(c + d*x)^(5/6))/(7*b) + (45*(1 + Sqrt[3])*(b*c - a*d)^2*Sqrt[a + b*x]*(c + d*x)^(1/6))/(112*b^(5/3)*d*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) + (45*3^(1/4)*(b*c - a*d)^(7/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(112*b^(5/3)*d^2*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)]) + (15*3^(3/4)*(1 - Sqrt[3])*(b*c - a*d)^(7/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(224*b^(5/3)*d^2*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)])

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ

$[b*c - a*d, 0] \ \&\& \text{LtQ}[-1, m, 0] \ \&\& \text{LeQ}[-1, n, 0] \ \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 225

$\text{Int}[1/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \ :> \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticF}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*3^{1/4}*s*\text{Sqrt}[a + b*x^6]*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]), x]] \ /; \text{FreeQ}\{\{a, b\}, x\}$

Rule 308

$\text{Int}[(x_)^4/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \ :> \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[3] - 1)*s^2/(2*r^2), \text{Int}[1/\text{Sqrt}[a + b*x^6], x], x] - \text{Dist}[1/(2*r^2), \text{Int}[(\text{Sqrt}[3] - 1)*s^2 - 2*r^2*x^4]/\text{Sqrt}[a + b*x^6], x], x]] \ /; \text{FreeQ}\{\{a, b\}, x\}$

Rule 1881

$\text{Int}[(c_) + (d_.)*(x_)^4/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \ :> \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(\text{Sqrt}[3] + 1)*d*s^3*x*\text{Sqrt}[a + b*x^6]/(2*a*r^2*(s + (1 + \text{Sqrt}[3])*r*x^2)), x] - \text{Simp}[(3^{1/4}*d*s*x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticE}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*r^2*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{Sqrt}[a + b*x^6]), x]] \ /; \text{FreeQ}\{\{a, b, c, d\}, x\} \ \&\& \text{EqQ}[2*\text{Rt}[b/a, 3]^2*c - (1 - \text{Sqrt}[3])*d, 0]$

Rubi steps

$$\begin{aligned}
\int \sqrt{a+bx} (c+dx)^{5/6} dx &= \frac{3(a+bx)^{3/2}(c+dx)^{5/6}}{7b} + \frac{(5(bc-ad)) \int \frac{\sqrt{a+bx}}{\sqrt[6]{c+dx}} dx}{14b} \\
&= \frac{15(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56bd} + \frac{3(a+bx)^{3/2}(c+dx)^{5/6}}{7b} - \frac{(15(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}\sqrt[6]{c+dx}} dx}{112bd} \\
&= \frac{15(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56bd} + \frac{3(a+bx)^{3/2}(c+dx)^{5/6}}{7b} - \frac{(45(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{a+bx}\sqrt[6]{c+dx}} dx \right)}{56bd} \\
&= \frac{15(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56bd} + \frac{3(a+bx)^{3/2}(c+dx)^{5/6}}{7b} + \frac{(45(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{a+bx}\sqrt[6]{c+dx}} dx \right)}{56bd} \\
&= \frac{15(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56bd} + \frac{3(a+bx)^{3/2}(c+dx)^{5/6}}{7b} + \frac{45(1+\sqrt{3})(bc-ad)^2}{112b^{5/3}d(\sqrt[3]{bc-ad} - (1+\sqrt{3}))}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.09

$$\frac{2(a+bx)^{3/2}(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b\left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]*(c + d*x)^(5/6), x]

[Out] (2*(a + b*x)^(3/2)*(c + d*x)^(5/6)*Hypergeometric2F1[-5/6, 3/2, 5/2, (d*(a + b*x))/(-b*c) + a*d])/(3*b*((b*(c + d*x))/(b*c - a*d))^(5/6))

fricas [F] time = 0.92, size = 0, normalized size = 0.00

$$\text{integral}\left(\sqrt{bx+a}(dx+c)^{\frac{5}{6}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(5/6), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/6), x)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(5/6), x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \sqrt{bx + a} (dx + c)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)*(d*x+c)^(5/6), x)

[Out] int((b*x+a)^(1/2)*(d*x+c)^(5/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{bx + a} (dx + c)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)*(d*x+c)^(5/6), x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)*(d*x + c)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \sqrt{a + bx} (c + dx)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)*(c + d*x)^(5/6), x)

[Out] int((a + b*x)^(1/2)*(c + d*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt{a + bx} (c + dx)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(1/2)*(d*x+c)**(5/6),x)
```

```
[Out] Integral(sqrt(a + b*x)*(c + d*x)**(5/6), x)
```

$$3.1744 \quad \int \frac{(c+dx)^{5/6}}{\sqrt{a+bx}} dx$$

Optimal. Leaf size=817

$$\frac{15\sqrt[4]{3}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad}-(1-\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)}{8b^{5/3}d\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

[Out] $3/4*(d*x+c)^{(5/6)}*(b*x+a)^{(1/2)}/b-15/8*(-a*d+b*c)*(d*x+c)^{(1/6)}*(1+3^{(1/2)})$
 $* (b*x+a)^{(1/2)}/b^{(5/3)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))$
 $-15/8*3^{(1/4)}*(-a*d+b*c)^{(4/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x$
 $+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2/((-a*d+b$
 $*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2})^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{($
 $1/3)* (d*x+c)^{(1/3)}*(1+3^{(1/2)})))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))$
 $*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2})^{(1/2)}, 1/4*6^{(1/2)}$
 $+1/4*2^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}$
 $*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2})^{(1/2)}/b^{(5/3)}/d/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2})^{(1/2)}-5/16*3^{(3/4)}*(-a*d+b*c)^{(4/3)}*(d*x+c)^{(1/6)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2})^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2})^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})* (1+3^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2})^{(1/2)}/b^{(5/3)}/d/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2})^{(1/2)}$

Rubi [A] time = 0.71, antiderivative size = 817, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {50, 63, 308, 225, 1881}

$$15\sqrt[4]{3}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad}-(1-\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)$$

$$8b^{5/3}d\sqrt{a+bx}\sqrt{\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/6)/Sqrt[a + b*x], x]

[Out] (3*Sqrt[a + b*x]*(c + d*x)^(5/6))/(4*b) - (15*(1 + Sqrt[3])*(b*c - a*d)*Sqrt[a + b*x]*(c + d*x)^(1/6))/(8*b^(5/3)*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) - (15*3^(1/4)*(b*c - a*d)^(4/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(8*b^(5/3)*d*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)]) - (5*3^(3/4)*(1 - Sqrt[3])*(b*c - a*d)^(4/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(16*b^(5/3)*d*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)])

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
```


ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rule 308

```
Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a,
3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a
+ b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqr
t[a + b*x^6], x], x]] /; FreeQ[{a, b}, x]
```

Rule 1881

```
Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r =
Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqr
t[a + b*x^6])/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x
*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*El
lipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + S
qrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sq
rt[a + b*x^6]), x]] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1
- Sqrt[3])*d, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/6}}{\sqrt{a+bx}} dx &= \frac{3\sqrt{a+bx}(c+dx)^{5/6}}{4b} + \frac{(5(bc-ad)) \int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx}{8b} \\
&= \frac{3\sqrt{a+bx}(c+dx)^{5/6}}{4b} + \frac{(15(bc-ad)) \text{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{4bd} \\
&= \frac{3\sqrt{a+bx}(c+dx)^{5/6}}{4b} - \frac{(15(bc-ad)) \text{Subst} \left(\int \frac{(-1+\sqrt{3})(bc-ad)^{2/3}-2b^{2/3}x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{8b^{5/3}d} \quad (15 (\\
&= \frac{3\sqrt{a+bx}(c+dx)^{5/6}}{4b} - \frac{15(1+\sqrt{3})(bc-ad)\sqrt{a+bx} \sqrt[6]{c+dx}}{8b^{5/3} \left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)} - \frac{15\sqrt[4]{3}(bc-ad)^{4/3} \sqrt[6]{c+dx}}{8b^{5/3} \left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.09

$$\frac{2\sqrt{a+bx}(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, \frac{1}{2}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/6)/Sqrt[a + b*x], x]

[Out] (2*Sqrt[a + b*x]*(c + d*x)^(5/6)*Hypergeometric2F1[-5/6, 1/2, 3/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*((b*(c + d*x))/(b*c - a*d))^(5/6))

fricas [F] time = 1.18, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(dx+c)^{\frac{5}{6}}}{\sqrt{bx+a}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(1/2), x, algorithm="fricas")

[Out] `integral((d*x + c)^(5/6)/sqrt(b*x + a), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(5/6)/(b*x+a)^(1/2),x, algorithm="giac")`

[Out] `integrate((d*x + c)^(5/6)/sqrt(b*x + a), x)`

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(5/6)/(b*x+a)^(1/2),x)`

[Out] `int((d*x+c)^(5/6)/(b*x+a)^(1/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{\sqrt{bx + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(5/6)/(b*x+a)^(1/2),x, algorithm="maxima")`

[Out] `integrate((d*x + c)^(5/6)/sqrt(b*x + a), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{\frac{5}{6}}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(5/6)/(a + b*x)^(1/2),x)`

[Out] `int((c + d*x)^(5/6)/(a + b*x)^(1/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{6}}}{\sqrt{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/6)/(b*x+a)**(1/2),x)

[Out] Integral((c + d*x)**(5/6)/sqrt(a + b*x), x)

$$3.1745 \quad \int \frac{(c+dx)^{5/6}}{(a+bx)^{3/2}} dx$$

Optimal. Leaf size=798

$$\frac{5(1+\sqrt{3})\sqrt{a+bx}\sqrt[6]{c+dx}d}{b^{5/3}(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} \frac{5\sqrt[4]{3}\sqrt[3]{bc-ad}\sqrt[6]{c+dx}(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx})}{\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c}}{(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx})}}}$$

[Out] $-2*(d*x+c)^{(5/6)}/b/(b*x+a)^{(1/2)}-5*d*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/b^{(5/3)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))-5*3^{(1/4)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/b^{(5/3)}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}-5/6*(a*d+b*c)^{(1/3)}*(d*x+c)^{(1/6)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticF(((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)}))*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}*3^{(3/4)}/b^{(5/3)}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.68, antiderivative size = 798, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {47, 63, 308, 225, 1881}

$$\frac{5(1 + \sqrt{3})\sqrt{a + bx}\sqrt[6]{c + dx}d}{b^{5/3}(\sqrt[3]{bc - ad} - (1 + \sqrt{3})\sqrt[3]{b}\sqrt[3]{c + dx})} - \frac{5\sqrt[4]{3}\sqrt[3]{bc - ad}\sqrt[6]{c + dx}(\sqrt[3]{bc - ad} - \sqrt[3]{b}\sqrt[3]{c + dx})}{\sqrt{\frac{(bc - ad)^{2/3} + \sqrt[3]{b}\sqrt[3]{c + ad}}{(\sqrt[3]{bc - ad} - (1 + \sqrt{3})\sqrt[3]{b}\sqrt[3]{c + dx})}}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/6)/(a + b*x)^(3/2), x]

[Out] (-2*(c + d*x)^(5/6))/(b*Sqrt[a + b*x]) - (5*(1 + Sqrt[3])*d*Sqrt[a + b*x]*(c + d*x)^(1/6))/(b^(5/3)*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) - (5*3^(1/4)*(b*c - a*d)^(1/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(b^(5/3)*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)]) - (5*(1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(2*3^(1/4)*b^(5/3)*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)])

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(IleQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rule 308

```
Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a,
3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a
+ b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqr
t[a + b*x^6], x], x]] /; FreeQ[{a, b}, x]
```

Rule 1881

```
Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r =
Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqr
t[a + b*x^6])/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x
*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*El
lipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + S
qrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sq
rt[a + b*x^6]), x]] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1
- Sqrt[3])*d, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/6}}{(a+bx)^{3/2}} dx &= -\frac{2(c+dx)^{5/6}}{b\sqrt{a+bx}} + \frac{(5d) \int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx}{3b} \\
&= -\frac{2(c+dx)^{5/6}}{b\sqrt{a+bx}} + \frac{10 \text{ Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{b} \\
&= -\frac{2(c+dx)^{5/6}}{b\sqrt{a+bx}} - \frac{5 \text{ Subst} \left(\int \frac{(-1+\sqrt{3})(bc-ad)^{2/3}-2b^{2/3}x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{b^{5/3}} - \frac{(5(1-\sqrt{3})(bc-ad)^{2/3})}{5\sqrt[4]{3} \sqrt[3]{bc-ad} \sqrt[6]{c+dx} (\sqrt[3]{bc-ad})} \\
&= -\frac{2(c+dx)^{5/6}}{b\sqrt{a+bx}} - \frac{5(1+\sqrt{3})d\sqrt{a+bx} \sqrt[6]{c+dx}}{b^{5/3} (\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.09

$$-\frac{2(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, -\frac{1}{2}, \frac{1}{2}, \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/6)/(a + b*x)^(3/2), x]

[Out] (-2*(c + d*x)^(5/6)*Hypergeometric2F1[-5/6, -1/2, 1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(b*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(5/6))

fricas [F] time = 1.42, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{5/6}}{b^2x^2 + 2abx + a^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(3/2), x, algorithm="fricas")

[Out] `integral(sqrt(b*x + a)*(d*x + c)^(5/6)/(b^2*x^2 + 2*a*b*x + a^2), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(5/6)/(b*x+a)^(3/2),x, algorithm="giac")`

[Out] `integrate((d*x + c)^(5/6)/(b*x + a)^(3/2), x)`

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(5/6)/(b*x+a)^(3/2),x)`

[Out] `int((d*x+c)^(5/6)/(b*x+a)^(3/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(5/6)/(b*x+a)^(3/2),x, algorithm="maxima")`

[Out] `integrate((d*x + c)^(5/6)/(b*x + a)^(3/2), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{\frac{5}{6}}}{(a + bx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(5/6)/(a + b*x)^(3/2),x)`

[Out] `int((c + d*x)^(5/6)/(a + b*x)^(3/2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{6}}}{(a + bx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/6)/(b*x+a)**(3/2),x)

[Out] Integral((c + d*x)**(5/6)/(a + b*x)**(3/2), x)

$$3.1746 \quad \int \frac{(c+dx)^{5/6}}{(a+bx)^{5/2}} dx$$

Optimal. Leaf size=854

$$\frac{10(1+\sqrt{3})\sqrt{a+bx}\sqrt[6]{c+dx}d^2}{9b^{5/3}(bc-ad)\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)} \frac{10\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}}{3^{3/4}b^{5/3}(bc-ad)^{2/3}\sqrt{a}}$$

[Out] $-2/3*(d*x+c)^{(5/6)}/b/(b*x+a)^{(3/2)}-10/9*d*(d*x+c)^{(5/6)}/b/(-a*d+b*c)/(b*x+a)^{(1/2)}-10/9*d^2*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/b^{(5/3)}/(-a*d+b*c)/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))-10/9*d*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*3^{(1/4)}/b^{(5/3)}/(-a*d+b*c)^{(2/3)}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}-5/27*d*(d*x+c)^{(1/6)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)})*((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*3^{(3/4)}/b^{(5/3)}/(-a*d+b*c)^{(2/3)}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.80, antiderivative size = 854, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {47, 51, 63, 308, 225, 1881}

$$\frac{10(1 + \sqrt{3})\sqrt{a + bx}\sqrt[6]{c + dx}d^2}{9b^{5/3}(bc - ad)\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3})\sqrt[3]{b}\sqrt[3]{c + dx}\right)} \cdot \frac{10\sqrt[6]{c + dx}\left(\sqrt[3]{bc - ad} - \sqrt[3]{b}\sqrt[3]{c + dx}\right)\sqrt{\frac{(bc - ad)^{2/3} + \sqrt[3]{b}\sqrt[3]{c + dx}}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3})\sqrt[3]{b}\sqrt[3]{c + dx}\right)}}}{3 \cdot 3^{3/4}b^{5/3}(bc - ad)^{2/3}\sqrt{a + bx}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/6)/(a + b*x)^(5/2), x]

[Out] (-2*(c + d*x)^(5/6))/(3*b*(a + b*x)^(3/2)) - (10*d*(c + d*x)^(5/6))/(9*b*(b*c - a*d)*Sqrt[a + b*x]) - (10*(1 + Sqrt[3])*d^2*Sqrt[a + b*x]*(c + d*x)^(1/6))/(9*b^(5/3)*(b*c - a*d)*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) - (10*d*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(3*3^(3/4)*b^(5/3)*(b*c - a*d)^(2/3)*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)]) - (5*(1 - Sqrt[3])*d*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(9*3^(1/4)*b^(5/3)*(b*c - a*d)^(2/3)*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)])

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) & IntLinearQ[a, b, c, d, m, n, x]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x]

```
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x]
```

Rule 308

```
Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a + b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqrt[a + b*x^6], x], x]] /; FreeQ[{a, b}, x]
```

Rule 1881

```
Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqrt[a + b*x^6])/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sqrt[a + b*x^6]), x]] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1 - Sqrt[3])*d, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/6}}{(a+bx)^{5/2}} dx &= -\frac{2(c+dx)^{5/6}}{3b(a+bx)^{3/2}} + \frac{(5d) \int \frac{1}{(a+bx)^{3/2} \sqrt[6]{c+dx}} dx}{9b} \\
&= -\frac{2(c+dx)^{5/6}}{3b(a+bx)^{3/2}} - \frac{10d(c+dx)^{5/6}}{9b(bc-ad)\sqrt{a+bx}} + \frac{(10d^2) \int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx}{27b(bc-ad)} \\
&= -\frac{2(c+dx)^{5/6}}{3b(a+bx)^{3/2}} - \frac{10d(c+dx)^{5/6}}{9b(bc-ad)\sqrt{a+bx}} + \frac{(20d) \operatorname{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{9b(bc-ad)} \\
&= -\frac{2(c+dx)^{5/6}}{3b(a+bx)^{3/2}} - \frac{10d(c+dx)^{5/6}}{9b(bc-ad)\sqrt{a+bx}} - \frac{(10d) \operatorname{Subst} \left(\int \frac{(-1+\sqrt{3})(bc-ad)^{2/3}-2b^{2/3}x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{9b^{5/3}(bc-ad)} \\
&= -\frac{2(c+dx)^{5/6}}{3b(a+bx)^{3/2}} - \frac{10d(c+dx)^{5/6}}{9b(bc-ad)\sqrt{a+bx}} - \frac{10(1+\sqrt{3})d^2\sqrt{a+bx}\sqrt[6]{c+dx}}{9b^{5/3}(bc-ad)\left(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.09

$$-\frac{2(c+dx)^{5/6} {}_2F_1\left(-\frac{3}{2}, -\frac{5}{6}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a+bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/6)/(a + b*x)^(5/2), x]

[Out] (-2*(c + d*x)^(5/6)*Hypergeometric2F1[-3/2, -5/6, -1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(5/6))

fricas [F] time = 0.98, size = 0, normalized size = 0.00

$$\operatorname{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{5/6}}{b^3 x^3 + 3ab^2 x^2 + 3a^2 bx + a^3}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(5/2),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/6)/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(5/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/6)/(b*x + a)^(5/2), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/6)/(b*x+a)^(5/2),x)

[Out] int((d*x+c)^(5/6)/(b*x+a)^(5/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(5/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/6)/(b*x + a)^(5/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{\frac{5}{6}}}{(a + bx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/6)/(a + b*x)^(5/2), x)
```

```
[Out] int((c + d*x)^(5/6)/(a + b*x)^(5/2), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(c + dx)^{\frac{5}{6}}}{(a + bx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/6)/(b*x+a)**(5/2), x)
```

```
[Out] Integral((c + d*x)**(5/6)/(a + b*x)**(5/2), x)
```


$$3.1747 \quad \int \frac{(c+dx)^{5/6}}{(a+bx)^{7/2}} dx$$

Optimal. Leaf size=896

$$\frac{8(1+\sqrt{3})\sqrt{a+bx}\sqrt[6]{c+dx}d^3}{27b^{5/3}(bc-ad)^2\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)} + \frac{8\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}}{9\sqrt[3]{4}b^{5/3}(bc-ad)^{5/3}\sqrt{a}}$$

[Out] $-2/5*(d*x+c)^{(5/6)}/b/(b*x+a)^{(5/2)}-2/9*d*(d*x+c)^{(5/6)}/b/(-a*d+b*c)/(b*x+a)^{(3/2)}+8/27*d^2*(d*x+c)^{(5/6)}/b/(-a*d+b*c)^2/(b*x+a)^{(1/2)}+8/27*d^3*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/b^{(5/3)}/(-a*d+b*c)^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))+8/27*d^2*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}*3^{(1/4)}/b^{(5/3)}/(-a*d+b*c)^{(5/3)}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}+4/81*d^2*(d*x+c)^{(1/6)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)}*(1-3^{(1/2)}))*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}*3^{(3/4)}/b^{(5/3)}/(-a*d+b*c)^{(5/3)}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.90, antiderivative size = 896, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {47, 51, 63, 308, 225, 1881}

$$\frac{8(1 + \sqrt{3})\sqrt{a + bx}\sqrt[6]{c + dx}d^3}{27b^{5/3}(bc - ad)^2(\sqrt[3]{bc - ad} - (1 + \sqrt{3})\sqrt[3]{b}\sqrt[3]{c + dx})} + \frac{8\sqrt[6]{c + dx}(\sqrt[3]{bc - ad} - \sqrt[3]{b}\sqrt[3]{c + dx})\sqrt{\frac{(bc - ad)^{2/3} + \sqrt[3]{b}\sqrt[3]{c + dx}}{(\sqrt[3]{bc - ad} - (1 + \sqrt{3}))\sqrt[3]{b}\sqrt[3]{c + dx}}}}{9 \cdot 3^{3/4}b^{5/3}(bc - ad)^{5/3}\sqrt{a + bx}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/6)/(a + b*x)^(7/2), x]

[Out] (-2*(c + d*x)^(5/6))/(5*b*(a + b*x)^(5/2)) - (2*d*(c + d*x)^(5/6))/(9*b*(b*c - a*d)*(a + b*x)^(3/2)) + (8*d^2*(c + d*x)^(5/6))/(27*b*(b*c - a*d)^2*Sqrt[a + b*x]) + (8*(1 + Sqrt[3])*d^3*Sqrt[a + b*x]*(c + d*x)^(1/6))/(27*b^(5/3)*(b*c - a*d)^2*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) + (8*d^2*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))]^2*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4])/(9*3^(3/4)*b^(5/3)*(b*c - a*d)^(5/3)*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))]^2]) + (4*(1 - Sqrt[3])*d^2*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))]^2]*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4])/(27*3^(1/4)*b^(5/3)*(b*c - a*d)^(5/3)*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))]^2])]

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)),
Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) &&
!(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &&
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
```

```

m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]

```

Rule 63

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 225

```

Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]

```

Rule 308

```

Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a,
3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a
+ b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqr
t[a + b*x^6], x], x]] /; FreeQ[{a, b}, x]

```

Rule 1881

```

Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r =
Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqr
t[a + b*x^6])/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x
*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*El
lipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + S
qrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sq
rt[a + b*x^6]), x]] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1
- Sqrt[3])*d, 0]

```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/6}}{(a+bx)^{7/2}} dx &= -\frac{2(c+dx)^{5/6}}{5b(a+bx)^{5/2}} + \frac{d \int \frac{1}{(a+bx)^{5/2} \sqrt[6]{c+dx}} dx}{3b} \\
&= -\frac{2(c+dx)^{5/6}}{5b(a+bx)^{5/2}} - \frac{2d(c+dx)^{5/6}}{9b(bc-ad)(a+bx)^{3/2}} - \frac{(4d^2) \int \frac{1}{(a+bx)^{3/2} \sqrt[6]{c+dx}} dx}{27b(bc-ad)} \\
&= -\frac{2(c+dx)^{5/6}}{5b(a+bx)^{5/2}} - \frac{2d(c+dx)^{5/6}}{9b(bc-ad)(a+bx)^{3/2}} + \frac{8d^2(c+dx)^{5/6}}{27b(bc-ad)^2 \sqrt{a+bx}} - \frac{(8d^3) \int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx}{81b(bc-ad)^2} \\
&= -\frac{2(c+dx)^{5/6}}{5b(a+bx)^{5/2}} - \frac{2d(c+dx)^{5/6}}{9b(bc-ad)(a+bx)^{3/2}} + \frac{8d^2(c+dx)^{5/6}}{27b(bc-ad)^2 \sqrt{a+bx}} - \frac{(16d^2) \text{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+bx}} dx \right)}{27b(bc-ad)^2} \\
&= -\frac{2(c+dx)^{5/6}}{5b(a+bx)^{5/2}} - \frac{2d(c+dx)^{5/6}}{9b(bc-ad)(a+bx)^{3/2}} + \frac{8d^2(c+dx)^{5/6}}{27b(bc-ad)^2 \sqrt{a+bx}} + \frac{(8d^2) \text{Subst} \left(\int \frac{(-1+\sqrt{3})(b)}{\sqrt{a-\frac{bc}{d}+bx}} dx \right)}{27b^{5/3}} \\
&= -\frac{2(c+dx)^{5/6}}{5b(a+bx)^{5/2}} - \frac{2d(c+dx)^{5/6}}{9b(bc-ad)(a+bx)^{3/2}} + \frac{8d^2(c+dx)^{5/6}}{27b(bc-ad)^2 \sqrt{a+bx}} + \frac{8(1+\sqrt{3})d^3}{27b^{5/3}(bc-ad)^2 \sqrt[3]{bc-ad}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.08

$$\frac{2(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{2}, -\frac{5}{6}; -\frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{5b(a+bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/6)/(a + b*x)^(7/2), x]

[Out] (-2*(c + d*x)^(5/6)*Hypergeometric2F1[-5/2, -5/6, -3/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(5/6))

fricas [F] time = 1.16, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{5}{6}}}{b^4 x^4 + 4ab^3 x^3 + 6a^2 b^2 x^2 + 4a^3 bx + a^4}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(7/2),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/6)/(b^4*x^4 + 4*a*b^3*x^3 + 6*a^2*b^2*x^2 + 4*a^3*b*x + a^4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(7/2),x, algorithm="giac")

[Out] integrate((d*x + c)^(5/6)/(b*x + a)^(7/2), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/6)/(b*x+a)^(7/2),x)

[Out] int((d*x+c)^(5/6)/(b*x+a)^(7/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(7/2),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/6)/(b*x + a)^(7/2), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{\frac{5}{6}}}{(a + bx)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(5/6)/(a + b*x)^(7/2), x)
```

```
[Out] int((c + d*x)^(5/6)/(a + b*x)^(7/2), x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{6}}}{(a + bx)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(5/6)/(b*x+a)**(7/2), x)
```

```
[Out] Integral((c + d*x)**(5/6)/(a + b*x)**(7/2), x)
```

$$3.1748 \quad \int \frac{(a+bx)^{5/2}}{\sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=890

$$\frac{243\sqrt[4]{3}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad}-(1-\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)}{448b^{2/3}d^4\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

[Out] $-9/28*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(5/6)}/d^2+3/10*(b*x+a)^{(5/2)}*(d*x+c)^{(5/6)}/d+81/224*(-a*d+b*c)^2*(d*x+c)^{(5/6)}*(b*x+a)^{(1/2)}/d^3+243/448*(-a*d+b*c)^3*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/b^{(2/3)}/d^3/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))+243/448*3^{(1/4)}*(-a*d+b*c)^{(10/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/b^{(2/3)}/d^4/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}+81/896*3^{(3/4)}*(-a*d+b*c)^{(10/3)}*(d*x+c)^{(1/6)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*((1-3^{(1/2)})*((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/b^{(2/3)}/d^4/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.95, antiderivative size = 890, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {50, 63, 308, 225, 1881}

$$243\sqrt[4]{3}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad}-(1-\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)$$

$$448b^{2/3}d^4\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2)/(c + d*x)^(1/6), x]

[Out] (81*(b*c - a*d)^2*Sqrt[a + b*x]*(c + d*x)^(5/6))/(224*d^3) - (9*(b*c - a*d)*(a + b*x)^(3/2)*(c + d*x)^(5/6))/(28*d^2) + (3*(a + b*x)^(5/2)*(c + d*x)^(5/6))/(10*d) + (243*(1 + Sqrt[3])*(b*c - a*d)^3*Sqrt[a + b*x]*(c + d*x)^(1/6))/(448*b^(2/3)*d^3*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) + (243*3^(1/4)*(b*c - a*d)^(10/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(448*b^(2/3)*d^4*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)]) + (81*3^(3/4)*(1 - Sqrt[3])*(b*c - a*d)^(10/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(896*b^(2/3)*d^4*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)])

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
```


$(d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 225

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^6], x_Symbol] \text{:>} \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticF}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*3^{1/4}*s*\text{Sqrt}[a + b*x^6]*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]), x]] /; \text{FreeQ}\{a, b\}, x]$

Rule 308

$\text{Int}[(x_)^4/\text{Sqrt}[(a_) + (b_)*(x_)^6], x_Symbol] \text{:>} \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[3] - 1)*s^2/(2*r^2), \text{Int}[1/\text{Sqrt}[a + b*x^6], x], x] - \text{Dist}[1/(2*r^2), \text{Int}[(\text{Sqrt}[3] - 1)*s^2 - 2*r^2*x^4]/\text{Sqrt}[a + b*x^6], x], x]] /; \text{FreeQ}\{a, b\}, x]$

Rule 1881

$\text{Int}[(c_) + (d_)*(x_)^4/\text{Sqrt}[(a_) + (b_)*(x_)^6], x_Symbol] \text{:>} \text{With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(1 + \text{Sqrt}[3])*d*s^3*x*\text{Sqrt}[a + b*x^6]/(2*a*r^2*(s + (1 + \text{Sqrt}[3])*r*x^2)), x] - \text{Simp}[(3^{1/4})*d*s*x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticE}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*r^2*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{Sqrt}[a + b*x^6]), x]] /; \text{FreeQ}\{a, b, c, d\}, x] \&\& \text{EqQ}[2*\text{Rt}[b/a, 3]^2*c - (1 - \text{Sqrt}[3])*d, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{\sqrt[6]{c+dx}} dx &= \frac{3(a+bx)^{5/2}(c+dx)^{5/6}}{10d} - \frac{(3(bc-ad)) \int \frac{(a+bx)^{3/2}}{\sqrt[6]{c+dx}} dx}{4d} \\
&= -\frac{9(bc-ad)(a+bx)^{3/2}(c+dx)^{5/6}}{28d^2} + \frac{3(a+bx)^{5/2}(c+dx)^{5/6}}{10d} + \frac{(27(bc-ad)^2) \int \frac{\sqrt{a+bx}}{\sqrt[6]{c+dx}} dx}{56d^2} \\
&= \frac{81(bc-ad)^2 \sqrt{a+bx} (c+dx)^{5/6}}{224d^3} - \frac{9(bc-ad)(a+bx)^{3/2}(c+dx)^{5/6}}{28d^2} + \frac{3(a+bx)^{5/2}(c+dx)^{5/6}}{10d} \\
&= \frac{81(bc-ad)^2 \sqrt{a+bx} (c+dx)^{5/6}}{224d^3} - \frac{9(bc-ad)(a+bx)^{3/2}(c+dx)^{5/6}}{28d^2} + \frac{3(a+bx)^{5/2}(c+dx)^{5/6}}{10d} \\
&= \frac{81(bc-ad)^2 \sqrt{a+bx} (c+dx)^{5/6}}{224d^3} - \frac{9(bc-ad)(a+bx)^{3/2}(c+dx)^{5/6}}{28d^2} + \frac{3(a+bx)^{5/2}(c+dx)^{5/6}}{10d} \\
&= \frac{81(bc-ad)^2 \sqrt{a+bx} (c+dx)^{5/6}}{224d^3} - \frac{9(bc-ad)(a+bx)^{3/2}(c+dx)^{5/6}}{28d^2} + \frac{3(a+bx)^{5/2}(c+dx)^{5/6}}{10d}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.08

$$\frac{2(a+bx)^{7/2} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{7}{2}; \frac{9}{2}; \frac{d(a+bx)}{ad-bc}\right)}{7b \sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/(c + d*x)^(1/6), x]

[Out] (2*(a + b*x)^(7/2)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 7/2, 9/2, (d*(a + b*x))/(-(b*c) + a*d)])/(7*b*(c + d*x)^(1/6))

fricas [F] time = 1.52, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(b^2x^2 + 2abx + a^2)\sqrt{bx+a}}{(dx+c)^{\frac{1}{6}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(5/2)/(d*x+c)^(1/6),x, algorithm="fricas")`

[Out] `integral((b^2*x^2 + 2*a*b*x + a^2)*sqrt(b*x + a)/(d*x + c)^(1/6), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(5/2)/(d*x+c)^(1/6),x, algorithm="giac")`

[Out] `integrate((b*x + a)^(5/2)/(d*x + c)^(1/6), x)`

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(5/2)/(d*x+c)^(1/6),x)`

[Out] `int((b*x+a)^(5/2)/(d*x+c)^(1/6),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(5/2)/(d*x+c)^(1/6),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(5/2)/(d*x + c)^(1/6), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{5/2}}{(c + dx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(5/2)/(c + d*x)^(1/6),x)
```

```
[Out] int((a + b*x)^(5/2)/(c + d*x)^(1/6), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(a + bx)^{\frac{5}{2}}}{\sqrt[6]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(5/2)/(d*x+c)**(1/6),x)
```

```
[Out] Integral((a + b*x)**(5/2)/(c + d*x)**(1/6), x)
```

$$3.1749 \quad \int \frac{(a+bx)^{3/2}}{\sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=855

$$81\sqrt[4]{3}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad}-(1-\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)$$

$$112b^{2/3}d^3\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

[Out] $3/7*(b*x+a)^{(3/2)}*(d*x+c)^{(5/6)}/d-27/56*(-a*d+b*c)*(d*x+c)^{(5/6)}*(b*x+a)^{(1/2)}/d^2-81/112*(-a*d+b*c)^2*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/b^{(2/3)}/d^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))-81/112*3^{(1/4)}*(-a*d+b*c)^{(7/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/b^{(2/3)}/d^3/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}-27/224*3^{(3/4)}*(-a*d+b*c)^{(7/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/b^{(2/3)}/d^3/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.79, antiderivative size = 855, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {50, 63, 308, 225, 1881}

$$81\sqrt[4]{3}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad}-(1-\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)$$

$$112b^{2/3}d^3\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)/(c + d*x)^(1/6), x]

[Out] (-27*(b*c - a*d)*Sqrt[a + b*x]*(c + d*x)^(5/6))/(56*d^2) + (3*(a + b*x)^(3/2)*(c + d*x)^(5/6))/(7*d) - (81*(1 + Sqrt[3])*(b*c - a*d)^2*Sqrt[a + b*x]*(c + d*x)^(1/6))/(112*b^(2/3)*d^2*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) - (81*3^(1/4)*(b*c - a*d)^(7/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(112*b^(2/3)*d^3*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]) - (27*3^(3/4)*(1 - Sqrt[3])*(b*c - a*d)^(7/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(224*b^(2/3)*d^3*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2])]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
```

$[b*c - a*d, 0] \ \&\& \text{LtQ}[-1, m, 0] \ \&\& \text{LeQ}[-1, n, 0] \ \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 225

$\text{Int}[1/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \ :> \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticF}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*3^{1/4}*s*\text{Sqrt}[a + b*x^6]*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]), x]] \ /; \text{FreeQ}[\{a, b\}, x]$

Rule 308

$\text{Int}[(x_)^4/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \ :> \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[3] - 1)*s^2/(2*r^2), \text{Int}[1/\text{Sqrt}[a + b*x^6], x], x] - \text{Dist}[1/(2*r^2), \text{Int}[(\text{Sqrt}[3] - 1)*s^2 - 2*r^2*x^4]/\text{Sqrt}[a + b*x^6], x], x]] \ /; \text{FreeQ}[\{a, b\}, x]$

Rule 1881

$\text{Int}[(c_) + (d_.)*(x_)^4/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \ :> \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(\text{Sqrt}[3] + 1)*d*s^3*x*\text{Sqrt}[a + b*x^6]/(2*a*r^2*(s + (1 + \text{Sqrt}[3])*r*x^2)), x] - \text{Simp}[(3^{1/4}*d*s*x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticE}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*r^2*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{Sqrt}[a + b*x^6]), x]] \ /; \text{FreeQ}[\{a, b, c, d\}, x] \ \&\& \text{EqQ}[2*\text{Rt}[b/a, 3]^2*c - (1 - \text{Sqrt}[3])*d, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{\sqrt[6]{c+dx}} dx &= \frac{3(a+bx)^{3/2}(c+dx)^{5/6}}{7d} - \frac{(9(bc-ad)) \int \frac{\sqrt{a+bx}}{\sqrt[6]{c+dx}} dx}{14d} \\
&= -\frac{27(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56d^2} + \frac{3(a+bx)^{3/2}(c+dx)^{5/6}}{7d} + \frac{(27(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}\sqrt[6]{c+dx}} dx}{112d^2} \\
&= -\frac{27(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56d^2} + \frac{3(a+bx)^{3/2}(c+dx)^{5/6}}{7d} + \frac{(81(bc-ad)^2) \text{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+bx}} dx \right)}{56d^3} \\
&= -\frac{27(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56d^2} + \frac{3(a+bx)^{3/2}(c+dx)^{5/6}}{7d} - \frac{(81(bc-ad)^2) \text{Subst} \left(\int \frac{(-1+\sqrt{3})}{\sqrt{\dots}} dx \right)}{112b^2} \\
&= -\frac{27(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56d^2} + \frac{3(a+bx)^{3/2}(c+dx)^{5/6}}{7d} - \frac{81(1+\sqrt{3})(bc-ad)^2\sqrt{a+bx}}{112b^{2/3}d^2(\sqrt[3]{bc-ad} - (1+\sqrt{3}))}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.09

$$\frac{2(a+bx)^{5/2} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc}\right)}{5b\sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(1/6), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 5/2, 7/2, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(c + d*x)^(1/6))

fricas [F] time = 1.08, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{1}{6}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/6),x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)/(d*x + c)^(1/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(1/6), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(1/6),x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{3/2}}{(c + dx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/(c + d*x)^(1/6),x)

```
[Out] int((a + b*x)^(3/2)/(c + d*x)^(1/6), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(a + bx)^{\frac{3}{2}}}{\sqrt[6]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(3/2)/(d*x+c)**(1/6),x)
```

```
[Out] Integral((a + b*x)**(3/2)/(c + d*x)**(1/6), x)
```

$$3.1750 \quad \int \frac{\sqrt{a+bx}}{\sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=820

$$9\sqrt[4]{3} \sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + b^{2/3} (c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} E \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right)$$

$$8b^{2/3} d^2 \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

[Out] $3/4*(d*x+c)^{(5/6)}*(b*x+a)^{(1/2)}/d+9/8*(-a*d+b*c)*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/b^{(2/3)}/d/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))+9/8*3^{(1/4)}*(-a*d+b*c)^{(4/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/b^{(2/3)}/d^2/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}+3/16*3^{(3/4)}*(-a*d+b*c)^{(4/3)}*(d*x+c)^{(1/6)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/b^{(2/3)}/d^2/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}$

Rubi [A] time = 0.69, antiderivative size = 820, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {50, 63, 308, 225, 1881}

$$\frac{9\sqrt[4]{3}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad}-(1-\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}{\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}\right)\right)}{8b^{2/3}d^2\sqrt{a+bx}\sqrt{\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/(c + d*x)^(1/6), x]

[Out] (3*Sqrt[a + b*x]*(c + d*x)^(5/6))/(4*d) + (9*(1 + Sqrt[3])*(b*c - a*d)*Sqrt[a + b*x]*(c + d*x)^(1/6))/(8*b^(2/3)*d*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) + (9*3^(1/4)*(b*c - a*d)^(4/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))]^2)*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4])/(8*b^(2/3)*d^2*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))]^2)]) + (3*3^(3/4)*(1 - Sqrt[3])*(b*c - a*d)^(4/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))]^2)*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4])/(16*b^(2/3)*d^2*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))]^2)])]

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
```

$[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 225

$\text{Int}[1/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \rightarrow \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticF}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*3^{1/4}*s*\text{Sqrt}[a + b*x^6]*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]), x]] /; \text{FreeQ}[\{a, b\}, x]$

Rule 308

$\text{Int}[(x_)^4/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \rightarrow \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[3] - 1)*s^2/(2*r^2), \text{Int}[1/\text{Sqrt}[a + b*x^6], x], x] - \text{Dist}[1/(2*r^2), \text{Int}[(\text{Sqrt}[3] - 1)*s^2 - 2*r^2*x^4]/\text{Sqrt}[a + b*x^6], x], x]] /; \text{FreeQ}[\{a, b\}, x]$

Rule 1881

$\text{Int}[(c_) + (d_.)*(x_)^4/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \rightarrow \text{With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(\text{Sqrt}[3] + 1)*d*s^3*x*\text{Sqrt}[a + b*x^6]/(2*a*r^2*(s + (1 + \text{Sqrt}[3])*r*x^2)), x] - \text{Simp}[(3^{1/4}*d*s*x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticE}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*r^2*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{Sqrt}[a + b*x^6]), x]] /; \text{FreeQ}[\{a, b, c, d\}, x] \&\& \text{EqQ}[2*\text{Rt}[b/a, 3]^2*c - (1 - \text{Sqrt}[3])*d, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{a+bx}}{\sqrt[6]{c+dx}} dx &= \frac{3\sqrt{a+bx}(c+dx)^{5/6}}{4d} - \frac{(3(bc-ad)) \int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx}{8d} \\
&= \frac{3\sqrt{a+bx}(c+dx)^{5/6}}{4d} - \frac{(9(bc-ad)) \text{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{4d^2} \\
&= \frac{3\sqrt{a+bx}(c+dx)^{5/6}}{4d} + \frac{(9(bc-ad)) \text{Subst} \left(\int \frac{(-1+\sqrt{3})(bc-ad)^{2/3}-2b^{2/3}x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{8b^{2/3}d^2} + \frac{(9(1-\sqrt{3})) \text{Subst} \left(\int \frac{(-1-\sqrt{3})(bc-ad)^{2/3}-2b^{2/3}x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{8b^{2/3}d^2} \\
&= \frac{3\sqrt{a+bx}(c+dx)^{5/6}}{4d} + \frac{9(1+\sqrt{3})(bc-ad)\sqrt{a+bx}\sqrt[6]{c+dx}}{8b^{2/3}d(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} + \frac{9\sqrt[4]{3}(bc-ad)^{4/3}\sqrt[6]{c+dx}}{8b^{2/3}d(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.09

$$\frac{2(a+bx)^{3/2} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{3}{2}, \frac{5}{2}, \frac{d(a+bx)}{ad-bc}\right)}{3b\sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(1/6), x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 3/2, 5/2, (d*(a + b*x))/(-b*c) + a*d])/(3*b*(c + d*x)^(1/6))

fricas [F] time = 1.26, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a}}{(dx+c)^{1/6}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/6), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)/(d*x + c)^(1/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/6),x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(1/6), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(1/6),x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(1/6),x)

[Out] int((a + b*x)^(1/2)/(c + d*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a + bx}}{\sqrt[6]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(1/6), x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(1/6), x)

$$3.1751 \quad \int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=780

$$\frac{3^{3/4} (1 - \sqrt{3}) \sqrt[6]{c+dx} \sqrt[3]{bc-ad} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})^2}} \operatorname{EllipticF}\left(c, \frac{2b^{2/3} d \sqrt{a+bx} \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})^2}}}{\sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})^2}}}}\right)}{2b^{2/3} d \sqrt{a+bx} \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})^2}}}$$

[Out] $-3*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/b^{(2/3)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)})*(d*x+c)^{(1/3)}*(1+3^{(1/2)})-3*3^{(1/4)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*\operatorname{EllipticE}((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/b^{(2/3)}/d/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}-1/2*3^{(3/4)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*\operatorname{EllipticF}((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)}))*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/b^{(2/3)}/d/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.58, antiderivative size = 780, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {63, 308, 225, 1881}

$$\frac{3(1 + \sqrt{3}) \sqrt{a+bx} \sqrt[6]{c+dx}}{b^{2/3} (\sqrt[3]{bc-ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})} \frac{3^{3/4} (1 - \sqrt{3}) \sqrt[6]{c+dx} \sqrt[3]{bc-ad} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})^2}} \operatorname{EllipticF}\left(c, \frac{2b^{2/3} d \sqrt{a+bx} \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})^2}}}{\sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})^2}}}}\right)}{2b^{2/3} d \sqrt{a+bx} \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx})^2}}}$$

Antiderivative was successfully verified.

```
[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(1/6)),x]
```

```
[Out] (-3*(1 + Sqrt[3])*Sqrt[a + b*x]*(c + d*x)^(1/6))/(b^(2/3)*((b*c - a*d)^(1/3)
) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) - (3*3^(1/4)*(b*c - a*d)^(1/3)*
(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c -
a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(
2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]*Ellip
ticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b
*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4]
)/(b^(2/3)*d*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/
3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(
c + d*x)^(1/3))^2)]) - (3^(3/4)*(1 - Sqrt[3])*(b*c - a*d)^(1/3)*(c + d*x)^(
1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3)
+ b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*
c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]*EllipticF[ArcCos
[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(
1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(2*b^(2/3
)*d*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1
/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(
1/3))^2)])]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])]/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rule 308

```
Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a,
3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a
+ b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqr
t[a + b*x^6], x], x]] /; FreeQ[{a, b}, x]
```

Rule 1881

```
Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r =
  Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqr
  t[a + b*x^6])/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x
  *(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*El
  lipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + S
  qrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sq
  rt[a + b*x^6]), x]] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1
  - Sqrt[3])*d, 0]
```

Rubi steps

$$\int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx = \frac{6 \operatorname{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{d}$$

$$= -\frac{3 \operatorname{Subst} \left(\int \frac{(-1+\sqrt{3})(bc-ad)^{2/3}-2b^{2/3}x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{b^{2/3}d} - \frac{(3(1-\sqrt{3})(bc-ad)^{2/3}) \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{b^{2/3}}$$

$$= -\frac{3(1+\sqrt{3})\sqrt{a+bx} \sqrt[6]{c+dx}}{b^{2/3}(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b} \sqrt[3]{c+dx})} - \frac{3^4 \sqrt{3} \sqrt[3]{bc-ad} \sqrt[6]{c+dx} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{b^{2/3}(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b} \sqrt[3]{c+dx})}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.09

$$\frac{2\sqrt{a+bx} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{1}{2}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(1/6)),x]

[Out] (2*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 1/2, 3/2, (d*(a + b*x))/(-b*c) + a*d])/(b*(c + d*x)^(1/6))

fricas [F] time = 0.90, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{5}{6}}}{bdx^2 + ac + (bc+ad)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/6),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/6)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a} (dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/6),x, algorithm="giac")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(1/6)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a} (dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(1/6),x)

[Out] int(1/(b*x+a)^(1/2)/(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a} (dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(1/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{\sqrt{a+bx} (c+dx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(1/2)*(c + d*x)^(1/6)), x)`

[Out] `int(1/((a + b*x)^(1/2)*(c + d*x)^(1/6)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/2)/(d*x+c)**(1/6), x)`

[Out] `Integral(1/(sqrt(a + b*x)*(c + d*x)**(1/6)), x)`

$$3.1752 \quad \int \frac{1}{(a+bx)^{3/2} \sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=813

$$\frac{2(1+\sqrt{3})\sqrt{a+bx}\sqrt[6]{c+dx}}{b^{2/3}(bc-ad)\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)} - \frac{2\sqrt[4]{3}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}}{b^{2/3}(bc-ad)^{2/3}\sqrt{a+bx}}$$

[Out] $-2*(d*x+c)^{(5/6)/(-a*d+b*c)/(b*x+a)^{(1/2)}-2*d*(d*x+c)^{(1/6)*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/b^{(2/3)/(-a*d+b*c)/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})-2*3^{(1/4)*(d*x+c)^{(1/6)*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2)})})^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2)})})*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})}*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2)})})^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)*(-a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)}+b^{(2/3)*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)}/b^{(2/3)/(-a*d+b*c)^{(2/3)/(b*x+a)^{(1/2)/(-b^{(1/3)*(d*x+c)^{(1/3)*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)}-1/3*(d*x+c)^{(1/6)*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2)})})^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2)})})*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})}*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2)})})^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)*(-a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)}+b^{(2/3)*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)}*3^{(3/4)}/b^{(2/3)/(-a*d+b*c)^{(2/3)/(b*x+a)^{(1/2)/(-b^{(1/3)*(d*x+c)^{(1/3)*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)}$

Rubi [A] time = 0.68, antiderivative size = 813, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {51, 63, 308, 225, 1881}

$$\frac{2(1 + \sqrt{3}) \sqrt{a + bx} \sqrt[6]{c + dx} d}{b^{2/3}(bc - ad) \left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)} \cdot \frac{2\sqrt[4]{3} \sqrt[6]{c + dx} \left(\sqrt[3]{bc - ad} - \sqrt[3]{b} \sqrt[3]{c + dx} \right) \sqrt{\frac{(bc - ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{c + dx}}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c + dx} \right)^2}}}{b^{2/3}(bc - ad)^{2/3} \sqrt{a + bx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/2)*(c + d*x)^(1/6)),x]

[Out]
$$\begin{aligned} & (-2*(c + d*x)^{(5/6)})/((b*c - a*d)*\text{Sqrt}[a + b*x]) - (2*(1 + \text{Sqrt}[3])*d*\text{Sqrt}[\\ & a + b*x]*(c + d*x)^{(1/6)})/(b^{(2/3)}*(b*c - a*d)*((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})) - (2*3^{(1/4)}*(c + d*x)^{(1/6)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3}))*\text{Sqrt}[((b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)})/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2]*\text{EllipticE}[\text{ArcCos}[(b*c - a*d)^{(1/3)} - (1 - \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})], (2 + \text{Sqrt}[3])/4)]/(b^{(2/3)}*(b*c - a*d)^{(2/3)}*\text{Sqrt}[a + b*x]*\text{Sqrt}[-((b^{(1/3)}*(c + d*x)^{(1/3)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}))/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2)]) - ((1 - \text{Sqrt}[3])*c + d*x)^{(1/6)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3}))*\text{Sqrt}[((b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)})/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2]*\text{EllipticF}[\text{ArcCos}[(b*c - a*d)^{(1/3)} - (1 - \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})], (2 + \text{Sqrt}[3])/4)]/(3^{(1/4)}*b^{(2/3)}*(b*c - a*d)^{(2/3)}*\text{Sqrt}[a + b*x]*\text{Sqrt}[-((b^{(1/3)}*(c + d*x)^{(1/3)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}))/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2)]) \end{aligned}$$

Rule 51

$$\text{Int}[(a + b*x)^m * (c + d*x)^n, x] := \text{Simp}[(a + b*x)^{m+1} * (c + d*x)^{n+1} / ((b*c - a*d) * (m+1)), x] - \text{Dist}[(d * (m + n + 2)) / ((b*c - a*d) * (m+1)), \text{Int}[(a + b*x)^{m+1} * (c + d*x)^n, x], x] /;$$

FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntegerQ[m]

Rule 63

$$\text{Int}[(a + b*x)^m * (c + d*x)^n, x] := \text{With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{p*(m+1) - 1} * (c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /;$$

FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]]

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rule 308

```
Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a,
3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a
+ b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqr
t[a + b*x^6], x], x]] /; FreeQ[{a, b}, x]
```

Rule 1881

```
Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r =
Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqr
t[a + b*x^6])/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x
*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*El
lipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + S
qrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sq
rt[a + b*x^6]), x]] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1
- Sqrt[3])*d, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{3/2} \sqrt[6]{c+dx}} dx &= -\frac{2(c+dx)^{5/6}}{(bc-ad)\sqrt{a+bx}} + \frac{(2d) \int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx}{3(bc-ad)} \\
&= -\frac{2(c+dx)^{5/6}}{(bc-ad)\sqrt{a+bx}} + \frac{4 \operatorname{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{bc-ad} \\
&= -\frac{2(c+dx)^{5/6}}{(bc-ad)\sqrt{a+bx}} - \frac{2 \operatorname{Subst} \left(\int \frac{(-1+\sqrt{3})(bc-ad)^{2/3}-2b^{2/3}x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{b^{2/3}(bc-ad)} - \frac{2(1-\sqrt{3})}{2\sqrt[4]{3}\sqrt[6]{c}} \\
&= -\frac{2(c+dx)^{5/6}}{(bc-ad)\sqrt{a+bx}} - \frac{2(1+\sqrt{3})d\sqrt{a+bx}\sqrt[6]{c+dx}}{b^{2/3}(bc-ad)\left(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)} - \frac{2\sqrt[4]{3}\sqrt[6]{c}}{2\sqrt[4]{3}\sqrt[6]{c}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.09

$$\frac{2\sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{2}, \frac{1}{6}, \frac{1}{2}, \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt{a+bx}\sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(1/6)),x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[-1/2, 1/6, 1/2, (d*(a + b*x))/(-b*c) + a*d])/(b*Sqrt[a + b*x]*(c + d*x)^(1/6))

fricas [F] time = 1.16, size = 0, normalized size = 0.00

$$\operatorname{integral} \left(\frac{\sqrt{bx+a}(dx+c)^{\frac{5}{6}}}{b^2dx^3 + a^2c + (b^2c + 2abd)x^2 + (2abc + a^2d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/6),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/6)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{3}{2}}(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(1/6)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{3}{2}}(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(1/6),x)

[Out] int(1/(b*x+a)^(3/2)/(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{3}{2}}(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(1/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{3/2}(c + dx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(1/6)),x)

[Out] int(1/((a + b*x)^(3/2)*(c + d*x)^(1/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} \sqrt[6]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(1/6), x)

[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(1/6)), x)

= 0.263, Rules used = {51, 63, 308, 225, 1881}

$$\frac{8(1 + \sqrt{3})\sqrt{a + bx}\sqrt[6]{c + dx}d^2}{9b^{2/3}(bc - ad)^2\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3})\sqrt[3]{b}\sqrt[3]{c + dx}\right)} + \frac{8\sqrt[6]{c + dx}\left(\sqrt[3]{bc - ad} - \sqrt[3]{b}\sqrt[3]{c + dx}\right)\sqrt{\frac{(bc - ad)^{2/3} + \sqrt[3]{b}\sqrt[3]{c + dx}}{\left(\sqrt[3]{bc - ad} - (1 + \sqrt{3})\sqrt[3]{b}\sqrt[3]{c + dx}\right)}}}{3^{3/4}b^{2/3}(bc - ad)^{5/3}\sqrt{a + bx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*(c + d*x)^(1/6)),x]

[Out] (-2*(c + d*x)^(5/6))/(3*(b*c - a*d)*(a + b*x)^(3/2)) + (8*d*(c + d*x)^(5/6))/(9*(b*c - a*d)^2*sqrt[a + b*x]) + (8*(1 + sqrt[3])*d^2*sqrt[a + b*x]*(c + d*x)^(1/6))/(9*b^(2/3)*(b*c - a*d)^2*((b*c - a*d)^(1/3) - (1 + sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) + (8*d*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + sqrt[3])/4)]/(3*3^(3/4)*b^(2/3)*(b*c - a*d)^(5/3)*sqrt[a + b*x]*sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]) + (4*(1 - sqrt[3])*d*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + sqrt[3])/4)]/(9*3^(1/4)*b^(2/3)*(b*c - a*d)^(5/3)*sqrt[a + b*x]*sqrt[-((b^(1/3)*(c + d*x)^(1/3))*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2])]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ

$[b*c - a*d, 0] \ \&\& \text{LtQ}[-1, m, 0] \ \&\& \text{LeQ}[-1, n, 0] \ \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \ \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 225

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^6], x_Symbol] \text{ :> With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticF}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*3^{(1/4)}*s*\text{Sqrt}[a + b*x^6]*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]), x]] \ /; \text{FreeQ}\{a, b\}, x]$

Rule 308

$\text{Int}[(x_)^4/\text{Sqrt}[(a_) + (b_)*(x_)^6], x_Symbol] \text{ :> With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[3] - 1)*s^2/(2*r^2), \text{Int}[1/\text{Sqrt}[a + b*x^6], x], x] - \text{Dist}[1/(2*r^2), \text{Int}[(\text{Sqrt}[3] - 1)*s^2 - 2*r^2*x^4]/\text{Sqrt}[a + b*x^6], x], x]] \ /; \text{FreeQ}\{a, b\}, x]$

Rule 1881

$\text{Int}[(c_) + (d_)*(x_)^4/\text{Sqrt}[(a_) + (b_)*(x_)^6], x_Symbol] \text{ :> With}[\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(\text{Sqrt}[3] + 1)*d*s^3*x*\text{Sqrt}[a + b*x^6]/(2*a*r^2*(s + (1 + \text{Sqrt}[3])*r*x^2)), x] - \text{Simp}[(3^{(1/4)}*d*s*x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticE}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])/(2*r^2*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{Sqrt}[a + b*x^6]), x]] \ /; \text{FreeQ}\{a, b, c, d\}, x] \ \&\& \ \text{EqQ}[2*\text{Rt}[b/a, 3]^2*c - (1 - \text{Sqrt}[3])*d, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/2} \sqrt[6]{c+dx}} dx &= -\frac{2(c+dx)^{5/6}}{3(bc-ad)(a+bx)^{3/2}} - \frac{(4d) \int \frac{1}{(a+bx)^{3/2} \sqrt[6]{c+dx}} dx}{9(bc-ad)} \\
&= -\frac{2(c+dx)^{5/6}}{3(bc-ad)(a+bx)^{3/2}} + \frac{8d(c+dx)^{5/6}}{9(bc-ad)^2 \sqrt{a+bx}} - \frac{(8d^2) \int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx}{27(bc-ad)^2} \\
&= -\frac{2(c+dx)^{5/6}}{3(bc-ad)(a+bx)^{3/2}} + \frac{8d(c+dx)^{5/6}}{9(bc-ad)^2 \sqrt{a+bx}} - \frac{(16d) \text{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d} + \frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{9(bc-ad)^2} \\
&= -\frac{2(c+dx)^{5/6}}{3(bc-ad)(a+bx)^{3/2}} + \frac{8d(c+dx)^{5/6}}{9(bc-ad)^2 \sqrt{a+bx}} + \frac{(8d) \text{Subst} \left(\int \frac{(-1+\sqrt{3})(bc-ad)^{2/3} - 2b^{2/3}}{\sqrt{a-\frac{bc}{d} + \frac{bx^6}{d}}} dx \right)}{9b^{2/3}(bc-ad)^2} \\
&= -\frac{2(c+dx)^{5/6}}{3(bc-ad)(a+bx)^{3/2}} + \frac{8d(c+dx)^{5/6}}{9(bc-ad)^2 \sqrt{a+bx}} + \frac{8(1+\sqrt{3})d^2 \sqrt{a+bx} \sqrt[6]{c+dx}}{9b^{2/3}(bc-ad)^2 (\sqrt[3]{bc-ad} - (1+\sqrt{3}))}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 73, normalized size = 0.09

$$-\frac{2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{3}{2}, \frac{1}{6}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc}\right)}{3b(a+bx)^{3/2} \sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(1/6)), x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[-3/2, 1/6, -1/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(a + b*x)^(3/2)*(c + d*x)^(1/6))

fricas [F] time = 1.20, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a} (dx+c)^{\frac{5}{6}}}{b^3 dx^4 + a^3 c + (b^3 c + 3 ab^2 d)x^3 + 3(ab^2 c + a^2 bd)x^2 + (3 a^2 bc + a^3 d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/6),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/6)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{2}}(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(1/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{2}}(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(1/6),x)

[Out] int(1/(b*x+a)^(5/2)/(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{2}}(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(1/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{5/2}(c + dx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/2)*(c + d*x)^(1/6)),x)


```
[Out] int(1/((a + b*x)^(5/2)*(c + d*x)^(1/6)), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{1}{(a + bx)^{\frac{5}{2}} \sqrt[6]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(1/6), x)
```

```
[Out] Integral(1/((a + b*x)**(5/2)*(c + d*x)**(1/6)), x)
```

$$3.1754 \quad \int \frac{(a+bx)^{5/2}}{(c+dx)^{5/6}} dx$$

Optimal. Leaf size=440

$$81 \cdot 3^{3/4} \sqrt[6]{c+dx} (bc-ad)^{8/3} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \hline 128d^4 \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

[Out] $-9/16*(-a*d+b*c)*(b*x+a)^{(3/2)}*(d*x+c)^{(1/6)}/d^2+3/8*(b*x+a)^{(5/2)}*(d*x+c)^{(1/6)}/d+81/64*(-a*d+b*c)^2*(d*x+c)^{(1/6)}*(b*x+a)^{(1/2)}/d^3-81/128*3^{(3/4)}*(-a*d+b*c)^{(8/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*\operatorname{EllipticF}((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/d^4/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.33, antiderivative size = 440, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 225}

$$81 \cdot 3^{3/4} \sqrt[6]{c+dx} (bc-ad)^{8/3} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \hline 128d^4 \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/2)}/(c + d*x)^{(5/6)}, x]$

[Out] $(81*(b*c - a*d)^2*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{(1/6)})/(64*d^3) - (9*(b*c - a*d)*(a + b*x)^{(3/2)}*(c + d*x)^{(1/6)})/(16*d^2) + (3*(a + b*x)^{(5/2)}*(c + d*x)^{(1/6)})/(8*d) - (81*3^{(3/4)}*(b*c - a*d)^{(8/3)}*(c + d*x)^{(1/6)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})*\operatorname{Sqrt}[\left((b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)} \right)/\left((b*c - a*d)^{(1/3)} - (1 + \sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2]$

```
Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2*EllipticF[ArcCos[((b*c - a*d)^(1/3) -
(1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*
b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(128*d^4*Sqrt[a + b*x]*Sqrt[-(
b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/(b
*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4)]/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x] /; FreeQ[{a, b}, x
]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{(c+dx)^{5/6}} dx &= \frac{3(a+bx)^{5/2} \sqrt[6]{c+dx}}{8d} - \frac{(15(bc-ad)) \int \frac{(a+bx)^{3/2}}{(c+dx)^{5/6}} dx}{16d} \\
&= -\frac{9(bc-ad)(a+bx)^{3/2} \sqrt[6]{c+dx}}{16d^2} + \frac{3(a+bx)^{5/2} \sqrt[6]{c+dx}}{8d} + \frac{(27(bc-ad)^2) \int \frac{\sqrt{a+bx}}{(c+dx)^{5/6}} dx}{32d^2} \\
&= \frac{81(bc-ad)^2 \sqrt{a+bx} \sqrt[6]{c+dx}}{64d^3} - \frac{9(bc-ad)(a+bx)^{3/2} \sqrt[6]{c+dx}}{16d^2} + \frac{3(a+bx)^{5/2} \sqrt[6]{c+dx}}{8d} \\
&= \frac{81(bc-ad)^2 \sqrt{a+bx} \sqrt[6]{c+dx}}{64d^3} - \frac{9(bc-ad)(a+bx)^{3/2} \sqrt[6]{c+dx}}{16d^2} + \frac{3(a+bx)^{5/2} \sqrt[6]{c+dx}}{8d} \\
&= \frac{81(bc-ad)^2 \sqrt{a+bx} \sqrt[6]{c+dx}}{64d^3} - \frac{9(bc-ad)(a+bx)^{3/2} \sqrt[6]{c+dx}}{16d^2} + \frac{3(a+bx)^{5/2} \sqrt[6]{c+dx}}{8d}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.17

$$\frac{2(a+bx)^{7/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/6} {}_2F_1 \left(\frac{5}{6}, \frac{7}{2}; \frac{9}{2}; \frac{d(a+bx)}{ad-bc} \right)}{7b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/(c + d*x)^(5/6), x]

[Out] (2*(a + b*x)^(7/2)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[5/6, 7/2, 9/2, (d*(a + b*x))/(-b*c) + a*d])/(7*b*(c + d*x)^(5/6))

fricas [F] time = 0.90, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(b^2x^2 + 2abx + a^2)\sqrt{bx+a}}{(dx+c)^{5/6}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(5/6), x, algorithm="fricas")

[Out] $\text{integral}((b^2*x^2 + 2*a*b*x + a^2)*\text{sqrt}(b*x + a)/(d*x + c)^{(5/6)}, x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)^{(5/2)}/(d*x+c)^{(5/6)}, x, \text{algorithm}="giac")$

[Out] $\text{integrate}((b*x + a)^{(5/2)}/(d*x + c)^{(5/6)}, x)$

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x+a)^{(5/2)}/(d*x+c)^{(5/6)}, x)$

[Out] $\text{int}((b*x+a)^{(5/2)}/(d*x+c)^{(5/6)}, x)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)^{(5/2)}/(d*x+c)^{(5/6)}, x, \text{algorithm}="maxima")$

[Out] $\text{integrate}((b*x + a)^{(5/2)}/(d*x + c)^{(5/6)}, x)$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{5/2}}{(c + dx)^{5/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^{(5/2)}/(c + d*x)^{(5/6)}, x)$

[Out] $\text{int}((a + b*x)^{(5/2)}/(c + d*x)^{(5/6)}, x)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{2}}}{(c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/2)/(d*x+c)**(5/6),x)

[Out] Integral((a + b*x)**(5/2)/(c + d*x)**(5/6), x)

$$3.1755 \quad \int \frac{(a+bx)^{3/2}}{(c+dx)^{5/6}} dx$$

Optimal. Leaf size=405

$$\frac{27^{3/4} \sqrt[6]{c+dx} (bc-ad)^{5/3} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right)}{\right)}{40d^3 \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

[Out] $\frac{3}{5} (b*x+a)^{3/2} (d*x+c)^{1/6} / d - 27/20 (-a*d+b*c) (d*x+c)^{1/6} (b*x+a)^{1/2} / d^2 + 27/40 * 3^{3/4} (-a*d+b*c)^{5/3} (d*x+c)^{1/6} ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) * (((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) * (1-3^{1/2}))^2 / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) * (1+3^{1/2}))^2)^{1/2} / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) * (1-3^{1/2})) * ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) * (1+3^{1/2})) * \operatorname{EllipticF} \left(\frac{1 - ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) * (1-3^{1/2}))^2}{((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) * (1+3^{1/2}))^2} \right)^{1/2}, 1/4 * 6^{1/2} + 1/4 * 2^{1/2}) * (((-a*d+b*c)^{2/3} + b^{1/3} (-a*d+b*c)^{1/3} (d*x+c)^{1/3} + b^{2/3} (d*x+c)^{2/3}) / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) * (1+3^{1/2}))^2)^{1/2} / d^3 / (b*x+a)^{1/2} / (-b^{1/3} (d*x+c)^{1/3}) * ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) * (1+3^{1/2}))^2)^{1/2}$

Rubi [A] time = 0.28, antiderivative size = 405, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 225}

$$\frac{27^{3/4} \sqrt[6]{c+dx} (bc-ad)^{5/3} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right)}{\right)}{40d^3 \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)/(c + d*x)^(5/6), x]

[Out] $(-27*(b*c - a*d)*\operatorname{Sqrt}[a + b*x]*(c + d*x)^{1/6}) / (20*d^2) + (3*(a + b*x)^{3/2}*(c + d*x)^{1/6}) / (5*d) + (27*3^{3/4}*(b*c - a*d)^{5/3}*(c + d*x)^{1/6}*((b*c - a*d)^{1/3} - b^{1/3}*(c + d*x)^{1/3})*\operatorname{Sqrt}[\frac{(b*c - a*d)^{2/3} + b^{1/3}*(c + d*x)^{2/3}}{(b*c - a*d)^{1/3} - b^{1/3}*(c + d*x)^{1/3}}]) / ((b*c - a*d)^{1/3} - (1 + \operatorname{Sqrt}[3])*b^{1/3}*(c + d*x)^{1/3})^2 * \operatorname{EllipticF}[\operatorname{ArcCos}[\frac{(b*c - a*d)^{1/3} - b^{1/3}*(c + d*x)^{1/3}}{(b*c - a*d)^{1/3} - (1 + \operatorname{Sqrt}[3])*b^{1/3}*(c + d*x)^{1/3}}]]$

$$- a*d)^{(1/3)} - (1 - \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)} / ((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)}), (2 + \text{Sqrt}[3])/4] / (40*d^3*\text{Sqrt}[a + b*x]*\text{Sqrt}[-((b^{(1/3)}*(c + d*x)^{(1/3)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)})) / ((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2])]$$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4]) / (2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{(c+dx)^{5/6}} dx &= \frac{3(a+bx)^{3/2} \sqrt[6]{c+dx}}{5d} - \frac{(9(bc-ad)) \int \frac{\sqrt{a+bx}}{(c+dx)^{5/6}} dx}{10d} \\
&= -\frac{27(bc-ad)\sqrt{a+bx} \sqrt[6]{c+dx}}{20d^2} + \frac{3(a+bx)^{3/2} \sqrt[6]{c+dx}}{5d} + \frac{(27(bc-ad)^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/6}} dx}{40d^2} \\
&= -\frac{27(bc-ad)\sqrt{a+bx} \sqrt[6]{c+dx}}{20d^2} + \frac{3(a+bx)^{3/2} \sqrt[6]{c+dx}}{5d} + \frac{(81(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx \right)}{20d^3} \\
&= -\frac{27(bc-ad)\sqrt{a+bx} \sqrt[6]{c+dx}}{20d^2} + \frac{3(a+bx)^{3/2} \sqrt[6]{c+dx}}{5d} + \frac{27 \cdot 3^{3/4} (bc-ad)^{5/3} \sqrt[6]{c+dx} \left(\sqrt[3]{bc} - \dots \right)}{\dots}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.18

$$\frac{2(a+bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/6} {}_2F_1 \left(\frac{5}{6}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc} \right)}{5b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(5/6), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[5/6, 5/2, 7/2, (d*(a + b*x))/(-b*c + a*d)])/(5*b*(c + d*x)^(5/6))

fricas [F] time = 0.63, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{3}{2}}}{(dx+c)^{\frac{5}{6}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(5/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)/(d*x + c)^(5/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(5/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(5/6), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(5/6),x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{(c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/(c + d*x)^(5/6),x)

[Out] int((a + b*x)^(3/2)/(c + d*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{3}{2}}}{(c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(3/2)/(d*x+c)**(5/6), x)

[Out] Integral((a + b*x)**(3/2)/(c + d*x)**(5/6), x)

$$3.1756 \quad \int \frac{\sqrt{a+bx}}{(c+dx)^{5/6}} dx$$

Optimal. Leaf size=372

$$\frac{3\sqrt{a+bx}\sqrt[6]{c+dx}}{2d} - \frac{3 \cdot 3^{3/4} \sqrt[6]{c+dx} (bc-ad)^{2/3} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{\sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b} \sqrt[3]{c+dx})^2}}} - \frac{4d^2 \sqrt{a+bx}}{\sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b} \sqrt[3]{c+dx})^2}}}$$

[Out] $\frac{3}{2} \cdot (d \cdot x + c)^{1/6} \cdot (b \cdot x + a)^{1/2} / d - \frac{3 \cdot 3^{3/4} \cdot (-a \cdot d + b \cdot c)^{2/3} \cdot (d \cdot x + c)^{1/6} \cdot ((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot (((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot (1 - 3^{1/2}))^2 / ((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot (1 + 3^{1/2}))^2}{(((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot (1 - 3^{1/2})) \cdot ((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot (1 + 3^{1/2}))} \cdot \text{EllipticF}(\frac{1 - ((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot (1 - 3^{1/2})}{((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot (1 + 3^{1/2})})^2 / ((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot (1 + 3^{1/2}))^2, \frac{1}{4} \cdot 6^{1/2} + \frac{1}{4} \cdot 2^{1/2}) \cdot (((-a \cdot d + b \cdot c)^{2/3} + b^{1/3} \cdot (-a \cdot d + b \cdot c)^{1/3} \cdot (d \cdot x + c)^{1/3}) + b^{2/3} \cdot (d \cdot x + c)^{2/3}) / (((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot (1 + 3^{1/2}))^2)^{1/2} / d^2 / (b \cdot x + a)^{1/2} / (-b^{1/3} \cdot (d \cdot x + c)^{1/3} \cdot ((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) / ((-a \cdot d + b \cdot c)^{1/3} - b^{1/3} \cdot (d \cdot x + c)^{1/3}) \cdot (1 + 3^{1/2}))^2)^{1/2}$

Rubi [A] time = 0.24, antiderivative size = 372, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {50, 63, 225}

$$\frac{3\sqrt{a+bx}\sqrt[6]{c+dx}}{2d} - \frac{3 \cdot 3^{3/4} \sqrt[6]{c+dx} (bc-ad)^{2/3} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{\sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b} \sqrt[3]{c+dx})^2}}} - \frac{4d^2 \sqrt{a+bx}}{\sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} (\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx})}{(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b} \sqrt[3]{c+dx})^2}}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/(c + d*x)^(5/6), x]

[Out] $\frac{(3 \cdot \text{Sqrt}[a + b \cdot x] \cdot (c + d \cdot x)^{1/6}) / (2 \cdot d) - (3 \cdot 3^{3/4} \cdot (b \cdot c - a \cdot d)^{2/3} \cdot (c + d \cdot x)^{1/6} \cdot ((b \cdot c - a \cdot d)^{1/3} - b^{1/3} \cdot (c + d \cdot x)^{1/3}) \cdot \text{Sqrt}[\frac{((b \cdot c - a \cdot d)^{2/3} + b^{1/3} \cdot (b \cdot c - a \cdot d)^{1/3} \cdot (c + d \cdot x)^{1/3}) + b^{2/3} \cdot (c + d \cdot x)^{2/3}}{((b \cdot c - a \cdot d)^{1/3} - (1 + \text{Sqrt}[3]) \cdot b^{1/3} \cdot (c + d \cdot x)^{1/3})^2}]} \cdot \text{EllipticF}[\text{ArcCos}[\frac{(b \cdot c - a \cdot d)^{1/3} - (1 - \text{Sqrt}[3]) \cdot b^{1/3} \cdot (c + d \cdot x)^{1/3}}{(b \cdot c - a \cdot d)^{1/3} - (1 + \text{Sqrt}[3]) \cdot b^{1/3} \cdot (c + d \cdot x)^{1/3}}], (2 + \text{Sqrt}[3]) / 4]) / (4$

$d^2 \sqrt{a + bx} \sqrt{-((b^{1/3}(c + dx)^{1/3}((bc - ad)^{1/3} - b^{1/3}(c + dx)^{1/3}))/((bc - ad)^{1/3} - (1 + \sqrt{3})b^{1/3}(c + dx)^{1/3}))^2}$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 ((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
 (b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
 c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
 [m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
 + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
 {p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
 (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
 [b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
 ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 225

Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
 s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
 (s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
 + (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
 t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x] /; FreeQ[{a, b}, x
]

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{a+bx}}{(c+dx)^{5/6}} dx &= \frac{3\sqrt{a+bx} \sqrt[6]{c+dx}}{2d} - \frac{(3(bc-ad)) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/6}} dx}{4d} \\
&= \frac{3\sqrt{a+bx} \sqrt[6]{c+dx}}{2d} - \frac{(9(bc-ad)) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{2d^2} \\
&= \frac{3\sqrt{a+bx} \sqrt[6]{c+dx}}{2d} - \frac{3 \cdot 3^{3/4} (bc-ad)^{2/3} \sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{bc-ad}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt[3]{b} \sqrt[3]{c+dx}) \right)}}}{4d^2 \sqrt{a+bx} \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt[3]{b} \sqrt[3]{c+dx}) \right)}}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.20

$$\frac{2(a+bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/6} {}_2F_1 \left(\frac{5}{6}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(5/6), x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[5/6, 3/2, 5/2, (d*(a + b*x))/(-(b*c) + a*d)]/(3*b*(c + d*x)^(5/6))

fricas [F] time = 0.90, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a}}{(dx+c)^{5/6}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(5/6), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)/(d*x + c)^(5/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{5/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(5/6),x, algorithm="giac")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(5/6), x)

maple [F] time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/2)/(d*x+c)^(5/6),x)

[Out] int((b*x+a)^(1/2)/(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate(sqrt(b*x + a)/(d*x + c)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/2)/(c + d*x)^(5/6),x)

[Out] int((a + b*x)^(1/2)/(c + d*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(5/6),x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(5/6), x)

$$3.1757 \quad \int \frac{1}{\sqrt{a+bx} (c+dx)^{5/6}} dx$$

Optimal. Leaf size=343

$$3^{3/4} \sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right)$$

$$d\sqrt{a+bx} \sqrt[3]{bc-ad} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

[Out] $3^{3/4} (d*x+c)^{1/6} ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) (((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) (1-3^{1/2}))^2 / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) (1+3^{1/2}))^2)^{1/2} / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) (1-3^{1/2})) * ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) (1+3^{1/2})) * \operatorname{EllipticF} \left((1 - ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) (1-3^{1/2}))^2 / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) (1+3^{1/2}))^2)^{1/2}, 1/4 * 6^{1/2} + 1/4 * 2^{1/2} \right) * (((-a*d+b*c)^{2/3} + b^{1/3} (-a*d+b*c)^{1/3} (d*x+c)^{1/3} + b^{2/3} (d*x+c)^{2/3}) / ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) (1+3^{1/2}))^2)^{1/2} / (-a*d+b*c)^{1/3} / (b*x+a)^{1/2} / (-b^{1/3} (d*x+c)^{1/3}) * ((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) / (((-a*d+b*c)^{1/3} - b^{1/3} (d*x+c)^{1/3}) (1+3^{1/2}))^2)^{1/2}$

Rubi [A] time = 0.19, antiderivative size = 343, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {63, 225}

$$3^{3/4} \sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3} (c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right)$$

$$d\sqrt{a+bx} \sqrt[3]{bc-ad} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}$$

Antiderivative was successfully verified.

[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(5/6)),x]

[Out] $(3^{3/4} (c + d*x)^{1/6} ((b*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3}) * \operatorname{Sqrt} [((b*c - a*d)^{2/3} + b^{1/3} (b*c - a*d)^{1/3} (c + d*x)^{1/3} + b^{2/3} (c + d*x)^{2/3}) / ((b*c - a*d)^{1/3} - (1 + \operatorname{Sqrt}[3]) * b^{1/3} (c + d*x)^{1/3})^2] * \operatorname{EllipticF} [\operatorname{ArcCos} [((b*c - a*d)^{1/3} - (1 - \operatorname{Sqrt}[3]) * b^{1/3} (c + d*x)^{1/3}) / ((b*c - a*d)^{1/3} - (1 + \operatorname{Sqrt}[3]) * b^{1/3} (c + d*x)^{1/3})], (2 + \operatorname{Sqrt}[3]) / 4]) / (d * (b*c - a*d)^{1/3} * \operatorname{Sqrt}[a + b*x] * \operatorname{Sqrt} [-(b^{1/3} (c + d*x)^{1/3}) * ((b*c - a*d)^{1/3} - b^{1/3} (c + d*x)^{1/3})] / ((b*c - a*d)^{1/3} - (1 + \operatorname{Sqrt}[3]) * b^{1/3} (c + d*x)^{1/3})^2])$

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rubi steps

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{5/6}} dx = \frac{6 \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{d}$$

$$= \frac{3^{3/4} \sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{bc-ad} \sqrt[3]{c+dx} + b^{2/3} (c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}\right)\right)}{d \sqrt[3]{bc-ad} \sqrt{a+bx} \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.21

$$\frac{2\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{2}, \frac{5}{6}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(5/6)), x]

[Out] (2*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[1/2, 5/6, 3/2, (d*(a + b*x))/(-b*c) + a*d])/(b*(c + d*x)^(5/6))

fricas [F] time = 0.74, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{\frac{1}{6}}}{bdx^2+ac+(bc+ad)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(5/6),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/6)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(5/6),x, algorithm="giac")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(5/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(5/6),x)

[Out] int(1/(b*x+a)^(1/2)/(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(5/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(1/2)*(c + d*x)^(5/6)), x)`

[Out] `int(1/((a + b*x)^(1/2)*(c + d*x)^(5/6)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a + bx} (c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/2)/(d*x+c)**(5/6), x)`

[Out] `Integral(1/(sqrt(a + b*x)*(c + d*x)**(5/6)), x)`

$$3.1758 \quad \int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/6}} dx$$

Optimal. Leaf size=372

$$2\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \frac{\sqrt[4]{3} \sqrt{a+bx} (bc-ad)^{4/3}}{\sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

[Out] $-2*(d*x+c)^{(1/6)} / (-a*d+b*c) / (b*x+a)^{(1/2)} - 2/3*(d*x+c)^{(1/6)} * ((-a*d+b*c)^{(1/3)} - b^{(1/3)}*(d*x+c)^{(1/3)}) * (((-a*d+b*c)^{(1/3)} - b^{(1/3)}*(d*x+c)^{(1/3)}) * (1+3^{(1/2)}))^{(1/2)} / (((-a*d+b*c)^{(1/3)} - b^{(1/3)}*(d*x+c)^{(1/3)}) * (1+3^{(1/2)}))^{(1/2)} / (((-a*d+b*c)^{(1/3)} - b^{(1/3)}*(d*x+c)^{(1/3)}) * (1+3^{(1/2)}))^{(1/2)} * (((-a*d+b*c)^{(1/3)} - b^{(1/3)}*(d*x+c)^{(1/3)}) * (1+3^{(1/2)}))^{(1/2)} * \operatorname{EllipticF}(((1 - ((-a*d+b*c)^{(1/3)} - b^{(1/3)}*(d*x+c)^{(1/3)}) * (1+3^{(1/2)}))^{(1/2)} / (((-a*d+b*c)^{(1/3)} - b^{(1/3)}*(d*x+c)^{(1/3)}) * (1+3^{(1/2)}))^{(1/2)})^{(1/2)}, 1/4*6^{(1/2)} + 1/4*2^{(1/2)}) * (((-a*d+b*c)^{(2/3)} + b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)} + b^{(2/3)}*(d*x+c)^{(2/3)}) / (((-a*d+b*c)^{(1/3)} - b^{(1/3)}*(d*x+c)^{(1/3)}) * (1+3^{(1/2)}))^{(1/2)} * 3^{(3/4)} / (-a*d+b*c)^{(4/3)} / (b*x+a)^{(1/2)} / (-b^{(1/3)}*(d*x+c)^{(1/3)} * ((-a*d+b*c)^{(1/3)} - b^{(1/3)}*(d*x+c)^{(1/3)}) / (((-a*d+b*c)^{(1/3)} - b^{(1/3)}*(d*x+c)^{(1/3)}) * (1+3^{(1/2)}))^{(1/2)}$

Rubi [A] time = 0.23, antiderivative size = 372, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {51, 63, 225}

$$2\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right) \\ \frac{\sqrt[4]{3} \sqrt{a+bx} (bc-ad)^{4/3}}{\sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/2)*(c + d*x)^(5/6)), x]

[Out] $(-2*(c+d*x)^{(1/6)}) / ((b*c-a*d)*\operatorname{Sqrt}[a+b*x]) - (2*(c+d*x)^{(1/6)} * ((b*c-a*d)^{(1/3)} - b^{(1/3)}*(c+d*x)^{(1/3)}) * \operatorname{Sqrt}(((b*c-a*d)^{(2/3)} + b^{(1/3)}*(b*c-a*d)^{(1/3)}*(c+d*x)^{(1/3)} + b^{(2/3)}*(c+d*x)^{(2/3)}) / (((b*c-a*d)^{(1/3)} - (1+\operatorname{Sqrt}[3])*b^{(1/3)}*(c+d*x)^{(1/3)})^{(1/2)} * \operatorname{EllipticF}[\operatorname{ArcCos}(((b*c-a*d)^{(1/3)} - (1-\operatorname{Sqrt}[3])*b^{(1/3)}*(c+d*x)^{(1/3)}) / ((b*c-a*d)^{(1/3)} - (1+\operatorname{Sqrt}[3])*b^{(1/3)}*(c+d*x)^{(1/3)})], (2+\operatorname{Sqrt}[3])/4]) / (3^{(1/4)}*(b*c-a*d)$

$$\text{)^{(4/3)} * \text{Sqrt}[a + b*x] * \text{Sqrt}[-((b^{(1/3)} * (c + d*x)^{(1/3)} * (b*c - a*d)^{(1/3)} - b^{(1/3)} * (c + d*x)^{(1/3)}) / ((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3]) * b^{(1/3)} * (c + d*x)^{(1/3)})^2]]$$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x] /; FreeQ[{a, b}, x
]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/6}} dx &= -\frac{2\sqrt[6]{c+dx}}{(bc-ad)\sqrt{a+bx}} - \frac{(2d) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/6}} dx}{3(bc-ad)} \\
&= -\frac{2\sqrt[6]{c+dx}}{(bc-ad)\sqrt{a+bx}} - \frac{4 \operatorname{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{bc-ad} \\
&= -\frac{2\sqrt[6]{c+dx}}{(bc-ad)\sqrt{a+bx}} - \frac{2\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{bc-ad} \sqrt[3]{c+dx}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \right)}}}{\sqrt[3]{bc-ad} - (1+\sqrt{3})} \\
&= -\frac{2\sqrt[6]{c+dx}}{(bc-ad)\sqrt{a+bx}} - \frac{\sqrt[4]{3} (bc-ad)^{4/3} \sqrt{a+bx}}{\sqrt[4]{3} (bc-ad)^{4/3} \sqrt{a+bx}}
\end{aligned}$$

Mathematica [C] time = 0.02, size = 71, normalized size = 0.19

$$-\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{5/6} {}_2F_1 \left(-\frac{1}{2}, \frac{5}{6}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt{a+bx}(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(5/6)), x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[-1/2, 5/6, 1/2, (d*(a + b*x))/(-b*c + a*d)]/(b*Sqrt[a + b*x]*(c + d*x)^(5/6))

fricas [F] time = 0.68, size = 0, normalized size = 0.00

$$\operatorname{integral} \left(\frac{\sqrt{bx+a}(dx+c)^{1/6}}{b^2dx^3+a^2c+(b^2c+2abd)x^2+(2abc+a^2d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(5/6), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/6)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{3/2}(dx+c)^{5/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(5/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(5/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{3}{2}} (dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(5/6),x)

[Out] int(1/(b*x+a)^(3/2)/(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{3}{2}} (dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(5/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} (c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(5/6)),x)

[Out] int(1/((a + b*x)^(3/2)*(c + d*x)^(5/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} (c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(5/6),x)

[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(5/6)), x)

$$3.1759 \quad \int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/6}} dx$$

Optimal. Leaf size=410

$$\frac{16d\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} \operatorname{EllipticF} \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right)}{9\sqrt[4]{3} \sqrt{a+bx} (bc-ad)^{7/3} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}}{}$$

[Out] $-2/3*(d*x+c)^{(1/6)/(-a*d+b*c)/(b*x+a)^{(3/2)+16/9*d*(d*x+c)^{(1/6)/(-a*d+b*c)^2/(b*x+a)^{(1/2)+16/27*d*(d*x+c)^{(1/6)*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)}*(1-3^{(1/2))})^2/((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)}*(1+3^{(1/2))})^2})^{(1/2)/((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)}*(1-3^{(1/2))})^2/((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)}*(1+3^{(1/2))})^2})^{(1/2),1/4*6^{(1/2)+1/4*2^{(1/2)}*((-a*d+b*c)^{(2/3)+b^{(1/3)*(-a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)+b^{(2/3)*(d*x+c)^{(2/3))}/((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)}*(1+3^{(1/2))})^2})^{(1/2)}*3^{(3/4)/(-a*d+b*c)^{(7/3)/(b*x+a)^{(1/2)/(-b^{(1/3)*(d*x+c)^{(1/3)*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)}*(1+3^{(1/2))})^2})^{(1/2)}$

Rubi [A] time = 0.27, antiderivative size = 410, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {51, 63, 225}

$$\frac{16d\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + (bc-ad)^{2/3} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} F \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right)}{9\sqrt[4]{3} \sqrt{a+bx} (bc-ad)^{7/3} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}}{}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a+b*x)^{(5/2)*(c+d*x)^{(5/6))}, x]$

[Out] $(-2*(c+d*x)^{(1/6))/(3*(b*c-a*d)*(a+b*x)^{(3/2)}) + (16*d*(c+d*x)^{(1/6))/(9*(b*c-a*d)^2*\operatorname{Sqrt}[a+b*x]) + (16*d*(c+d*x)^{(1/6)*((b*c-a*d)^{(1/3)-b^{(1/3)*(c+d*x)^{(1/3)}*\operatorname{Sqrt}[(b*c-a*d)^{(2/3)+b^{(1/3)*(b*c-a*d)^{(1/3)*(c+d*x)^{(1/3)+b^{(2/3)*(c+d*x)^{(2/3))}/((b*c-a*d)^{(1/3)-(1+\operatorname{Sqrt}[3])*b^{(1/3)*(c+d*x)^{(1/3)})^2})*\operatorname{EllipticF}[\operatorname{ArcCos}[(b*c-a*d)^{(1/3)-$

$$\frac{(1 - \sqrt{3})b^{1/3}(c + dx)^{1/3}}{(b^2c - a^2d)^{1/3} - (1 + \sqrt{3})b^{1/3}(c + dx)^{1/3}} \cdot \frac{(2 + \sqrt{3})/4}{(9 \cdot 3^{1/4})(b^2c - a^2d)^{7/3} \sqrt{a + bx} \sqrt{-(b^{1/3}(c + dx)^{1/3}((b^2c - a^2d)^{1/3} - b^{1/3}(c + dx)^{1/3})) / ((b^2c - a^2d)^{1/3} - (1 + \sqrt{3})b^{1/3}(c + dx)^{1/3})^2}}$$

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[
n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])]/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/2}(c+dx)^{5/6}} dx &= -\frac{2\sqrt[6]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} - \frac{(8d) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{5/6}} dx}{9(bc-ad)} \\
&= -\frac{2\sqrt[6]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{16d\sqrt[6]{c+dx}}{9(bc-ad)^2\sqrt{a+bx}} + \frac{(16d^2) \int \frac{1}{\sqrt{a+bx}(c+dx)^{5/6}} dx}{27(bc-ad)^2} \\
&= -\frac{2\sqrt[6]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{16d\sqrt[6]{c+dx}}{9(bc-ad)^2\sqrt{a+bx}} + \frac{(32d) \text{Subst} \left(\int \frac{1}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{9(bc-ad)^2} \\
&= -\frac{2\sqrt[6]{c+dx}}{3(bc-ad)(a+bx)^{3/2}} + \frac{16d\sqrt[6]{c+dx}}{9(bc-ad)^2\sqrt{a+bx}} + \frac{16d\sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{9(bc-ad)^2}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 73, normalized size = 0.18

$$\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{5/6} {}_2F_1 \left(-\frac{3}{2}, \frac{5}{6}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(a+bx)^{3/2}(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(5/6)), x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[-3/2, 5/6, -1/2, (d*(a + b*x))/(-b*c) + a*d])/(3*b*(a + b*x)^(3/2)*(c + d*x)^(5/6))

fricas [F] time = 0.76, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a}(dx+c)^{\frac{1}{6}}}{b^3dx^4 + a^3c + (b^3c + 3ab^2d)x^3 + 3(ab^2c + a^2bd)x^2 + (3a^2bc + a^3d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(5/6), x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(1/6)/(b^3*d*x^4 + a^3*c + (b^3*c + 3*a*b^2*d)*x^3 + 3*(a*b^2*c + a^2*b*d)*x^2 + (3*a^2*b*c + a^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(5/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(5/6)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(5/6),x)

[Out] int(1/(b*x+a)^(5/2)/(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(5/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{2}}(c+dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/2)*(c + d*x)^(5/6)),x)

[Out] int(1/((a + b*x)^(5/2)*(c + d*x)^(5/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{2}}(c+dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(5/2)/(d*x+c)**(5/6),x)
```

```
[Out] Integral(1/((a + b*x)**(5/2)*(c + d*x)**(5/6)), x)
```

$$3.1760 \quad \int \frac{(a+bx)^{5/2}}{(c+dx)^{7/6}} dx$$

Optimal. Leaf size=880

$$\frac{6(a+bx)^{5/2}}{d\sqrt[6]{c+dx}} + \frac{45b(c+dx)^{5/6}(a+bx)^{3/2}}{7d^2} - \frac{405b(bc-ad)(c+dx)^{5/6}\sqrt{a+bx}}{56d^3} - \frac{1215(1+\sqrt{3})\sqrt[3]{b}(bc-ad)^2\sqrt[6]{c+dx}}{112d^3(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b})}$$

[Out] $-6*(b*x+a)^{(5/2)}/d/(d*x+c)^{(1/6)}+45/7*b*(b*x+a)^{(3/2)}*(d*x+c)^{(5/6)}/d^2-405/56*b*(-a*d+b*c)*(d*x+c)^{(5/6)}*(b*x+a)^{(1/2)}/d^3-1215/112*b^{(1/3)}*(-a*d+b*c)^2*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/d^3/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))-1215/112*3^{(1/4)}*b^{(1/3)}*(-a*d+b*c)^{(7/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/d^4/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}-405/224*3^{(3/4)}*b^{(1/3)}*(-a*d+b*c)^{(7/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/d^4/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.90, antiderivative size = 880, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {47, 50, 63, 308, 225, 1881}

$$\frac{6(a+bx)^{5/2}}{d\sqrt[6]{c+dx}} + \frac{45b(c+dx)^{5/6}(a+bx)^{3/2}}{7d^2} - \frac{405b(bc-ad)(c+dx)^{5/6}\sqrt{a+bx}}{56d^3} - \frac{1215(1+\sqrt{3})\sqrt[3]{b}(bc-ad)^2\sqrt[6]{c+dx}}{112d^3(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/2)/(c + d*x)^(7/6), x]

[Out] (-6*(a + b*x)^(5/2))/(d*(c + d*x)^(1/6)) - (405*b*(b*c - a*d)*Sqrt[a + b*x] * (c + d*x)^(5/6))/(56*d^3) + (45*b*(a + b*x)^(3/2)*(c + d*x)^(5/6))/(7*d^2) - (1215*(1 + Sqrt[3])*b^(1/3)*(b*c - a*d)^2*Sqrt[a + b*x]*(c + d*x)^(1/6)) / (112*d^3*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) - (1215*3^(1/4)*b^(1/3)*(b*c - a*d)^(7/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)) * (c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3)] / ((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2 * EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3)) / ((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4]) / (112*d^4*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))) / ((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]) - (405*3^(3/4)*(1 - Sqrt[3])*b^(1/3)*(b*c - a*d)^(7/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)) * (c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3)] / ((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2 * EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3)) / ((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4]) / (224*d^4*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))) / ((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2])]

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
```

```
(b*(m + n + 1)), Int[(a + b*x)^(m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rule 308

```
Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a,
3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a
+ b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqr
t[a + b*x^6], x], x]] /; FreeQ[{a, b}, x]
```

Rule 1881

```
Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r =
Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqr
t[a + b*x^6]/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x
*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*El
lipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + S
qrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sq
rt[a + b*x^6]), x]] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1
- Sqrt[3])*d, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/2}}{(c+dx)^{7/6}} dx &= -\frac{6(a+bx)^{5/2}}{d\sqrt[6]{c+dx}} + \frac{(15b) \int \frac{(a+bx)^{3/2}}{\sqrt[6]{c+dx}} dx}{d} \\
&= -\frac{6(a+bx)^{5/2}}{d\sqrt[6]{c+dx}} + \frac{45b(a+bx)^{3/2}(c+dx)^{5/6}}{7d^2} - \frac{(135b(bc-ad)) \int \frac{\sqrt{a+bx}}{\sqrt[6]{c+dx}} dx}{14d^2} \\
&= -\frac{6(a+bx)^{5/2}}{d\sqrt[6]{c+dx}} - \frac{405b(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56d^3} + \frac{45b(a+bx)^{3/2}(c+dx)^{5/6}}{7d^2} + \frac{(405b(bc-a}}{14d^2} \\
&= -\frac{6(a+bx)^{5/2}}{d\sqrt[6]{c+dx}} - \frac{405b(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56d^3} + \frac{45b(a+bx)^{3/2}(c+dx)^{5/6}}{7d^2} + \frac{(1215b(bc-a}}{14d^2} \\
&= -\frac{6(a+bx)^{5/2}}{d\sqrt[6]{c+dx}} - \frac{405b(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56d^3} + \frac{45b(a+bx)^{3/2}(c+dx)^{5/6}}{7d^2} - \frac{(1215\sqrt[3]{b}(bc-a}}{14d^2} \\
&= -\frac{6(a+bx)^{5/2}}{d\sqrt[6]{c+dx}} - \frac{405b(bc-ad)\sqrt{a+bx}(c+dx)^{5/6}}{56d^3} + \frac{45b(a+bx)^{3/2}(c+dx)^{5/6}}{7d^2} - \frac{1215(1+\sqrt{3})}{112d^3} \left(\frac{\sqrt[3]{bc-a}}{d} \right)
\end{aligned}$$

Mathematica [C] time = 0.08, size = 73, normalized size = 0.08

$$\frac{2(a+bx)^{7/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{7/6} {}_2F_1 \left(\frac{7}{6}, \frac{7}{2}; \frac{9}{2}; \frac{d(a+bx)}{ad-bc} \right)}{7b(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/2)/(c + d*x)^(7/6), x]

[Out] (2*(a + b*x)^(7/2)*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[7/6, 7/2, 9/2, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*(c + d*x)^(7/6))

fricas [F] time = 0.96, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(b^2x^2 + 2abx + a^2)\sqrt{bx+a}(dx+c)^{5/6}}{d^2x^2 + 2cdx + c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(7/6),x, algorithm="fricas")

[Out] integral((b^2*x^2 + 2*a*b*x + a^2)*sqrt(b*x + a)*(d*x + c)^(5/6)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(7/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/2)/(d*x + c)^(7/6), x)

maple [F] time = 0.13, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/2)/(d*x+c)^(7/6),x)

[Out] int((b*x+a)^(5/2)/(d*x+c)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{2}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/2)/(d*x+c)^(7/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/2)/(d*x + c)^(7/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{5/2}}{(c + dx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(5/2)/(c + d*x)^(7/6), x)
```

```
[Out] int((a + b*x)^(5/2)/(c + d*x)^(7/6), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(a + bx)^{\frac{5}{2}}}{(c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(5/2)/(d*x+c)**(7/6), x)
```

```
[Out] Integral((a + b*x)**(5/2)/(c + d*x)**(7/6), x)
```

$$3.1761 \quad \int \frac{(a+bx)^{3/2}}{(c+dx)^{7/6}} dx$$

Optimal. Leaf size=844

$$\frac{6(a+bx)^{3/2}}{d\sqrt[6]{c+dx}} + \frac{27b(c+dx)^{5/6}\sqrt{a+bx}}{4d^2} + \frac{81(1+\sqrt{3})\sqrt[3]{b}(bc-ad)\sqrt[6]{c+dx}\sqrt{a+bx}}{8d^2(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} + \frac{81\sqrt[4]{3}\sqrt[3]{b}(bc-ad)^{4/3}\sqrt[6]{c+dx}}{8d^2(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})}$$

[Out] $-6*(b*x+a)^{(3/2)}/d/(d*x+c)^{(1/6)}+27/4*b*(d*x+c)^{(5/6)}*(b*x+a)^{(1/2)}/d^2+81/8*b^{(1/3)}*(-a*d+b*c)*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/d^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))+81/8*3^{(1/4)}*b^{(1/3)}*(-a*d+b*c)^{(4/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/d^3/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}+27/16*3^{(3/4)}*b^{(1/3)}*(-a*d+b*c)^{(4/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/d^3/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}$

Rubi [A] time = 0.77, antiderivative size = 844, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.316, Rules used = {47, 50, 63, 308, 225, 1881}

$$-\frac{6(a+bx)^{3/2}}{d\sqrt[6]{c+dx}} + \frac{27b(c+dx)^{5/6}\sqrt{a+bx}}{4d^2} + \frac{81(1+\sqrt{3})\sqrt[3]{b}(bc-ad)\sqrt[6]{c+dx}\sqrt{a+bx}}{8d^2(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} + \frac{81\sqrt[4]{3}\sqrt[3]{b}(bc-ad)^{4/3}\sqrt[6]{c+dx}}{8d^2(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(3/2)/(c + d*x)^(7/6), x]

[Out] (-6*(a + b*x)^(3/2))/(d*(c + d*x)^(1/6)) + (27*b*Sqrt[a + b*x]*(c + d*x)^(5/6))/(4*d^2) + (81*(1 + Sqrt[3])*b^(1/3)*(b*c - a*d)*Sqrt[a + b*x]*(c + d*x)^(1/6))/(8*d^2*((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))) + (81*3^(1/4)*b^(1/3)*(b*c - a*d)^(4/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticE[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(8*d^3*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)]) + (27*3^(3/4)*(1 - Sqrt[3])*b^(1/3)*(b*c - a*d)^(4/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))]/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4)]/(16*d^3*Sqrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*(b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2)])

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)),
Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) &&
!(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
```

$c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{GtQ}[n, 0] \&\& \text{NeQ}[m + n + 1, 0] \&\& \text{!(IGtQ}[m, 0] \&\& (\text{!IntegerQ}[n] \mid\mid (\text{GtQ}[m, 0] \&\& \text{LtQ}[m - n, 0]))) \&\& \text{!ILtQ}[m + n + 2, 0] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\text{Int}[(a_.) + (b_.)*(x_)^m]*((c_.) + (d_.)*(x_)^n), x_Symbol] \text{:> With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{p*(m+1)-1}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] \text{/; FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 225

$\text{Int}[1/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \text{:> With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticF}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])]/(2*3^{(1/4)}*s*\text{Sqrt}[a + b*x^6]*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]), x]] \text{/; FreeQ}\{a, b\}, x]$

Rule 308

$\text{Int}[(x_)^4/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \text{:> With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Dist}[(\text{Sqrt}[3] - 1)*s^2/(2*r^2), \text{Int}[1/\text{Sqrt}[a + b*x^6], x], x] - \text{Dist}[1/(2*r^2), \text{Int}[(\text{Sqrt}[3] - 1)*s^2 - 2*r^2*x^4]/\text{Sqrt}[a + b*x^6], x], x]] \text{/; FreeQ}\{a, b\}, x]$

Rule 1881

$\text{Int}[(c_) + (d_.)*(x_)^4]/\text{Sqrt}[(a_) + (b_.)*(x_)^6], x_Symbol] \text{:> With}\{r = \text{Numer}[\text{Rt}[b/a, 3]], s = \text{Denom}[\text{Rt}[b/a, 3]]\}, \text{Simp}[(1 + \text{Sqrt}[3])*d*s^3*x*\text{Sqrt}[a + b*x^6]/(2*a*r^2*(s + (1 + \text{Sqrt}[3])*r*x^2)), x] - \text{Simp}[(3^{(1/4)}*d*s*x*(s + r*x^2)*\text{Sqrt}[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{EllipticE}[\text{ArcCos}[(s + (1 - \text{Sqrt}[3])*r*x^2)/(s + (1 + \text{Sqrt}[3])*r*x^2)], (2 + \text{Sqrt}[3])/4])]/(2*r^2*\text{Sqrt}[(r*x^2*(s + r*x^2))/(s + (1 + \text{Sqrt}[3])*r*x^2)^2]*\text{Sqrt}[a + b*x^6]), x]] \text{/; FreeQ}\{a, b, c, d\}, x] \&\& \text{EqQ}[2*\text{Rt}[b/a, 3]^2*c - (1 - \text{Sqrt}[3])*d, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{3/2}}{(c+dx)^{7/6}} dx &= -\frac{6(a+bx)^{3/2}}{d\sqrt[6]{c+dx}} + \frac{(9b) \int \frac{\sqrt{a+bx}}{\sqrt[6]{c+dx}} dx}{d} \\
&= -\frac{6(a+bx)^{3/2}}{d\sqrt[6]{c+dx}} + \frac{27b\sqrt{a+bx}(c+dx)^{5/6}}{4d^2} - \frac{(27b(bc-ad)) \int \frac{1}{\sqrt{a+bx}\sqrt[6]{c+dx}} dx}{8d^2} \\
&= -\frac{6(a+bx)^{3/2}}{d\sqrt[6]{c+dx}} + \frac{27b\sqrt{a+bx}(c+dx)^{5/6}}{4d^2} - \frac{(81b(bc-ad)) \text{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{4d^3} \\
&= -\frac{6(a+bx)^{3/2}}{d\sqrt[6]{c+dx}} + \frac{27b\sqrt{a+bx}(c+dx)^{5/6}}{4d^2} + \frac{(81\sqrt[3]{b}(bc-ad)) \text{Subst} \left(\int \frac{(-1+\sqrt{3})(bc-ad)^{2/3}-2b^{2/3}x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx \right)}{8d^3} \\
&= -\frac{6(a+bx)^{3/2}}{d\sqrt[6]{c+dx}} + \frac{27b\sqrt{a+bx}(c+dx)^{5/6}}{4d^2} + \frac{81(1+\sqrt{3})\sqrt[3]{b}(bc-ad)\sqrt{a+bx}\sqrt[6]{c+dx}}{8d^2(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} + \frac{81\sqrt[4]{b}}{8d^2}
\end{aligned}$$

Mathematica [C] time = 0.07, size = 73, normalized size = 0.09

$$\frac{2(a+bx)^{5/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{7/6} {}_2F_1 \left(\frac{7}{6}, \frac{5}{2}; \frac{7}{2}; \frac{d(a+bx)}{ad-bc} \right)}{5b(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(3/2)/(c + d*x)^(7/6), x]

[Out] (2*(a + b*x)^(5/2)*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[7/6, 5/2, 7/2, (d*(a + b*x))/(-b*c + a*d)]/(5*b*(c + d*x)^(7/6))

fricas [F] time = 1.02, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{3}{2}}(dx+c)^{\frac{5}{6}}}{d^2x^2+2cdx+c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(7/6),x, algorithm="fricas")

[Out] integral((b*x + a)^(3/2)*(d*x + c)^(5/6)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(7/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(7/6), x)

maple [F] time = 0.13, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(3/2)/(d*x+c)^(7/6),x)

[Out] int((b*x+a)^(3/2)/(d*x+c)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{3}{2}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(3/2)/(d*x+c)^(7/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(3/2)/(d*x + c)^(7/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{3/2}}{(c + dx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(3/2)/(c + d*x)^(7/6),x)

```
[Out] int((a + b*x)^(3/2)/(c + d*x)^(7/6), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(a + bx)^{\frac{3}{2}}}{(c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(3/2)/(d*x+c)**(7/6),x)
```

```
[Out] Integral((a + b*x)**(3/2)/(c + d*x)**(7/6), x)
```


$$3.1762 \quad \int \frac{\sqrt{a+bx}}{(c+dx)^{7/6}} dx$$

Optimal. Leaf size=806

$$\frac{9\sqrt[4]{3} \sqrt[3]{b} \sqrt[3]{bc-ad} \sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}} E \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad}}{\sqrt[3]{bc-ad}} \right)}{d^2 \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx} \right)^2}}}$$

[Out] $-6*(b*x+a)^{(1/2)}/d/(d*x+c)^{(1/6)}-9*b^{(1/3)}*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/d/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))-9*3^{(1/4)}*b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^{2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2}})^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^{2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2}})^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2}})^{(1/2)}/d^{2/2}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2}})^{(1/2)}-3/2*3^{(3/4)}*b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/6)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^{2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2}})^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1-3^{(1/2)}))^{2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2}})^{(1/2)}, 1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2}})^{(1/2)}/d^{2/2}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^{2}})^{(1/2)}$

Rubi [A] time = 0.67, antiderivative size = 806, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {47, 63, 308, 225, 1881}

$$\frac{9\sqrt[4]{3}\sqrt[3]{b}\sqrt[3]{bc-ad}\sqrt[6]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)\sqrt{\frac{(bc-ad)^{2/3}+\sqrt[3]{b}\sqrt[3]{c+dx}\sqrt[3]{bc-ad}+b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}E\left(\cos^{-1}\left(\frac{\sqrt[3]{bc-ad}-\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}}\right)}{d^2\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}}}{d^2\sqrt{a+bx}\sqrt{-\frac{\sqrt[3]{b}\sqrt[3]{c+dx}\left(\sqrt[3]{bc-ad}-\sqrt[3]{b}\sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad}-(1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx}\right)^2}}}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*x]/(c + d*x)^(7/6), x]

[Out]
$$\begin{aligned} & (-6\sqrt{a+bx})/(d(c+d*x)^{1/6}) - (9(1+\sqrt{3})b^{1/3}\sqrt{a+bx} \\ & * (c+d*x)^{1/6})/(d((b*c-a*d)^{1/3} - (1+\sqrt{3})b^{1/3}(c+d*x)^{1/3})) - (9*3^{1/4}b^{1/3}(b*c-a*d)^{1/3}(c+d*x)^{1/6} \\ & * ((b*c-a*d)^{1/3} - b^{1/3}(c+d*x)^{1/3})\sqrt{((b*c-a*d)^{2/3} + b^{1/3}(b*c-a*d)^{1/3}(c+d*x)^{1/3} + b^{2/3}(c+d*x)^{2/3})} \\ & / ((b*c-a*d)^{1/3} - (1+\sqrt{3})b^{1/3}(c+d*x)^{1/3})^2 * \text{EllipticE}[\text{ArcCos}[\frac{(b*c-a*d)^{1/3} - (1-\sqrt{3})b^{1/3}(c+d*x)^{1/3}}{(b*c-a*d)^{1/3} - (1+\sqrt{3})b^{1/3}(c+d*x)^{1/3}}], (2+\sqrt{3})/4]) \\ & / (d^2\sqrt{a+bx}\sqrt{-(b^{1/3}(c+d*x)^{1/3}((b*c-a*d)^{1/3} - b^{1/3}(c+d*x)^{1/3}))/((b*c-a*d)^{1/3} - (1+\sqrt{3})b^{1/3}(c+d*x)^{1/3})^2}}) \\ & - (3*3^{3/4}(1-\sqrt{3})b^{1/3}(b*c-a*d)^{1/3}(c+d*x)^{1/6} * ((b*c-a*d)^{1/3} - b^{1/3}(c+d*x)^{1/3})\sqrt{((b*c-a*d)^{2/3} + b^{1/3}(b*c-a*d)^{1/3}(c+d*x)^{1/3} + b^{2/3}(c+d*x)^{2/3})} \\ & / ((b*c-a*d)^{1/3} - (1+\sqrt{3})b^{1/3}(c+d*x)^{1/3})^2 * \text{EllipticF}[\text{ArcCos}[\frac{(b*c-a*d)^{1/3} - (1-\sqrt{3})b^{1/3}(c+d*x)^{1/3}}{(b*c-a*d)^{1/3} - (1+\sqrt{3})b^{1/3}(c+d*x)^{1/3}}], (2+\sqrt{3})/4]) \\ & / (2*d^2\sqrt{a+bx}\sqrt{-(b^{1/3}(c+d*x)^{1/3}((b*c-a*d)^{1/3} - b^{1/3}(c+d*x)^{1/3}))/((b*c-a*d)^{1/3} - (1+\sqrt{3})b^{1/3}(c+d*x)^{1/3})^2}}) \end{aligned}$$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &&
& IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den

ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rule 308

```
Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a,
3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a
+ b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqr
t[a + b*x^6], x], x]] /; FreeQ[{a, b}, x]
```

Rule 1881

```
Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r =
Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqr
t[a + b*x^6])/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x
*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*El
lipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + S
qrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sq
rt[a + b*x^6]), x]] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1
- Sqrt[3])*d, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt{a+bx}}{(c+dx)^{7/6}} dx &= -\frac{6\sqrt{a+bx}}{d\sqrt[6]{c+dx}} + \frac{(3b) \int \frac{1}{\sqrt{a+bx} \sqrt[6]{c+dx}} dx}{d} \\
&= -\frac{6\sqrt{a+bx}}{d\sqrt[6]{c+dx}} + \frac{(18b) \text{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{d^2} \\
&= -\frac{6\sqrt{a+bx}}{d\sqrt[6]{c+dx}} - \frac{(9\sqrt[3]{b}) \text{Subst} \left(\int \frac{(-1+\sqrt{3})(bc-ad)^{2/3}-2b^{2/3}x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{d^2} - \frac{(9(1-\sqrt{3})\sqrt[3]{b}(bc-ad)^{2/3})}{d^2} \\
&= -\frac{6\sqrt{a+bx}}{d\sqrt[6]{c+dx}} - \frac{9(1+\sqrt{3})\sqrt[3]{b}\sqrt{a+bx}\sqrt[6]{c+dx}}{d(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} - \frac{9^4\sqrt[3]{b}\sqrt[3]{bc-ad}\sqrt[6]{c+dx}(\sqrt[3]{bc-ad})}{d^2}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.09

$$\frac{2(a+bx)^{3/2} \left(\frac{b(c+dx)}{bc-ad} \right)^{7/6} {}_2F_1 \left(\frac{7}{6}, \frac{3}{2}; \frac{5}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[a + b*x]/(c + d*x)^(7/6), x]

[Out] (2*(a + b*x)^(3/2)*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[7/6, 3/2, 5/2, (d*(a + b*x))/(-b*c) + a*d])/(3*b*(c + d*x)^(7/6))

fricas [F] time = 0.97, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a}(dx+c)^{5/6}}{d^2x^2+2cdx+c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/2)/(d*x+c)^(7/6), x, algorithm="fricas")

[Out] `integral(sqrt(b*x + a)*(d*x + c)^(5/6)/(d^2*x^2 + 2*c*d*x + c^2), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)/(d*x+c)^(7/6),x, algorithm="giac")`

[Out] `integrate(sqrt(b*x + a)/(d*x + c)^(7/6), x)`

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(1/2)/(d*x+c)^(7/6),x)`

[Out] `int((b*x+a)^(1/2)/(d*x+c)^(7/6),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{bx+a}}{(dx+c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/2)/(d*x+c)^(7/6),x, algorithm="maxima")`

[Out] `integrate(sqrt(b*x + a)/(d*x + c)^(7/6), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{\sqrt{a+bx}}{(c+dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/2)/(c + d*x)^(7/6),x)`

[Out] `int((a + b*x)^(1/2)/(c + d*x)^(7/6), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt{a + bx}}{(c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/2)/(d*x+c)**(7/6),x)

[Out] Integral(sqrt(a + b*x)/(c + d*x)**(7/6), x)

$$3.1763 \quad \int \frac{1}{\sqrt{a+bx} (c+dx)^{7/6}} dx$$

Optimal. Leaf size=817

$$6\sqrt[4]{3} \sqrt[3]{b} \sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}} E \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right)$$

$$d(bc-ad)^{2/3} \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}}$$

[Out] $6*(b*x+a)^{(1/2)/(-a*d+b*c)/(d*x+c)^{(1/6)}+6*b^{(1/3)*(d*x+c)^{(1/6)*(1+3^{(1/2)})}$
 $)*(b*x+a)^{(1/2)/(-a*d+b*c)/((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})}$
 $2)))+6*3^{(1/4)*b^{(1/3)*(d*x+c)^{(1/6)*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)}$
 $)}*(((a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2)})})^2/((-a*d+b*c)^{(1/3)}$
 $-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)/((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*$
 $x+c)^{(1/3)*(1-3^{(1/2)})})*((a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})}$
 $)*EllipticE((1-((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2)})})^2/((-a*$
 $d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)}, 1/4*6^{(1/2)+1/4*2^{(1/2)}$
 $)*(((a*d+b*c)^{(2/3)+b^{(1/3)*(-a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)+b^{(2/3)*(d*$
 $*x+c)^{(2/3)/((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)/$
 $d/((-a*d+b*c)^{(2/3)/(b*x+a)^{(1/2)/(-b^{(1/3)*(d*x+c)^{(1/3)*((-a*d+b*c)^{(1/3)-$
 $b^{(1/3)*(d*x+c)^{(1/3)/((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})$
 $)^2)^{(1/2)+3^{(3/4)*b^{(1/3)*(d*x+c)^{(1/6)*((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)}$
 $)}*(((a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2)})})^2/((-a*d+b*c)^{(1/3)-$
 $b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)/((-a*d+b*c)^{(1/3)-b^{(1/3)*}$
 $(d*x+c)^{(1/3)*(1-3^{(1/2)})})*((a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)}$
 $2)))*EllipticF((1-((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2)})})^2/((-$
 $-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})^2)^{(1/2)}, 1/4*6^{(1/2)+1/4$
 $*2^{(1/2)}*(1-3^{(1/2)})*(((a*d+b*c)^{(2/3)+b^{(1/3)*(-a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)+b^{(2/3)*(d*$
 $1/3)+b^{(2/3)*(d*x+c)^{(2/3)/((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2)})})$
 $)^2)^{(1/2)/d/((-a*d+b*c)^{(2/3)/(b*x+a)^{(1/2)/(-b^{(1/3)*(d*x+c)^{(1/3)*((-$
 $a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)/((-a*d+b*c)^{(1/3)-b^{(1/3)*(d*x+c)^{(1/3)$
 $3)*(1+3^{(1/2)})})^2)^{(1/2)}$

Rubi [A] time = 0.67, antiderivative size = 817, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {51, 63, 308, 225, 1881}

$$6\sqrt[4]{3} \sqrt[3]{b} \sqrt[6]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx} \right) \sqrt{\frac{(bc-ad)^{2/3} + \sqrt[3]{b} \sqrt[3]{c+dx} \sqrt[3]{bc-ad} + b^{2/3}(c+dx)^{2/3}}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}} E \left(\cos^{-1} \left(\frac{\sqrt[3]{bc-ad} - (1-\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}}{\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}} \right) \right)$$

$$d(bc-ad)^{2/3} \sqrt{a+bx} \sqrt{-\frac{\sqrt[3]{b} \sqrt[3]{c+dx} \left(\sqrt[3]{bc-ad} - \sqrt[3]{b} \sqrt[3]{c+dx}\right)}{\left(\sqrt[3]{bc-ad} - (1+\sqrt{3}) \sqrt[3]{b} \sqrt[3]{c+dx}\right)^2}}$$

Antiderivative was successfully verified.

```
[In] Int[1/(Sqrt[a + b*x]*(c + d*x)^(7/6)),x]
```

```
[Out] (6*Sqrt[a + b*x])/((b*c - a*d)*(c + d*x)^(1/6)) + (6*(1 + Sqrt[3])*b^(1/3)*
Sqrt[a + b*x]*(c + d*x)^(1/6))/((b*c - a*d)*((b*c - a*d)^(1/3) - (1 + Sqrt[
3])*b^(1/3)*(c + d*x)^(1/3))) + (6*3^(1/4)*b^(1/3)*(c + d*x)^(1/6)*((b*c -
a*d)^(1/3) - b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*
c - a*d)^(1/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))/((b*c - a*d)^(1/3
) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]*EllipticE[ArcCos[((b*c - a*d)
^(1/3) - (1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + S
qrt[3])*b^(1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4])/((d*(b*c - a*d)^(2/3)*S
qrt[a + b*x]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(
c + d*x)^(1/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3
))^2])) + (3^(3/4)*(1 - Sqrt[3])*b^(1/3)*(c + d*x)^(1/6)*((b*c - a*d)^(1/3)
- b^(1/3)*(c + d*x)^(1/3))*Sqrt[((b*c - a*d)^(2/3) + b^(1/3)*(b*c - a*d)^(1
/3)*(c + d*x)^(1/3) + b^(2/3)*(c + d*x)^(2/3))/((b*c - a*d)^(1/3) - (1 + Sq
rt[3])*b^(1/3)*(c + d*x)^(1/3))^2]*EllipticF[ArcCos[((b*c - a*d)^(1/3) - (1
- Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(
1/3)*(c + d*x)^(1/3))], (2 + Sqrt[3])/4])/((d*(b*c - a*d)^(2/3)*Sqrt[a + b*x
]*Sqrt[-((b^(1/3)*(c + d*x)^(1/3)*((b*c - a*d)^(1/3) - b^(1/3)*(c + d*x)^(1
/3)))/((b*c - a*d)^(1/3) - (1 + Sqrt[3])*b^(1/3)*(c + d*x)^(1/3))^2]))]
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x]
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
```


]

Rule 308

Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a + b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqrt[a + b*x^6], x], x] /; FreeQ[{a, b}, x]

Rule 1881

Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqrt[a + b*x^6])/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sqrt[a + b*x^6]), x] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1 - Sqrt[3])*d, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{\sqrt{a+bx}(c+dx)^{7/6}} dx &= \frac{6\sqrt{a+bx}}{(bc-ad)\sqrt[6]{c+dx}} - \frac{(2b) \int \frac{1}{\sqrt{a+bx}\sqrt[6]{c+dx}} dx}{bc-ad} \\
 &= \frac{6\sqrt{a+bx}}{(bc-ad)\sqrt[6]{c+dx}} - \frac{(12b) \text{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{d(bc-ad)} \\
 &= \frac{6\sqrt{a+bx}}{(bc-ad)\sqrt[6]{c+dx}} + \frac{(6\sqrt[3]{b}) \text{Subst} \left(\int \frac{(-1+\sqrt{3})(bc-ad)^{2/3}-2b^{2/3}x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx, x, \sqrt[6]{c+dx} \right)}{d(bc-ad)} + \dots \\
 &= \frac{6\sqrt{a+bx}}{(bc-ad)\sqrt[6]{c+dx}} + \frac{6(1+\sqrt{3})\sqrt[3]{b}\sqrt{a+bx}\sqrt[6]{c+dx}}{(bc-ad)(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} + \frac{6^4\sqrt{3}\sqrt[3]{b}\sqrt[6]{c+dx}}{\dots}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.09

$$\frac{2\sqrt{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{7/6} {}_2F_1\left(\frac{1}{2}, \frac{7}{6}; \frac{3}{2}; \frac{d(a+bx)}{ad-bc}\right)}{b(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/(Sqrt[a + b*x]*(c + d*x)^(7/6)),x]

[Out] (2*Sqrt[a + b*x]*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[1/2, 7/6, 3/2, (d*(a + b*x))/(-b*c) + a*d])/(b*(c + d*x)^(7/6))

fricas [F] time = 1.15, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\sqrt{bx+a}(dx+c)^{5/6}}{bd^2x^3+ac^2+(2bcd+ad^2)x^2+(bc^2+2acd)x},x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(7/6),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/6)/(b*d^2*x^3 + a*c^2 + (2*b*c*d + a*d^2)*x^2 + (b*c^2 + 2*a*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(7/6),x, algorithm="giac")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(7/6)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/2)/(d*x+c)^(7/6),x)

[Out] int(1/(b*x+a)^(1/2)/(d*x+c)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{bx+a}(dx+c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/2)/(d*x+c)^(7/6),x, algorithm="maxima")

[Out] integrate(1/(sqrt(b*x + a)*(d*x + c)^(7/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/2)*(c + d*x)^(7/6)),x)

[Out] int(1/((a + b*x)^(1/2)*(c + d*x)^(7/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt{a+bx}(c+dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/2)/(d*x+c)**(7/6),x)

[Out] Integral(1/(sqrt(a + b*x)*(c + d*x)**(7/6)), x)

$$3.1764 \quad \int \frac{1}{(a+bx)^{3/2}(c+dx)^{7/6}} dx$$

Optimal. Leaf size=844

$$\frac{8\sqrt{a+bx}d}{(bc-ad)^2\sqrt[6]{c+dx}} - \frac{8(1+\sqrt{3})\sqrt[3]{b}\sqrt{a+bx}\sqrt[6]{c+dx}d}{(bc-ad)^2(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} - \frac{8\sqrt[4]{3}\sqrt[3]{b}\sqrt[6]{c+dx}(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx})}{(bc-ad)^2(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})}$$

[Out]
$$\frac{-2/(-a*d+b*c)/(d*x+c)^{(1/6)/(b*x+a)^{(1/2)}-8*d*(b*x+a)^{(1/2)/(-a*d+b*c)^{2/(d*x+c)^{(1/6)}-8*b^{(1/3)*d*(d*x+c)^{(1/6)*(1+3^{(1/2))}(b*x+a)^{(1/2)/(-a*d+b*c)^{2/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})-8*3^{(1/4)*b^{(1/3)*(d*x+c)^{(1/6)*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3))}*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2))})^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})^2)^{(1/2)/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2))})}*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})})*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2))})^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)*(-a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)}+b^{(2/3)*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})^2)^{(1/2)/(-a*d+b*c)^{(5/3)/(b*x+a)^{(1/2)/(-b^{(1/3)*(d*x+c)^{(1/3)*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})^2)^{(1/2)}-4/3*b^{(1/3)*(d*x+c)^{(1/6)*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3))}*(((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2))})^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})^2)^{(1/2)/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2))})}*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})})*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1-3^{(1/2))})^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)})*(((-a*d+b*c)^{(2/3)}+b^{(1/3)*(-a*d+b*c)^{(1/3)*(d*x+c)^{(1/3)}+b^{(2/3)*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})^2)^{(1/2)}*3^{(3/4)/(-a*d+b*c)^{(5/3)/(b*x+a)^{(1/2)/(-b^{(1/3)*(d*x+c)^{(1/3)*((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)*(d*x+c)^{(1/3)*(1+3^{(1/2))})^2)^{(1/2)}$$

Rubi [A] time = 0.76, antiderivative size = 844, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {51, 63, 308, 225, 1881}

$$\frac{8\sqrt{a+bx}d}{(bc-ad)^2\sqrt[6]{c+dx}} - \frac{8(1+\sqrt{3})\sqrt[3]{b}\sqrt{a+bx}\sqrt[6]{c+dx}d}{(bc-ad)^2(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} - \frac{8\sqrt[4]{3}\sqrt[3]{b}\sqrt[6]{c+dx}(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx})}{(bc-ad)^2(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(3/2)*(c + d*x)^(7/6)),x]

[Out]
$$\begin{aligned} & -2/((b*c - a*d)*\text{Sqrt}[a + b*x]*(c + d*x)^{(1/6)}) - (8*d*\text{Sqrt}[a + b*x])/((b*c - a*d)^2*(c + d*x)^{(1/6)}) - (8*(1 + \text{Sqrt}[3])*b^{(1/3)}*d*\text{Sqrt}[a + b*x]*(c + d*x)^{(1/6)})/((b*c - a*d)^2*((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})) - (8*3^{(1/4)}*b^{(1/3)}*(c + d*x)^{(1/6)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}))*\text{Sqrt}[(b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)}]/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2*\text{EllipticE}[\text{ArcCos}[(b*c - a*d)^{(1/3)} - (1 - \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)}]/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})], (2 + \text{Sqrt}[3])/4])/((b*c - a*d)^{(5/3)}*\text{Sqrt}[a + b*x]*\text{Sqrt}[-(b^{(1/3)}*(c + d*x)^{(1/3)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}))/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2]) - (4*(1 - \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/6)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}))*\text{Sqrt}[(b*c - a*d)^{(2/3)} + b^{(1/3)}*(b*c - a*d)^{(1/3)}*(c + d*x)^{(1/3)} + b^{(2/3)}*(c + d*x)^{(2/3)}]/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2*\text{EllipticF}[\text{ArcCos}[(b*c - a*d)^{(1/3)} - (1 - \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)}]/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})], (2 + \text{Sqrt}[3])/4)]/(3^{(1/4)}*(b*c - a*d)^{(5/3)}*\text{Sqrt}[a + b*x]*\text{Sqrt}[-(b^{(1/3)}*(c + d*x)^{(1/3)}*((b*c - a*d)^{(1/3)} - b^{(1/3)}*(c + d*x)^{(1/3)}))/((b*c - a*d)^{(1/3)} - (1 + \text{Sqrt}[3])*b^{(1/3)}*(c + d*x)^{(1/3)})^2]) \end{aligned}$$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 225

Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])]/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr

```
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2], x]] /; FreeQ[{a, b}, x]
```

Rule 308

```
Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a + b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqrt[a + b*x^6], x], x]] /; FreeQ[{a, b}, x]
```

Rule 1881

```
Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqrt[a + b*x^6])/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sqrt[a + b*x^6]), x]] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1 - Sqrt[3])*d, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{3/2}(c+dx)^{7/6}} dx &= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[6]{c+dx}} - \frac{(4d) \int \frac{1}{\sqrt{a+bx}(c+dx)^{7/6}} dx}{3(bc-ad)} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[6]{c+dx}} - \frac{8d\sqrt{a+bx}}{(bc-ad)^2\sqrt[6]{c+dx}} + \frac{(8bd) \int \frac{1}{\sqrt{a+bx}\sqrt[6]{c+dx}} dx}{3(bc-ad)^2} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[6]{c+dx}} - \frac{8d\sqrt{a+bx}}{(bc-ad)^2\sqrt[6]{c+dx}} + \frac{(16b) \text{Subst} \left(\int \frac{x^4}{\sqrt{a-\frac{bc}{d}+\frac{bx^6}{d}}} dx \right)}{(bc-ad)^2} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[6]{c+dx}} - \frac{8d\sqrt{a+bx}}{(bc-ad)^2\sqrt[6]{c+dx}} - \frac{(8\sqrt[3]{b}) \text{Subst} \left(\int \frac{(-1+\sqrt{3})(bc-a)}{\sqrt{a-\frac{bc}{d}}} dx \right)}{(bc-ad)^2} \\
&= -\frac{2}{(bc-ad)\sqrt{a+bx}\sqrt[6]{c+dx}} - \frac{8d\sqrt{a+bx}}{(bc-ad)^2\sqrt[6]{c+dx}} - \frac{8(1+\sqrt{3})\sqrt[3]{b}d\sqrt{a+bx}}{(bc-ad)^2(\sqrt[3]{bc-ad} - (1+\sqrt{3}))}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.08

$$-\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{7/6} {}_2F_1 \left(-\frac{1}{2}, \frac{7}{6}; \frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt{a+bx}(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(3/2)*(c + d*x)^(7/6)),x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[-1/2, 7/6, 1/2, (d*(a + b*x))/(-b*c + a*d)])/(b*Sqrt[a + b*x]*(c + d*x)^(7/6))

fricas [F] time = 1.20, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a}(dx+c)^{\frac{5}{6}}}{b^2d^2x^4 + a^2c^2 + 2(b^2cd + abd^2)x^3 + (b^2c^2 + 4abcd + a^2d^2)x^2 + 2(abc^2 + a^2cd)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(7/6),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/6)/(b^2*d^2*x^4 + a^2*c^2 + 2*(b^2*c*d + a*b*d^2)*x^3 + (b^2*c^2 + 4*a*b*c*d + a^2*d^2)*x^2 + 2*(a*b*c^2 + a^2*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{3}{2}}(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(7/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(7/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{3}{2}}(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(3/2)/(d*x+c)^(7/6),x)

[Out] int(1/(b*x+a)^(3/2)/(d*x+c)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{3}{2}}(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(3/2)/(d*x+c)^(7/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(3/2)*(d*x + c)^(7/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + bx)^{3/2}(c + dx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(3/2)*(c + d*x)^(7/6)),x)


```
[Out] int(1/((a + b*x)^(3/2)*(c + d*x)^(7/6)), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{1}{(a + bx)^{\frac{3}{2}} (c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(3/2)/(d*x+c)**(7/6), x)
```

```
[Out] Integral(1/((a + b*x)**(3/2)*(c + d*x)**(7/6)), x)
```

$$3.1765 \quad \int \frac{1}{(a+bx)^{5/2}(c+dx)^{7/6}} dx$$

Optimal. Leaf size=893

$$\frac{80\sqrt{a+bx}d^2}{9(bc-ad)^3\sqrt[6]{c+dx}} + \frac{80(1+\sqrt{3})\sqrt[3]{b}\sqrt{a+bx}\sqrt[6]{c+dx}d^2}{9(bc-ad)^3(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} + \frac{80\sqrt[3]{b}\sqrt[6]{c+dx}(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx})}{3^3}$$

[Out]
$$\begin{aligned} & -2/3/(-a*d+b*c)/(b*x+a)^{(3/2)}/(d*x+c)^{(1/6)}+20/9*d/(-a*d+b*c)^2/(d*x+c)^{(1/6)}/(b*x+a)^{(1/2)}+80/9*d^2*(b*x+a)^{(1/2)}/(-a*d+b*c)^3/(d*x+c)^{(1/6)}+80/9*b^{(1/3)}*d^2*(d*x+c)^{(1/6)}*(1+3^{(1/2)})*(b*x+a)^{(1/2)}/(-a*d+b*c)^3/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))+80/9*b^{(1/3)}*d*(d*x+c)^{(1/6)}*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticE((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*3^{(1/4)}/(-a*d+b*c)^{(8/3)}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}+40/27*b^{(1/3)}*d*(d*x+c)^{(1/6)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)})*(((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)}))*EllipticF((1-((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)},1/4*6^{(1/2)}+1/4*2^{(1/2)})*(1-3^{(1/2)})*((a*d+b*c)^{(2/3)}+b^{(1/3)}*(-a*d+b*c)^{(1/3)}*(d*x+c)^{(1/3)}+b^{(2/3)}*(d*x+c)^{(2/3)})/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)}*3^{(3/4)}/(-a*d+b*c)^{(8/3)}/(b*x+a)^{(1/2)}/(-b^{(1/3)}*(d*x+c)^{(1/3)}*((a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}))/((-a*d+b*c)^{(1/3)}-b^{(1/3)}*(d*x+c)^{(1/3)}*(1+3^{(1/2)})))^2)^{(1/2)} \end{aligned}$$

Rubi [A] time = 0.87, antiderivative size = 893, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$

= 0.263, Rules used = {51, 63, 308, 225, 1881}

$$\frac{80\sqrt{a+bx}d^2}{9(bc-ad)^3\sqrt[6]{c+dx}} + \frac{80(1+\sqrt{3})\sqrt[3]{b}\sqrt{a+bx}\sqrt[6]{c+dx}d^2}{9(bc-ad)^3(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})} + \frac{80\sqrt[3]{b}\sqrt[6]{c+dx}(\sqrt[3]{bc-ad} - \sqrt[3]{b}\sqrt[3]{c+dx})}{9(bc-ad)^3(\sqrt[3]{bc-ad} - (1+\sqrt{3})\sqrt[3]{b}\sqrt[3]{c+dx})}$$

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Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/2)*(c + d*x)^(7/6)),x]

[Out]
$$-2/(3*(b*c - a*d)*(a + b*x)^{(3/2)*(c + d*x)^{(1/6))} + (20*d)/(9*(b*c - a*d)^2*\sqrt{a + b*x}*(c + d*x)^{(1/6))} + (80*d^2*\sqrt{a + b*x})/(9*(b*c - a*d)^3*(c + d*x)^{(1/6))} + (80*(1 + \sqrt{3})*b^{(1/3)*d^2*\sqrt{a + b*x}*(c + d*x)^{(1/6))}/(9*(b*c - a*d)^3*((b*c - a*d)^{(1/3)} - (1 + \sqrt{3})*b^{(1/3)*(c + d*x)^{(1/3))}) + (80*b^{(1/3)*d*(c + d*x)^{(1/6))*((b*c - a*d)^{(1/3)} - b^{(1/3)*(c + d*x)^{(1/3)})*\sqrt{((b*c - a*d)^{(2/3)} + b^{(1/3)*(b*c - a*d)^{(1/3)*(c + d*x)^{(1/3)} + b^{(2/3)*(c + d*x)^{(2/3))}/((b*c - a*d)^{(1/3)} - (1 + \sqrt{3})*b^{(1/3)*(c + d*x)^{(1/3)})^2}*EllipticE[ArcCos[((b*c - a*d)^{(1/3)} - (1 - \sqrt{3})*b^{(1/3)*(c + d*x)^{(1/3))}/((b*c - a*d)^{(1/3)} - (1 + \sqrt{3})*b^{(1/3)*(c + d*x)^{(1/3)})], (2 + \sqrt{3})/4)/(3*3^{(3/4)*(b*c - a*d)^{(8/3)*\sqrt{a + b*x}*\sqrt{-((b^{(1/3)*(c + d*x)^{(1/3))*((b*c - a*d)^{(1/3)} - b^{(1/3)*(c + d*x)^{(1/3))}/((b*c - a*d)^{(1/3)} - (1 + \sqrt{3})*b^{(1/3)*(c + d*x)^{(1/3)})^2})} + (40*(1 - \sqrt{3})*b^{(1/3)*d*(c + d*x)^{(1/6))*((b*c - a*d)^{(1/3)} - b^{(1/3)*(c + d*x)^{(1/3)})*\sqrt{((b*c - a*d)^{(2/3)} + b^{(1/3)*(b*c - a*d)^{(1/3)*(c + d*x)^{(1/3)} + b^{(2/3)*(c + d*x)^{(2/3))}/((b*c - a*d)^{(1/3)} - (1 + \sqrt{3})*b^{(1/3)*(c + d*x)^{(1/3)})^2}*EllipticF[ArcCos[((b*c - a*d)^{(1/3)} - (1 - \sqrt{3})*b^{(1/3)*(c + d*x)^{(1/3))}/((b*c - a*d)^{(1/3)} - (1 + \sqrt{3})*b^{(1/3)*(c + d*x)^{(1/3)})], (2 + \sqrt{3})/4)/(9*3^{(1/4)*(b*c - a*d)^{(8/3)*\sqrt{a + b*x}*\sqrt{-((b^{(1/3)*(c + d*x)^{(1/3))*((b*c - a*d)^{(1/3)} - b^{(1/3)*(c + d*x)^{(1/3))}/((b*c - a*d)^{(1/3)} - (1 + \sqrt{3})*b^{(1/3)*(c + d*x)^{(1/3)})^2})]$$

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +

```
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 225

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a, 3]],
s = Denom[Rt[b/a, 3]]}, Simp[(x*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/
(s + (1 + Sqrt[3])*r*x^2)^2]*EllipticF[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s
+ (1 + Sqrt[3])*r*x^2)], (2 + Sqrt[3])/4])/(2*3^(1/4)*s*Sqrt[a + b*x^6]*Sqr
t[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]), x]] /; FreeQ[{a, b}, x
]
```

Rule 308

```
Int[(x_)^4/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r = Numer[Rt[b/a,
3]], s = Denom[Rt[b/a, 3]]}, Dist[((Sqrt[3] - 1)*s^2)/(2*r^2), Int[1/Sqrt[a
+ b*x^6], x], x] - Dist[1/(2*r^2), Int[((Sqrt[3] - 1)*s^2 - 2*r^2*x^4)/Sqr
t[a + b*x^6], x], x]] /; FreeQ[{a, b}, x]
```

Rule 1881

```
Int[((c_) + (d_.)*(x_)^4)/Sqrt[(a_) + (b_.)*(x_)^6], x_Symbol] := With[{r =
Numer[Rt[b/a, 3]], s = Denom[Rt[b/a, 3]]}, Simp[((1 + Sqrt[3])*d*s^3*x*Sqr
t[a + b*x^6])/(2*a*r^2*(s + (1 + Sqrt[3])*r*x^2)), x] - Simp[(3^(1/4)*d*s*x
*(s + r*x^2)*Sqrt[(s^2 - r*s*x^2 + r^2*x^4)/(s + (1 + Sqrt[3])*r*x^2)^2]*El
lipticE[ArcCos[(s + (1 - Sqrt[3])*r*x^2)/(s + (1 + Sqrt[3])*r*x^2)], (2 + S
qrt[3])/4])/(2*r^2*Sqrt[(r*x^2*(s + r*x^2))/(s + (1 + Sqrt[3])*r*x^2)^2]*Sq
rt[a + b*x^6]), x]] /; FreeQ[{a, b, c, d}, x] && EqQ[2*Rt[b/a, 3]^2*c - (1
- Sqrt[3])*d, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/2}(c+dx)^{7/6}} dx &= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[6]{c+dx}} - \frac{(10d) \int \frac{1}{(a+bx)^{3/2}(c+dx)^{7/6}} dx}{9(bc-ad)} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[6]{c+dx}} + \frac{20d}{9(bc-ad)^2\sqrt{a+bx}\sqrt[6]{c+dx}} + \frac{(40d^2) \int \frac{1}{\sqrt{a+bx}}}{27(bc-ad)} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[6]{c+dx}} + \frac{20d}{9(bc-ad)^2\sqrt{a+bx}\sqrt[6]{c+dx}} + \frac{80d^2\sqrt{a+bx}}{9(bc-ad)^3\sqrt[6]{c+dx}} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[6]{c+dx}} + \frac{20d}{9(bc-ad)^2\sqrt{a+bx}\sqrt[6]{c+dx}} + \frac{80d^2\sqrt{a+bx}}{9(bc-ad)^3\sqrt[6]{c+dx}} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[6]{c+dx}} + \frac{20d}{9(bc-ad)^2\sqrt{a+bx}\sqrt[6]{c+dx}} + \frac{80d^2\sqrt{a+bx}}{9(bc-ad)^3\sqrt[6]{c+dx}} \\
&= -\frac{2}{3(bc-ad)(a+bx)^{3/2}\sqrt[6]{c+dx}} + \frac{20d}{9(bc-ad)^2\sqrt{a+bx}\sqrt[6]{c+dx}} + \frac{80d^2\sqrt{a+bx}}{9(bc-ad)^3\sqrt[6]{c+dx}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.08

$$-\frac{2 \left(\frac{b(c+dx)}{bc-ad} \right)^{7/6} {}_2F_1 \left(-\frac{3}{2}, \frac{7}{6}; -\frac{1}{2}; \frac{d(a+bx)}{ad-bc} \right)}{3b(a+bx)^{3/2}(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/2)*(c + d*x)^(7/6)),x]

[Out] (-2*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[-3/2, 7/6, -1/2, (d*(a + b*x))/(-b*c + a*d)]/(3*b*(a + b*x)^(3/2)*(c + d*x)^(7/6))

fricas [F] time = 0.87, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{\sqrt{bx+a}(dx+c)^{\frac{5}{6}}}{b^3d^2x^5 + a^3c^2 + (2b^3cd + 3ab^2d^2)x^4 + (b^3c^2 + 6ab^2cd + 3a^2bd^2)x^3 + (3ab^2c^2 + 6a^2bcd + a^3d^2)x^2 + \dots} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(7/6),x, algorithm="fricas")

[Out] integral(sqrt(b*x + a)*(d*x + c)^(5/6)/(b^3*d^2*x^5 + a^3*c^2 + (2*b^3*c*d + 3*a*b^2*d^2)*x^4 + (b^3*c^2 + 6*a*b^2*c*d + 3*a^2*b*d^2)*x^3 + (3*a*b^2*c^2 + 6*a^2*b*c*d + a^3*d^2)*x^2 + (3*a^2*b*c^2 + 2*a^3*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(7/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(7/6)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/2)/(d*x+c)^(7/6),x)

[Out] int(1/(b*x+a)^(5/2)/(d*x+c)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{2}}(dx+c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/2)/(d*x+c)^(7/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/2)*(d*x + c)^(7/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{5/2}(c+dx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(5/2)*(c + d*x)^(7/6)), x)`

[Out] `int(1/((a + b*x)^(5/2)*(c + d*x)^(7/6)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{5}{2}} (c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/2)/(d*x+c)**(7/6), x)`

[Out] `Integral(1/((a + b*x)**(5/2)*(c + d*x)**(7/6)), x)`

3.1766 $\int \sqrt[6]{a+bx} (c+dx)^{13/6} dx$

Optimal. Leaf size=84

$$\frac{6(a+bx)^{7/6} \sqrt[6]{c+dx} (bc-ad)^2 {}_2F_1\left(-\frac{13}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b^3 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

[Out] $6/7*(-a*d+b*c)^2*(b*x+a)^{(7/6)}*(d*x+c)^{(1/6)}*\text{hypergeom}([-13/6, 7/6], [13/6], -d*(b*x+a)/(-a*d+b*c))/b^3/(b*(d*x+c)/(-a*d+b*c))^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{7/6} \sqrt[6]{c+dx} (bc-ad)^2 {}_2F_1\left(-\frac{13}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b^3 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)*(c + d*x)^(13/6), x]

[Out] $(6*(b*c - a*d)^2*(a + b*x)^{(7/6)}*(c + d*x)^{(1/6)}*\text{Hypergeometric2F1}[-13/6, 7/6, 13/6, -((d*(a + b*x))/(b*c - a*d))])/(7*b^3*((b*(c + d*x))/(b*c - a*d))^{(1/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/(b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n], Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \sqrt[6]{a+bx} (c+dx)^{13/6} dx = \frac{((bc-ad)^2 \sqrt[6]{c+dx}) \int \sqrt[6]{a+bx} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad} \right)^{13/6} dx}{b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

$$= \frac{6(bc-ad)^2 (a+bx)^{7/6} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{13}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b^3 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Mathematica [A] time = 0.11, size = 73, normalized size = 0.87

$$\frac{6(a+bx)^{7/6} (c+dx)^{13/6} {}_2F_1\left(-\frac{13}{6}, \frac{7}{6}; \frac{13}{6}; \frac{d(a+bx)}{ad-bc}\right)}{7b \left(\frac{b(c+dx)}{bc-ad}\right)^{13/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)*(c + d*x)^(13/6), x]

[Out] (6*(a + b*x)^(7/6)*(c + d*x)^(13/6)*Hypergeometric2F1[-13/6, 7/6, 13/6, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*((b*(c + d*x))/(b*c - a*d))^(13/6))

fricas [F] time = 0.74, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(d^2x^2 + 2cdx + c^2\right)(bx + a)^{\frac{1}{6}}(dx + c)^{\frac{13}{6}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)*(d*x+c)^(13/6), x, algorithm="fricas")

[Out] integral((d^2*x^2 + 2*c*d*x + c^2)*(b*x + a)^(1/6)*(d*x + c)^(13/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{6}}(dx + c)^{\frac{13}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)*(d*x+c)^(13/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)*(d*x + c)^(13/6), x)

maple [F] time = 0.19, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{6}} (dx + c)^{\frac{13}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)*(d*x+c)^(13/6),x)

[Out] int((b*x+a)^(1/6)*(d*x+c)^(13/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{6}} (dx + c)^{\frac{13}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)*(d*x+c)^(13/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)*(d*x + c)^(13/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{1/6} (c + dx)^{13/6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/6)*(c + d*x)^(13/6),x)

[Out] int((a + b*x)^(1/6)*(c + d*x)^(13/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/6)*(d*x+c)**(13/6),x)

[Out] Timed out

3.1767 $\int \sqrt[6]{a + bx} (c + dx)^{7/6} dx$

Optimal. Leaf size=82

$$\frac{6(a + bx)^{7/6} \sqrt[6]{c + dx} (bc - ad) {}_2F_1\left(-\frac{7}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

[Out] $6/7*(-a*d+b*c)*(b*x+a)^{(7/6)}*(d*x+c)^{(1/6)}*\text{hypergeom}([-7/6, 7/6], [13/6], -d*(b*x+a)/(-a*d+b*c))/b^2/(b*(d*x+c)/(-a*d+b*c))^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a + bx)^{7/6} \sqrt[6]{c + dx} (bc - ad) {}_2F_1\left(-\frac{7}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(1/6)}*(c + d*x)^{(7/6)}, x]$

[Out] $(6*(b*c - a*d)*(a + b*x)^{(7/6)}*(c + d*x)^{(1/6)}*\text{Hypergeometric2F1}[-7/6, 7/6, 13/6, -((d*(a + b*x))/(b*c - a*d))])/(7*b^2*((b*(c + d*x))/(b*c - a*d))^{(1/6)})$

Rule 69

$\text{Int}[(a_ + (b_)*x_)^{(m_)}*((c_ + (d_)*x_))^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& \text{GtQ}[b/(b*c - a*d), 0] \&\& (\text{RationalQ}[m] \parallel !(\text{RationalQ}[n] \&\& \text{GtQ}[-(d/(b*c - a*d)), 0]))$

Rule 70

$\text{Int}[(a_ + (b_)*x_)^{(m_)}*((c_ + (d_)*x_))^{(n_)}, x_Symbol] \rightarrow \text{Dist}[(c + d*x)^{\text{FracPart}[n]}/(b/(b*c - a*d))^{\text{IntPart}[n]}*((b*(c + d*x))/(b*c - a*d))^{\text{FracPart}[n]}], \text{Int}[(a + b*x)^m*\text{Simp}[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& (\text{RationalQ}[m] \parallel !\text{SimplerQ}[n + 1, m + 1])$

Rubi steps

$$\int \sqrt[6]{a+bx} (c+dx)^{7/6} dx = \frac{((bc-ad)\sqrt[6]{c+dx}) \int \sqrt[6]{a+bx} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{7/6} dx}{b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

$$= \frac{6(bc-ad)(a+bx)^{7/6} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{7}{6}, \frac{7}{6}, \frac{13}{6}, -\frac{d(a+bx)}{bc-ad}\right)}{7b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Mathematica [A] time = 0.06, size = 73, normalized size = 0.89

$$\frac{6(a+bx)^{7/6}(c+dx)^{7/6} {}_2F_1\left(-\frac{7}{6}, \frac{7}{6}, \frac{13}{6}, \frac{d(a+bx)}{ad-bc}\right)}{7b \left(\frac{b(c+dx)}{bc-ad}\right)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)*(c + d*x)^(7/6), x]

[Out] (6*(a + b*x)^(7/6)*(c + d*x)^(7/6)*Hypergeometric2F1[-7/6, 7/6, 13/6, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*((b*(c + d*x))/(b*c - a*d))^(7/6))

fricas [F] time = 0.64, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bx+a\right)^{\frac{1}{6}}(dx+c)^{\frac{7}{6}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)*(d*x+c)^(7/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/6)*(d*x + c)^(7/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx+a)^{\frac{1}{6}}(dx+c)^{\frac{7}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)*(d*x+c)^(7/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)*(d*x + c)^(7/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{6}} (dx + c)^{\frac{7}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)*(d*x+c)^(7/6),x)

[Out] int((b*x+a)^(1/6)*(d*x+c)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{6}} (dx + c)^{\frac{7}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)*(d*x+c)^(7/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)*(d*x + c)^(7/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{1/6} (c + dx)^{7/6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/6)*(c + d*x)^(7/6),x)

[Out] int((a + b*x)^(1/6)*(c + d*x)^(7/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt[6]{a + bx} (c + dx)^{\frac{7}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/6)*(d*x+c)**(7/6),x)

[Out] Integral((a + b*x)**(1/6)*(c + d*x)**(7/6), x)

3.1768 $\int \sqrt[6]{a+bx} \sqrt[6]{c+dx} dx$

Optimal. Leaf size=74

$$\frac{6(a+bx)^{7/6} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

[Out] $6/7*(b*x+a)^{(7/6)}*(d*x+c)^{(1/6)}*\text{hypergeom}([-1/6, 7/6], [13/6], -d*(b*x+a)/(-a*d+b*c))/b/(b*(d*x+c)/(-a*d+b*c))^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{7/6} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)*(c + d*x)^(1/6), x]

[Out] $(6*(a + b*x)^{(7/6)}*(c + d*x)^{(1/6)}*\text{Hypergeometric2F1}[-1/6, 7/6, 13/6, -((d*(a + b*x))/(b*c - a*d))])/ (7*b*((b*(c + d*x))/(b*c - a*d))^{(1/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/ (b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \sqrt[6]{a+bx} \sqrt[6]{c+dx} dx = \frac{\sqrt[6]{c+dx} \int \sqrt[6]{a+bx} \sqrt{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}} dx}{\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

$$= \frac{6(a+bx)^{7/6} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Mathematica [A] time = 0.04, size = 73, normalized size = 0.99

$$\frac{6(a+bx)^{7/6} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{7}{6}; \frac{13}{6}; \frac{d(a+bx)}{ad-bc}\right)}{7b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)*(c + d*x)^(1/6), x]

[Out] (6*(a + b*x)^(7/6)*(c + d*x)^(1/6)*Hypergeometric2F1[-1/6, 7/6, 13/6, (d*(a + b*x))/(-(b*c) + a*d)])/(7*b*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [F] time = 0.67, size = 0, normalized size = 0.00

$$\text{integral}\left((bx+a)^{\frac{1}{6}}(dx+c)^{\frac{1}{6}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)*(d*x+c)^(1/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/6)*(d*x + c)^(1/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx+a)^{\frac{1}{6}}(dx+c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)*(d*x+c)^(1/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)*(d*x + c)^(1/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{6}} (dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(1/6)*(d*x+c)^(1/6),x)`

[Out] `int((b*x+a)^(1/6)*(d*x+c)^(1/6),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{6}} (dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/6)*(d*x+c)^(1/6),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(1/6)*(d*x + c)^(1/6), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{1/6} (c + dx)^{1/6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/6)*(c + d*x)^(1/6),x)`

[Out] `int((a + b*x)^(1/6)*(c + d*x)^(1/6), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt[6]{a + bx} \sqrt[6]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/6)*(d*x+c)**(1/6),x)`

[Out] `Integral((a + b*x)**(1/6)*(c + d*x)**(1/6), x)`

$$3.1769 \quad \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{5/6}} dx$$

Optimal. Leaf size=74

$$\frac{6(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{5}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b(c+dx)^{5/6}}$$

[Out] $6/7*(b*x+a)^{(7/6)}*(b*(d*x+c)/(-a*d+b*c))^{(5/6)}*\text{hypergeom}([5/6, 7/6], [13/6], -d*(b*x+a)/(-a*d+b*c))/b/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{5}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)/(c + d*x)^(5/6), x]

[Out] $(6*(a + b*x)^{(7/6)}*((b*(c + d*x))/(b*c - a*d))^{(5/6)}*\text{Hypergeometric2F1}[5/6, 7/6, 13/6, -((d*(a + b*x))/(b*c - a*d))]/(7*b*(c + d*x)^{(5/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{5/6}} dx = \frac{\left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} \int \frac{\sqrt[6]{a+bx}}{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{5/6}} dx}{(c+dx)^{5/6}}$$

$$= \frac{6(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{5}{6}, \frac{7}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7b(c+dx)^{5/6}}$$

Mathematica [A] time = 0.04, size = 73, normalized size = 0.99

$$\frac{6(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{5}{6}, \frac{7}{6}; \frac{13}{6}; \frac{d(a+bx)}{ad-bc}\right)}{7b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)/(c + d*x)^(5/6), x]

[Out] (6*(a + b*x)^(7/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[5/6, 7/6, 13/6, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*(c + d*x)^(5/6))

fricas [F] time = 0.91, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{6}}}{(dx+c)^{\frac{5}{6}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(5/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/6)/(d*x + c)^(5/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{6}}}{(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(5/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(5/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)/(d*x+c)^(5/6),x)

[Out] int((b*x+a)^(1/6)/(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{1/6}}{(c + dx)^{5/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/6)/(c + d*x)^(5/6),x)

[Out] int((a + b*x)^(1/6)/(c + d*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{a + bx}}{(c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/6)/(d*x+c)**(5/6),x)

[Out] Integral((a + b*x)**(1/6)/(c + d*x)**(5/6), x)

$$3.1770 \quad \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{11/6}} dx$$

Optimal. Leaf size=81

$$\frac{6(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{7}{6}, \frac{11}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7(c+dx)^{5/6}(bc-ad)}$$

[Out] $6/7*(b*x+a)^{(7/6)}*(b*(d*x+c)/(-a*d+b*c))^{(5/6)}*\text{hypergeom}([7/6, 11/6], [13/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{7}{6}, \frac{11}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7(c+dx)^{5/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)/(c + d*x)^(11/6), x]

[Out] $(6*(a + b*x)^{(7/6)}*((b*(c + d*x))/(b*c - a*d))^{(5/6)}*\text{Hypergeometric2F1}[7/6, 11/6, 13/6, -((d*(a + b*x))/(b*c - a*d))]/(7*(b*c - a*d)*(c + d*x)^{(5/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{11/6}} dx = \frac{\left(b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}\right) \int \frac{\sqrt[6]{a+bx}}{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{11/6}} dx}{(bc-ad)(c+dx)^{5/6}}$$

$$= \frac{6(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{7}{6}, \frac{11}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7(bc-ad)(c+dx)^{5/6}}$$

Mathematica [A] time = 0.07, size = 73, normalized size = 0.90

$$\frac{6(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{11/6} {}_2F_1\left(\frac{7}{6}, \frac{11}{6}; \frac{13}{6}; \frac{d(a+bx)}{ad-bc}\right)}{7b(c+dx)^{11/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)/(c + d*x)^(11/6), x]

[Out] (6*(a + b*x)^(7/6)*((b*(c + d*x))/(b*c - a*d))^(11/6)*Hypergeometric2F1[7/6, 11/6, 13/6, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*(c + d*x)^(11/6))

fricas [F] time = 0.67, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{1}{6}}}{d^2x^2+2cdx+c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(11/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/6)*(d*x + c)^(1/6)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{6}}}{(dx+c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(11/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(11/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)/(d*x+c)^(11/6),x)

[Out] int((b*x+a)^(1/6)/(d*x+c)^(11/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(11/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(11/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{1}{6}}}{(c + dx)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/6)/(c + d*x)^(11/6),x)

[Out] int((a + b*x)^(1/6)/(c + d*x)^(11/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{a + bx}}{(c + dx)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/6)/(d*x+c)**(11/6),x)

[Out] Integral((a + b*x)**(1/6)/(c + d*x)**(11/6), x)

$$3.1771 \quad \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{17/6}} dx$$

Optimal. Leaf size=82

$$\frac{6b(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{7}{6}, \frac{17}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7(c+dx)^{5/6}(bc-ad)^2}$$

[Out] $6/7*b*(b*x+a)^{(7/6)}*(b*(d*x+c)/(-a*d+b*c))^{(5/6)}*hypergeom([7/6, 17/6], [13/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^2/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6b(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{7}{6}, \frac{17}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7(c+dx)^{5/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)/(c + d*x)^(17/6), x]

[Out] $(6*b*(a + b*x)^{(7/6)}*((b*(c + d*x))/(b*c - a*d))^{(5/6)}*Hypergeometric2F1[7/6, 17/6, 13/6, -((d*(a + b*x))/(b*c - a*d))]/(7*(b*c - a*d)^2*(c + d*x)^{(5/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{17/6}} dx = \frac{\left(b^2 \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}\right) \int \frac{\sqrt[6]{a+bx}}{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{17/6}} dx}{(bc-ad)^2 (c+dx)^{5/6}}$$

$$= \frac{6b(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{7}{6}, \frac{17}{6}; \frac{13}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{7(bc-ad)^2 (c+dx)^{5/6}}$$

Mathematica [A] time = 0.05, size = 81, normalized size = 0.99

$$\frac{6b(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{7}{6}, \frac{17}{6}; \frac{13}{6}; \frac{d(a+bx)}{ad-bc}\right)}{7(c+dx)^{5/6} (bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)/(c + d*x)^(17/6), x]

[Out] (6*b*(a + b*x)^(7/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[7/6, 17/6, 13/6, (d*(a + b*x))/(-(b*c) + a*d)]/(7*(b*c - a*d)^2*(c + d*x)^(5/6))

fricas [F] time = 0.71, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{1}{6}}}{d^3x^3+3cd^2x^2+3c^2dx+c^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(17/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/6)*(d*x + c)^(1/6)/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{6}}}{(dx+c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(17/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(17/6), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)/(d*x+c)^(17/6), x)

[Out] int((b*x+a)^(1/6)/(d*x+c)^(17/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(17/6), x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(17/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{1/6}}{(c + dx)^{17/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/6)/(c + d*x)^(17/6), x)

[Out] int((a + b*x)^(1/6)/(c + d*x)^(17/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/6)/(d*x+c)**(17/6), x)

[Out] Timed out

3.1772 $\int \sqrt[6]{a+bx} (c+dx)^{5/6} dx$

Optimal. Leaf size=427

$$\frac{5(bc-ad)^2 \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{11/6}d^{7/6}} - \frac{5(bc-ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{11/6}d^{7/6}} + \frac{5(bc-ad)^2}{144b^{11/6}d^{7/6}}$$

[Out] $5/12*(-a*d+b*c)*(b*x+a)^{(1/6)}*(d*x+c)^{(5/6)}/b/d+1/2*(b*x+a)^{(7/6)}*(d*x+c)^{(5/6)}/b-5/36*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(11/6)}/d^{(7/6)}+5/144*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(11/6)}/d^{(7/6)}-5/144*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(11/6)}/d^{(7/6)}-5/72*(-a*d+b*c)^2*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(11/6)}/d^{(7/6)}*3^{(1/2)}-5/72*(-a*d+b*c)^2*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(11/6)}/d^{(7/6)}*3^{(1/2)}$

Rubi [A] time = 0.64, antiderivative size = 427, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {50, 63, 240, 210, 634, 618, 204, 628, 208}

$$\frac{5(bc-ad)^2 \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{11/6}d^{7/6}} - \frac{5(bc-ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{11/6}d^{7/6}} + \frac{5(bc-ad)^2}{144b^{11/6}d^{7/6}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(1/6)}*(c + d*x)^{(5/6)}, x]$

[Out] $(5*(b*c - a*d)*(a + b*x)^{(1/6)}*(c + d*x)^{(5/6)})/(12*b*d) + ((a + b*x)^{(7/6)}*(c + d*x)^{(5/6)})/(2*b) + (5*(b*c - a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(11/6)}*d^{(7/6)}) - (5*(b*c - a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(11/6)}*d^{(7/6)}) - (5*(b*c - a*d)^2*\operatorname{ArcTanh}[(d^{(1/6)}*(a + b*x)^{(1/6)})/(b^{(1/6)}*(c + d*x)^{(1/6)})]/(36*b^{(11/6)}*d^{(7/6)}) + (5*(b*c - a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})]/(144*b^{(11/6)}*d^{(7/6)}) - (5*(b*c - a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})]/(144*b^{(11/6)}*d^{(7/6)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m+1)}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/$

```
(b*(m + n + 1)), Int[(a + b*x)^(m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rule 210

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Module[{r = Numerator[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r - s*Cos[(2*k*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r + s*Cos[(2*k*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^2*Int[1/(r^2 - s^2*x^2), x])/(a*n) + Dist[(2*r)/(a*n), Sum[u, {k, 1, (n - 2)/4}], x], x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && NegQ[a/b]
```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c},
```

$x] \&\& \text{NeQ}[b^2 - 4*a*c, 0]$

Rule 628

$\text{Int}[\frac{(d_.) + (e_.)*(x_.)}{(a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2}, x_Symbol] \rightarrow \text{Simp}[(d*\text{Log}[\text{RemoveContent}[a + b*x + c*x^2, x]])/b, x] /; \text{FreeQ}[\{a, b, c, d, e\}, x] \&\& \text{EqQ}[2*c*d - b*e, 0]$

Rule 634

$\text{Int}[\frac{(d_.) + (e_.)*(x_.)}{(a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2}, x_Symbol] \rightarrow \text{Dist}[(2*c*d - b*e)/(2*c), \text{Int}[1/(a + b*x + c*x^2), x], x] + \text{Dist}[e/(2*c), \text{Int}[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; \text{FreeQ}[\{a, b, c, d, e\}, x] \&\& \text{NeQ}[2*c*d - b*e, 0] \&\& \text{NeQ}[b^2 - 4*a*c, 0] \&\& \text{!NiceSqrtQ}[b^2 - 4*a*c]$

Rubi steps

$$\begin{aligned}
\int \sqrt[6]{a+bx} (c+dx)^{5/6} dx &= \frac{(a+bx)^{7/6} (c+dx)^{5/6}}{2b} + \frac{(5(bc-ad)) \int \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} dx}{12b} \\
&= \frac{5(bc-ad) \sqrt[6]{a+bx} (c+dx)^{5/6}}{12bd} + \frac{(a+bx)^{7/6} (c+dx)^{5/6}}{2b} - \frac{(5(bc-ad)^2) \int \frac{1}{(a+bx)^{5/6} \sqrt[6]{c+dx}}}{72bd} \\
&= \frac{5(bc-ad) \sqrt[6]{a+bx} (c+dx)^{5/6}}{12bd} + \frac{(a+bx)^{7/6} (c+dx)^{5/6}}{2b} - \frac{(5(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt[6]{c}} \right)}{12b^2} \\
&= \frac{5(bc-ad) \sqrt[6]{a+bx} (c+dx)^{5/6}}{12bd} + \frac{(a+bx)^{7/6} (c+dx)^{5/6}}{2b} - \frac{(5(bc-ad)^2) \text{Subst} \left(\int \frac{1}{1-d} \right)}{12b^2 d} \\
&= \frac{5(bc-ad) \sqrt[6]{a+bx} (c+dx)^{5/6}}{12bd} + \frac{(a+bx)^{7/6} (c+dx)^{5/6}}{2b} - \frac{(5(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt[3]{b}} \right)}{36b^2} \\
&= \frac{5(bc-ad) \sqrt[6]{a+bx} (c+dx)^{5/6}}{12bd} + \frac{(a+bx)^{7/6} (c+dx)^{5/6}}{2b} - \frac{5(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{36b^{11/6} d^{7/6}} \\
&= \frac{5(bc-ad) \sqrt[6]{a+bx} (c+dx)^{5/6}}{12bd} + \frac{(a+bx)^{7/6} (c+dx)^{5/6}}{2b} - \frac{5(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{36b^{11/6} d^{7/6}} \\
&= \frac{5(bc-ad) \sqrt[6]{a+bx} (c+dx)^{5/6}}{12bd} + \frac{(a+bx)^{7/6} (c+dx)^{5/6}}{2b} + \frac{5(bc-ad)^2 \tan^{-1} \left(\frac{1 - \frac{2 \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{24\sqrt{3} b^{11/6} d^{7/6}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.17

$$\frac{6(a+bx)^{7/6} (c+dx)^{5/6} {}_2F_1 \left(-\frac{5}{6}, \frac{7}{6}; \frac{13}{6}; \frac{d(a+bx)}{ad-bc} \right)}{7b \left(\frac{b(c+dx)}{bc-ad} \right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)*(c + d*x)^(5/6), x]

[Out] (6*(a + b*x)^(7/6)*(c + d*x)^(5/6)*Hypergeometric2F1[-5/6, 7/6, 13/6, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*((b*(c + d*x))/(b*c - a*d))^(5/6))

$$\begin{aligned}
& 95*a^8*b^4*c^4*d^9 - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b^2*c^2*d^{11} - 12*a^{11}* \\
& b*c*d^{12} + a^{12}*d^{13}*x)) + 20*\sqrt{3}*b*d*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + \\
& 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5* \\
& *b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4* \\
& d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}* \\
& d^{12})/(b^{11}*d^7))^{(1/6)}*\arctan(-1/3*(2*\sqrt{3})*(b^{11}*c^2*d^6 - 2*a*b^{10}*c*d \\
& ^7 + a^2*b^9*d^8)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^{12}*c^{12} - 12*a*b^{11}*c \\
& ^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - \\
& 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b \\
& ^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} \\
& + a^{12}*d^{12})/(b^{11}*d^7))^{(5/6)} - 2*\sqrt{3}*(b^9*d^7*x + b^9*c*d^6)*\sqrt{-((\\
& b^4*c^2*d - 2*a*b^3*c*d^2 + a^2*b^2*d^3)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((\\
& b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + \\
& 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7* \\
& b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d \\
& ^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^{11}*d^7))^{(1/6)} - (b^4*c^4 - 4*a*b^3* \\
& c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*(b*x + a)^{(1/3)}*(d*x + \\
& c)^{(2/3)} - (b^4*d^3*x + b^4*c*d^2)*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2 \\
& *b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^ \\
& 7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 2 \\
& 20*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(\\
& b^{11}*d^7))^{(1/3)})/(d*x + c))*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c \\
& ^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + \\
& 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9* \\
& b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^{11}*d^ \\
& 7))^{(5/6)} - \sqrt{3}*(b^{12}*c^{13} - 12*a*b^{11}*c^{12}*d + 66*a^2*b^{10}*c^{11}*d^2 - \\
& 220*a^3*b^9*c^{10}*d^3 + 495*a^4*b^8*c^9*d^4 - 792*a^5*b^7*c^8*d^5 + 924*a^6* \\
& b^6*c^7*d^6 - 792*a^7*b^5*c^6*d^7 + 495*a^8*b^4*c^5*d^8 - 220*a^9*b^3*c^4*d \\
& ^9 + 66*a^{10}*b^2*c^3*d^{10} - 12*a^{11}*b*c^2*d^{11} + a^{12}*c*d^{12} + (b^{12}*c^{12}*d \\
& - 12*a*b^{11}*c^{11}*d^2 + 66*a^2*b^{10}*c^{10}*d^3 - 220*a^3*b^9*c^9*d^4 + 495*a^ \\
& 4*b^8*c^8*d^5 - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - 792*a^7*b^5*c^5 \\
& *d^8 + 495*a^8*b^4*c^4*d^9 - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b^2*c^2*d^{11} - \\
& 12*a^{11}*b*c*d^{12} + a^{12}*d^{13})*x))/(b^{12}*c^{13} - 12*a*b^{11}*c^{12}*d + 66*a^2*b^ \\
& 10*c^{11}*d^2 - 220*a^3*b^9*c^{10}*d^3 + 495*a^4*b^8*c^9*d^4 - 792*a^5*b^7*c^8* \\
& d^5 + 924*a^6*b^6*c^7*d^6 - 792*a^7*b^5*c^6*d^7 + 495*a^8*b^4*c^5*d^8 - 220 \\
& *a^9*b^3*c^4*d^9 + 66*a^{10}*b^2*c^3*d^{10} - 12*a^{11}*b*c^2*d^{11} + a^{12}*c*d^{12} \\
& + (b^{12}*c^{12}*d - 12*a*b^{11}*c^{11}*d^2 + 66*a^2*b^{10}*c^{10}*d^3 - 220*a^3*b^9*c^ \\
& 9*d^4 + 495*a^4*b^8*c^8*d^5 - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - 7 \\
& 92*a^7*b^5*c^5*d^8 + 495*a^8*b^4*c^4*d^9 - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b \\
& ^2*c^2*d^{11} - 12*a^{11}*b*c*d^{12} + a^{12}*d^{13})*x)) - 5*b*d*((b^{12}*c^{12} - 12*a* \\
& b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8* \\
& d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495 \\
& *a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c \\
& *d^{11} + a^{12}*d^{12})/(b^{11}*d^7))^{(1/6)}*\log(25*((b^4*c^2*d - 2*a*b^3*c*d^2 + a \\
& ^2*b^2*d^3)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d
\end{aligned}$$

$$\begin{aligned}
& + 66*a^2*b^10*c^10*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 \\
& *d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^10*b^2*c^2*d^10 - 12*a^11*b*c*d^11 + a^12*d^12)/(b^11*d^7))^{(1/6)} + (b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4 \\
& *a^3*b*c*d^3 + a^4*d^4)*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)} + (b^4*d^3*x + b^4*c*d^2)*((b^12*c^12 - 12*a*b^11*c^11*d + 66*a^2*b^10*c^10*d^2 - 220*a^3*b^9*c^9*d^3 \\
& + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^10*b^2*c^2*d^10 - 12*a^11*b*c*d^11 + a^12*d^12)/(b^11*d^7))^{(1/3)} \\
& /((d*x + c)) + 5*b*d*((b^12*c^12 - 12*a*b^11*c^11*d + 66*a^2*b^10*c^10*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 \\
& - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^10*b^2*c^2*d^10 - 12*a^11*b*c*d^11 + a^12*d^12)/(b^11*d^7))^{(1/6)}*log(-25*((b^4*c^2*d - 2*a*b^3*c*d^2 + a^2*b^2*d^3)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^12*c^12 - 12*a*b^11*c^11*d + 66*a^2*b^10*c^10*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^10*b^2*c^2*d^10 - 12*a^11*b*c*d^11 + a^12*d^12)/(b^11*d^7))^{(1/6)} - (b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)} - (b^4*d^3*x + b^4*c*d^2)*((b^12*c^12 - 12*a*b^11*c^11*d + 66*a^2*b^10*c^10*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^10*b^2*c^2*d^10 - 12*a^11*b*c*d^11 + a^12*d^12)/(b^11*d^7))^{(1/3)})))/(d*x + c)) - 10*b*d*((b^12*c^12 - 12*a*b^11*c^11*d + 66*a^2*b^10*c^10*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^10*b^2*c^2*d^10 - 12*a^11*b*c*d^11 + a^12*d^12)/(b^11*d^7))^{(1/6)}*log(5*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)} + (b^2*d^2*x + b^2*c*d)*((b^12*c^12 - 12*a*b^11*c^11*d + 66*a^2*b^10*c^10*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^10*b^2*c^2*d^10 - 12*a^11*b*c*d^11 + a^12*d^12)/(b^11*d^7))^{(1/6)})))/(d*x + c)) + 10*b*d*((b^12*c^12 - 12*a*b^11*c^11*d + 66*a^2*b^10*c^10*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^10*b^2*c^2*d^10 - 12*a^11*b*c*d^11 + a^12*d^12)/(b^11*d^7))^{(1/6)}*log(5*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)} - (b^2*d^2*x + b^2*c*d)*((b^12*c^12 - 12*a*b^11*c^11*d + 66*a^2*b^10*c^10*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^10*b^2*c^2*d^10 - 12*a^11*b*c*d^11 + a^12*d^12)/(b^11*d^7))^{(1/6)})))/(d*x + c)) + 12*(6*b*d*x + 5*b*c + a*d)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}/(b*d)
\end{aligned}$$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)*(d*x+c)^(5/6),x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{6}} (dx + c)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)*(d*x+c)^(5/6),x)

[Out] int((b*x+a)^(1/6)*(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{1}{6}} (dx + c)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)*(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)*(d*x + c)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{1/6} (c + dx)^{5/6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/6)*(c + d*x)^(5/6),x)

[Out] int((a + b*x)^(1/6)*(c + d*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \sqrt[6]{a + bx} (c + dx)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/6)*(d*x+c)**(5/6),x)

[Out] Integral((a + b*x)**(1/6)*(c + d*x)**(5/6), x)

$$3.1773 \quad \int \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=378

$$\frac{(bc - ad) \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12b^{5/6}d^{7/6}} - \frac{(bc - ad) \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12b^{5/6}d^{7/6}} + \frac{(bc - ad) \tan^{-1}\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2\sqrt{3}}$$

[Out] $(b*x+a)^{(1/6)}*(d*x+c)^{(5/6)}/d-1/3*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(5/6)}/d^{(7/6)}+1/12*(-a*d+b*c)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(5/6)}/d^{(7/6)}-1/12*(-a*d+b*c)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(5/6)}/d^{(7/6)}-1/6*(-a*d+b*c)*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(5/6)}/d^{(7/6)}*3^{(1/2)}-1/6*(-a*d+b*c)*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(5/6)}/d^{(7/6)}*3^{(1/2)}$

Rubi [A] time = 0.50, antiderivative size = 378, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {50, 63, 240, 210, 634, 618, 204, 628, 208}

$$\frac{(bc - ad) \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12b^{5/6}d^{7/6}} - \frac{(bc - ad) \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12b^{5/6}d^{7/6}} + \frac{(bc - ad) \tan^{-1}\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2\sqrt{3}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)/(c + d*x)^(1/6), x]

[Out] $((a + b*x)^{(1/6)}*(c + d*x)^{(5/6)})/d + ((b*c - a*d)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(2*\operatorname{Sqrt}[3]*b^{(5/6)}*d^{(7/6)}) - ((b*c - a*d)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(2*\operatorname{Sqrt}[3]*b^{(5/6)}*d^{(7/6)}) - ((b*c - a*d)*\operatorname{ArcTanh}[(d^{(1/6)}*(a + b*x)^{(1/6)})/(b^{(1/6)}*(c + d*x)^{(1/6)})]/(3*b^{(5/6)}*d^{(7/6)}) + ((b*c - a*d)*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})]/(12*b^{(5/6)}*d^{(7/6)}) - ((b*c - a*d)*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})]/(12*b^{(5/6)}*d^{(7/6)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/

```
(b*(m + n + 1)), Int[(a + b*x)^(m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rule 210

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Module[{r = Numerator[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r - s*Cos[(2*k*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r + s*Cos[(2*k*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^2*Int[1/(r^2 - s^2*x^2), x])/(a*n) + Dist[(2*r)/(a*n), Sum[u, {k, 1, (n - 2)/4}], x], x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && NegQ[a/b]
```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c},
```

$x] \&\& \text{NeQ}[b^2 - 4*a*c, 0]$

Rule 628

$\text{Int}[\frac{(d_.) + (e_.)*(x_.)}{(a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2}, x_Symbol] \rightarrow \text{Simp}[(d*\text{Log}[\text{RemoveContent}[a + b*x + c*x^2, x]])/b, x] /; \text{FreeQ}[\{a, b, c, d, e\}, x] \&\& \text{EqQ}[2*c*d - b*e, 0]$

Rule 634

$\text{Int}[\frac{(d_.) + (e_.)*(x_.)}{(a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2}, x_Symbol] \rightarrow \text{Dist}[(2*c*d - b*e)/(2*c), \text{Int}[1/(a + b*x + c*x^2), x], x] + \text{Dist}[e/(2*c), \text{Int}[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; \text{FreeQ}[\{a, b, c, d, e\}, x] \&\& \text{NeQ}[2*c*d - b*e, 0] \&\& \text{NeQ}[b^2 - 4*a*c, 0] \&\& \text{!NiceSqrtQ}[b^2 - 4*a*c]$

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} dx &= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{d} - \frac{(bc-ad) \int \frac{1}{(a+bx)^{5/6} \sqrt[6]{c+dx}} dx}{6d} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{d} - \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{1}{\sqrt[6]{c-\frac{ad}{b}+\frac{dx^6}{b}}} dx, x, \sqrt[6]{a+bx} \right)}{bd} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{d} - \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{1}{1-\frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{bd} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{d} - \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{\sqrt[6]{b}-\frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b}-\sqrt[6]{b} \sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{3b^{5/6}d} - \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{-\sqrt[6]{b} \sqrt[6]{d}+2\sqrt[3]{d}x}{\sqrt[3]{b}-\sqrt[6]{b} \sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{12b^{5/6}d^{7/6}} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{d} - \frac{(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3b^{5/6}d^{7/6}} + \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{-\sqrt[6]{b} \sqrt[6]{d}+2\sqrt[3]{d}x}{\sqrt[3]{b}-\sqrt[6]{b} \sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{12b^{5/6}d^{7/6}} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{d} - \frac{(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3b^{5/6}d^{7/6}} + \frac{(bc-ad) \log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} - \frac{\sqrt[6]{b} \sqrt[6]{d}}{\sqrt[6]{c+dx}} \right)}{12b^{5/6}d^{7/6}} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{d} + \frac{(bc-ad) \tan^{-1} \left(\frac{1-\frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3} b^{5/6}d^{7/6}} - \frac{(bc-ad) \tan^{-1} \left(\frac{1+\frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3} b^{5/6}d^{7/6}} - \frac{(bc-ad) \log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} - \frac{\sqrt[6]{b} \sqrt[6]{d}}{\sqrt[6]{c+dx}} \right)}{12b^{5/6}d^{7/6}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.19

$$\frac{6(a+bx)^{7/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(\frac{1}{6}, \frac{7}{6}; \frac{13}{6}; \frac{d(a+bx)}{ad-bc} \right)}{7b \sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)/(c + d*x)^(1/6), x]

[Out] (6*(a + b*x)^(7/6)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 7/6, 13/6, (d*(a + b*x))/(-(b*c) + a*d)]/(7*b*(c + d*x)^(1/6))

fricas [B] time = 0.93, size = 3025, normalized size = 8.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(1/6),x, algorithm="fricas")

[Out]
$$-1/12*(4*\sqrt{3}*d*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{1/6})*\arctan(1/3*(2*\sqrt{3}*(b^5*c*d^6 - a*b^4*d^7)*(b*x + a)^{1/6}*(d*x + c)^{5/6})*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{5/6} + 2*\sqrt{3}*(b^4*d^7*x + b^4*c*d^6)*\sqrt{((b^2*c*d - a*b*d^2)*(b*x + a)^{1/6}*(d*x + c)^{5/6})*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{1/6} + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^{1/3}*(d*x + c)^{2/3} + (b^2*d^3*x + b^2*c*d^2)*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{1/3})/(d*x + c))*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{5/6} + \sqrt{3}*(b^6*c^7 - 6*a*b^5*c^6*d + 15*a^2*b^4*c^5*d^2 - 20*a^3*b^3*c^4*d^3 + 15*a^4*b^2*c^3*d^4 - 6*a^5*b*c^2*d^5 + a^6*c*d^6 + (b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 - 20*a^3*b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7)*x))/(b^6*c^7 - 6*a*b^5*c^6*d + 15*a^2*b^4*c^5*d^2 - 20*a^3*b^3*c^4*d^3 + 15*a^4*b^2*c^3*d^4 - 6*a^5*b*c^2*d^5 + a^6*c*d^6 + (b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 - 20*a^3*b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7)*x)) + 4*\sqrt{3}*d*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{1/6})*\arctan(1/3*(2*\sqrt{3}*(b^5*c*d^6 - a*b^4*d^7)*(b*x + a)^{1/6}*(d*x + c)^{5/6})*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{5/6} + 2*\sqrt{3}*(b^4*d^7*x + b^4*c*d^6)*\sqrt{-((b^2*c*d - a*b*d^2)*(b*x + a)^{1/6}*(d*x + c)^{5/6})*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{1/6} - (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^{1/3}*(d*x + c)^{2/3} - (b^2*d^3*x + b^2*c*d^2)*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{1/3})/(d*x + c))*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{5/6} - \sqrt{3}*(b^6*c^7 - 6*a*b^5*c^6*d + 15*a^2*b^4*c^5*d^2 - 20*a^3*b^3*c^4*d^3 + 15*a^4*b^2*c^3*d^4 - 6*a^5*b*c^2*d^5 + a^6*c*d^6 + (b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 - 20*a^3*b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7)*x))/(b^6*c^7 - 6*a*b^5*c^6*d + 15*a^2*b^4*c^5*d^2 - 20*a^3*b^3*c^4*d^3 + 15*a^4*b^2*c^3*d^4 - 6*a^5*b*c^2*d^5 + a^6*c*d^6 + (b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 - 20*a^3*b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7)*x)) + d*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b^5*d^7))^{1/6})*\log(((b^2*c*d - a*b*d^2)*(b*x$$

$$\begin{aligned}
& + a^{1/6} (dx + c)^{5/6} \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^5 d^7) \right)^{1/6} \\
& + (b^2 c^2 - 2 a b c d + a^2 d^2) (b x + a)^{1/3} (dx + c)^{2/3} \\
& + (b^2 d^3 x + b^2 c d^2) \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^5 d^7) \right)^{1/3} \\
& / (dx + c) - d \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^5 d^7) \right)^{1/6} \\
& * \log \left(- \left((b^2 c d - a b d^2) (b x + a)^{1/6} (dx + c)^{5/6} \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^5 d^7) \right)^{1/6} \right. \right. \\
& \left. \left. - (b^2 c^2 - 2 a b c d + a^2 d^2) (b x + a)^{1/3} (dx + c)^{2/3} - (b^2 d^3 x + b^2 c d^2) \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^5 d^7) \right)^{1/3} \right) / (dx + c) \right) \\
& + 2 d \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^5 d^7) \right)^{1/6} \\
& * \log \left(- \left((b c - a d) (b x + a)^{1/6} (dx + c)^{5/6} + (b d^2 x + b c d) \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^5 d^7) \right)^{1/6} \right) / (dx + c) \right) \\
& - 2 d \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^5 d^7) \right)^{1/6} \\
& * \log \left(- \left((b c - a d) (b x + a)^{1/6} (dx + c)^{5/6} - (b d^2 x + b c d) \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^5 d^7) \right)^{1/6} \right) / (dx + c) \right) \\
& - 12 (b x + a)^{1/6} (dx + c)^{5/6} / d
\end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(1/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(1/6), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)/(d*x+c)^(1/6),x)

[Out] int((b*x+a)^(1/6)/(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{1/6}}{(c + dx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/6)/(c + d*x)^(1/6),x)

[Out] int((a + b*x)^(1/6)/(c + d*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{a + bx}}{\sqrt[6]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/6)/(d*x+c)**(1/6),x)

[Out] Integral((a + b*x)**(1/6)/(c + d*x)**(1/6), x)

$$3.1774 \quad \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{7/6}} dx$$

Optimal. Leaf size=332

$$\frac{\sqrt[6]{b} \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{7/6}} + \frac{\sqrt[6]{b} \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{7/6}} - \frac{\sqrt{3} \sqrt[6]{b} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{b}}{\sqrt{3}}\right)}{d^{7/6}}$$

[Out] $-6*(b*x+a)^{(1/6)}/d/(d*x+c)^{(1/6)}+2*b^{(1/6)}*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/d^{(7/6)}-1/2*b^{(1/6)}*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)})/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/d^{(7/6)}+1/2*b^{(1/6)}*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)})/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/d^{(7/6)}+b^{(1/6)}*\arctan(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/d^{(7/6)}+b^{(1/6)}*\arctan(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/d^{(7/6)}$

Rubi [A] time = 0.49, antiderivative size = 332, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 63, 240, 210, 634, 618, 204, 628, 208}

$$\frac{\sqrt[6]{b} \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{7/6}} + \frac{\sqrt[6]{b} \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{7/6}} - \frac{\sqrt{3} \sqrt[6]{b} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{b}}{\sqrt{3}}\right)}{d^{7/6}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)/(c + d*x)^(7/6), x]

[Out] $(-6*(a + b*x)^{(1/6)})/(d*(c + d*x)^{(1/6)}) - (\operatorname{Sqrt}[3]*b^{(1/6)}*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3]] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)}))/d^{(7/6)} + (\operatorname{Sqrt}[3]*b^{(1/6)}*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3]] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)}))/d^{(7/6)} + (2*b^{(1/6)}*\operatorname{ArcTanh}[(d^{(1/6)}*(a + b*x)^{(1/6)})/(b^{(1/6)}*(c + d*x)^{(1/6)})])/d^{(7/6)} - (b^{(1/6)}*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)}] - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})/(2*d^{(7/6)}) + (b^{(1/6)}*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)}] + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})/(2*d^{(7/6)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&

NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 204

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rule 210

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Module[{r = Numerator[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r - s*Cos[(2*k*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r + s*Cos[(2*k*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^2*Int[1/(r^2 - s^2*x^2), x])/(a*n) + Dist[(2*r)/(a*n), Sum[u, {k, 1, (n - 2)/4}], x], x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && NegQ[a/b]

Rule 240

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/n]

Rule 618

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rule 628

```
Int[((d_) + (e_)*(x_))/((a_) + (b_)*(x_) + (c_)*(x_)^2), x_Symbol] := S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_) + (e_)*(x_))/((a_) + (b_)*(x_) + (c_)*(x_)^2), x_Symbol] := D
ist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), In
t[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ
[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{7/6}} dx &= -\frac{6\sqrt[6]{a+bx}}{d\sqrt[6]{c+dx}} + \frac{b \int \frac{1}{(a+bx)^{5/6} \sqrt[6]{c+dx}} dx}{d} \\
&= -\frac{6\sqrt[6]{a+bx}}{d\sqrt[6]{c+dx}} + \frac{6 \operatorname{Subst} \left(\int \frac{1}{\sqrt[6]{c-\frac{ad}{b} + \frac{dx^6}{b}}} dx, x, \sqrt[6]{a+bx} \right)}{d} \\
&= -\frac{6\sqrt[6]{a+bx}}{d\sqrt[6]{c+dx}} + \frac{6 \operatorname{Subst} \left(\int \frac{1}{1-\frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{d} \\
&= -\frac{6\sqrt[6]{a+bx}}{d\sqrt[6]{c+dx}} + \frac{(2\sqrt[6]{b}) \operatorname{Subst} \left(\int \frac{\sqrt[6]{b} - \frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{d} + \frac{(2\sqrt[6]{b}) \operatorname{Subst} \left(\int \frac{\sqrt[6]{b} + \frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b} + \sqrt[6]{b} \sqrt[6]{d}x} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{d} \\
&= -\frac{6\sqrt[6]{a+bx}}{d\sqrt[6]{c+dx}} + \frac{2\sqrt[6]{b} \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{d^{7/6}} - \frac{\sqrt[6]{b} \operatorname{Subst} \left(\int \frac{-\sqrt[6]{b} \sqrt[6]{d} + 2\sqrt[3]{d}x}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2d^{7/6}} + \frac{\sqrt[6]{b}}{d^{7/6}} \\
&= -\frac{6\sqrt[6]{a+bx}}{d\sqrt[6]{c+dx}} + \frac{2\sqrt[6]{b} \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{d^{7/6}} - \frac{\sqrt[6]{b} \log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} - \frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2d^{7/6}} + \frac{\sqrt[6]{b} \log}{d^{7/6}} \\
&= -\frac{6\sqrt[6]{a+bx}}{d\sqrt[6]{c+dx}} - \frac{\sqrt{3} \sqrt[6]{b} \tan^{-1} \left(\frac{1 - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{d^{7/6}} + \frac{\sqrt{3} \sqrt[6]{b} \tan^{-1} \left(\frac{1 + \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{d^{7/6}} + \frac{2\sqrt[6]{b} \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{d^{7/6}}
\end{aligned}$$

Mathematica [C] time = 0.06, size = 73, normalized size = 0.22

$$\frac{6(a+bx)^{7/6} \left(\frac{b(c+dx)}{bc-ad} \right)^{7/6} {}_2F_1 \left(\frac{7}{6}, \frac{7}{6}; \frac{13}{6}; \frac{d(a+bx)}{ad-bc} \right)}{7b(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)/(c + d*x)^(7/6), x]

[Out] (6*(a + b*x)^(7/6)*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[7/6, 7/6, 13/6, (d*(a + b*x))/(-b*c) + a*d])/(7*b*(c + d*x)^(7/6))

fricas [B] time = 0.92, size = 663, normalized size = 2.00

$$4\sqrt{3}\left(d^2x + cd\right)\left(\frac{b}{d^7}\right)^{\frac{1}{6}} \arctan\left(\frac{2\sqrt{3}(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{5}{6}}d^6\left(\frac{b}{d^7}\right)^{\frac{5}{6}} - 2\sqrt{3}(d^7x+cd^6)\sqrt{\frac{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{5}{6}}d\left(\frac{b}{d^7}\right)^{\frac{1}{6}} + (d^3x+cd^2)\left(\frac{b}{d^7}\right)^{\frac{1}{3}} + (bx+a)^{\frac{1}{3}}(dx+c)^{\frac{2}{3}}}{dx+c}}}{3(bdx+bc)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(7/6),x, algorithm="fricas")

[Out]
$$\begin{aligned} & -1/2*(4*\sqrt{3}*(d^2*x + c*d)*(b/d^7)^{(1/6)}*\arctan(-1/3*(2*\sqrt{3}*(b*x + a) \\ &)^{(1/6)}*(d*x + c)^{(5/6)}*d^6*(b/d^7)^{(5/6)} - 2*\sqrt{3}*(d^7*x + c*d^6)*\sqrt{ \\ & ((b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*d*(b/d^7)^{(1/6)} + (d^3*x + c*d^2)*(b/d^7)^{(1/3)} + (b*x + a)^{(1/3)}*(d*x + c)^{(2/3)})/(d*x + c)}*(b/d^7)^{(5/6)} + \sqrt{3} \\ & *(b*d*x + b*c))/(b*d*x + b*c)) + 4*\sqrt{3}*(d^2*x + c*d)*(b/d^7)^{(1/6)}*\arct \\ & \arctan(-1/3*(2*\sqrt{3}*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*d^6*(b/d^7)^{(5/6)} - 2*\sqrt{3} \\ & *(d^7*x + c*d^6)*\sqrt{-(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*d*(b/d^7)^{(1/6)} \\ &) - (d^3*x + c*d^2)*(b/d^7)^{(1/3)} - (b*x + a)^{(1/3)}*(d*x + c)^{(2/3)})/(d*x + \\ & c)}*(b/d^7)^{(5/6)} - \sqrt{3}*(b*d*x + b*c))/(b*d*x + b*c)) - (d^2*x + c*d)* \\ & (b/d^7)^{(1/6)}*\log(4*((b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*d*(b/d^7)^{(1/6)} + (d^3 \\ & *x + c*d^2)*(b/d^7)^{(1/3)} + (b*x + a)^{(1/3)}*(d*x + c)^{(2/3)})/(d*x + c)) + (\\ & d^2*x + c*d)*(b/d^7)^{(1/6)}*\log(-4*((b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*d*(b/d^7 \\ &)^{(1/6)} - (d^3*x + c*d^2)*(b/d^7)^{(1/3)} - (b*x + a)^{(1/3)}*(d*x + c)^{(2/3)})/ \\ & (d*x + c)) - 2*(d^2*x + c*d)*(b/d^7)^{(1/6)}*\log(((d^2*x + c*d)*(b/d^7)^{(1/6)} \\ & + (b*x + a)^{(1/6)}*(d*x + c)^{(5/6)})/(d*x + c)) + 2*(d^2*x + c*d)*(b/d^7)^{(1 \\ & /6)}*\log(-((d^2*x + c*d)*(b/d^7)^{(1/6)} - (b*x + a)^{(1/6)}*(d*x + c)^{(5/6)})/(d \\ & *x + c)) + 12*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)})/(d^2*x + c*d) \end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{6}}}{(dx+c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(7/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(7/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{6}}}{(dx+c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(1/6)/(d*x+c)^(7/6),x)`

[Out] `int((b*x+a)^(1/6)/(d*x+c)^(7/6),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1/6)/(d*x+c)^(7/6),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(1/6)/(d*x + c)^(7/6), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{1/6}}{(c + dx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/6)/(c + d*x)^(7/6),x)`

[Out] `int((a + b*x)^(1/6)/(c + d*x)^(7/6), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{a + bx}}{(c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/6)/(d*x+c)**(7/6),x)`

[Out] `Integral((a + b*x)**(1/6)/(c + d*x)**(7/6), x)`

$$3.1775 \quad \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{13/6}} dx$$

Optimal. Leaf size=32

$$\frac{6(a+bx)^{7/6}}{7(c+dx)^{7/6}(bc-ad)}$$

[Out] $6/7*(b*x+a)^{(7/6)/(-a*d+b*c)/(d*x+c)^{(7/6)}$

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{6(a+bx)^{7/6}}{7(c+dx)^{7/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)/(c + d*x)^(13/6), x]

[Out] (6*(a + b*x)^(7/6))/(7*(b*c - a*d)*(c + d*x)^(7/6))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{13/6}} dx = \frac{6(a+bx)^{7/6}}{7(bc-ad)(c+dx)^{7/6}}$$

Mathematica [A] time = 0.02, size = 32, normalized size = 1.00

$$\frac{6(a+bx)^{7/6}}{7(c+dx)^{7/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)/(c + d*x)^(13/6), x]

[Out] (6*(a + b*x)^(7/6))/(7*(b*c - a*d)*(c + d*x)^(7/6))

fricas [B] time = 0.84, size = 65, normalized size = 2.03

$$\frac{6 (bx + a)^{\frac{7}{6}} (dx + c)^{\frac{5}{6}}}{7 (bc^3 - ac^2d + (bcd^2 - ad^3)x^2 + 2 (bc^2d - acd^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(13/6),x, algorithm="fricas")

[Out] 6/7*(b*x + a)^(7/6)*(d*x + c)^(5/6)/(b*c^3 - a*c^2*d + (b*c*d^2 - a*d^3)*x^2 + 2*(b*c^2*d - a*c*d^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(13/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(13/6), x)

maple [A] time = 0.01, size = 27, normalized size = 0.84

$$\frac{6 (bx + a)^{\frac{7}{6}}}{7 (dx + c)^{\frac{7}{6}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)/(d*x+c)^(13/6),x)

[Out] -6/7*(b*x+a)^(7/6)/(d*x+c)^(7/6)/(a*d-b*c)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(13/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(13/6), x)

mupad [B] time = 0.56, size = 130, normalized size = 4.06

$$\frac{\left(\frac{6a(a+bx)^{1/6}}{7ad^3-7bcd^2} + \frac{6bx(a+bx)^{1/6}}{7ad^3-7bcd^2}\right)(c+dx)^{5/6}}{x^2 - \frac{7bc^3-7ac^2d}{7ad^3-7bcd^2} + \frac{14cdx(ad-bc)}{7ad^3-7bcd^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/6)/(c + d*x)^(13/6), x)

[Out] -(((6*a*(a + b*x)^(1/6))/(7*a*d^3 - 7*b*c*d^2) + (6*b*x*(a + b*x)^(1/6))/(7*a*d^3 - 7*b*c*d^2))*(c + d*x)^(5/6))/(x^2 - (7*b*c^3 - 7*a*c^2*d)/(7*a*d^3 - 7*b*c*d^2) + (14*c*d*x*(a*d - b*c))/(7*a*d^3 - 7*b*c*d^2))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/6)/(d*x+c)**(13/6), x)

[Out] Integral((a + b*x)**(1/6)/(c + d*x)**(13/6), x)

$$3.1776 \quad \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{19/6}} dx$$

Optimal. Leaf size=66

$$\frac{36b(a+bx)^{7/6}}{91(c+dx)^{7/6}(bc-ad)^2} + \frac{6(a+bx)^{7/6}}{13(c+dx)^{13/6}(bc-ad)}$$

[Out] $6/13*(b*x+a)^{(7/6)/(-a*d+b*c)/(d*x+c)^{(13/6)+36/91*b*(b*x+a)^{(7/6)/(-a*d+b*c)^2/(d*x+c)^{(7/6)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{36b(a+bx)^{7/6}}{91(c+dx)^{7/6}(bc-ad)^2} + \frac{6(a+bx)^{7/6}}{13(c+dx)^{13/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)/(c + d*x)^(19/6), x]

[Out] $(6*(a + b*x)^{(7/6)})/(13*(b*c - a*d)*(c + d*x)^{(13/6)}) + (36*b*(a + b*x)^{(7/6)})/(91*(b*c - a*d)^2*(c + d*x)^{(7/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{19/6}} dx = \frac{6(a+bx)^{7/6}}{13(bc-ad)(c+dx)^{13/6}} + \frac{(6b) \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{13/6}} dx}{13(bc-ad)}$$

$$= \frac{6(a+bx)^{7/6}}{13(bc-ad)(c+dx)^{13/6}} + \frac{36b(a+bx)^{7/6}}{91(bc-ad)^2(c+dx)^{7/6}}$$

Mathematica [A] time = 0.03, size = 46, normalized size = 0.70

$$\frac{6(a+bx)^{7/6}(-7ad+13bc+6bdx)}{91(c+dx)^{13/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)/(c + d*x)^(19/6), x]

[Out] (6*(a + b*x)^(7/6)*(13*b*c - 7*a*d + 6*b*d*x))/(91*(b*c - a*d)^2*(c + d*x)^(13/6))

fricas [B] time = 0.79, size = 175, normalized size = 2.65

$$\frac{6(6b^2dx^2 + 13abc - 7a^2d + (13b^2c - abd)x)(bx + a)^{\frac{1}{6}}(dx + c)^{\frac{5}{6}}}{91(b^2c^5 - 2abc^4d + a^2c^3d^2 + (b^2c^2d^3 - 2abcd^4 + a^2d^5)x^3 + 3(b^2c^3d^2 - 2abc^2d^3 + a^2cd^4)x^2 + 3(b^2c^4d - 2abc^3d^2 + a^2c^2d^3)x + 3a^2cd^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(19/6), x, algorithm="fricas")

[Out] 6/91*(6*b^2*d*x^2 + 13*a*b*c - 7*a^2*d + (13*b^2*c - a*b*d)*x)*(b*x + a)^(1/6)*(d*x + c)^(5/6)/(b^2*c^5 - 2*a*b*c^4*d + a^2*c^3*d^2 + (b^2*c^2*d^3 - 2*a*b*c*d^4 + a^2*d^5)*x^3 + 3*(b^2*c^3*d^2 - 2*a*b*c^2*d^3 + a^2*c*d^4)*x^2 + 3*(b^2*c^4*d - 2*a*b*c^3*d^2 + a^2*c^2*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{6}}}{(dx+c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(19/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(19/6), x)

maple [A] time = 0.01, size = 54, normalized size = 0.82

$$\frac{6(bx+a)^{\frac{7}{6}}(-6bdx+7ad-13bc)}{91(dx+c)^{\frac{13}{6}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)/(d*x+c)^(19/6),x)

[Out] -6/91*(b*x+a)^(7/6)*(-6*b*d*x+7*a*d-13*b*c)/(d*x+c)^(13/6)/(a^2*d^2-2*a*b*c*d+b^2*c^2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{6}}}{(dx+c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(19/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(19/6), x)

mupad [B] time = 0.75, size = 137, normalized size = 2.08

$$\frac{(c+dx)^{5/6} \left(\frac{36b^2x^2(a+bx)^{1/6}}{91d^2(ad-bc)^2} - \frac{(42a^2d-78abc)(a+bx)^{1/6}}{91d^3(ad-bc)^2} + \frac{x(78b^2c-6abd)(a+bx)^{1/6}}{91d^3(ad-bc)^2} \right)}{x^3 + \frac{c^3}{d^3} + \frac{3cx^2}{d} + \frac{3c^2x}{d^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/6)/(c + d*x)^(19/6),x)

[Out] ((c + d*x)^(5/6)*((36*b^2*x^2*(a + b*x)^(1/6))/(91*d^2*(a*d - b*c)^2) - ((42*a^2*d - 78*a*b*c)*(a + b*x)^(1/6))/(91*d^3*(a*d - b*c)^2) + (x*(78*b^2*c - 6*a*b*d)*(a + b*x)^(1/6))/(91*d^3*(a*d - b*c)^2)))/(x^3 + c^3/d^3 + (3*c*x^2)/d + (3*c^2*x)/d^2)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/6)/(d*x+c)**(19/6),x)

[Out] Timed out

$$3.1777 \quad \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{25/6}} dx$$

Optimal. Leaf size=101

$$\frac{432b^2(a+bx)^{7/6}}{1729(c+dx)^{7/6}(bc-ad)^3} + \frac{72b(a+bx)^{7/6}}{247(c+dx)^{13/6}(bc-ad)^2} + \frac{6(a+bx)^{7/6}}{19(c+dx)^{19/6}(bc-ad)}$$

[Out] $6/19*(b*x+a)^{(7/6)/(-a*d+b*c)/(d*x+c)^{(19/6)}+72/247*b*(b*x+a)^{(7/6)/(-a*d+b*c)^2/(d*x+c)^{(13/6)}+432/1729*b^2*(b*x+a)^{(7/6)/(-a*d+b*c)^3/(d*x+c)^{(7/6)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{432b^2(a+bx)^{7/6}}{1729(c+dx)^{7/6}(bc-ad)^3} + \frac{72b(a+bx)^{7/6}}{247(c+dx)^{13/6}(bc-ad)^2} + \frac{6(a+bx)^{7/6}}{19(c+dx)^{19/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)/(c + d*x)^(25/6), x]

[Out] $(6*(a + b*x)^{(7/6)})/(19*(b*c - a*d)*(c + d*x)^{(19/6)}) + (72*b*(a + b*x)^{(7/6)})/(247*(b*c - a*d)^2*(c + d*x)^{(13/6)}) + (432*b^2*(a + b*x)^{(7/6)})/(1729*(b*c - a*d)^3*(c + d*x)^{(7/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{25/6}} dx &= \frac{6(a+bx)^{7/6}}{19(bc-ad)(c+dx)^{19/6}} + \frac{(12b) \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{19/6}} dx}{19(bc-ad)} \\ &= \frac{6(a+bx)^{7/6}}{19(bc-ad)(c+dx)^{19/6}} + \frac{72b(a+bx)^{7/6}}{247(bc-ad)^2(c+dx)^{13/6}} + \frac{(72b^2) \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{13/6}} dx}{247(bc-ad)^2} \\ &= \frac{6(a+bx)^{7/6}}{19(bc-ad)(c+dx)^{19/6}} + \frac{72b(a+bx)^{7/6}}{247(bc-ad)^2(c+dx)^{13/6}} + \frac{432b^2(a+bx)^{7/6}}{1729(bc-ad)^3(c+dx)^{7/6}} \end{aligned}$$

Mathematica [A] time = 0.06, size = 77, normalized size = 0.76

$$\frac{6(a+bx)^{7/6} (91a^2d^2 - 14abd(19c+6dx) + b^2(247c^2 + 228cdx + 72d^2x^2))}{1729(c+dx)^{19/6}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)/(c + d*x)^(25/6), x]

[Out] (6*(a + b*x)^(7/6)*(91*a^2*d^2 - 14*a*b*d*(19*c + 6*d*x) + b^2*(247*c^2 + 228*c*d*x + 72*d^2*x^2)))/(1729*(b*c - a*d)^3*(c + d*x)^(19/6))

fricas [B] time = 0.88, size = 338, normalized size = 3.35

$$\frac{6(72b^3d^2x^3 + 247ab^2c^2 - 266a^2bcd + 91a^3d^2 + 12(19b^3cd - 1729(b^3c^7 - 3ab^2c^6d + 3a^2bc^5d^2 - a^3c^4d^3 + (b^3c^3d^4 - 3ab^2c^2d^5 + 3a^2bcd^6 - a^3d^7)x^4 + 4(b^3c^4d^3 - 3ab^2c^3d^4 +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(25/6), x, algorithm="fricas")

[Out] 6/1729*(72*b^3*d^2*x^3 + 247*a*b^2*c^2 - 266*a^2*b*c*d + 91*a^3*d^2 + 12*(19*b^3*c*d - a*b^2*d^2)*x^2 + (247*b^3*c^2 - 38*a*b^2*c*d + 7*a^2*b*d^2)*x)*(b*x + a)^(1/6)*(d*x + c)^(5/6)/(b^3*c^7 - 3*a*b^2*c^6*d + 3*a^2*b*c^5*d^2 - a^3*c^4*d^3 + (b^3*c^3*d^4 - 3*a*b^2*c^2*d^5 + 3*a^2*b*c*d^6 - a^3*d^7)*x^4 + 4*(b^3*c^4*d^3 - 3*a*b^2*c^3*d^4 + 3*a^2*b*c^2*d^5 - a^3*c*d^6)*x^3 + 6*(b^3*c^5*d^2 - 3*a*b^2*c^4*d^3 + 3*a^2*b*c^3*d^4 - a^3*c^2*d^5)*x^2 + 4*(b^3*c^6*d - 3*a*b^2*c^5*d^2 + 3*a^2*b*c^4*d^3 - a^3*c^3*d^4)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{1}{6}}}{(dx+c)^{\frac{25}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(25/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(25/6), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{6 (bx + a)^{\frac{7}{6}} (72b^2x^2d^2 - 84abd^2x + 228b^2cdx + 91a^2d^2 - 266abcd + 247b^2c^2)}{1729 (dx + c)^{\frac{19}{6}} (a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)/(d*x+c)^(25/6),x)

[Out] -6/1729*(b*x+a)^(7/6)*(72*b^2*d^2*x^2-84*a*b*d^2*x+228*b^2*c*d*x+91*a^2*d^2-266*a*b*c*d+247*b^2*c^2)/(d*x+c)^(19/6)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{25}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(25/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(25/6), x)

mupad [B] time = 0.95, size = 213, normalized size = 2.11

$$\frac{(c + dx)^{5/6} \left(\frac{(a+bx)^{1/6} (546a^3d^2 - 1596a^2bcd + 1482ab^2c^2)}{1729d^4(ad-bc)^3} + \frac{432b^3x^3(a+bx)^{1/6}}{1729d^2(ad-bc)^3} + \frac{x(a+bx)^{1/6} (42a^2bd^2 - 228ab^2cd + 1482b^3c^2)}{1729d^4(ad-bc)^3} - \frac{72b^2x^2(a+bx)^{1/6}}{1729d^4(ad-bc)^3} \right)}{x^4 + \frac{c^4}{d^4} + \frac{4cx^3}{d} + \frac{4c^3x}{d^3} + \frac{6c^2x^2}{d^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(1/6)/(c + d*x)^(25/6),x)

[Out] -((c + d*x)^(5/6)*((a + b*x)^(1/6)*(546*a^3*d^2 + 1482*a*b^2*c^2 - 1596*a^2*b*c*d))/(1729*d^4*(a*d - b*c)^3) + (432*b^3*x^3*(a + b*x)^(1/6))/(1729*d^2*(a*d - b*c)^3) + (x*(a + b*x)^(1/6)*(1482*b^3*c^2 + 42*a^2*b*d^2 - 228*a*b^2*c*d))/(1729*d^4*(a*d - b*c)^3) - (72*b^2*x^2*(a*d - 19*b*c)*(a + b*x)^(1/6))/(1729*d^4*(a*d - b*c)^3)

$$\frac{1/6)}{(1729*d^3*(a*d - b*c)^3)))/(x^4 + c^4/d^4 + (4*c*x^3)/d + (4*c^3*x)/d^3 + (6*c^2*x^2)/d^2)$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(1/6)/(d*x+c)**(25/6),x)

[Out] Timed out

$$3.1778 \quad \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{31/6}} dx$$

Optimal. Leaf size=136

$$\frac{7776b^3(a+bx)^{7/6}}{43225(c+dx)^{7/6}(bc-ad)^4} + \frac{1296b^2(a+bx)^{7/6}}{6175(c+dx)^{13/6}(bc-ad)^3} + \frac{108b(a+bx)^{7/6}}{475(c+dx)^{19/6}(bc-ad)^2} + \frac{6(a+bx)^{7/6}}{25(c+dx)^{25/6}(bc-ad)}$$

[Out] $6/25*(b*x+a)^{(7/6)/(-a*d+b*c)/(d*x+c)^{(25/6)+108/475*b*(b*x+a)^{(7/6)/(-a*d+b*c)^2/(d*x+c)^{(19/6)+1296/6175*b^2*(b*x+a)^{(7/6)/(-a*d+b*c)^3/(d*x+c)^{(13/6)+7776/43225*b^3*(b*x+a)^{(7/6)/(-a*d+b*c)^4/(d*x+c)^{(7/6)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{7776b^3(a+bx)^{7/6}}{43225(c+dx)^{7/6}(bc-ad)^4} + \frac{1296b^2(a+bx)^{7/6}}{6175(c+dx)^{13/6}(bc-ad)^3} + \frac{108b(a+bx)^{7/6}}{475(c+dx)^{19/6}(bc-ad)^2} + \frac{6(a+bx)^{7/6}}{25(c+dx)^{25/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1/6)/(c + d*x)^(31/6), x]

[Out] $(6*(a + b*x)^{(7/6)})/(25*(b*c - a*d)*(c + d*x)^{(25/6)}) + (108*b*(a + b*x)^{(7/6)})/(475*(b*c - a*d)^2*(c + d*x)^{(19/6)}) + (1296*b^2*(a + b*x)^{(7/6)})/(6175*(b*c - a*d)^3*(c + d*x)^{(13/6)}) + (7776*b^3*(a + b*x)^{(7/6)})/(43225*(b*c - a*d)^4*(c + d*x)^{(7/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[6]{a+bx}}{(c+dx)^{31/6}} dx &= \frac{6(a+bx)^{7/6}}{25(bc-ad)(c+dx)^{25/6}} + \frac{(18b) \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{25/6}} dx}{25(bc-ad)} \\
&= \frac{6(a+bx)^{7/6}}{25(bc-ad)(c+dx)^{25/6}} + \frac{108b(a+bx)^{7/6}}{475(bc-ad)^2(c+dx)^{19/6}} + \frac{(216b^2) \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{19/6}} dx}{475(bc-ad)^2} \\
&= \frac{6(a+bx)^{7/6}}{25(bc-ad)(c+dx)^{25/6}} + \frac{108b(a+bx)^{7/6}}{475(bc-ad)^2(c+dx)^{19/6}} + \frac{1296b^2(a+bx)^{7/6}}{6175(bc-ad)^3(c+dx)^{13/6}} + \frac{(1296b^3)}{6175} \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{13/6}} dx \\
&= \frac{6(a+bx)^{7/6}}{25(bc-ad)(c+dx)^{25/6}} + \frac{108b(a+bx)^{7/6}}{475(bc-ad)^2(c+dx)^{19/6}} + \frac{1296b^2(a+bx)^{7/6}}{6175(bc-ad)^3(c+dx)^{13/6}} + \frac{7776b^3}{43225(bc-ad)^4} \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{13/6}} dx
\end{aligned}$$

Mathematica [A] time = 0.08, size = 118, normalized size = 0.87

$$\frac{6(a+bx)^{7/6} \left(-1729a^3d^3 + 273a^2bd^2(25c+6dx) - 21ab^2d(475c^2 + 300cdx + 72d^2x^2) \right) + b^3 \left(6175c^3 + 8550c^2dx + 5400cd^2x^2 + 1296d^3x^3 \right)}{43225(c+dx)^{25/6}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1/6)/(c + d*x)^(31/6), x]

[Out] (6*(a + b*x)^(7/6)*(-1729*a^3*d^3 + 273*a^2*b*d^2*(25*c + 6*d*x) - 21*a*b^2*d*(475*c^2 + 300*c*d*x + 72*d^2*x^2) + b^3*(6175*c^3 + 8550*c^2*d*x + 5400*c*d^2*x^2 + 1296*d^3*x^3))/(43225*(b*c - a*d)^4*(c + d*x)^(25/6))

fricas [B] time = 0.81, size = 533, normalized size = 3.92

$$\frac{6 \left(1296 b^4 d^3 x^4 + 6175 a b^3 c^3 - 9975 a^2 b^2 c^2 d + 6825 a^3 b c d^2 - 1729 a^4 d^3 + 216 (25 b^4 c d^2 - a b^3 d^3) x^3 + 18 (475 b^4 c^2 d - 50 a b^3 c d^2 + 7 a^2 b^2 d^3) x^2 + (6175 b^4 c^3 - 1425 a b^3 c^2 d + 525 a^2 b^2 c d^2 - 91 a^3 b d^3) x \right) (b x + a)^{1/6} (d x + c)^{5/6}}{43225 \left(b^4 c^9 - 4 a b^3 c^8 d + 6 a^2 b^2 c^7 d^2 - 4 a^3 b c^6 d^3 + a^4 c^5 d^4 + (b^4 c^4 d^5 - 4 a b^3 c^3 d^6 + 6 a^2 b^2 c^2 d^7 - 4 a^3 b c d^8 + a^4 d^9) x \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(31/6), x, algorithm="fricas")

[Out] 6/43225*(1296*b^4*d^3*x^4 + 6175*a*b^3*c^3 - 9975*a^2*b^2*c^2*d + 6825*a^3*b*c*d^2 - 1729*a^4*d^3 + 216*(25*b^4*c*d^2 - a*b^3*d^3)*x^3 + 18*(475*b^4*c^2*d - 50*a*b^3*c*d^2 + 7*a^2*b^2*d^3)*x^2 + (6175*b^4*c^3 - 1425*a*b^3*c^2*d + 525*a^2*b^2*c*d^2 - 91*a^3*b*d^3)*x)*(b*x + a)^(1/6)*(d*x + c)^(5/6)/(b^4*c^9 - 4*a*b^3*c^8*d + 6*a^2*b^2*c^7*d^2 - 4*a^3*b*c^6*d^3 + a^4*c^5*d^4 + (b^4*c^4*d^5 - 4*a*b^3*c^3*d^6 + 6*a^2*b^2*c^2*d^7 - 4*a^3*b*c*d^8 + a^4*d^9)*x)

$*d^9)*x^5 + 5*(b^4*c^5*d^4 - 4*a*b^3*c^4*d^5 + 6*a^2*b^2*c^3*d^6 - 4*a^3*b*c^2*d^7 + a^4*c*d^8)*x^4 + 10*(b^4*c^6*d^3 - 4*a*b^3*c^5*d^4 + 6*a^2*b^2*c^4*d^5 - 4*a^3*b*c^3*d^6 + a^4*c^2*d^7)*x^3 + 10*(b^4*c^7*d^2 - 4*a*b^3*c^6*d^3 + 6*a^2*b^2*c^5*d^4 - 4*a^3*b*c^4*d^5 + a^4*c^3*d^6)*x^2 + 5*(b^4*c^8*d - 4*a*b^3*c^7*d^2 + 6*a^2*b^2*c^6*d^3 - 4*a^3*b*c^5*d^4 + a^4*c^4*d^5)*x$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{31}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(31/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(31/6), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{6(bx + a)^{\frac{7}{6}} \left(-1296b^3d^3x^3 + 1512ab^2d^3x^2 - 5400b^3cd^2x^2 - 1638a^2bd^3x + 6300ab^2cd^2x - 8550b^3c^2dx + 1729a^3d^3 \right)}{43225(dx + c)^{\frac{25}{6}} \left(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(1/6)/(d*x+c)^(31/6),x)

[Out] $-6/43225*(b*x+a)^{(7/6)}*(-1296*b^3*d^3*x^3+1512*a*b^2*d^3*x^2-5400*b^3*c*d^2*x^2-1638*a^2*b*d^3*x+6300*a*b^2*c*d^2*x-8550*b^3*c^2*d*x+1729*a^3*d^3-6825*a^2*b*c*d^2+9975*a*b^2*c^2*d-6175*b^3*c^3)/(d*x+c)^{(25/6)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{31}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1/6)/(d*x+c)^(31/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(1/6)/(d*x + c)^(31/6), x)

mupad [B] time = 1.15, size = 302, normalized size = 2.22

$$\frac{(c + dx)^{5/6} \left(\frac{7776b^4x^4(a+bx)^{1/6}}{43225d^2(ad-bc)^4} - \frac{(a+bx)^{1/6} (10374a^4d^3-40950a^3bcd^2+59850a^2b^2c^2d-37050ab^3c^3)}{43225d^5(ad-bc)^4} + \frac{x(a+bx)^{1/6} (-546a^3bd^3+3150a^2b^2cd^2-10374a^4d^3+40950a^3bcd^2-59850a^2b^2c^2d+37050ab^3c^3)}{43225d^5(ad-bc)^4} \right)}{x^5 + \frac{c^5}{d^5} + \frac{5cx^4}{d} + \frac{5c^4x}{d^4} + \frac{10c^3}{d^3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(1/6)/(c + d*x)^(31/6),x)`

[Out] $((c + d*x)^{(5/6)}*((7776*b^4*x^4*(a + b*x)^{(1/6)})/(43225*d^2*(a*d - b*c)^4) - ((a + b*x)^{(1/6)}*(10374*a^4*d^3 - 37050*a*b^3*c^3 + 59850*a^2*b^2*c^2*d - 40950*a^3*b*c*d^2))/(43225*d^5*(a*d - b*c)^4) + (x*(a + b*x)^{(1/6)}*(37050*b^4*c^3 - 546*a^3*b*d^3 + 3150*a^2*b^2*c*d^2 - 8550*a*b^3*c^2*d))/(43225*d^5*(a*d - b*c)^4) + (108*b^2*x^2*(a + b*x)^{(1/6)}*(7*a^2*d^2 + 475*b^2*c^2 - 50*a*b*c*d))/(43225*d^4*(a*d - b*c)^4) - (1296*b^3*x^3*(a*d - 25*b*c)*(a + b*x)^{(1/6)})/(43225*d^3*(a*d - b*c)^4))/(x^5 + c^5/d^5 + (5*c*x^4)/d + (5*c^4*x)/d^4 + (10*c^2*x^3)/d^2 + (10*c^3*x^2)/d^3)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1/6)/(d*x+c)**(31/6),x)`

[Out] Timed out

3.1779 $\int (a + bx)^{5/6} \sqrt[6]{c + dx} dx$

Optimal. Leaf size=427

$$\frac{5(bc - ad)^2 \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{7/6}d^{11/6}} - \frac{5(bc - ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{7/6}d^{11/6}} - \frac{5(bc - ad)}{144b^{7/6}d^{11/6}}$$

[Out] $1/12*(-a*d+b*c)*(b*x+a)^{(5/6)}*(d*x+c)^{(1/6)}/b/d+1/2*(b*x+a)^{(11/6)}*(d*x+c)^{(1/6)}/b-5/36*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(7/6)}/d^{(11/6)}+5/144*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(7/6)}/d^{(11/6)}-5/144*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(7/6)}/d^{(11/6)}+5/72*(-a*d+b*c)^2*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(7/6)}/d^{(11/6)}*3^{(1/2)}+5/72*(-a*d+b*c)^2*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(7/6)}/d^{(11/6)}*3^{(1/2)}$

Rubi [A] time = 0.64, antiderivative size = 427, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {50, 63, 331, 296, 634, 618, 204, 628, 208}

$$\frac{5(bc - ad)^2 \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{7/6}d^{11/6}} - \frac{5(bc - ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{7/6}d^{11/6}} - \frac{5(bc - ad)}{144b^{7/6}d^{11/6}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/6)}*(c + d*x)^{(1/6)}, x]$

[Out] $((b*c - a*d)*(a + b*x)^{(5/6)}*(c + d*x)^{(1/6)})/(12*b*d) + ((a + b*x)^{(11/6)}*(c + d*x)^{(1/6)})/(2*b) - (5*(b*c - a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(7/6)}*d^{(11/6)}) + (5*(b*c - a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(7/6)}*d^{(11/6)}) - (5*(b*c - a*d)^2*\operatorname{ArcTanh}[(d^{(1/6)}*(a + b*x)^{(1/6)})/(b^{(1/6)}*(c + d*x)^{(1/6)})]/(36*b^{(7/6)}*d^{(11/6)}) + (5*(b*c - a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)}]/(144*b^{(7/6)}*d^{(11/6)}) - (5*(b*c - a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)}]/(144*b^{(7/6)}*d^{(11/6)})$

Rule 50

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n)}/(b*(m + n + 1)), x] + \operatorname{Dist}[(n*(b*c - a*d)]/$

```
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rule 296

```
Int[(x_)^(m_.)/((a_) + (b_.)*(x_)^(n_.)), x_Symbol] := Module[{r = Numerator
[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r*cos
[(2*k*m*Pi)/n] - s*cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 - 2*r*s*cos[(2*k*Pi)/n]*
x + s^2*x^2), x] + Int[(r*cos[(2*k*m*Pi)/n] + s*cos[(2*k*(m + 1)*Pi)/n]*x)/
(r^2 + 2*r*s*cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^(m + 2)*Int[1/(r^2 - s^
2*x^2), x])/(a*n*s^m) + Dist[(2*r^(m + 1))/(a*n*s^m), Sum[u, {k, 1, (n - 2)
/4}], x], x]] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && IGtQ[m, 0] && Lt
Q[m, n - 1] && NegQ[a/b]
```

Rule 331

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_.))^(p_), x_Symbol] := Dist[a^(p + (m +
1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)
^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2
^(-1)] && IntegersQ[m, p + (m + 1)/n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_.) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), Int[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]
```

Rubi steps

$$\begin{aligned}
\int (a+bx)^{5/6} \sqrt[6]{c+dx} \, dx &= \frac{(a+bx)^{11/6} \sqrt[6]{c+dx}}{2b} + \frac{(bc-ad) \int \frac{(a+bx)^{5/6}}{(c+dx)^{5/6}} \, dx}{12b} \\
&= \frac{(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12bd} + \frac{(a+bx)^{11/6} \sqrt[6]{c+dx}}{2b} - \frac{(5(bc-ad)^2) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{5/6}} \, dx}{72bd} \\
&= \frac{(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12bd} + \frac{(a+bx)^{11/6} \sqrt[6]{c+dx}}{2b} - \frac{(5(bc-ad)^2) \operatorname{Subst} \left(\int \frac{x^4}{\left(c-\frac{ad}{b}+\frac{dx}{b}\right)^{5/6}} \, dx \right)}{12b^2d} \\
&= \frac{(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12bd} + \frac{(a+bx)^{11/6} \sqrt[6]{c+dx}}{2b} - \frac{(5(bc-ad)^2) \operatorname{Subst} \left(\int \frac{x^4}{1-\frac{dx^6}{b}} \, dx \right)}{12b^2d} \\
&= \frac{(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12bd} + \frac{(a+bx)^{11/6} \sqrt[6]{c+dx}}{2b} - \frac{(5(bc-ad)^2) \operatorname{Subst} \left(\int \frac{-\frac{\sqrt[6]{b}}{2}}{\sqrt[3]{b}-\sqrt[6]{b}} \, dx \right)}{36b^{7/6}d^{5/6}} \\
&= \frac{(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12bd} + \frac{(a+bx)^{11/6} \sqrt[6]{c+dx}}{2b} - \frac{5(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt[6]{a} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{36b^{7/6}d^{11/6}} \\
&= \frac{(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12bd} + \frac{(a+bx)^{11/6} \sqrt[6]{c+dx}}{2b} - \frac{5(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt[6]{a} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{36b^{7/6}d^{11/6}} \\
&= \frac{(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12bd} + \frac{(a+bx)^{11/6} \sqrt[6]{c+dx}}{2b} - \frac{5(bc-ad)^2 \tan^{-1} \left(\frac{1-2\frac{\sqrt[6]{a} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{24\sqrt{3} b^{7/6} d^{11/6}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.17

$$\frac{6(a+bx)^{11/6} \sqrt[6]{c+dx} {}_2F_1 \left(-\frac{1}{6}, \frac{11}{6}; \frac{17}{6}; \frac{d(a+bx)}{ad-bc} \right)}{11b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)*(c + d*x)^(1/6), x]

[Out] (6*(a + b*x)^(11/6)*(c + d*x)^(1/6)*Hypergeometric2F1[-1/6, 11/6, 17/6, (d*(a + b*x))/(-(b*c) + a*d)]/(11*b*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [B] time = 1.26, size = 5633, normalized size = 13.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)*(d*x+c)^(1/6),x, algorithm="fricas")

[Out]
$$\frac{1}{144} \cdot (20 \sqrt{3} b d ((b^{12} c^{12} - 12 a b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^7 d^{11}))^{1/6} \arctan(-1/3 (2 \sqrt{3} (b^8 c^2 d^9 - 2 a b^7 c d^{10} + a^2 b^6 d^{11})) (b x + a)^{5/6} (d x + c)^{1/6} ((b^{12} c^{12} - 12 a b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^7 d^{11}))^{1/6} - 2 \sqrt{3} (b^7 d^9 x + a b^6 d^9) \sqrt{((b^3 c^2 d^2 - 2 a b^2 c d^3 + a^2 b d^4) (b x + a)^{5/6} (d x + c)^{1/6} ((b^{12} c^{12} - 12 a b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^7 d^{11}))^{1/6} + (b^4 c^4 - 4 a b^3 c^3 d + 6 a^2 b^2 c^2 d^2 - 4 a^3 b c d^3 + a^4 d^4) (b x + a)^{2/3} (d x + c)^{1/3} + (b^3 d^4 x + a b^2 d^4) ((b^{12} c^{12} - 12 a b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^7 d^{11}))^{1/6} + \sqrt{3} (a b^{12} c^{12} - 12 a^2 b^{11} c^{11} d + 66 a^3 b^{10} c^{10} d^2 - 220 a^4 b^9 c^9 d^3 + 495 a^5 b^8 c^8 d^4 - 792 a^6 b^7 c^7 d^5 + 924 a^7 b^6 c^6 d^6 - 792 a^8 b^5 c^5 d^7 + 495 a^9 b^4 c^4 d^8 - 220 a^{10} b^3 c^3 d^9 + 66 a^{11} b^2 c^2 d^{10} - 12 a^{12} b c d^{11} + a^{13} d^{12} + (b^{13} c^{12} - 12 a b^{12} c^{11} d + 66 a^2 b^{11} c^{10} d^2 - 220 a^3 b^{10} c^9 d^3 + 495 a^4 b^9 c^8 d^4 - 792 a^5 b^8 c^7 d^5 + 924 a^6 b^7 c^6 d^6 - 792 a^7 b^6 c^5 d^7 + 495 a^8 b^5 c^4 d^8 - 220 a^9 b^4 c^3 d^9 + 66 a^{10} b^3 c^2 d^{10} - 12 a^{11} b^2 c d^{11} + a^{12} b d^{12}) x)) / (a b^{12} c^{12} - 12 a^2 b^{11} c^{11} d + 66 a^3 b^{10} c^{10} d^2 - 220 a^4 b^9 c^9 d^3 + 495 a^5 b^8 c^8 d^4 - 792 a^6 b^7 c^7 d^5 + 924 a^7 b^6 c^6 d^6 - 792 a^8 b^5 c^5 d^7 + 495 a^9 b^4 c^4 d^8 - 220 a^{10} b^3 c^3 d^9 + 66 a^{11} b^2 c^2 d^{10} - 12 a^{12} b c d^{11} + a^{13} d^{12} + (b^{13} c^{12} - 12 a b^{12} c^{11} d + 66 a^2 b^{11} c^{10} d^2 - 220 a^3 b^{10} c^9 d^3 + 495 a^4 b^9 c^8 d^4 - 792 a^5 b^8 c^7 d^5 + 924 a^6 b^7 c^6 d^6 - 792 a^7 b^6 c^5 d^7 + 495 a^8 b^5 c^4 d^8 - 220 a^9 b^4 c^3 d^9 + 66 a^{10} b^3 c^2 d^{10} - 12 a^{11} b^2 c d^{11} + a^{12} b d^{12}))$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{6}} (dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)*(d*x+c)^(1/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)*(d*x + c)^(1/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{6}} (dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)*(d*x+c)^(1/6),x)

[Out] int((b*x+a)^(5/6)*(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{6}} (dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)*(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)*(d*x + c)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + bx)^{\frac{5}{6}} (c + dx)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)*(c + d*x)^(1/6),x)

[Out] int((a + b*x)^(5/6)*(c + d*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{5}{6}} \sqrt[6]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)*(d*x+c)**(1/6),x)

[Out] Integral((a + b*x)**(5/6)*(c + d*x)**(1/6), x)

$$3.1780 \quad \int \frac{(a+bx)^{5/6}}{(c+dx)^{5/6}} dx$$

Optimal. Leaf size=378

$$\frac{5(bc - ad) \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12\sqrt[6]{b} d^{11/6}} - \frac{5(bc - ad) \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12\sqrt[6]{b} d^{11/6}} - \frac{5(bc - ad) \operatorname{arctan}\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12\sqrt[6]{b} d^{11/6}}$$

[Out] $(b*x+a)^{(5/6)}*(d*x+c)^{(1/6)}/d-5/3*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(1/6)}/d^{(11/6)}+5/12*(-a*d+b*c)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)})-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}/b^{(1/6)}/d^{(11/6)}-5/12*(-a*d+b*c)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)})+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}/b^{(1/6)}/d^{(11/6)}+5/6*(-a*d+b*c)*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(1/6)}/d^{(11/6)}*3^{(1/2)}+5/6*(-a*d+b*c)*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(1/6)}/d^{(11/6)}*3^{(1/2)}$

Rubi [A] time = 0.56, antiderivative size = 378, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {50, 63, 331, 296, 634, 618, 204, 628, 208}

$$\frac{5(bc - ad) \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12\sqrt[6]{b} d^{11/6}} - \frac{5(bc - ad) \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12\sqrt[6]{b} d^{11/6}} - \frac{5(bc - ad) \operatorname{arctan}\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12\sqrt[6]{b} d^{11/6}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/6)}/(c + d*x)^{(5/6)}, x]$

[Out] $((a + b*x)^{(5/6)}*(c + d*x)^{(1/6)})/d - (5*(b*c - a*d)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(2*\operatorname{Sqrt}[3]*b^{(1/6)}*d^{(11/6)}) + (5*(b*c - a*d)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(2*\operatorname{Sqrt}[3]*b^{(1/6)}*d^{(11/6)}) - (5*(b*c - a*d)*\operatorname{ArcTanh}[(d^{(1/6)}*(a + b*x)^{(1/6)})/(b^{(1/6)}*(c + d*x)^{(1/6)})]/(3*b^{(1/6)}*d^{(11/6)}) + (5*(b*c - a*d)*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)}]/(12*b^{(1/6)}*d^{(11/6)}) - (5*(b*c - a*d)*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)}]/(12*b^{(1/6)}*d^{(11/6)})$

Rule 50

$\operatorname{Int}[(a + b*x)^m*(c + d*x)^n, x] := \operatorname{Simp}[(a + b*x)^{m+1}*(c + d*x)^n/(b*(m+n+1)), x] + \operatorname{Dist}[(n*(b*c - a*d))/$

```
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rule 296

```
Int[(x_)^(m_.)/((a_) + (b_.)*(x_)^(n_.)), x_Symbol] := Module[{r = Numerator[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r*Cos[(2*k*m*Pi)/n] - s*Cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r*Cos[(2*k*m*Pi)/n] + s*Cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^(m + 2)*Int[1/(r^2 - s^2*x^2), x])/(a*n*s^m) + Dist[(2*r^(m + 1))/(a*n*s^m), Sum[u, {k, 1, (n - 2)/4}], x], x]] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && IGtQ[m, 0] && LtQ[m, n - 1] && NegQ[a/b]
```

Rule 331

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_.))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_.) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), Int[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/6}}{(c+dx)^{5/6}} dx &= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{d} - \frac{(5(bc-ad)) \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{5/6}} dx}{6d} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{d} - \frac{(5(bc-ad)) \text{Subst} \left(\int \frac{x^4}{\left(c - \frac{ad}{b} + \frac{dx^6}{b}\right)^{5/6}} dx, x, \sqrt[6]{a+bx} \right)}{bd} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{d} - \frac{(5(bc-ad)) \text{Subst} \left(\int \frac{x^4}{1 - \frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{bd} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{d} - \frac{(5(bc-ad)) \text{Subst} \left(\int \frac{1}{\sqrt[3]{b} - \sqrt[3]{d} x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{3d^{5/3}} - \frac{(5(bc-ad)) \text{Subst} \left(\int \frac{1}{\sqrt[3]{b} - \sqrt[3]{d} x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{3d^{5/3}} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{d} - \frac{5(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3\sqrt[6]{b} d^{11/6}} + \frac{(5(bc-ad)) \text{Subst} \left(\int \frac{-\sqrt[6]{b} \sqrt[6]{d} + 2\sqrt[3]{d} x}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d} x + \sqrt[3]{d} x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{12\sqrt[6]{b} d^{11/6}} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{d} - \frac{5(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3\sqrt[6]{b} d^{11/6}} + \frac{5(bc-ad) \log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} - \frac{\sqrt[6]{b} \sqrt[6]{d}}{\sqrt[6]{c+dx}} \right)}{12\sqrt[6]{b} d^{11/6}} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{d} - \frac{5(bc-ad) \tan^{-1} \left(\frac{1 - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3} \sqrt[6]{b} d^{11/6}} + \frac{5(bc-ad) \tan^{-1} \left(\frac{1 + \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3} \sqrt[6]{b} d^{11/6}} - \frac{5(bc-ad)}{2\sqrt{3} \sqrt[6]{b} d^{11/6}}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.19

$$\frac{6(a+bx)^{11/6} \left(\frac{b(c+dx)}{bc-ad} \right)^{5/6} {}_2F_1 \left(\frac{5}{6}, \frac{11}{6}; \frac{17}{6}; \frac{d(a+bx)}{ad-bc} \right)}{11b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)/(c + d*x)^(5/6), x]

[Out] (6*(a + b*x)^(11/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[5/6, 11/6, 17/6, (d*(a + b*x))/(-b*c + a*d)]/(11*b*(c + d*x)^(5/6))

fricas [B] time = 1.28, size = 2997, normalized size = 7.93

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(5/6),x, algorithm="fricas")

[Out]
$$\begin{aligned} & -1/12*(20*\sqrt{3}*d*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(1/6)} \\ &)*\arctan(1/3*(2*\sqrt{3}*(b^2*c*d^9 - a*b*d^{10})*(b*x + a)^{(5/6})*(d*x + c)^{(1/6)} \\ &)*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(5/6)} + 2*\sqrt{3}*(b \\ & ^2*d^9*x + a*b*d^9)*\sqrt{((b*c*d^2 - a*d^3)*(b*x + a)^{(5/6})*(d*x + c)^{(1/6)} \\ &)*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(1/6)} + (b^2*c^2 - 2*a \\ & *b*c*d + a^2*d^2)*(b*x + a)^{(2/3})*(d*x + c)^{(1/3)} + (b*d^4*x + a*d^4)*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(1/3)} \\ &)/(b*x + a)*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(5/6)} + \sqrt{3}*(a*b^6*c^6 - 6*a^2*b^5*c^5*d + 15*a^3*b^4*c^4*d^2 - 20*a^4*b^3*c^3*d^3 + 15*a^5*b^2*c^2*d^4 - 6 \\ & *a^6*b*c*d^5 + a^7*d^6 + (b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20 \\ & *a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)*x)/(a \\ & *b^6*c^6 - 6*a^2*b^5*c^5*d + 15*a^3*b^4*c^4*d^2 - 20*a^4*b^3*c^3*d^3 + 15*a^5*b^2*c^2*d^4 - 6*a^6*b*c*d^5 + a^7*d^6 + (b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + \\ & a^6*b*d^6)*x) + 20*\sqrt{3}*d*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(1/6)}*\arctan(1/3*(2*\sqrt{3}*(b^2*c*d^9 - a*b*d^{10})*(b*x + a)^{(5/6})*(d*x + c)^{(1/6)} \\ &)*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(5/6)} + 2 \\ & *\sqrt{3}*(b^2*d^9*x + a*b*d^9)*\sqrt{-((b*c*d^2 - a*d^3)*(b*x + a)^{(5/6})*(d*x + c)^{(1/6)} \\ &)*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(1/6)} - (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^{(2/3})*(d*x + c)^{(1/3)} - (b*d^4*x + a \\ & *d^4)*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(1/3)} \\ &)/(b*x + a)*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(5/6)} - \sqrt{3}*(a*b^6*c^6 - 6*a^2*b^5*c^5*d + 15*a^3*b^4*c^4*d^2 - 20*a^4*b^3*c^3*d^3 + 15*a^5*b^2*c^2*d^4 - 6*a^6*b*c*d^5 + a^7*d^6 + (b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)*x) \\ &)/(a*b^6*c^6 - 6*a^2*b^5*c^5*d + 15*a^3*b^4*c^4*d^2 - 20*a^4*b^3*c^3*d^3 + 15*a^5*b^2*c^2*d^4 - 6*a^6*b*c*d^5 + a^7*d^6 + (b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)*x) \\ &) + 5*d*((b^6*c^6 - 6*a*b^5*c^5*d + 15*a^2*b^4*c^4*d^2 - 20*a^3*b^3*c^3*d^3 + 15*a^4*b^2*c^2*d^4 - 6*a^5*b*c*d^5 + a^6*d^6)/(b*d^{11}))^{(1/6)}*\log(25*((b*c*d^2 - a*d^3)*(b*x + a)^{(5/6})*(d*x + c)^{(1/6)}*(\\ & \end{aligned}$$

$$\begin{aligned} & (b^6c^6 - 6ab^5c^5d + 15a^2b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^4b^2c^2d^4 - 6a^5b^1c^1d^5 + a^6d^6)/(b^11)^{1/6} + (b^2c^2 - 2ab^1c^1d + a^2d^2)(bx + a)^{2/3}(dx + c)^{1/3} + (b^4d^4x + a^4d^4)((b^6c^6 - 6ab^5c^5d + 15a^2b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^4b^2c^2d^4 - 6a^5b^1c^1d^5 + a^6d^6)/(b^11)^{1/3})/(bx + a) - 5d((b^6c^6 - 6ab^5c^5d + 15a^2b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^4b^2c^2d^4 - 6a^5b^1c^1d^5 + a^6d^6)/(b^11)^{1/6}) \log(-25((b^1c^1d^2 - a^3d^3)(bx + a)^{5/6}(dx + c)^{1/6})((b^6c^6 - 6ab^5c^5d + 15a^2b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^4b^2c^2d^4 - 6a^5b^1c^1d^5 + a^6d^6)/(b^11)^{1/6}) - (b^2c^2 - 2ab^1c^1d + a^2d^2)(bx + a)^{2/3}(dx + c)^{1/3} - (b^4d^4x + a^4d^4)((b^6c^6 - 6ab^5c^5d + 15a^2b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^4b^2c^2d^4 - 6a^5b^1c^1d^5 + a^6d^6)/(b^11)^{1/3}))/(bx + a) + 10d((b^6c^6 - 6ab^5c^5d + 15a^2b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^4b^2c^2d^4 - 6a^5b^1c^1d^5 + a^6d^6)/(b^11)^{1/6}) \log(-5((b^1c^1 - a^1d)(bx + a)^{5/6}(dx + c)^{1/6}) + (b^2d^2x + a^2d^2)((b^6c^6 - 6ab^5c^5d + 15a^2b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^4b^2c^2d^4 - 6a^5b^1c^1d^5 + a^6d^6)/(b^11)^{1/6}))/(bx + a) - 10d((b^6c^6 - 6ab^5c^5d + 15a^2b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^4b^2c^2d^4 - 6a^5b^1c^1d^5 + a^6d^6)/(b^11)^{1/6}) \log(-5((b^1c^1 - a^1d)(bx + a)^{5/6}(dx + c)^{1/6}) - (b^2d^2x + a^2d^2)((b^6c^6 - 6ab^5c^5d + 15a^2b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^4b^2c^2d^4 - 6a^5b^1c^1d^5 + a^6d^6)/(b^11)^{1/6}))/(bx + a) - 12(bx + a)^{5/6}(dx + c)^{1/6})/d \end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(5/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(5/6), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)/(d*x+c)^(5/6),x)

[Out] int((b*x+a)^(5/6)/(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{5/6}}{(c + dx)^{5/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)/(c + d*x)^(5/6),x)

[Out] int((a + b*x)^(5/6)/(c + d*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{6}}}{(c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)/(d*x+c)**(5/6),x)

[Out] Integral((a + b*x)**(5/6)/(c + d*x)**(5/6), x)

$$3.1781 \quad \int \frac{(a+bx)^{5/6}}{(c+dx)^{11/6}} dx$$

Optimal. Leaf size=334

$$\frac{b^{5/6} \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{11/6}} + \frac{b^{5/6} \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{11/6}} + \frac{\sqrt{3} b^{5/6} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{d}}{\sqrt{3}\sqrt[6]{c+dx}}\right)}{d^{11/6}}$$

[Out] $-6/5*(b*x+a)^{(5/6)}/d/(d*x+c)^{(5/6)}+2*b^{(5/6)}*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/d^{(11/6)}-1/2*b^{(5/6)}*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)})/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}/d^{(11/6)}+1/2*b^{(5/6)}*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)})/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}/d^{(11/6)}-b^{(5/6)}*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})*3^{(1/2)}/d^{(11/6)}-b^{(5/6)}*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})*3^{(1/2)}/d^{(11/6)}$

Rubi [A] time = 0.56, antiderivative size = 334, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 63, 331, 296, 634, 618, 204, 628, 208}

$$\frac{b^{5/6} \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{11/6}} + \frac{b^{5/6} \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{11/6}} + \frac{\sqrt{3} b^{5/6} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{d}}{\sqrt{3}\sqrt[6]{c+dx}}\right)}{d^{11/6}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*x)^{(5/6)}/(c + d*x)^{(11/6)}, x]$

[Out] $(-6*(a + b*x)^{(5/6)})/(5*d*(c + d*x)^{(5/6)}) + (\operatorname{Sqrt}[3]*b^{(5/6)}*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/d^{(11/6)} - (\operatorname{Sqrt}[3]*b^{(5/6)}*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/d^{(11/6)} + (2*b^{(5/6)}*\operatorname{ArcTanh}[d^{(1/6)}*(a + b*x)^{(1/6)}/(b^{(1/6)}*(c + d*x)^{(1/6)})])/d^{(11/6)} - (b^{(5/6)}*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)}])/d^{(11/6)} + (b^{(5/6)}*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)}])/d^{(11/6)})$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{GtQ}[n, 0] \&\& \operatorname{LtQ}[m, -1] \&\& \operatorname{IntegerQ}[n] \&\& \operatorname{IntegerQ}[m]$

$rQ[m] \&\& \text{!(ILeQ}[m + n + 2, 0] \&\& (\text{FractionQ}[m] \text{ || GeQ}[2*n + m + 1, 0])) \&$
 $\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 63

$\text{Int}[\text{((a_.) + (b_.)*(x_))}^m * \text{((c_.) + (d_.)*(x_))}^n, x_Symbol] \text{ :> With}[\{p = \text{Denominator}[m]\}, \text{Dist}[p/b, \text{Subst}[\text{Int}[x^{(p*(m+1)-1)} * (c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}], x]] \text{ /; FreeQ}\{a, b, c, d\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{LtQ}[-1, m, 0] \&\& \text{LeQ}[-1, n, 0] \&\& \text{LeQ}[\text{Denominator}[n], \text{Denominator}[m]] \&\& \text{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 204

$\text{Int}[\text{((a_.) + (b_.)*(x_)^2)}^{-1}, x_Symbol] \text{ :> -Simp}[\text{ArcTan}[\text{Rt}[-b, 2]*x]/\text{Rt}[-a, 2]]/\text{Rt}[-a, 2]*\text{Rt}[-b, 2], x] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{PosQ}[a/b] \&\& (\text{LtQ}[a, 0] \text{ || LtQ}[b, 0])$

Rule 208

$\text{Int}[\text{((a_.) + (b_.)*(x_)^2)}^{-1}, x_Symbol] \text{ :> Simp}[\text{Rt}[-(a/b), 2]*\text{ArcTanh}[x/\text{Rt}[-(a/b), 2]]/a, x] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{NegQ}[a/b]$

Rule 296

$\text{Int}[(x_)^m / \text{((a_.) + (b_.)*(x_)^n)}, x_Symbol] \text{ :> Module}\{r = \text{Numerator}[\text{Rt}[-(a/b), n]], s = \text{Denominator}[\text{Rt}[-(a/b), n]], k, u\}, \text{Simp}[u = \text{Int}[(r*\text{Cos}[(2*k*m*Pi)/n] - s*\text{Cos}[(2*k*(m+1)*Pi)/n]*x)/(r^2 - 2*r*s*\text{Cos}[(2*k*Pi)/n]*x + s^2*x^2), x] + \text{Int}[(r*\text{Cos}[(2*k*m*Pi)/n] + s*\text{Cos}[(2*k*(m+1)*Pi)/n]*x)/(r^2 + 2*r*s*\text{Cos}[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^{(m+2)}*\text{Int}[1/(r^2 - s^2*x^2), x])/ (a*n*s^m) + \text{Dist}[(2*r^{(m+1)})/(a*n*s^m), \text{Sum}[u, \{k, 1, (n-2)/4\}], x], x]] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{IGtQ}[(n-2)/4, 0] \&\& \text{IGtQ}[m, 0] \&\& \text{LtQ}[m, n-1] \&\& \text{NegQ}[a/b]$

Rule 331

$\text{Int}[(x_)^m * \text{((a_.) + (b_.)*(x_)^n)}^p, x_Symbol] \text{ :> Dist}[a^{(p+(m+1)/n)}, \text{Subst}[\text{Int}[x^m / (1 - b*x^n)^{(p+(m+1)/n+1)}, x], x, x/(a + b*x^n)^{(1/n)}], x] \text{ /; FreeQ}\{a, b\}, x] \&\& \text{IGtQ}[n, 0] \&\& \text{LtQ}[-1, p, 0] \&\& \text{NeQ}[p, -2] \&\& \text{IntegersQ}[m, p + (m+1)/n]$

Rule 618

$\text{Int}[\text{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)}^{-1}, x_Symbol] \text{ :> Dist}[-2, \text{Subst}[\text{Int}[1/\text{Simp}[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] \text{ /; FreeQ}\{a, b, c\},$

$x] \&\& \text{NeQ}[b^2 - 4*a*c, 0]$

Rule 628

$\text{Int}[\frac{(d_.) + (e_.)*(x_.)}{(a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2}, x_Symbol] \rightarrow \text{Simp}[(d*\text{Log}[\text{RemoveContent}[a + b*x + c*x^2, x]])/b, x] /; \text{FreeQ}[\{a, b, c, d, e\}, x] \&\& \text{EqQ}[2*c*d - b*e, 0]$

Rule 634

$\text{Int}[\frac{(d_.) + (e_.)*(x_.)}{(a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2}, x_Symbol] \rightarrow \text{Dist}[(2*c*d - b*e)/(2*c), \text{Int}[1/(a + b*x + c*x^2), x], x] + \text{Dist}[e/(2*c), \text{Int}[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; \text{FreeQ}[\{a, b, c, d, e\}, x] \&\& \text{NeQ}[2*c*d - b*e, 0] \&\& \text{NeQ}[b^2 - 4*a*c, 0] \&\& \text{!NiceSqrtQ}[b^2 - 4*a*c]$

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/6}}{(c+dx)^{11/6}} dx &= -\frac{6(a+bx)^{5/6}}{5d(c+dx)^{5/6}} + \frac{b \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{5/6}} dx}{d} \\
&= -\frac{6(a+bx)^{5/6}}{5d(c+dx)^{5/6}} + \frac{6 \operatorname{Subst} \left(\int \frac{x^4}{\left(c - \frac{ad}{b} + \frac{dx^6}{b}\right)^{5/6}} dx, x, \sqrt[6]{a+bx} \right)}{d} \\
&= -\frac{6(a+bx)^{5/6}}{5d(c+dx)^{5/6}} + \frac{6 \operatorname{Subst} \left(\int \frac{x^4}{1 - \frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{d} \\
&= -\frac{6(a+bx)^{5/6}}{5d(c+dx)^{5/6}} + \frac{(2b^{5/6}) \operatorname{Subst} \left(\int \frac{-\frac{\sqrt[6]{b}}{2} - \frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{d^{5/3}} + \frac{(2b^{5/6}) \operatorname{Subst} \left(\int \frac{-\frac{\sqrt[6]{b}}{2} + \frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b} + \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{d^{5/3}} \\
&= -\frac{6(a+bx)^{5/6}}{5d(c+dx)^{5/6}} + \frac{2b^{5/6} \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{d^{11/6}} - \frac{b^{5/6} \operatorname{Subst} \left(\int \frac{-\sqrt[6]{b} \sqrt[6]{d} + 2\sqrt[3]{d}x}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2d^{11/6}} \\
&= -\frac{6(a+bx)^{5/6}}{5d(c+dx)^{5/6}} + \frac{2b^{5/6} \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{d^{11/6}} - \frac{b^{5/6} \log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} - \frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2d^{11/6}} + \frac{b^{5/6} \operatorname{Subst} \left(\int \frac{-\sqrt[6]{b} \sqrt[6]{d} + 2\sqrt[3]{d}x}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2d^{11/6}} \\
&= -\frac{6(a+bx)^{5/6}}{5d(c+dx)^{5/6}} + \frac{\sqrt{3} b^{5/6} \tan^{-1} \left(\frac{1 - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{d^{11/6}} - \frac{\sqrt{3} b^{5/6} \tan^{-1} \left(\frac{1 + \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{d^{11/6}} + \frac{2b^{5/6} \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{d^{11/6}}
\end{aligned}$$

Mathematica [C] time = 0.07, size = 73, normalized size = 0.22

$$\frac{6(a+bx)^{11/6} \left(\frac{b(c+dx)}{bc-ad} \right)^{11/6} {}_2F_1 \left(\frac{11}{6}, \frac{11}{6}; \frac{17}{6}; \frac{d(a+bx)}{ad-bc} \right)}{11b(c+dx)^{11/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)/(c + d*x)^(11/6), x]

[Out] (6*(a + b*x)^(11/6)*((b*(c + d*x))/(b*c - a*d))^(11/6)*Hypergeometric2F1[11/6, 11/6, 17/6, (d*(a + b*x))/(-(b*c) + a*d)]/(11*b*(c + d*x)^(11/6))

fricas [B] time = 1.01, size = 755, normalized size = 2.26

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(11/6),x, algorithm="fricas")

[Out]
$$\begin{aligned} & -1/10*(20*\sqrt{3}*(d^2*x + c*d)*(b^5/d^{11})^{1/6}*\arctan(-1/3*(2*\sqrt{3})*(b*x + a)^{5/6}*(d*x + c)^{1/6}*b*d^9*(b^5/d^{11})^{5/6} - 2*\sqrt{3}*(b*d^9*x + a*d^9)*\sqrt{((b*x + a)^{5/6}*(d*x + c)^{1/6}*b*d^2*(b^5/d^{11})^{1/6} + (b*x + a)^{2/3}*(d*x + c)^{1/3}*b^2 + (b*d^4*x + a*d^4)*(b^5/d^{11})^{1/3}})/(b*x + a))*(b^5/d^{11})^{5/6} + \sqrt{3}*(b^6*x + a*b^5))/(b^6*x + a*b^5)) + 20*\sqrt{3}*(d^2*x + c*d)*(b^5/d^{11})^{1/6}*\arctan(-1/3*(2*\sqrt{3})*(b*x + a)^{5/6}*(d*x + c)^{1/6}*b*d^9*(b^5/d^{11})^{5/6} - 2*\sqrt{3}*(b*d^9*x + a*d^9)*\sqrt{-(b*x + a)^{5/6}*(d*x + c)^{1/6}*b*d^2*(b^5/d^{11})^{1/6} - (b*x + a)^{2/3}*(d*x + c)^{1/3}*b^2 - (b*d^4*x + a*d^4)*(b^5/d^{11})^{1/3}})/(b*x + a))*(b^5/d^{11})^{5/6} - \sqrt{3}*(b^6*x + a*b^5))/(b^6*x + a*b^5)) - 5*(d^2*x + c*d)*(b^5/d^{11})^{1/6}*\log(4*((b*x + a)^{5/6}*(d*x + c)^{1/6}*b*d^2*(b^5/d^{11})^{1/6} + (b*x + a)^{2/3}*(d*x + c)^{1/3}*b^2 + (b*d^4*x + a*d^4)*(b^5/d^{11})^{1/3}))/((b*x + a)) + 5*(d^2*x + c*d)*(b^5/d^{11})^{1/6}*\log(-4*((b*x + a)^{5/6}*(d*x + c)^{1/6}*b*d^2*(b^5/d^{11})^{1/6} - (b*x + a)^{2/3}*(d*x + c)^{1/3}*b^2 - (b*d^4*x + a*d^4)*(b^5/d^{11})^{1/3}))/((b*x + a)) - 10*(d^2*x + c*d)*(b^5/d^{11})^{1/6}*\log(((b*x + a)^{5/6}*(d*x + c)^{1/6}*b + (b*d^2*x + a*d^2)*(b^5/d^{11})^{1/6}))/((b*x + a)) + 10*(d^2*x + c*d)*(b^5/d^{11})^{1/6}*\log(((b*x + a)^{5/6}*(d*x + c)^{1/6}*b - (b*d^2*x + a*d^2)*(b^5/d^{11})^{1/6}))/((b*x + a)) + 12*(b*x + a)^{5/6}*(d*x + c)^{1/6}))/((d^2*x + c*d)) \end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{6}}}{(dx+c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(11/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(11/6), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{6}}}{(dx+c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)/(d*x+c)^(11/6),x)

[Out] int((b*x+a)^(5/6)/(d*x+c)^(11/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(11/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(11/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{5/6}}{(c + dx)^{11/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)/(c + d*x)^(11/6),x)

[Out] int((a + b*x)^(5/6)/(c + d*x)^(11/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{6}}}{(c + dx)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)/(d*x+c)**(11/6),x)

[Out] Integral((a + b*x)**(5/6)/(c + d*x)**(11/6), x)

$$3.1782 \quad \int \frac{(a+bx)^{5/6}}{(c+dx)^{17/6}} dx$$

Optimal. Leaf size=32

$$\frac{6(a+bx)^{11/6}}{11(c+dx)^{11/6}(bc-ad)}$$

[Out] 6/11*(b*x+a)^(11/6)/(-a*d+b*c)/(d*x+c)^(11/6)

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{6(a+bx)^{11/6}}{11(c+dx)^{11/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/6)/(c + d*x)^(17/6), x]

[Out] (6*(a + b*x)^(11/6))/(11*(b*c - a*d)*(c + d*x)^(11/6))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(a+bx)^{5/6}}{(c+dx)^{17/6}} dx = \frac{6(a+bx)^{11/6}}{11(bc-ad)(c+dx)^{11/6}}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 1.00

$$\frac{6(a+bx)^{11/6}}{11(c+dx)^{11/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)/(c + d*x)^(17/6), x]

[Out] (6*(a + b*x)^(11/6))/(11*(b*c - a*d)*(c + d*x)^(11/6))

fricas [B] time = 0.79, size = 65, normalized size = 2.03

$$\frac{6 (bx + a)^{\frac{11}{6}} (dx + c)^{\frac{1}{6}}}{11 (bc^3 - ac^2d + (bcd^2 - ad^3)x^2 + 2(bc^2d - acd^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(17/6),x, algorithm="fricas")

[Out] 6/11*(b*x + a)^(11/6)*(d*x + c)^(1/6)/(b*c^3 - a*c^2*d + (b*c*d^2 - a*d^3)*x^2 + 2*(b*c^2*d - a*c*d^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(17/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(17/6), x)

maple [A] time = 0.00, size = 27, normalized size = 0.84

$$\frac{6 (bx + a)^{\frac{11}{6}}}{11 (dx + c)^{\frac{11}{6}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)/(d*x+c)^(17/6),x)

[Out] -6/11*(b*x+a)^(11/6)/(d*x+c)^(11/6)/(a*d-b*c)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(17/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(17/6), x)

mupad [B] time = 0.59, size = 130, normalized size = 4.06

$$\frac{\left(\frac{6a(a+bx)^{5/6}}{11ad^3-11bcd^2} + \frac{6bx(a+bx)^{5/6}}{11ad^3-11bcd^2}\right)(c+dx)^{1/6}}{x^2 - \frac{11bc^3-11a^2d}{11ad^3-11bcd^2} + \frac{22cdx(ad-bc)}{11ad^3-11bcd^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)/(c + d*x)^(17/6),x)

[Out] -(((6*a*(a + b*x)^(5/6))/(11*a*d^3 - 11*b*c*d^2) + (6*b*x*(a + b*x)^(5/6))/(11*a*d^3 - 11*b*c*d^2))*(c + d*x)^(1/6))/(x^2 - (11*b*c^3 - 11*a*c^2*d)/(11*a*d^3 - 11*b*c*d^2) + (22*c*d*x*(a*d - b*c))/(11*a*d^3 - 11*b*c*d^2))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)/(d*x+c)**(17/6),x)

[Out] Timed out

$$3.1783 \quad \int \frac{(a+bx)^{5/6}}{(c+dx)^{23/6}} dx$$

Optimal. Leaf size=66

$$\frac{36b(a+bx)^{11/6}}{187(c+dx)^{11/6}(bc-ad)^2} + \frac{6(a+bx)^{11/6}}{17(c+dx)^{17/6}(bc-ad)}$$

[Out] $6/17*(b*x+a)^{(11/6)/(-a*d+b*c)/(d*x+c)^{(17/6)+36/187*b*(b*x+a)^{(11/6)/(-a*d+b*c)^2/(d*x+c)^{(11/6)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{36b(a+bx)^{11/6}}{187(c+dx)^{11/6}(bc-ad)^2} + \frac{6(a+bx)^{11/6}}{17(c+dx)^{17/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/6)/(c + d*x)^(23/6), x]

[Out] $(6*(a + b*x)^{(11/6))/(17*(b*c - a*d)*(c + d*x)^{(17/6))} + (36*b*(a + b*x)^{(11/6))/(187*(b*c - a*d)^2*(c + d*x)^{(11/6))}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[n] && !IntegerQ[m] && !IntegerQ[n]

Rubi steps

$$\int \frac{(a+bx)^{5/6}}{(c+dx)^{23/6}} dx = \frac{6(a+bx)^{11/6}}{17(bc-ad)(c+dx)^{17/6}} + \frac{(6b) \int \frac{(a+bx)^{5/6}}{(c+dx)^{17/6}} dx}{17(bc-ad)}$$

$$= \frac{6(a+bx)^{11/6}}{17(bc-ad)(c+dx)^{17/6}} + \frac{36b(a+bx)^{11/6}}{187(bc-ad)^2(c+dx)^{11/6}}$$

Mathematica [A] time = 0.03, size = 46, normalized size = 0.70

$$\frac{6(a+bx)^{11/6}(-11ad+17bc+6bdx)}{187(c+dx)^{17/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)/(c + d*x)^(23/6), x]

[Out] (6*(a + b*x)^(11/6)*(17*b*c - 11*a*d + 6*b*d*x))/(187*(b*c - a*d)^2*(c + d*x)^(17/6))

fricas [B] time = 0.90, size = 175, normalized size = 2.65

$$\frac{6(6b^2dx^2 + 17abc - 11a^2d + (17b^2c - 5abd)x)(bx+a)^{5/6}(dx+c)^{1/6}}{187(b^2c^5 - 2abc^4d + a^2c^3d^2 + (b^2c^2d^3 - 2abcd^4 + a^2d^5)x^3 + 3(b^2c^3d^2 - 2abc^2d^3 + a^2cd^4)x^2 + 3(b^2c^4d - 2abc^3d^2 + a^2c^2d^3)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(23/6), x, algorithm="fricas")

[Out] 6/187*(6*b^2*d*x^2 + 17*a*b*c - 11*a^2*d + (17*b^2*c - 5*a*b*d)*x)*(b*x + a)^(5/6)*(d*x + c)^(1/6)/(b^2*c^5 - 2*a*b*c^4*d + a^2*c^3*d^2 + (b^2*c^2*d^3 - 2*a*b*c*d^4 + a^2*d^5)*x^3 + 3*(b^2*c^3*d^2 - 2*a*b*c^2*d^3 + a^2*c*d^4)*x^2 + 3*(b^2*c^4*d - 2*a*b*c^3*d^2 + a^2*c^2*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{5/6}}{(dx+c)^{23/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(23/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(23/6), x)

maple [A] time = 0.00, size = 54, normalized size = 0.82

$$\frac{6 (bx + a)^{\frac{11}{6}} (-6bdx + 11ad - 17bc)}{187 (dx + c)^{\frac{17}{6}} (a^2d^2 - 2abcd + b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)/(d*x+c)^(23/6),x)

[Out] $-6/187*(b*x+a)^{(11/6)}*(-6*b*d*x+11*a*d-17*b*c)/(d*x+c)^{(17/6)}/(a^2*d^2-2*a*b*c*d+b^2*c^2)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{23}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(23/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(23/6), x)

mupad [B] time = 0.74, size = 137, normalized size = 2.08

$$\frac{(c + dx)^{1/6} \left(\frac{36 b^2 x^2 (a+bx)^{5/6}}{187 d^2 (a d - b c)^2} - \frac{(66 a^2 d - 102 a b c) (a+bx)^{5/6}}{187 d^3 (a d - b c)^2} + \frac{x (102 b^2 c - 30 a b d) (a+bx)^{5/6}}{187 d^3 (a d - b c)^2} \right)}{x^3 + \frac{c^3}{d^3} + \frac{3 c x^2}{d} + \frac{3 c^2 x}{d^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)/(c + d*x)^(23/6),x)

[Out] $((c + d*x)^{(1/6)}*((36*b^2*x^2*(a + b*x)^{(5/6)})/(187*d^2*(a*d - b*c)^2) - ((66*a^2*d - 102*a*b*c)*(a + b*x)^{(5/6)})/(187*d^3*(a*d - b*c)^2) + (x*(102*b^2*c - 30*a*b*d)*(a + b*x)^{(5/6)})/(187*d^3*(a*d - b*c)^2)))/(x^3 + c^3/d^3 + (3*c*x^2)/d + (3*c^2*x)/d^2)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)/(d*x+c)**(23/6),x)

[Out] Timed out

$$3.1784 \quad \int \frac{(a+bx)^{5/6}}{(c+dx)^{29/6}} dx$$

Optimal. Leaf size=101

$$\frac{432b^2(a+bx)^{11/6}}{4301(c+dx)^{11/6}(bc-ad)^3} + \frac{72b(a+bx)^{11/6}}{391(c+dx)^{17/6}(bc-ad)^2} + \frac{6(a+bx)^{11/6}}{23(c+dx)^{23/6}(bc-ad)}$$

[Out] $6/23*(b*x+a)^{(11/6)/(-a*d+b*c)/(d*x+c)^{(23/6)}+72/391*b*(b*x+a)^{(11/6)/(-a*d+b*c)^2/(d*x+c)^{(17/6)}+432/4301*b^2*(b*x+a)^{(11/6)/(-a*d+b*c)^3/(d*x+c)^{(11/6)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{432b^2(a+bx)^{11/6}}{4301(c+dx)^{11/6}(bc-ad)^3} + \frac{72b(a+bx)^{11/6}}{391(c+dx)^{17/6}(bc-ad)^2} + \frac{6(a+bx)^{11/6}}{23(c+dx)^{23/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/6)/(c + d*x)^(29/6), x]

[Out] $(6*(a + b*x)^{(11/6)})/(23*(b*c - a*d)*(c + d*x)^{(23/6)}) + (72*b*(a + b*x)^{(11/6)})/(391*(b*c - a*d)^2*(c + d*x)^{(17/6)}) + (432*b^2*(a + b*x)^{(11/6)})/(4301*(b*c - a*d)^3*(c + d*x)^{(11/6)})$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{
  a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
  1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
  ((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
  + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
  LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
  (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
  Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/6}}{(c+dx)^{29/6}} dx &= \frac{6(a+bx)^{11/6}}{23(bc-ad)(c+dx)^{23/6}} + \frac{(12b) \int \frac{(a+bx)^{5/6}}{(c+dx)^{23/6}} dx}{23(bc-ad)} \\
&= \frac{6(a+bx)^{11/6}}{23(bc-ad)(c+dx)^{23/6}} + \frac{72b(a+bx)^{11/6}}{391(bc-ad)^2(c+dx)^{17/6}} + \frac{(72b^2) \int \frac{(a+bx)^{5/6}}{(c+dx)^{17/6}} dx}{391(bc-ad)^2} \\
&= \frac{6(a+bx)^{11/6}}{23(bc-ad)(c+dx)^{23/6}} + \frac{72b(a+bx)^{11/6}}{391(bc-ad)^2(c+dx)^{17/6}} + \frac{432b^2(a+bx)^{11/6}}{4301(bc-ad)^3(c+dx)^{11/6}}
\end{aligned}$$

Mathematica [A] time = 0.06, size = 77, normalized size = 0.76

$$\frac{6(a+bx)^{11/6} (187a^2d^2 - 22abd(23c+6dx) + b^2(391c^2 + 276cdx + 72d^2x^2))}{4301(c+dx)^{23/6}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)/(c + d*x)^(29/6), x]

[Out] (6*(a + b*x)^(11/6)*(187*a^2*d^2 - 22*a*b*d*(23*c + 6*d*x) + b^2*(391*c^2 + 276*c*d*x + 72*d^2*x^2)))/(4301*(b*c - a*d)^3*(c + d*x)^(23/6))

fricas [B] time = 1.12, size = 338, normalized size = 3.35

$$\frac{6(72b^3d^2x^3 + 391ab^2c^2 - 506a^2bcd + 187a^3d^2 + 12(23b^3cd - 5a^2b^2d^2))x^2 + (391b^3c^2 - 230a^2b^2cd + 55a^2b^2d^2)x + (b^3c^4d^3 - a^3c^4d^3 + (b^3c^3d^4 - 3ab^2c^2d^5 + 3a^2bcd^6 - a^3d^7))x^4 + 4(b^3c^4d^3 - 3ab^2c^3d^4 - 3a^2b^2c^5d^2 + 3a^2b^2c^4d^3 + 3a^2b^2c^3d^4 - a^3c^2d^5)x^2 + 4(b^3c^6d - 3a^2b^2c^5d^2 + 3a^2b^2c^4d^3 - a^3c^3d^4)x}{4301(b^3c^7 - 3ab^2c^6d + 3a^2bc^5d^2 - a^3c^4d^3 + (b^3c^3d^4 - 3ab^2c^2d^5 + 3a^2bcd^6 - a^3d^7))x^4 + 4(b^3c^4d^3 - 3ab^2c^3d^4 - 3a^2b^2c^5d^2 + 3a^2b^2c^4d^3 - a^3c^2d^5)x^2 + 4(b^3c^6d - 3a^2b^2c^5d^2 + 3a^2b^2c^4d^3 - a^3c^3d^4)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(29/6), x, algorithm="fricas")

[Out] 6/4301*(72*b^3*d^2*x^3 + 391*a*b^2*c^2 - 506*a^2*b*c*d + 187*a^3*d^2 + 12*(23*b^3*c*d - 5*a*b^2*d^2))*x^2 + (391*b^3*c^2 - 230*a*b^2*c*d + 55*a^2*b*d^2)*x*(b*x + a)^(5/6)*(d*x + c)^(1/6)/(b^3*c^7 - 3*a*b^2*c^6*d + 3*a^2*b*c^5*d^2 - a^3*c^4*d^3 + (b^3*c^3*d^4 - 3*a*b^2*c^2*d^5 + 3*a^2*b*c*d^6 - a^3*d^7))*x^4 + 4*(b^3*c^4*d^3 - 3*a*b^2*c^3*d^4 + 3*a^2*b*c^2*d^5 - a^3*c*d^6)*x^3 + 6*(b^3*c^5*d^2 - 3*a*b^2*c^4*d^3 + 3*a^2*b*c^3*d^4 - a^3*c^2*d^5)*x^2 + 4*(b^3*c^6*d - 3*a*b^2*c^5*d^2 + 3*a^2*b*c^4*d^3 - a^3*c^3*d^4)*x

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{6}}}{(dx+c)^{\frac{29}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(29/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(29/6), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{6 (bx + a)^{\frac{11}{6}} (72b^2x^2d^2 - 132abd^2x + 276b^2cdx + 187a^2d^2 - 506abcd + 391b^2c^2)}{4301 (dx + c)^{\frac{23}{6}} (a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)/(d*x+c)^(29/6),x)

[Out] -6/4301*(b*x+a)^(11/6)*(72*b^2*d^2*x^2-132*a*b*d^2*x+276*b^2*c*d*x+187*a^2*d^2-506*a*b*c*d+391*b^2*c^2)/(d*x+c)^(23/6)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{29}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(29/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(29/6), x)

mupad [B] time = 0.94, size = 214, normalized size = 2.12

$$\frac{(c + dx)^{1/6} \left(\frac{(a+bx)^{5/6} (1122a^3d^2 - 3036a^2bcd + 2346ab^2c^2)}{4301d^4(ad-bc)^3} + \frac{432b^3x^3(a+bx)^{5/6}}{4301d^2(ad-bc)^3} + \frac{x(a+bx)^{5/6} (330a^2bd^2 - 1380ab^2cd + 2346b^3c^2)}{4301d^4(ad-bc)^3} \right)}{x^4 + \frac{c^4}{d^4} + \frac{4cx^3}{d} + \frac{4c^3x}{d^3} + \frac{6c^2x^2}{d^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)/(c + d*x)^(29/6),x)

[Out] -((c + d*x)^(1/6)*((a + b*x)^(5/6)*(1122*a^3*d^2 + 2346*a*b^2*c^2 - 3036*a^2*b*c*d))/(4301*d^4*(a*d - b*c)^3) + (432*b^3*x^3*(a + b*x)^(5/6))/(4301*d^2*(a*d - b*c)^3) + (x*(a + b*x)^(5/6)*(2346*b^3*c^2 + 330*a^2*b*d^2 - 1380*a*b^2*c*d))/(4301*d^4*(a*d - b*c)^3) - (72*b^2*x^2*(5*a*d - 23*b*c)*(a + b

$$\frac{x^{5/6}}{(4301d^3(ad - bc)^3)} \cdot \frac{1}{(x^4 + c^4/d^4 + (4cx^3)/d + (4c^3x)/d^3 + (6c^2x^2)/d^2)}$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)/(d*x+c)**(29/6),x)

[Out] Timed out

$$3.1785 \quad \int \frac{(a+bx)^{5/6}}{(c+dx)^{35/6}} dx$$

Optimal. Leaf size=136

$$\frac{7776b^3(a+bx)^{11/6}}{124729(c+dx)^{11/6}(bc-ad)^4} + \frac{1296b^2(a+bx)^{11/6}}{11339(c+dx)^{17/6}(bc-ad)^3} + \frac{108b(a+bx)^{11/6}}{667(c+dx)^{23/6}(bc-ad)^2} + \frac{6(a+bx)^{11/6}}{29(c+dx)^{29/6}(bc-ad)}$$

[Out] $6/29*(b*x+a)^{(11/6)/(-a*d+b*c)/(d*x+c)^{(29/6)}+108/667*b*(b*x+a)^{(11/6)/(-a*d+b*c)^2/(d*x+c)^{(23/6)}+1296/11339*b^2*(b*x+a)^{(11/6)/(-a*d+b*c)^3/(d*x+c)^{(17/6)}+7776/124729*b^3*(b*x+a)^{(11/6)/(-a*d+b*c)^4/(d*x+c)^{(11/6)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{7776b^3(a+bx)^{11/6}}{124729(c+dx)^{11/6}(bc-ad)^4} + \frac{1296b^2(a+bx)^{11/6}}{11339(c+dx)^{17/6}(bc-ad)^3} + \frac{108b(a+bx)^{11/6}}{667(c+dx)^{23/6}(bc-ad)^2} + \frac{6(a+bx)^{11/6}}{29(c+dx)^{29/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/6)/(c + d*x)^(35/6), x]

[Out] $(6*(a + b*x)^{(11/6)})/(29*(b*c - a*d)*(c + d*x)^{(29/6)}) + (108*b*(a + b*x)^{(11/6)})/(667*(b*c - a*d)^2*(c + d*x)^{(23/6)}) + (1296*b^2*(a + b*x)^{(11/6)})/(11339*(b*c - a*d)^3*(c + d*x)^{(17/6)}) + (7776*b^3*(a + b*x)^{(11/6)})/(124729*(b*c - a*d)^4*(c + d*x)^{(11/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{5/6}}{(c+dx)^{35/6}} dx &= \frac{6(a+bx)^{11/6}}{29(bc-ad)(c+dx)^{29/6}} + \frac{(18b) \int \frac{(a+bx)^{5/6}}{(c+dx)^{29/6}} dx}{29(bc-ad)} \\
&= \frac{6(a+bx)^{11/6}}{29(bc-ad)(c+dx)^{29/6}} + \frac{108b(a+bx)^{11/6}}{667(bc-ad)^2(c+dx)^{23/6}} + \frac{(216b^2) \int \frac{(a+bx)^{5/6}}{(c+dx)^{23/6}} dx}{667(bc-ad)^2} \\
&= \frac{6(a+bx)^{11/6}}{29(bc-ad)(c+dx)^{29/6}} + \frac{108b(a+bx)^{11/6}}{667(bc-ad)^2(c+dx)^{23/6}} + \frac{1296b^2(a+bx)^{11/6}}{11339(bc-ad)^3(c+dx)^{17/6}} + \frac{(1296b^3) \int \frac{(a+bx)^{5/6}}{(c+dx)^{17/6}} dx}{11339(bc-ad)^3} \\
&= \frac{6(a+bx)^{11/6}}{29(bc-ad)(c+dx)^{29/6}} + \frac{108b(a+bx)^{11/6}}{667(bc-ad)^2(c+dx)^{23/6}} + \frac{1296b^2(a+bx)^{11/6}}{11339(bc-ad)^3(c+dx)^{17/6}} + \frac{1296b^3(a+bx)^{11/6}}{124729(bc-ad)^4}
\end{aligned}$$

Mathematica [A] time = 0.09, size = 118, normalized size = 0.87

$$\frac{6(a+bx)^{11/6} \left(-4301a^3d^3 + 561a^2bd^2(29c+6dx) - 33ab^2d(667c^2 + 348cdx + 72d^2x^2) + b^3(11339c^3 + 12006c^2dx + 264cd^2x^2 + 1296d^3x^3) \right)}{124729(c+dx)^{29/6}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)/(c + d*x)^(35/6), x]

[Out] (6*(a + b*x)^(11/6)*(-4301*a^3*d^3 + 561*a^2*b*d^2*(29*c + 6*d*x) - 33*a*b^2*d*(667*c^2 + 348*c*d*x + 72*d^2*x^2) + b^3*(11339*c^3 + 12006*c^2*d*x + 264*c*d^2*x^2 + 1296*d^3*x^3)))/(124729*(b*c - a*d)^4*(c + d*x)^(29/6))

fricas [B] time = 0.81, size = 533, normalized size = 3.92

$$\frac{6 \left(1296b^4d^3x^4 + 11339ab^3c^3 - 22011a^2b^2c^2d + 16269a^3b^2cd^2 - 4301a^4d^3 + 216(29b^4cd^2 - 5ab^3d^3)x^3 + 18(667b^4c^2d - 290ab^3cd^2 + 55a^2b^2d^3)x^2 + (11339b^4c^3 - 10005a^3b^3c^2d + 4785a^2b^2cd^2 - 935a^3b^2d^3)x \right) (b*x + a)^{5/6} (d*x + c)^{1/6}}{124729 \left(b^4c^9 - 4ab^3c^8d + 6a^2b^2c^7d^2 - 4a^3bc^6d^3 + a^4c^5d^4 + (b^4c^4d^5 - 4ab^3c^3d^6 + 6a^2b^2c^2d^7 - 4a^3bcd^8 + a^4d^9)x^5 + 5(b^4c^5d^4 - 4ab^3c^4d^5 + 6a^2b^2c^3d^6 - 4a^3b^2cd^7 + a^4c^2d^8)x^4 + 10(b^4c^6d^3 - 4ab^3c^5d^4 + 6a^2b^2c^4d^5 - 4a^3b^2cd^6 + a^4c^3d^7)x^3 + 10(b^4c^7d^2 - 4ab^3c^6d^3 + 6a^2b^2c^5d^4 - 4a^3b^2cd^5 + a^4c^4d^6)x^2 + 10(b^4c^8d - 4ab^3c^7d^2 + 6a^2b^2c^6d^3 - 4a^3b^2cd^4 + a^4c^5d^5)x + 10(b^4c^9 - 4ab^3c^8d + 6a^2b^2c^7d^2 - 4a^3bcd^8 + a^4d^9) \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(35/6), x, algorithm="fricas")

[Out] 6/124729*(1296*b^4*d^3*x^4 + 11339*a*b^3*c^3 - 22011*a^2*b^2*c^2*d + 16269*a^3*b^2*c*d^2 - 4301*a^4*d^3 + 216*(29*b^4*c*d^2 - 5*a*b^3*d^3)*x^3 + 18*(667*b^4*c^2*d - 290*a*b^3*c*d^2 + 55*a^2*b^2*d^3)*x^2 + (11339*b^4*c^3 - 10005*a^3*b^3*c^2*d + 4785*a^2*b^2*c*d^2 - 935*a^3*b^2*d^3)*x)*(b*x + a)^(5/6)*(d*x + c)^(1/6)/(b^4*c^9 - 4*a*b^3*c^8*d + 6*a^2*b^2*c^7*d^2 - 4*a^3*b^2*c^6*d^3 + a^4*c^5*d^4 + (b^4*c^4*d^5 - 4*a*b^3*c^3*d^6 + 6*a^2*b^2*c^2*d^7 - 4*a^3*b^2*c*d^8 + a^4*d^9)*x^5 + 5*(b^4*c^5*d^4 - 4*a*b^3*c^4*d^5 + 6*a^2*b^2*c^3*d^6 - 4*a^3*b^2*c^2*d^7 + a^4*c*d^8)*x^4 + 10*(b^4*c^6*d^3 - 4*a*b^3*c^5*d^4 + 6*a^2*b^2*c^4*d^5 - 4*a^3*b^2*c^3*d^6 + a^4*c^2*d^7)*x^3 + 10*(b^4*c^7*d^2 - 4*a*b^3*c^6*d^3 + 6*a^2*b^2*c^5*d^4 - 4*a^3*b^2*c^4*d^5 + a^4*c^3*d^6)*x^2 + 10*(b^4*c^8*d - 4*a*b^3*c^7*d^2 + 6*a^2*b^2*c^6*d^3 - 4*a^3*b^2*c^5*d^4 + a^4*c^4*d^5)*x + 10*(b^4*c^9 - 4*a*b^3*c^8*d + 6*a^2*b^2*c^7*d^2 - 4*a^3*b^2*c^6*d^3 + a^4*c^5*d^5))

$$6*a^2*b^2*c^4*d^5 - 4*a^3*b*c^3*d^6 + a^4*c^2*d^7)*x^3 + 10*(b^4*c^7*d^2 - 4*a*b^3*c^6*d^3 + 6*a^2*b^2*c^5*d^4 - 4*a^3*b*c^4*d^5 + a^4*c^3*d^6)*x^2 + 5*(b^4*c^8*d - 4*a*b^3*c^7*d^2 + 6*a^2*b^2*c^6*d^3 - 4*a^3*b*c^5*d^4 + a^4*c^4*d^5)*x)$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{6}}}{(dx+c)^{\frac{35}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(35/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(35/6), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{6(bx+a)^{\frac{11}{6}}(-1296b^3d^3x^3+2376ab^2d^3x^2-6264b^3cd^2x^2-3366a^2bd^3x+11484ab^2cd^2x-12006b^3c^2dx+43128b^3c^2d^2x-12006b^3c^2d^2x+43128b^3c^2d^2x-12006b^3c^2d^2x+43128b^3c^2d^2x)}{124729(dx+c)^{\frac{29}{6}}(a^4d^4-4a^3bcd^3+6a^2b^2c^2d^2-4ab^3c^3d+b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)/(d*x+c)^(35/6),x)

[Out] -6/124729*(b*x+a)^(11/6)*(-1296*b^3*d^3*x^3+2376*a*b^2*d^3*x^2-6264*b^3*c*d^3*x^2-3366*a^2*b*d^3*x+11484*a*b^2*c*d^2*x-12006*b^3*c^2*d*x+4301*a^3*d^3-16269*a^2*b*c*d^2+22011*a*b^2*c^2*d-11339*b^3*c^3)/(d*x+c)^(29/6)/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{6}}}{(dx+c)^{\frac{35}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(35/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(35/6), x)

mupad [B] time = 1.16, size = 303, normalized size = 2.23

$$(c+dx)^{1/6} \left(\frac{7776b^4x^4(a+bx)^{5/6}}{124729d^2(ad-bc)^4} - \frac{(a+bx)^{5/6}(25806a^4d^3-97614a^3bcd^2+132066a^2b^2c^2d-68034ab^3c^3)}{124729d^5(ad-bc)^4} \right) + \frac{x(a+bx)^{5/6}(-5610a^3bd^3+28710a^2b^2cd^2-12006ab^3c^2d+43128b^3c^2d^2)}{124729d^5(ad-bc)^4} + x^5 + \frac{c^5}{d^5} + \frac{5cx^4}{d} + \frac{5c^4x}{d^4} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^{(5/6)}/(c + d*x)^{(35/6)}, x)$

[Out] $((c + d*x)^{(1/6)}*((7776*b^4*x^4*(a + b*x)^{(5/6)})/(124729*d^2*(a*d - b*c)^4) - ((a + b*x)^{(5/6)}*(25806*a^4*d^3 - 68034*a*b^3*c^3 + 132066*a^2*b^2*c^2*d - 97614*a^3*b*c*d^2)))/(124729*d^5*(a*d - b*c)^4) + (x*(a + b*x)^{(5/6)}*(68034*b^4*c^3 - 5610*a^3*b*d^3 + 28710*a^2*b^2*c*d^2 - 60030*a*b^3*c^2*d))/(124729*d^5*(a*d - b*c)^4) + (108*b^2*x^2*(a + b*x)^{(5/6)}*(55*a^2*d^2 + 667*b^2*c^2 - 290*a*b*c*d))/(124729*d^4*(a*d - b*c)^4) - (1296*b^3*x^3*(5*a*d - 29*b*c)*(a + b*x)^{(5/6)})/(124729*d^3*(a*d - b*c)^4))/(x^5 + c^5/d^5 + (5*c*x^4)/d + (5*c^4*x)/d^4 + (10*c^2*x^3)/d^2 + (10*c^3*x^2)/d^3)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)^{(5/6)}/(d*x+c)^{(35/6)}, x)$

[Out] Timed out

3.1786 $\int (a + bx)^{5/6} (c + dx)^{11/6} dx$

Optimal. Leaf size=82

$$\frac{6(a + bx)^{11/6}(c + dx)^{5/6}(bc - ad) {}_2F_1\left(-\frac{11}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11b^2 \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

[Out] 6/11*(-a*d+b*c)*(b*x+a)^(11/6)*(d*x+c)^(5/6)*hypergeom([-11/6, 11/6], [17/6], -d*(b*x+a)/(-a*d+b*c))/b^2/(b*(d*x+c)/(-a*d+b*c))^(5/6)

Rubi [A] time = 0.03, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a + bx)^{11/6}(c + dx)^{5/6}(bc - ad) {}_2F_1\left(-\frac{11}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11b^2 \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/6)*(c + d*x)^(11/6), x]

[Out] (6*(b*c - a*d)*(a + b*x)^(11/6)*(c + d*x)^(5/6)*Hypergeometric2F1[-11/6, 11/6, 17/6, -((d*(a + b*x))/(b*c - a*d))]/(11*b^2*((b*(c + d*x))/(b*c - a*d))^(5/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/(b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n], Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int (a + bx)^{5/6} (c + dx)^{11/6} dx = \frac{((bc - ad)(c + dx)^{5/6}) \int (a + bx)^{5/6} \left(\frac{bc}{bc - ad} + \frac{bdx}{bc - ad} \right)^{11/6} dx}{b \left(\frac{b(c+dx)}{bc - ad} \right)^{5/6}}$$

$$= \frac{6(bc - ad)(a + bx)^{11/6} (c + dx)^{5/6} {}_2F_1 \left(-\frac{11}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc - ad} \right)}{11b^2 \left(\frac{b(c+dx)}{bc - ad} \right)^{5/6}}$$

Mathematica [A] time = 0.08, size = 73, normalized size = 0.89

$$\frac{6(a + bx)^{11/6} (c + dx)^{11/6} {}_2F_1 \left(-\frac{11}{6}, \frac{11}{6}; \frac{17}{6}; \frac{d(a+bx)}{ad - bc} \right)}{11b \left(\frac{b(c+dx)}{bc - ad} \right)^{11/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)*(c + d*x)^(11/6), x]

[Out] (6*(a + b*x)^(11/6)*(c + d*x)^(11/6)*Hypergeometric2F1[-11/6, 11/6, 17/6, (d*(a + b*x))/(-b*c) + a*d])/(11*b*((b*(c + d*x))/(b*c - a*d))^(11/6))

fricas [F] time = 1.78, size = 0, normalized size = 0.00

$$\text{integral} \left((bx + a)^{\frac{5}{6}} (dx + c)^{\frac{11}{6}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)*(d*x+c)^(11/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(11/6), x)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)*(d*x+c)^(11/6), x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{6}} (dx + c)^{\frac{11}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)*(d*x+c)^(11/6),x)

[Out] int((b*x+a)^(5/6)*(d*x+c)^(11/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{6}} (dx + c)^{\frac{11}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)*(d*x+c)^(11/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)*(d*x + c)^(11/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{\frac{5}{6}} (c + dx)^{\frac{11}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)*(c + d*x)^(11/6),x)

[Out] int((a + b*x)^(5/6)*(c + d*x)^(11/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)*(d*x+c)**(11/6),x)

[Out] Timed out

3.1787 $\int (a + bx)^{5/6} (c + dx)^{5/6} dx$

Optimal. Leaf size=74

$$\frac{6(a + bx)^{11/6} (c + dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

[Out] $6/11*(b*x+a)^{(11/6)}*(d*x+c)^{(5/6)}*\text{hypergeom}([-5/6, 11/6], [17/6], -d*(b*x+a)/(-a*d+b*c))/b/(b*(d*x+c)/(-a*d+b*c))^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a + bx)^{11/6} (c + dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(5/6)}*(c + d*x)^{(5/6)}, x]$

[Out] $(6*(a + b*x)^{(11/6)}*(c + d*x)^{(5/6)}*\text{Hypergeometric2F1}[-5/6, 11/6, 17/6, -((d*(a + b*x))/(b*c - a*d))])/((11*b*((b*(c + d*x))/(b*c - a*d))^{(5/6)})$

Rule 69

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& \text{GtQ}[b/(b*c - a*d), 0] \&\& (\text{RationalQ}[m] \parallel !(\text{RationalQ}[n] \&\& \text{GtQ}[-(d/(b*c - a*d)), 0]))$

Rule 70

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Dist}[(c + d*x)^{\text{FracPart}[n]}/((b/(b*c - a*d))^{\text{IntPart}[n]}*((b*(c + d*x))/(b*c - a*d))^{\text{FracPart}[n]}), \text{Int}[(a + b*x)^m*\text{Simp}[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x], x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& (\text{RationalQ}[m] \parallel !\text{SimplerQ}[n + 1, m + 1])$

Rubi steps

$$\int (a + bx)^{5/6} (c + dx)^{5/6} dx = \frac{(c + dx)^{5/6} \int (a + bx)^{5/6} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad} \right)^{5/6} dx}{\left(\frac{b(c+dx)}{bc-ad} \right)^{5/6}}$$

$$= \frac{6(a + bx)^{11/6} (c + dx)^{5/6} {}_2F_1 \left(-\frac{5}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad} \right)}{11b \left(\frac{b(c+dx)}{bc-ad} \right)^{5/6}}$$

Mathematica [A] time = 0.04, size = 73, normalized size = 0.99

$$\frac{6(a + bx)^{11/6} (c + dx)^{5/6} {}_2F_1 \left(-\frac{5}{6}, \frac{11}{6}; \frac{17}{6}; \frac{d(a+bx)}{ad-bc} \right)}{11b \left(\frac{b(c+dx)}{bc-ad} \right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)*(c + d*x)^(5/6), x]

[Out] (6*(a + b*x)^(11/6)*(c + d*x)^(5/6)*Hypergeometric2F1[-5/6, 11/6, 17/6, (d*(a + b*x))/(-(b*c) + a*d)])/(11*b*((b*(c + d*x))/(b*c - a*d))^(5/6))

fricas [F] time = 2.09, size = 0, normalized size = 0.00

$$\text{integral} \left((bx + a)^{\frac{5}{6}} (dx + c)^{\frac{5}{6}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)*(d*x+c)^(5/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6), x)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)*(d*x+c)^(5/6), x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{6}} (dx + c)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)*(d*x+c)^(5/6),x)

[Out] int((b*x+a)^(5/6)*(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{5}{6}} (dx + c)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)*(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)*(d*x + c)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{\frac{5}{6}} (c + dx)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)*(c + d*x)^(5/6),x)

[Out] int((a + b*x)^(5/6)*(c + d*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{5}{6}} (c + dx)^{\frac{5}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)*(d*x+c)**(5/6),x)

[Out] Integral((a + b*x)**(5/6)*(c + d*x)**(5/6), x)

$$3.1788 \quad \int \frac{(a+bx)^{5/6}}{\sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=74

$$\frac{6(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11b\sqrt[6]{c+dx}}$$

[Out] 6/11*(b*x+a)^(11/6)*(b*(d*x+c)/(-a*d+b*c))^(1/6)*hypergeom([1/6, 11/6], [17/6], -d*(b*x+a)/(-a*d+b*c))/b/(d*x+c)^(1/6)

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11b\sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/6)/(c + d*x)^(1/6), x]

[Out] (6*(a + b*x)^(11/6)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 11/6, 17/6, -((d*(a + b*x))/(b*c - a*d))]/(11*b*(c + d*x)^(1/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(a+bx)^{5/6}}{\sqrt[6]{c+dx}} dx = \frac{\sqrt[6]{\frac{b(c+dx)}{bc-ad}} \int \frac{(a+bx)^{5/6}}{\sqrt[6]{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}}} dx}{\sqrt[6]{c+dx}}$$

$$= \frac{6(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11b\sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.04, size = 73, normalized size = 0.99

$$\frac{6(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{11}{6}; \frac{17}{6}; \frac{d(a+bx)}{ad-bc}\right)}{11b\sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)/(c + d*x)^(1/6), x]

[Out] (6*(a + b*x)^(11/6)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 11/6, 17/6, (d*(a + b*x))/(-(b*c) + a*d)]/(11*b*(c + d*x)^(1/6))

fricas [F] time = 1.72, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{5}{6}}}{(dx+c)^{\frac{1}{6}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(1/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)/(d*x + c)^(1/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{6}}}{(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(1/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(1/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)/(d*x+c)^(1/6), x)

[Out] int((b*x+a)^(5/6)/(d*x+c)^(1/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(1/6), x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{5}{6}}}{(c + dx)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)/(c + d*x)^(1/6), x)

[Out] int((a + b*x)^(5/6)/(c + d*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{6}}}{\sqrt[6]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)/(d*x+c)**(1/6), x)

[Out] Integral((a + b*x)**(5/6)/(c + d*x)**(1/6), x)

$$3.1789 \quad \int \frac{(a+bx)^{5/6}}{(c+dx)^{7/6}} dx$$

Optimal. Leaf size=81

$$\frac{6(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{7}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11 \sqrt[6]{c+dx} (bc-ad)}$$

[Out] 6/11*(b*x+a)^(11/6)*(b*(d*x+c)/(-a*d+b*c))^(1/6)*hypergeom([7/6, 11/6], [17/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)/(d*x+c)^(1/6)

Rubi [A] time = 0.02, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{7}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11 \sqrt[6]{c+dx} (bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/6)/(c + d*x)^(7/6), x]

[Out] (6*(a + b*x)^(11/6)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[7/6, 11/6, 17/6, -((d*(a + b*x))/(b*c - a*d))]/(11*(b*c - a*d)*(c + d*x)^(1/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(a+bx)^{5/6}}{(c+dx)^{7/6}} dx = \frac{\left(b\sqrt[6]{\frac{b(c+dx)}{bc-ad}}\right) \int \frac{(a+bx)^{5/6}}{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{7/6}} dx}{(bc-ad)\sqrt[6]{c+dx}}$$

$$= \frac{6(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{7}{6}, \frac{11}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11(bc-ad)\sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.06, size = 73, normalized size = 0.90

$$\frac{6(a+bx)^{11/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{7/6} {}_2F_1\left(\frac{7}{6}, \frac{11}{6}; \frac{17}{6}; \frac{d(a+bx)}{ad-bc}\right)}{11b(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)/(c + d*x)^(7/6), x]

[Out] (6*(a + b*x)^(11/6)*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[7/6, 11/6, 17/6, (d*(a + b*x))/(-b*c + a*d)]/(11*b*(c + d*x)^(7/6))

fricas [F] time = 2.13, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{5/6}(dx+c)^{5/6}}{d^2x^2+2cdx+c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(7/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{5/6}}{(dx+c)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(7/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(7/6), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)/(d*x+c)^(7/6),x)

[Out] int((b*x+a)^(5/6)/(d*x+c)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(7/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(7/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{5}{6}}}{(c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)/(c + d*x)^(7/6),x)

[Out] int((a + b*x)^(5/6)/(c + d*x)^(7/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{6}}}{(c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)/(d*x+c)**(7/6),x)

[Out] Integral((a + b*x)**(5/6)/(c + d*x)**(7/6), x)

$$3.1790 \quad \int \frac{(a+bx)^{5/6}}{(c+dx)^{13/6}} dx$$

Optimal. Leaf size=82

$$\frac{6b(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{11}{6}, \frac{13}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11 \sqrt[6]{c+dx} (bc-ad)^2}$$

[Out] $6/11*b*(b*x+a)^{(11/6)}*(b*(d*x+c)/(-a*d+b*c))^{(1/6)}*hypergeom([11/6, 13/6], [17/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^2/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6b(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{11}{6}, \frac{13}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11 \sqrt[6]{c+dx} (bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/6)/(c + d*x)^(13/6), x]

[Out] $(6*b*(a + b*x)^{(11/6)}*((b*(c + d*x))/(b*c - a*d))^{(1/6)}*Hypergeometric2F1[11/6, 13/6, 17/6, -((d*(a + b*x))/(b*c - a*d))]/(11*(b*c - a*d)^2*(c + d*x)^{(1/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(a+bx)^{5/6}}{(c+dx)^{13/6}} dx = \frac{\left(b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}\right) \int \frac{(a+bx)^{5/6}}{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{13/6}} dx}{(bc-ad)^2 \sqrt[6]{c+dx}}$$

$$= \frac{6b(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{11}{6}, \frac{13}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11(bc-ad)^2 \sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.08, size = 73, normalized size = 0.89

$$\frac{6(a+bx)^{11/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{13/6} {}_2F_1\left(\frac{11}{6}, \frac{13}{6}; \frac{17}{6}; \frac{d(a+bx)}{ad-bc}\right)}{11b(c+dx)^{13/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)/(c + d*x)^(13/6), x]

[Out] (6*(a + b*x)^(11/6)*((b*(c + d*x))/(b*c - a*d))^(13/6)*Hypergeometric2F1[11/6, 13/6, 17/6, (d*(a + b*x))/(-(b*c) + a*d)]/(11*b*(c + d*x)^(13/6))

fricas [F] time = 1.79, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{5}{6}}}{d^3x^3+3cd^2x^2+3c^2dx+c^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(13/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{5}{6}}}{(dx+c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(13/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(13/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)/(d*x+c)^(13/6), x)

[Out] int((b*x+a)^(5/6)/(d*x+c)^(13/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(13/6), x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(13/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{5}{6}}}{(c + dx)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)/(c + d*x)^(13/6), x)

[Out] int((a + b*x)^(5/6)/(c + d*x)^(13/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{5}{6}}}{(c + dx)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)/(d*x+c)**(13/6), x)

[Out] Integral((a + b*x)**(5/6)/(c + d*x)**(13/6), x)

$$3.1791 \quad \int \frac{(a+bx)^{5/6}}{(c+dx)^{19/6}} dx$$

Optimal. Leaf size=84

$$\frac{6b^2(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{11}{6}, \frac{19}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11 \sqrt[6]{c+dx} (bc-ad)^3}$$

[Out] 6/11*b^2*(b*x+a)^(11/6)*(b*(d*x+c)/(-a*d+b*c))^(1/6)*hypergeom([11/6, 19/6], [17/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^3/(d*x+c)^(1/6)

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6b^2(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{11}{6}, \frac{19}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11 \sqrt[6]{c+dx} (bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(5/6)/(c + d*x)^(19/6), x]

[Out] (6*b^2*(a + b*x)^(11/6)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[11/6, 19/6, 17/6, -((d*(a + b*x))/(b*c - a*d))]/(11*(b*c - a*d)^3*(c + d*x)^(1/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(a+bx)^{5/6}}{(c+dx)^{19/6}} dx = \frac{\left(b^3 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}\right) \int \frac{(a+bx)^{5/6}}{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{19/6}} dx}{(bc-ad)^3 \sqrt[6]{c+dx}}$$

$$= \frac{6b^2(a+bx)^{11/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{11}{6}, \frac{19}{6}; \frac{17}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{11(bc-ad)^3 \sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.05, size = 81, normalized size = 0.96

$$\frac{6b(a+bx)^{11/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{7/6} {}_2F_1\left(\frac{11}{6}, \frac{19}{6}; \frac{17}{6}; \frac{d(a+bx)}{ad-bc}\right)}{11(c+dx)^{7/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(5/6)/(c + d*x)^(19/6), x]

[Out] (6*b*(a + b*x)^(11/6)*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[11/6, 19/6, 17/6, (d*(a + b*x))/(-(b*c) + a*d)]/(11*(b*c - a*d)^2*(c + d*x)^(7/6))

fricas [F] time = 1.81, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{5/6}(dx+c)^{5/6}}{d^4x^4+4cd^3x^3+6c^2d^2x^2+4c^3dx+c^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(19/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(d^4*x^4 + 4*c*d^3*x^3 + 6*c^2*d^2*x^2 + 4*c^3*d*x + c^4), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{5/6}}{(dx+c)^{19/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(19/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(19/6), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(5/6)/(d*x+c)^(19/6), x)

[Out] int((b*x+a)^(5/6)/(d*x+c)^(19/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{5}{6}}}{(dx + c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(5/6)/(d*x+c)^(19/6), x, algorithm="maxima")

[Out] integrate((b*x + a)^(5/6)/(d*x + c)^(19/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{5/6}}{(c + dx)^{19/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(5/6)/(c + d*x)^(19/6), x)

[Out] int((a + b*x)^(5/6)/(c + d*x)^(19/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(5/6)/(d*x+c)**(19/6), x)

[Out] Timed out

3.1792 $\int (a + bx)^{7/6} (c + dx)^{13/6} dx$

Optimal. Leaf size=84

$$\frac{6(a + bx)^{13/6} \sqrt[6]{c + dx} (bc - ad)^2 {}_2F_1\left(-\frac{13}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b^3 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

[Out] 6/13*(-a*d+b*c)^2*(b*x+a)^(13/6)*(d*x+c)^(1/6)*hypergeom([-13/6, 13/6], [19/6], -d*(b*x+a)/(-a*d+b*c))/b^3/(b*(d*x+c)/(-a*d+b*c))^(1/6)

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a + bx)^{13/6} \sqrt[6]{c + dx} (bc - ad)^2 {}_2F_1\left(-\frac{13}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b^3 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)*(c + d*x)^(13/6), x]

[Out] (6*(b*c - a*d)^2*(a + b*x)^(13/6)*(c + d*x)^(1/6)*Hypergeometric2F1[-13/6, 13/6, 19/6, -((d*(a + b*x))/(b*c - a*d))]/(13*b^3*((b*(c + d*x))/(b*c - a*d))^(1/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int (a + bx)^{7/6} (c + dx)^{13/6} dx = \frac{((bc - ad)^2 \sqrt[6]{c + dx}) \int (a + bx)^{7/6} \left(\frac{bc}{bc - ad} + \frac{bdx}{bc - ad} \right)^{13/6} dx}{b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

$$= \frac{6(bc - ad)^2 (a + bx)^{13/6} \sqrt[6]{c + dx} {}_2F_1 \left(-\frac{13}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad} \right)}{13b^3 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Mathematica [A] time = 0.11, size = 73, normalized size = 0.87

$$\frac{6(a + bx)^{13/6} (c + dx)^{13/6} {}_2F_1 \left(-\frac{13}{6}, \frac{13}{6}; \frac{19}{6}; \frac{d(a+bx)}{ad-bc} \right)}{13b \left(\frac{b(c+dx)}{bc-ad} \right)^{13/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)*(c + d*x)^(13/6), x]

[Out] (6*(a + b*x)^(13/6)*(c + d*x)^(13/6)*Hypergeometric2F1[-13/6, 13/6, 19/6, (d*(a + b*x))/(-b*c) + a*d])/(13*b*((b*(c + d*x))/(b*c - a*d))^(13/6))

fricas [F] time = 1.08, size = 0, normalized size = 0.00

$$\text{integral} \left((bd^2x^3 + ac^2 + (2bcd + ad^2)x^2 + (bc^2 + 2acd)x)(bx + a)^{\frac{1}{6}}(dx + c)^{\frac{1}{6}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)*(d*x+c)^(13/6), x, algorithm="fricas")

[Out] integral((b*d^2*x^3 + a*c^2 + (2*b*c*d + a*d^2)*x^2 + (b*c^2 + 2*a*c*d)*x)*(b*x + a)^(1/6)*(d*x + c)^(1/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{7}{6}}(dx + c)^{\frac{13}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)*(d*x+c)^(13/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)*(d*x + c)^(13/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{7}{6}} (dx + c)^{\frac{13}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)*(d*x+c)^(13/6),x)

[Out] int((b*x+a)^(7/6)*(d*x+c)^(13/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{7}{6}} (dx + c)^{\frac{13}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)*(d*x+c)^(13/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)*(d*x + c)^(13/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{\frac{7}{6}} (c + dx)^{\frac{13}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)*(c + d*x)^(13/6),x)

[Out] int((a + b*x)^(7/6)*(c + d*x)^(13/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)*(d*x+c)**(13/6),x)

[Out] Timed out

3.1793 $\int (a + bx)^{7/6} (c + dx)^{7/6} dx$

Optimal. Leaf size=82

$$\frac{6(a + bx)^{13/6} \sqrt[6]{c + dx} (bc - ad) {}_2F_1\left(-\frac{7}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

[Out] $6/13*(-a*d+b*c)*(b*x+a)^{(13/6)*(d*x+c)^{(1/6)*\text{hypergeom}([-7/6, 13/6], [19/6], -d*(b*x+a)/(-a*d+b*c))}/b^2/(b*(d*x+c)/(-a*d+b*c))^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a + bx)^{13/6} \sqrt[6]{c + dx} (bc - ad) {}_2F_1\left(-\frac{7}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(7/6)*(c + d*x)^{(7/6)}, x]$

[Out] $(6*(b*c - a*d)*(a + b*x)^{(13/6)*(c + d*x)^{(1/6)*\text{Hypergeometric2F1}[-7/6, 13/6, 19/6, -((d*(a + b*x))/(b*c - a*d))])/(13*b^2*((b*(c + d*x))/(b*c - a*d))^{(1/6)})$

Rule 69

$\text{Int}[(a + b*x)^{(m+1)*\text{Hypergeometric2F1}[-n, m+1, m+2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m+1)*(b/(b*c - a*d))^n), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

$\text{Int}[(a + b*x)^m * \text{FracPart}[n] / ((b/(b*c - a*d))^{\text{IntPart}[n]} * ((b*(c + d*x))/(b*c - a*d))^{\text{FracPart}[n]}), \text{Int}[(a + b*x)^m * \text{Simp}[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d)], x]^n, x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int (a + bx)^{7/6} (c + dx)^{7/6} dx = \frac{((bc - ad)\sqrt[6]{c + dx}) \int (a + bx)^{7/6} \left(\frac{bc}{bc - ad} + \frac{bdx}{bc - ad}\right)^{7/6} dx}{b\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

$$= \frac{6(bc - ad)(a + bx)^{13/6} \sqrt[6]{c + dx} {}_2F_1\left(-\frac{7}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Mathematica [A] time = 0.07, size = 73, normalized size = 0.89

$$\frac{6(a + bx)^{13/6} (c + dx)^{7/6} {}_2F_1\left(-\frac{7}{6}, \frac{13}{6}; \frac{19}{6}; \frac{d(a+bx)}{ad-bc}\right)}{13b \left(\frac{b(c+dx)}{bc-ad}\right)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)*(c + d*x)^(7/6), x]

[Out] (6*(a + b*x)^(13/6)*(c + d*x)^(7/6)*Hypergeometric2F1[-7/6, 13/6, 19/6, (d*(a + b*x))/(-(b*c) + a*d)]/(13*b*((b*(c + d*x))/(b*c - a*d))^(7/6))

fricas [F] time = 1.03, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bdx^2 + ac + (bc + ad)x\right)(bx + a)^{\frac{1}{6}}(dx + c)^{\frac{1}{6}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)*(d*x+c)^(7/6), x, algorithm="fricas")

[Out] integral((b*d*x^2 + a*c + (b*c + a*d)*x)*(b*x + a)^(1/6)*(d*x + c)^(1/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{7}{6}} (dx + c)^{\frac{7}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)*(d*x+c)^(7/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)*(d*x + c)^(7/6), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{7}{6}} (dx + c)^{\frac{7}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)*(d*x+c)^(7/6),x)

[Out] int((b*x+a)^(7/6)*(d*x+c)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{7}{6}} (dx + c)^{\frac{7}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)*(d*x+c)^(7/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)*(d*x + c)^(7/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{\frac{7}{6}} (c + dx)^{\frac{7}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)*(c + d*x)^(7/6),x)

[Out] int((a + b*x)^(7/6)*(c + d*x)^(7/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)*(d*x+c)**(7/6),x)

[Out] Timed out

3.1794 $\int (a + bx)^{7/6} \sqrt[6]{c + dx} dx$

Optimal. Leaf size=74

$$\frac{6(a + bx)^{13/6} \sqrt[6]{c + dx} {}_2F_1\left(-\frac{1}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

[Out] $6/13*(b*x+a)^{(13/6)}*(d*x+c)^{(1/6)}*\text{hypergeom}([-1/6, 13/6], [19/6], -d*(b*x+a)/(-a*d+b*c))/b/(b*(d*x+c)/(-a*d+b*c))^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a + bx)^{13/6} \sqrt[6]{c + dx} {}_2F_1\left(-\frac{1}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(7/6)}*(c + d*x)^{(1/6)}, x]$

[Out] $(6*(a + b*x)^{(13/6)}*(c + d*x)^{(1/6)}*\text{Hypergeometric2F1}[-1/6, 13/6, 19/6, -(d*(a + b*x))/(b*c - a*d)])/(13*b*((b*(c + d*x))/(b*c - a*d))^{(1/6)})$

Rule 69

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(c + b*x)^{(m + 1)}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -(d*(a + b*x))/(b*c - a*d)]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Dist}[(c + d*x)^{\text{FracPart}[n]}/((b/(b*c - a*d))^{\text{IntPart}[n]}*((b*(c + d*x))/(b*c - a*d))^{\text{FracPart}[n]}), \text{Int}[(a + b*x)^m*\text{Simp}[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x], x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int (a + bx)^{7/6} \sqrt[6]{c + dx} \, dx = \frac{\sqrt[6]{c + dx} \int (a + bx)^{7/6} \sqrt[6]{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}} \, dx}{\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

$$= \frac{6(a + bx)^{13/6} \sqrt[6]{c + dx} {}_2F_1\left(-\frac{1}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Mathematica [A] time = 0.04, size = 73, normalized size = 0.99

$$\frac{6(a + bx)^{13/6} \sqrt[6]{c + dx} {}_2F_1\left(-\frac{1}{6}, \frac{13}{6}; \frac{19}{6}; \frac{d(a+bx)}{ad-bc}\right)}{13b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)*(c + d*x)^(1/6), x]

[Out] (6*(a + b*x)^(13/6)*(c + d*x)^(1/6)*Hypergeometric2F1[-1/6, 13/6, 19/6, (d*(a + b*x))/(-(b*c) + a*d)])/(13*b*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [F] time = 0.77, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(bx + a\right)^{\frac{7}{6}}\left(dx + c\right)^{\frac{1}{6}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)*(d*x+c)^(1/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(7/6)*(d*x + c)^(1/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{7}{6}}(dx + c)^{\frac{1}{6}} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)*(d*x+c)^(1/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)*(d*x + c)^(1/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{7}{6}} (dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)*(d*x+c)^(1/6),x)

[Out] int((b*x+a)^(7/6)*(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{\frac{7}{6}} (dx + c)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)*(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)*(d*x + c)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{\frac{7}{6}} (c + dx)^{\frac{1}{6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)*(c + d*x)^(1/6),x)

[Out] int((a + b*x)^(7/6)*(c + d*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + bx)^{\frac{7}{6}} \sqrt[6]{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)*(d*x+c)**(1/6),x)

[Out] Integral((a + b*x)**(7/6)*(c + d*x)**(1/6), x)

$$3.1795 \quad \int \frac{(a+bx)^{7/6}}{(c+dx)^{5/6}} dx$$

Optimal. Leaf size=74

$$\frac{6(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{5}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b(c+dx)^{5/6}}$$

[Out] 6/13*(b*x+a)^(13/6)*(b*(d*x+c)/(-a*d+b*c))^(5/6)*hypergeom([5/6, 13/6], [19/6], -d*(b*x+a)/(-a*d+b*c))/b/(d*x+c)^(5/6)

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{5}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)/(c + d*x)^(5/6), x]

[Out] (6*(a + b*x)^(13/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[5/6, 13/6, 19/6, -((d*(a + b*x))/(b*c - a*d))]/(13*b*(c + d*x)^(5/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(a+bx)^{7/6}}{(c+dx)^{5/6}} dx = \frac{\left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} \int \frac{(a+bx)^{7/6}}{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{5/6}} dx}{(c+dx)^{5/6}}$$

$$= \frac{6(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{5}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13b(c+dx)^{5/6}}$$

Mathematica [A] time = 0.04, size = 73, normalized size = 0.99

$$\frac{6(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{5}{6}, \frac{13}{6}; \frac{19}{6}; \frac{d(a+bx)}{ad-bc}\right)}{13b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)/(c + d*x)^(5/6), x]

[Out] (6*(a + b*x)^(13/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[5/6, 13/6, 19/6, (d*(a + b*x))/(-(b*c) + a*d)]/(13*b*(c + d*x)^(5/6))

fricas [F] time = 0.91, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{7}{6}}}{(dx+c)^{\frac{5}{6}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(5/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(7/6)/(d*x + c)^(5/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{7}{6}}}{(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(5/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(5/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)/(d*x+c)^(5/6), x)

[Out] int((b*x+a)^(7/6)/(d*x+c)^(5/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(5/6), x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{7}{6}}}{(c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)/(c + d*x)^(5/6), x)

[Out] int((a + b*x)^(7/6)/(c + d*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{7}{6}}}{(c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)/(d*x+c)**(5/6), x)

[Out] Integral((a + b*x)**(7/6)/(c + d*x)**(5/6), x)

$$3.1796 \quad \int \frac{(a+bx)^{7/6}}{(c+dx)^{11/6}} dx$$

Optimal. Leaf size=81

$$\frac{6(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{11}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13(c+dx)^{5/6}(bc-ad)}$$

[Out] 6/13*(b*x+a)^(13/6)*(b*(d*x+c)/(-a*d+b*c))^(5/6)*hypergeom([11/6, 13/6], [19/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)/(d*x+c)^(5/6)

Rubi [A] time = 0.02, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{11}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13(c+dx)^{5/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)/(c + d*x)^(11/6), x]

[Out] (6*(a + b*x)^(13/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[11/6, 13/6, 19/6, -((d*(a + b*x))/(b*c - a*d))]/(13*(b*c - a*d)*(c + d*x)^(5/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(a+bx)^{7/6}}{(c+dx)^{11/6}} dx = \frac{\left(b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}\right) \int \frac{(a+bx)^{7/6}}{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{11/6}} dx}{(bc-ad)(c+dx)^{5/6}}$$

$$= \frac{6(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{11}{6}, \frac{13}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13(bc-ad)(c+dx)^{5/6}}$$

Mathematica [A] time = 0.07, size = 73, normalized size = 0.90

$$\frac{6(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{11/6} {}_2F_1\left(\frac{11}{6}, \frac{13}{6}; \frac{19}{6}; \frac{d(a+bx)}{ad-bc}\right)}{13b(c+dx)^{11/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)/(c + d*x)^(11/6), x]

[Out] (6*(a + b*x)^(13/6)*((b*(c + d*x))/(b*c - a*d))^(11/6)*Hypergeometric2F1[11/6, 13/6, 19/6, (d*(a + b*x))/(-(b*c) + a*d)]/(13*b*(c + d*x)^(11/6))

fricas [F] time = 1.01, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{7/6}(dx+c)^{1/6}}{d^2x^2+2cdx+c^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(11/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(7/6)*(d*x + c)^(1/6)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{7/6}}{(dx+c)^{11/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(11/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(11/6), x)

maple [F] time = 0.16, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)/(d*x+c)^(11/6),x)

[Out] int((b*x+a)^(7/6)/(d*x+c)^(11/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(11/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(11/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{\frac{7}{6}}}{(c + dx)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)/(c + d*x)^(11/6),x)

[Out] int((a + b*x)^(7/6)/(c + d*x)^(11/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{7}{6}}}{(c + dx)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)/(d*x+c)**(11/6),x)

[Out] Integral((a + b*x)**(7/6)/(c + d*x)**(11/6), x)

$$3.1797 \quad \int \frac{(a+bx)^{7/6}}{(c+dx)^{17/6}} dx$$

Optimal. Leaf size=82

$$\frac{6b(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{13}{6}, \frac{17}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13(c+dx)^{5/6}(bc-ad)^2}$$

[Out] 6/13*b*(b*x+a)^(13/6)*(b*(d*x+c)/(-a*d+b*c))^(5/6)*hypergeom([13/6, 17/6], [19/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^2/(d*x+c)^(5/6)

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6b(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{13}{6}, \frac{17}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13(c+dx)^{5/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)/(c + d*x)^(17/6), x]

[Out] (6*b*(a + b*x)^(13/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[13/6, 17/6, 19/6, -((d*(a + b*x))/(b*c - a*d))]/(13*(b*c - a*d)^2*(c + d*x)^(5/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(a+bx)^{7/6}}{(c+dx)^{17/6}} dx = \frac{\left(b^2 \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}\right) \int \frac{(a+bx)^{7/6}}{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{17/6}} dx}{(bc-ad)^2 (c+dx)^{5/6}}$$

$$= \frac{6b(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{13}{6}, \frac{17}{6}; \frac{19}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{13(bc-ad)^2 (c+dx)^{5/6}}$$

Mathematica [A] time = 0.05, size = 81, normalized size = 0.99

$$\frac{6b(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{13}{6}, \frac{17}{6}; \frac{19}{6}; \frac{d(a+bx)}{ad-bc}\right)}{13(c+dx)^{5/6} (bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)/(c + d*x)^(17/6), x]

[Out] (6*b*(a + b*x)^(13/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[13/6, 17/6, 19/6, (d*(a + b*x))/(-(b*c) + a*d)]/(13*(b*c - a*d)^2*(c + d*x)^(5/6))

fricas [F] time = 0.83, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{7}{6}}(dx+c)^{\frac{1}{6}}}{d^3x^3+3cd^2x^2+3c^2dx+c^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(17/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(7/6)*(d*x + c)^(1/6)/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{7}{6}}}{(dx+c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(17/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(17/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)/(d*x+c)^(17/6), x)

[Out] int((b*x+a)^(7/6)/(d*x+c)^(17/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(17/6), x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(17/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{7/6}}{(c + dx)^{17/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)/(c + d*x)^(17/6), x)

[Out] int((a + b*x)^(7/6)/(c + d*x)^(17/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)/(d*x+c)**(17/6), x)

[Out] Timed out

$$3.1798 \quad \int \frac{(a+bx)^{7/6}}{\sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=424

$$\frac{7(bc-ad)^2 \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{5/6}d^{13/6}} + \frac{7(bc-ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{5/6}d^{13/6}} - \frac{7(bc-ad)}{144b^{5/6}d^{13/6}}$$

[Out] $-7/12*(-a*d+b*c)*(b*x+a)^{(1/6)}*(d*x+c)^{(5/6)}/d^{2+1/2}*(b*x+a)^{(7/6)}*(d*x+c)^{(5/6)}/d^{7/36}*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(5/6)}/d^{(13/6)}-7/144*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(5/6)}/d^{(13/6)}+7/144*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(5/6)}/d^{(13/6)}+7/72*(-a*d+b*c)^2*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(5/6)}/d^{(13/6)}*3^{(1/2)}+7/72*(-a*d+b*c)^2*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(5/6)}/d^{(13/6)}*3^{(1/2)}$

Rubi [A] time = 0.55, antiderivative size = 424, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {50, 63, 240, 210, 634, 618, 204, 628, 208}

$$\frac{7(bc-ad)^2 \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{5/6}d^{13/6}} + \frac{7(bc-ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{5/6}d^{13/6}} - \frac{7(bc-ad)}{144b^{5/6}d^{13/6}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)/(c + d*x)^(1/6), x]

[Out] $(-7*(b*c - a*d)*(a + b*x)^{(1/6)}*(c + d*x)^{(5/6)})/(12*d^2) + ((a + b*x)^{(7/6)}*(c + d*x)^{(5/6)})/(2*d) - (7*(b*c - a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(5/6)}*d^{(13/6)}) + (7*(b*c - a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(5/6)}*d^{(13/6)}) + (7*(b*c - a*d)^2*\operatorname{ArcTanh}[d^{(1/6)}*(a + b*x)^{(1/6)}/(b^{(1/6)}*(c + d*x)^{(1/6)})]/(36*b^{(5/6)}*d^{(13/6)}) - (7*(b*c - a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})]/(144*b^{(5/6)}*d^{(13/6)}) + (7*(b*c - a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})]/(144*b^{(5/6)}*d^{(13/6)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rule 210

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Module[{r = Numerator[Rt[-(
a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r - s*Cos[(
2*k*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r + s*Co
s[(2*k*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^2*Int[
1/(r^2 - s^2*x^2), x])/(a*n) + Dist[(2*r)/(a*n), Sum[u, {k, 1, (n - 2)/4}],
x], x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && NegQ[a/b]
```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int
[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a,
b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/
n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_.) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), Int[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/6}}{\sqrt[6]{c+dx}} dx &= \frac{(a+bx)^{7/6}(c+dx)^{5/6}}{2d} - \frac{(7(bc-ad)) \int \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} dx}{12d} \\
&= -\frac{7(bc-ad)\sqrt[6]{a+bx}(c+dx)^{5/6}}{12d^2} + \frac{(a+bx)^{7/6}(c+dx)^{5/6}}{2d} + \frac{(7(bc-ad)^2) \int \frac{1}{(a+bx)^{5/6}\sqrt[6]{c+dx}} dx}{72d^2} \\
&= -\frac{7(bc-ad)\sqrt[6]{a+bx}(c+dx)^{5/6}}{12d^2} + \frac{(a+bx)^{7/6}(c+dx)^{5/6}}{2d} + \frac{(7(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt[6]{c-\frac{ad}{b}+\frac{dx^6}{b}}} dx \right)}{12bd^2} \\
&= -\frac{7(bc-ad)\sqrt[6]{a+bx}(c+dx)^{5/6}}{12d^2} + \frac{(a+bx)^{7/6}(c+dx)^{5/6}}{2d} + \frac{(7(bc-ad)^2) \text{Subst} \left(\int \frac{1}{1-\frac{dx^6}{b}} dx \right)}{12bd^2} \\
&= -\frac{7(bc-ad)\sqrt[6]{a+bx}(c+dx)^{5/6}}{12d^2} + \frac{(a+bx)^{7/6}(c+dx)^{5/6}}{2d} + \frac{(7(bc-ad)^2) \text{Subst} \left(\int \frac{\sqrt[6]{b}-\sqrt[6]{d}}{\sqrt[3]{b}-\sqrt[6]{b}\sqrt[6]{d}} dx \right)}{36b^{5/6}d^2} \\
&= -\frac{7(bc-ad)\sqrt[6]{a+bx}(c+dx)^{5/6}}{12d^2} + \frac{(a+bx)^{7/6}(c+dx)^{5/6}}{2d} + \frac{7(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} \right)}{36b^{5/6}d^{13/6}} \\
&= -\frac{7(bc-ad)\sqrt[6]{a+bx}(c+dx)^{5/6}}{12d^2} + \frac{(a+bx)^{7/6}(c+dx)^{5/6}}{2d} + \frac{7(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} \right)}{36b^{5/6}d^{13/6}} \\
&= -\frac{7(bc-ad)\sqrt[6]{a+bx}(c+dx)^{5/6}}{12d^2} + \frac{(a+bx)^{7/6}(c+dx)^{5/6}}{2d} - \frac{7(bc-ad)^2 \tan^{-1} \left(\frac{1-2\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} \right)}{24\sqrt{3}b^{5/6}d^{13/6}} +
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.17

$$\frac{6(a+bx)^{13/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(\frac{1}{6}, \frac{13}{6}; \frac{19}{6}; \frac{d(a+bx)}{ad-bc} \right)}{13b\sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)/(c + d*x)^(1/6), x]

[Out] (6*(a + b*x)^(13/6)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 13/6, 19/6, (d*(a + b*x))/(-(b*c) + a*d)]/(13*b*(c + d*x)^(1/6))

fricas [B] time = 1.14, size = 5633, normalized size = 13.29

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(1/6),x, algorithm="fricas")

[Out]
$$\begin{aligned} & -1/144*(28*\sqrt{3}*d^2*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^5*d^{13}))^{(1/6)} \\ & * \arctan(-1/3*(2*\sqrt{3}*(b^6*c^2*d^{11} - 2*a*b^5*c*d^{12} + a^2*b^4*d^{13})*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^5*d^{13}))^{(1/6)} \\ & - 2*\sqrt{3}*(b^4*d^{12}*x + b^4*c*d^{11})*\sqrt{((b^3*c^2*d^2 - 2*a*b^2*c*d^3 + a^2*b*d^4)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^5*d^{13}))^{(1/6)} \\ & + (b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)} + (b^2*d^5*x + b^2*c*d^4)*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^5*d^{13}))^{(1/3)}) \\ & / (d*x + c))*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^5*d^{13}))^{(5/6)} \\ & + \sqrt{3}*(b^{12}*c^{13} - 12*a*b^{11}*c^{12}*d + 66*a^2*b^{10}*c^{11}*d^2 - 220*a^3*b^9*c^{10}*d^3 + 495*a^4*b^8*c^9*d^4 - 792*a^5*b^7*c^8*d^5 + 924*a^6*b^6*c^7*d^6 - 792*a^7*b^5*c^6*d^7 + 495*a^8*b^4*c^5*d^8 - 220*a^9*b^3*c^4*d^9 + 66*a^{10}*b^2*c^3*d^{10} - 12*a^{11}*b*c^2*d^{11} + a^{12}*c*d^{12} + (b^{12}*c^{12}*d - 12*a*b^{11}*c^{11}*d^2 + 66*a^2*b^{10}*c^{10}*d^3 - 220*a^3*b^9*c^9*d^4 + 495*a^4*b^8*c^8*d^5 - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - 792*a^7*b^5*c^5*d^8 + 495*a^8*b^4*c^4*d^9 - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b^2*c^2*d^{11} - 12*a^{11}*b*c*d^{12} + a^{12}*d^{13})*x) \\ &)/(b^{12}*c^{13} - 12*a*b^{11}*c^{12}*d + 66*a^2*b^{10}*c^{11}*d^2 - 220*a^3*b^9*c^{10}*d^3 + 495*a^4*b^8*c^9*d^4 - 792*a^5*b^7*c^8*d^5 + 924*a^6*b^6*c^7*d^6 - 792*a^7*b^5*c^6*d^7 + 495*a^8*b^4*c^5*d^8 - 220*a^9*b^3*c^4*d^9 + 66*a^{10}*b^2*c^3*d^{10} - 12*a^{11}*b*c^2*d^{11} + a^{12}*c*d^{12} + (b^{12}*c^{12}*d - 12*a*b^{11}*c^{11}*d^2 + 66*a^2*b^{10}*c^{10}*d^3 - 220*a^3*b^9*c^9*d^4 + 495*a^4*b^8*c^8*d^5 - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - 792*a^7*b^5*c^5*d^8 \end{aligned}$$

$$\begin{aligned}
& + 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66a^{10}b^2c^2d^{11} - 12a^{11}b^1c^1d^{12} + a^{12}d^{13})x) + 28\sqrt{3}d^2((b^{12}c^{12} - 12a^1b^{11}c^{11} \\
& *d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - 792 \\
& *a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 + 495a^8b^4c^4 \\
& *d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a \\
& ^{12}d^{12})/(b^5d^{13})^{(1/6)}\arctan(-1/3*(2\sqrt{3}*(b^6c^2d^{11} - 2a^1b^5 \\
& *c^1d^{12} + a^2b^4d^{13})*(bx + a)^{(1/6)}*(dx + c)^{(5/6)}*((b^{12}c^{12} - 12a^1b \\
& ^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - 792 \\
& *a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 + 495 \\
& *a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1 \\
& *d^{11} + a^{12}d^{12})/(b^5d^{13})^{(5/6)} - 2\sqrt{3}*(b^4d^{12}x + b^4c^1d^{11}) * \\
& \sqrt{-(b^3c^2d^2 - 2a^1b^2c^1d^3 + a^2b^1d^4)*(bx + a)^{(1/6)}*(dx + c)^{(\\
& 5/6)}*((b^{12}c^{12} - 12a^1b^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9 \\
& *d^3 + 495a^4b^8c^8d^4 - 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - 7 \\
& 92a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2 \\
& *c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12}d^{12})/(b^5d^{13})^{(1/6)} - (b^4c^4 - 4 \\
& *a^1b^3c^3d + 6a^2b^2c^2d^2 - 4a^3b^1c^1d^3 + a^4d^4)*(bx + a)^{(1/3)} \\
& *(dx + c)^{(2/3)} - (b^2d^5x + b^2c^1d^4)*((b^{12}c^{12} - 12a^1b^{11}c^{11}d + \\
& 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - 792a^5 \\
& *b^7c^7d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 + 495a^8b^4c^4 \\
& *d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12} \\
& *d^{12})/(b^5d^{13})^{(1/3)})/(dx + c)*((b^{12}c^{12} - 12a^1b^{11}c^{11}d + 66a^2 \\
& *b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - 792a^5b^7c^7 \\
& *d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - 2 \\
& 20a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12}d^{12})/(\\
& b^5d^{13})^{(5/6)} - \sqrt{3}*(b^{12}c^{13} - 12a^1b^{11}c^{12}d + 66a^2b^{10}c^{11} \\
& *d^2 - 220a^3b^9c^{10}d^3 + 495a^4b^8c^9d^4 - 792a^5b^7c^8d^5 + 9 \\
& 24a^6b^6c^7d^6 - 792a^7b^5c^6d^7 + 495a^8b^4c^5d^8 - 220a^9b^3 \\
& *c^4d^9 + 66a^{10}b^2c^3d^{10} - 12a^{11}b^1c^2d^{11} + a^{12}c^1d^{12} + (b^{12} \\
& *c^{12}d - 12a^1b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 + \\
& 495a^4b^8c^8d^5 - 792a^5b^7c^7d^6 + 924a^6b^6c^6d^7 - 792a^7b^5 \\
& *c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66a^{10}b^2c^2 \\
& *d^{11} - 12a^{11}b^1c^1d^{12} + a^{12}d^{13})x))/((b^{12}c^{13} - 12a^1b^{11}c^{12}d + 66 \\
& *a^2b^{10}c^{11}d^2 - 220a^3b^9c^{10}d^3 + 495a^4b^8c^9d^4 - 792a^5b^7 \\
& *c^8d^5 + 924a^6b^6c^7d^6 - 792a^7b^5c^6d^7 + 495a^8b^4c^5d^8 - 220a^9b^3 \\
& *c^4d^9 + 66a^{10}b^2c^3d^{10} - 12a^{11}b^1c^2d^{11} + a^{12}c^1d^{12} + (b^{12} \\
& *c^{12}d - 12a^1b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 + \\
& 495a^4b^8c^8d^5 - 792a^5b^7c^7d^6 + 924a^6b^6c^6d^7 - 792a^7b^5 \\
& *c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66 \\
& *a^{10}b^2c^2d^{11} - 12a^{11}b^1c^1d^{12} + a^{12}d^{13})x) - 7d^2*((b^{12}c^{12} \\
& - 12a^1b^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8 \\
& *c^8d^4 - 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 \\
& + 495a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1 \\
& *d^{11} + a^{12}d^{12})/(b^5d^{13})^{(1/6)}*\log(49*((b^3c^2d^2 - 2a^1b^2 \\
& *c^1d^3 + a^2b^1d^4)*(bx + a)^{(1/6)}*(dx + c)^{(5/6)}*((b^{12}c^{12} - 12a^1b^{11}
\end{aligned}$$

$$\begin{aligned}
& c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - \\
& 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - \\
& 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12}d^{12}) / (b^5d^{13})^{(1/6)} + (b^4c^4 - 4a^3b^3c^3d + 6a^2b^2c^2d^2 - \\
& 4a^3b^3c^3d + a^4d^4) * (b^2d^5x + b^2c^4d^4) * ((b^{12}c^{12} - 12a^3b^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + \\
& 495a^4b^8c^8d^4 - 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - \\
& 12a^{11}b^1c^1d^{11} + a^{12}d^{12}) / (b^5d^{13})^{(1/3)}) / (dx + c) + 7d^2 * ((b^{12}c^{12} - 12a^3b^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + \\
& 495a^4b^8c^8d^4 - 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - \\
& 12a^{11}b^1c^1d^{11} + a^{12}d^{12}) / (b^5d^{13})^{(1/6)} * \log(-49 * ((b^3c^2d^2 - 2a^2b^2c^2d^3 + a^2b^4d^4) * (b^2d^5x + b^2c^4d^4) * ((b^{12}c^{12} - 12a^3b^{11}c^{11}d + \\
& 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - \\
& 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12}d^{12}) / (b^5d^{13})^{(1/6)} - (b^4c^4 - 4a^3b^3c^3d + 6a^2b^2c^2d^2 - \\
& 4a^3b^3c^3d + a^4d^4) * (b^2d^5x + b^2c^4d^4) * ((b^{12}c^{12} - 12a^3b^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - \\
& 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12}d^{12}) / (b^5d^{13})^{(1/3)}) / (dx + c) - \\
& 14d^2 * ((b^{12}c^{12} - 12a^3b^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - \\
& 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12}d^{12}) / (b^5d^{13})^{(1/6)} * \log(7 * ((b^2c^2 - 2a^2b^2c^2d + a^2d^2) * (b^2d^5x + \\
& b^2c^4d^4) * ((b^{12}c^{12} - 12a^3b^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - \\
& 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12}d^{12}) / (b^5d^{13})^{(1/6)}) / (dx + c) + \\
& 14d^2 * ((b^{12}c^{12} - 12a^3b^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - \\
& 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12}d^{12}) / (b^5d^{13})^{(1/6)} * \log(7 * ((b^2c^2 - 2a^2b^2c^2d + a^2d^2) * (b^2d^5x + \\
& b^2c^4d^4) * ((b^{12}c^{12} - 12a^3b^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - \\
& 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12}d^{12}) / (b^5d^{13})^{(1/6)}) / (dx + c) - \\
& 12 * (6b^6d^6x - 7b^6c^6 + 13a^6d^6) * (b^2d^5x + b^2c^4d^4) * ((b^{12}c^{12} - 12a^3b^{11}c^{11}d + 66a^2b^{10}c^{10}d^2 - 220a^3b^9c^9d^3 + 495a^4b^8c^8d^4 - \\
& 792a^5b^7c^7d^5 + 924a^6b^6c^6d^6 - 792a^7b^5c^5d^7 + 495a^8b^4c^4d^8 - 220a^9b^3c^3d^9 + 66a^{10}b^2c^2d^{10} - 12a^{11}b^1c^1d^{11} + a^{12}d^{12}) / (b^5d^{13})^{(1/6)} * (dx + c)^{(5/6)} / d^2
\end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(1/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(1/6), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)/(d*x+c)^(1/6),x)

[Out] int((b*x+a)^(7/6)/(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{7/6}}{(c + dx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)/(c + d*x)^(1/6),x)

[Out] int((a + b*x)^(7/6)/(c + d*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{7}{6}}}{\sqrt[6]{c + dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)/(d*x+c)**(1/6),x)

[Out] Integral((a + b*x)**(7/6)/(c + d*x)**(1/6), x)

$$3.1799 \quad \int \frac{(a+bx)^{7/6}}{(c+dx)^{7/6}} dx$$

Optimal. Leaf size=403

$$\frac{7\sqrt[6]{b}(bc-ad)\log\left(-\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}+\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}}+\sqrt[3]{b}\right)}{12d^{13/6}}-\frac{7\sqrt[6]{b}(bc-ad)\log\left(\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}+\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}}+\sqrt[3]{b}\right)}{12d^{13/6}}+\frac{7\sqrt[6]{b}}{d^2}$$

[Out] $-6*(b*x+a)^{(7/6)}/d/(d*x+c)^{(1/6)}+7*b*(b*x+a)^{(1/6)}*(d*x+c)^{(5/6)}/d^2-7/3*b^{(1/6)}*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/d^{(13/6)}+7/12*b^{(1/6)}*(-a*d+b*c)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/d^{(13/6)}-7/12*b^{(1/6)}*(-a*d+b*c)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/d^{(13/6)}-7/6*b^{(1/6)}*(-a*d+b*c)*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/d^{(13/6)}*3^{(1/2)}-7/6*b^{(1/6)}*(-a*d+b*c)*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/d^{(13/6)}*3^{(1/2)}$

Rubi [A] time = 0.53, antiderivative size = 403, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 10, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.526$, Rules used = {47, 50, 63, 240, 210, 634, 618, 204, 628, 208}

$$\frac{7b\sqrt[6]{a+bx}(c+dx)^{5/6}}{d^2}+\frac{7\sqrt[6]{b}(bc-ad)\log\left(-\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}+\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}}+\sqrt[3]{b}\right)}{12d^{13/6}}-\frac{7\sqrt[6]{b}(bc-ad)\log\left(\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}+\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}}+\sqrt[3]{b}\right)}{12d^{13/6}}+\frac{7\sqrt[6]{b}}{d^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)/(c + d*x)^(7/6), x]

[Out] $(-6*(a+b*x)^{(7/6)})/(d*(c+d*x)^{(1/6)})+(7*b*(a+b*x)^{(1/6)}*(c+d*x)^{(5/6)})/d^2+(7*b^{(1/6)}*(b*c-a*d)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3]-(2*d^{(1/6)}*(a+b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c+d*x)^{(1/6)})]/(2*\operatorname{Sqrt}[3]*d^{(13/6)})-(7*b^{(1/6)}*(b*c-a*d)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3]+(2*d^{(1/6)}*(a+b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c+d*x)^{(1/6)})]/(2*\operatorname{Sqrt}[3]*d^{(13/6)})-(7*b^{(1/6)}*(b*c-a*d)*\operatorname{ArcTanh}[(d^{(1/6)}*(a+b*x)^{(1/6)})/(b^{(1/6)}*(c+d*x)^{(1/6)})]/(3*d^{(13/6)})+(7*b^{(1/6)}*(b*c-a*d)*\operatorname{Log}[b^{(1/3)}+(d^{(1/3)}*(a+b*x)^{(1/3)})/(c+d*x)^{(1/3)}-(b^{(1/6)}*d^{(1/6)}*(a+b*x)^{(1/6)})/(c+d*x)^{(1/6)}]/(12*d^{(13/6)})-(7*b^{(1/6)}*(b*c-a*d)*\operatorname{Log}[b^{(1/3)}+(d^{(1/3)}*(a+b*x)^{(1/3)})/(c+d*x)^{(1/3)}+(b^{(1/6)}*d^{(1/6)}*(a+b*x)^{(1/6)})/(c+d*x)^{(1/6)}]/(12*d^{(13/6)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I

```

nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
  NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) &&
  !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]

```

Rule 50

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && ( !IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 63

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 204

```

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])

```

Rule 208

```

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

```

Rule 210

```

Int[((a_) + (b_.)*(x_)^(n_))^(n_ - 1), x_Symbol] := Module[{r = Numerator[Rt[-(
a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r - s*Cos[(
2*k*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r + s*Co
s[(2*k*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^2*Int[
1/(r^2 - s^2*x^2), x])/(a*n) + Dist[(2*r)/(a*n), Sum[u, {k, 1, (n - 2)/4}],
x], x]] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && NegQ[a/b]

```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int
[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a,
b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/
n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[In
t[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c},
x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_) + (e_.)*(x_))/((a_) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := D
ist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), In
t[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ
[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/6}}{(c+dx)^{7/6}} dx &= -\frac{6(a+bx)^{7/6}}{d\sqrt[6]{c+dx}} + \frac{(7b) \int \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} dx}{d} \\
&= -\frac{6(a+bx)^{7/6}}{d\sqrt[6]{c+dx}} + \frac{7b\sqrt[6]{a+bx}(c+dx)^{5/6}}{d^2} - \frac{(7b(bc-ad)) \int \frac{1}{(a+bx)^{5/6}\sqrt[6]{c+dx}} dx}{6d^2} \\
&= -\frac{6(a+bx)^{7/6}}{d\sqrt[6]{c+dx}} + \frac{7b\sqrt[6]{a+bx}(c+dx)^{5/6}}{d^2} - \frac{(7(bc-ad)) \operatorname{Subst} \left(\int \frac{1}{\sqrt[6]{c-\frac{ad}{b}+\frac{dx^6}{b}}} dx, x, \sqrt[6]{a+bx} \right)}{d^2} \\
&= -\frac{6(a+bx)^{7/6}}{d\sqrt[6]{c+dx}} + \frac{7b\sqrt[6]{a+bx}(c+dx)^{5/6}}{d^2} - \frac{(7(bc-ad)) \operatorname{Subst} \left(\int \frac{1}{1-\frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{d^2} \\
&= -\frac{6(a+bx)^{7/6}}{d\sqrt[6]{c+dx}} + \frac{7b\sqrt[6]{a+bx}(c+dx)^{5/6}}{d^2} - \frac{(7\sqrt[6]{b}(bc-ad)) \operatorname{Subst} \left(\int \frac{\sqrt[6]{b}-\frac{\sqrt[6]{a}x}{2}}{\sqrt[3]{b}-\sqrt[6]{b}\sqrt[6]{a}x+\sqrt[3]{a}x^2} dx, x, \frac{\sqrt[6]{a}}{\sqrt[6]{c+dx}} \right)}{3d^2} \\
&= -\frac{6(a+bx)^{7/6}}{d\sqrt[6]{c+dx}} + \frac{7b\sqrt[6]{a+bx}(c+dx)^{5/6}}{d^2} - \frac{7\sqrt[6]{b}(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{a}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} \right)}{3d^{13/6}} + \frac{(7\sqrt[6]{b}(bc-ad))}{3d^{13/6}} \\
&= -\frac{6(a+bx)^{7/6}}{d\sqrt[6]{c+dx}} + \frac{7b\sqrt[6]{a+bx}(c+dx)^{5/6}}{d^2} - \frac{7\sqrt[6]{b}(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{a}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} \right)}{3d^{13/6}} + \frac{7\sqrt[6]{b}(bc-ad)}{3d^{13/6}} \\
&= -\frac{6(a+bx)^{7/6}}{d\sqrt[6]{c+dx}} + \frac{7b\sqrt[6]{a+bx}(c+dx)^{5/6}}{d^2} + \frac{7\sqrt[6]{b}(bc-ad) \tan^{-1} \left(\frac{1-\frac{2\sqrt[6]{a}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3}d^{13/6}} - \frac{7\sqrt[6]{b}(bc-ad)}{2\sqrt{3}d^{13/6}}
\end{aligned}$$

Mathematica [C] time = 0.07, size = 73, normalized size = 0.18

$$\frac{6(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad} \right)^{7/6} {}_2F_1 \left(\frac{7}{6}, \frac{13}{6}; \frac{19}{6}; \frac{d(a+bx)}{ad-bc} \right)}{13b(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)/(c + d*x)^(7/6), x]

[Out] $(6*(a + b*x)^{(13/6)*((b*(c + d*x))/(b*c - a*d))^{(7/6)*\text{Hypergeometric2F1}[7/6, 13/6, 19/6, (d*(a + b*x))/(-(b*c) + a*d)]})/(13*b*(c + d*x)^{(7/6)})$

fricas [B] time = 1.21, size = 3084, normalized size = 7.65

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(7/6)/(d*x+c)^(7/6),x, algorithm="fricas")`

[Out]
$$\begin{aligned} & -1/12*(28*\sqrt{3}*(d^3*x + c*d^2))*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^{13})^{(1/6)}*\arctan(1/3*(2*\sqrt{3}*(b*c*d^{11} - a*d^{12})*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^{13})^{(5/6)} + 2*\sqrt{3}*(d^{12}*x + c*d^{11})*\sqrt{((b*c*d^2 - a*d^3)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^{13})^{(1/6)} + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)} + (d^5*x + c*d^4)*(b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^{13})^{(1/3)})/(d*x + c))*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^{13})^{(5/6)} + \sqrt{3}*(b^7*c^7 - 6*a*b^6*c^6*d + 15*a^2*b^5*c^5*d^2 - 20*a^3*b^4*c^4*d^3 + 15*a^4*b^3*c^3*d^4 - 6*a^5*b^2*c^2*d^5 + a^6*b*c*d^6 + (b^7*c^6*d - 6*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 - 20*a^3*b^4*c^3*d^4 + 15*a^4*b^3*c^2*d^5 - 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x))/(b^7*c^7 - 6*a*b^6*c^6*d + 15*a^2*b^5*c^5*d^2 - 20*a^3*b^4*c^4*d^3 + 15*a^4*b^3*c^3*d^4 - 6*a^5*b^2*c^2*d^5 + a^6*b*c*d^6 + (b^7*c^6*d - 6*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 - 20*a^3*b^4*c^3*d^4 + 15*a^4*b^3*c^2*d^5 - 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x)) + 28*\sqrt{3}*(d^3*x + c*d^2))*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^{13})^{(1/6)}*\arctan(1/3*(2*\sqrt{3}*(b*c*d^{11} - a*d^{12})*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^{13})^{(5/6)} + 2*\sqrt{3}*(d^{12}*x + c*d^{11})*\sqrt{-(b*c*d^2 - a*d^3)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^{13})^{(1/6)} - (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)} - (d^5*x + c*d^4)*(b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^{13})^{(1/3)})/(d*x + c))*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^{13})^{(5/6)} - \sqrt{3}*(b^7*c^7 - 6*a*b^6*c^6*d + 15*a^2*b^5*c^5*d^2 - 20*a^3*b^4*c^4*d^3 + 15*a^4*b^3*c^3*d^4 - 6*a^5*b^2*c^2*d^5 + a^6*b*c*d^6 + (b^7*c^6*d - 6*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 - 20*a^3*b^4*c^3*d^4 + 15*a^4*b^3*c^2*d^5 - 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x))/(b^7*c^7 - 6*a*b^6*c^6*d + 15*a^2*b^5*c^5*d^2 - 20*a^3*b^4*c^4*d^3 + 15*a^4*b^3*c^3*d^4 - 6*a^5*b^2*c^2*d^5 + a^6*b*c*d^6 + (b^7*c^6*d - 6*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 - 20*a^3*b^4*c^3*d^4 + 15*a^4*b^3*c^2*d^5 - 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x)) \end{aligned}$$

```

*c^2*d^5 - 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x))/(b^7*c^7 - 6*a*b^6*c^6*d + 15*a
^2*b^5*c^5*d^2 - 20*a^3*b^4*c^4*d^3 + 15*a^4*b^3*c^3*d^4 - 6*a^5*b^2*c^2*d^
5 + a^6*b*c*d^6 + (b^7*c^6*d - 6*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 - 20*a^
3*b^4*c^3*d^4 + 15*a^4*b^3*c^2*d^5 - 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x)) + 7*(
d^3*x + c*d^2)*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*
c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^13)^(1/6)*log
(49*((b*c*d^2 - a*d^3)*(b*x + a)^(1/6)*(d*x + c)^(5/6))*((b^7*c^6 - 6*a*b^6*
c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^
5*b^2*c*d^5 + a^6*b*d^6)/d^13)^(1/6) + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x
+ a)^(1/3)*(d*x + c)^(2/3) + (d^5*x + c*d^4)*((b^7*c^6 - 6*a*b^6*c^5*d + 1
5*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d
^5 + a^6*b*d^6)/d^13)^(1/3))/(d*x + c)) - 7*(d^3*x + c*d^2)*((b^7*c^6 - 6*a
*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 -
6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^13)^(1/6)*log(-49*((b*c*d^2 - a*d^3)*(b*x +
a)^(1/6)*(d*x + c)^(5/6))*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 -
20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^13
)^(1/6) - (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^(1/3)*(d*x + c)^(2/3) -
(d^5*x + c*d^4)*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^
4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^13)^(1/3))/
(d*x + c)) + 14*(d^3*x + c*d^2)*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*
d^2 - 20*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6
)/d^13)^(1/6)*log(-7*((b*c - a*d)*(b*x + a)^(1/6)*(d*x + c)^(5/6) + (d^3*x
+ c*d^2)*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^
3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^13)^(1/6)))/(d*x + c
)) - 14*(d^3*x + c*d^2)*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20
*a^3*b^4*c^3*d^3 + 15*a^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^13)^
(1/6)*log(-7*((b*c - a*d)*(b*x + a)^(1/6)*(d*x + c)^(5/6) - (d^3*x + c*d^2)
*((b^7*c^6 - 6*a*b^6*c^5*d + 15*a^2*b^5*c^4*d^2 - 20*a^3*b^4*c^3*d^3 + 15*a
^4*b^3*c^2*d^4 - 6*a^5*b^2*c*d^5 + a^6*b*d^6)/d^13)^(1/6)))/(d*x + c)) - 12*
(b*d*x + 7*b*c - 6*a*d)*(b*x + a)^(1/6)*(d*x + c)^(5/6))/(d^3*x + c*d^2)

```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(7/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(7/6), x)

maple [F] time = 0.14, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)/(d*x+c)^(7/6),x)

[Out] int((b*x+a)^(7/6)/(d*x+c)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(7/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(7/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{\frac{7}{6}}}{(c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)/(c + d*x)^(7/6),x)

[Out] int((a + b*x)^(7/6)/(c + d*x)^(7/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^{\frac{7}{6}}}{(c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)/(d*x+c)**(7/6),x)

[Out] Integral((a + b*x)**(7/6)/(c + d*x)**(7/6), x)

$$3.1800 \quad \int \frac{(a+bx)^{7/6}}{(c+dx)^{13/6}} dx$$

Optimal. Leaf size=358

$$\frac{b^{7/6} \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{13/6}} + \frac{b^{7/6} \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{13/6}} - \frac{\sqrt{3} b^{7/6} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{d}}{\sqrt{3}\sqrt[6]{b}}\right)}{d^{13/6}}$$

[Out] $-6/7*(b*x+a)^{(7/6)}/d/(d*x+c)^{(7/6)}-6*b*(b*x+a)^{(1/6)}/d^2/(d*x+c)^{(1/6)}+2*b^{(7/6)*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/d^{(13/6)}-1/2*b^{(7/6)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/6)}-b^{(1/6)*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/d^{(13/6)}+1/2*b^{(7/6)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/d^{(13/6)}+b^{(7/6)*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})*3^{(1/2)}/d^{(13/6)}+b^{(7/6)*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})*3^{(1/2)}/d^{(13/6)}$

Rubi [A] time = 0.50, antiderivative size = 358, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 63, 240, 210, 634, 618, 204, 628, 208}

$$\frac{b^{7/6} \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{13/6}} + \frac{b^{7/6} \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2d^{13/6}} - \frac{\sqrt{3} b^{7/6} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{d}}{\sqrt{3}\sqrt[6]{b}}\right)}{d^{13/6}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)/(c + d*x)^(13/6), x]

[Out] $(-6*(a + b*x)^{(7/6)}/(7*d*(c + d*x)^{(7/6)}) - (6*b*(a + b*x)^{(1/6)})/(d^2*(c + d*x)^{(1/6)}) - (\operatorname{Sqrt}[3]*b^{(7/6)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/d^{(13/6)} + (\operatorname{Sqrt}[3]*b^{(7/6)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/d^{(13/6)} + (2*b^{(7/6)*\operatorname{ArcTanh}[(d^{(1/6)}*(a + b*x)^{(1/6)})/(b^{(1/6)}*(c + d*x)^{(1/6)})])/d^{(13/6)} - (b^{(7/6)*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})}/(2*d^{(13/6)}) + (b^{(7/6)*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})}/(2*d^{(13/6)})$

Rule 47

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&

NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 204

Int[((a_.) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rule 210

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Module[{r = Numerator[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r - s*Cos[(2*k*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r + s*Cos[(2*k*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^2*Int[1/(r^2 - s^2*x^2), x])/(a*n) + Dist[(2*r)/(a*n), Sum[u, {k, 1, (n - 2)/4}], x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && NegQ[a/b]

Rule 240

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/n]

Rule 618

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rule 628

```
Int[((d_) + (e_)*(x_))/((a_) + (b_)*(x_) + (c_)*(x_)^2), x_Symbol] :> S
imp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d,
e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_) + (e_)*(x_))/((a_) + (b_)*(x_) + (c_)*(x_)^2), x_Symbol] :> D
ist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), In
t[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ
[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]
```

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/6}}{(c+dx)^{13/6}} dx &= -\frac{6(a+bx)^{7/6}}{7d(c+dx)^{7/6}} + \frac{b \int \frac{\sqrt[6]{a+bx}}{(c+dx)^{7/6}} dx}{d} \\
&= -\frac{6(a+bx)^{7/6}}{7d(c+dx)^{7/6}} - \frac{6b\sqrt[6]{a+bx}}{d^2\sqrt[6]{c+dx}} + \frac{b^2 \int \frac{1}{(a+bx)^{5/6}\sqrt[6]{c+dx}} dx}{d^2} \\
&= -\frac{6(a+bx)^{7/6}}{7d(c+dx)^{7/6}} - \frac{6b\sqrt[6]{a+bx}}{d^2\sqrt[6]{c+dx}} + \frac{(6b) \text{Subst} \left(\int \frac{1}{\sqrt[6]{c-\frac{ad}{b}+\frac{dx^6}{b}}} dx, x, \sqrt[6]{a+bx} \right)}{d^2} \\
&= -\frac{6(a+bx)^{7/6}}{7d(c+dx)^{7/6}} - \frac{6b\sqrt[6]{a+bx}}{d^2\sqrt[6]{c+dx}} + \frac{(6b) \text{Subst} \left(\int \frac{1}{1-\frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{d^2} \\
&= -\frac{6(a+bx)^{7/6}}{7d(c+dx)^{7/6}} - \frac{6b\sqrt[6]{a+bx}}{d^2\sqrt[6]{c+dx}} + \frac{(2b^{7/6}) \text{Subst} \left(\int \frac{\sqrt[6]{b}-\frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b}-\sqrt[6]{b}\sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{d^2} + \frac{(2b^{7/6}) \text{Subst} \left(\int \frac{\sqrt[6]{b}+\frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b}+\sqrt[6]{b}\sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{d^2} \\
&= -\frac{6(a+bx)^{7/6}}{7d(c+dx)^{7/6}} - \frac{6b\sqrt[6]{a+bx}}{d^2\sqrt[6]{c+dx}} + \frac{2b^{7/6} \tanh^{-1} \left(\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} \right)}{d^{13/6}} - \frac{b^{7/6} \text{Subst} \left(\int \frac{-\sqrt[6]{b}\sqrt[6]{d}+2\sqrt[3]{d}x}{\sqrt[3]{b}-\sqrt[6]{b}\sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2d^{13/6}} \\
&= -\frac{6(a+bx)^{7/6}}{7d(c+dx)^{7/6}} - \frac{6b\sqrt[6]{a+bx}}{d^2\sqrt[6]{c+dx}} + \frac{2b^{7/6} \tanh^{-1} \left(\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} \right)}{d^{13/6}} - \frac{b^{7/6} \log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} - \frac{\sqrt[6]{b}\sqrt[6]{c+dx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} \right)}{2d^{13/6}} \\
&= -\frac{6(a+bx)^{7/6}}{7d(c+dx)^{7/6}} - \frac{6b\sqrt[6]{a+bx}}{d^2\sqrt[6]{c+dx}} - \frac{\sqrt{3}b^{7/6} \tan^{-1} \left(\frac{1-\frac{2\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{d^{13/6}} + \frac{\sqrt{3}b^{7/6} \tan^{-1} \left(\frac{1+\frac{2\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{d^{13/6}}
\end{aligned}$$

Mathematica [C] time = 0.09, size = 73, normalized size = 0.20

$$\frac{6(a+bx)^{13/6} \left(\frac{b(c+dx)}{bc-ad} \right)^{13/6} {}_2F_1 \left(\frac{13}{6}, \frac{13}{6}; \frac{19}{6}; \frac{d(a+bx)}{ad-bc} \right)}{13b(c+dx)^{13/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)/(c + d*x)^(13/6), x]

[Out] $(6*(a + b*x)^{(13/6)*((b*(c + d*x))/(b*c - a*d))^{(13/6)*Hypergeometric2F1[13/6, 13/6, 19/6, (d*(a + b*x))/(-(b*c) + a*d)]})/(13*b*(c + d*x)^{(13/6)}$

fricas [B] time = 1.14, size = 855, normalized size = 2.39

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(7/6)/(d*x+c)^(13/6),x, algorithm="fricas")`

[Out] $-1/14*(28*\sqrt{3}*(d^4*x^2 + 2*c*d^3*x + c^2*d^2)*(b^7/d^{13})^{(1/6)}*\arctan(-1/3*(2*\sqrt{3}*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*b*d^{11}*(b^7/d^{13})^{(5/6)} - 2*\sqrt{3}*(d^{12}*x + c*d^{11})*\sqrt{((b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*b*d^2*(b^7/d^{13})^{(1/6)} + (b*x + a)^{(1/3)}*(d*x + c)^{(2/3)}*b^2 + (d^5*x + c*d^4)*(b^7/d^{13})^{(1/3)})/(d*x + c)}*(b^7/d^{13})^{(5/6)} + \sqrt{3}*(b^7*d*x + b^7*c))/(b^7*d*x + b^7*c)) + 28*\sqrt{3}*(d^4*x^2 + 2*c*d^3*x + c^2*d^2)*(b^7/d^{13})^{(1/6)}*\arctan(-1/3*(2*\sqrt{3}*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*b*d^{11}*(b^7/d^{13})^{(5/6)} - 2*\sqrt{3}*(d^{12}*x + c*d^{11})*\sqrt{-((b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*b*d^2*(b^7/d^{13})^{(1/6)} - (b*x + a)^{(1/3)}*(d*x + c)^{(2/3)}*b^2 - (d^5*x + c*d^4)*(b^7/d^{13})^{(1/3)})/(d*x + c)}*(b^7/d^{13})^{(5/6)} - \sqrt{3}*(b^7*d*x + b^7*c))/(b^7*d*x + b^7*c)) - 7*(d^4*x^2 + 2*c*d^3*x + c^2*d^2)*(b^7/d^{13})^{(1/6)}*\log(4*((b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*b*d^2*(b^7/d^{13})^{(1/6)} + (b*x + a)^{(1/3)}*(d*x + c)^{(2/3)}*b^2 + (d^5*x + c*d^4)*(b^7/d^{13})^{(1/3)})/(d*x + c)) + 7*(d^4*x^2 + 2*c*d^3*x + c^2*d^2)*(b^7/d^{13})^{(1/6)}*\log(-4*((b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*b*d^2*(b^7/d^{13})^{(1/6)} - (b*x + a)^{(1/3)}*(d*x + c)^{(2/3)}*b^2 - (d^5*x + c*d^4)*(b^7/d^{13})^{(1/3)})/(d*x + c)) - 14*(d^4*x^2 + 2*c*d^3*x + c^2*d^2)*(b^7/d^{13})^{(1/6)}*\log(((b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*b + (d^3*x + c*d^2)*(b^7/d^{13})^{(1/6)})/(d*x + c)) + 14*(d^4*x^2 + 2*c*d^3*x + c^2*d^2)*(b^7/d^{13})^{(1/6)}*\log(((b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*b - (d^3*x + c*d^2)*(b^7/d^{13})^{(1/6)})/(d*x + c)) + 12*(8*b*d*x + 7*b*c + a*d)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)})/(d^4*x^2 + 2*c*d^3*x + c^2*d^2)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(7/6)/(d*x+c)^(13/6),x, algorithm="giac")`

[Out] `integrate((b*x + a)^(7/6)/(d*x + c)^(13/6), x)`

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)/(d*x+c)^(13/6),x)

[Out] int((b*x+a)^(7/6)/(d*x+c)^(13/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(13/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(13/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(a + bx)^{\frac{7}{6}}}{(c + dx)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)/(c + d*x)^(13/6),x)

[Out] int((a + b*x)^(7/6)/(c + d*x)^(13/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)/(d*x+c)**(13/6),x)

[Out] Timed out

$$3.1801 \quad \int \frac{(a+bx)^{7/6}}{(c+dx)^{19/6}} dx$$

Optimal. Leaf size=32

$$\frac{6(a+bx)^{13/6}}{13(c+dx)^{13/6}(bc-ad)}$$

[Out] 6/13*(b*x+a)^(13/6)/(-a*d+b*c)/(d*x+c)^(13/6)

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{6(a+bx)^{13/6}}{13(c+dx)^{13/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)/(c + d*x)^(19/6), x]

[Out] (6*(a + b*x)^(13/6))/(13*(b*c - a*d)*(c + d*x)^(13/6))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{(a+bx)^{7/6}}{(c+dx)^{19/6}} dx = \frac{6(a+bx)^{13/6}}{13(bc-ad)(c+dx)^{13/6}}$$

Mathematica [A] time = 0.02, size = 32, normalized size = 1.00

$$\frac{6(a+bx)^{13/6}}{13(c+dx)^{13/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)/(c + d*x)^(19/6), x]

[Out] (6*(a + b*x)^(13/6))/(13*(b*c - a*d)*(c + d*x)^(13/6))

fricas [B] time = 0.90, size = 104, normalized size = 3.25

$$\frac{6(b^2x^2 + 2abx + a^2)(bx + a)^{\frac{1}{6}}(dx + c)^{\frac{5}{6}}}{13(bc^4 - ac^3d + (bcd^3 - ad^4)x^3 + 3(bc^2d^2 - acd^3)x^2 + 3(bc^3d - ac^2d^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(19/6),x, algorithm="fricas")

[Out] 6/13*(b^2*x^2 + 2*a*b*x + a^2)*(b*x + a)^(1/6)*(d*x + c)^(5/6)/(b*c^4 - a*c^3*d + (b*c*d^3 - a*d^4)*x^3 + 3*(b*c^2*d^2 - a*c*d^3)*x^2 + 3*(b*c^3*d - a*c^2*d^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(19/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(19/6), x)

maple [A] time = 0.01, size = 27, normalized size = 0.84

$$\frac{6(bx + a)^{\frac{13}{6}}}{13(dx + c)^{\frac{13}{6}}(ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)/(d*x+c)^(19/6),x)

[Out] -6/13*(b*x+a)^(13/6)/(d*x+c)^(13/6)/(a*d-b*c)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(19/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(19/6), x)

mupad [B] time = 0.76, size = 199, normalized size = 6.22

$$\frac{(c + dx)^{5/6} \left(\frac{6a^2(a+bx)^{1/6}}{13ad^4-13bcd^3} + \frac{6b^2x^2(a+bx)^{1/6}}{13ad^4-13bcd^3} + \frac{12abx(a+bx)^{1/6}}{13ad^4-13bcd^3} \right)}{x^3 - \frac{13bc^4-13ac^3d}{13ad^4-13bcd^3} + \frac{39cd^2x^2(ad-bc)}{13ad^4-13bcd^3} + \frac{39c^2dx(ad-bc)}{13ad^4-13bcd^3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)/(c + d*x)^(19/6),x)

[Out] -((c + d*x)^(5/6)*((6*a^2*(a + b*x)^(1/6))/(13*a*d^4 - 13*b*c*d^3) + (6*b^2*x^2*(a + b*x)^(1/6))/(13*a*d^4 - 13*b*c*d^3) + (12*a*b*x*(a + b*x)^(1/6))/(13*a*d^4 - 13*b*c*d^3)))/(x^3 - (13*b*c^4 - 13*a*c^3*d)/(13*a*d^4 - 13*b*c*d^3) + (39*c*d^2*x^2*(a*d - b*c))/(13*a*d^4 - 13*b*c*d^3) + (39*c^2*d*x*(a*d - b*c))/(13*a*d^4 - 13*b*c*d^3))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)/(d*x+c)**(19/6),x)

[Out] Timed out

$$3.1802 \quad \int \frac{(a+bx)^{7/6}}{(c+dx)^{25/6}} dx$$

Optimal. Leaf size=66

$$\frac{36b(a+bx)^{13/6}}{247(c+dx)^{13/6}(bc-ad)^2} + \frac{6(a+bx)^{13/6}}{19(c+dx)^{19/6}(bc-ad)}$$

[Out] $6/19*(b*x+a)^{(13/6)/(-a*d+b*c)/(d*x+c)^{(19/6)+36/247*b*(b*x+a)^{(13/6)/(-a*d+b*c)^2/(d*x+c)^{(13/6)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{36b(a+bx)^{13/6}}{247(c+dx)^{13/6}(bc-ad)^2} + \frac{6(a+bx)^{13/6}}{19(c+dx)^{19/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)/(c + d*x)^(25/6), x]

[Out] $(6*(a + b*x)^{(13/6))/(19*(b*c - a*d)*(c + d*x)^{(19/6))} + (36*b*(a + b*x)^{(13/6))/(247*(b*c - a*d)^2*(c + d*x)^{(13/6))}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[n] && !IntegerQ[m] && !IntegerQ[n]

Rubi steps

$$\int \frac{(a+bx)^{7/6}}{(c+dx)^{25/6}} dx = \frac{6(a+bx)^{13/6}}{19(bc-ad)(c+dx)^{19/6}} + \frac{(6b) \int \frac{(a+bx)^{7/6}}{(c+dx)^{19/6}} dx}{19(bc-ad)}$$

$$= \frac{6(a+bx)^{13/6}}{19(bc-ad)(c+dx)^{19/6}} + \frac{36b(a+bx)^{13/6}}{247(bc-ad)^2(c+dx)^{13/6}}$$

Mathematica [A] time = 0.04, size = 46, normalized size = 0.70

$$\frac{6(a+bx)^{13/6}(-13ad+19bc+6bdx)}{247(c+dx)^{19/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)/(c + d*x)^(25/6), x]

[Out] (6*(a + b*x)^(13/6)*(19*b*c - 13*a*d + 6*b*d*x))/(247*(b*c - a*d)^2*(c + d*x)^(19/6))

fricas [B] time = 1.00, size = 235, normalized size = 3.56

$$\frac{6(6b^3dx^3 + 19a^2bc - 13a^3d + (19b^3c - ab^2d)x^2 + 2(19ab^2c - 10a^2bd)x)(bx)}{247(b^2c^6 - 2abc^5d + a^2c^4d^2 + (b^2c^2d^4 - 2abcd^5 + a^2d^6)x^4 + 4(b^2c^3d^3 - 2abc^2d^4 + a^2cd^5)x^3 + 6(b^2c^4d^2 - 2abc^3d^3 + a^2c^2d^4)x^2 + 4(b^2c^5d - 2a^2b^2c^4d^2 + a^2c^3d^3)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(25/6), x, algorithm="fricas")

[Out] 6/247*(6*b^3*d*x^3 + 19*a^2*b*c - 13*a^3*d + (19*b^3*c - a*b^2*d)*x^2 + 2*(19*a*b^2*c - 10*a^2*b*d)*x)*(b*x + a)^(1/6)*(d*x + c)^(5/6)/(b^2*c^6 - 2*a*b*c^5*d + a^2*c^4*d^2 + (b^2*c^2*d^4 - 2*a*b*c*d^5 + a^2*d^6)*x^4 + 4*(b^2*c^3*d^3 - 2*a*b*c^2*d^4 + a^2*c*d^5)*x^3 + 6*(b^2*c^4*d^2 - 2*a*b*c^3*d^3 + a^2*c^2*d^4)*x^2 + 4*(b^2*c^5*d - 2*a*b*c^4*d^2 + a^2*c^3*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{7}{6}}}{(dx+c)^{\frac{25}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(25/6), x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(25/6), x)

maple [A] time = 0.00, size = 54, normalized size = 0.82

$$\frac{6 (bx + a)^{\frac{13}{6}} (-6bdx + 13ad - 19bc)}{247 (dx + c)^{\frac{19}{6}} (a^2d^2 - 2abcd + b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)/(d*x+c)^(25/6), x)

[Out] -6/247*(b*x+a)^(13/6)*(-6*b*d*x+13*a*d-19*b*c)/(d*x+c)^(19/6)/(a^2*d^2-2*a*b*c*d+b^2*c^2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{25}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(25/6), x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(25/6), x)

mupad [B] time = 0.91, size = 189, normalized size = 2.86

$$\frac{(c + dx)^{5/6} \left(\frac{(78a^3d - 114a^2bc)(a+bx)^{1/6}}{247d^4(ad-bc)^2} - \frac{36b^3x^3(a+bx)^{1/6}}{247d^3(ad-bc)^2} - \frac{x^2(114b^3c - 6ab^2d)(a+bx)^{1/6}}{247d^4(ad-bc)^2} + \frac{12abx(10ad - 19bc)(a+bx)^{1/6}}{247d^4(ad-bc)^2} \right)}{x^4 + \frac{c^4}{d^4} + \frac{4cx^3}{d} + \frac{4c^3x}{d^3} + \frac{6c^2x^2}{d^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)/(c + d*x)^(25/6), x)

[Out] -((c + d*x)^(5/6)*(((78*a^3*d - 114*a^2*b*c)*(a + b*x)^(1/6))/(247*d^4*(a*d - b*c)^2) - (36*b^3*x^3*(a + b*x)^(1/6))/(247*d^3*(a*d - b*c)^2) - (x^2*(14*b^3*c - 6*a*b^2*d)*(a + b*x)^(1/6))/(247*d^4*(a*d - b*c)^2) + (12*a*b*x*(10*a*d - 19*b*c)*(a + b*x)^(1/6))/(247*d^4*(a*d - b*c)^2)))/(x^4 + c^4/d^4 + (4*c*x^3)/d + (4*c^3*x)/d^3 + (6*c^2*x^2)/d^2)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(7/6)/(d*x+c)**(25/6),x)
```

```
[Out] Timed out
```


$$3.1803 \quad \int \frac{(a+bx)^{7/6}}{(c+dx)^{31/6}} dx$$

Optimal. Leaf size=101

$$\frac{432b^2(a+bx)^{13/6}}{6175(c+dx)^{13/6}(bc-ad)^3} + \frac{72b(a+bx)^{13/6}}{475(c+dx)^{19/6}(bc-ad)^2} + \frac{6(a+bx)^{13/6}}{25(c+dx)^{25/6}(bc-ad)}$$

[Out] $6/25*(b*x+a)^{(13/6)/(-a*d+b*c)/(d*x+c)^{(25/6)+72/475*b*(b*x+a)^{(13/6)/(-a*d+b*c)^2/(d*x+c)^{(19/6)+432/6175*b^2*(b*x+a)^{(13/6)/(-a*d+b*c)^3/(d*x+c)^{(13/6)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{432b^2(a+bx)^{13/6}}{6175(c+dx)^{13/6}(bc-ad)^3} + \frac{72b(a+bx)^{13/6}}{475(c+dx)^{19/6}(bc-ad)^2} + \frac{6(a+bx)^{13/6}}{25(c+dx)^{25/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)/(c + d*x)^(31/6), x]

[Out] $(6*(a + b*x)^{(13/6))/(25*(b*c - a*d)*(c + d*x)^{(25/6))} + (72*b*(a + b*x)^{(13/6))/(475*(b*c - a*d)^2*(c + d*x)^{(19/6))} + (432*b^2*(a + b*x)^{(13/6))/(6175*(b*c - a*d)^3*(c + d*x)^{(13/6))}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned} \int \frac{(a+bx)^{7/6}}{(c+dx)^{31/6}} dx &= \frac{6(a+bx)^{13/6}}{25(bc-ad)(c+dx)^{25/6}} + \frac{(12b) \int \frac{(a+bx)^{7/6}}{(c+dx)^{25/6}} dx}{25(bc-ad)} \\ &= \frac{6(a+bx)^{13/6}}{25(bc-ad)(c+dx)^{25/6}} + \frac{72b(a+bx)^{13/6}}{475(bc-ad)^2(c+dx)^{19/6}} + \frac{(72b^2) \int \frac{(a+bx)^{7/6}}{(c+dx)^{19/6}} dx}{475(bc-ad)^2} \\ &= \frac{6(a+bx)^{13/6}}{25(bc-ad)(c+dx)^{25/6}} + \frac{72b(a+bx)^{13/6}}{475(bc-ad)^2(c+dx)^{19/6}} + \frac{432b^2(a+bx)^{13/6}}{6175(bc-ad)^3(c+dx)^{13/6}} \end{aligned}$$

Mathematica [A] time = 0.06, size = 77, normalized size = 0.76

$$\frac{6(a+bx)^{13/6} (247a^2d^2 - 26abd(25c+6dx) + b^2(475c^2 + 300cdx + 72d^2x^2))}{6175(c+dx)^{25/6}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)/(c + d*x)^(31/6), x]

[Out] (6*(a + b*x)^(13/6)*(247*a^2*d^2 - 26*a*b*d*(25*c + 6*d*x) + b^2*(475*c^2 + 300*c*d*x + 72*d^2*x^2)))/(6175*(b*c - a*d)^3*(c + d*x)^(25/6))

fricas [B] time = 1.00, size = 427, normalized size = 4.23

$$\frac{6(72b^4d^2x^4 + 475a^2b^2c^2 - 650a^3bcd + 247a^4d^2 + 12(25b^4c^2d - ab^3d^2)x^3 + (475b^4c^2 - 50a^2b^3cd + 7a^2b^2d^2)x^2 + 2(475ab^3c^2 - 500a^2b^2cd + 169a^3bd^2)x)(b*x + a)^{1/6}(d*x + c)^{5/6}}{6175(b^3c^8 - 3ab^2c^7d + 3a^2bc^6d^2 - a^3c^5d^3 + (b^3c^3d^5 - 3ab^2c^2d^6 + 3a^2bcd^7 - a^3d^8)x^5 + 5(b^3c^4d^4 - 3ab^2c^3d^5 + 3a^2b^2c^4d^4 - 3a^2b^2c^3d^5 - a^3c^2d^6)x^3 + 10(b^3c^6d^2 - 3a^2b^2c^5d^3 + 3a^2b^2c^4d^4 - a^3c^3d^5)x^2 + 5(b^3c^7d - 3a^2b^2c^6d^2 + 3a^2b^2c^5d^3 - a^3c^4d^4)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(31/6), x, algorithm="fricas")

[Out] 6/6175*(72*b^4*d^2*x^4 + 475*a^2*b^2*c^2 - 650*a^3*b*c*d + 247*a^4*d^2 + 12*(25*b^4*c*d - a*b^3*d^2)*x^3 + (475*b^4*c^2 - 50*a*b^3*c*d + 7*a^2*b^2*d^2)*x^2 + 2*(475*a*b^3*c^2 - 500*a^2*b^2*c*d + 169*a^3*b*d^2)*x)*(b*x + a)^(1/6)*(d*x + c)^(5/6)/(b^3*c^8 - 3*a*b^2*c^7*d + 3*a^2*b*c^6*d^2 - a^3*c^5*d^3 + (b^3*c^3*d^5 - 3*a*b^2*c^2*d^6 + 3*a^2*b*c*d^7 - a^3*d^8)*x^5 + 5*(b^3*c^4*d^4 - 3*a*b^2*c^3*d^5 + 3*a^2*b^2*c^4*d^4 - a^3*c^2*d^6)*x^3 + 10*(b^3*c^6*d^2 - 3*a*b^2*c^5*d^3 + 3*a^2*b^2*c^4*d^4 - a^3*c^3*d^5)*x^2 + 5*(b^3*c^7*d - 3*a^2*b^2*c^6*d^2 + 3*a^2*b^2*c^5*d^3 - a^3*c^4*d^4)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx+a)^{\frac{7}{6}}}{(dx+c)^{\frac{31}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(31/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(31/6), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{6 (bx + a)^{\frac{13}{6}} \left(72b^2x^2d^2 - 156abd^2x + 300b^2cdx + 247a^2d^2 - 650abcd + 475b^2c^2 \right)}{6175 (dx + c)^{\frac{25}{6}} \left(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)/(d*x+c)^(31/6),x)

[Out] -6/6175*(b*x+a)^(13/6)*(72*b^2*d^2*x^2-156*a*b*d^2*x+300*b^2*c*d*x+247*a^2*d^2-650*a*b*c*d+475*b^2*c^2)/(d*x+c)^(25/6)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{31}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(31/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(31/6), x)

mupad [B] time = 1.14, size = 278, normalized size = 2.75

$$\frac{(c + dx)^{5/6} \left(\frac{(a+bx)^{1/6} (1482 a^4 d^2 - 3900 a^3 b c d + 2850 a^2 b^2 c^2)}{6175 d^5 (a d - b c)^3} + \frac{432 b^4 x^4 (a+bx)^{1/6}}{6175 d^3 (a d - b c)^3} + \frac{x^2 (a+bx)^{1/6} (42 a^2 b^2 d^2 - 300 a b^3 c d + 2850 b^4 c^2)}{6175 d^5 (a d - b c)^3} \right)}{x^5 + \frac{c^5}{d^5} + \frac{5 c x^4}{d} + \frac{5 c^4 x}{d^4} + \frac{10 c^2 x^3}{d^2} + \frac{10 c^3 x^2}{d^3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)/(c + d*x)^(31/6),x)

[Out] -((c + d*x)^(5/6)*(((a + b*x)^(1/6)*(1482*a^4*d^2 + 2850*a^2*b^2*c^2 - 3900*a^3*b*c*d))/(6175*d^5*(a*d - b*c)^3) + (432*b^4*x^4*(a + b*x)^(1/6))/(6175*d^3*(a*d - b*c)^3) + (x^2*(a + b*x)^(1/6)*(2850*b^4*c^2 + 42*a^2*b^2*d^2 - 300*a*b^3*c*d))/(6175*d^5*(a*d - b*c)^3) - (72*b^3*x^3*(a*d - 25*b*c)*(a + b*x)^(1/6))/(6175*d^4*(a*d - b*c)^3) + (12*a*b*x*(a + b*x)^(1/6)*(169*a^2*

$$\frac{d^2 + 475b^2c^2 - 500abc*d}{(6175d^5(ad - bc)^3)} \cdot \left(x^5 + \frac{c^5}{d^5} + \frac{5cx^4}{d} + \frac{5c^4x}{d^4} + \frac{10c^2x^3}{d^2} + \frac{10c^3x^2}{d^3} \right)$$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)/(d*x+c)**(31/6),x)

[Out] Timed out

$$3.1804 \quad \int \frac{(a+bx)^{7/6}}{(c+dx)^{37/6}} dx$$

Optimal. Leaf size=136

$$\frac{7776b^3(a+bx)^{13/6}}{191425(c+dx)^{13/6}(bc-ad)^4} + \frac{1296b^2(a+bx)^{13/6}}{14725(c+dx)^{19/6}(bc-ad)^3} + \frac{108b(a+bx)^{13/6}}{775(c+dx)^{25/6}(bc-ad)^2} + \frac{6(a+bx)^{13/6}}{31(c+dx)^{31/6}(bc-ad)}$$

[Out] $6/31*(b*x+a)^{(13/6)/(-a*d+b*c)/(d*x+c)^{(31/6)+108/775*b*(b*x+a)^{(13/6)/(-a*d+b*c)^2/(d*x+c)^{(25/6)+1296/14725*b^2*(b*x+a)^{(13/6)/(-a*d+b*c)^3/(d*x+c)^{(19/6)+7776/191425*b^3*(b*x+a)^{(13/6)/(-a*d+b*c)^4/(d*x+c)^{(13/6)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{7776b^3(a+bx)^{13/6}}{191425(c+dx)^{13/6}(bc-ad)^4} + \frac{1296b^2(a+bx)^{13/6}}{14725(c+dx)^{19/6}(bc-ad)^3} + \frac{108b(a+bx)^{13/6}}{775(c+dx)^{25/6}(bc-ad)^2} + \frac{6(a+bx)^{13/6}}{31(c+dx)^{31/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(7/6)/(c + d*x)^(37/6), x]

[Out] $(6*(a + b*x)^{(13/6)})/(31*(b*c - a*d)*(c + d*x)^{(31/6)}) + (108*b*(a + b*x)^{(13/6)})/(775*(b*c - a*d)^2*(c + d*x)^{(25/6)}) + (1296*b^2*(a + b*x)^{(13/6)})/(14725*(b*c - a*d)^3*(c + d*x)^{(19/6)}) + (7776*b^3*(a + b*x)^{(13/6)})/(191425*(b*c - a*d)^4*(c + d*x)^{(13/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[n] && !IntegerQ[m] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{(a+bx)^{7/6}}{(c+dx)^{37/6}} dx &= \frac{6(a+bx)^{13/6}}{31(bc-ad)(c+dx)^{31/6}} + \frac{(18b) \int \frac{(a+bx)^{7/6}}{(c+dx)^{31/6}} dx}{31(bc-ad)} \\
&= \frac{6(a+bx)^{13/6}}{31(bc-ad)(c+dx)^{31/6}} + \frac{108b(a+bx)^{13/6}}{775(bc-ad)^2(c+dx)^{25/6}} + \frac{(216b^2) \int \frac{(a+bx)^{7/6}}{(c+dx)^{25/6}} dx}{775(bc-ad)^2} \\
&= \frac{6(a+bx)^{13/6}}{31(bc-ad)(c+dx)^{31/6}} + \frac{108b(a+bx)^{13/6}}{775(bc-ad)^2(c+dx)^{25/6}} + \frac{1296b^2(a+bx)^{13/6}}{14725(bc-ad)^3(c+dx)^{19/6}} + \frac{(1296b^3) \int \frac{(a+bx)^{7/6}}{(c+dx)^{19/6}} dx}{14725(bc-ad)^3} \\
&= \frac{6(a+bx)^{13/6}}{31(bc-ad)(c+dx)^{31/6}} + \frac{108b(a+bx)^{13/6}}{775(bc-ad)^2(c+dx)^{25/6}} + \frac{1296b^2(a+bx)^{13/6}}{14725(bc-ad)^3(c+dx)^{19/6}} + \frac{7776b^3(a+bx)^{13/6}}{191425(bc-ad)^4}
\end{aligned}$$

Mathematica [A] time = 0.09, size = 118, normalized size = 0.87

$$\frac{6(a+bx)^{13/6} \left(-6175a^3d^3 + 741a^2bd^2(31c+6dx) - 39ab^2d(775c^2 + 372cdx + 72d^2x^2) + b^3(14725c^3 + 13950c^2dx + 696cd^2x^2 + 1296d^3x^3) \right)}{191425(c+dx)^{31/6}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(7/6)/(c + d*x)^(37/6), x]

[Out] (6*(a + b*x)^(13/6)*(-6175*a^3*d^3 + 741*a^2*b*d^2*(31*c + 6*d*x) - 39*a*b^2*d*(775*c^2 + 372*c*d*x + 72*d^2*x^2) + b^3*(14725*c^3 + 13950*c^2*d*x + 696*c*d^2*x^2 + 1296*d^3*x^3))/(191425*(b*c - a*d)^4*(c + d*x)^(31/6))

fricas [B] time = 1.04, size = 649, normalized size = 4.77

$$\frac{6(1296b^5d^3x^5 + 14725a^2b^3c^3 - 30225a^3b^2c^2d + 22971a^4b^2cd^2 - 6175a^5d^3 + 216(31b^5cd^2 - ab^4d^3)x^4 + 18(775b^5c^2d - 62ab^4cd^2 + 7a^2b^3d^3)x^3 + (14725b^5c^3 - 2325ab^4c^2d + 651a^2b^3cd^2 - 91a^3b^2d^3)x^2 + 2(14725ab^4c^3 - 23250a^2b^3c^2d + 15717a^3b^2cd^2 - 3952a^4bd^3)x)(b*x + a)^{(1/6)}(d*x + c)^{(5/6)}}{(b^4c^{10} - 4ab^3c^9d + 6a^2b^2c^8d^2 - 4a^3bc^7d^3 + a^4c^6d^4 + (b^4c^4d^6 - 4ab^3c^3d^7 + 6a^2b^2c^2d^8 - 4a^3bcd^9 + a^4d^{10}))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(37/6), x, algorithm="fricas")

[Out] 6/191425*(1296*b^5*d^3*x^5 + 14725*a^2*b^3*c^3 - 30225*a^3*b^2*c^2*d + 22971*a^4*b^2*c*d^2 - 6175*a^5*d^3 + 216*(31*b^5*c*d^2 - a*b^4*d^3)*x^4 + 18*(775*b^5*c^2*d - 62*a*b^4*c*d^2 + 7*a^2*b^3*d^3)*x^3 + (14725*b^5*c^3 - 2325*a*b^4*c^2*d + 651*a^2*b^3*c*d^2 - 91*a^3*b^2*d^3)*x^2 + 2*(14725*a*b^4*c^3 - 23250*a^2*b^3*c^2*d + 15717*a^3*b^2*c*d^2 - 3952*a^4*b*d^3)*x*(b*x + a)^(1/6)*(d*x + c)^(5/6)/(b^4*c^10 - 4*a*b^3*c^9*d + 6*a^2*b^2*c^8*d^2 - 4*a^3*b*c^7*d^3 + a^4*c^6*d^4 + (b^4*c^4*d^6 - 4*a*b^3*c^3*d^7 + 6*a^2*b^2*c^2*d^8 - 4*a^3*b*c*d^9 + a^4*d^10)*x^6 + 6*(b^4*c^5*d^5 - 4*a*b^3*c^4*d^6 + 6*a^2*b^2*c^3*d^7 - 4*a^3*b*c^2*d^8 + 5*a^4*d^9))

$*b^2*c^3*d^7 - 4*a^3*b*c^2*d^8 + a^4*c*d^9)*x^5 + 15*(b^4*c^6*d^4 - 4*a*b^3*c^5*d^5 + 6*a^2*b^2*c^4*d^6 - 4*a^3*b*c^3*d^7 + a^4*c^2*d^8)*x^4 + 20*(b^4*c^7*d^3 - 4*a*b^3*c^6*d^4 + 6*a^2*b^2*c^5*d^5 - 4*a^3*b*c^4*d^6 + a^4*c^3*d^7)*x^3 + 15*(b^4*c^8*d^2 - 4*a*b^3*c^7*d^3 + 6*a^2*b^2*c^6*d^4 - 4*a^3*b*c^5*d^5 + a^4*c^4*d^6)*x^2 + 6*(b^4*c^9*d - 4*a*b^3*c^8*d^2 + 6*a^2*b^2*c^7*d^3 - 4*a^3*b*c^6*d^4 + a^4*c^5*d^5)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{37}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(37/6),x, algorithm="giac")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(37/6), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{6(bx + a)^{\frac{13}{6}} \left(-1296b^3d^3x^3 + 2808ab^2d^3x^2 - 6696b^3cd^2x^2 - 4446a^2bd^3x + 14508ab^2cd^2x - 13950b^3c^2dx + 6 \right)}{191425(dx + c)^{\frac{31}{6}} \left(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + \dots \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(7/6)/(d*x+c)^(37/6),x)

[Out] $-6/191425*(b*x+a)^{(13/6)}*(-1296*b^3*d^3*x^3+2808*a*b^2*d^3*x^2-6696*b^3*c*d^2*x^2-4446*a^2*b*d^3*x+14508*a*b^2*c*d^2*x-13950*b^3*c^2*d*x+6175*a^3*d^3-22971*a^2*b*c*d^2+30225*a*b^2*c^2*d-14725*b^3*c^3)/(d*x+c)^{(31/6)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{\frac{7}{6}}}{(dx + c)^{\frac{37}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(7/6)/(d*x+c)^(37/6),x, algorithm="maxima")

[Out] integrate((b*x + a)^(7/6)/(d*x + c)^(37/6), x)

mupad [B] time = 1.43, size = 385, normalized size = 2.83

$$(c + dx)^{5/6} \left(\frac{7776 b^5 x^5 (a+bx)^{1/6}}{191425 d^3 (ad-bc)^4} - \frac{(a+bx)^{1/6} (37050 a^5 d^3 - 137826 a^4 b c d^2 + 181350 a^3 b^2 c^2 d - 88350 a^2 b^3 c^3)}{191425 d^6 (ad-bc)^4} + \frac{x^2 (a+bx)^{1/6} (-546 a^3 b^2 d^3 + 3906 a^2 b^3 c d^2 - 13950 a b^4 c^2 d + 176700 a^2 b^4 c^3 - 47424 a^4 b^3 c d^3 - 279000 a^2 b^3 c^2 d + 188604 a^3 b^2 c^2 d^2)}{191425 d^6 (ad-bc)^4} \right) + \frac{x (a+bx)^{1/6} (108 b^3 x^3 (a+bx)^{1/6} (7 a^2 d^2 + 775 b^2 c^2 - 62 a b c d) - (1296 b^4 x^4 (a d - 31 b c) (a+bx)^{1/6}) / (191425 d^4 (ad-bc)^4))}{(x^6 + c^6/d^6 + (6 c x^5)/d + (6 c^5 x)/d^5 + (15 c^2 x^4)/d^2 + (20 c^3 x^3)/d^3 + (15 c^4 x^2)/d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(7/6)/(c + d*x)^(37/6),x)

[Out] ((c + d*x)^(5/6)*((7776*b^5*x^5*(a + b*x)^(1/6))/(191425*d^3*(a*d - b*c)^4) - ((a + b*x)^(1/6)*(37050*a^5*d^3 - 88350*a^2*b^3*c^3 + 181350*a^3*b^2*c^2*d - 137826*a^4*b*c*d^2))/(191425*d^6*(a*d - b*c)^4) + (x^2*(a + b*x)^(1/6)*(88350*b^5*c^3 - 546*a^3*b^2*d^3 + 3906*a^2*b^3*c*d^2 - 13950*a*b^4*c^2*d))/(191425*d^6*(a*d - b*c)^4) + (x*(a + b*x)^(1/6)*(176700*a*b^4*c^3 - 47424*a^4*b*d^3 - 279000*a^2*b^3*c^2*d + 188604*a^3*b^2*c*d^2))/(191425*d^6*(a*d - b*c)^4) + (108*b^3*x^3*(a + b*x)^(1/6)*(7*a^2*d^2 + 775*b^2*c^2 - 62*a*b*c*d))/(191425*d^5*(a*d - b*c)^4) - (1296*b^4*x^4*(a*d - 31*b*c)*(a + b*x)^(1/6))/(191425*d^4*(a*d - b*c)^4)))/(x^6 + c^6/d^6 + (6*c*x^5)/d + (6*c^5*x)/d^5 + (15*c^2*x^4)/d^2 + (20*c^3*x^3)/d^3 + (15*c^4*x^2)/d^4)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(7/6)/(d*x+c)**(37/6),x)

[Out] Timed out

$$3.1805 \quad \int \frac{(c+dx)^{7/6}}{\sqrt[6]{a+bx}} dx$$

Optimal. Leaf size=424

$$\frac{7(bc-ad)^2 \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{13/6}d^{5/6}} + \frac{7(bc-ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{13/6}d^{5/6}} + \frac{7(bc-ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{13/6}d^{5/6}}$$

[Out] $7/12*(-a*d+b*c)*(b*x+a)^{(5/6)}*(d*x+c)^{(1/6)}/b^{2+1/2}*(b*x+a)^{(5/6)}*(d*x+c)^{(7/6)}/b+7/36*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(13/6)}/d^{(5/6)}-7/144*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(13/6)}/d^{(5/6)}+7/144*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(13/6)}/d^{(5/6)}-7/72*(-a*d+b*c)^2*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(13/6)}/d^{(5/6)}*3^{(1/2)}-7/72*(-a*d+b*c)^2*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(13/6)}/d^{(5/6)}*3^{(1/2)}$

Rubi [A] time = 0.61, antiderivative size = 424, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {50, 63, 331, 296, 634, 618, 204, 628, 208}

$$\frac{7(bc-ad)^2 \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{13/6}d^{5/6}} + \frac{7(bc-ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{13/6}d^{5/6}} + \frac{7(bc-ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{13/6}d^{5/6}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(7/6)}/(a + b*x)^{(1/6)}, x]$

[Out] $(7*(b*c - a*d)*(a + b*x)^{(5/6)}*(c + d*x)^{(1/6)})/(12*b^2) + ((a + b*x)^{(5/6)}*(c + d*x)^{(7/6)})/(2*b) + (7*(b*c - a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(13/6)}*d^{(5/6)}) - (7*(b*c - a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(13/6)}*d^{(5/6)}) + (7*(b*c - a*d)^2*\operatorname{ArcTanh}[(d^{(1/6)}*(a + b*x)^{(1/6)})/(b^{(1/6)}*(c + d*x)^{(1/6)})]/(36*b^{(13/6)}*d^{(5/6)}) - (7*(b*c - a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})]/(144*b^{(13/6)}*d^{(5/6)}) + (7*(b*c - a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})]/(144*b^{(13/6)}*d^{(5/6)})$

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rule 296

```
Int[(x_)^(m_.)/((a_) + (b_.)*(x_)^(n_)), x_Symbol] := Module[{r = Numerator
[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r*Cos
[(2*k*m*Pi)/n] - s*Cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*
x + s^2*x^2), x] + Int[(r*Cos[(2*k*m*Pi)/n] + s*Cos[(2*k*(m + 1)*Pi)/n]*x)/
(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^(m + 2)*Int[1/(r^2 - s^
2*x^2), x])/(a*n*s^m) + Dist[(2*r^(m + 1))/(a*n*s^m), Sum[u, {k, 1, (n - 2)
/4}], x], x]] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && IGtQ[m, 0] && Lt
Q[m, n - 1] && NegQ[a/b]
```

Rule 331

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m +
1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)
^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2
^(-1)] && IntegersQ[m, p + (m + 1)/n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_.) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), Int[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{7/6}}{\sqrt[6]{a+bx}} dx &= \frac{(a+bx)^{5/6}(c+dx)^{7/6}}{2b} + \frac{(7(bc-ad)) \int \frac{\sqrt[6]{c+dx}}{\sqrt[6]{a+bx}} dx}{12b} \\
&= \frac{7(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12b^2} + \frac{(a+bx)^{5/6}(c+dx)^{7/6}}{2b} + \frac{(7(bc-ad)^2) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{5/6}} dx}{72b^2} \\
&= \frac{7(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12b^2} + \frac{(a+bx)^{5/6}(c+dx)^{7/6}}{2b} + \frac{(7(bc-ad)^2) \text{Subst} \left(\int \frac{x^4}{\left(c-\frac{ad}{b}+\frac{dx^6}{b}\right)^{5/6}} dx \right)}{12b^3} \\
&= \frac{7(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12b^2} + \frac{(a+bx)^{5/6}(c+dx)^{7/6}}{2b} + \frac{(7(bc-ad)^2) \text{Subst} \left(\int \frac{x^4}{1-\frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{b} \right)}{12b^3} \\
&= \frac{7(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12b^2} + \frac{(a+bx)^{5/6}(c+dx)^{7/6}}{2b} + \frac{(7(bc-ad)^2) \text{Subst} \left(\int \frac{-\frac{\sqrt[6]{b}}{2}-\frac{\sqrt[6]{dx}}{2}}{\sqrt[3]{b}-\sqrt[6]{b}\sqrt[6]{dx}x+\sqrt[6]{d}} dx \right)}{36b^{13/6}d^{2/3}} \\
&= \frac{7(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12b^2} + \frac{(a+bx)^{5/6}(c+dx)^{7/6}}{2b} + \frac{7(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} \right)}{36b^{13/6}d^{5/6}} \\
&= \frac{7(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12b^2} + \frac{(a+bx)^{5/6}(c+dx)^{7/6}}{2b} + \frac{7(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} \right)}{36b^{13/6}d^{5/6}} \\
&= \frac{7(bc-ad)(a+bx)^{5/6} \sqrt[6]{c+dx}}{12b^2} + \frac{(a+bx)^{5/6}(c+dx)^{7/6}}{2b} + \frac{7(bc-ad)^2 \tan^{-1} \left(\frac{1-2\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{24\sqrt{3}b^{13/6}d^{5/6}}
\end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.17

$$\frac{6(a+bx)^{5/6}(c+dx)^{7/6} {}_2F_1 \left(-\frac{7}{6}, \frac{5}{6}; \frac{11}{6}; \frac{d(a+bx)}{ad-bc} \right)}{5b \left(\frac{b(c+dx)}{bc-ad} \right)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(7/6)/(a + b*x)^(1/6), x]

[Out] $(6*(a + b*x)^{(5/6)}*(c + d*x)^{(7/6)}*\text{Hypergeometric2F1}[-7/6, 5/6, 11/6, (d*(a + b*x))/(-b*c) + a*d])/(5*b*((b*(c + d*x))/(b*c - a*d))^{(7/6)})$

fricas [B] time = 1.31, size = 5633, normalized size = 13.29

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(7/6)/(b*x+a)^(1/6),x, algorithm="fricas")`

[Out]
$$\begin{aligned} & -1/144*(28*\sqrt{3}*b^2*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^{13}d^5))^{(1/6)}*\arctan(-1/3*(2*\sqrt{3}*(b^{13}c^2d^4 - 2*a*b^{12}c*d^5 + a^2*b^{11}d^6)*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^{13}d^5))^{(1/6)} - 2*\sqrt{3}*(b^{12}d^4*x + a*b^{11}d^4)*\sqrt{((b^4c^2d - 2*a*b^3c*d^2 + a^2*b^2d^3)*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^{13}d^5))^{(1/6)} + (b^4c^4 - 4*a*b^3c^3d + 6*a^2b^2c^2d^2 - 4*a^3b*c*d^3 + a^4d^4)*(b*x + a)^{(2/3)}*(d*x + c)^{(1/3)} + (b^5d^2*x + a*b^4d^2)*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^{13}d^5))^{(1/3)})/(b*x + a))*((b^{12}c^{12} - 12*a*b^{11}c^{11}d + 66*a^2*b^{10}c^{10}d^2 - 220*a^3*b^9c^9d^3 + 495*a^4*b^8c^8d^4 - 792*a^5*b^7c^7d^5 + 924*a^6*b^6c^6d^6 - 792*a^7*b^5c^5d^7 + 495*a^8*b^4c^4d^8 - 220*a^9*b^3c^3d^9 + 66*a^{10}b^2c^2d^{10} - 12*a^{11}b*c*d^{11} + a^{12}d^{12})/(b^{13}d^5))^{(5/6)} + \sqrt{3}*(a*b^{12}c^{12} - 12*a^2*b^{11}c^{11}d + 66*a^3*b^{10}c^{10}d^2 - 220*a^4*b^9c^9d^3 + 495*a^5*b^8c^8d^4 - 792*a^6*b^7c^7d^5 + 924*a^7*b^6c^6d^6 - 792*a^8*b^5c^5d^7 + 495*a^9*b^4c^4d^8 - 220*a^{10}b^3c^3d^9 + 66*a^{11}b^2c^2d^{10} - 12*a^{12}b*c*d^{11} + a^{13}d^{12} + (b^{13}c^{12} - 12*a*b^{12}c^{11}d + 66*a^2*b^{11}c^{10}d^2 - 220*a^3*b^{10}c^9d^3 + 495*a^4*b^9c^8d^4 - 792*a^5*b^8c^7d^5 + 924*a^6*b^7c^6d^6 - 792*a^7*b^6c^5d^7 + 495*a^8*b^5c^4d^8 - 220*a^9*b^4c^3d^9 + 66*a^{10}b^3c^2d^{10} - 12*a^{11}b^2c*d^{11} + a^{12}b*d^{12})*x)/(a*b^{12}c^{12} - 12*a^2*b^{11}c^{11}d + 66*a^3*b^{10}c^{10}d^2 - 220*a^4*b^9c^9d^3 + 495*a^5*b^8c^8d^4 - 792*a^6*b^7c^7d^5 + 924*a^7*b^6c^6d^6 - 792*a^8*b^5c^5d^7 + 495*a^9*b^4c^4d^8 - 220*a^{10}b^3c^3d^9 + 66*a^{11}b^2c^2d^{10} - 12*a^{12}b*c*d^{11} + a^{13}d^{12} + (b^{13}c^{12} - 12* \end{aligned}$$

$$\begin{aligned}
& a^8 b^{12} c^{11} d + 66 a^2 b^{11} c^{10} d^2 - 220 a^3 b^{10} c^9 d^3 + 495 a^4 b^9 c^8 d^4 - 792 a^5 b^8 c^7 d^5 + 924 a^6 b^7 c^6 d^6 - 792 a^7 b^6 c^5 d^7 + \\
& 495 a^8 b^5 c^4 d^8 - 220 a^9 b^4 c^3 d^9 + 66 a^{10} b^3 c^2 d^{10} - 12 a^{11} b^2 c d^{11} + a^{12} b d^{12} * x) + 28 * \text{sqrt}(3) * b^2 * ((b^{12} c^{12} - 12 a^8 b^{11} c^{11} \\
& * d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - \\
& 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{13} d^5))^{(1/6)} * \arctan(-1/3 * (2 * \text{sqrt}(3) * (b^{13} c^2 d^4 - 2 a^8 b^{12} \\
& * c d^5 + a^2 b^{11} d^6)) * (b * x + a)^{(5/6)} * (d * x + c)^{(1/6)} * ((b^{12} c^{12} - 12 a^8 b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - \\
& 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{13} d^5))^{(1/6)} - \\
& 2 * \text{sqrt}(3) * (b^{12} d^4 * x + a^8 b^{11} d^4) * \text{sqrt}(-((b^4 c^2 d - 2 a^8 b^3 c d^2 + a^2 b^2 d^3) * (b * x + a)^{(5/6)} * (d * x + c)^{(1/6)} * ((b^{12} c^{12} - 12 a^8 b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - \\
& 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{13} d^5))^{(1/6)} - \\
& (b^4 c^4 - 4 a^8 b^3 c^3 d + 6 a^2 b^2 c^2 d^2 - 4 a^3 b c^2 d^3 + a^4 d^4) * (b * x + a)^{(2/3)} * (d * x + c)^{(1/3)} - (b^5 d^2 * x + a^8 b^4 d^2) * ((b^{12} c^{12} - 12 a^8 b^{11} c^{11} d + \\
& 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - \\
& 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{13} d^5))^{(1/3)} / (b * x + a) * ((b^{12} c^{12} - 12 a^8 b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + \\
& 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{13} d^5))^{(5/6)} - \text{sqrt}(3) * (a^8 b^{12} c^{12} - 12 a^2 b^{11} c^{11} d + 66 a^3 b^{10} c^{10} d^2 - \\
& 220 a^4 b^9 c^9 d^3 + 495 a^5 b^8 c^8 d^4 - 792 a^6 b^7 c^7 d^5 + 924 a^7 b^6 c^6 d^6 - 792 a^8 b^5 c^5 d^7 + 495 a^9 b^4 c^4 d^8 - 220 a^{10} b^3 c^3 d^9 + 66 a^{11} b^2 c^2 d^{10} - 12 a^{12} b c d^{11} + \\
& a^{13} d^{12} + (b^{13} c^{12} - 12 a^8 b^{12} c^{11} d + 66 a^2 b^{11} c^{10} d^2 - 220 a^3 b^{10} c^9 d^3 + 495 a^4 b^9 c^8 d^4 - 792 a^5 b^8 c^7 d^5 + 924 a^6 b^7 c^6 d^6 - 792 a^7 b^6 c^5 d^7 + 495 a^8 b^5 c^4 d^8 - \\
& 220 a^9 b^4 c^3 d^9 + 66 a^{10} b^3 c^2 d^{10} - 12 a^{11} b^2 c d^{11} + a^{12} b d^{12}) * x) / (a^8 b^{12} c^{12} - 12 a^2 b^{11} c^{11} d + 66 a^3 b^{10} c^{10} d^2 - 220 a^4 b^9 c^9 d^3 + 495 a^5 b^8 c^8 d^4 - \\
& 792 a^6 b^7 c^7 d^5 + 924 a^7 b^6 c^6 d^6 - 792 a^8 b^5 c^5 d^7 + 495 a^9 b^4 c^4 d^8 - 220 a^{10} b^3 c^3 d^9 + 66 a^{11} b^2 c^2 d^{10} - 12 a^{12} b c d^{11} + a^{13} d^{12} + (b^{13} c^{12} - 12 a^8 b^{12} c^{11} d + \\
& 66 a^2 b^{11} c^{10} d^2 - 220 a^3 b^{10} c^9 d^3 + 495 a^4 b^9 c^8 d^4 - 792 a^5 b^8 c^7 d^5 + 924 a^6 b^7 c^6 d^6 - 792 a^7 b^6 c^5 d^7 + 495 a^8 b^5 c^4 d^8 - 220 a^9 b^4 c^3 d^9 + 66 a^{10} b^3 c^2 d^{10} - \\
& 12 a^{11} b^2 c d^{11} + a^{12} b d^{12}) * x) - 7 * b^2 * ((b^{12} c^{12} - 12 a^8 b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - \\
& 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} b d^{12}) * x) - 7 * b^2 * ((b^{12} c^{12} - 12 a^8 b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + \\
& 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} b d^{12}) * x)
\end{aligned}$$

$$\begin{aligned}
& \left(11*b*c*d^{11} + a^{12}*d^{12} \right) / \left(b^{13}*d^5 \right)^{1/6} * \log \left(49 * \left(b^4*c^2*d - 2*a*b^3*c*d^2 + a^2*b^2*d^3 \right) * (b*x + a)^{5/6} * (d*x + c)^{1/6} * \left(b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12} \right) / \left(b^{13}*d^5 \right)^{1/6} \right. \\
& + \left(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4 \right) * (b*x + a)^{2/3} * (d*x + c)^{1/3} + \left(b^5*d^2*x + a*b^4*d^2 \right) * \left(b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12} \right) / \left(b^{13}*d^5 \right)^{1/6} \left. \right) / (b*x + a) \\
& + 7*b^2 * \left(b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12} \right) / \left(b^{13}*d^5 \right)^{1/6} * \log \left(-49 * \left(b^4*c^2*d - 2*a*b^3*c*d^2 + a^2*b^2*d^3 \right) * (b*x + a)^{5/6} * (d*x + c)^{1/6} * \left(b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12} \right) / \left(b^{13}*d^5 \right)^{1/6} \right. \\
& - \left(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4 \right) * (b*x + a)^{2/3} * (d*x + c)^{1/3} - \left(b^5*d^2*x + a*b^4*d^2 \right) * \left(b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12} \right) / \left(b^{13}*d^5 \right)^{1/6} \left. \right) / (b*x + a) \\
& - 14*b^2 * \left(b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12} \right) / \left(b^{13}*d^5 \right)^{1/6} * \log \left(7 * \left(b^2*c^2 - 2*a*b*c*d + a^2*d^2 \right) * (b*x + a)^{5/6} * (d*x + c)^{1/6} + \left(b^3*d*x + a*b^2*d \right) * \left(b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12} \right) / \left(b^{13}*d^5 \right)^{1/6} \right. \\
& \left. \right) / (b*x + a) + 14*b^2 * \left(b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12} \right) / \left(b^{13}*d^5 \right)^{1/6} * \log \left(7 * \left(b^2*c^2 - 2*a*b*c*d + a^2*d^2 \right) * (b*x + a)^{5/6} * (d*x + c)^{1/6} - \left(b^3*d*x + a*b^2*d \right) * \left(b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12} \right) / \left(b^{13}*d^5 \right)^{1/6} \right. \\
& \left. \right) / (b*x + a) - 12 * \left(6*b*d*x + 13*b*c - 7*a*d \right) * (b*x + a)^{5/6} * (d*x + c)^{1/6} / b^2
\end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{7}{6}}}{(bx + a)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(7/6)/(b*x+a)^(1/6),x, algorithm="giac")

[Out] integrate((d*x + c)^(7/6)/(b*x + a)^(1/6), x)

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{7}{6}}}{(bx + a)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(7/6)/(b*x+a)^(1/6),x)

[Out] int((d*x+c)^(7/6)/(b*x+a)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{7}{6}}}{(bx + a)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(7/6)/(b*x+a)^(1/6),x, algorithm="maxima")

[Out] integrate((d*x + c)^(7/6)/(b*x + a)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{7/6}}{(a + bx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(7/6)/(a + b*x)^(1/6),x)

[Out] int((c + d*x)^(7/6)/(a + b*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{7}{6}}}{\sqrt[6]{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(7/6)/(b*x+a)**(1/6), x)

[Out] Integral((c + d*x)**(7/6)/(a + b*x)**(1/6), x)

$$3.1806 \quad \int \frac{\sqrt[6]{c+dx}}{\sqrt[6]{a+bx}} dx$$

Optimal. Leaf size=378

$$\frac{(bc - ad) \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12b^{7/6}d^{5/6}} + \frac{(bc - ad) \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12b^{7/6}d^{5/6}} + \frac{(bc - ad) \tan^{-1}\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2\sqrt[6]{b^2 d^2}}$$

[Out] $(b*x+a)^{(5/6)}*(d*x+c)^{(1/6)}/b+1/3*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(7/6)}/d^{(5/6)}-1/12*(-a*d+b*c)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(7/6)}/d^{(5/6)}+1/12*(-a*d+b*c)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(7/6)}/d^{(5/6)}-1/6*(-a*d+b*c)*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(7/6)}/d^{(5/6)}*3^{(1/2)}-1/6*(-a*d+b*c)*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(7/6)}/d^{(5/6)}*3^{(1/2)}$

Rubi [A] time = 0.56, antiderivative size = 378, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {50, 63, 331, 296, 634, 618, 204, 628, 208}

$$\frac{(bc - ad) \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12b^{7/6}d^{5/6}} + \frac{(bc - ad) \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{12b^{7/6}d^{5/6}} + \frac{(bc - ad) \tan^{-1}\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2\sqrt[6]{b^2 d^2}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/6)/(a + b*x)^(1/6), x]

[Out] $((a + b*x)^{(5/6)}*(c + d*x)^{(1/6)}/b + ((b*c - a*d)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/(2*\operatorname{Sqrt}[3]*b^{(7/6)}*d^{(5/6)}) - ((b*c - a*d)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/(2*\operatorname{Sqrt}[3]*b^{(7/6)}*d^{(5/6)}) + ((b*c - a*d)*\operatorname{ArcTanh}[(d^{(1/6)}*(a + b*x)^{(1/6)})/(b^{(1/6)}*(c + d*x)^{(1/6)})])/(3*b^{(7/6)}*d^{(5/6)}) - ((b*c - a*d)*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})])/(12*b^{(7/6)}*d^{(5/6)}) + ((b*c - a*d)*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})])/(12*b^{(7/6)}*d^{(5/6)})$

Rule 50

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(a + b*x)^(m + 1)*(c + d*x)^n/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/

$(b*(m + n + 1)), \text{Int}[(a + b*x)^m*(c + d*x)^{(n - 1)}, x], x] /;$ FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

$\text{Int}[(a_. + (b_.)*(x_.))^m*((c_.) + (d_.)*(x_.))^n, x_Symbol] :=$ With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 204

$\text{Int}[(a_. + (b_.)*(x_.)^2)^{-1}, x_Symbol] :=$ -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 208

$\text{Int}[(a_. + (b_.)*(x_.)^2)^{-1}, x_Symbol] :=$ Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rule 296

$\text{Int}[(x_.)^m/((a_.) + (b_.)*(x_.)^n), x_Symbol] :=$ Module[{r = Numerator[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r*Cos[(2*k*m*Pi)/n] - s*Cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r*Cos[(2*k*m*Pi)/n] + s*Cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^(m + 2)*Int[1/(r^2 - s^2*x^2), x])/(a*n*s^m) + Dist[(2*r^(m + 1))/(a*n*s^m), Sum[u, {k, 1, (n - 2)/4}], x], x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && IGtQ[m, 0] && LtQ[m, n - 1] && NegQ[a/b]

Rule 331

$\text{Int}[(x_.)^m*((a_.) + (b_.)*(x_.)^n)^p, x_Symbol] :=$ Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_.) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), Int[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[6]{c+dx}}{\sqrt[6]{a+bx}} dx &= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{b} + \frac{(bc-ad) \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{5/6}} dx}{6b} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{b} + \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{x^4}{\left(c - \frac{ad}{b} + \frac{dx^6}{b}\right)^{5/6}} dx, x, \sqrt[6]{a+bx} \right)}{b^2} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{b} + \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{x^4}{1 - \frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{b^2} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{b} + \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{-\frac{\sqrt[6]{b}}{3} - \frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{3b^{7/6}d^{2/3}} + \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{-\sqrt[6]{b} \sqrt[6]{d} + 2\sqrt[3]{d}x}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{12b^{7/6}d^{5/6}} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{b} + \frac{(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3b^{7/6}d^{5/6}} - \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{-\sqrt[6]{b} \sqrt[6]{d} + 2\sqrt[3]{d}x}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{12b^{7/6}d^{5/6}} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{b} + \frac{(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3b^{7/6}d^{5/6}} - \frac{(bc-ad) \log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} - \frac{\sqrt[6]{b} \sqrt[6]{d}}{\sqrt[6]{c+dx}} \right)}{12b^{7/6}d^{5/6}} \\
&= \frac{(a+bx)^{5/6} \sqrt[6]{c+dx}}{b} + \frac{(bc-ad) \tan^{-1} \left(\frac{1 - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3} b^{7/6} d^{5/6}} - \frac{(bc-ad) \tan^{-1} \left(\frac{1 + \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3} b^{7/6} d^{5/6}} + \frac{(bc-ad) \operatorname{Subst} \left(\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{5/6}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{6b}
\end{aligned}$$

Mathematica [C] time = 0.04, size = 73, normalized size = 0.19

$$\frac{6(a+bx)^{5/6} \sqrt[6]{c+dx} {}_2F_1 \left(-\frac{1}{6}, \frac{5}{6}; \frac{11}{6}; \frac{d(a+bx)}{ad-bc} \right)}{5b \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/6)/(a + b*x)^(1/6), x]

[Out] (6*(a + b*x)^(5/6)*(c + d*x)^(1/6)*Hypergeometric2F1[-1/6, 5/6, 11/6, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [B] time = 1.22, size = 3025, normalized size = 8.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(1/6),x, algorithm="fricas")

[Out]
$$\frac{1}{12} \cdot (4 \sqrt{3}) \cdot b \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{1/6} \cdot \arctan\left(\frac{1}{3} \cdot (2 \sqrt{3}) \cdot (b^7 c d^4 - a b^6 d^5) \cdot (b x + a)^{5/6} \cdot (d x + c)^{1/6}\right) \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{5/6} + 2 \sqrt{3} \cdot (b^7 d^4 x + a b^6 d^4) \cdot \sqrt{((b^2 c d - a b d^2) \cdot (b x + a)^{5/6} \cdot (d x + c)^{1/6}) \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{1/6}} + (b^2 c^2 - 2 a b c d + a^2 d^2) \cdot (b x + a)^{2/3} \cdot (d x + c)^{1/3} + (b^3 d^2 x + a b^2 d^2) \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{1/3} / (b x + a) \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{5/6} + \sqrt{3} \cdot (a b^6 c^6 - 6 a^2 b^5 c^5 d + 15 a^3 b^4 c^4 d^2 - 20 a^4 b^3 c^3 d^3 + 15 a^5 b^2 c^2 d^4 - 6 a^6 b c d^5 + a^7 d^6 + (b^7 c^6 - 6 a b^6 c^5 d + 15 a^2 b^5 c^4 d^2 - 20 a^3 b^4 c^3 d^3 + 15 a^4 b^3 c^2 d^4 - 6 a^5 b^2 c d^5 + a^6 b d^6) \cdot x) / (a b^6 c^6 - 6 a^2 b^5 c^5 d + 15 a^3 b^4 c^4 d^2 - 20 a^4 b^3 c^3 d^3 + 15 a^5 b^2 c^2 d^4 - 6 a^6 b c d^5 + a^7 d^6 + (b^7 c^6 - 6 a b^6 c^5 d + 15 a^2 b^5 c^4 d^2 - 20 a^3 b^4 c^3 d^3 + 15 a^4 b^3 c^2 d^4 - 6 a^5 b^2 c d^5 + a^6 b d^6) \cdot x)) + 4 \sqrt{3} \cdot b \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{1/6} \cdot \arctan\left(\frac{1}{3} \cdot (2 \sqrt{3}) \cdot (b^7 c d^4 - a b^6 d^5) \cdot (b x + a)^{5/6} \cdot (d x + c)^{1/6}\right) \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{5/6} + 2 \sqrt{3} \cdot (b^7 d^4 x + a b^6 d^4) \cdot \sqrt{-((b^2 c d - a b d^2) \cdot (b x + a)^{5/6} \cdot (d x + c)^{1/6}) \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{1/6}} - (b^2 c^2 - 2 a b c d + a^2 d^2) \cdot (b x + a)^{2/3} \cdot (d x + c)^{1/3} - (b^3 d^2 x + a b^2 d^2) \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{1/3} / (b x + a) \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{5/6} - \sqrt{3} \cdot (a b^6 c^6 - 6 a^2 b^5 c^5 d + 15 a^3 b^4 c^4 d^2 - 20 a^4 b^3 c^3 d^3 + 15 a^5 b^2 c^2 d^4 - 6 a^6 b c d^5 + a^7 d^6 + (b^7 c^6 - 6 a b^6 c^5 d + 15 a^2 b^5 c^4 d^2 - 20 a^3 b^4 c^3 d^3 + 15 a^4 b^3 c^2 d^4 - 6 a^5 b^2 c d^5 + a^6 b d^6) \cdot x) / (a b^6 c^6 - 6 a^2 b^5 c^5 d + 15 a^3 b^4 c^4 d^2 - 20 a^4 b^3 c^3 d^3 + 15 a^5 b^2 c^2 d^4 - 6 a^6 b c d^5 + a^7 d^6 + (b^7 c^6 - 6 a b^6 c^5 d + 15 a^2 b^5 c^4 d^2 - 20 a^3 b^4 c^3 d^3 + 15 a^4 b^3 c^2 d^4 - 6 a^5 b^2 c d^5 + a^6 b d^6) \cdot x)) + b \cdot ((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5))^{1/6} \cdot \log(((b^2 c d - a b d^2) \cdot (b x +$$

$$\begin{aligned}
& a^{5/6} (dx + c)^{1/6} \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5) \right)^{1/6} \\
& + (b^2 c^2 - 2 a b c d + a^2 d^2) (b x + a)^{2/3} (dx + c)^{1/3} \\
& + (b^3 d^2 x + a b^2 d^2) \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5) \right)^{1/3} \\
&) / (b x + a) - b \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5) \right)^{1/6} \\
& * \log \left(- \left((b^2 c d - a b d^2) (b x + a)^{5/6} (dx + c)^{1/6} \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5) \right)^{1/6} \right. \right. \\
& \left. \left. - (b^2 c^2 - 2 a b c d + a^2 d^2) (b x + a)^{2/3} (dx + c)^{1/3} - (b^3 d^2 x + a b^2 d^2) \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5) \right)^{1/3} \right) / (b x + a) \right) \\
& + 2 b \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5) \right)^{1/6} \\
& * \log \left(- \left((b c - a d) (b x + a)^{5/6} (dx + c)^{1/6} + (b^2 d x + a b d) \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5) \right)^{1/6} \right) / (b x + a) \right) \\
& - 2 b \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5) \right)^{1/6} \\
& * \log \left(- \left((b c - a d) (b x + a)^{5/6} (dx + c)^{1/6} - (b^2 d x + a b d) \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^7 d^5) \right)^{1/6} \right) / (b x + a) \right) \\
& + 12 (b x + a)^{5/6} (dx + c)^{1/6} / b
\end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((dx+c)^(1/6)/(bx+a)^(1/6),x, algorithm="giac")

[Out] integrate((dx + c)^(1/6)/(bx + a)^(1/6), x)

maple [F] time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((dx+c)^(1/6)/(bx+a)^(1/6),x)

[Out] int((dx+c)^(1/6)/(bx+a)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(1/6),x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/6)/(b*x + a)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/6}}{(a + bx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/6)/(a + b*x)^(1/6),x)

[Out] int((c + d*x)^(1/6)/(a + b*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{c + dx}}{\sqrt[6]{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/6)/(b*x+a)**(1/6),x)

[Out] Integral((c + d*x)**(1/6)/(a + b*x)**(1/6), x)

$$3.1807 \quad \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{5/6}} dx$$

Optimal. Leaf size=309

$$\frac{\log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2\sqrt[6]{b} d^{5/6}} + \frac{\log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2\sqrt[6]{b} d^{5/6}} + \frac{\sqrt{3} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt{3} \sqrt[6]{b} \sqrt[6]{c+dx}}\right)}{\sqrt[6]{b} d^{5/6}}$$

[Out] $2*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(1/6)}/d^{(5/6)}-1/2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(1/6)}/d^{(5/6)}+1/2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(1/6)}/d^{(5/6)}-\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})*3^{(1/2)}/b^{(1/6)}/d^{(5/6)}-\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})*3^{(1/2)}/b^{(1/6)}/d^{(5/6)}$

Rubi [A] time = 0.51, antiderivative size = 309, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {63, 331, 296, 634, 618, 204, 628, 208}

$$\frac{\log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2\sqrt[6]{b} d^{5/6}} + \frac{\log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2\sqrt[6]{b} d^{5/6}} + \frac{\sqrt{3} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt{3} \sqrt[6]{b} \sqrt[6]{c+dx}}\right)}{\sqrt[6]{b} d^{5/6}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a + b*x)^{(1/6)}*(c + d*x)^{(5/6))}, x]$

[Out] $(\operatorname{Sqrt}[3]*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/b^{(1/6)}*d^{(5/6)} - (\operatorname{Sqrt}[3]*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/b^{(1/6)}*d^{(5/6)} + (2*\operatorname{ArcTan}[(d^{(1/6)}*(a + b*x)^{(1/6)})/b^{(1/6)}*(c + d*x)^{(1/6)}])/b^{(1/6)}*d^{(5/6)} - \operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)}]/(2*b^{(1/6)}*d^{(5/6)}) + \operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)}]/(2*b^{(1/6)}*d^{(5/6)})]$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_)}*((c_.) + (d_.)*(x_))^{(n_)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m+1)-1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{(1/p)}, x]] /; \operatorname{FreeQ}[\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rule 296

```
Int[(x_)^(m_.)/((a_) + (b_.)*(x_)^(n_)), x_Symbol] := Module[{r = Numerator[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r*Cos[(2*k*m*Pi)/n] - s*Cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r*Cos[(2*k*m*Pi)/n] + s*Cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^(m + 2)*Int[1/(r^2 - s^2*x^2), x])/(a*n*s^m) + Dist[(2*r^(m + 1))/(a*n*s^m), Sum[u, {k, 1, (n - 2)/4}], x, x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && IGtQ[m, 0] && LtQ[m, n - 1] && NegQ[a/b]
```

Rule 331

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_.) + (e_.)*(x_))/((a_) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), In
```

t[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ
 [2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{5/6}} dx &= \frac{6 \operatorname{Subst}\left(\int \frac{x^4}{\left(c-\frac{ad}{b}+\frac{dx^6}{b}\right)^{5/6}} dx, x, \sqrt[6]{a+bx}\right)}{b} \\
 &= \frac{6 \operatorname{Subst}\left(\int \frac{x^4}{1-\frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}\right)}{b} \\
 &= \frac{2 \operatorname{Subst}\left(\int \frac{1}{\sqrt[3]{b}-\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}\right)}{d^{2/3}} + \frac{2 \operatorname{Subst}\left(\int \frac{-\frac{\sqrt[6]{b}}{2}-\frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b}-\sqrt[6]{b}\sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}\right)}{\sqrt[6]{b}d^{2/3}} + \dots \\
 &= \frac{2 \tanh^{-1}\left(\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}\right)}{\sqrt[6]{b}d^{5/6}} - \frac{\operatorname{Subst}\left(\int \frac{-\sqrt[6]{b}\sqrt[6]{d}+2\sqrt[3]{d}x}{\sqrt[3]{b}-\sqrt[6]{b}\sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}\right)}{2\sqrt[6]{b}d^{5/6}} + \frac{\operatorname{Subst}\left(\int \frac{\sqrt[6]{b}}{\sqrt[3]{b}+\sqrt[6]{b}\sqrt[6]{d}x} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}\right)}{\sqrt[6]{b}d^{5/6}} \\
 &= \frac{2 \tanh^{-1}\left(\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}\right)}{\sqrt[6]{b}d^{5/6}} - \frac{\log\left(\sqrt[3]{b} + \frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}} - \frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}\right)}{2\sqrt[6]{b}d^{5/6}} + \frac{\log\left(\sqrt[3]{b} + \frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}\right)}{2\sqrt[6]{b}d^{5/6}} \\
 &= \frac{\sqrt{3} \tan^{-1}\left(\frac{1-2\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}}{\sqrt{3}}\right)}{\sqrt[6]{b}d^{5/6}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{1+2\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}}{\sqrt{3}}\right)}{\sqrt[6]{b}d^{5/6}} + \frac{2 \tanh^{-1}\left(\frac{\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}\right)}{\sqrt[6]{b}d^{5/6}} - \frac{\log\left(\sqrt[3]{b} + \frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[6]{b}\sqrt[6]{c+dx}}\right)}{\sqrt[6]{b}d^{5/6}}
 \end{aligned}$$

Mathematica [C] time = 0.05, size = 73, normalized size = 0.24

$$\frac{6(a+bx)^{5/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{5}{6}, \frac{5}{6}; \frac{11}{6}; \frac{d(a+bx)}{ad-bc}\right)}{5b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/6)*(c + d*x)^(5/6)), x]

[Out] (6*(a + b*x)^(5/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[5/6, 5/6, 11/6, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(c + d*x)^(5/6))

fricas [B] time = 1.08, size = 620, normalized size = 2.01

$$-2\sqrt{3}\left(\frac{1}{bd^5}\right)^{\frac{1}{6}}\arctan\left(-\frac{2\sqrt{3}(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{1}{6}}bd^4\left(\frac{1}{bd^5}\right)^{\frac{5}{6}}-2\sqrt{3}(b^2d^4x+abd^4)\sqrt{\frac{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{1}{6}}d\left(\frac{1}{bd^5}\right)^{\frac{1}{6}}+(bd^2x+ad^2)}{bx+a}}}{3(bx+a)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(5/6),x, algorithm="fricas")

[Out] $-2*\sqrt{3}*(1/(b*d^5))^{(1/6)}*\arctan(-1/3*(2*\sqrt{3}*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*b*d^4*(1/(b*d^5))^{(5/6)} - 2*\sqrt{3}*(b^2*d^4*x + a*b*d^4)*\sqrt{((b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*d*(1/(b*d^5))^{(1/6)} + (b*d^2*x + a*d^2)*(1/(b*d^5))^{(1/3)} + (b*x + a)^{(2/3)}*(d*x + c)^{(1/3)})/(b*x + a)}*(1/(b*d^5))^{(5/6)} + \sqrt{3}*(b*x + a))/(b*x + a) - 2*\sqrt{3}*(1/(b*d^5))^{(1/6)}*\arctan(-1/3*(2*\sqrt{3}*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*b*d^4*(1/(b*d^5))^{(5/6)} - 2*\sqrt{3}*(b^2*d^4*x + a*b*d^4)*\sqrt{-((b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*d*(1/(b*d^5))^{(1/6)} - (b*d^2*x + a*d^2)*(1/(b*d^5))^{(1/3)} - (b*x + a)^{(2/3)}*(d*x + c)^{(1/3)})/(b*x + a)}*(1/(b*d^5))^{(5/6)} - \sqrt{3}*(b*x + a))/(b*x + a) + 1/2*(1/(b*d^5))^{(1/6)}*\log(4*((b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*d*(1/(b*d^5))^{(1/6)} + (b*d^2*x + a*d^2)*(1/(b*d^5))^{(1/3)} + (b*x + a)^{(2/3)}*(d*x + c)^{(1/3)})/(b*x + a) - 1/2*(1/(b*d^5))^{(1/6)}*\log(-4*((b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*d*(1/(b*d^5))^{(1/6)} - (b*d^2*x + a*d^2)*(1/(b*d^5))^{(1/3)} - (b*x + a)^{(2/3)}*(d*x + c)^{(1/3)})/(b*x + a) + (1/(b*d^5))^{(1/6)}*\log(((b*d*x + a*d)*(1/(b*d^5))^{(1/6)} + (b*x + a)^{(5/6)}*(d*x + c)^{(1/6)})/(b*x + a) - (1/(b*d^5))^{(1/6)}*\log(-((b*d*x + a*d)*(1/(b*d^5))^{(1/6)} - (b*x + a)^{(5/6)}*(d*x + c)^{(1/6)})/(b*x + a))$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(5/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(5/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(1/6)/(d*x+c)^(5/6),x)`

[Out] `int(1/(b*x+a)^(1/6)/(d*x+c)^(5/6),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(1/6)/(d*x+c)^(5/6),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(1/6)*(d*x + c)^(5/6)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{1/6}(c+dx)^{5/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(1/6)*(c + d*x)^(5/6)),x)`

[Out] `int(1/((a + b*x)^(1/6)*(c + d*x)^(5/6)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/6)/(d*x+c)**(5/6),x)`

[Out] `Integral(1/((a + b*x)**(1/6)*(c + d*x)**(5/6)), x)`

$$3.1808 \quad \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{11/6}} dx$$

Optimal. Leaf size=32

$$\frac{6(a+bx)^{5/6}}{5(c+dx)^{5/6}(bc-ad)}$$

[Out] 6/5*(b*x+a)^(5/6)/(-a*d+b*c)/(d*x+c)^(5/6)

Rubi [A] time = 0.00, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{6(a+bx)^{5/6}}{5(c+dx)^{5/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/6)*(c + d*x)^(11/6)),x]

[Out] (6*(a + b*x)^(5/6))/(5*(b*c - a*d)*(c + d*x)^(5/6))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{11/6}} dx = \frac{6(a+bx)^{5/6}}{5(bc-ad)(c+dx)^{5/6}}$$

Mathematica [A] time = 0.01, size = 32, normalized size = 1.00

$$\frac{6(a+bx)^{5/6}}{5(c+dx)^{5/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/6)*(c + d*x)^(11/6)),x]

[Out] (6*(a + b*x)^(5/6))/(5*(b*c - a*d)*(c + d*x)^(5/6))

fricas [A] time = 0.98, size = 42, normalized size = 1.31

$$\frac{6 (bx + a)^{\frac{5}{6}} (dx + c)^{\frac{1}{6}}}{5 (bc^2 - acd + (bcd - ad^2)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(11/6),x, algorithm="fricas")

[Out] 6/5*(b*x + a)^(5/6)*(d*x + c)^(1/6)/(b*c^2 - a*c*d + (b*c*d - a*d^2)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{6}} (dx + c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(11/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(11/6)), x)

maple [A] time = 0.00, size = 27, normalized size = 0.84

$$-\frac{6 (bx + a)^{\frac{5}{6}}}{5 (dx + c)^{\frac{5}{6}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/6)/(d*x+c)^(11/6),x)

[Out] -6/5*(b*x+a)^(5/6)/(d*x+c)^(5/6)/(a*d-b*c)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{6}} (dx + c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(11/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(11/6)), x)

mupad [B] time = 0.76, size = 27, normalized size = 0.84

$$-\frac{6(a+bx)^{5/6}}{(5ad-5bc)(c+dx)^{5/6}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(1/6)*(c + d*x)^(11/6)),x)`

[Out] `-(6*(a + b*x)^(5/6))/((5*a*d - 5*b*c)*(c + d*x)^(5/6))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/6)/(d*x+c)**(11/6),x)`

[Out] `Integral(1/((a + b*x)**(1/6)*(c + d*x)**(11/6)), x)`

$$3.1809 \quad \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{17/6}} dx$$

Optimal. Leaf size=66

$$\frac{36b(a+bx)^{5/6}}{55(c+dx)^{5/6}(bc-ad)^2} + \frac{6(a+bx)^{5/6}}{11(c+dx)^{11/6}(bc-ad)}$$

[Out] $6/11*(b*x+a)^{(5/6)/(-a*d+b*c)/(d*x+c)^{(11/6)+36/55*b*(b*x+a)^{(5/6)/(-a*d+b*c)^2/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{36b(a+bx)^{5/6}}{55(c+dx)^{5/6}(bc-ad)^2} + \frac{6(a+bx)^{5/6}}{11(c+dx)^{11/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/6)*(c + d*x)^(17/6)), x]

[Out] $(6*(a + b*x)^{(5/6)}/(11*(b*c - a*d)*(c + d*x)^{(11/6)} + (36*b*(a + b*x)^{(5/6)}/(55*(b*c - a*d)^2*(c + d*x)^{(5/6))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[m] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{17/6}} dx = \frac{6(a+bx)^{5/6}}{11(bc-ad)(c+dx)^{11/6}} + \frac{(6b) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{11/6}} dx}{11(bc-ad)}$$

$$= \frac{6(a+bx)^{5/6}}{11(bc-ad)(c+dx)^{11/6}} + \frac{36b(a+bx)^{5/6}}{55(bc-ad)^2(c+dx)^{5/6}}$$

Mathematica [A] time = 0.03, size = 46, normalized size = 0.70

$$\frac{6(a+bx)^{5/6}(-5ad+11bc+6bdx)}{55(c+dx)^{11/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/6)*(c + d*x)^(17/6)), x]

[Out] (6*(a + b*x)^(5/6)*(11*b*c - 5*a*d + 6*b*d*x))/(55*(b*c - a*d)^2*(c + d*x)^(11/6))

fricas [B] time = 0.91, size = 118, normalized size = 1.79

$$\frac{6(6bdx + 11bc - 5ad)(bx + a)^{5/6}(dx + c)^{1/6}}{55(b^2c^4 - 2abc^3d + a^2c^2d^2 + (b^2c^2d^2 - 2abcd^3 + a^2d^4)x^2 + 2(b^2c^3d - 2abc^2d^2 + a^2cd^3)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(17/6), x, algorithm="fricas")

[Out] 6/55*(6*b*d*x + 11*b*c - 5*a*d)*(b*x + a)^(5/6)*(d*x + c)^(1/6)/(b^2*c^4 - 2*a*b*c^3*d + a^2*c^2*d^2 + (b^2*c^2*d^2 - 2*a*b*c*d^3 + a^2*d^4)*x^2 + 2*(b^2*c^3*d - 2*a*b*c^2*d^2 + a^2*c*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{1/6}(dx+c)^{17/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(17/6), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(17/6)), x)

maple [A] time = 0.00, size = 54, normalized size = 0.82

$$\frac{6(bx+a)^{\frac{5}{6}}(-6bdx+5ad-11bc)}{55(dx+c)^{\frac{11}{6}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/6)/(d*x+c)^(17/6),x)

[Out] -6/55*(b*x+a)^(5/6)*(-6*b*d*x+5*a*d-11*b*c)/(d*x+c)^(11/6)/(a^2*d^2-2*a*b*c*d+b^2*c^2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(17/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(17/6)), x)

mupad [B] time = 0.86, size = 127, normalized size = 1.92

$$\frac{(c+dx)^{1/6} \left(\frac{x(66cb^2+6adb)}{55d^2(ad-bc)^2} - \frac{30a^2d-66abc}{55d^2(ad-bc)^2} + \frac{36b^2x^2}{55d(ad-bc)^2} \right)}{x^2(a+bx)^{1/6} + \frac{c^2(a+bx)^{1/6}}{d^2} + \frac{2cx(a+bx)^{1/6}}{d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a+b*x)^(1/6)*(c+d*x)^(17/6)),x)

[Out] ((c+d*x)^(1/6)*((x*(66*b^2*c+6*a*b*d))/(55*d^2*(a*d-b*c)^2) - (30*a^2*d-66*a*b*c)/(55*d^2*(a*d-b*c)^2) + (36*b^2*x^2)/(55*d*(a*d-b*c)^2)) / (x^2*(a+b*x)^(1/6) + (c^2*(a+b*x)^(1/6))/d^2 + (2*c*x*(a+b*x)^(1/6))/d)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/6)/(d*x+c)**(17/6),x)

[Out] Timed out

$$3.1810 \quad \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{23/6}} dx$$

Optimal. Leaf size=101

$$\frac{432b^2(a+bx)^{5/6}}{935(c+dx)^{5/6}(bc-ad)^3} + \frac{72b(a+bx)^{5/6}}{187(c+dx)^{11/6}(bc-ad)^2} + \frac{6(a+bx)^{5/6}}{17(c+dx)^{17/6}(bc-ad)}$$

[Out] $6/17*(b*x+a)^{(5/6)/(-a*d+b*c)/(d*x+c)^{(17/6)}+72/187*b*(b*x+a)^{(5/6)/(-a*d+b*c)^2/(d*x+c)^{(11/6)}+432/935*b^2*(b*x+a)^{(5/6)/(-a*d+b*c)^3/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{432b^2(a+bx)^{5/6}}{935(c+dx)^{5/6}(bc-ad)^3} + \frac{72b(a+bx)^{5/6}}{187(c+dx)^{11/6}(bc-ad)^2} + \frac{6(a+bx)^{5/6}}{17(c+dx)^{17/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/6)*(c + d*x)^(23/6)),x]

[Out] $(6*(a + b*x)^{(5/6)})/(17*(b*c - a*d)*(c + d*x)^{(17/6)}) + (72*b*(a + b*x)^{(5/6)})/(187*(b*c - a*d)^2*(c + d*x)^{(11/6)}) + (432*b^2*(a + b*x)^{(5/6)})/(935*(b*c - a*d)^3*(c + d*x)^{(5/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{23/6}} dx &= \frac{6(a+bx)^{5/6}}{17(bc-ad)(c+dx)^{17/6}} + \frac{(12b) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{17/6}} dx}{17(bc-ad)} \\
&= \frac{6(a+bx)^{5/6}}{17(bc-ad)(c+dx)^{17/6}} + \frac{72b(a+bx)^{5/6}}{187(bc-ad)^2(c+dx)^{11/6}} + \frac{(72b^2) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{11/6}} dx}{187(bc-ad)^2} \\
&= \frac{6(a+bx)^{5/6}}{17(bc-ad)(c+dx)^{17/6}} + \frac{72b(a+bx)^{5/6}}{187(bc-ad)^2(c+dx)^{11/6}} + \frac{432b^2(a+bx)^{5/6}}{935(bc-ad)^3(c+dx)^{5/6}}
\end{aligned}$$

Mathematica [A] time = 0.05, size = 77, normalized size = 0.76

$$\frac{6(a+bx)^{5/6} (55a^2d^2 - 10abd(17c+6dx) + b^2(187c^2 + 204cdx + 72d^2x^2))}{935(c+dx)^{17/6}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/6)*(c + d*x)^(23/6)), x]

[Out] (6*(a + b*x)^(5/6)*(55*a^2*d^2 - 10*a*b*d*(17*c + 6*d*x) + b^2*(187*c^2 + 204*c*d*x + 72*d^2*x^2))/(935*(b*c - a*d)^3*(c + d*x)^(17/6))

fricas [B] time = 0.83, size = 252, normalized size = 2.50

$$\frac{6(72b^2d^2x^2 + 187b^2c^2 - 170abcd + 55a^2d^2 + 12(17b^2cd - 5abcd))}{935(b^3c^6 - 3ab^2c^5d + 3a^2bc^4d^2 - a^3c^3d^3 + (b^3c^3d^3 - 3ab^2c^2d^4 + 3a^2bcd^5 - a^3d^6)x^3 + 3(b^3c^4d^2 - 3ab^2c^3d^3 + 3a^2bc^2d^4 - a^3c^2d^5)x^2 + 3(b^3c^5d - 3a^2b^2c^4d^2 + 3a^2b^2c^3d^3 - a^3c^2d^4)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(23/6), x, algorithm="fricas")

[Out] 6/935*(72*b^2*d^2*x^2 + 187*b^2*c^2 - 170*a*b*c*d + 55*a^2*d^2 + 12*(17*b^2*c*d - 5*a*b*d^2)*x)*(b*x + a)^(5/6)*(d*x + c)^(1/6)/(b^3*c^6 - 3*a*b^2*c^5*d + 3*a^2*b*c^4*d^2 - a^3*c^3*d^3 + (b^3*c^3*d^3 - 3*a*b^2*c^2*d^4 + 3*a^2*b*c*d^5 - a^3*d^6)*x^3 + 3*(b^3*c^4*d^2 - 3*a*b^2*c^3*d^3 + 3*a^2*b*c^2*d^4 - a^3*c*d^5)*x^2 + 3*(b^3*c^5*d - 3*a*b^2*c^4*d^2 + 3*a^2*b*c^3*d^3 - a^3*c^2*d^4)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{23}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(23/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(23/6)), x)

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{6 (bx + a)^{\frac{5}{6}} (72b^2x^2d^2 - 60abd^2x + 204b^2cdx + 55a^2d^2 - 170abcd + 187b^2c^2)}{935 (dx + c)^{\frac{17}{6}} (a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/6)/(d*x+c)^(23/6),x)

[Out] -6/935*(b*x+a)^(5/6)*(72*b^2*d^2*x^2-60*a*b*d^2*x+204*b^2*c*d*x+55*a^2*d^2-170*a*b*c*d+187*b^2*c^2)/(d*x+c)^(17/6)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{6}}(dx + c)^{\frac{23}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(23/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(23/6)), x)

mupad [B] time = 1.03, size = 203, normalized size = 2.01

$$\frac{(c + dx)^{1/6} \left(\frac{330a^3d^2 - 1020a^2bcd + 1122ab^2c^2}{935d^3(ad-bc)^3} + \frac{x(-30a^2bd^2 + 204ab^2cd + 1122b^3c^2)}{935d^3(ad-bc)^3} + \frac{432b^3x^3}{935d(ad-bc)^3} + \frac{72b^2x^2(ad+17bc)}{935d^2(ad-bc)^3} \right)}{x^3(a+bx)^{1/6} + \frac{c^3(a+bx)^{1/6}}{d^3} + \frac{3cx^2(a+bx)^{1/6}}{d} + \frac{3c^2x(a+bx)^{1/6}}{d^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/6)*(c + d*x)^(23/6)),x)

[Out] -((c + d*x)^(1/6)*((330*a^3*d^2 + 1122*a*b^2*c^2 - 1020*a^2*b*c*d)/(935*d^3*(a*d - b*c)^3) + (x*(1122*b^3*c^2 - 30*a^2*b*d^2 + 204*a*b^2*c*d))/(935*d^3*(a*d - b*c)^3) + (432*b^3*x^3)/(935*d*(a*d - b*c)^3) + (72*b^2*x^2*(a*d + 17*b*c))/(935*d^2*(a*d - b*c)^3))/(x^3*(a + b*x)^(1/6) + (c^3*(a + b*x)^(1/6))/d^3 + (3*c*x^2*(a + b*x)^(1/6))/d + (3*c^2*x*(a + b*x)^(1/6))/d^2)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/6)/(d*x+c)**(23/6), x)

[Out] Timed out

$$3.1811 \quad \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{29/6}} dx$$

Optimal. Leaf size=136

$$\frac{7776b^3(a+bx)^{5/6}}{21505(c+dx)^{5/6}(bc-ad)^4} + \frac{1296b^2(a+bx)^{5/6}}{4301(c+dx)^{11/6}(bc-ad)^3} + \frac{108b(a+bx)^{5/6}}{391(c+dx)^{17/6}(bc-ad)^2} + \frac{6(a+bx)^{5/6}}{23(c+dx)^{23/6}(bc-ad)}$$

[Out] $6/23*(b*x+a)^{(5/6)/(-a*d+b*c)/(d*x+c)^{(23/6)+108/391*b*(b*x+a)^{(5/6)/(-a*d+b*c)^2/(d*x+c)^{(17/6)+1296/4301*b^2*(b*x+a)^{(5/6)/(-a*d+b*c)^3/(d*x+c)^{(11/6)+7776/21505*b^3*(b*x+a)^{(5/6)/(-a*d+b*c)^4/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{7776b^3(a+bx)^{5/6}}{21505(c+dx)^{5/6}(bc-ad)^4} + \frac{1296b^2(a+bx)^{5/6}}{4301(c+dx)^{11/6}(bc-ad)^3} + \frac{108b(a+bx)^{5/6}}{391(c+dx)^{17/6}(bc-ad)^2} + \frac{6(a+bx)^{5/6}}{23(c+dx)^{23/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/6)*(c + d*x)^(29/6)), x]

[Out] $(6*(a + b*x)^{(5/6)})/(23*(b*c - a*d)*(c + d*x)^{(23/6)}) + (108*b*(a + b*x)^{(5/6)})/(391*(b*c - a*d)^2*(c + d*x)^{(17/6)}) + (1296*b^2*(a + b*x)^{(5/6)})/(4301*(b*c - a*d)^3*(c + d*x)^{(11/6)}) + (7776*b^3*(a + b*x)^{(5/6)})/(21505*(b*c - a*d)^4*(c + d*x)^{(5/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{29/6}} dx &= \frac{6(a+bx)^{5/6}}{23(bc-ad)(c+dx)^{23/6}} + \frac{(18b) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{23/6}} dx}{23(bc-ad)} \\
&= \frac{6(a+bx)^{5/6}}{23(bc-ad)(c+dx)^{23/6}} + \frac{108b(a+bx)^{5/6}}{391(bc-ad)^2(c+dx)^{17/6}} + \frac{(216b^2) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{17/6}} dx}{391(bc-ad)^2} \\
&= \frac{6(a+bx)^{5/6}}{23(bc-ad)(c+dx)^{23/6}} + \frac{108b(a+bx)^{5/6}}{391(bc-ad)^2(c+dx)^{17/6}} + \frac{1296b^2(a+bx)^{5/6}}{4301(bc-ad)^3(c+dx)^{11/6}} + \dots \\
&= \frac{6(a+bx)^{5/6}}{23(bc-ad)(c+dx)^{23/6}} + \frac{108b(a+bx)^{5/6}}{391(bc-ad)^2(c+dx)^{17/6}} + \frac{1296b^2(a+bx)^{5/6}}{4301(bc-ad)^3(c+dx)^{11/6}} + \dots
\end{aligned}$$

Mathematica [A] time = 0.07, size = 118, normalized size = 0.87

$$\frac{6(a+bx)^{5/6} \left(-935a^3d^3 + 165a^2bd^2(23c+6dx) - 15ab^2d(391c^2 + 276cdx + 72d^2x^2) \right) + b^3(4301c^3 + 7038c^2dx + 4968cd^2x^2 + 1296d^3x^3)}{21505(c+dx)^{23/6}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/6)*(c + d*x)^(29/6)),x]

[Out] (6*(a + b*x)^(5/6)*(-935*a^3*d^3 + 165*a^2*b*d^2*(23*c + 6*d*x) - 15*a*b^2*d*(391*c^2 + 276*c*d*x + 72*d^2*x^2) + b^3*(4301*c^3 + 7038*c^2*d*x + 4968*c*d^2*x^2 + 1296*d^3*x^3)))/(21505*(b*c - a*d)^4*(c + d*x)^(23/6))

fricas [B] time = 0.99, size = 420, normalized size = 3.09

$$\frac{6(1296b^3d^3x^3 + 4301b^3c^3 - 5865ab^2c^2d + 3795a^2b^2c^2d^2 - 935a^3d^3 + 216(23b^3c^2d^2 - 5a^2b^2d^3)x^2 + 18(391b^3c^2d - 230a^2b^2c^2d^2 + 55a^2b^2d^3)x)(b^4c^4d^4 - 4ab^3c^3d^5 + 6a^2b^2c^2d^6 - 4a^3bcd^7 + a^4d^8)}{21505(b^4c^8 - 4ab^3c^7d + 6a^2b^2c^6d^2 - 4a^3bc^5d^3 + a^4c^4d^4 + (b^4c^4d^4 - 4ab^3c^3d^5 + 6a^2b^2c^2d^6 - 4a^3bcd^7 + a^4d^8))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(29/6),x, algorithm="fricas")

[Out] 6/21505*(1296*b^3*d^3*x^3 + 4301*b^3*c^3 - 5865*a*b^2*c^2*d + 3795*a^2*b^2*c^2*d^2 - 935*a^3*d^3 + 216*(23*b^3*c^2*d^2 - 5*a^2*b^2*d^3)*x^2 + 18*(391*b^3*c^2*d - 230*a^2*b^2*c^2*d^2 + 55*a^2*b^2*d^3)*x)*(b*x + a)^(5/6)*(d*x + c)^(1/6)/(b^4*c^4*d^4 - 4*a*b^3*c^3*d^5 + 6*a^2*b^2*c^2*d^6 - 4*a^3*b*c*d^7 + a^4*d^8)*x^4 + 4*(b^4*c^5*d^3 - 4*a*b^3*c^4*d^4 + 6*a^2*b^2*c^3*d^5 - 4*a^3*b*c^2*d^6 + a^4*c*d^7)*x^3 + 6*(b^4*c^6*d^2 - 4*a*b^3*c^5*d^3 + 6*a^2*b^2*c^4*d^4 - 4*a^3*b*c^3*d^5 + 6*a^2*b^2*c^2*d^6 - 4*a^3*b*c*d^7 + a^4*d^8)*x^2 + 18*(391*b^3*c^2*d - 230*a^2*b^2*c^2*d^2 + 55*a^2*b^2*d^3)*x + 6*(1296*b^3*d^3*x^3 + 4301*b^3*c^3 - 5865*a*b^2*c^2*d + 3795*a^2*b^2*c^2*d^2 - 935*a^3*d^3)

$$4 - 4*a^3*b*c^3*d^5 + a^4*c^2*d^6)*x^2 + 4*(b^4*c^7*d - 4*a*b^3*c^6*d^2 + 6*a^2*b^2*c^5*d^3 - 4*a^3*b*c^4*d^4 + a^4*c^3*d^5)*x)$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{29}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(29/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(29/6)), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{6(bx+a)^{\frac{5}{6}}(-1296b^3d^3x^3 + 1080ab^2d^3x^2 - 4968b^3cd^2x^2 - 990a^2bd^3x + 4140ab^2cd^2x - 7038b^3c^2dx + 935a^3d^3)}{21505(dx+c)^{\frac{23}{6}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/6)/(d*x+c)^(29/6),x)

[Out] -6/21505*(b*x+a)^(5/6)*(-1296*b^3*d^3*x^3+1080*a*b^2*d^3*x^2-4968*b^3*c*d^2*x^2-990*a^2*b*d^3*x+4140*a*b^2*c*d^2*x-7038*b^3*c^2*d*x+935*a^3*d^3-3795*a^2*b*c*d^2+5865*a*b^2*c^2*d-4301*b^3*c^3)/(d*x+c)^(23/6)/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{29}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(29/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(29/6)), x)

mupad [B] time = 1.20, size = 292, normalized size = 2.15

$$(c+dx)^{1/6} \left(\frac{7776b^4x^4}{21505d(ad-bc)^4} - \frac{5610a^4d^3-22770a^3bcd^2+35190a^2b^2c^2d-25806ab^3c^3}{21505d^4(ad-bc)^4} + \frac{x(330a^3bd^3-2070a^2b^2cd^2+7038ab^3c^2d+25806ab^3c^2d+25806ab^3c^2d)}{21505d^4(ad-bc)^4} \right) \\ x^4(a+bx)^{1/6} + \frac{c^4(a+bx)^{1/6}}{d^4} + \frac{6c^2x^2(a+bx)^{1/6}}{d^2} + \frac{4cx^3(a+bx)^{1/6}}{d} + \frac{4c^3x^4(a+bx)^{1/6}}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(1/6)*(c + d*x)^(29/6)),x)`

[Out] $((c + d*x)^{(1/6)} * ((7776*b^4*x^4)/(21505*d*(a*d - b*c)^4) - (5610*a^4*d^3 - 25806*a*b^3*c^3 + 35190*a^2*b^2*c^2*d - 22770*a^3*b*c*d^2)/(21505*d^4*(a*d - b*c)^4) + (x*(25806*b^4*c^3 + 330*a^3*b*d^3 - 2070*a^2*b^2*c*d^2 + 7038*a*b^3*c^2*d))/(21505*d^4*(a*d - b*c)^4) + (1296*b^3*x^3*(a*d + 23*b*c))/(21505*d^2*(a*d - b*c)^4) + (108*b^2*x^2*(391*b^2*c^2 - 5*a^2*d^2 + 46*a*b*c*d))/(21505*d^3*(a*d - b*c)^4)) / (x^4*(a + b*x)^{(1/6)} + (c^4*(a + b*x)^{(1/6)}) / d^4 + (6*c^2*x^2*(a + b*x)^{(1/6)}) / d^2 + (4*c*x^3*(a + b*x)^{(1/6)}) / d + (4*c^3*x*(a + b*x)^{(1/6)}) / d^3)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/6)/(d*x+c)**(29/6),x)`

[Out] Timed out

$$3.1812 \quad \int \frac{(c+dx)^{11/6}}{\sqrt[6]{a+bx}} dx$$

Optimal. Leaf size=82

$$\frac{6(a+bx)^{5/6}(c+dx)^{5/6}(bc-ad) {}_2F_1\left(-\frac{11}{6}, \frac{5}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5b^2 \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

[Out] 6/5*(-a*d+b*c)*(b*x+a)^(5/6)*(d*x+c)^(5/6)*hypergeom([-11/6, 5/6], [11/6], -d*(b*x+a)/(-a*d+b*c))/b^2/(b*(d*x+c)/(-a*d+b*c))^(5/6)

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{5/6}(c+dx)^{5/6}(bc-ad) {}_2F_1\left(-\frac{11}{6}, \frac{5}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5b^2 \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(11/6)/(a + b*x)^(1/6), x]

[Out] (6*(b*c - a*d)*(a + b*x)^(5/6)*(c + d*x)^(5/6)*Hypergeometric2F1[-11/6, 5/6, 11/6, -((d*(a + b*x))/(b*c - a*d))]/(5*b^2*((b*(c + d*x))/(b*c - a*d))^(5/6))

Rule 69

```
Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))
```

Rule 70

```
Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])
```

Rubi steps

$$\int \frac{(c + dx)^{11/6}}{\sqrt[6]{a + bx}} dx = \frac{((bc - ad)(c + dx)^{5/6}) \int \frac{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{11/6}}{\sqrt[6]{a+bx}} dx}{b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

$$= \frac{6(bc - ad)(a + bx)^{5/6}(c + dx)^{5/6} {}_2F_1\left(-\frac{11}{6}, \frac{5}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5b^2 \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Mathematica [A] time = 0.07, size = 73, normalized size = 0.89

$$\frac{6(a + bx)^{5/6}(c + dx)^{11/6} {}_2F_1\left(-\frac{11}{6}, \frac{5}{6}; \frac{11}{6}; \frac{d(a+bx)}{ad-bc}\right)}{5b \left(\frac{b(c+dx)}{bc-ad}\right)^{11/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(11/6)/(a + b*x)^(1/6), x]

[Out] (6*(a + b*x)^(5/6)*(c + d*x)^(11/6)*Hypergeometric2F1[-11/6, 5/6, 11/6, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*((b*(c + d*x))/(b*c - a*d))^(11/6))

fricas [F] time = 1.90, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(dx + c)^{\frac{11}{6}}}{(bx + a)^{\frac{1}{6}}}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(11/6)/(b*x+a)^(1/6), x, algorithm="fricas")

[Out] integral((d*x + c)^(11/6)/(b*x + a)^(1/6), x)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(11/6)/(b*x+a)^(1/6), x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{11}{6}}}{(bx + a)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(11/6)/(b*x+a)^(1/6),x)

[Out] int((d*x+c)^(11/6)/(b*x+a)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{11}{6}}}{(bx + a)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(11/6)/(b*x+a)^(1/6),x, algorithm="maxima")

[Out] integrate((d*x + c)^(11/6)/(b*x + a)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{11/6}}{(a + bx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(11/6)/(a + b*x)^(1/6),x)

[Out] int((c + d*x)^(11/6)/(a + b*x)^(1/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(11/6)/(b*x+a)**(1/6),x)

[Out] Timed out

$$3.1813 \quad \int \frac{(c+dx)^{5/6}}{\sqrt[6]{a+bx}} dx$$

Optimal. Leaf size=74

$$\frac{6(a+bx)^{5/6}(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, \frac{5}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5b\left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

[Out] $6/5*(b*x+a)^{(5/6)}*(d*x+c)^{(5/6)}*\text{hypergeom}\left([-5/6, 5/6], [11/6], -d*(b*x+a)/(-a*d+b*c)\right)/b/(b*(d*x+c)/(-a*d+b*c))^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{5/6}(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, \frac{5}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5b\left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/6)/(a + b*x)^(1/6), x]

[Out] $(6*(a+b*x)^{(5/6)}*(c+d*x)^{(5/6)}*\text{Hypergeometric2F1}[-5/6, 5/6, 11/6, -((d*(a+b*x))/(b*c-a*d))])/(5*b*((b*(c+d*x))/(b*c-a*d))^{(5/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(c+dx)^{5/6}}{\sqrt[6]{a+bx}} dx = \frac{(c+dx)^{5/6} \int \frac{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{5/6}}{\sqrt[6]{a+bx}} dx}{\left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

$$= \frac{6(a+bx)^{5/6}(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, \frac{5}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Mathematica [A] time = 0.04, size = 73, normalized size = 0.99

$$\frac{6(a+bx)^{5/6}(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, \frac{5}{6}; \frac{11}{6}; \frac{d(a+bx)}{ad-bc}\right)}{5b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/6)/(a + b*x)^(1/6), x]

[Out] (6*(a + b*x)^(5/6)*(c + d*x)^(5/6)*Hypergeometric2F1[-5/6, 5/6, 11/6, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*((b*(c + d*x))/(b*c - a*d))^(5/6))

fricas [F] time = 2.06, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx+c)^{\frac{5}{6}}}{(bx+a)^{\frac{1}{6}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(1/6), x, algorithm="fricas")

[Out] integral((d*x + c)^(5/6)/(b*x + a)^(1/6), x)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(1/6), x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/6)/(b*x+a)^(1/6),x)

[Out] int((d*x+c)^(5/6)/(b*x+a)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(1/6),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/6)/(b*x + a)^(1/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{5/6}}{(a + bx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/6)/(a + b*x)^(1/6),x)

[Out] int((c + d*x)^(5/6)/(a + b*x)^(1/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{6}}}{\sqrt[6]{a + bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/6)/(b*x+a)**(1/6),x)

[Out] Integral((c + d*x)**(5/6)/(a + b*x)**(1/6), x)

$$3.1814 \quad \int \frac{1}{\sqrt[6]{a+bx} \sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=74

$$\frac{6(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{5}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5b\sqrt[6]{c+dx}}$$

[Out] 6/5*(b*x+a)^(5/6)*(b*(d*x+c)/(-a*d+b*c))^(1/6)*hypergeom([1/6, 5/6],[11/6], -d*(b*x+a)/(-a*d+b*c))/b/(d*x+c)^(1/6)

Rubi [A] time = 0.02, antiderivative size = 74, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{5}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5b\sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/6)*(c + d*x)^(1/6)),x]

[Out] (6*(a + b*x)^(5/6)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 5/6, 11/6, -((d*(a + b*x))/(b*c - a*d))]/(5*b*(c + d*x)^(1/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{\sqrt[6]{a+bx}\sqrt[6]{c+dx}} dx = \frac{\sqrt[6]{\frac{b(c+dx)}{bc-ad}} \int \frac{1}{\sqrt[6]{a+bx}\sqrt[6]{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}}} dx}{\sqrt[6]{c+dx}}$$

$$= \frac{6(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{5}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5b\sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.03, size = 73, normalized size = 0.99

$$\frac{6(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{1}{6}, \frac{5}{6}; \frac{11}{6}; \frac{d(a+bx)}{ad-bc}\right)}{5b\sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/6)*(c + d*x)^(1/6)), x]

[Out] (6*(a + b*x)^(5/6)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 5/6, 11/6, (d*(a + b*x))/(-b*c) + a*d])/(5*b*(c + d*x)^(1/6))

fricas [F] time = 1.82, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{5}{6}}}{bdx^2+ac+(bc+ad)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(1/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(1/6), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(1/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(1/6)/(d*x+c)^(1/6),x)`

[Out] `int(1/(b*x+a)^(1/6)/(d*x+c)^(1/6),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(1/6)/(d*x+c)^(1/6),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(1/6)*(d*x + c)^(1/6)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{1/6}(c+dx)^{1/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(1/6)*(c + d*x)^(1/6)),x)`

[Out] `int(1/((a + b*x)^(1/6)*(c + d*x)^(1/6)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[6]{a+bx}\sqrt[6]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(1/6)/(d*x+c)**(1/6),x)`

[Out] `Integral(1/((a + b*x)**(1/6)*(c + d*x)**(1/6)), x)`

$$3.1815 \quad \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{7/6}} dx$$

Optimal. Leaf size=81

$$\frac{6(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{5}{6}, \frac{7}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5\sqrt[6]{c+dx} (bc-ad)}$$

[Out] $6/5*(b*x+a)^{(5/6)}*(b*(d*x+c)/(-a*d+b*c))^{(1/6)}*\text{hypergeom}([5/6, 7/6], [11/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{5}{6}, \frac{7}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5\sqrt[6]{c+dx} (bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/6)*(c + d*x)^(7/6)), x]

[Out] $(6*(a + b*x)^{(5/6)}*((b*(c + d*x))/(b*c - a*d))^{(1/6)}*\text{Hypergeometric2F1}[5/6, 7/6, 11/6, -((d*(a + b*x))/(b*c - a*d))]/(5*(b*c - a*d)*(c + d*x)^{(1/6)})$

Rule 69

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{7/6}} dx = \frac{\left(b\sqrt[6]{\frac{b(c+dx)}{bc-ad}}\right) \int \frac{1}{\sqrt[6]{a+bx}\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{7/6}} dx}{(bc-ad)\sqrt[6]{c+dx}}$$

$$= \frac{6(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{5}{6}, \frac{7}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5(bc-ad)\sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.05, size = 73, normalized size = 0.90

$$\frac{6(a+bx)^{5/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{7/6} {}_2F_1\left(\frac{5}{6}, \frac{7}{6}; \frac{11}{6}; \frac{d(a+bx)}{ad-bc}\right)}{5b(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/6)*(c + d*x)^(7/6)), x]

[Out] (6*(a + b*x)^(5/6)*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[5/6, 7/6, 11/6, (d*(a + b*x))/(-b*c + a*d)])/(5*b*(c + d*x)^(7/6))

fricas [F] time = 1.88, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{5/6}(dx+c)^{5/6}}{bd^2x^3+ac^2+(2bcd+ad^2)x^2+(bc^2+2acd)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(7/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(b*d^2*x^3 + a*c^2 + (2*b*c*d + a*d^2)*x^2 + (b*c^2 + 2*a*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{1/6}(dx+c)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(7/6), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(7/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{6}} (dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/6)/(d*x+c)^(7/6), x)

[Out] int(1/(b*x+a)^(1/6)/(d*x+c)^(7/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{6}} (dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(7/6), x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(7/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{1/6} (c + dx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/6)*(c + d*x)^(7/6)), x)

[Out] int(1/((a + b*x)^(1/6)*(c + d*x)^(7/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[6]{a + bx} (c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/6)/(d*x+c)**(7/6), x)

[Out] Integral(1/((a + b*x)**(1/6)*(c + d*x)**(7/6)), x)

$$3.1816 \quad \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{13/6}} dx$$

Optimal. Leaf size=82

$$\frac{6b(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{5}{6}, \frac{13}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5\sqrt[6]{c+dx} (bc-ad)^2}$$

[Out] $6/5*b*(b*x+a)^{(5/6)}*(b*(d*x+c)/(-a*d+b*c))^{(1/6)}*\text{hypergeom}([5/6, 13/6], [11/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^2/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6b(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{5}{6}, \frac{13}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5\sqrt[6]{c+dx} (bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/6)*(c + d*x)^(13/6)),x]

[Out] $(6*b*(a + b*x)^{(5/6)}*((b*(c + d*x))/(b*c - a*d))^{(1/6)}*\text{Hypergeometric2F1}[5/6, 13/6, 11/6, -((d*(a + b*x))/(b*c - a*d))]/(5*(b*c - a*d)^2*(c + d*x)^{(1/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{13/6}} dx = \frac{\left(b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}\right) \int \frac{1}{\sqrt[6]{a+bx} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{13/6}} dx}{(bc-ad)^2 \sqrt[6]{c+dx}}$$

$$= \frac{6b(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{5}{6}, \frac{13}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5(bc-ad)^2 \sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.06, size = 73, normalized size = 0.89

$$\frac{6(a+bx)^{5/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{13/6} {}_2F_1\left(\frac{5}{6}, \frac{13}{6}; \frac{11}{6}; \frac{d(a+bx)}{ad-bc}\right)}{5b(c+dx)^{13/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/6)*(c + d*x)^(13/6)), x]

[Out] (6*(a + b*x)^(5/6)*((b*(c + d*x))/(b*c - a*d))^(13/6)*Hypergeometric2F1[5/6, 13/6, 11/6, (d*(a + b*x))/(-(b*c) + a*d)]/(5*b*(c + d*x)^(13/6))

fricas [F] time = 1.59, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^5(dx+c)^5}{bd^3x^4+ac^3+(3bcd^2+ad^3)x^3+3(bc^2d+acd^2)x^2+(bc^3+3ac^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(13/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(b*d^3*x^4 + a*c^3 + (3*b*c*d^2 + a*d^3)*x^3 + 3*(b*c^2*d + a*c*d^2)*x^2 + (b*c^3 + 3*a*c^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(13/6), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(13/6)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{6}} (dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/6)/(d*x+c)^(13/6), x)

[Out] int(1/(b*x+a)^(1/6)/(d*x+c)^(13/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{6}} (dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(13/6), x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(13/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{1/6} (c + dx)^{13/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/6)*(c + d*x)^(13/6)), x)

[Out] int(1/((a + b*x)^(1/6)*(c + d*x)^(13/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{\sqrt[6]{a + bx} (c + dx)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/6)/(d*x+c)**(13/6), x)

[Out] Integral(1/((a + b*x)**(1/6)*(c + d*x)**(13/6)), x)

$$3.1817 \quad \int \frac{1}{\sqrt[6]{a+bx} (c+dx)^{19/6}} dx$$

Optimal. Leaf size=84

$$\frac{6b^2(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{5}{6}, \frac{19}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5\sqrt[6]{c+dx} (bc-ad)^3}$$

[Out] $6/5*b^2*(b*x+a)^{(5/6)}*(b*(d*x+c)/(-a*d+b*c))^{(1/6)}*\text{hypergeom}([5/6, 19/6], [11/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^3/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6b^2(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{5}{6}, \frac{19}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5\sqrt[6]{c+dx} (bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(1/6)*(c + d*x)^(19/6)), x]

[Out] $(6*b^2*(a + b*x)^{(5/6)}*((b*(c + d*x))/(b*c - a*d))^{(1/6)}*\text{Hypergeometric2F1}[5/6, 19/6, 11/6, -((d*(a + b*x))/(b*c - a*d))]/(5*(b*c - a*d)^3*(c + d*x)^{(1/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{19/6}} dx = \frac{\left(b^3 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}\right) \int \frac{1}{\sqrt[6]{a+bx} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{19/6}} dx}{(bc-ad)^3 \sqrt[6]{c+dx}}$$

$$= \frac{6b^2(a+bx)^{5/6} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(\frac{5}{6}, \frac{19}{6}; \frac{11}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{5(bc-ad)^3 \sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.04, size = 81, normalized size = 0.96

$$\frac{6b(a+bx)^{5/6} \left(\frac{b(c+dx)}{bc-ad}\right)^{7/6} {}_2F_1\left(\frac{5}{6}, \frac{19}{6}; \frac{11}{6}; \frac{d(a+bx)}{ad-bc}\right)}{5(c+dx)^{7/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(1/6)*(c + d*x)^(19/6)), x]

[Out] (6*b*(a + b*x)^(5/6)*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[5/6, 19/6, 11/6, (d*(a + b*x))/(-(b*c) + a*d)]/(5*(b*c - a*d)^2*(c + d*x)^(7/6))

fricas [F] time = 1.64, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{5/6} (dx+c)^{5/6}}{bd^4x^5 + ac^4 + (4bcd^3 + ad^4)x^4 + 2(3bc^2d^2 + 2acd^3)x^3 + 2(2bc^3d + 3ac^2d^2)x^2 + (bc^4 + 4ac^3d)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(19/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(b*d^4*x^5 + a*c^4 + (4*b*c*d^3 + a*d^4)*x^4 + 2*(3*b*c^2*d^2 + 2*a*c*d^3)*x^3 + 2*(2*b*c^3*d + 3*a*c^2*d^2)*x^2 + (b*c^4 + 4*a*c^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{1/6}(dx+c)^{19/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(19/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(19/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{6}} (dx + c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(1/6)/(d*x+c)^(19/6),x)

[Out] int(1/(b*x+a)^(1/6)/(d*x+c)^(19/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{1}{6}} (dx + c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(1/6)/(d*x+c)^(19/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(1/6)*(d*x + c)^(19/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{\frac{1}{6}} (c + dx)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(1/6)*(c + d*x)^(19/6)),x)

[Out] int(1/((a + b*x)^(1/6)*(c + d*x)^(19/6)), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(1/6)/(d*x+c)**(19/6),x)

[Out] Timed out

$$3.1818 \quad \int \frac{(c+dx)^{13/6}}{(a+bx)^{5/6}} dx$$

Optimal. Leaf size=82

$$\frac{6\sqrt[6]{a+bx}\sqrt[6]{c+dx}(bc-ad)^2 {}_2F_1\left(-\frac{13}{6}, \frac{1}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b^3\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

[Out] $6*(-a*d+b*c)^2*(b*x+a)^{(1/6)}*(d*x+c)^{(1/6)}*\text{hypergeom}\left(-\frac{13}{6}, \frac{1}{6}, \left[\frac{7}{6}\right], -d*(b*x+a)/(-a*d+b*c)\right)/b^3/(b*(d*x+c)/(-a*d+b*c))^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6\sqrt[6]{a+bx}\sqrt[6]{c+dx}(bc-ad)^2 {}_2F_1\left(-\frac{13}{6}, \frac{1}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b^3\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(13/6)/(a + b*x)^(5/6), x]

[Out] $(6*(b*c - a*d)^2*(a + b*x)^{(1/6)}*(c + d*x)^{(1/6)}*\text{Hypergeometric2F1}\left[-\frac{13}{6}, \frac{1}{6}, \frac{7}{6}, -\left(\frac{d*(a + b*x)}{b*c - a*d}\right)\right])/(b^3*\left(\frac{b*(c + d*x)}{b*c - a*d}\right)^{(1/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -(d*(a + b*x))/(b*c - a*d)])/((b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(c + dx)^{13/6}}{(a + bx)^{5/6}} dx = \frac{\left((bc - ad)^2 \sqrt[6]{c + dx}\right) \int \frac{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{13/6}}{(a+bx)^{5/6}} dx}{b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

$$= \frac{6(bc - ad)^2 \sqrt[6]{a + bx} \sqrt[6]{c + dx} {}_2F_1\left(-\frac{13}{6}, \frac{1}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b^3 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Mathematica [A] time = 0.09, size = 71, normalized size = 0.87

$$\frac{6\sqrt[6]{a + bx} (c + dx)^{13/6} {}_2F_1\left(-\frac{13}{6}, \frac{1}{6}; \frac{7}{6}; \frac{d(a+bx)}{ad-bc}\right)}{b \left(\frac{b(c+dx)}{bc-ad}\right)^{13/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(13/6)/(a + b*x)^(5/6), x]

[Out] (6*(a + b*x)^(1/6)*(c + d*x)^(13/6)*Hypergeometric2F1[-13/6, 1/6, 7/6, (d*(a + b*x))/(-(b*c) + a*d)]/(b*((b*(c + d*x))/(b*c - a*d))^(13/6))

fricas [F] time = 1.01, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(d^2x^2 + 2cdx + c^2)(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{5}{6}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(13/6)/(b*x+a)^(5/6), x, algorithm="fricas")

[Out] integral((d^2*x^2 + 2*c*d*x + c^2)*(d*x + c)^(1/6)/(b*x + a)^(5/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{13}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(13/6)/(b*x+a)^(5/6), x, algorithm="giac")

[Out] integrate((d*x + c)^(13/6)/(b*x + a)^(5/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{13}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(13/6)/(b*x+a)^(5/6),x)

[Out] int((d*x+c)^(13/6)/(b*x+a)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{13}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(13/6)/(b*x+a)^(5/6),x, algorithm="maxima")

[Out] integrate((d*x + c)^(13/6)/(b*x + a)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{\frac{13}{6}}}{(a + bx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(13/6)/(a + b*x)^(5/6),x)

[Out] int((c + d*x)^(13/6)/(a + b*x)^(5/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(13/6)/(b*x+a)**(5/6),x)

[Out] Timed out

$$3.1819 \quad \int \frac{(c+dx)^{7/6}}{(a+bx)^{5/6}} dx$$

Optimal. Leaf size=80

$$\frac{6\sqrt[6]{a+bx}\sqrt[6]{c+dx}(bc-ad) {}_2F_1\left(-\frac{7}{6}, \frac{1}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b^2\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

[Out] 6*(-a*d+b*c)*(b*x+a)^(1/6)*(d*x+c)^(1/6)*hypergeom([-7/6, 1/6], [7/6], -d*(b*x+a)/(-a*d+b*c))/b^2/(b*(d*x+c)/(-a*d+b*c))^(1/6)

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6\sqrt[6]{a+bx}\sqrt[6]{c+dx}(bc-ad) {}_2F_1\left(-\frac{7}{6}, \frac{1}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b^2\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(7/6)/(a + b*x)^(5/6), x]

[Out] (6*(b*c - a*d)*(a + b*x)^(1/6)*(c + d*x)^(1/6)*Hypergeometric2F1[-7/6, 1/6, 7/6, -(d*(a + b*x))/(b*c - a*d)])/(b^2*((b*(c + d*x))/(b*c - a*d))^(1/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -(d*(a + b*x))/(b*c - a*d)])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(c + dx)^{7/6}}{(a + bx)^{5/6}} dx = \frac{\left((bc - ad)\sqrt[6]{c + dx}\right) \int \frac{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{7/6}}{(a+bx)^{5/6}} dx}{b\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

$$= \frac{6(bc - ad)\sqrt[6]{a + bx}\sqrt[6]{c + dx} {}_2F_1\left(-\frac{7}{6}, \frac{1}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b^2\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Mathematica [A] time = 0.05, size = 71, normalized size = 0.89

$$\frac{6\sqrt[6]{a + bx}(c + dx)^{7/6} {}_2F_1\left(-\frac{7}{6}, \frac{1}{6}; \frac{7}{6}; \frac{d(a+bx)}{ad-bc}\right)}{b\left(\frac{b(c+dx)}{bc-ad}\right)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(7/6)/(a + b*x)^(5/6), x]

[Out] (6*(a + b*x)^(1/6)*(c + d*x)^(7/6)*Hypergeometric2F1[-7/6, 1/6, 7/6, (d*(a + b*x))/(-(b*c) + a*d)]/(b*((b*(c + d*x))/(b*c - a*d))^(7/6))

fricas [F] time = 1.00, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx + c)^{\frac{7}{6}}}{(bx + a)^{\frac{5}{6}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(7/6)/(b*x+a)^(5/6), x, algorithm="fricas")

[Out] integral((d*x + c)^(7/6)/(b*x + a)^(5/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{7}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(7/6)/(b*x+a)^(5/6), x, algorithm="giac")

[Out] integrate((d*x + c)^(7/6)/(b*x + a)^(5/6), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{7}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(7/6)/(b*x+a)^(5/6), x)

[Out] int((d*x+c)^(7/6)/(b*x+a)^(5/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{7}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(7/6)/(b*x+a)^(5/6), x, algorithm="maxima")

[Out] integrate((d*x + c)^(7/6)/(b*x + a)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{7/6}}{(a + bx)^{5/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(7/6)/(a + b*x)^(5/6), x)

[Out] int((c + d*x)^(7/6)/(a + b*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{7}{6}}}{(a + bx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(7/6)/(b*x+a)**(5/6), x)

[Out] Integral((c + d*x)**(7/6)/(a + b*x)**(5/6), x)

$$3.1820 \quad \int \frac{\sqrt[6]{c+dx}}{(a+bx)^{5/6}} dx$$

Optimal. Leaf size=72

$$\frac{6\sqrt[6]{a+bx} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{1}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

[Out] $6*(b*x+a)^{(1/6)}*(d*x+c)^{(1/6)}*\text{hypergeom}([-1/6, 1/6], [7/6], -d*(b*x+a)/(-a*d+b*c))/b/(b*(d*x+c)/(-a*d+b*c))^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6\sqrt[6]{a+bx} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{1}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1/6)/(a + b*x)^(5/6), x]

[Out] $(6*(a + b*x)^{(1/6)}*(c + d*x)^{(1/6)}*\text{Hypergeometric2F1}[-1/6, 1/6, 7/6, -((d*(a + b*x))/(b*c - a*d))]/(b*((b*(c + d*x))/(b*c - a*d))^{(1/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{\sqrt[6]{c+dx}}{(a+bx)^{5/6}} dx = \frac{\sqrt[6]{c+dx} \int \frac{\sqrt[6]{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}}}{(a+bx)^{5/6}} dx}{\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

$$= \frac{6\sqrt[6]{a+bx} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{1}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Mathematica [A] time = 0.03, size = 71, normalized size = 0.99

$$\frac{6\sqrt[6]{a+bx} \sqrt[6]{c+dx} {}_2F_1\left(-\frac{1}{6}, \frac{1}{6}; \frac{7}{6}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/6)/(a + b*x)^(5/6), x]

[Out] (6*(a + b*x)^(1/6)*(c + d*x)^(1/6)*Hypergeometric2F1[-1/6, 1/6, 7/6, (d*(a + b*x))/(-(b*c) + a*d)]/(b*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [F] time = 0.98, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx+c)^{\frac{1}{6}}}{(bx+a)^{\frac{5}{6}}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(5/6), x, algorithm="fricas")

[Out] integral((d*x + c)^(1/6)/(b*x + a)^(5/6), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{6}}}{(bx+a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(5/6), x, algorithm="giac")

[Out] integrate((d*x + c)^(1/6)/(b*x + a)^(5/6), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(1/6)/(b*x+a)^(5/6), x)

[Out] int((d*x+c)^(1/6)/(b*x+a)^(5/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(5/6), x, algorithm="maxima")

[Out] integrate((d*x + c)^(1/6)/(b*x + a)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{1/6}}{(a + bx)^{5/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(1/6)/(a + b*x)^(5/6), x)

[Out] int((c + d*x)^(1/6)/(a + b*x)^(5/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{c + dx}}{(a + bx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(1/6)/(b*x+a)**(5/6), x)

[Out] Integral((c + d*x)**(1/6)/(a + b*x)**(5/6), x)

$$3.1821 \quad \int \frac{1}{(a+bx)^{5/6}(c+dx)^{5/6}} dx$$

Optimal. Leaf size=72

$$\frac{6\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{5}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b(c+dx)^{5/6}}$$

[Out] $6*(b*x+a)^{(1/6)}*(b*(d*x+c)/(-a*d+b*c))^{(5/6)}*\text{hypergeom}([1/6, 5/6], [7/6], -d*(b*x+a)/(-a*d+b*c))/b/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{5}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/6)*(c + d*x)^(5/6)), x]

[Out] $(6*(a + b*x)^{(1/6)}*((b*(c + d*x))/(b*c - a*d))^{(5/6)}*\text{Hypergeometric2F1}[1/6, 5/6, 7/6, -((d*(a + b*x))/(b*c - a*d))]/(b*(c + d*x)^{(5/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/(b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n], Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{5/6}} dx = \frac{\left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} \int \frac{1}{(a+bx)^{5/6} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{5/6}} dx}{(c+dx)^{5/6}}$$

$$= \frac{6\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{5}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b(c+dx)^{5/6}}$$

Mathematica [A] time = 0.04, size = 71, normalized size = 0.99

$$\frac{6\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{5}{6}; \frac{7}{6}; \frac{d(a+bx)}{ad-bc}\right)}{b(c+dx)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/6)*(c + d*x)^(5/6)),x]

[Out] (6*(a + b*x)^(1/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[1/6, 5/6, 7/6, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(c + d*x)^(5/6))

fricas [F] time = 0.61, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{1}{6}}}{bdx^2+ac+(bc+ad)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(5/6),x, algorithm="fricas")

[Out] integral((b*x + a)^(1/6)*(d*x + c)^(1/6)/(b*d*x^2 + a*c + (b*c + a*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(5/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/6)*(d*x + c)^(5/6)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/6)/(d*x+c)^(5/6),x)

[Out] int(1/(b*x+a)^(5/6)/(d*x+c)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(5/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/6)*(d*x + c)^(5/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{\frac{5}{6}}(c+dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/6)*(c + d*x)^(5/6)),x)

[Out] int(1/((a + b*x)^(5/6)*(c + d*x)^(5/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{6}}(c+dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/6)/(d*x+c)**(5/6),x)

[Out] Integral(1/((a + b*x)**(5/6)*(c + d*x)**(5/6)), x)

$$3.1822 \quad \int \frac{1}{(a+bx)^{5/6}(c+dx)^{11/6}} dx$$

Optimal. Leaf size=79

$$\frac{6\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{11}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{(c+dx)^{5/6}(bc-ad)}$$

[Out] $6*(b*x+a)^{(1/6)}*(b*(d*x+c)/(-a*d+b*c))^{(5/6)}*\text{hypergeom}([1/6, 11/6], [7/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{11}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{(c+dx)^{5/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/6)*(c + d*x)^(11/6)),x]

[Out] $(6*(a + b*x)^{(1/6)}*((b*(c + d*x))/(b*c - a*d))^{(5/6)}*\text{Hypergeometric2F1}[1/6, 11/6, 7/6, -((d*(a + b*x))/(b*c - a*d))]/((b*c - a*d)*(c + d*x)^{(5/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/(b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n], Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{11/6}} dx = \frac{\left(b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}\right) \int \frac{1}{(a+bx)^{5/6} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{11/6}} dx}{(bc-ad)(c+dx)^{5/6}}$$

$$= \frac{6\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{11}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{(bc-ad)(c+dx)^{5/6}}$$

Mathematica [A] time = 0.06, size = 71, normalized size = 0.90

$$\frac{6\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{11/6} {}_2F_1\left(\frac{1}{6}, \frac{11}{6}; \frac{7}{6}; \frac{d(a+bx)}{ad-bc}\right)}{b(c+dx)^{11/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/6)*(c + d*x)^(11/6)), x]

[Out] (6*(a + b*x)^(1/6)*((b*(c + d*x))/(b*c - a*d))^(11/6)*Hypergeometric2F1[1/6, 11/6, 7/6, (d*(a + b*x))/(-b*c) + a*d])/(b*(c + d*x)^(11/6))

fricas [F] time = 1.02, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{1}{6}}}{bd^2x^3+ac^2+(2bcd+ad^2)x^2+(bc^2+2acd)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(11/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/6)*(d*x + c)^(1/6)/(b*d^2*x^3 + a*c^2 + (2*b*c*d + a*d^2)*x^2 + (b*c^2 + 2*a*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(11/6), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/6)*(d*x + c)^(11/6)), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/6)/(d*x+c)^(11/6),x)

[Out] int(1/(b*x+a)^(5/6)/(d*x+c)^(11/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(11/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/6)*(d*x + c)^(11/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{\frac{5}{6}}(c+dx)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/6)*(c + d*x)^(11/6)),x)

[Out] int(1/((a + b*x)^(5/6)*(c + d*x)^(11/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{6}}(c+dx)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/6)/(d*x+c)**(11/6),x)

[Out] Integral(1/((a + b*x)**(5/6)*(c + d*x)**(11/6)), x)

$$3.1823 \quad \int \frac{1}{(a+bx)^{5/6}(c+dx)^{17/6}} dx$$

Optimal. Leaf size=80

$$\frac{6b\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{17}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{(c+dx)^{5/6}(bc-ad)^2}$$

[Out] 6*b*(b*x+a)^(1/6)*(b*(d*x+c)/(-a*d+b*c))^(5/6)*hypergeom([1/6, 17/6], [7/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^2/(d*x+c)^(5/6)

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6b\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{17}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{(c+dx)^{5/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/6)*(c + d*x)^(17/6)), x]

[Out] (6*b*(a + b*x)^(1/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[1/6, 17/6, 7/6, -((d*(a + b*x))/(b*c - a*d))]/((b*c - a*d)^2*(c + d*x)^(5/6))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{17/6}} dx = \frac{\left(b^2 \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}\right) \int \frac{1}{(a+bx)^{5/6} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{17/6}} dx}{(bc-ad)^2(c+dx)^{5/6}}$$

$$= \frac{6b\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{17}{6}; \frac{7}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{(bc-ad)^2(c+dx)^{5/6}}$$

Mathematica [A] time = 0.04, size = 79, normalized size = 0.99

$$\frac{6b\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6} {}_2F_1\left(\frac{1}{6}, \frac{17}{6}; \frac{7}{6}; \frac{d(a+bx)}{ad-bc}\right)}{(c+dx)^{5/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/6)*(c + d*x)^(17/6)), x]

[Out] (6*b*(a + b*x)^(1/6)*((b*(c + d*x))/(b*c - a*d))^(5/6)*Hypergeometric2F1[1/6, 17/6, 7/6, (d*(a + b*x))/(-b*c + a*d)]/((b*c - a*d)^2*(c + d*x)^(5/6))

fricas [F] time = 0.83, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{1}{6}}}{bd^3x^4 + ac^3 + (3bcd^2 + ad^3)x^3 + 3(bc^2d + acd^2)x^2 + (bc^3 + 3ac^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(17/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(1/6)*(d*x + c)^(1/6)/(b*d^3*x^4 + a*c^3 + (3*b*c*d^2 + a*d^3)*x^3 + 3*(b*c^2*d + a*c*d^2)*x^2 + (b*c^3 + 3*a*c^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(17/6), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/6)*(d*x + c)^(17/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{6}} (dx + c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/6)/(d*x+c)^(17/6),x)

[Out] int(1/(b*x+a)^(5/6)/(d*x+c)^(17/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{6}} (dx + c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(17/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/6)*(d*x + c)^(17/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{\frac{5}{6}} (c + dx)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/6)*(c + d*x)^(17/6)),x)

[Out] int(1/((a + b*x)^(5/6)*(c + d*x)^(17/6)), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/6)/(d*x+c)**(17/6),x)

[Out] Timed out

$$3.1824 \quad \int \frac{(c+dx)^{11/6}}{(a+bx)^{5/6}} dx$$

Optimal. Leaf size=424

$$\frac{55(bc - ad)^2 \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{17/6} \sqrt[6]{d}} + \frac{55(bc - ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{17/6} \sqrt[6]{d}} - \frac{55(bc - ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{17/6} \sqrt[6]{d}}$$

[Out] $11/12*(-a*d+b*c)*(b*x+a)^{(1/6)}*(d*x+c)^{(5/6)}/b^{2+1/2}*(b*x+a)^{(1/6)}*(d*x+c)^{(11/6)}/b+55/36*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(17/6)}/d^{(1/6)}-55/144*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)})/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(17/6)}/d^{(1/6)}+55/144*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)})/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(17/6)}/d^{(1/6)}+55/72*(-a*d+b*c)^2*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})*3^{(1/2)}/b^{(17/6)}/d^{(1/6)}*3^{(1/2)}+55/72*(-a*d+b*c)^2*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})*3^{(1/2)}/b^{(17/6)}/d^{(1/6)}*3^{(1/2)}$

Rubi [A] time = 0.55, antiderivative size = 424, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {50, 63, 240, 210, 634, 618, 204, 628, 208}

$$\frac{11\sqrt[6]{a+bx}(c+dx)^{5/6}(bc-ad)}{12b^2} - \frac{55(bc-ad)^2 \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{17/6} \sqrt[6]{d}} + \frac{55(bc-ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{17/6} \sqrt[6]{d}} - \frac{55(bc-ad)^2 \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{17/6} \sqrt[6]{d}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(11/6)}/(a + b*x)^{(5/6)}, x]$

[Out] $(11*(b*c - a*d)*(a + b*x)^{(1/6)}*(c + d*x)^{(5/6)})/(12*b^2) + ((a + b*x)^{(1/6)}*(c + d*x)^{(11/6)})/(2*b) - (55*(b*c - a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(17/6)}*d^{(1/6)}) + (55*(b*c - a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(17/6)}*d^{(1/6)}) + (55*(b*c - a*d)^2*\operatorname{ArcTanh}[(d^{(1/6)}*(a + b*x)^{(1/6)})/(b^{(1/6)}*(c + d*x)^{(1/6)})]/(36*b^{(17/6)}*d^{(1/6)}) - (55*(b*c - a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})]/(144*b^{(17/6)}*d^{(1/6)}) + (55*(b*c - a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})]/(144*b^{(17/6)}*d^{(1/6)})$

Rule 50


```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rule 210

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Module[{r = Numerator[Rt[-(
a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r - s*Cos[(
2*k*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r + s*Co
s[(2*k*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^2*Int[
1/(r^2 - s^2*x^2), x])/(a*n) + Dist[(2*r)/(a*n), Sum[u, {k, 1, (n - 2)/4}],
x], x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && NegQ[a/b]
```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int
[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a,
b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/
n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_.) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), Int[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{11/6}}{(a+bx)^{5/6}} dx &= \frac{\sqrt[6]{a+bx} (c+dx)^{11/6}}{2b} + \frac{(11(bc-ad)) \int \frac{(c+dx)^{5/6}}{(a+bx)^{5/6}} dx}{12b} \\
&= \frac{11(bc-ad)\sqrt[6]{a+bx} (c+dx)^{5/6}}{12b^2} + \frac{\sqrt[6]{a+bx} (c+dx)^{11/6}}{2b} + \frac{(55(bc-ad)^2) \int \frac{1}{(a+bx)^{5/6} \sqrt[6]{c+dx}} dx}{72b^2} \\
&= \frac{11(bc-ad)\sqrt[6]{a+bx} (c+dx)^{5/6}}{12b^2} + \frac{\sqrt[6]{a+bx} (c+dx)^{11/6}}{2b} + \frac{(55(bc-ad)^2) \text{Subst} \left(\int \frac{1}{\sqrt[6]{c-\frac{ad}{b} + \frac{dx}{b}}} dx \right)}{12b^3} \\
&= \frac{11(bc-ad)\sqrt[6]{a+bx} (c+dx)^{5/6}}{12b^2} + \frac{\sqrt[6]{a+bx} (c+dx)^{11/6}}{2b} + \frac{(55(bc-ad)^2) \text{Subst} \left(\int \frac{1}{1-\frac{dx^6}{b}} dx \right)}{12b^3} \\
&= \frac{11(bc-ad)\sqrt[6]{a+bx} (c+dx)^{5/6}}{12b^2} + \frac{\sqrt[6]{a+bx} (c+dx)^{11/6}}{2b} + \frac{(55(bc-ad)^2) \text{Subst} \left(\int \frac{\sqrt[6]{b}-}{\sqrt[3]{b}-\sqrt[6]{b} \sqrt[6]{a}} dx \right)}{36b^{17/6}} \\
&= \frac{11(bc-ad)\sqrt[6]{a+bx} (c+dx)^{5/6}}{12b^2} + \frac{\sqrt[6]{a+bx} (c+dx)^{11/6}}{2b} + \frac{55(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{36b^{17/6} \sqrt[6]{d}} \\
&= \frac{11(bc-ad)\sqrt[6]{a+bx} (c+dx)^{5/6}}{12b^2} + \frac{\sqrt[6]{a+bx} (c+dx)^{11/6}}{2b} + \frac{55(bc-ad)^2 \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{36b^{17/6} \sqrt[6]{d}} \\
&= \frac{11(bc-ad)\sqrt[6]{a+bx} (c+dx)^{5/6}}{12b^2} + \frac{\sqrt[6]{a+bx} (c+dx)^{11/6}}{2b} - \frac{55(bc-ad)^2 \tan^{-1} \left(\frac{1-\frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{24\sqrt{3} b^{17/6} \sqrt[6]{d}}
\end{aligned}$$

Mathematica [C] time = 0.06, size = 71, normalized size = 0.17

$$\frac{6\sqrt[6]{a+bx} (c+dx)^{11/6} {}_2F_1 \left(-\frac{11}{6}, \frac{1}{6}; \frac{7}{6}; \frac{d(a+bx)}{ad-bc} \right)}{b \left(\frac{b(c+dx)}{bc-ad} \right)^{11/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(11/6)/(a + b*x)^(5/6), x]

[Out] $(6*(a + b*x)^{(1/6)}*(c + d*x)^{(11/6)}*\text{Hypergeometric2F1}[-11/6, 1/6, 7/6, (d*(a + b*x))/(-(b*c) + a*d)])/(b*((b*(c + d*x))/(b*c - a*d))^{(11/6)})$

fricas [B] time = 1.32, size = 5591, normalized size = 13.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(11/6)/(b*x+a)^(5/6),x, algorithm="fricas")`

[Out]
$$\begin{aligned} & -1/144*(220*\sqrt{3}*b^2*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^{17}*d))^{(1/6)} \\ & * \arctan(-1/3*(2*\sqrt{3}*(b^{16}*c^2*d - 2*a*b^{15}*c*d^2 + a^2*b^{14}*d^3)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^{17}*d))^{(1/6)} \\ & - 2*\sqrt{3}*(b^{14}*d^2*x + b^{14}*c*d)*\sqrt{((b^5*c^2 - 2*a*b^4*c*d + a^2*b^3*d^2)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^{17}*d))^{(1/6)} \\ & + (b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)} + (b^6*d*x + b^6*c)*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^{17}*d))^{(1/3)})/(d*x + c))*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12})/(b^{17}*d))^{(1/6)} \\ & + \sqrt{3}*(b^{12}*c^{13} - 12*a*b^{11}*c^{12}*d + 66*a^2*b^{10}*c^{11}*d^2 - 220*a^3*b^9*c^{10}*d^3 + 495*a^4*b^8*c^9*d^4 - 792*a^5*b^7*c^8*d^5 + 924*a^6*b^6*c^7*d^6 - 792*a^7*b^5*c^6*d^7 + 495*a^8*b^4*c^5*d^8 - 220*a^9*b^3*c^4*d^9 + 66*a^{10}*b^2*c^3*d^{10} - 12*a^{11}*b*c^2*d^{11} + a^{12}*c*d^{12} + (b^{12}*c^{12}*d - 12*a*b^{11}*c^{11}*d^2 + 66*a^2*b^{10}*c^{10}*d^3 - 220*a^3*b^9*c^9*d^4 + 495*a^4*b^8*c^8*d^5 - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - 792*a^7*b^5*c^5*d^8 + 495*a^8*b^4*c^4*d^9 - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b^2*c^2*d^{11} - 12*a^{11}*b*c*d^{12} + a^{12}*d^{13})*x))/(b^{12}*c^{13} - 12*a*b^{11}*c^{12}*d + 66*a^2*b^{10}*c^{11}*d^2 - 220*a^3*b^9*c^{10}*d^3 + 495*a^4*b^8*c^9*d^4 - 792*a^5*b^7*c^8*d^5 + 924*a^6*b^6*c^7*d^6 - 792*a^7*b^5*c^6*d^7 + 495*a^8*b^4*c^5*d^8 - 220*a^9*b^3*c^4*d^9 + 66*a^{10}*b^2*c^3*d^{10} - 12*a^{11}*b*c^2*d^{11} + a^{12}*c*d^{12} + (b^{12}*c^{12}*d - 12*a*b^{11}*c^{11}*d^2 + 66* \end{aligned}$$

$$\begin{aligned}
& a^2 b^{10} c^{10} d^3 - 220 a^3 b^9 c^9 d^4 + 495 a^4 b^8 c^8 d^5 - 792 a^5 b^7 c^7 d^6 + 924 a^6 b^6 c^6 d^7 - 792 a^7 b^5 c^5 d^8 + 495 a^8 b^4 c^4 d^9 \\
& - 220 a^9 b^3 c^3 d^{10} + 66 a^{10} b^2 c^2 d^{11} - 12 a^{11} b c d^{12} + a^{12} d^{13} \\
& (3) x) + 220 \sqrt{3} b^2 ((b^{12} c^{12} - 12 a b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 \\
& a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{17} d))^{(1/6)} \\
& \arctan(-1/3 (2 \sqrt{3} (b^{16} c^2 d - 2 a b^{15} c d^2 + a^2 b^{14} d^3)) (b x + a)^{(1/6)} (d x + c)^{(5/6)} ((b^{12} c^{12} - 12 a b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 \\
& a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{17} d))^{(1/6)} - 2 \sqrt{3} (b^{14} d^2 x + b^{14} c d) \sqrt{-((b^5 c^2 - 2 a b^4 c d + a^2 b^3 d^2) (b x + a)^{(1/6)} (d x + c)^{(5/6)} ((b^{12} c^{12} - 12 a b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{17} d))^{(1/6)} - (b^4 c^4 - 4 a b^3 c^3 d + 6 a^2 b^2 c^2 d^2 - 4 a^3 b c d^3 + a^4 d^4) (b x + a)^{(1/3)} (d x + c)^{(2/3)} - (b^6 d x + b^6 c) ((b^{12} c^{12} - 12 a b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{17} d))^{(1/3)}} / (d x + c) ((b^{12} c^{12} - 12 a b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{17} d))^{(5/6)} - \sqrt{3} (b^{12} c^{13} - 12 a b^{11} c^{12} d + 66 a^2 b^{10} c^{11} d^2 - 220 a^3 b^9 c^{10} d^3 + 495 a^4 b^8 c^9 d^4 - 792 a^5 b^7 c^8 d^5 + 924 a^6 b^6 c^7 d^6 - 792 a^7 b^5 c^6 d^7 + 495 a^8 b^4 c^5 d^8 - 220 a^9 b^3 c^4 d^9 + 66 a^{10} b^2 c^3 d^{10} - 12 a^{11} b c^2 d^{11} + a^{12} c d^{12} + (b^{12} c^{12} d - 12 a b^{11} c^{11} d^2 + 66 a^2 b^{10} c^{10} d^3 - 220 a^3 b^9 c^9 d^4 + 495 a^4 b^8 c^8 d^5 - 792 a^5 b^7 c^7 d^6 + 924 a^6 b^6 c^6 d^7 - 792 a^7 b^5 c^5 d^8 + 495 a^8 b^4 c^4 d^9 - 220 a^9 b^3 c^3 d^{10} + 66 a^{10} b^2 c^2 d^{11} - 12 a^{11} b c d^{12} + a^{12} d^{13}) x) / (b^{12} c^{13} - 12 a b^{11} c^{12} d + 66 a^2 b^{10} c^{11} d^2 - 220 a^3 b^9 c^{10} d^3 + 495 a^4 b^8 c^9 d^4 - 792 a^5 b^7 c^8 d^5 + 924 a^6 b^6 c^7 d^6 - 792 a^7 b^5 c^6 d^7 + 495 a^8 b^4 c^5 d^8 - 220 a^9 b^3 c^4 d^9 + 66 a^{10} b^2 c^3 d^{10} - 12 a^{11} b c^2 d^{11} + a^{12} c d^{12} + (b^{12} c^{12} d - 12 a b^{11} c^{11} d^2 + 66 a^2 b^{10} c^{10} d^3 - 220 a^3 b^9 c^9 d^4 + 495 a^4 b^8 c^8 d^5 - 792 a^5 b^7 c^7 d^6 + 924 a^6 b^6 c^6 d^7 - 792 a^7 b^5 c^5 d^8 + 495 a^8 b^4 c^4 d^9 - 220 a^9 b^3 c^3 d^{10} + 66 a^{10} b^2 c^2 d^{11} - 12 a^{11} b c d^{12} + a^{12} d^{13}) x) - 55 b^2 ((b^{12} c^{12} - 12 a b^{11} c^{11} d + 66 a^2 b^{10} c^{10} d^2 - 220 a^3 b^9 c^9 d^3 + 495 a^4 b^8 c^8 d^4 - 792 a^5 b^7 c^7 d^5 + 924 a^6 b^6 c^6 d^6 - 792 a^7 b^5 c^5 d^7 + 495 a^8 b^4 c^4 d^8 - 220 a^9 b^3 c^3 d^9 + 66 a^{10} b^2 c^2 d^{10} - 12 a^{11} b c d^{11} + a^{12} d^{12}) / (b^{17} d))^{(1/6)} \log
\end{aligned}$$

$$\begin{aligned}
& (3025*((b^5*c^2 - 2*a*b^4*c*d + a^2*b^3*d^2)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)} \\
&)*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12}))/((b^{17}*d))^{(1/6)} + (b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)} + (b^6*d*x + b^6*c)*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12}))/((b^{17}*d))^{(1/3)})))/(d*x + c) + 55*b^2*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12}))/((b^{17}*d))^{(1/6)}*log(-3025*((b^5*c^2 - 2*a*b^4*c*d + a^2*b^3*d^2)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12}))/((b^{17}*d))^{(1/6)} - (b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*(b*x + a)^{(1/3)}*(d*x + c)^{(2/3)} - (b^6*d*x + b^6*c)*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12}))/((b^{17}*d))^{(1/3)})))/(d*x + c) - 110*b^2*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12}))/((b^{17}*d))^{(1/6)}*log(55*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)} + (b^3*d*x + b^3*c)*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12}))/((b^{17}*d))^{(1/6)})))/(d*x + c) + 110*b^2*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12}))/((b^{17}*d))^{(1/6)}*log(55*((b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)} - (b^3*d*x + b^3*c)*((b^{12}*c^{12} - 12*a*b^{11}*c^{11}*d + 66*a^2*b^{10}*c^{10}*d^2 - 220*a^3*b^9*c^9*d^3 + 495*a^4*b^8*c^8*d^4 - 792*a^5*b^7*c^7*d^5 + 924*a^6*b^6*c^6*d^6 - 792*a^7*b^5*c^5*d^7 + 495*a^8*b^4*c^4*d^8 - 220*a^9*b^3*c^3*d^9 + 66*a^{10}*b^2*c^2*d^{10} - 12*a^{11}*b*c*d^{11} + a^{12}*d^{12}))/((b^{17}*d))^{(1/6)})))/(d*x + c) - 12*(6*b*d*x + 17*b*c - 11*a*d)*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}/b^2
\end{aligned}$$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(11/6)/(b*x+a)^(5/6),x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{11}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(11/6)/(b*x+a)^(5/6),x)

[Out] int((d*x+c)^(11/6)/(b*x+a)^(5/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{11}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(11/6)/(b*x+a)^(5/6),x, algorithm="maxima")

[Out] integrate((d*x + c)^(11/6)/(b*x + a)^(5/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{11/6}}{(a + bx)^{5/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(11/6)/(a + b*x)^(5/6),x)

[Out] int((c + d*x)^(11/6)/(a + b*x)^(5/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(11/6)/(b*x+a)**(5/6),x)
```

```
[Out] Timed out
```



```
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n + 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rule 210

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Module[{r = Numerator[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r - s*Cos[(2*k*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r + s*Cos[(2*k*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^2*Int[1/(r^2 - s^2*x^2), x])/(a*n) + Dist[(2*r)/(a*n), Sum[u, {k, 1, (n - 2)/4}], x], x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && NegQ[a/b]
```

Rule 240

```
Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c},
```

$x] \&\& \text{NeQ}[b^2 - 4*a*c, 0]$

Rule 628

$\text{Int}[\frac{(d_.) + (e_.)x}{(a_.) + (b_.)x + (c_.)x^2}, x_Symbol] \rightarrow \text{Simp}[\frac{d \cdot \text{Log}[\text{RemoveContent}[a + bx + cx^2, x]]}{b}, x] /;$ $\text{FreeQ}\{a, b, c, d, e\}, x] \&\& \text{EqQ}[2*c*d - b*e, 0]$

Rule 634

$\text{Int}[\frac{(d_.) + (e_.)x}{(a_.) + (b_.)x + (c_.)x^2}, x_Symbol] \rightarrow \text{Dist}[\frac{2*c*d - b*e}{2*c}, \text{Int}[1/(a + bx + cx^2), x], x] + \text{Dist}[e/(2*c), \text{Int}[\frac{b + 2*c*x}{a + bx + cx^2}, x], x] /;$ $\text{FreeQ}\{a, b, c, d, e\}, x] \&\& \text{NeQ}[2*c*d - b*e, 0] \&\& \text{NeQ}[b^2 - 4*a*c, 0] \&\& \text{!NiceSqrtQ}[b^2 - 4*a*c]$

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{5/6}}{(a+bx)^{5/6}} dx &= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{b} + \frac{(5(bc-ad)) \int \frac{1}{(a+bx)^{5/6} \sqrt[6]{c+dx}} dx}{6b} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{b} + \frac{(5(bc-ad)) \operatorname{Subst} \left(\int \frac{1}{\sqrt[6]{c-\frac{ad}{b}+\frac{dx^6}{b}}} dx, x, \sqrt[6]{a+bx} \right)}{b^2} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{b} + \frac{(5(bc-ad)) \operatorname{Subst} \left(\int \frac{1}{1-\frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{b^2} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{b} + \frac{(5(bc-ad)) \operatorname{Subst} \left(\int \frac{\sqrt[6]{b}-\frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b}-\sqrt[6]{b} \sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{3b^{11/6}} + \frac{(5(bc-ad)) \operatorname{Subst} \left(\int \frac{1}{\sqrt[3]{b}-\sqrt[6]{b} \sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{4b^{5/3}} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{b} + \frac{5(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3b^{11/6} \sqrt[6]{d}} + \frac{(5(bc-ad)) \operatorname{Subst} \left(\int \frac{1}{\sqrt[3]{b}-\sqrt[6]{b} \sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{4b^{5/3}} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{b} + \frac{5(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3b^{11/6} \sqrt[6]{d}} - \frac{5(bc-ad) \log \left(\sqrt[3]{b} + \frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[3]{c+dx}} - \frac{\sqrt[6]{b} \sqrt[6]{c+dx}}{\sqrt[3]{d}} \right)}{12b^{11/6} \sqrt[6]{d}} \\
&= \frac{\sqrt[6]{a+bx} (c+dx)^{5/6}}{b} - \frac{5(bc-ad) \tan^{-1} \left(\frac{1-\frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3} b^{11/6} \sqrt[6]{d}} + \frac{5(bc-ad) \tan^{-1} \left(\frac{1+\frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3} b^{11/6} \sqrt[6]{d}} + \frac{5(bc-ad) \log \left(\sqrt[3]{b} + \frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[3]{c+dx}} - \frac{\sqrt[6]{b} \sqrt[6]{c+dx}}{\sqrt[3]{d}} \right)}{12b^{11/6} \sqrt[6]{d}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 71, normalized size = 0.19

$$\frac{6\sqrt[6]{a+bx} (c+dx)^{5/6} {}_2F_1 \left(-\frac{5}{6}, \frac{1}{6}; \frac{7}{6}; \frac{d(a+bx)}{ad-bc} \right)}{b \left(\frac{b(c+dx)}{bc-ad} \right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/6)/(a + b*x)^(5/6), x]

[Out] (6*(a + b*x)^(1/6)*(c + d*x)^(5/6)*Hypergeometric2F1[-5/6, 1/6, 7/6, (d*(a + b*x))/(-b*c) + a*d])/(b*((b*(c + d*x))/(b*c - a*d))^(5/6))

fricas [B] time = 0.85, size = 2997, normalized size = 7.93

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(5/6),x, algorithm="fricas")

[Out]
$$\frac{1}{12} \cdot (20 \sqrt{3}) \cdot b \cdot \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^{11} d) \right)^{1/6} \cdot \arctan \left(\frac{1}{3} \cdot (2 \sqrt{3}) \cdot (b^{10} c d - a b^9 d^2) \cdot (b x + a)^{1/6} \cdot (d x + c)^{5/6} \right) \cdot \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^{11} d) \right)^{5/6} + 2 \sqrt{3} \cdot (b^9 d^2 x + b^9 c d) \cdot \sqrt{\left((b^3 c - a b^2 d) \cdot (b x + a)^{1/6} \cdot (d x + c)^{5/6} \cdot \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^{11} d) \right)^{1/6} + (b^2 c^2 - 2 a b c d + a^2 d^2) \cdot (b x + a)^{1/3} \cdot (d x + c)^{2/3} + (b^4 d x + b^4 c) \cdot \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^{11} d) \right)^{1/3} \right) / (d x + c)} \cdot \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^{11} d) \right)^{5/6} + \sqrt{3} \cdot (b^6 c^7 - 6 a b^5 c^6 d + 15 a^2 b^4 c^5 d^2 - 20 a^3 b^3 c^4 d^3 + 15 a^4 b^2 c^3 d^4 - 6 a^5 b c^2 d^5 + a^6 c d^6 + (b^6 c^6 d - 6 a b^5 c^5 d^2 + 15 a^2 b^4 c^4 d^3 - 20 a^3 b^3 c^3 d^4 + 15 a^4 b^2 c^2 d^5 - 6 a^5 b c d^6 + a^6 d^7) \cdot x) / (b^6 c^7 - 6 a b^5 c^6 d + 15 a^2 b^4 c^5 d^2 - 20 a^3 b^3 c^4 d^3 + 15 a^4 b^2 c^3 d^4 - 6 a^5 b c^2 d^5 + a^6 c d^6 + (b^6 c^6 d - 6 a b^5 c^5 d^2 + 15 a^2 b^4 c^4 d^3 - 20 a^3 b^3 c^3 d^4 + 15 a^4 b^2 c^2 d^5 - 6 a^5 b c d^6 + a^6 d^7) \cdot x)) + 20 \sqrt{3} \cdot b \cdot \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^{11} d) \right)^{1/6} \cdot \arctan \left(\frac{1}{3} \cdot (2 \sqrt{3}) \cdot (b^{10} c d - a b^9 d^2) \cdot (b x + a)^{1/6} \cdot (d x + c)^{5/6} \right) \cdot \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^{11} d) \right)^{5/6} + 2 \sqrt{3} \cdot (b^9 d^2 x + b^9 c d) \cdot \sqrt{\left((b^3 c - a b^2 d) \cdot (b x + a)^{1/6} \cdot (d x + c)^{5/6} \cdot \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^{11} d) \right)^{1/6} - (b^2 c^2 - 2 a b c d + a^2 d^2) \cdot (b x + a)^{1/3} \cdot (d x + c)^{2/3} - (b^4 d x + b^4 c) \cdot \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^{11} d) \right)^{1/3} \right) / (d x + c)} \cdot \left((b^6 c^6 - 6 a b^5 c^5 d + 15 a^2 b^4 c^4 d^2 - 20 a^3 b^3 c^3 d^3 + 15 a^4 b^2 c^2 d^4 - 6 a^5 b c d^5 + a^6 d^6) / (b^{11} d) \right)^{5/6} - \sqrt{3} \cdot (b^6 c^7 - 6 a b^5 c^6 d + 15 a^2 b^4 c^5 d^2 - 20 a^3 b^3 c^4 d^3 + 15 a^4 b^2 c^3 d^4 - 6 a^5 b c^2 d^5 + a^6 c d^6 + (b^6 c^6 d - 6 a b^5 c^5 d^2 + 15 a^2 b^4 c^4 d^3 - 20 a^3 b^3 c^3 d^4 + 15 a^4 b^2 c^2 d^5 - 6 a^5 b c d^6 + a^6 d^7) \cdot x) / (b^6 c^7 - 6 a b^5 c^6 d + 15 a^2 b^4 c^5 d^2 - 20 a^3 b^3 c^4 d^3 + 15 a^4 b^2 c^3 d^4 - 6 a^5 b c^2 d^5 + a^6 c d^6 + (b^6 c^6 d - 6 a b^5 c^5 d^2 + 15 a^2 b^4 c^4 d^3 - 20 a^3 b^3 c^3 d^4 + 15 a^4 b^2 c^2 d^5 - 6 a^5 b c d^6 + a^6 d^7) \cdot x))$$

$$\begin{aligned}
& c^5d^2 + 15a^2b^4c^4d^3 - 20a^3b^3c^3d^4 + 15a^4b^2c^2d^5 - 6a^5b^2c^2d^6 + a^6d^7) * x) + 5b * ((b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * \log(25 * ((b^3c - a^2b^2d) * (b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * (d^5x + c)^{(5/6)} * ((b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} + (b^2c^2 - 2a^2b^2c^2d + a^2d^2) * (b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/3)} * (d^5x + c)^{(2/3)} + (b^4d^5x + b^4c) * ((b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/3)}) / (d^5x + c) - 5b * ((b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * \log(-25 * ((b^3c - a^2b^2d) * (b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * (b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} - (b^2c^2 - 2a^2b^2c^2d + a^2d^2) * (b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/3)} * (d^5x + c)^{(2/3)} - (b^4d^5x + b^4c) * ((b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/3)}) / (d^5x + c) + 10b * ((b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * \log(-5 * ((b^3c - a^2b^2d) * (b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * (b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * (d^5x + c)^{(5/6)} + (b^2d^5x + b^2c) * ((b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)}) / (d^5x + c) - 10b * ((b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * \log(-5 * ((b^3c - a^2b^2d) * (b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * (b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * (d^5x + c)^{(5/6)} - (b^2d^5x + b^2c) * ((b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)}) / (d^5x + c) + 12 * (b^6c^6 - 6a^5b^5c^5d + 15a^4b^4c^4d^2 - 20a^3b^3c^3d^3 + 15a^2b^2c^2d^4 - 6a^5b^5c^5d + a^6d^6) / (b^{11}d))^{(1/6)} * (d^5x + c)^{(5/6)} / b
\end{aligned}$$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(5/6),x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(5/6)/(b*x+a)^(5/6),x)`

[Out] `int((d*x+c)^(5/6)/(b*x+a)^(5/6),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(5/6)/(b*x+a)^(5/6),x, algorithm="maxima")`

[Out] `integrate((d*x + c)^(5/6)/(b*x + a)^(5/6), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{5/6}}{(a + bx)^{5/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(5/6)/(a + b*x)^(5/6),x)`

[Out] `int((c + d*x)^(5/6)/(a + b*x)^(5/6), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{6}}}{(a + bx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(5/6)/(b*x+a)**(5/6),x)`

[Out] `Integral((c + d*x)**(5/6)/(a + b*x)**(5/6), x)`

$$3.1826 \quad \int \frac{1}{(a+bx)^{5/6} \sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=309

$$\frac{\log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2b^{5/6} \sqrt[6]{d}} + \frac{\log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2b^{5/6} \sqrt[6]{d}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt{3} \sqrt[6]{b} \sqrt[6]{c+dx}}\right)}{b^{5/6} \sqrt[6]{d}} + \dots$$

[Out] $2*\operatorname{arctanh}(d^{1/6}*(b*x+a)^{1/6}/b^{1/6}/(d*x+c)^{1/6})/b^{5/6}/d^{1/6}-1/2*\ln(b^{1/3}+d^{1/3}*(b*x+a)^{1/3}/(d*x+c)^{1/3}-b^{1/6}*d^{1/6}*(b*x+a)^{1/6}/(d*x+c)^{1/6})/b^{5/6}/d^{1/6}+1/2*\ln(b^{1/3}+d^{1/3}*(b*x+a)^{1/3}/(d*x+c)^{1/3}+b^{1/6}*d^{1/6}*(b*x+a)^{1/6}/(d*x+c)^{1/6})/b^{5/6}/d^{1/6}+\operatorname{arctan}(-1/3*3^{1/2}+2/3*d^{1/6}*(b*x+a)^{1/6}/b^{1/6}/(d*x+c)^{1/6})*3^{1/2})/b^{5/6}/d^{1/6}+\operatorname{arctan}(1/3*3^{1/2}+2/3*d^{1/6}*(b*x+a)^{1/6}/b^{1/6}/(d*x+c)^{1/6})*3^{1/2})/b^{5/6}/d^{1/6}$

Rubi [A] time = 0.44, antiderivative size = 309, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 8, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.421$, Rules used = {63, 240, 210, 634, 618, 204, 628, 208}

$$\frac{\log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2b^{5/6} \sqrt[6]{d}} + \frac{\log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2b^{5/6} \sqrt[6]{d}} - \frac{\sqrt{3} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt{3} \sqrt[6]{b} \sqrt[6]{c+dx}}\right)}{b^{5/6} \sqrt[6]{d}} + \dots$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((a + b*x)^{5/6}*(c + d*x)^{1/6}), x]$

[Out] $-((\operatorname{Sqrt}[3]*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{1/6}*(a + b*x)^{1/6})/(\operatorname{Sqrt}[3]*b^{1/6}*(c + d*x)^{1/6})])/(b^{5/6}*d^{1/6})) + (\operatorname{Sqrt}[3]*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{1/6}*(a + b*x)^{1/6})/(\operatorname{Sqrt}[3]*b^{1/6}*(c + d*x)^{1/6})])/(b^{5/6}*d^{1/6})) + (2*\operatorname{ArcTanh}[(d^{1/6}*(a + b*x)^{1/6})/b^{1/6}/(c + d*x)^{1/6}])/(b^{5/6}*d^{1/6}) - \operatorname{Log}[b^{1/3} + (d^{1/3}*(a + b*x)^{1/3})/(c + d*x)^{1/3} - (b^{1/6}*d^{1/6}*(a + b*x)^{1/6})/(c + d*x)^{1/6}]/(2*b^{5/6}*d^{1/6}) + \operatorname{Log}[b^{1/3} + (d^{1/3}*(a + b*x)^{1/3})/(c + d*x)^{1/3} + (b^{1/6}*d^{1/6}*(a + b*x)^{1/6})/(c + d*x)^{1/6}]/(2*b^{5/6}*d^{1/6})$

Rule 63

$\operatorname{Int}[(a_. + (b_.)*(x_.))^{(m_.)}*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \operatorname{With}[\{p = \operatorname{Denominator}[m]\}, \operatorname{Dist}[p/b, \operatorname{Subst}[\operatorname{Int}[x^{(p*(m + 1) - 1)}*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^{1/p}], x]] /; \operatorname{FreeQ}[\{a, b, c, d\}, x] \&\& \operatorname{NeQ}[b*c - a*d, 0] \&\& \operatorname{LtQ}[-1, m, 0] \&\& \operatorname{LeQ}[-1, n, 0] \&\& \operatorname{LeQ}[\operatorname{Denominator}[n], \operatorname{Denominator}[m]] \&\& \operatorname{IntLinearQ}[a, b, c, d, m, n, x]$

Rule 204

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rule 210

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Module[{r = Numerator[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r - s*Cos[(2*k*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r + s*Cos[(2*k*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^2*Int[1/(r^2 - s^2*x^2), x])/(a*n) + Dist[(2*r)/(a*n), Sum[u, {k, 1, (n - 2)/4}], x, x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && NegQ[a/b]

Rule 240

Int[((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + 1/n), Subst[Int[1/(1 - b*x^n)^(p + 1/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegerQ[p + 1/n]

Rule 618

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rule 628

Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]

Rule 634

Int[((d_.) + (e_.)*(x_))/((a_) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), Int[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ

$[2*c*d - b*e, 0] \ \&\& \ \text{NeQ}[b^2 - 4*a*c, 0] \ \&\& \ \text{!NiceSqrtQ}[b^2 - 4*a*c]$

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a+bx)^{5/6} \sqrt[6]{c+dx}} dx &= \frac{6 \text{Subst} \left(\int \frac{1}{\sqrt[6]{c-\frac{ad}{b}+\frac{dx^6}{b}}} dx, x, \sqrt[6]{a+bx} \right)}{b} \\
 &= \frac{6 \text{Subst} \left(\int \frac{1}{1-\frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{b} \\
 &= \frac{2 \text{Subst} \left(\int \frac{\sqrt[6]{b}-\frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b}-\sqrt[6]{b} \sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{b^{5/6}} + \frac{2 \text{Subst} \left(\int \frac{\sqrt[6]{b}+\frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b}+\sqrt[6]{b} \sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{b^{5/6}} \\
 &= \frac{2 \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{b^{5/6} \sqrt[6]{d}} + \frac{3 \text{Subst} \left(\int \frac{1}{\sqrt[3]{b}-\sqrt[6]{b} \sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2b^{2/3}} + \frac{3 \text{Subst} \left(\int \frac{1}{\sqrt[3]{b}+\sqrt[6]{b} \sqrt[6]{d}x+\sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2b^{2/3}} \\
 &= \frac{2 \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{b^{5/6} \sqrt[6]{d}} - \frac{\log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} - \frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2b^{5/6} \sqrt[6]{d}} + \frac{\log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2b^{5/6} \sqrt[6]{d}} \\
 &= -\frac{\sqrt{3} \tan^{-1} \left(\frac{1-\frac{2 \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{b^{5/6} \sqrt[6]{d}} + \frac{\sqrt{3} \tan^{-1} \left(\frac{1+\frac{2 \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{b^{5/6} \sqrt[6]{d}} + \frac{2 \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{b^{5/6} \sqrt[6]{d}} - \frac{\log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2b^{5/6} \sqrt[6]{d}}
 \end{aligned}$$

Mathematica [C] time = 0.04, size = 71, normalized size = 0.23

$$\frac{6 \sqrt[6]{a+bx} \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1 \left(\frac{1}{6}, \frac{1}{6}; \frac{7}{6}; \frac{d(a+bx)}{ad-bc} \right)}{b \sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/6)*(c + d*x)^(1/6)),x]

[Out] (6*(a + b*x)^(1/6)*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[1/6, 1/6, 7/6, (d*(a + b*x))/(-b*c + a*d)]/(b*(c + d*x)^(1/6))

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(5/6)/(d*x+c)^(1/6),x)`

[Out] `int(1/(b*x+a)^(5/6)/(d*x+c)^(1/6),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/6)/(d*x+c)^(1/6),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(5/6)*(d*x + c)^(1/6)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{6}}(c+dx)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(5/6)*(c + d*x)^(1/6)),x)`

[Out] `int(1/((a + b*x)^(5/6)*(c + d*x)^(1/6)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{5}{6}}\sqrt[6]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/6)/(d*x+c)**(1/6),x)`

[Out] `Integral(1/((a + b*x)**(5/6)*(c + d*x)**(1/6)), x)`

$$3.1827 \quad \int \frac{1}{(a+bx)^{5/6}(c+dx)^{7/6}} dx$$

Optimal. Leaf size=30

$$\frac{6\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}(bc-ad)}$$

[Out] $6*(b*x+a)^{(1/6)/(-a*d+b*c)/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.00, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{6\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)^{(5/6})*(c + d*x)^{(7/6})),x]$

[Out] $(6*(a + b*x)^{(1/6}))/((b*c - a*d)*(c + d*x)^{(1/6}))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \text{ :> Simp} [(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}]/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{EqQ}[m + n + 2, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{7/6}} dx = \frac{6\sqrt[6]{a+bx}}{(bc-ad)\sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$\frac{6\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/((a + b*x)^{(5/6})*(c + d*x)^{(7/6})),x]$

[Out] $(6*(a + b*x)^{(1/6)})/((b*c - a*d)*(c + d*x)^{(1/6)})$

fricas [A] time = 0.94, size = 42, normalized size = 1.40

$$\frac{6 (bx + a)^{\frac{1}{6}} (dx + c)^{\frac{5}{6}}}{bc^2 - acd + (bcd - ad^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/6)/(d*x+c)^(7/6),x, algorithm="fricas")`

[Out] $6*(b*x + a)^{(1/6)}*(d*x + c)^{(5/6)}/(b*c^2 - a*c*d + (b*c*d - a*d^2)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{6}}(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/6)/(d*x+c)^(7/6),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(5/6)*(d*x + c)^(7/6)), x)`

maple [A] time = 0.00, size = 27, normalized size = 0.90

$$-\frac{6 (bx + a)^{\frac{1}{6}}}{(dx + c)^{\frac{1}{6}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(5/6)/(d*x+c)^(7/6),x)`

[Out] $-6*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}/(a*d-b*c)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{6}}(dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/6)/(d*x+c)^(7/6),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(5/6)*(d*x + c)^(7/6)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{1}{(a + bx)^{5/6} (c + dx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/6)*(c + d*x)^(7/6)), x)

[Out] int(1/((a + b*x)^(5/6)*(c + d*x)^(7/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{5/6} (c + dx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/6)/(d*x+c)**(7/6), x)

[Out] Integral(1/((a + b*x)**(5/6)*(c + d*x)**(7/6)), x)

$$3.1828 \quad \int \frac{1}{(a+bx)^{5/6}(c+dx)^{13/6}} dx$$

Optimal. Leaf size=66

$$\frac{36b\sqrt[6]{a+bx}}{7\sqrt[6]{c+dx}(bc-ad)^2} + \frac{6\sqrt[6]{a+bx}}{7(c+dx)^{7/6}(bc-ad)}$$

[Out] $6/7*(b*x+a)^{(1/6)/(-a*d+b*c)/(d*x+c)^{(7/6)+36/7*b*(b*x+a)^{(1/6)/(-a*d+b*c)^2/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.01, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{36b\sqrt[6]{a+bx}}{7\sqrt[6]{c+dx}(bc-ad)^2} + \frac{6\sqrt[6]{a+bx}}{7(c+dx)^{7/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/6)*(c + d*x)^(13/6)),x]

[Out] $(6*(a + b*x)^{(1/6)})/(7*(b*c - a*d)*(c + d*x)^{(7/6)}) + (36*b*(a + b*x)^{(1/6)})/(7*(b*c - a*d)^2*(c + d*x)^{(1/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{13/6}} dx = \frac{6\sqrt[6]{a+bx}}{7(bc-ad)(c+dx)^{7/6}} + \frac{(6b) \int \frac{1}{(a+bx)^{5/6}(c+dx)^{7/6}} dx}{7(bc-ad)}$$

$$= \frac{6\sqrt[6]{a+bx}}{7(bc-ad)(c+dx)^{7/6}} + \frac{36b\sqrt[6]{a+bx}}{7(bc-ad)^2\sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.02, size = 46, normalized size = 0.70

$$\frac{6\sqrt[6]{a+bx}(-ad+7bc+6bdx)}{7(c+dx)^{7/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/6)*(c + d*x)^(13/6)), x]

[Out] (6*(a + b*x)^(1/6)*(7*b*c - a*d + 6*b*d*x))/(7*(b*c - a*d)^2*(c + d*x)^(7/6))

fricas [B] time = 0.86, size = 118, normalized size = 1.79

$$\frac{6(6bdx + 7bc - ad)(bx + a)^{\frac{1}{6}}(dx + c)^{\frac{5}{6}}}{7(b^2c^4 - 2abc^3d + a^2c^2d^2 + (b^2c^2d^2 - 2abcd^3 + a^2d^4)x^2 + 2(b^2c^3d - 2abc^2d^2 + a^2cd^3)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(13/6), x, algorithm="fricas")

[Out] 6/7*(6*b*d*x + 7*b*c - a*d)*(b*x + a)^(1/6)*(d*x + c)^(5/6)/(b^2*c^4 - 2*a*b*c^3*d + a^2*c^2*d^2 + (b^2*c^2*d^2 - 2*a*b*c*d^3 + a^2*d^4)*x^2 + 2*(b^2*c^3*d - 2*a*b*c^2*d^2 + a^2*c*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(13/6), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/6)*(d*x + c)^(13/6)), x)

maple [A] time = 0.01, size = 53, normalized size = 0.80

$$-\frac{6(bx+a)^{\frac{1}{6}}(-6bdx+ad-7bc)}{7(dx+c)^{\frac{7}{6}}(a^2d^2-2abcd+b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/6)/(d*x+c)^(13/6),x)

[Out] -6/7*(b*x+a)^(1/6)*(-6*b*d*x+a*d-7*b*c)/(d*x+c)^(7/6)/(a^2*d^2-2*a*b*c*d+b^2*c^2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(13/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/6)*(d*x + c)^(13/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{1}{(a+bx)^{\frac{5}{6}}(c+dx)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(5/6)*(c + d*x)^(13/6)),x)

[Out] int(1/((a + b*x)^(5/6)*(c + d*x)^(13/6)), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(5/6)/(d*x+c)**(13/6),x)

[Out] Timed out

$$3.1829 \quad \int \frac{1}{(a+bx)^{5/6}(c+dx)^{19/6}} dx$$

Optimal. Leaf size=101

$$\frac{432b^2\sqrt[6]{a+bx}}{91\sqrt[6]{c+dx}(bc-ad)^3} + \frac{72b\sqrt[6]{a+bx}}{91(c+dx)^{7/6}(bc-ad)^2} + \frac{6\sqrt[6]{a+bx}}{13(c+dx)^{13/6}(bc-ad)}$$

[Out] $6/13*(b*x+a)^{(1/6)/(-a*d+b*c)/(d*x+c)^{(13/6)+72/91*b*(b*x+a)^{(1/6)/(-a*d+b*c)^2/(d*x+c)^{(7/6)+432/91*b^2*(b*x+a)^{(1/6)/(-a*d+b*c)^3/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 101, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{432b^2\sqrt[6]{a+bx}}{91\sqrt[6]{c+dx}(bc-ad)^3} + \frac{72b\sqrt[6]{a+bx}}{91(c+dx)^{7/6}(bc-ad)^2} + \frac{6\sqrt[6]{a+bx}}{13(c+dx)^{13/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/6)*(c + d*x)^(19/6)), x]

[Out] $(6*(a + b*x)^{(1/6)}/(13*(b*c - a*d)*(c + d*x)^{(13/6)) + (72*b*(a + b*x)^{(1/6)}/(91*(b*c - a*d)^2*(c + d*x)^{(7/6)) + (432*b^2*(a + b*x)^{(1/6)}/(91*(b*c - a*d)^3*(c + d*x)^{(1/6))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/6}(c+dx)^{19/6}} dx &= \frac{6\sqrt[6]{a+bx}}{13(bc-ad)(c+dx)^{13/6}} + \frac{(12b) \int \frac{1}{(a+bx)^{5/6}(c+dx)^{13/6}} dx}{13(bc-ad)} \\
&= \frac{6\sqrt[6]{a+bx}}{13(bc-ad)(c+dx)^{13/6}} + \frac{72b\sqrt[6]{a+bx}}{91(bc-ad)^2(c+dx)^{7/6}} + \frac{(72b^2) \int \frac{1}{(a+bx)^{5/6}(c+dx)^{7/6}} dx}{91(bc-ad)^2} \\
&= \frac{6\sqrt[6]{a+bx}}{13(bc-ad)(c+dx)^{13/6}} + \frac{72b\sqrt[6]{a+bx}}{91(bc-ad)^2(c+dx)^{7/6}} + \frac{432b^2\sqrt[6]{a+bx}}{91(bc-ad)^3\sqrt[6]{c+dx}}
\end{aligned}$$

Mathematica [A] time = 0.04, size = 77, normalized size = 0.76

$$\frac{6\sqrt[6]{a+bx} (7a^2d^2 - 2abd(13c + 6dx) + b^2(91c^2 + 156cdx + 72d^2x^2))}{91(c+dx)^{13/6}(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/6)*(c + d*x)^(19/6)), x]

[Out] (6*(a + b*x)^(1/6)*(7*a^2*d^2 - 2*a*b*d*(13*c + 6*d*x) + b^2*(91*c^2 + 156*c*d*x + 72*d^2*x^2)))/(91*(b*c - a*d)^3*(c + d*x)^(13/6))

fricas [B] time = 0.62, size = 252, normalized size = 2.50

$$\frac{6(72b^2d^2x^2 + 91b^2c^2 - 26abcd + 7a^2d^2 + 12(13b^2cd - abd^2)x)}{91(b^3c^6 - 3ab^2c^5d + 3a^2bc^4d^2 - a^3c^3d^3 + (b^3c^3d^3 - 3ab^2c^2d^4 + 3a^2bcd^5 - a^3d^6)x^3 + 3(b^3c^4d^2 - 3ab^2c^3d^3 + 3a^2bcd^4 - a^3c^2d^5)x^2 + 3(b^3c^5d - 3a^2b^2c^4d^2 + 3a^2b^2c^3d^3 - a^3c^2d^4)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(19/6), x, algorithm="fricas")

[Out] 6/91*(72*b^2*d^2*x^2 + 91*b^2*c^2 - 26*a*b*c*d + 7*a^2*d^2 + 12*(13*b^2*c*d - a*b*d^2)*x)*(b*x + a)^(1/6)*(d*x + c)^(5/6)/(b^3*c^6 - 3*a*b^2*c^5*d + 3*a^2*b*c^4*d^2 - a^3*c^3*d^3 + (b^3*c^3*d^3 - 3*a*b^2*c^2*d^4 + 3*a^2*b*c*d^5 - a^3*d^6)*x^3 + 3*(b^3*c^4*d^2 - 3*a*b^2*c^3*d^3 + 3*a^2*b*c^2*d^4 - a^3*c*d^5)*x^2 + 3*(b^3*c^5*d - 3*a*b^2*c^4*d^2 + 3*a^2*b*c^3*d^3 - a^3*c^2*d^4)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/6)/(d*x+c)^(19/6),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(5/6)*(d*x + c)^(19/6)), x)`

maple [A] time = 0.01, size = 105, normalized size = 1.04

$$\frac{6 (bx + a)^{\frac{1}{6}} \left(72b^2x^2d^2 - 12abd^2x + 156b^2cdx + 7a^2d^2 - 26abcd + 91b^2c^2 \right)}{91 (dx + c)^{\frac{13}{6}} \left(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(5/6)/(d*x+c)^(19/6),x)`

[Out] `-6/91*(b*x+a)^(1/6)*(72*b^2*d^2*x^2-12*a*b*d^2*x+156*b^2*c*d*x+7*a^2*d^2-26*a*b*c*d+91*b^2*c^2)/(d*x+c)^(13/6)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{5}{6}}(dx + c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(5/6)/(d*x+c)^(19/6),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(5/6)*(d*x + c)^(19/6)), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{5/6} (c + dx)^{19/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(5/6)*(c + d*x)^(19/6)),x)`

[Out] `int(1/((a + b*x)^(5/6)*(c + d*x)^(19/6)), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(5/6)/(d*x+c)**(19/6),x)`

[Out] Timed out

$$3.1830 \quad \int \frac{1}{(a+bx)^{5/6}(c+dx)^{25/6}} dx$$

Optimal. Leaf size=136

$$\frac{7776b^3\sqrt[6]{a+bx}}{1729\sqrt[6]{c+dx}(bc-ad)^4} + \frac{1296b^2\sqrt[6]{a+bx}}{1729(c+dx)^{7/6}(bc-ad)^3} + \frac{108b\sqrt[6]{a+bx}}{247(c+dx)^{13/6}(bc-ad)^2} + \frac{6\sqrt[6]{a+bx}}{19(c+dx)^{19/6}(bc-ad)}$$

[Out] $6/19*(b*x+a)^{(1/6)/(-a*d+b*c)/(d*x+c)^{(19/6)}+108/247*b*(b*x+a)^{(1/6)/(-a*d+b*c)^2/(d*x+c)^{(13/6)}+1296/1729*b^2*(b*x+a)^{(1/6)/(-a*d+b*c)^3/(d*x+c)^{(7/6)}+7776/1729*b^3*(b*x+a)^{(1/6)/(-a*d+b*c)^4/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.03, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{7776b^3\sqrt[6]{a+bx}}{1729\sqrt[6]{c+dx}(bc-ad)^4} + \frac{1296b^2\sqrt[6]{a+bx}}{1729(c+dx)^{7/6}(bc-ad)^3} + \frac{108b\sqrt[6]{a+bx}}{247(c+dx)^{13/6}(bc-ad)^2} + \frac{6\sqrt[6]{a+bx}}{19(c+dx)^{19/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(5/6)*(c + d*x)^(25/6)),x]

[Out] $(6*(a + b*x)^{(1/6)})/(19*(b*c - a*d)*(c + d*x)^{(19/6)}) + (108*b*(a + b*x)^{(1/6)})/(247*(b*c - a*d)^2*(c + d*x)^{(13/6)}) + (1296*b^2*(a + b*x)^{(1/6)})/(1729*(b*c - a*d)^3*(c + d*x)^{(7/6)}) + (7776*b^3*(a + b*x)^{(1/6)})/(1729*(b*c - a*d)^4*(c + d*x)^{(1/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[m] && !IntegerQ[n] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n])) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{5/6}(c+dx)^{25/6}} dx &= \frac{6\sqrt[6]{a+bx}}{19(bc-ad)(c+dx)^{19/6}} + \frac{(18b) \int \frac{1}{(a+bx)^{5/6}(c+dx)^{19/6}} dx}{19(bc-ad)} \\
&= \frac{6\sqrt[6]{a+bx}}{19(bc-ad)(c+dx)^{19/6}} + \frac{108b\sqrt[6]{a+bx}}{247(bc-ad)^2(c+dx)^{13/6}} + \frac{(216b^2) \int \frac{1}{(a+bx)^{5/6}(c+dx)^{13/6}}}{247(bc-ad)^2} \\
&= \frac{6\sqrt[6]{a+bx}}{19(bc-ad)(c+dx)^{19/6}} + \frac{108b\sqrt[6]{a+bx}}{247(bc-ad)^2(c+dx)^{13/6}} + \frac{1296b^2\sqrt[6]{a+bx}}{1729(bc-ad)^3(c+dx)^{7/6}} \\
&= \frac{6\sqrt[6]{a+bx}}{19(bc-ad)(c+dx)^{19/6}} + \frac{108b\sqrt[6]{a+bx}}{247(bc-ad)^2(c+dx)^{13/6}} + \frac{1296b^2\sqrt[6]{a+bx}}{1729(bc-ad)^3(c+dx)^{7/6}}
\end{aligned}$$

Mathematica [A] time = 0.06, size = 118, normalized size = 0.87

$$\frac{6\sqrt[6]{a+bx} \left(-91a^3d^3 + 21a^2bd^2(19c+6dx) - 3ab^2d(247c^2 + 228cdx + 72d^2x^2) + b^3(1729c^3 + 4446c^2dx + 4104cd^2x^2 + 1296d^3x^3) \right)}{1729(c+dx)^{19/6}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(5/6)*(c + d*x)^(25/6)), x]

[Out] (6*(a + b*x)^(1/6)*(-91*a^3*d^3 + 21*a^2*b*d^2*(19*c + 6*d*x) - 3*a*b^2*d*(247*c^2 + 228*c*d*x + 72*d^2*x^2) + b^3*(1729*c^3 + 4446*c^2*d*x + 4104*c*d^2*x^2 + 1296*d^3*x^3)))/(1729*(b*c - a*d)^4*(c + d*x)^(19/6))

fricas [B] time = 0.92, size = 420, normalized size = 3.09

$$\frac{6 \left(1296 b^3 d^3 x^3 + 1729 b^3 c^3 - 741 a b^2 c^2 d \right)}{1729 \left(b^4 c^8 - 4 a b^3 c^7 d + 6 a^2 b^2 c^6 d^2 - 4 a^3 b c^5 d^3 + a^4 c^4 d^4 + \left(b^4 c^4 d^4 - 4 a b^3 c^3 d^5 + 6 a^2 b^2 c^2 d^6 - 4 a^3 b c d^7 + a^4 d^8 \right) x \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(25/6), x, algorithm="fricas")

[Out] 6/1729*(1296*b^3*d^3*x^3 + 1729*b^3*c^3 - 741*a*b^2*c^2*d + 399*a^2*b*c*d^2 - 91*a^3*d^3 + 216*(19*b^3*c*d^2 - a*b^2*d^3)*x^2 + 18*(247*b^3*c^2*d - 38*a*b^2*c*d^2 + 7*a^2*b*d^3)*x)*(b*x + a)^(1/6)*(d*x + c)^(5/6)/(b^4*c^8 - 4*a*b^3*c^7*d + 6*a^2*b^2*c^6*d^2 - 4*a^3*b*c^5*d^3 + a^4*c^4*d^4 + (b^4*c^4*d^4 - 4*a*b^3*c^3*d^5 + 6*a^2*b^2*c^2*d^6 - 4*a^3*b*c*d^7 + a^4*d^8)*x^4 + 4*(b^4*c^5*d^3 - 4*a*b^3*c^4*d^4 + 6*a^2*b^2*c^3*d^5 - 4*a^3*b*c^2*d^6 + a

$$\begin{aligned} &^4*c*d^7)*x^3 + 6*(b^4*c^6*d^2 - 4*a*b^3*c^5*d^3 + 6*a^2*b^2*c^4*d^4 - 4*a^3*b*c^3*d^5 + a^4*c^2*d^6)*x^2 + 4*(b^4*c^7*d - 4*a*b^3*c^6*d^2 + 6*a^2*b^2*c^5*d^3 - 4*a^3*b*c^4*d^4 + a^4*c^3*d^5)*x \end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{25}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(25/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(5/6)*(d*x + c)^(25/6)), x)

maple [A] time = 0.01, size = 171, normalized size = 1.26

$$\frac{6(bx+a)^{\frac{1}{6}}(-1296b^3d^3x^3 + 216ab^2d^3x^2 - 4104b^3cd^2x^2 - 126a^2bd^3x + 684ab^2cd^2x - 4446b^3c^2dx + 91a^3d^3 - 1729(dx+c)^{\frac{19}{6}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4))}{1729(dx+c)^{\frac{19}{6}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(5/6)/(d*x+c)^(25/6),x)

[Out]
$$\begin{aligned} &-6/1729*(b*x+a)^{(1/6)}*(-1296*b^3*d^3*x^3+216*a*b^2*d^3*x^2-4104*b^3*c*d^2*x^2-126*a^2*b*d^3*x+684*a*b^2*c*d^2*x-4446*b^3*c^2*d*x+91*a^3*d^3-399*a^2*b*c*d^2+741*a*b^2*c^2*d-1729*b^3*c^3)/(d*x+c)^{(19/6)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4) \end{aligned}$$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{25}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(5/6)/(d*x+c)^(25/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(5/6)*(d*x + c)^(25/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{5/6}(c+dx)^{25/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.


```
[In] int(1/((a + b*x)^(5/6)*(c + d*x)^(25/6)), x)
```

```
[Out] int(1/((a + b*x)^(5/6)*(c + d*x)^(25/6)), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(5/6)/(d*x+c)**(25/6), x)
```

```
[Out] Timed out
```

$$3.1831 \quad \int \frac{(c+dx)^{13/6}}{(a+bx)^{7/6}} dx$$

Optimal. Leaf size=449

$$\frac{91\sqrt[6]{d}(bc-ad)^2 \log\left(-\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{19/6}} + \frac{91\sqrt[6]{d}(bc-ad)^2 \log\left(\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{19/6}} + \dots$$

[Out] $91/12*d*(-a*d+b*c)*(b*x+a)^{(5/6)}*(d*x+c)^{(1/6)}/b^3+13/2*d*(b*x+a)^{(5/6)}*(d*x+c)^{(7/6)}/b^2-6*(d*x+c)^{(13/6)}/b/(b*x+a)^{(1/6)}+91/36*d^{(1/6)}*(-a*d+b*c)^2*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(19/6)}-91/144*d^{(1/6)}*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(19/6)}+91/144*d^{(1/6)}*(-a*d+b*c)^2*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(19/6)}-91/72*d^{(1/6)}*(-a*d+b*c)^2*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(19/6)}*3^{(1/2)}-91/72*d^{(1/6)}*(-a*d+b*c)^2*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(19/6)}*3^{(1/2)}$

Rubi [A] time = 0.66, antiderivative size = 449, normalized size of antiderivative = 1.00, number of steps used = 15, number of rules used = 10, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.526$, Rules used = {47, 50, 63, 331, 296, 634, 618, 204, 628, 208}

$$\frac{13d(a+bx)^{5/6}(c+dx)^{7/6}}{2b^2} + \frac{91d(a+bx)^{5/6}\sqrt[6]{c+dx}(bc-ad)}{12b^3} - \frac{91\sqrt[6]{d}(bc-ad)^2 \log\left(-\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{144b^{19/6}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c+dx)^{(13/6)}/(a+bx)^{(7/6)}, x]$

[Out] $(91*d*(b*c-a*d)*(a+bx)^{(5/6)}*(c+dx)^{(1/6)})/(12*b^3) + (13*d*(a+bx)^{(5/6)}*(c+dx)^{(7/6)})/(2*b^2) - (6*(c+dx)^{(13/6)})/(b*(a+bx)^{(1/6)}) + (91*d^{(1/6)}*(b*c-a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a+bx)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c+dx)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(19/6)}) - (91*d^{(1/6)}*(b*c-a*d)^2*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a+bx)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c+dx)^{(1/6)})]/(24*\operatorname{Sqrt}[3]*b^{(19/6)}) + (91*d^{(1/6)}*(b*c-a*d)^2*\operatorname{ArcTanh}[(d^{(1/6)}*(a+bx)^{(1/6)})/(b^{(1/6)}*(c+dx)^{(1/6)})]/(36*b^{(19/6)}) - (91*d^{(1/6)}*(b*c-a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a+bx)^{(1/3)})/(c+dx)^{(1/3)} - (b^{(1/6)}*d^{(1/6)}*(a+bx)^{(1/6)})/(c+dx)^{(1/6)}]/(144*b^{(19/6)}) + (91*d^{(1/6)}*(b*c-a*d)^2*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a+bx)^{(1/3)})/(c+dx)^{(1/3)} + (b^{(1/6)}*d^{(1/6)}*(a+bx)^{(1/6)})/(c+dx)^{(1/6)}]/(144*b^{(19/6)})$

Rule 47

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + 1)), x] - Dist[(d*n)/(b*(m + 1)), I
nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !Intege
rQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]
```

Rule 50

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ
[m, 0] && (!IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 204

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rule 296

```
Int[(x_)^(m_.)/((a_) + (b_.)*(x_)^(n_.)), x_Symbol] := Module[{r = Numerator
[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r*cos
[(2*k*m*Pi)/n] - s*cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 - 2*r*s*cos[(2*k*Pi)/n]*
x + s^2*x^2), x] + Int[(r*cos[(2*k*m*Pi)/n] + s*cos[(2*k*(m + 1)*Pi)/n]*x)/
(r^2 + 2*r*s*cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^(m + 2)*Int[1/(r^2 - s^
2*x^2), x])/(a*n*s^m) + Dist[(2*r^(m + 1))/(a*n*s^m), Sum[u, {k, 1, (n - 2)
```

/4}], x], x]] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && IGtQ[m, 0] && LtQ[m, n - 1] && NegQ[a/b]

Rule 331

Int[(x_)^(m_)*((a_) + (b_)*(x_)^(n_))^(p_), x_Symbol] :> Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]

Rule 618

Int[((a_) + (b_)*(x_) + (c_)*(x_)^2)^(-1), x_Symbol] :> Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]

Rule 628

Int[((d_) + (e_)*(x_))/((a_) + (b_)*(x_) + (c_)*(x_)^2), x_Symbol] :> Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]

Rule 634

Int[((d_) + (e_)*(x_))/((a_) + (b_)*(x_) + (c_)*(x_)^2), x_Symbol] :> Dist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), Int[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{13/6}}{(a+bx)^{7/6}} dx &= -\frac{6(c+dx)^{13/6}}{b\sqrt[6]{a+bx}} + \frac{(13d) \int \frac{(c+dx)^{7/6}}{\sqrt[6]{a+bx}} dx}{b} \\
&= \frac{13d(a+bx)^{5/6}(c+dx)^{7/6}}{2b^2} - \frac{6(c+dx)^{13/6}}{b\sqrt[6]{a+bx}} + \frac{(91d(bc-ad)) \int \frac{\sqrt[6]{c+dx}}{\sqrt[6]{a+bx}} dx}{12b^2} \\
&= \frac{91d(bc-ad)(a+bx)^{5/6}\sqrt[6]{c+dx}}{12b^3} + \frac{13d(a+bx)^{5/6}(c+dx)^{7/6}}{2b^2} - \frac{6(c+dx)^{13/6}}{b\sqrt[6]{a+bx}} + \frac{(91d(bc-ad))}{12b^2} \\
&= \frac{91d(bc-ad)(a+bx)^{5/6}\sqrt[6]{c+dx}}{12b^3} + \frac{13d(a+bx)^{5/6}(c+dx)^{7/6}}{2b^2} - \frac{6(c+dx)^{13/6}}{b\sqrt[6]{a+bx}} + \frac{(91d(bc-ad))}{12b^2} \\
&= \frac{91d(bc-ad)(a+bx)^{5/6}\sqrt[6]{c+dx}}{12b^3} + \frac{13d(a+bx)^{5/6}(c+dx)^{7/6}}{2b^2} - \frac{6(c+dx)^{13/6}}{b\sqrt[6]{a+bx}} + \frac{(91d(bc-ad))}{12b^2} \\
&= \frac{91d(bc-ad)(a+bx)^{5/6}\sqrt[6]{c+dx}}{12b^3} + \frac{13d(a+bx)^{5/6}(c+dx)^{7/6}}{2b^2} - \frac{6(c+dx)^{13/6}}{b\sqrt[6]{a+bx}} + \frac{(91\sqrt[3]{d}(bc-ad))}{12b^2} \\
&= \frac{91d(bc-ad)(a+bx)^{5/6}\sqrt[6]{c+dx}}{12b^3} + \frac{13d(a+bx)^{5/6}(c+dx)^{7/6}}{2b^2} - \frac{6(c+dx)^{13/6}}{b\sqrt[6]{a+bx}} + \frac{91\sqrt[6]{d}(bc-ad)}{12b^2} \\
&= \frac{91d(bc-ad)(a+bx)^{5/6}\sqrt[6]{c+dx}}{12b^3} + \frac{13d(a+bx)^{5/6}(c+dx)^{7/6}}{2b^2} - \frac{6(c+dx)^{13/6}}{b\sqrt[6]{a+bx}} + \frac{91\sqrt[6]{d}(bc-ad)}{12b^2} \\
&= \frac{91d(bc-ad)(a+bx)^{5/6}\sqrt[6]{c+dx}}{12b^3} + \frac{13d(a+bx)^{5/6}(c+dx)^{7/6}}{2b^2} - \frac{6(c+dx)^{13/6}}{b\sqrt[6]{a+bx}} + \frac{91\sqrt[6]{d}(bc-ad)}{12b^2}
\end{aligned}$$

Mathematica [C] time = 0.08, size = 71, normalized size = 0.16

$$-\frac{6(c+dx)^{13/6} {}_2F_1\left(-\frac{13}{6}, -\frac{1}{6}; \frac{5}{6}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{13/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(13/6)/(a + b*x)^(7/6),x]

[Out] (-6*(c + d*x)^(13/6)*Hypergeometric2F1[-13/6, -1/6, 5/6, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(a + b*x)^(1/6)*((b*(c + d*x))/(b*c - a*d))^(13/6))

fricas [B] time = 1.40, size = 5690, normalized size = 12.67

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(13/6)/(b*x+a)^(7/6),x, algorithm="fricas")

[Out]
$$\begin{aligned} & -1/144*(364*\sqrt{3}*(b^4*x + a*b^3)*((b^{12}*c^{12}*d - 12*a*b^{11}*c^{11}*d^2 + 66 \\ & *a^2*b^{10}*c^{10}*d^3 - 220*a^3*b^9*c^9*d^4 + 495*a^4*b^8*c^8*d^5 - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - 792*a^7*b^5*c^5*d^8 + 495*a^8*b^4*c^4*d^9 \\ & - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b^2*c^2*d^{11} - 12*a^{11}*b*c*d^{12} + a^{12}*d^{13})/b^{19})^{1/6}*\arctan(-1/3*(2*\sqrt{3}*(b^{18}*c^2 - 2*a*b^{17}*c*d + a^2*b^{16}* \\ & d^2)*(b*x + a)^{5/6}*(d*x + c)^{1/6}*((b^{12}*c^{12}*d - 12*a*b^{11}*c^{11}*d^2 + 6 \\ & 6*a^2*b^{10}*c^{10}*d^3 - 220*a^3*b^9*c^9*d^4 + 495*a^4*b^8*c^8*d^5 - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - 792*a^7*b^5*c^5*d^8 + 495*a^8*b^4*c^4*d^9 \\ & - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b^2*c^2*d^{11} - 12*a^{11}*b*c*d^{12} + a^{12}*d^{13})/b^{19})^{5/6} - 2*\sqrt{3}*(b^{17}*x + a*b^{16})*\sqrt{((b^5*c^2 - 2*a*b^4*c*d \\ & + a^2*b^3*d^2)*(b*x + a)^{5/6}*(d*x + c)^{1/6}*((b^{12}*c^{12}*d - 12*a*b^{11}*c^{11}*d^2 + 66*a^2*b^{10}*c^{10}*d^3 - 220*a^3*b^9*c^9*d^4 + 495*a^4*b^8*c^8*d^5 \\ & - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - 792*a^7*b^5*c^5*d^8 + 495*a^8*b^4*c^4*d^9 - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b^2*c^2*d^{11} - 12*a^{11}*b*c*d^{12} + a^{12}*d^{13})/b^{19})^{1/6} + (b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 \\ & - 4*a^3*b*c*d^3 + a^4*d^4)*(b*x + a)^{2/3}*(d*x + c)^{1/3} + (b^7*x + a*b^6) \\ &)*((b^{12}*c^{12}*d - 12*a*b^{11}*c^{11}*d^2 + 66*a^2*b^{10}*c^{10}*d^3 - 220*a^3*b^9*c^9*d^4 + 495*a^4*b^8*c^8*d^5 - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - \\ & 792*a^7*b^5*c^5*d^8 + 495*a^8*b^4*c^4*d^9 - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b^2*c^2*d^{11} - 12*a^{11}*b*c*d^{12} + a^{12}*d^{13})/b^{19})^{1/3})/(b*x + a)*((b^{12} \\ & *c^{12}*d - 12*a*b^{11}*c^{11}*d^2 + 66*a^2*b^{10}*c^{10}*d^3 - 220*a^3*b^9*c^9*d^4 + \\ & 495*a^4*b^8*c^8*d^5 - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - 792*a^7*b^5*c^5*d^8 + 495*a^8*b^4*c^4*d^9 - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b^2*c^2*d^{11} - \\ & 12*a^{11}*b*c*d^{12} + a^{12}*d^{13})/b^{19})^{5/6} + \sqrt{3}*(a*b^{12}*c^{12}*d - \\ & 12*a^2*b^{11}*c^{11}*d^2 + 66*a^3*b^{10}*c^{10}*d^3 - 220*a^4*b^9*c^9*d^4 + 495*a^5*b^8*c^8*d^5 - 792*a^6*b^7*c^7*d^6 + 924*a^7*b^6*c^6*d^7 - 792*a^8*b^5*c^5*d^8 + 495*a^9*b^4*c^4*d^9 - 220*a^{10}*b^3*c^3*d^{10} + 66*a^{11}*b^2*c^2*d^{11} - \\ & 12*a^{12}*b*c*d^{12} + a^{13}*d^{13} + (b^{13}*c^{12}*d - 12*a*b^{12}*c^{11}*d^2 + 66*a^2*b^{11}*c^{10}*d^3 - 220*a^3*b^{10}*c^9*d^4 + 495*a^4*b^9*c^8*d^5 - 792*a^5*b^8*c^7*d^6 + 924*a^6*b^7*c^6*d^7 - 792*a^7*b^6*c^5*d^8 + 495*a^8*b^5*c^4*d^9 - 2 \\ & 20*a^9*b^4*c^3*d^{10} + 66*a^{10}*b^3*c^2*d^{11} - 12*a^{11}*b^2*c*d^{12} + a^{12}*b*d^{13})/b^{19})^{1/3} \end{aligned}$$

$$\begin{aligned}
& 13)x)) / (a^2 b^9 c^9 d^4 + 495 a^5 b^8 c^8 d^5 - 792 a^6 b^7 c^7 d^6 + 924 a^7 b^6 c^6 d^7 - 792 a^8 b^5 c^5 d^8 + 495 a^9 b^4 c^4 d^9 - 220 a^{10} b^3 c^3 d^{10} \\
& + 66 a^{11} b^2 c^2 d^{11} - 12 a^{12} b c d^{12} + a^{13} d^{13} + (b^{13} c^{12} d - 12 a b^{12} c^{11} d^2 + 66 a^2 b^{11} c^{10} d^3 - 220 a^3 b^{10} c^9 d^4 + 495 a^4 b^9 c^8 d^5 \\
& - 792 a^5 b^8 c^7 d^6 + 924 a^6 b^7 c^6 d^7 - 792 a^7 b^6 c^5 d^8 + 495 a^8 b^5 c^4 d^9 - 220 a^9 b^4 c^3 d^{10} + 66 a^{10} b^3 c^2 d^{11} - 12 a^{11} b^2 c d^{12} + a^{12} b d^{13}) x)) \\
& + 364 \sqrt{3} (b^4 x + a b^3) ((b^{12} c^{12} d - 12 a b^{11} c^{11} d^2 + 66 a^2 b^{10} c^{10} d^3 - 220 a^3 b^9 c^9 d^4 + 495 a^4 b^8 c^8 d^5 - 792 a^5 b^7 c^7 d^6 + 924 a^6 b^6 c^6 d^7 - 792 a^7 b^5 c^5 d^8 \\
& + 495 a^8 b^4 c^4 d^9 - 220 a^9 b^3 c^3 d^{10} + 66 a^{10} b^2 c^2 d^{11} - 12 a^{11} b c d^{12} + a^{12} d^{13}) / b^{19})^{1/6} \arctan(-1/3 (2 \sqrt{3} (b^{18} c^2 - 2 a b^{17} c d + a^2 b^{16} d^2) (b x + a)^{5/6} (d x + c)^{1/6} \\
& ((b^{12} c^{12} d - 12 a b^{11} c^{11} d^2 + 66 a^2 b^{10} c^{10} d^3 - 220 a^3 b^9 c^9 d^4 + 495 a^4 b^8 c^8 d^5 - 792 a^5 b^7 c^7 d^6 + 924 a^6 b^6 c^6 d^7 - 792 a^7 b^5 c^5 d^8 \\
& + 495 a^8 b^4 c^4 d^9 - 220 a^9 b^3 c^3 d^{10} + 66 a^{10} b^2 c^2 d^{11} - 12 a^{11} b c d^{12} + a^{12} d^{13}) / b^{19})^{5/6} - 2 \sqrt{3} (b^{17} x + a b^{16}) \sqrt{3} \\
& ((b^5 c^2 - 2 a b^4 c d + a^2 b^3 d^2) (b x + a)^{5/6} (d x + c)^{1/6} ((b^{12} c^{12} d - 12 a b^{11} c^{11} d^2 + 66 a^2 b^{10} c^{10} d^3 - 220 a^3 b^9 c^9 d^4 + 495 a^4 b^8 c^8 d^5 \\
& - 792 a^5 b^7 c^7 d^6 + 924 a^6 b^6 c^6 d^7 - 792 a^7 b^5 c^5 d^8 + 495 a^8 b^4 c^4 d^9 - 220 a^9 b^3 c^3 d^{10} + 66 a^{10} b^2 c^2 d^{11} - 12 a^{11} b c d^{12} + a^{12} d^{13}) / b^{19})^{1/6} \\
& - (b^4 c^4 - 4 a b^3 c^3 d + 6 a^2 b^2 c^2 d^2 - 4 a^3 b c d^3 + a^4 d^4) (b x + a)^{2/3} (d x + c)^{1/3} - (b^7 x + a b^6) ((b^{12} c^{12} d - 12 a b^{11} c^{11} d^2 + 66 a^2 b^{10} c^{10} d^3 - 220 a^3 b^9 c^9 d^4 + 495 a^4 b^8 c^8 d^5 \\
& - 792 a^5 b^7 c^7 d^6 + 924 a^6 b^6 c^6 d^7 - 792 a^7 b^5 c^5 d^8 + 495 a^8 b^4 c^4 d^9 - 220 a^9 b^3 c^3 d^{10} + 66 a^{10} b^2 c^2 d^{11} - 12 a^{11} b c d^{12} + a^{12} d^{13}) / b^{19})^{1/3} \\
&)) / (b x + a) ((b^{12} c^{12} d - 12 a b^{11} c^{11} d^2 + 66 a^2 b^{10} c^{10} d^3 - 220 a^3 b^9 c^9 d^4 + 495 a^4 b^8 c^8 d^5 - 792 a^5 b^7 c^7 d^6 + 924 a^6 b^6 c^6 d^7 - 792 a^7 b^5 c^5 d^8 \\
& + 495 a^8 b^4 c^4 d^9 - 220 a^9 b^3 c^3 d^{10} + 66 a^{10} b^2 c^2 d^{11} - 12 a^{11} b c d^{12} + a^{12} d^{13}) / b^{19})^{5/6} - \sqrt{3} (a b^{12} c^{12} d - 12 a^2 b^{11} c^{11} d^2 + 66 a^3 b^{10} c^{10} d^3 - 2 \\
& 20 a^4 b^9 c^9 d^4 + 495 a^5 b^8 c^8 d^5 - 792 a^6 b^7 c^7 d^6 + 924 a^7 b^6 c^6 d^7 - 792 a^8 b^5 c^5 d^8 + 495 a^9 b^4 c^4 d^9 - 220 a^{10} b^3 c^3 d^{10} + 66 a^{11} b^2 c^2 d^{11} - 12 a^{12} b c d^{12} + a^{13} d^{13} \\
& + (b^{13} c^{12} d - 12 a b^{12} c^{11} d^2 + 66 a^2 b^{11} c^{10} d^3 - 220 a^3 b^{10} c^9 d^4 + 495 a^4 b^9 c^8 d^5 - 792 a^5 b^8 c^7 d^6 + 924 a^6 b^7 c^6 d^7 - 792 a^7 b^6 c^5 d^8 \\
& + 495 a^8 b^5 c^4 d^9 - 220 a^9 b^4 c^3 d^{10} + 66 a^{10} b^3 c^2 d^{11} - 12 a^{11} b^2 c d^{12} + a^{12} b d^{13}) x)) / (a b^{12} c^{12} d - 12 a^2 b^{11} c^{11} d^2 + 66 a^3 b^{10} c^{10} d^3 - 220 a^4 b^9 c^9 d^4 + 495 a^5 b^8 c^8 d^5 \\
& - 792 a^6 b^7 c^7 d^6 + 924 a^7 b^6 c^6 d^7 - 792 a^8 b^5 c^5 d^8 + 495 a^9 b^4 c^4 d^9 - 220 a^{10} b^3 c^3 d^{10} + 66 a^{11} b^2 c^2 d^{11} - 12 a^{12} b c d^{12} + a^{13} d^{13} + (b^{13} c^{12} d - 12 a b^{12} c^{11} d^2 + 66 a^2 b^{11} c^{10} d^3 - 220 a^3 b^{10} c^9 d^4 + 495 a^4 b^9 c^8 d^5 \\
& - 792 a^5 b^8 c^7 d^6 + 924 a^6 b^7 c^6 d^7 - 792 a^7 b^6 c^5 d^8 + 495 a^8 b^5 c^4 d^9 - 220 a^9 b^4 c^3 d^{10} + 66 a^{10} b^3 c^2 d^{11} - 12 a^{11} b^2 c d^{12} + a^{12} b d^{13}) x)) / (a b^{12} c^{12} d - 12 a^2 b^{11} c^{11} d^2 + 66 a^3 b^{10} c^{10} d^3 - 220 a^4 b^9 c^9 d^4 + 495 a^5 b^8 c^8 d^5 - 792 a^6 b^7 c^7 d^6 + 924 a^7 b^6 c^6 d^7 - 792 a^8 b^5 c^5 d^8 + 495 a^9 b^4 c^4 d^9 - 220 a^{10} b^3 c^3 d^{10} + 66 a^{11} b^2 c^2 d^{11} - 12 a^{12} b c d^{12} + a^{13} d^{13} + (b^{13} c^{12} d - 12 a b^{12} c^{11} d^2 + 66 a^2 b^{11} c^{10} d^3 - 220 a^3 b^{10} c^9 d^4 + 495 a^4 b^9 c^8 d^5 - 792 a^5 b^8 c^7 d^6 + 924 a^6 b^7 c^6 d^7 - 792 a^7 b^6 c^5 d^8 + 495 a^8 b^5 c^4 d^9 - 220 a^9 b^4 c^3 d^{10} + 66 a^{10} b^3 c^2 d^{11} - 12 a^{11} b^2 c d^{12} + a^{12} b d^{13}) x))
\end{aligned}$$

$$\begin{aligned}
& *a^{10}b^3c^2d^{11} - 12a^{11}b^2cd^{12} + a^{12}b^2d^{13})x)) - 91*(b^4x + a \\
& b^3)*((b^{12}c^{12}d - 12a*b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 + 495a^4b^8c^8d^5 - 792a^5b^7c^7d^6 + 924a^6b^6c^6d^7 \\
& - 792a^7b^5c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66a^{10}b^2c^2d^{11} - 12a^{11}b^2cd^{12} + a^{12}d^{13})/b^{19})^{(1/6)}*\log(8281*((b^5c^2 \\
& c^2 - 2a*b^4c*d + a^2b^3d^2)*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*((b^{12}c^{12}d - 12a*b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 + 495 \\
& *a^4b^8c^8d^5 - 792a^5b^7c^7d^6 + 924a^6b^6c^6d^7 - 792a^7b^5c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66a^{10}b^2c^2d^{11} \\
& - 12a^{11}b^2cd^{12} + a^{12}d^{13})/b^{19})^{(1/6)} + (b^4c^4 - 4a*b^3c^3d + 6 \\
& *a^2b^2c^2d^2 - 4a^3b^2c^2d^2 + a^4d^4)*(b*x + a)^{(2/3)}*(d*x + c)^{(1/3)} \\
& + (b^7x + a*b^6)*((b^{12}c^{12}d - 12a*b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 + 495a^4b^8c^8d^5 - 792a^5b^7c^7d^6 + 924a^6b^6c^6d^7 - 792a^7b^5c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3 \\
& *d^{10} + 66a^{10}b^2c^2d^{11} - 12a^{11}b^2cd^{12} + a^{12}d^{13})/b^{19})^{(1/3)})/ \\
& (b*x + a)) + 91*(b^4x + a*b^3)*((b^{12}c^{12}d - 12a*b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 + 495a^4b^8c^8d^5 - 792a^5b^7c^7 \\
& *d^6 + 924a^6b^6c^6d^7 - 792a^7b^5c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66a^{10}b^2c^2d^{11} - 12a^{11}b^2cd^{12} + a^{12}d^{13})/ \\
& b^{19})^{(1/6)}*\log(-8281*((b^5c^2 - 2a*b^4c*d + a^2b^3d^2)*(b*x + a)^{(5/6)} \\
&)*(d*x + c)^{(1/6)}*((b^{12}c^{12}d - 12a*b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 \\
& - 220a^3b^9c^9d^4 + 495a^4b^8c^8d^5 - 792a^5b^7c^7d^6 + 924a^6b^6c^6d^7 - 792a^7b^5c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3 \\
& *d^{10} + 66a^{10}b^2c^2d^{11} - 12a^{11}b^2cd^{12} + a^{12}d^{13})/b^{19})^{(1/6)} - \\
& (b^4c^4 - 4a*b^3c^3d + 6a^2b^2c^2d^2 - 4a^3b^2c^2d^2 + a^4d^4)*(b*x \\
& + a)^{(2/3)}*(d*x + c)^{(1/3)} - (b^7x + a*b^6)*((b^{12}c^{12}d - 12a*b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 + 495a^4b^8c^8d^5 - \\
& 792a^5b^7c^7d^6 + 924a^6b^6c^6d^7 - 792a^7b^5c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66a^{10}b^2c^2d^{11} - 12a^{11}b^2cd^{12} + a^{12}d^{13})/b^{19})^{(1/3)})/ \\
& (b*x + a)) - 182*(b^4x + a*b^3)*((b^{12}c^{12}d - 12a*b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 + 495a^4b^8c^8d^5 - 792a^5b^7c^7 \\
& *d^6 + 924a^6b^6c^6d^7 - 792a^7b^5c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66a^{10}b^2c^2d^{11} - 12a^{11}b^2cd^{12} + a^{12}d^{13})/b^{19})^{(1/6)}*\log(91*((b^2c^2 - 2a*b*c*d + a^2 \\
& *d^2)*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)} + (b^4x + a*b^3)*((b^{12}c^{12}d - 12a \\
& *b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 + 495a^4b^8c^8d^5 - 792a^5b^7c^7d^6 + 924a^6b^6c^6d^7 - 792a^7b^5c^5d^8 + \\
& 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66a^{10}b^2c^2d^{11} - 12a^{11}b^2cd^{12} + a^{12}d^{13})/b^{19})^{(1/6)})/(b*x + a)) + 182*(b^4x + a*b^3)*((b^{12}c^{12}d - 12a*b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 \\
& + 495a^4b^8c^8d^5 - 792a^5b^7c^7d^6 + 924a^6b^6c^6d^7 - 792a^7b^5c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66a^{10}b^2c^2d^{11} - 12a^{11}b^2cd^{12} + a^{12}d^{13})/b^{19})^{(1/6)}*\log(91*((b^2c^2 - 2a*b*c \\
& *d + a^2d^2)*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)} - (b^4x + a*b^3)*((b^{12}c^{12}d - 12a*b^{11}c^{11}d^2 + 66a^2b^{10}c^{10}d^3 - 220a^3b^9c^9d^4 + 495 \\
& *a^4b^8c^8d^5 - 792a^5b^7c^7d^6 + 924a^6b^6c^6d^7 - 792a^7b^5c^5d^8 + 495a^8b^4c^4d^9 - 220a^9b^3c^3d^{10} + 66a^{10}b^2c^2d^{11} - 12a^{11}b^2cd^{12} + a^{12}d^{13})/b^{19})^{(1/6)}))
\end{aligned}$$

$*a^4*b^8*c^8*d^5 - 792*a^5*b^7*c^7*d^6 + 924*a^6*b^6*c^6*d^7 - 792*a^7*b^5*c^5*d^8 + 495*a^8*b^4*c^4*d^9 - 220*a^9*b^3*c^3*d^{10} + 66*a^{10}*b^2*c^2*d^{11} - 12*a^{11}*b*c*d^{12} + a^{12}*d^{13})/(b^{19})^{(1/6)} / (b*x + a) - 12*(6*b^2*d^2*x^2 - 72*b^2*c^2 + 169*a*b*c*d - 91*a^2*d^2 + (25*b^2*c*d - 13*a*b*d^2)*x)*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)} / (b^4*x + a*b^3)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{13}{6}}}{(bx + a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(13/6)/(b*x+a)^(7/6),x, algorithm="giac")

[Out] integrate((d*x + c)^(13/6)/(b*x + a)^(7/6), x)

maple [F] time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{13}{6}}}{(bx + a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(13/6)/(b*x+a)^(7/6),x)

[Out] int((d*x+c)^(13/6)/(b*x+a)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{13}{6}}}{(bx + a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(13/6)/(b*x+a)^(7/6),x, algorithm="maxima")

[Out] integrate((d*x + c)^(13/6)/(b*x + a)^(7/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{13/6}}{(a + bx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^(13/6)/(a + b*x)^(7/6),x)
```

```
[Out] int((c + d*x)^(13/6)/(a + b*x)^(7/6), x)
```

```
sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00
```

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**(13/6)/(b*x+a)**(7/6),x)
```

```
[Out] Timed out
```

$$3.1832 \quad \int \frac{(c+dx)^{7/6}}{(a+bx)^{7/6}} dx$$

Optimal. Leaf size=403

$$\frac{7\sqrt[6]{d}(bc-ad)\log\left(-\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}+\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}}+\sqrt[3]{b}\right)}{12b^{13/6}}+\frac{7\sqrt[6]{d}(bc-ad)\log\left(\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}+\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}}+\sqrt[3]{b}\right)}{12b^{13/6}}+\dots$$

[Out] $7*d*(b*x+a)^{(5/6)}*(d*x+c)^{(1/6)}/b^2-6*(d*x+c)^{(7/6)}/b/(b*x+a)^{(1/6)}+7/3*d^{(1/6)}*(-a*d+b*c)*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)})/b^{(13/6)}-7/12*d^{(1/6)}*(-a*d+b*c)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(13/6)}+7/12*d^{(1/6)}*(-a*d+b*c)*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)}/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)})/b^{(13/6)}-7/6*d^{(1/6)}*(-a*d+b*c)*\arctan(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(13/6)}*3^{(1/2)}-7/6*d^{(1/6)}*(-a*d+b*c)*\arctan(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)}/(d*x+c)^{(1/6)}*3^{(1/2)})/b^{(13/6)}*3^{(1/2)}$

Rubi [A] time = 0.60, antiderivative size = 403, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 10, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.526$, Rules used = {47, 50, 63, 331, 296, 634, 618, 204, 628, 208}

$$\frac{7d(a+bx)^{5/6}\sqrt[6]{c+dx}}{b^2}-\frac{7\sqrt[6]{d}(bc-ad)\log\left(-\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}+\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}}+\sqrt[3]{b}\right)}{12b^{13/6}}+\frac{7\sqrt[6]{d}(bc-ad)\log\left(\frac{\sqrt[6]{b}\sqrt[6]{d}\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}}+\frac{\sqrt[3]{d}\sqrt[3]{a+bx}}{\sqrt[3]{c+dx}}+\sqrt[3]{b}\right)}{12b^{13/6}}+\dots$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c+dx)^{(7/6)}/(a+bx)^{(7/6)},x]$

[Out] $(7*d*(a+b*x)^{(5/6)}*(c+d*x)^{(1/6)}/b^2-(6*(c+d*x)^{(7/6)}/(b*(a+b*x)^{(1/6)})+(7*d^{(1/6)}*(b*c-a*d)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3]-(2*d^{(1/6)}*(a+b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c+d*x)^{(1/6)})])/(2*\operatorname{Sqrt}[3]*b^{(13/6)})-(7*d^{(1/6)}*(b*c-a*d)*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3]+(2*d^{(1/6)}*(a+b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c+d*x)^{(1/6)})])/(2*\operatorname{Sqrt}[3]*b^{(13/6)})+(7*d^{(1/6)}*(b*c-a*d)*\operatorname{ArcTanh}(d^{(1/6)}*(a+b*x)^{(1/6)}/(b^{(1/6)}*(c+d*x)^{(1/6)})))/(3*b^{(13/6)})-(7*d^{(1/6)}*(b*c-a*d)*\operatorname{Log}[b^{(1/3)}+(d^{(1/3)}*(a+b*x)^{(1/3)})/(c+d*x)^{(1/3)}-(b^{(1/6)}*d^{(1/6)}*(a+b*x)^{(1/6)})/(c+d*x)^{(1/6)}])/(12*b^{(13/6)})+(7*d^{(1/6)}*(b*c-a*d)*\operatorname{Log}[b^{(1/3)}+(d^{(1/3)}*(a+b*x)^{(1/3)})/(c+d*x)^{(1/3)}+(b^{(1/6)}*d^{(1/6)}*(a+b*x)^{(1/6)})/(c+d*x)^{(1/6)}])/(12*b^{(13/6)})$

Rule 47

$\operatorname{Int}[(a_.)+(b_.)*(x_.))^{(m_.)*((c_.)+(d_.)*(x_.))^{(n_.)},x_Symbol] \rightarrow \operatorname{Simp}[(a+b*x)^{(m+1)}*(c+d*x)^n/(b*(m+1)),x]-\operatorname{Dist}[(d*n)/(b*(m+1)),I]$

```

nt[(a + b*x)^(m + 1)*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b, c, d}, x] &&
  NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) &&
  !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) &
& IntLinearQ[a, b, c, d, m, n, x]

```

Rule 50

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^n)/(b*(m + n + 1)), x] + Dist[(n*(b*c - a*d))/
(b*(m + n + 1)), Int[(a + b*x)^m*(c + d*x)^(n - 1), x], x] /; FreeQ[{a, b,
c, d}, x] && NeQ[b*c - a*d, 0] && GtQ[n, 0] && NeQ[m + n + 1, 0] && !(IGtQ[
m, 0] && ( !IntegerQ[n] || (GtQ[m, 0] && LtQ[m - n, 0]))) && !ILtQ[m + n
+ 2, 0] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 63

```

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[
b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

```

Rule 204

```

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[
-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[
a, 0] || LtQ[b, 0])

```

Rule 208

```

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

```

Rule 296

```

Int[(x_)^(m_.)/((a_) + (b_.)*(x_)^(n_)), x_Symbol] := Module[{r = Numerator
[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r*cos
[(2*k*m*Pi)/n] - s*cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 - 2*r*s*cos[(2*k*Pi)/n]*
x + s^2*x^2), x] + Int[(r*cos[(2*k*m*Pi)/n] + s*cos[(2*k*(m + 1)*Pi)/n]*x)/
(r^2 + 2*r*s*cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^(m + 2)*Int[1/(r^2 - s^
2*x^2), x])/(a*n*s^m) + Dist[(2*r^(m + 1))/(a*n*s^m), Sum[u, {k, 1, (n - 2)
/4}], x], x]] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && IGtQ[m, 0] && Lt
Q[m, n - 1] && NegQ[a/b]

```

Rule 331

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]
```

Rule 618

```
Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c}, x] && NeQ[b^2 - 4*a*c, 0]
```

Rule 628

```
Int[((d_) + (e_.)*(x_))/((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Simp[(d*Log[RemoveContent[a + b*x + c*x^2, x]])/b, x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[2*c*d - b*e, 0]
```

Rule 634

```
Int[((d_.) + (e_.)*(x_))/((a_) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[(2*c*d - b*e)/(2*c), Int[1/(a + b*x + c*x^2), x], x] + Dist[e/(2*c), Int[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; FreeQ[{a, b, c, d, e}, x] && NeQ[2*c*d - b*e, 0] && NeQ[b^2 - 4*a*c, 0] && !NiceSqrtQ[b^2 - 4*a*c]
```

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^{7/6}}{(a+bx)^{7/6}} dx &= -\frac{6(c+dx)^{7/6}}{b\sqrt[6]{a+bx}} + \frac{(7d) \int \frac{\sqrt[6]{c+dx}}{\sqrt[6]{a+bx}} dx}{b} \\
&= \frac{7d(a+bx)^{5/6} \sqrt[6]{c+dx}}{b^2} - \frac{6(c+dx)^{7/6}}{b\sqrt[6]{a+bx}} + \frac{(7d(bc-ad)) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{5/6}} dx}{6b^2} \\
&= \frac{7d(a+bx)^{5/6} \sqrt[6]{c+dx}}{b^2} - \frac{6(c+dx)^{7/6}}{b\sqrt[6]{a+bx}} + \frac{(7d(bc-ad)) \operatorname{Subst} \left(\int \frac{x^4}{\left(c - \frac{ad}{b} + \frac{dx^6}{b}\right)^{5/6}} dx, x, \sqrt[6]{a+bx} \right)}{b^3} \\
&= \frac{7d(a+bx)^{5/6} \sqrt[6]{c+dx}}{b^2} - \frac{6(c+dx)^{7/6}}{b\sqrt[6]{a+bx}} + \frac{(7d(bc-ad)) \operatorname{Subst} \left(\int \frac{x^4}{1 - \frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{b^3} \\
&= \frac{7d(a+bx)^{5/6} \sqrt[6]{c+dx}}{b^2} - \frac{6(c+dx)^{7/6}}{b\sqrt[6]{a+bx}} + \frac{(7\sqrt[3]{d}(bc-ad)) \operatorname{Subst} \left(\int \frac{-\frac{\sqrt[6]{b}}{2} - \frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{3b^{13/6}} \\
&= \frac{7d(a+bx)^{5/6} \sqrt[6]{c+dx}}{b^2} - \frac{6(c+dx)^{7/6}}{b\sqrt[6]{a+bx}} + \frac{7\sqrt[6]{d}(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3b^{13/6}} - \frac{7\sqrt[6]{d}(bc-ad)}{3b^{13/6}} \\
&= \frac{7d(a+bx)^{5/6} \sqrt[6]{c+dx}}{b^2} - \frac{6(c+dx)^{7/6}}{b\sqrt[6]{a+bx}} + \frac{7\sqrt[6]{d}(bc-ad) \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3b^{13/6}} - \frac{7\sqrt[6]{d}(bc-ad) \log \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{3b^{13/6}} \\
&= \frac{7d(a+bx)^{5/6} \sqrt[6]{c+dx}}{b^2} - \frac{6(c+dx)^{7/6}}{b\sqrt[6]{a+bx}} + \frac{7\sqrt[6]{d}(bc-ad) \tan^{-1} \left(\frac{1 - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3} b^{13/6}} - \frac{7\sqrt[6]{d}(bc-ad) \tan^{-1} \left(\frac{1 - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{2\sqrt{3} b^{13/6}}
\end{aligned}$$

Mathematica [C] time = 0.06, size = 71, normalized size = 0.18

$$-\frac{6(c+dx)^{7/6} {}_2F_1 \left(-\frac{7}{6}, -\frac{1}{6}; \frac{5}{6}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad} \right)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(7/6)/(a + b*x)^(7/6), x]

$$\begin{aligned} & c^2*d^5 - 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x)/(a*b^6*c^6*d - 6*a^2*b^5*c^5*d^2 \\ & + 15*a^3*b^4*c^4*d^3 - 20*a^4*b^3*c^3*d^4 + 15*a^5*b^2*c^2*d^5 - 6*a^6*b*c \\ & *d^6 + a^7*d^7 + (b^7*c^6*d - 6*a*b^6*c^5*d^2 + 15*a^2*b^5*c^4*d^3 - 20*a^3 \\ & *b^4*c^3*d^4 + 15*a^4*b^3*c^2*d^5 - 6*a^5*b^2*c*d^6 + a^6*b*d^7)*x)) + 7*(b \\ & ^3*x + a*b^2)*((b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 - 20*a^3*b \\ & ^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7)/b^13)^(1/6)*log(\\ & 49*((b^3*c - a*b^2*d)*(b*x + a)^(5/6)*(d*x + c)^(1/6))*((b^6*c^6*d - 6*a*b^5 \\ & *c^5*d^2 + 15*a^2*b^4*c^4*d^3 - 20*a^3*b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6 \\ & *a^5*b*c*d^6 + a^6*d^7)/b^13)^(1/6) + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x \\ & + a)^(2/3)*(d*x + c)^(1/3) + (b^5*x + a*b^4)*((b^6*c^6*d - 6*a*b^5*c^5*d^2 \\ & + 15*a^2*b^4*c^4*d^3 - 20*a^3*b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c* \\ & d^6 + a^6*d^7)/b^13)^(1/3))/(b*x + a)) - 7*(b^3*x + a*b^2)*((b^6*c^6*d - 6* \\ & a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 - 20*a^3*b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 \\ & - 6*a^5*b*c*d^6 + a^6*d^7)/b^13)^(1/6)*log(-49*((b^3*c - a*b^2*d)*(b*x + \\ & a)^(5/6)*(d*x + c)^(1/6))*((b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 \\ & - 20*a^3*b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7)/b^13) \\ & ^{(1/6) - (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*(b*x + a)^(2/3)*(d*x + c)^(1/3) - \\ & (b^5*x + a*b^4)*((b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 - 20*a^3 \\ & *b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7)/b^13)^(1/3))/(\\ & b*x + a)) + 14*(b^3*x + a*b^2)*((b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 \\ & ^4*d^3 - 20*a^3*b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7) \\ & /b^13)^(1/6)*log(-7*((b*c - a*d)*(b*x + a)^(5/6)*(d*x + c)^(1/6) + (b^3*x + \\ & a*b^2)*((b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 - 20*a^3*b^3*c^3 \\ & *d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7)/b^13)^(1/6)))/(b*x + a) \\ &) - 14*(b^3*x + a*b^2)*((b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 - \\ & 20*a^3*b^3*c^3*d^4 + 15*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7)/b^13)^(\\ & 1/6)*log(-7*((b*c - a*d)*(b*x + a)^(5/6)*(d*x + c)^(1/6) - (b^3*x + a*b^2)* \\ & ((b^6*c^6*d - 6*a*b^5*c^5*d^2 + 15*a^2*b^4*c^4*d^3 - 20*a^3*b^3*c^3*d^4 + 1 \\ & 5*a^4*b^2*c^2*d^5 - 6*a^5*b*c*d^6 + a^6*d^7)/b^13)^(1/6)))/(b*x + a)) + 12*(\\ & b*d*x - 6*b*c + 7*a*d)*(b*x + a)^(5/6)*(d*x + c)^(1/6))/(b^3*x + a*b^2) \end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{7}{6}}}{(bx+a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(7/6)/(b*x+a)^(7/6),x, algorithm="giac")

[Out] integrate((d*x + c)^(7/6)/(b*x + a)^(7/6), x)

maple [F] time = 0.13, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{7}{6}}}{(bx + a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(7/6)/(b*x+a)^(7/6),x)

[Out] int((d*x+c)^(7/6)/(b*x+a)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{7}{6}}}{(bx + a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(7/6)/(b*x+a)^(7/6),x, algorithm="maxima")

[Out] integrate((d*x + c)^(7/6)/(b*x + a)^(7/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{\frac{7}{6}}}{(a + bx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(7/6)/(a + b*x)^(7/6),x)

[Out] int((c + d*x)^(7/6)/(a + b*x)^(7/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{7}{6}}}{(a + bx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(7/6)/(b*x+a)**(7/6),x)

[Out] Integral((c + d*x)**(7/6)/(a + b*x)**(7/6), x)

$$3.1833 \quad \int \frac{\sqrt[6]{c+dx}}{(a+bx)^{7/6}} dx$$

Optimal. Leaf size=332

$$\frac{\sqrt[6]{d} \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2b^{7/6}} + \frac{\sqrt[6]{d} \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2b^{7/6}} + \frac{\sqrt{3} \sqrt[6]{d} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{d}}{\sqrt{3}\sqrt[6]{c+dx}}\right)}{b^{7/6}}$$

[Out] $-6*(d*x+c)^{(1/6)}/b/(b*x+a)^{(1/6)}+2*d^{(1/6)}*\operatorname{arctanh}(d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)})/(d*x+c)^{(1/6)}/b^{(7/6)}-1/2*d^{(1/6)}*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)})/(d*x+c)^{(1/3)}-b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}/b^{(7/6)}+1/2*d^{(1/6)}*\ln(b^{(1/3)}+d^{(1/3)}*(b*x+a)^{(1/3)})/(d*x+c)^{(1/3)}+b^{(1/6)}*d^{(1/6)}*(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}/b^{(7/6)}-d^{(1/6)}*\operatorname{arctan}(-1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)})/(d*x+c)^{(1/6)}*3^{(1/2)}/b^{(7/6)}-d^{(1/6)}*\operatorname{arctan}(1/3*3^{(1/2)}+2/3*d^{(1/6)}*(b*x+a)^{(1/6)}/b^{(1/6)})/(d*x+c)^{(1/6)}*3^{(1/2)}/b^{(7/6)}$

Rubi [A] time = 0.54, antiderivative size = 332, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 9, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.474$, Rules used = {47, 63, 331, 296, 634, 618, 204, 628, 208}

$$\frac{\sqrt[6]{d} \log\left(-\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2b^{7/6}} + \frac{\sqrt[6]{d} \log\left(\frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[3]{d} \sqrt[3]{a+bx}}{\sqrt[3]{c+dx}} + \sqrt[3]{b}\right)}{2b^{7/6}} + \frac{\sqrt{3} \sqrt[6]{d} \tan^{-1}\left(\frac{1}{\sqrt{3}} - \frac{2\sqrt[6]{d}}{\sqrt{3}\sqrt[6]{c+dx}}\right)}{b^{7/6}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^{(1/6)}/(a + b*x)^{(7/6)}, x]$

[Out] $(-6*(c + d*x)^{(1/6)}/(b*(a + b*x)^{(1/6)}) + (\operatorname{Sqrt}[3]*d^{(1/6)}*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] - (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/b^{(7/6)} - (\operatorname{Sqrt}[3]*d^{(1/6)}*\operatorname{ArcTan}[1/\operatorname{Sqrt}[3] + (2*d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/b^{(7/6)} + (2*d^{(1/6)}*\operatorname{ArcTanh}[(d^{(1/6)}*(a + b*x)^{(1/6)})/(\operatorname{Sqrt}[3]*b^{(1/6)}*(c + d*x)^{(1/6)})])/b^{(7/6)} - (d^{(1/6)}*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)}] - (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})/(2*b^{(7/6)}) + (d^{(1/6)}*\operatorname{Log}[b^{(1/3)} + (d^{(1/3)}*(a + b*x)^{(1/3)})/(c + d*x)^{(1/3)}] + (b^{(1/6)}*d^{(1/6)}*(a + b*x)^{(1/6)})/(c + d*x)^{(1/6)})/(2*b^{(7/6)})$

Rule 47

$\operatorname{Int}[(a_. + (b_.)*(x_))^{(m_.)}*((c_.) + (d_.)*(x_))^{(n_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^n/(b*(m + 1)), x] - \operatorname{Dist}[(d*n)/(b*(m + 1)), \operatorname{Int}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n - 1)}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d\}, x \&\&$

NeQ[b*c - a*d, 0] && GtQ[n, 0] && LtQ[m, -1] && !(IntegerQ[n] && !IntegerQ[m]) && !(ILeQ[m + n + 2, 0] && (FractionQ[m] || GeQ[2*n + m + 1, 0])) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 204

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := -Simp[ArcTan[(Rt[-b, 2]*x)/Rt[-a, 2]]/(Rt[-a, 2]*Rt[-b, 2]), x] /; FreeQ[{a, b}, x] && PosQ[a/b] && (LtQ[a, 0] || LtQ[b, 0])

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rule 296

Int[(x_)^(m_.)/((a_) + (b_.)*(x_)^(n_)), x_Symbol] := Module[{r = Numerator[Rt[-(a/b), n]], s = Denominator[Rt[-(a/b), n]], k, u}, Simp[u = Int[(r*Cos[(2*k*m*Pi)/n] - s*Cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 - 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x] + Int[(r*Cos[(2*k*m*Pi)/n] + s*Cos[(2*k*(m + 1)*Pi)/n]*x)/(r^2 + 2*r*s*Cos[(2*k*Pi)/n]*x + s^2*x^2), x]; (2*r^(m + 2)*Int[1/(r^2 - s^2*x^2), x])/(a*n*s^m) + Dist[(2*r^(m + 1))/(a*n*s^m), Sum[u, {k, 1, (n - 2)/4}], x, x] /; FreeQ[{a, b}, x] && IGtQ[(n - 2)/4, 0] && IGtQ[m, 0] && LtQ[m, n - 1] && NegQ[a/b]

Rule 331

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[a^(p + (m + 1)/n), Subst[Int[x^m/(1 - b*x^n)^(p + (m + 1)/n + 1), x], x, x/(a + b*x^n)^(1/n)], x] /; FreeQ[{a, b}, x] && IGtQ[n, 0] && LtQ[-1, p, 0] && NeQ[p, -2^(-1)] && IntegersQ[m, p + (m + 1)/n]

Rule 618

Int[((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)^(-1), x_Symbol] := Dist[-2, Subst[Int[1/Simp[b^2 - 4*a*c - x^2, x], x], x, b + 2*c*x], x] /; FreeQ[{a, b, c},

$x] \&\& \text{NeQ}[b^2 - 4*a*c, 0]$

Rule 628

$\text{Int}[(d_.) + (e_.)*(x_.)]/((a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2), x_Symbol] \rightarrow \text{Simp}[(d*\text{Log}[\text{RemoveContent}[a + b*x + c*x^2, x]])/b, x] /; \text{FreeQ}\{a, b, c, d, e\}, x] \&\& \text{EqQ}[2*c*d - b*e, 0]$

Rule 634

$\text{Int}[(d_.) + (e_.)*(x_.)]/((a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2), x_Symbol] \rightarrow \text{Dist}[(2*c*d - b*e)/(2*c), \text{Int}[1/(a + b*x + c*x^2), x], x] + \text{Dist}[e/(2*c), \text{Int}[(b + 2*c*x)/(a + b*x + c*x^2), x], x] /; \text{FreeQ}\{a, b, c, d, e\}, x] \&\& \text{NeQ}[2*c*d - b*e, 0] \&\& \text{NeQ}[b^2 - 4*a*c, 0] \&\& \text{!NiceSqrtQ}[b^2 - 4*a*c]$

Rubi steps

$$\begin{aligned}
\int \frac{\sqrt[6]{c+dx}}{(a+bx)^{7/6}} dx &= -\frac{6\sqrt[6]{c+dx}}{b\sqrt[6]{a+bx}} + \frac{d \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{5/6}} dx}{b} \\
&= -\frac{6\sqrt[6]{c+dx}}{b\sqrt[6]{a+bx}} + \frac{(6d) \text{ Subst} \left(\int \frac{x^4}{\left(c - \frac{ad}{b} + \frac{dx^6}{b}\right)^{5/6}} dx, x, \sqrt[6]{a+bx} \right)}{b^2} \\
&= -\frac{6\sqrt[6]{c+dx}}{b\sqrt[6]{a+bx}} + \frac{(6d) \text{ Subst} \left(\int \frac{x^4}{1 - \frac{dx^6}{b}} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{b^2} \\
&= -\frac{6\sqrt[6]{c+dx}}{b\sqrt[6]{a+bx}} + \frac{(2\sqrt[3]{d}) \text{ Subst} \left(\int \frac{-\frac{\sqrt[6]{b}}{2} - \frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{b^{7/6}} + \frac{(2\sqrt[3]{d}) \text{ Subst} \left(\int \frac{-\frac{\sqrt[6]{b}}{2} + \frac{\sqrt[6]{d}x}{2}}{\sqrt[3]{b} + \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{b^{7/6}} \\
&= -\frac{6\sqrt[6]{c+dx}}{b\sqrt[6]{a+bx}} + \frac{2\sqrt[6]{d} \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{b^{7/6}} - \frac{\sqrt[6]{d} \text{ Subst} \left(\int \frac{-\sqrt[6]{b} \sqrt[6]{d} + 2\sqrt[3]{d}x}{\sqrt[3]{b} - \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2b^{7/6}} + \frac{\sqrt[6]{d} \text{ Subst} \left(\int \frac{\sqrt[6]{b} \sqrt[6]{d} + 2\sqrt[3]{d}x}{\sqrt[3]{b} + \sqrt[6]{b} \sqrt[6]{d}x + \sqrt[3]{d}x^2} dx, x, \frac{\sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2b^{7/6}} \\
&= -\frac{6\sqrt[6]{c+dx}}{b\sqrt[6]{a+bx}} + \frac{2\sqrt[6]{d} \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{b^{7/6}} - \frac{\sqrt[6]{d} \log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} - \frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2b^{7/6}} + \frac{\sqrt[6]{d} \log \left(\sqrt[3]{b} + \frac{\sqrt[3]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} + \frac{\sqrt[6]{b} \sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{c+dx}} \right)}{2b^{7/6}} \\
&= -\frac{6\sqrt[6]{c+dx}}{b\sqrt[6]{a+bx}} + \frac{\sqrt{3} \sqrt[6]{d} \tan^{-1} \left(\frac{1 - \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{b^{7/6}} - \frac{\sqrt{3} \sqrt[6]{d} \tan^{-1} \left(\frac{1 + \frac{2\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}}}{\sqrt{3}} \right)}{b^{7/6}} + \frac{2\sqrt[6]{d} \tanh^{-1} \left(\frac{\sqrt[6]{d} \sqrt[6]{a+bx}}{\sqrt[6]{b} \sqrt[6]{c+dx}} \right)}{b^{7/6}}
\end{aligned}$$

Mathematica [C] time = 0.03, size = 71, normalized size = 0.21

$$-\frac{6\sqrt[6]{c+dx} {}_2F_1 \left(-\frac{1}{6}, -\frac{1}{6}; \frac{5}{6}; \frac{d(a+bx)}{ad-bc} \right)}{b\sqrt[6]{a+bx} \sqrt[6]{\frac{b(c+dx)}{bc-ad}}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1/6)/(a + b*x)^(7/6), x]

[Out] (-6*(c + d*x)^(1/6)*Hypergeometric2F1[-1/6, -1/6, 5/6, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(a + b*x)^(1/6)*((b*(c + d*x))/(b*c - a*d))^(1/6))

fricas [B] time = 0.93, size = 663, normalized size = 2.00

$$4\sqrt{3}(b^2x+ab)\left(\frac{d}{b^7}\right)^{\frac{1}{6}}\arctan\left(\frac{2\sqrt{3}(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{1}{6}}b^6\left(\frac{d}{b^7}\right)^{\frac{5}{6}}-2\sqrt{3}(b^7x+ab^6)\sqrt{\frac{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{1}{6}}b\left(\frac{d}{b^7}\right)^{\frac{1}{6}}+(b^3x+ab^2)\left(\frac{d}{b^7}\right)^{\frac{1}{3}}+(bx+a)^{\frac{2}{3}}(dx+c)^{\frac{1}{3}}}{bx+a}}}{3(bdx+ad)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(7/6),x, algorithm="fricas")

[Out]
$$\begin{aligned} & -1/2*(4*\sqrt{3}*(b^2*x + a*b)*(d/b^7)^{(1/6)}*\arctan(-1/3*(2*\sqrt{3}*(b*x + a) \\ &)^{(5/6)}*(d*x + c)^{(1/6)}*b^6*(d/b^7)^{(5/6)} - 2*\sqrt{3}*(b^7*x + a*b^6)*\sqrt{ \\ & ((b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*b*(d/b^7)^{(1/6)} + (b^3*x + a*b^2)*(d/b^7)^{(1/3)} + (b*x + a)^{(2/3)}*(d*x + c)^{(1/3)})/(b*x + a))* \\ & (d/b^7)^{(5/6)} + \sqrt{3}*(b*d*x + a*d))/(b*d*x + a*d)) + 4*\sqrt{3}*(b^2*x + a*b)*(d/b^7)^{(1/6)}*\arctan \\ & (-1/3*(2*\sqrt{3}*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*b^6*(d/b^7)^{(5/6)} - 2*\sqrt{3}*(b^7*x + a*b^6)*\sqrt{ \\ & ((b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*b*(d/b^7)^{(1/6)} + (b^3*x + a*b^2)*(d/b^7)^{(1/3)} + (b*x + a)^{(2/3)}*(d*x + c)^{(1/3)})/(b*x + \\ & a))* \\ & (d/b^7)^{(5/6)} - \sqrt{3}*(b*d*x + a*d))/(b*d*x + a*d)) - (b^2*x + a*b)*(d/b^7)^{(1/6)}*\log(4*((b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*b*(d/b^7)^{(1/6)} + (b^3*x + a*b^2)*(d/b^7)^{(1/3)} + (b*x + a)^{(2/3)}*(d*x + c)^{(1/3)})/(b*x + a)) + (b^2*x + a*b)*(d/b^7)^{(1/6)}*\log(-4*((b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}*b*(d/b^7)^{(1/6)} - (b^3*x + a*b^2)*(d/b^7)^{(1/3)} - (b*x + a)^{(2/3)}*(d*x + c)^{(1/3)})/(b*x + a)) - 2*(b^2*x + a*b)*(d/b^7)^{(1/6)}*\log(((b^2*x + a*b)*(d/b^7)^{(1/6)} + (b*x + a)^{(5/6)}*(d*x + c)^{(1/6)})/(b*x + a)) + 2*(b^2*x + a*b)*(d/b^7)^{(1/6)}*\log(-((b^2*x + a*b)*(d/b^7)^{(1/6)} - (b*x + a)^{(5/6)}*(d*x + c)^{(1/6)})/(b*x + a)) + 12*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)})/(b^2*x + a*b) \end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{6}}}{(bx+a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(1/6)/(b*x+a)^(7/6),x, algorithm="giac")

[Out] integrate((d*x + c)^(1/6)/(b*x + a)^(7/6), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^{\frac{1}{6}}}{(bx+a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^(1/6)/(b*x+a)^(7/6),x)`

[Out] `int((d*x+c)^(1/6)/(b*x+a)^(7/6),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^(1/6)/(b*x+a)^(7/6),x, algorithm="maxima")`

[Out] `integrate((d*x + c)^(1/6)/(b*x + a)^(7/6), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^{1/6}}{(a + bx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^(1/6)/(a + b*x)^(7/6),x)`

[Out] `int((c + d*x)^(1/6)/(a + b*x)^(7/6), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\sqrt[6]{c + dx}}{(a + bx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**(1/6)/(b*x+a)**(7/6),x)`

[Out] `Integral((c + d*x)**(1/6)/(a + b*x)**(7/6), x)`

$$3.1834 \quad \int \frac{1}{(a+bx)^{7/6}(c+dx)^{5/6}} dx$$

Optimal. Leaf size=30

$$-\frac{6\sqrt[6]{c+dx}}{\sqrt[6]{a+bx}(bc-ad)}$$

[Out] $-6*(d*x+c)^{(1/6)/(-a*d+b*c)/(b*x+a)^{(1/6)}$

Rubi [A] time = 0.00, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{6\sqrt[6]{c+dx}}{\sqrt[6]{a+bx}(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[1/((a + b*x)^{(7/6})*(c + d*x)^{(5/6})), x]$

[Out] $(-6*(c + d*x)^{(1/6}))/((b*c - a*d)*(a + b*x)^{(1/6}))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Simp} [((a + b*x)^{(m + 1})*(c + d*x)^{(n + 1}))/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}[\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{EqQ}[m + n + 2, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rubi steps

$$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{5/6}} dx = -\frac{6\sqrt[6]{c+dx}}{(bc-ad)\sqrt[6]{a+bx}}$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$\frac{6\sqrt[6]{c+dx}}{\sqrt[6]{a+bx}(ad-bc)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[1/((a + b*x)^{(7/6})*(c + d*x)^{(5/6})), x]$

[Out] $(6*(c + d*x)^{(1/6)})/((-b*c) + a*d)*(a + b*x)^{(1/6)}$

fricas [A] time = 0.95, size = 42, normalized size = 1.40

$$\frac{6 (bx + a)^{\frac{5}{6}} (dx + c)^{\frac{1}{6}}}{abc - a^2d + (b^2c - abd)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(7/6)/(d*x+c)^(5/6),x, algorithm="fricas")`

[Out] $-6*(b*x + a)^{(5/6)}*(d*x + c)^{(1/6)}/(a*b*c - a^2*d + (b^2*c - a*b*d)*x)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{6}}(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(7/6)/(d*x+c)^(5/6),x, algorithm="giac")`

[Out] `integrate(1/((b*x + a)^(7/6)*(d*x + c)^(5/6)), x)`

maple [A] time = 0.01, size = 27, normalized size = 0.90

$$\frac{6 (dx + c)^{\frac{1}{6}}}{(bx + a)^{\frac{1}{6}} (ad - bc)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(b*x+a)^(7/6)/(d*x+c)^(5/6),x)`

[Out] $6/(b*x+a)^{(1/6)}*(d*x+c)^{(1/6)}/(a*d-b*c)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{6}}(dx + c)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)^(7/6)/(d*x+c)^(5/6),x, algorithm="maxima")`

[Out] `integrate(1/((b*x + a)^(7/6)*(d*x + c)^(5/6)), x)`

mupad [B] time = 0.68, size = 26, normalized size = 0.87

$$\frac{6(c + dx)^{1/6}}{(ad - bc)(a + bx)^{1/6}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(7/6)*(c + d*x)^(5/6)),x)`

[Out] `(6*(c + d*x)^(1/6))/((a*d - b*c)*(a + b*x)^(1/6))`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{7}{6}} (c + dx)^{\frac{5}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(7/6)/(d*x+c)**(5/6),x)`

[Out] `Integral(1/((a + b*x)**(7/6)*(c + d*x)**(5/6)), x)`

$$3.1835 \quad \int \frac{1}{(a+bx)^{7/6}(c+dx)^{11/6}} dx$$

Optimal. Leaf size=64

$$-\frac{36d(a+bx)^{5/6}}{5(c+dx)^{5/6}(bc-ad)^2} - \frac{6}{\sqrt[6]{a+bx}(c+dx)^{5/6}(bc-ad)}$$

[Out] $-6/(-a*d+b*c)/(b*x+a)^{(1/6)}/(d*x+c)^{(5/6)}-36/5*d*(b*x+a)^{(5/6)/(-a*d+b*c)^2/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.01, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{36d(a+bx)^{5/6}}{5(c+dx)^{5/6}(bc-ad)^2} - \frac{6}{\sqrt[6]{a+bx}(c+dx)^{5/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/6)*(c + d*x)^(11/6)), x]

[Out] $-6/((b*c - a*d)*(a + b*x)^{(1/6)*(c + d*x)^{(5/6)}) - (36*d*(a + b*x)^{(5/6)})/(5*(b*c - a*d)^2*(c + d*x)^{(5/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{11/6}} dx = -\frac{6}{(bc-ad)\sqrt[6]{a+bx}(c+dx)^{5/6}} - \frac{(6d) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{11/6}} dx}{bc-ad}$$

$$= -\frac{6}{(bc-ad)\sqrt[6]{a+bx}(c+dx)^{5/6}} - \frac{36d(a+bx)^{5/6}}{5(bc-ad)^2(c+dx)^{5/6}}$$

Mathematica [A] time = 0.03, size = 45, normalized size = 0.70

$$-\frac{6(ad+5bc+6bdx)}{5\sqrt[6]{a+bx}(c+dx)^{5/6}(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a+b*x)^(7/6)*(c+d*x)^(11/6)),x]

[Out] (-6*(5*b*c+a*d+6*b*d*x))/(5*(b*c-a*d)^2*(a+b*x)^(1/6)*(c+d*x)^(5/6))

fricas [B] time = 0.98, size = 126, normalized size = 1.97

$$\frac{6(6bdx+5bc+ad)(bx+a)^{5/6}(dx+c)^{1/6}}{5(ab^2c^3-2a^2bc^2d+a^3cd^2+(b^3c^2d-2ab^2cd^2+a^2bd^3)x^2+(b^3c^3-ab^2c^2d-a^2bcd^2+a^3d^3)x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(11/6),x, algorithm="fricas")

[Out] -6/5*(6*b*d*x+5*b*c+a*d)*(b*x+a)^(5/6)*(d*x+c)^(1/6)/(a*b^2*c^3-2*a^2*b*c^2*d+a^3*c*d^2+(b^3*c^2*d-2*a*b^2*c*d^2+a^2*b*d^3)*x^2+(b^3*c^3-a*b^2*c^2*d-a^2*b*c*d^2+a^3*d^3)*x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{7/6}(dx+c)^{11/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(11/6),x, algorithm="giac")

[Out] integrate(1/((b*x+a)^(7/6)*(d*x+c)^(11/6)),x)

maple [A] time = 0.01, size = 53, normalized size = 0.83

$$-\frac{6(6bdx + ad + 5bc)}{5(bx + a)^{\frac{1}{6}}(dx + c)^{\frac{5}{6}}(a^2d^2 - 2abcd + b^2c^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/6)/(d*x+c)^(11/6), x)

[Out] -6/5*(6*b*d*x+a*d+5*b*c)/(b*x+a)^(1/6)/(d*x+c)^(5/6)/(a^2*d^2-2*a*b*c*d+b^2*c^2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{6}}(dx + c)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(11/6), x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(11/6)), x)

mupad [B] time = 0.83, size = 72, normalized size = 1.12

$$-\frac{\left(\frac{36bx}{5(ad-bc)^2} + \frac{6ad+30bc}{5d(ad-bc)^2}\right)(c+dx)^{1/6}}{x(a+bx)^{1/6} + \frac{c(a+bx)^{1/6}}{d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/6)*(c + d*x)^(11/6)), x)

[Out] -(((36*b*x)/(5*(a*d - b*c)^2) + (6*a*d + 30*b*c)/(5*d*(a*d - b*c)^2))*(c + d*x)^(1/6))/(x*(a + b*x)^(1/6) + (c*(a + b*x)^(1/6))/d)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{7}{6}}(c + dx)^{\frac{11}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/6)/(d*x+c)**(11/6), x)

[Out] Integral(1/((a + b*x)**(7/6)*(c + d*x)**(11/6)), x)

$$3.1836 \quad \int \frac{1}{(a+bx)^{7/6}(c+dx)^{17/6}} dx$$

Optimal. Leaf size=98

$$-\frac{432bd(a+bx)^{5/6}}{55(c+dx)^{5/6}(bc-ad)^3} - \frac{72d(a+bx)^{5/6}}{11(c+dx)^{11/6}(bc-ad)^2} - \frac{6}{\sqrt[6]{a+bx}(c+dx)^{11/6}(bc-ad)}$$

[Out] $-6/(-a*d+b*c)/(b*x+a)^{(1/6)}/(d*x+c)^{(11/6)}-72/11*d*(b*x+a)^{(5/6)}/(-a*d+b*c)^2/(d*x+c)^{(11/6)}-432/55*b*d*(b*x+a)^{(5/6)}/(-a*d+b*c)^3/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{432bd(a+bx)^{5/6}}{55(c+dx)^{5/6}(bc-ad)^3} - \frac{72d(a+bx)^{5/6}}{11(c+dx)^{11/6}(bc-ad)^2} - \frac{6}{\sqrt[6]{a+bx}(c+dx)^{11/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/6)*(c + d*x)^(17/6)), x]

[Out] $-6/((b*c - a*d)*(a + b*x)^{(1/6)*(c + d*x)^{(11/6)}} - (72*d*(a + b*x)^{(5/6)})/(11*(b*c - a*d)^2*(c + d*x)^{(11/6)}) - (432*b*d*(a + b*x)^{(5/6)})/(55*(b*c - a*d)^3*(c + d*x)^{(5/6)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(17/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(17/6)), x)

maple [A] time = 0.01, size = 105, normalized size = 1.07

$$\frac{6 \left(-72b^2x^2d^2 - 12abd^2x - 132b^2cdx + 5a^2d^2 - 22abcd - 55b^2c^2 \right)}{55(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{11}{6}} \left(a^3d^3 - 3a^2bcd^2 + 3ab^2c^2d - b^3c^3 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/6)/(d*x+c)^(17/6),x)

[Out] -6/55*(-72*b^2*d^2*x^2-12*a*b*d^2*x-132*b^2*c*d*x+5*a^2*d^2-22*a*b*c*d-55*b^2*c^2)/(b*x+a)^(1/6)/(d*x+c)^(11/6)/(a^3*d^3-3*a^2*b*c*d^2+3*a*b^2*c^2*d-b^3*c^3)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{6}}(dx+c)^{\frac{17}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(17/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(17/6)), x)

mupad [B] time = 0.96, size = 132, normalized size = 1.35

$$\frac{(c+dx)^{1/6} \left(\frac{432b^2x^2}{55(ad-bc)^3} + \frac{-30a^2d^2+132abcd+330b^2c^2}{55d^2(ad-bc)^3} + \frac{72bx(ad+11bc)}{55d(ad-bc)^3} \right)}{x^2(a+bx)^{1/6} + \frac{c^2(a+bx)^{1/6}}{d^2} + \frac{2cx(a+bx)^{1/6}}{d}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/6)*(c + d*x)^(17/6)),x)

[Out] ((c + d*x)^(1/6)*((432*b^2*x^2)/(55*(a*d - b*c)^3) + (330*b^2*c^2 - 30*a^2*d^2 + 132*a*b*c*d)/(55*d^2*(a*d - b*c)^3) + (72*b*x*(a*d + 11*b*c))/(55*d*(a*d - b*c)^3))/(x^2*(a + b*x)^(1/6) + (c^2*(a + b*x)^(1/6))/d^2 + (2*c*x*(a + b*x)^(1/6))/d)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(b*x+a)**(7/6)/(d*x+c)**(17/6),x)
```

```
[Out] Timed out
```

$$3.1837 \quad \int \frac{1}{(a+bx)^{7/6}(c+dx)^{23/6}} dx$$

Optimal. Leaf size=134

$$\frac{7776b^2d(a+bx)^{5/6}}{935(c+dx)^{5/6}(bc-ad)^4} - \frac{1296bd(a+bx)^{5/6}}{187(c+dx)^{11/6}(bc-ad)^3} - \frac{108d(a+bx)^{5/6}}{17(c+dx)^{17/6}(bc-ad)^2} - \frac{6}{\sqrt[6]{a+bx}(c+dx)^{17/6}(bc-ad)}$$

[Out] $-6/(-a*d+b*c)/(b*x+a)^{(1/6)}/(d*x+c)^{(17/6)}-108/17*d*(b*x+a)^{(5/6)}/(-a*d+b*c)^2/(d*x+c)^{(17/6)}-1296/187*b*d*(b*x+a)^{(5/6)}/(-a*d+b*c)^3/(d*x+c)^{(11/6)}-7776/935*b^2*d*(b*x+a)^{(5/6)}/(-a*d+b*c)^4/(d*x+c)^{(5/6)}$

Rubi [A] time = 0.03, antiderivative size = 134, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{7776b^2d(a+bx)^{5/6}}{935(c+dx)^{5/6}(bc-ad)^4} - \frac{1296bd(a+bx)^{5/6}}{187(c+dx)^{11/6}(bc-ad)^3} - \frac{108d(a+bx)^{5/6}}{17(c+dx)^{17/6}(bc-ad)^2} - \frac{6}{\sqrt[6]{a+bx}(c+dx)^{17/6}(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/6)*(c + d*x)^(23/6)), x]

[Out] $-6/((b*c - a*d)*(a + b*x)^{(1/6)*(c + d*x)^{(17/6))} - (108*d*(a + b*x)^{(5/6)})/(17*(b*c - a*d)^2*(c + d*x)^{(17/6))} - (1296*b*d*(a + b*x)^{(5/6)})/(187*(b*c - a*d)^3*(c + d*x)^{(11/6))} - (7776*b^2*d*(a + b*x)^{(5/6)})/(935*(b*c - a*d)^4*(c + d*x)^{(5/6))}$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int \frac{1}{(a+bx)^{7/6}(c+dx)^{23/6}} dx &= -\frac{6}{(bc-ad)\sqrt[6]{a+bx}(c+dx)^{17/6}} - \frac{(18d) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{23/6}} dx}{bc-ad} \\
&= -\frac{6}{(bc-ad)\sqrt[6]{a+bx}(c+dx)^{17/6}} - \frac{108d(a+bx)^{5/6}}{17(bc-ad)^2(c+dx)^{17/6}} - \frac{(216bd) \int \frac{1}{\sqrt[6]{a+bx}(c+dx)^{17/6}} dx}{17(bc-ad)^2} \\
&= -\frac{6}{(bc-ad)\sqrt[6]{a+bx}(c+dx)^{17/6}} - \frac{108d(a+bx)^{5/6}}{17(bc-ad)^2(c+dx)^{17/6}} - \frac{1296bd(a+bx)^5}{187(bc-ad)^3(c+dx)^{17/6}} \\
&= -\frac{6}{(bc-ad)\sqrt[6]{a+bx}(c+dx)^{17/6}} - \frac{108d(a+bx)^{5/6}}{17(bc-ad)^2(c+dx)^{17/6}} - \frac{1296bd(a+bx)^5}{187(bc-ad)^3(c+dx)^{17/6}}
\end{aligned}$$

Mathematica [A] time = 0.06, size = 118, normalized size = 0.88

$$\frac{6(55a^3d^3 - 15a^2bd^2(17c + 6dx) + 3ab^2d(187c^2 + 204cdx + 72d^2x^2) + b^3(935c^3 + 3366c^2dx + 3672cd^2x^2 + 1296d^3x^3))}{935\sqrt[6]{a+bx}(c+dx)^{17/6}(bc-ad)^4}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/6)*(c + d*x)^(23/6)), x]

[Out] (-6*(55*a^3*d^3 - 15*a^2*b*d^2*(17*c + 6*d*x) + 3*a*b^2*d*(187*c^2 + 204*c*d*x + 72*d^2*x^2) + b^3*(935*c^3 + 3366*c^2*d*x + 3672*c*d^2*x^2 + 1296*d^3*x^3)))/(935*(b*c - a*d)^4*(a + b*x)^(1/6)*(c + d*x)^(17/6))

fricas [B] time = 1.09, size = 457, normalized size = 3.41

$$\frac{6(1296b^3d^3x^3 + 935b^3c^3 + 561a*b^2*c^2*d - 255a^2*b*c*d^2 + 55a^3*d^3 + 216*(17*b^3*c*d^2 + a*b^2*d^3)*x^2 + 18*(187*b^3*c^2*d + 34*a*b^2*c*d^2 - 5*a^2*b*d^3)*x)*(b*x + a)^(5/6)*(d*x + c)^(1/6)/(a*b^4*c^7 - 4*a^2*b^3*c^6*d + 6*a^3*b^2*c^5*d^2 - 4*a^4*b*c^4*d^3 + a^5*c^3*d^4 + (b^5*c^4*d^3 - 4*ab^4*c^3*d^4 + 6*a^2*b^3*c^2*d^5 - 4*a^3*b^2*c*d^6 + a^4*b*d^7))}{935}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(23/6), x, algorithm="fricas")

[Out] -6/935*(1296*b^3*d^3*x^3 + 935*b^3*c^3 + 561*a*b^2*c^2*d - 255*a^2*b*c*d^2 + 55*a^3*d^3 + 216*(17*b^3*c*d^2 + a*b^2*d^3)*x^2 + 18*(187*b^3*c^2*d + 34*a*b^2*c*d^2 - 5*a^2*b*d^3)*x)*(b*x + a)^(5/6)*(d*x + c)^(1/6)/(a*b^4*c^7 - 4*a^2*b^3*c^6*d + 6*a^3*b^2*c^5*d^2 - 4*a^4*b*c^4*d^3 + a^5*c^3*d^4 + (b^5*c^4*d^3 - 4*a*b^4*c^3*d^4 + 6*a^2*b^3*c^2*d^5 - 4*a^3*b^2*c*d^6 + a^4*b*d^7))

) $x^4 + (3b^5c^5d^2 - 11ab^4c^4d^3 + 14a^2b^3c^3d^4 - 6a^3b^2c^2d^5 - a^4b^1c^1d^6 + a^5d^7)x^3 + 3(b^5c^6d - 3ab^4c^5d^2 + 2a^2b^3c^4d^3 + 2a^3b^2c^3d^4 - 3a^4b^1c^2d^5 + a^5c^1d^6)x^2 + (b^5c^7 - ab^4c^6d - 6a^2b^3c^5d^2 + 14a^3b^2c^4d^3 - 11a^4b^1c^3d^4 + 3a^5c^2d^5)x$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{6}}(dx+c)^{\frac{23}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(23/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(23/6)), x)

maple [A] time = 0.01, size = 171, normalized size = 1.28

$$\frac{6(1296b^3d^3x^3 + 216ab^2d^3x^2 + 3672b^3cd^2x^2 - 90a^2bd^3x + 612ab^2cd^2x + 3366b^3c^2dx + 55a^3d^3 - 255a^2bcd^2 - 935(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{17}{6}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4))}{935(bx+a)^{\frac{1}{6}}(dx+c)^{\frac{17}{6}}(a^4d^4 - 4a^3bcd^3 + 6a^2b^2c^2d^2 - 4ab^3c^3d + b^4c^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/6)/(d*x+c)^(23/6),x)

[Out] $-6/935*(1296*b^3*d^3*x^3+216*a*b^2*d^3*x^2+3672*b^3*c*d^2*x^2-90*a^2*b*d^3*x+612*a*b^2*c*d^2*x+3366*b^3*c^2*d*x+55*a^3*d^3-255*a^2*b*c*d^2+561*a*b^2*c^2*d+935*b^3*c^3)/(b*x+a)^{(1/6)}/(d*x+c)^{(17/6)}/(a^4*d^4-4*a^3*b*c*d^3+6*a^2*b^2*c^2*d^2-4*a*b^3*c^3*d+b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{6}}(dx+c)^{\frac{23}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(23/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(23/6)), x)

mupad [B] time = 1.15, size = 209, normalized size = 1.56

$$\frac{(c+dx)^{1/6} \left(\frac{7776b^3x^3}{935(ad-bc)^4} + \frac{330a^3d^3-1530a^2bcd^2+3366ab^2c^2d+5610b^3c^3}{935d^3(ad-bc)^4} + \frac{108bx(-5a^2d^2+34abcd+187b^2c^2)}{935d^2(ad-bc)^4} + \frac{1296b^2x^2(ad+bc)}{935d(ad-bc)^4} \right)}{x^3(a+bx)^{1/6} + \frac{c^3(a+bx)^{1/6}}{d^3} + \frac{3cx^2(a+bx)^{1/6}}{d} + \frac{3c^2x(a+bx)^{1/6}}{d^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + b*x)^(7/6)*(c + d*x)^(23/6)),x)`

[Out] $-\left((c + d*x)^{1/6} * \left(\frac{7776*b^3*x^3}{935*(a*d - b*c)^4} + (330*a^3*d^3 + 5610*b^3*c^3 + 3366*a*b^2*c^2*d - 1530*a^2*b*c*d^2)\right) / (935*d^3*(a*d - b*c)^4) + (108*b*x*(187*b^2*c^2 - 5*a^2*d^2 + 34*a*b*c*d)) / (935*d^2*(a*d - b*c)^4) + (1296*b^2*x^2*(a*d + 17*b*c)) / (935*d*(a*d - b*c)^4)\right) / (x^3*(a + b*x)^{1/6} + (c^3*(a + b*x)^{1/6})/d^3 + (3*c*x^2*(a + b*x)^{1/6})/d + (3*c^2*x*(a + b*x)^{1/6})/d^2)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(b*x+a)**(7/6)/(d*x+c)**(23/6),x)`

[Out] Timed out

$$3.1838 \quad \int \frac{(c+dx)^{11/6}}{(a+bx)^{7/6}} dx$$

Optimal. Leaf size=80

$$\frac{6(c+dx)^{5/6}(bc-ad) {}_2F_1\left(-\frac{11}{6}, -\frac{1}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b^2 \sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

[Out] $-6*(-a*d+b*c)*(d*x+c)^{(5/6)}*\text{hypergeom}\left([-\frac{11}{6}, -\frac{1}{6}], [\frac{5}{6}], -d*(b*x+a)/(-a*d+b*c)\right)/b^2/(b*x+a)^{(1/6)}/(b*(d*x+c)/(-a*d+b*c))^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(c+dx)^{5/6}(bc-ad) {}_2F_1\left(-\frac{11}{6}, -\frac{1}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b^2 \sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(11/6)/(a + b*x)^(7/6), x]

[Out] $(-6*(b*c - a*d)*(c + d*x)^{(5/6)}*\text{Hypergeometric2F1}[-11/6, -1/6, 5/6, -((d*(a + b*x))/(b*c - a*d))])/(b^2*(a + b*x)^{(1/6)}*((b*(c + d*x))/(b*c - a*d))^{(5/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(c + dx)^{11/6}}{(a + bx)^{7/6}} dx = \frac{((bc - ad)(c + dx)^{5/6}) \int \frac{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{11/6}}{(a+bx)^{7/6}} dx}{b \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

$$= -\frac{6(bc - ad)(c + dx)^{5/6} {}_2F_1\left(-\frac{11}{6}, -\frac{1}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b^2 \sqrt[6]{a + bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Mathematica [A] time = 0.06, size = 71, normalized size = 0.89

$$\frac{6(c + dx)^{11/6} {}_2F_1\left(-\frac{11}{6}, -\frac{1}{6}; \frac{5}{6}; \frac{d(a+bx)}{ad-bc}\right)}{b \sqrt[6]{a + bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{11/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(11/6)/(a + b*x)^(7/6), x]

[Out] (-6*(c + d*x)^(11/6)*Hypergeometric2F1[-11/6, -1/6, 5/6, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(a + b*x)^(1/6)*((b*(c + d*x))/(b*c - a*d))^(11/6))

fricas [F] time = 1.79, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^{\frac{5}{6}}(dx + c)^{\frac{11}{6}}}{b^2x^2 + 2abx + a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(11/6)/(b*x+a)^(7/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(11/6)/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(11/6)/(b*x+a)^(7/6), x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{11}{6}}}{(bx + a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(11/6)/(b*x+a)^(7/6),x)

[Out] int((d*x+c)^(11/6)/(b*x+a)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{11}{6}}}{(bx + a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(11/6)/(b*x+a)^(7/6),x, algorithm="maxima")

[Out] integrate((d*x + c)^(11/6)/(b*x + a)^(7/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{11/6}}{(a + bx)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(11/6)/(a + b*x)^(7/6),x)

[Out] int((c + d*x)^(11/6)/(a + b*x)^(7/6), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(11/6)/(b*x+a)**(7/6),x)

[Out] Timed out

$$3.1839 \quad \int \frac{(c+dx)^{5/6}}{(a+bx)^{7/6}} dx$$

Optimal. Leaf size=72

$$\frac{6(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, -\frac{1}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

[Out] $-6*(d*x+c)^{(5/6)*\text{hypergeom}([-5/6, -1/6], [5/6], -d*(b*x+a)/(-a*d+b*c))}/b/(b*x+a)^{(1/6)}/(b*(d*x+c)/(-a*d+b*c))^{(5/6)}$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, -\frac{1}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(5/6)/(a + b*x)^(7/6), x]

[Out] $(-6*(c+d*x)^{(5/6)*\text{Hypergeometric2F1}[-5/6, -1/6, 5/6, -((d*(a+b*x))/(b*c-a*d))])/(b*(a+b*x)^{(1/6)*((b*(c+d*x))/(b*c-a*d))^{(5/6)}}$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{(c+dx)^{5/6}}{(a+bx)^{7/6}} dx = \frac{(c+dx)^{5/6} \int \frac{\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{5/6}}{(a+bx)^{7/6}} dx}{\left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

$$= -\frac{6(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, -\frac{1}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Mathematica [A] time = 0.03, size = 71, normalized size = 0.99

$$-\frac{6(c+dx)^{5/6} {}_2F_1\left(-\frac{5}{6}, -\frac{1}{6}; \frac{5}{6}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[6]{a+bx} \left(\frac{b(c+dx)}{bc-ad}\right)^{5/6}}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(5/6)/(a + b*x)^(7/6), x]

[Out] (-6*(c + d*x)^(5/6)*Hypergeometric2F1[-5/6, -1/6, 5/6, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(a + b*x)^(1/6)*((b*(c + d*x))/(b*c - a*d))^(5/6))

fricas [F] time = 1.68, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{5}{6}}}{b^2x^2+2abx+a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(7/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(7/6), x, algorithm="giac")

[Out] Timed out

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^(5/6)/(b*x+a)^(7/6),x)

[Out] int((d*x+c)^(5/6)/(b*x+a)^(7/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^{\frac{5}{6}}}{(bx + a)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^(5/6)/(b*x+a)^(7/6),x, algorithm="maxima")

[Out] integrate((d*x + c)^(5/6)/(b*x + a)^(7/6), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^{\frac{5}{6}}}{(a + bx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^(5/6)/(a + b*x)^(7/6),x)

[Out] int((c + d*x)^(5/6)/(a + b*x)^(7/6), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^{\frac{5}{6}}}{(a + bx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**(5/6)/(b*x+a)**(7/6),x)

[Out] Integral((c + d*x)**(5/6)/(a + b*x)**(7/6), x)

$$3.1840 \quad \int \frac{1}{(a+bx)^{7/6} \sqrt[6]{c+dx}} dx$$

Optimal. Leaf size=72

$$\frac{6\sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{1}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[6]{a+bx} \sqrt[6]{c+dx}}$$

[Out] $-6*(b*(d*x+c)/(-a*d+b*c))^{(1/6)}*\text{hypergeom}([-1/6, 1/6], [5/6], -d*(b*x+a)/(-a*d+b*c))/b/(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6\sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{1}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[6]{a+bx} \sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/6)*(c + d*x)^(1/6)),x]

[Out] $(-6*((b*(c + d*x))/(b*c - a*d))^{(1/6)}*\text{Hypergeometric2F1}[-1/6, 1/6, 5/6, -((d*(a + b*x))/(b*c - a*d))])/((b*(a + b*x))^{(1/6)}*(c + d*x)^{(1/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/((b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{7/6} \sqrt[6]{c+dx}} dx = \frac{\sqrt[6]{\frac{b(c+dx)}{bc-ad}} \int \frac{1}{(a+bx)^{7/6} \sqrt[6]{\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}}} dx}{\sqrt[6]{c+dx}}$$

$$= -\frac{6\sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{1}{6}, \frac{5}{6}, -\frac{d(a+bx)}{bc-ad}\right)}{b\sqrt[6]{a+bx} \sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.03, size = 71, normalized size = 0.99

$$-\frac{6\sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{1}{6}, \frac{5}{6}, \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[6]{a+bx} \sqrt[6]{c+dx}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/6)*(c + d*x)^(1/6)), x]

[Out] (-6*((b*(c + d*x))/(b*c - a*d))^(1/6)*Hypergeometric2F1[-1/6, 1/6, 5/6, (d*(a + b*x))/(-b*c) + a*d])/(b*(a + b*x)^(1/6)*(c + d*x)^(1/6))

fricas [F] time = 1.85, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{5}{6}}}{b^2dx^3+a^2c+(b^2c+2abd)x^2+(2abc+a^2d)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(1/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(b^2*d*x^3 + a^2*c + (b^2*c + 2*a*b*d)*x^2 + (2*a*b*c + a^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{6}}(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(1/6), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(1/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{6}}(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/6)/(d*x+c)^(1/6),x)

[Out] int(1/(b*x+a)^(7/6)/(d*x+c)^(1/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{6}}(dx+c)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(1/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(1/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a+bx)^{\frac{7}{6}}(c+dx)^{\frac{1}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/6)*(c + d*x)^(1/6)),x)

[Out] int(1/((a + b*x)^(7/6)*(c + d*x)^(1/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+bx)^{\frac{7}{6}}\sqrt[6]{c+dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/6)/(d*x+c)**(1/6),x)

[Out] Integral(1/((a + b*x)**(7/6)*(c + d*x)**(1/6)), x)

$$3.1841 \quad \int \frac{1}{(a+bx)^{7/6}(c+dx)^{7/6}} dx$$

Optimal. Leaf size=79

$$-\frac{6\sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{7}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{\sqrt[6]{a+bx} \sqrt[6]{c+dx} (bc-ad)}$$

[Out] $-6*(b*(d*x+c)/(-a*d+b*c))^{(1/6)}*\text{hypergeom}([-1/6, 7/6], [5/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)/(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$-\frac{6\sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{7}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{\sqrt[6]{a+bx} \sqrt[6]{c+dx} (bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/6)*(c + d*x)^(7/6)), x]

[Out] $(-6*((b*(c + d*x))/(b*c - a*d))^{(1/6)}*\text{Hypergeometric2F1}[-1/6, 7/6, 5/6, -((d*(a + b*x))/(b*c - a*d))])/((b*c - a*d)*(a + b*x)^{(1/6)*(c + d*x)^{(1/6)}}$

Rule 69

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{7/6}} dx = \frac{\left(b\sqrt[6]{\frac{b(c+dx)}{bc-ad}}\right) \int \frac{1}{(a+bx)^{7/6}\left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{7/6}} dx}{(bc-ad)\sqrt[6]{c+dx}}$$

$$= -\frac{6\sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{7}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{(bc-ad)\sqrt[6]{a+bx}\sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.05, size = 71, normalized size = 0.90

$$-\frac{6\left(\frac{b(c+dx)}{bc-ad}\right)^{7/6} {}_2F_1\left(-\frac{1}{6}, \frac{7}{6}; \frac{5}{6}; \frac{d(a+bx)}{ad-bc}\right)}{b\sqrt[6]{a+bx}(c+dx)^{7/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/6)*(c + d*x)^(7/6)), x]

[Out] (-6*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[-1/6, 7/6, 5/6, (d*(a + b*x))/(-b*c + a*d)])/(b*(a + b*x)^(1/6)*(c + d*x)^(7/6))

fricas [F] time = 1.64, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx+a)^{5/6}(dx+c)^{5/6}}{b^2d^2x^4 + a^2c^2 + 2(b^2cd + abd^2)x^3 + (b^2c^2 + 4abcd + a^2d^2)x^2 + 2(abc^2 + a^2cd)x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(7/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(b^2*d^2*x^4 + a^2*c^2 + 2*(b^2*c*d + a*b*d^2)*x^3 + (b^2*c^2 + 4*a*b*c*d + a^2*d^2)*x^2 + 2*(a*b*c^2 + a^2*c*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{7/6}(dx+c)^{7/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(7/6), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(7/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{6}} (dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/6)/(d*x+c)^(7/6), x)

[Out] int(1/(b*x+a)^(7/6)/(d*x+c)^(7/6), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{6}} (dx + c)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(7/6), x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(7/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{\frac{7}{6}} (c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/6)*(c + d*x)^(7/6)), x)

[Out] int(1/((a + b*x)^(7/6)*(c + d*x)^(7/6)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + bx)^{\frac{7}{6}} (c + dx)^{\frac{7}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/6)/(d*x+c)**(7/6), x)

[Out] Integral(1/((a + b*x)**(7/6)*(c + d*x)**(7/6)), x)

$$3.1842 \quad \int \frac{1}{(a+bx)^{7/6}(c+dx)^{13/6}} dx$$

Optimal. Leaf size=80

$$\frac{6b \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{13}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{\sqrt[6]{a+bx} \sqrt[6]{c+dx} (bc-ad)^2}$$

[Out] $-6*b*(b*(d*x+c)/(-a*d+b*c))^{(1/6)}*\text{hypergeom}([-1/6, 13/6], [5/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^2/(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6b \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{13}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{\sqrt[6]{a+bx} \sqrt[6]{c+dx} (bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/6)*(c + d*x)^(13/6)), x]

[Out] $(-6*b*((b*(c + d*x))/(b*c - a*d))^{(1/6)}*\text{Hypergeometric2F1}[-1/6, 13/6, 5/6, -((d*(a + b*x))/(b*c - a*d))]/((b*c - a*d)^2*(a + b*x)^{(1/6)*(c + d*x)^{(1/6)})}$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{13/6}} dx = \frac{\left(b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}\right) \int \frac{1}{(a+bx)^{7/6} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{13/6}} dx}{(bc-ad)^2 \sqrt[6]{c+dx}}$$

$$= -\frac{6b \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{13}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{(bc-ad)^2 \sqrt[6]{a+bx} \sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.06, size = 71, normalized size = 0.89

$$-\frac{6 \left(\frac{b(c+dx)}{bc-ad}\right)^{13/6} {}_2F_1\left(-\frac{1}{6}, \frac{13}{6}; \frac{5}{6}; \frac{d(a+bx)}{ad-bc}\right)}{b \sqrt[6]{a+bx} (c+dx)^{13/6}}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/6)*(c + d*x)^(13/6)),x]

[Out] (-6*((b*(c + d*x))/(b*c - a*d))^(13/6)*Hypergeometric2F1[-1/6, 13/6, 5/6, (d*(a + b*x))/(-b*c + a*d)])/(b*(a + b*x)^(1/6)*(c + d*x)^(13/6))

fricas [F] time = 1.52, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^5(dx+c)^5}{b^2d^3x^5 + a^2c^3 + (3b^2cd^2 + 2abd^3)x^4 + (3b^2c^2d + 6abcd^2 + a^2d^3)x^3 + (b^2c^3 + 6abc^2d + 3a^2cd^2)x^2 + \dots} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(13/6),x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(b^2*d^3*x^5 + a^2*c^3 + (3*b^2*c*d^2 + 2*a*b*d^3)*x^4 + (3*b^2*c^2*d + 6*a*b*c*d^2 + a^2*d^3)*x^3 + (b^2*c^3 + 6*a*b*c^2*d + 3*a^2*c*d^2)*x^2 + (2*a*b*c^3 + 3*a^2*c^2*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{7/6}(dx+c)^{13/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(13/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(13/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{6}} (dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/6)/(d*x+c)^(13/6),x)

[Out] int(1/(b*x+a)^(7/6)/(d*x+c)^(13/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{6}} (dx + c)^{\frac{13}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(13/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(13/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{7/6} (c + dx)^{13/6}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/6)*(c + d*x)^(13/6)),x)

[Out] int(1/((a + b*x)^(7/6)*(c + d*x)^(13/6)), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/6)/(d*x+c)**(13/6),x)

[Out] Timed out

$$3.1843 \quad \int \frac{1}{(a+bx)^{7/6}(c+dx)^{19/6}} dx$$

Optimal. Leaf size=82

$$\frac{6b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{19}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{\sqrt[6]{a+bx} \sqrt[6]{c+dx} (bc-ad)^3}$$

[Out] $-6*b^2*(b*(d*x+c)/(-a*d+b*c))^{(1/6)}*\text{hypergeom}([-1/6, 19/6], [5/6], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^3/(b*x+a)^{(1/6)}/(d*x+c)^{(1/6)}$

Rubi [A] time = 0.02, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{6b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{19}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{\sqrt[6]{a+bx} \sqrt[6]{c+dx} (bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Int[1/((a + b*x)^(7/6)*(c + d*x)^(19/6)), x]

[Out] $(-6*b^2*((b*(c + d*x))/(b*c - a*d))^{(1/6)}*\text{Hypergeometric2F1}[-1/6, 19/6, 5/6, -(d*(a + b*x))/(b*c - a*d)])/((b*c - a*d)^3*(a + b*x)^{(1/6)}*(c + d*x)^{(1/6)})$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -(d*(a + b*x))/(b*c - a*d)])/(b*(m + 1)*(b*(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int \frac{1}{(a+bx)^{7/6}(c+dx)^{19/6}} dx = \frac{\left(b^3 \sqrt[6]{\frac{b(c+dx)}{bc-ad}}\right) \int \frac{1}{(a+bx)^{7/6} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad}\right)^{19/6}} dx}{(bc-ad)^3 \sqrt[6]{c+dx}}$$

$$= \frac{6b^2 \sqrt[6]{\frac{b(c+dx)}{bc-ad}} {}_2F_1\left(-\frac{1}{6}, \frac{19}{6}; \frac{5}{6}; -\frac{d(a+bx)}{bc-ad}\right)}{(bc-ad)^3 \sqrt[6]{a+bx} \sqrt[6]{c+dx}}$$

Mathematica [A] time = 0.05, size = 79, normalized size = 0.96

$$\frac{6b \left(\frac{b(c+dx)}{bc-ad}\right)^{7/6} {}_2F_1\left(-\frac{1}{6}, \frac{19}{6}; \frac{5}{6}; \frac{d(a+bx)}{ad-bc}\right)}{\sqrt[6]{a+bx} (c+dx)^{7/6} (bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((a + b*x)^(7/6)*(c + d*x)^(19/6)), x]

[Out] (-6*b*((b*(c + d*x))/(b*c - a*d))^(7/6)*Hypergeometric2F1[-1/6, 19/6, 5/6, (d*(a + b*x))/(-b*c + a*d)]/((b*c - a*d)^2*(a + b*x)^(1/6)*(c + d*x)^(7/6))

fricas [F] time = 1.69, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx+a)^{\frac{5}{6}}(dx+c)^{\frac{5}{6}}}{b^2d^4x^6 + a^2c^4 + 2(2b^2cd^3 + abd^4)x^5 + (6b^2c^2d^2 + 8abcd^3 + a^2d^4)x^4 + 4(b^2c^3d + 3abc^2d^2 + a^2cd^3)x^3 + 2(a^2c^3d + 3abc^2d^2 + a^2cd^3)x^2 + 2(a^2c^3d + 3abc^2d^2 + a^2cd^3)x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(19/6), x, algorithm="fricas")

[Out] integral((b*x + a)^(5/6)*(d*x + c)^(5/6)/(b^2*d^4*x^6 + a^2*c^4 + 2*(2*b^2*c*d^3 + a*b*d^4)*x^5 + (6*b^2*c^2*d^2 + 8*a*b*c*d^3 + a^2*d^4)*x^4 + 4*(b^2*c^3*d + 3*a*b*c^2*d^2 + a^2*c*d^3)*x^3 + (b^2*c^4 + 8*a*b*c^3*d + 6*a^2*c^2*d^2)*x^2 + 2*(a*b*c^4 + 2*a^2*c^3*d)*x), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx+a)^{\frac{7}{6}}(dx+c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(19/6),x, algorithm="giac")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(19/6)), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{6}} (dx + c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^(7/6)/(d*x+c)^(19/6),x)

[Out] int(1/(b*x+a)^(7/6)/(d*x+c)^(19/6),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{7}{6}} (dx + c)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^(7/6)/(d*x+c)^(19/6),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^(7/6)*(d*x + c)^(19/6)), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + bx)^{\frac{7}{6}} (c + dx)^{\frac{19}{6}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^(7/6)*(c + d*x)^(19/6)),x)

[Out] int(1/((a + b*x)^(7/6)*(c + d*x)^(19/6)), x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**(7/6)/(d*x+c)**(19/6),x)

[Out] Timed out

$$3.1844 \quad \int (a + bx)^m (a + b(2 + m)x) dx$$

Optimal. Leaf size=11

$$x(a + bx)^{m+1}$$

[Out] x*(b*x+a)^(1+m)

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {34}

$$x(a + bx)^{m+1}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^m*(a + b*(2 + m)*x), x]

[Out] x*(a + b*x)^(1 + m)

Rule 34

Int[((a_) + (b_.)*(x_))^(m_.)*((c_) + (d_.)*(x_)), x_Symbol] :> Simp[(d*x*(a + b*x)^(m + 1))/(b*(m + 2)), x] /; FreeQ[{a, b, c, d, m}, x] && EqQ[a*d - b*c*(m + 2), 0]

Rubi steps

$$\int (a + bx)^m (a + b(2 + m)x) dx = x(a + bx)^{1+m}$$

Mathematica [A] time = 0.01, size = 11, normalized size = 1.00

$$x(a + bx)^{m+1}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^m*(a + b*(2 + m)*x), x]

[Out] x*(a + b*x)^(1 + m)

fricas [A] time = 0.99, size = 17, normalized size = 1.55

$$(bx^2 + ax)(bx + a)^m$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(a+b*(2+m)*x),x, algorithm="fricas")

[Out] (b*x^2 + a*x)*(b*x + a)^m

giac [B] time = 1.00, size = 23, normalized size = 2.09

$$(bx + a)^m bx^2 + (bx + a)^m ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(a+b*(2+m)*x),x, algorithm="giac")

[Out] (b*x + a)^m*b*x^2 + (b*x + a)^m*a*x

maple [A] time = 0.00, size = 12, normalized size = 1.09

$$x(bx + a)^{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^m*(a+b*(m+2)*x),x)

[Out] x*(b*x+a)^(m+1)

maxima [B] time = 1.12, size = 106, normalized size = 9.64

$$\frac{(b^2(m+1)x^2 + abmx - a^2)(bx + a)^m m}{(m^2 + 3m + 2)b} + \frac{2(b^2(m+1)x^2 + abmx - a^2)(bx + a)^m}{(m^2 + 3m + 2)b} + \frac{(bx + a)^{m+1} a}{b(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(a+b*(2+m)*x),x, algorithm="maxima")

[Out] (b^2*(m + 1)*x^2 + a*b*m*x - a^2)*(b*x + a)^m*m/((m^2 + 3*m + 2)*b) + 2*(b^2*(m + 1)*x^2 + a*b*m*x - a^2)*(b*x + a)^m/((m^2 + 3*m + 2)*b) + (b*x + a)^(m + 1)*a/(b*(m + 1))

mupad [B] time = 0.46, size = 11, normalized size = 1.00

$$x(a + bx)^{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x*(m + 2))*(a + b*x)^m,x)

[Out] x*(a + b*x)^(m + 1)

sympy [B] time = 0.27, size = 20, normalized size = 1.82

$$ax(a + bx)^m + bx^2(a + bx)^m$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**m*(a+b*(2+m)*x),x)

[Out] a*x*(a + b*x)**m + b*x**2*(a + b*x)**m

3.1845 $\int (a + bx)^m (c + dx)^n dx$

Optimal. Leaf size=61

$$-\frac{(a + bx)^{m+1}(c + dx)^{n+1} {}_2F_1\left(1, m + n + 2; n + 2; \frac{b(c+dx)}{bc-ad}\right)}{(n + 1)(bc - ad)}$$

[Out] $-(b*x+a)^{(1+m)}*(d*x+c)^{(1+n)}*\text{hypergeom}([1, 2+m+n], [2+n], b*(d*x+c)/(-a*d+b*c))/(-a*d+b*c)/(1+n)$

Rubi [A] time = 0.03, antiderivative size = 74, normalized size of antiderivative = 1.21, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {70, 69}

$$\frac{(a + bx)^{m+1}(c + dx)^n \left(\frac{b(c+dx)}{bc-ad}\right)^{-n} {}_2F_1\left(m + 1, -n; m + 2; -\frac{d(a+bx)}{bc-ad}\right)}{b(m + 1)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^m*(c + d*x)^n,x]

[Out] $((a + b*x)^{(1 + m)}*(c + d*x)^n*\text{Hypergeometric2F1}[1 + m, -n, 2 + m, -((d*(a + b*x))/(b*c - a*d))])/(b*(1 + m)*((b*(c + d*x))/(b*c - a*d))^n)$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int (a + bx)^m (c + dx)^n dx = \left((c + dx)^n \left(\frac{b(c + dx)}{bc - ad} \right)^{-n} \right) \int (a + bx)^m \left(\frac{bc}{bc - ad} + \frac{bdx}{bc - ad} \right)^n dx$$

$$= \frac{(a + bx)^{1+m} (c + dx)^n \left(\frac{b(c+dx)}{bc-ad} \right)^{-n} {}_2F_1 \left(1 + m, -n; 2 + m; -\frac{d(a+bx)}{bc-ad} \right)}{b(1 + m)}$$

Mathematica [A] time = 0.04, size = 73, normalized size = 1.20

$$\frac{(a + bx)^{m+1} (c + dx)^n \left(\frac{b(c+dx)}{bc-ad} \right)^{-n} {}_2F_1 \left(m + 1, -n; m + 2; \frac{d(a+bx)}{ad-bc} \right)}{b(m + 1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^m*(c + d*x)^n,x]

[Out] ((a + b*x)^(1 + m)*(c + d*x)^n*Hypergeometric2F1[1 + m, -n, 2 + m, (d*(a + b*x))/(-(b*c) + a*d)])/(b*(1 + m)*((b*(c + d*x))/(b*c - a*d))^n)

fricas [F] time = 0.68, size = 0, normalized size = 0.00

$$\text{integral} \left((bx + a)^m (dx + c)^n, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(d*x+c)^n,x, algorithm="fricas")

[Out] integral((b*x + a)^m*(d*x + c)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^m (dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(d*x+c)^n,x, algorithm="giac")

[Out] integrate((b*x + a)^m*(d*x + c)^n, x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^m (dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^m*(d*x+c)^n,x)`

[Out] `int((b*x+a)^m*(d*x+c)^n,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^m (dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^m*(d*x+c)^n,x, algorithm="maxima")`

[Out] `integrate((b*x + a)^m*(d*x + c)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (a + bx)^m (c + dx)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^m*(c + d*x)^n,x)`

[Out] `int((a + b*x)^m*(c + d*x)^n, x)`

sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**m*(d*x+c)**n,x)`

[Out] Exception raised: HeuristicGCDFailed

3.1846 $\int (a + bx)^m (c + dx)^3 dx$

Optimal. Leaf size=110

$$\frac{3d^2(bc - ad)(a + bx)^{m+3}}{b^4(m + 3)} + \frac{(bc - ad)^3(a + bx)^{m+1}}{b^4(m + 1)} + \frac{3d(bc - ad)^2(a + bx)^{m+2}}{b^4(m + 2)} + \frac{d^3(a + bx)^{m+4}}{b^4(m + 4)}$$

[Out] $(-a*d+b*c)^3*(b*x+a)^(1+m)/b^4/(1+m)+3*d*(-a*d+b*c)^2*(b*x+a)^(2+m)/b^4/(2+m)+3*d^2*(-a*d+b*c)*(b*x+a)^(3+m)/b^4/(3+m)+d^3*(b*x+a)^(4+m)/b^4/(4+m)$

Rubi [A] time = 0.05, antiderivative size = 110, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{3d^2(bc - ad)(a + bx)^{m+3}}{b^4(m + 3)} + \frac{(bc - ad)^3(a + bx)^{m+1}}{b^4(m + 1)} + \frac{3d(bc - ad)^2(a + bx)^{m+2}}{b^4(m + 2)} + \frac{d^3(a + bx)^{m+4}}{b^4(m + 4)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^m*(c + d*x)^3, x]

[Out] $((b*c - a*d)^3*(a + b*x)^(1 + m))/(b^4*(1 + m)) + (3*d*(b*c - a*d)^2*(a + b*x)^(2 + m))/(b^4*(2 + m)) + (3*d^2*(b*c - a*d)*(a + b*x)^(3 + m))/(b^4*(3 + m)) + (d^3*(a + b*x)^(4 + m))/(b^4*(4 + m))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^m (c + dx)^3 dx &= \int \left(\frac{(bc - ad)^3(a + bx)^m}{b^3} + \frac{3d(bc - ad)^2(a + bx)^{1+m}}{b^3} + \frac{3d^2(bc - ad)(a + bx)^{2+m}}{b^3} + \frac{d^3(a + bx)^{3+m}}{b^3} \right) dx \\ &= \frac{(bc - ad)^3(a + bx)^{1+m}}{b^4(1 + m)} + \frac{3d(bc - ad)^2(a + bx)^{2+m}}{b^4(2 + m)} + \frac{3d^2(bc - ad)(a + bx)^{3+m}}{b^4(3 + m)} + \frac{d^3(a + bx)^{4+m}}{b^4(4 + m)} \end{aligned}$$

Mathematica [A] time = 0.11, size = 94, normalized size = 0.85

$$\frac{(a + bx)^{m+1} \left(\frac{3d^2(a+bx)^2(bc-ad)}{m+3} + \frac{3d(a+bx)(bc-ad)^2}{m+2} + \frac{(bc-ad)^3}{m+1} + \frac{d^3(a+bx)^3}{m+4} \right)}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((a + b*x)^m*(c + d*x)^3, x)$

[Out] $(d^3*x^4*(a + b*x)^m*(11*m + 6*m^2 + m^3 + 6))/(50*m + 35*m^2 + 10*m^3 + m^4 + 24) + (a*(a + b*x)^m*(24*b^3*c^3 - 6*a^3*d^3 + 26*b^3*c^3*m + 9*b^3*c^3*m^2 + b^3*c^3*m^3 - 36*a*b^2*c^2*d + 24*a^2*b*c*d^2 - 21*a*b^2*c^2*d*m + 6*a^2*b*c*d^2*m - 3*a*b^2*c^2*d*m^2))/(b^4*(50*m + 35*m^2 + 10*m^3 + m^4 + 24)) + (x*(a + b*x)^m*(24*b^4*c^3 + 26*b^4*c^3*m + 9*b^4*c^3*m^2 + b^4*c^3*m^3 + 6*a^3*b*d^3*m + 36*a*b^3*c^2*d*m - 24*a^2*b^2*c*d^2*m + 21*a*b^3*c^2*d*m^2 + 3*a*b^3*c^2*d*m^3 - 6*a^2*b^2*c*d^2*m^2))/(b^4*(50*m + 35*m^2 + 10*m^3 + m^4 + 24)) + (3*d*x^2*(m + 1)*(a + b*x)^m*(12*b^2*c^2 - a^2*d^2*m + 7*b^2*c^2*m + b^2*c^2*m^2 + 4*a*b*c*d*m + a*b*c*d*m^2))/(b^2*(50*m + 35*m^2 + 10*m^3 + m^4 + 24)) + (d^2*x^3*(a + b*x)^m*(12*b*c + a*d*m + 3*b*c*m)*(3*m + m^2 + 2))/(b*(50*m + 35*m^2 + 10*m^3 + m^4 + 24))$

sympy [A] time = 4.67, size = 4058, normalized size = 36.89

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((b*x+a)**m*(d*x+c)**3, x)$

[Out] $\text{Piecewise}((a**m*(c**3*x + 3*c**2*d*x**2/2 + c*d**2*x**3 + d**3*x**4/4), \text{Eq}(b, 0)), (6*a**3*d**3*\log(a/b + x)/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 11*a**3*d**3/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) - 6*a**2*b*c*d**2/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 18*a**2*b*d**3*x*\log(a/b + x)/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 27*a**2*b*d**3*x/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) - 3*a*b**2*c**2*d/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) - 18*a*b**2*c*d**2*x/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 18*a*b**2*d**3*x**2*\log(a/b + x)/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 18*a*b**2*d**3*x**2/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) - 2*b**3*c**3/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) - 9*b**3*c**2*d*x/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) - 18*b**3*c*d**2*x**2/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3) + 6*b**3*d**3*x**3*\log(a/b + x)/(6*a**3*b**4 + 18*a**2*b**5*x + 18*a*b**6*x**2 + 6*b**7*x**3), \text{Eq}(m, -4)), (-6*a**3*d**3*\log(a/b + x)/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) - 9*a**3*d**3/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) + 6*a**2*b*c*d**2*\log(a/b + x)/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) + 9*a**2*b*c*d**2/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) - 12*a**2*b*d**3*x*\log(a/b + x)/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) - 12*a**2*b*d**3*x/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) - 3*a*b**2*c**2*d/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) + 12*a*b**$

$$\begin{aligned}
& 2*c*d**2*x*log(a/b + x)/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) + 12*a*b** \\
& 2*c*d**2*x/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) - 6*a*b**2*d**3*x**2*log \\
& g(a/b + x)/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2) - b**3*c**3/(2*a**2*b** \\
& 4 + 4*a*b**5*x + 2*b**6*x**2) - 6*b**3*c**2*d*x/(2*a**2*b**4 + 4*a*b**5*x + \\
& 2*b**6*x**2) + 6*b**3*c*d**2*x**2*log(a/b + x)/(2*a**2*b**4 + 4*a*b**5*x + \\
& 2*b**6*x**2) + 2*b**3*d**3*x**3/(2*a**2*b**4 + 4*a*b**5*x + 2*b**6*x**2), \\
& Eq(m, -3)), (6*a**3*d**3*log(a/b + x)/(2*a*b**4 + 2*b**5*x) + 6*a**3*d**3/(\\
& 2*a*b**4 + 2*b**5*x) - 12*a**2*b*c*d**2*log(a/b + x)/(2*a*b**4 + 2*b**5*x) \\
& - 12*a**2*b*c*d**2/(2*a*b**4 + 2*b**5*x) + 6*a**2*b*d**3*x*log(a/b + x)/(2* \\
& a*b**4 + 2*b**5*x) + 6*a*b**2*c**2*d*log(a/b + x)/(2*a*b**4 + 2*b**5*x) + 6 \\
& *a*b**2*c**2*d/(2*a*b**4 + 2*b**5*x) - 12*a*b**2*c*d**2*x*log(a/b + x)/(2*a \\
& *b**4 + 2*b**5*x) - 3*a*b**2*d**3*x**2/(2*a*b**4 + 2*b**5*x) - 2*b**3*c**3/ \\
& (2*a*b**4 + 2*b**5*x) + 6*b**3*c**2*d*x*log(a/b + x)/(2*a*b**4 + 2*b**5*x) \\
& + 6*b**3*c*d**2*x**2/(2*a*b**4 + 2*b**5*x) + b**3*d**3*x**3/(2*a*b**4 + 2*b \\
& **5*x), Eq(m, -2)), (-a**3*d**3*log(a/b + x)/b**4 + 3*a**2*c*d**2*log(a/b + \\
& x)/b**3 + a**2*d**3*x/b**3 - 3*a*c**2*d*log(a/b + x)/b**2 - 3*a*c*d**2*x/b \\
& **2 - a*d**3*x**2/(2*b**2) + c**3*log(a/b + x)/b + 3*c**2*d*x/b + 3*c*d**2* \\
& x**2/(2*b) + d**3*x**3/(3*b), Eq(m, -1)), (-6*a**4*d**3*(a + b*x)**m/(b**4* \\
& m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 6*a**3*b*c*d**2 \\
& *m*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b \\
& **4) + 24*a**3*b*c*d**2*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m** \\
& *2 + 50*b**4*m + 24*b**4) + 6*a**3*b*d**3*m*x*(a + b*x)**m/(b**4*m**4 + 10* \\
& b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) - 3*a**2*b**2*c**2*d*m**2*(\\
& a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) \\
& - 21*a**2*b**2*c**2*d*m*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m \\
& **2 + 50*b**4*m + 24*b**4) - 36*a**2*b**2*c**2*d*(a + b*x)**m/(b**4*m**4 + \\
& 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) - 6*a**2*b**2*c*d**2*m** \\
& 2*x*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24* \\
& b**4) - 24*a**2*b**2*c*d**2*m*x*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35 \\
& *b**4*m**2 + 50*b**4*m + 24*b**4) - 3*a**2*b**2*d**3*m**2*x**2*(a + b*x)**m \\
& /(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) - 3*a**2*b \\
& **2*d**3*m*x**2*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50* \\
& b**4*m + 24*b**4) + a*b**3*c**3*m**3*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 \\
& + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 9*a*b**3*c**3*m**2*(a + b*x)**m/(b \\
& **4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 26*a*b**3*c \\
& **3*m*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 2 \\
& 4*b**4) + 24*a*b**3*c**3*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m \\
& **2 + 50*b**4*m + 24*b**4) + 3*a*b**3*c**2*d*m**3*x*(a + b*x)**m/(b**4*m**4 \\
& + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 21*a*b**3*c**2*d*m* \\
& *2*x*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24 \\
& *b**4) + 36*a*b**3*c**2*d*m*x*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b \\
& **4*m**2 + 50*b**4*m + 24*b**4) + 3*a*b**3*c*d**2*m**3*x**2*(a + b*x)**m/(b \\
& **4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 15*a*b**3*c \\
& *d**2*m**2*x**2*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50* \\
& b**4*m + 24*b**4) + 12*a*b**3*c*d**2*m*x**2*(a + b*x)**m/(b**4*m**4 + 10*b*
\end{aligned}$$

```

*4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + a*b**3*d**3*m**3*x**3*(a +
b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 3
*a*b**3*d**3*m**2*x**3*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**
2 + 50*b**4*m + 24*b**4) + 2*a*b**3*d**3*m*x**3*(a + b*x)**m/(b**4*m**4 + 1
0*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + b**4*c**3*m**3*x*(a + b
*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 9*
b**4*c**3*m**2*x*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50
*b**4*m + 24*b**4) + 26*b**4*c**3*m*x*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**
3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 24*b**4*c**3*x*(a + b*x)**m/(b**4
*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 3*b**4*c**2*d
m**3*x**2*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m
+ 24*b**4) + 24*b**4*c**2*d*m**2*x**2*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**
3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 57*b**4*c**2*d*m*x**2*(a + b*x)*
**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 36*b**
4*c**2*d*x**2*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b
**4*m + 24*b**4) + 3*b**4*c*d**2*m**3*x**3*(a + b*x)**m/(b**4*m**4 + 10*b**4
*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 21*b**4*c*d**2*m**2*x**3*(a +
b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) +
42*b**4*c*d**2*m*x**3*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2
+ 50*b**4*m + 24*b**4) + 24*b**4*c*d**2*x**3*(a + b*x)**m/(b**4*m**4 + 10*
b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + b**4*d**3*m**3*x**4*(a +
b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 6
*b**4*d**3*m**2*x**4*(a + b*x)**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2
+ 50*b**4*m + 24*b**4) + 11*b**4*d**3*m*x**4*(a + b*x)**m/(b**4*m**4 + 10*b
**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4) + 6*b**4*d**3*x**4*(a + b*x)
**m/(b**4*m**4 + 10*b**4*m**3 + 35*b**4*m**2 + 50*b**4*m + 24*b**4), True))

```

3.1847 $\int (a + bx)^m (c + dx)^2 dx$

Optimal. Leaf size=78

$$\frac{(bc - ad)^2(a + bx)^{m+1}}{b^3(m + 1)} + \frac{2d(bc - ad)(a + bx)^{m+2}}{b^3(m + 2)} + \frac{d^2(a + bx)^{m+3}}{b^3(m + 3)}$$

[Out] $(-a*d+b*c)^2*(b*x+a)^{(1+m)}/b^3/(1+m)+2*d*(-a*d+b*c)*(b*x+a)^{(2+m)}/b^3/(2+m)+d^2*(b*x+a)^{(3+m)}/b^3/(3+m)$

Rubi [A] time = 0.03, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{(bc - ad)^2(a + bx)^{m+1}}{b^3(m + 1)} + \frac{2d(bc - ad)(a + bx)^{m+2}}{b^3(m + 2)} + \frac{d^2(a + bx)^{m+3}}{b^3(m + 3)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^m*(c + d*x)^2,x]

[Out] $((b*c - a*d)^2*(a + b*x)^{(1 + m)})/(b^3*(1 + m)) + (2*d*(b*c - a*d)*(a + b*x)^{(2 + m)})/(b^3*(2 + m)) + (d^2*(a + b*x)^{(3 + m)})/(b^3*(3 + m))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^m (c + dx)^2 dx &= \int \left(\frac{(bc - ad)^2(a + bx)^m}{b^2} + \frac{2d(bc - ad)(a + bx)^{1+m}}{b^2} + \frac{d^2(a + bx)^{2+m}}{b^2} \right) dx \\ &= \frac{(bc - ad)^2(a + bx)^{1+m}}{b^3(1 + m)} + \frac{2d(bc - ad)(a + bx)^{2+m}}{b^3(2 + m)} + \frac{d^2(a + bx)^{3+m}}{b^3(3 + m)} \end{aligned}$$

Mathematica [A] time = 0.10, size = 67, normalized size = 0.86

$$\frac{(a + bx)^{m+1} \left(\frac{2d(a+bx)(bc-ad)}{m+2} + \frac{(bc-ad)^2}{m+1} + \frac{d^2(a+bx)^2}{m+3} \right)}{b^3}$$

[In] int((b*x+a)^m*(d*x+c)^2,x)

[Out] (b*x+a)^(m+1)*(b^2*d^2*m^2*x^2+2*b^2*c*d*m^2*x+3*b^2*d^2*m*x^2-2*a*b*d^2*m*x+b^2*c^2*m^2+8*b^2*c*d*m*x+2*b^2*d^2*x^2-2*a*b*c*d*m-2*a*b*d^2*x+5*b^2*c^2*m+6*b^2*c*d*x+2*a^2*d^2-6*a*b*c*d+6*b^2*c^2)/b^3/(m^3+6*m^2+11*m+6)

maxima [A] time = 1.15, size = 138, normalized size = 1.77

$$\frac{2(b^2(m+1)x^2 + abmx - a^2)(bx + a)^m cd}{(m^2 + 3m + 2)b^2} + \frac{(bx + a)^{m+1}c^2}{b(m+1)} + \frac{((m^2 + 3m + 2)b^3x^3 + (m^2 + m)ab^2x^2 - 2a^2bmx + 2(m^3 + 6m^2 + 11m + 6)b^3)}{(m^3 + 6m^2 + 11m + 6)b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(d*x+c)^2,x, algorithm="maxima")

[Out] 2*(b^2*(m+1)*x^2 + a*b*m*x - a^2)*(b*x + a)^m*c*d/((m^2 + 3*m + 2)*b^2) + (b*x + a)^(m+1)*c^2/(b*(m+1)) + ((m^2 + 3*m + 2)*b^3*x^3 + (m^2 + m)*b^2*x^2 - 2*a^2*b*m*x + 2*a^3)*(b*x + a)^m*d^2/((m^3 + 6*m^2 + 11*m + 6)*b^3)

mapad [B] time = 0.66, size = 226, normalized size = 2.90

$$(a + bx)^m \left(\frac{a(2a^2d^2 - 2abcdm - 6abcd + b^2c^2m^2 + 5b^2c^2m + 6b^2c^2)}{b^3(m^3 + 6m^2 + 11m + 6)} + \frac{d^2x^3(m^2 + 3m + 2)}{m^3 + 6m^2 + 11m + 6} + \frac{x(-2a^2)}{m^3 + 6m^2 + 11m + 6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^m*(c + d*x)^2,x)

[Out] (a + b*x)^m*((a*(2*a^2*d^2 + 6*b^2*c^2 + 5*b^2*c^2*m + b^2*c^2*m^2 - 6*a*b*c*d - 2*a*b*c*d*m))/(b^3*(11*m + 6*m^2 + m^3 + 6)) + (d^2*x^3*(3*m + m^2 + 2))/(11*m + 6*m^2 + m^3 + 6) + (x*(6*b^3*c^2 + 5*b^3*c^2*m + b^3*c^2*m^2 - 2*a^2*b*d^2*m + 2*a*b^2*c*d*m^2 + 6*a*b^2*c*d*m))/(b^3*(11*m + 6*m^2 + m^3 + 6)) + (d*x^2*(m + 1)*(6*b*c + a*d*m + 2*b*c*m))/(b*(11*m + 6*m^2 + m^3 + 6)))

sympy [A] time = 2.14, size = 1506, normalized size = 19.31

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**m*(d*x+c)**2,x)

[Out] Piecewise((a**m*(c**2*x + c*d*x**2 + d**2*x**3/3), Eq(b, 0)), (2*a**2*d**2*log(a/b + x)/(2*a**2*b**3 + 4*a*b**4*x + 2*b**5*x**2) + 3*a**2*d**2/(2*a**2

```

*b**3 + 4*a*b**4*x + 2*b**5*x**2) - 2*a*b*c*d/(2*a**2*b**3 + 4*a*b**4*x + 2
*b**5*x**2) + 4*a*b*d**2*x*log(a/b + x)/(2*a**2*b**3 + 4*a*b**4*x + 2*b**5*
x**2) + 4*a*b*d**2*x/(2*a**2*b**3 + 4*a*b**4*x + 2*b**5*x**2) - b**2*c**2/(
2*a**2*b**3 + 4*a*b**4*x + 2*b**5*x**2) - 4*b**2*c*d*x/(2*a**2*b**3 + 4*a*b
**4*x + 2*b**5*x**2) + 2*b**2*d**2*x**2*log(a/b + x)/(2*a**2*b**3 + 4*a*b**
4*x + 2*b**5*x**2), Eq(m, -3)), (-2*a**2*d**2*log(a/b + x)/(a*b**3 + b**4*x
) - 2*a**2*d**2/(a*b**3 + b**4*x) + 2*a*b*c*d*log(a/b + x)/(a*b**3 + b**4*x
) + 2*a*b*c*d/(a*b**3 + b**4*x) - 2*a*b*d**2*x*log(a/b + x)/(a*b**3 + b**4*
x) - b**2*c**2/(a*b**3 + b**4*x) + 2*b**2*c*d*x*log(a/b + x)/(a*b**3 + b**4
*x) + b**2*d**2*x**2/(a*b**3 + b**4*x), Eq(m, -2)), (a**2*d**2*log(a/b + x)
/b**3 - 2*a*c*d*log(a/b + x)/b**2 - a*d**2*x/b**2 + c**2*log(a/b + x)/b + 2
*c*d*x/b + d**2*x**2/(2*b), Eq(m, -1)), (2*a**3*d**2*(a + b*x)**m/(b**3*m**
3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) - 2*a**2*b*c*d*m*(a + b*x)**m/(b**3*m
**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) - 6*a**2*b*c*d*(a + b*x)**m/(b**3*m
**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) - 2*a**2*b*d**2*m*x*(a + b*x)**m/(b
**3*m**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) + a*b**2*c**2*m**2*(a + b*x)**
m/(b**3*m**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) + 5*a*b**2*c**2*m*(a + b*x
)**m/(b**3*m**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) + 6*a*b**2*c**2*(a + b*
x)**m/(b**3*m**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) + 2*a*b**2*c*d*m**2*x*
(a + b*x)**m/(b**3*m**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) + 6*a*b**2*c*d*
m*x*(a + b*x)**m/(b**3*m**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) + a*b**2*d
**2*m**2*x**2*(a + b*x)**m/(b**3*m**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) +
a*b**2*d**2*m*x**2*(a + b*x)**m/(b**3*m**3 + 6*b**3*m**2 + 11*b**3*m + 6*b
**3) + b**3*c**2*m**2*x*(a + b*x)**m/(b**3*m**3 + 6*b**3*m**2 + 11*b**3*m +
6*b**3) + 5*b**3*c**2*m*x*(a + b*x)**m/(b**3*m**3 + 6*b**3*m**2 + 11*b**3*m
+ 6*b**3) + 6*b**3*c**2*x*(a + b*x)**m/(b**3*m**3 + 6*b**3*m**2 + 11*b**3*
m + 6*b**3) + 2*b**3*c*d*m**2*x**2*(a + b*x)**m/(b**3*m**3 + 6*b**3*m**2 +
11*b**3*m + 6*b**3) + 8*b**3*c*d*m*x**2*(a + b*x)**m/(b**3*m**3 + 6*b**3*m
**2 + 11*b**3*m + 6*b**3) + 6*b**3*c*d*x**2*(a + b*x)**m/(b**3*m**3 + 6*b**3
*m**2 + 11*b**3*m + 6*b**3) + b**3*d**2*m**2*x**3*(a + b*x)**m/(b**3*m**3 +
6*b**3*m**2 + 11*b**3*m + 6*b**3) + 3*b**3*d**2*m*x**3*(a + b*x)**m/(b**3*
m**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3) + 2*b**3*d**2*x**3*(a + b*x)**m/(b
**3*m**3 + 6*b**3*m**2 + 11*b**3*m + 6*b**3), True))

```

3.1848 $\int (a + bx)^m (c + dx) dx$

Optimal. Leaf size=46

$$\frac{(bc - ad)(a + bx)^{m+1}}{b^2(m + 1)} + \frac{d(a + bx)^{m+2}}{b^2(m + 2)}$$

[Out] $(-a*d+b*c)*(b*x+a)^{(1+m)}/b^2/(1+m)+d*(b*x+a)^{(2+m)}/b^2/(2+m)$

Rubi [A] time = 0.02, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{(bc - ad)(a + bx)^{m+1}}{b^2(m + 1)} + \frac{d(a + bx)^{m+2}}{b^2(m + 2)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^m*(c + d*x), x]$

[Out] $((b*c - a*d)*(a + b*x)^{(1 + m)})/(b^2*(1 + m)) + (d*(a + b*x)^{(2 + m)})/(b^2*(2 + m))$

Rule 43

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] :> \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0])) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0]$

Rubi steps

$$\begin{aligned} \int (a + bx)^m (c + dx) dx &= \int \left(\frac{(bc - ad)(a + bx)^m}{b} + \frac{d(a + bx)^{1+m}}{b} \right) dx \\ &= \frac{(bc - ad)(a + bx)^{1+m}}{b^2(1 + m)} + \frac{d(a + bx)^{2+m}}{b^2(2 + m)} \end{aligned}$$

Mathematica [A] time = 0.03, size = 41, normalized size = 0.89

$$\frac{(a + bx)^{m+1}(-ad + bc(m + 2) + bd(m + 1)x)}{b^2(m + 1)(m + 2)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^m*(c + d*x), x]

[Out] ((a + b*x)^(1 + m)*(-a*d) + b*c*(2 + m) + b*d*(1 + m)*x)/(b^2*(1 + m)*(2 + m))

fricas [A] time = 1.00, size = 83, normalized size = 1.80

$$\frac{(abc m + 2 abc - a^2 d + (b^2 d m + b^2 d)x^2 + (2 b^2 c + (b^2 c + a b d)m)x)(b x + a)^m}{b^2 m^2 + 3 b^2 m + 2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(d*x+c), x, algorithm="fricas")

[Out] (a*b*c*m + 2*a*b*c - a^2*d + (b^2*d*m + b^2*d)*x^2 + (2*b^2*c + (b^2*c + a*b*d)*m)*x)*(b*x + a)^m/(b^2*m^2 + 3*b^2*m + 2*b^2)

giac [B] time = 0.86, size = 132, normalized size = 2.87

$$\frac{(b x + a)^m b^2 d m x^2 + (b x + a)^m b^2 c m x + (b x + a)^m a b d m x + (b x + a)^m b^2 d x^2 + (b x + a)^m a b c m + 2 (b x + a)^m b^2 c x + (b x + a)^m a^2 d}{b^2 m^2 + 3 b^2 m + 2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(d*x+c), x, algorithm="giac")

[Out] ((b*x + a)^m*b^2*d*m*x^2 + (b*x + a)^m*b^2*c*m*x + (b*x + a)^m*a*b*d*m*x + (b*x + a)^m*b^2*d*x^2 + (b*x + a)^m*a*b*c*m + 2*(b*x + a)^m*b^2*c*x + 2*(b*x + a)^m*a*b*c - (b*x + a)^m*a^2*d)/(b^2*m^2 + 3*b^2*m + 2*b^2)

maple [A] time = 0.00, size = 49, normalized size = 1.07

$$\frac{(-b d m x - b c m - b d x + a d - 2 b c)(b x + a)^{m+1}}{(m^2 + 3 m + 2) b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^m*(d*x+c), x)

[Out] -(b*x+a)^(m+1)*(-b*d*m*x-b*c*m-b*d*x+a*d-2*b*c)/b^2/(m^2+3*m+2)

maxima [A] time = 1.06, size = 63, normalized size = 1.37

$$\frac{(b^2(m+1)x^2 + a b m x - a^2)(b x + a)^m d}{(m^2 + 3 m + 2) b^2} + \frac{(b x + a)^{m+1} c}{b(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(d*x+c),x, algorithm="maxima")

[Out] (b^2*(m + 1)*x^2 + a*b*m*x - a^2)*(b*x + a)^m*d/((m^2 + 3*m + 2)*b^2) + (b*x + a)^(m + 1)*c/(b*(m + 1))

mupad [B] time = 0.48, size = 88, normalized size = 1.91

$$(a + bx)^m \left(\frac{a(2bc - ad + bcm)}{b^2(m^2 + 3m + 2)} + \frac{x(2b^2c + b^2cm + abdm)}{b^2(m^2 + 3m + 2)} + \frac{dx^2(m + 1)}{m^2 + 3m + 2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^m*(c + d*x),x)

[Out] (a + b*x)^m*((a*(2*b*c - a*d + b*c*m))/(b^2*(3*m + m^2 + 2)) + (x*(2*b^2*c + b^2*c*m + a*b*d*m))/(b^2*(3*m + m^2 + 2)) + (d*x^2*(m + 1))/(3*m + m^2 + 2))

sympy [A] time = 0.86, size = 377, normalized size = 8.20

$$\left\{ \begin{array}{l} a^m \left(cx + \frac{dx^2}{2} \right) \\ \frac{ad \log\left(\frac{a}{b} + x\right)}{ab^2 + b^3x} + \frac{ad}{ab^2 + b^3x} - \frac{bc}{ab^2 + b^3x} + \frac{bdx \log\left(\frac{a}{b} + x\right)}{ab^2 + b^3x} \\ -\frac{ad \log\left(\frac{a}{b} + x\right)}{b^2} + \frac{c \log\left(\frac{a}{b} + x\right)}{b} + \frac{dx}{b} \\ -\frac{a^2d(a+bx)^m}{b^2m^2+3b^2m+2b^2} + \frac{abc m(a+bx)^m}{b^2m^2+3b^2m+2b^2} + \frac{2abc(a+bx)^m}{b^2m^2+3b^2m+2b^2} + \frac{abdmx(a+bx)^m}{b^2m^2+3b^2m+2b^2} + \frac{b^2cmx(a+bx)^m}{b^2m^2+3b^2m+2b^2} + \frac{2b^2cx(a+bx)^m}{b^2m^2+3b^2m+2b^2} + \frac{b^2dmx^2(a+bx)^m}{b^2m^2+3b^2m+2b^2} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**m*(d*x+c),x)

[Out] Piecewise((a**m*(c*x + d*x**2/2), Eq(b, 0)), (a*d*log(a/b + x)/(a*b**2 + b**3*x) + a*d/(a*b**2 + b**3*x) - b*c/(a*b**2 + b**3*x) + b*d*x*log(a/b + x)/(a*b**2 + b**3*x), Eq(m, -2)), (-a*d*log(a/b + x)/b**2 + c*log(a/b + x)/b + d*x/b, Eq(m, -1)), (-a**2*d*(a + b*x)**m/(b**2*m**2 + 3*b**2*m + 2*b**2) + a*b*c*m*(a + b*x)**m/(b**2*m**2 + 3*b**2*m + 2*b**2) + 2*a*b*c*(a + b*x)**m/(b**2*m**2 + 3*b**2*m + 2*b**2) + a*b*d*m*x*(a + b*x)**m/(b**2*m**2 + 3*b**2*m + 2*b**2) + b**2*c*m*x*(a + b*x)**m/(b**2*m**2 + 3*b**2*m + 2*b**2) + 2*b**2*c*x*(a + b*x)**m/(b**2*m**2 + 3*b**2*m + 2*b**2) + b**2*d*m*x**2*(a + b*x)**m/(b**2*m**2 + 3*b**2*m + 2*b**2) + b**2*d*x**2*(a + b*x)**m/(b**2*m**2 + 3*b**2*m + 2*b**2), True))

$$3.1849 \quad \int \frac{(a+bx)^m}{c+dx} dx$$

Optimal. Leaf size=51

$$\frac{(a+bx)^{m+1} {}_2F_1\left(1, m+1; m+2; -\frac{d(a+bx)}{bc-ad}\right)}{(m+1)(bc-ad)}$$

[Out] (b*x+a)^(1+m)*hypergeom([1, 1+m], [2+m], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)/(1+m)

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {68}

$$\frac{(a+bx)^{m+1} {}_2F_1\left(1, m+1; m+2; -\frac{d(a+bx)}{bc-ad}\right)}{(m+1)(bc-ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^m/(c + d*x), x]

[Out] ((a + b*x)^(1 + m)*Hypergeometric2F1[1, 1 + m, 2 + m, -((d*(a + b*x))/(b*c - a*d))])/((b*c - a*d)*(1 + m))

Rule 68

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[(((b*c - a*d)^n*(a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/((b^(n + 1)*(m + 1)), x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && IntegerQ[n]

Rubi steps

$$\int \frac{(a+bx)^m}{c+dx} dx = \frac{(a+bx)^{1+m} {}_2F_1\left(1, 1+m; 2+m; -\frac{d(a+bx)}{bc-ad}\right)}{(bc-ad)(1+m)}$$

Mathematica [A] time = 0.01, size = 51, normalized size = 1.00

$$-\frac{(a+bx)^{m+1} {}_2F_1\left(1, m+1; m+2; \frac{d(a+bx)}{ad-bc}\right)}{(m+1)(ad-bc)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^m/(c + d*x),x]

[Out] -(((a + b*x)^(1 + m)*Hypergeometric2F1[1, 1 + m, 2 + m, (d*(a + b*x))/(-(b*c) + a*d)])/((-b*c) + a*d)*(1 + m))

fricas [F] time = 0.80, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^m}{dx + c}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c),x, algorithm="fricas")

[Out] integral((b*x + a)^m/(d*x + c), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{dx + c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c),x, algorithm="giac")

[Out] integrate((b*x + a)^m/(d*x + c), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{dx + c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^m/(d*x+c),x)

[Out] int((b*x+a)^m/(d*x+c),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{dx + c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c),x, algorithm="maxima")

[Out] integrate((b*x + a)^m/(d*x + c), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^m}{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^m/(c + d*x), x)

[Out] int((a + b*x)^m/(c + d*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^m}{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**m/(d*x+c), x)

[Out] Integral((a + b*x)**m/(c + d*x), x)

$$3.1850 \quad \int \frac{(a+bx)^m}{(c+dx)^2} dx$$

Optimal. Leaf size=52

$$\frac{b(a+bx)^{m+1} {}_2F_1\left(2, m+1; m+2; -\frac{d(a+bx)}{bc-ad}\right)}{(m+1)(bc-ad)^2}$$

[Out] b*(b*x+a)^(1+m)*hypergeom([2, 1+m], [2+m], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^2/(1+m)

Rubi [A] time = 0.01, antiderivative size = 52, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {68}

$$\frac{b(a+bx)^{m+1} {}_2F_1\left(2, m+1; m+2; -\frac{d(a+bx)}{bc-ad}\right)}{(m+1)(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^m/(c + d*x)^2, x]

[Out] (b*(a + b*x)^(1 + m)*Hypergeometric2F1[2, 1 + m, 2 + m, -((d*(a + b*x))/(b*c - a*d))])/((b*c - a*d)^2*(1 + m))

Rule 68

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((b*c - a*d)^n*(a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/((b^(n + 1)*(m + 1)), x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && IntegerQ[n]

Rubi steps

$$\int \frac{(a+bx)^m}{(c+dx)^2} dx = \frac{b(a+bx)^{1+m} {}_2F_1\left(2, 1+m; 2+m; -\frac{d(a+bx)}{bc-ad}\right)}{(bc-ad)^2(1+m)}$$

Mathematica [A] time = 0.02, size = 52, normalized size = 1.00

$$\frac{b(a+bx)^{m+1} {}_2F_1\left(2, m+1; m+2; -\frac{d(a+bx)}{bc-ad}\right)}{(m+1)(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^m/(c + d*x)^2,x]

[Out] (b*(a + b*x)^(1 + m)*Hypergeometric2F1[2, 1 + m, 2 + m, -((d*(a + b*x))/(b*c - a*d))]/((b*c - a*d)^2*(1 + m))

fricas [F] time = 0.84, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^m}{d^2x^2 + 2cdx + c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c)^2,x, algorithm="fricas")

[Out] integral((b*x + a)^m/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{(dx + c)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c)^2,x, algorithm="giac")

[Out] integrate((b*x + a)^m/(d*x + c)^2, x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{(dx + c)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^m/(d*x+c)^2,x)

[Out] int((b*x+a)^m/(d*x+c)^2,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{(dx + c)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c)^2,x, algorithm="maxima")

[Out] integrate((b*x + a)^m/(d*x + c)^2, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^m}{(c + dx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^m/(c + d*x)^2, x)

[Out] int((a + b*x)^m/(c + d*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^m}{(c + dx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**m/(d*x+c)**2, x)

[Out] Integral((a + b*x)**m/(c + d*x)**2, x)

$$3.1851 \quad \int \frac{(a+bx)^m}{(c+dx)^3} dx$$

Optimal. Leaf size=54

$$\frac{b^2(a+bx)^{m+1} {}_2F_1\left(3, m+1; m+2; -\frac{d(a+bx)}{bc-ad}\right)}{(m+1)(bc-ad)^3}$$

[Out] $b^2*(b*x+a)^{(1+m)}*\text{hypergeom}([3, 1+m], [2+m], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)^3/(1+m)$

Rubi [A] time = 0.01, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {68}

$$\frac{b^2(a+bx)^{m+1} {}_2F_1\left(3, m+1; m+2; -\frac{d(a+bx)}{bc-ad}\right)}{(m+1)(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^m/(c + d*x)^3, x]

[Out] $(b^2*(a + b*x)^{(1 + m)}*\text{Hypergeometric2F1}[3, 1 + m, 2 + m, -((d*(a + b*x))/(b*c - a*d))])/((b*c - a*d)^3*(1 + m))$

Rule 68

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((b*c - a*d)^n*(a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/((b^(n + 1)*(m + 1)), x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && IntegerQ[n]

Rubi steps

$$\int \frac{(a+bx)^m}{(c+dx)^3} dx = \frac{b^2(a+bx)^{1+m} {}_2F_1\left(3, 1+m; 2+m; -\frac{d(a+bx)}{bc-ad}\right)}{(bc-ad)^3(1+m)}$$

Mathematica [A] time = 0.02, size = 54, normalized size = 1.00

$$\frac{b^2(a+bx)^{m+1} {}_2F_1\left(3, m+1; m+2; -\frac{d(a+bx)}{bc-ad}\right)}{(m+1)(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^m/(c + d*x)^3,x]

[Out] (b^2*(a + b*x)^(1 + m)*Hypergeometric2F1[3, 1 + m, 2 + m, -((d*(a + b*x))/(b*c - a*d))])/((b*c - a*d)^3*(1 + m))

fricas [F] time = 0.96, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^m}{d^3x^3 + 3cd^2x^2 + 3c^2dx + c^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c)^3,x, algorithm="fricas")

[Out] integral((b*x + a)^m/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{(dx + c)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c)^3,x, algorithm="giac")

[Out] integrate((b*x + a)^m/(d*x + c)^3, x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{(dx + c)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^m/(d*x+c)^3,x)

[Out] int((b*x+a)^m/(d*x+c)^3,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{(dx + c)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c)^3,x, algorithm="maxima")

[Out] integrate((b*x + a)^m/(d*x + c)^3, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^m}{(c + dx)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^m/(c + d*x)^3,x)

[Out] int((a + b*x)^m/(c + d*x)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^m}{(c + dx)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**m/(d*x+c)**3,x)

[Out] Integral((a + b*x)**m/(c + d*x)**3, x)

3.1852 $\int (a + bx)^3 (c + dx)^n dx$

Optimal. Leaf size=111

$$-\frac{3b^2(bc - ad)(c + dx)^{n+3}}{d^4(n + 3)} - \frac{(bc - ad)^3(c + dx)^{n+1}}{d^4(n + 1)} + \frac{3b(bc - ad)^2(c + dx)^{n+2}}{d^4(n + 2)} + \frac{b^3(c + dx)^{n+4}}{d^4(n + 4)}$$

[Out] $-(-a*d+b*c)^3*(d*x+c)^(1+n)/d^4/(1+n)+3*b*(-a*d+b*c)^2*(d*x+c)^(2+n)/d^4/(2+n)-3*b^2*(-a*d+b*c)*(d*x+c)^(3+n)/d^4/(3+n)+b^3*(d*x+c)^(4+n)/d^4/(4+n)$

Rubi [A] time = 0.06, antiderivative size = 111, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$-\frac{3b^2(bc - ad)(c + dx)^{n+3}}{d^4(n + 3)} - \frac{(bc - ad)^3(c + dx)^{n+1}}{d^4(n + 1)} + \frac{3b(bc - ad)^2(c + dx)^{n+2}}{d^4(n + 2)} + \frac{b^3(c + dx)^{n+4}}{d^4(n + 4)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^3*(c + d*x)^n, x]

[Out] $-(((b*c - a*d)^3*(c + d*x)^(1 + n))/(d^4*(1 + n))) + (3*b*(b*c - a*d)^2*(c + d*x)^(2 + n))/(d^4*(2 + n)) - (3*b^2*(b*c - a*d)*(c + d*x)^(3 + n))/(d^4*(3 + n)) + (b^3*(c + d*x)^(4 + n))/(d^4*(4 + n))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^3 (c + dx)^n dx &= \int \left(\frac{(-bc + ad)^3 (c + dx)^n}{d^3} + \frac{3b(bc - ad)^2 (c + dx)^{1+n}}{d^3} - \frac{3b^2(bc - ad)(c + dx)^{2+n}}{d^3} + \frac{b^3(c + dx)^{3+n}}{d^3} \right) dx \\ &= -\frac{(bc - ad)^3 (c + dx)^{1+n}}{d^4(1 + n)} + \frac{3b(bc - ad)^2 (c + dx)^{2+n}}{d^4(2 + n)} - \frac{3b^2(bc - ad)(c + dx)^{3+n}}{d^4(3 + n)} + \frac{b^3(c + dx)^{4+n}}{d^4(4 + n)} \end{aligned}$$

Mathematica [A] time = 0.11, size = 95, normalized size = 0.86

$$\frac{(c + dx)^{n+1} \left(-\frac{3b^2(c+dx)^2(bc-ad)}{n+3} + \frac{3b(c+dx)(bc-ad)^2}{n+2} - \frac{(bc-ad)^3}{n+1} + \frac{b^3(c+dx)^3}{n+4} \right)}{d^4}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^3*(c + d*x)^n,x]

[Out] ((c + d*x)^(1 + n)*(-(b*c - a*d)^3/(1 + n)) + (3*b*(b*c - a*d)^2*(c + d*x))/(2 + n) - (3*b^2*(b*c - a*d)*(c + d*x)^2)/(3 + n) + (b^3*(c + d*x)^3)/(4 + n))/d^4

fricas [B] time = 0.93, size = 496, normalized size = 4.47

$$\frac{(a^3cd^3n^3 - 6b^3c^4 + 24ab^2c^3d - 36a^2bc^2d^2 + 24a^3cd^3 + (b^3d^4n^3 + 6b^3d^4n^2 + 11b^3d^4n + 6b^3d^4)x^4 + (24ab^2d^4n^3 - 6b^3c^4 + 24ab^2c^3d - 36a^2bc^2d^2 + 24a^3cd^3)x^4 + (24ab^2d^4n^3 - 6b^3c^4 + 24ab^2c^3d - 36a^2bc^2d^2 + 24a^3cd^3)x^4 + (24ab^2d^4n^3 - 6b^3c^4 + 24ab^2c^3d - 36a^2bc^2d^2 + 24a^3cd^3)x^4}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^n,x, algorithm="fricas")

[Out] (a^3*c*d^3*n^3 - 6*b^3*c^4 + 24*a*b^2*c^3*d - 36*a^2*b*c^2*d^2 + 24*a^3*c*d^3 + (b^3*d^4*n^3 + 6*b^3*d^4*n^2 + 11*b^3*d^4*n + 6*b^3*d^4)*x^4 + (24*a*b^2*d^4 + (b^3*c*d^3 + 3*a*b^2*d^4)*n^3 + 3*(b^3*c*d^3 + 7*a*b^2*d^4)*n^2 + 2*(b^3*c*d^3 + 21*a*b^2*d^4)*n)*x^3 - 3*(a^2*b*c^2*d^2 - 3*a^3*c*d^3)*n^2 + 3*(12*a^2*b*d^4 + (a*b^2*c*d^3 + a^2*b*d^4)*n^3 - (b^3*c^2*d^2 - 5*a*b^2*c*d^3 - 8*a^2*b*d^4)*n^2 - (b^3*c^2*d^2 - 4*a*b^2*c*d^3 - 19*a^2*b*d^4)*n)*x^2 + (6*a*b^2*c^3*d - 21*a^2*b*c^2*d^2 + 26*a^3*c*d^3)*n + (24*a^3*d^4 + (3*a^2*b*c*d^3 + a^3*d^4)*n^3 - 3*(2*a*b^2*c^2*d^2 - 7*a^2*b*c*d^3 - 3*a^3*d^4)*n^2 + 2*(3*b^3*c^3*d - 12*a*b^2*c^2*d^2 + 18*a^2*b*c*d^3 + 13*a^3*d^4)*n)*x)*(d*x + c)^n/(d^4*n^4 + 10*d^4*n^3 + 35*d^4*n^2 + 50*d^4*n + 24*d^4)

giac [B] time = 0.98, size = 833, normalized size = 7.50

$$\frac{(dx + c)^n b^3 d^4 n^3 x^4 + (dx + c)^n b^3 c d^3 n^3 x^3 + 3(dx + c)^n a b^2 d^4 n^3 x^3 + 6(dx + c)^n b^3 d^4 n^2 x^4 + 3(dx + c)^n a b^2 c d^3 n^3 x^2}{d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^3*(d*x+c)^n,x, algorithm="giac")

[Out] ((d*x + c)^n*b^3*d^4*n^3*x^4 + (d*x + c)^n*b^3*c*d^3*n^3*x^3 + 3*(d*x + c)^n*a*b^2*d^4*n^3*x^3 + 6*(d*x + c)^n*b^3*d^4*n^2*x^4 + 3*(d*x + c)^n*a*b^2*c*d^3*n^3*x^2 + 3*(d*x + c)^n*a^2*b*d^4*n^3*x^2 + 3*(d*x + c)^n*b^3*c*d^3*n^2*x^3 + 21*(d*x + c)^n*a*b^2*d^4*n^2*x^3 + 11*(d*x + c)^n*b^3*d^4*n*x^4 + 3*(d*x + c)^n*a^2*b*c*d^3*n^3*x + (d*x + c)^n*a^3*d^4*n^3*x - 3*(d*x + c)^n*b^3*c^2*d^2*n^2*x^2 + 15*(d*x + c)^n*a*b^2*c*d^3*n^2*x^2 + 24*(d*x + c)^n*a^2*b*d^4*n^2*x^2 + 2*(d*x + c)^n*b^3*c*d^3*n*x^3 + 42*(d*x + c)^n*a*b^2*d^4*n*x^3 + 6*(d*x + c)^n*b^3*d^4*x^4 + (d*x + c)^n*a^3*c*d^3*n^3 - 6*(d*x + c)^n*a*b^2*c^2*d^2*n^2*x + 21*(d*x + c)^n*a^2*b*c*d^3*n^2*x + 9*(d*x + c)^n*a^3*d^4*n^2*x - 3*(d*x + c)^n*b^3*c^2*d^2*n*x^2 + 12*(d*x + c)^n*a*b^2*c*d^3*n^3)

$$\frac{3n^2x^2 + 57(dx+c)^n a^2 b d^4 n x^2 + 24(dx+c)^n a b^2 d^4 x^3 - 3(dx+c)^n a^2 b c^2 d^2 n^2 + 9(dx+c)^n a^3 c d^3 n^2 + 6(dx+c)^n b^3 c^3 d n x - 24(dx+c)^n a b^2 c^2 d^2 n x + 36(dx+c)^n a^2 b c d^3 n x + 26(dx+c)^n a^3 d^4 n x + 36(dx+c)^n a^2 b d^4 x^2 + 6(dx+c)^n a b^2 c^3 d n - 21(dx+c)^n a^2 b c^2 d^2 n + 26(dx+c)^n a^3 c d^3 n + 24(dx+c)^n a^3 d^4 x - 6(dx+c)^n b^3 c^4 + 24(dx+c)^n a b^2 c^3 d - 36(dx+c)^n a^2 b c^2 d^2 + 24(dx+c)^n a^3 c d^3}{(d^4 n^4 + 10d^4 n^3 + 35d^4 n^2 + 50d^4 n + 24d^4)}$$

maple [B] time = 0.01, size = 386, normalized size = 3.48

$$\frac{(b^3 d^3 n^3 x^3 + 3a b^2 d^3 n^3 x^2 + 6b^3 d^3 n^2 x^3 + 3a^2 b d^3 n^3 x + 21a b^2 d^3 n^2 x^2 - 3b^3 c d^2 n^2 x^2 + 11b^3 d^3 n x^3 + a^3 d^3 n^3 + 24a^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^3*(d*x+c)^n,x)`

[Out] $(dx+c)^{(n+1)} * (b^3 d^3 n^3 x^3 + 3a b^2 d^3 n^3 x^2 + 6b^3 d^3 n^2 x^3 + 3a^2 b d^3 n^3 x + 21a b^2 d^3 n^2 x^2 - 3b^3 c d^2 n^2 x^2 + 11b^3 d^3 n x^3 + a^3 d^3 n^3 + 24a^2 b d^3 n^2 x - 6a b^2 c d^2 n^2 x + 42a b^2 d^3 n x^2 - 9b^3 c d^2 n x^2 + 6b^3 d^3 x^3 + 9a^3 d^3 n^2 - 3a^2 b c d^2 n^2 + 57a^2 b d^3 n x - 30a b^2 c d^2 n x + 24a b^2 d^3 x^2 + 6b^3 c^2 d n x - 6b^3 c d^2 x^2 + 26a^3 d^3 n - 21a^2 b c d^2 n + 36a^2 b d^3 x + 6a b^2 c^2 d n - 24a b^2 c d^2 x + 6b^3 c^2 d x + 24a^3 d^3 - 36a^2 b c d^2 + 24a b^2 c^2 d - 6b^3 c^3) / d^4 / (n^4 + 10n^3 + 5n^2 + 50n + 24)$

maxima [B] time = 1.30, size = 246, normalized size = 2.22

$$\frac{3(d^2(n+1)x^2 + cdnx - c^2)(dx+c)^n a^2 b}{(n^2 + 3n + 2)d^2} + \frac{(dx+c)^{n+1} a^3}{d(n+1)} + \frac{3((n^2 + 3n + 2)d^3 x^3 + (n^2 + n)cd^2 x^2 - 2c^2 dnx + 2c^3)}{(n^3 + 6n^2 + 11n + 6)d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^3*(d*x+c)^n,x, algorithm="maxima")`

[Out] $3(d^2(n+1)x^2 + c d n x - c^2)(dx+c)^n a^2 b / ((n^2 + 3n + 2)d^2) + (dx+c)^{(n+1)} a^3 / (d(n+1)) + 3((n^2 + 3n + 2)d^3 x^3 + (n^2 + n)cd^2 x^2 - 2c^2 d n x + 2c^3)(dx+c)^n a b^2 / ((n^3 + 6n^2 + 11n + 6)d^3) + ((n^3 + 6n^2 + 11n + 6)d^4 x^4 + (n^3 + 3n^2 + 2n)cd^3 x^3 - 3(n^2 + n)c^2 d^2 x^2 + 6c^3 d n x - 6c^4)(dx+c)^n b^3 / ((n^4 + 10n^3 + 35n^2 + 50n + 24)d^4)$

mupad [B] time = 0.91, size = 478, normalized size = 4.31

$$\frac{x(c+dx)^n (a^3 d^4 n^3 + 9a^3 d^4 n^2 + 26a^3 d^4 n + 24a^3 d^4 + 3a^2 b c d^3 n^3 + 21a^2 b c d^3 n^2 + 36a^2 b c d^3 n - 6a b^2 c^2 d^4 (n^4 + 10n^3 + 35n^2 + 50n + 24))}{d^4 (n^4 + 10n^3 + 35n^2 + 50n + 24)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^3*(c + d*x)^n,x)`

[Out] $(x*(c + d*x)^n*(24*a^3*d^4 + 26*a^3*d^4*n + 9*a^3*d^4*n^2 + a^3*d^4*n^3 + 6*b^3*c^3*d*n + 36*a^2*b*c*d^3*n - 24*a*b^2*c^2*d^2*n + 21*a^2*b*c*d^3*n^2 + 3*a^2*b*c*d^3*n^3 - 6*a*b^2*c^2*d^2*n^2))/(d^4*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (b^3*x^4*(c + d*x)^n*(11*n + 6*n^2 + n^3 + 6))/(50*n + 35*n^2 + 10*n^3 + n^4 + 24) + (c*(c + d*x)^n*(24*a^3*d^3 - 6*b^3*c^3 + 26*a^3*d^3*n + 9*a^3*d^3*n^2 + a^3*d^3*n^3 + 24*a*b^2*c^2*d - 36*a^2*b*c*d^2 + 6*a*b^2*c^2*d*n - 21*a^2*b*c*d^2*n - 3*a^2*b*c*d^2*n^2))/(d^4*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (3*b*x^2*(n + 1)*(c + d*x)^n*(12*a^2*d^2 + 7*a^2*d^2*n - b^2*c^2*n + a^2*d^2*n^2 + 4*a*b*c*d*n + a*b*c*d*n^2))/(d^2*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (b^2*x^3*(c + d*x)^n*(12*a*d + 3*a*d*n + b*c*n)*(3*n + n^2 + 2))/(d*(50*n + 35*n^2 + 10*n^3 + n^4 + 24))$

sympy [A] time = 4.44, size = 4058, normalized size = 36.56

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**3*(d*x+c)**n,x)`

[Out] $\text{Piecewise}((c**n*(a**3*x + 3*a**2*b*x**2/2 + a*b**2*x**3 + b**3*x**4/4), \text{Eq}(d, 0)), (-2*a**3*d**3/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) - 3*a**2*b*c*d**2/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) - 9*a**2*b*d**3*x/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) - 6*a*b**2*c**2*d/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) - 18*a*b**2*c*d**2*x/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) - 18*a*b**2*d**3*x**2/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) + 6*b**3*c**3*log(c/d + x)/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) + 11*b**3*c**3/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) + 18*b**3*c**2*d*x*log(c/d + x)/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) + 27*b**3*c**2*d*x/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) + 18*b**3*c*d**2*x**2*log(c/d + x)/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) + 18*b**3*c*d**2*x**2/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) + 6*b**3*d**3*x**3*log(c/d + x)/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3) + 6*b**3*d**3*x**3/(6*c**3*d**4 + 18*c**2*d**5*x + 18*c*d**6*x**2 + 6*d**7*x**3), \text{Eq}(n, -4)), (-a**3*d**3/(2*c**2*d**4 + 4*c*d**5*x + 2*d**6*x**2) - 3*a**2*b*c*d**2/(2*c**2*d**4 + 4*c*d**5*x + 2*d**6*x**2) - 6*a**2*b*d**3*x/(2*c**2*d**4 + 4*c*d**5*x + 2*d**6*x**2) + 6*a*b**2*c**2*d*log(c/d + x)/(2*c**2*d**4 + 4*c*d**5*x + 2*d**6*x**2) + 9*a*b**2*c**2*d/(2*c**2*d**4 + 4*c*d**5*x + 2*d**6*x**2) + 12*a*b**2*c*d**2*x*log(c/d + x)/(2*c**2*d**4 + 4*c*d**5*x + 2*d**6*x**2) + 12*a*b**2*c*d**2*x/(2*c**2*d**4 + 4*c*d**5*x + 2*d**6*x**2) + 6*a*b**2*d**3*$

$$\begin{aligned}
& x^{**2} \log(c/d + x) / (2*c^{**2}*d^{**4} + 4*c*d^{**5}*x + 2*d^{**6}*x^{**2}) - 6*b^{**3}*c^{**3} \log(c/d + x) / (2*c^{**2}*d^{**4} + 4*c*d^{**5}*x + 2*d^{**6}*x^{**2}) - 9*b^{**3}*c^{**3} / (2*c^{**2}*d^{**4} + 4*c*d^{**5}*x + 2*d^{**6}*x^{**2}) - 12*b^{**3}*c^{**2}*d*x \log(c/d + x) / (2*c^{**2}*d^{**4} + 4*c*d^{**5}*x + 2*d^{**6}*x^{**2}) - 12*b^{**3}*c^{**2}*d*x / (2*c^{**2}*d^{**4} + 4*c*d^{**5}*x + 2*d^{**6}*x^{**2}) - 6*b^{**3}*c*d^{**2}*x^{**2} \log(c/d + x) / (2*c^{**2}*d^{**4} + 4*c*d^{**5}*x + 2*d^{**6}*x^{**2}) + 2*b^{**3}*d^{**3}*x^{**3} / (2*c^{**2}*d^{**4} + 4*c*d^{**5}*x + 2*d^{**6}*x^{**2}), \\
& \text{Eq}(n, -3)), (-2*a^{**3}*d^{**3} / (2*c*d^{**4} + 2*d^{**5}*x) + 6*a^{**2}*b*c*d^{**2} \log(c/d + x) / (2*c*d^{**4} + 2*d^{**5}*x) + 6*a^{**2}*b*c*d^{**2} / (2*c*d^{**4} + 2*d^{**5}*x) + 6*a^{**2} \\
& *b*d^{**3}*x \log(c/d + x) / (2*c*d^{**4} + 2*d^{**5}*x) - 12*a*b^{**2}*c^{**2}*d \log(c/d + x) / (2*c*d^{**4} + 2*d^{**5}*x) - 12*a*b^{**2}*c^{**2}*d / (2*c*d^{**4} + 2*d^{**5}*x) - 12*a*b^{**2} \\
& *c*d^{**2}*x \log(c/d + x) / (2*c*d^{**4} + 2*d^{**5}*x) + 6*a*b^{**2}*d^{**3}*x^{**2} / (2*c*d^{**4} + 2*d^{**5}*x) + 6*b^{**3}*c^{**3} \log(c/d + x) / (2*c*d^{**4} + 2*d^{**5}*x) + 6*b^{**3}*c^{**3} \\
& / (2*c*d^{**4} + 2*d^{**5}*x) + 6*b^{**3}*c^{**2}*d*x \log(c/d + x) / (2*c*d^{**4} + 2*d^{**5}*x) - 3*b^{**3}*c*d^{**2}*x^{**2} / (2*c*d^{**4} + 2*d^{**5}*x) + b^{**3}*d^{**3}*x^{**3} / (2*c*d^{**4} + 2 \\
& *d^{**5}*x), \text{Eq}(n, -2)), (a^{**3} \log(c/d + x) / d - 3*a^{**2}*b*c \log(c/d + x) / d^{**2} + 3*a^{**2}*b*x / d + 3*a*b^{**2}*c^{**2} \log(c/d + x) / d^{**3} - 3*a*b^{**2}*c*x / d^{**2} + 3*a*b \\
& **2*x^{**2} / (2*d) - b^{**3}*c^{**3} \log(c/d + x) / d^{**4} + b^{**3}*c^{**2}*x / d^{**3} - b^{**3}*c*x \\
& **2 / (2*d^{**2}) + b^{**3}*x^{**3} / (3*d), \text{Eq}(n, -1)), (a^{**3}*c*d^{**3}*n^{**3}*(c + d*x)**n / (\\
& d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) + 9*a^{**3}*c*d \\
& **3*n^{**2}*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n \\
& + 24*d^{**4}) + 26*a^{**3}*c*d^{**3}*n*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d \\
& **4*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) + 24*a^{**3}*c*d^{**3}*(c + d*x)**n / (d^{**4}*n^{**4} + \\
& 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) + a^{**3}*d^{**4}*n^{**3}*x*(c + \\
& d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) + 9 \\
& *a^{**3}*d^{**4}*n^{**2}*x*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 5 \\
& 0*d^{**4}*n + 24*d^{**4}) + 26*a^{**3}*d^{**4}*n*x*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n \\
& **3 + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) + 24*a^{**3}*d^{**4}*x*(c + d*x)**n / (d^{**4} \\
& *n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) - 3*a^{**2}*b*c^{**2} \\
& *d^{**2}*n^{**2}*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n \\
& + 24*d^{**4}) - 21*a^{**2}*b*c^{**2}*d^{**2}*n*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} \\
& + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) - 36*a^{**2}*b*c^{**2}*d^{**2}*(c + d*x)**n / (\\
& d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) + 3*a^{**2}*b*c \\
& *d^{**3}*n^{**3}*x*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4} \\
& *n + 24*d^{**4}) + 21*a^{**2}*b*c*d^{**3}*n^{**2}*x*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n \\
& **3 + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) + 36*a^{**2}*b*c*d^{**3}*n*x*(c + d*x) \\
& **n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) + 3*a^{**2} \\
& *b*d^{**4}*n^{**3}*x^{**2}*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + \\
& 50*d^{**4}*n + 24*d^{**4}) + 24*a^{**2}*b*d^{**4}*n^{**2}*x^{**2}*(c + d*x)**n / (d^{**4}*n^{**4} + 1 \\
& 0*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) + 57*a^{**2}*b*d^{**4}*n*x^{**2}*(\\
& c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) \\
& + 36*a^{**2}*b*d^{**4}*x^{**2}*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} \\
& + 50*d^{**4}*n + 24*d^{**4}) + 6*a*b^{**2}*c^{**3}*d*n*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d \\
& **4*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) + 24*a*b^{**2}*c^{**3}*d*(c + d*x) \\
& **n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2} + 50*d^{**4}*n + 24*d^{**4}) - 6*a*b \\
& **2*c^{**2}*d^{**2}*n^{**2}*x*(c + d*x)**n / (d^{**4}*n^{**4} + 10*d^{**4}*n^{**3} + 35*d^{**4}*n^{**2}
\end{aligned}$$

$$\begin{aligned}
& + 50*d^{4*n} + 24*d^4) - 24*a*b^2*c^2*d^2*n*x*(c + d*x)^n/(d^{4*n+4} + \\
& 10*d^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + 3*a*b^2*c*d^3*n^3*x \\
& ^2*(c + d*x)^n/(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24* \\
& d^4) + 15*a*b^2*c*d^3*n^2*x^2*(c + d*x)^n/(d^{4*n+4} + 10*d^{4*n+3} + \\
& 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + 12*a*b^2*c*d^3*n*x^2*(c + d*x)^n \\
& /(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + 3*a*b^2 \\
& *d^{4*n+3}*x^3*(c + d*x)^n/(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} + 50* \\
& d^{4*n} + 24*d^4) + 21*a*b^2*d^{4*n+2}*x^3*(c + d*x)^n/(d^{4*n+4} + 10*d \\
& ^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + 42*a*b^2*d^{4*n}*x^3*(c + \\
& d*x)^n/(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + \\
& 24*a*b^2*d^{4*n}*x^3*(c + d*x)^n/(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} + \\
& 50*d^{4*n} + 24*d^4) - 6*b^3*c^4*(c + d*x)^n/(d^{4*n+4} + 10*d^{4*n+3} \\
& + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + 6*b^3*c^3*d*n*x*(c + d*x)^n/(d^{4* \\
& n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) - 3*b^3*c^2*d \\
& ^2*n^2*x^2*(c + d*x)^n/(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} + 50*d^{4* \\
& n} + 24*d^4) - 3*b^3*c^2*d^2*n*x^2*(c + d*x)^n/(d^{4*n+4} + 10*d^{4* \\
& n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + b^3*c*d^3*n^3*x^3*(c + d* \\
& x)^n/(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + 3*b \\
& ^3*c*d^3*n^2*x^3*(c + d*x)^n/(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} \\
& + 50*d^{4*n} + 24*d^4) + 2*b^3*c*d^3*n*x^3*(c + d*x)^n/(d^{4*n+4} + 10* \\
& d^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + b^3*d^{4*n+3}*x^4*(c + \\
& d*x)^n/(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + 6 \\
& *b^3*d^{4*n+2}*x^4*(c + d*x)^n/(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} \\
& + 50*d^{4*n} + 24*d^4) + 11*b^3*d^{4*n}*x^4*(c + d*x)^n/(d^{4*n+4} + 10*d \\
& ^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4) + 6*b^3*d^{4*n}*x^4*(c + d*x) \\
& ^n/(d^{4*n+4} + 10*d^{4*n+3} + 35*d^{4*n+2} + 50*d^{4*n} + 24*d^4), True))
\end{aligned}$$

3.1853 $\int (a + bx)^2 (c + dx)^n dx$

Optimal. Leaf size=78

$$\frac{(bc - ad)^2 (c + dx)^{n+1}}{d^3 (n + 1)} - \frac{2b(bc - ad)(c + dx)^{n+2}}{d^3 (n + 2)} + \frac{b^2 (c + dx)^{n+3}}{d^3 (n + 3)}$$

[Out] $(-a*d+b*c)^2*(d*x+c)^(1+n)/d^3/(1+n)-2*b*(-a*d+b*c)*(d*x+c)^(2+n)/d^3/(2+n)+b^2*(d*x+c)^(3+n)/d^3/(3+n)$

Rubi [A] time = 0.03, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {43}

$$\frac{(bc - ad)^2 (c + dx)^{n+1}}{d^3 (n + 1)} - \frac{2b(bc - ad)(c + dx)^{n+2}}{d^3 (n + 2)} + \frac{b^2 (c + dx)^{n+3}}{d^3 (n + 3)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^2*(c + d*x)^n,x]

[Out] $((b*c - a*d)^2*(c + d*x)^(1 + n))/(d^3*(1 + n)) - (2*b*(b*c - a*d)*(c + d*x)^(2 + n))/(d^3*(2 + n)) + (b^2*(c + d*x)^(3 + n))/(d^3*(3 + n))$

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int (a + bx)^2 (c + dx)^n dx &= \int \left(\frac{(-bc + ad)^2 (c + dx)^n}{d^2} - \frac{2b(bc - ad)(c + dx)^{1+n}}{d^2} + \frac{b^2 (c + dx)^{2+n}}{d^2} \right) dx \\ &= \frac{(bc - ad)^2 (c + dx)^{1+n}}{d^3 (1 + n)} - \frac{2b(bc - ad)(c + dx)^{2+n}}{d^3 (2 + n)} + \frac{b^2 (c + dx)^{3+n}}{d^3 (3 + n)} \end{aligned}$$

Mathematica [A] time = 0.10, size = 67, normalized size = 0.86

$$\frac{(c + dx)^{n+1} \left(-\frac{2b(c+dx)(bc-ad)}{n+2} + \frac{(bc-ad)^2}{n+1} + \frac{b^2(c+dx)^2}{n+3} \right)}{d^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^2*(c + d*x)^n,x]

[Out] ((c + d*x)^(1 + n)*((b*c - a*d)^2/(1 + n) - (2*b*(b*c - a*d)*(c + d*x))/(2 + n) + (b^2*(c + d*x)^2)/(3 + n))/d^3

fricas [B] time = 1.20, size = 237, normalized size = 3.04

$$\frac{(a^2cd^2n^2 + 2b^2c^3 - 6abc^2d + 6a^2cd^2 + (b^2d^3n^2 + 3b^2d^3n + 2b^2d^3)x^3 + (6abd^3 + (b^2cd^2 + 2abd^3)n^2 + (b^2cd^2 + 2abd^3)n)x^2 + (2a^2cd^2 + 8a^2cd^2 + a^2d^3)n^2 - (2b^2c^2d - 6a^2cd^2 - 5a^2d^3)n)x}{d^3n^3 + 6d^3n^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^n,x, algorithm="fricas")

[Out] (a^2*c*d^2*n^2 + 2*b^2*c^3 - 6*a*b*c^2*d + 6*a^2*c*d^2 + (b^2*d^3*n^2 + 3*b^2*d^3*n + 2*b^2*d^3)*x^3 + (6*a*b*d^3 + (b^2*c*d^2 + 2*a*b*d^3)*n^2 + (b^2*c*d^2 + 8*a*b*d^3)*n)*x^2 - (2*a*b*c^2*d - 5*a^2*c*d^2)*n + (6*a^2*d^3 + (2*a*b*c*d^2 + a^2*d^3)*n^2 - (2*b^2*c^2*d - 6*a*b*c*d^2 - 5*a^2*d^3)*n)*x*(d*x + c)^n/(d^3*n^3 + 6*d^3*n^2 + 11*d^3*n + 6*d^3)

giac [B] time = 0.93, size = 385, normalized size = 4.94

$$\frac{(dx + c)^n b^2 d^3 n^2 x^3 + (dx + c)^n b^2 c d^2 n^2 x^2 + 2(dx + c)^n a b d^3 n^2 x^2 + 3(dx + c)^n b^2 d^3 n x^3 + 2(dx + c)^n a b c d^2 n^2 x + (dx + c)^n a^2 c d^2 n^2}{d^3 n^3 + 6 d^3 n^2 + 11 d^3 n + 6 d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^2*(d*x+c)^n,x, algorithm="giac")

[Out] ((d*x + c)^n*b^2*d^3*n^2*x^3 + (d*x + c)^n*b^2*c*d^2*n^2*x^2 + 2*(d*x + c)^n*a*b*d^3*n^2*x^2 + 3*(d*x + c)^n*b^2*d^3*n*x^3 + 2*(d*x + c)^n*a*b*c*d^2*n^2*x + (d*x + c)^n*a^2*d^3*n^2*x + (d*x + c)^n*b^2*c*d^2*n*x^2 + 8*(d*x + c)^n*a*b*d^3*n*x^2 + 2*(d*x + c)^n*b^2*d^3*x^3 + (d*x + c)^n*a^2*c*d^2*n^2 - 2*(d*x + c)^n*b^2*c^2*d*n*x + 6*(d*x + c)^n*a*b*c*d^2*n*x + 5*(d*x + c)^n*a^2*d^3*n*x + 6*(d*x + c)^n*a*b*d^3*x^2 - 2*(d*x + c)^n*a*b*c^2*d*n + 5*(d*x + c)^n*a^2*c*d^2*n + 6*(d*x + c)^n*a^2*d^3*x + 2*(d*x + c)^n*b^2*c^3 - 6*(d*x + c)^n*a*b*c^2*d + 6*(d*x + c)^n*a^2*c*d^2)/(d^3*n^3 + 6*d^3*n^2 + 11*d^3*n + 6*d^3)

maple [B] time = 0.01, size = 159, normalized size = 2.04

$$\frac{(b^2d^2n^2x^2 + 2abd^2n^2x + 3b^2d^2nx^2 + a^2d^2n^2 + 8abd^2nx - 2b^2cdnx + 2b^2x^2d^2 + 5a^2d^2n - 2abcdn + 6abd^2x - a^2d^2n^2)}{(n^3 + 6n^2 + 11n + 6)d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^2*(d*x+c)^n,x)`

[Out] $(d*x+c)^{(n+1)}*(b^2*d^2*n^2*x^2+2*a*b*d^2*n^2*x+3*b^2*d^2*n*x^2+a^2*d^2*n^2+8*a*b*d^2*n*x-2*b^2*c*d*n*x+2*b^2*d^2*x^2+5*a^2*d^2*n-2*a*b*c*d*n+6*a*b*d^2*x-2*b^2*c*d*x+6*a^2*d^2-6*a*b*c*d+2*b^2*c^2)/d^3/(n^3+6*n^2+11*n+6)$

maxima [A] time = 1.17, size = 138, normalized size = 1.77

$$\frac{2(d^2(n+1)x^2 + cdnx - c^2)(dx + c)^n ab}{(n^2 + 3n + 2)d^2} + \frac{(dx + c)^{n+1} a^2}{d(n+1)} + \frac{((n^2 + 3n + 2)d^3 x^3 + (n^2 + n)cd^2 x^2 - 2c^2 dnx + 2c^3)(d^3)}{(n^3 + 6n^2 + 11n + 6)d^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^2*(d*x+c)^n,x, algorithm="maxima")`

[Out] $2*(d^2*(n+1)*x^2 + c*d*n*x - c^2)*(d*x + c)^n*a*b/((n^2 + 3*n + 2)*d^2) + (d*x + c)^{(n+1)}*a^2/(d*(n+1)) + ((n^2 + 3*n + 2)*d^3*x^3 + (n^2 + n)*c*d^2*x^2 - 2*c^2*d*n*x + 2*c^3)*(d*x + c)^n*b^2/((n^3 + 6*n^2 + 11*n + 6)*d^3)$

mapad [B] time = 0.62, size = 226, normalized size = 2.90

$$(c + dx)^n \left(\frac{c(a^2 d^2 n^2 + 5a^2 d^2 n + 6a^2 d^2 - 2abcdn - 6abcd + 2b^2 c^2)}{d^3(n^3 + 6n^2 + 11n + 6)} + \frac{b^2 x^3 (n^2 + 3n + 2)}{n^3 + 6n^2 + 11n + 6} + \frac{x(a^2 d^3 n^2)}{n^3 + 6n^2 + 11n + 6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^2*(c + d*x)^n,x)`

[Out] $(c + d*x)^n*((c*(6*a^2*d^2 + 2*b^2*c^2 + 5*a^2*d^2*n + a^2*d^2*n^2 - 6*a*b*c*d - 2*a*b*c*d*n))/(d^3*(11*n + 6*n^2 + n^3 + 6)) + (b^2*x^3*(3*n + n^2 + 2))/(11*n + 6*n^2 + n^3 + 6) + (x*(6*a^2*d^3 + 5*a^2*d^3*n + a^2*d^3*n^2 - 2*b^2*c^2*d*n + 2*a*b*c*d^2*n^2 + 6*a*b*c*d^2*n))/(d^3*(11*n + 6*n^2 + n^3 + 6)) + (b*x^2*(n + 1)*(6*a*d + 2*a*d*n + b*c*n))/(d*(11*n + 6*n^2 + n^3 + 6)))$

sympy [A] time = 2.09, size = 1506, normalized size = 19.31

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**2*(d*x+c)**n,x)`

[Out] `Piecewise((c**n*(a**2*x + a*b*x**2 + b**2*x**3/3), Eq(d, 0)), (-a**2*d**2/(2*c**2*d**3 + 4*c*d**4*x + 2*d**5*x**2) - 2*a*b*c*d/(2*c**2*d**3 + 4*c*d**4`

```

*x + 2*d**5*x**2) - 4*a*b*d**2*x/(2*c**2*d**3 + 4*c*d**4*x + 2*d**5*x**2) +
  2*b**2*c**2*log(c/d + x)/(2*c**2*d**3 + 4*c*d**4*x + 2*d**5*x**2) + 3*b**2
*c**2/(2*c**2*d**3 + 4*c*d**4*x + 2*d**5*x**2) + 4*b**2*c*d*x*log(c/d + x)/
(2*c**2*d**3 + 4*c*d**4*x + 2*d**5*x**2) + 4*b**2*c*d*x/(2*c**2*d**3 + 4*c*
d**4*x + 2*d**5*x**2) + 2*b**2*d**2*x**2*log(c/d + x)/(2*c**2*d**3 + 4*c*d*
**4*x + 2*d**5*x**2), Eq(n, -3)), (-a**2*d**2/(c*d**3 + d**4*x) + 2*a*b*c*d*
log(c/d + x)/(c*d**3 + d**4*x) + 2*a*b*c*d/(c*d**3 + d**4*x) + 2*a*b*d**2*x
*log(c/d + x)/(c*d**3 + d**4*x) - 2*b**2*c**2*log(c/d + x)/(c*d**3 + d**4*x
) - 2*b**2*c**2/(c*d**3 + d**4*x) - 2*b**2*c*d*x*log(c/d + x)/(c*d**3 + d**
4*x) + b**2*d**2*x**2/(c*d**3 + d**4*x), Eq(n, -2)), (a**2*log(c/d + x)/d -
  2*a*b*c*log(c/d + x)/d**2 + 2*a*b*x/d + b**2*c**2*log(c/d + x)/d**3 - b**2
*c*x/d**2 + b**2*x**2/(2*d), Eq(n, -1)), (a**2*c*d**2*n**2*(c + d*x)**n/(d*
**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) + 5*a**2*c*d**2*n*(c + d*x)**n/
(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) + 6*a**2*c*d**2*(c + d*x)**n
/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) + a**2*d**3*n**2*x*(c + d*x
)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) + 5*a**2*d**3*n*x*(c +
d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) + 6*a**2*d**3*x*(c +
d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) - 2*a*b*c**2*d*n*(c
+ d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) - 6*a*b*c**2*d*(c
+ d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) + 2*a*b*c*d**2*n*
**2*x*(c + d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) + 6*a*b*c
d**2*n*x*(c + d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) + 2*a*
b*d**3*n**2*x**2*(c + d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3
) + 8*a*b*d**3*n*x**2*(c + d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6
*d**3) + 6*a*b*d**3*x**2*(c + d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n
+ 6*d**3) + 2*b**2*c**3*(c + d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**3*n +
6*d**3) - 2*b**2*c**2*d*n*x*(c + d*x)**n/(d**3*n**3 + 6*d**3*n**2 + 11*d**
3*n + 6*d**3) + b**2*c*d**2*n**2*x**2*(c + d*x)**n/(d**3*n**3 + 6*d**3*n**2
+ 11*d**3*n + 6*d**3) + b**2*c*d**2*n*x**2*(c + d*x)**n/(d**3*n**3 + 6*d**
3*n**2 + 11*d**3*n + 6*d**3) + b**2*d**3*n**2*x**3*(c + d*x)**n/(d**3*n**3
+ 6*d**3*n**2 + 11*d**3*n + 6*d**3) + 3*b**2*d**3*n*x**3*(c + d*x)**n/(d**3
*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3) + 2*b**2*d**3*x**3*(c + d*x)**n/(
d**3*n**3 + 6*d**3*n**2 + 11*d**3*n + 6*d**3), True))

```

3.1854 $\int (a + bx)(c + dx)^n dx$

Optimal. Leaf size=47

$$\frac{b(c + dx)^{n+2}}{d^2(n + 2)} - \frac{(bc - ad)(c + dx)^{n+1}}{d^2(n + 1)}$$

[Out] $-(-a*d+b*c)*(d*x+c)^(1+n)/d^2/(1+n)+b*(d*x+c)^(2+n)/d^2/(2+n)$

Rubi [A] time = 0.02, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.077$, Rules used = {43}

$$\frac{b(c + dx)^{n+2}}{d^2(n + 2)} - \frac{(bc - ad)(c + dx)^{n+1}}{d^2(n + 1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)*(c + d*x)^n, x]$

[Out] $-(((b*c - a*d)*(c + d*x)^(1 + n))/(d^2*(1 + n))) + (b*(c + d*x)^(2 + n))/(d^2*(2 + n))$

Rule 43

$\text{Int}[(a_.) + (b_.)*(x_.)]^(m_.)*((c_.) + (d_.)*(x_.))^(n_.), x_Symbol] :> \text{Int}[\text{ExpandIntegrand}[(a + b*x)^m*(c + d*x)^n, x], x] /; \text{FreeQ}[\{a, b, c, d, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (!\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0]) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int (a + bx)(c + dx)^n dx &= \int \left(\frac{(-bc + ad)(c + dx)^n}{d} + \frac{b(c + dx)^{1+n}}{d} \right) dx \\ &= -\frac{(bc - ad)(c + dx)^{1+n}}{d^2(1 + n)} + \frac{b(c + dx)^{2+n}}{d^2(2 + n)} \end{aligned}$$

Mathematica [A] time = 0.04, size = 41, normalized size = 0.87

$$\frac{(c + dx)^{n+1}(ad(n + 2) - bc + bd(n + 1)x)}{d^2(n + 1)(n + 2)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)*(c + d*x)^n,x]

[Out] ((c + d*x)^(1 + n)*(-(b*c) + a*d*(2 + n) + b*d*(1 + n)*x))/(d^2*(1 + n)*(2 + n))

fricas [A] time = 0.94, size = 83, normalized size = 1.77

$$\frac{(acd n - bc^2 + 2acd + (bd^2 n + bd^2)x^2 + (2ad^2 + (bcd + ad^2)n)x)(dx + c)^n}{d^2 n^2 + 3d^2 n + 2d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^n,x, algorithm="fricas")

[Out] (a*c*d*n - b*c^2 + 2*a*c*d + (b*d^2*n + b*d^2)*x^2 + (2*a*d^2 + (b*c*d + a*d^2)*n)*x)*(d*x + c)^n/(d^2*n^2 + 3*d^2*n + 2*d^2)

giac [B] time = 1.00, size = 132, normalized size = 2.81

$$\frac{(dx + c)^n bd^2 nx^2 + (dx + c)^n bcdnx + (dx + c)^n ad^2 nx + (dx + c)^n bd^2 x^2 + (dx + c)^n acdn + 2(dx + c)^n ad^2 x - (dx + c)^n bcd^2}{d^2 n^2 + 3d^2 n + 2d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^n,x, algorithm="giac")

[Out] ((d*x + c)^n*b*d^2*n*x^2 + (d*x + c)^n*b*c*d*n*x + (d*x + c)^n*a*d^2*n*x + (d*x + c)^n*b*d^2*x^2 + (d*x + c)^n*a*c*d*n + 2*(d*x + c)^n*a*d^2*x - (d*x + c)^n*b*c^2 + 2*(d*x + c)^n*a*c*d)/(d^2*n^2 + 3*d^2*n + 2*d^2)

maple [A] time = 0.00, size = 46, normalized size = 0.98

$$\frac{(bdnx + adn + bdx + 2ad - bc)(dx + c)^{n+1}}{(n^2 + 3n + 2)d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)*(d*x+c)^n,x)

[Out] (d*x+c)^(n+1)*(b*d*n*x+a*d*n+b*d*x+2*a*d-b*c)/d^2/(n^2+3*n+2)

maxima [A] time = 1.17, size = 63, normalized size = 1.34

$$\frac{(d^2(n+1)x^2 + cdx - c^2)(dx + c)^n b}{(n^2 + 3n + 2)d^2} + \frac{(dx + c)^{n+1} a}{d(n+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)^n,x, algorithm="maxima")

[Out] $(d^2*(n+1)*x^2 + c*d*n*x - c^2)*(d*x + c)^n*b/((n^2 + 3*n + 2)*d^2) + (d*x + c)^{(n+1)}*a/(d*(n+1))$

mupad [B] time = 0.49, size = 88, normalized size = 1.87

$$(c + dx)^n \left(\frac{c(2ad - bc + adn)}{d^2(n^2 + 3n + 2)} + \frac{bx^2(n+1)}{n^2 + 3n + 2} + \frac{x(2ad^2 + ad^2n + bcdn)}{d^2(n^2 + 3n + 2)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)*(c + d*x)^n,x)

[Out] $(c + d*x)^n*((c*(2*a*d - b*c + a*d*n))/(d^2*(3*n + n^2 + 2)) + (b*x^2*(n + 1))/(3*n + n^2 + 2) + (x*(2*a*d^2 + a*d^2*n + b*c*d*n))/(d^2*(3*n + n^2 + 2)))$

sympy [A] time = 0.82, size = 377, normalized size = 8.02

$$\left\{ \begin{array}{l} c^n \left(ax + \frac{bx^2}{2} \right) \\ -\frac{ad}{cd^2+d^3x} + \frac{bc \log\left(\frac{c}{d}+x\right)}{cd^2+d^3x} + \frac{bc}{cd^2+d^3x} + \frac{bdx \log\left(\frac{c}{d}+x\right)}{cd^2+d^3x} \\ \frac{a \log\left(\frac{c}{d}+x\right)}{d} - \frac{bc \log\left(\frac{c}{d}+x\right)}{d^2} + \frac{bx}{d} \\ \frac{acd n(c+dx)^n}{d^2 n^2 + 3d^2 n + 2d^2} + \frac{2acd(c+dx)^n}{d^2 n^2 + 3d^2 n + 2d^2} + \frac{ad^2 n x(c+dx)^n}{d^2 n^2 + 3d^2 n + 2d^2} + \frac{2ad^2 x(c+dx)^n}{d^2 n^2 + 3d^2 n + 2d^2} - \frac{bc^2(c+dx)^n}{d^2 n^2 + 3d^2 n + 2d^2} + \frac{bcd n x(c+dx)^n}{d^2 n^2 + 3d^2 n + 2d^2} + \frac{bd^2 n x^2(c+dx)^n}{d^2 n^2 + 3d^2 n + 2d^2} + \frac{bc^2 n x^2(c+dx)^n}{d^2 n^2 + 3d^2 n + 2d^2} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)*(d*x+c)**n,x)

[Out] Piecewise((c**n*(a*x + b*x**2/2), Eq(d, 0)), (-a*d/(c*d**2 + d**3*x) + b*c*log(c/d + x)/(c*d**2 + d**3*x) + b*c/(c*d**2 + d**3*x) + b*d*x*log(c/d + x)/(c*d**2 + d**3*x), Eq(n, -2)), (a*log(c/d + x)/d - b*c*log(c/d + x)/d**2 + b*x/d, Eq(n, -1)), (a*c*d*n*(c + d*x)**n/(d**2*n**2 + 3*d**2*n + 2*d**2) + 2*a*c*d*(c + d*x)**n/(d**2*n**2 + 3*d**2*n + 2*d**2) + a*d**2*n*x*(c + d*x)**n/(d**2*n**2 + 3*d**2*n + 2*d**2) + 2*a*d**2*x*(c + d*x)**n/(d**2*n**2 + 3*d**2*n + 2*d**2) - b*c**2*(c + d*x)**n/(d**2*n**2 + 3*d**2*n + 2*d**2) + b*c*d*n*x*(c + d*x)**n/(d**2*n**2 + 3*d**2*n + 2*d**2) + b*d**2*n*x**2*(c + d*x)**n/(d**2*n**2 + 3*d**2*n + 2*d**2) + b*d**2*x**2*(c + d*x)**n/(d**2*n**2 + 3*d**2*n + 2*d**2), True))

3.1855 $\int (c + dx)^n dx$

Optimal. Leaf size=18

$$\frac{(c + dx)^{n+1}}{d(n + 1)}$$

[Out] $(d*x+c)^{(1+n)}/d/(1+n)$

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {32}

$$\frac{(c + dx)^{n+1}}{d(n + 1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^n, x]$

[Out] $(c + d*x)^{(1 + n)}/(d*(1 + n))$

Rule 32

$\text{Int}[(a_.) + (b_.)*(x_)]^{(m_)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}/(b*(m + 1)), x] /; \text{FreeQ}\{a, b, m\}, x \ \&\& \ \text{NeQ}\{m, -1\}$

Rubi steps

$$\int (c + dx)^n dx = \frac{(c + dx)^{1+n}}{d(1 + n)}$$

Mathematica [A] time = 0.01, size = 17, normalized size = 0.94

$$\frac{(c + dx)^{n+1}}{dn + d}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(c + d*x)^n, x]$

[Out] $(c + d*x)^{(1 + n)}/(d + d*n)$

fricas [A] time = 0.70, size = 20, normalized size = 1.11

$$\frac{(dx + c)(dx + c)^n}{dn + d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n,x, algorithm="fricas")

[Out] (d*x + c)*(d*x + c)^n/(d*n + d)

giac [A] time = 1.02, size = 18, normalized size = 1.00

$$\frac{(dx + c)^{n+1}}{d(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n,x, algorithm="giac")

[Out] (d*x + c)^(n + 1)/(d*(n + 1))

maple [A] time = 0.00, size = 19, normalized size = 1.06

$$\frac{(dx + c)^{n+1}}{(n + 1)d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^n,x)

[Out] (d*x+c)^(n+1)/d/(n+1)

maxima [A] time = 1.12, size = 18, normalized size = 1.00

$$\frac{(dx + c)^{n+1}}{d(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n,x, algorithm="maxima")

[Out] (d*x + c)^(n + 1)/(d*(n + 1))

mupad [B] time = 0.38, size = 18, normalized size = 1.00

$$\frac{(c + dx)^{n+1}}{d(n + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^n,x)

[Out] $(c + dx)^{n+1}/(d(n+1))$

sympy [A] time = 0.06, size = 20, normalized size = 1.11

$$\frac{\begin{cases} \frac{(c+dx)^{n+1}}{n+1} & \text{for } n \neq -1 \\ \log(c+dx) & \text{otherwise} \end{cases}}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**n,x)

[Out] Piecewise(((c + d*x)**(n + 1)/(n + 1), Ne(n, -1)), (log(c + d*x), True))/d

$$3.1856 \quad \int \frac{(c+dx)^n}{a+bx} dx$$

Optimal. Leaf size=51

$$-\frac{(c+dx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{b(c+dx)}{bc-ad}\right)}{(n+1)(bc-ad)}$$

[Out] $-(d*x+c)^{(1+n)}*\text{hypergeom}([1, 1+n], [2+n], b*(d*x+c)/(-a*d+b*c))/(-a*d+b*c)/(1+n)$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {68}

$$-\frac{(c+dx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{b(c+dx)}{bc-ad}\right)}{(n+1)(bc-ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^n/(a + b*x), x]$

[Out] $-\left(\frac{(c + d*x)^{(1 + n)}*\text{Hypergeometric2F1}[1, 1 + n, 2 + n, (b*(c + d*x))/(b*c - a*d)]}{(b*c - a*d)*(1 + n)}\right)$

Rule 68

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] :> \text{Simp}[\left(\frac{b*c - a*d}{a + b*x}\right)^{n+1}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -\left(\frac{d*(a + b*x)}{b*c - a*d}\right)]/(b^{(n+1)}*(m+1)), x] /;$ FreeQ[{a, b, c, d, m}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && IntegerQ[n]

Rubi steps

$$\int \frac{(c+dx)^n}{a+bx} dx = -\frac{(c+dx)^{1+n} {}_2F_1\left(1, 1+n; 2+n; \frac{b(c+dx)}{bc-ad}\right)}{(bc-ad)(1+n)}$$

Mathematica [A] time = 0.01, size = 51, normalized size = 1.00

$$-\frac{(c+dx)^{n+1} {}_2F_1\left(1, n+1; n+2; \frac{b(c+dx)}{bc-ad}\right)}{(n+1)(bc-ad)}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^n/(a + b*x),x]

[Out] -(((c + d*x)^(1 + n)*Hypergeometric2F1[1, 1 + n, 2 + n, (b*(c + d*x))/(b*c - a*d)])/((b*c - a*d)*(1 + n)))

fricas [F] time = 0.64, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx + c)^n}{bx + a}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/(b*x+a),x, algorithm="fricas")

[Out] integral((d*x + c)^n/(b*x + a), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{bx + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/(b*x+a),x, algorithm="giac")

[Out] integrate((d*x + c)^n/(b*x + a), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{bx + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^n/(b*x+a),x)

[Out] int((d*x+c)^n/(b*x+a),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{bx + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/(b*x+a),x, algorithm="maxima")

[Out] integrate((d*x + c)^n/(b*x + a), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(c + dx)^n}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^n/(a + b*x),x)

[Out] int((c + d*x)^n/(a + b*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^n}{a + bx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**n/(b*x+a),x)

[Out] Integral((c + d*x)**n/(a + b*x), x)

$$3.1857 \quad \int \frac{(c+dx)^n}{(a+bx)^2} dx$$

Optimal. Leaf size=51

$$\frac{d(c+dx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{b(c+dx)}{bc-ad}\right)}{(n+1)(bc-ad)^2}$$

[Out] $d*(d*x+c)^{(1+n)}*\text{hypergeom}([2, 1+n], [2+n], b*(d*x+c)/(-a*d+b*c))/(-a*d+b*c)^2/(1+n)$

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {68}

$$\frac{d(c+dx)^{n+1} {}_2F_1\left(2, n+1; n+2; \frac{b(c+dx)}{bc-ad}\right)}{(n+1)(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^n/(a + b*x)^2, x]$

[Out] $(d*(c + d*x)^{(1 + n)}*\text{Hypergeometric2F1}[2, 1 + n, 2 + n, (b*(c + d*x))/(b*c - a*d)])/((b*c - a*d)^2*(1 + n))$

Rule 68

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(b*c - a*d)^n*(a + b*x)^{(m + 1)}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b^{(n + 1)}*(m + 1)), x] /;$ $\text{FreeQ}\{a, b, c, d, m\}, x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{!IntegerQ}[m] \&\& \text{IntegerQ}[n]$

Rubi steps

$$\int \frac{(c+dx)^n}{(a+bx)^2} dx = \frac{d(c+dx)^{1+n} {}_2F_1\left(2, 1+n; 2+n; \frac{b(c+dx)}{bc-ad}\right)}{(bc-ad)^2(1+n)}$$

Mathematica [A] time = 0.02, size = 52, normalized size = 1.02

$$\frac{d(c+dx)^{n+1} {}_2F_1\left(2, n+1; n+2; -\frac{b(c+dx)}{ad-bc}\right)}{(n+1)(ad-bc)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^n/(a + b*x)^2,x]

[Out] (d*(c + d*x)^(1 + n)*Hypergeometric2F1[2, 1 + n, 2 + n, -((b*(c + d*x))/(-(b*c) + a*d))])/((-b*c) + a*d)^2*(1 + n))

fricas [F] time = 0.69, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx + c)^n}{b^2x^2 + 2abx + a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/(b*x+a)^2,x, algorithm="fricas")

[Out] integral((d*x + c)^n/(b^2*x^2 + 2*a*b*x + a^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{(bx + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/(b*x+a)^2,x, algorithm="giac")

[Out] integrate((d*x + c)^n/(b*x + a)^2, x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{(bx + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^n/(b*x+a)^2,x)

[Out] int((d*x+c)^n/(b*x+a)^2,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{(bx + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/(b*x+a)^2,x, algorithm="maxima")

[Out] integrate((d*x + c)^n/(b*x + a)^2, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(c + dx)^n}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^n/(a + b*x)^2,x)

[Out] int((c + d*x)^n/(a + b*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^n}{(a + bx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**n/(b*x+a)**2,x)

[Out] Integral((c + d*x)**n/(a + b*x)**2, x)

$$3.1858 \quad \int \frac{(c+dx)^n}{(a+bx)^3} dx$$

Optimal. Leaf size=54

$$\frac{d^2(c+dx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{b(c+dx)}{bc-ad}\right)}{(n+1)(bc-ad)^3}$$

[Out] $-d^2*(d*x+c)^{(1+n)}*\text{hypergeom}([3, 1+n], [2+n], b*(d*x+c)/(-a*d+b*c))/(-a*d+b*c)^3/(1+n)$

Rubi [A] time = 0.02, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {68}

$$\frac{d^2(c+dx)^{n+1} {}_2F_1\left(3, n+1; n+2; \frac{b(c+dx)}{bc-ad}\right)}{(n+1)(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^n/(a + b*x)^3, x]

[Out] $-((d^2*(c + d*x)^{(1 + n)}*\text{Hypergeometric2F1}[3, 1 + n, 2 + n, (b*(c + d*x))/(b*c - a*d)])/((b*c - a*d)^3*(1 + n))$

Rule 68

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((b*c - a*d)^n*(a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b^(n + 1)*(m + 1)), x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && IntegerQ[n]

Rubi steps

$$\int \frac{(c+dx)^n}{(a+bx)^3} dx = -\frac{d^2(c+dx)^{1+n} {}_2F_1\left(3, 1+n; 2+n; \frac{b(c+dx)}{bc-ad}\right)}{(bc-ad)^3(1+n)}$$

Mathematica [A] time = 0.02, size = 54, normalized size = 1.00

$$\frac{d^2(c+dx)^{n+1} {}_2F_1\left(3, n+1; n+2; -\frac{b(c+dx)}{ad-bc}\right)}{(n+1)(ad-bc)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^n/(a + b*x)^3,x]

[Out] (d^2*(c + d*x)^(1 + n)*Hypergeometric2F1[3, 1 + n, 2 + n, -((b*(c + d*x))/(-b*c) + a*d)))/((-b*c) + a*d)^3*(1 + n))

fricas [F] time = 0.65, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(dx + c)^n}{b^3x^3 + 3ab^2x^2 + 3a^2bx + a^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/(b*x+a)^3,x, algorithm="fricas")

[Out] integral((d*x + c)^n/(b^3*x^3 + 3*a*b^2*x^2 + 3*a^2*b*x + a^3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{(bx + a)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/(b*x+a)^3,x, algorithm="giac")

[Out] integrate((d*x + c)^n/(b*x + a)^3, x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{(bx + a)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^n/(b*x+a)^3,x)

[Out] int((d*x+c)^n/(b*x+a)^3,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{(bx + a)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/(b*x+a)^3,x, algorithm="maxima")

[Out] integrate((d*x + c)^n/(b*x + a)^3, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(c + dx)^n}{(a + bx)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^n/(a + b*x)^3, x)

[Out] int((c + d*x)^n/(a + b*x)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^n}{(a + bx)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**n/(b*x+a)**3, x)

[Out] Integral((c + d*x)**n/(a + b*x)**3, x)

3.1859 $\int (a + bx)^{-4+n} (c + dx)^{-n} dx$

Optimal. Leaf size=143

$$-\frac{2d^2(a+bx)^{n-1}(c+dx)^{1-n}}{(1-n)(2-n)(3-n)(bc-ad)^3} - \frac{(a+bx)^{n-3}(c+dx)^{1-n}}{(3-n)(bc-ad)} + \frac{2d(a+bx)^{n-2}(c+dx)^{1-n}}{(2-n)(3-n)(bc-ad)^2}$$

[Out] $-(b*x+a)^{-3+n}*(d*x+c)^{(1-n)/(-a*d+b*c)/(3-n)+2*d*(b*x+a)^{-2+n}*(d*x+c)^{(1-n)/(-a*d+b*c)^2/(2-n)/(3-n)-2*d^2*(b*x+a)^{-1+n}*(d*x+c)^{(1-n)/(-a*d+b*c)^3/(1-n)/(2-n)/(3-n)}$

Rubi [A] time = 0.06, antiderivative size = 143, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{2d^2(a+bx)^{n-1}(c+dx)^{1-n}}{(1-n)(2-n)(3-n)(bc-ad)^3} - \frac{(a+bx)^{n-3}(c+dx)^{1-n}}{(3-n)(bc-ad)} + \frac{2d(a+bx)^{n-2}(c+dx)^{1-n}}{(2-n)(3-n)(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{-4 + n}/(c + d*x)^n, x]$

[Out] $-\left(\frac{(a + b*x)^{-3 + n}*(c + d*x)^{(1 - n)}}{(b*c - a*d)*(3 - n)}\right) + \left(\frac{2*d*(a + b*x)^{-2 + n}*(c + d*x)^{(1 - n)}}{(b*c - a*d)^2*(2 - n)*(3 - n)} - \frac{2*d^2*(a + b*x)^{-1 + n}*(c + d*x)^{(1 - n)}}{(b*c - a*d)^3*(1 - n)*(2 - n)*(3 - n)}\right)$

Rule 37

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[\frac{(a + b*x)^{m+1}*(c + d*x)^{n+1}}{(b*c - a*d)*(m+1)}, x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{EqQ}[m + n + 2, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rule 45

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[\frac{(a + b*x)^{m+1}*(c + d*x)^{n+1}}{(b*c - a*d)*(m+1)}, x] - \text{Dist}[\frac{d*Simplify[m + n + 2]}{(b*c - a*d)*(m+1)}, \text{Int}[(a + b*x)^{Simplify[m+1]}*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{IntegerQ}[n] \ \&\& \ (\text{EqQ}[a, 0] \ \|\ \text{NeQ}[c, 0] \ \&\& \ \text{LtQ}[m - n, 0] \ \&\& \ \text{IntegerQ}[n]) \ \&\& \ (\text{SumSimplerQ}[m, 1] \ \|\ \text{SumSimplerQ}[n, 1])$

Rubi steps

$$\begin{aligned}
\int (a+bx)^{-4+n}(c+dx)^{-n} dx &= -\frac{(a+bx)^{-3+n}(c+dx)^{1-n}}{(bc-ad)(3-n)} - \frac{(2d) \int (a+bx)^{-3+n}(c+dx)^{-n} dx}{(bc-ad)(3-n)} \\
&= -\frac{(a+bx)^{-3+n}(c+dx)^{1-n}}{(bc-ad)(3-n)} + \frac{2d(a+bx)^{-2+n}(c+dx)^{1-n}}{(bc-ad)^2(2-n)(3-n)} + \frac{(2d^2) \int (a+bx)^{-2+n}(c+dx)^{-n} dx}{(bc-ad)^2(2-n)(3-n)} \\
&= -\frac{(a+bx)^{-3+n}(c+dx)^{1-n}}{(bc-ad)(3-n)} + \frac{2d(a+bx)^{-2+n}(c+dx)^{1-n}}{(bc-ad)^2(2-n)(3-n)} - \frac{2d^2(a+bx)^{-1+n}(c+dx)^{-n}}{(bc-ad)^3(1-n)(2-n)}
\end{aligned}$$

Mathematica [A] time = 0.10, size = 112, normalized size = 0.78

$$\frac{(a+bx)^{n-3}(c+dx)^{1-n} \left(a^2 d^2 (n^2 - 5n + 6) - 2abd(n-3)(c(n-1) + dx) + b^2 (c^2 (n^2 - 3n + 2) + 2cd(n-1)x + 2d^2 x^2) \right)}{(n-3)(n-2)(n-1)(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-4 + n)/(c + d*x)^n, x]

[Out] ((a + b*x)^(-3 + n)*(c + d*x)^(1 - n)*(a^2*d^2*(6 - 5*n + n^2) - 2*a*b*d*(-3 + n)*(c*(-1 + n) + d*x) + b^2*(c^2*(2 - 3*n + n^2) + 2*c*d*(-1 + n)*x + 2*d^2*x^2)))/((b*c - a*d)^3*(-3 + n)*(-2 + n)*(-1 + n))

fricas [B] time = 0.93, size = 512, normalized size = 3.58

$$\frac{(2b^3d^3x^4 + 2ab^2c^3 - 6a^2bc^2d + 6a^3cd^2 + 2(4ab^2d^3 + (b^3cd^2 - ab^2d^3)n)x^3 + (ab^2c^3 - 2a^2bc^2d + a^3cd^2)n^2 + (6b^3c^3 - 18ab^2c^2d + 18a^2b^2c^2d - 6a^3d^3 - (b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3)n)x^2 - (3a^2b^2c^3 - 8a^2b^2c^2d + 5a^3cd^2)n + (2b^3c^3 - 6a^2b^2c^2d + 6a^2b^2c^2d + 6a^3d^3 + (b^3c^3 - a^2b^2c^2d - a^2b^2c^2d + a^3d^3)n)n^2 - (3b^3c^3 - 7a^2b^2c^2d + 5a^3d^3)n)x)(b*x + a)^{(n-4)}}{(6b^3c^3 - 18ab^2c^2d + 18a^2b^2c^2d - 6a^3d^3 - (b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3)n)^3 + 6*(b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3)n^2 - 11*(b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3)n)*(d*x + c)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-4+n)/((d*x+c)^n), x, algorithm="fricas")

[Out] -(2*b^3*d^3*x^4 + 2*a*b^2*c^3 - 6*a^2*b*c^2*d + 6*a^3*c*d^2 + 2*(4*a*b^2*d^3 + (b^3*c*d^2 - a*b^2*d^3)*n)*x^3 + (a*b^2*c^3 - 2*a^2*b*c^2*d + a^3*c*d^2)*n^2 + (12*a^2*b*d^3 + (b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*n^2 - (b^3*c^2*d - 8*a*b^2*c*d^2 + 7*a^2*b*d^3)*n)*x^2 - (3*a*b^2*c^3 - 8*a^2*b*c^2*d + 5*a^3*c*d^2)*n + (2*b^3*c^3 - 6*a*b^2*c^2*d + 6*a^2*b*c*d^2 + 6*a^3*d^3 + (b^3*c^3 - a*b^2*c^2*d - a^2*b*c*d^2 + a^3*d^3)*n)n^2 - (3*b^3*c^3 - 7*a*b^2*c^2*d - a^2*b*c*d^2 + 5*a^3*d^3)*n)*x*(b*x + a)^(n - 4)/((6*b^3*c^3 - 18*a*b^2*c^2*d + 18*a^2*b*c*d^2 - 6*a^3*d^3 - (b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*n)^3 + 6*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*n^2 - 11*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b*c*d^2 - a^3*d^3)*n)*(d*x + c)^n)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n-4}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-4+n)/((d*x+c)^n),x, algorithm="giac")

[Out] integrate((b*x + a)^(n - 4)/(d*x + c)^n, x)

maple [B] time = 0.01, size = 322, normalized size = 2.25

$$\frac{(dx + c) \left(a^2 d^2 n^2 - 2abcd n^2 - 2ab d^2 n x + b^2 c^2 n^2 + 2b^2 c d n x + 2b^2 x^2 d^2 - 5a^2 d^2 n + 8abcd n + 6ab d^2 x - a^3 d^3 n^3 - 3a^2 b c d^2 n^3 + 3a b^2 c^2 d n^3 - b^3 c^3 n^3 - 6a^3 d^3 n^2 + 18a^2 b c d^2 n^2 - 18a b^2 c^2 d n^2 + 6b^3 c^3 n^2 + 11a^3 d^3 n - 33a^2 b c d^2 n - 33a b^2 c^2 d n + 11b^3 c^3 \right)}{(dx + c)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(-4+n)/((d*x+c)^n),x)

[Out]
$$-(b*x+a)^{(n-3)}*(d*x+c)*(a^2*d^2*n^2-2*a*b*c*d*n^2-2*a*b*d^2*n*x+b^2*c^2*n^2+2*b^2*c*d*n*x+2*b^2*d^2*x^2-5*a^2*d^2*n+8*a*b*c*d*n+6*a*b*d^2*x-3*b^2*c^2*n-2*b^2*c*d*x+6*a^2*d^2-6*a*b*c*d+2*b^2*c^2)/(a^3*d^3*n^3-3*a^2*b*c*d^2*n^3+3*a*b^2*c^2*d*n^3-b^3*c^3*n^3-6*a^3*d^3*n^2+18*a^2*b*c*d^2*n^2-18*a*b^2*c^2*d*n^2+6*b^3*c^3*n^2+11*a^3*d^3*n-33*a^2*b*c*d^2*n+33*a*b^2*c^2*d*n-11*b^3*c^3*n-6*a^3*d^3+18*a^2*b*c*d^2-18*a*b^2*c^2*d+6*b^3*c^3)/((d*x+c)^n)$$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n-4}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-4+n)/((d*x+c)^n),x, algorithm="maxima")

[Out] integrate((b*x + a)^(n - 4)/(d*x + c)^n, x)

mupad [B] time = 1.10, size = 528, normalized size = 3.69

$$\frac{x(a + bx)^{n-4} \left(a^3 d^3 n^2 - 5a^3 d^3 n + 6a^3 d^3 - a^2 b c d^2 n^2 + a^2 b c d^2 n + 6a^2 b c d^2 - a b^2 c^2 d n^2 + 7a b^2 c^2 d n - a^3 d^3 n^3 + 3a^2 b c d^2 n^3 - 3a b^2 c^2 d n^3 + b^3 c^3 n^3 - 6a^3 d^3 n^2 + 18a^2 b c d^2 n^2 - 18a b^2 c^2 d n^2 + 6b^3 c^3 n^2 + 11a^3 d^3 n - 33a^2 b c d^2 n + 33a b^2 c^2 d n - 11b^3 c^3 n - 6a^3 d^3 + 18a^2 b c d^2 - 18a b^2 c^2 d + 6b^3 c^3 \right)}{(ad - bc)^3 (c + dx)^n (n^3 - 6n^2 + 11n - 6)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(n - 4)/(c + d*x)^n,x)

```
[Out] - (x*(a + b*x)^(n - 4)*(6*a^3*d^3 + 2*b^3*c^3 - 5*a^3*d^3*n - 3*b^3*c^3*n +
a^3*d^3*n^2 + b^3*c^3*n^2 - 6*a*b^2*c^2*d + 6*a^2*b*c*d^2 + 7*a*b^2*c^2*d*
n + a^2*b*c*d^2*n - a*b^2*c^2*d*n^2 - a^2*b*c*d^2*n^2))/((a*d - b*c)^3*(c +
d*x)^n*(11*n - 6*n^2 + n^3 - 6)) - (a*c*(a + b*x)^(n - 4)*(6*a^2*d^2 + 2*b
^2*c^2 - 5*a^2*d^2*n - 3*b^2*c^2*n + a^2*d^2*n^2 + b^2*c^2*n^2 - 6*a*b*c*d
+ 8*a*b*c*d*n - 2*a*b*c*d*n^2))/((a*d - b*c)^3*(c + d*x)^n*(11*n - 6*n^2 +
n^3 - 6)) - (2*b^3*d^3*x^4*(a + b*x)^(n - 4))/((a*d - b*c)^3*(c + d*x)^n*(1
1*n - 6*n^2 + n^3 - 6)) - (b*d*x^2*(a + b*x)^(n - 4)*(12*a^2*d^2 - 7*a^2*d^
2*n - b^2*c^2*n + a^2*d^2*n^2 + b^2*c^2*n^2 + 8*a*b*c*d*n - 2*a*b*c*d*n^2))
/((a*d - b*c)^3*(c + d*x)^n*(11*n - 6*n^2 + n^3 - 6)) - (2*b^2*d^2*x^3*(a +
b*x)^(n - 4)*(4*a*d - a*d*n + b*c*n))/((a*d - b*c)^3*(c + d*x)^n*(11*n - 6
*n^2 + n^3 - 6))
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(-4+n)/((d*x+c)**n),x)
```

```
[Out] Timed out
```


3.1860 $\int (a + bx)^{-3+n} (c + dx)^{-n} dx$

Optimal. Leaf size=86

$$\frac{d(a + bx)^{n-1}(c + dx)^{1-n}}{(1-n)(2-n)(bc - ad)^2} - \frac{(a + bx)^{n-2}(c + dx)^{1-n}}{(2-n)(bc - ad)}$$

[Out] $-(b*x+a)^{-2+n}*(d*x+c)^{(1-n)/(-a*d+b*c)/(2-n)+d*(b*x+a)^{-1+n}*(d*x+c)^{(1-n)/(-a*d+b*c)^2/(1-n)/(2-n)}$

Rubi [A] time = 0.01, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{d(a + bx)^{n-1}(c + dx)^{1-n}}{(1-n)(2-n)(bc - ad)^2} - \frac{(a + bx)^{n-2}(c + dx)^{1-n}}{(2-n)(bc - ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-3 + n)/(c + d*x)^n, x]

[Out] $-(((a + b*x)^{-2 + n}*(c + d*x)^{(1 - n)})/((b*c - a*d)*(2 - n))) + (d*(a + b*x)^{-1 + n}*(c + d*x)^{(1 - n)})/((b*c - a*d)^2*(1 - n)*(2 - n))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && IntegerQ[m + n + 2] && !IntegerQ[n] && !IntegerQ[m] && !IntegerQ[n - 1] && !IntegerQ[m - 1] && !IntegerQ[n]

Rubi steps

$$\int (a + bx)^{-3+n}(c + dx)^{-n} dx = -\frac{(a + bx)^{-2+n}(c + dx)^{1-n}}{(bc - ad)(2 - n)} - \frac{d \int (a + bx)^{-2+n}(c + dx)^{-n} dx}{(bc - ad)(2 - n)}$$

$$= -\frac{(a + bx)^{-2+n}(c + dx)^{1-n}}{(bc - ad)(2 - n)} + \frac{d(a + bx)^{-1+n}(c + dx)^{1-n}}{(bc - ad)^2(1 - n)(2 - n)}$$

Mathematica [A] time = 0.04, size = 59, normalized size = 0.69

$$\frac{(a + bx)^{n-2}(c + dx)^{1-n}(-ad(n - 2) + bc(n - 1) + bdx)}{(n - 2)(n - 1)(bc - ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-3 + n)/(c + d*x)^n,x]

[Out] ((a + b*x)^(-2 + n)*(c + d*x)^(1 - n)*(-(a*d*(-2 + n)) + b*c*(-1 + n) + b*d*x))/((b*c - a*d)^2*(-2 + n)*(-1 + n))

fricas [B] time = 0.88, size = 206, normalized size = 2.40

$$\frac{(b^2d^2x^3 - abc^2 + 2a^2cd + (3abd^2 + (b^2cd - abd^2)n)x^2 + (abc^2 - a^2cd)n - (b^2c^2 - 2abcd - 2a^2d^2 - (b^2c^2 - a^2d^2)n)(dx + c)^n)}{(2b^2c^2 - 4abcd + 2a^2d^2 + (b^2c^2 - 2abcd + a^2d^2)n^2 - 3(b^2c^2 - 2abcd + a^2d^2)n)(dx + c)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-3+n)/((d*x+c)^n),x, algorithm="fricas")

[Out] (b^2*d^2*x^3 - a*b*c^2 + 2*a^2*c*d + (3*a*b*d^2 + (b^2*c*d - a*b*d^2)*n)*x^2 + (a*b*c^2 - a^2*c*d)*n - (b^2*c^2 - 2*a*b*c*d - 2*a^2*d^2 - (b^2*c^2 - a^2*d^2)*n)*x*(b*x + a)^(n - 3)/((2*b^2*c^2 - 4*a*b*c*d + 2*a^2*d^2 + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*n)^2 - 3*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*n)*(d*x + c)^n)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n-3}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-3+n)/((d*x+c)^n),x, algorithm="giac")

[Out] integrate((b*x + a)^(n - 3)/(d*x + c)^n, x)

maple [A] time = 0.01, size = 127, normalized size = 1.48

$$\frac{(dx + c)(adn - bcn - bdx - 2ad + bc)(bx + a)^{n-2}(dx + c)^{-n}}{a^2d^2n^2 - 2abcdn^2 + b^2c^2n^2 - 3a^2d^2n + 6abcdn - 3b^2c^2n + 2a^2d^2 - 4abcd + 2b^2c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(n-3)/((d*x+c)^n), x)

[Out] $-(b*x+a)^{(n-2)}*(d*x+c)*(a*d*n-b*c*n-b*d*x-2*a*d+b*c)/(a^2*d^2*n^2-2*a*b*c*d*n^2+b^2*c^2*n^2-3*a^2*d^2*n+6*a*b*c*d*n-3*b^2*c^2*n+2*a^2*d^2-4*a*b*c*d+2*b^2*c^2)/((d*x+c)^n)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n-3}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-3+n)/((d*x+c)^n), x, algorithm="maxima")

[Out] integrate((b*x + a)^(n - 3)/(d*x + c)^n, x)

mupad [B] time = 0.77, size = 220, normalized size = 2.56

$$(a + bx)^{n-3} \left(\frac{x(2a^2d^2 - b^2c^2 - a^2d^2n + b^2c^2n + 2abcd)}{(ad - bc)^2(c + dx)^n(n^2 - 3n + 2)} + \frac{b^2d^2x^3}{(ad - bc)^2(c + dx)^n(n^2 - 3n + 2)} + \frac{ac(2}{(ad - bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^(n - 3)/(c + d*x)^n, x)

[Out] $(a + b*x)^{(n - 3)}*((x*(2*a^2*d^2 - b^2*c^2 - a^2*d^2*n + b^2*c^2*n + 2*a*b*c*d))/((a*d - b*c)^2*(c + d*x)^n*(n^2 - 3*n + 2)) + (b^2*d^2*x^3)/((a*d - b*c)^2*(c + d*x)^n*(n^2 - 3*n + 2)) + (a*c*(2*a*d - b*c - a*d*n + b*c*n))/((a*d - b*c)^2*(c + d*x)^n*(n^2 - 3*n + 2)) + (b*d*x^2*(3*a*d - a*d*n + b*c*n))/((a*d - b*c)^2*(c + d*x)^n*(n^2 - 3*n + 2)))$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(-3+n)/((d*x+c)**n), x)

[Out] Timed out

$$3.1861 \quad \int (a + bx)^{-2+n} (c + dx)^{-n} dx$$

Optimal. Leaf size=39

$$-\frac{(a + bx)^{n-1}(c + dx)^{1-n}}{(1 - n)(bc - ad)}$$

[Out] $-(b*x+a)^{-1+n}*(d*x+c)^{1-n}/(-a*d+b*c)/(1-n)$

Rubi [A] time = 0.00, antiderivative size = 39, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$-\frac{(a + bx)^{n-1}(c + dx)^{1-n}}{(1 - n)(bc - ad)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{-2 + n}/(c + d*x)^n, x]$

[Out] $-\frac{((a + b*x)^{-1 + n}*(c + d*x)^{1 - n})}{((b*c - a*d)*(1 - n))}$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}]/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{EqQ}[m + n + 2, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rubi steps

$$\int (a + bx)^{-2+n} (c + dx)^{-n} dx = -\frac{(a + bx)^{-1+n} (c + dx)^{1-n}}{(bc - ad)(1 - n)}$$

Mathematica [A] time = 0.02, size = 36, normalized size = 0.92

$$\frac{(a + bx)^{n-1}(c + dx)^{1-n}}{(n - 1)(bc - ad)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(a + b*x)^{-2 + n}/(c + d*x)^n, x]$

[Out] $((a + b*x)^{-1 + n}*(c + d*x)^{1 - n})/((b*c - a*d)*(-1 + n))$

fricas [A] time = 1.05, size = 60, normalized size = 1.54

$$\frac{(bdx^2 + ac + (bc + ad)x)(bx + a)^{n-2}}{(bc - ad - (bc - ad)n)(dx + c)^n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-2+n)/((d*x+c)^n),x, algorithm="fricas")

[Out] -(b*d*x^2 + a*c + (b*c + a*d)*x)*(b*x + a)^(n - 2)/((b*c - a*d - (b*c - a*d)*n)*(d*x + c)^n)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n-2}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-2+n)/((d*x+c)^n),x, algorithm="giac")

[Out] integrate((b*x + a)^(n - 2)/(d*x + c)^n, x)

maple [A] time = 0.00, size = 45, normalized size = 1.15

$$\frac{(dx + c)(bx + a)^{n-1}(dx + c)^{-n}}{adn - bcn - ad + bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(n-2)/((d*x+c)^n),x)

[Out] -(b*x+a)^(n-1)*(d*x+c)/(a*d*n-b*c*n-a*d+b*c)/((d*x+c)^n)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n-2}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-2+n)/((d*x+c)^n),x, algorithm="maxima")

[Out] integrate((b*x + a)^(n - 2)/(d*x + c)^n, x)

mupad [B] time = 0.56, size = 102, normalized size = 2.62

$$-(a + bx)^{n-2} \left(\frac{ac}{(ad - bc)(n - 1)(c + dx)^n} + \frac{x(ad + bc)}{(ad - bc)(n - 1)(c + dx)^n} + \frac{bdx^2}{(ad - bc)(n - 1)(c + dx)^n} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*x)^(n - 2)/(c + d*x)^n,x)
```

```
[Out] -(a + b*x)^(n - 2)*((a*c)/((a*d - b*c)*(n - 1)*(c + d*x)^n) + (x*(a*d + b*c)))/((a*d - b*c)*(n - 1)*(c + d*x)^n) + (b*d*x^2)/((a*d - b*c)*(n - 1)*(c + d*x)^n)
```

```
sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00
```

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(-2+n)/((d*x+c)**n),x)
```

```
[Out] Exception raised: HeuristicGCDFailed
```

3.1862 $\int (a + bx)^{-1+n} (c + dx)^{-n} dx$

Optimal. Leaf size=66

$$\frac{(a + bx)^n (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad}\right)^n {}_2F_1\left(n, n; n+1; -\frac{d(a+bx)}{bc-ad}\right)}{bn}$$

[Out] (b*x+a)^n*(b*(d*x+c)/(-a*d+b*c))^n*hypergeom([n, n], [1+n], -d*(b*x+a)/(-a*d+b*c))/b/n/((d*x+c)^n)

Rubi [A] time = 0.02, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{(a + bx)^n (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad}\right)^n {}_2F_1\left(n, n; n+1; -\frac{d(a+bx)}{bc-ad}\right)}{bn}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-1 + n)/(c + d*x)^n, x]

[Out] ((a + b*x)^n*((b*(c + d*x))/(b*c - a*d))^n*Hypergeometric2F1[n, n, 1 + n, -((d*(a + b*x))/(b*c - a*d))]/(b*n*(c + d*x)^n)

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/((b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n]), Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int (a + bx)^{-1+n} (c + dx)^{-n} dx = \left((c + dx)^{-n} \left(\frac{b(c + dx)}{bc - ad} \right)^n \right) \int (a + bx)^{-1+n} \left(\frac{bc}{bc - ad} + \frac{bdx}{bc - ad} \right)^{-n} dx$$

$$= \frac{(a + bx)^n (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n; 1 + n; -\frac{d(a+bx)}{bc-ad} \right)}{bn}$$

Mathematica [A] time = 0.03, size = 65, normalized size = 0.98

$$\frac{(a + bx)^n (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n; n + 1; \frac{d(a+bx)}{ad-bc} \right)}{bn}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-1 + n)/(c + d*x)^n,x]

[Out] ((a + b*x)^n*((b*(c + d*x))/(b*c - a*d))^n*Hypergeometric2F1[n, n, 1 + n, (d*(a + b*x))/(-b*c) + a*d])/(b*n*(c + d*x)^n)

fricas [F] time = 0.85, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^{n-1}}{(dx + c)^n}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-1+n)/((d*x+c)^n),x, algorithm="fricas")

[Out] integral((b*x + a)^(n - 1)/(d*x + c)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n-1}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-1+n)/((d*x+c)^n),x, algorithm="giac")

[Out] integrate((b*x + a)^(n - 1)/(d*x + c)^n, x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{n-1} (dx + c)^{-n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(n-1)/((d*x+c)^n),x)`

[Out] `int((b*x+a)^(n-1)/((d*x+c)^n),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n-1}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(-1+n)/((d*x+c)^n),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(n - 1)/(d*x + c)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^{n-1}}{(c + dx)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(n - 1)/(c + d*x)^n,x)`

[Out] `int((a + b*x)^(n - 1)/(c + d*x)^n, x)`

sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(-1+n)/((d*x+c)**n),x)`

[Out] Exception raised: HeuristicGCDFailed

3.1863 $\int (a + bx)^n (c + dx)^{-n} dx$

Optimal. Leaf size=72

$$\frac{(a + bx)^{n+1} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n+1; n+2; -\frac{d(a+bx)}{bc-ad} \right)}{b(n+1)}$$

[Out] $(b*x+a)^{(1+n)}*(b*(d*x+c)/(-a*d+b*c))^{-n}*\text{hypergeom}([n, 1+n], [2+n], -d*(b*x+a)/(-a*d+b*c))/b/(1+n)/((d*x+c)^n)$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {70, 69}

$$\frac{(a + bx)^{n+1} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n+1; n+2; -\frac{d(a+bx)}{bc-ad} \right)}{b(n+1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^n/(c + d*x)^n, x]$

[Out] $((a + b*x)^{(1 + n)}*((b*(c + d*x))/(b*c - a*d))^{-n}*\text{Hypergeometric2F1}[n, 1 + n, 2 + n, -((d*(a + b*x))/(b*c - a*d))]/(b*(1 + n)*(c + d*x)^n)$

Rule 69

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& \text{GtQ}[b/(b*c - a*d), 0] \&\& (\text{RationalQ}[m] \parallel !(\text{RationalQ}[n] \&\& \text{GtQ}[-(d/(b*c - a*d)), 0]))$

Rule 70

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Dist}[(c + d*x)^{\text{FracPart}[n]}/(b/(b*c - a*d))^{\text{IntPart}[n]}*((b*(c + d*x))/(b*c - a*d))^{\text{FracPart}[n]}], \text{Int}[(a + b*x)^m*\text{Simp}[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& (\text{RationalQ}[m] \parallel !\text{SimplerQ}[n + 1, m + 1])$

Rubi steps

$$\int (a + bx)^n (c + dx)^{-n} dx = \left((c + dx)^{-n} \left(\frac{b(c + dx)}{bc - ad} \right)^n \right) \int (a + bx)^n \left(\frac{bc}{bc - ad} + \frac{bdx}{bc - ad} \right)^{-n} dx$$

$$= \frac{(a + bx)^{1+n} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, 1 + n; 2 + n; -\frac{d(a+bx)}{bc-ad} \right)}{b(1 + n)}$$

Mathematica [A] time = 0.03, size = 71, normalized size = 0.99

$$\frac{(a + bx)^{n+1} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n + 1; n + 2; \frac{d(a+bx)}{ad-bc} \right)}{b(n + 1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/(c + d*x)^n,x]

[Out] ((a + b*x)^(1 + n)*((b*(c + d*x))/(b*c - a*d))^n*Hypergeometric2F1[n, 1 + n, 2 + n, (d*(a + b*x))/(-b*c) + a*d])/(b*(1 + n)*(c + d*x)^n)

fricas [F] time = 0.79, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^n}{(dx + c)^n}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/((d*x+c)^n),x, algorithm="fricas")

[Out] integral((b*x + a)^n/(d*x + c)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/((d*x+c)^n),x, algorithm="giac")

[Out] integrate((b*x + a)^n/(d*x + c)^n, x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^n (dx + c)^{-n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^n/((d*x+c)^n),x)`

[Out] `int((b*x+a)^n/((d*x+c)^n),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^n/((d*x+c)^n),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^n/(d*x + c)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^n}{(c + dx)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^n/(c + d*x)^n,x)`

[Out] `int((a + b*x)^n/(c + d*x)^n, x)`

sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**n/((d*x+c)**n),x)`

[Out] Exception raised: HeuristicGCDFailed

3.1864 $\int (a + bx)^{1+n} (c + dx)^{-n} dx$

Optimal. Leaf size=72

$$\frac{(a + bx)^{n+2} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n+2; n+3; -\frac{d(a+bx)}{bc-ad} \right)}{b(n+2)}$$

[Out] (b*x+a)^(2+n)*(b*(d*x+c)/(-a*d+b*c))^n*hypergeom([n, 2+n], [3+n], -d*(b*x+a)/(-a*d+b*c))/b/(2+n)/((d*x+c)^n)

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{(a + bx)^{n+2} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n+2; n+3; -\frac{d(a+bx)}{bc-ad} \right)}{b(n+2)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(1 + n)/(c + d*x)^n, x]

[Out] ((a + b*x)^(2 + n)*((b*(c + d*x))/(b*c - a*d))^n*Hypergeometric2F1[n, 2 + n, 3 + n, -((d*(a + b*x))/(b*c - a*d))]/(b*(2 + n)*(c + d*x)^n)

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[(((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Dist[(c + d*x)^FracPart[n]/(b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n], Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int (a + bx)^{1+n} (c + dx)^{-n} dx = \left((c + dx)^{-n} \left(\frac{b(c + dx)}{bc - ad} \right)^n \right) \int (a + bx)^{1+n} \left(\frac{bc}{bc - ad} + \frac{bdx}{bc - ad} \right)^{-n} dx$$

$$= \frac{(a + bx)^{2+n} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, 2 + n; 3 + n; -\frac{d(a+bx)}{bc-ad} \right)}{b(2 + n)}$$

Mathematica [A] time = 0.06, size = 89, normalized size = 1.24

$$\frac{(bc - ad)(a + bx)^n (c + dx)^{1-n} \left(\frac{d(a+bx)}{ad-bc} \right)^{-n} {}_2F_1 \left(-n - 1, 1 - n; 2 - n; \frac{b(c+dx)}{bc-ad} \right)}{d^2(n - 1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1 + n)/(c + d*x)^n,x]

[Out] ((b*c - a*d)*(a + b*x)^n*(c + d*x)^(1 - n)*Hypergeometric2F1[-1 - n, 1 - n, 2 - n, (b*(c + d*x))/(b*c - a*d)]/(d^2*(-1 + n)*((d*(a + b*x))/(-(b*c) + a*d))^n)

fricas [F] time = 0.74, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^{n+1}}{(dx + c)^n}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1+n)/((d*x+c)^n),x, algorithm="fricas")

[Out] integral((b*x + a)^(n + 1)/(d*x + c)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n+1}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1+n)/((d*x+c)^n),x, algorithm="giac")

[Out] integrate((b*x + a)^(n + 1)/(d*x + c)^n, x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{n+1} (dx + c)^{-n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(n+1)/((d*x+c)^n),x)`

[Out] `int((b*x+a)^(n+1)/((d*x+c)^n),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n+1}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1+n)/((d*x+c)^n),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(n + 1)/(d*x + c)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{n+1}}{(c + dx)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(n + 1)/(c + d*x)^n,x)`

[Out] `int((a + b*x)^(n + 1)/(c + d*x)^n, x)`

sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1+n)/((d*x+c)**n),x)`

[Out] Exception raised: HeuristicGCDFailed

3.1865 $\int (a + bx)^{2+n} (c + dx)^{-n} dx$

Optimal. Leaf size=72

$$\frac{(a + bx)^{n+3} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n+3; n+4; -\frac{d(a+bx)}{bc-ad} \right)}{b(n+3)}$$

[Out] $(b*x+a)^{(3+n)}*(b*(d*x+c)/(-a*d+b*c))^{n}*hypergeom([n, 3+n], [4+n], -d*(b*x+a)/(-a*d+b*c))/b/(3+n)/((d*x+c)^n)$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{(a + bx)^{n+3} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n+3; n+4; -\frac{d(a+bx)}{bc-ad} \right)}{b(n+3)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(2 + n)}/(c + d*x)^n, x]$

[Out] $((a + b*x)^{(3 + n)}*((b*(c + d*x))/(b*c - a*d))^{n}*Hypergeometric2F1[n, 3 + n, 4 + n, -((d*(a + b*x))/(b*c - a*d))]/(b*(3 + n)*(c + d*x)^n)$

Rule 69

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& \text{GtQ}[b/(b*c - a*d), 0] \&\& (\text{RationalQ}[m] || !(\text{RationalQ}[n] \&\& \text{GtQ}[-(d/(b*c - a*d)), 0]))$

Rule 70

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Dist}[(c + d*x)^{\text{FracPart}[n]}/(b/(b*c - a*d))^{\text{IntPart}[n]}*((b*(c + d*x))/(b*c - a*d))^{\text{FracPart}[n]}, \text{Int}[(a + b*x)^m*\text{Simp}[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& (\text{RationalQ}[m] || !\text{SimplerQ}[n + 1, m + 1])$

Rubi steps

$$\int (a + bx)^{2+n} (c + dx)^{-n} dx = \left((c + dx)^{-n} \left(\frac{b(c + dx)}{bc - ad} \right)^n \right) \int (a + bx)^{2+n} \left(\frac{bc}{bc - ad} + \frac{bdx}{bc - ad} \right)^{-n} dx$$

$$= \frac{(a + bx)^{3+n} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, 3 + n; 4 + n; -\frac{d(a+bx)}{bc-ad} \right)}{b(3 + n)}$$

Mathematica [A] time = 0.05, size = 92, normalized size = 1.28

$$-\frac{(bc - ad)^2 (a + bx)^n (c + dx)^{1-n} \left(\frac{d(a+bx)}{ad-bc} \right)^{-n} {}_2F_1 \left(-n - 2, 1 - n; 2 - n; \frac{b(c+dx)}{bc-ad} \right)}{d^3(n - 1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(2 + n)/(c + d*x)^n, x]

[Out] -(((b*c - a*d)^2*(a + b*x)^n*(c + d*x)^(1 - n)*Hypergeometric2F1[-2 - n, 1 - n, 2 - n, (b*(c + d*x))/(b*c - a*d]])/(d^3*(-1 + n)*((d*(a + b*x))/(-(b*c) + a*d))^n))

fricas [F] time = 0.81, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^{n+2}}{(dx + c)^n}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2+n)/((d*x+c)^n), x, algorithm="fricas")

[Out] integral((b*x + a)^(n + 2)/(d*x + c)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n+2}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(2+n)/((d*x+c)^n), x, algorithm="giac")

[Out] integrate((b*x + a)^(n + 2)/(d*x + c)^n, x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int (bx + a)^{n+2} (dx + c)^{-n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(n+2)/((d*x+c)^n),x)`

[Out] `int((b*x+a)^(n+2)/((d*x+c)^n),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^{n+2}}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(2+n)/((d*x+c)^n),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(n + 2)/(d*x + c)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{n+2}}{(c + dx)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(n + 2)/(c + d*x)^n,x)`

[Out] `int((a + b*x)^(n + 2)/(c + d*x)^n, x)`

sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(2+n)/((d*x+c)**n),x)`

[Out] Exception raised: HeuristicGCDFailed

3.1866 $\int (a + bx)^{-n} (c + dx)^n dx$

Optimal. Leaf size=72

$$\frac{(a + bx)^{-n} (c + dx)^{n+1} \left(-\frac{d(a+bx)}{bc-ad} \right)^n {}_2F_1 \left(n, n+1; n+2; \frac{b(c+dx)}{bc-ad} \right)}{d(n+1)}$$

[Out] $(-d*(b*x+a)/(-a*d+b*c))^{n+1}*(d*x+c)^{(1+n)}*\text{hypergeom}([n, 1+n], [2+n], b*(d*x+c)/(-a*d+b*c))/d/(1+n)/((b*x+a)^n)$

Rubi [A] time = 0.03, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {70, 69}

$$\frac{(a + bx)^{-n} (c + dx)^{n+1} \left(-\frac{d(a+bx)}{bc-ad} \right)^n {}_2F_1 \left(n, n+1; n+2; \frac{b(c+dx)}{bc-ad} \right)}{d(n+1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^n/(a + b*x)^n, x]$

[Out] $((-((d*(a + b*x))/(b*c - a*d)))^{n+1}*(c + d*x)^{(1 + n)}*\text{Hypergeometric2F1}[n, 1 + n, 2 + n, (b*(c + d*x))/(b*c - a*d)])/d*(1 + n)*(a + b*x)^n)$

Rule 69

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& \text{GtQ}[b/(b*c - a*d), 0] \&\& (\text{RationalQ}[m] \mid\mid !(\text{RationalQ}[n] \&\& \text{GtQ}[-(d/(b*c - a*d)), 0]))$

Rule 70

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] \rightarrow \text{Dist}[(c + d*x)^{\text{FracPart}[n]}/(b/(b*c - a*d))^{\text{IntPart}[n]}*((b*(c + d*x))/(b*c - a*d))^{\text{FracPart}[n]}], \text{Int}[(a + b*x)^m*\text{Simp}[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& (\text{RationalQ}[m] \mid\mid !\text{SimplerQ}[n + 1, m + 1])$

Rubi steps

$$\int (a + bx)^{-n} (c + dx)^n dx = \left((a + bx)^{-n} \left(\frac{d(a + bx)}{-bc + ad} \right)^n \right) \int (c + dx)^n \left(-\frac{ad}{bc - ad} - \frac{bdx}{bc - ad} \right)^{-n} dx$$

$$= \frac{(a + bx)^{-n} \left(-\frac{d(a+bx)}{bc-ad} \right)^n (c + dx)^{1+n} {}_2F_1 \left(n, 1 + n; 2 + n; \frac{b(c+dx)}{bc-ad} \right)}{d(1 + n)}$$

Mathematica [A] time = 0.03, size = 71, normalized size = 0.99

$$\frac{(a + bx)^{-n} (c + dx)^{n+1} \left(\frac{d(a+bx)}{ad-bc} \right)^n {}_2F_1 \left(n, n + 1; n + 2; \frac{b(c+dx)}{bc-ad} \right)}{d(n + 1)}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^n/(a + b*x)^n,x]

[Out] (((d*(a + b*x))/(- (b*c) + a*d))^n*(c + d*x)^(1 + n)*Hypergeometric2F1[n, 1 + n, 2 + n, (b*(c + d*x))/(b*c - a*d)]/(d*(1 + n)*(a + b*x)^n)

fricas [F] time = 1.08, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(dx + c)^n}{(bx + a)^n}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/((b*x+a)^n),x, algorithm="fricas")

[Out] integral((d*x + c)^n/(b*x + a)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{(bx + a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^n/((b*x+a)^n),x, algorithm="giac")

[Out] integrate((d*x + c)^n/(b*x + a)^n, x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n} (dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^n/((b*x+a)^n),x)`

[Out] `int((d*x+c)^n/((b*x+a)^n),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^n}{(bx + a)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^n/((b*x+a)^n),x, algorithm="maxima")`

[Out] `integrate((d*x + c)^n/(b*x + a)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^n}{(a + bx)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^n/(a + b*x)^n,x)`

[Out] `int((c + d*x)^n/(a + b*x)^n, x)`

sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**n/((b*x+a)**n),x)`

[Out] Exception raised: HeuristicGCDFailed

3.1867 $\int (a + bx)^{-1-n} (c + dx)^n dx$

Optimal. Leaf size=75

$$\frac{(a + bx)^{-n} (c + dx)^n \left(\frac{b(c+dx)}{bc-ad} \right)^{-n} {}_2F_1 \left(-n, -n; 1 - n; -\frac{d(a+bx)}{bc-ad} \right)}{bn}$$

[Out] $-(d*x+c)^n \text{hypergeom}([-n, -n], [1-n], -d*(b*x+a)/(-a*d+b*c))/b/n/((b*x+a)^n)/((b*(d*x+c)/(-a*d+b*c))^n)$

Rubi [A] time = 0.02, antiderivative size = 75, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{(a + bx)^{-n} (c + dx)^n \left(\frac{b(c+dx)}{bc-ad} \right)^{-n} {}_2F_1 \left(-n, -n; 1 - n; -\frac{d(a+bx)}{bc-ad} \right)}{bn}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{-1 - n} * (c + d*x)^n, x]$

[Out] $-\left(\left(\left(c + d*x\right)^n \text{Hypergeometric2F1}[-n, -n, 1 - n, -\left(\left(d*(a + b*x)\right)/\left(b*c - a*d\right)\right]\right)\right)/\left(b*n*(a + b*x)^n*\left(\left(b*(c + d*x)\right)/\left(b*c - a*d\right)\right)^n\right)$

Rule 69

$\text{Int}[\left((a_) + (b_)*(x_)\right)^{(m_)*\left((c_) + (d_)*(x_)\right)^{(n_)}, x_Symbol] \rightarrow \text{Simp}[\left((a + b*x)^{(m + 1)}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -\left(\left(d*(a + b*x)\right)/\left(b*c - a*d\right)\right]\right)/\left(b*(m + 1)*\left(b/\left(b*c - a*d\right)\right)^n\right), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

$\text{Int}[\left((a_) + (b_)*(x_)\right)^{(m_)*\left((c_) + (d_)*(x_)\right)^{(n_)}, x_Symbol] \rightarrow \text{Dist}[\left((c + d*x)^{\text{FracPart}[n]}/\left(\left(b/\left(b*c - a*d\right)\right)^{\text{IntPart}[n]}*\left(\left(b*(c + d*x)\right)/\left(b*c - a*d\right)\right)^{\text{FracPart}[n]}\right), \text{Int}[\left(a + b*x\right)^m*\text{Simp}[\left(b*c\right)/\left(b*c - a*d\right) + \left(b*d*x\right)/\left(b*c - a*d\right), x]^n, x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int (a + bx)^{-1-n} (c + dx)^n dx = \left((c + dx)^n \left(\frac{b(c + dx)}{bc - ad} \right)^{-n} \right) \int (a + bx)^{-1-n} \left(\frac{bc}{bc - ad} + \frac{bdx}{bc - ad} \right)^n dx$$

$$= - \frac{(a + bx)^{-n} (c + dx)^n \left(\frac{b(c+dx)}{bc-ad} \right)^{-n} {}_2F_1 \left(-n, -n; 1 - n; -\frac{d(a+bx)}{bc-ad} \right)}{bn}$$

Mathematica [A] time = 0.03, size = 74, normalized size = 0.99

$$- \frac{(a + bx)^{-n} (c + dx)^n \left(\frac{b(c+dx)}{bc-ad} \right)^{-n} {}_2F_1 \left(-n, -n; 1 - n; \frac{d(a+bx)}{ad-bc} \right)}{bn}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-1 - n)*(c + d*x)^n,x]

[Out] -(((c + d*x)^n*Hypergeometric2F1[-n, -n, 1 - n, (d*(a + b*x))/(-(b*c) + a*d)])/(b*n*(a + b*x)^n*((b*(c + d*x))/(b*c - a*d))^n))

fricas [F] time = 0.67, size = 0, normalized size = 0.00

$$\text{integral} \left((bx + a)^{-n-1} (dx + c)^n, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-1-n)*(d*x+c)^n,x, algorithm="fricas")

[Out] integral((b*x + a)^(-n - 1)*(d*x + c)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n-1} (dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-1-n)*(d*x+c)^n,x, algorithm="giac")

[Out] integrate((b*x + a)^(-n - 1)*(d*x + c)^n, x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n-1} (dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(-1-n)*(d*x+c)^n,x)`

[Out] `int((b*x+a)^(-1-n)*(d*x+c)^n,x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n-1}(dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(-1-n)*(d*x+c)^n,x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(-n - 1)*(d*x + c)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^n}{(a + bx)^{n+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^n/(a + b*x)^(n + 1),x)`

[Out] `int((c + d*x)^n/(a + b*x)^(n + 1), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(-1-n)*(d*x+c)**n,x)`

[Out] Timed out

$$3.1868 \quad \int (a + bx)^{-2-n} (c + dx)^n dx$$

Optimal. Leaf size=37

$$\frac{(a + bx)^{-n-1} (c + dx)^{n+1}}{(n + 1)(bc - ad)}$$

[Out] $-(b*x+a)^{-(-1-n)}*(d*x+c)^{(1+n)/(-a*d+b*c)/(1+n)}$

Rubi [A] time = 0.01, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{(a + bx)^{-n-1} (c + dx)^{n+1}}{(n + 1)(bc - ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-2 - n)*(c + d*x)^n, x]

[Out] $-(((a + b*x)^{-(-1 - n)}*(c + d*x)^{(1 + n)})/((b*c - a*d)*(1 + n)))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^{-2-n} (c + dx)^n dx = -\frac{(a + bx)^{-1-n} (c + dx)^{1+n}}{(bc - ad)(1 + n)}$$

Mathematica [A] time = 0.02, size = 38, normalized size = 1.03

$$\frac{(a + bx)^{-n-1} (c + dx)^{n+1}}{(-n - 1)(bc - ad)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-2 - n)*(c + d*x)^n, x]

[Out] $((a + b*x)^{-(-1 - n)}*(c + d*x)^{(1 + n)})/((b*c - a*d)*(-1 - n))$

fricas [A] time = 0.73, size = 59, normalized size = 1.59

$$\frac{(bdx^2 + ac + (bc + ad)x)(bx + a)^{-n-2}(dx + c)^n}{bc - ad + (bc - ad)n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-2-n)*(d*x+c)^n,x, algorithm="fricas")

[Out] -(b*d*x^2 + a*c + (b*c + a*d)*x)*(b*x + a)^(-n - 2)*(d*x + c)^n/(b*c - a*d + (b*c - a*d)*n)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n-2}(dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-2-n)*(d*x+c)^n,x, algorithm="giac")

[Out] integrate((b*x + a)^(-n - 2)*(d*x + c)^n, x)

maple [A] time = 0.00, size = 41, normalized size = 1.11

$$\frac{(bx + a)^{-n-1}(dx + c)^{n+1}}{adn - bcn + ad - bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(-n-2)*(d*x+c)^n,x)

[Out] (b*x+a)^(-n-1)*(d*x+c)^(n+1)/(a*d*n-b*c*n+a*d-b*c)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n-2}(dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-2-n)*(d*x+c)^n,x, algorithm="maxima")

[Out] integrate((b*x + a)^(-n - 2)*(d*x + c)^n, x)

mupad [B] time = 0.53, size = 97, normalized size = 2.62

$$\frac{\frac{ac(c+dx)^n}{(ad-bc)(n+1)} + \frac{x(ad+bc)(c+dx)^n}{(ad-bc)(n+1)} + \frac{bdx^2(c+dx)^n}{(ad-bc)(n+1)}}{(a+bx)^{n+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^n/(a + b*x)^(n + 2),x)
```

```
[Out] ((a*c*(c + d*x)^n)/((a*d - b*c)*(n + 1)) + (x*(a*d + b*c)*(c + d*x)^n)/((a*d - b*c)*(n + 1)) + (b*d*x^2*(c + d*x)^n)/((a*d - b*c)*(n + 1)))/(a + b*x)^(n + 2)
```

```
sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00
```

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(-2-n)*(d*x+c)**n,x)
```

```
[Out] Exception raised: HeuristicGCDFailed
```

3.1869 $\int (a + bx)^{-3-n} (c + dx)^n dx$

Optimal. Leaf size=80

$$\frac{d(a + bx)^{-n-1}(c + dx)^{n+1}}{(n + 1)(n + 2)(bc - ad)^2} - \frac{(a + bx)^{-n-2}(c + dx)^{n+1}}{(n + 2)(bc - ad)}$$

[Out] $-(b*x+a)^{-2-n}*(d*x+c)^{(1+n)} / (-a*d+b*c) / (2+n) + d*(b*x+a)^{-1-n}*(d*x+c)^{(1+n)} / (-a*d+b*c)^2 / (1+n) / (2+n)$

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{d(a + bx)^{-n-1}(c + dx)^{n+1}}{(n + 1)(n + 2)(bc - ad)^2} - \frac{(a + bx)^{-n-2}(c + dx)^{n+1}}{(n + 2)(bc - ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-3 - n)*(c + d*x)^n, x]

[Out] $-(((a + b*x)^{-2 - n}*(c + d*x)^{(1 + n)}) / ((b*c - a*d)*(2 + n))) + (d*(a + b*x)^{-1 - n}*(c + d*x)^{(1 + n)}) / ((b*c - a*d)^2*(1 + n)*(2 + n))$

Rule 37

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp
[((a + b*x)^(m + 1)*(c + d*x)^(n + 1)) / ((b*c - a*d)*(m + 1)), x] /; FreeQ[{
a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
1]
```

Rule 45

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1)) / ((b*c - a*d)*(m + 1)), x] - Dist[(d*S
implify[m + n + 2]) / ((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
+ d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
(EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
Q[m, 1] || !SumSimplerQ[n, 1])
```

Rubi steps

$$\int (a + bx)^{-3-n}(c + dx)^n dx = -\frac{(a + bx)^{-2-n}(c + dx)^{1+n}}{(bc - ad)(2 + n)} - \frac{d \int (a + bx)^{-2-n}(c + dx)^n dx}{(bc - ad)(2 + n)}$$

$$= -\frac{(a + bx)^{-2-n}(c + dx)^{1+n}}{(bc - ad)(2 + n)} + \frac{d(a + bx)^{-1-n}(c + dx)^{1+n}}{(bc - ad)^2(1 + n)(2 + n)}$$

Mathematica [A] time = 0.03, size = 60, normalized size = 0.75

$$\frac{(a + bx)^{-n-2}(c + dx)^{n+1}(ad(n + 2) - b(cn + c - dx))}{(n + 1)(n + 2)(bc - ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-3 - n)*(c + d*x)^n,x]

[Out] ((a + b*x)^(-2 - n)*(c + d*x)^(1 + n)*(a*d*(2 + n) - b*(c + c*n - d*x)))/((b*c - a*d)^2*(1 + n)*(2 + n))

fricas [B] time = 0.98, size = 207, normalized size = 2.59

$$\frac{(b^2 d^2 x^3 - abc^2 + 2 a^2 cd + (3 abd^2 - (b^2 cd - abd^2)n)x^2 - (abc^2 - a^2 cd)n - (b^2 c^2 - 2 abcd - 2 a^2 d^2 + (b^2 c^2 - a^2 d^2)n)}{2 b^2 c^2 - 4 abcd + 2 a^2 d^2 + (b^2 c^2 - 2 abcd + a^2 d^2)n^2 + 3 (b^2 c^2 - 2 abcd + a^2 d^2)n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-3-n)*(d*x+c)^n,x, algorithm="fricas")

[Out] (b^2*d^2*x^3 - a*b*c^2 + 2*a^2*c*d + (3*a*b*d^2 - (b^2*c*d - a*b*d^2)*n)*x^2 - (a*b*c^2 - a^2*c*d)*n - (b^2*c^2 - 2*a*b*c*d - 2*a^2*d^2 + (b^2*c^2 - a^2*d^2)*n)*x)*(b*x + a)^(-n - 3)*(d*x + c)^n/(2*b^2*c^2 - 4*a*b*c*d + 2*a^2*d^2 + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*n^2 + 3*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*n)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n-3}(dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-3-n)*(d*x+c)^n,x, algorithm="giac")

[Out] integrate((b*x + a)^(-n - 3)*(d*x + c)^n, x)

maple [A] time = 0.00, size = 123, normalized size = 1.54

$$\frac{(adn - bcn + bdx + 2ad - bc)(bx + a)^{-n-2}(dx + c)^{n+1}}{a^2d^2n^2 - 2abcdn^2 + b^2c^2n^2 + 3a^2d^2n - 6abcdn + 3b^2c^2n + 2a^2d^2 - 4abcd + 2b^2c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(-3-n)*(d*x+c)^n,x)

[Out] (b*x+a)^(-n-2)*(d*x+c)^(n+1)*(a*d*n-b*c*n+b*d*x+2*a*d-b*c)/(a^2*d^2*n^2-2*a*b*c*d*n^2+b^2*c^2*n^2+3*a^2*d^2*n-6*a*b*c*d*n+3*b^2*c^2*n+2*a^2*d^2-4*a*b*c*d+2*b^2*c^2)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n-3}(dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-3-n)*(d*x+c)^n,x, algorithm="maxima")

[Out] integrate((b*x + a)^(-n - 3)*(d*x + c)^n, x)

mupad [B] time = 0.74, size = 214, normalized size = 2.68

$$\frac{x(c+dx)^n(2a^2d^2-b^2c^2+a^2d^2n-b^2c^2n+2abcd)}{(ad-bc)^2(n^2+3n+2)} + \frac{ac(c+dx)^n(2ad-bc+adn-bcn)}{(ad-bc)^2(n^2+3n+2)} + \frac{b^2d^2x^3(c+dx)^n}{(ad-bc)^2(n^2+3n+2)} + \frac{bdx^2(c+dx)^n(3ad+adn-bcn)}{(ad-bc)^2(n^2+3n+2)}$$

$$(a+bx)^{n+3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^n/(a + b*x)^(n + 3),x)

[Out] ((x*(c + d*x)^n*(2*a^2*d^2 - b^2*c^2 + a^2*d^2*n - b^2*c^2*n + 2*a*b*c*d))/((a*d - b*c)^2*(3*n + n^2 + 2)) + (a*c*(c + d*x)^n*(2*a*d - b*c + a*d*n - b*c*n))/((a*d - b*c)^2*(3*n + n^2 + 2)) + (b^2*d^2*x^3*(c + d*x)^n)/((a*d - b*c)^2*(3*n + n^2 + 2)) + (b*d*x^2*(c + d*x)^n*(3*a*d + a*d*n - b*c*n))/((a*d - b*c)^2*(3*n + n^2 + 2)))/(a + b*x)^(n + 3)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(-3-n)*(d*x+c)**n,x)

[Out] Timed out

3.1870 $\int (a + bx)^{-4-n} (c + dx)^n dx$

Optimal. Leaf size=131

$$-\frac{2d^2(a+bx)^{-n-1}(c+dx)^{n+1}}{(n+1)(n+2)(n+3)(bc-ad)^3} - \frac{(a+bx)^{-n-3}(c+dx)^{n+1}}{(n+3)(bc-ad)} + \frac{2d(a+bx)^{-n-2}(c+dx)^{n+1}}{(n+2)(n+3)(bc-ad)^2}$$

[Out] $-(b*x+a)^{-(-3-n)*(d*x+c)^{(1+n)/(-a*d+b*c)/(3+n)+2*d*(b*x+a)^{-(-2-n)*(d*x+c)^{(1+n)/(-a*d+b*c)^2/(2+n)/(3+n)-2*d^2*(b*x+a)^{-(-1-n)*(d*x+c)^{(1+n)/(-a*d+b*c)^3/(1+n)/(2+n)/(3+n)}$

Rubi [A] time = 0.05, antiderivative size = 131, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{2d^2(a+bx)^{-n-1}(c+dx)^{n+1}}{(n+1)(n+2)(n+3)(bc-ad)^3} - \frac{(a+bx)^{-n-3}(c+dx)^{n+1}}{(n+3)(bc-ad)} + \frac{2d(a+bx)^{-n-2}(c+dx)^{n+1}}{(n+2)(n+3)(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-4 - n)*(c + d*x)^n, x]

[Out] $-\left(\frac{(a + b*x)^{-3 - n}*(c + d*x)^{(1 + n)}}{(b*c - a*d)*(3 + n)}\right) + \left(\frac{2*d*(a + b*x)^{-2 - n}*(c + d*x)^{(1 + n)}}{(b*c - a*d)^2*(2 + n)*(3 + n)} - \frac{2*d^2*(a + b*x)^{-1 - n}*(c + d*x)^{(1 + n)}}{(b*c - a*d)^3*(1 + n)*(2 + n)*(3 + n)}\right)$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int (a+bx)^{-4-n}(c+dx)^n dx &= -\frac{(a+bx)^{-3-n}(c+dx)^{1+n}}{(bc-ad)(3+n)} - \frac{(2d) \int (a+bx)^{-3-n}(c+dx)^n dx}{(bc-ad)(3+n)} \\
&= -\frac{(a+bx)^{-3-n}(c+dx)^{1+n}}{(bc-ad)(3+n)} + \frac{2d(a+bx)^{-2-n}(c+dx)^{1+n}}{(bc-ad)^2(2+n)(3+n)} + \frac{(2d^2) \int (a+bx)^{-2-n}(c+dx)^n dx}{(bc-ad)^2(2+n)(3+n)} \\
&= -\frac{(a+bx)^{-3-n}(c+dx)^{1+n}}{(bc-ad)(3+n)} + \frac{2d(a+bx)^{-2-n}(c+dx)^{1+n}}{(bc-ad)^2(2+n)(3+n)} - \frac{2d^2(a+bx)^{-1-n}(c+dx)^n}{(bc-ad)^3(1+n)(2+n)(3+n)}
\end{aligned}$$

Mathematica [A] time = 0.08, size = 113, normalized size = 0.86

$$\frac{(a+bx)^{-n-3}(c+dx)^{n+1} \left(a^2 d^2 (n^2 + 5n + 6) - 2abd(n+3)(cn + c - dx) + b^2 (c^2 (n^2 + 3n + 2) - 2cd(n+1)x + 2d^2) \right)}{(n+1)(n+2)(n+3)(bc-ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-4 - n)*(c + d*x)^n,x]

[Out] -(((a + b*x)^(-3 - n)*(c + d*x)^(1 + n)*(a^2*d^2*(6 + 5*n + n^2) - 2*a*b*d*(3 + n)*(c + c*n - d*x) + b^2*(c^2*(2 + 3*n + n^2) - 2*c*d*(1 + n)*x + 2*d^2*x^2)))/((b*c - a*d)^3*(1 + n)*(2 + n)*(3 + n)))

fricas [B] time = 0.99, size = 509, normalized size = 3.89

$$\frac{(2b^3d^3x^4 + 2ab^2c^3 - 6a^2bc^2d + 6a^3cd^2 + 2(4ab^2d^3 - (b^3cd^2 - ab^2d^3)n)x^3 + (ab^2c^3 - 2a^2bc^2d + a^3cd^2)n^2 + (b^3c^3 - 3ab^2c^2d + 3a^2b^2cd^2 - a^3d^3)n)x}{6b^3c^3 - 18a^2b^2c^2d + 18a^2b^2cd^2 - 6a^3d^3 + (b^3c^3 - 3a^2b^2c^2d + 3a^2b^2cd^2 - a^3d^3)n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-4-n)*(d*x+c)^n,x, algorithm="fricas")

[Out] -(2*b^3*d^3*x^4 + 2*a*b^2*c^3 - 6*a^2*b*c^2*d + 6*a^3*c*d^2 + 2*(4*a*b^2*d^3 - (b^3*c*d^2 - a*b^2*d^3)*n)*x^3 + (a*b^2*c^3 - 2*a^2*b*c^2*d + a^3*c*d^2)*n^2 + (12*a^2*b*d^3 + (b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*n^2 + (b^3*c^2*d - 8*a*b^2*c*d^2 + 7*a^2*b*d^3)*n)*x^2 + (3*a*b^2*c^3 - 8*a^2*b*c^2*d + 5*a^3*c*d^2)*n + (2*b^3*c^3 - 6*a*b^2*c^2*d + 6*a^2*b*c*d^2 + 6*a^3*d^3 + (b^3*c^3 - a*b^2*c^2*d - a^2*b*c*d^2 + a^3*d^3)*n^2 + (3*b^3*c^3 - 7*a*b^2*c^2*d - a^2*b*c*d^2 + 5*a^3*d^3)*n)*x)*(b*x + a)^(-n - 4)*(d*x + c)^n/(6*b^3*c^3 - 18*a*b^2*c^2*d + 18*a^2*b^2*c*d^2 - 6*a^3*d^3 + (b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b^2*c*d^2 - a^3*d^3)*n^2 + 11*(b^3*c^3 - 3*a*b^2*c^2*d + 3*a^2*b^2*c*d^2 - a^3*d^3)*n)


```
[Out] (x*(c + d*x)^n*(6*a^3*d^3 + 2*b^3*c^3 + 5*a^3*d^3*n + 3*b^3*c^3*n + a^3*d^3
*n^2 + b^3*c^3*n^2 - 6*a*b^2*c^2*d + 6*a^2*b*c*d^2 - 7*a*b^2*c^2*d*n - a^2*
b*c*d^2*n - a*b^2*c^2*d*n^2 - a^2*b*c*d^2*n^2))/((a*d - b*c)^3*(a + b*x)^(n
+ 4)*(11*n + 6*n^2 + n^3 + 6)) + (a*c*(c + d*x)^n*(6*a^2*d^2 + 2*b^2*c^2 +
5*a^2*d^2*n + 3*b^2*c^2*n + a^2*d^2*n^2 + b^2*c^2*n^2 - 6*a*b*c*d - 8*a*b*
c*d*n - 2*a*b*c*d*n^2))/((a*d - b*c)^3*(a + b*x)^(n + 4)*(11*n + 6*n^2 + n^
3 + 6)) + (2*b^3*d^3*x^4*(c + d*x)^n)/((a*d - b*c)^3*(a + b*x)^(n + 4)*(11*
n + 6*n^2 + n^3 + 6)) + (b*d*x^2*(c + d*x)^n*(12*a^2*d^2 + 7*a^2*d^2*n + b^
2*c^2*n + a^2*d^2*n^2 + b^2*c^2*n^2 - 8*a*b*c*d*n - 2*a*b*c*d*n^2))/((a*d -
b*c)^3*(a + b*x)^(n + 4)*(11*n + 6*n^2 + n^3 + 6)) + (2*b^2*d^2*x^3*(c + d
*x)^n*(4*a*d + a*d*n - b*c*n))/((a*d - b*c)^3*(a + b*x)^(n + 4)*(11*n + 6*n
^2 + n^3 + 6))
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(-4-n)*(d*x+c)**n,x)
```

```
[Out] Timed out
```

3.1871 $\int (a + bx)^{-5-n} (c + dx)^n dx$

Optimal. Leaf size=186

$$\frac{6d^3(a+bx)^{-n-1}(c+dx)^{n+1}}{(n+1)(n+2)(n+3)(n+4)(bc-ad)^4} - \frac{6d^2(a+bx)^{-n-2}(c+dx)^{n+1}}{(n+2)(n+3)(n+4)(bc-ad)^3} - \frac{(a+bx)^{-n-4}(c+dx)^{n+1}}{(n+4)(bc-ad)} + \frac{3d(a+bx)^{-n}}{(n+3)(n+4)}$$

[Out] $-(b*x+a)^{-4-n}*(d*x+c)^{1+n}/(-a*d+b*c)/(4+n)+3*d*(b*x+a)^{-3-n}*(d*x+c)^{1+n}/(-a*d+b*c)^2/(3+n)/(4+n)-6*d^2*(b*x+a)^{-2-n}*(d*x+c)^{1+n}/(-a*d+b*c)^3/(2+n)/(3+n)/(4+n)+6*d^3*(b*x+a)^{-1-n}*(d*x+c)^{1+n}/(-a*d+b*c)^4/(1+n)/(2+n)/(3+n)/(4+n)$

Rubi [A] time = 0.09, antiderivative size = 186, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$-\frac{6d^2(a+bx)^{-n-2}(c+dx)^{n+1}}{(n+2)(n+3)(n+4)(bc-ad)^3} + \frac{6d^3(a+bx)^{-n-1}(c+dx)^{n+1}}{(n+1)(n+2)(n+3)(n+4)(bc-ad)^4} - \frac{(a+bx)^{-n-4}(c+dx)^{n+1}}{(n+4)(bc-ad)} + \frac{3d(a+bx)^{-n}}{(n+3)(n+4)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-5 - n)*(c + d*x)^n, x]

[Out] $-(((a + b*x)^{-4 - n}*(c + d*x)^{1 + n})/((b*c - a*d)*(4 + n))) + (3*d*(a + b*x)^{-3 - n}*(c + d*x)^{1 + n})/((b*c - a*d)^2*(3 + n)*(4 + n)) - (6*d^2*(a + b*x)^{-2 - n}*(c + d*x)^{1 + n})/((b*c - a*d)^3*(2 + n)*(3 + n)*(4 + n)) + (6*d^3*(a + b*x)^{-1 - n}*(c + d*x)^{1 + n})/((b*c - a*d)^4*(1 + n)*(2 + n)*(3 + n)*(4 + n))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\begin{aligned}
\int (a+bx)^{-5-n}(c+dx)^n dx &= -\frac{(a+bx)^{-4-n}(c+dx)^{1+n}}{(bc-ad)(4+n)} - \frac{(3d) \int (a+bx)^{-4-n}(c+dx)^n dx}{(bc-ad)(4+n)} \\
&= -\frac{(a+bx)^{-4-n}(c+dx)^{1+n}}{(bc-ad)(4+n)} + \frac{3d(a+bx)^{-3-n}(c+dx)^{1+n}}{(bc-ad)^2(3+n)(4+n)} + \frac{(6d^2) \int (a+bx)^{-3-n}(c+dx)^n dx}{(bc-ad)^2(3+n)(4+n)} \\
&= -\frac{(a+bx)^{-4-n}(c+dx)^{1+n}}{(bc-ad)(4+n)} + \frac{3d(a+bx)^{-3-n}(c+dx)^{1+n}}{(bc-ad)^2(3+n)(4+n)} - \frac{6d^2(a+bx)^{-2-n}(c+dx)^n}{(bc-ad)^3(2+n)(3+n)(4+n)} \\
&= -\frac{(a+bx)^{-4-n}(c+dx)^{1+n}}{(bc-ad)(4+n)} + \frac{3d(a+bx)^{-3-n}(c+dx)^{1+n}}{(bc-ad)^2(3+n)(4+n)} - \frac{6d^2(a+bx)^{-2-n}(c+dx)^n}{(bc-ad)^3(2+n)(3+n)(4+n)}
\end{aligned}$$

Mathematica [A] time = 0.12, size = 195, normalized size = 1.05

$$\frac{(a+bx)^{-n-4}(c+dx)^{n+1} (a^3 d^3 (n^3 + 9n^2 + 26n + 24) - 3a^2 b d^2 (n^2 + 7n + 12) (cn + c - dx) + 3ab^2 d(n+4) (c^2 (n+1)(n+2)(n+3) - 3c^2 d(2+3n+n^2)x + 6c^2 d^2(1+n)x^2 - 6d^3 x^3))}{(n+1)(n+2)(n+3)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-5 - n)*(c + d*x)^n, x]

[Out] ((a + b*x)^(-4 - n)*(c + d*x)^(1 + n)*(a^3*d^3*(24 + 26*n + 9*n^2 + n^3) - 3*a^2*b*d^2*(12 + 7*n + n^2)*(c + c*n - d*x) + 3*a*b^2*d*(4 + n)*(c^2*(2 + 3*n + n^2) - 2*c*d*(1 + n)*x + 2*d^2*x^2) - b^3*(c^3*(6 + 11*n + 6*n^2 + n^3) - 3*c^2*d*(2 + 3*n + n^2)*x + 6*c*d^2*(1 + n)*x^2 - 6*d^3*x^3)))/((b*c - a*d)^4*(1 + n)*(2 + n)*(3 + n)*(4 + n))

fricas [B] time = 0.98, size = 959, normalized size = 5.16

$$\frac{(6b^4d^4x^5 - 6ab^3c^4 + 24a^2b^2c^3d - 36a^3bc^2d^2 + 24a^4cd^3 + 6(5ab^3d^4 - (b^4cd^3 - ab^3d^4)n)x^4 - (ab^3c^4 - 3a^2b^2c^3d)x^3 + (6a^3b^2c^3d^2 - 6a^2b^3c^2d^2 + 24a^3b^2c^2d^2 - 36a^4b^2c^2d^2 + 24a^5b^2c^2d^2)x^2 - (6a^4b^3c^2d^2 - 6a^5b^3c^2d^2)x + 6a^6b^3c^2d^2)}{(b^4cd^3 - ab^3d^4)n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-5-n)*(d*x+c)^n, x, algorithm="fricas")

[Out] (6*b^4*d^4*x^5 - 6*a*b^3*c^4 + 24*a^2*b^2*c^3*d - 36*a^3*b*c^2*d^2 + 24*a^4*c*d^3 + 6*(5*a*b^3*d^4 - (b^4*c*d^3 - a*b^3*d^4)*n)*x^4 - (a*b^3*c^4 - 3*a^2*b^2*c^3*d + 3*a^3*b*c^2*d^2 - a^4*c*d^3)*n^3 + 3*(20*a^2*b^2*d^4 + (b^4*c^2*d^2 - 2*a*b^3*c*d^3 + a^2*b^2*d^4)*n^2 + (b^4*c^2*d^2 - 10*a*b^3*c*d^3 + 9*a^2*b^2*d^4)*n)*x^3 - 3*(2*a*b^3*c^4 - 7*a^2*b^2*c^3*d + 8*a^3*b*c^2*d^2 - 3*a^4*c*d^3)*n^2 + (60*a^3*b*d^4 - (b^4*c^3*d - 3*a*b^3*c^2*d^2 + 3*a^2*b^2*d^4)*n)*x^2 - (60*a^4*b*d^4 - (b^4*c^3*d - 3*a*b^3*c^2*d^2 + 3*a^2*b^2*d^4)*n)*x + 60*a^5*b*d^4 - (b^4*c^3*d - 3*a*b^3*c^2*d^2 + 3*a^2*b^2*d^4)*n

```

*b^2*c*d^3 - a^3*b*d^4)*n^3 - 3*(b^4*c^3*d - 6*a*b^3*c^2*d^2 + 9*a^2*b^2*c*
d^3 - 4*a^3*b*d^4)*n^2 - (2*b^4*c^3*d - 15*a*b^3*c^2*d^2 + 60*a^2*b^2*c*d^3
- 47*a^3*b*d^4)*n)*x^2 - (11*a*b^3*c^4 - 42*a^2*b^2*c^3*d + 57*a^3*b*c^2*d
^2 - 26*a^4*c*d^3)*n - (6*b^4*c^4 - 24*a*b^3*c^3*d + 36*a^2*b^2*c^2*d^2 - 2
4*a^3*b*c*d^3 - 24*a^4*d^4 + (b^4*c^4 - 2*a*b^3*c^3*d + 2*a^3*b*c*d^3 - a^4
*d^4)*n^3 + 3*(2*b^4*c^4 - 6*a*b^3*c^3*d + 3*a^2*b^2*c^2*d^2 + 4*a^3*b*c*d^
3 - 3*a^4*d^4)*n^2 + (11*b^4*c^4 - 40*a*b^3*c^3*d + 45*a^2*b^2*c^2*d^2 + 10
*a^3*b*c*d^3 - 26*a^4*d^4)*n)*x)*(b*x + a)^(-n - 5)*(d*x + c)^n/(24*b^4*c^4
- 96*a*b^3*c^3*d + 144*a^2*b^2*c^2*d^2 - 96*a^3*b*c*d^3 + 24*a^4*d^4 + (b^
4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*n^4 +
10*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4*d^4)*
n^3 + 35*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3 + a^4
*d^4)*n^2 + 50*(b^4*c^4 - 4*a*b^3*c^3*d + 6*a^2*b^2*c^2*d^2 - 4*a^3*b*c*d^3
+ a^4*d^4)*n)

```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n-5}(dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)^(-5-n)*(d*x+c)^n,x, algorithm="giac")
```

```
[Out] integrate((b*x + a)^(-n - 5)*(d*x + c)^n, x)
```

maple [B] time = 0.01, size = 661, normalized size = 3.55

$$\frac{(a^3 d^3 n^3 - 3a^2 b c d^2 n^3 + 3a^2 b d^3 n^2 x + 3a b^2 c^2 d n^3 - 6a b^2 c d^2 n^2 x + 6a b^2 d^3 n x^2 - b^3 c^3 n^3 + 3b^3 c^2 d n^2 x - 6b^3 c d^2 n x^2 + 3b^3 d^3 n x^3 - 3b^3 c^2 d^2 n^2 x^2 + 6b^3 c d^3 n x^3 - 3b^3 d^3 n^2 x^2 - 24a^2 b^2 c d^2 n^2 + 21a^2 b^2 d^3 n^2 x + 21a^2 b^2 c^2 d^2 n^2 - 30a^2 b^2 c d^2 n^2 x + 24a^2 b^2 d^3 n^2 x^2 - 6b^3 c^3 n^2 + 9b^3 c^2 d n^2 x - 6b^3 c d^2 x^2 + 26a^3 d^3 n - 57a^2 b^2 c d^2 n + 36a^2 b^2 d^3 n x + 42a^2 b^2 c^2 d n - 24a^2 b^2 c d^2 x - 11b^3 c^3 n + 6b^3 c^2 d x + 24a^3 d^3 - 36a^2 b^2 c d^2 + 24a^2 b^2 c^2 d - 6b^3 c^3)/(a^4 d^4 n^4 - 4a^3 b c d^3 n^4 + 6a^2 b^2 c^2 d^2 n^4 - 4a b^3 c^3 d n^4 + b^4 c^4 n^4 + 10a^4 d^4 n^3 - 40a^3 b c d^3 n^3 + 60a^2 b^2 c^2 d^2 n^3 - 40a b^3 c^3 d n^3 + 10b^4 c^4 n^3 + 35a^4 d^4 n^2 - 140a^3 b^2 c d^3 n^2 + 210a^2 b^2 c^2 d^2 n^2 - 140a b^3 c^3 d n^2 + 35b^4 c^4 n^2 + 50a^4 d^4 n - 200a^3 b^2 c d^3 n + 300a^2 b^2 c^2 d^2 n - 200a b^3 c^3 d n + 50b^4 c^4 n)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((b*x+a)^(-5-n)*(d*x+c)^n,x)
```

```
[Out] (b*x+a)^(-4-n)*(d*x+c)^(n+1)*(a^3*d^3*n^3-3*a^2*b*c*d^2*n^3+3*a^2*b*d^3*n^2
*x+3*a*b^2*c^2*d*n^3-6*a*b^2*c*d^2*n^2*x+6*a*b^2*d^3*n*x^2-b^3*c^3*n^3+3*b^
3*c^2*d*n^2*x-6*b^3*c*d^2*n*x^2+6*b^3*d^3*x^3+9*a^3*d^3*n^2-24*a^2*b*c*d^2*
n^2+21*a^2*b*d^3*n*x+21*a*b^2*c^2*d*n^2-30*a*b^2*c*d^2*n*x+24*a*b^2*d^3*x^2
-6*b^3*c^3*n^2+9*b^3*c^2*d*n*x-6*b^3*c*d^2*x^2+26*a^3*d^3*n-57*a^2*b*c*d^2*
n+36*a^2*b*d^3*x+42*a*b^2*c^2*d*n-24*a*b^2*c*d^2*x-11*b^3*c^3*n+6*b^3*c^2*d
*x+24*a^3*d^3-36*a^2*b*c*d^2+24*a*b^2*c^2*d-6*b^3*c^3)/(a^4*d^4*n^4-4*a^3*b
*c*d^3*n^4+6*a^2*b^2*c^2*d^2*n^4-4*a*b^3*c^3*d*n^4+b^4*c^4*n^4+10*a^4*d^4*n
^3-40*a^3*b*c*d^3*n^3+60*a^2*b^2*c^2*d^2*n^3-40*a*b^3*c^3*d*n^3+10*b^4*c^4*
n^3+35*a^4*d^4*n^2-140*a^3*b*c*d^3*n^2+210*a^2*b^2*c^2*d^2*n^2-140*a*b^3*c^
3*d*n^2+35*b^4*c^4*n^2+50*a^4*d^4*n-200*a^3*b^2*c*d^3*n+300*a^2*b^2*c^2*d^2*n
-200*a b^3 c^3 d n + 50 b^4 c^4 n)

```

$-200*a*b^3*c^3*d*n+50*b^4*c^4*n+24*a^4*d^4-96*a^3*b*c*d^3+144*a^2*b^2*c^2*d^2-96*a*b^3*c^3*d+24*b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-n-5}(dx + c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-5-n)*(d*x+c)^n,x, algorithm="maxima")

[Out] integrate((b*x + a)^(-n - 5)*(d*x + c)^n, x)

mupad [B] time = 1.64, size = 944, normalized size = 5.08

$$\frac{ac(c+dx)^n (a^3 d^3 n^3 + 9 a^3 d^3 n^2 + 26 a^3 d^3 n + 24 a^3 d^3 - 3 a^2 b c d^2 n^3 - 24 a^2 b c d^2 n^2 - 57 a^2 b c d^2 n - 36 a^2 b c d^2 + 42 a^2 b c d^2 n + 21 a^2 b c d^2 n^2 - 24 a^2 b c d^2 n^3)}{(ad - bc)^4 (a + bx)^{n+5} (n^4 + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^n/(a + b*x)^(n + 5),x)

[Out] $(a*c*(c + d*x)^n*(24*a^3*d^3 - 6*b^3*c^3 + 26*a^3*d^3*n - 11*b^3*c^3*n + 9*a^3*d^3*n^2 - 6*b^3*c^3*n^2 + a^3*d^3*n^3 - b^3*c^3*n^3 + 24*a*b^2*c^2*d - 36*a^2*b*c*d^2 + 42*a*b^2*c^2*d*n - 57*a^2*b*c*d^2*n + 21*a*b^2*c^2*d*n^2 - 24*a^2*b*c*d^2*n^2 + 3*a*b^2*c^2*d*n^3 - 3*a^2*b*c*d^2*n^3))/((a*d - b*c)^4*(a + b*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) - (x*(c + d*x)^n*(6*b^4*c^4 - 24*a^4*d^4 - 26*a^4*d^4*n + 11*b^4*c^4*n - 9*a^4*d^4*n^2 + 6*b^4*c^4*n^2 - a^4*d^4*n^3 + b^4*c^4*n^3 + 36*a^2*b^2*c^2*d^2 - 24*a*b^3*c^3*d - 24*a^3*b*c*d^3 - 40*a*b^3*c^3*d*n + 10*a^3*b*c*d^3*n + 9*a^2*b^2*c^2*d^2*n^2 - 18*a*b^3*c^3*d*n^2 + 12*a^3*b*c*d^3*n^2 - 2*a*b^3*c^3*d*n^3 + 2*a^3*b*c*d^3*n^3 + 45*a^2*b^2*c^2*d^2*n))/((a*d - b*c)^4*(a + b*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (6*b^4*d^4*x^5*(c + d*x)^n)/((a*d - b*c)^4*(a + b*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (3*b^2*d^2*x^3*(c + d*x)^n*(20*a^2*d^2 + 9*a^2*d^2*n + b^2*c^2*n + a^2*d^2*n^2 + b^2*c^2*n^2 - 10*a*b*c*d*n - 2*a*b*c*d*n^2))/((a*d - b*c)^4*(a + b*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (6*b^3*d^3*x^4*(c + d*x)^n*(5*a*d + a*d*n - b*c*n))/((a*d - b*c)^4*(a + b*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (b*d*x^2*(c + d*x)^n*(60*a^3*d^3 + 47*a^3*d^3*n - 2*b^3*c^3*n + 12*a^3*d^3*n^2 - 3*b^3*c^3*n^2 + a^3*d^3*n^3 - b^3*c^3*n^3 + 15*a*b^2*c^2*d*n - 60*a^2*b*c*d^2*n + 18*a*b^2*c^2*d*n^2 - 27*a^2*b*c*d^2*n^2 + 3*a*b^2*c^2*d*n^3 - 3*a^2*b*c*d^2*n^3))/((a*d - b*c)^4*(a + b*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24))$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**(-5-n)*(d*x+c)**n,x)
```

```
[Out] Timed out
```

3.1872 $\int (a + bx)^n (c + dx)^{-n} dx$

Optimal. Leaf size=72

$$\frac{(a + bx)^{n+1} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n+1; n+2; -\frac{d(a+bx)}{bc-ad} \right)}{b(n+1)}$$

[Out] $(b*x+a)^{(1+n)}*(b*(d*x+c)/(-a*d+b*c))^{-n}$ hypergeom([n, 1+n], [2+n], $-d*(b*x+a)/(-a*d+b*c)$)/b/(1+n)/((d*x+c)^n)

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {70, 69}

$$\frac{(a + bx)^{n+1} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n+1; n+2; -\frac{d(a+bx)}{bc-ad} \right)}{b(n+1)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n/(c + d*x)^n, x]

[Out] $((a + b*x)^{(1 + n)}*((b*(c + d*x))/(b*c - a*d))^{-n}$ Hypergeometric2F1[n, 1 + n, 2 + n, $-((d*(a + b*x))/(b*c - a*d))$]/(b*(1 + n)*(c + d*x)^n)

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, $-((d*(a + b*x))/(b*c - a*d))$]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Dist[(c + d*x)^FracPart[n]/(b/(b*c - a*d))^IntPart[n]*((b*(c + d*x))/(b*c - a*d))^FracPart[n], Int[(a + b*x)^m*Simp[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int (a + bx)^n (c + dx)^{-n} dx = \left((c + dx)^{-n} \left(\frac{b(c + dx)}{bc - ad} \right)^n \right) \int (a + bx)^n \left(\frac{bc}{bc - ad} + \frac{bdx}{bc - ad} \right)^{-n} dx$$

$$= \frac{(a + bx)^{1+n} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, 1 + n; 2 + n; -\frac{d(a+bx)}{bc-ad} \right)}{b(1 + n)}$$

Mathematica [A] time = 0.02, size = 71, normalized size = 0.99

$$\frac{(a + bx)^{n+1} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(n, n + 1; n + 2; \frac{d(a+bx)}{ad-bc} \right)}{b(n + 1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n/(c + d*x)^n,x]

[Out] ((a + b*x)^(1 + n)*((b*(c + d*x))/(b*c - a*d))^n*Hypergeometric2F1[n, 1 + n, 2 + n, (d*(a + b*x))/(-b*c) + a*d])/(b*(1 + n)*(c + d*x)^n)

fricas [F] time = 0.98, size = 0, normalized size = 0.00

$$\text{integral} \left(\frac{(bx + a)^n}{(dx + c)^n}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/((d*x+c)^n),x, algorithm="fricas")

[Out] integral((b*x + a)^n/(d*x + c)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n/((d*x+c)^n),x, algorithm="giac")

[Out] integrate((b*x + a)^n/(d*x + c)^n, x)

maple [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n (dx + c)^{-n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^n/((d*x+c)^n),x)`

[Out] `int((b*x+a)^n/((d*x+c)^n),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^n}{(dx + c)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^n/((d*x+c)^n),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^n/(d*x + c)^n, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^n}{(c + dx)^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^n/(c + d*x)^n,x)`

[Out] `int((a + b*x)^n/(c + d*x)^n, x)`

sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**n/((d*x+c)**n),x)`

[Out] Exception raised: HeuristicGCDFailed

3.1873 $\int (a + bx)^n (c + dx)^{-1-n} dx$

Optimal. Leaf size=75

$$\frac{(a + bx)^n (c + dx)^{-n} \left(-\frac{d(a+bx)}{bc-ad}\right)^{-n} {}_2F_1\left(-n, -n; 1 - n; \frac{b(c+dx)}{bc-ad}\right)}{dn}$$

[Out] $-(b*x+a)^n \text{hypergeom}([-n, -n], [1-n], b*(d*x+c)/(-a*d+b*c))/d/n/((-d*(b*x+a)/(-a*d+b*c))^n)/((d*x+c)^n)$

Rubi [A] time = 0.03, antiderivative size = 75, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {70, 69}

$$\frac{(a + bx)^n (c + dx)^{-n} \left(-\frac{d(a+bx)}{bc-ad}\right)^{-n} {}_2F_1\left(-n, -n; 1 - n; \frac{b(c+dx)}{bc-ad}\right)}{dn}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^n*(c + d*x)^{-1 - n}, x]$

[Out] $-(((a + b*x)^n \text{Hypergeometric2F1}[-n, -n, 1 - n, (b*(c + d*x))/(b*c - a*d)])/(d*n*(-((d*(a + b*x))/(b*c - a*d)))^n*(c + d*x)^n)$

Rule 69

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{m+1} \text{Hypergeometric2F1}[-n, m+1, m+2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m+1)*(b/(b*c - a*d))^n), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& \text{GtQ}[b/(b*c - a*d), 0] \&\& (\text{RationalQ}[m] \mid\mid !(\text{RationalQ}[n] \&\& \text{GtQ}[-(d/(b*c - a*d)), 0]))$

Rule 70

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x_Symbol] \rightarrow \text{Dist}[(c + d*x)^{\text{FracPart}[n]}/(b/(b*c - a*d))^{\text{IntPart}[n]}*((b*(c + d*x))/(b*c - a*d))^{\text{FracPart}[n]}, \text{Int}[(a + b*x)^m \text{Simp}[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \&\& \text{NeQ}[b*c - a*d, 0] \&\& !\text{IntegerQ}[m] \&\& !\text{IntegerQ}[n] \&\& (\text{RationalQ}[m] \mid\mid !\text{SimplerQ}[n + 1, m + 1])$

Rubi steps

$$\int (a + bx)^n (c + dx)^{-1-n} dx = \left((a + bx)^n \left(\frac{d(a + bx)}{-bc + ad} \right)^{-n} \right) \int (c + dx)^{-1-n} \left(-\frac{ad}{bc - ad} - \frac{bdx}{bc - ad} \right)^n dx$$

$$= -\frac{(a + bx)^n \left(-\frac{d(a+bx)}{bc-ad} \right)^{-n} (c + dx)^{-n} {}_2F_1 \left(-n, -n; 1 - n; \frac{b(c+dx)}{bc-ad} \right)}{dn}$$

Mathematica [A] time = 0.03, size = 74, normalized size = 0.99

$$-\frac{(a + bx)^n (c + dx)^{-n} \left(\frac{d(a+bx)}{ad-bc} \right)^{-n} {}_2F_1 \left(-n, -n; 1 - n; \frac{b(c+dx)}{bc-ad} \right)}{dn}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n*(c + d*x)^(-1 - n), x]

[Out] -(((a + b*x)^n*Hypergeometric2F1[-n, -n, 1 - n, (b*(c + d*x))/(b*c - a*d)])) / (d*n*((d*(a + b*x))/(-b*c) + a*d))^n*(c + d*x)^n)

fricas [F] time = 0.58, size = 0, normalized size = 0.00

$$\text{integral} \left((bx + a)^n (dx + c)^{-n-1}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(d*x+c)^(-1-n), x, algorithm="fricas")

[Out] integral((b*x + a)^n*(d*x + c)^(-n - 1), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n (dx + c)^{-n-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(d*x+c)^(-1-n), x, algorithm="giac")

[Out] integrate((b*x + a)^n*(d*x + c)^(-n - 1), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^n (dx + c)^{-n-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^n*(d*x+c)^(-n-1),x)`

[Out] `int((b*x+a)^n*(d*x+c)^(-n-1),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n (dx + c)^{-n-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^n*(d*x+c)^(-1-n),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^n*(d*x + c)^(-n - 1), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^n}{(c + dx)^{n+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^n/(c + d*x)^(n + 1),x)`

[Out] `int((a + b*x)^n/(c + d*x)^(n + 1), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**n*(d*x+c)**(-1-n),x)`

[Out] Timed out

$$3.1874 \quad \int (a + bx)^n (c + dx)^{-2-n} dx$$

Optimal. Leaf size=36

$$\frac{(a + bx)^{n+1}(c + dx)^{-n-1}}{(n + 1)(bc - ad)}$$

[Out] (b*x+a)^(1+n)*(d*x+c)^(-1-n)/(-a*d+b*c)/(1+n)

Rubi [A] time = 0.00, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {37}

$$\frac{(a + bx)^{n+1}(c + dx)^{-n-1}}{(n + 1)(bc - ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n*(c + d*x)^(-2 - n), x]

[Out] ((a + b*x)^(1 + n)*(c + d*x)^(-1 - n))/((b*c - a*d)*(1 + n))

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp [((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rubi steps

$$\int (a + bx)^n (c + dx)^{-2-n} dx = \frac{(a + bx)^{1+n}(c + dx)^{-1-n}}{(bc - ad)(1 + n)}$$

Mathematica [A] time = 0.01, size = 36, normalized size = 1.00

$$\frac{(a + bx)^{n+1}(c + dx)^{-n-1}}{(n + 1)(bc - ad)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n*(c + d*x)^(-2 - n), x]

[Out] ((a + b*x)^(1 + n)*(c + d*x)^(-1 - n))/((b*c - a*d)*(1 + n))

fricas [A] time = 0.84, size = 58, normalized size = 1.61

$$\frac{(bdx^2 + ac + (bc + ad)x)(bx + a)^n(dx + c)^{-n-2}}{bc - ad + (bc - ad)n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(d*x+c)^(-2-n),x, algorithm="fricas")

[Out] (b*d*x^2 + a*c + (b*c + a*d)*x)*(b*x + a)^n*(d*x + c)^(-n - 2)/(b*c - a*d + (b*c - a*d)*n)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n(dx + c)^{-n-2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(d*x+c)^(-2-n),x, algorithm="giac")

[Out] integrate((b*x + a)^n*(d*x + c)^(-n - 2), x)

maple [A] time = 0.00, size = 42, normalized size = 1.17

$$\frac{(bx + a)^{n+1}(dx + c)^{-n-1}}{adn - bcn + ad - bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n*(d*x+c)^(-n-2),x)

[Out] -(b*x+a)^(n+1)*(d*x+c)^(-n-1)/(a*d*n-b*c*n+a*d-b*c)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n(dx + c)^{-n-2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(d*x+c)^(-2-n),x, algorithm="maxima")

[Out] integrate((b*x + a)^n*(d*x + c)^(-n - 2), x)

mupad [B] time = 0.56, size = 98, normalized size = 2.72

$$\frac{\frac{ac(a+bx)^n}{(a-d-bc)(n+1)} + \frac{x(ad+bc)(a+bx)^n}{(a-d-bc)(n+1)} + \frac{bdx^2(a+bx)^n}{(a-d-bc)(n+1)}}{(c+dx)^{n+2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^n/(c + d*x)^(n + 2),x)`

[Out] $-\frac{(a*c*(a + b*x)^n)/((a*d - b*c)*(n + 1)) + (x*(a*d + b*c)*(a + b*x)^n)/((a*d - b*c)*(n + 1)) + (b*d*x^2*(a + b*x)^n)/((a*d - b*c)*(n + 1))}{(c + d*x)^{n + 2}}$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**n*(d*x+c)**(-2-n),x)`

[Out] Timed out

3.1875 $\int (a + bx)^n (c + dx)^{-3-n} dx$

Optimal. Leaf size=79

$$\frac{(a + bx)^{n+1}(c + dx)^{-n-2}}{(n + 2)(bc - ad)} + \frac{b(a + bx)^{n+1}(c + dx)^{-n-1}}{(n + 1)(n + 2)(bc - ad)^2}$$

[Out] $(b*x+a)^{(1+n)}*(d*x+c)^{(-2-n)/(-a*d+b*c)/(2+n)+b*(b*x+a)^{(1+n)}*(d*x+c)^{(-1-n)/(-a*d+b*c)^2/(1+n)/(2+n)}$

Rubi [A] time = 0.02, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{(a + bx)^{n+1}(c + dx)^{-n-2}}{(n + 2)(bc - ad)} + \frac{b(a + bx)^{n+1}(c + dx)^{-n-1}}{(n + 1)(n + 2)(bc - ad)^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^n*(c + d*x)^(-3 - n), x]

[Out] $((a + b*x)^{(1 + n)}*(c + d*x)^{(-2 - n)})/((b*c - a*d)*(2 + n)) + (b*(a + b*x)^{(1 + n)}*(c + d*x)^{(-1 - n)})/((b*c - a*d)^2*(1 + n)*(2 + n))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 $((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] /;$ FreeQ[{
 a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -
 1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[
 $((a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)})/((b*c - a*d)*(m + 1)), x] -$ Dist[(d*S
 implify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c
 + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && I
 LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] &&
 (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimpler
 Q[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int (a + bx)^n (c + dx)^{-3-n} dx = \frac{(a + bx)^{1+n} (c + dx)^{-2-n}}{(bc - ad)(2 + n)} + \frac{b \int (a + bx)^n (c + dx)^{-2-n} dx}{(bc - ad)(2 + n)}$$

$$= \frac{(a + bx)^{1+n} (c + dx)^{-2-n}}{(bc - ad)(2 + n)} + \frac{b(a + bx)^{1+n} (c + dx)^{-1-n}}{(bc - ad)^2 (1 + n)(2 + n)}$$

Mathematica [A] time = 0.04, size = 59, normalized size = 0.75

$$\frac{(a + bx)^{n+1} (c + dx)^{-n-2} (-ad(n + 1) + bc(n + 2) + bdx)}{(n + 1)(n + 2)(bc - ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n*(c + d*x)^(-3 - n), x]

[Out] ((a + b*x)^(1 + n)*(c + d*x)^(-2 - n)*(-a*d*(1 + n)) + b*c*(2 + n) + b*d*x)/((b*c - a*d)^2*(1 + n)*(2 + n))

fricas [B] time = 0.56, size = 205, normalized size = 2.59

$$\frac{(b^2 d^2 x^3 + 2 abc^2 - a^2 cd + (3 b^2 cd + (b^2 cd - abd^2)n)x^2 + (abc^2 - a^2 cd)n + (2 b^2 c^2 + 2 abcd - a^2 d^2 + (b^2 c^2 - a^2 d^2)n)}{2 b^2 c^2 - 4 abcd + 2 a^2 d^2 + (b^2 c^2 - 2 abcd + a^2 d^2)n^2 + 3 (b^2 c^2 - 2 abcd + a^2 d^2)n}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(d*x+c)^(-3-n), x, algorithm="fricas")

[Out] (b^2*d^2*x^3 + 2*a*b*c^2 - a^2*c*d + (3*b^2*c*d + (b^2*c*d - a*b*d^2)*n)*x^2 + (a*b*c^2 - a^2*c*d)*n + (2*b^2*c^2 + 2*a*b*c*d - a^2*d^2 + (b^2*c^2 - a^2*d^2)*n)*x*(b*x + a)^n*(d*x + c)^(-n - 3)/(2*b^2*c^2 - 4*a*b*c*d + 2*a^2*d^2 + (b^2*c^2 - 2*a*b*c*d + a^2*d^2)*n^2 + 3*(b^2*c^2 - 2*a*b*c*d + a^2*d^2)*n)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n (dx + c)^{-n-3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(d*x+c)^(-3-n), x, algorithm="giac")

[Out] integrate((b*x + a)^n*(d*x + c)^(-n - 3), x)

maple [A] time = 0.00, size = 124, normalized size = 1.57

$$\frac{(adn - bcn - bdx + ad - 2bc)(bx + a)^{n+1}(dx + c)^{-n-2}}{a^2d^2n^2 - 2abcdn^2 + b^2c^2n^2 + 3a^2d^2n - 6abcdn + 3b^2c^2n + 2a^2d^2 - 4abcd + 2b^2c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^n*(d*x+c)^(-n-3), x)

[Out] $-(b*x+a)^{(n+1)}*(d*x+c)^{(-n-2)}*(a*d*n-b*c*n-b*d*x+a*d-2*b*c)/(a^2*d^2*n^2-2*a*b*c*d*n^2+b^2*c^2*n^2+3*a^2*d^2*n-6*a*b*c*d*n+3*b^2*c^2*n+2*a^2*d^2-4*a*b*c*d+2*b^2*c^2)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n(dx + c)^{-n-3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(d*x+c)^(-3-n), x, algorithm="maxima")

[Out] integrate((b*x + a)^n*(d*x + c)^(-n - 3), x)

mupad [B] time = 0.74, size = 214, normalized size = 2.71

$$\frac{x(a+bx)^n(2b^2c^2-a^2d^2-a^2d^2n+b^2c^2n+2abcd)}{(a-dc)^2(n^2+3n+2)} - \frac{ac(a+bx)^n(ad-2bc+adn-bcn)}{(a-dc)^2(n^2+3n+2)} + \frac{b^2d^2x^3(a+bx)^n}{(a-dc)^2(n^2+3n+2)} + \frac{bdx^2(a+bx)^n(3bc-adn+bc)}{(a-dc)^2(n^2+3n+2)}$$

$$(c + dx)^{n+3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/(c + d*x)^(n + 3), x)

[Out] $((x*(a + b*x)^n*(2*b^2*c^2 - a^2*d^2 - a^2*d^2*n + b^2*c^2*n + 2*a*b*c*d))/((a*d - b*c)^2*(3*n + n^2 + 2)) - (a*c*(a + b*x)^n*(a*d - 2*b*c + a*d*n - b*c*n))/((a*d - b*c)^2*(3*n + n^2 + 2)) + (b^2*d^2*x^3*(a + b*x)^n)/((a*d - b*c)^2*(3*n + n^2 + 2)) + (b*d*x^2*(a + b*x)^n*(3*b*c - a*d*n + b*c*n))/((a*d - b*c)^2*(3*n + n^2 + 2)))/(c + d*x)^{(n + 3)}$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**n*(d*x+c)**(-3-n), x)

[Out] Timed out

3.1876 $\int (a + bx)^n (c + dx)^{-4-n} dx$

Optimal. Leaf size=130

$$\frac{2b^2(a + bx)^{n+1}(c + dx)^{-n-1}}{(n + 1)(n + 2)(n + 3)(bc - ad)^3} + \frac{(a + bx)^{n+1}(c + dx)^{-n-3}}{(n + 3)(bc - ad)} + \frac{2b(a + bx)^{n+1}(c + dx)^{-n-2}}{(n + 2)(n + 3)(bc - ad)^2}$$

[Out] $(b*x+a)^{(1+n)}*(d*x+c)^{(-3-n)/(-a*d+b*c)/(3+n)}+2*b*(b*x+a)^{(1+n)}*(d*x+c)^{(-2-n)/(-a*d+b*c)^2/(2+n)/(3+n)}+2*b^2*(b*x+a)^{(1+n)}*(d*x+c)^{(-1-n)/(-a*d+b*c)^3/(1+n)/(2+n)/(3+n)}$

Rubi [A] time = 0.04, antiderivative size = 130, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{2b^2(a + bx)^{n+1}(c + dx)^{-n-1}}{(n + 1)(n + 2)(n + 3)(bc - ad)^3} + \frac{(a + bx)^{n+1}(c + dx)^{-n-3}}{(n + 3)(bc - ad)} + \frac{2b(a + bx)^{n+1}(c + dx)^{-n-2}}{(n + 2)(n + 3)(bc - ad)^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^n*(c + d*x)^{-4 - n}, x]$

[Out] $((a + b*x)^{(1 + n)}*(c + d*x)^{(-3 - n)})/((b*c - a*d)*(3 + n)) + (2*b*(a + b*x)^{(1 + n)}*(c + d*x)^{(-2 - n)})/((b*c - a*d)^2*(2 + n)*(3 + n)) + (2*b^2*(a + b*x)^{(1 + n)}*(c + d*x)^{(-1 - n)})/((b*c - a*d)^3*(1 + n)*(2 + n)*(3 + n))$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{EqQ}[m + n + 2, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rule 45

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}/((b*c - a*d)*(m + 1)), x] - \text{Dist}[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), \text{Int}[(a + b*x)^{\text{Simplify}[m + 1]}*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{I} \ \text{LtQ}[\text{Simplify}[m + n + 2], 0] \ \&\& \ \text{NeQ}[m, -1] \ \&\& \ !(\text{LtQ}[m, -1] \ \&\& \ \text{LtQ}[n, -1] \ \&\& \ (\text{EqQ}[a, 0] \ || \ (\text{NeQ}[c, 0] \ \&\& \ \text{LtQ}[m - n, 0] \ \&\& \ \text{IntegerQ}[n]))) \ \&\& \ (\text{SumSimplerQ}[m, 1] \ || \ !\text{SumSimplerQ}[n, 1])$

Rubi steps

$$\begin{aligned} \int (a + bx)^n (c + dx)^{-4-n} dx &= \frac{(a + bx)^{1+n} (c + dx)^{-3-n}}{(bc - ad)(3 + n)} + \frac{(2b) \int (a + bx)^n (c + dx)^{-3-n} dx}{(bc - ad)(3 + n)} \\ &= \frac{(a + bx)^{1+n} (c + dx)^{-3-n}}{(bc - ad)(3 + n)} + \frac{2b(a + bx)^{1+n} (c + dx)^{-2-n}}{(bc - ad)^2(2 + n)(3 + n)} + \frac{(2b^2) \int (a + bx)^n (c + dx)^{-2-n} dx}{(bc - ad)^2(2 + n)(3 + n)} \\ &= \frac{(a + bx)^{1+n} (c + dx)^{-3-n}}{(bc - ad)(3 + n)} + \frac{2b(a + bx)^{1+n} (c + dx)^{-2-n}}{(bc - ad)^2(2 + n)(3 + n)} + \frac{2b^2(a + bx)^{1+n} (c + dx)^{-1-n}}{(bc - ad)^3(1 + n)(2 + n)(3 + n)} \end{aligned}$$

Mathematica [A] time = 0.09, size = 112, normalized size = 0.86

$$\frac{(a + bx)^{n+1} (c + dx)^{-n-3} (a^2 d^2 (n^2 + 3n + 2) - 2abd(n + 1)(c(n + 3) + dx) + b^2 (c^2 (n^2 + 5n + 6) + 2cd(n + 3)x + 2x^2))}{(n + 1)(n + 2)(n + 3)(bc - ad)^3}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^n*(c + d*x)^(-4 - n), x]

[Out] ((a + b*x)^(1 + n)*(c + d*x)^(-3 - n)*(a^2*d^2*(2 + 3*n + n^2) - 2*a*b*d*(1 + n)*(c*(3 + n) + d*x) + b^2*(c^2*(6 + 5*n + n^2) + 2*c*d*(3 + n)*x + 2*d^2*x^2)))/((b*c - a*d)^3*(1 + n)*(2 + n)*(3 + n))

fricas [B] time = 0.79, size = 507, normalized size = 3.90

$$\frac{(2b^3d^3x^4 + 6ab^2c^3 - 6a^2bc^2d + 2a^3cd^2 + 2(4b^3cd^2 + (b^3cd^2 - ab^2d^3)n)x^3 + (ab^2c^3 - 2a^2bc^2d + a^3cd^2)n^2 + (6b^3c^3 - 18ab^2c^3 + 18a^2b^2c^3 - 6a^3d^3 + (b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3)n^2 + 11(b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3)n))}{6b^3c^3 - 18ab^2c^3 + 18a^2b^2c^3 - 6a^3d^3 + (b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3)n^2 + 11(b^3c^3 - 3a^2b^2c^2d + 3a^2b^2c^2d - a^3d^3)n)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(d*x+c)^(-4-n), x, algorithm="fricas")

[Out] (2*b^3*d^3*x^4 + 6*a*b^2*c^3 - 6*a^2*b*c^2*d + 2*a^3*c*d^2 + 2*(4*b^3*c*d^2 + (b^3*c*d^2 - a*b^2*d^3)*n)*x^3 + (a*b^2*c^3 - 2*a^2*b*c^2*d + a^3*c*d^2)*n^2 + (12*b^3*c^2*d + (b^3*c^2*d - 2*a*b^2*c*d^2 + a^2*b*d^3)*n^2 + (7*b^3*c^2*d - 8*a*b^2*c*d^2 + a^2*b*d^3)*n)*x^2 + (5*a*b^2*c^3 - 8*a^2*b*c^2*d + 3*a^3*c*d^2)*n + (6*b^3*c^3 + 6*a*b^2*c^2*d - 6*a^2*b*c*d^2 + 2*a^3*d^3 + (b^3*c^3 - a*b^2*c^2*d - a^2*b*c*d^2 + a^3*d^3)*n^2 + (5*b^3*c^3 - a*b^2*c^2*d - 7*a^2*b*c*d^2 + 3*a^3*d^3)*n)*x*(b*x + a)^n*(d*x + c)^(-n - 4)/(6*b^3*c^3 - 18*a*b^2*c^2*d + 18*a^2*b*c*d^2 - 6*a^3*d^3 + (b^3*c^3 - 3*a^2*b^2*c^2*d + 3*a^2*b^2*c^2*d - a^3*d^3)*n^2 + 11*(b^3*c^3 - 3*a^2*b^2*c^2*d + 3*a^2*b^2*c^2*d - a^3*d^3)*n)


```
[Out] - (x*(a + b*x)^n*(2*a^3*d^3 + 6*b^3*c^3 + 3*a^3*d^3*n + 5*b^3*c^3*n + a^3*d
^3*n^2 + b^3*c^3*n^2 + 6*a*b^2*c^2*d - 6*a^2*b*c*d^2 - a*b^2*c^2*d*n - 7*a^
2*b*c*d^2*n - a*b^2*c^2*d*n^2 - a^2*b*c*d^2*n^2))/((a*d - b*c)^3*(c + d*x)^
(n + 4)*(11*n + 6*n^2 + n^3 + 6)) - (a*c*(a + b*x)^n*(2*a^2*d^2 + 6*b^2*c^2
+ 3*a^2*d^2*n + 5*b^2*c^2*n + a^2*d^2*n^2 + b^2*c^2*n^2 - 6*a*b*c*d - 8*a*
b*c*d*n - 2*a*b*c*d*n^2))/((a*d - b*c)^3*(c + d*x)^(n + 4)*(11*n + 6*n^2 +
n^3 + 6)) - (2*b^3*d^3*x^4*(a + b*x)^n)/((a*d - b*c)^3*(c + d*x)^(n + 4)*(1
1*n + 6*n^2 + n^3 + 6)) - (b*d*x^2*(a + b*x)^n*(12*b^2*c^2 + a^2*d^2*n + 7*
b^2*c^2*n + a^2*d^2*n^2 + b^2*c^2*n^2 - 8*a*b*c*d*n - 2*a*b*c*d*n^2))/((a*d
- b*c)^3*(c + d*x)^(n + 4)*(11*n + 6*n^2 + n^3 + 6)) - (2*b^2*d^2*x^3*(a +
b*x)^n*(4*b*c - a*d*n + b*c*n))/((a*d - b*c)^3*(c + d*x)^(n + 4)*(11*n + 6
*n^2 + n^3 + 6))
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**n*(d*x+c)**(-4-n), x)
```

```
[Out] Timed out
```

3.1877 $\int (a + bx)^n (c + dx)^{-5-n} dx$

Optimal. Leaf size=185

$$\frac{6b^3(a+bx)^{n+1}(c+dx)^{-n-1}}{(n+1)(n+2)(n+3)(n+4)(bc-ad)^4} + \frac{6b^2(a+bx)^{n+1}(c+dx)^{-n-2}}{(n+2)(n+3)(n+4)(bc-ad)^3} + \frac{(a+bx)^{n+1}(c+dx)^{-n-4}}{(n+4)(bc-ad)} + \frac{3b(a+bx)^{n+1}}{(n+3)(n+4)}$$

[Out] $(b*x+a)^{(1+n)}*(d*x+c)^{(-4-n)/(-a*d+b*c)/(4+n)+3*b*(b*x+a)^{(1+n)}*(d*x+c)^{(-3-n)/(-a*d+b*c)^2/(3+n)/(4+n)+6*b^2*(b*x+a)^{(1+n)}*(d*x+c)^{(-2-n)/(-a*d+b*c)^3/(2+n)/(3+n)/(4+n)+6*b^3*(b*x+a)^{(1+n)}*(d*x+c)^{(-1-n)/(-a*d+b*c)^4/(1+n)/(2+n)/(3+n)/(4+n)}$

Rubi [A] time = 0.06, antiderivative size = 185, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {45, 37}

$$\frac{6b^2(a+bx)^{n+1}(c+dx)^{-n-2}}{(n+2)(n+3)(n+4)(bc-ad)^3} + \frac{6b^3(a+bx)^{n+1}(c+dx)^{-n-1}}{(n+1)(n+2)(n+3)(n+4)(bc-ad)^4} + \frac{(a+bx)^{n+1}(c+dx)^{-n-4}}{(n+4)(bc-ad)} + \frac{3b(a+bx)^{n+1}}{(n+3)(n+4)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^n*(c + d*x)^{-5 - n}, x]$

[Out] $((a + b*x)^{(1 + n)}*(c + d*x)^{(-4 - n)/((b*c - a*d)*(4 + n))} + (3*b*(a + b*x)^{(1 + n)}*(c + d*x)^{(-3 - n)/((b*c - a*d)^2*(3 + n)*(4 + n))} + (6*b^2*(a + b*x)^{(1 + n)}*(c + d*x)^{(-2 - n)/((b*c - a*d)^3*(2 + n)*(3 + n)*(4 + n))} + (6*b^3*(a + b*x)^{(1 + n)}*(c + d*x)^{(-1 - n)/((b*c - a*d)^4*(1 + n)*(2 + n)*(3 + n)*(4 + n))})$

Rule 37

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}/((b*c - a*d)*(m + 1)), x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{EqQ}[m + n + 2, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rule 45

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)*((c_.) + (d_.)*(x_.))^{(n_.)}, x_Symbol] := \text{Simp}[(a + b*x)^{(m + 1)}*(c + d*x)^{(n + 1)}/((b*c - a*d)*(m + 1)), x] - \text{Dist}[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), \text{Int}[(a + b*x)^{\text{Simplify}[m + 1]}*(c + d*x)^n, x], x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x] \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{LtQ}[\text{Simplify}[m + n + 2], 0] \ \&\& \ \text{NeQ}[m, -1] \ \&\& \ !(\text{LtQ}[m, -1] \ \&\& \ \text{LtQ}[n, -1] \ \&\& \ (\text{EqQ}[a, 0] \ || \ (\text{NeQ}[c, 0] \ \&\& \ \text{LtQ}[m - n, 0] \ \&\& \ \text{IntegerQ}[n]))) \ \&\& \ (\text{SumSimplerQ}[m, 1] \ || \ !\text{SumSimplerQ}[n, 1])$

$n-200*a*b^3*c^3*d*n+50*b^4*c^4*n+24*a^4*d^4-96*a^3*b*c*d^3+144*a^2*b^2*c^2*d^2-96*a*b^3*c^3*d+24*b^4*c^4)$

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^n (dx + c)^{-n-5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^n*(d*x+c)^(-5-n),x, algorithm="maxima")

[Out] integrate((b*x + a)^n*(d*x + c)^(-n - 5), x)

mupad [B] time = 1.61, size = 945, normalized size = 5.11

$$\frac{6b^4d^4x^5(a+bx)^n}{(ad-bc)^4(c+dx)^{n+5}(n^4+10n^3+35n^2+50n+24)} - \frac{ac(a+bx)^n(a^3d^3n^3+6a^3d^3n^2+11a^3d^3n+6a^3}{(ad-bc)^4(c+dx)^{n+5}(n^4+10n^3+35n^2+50n+24)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^n/(c + d*x)^(n + 5),x)

[Out] $(6*b^4*d^4*x^5*(a + b*x)^n)/((a*d - b*c)^4*(c + d*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) - (a*c*(a + b*x)^n*(6*a^3*d^3 - 24*b^3*c^3 + 11*a^3*d^3*n - 26*b^3*c^3*n + 6*a^3*d^3*n^2 - 9*b^3*c^3*n^2 + a^3*d^3*n^3 - b^3*c^3*n^3 + 36*a*b^2*c^2*d - 24*a^2*b*c*d^2 + 57*a*b^2*c^2*d*n - 42*a^2*b*c*d^2*n + 24*a*b^2*c^2*d*n^2 - 21*a^2*b*c*d^2*n^2 + 3*a*b^2*c^2*d*n^3 - 3*a^2*b*c*d^2*n^3))/((a*d - b*c)^4*(c + d*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) - (x*(a + b*x)^n*(6*a^4*d^4 - 24*b^4*c^4 + 11*a^4*d^4*n - 26*b^4*c^4*n + 6*a^4*d^4*n^2 - 9*b^4*c^4*n^2 + a^4*d^4*n^3 - b^4*c^4*n^3 + 36*a^2*b^2*c^2*d^2 - 24*a*b^3*c^3*d - 24*a^3*b*c*d^3 + 10*a*b^3*c^3*d*n - 40*a^3*b*c*d^3*n + 9*a^2*b^2*c^2*d^2*n^2 + 12*a*b^3*c^3*d*n^2 - 18*a^3*b*c*d^3*n^2 + 2*a*b^3*c^3*d*n^3 - 2*a^3*b*c*d^3*n^3 + 45*a^2*b^2*c^2*d^2*n))/((a*d - b*c)^4*(c + d*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (3*b^2*d^2*x^3*(a + b*x)^n*(20*b^2*c^2 + a^2*d^2*n + 9*b^2*c^2*n + a^2*d^2*n^2 + b^2*c^2*n^2 - 10*a*b*c*d*n - 2*a*b*c*d*n^2))/((a*d - b*c)^4*(c + d*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (6*b^3*d^3*x^4*(a + b*x)^n*(5*b*c - a*d*n + b*c*n))/((a*d - b*c)^4*(c + d*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24)) + (b*d*x^2*(a + b*x)^n*(60*b^3*c^3 - 2*a^3*d^3*n + 47*b^3*c^3*n - 3*a^3*d^3*n^2 + 12*b^3*c^3*n^2 - a^3*d^3*n^3 + b^3*c^3*n^3 - 60*a*b^2*c^2*d*n + 15*a^2*b*c*d^2*n - 27*a*b^2*c^2*d*n^2 + 18*a^2*b*c*d^2*n^2 - 3*a*b^2*c^2*d*n^3 + 3*a^2*b*c*d^2*n^3))/((a*d - b*c)^4*(c + d*x)^(n + 5)*(50*n + 35*n^2 + 10*n^3 + n^4 + 24))$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x+a)**n*(d*x+c)**(-5-n),x)
```

```
[Out] Timed out
```

3.1878 $\int (a + bx)^{-2+n} (c + dx)^{1-n} dx$

Optimal. Leaf size=83

$$\frac{(bc - ad)(a + bx)^{n-1}(c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad}\right)^n {}_2F_1\left(n-1, n-1; n; -\frac{d(a+bx)}{bc-ad}\right)}{b^2(1-n)}$$

[Out] $-(-a*d+b*c)*(b*x+a)^{-1+n}*(b*(d*x+c)/(-a*d+b*c))^n*\text{hypergeom}([-1+n, -1+n], [n], -d*(b*x+a)/(-a*d+b*c))/b^2/(1-n)/((d*x+c)^n)$

Rubi [A] time = 0.03, antiderivative size = 83, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.095$, Rules used = {70, 69}

$$\frac{(bc - ad)(a + bx)^{n-1}(c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad}\right)^n {}_2F_1\left(n-1, n-1; n; -\frac{d(a+bx)}{bc-ad}\right)}{b^2(1-n)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{-2 + n}*(c + d*x)^{(1 - n)}, x]$

[Out] $-(((b*c - a*d)*(a + b*x)^{-1 + n}*((b*(c + d*x))/(b*c - a*d))^n*\text{Hypergeometric2F1}[-1 + n, -1 + n, n, -((d*(a + b*x))/(b*c - a*d))]/(b^2*(1 - n)*(c + d*x)^n))$

Rule 69

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x] \rightarrow \text{Simp}[\frac{(a + b*x)^{m+1}*\text{Hypergeometric2F1}[-n, m+1, m+2, -((d*(a + b*x))/(b*c - a*d))]}{(b*(m+1)*(b/(b*c - a*d))^n)}, x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ !\text{IntegerQ}[m] \ \&\& \ !\text{IntegerQ}[n] \ \&\& \ \text{GtQ}[b/(b*c - a*d), 0] \ \&\& \ (\text{RationalQ}[m] \ || \ !(\text{RationalQ}[n] \ \&\& \ \text{GtQ}[-(d/(b*c - a*d)), 0]))$

Rule 70

$\text{Int}[(a + b*x)^m*(c + d*x)^n, x] \rightarrow \text{Dist}[(c + d*x)^{\text{FracPart}[n]}/(b/(b*c - a*d))^{\text{IntPart}[n]}*((b*(c + d*x))/(b*c - a*d))^{\text{FracPart}[n]}, \text{Int}[(a + b*x)^m*\text{Simp}[(b*c)/(b*c - a*d] + (b*d*x)/(b*c - a*d), x]^n, x] /; \text{FreeQ}\{a, b, c, d, m, n\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ !\text{IntegerQ}[m] \ \&\& \ !\text{IntegerQ}[n] \ \&\& \ (\text{RationalQ}[m] \ || \ !\text{SimplerQ}[n + 1, m + 1])$

Rubi steps

$$\int (a + bx)^{-2+n} (c + dx)^{1-n} dx = \frac{\left((bc - ad)(c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n \right) \int (a + bx)^{-2+n} \left(\frac{bc}{bc-ad} + \frac{bdx}{bc-ad} \right)^{1-n} dx}{b}$$

$$= -\frac{(bc - ad)(a + bx)^{-1+n} (c + dx)^{-n} \left(\frac{b(c+dx)}{bc-ad} \right)^n {}_2F_1 \left(-1 + n, -1 + n; n; -\frac{d(a+bx)}{bc-ad} \right)}{b^2(1 - n)}$$

Mathematica [A] time = 0.06, size = 75, normalized size = 0.90

$$\frac{(a + bx)^{n-1} (c + dx)^{1-n} \left(\frac{b(c+dx)}{bc-ad} \right)^{n-1} {}_2F_1 \left(n - 1, n - 1; n; \frac{d(a+bx)}{ad-bc} \right)}{b(n - 1)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-2 + n)*(c + d*x)^(1 - n), x]

[Out] ((a + b*x)^(-1 + n)*(c + d*x)^(1 - n)*((b*(c + d*x))/(b*c - a*d))^(-1 + n)*Hypergeometric2F1[-1 + n, -1 + n, n, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(-1 + n))

fricas [F] time = 0.57, size = 0, normalized size = 0.00

$$\text{integral} \left((bx + a)^{n-2} (dx + c)^{-n+1}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-2+n)*(d*x+c)^(1-n), x, algorithm="fricas")

[Out] integral((b*x + a)^(n - 2)*(d*x + c)^(-n + 1), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{n-2} (dx + c)^{-n+1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-2+n)*(d*x+c)^(1-n), x, algorithm="giac")

[Out] integrate((b*x + a)^(n - 2)*(d*x + c)^(-n + 1), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{n-2} (dx + c)^{-n+1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(n-2)*(d*x+c)^(1-n),x)`

[Out] `int((b*x+a)^(n-2)*(d*x+c)^(1-n),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{n-2} (dx + c)^{-n+1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(-2+n)*(d*x+c)^(1-n),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(n - 2)*(d*x + c)^(-n + 1), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + bx)^{n-2} (c + dx)^{1-n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(n - 2)*(c + d*x)^(1 - n),x)`

[Out] `int((a + b*x)^(n - 2)*(c + d*x)^(1 - n), x)`

sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(-2+n)*(d*x+c)**(1-n),x)`

[Out] Exception raised: HeuristicGCDFailed

3.1879 $\int (a + bx)^{1+n} (c + dx)^{-1-n} dx$

Optimal. Leaf size=84

$$\frac{(bc - ad)(a + bx)^n (c + dx)^{-n} \left(-\frac{d(a+bx)}{bc-ad}\right)^{-n} {}_2F_1\left(-n-1, -n; 1-n; \frac{b(c+dx)}{bc-ad}\right)}{d^{2n}}$$

[Out] $(-a*d+b*c)*(b*x+a)^n*\text{hypergeom}([-n, -1-n], [1-n], b*(d*x+c)/(-a*d+b*c))/d^{2/n}/((-d*(b*x+a)/(-a*d+b*c))^n)/((d*x+c)^n)$

Rubi [A] time = 0.03, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.095$, Rules used = {70, 69}

$$\frac{(bc - ad)(a + bx)^n (c + dx)^{-n} \left(-\frac{d(a+bx)}{bc-ad}\right)^{-n} {}_2F_1\left(-n-1, -n; 1-n; \frac{b(c+dx)}{bc-ad}\right)}{d^{2n}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*x)^{(1 + n)}*(c + d*x)^{(-1 - n)}, x]$

[Out] $((b*c - a*d)*(a + b*x)^n*\text{Hypergeometric2F1}[-1 - n, -n, 1 - n, (b*(c + d*x))/(b*c - a*d)]/(d^{2*n}*(-(d*(a + b*x))/(b*c - a*d)))^n*(c + d*x)^n)$

Rule 69

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_) + (d_)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Simp}[(c + d*x)^{(m + 1)}*\text{Hypergeometric2F1}[-n, m + 1, m + 2, -(d*(a + b*x))/(b*c - a*d)]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 70

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_) + (d_)*(x_))^{(n_)}, x_Symbol] \rightarrow \text{Dist}[(c + d*x)^{\text{FracPart}[n]}/(b/(b*c - a*d))^{\text{IntPart}[n]}*((b*(c + d*x))/(b*c - a*d))^{\text{FracPart}[n]}], \text{Int}[(a + b*x)^m*\text{Simp}[(b*c)/(b*c - a*d) + (b*d*x)/(b*c - a*d), x]^n, x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && (RationalQ[m] || !SimplerQ[n + 1, m + 1])

Rubi steps

$$\int (a + bx)^{1+n} (c + dx)^{-1-n} dx = \frac{\left((-bc + ad)(a + bx)^n \left(\frac{d(a+bx)}{-bc+ad} \right)^{-n} \right) \int (c + dx)^{-1-n} \left(-\frac{ad}{bc-ad} - \frac{bdx}{bc-ad} \right)^{1+n} dx}{d}$$

$$= \frac{(bc - ad)(a + bx)^n \left(-\frac{d(a+bx)}{bc-ad} \right)^{-n} (c + dx)^{-n} {}_2F_1 \left(-1 - n, -n; 1 - n; \frac{b(c+dx)}{bc-ad} \right)}{d^2 n}$$

Mathematica [A] time = 0.05, size = 83, normalized size = 0.99

$$\frac{(bc - ad)(a + bx)^n (c + dx)^{-n} \left(\frac{d(a+bx)}{ad-bc} \right)^{-n} {}_2F_1 \left(-n - 1, -n; 1 - n; \frac{b(c+dx)}{bc-ad} \right)}{d^2 n}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(1 + n)*(c + d*x)^(-1 - n), x]

[Out] ((b*c - a*d)*(a + b*x)^n*Hypergeometric2F1[-1 - n, -n, 1 - n, (b*(c + d*x))/(b*c - a*d)]/(d^2*n*((d*(a + b*x))/(-b*c) + a*d))^n*(c + d*x)^n

fricas [F] time = 0.74, size = 0, normalized size = 0.00

$$\text{integral} \left((bx + a)^{n+1} (dx + c)^{-n-1}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1+n)*(d*x+c)^(-1-n), x, algorithm="fricas")

[Out] integral((b*x + a)^(n + 1)*(d*x + c)^(-n - 1), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{n+1} (dx + c)^{-n-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(1+n)*(d*x+c)^(-1-n), x, algorithm="giac")

[Out] integrate((b*x + a)^(n + 1)*(d*x + c)^(-n - 1), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (bx + a)^{n+1} (dx + c)^{-n-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^(n+1)*(d*x+c)^(-n-1),x)`

[Out] `int((b*x+a)^(n+1)*(d*x+c)^(-n-1),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{n+1} (dx + c)^{-n-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^(1+n)*(d*x+c)^(-1-n),x, algorithm="maxima")`

[Out] `integrate((b*x + a)^(n + 1)*(d*x + c)^(-n - 1), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + bx)^{n+1}}{(c + dx)^{n+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*x)^(n + 1)/(c + d*x)^(n + 1),x)`

[Out] `int((a + b*x)^(n + 1)/(c + d*x)^(n + 1), x)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**(1+n)*(d*x+c)**(-1-n),x)`

[Out] Timed out

$$3.1880 \quad \int (a + bx)^m (c + dx)^{1+2n-2(1+n)} dx$$

Optimal. Leaf size=51

$$\frac{(a + bx)^{m+1} {}_2F_1\left(1, m + 1; m + 2; -\frac{d(a+bx)}{bc-ad}\right)}{(m + 1)(bc - ad)}$$

[Out] (b*x+a)^(1+m)*hypergeom([1, 1+m], [2+m], -d*(b*x+a)/(-a*d+b*c))/(-a*d+b*c)/(1+m)

Rubi [A] time = 0.01, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 24, $\frac{\text{number of rules}}{\text{integrand size}} = 0.083$, Rules used = {7, 68}

$$\frac{(a + bx)^{m+1} {}_2F_1\left(1, m + 1; m + 2; -\frac{d(a+bx)}{bc-ad}\right)}{(m + 1)(bc - ad)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^m*(c + d*x)^(1 + 2*n - 2*(1 + n)), x]

[Out] ((a + b*x)^(1 + m)*Hypergeometric2F1[1, 1 + m, 2 + m, -((d*(a + b*x))/(b*c - a*d))])/((b*c - a*d)*(1 + m))

Rule 7

Int[(u_)*(Px_)^(p_), x_Symbol] := Int[u*Px^Simplify[p], x] /; PolyQ[Px, x] && !RationalQ[p] && FreeQ[p, x] && RationalQ[Simplify[p]]

Rule 68

Int[((a_) + (b_)*(x_))^(m_)*((c_) + (d_)*(x_))^(n_), x_Symbol] := Simp[(((b*c - a*d)^n*(a + b*x)^(m+1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/((b^(n + 1)*(m + 1)), x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && IntegerQ[n]

Rubi steps

$$\begin{aligned} \int (a + bx)^m (c + dx)^{1+2n-2(1+n)} dx &= \int \frac{(a + bx)^m}{c + dx} dx \\ &= \frac{(a + bx)^{1+m} {}_2F_1\left(1, 1 + m; 2 + m; -\frac{d(a+bx)}{bc-ad}\right)}{(bc - ad)(1 + m)} \end{aligned}$$

Mathematica [A] time = 0.02, size = 51, normalized size = 1.00

$$\frac{(a + bx)^{m+1} {}_2F_1\left(1, m + 1; m + 2; \frac{d(a+bx)}{ad-bc}\right)}{(m + 1)(ad - bc)}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^m*(c + d*x)^(1 + 2*n - 2*(1 + n)), x]

[Out] -(((a + b*x)^(1 + m)*Hypergeometric2F1[1, 1 + m, 2 + m, (d*(a + b*x))/(-(b*c) + a*d)])/((-b*c) + a*d)*(1 + m))

fricas [F] time = 0.76, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(bx + a)^m}{dx + c}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c), x, algorithm="fricas")

[Out] integral((b*x + a)^m/(d*x + c), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{dx + c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c), x, algorithm="giac")

[Out] integrate((b*x + a)^m/(d*x + c), x)

maple [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{dx + c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)*(b*x+a)^m, x)

[Out] int(1/(d*x+c)*(b*x+a)^m, x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(bx + a)^m}{dx + c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m/(d*x+c),x, algorithm="maxima")

[Out] integrate((b*x + a)^m/(d*x + c), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(a + bx)^m}{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^m/(c + d*x),x)

[Out] int((a + b*x)^m/(c + d*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + bx)^m}{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**m/(d*x+c),x)

[Out] Integral((a + b*x)**m/(c + d*x), x)

$$3.1881 \quad \int \frac{(c+dx)^{1+2n-2(1+n)}}{(a+bx)^2} dx$$

Optimal. Leaf size=57

$$-\frac{1}{(a+bx)(bc-ad)} - \frac{d \log(a+bx)}{(bc-ad)^2} + \frac{d \log(c+dx)}{(bc-ad)^2}$$

[Out] $-1/(-a*d+b*c)/(b*x+a)-d*\ln(b*x+a)/(-a*d+b*c)^2+d*\ln(d*x+c)/(-a*d+b*c)^2$

Rubi [A] time = 0.03, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 24, $\frac{\text{number of rules}}{\text{integrand size}} = 0.083$, Rules used = {7, 44}

$$-\frac{1}{(a+bx)(bc-ad)} - \frac{d \log(a+bx)}{(bc-ad)^2} + \frac{d \log(c+dx)}{(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^(1 + 2*n - 2*(1 + n))/(a + b*x)^2, x]

[Out] $-(1/((b*c - a*d)*(a + b*x))) - (d*\text{Log}[a + b*x])/(b*c - a*d)^2 + (d*\text{Log}[c + d*x])/(b*c - a*d)^2$

Rule 7

Int[(u_.)*(Px_)^(p_), x_Symbol] :> Int[u*Px^Simplify[p], x] /; PolyQ[Px, x] && !RationalQ[p] && FreeQ[p, x] && RationalQ[Simplify[p]]

Rule 44

Int[((a_) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && ILtQ[m, 0] && IntegerQ[n] && !(IGtQ[n, 0] && LtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^{1+2n-2(1+n)}}{(a+bx)^2} dx &= \int \frac{1}{(a+bx)^2(c+dx)} dx \\ &= \int \left(\frac{b}{(bc-ad)(a+bx)^2} - \frac{bd}{(bc-ad)^2(a+bx)} + \frac{d^2}{(bc-ad)^2(c+dx)} \right) dx \\ &= -\frac{1}{(bc-ad)(a+bx)} - \frac{d \log(a+bx)}{(bc-ad)^2} + \frac{d \log(c+dx)}{(bc-ad)^2} \end{aligned}$$

Mathematica [A] time = 0.03, size = 53, normalized size = 0.93

$$\frac{d(a+bx)\log(c+dx) - d(a+bx)\log(a+bx) + ad - bc}{(a+bx)(bc-ad)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^(1 + 2*n - 2*(1 + n))/(a + b*x)^2,x]

[Out] $(-(b*c) + a*d - d*(a + b*x)*\text{Log}[a + b*x] + d*(a + b*x)*\text{Log}[c + d*x])/((b*c - a*d)^2*(a + b*x))$

fricas [A] time = 0.69, size = 93, normalized size = 1.63

$$-\frac{bc - ad + (bdx + ad)\log(bx + a) - (bdx + ad)\log(dx + c)}{ab^2c^2 - 2a^2bcd + a^3d^2 + (b^3c^2 - 2ab^2cd + a^2bd^2)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c),x, algorithm="fricas")

[Out] $-(b*c - a*d + (b*d*x + a*d)*\log(b*x + a) - (b*d*x + a*d)*\log(d*x + c))/(a*b^2*c^2 - 2*a^2*b*c*d + a^3*d^2 + (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*x)$

giac [A] time = 0.92, size = 78, normalized size = 1.37

$$\frac{bd \log\left(\left|\frac{bc}{bx+a} - \frac{ad}{bx+a} + d\right|\right)}{b^3c^2 - 2ab^2cd + a^2bd^2} - \frac{b}{(b^2c - abd)(bx + a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c),x, algorithm="giac")

[Out] $b*d*\log(\text{abs}(b*c/(b*x + a) - a*d/(b*x + a) + d))/(b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2) - b/((b^2*c - a*b*d)*(b*x + a))$

maple [A] time = 0.01, size = 57, normalized size = 1.00

$$-\frac{d \ln(bx + a)}{(ad - bc)^2} + \frac{d \ln(dx + c)}{(ad - bc)^2} + \frac{1}{(ad - bc)(bx + a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(b*x+a)^2/(d*x+c),x)

[Out] $d/(a*d-b*c)^2*\ln(d*x+c)+1/(a*d-b*c)/(b*x+a)-d/(a*d-b*c)^2*\ln(b*x+a)$

maxima [A] time = 1.16, size = 92, normalized size = 1.61

$$-\frac{d \log(bx + a)}{b^2c^2 - 2abcd + a^2d^2} + \frac{d \log(dx + c)}{b^2c^2 - 2abcd + a^2d^2} - \frac{1}{abc - a^2d + (b^2c - abd)x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)^2/(d*x+c),x, algorithm="maxima")

[Out] -d*log(b*x + a)/(b^2*c^2 - 2*a*b*c*d + a^2*d^2) + d*log(d*x + c)/(b^2*c^2 - 2*a*b*c*d + a^2*d^2) - 1/(a*b*c - a^2*d + (b^2*c - a*b*d)*x)

mupad [B] time = 0.44, size = 46, normalized size = 0.81

$$\frac{1}{(ad - bc)(a + bx)} - \frac{d \ln\left(\frac{a+bx}{c+dx}\right)}{(ad - bc)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^2*(c + d*x)),x)

[Out] 1/((a*d - b*c)*(a + b*x)) - (d*log((a + b*x)/(c + d*x)))/(a*d - b*c)^2

sympy [B] time = 0.69, size = 233, normalized size = 4.09

$$\frac{d \log\left(x + \frac{-\frac{a^3d^4}{(ad-bc)^2} + \frac{3a^2bcd^3}{(ad-bc)^2} - \frac{3ab^2c^2d^2}{(ad-bc)^2} + ad^2 + \frac{b^3c^3d}{(ad-bc)^2} + bcd}{2ba^2}\right)}{(ad - bc)^2} - \frac{d \log\left(x + \frac{\frac{a^3d^4}{(ad-bc)^2} - \frac{3a^2bcd^3}{(ad-bc)^2} + \frac{3ab^2c^2d^2}{(ad-bc)^2} + ad^2 - \frac{b^3c^3d}{(ad-bc)^2} + bcd}{2ba^2}\right)}{(ad - bc)^2} + \frac{1}{a^2d - abc + \dots}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(b*x+a)**2/(d*x+c),x)

[Out] d*log(x + (-a**3*d**4/(a*d - b*c)**2 + 3*a**2*b*c*d**3/(a*d - b*c)**2 - 3*a*b**2*c**2*d**2/(a*d - b*c)**2 + a*d**2 + b**3*c**3*d/(a*d - b*c)**2 + b*c*d)/(2*b*d**2))/(a*d - b*c)**2 - d*log(x + (a**3*d**4/(a*d - b*c)**2 - 3*a**2*b*c*d**3/(a*d - b*c)**2 + 3*a*b**2*c**2*d**2/(a*d - b*c)**2 + a*d**2 - b**3*c**3*d/(a*d - b*c)**2 + b*c*d)/(2*b*d**2))/(a*d - b*c)**2 + 1/(a**2*d - a*b*c + x*(a*b*d - b**2*c))

$$3.1882 \quad \int (a + bx)^m (ac(1 + m) + bc(2 + m)x)^{-3-m} dx$$

Optimal. Leaf size=95

$$\frac{(a + bx)^{m+1}(ac(m + 1) + bc(m + 2)x)^{-m-1}}{a^2bc^2(m + 1)(m + 2)} - \frac{(a + bx)^{m+1}(ac(m + 1) + bc(m + 2)x)^{-m-2}}{abc(m + 2)}$$

[Out] $-(b*x+a)^{(1+m)}*(a*c*(1+m)+b*c*(2+m)*x)^{(-2-m)}/a/b/c/(2+m)+(b*x+a)^{(1+m)}*(a*c*(1+m)+b*c*(2+m)*x)^{(-1-m)}/a^2/b/c^2/(m^2+3*m+2)$

Rubi [A] time = 0.04, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 28, $\frac{\text{number of rules}}{\text{integrand size}} = 0.071$, Rules used = {45, 37}

$$\frac{(a + bx)^{m+1}(ac(m + 1) + bc(m + 2)x)^{-m-1}}{a^2bc^2(m + 1)(m + 2)} - \frac{(a + bx)^{m+1}(ac(m + 1) + bc(m + 2)x)^{-m-2}}{abc(m + 2)}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^m*(a*c*(1 + m) + b*c*(2 + m)*x)^(-3 - m), x]

[Out] $-(((a + b*x)^{(1 + m)}*(a*c*(1 + m) + b*c*(2 + m)*x)^{(-2 - m)})/(a*b*c*(2 + m)) + ((a + b*x)^{(1 + m)}*(a*c*(1 + m) + b*c*(2 + m)*x)^{(-1 - m)})/(a^2*b*c^2*(1 + m)*(2 + m))$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int (a + bx)^m (ac(1 + m) + bc(2 + m)x)^{-3-m} dx = -\frac{(a + bx)^{1+m} (ac(1 + m) + bc(2 + m)x)^{-2-m}}{abc(2 + m)} - \frac{\int (a + bx)^m (ac(1 + m) + bc(2 + m)x)^{-3-m} dx}{a}$$

$$= -\frac{(a + bx)^{1+m} (ac(1 + m) + bc(2 + m)x)^{-2-m}}{abc(2 + m)} + \frac{(a + bx)^{1+m} (ac(1 + m) + bc(2 + m)x)^{-3-m}}{a^2 bc^2 (1 + m)}$$

Mathematica [A] time = 0.07, size = 54, normalized size = 0.57

$$\frac{x(a + bx)^{m+1} (ac(m + 1) + bc(m + 2)x)^{-m}}{a^2 c^3 (m + 1) (a(m + 1) + b(m + 2)x)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^m*(a*c*(1 + m) + b*c*(2 + m)*x)^(-3 - m), x]

[Out] (x*(a + b*x)^(1 + m))/(a^2*c^3*(1 + m)*(a*(1 + m) + b*(2 + m)*x)^2*(a*c*(1 + m) + b*c*(2 + m)*x)^m)

fricas [A] time = 0.72, size = 85, normalized size = 0.89

$$\frac{((b^2 m + 2 b^2)x^3 + (2 abm + 3 ab)x^2 + (a^2 m + a^2)x)(acm + ac + (bcm + 2 bc)x)^{-m-3} (bx + a)^m}{a^2 m + a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(a*c*(1+m)+b*c*(2+m)*x)^(-3-m), x, algorithm="fricas")

[Out] ((b^2*m + 2*b^2)*x^3 + (2*a*b*m + 3*a*b)*x^2 + (a^2*m + a^2)*x)*(a*c*m + a*c + (b*c*m + 2*b*c)*x)^(-m - 3)*(b*x + a)^m/(a^2*m + a^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bc(m + 2)x + ac(m + 1))^{-m-3} (bx + a)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^m*(a*c*(1+m)+b*c*(2+m)*x)^(-3-m), x, algorithm="giac")

[Out] integrate((b*c*(m + 2)*x + a*c*(m + 1))(-m - 3)*(b*x + a)^m, x)

maple [A] time = 0.01, size = 57, normalized size = 0.60

$$\frac{(bxm + am + 2bx + a)x(bx + a)^{m+1} (bcxm + acm + 2bcx + ac)^{-m-3}}{(m + 1)a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((b*x+a)^m*(a*c*(m+1)+b*c*(m+2)*x)^(-3-m), x)`

[Out] `(b*x+a)^(m+1)*(b*m*x+a*m+2*b*x+a)/a^2/(m+1)*x*(b*c*m*x+a*c*m+2*b*c*x+a*c)^(-3-m)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bc(m+2)x + ac(m+1))^{-m-3} (bx+a)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)^m*(a*c*(1+m)+b*c*(2+m)*x)^(-3-m), x, algorithm="maxima")`

[Out] `integrate((b*c*(m+2)*x + a*c*(m+1))^(m+3)*(b*x+a)^m, x)`

mupad [B] time = 1.04, size = 81, normalized size = 0.85

$$\frac{x(a+bx)^m + \frac{bx^2(2m+3)(a+bx)^m}{a(m+1)} + \frac{b^2x^3(m+2)(a+bx)^m}{a^2(m+1)}}{(ac(m+1) + bcx(m+2))^{m+3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*x)^m/(a*c*(m+1)+b*c*x*(m+2))^(m+3), x)`

[Out] `(x*(a+b*x)^m + (b*x^2*(2*m+3)*(a+b*x)^m)/(a*(m+1)) + (b^2*x^3*(m+2)*(a+b*x)^m)/(a^2*(m+1)))/(a*c*(m+1)+b*c*x*(m+2))^(m+3)`

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((b*x+a)**m*(a*c*(1+m)+b*c*(2+m)*x)**(-3-m), x)`

[Out] Timed out

$$3.1883 \quad \int (a + bx)^{-1 - \frac{bc}{bc-ad}} (c + dx)^{-1 + \frac{ad}{bc-ad}} dx$$

Optimal. Leaf size=97

$$\frac{(a + bx)^{-\frac{ad}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{abc} - \frac{(a + bx)^{-\frac{bc}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{bc}$$

[Out] $-(d*x+c)^{(a*d/(-a*d+b*c))}/b/c/((b*x+a)^{(b*c/(-a*d+b*c))) + (d*x+c)^{(a*d/(-a*d+b*c))}/a/b/c/((b*x+a)^{(a*d/(-a*d+b*c)))}$

Rubi [A] time = 0.02, antiderivative size = 97, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 44, $\frac{\text{number of rules}}{\text{integrand size}} = 0.045$, Rules used = {45, 37}

$$\frac{(a + bx)^{-\frac{ad}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{abc} - \frac{(a + bx)^{-\frac{bc}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{bc}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^(-1 - (b*c)/(b*c - a*d))*(c + d*x)^(-1 + (a*d)/(b*c - a*d)), x]

[Out] $-((c + d*x)^{(a*d)/(b*c - a*d)}/(b*c*(a + b*x)^{(b*c)/(b*c - a*d)})) + (c + d*x)^{(a*d)/(b*c - a*d)}/(a*b*c*(a + b*x)^{(a*d)/(b*c - a*d)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int (a + bx)^{-1 - \frac{bc}{bc-ad}} (c + dx)^{-1 + \frac{ad}{bc-ad}} dx = -\frac{(a + bx)^{-\frac{bc}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{bc} - \frac{d \int (a + bx)^{-\frac{bc}{bc-ad}} (c + dx)^{-1 + \frac{ad}{bc-ad}} dx}{bc}$$

$$= -\frac{(a + bx)^{-\frac{bc}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{bc} + \frac{(a + bx)^{-\frac{ad}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{abc}$$

Mathematica [A] time = 0.04, size = 46, normalized size = 0.47

$$\frac{x(a + bx)^{\frac{bc}{ad-bc}} (c + dx)^{\frac{ad}{bc-ad}}}{ac}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^(-1 - (b*c)/(b*c - a*d))*(c + d*x)^(-1 + (a*d)/(b*c - a*d)), x]

[Out] (x*(a + b*x)^((b*c)/(-(b*c) + a*d))*(c + d*x)^((a*d)/(b*c - a*d)))/(a*c)

fricas [A] time = 0.79, size = 84, normalized size = 0.87

$$\frac{bdx^3 + acx + (bc + ad)x^2}{(bx + a)^{\frac{2bc-ad}{bc-ad}} (dx + c)^{\frac{bc-2ad}{bc-ad}} ac}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-1-b*c/(-a*d+b*c))*(d*x+c)^(-1+a*d/(-a*d+b*c)), x, algorithm="fricas")

[Out] (b*d*x^3 + a*c*x + (b*c + a*d)*x^2)/((b*x + a)^((2*b*c - a*d)/(b*c - a*d))*(d*x + c)^((b*c - 2*a*d)/(b*c - a*d))*a*c)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-\frac{bc}{bc-ad}-1} (dx + c)^{\frac{ad}{bc-ad}-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-1-b*c/(-a*d+b*c))*(d*x+c)^(-1+a*d/(-a*d+b*c)), x, algorithm="giac")

[Out] integrate((b*x + a)^(-b*c/(b*c - a*d) - 1)*(d*x + c)^(a*d/(b*c - a*d) - 1), x)

maple [A] time = 0.00, size = 66, normalized size = 0.68

$$\frac{x(bx + a)^{1 - \frac{ad-2bc}{ad-bc}} (dx + c)^{1 - \frac{2ad-bc}{ad-bc}}}{ac}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^(-1-b*c/(-a*d+b*c))*(d*x+c)^(-1+a*d/(-a*d+b*c)),x)

[Out] (b*x+a)^(1-(a*d-2*b*c)/(a*d-b*c))*(d*x+c)^(1-(2*a*d-b*c)/(a*d-b*c))/a/c*x

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (bx + a)^{-\frac{bc}{bc-ad}-1} (dx + c)^{\frac{ad}{bc-ad}-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^(-1-b*c/(-a*d+b*c))*(d*x+c)^(-1+a*d/(-a*d+b*c)),x, algorithm="maxima")

[Out] integrate((b*x + a)^(-b*c/(b*c - a*d) - 1)*(d*x + c)^(a*d/(b*c - a*d) - 1), x)

mupad [B] time = 2.14, size = 119, normalized size = 1.23

$$\frac{x(a + bx)^{\frac{bc}{ad-bc}-1} + \frac{x^2(ad+bc)(a+bx)^{\frac{bc}{ad-bc}-1}}{ac} + \frac{bdx^3(a+bx)^{\frac{bc}{ad-bc}-1}}{ac}}{(c + dx)^{\frac{ad}{ad-bc}+1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*x)^((b*c)/(a*d - b*c) - 1)/(c + d*x)^((a*d)/(a*d - b*c) + 1),x)

[Out] (x*(a + b*x)^((b*c)/(a*d - b*c) - 1) + (x^2*(a*d + b*c)*(a + b*x)^((b*c)/(a*d - b*c) - 1))/(a*c) + (b*d*x^3*(a + b*x)^((b*c)/(a*d - b*c) - 1))/(a*c))/(c + d*x)^((a*d)/(a*d - b*c) + 1)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**(-1-b*c/(-a*d+b*c))*(d*x+c)**(-1+a*d/(-a*d+b*c)),x)

[Out] Timed out

$$3.1884 \quad \int (a + bx)^{\frac{-2bc+ad}{bc-ad}} (c + dx)^{\frac{bc-2ad}{-bc+ad}} dx$$

Optimal. Leaf size=97

$$\frac{(a + bx)^{-\frac{ad}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{abc} - \frac{(a + bx)^{-\frac{bc}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{bc}$$

[Out] $-(d*x+c)^{(a*d/(-a*d+b*c))}/b/c/((b*x+a)^{(b*c/(-a*d+b*c))})+(d*x+c)^{(a*d/(-a*d+b*c))}/a/b/c/((b*x+a)^{(a*d/(-a*d+b*c))})$

Rubi [A] time = 0.02, antiderivative size = 97, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 51, $\frac{\text{number of rules}}{\text{integrand size}} = 0.039$, Rules used = {45, 37}

$$\frac{(a + bx)^{-\frac{ad}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{abc} - \frac{(a + bx)^{-\frac{bc}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{bc}$$

Antiderivative was successfully verified.

[In] Int[(a + b*x)^((-2*b*c + a*d)/(b*c - a*d))*(c + d*x)^((b*c - 2*a*d)/(-(b*c) + a*d)), x]

[Out] $-((c + d*x)^{(a*d)/(b*c - a*d)}/(b*c*(a + b*x)^{(b*c)/(b*c - a*d)})) + (c + d*x)^{(a*d)/(b*c - a*d)}/(a*b*c*(a + b*x)^{(a*d)/(b*c - a*d)})$

Rule 37

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n + 2, 0] && NeQ[m, -1]

Rule 45

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*Simplify[m + n + 2])/((b*c - a*d)*(m + 1)), Int[(a + b*x)^Simplify[m + 1]*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !LtQ[Simplify[m + n + 2], 0] && NeQ[m, -1] && !(LtQ[m, -1] && LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && (SumSimplerQ[m, 1] || !SumSimplerQ[n, 1])

Rubi steps

$$\int (a + bx)^{\frac{-2bc+ad}{bc-ad}} (c + dx)^{\frac{bc-2ad}{-bc+ad}} dx = -\frac{(a + bx)^{\frac{bc}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{bc} - \frac{d \int (a + bx)^{\frac{bc}{-bc+ad}} (c + dx)^{\frac{bc-2ad}{-bc+ad}} dx}{bc}$$

$$= -\frac{(a + bx)^{\frac{bc}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{bc} + \frac{(a + bx)^{\frac{-ad}{bc-ad}} (c + dx)^{\frac{ad}{bc-ad}}}{abc}$$

Mathematica [A] time = 0.07, size = 46, normalized size = 0.47

$$\frac{x(a + bx)^{\frac{bc}{ad-bc}} (c + dx)^{\frac{ad}{bc-ad}}}{ac}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*x)^((-2*b*c + a*d)/(b*c - a*d))*(c + d*x)^((b*c - 2*a*d)/(-b*c + a*d)), x]

[Out] (x*(a + b*x)^((b*c)/(-b*c + a*d))*(c + d*x)^((a*d)/(b*c - a*d)))/(a*c)

fricas [A] time = 1.07, size = 84, normalized size = 0.87

$$\frac{bdx^3 + acx + (bc + ad)x^2}{(bx + a)^{\frac{2bc-ad}{bc-ad}} (dx + c)^{\frac{bc-2ad}{bc-ad}} ac}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^((a*d-2*b*c)/(-a*d+b*c))*(d*x+c)^((-2*a*d+b*c)/(a*d-b*c)), x, algorithm="fricas")

[Out] (b*d*x^3 + a*c*x + (b*c + a*d)*x^2)/((b*x + a)^((2*b*c - a*d)/(b*c - a*d))*(d*x + c)^((b*c - 2*a*d)/(b*c - a*d))*a*c)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{2bc-ad}{bc-ad}} (dx + c)^{\frac{bc-2ad}{bc-ad}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^((a*d-2*b*c)/(-a*d+b*c))*(d*x+c)^((-2*a*d+b*c)/(a*d-b*c)), x, algorithm="giac")

[Out] integrate(1/((b*x + a)^((2*b*c - a*d)/(b*c - a*d))*(d*x + c)^((b*c - 2*a*d)/(b*c - a*d))), x)

maple [A] time = 0.00, size = 66, normalized size = 0.68

$$\frac{x (bx + a)^{1 - \frac{ad-2bc}{ad-bc}} (dx + c)^{1 - \frac{2ad-bc}{ad-bc}}}{ac}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x+a)^((a*d-2*b*c)/(-a*d+b*c))*(d*x+c)^((-2*a*d+b*c)/(a*d-b*c)),x)

[Out] 1/a/c*x*(b*x+a)^(1-(a*d-2*b*c)/(a*d-b*c))*(d*x+c)^(1-(2*a*d-b*c)/(a*d-b*c))

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(bx + a)^{\frac{2bc-ad}{bc-ad}} (dx + c)^{\frac{bc-2ad}{bc-ad}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)^((a*d-2*b*c)/(-a*d+b*c))*(d*x+c)^((-2*a*d+b*c)/(a*d-b*c)),x, algorithm="maxima")

[Out] integrate(1/((b*x + a)^((2*b*c - a*d)/(b*c - a*d))*(d*x + c)^((b*c - 2*a*d)/(b*c - a*d))), x)

mupad [B] time = 0.85, size = 142, normalized size = 1.46

$$\frac{\frac{x}{(a+bx)^{\frac{ad-2bc}{ad-bc}}} + \frac{x^2(ad+bc)}{ac(a+bx)^{\frac{ad-2bc}{ad-bc}}} + \frac{bdx^3}{ac(a+bx)^{\frac{ad-2bc}{ad-bc}}}}{(c+dx)^{\frac{2ad-bc}{ad-bc}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*x)^((a*d - 2*b*c)/(a*d - b*c))*(c + d*x)^((2*a*d - b*c)/(a*d - b*c))),x)

[Out] (x/(a + b*x)^((a*d - 2*b*c)/(a*d - b*c)) + (x^2*(a*d + b*c))/(a*c*(a + b*x)^((a*d - 2*b*c)/(a*d - b*c))) + (b*d*x^3)/(a*c*(a + b*x)^((a*d - 2*b*c)/(a*d - b*c)))/(c + d*x)^((2*a*d - b*c)/(a*d - b*c))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x+a)**((a*d-2*b*c)/(-a*d+b*c))*(d*x+c)**((-2*a*d+b*c)/(a*d-b*c)),x)

[Out] Timed out

$$3.1885 \quad \int \frac{(1-x)^n}{\sqrt{1+x}} dx$$

Optimal. Leaf size=30

$$2^{n+1}\sqrt{x+1} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; \frac{x+1}{2}\right)$$

[Out] $2^{(1+n)} \text{hypergeom}([1/2, -n], [3/2], 1/2+1/2*x) * (1+x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {69}

$$2^{n+1}\sqrt{x+1} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; \frac{x+1}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^n/Sqrt[1 + x], x]

[Out] $2^{(1+n)} \text{Sqrt}[1+x] \text{Hypergeometric2F1}[1/2, -n, 3/2, (1+x)/2]$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))])/(b*(m + 1)*(b/(b*c - a*d))^(n)), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rubi steps

$$\int \frac{(1-x)^n}{\sqrt{1+x}} dx = 2^{1+n}\sqrt{1+x} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; \frac{1+x}{2}\right)$$

Mathematica [A] time = 0.01, size = 30, normalized size = 1.00

$$2^{n+1}\sqrt{x+1} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; \frac{x+1}{2}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^n/Sqrt[1 + x], x]

[Out] $2^{(1+n)} \sqrt{1+x} \text{Hypergeometric2F1}\left[\frac{1}{2}, -n, \frac{3}{2}, \frac{(1+x)}{2}\right]$

fricas [F] time = 0.95, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(-x+1)^n}{\sqrt{x+1}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^n/(1+x)^(1/2),x, algorithm="fricas")`

[Out] `integral((-x + 1)^n/sqrt(x + 1), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x+1)^n}{\sqrt{x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^n/(1+x)^(1/2),x, algorithm="giac")`

[Out] `integrate((-x + 1)^n/sqrt(x + 1), x)`

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(-x+1)^n}{\sqrt{x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((-x+1)^n/(x+1)^(1/2),x)`

[Out] `int((-x+1)^n/(x+1)^(1/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(-x+1)^n}{\sqrt{x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1-x)^n/(1+x)^(1/2),x, algorithm="maxima")`

[Out] `integrate((-x + 1)^n/sqrt(x + 1), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(1-x)^n}{\sqrt{x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^n/(x + 1)^(1/2), x)

[Out] int((1 - x)^n/(x + 1)^(1/2), x)

sympy [C] time = 2.11, size = 29, normalized size = 0.97

$$2 \cdot 2^n \sqrt{x+1} {}_2F_1 \left(\begin{matrix} \frac{1}{2}, -n \\ \frac{3}{2} \end{matrix} \middle| \frac{(x+1)e^{2i\pi}}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**n/(1+x)**(1/2), x)

[Out] 2*2**n*sqrt(x + 1)*hyper((1/2, -n), (3/2,), (x + 1)*exp_polar(2*I*pi)/2)

$$3.1886 \quad \int \frac{(1+x)^n}{\sqrt{1-x}} dx$$

Optimal. Leaf size=35

$$-2^{n+1}\sqrt{1-x} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; \frac{1-x}{2}\right)$$

[Out] $-2^{(1+n)}*\text{hypergeom}([1/2, -n], [3/2], 1/2-1/2*x)*(1-x)^{(1/2)}$

Rubi [A] time = 0.01, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {69}

$$-2^{n+1}\sqrt{1-x} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; \frac{1-x}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[(1 + x)^n/Sqrt[1 - x], x]

[Out] $-(2^{(1+n)}*\text{Sqrt}[1-x]*\text{Hypergeometric2F1}[1/2, -n, 3/2, (1-x)/2])$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rubi steps

$$\int \frac{(1+x)^n}{\sqrt{1-x}} dx = -2^{1+n}\sqrt{1-x} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; \frac{1-x}{2}\right)$$

Mathematica [A] time = 0.01, size = 35, normalized size = 1.00

$$-2^{n+1}\sqrt{1-x} {}_2F_1\left(\frac{1}{2}, -n; \frac{3}{2}; \frac{1-x}{2}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 + x)^n/Sqrt[1 - x], x]

[Out] $-(2^{(1+n)}\sqrt{1-x}\text{Hypergeometric2F1}[1/2, -n, 3/2, (1-x)/2])$

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(-\frac{(x+1)^n\sqrt{-x+1}}{x-1}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)^n/(1-x)^(1/2),x, algorithm="fricas")`

[Out] `integral(-(x+1)^n*sqrt(-x+1)/(x-1), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(x+1)^n}{\sqrt{-x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)^n/(1-x)^(1/2),x, algorithm="giac")`

[Out] `integrate((x+1)^n/sqrt(-x+1), x)`

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(x+1)^n}{\sqrt{-x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((x+1)^n/(-x+1)^(1/2),x)`

[Out] `int((x+1)^n/(-x+1)^(1/2),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(x+1)^n}{\sqrt{-x+1}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((1+x)^n/(1-x)^(1/2),x, algorithm="maxima")`

[Out] `integrate((x+1)^n/sqrt(-x+1), x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{(x+1)^n}{\sqrt{1-x}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((x + 1)^n/(1 - x)^(1/2), x)

[Out] int((x + 1)^n/(1 - x)^(1/2), x)

sympy [C] time = 2.12, size = 31, normalized size = 0.89

$$-2 \cdot 2^n i \sqrt{x-1} {}_2F_1 \left(\begin{matrix} \frac{1}{2}, -n \\ \frac{3}{2} \end{matrix} \middle| \frac{(x-1)e^{i\pi}}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1+x)**n/(1-x)**(1/2), x)

[Out] -2*2**n*I*sqrt(x - 1)*hyper((1/2, -n), (3/2,), (x - 1)*exp_polar(I*pi)/2)

$$3.1887 \quad \int (1-x)^n (1+x)^{7/3} dx$$

Optimal. Leaf size=33

$$\frac{3}{5} 2^{n-1} (x+1)^{10/3} {}_2F_1\left(\frac{10}{3}, -n; \frac{13}{3}; \frac{x+1}{2}\right)$$

[Out] $3/5 * 2^{(-1+n)} * (1+x)^{(10/3)} * \text{hypergeom}([10/3, -n], [13/3], 1/2+1/2*x)$

Rubi [A] time = 0.01, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {69}

$$\frac{3}{5} 2^{n-1} (x+1)^{10/3} {}_2F_1\left(\frac{10}{3}, -n; \frac{13}{3}; \frac{x+1}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^n*(1 + x)^(7/3), x]

[Out] $(3 * 2^{(-1 + n)} * (1 + x)^{(10/3)} * \text{Hypergeometric2F1}[10/3, -n, 13/3, (1 + x)/2]) / 5$

Rule 69

```
Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((
a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c -
a*d))])/(b*(m + 1)*(b/(b*c - a*d))^(n)), x] /; FreeQ[{a, b, c, d, m, n}, x]
&& NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d)
, 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))
```

Rubi steps

$$\int (1-x)^n (1+x)^{7/3} dx = \frac{3}{5} 2^{-1+n} (1+x)^{10/3} {}_2F_1\left(\frac{10}{3}, -n; \frac{13}{3}; \frac{1+x}{2}\right)$$

Mathematica [A] time = 0.02, size = 33, normalized size = 1.00

$$\frac{3}{5} 2^{n-1} (x+1)^{10/3} {}_2F_1\left(\frac{10}{3}, -n; \frac{13}{3}; \frac{x+1}{2}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^n*(1 + x)^(7/3),x]

[Out] (3*2^(-1 + n)*(1 + x)^(10/3)*Hypergeometric2F1[10/3, -n, 13/3, (1 + x)/2])/5

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(x^2 + 2x + 1\right)(x + 1)^{\frac{1}{3}}(-x + 1)^n, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^n*(1+x)^(7/3),x, algorithm="fricas")

[Out] integral((x^2 + 2*x + 1)*(x + 1)^(1/3)*(-x + 1)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (x + 1)^{\frac{7}{3}}(-x + 1)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^n*(1+x)^(7/3),x, algorithm="giac")

[Out] integrate((x + 1)^(7/3)*(-x + 1)^n, x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (x + 1)^{\frac{7}{3}}(-x + 1)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^n*(x+1)^(7/3),x)

[Out] int((-x+1)^n*(x+1)^(7/3),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (x + 1)^{\frac{7}{3}}(-x + 1)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^n*(1+x)^(7/3),x, algorithm="maxima")

[Out] integrate((x + 1)^(7/3)*(-x + 1)^n, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int (1-x)^n (x+1)^{7/3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^n*(x + 1)^(7/3), x)

[Out] int((1 - x)^n*(x + 1)^(7/3), x)

sympy [C] time = 89.94, size = 37, normalized size = 1.12

$$\frac{2^n (x+1)^{\frac{10}{3}} \Gamma\left(\frac{10}{3}\right) {}_2F_1\left(\frac{10}{3}, -n \middle| \frac{(x+1)e^{2i\pi}}{2}\right)}{\Gamma\left(\frac{13}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**n*(1+x)**(7/3), x)

[Out] 2**n*(x + 1)**(10/3)*gamma(10/3)*hyper((10/3, -n), (13/3,), (x + 1)*exp_polar(2*I*pi)/2)/gamma(13/3)

$$3.1888 \quad \int (1-x)^{7/3} (1+x)^n dx$$

Optimal. Leaf size=37

$$-\frac{3}{5} 2^{n-1} (1-x)^{10/3} {}_2F_1\left(\frac{10}{3}, -n; \frac{13}{3}; \frac{1-x}{2}\right)$$

[Out] $-3/5*2^{(-1+n)}*(1-x)^{(10/3)}*\text{hypergeom}([10/3, -n], [13/3], 1/2-1/2*x)$

Rubi [A] time = 0.01, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {69}

$$-\frac{3}{5} 2^{n-1} (1-x)^{10/3} {}_2F_1\left(\frac{10}{3}, -n; \frac{13}{3}; \frac{1-x}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[(1 - x)^(7/3)*(1 + x)^n,x]

[Out] $(-3*2^{(-1+n)}*(1-x)^{(10/3)}*\text{Hypergeometric2F1}[10/3, -n, 13/3, (1-x)/2])/5$

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rubi steps

$$\int (1-x)^{7/3} (1+x)^n dx = -\frac{3}{5} 2^{-1+n} (1-x)^{10/3} {}_2F_1\left(\frac{10}{3}, -n; \frac{13}{3}; \frac{1-x}{2}\right)$$

Mathematica [A] time = 0.02, size = 37, normalized size = 1.00

$$-\frac{3}{5} 2^{n-1} (1-x)^{10/3} {}_2F_1\left(\frac{10}{3}, -n; \frac{13}{3}; \frac{1-x}{2}\right)$$

Antiderivative was successfully verified.

[In] Integrate[(1 - x)^(7/3)*(1 + x)^n,x]

[Out] $(-3 \cdot 2^{-(1+n)} \cdot (1-x)^{(10/3)} \cdot \text{Hypergeometric2F1}[10/3, -n, 13/3, (1-x)/2]) / 5$

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\left(x^2 - 2x + 1\right)(x + 1)^n(-x + 1)^{\frac{1}{3}}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/3)*(1+x)^n,x, algorithm="fricas")

[Out] integral((x^2 - 2*x + 1)*(x + 1)^n*(-x + 1)^(1/3), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (x + 1)^n (-x + 1)^{\frac{7}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/3)*(1+x)^n,x, algorithm="giac")

[Out] integrate((x + 1)^n*(-x + 1)^(7/3), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int (-x + 1)^{\frac{7}{3}} (x + 1)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-x+1)^(7/3)*(x+1)^n,x)

[Out] int((-x+1)^(7/3)*(x+1)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (x + 1)^n (-x + 1)^{\frac{7}{3}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)^(7/3)*(1+x)^n,x, algorithm="maxima")

[Out] integrate((x + 1)^n*(-x + 1)^(7/3), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.03

$$\int (1-x)^{7/3} (x+1)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((1 - x)^(7/3)*(x + 1)^n,x)

[Out] int((1 - x)^(7/3)*(x + 1)^n, x)

sympy [C] time = 90.09, size = 42, normalized size = 1.14

$$\frac{\sqrt[3]{-1} \cdot 2^n (x-1)^{\frac{10}{3}} \Gamma\left(\frac{10}{3}\right) {}_2F_1\left(\frac{10}{3}, -n \middle| \frac{(x-1)e^{i\pi}}{2}\right)}{\Gamma\left(\frac{13}{3}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((1-x)**(7/3)*(1+x)**n,x)

[Out] (-1)**(1/3)*2**n*(x - 1)**(10/3)*gamma(10/3)*hyper((10/3, -n), (13/3,), (x - 1)*exp_polar(I*pi)/2)/gamma(13/3)

3.1889 $\int (1 + 2x)^{-m} (2 + 3x)^m dx$

Optimal. Leaf size=47

$$\frac{2^{-m-1}(2x+1)^{1-m} {}_2F_1(1-m, -m; 2-m; -3(2x+1))}{1-m}$$

[Out] $2^{(-1-m)}*(1+2*x)^{(1-m)}*\text{hypergeom}([-m, 1-m], [2-m], -3-6*x)/(1-m)$

Rubi [A] time = 0.01, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {69}

$$\frac{2^{-m-1}(2x+1)^{1-m} {}_2F_1(1-m, -m; 2-m; -3(2x+1))}{1-m}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(2 + 3*x)^m/(1 + 2*x)^m, x]$

[Out] $(2^{(-1-m)}*(1+2*x)^{(1-m)}*\text{Hypergeometric2F1}[1-m, -m, 2-m, -3*(1+2*x)])/(1-m)$

Rule 69

$\text{Int}[(a_ + (b_)*(x_))^{(m_)}*((c_ + (d_)*(x_))^{(n_)}), x_Symbol] :> \text{Simp}[(a + b*x)^{(m+1)}*\text{Hypergeometric2F1}[-n, m+1, m+2, -((d*(a+b*x))/(b*c-a*d))]/(b*(m+1)*(b/(b*c-a*d))^{(n)}), x] /;$ FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rubi steps

$$\int (1 + 2x)^{-m} (2 + 3x)^m dx = \frac{2^{-1-m}(1 + 2x)^{1-m} {}_2F_1(1-m, -m; 2-m; -3(1 + 2x))}{1-m}$$

Mathematica [A] time = 0.02, size = 47, normalized size = 1.00

$$\frac{2^{-m-1}(2x+1)^{1-m} {}_2F_1(1-m, -m; 2-m; -3(2x+1))}{1-m}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(2 + 3*x)^m/(1 + 2*x)^m, x]$

[Out] $(2^{(-1 - m)}(1 + 2x)^{(1 - m)}\text{Hypergeometric2F1}[1 - m, -m, 2 - m, -3*(1 + 2*x)])/(1 - m)$

fricas [F] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(3x + 2)^m}{(2x + 1)^m}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((2+3*x)^m/((1+2*x)^m),x, algorithm="fricas")`

[Out] `integral((3*x + 2)^m/(2*x + 1)^m, x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(3x + 2)^m}{(2x + 1)^m} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((2+3*x)^m/((1+2*x)^m),x, algorithm="giac")`

[Out] `integrate((3*x + 2)^m/(2*x + 1)^m, x)`

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int (2x + 1)^{-m} (3x + 2)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((3*x+2)^m/((2*x+1)^m),x)`

[Out] `int((3*x+2)^m/((2*x+1)^m),x)`

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(3x + 2)^m}{(2x + 1)^m} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((2+3*x)^m/((1+2*x)^m),x, algorithm="maxima")`

[Out] `integrate((3*x + 2)^m/(2*x + 1)^m, x)`

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{(3x+2)^m}{(2x+1)^m} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((3*x + 2)^m/(2*x + 1)^m,x)

[Out] int((3*x + 2)^m/(2*x + 1)^m, x)

sympy [C] time = 25.03, size = 42, normalized size = 0.89

$$\frac{3^{2m} \left(x + \frac{2}{3}\right) \left(x + \frac{2}{3}\right)^m e^{-i\pi m} \Gamma(m+1) {}_2F_1\left(\begin{matrix} m, m+1 \\ m+2 \end{matrix} \middle| 6x+4\right)}{\Gamma(m+2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((2+3*x)**m/((1+2*x)**m),x)

[Out] 3**(2*m)*(x + 2/3)*(x + 2/3)**m*exp(-I*pi*m)*gamma(m + 1)*hyper((m, m + 1), (m + 2,), 6*x + 4)/gamma(m + 2)

$$3.1890 \quad \int \left(\frac{d(a+bx)}{-bc+ad} \right)^m (c+dx)^n dx$$

Optimal. Leaf size=45

$$\frac{(c+dx)^{n+1} {}_2F_1\left(-m, n+1; n+2; \frac{b(c+dx)}{bc-ad}\right)}{d(n+1)}$$

[Out] (d*x+c)^(1+n)*hypergeom([-m, 1+n], [2+n], b*(d*x+c)/(-a*d+b*c))/d/(1+n)

Rubi [A] time = 0.02, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 27, $\frac{\text{number of rules}}{\text{integrand size}} = 0.074$, Rules used = {186, 69}

$$\frac{(c+dx)^{n+1} {}_2F_1\left(-m, n+1; n+2; \frac{b(c+dx)}{bc-ad}\right)}{d(n+1)}$$

Antiderivative was successfully verified.

[In] Int[((d*(a + b*x))/(-b*c) + a*d))^m*(c + d*x)^n,x]

[Out] ((c + d*x)^(1 + n)*Hypergeometric2F1[-m, 1 + n, 2 + n, (b*(c + d*x))/(b*c - a*d)])/(d*(1 + n))

Rule 69

Int[((a_) + (b_.)*(x_))^(m_)*((c_) + (d_.)*(x_))^(n_), x_Symbol] := Simp[((a + b*x)^(m + 1)*Hypergeometric2F1[-n, m + 1, m + 2, -((d*(a + b*x))/(b*c - a*d))]/(b*(m + 1)*(b/(b*c - a*d))^n), x] /; FreeQ[{a, b, c, d, m, n}, x] && NeQ[b*c - a*d, 0] && !IntegerQ[m] && !IntegerQ[n] && GtQ[b/(b*c - a*d), 0] && (RationalQ[m] || !(RationalQ[n] && GtQ[-(d/(b*c - a*d)), 0]))

Rule 186

Int[(u_)^(m_.)*(v_)^(n_.), x_Symbol] := Int[ExpandToSum[u, x]^m*ExpandToSum[v, x]^n, x] /; FreeQ[{m, n}, x] && LinearQ[{u, v}, x] && !LinearMatchQ[{u, v}, x]

Rubi steps

$$\int \left(\frac{d(a+bx)}{-bc+ad} \right)^m (c+dx)^n dx = \int (c+dx)^n \left(-\frac{ad}{bc-ad} - \frac{bdx}{bc-ad} \right)^m dx$$

$$= \frac{(c+dx)^{1+n} {}_2F_1 \left(-m, 1+n; 2+n; \frac{b(c+dx)}{bc-ad} \right)}{d(1+n)}$$

Mathematica [A] time = 0.04, size = 88, normalized size = 1.96

$$\frac{(a+bx)(c+dx)^n \left(\frac{d(a+bx)}{ad-bc} \right)^m \left(\frac{b(c+dx)}{bc-ad} \right)^{-n} {}_2F_1 \left(m+1, -n; m+2; \frac{d(a+bx)}{ad-bc} \right)}{b(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[((d*(a + b*x))/(-(b*c) + a*d))^m*(c + d*x)^n,x]

[Out] ((a + b*x)*((d*(a + b*x))/(-(b*c) + a*d))^m*(c + d*x)^n*Hypergeometric2F1[1 + m, -n, 2 + m, (d*(a + b*x))/(-(b*c) + a*d)]/(b*(1 + m)*((b*(c + d*x))/(b*c - a*d))^n)

fricas [F] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral} \left((dx + c)^n \left(-\frac{bdx + ad}{bc - ad} \right)^m, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*(b*x+a)/(a*d-b*c))^m*(d*x+c)^n,x, algorithm="fricas")

[Out] integral((d*x + c)^n*(-(b*d*x + a*d)/(b*c - a*d))^m, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx + c)^n \left(-\frac{(bx + a)d}{bc - ad} \right)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*(b*x+a)/(a*d-b*c))^m*(d*x+c)^n,x, algorithm="giac")

[Out] integrate((d*x + c)^n*(-(b*x + a)*d/(b*c - a*d))^m, x)

maple [F] time = 0.15, size = 0, normalized size = 0.00

$$\int \left(\frac{(bx+a)d}{ad-bc} \right)^m (dx+c)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*(b*x+a)/(a*d-b*c))^m*(d*x+c)^n,x)

[Out] int((d*(b*x+a)/(a*d-b*c))^m*(d*x+c)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx+c)^n \left(-\frac{(bx+a)d}{bc-ad} \right)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*(b*x+a)/(a*d-b*c))^m*(d*x+c)^n,x, algorithm="maxima")

[Out] integrate((d*x+c)^n*(-(b*x+a)*d/(b*c-a*d))^m,x)

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int (c+dx)^n \left(\frac{d(a+bx)}{ad-bc} \right)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c+d*x)^n*((d*(a+b*x))/(a*d-b*c))^m,x)

[Out] int((c+d*x)^n*((d*(a+b*x))/(a*d-b*c))^m,x)

sympy [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*(b*x+a)/(a*d-b*c))^m*(d*x+c)^n,x)

[Out] Exception raised: HeuristicGCDFailed

3.1891 $\int (a + bx + cx^2 + dx^3) dx$

Optimal. Leaf size=28

$$ax + \frac{bx^2}{2} + \frac{cx^3}{3} + \frac{dx^4}{4}$$

[Out] a*x+1/2*b*x^2+1/3*c*x^3+1/4*d*x^4

Rubi [A] time = 0.00, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$ax + \frac{bx^2}{2} + \frac{cx^3}{3} + \frac{dx^4}{4}$$

Antiderivative was successfully verified.

[In] Int[a + b*x + c*x^2 + d*x^3, x]

[Out] a*x + (b*x^2)/2 + (c*x^3)/3 + (d*x^4)/4

Rubi steps

$$\int (a + bx + cx^2 + dx^3) dx = ax + \frac{bx^2}{2} + \frac{cx^3}{3} + \frac{dx^4}{4}$$

Mathematica [A] time = 0.00, size = 28, normalized size = 1.00

$$ax + \frac{bx^2}{2} + \frac{cx^3}{3} + \frac{dx^4}{4}$$

Antiderivative was successfully verified.

[In] Integrate[a + b*x + c*x^2 + d*x^3, x]

[Out] a*x + (b*x^2)/2 + (c*x^3)/3 + (d*x^4)/4

fricas [A] time = 0.39, size = 22, normalized size = 0.79

$$\frac{1}{4}x^4d + \frac{1}{3}x^3c + \frac{1}{2}x^2b + xa$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(d*x^3+c*x^2+b*x+a,x, algorithm="fricas")

[Out] $1/4*x^4*d + 1/3*x^3*c + 1/2*x^2*b + x*a$

giac [A] time = 1.01, size = 22, normalized size = 0.79

$$\frac{1}{4}dx^4 + \frac{1}{3}cx^3 + \frac{1}{2}bx^2 + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(d*x^3+c*x^2+b*x+a,x, algorithm="giac")`

[Out] $1/4*d*x^4 + 1/3*c*x^3 + 1/2*b*x^2 + a*x$

maple [A] time = 0.00, size = 23, normalized size = 0.82

$$\frac{1}{4}dx^4 + \frac{1}{3}cx^3 + \frac{1}{2}bx^2 + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(d*x^3+c*x^2+b*x+a,x)`

[Out] $a*x+1/2*b*x^2+1/3*c*x^3+1/4*d*x^4$

maxima [A] time = 1.07, size = 22, normalized size = 0.79

$$\frac{1}{4}dx^4 + \frac{1}{3}cx^3 + \frac{1}{2}bx^2 + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(d*x^3+c*x^2+b*x+a,x, algorithm="maxima")`

[Out] $1/4*d*x^4 + 1/3*c*x^3 + 1/2*b*x^2 + a*x$

mupad [B] time = 0.04, size = 22, normalized size = 0.79

$$\frac{dx^4}{4} + \frac{cx^3}{3} + \frac{bx^2}{2} + ax$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(a + b*x + c*x^2 + d*x^3,x)`

[Out] $a*x + (b*x^2)/2 + (c*x^3)/3 + (d*x^4)/4$

sympy [A] time = 0.06, size = 22, normalized size = 0.79

$$ax + \frac{bx^2}{2} + \frac{cx^3}{3} + \frac{dx^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(d*x**3+c*x**2+b*x+a,x)
```

```
[Out] a*x + b*x**2/2 + c*x**3/3 + d*x**4/4
```

$$3.1892 \quad \int (-x^3 + x^4) dx$$

Optimal. Leaf size=15

$$\frac{x^5}{5} - \frac{x^4}{4}$$

[Out] $-1/4*x^4+1/5*x^5$

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{x^5}{5} - \frac{x^4}{4}$$

Antiderivative was successfully verified.

[In] Int[-x^3 + x^4, x]

[Out] $-x^4/4 + x^5/5$

Rubi steps

$$\int (-x^3 + x^4) dx = -\frac{x^4}{4} + \frac{x^5}{5}$$

Mathematica [A] time = 0.00, size = 15, normalized size = 1.00

$$\frac{x^5}{5} - \frac{x^4}{4}$$

Antiderivative was successfully verified.

[In] Integrate[-x^3 + x^4, x]

[Out] $-1/4*x^4 + x^5/5$

fricas [A] time = 0.38, size = 11, normalized size = 0.73

$$\frac{1}{5}x^5 - \frac{1}{4}x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4-x^3,x, algorithm="fricas")

[Out] $1/5*x^5 - 1/4*x^4$

giac [A] time = 1.08, size = 11, normalized size = 0.73

$$\frac{1}{5}x^5 - \frac{1}{4}x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4-x^3,x, algorithm="giac")`

[Out] $1/5*x^5 - 1/4*x^4$

maple [A] time = 0.00, size = 12, normalized size = 0.80

$$\frac{1}{5}x^5 - \frac{1}{4}x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^4-x^3,x)`

[Out] $-1/4*x^4+1/5*x^5$

maxima [A] time = 1.08, size = 11, normalized size = 0.73

$$\frac{1}{5}x^5 - \frac{1}{4}x^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4-x^3,x, algorithm="maxima")`

[Out] $1/5*x^5 - 1/4*x^4$

mupad [B] time = 0.02, size = 10, normalized size = 0.67

$$\frac{x^4 (4x - 5)}{20}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^4 - x^3,x)`

[Out] $(x^4*(4*x - 5))/20$

sympy [A] time = 0.05, size = 8, normalized size = 0.53

$$\frac{x^5}{5} - \frac{x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4-x**3,x)
```

```
[Out] x**5/5 - x**4/4
```

3.1893

$$\int (-1 + x^5) dx$$

Optimal. Leaf size=11

$$\frac{x^6}{6} - x$$

[Out] -x+1/6*x^6

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{x^6}{6} - x$$

Antiderivative was successfully verified.

[In] Int[-1 + x^5,x]

[Out] -x + x^6/6

Rubi steps

$$\int (-1 + x^5) dx = -x + \frac{x^6}{6}$$

Mathematica [A] time = 0.00, size = 11, normalized size = 1.00

$$\frac{x^6}{6} - x$$

Antiderivative was successfully verified.

[In] Integrate[-1 + x^5,x]

[Out] -x + x^6/6

fricas [A] time = 0.38, size = 9, normalized size = 0.82

$$\frac{1}{6}x^6 - x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5-1,x, algorithm="fricas")

[Out] $1/6*x^6 - x$

giac [A] time = 0.94, size = 9, normalized size = 0.82

$$\frac{1}{6}x^6 - x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^5-1,x, algorithm="giac")`

[Out] $1/6*x^6 - x$

maple [A] time = 0.00, size = 10, normalized size = 0.91

$$\frac{1}{6}x^6 - x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^5-1,x)`

[Out] $-x+1/6*x^6$

maxima [A] time = 0.96, size = 9, normalized size = 0.82

$$\frac{1}{6}x^6 - x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^5-1,x, algorithm="maxima")`

[Out] $1/6*x^6 - x$

mupad [B] time = 0.02, size = 8, normalized size = 0.73

$$\frac{x(x^5 - 6)}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^5 - 1,x)`

[Out] $(x*(x^5 - 6))/6$

sympy [A] time = 0.05, size = 5, normalized size = 0.45

$$\frac{x^6}{6} - x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5-1,x)
```

```
[Out] x**6/6 - x
```

3.1894 $\int (7 + 4x) dx$

Optimal. Leaf size=9

$$2x^2 + 7x$$

[Out] $2*x^2+7*x$

Rubi [A] time = 0.00, antiderivative size = 9, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 5, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$2x^2 + 7x$$

Antiderivative was successfully verified.

[In] `Int[7 + 4*x, x]`

[Out] $7*x + 2*x^2$

Rubi steps

$$\int (7 + 4x) dx = 7x + 2x^2$$

Mathematica [A] time = 0.00, size = 9, normalized size = 1.00

$$2x^2 + 7x$$

Antiderivative was successfully verified.

[In] `Integrate[7 + 4*x, x]`

[Out] $7*x + 2*x^2$

fricas [A] time = 0.42, size = 9, normalized size = 1.00

$$2x^2 + 7x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(7+4*x, x, algorithm="fricas")`

[Out] $2*x^2 + 7*x$

giac [A] time = 0.96, size = 9, normalized size = 1.00

$$2x^2 + 7x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(7+4*x,x, algorithm="giac")

[Out] 2*x^2 + 7*x

maple [A] time = 0.00, size = 10, normalized size = 1.11

$$2x^2 + 7x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(7+4*x,x)

[Out] 2*x^2+7*x

maxima [A] time = 1.01, size = 9, normalized size = 1.00

$$2x^2 + 7x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(7+4*x,x, algorithm="maxima")

[Out] 2*x^2 + 7*x

mupad [B] time = 0.03, size = 7, normalized size = 0.78

$$x(2x + 7)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(4*x + 7,x)

[Out] x*(2*x + 7)

sympy [A] time = 0.05, size = 7, normalized size = 0.78

$$2x^2 + 7x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(7+4*x,x)

[Out] 2*x**2 + 7*x

3.1895

$$\int (4x + \pi x^3) dx$$

Optimal. Leaf size=14

$$\frac{\pi x^4}{4} + 2x^2$$

[Out] 2*x^2+1/4*Pi*x^4

Rubi [A] time = 0.00, antiderivative size = 14, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{\pi x^4}{4} + 2x^2$$

Antiderivative was successfully verified.

[In] Int[4*x + Pi*x^3,x]

[Out] 2*x^2 + (Pi*x^4)/4

Rubi steps

$$\int (4x + \pi x^3) dx = 2x^2 + \frac{\pi x^4}{4}$$

Mathematica [A] time = 0.00, size = 14, normalized size = 1.00

$$\frac{\pi x^4}{4} + 2x^2$$

Antiderivative was successfully verified.

[In] Integrate[4*x + Pi*x^3,x]

[Out] 2*x^2 + (Pi*x^4)/4

fricas [A] time = 0.43, size = 12, normalized size = 0.86

$$\frac{1}{4} \pi x^4 + 2x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(pi*x^3+4*x,x, algorithm="fricas")

[Out] $1/4*\pi*x^4 + 2*x^2$

giac [A] time = 1.06, size = 12, normalized size = 0.86

$$\frac{1}{4} \pi x^4 + 2 x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(pi*x^3+4*x,x, algorithm="giac")`

[Out] $1/4*\pi*x^4 + 2*x^2$

maple [A] time = 0.00, size = 13, normalized size = 0.93

$$\frac{1}{4} \pi x^4 + 2 x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(Pi*x^3+4*x,x)`

[Out] $2*x^2+1/4*Pi*x^4$

maxima [A] time = 1.00, size = 12, normalized size = 0.86

$$\frac{1}{4} \pi x^4 + 2 x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(pi*x^3+4*x,x, algorithm="maxima")`

[Out] $1/4*\pi*x^4 + 2*x^2$

mupad [B] time = 0.02, size = 12, normalized size = 0.86

$$\frac{\Pi x^4}{4} + 2 x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(4*x + Pi*x^3,x)`

[Out] $(\pi*x^4)/4 + 2*x^2$

sympy [A] time = 0.06, size = 10, normalized size = 0.71

$$\frac{\pi x^4}{4} + 2 x^2$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(pi*x**3+4*x,x)
```

```
[Out] pi*x**4/4 + 2*x**2
```

3.1896 $\int (2x + 5x^2) dx$

Optimal. Leaf size=11

$$\frac{5x^3}{3} + x^2$$

[Out] $x^2 + 5/3*x^3$

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{5x^3}{3} + x^2$$

Antiderivative was successfully verified.

[In] Int[2*x + 5*x^2,x]

[Out] $x^2 + (5*x^3)/3$

Rubi steps

$$\int (2x + 5x^2) dx = x^2 + \frac{5x^3}{3}$$

Mathematica [A] time = 0.00, size = 11, normalized size = 1.00

$$\frac{5x^3}{3} + x^2$$

Antiderivative was successfully verified.

[In] Integrate[2*x + 5*x^2,x]

[Out] $x^2 + (5*x^3)/3$

fricas [A] time = 0.40, size = 9, normalized size = 0.82

$$\frac{5}{3}x^3 + x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(5*x^2+2*x,x, algorithm="fricas")

[Out] $5/3*x^3 + x^2$

giac [A] time = 1.10, size = 9, normalized size = 0.82

$$\frac{5}{3}x^3 + x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(5*x^2+2*x,x, algorithm="giac")`

[Out] $5/3*x^3 + x^2$

maple [A] time = 0.00, size = 10, normalized size = 0.91

$$\frac{5}{3}x^3 + x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(5*x^2+2*x,x)`

[Out] $x^2+5/3*x^3$

maxima [A] time = 1.10, size = 9, normalized size = 0.82

$$\frac{5}{3}x^3 + x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(5*x^2+2*x,x, algorithm="maxima")`

[Out] $5/3*x^3 + x^2$

mupad [B] time = 0.02, size = 10, normalized size = 0.91

$$\frac{x^2 (5x + 3)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(2*x + 5*x^2,x)`

[Out] $(x^2*(5*x + 3))/3$

sympy [A] time = 0.05, size = 8, normalized size = 0.73

$$\frac{5x^3}{3} + x^2$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(5*x**2+2*x,x)
```

```
[Out] 5*x**3/3 + x**2
```

$$3.1897 \quad \int \left(\frac{x^2}{2} + \frac{x^3}{3} \right) dx$$

Optimal. Leaf size=15

$$\frac{x^4}{12} + \frac{x^3}{6}$$

[Out] 1/6*x^3+1/12*x^4

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{x^4}{12} + \frac{x^3}{6}$$

Antiderivative was successfully verified.

[In] Int[x^2/2 + x^3/3,x]

[Out] x^3/6 + x^4/12

Rubi steps

$$\int \left(\frac{x^2}{2} + \frac{x^3}{3} \right) dx = \frac{x^3}{6} + \frac{x^4}{12}$$

Mathematica [A] time = 0.00, size = 15, normalized size = 1.00

$$\frac{x^4}{12} + \frac{x^3}{6}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/2 + x^3/3,x]

[Out] x^3/6 + x^4/12

fricas [A] time = 0.40, size = 11, normalized size = 0.73

$$\frac{1}{12}x^4 + \frac{1}{6}x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/2*x^2+1/3*x^3,x, algorithm="fricas")

[Out] $1/12*x^4 + 1/6*x^3$

giac [A] time = 0.89, size = 11, normalized size = 0.73

$$\frac{1}{12}x^4 + \frac{1}{6}x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/2*x^2+1/3*x^3,x, algorithm="giac")`

[Out] $1/12*x^4 + 1/6*x^3$

maple [A] time = 0.00, size = 12, normalized size = 0.80

$$\frac{1}{12}x^4 + \frac{1}{6}x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/2*x^2+1/3*x^3,x)`

[Out] $1/6*x^3+1/12*x^4$

maxima [A] time = 1.05, size = 11, normalized size = 0.73

$$\frac{1}{12}x^4 + \frac{1}{6}x^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/2*x^2+1/3*x^3,x, algorithm="maxima")`

[Out] $1/12*x^4 + 1/6*x^3$

mupad [B] time = 0.02, size = 8, normalized size = 0.53

$$\frac{x^3 (x + 2)}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2/2 + x^3/3,x)`

[Out] $(x^3*(x + 2))/12$

sympy [A] time = 0.06, size = 8, normalized size = 0.53

$$\frac{x^4}{12} + \frac{x^3}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/2*x**2+1/3*x**3,x)
```

```
[Out] x**4/12 + x**3/6
```

3.1898

$$\int (3 - 5x + 2x^2) dx$$

Optimal. Leaf size=18

$$\frac{2x^3}{3} - \frac{5x^2}{2} + 3x$$

[Out] 3*x-5/2*x^2+2/3*x^3

Rubi [A] time = 0.00, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{2x^3}{3} - \frac{5x^2}{2} + 3x$$

Antiderivative was successfully verified.

[In] Int[3 - 5*x + 2*x^2, x]

[Out] 3*x - (5*x^2)/2 + (2*x^3)/3

Rubi steps

$$\int (3 - 5x + 2x^2) dx = 3x - \frac{5x^2}{2} + \frac{2x^3}{3}$$

Mathematica [A] time = 0.00, size = 18, normalized size = 1.00

$$\frac{2x^3}{3} - \frac{5x^2}{2} + 3x$$

Antiderivative was successfully verified.

[In] Integrate[3 - 5*x + 2*x^2, x]

[Out] 3*x - (5*x^2)/2 + (2*x^3)/3

fricas [A] time = 0.37, size = 14, normalized size = 0.78

$$\frac{2}{3}x^3 - \frac{5}{2}x^2 + 3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(2*x^2-5*x+3,x, algorithm="fricas")

[Out] $\frac{2}{3}x^3 - \frac{5}{2}x^2 + 3x$

giac [A] time = 0.85, size = 14, normalized size = 0.78

$$\frac{2}{3}x^3 - \frac{5}{2}x^2 + 3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(2*x^2-5*x+3,x, algorithm="giac")`

[Out] $\frac{2}{3}x^3 - \frac{5}{2}x^2 + 3x$

maple [A] time = 0.00, size = 15, normalized size = 0.83

$$\frac{2}{3}x^3 - \frac{5}{2}x^2 + 3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(2*x^2-5*x+3,x)`

[Out] $3x - \frac{5}{2}x^2 + \frac{2}{3}x^3$

maxima [A] time = 0.97, size = 14, normalized size = 0.78

$$\frac{2}{3}x^3 - \frac{5}{2}x^2 + 3x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(2*x^2-5*x+3,x, algorithm="maxima")`

[Out] $\frac{2}{3}x^3 - \frac{5}{2}x^2 + 3x$

mupad [B] time = 0.02, size = 13, normalized size = 0.72

$$\frac{x(4x^2 - 15x + 18)}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(2*x^2 - 5*x + 3,x)`

[Out] $(x*(4*x^2 - 15*x + 18))/6$

sympy [A] time = 0.06, size = 15, normalized size = 0.83

$$\frac{2x^3}{3} - \frac{5x^2}{2} + 3x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(2*x**2-5*x+3,x)
```

```
[Out] 2*x**3/3 - 5*x**2/2 + 3*x
```

$$3.1899 \quad \int (-2x + x^2 + x^3) dx$$

Optimal. Leaf size=20

$$\frac{x^4}{4} + \frac{x^3}{3} - x^2$$

[Out] $-x^2 + 1/3*x^3 + 1/4*x^4$

Rubi [A] time = 0.00, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{x^4}{4} + \frac{x^3}{3} - x^2$$

Antiderivative was successfully verified.

[In] Int[-2*x + x^2 + x^3, x]

[Out] $-x^2 + x^3/3 + x^4/4$

Rubi steps

$$\int (-2x + x^2 + x^3) dx = -x^2 + \frac{x^3}{3} + \frac{x^4}{4}$$

Mathematica [A] time = 0.00, size = 20, normalized size = 1.00

$$\frac{x^4}{4} + \frac{x^3}{3} - x^2$$

Antiderivative was successfully verified.

[In] Integrate[-2*x + x^2 + x^3, x]

[Out] $-x^2 + x^3/3 + x^4/4$

fricas [A] time = 0.38, size = 16, normalized size = 0.80

$$\frac{1}{4}x^4 + \frac{1}{3}x^3 - x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3+x^2-2*x,x, algorithm="fricas")

[Out] $1/4*x^4 + 1/3*x^3 - x^2$

giac [A] time = 1.10, size = 16, normalized size = 0.80

$$\frac{1}{4}x^4 + \frac{1}{3}x^3 - x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3+x^2-2*x,x, algorithm="giac")`

[Out] $1/4*x^4 + 1/3*x^3 - x^2$

maple [A] time = 0.00, size = 17, normalized size = 0.85

$$\frac{1}{4}x^4 + \frac{1}{3}x^3 - x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^3+x^2-2*x,x)`

[Out] $-x^2+1/3*x^3+1/4*x^4$

maxima [A] time = 0.97, size = 16, normalized size = 0.80

$$\frac{1}{4}x^4 + \frac{1}{3}x^3 - x^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^3+x^2-2*x,x, algorithm="maxima")`

[Out] $1/4*x^4 + 1/3*x^3 - x^2$

mupad [B] time = 0.03, size = 15, normalized size = 0.75

$$\frac{x^2 (3x^2 + 4x - 12)}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2 - 2*x + x^3,x)`

[Out] $(x^2*(4*x + 3*x^2 - 12))/12$

sympy [A] time = 0.05, size = 12, normalized size = 0.60

$$\frac{x^4}{4} + \frac{x^3}{3} - x^2$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3+x**2-2*x,x)
```

```
[Out] x**4/4 + x**3/3 - x**2
```

$$3.1900 \quad \int (1 - x^2 - 3x^5) dx$$

Optimal. Leaf size=16

$$-\frac{x^6}{2} - \frac{x^3}{3} + x$$

[Out] $x - \frac{1}{3}x^3 - \frac{1}{2}x^6$

Rubi [A] time = 0.00, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$-\frac{x^6}{2} - \frac{x^3}{3} + x$$

Antiderivative was successfully verified.

[In] `Int[1 - x^2 - 3*x^5, x]`

[Out] $x - x^3/3 - x^6/2$

Rubi steps

$$\int (1 - x^2 - 3x^5) dx = x - \frac{x^3}{3} - \frac{x^6}{2}$$

Mathematica [A] time = 0.00, size = 16, normalized size = 1.00

$$-\frac{x^6}{2} - \frac{x^3}{3} + x$$

Antiderivative was successfully verified.

[In] `Integrate[1 - x^2 - 3*x^5, x]`

[Out] $x - x^3/3 - x^6/2$

fricas [A] time = 0.39, size = 12, normalized size = 0.75

$$-\frac{1}{2}x^6 - \frac{1}{3}x^3 + x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-3*x^5-x^2+1,x, algorithm="fricas")`

[Out] $-1/2*x^6 - 1/3*x^3 + x$

giac [A] time = 0.96, size = 12, normalized size = 0.75

$$-\frac{1}{2}x^6 - \frac{1}{3}x^3 + x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-3*x^5-x^2+1,x, algorithm="giac")`

[Out] $-1/2*x^6 - 1/3*x^3 + x$

maple [A] time = 0.00, size = 13, normalized size = 0.81

$$-\frac{1}{2}x^6 - \frac{1}{3}x^3 + x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-3*x^5-x^2+1,x)`

[Out] $x-1/3*x^3-1/2*x^6$

maxima [A] time = 0.98, size = 12, normalized size = 0.75

$$-\frac{1}{2}x^6 - \frac{1}{3}x^3 + x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-3*x^5-x^2+1,x, algorithm="maxima")`

[Out] $-1/2*x^6 - 1/3*x^3 + x$

mupad [B] time = 0.02, size = 12, normalized size = 0.75

$$-\frac{x^6}{2} - \frac{x^3}{3} + x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1 - 3*x^5 - x^2,x)`

[Out] $x - x^3/3 - x^6/2$

sympy [A] time = 0.06, size = 10, normalized size = 0.62

$$-\frac{x^6}{2} - \frac{x^3}{3} + x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-3*x**5-x**2+1,x)
```

```
[Out] -x**6/2 - x**3/3 + x
```


$$3.1901 \quad \int (5 + 2x + 3x^2 + 4x^3) dx$$

Optimal. Leaf size=13

$$x^4 + x^3 + x^2 + 5x$$

[Out] $x^4+x^3+x^2+5*x$

Rubi [A] time = 0.00, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$x^4 + x^3 + x^2 + 5x$$

Antiderivative was successfully verified.

[In] Int[5 + 2*x + 3*x^2 + 4*x^3, x]

[Out] 5*x + x^2 + x^3 + x^4

Rubi steps

$$\int (5 + 2x + 3x^2 + 4x^3) dx = 5x + x^2 + x^3 + x^4$$

Mathematica [A] time = 0.00, size = 13, normalized size = 1.00

$$x^4 + x^3 + x^2 + 5x$$

Antiderivative was successfully verified.

[In] Integrate[5 + 2*x + 3*x^2 + 4*x^3, x]

[Out] 5*x + x^2 + x^3 + x^4

fricas [A] time = 0.38, size = 13, normalized size = 1.00

$$x^4 + x^3 + x^2 + 5x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(4*x^3+3*x^2+2*x+5,x, algorithm="fricas")

[Out] $x^4 + x^3 + x^2 + 5*x$

giac [A] time = 1.00, size = 13, normalized size = 1.00

$$x^4 + x^3 + x^2 + 5x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(4*x^3+3*x^2+2*x+5,x, algorithm="giac")

[Out] x^4 + x^3 + x^2 + 5*x

maple [A] time = 0.00, size = 14, normalized size = 1.08

$$x^4 + x^3 + x^2 + 5x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(4*x^3+3*x^2+2*x+5,x)

[Out] x^4+x^3+x^2+5*x

maxima [A] time = 1.14, size = 13, normalized size = 1.00

$$x^4 + x^3 + x^2 + 5x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(4*x^3+3*x^2+2*x+5,x, algorithm="maxima")

[Out] x^4 + x^3 + x^2 + 5*x

mupad [B] time = 0.03, size = 13, normalized size = 1.00

$$x^4 + x^3 + x^2 + 5x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(2*x + 3*x^2 + 4*x^3 + 5,x)

[Out] 5*x + x^2 + x^3 + x^4

sympy [A] time = 0.06, size = 12, normalized size = 0.92

$$x^4 + x^3 + x^2 + 5x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(4*x**3+3*x**2+2*x+5,x)

[Out] x**4 + x**3 + x**2 + 5*x

$$3.1902 \quad \int \left(a + \frac{d}{x^3} + \frac{c}{x^2} + \frac{b}{x} \right) dx$$

Optimal. Leaf size=22

$$ax + b \log(x) - \frac{c}{x} - \frac{d}{2x^2}$$

[Out] $-1/2*d/x^2 - c/x + a*x + b*\ln(x)$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$ax + b \log(x) - \frac{c}{x} - \frac{d}{2x^2}$$

Antiderivative was successfully verified.

[In] Int[a + d/x^3 + c/x^2 + b/x, x]

[Out] $-d/(2*x^2) - c/x + a*x + b*\text{Log}[x]$

Rubi steps

$$\int \left(a + \frac{d}{x^3} + \frac{c}{x^2} + \frac{b}{x} \right) dx = -\frac{d}{2x^2} - \frac{c}{x} + ax + b \log(x)$$

Mathematica [A] time = 0.01, size = 22, normalized size = 1.00

$$ax + b \log(x) - \frac{c}{x} - \frac{d}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[a + d/x^3 + c/x^2 + b/x, x]

[Out] $-1/2*d/x^2 - c/x + a*x + b*\text{Log}[x]$

fricas [A] time = 0.44, size = 27, normalized size = 1.23

$$\frac{2ax^3 + 2bx^2 \log(x) - 2cx - d}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(a+d/x^3+c/x^2+b/x,x, algorithm="fricas")

[Out] $1/2*(2*a*x^3 + 2*b*x^2*\log(x) - 2*c*x - d)/x^2$

giac [A] time = 0.85, size = 21, normalized size = 0.95

$$ax + b \log(|x|) - \frac{c}{x} - \frac{d}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(a+d/x^3+c/x^2+b/x,x, algorithm="giac")`

[Out] $a*x + b*\log(\text{abs}(x)) - c/x - 1/2*d/x^2$

maple [A] time = 0.00, size = 21, normalized size = 0.95

$$ax + b \ln(x) - \frac{c}{x} - \frac{d}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(a+d/x^3+c/x^2+b/x,x)`

[Out] $-1/2*d/x^2 - c/x + a*x + b*\ln(x)$

maxima [A] time = 1.03, size = 20, normalized size = 0.91

$$ax + b \log(x) - \frac{c}{x} - \frac{d}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(a+d/x^3+c/x^2+b/x,x, algorithm="maxima")`

[Out] $a*x + b*\log(x) - c/x - 1/2*d/x^2$

mupad [B] time = 0.04, size = 20, normalized size = 0.91

$$ax - \frac{\frac{d}{2} + cx}{x^2} + b \ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(a + b/x + c/x^2 + d/x^3,x)`

[Out] $a*x - (d/2 + c*x)/x^2 + b*\log(x)$

sympy [A] time = 0.16, size = 20, normalized size = 0.91

$$ax + b \log(x) + \frac{-2cx - d}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(a+d/x**3+c/x**2+b/x,x)
```

```
[Out] a*x + b*log(x) + (-2*c*x - d)/(2*x**2)
```

$$3.1903 \quad \int \left(\frac{1}{x^5} + x + x^5 \right) dx$$

Optimal. Leaf size=22

$$\frac{x^6}{6} - \frac{1}{4x^4} + \frac{x^2}{2}$$

[Out] $-1/4/x^4+1/2*x^2+1/6*x^6$

Rubi [A] time = 0.00, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{x^6}{6} + \frac{x^2}{2} - \frac{1}{4x^4}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^{(-5)} + x + x^5, x]$

[Out] $-1/(4*x^4) + x^2/2 + x^6/6$

Rubi steps

$$\int \left(\frac{1}{x^5} + x + x^5 \right) dx = -\frac{1}{4x^4} + \frac{x^2}{2} + \frac{x^6}{6}$$

Mathematica [A] time = 0.00, size = 22, normalized size = 1.00

$$\frac{x^6}{6} - \frac{1}{4x^4} + \frac{x^2}{2}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[x^{(-5)} + x + x^5, x]$

[Out] $-1/4*1/x^4 + x^2/2 + x^6/6$

fricas [A] time = 0.43, size = 17, normalized size = 0.77

$$\frac{2x^{10} + 6x^6 - 3}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^5+x+x^5,x, \text{algorithm}="fricas")$

[Out] $1/12*(2*x^{10} + 6*x^6 - 3)/x^4$

giac [A] time = 0.81, size = 16, normalized size = 0.73

$$\frac{1}{6}x^6 + \frac{1}{2}x^2 - \frac{1}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^5+x+x^5,x, algorithm="giac")`

[Out] $1/6*x^6 + 1/2*x^2 - 1/4/x^4$

maple [A] time = 0.00, size = 17, normalized size = 0.77

$$\frac{x^6}{6} + \frac{x^2}{2} - \frac{1}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^5+x+x^5,x)`

[Out] $-1/4/x^4+1/2*x^2+1/6*x^6$

maxima [A] time = 1.08, size = 16, normalized size = 0.73

$$\frac{1}{6}x^6 + \frac{1}{2}x^2 - \frac{1}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^5+x+x^5,x, algorithm="maxima")`

[Out] $1/6*x^6 + 1/2*x^2 - 1/4/x^4$

mupad [B] time = 0.03, size = 17, normalized size = 0.77

$$\frac{2x^{10} + 6x^6 - 3}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x + 1/x^5 + x^5,x)`

[Out] $(6*x^6 + 2*x^{10} - 3)/(12*x^4)$

sympy [A] time = 0.08, size = 15, normalized size = 0.68

$$\frac{x^6}{6} + \frac{x^2}{2} - \frac{1}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**5+x+x**5,x)
```

```
[Out] x**6/6 + x**2/2 - 1/(4*x**4)
```


$$3.1904 \quad \int \left(\frac{1}{x^3} + \frac{1}{x^2} + \frac{1}{x} \right) dx$$

Optimal. Leaf size=15

$$-\frac{1}{2x^2} - \frac{1}{x} + \log(x)$$

[Out] -1/2/x^2-1/x+ln(x)

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$-\frac{1}{2x^2} - \frac{1}{x} + \log(x)$$

Antiderivative was successfully verified.

[In] Int[x^(-3) + x^(-2) + x^(-1), x]

[Out] -1/(2*x^2) - x^(-1) + Log[x]

Rubi steps

$$\int \left(\frac{1}{x^3} + \frac{1}{x^2} + \frac{1}{x} \right) dx = -\frac{1}{2x^2} - \frac{1}{x} + \log(x)$$

Mathematica [A] time = 0.00, size = 15, normalized size = 1.00

$$-\frac{1}{2x^2} - \frac{1}{x} + \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[x^(-3) + x^(-2) + x^(-1), x]

[Out] -1/2*1/x^2 - x^(-1) + Log[x]

fricas [A] time = 0.47, size = 17, normalized size = 1.13

$$\frac{2x^2 \log(x) - 2x - 1}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^3+1/x^2+1/x,x, algorithm="fricas")

[Out] $1/2*(2*x^2*\log(x) - 2*x - 1)/x^2$

giac [A] time = 1.08, size = 14, normalized size = 0.93

$$-\frac{1}{x} - \frac{1}{2x^2} + \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^3+1/x^2+1/x,x, algorithm="giac")`

[Out] $-1/x - 1/2/x^2 + \log(\text{abs}(x))$

maple [A] time = 0.00, size = 14, normalized size = 0.93

$$\ln(x) - \frac{1}{x} - \frac{1}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x^3+1/x^2+1/x,x)`

[Out] $-1/2/x^2-1/x+\ln(x)$

maxima [A] time = 1.04, size = 13, normalized size = 0.87

$$-\frac{1}{x} - \frac{1}{2x^2} + \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^3+1/x^2+1/x,x, algorithm="maxima")`

[Out] $-1/x - 1/2/x^2 + \log(x)$

mupad [B] time = 0.03, size = 11, normalized size = 0.73

$$\ln(x) - \frac{x + \frac{1}{2}}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x + 1/x^2 + 1/x^3,x)`

[Out] $\log(x) - (x + 1/2)/x^2$

sympy [A] time = 0.09, size = 14, normalized size = 0.93

$$\log(x) + \frac{-2x - 1}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x**3+1/x**2+1/x,x)
```

```
[Out] log(x) + (-2*x - 1)/(2*x**2)
```

$$3.1905 \quad \int \left(-\frac{2}{x^2} + \frac{3}{x} \right) dx$$

Optimal. Leaf size=10

$$\frac{2}{x} + 3 \log(x)$$

[Out] 2/x+3*ln(x)

Rubi [A] time = 0.00, antiderivative size = 10, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{2}{x} + 3 \log(x)$$

Antiderivative was successfully verified.

[In] Int[-2/x^2 + 3/x,x]

[Out] 2/x + 3*Log[x]

Rubi steps

$$\int \left(-\frac{2}{x^2} + \frac{3}{x} \right) dx = \frac{2}{x} + 3 \log(x)$$

Mathematica [A] time = 0.00, size = 10, normalized size = 1.00

$$\frac{2}{x} + 3 \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[-2/x^2 + 3/x,x]

[Out] 2/x + 3*Log[x]

fricas [A] time = 0.47, size = 11, normalized size = 1.10

$$\frac{3x \log(x) + 2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-2/x^2+3/x,x, algorithm="fricas")

[Out] $(3*x*\log(x) + 2)/x$

giac [A] time = 1.12, size = 11, normalized size = 1.10

$$\frac{2}{x} + 3 \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-2/x^2+3/x,x, algorithm="giac")`

[Out] $2/x + 3*\log(\text{abs}(x))$

maple [A] time = 0.00, size = 11, normalized size = 1.10

$$3 \ln(x) + \frac{2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-2/x^2+3/x,x)`

[Out] $2/x+3*\ln(x)$

maxima [A] time = 1.03, size = 10, normalized size = 1.00

$$\frac{2}{x} + 3 \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-2/x^2+3/x,x, algorithm="maxima")`

[Out] $2/x + 3*\log(x)$

mupad [B] time = 0.03, size = 10, normalized size = 1.00

$$3 \ln(x) + \frac{2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(3/x - 2/x^2,x)`

[Out] $3*\log(x) + 2/x$

sympy [A] time = 0.08, size = 7, normalized size = 0.70

$$3 \log(x) + \frac{2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-2/x**2+3/x,x)
```

```
[Out] 3*log(x) + 2/x
```

$$3.1906 \quad \int \left(-\frac{1}{7x^6} + x^6 \right) dx$$

Optimal. Leaf size=15

$$\frac{x^7}{7} + \frac{1}{35x^5}$$

[Out] 1/35/x^5+1/7*x^7

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{x^7}{7} + \frac{1}{35x^5}$$

Antiderivative was successfully verified.

[In] Int[-1/(7*x^6) + x^6,x]

[Out] 1/(35*x^5) + x^7/7

Rubi steps

$$\int \left(-\frac{1}{7x^6} + x^6 \right) dx = \frac{1}{35x^5} + \frac{x^7}{7}$$

Mathematica [A] time = 0.00, size = 15, normalized size = 1.00

$$\frac{x^7}{7} + \frac{1}{35x^5}$$

Antiderivative was successfully verified.

[In] Integrate[-1/7*1/x^6 + x^6,x]

[Out] 1/(35*x^5) + x^7/7

fricas [A] time = 0.43, size = 12, normalized size = 0.80

$$\frac{5x^{12} + 1}{35x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-1/7/x^6+x^6,x, algorithm="fricas")

[Out] $1/35*(5*x^{12} + 1)/x^5$

giac [A] time = 1.08, size = 11, normalized size = 0.73

$$\frac{1}{7}x^7 + \frac{1}{35x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-1/7/x^6+x^6,x, algorithm="giac")`

[Out] $1/7*x^7 + 1/35/x^5$

maple [A] time = 0.00, size = 12, normalized size = 0.80

$$\frac{x^7}{7} + \frac{1}{35x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-1/7/x^6+x^6,x)`

[Out] $1/35/x^5+1/7*x^7$

maxima [A] time = 0.97, size = 11, normalized size = 0.73

$$\frac{1}{7}x^7 + \frac{1}{35x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-1/7/x^6+x^6,x, algorithm="maxima")`

[Out] $1/7*x^7 + 1/35/x^5$

mupad [B] time = 0.03, size = 12, normalized size = 0.80

$$\frac{5x^{12} + 1}{35x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^6 - 1/(7*x^6),x)`

[Out] $(5*x^{12} + 1)/(35*x^5)$

sympy [A] time = 0.08, size = 10, normalized size = 0.67

$$\frac{x^7}{7} + \frac{1}{35x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-1/7/x**6+x**6,x)
```

```
[Out] x**7/7 + 1/(35*x**5)
```

$$3.1907 \quad \int \left(1 + \frac{1}{x} + x\right) dx$$

Optimal. Leaf size=11

$$\frac{x^2}{2} + x + \log(x)$$

[Out] $x + \frac{1}{2}x^2 + \ln(x)$

Rubi [A] time = 0.00, antiderivative size = 11, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{x^2}{2} + x + \log(x)$$

Antiderivative was successfully verified.

[In] Int[1 + x⁽⁻¹⁾ + x, x]

[Out] x + x²/2 + Log[x]

Rubi steps

$$\int \left(1 + \frac{1}{x} + x\right) dx = x + \frac{x^2}{2} + \log(x)$$

Mathematica [A] time = 0.00, size = 11, normalized size = 1.00

$$\frac{x^2}{2} + x + \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[1 + x⁽⁻¹⁾ + x, x]

[Out] x + x²/2 + Log[x]

fricas [A] time = 0.43, size = 9, normalized size = 0.82

$$\frac{1}{2}x^2 + x + \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1+1/x+x,x, algorithm="fricas")

[Out] $1/2*x^2 + x + \log(x)$

giac [A] time = 0.89, size = 10, normalized size = 0.91

$$\frac{1}{2}x^2 + x + \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1+1/x+x,x, algorithm="giac")`

[Out] $1/2*x^2 + x + \log(\text{abs}(x))$

maple [A] time = 0.00, size = 10, normalized size = 0.91

$$\frac{x^2}{2} + x + \ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1+1/x+x,x)`

[Out] $x+1/2*x^2+\ln(x)$

maxima [A] time = 0.92, size = 9, normalized size = 0.82

$$\frac{1}{2}x^2 + x + \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1+1/x+x,x, algorithm="maxima")`

[Out] $1/2*x^2 + x + \log(x)$

mupad [B] time = 0.03, size = 9, normalized size = 0.82

$$x + \ln(x) + \frac{x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x + 1/x + 1,x)`

[Out] $x + \log(x) + x^2/2$

sympy [A] time = 0.08, size = 8, normalized size = 0.73

$$\frac{x^2}{2} + x + \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1+1/x+x,x)
```

```
[Out] x**2/2 + x + log(x)
```

$$3.1908 \quad \int \left(-\frac{3}{x^3} + \frac{4}{x^2} \right) dx$$

Optimal. Leaf size=13

$$\frac{3}{2x^2} - \frac{4}{x}$$

[Out] 3/2/x^2-4/x

Rubi [A] time = 0.00, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{3}{2x^2} - \frac{4}{x}$$

Antiderivative was successfully verified.

[In] Int[-3/x^3 + 4/x^2, x]

[Out] 3/(2*x^2) - 4/x

Rubi steps

$$\int \left(-\frac{3}{x^3} + \frac{4}{x^2} \right) dx = \frac{3}{2x^2} - \frac{4}{x}$$

Mathematica [A] time = 0.00, size = 13, normalized size = 1.00

$$\frac{3}{2x^2} - \frac{4}{x}$$

Antiderivative was successfully verified.

[In] Integrate[-3/x^3 + 4/x^2, x]

[Out] 3/(2*x^2) - 4/x

fricas [A] time = 0.41, size = 10, normalized size = 0.77

$$-\frac{8x-3}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-3/x^3+4/x^2,x, algorithm="fricas")

[Out] $-1/2*(8*x - 3)/x^2$

giac [A] time = 0.90, size = 11, normalized size = 0.85

$$-\frac{4}{x} + \frac{3}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-3/x^3+4/x^2,x, algorithm="giac")`

[Out] $-4/x + 3/2/x^2$

maple [A] time = 0.00, size = 12, normalized size = 0.92

$$-\frac{4}{x} + \frac{3}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-3/x^3+4/x^2,x)`

[Out] $3/2/x^2-4/x$

maxima [A] time = 0.97, size = 11, normalized size = 0.85

$$-\frac{4}{x} + \frac{3}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-3/x^3+4/x^2,x, algorithm="maxima")`

[Out] $-4/x + 3/2/x^2$

mupad [B] time = 0.03, size = 10, normalized size = 0.77

$$-\frac{8x - 3}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(4/x^2 - 3/x^3,x)`

[Out] $-(8*x - 3)/(2*x^2)$

sympy [A] time = 0.08, size = 8, normalized size = 0.62

$$\frac{3 - 8x}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-3/x**3+4/x**2,x)
```

```
[Out] (3 - 8*x)/(2*x**2)
```

$$3.1909 \quad \int \left(\frac{1}{x} + 2x + x^2 \right) dx$$

Optimal. Leaf size=13

$$\frac{x^3}{3} + x^2 + \log(x)$$

[Out] $x^2 + 1/3 * x^3 + \ln(x)$

Rubi [A] time = 0.00, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{x^3}{3} + x^2 + \log(x)$$

Antiderivative was successfully verified.

[In] Int[x⁽⁻¹⁾ + 2*x + x², x]

[Out] x² + x³/3 + Log[x]

Rubi steps

$$\int \left(\frac{1}{x} + 2x + x^2 \right) dx = x^2 + \frac{x^3}{3} + \log(x)$$

Mathematica [A] time = 0.00, size = 13, normalized size = 1.00

$$\frac{x^3}{3} + x^2 + \log(x)$$

Antiderivative was successfully verified.

[In] Integrate[x⁽⁻¹⁾ + 2*x + x², x]

[Out] x² + x³/3 + Log[x]

fricas [A] time = 0.47, size = 11, normalized size = 0.85

$$\frac{1}{3} x^3 + x^2 + \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x+2*x+x², x, algorithm="fricas")

[Out] $\frac{1}{3}x^3 + x^2 + \log(x)$

giac [A] time = 1.01, size = 12, normalized size = 0.92

$$\frac{1}{3}x^3 + x^2 + \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x+2*x+x^2,x, algorithm="giac")`

[Out] $\frac{1}{3}x^3 + x^2 + \log(\text{abs}(x))$

maple [A] time = 0.00, size = 12, normalized size = 0.92

$$\frac{x^3}{3} + x^2 + \ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/x+2*x+x^2,x)`

[Out] $x^2 + \frac{1}{3}x^3 + \ln(x)$

maxima [A] time = 1.08, size = 11, normalized size = 0.85

$$\frac{1}{3}x^3 + x^2 + \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x+2*x+x^2,x, algorithm="maxima")`

[Out] $\frac{1}{3}x^3 + x^2 + \log(x)$

mupad [B] time = 0.03, size = 11, normalized size = 0.85

$$\ln(x) + x^2 + \frac{x^3}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(2*x + 1/x + x^2,x)`

[Out] $\log(x) + x^2 + x^3/3$

sympy [A] time = 0.08, size = 10, normalized size = 0.77

$$\frac{x^3}{3} + x^2 + \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x+2*x+x**2,x)
```

```
[Out] x**3/3 + x**2 + log(x)
```

3.1910

$$\int (x^{5/6} - x^3) dx$$

Optimal. Leaf size=17

$$\frac{6x^{11/6}}{11} - \frac{x^4}{4}$$

[Out] 6/11*x^(11/6)-1/4*x^4

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{6x^{11/6}}{11} - \frac{x^4}{4}$$

Antiderivative was successfully verified.

[In] Int[x^(5/6) - x^3,x]

[Out] (6*x^(11/6))/11 - x^4/4

Rubi steps

$$\int (x^{5/6} - x^3) dx = \frac{6x^{11/6}}{11} - \frac{x^4}{4}$$

Mathematica [A] time = 0.00, size = 17, normalized size = 1.00

$$\frac{6x^{11/6}}{11} - \frac{x^4}{4}$$

Antiderivative was successfully verified.

[In] Integrate[x^(5/6) - x^3,x]

[Out] (6*x^(11/6))/11 - x^4/4

fricas [A] time = 0.44, size = 11, normalized size = 0.65

$$-\frac{1}{4}x^4 + \frac{6}{11}x^{\frac{11}{6}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^(5/6)-x^3,x, algorithm="fricas")

[Out] $-1/4*x^4 + 6/11*x^{(11/6)}$

giac [A] time = 1.06, size = 11, normalized size = 0.65

$$-\frac{1}{4}x^4 + \frac{6}{11}x^{\frac{11}{6}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/6)-x^3,x, algorithm="giac")`

[Out] $-1/4*x^4 + 6/11*x^{(11/6)}$

maple [A] time = 0.00, size = 12, normalized size = 0.71

$$-\frac{x^4}{4} + \frac{6x^{\frac{11}{6}}}{11}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/6)-x^3,x)`

[Out] $6/11*x^{(11/6)}-1/4*x^4$

maxima [A] time = 1.07, size = 11, normalized size = 0.65

$$-\frac{1}{4}x^4 + \frac{6}{11}x^{\frac{11}{6}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^(5/6)-x^3,x, algorithm="maxima")`

[Out] $-1/4*x^4 + 6/11*x^{(11/6)}$

mupad [B] time = 0.03, size = 11, normalized size = 0.65

$$\frac{6x^{11/6}}{11} - \frac{x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(5/6) - x^3,x)`

[Out] $(6*x^{(11/6)})/11 - x^4/4$

sympy [A] time = 0.06, size = 12, normalized size = 0.71

$$\frac{6x^{\frac{11}{6}}}{11} - \frac{x^4}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**(5/6)-x**3,x)
```

```
[Out] 6*x**(11/6)/11 - x**4/4
```

$$3.1911 \quad \int (33 + \sqrt[33]{x}) dx$$

Optimal. Leaf size=13

$$\frac{33x^{34/33}}{34} + 33x$$

[Out] 33*x+33/34*x^(34/33)

Rubi [A] time = 0.00, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{33x^{34/33}}{34} + 33x$$

Antiderivative was successfully verified.

[In] Int[33 + x^(1/33), x]

[Out] 33*x + (33*x^(34/33))/34

Rubi steps

$$\int (33 + \sqrt[33]{x}) dx = 33x + \frac{33x^{34/33}}{34}$$

Mathematica [A] time = 0.00, size = 13, normalized size = 1.00

$$\frac{33x^{34/33}}{34} + 33x$$

Antiderivative was successfully verified.

[In] Integrate[33 + x^(1/33), x]

[Out] 33*x + (33*x^(34/33))/34

fricas [A] time = 0.43, size = 9, normalized size = 0.69

$$\frac{33}{34} x^{34/33} + 33x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(33+x^(1/33),x, algorithm="fricas")

[Out] $33/34*x^{(34/33)} + 33*x$

giac [A] time = 0.85, size = 9, normalized size = 0.69

$$\frac{33}{34} x^{\frac{34}{33}} + 33x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(33+x^(1/33),x, algorithm="giac")`

[Out] $33/34*x^{(34/33)} + 33*x$

maple [A] time = 0.00, size = 10, normalized size = 0.77

$$\frac{33x^{\frac{34}{33}}}{34} + 33x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(33+x^(1/33),x)`

[Out] $33*x+33/34*x^{(34/33)}$

maxima [A] time = 1.00, size = 9, normalized size = 0.69

$$\frac{33}{34} x^{\frac{34}{33}} + 33x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(33+x^(1/33),x, algorithm="maxima")`

[Out] $33/34*x^{(34/33)} + 33*x$

mupad [B] time = 0.02, size = 8, normalized size = 0.62

$$\frac{33x(x^{1/33} + 34)}{34}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/33) + 33,x)`

[Out] $(33*x*(x^{(1/33)} + 34))/34$

sympy [A] time = 0.06, size = 10, normalized size = 0.77

$$\frac{33x^{\frac{34}{33}}}{34} + 33x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(33+x**(1/33),x)
```

```
[Out] 33*x**(34/33)/34 + 33*x
```


$$3.1912 \quad \int \left(\frac{1}{2\sqrt{x}} + 2\sqrt{x} \right) dx$$

Optimal. Leaf size=15

$$\frac{4x^{3/2}}{3} + \sqrt{x}$$

[Out] 4/3*x^(3/2)+x^(1/2)

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{4x^{3/2}}{3} + \sqrt{x}$$

Antiderivative was successfully verified.

[In] Int[1/(2*Sqrt[x]) + 2*Sqrt[x], x]

[Out] Sqrt[x] + (4*x^(3/2))/3

Rubi steps

$$\int \left(\frac{1}{2\sqrt{x}} + 2\sqrt{x} \right) dx = \sqrt{x} + \frac{4x^{3/2}}{3}$$

Mathematica [A] time = 0.01, size = 14, normalized size = 0.93

$$\frac{1}{3}\sqrt{x}(4x + 3)$$

Antiderivative was successfully verified.

[In] Integrate[1/(2*Sqrt[x]) + 2*Sqrt[x], x]

[Out] (Sqrt[x]*(3 + 4*x))/3

fricas [A] time = 0.44, size = 10, normalized size = 0.67

$$\frac{1}{3}(4x + 3)\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/2/x^(1/2)+2*x^(1/2), x, algorithm="fricas")

[Out] $1/3*(4*x + 3)*\text{sqrt}(x)$

giac [A] time = 1.08, size = 9, normalized size = 0.60

$$\frac{4}{3}x^{\frac{3}{2}} + \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/2/x^(1/2)+2*x^(1/2),x, algorithm="giac")`

[Out] $4/3*x^{(3/2)} + \text{sqrt}(x)$

maple [A] time = 0.00, size = 11, normalized size = 0.73

$$\frac{(4x + 3)\sqrt{x}}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/2/x^(1/2)+2*x^(1/2),x)`

[Out] $1/3*x^{(1/2)}*(4*x+3)$

maxima [A] time = 1.11, size = 9, normalized size = 0.60

$$\frac{4}{3}x^{\frac{3}{2}} + \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/2/x^(1/2)+2*x^(1/2),x, algorithm="maxima")`

[Out] $4/3*x^{(3/2)} + \text{sqrt}(x)$

mupad [B] time = 0.02, size = 10, normalized size = 0.67

$$\frac{\sqrt{x}(4x + 3)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/(2*x^(1/2)) + 2*x^(1/2),x)`

[Out] $(x^{(1/2)}*(4*x + 3))/3$

sympy [A] time = 0.06, size = 12, normalized size = 0.80

$$\frac{4x^{\frac{3}{2}}}{3} + \sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/2/x**(1/2)+2*x**(1/2),x)
```

```
[Out] 4*x**(3/2)/3 + sqrt(x)
```

$$\mathbf{3.1913} \quad \int \left(-\frac{1}{x^2} + \frac{10}{x} + 6\sqrt{x} \right) dx$$

Optimal. Leaf size=15

$$4x^{3/2} + \frac{1}{x} + 10 \log(x)$$

[Out] $1/x+4*x^{(3/2)}+10*\ln(x)$

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$4x^{3/2} + \frac{1}{x} + 10 \log(x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[-x^{(-2)} + 10/x + 6*\text{Sqrt}[x], x]$

[Out] $x^{(-1)} + 4*x^{(3/2)} + 10*\text{Log}[x]$

Rubi steps

$$\int \left(-\frac{1}{x^2} + \frac{10}{x} + 6\sqrt{x} \right) dx = \frac{1}{x} + 4x^{3/2} + 10 \log(x)$$

Mathematica [A] time = 0.01, size = 15, normalized size = 1.00

$$4x^{3/2} + \frac{1}{x} + 10 \log(x)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[-x^{(-2)} + 10/x + 6*\text{Sqrt}[x], x]$

[Out] $x^{(-1)} + 4*x^{(3/2)} + 10*\text{Log}[x]$

fricas [A] time = 0.44, size = 18, normalized size = 1.20

$$\frac{4x^{\frac{5}{2}} + 20x \log(\sqrt{x}) + 1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(-1/x^2+10/x+6*x^{(1/2)}, x, \text{algorithm}=\text{"fricas"})$

[Out] $(4x^{5/2} + 20x \log(\sqrt{x}) + 1)/x$

giac [A] time = 0.95, size = 14, normalized size = 0.93

$$4x^{\frac{3}{2}} + \frac{1}{x} + 10 \log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-1/x^2+10/x+6*x^(1/2),x, algorithm="giac")`

[Out] $4x^{3/2} + 1/x + 10 \log(\text{abs}(x))$

maple [A] time = 0.00, size = 14, normalized size = 0.93

$$4x^{\frac{3}{2}} + 10 \ln(x) + \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-1/x^2+10/x+6*x^(1/2),x)`

[Out] $1/x + 4x^{3/2} + 10 \ln(x)$

maxima [A] time = 1.02, size = 13, normalized size = 0.87

$$4x^{\frac{3}{2}} + \frac{1}{x} + 10 \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-1/x^2+10/x+6*x^(1/2),x, algorithm="maxima")`

[Out] $4x^{3/2} + 1/x + 10 \log(x)$

mupad [B] time = 0.29, size = 15, normalized size = 1.00

$$20 \ln(\sqrt{x}) + \frac{1}{x} + 4x^{3/2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(10/x - 1/x^2 + 6*x^(1/2),x)`

[Out] $20 \log(x^{1/2}) + 1/x + 4x^{3/2}$

sympy [A] time = 0.06, size = 14, normalized size = 0.93

$$4x^{\frac{3}{2}} + 10 \log(x) + \frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-1/x**2+10/x+6*x**(1/2),x)
```

```
[Out] 4*x**(3/2) + 10*log(x) + 1/x
```

$$3.1914 \quad \int \left(\frac{1}{x^{3/2}} + x^{3/2} \right) dx$$

Optimal. Leaf size=17

$$\frac{2x^{5/2}}{5} - \frac{2}{\sqrt{x}}$$

[Out] 2/5*x^(5/2)-2/x^(1/2)

Rubi [A] time = 0.00, antiderivative size = 17, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 11, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{2x^{5/2}}{5} - \frac{2}{\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Int[x^(-3/2) + x^(3/2), x]

[Out] -2/Sqrt[x] + (2*x^(5/2))/5

Rubi steps

$$\int \left(\frac{1}{x^{3/2}} + x^{3/2} \right) dx = -\frac{2}{\sqrt{x}} + \frac{2x^{5/2}}{5}$$

Mathematica [A] time = 0.01, size = 14, normalized size = 0.82

$$\frac{2(x^3 - 5)}{5\sqrt{x}}$$

Antiderivative was successfully verified.

[In] Integrate[x^(-3/2) + x^(3/2), x]

[Out] (2*(-5 + x^3))/(5*Sqrt[x])

fricas [A] time = 0.43, size = 10, normalized size = 0.59

$$\frac{2(x^3 - 5)}{5\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)+x^(3/2),x, algorithm="fricas")

[Out] 2/5*(x^3 - 5)/sqrt(x)

giac [A] time = 1.14, size = 11, normalized size = 0.65

$$\frac{2}{5}x^{\frac{5}{2}} - \frac{2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)+x^(3/2),x, algorithm="giac")

[Out] 2/5*x^(5/2) - 2/sqrt(x)

maple [A] time = 0.00, size = 11, normalized size = 0.65

$$\frac{\frac{2x^3}{5} - 2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2)+x^(3/2),x)

[Out] 2/5*(x^3-5)/x^(1/2)

maxima [A] time = 1.00, size = 11, normalized size = 0.65

$$\frac{2}{5}x^{\frac{5}{2}} - \frac{2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^(3/2)+x^(3/2),x, algorithm="maxima")

[Out] 2/5*x^(5/2) - 2/sqrt(x)

mupad [B] time = 0.03, size = 12, normalized size = 0.71

$$\frac{2x^3 - 10}{5\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^(3/2) + x^(3/2),x)

[Out] (2*x^3 - 10)/(5*x^(1/2))

sympy [A] time = 0.06, size = 14, normalized size = 0.82

$$\frac{2x^{\frac{5}{2}}}{5} - \frac{2}{\sqrt{x}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**(3/2)+x**(3/2),x)

[Out] 2*x**(5/2)/5 - 2/sqrt(x)

3.1915

$$\int \left(-5x^{3/2} + 7x^{5/2}\right) dx$$

Optimal. Leaf size=15

$$2x^{7/2} - 2x^{5/2}$$

[Out] $-2*x^{(5/2)}+2*x^{(7/2)}$

Rubi [A] time = 0.00, antiderivative size = 15, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$2x^{7/2} - 2x^{5/2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[-5*x^{(3/2)} + 7*x^{(5/2)}, x]$

[Out] $-2*x^{(5/2)} + 2*x^{(7/2)}$

Rubi steps

$$\int \left(-5x^{3/2} + 7x^{5/2}\right) dx = -2x^{5/2} + 2x^{7/2}$$

Mathematica [A] time = 0.00, size = 10, normalized size = 0.67

$$2(x-1)x^{5/2}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[-5*x^{(3/2)} + 7*x^{(5/2)}, x]$

[Out] $2*(-1 + x)*x^{(5/2)}$

fricas [A] time = 0.44, size = 14, normalized size = 0.93

$$2(x^3 - x^2)\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(-5*x^{(3/2)}+7*x^{(5/2)}, x, \text{algorithm}=\text{"fricas"})$

[Out] $2*(x^3 - x^2)*\text{sqrt}(x)$

giac [A] time = 0.89, size = 11, normalized size = 0.73

$$2x^{7/2} - 2x^{5/2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-5*x^(3/2)+7*x^(5/2),x, algorithm="giac")`

[Out] $2*x^{(7/2)} - 2*x^{(5/2)}$

maple [A] time = 0.00, size = 9, normalized size = 0.60

$$2(x-1)x^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-5*x^(3/2)+7*x^(5/2),x)`

[Out] $2*x^{(5/2)}*(x-1)$

maxima [A] time = 1.01, size = 11, normalized size = 0.73

$$2x^{\frac{7}{2}} - 2x^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-5*x^(3/2)+7*x^(5/2),x, algorithm="maxima")`

[Out] $2*x^{(7/2)} - 2*x^{(5/2)}$

mupad [B] time = 0.03, size = 8, normalized size = 0.53

$$2x^{5/2}(x-1)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(7*x^(5/2) - 5*x^(3/2),x)`

[Out] $2*x^{(5/2)}*(x - 1)$

sympy [A] time = 0.06, size = 12, normalized size = 0.80

$$2x^{\frac{7}{2}} - 2x^{\frac{5}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-5*x**(3/2)+7*x**(5/2),x)`

[Out] $2*x^{(7/2)} - 2*x^{(5/2)}$

$$3.1916 \quad \int \left(\frac{2}{\sqrt{x}} + \sqrt{x} - \frac{x}{2} \right) dx$$

Optimal. Leaf size=24

$$\frac{2x^{3/2}}{3} - \frac{x^2}{4} + 4\sqrt{x}$$

[Out] 2/3*x^(3/2)-1/4*x^2+4*x^(1/2)

Rubi [A] time = 0.00, antiderivative size = 24, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$-\frac{x^2}{4} + \frac{2x^{3/2}}{3} + 4\sqrt{x}$$

Antiderivative was successfully verified.

[In] Int[2/Sqrt[x] + Sqrt[x] - x/2,x]

[Out] 4*Sqrt[x] + (2*x^(3/2))/3 - x^2/4

Rubi steps

$$\int \left(\frac{2}{\sqrt{x}} + \sqrt{x} - \frac{x}{2} \right) dx = 4\sqrt{x} + \frac{2x^{3/2}}{3} - \frac{x^2}{4}$$

Mathematica [A] time = 0.00, size = 24, normalized size = 1.00

$$\frac{2x^{3/2}}{3} - \frac{x^2}{4} + 4\sqrt{x}$$

Antiderivative was successfully verified.

[In] Integrate[2/Sqrt[x] + Sqrt[x] - x/2,x]

[Out] 4*Sqrt[x] + (2*x^(3/2))/3 - x^2/4

fricas [A] time = 0.60, size = 14, normalized size = 0.58

$$-\frac{1}{4}x^2 + \frac{2}{3}(x+6)\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-1/2*x+2/x^(1/2)+x^(1/2),x, algorithm="fricas")

[Out] -1/4*x^2 + 2/3*(x + 6)*sqrt(x)

giac [A] time = 1.09, size = 16, normalized size = 0.67

$$-\frac{1}{4}x^2 + \frac{2}{3}x^{\frac{3}{2}} + 4\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-1/2*x+2/x^(1/2)+x^(1/2),x, algorithm="giac")

[Out] -1/4*x^2 + 2/3*x^(3/2) + 4*sqrt(x)

maple [A] time = 0.00, size = 17, normalized size = 0.71

$$-\frac{x^2}{4} + \frac{2x^{\frac{3}{2}}}{3} + 4\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-1/2*x+2/x^(1/2)+x^(1/2),x)

[Out] 2/3*x^(3/2)-1/4*x^2+4*x^(1/2)

maxima [A] time = 1.05, size = 16, normalized size = 0.67

$$-\frac{1}{4}x^2 + \frac{2}{3}x^{\frac{3}{2}} + 4\sqrt{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-1/2*x+2/x^(1/2)+x^(1/2),x, algorithm="maxima")

[Out] -1/4*x^2 + 2/3*x^(3/2) + 4*sqrt(x)

mupad [B] time = 0.03, size = 15, normalized size = 0.62

$$\frac{\sqrt{x} (8x - 3x^{3/2} + 48)}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(2/x^(1/2) - x/2 + x^(1/2),x)

[Out] (x^(1/2)*(8*x - 3*x^(3/2) + 48))/12

sympy [A] time = 0.06, size = 19, normalized size = 0.79

$$\frac{2x^{\frac{3}{2}}}{3} + 4\sqrt{x} - \frac{x^2}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-1/2*x+2/x**(1/2)+x**(1/2),x)

[Out] 2*x**(3/2)/3 + 4*sqrt(x) - x**2/4

$$3.1917 \quad \int \left(-\frac{2}{x} + \frac{\sqrt{x}}{5} + x^{3/2} \right) dx$$

Optimal. Leaf size=23

$$\frac{2x^{5/2}}{5} + \frac{2x^{3/2}}{15} - 2\log(x)$$

[Out] 2/15*x^(3/2)+2/5*x^(5/2)-2*ln(x)

Rubi [A] time = 0.00, antiderivative size = 23, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 0, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\frac{2x^{5/2}}{5} + \frac{2x^{3/2}}{15} - 2\log(x)$$

Antiderivative was successfully verified.

[In] Int[-2/x + Sqrt[x]/5 + x^(3/2), x]

[Out] (2*x^(3/2))/15 + (2*x^(5/2))/5 - 2*Log[x]

Rubi steps

$$\int \left(-\frac{2}{x} + \frac{\sqrt{x}}{5} + x^{3/2} \right) dx = \frac{2x^{3/2}}{15} + \frac{2x^{5/2}}{5} - 2\log(x)$$

Mathematica [A] time = 0.01, size = 23, normalized size = 1.00

$$\frac{2x^{5/2}}{5} + \frac{2x^{3/2}}{15} - 2\log(x)$$

Antiderivative was successfully verified.

[In] Integrate[-2/x + Sqrt[x]/5 + x^(3/2), x]

[Out] (2*x^(3/2))/15 + (2*x^(5/2))/5 - 2*Log[x]

fricas [A] time = 0.77, size = 19, normalized size = 0.83

$$\frac{2}{15} (3x^2 + x)\sqrt{x} - 4 \log(\sqrt{x})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-2/x+x^(3/2)+1/5*x^(1/2),x, algorithm="fricas")

[Out] $2/15*(3*x^2 + x)*\text{sqrt}(x) - 4*\log(\text{sqrt}(x))$

giac [A] time = 0.82, size = 16, normalized size = 0.70

$$\frac{2}{5}x^{\frac{5}{2}} + \frac{2}{15}x^{\frac{3}{2}} - 2\log(|x|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-2/x+x^(3/2)+1/5*x^(1/2),x, algorithm="giac")`

[Out] $2/5*x^{(5/2)} + 2/15*x^{(3/2)} - 2*\log(\text{abs}(x))$

maple [A] time = 0.00, size = 16, normalized size = 0.70

$$\frac{2x^{\frac{5}{2}}}{5} + \frac{2x^{\frac{3}{2}}}{15} - 2\ln(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(-2/x+x^(3/2)+1/5*x^(1/2),x)`

[Out] $2/15*x^{(3/2)}+2/5*x^{(5/2)}-2*\ln(x)$

maxima [A] time = 1.03, size = 15, normalized size = 0.65

$$\frac{2}{5}x^{\frac{5}{2}} + \frac{2}{15}x^{\frac{3}{2}} - 2\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(-2/x+x^(3/2)+1/5*x^(1/2),x, algorithm="maxima")`

[Out] $2/5*x^{(5/2)} + 2/15*x^{(3/2)} - 2*\log(x)$

mupad [B] time = 0.28, size = 17, normalized size = 0.74

$$\frac{2x^{3/2}}{15} - 4\ln(\sqrt{x}) + \frac{2x^{5/2}}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^(1/2)/5 - 2/x + x^(3/2),x)`

[Out] $(2*x^{(3/2)})/15 - 4*\log(x^{(1/2)}) + (2*x^{(5/2)})/5$

sympy [A] time = 0.06, size = 20, normalized size = 0.87

$$\frac{2x^{\frac{5}{2}}}{5} + \frac{2x^{\frac{3}{2}}}{15} - 2\log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-2/x+x**(3/2)+1/5*x**(1/2),x)
```

```
[Out] 2*x**(5/2)/5 + 2*x**(3/2)/15 - 2*log(x)
```


Chapter 4

Listing of Grading functions

The following are the current version of the grading functions used for grading the quality of the antiderivative with reference to the optimal antiderivative included in the test suite.

There is a version for Maple and for Mathematica/Rubi. There is a version for grading Sympy and version for use with Sagemath.

The following are links to the current source code.

The following are the listings of source code of the grading functions.

4.0.1 Mathematica and Rubi grading function

```
(* Original version thanks to Albert Rich emailed on 03/21/2017 *)
(* ::Package:: *)

(* ::Subsection:: *)
(*GradeAntiderivative[result,optimal]*)

(* ::Text:: *)
(*If result and optimal are mathematical expressions, *)
(*      GradeAntiderivative[result,optimal] returns*)
(* "F" if the result fails to integrate an expression that*)
(*      is integrable*)
(* "C" if result involves higher level functions than necessary*)
(* "B" if result is more than twice the size of the optimal*)
(*      antiderivative*)
(* "A" if result can be considered optimal*)

GradeAntiderivative[result_,optimal_] :=
  If[ExpnType[result]<=ExpnType[optimal],
```

```

If[FreeQ[result,Complex] || Not[FreeQ[optimal,Complex]],
  If[LeafCount[result]<=2*LeafCount[optimal],
    "A",
    "B"],
  "C"],
If[FreeQ[result,Integrate] && FreeQ[result,Int],
  "C",
"F"]]

```

```

(* ::Text:: *)
(*The following summarizes the type number assigned an *)
(*expression based on the functions it involves*)
(*1 = rational function*)
(*2 = algebraic function*)
(*3 = elementary function*)
(*4 = special function*)
(*5 = hyperpergeometric function*)
(*6 = appell function*)
(*7 = rootsum function*)
(*8 = integrate function*)
(*9 = unknown function*)

```

```

ExpnType[expn_] :=
  If[AtomQ[expn],
    1,
  If[ListQ[expn],
    Max[Map[ExpnType,expn]],
  If[Head[expn]===Power,
    If[IntegerQ[expn[[2]]],
      ExpnType[expn[[1]]],
    If[Head[expn[[2]]]===Rational,
      If[IntegerQ[expn[[1]]] || Head[expn[[1]]]===Rational,
        1,
        Max[ExpnType[expn[[1]],2]],
      Max[ExpnType[expn[[1]],ExpnType[expn[[2]],3]],
    If[Head[expn]===Plus || Head[expn]===Times,
      Max[ExpnType[First[expn]],ExpnType[Rest[expn]]],
    If[ElementaryFunctionQ[Head[expn]],
      Max[3,ExpnType[expn[[1]]],
    If[SpecialFunctionQ[Head[expn]],
      Apply[Max,Append[Map[ExpnType,Apply[List,expn]],4]],
    If[HypergeometricFunctionQ[Head[expn]],
      Apply[Max,Append[Map[ExpnType,Apply[List,expn]],5]],
    If[AppellFunctionQ[Head[expn]],
      Apply[Max,Append[Map[ExpnType,Apply[List,expn]],6]],

```

```

If[Head[expn]===RootSum,
  Apply[Max,Append[Map[ExpnType,Apply[List,expn]],7]],
If[Head[expn]===Integrate || Head[expn]===Int,
  Apply[Max,Append[Map[ExpnType,Apply[List,expn]],8]],
9]]]]]]]]]]

ElementaryFunctionQ[func_] :=
MemberQ[{
  Exp,Log,
  Sin,Cos,Tan,Cot,Sec,Csc,
  ArcSin,ArcCos,ArcTan,ArcCot,ArcSec,ArcCsc,
  Sinh,Cosh,Tanh,Coth,Sech,Csch,
  ArcSinh,ArcCosh,ArcTanh,ArcCoth,ArcSech,ArcCsch
},func]

SpecialFunctionQ[func_] :=
MemberQ[{
  Erf, Erfc, Erfi,
  FresnelS, FresnelC,
  ExpIntegralE, ExpIntegralEi, LogIntegral,
  SinIntegral, CosIntegral, SinhIntegral, CoshIntegral,
  Gamma, LogGamma, PolyGamma,
  Zeta, PolyLog, ProductLog,
  EllipticF, EllipticE, EllipticPi
},func]

HypergeometricFunctionQ[func_] :=
MemberQ[{Hypergeometric1F1,Hypergeometric2F1,HypergeometricPFQ},func]

AppellFunctionQ[func_] :=
MemberQ[{AppellF1},func]

```

4.0.2 Maple grading function

```

# File: GradeAntiderivative.mpl
# Original version thanks to Albert Rich emailed on 03/21/2017

#Nasser 03/22/2017 Use Maple leaf count instead since buildin
#Nasser 03/23/2017 missing 'ln' for ElementaryFunctionQ added
#Nasser 03/24/2017 corrected the check for complex result
#Nasser 10/27/2017 check for leafsize and do not call ExpnType()
#
# if leaf size is "too large". Set at 500,000

```

```

#Nasser 12/22/2019  Added debug flag, added 'dilog' to special functions
#                   see problem 156, file Apostol_Problems

GradeAntiderivative := proc(result,optimal)
local leaf_count_result, leaf_count_optimal,ExpnType_result,ExpnType_optimal,
    debug:=false;

    leaf_count_result:=leafcount(result);
    #do NOT call ExpnType() if leaf size is too large. Recursion problem
    if leaf_count_result > 500000 then
        return "B";
    fi;

    leaf_count_optimal:=leafcount(optimal);

    ExpnType_result:=ExpnType(result);
    ExpnType_optimal:=ExpnType(optimal);

    if debug then
        print("ExpnType_result",ExpnType_result," ExpnType_optimal=",
ExpnType_optimal);
    fi;

# If result and optimal are mathematical expressions,
# GradeAntiderivative[result,optimal] returns
# "F" if the result fails to integrate an expression that
#   is integrable
# "C" if result involves higher level functions than necessary
# "B" if result is more than twice the size of the optimal
#   antiderivative
# "A" if result can be considered optimal

#This check below actually is not needed, since I only
#call this grading only for passed integrals. i.e. I check
#for "F" before calling this. But no harm of keeping it here.
#just in case.

if not type(result,freeof('int')) then
    return "F";
end if;

if ExpnType_result<=ExpnType_optimal then
    if debug then
        print("ExpnType_result<=ExpnType_optimal");
    fi;

```

```

if is_contains_complex(result) then
  if is_contains_complex(optimal) then
    if debug then
      print("both result and optimal complex");
    fi;
    #both result and optimal complex
    if leaf_count_result<=2*leaf_count_optimal then
      return "A";
    else
      return "B";
    end if
  else #result contains complex but optimal is not
    if debug then
      print("result contains complex but optimal is not");
    fi;
    return "C";
  end if
else # result do not contain complex
  # this assumes optimal do not as well
  if debug then
    print("result do not contain complex, this assumes optimal do not
as well");
  fi;
  if leaf_count_result<=2*leaf_count_optimal then
    if debug then
      print("leaf_count_result<=2*leaf_count_optimal");
    fi;
    return "A";
  else
    if debug then
      print("leaf_count_result>2*leaf_count_optimal");
    fi;
    return "B";
  end if
end if
else #ExpnType(result) > ExpnType(optimal)
  if debug then
    print("ExpnType(result) > ExpnType(optimal)");
  fi;
  return "C";
end if

end proc:

#
# is_contains_complex(result)
# takes expressions and returns true if it contains "I" else false

```

```

#
#Nasser 032417
is_contains_complex:= proc(expression)
  return (has(expression,I));
end proc:

# The following summarizes the type number assigned an expression
# based on the functions it involves
# 1 = rational function
# 2 = algebraic function
# 3 = elementary function
# 4 = special function
# 5 = hyperpergeometric function
# 6 = appell function
# 7 = rootsum function
# 8 = integrate function
# 9 = unknown function

ExpnType := proc(expn)
  if type(expn,'atomic') then
    1
  elif type(expn,'list') then
    apply(max,map(ExpnType,expn))
  elif type(expn,'sqrt') then
    if type(op(1,expn),'rational') then
      1
    else
      max(2,ExpnType(op(1,expn)))
    end if
  elif type(expn,'^^') then
    if type(op(2,expn),'integer') then
      ExpnType(op(1,expn))
    elif type(op(2,expn),'rational') then
      if type(op(1,expn),'rational') then
        1
      else
        max(2,ExpnType(op(1,expn)))
      end if
    else
      max(3,ExpnType(op(1,expn)),ExpnType(op(2,expn)))
    end if
  elif type(expn,'`+`') or type(expn,'`*`') then
    max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
  elif ElementaryFunctionQ(op(0,expn)) then
    max(3,ExpnType(op(1,expn)))
  elif SpecialFunctionQ(op(0,expn)) then
    max(4,apply(max,map(ExpnType,[op(expn)])))
  end if
end proc:

```



```

elif HypergeometricFunctionQ(op(0,expn)) then
  max(5,apply(max,map(ExpnType,[op(expn)])))
elif AppellFunctionQ(op(0,expn)) then
  max(6,apply(max,map(ExpnType,[op(expn)])))
elif op(0,expn)='int' then
  max(8,apply(max,map(ExpnType,[op(expn)]))) else
9
end if
end proc:

ElementaryFunctionQ := proc(func)
  member(func,[
    exp,log,ln,
    sin,cos,tan,cot,sec,csc,
    arcsin,arccos,arctan,arccot,arcsec,arccsc,
    sinh,cosh,tanh,coth,sech,csch,
    arcsinh,arccosh,arctanh,arccoth,arcsech,arccsch])
end proc:

SpecialFunctionQ := proc(func)
  member(func,[
    erf,erfc,erfi,
    FresnelS,FresnelC,
    Ei,Ei,Li,Si,Ci,Shi,Chi,
    GAMMA,lnGAMMA,Psi,Zeta,polylog,dilog,LambertW,
    EllipticF,EllipticE,EllipticPi])
end proc:

HypergeometricFunctionQ := proc(func)
  member(func,[Hypergeometric1F1,hypergeom,HypergeometricPFQ])
end proc:

AppellFunctionQ := proc(func)
  member(func,[AppellF1])
end proc:

# u is a sum or product. rest(u) returns all but the
# first term or factor of u.
rest := proc(u) local v;
  if nops(u)=2 then
    op(2,u)
  else
    apply(op(0,u),op(2..nops(u),u))
  end if
end proc:

```

```
#leafcount(u) returns the number of nodes in u.
#Nasser 3/23/17 Replaced by build-in leafCount from package in Maple
leafcount := proc(u)
    MmaTranslator[Mma][LeafCount](u);
end proc:
```

4.0.3 Sympy grading function

```
#Dec 24, 2019. Nasser M. Abbasi:
#           Port of original Maple grading function by
#           Albert Rich to use with Sympy/Python
#Dec 27, 2019 Nasser. Added `RootSum`. See problem 177, Timofeev file
#           added 'exp_polar'
from sympy import *

def leaf_count(expr):
    #sympy do not have leaf count function. This is approximation
    return round(1.7*count_ops(expr))

def is_sqrt(expr):
    if isinstance(expr,Pow):
        if expr.args[1] == Rational(1,2):
            return True
        else:
            return False
    else:
        return False

def is_elementary_function(func):
    return func in [exp,log,ln,sin,cos,tan,cot,sec,csc,
                    asin,acos,atan,acot,asec,acsc,sinh,cosh,tanh,coth,sech,csch,
                    asinh,acosh,atanh,acoth,asech,acsch
                    ]

def is_special_function(func):
    return func in [ erf,erfc,erfi,
                    fresnels,fresnelc,Ei,Ei,Li,Si,Ci,Shi,Chi,
                    gamma,loggamma,digamma,zeta,polylog,LambertW,
                    elliptic_f,elliptic_e,elliptic_pi,exp_polar
                    ]

def is_hypergeometric_function(func):
    return func in [hyper]

def is_appell_function(func):
    return func in [appellf1]
```

```

def is_atom(expn):
    try:
        if expn.isAtom or isinstance(expn,int) or isinstance(expn,float):
            return True
        else:
            return False

    except AttributeError as error:
        return False

def expnType(expn):
    debug=False
    if debug:
        print("expn=",expn,"type(expn)=",type(expn))

    if is_atom(expn):
        return 1
    elif isinstance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
            return 1
        else:
            return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
    elif isinstance(expn,Pow): #type(expn,'`^`')
        if isinstance(expn.args[1],Integer): #type(op(2,expn),'integer')
            return expnType(expn.args[0]) #ExpnType(op(1,expn))
        elif isinstance(expn.args[1],Rational): #type(op(2,expn),'rational')
            if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
                return 1
            else:
                return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)
    ))
    else:
        return max(3,expnType(expn.args[0]),expnType(expn.args[1])) #max(3,
    ExpnType(op(1,expn)),ExpnType(op(2,expn)))
    elif isinstance(expn,Add) or isinstance(expn,Mul): #type(expn,'`+`') or type
    (expn,'`*`')
        m1 = expnType(expn.args[0])
        m2 = expnType(list(expn.args[1:]))
        return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
    elif is_elementary_function(expn.func): #ElementaryFunctionQ(op(0,expn))
        return max(3,expnType(expn.args[0])) #max(3,ExpnType(op(1,expn)))
    elif is_special_function(expn.func): #SpecialFunctionQ(op(0,expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(4,m1) #max(4,apply(max,map(ExpnType,[op(expn)])))

```

```

elif is_hypergeometric_function(expn.func): #HypergeometricFunctionQ(op(0,
expn))
    m1 = max(map(expnType, list(expn.args)))
    return max(5,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
elif is_appell_function(expn.func):
    m1 = max(map(expnType, list(expn.args)))
    return max(6,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
elif isinstance(expn,RootSum):
    m1 = max(map(expnType, list(expn.args))) #Apply[Max,Append[Map[ExpnType,
Apply[List,expn]],7]],
    return max(7,m1)
elif str(expn).find("Integral") != -1:
    m1 = max(map(expnType, list(expn.args)))
    return max(8,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
else:
    return 9

#main function
def grade_antiderivative(result,optimal):

    leaf_count_result = leaf_count(result)
    leaf_count_optimal = leaf_count(optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

    if str(result).find("Integral") != -1:
        return "F"

    if expnType_result <= expnType_optimal:
        if result.has(I):
            if optimal.has(I): #both result and optimal complex
                if leaf_count_result <= 2*leaf_count_optimal:
                    return "A"
                else:
                    return "B"
            else: #result contains complex but optimal is not
                return "C"
        else: # result do not contain complex, this assumes optimal do not as
well
            if leaf_count_result <= 2*leaf_count_optimal:
                return "A"
            else:
                return "B"
    else:
        return "C"

```

4.0.4 SageMath grading function

```

#Dec 24, 2019. Nasser: Ported original Maple grading function by
#           Albert Rich to use with Sagemath. This is used to
#           grade Fracas, Giac and Maxima results.
#Dec 24, 2019. Nasser: Added 'exp_integral_e' and 'sng', 'sin_integral'
#           'arctan2','floor','abs','log_integral'

from sage.all import *
from sage.symbolic.operators import add_vararg, mul_vararg

debug=False;

def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)

def is_sqrt(expr):
    if expr.operator() == operator.pow: #isinstance(expr,Pow):
        if expr.operands()[1]==1/2: #expr.args[1] == Rational(1,2):
            if debug: print ("expr is sqrt")
            return True
        else:
            return False
    else:
        return False

def is_elementary_function(func):
    debug=False
    m = func.name() in ['exp','log','ln',
        'sin','cos','tan','cot','sec','csc',
        'arcsin','arccos','arctan','arccot','arcsec','arccsc',
        'sinh','cosh','tanh','coth','sech','csch',
        'arcsinh','arccosh','arctanh','arccoth','arcsech','arccsch','sgn',
        'arctan2','floor','abs'
    ]
    if debug:
        if m:

```

```

        print ("func ", func , " is elementary_function")
    else:
        print ("func ", func , " is NOT elementary_function")

    return m

def is_special_function(func):
    debug=False
    if debug: print ("type(func)=", type(func))

    m= func.name() in ['erf','erfc','erfi','fresnel_sin','fresnel_cos','Ei',
        'Ei','Li','Si','sin_integral','Ci','cos_integral','Shi','
sinh_integral'
        'Chi','cosh_integral','gamma','log_gamma','psi,zeta',
        'polylog','lambert_w','elliptic_f','elliptic_e',
        'elliptic_pi','exp_integral_e','log_integral']

    if debug:
        print ("m=",m)
        if m:
            print ("func ", func ," is special_function")
        else:
            print ("func ", func ," is NOT special_function")

    return m

def is_hypergeometric_function(func):
    return func.name() in ['hypergeometric','hypergeometric_M','hypergeometric_U
']

def is_appell_function(func):
    return func.name() in ['hypergeometric']    #[appellf1] can't find this in
sagemath

def is_atom(expn):

    debug=False
    if debug: print ("Enter is_atom")

    #thanks to answer at https://ask.sagemath.org/question/49179/what-is-sagemath-equivalent-to-atomic-type-in-maple/
    try:
        if expn.parent() is SR:

```

```

        return expn.operator() is None
    if expn.parent() in (ZZ, QQ, AA, QQbar):
        return expn in expn.parent() # Should always return True
    if hasattr(expn.parent(), "base_ring") and hasattr(expn.parent(), "gens"):
        return expn in expn.parent().base_ring() or expn in expn.parent().
gens()
    return False

except AttributeError as error:
    return False

def expnType(expn):

    if debug:
        print(">>>>Enter expnType, expn=", expn)
        print(">>>>is_atom(expn)=", is_atom(expn))

    if is_atom(expn):
        return 1
    elif type(expn)==list: #instance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if type(expn.operands()[0])==Rational: #type(instance(expn.args[0],
Rational):
            return 1
        else:
            return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.
args[0]))
    elif expn.operator() == operator.pow: #instance(expn,Pow)
        if type(expn.operands()[1])==Integer: #instance(expn.args[1],Integer)
            return expnType(expn.operands()[0]) #expnType(expn.args[0])
        elif type(expn.operands()[1])==Rational: #instance(expn.args[1],
Rational)
            if type(expn.operands()[0])==Rational: #instance(expn.args[0],
Rational)
                return 1
            else:
                return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.
args[0]))
        else:
            return max(3,expnType(expn.operands()[0]),expnType(expn.operands()
[1])) #max(3,expnType(expn.operands()[0]),expnType(expn.operands()[1]))
    elif expn.operator() == add_vararg or expn.operator() == mul_vararg: #
instance(expn,Add) or instance(expn,Mul)
        m1 = expnType(expn.operands()[0]) #expnType(expn.args[0])
        m2 = expnType(expn.operands()[1:]) #expnType(list(expn.args[1:]))

```

```

    return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
elif is_elementary_function(expn.operator()): #is_elementary_function(expn.
func)
    return max(3,expnType(expn.operands()[0]))
elif is_special_function(expn.operator()): #is_special_function(expn.func)
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))
    return max(4,m1) #max(4,m1)
elif is_hypergeometric_function(expn.operator()): #
is_hypergeometric_function(expn.func)
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))
    return max(5,m1) #max(5,m1)
elif is_appell_function(expn.operator()):
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))
    return max(6,m1) #max(6,m1)
elif str(expn).find("Integral") != -1: #this will never happen, since it
#is checked before calling the grading function that is passed.
#but kept it here.
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))
    return max(8,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
else:
    return 9

```

```
#main function
```

```
def grade_antiderivative(result,optimal):
```

```

    if debug: print ("Enter grade_antiderivative for sagemath")

    leaf_count_result = tree_size(result) #leaf_count(result)
    leaf_count_optimal = tree_size(optimal) #leaf_count(optimal)

    if debug: print ("leaf_count_result=", leaf_count_result, "
leaf_count_optimal=",leaf_count_optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

    if debug: print ("expnType_result=", expnType_result, "expnType_optimal=",
expnType_optimal)

    if expnType_result <= expnType_optimal:
        if result.has(I):
            if optimal.has(I): #both result and optimal complex

```



```
        if leaf_count_result <= 2*leaf_count_optimal:
            return "A"
        else:
            return "B"
    else: #result contains complex but optimal is not
        return "C"
else: # result do not contain complex, this assumes optimal do not as
well
    if leaf_count_result <= 2*leaf_count_optimal:
        return "A"
    else:
        return "B"
else:
    return "C"
```